



Higgs mass, cross sections, CP, self-coupling

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On behalf of the FCC Higgs/Top performance working group

FCC Physics Workshop 2025, CERN, Jan. 14, 2025



Outline

- ❖ Introduction
- ❖ Higgs mass
- ❖ ZH cross-section
- ❖ CP
- ❖ Self-coupling
- ❖ Conclusion

Higgs: Introduction



15 years operation



~ 25 years operation

FCC-ee

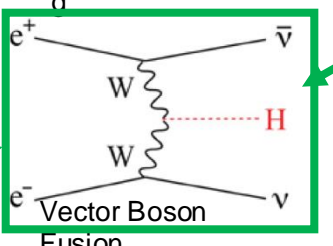
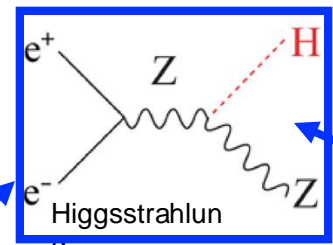
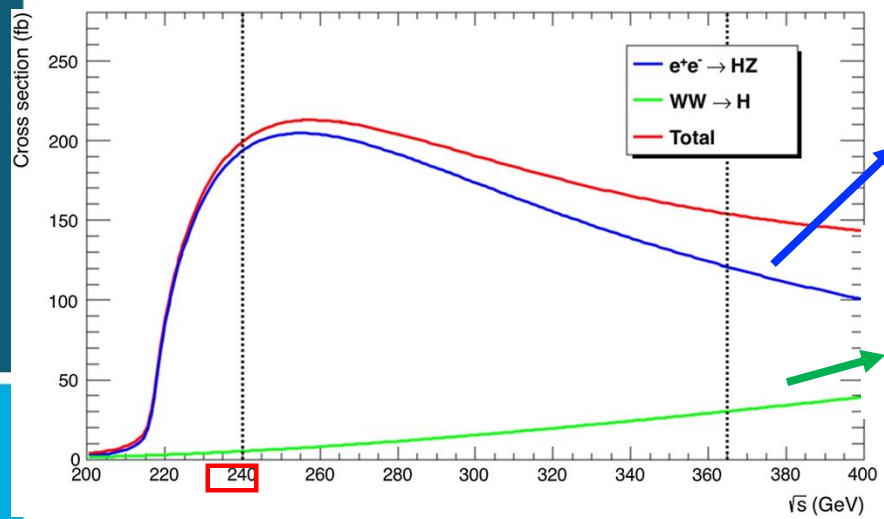
FCC-hh

Baseline:

Working point	Z, years 1-2	Z, later	WW, years 1-2	WW, later
\sqrt{s} (GeV)	88, 91, 94		157, 163	
Lumi/IP ($10^{34} \text{ cm}^{-2} \text{ s}^{-1}$)	70	140	10	20
Lumi/year (ab^{-1})	34	68	4.8	9.6
Run time (year)	2	2	2	0
Number of events	$6 \cdot 10^{12}$ Z		$2.4 \cdot 10^8$ WW	

ZH	tt	
240	340-350	365
5.0	0.75	1.20
2.4	0.36	0.58
3	1	4
$1.45 \cdot 10^6$ HZ + 45k WW \rightarrow H	$1.9 \cdot 10^6$ tt +330k HZ +80k WW \rightarrow H	

Main energy point for Higgs studies



Main Production Mechanisms at 240 and 365 GeV

- ZH production "Higgs-strahlung"
- Vector Boson Fusion (VBF): WW dominant

Optional run at 125 GeV s-channel

$$e^+ e^- \rightarrow H$$

- Direct Probe of electron-Yukawa coupling
- Requires beam monochromatization

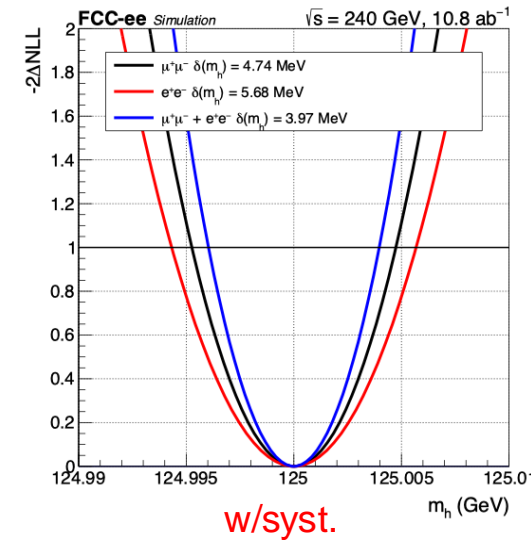
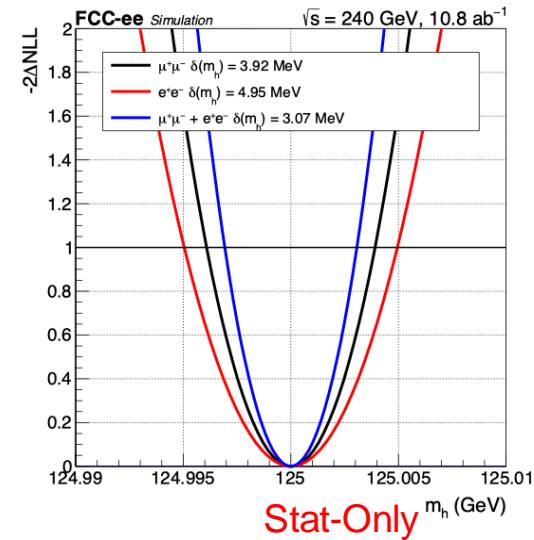
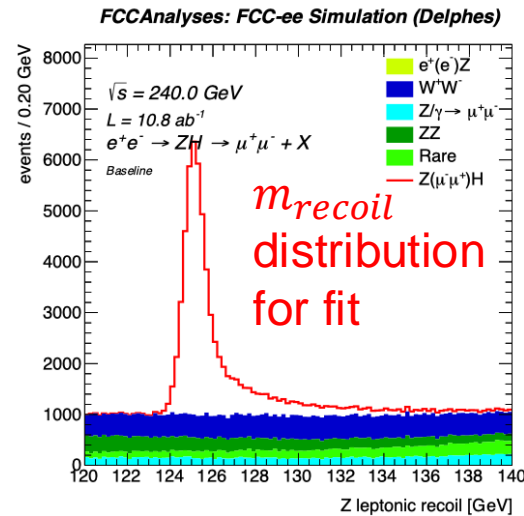
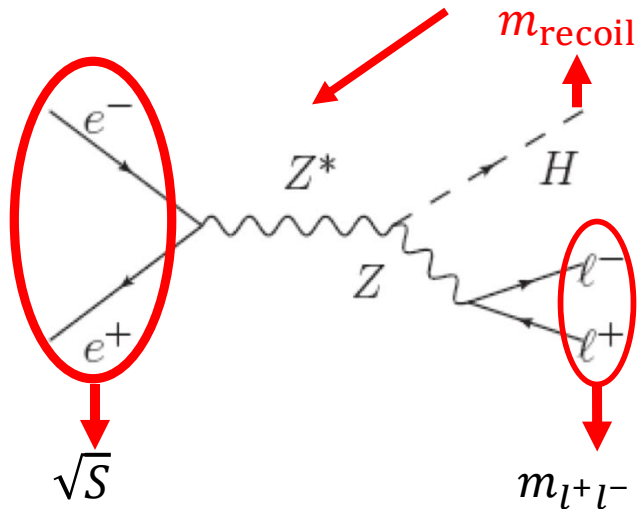
Higgs mass

$\sqrt{s} = 240 \text{ GeV}$
 $L = 10.8 \text{ ab}^{-1}$

Gregorio Bernardi
 Jan Eysermans
 Ang Li
 DOI [10.17181](https://doi.org/10.17181)

- ❖ Current best from LHC $\delta m_H \sim 100 \text{ MeV}$
- ❖ At FCC-ee, Higgs mass will reach **MeV level** accuracy, ($\Gamma_H \sim 4.1 \text{ MeV}$)
- ❖ Electron and Muons final states: $e^+e^- \rightarrow ZH \rightarrow l^+l^- + XX$, ($Z \rightarrow \mu^+\mu^-, e^+e^-$)
- ❖ M_{recoil} from the Z production without measuring the Higgs production final state

$$m_{recoil}^2 = (\sqrt{s} - E_{l\bar{l}})^2 - p_{l\bar{l}}^2 = s - 2E_{l\bar{l}}\sqrt{s} + m_{l\bar{l}}^2$$



Higgs mass, Fit with analytic shape

- Signal Shape: 2 Crystal-Ball with Gaussian core
- Backgrounds modelled as polynomial (3rd order)
- Signal and background injected in Combine, m_H as POI

Uncertainty Stat-Only, and w/ systematics:

➤ Higgs mass: **3.07 MeV → 3.97 MeV**

Dominant Syst. Unc. :

