

# Accessing the strong interaction in three-hadron systems with ALICE

**Bhawani Singh**

Technical University of Munich (TUM), Germany

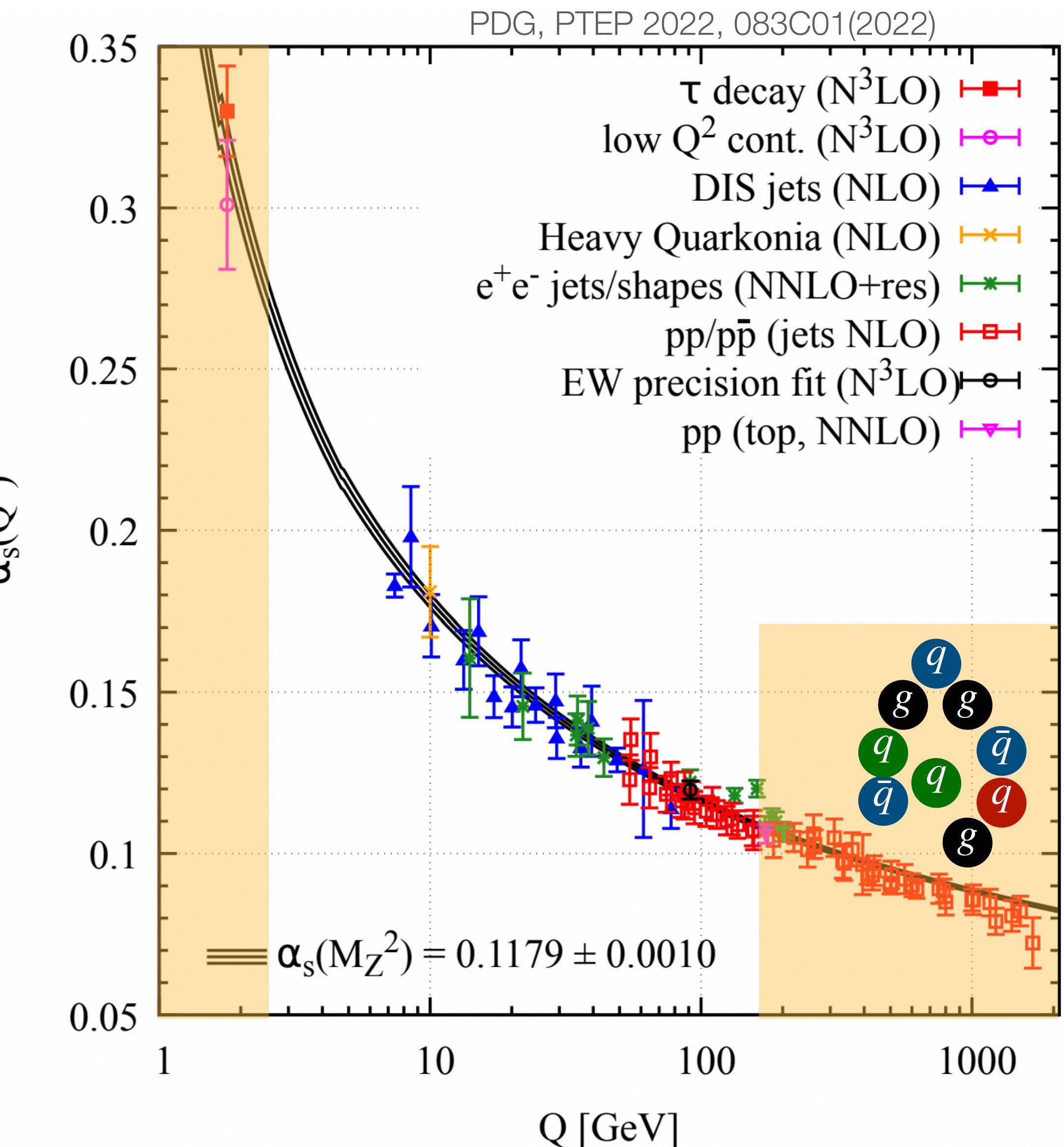
On behalf of the ALICE Collaboration (based on Phys. Rev. X 14, 031051 (2024))

**LHC Seminar, 26.11.2024**

✉ bhawani.singh@cern.ch

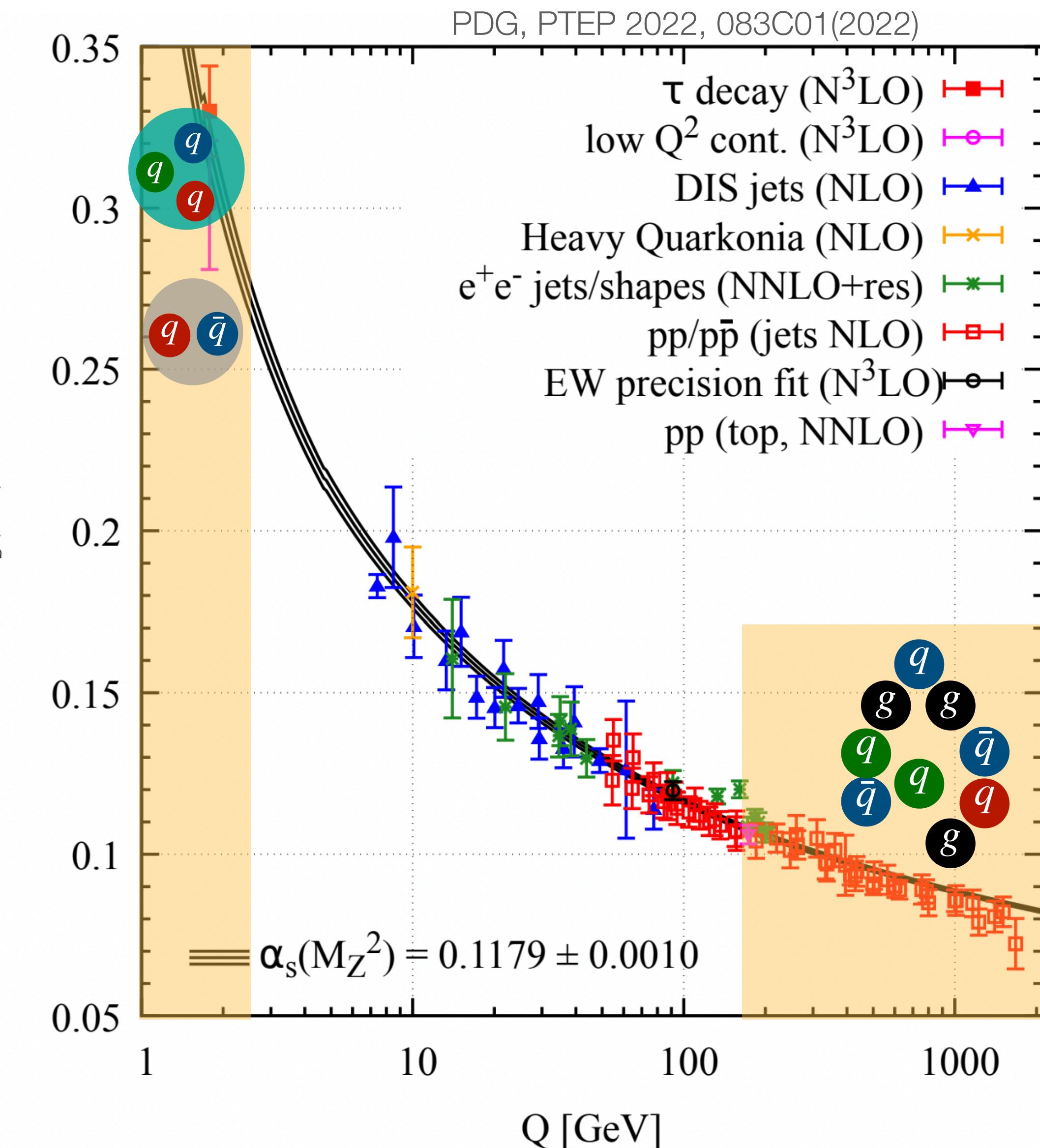
# Hadronic interactions and QCD

- Non-perturbative QCD  $\rightarrow Q \sim 1 \text{ GeV}$



# Hadronic interactions and QCD

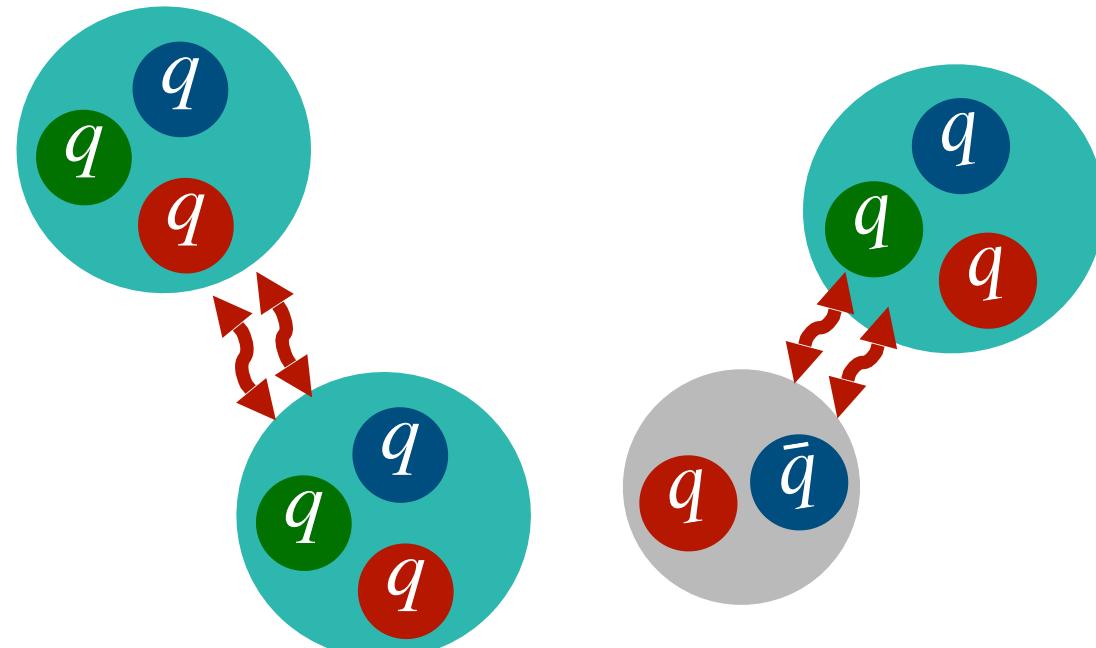
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- Use effective field theories (residual strong interaction)
  - Hadrons as degrees of freedom (baryons, mesons)



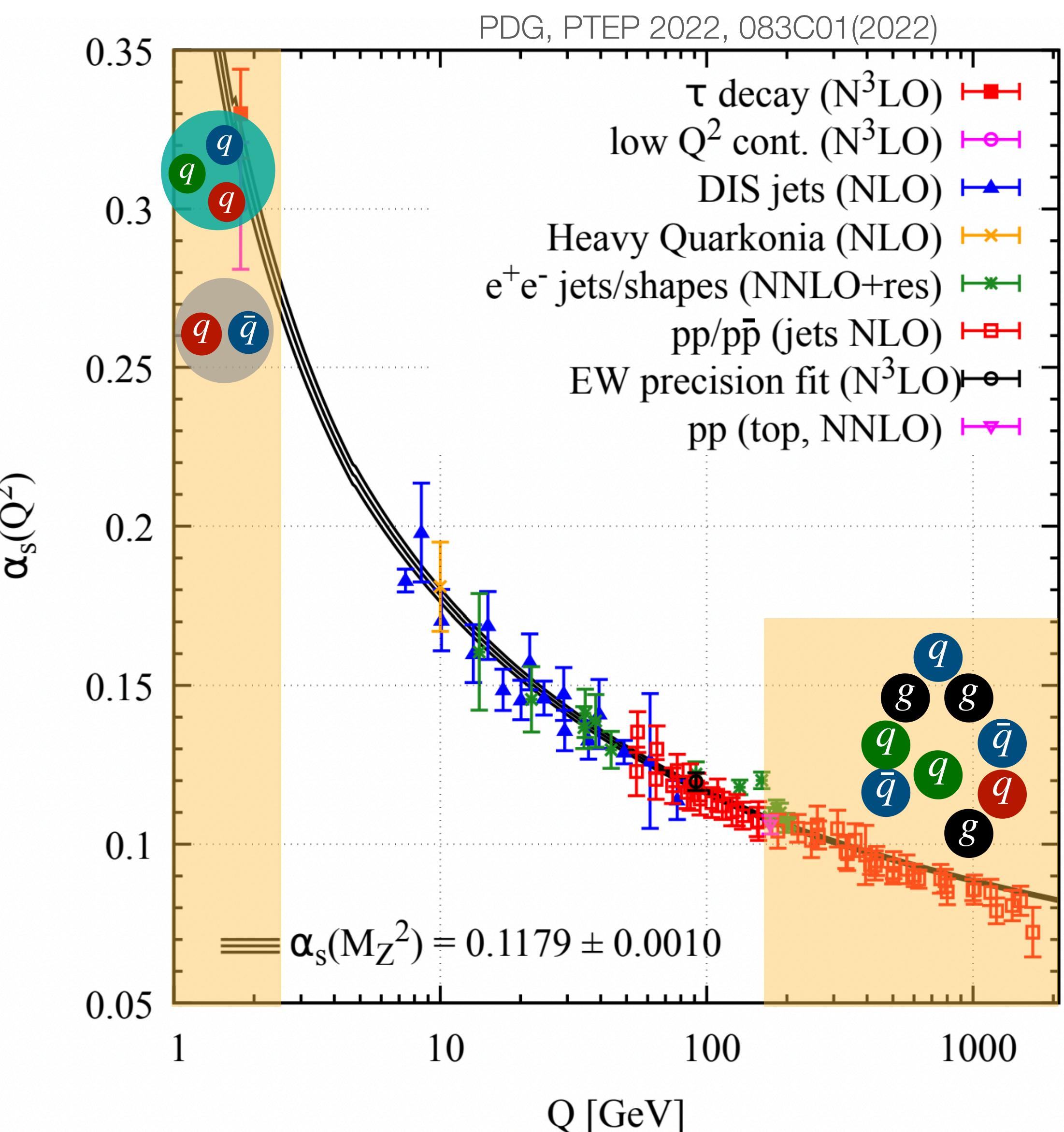
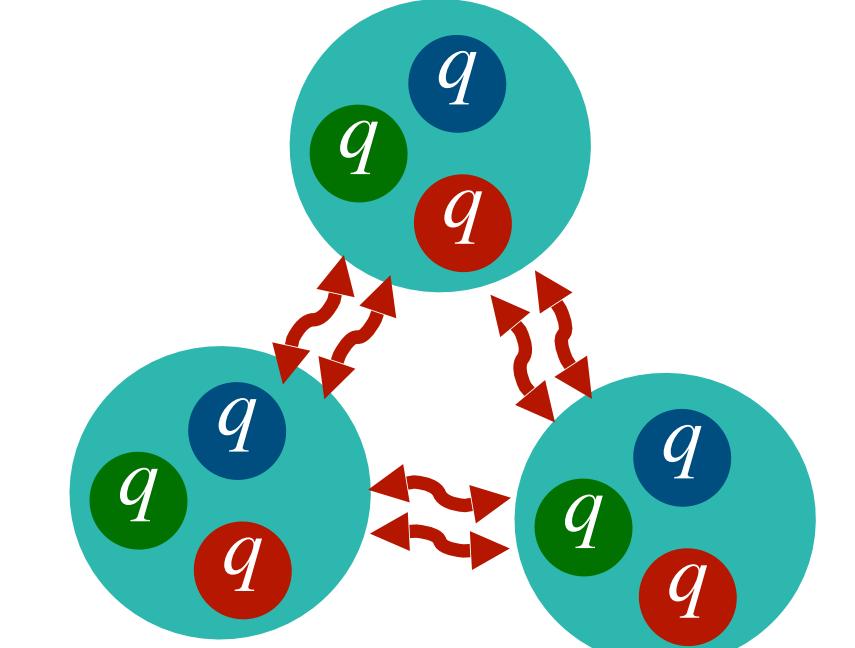
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  - Hadrons as degrees of freedom (baryons, mesons)
  - Need for experimental data of hadronic interactions
  - Constrain low-energy constants in the EFTs

Two-body interaction

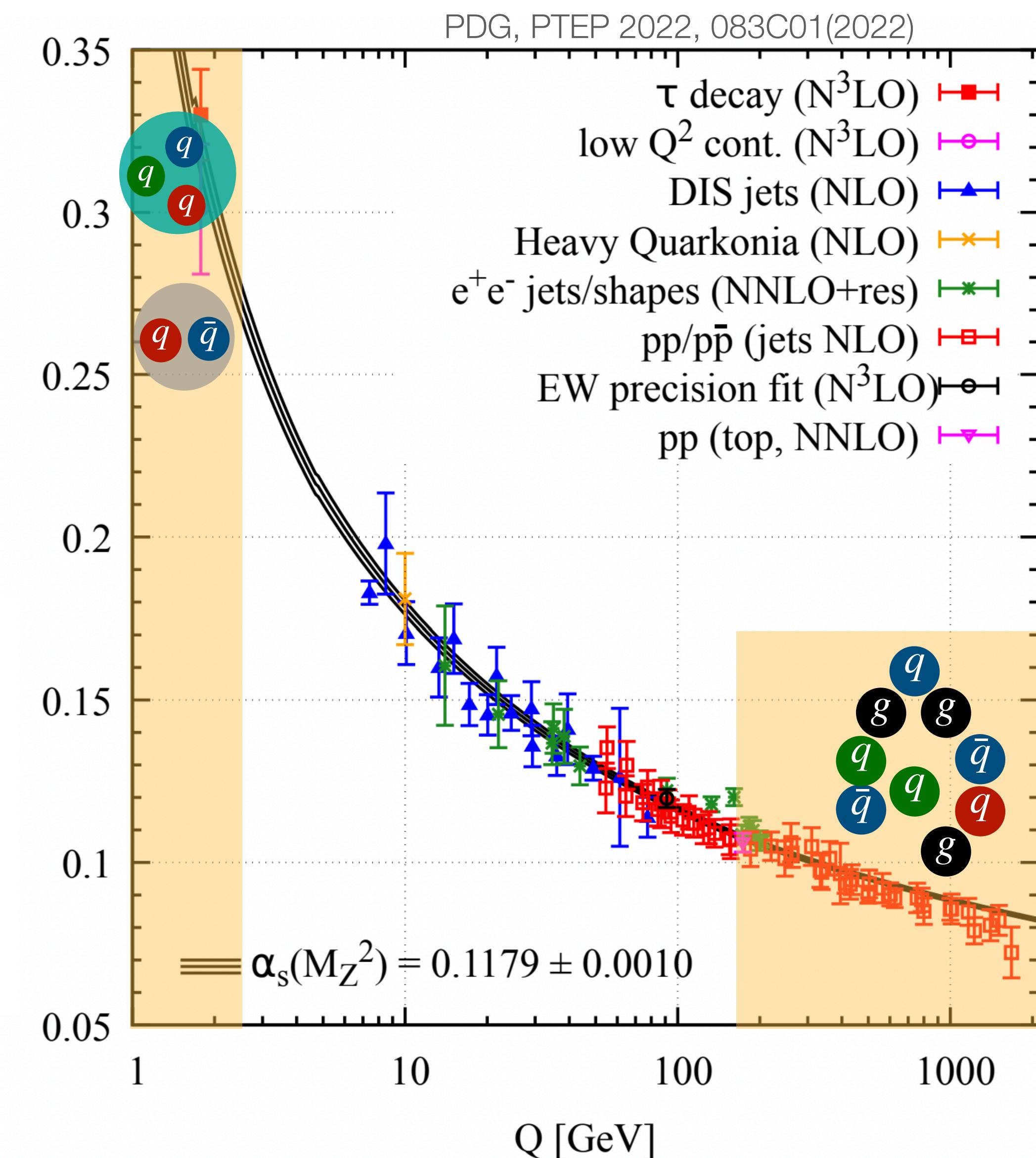
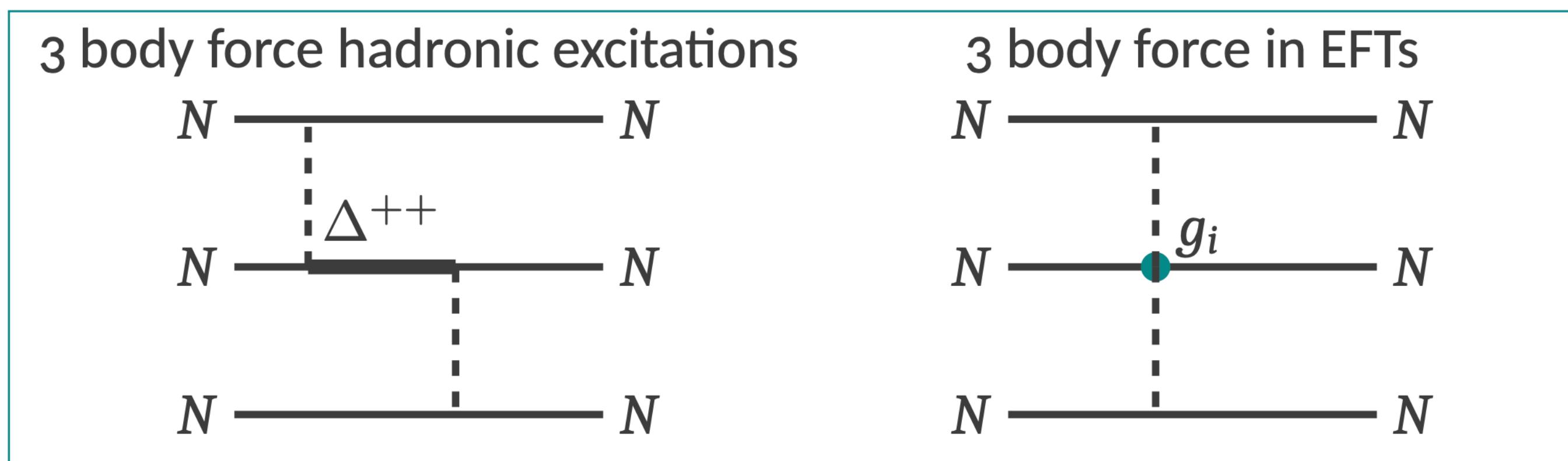


Many-body interaction



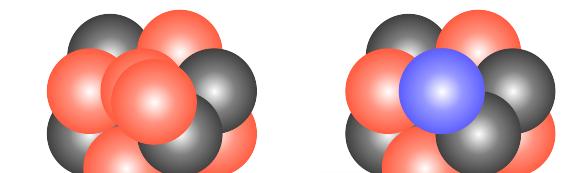
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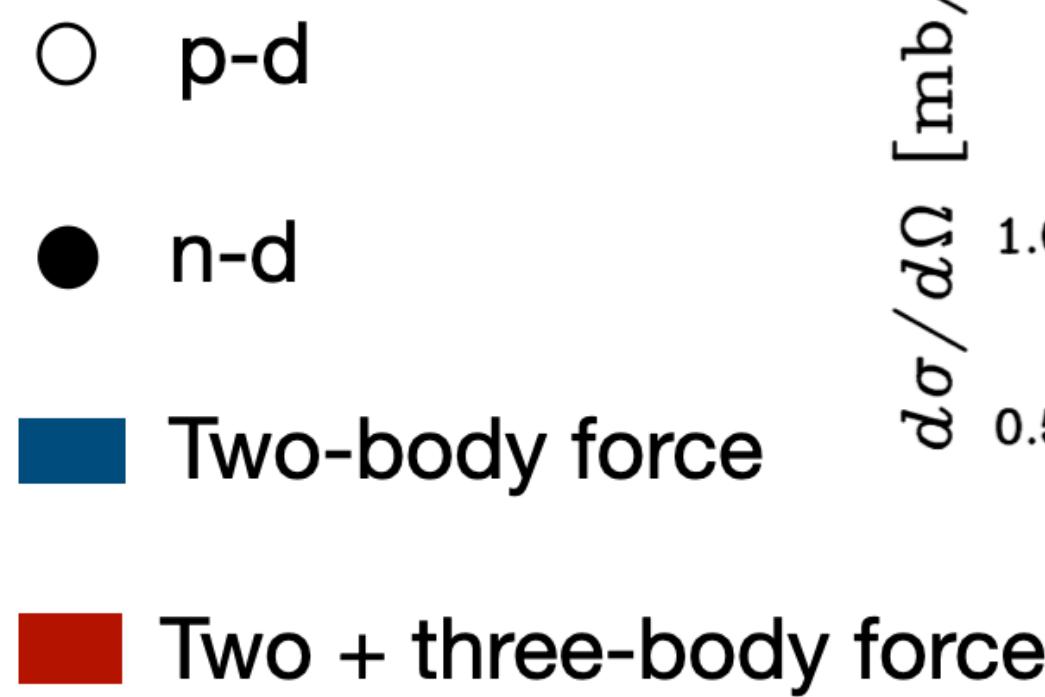
# Need for many-body hadronic interaction

Nuclei/hypernuclei

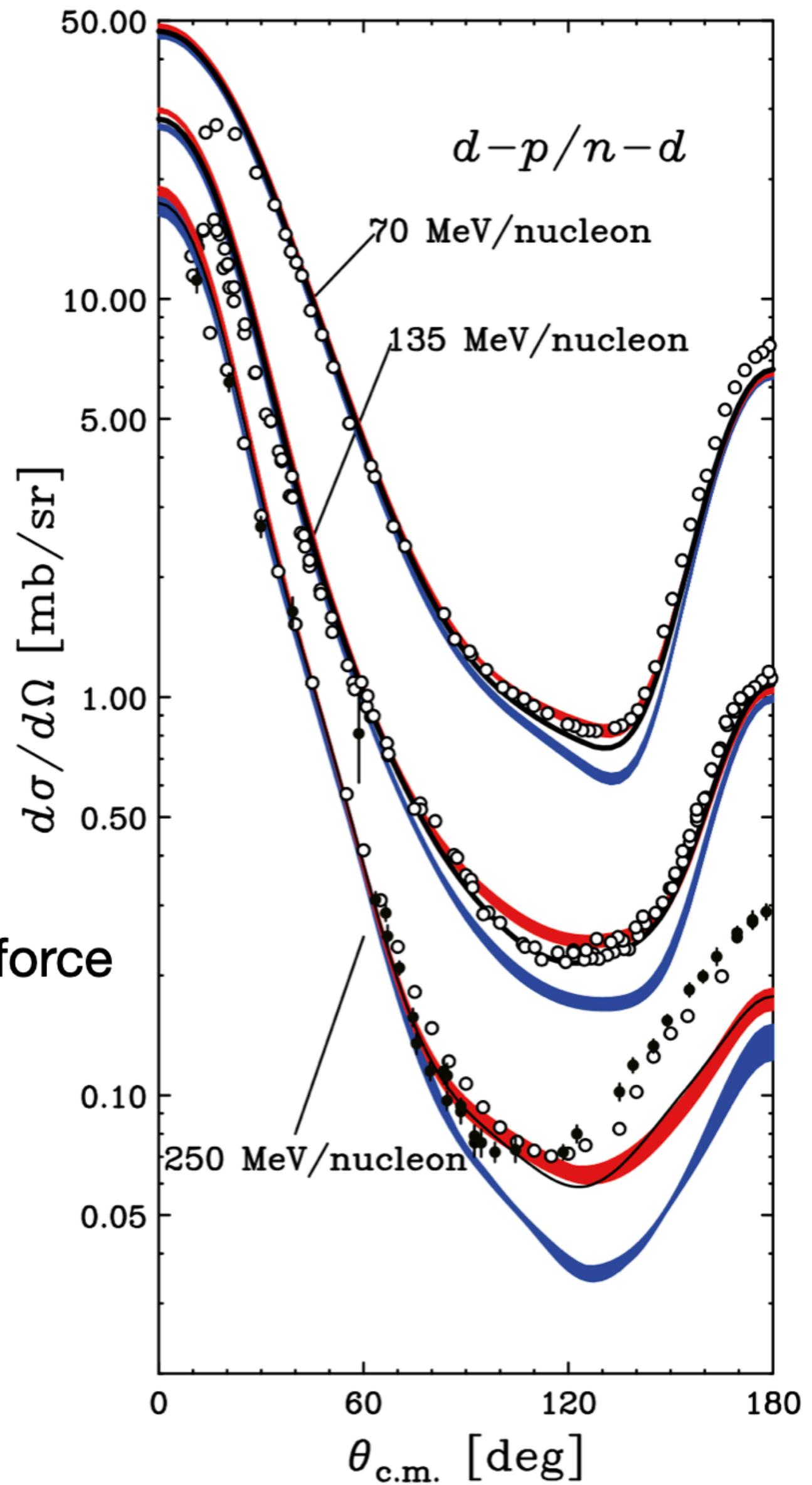


$\rho_0$

- Explanation for nucleon-deuteron scattering observables: requires the presence of three-body interaction<sup>[1]</sup>

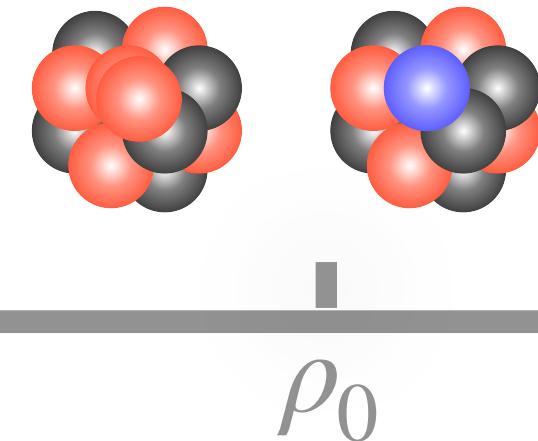


[1] K. Sekiguchi, Few-Body Syst 60, 56 (2019)

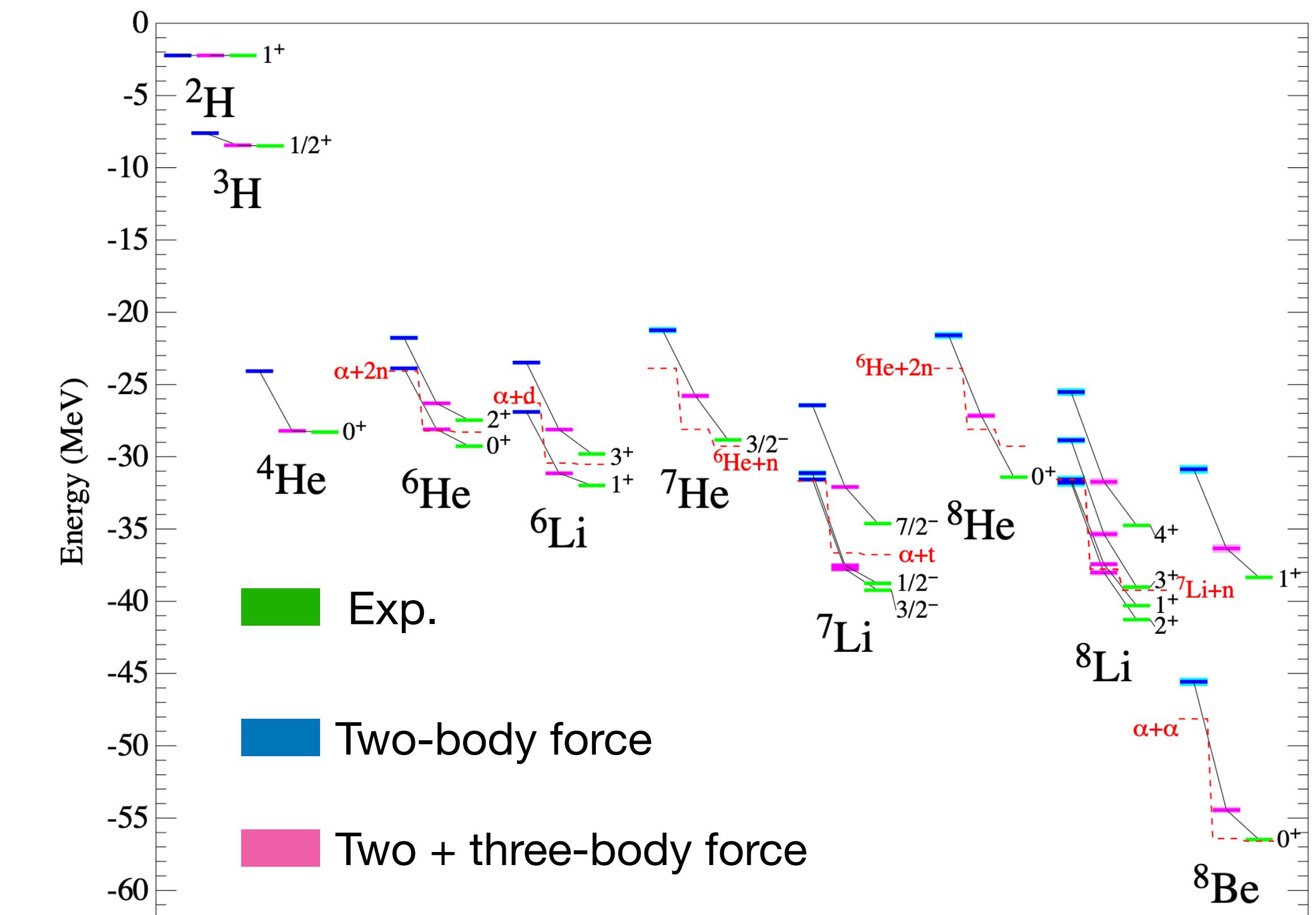


# Need for many-body hadronic interaction

Nuclei/hypernuclei



- Explanation for nucleon-deuteron scattering observables: requires the presence of three-body interaction<sup>[1]</sup>
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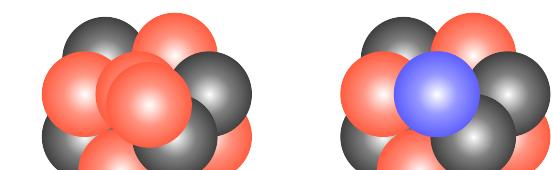


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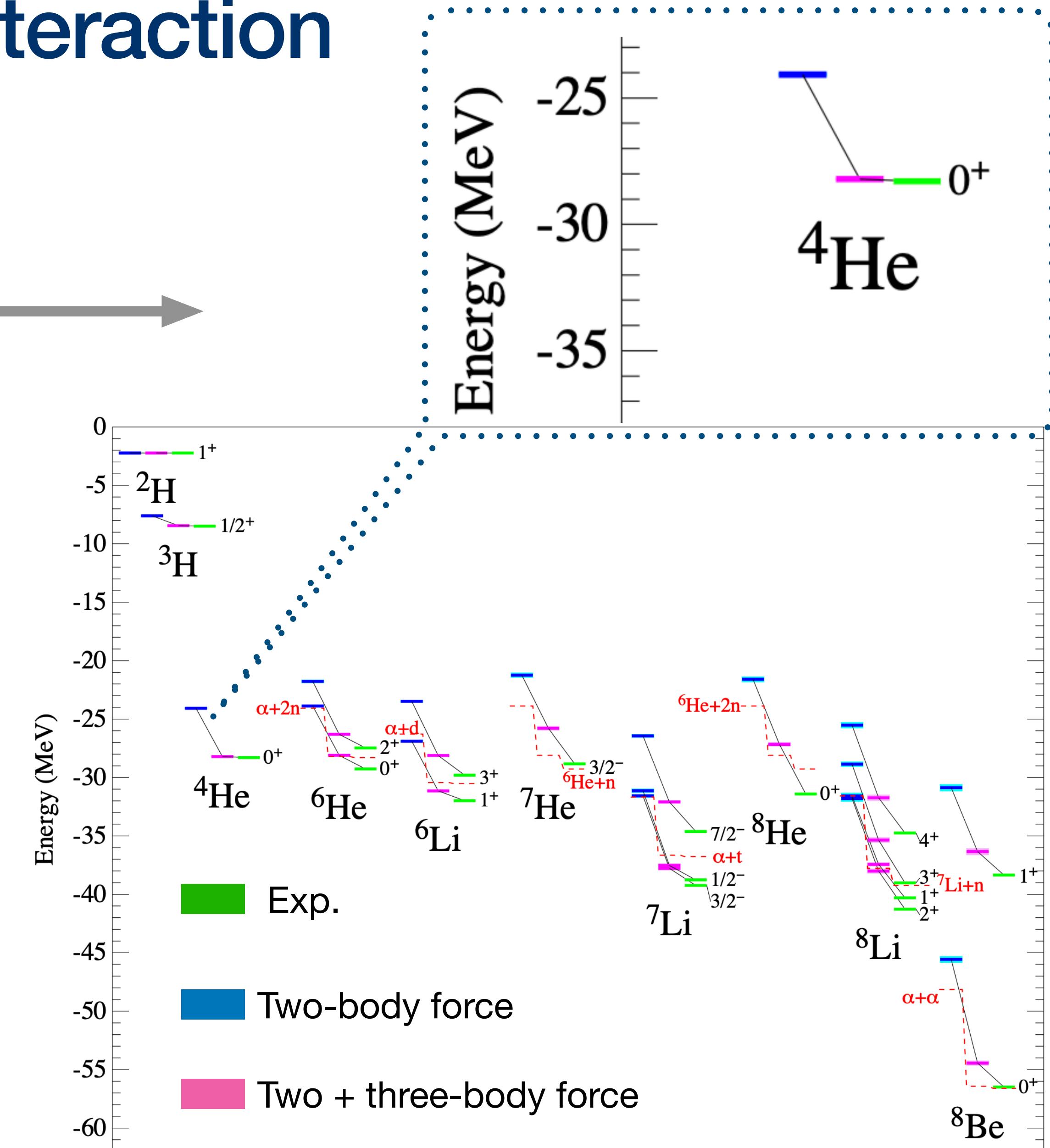


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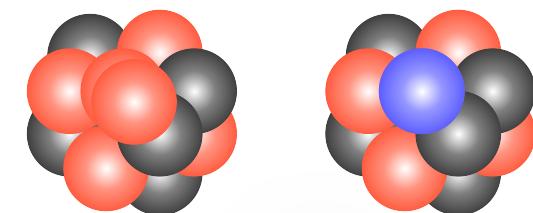
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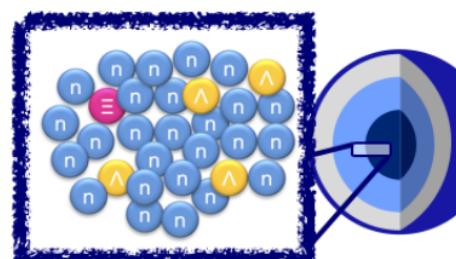
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$$\rho_0$$

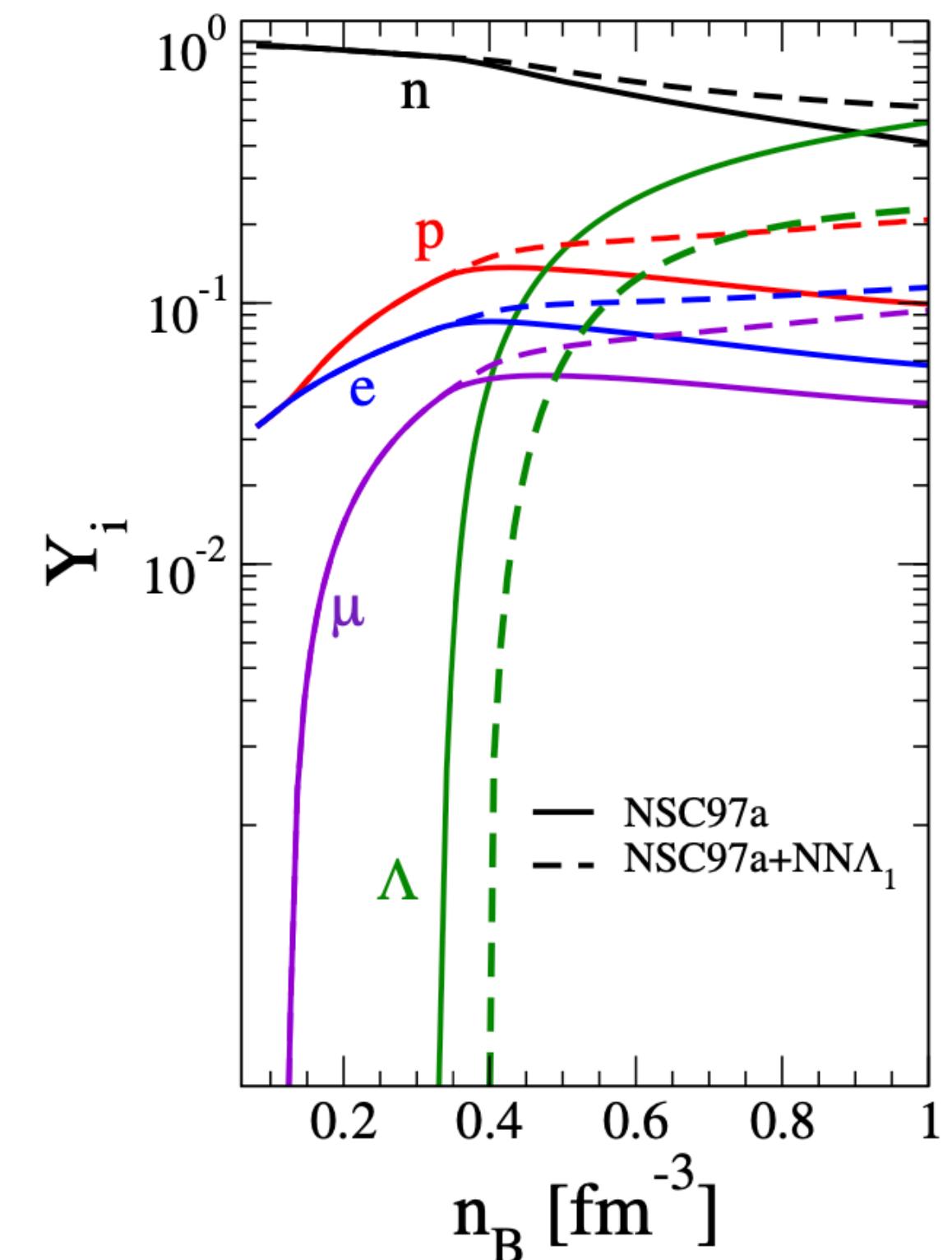
Dense nuclear matter: neutron star



$$3\rho_0$$



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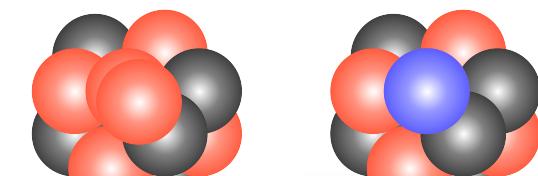
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[4] D. Logoteta et al, Eur. Phys. J. A (2019) 55: 207

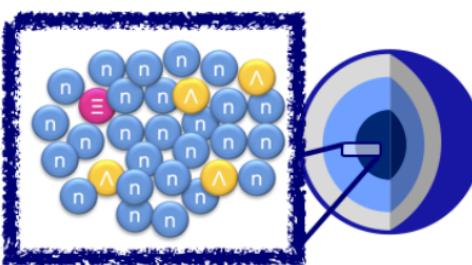
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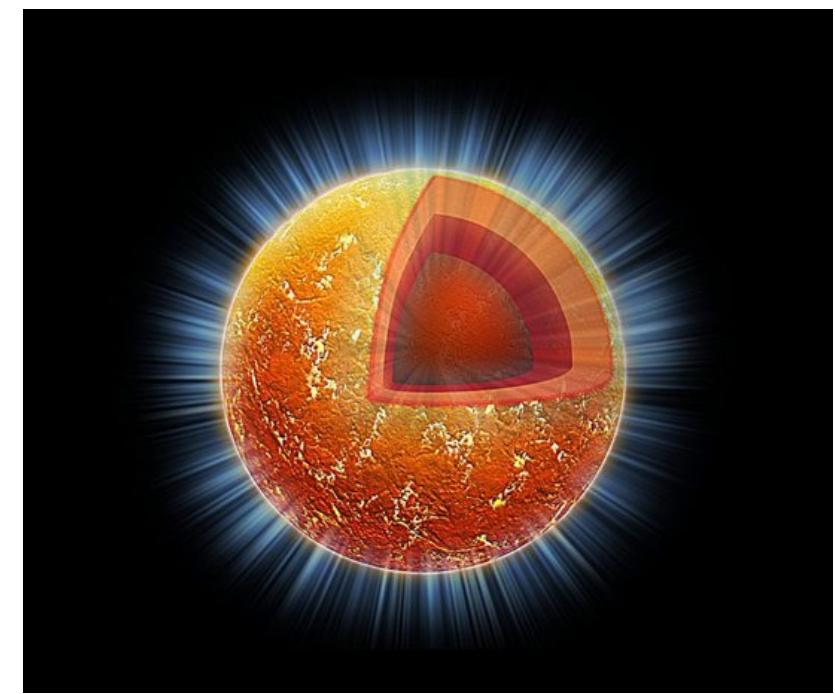


