

# NATURALNESS AT FCC




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Higgs Mass  
Squared


$$m_h^2 |H|^2$$

WEAK FORCE, STRUCTURE OF NUCLEI, COMPLEX  
CHEMISTRY, ...

$$m_h^2 \sim \frac{y_t^2 M_{\text{Pl}}^2}{16\pi^2}$$



Symmetry~ $10^{34}$  Experiment



$$m_h^2 = 0$$

Special

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Planck

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New  
Symmetry

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SM

$$m_h^2 \sim \frac{y_t^2 M_S^2}{16\pi^2}$$

$M_S$

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Planck

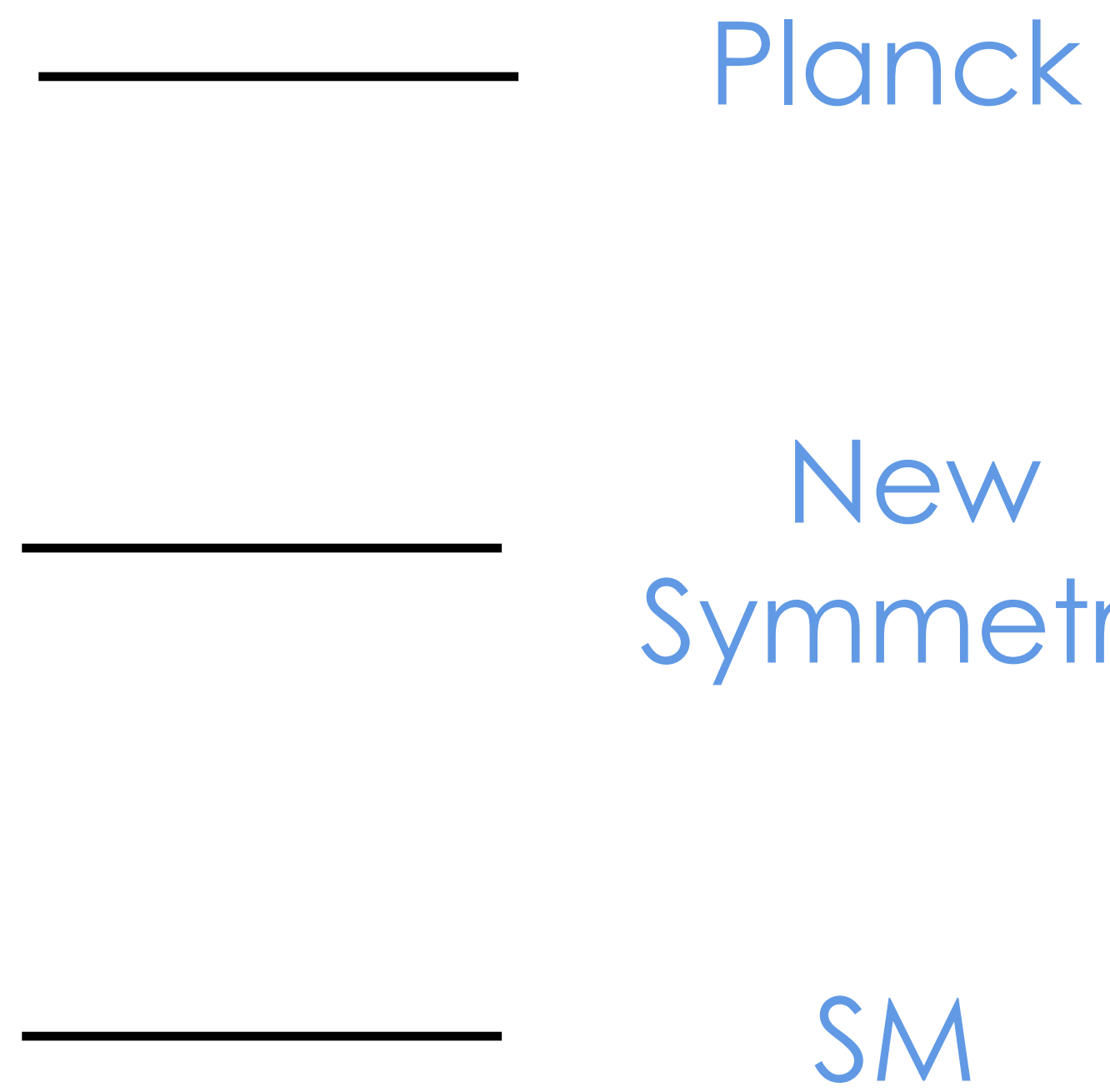
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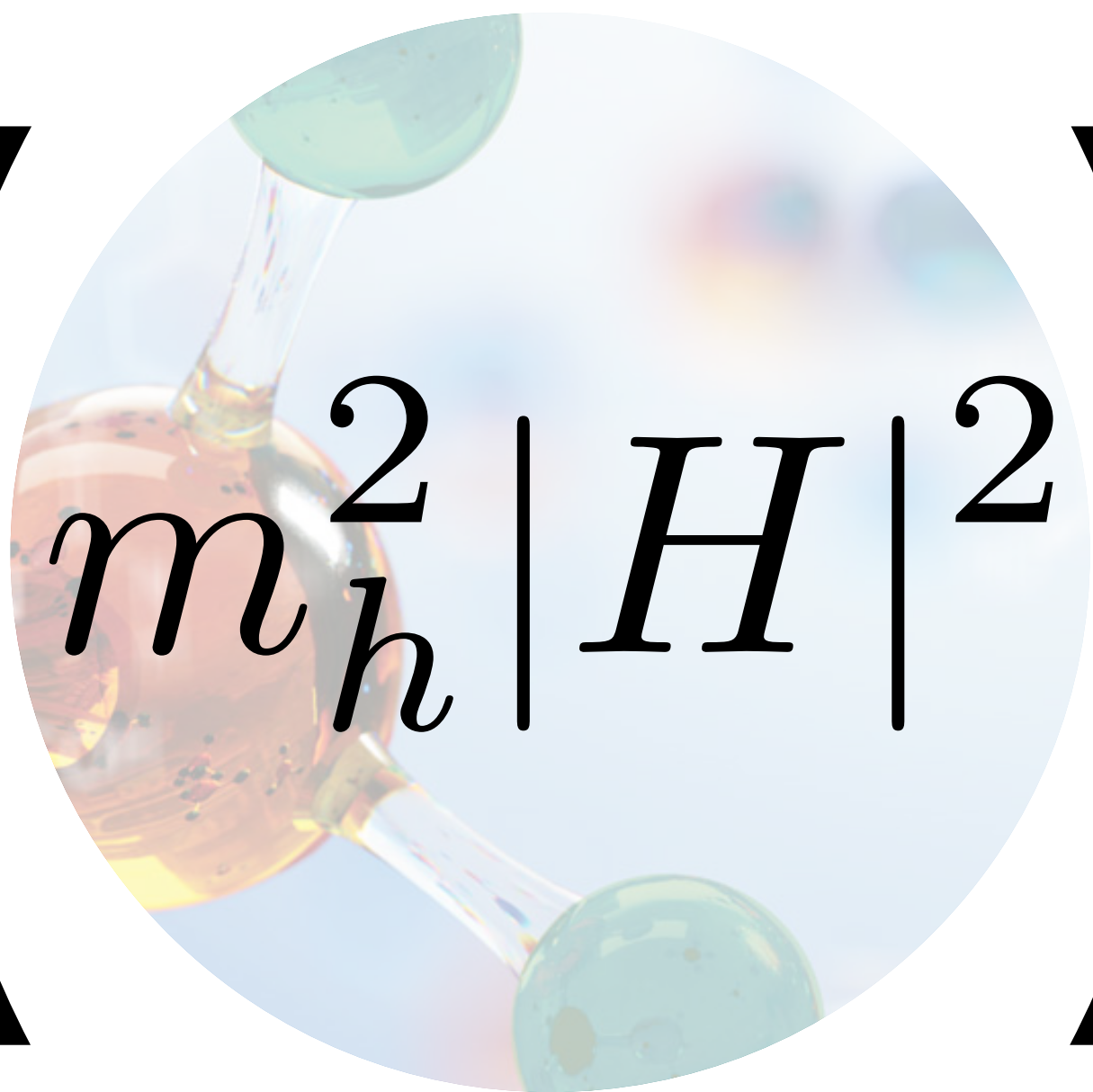
New  
Symmetry

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SM

Supersymmetry or Scale Invariance




$$\left( m_h^2 |H|^2 \right)$$

We have been looking  
for answers at energies  
close to the Higgs mass  
for more than 40 years

Higgs Boson



and we have  
not found them

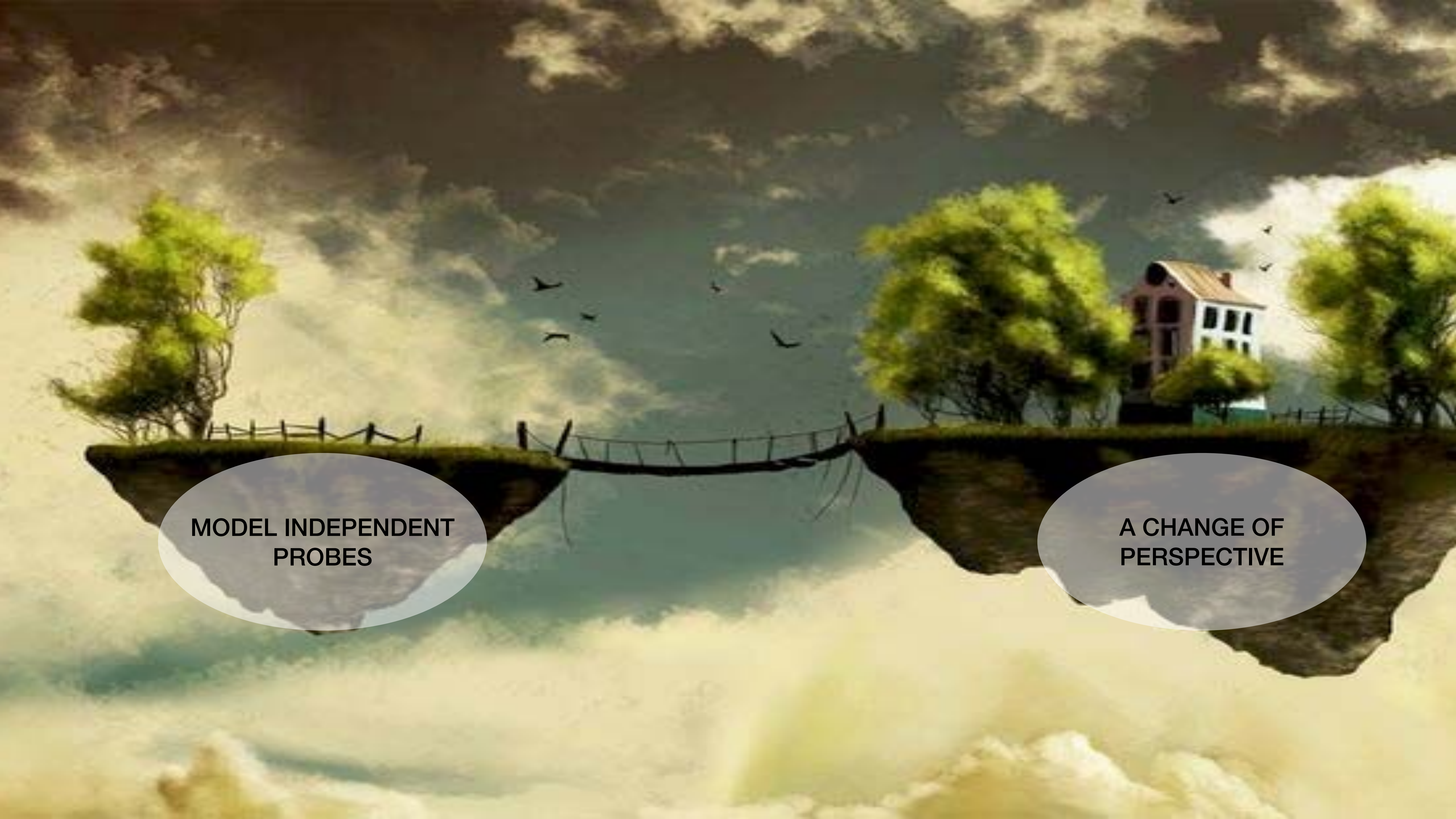


It doesn't work at all for the cosmological constant

$$\Lambda \simeq (0.1 \text{ meV})^4$$



**WHAT NOW?**

A surreal landscape featuring a floating island with a wooden bridge connecting two sections. On the right section, there is a two-story house with a red roof and white trim, surrounded by green trees. The sky is filled with dark, dramatic clouds and several birds in flight. The overall scene is ethereal and dreamlike.