Centre-of-mass with ~ 2 MeV

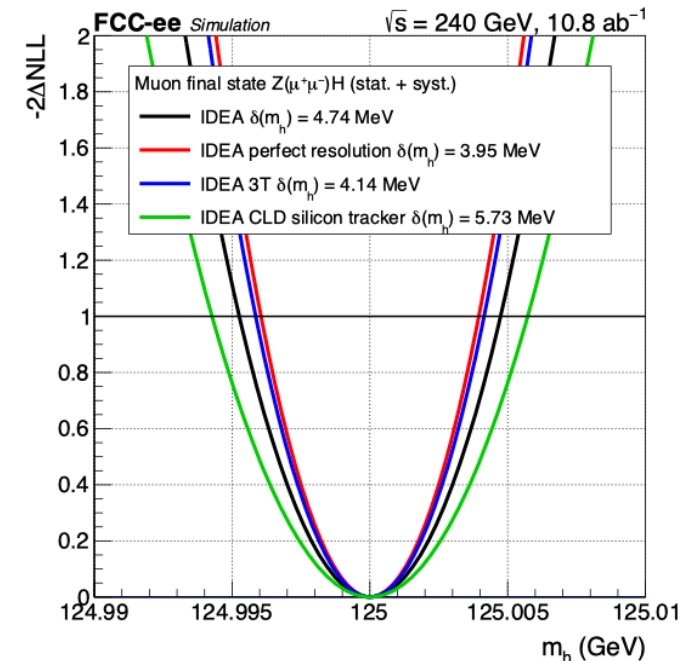
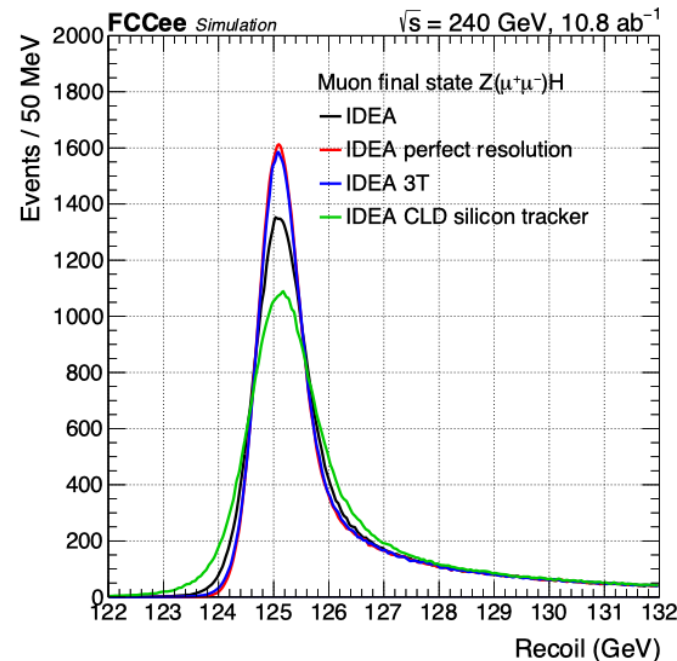
Higgs mass

Some extended studies performed regarding detector effects

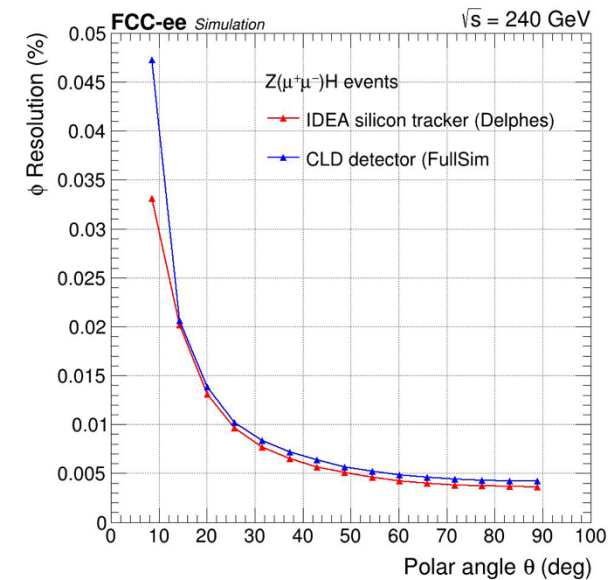
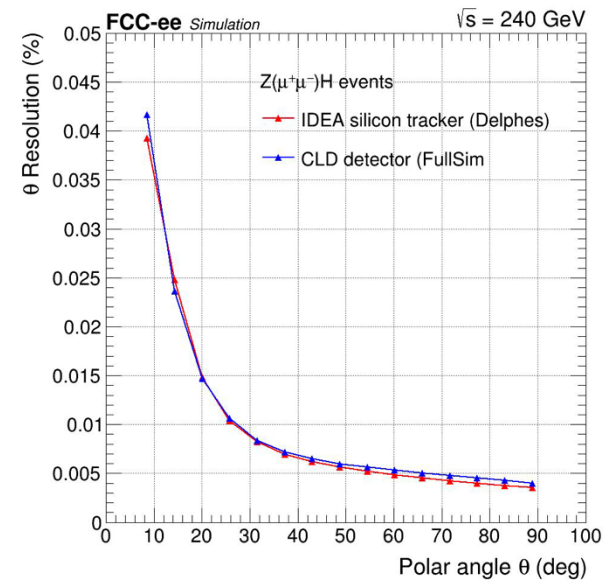
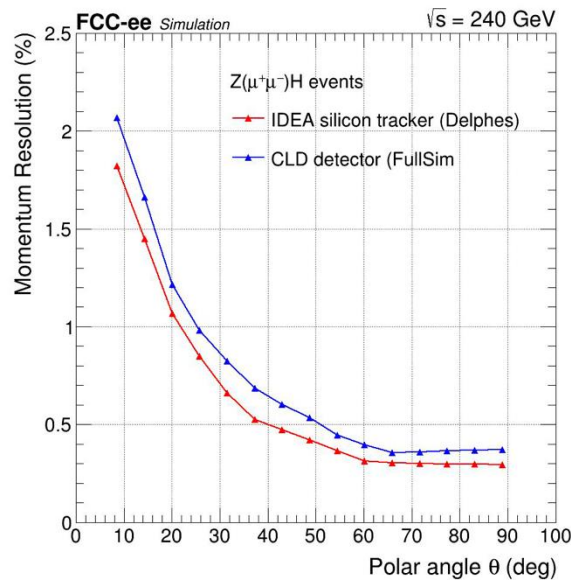
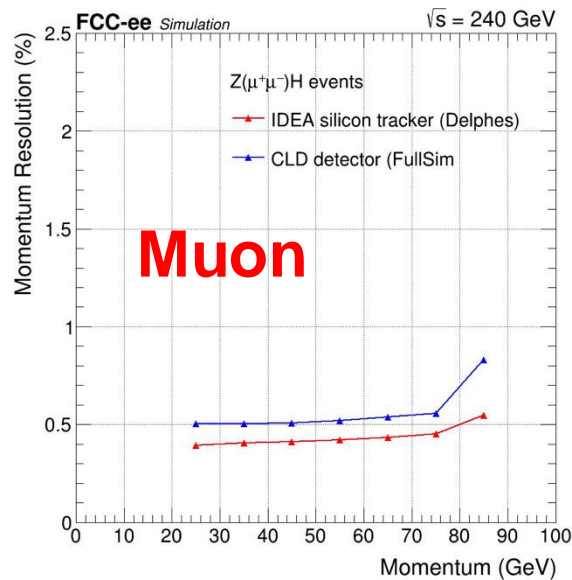
- Assuming “perfect” (generator-level) momentum resolution
- Nominal 2 T magnetic field → 3 T (stronger field → better tracking)
- IDEA drift chamber → CLD silicon tracker

	Combined
Nominal	3.07 (3.97)
Ideal resolution	2.42 (3.40)
Magnetic Field 3T	2.54 (3.52)
CLD 2T (silicon tracker)	3.86 (4.55)

Feedbacks to the Detector Design from Analysis

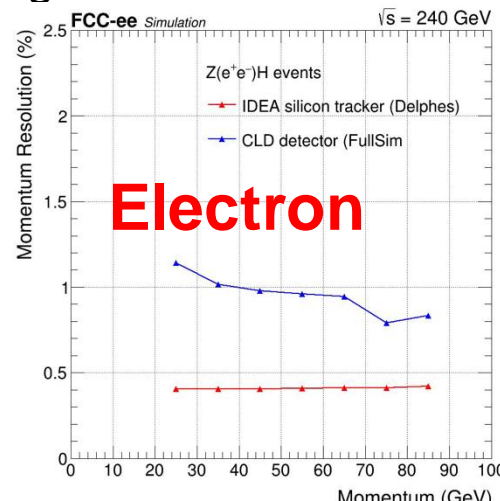


FullSim: Momentum and Angular resolution



➤ Muon resolutions based on $Z(\mu\mu)H$ events

- Slightly worse momentum in FullSim (residual difference in material budget, smearing)
- Angular resolutions OK



Electron resolutions based on $Z(ee)H$ events

- Visibly worse momentum in FullSim
- No Bremsstrahlung recovery in CLD reconstruction
Some work already done
Emmanuel/Michele: Detector requirements for ECAL ([Link](#))
BNL attempt for MVA-based brem recovery ([Link](#))

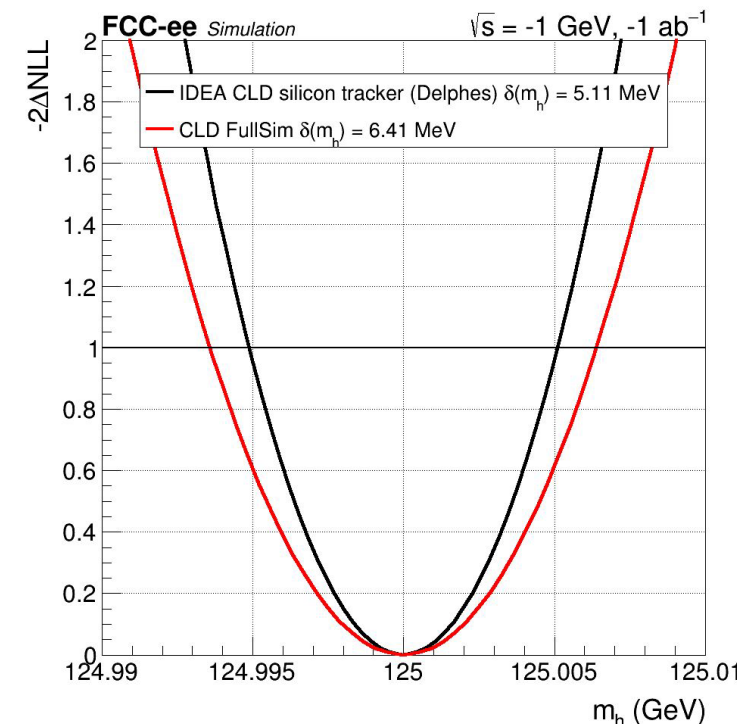
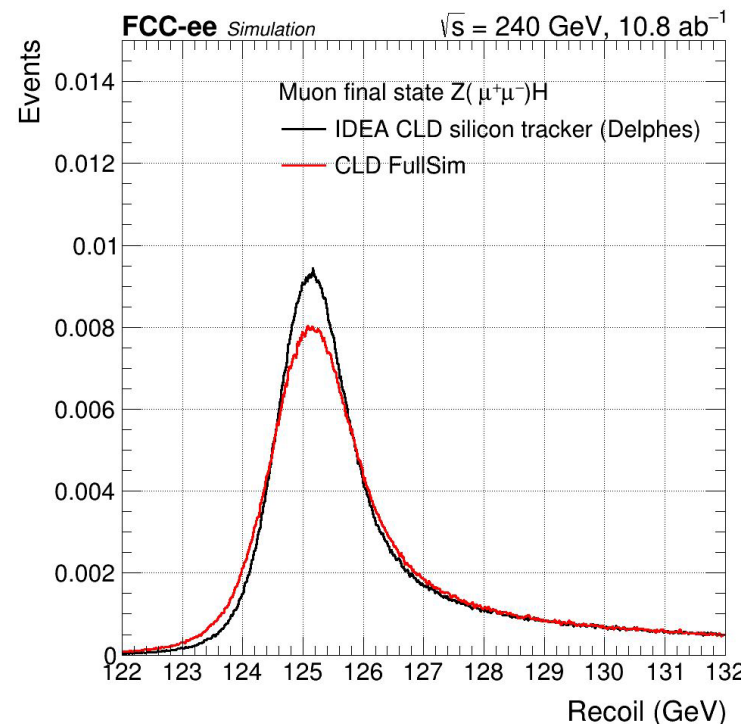
Higgs mass with Full Sim (Muon)

