

Muon Energy Reconstruction in the ANTARES Detector



ERLANGEN CENTRE
FOR ASTROPARTICLE
PHYSICS

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Task and Tools

What there is

$$-dE/dx = a(E) + b(E)E$$

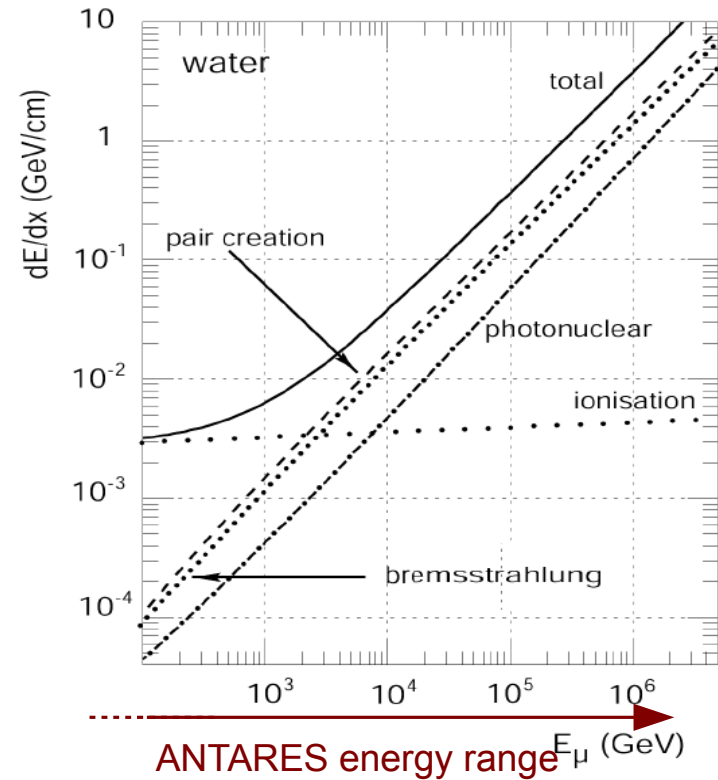
Muon energy loss

- is highly stochastic,
- consists of almost constant ionization loss $a(E)$
- and energy dependent radiative losses $b(E)E$, dominant above 1 TeV.

What we have

Muon energy is correlated to

- number of photons emitted per unit length,
- total charge measured by the detector,
- distribution of photons in the detector
- time residuals of photons



$$E(A, N, x, t)$$

The four ways towards energy



Challenge in ANTARES:

Hit selection is needed to suppress K40 and bioluminescence background (eg. using all hits within a certain distance and time residual relative to the track)

For ANTARES four different energy reconstruction methods exist, using various features of the muon energy loss processes, applying different statistical methods, reaching different levels of complexity.

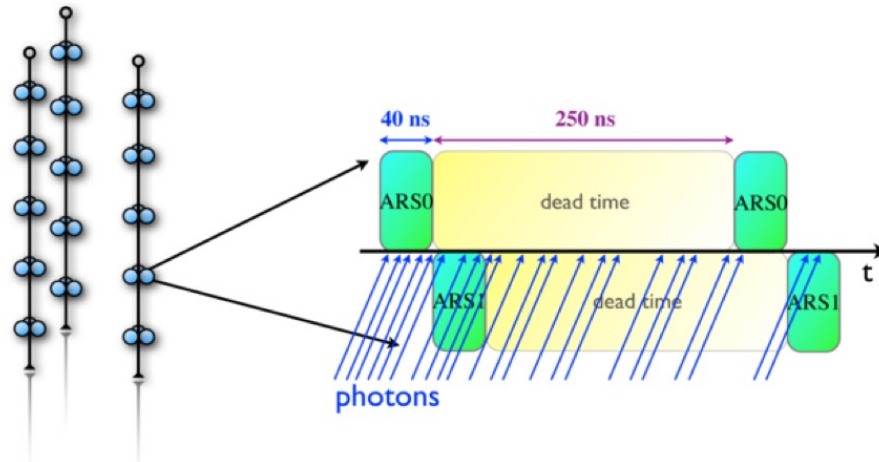
R-Estimator	dE/dx	ANN	Max. Likelihood
hit counting	parameter fitting charge estimate	PDF modelling machine based	analytical
N, t	A	A, N, x, t	A, N, x, t

Using Timing Information: the R-Estimator

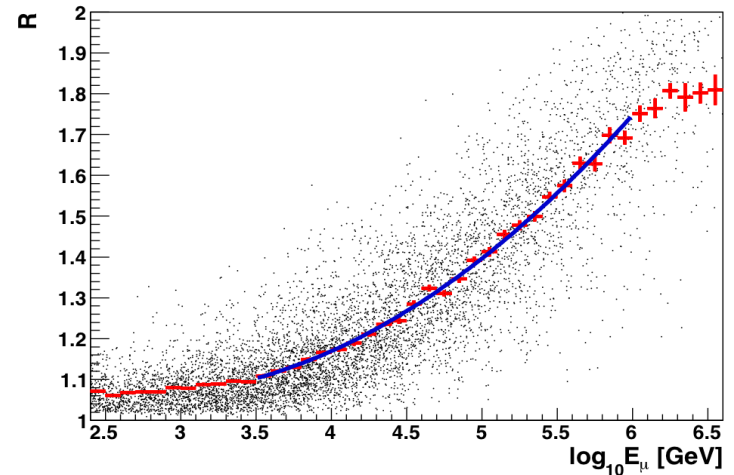
R = number of hit repetitions per OM

- within 100m from the track
- with time residuals < 500 ns

Parameter correlated to arrival time and
Number of hits,
used for polynomial fit on MC to find $E(R)$



$$E(A, N, x, t)$$



- specialized to $E > 10$ TeV
- used for Diffuse Flux analysis (Phys.Lett.B696:16-22,2011)