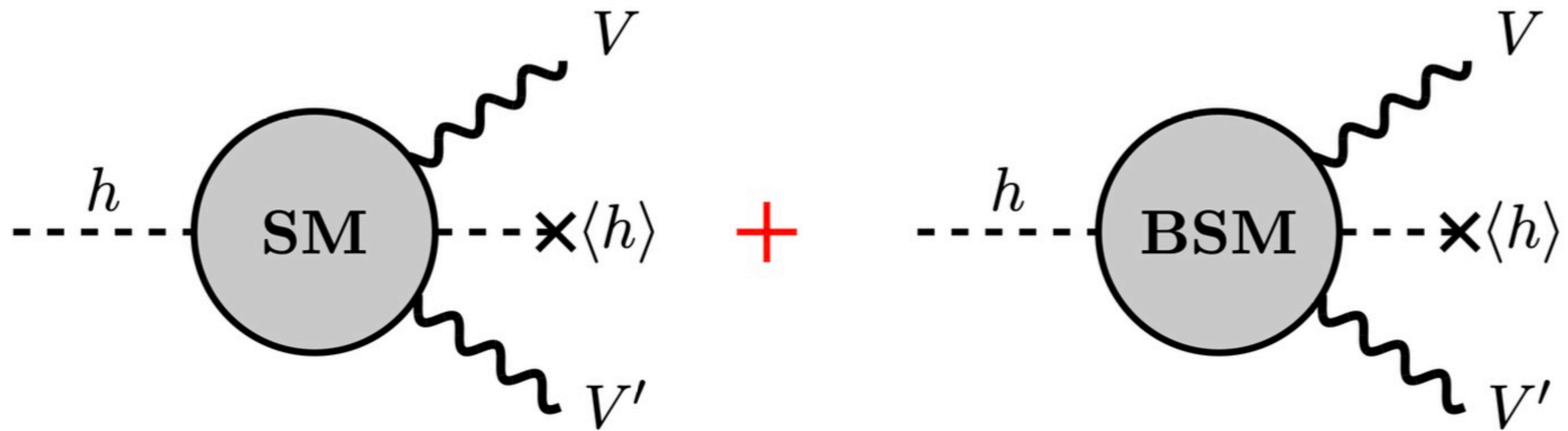
**MODEL INDEPENDENT  
PROBES**

**A CHANGE OF  
PERSPECTIVE**

A surreal landscape featuring a floating island with a bridge, a house, and birds in a cloudy sky. The scene is set against a backdrop of a cloudy sky with a rainbow visible at the bottom. The island is a flat, grassy platform that appears to be suspended in the air. A simple wooden bridge with a railing spans across the gap between two parts of the island. On the right side of the island, there is a two-story house with a red roof and white walls. Several trees with green foliage are scattered across the island. In the sky, several birds are seen in flight. The overall atmosphere is dreamlike and ethereal.

MODEL INDEPENDENT  
PROBES







If you observe a deviation in Higgs couplings you can set an upper bound on the scale where **new bosons** must appear





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F. Nortier, G. Rigo, P. Sesma '24

RTD, F. Nortier, G. Rigo, P. Sesma '23

K. Blum, RTD, J. Fan '15

N. Arkani-Hamed, K. Blum, RTD, J. Fan '12







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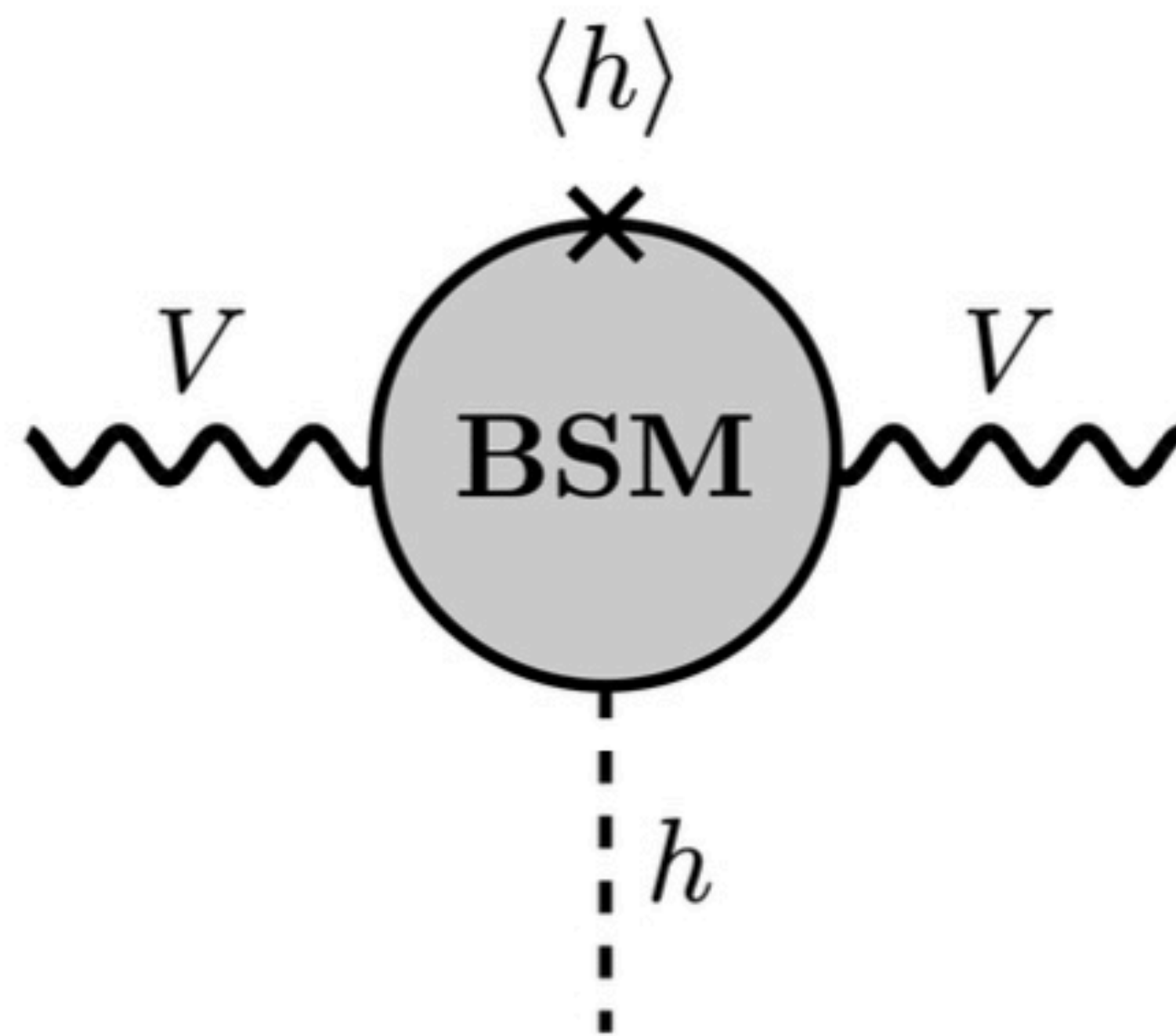




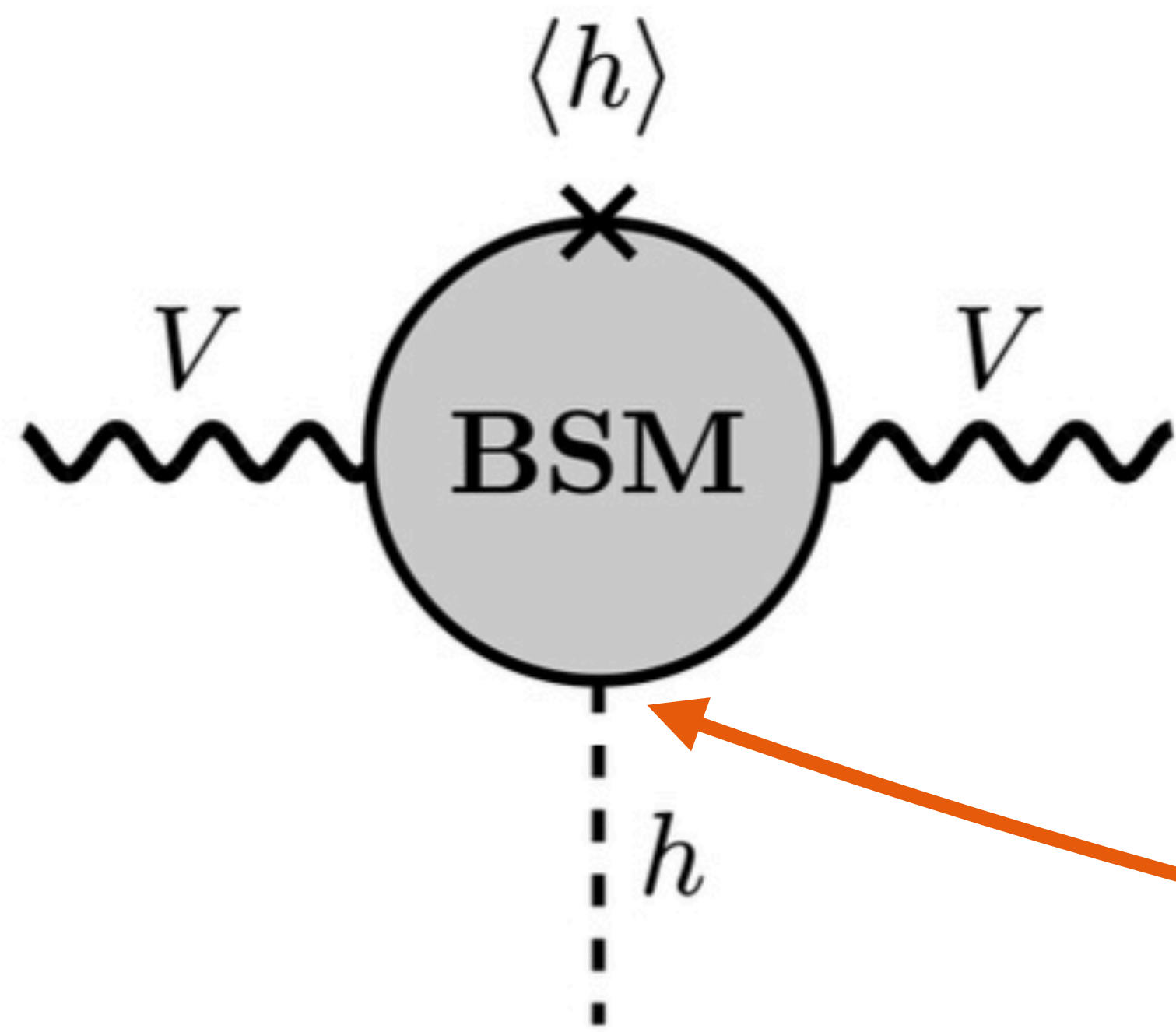
Imagine that you observed a deviation in hWW and have then discovered the fermions that generate it



