DA studies with Xsuite

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189th FCC-ee Accelerator Design Meeting – July 25th, 2024

Model and notation corrections

• X, Y =
$$J_{x,y} \cos(\Phi)$$
, PX, PY = $J_{x,y} \sin(\Phi)$

- $J_x = (2 \epsilon_x)^{1/2}$ hence $J_x/J_y = (\epsilon_x/\epsilon_y)^{1/2} = (\epsilon_x/0.002\epsilon_x)^{1/2} \approx 22.36$
- $A_x = (2 J_x)^{1/2} = (x^2 + p_x^2)^{1/2}$ called amplitude
- x and p_x are normalised hence the normalised amplitude is plotted

Fig. 2.11. Dynamic apertures in z-x plane after sextupole optimisation with particle tracking for each energy. The initial vertical amplitude for the tracking is always set to $J_y/J_x = \varepsilon_y/\varepsilon_x$. The number of turns corresponds to about 2 longitudinal damping times.

Additionally, the SR model only features **damping** as the 'mean' model in Xsuite.

Oide's DA - Macroparticle grid





'Brute force' grid

Grid resulting from bisection

Resulting DA

As you increase the 'depth' of tracked macroparticle in action J, the central area becomes increasingly whiter, proving the particles survived.

Some parts of the central region appear less white because of the average between phase planes because some planes have no data at this (δ ,J) position.



Results with increasing number of turns

LCC V24.3 | E_{beam}=45.6 GeV, I_{beam}=1456mA (N=2.45E+11ppb), 2000 turns LCC V24.3 | E_{beam}=45.6 GeV, I_{beam}=1456mA (N=2.45E+11ppb), 2400 turns LCC V24.3 | Ebeam = 45.6 GeV, Ibeam = 1456mA (N=2.45E+11ppb), 900 turns $\varepsilon_x = 0.69$ nm.rad, $\varepsilon_v / \varepsilon_x = 2$ %, $\sigma_{\delta} = 0.037$ %, $\sigma_z = 5.2$ nm, $\beta_{x,v}^* = \{0.10$ m, 0.7 nm} $\epsilon_x = 0.69$ nm.rad, $\epsilon_v / \epsilon_x = 2\%$, $\sigma_{\delta} = 0.037\%$, $\sigma_z = 5.2$ nm, $\beta_{x,v}^* = \{0.10$ nm, 0.7 nm} $\varepsilon_x = 0.69$ nm.rad, $\varepsilon_y/\varepsilon_x = 2$ ‰, $\sigma_{\delta} = 0.037$ %, $\sigma_z = 5.2$ nm, $\beta_{x,y}^* = \{0.10$ m, 0.7 nm} V_{rf} 400|800MHz=0.1GV|0.0GV, Q_{x|v|s}={198.200, 174.299, 0.030}, Crab waist=80% V_{rf} 400|800MHz=0.1GV|0.0GV, Q_{x|y|s}={198.200, 174.299, 0.030}, Crab waist=80% V_{rf} 400|800MHz=0.1GV|0.0GV, $Q_{x|y|s}$ ={198.200, 174.299, 0.030}, Crab waist=80% 2000 $\phi = 0$ 20 20 20 -800 1750 $\phi = \pi/4$ $\phi = \pi/4$ $\phi = \pi/4$ 2000 $\phi = \pi/2$ $\phi = \pi/2$ $\phi = \pi/2$ $A_{x}(\phi)$ $A_x(\phi)$ 700 1500 $\phi = 3\pi/4$ $\phi = 3\pi/4$ $\phi = 3\pi/4$ 10 10 600 pe Normalised amplitude Normalised amplitude 1500 panvived 1250 🖉 500 500 400 sunn 300 1000 In 1000 Sun Turns : 750 -10500 200 500 100 250 -20-20 -1.5-1.0-0.5 0.0 0.5 1.0 1.5 -0.5 -0.50.0 0.5 1.0 -1.5-1.00.0 0.5 1.0 1.5 -1.5-1.01.5 δ[%] δ[%] δ[%] -20-100 10 20 30 -30 -20 -100 10 20 30 -20 -1010 20 30 $\delta [\sigma_{\delta}^{SR}]$ $\delta \left[\sigma_{\delta}^{SR} \right]$ $\delta \left[\sigma_{\delta}^{SR} \right]$

900 turns ~ 2h40 Including slicing and Xsuite line conversion from MADX sequence

malised amplitude $A_x(\phi)$

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2000 turns ~ 3h32 including slicing and Xsuite line conversion from MADX sequence

2400 turns ~ 5h50 including slicing and Xsuite line conversion from MADX sequence

Probably an expected behaviour without quantum fluctuation.

Reduction to one RF section

From 4 RF cavities at 400MHz evenly distributed in the ring (one in each straight section) to **1 RF section** including 400 MHz RF cavities and 800 MHz RF cavities.