Using Charge Deposition: dE/dx estimator

Estimate energy loss from total charge A

$$E(A, N, x, t)$$

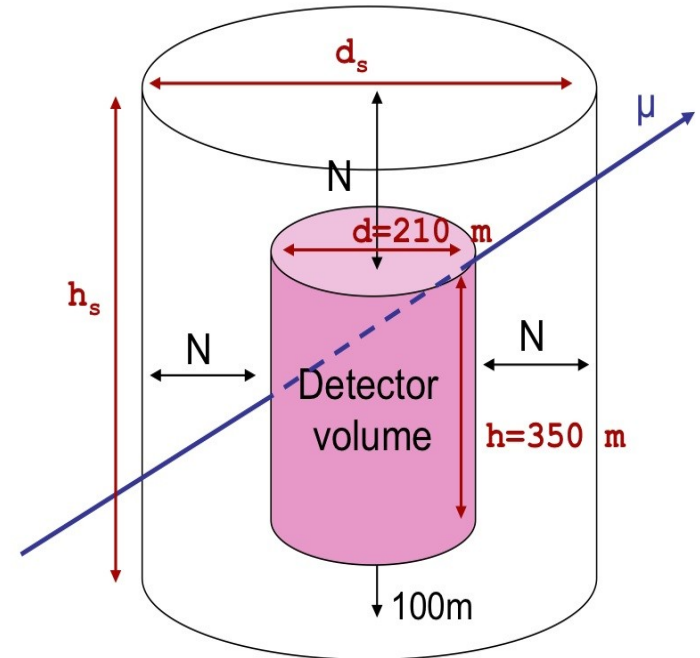
$$\left\langle \frac{dE}{dx} \right\rangle \approx \rho = \frac{1}{L_{Det}} \frac{\sum A}{p_{acc}}$$

Weighted by

L_{Det} track length in sensitive volume

p_{acc} total detector acceptance

$E(\rho)$ derived from fit on MC



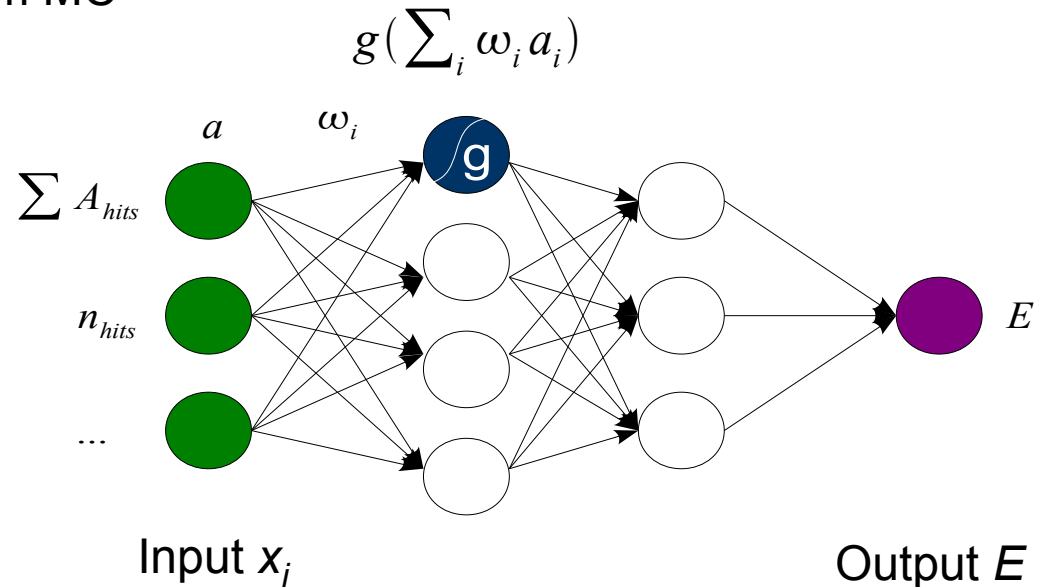
Use it all: Artificial Neural Nets (ANNs)

$$E(A, N, x, t)$$

PDF modelling by machine learning

- 56 parameters x_i describe location, charge and time of hits and track
- preprocessing performed to distinguish independent features
- training sets of (x_i, E) derived from MC

- Modelling of PDF by applying learning algorithm to ANN (adjusting connection weights for error minimization on training set)



Alternative: Maximum Likelihood method



Likelihood of energy from analytical PDF

$$E(A, N, x, t)$$

$$L_{Det}(E) = \prod_i^{N_{OM}} P_i(E)$$

For each hit OM, the probability of seeing a given amplitude is multiplied

$$P(A; \langle n \rangle) = \sum_{n=1}^{n_{max}} P_p(n; \langle n \rangle) P_g(A; n)$$

$P_p(n; \langle n \rangle)$ Poissonian probability to measure n photons if average is $\langle n \rangle$