$\rho_0$

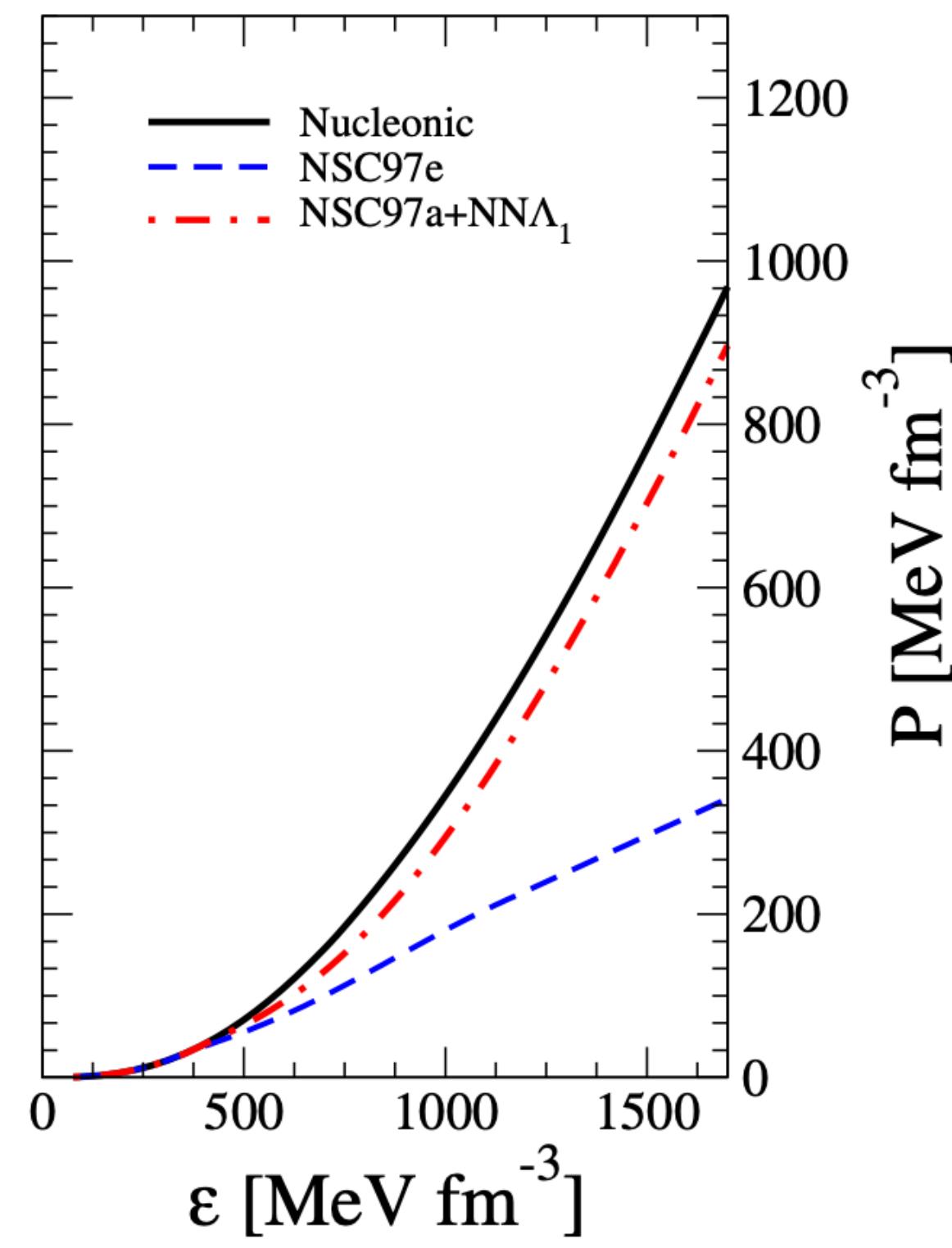
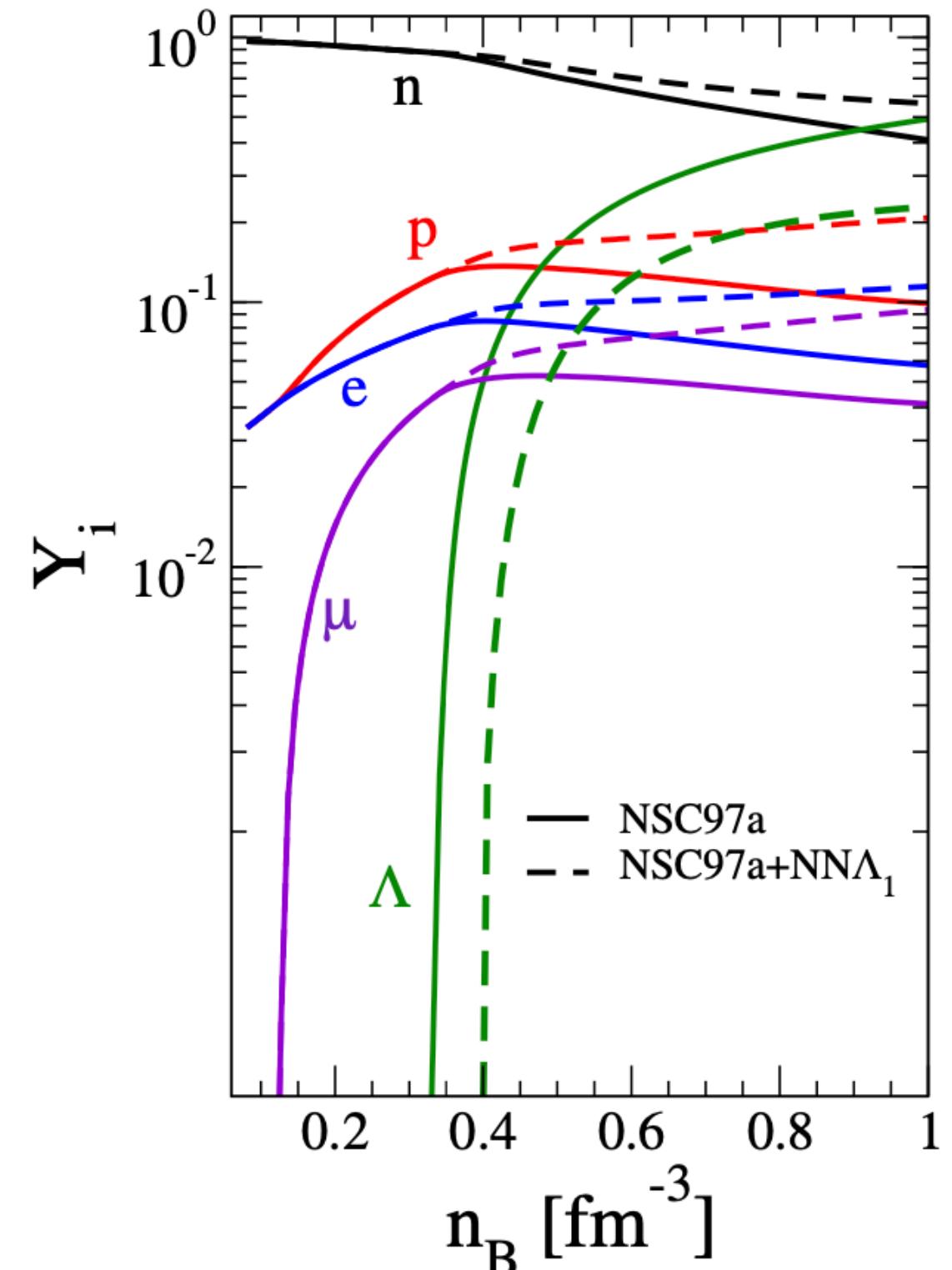
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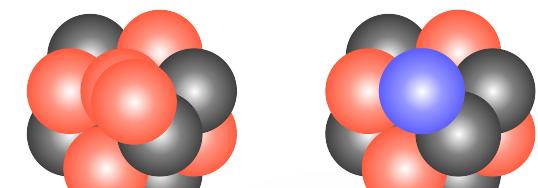
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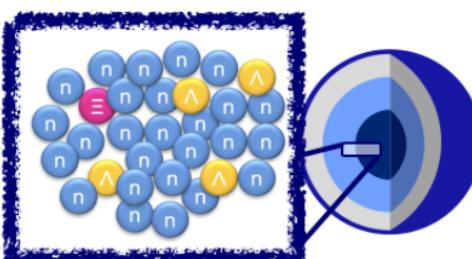
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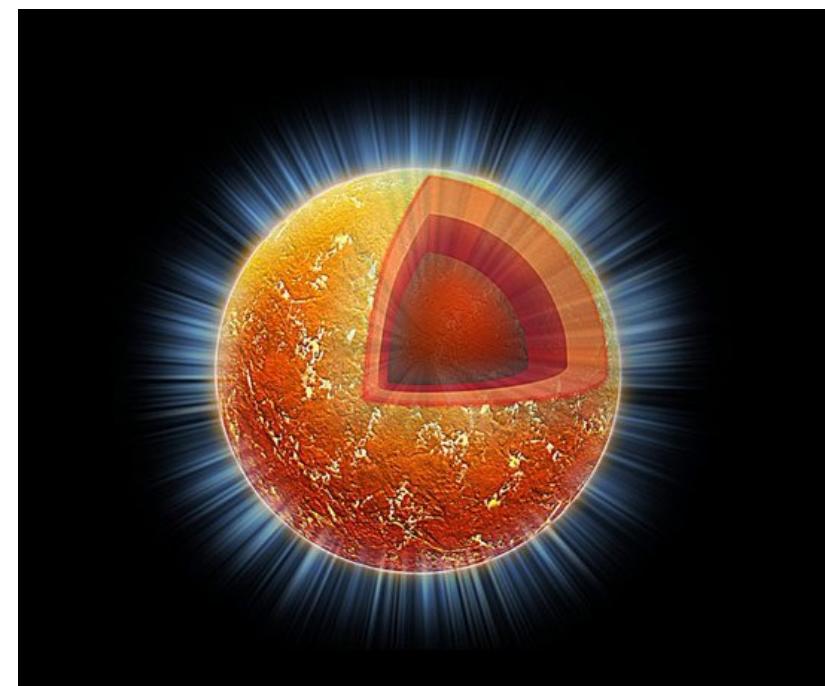


$\rho_0$

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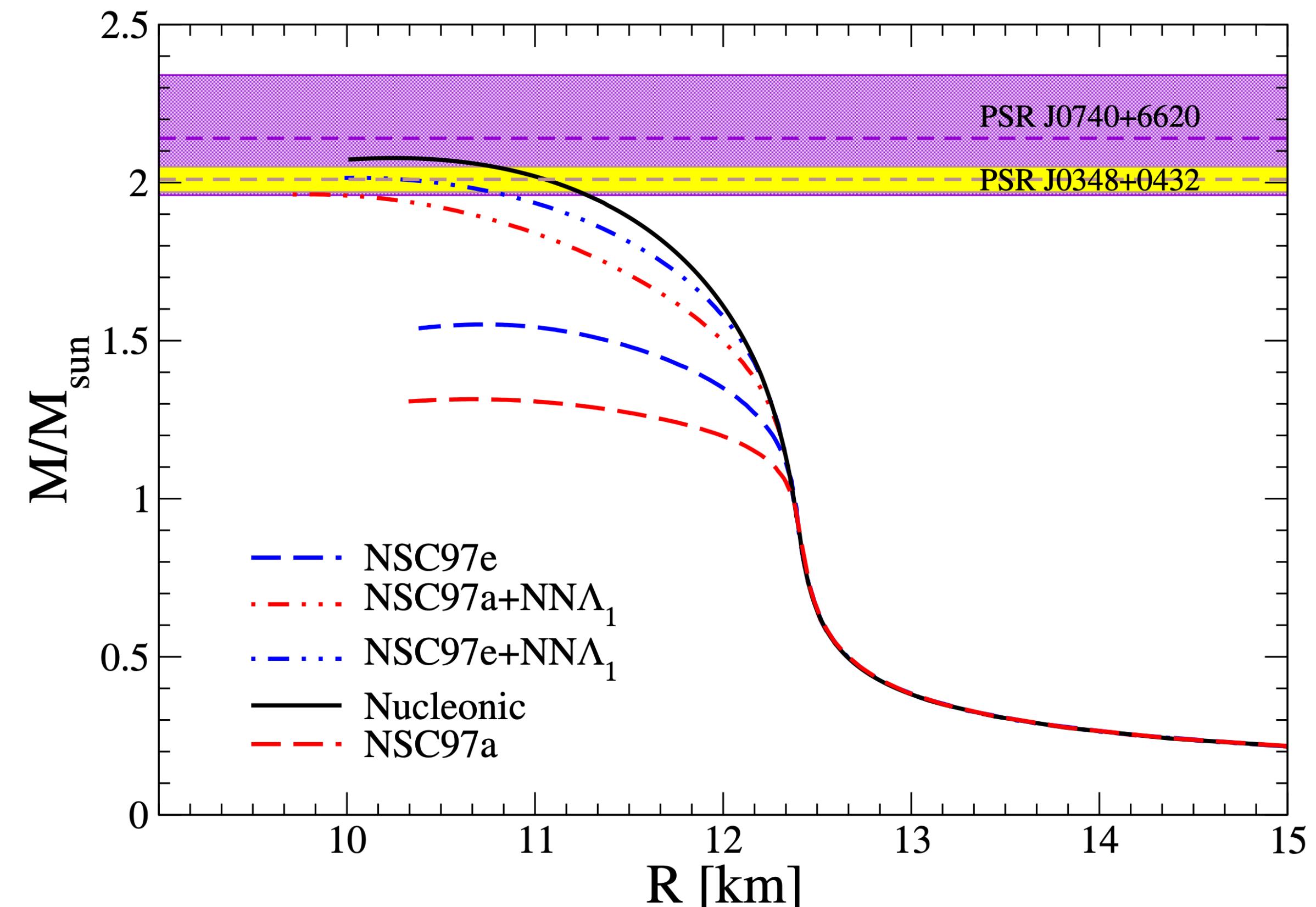
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- We need new tools to study three-body hadronic interaction

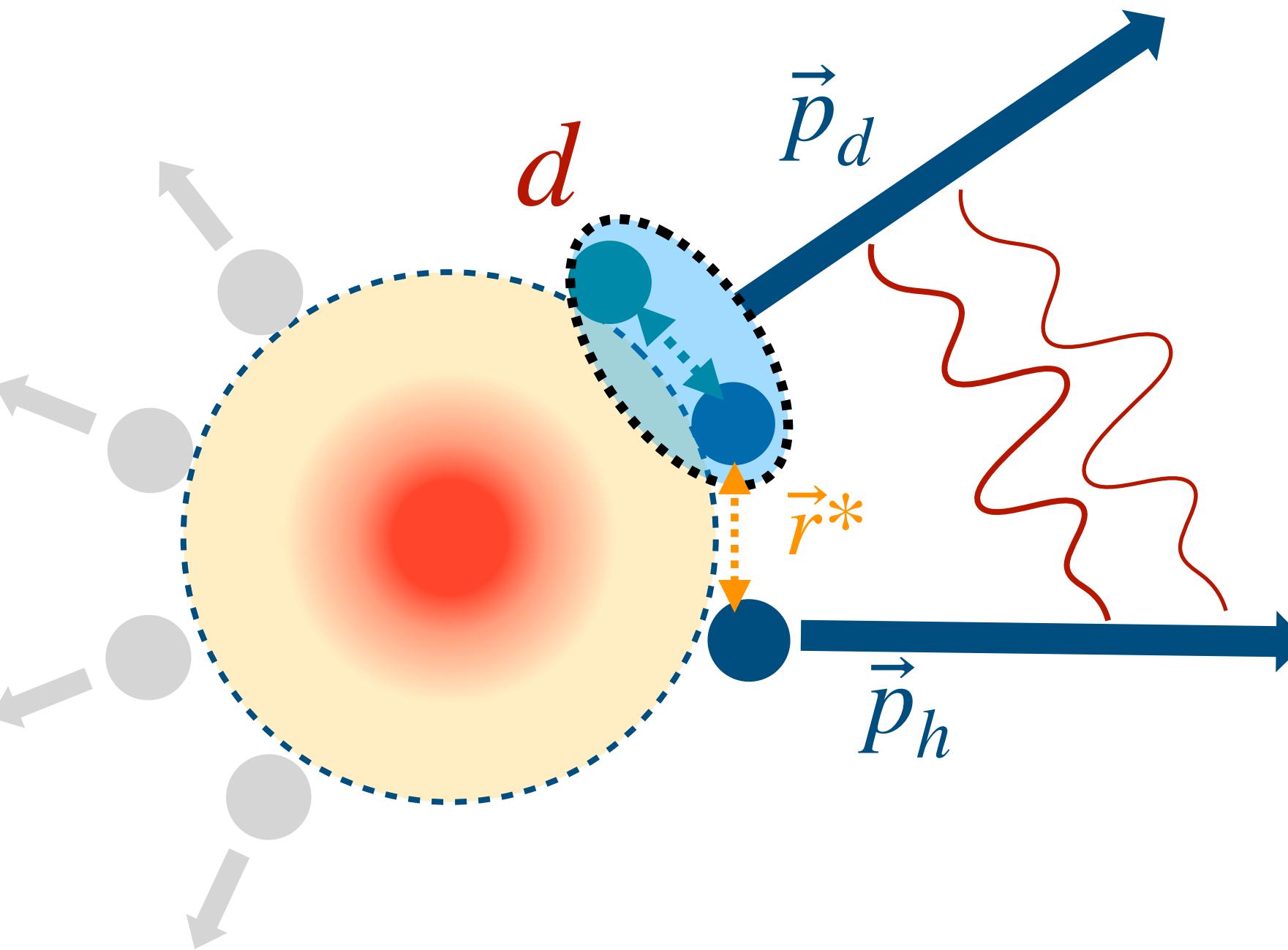
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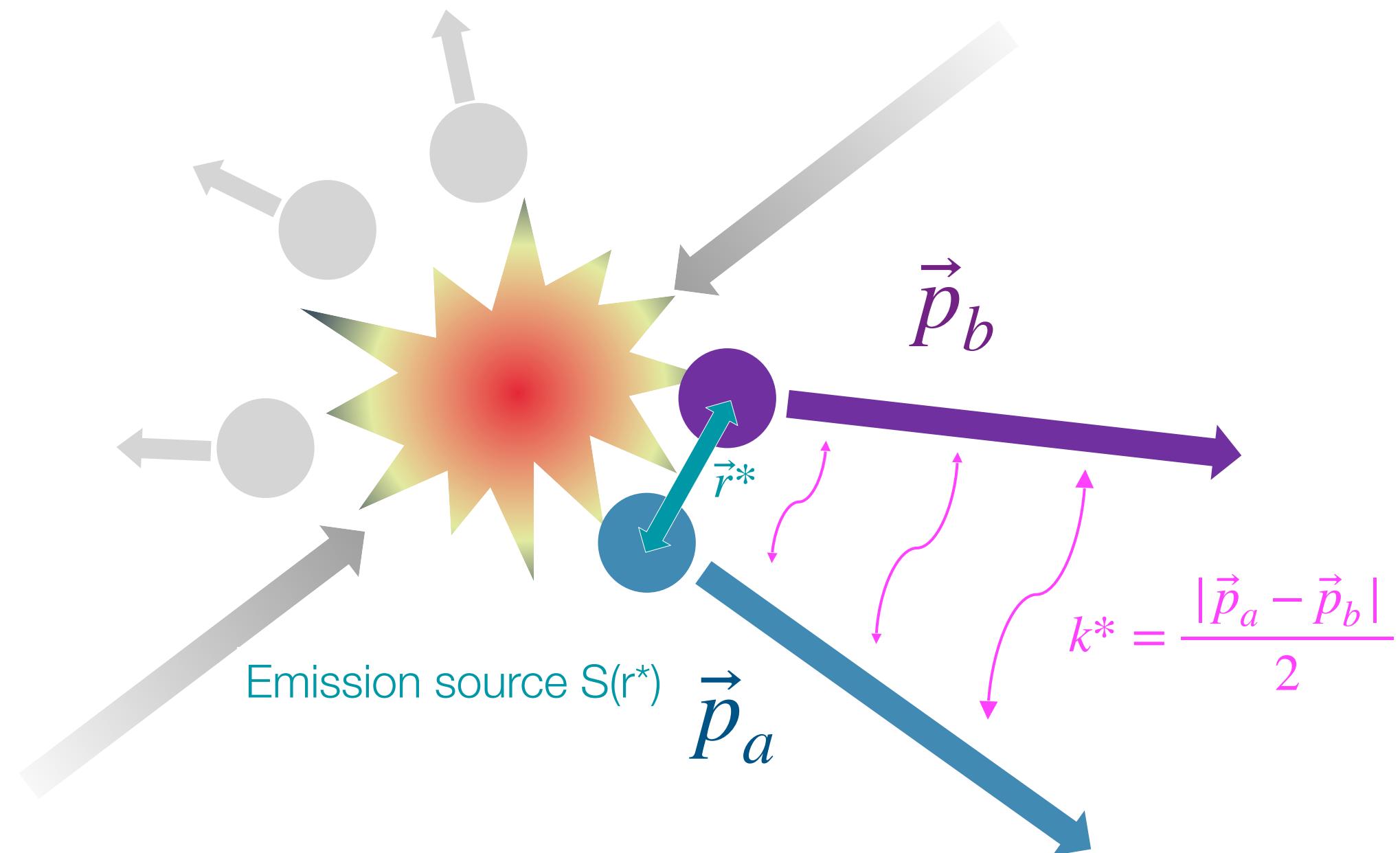
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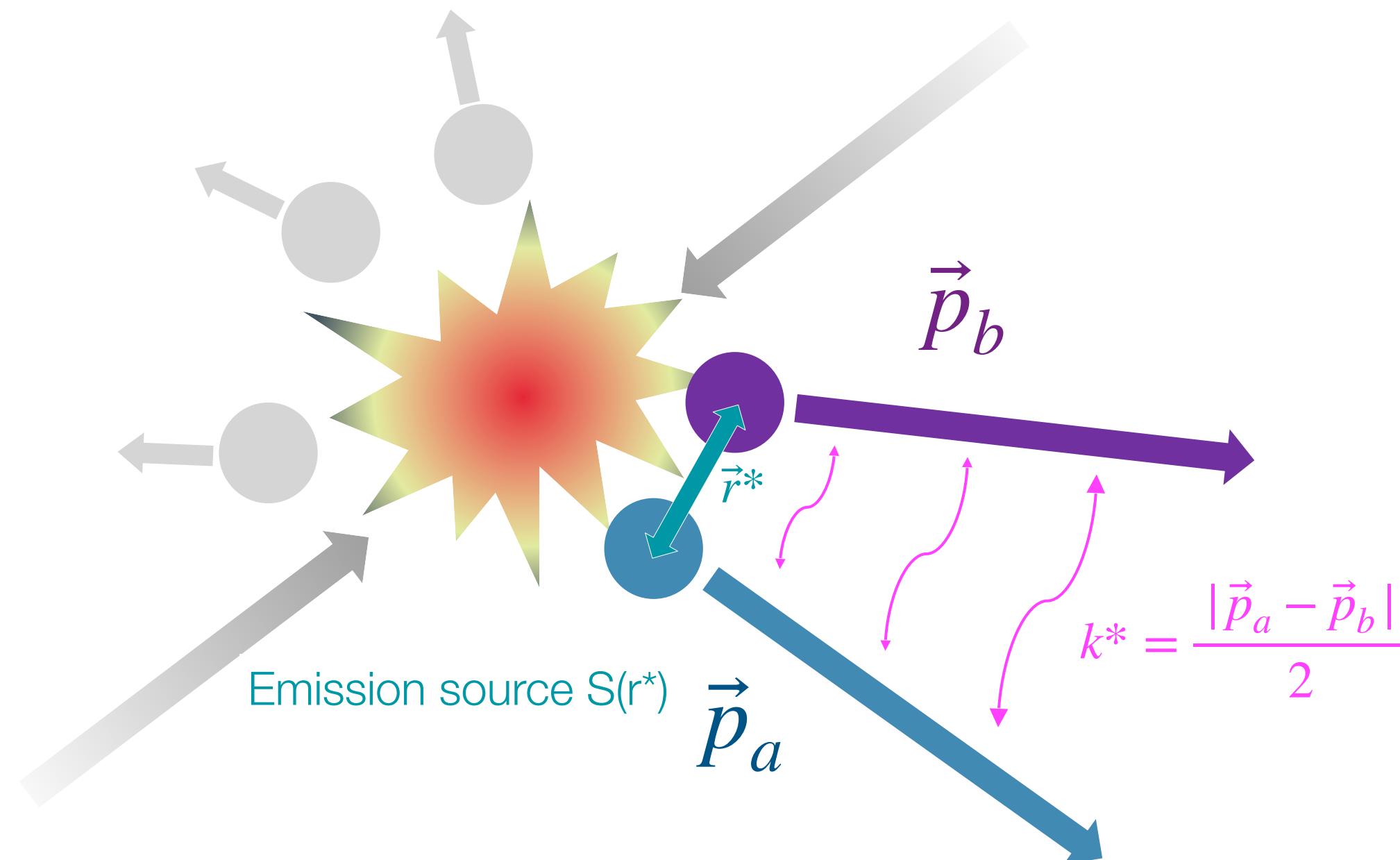


Access interaction three-hadron system with hadron-deuteron correlation

# Femtoscopy: momentum space correlations



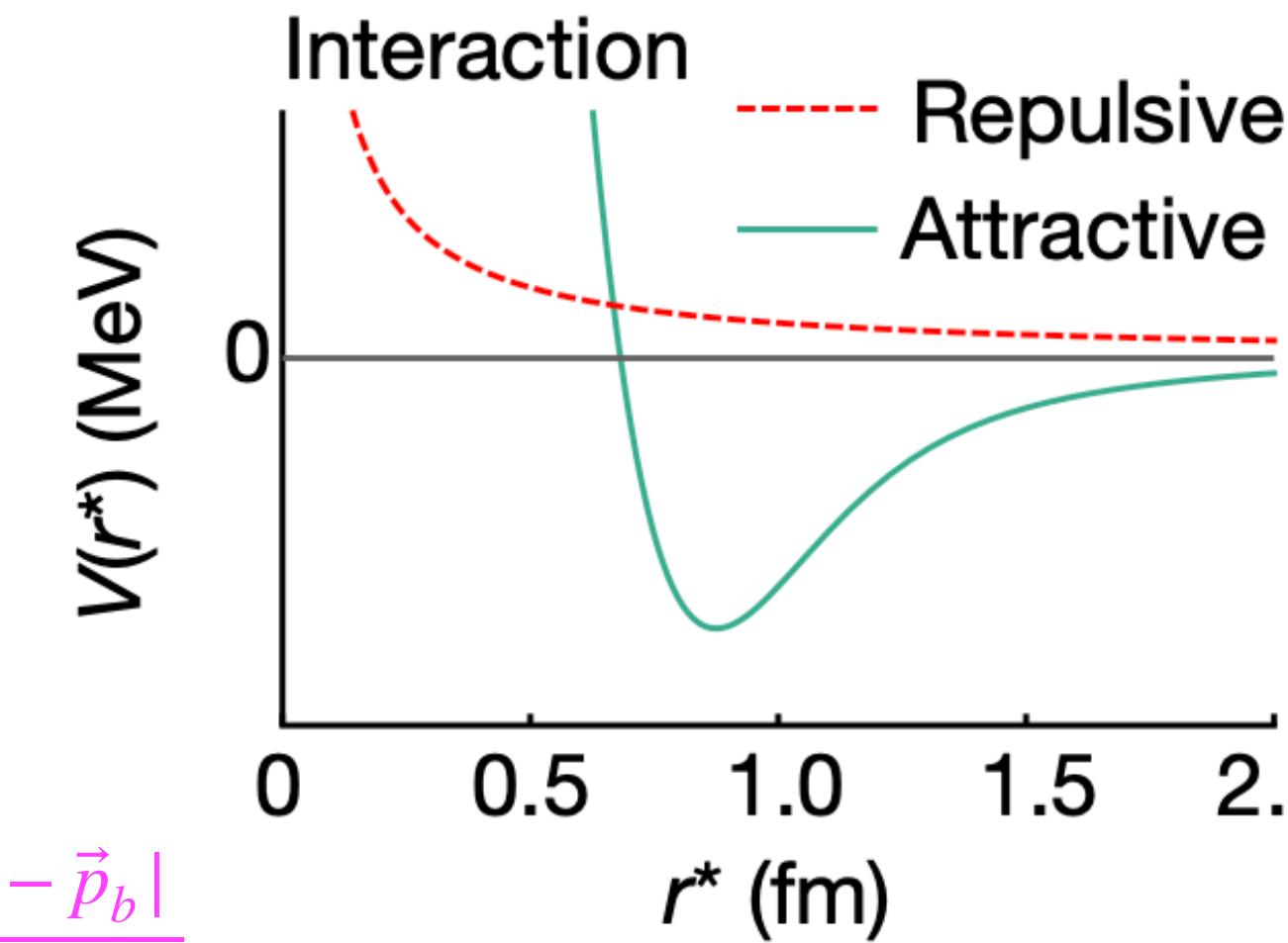
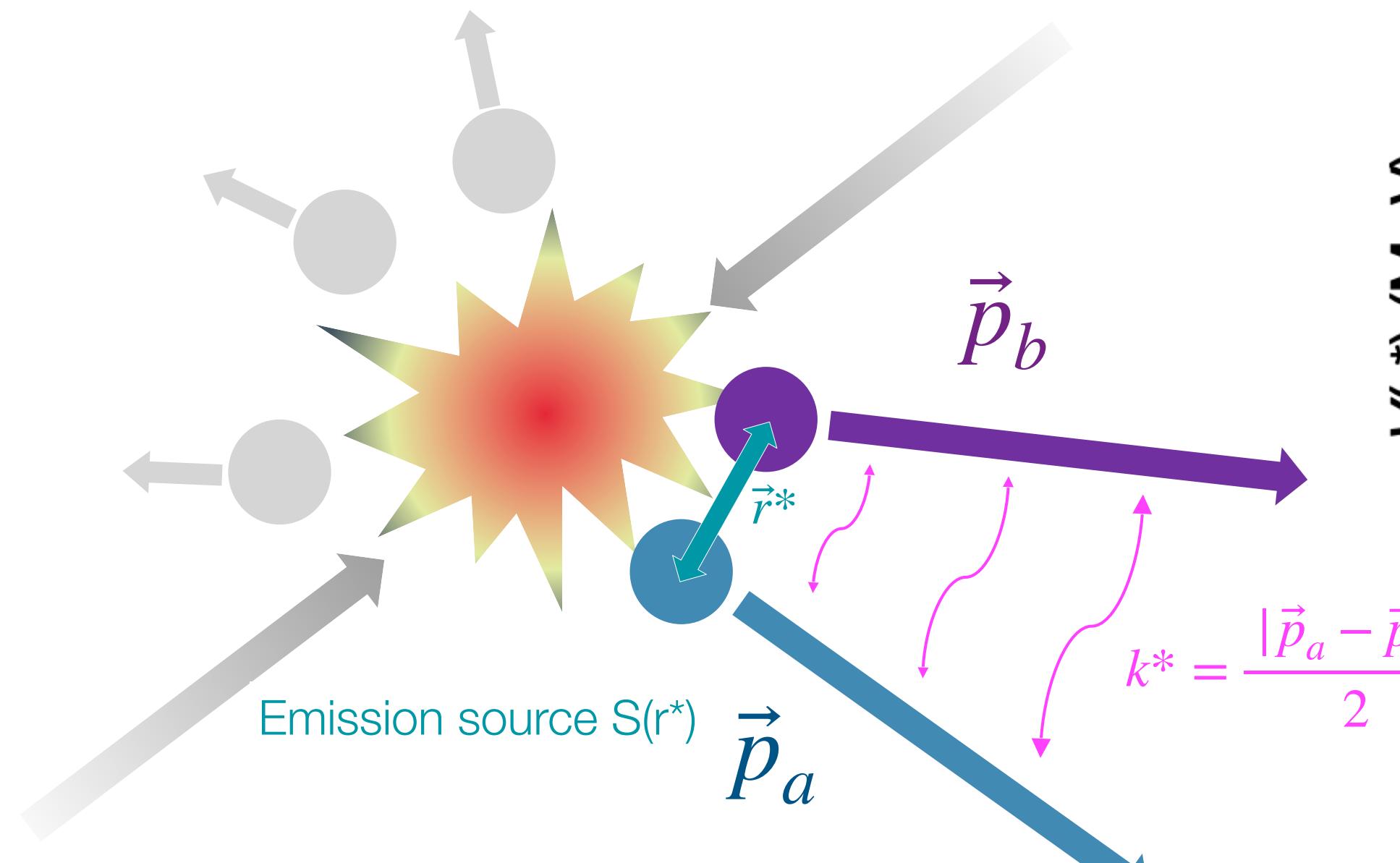
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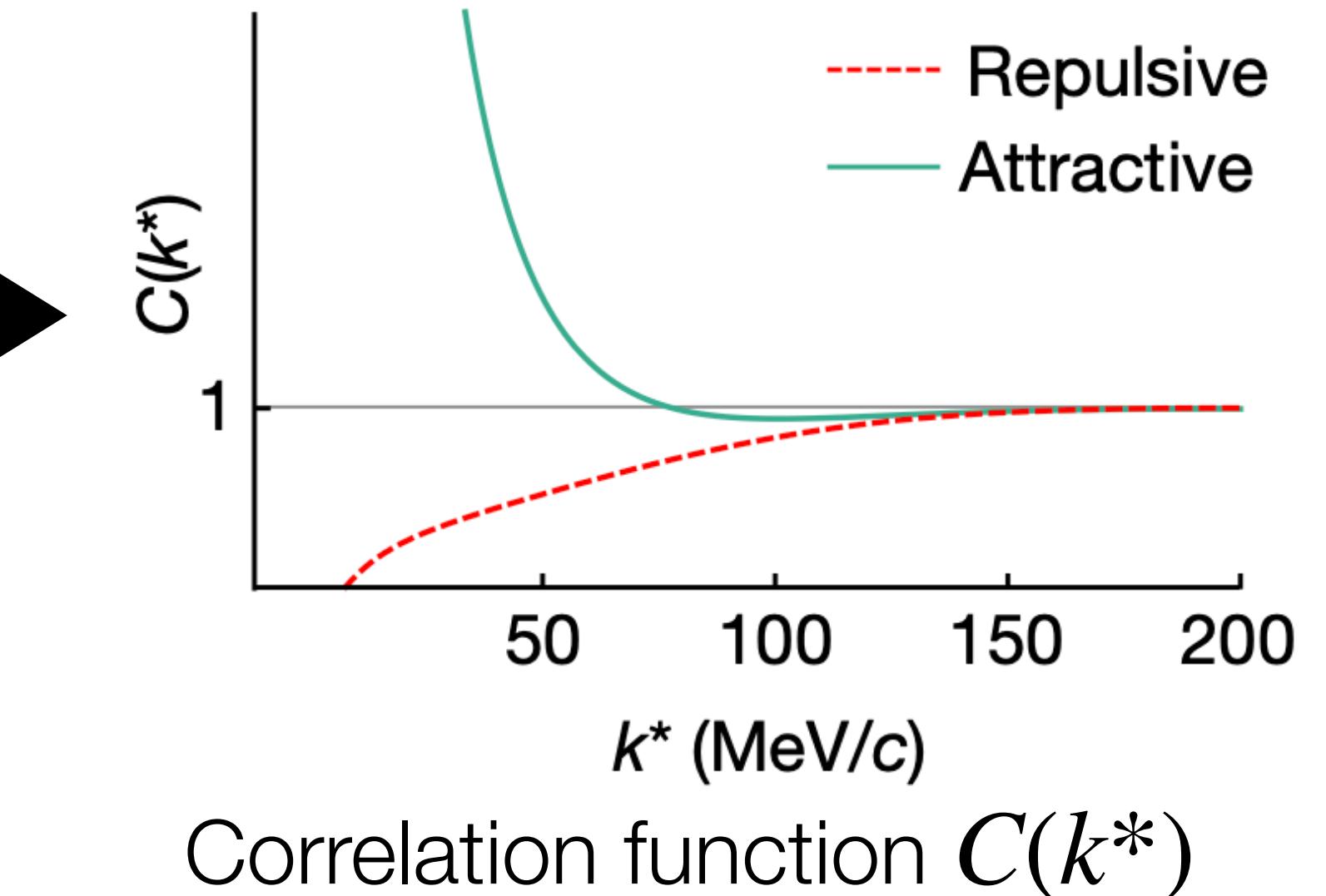
$$C(k^*) = \underbrace{\mathcal{N} \frac{N_{\text{same}}(k^*)}{N_{\text{mixed}}(k^*)}}_{\text{experimental definition}} = \underbrace{\int S(\vec{r}^*) \left| \psi(\vec{k}^*, \vec{r}^*) \right|^2 d^3 r^*}_{\text{theoretical definition}} \xrightarrow{k^* \rightarrow \infty} 1$$

S.E. Koonin et al, Phys. Lett. B 70 43 (1977)  
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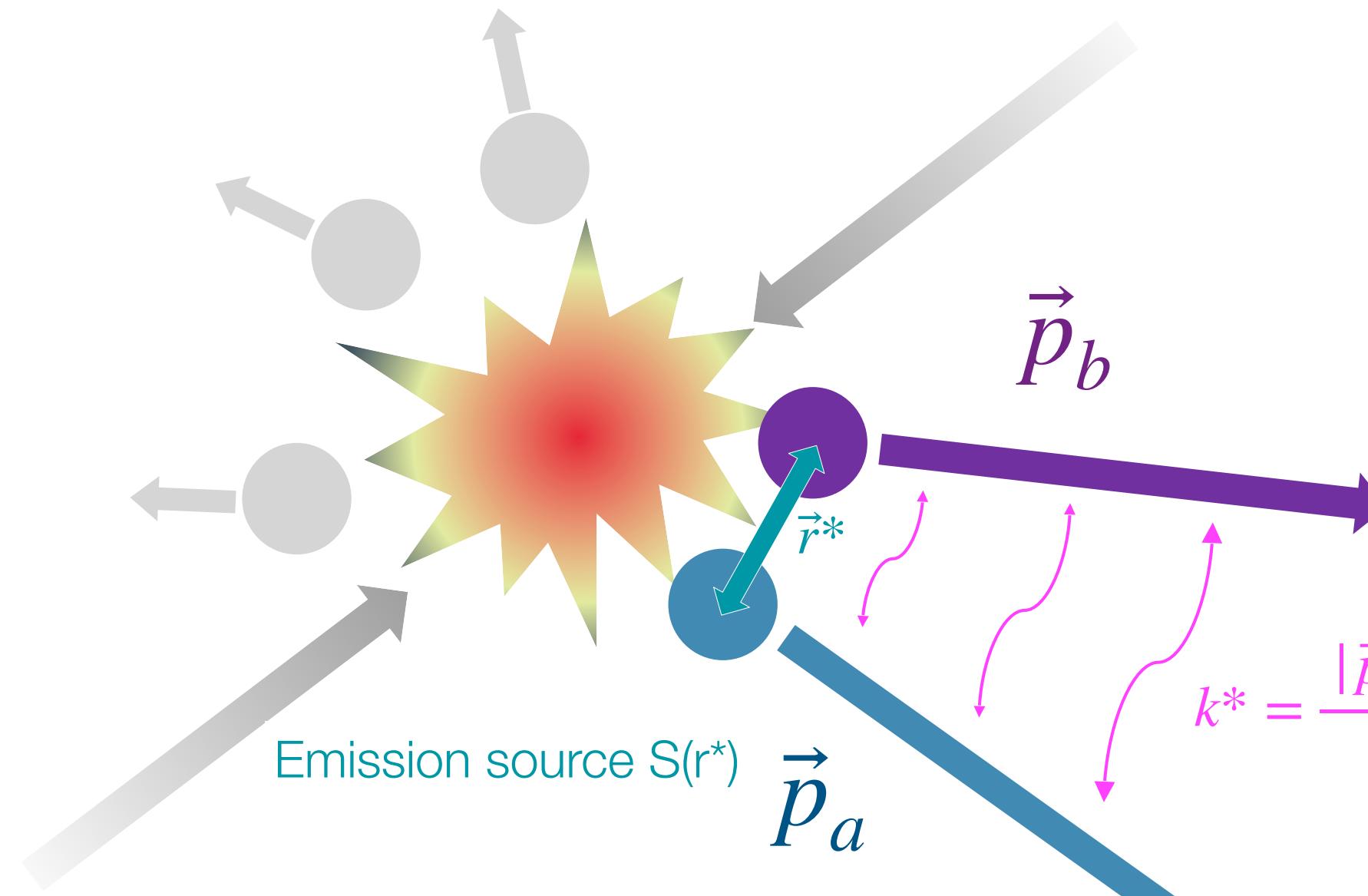
Schrödinger equation  
Two-particle wave function  
 $\psi(\vec{k}^*, \vec{r}^*)$



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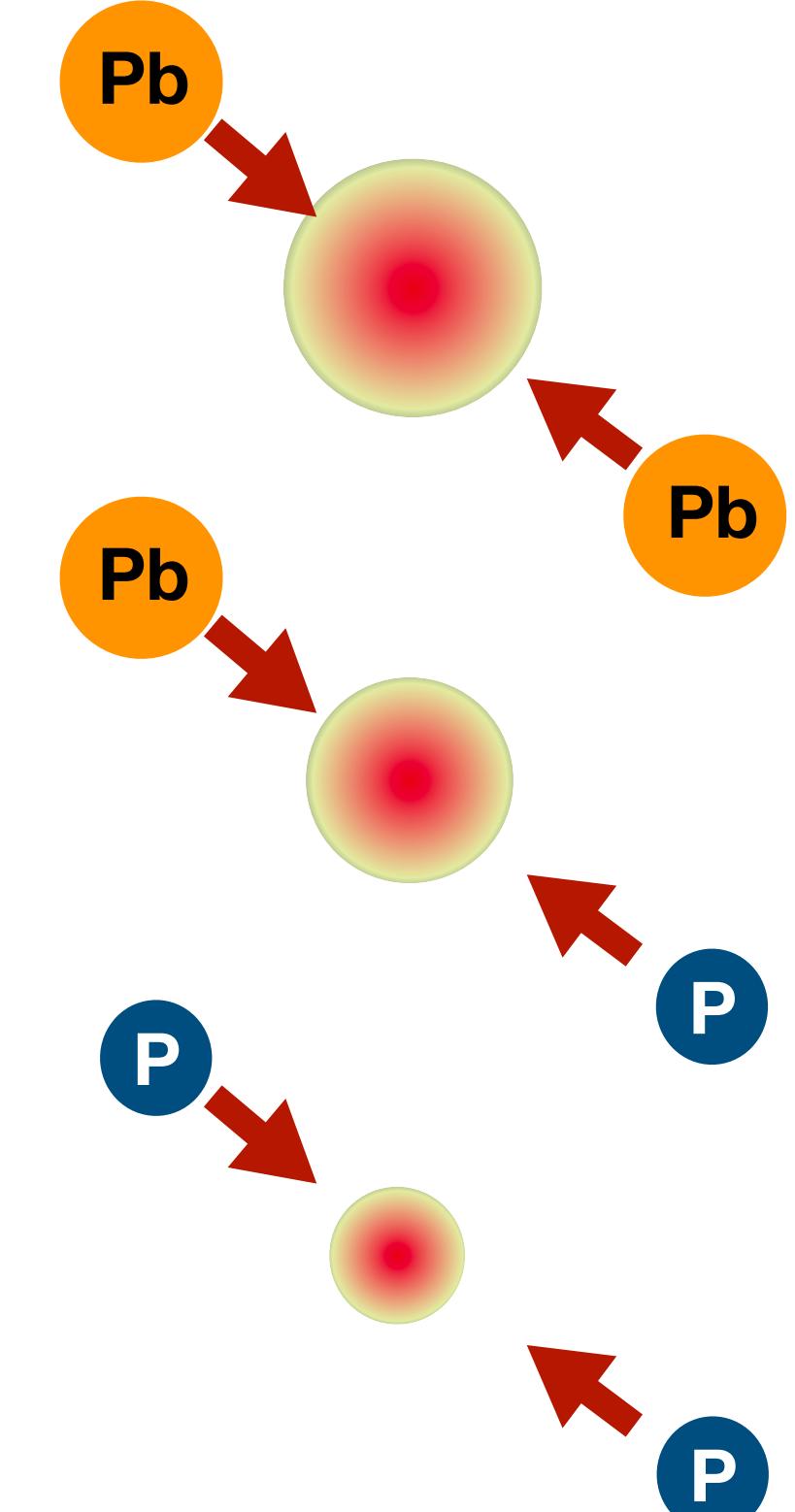