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- FullSim recoil distribution slightly worse than Delphes
- Repeat the fit producer as for the Delphes analysis
 - Fit recoil distributions with Crystal Ball and Gauss
 - Statistical-only fit, no systematics

	Uncertainty
Delphes	5.11 MeV
FullSim	6.41 MeV

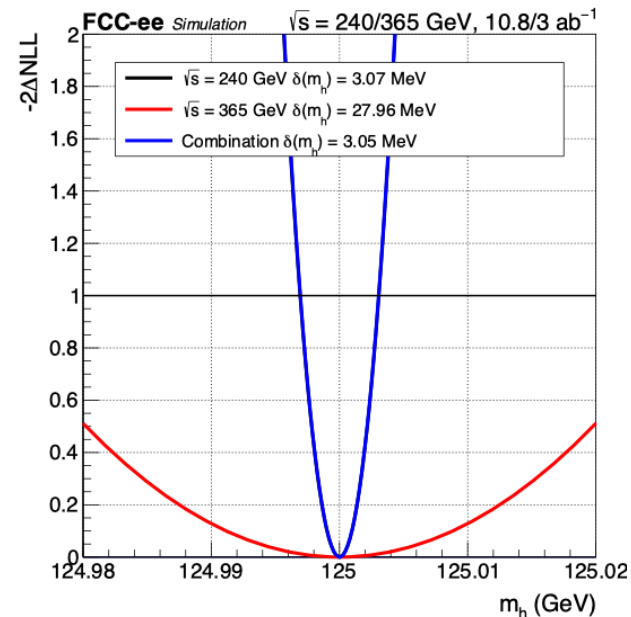
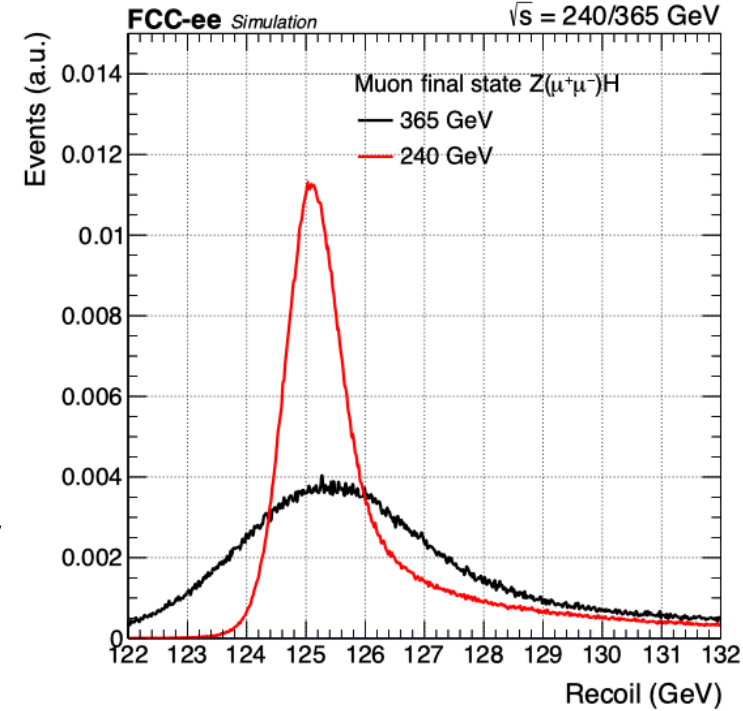
- FullSim is 25% worse than Delphes



Higgs mass at 365 GeV

❖ At $\sqrt{s} = 365$ GeV

- Reduced statistics
- Broadened recoil distribution
- 365 GeV only: 27.96(28.79) MeV uncertainty on Higgs mass on Electron (Muon) channel
- Combined with 240 GeV brings it down from **3.07** MeV **3.05** MeV (Stat-Only) **~1%** improvement



Total ZH production cross-section

Measure the ZH cross-section in a **Model-Independent** way

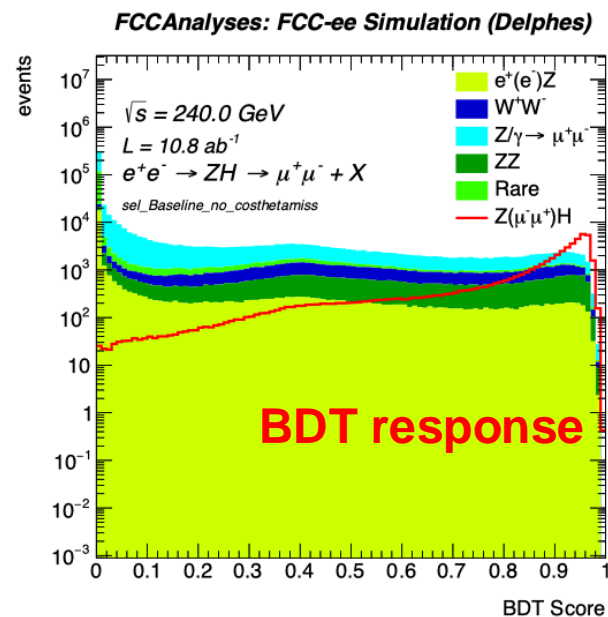
- Unique to electron-positron colliders because of known initial state
- Challenge to ensure **model-independent**
- Once know, determine couplings to $H \rightarrow XX$ in a model independent way

$$\sigma_{ZH} \times Br(H \rightarrow X\bar{X}) \propto \frac{g_{HZZ}^2 \times g_{HXX}^2}{\Gamma_H}$$

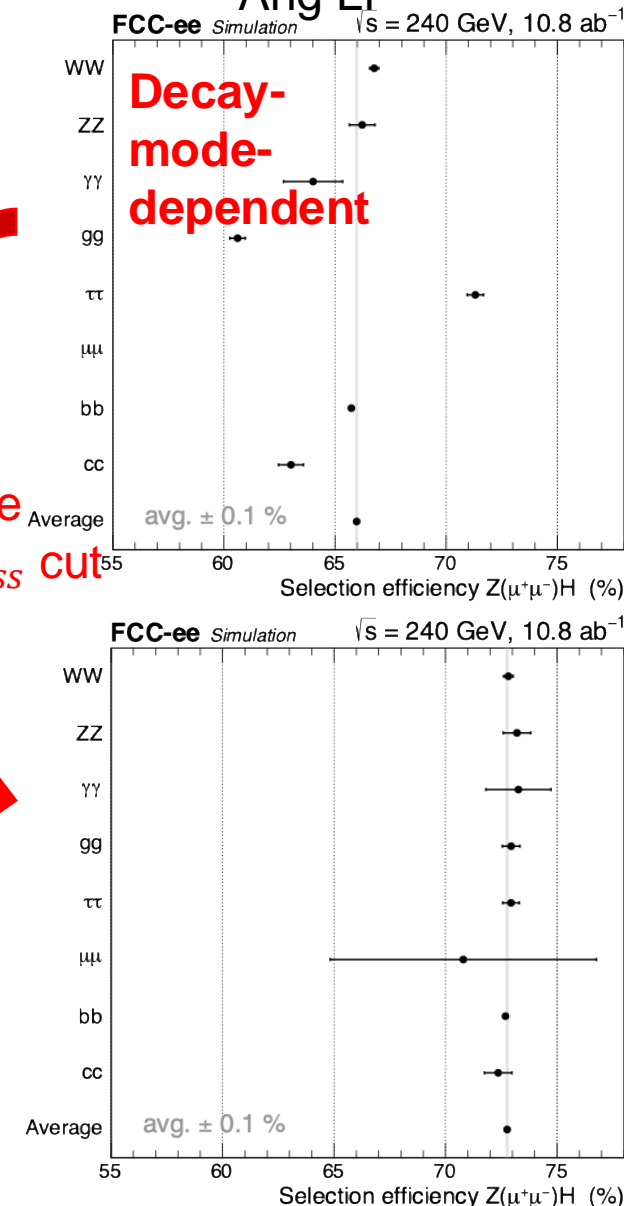
At FCC-ee ZH cross-section is expected to ~0.5 % accuracy

- $e^+e^- \rightarrow ZH \rightarrow l^+l^- + XX, (Z \rightarrow \mu^+\mu^-, e^+e^-)$

- Remove Decay-Mode dependent event selection $\rightarrow \cos \theta_{miss}$
- Introduce BDT approach to keep decay-mode independency
- Fit BDT distribution