$P_g(A; n)$ Gaussian probability of n photons to produce amplitude A

For each OM without hit, the probability to see nothing is used

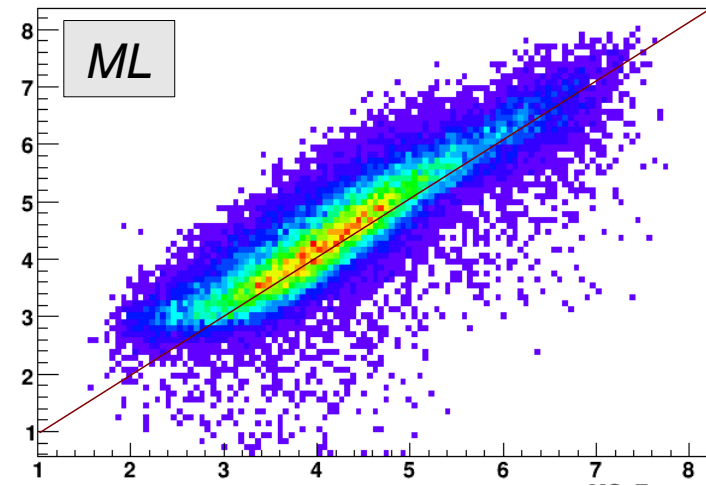
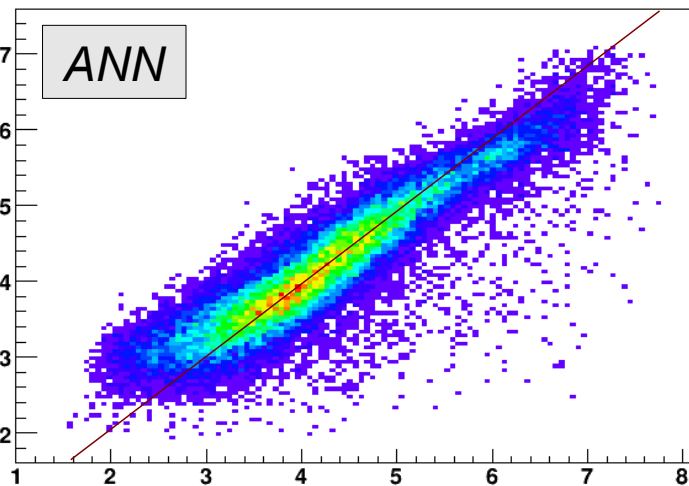
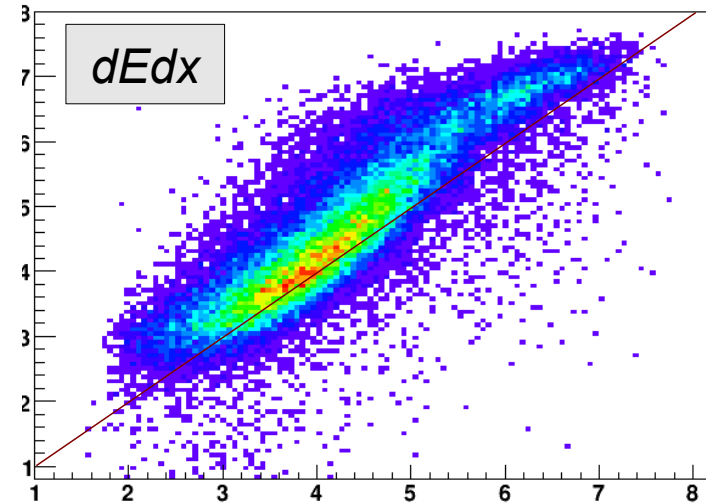
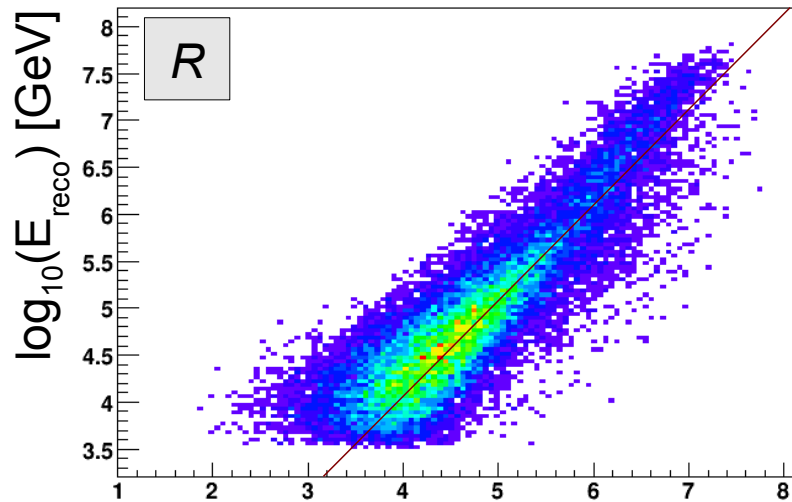
$$P(0, \langle n_{pe} \rangle) = e^{-\langle n \rangle} + P_{threshold}(\langle n \rangle)$$

$P_{threshold}(\langle n \rangle)$ Probability to have a photon below the PMT threshold

The energy is derived from minimizing $-\log(L_{Det}(E))$ using $\langle n \rangle(E)$ of the PDF.

Overall performance

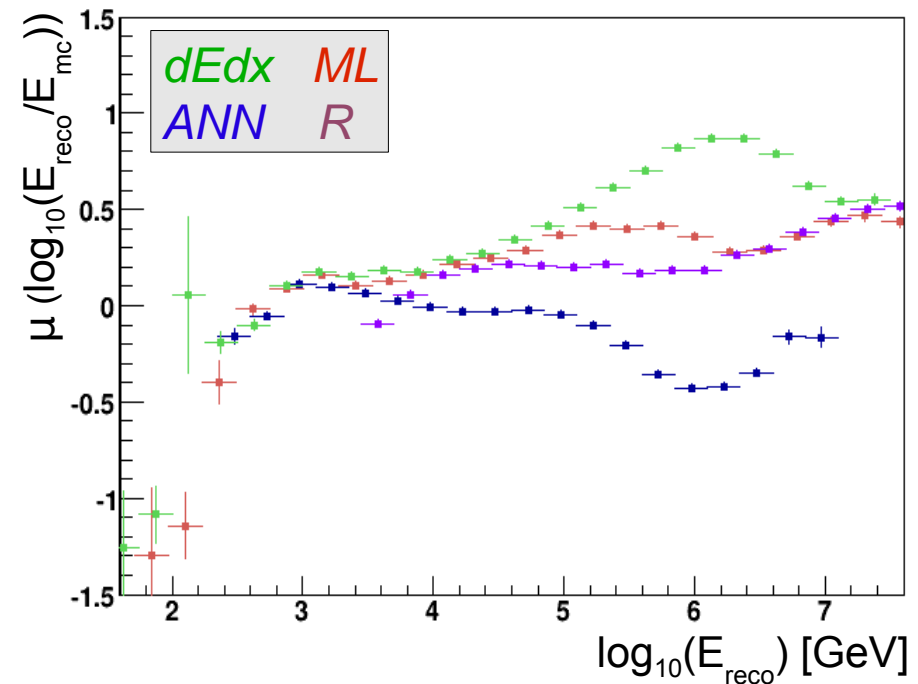
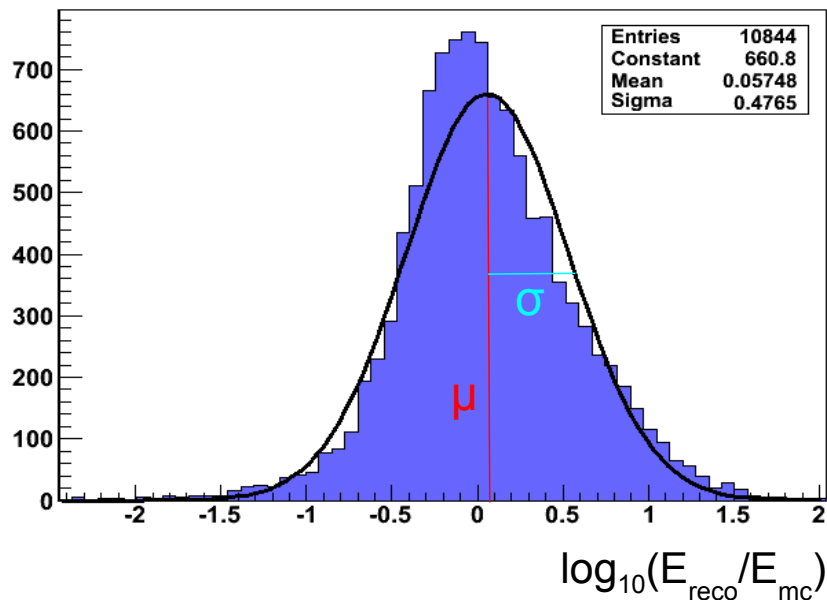
MC, upgoing neutrinos, Aafit track, $E^{-1.4}$



$\log_{10}(E_{\text{mc}})$ [GeV]

Quantifying reconstruction errors

If reconstruction yields E_{reco} , what do I know about the true energy?