## Collisions system sizes

Pb-Pb: 5–10 fm

p-Pb: 2–4 fm

pp: 1–1.5 fm

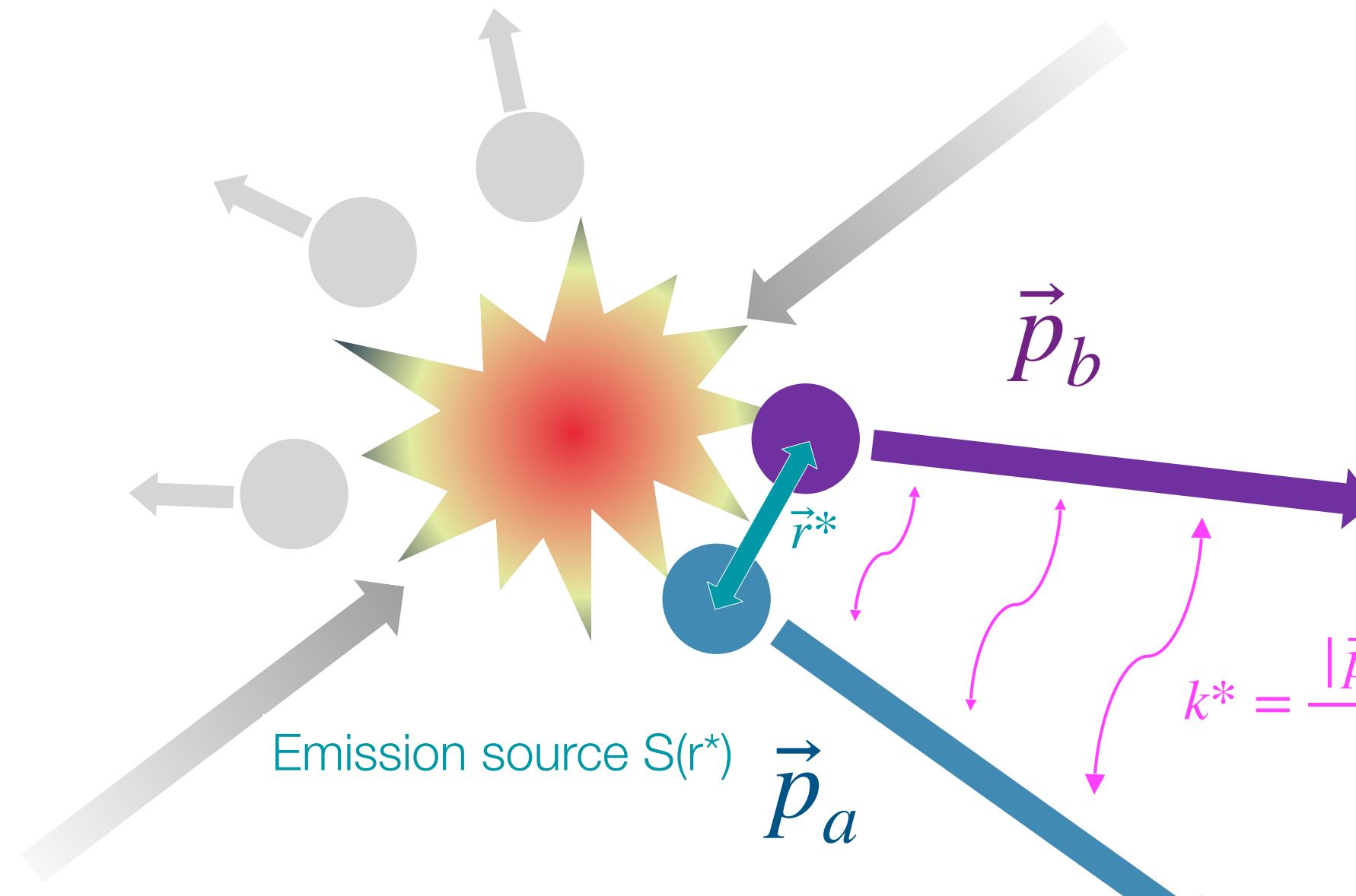


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experimental definition

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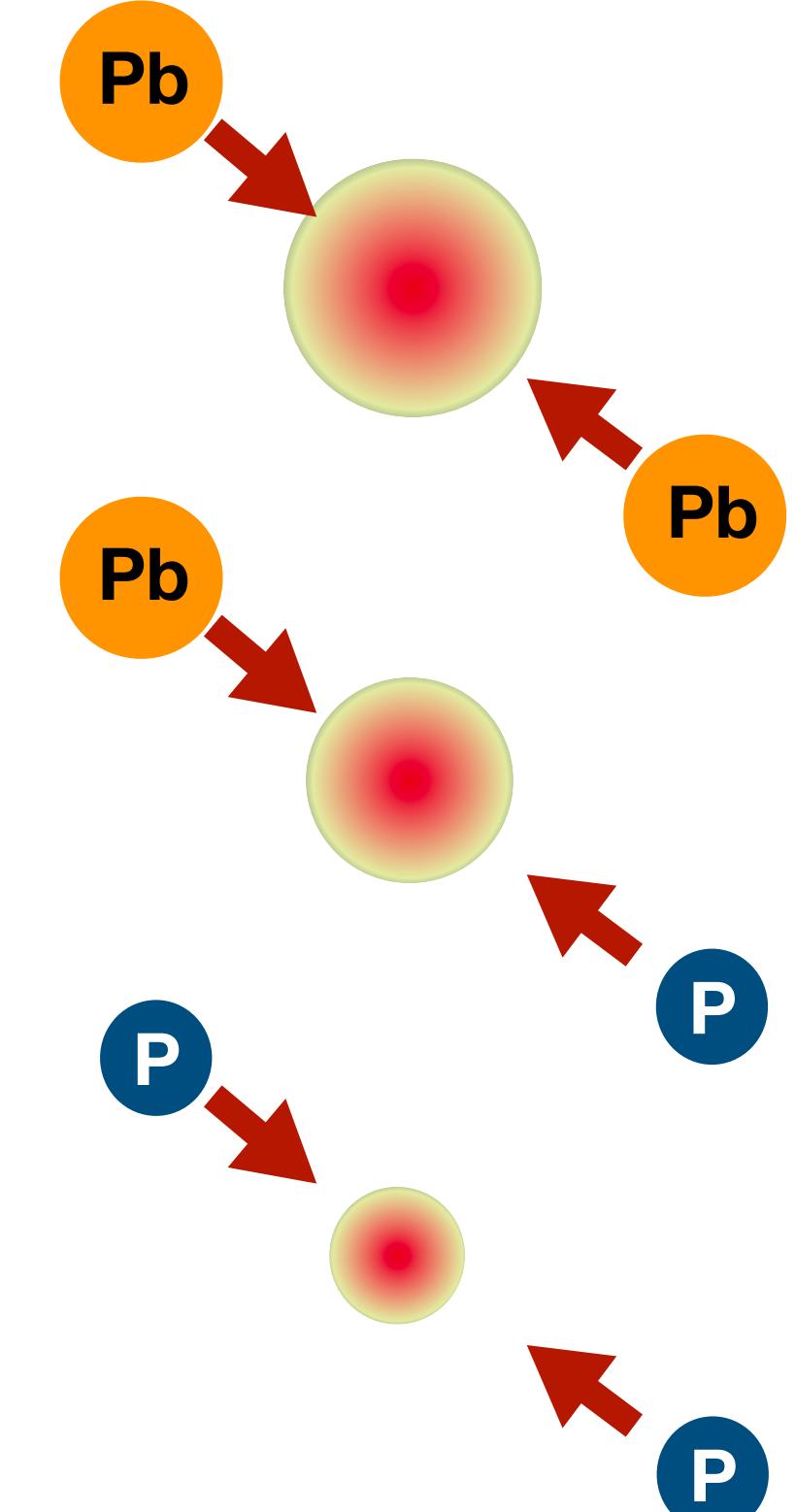


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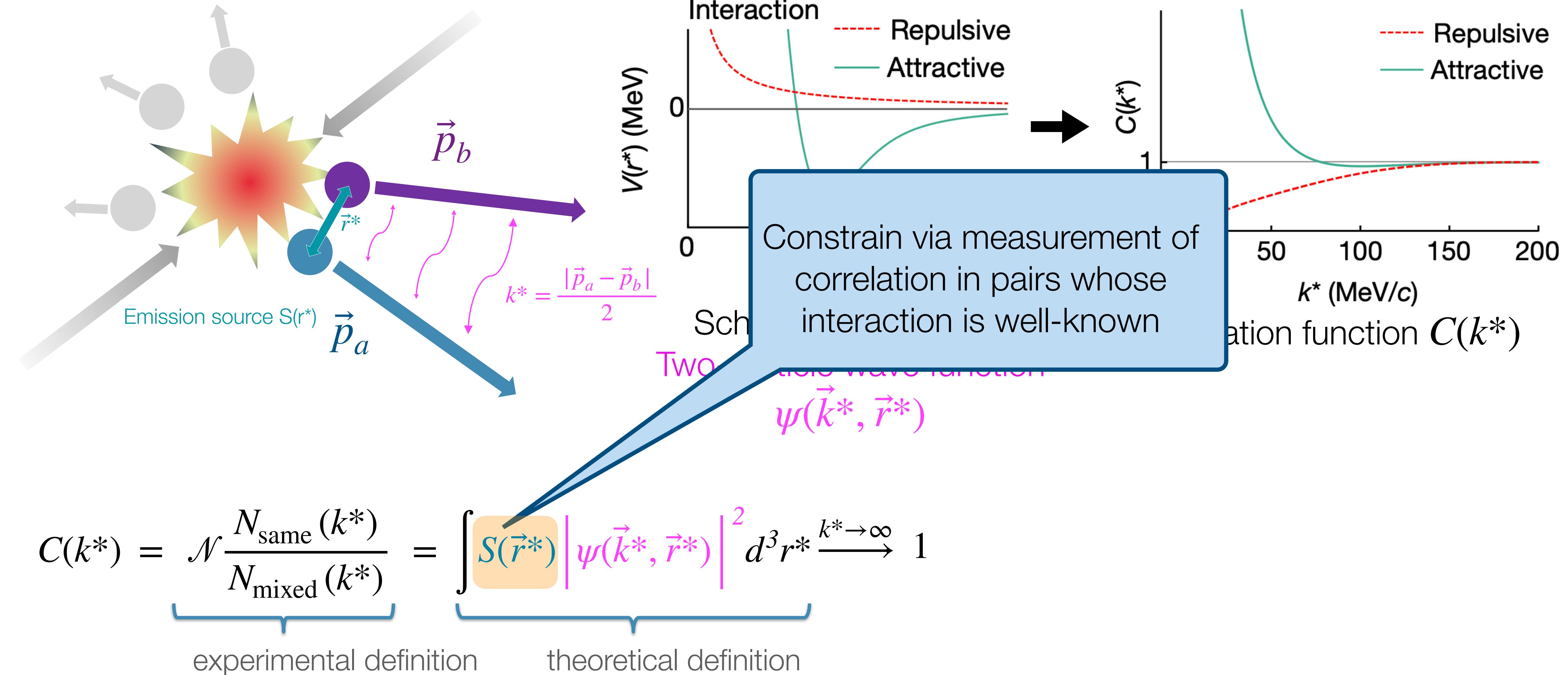


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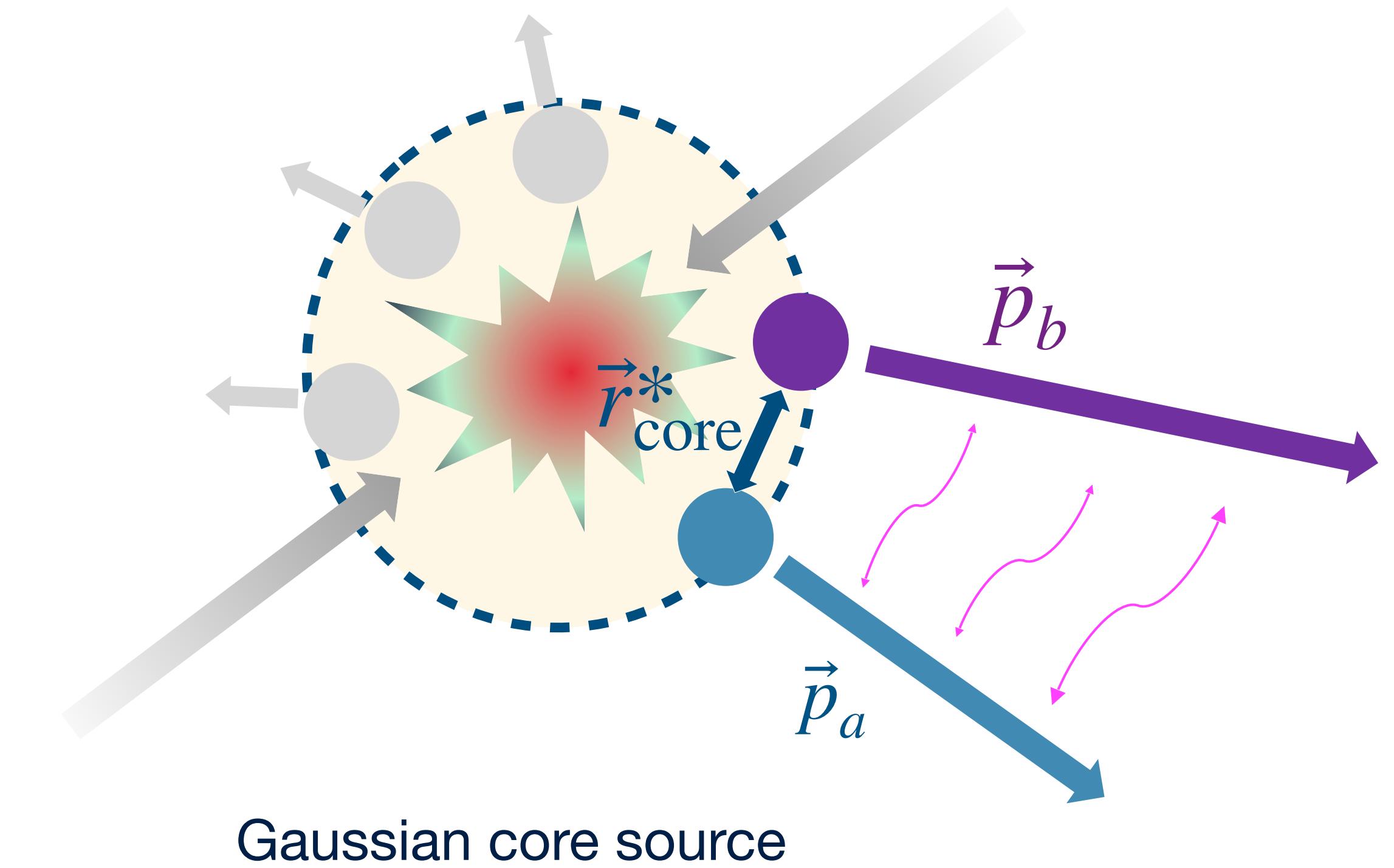


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# The emission source in pp collisions

- Source modeling is based on
  - Emission of all primordial particles (Gaussian)

$$S(r^*) = \frac{1}{(4\pi r_{\text{core}}^2)^{3/2}} \exp\left(-\frac{r^{*2}}{4 r_{\text{core}}^2}\right)$$

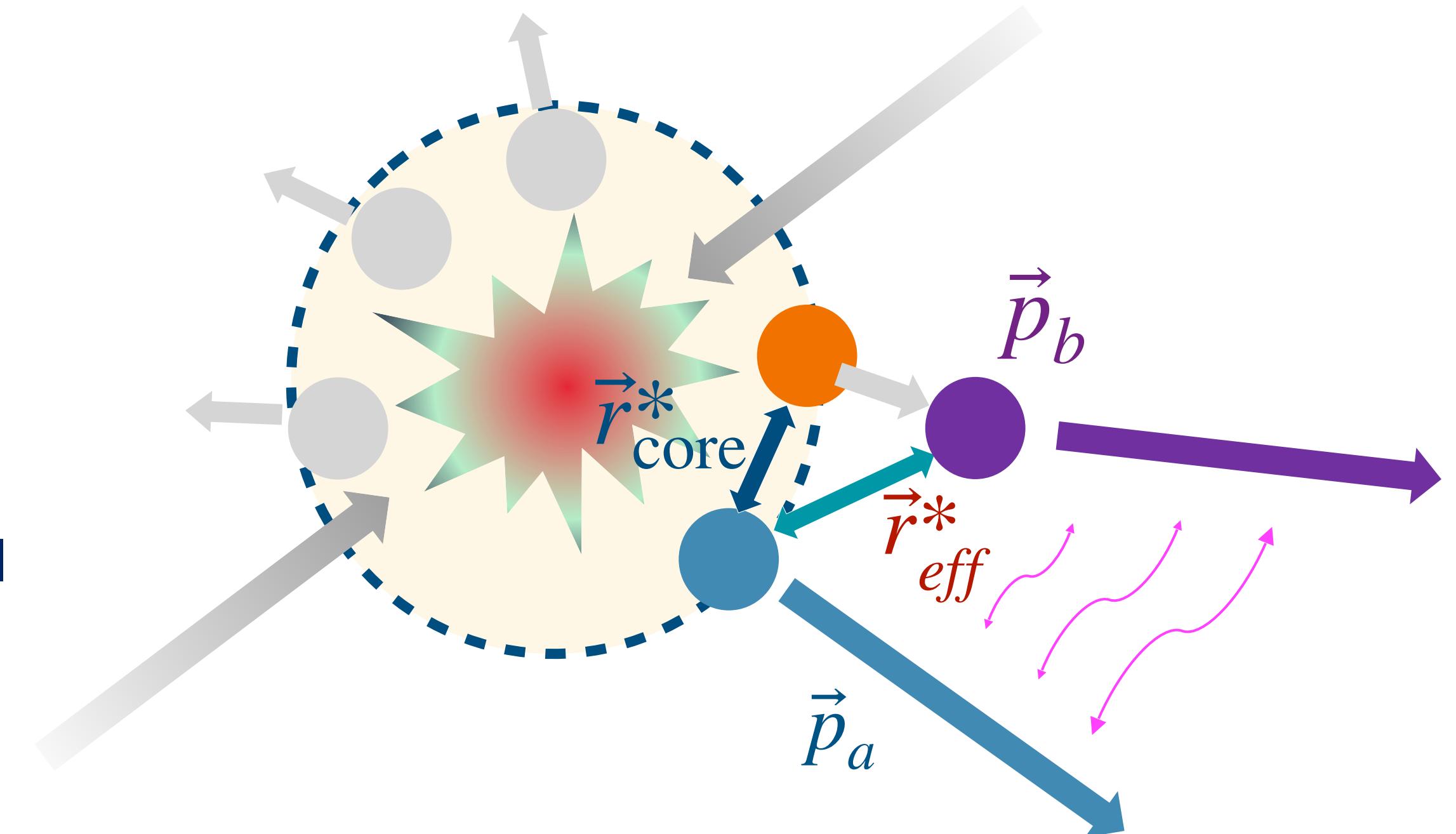


# The emission source in pp collisions

- Source modeling is based on
  - Emission of all primordial particles (Gaussian)
  - Short-lived resonances ( $c\tau \sim 1$  fm :  $\Delta, N^*, \Sigma^*$ )

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⊕ resonance tail



- Resonance contributions
  - Dependent on the particle species
  - Fixed from the statistical hadronization model<sup>[1]</sup> and EPOS<sup>[2]</sup>
  - $r_{\text{core}}$  : particle-emitting source can be studied using particle pairs with known interaction

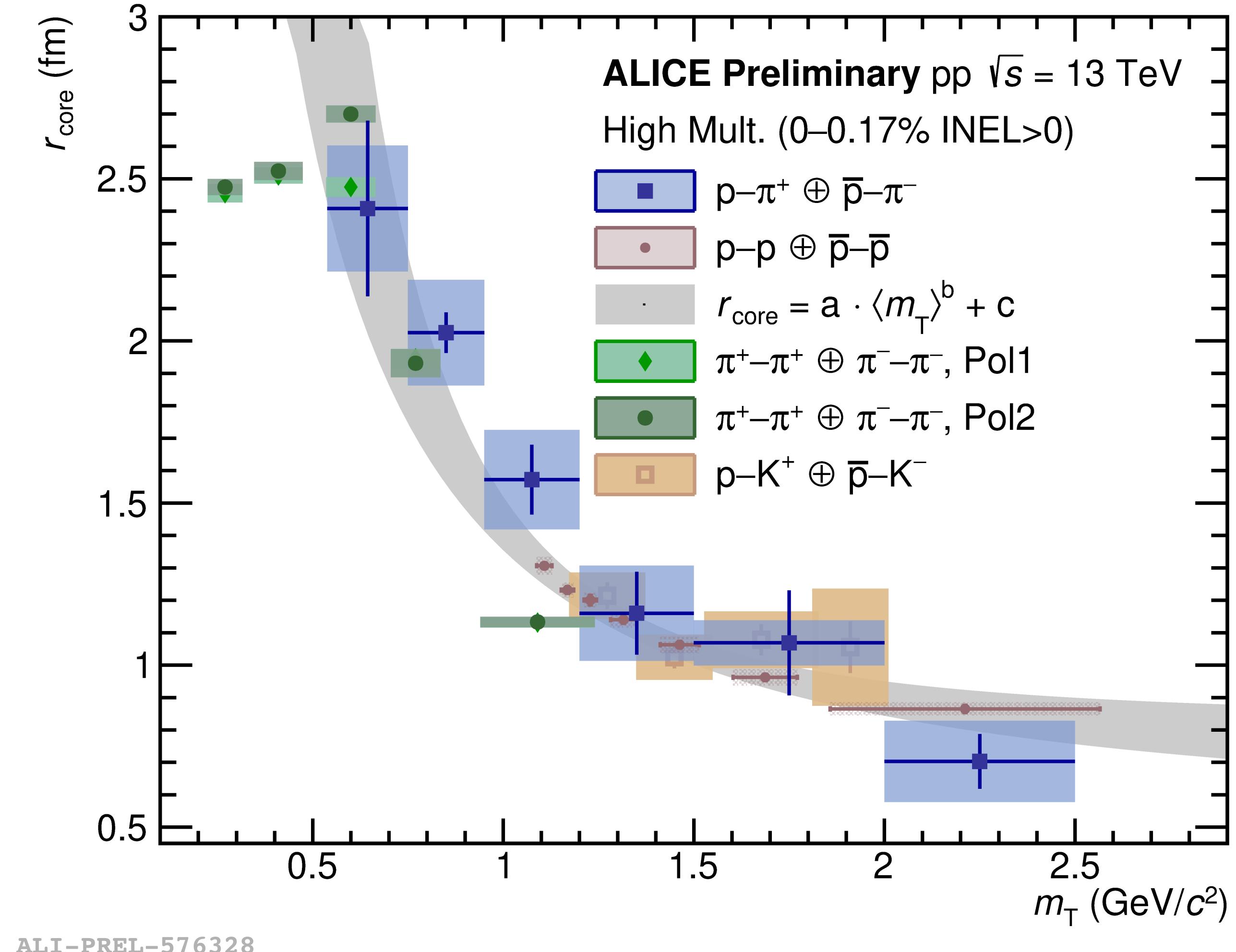
Gaussian core ⊕ resonance contributions

[1] V. Vovchenko et al, Comput. Phys. Comm. 244 (2019)

[2] T. Pierog et al, Phy. Rev. C 92, 034906 (2015)

# A common source for all hadrons in pp collisions

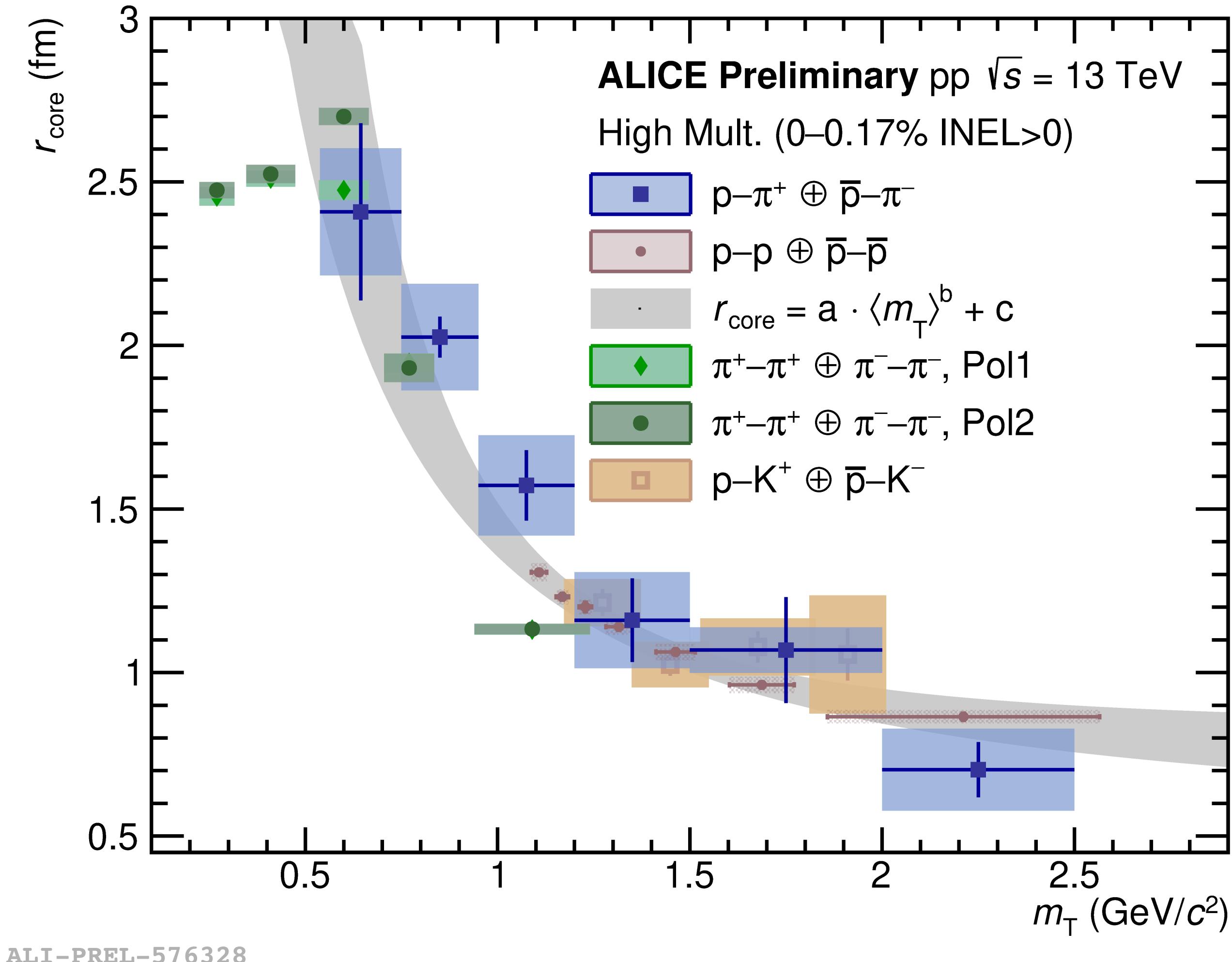
- Particle-emitting sources studied with
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  - p-p [ALICE, Phys. Lett. B 811 135849 \(2020\)](#)
  - p-K<sup>+</sup> [ALICE, arXiv:2311.14527](#)
  - π<sup>±</sup>-π<sup>±</sup> [ALICE, arXiv:2311.14527](#)
  - p-π<sup>±</sup> (paper in preparation)



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- **A common primordial source for all hadrons in high-multiplicity pp collisions!**
- Use the source size for particle pairs with unknown interaction
- Possibility to study interaction for exotic pairs



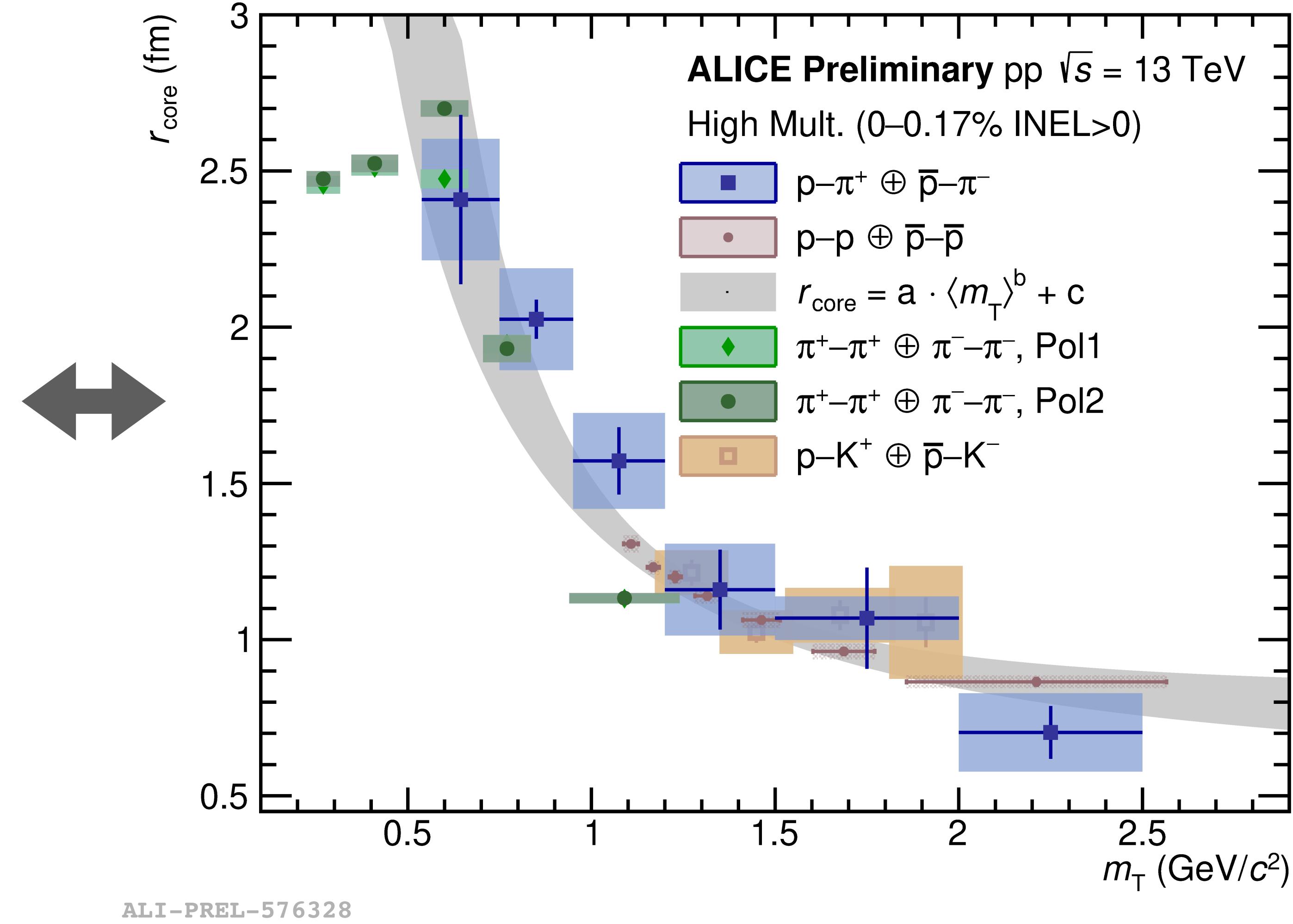
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# A common source for all hadrons in pp collisions

## Recent ALICE femtoscopy measurements

PRC 99 (2019) 2, 024001	p-p, p- $\Lambda$ , $\Lambda$ - $\Lambda$ (methods)
PLB 797 (2019), 134822	$\Lambda$ - $\Lambda$
PRL 123 (2019), 112002	p- $\Xi$
PRL 124 (2020) 092301	p-K
PLB 805 (2020), 135419	p- $\Sigma^0$
PLB 811 (2020), 135849	p-p, p- $\Lambda$
Nature 588 (2020) 232-238	p- $\Xi$ , p- $\Omega$
PRL 127 (2021), 172301	p- $\phi$
PLB 822 (2021) 136708	p-K
PRC 103 (2021) 5, 055201	$\Lambda$ -K
PLB 833 (2022), 137272	p- $\Lambda$
PLB 829 (2022), 137060	baryon-(anti)baryon
PRD 106 (2022) 5, 052010	p-D
PLB 833 (2022) 137335	$K^0$ - $K^0$ , $K^{ch}$ - $K^0$
PLB 844 (2022), 137223	$\Lambda$ - $\Xi$
EPJA 59 (2023) 7, 145	p-p-p, p-p- $\Lambda$
EPJA 59 (2023) 12, 298	p-p-K
EPJC 83 (2023) 4, 340	p-K
PLB 845 (2023), 138145	$\Lambda$ -K
PRD 110, 032004	$K/\pi$ -D
PRX 14 (2024) 3, 031051	p-d, K-d

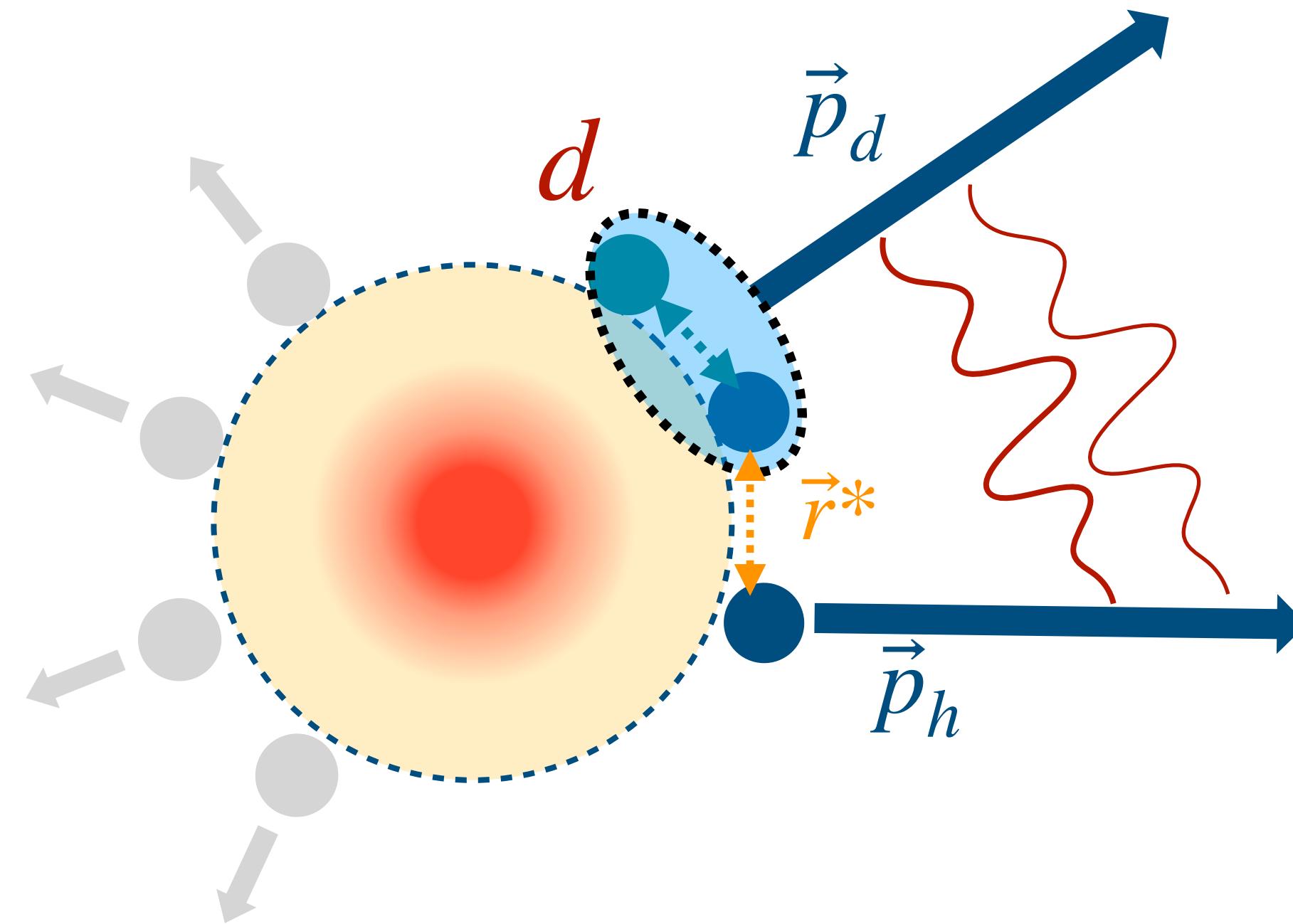
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# Today: three-hadron systems

- Hadron-deuteron correlations provide an indirect way to study the strong interaction in system of three hadrons

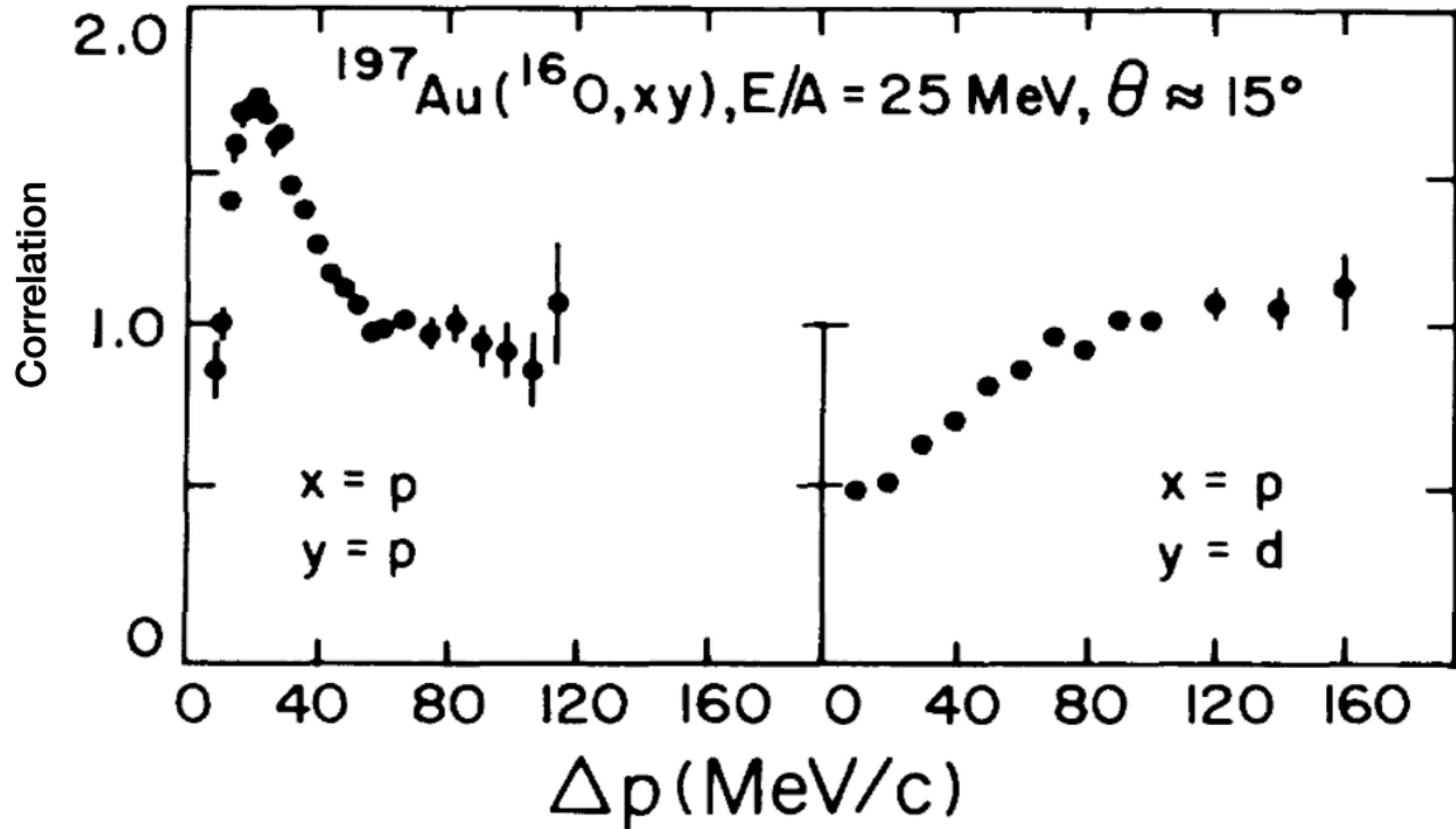


**$K^+$ -d and p-d systems**

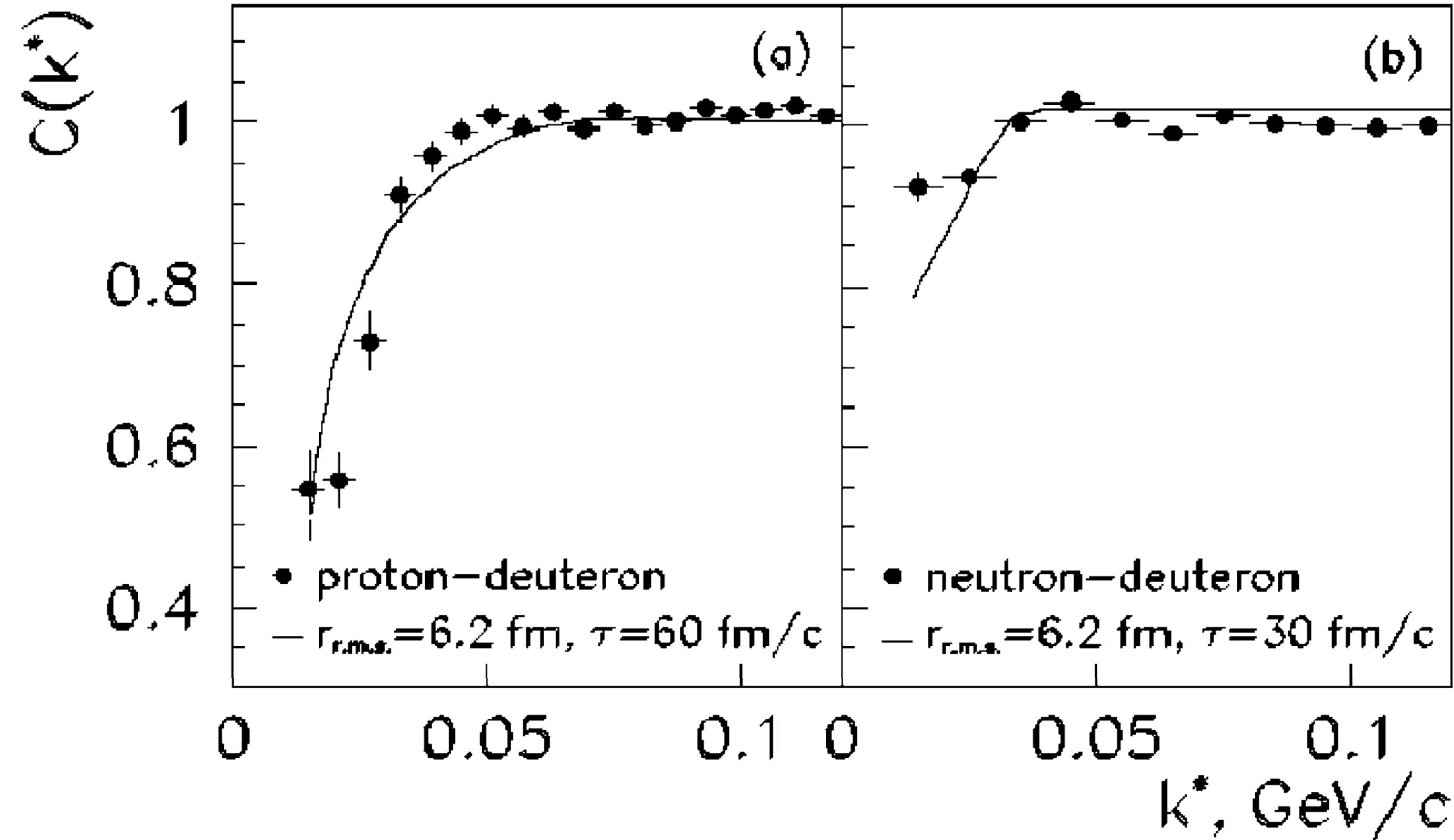
# So far... hadron-deuteron correlations

- At very low energy (~ GeV beam energy), fixed target experiments<sup>[1-4]</sup>

Michigan State University (C. B. Chitwood et al., PRL 54, 302 (1985))



GANIL (K. Wosinska et al., EPJA 32, 55–59 (2007))

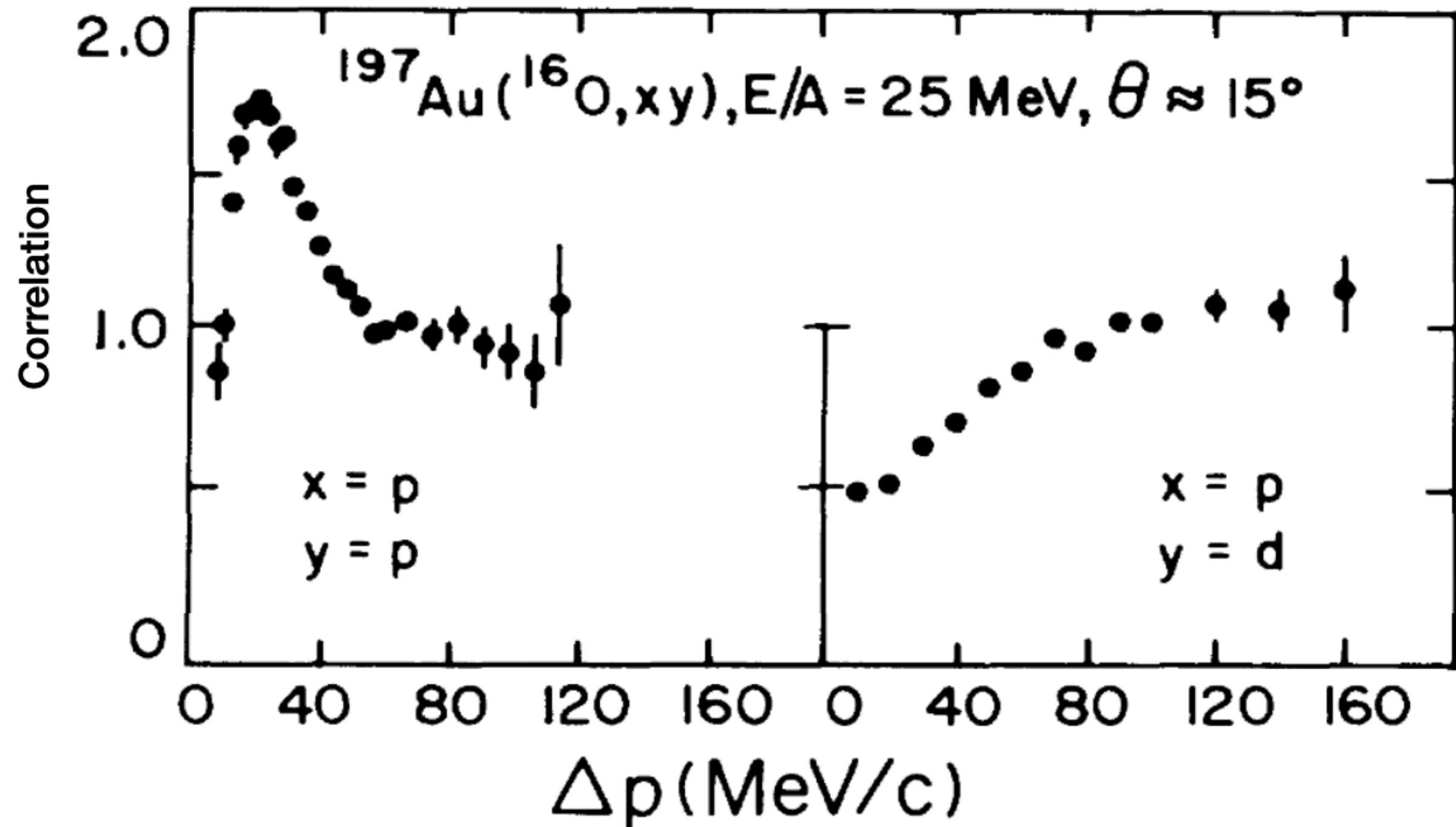


- [1] C. B. Chitwood et al, Phys. Rev. Lett. 54, 302 (1985)
- [2] J. Pochodzalla et al, Phys. Rev. C 35, 1695 (1986)
- [3] J. Pochodzalla et al, Phys. Lett. B 175 (1986)
- [4] K. Wosinska et al, Eur. Phys. J. A 32, 55–59 (2007)

