

# Measurement of Charge Dependent Directed Flow at RHIC



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“西子”前沿核物理研讨会 2024

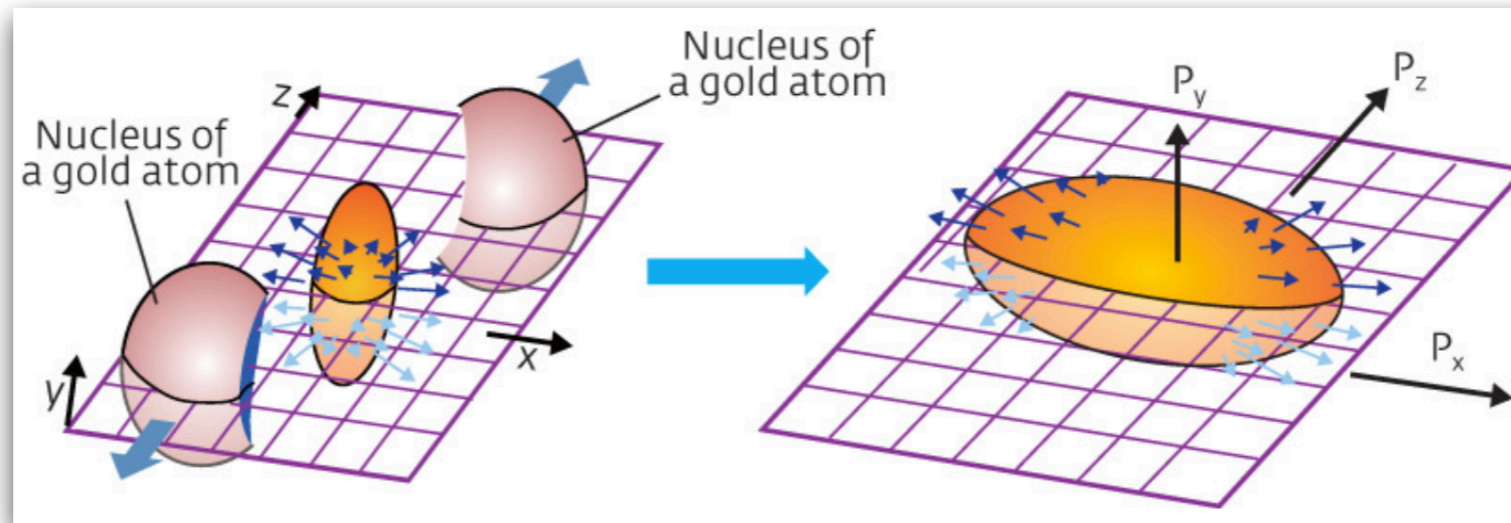
*October 18-20, Zhejiang University, Hangzhou*



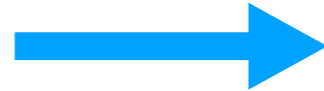
# Outline

- Motivation (directed flow)
- Electromagnetic field effects in HIC
- STAR detector and event plane reconstruction
- Results of charge dependent directed flow ( $\Delta v_1$ )
  - Quark coalescence hypothesis
  - $\Delta v_1$  in asymmetric collisions (Cu+Au)
  - $\Delta v_1$  for charm hadrons
  - $\Delta v_1$  for Light hadrons
- Summary and outlook

# Collective flow



**Co-ordinate space anisotropy**



**Momentum space anisotropy**

## Observables

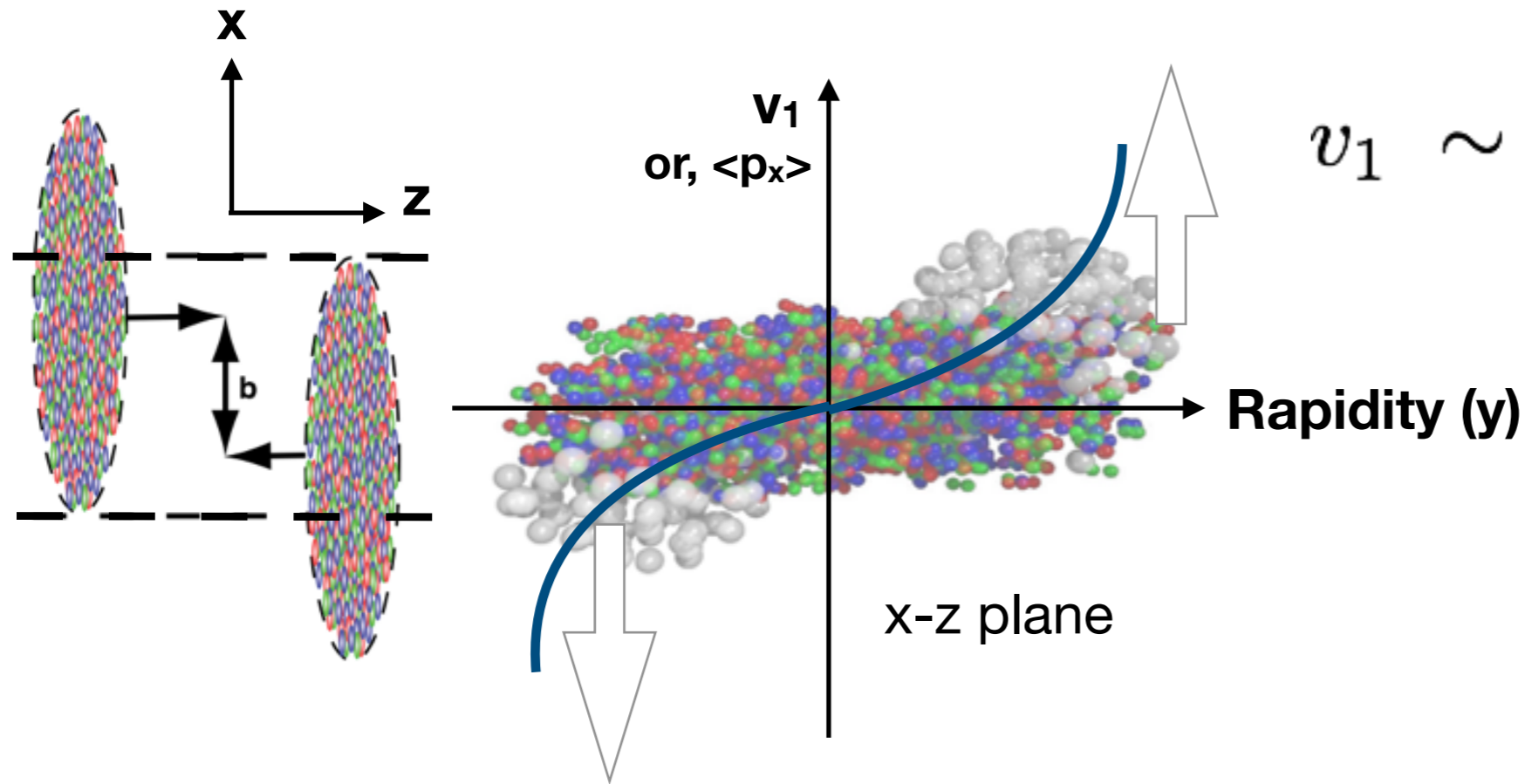
$$E \frac{d^3N}{dp^3} = \frac{1}{2\pi} \frac{d^2N}{p_T dp_T dy} \left( 1 + \sum 2v_n \cos n(\phi - \Psi_n^{EP}) \right)$$

- $v_1$  : Directed flow
- $v_2$  : Elliptic flow
- $v_3$  : Triangular flow

Flow coefficients are sensitive to:  
initial/final state properties of the medium, EoS and degrees of freedom

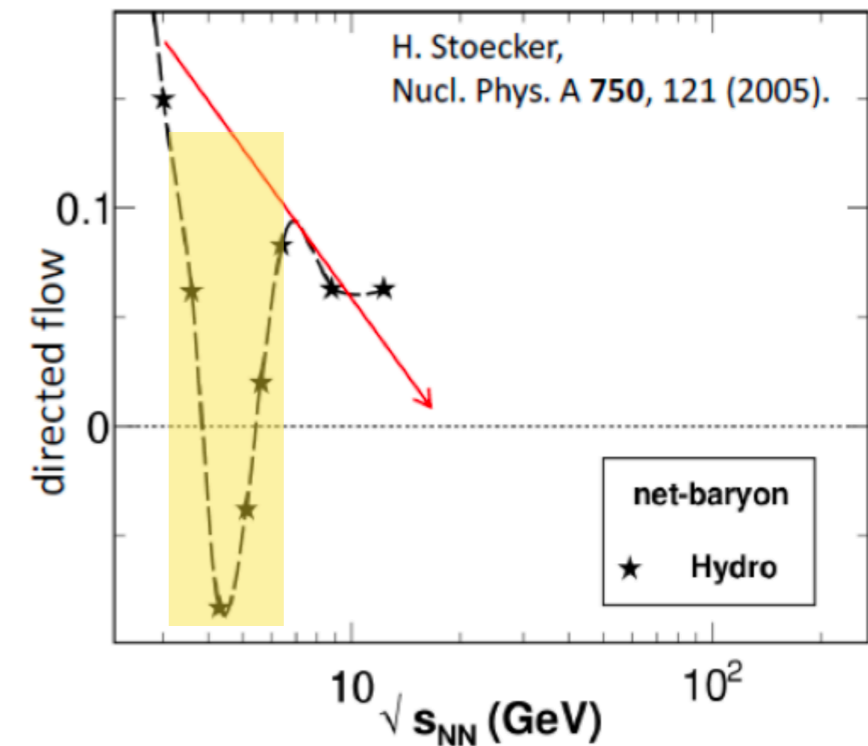


# Directed flow in heavy ion collisions



$$v_1 \sim \langle \cos(\phi - \Psi_R) \rangle$$

Hydro: Net-baryon  $v_1$



- Directed flow is the sideward collective motion of the produced particles within the reaction plane (x-z plane)
- Directed flow developed early in the collisions around time scale  $2R/\gamma \sim 0.1$  fm/c
- **Probe of early stage of collisions**
- Sensitive to the pressure
- Sensitive to the EoS

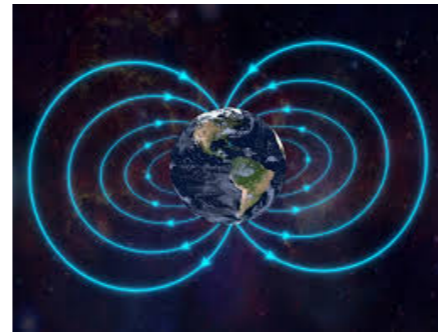
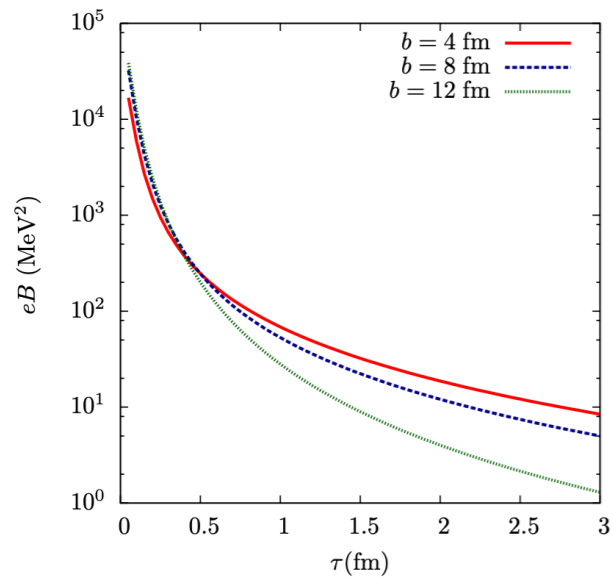
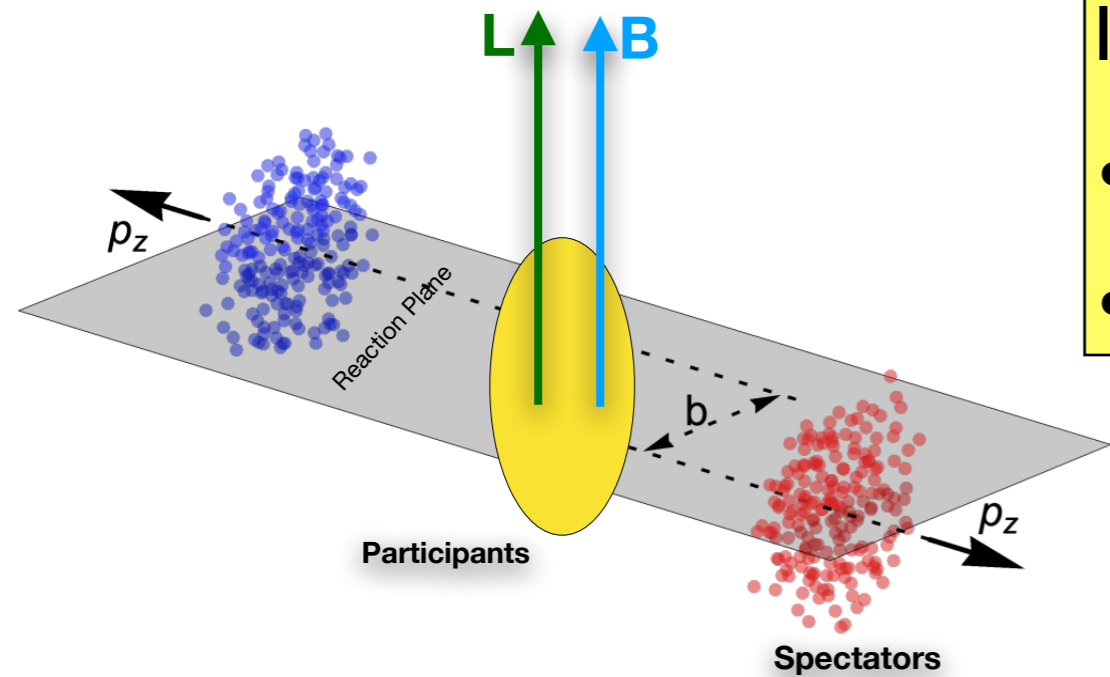
- EoS **without** 1st order PT  
**Monotonic** energy dependence
- EoS **with** 1st order PT  
**Non-Monotonic** energy dependence, dip in  $dv_1/dy$



# QCD matter under extreme conditions

In non-central heavy-ion collisions

- **Initial rapid rotation** ( $\omega \sim 10^{21} \text{ s}^{-1}$ )
- **Initial strong magnetic field** ( $B \sim 10^{18} \text{ Gauss}$ )



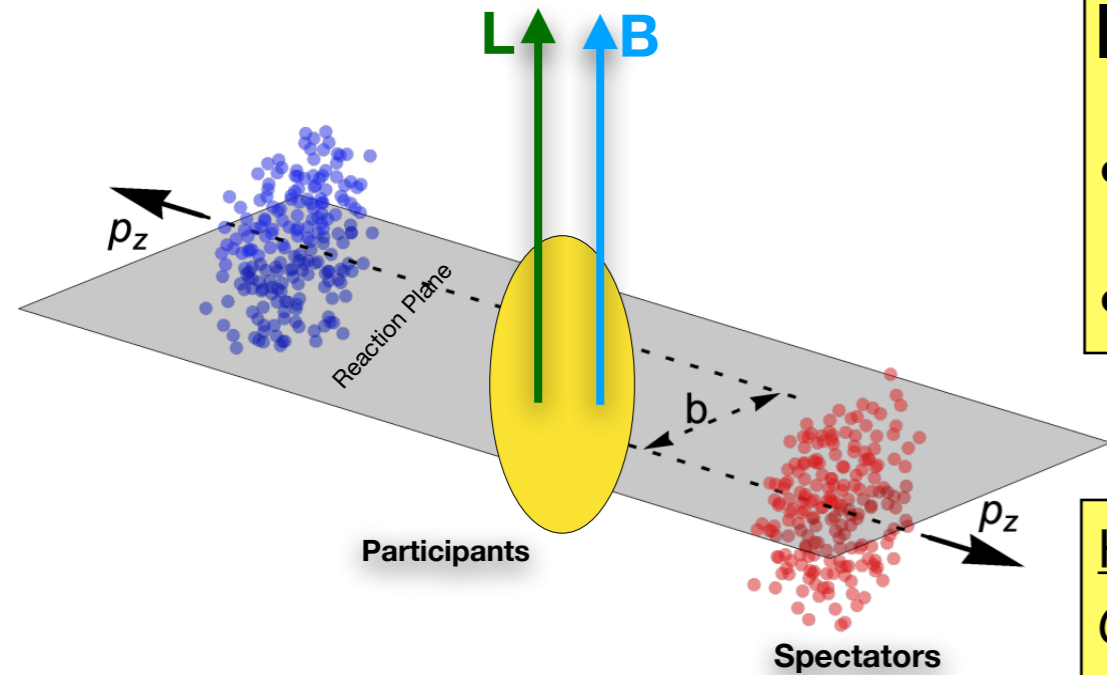
Earth's geomagnetic field  $\sim 0.5 \text{ G}$



Neutron star  $\sim 10^{14} \text{ G}$

- Ultra strong magnetic field can give rise wide range of exciting phenomena with applications in cosmology, neutron star and HIC

# QCD matter under extreme conditions



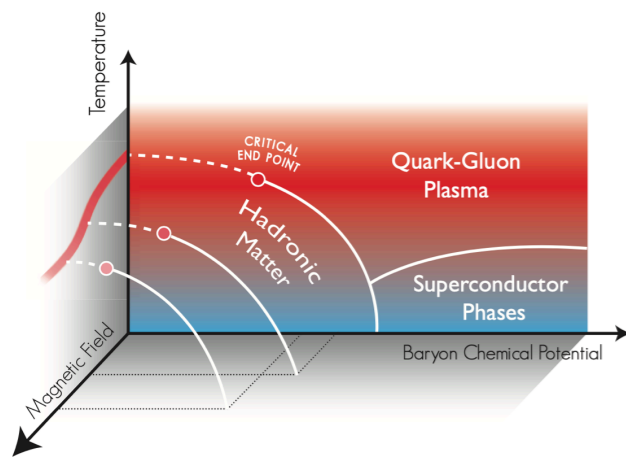
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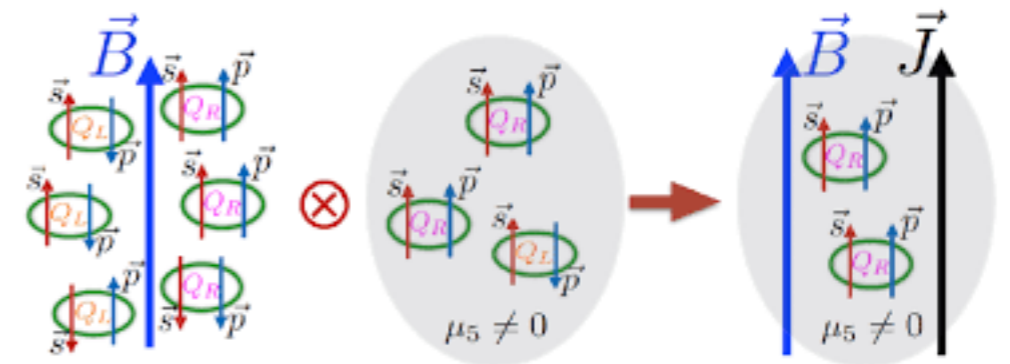
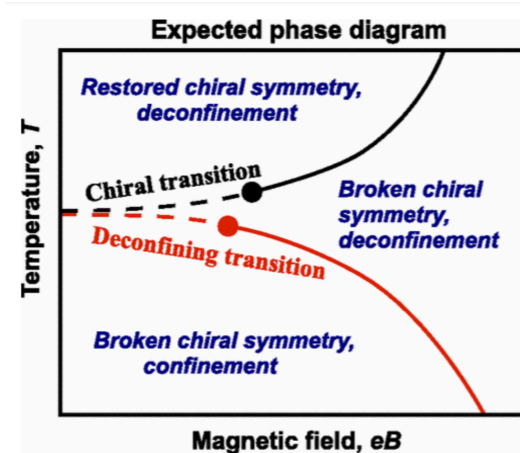
Heavy-ion collisions:

*Controlled experiment* to study QCD medium under rapid rotation and electro-magnetic field

*New frontier* research to understand the properties of QCD medium

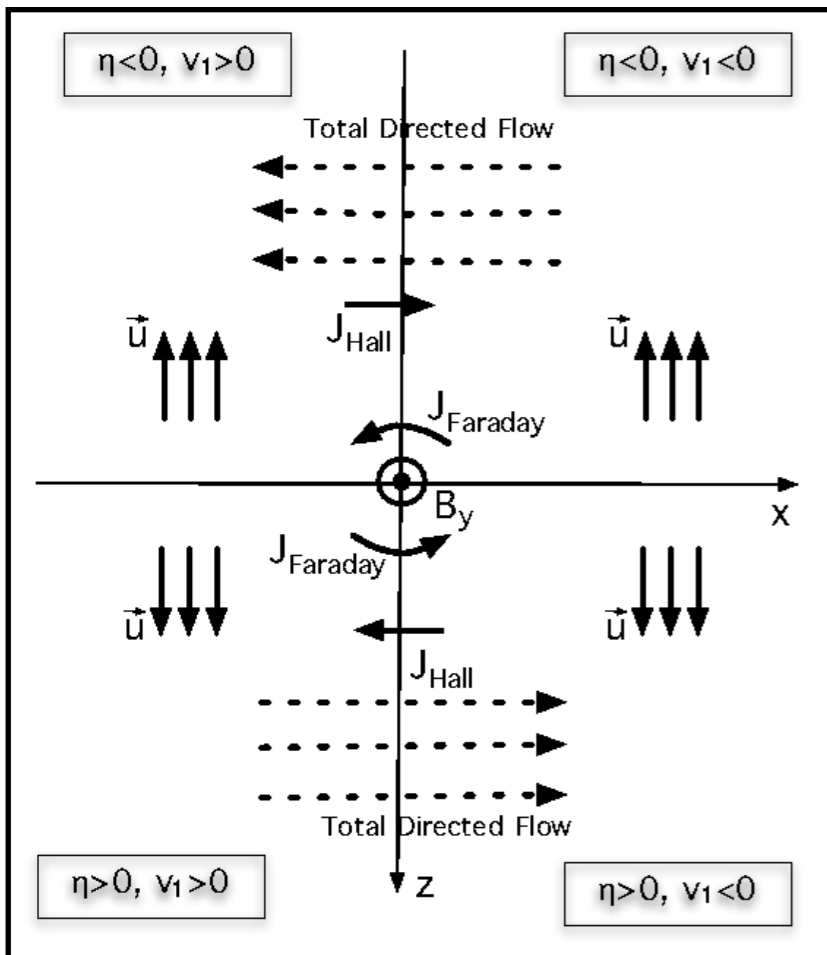


Impact on QCD phase transition, chiral symmetry restoration



Impact on QCD vacuum and its topology (Chiral Magnetic Effect)

# Electromagnetic effects in HIC



Gursoy et al, PRC 89, 054905 (2014)