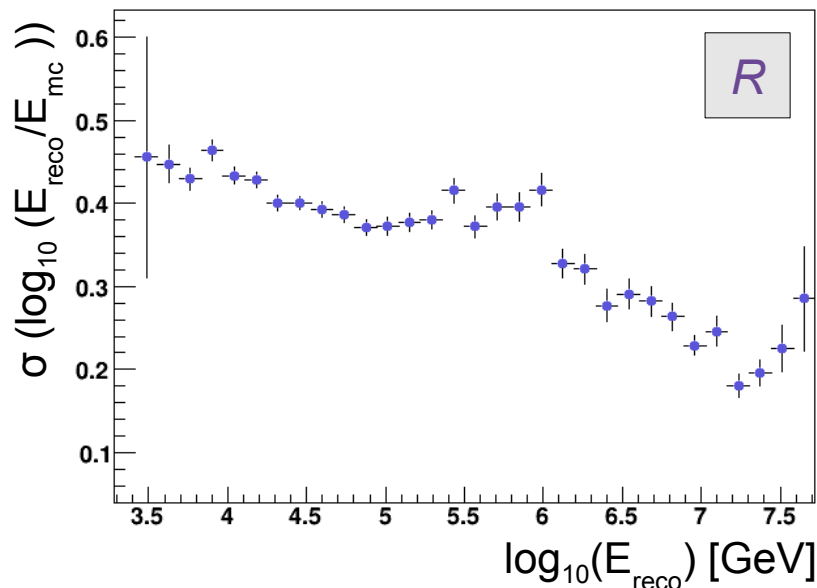


Resolution is measured by a Gaussian fit of $\log_{10}(E_{\text{reco}}) - \log_{10}(E_{\text{mc}})$ in bins over reconstructed or MC energy axis.