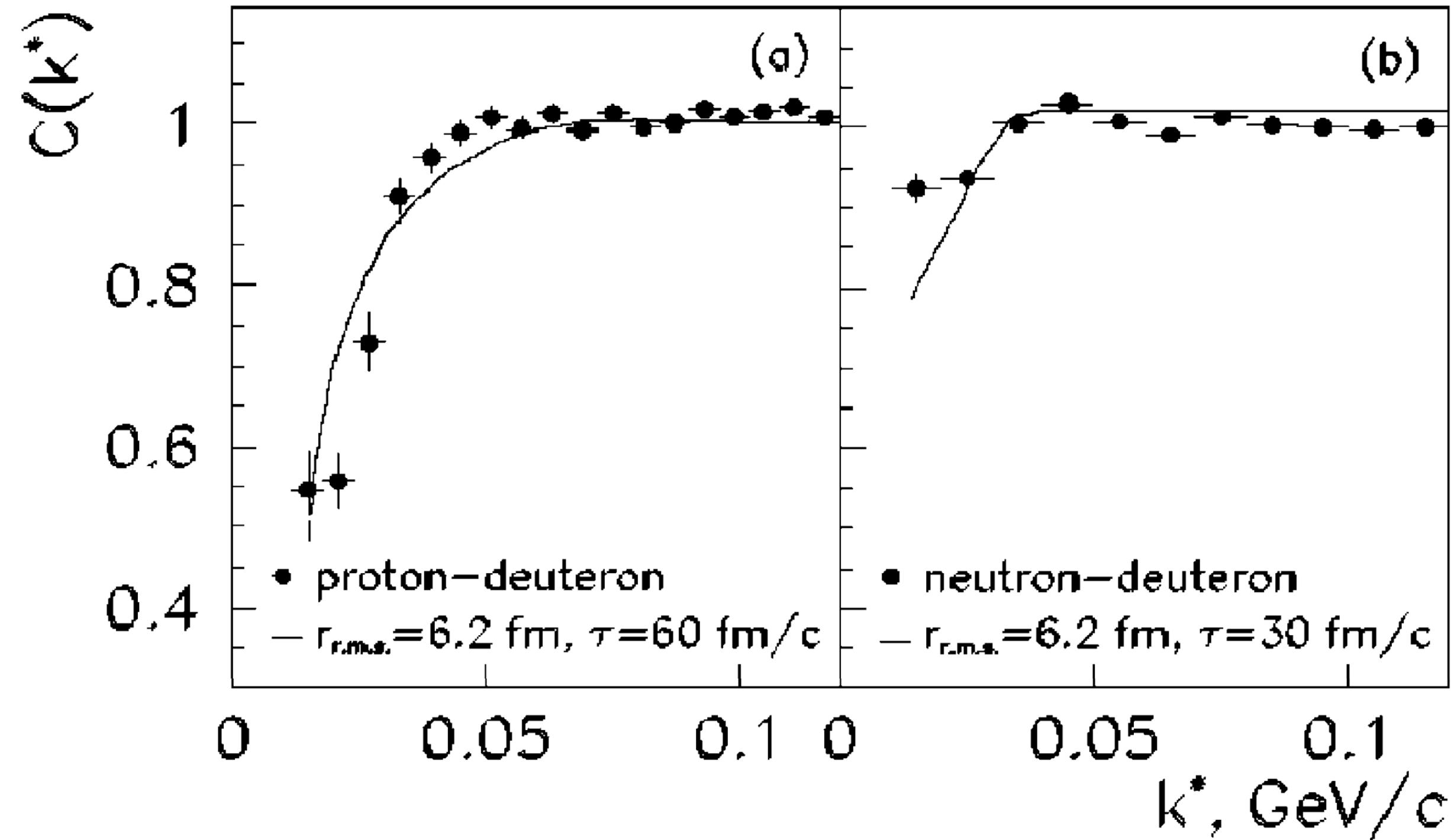
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- Large source size → dominant Coulomb interaction
- No **full-fledged calculations** and unconstrained source distributions

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# A Large Ion Collider Experiment

- Excellent tracking and particle identification (PID) capabilities

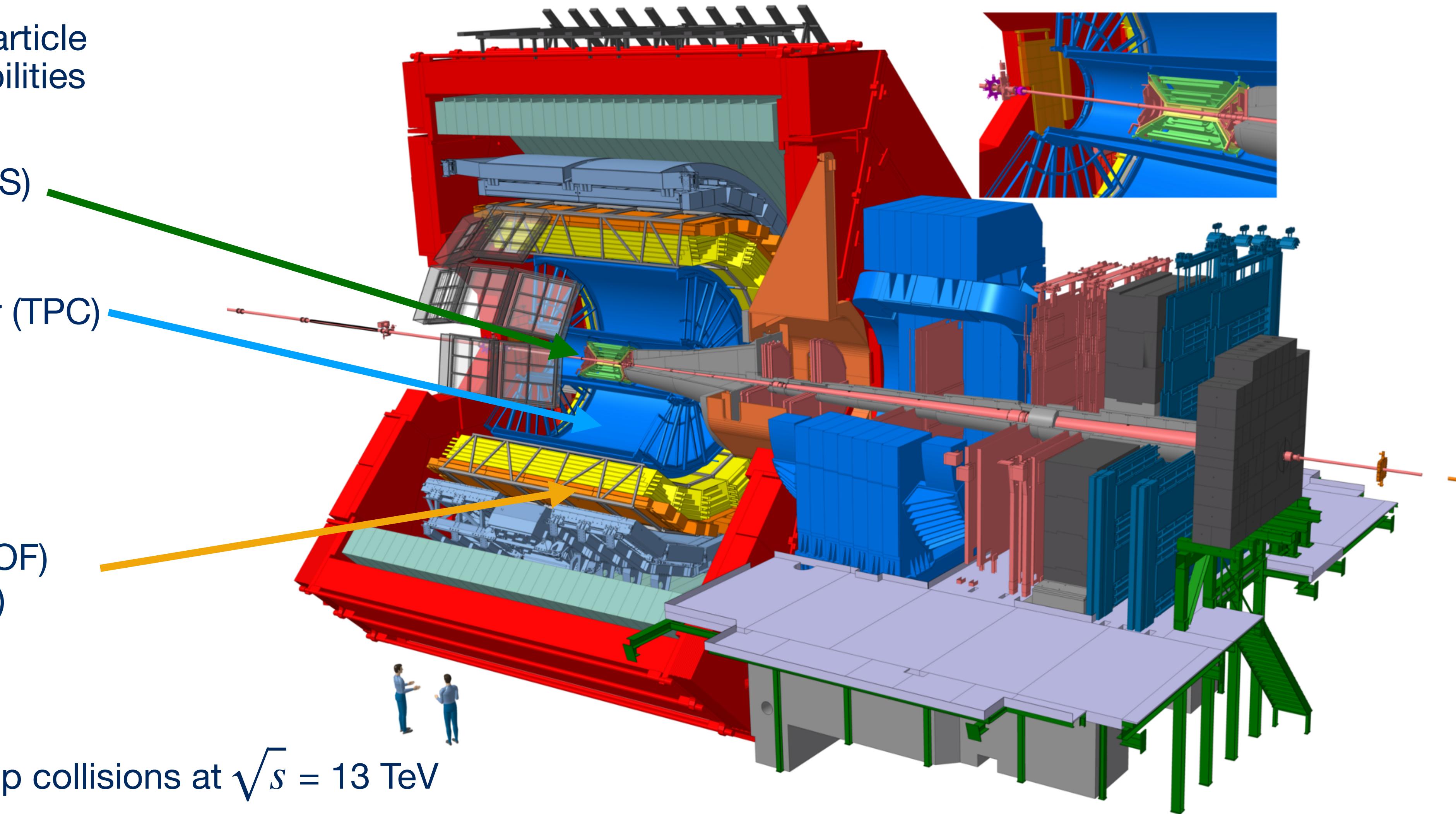
Inner Tracking System (ITS)  
Tracking, vertex

Time Projection Chamber (TPC)  
Tracking, PID ( $dE/dx$ )

Time Of Flight detector (TOF)  
PID (TOF measurement)

- Run 2 data-set

-  $10^9$  high-multiplicity pp collisions at  $\sqrt{s} = 13$  TeV



ALICE : [ITS](#) and [TPC](#) upgrades

Int.J.Mod.Phys.A 29 (2014) 1430044  
JINST 3 (2008) S08002

# A Large Ion Collider Experiment

- Excellent tracking and particle identification (PID) capabilities

Inner Tracking System (ITS)  
Tracking, vertex

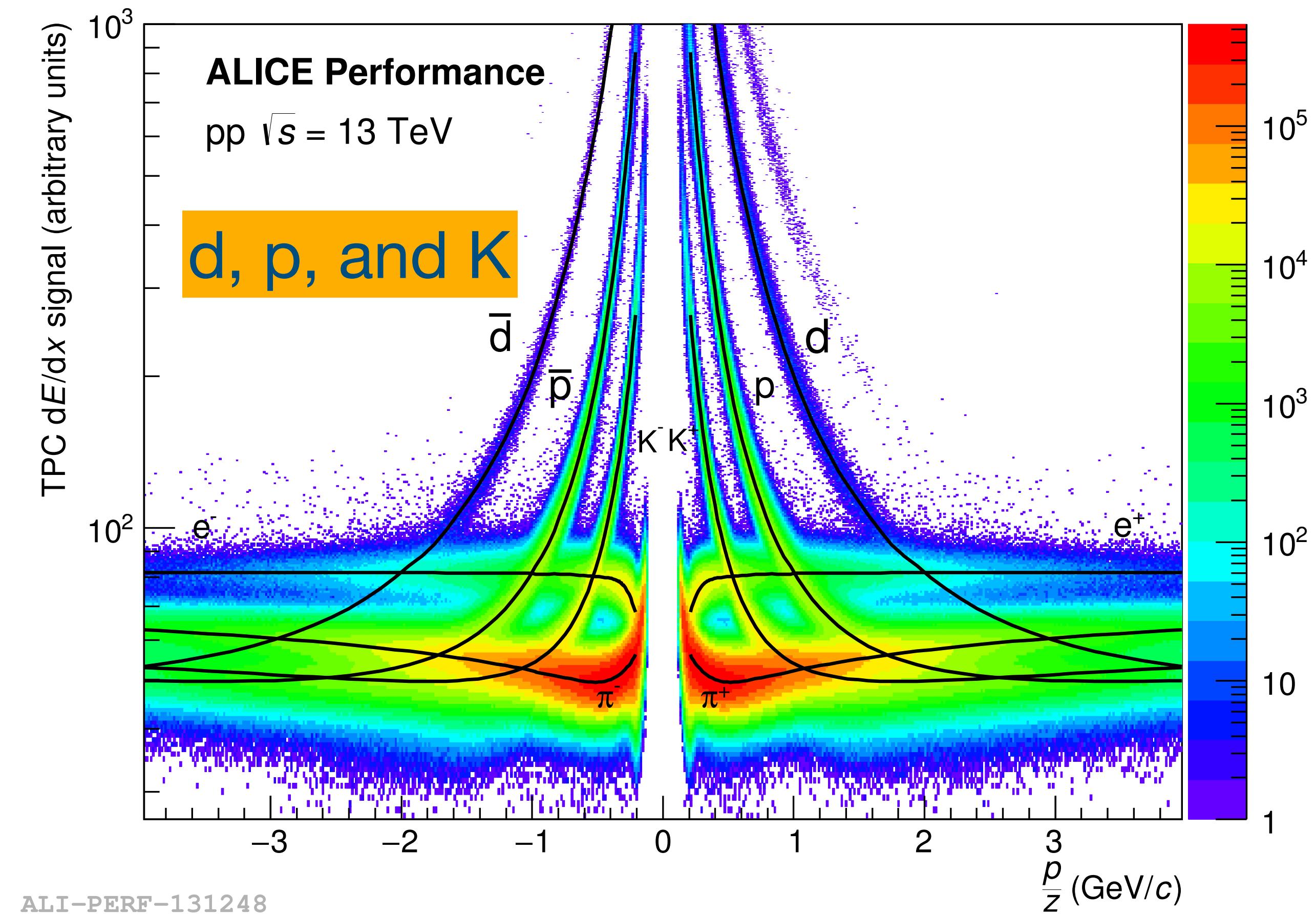
Time Projection Chamber (TPC)  
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Time Of Flight detector (TOF)  
PID (TOF measurement)

- Run 2 data-set

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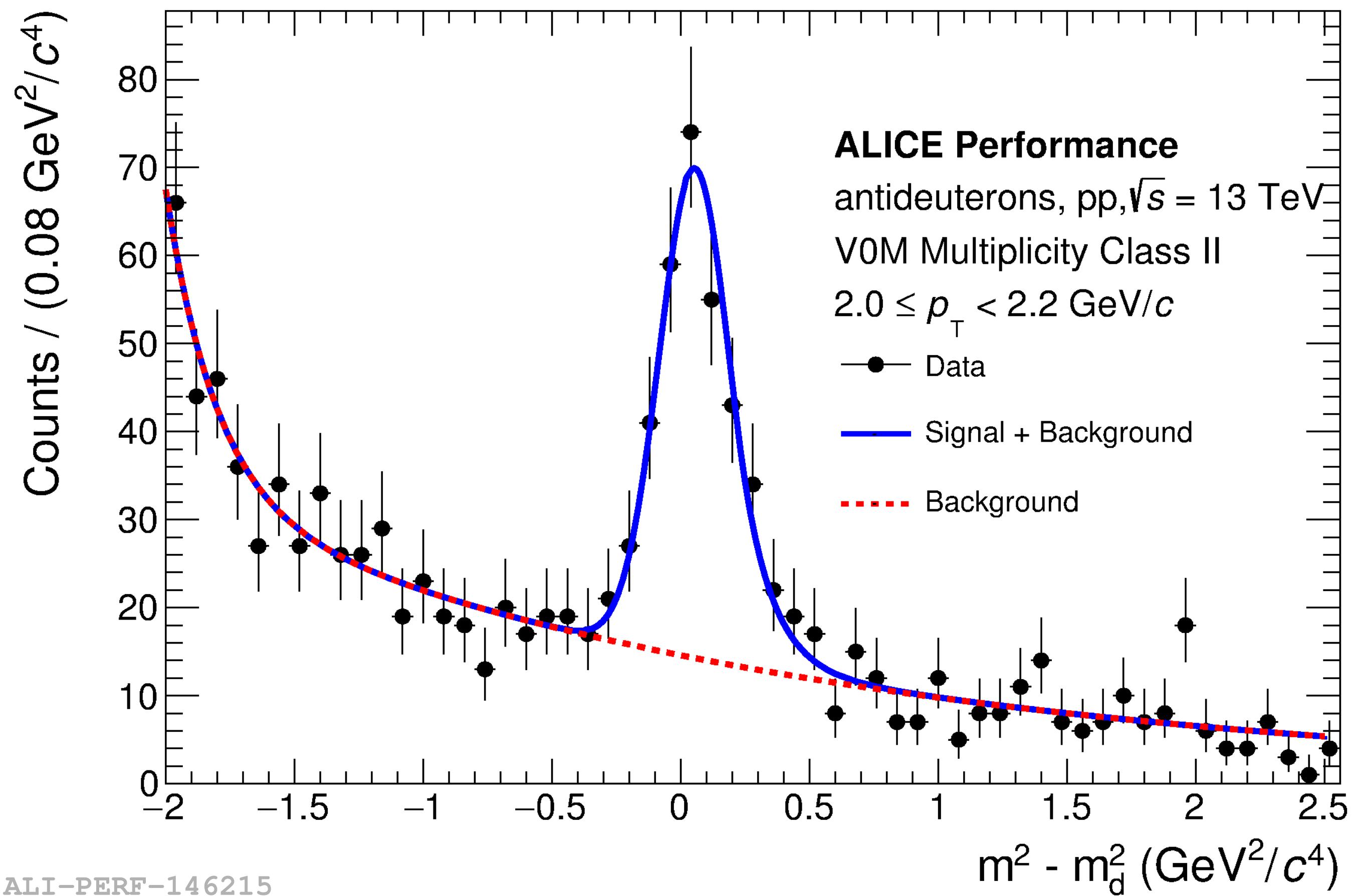
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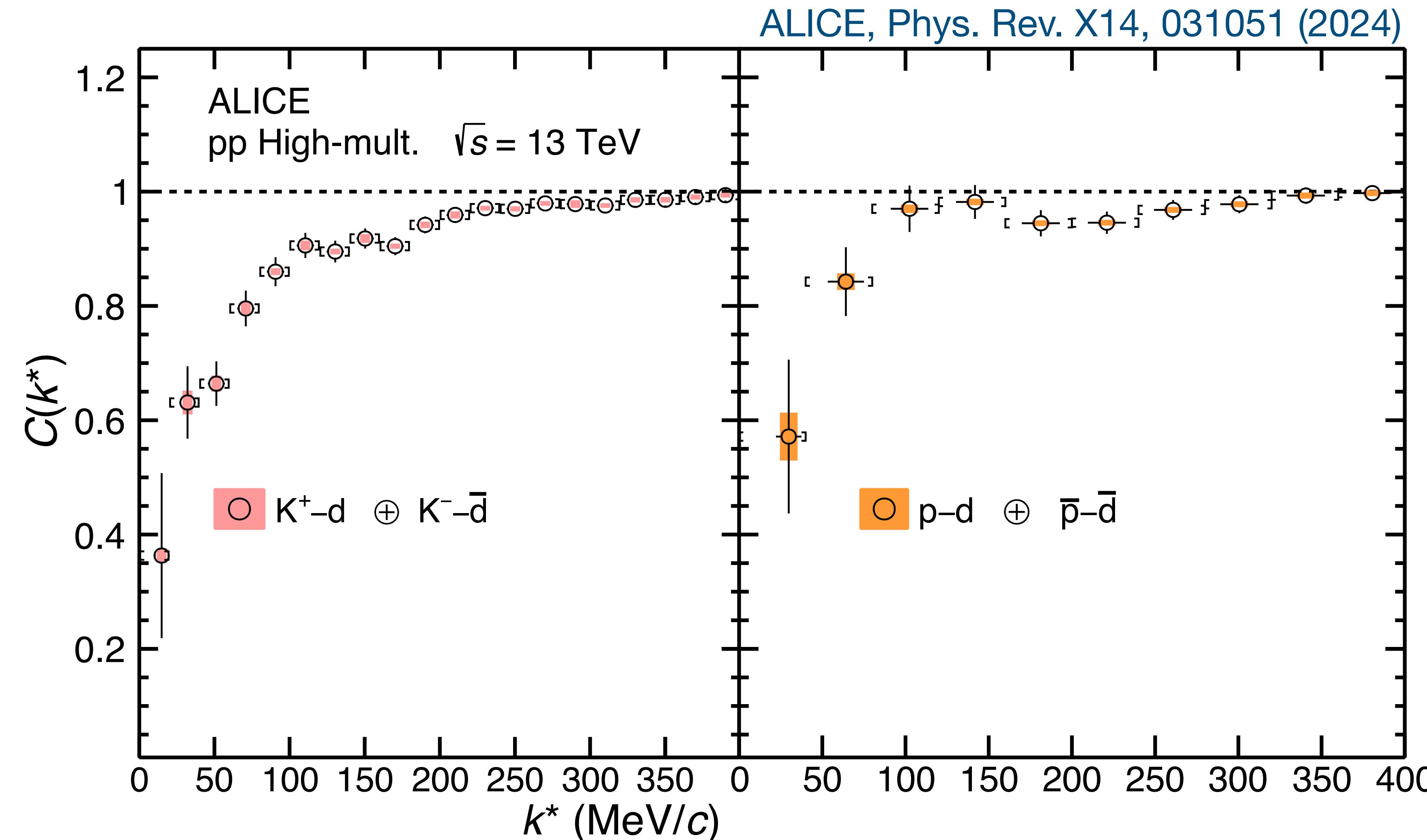
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# Hadron-deuteron correlations in pp collisions at LHC

- First measurements of p-d and K<sup>+</sup>-d correlation functions at the LHC



# Femtoscopic correlations and modeling

- The femtoscopic correlation consists of various contributions<sup>[1-2]</sup>

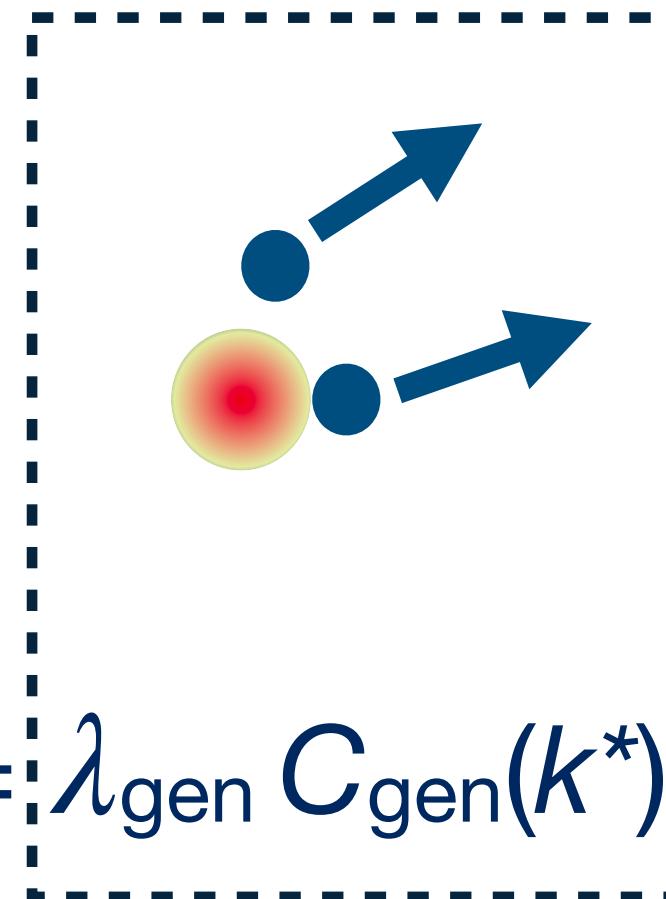
$$C_{\text{femto}}(k^*) = \lambda_{\text{gen}} C_{\text{gen}}(k^*) \oplus \lambda_{\text{feed}} C_{\text{feed}}(k^*) \oplus \lambda_{\text{misid}} C_{\text{misid}}(k^*) \oplus \dots$$

[1] D. Mihaylov et al. Eur. Phys. J. C78 (2018) 394

[2] R. Lednicky, Phys. Part. Nuclei 40, 307–352 (2009)

# Femtoscopic correlations and modeling

- The femtoscopic correlation consists of various contributions<sup>[1-2]</sup>
  - Genuine interaction from primordial particle



The diagram shows three particles: two blue dots and one yellow dot with a red center, all connected by arrows indicating interactions. They are contained within a dashed square frame.

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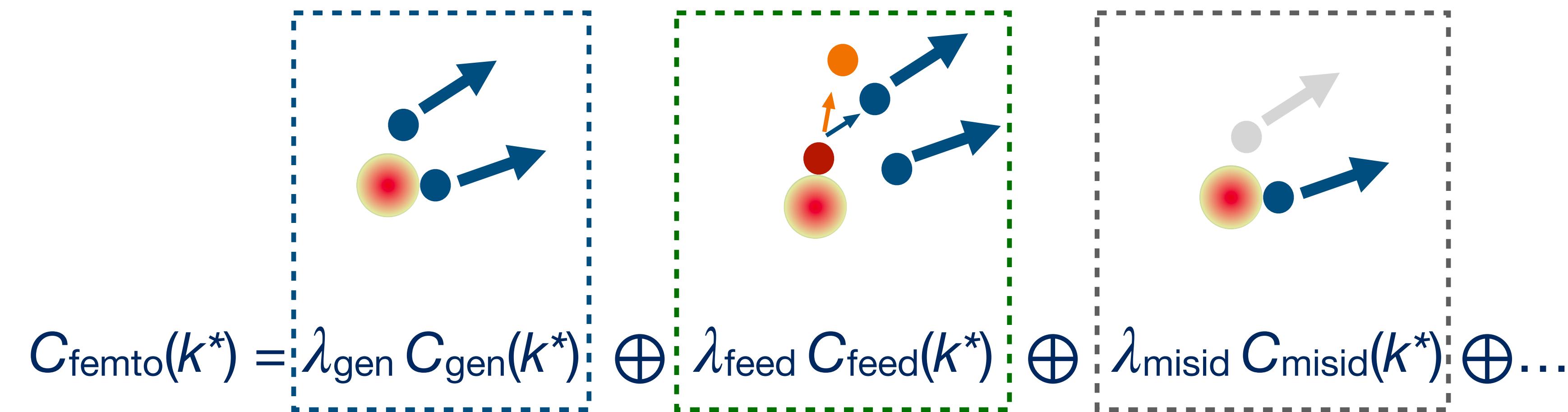
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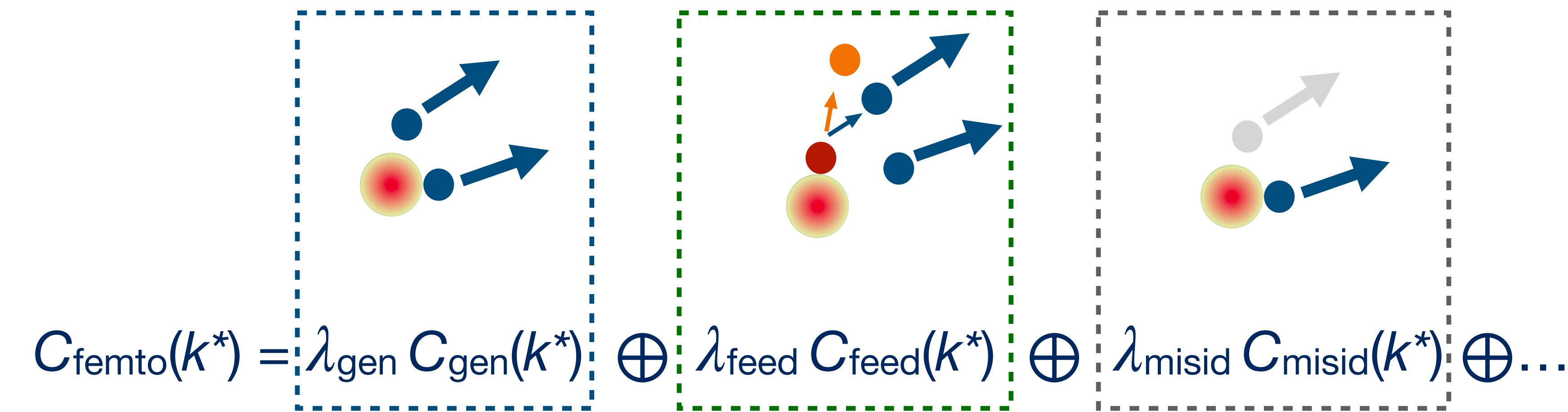


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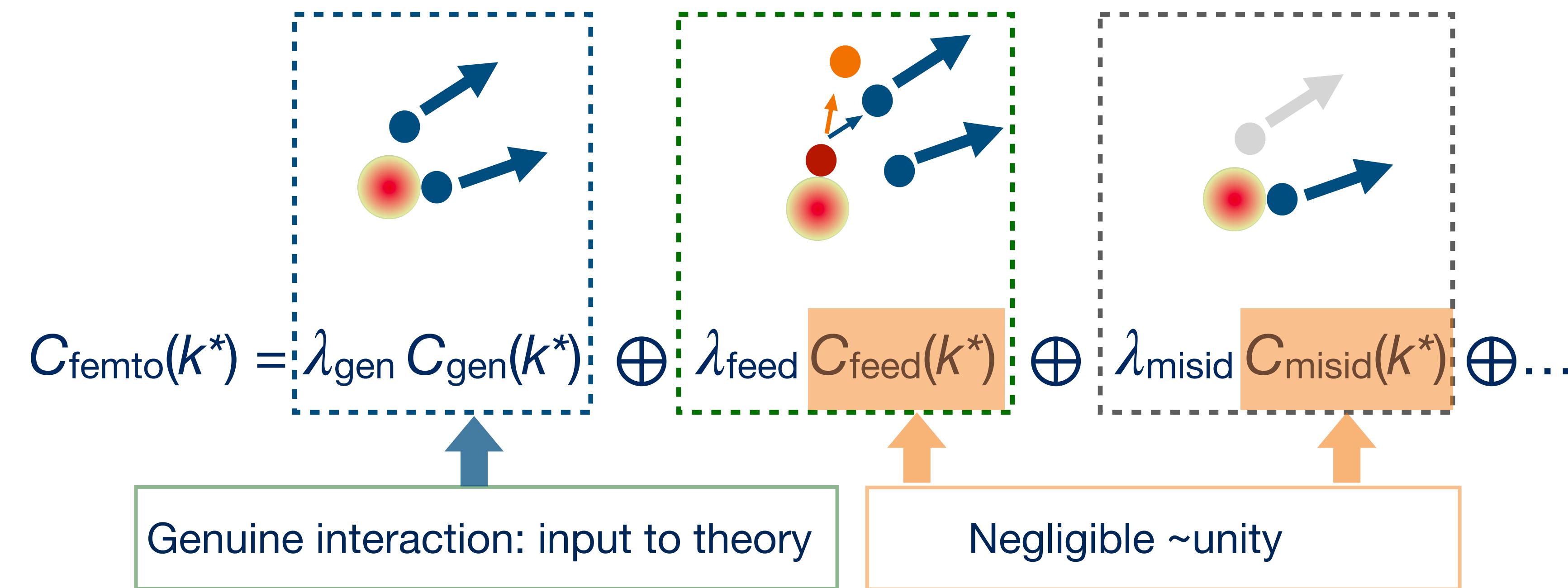
- A data-driven approach to quantify contributions ( lambda parameters  $\lambda_{ij} = \mathcal{P}_i \cdot f_i \times \mathcal{P}_j \cdot f_j$  with  $\sum_{ij} \lambda_{ij} = 1$  )
  - Purity of the individual particles ( $\mathcal{P}_i$ ) and feed-down fractions ( $f_i$ )

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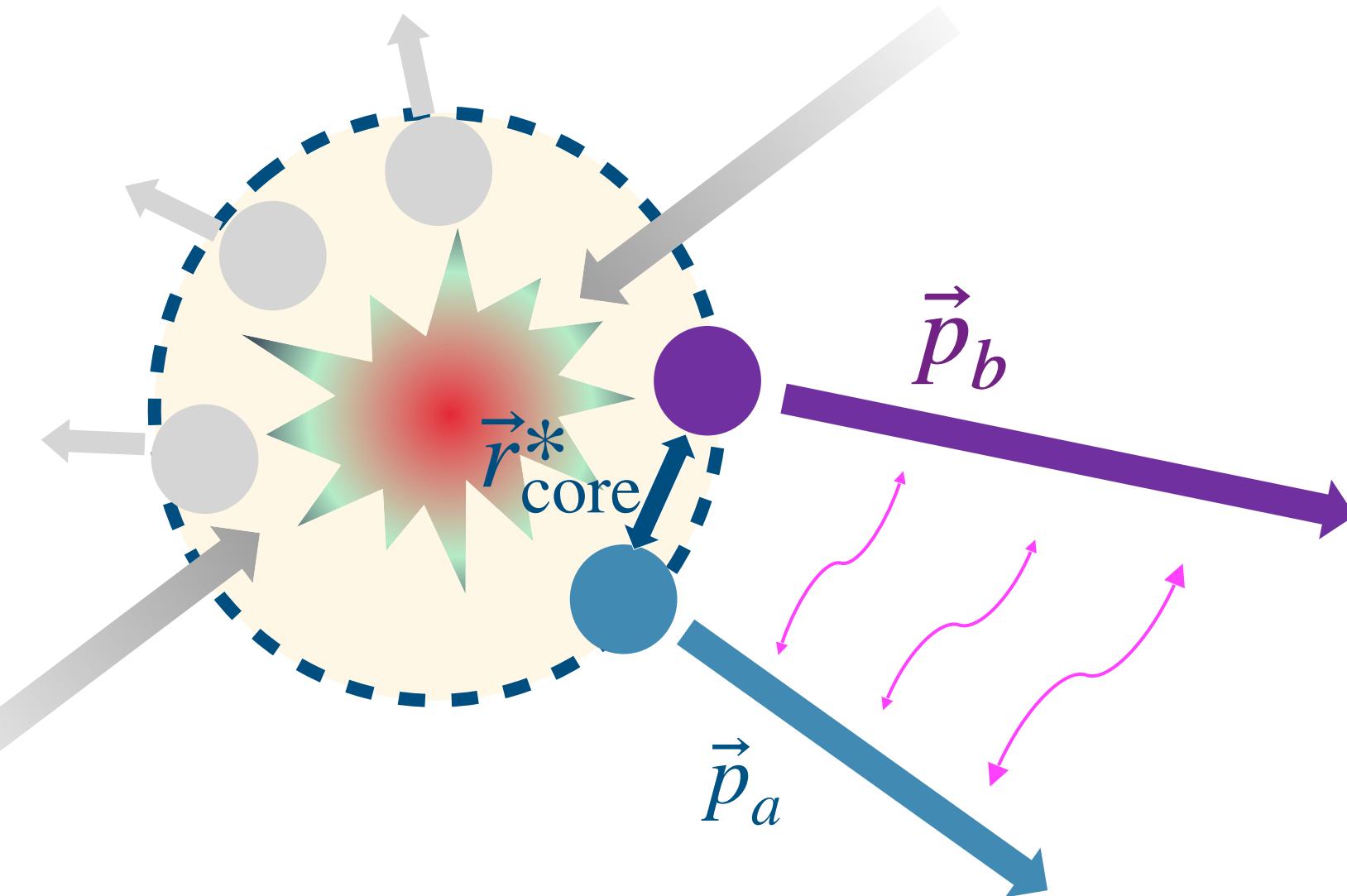


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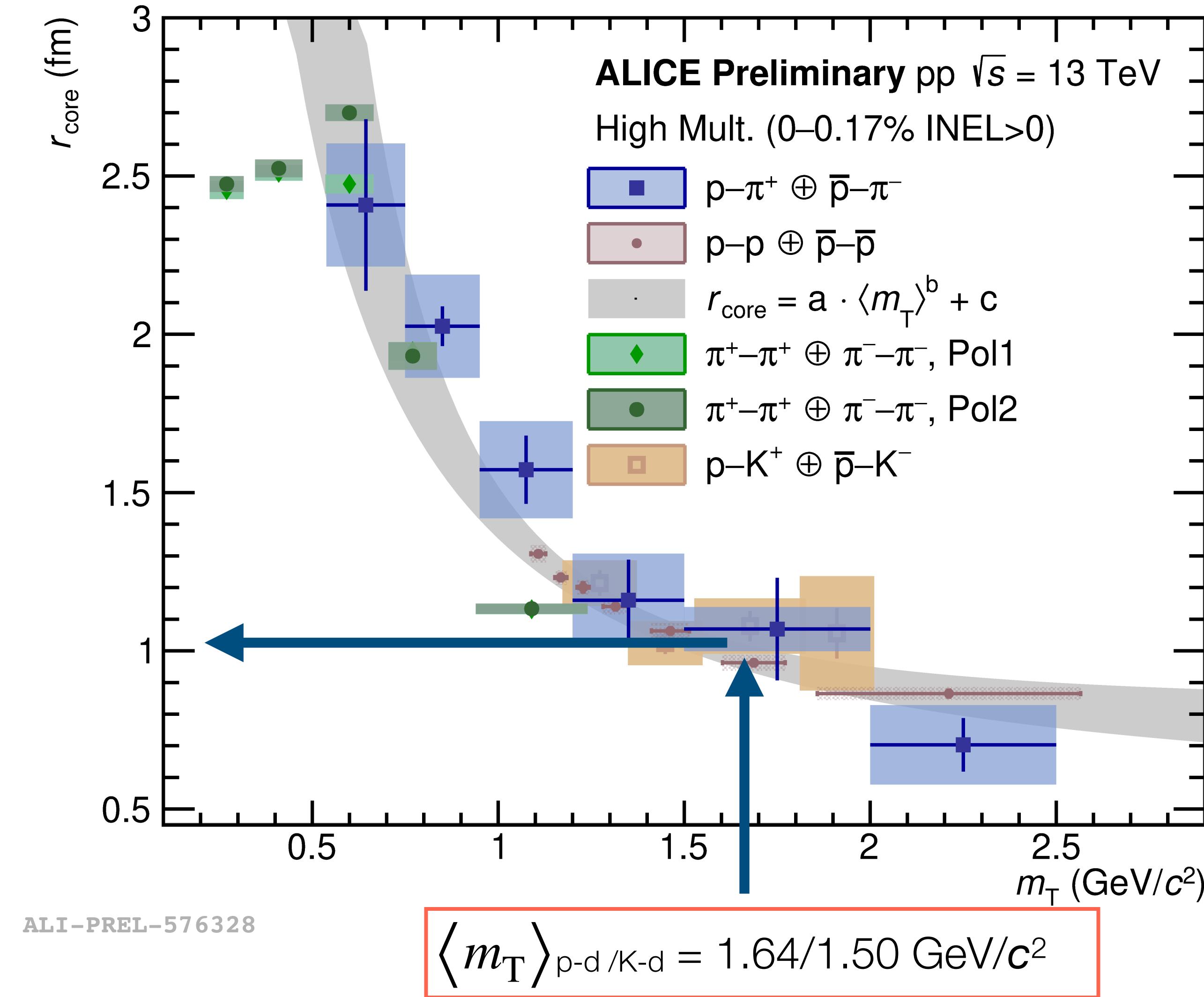
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# Source for kaon-deuteron and proton-deuteron pairs

- Primordial source size for  $K^+ - d$  and  $p - d$  systems

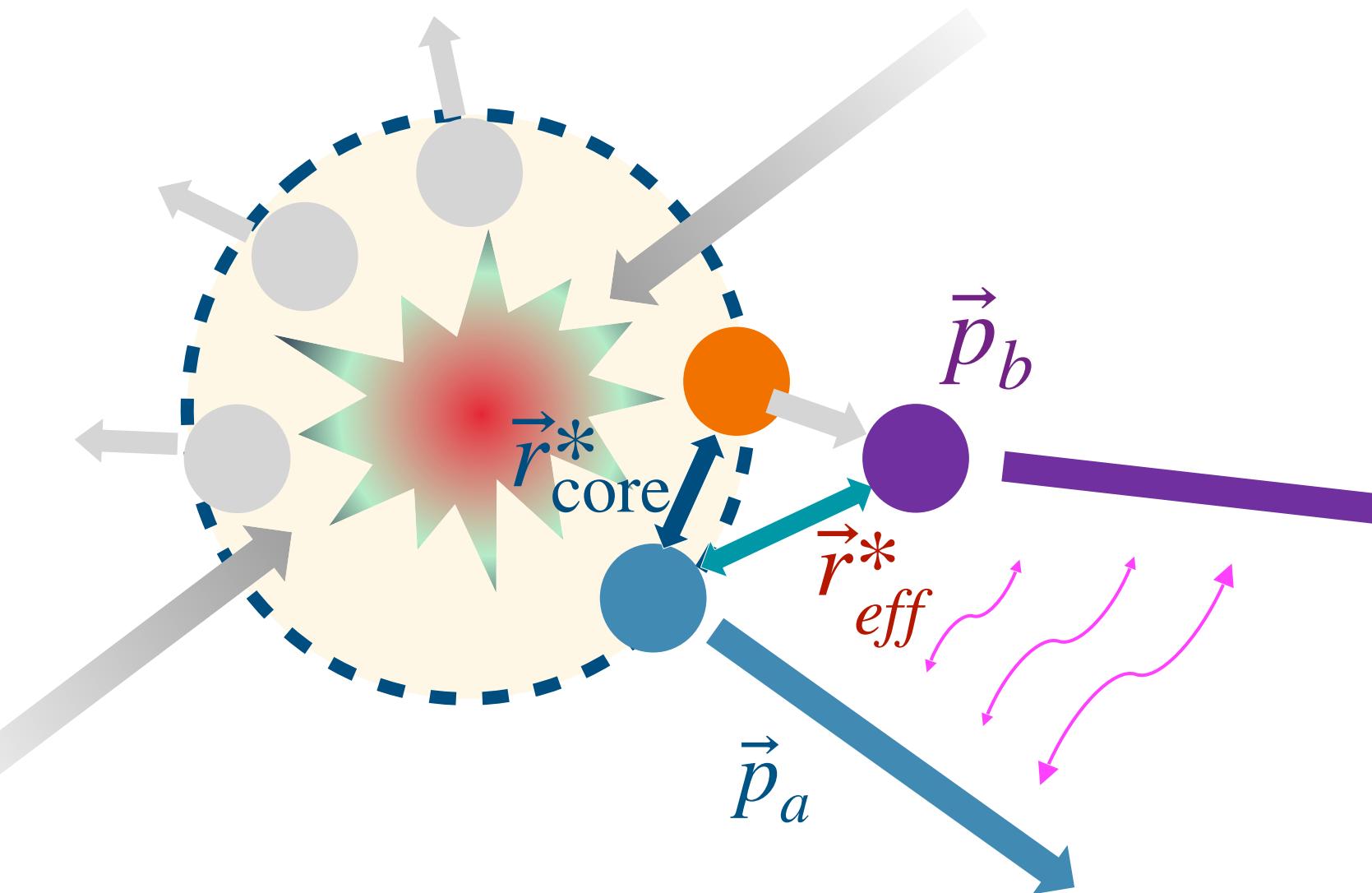


Source size	mean value: $p - d$	mean value: $K^+ - d$
$r_{\text{core}}$	$0.99 \pm 0.05 \text{ fm}$	$1.04 \pm 0.04 \text{ fm}$

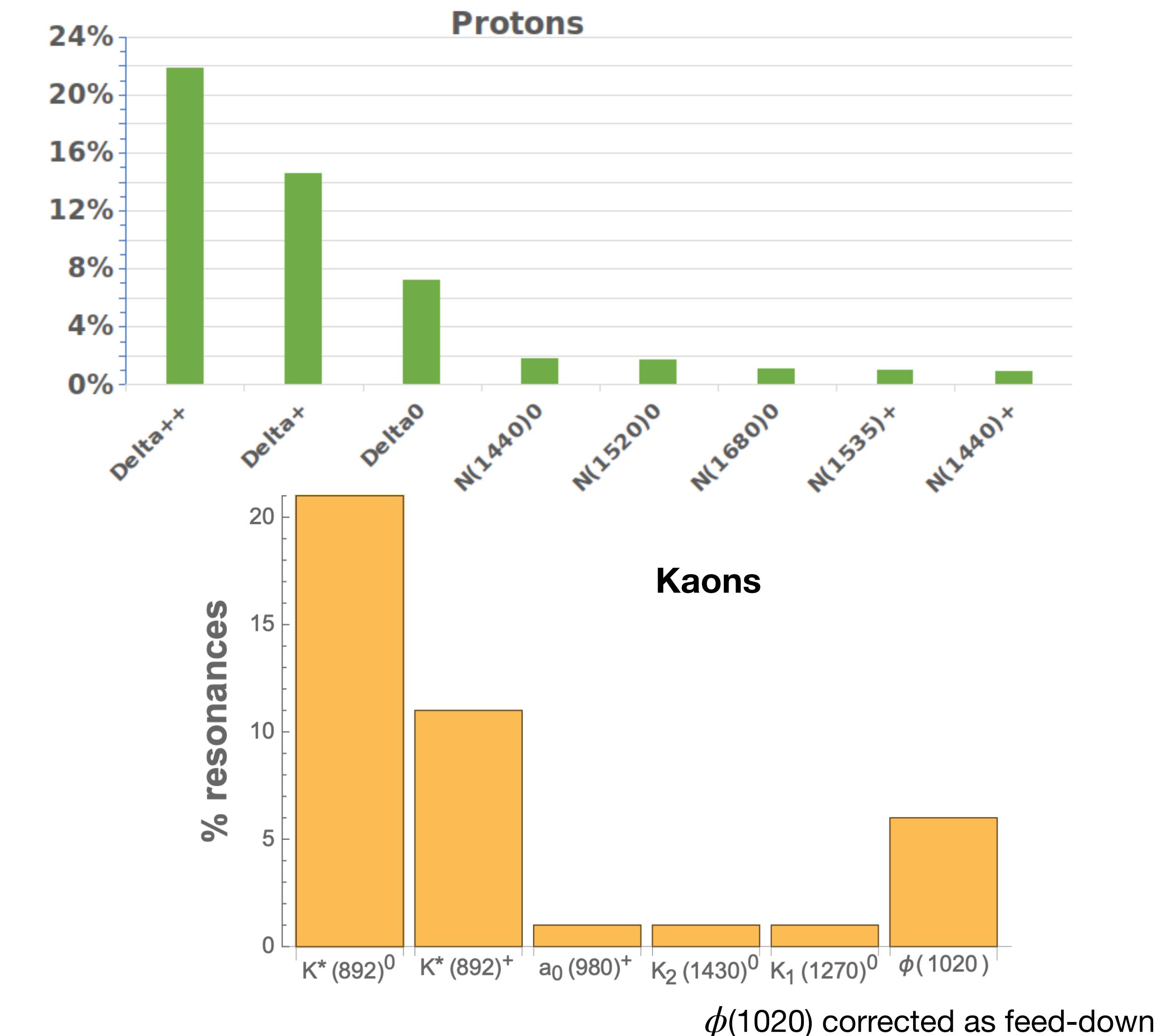


# Source for kaon-deuteron and proton-deuteron pairs

- Primordial source size for  $K^+ - d$  and  $p - d$  systems
- Source radius is effectively increased by **short-lived strongly decaying resonance**



Source size	mean value: $p - d$	mean value: $K^+ - d$
$r_{core}$	$0.99 \pm 0.05$ fm	$1.04 \pm 0.04$ fm
$r_{eff}$	$1.08 \pm 0.06$ fm	$1.35 \pm 0.05$ fm



# Theoretical approach correlation functions

- Potential approach: solve Schrödinger equation for the two-hadron system<sup>[1]</sup>

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  - Considers Coulomb effects