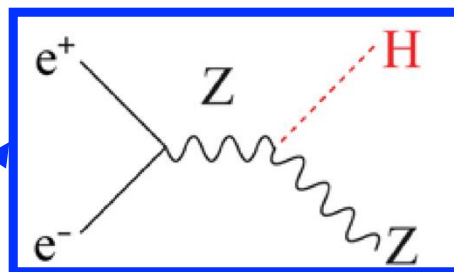
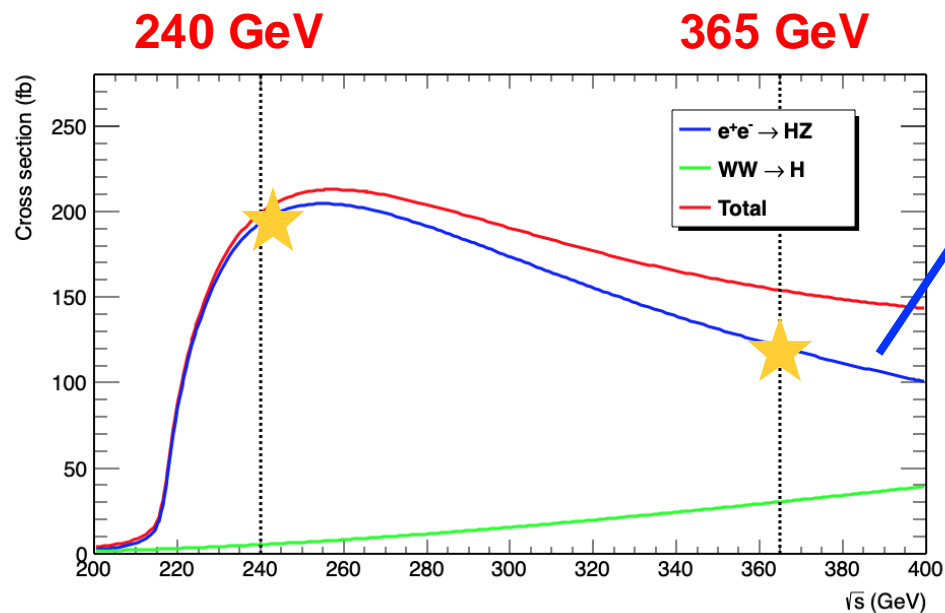


Remove $\cos \theta_{miss}$ cut

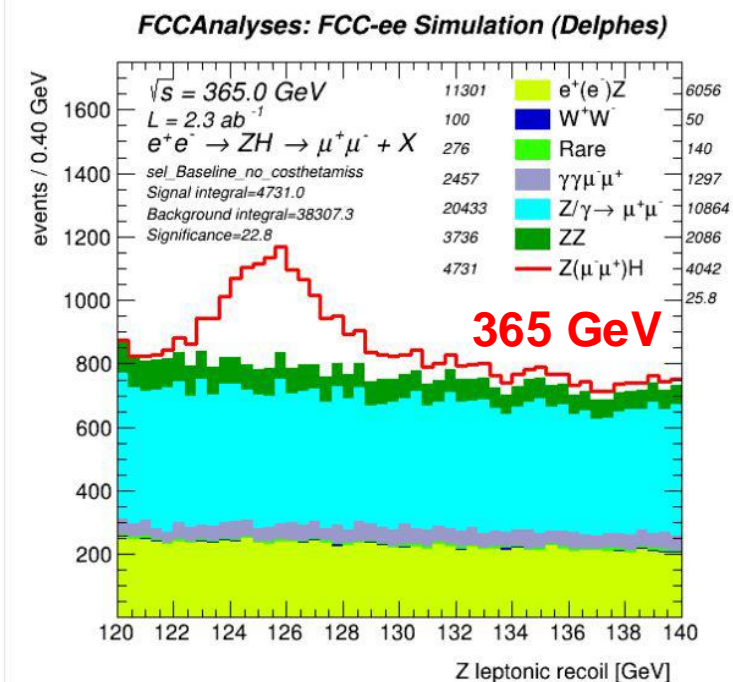
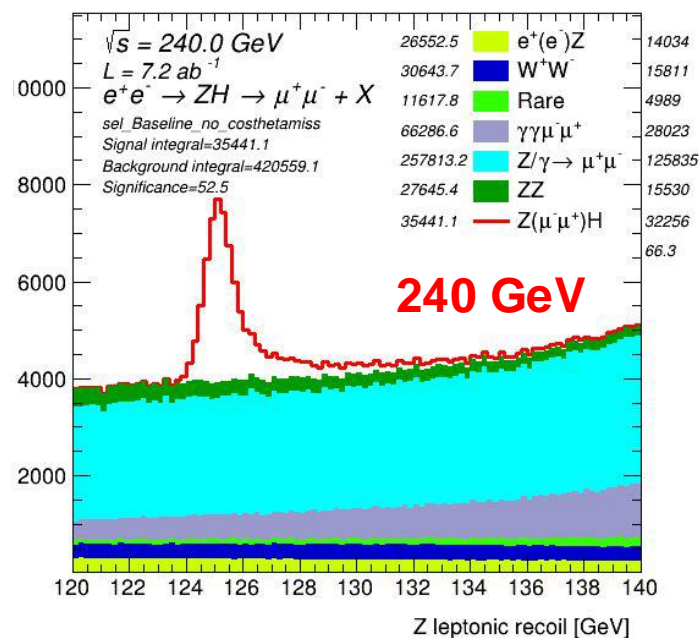


Total ZH production cross-section

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FCCAnalyses: FCC-ee Simulation (Delphes)

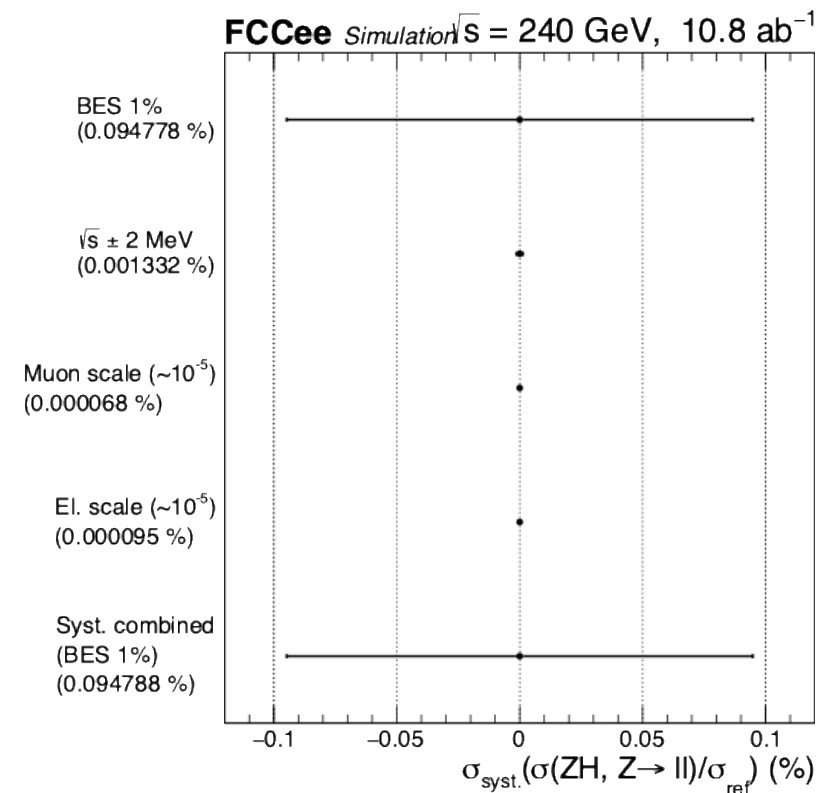
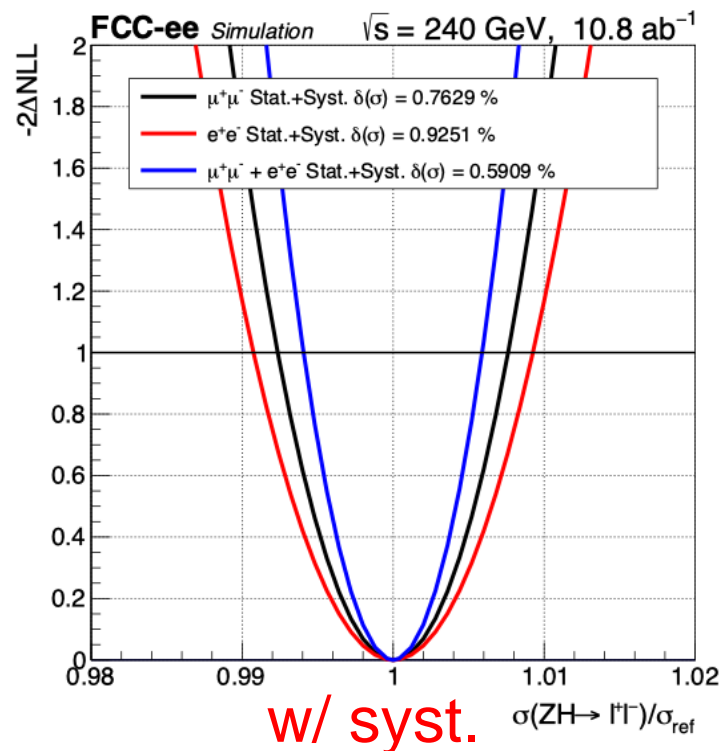
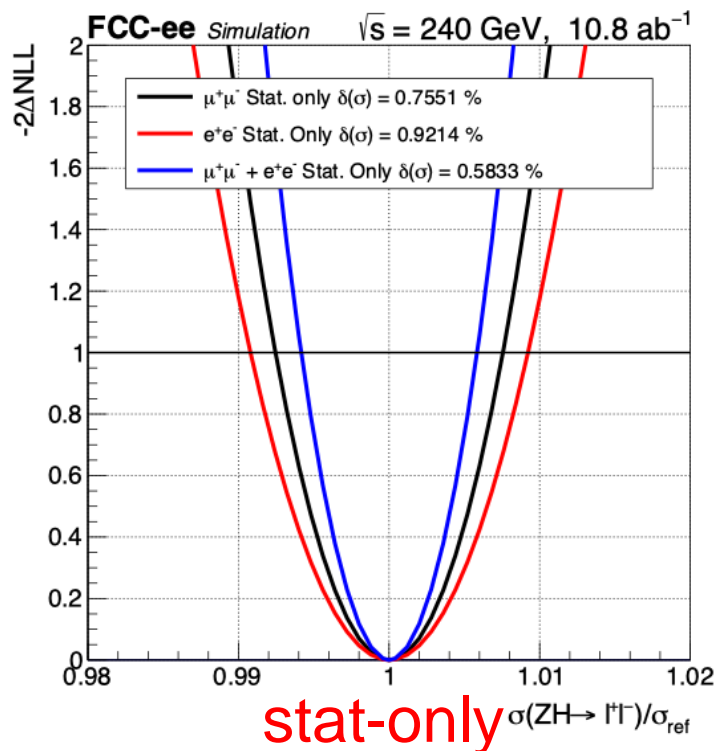