## Observable

$$v_1 \sim \langle \cos(\phi - \Psi_R) \rangle$$

$$\Delta v_1 \sim v_1(h^+) - v_1(h^-)$$

(sensitive to EM effects)

- The moving spectators can produce enormously large **B** field ( $eB \sim 10^{18}$  G)
- There could be three competitive effects
- Hall effect:  $\mathbf{F} = q \mathbf{v} \times \mathbf{B}$   
Lorentz force exerts a sideways push on charged particles  
In opposite directions for opposite particles  
(along -ve X-direction in +ve rapidity and vice-versa)
- Faraday effect:  $\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$   
Time dependent **B** field generates a large **E** field  
Induced Faraday current will oppose the drift due to **B** field
- Coulomb effect:  
Coulomb field of the charged spectators

## • Imprints of EM field effects

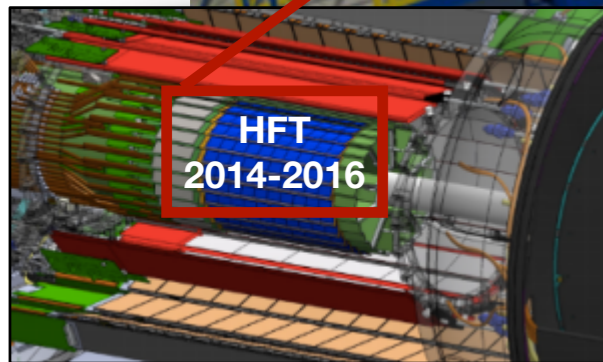
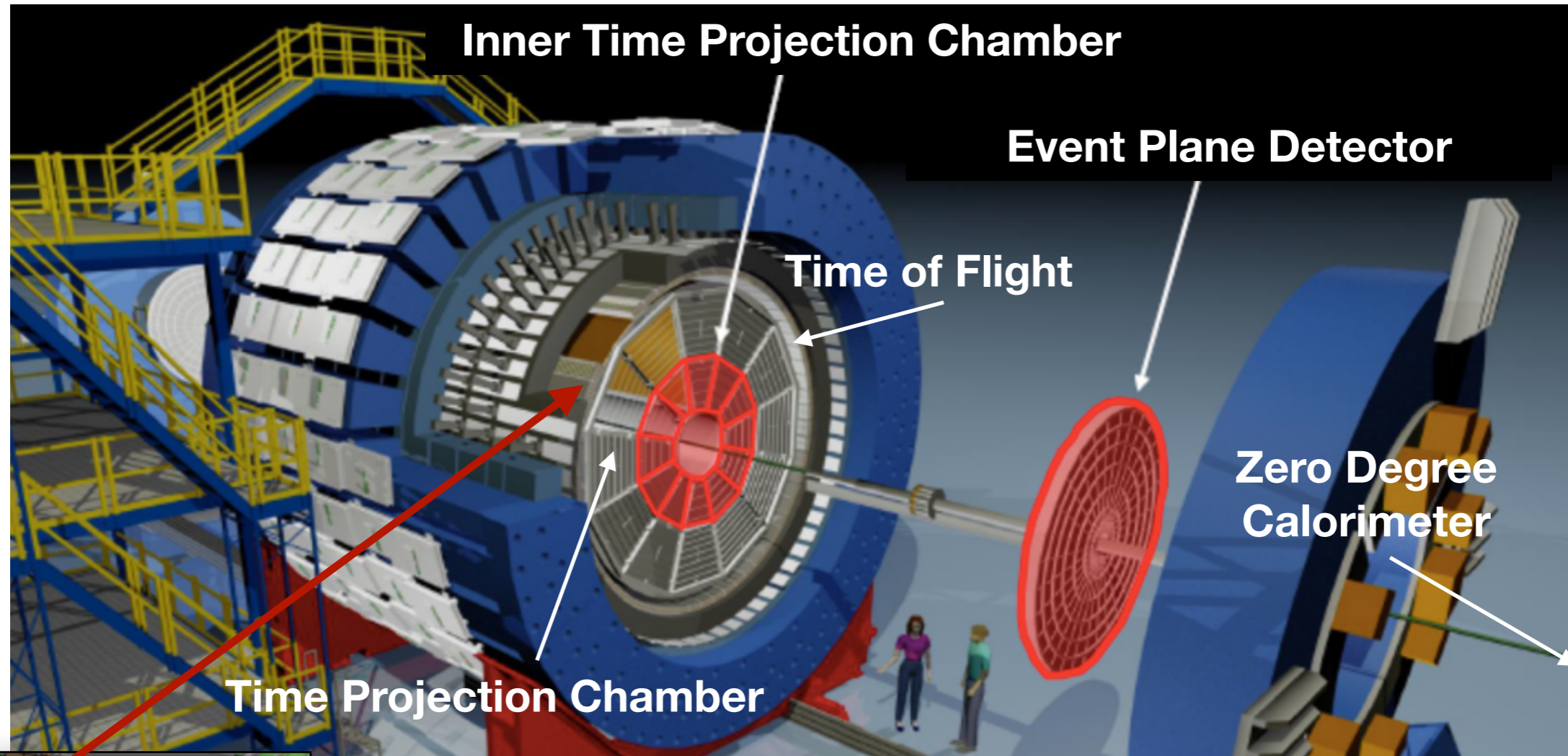
• Hall: positive  $\Delta v_1$

• Faraday: negative  $\Delta v_1$

• Coulomb: negative  $\Delta v_1$



# STAR detector



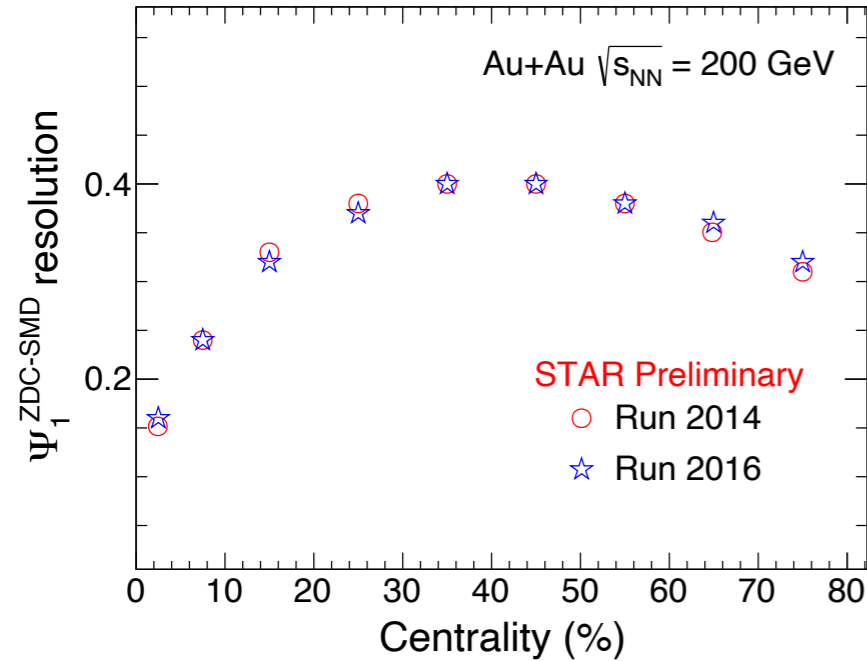
**Heavy Flavor Tracker  
(2014-2016)**

- Uniform acceptance, full azimuthal coverage, excellent PID capability
- TPC: tracking, centrality and event plane
- EPD, ZDC, BBC: event plane
- TPC+TOF: particle identification

# Event plane reconstruction

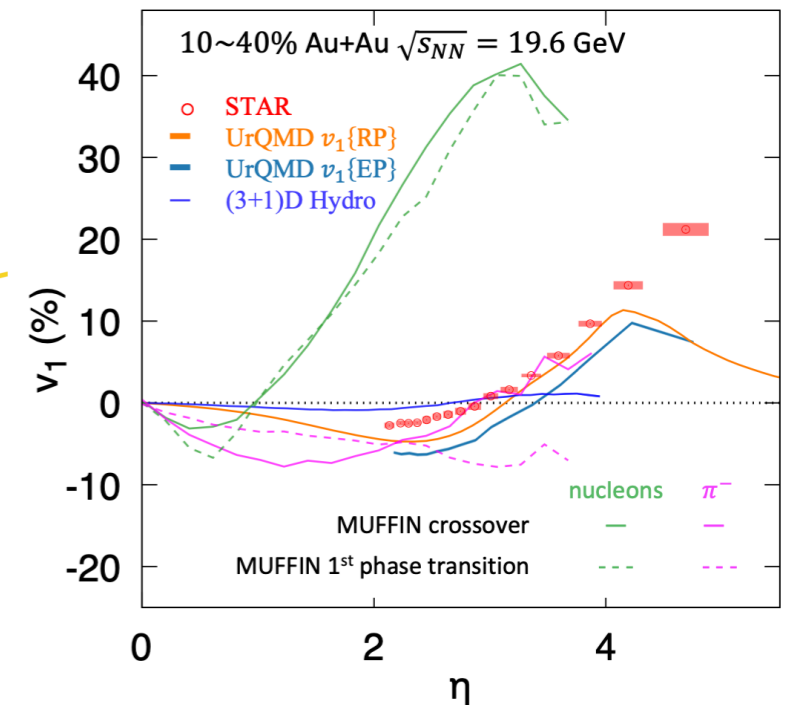
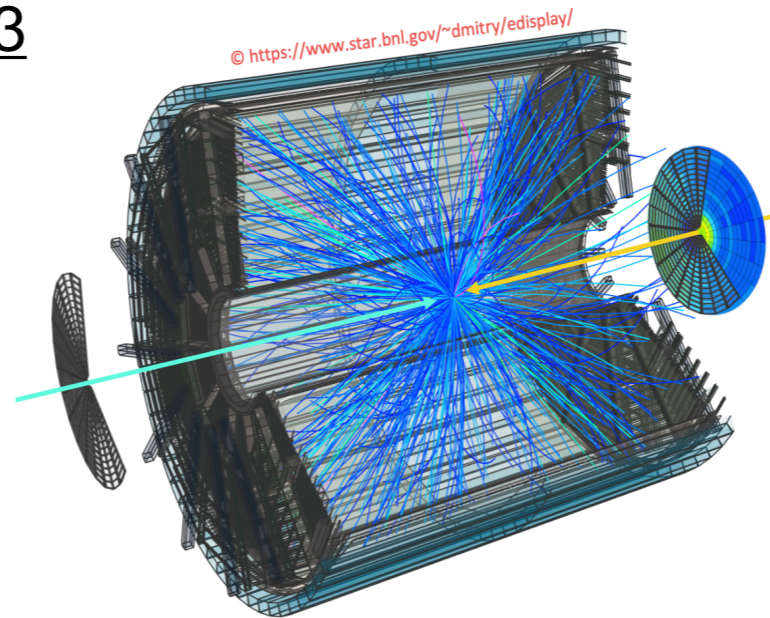
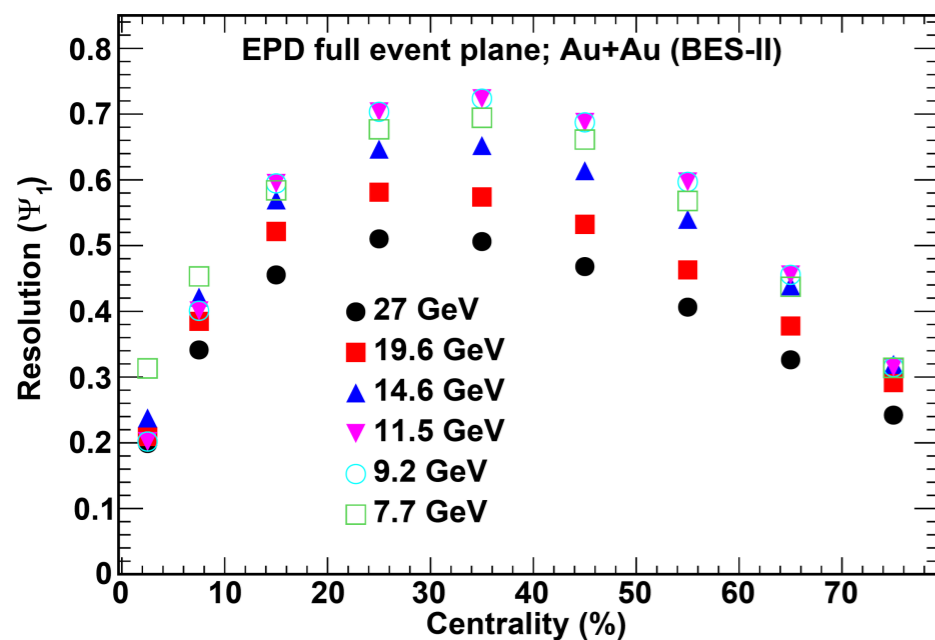
top-RHIC energy: ZDC-SMD  $|\eta| > 6.4$ :

$$v_1 \sim \frac{\langle \cos(\phi - \Psi_{EP}) \rangle}{EP - \text{resolution}}$$



- $v_1$  signal is significant at forward rapidity
- Better  $\psi_1$  resolution than mid-rapidity detectors
- Large  $\eta$ -gap significantly reduces non-flow contribution

BES-II (7.7 - 27 GeV): EPD  $2.1 < |\eta| < 5.3$



STAR: 2406.18213 (accepted in PRC)

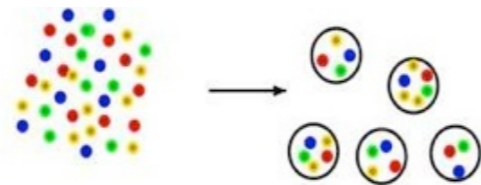
# Quark coalescence using directed flow

Test the assumption that the de-confined quarks acquired  $v_n$ , then they form hadrons:

$$v_n^{\text{hadron}} = \sum v_n^{\text{constituent-quarks}}$$

The origin of scaling is interpreted as an evidence for dominance of quark degrees of freedom

Particle	Quark content
anti- $\Lambda$	uds
anti-p	uud
K-	us



qq vs. qqq



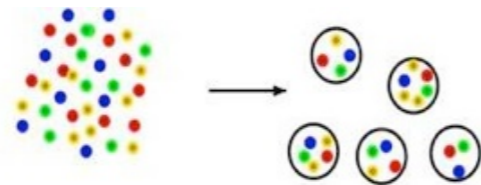
# Quark coalescence hypothesis

Test the assumption that the de-confined quarks acquired  $v_n$ , then they form hadrons:

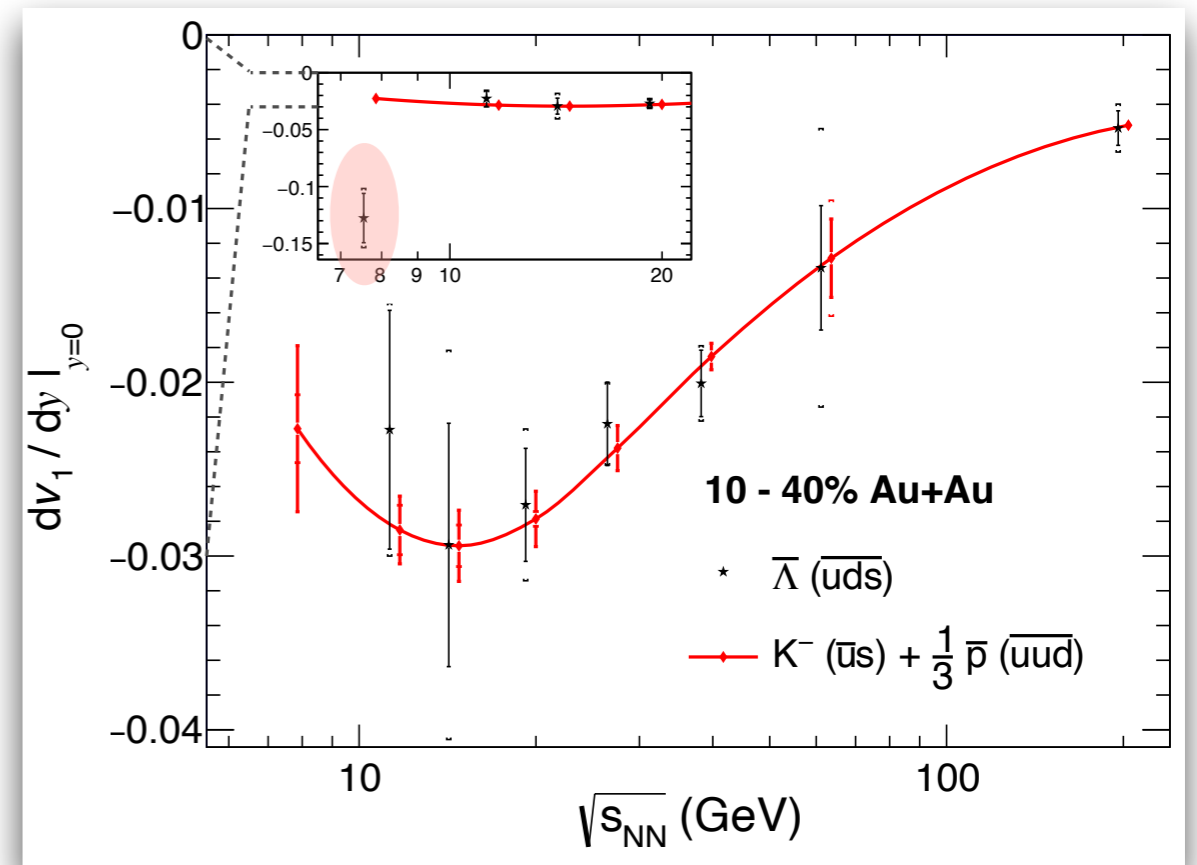
$$v_n^{\text{hadron}} = \sum v_n^{\text{constituent-quarks}}$$

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qq vs. qqq

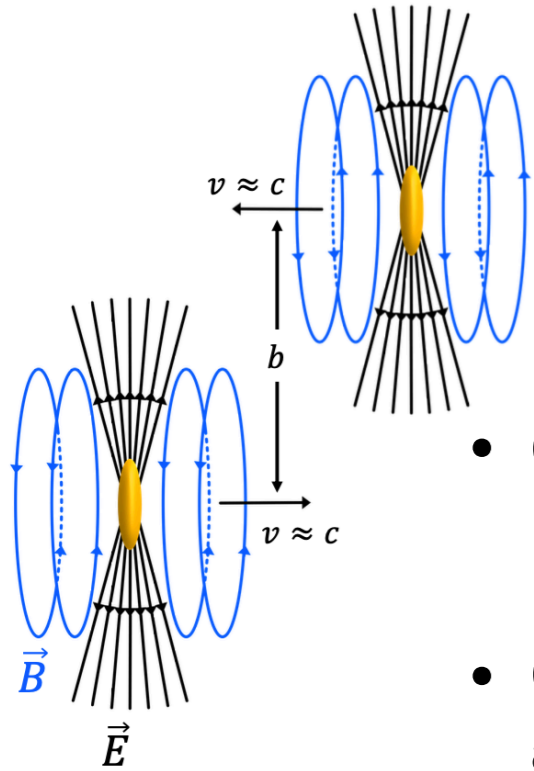


STAR: PRL 112, 162301 (2014)  
PRL 120, 062301 (2018)

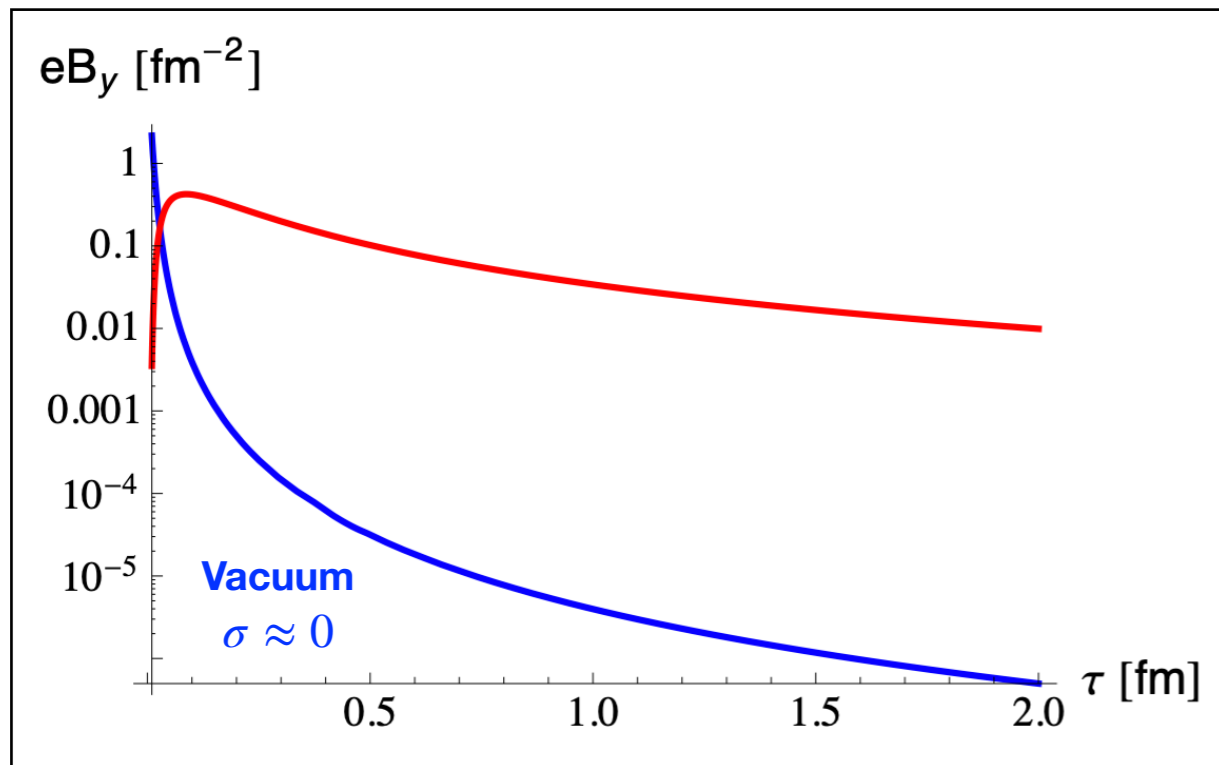
- Using anti-particles **quark coalescence sum rule**:
- Holds for  $\sqrt{s_{\text{NN}}} \geq 11.5$  GeV
- Breaks at  $\sqrt{s_{\text{NN}}} = 7.7$  GeV