Single RF section for the LCC lattice (nominal)

Single RF section same total RF voltage

 $\begin{array}{l} LCC_V24.3 \mid E_{beam}{=}182.5 \mbox{ GeV, } I_{beam}{=}5mA \ (N{=}2.02E{+}11ppb), \ 50 \ turns \\ \epsilon_x{=}2.12nm.rad, \ \epsilon_y/\epsilon_x {=}2\%, \ \sigma_s{=}0.148\%, \ \sigma_z{=}1.8mm, \ \beta_{x,y}^{*}{=}\{1.00m, \ 1.6mm\} \\ V_{rf}\ 400|800MHz{=}2.10GV|9.20GV, \ Q_{x|y|s}{=}\{350.205, \ 266.294, \ 0.115\}, \ Crab \ waist{=}40\% \end{array}$



$$\begin{split} & LCC_V24.3 \mid E_{beam}{=}182.5 \text{ GeV}, \ I_{beam}{=}5\text{mA} \ (\text{N}{=}2.02\text{E}{+}11\text{ppb}), \ 50 \ \text{turns} \\ & \epsilon_x{=}2.12\text{nm.rad}, \ \epsilon_y/\epsilon_x {=}2\%, \ \sigma_\delta{=}0.148\%, \ \sigma_z{=}1.8\text{nm}, \ \beta_{x,y}^*{=}\{1.00\text{m}, \ 1.6\text{nm}\} \\ & V_{rf} \ 400|800\text{MHz}{=}2.10\text{GV}|9.20\text{GV}, \ Q_{x|y|s}{=}\{350.205, \ 266.294, \ 0.115\}, \ \text{Crab waist}{=}40\% \end{split}$$



Single RF section **10%** lower total RF voltage

$$\begin{split} & LCC_V24.3 \mid E_{beam}{=}182.5 \text{ GeV}, \ I_{beam}{=}5\text{mA} \ (\text{N}{=}1.77\text{E}{+}11\text{ppb}), \ 50 \ \text{turns} \\ & \epsilon_x{=}2.12\text{nm.rad}, \ \epsilon_y/\epsilon_x{=}2\%, \ \sigma_\sigma{=}0.148\%, \ \sigma_z{=}2.1\text{nm}, \ \beta_{x,y}^{*}{=}\{1.00\text{m}, \ 1.6\text{mm}\} \\ & V_{rf} \ 400|800\text{MHz}{=}1.87\text{GV}|8.19\text{GV}, \ Q_{x|y|s}{=}\{350.205, \ 266.294, \ 0.095\}, \ \text{Crab} \ \text{waist}{=}40\% \end{split}$$



$$\begin{split} & \text{LCC}_V24.3 \mid \text{E}_{\text{beam}}{=}182.5 \text{ GeV}, \text{I}_{\text{beam}}{=}5\text{mA} (\text{N}{=}1.77\text{E}{+}11\text{ppb}), \text{ 50 turns} \\ & \epsilon_x{=}2.12\text{nm.rad}, \epsilon_y/\epsilon_x = 2\%, \sigma_{\delta}{=}0.148\%, \sigma_z{=}2.1\text{nm}, \beta_{x,y}^*{=}\{1.00\text{m}, 1.6\text{nm}\} \\ & \text{V}_{rf} 400|800\text{MHz}{=}1.87\text{GV}|8.19\text{GV}, Q_{x|y|s}{=}\{350.205, 266.294, 0.095\}, \text{Crab waist}{=}40\% \end{split}$$



Single RF section **15%** lower total RF voltage

$$\begin{split} & \text{LCC}_V24.3 \mid \text{E}_{\text{beam}}=182.5 \text{ GeV}, \text{ I}_{\text{beam}}=5\text{mA} (\text{N}=1.77\text{E}+11\text{ppb}), 50 \text{ turns} \\ & \epsilon_x=2.12\text{nm.rad}, \epsilon_y/\epsilon_x=2\infty, \ \sigma_{\sigma}=0.148\%, \ \sigma_z=2.4\text{mm}, \ \beta_{x,y}^*=\{1.00\text{m}, \ 1.6\text{mm}\} \\ & \text{V}_{rf} \ 400|800\text{MHz}=1.78\text{GV}| 7.82\text{GV}, \ & \text{Q}_{x|y|s}=\{350.205, \ 266.294, \ 0.084\}, \ \text{Crab waist}=40\% \end{split}$$



LCC_V24.3 | E_{beam}=182.5 GeV, I_{beam}=5mA (N=1.77E+11ppb), 50 turns ϵ_x =2.12nm.rad, ϵ_y/ϵ_x =2%, σ_σ =0.148%, σ_z =2.4mm, $\beta^*_{x,y}$ ={1.00m, 1.6mm} V_{rf} 400|800MHz=1.78GV|7.82GV, Q_{xivis}={350.205, 266.294, 0.084}, Crab waist=40%



MA comparison between SAD and Xsuite for the V24 version of the GHC lattice V24



GHC V24 | E_{beam}=45.6 GeV, I_{beam}=1282mA (N=2.16E+11ppb), 512 turns $\epsilon_x = 0.70$ nm.rad, $\epsilon_y / \epsilon_x = 2$ ‰, $\sigma_\delta = 0.039$ %, $\sigma_z = 5.5$ nm, $\beta_{x,y}^* = \{0.10$ m, 0.7 nm} V_{rf} 400|800MHz=0.08GV|0.00GV, Q_{x|y|s}={218.156, 222.199, 0.029}, Crab waist=70%