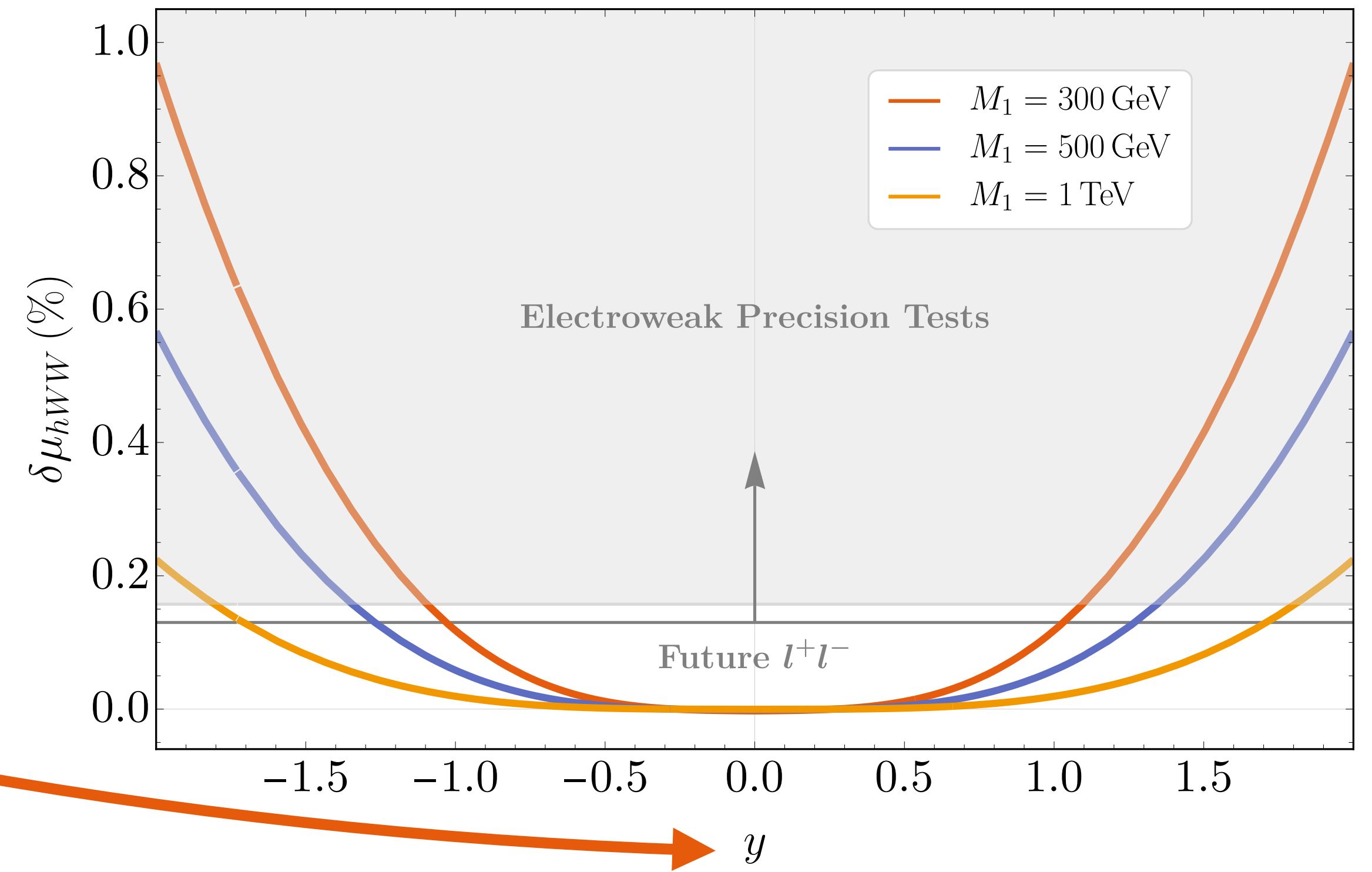
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doublet + singlet w/  $Q = 0$ ,  $y = y^c$



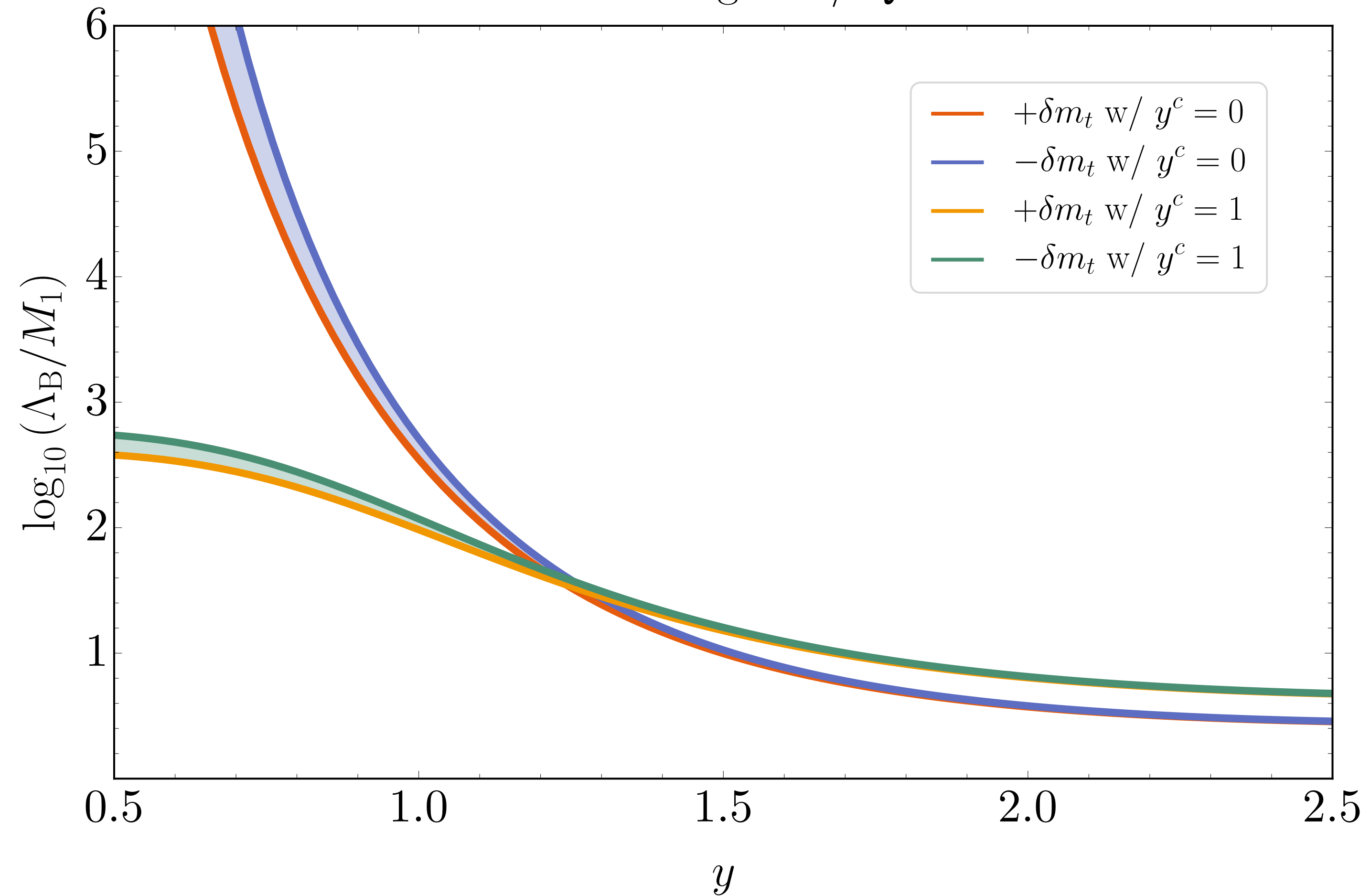
Large Yukawa couplings are “bad”