- Quark coalescence hypothesis holds over a broad range of energies

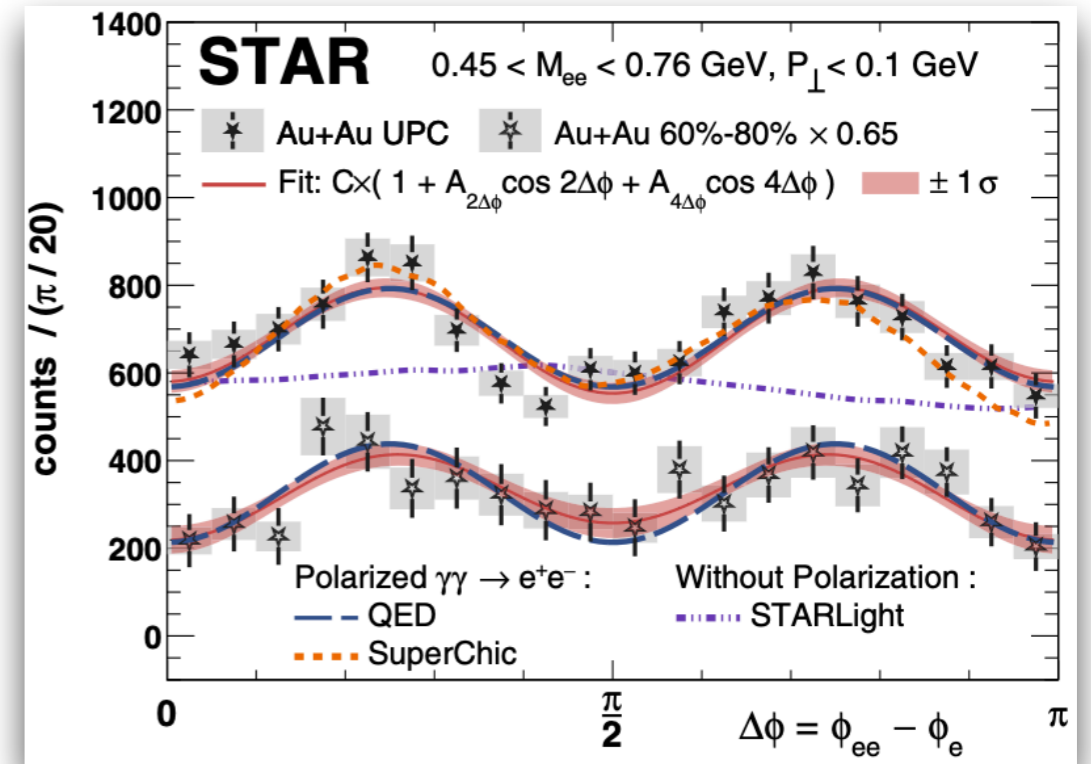
# Electromagnetic field in UPC



- Charged nuclei produce highly Lorentz contracted EM field
- Cross-sections for  $\gamma\gamma \rightarrow e^+e^-$  are related to EM field strength and configuration



## Ultra Peripheral Collisions (UPC)

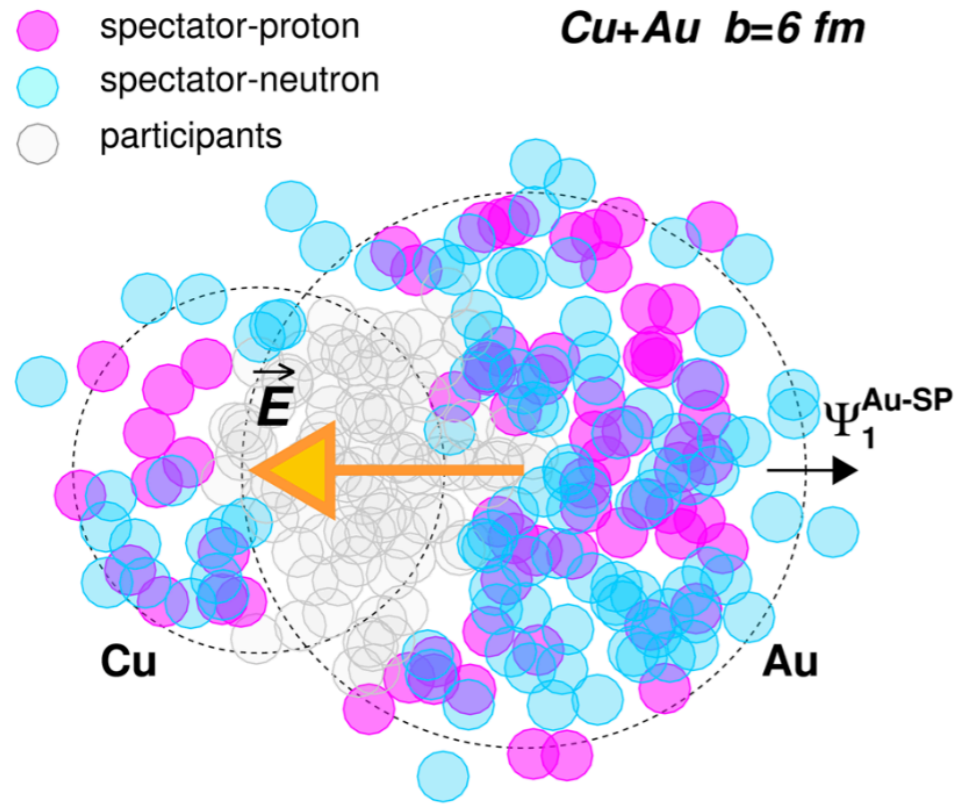


STAR, PRL 127, 052302 (2021)

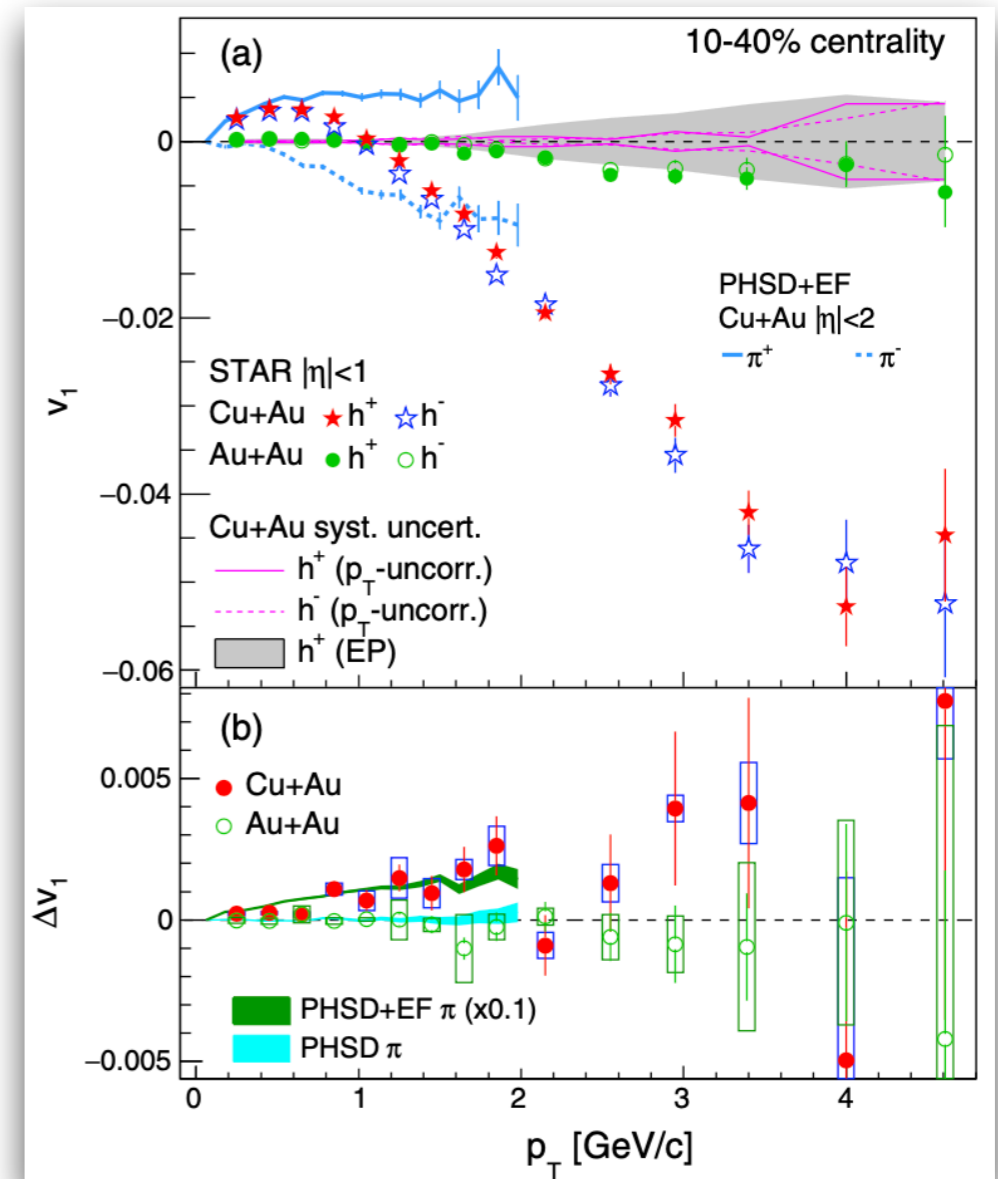
- Observed large  $\cos(4\Delta\phi)$  modulation
- Features consistent with strong EM field

- No QGP medium
- B field in vacuum

# Electric field in asymmetric collision system



## Inclusive charged particles

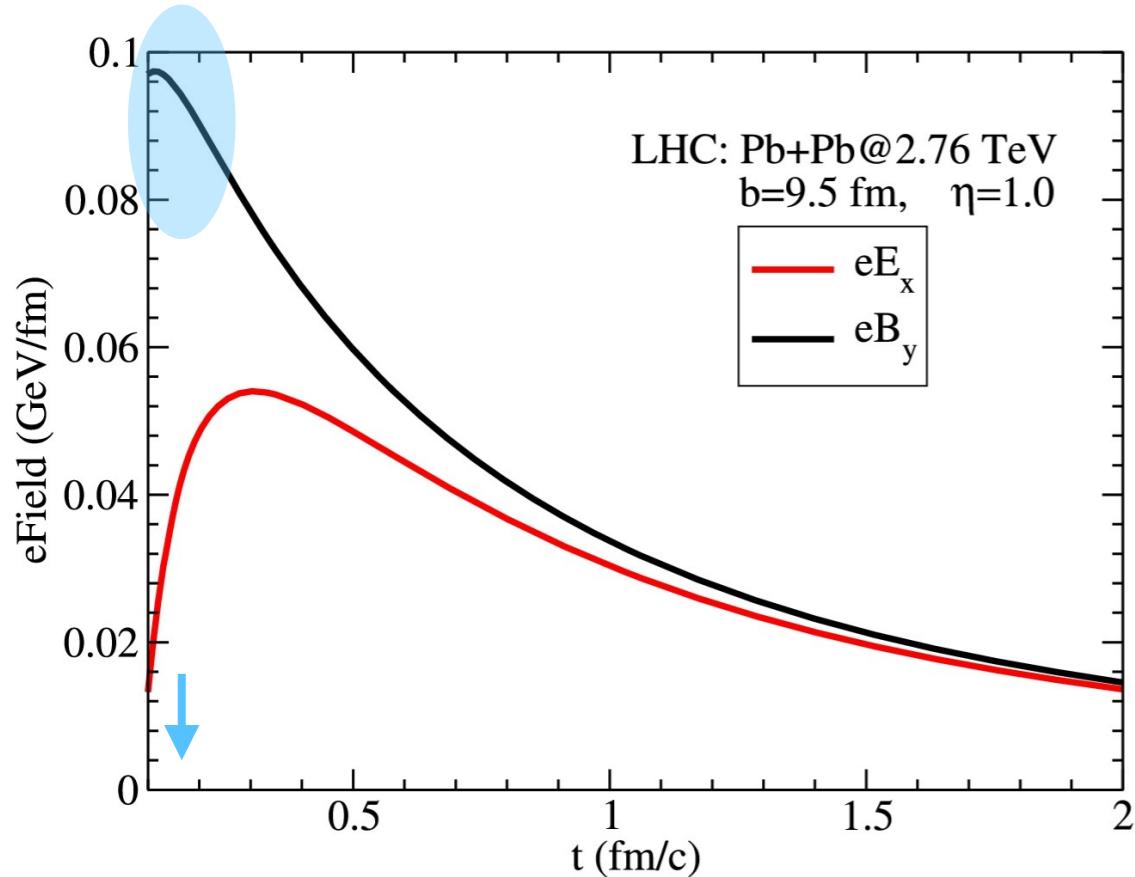


STAR, PRL 118, 012301 (2017)

- In asymmetric collision system  $\rightarrow$  in-plane  $\mathbf{E}$  field (Coulomb effect)
- $\Delta v_1$  in Cu+Au qualitatively agrees with expectation
- Can constrain electrical conductivity of the medium



# Charm hadron directed flow splitting

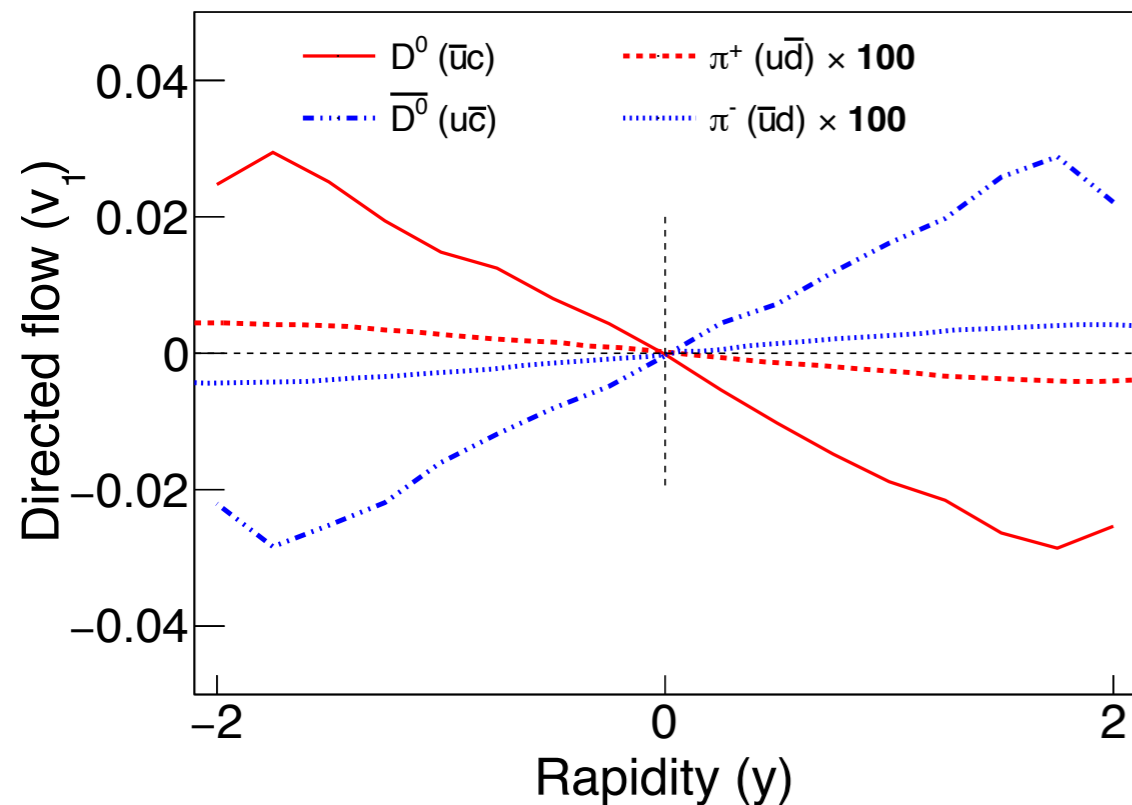


## Charm quark

Formation time:  $\tau_{cQ} \sim 0.1$  fm/c  
 Long relaxation time

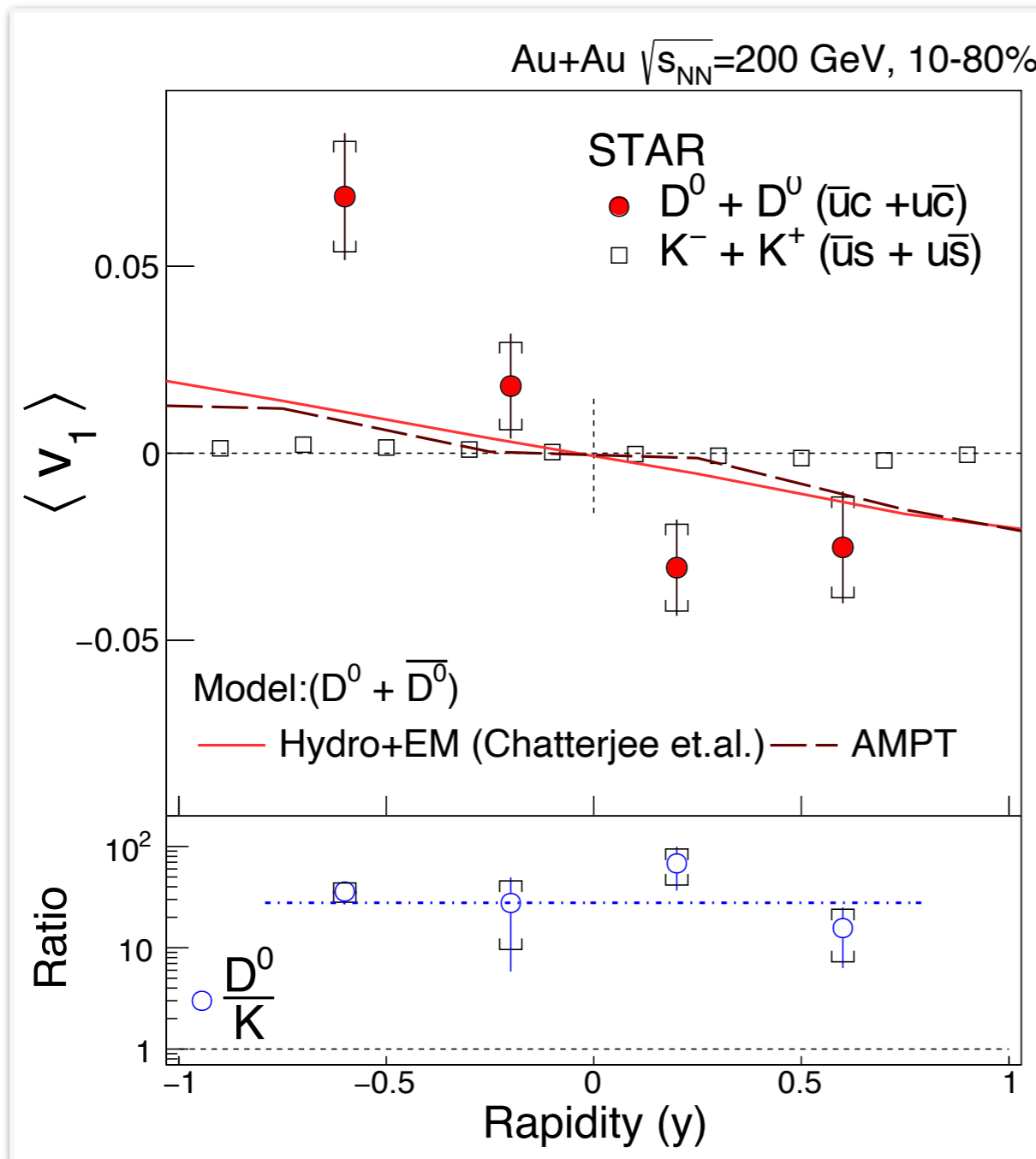
Sensitive to early time B-field  
 Can retain its memory

- B field in QGP

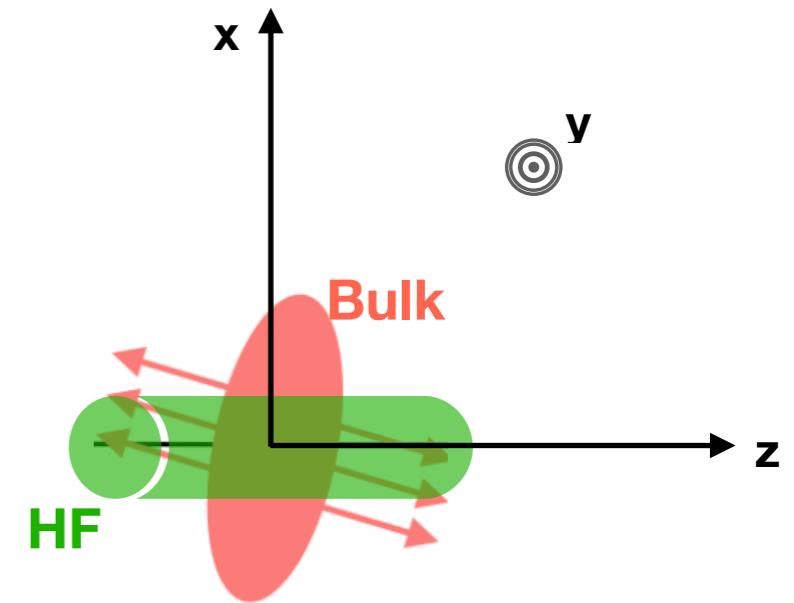


Das et al, PLB 768, 260 (2017)

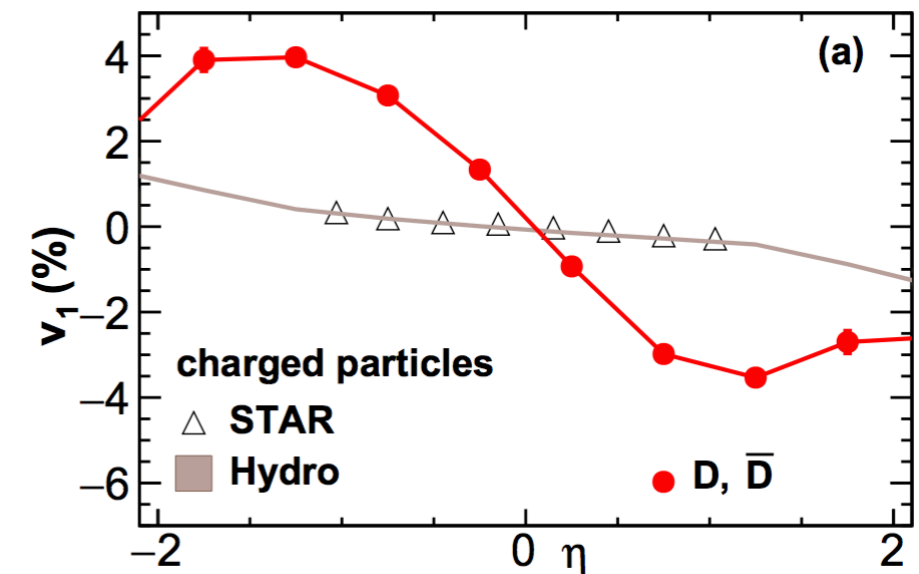
# Observation of $D^0$ directed flow



STAR, PRL 123, 162301 (2019)