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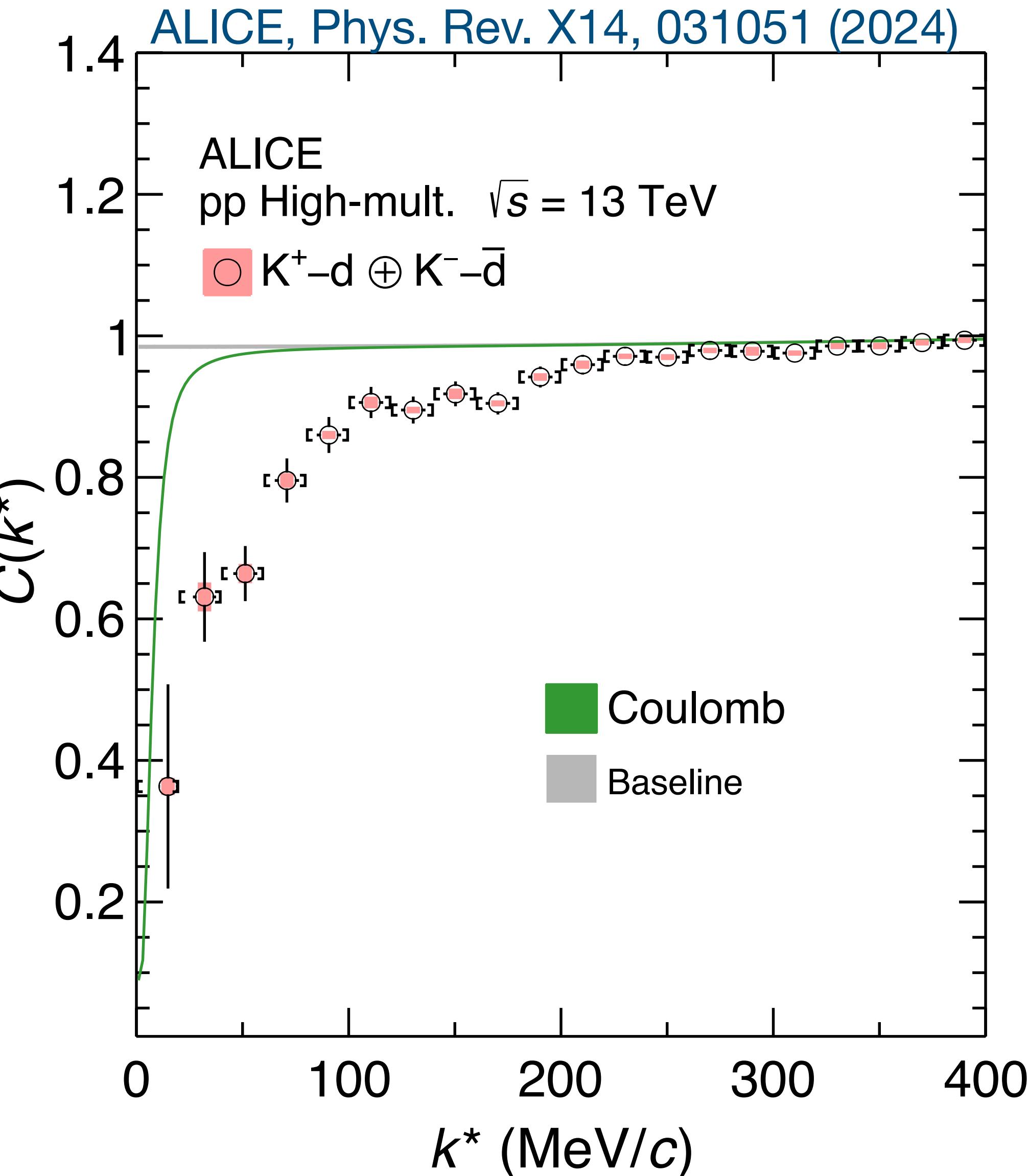
- $f_c$ : Coulomb normalized scattering amplitude for strong interaction,  $F$  and  $\tilde{G}$  are Coulomb functions
  - $a_0$ : scattering length
  - $d_0$ : effective range

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# Kaon-deuteron correlation function

- Assuming  $m_T$ -scaling holds for d,  $r_{\text{eff}} = 1.35 \pm 0.05$  fm
- Coulomb potential: disagree



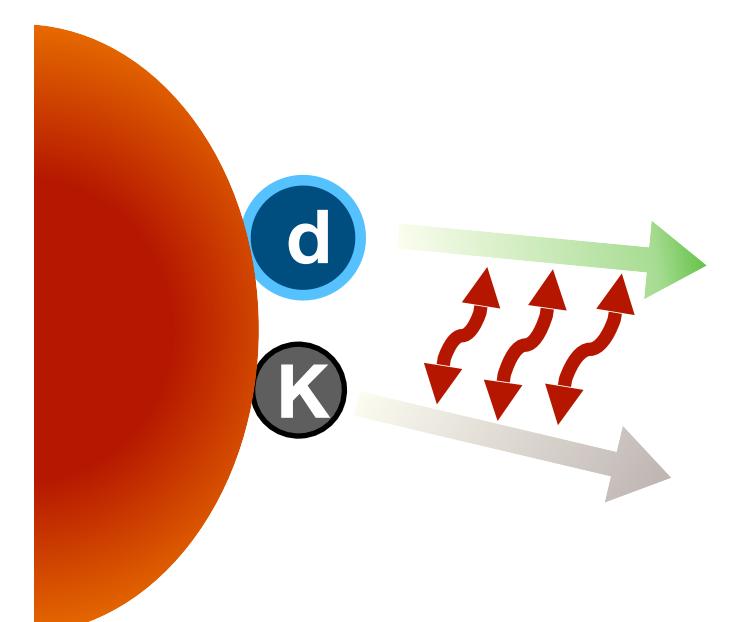
[1] R. Lednický, Phys. Part. Nuc. 40, (2009)

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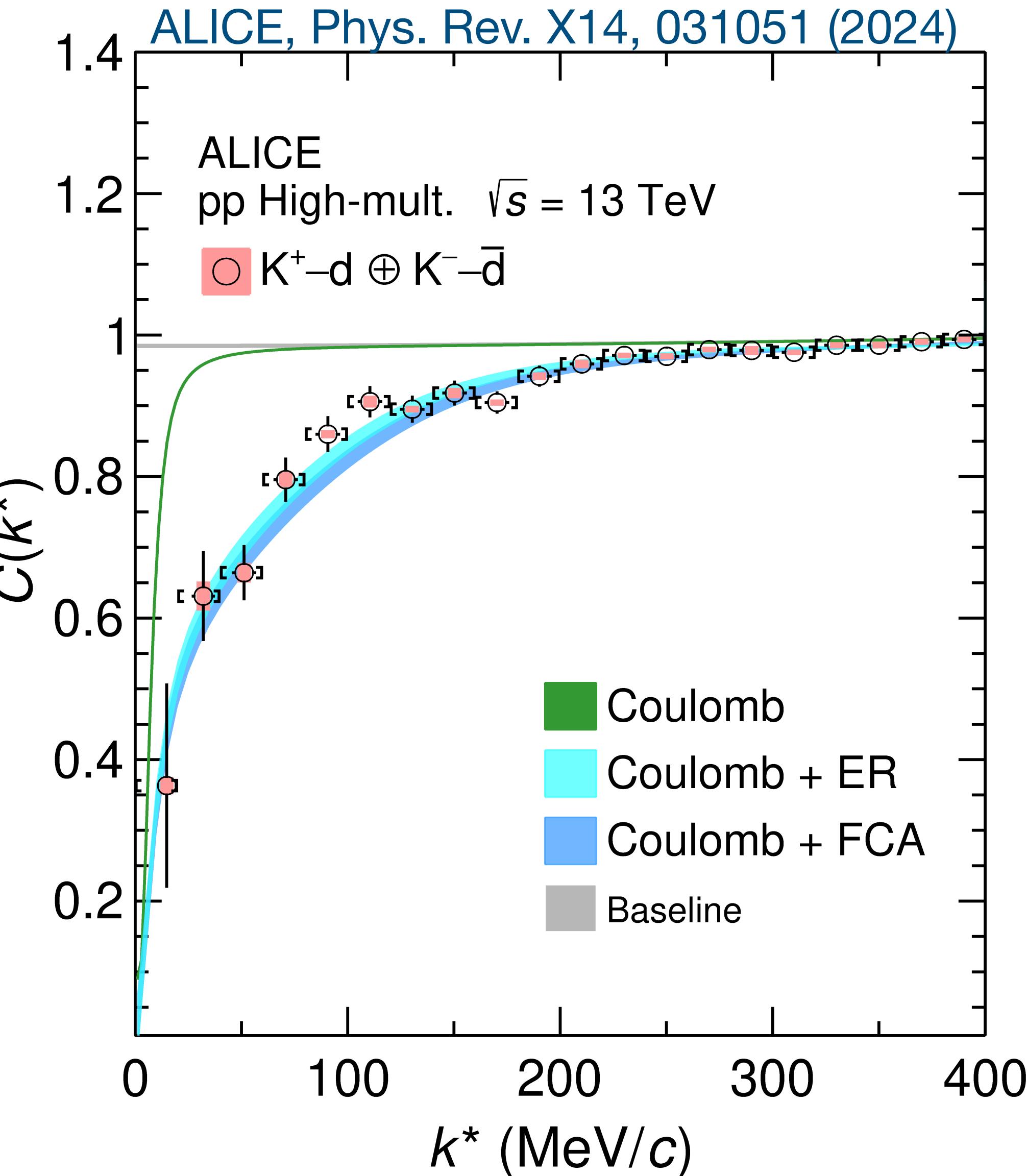
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- Strong interaction in  $K^+ - d$  as an **effective two-body system**:  
Lednický-Lyuboshits approach<sup>[1]</sup>
  - Effective-Range approx. (ER):  $a_0 = -0.47$  fm,  $d_0 = -1.75$  fm<sup>[2]</sup>
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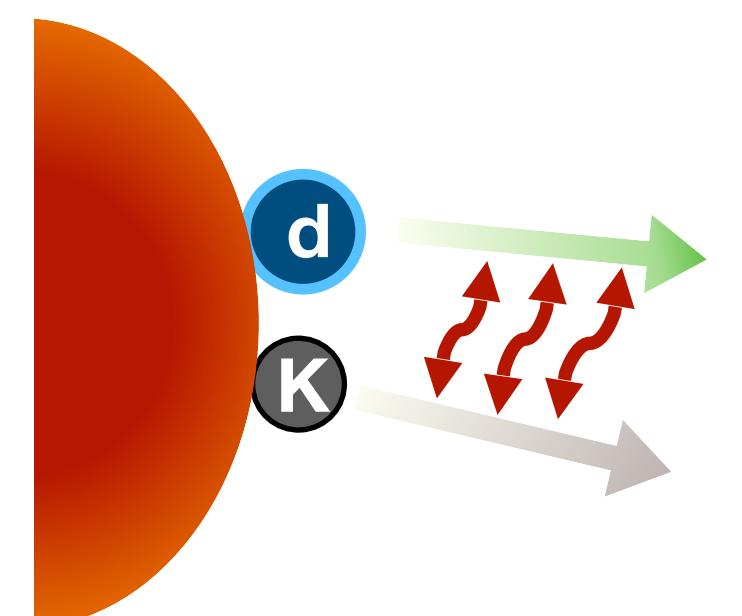
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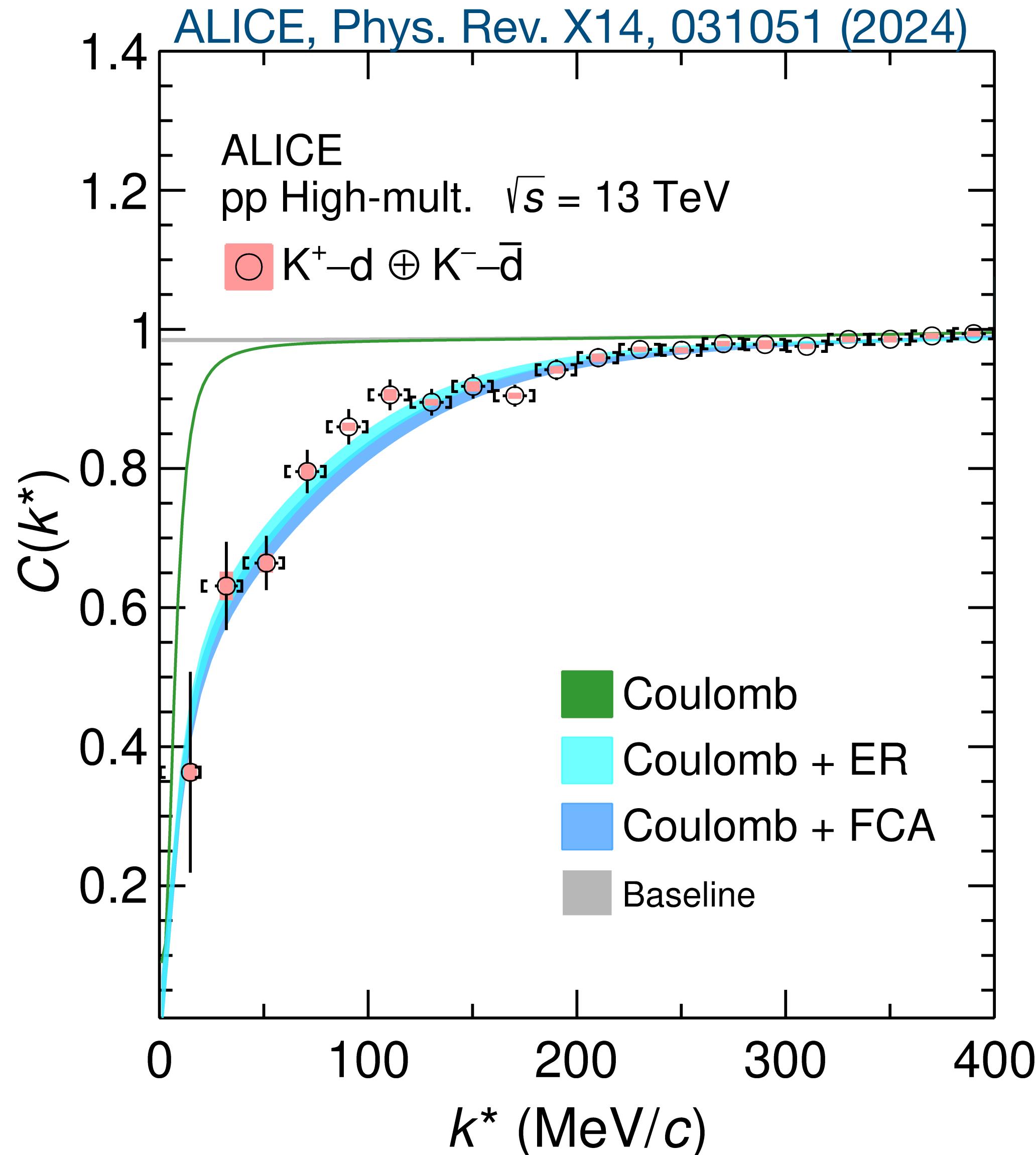
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- Deuterons follow the  $m_T$ -scaling, and an effective two-body approach can describe the  $K^+ - d$  system**



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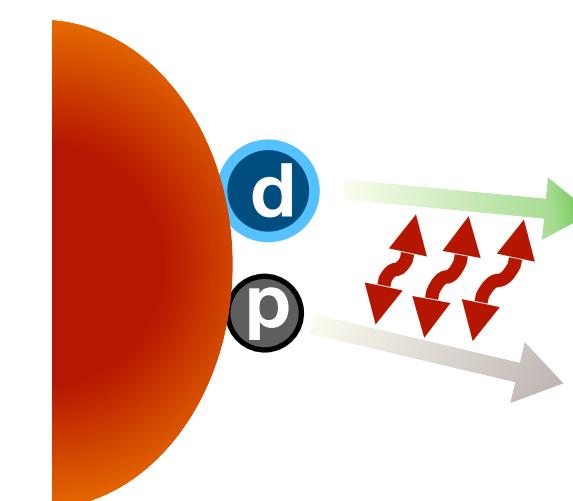
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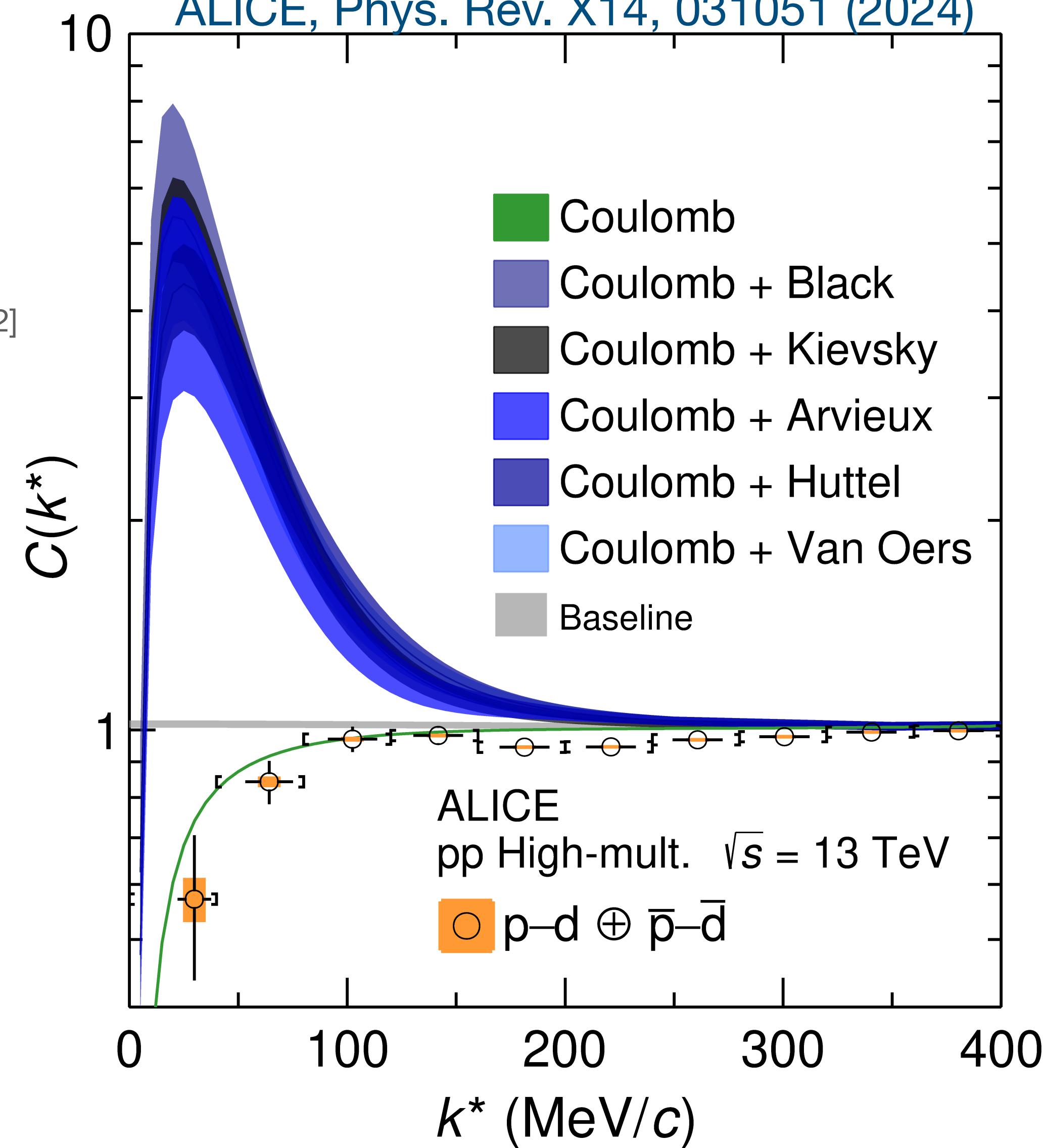


# Proton-deuteron correlation function

- Assuming p-d as an **effective two-body**: Lednický-Lyuboshits approach<sup>[1]</sup>
- Source size  $r_{\text{eff}} = 1.08 \pm 0.06 \text{ fm}$
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ALICE, Phys. Rev. X14, 031051 (2024)



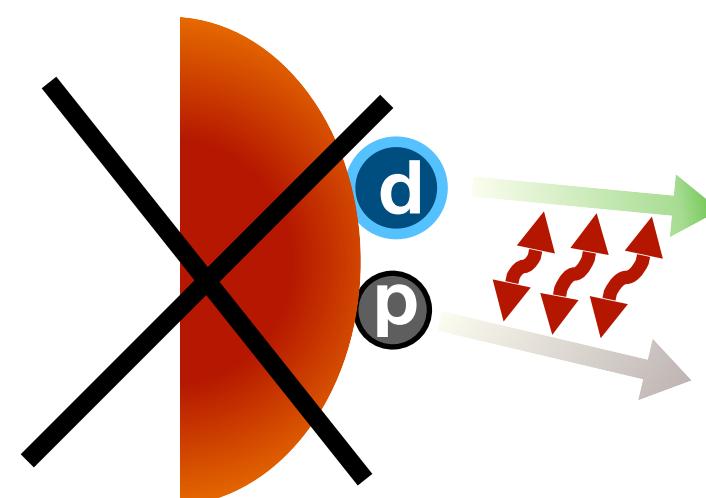
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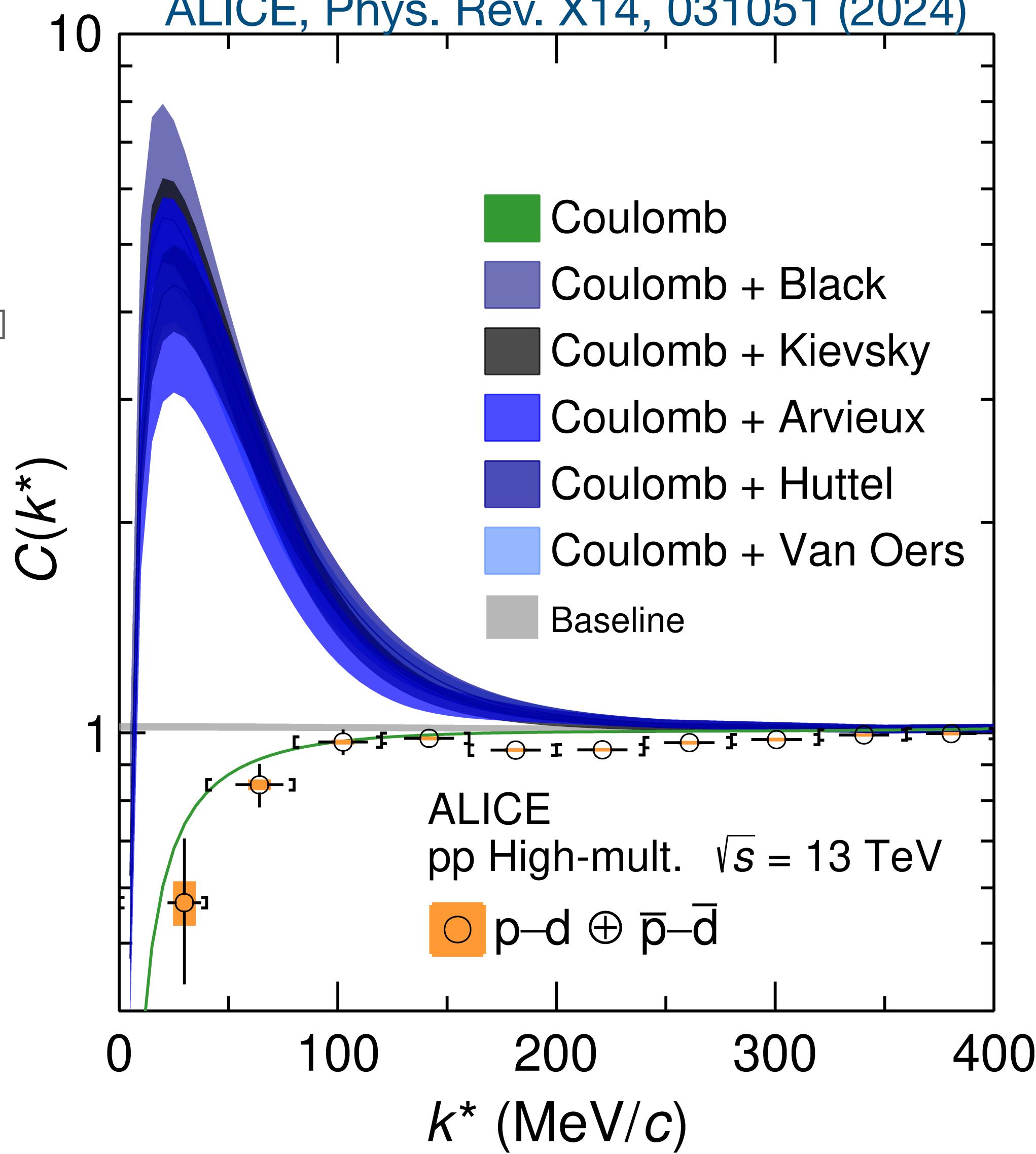
ALI-PUB-556039

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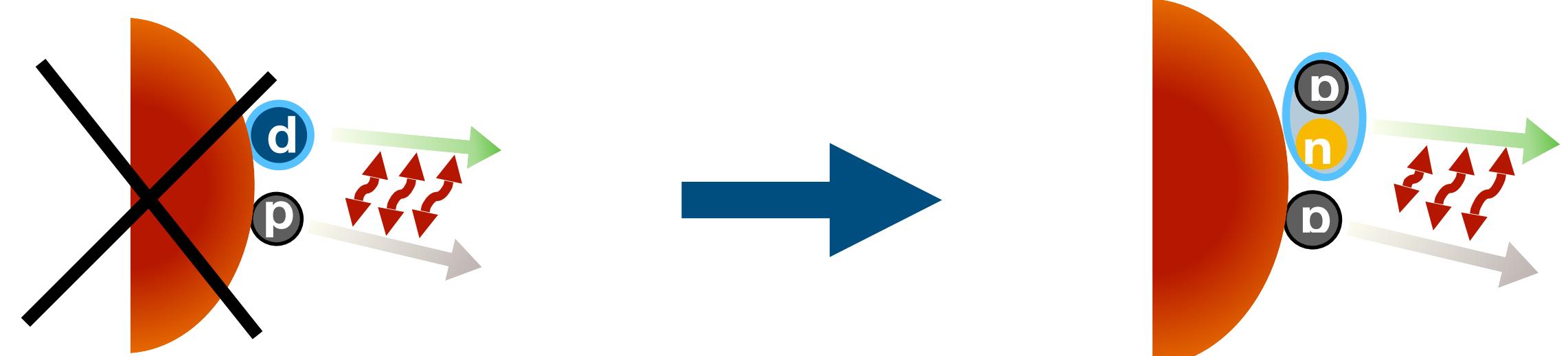
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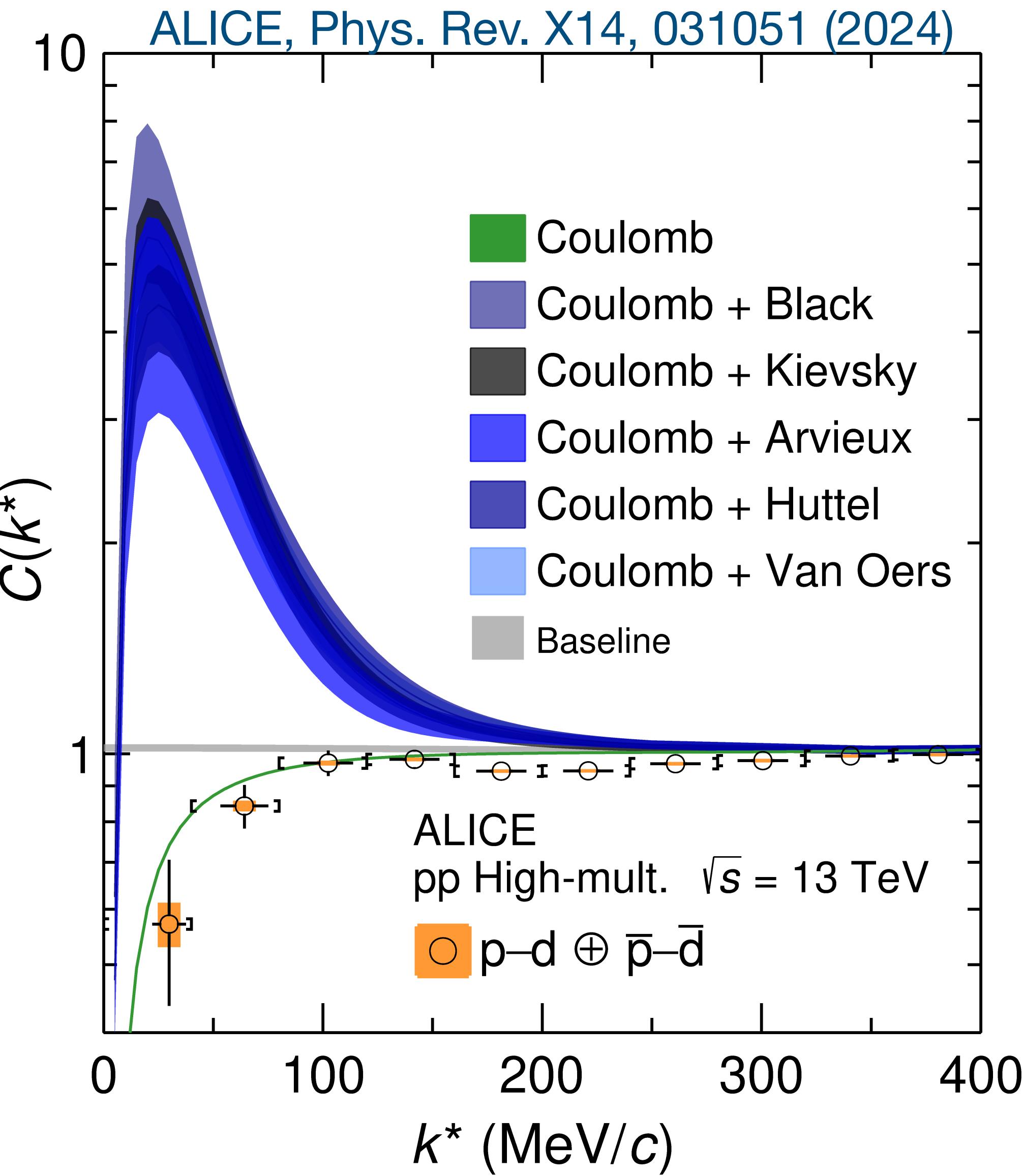
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**Need for three-body calculations accounting for p-(pn) dynamics**



[1] R. Lednický, Phys. Part. Nuc. 40, (2009)

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# Full three-body treatment for p-d

- Start from p-(pn) system that forms p-d state asymptotically:

$$\begin{aligned} C_{pd}(k^*) &= \frac{1}{6A_d} \sum_{m_1, m_2} \int d^3r_1 d^3r_2 d^3r_3 S_1(r_1) S_1(r_2) S_1(r_3) \left| \Psi_{m_1, m_2, k^*} \right|^2 \\ &= \frac{1}{16A_d} \int S(\rho, R_M) \left| \Psi(k^*, \rho) \right|^2 \rho^5 d\rho d\Omega \end{aligned}$$

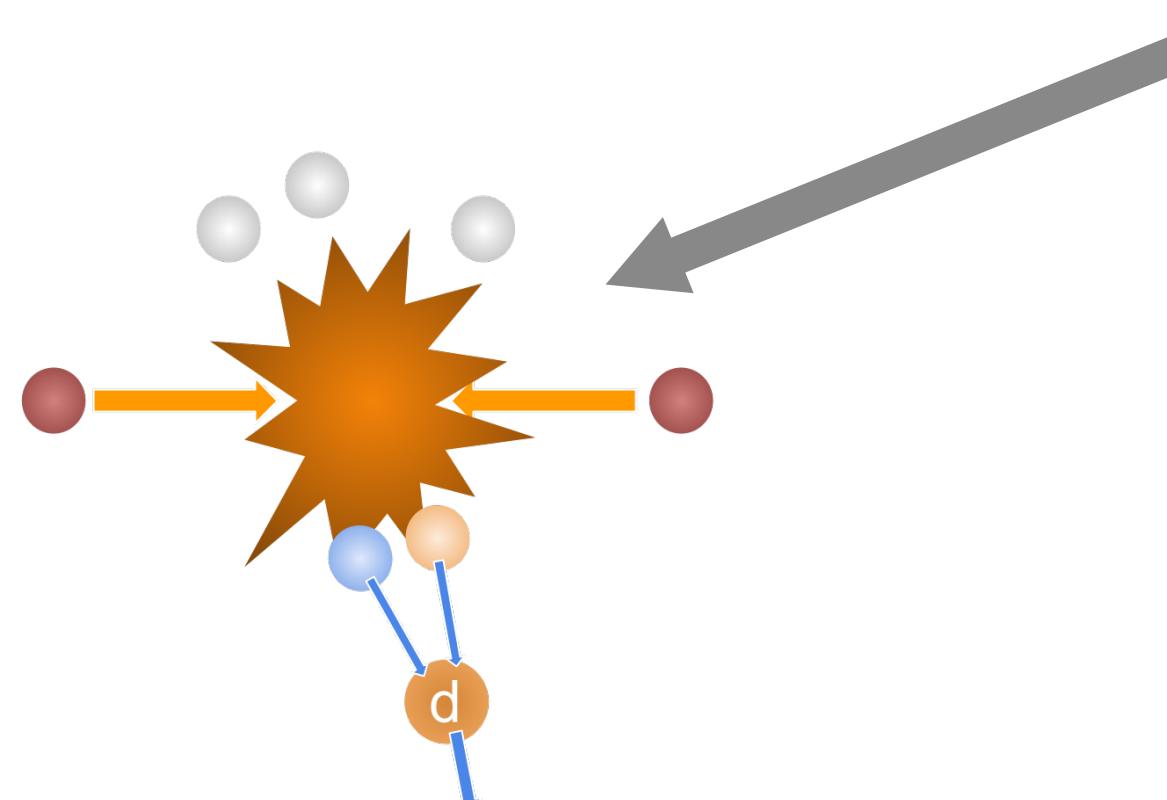
M. Viviani, B. Singh et al. Phys. Rev. C 108, 064002 (2023)

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M. Viviani, B. Singh et al. Phys. Rev. C 108, 064002 (2023)

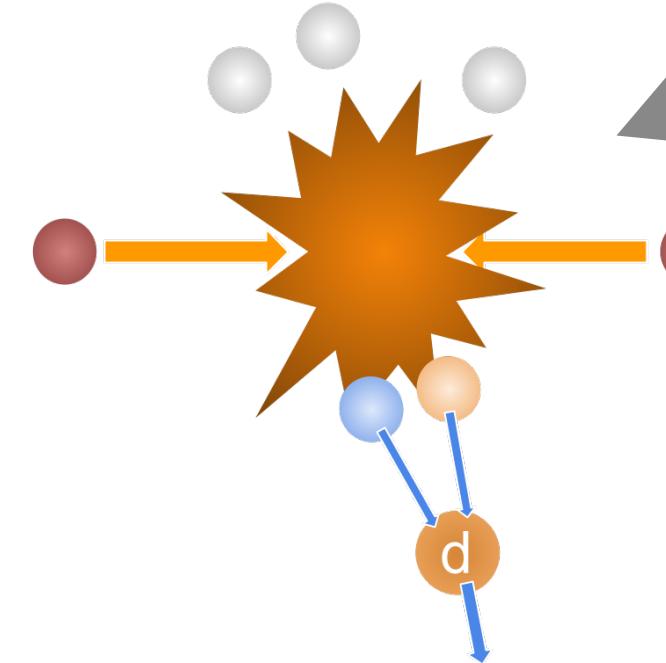
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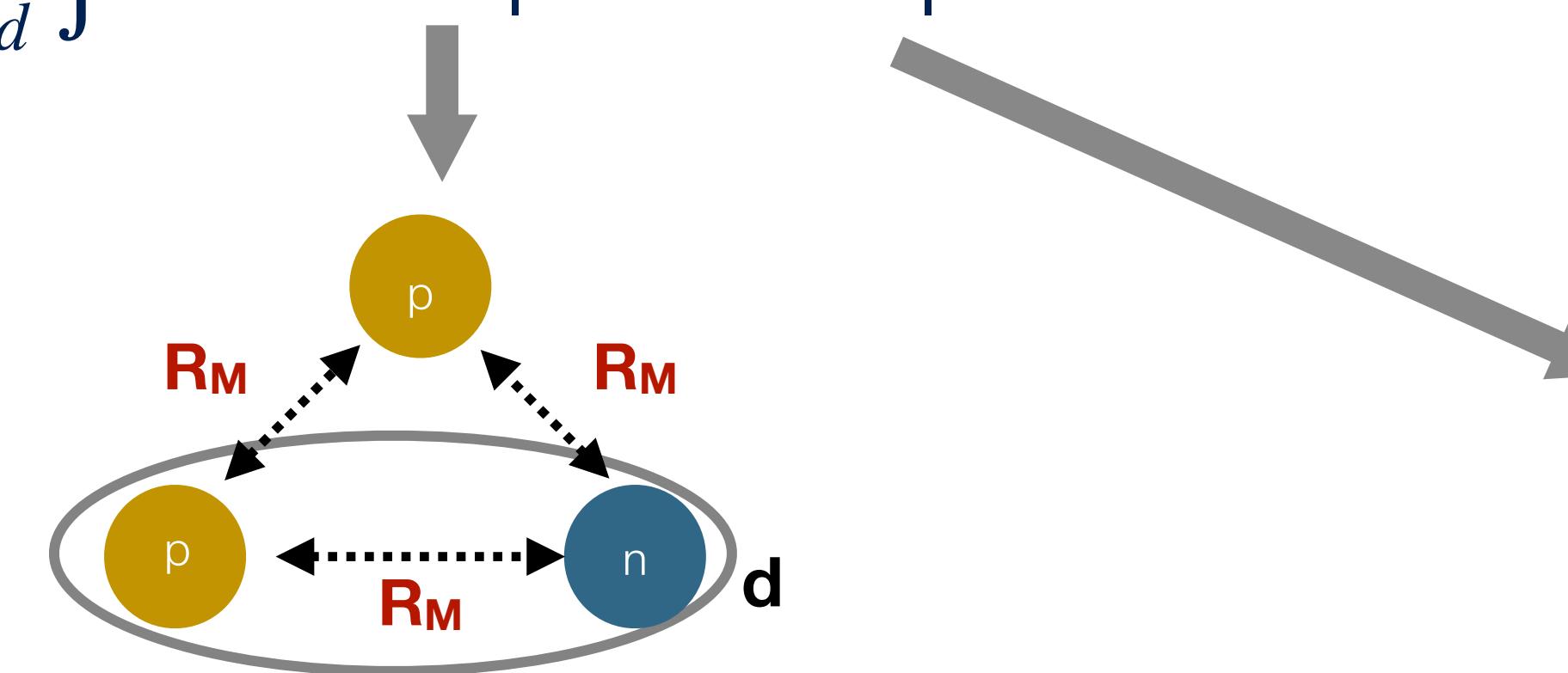
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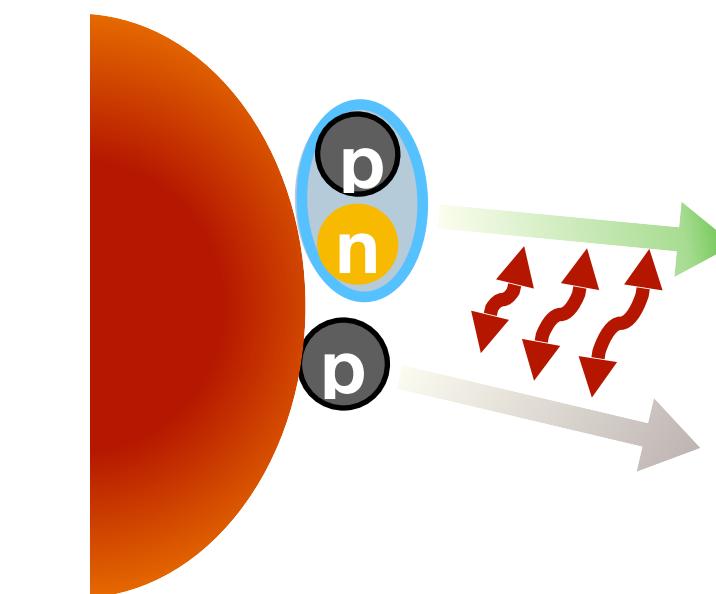
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$\Psi(k^*, \rho)$  the three-nucleon wave function

M. Viviani, B. Singh et al. Phys. Rev. C 108, 064002 (2023)

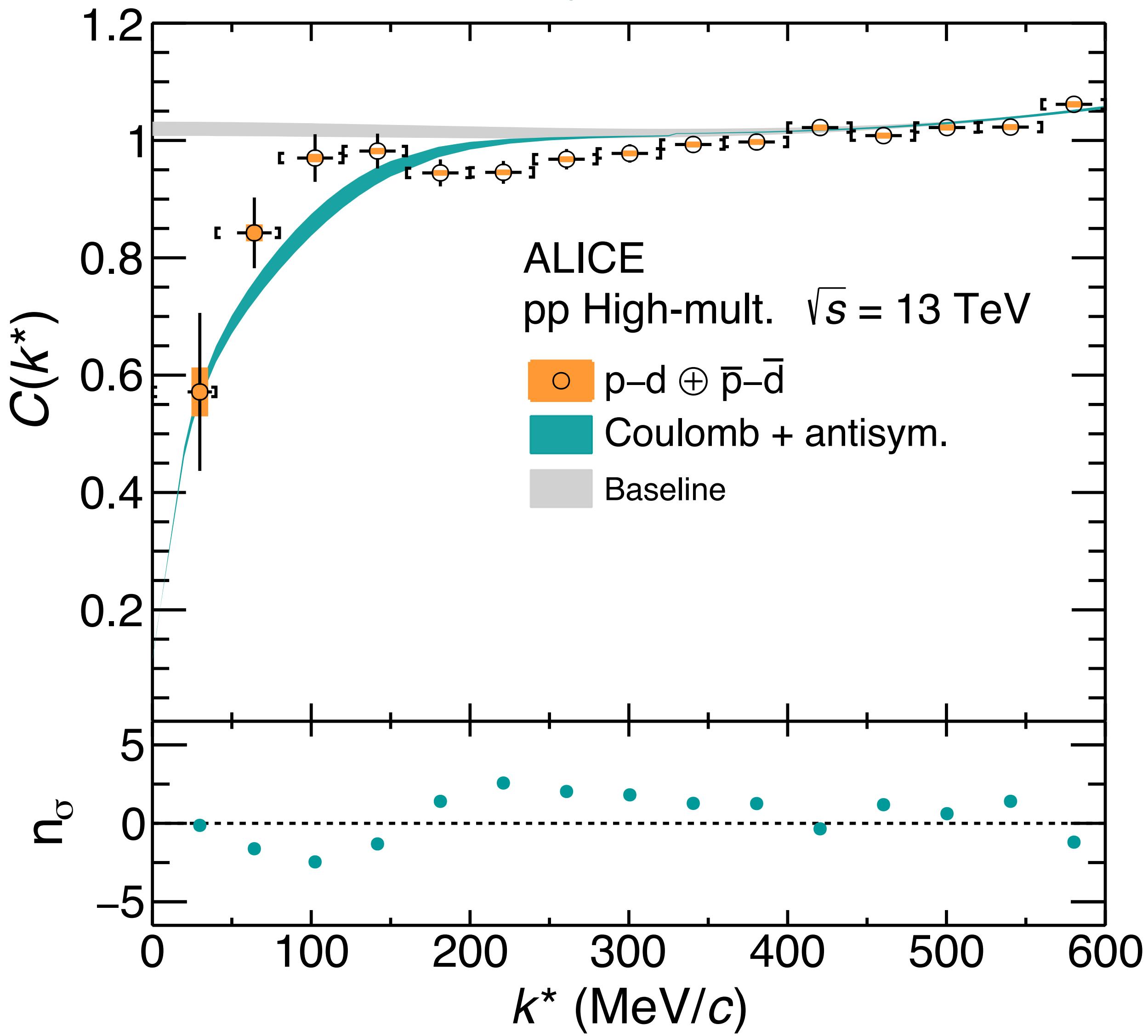
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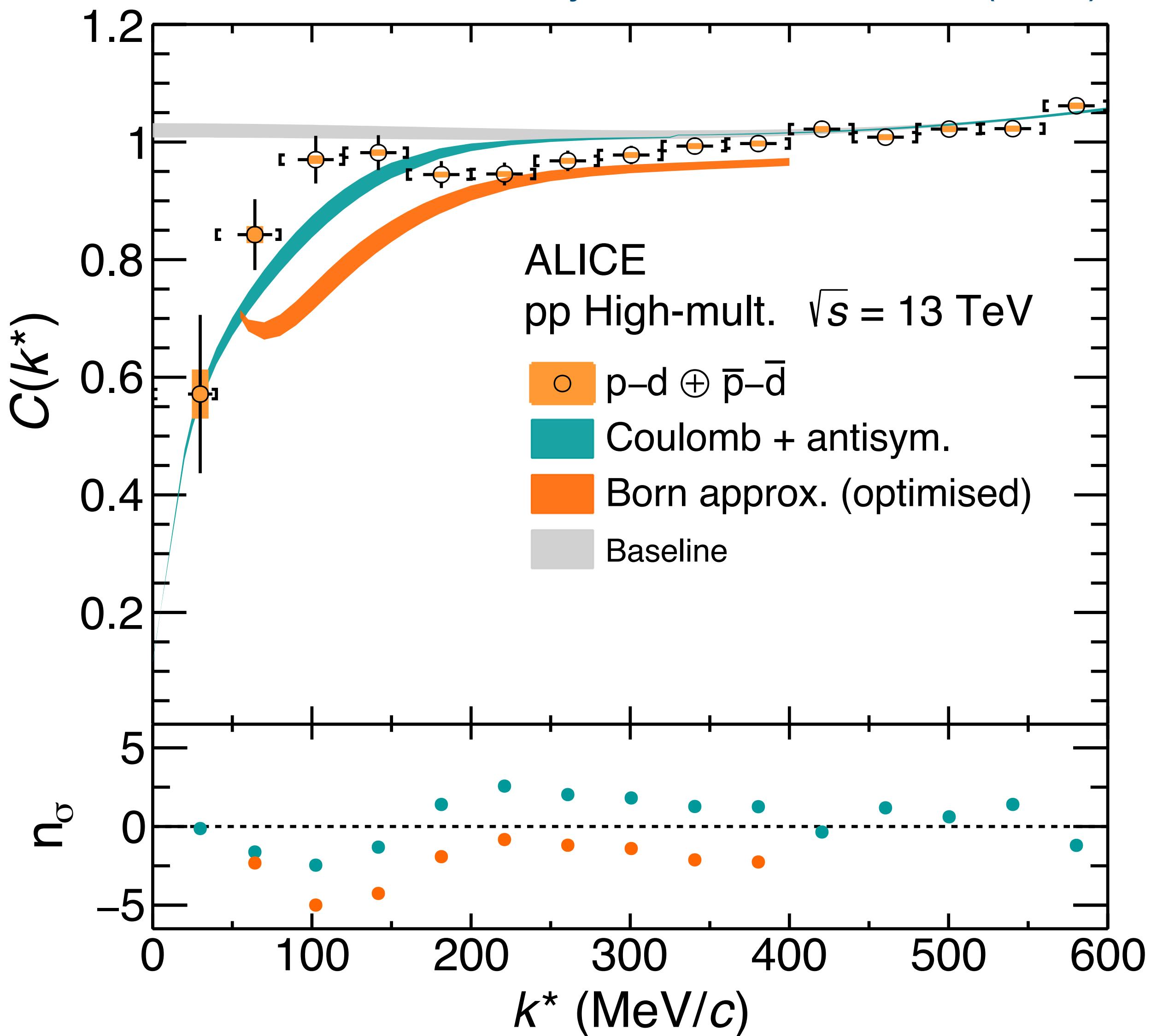
ALICE, Phys. Rev. X14, 031051 (2024)