365 GeV has

- Worse resolution
- But Negligible WW background

ZH cross-section @ $\sqrt{s} = 240$ GeV

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DOI [10.17181](https://doi.org/10.17181)



➤ Likelihood scan to extract ZH cross-section uncertainty

- Muon channel 0.76%
- Electron channel 0.92%

➤ Combined uncertainty 0.58% (stat. only)

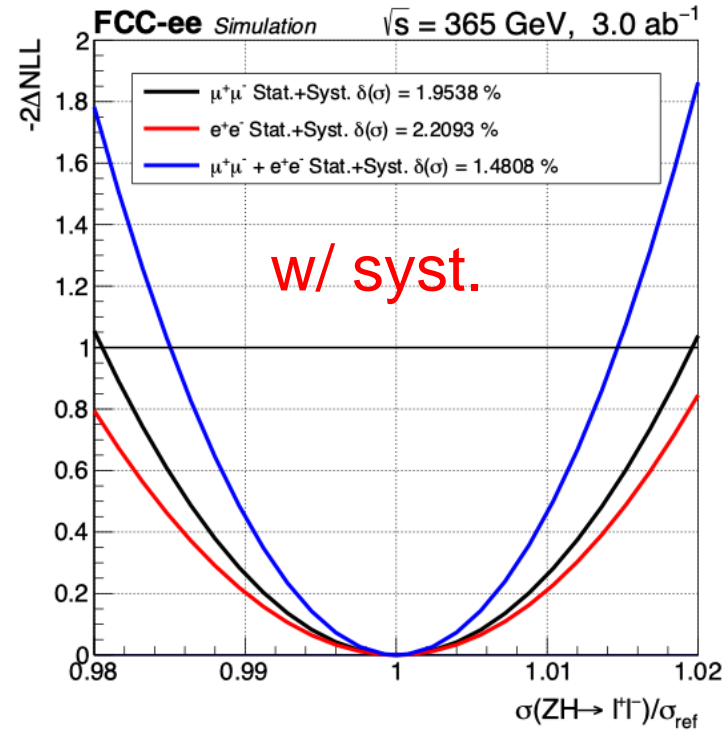
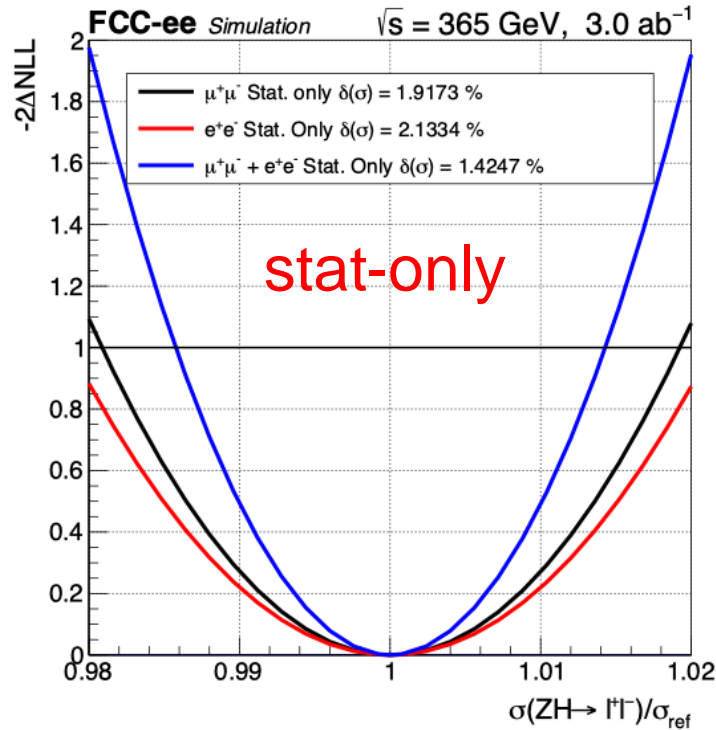
- Sensitivity driven by muon channel; electrons gain $\sim 24\%$

➤ Systematics are negligible (0.58% \rightarrow 0.59%)

- Leading Systematic is BES

ZH cross-section @ $\sqrt{s} = 365$ GeV

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$\delta\sigma_{ZH}/\sigma_{ZH}$	stat-only	w/ syst.
$\sqrt{s} = 240$ GeV, 10.8 ab^{-1}	0.58%	0.59%
$\sqrt{s} = 365$ GeV, 3.0 ab^{-1}	1.42%	1.48%

Higgs CP studies

$\sqrt{s} = 240 \text{ GeV}$
 $L = 7.2 \text{ ab}^{-1}$

Jan Eysermans,
 Andrei Gritsan,
 Lucas Mandacaru Guerra,
 Nicholas Pinto,
 Valdis Slokenbergs

❖ Include $H \rightarrow X$,

- $Z \rightarrow ee, \mu\mu$
- $Z \rightarrow qq$ (uu, dd, ss, cc) and
- $Z \rightarrow bb$

$$f_{CP}^{HX} \equiv \frac{\Gamma_{H \rightarrow X}^{CP \text{ odd}}}{\Gamma_{H \rightarrow X}^{CP \text{ odd}} + \Gamma_{H \rightarrow X}^{CP \text{ even}}}$$

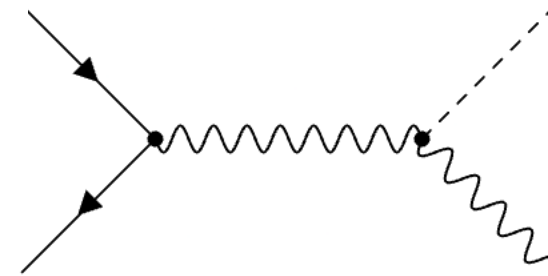
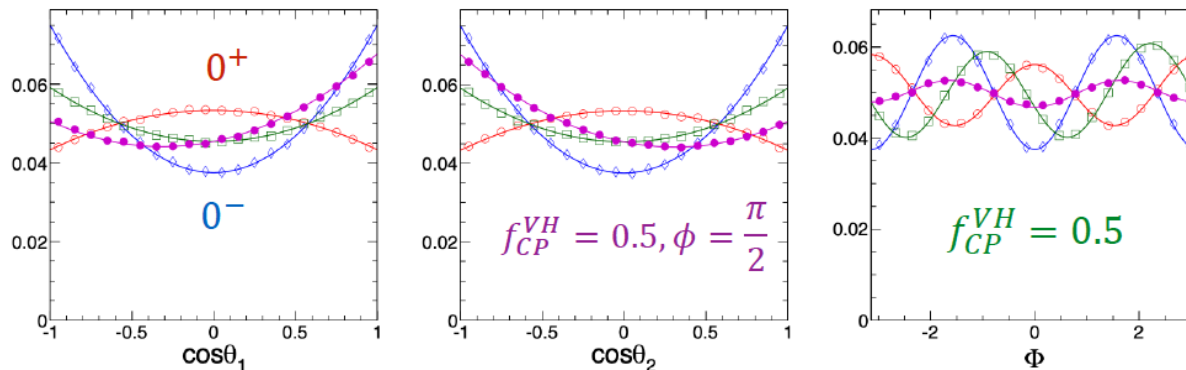
❖ Optimal observables in leptonic final state

$$D_{0^-} = \frac{P(0^-)}{P(0^+) + P(0^-)}$$

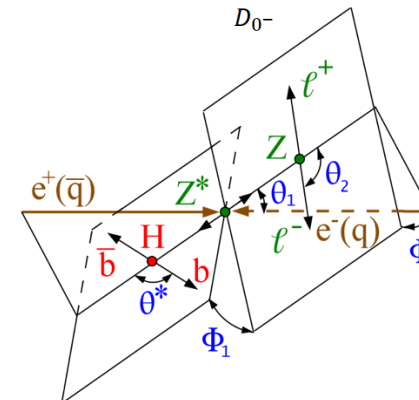
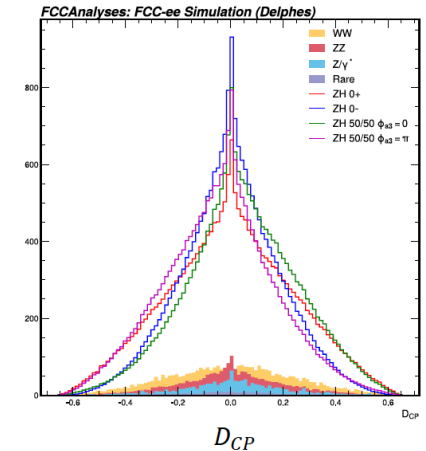
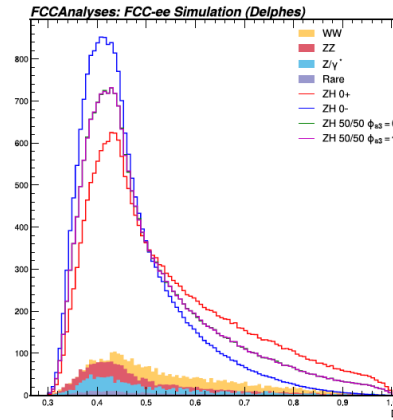
$$D_{CP} = \frac{P(int)}{2\sqrt{P(0^+) * P(0^-)}}$$

- D_{0^-} : Separate CP-even distribution from CP-odd.
- D_{CP} : Separate two equal mixtures of CP-even and CP-odd with different phases of the CP-odd coupling.