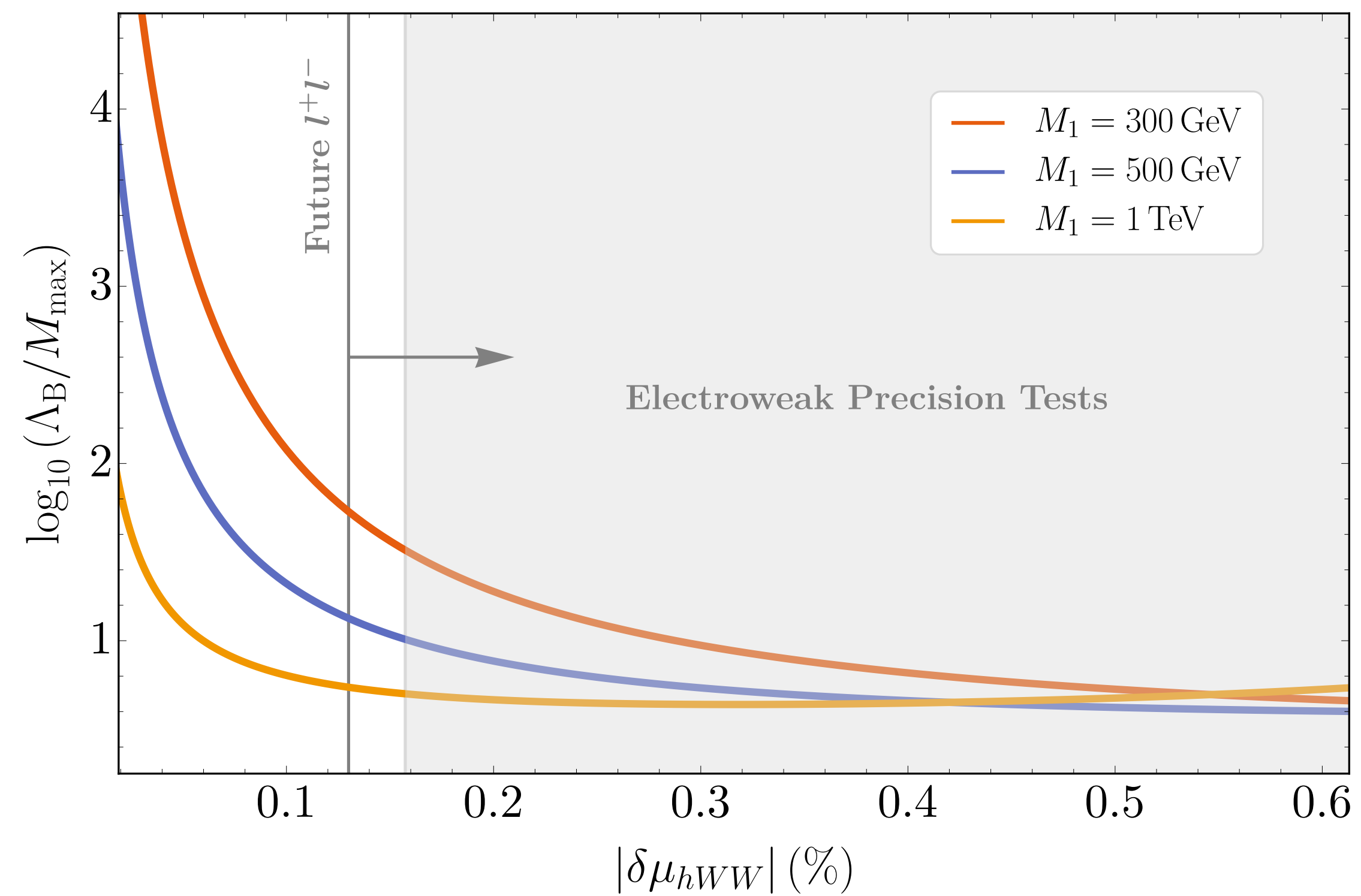
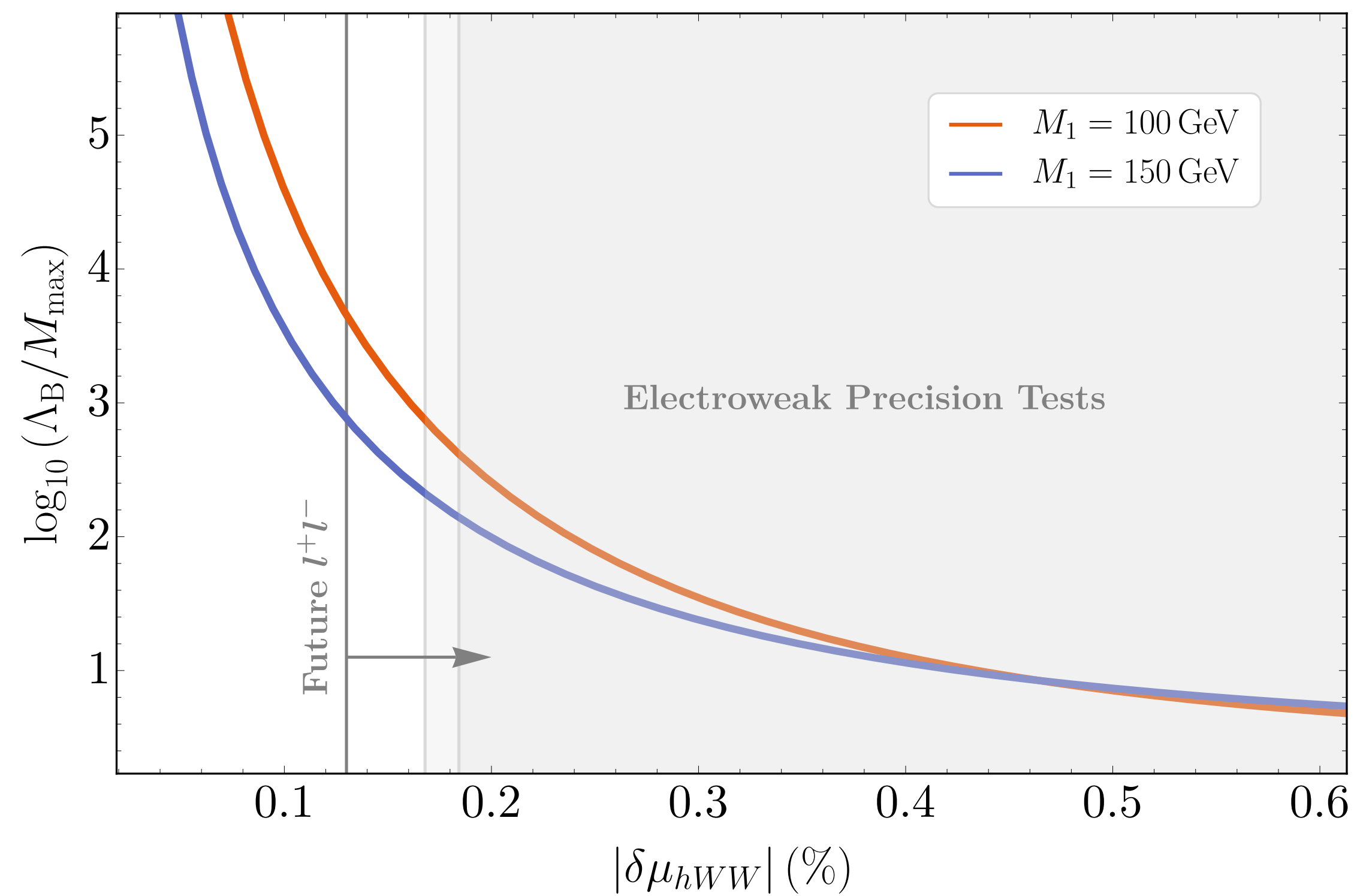
$$\frac{d\lambda}{d \log E} \sim \frac{y^4}{16\pi^2}$$

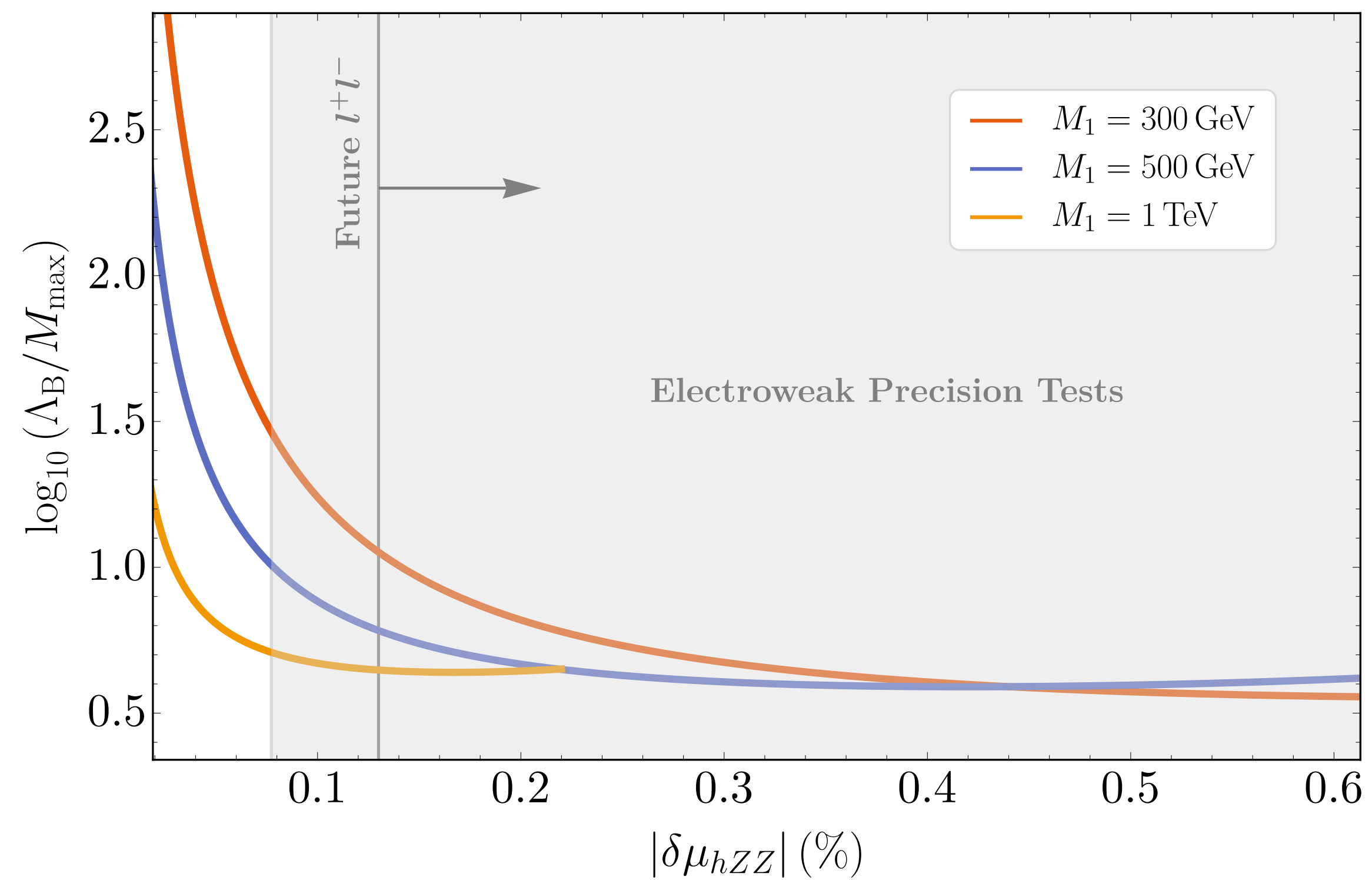
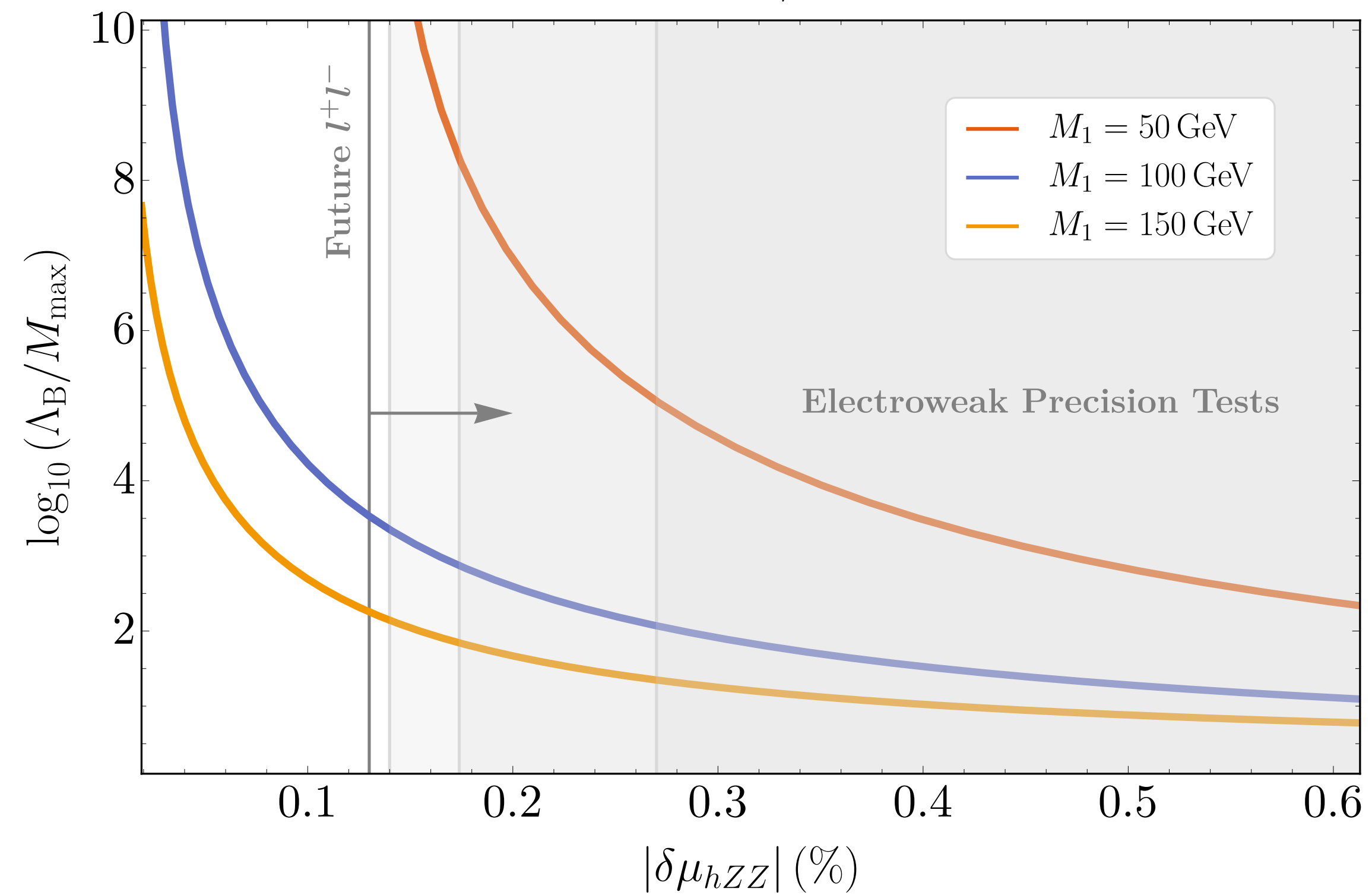
$$\frac{dy}{d \log E} \sim \frac{y^3}{16\pi^2}$$

# Large Yukawa couplings are “bad”

doublet + singlet w/  $Q = 0$



doublet + singlet w/  $Q = 0, y = y^c$ doublet + singlet w/  $Q = 0, y = y^c$ 

doublet + singlet w/  $Q = 0, y = y^c$ doublet + singlet w/  $Q = 0, y = y^c$ 




If you see a deviation in  $hWW$  or  $hZZ$  at HL-LHC or FCC-ee  
you will detect new bosons at FCC-hh (at the latest)

**RTD, F. Nortier, G. Rigo, P. Sesma '23**



A CHANGE OF  
PERSPECTIVE

1. We tune
2. There is no mass scale beyond the SM  
[1305.6939]
3. The Higgs mass and the CC are inputs
4. UV/IR Mixing [1909.01365]
5. Swampland on steroids



1.