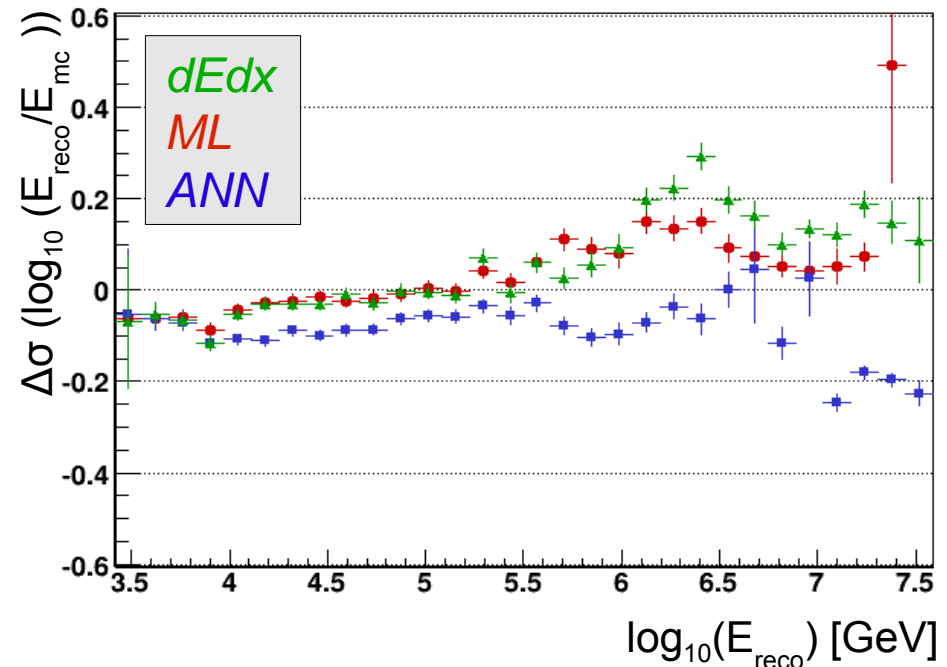
Performance on neutrino induced muons

R-Estimator has already been used for diffuse flux analysis

→ taken as reference for newer methods



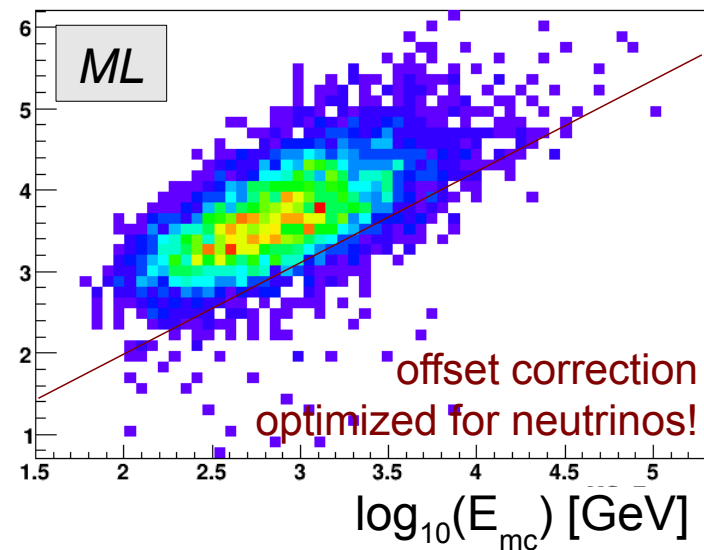
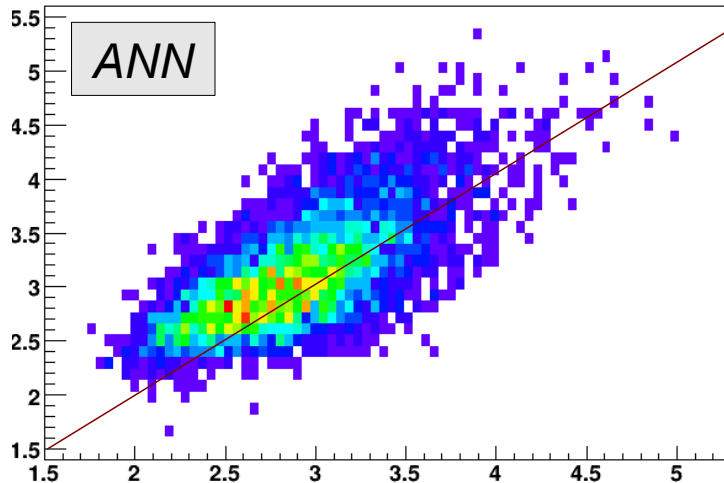
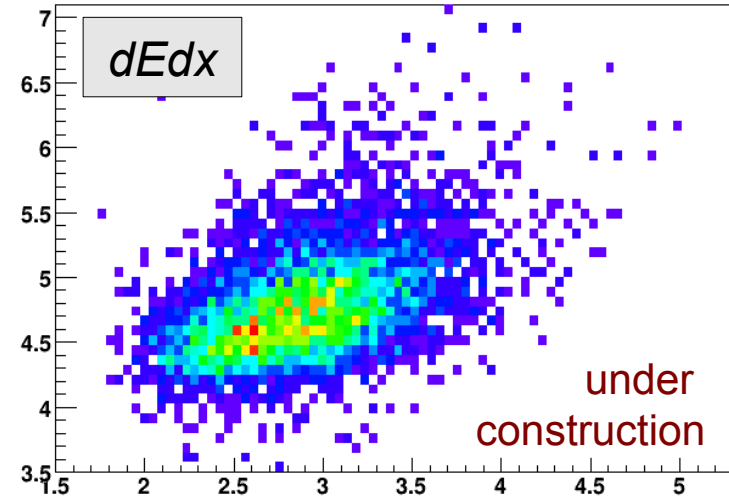
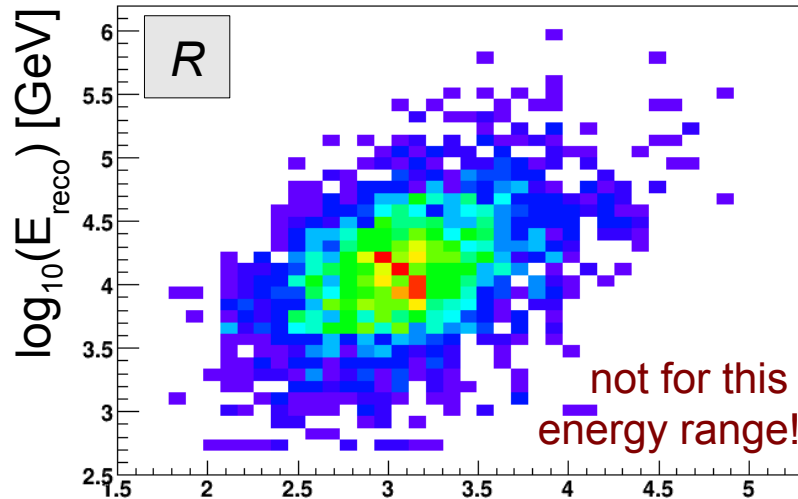
$$\Delta \sigma = \log_{10}(E_{\text{reco}}/E_{\text{MC}})_{\text{method}} - \log_{10}(E_{\text{reco}}/E_{\text{MC}})_R$$



Good resolution of factor 2 can be reached above 10 TeV

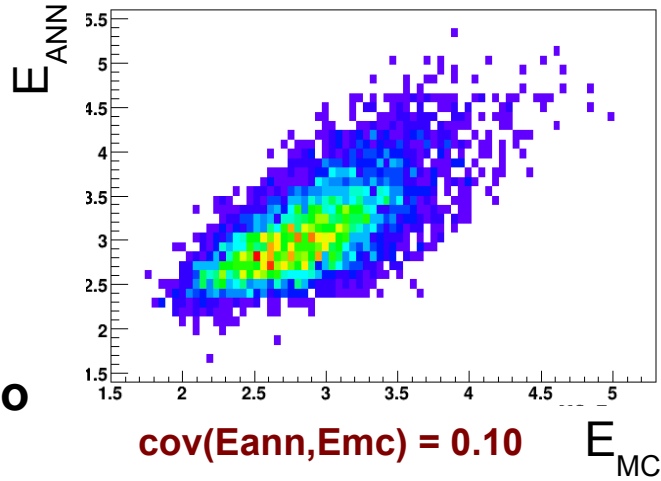
Applying estimators on atmospheric muon

MC, atmospheric muons, MC track

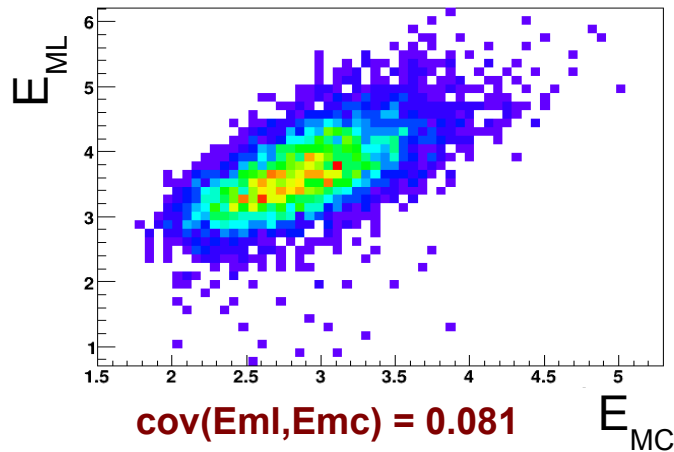


Correlation between reconstruction errors?