❖ $\cos\theta_1, \cos\theta_2$ and ϕ in hadronic final states



[Link](#)



[1309.4819](#)

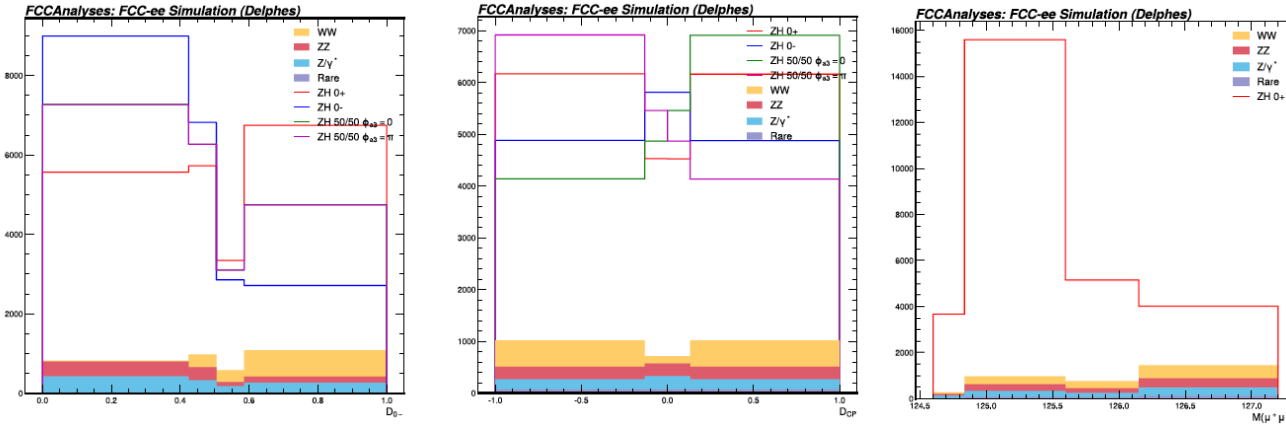
Higgs CP studies

❖ Lepton channel:

Fit on 3D Histogram formed from D_{0-} , D_{CP} and M_{recoil}

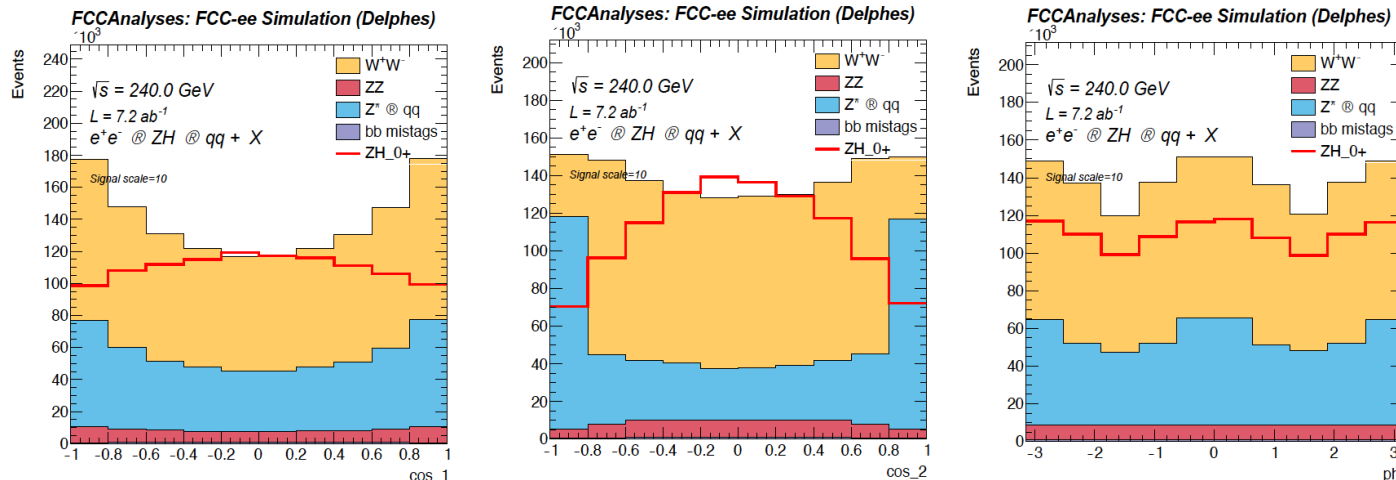
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Lucas Mandacaru Guerra,
Nicholas Pinto,
Valdis Slokenbergs

[Link](#)



❖ Hadronic channel:

Fit on $\cos\theta_1$, $\cos\theta_2$ and ϕ

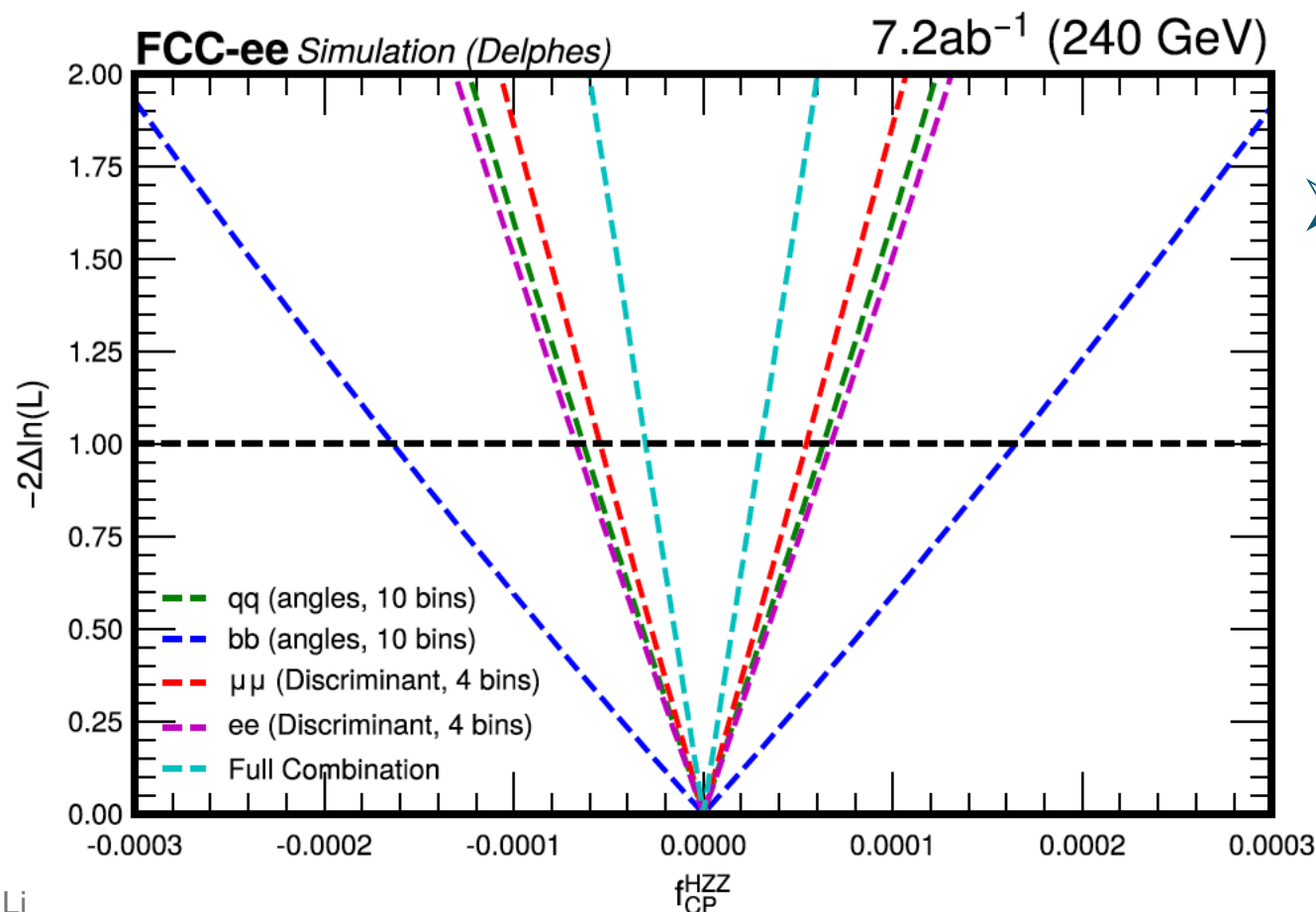


Higgs CP studies

Jan Eysermans,
Andrei Gritsan,
Lucas Mandacaru Guerra,
Nicholas Pinto,
Valdis Slokenbergs

[Link](#)

- Fits with Reconstructed Signal,
 $Z \rightarrow qq, bb, ee, \mu\mu$:



$$f_{CP}^{HX} \equiv \frac{\Gamma_{H \rightarrow X}^{CP \text{ odd}}}{\Gamma_{H \rightarrow X}^{CP \text{ odd}} + \Gamma_{H \rightarrow X}^{CP \text{ even}}}$$

- f_{CP}^{HZZ} at 68% Confidence Level

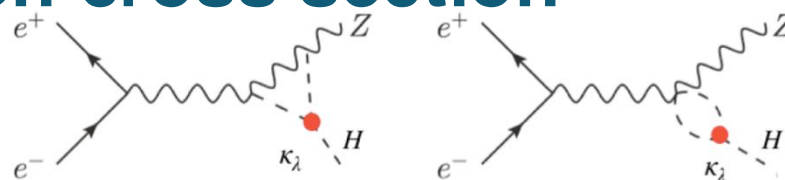
- $qq \sim \pm 6.3 \times 10^{-5}$
- $bb \sim \pm 1.6 \times 10^{-5}$
- $\mu\mu \sim \pm 5.5 \times 10^{-5}$
- $ee \sim \pm 6.7 \times 10^{-5}$
- Combined $\sim \pm 3.0 \times 10^{-5}$

- Combined result represents
~79% of Z decays

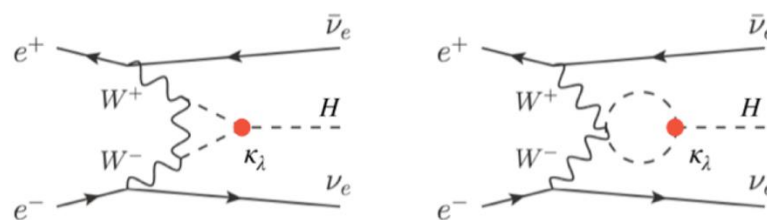
Self-coupling

Probe trilinear Higgs self-coupling λ_3 (λ_{HHH}) through **single Higgs** boson cross section

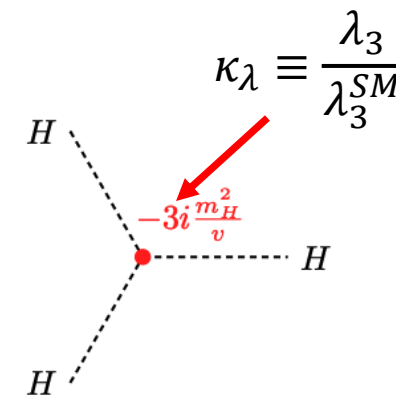
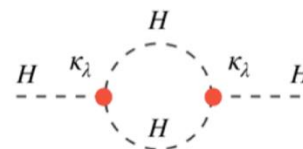
□ Higgs-strahlung: $e^+e^- \rightarrow ZH$