Drag force between the tilted bulk and the HFs

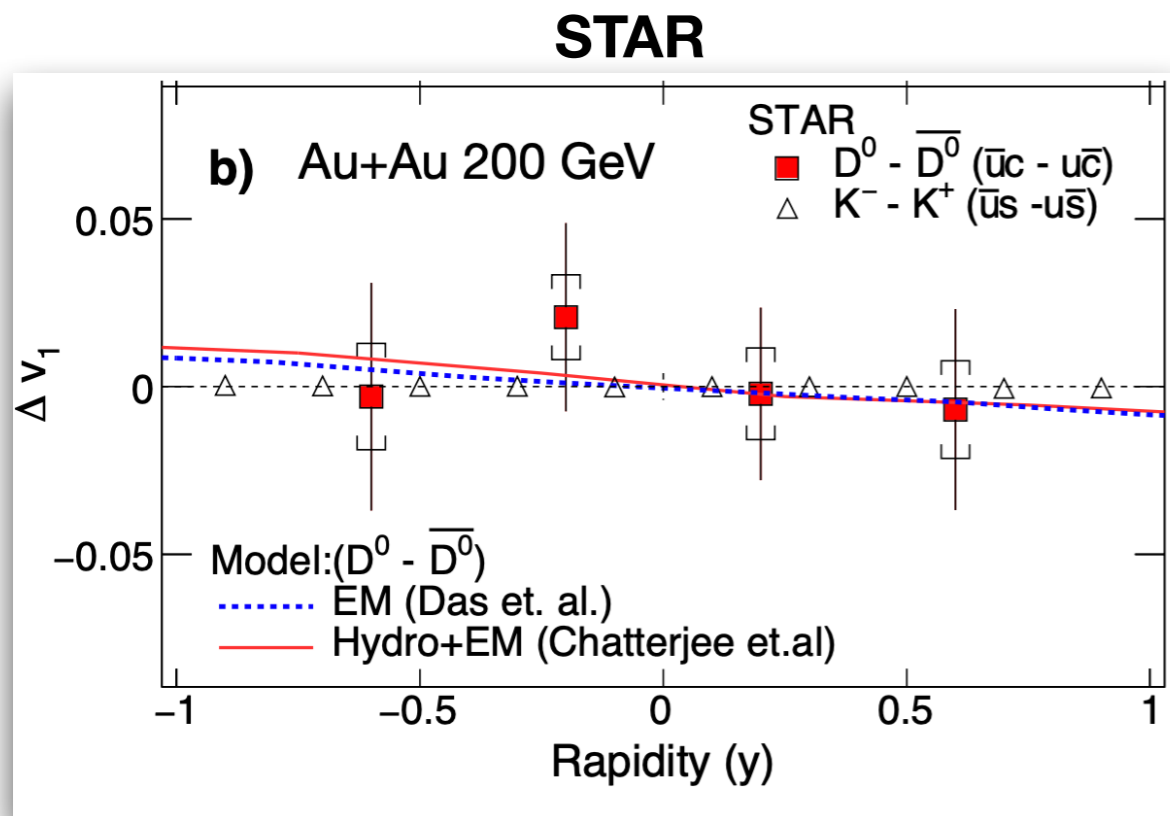


- First observation of non zero charm  $v_1$
- $v_1$ :  $D^0 \gg K$

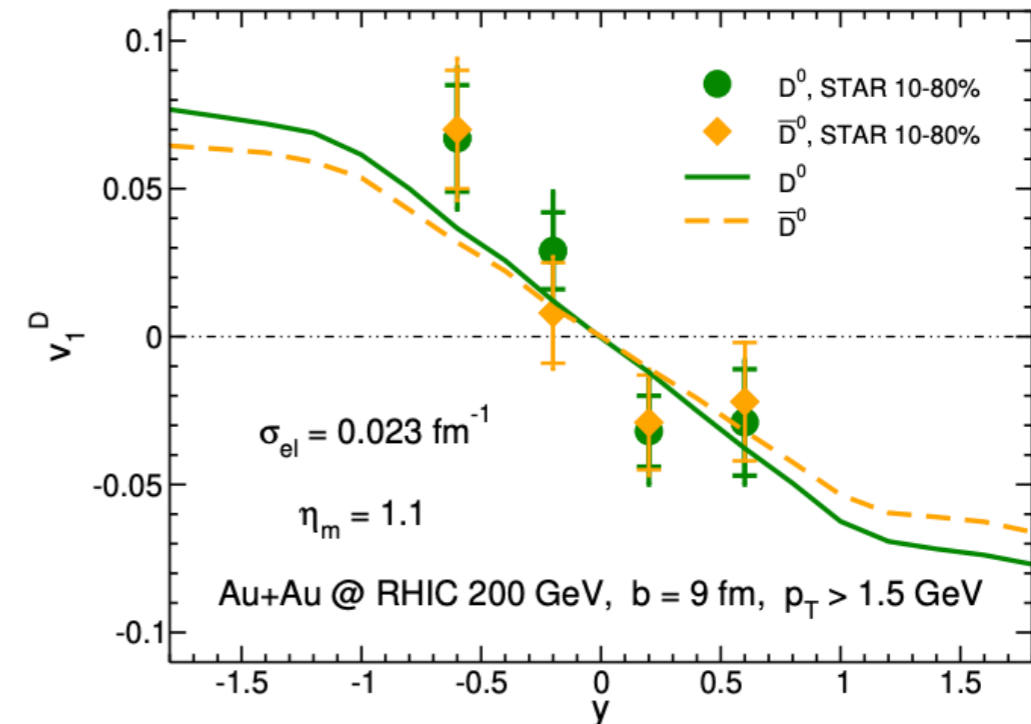
# Charge dependent $D^0$ directed flow ( $\Delta v_1$ )

Model: with electrical conductivity of QGP

$$\sigma \sim 0.023 \text{ fm}^{-1}$$



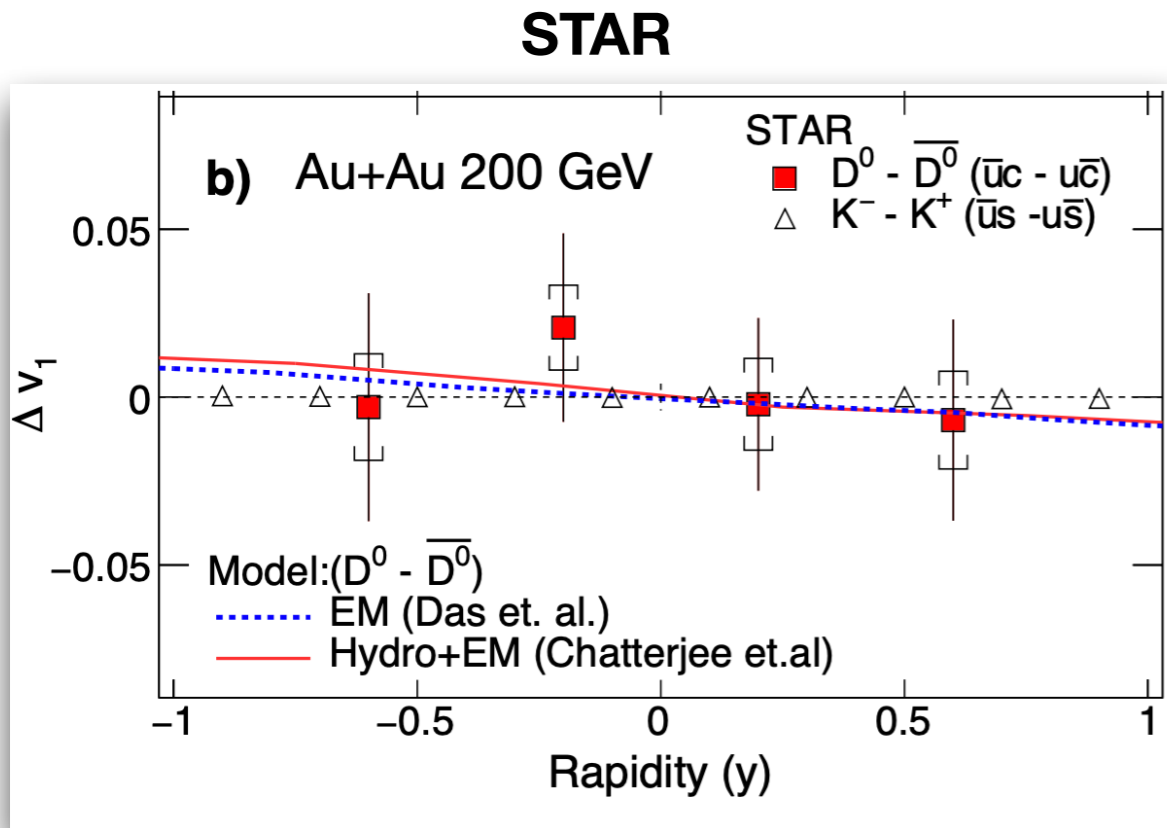
STAR, PRL 123, 162301 (2019)



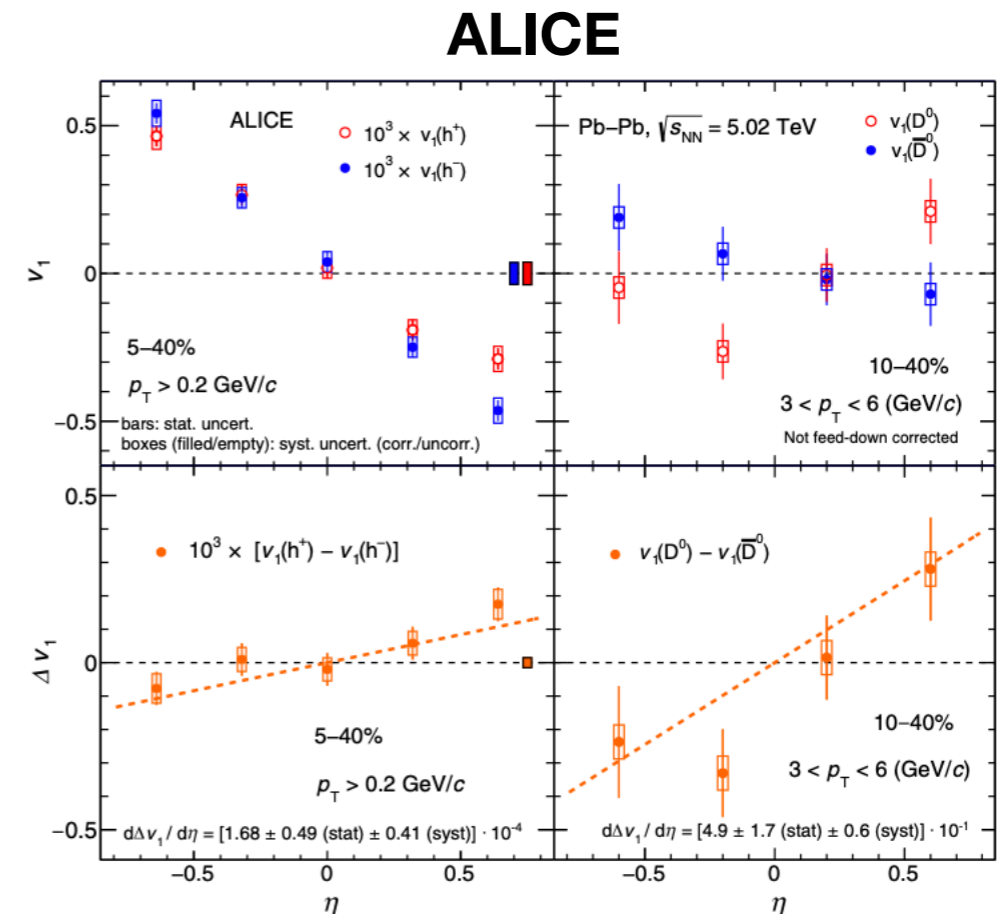
Oliva et al, JHEP 05, 034 (2021)

- First attempt to probe EM field effects via charm  $v_1$
- $\Delta v_1$  were inconclusive, not enough precision to constrain QGP conductivity

# Charge dependent charm hadron directed flow



*Not sufficient precision at STAR*



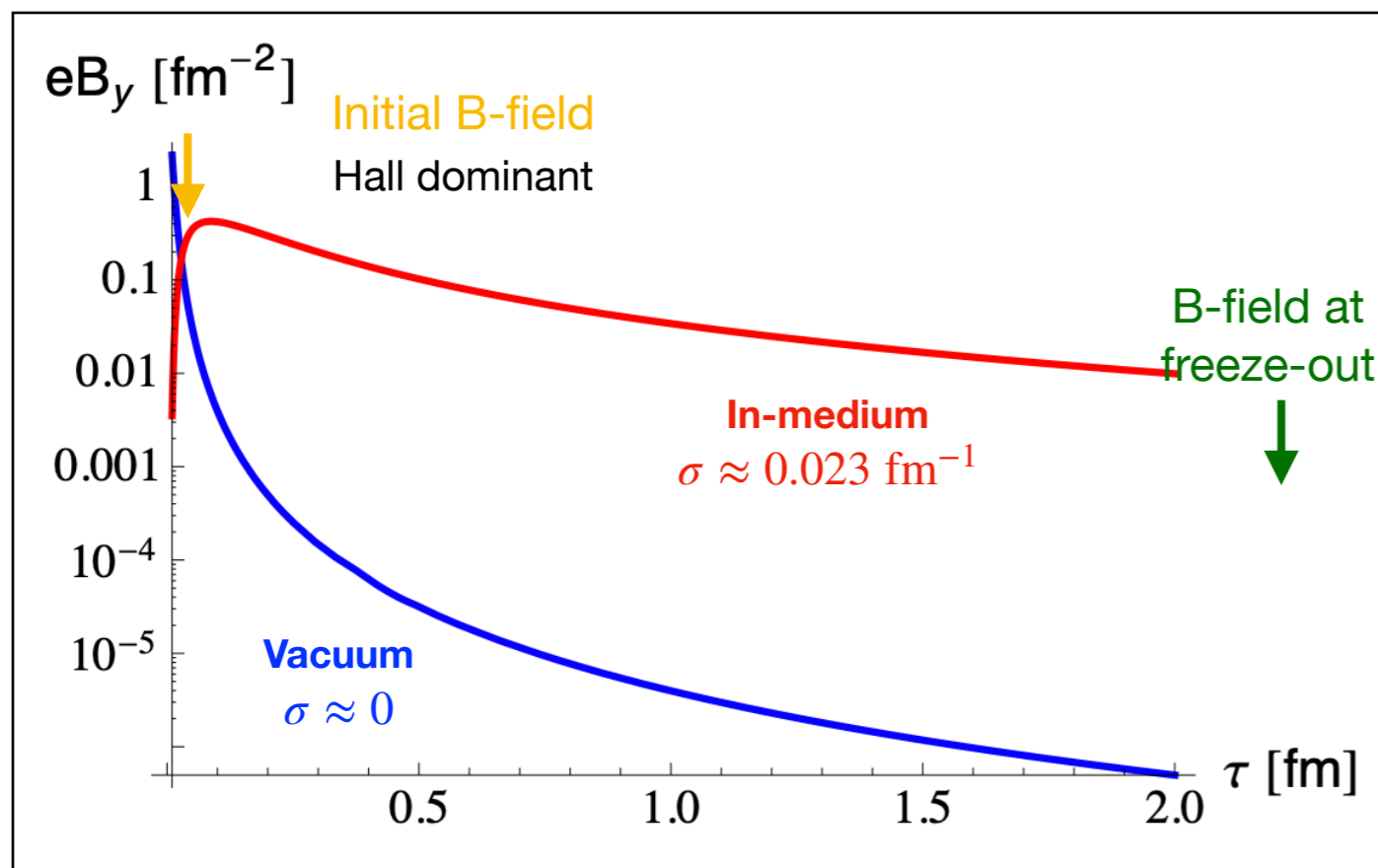
*Not sufficient precision at ALICE  
 (Run-3 can provide good precision)*

- First attempt to probe EM field effects via charm  $v_1$
- $\Delta v_1$  were inconclusive for both RHIC and LHC

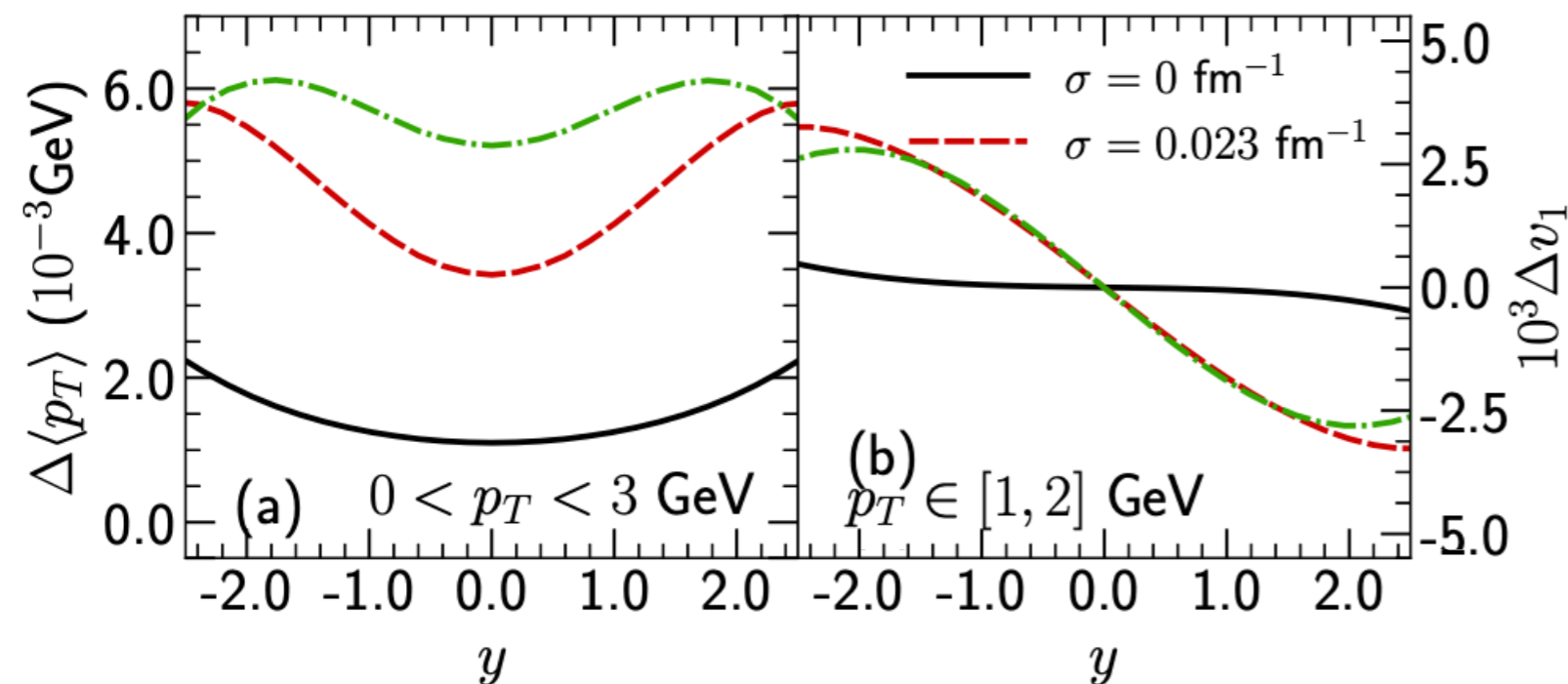
Charm hadrons are promising probe but challenging ...



# Charge dependent light hadron directed flow

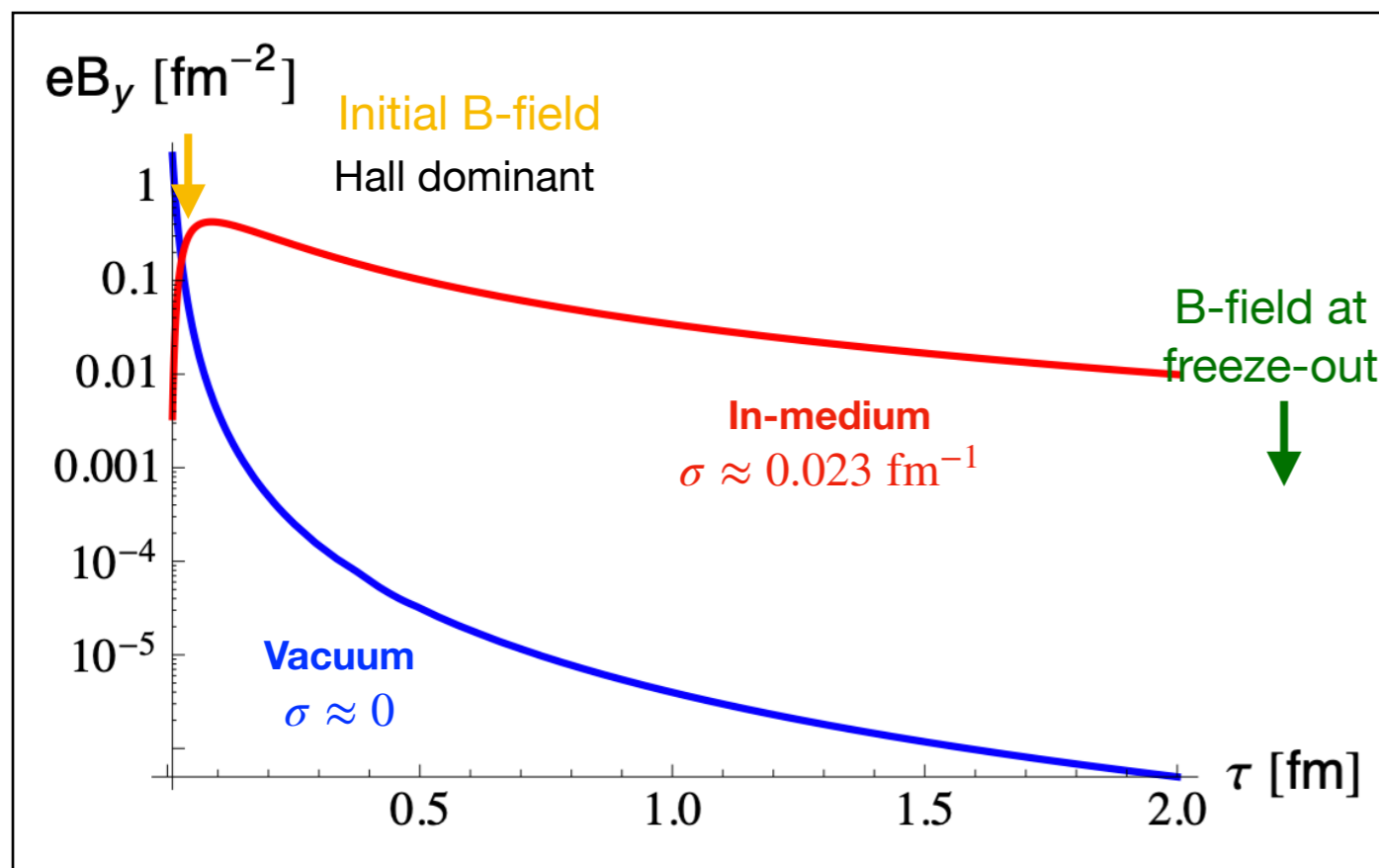


- **Imprints of EM field effects**
- Hall: **positive**  $\Delta v_1$
- Faraday: **negative**  $\Delta v_1$
- Coulomb: **negative**  $\Delta v_1$



- $\Delta v_1$  sensitive to QGP conductivity

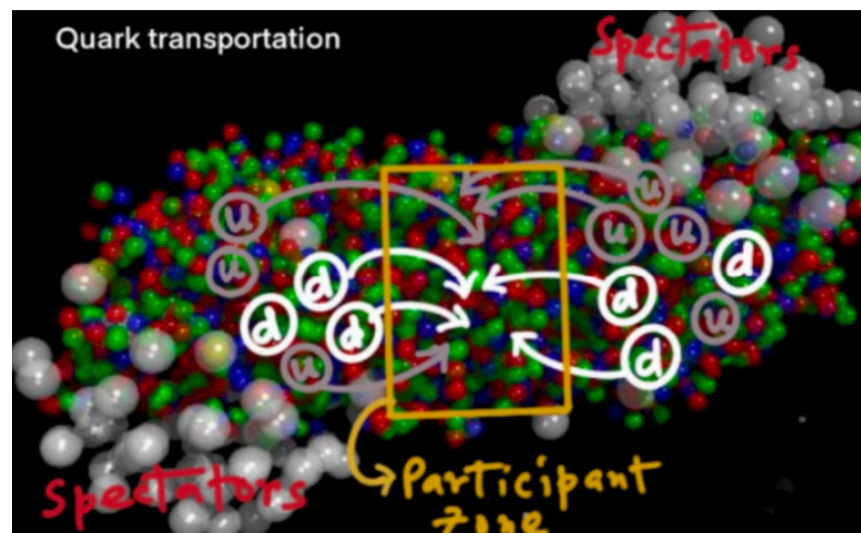
# Charge dependent light hadron directed flow



- **Imprints of EM field effects**
- Hall: **positive**  $\Delta v_1$
- Faraday: **negative**  $\Delta v_1$
- Coulomb: **negative**  $\Delta v_1$

- **Non-EM field effects**
- Transport:  $\Delta v_1^\dagger \neq 0$
- ....