We tune

2.

In 4D you get GR with  
ghosts

3.

We don't know any  
theory of QG that does it

4.

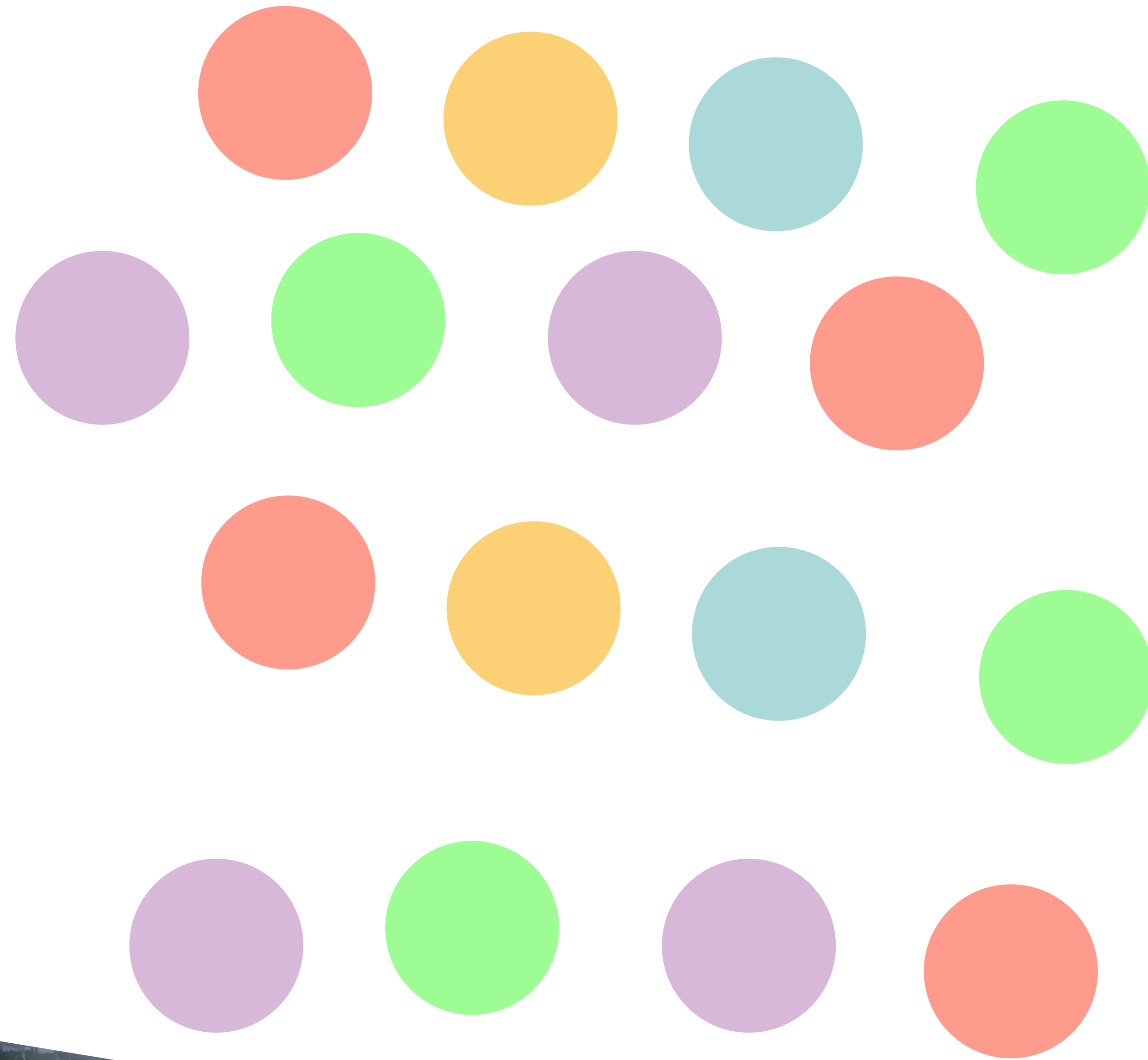
Possible, but we don't  
have any idea how to  
write a theory that works

5.

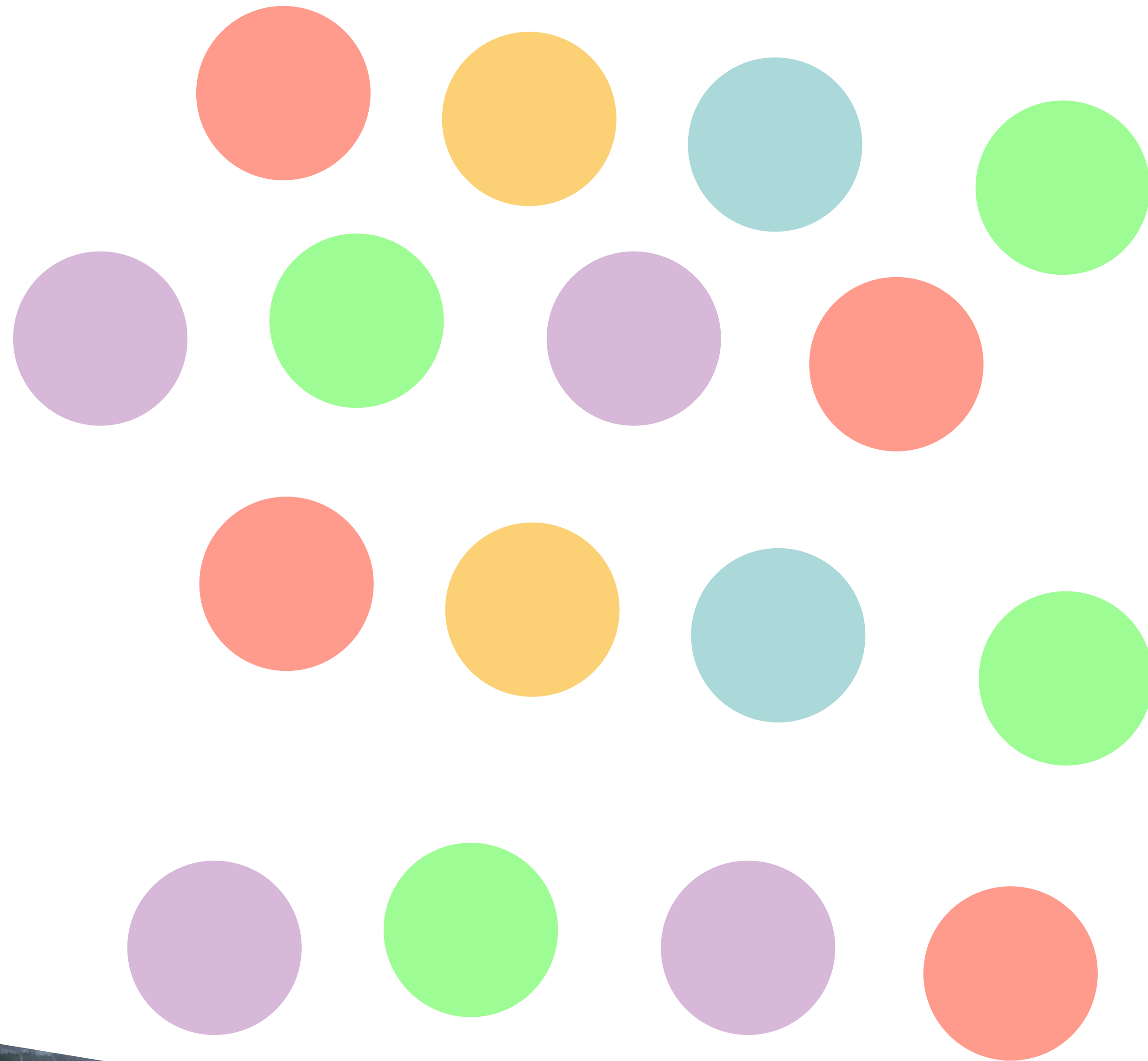
6.

**There is a landscape**





Causally  
Disconnected  
Universes with  
different values of  
the Standard Model  
parameters,  
populated by  
inflation



1. One day it can be tested experimentally
2. Currently our most concrete explanation for the cosmological constant
3. It probably exists independently of the problem