□ WW-fusion: $e^+e^- \rightarrow \nu\bar{\nu}H$



□ Higgs self-energy



$$\Sigma_{NLO} = Z_H \Sigma_{LO} (1 + \kappa_\lambda C_1)$$

NLO ZH cross-section

LO ZH cross-section

Higgs self-coupling can be measured through the NLO variations on the total ZH cross-section thanks to sufficient statistics

Self-coupling

Elizabeth Brost,
Robert Szafron,
Abraham Tishelman-Charny
DOI 10.17181/gtesb-a8354

- [2409.11466](#) shows how to rewrite κ_λ in terms of C_ϕ :
A dim-6 operator which affects the Higgs self-coupling vertex

- Using κ_λ parameterization equation derived in [JHEP02 \(2018\) 178](#), but replacing κ_λ with SMEFT definition:

$$\kappa_\lambda \longrightarrow 1 - \frac{2v^4}{m_H^2 \Lambda^2} C_\phi = 1 - 0.47 C_\phi \left(\frac{1 \text{ TeV}}{\Lambda} \right)^2 + \mathcal{O}\left(\frac{1}{\Lambda^4}\right)$$

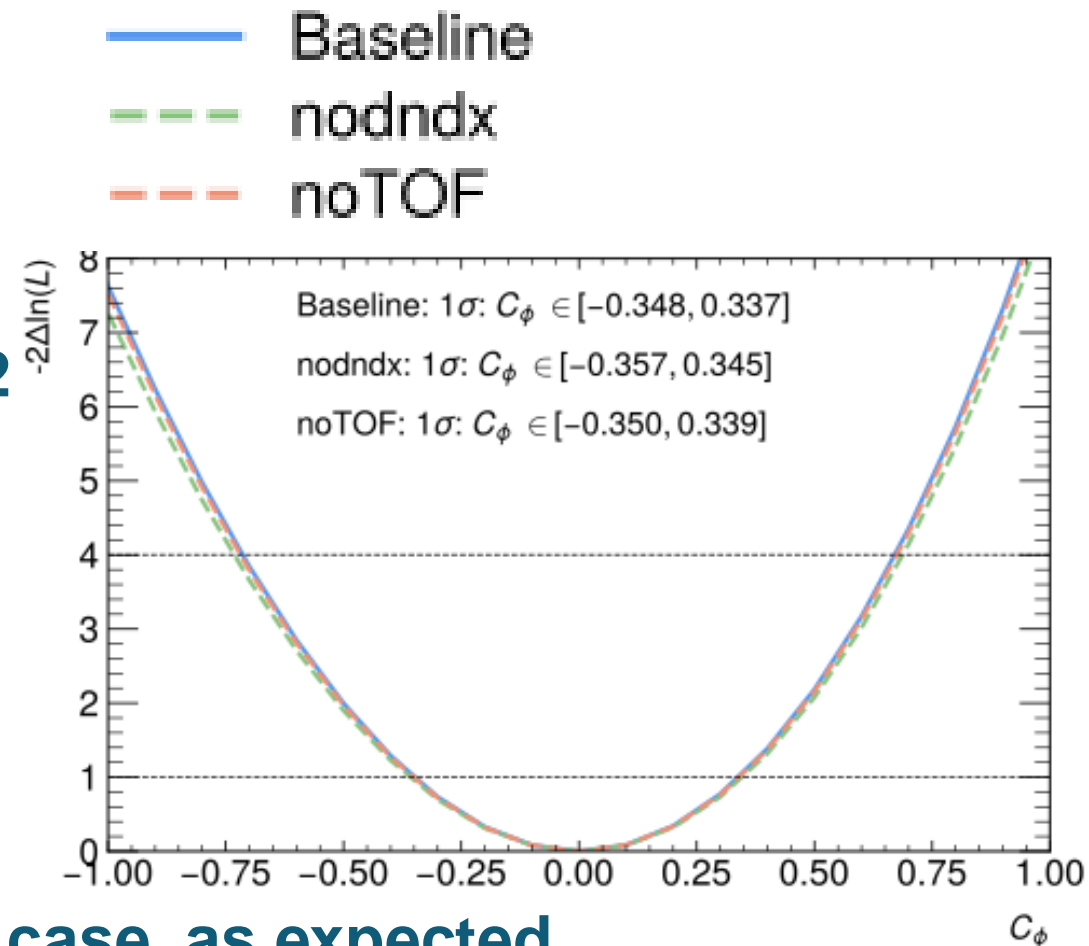
- Assuming a scale of $\Lambda = 1 \text{ TeV}$, can approximate to:

$$\kappa_\lambda \longrightarrow 1 - 0.47 C_\phi$$

Self-coupling

Elizabeth Brost,
Robert Szafron,
Abraham Tishelman-Charny
DOI 10.17181/gtesb-a8354

- Fully-hadronic ZH analysis
- Vary C_ϕ from -1 to 1 (valid range without including higher-order contributions)
- Do this for baseline IDEA (Delphes) and 2 detector variations:
 - Nodndx: No cluster counting information
 - noTOF: No time-of-flight information
- Centered at $C_\phi = 0$ ($\kappa_\lambda = 1$)
 - Makes sense as this is the SM value
- Slightly less sensitivity from the Nodndx case, as expected



Summary

❖ Higgs mass

- At 240 GeV, Higgs mass uncertainty reach 3.07 (3.97) MeV
- Including 365 GeV, Higgs mass uncertainty improved ~ 1%
- For FullSim, in the muon channel, reached 6.41 MeV uncertainty, 25% worse than Delphes-based analysis (5.11 MeV)

❖ ZH cross section

- ZH cross-section reach ~0.59% (at 240 GeV), ~1.48% (at 365 GeV)

❖ CP

- Combined $f_{CP}^{HZZ} \sim \pm 3 \times 10^{-5}$
- Combined result represents ~79% of Z decays

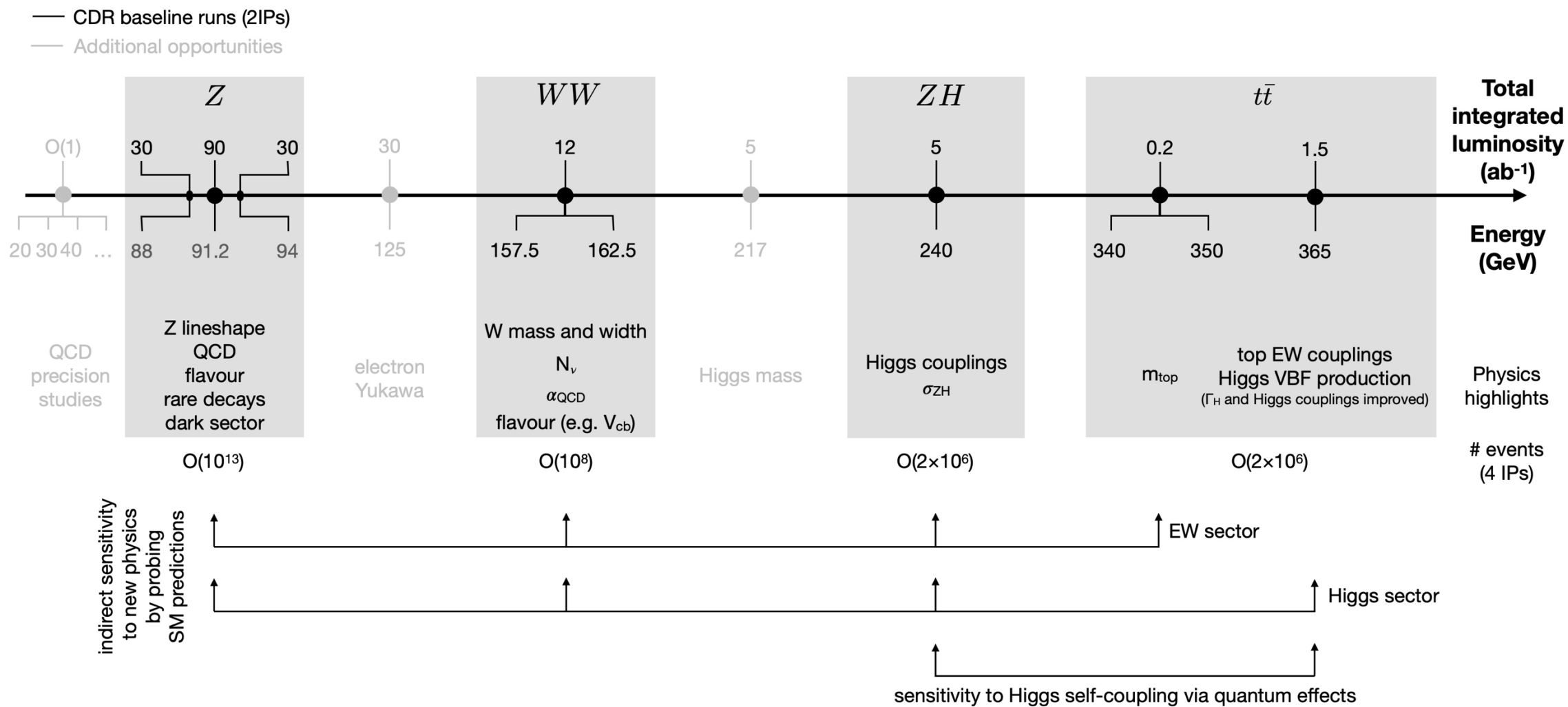
❖ Self-coupling

- Cross-section in terms of SMEFT parameter C_ϕ
- Constraint on $C_\phi \in [-0.348, 0.337]$