Transported quark effect:  $\Delta v_1 \neq 0$

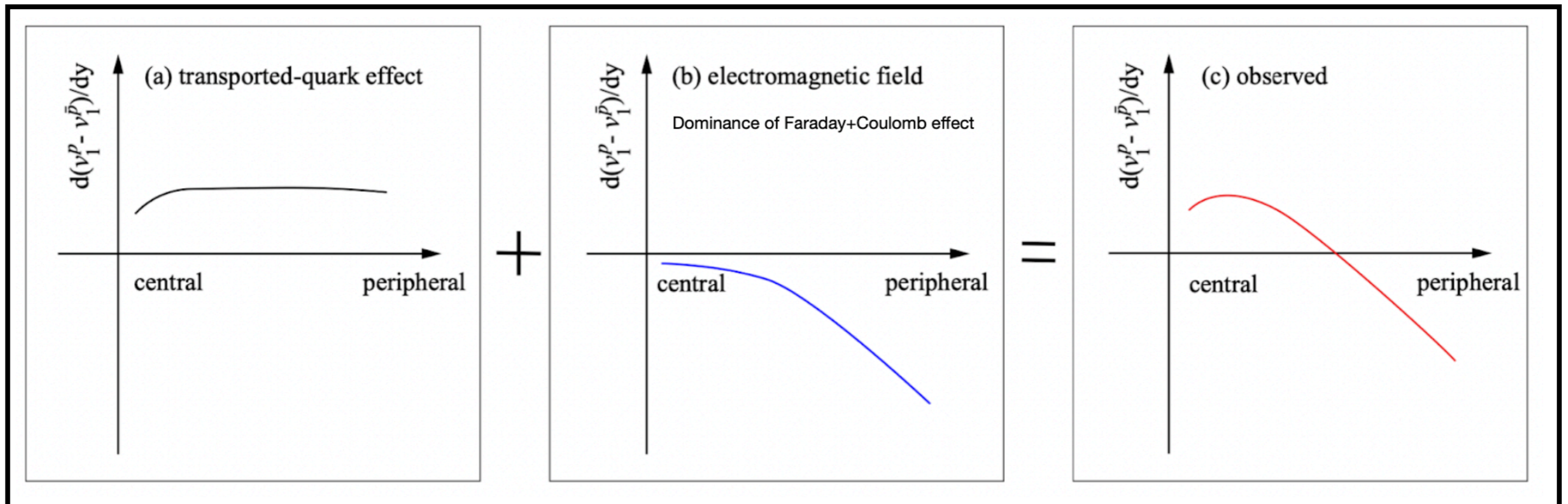


“u” and “d” quarks transported from incoming nuclei towards mid-rapidity

$p : \boxed{uud}$	$\frac{dv_1^+}{dy} - \frac{dv_1^-}{dy} > 0$
$\bar{p} : \bar{u}\bar{u}\bar{d}$	$\frac{dv_1^+}{dy} - \frac{dv_1^-}{dy} > 0$
$K^+ : \boxed{u\bar{s}}$	$\frac{dv_1^+}{dy} - \frac{dv_1^-}{dy} > 0$
$K^- : \bar{u}s$	$\frac{dv_1^+}{dy} - \frac{dv_1^-}{dy} > 0$
$\pi^+ : \boxed{u\bar{d}}$	$\frac{dv_1^+}{dy} - \frac{dv_1^-}{dy} < 0$
$\pi^- : \bar{u}\boxed{d}$	$\frac{dv_1^+}{dy} - \frac{dv_1^-}{dy} < 0$
( #d > #u, Au neutron rich )	

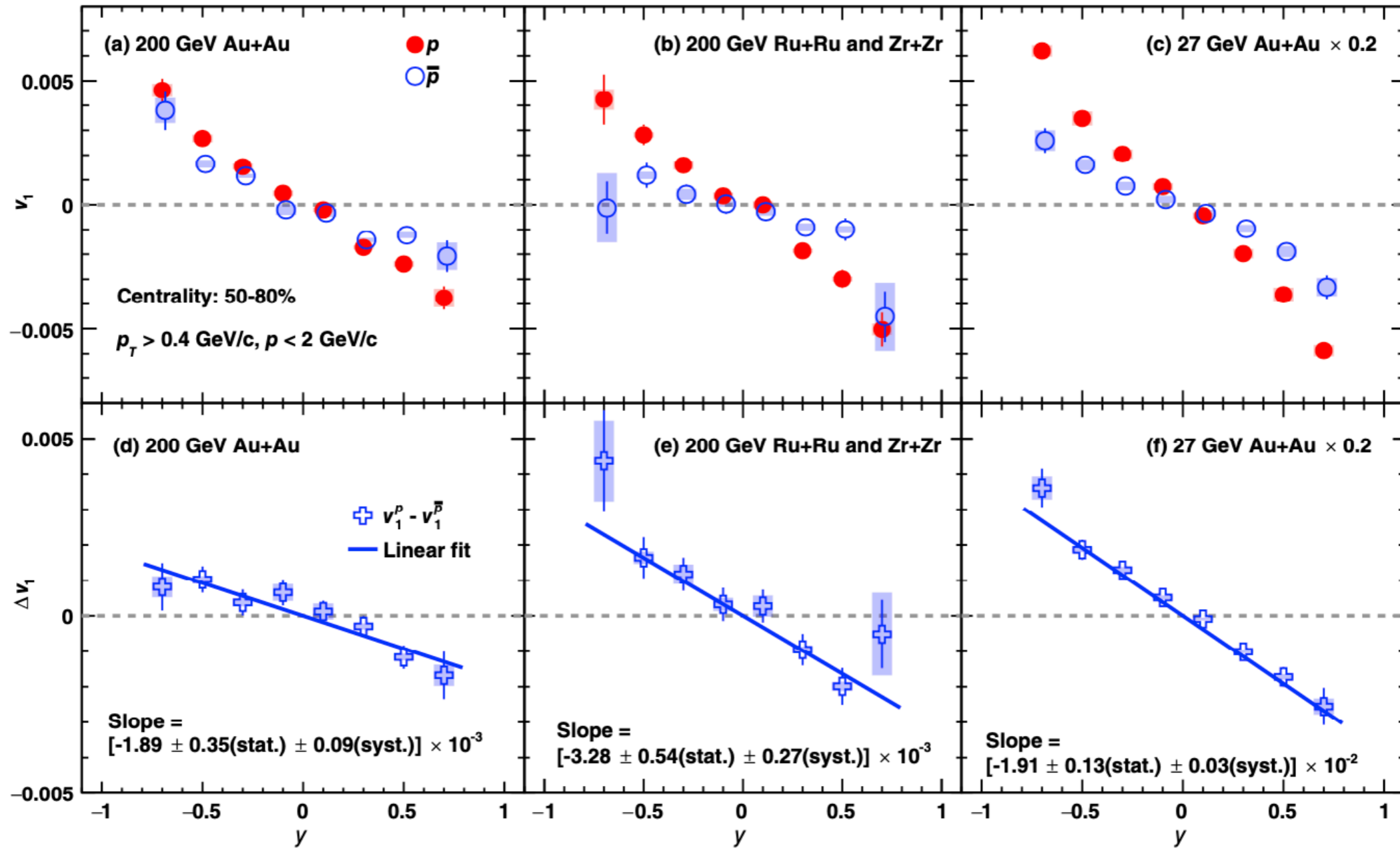
# Charge dependent light hadron directed flow

- Naive expectation for protons: EM field + transport



- For protons  $\Delta v_1$  can change sign  
(if Faraday+Coulomb dominates over Hall effect)

# Light hadron directed flow $v_1$

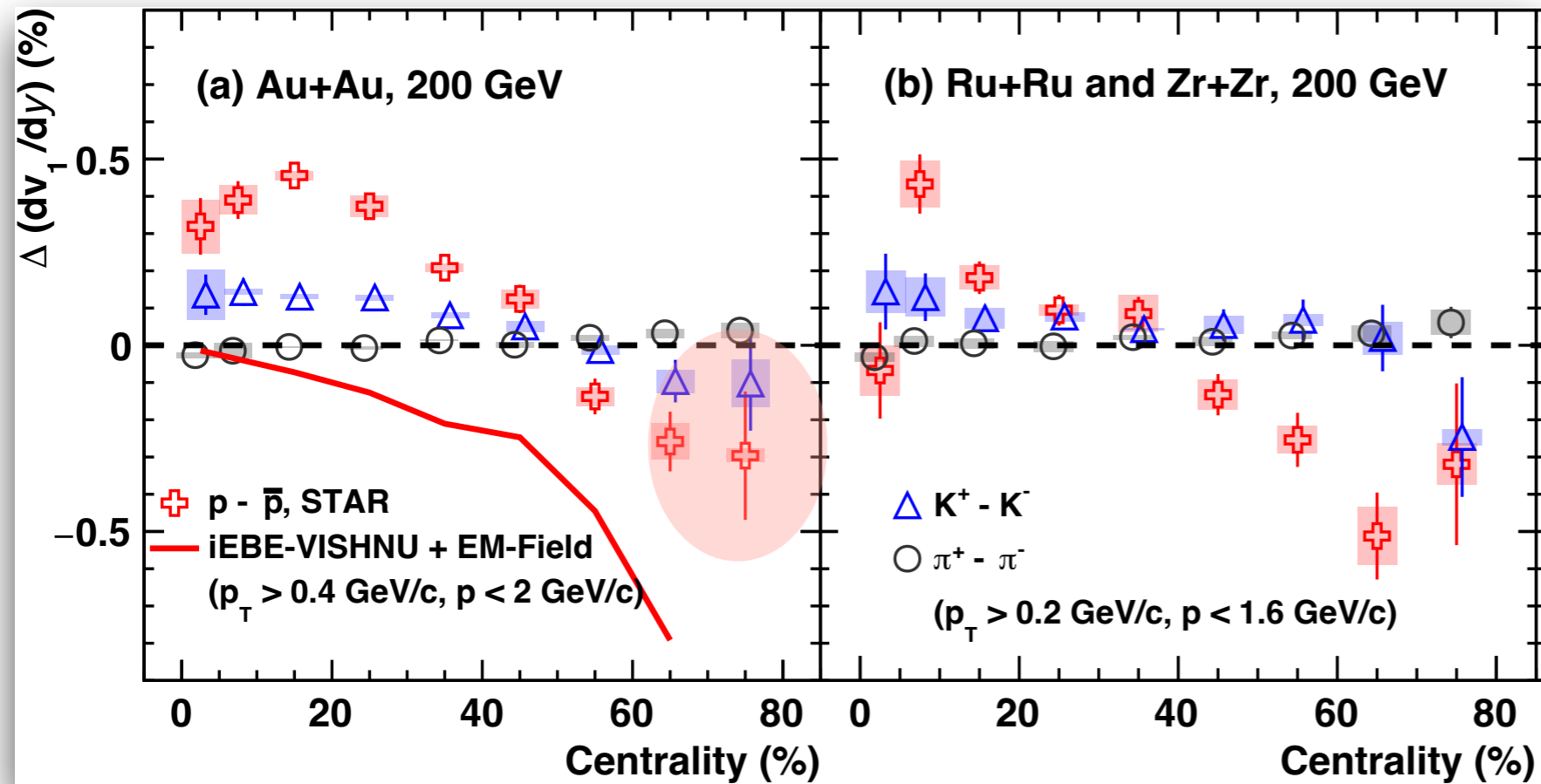


STAR, PRX 14, 011028 (2024)

- Significant splitting for proton's  $\Delta v_1$  ( $> 5\sigma$  significance)  
(Negative  $\Delta v_1$  consistent with Faraday+Coulomb dominates over Hall effect)



# Charge dependent light quark directed flow

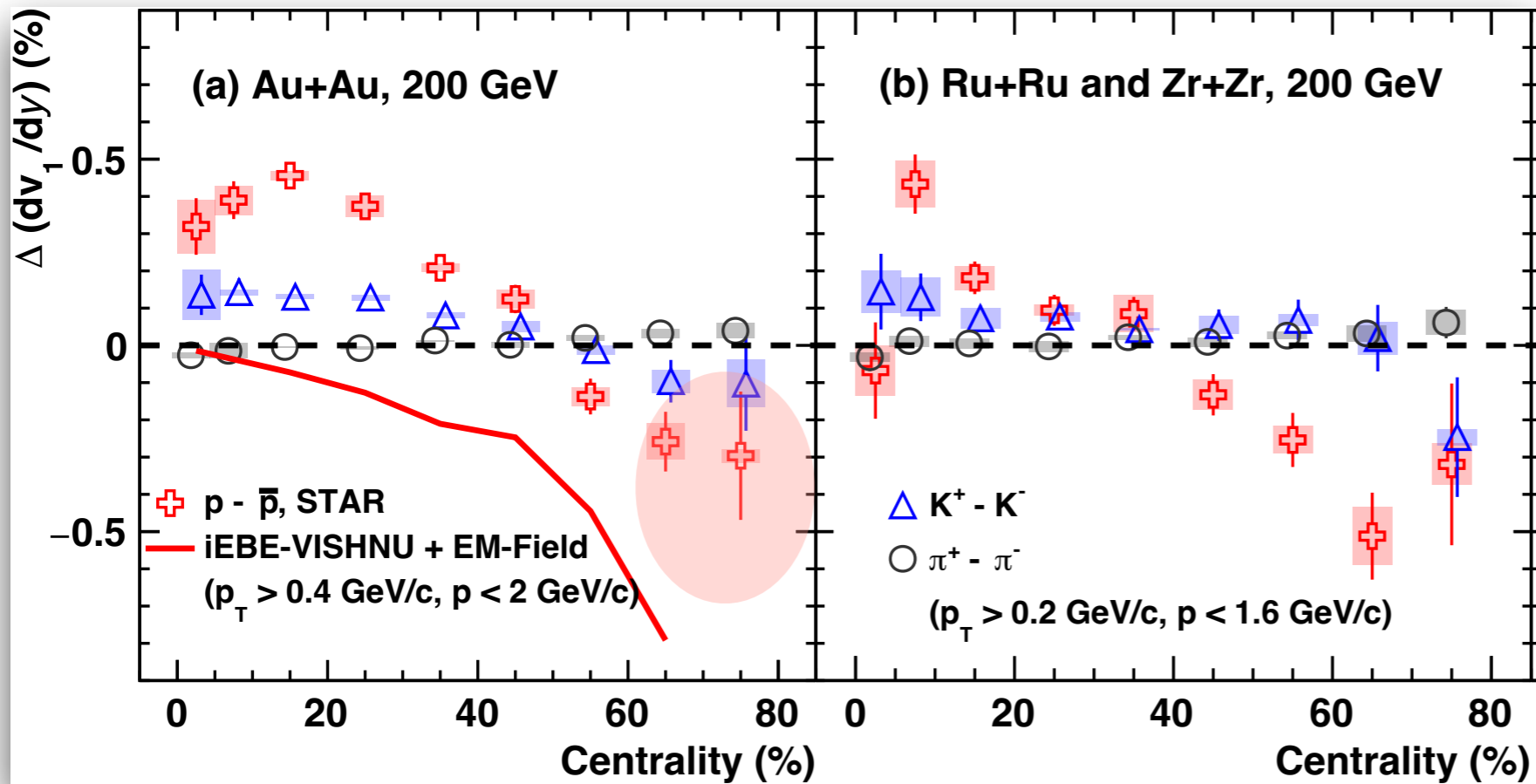


STAR, PRX 14, 011028 (2024)

- For protons and kaons: sign change in  $\Delta v_1$  in peripheral collisions  
(Negative  $\Delta v_1$  consistent with Faraday+Coulomb dominates over Hall effect)
- Model iEBE-VISHNU + EM:  $\sigma \sim 0.023 \text{ fm}^{-1}$  (falls within a reasonable range)

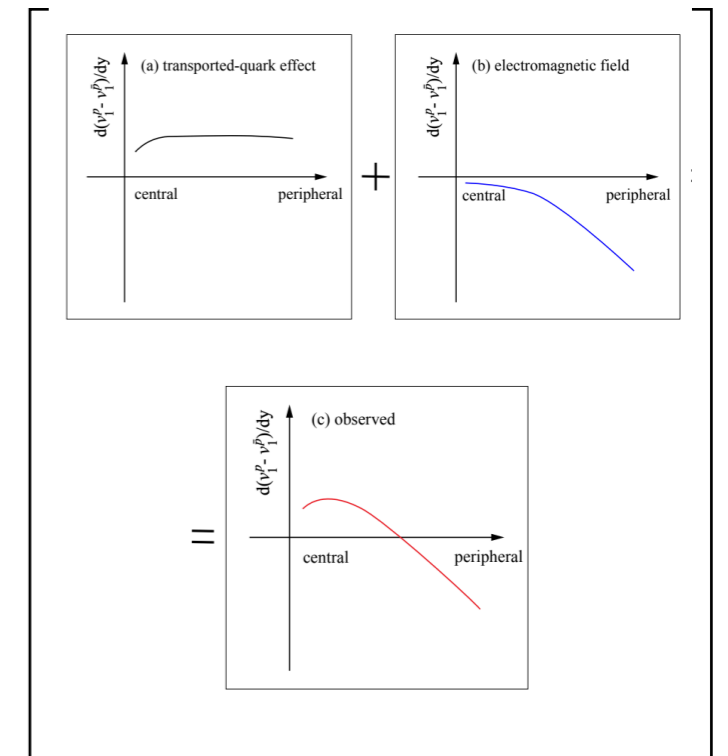
# Charge dependent light quark directed flow

## Observation



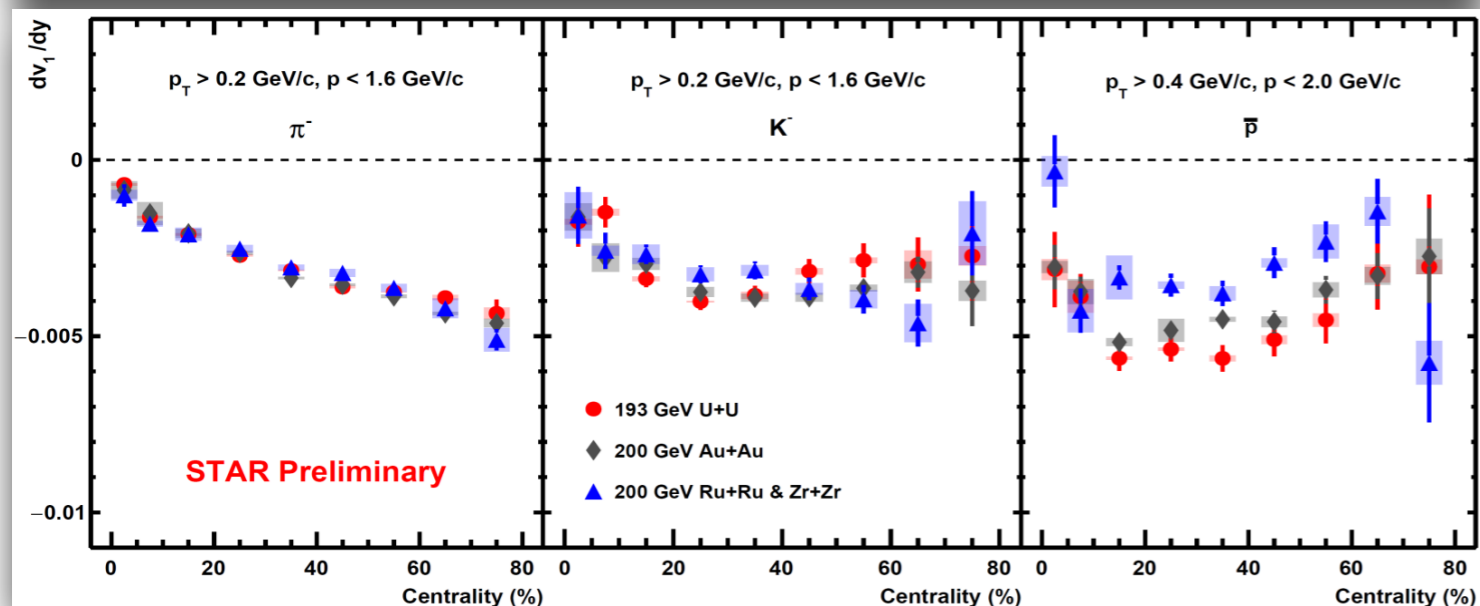
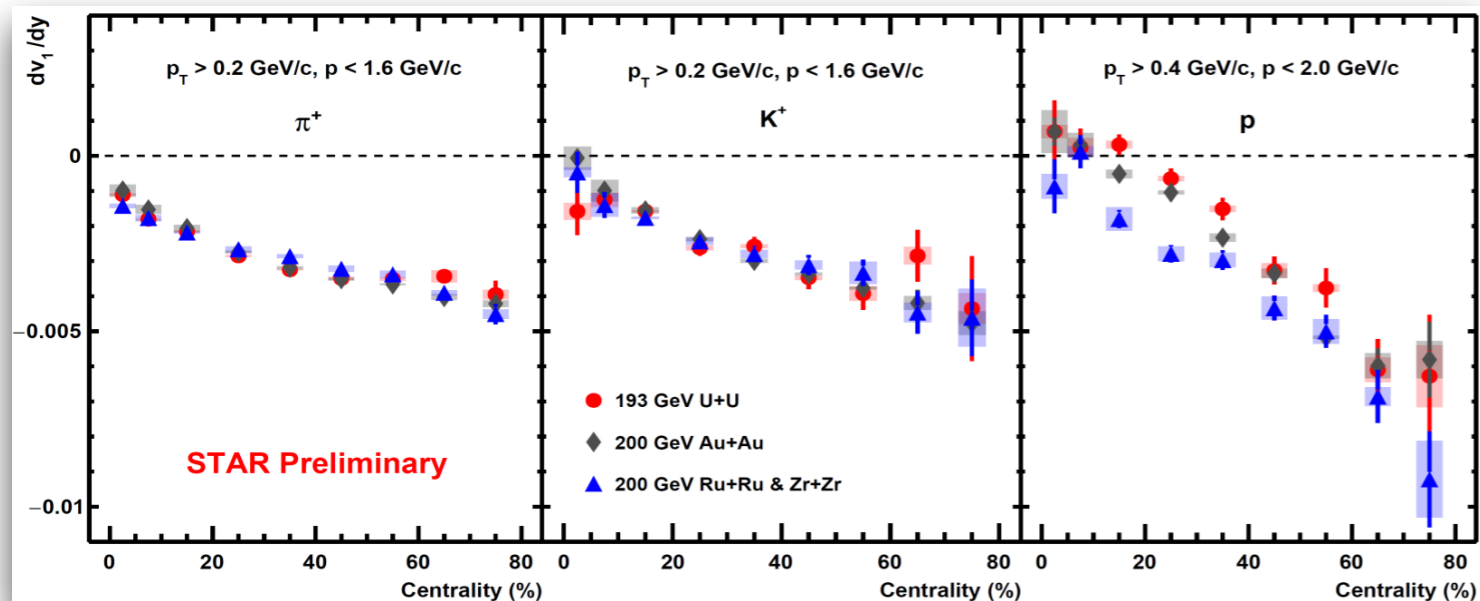
STAR, PRX 14, 011028 (2024)