# Asymptotic form of strong interaction in p-d system

- Coulomb only: does not describe the data
- Born approximated wavefunction NN [1-2] NNN potentials<sup>[3]</sup>
  - Perform antisymmetrization
  - Approximate the wavefunction by ignoring centrifugal core interaction
  - Asymptotic form of strong interaction is insufficient to capture the dynamics of nucleons  
 $\sim 1 \text{ fm}$

ALICE, Phys. Rev. X14, 031051 (2024)



[1] M. Viviani, B. Singh et al. Phys. Rev. C108, 064002 (2023)

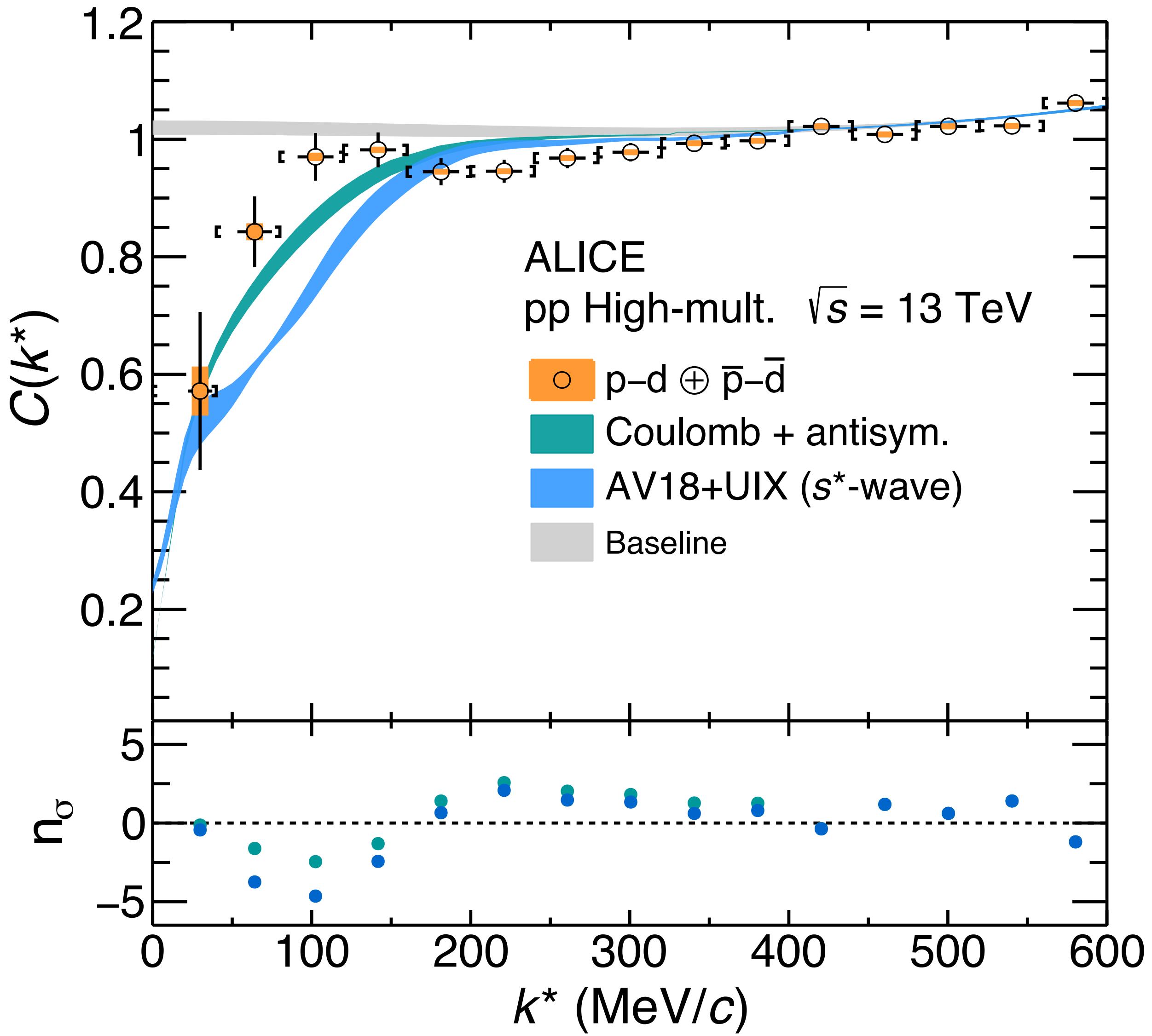
[2] AV 18 NN potential: R. B. Wiringa et al. Phys. Rev. C 51, 38 (1995)

[3] UIX NNN potential: B. S. Pudliner et al. Phys. Rev. Lett. 74, 4396 (1995)

# Two- and three-body interaction at short distance

- Full three-body dynamics at short distances using AV18+UIX potentials<sup>[1-3]</sup>
  - **s-wave:** undershoots due to repulsion in s-wave

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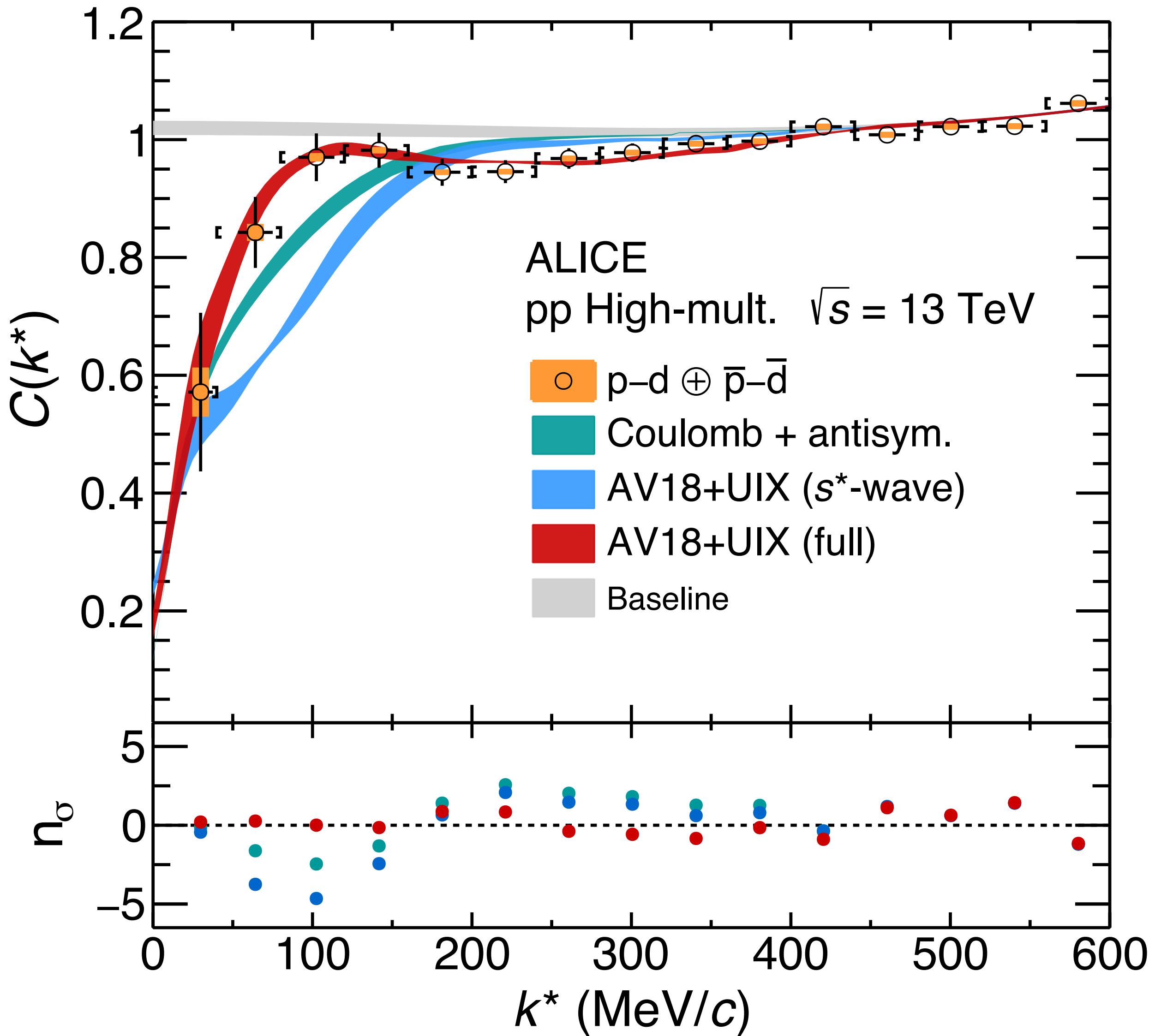
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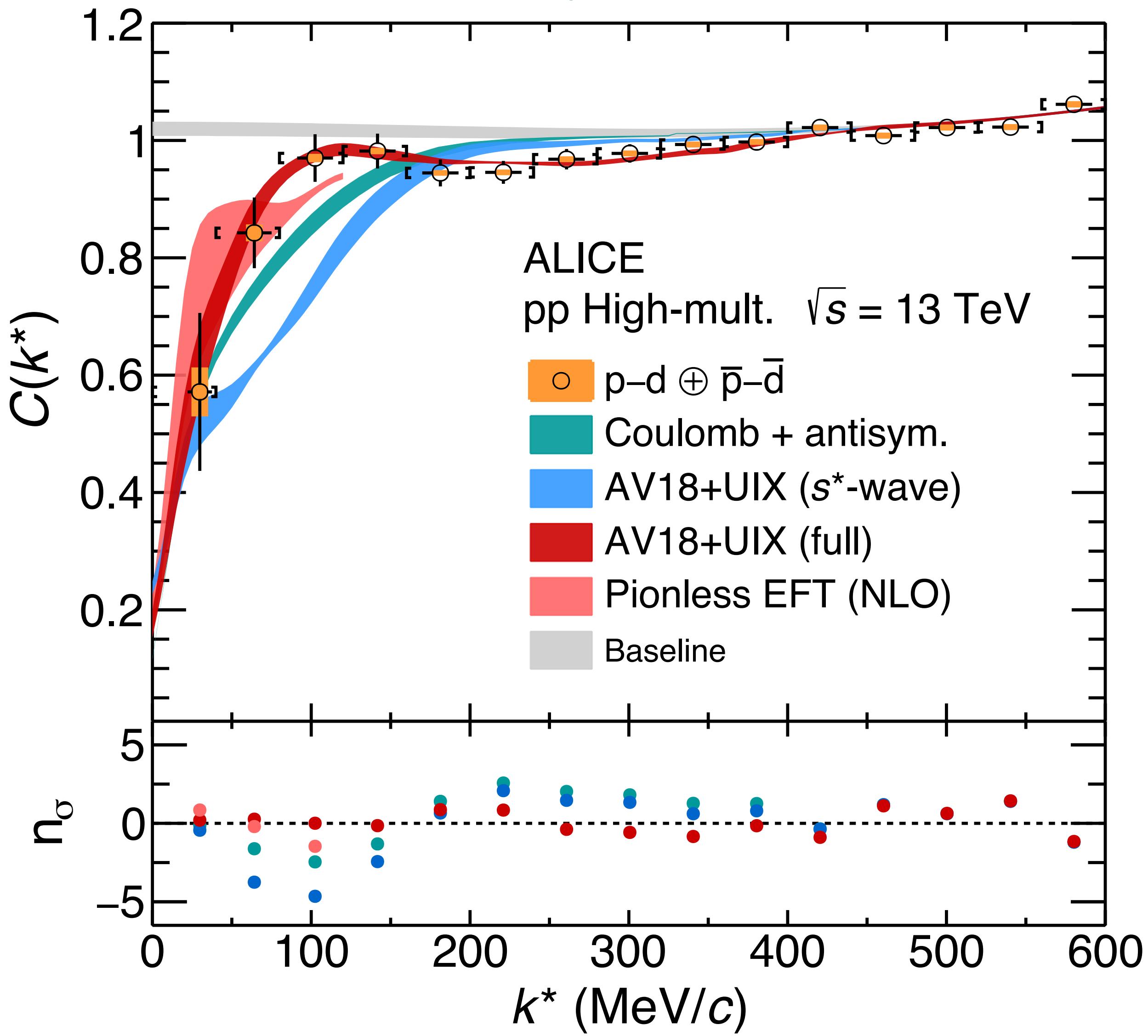
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- **Pionless EFT NLO (s+p+d waves):**
  - Agree with data within  $n_\sigma \sim 2$  for  $k^* < 120$  MeV/c
  - Dynamics of the three-body p-(pn) system at short distances!
  - Inclusion of the higher partial waves

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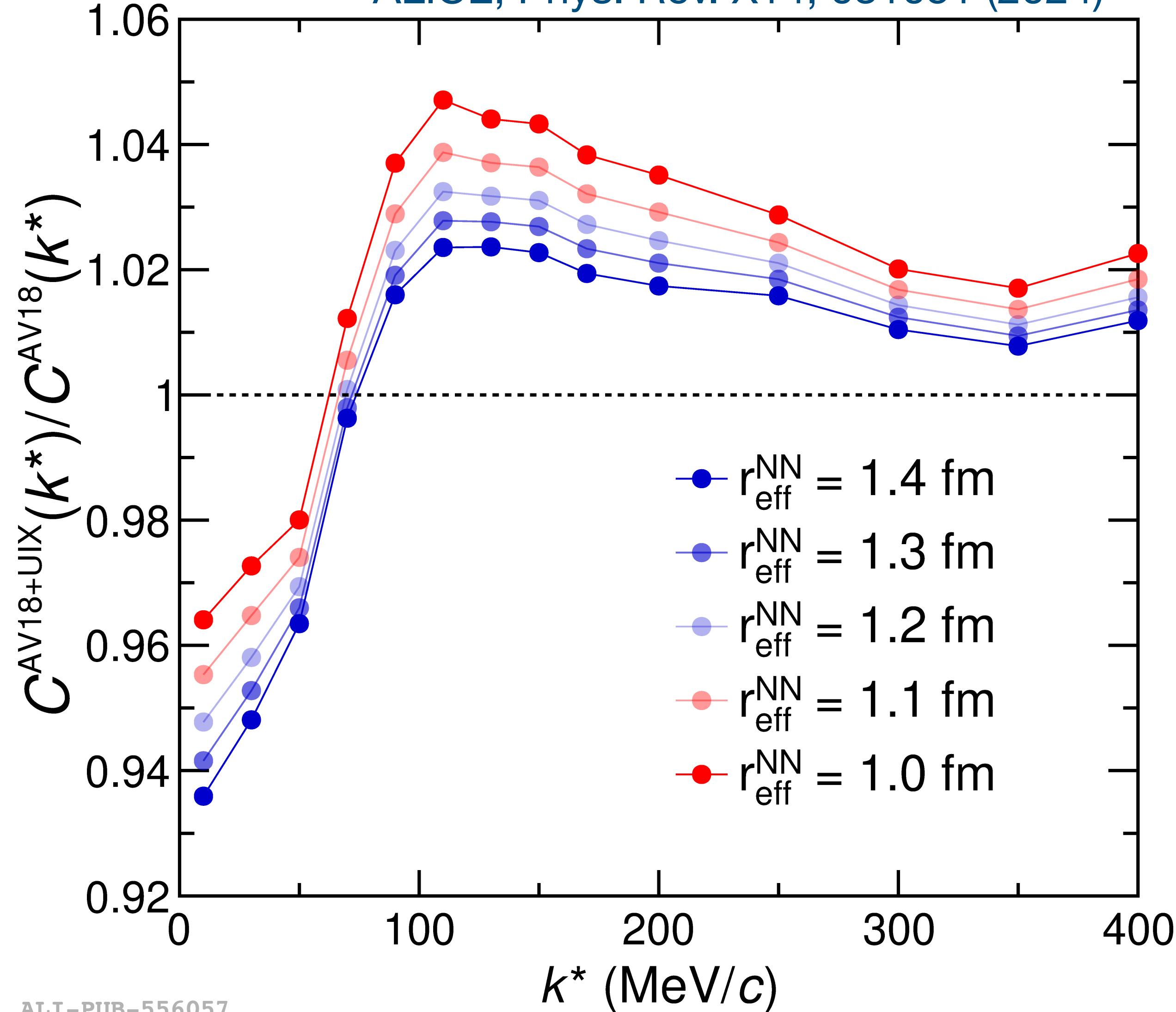
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# Sensitivity to genuine three-body force

- Genuine three-body strong interaction effects:
  - Ratio of CF with and without UIX potential<sup>[1]</sup>
  - Up to ~5% effects due to genuine three-body strong interaction
  - LHC Run 2: limited statistics

ALICE, Phys. Rev. X14, 031051 (2024)

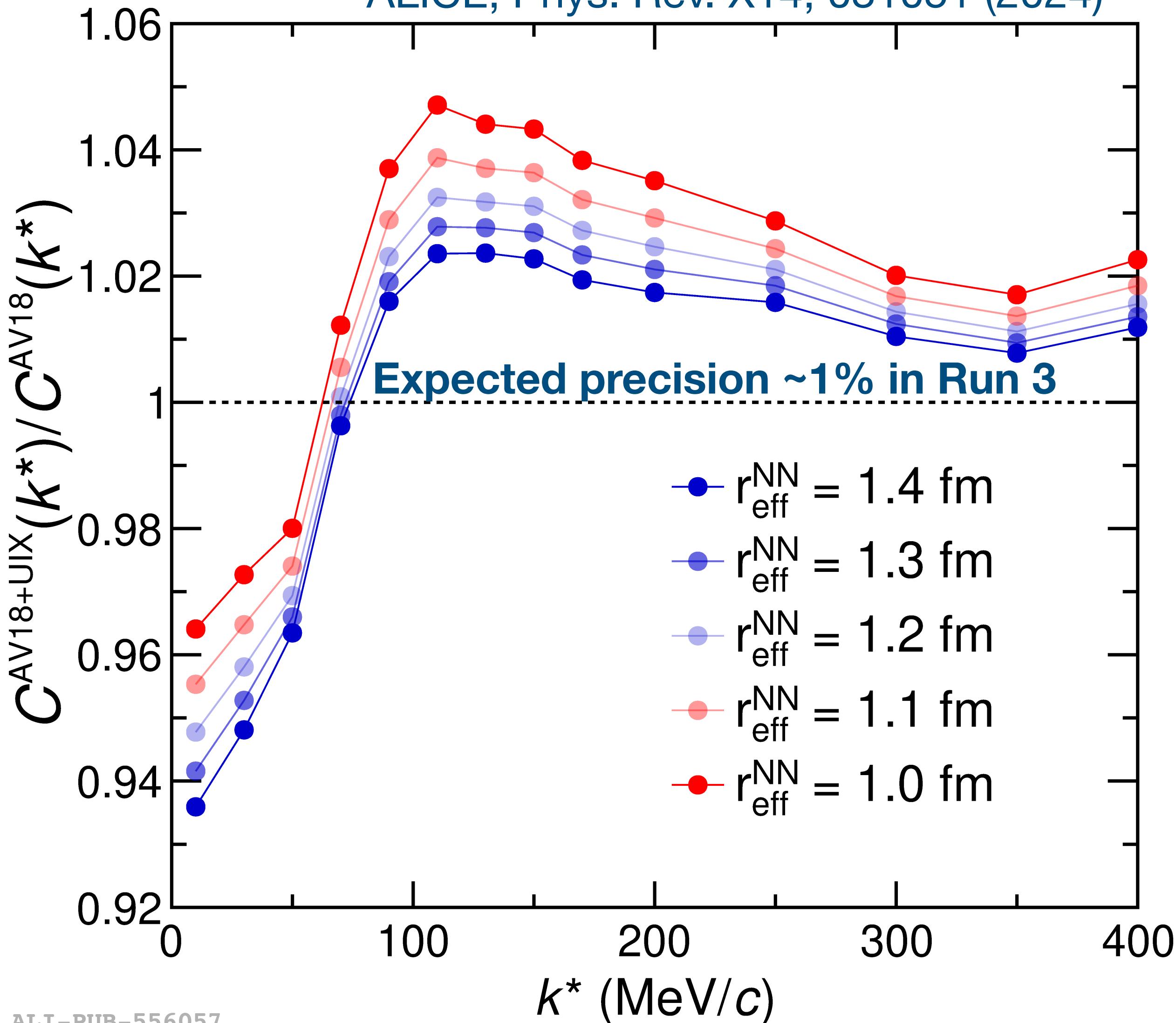


[1] M. Viviani, B. Singh et al. Phys. Rev. C108, 064002 (2023)

# Sensitivity to genuine three-body force

- Genuine three-body strong interaction effects:
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- **LHC Run 3:** ~2 orders of magnitude increase in pair statistics
  - Possibility to perform  $m_T$  differential analysis

ALICE, Phys. Rev. X14, 031051 (2024)

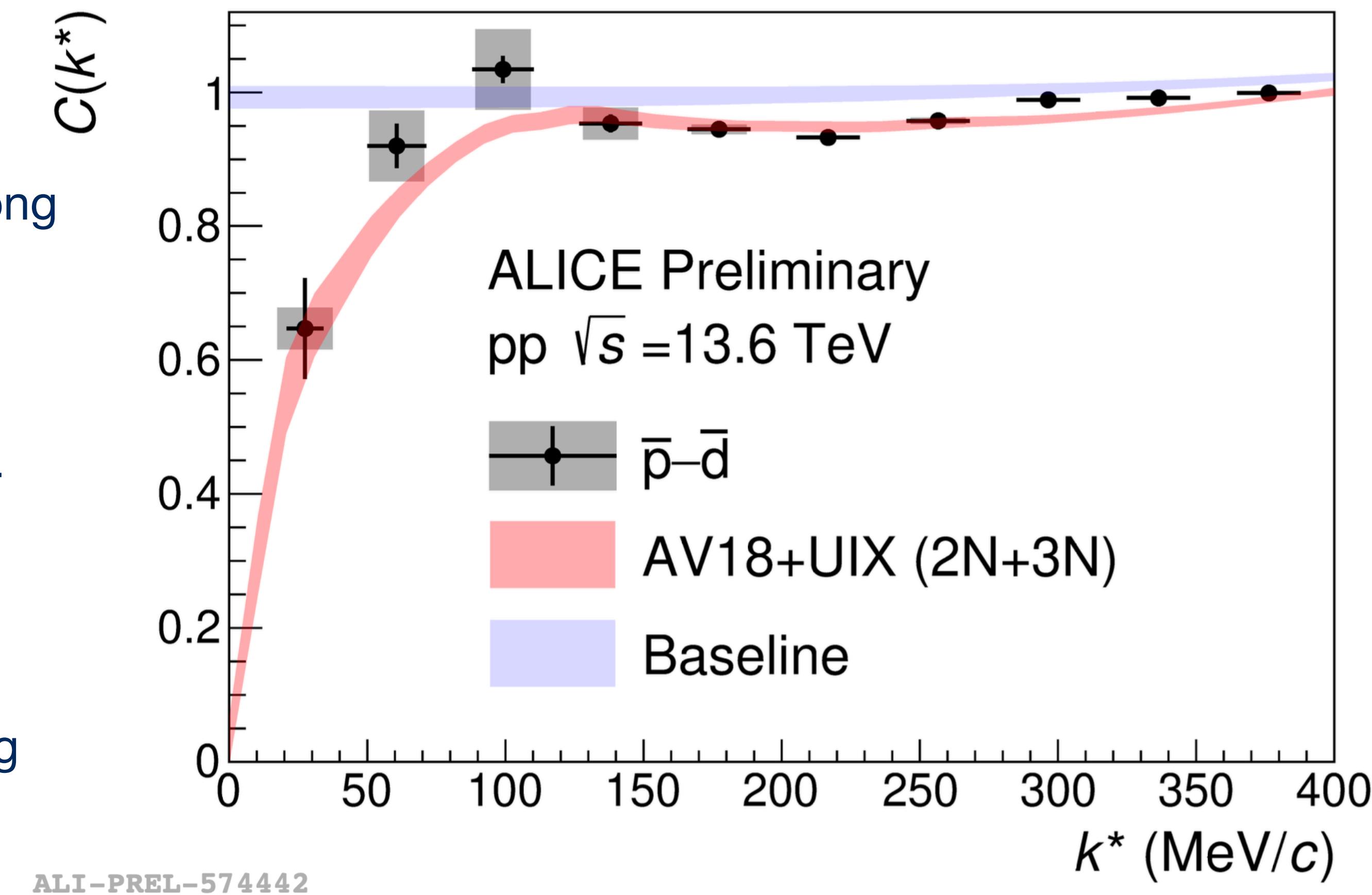


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ALI-PUB-556057

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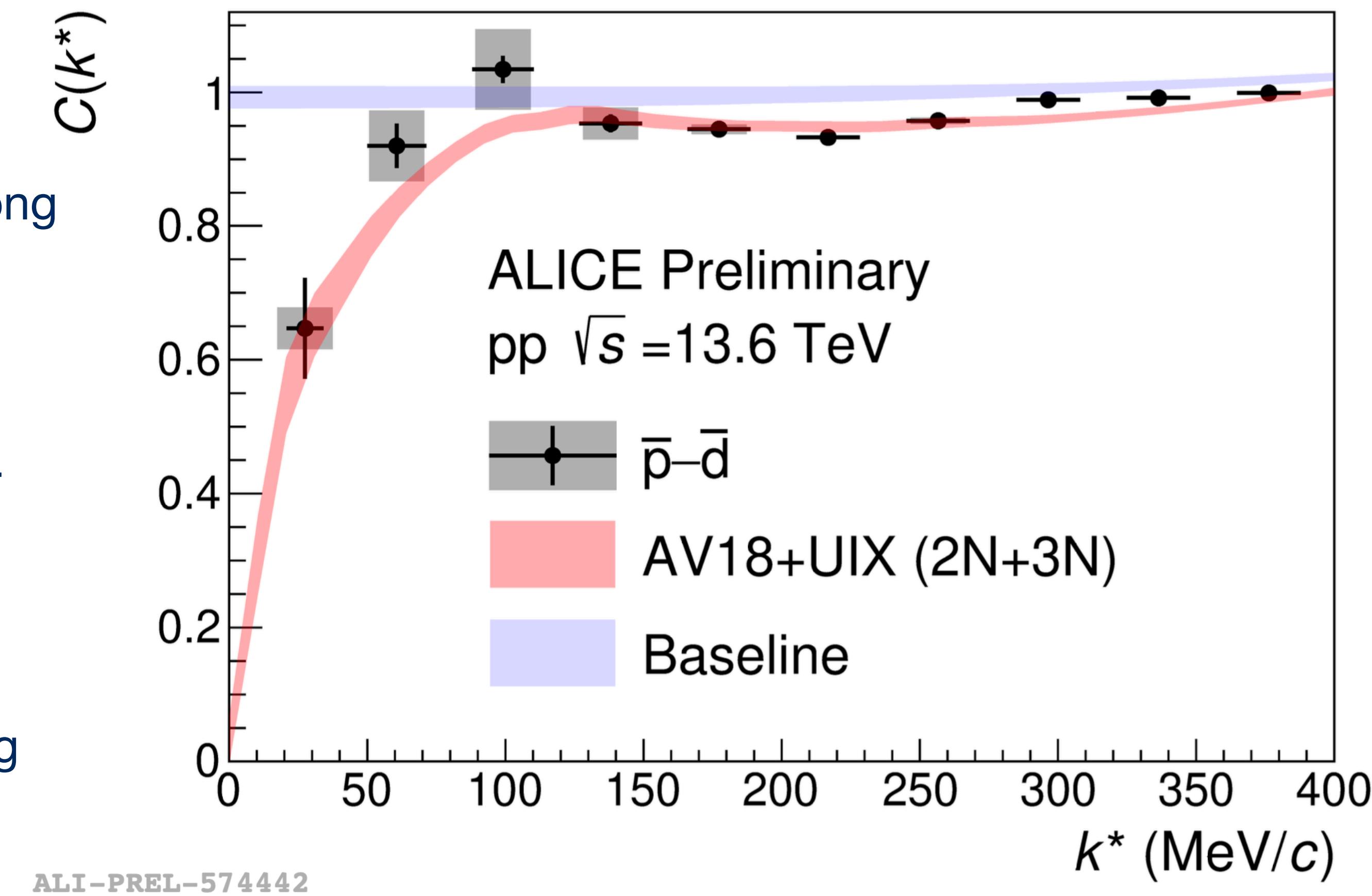
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[1] M. Viviani, B. Singh et al. Phys. Rev. C108,064002 (2023)

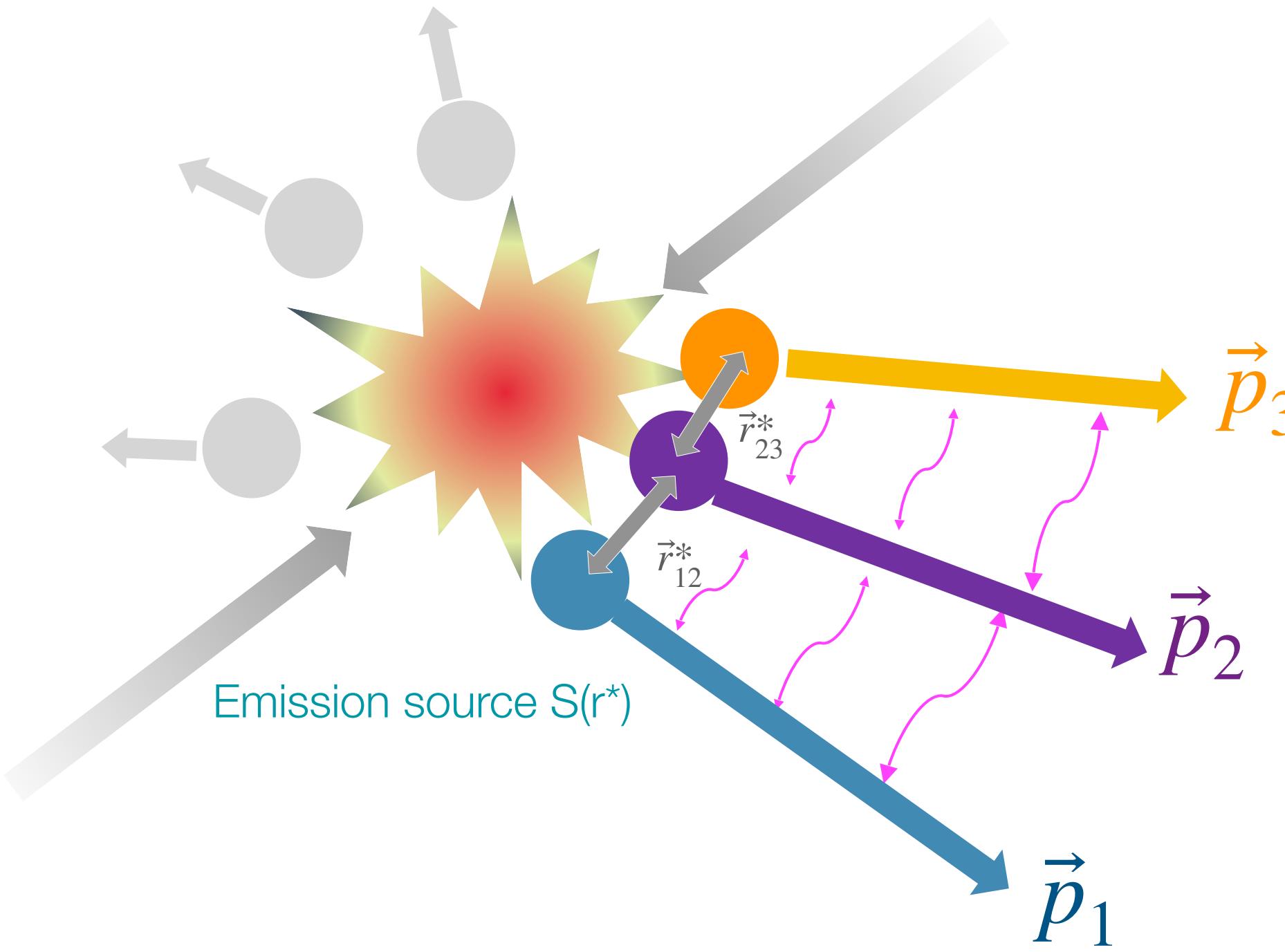
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**Avenue for the study of hadron–deuteron systems, including charm and strange hadrons!**

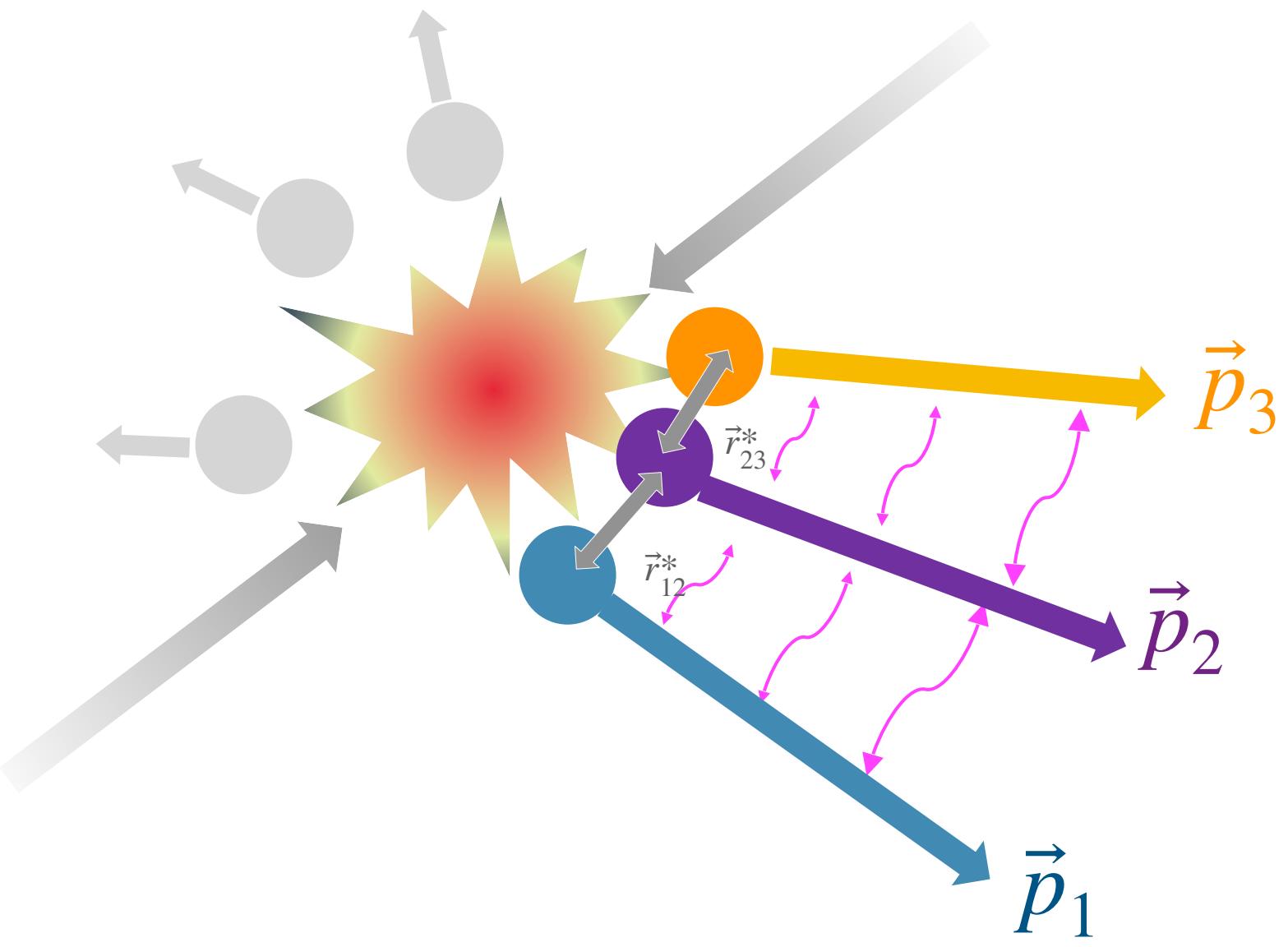
[1] M. Viviani, B. Singh et al. Phys. Rev. C108, 064002 (2023)



**Study correlations among three unbound hadrons  
(3 to 3 scattering process)**

# Three-body femtoscopy

- Study interaction in hadron-triplets via three-particle correlations



- Use Lorentz-invariant hyper-momentum  $Q_3 = \sqrt{-q_{12}^2 - q_{23}^2 - q_{13}^2}$

$$C(Q_3) = N \frac{N_{\text{same}}(Q_3)}{N_{\text{mixed}}(Q_3)}$$

experimental definition [1-2]

$$C(Q_3) = \int S(\rho) \left| \Psi(Q_3, \rho) \right|^2 \rho^5 d\rho$$

theoretical definition [3]

$$\rho = 2\sqrt{r_{12}^2 + r_{23}^2 + r_{31}^2}$$

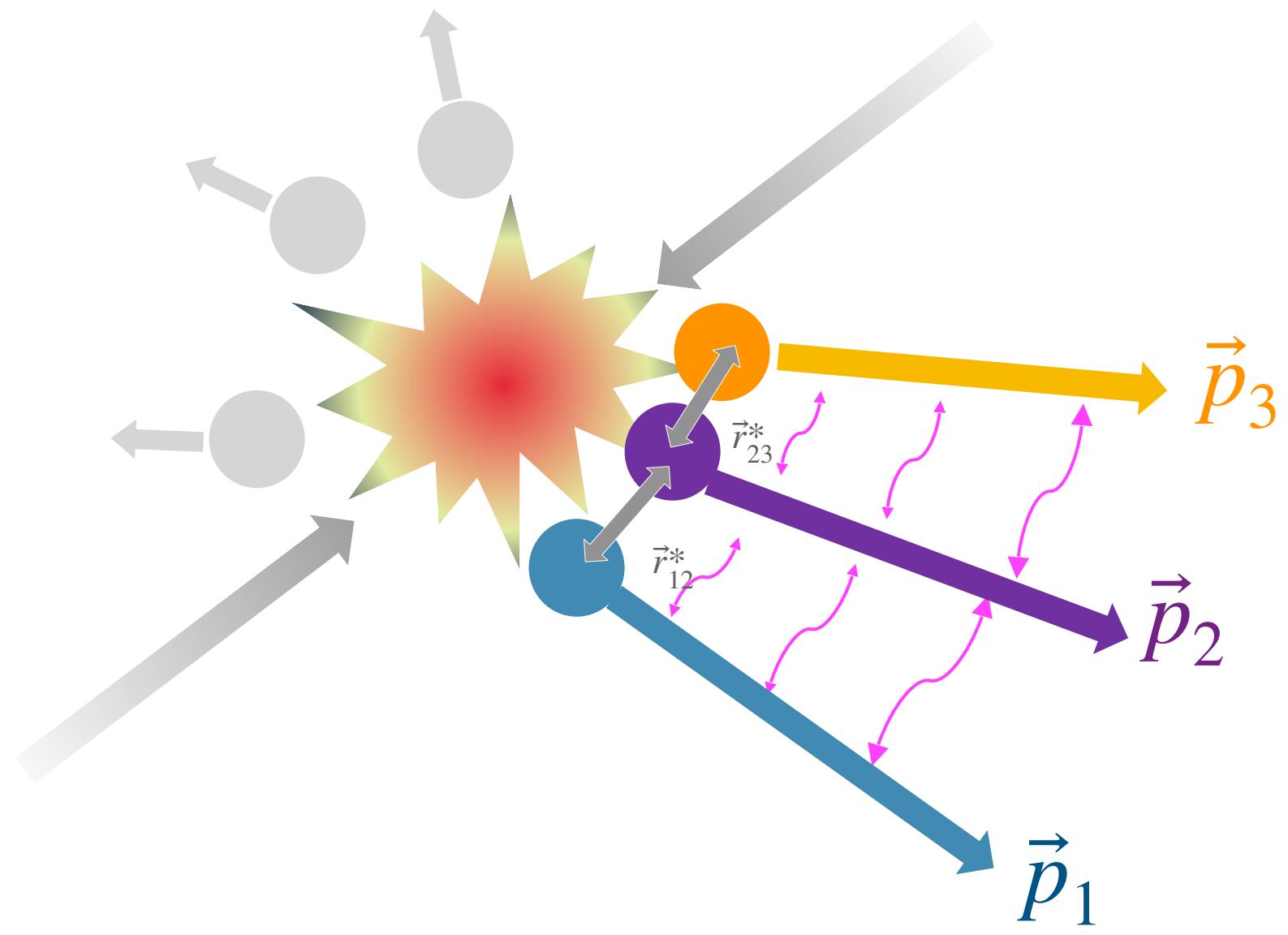
[1] ALICE Coll, Eur. Phys. J. A 59, 145 (2023)

[2] R. Del Grande et al, Eur. Phys. J. C 82 (2022) 244

[3] A. Kievsky et al, Phys. Rev. C 109 (2024) 3, 034006

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Exp:

ALICE Coll., EPJ A 59, 145 (2023)

ALICE Coll., EPJ A 59, 298 (2023)

Theory (Munich and PISA group)