Backup

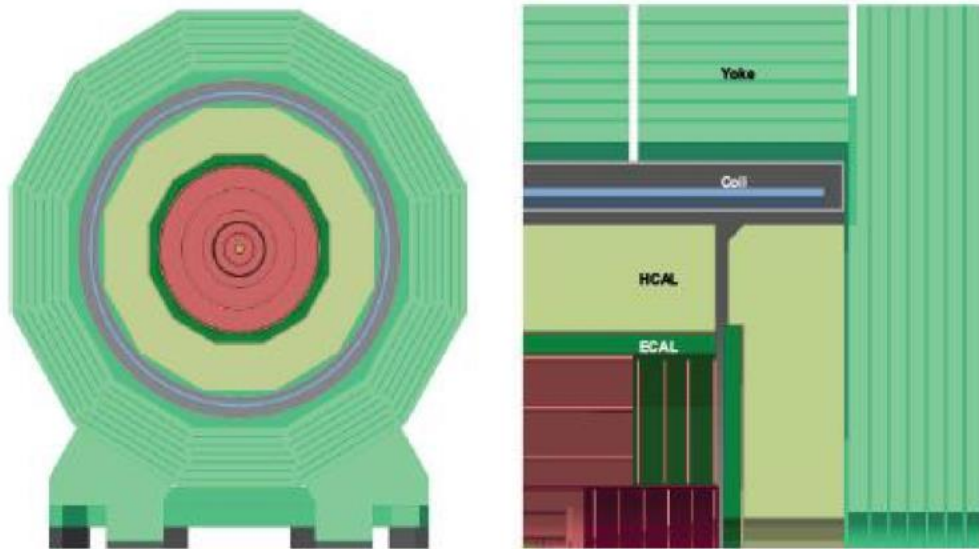
FCC-ee

FCC-ee Physics Runs Ordered by Energy



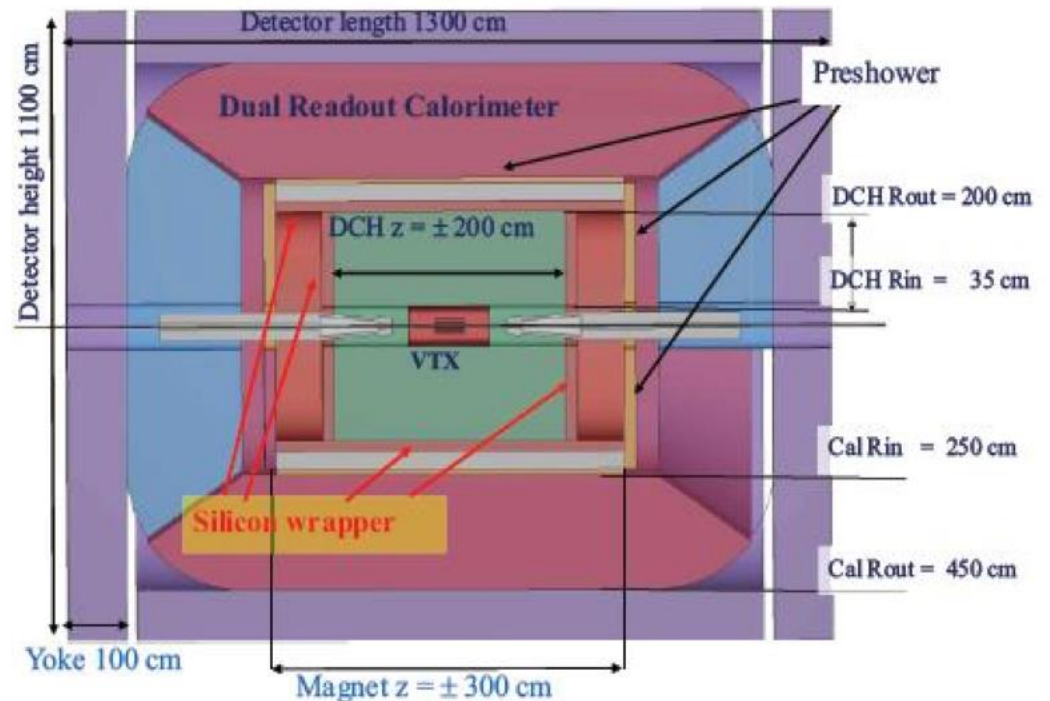
Detectors

CLD



- conceptually extended from the CLIC detector design
 - full silicon tracker
 - 2T magnetic field
 - high granular silicon-tungsten ECAL
 - high granular scintillator-steel HCAL
 - instrumented steel-yoke with RPC for muon detection

IDEA



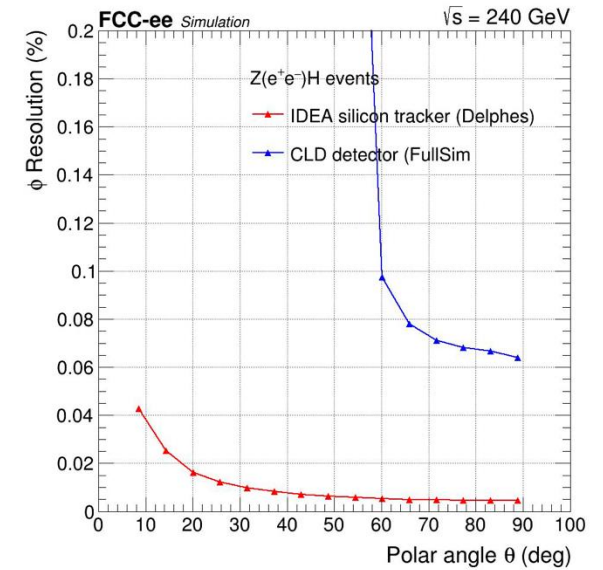
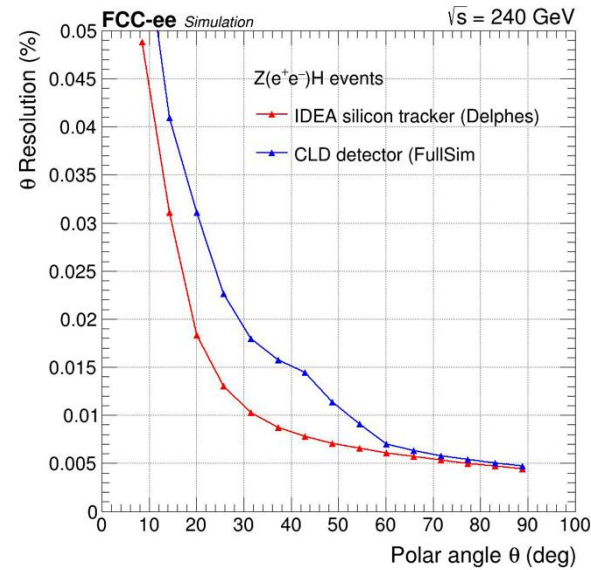
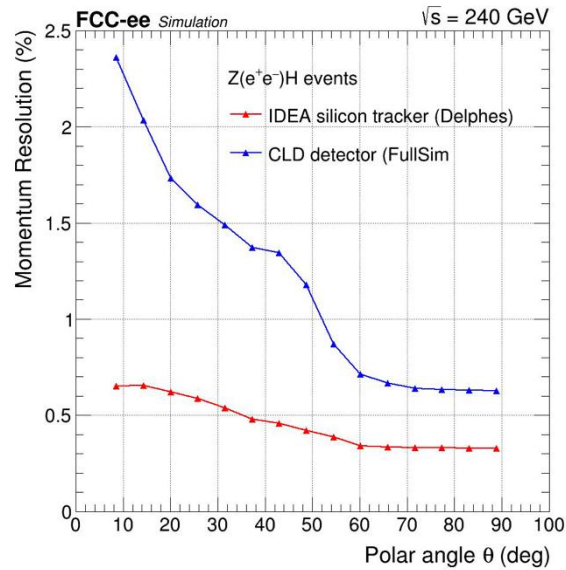
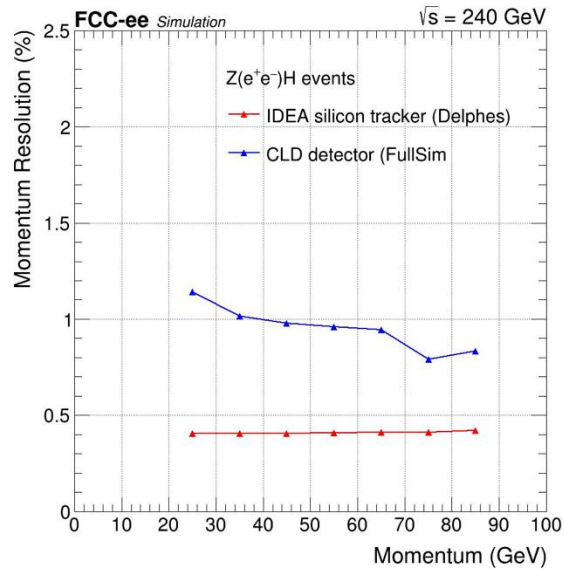
- explicitly designed for FCC-ee/CepC
 - silicon vertex
 - low X_0 drift chamber
 - drift-chamber silicon wrapper
 - MPGD/magnet coil/lead preshower
 - dual-readout calorimeter: lead-scintillating/cerenkov fibers
 - μ Rwell for muon detection

Higgs mass

Some extended studies performed regarding detector effects

	Final state	Muon	Electron	Combination
Nominal configuration	Nominal	3.92(4.74)	4.95(5.68)	3.07(3.97)
Crystal ECAL to Dual Readout	Inclusive	3.92(4.74)	4.95(5.68)	3.10(3.97)
	Degradation electron resolution	3.92(4.74)	5.79(6.33)	3.24(4.12)
Nominal 2 T → field 3 T	Magnetic field 3T	3.22(4.14)	4.11(4.83)	2.54(3.52)
IDEA drift chamber → CLD Si tracker	Silicon tracker	5.11(5.73)	5.89(6.42)	3.86(4.55)
Impact of Beam Energy Spread	BES 6% uncertainty	3.92(4.79)	4.95(5.92)	3.07(3.98)
	Disable BES	2.11(3.31)	2.93(3.88)	1.71(2.92)
Perfect (=gen-level) momentum resolution	Ideal resolution	3.12(3.95)	3.58(4.52)	2.42(3.40)
	Freeze backgrounds	3.91(4.74)	4.95(5.67)	3.07(3.96)
	Remove backgrounds	3.08(4.13)	3.51(4.58)	2.31(3.45)

Momentum and Angular resolution



Electron resolutions based on Z(ee)H events

- Visibly worse momentum in FullSim
- No Bremsstrahlung recovery in CLD reconstruction