# ONE EXAMPLE

C.Csaki, RTD, M. Geller, A. Ismail '21

**Landscape** of Higgs Masses populated by inflation

$$-\Lambda_H^2 \leq m_H^2 \leq \Lambda_H^2$$

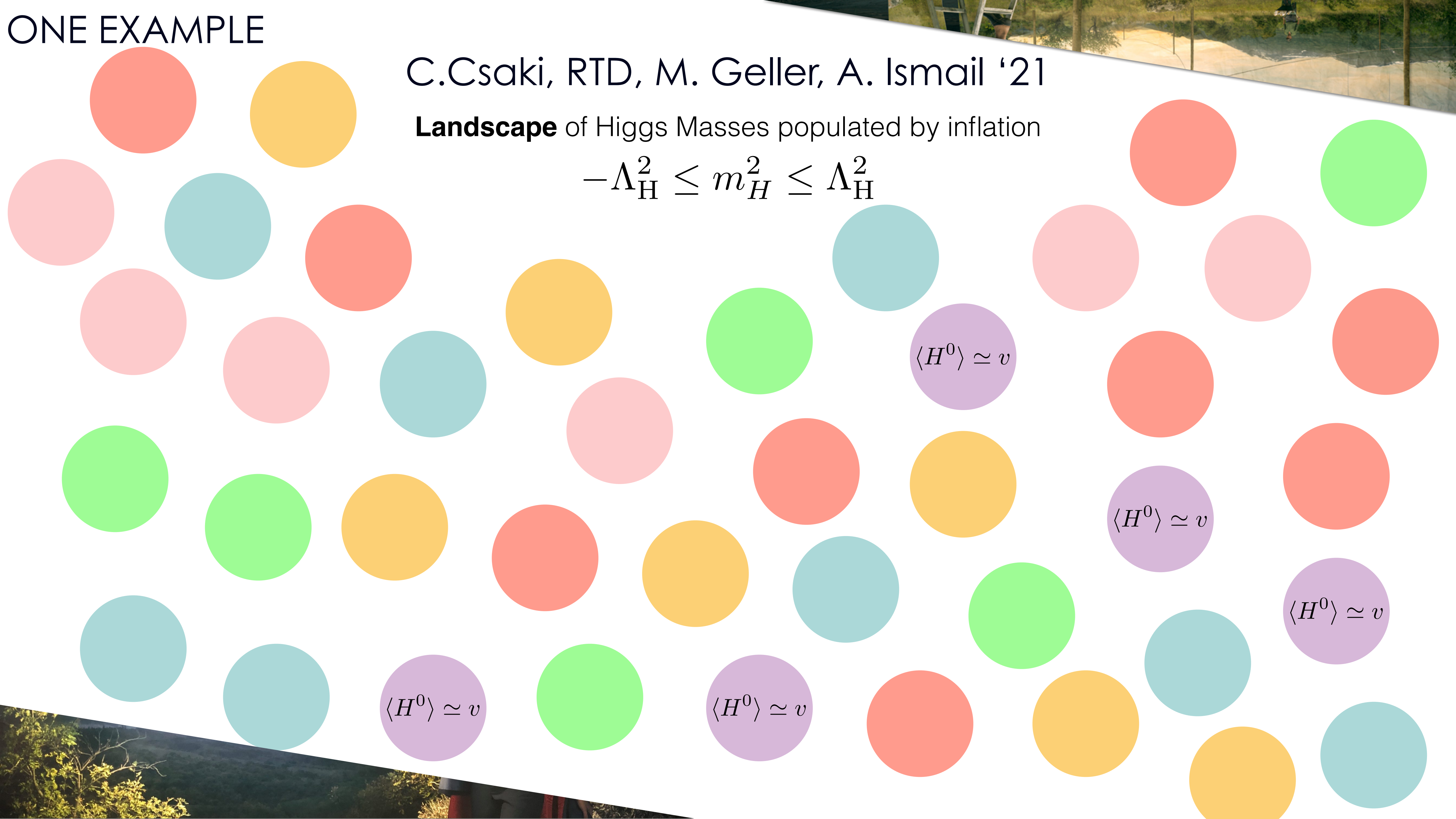
$$\langle H^0 \rangle \simeq v$$

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# ONE EXAMPLE

**After a time**

$$t_c < M_{\text{Pl}}/\Lambda_{\text{H}}^2$$

All patches where the Higgs  
vev

$$\langle H^0 \rangle \equiv h$$

Is outside of a certain range

$$h_{\text{min}} \lesssim h \leq h_{\text{crit}}$$

**crunch**

$$\langle H^0 \rangle \simeq v$$

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# ONE EXAMPLE

Only universes with the observed value of the weak scale can live longer than a Planck time and inflate. **Today the multiverse looks like:**

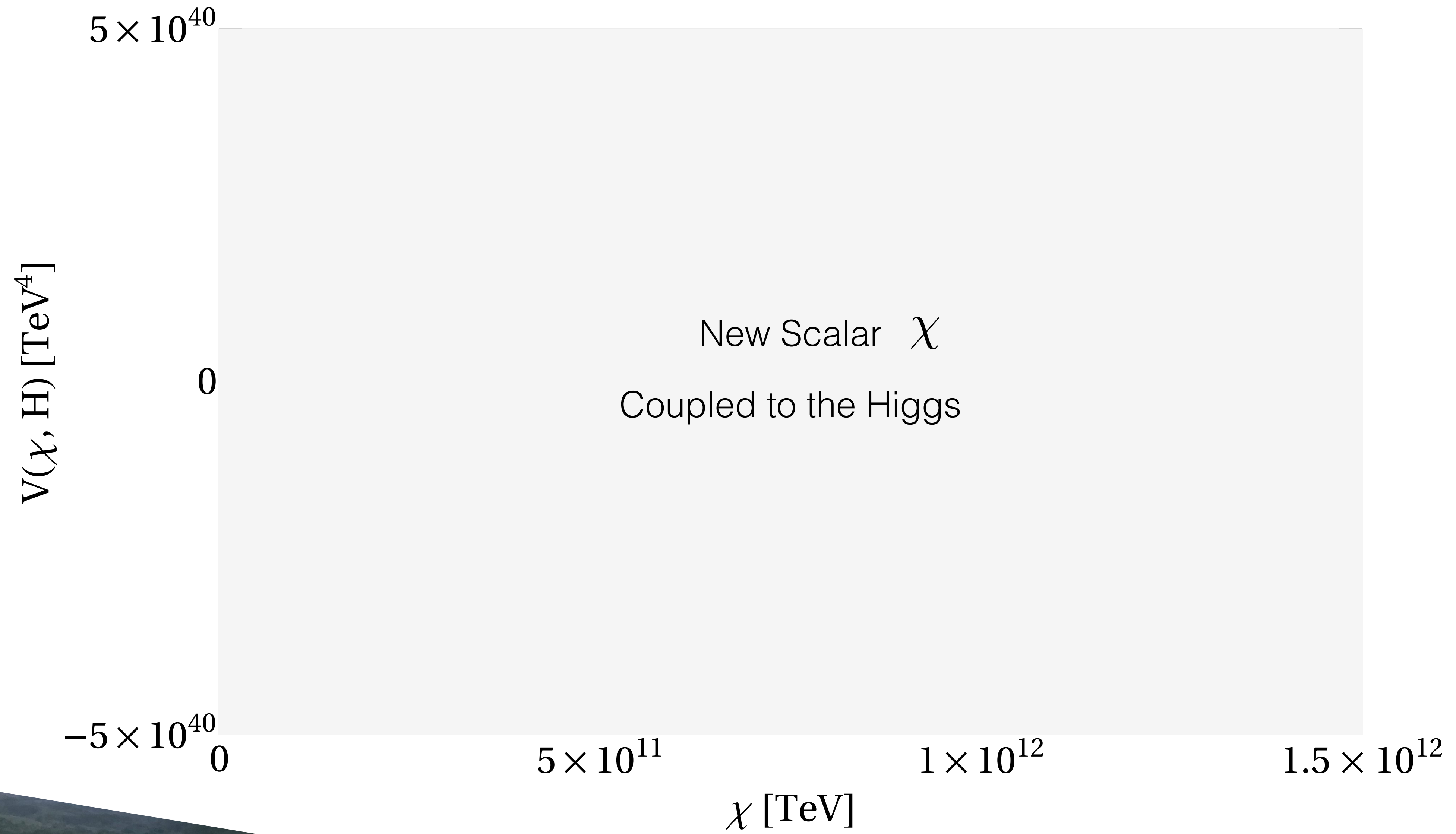
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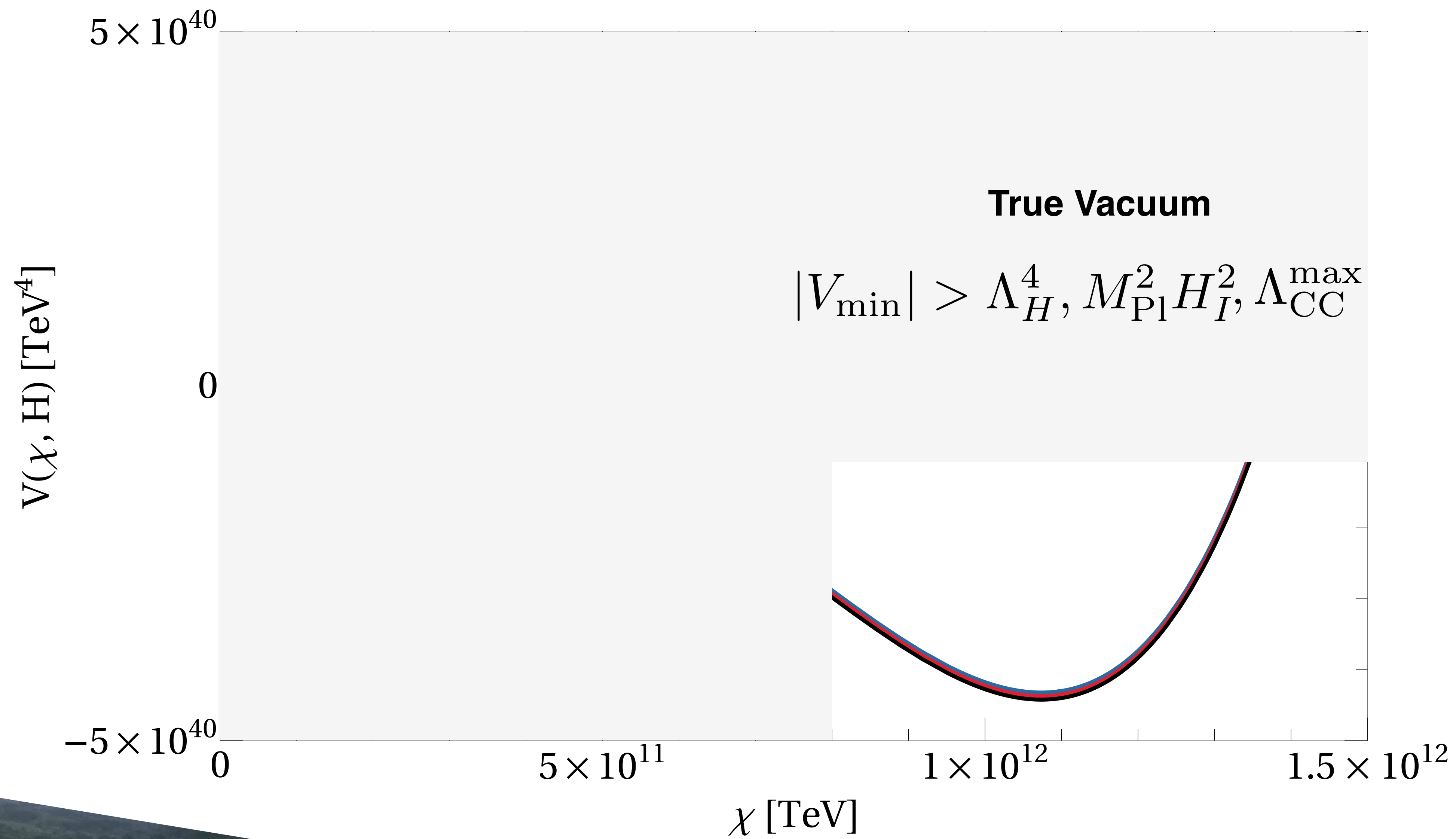
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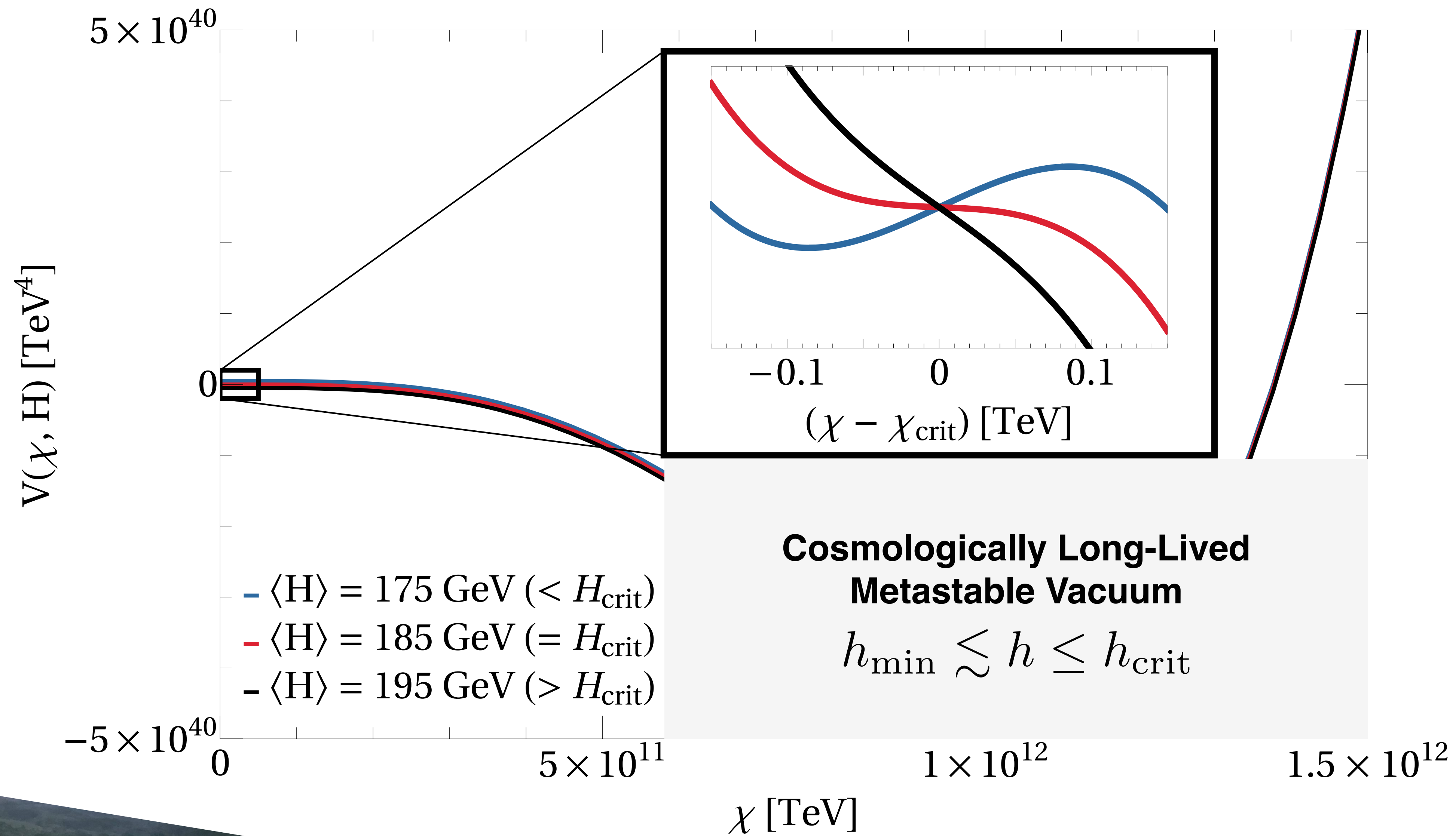
# ONE EXAMPLE