R. Del Grande et al. EPJC 82 (2022) 244

M. Viviani et al, PRC 108 (2023) 6, 064002

A. Kievsky, et al., PRC 109 (2024) 3, 034006

B. E. Garrido et al., arXiv: 2408.01750 (2024)

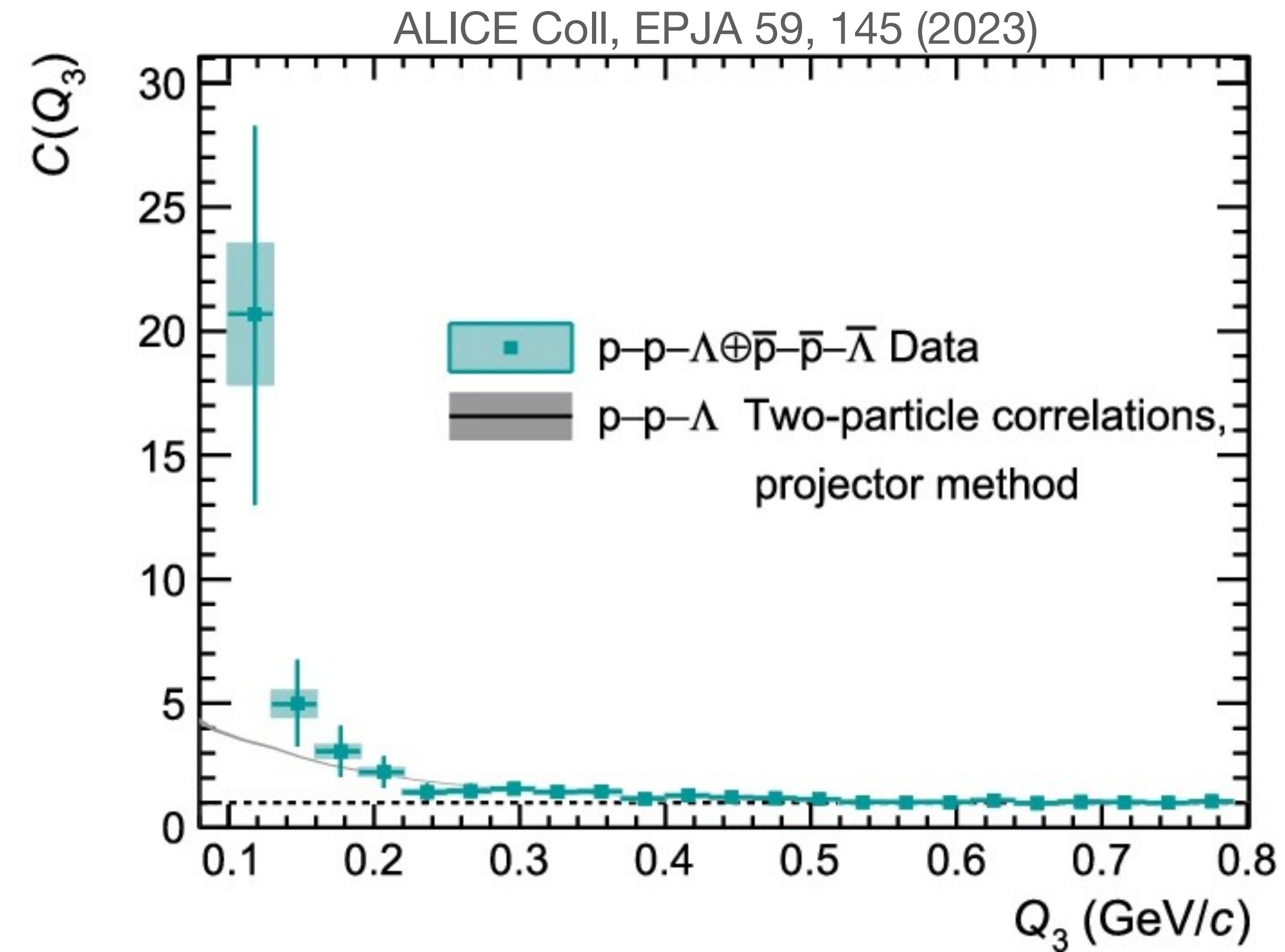
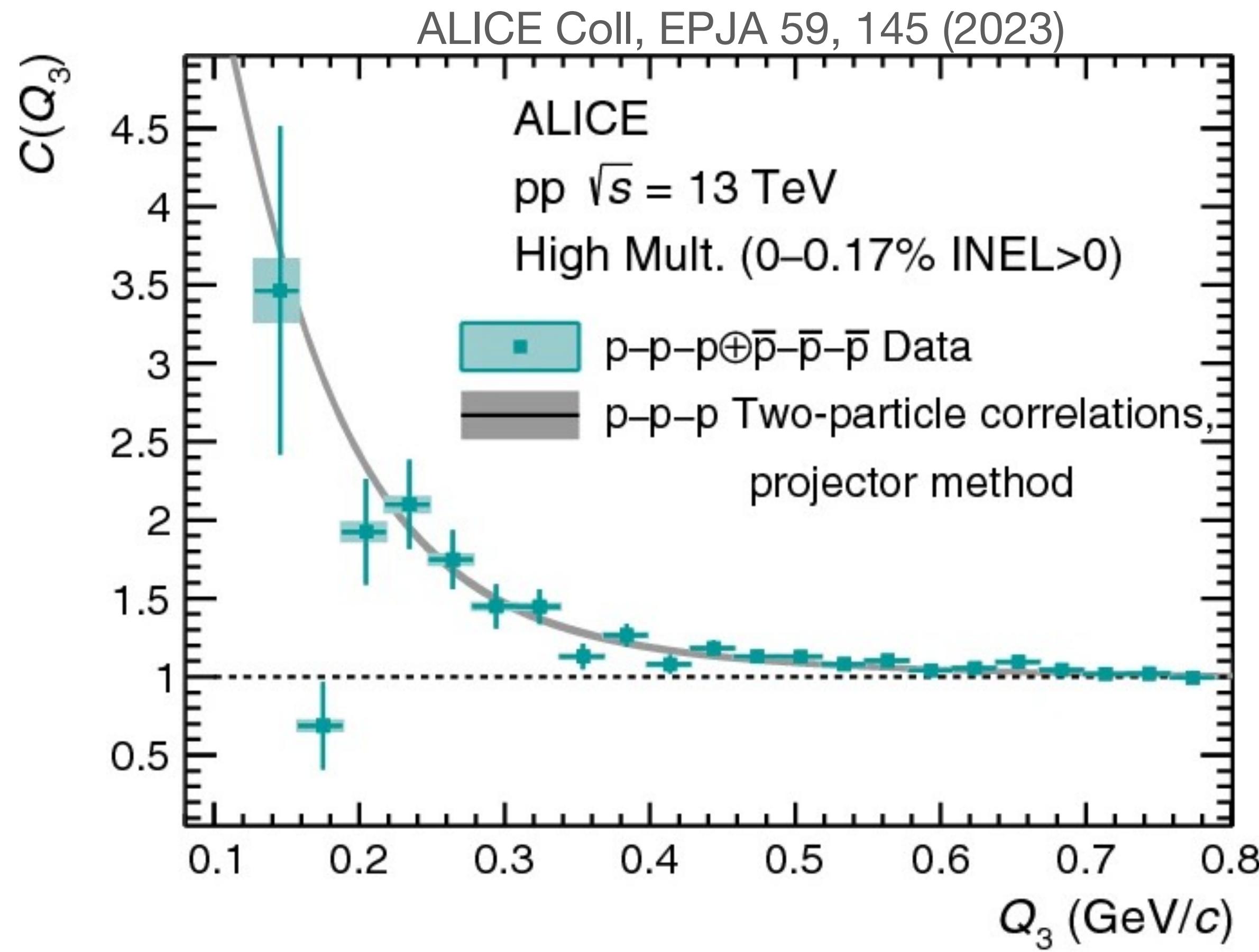
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# Three-body femtoscopy with ALICE

- Hadron-triplets via three-particle correlations: p-p-p and p-p- $\Lambda$

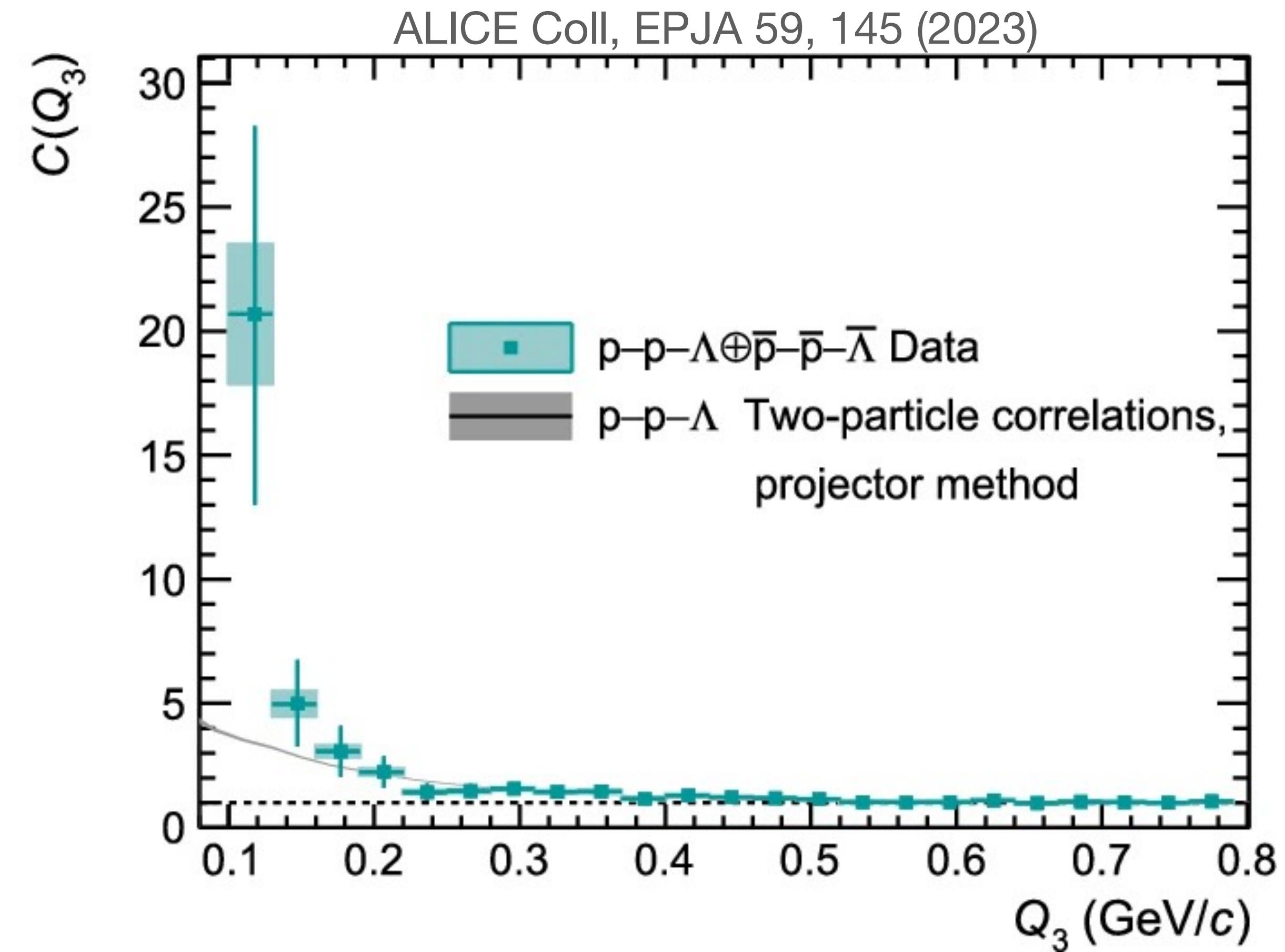
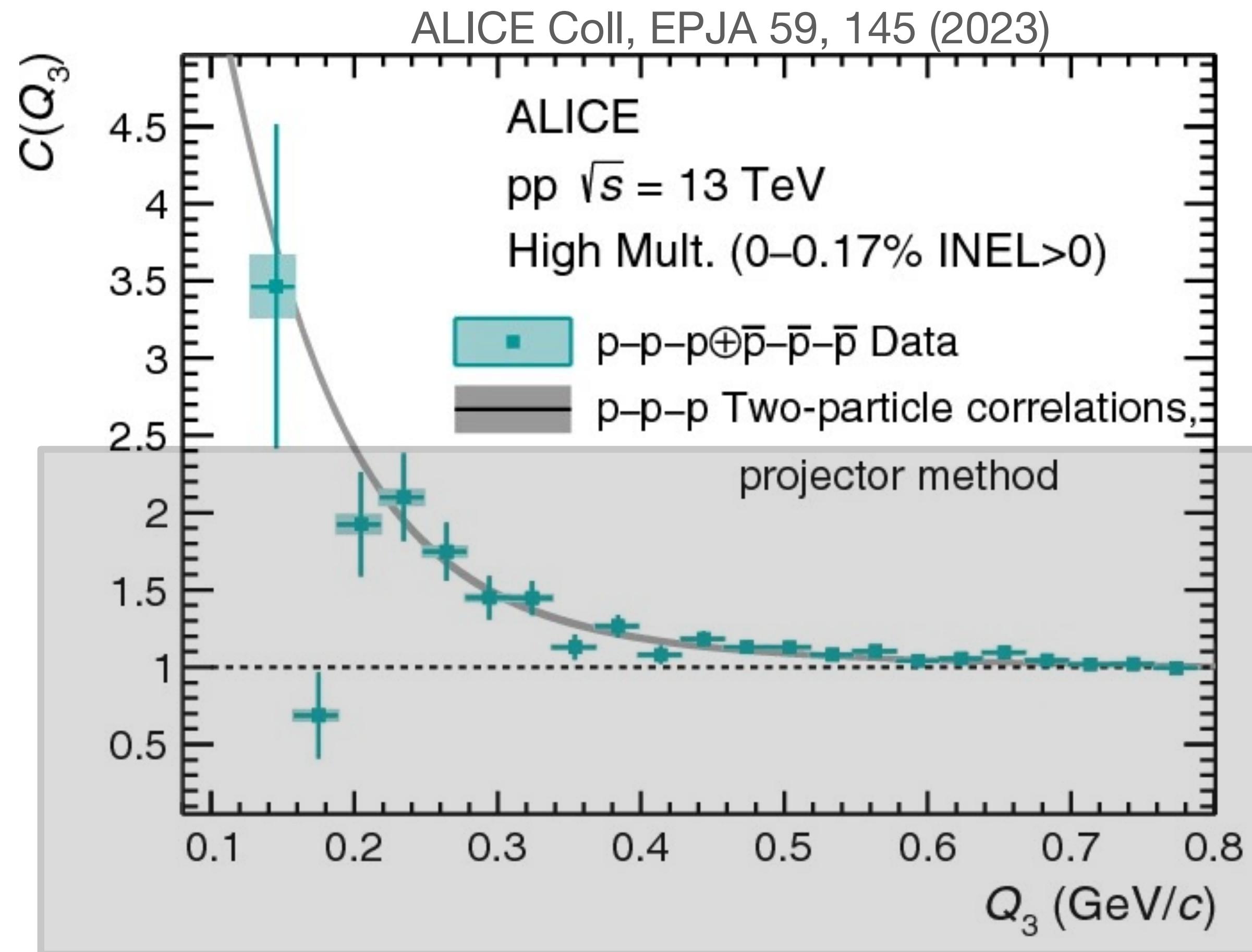


- Direct access to two- and three-body forces in p-p-p and p-p- $\Lambda$  systems

**Projector:** Del Grande et al, Eur. Phys. J. C 82, 244 (2022)

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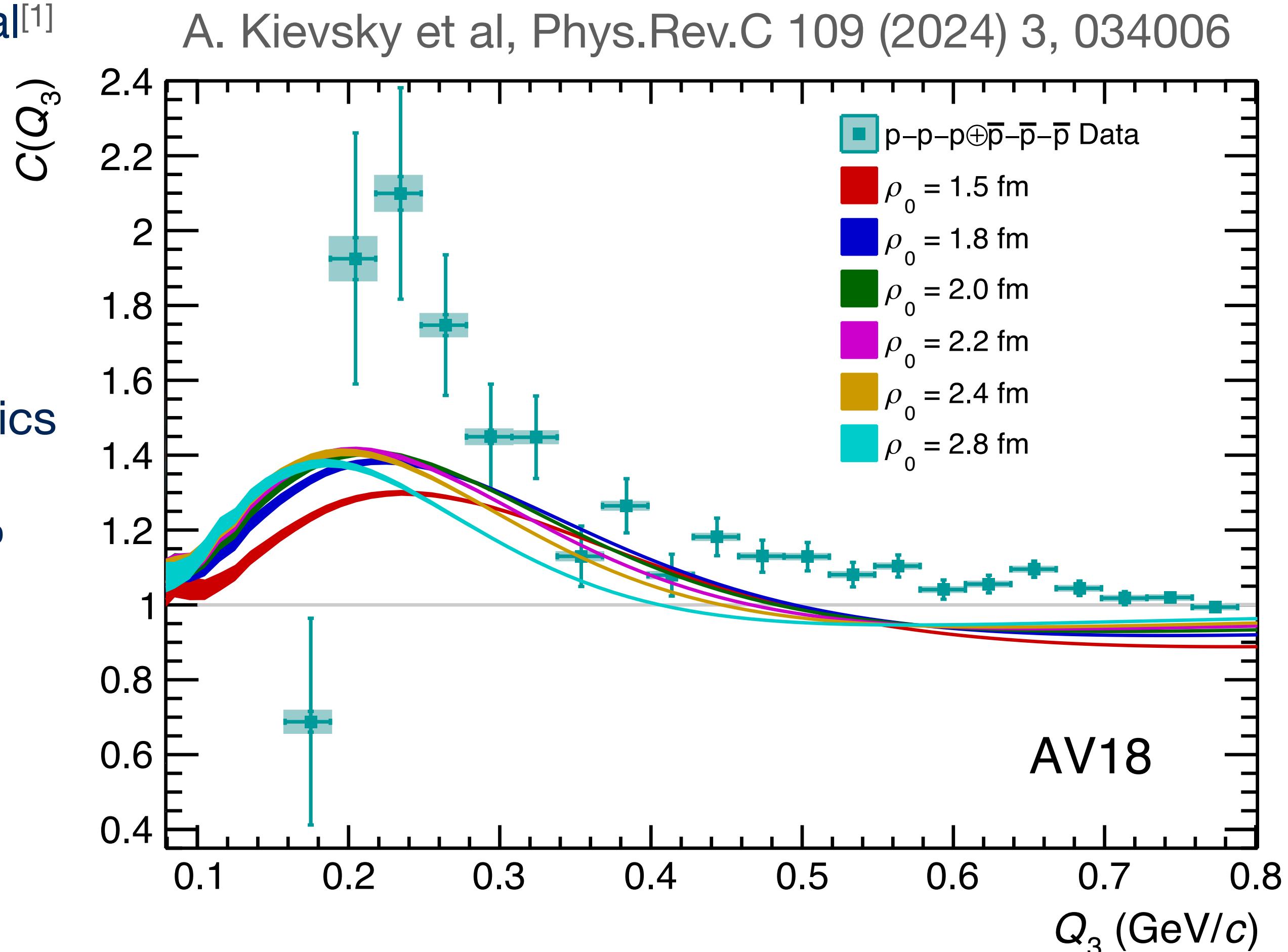
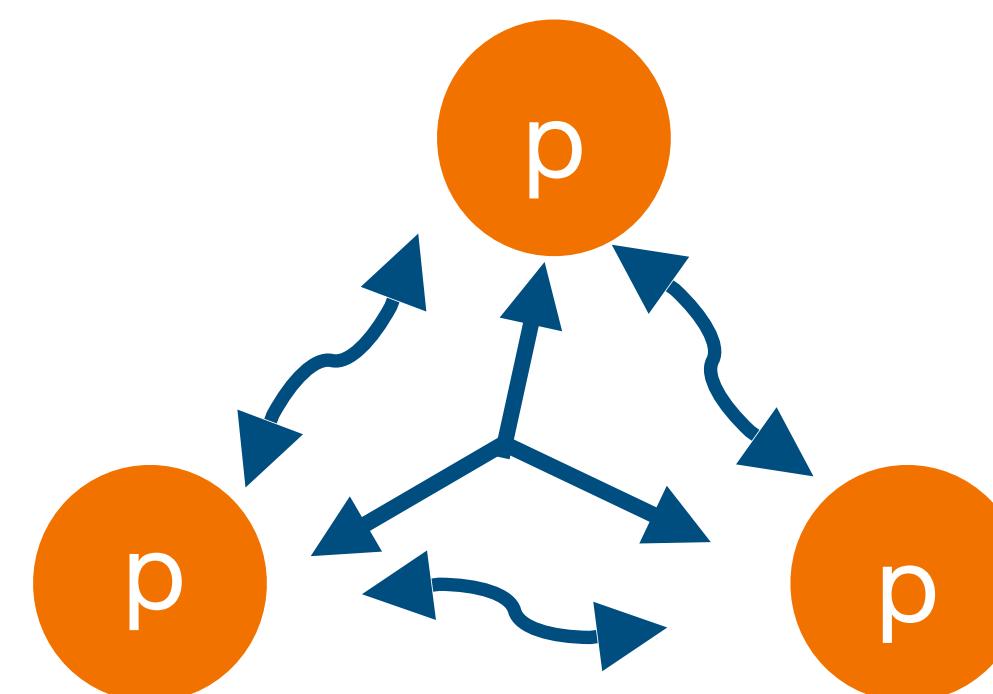
**Projector:** Del Grande et al, Eur. Phys. J. C 82, 244 (2022)

# p-p-p correlation using AV18 potential

- Three-body correlation function AV18 and UIX potential<sup>[1]</sup>

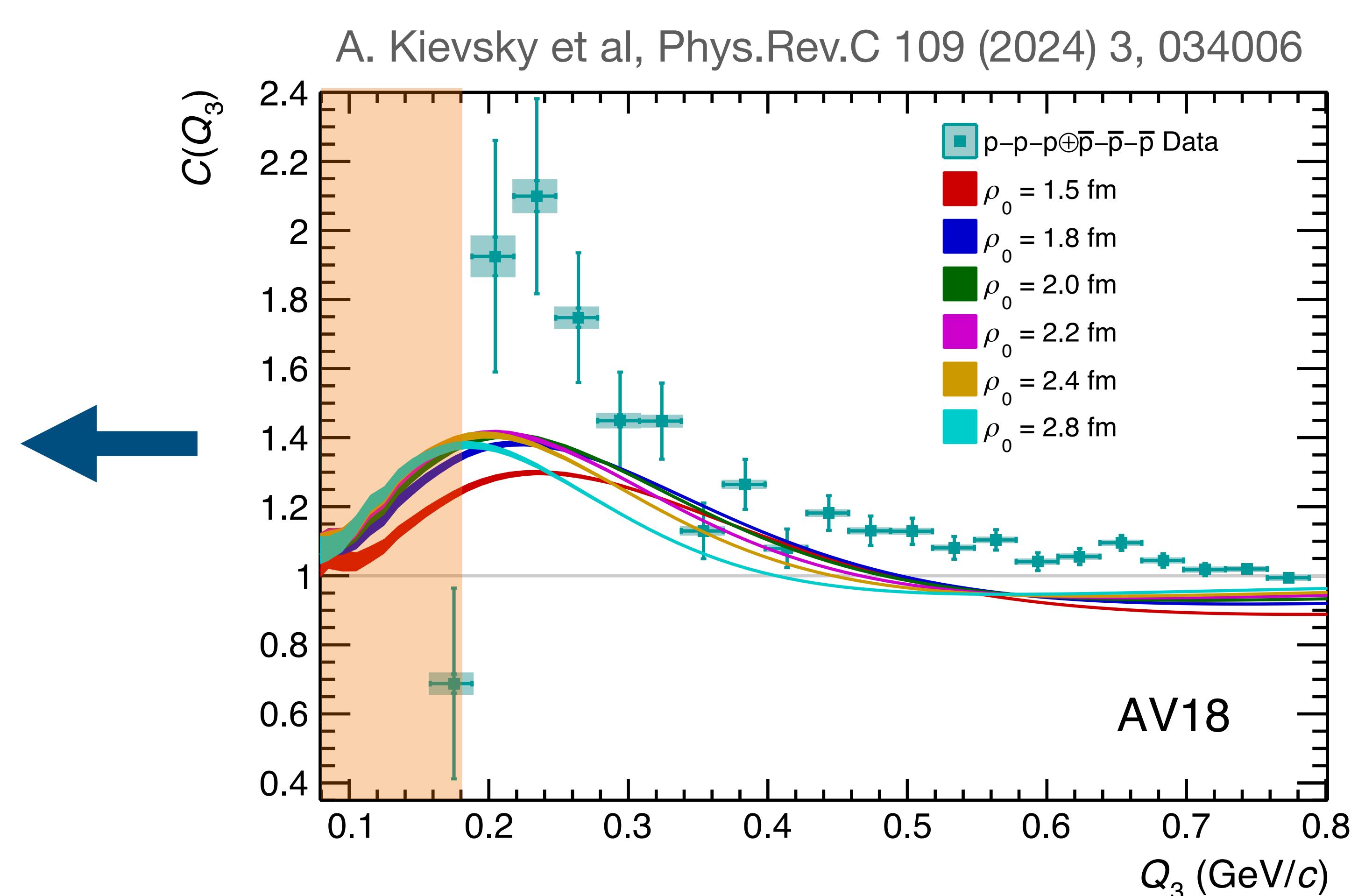
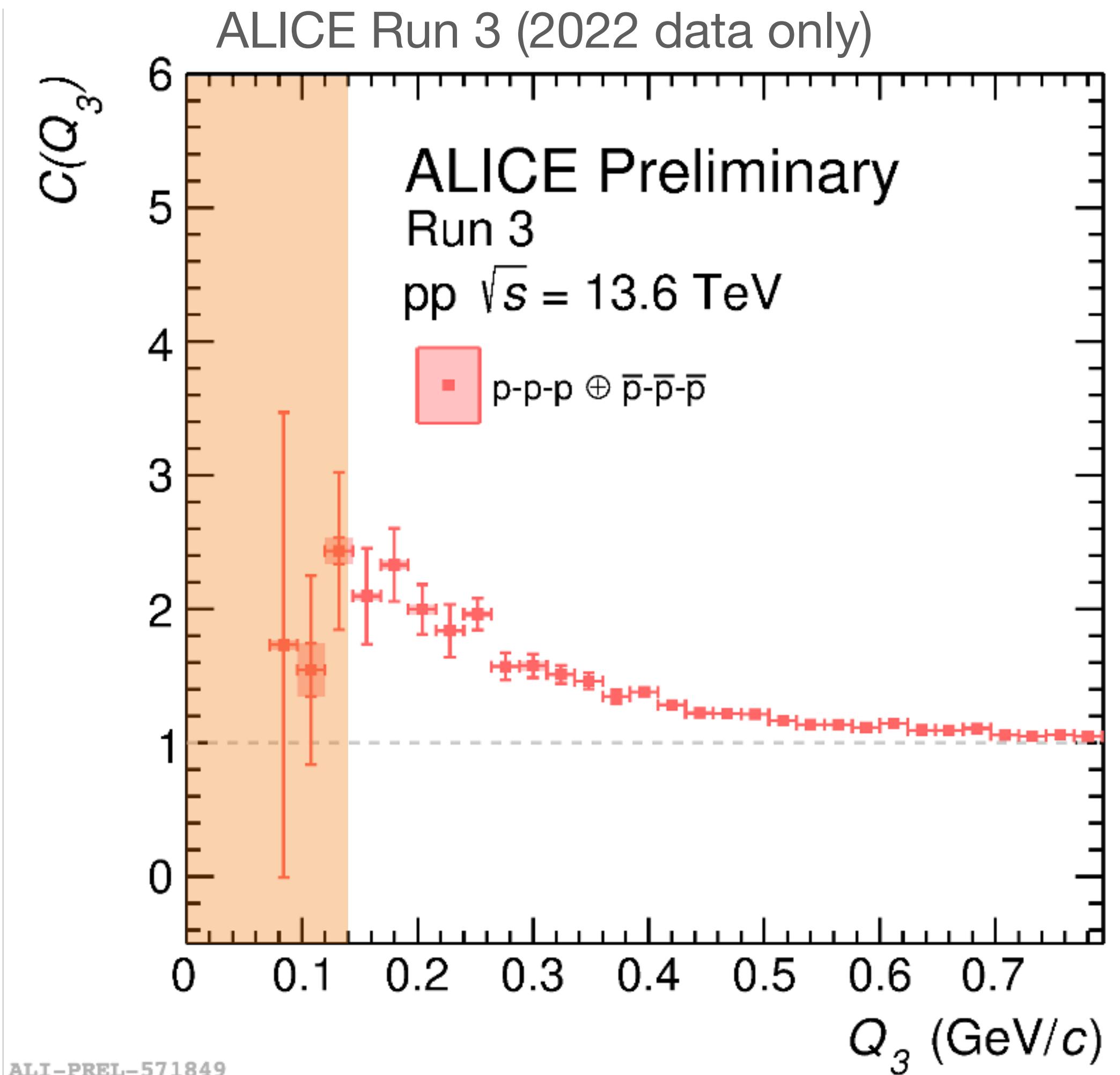
$$C(Q_3) = \int S(\rho) \left| \Psi(Q_3, \rho) \right|^2 \rho^5 d\rho$$

- $\Psi(Q_3, \rho)$  computed using **only pp AV18** strong interaction, Coulomb corrections, and quantum statistics
- Negligible contribution from NNN (via UIX) found < 1%
- Attractive AV18 interaction: results peak
- Pauli-blocking: depletion in  $C(Q_3)$



[1] A. Kievsky et al, Phys. Rev. C 109 (2024) 3, 034006

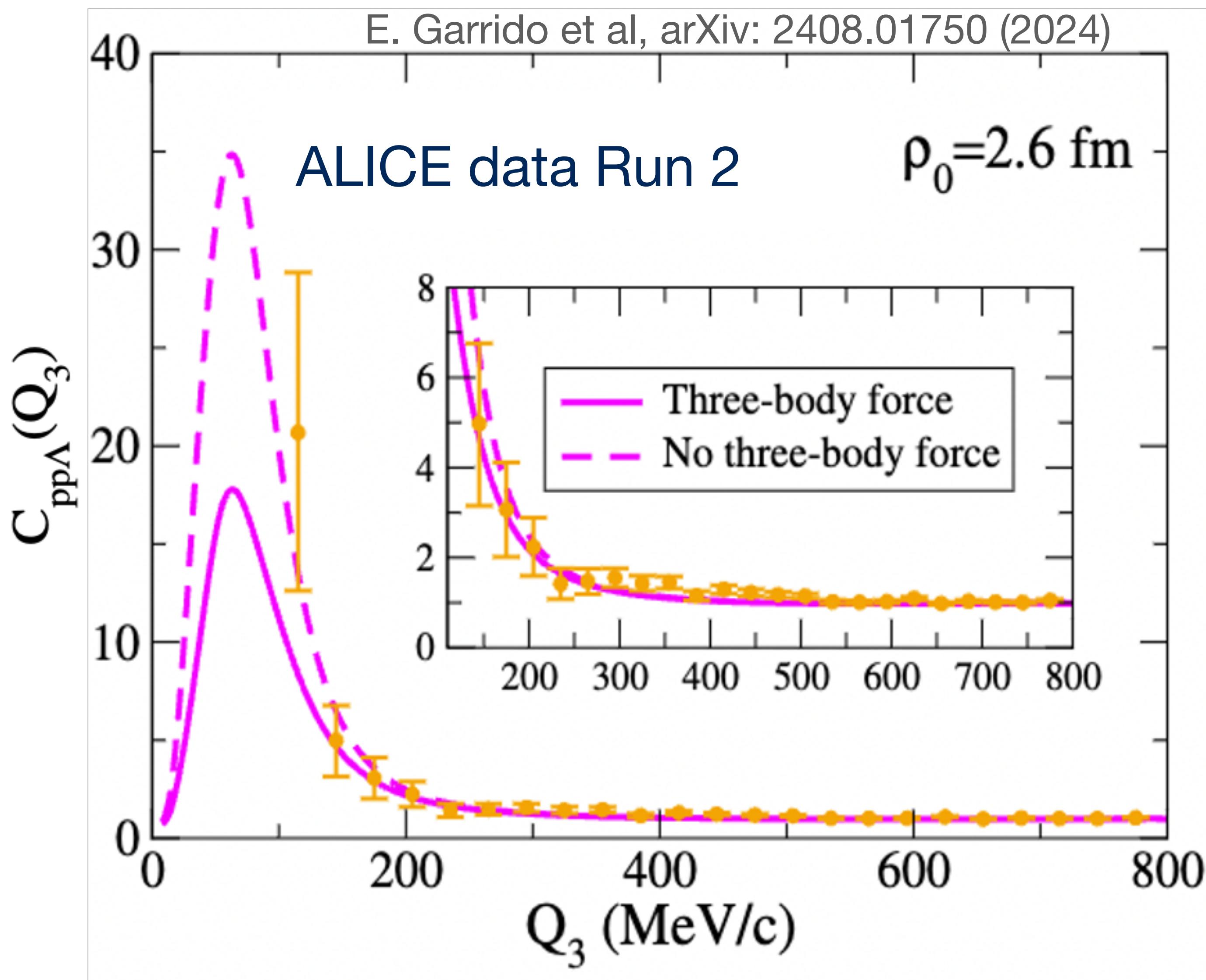
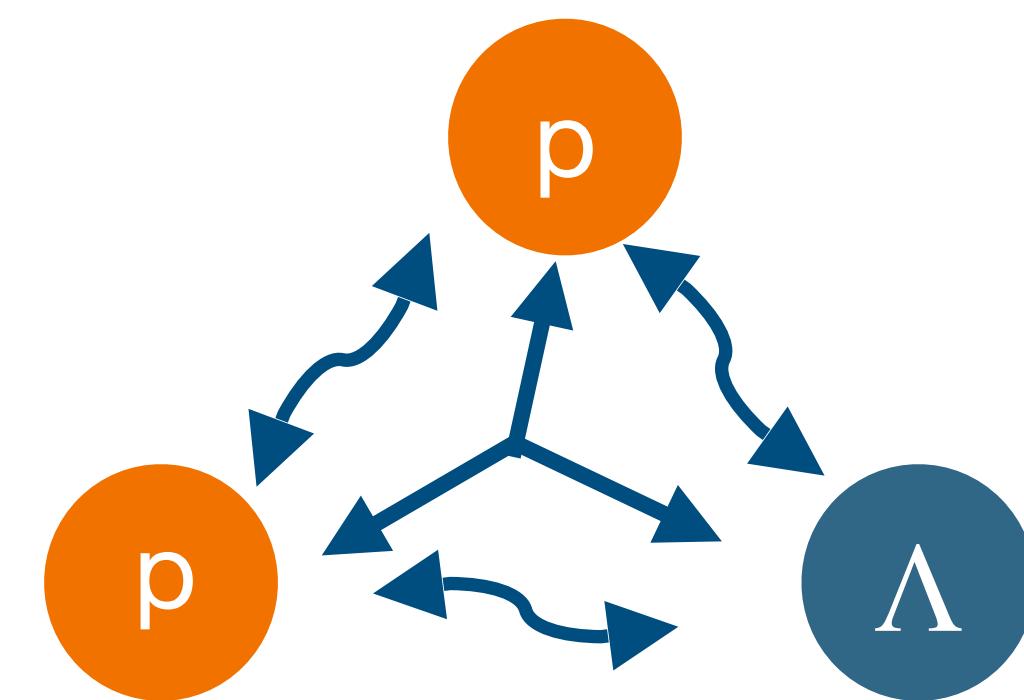
# p-p-p correlation in Run 3



By the end of Run 3, 100 times more triplets w.r.t Run 2 statistics, estimated with dedicated software triggers!

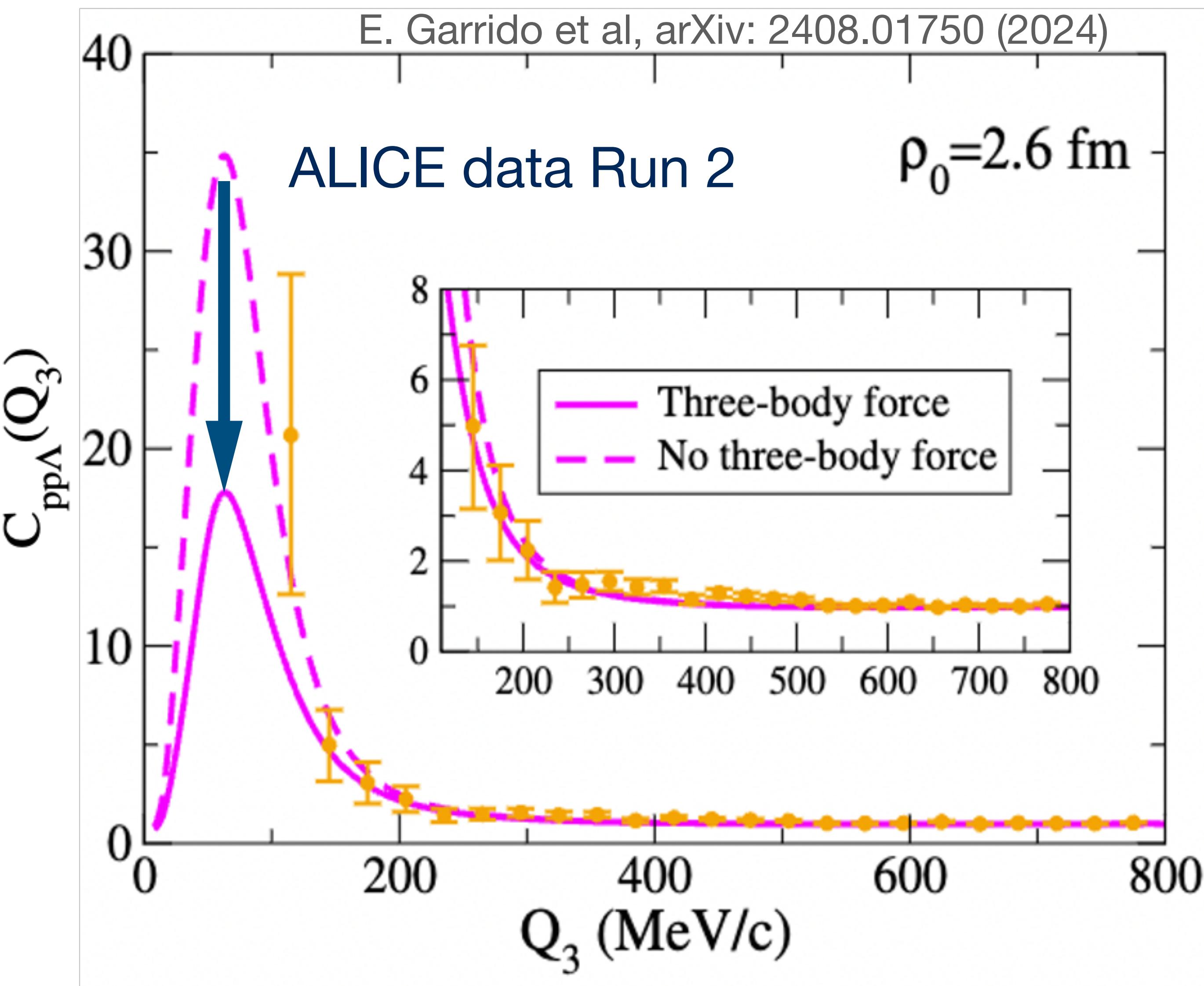
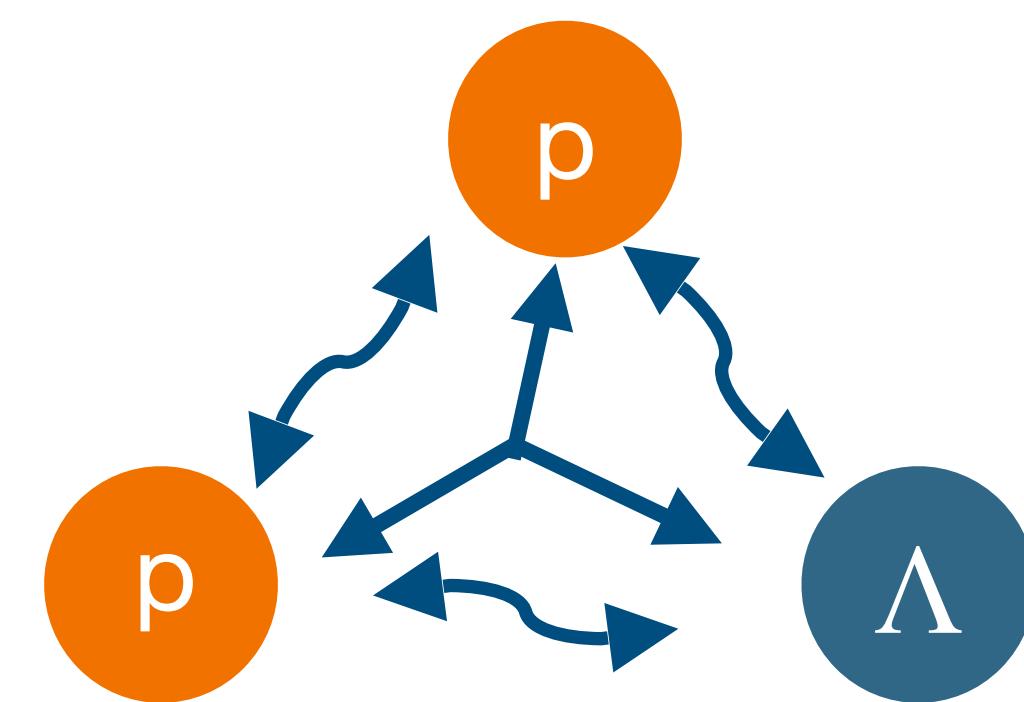
# Theoretical p-p- $\Lambda$ correlation

- Three-particle emission source modeled as three single-particle emitters constrained to data [1]
- Modeling includes experimental corrections (e.g. feed-down)

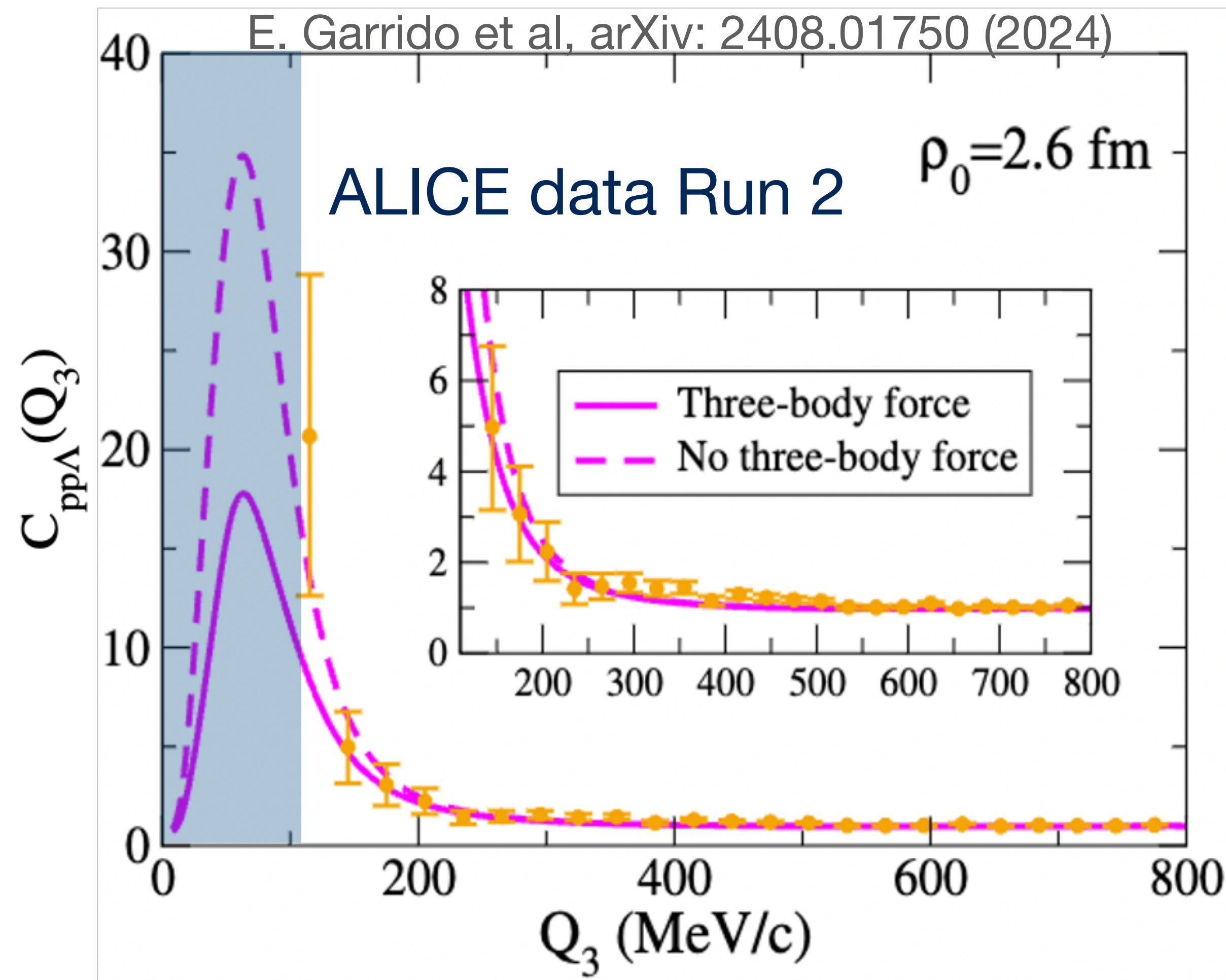
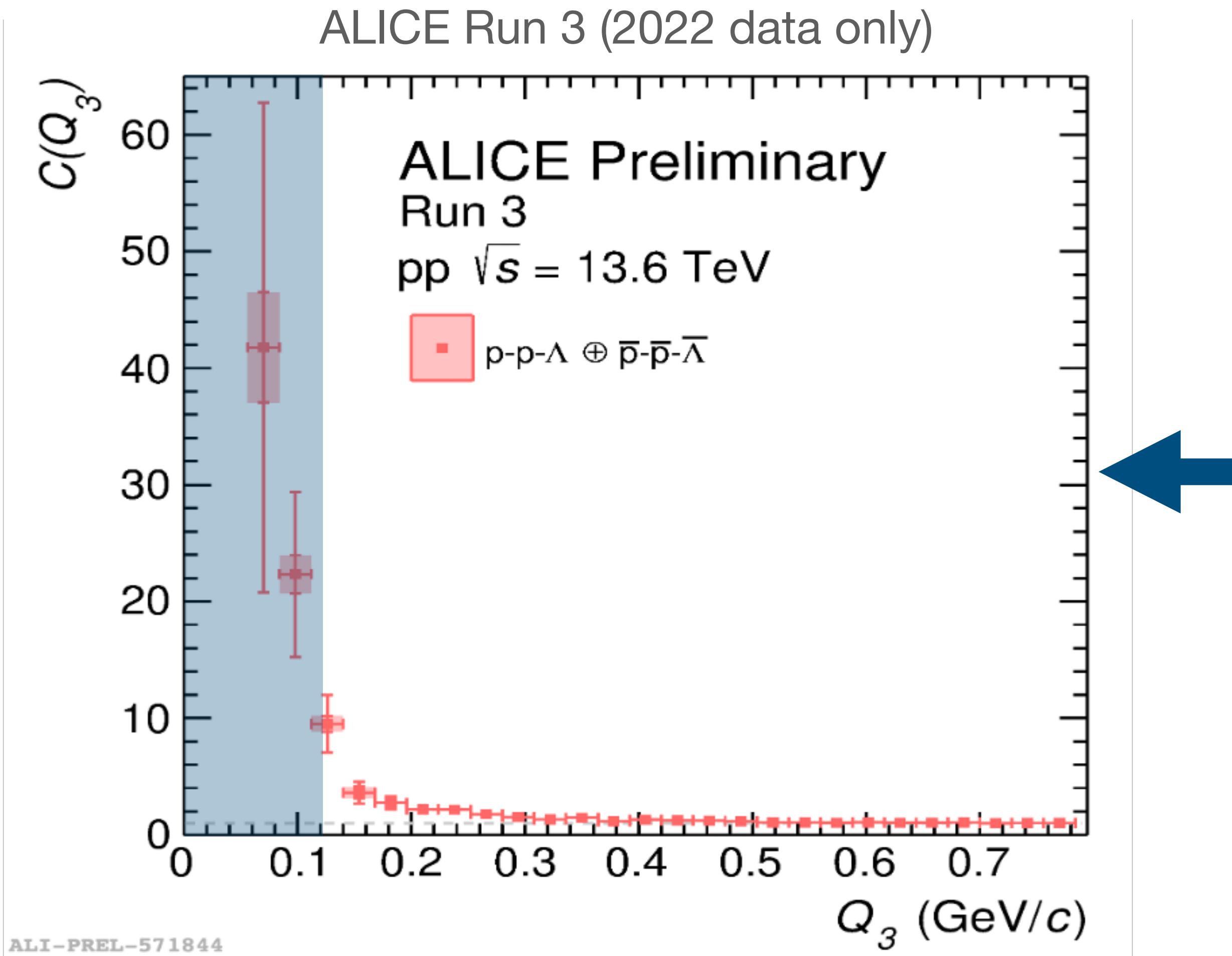


# Theoretical p-p- $\Lambda$ correlation

- Three-particle emission source modeled as three single-particle emitters constrained to data [1]
- Modeling includes experimental corrections (e.g. feed-down)
- The most interesting region  $Q_3 < 100 \text{ MeV}/c$  not yet accessed by data