GHC_V24 | E_{beam}=120.0 GeV, I_{beam}=26mA (N=1.70E+11ppb), 150 turns $\epsilon_x = 0.66$ nm.rad, $\epsilon_y / \epsilon_x = 2$ ‰, $\sigma_\delta = 0.104$ %, $\sigma_z = 3.2$ nm, $\beta_{x,y}^* = \{0.20$ m, 1.0 nm} V_{rf} 400|800MHz=2.09GV|0.00GV, Q_{x|y|s}={398.138, 398.208, 0.033}, Crab waist=50%



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GHC_V24 | E_{beam}=182.5 GeV, I_{beam}=5mA (N=1.47E+11ppb), 50 turns $\epsilon_x = 1.51$ nm.rad, $\epsilon_y/\epsilon_x = 2$ %, $\sigma_{\delta} = 0.157$ %, $\sigma_z = 1.8$ nm, $\beta_{x,y}^* = \{0.90$ m, 1.4 nm} V_{rf} 400|800MHz=2.10GV|9.20GV, $Q_{x|y|s}$ ={398.138, 398.208, 0.089}, Crab waist=40%





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Differences between Xsuite and SAD (LCC)

- I spotted differences with the variable cs_comp that is not used (at least in the converted MADX file, Oide-san sent me.)
- DA recomputed without decapoles and cs_comp = 0 that would explain the differences observed with and without crab sextupoles as the decapoles are turned on also without crab waist.



Relaxed optics DA/MA



$$\begin{split} & \text{LCC_V24.3} \mid \text{E}_{\text{beam}} = 45.6 \text{ GeV}, \text{ } \text{I}_{\text{beam}} = 1456\text{mA} \text{ } (\text{N} = 2.45\text{E} + 11\text{ppb}), \text{ } 512 \text{ turns} \\ & \epsilon_x = 0.68\text{nm.rad}, \ \epsilon_y / \epsilon_x = 2\%, \ \sigma_\delta = 0.037\%, \ \sigma_z = 5.2\text{nm}, \ \beta_{x,y}^* = \{0.30\text{m}, \ 2.5\text{mm}\} \\ & \text{V}_{rf} \text{ } 400|800\text{MHz} = 0.08\text{GV}|0.00\text{GV}, \ Q_{x|y|s} = \{198.200, \ 174.300, \ 0.030\}, \text{ Crab waist} = 0\% \end{split}$$



20

10

-10

-20-

-1.5

-40

-1.0

-30

-0.5

-10

-20

 $A_{\chi}(\phi)$

amplitude

Normalised

 $\begin{array}{l} GHC_V23 \mid E_{beam}{=}45.6 \; GeV, \; I_{beam}{=}1282mA \; (N{=}2.16E{+}11ppb), \; 512 \; turns \\ \epsilon_x{=}0.70nm.rad, \; \epsilon_y/\epsilon_x {=} 2\%, \; \sigma_{\sigma}{=}0.039\%, \; \sigma_z{=}5.5mm, \; \beta_{x,\;y}^{*}{=}\{0.10m,\; 0.7mm\} \\ V_{rf}\; 400|800MHz{=}0.08GV|0.00GV, \; Q_{x|y|s}{=}\{218.156,\; 222.199,\; 0.029\}. \; Crab \; waist{=}0\% \end{array}$



$$\label{eq:GHC_V24} \begin{split} & \mbox{GHC_V24} \mid \mbox{E}_{beam} = 45.6 \mbox{ GeV}, \mbox{ } \mbox{I}_{beam} = 1282 \mbox{mA} \mbox{ (N=2.16E+11ppb)}, \mbox{ 512 turns} \\ & \mbox{ } \mbox{$$



LCC_V24.3 | E_{beam} =45.6 GeV, I_{beam} =1456mA (N=2.45E+11ppb), 512 turns ϵ_x =0.68nm.rad, ϵ_y/ϵ_x = 2‰, σ_o =0.037%, σ_z =5.2mm, $\beta_{x,y}^*$ ={0.30m, 7.0mm} V_{rf} 400|800MHz=0.08GV|0.00GV, $Q_{x|y|s}$ ={198.200, 174.300, 0.030}, Crab waist=0%

0.0

δ [%]

0

 $\delta [\sigma_5^{SR}]$

0.5

20

10

1.0

30

 $\varepsilon_x = 0.68$ nm.rad, $\varepsilon_y/\varepsilon_x = 2$ ‰, $\sigma_{\delta} = 0.037$ %, $\sigma_z = 5.2$ nm, $\beta_{x,y}^* = \{0.30$ m, 7.0 nm}

V_{rf} 400|800MHz=0.08GV|0.00GV, Q_{xlvls}={198.200, 174.300, 0.030}, Crab waist=0%

500

400

survived

- 200 5

- 100

1.5

40

 $\phi = 0$

 $\phi = \pi/4$

 $\phi = \pi/2$

 $\phi = 3\pi/4$