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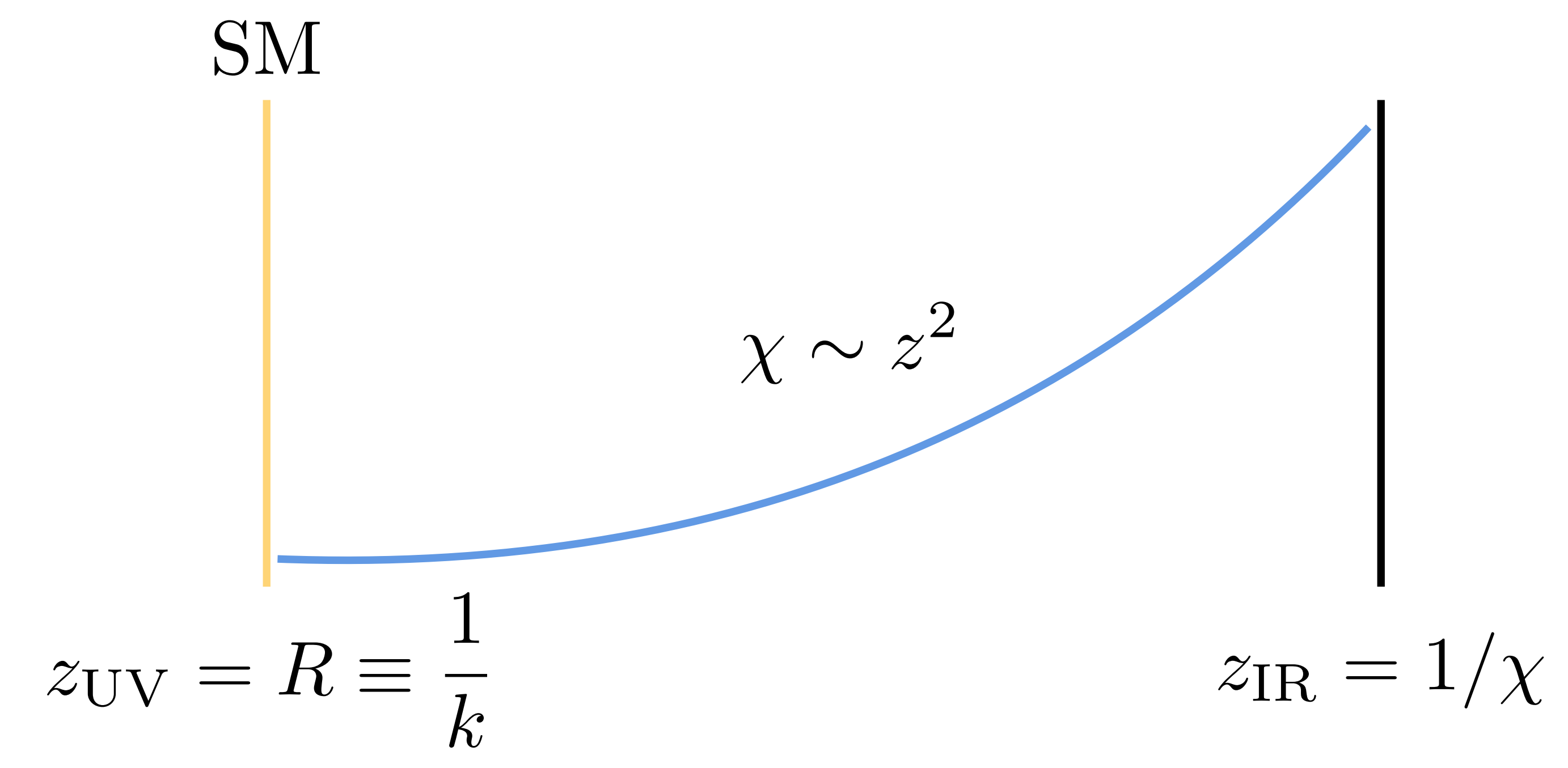


# ONE EXAMPLE



# CRUNCHING FROM SCALE INVARIANCE

$$ds^2 = \left(\frac{R}{z}\right)^2 (\eta_{\mu\nu} dx^\mu dx^\nu - dz^2)$$



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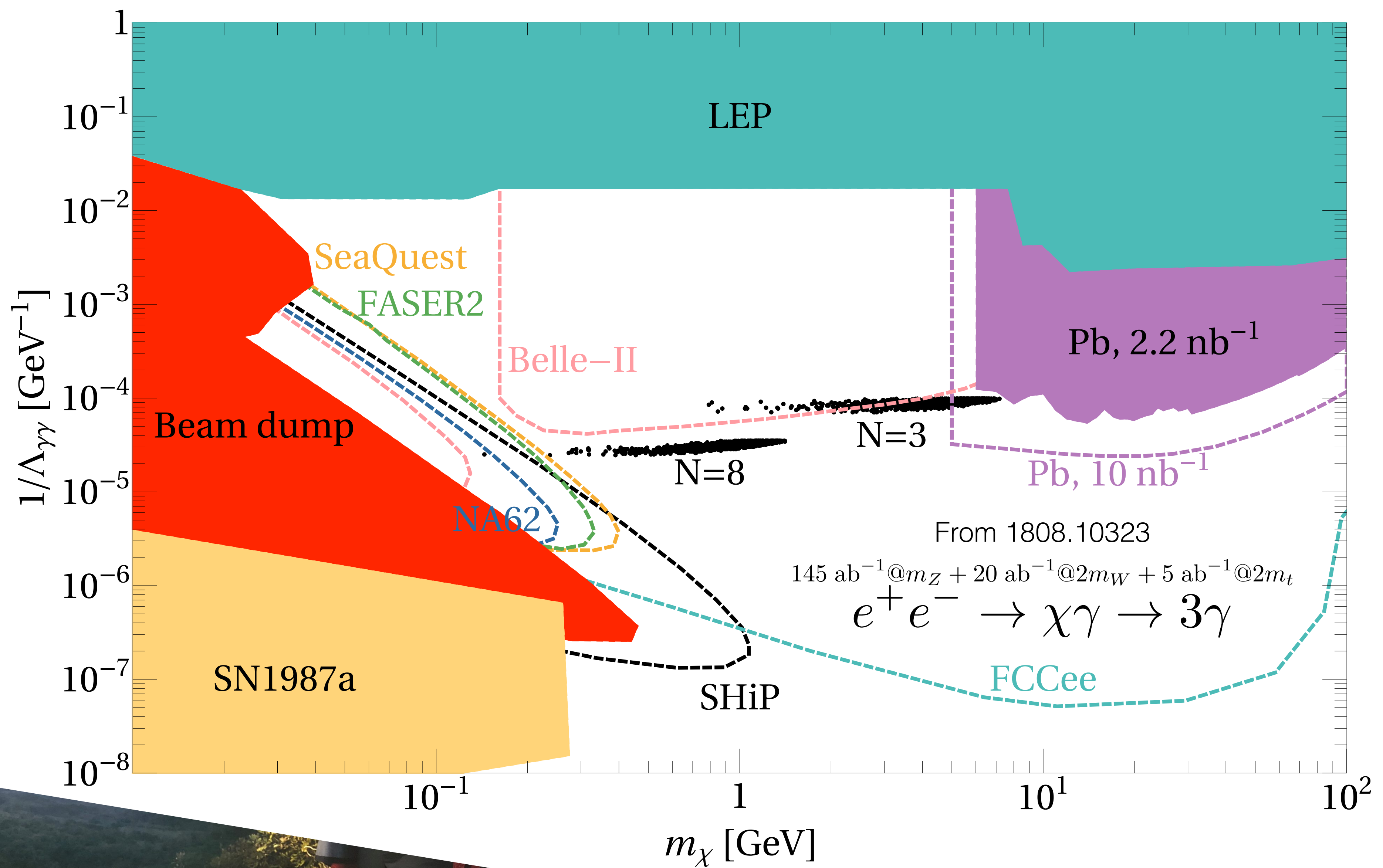
SM