## Expectation



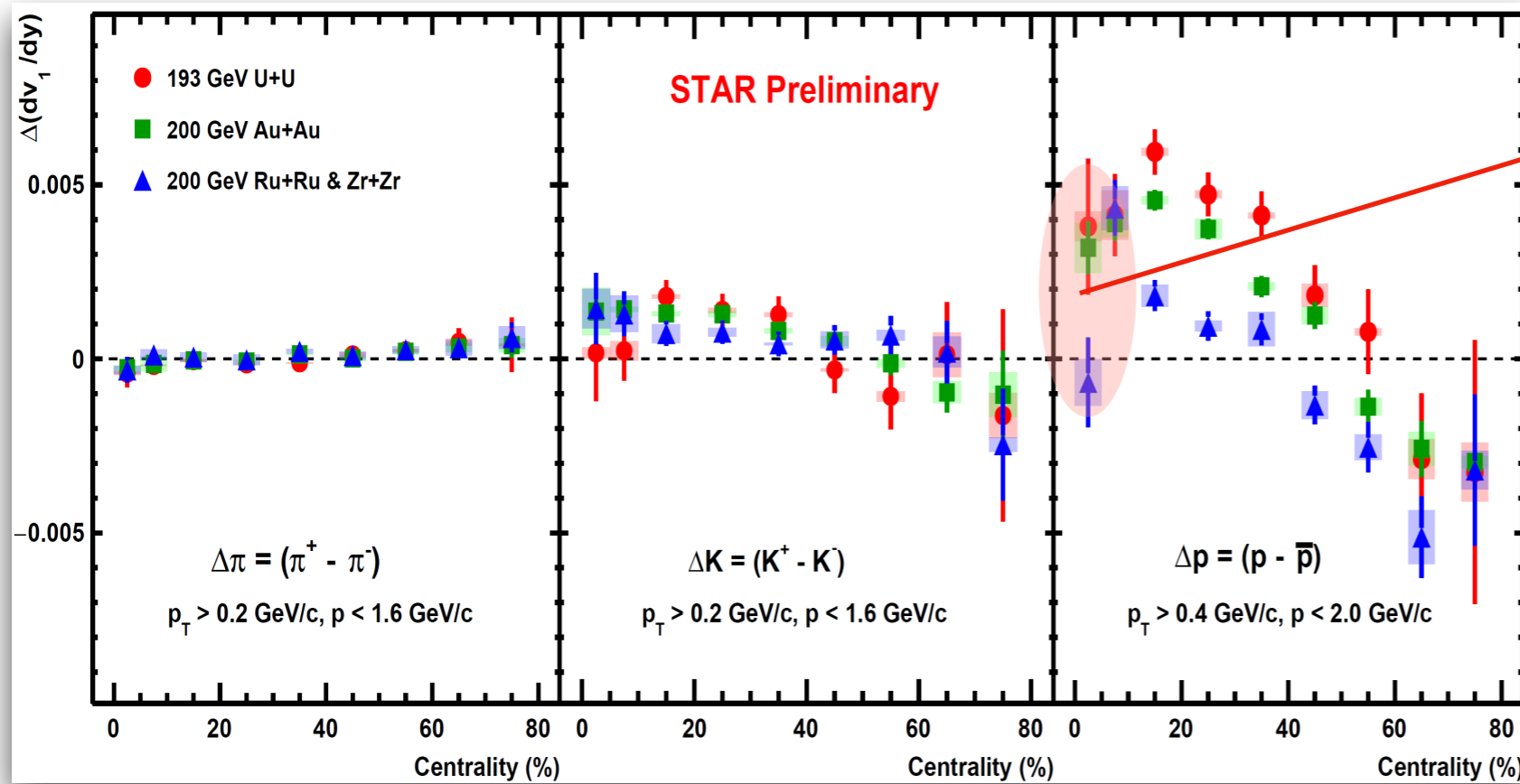
- For protons and kaons: sign change in  $\Delta v_1$  in peripheral collisions  
(Negative  $\Delta v_1$  consistent with Faraday+Coulomb dominates over Hall effect)
- For pions:  $\Delta v_1 \sim 0$  (large uncertainty)

# Light hadron $dv_1/dy$ : system size dependence



- pions & kaons: U+U  $\sim$  Au+Au  $\sim$  Isobar
- protons: U+U < Au+Au < Isobar
- anti-protons: U+U > Au+Au > Isobar

# Light hadron $\Delta dv_1/dy$ : system size dependence



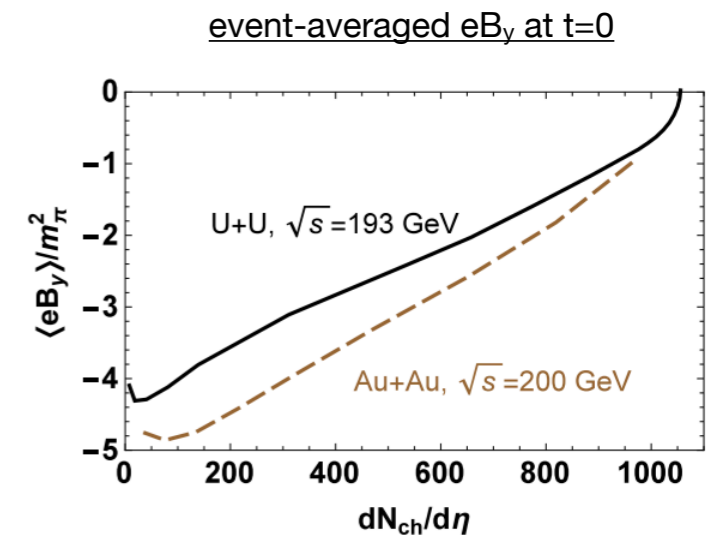
Splitting in most-central collisions  
Can be related to baryon transport

*Parida et al, 2305.08806*

- Interplay of baryon transport and electromagnetic field effects across centralities
- Require proper modeling to understand the data

in different systems several factors to be considered:

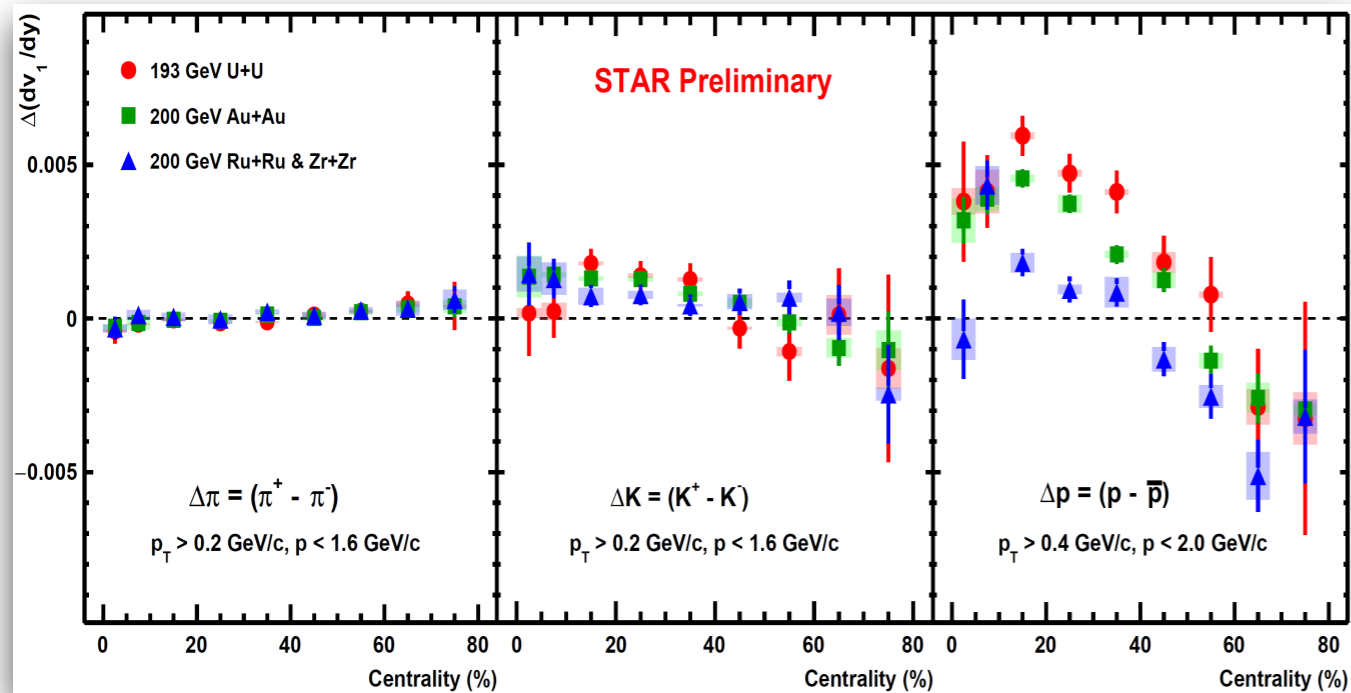
- strength and lifetime of EM-field
- QGP lifetime and conductivity
- transport
- ...



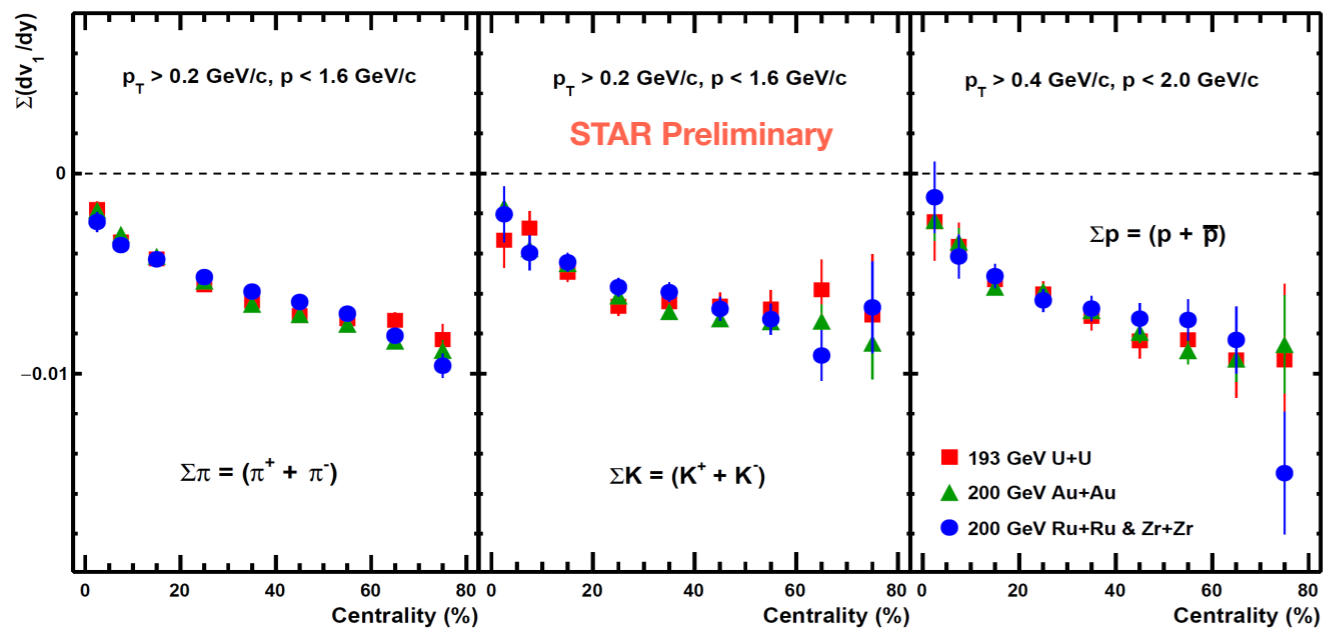
*Bloczynski et al, NPA 939, 85 (2015)*



# Light hadron $\Delta dv_1/dy$ : system size dependence

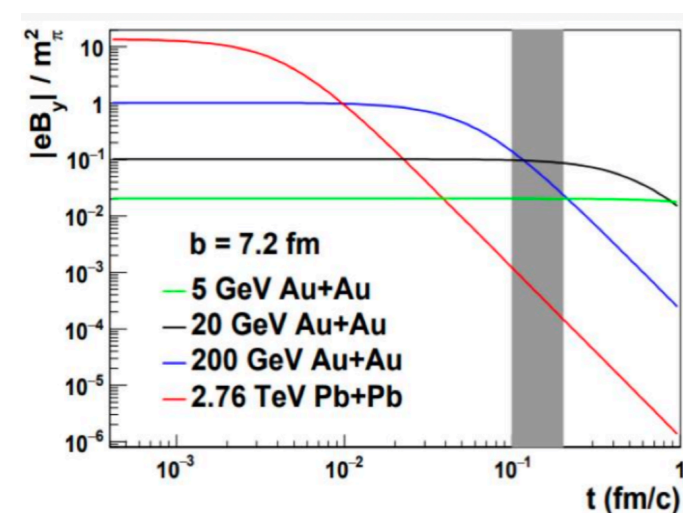
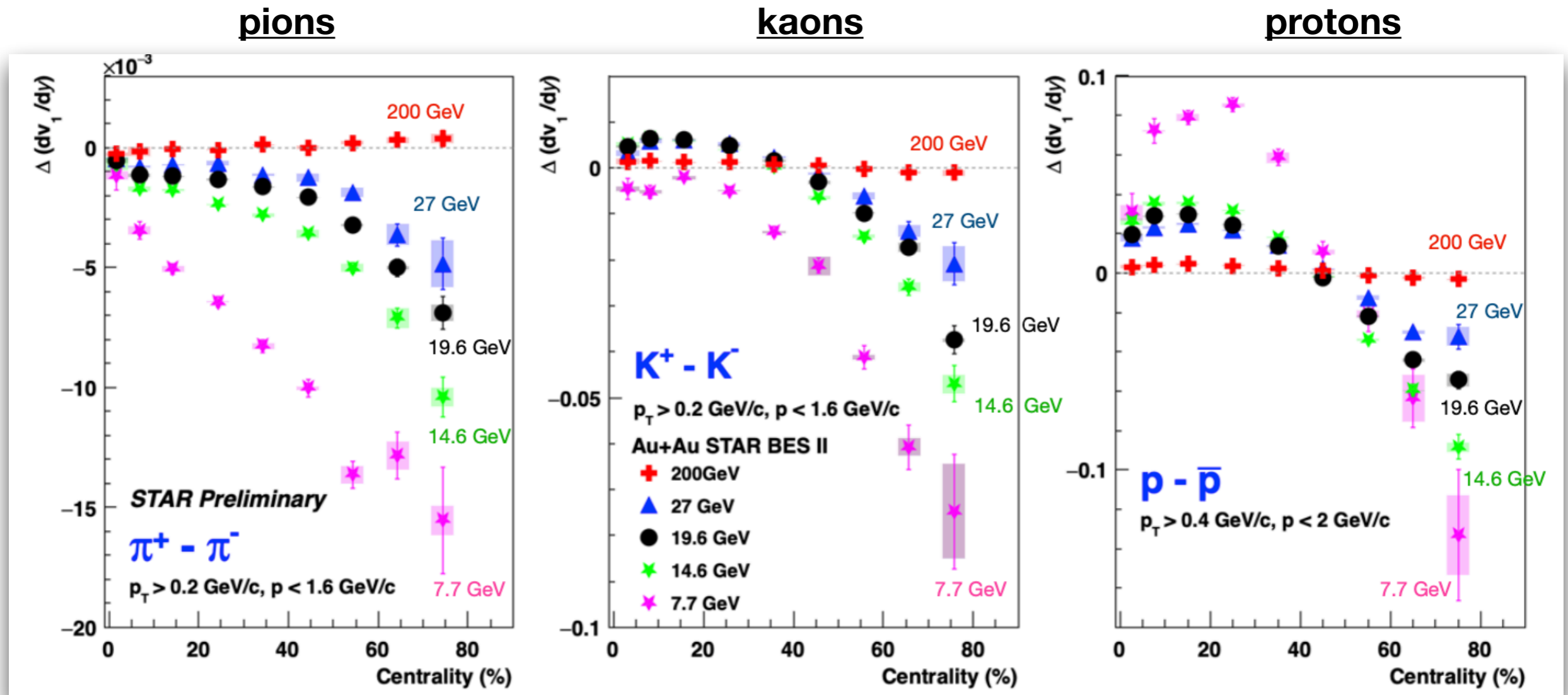


- Difference  $\Delta v_1$ :  $h^+ - h^-$
- pions & kaons: U+U  $\sim$  Au+Au  $\sim$  Isobar
- protons: U+U  $<$  Au+Au  $<$  Isobar



- Sum  $\Sigma v_1$ :  $h^+ + h^-$
- pions & kaons: U+U  $\sim$  Au+Au  $\sim$  Isobar
- protons: U+U  $\sim$  Au+Au  $\sim$  Isobar

# Light hadron $\Delta dv_1/dy$ : beam energy dependence



- In peripheral, negative  $\Delta v_1$  increases with decreasing beam energy
- consistent with dominance of Faraday and coulomb effect

With decreasing energy:

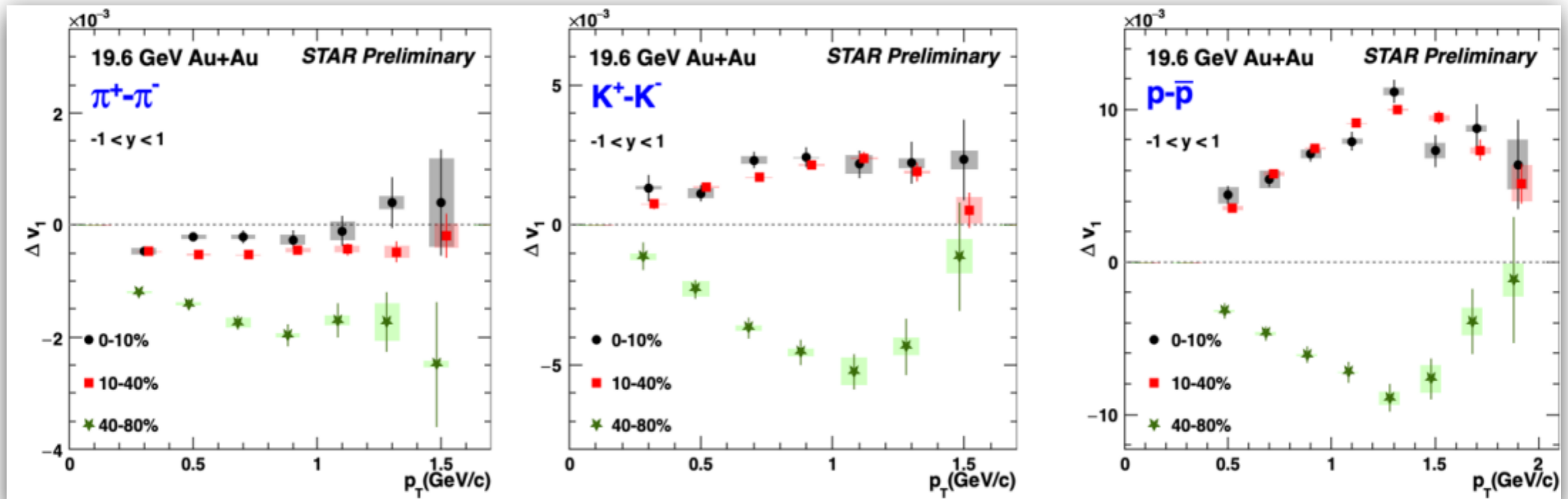
- Nuclear passage time is large and B-field lifetime could be longer
- Lifetime of fireball could be shorter

# Light hadron $v_1(p_T)$ : beam energy dependence

pions

kaons

protons



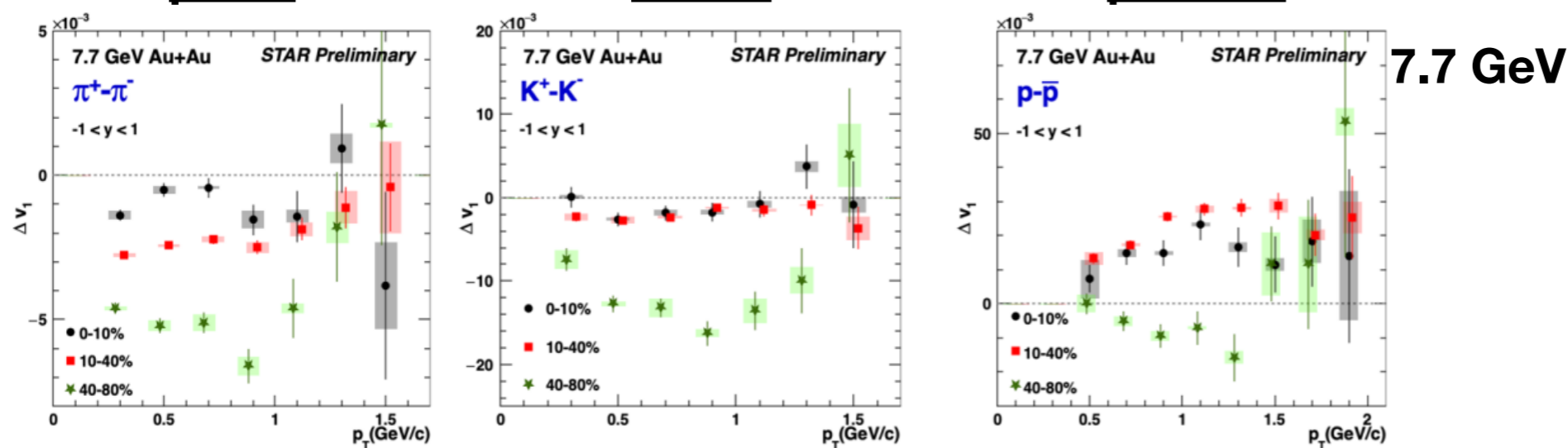
- Peripheral collisions (40-80%):
- Negative  $\Delta v_1$  increases linearly with  $p_T$
- Qualitatively Consistent with EM prediction