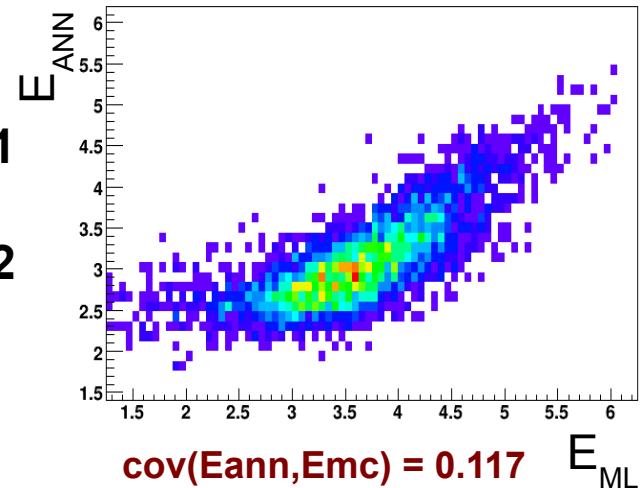
MC track



Ereco
vs
Etrue



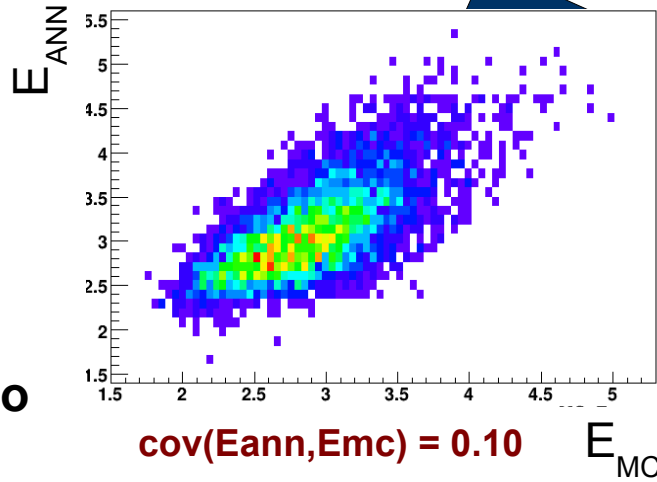
Reconstructed track



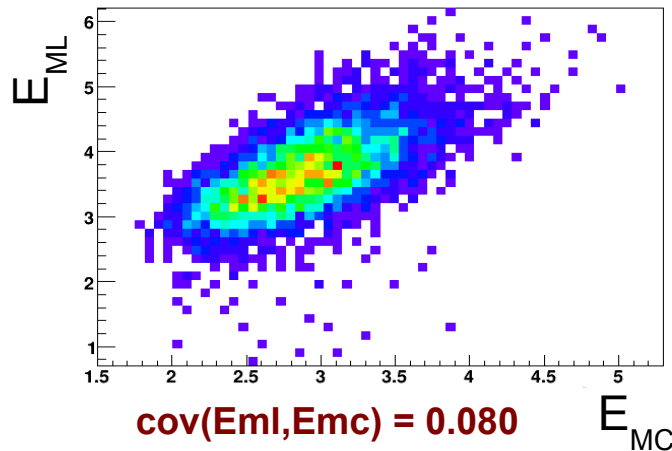
Ereco1
vs
Ereco2

Correlation between reconstruction errors?

MC track



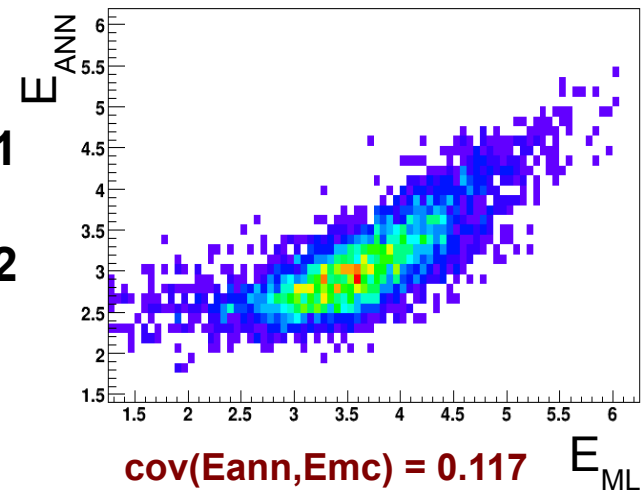
Ereco
vs
Etrue



Track reconstruction errors
similarly effect both
methods

Reconstructed track

Ereco1
vs
Ereco2

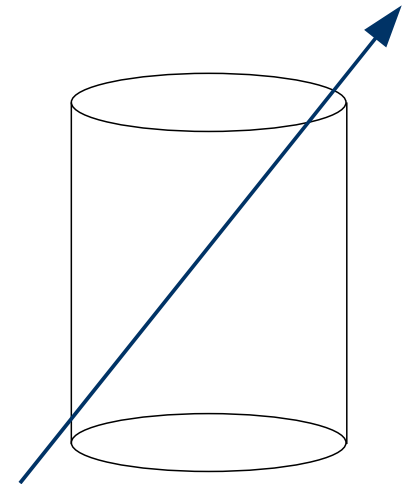
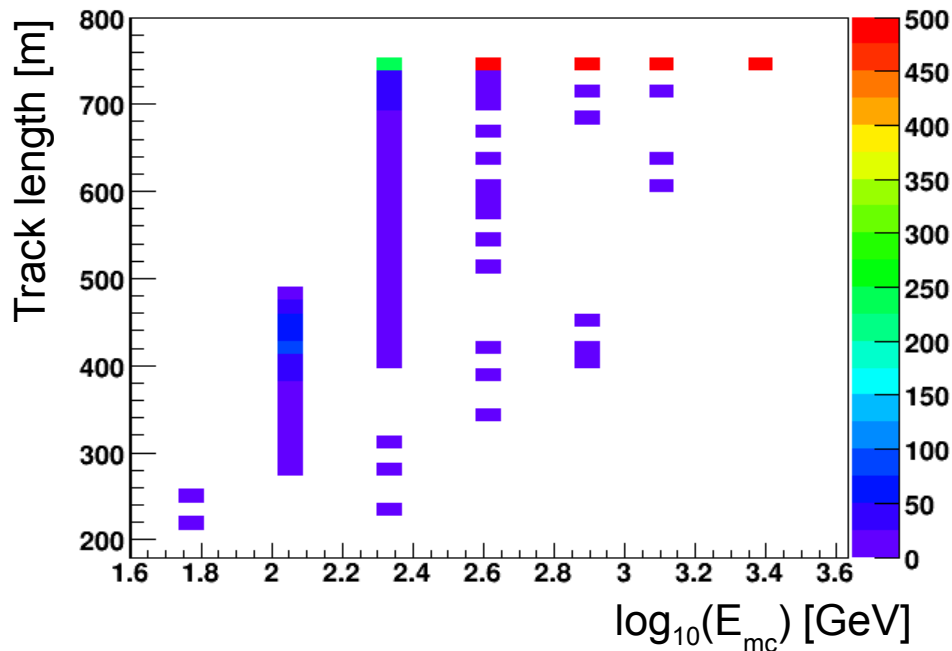


Some stochastic effect due to
energy loss characteristics?