$H, W, Z, \gamma$   
 $\phi_{\text{GW}}$

$$z_{\text{UV}} = R \equiv \frac{1}{k}$$

$$z_{\text{IR}} = 1/\chi$$

# A LIGHT DILATON





A GENERAL LESSON

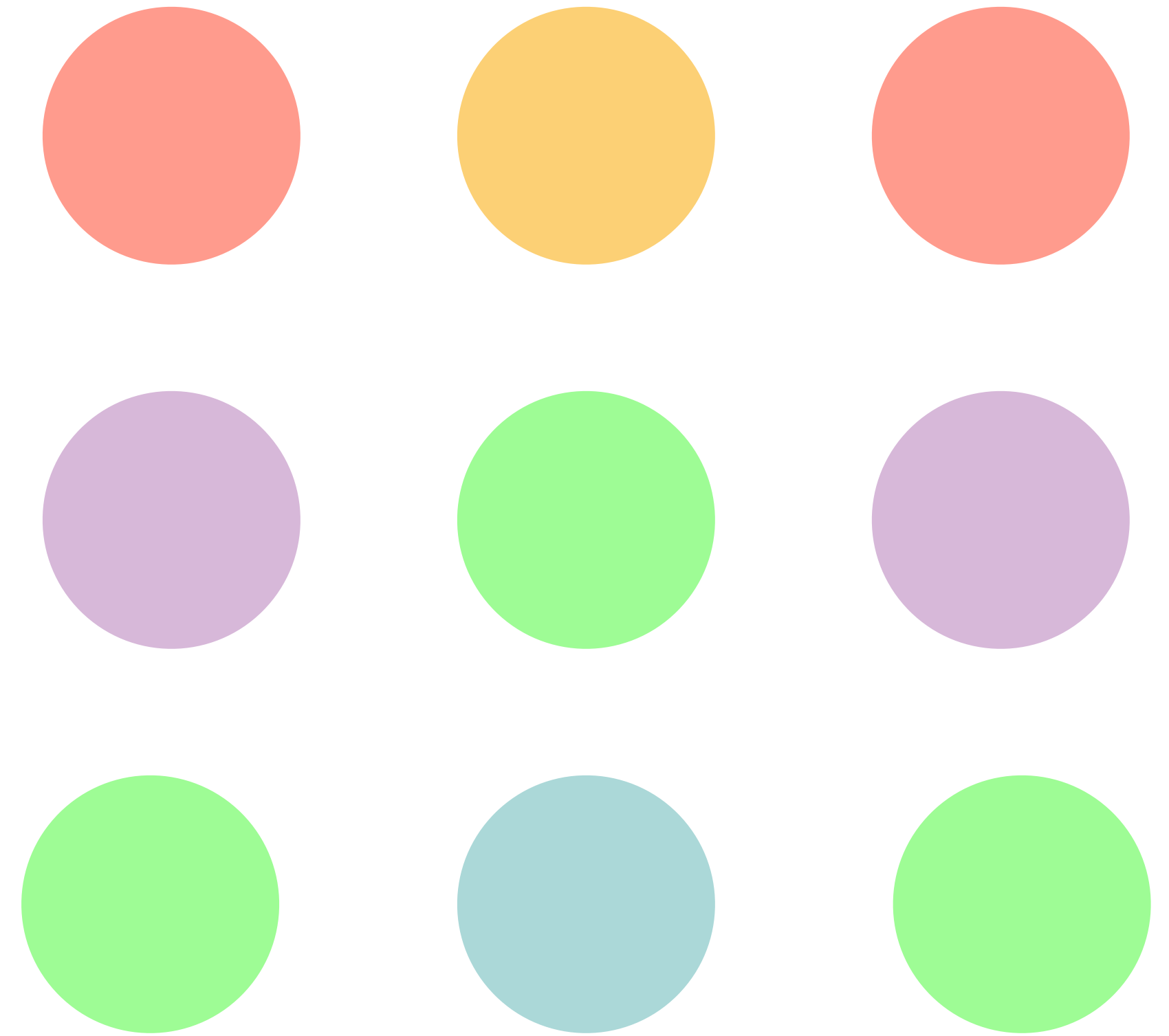


# GENERAL STRUCTURE

Symmetric Sector

$$M_S \ll M_{Pl}$$

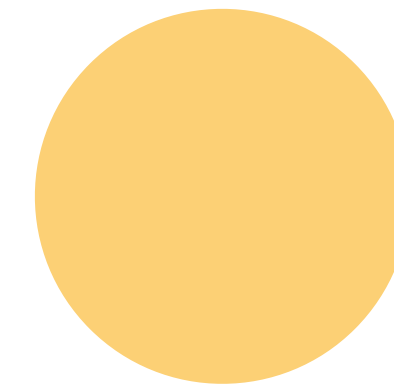
SM Landscape



Symmetric Sector

$$M_S \ll M_{\text{Pl}}$$

SM Landscape

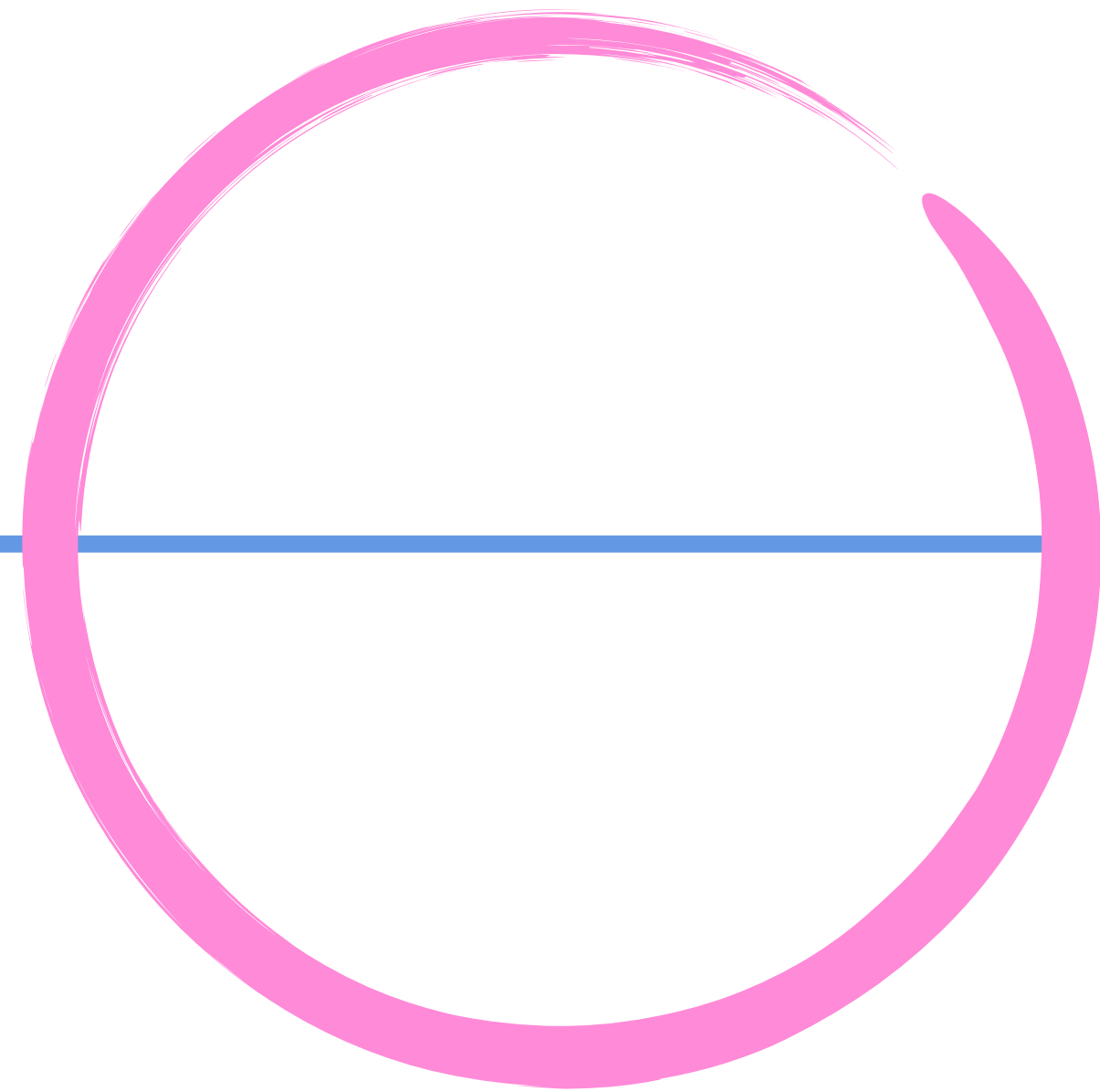


**An event triggered by the symmetric sector selects the observed**

$$m_h^2$$

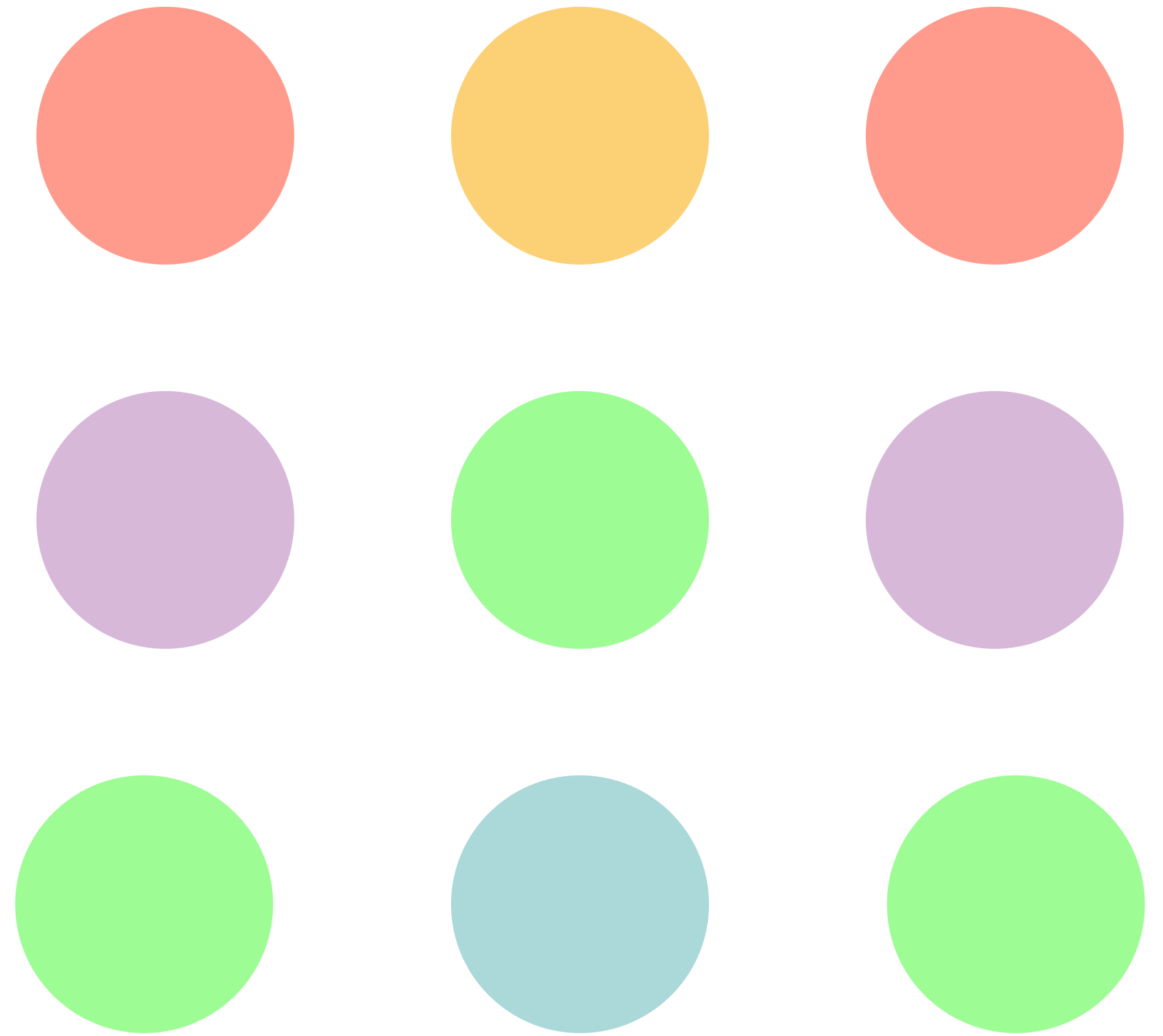
Symmetric Sector

$$\Lambda_S \ll M_{\text{Pl}}$$



Sensitive to  
the  
Higgs mass

SM Landscape





$G\tilde{G}$

ALPs

$F\tilde{F} + yLHE^c$

$m \lesssim v \simeq 174 \text{ GeV}$   
HL-LHC and FCC-ee

$H_1H_2$

$m \lesssim v \simeq 174 \text{ GeV}$   
HL-LHC and FCC-ee