# Light hadron $v_1(p_T)$ : beam energy dependence

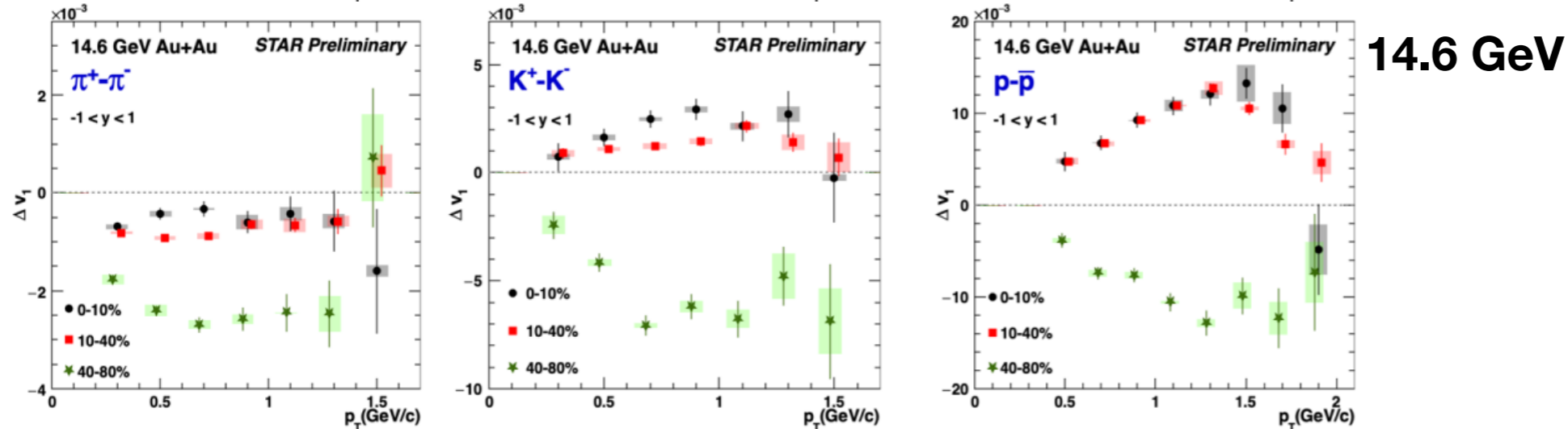
pions

kaons

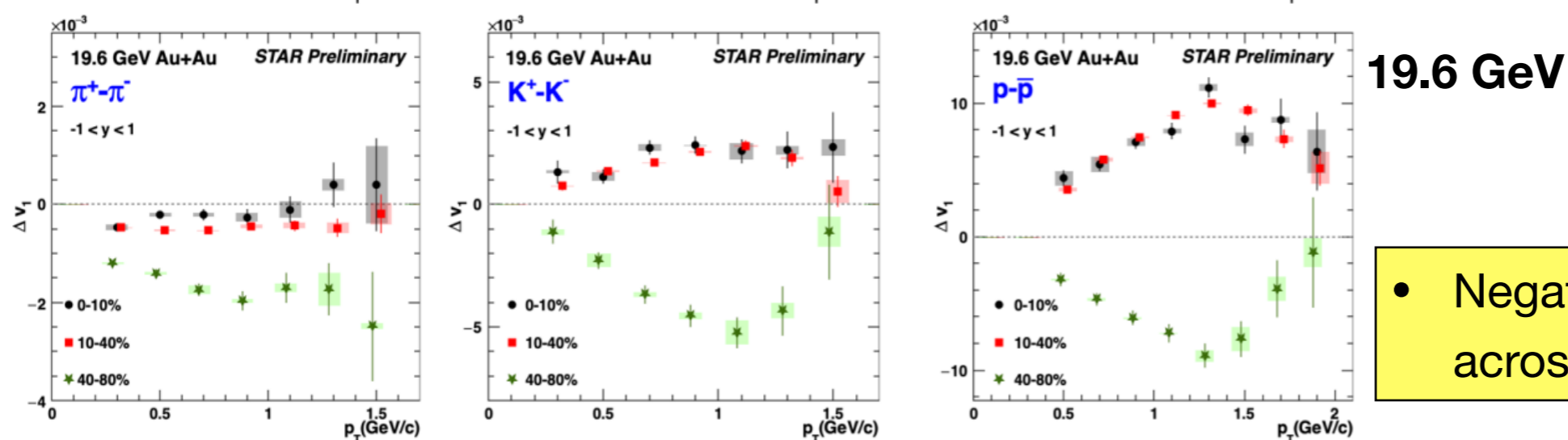
protons



7.7 GeV



14.6 GeV



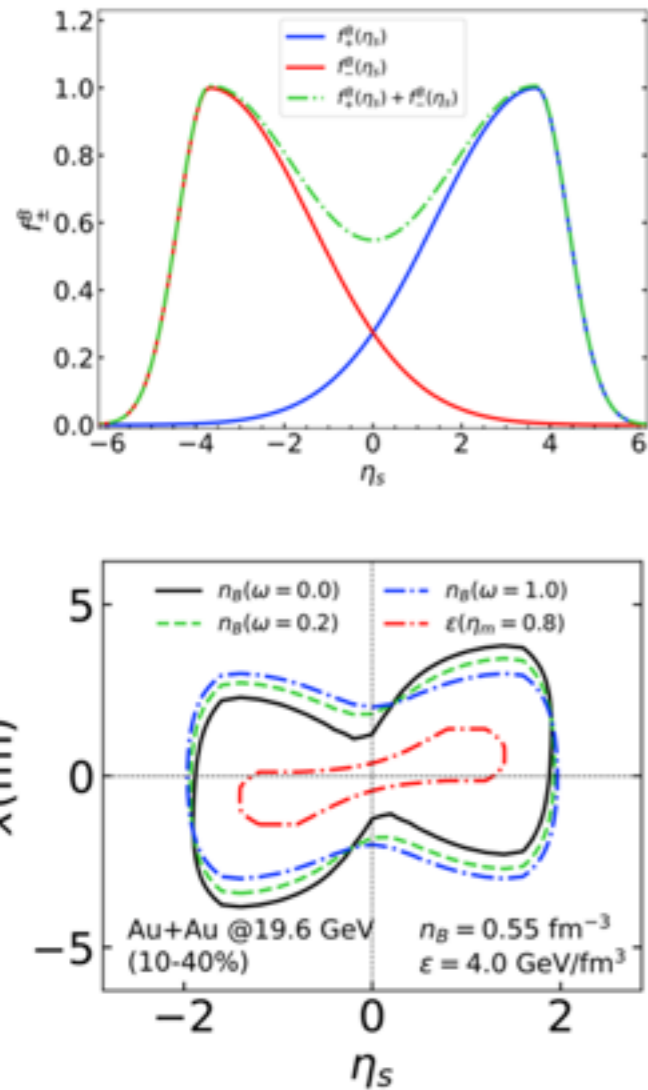
19.6 GeV

• Negative  $\Delta v_1$  pattern consistent across BES energies

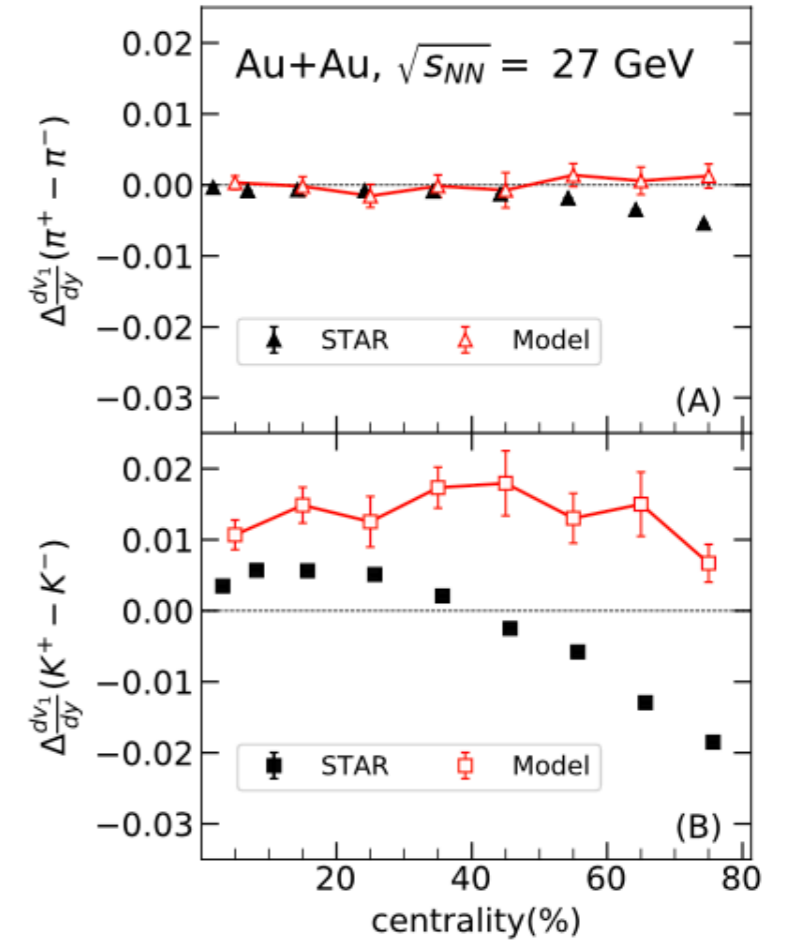
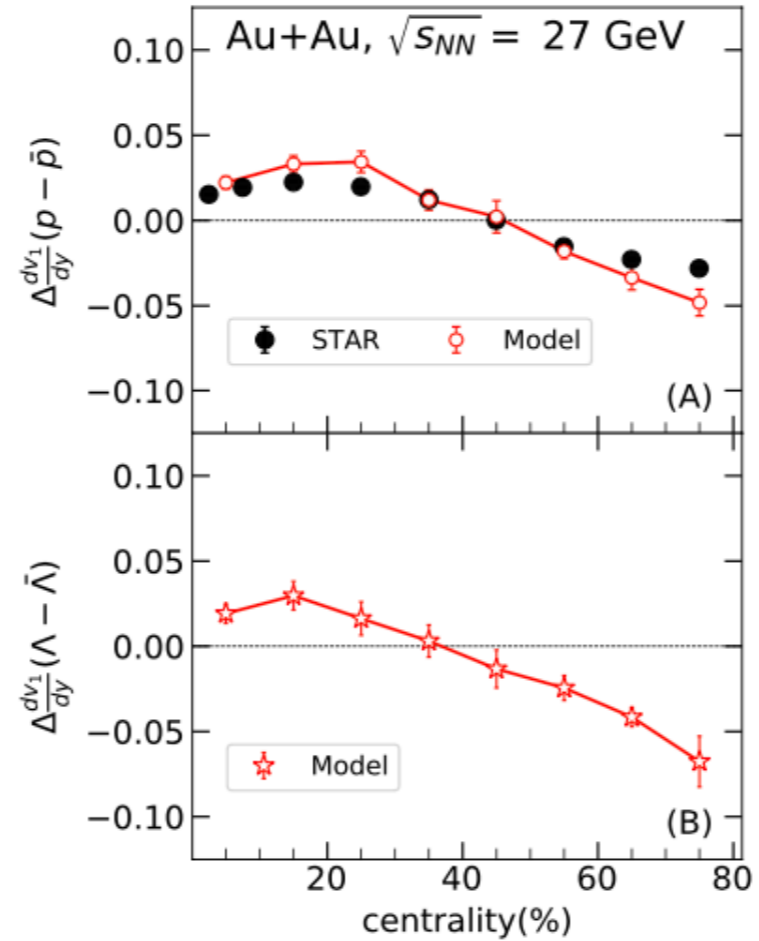


# Hydro with baryonic profile

Initial baryon profile



$\Delta v_1$  from Hydro without EM field

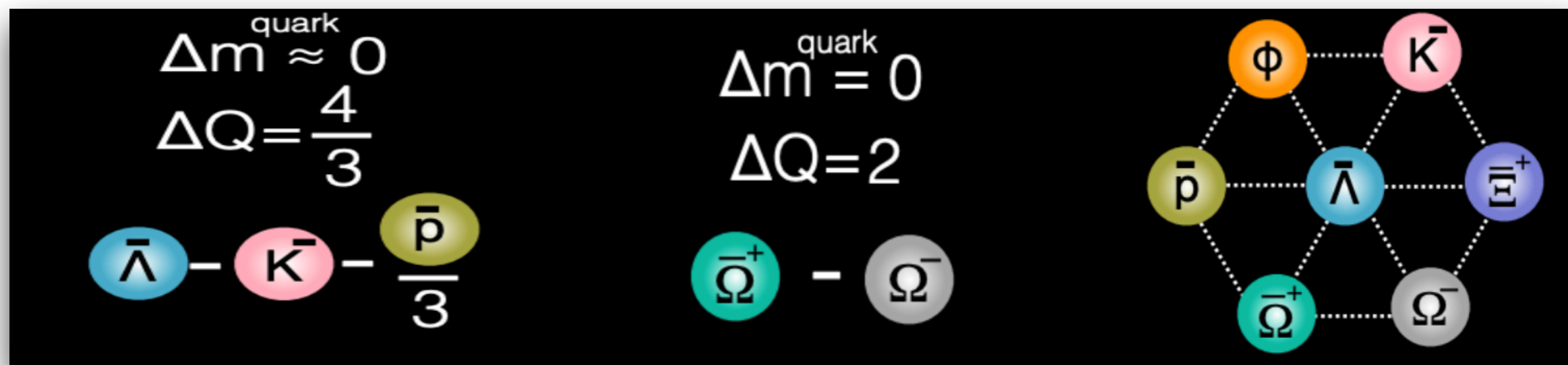


Parida et al, 2305.08806

- Hydrodynamic model with a baryonic profile (without EM) can qualitatively capture proton  $\Delta v_1$
- However, it can not explain negative  $\Delta v_1$  for pions and kaons
- Require modeling transport+EM to better understand  $\Delta v_1$

# Light hadron $\Delta v_1/dy$ : using only produced quarks

$\Delta v_1$  measured using combination of transported-quark-free hadrons

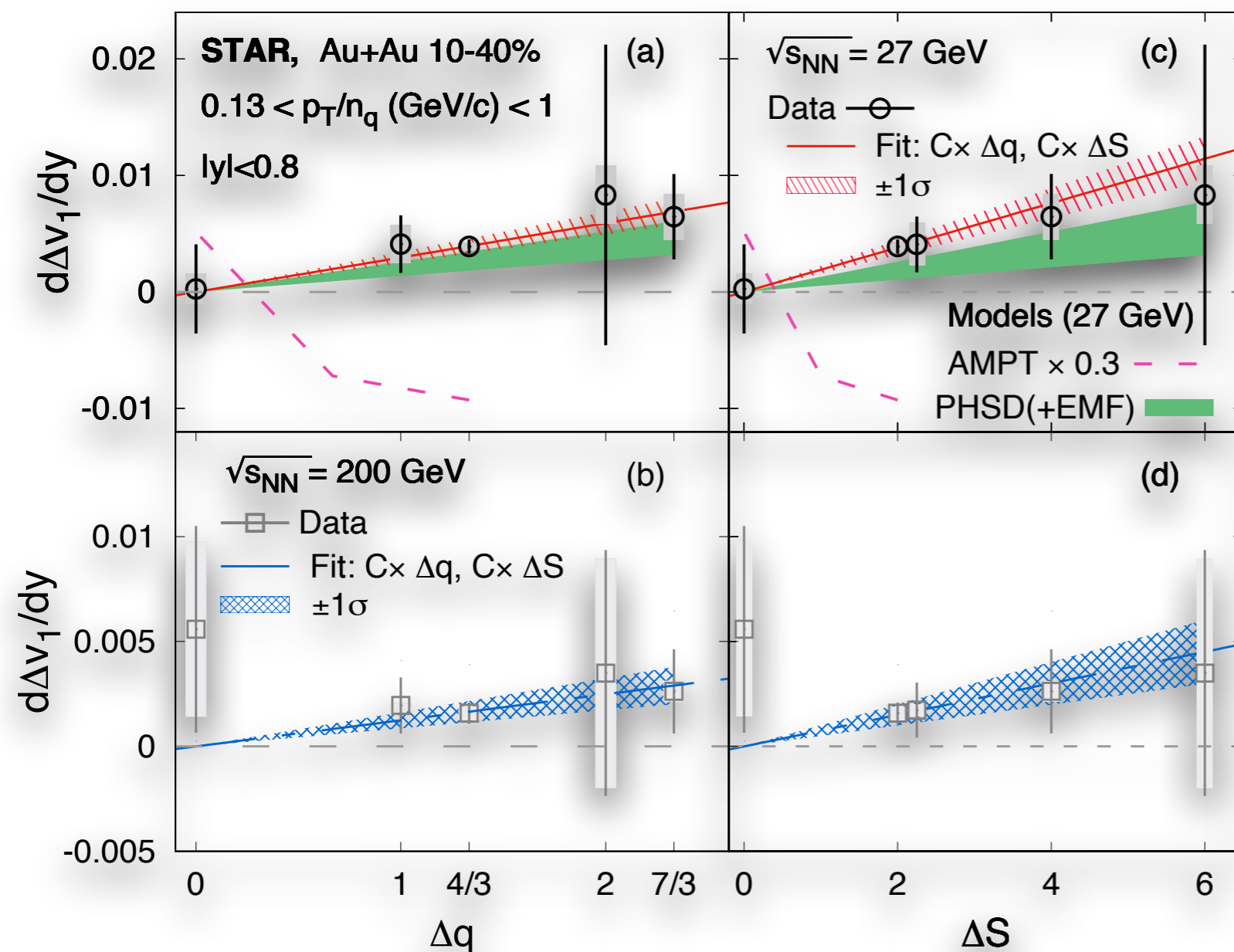


Combination of particle with similar mass but different  $\Delta q$  and  $\Delta S$

Index	Quark mass	$\Delta q$	$\Delta S$	$\Delta v_1$ combination
1	$\Delta m = 0$	0	0	$[\bar{p}(\bar{u}\bar{u}\bar{d}) + \phi(s\bar{s})] - [K^-(\bar{u}s) + \bar{\Lambda}(\bar{u}\bar{d}\bar{s})]$
2	$\Delta m \approx 0$	1	2	$[\bar{\Lambda}(\bar{u}\bar{d}\bar{s})] - [\frac{1}{3}\Omega^-(sss) + \frac{2}{3}\bar{p}(\bar{u}\bar{u}\bar{d})]$
3	$\Delta m \approx 0$	$\frac{4}{3}$	2	$[\bar{\Lambda}(\bar{u}\bar{d}\bar{s})] - [K^-(\bar{u}s) + \frac{1}{3}\bar{p}(\bar{u}\bar{u}\bar{d})]$
4	$\Delta m = 0$	2	6	$[\bar{\Omega}^+(\bar{s}\bar{s}\bar{s})] - [\Omega^-(sss)]$
5	$\Delta m \approx 0$	$\frac{7}{3}$	4	$[\bar{\Xi}^+(\bar{d}\bar{s}\bar{s})] - [K^-(\bar{u}s) + \frac{1}{3}\Omega^-(sss)]$

- Study  $\Delta v_1$  as function of charge difference ( $\Delta q$ ) and strangeness difference ( $\Delta S$ )

# Light hadron $\Delta v_1/dy$ : using only produced quarks



STAR, 2304.02831

- $\Delta v_1$  is positive
- $\Delta v_1$  increases with  $\Delta q$  and  $\Delta S$
- $\Delta v_1$  increases with decrease in beam energy

$\Delta v_1$  consistent with dominance of Hall effect over Faraday+coulomb in mid-central collisions

New Proposals:

2D fit to decompose the correlation between  $\Delta q$  and  $\Delta S$

Role of baryon transport, some cases with  $\Delta q, \Delta S \neq 0$  also have  $\Delta B \neq 0$

Nayak et al PLB 849, 138479 (2024)

Parida et al, 2305.08806

# Summary

- Background strong EM field rich in physics and interdisciplinary  
(pre-condition for CME, QCD phase transition, chiral symmetry and many more)
- Measurement of charge dependent directed flow ( $\Delta v_1$ )
  - Coulomb effect in asymmetric collisions (Cu+Au)
  - For charm hadrons (early production) Hall effect is relevant
  - For light hadrons: dominance of Faraday and coulomb in peripheral collisions

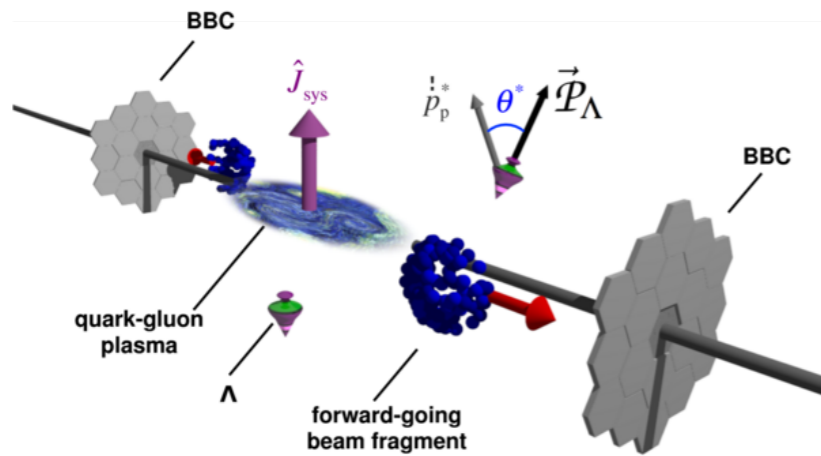
Imprints of electromagnetic field effects observed in HIC

  - Constrain strength and lifetime of EM-field
  - Provide knowledge of electrical conductivity of the QGP medium
  - Provide information on transport mechanism

- More theory input is needed to understand system-size and energy dependence of  $\Delta v_1$