Estimating effect of energy loss fluctuations

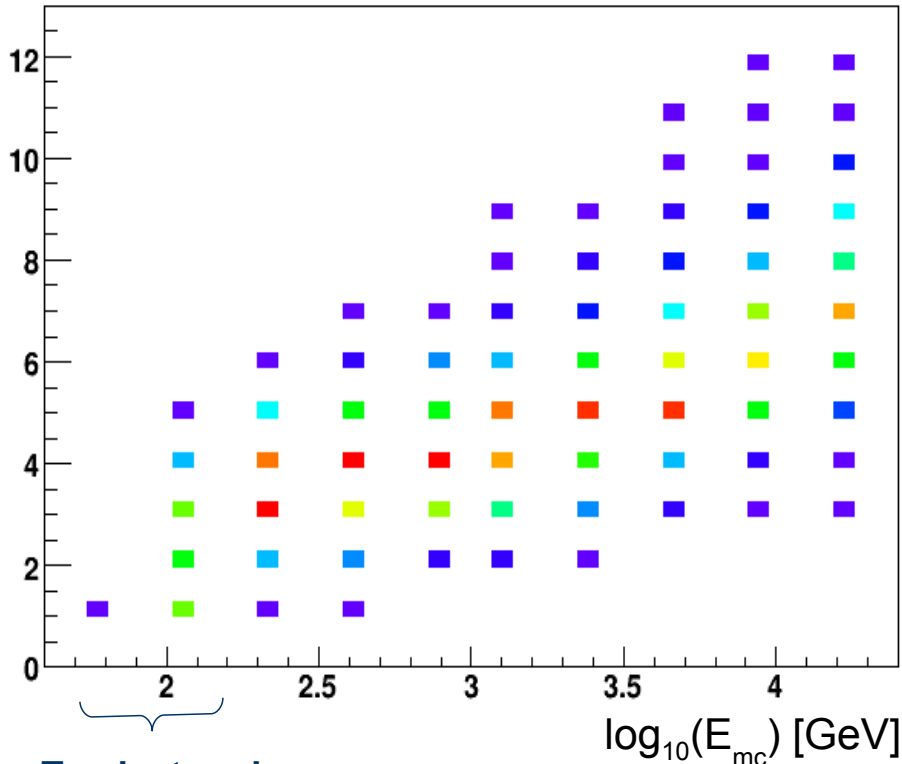
- Idea:**
- Simulate the same track with the same energy repeatedly
 - Scan detector using various tracks and different energies
 - (reconstruct events)

Example: Zenith = 130°, through detector center,
Energy = 63 GeV – 15 TeV (at simulation can),
500 repetitions