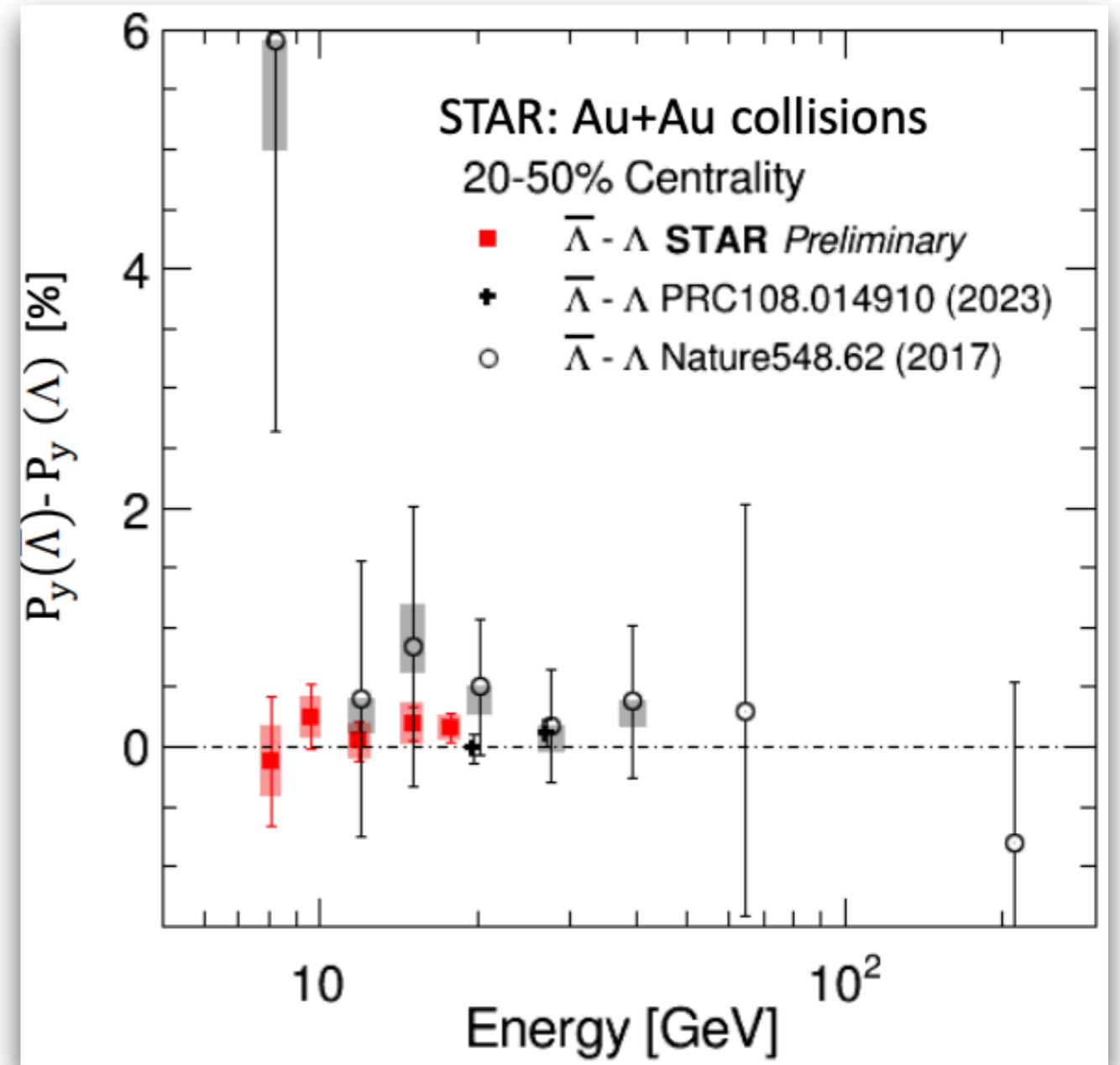
# Outlook-I: Polarization difference $P_{\Lambda} - P_{\bar{\Lambda}}$



Global spin polarization:

$$P_H = \frac{8}{\pi\alpha_H} \frac{\langle \sin(\Psi_1 - \phi_d^*) \rangle}{\text{Res}(\Psi_1)}$$

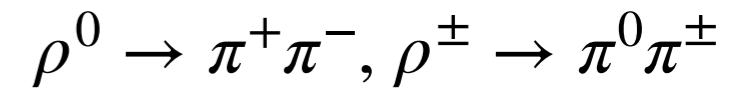
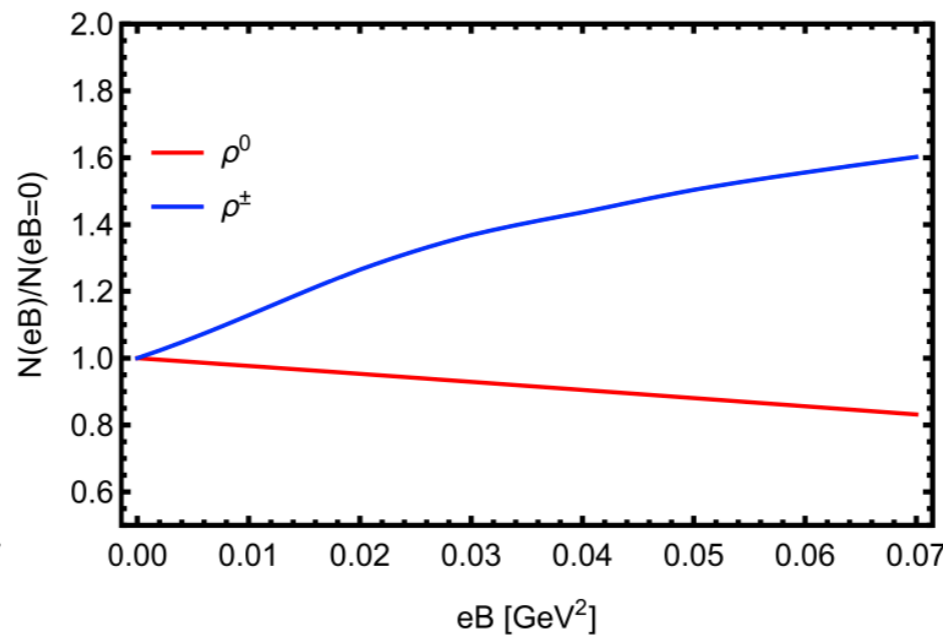
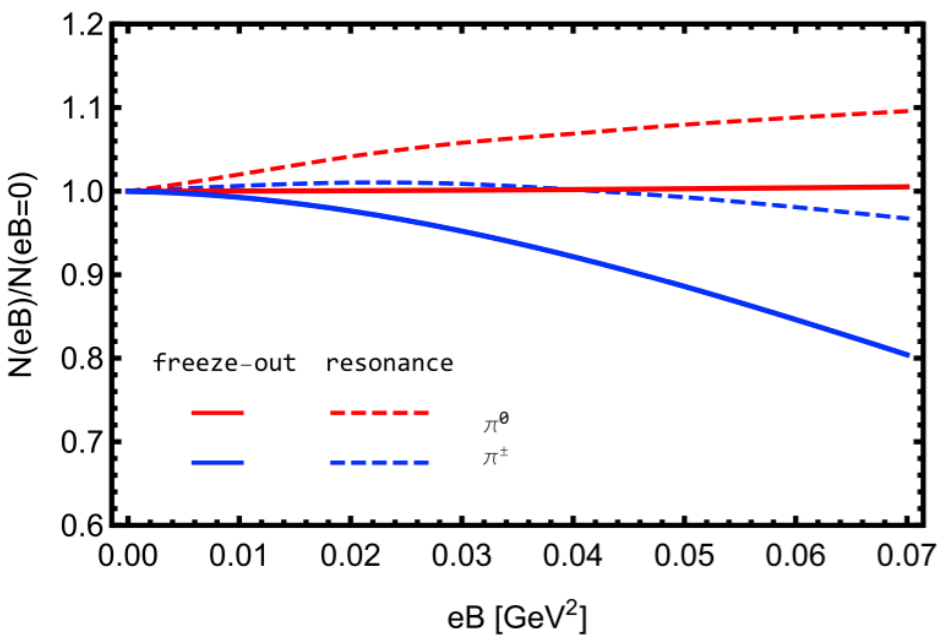
$$P_{\Lambda} - P_{\bar{\Lambda}} = 2 \frac{\mu_{\Lambda} B}{T}$$



From precise BES-II data:

- Upper limit on late-stage B-field:
- $B < 9.4 \times 10^{12}$  T at 19.6 GeV and  $B < 1.4 \times 10^{13}$  T at 19.6 GeV
- Polarization of hyperons with different magnetic moments ( $\Lambda$ ,  $\Xi$ ,  $\Omega$ )

# Outlook-II: Neutral and charged vector mesons

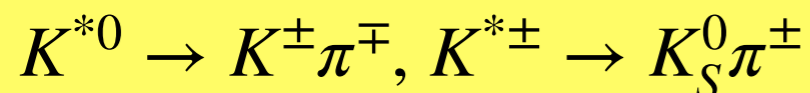


*Kun et al, PLB 809, 135706 (2020)*

- Under B-field, one expect  $N_{\rho^\pm} > N_{\rho^0}$  from **Landau level splitting** (isospin violation)

$$\epsilon_{n,s_z}^2(p_z) = p_z^2 + (2n - 2 \text{sign}(q)s_z + 1) |qB| + m^2$$

- $K^{*\pm}, K^{*0} \rightarrow$  easier reconstruction, negligible feed down effect
- Yield and ratios ( $K^{*\pm}/K^{*0}$ ) can be useful in late-stage B-field and possibility of many associated phenomenon (landau splitting, vector meson condensation ....)



$$K^{*0}(d\bar{s}) : \mu_d \approx -0.97, \mu_{\bar{s}} \approx 0.61\mu_N$$

$$K^{*+}(u\bar{s}) : \mu_d \approx 1.85, \mu_{\bar{s}} \approx 0.61\mu_N$$

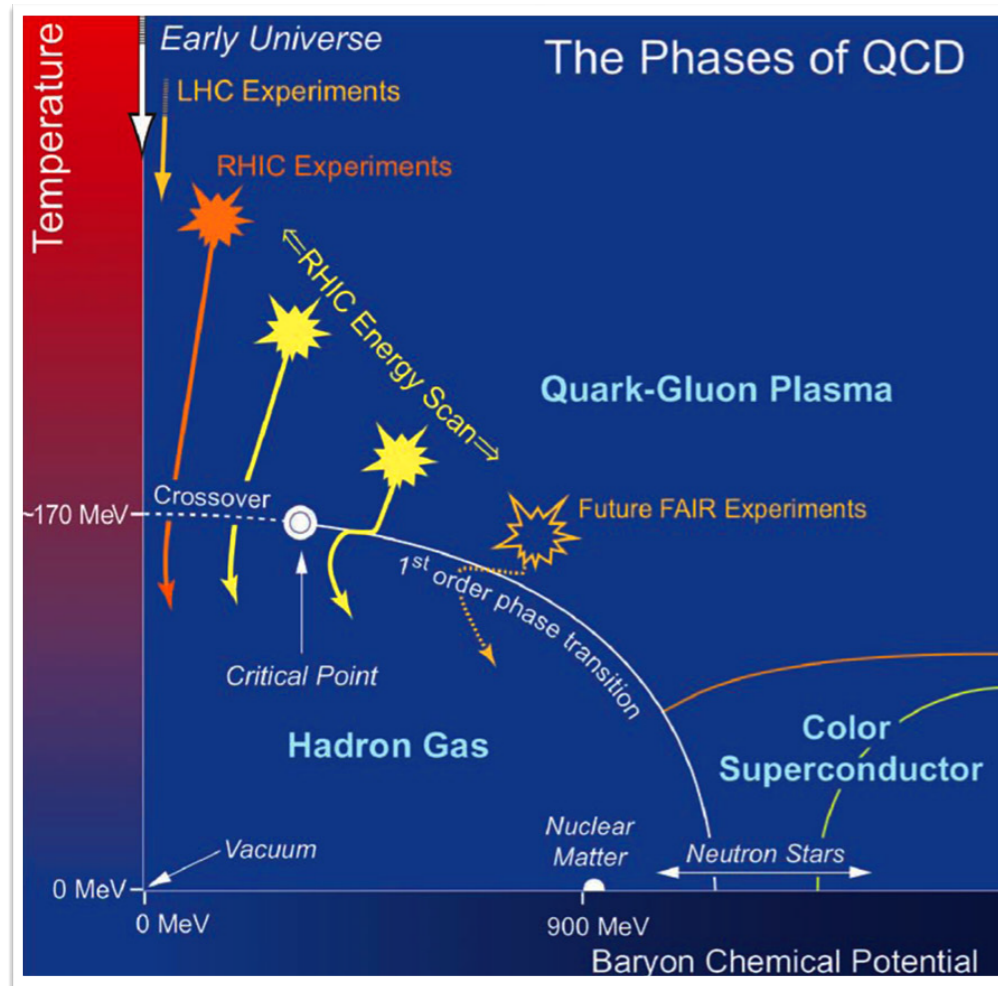
*Stay tuned till upcoming Quark Matter*

Thank you for your attention

Many thanks to STAR colleagues for discussion

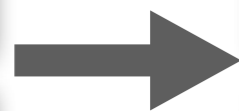
# QCD phase diagram and RHIC Beam Energy Scan

## Conjectured QCD Phase diagram



Partonic  
dominant

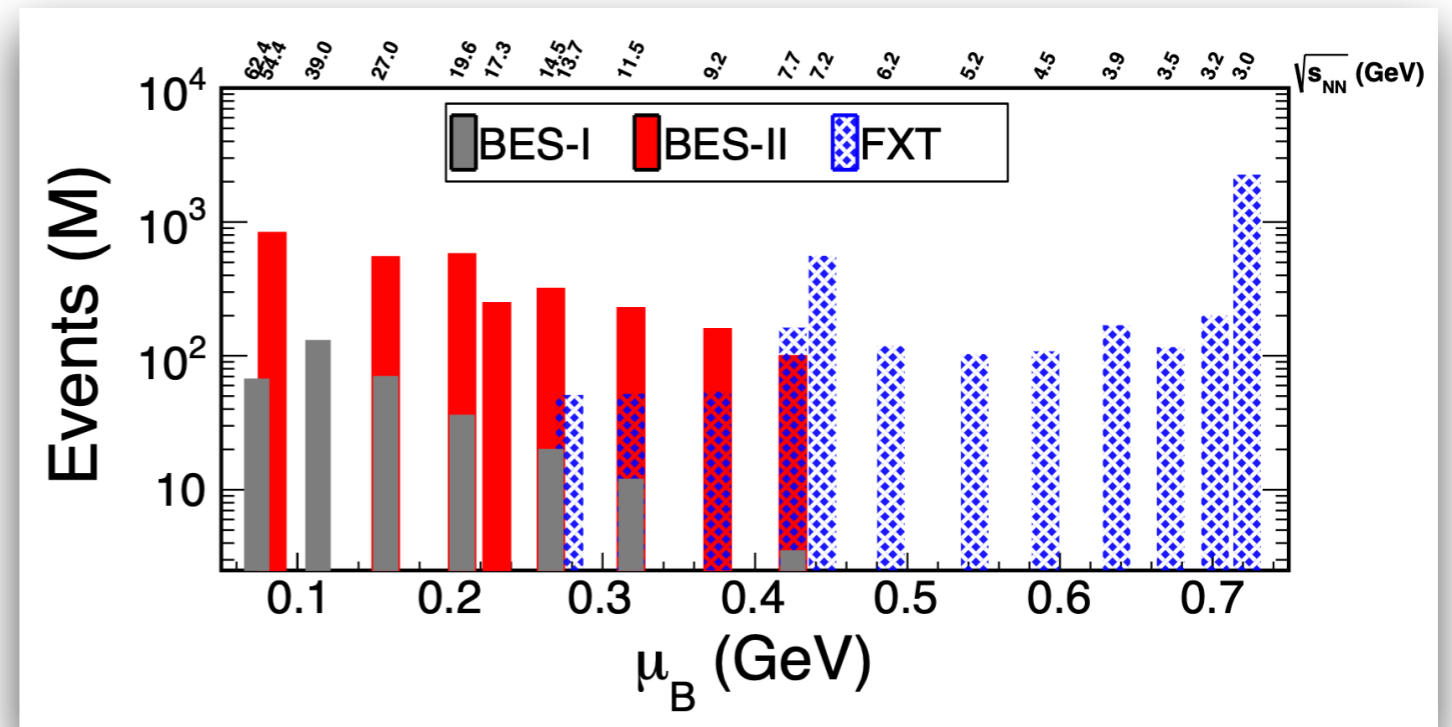
Meson  
dominant



Hadronic  
dominant

Baryon  
dominant

## BES Program:



Collider: 7.7, 9.2, 11.5, 14.6, 17.3, 19.6, 27, 39, 54.4, 62.4, 200 (GeV)

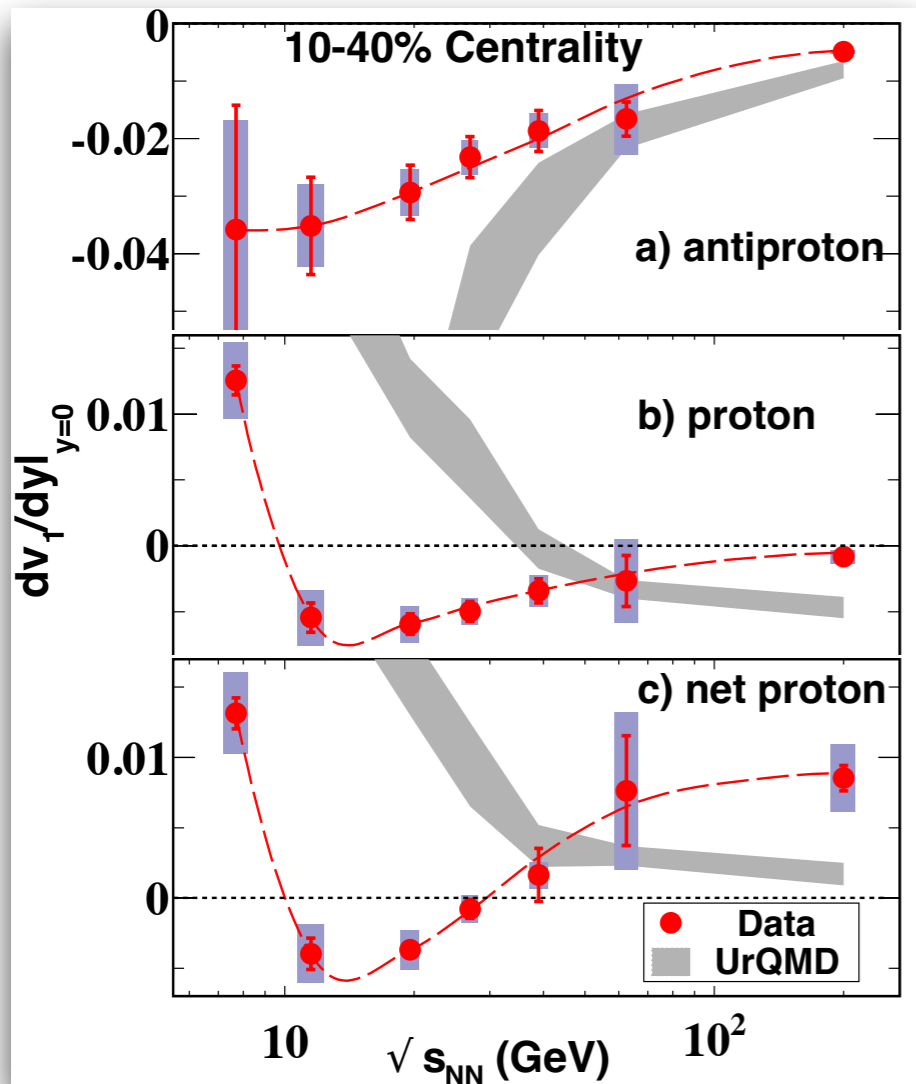
Fixed Target: 3.0, 3.2, 3.5, 3.9, 4.5, 5.2, 6.2, 7.2, 7.7, 9.2, 11.5, 13.7 (GeV)

most precise data to map the QCD phase diagram

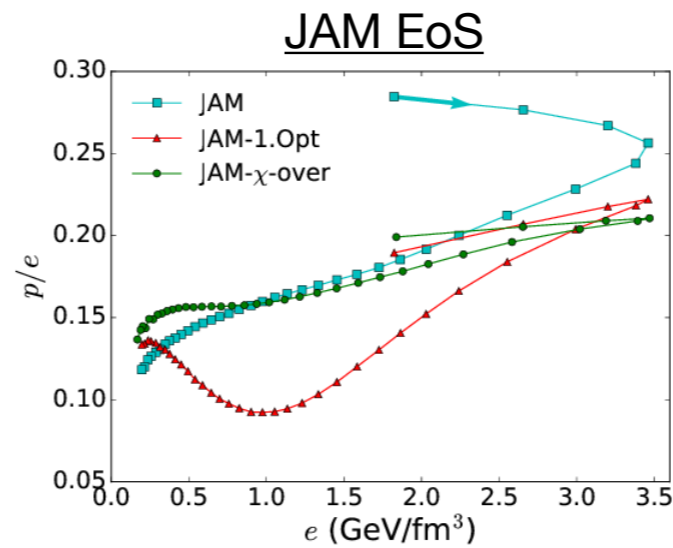
- Find signatures of Phase Transition
- QCD Critical point
- Turn-off of QGP signatures

# Directed flow from BES-I

**BES-I** STAR: PRL 112, 162301 (2014)

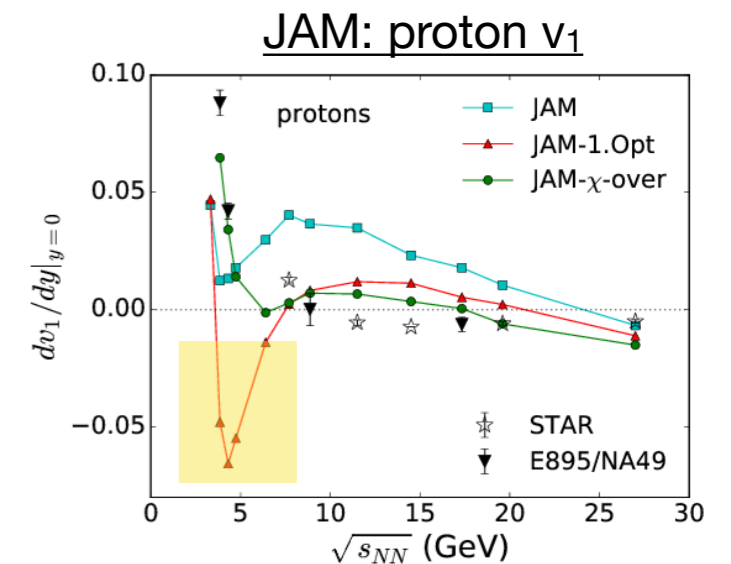


## Model



At 1<sup>st</sup> order phase transition, pressure drops as speed of sound goes to zero

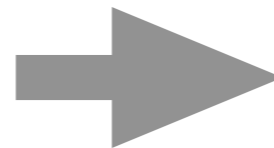
Y. Nara et al, PLB 769, 543-548 (2017)



## Primary observations

Around 10-20 GeV:

- proton  $v_1$  changes sign
- net-proton  $v_1$  change sign twice with a minima



Features qualitatively resemble the model prediction with 1<sup>st</sup> order phase transition