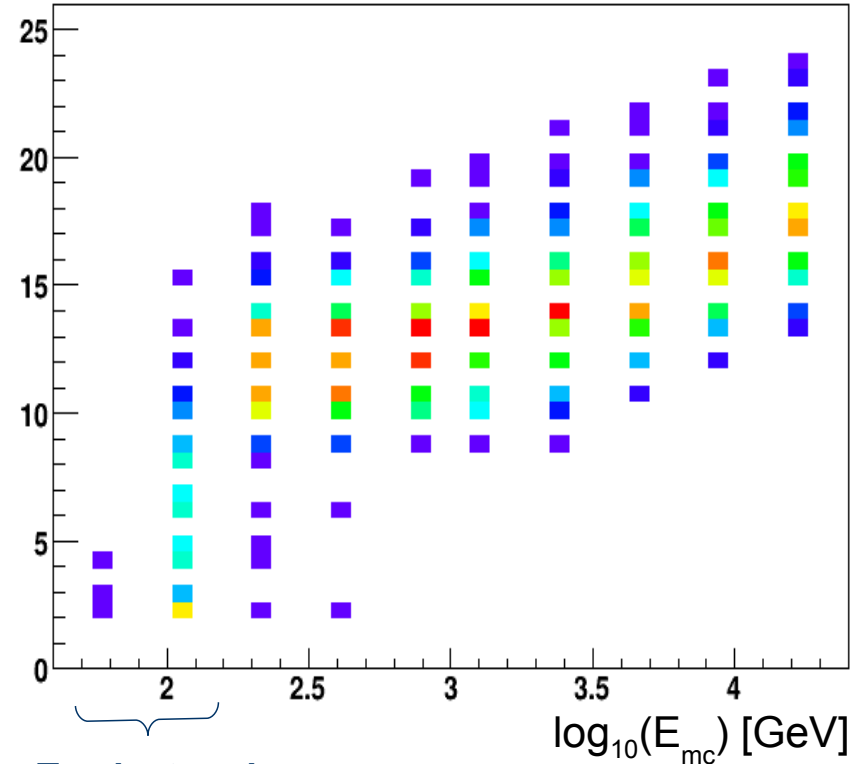
Detection units with photons from track

Number of lines with hits



Track stopping
in detector

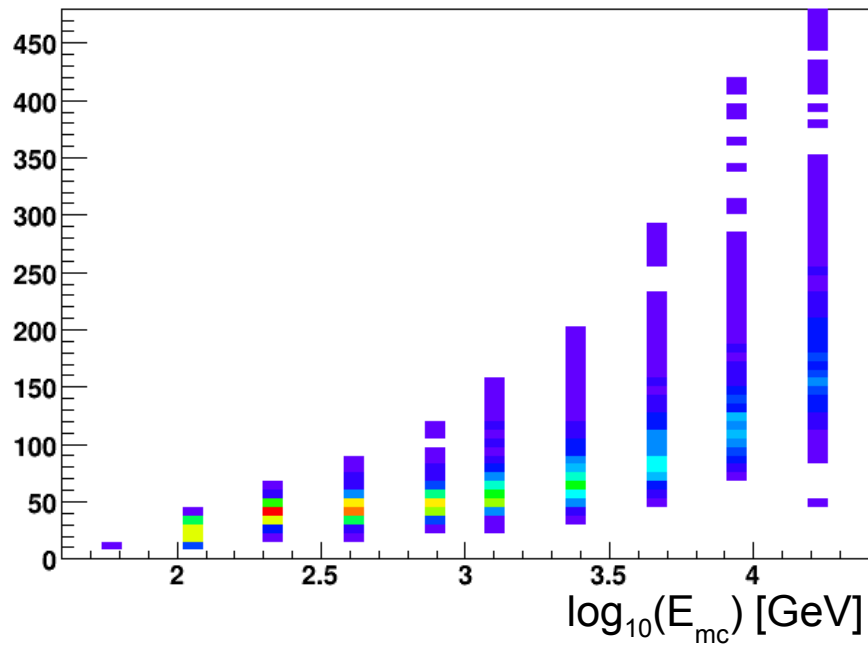
Number of storeys with hits



Track stopping
in detector

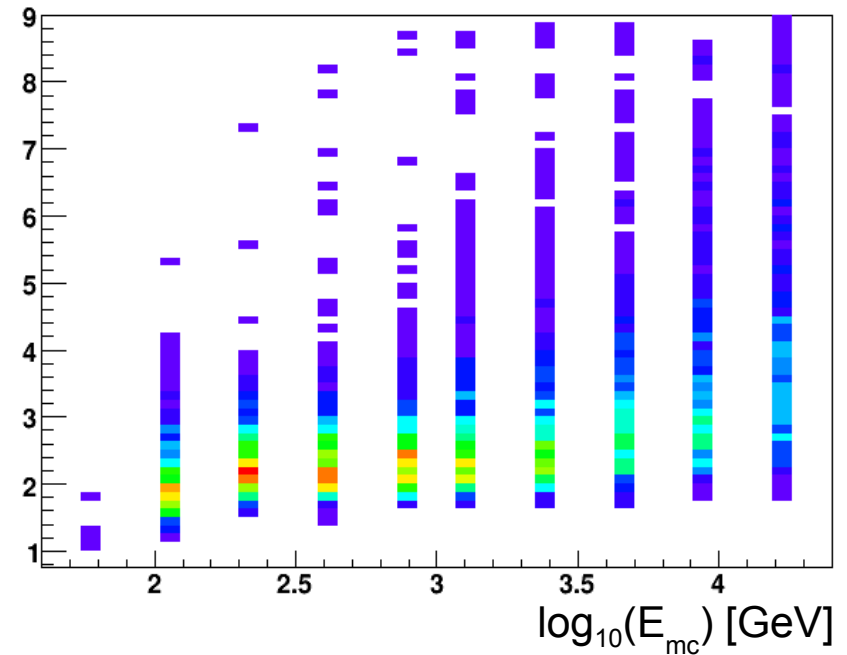
Charge deposition and hit numbers

Number of hits



Onset of photon production
through radiative processes

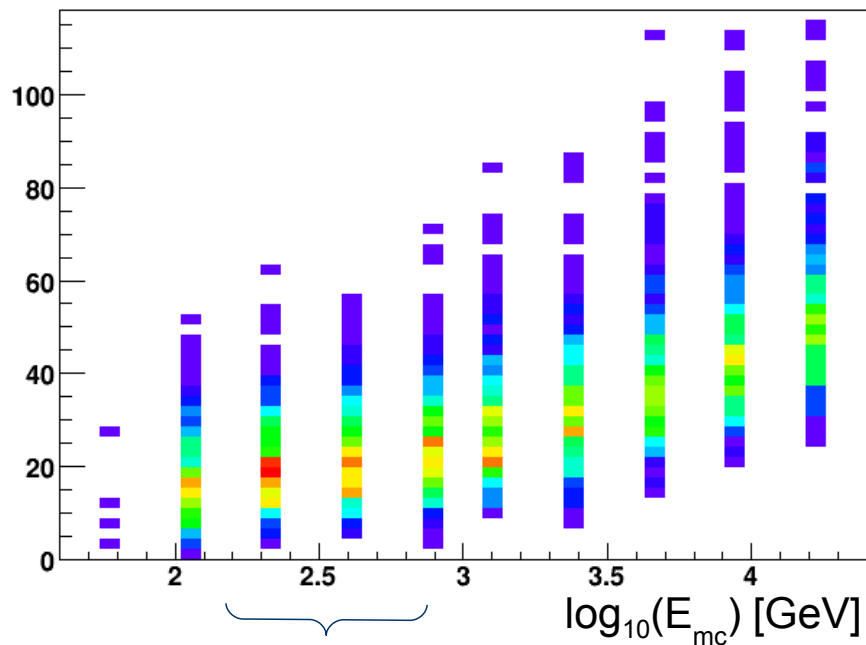
Average charge per hit (p.e.)



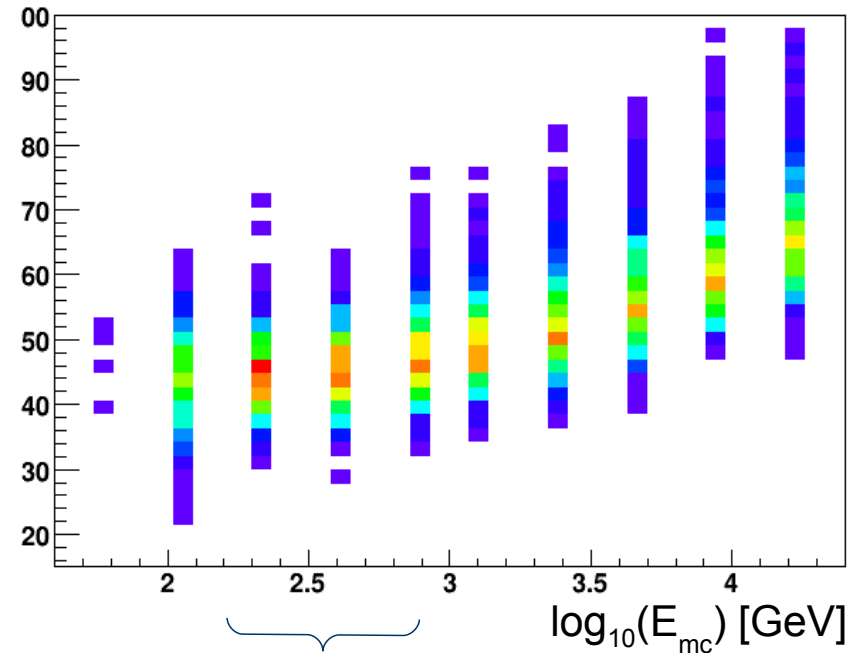
Onset of photon production
through radiative processes

Hit times and location

Average time residual* of hits



Average Cherekov distance* of hits



Track traversing whole detector, constant energy loss from ionization *Arrival time and distance of photon assuming emission from track under Cherenkov angle



Work in progress! Systematic studies can be used to understand the influence of stochastic energy loss on reconstruction.

Summary and Outlook



Four energy reconstruction methods are used at ANTARES and have been presented,

- Using both parameter fits and pdf-related estimates,
- Reaching a resolution between 0.25 – 0.4 in $\log_{10}(\Delta E)$ for upgoing muons above 10 TeV,
- Showing correlated reconstruction behavior which are partly due to energy loss characteristics.
- Systematic studies of energy loss characteristics can be used to understand and increase the estimator performance for the analysis of muon energies below 1 TeV.