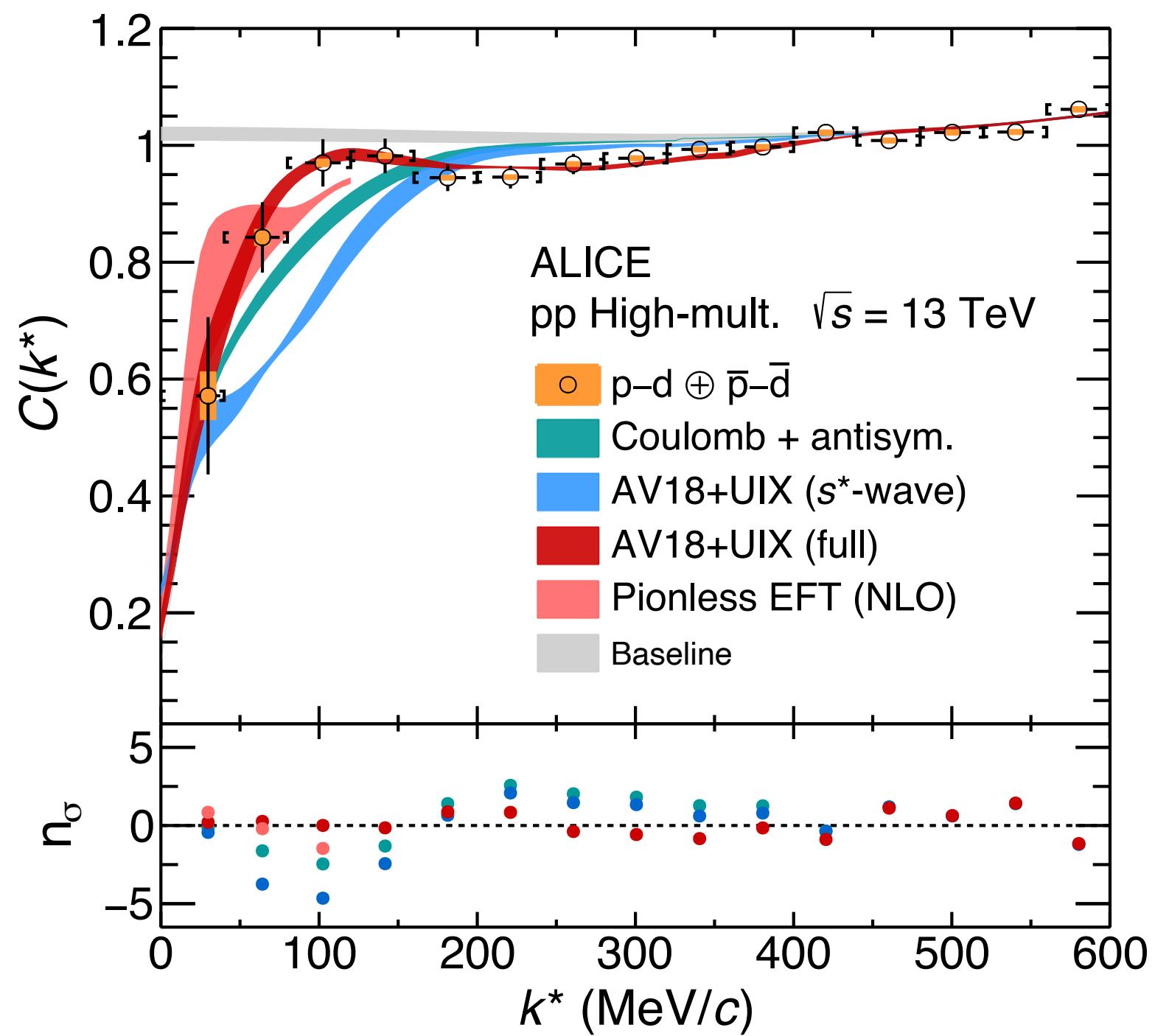
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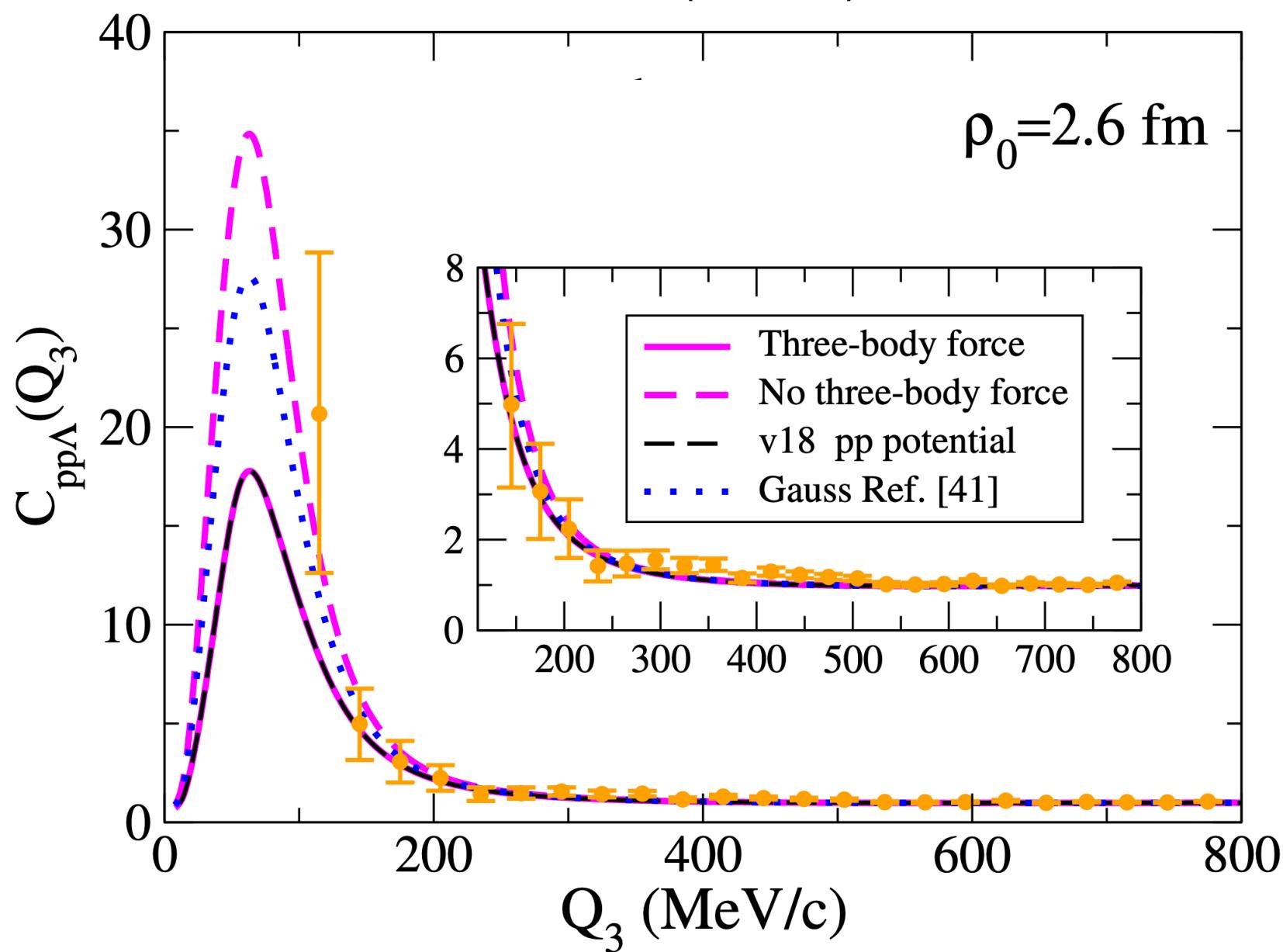
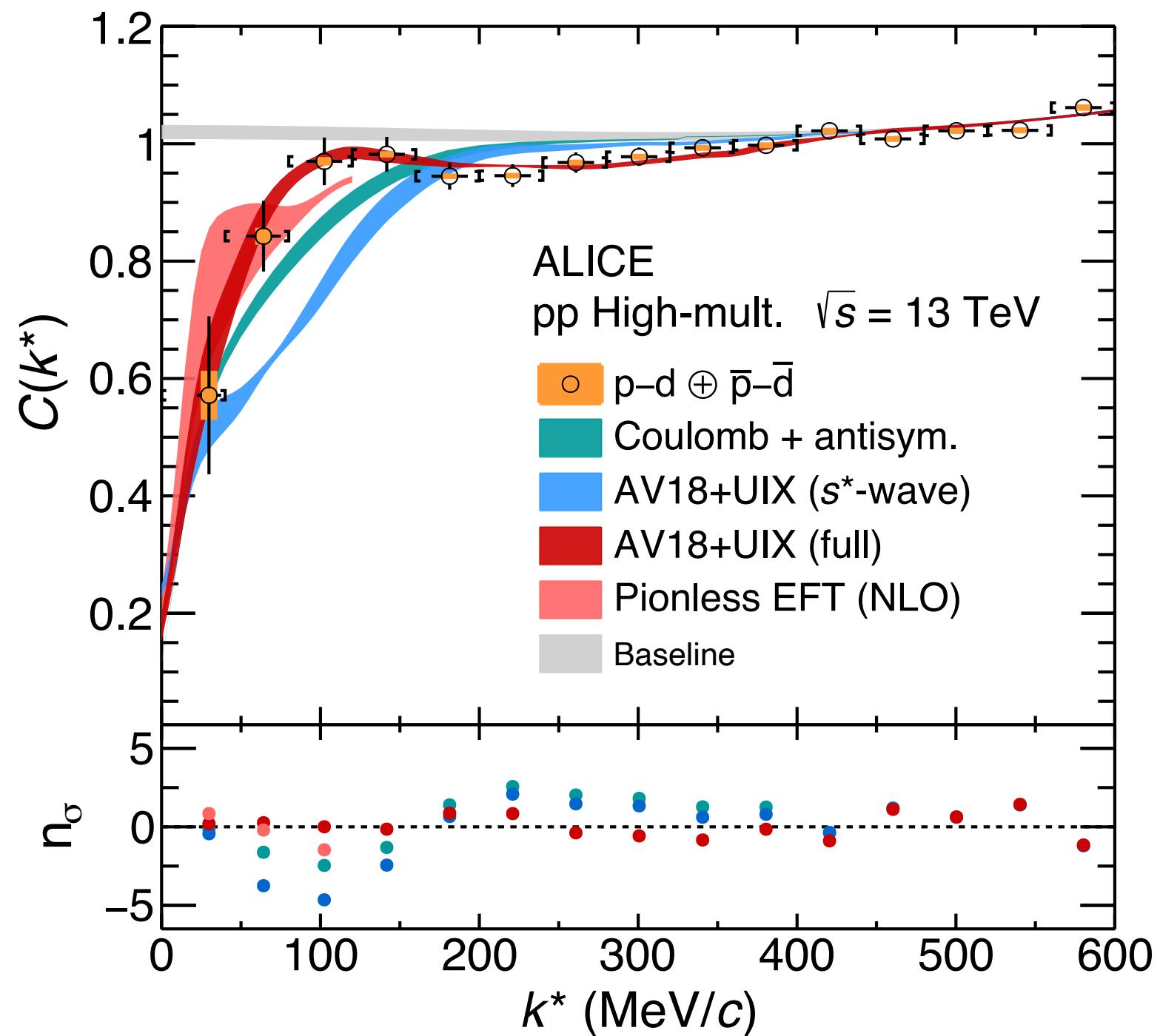
# Conclusions and Outlook

- **K<sup>+</sup>-d**: deuterons follow source size scaling for all hadrons in pp collisions
- **p-d**
  - Access to three-body strong interaction
  - Sensitive to the inclusion of higher partial waves



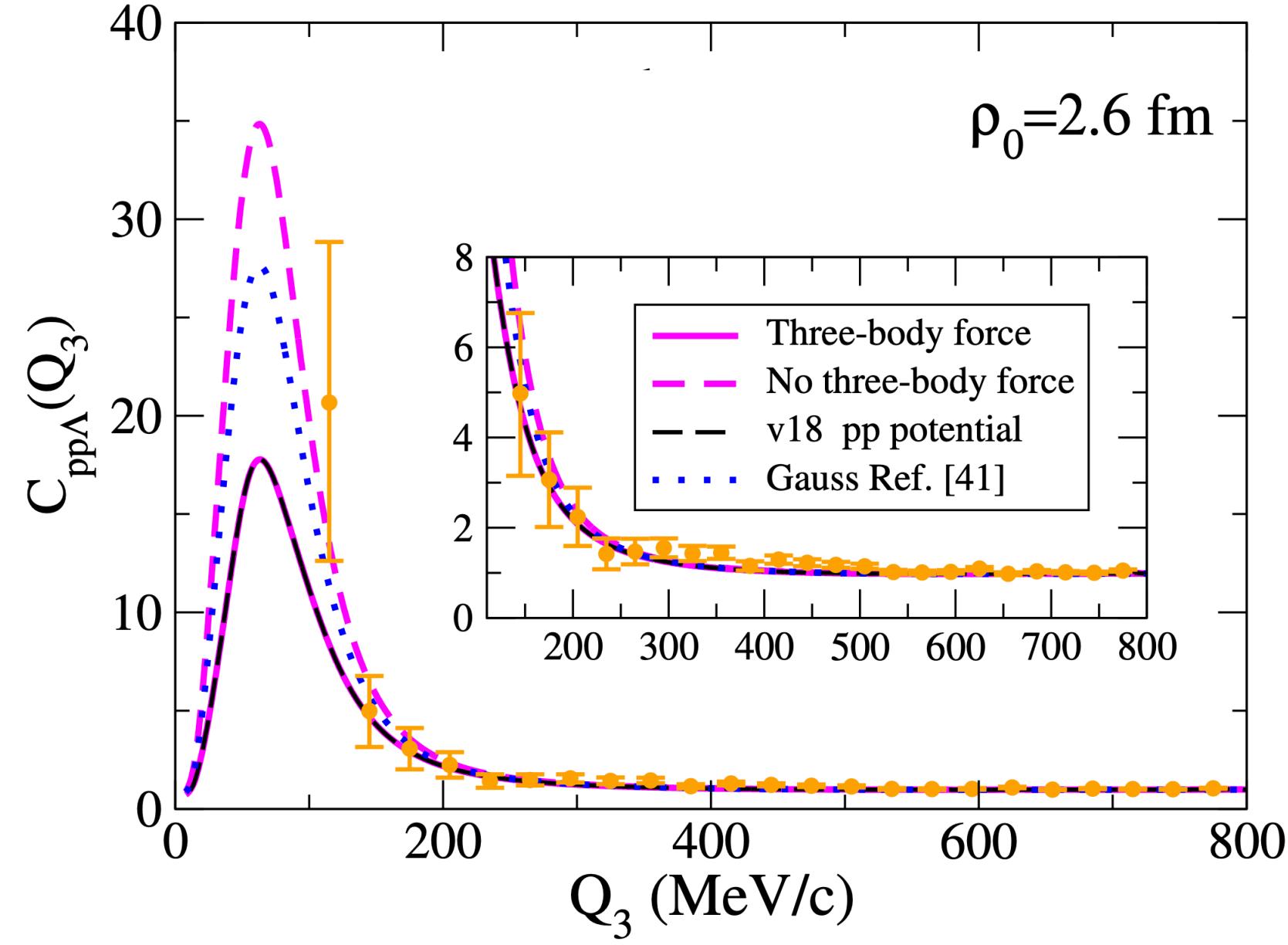
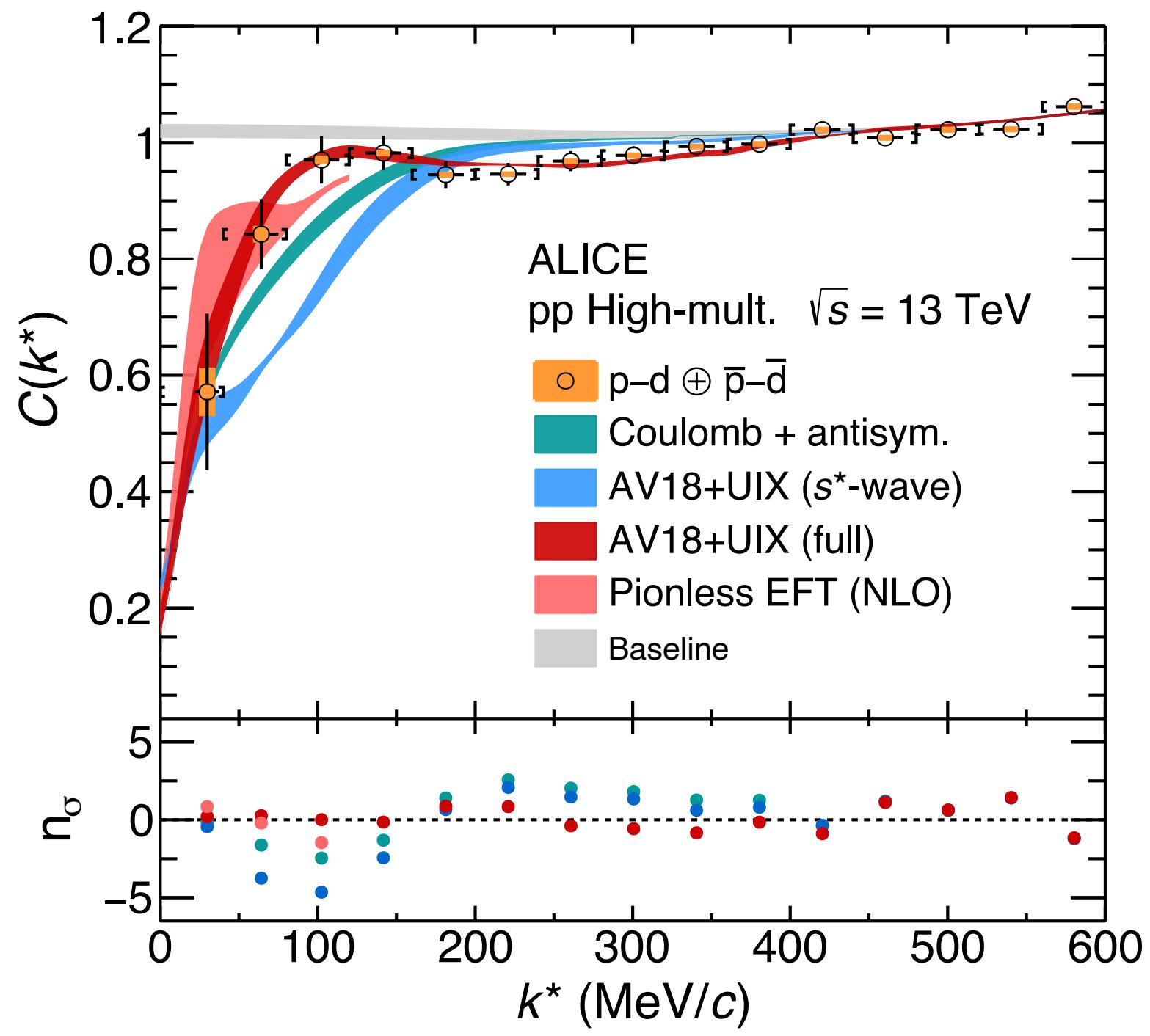
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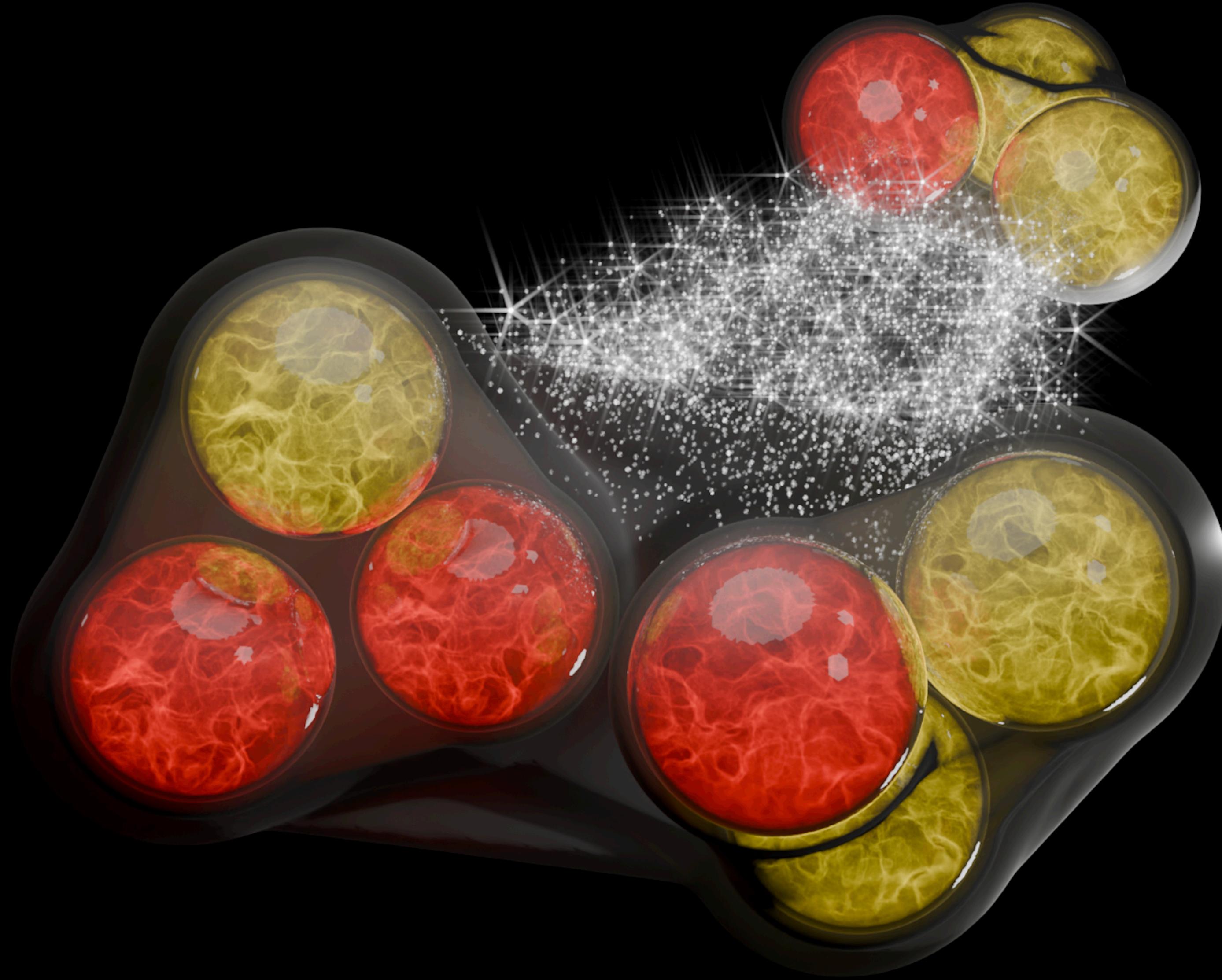
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- **p-p-p:** insignificant three-body force due to Pauli-blocking effects
- **p-p-Λ:** 3-body force with strangeness up to 40%
- **Large statistics of LHC Run 3 and Run 4**
  - p-p correlation in LHC Run 3: source constrained for all interaction studies
  - Ongoing studies for p-d, Λ-d, p-p-p, and p-p-Λ from LHC Run 3





**Thank you for your attention!**

# **Additional slides**

# Asymptotic form of strong interaction in p-d system

- Coulomb only: does not describe the data
- Born approximated wavefunction AV18(2N) [1-2] UIX (NNN) potentials [3]
- Asymptotic form of strong interaction is insufficient to capture the dynamics of nucleons  $\sim 1$  fm

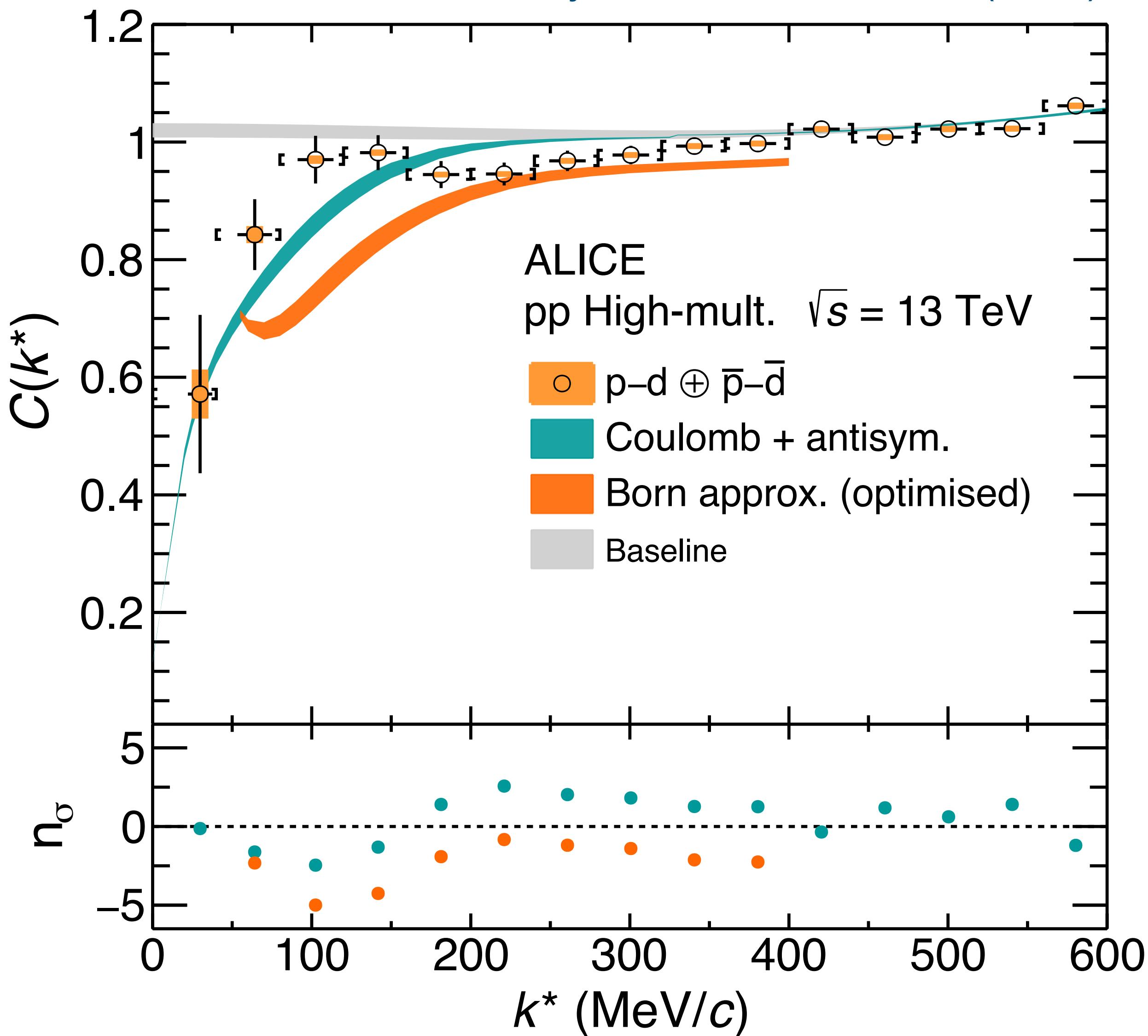
$$\Psi_{LSJJ_z} = \sum_{n,\alpha} \frac{u_{n,\alpha}(\rho)}{\rho^{5/2}} \gamma_{n,\alpha}(\Omega) + \frac{1}{\sqrt{3}} \sum_{\ell}^{\text{even perm.}} \left\{ Y_L(\hat{\mathbf{y}}_\ell) [\varphi^d(i,j)\chi(\ell)]_S \right\}_{JJ_z} \frac{F_L(\eta, ky_\ell)}{ky_\ell} + \sum_{L'S'} T_{LS,L'S'}^J \frac{1}{\sqrt{3}} \sum_{\ell}^{\text{even perm.}} \left\{ Y_{L'}(\hat{\mathbf{y}}_\ell) [\varphi^d(i,j)\chi(\ell)]_{S'} \right\}_{JJ_z} \times \frac{\bar{G}_{L'}(\eta, ky_\ell) + iF_{L'}(\eta, ky_\ell)}{ky_\ell}.$$

[1] M. Viviani, B. Singh et al. Phys. Rev. C108, 064002 (2023)

[2] R. B. Wiringa et al. Phys. Rev. C 51, 38 (1995)

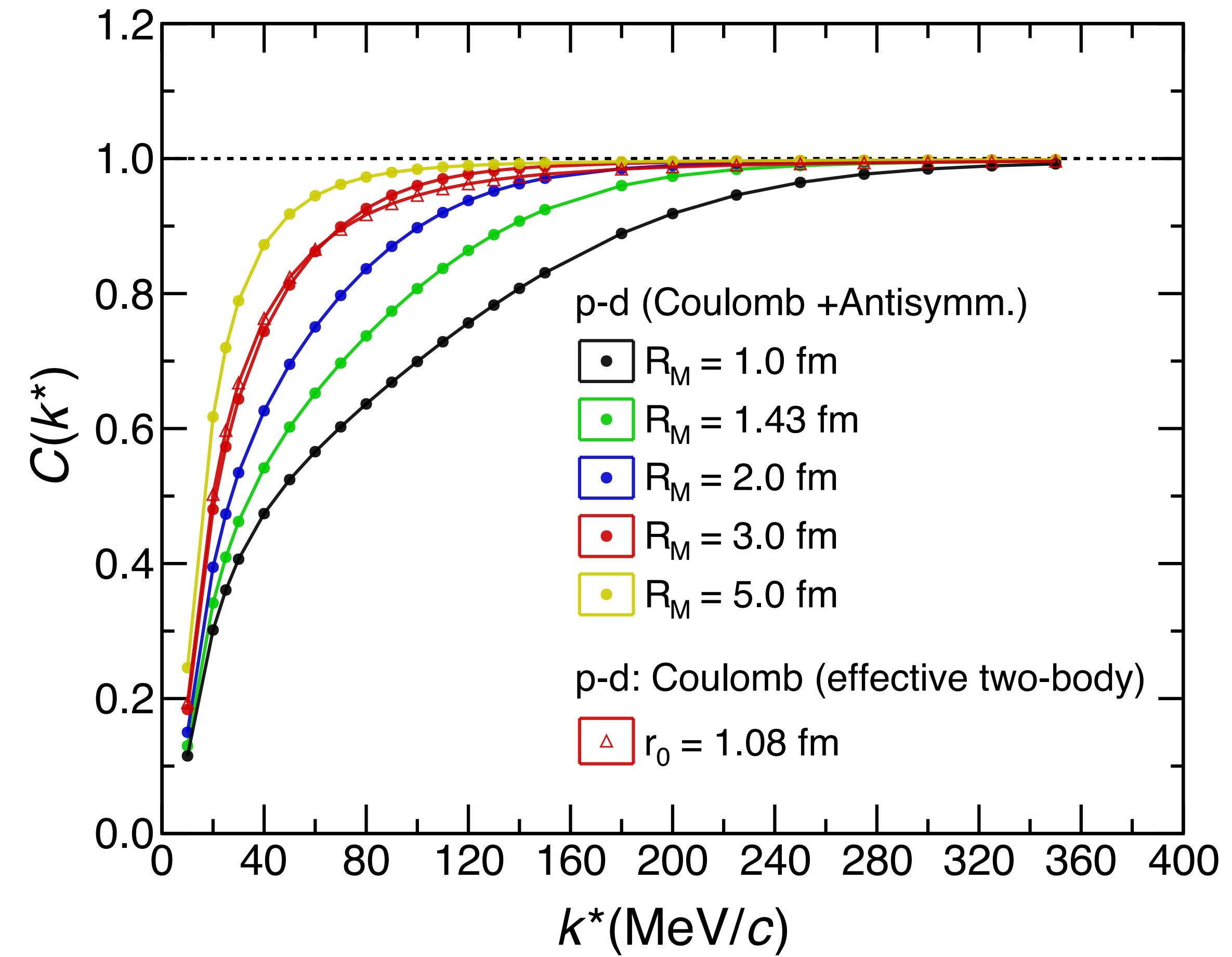
[3] B. S. Pudliner et al. Phys. Rev. Lett. 74, 4396 (1995)

ALICE, Phys. Rev. X14, 031051 (2024)



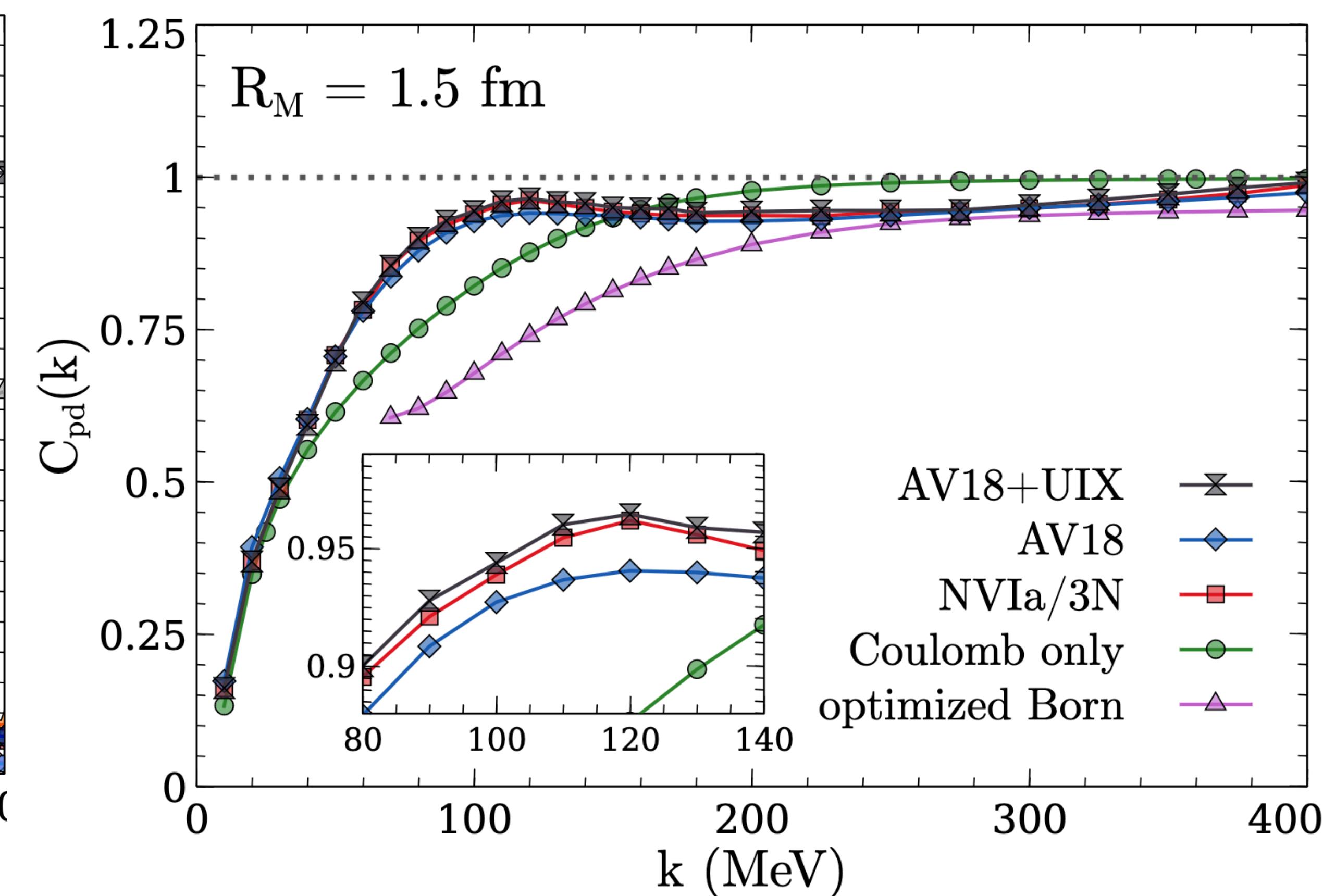
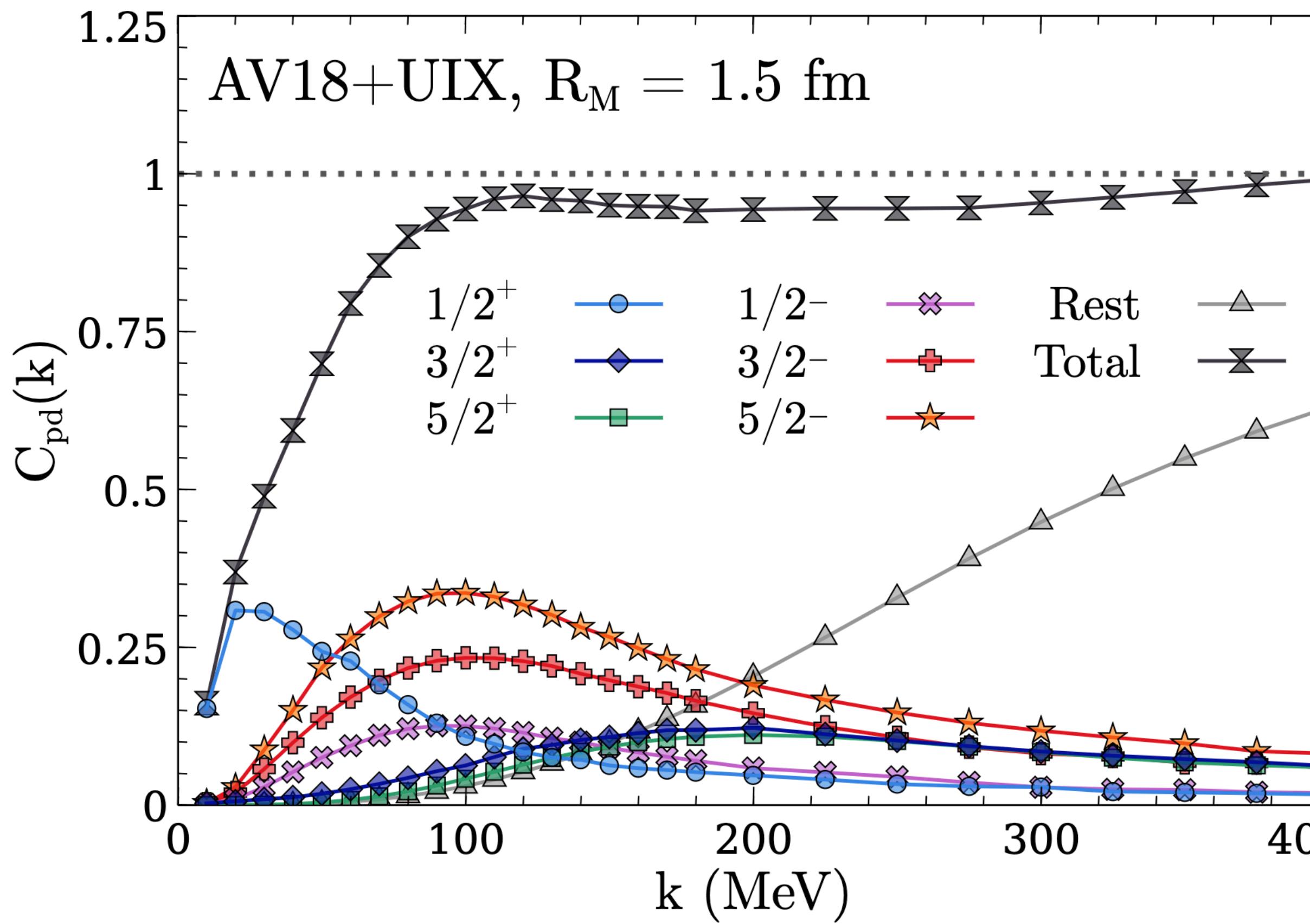
# Coulomb interaction in p-d system

- Complete p-pn dynamics, but the strong interaction is absent at very short-range!
  - $r_{\text{NN,eff}} = 1.43 \pm 0.16 \text{ fm}$  (nucleon-nucleon distance)
- In the case of the two-body picture Coulomb-only interaction differs from the one using the p-(pn) dynamics
- Two-body source  $1.08 \pm 0.06 \text{ fm}$  (proton-deuteron distance)
  - More repulsion due to the Pauli-blocking



# AV18+UIX vs NVIa3 3N Chiral potentials

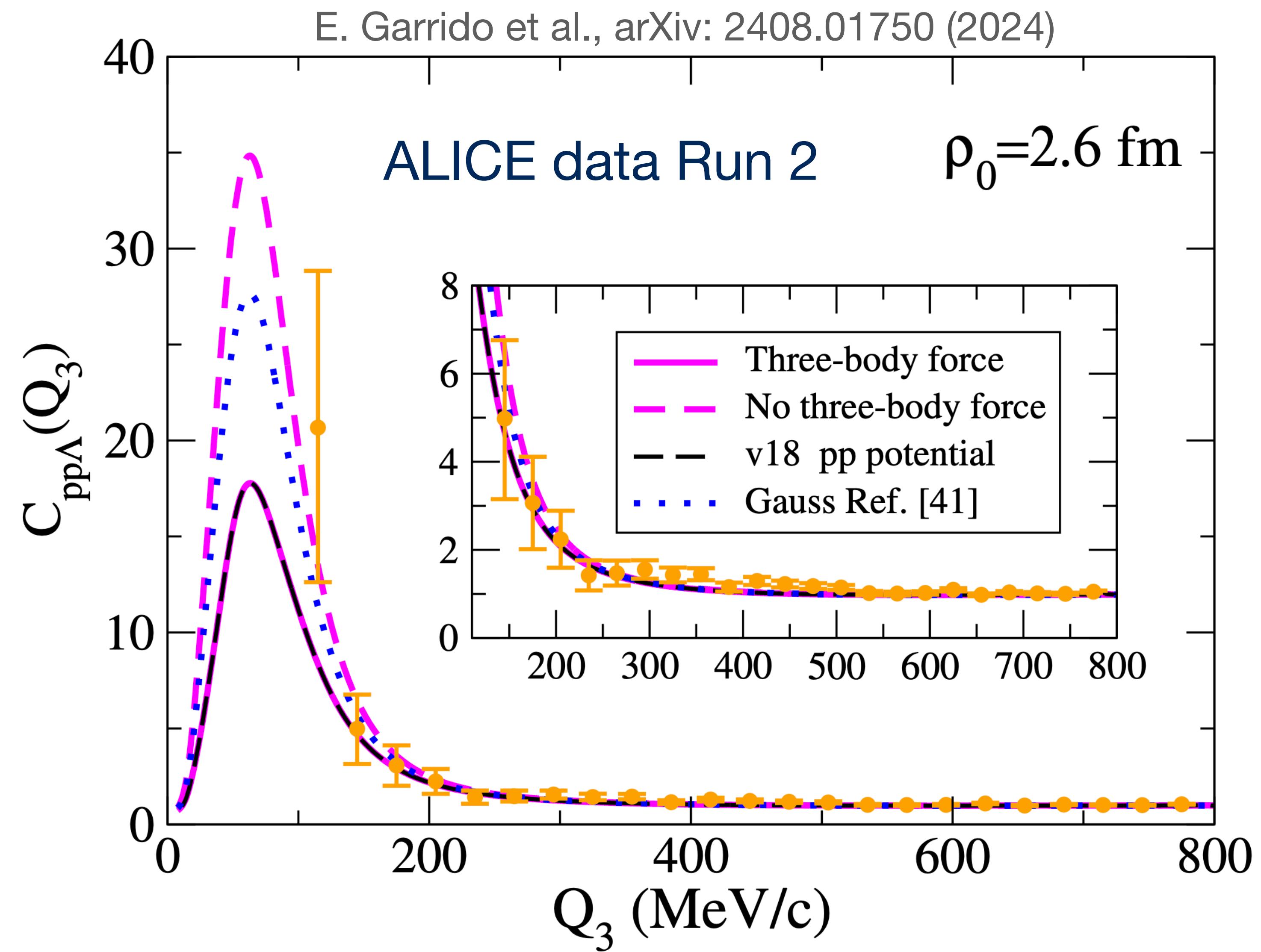
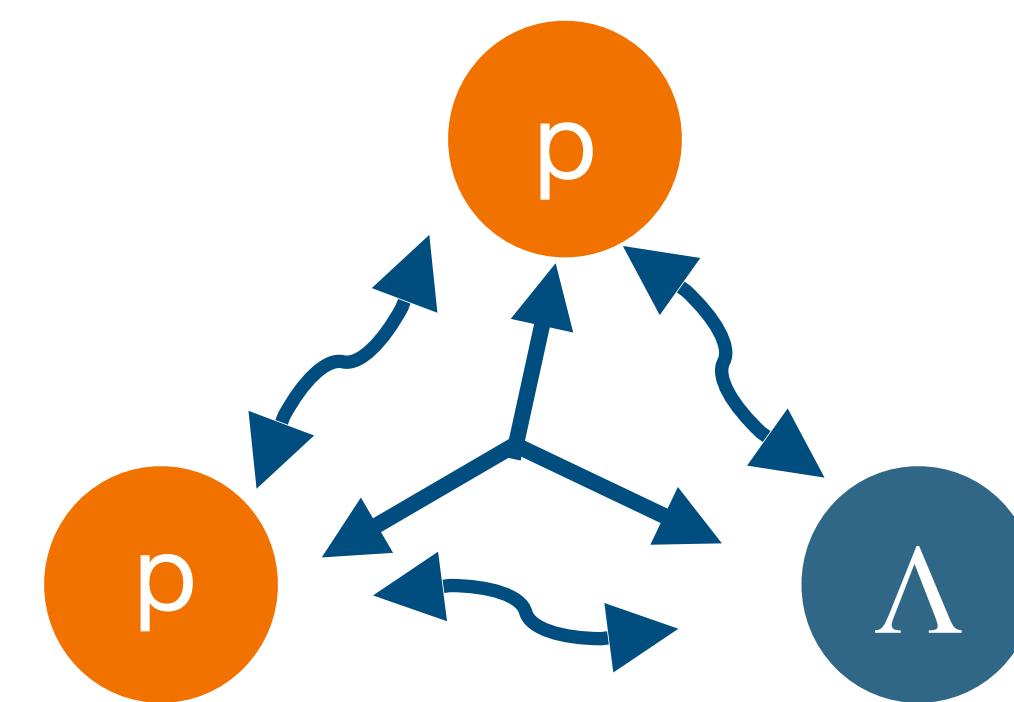
- Precise calculation using AV18+UIX as well NVIa3/3N chiral potentials



M. Viviani, B. Singh et al. Phys. Rev. C 108, 064002 (2023)

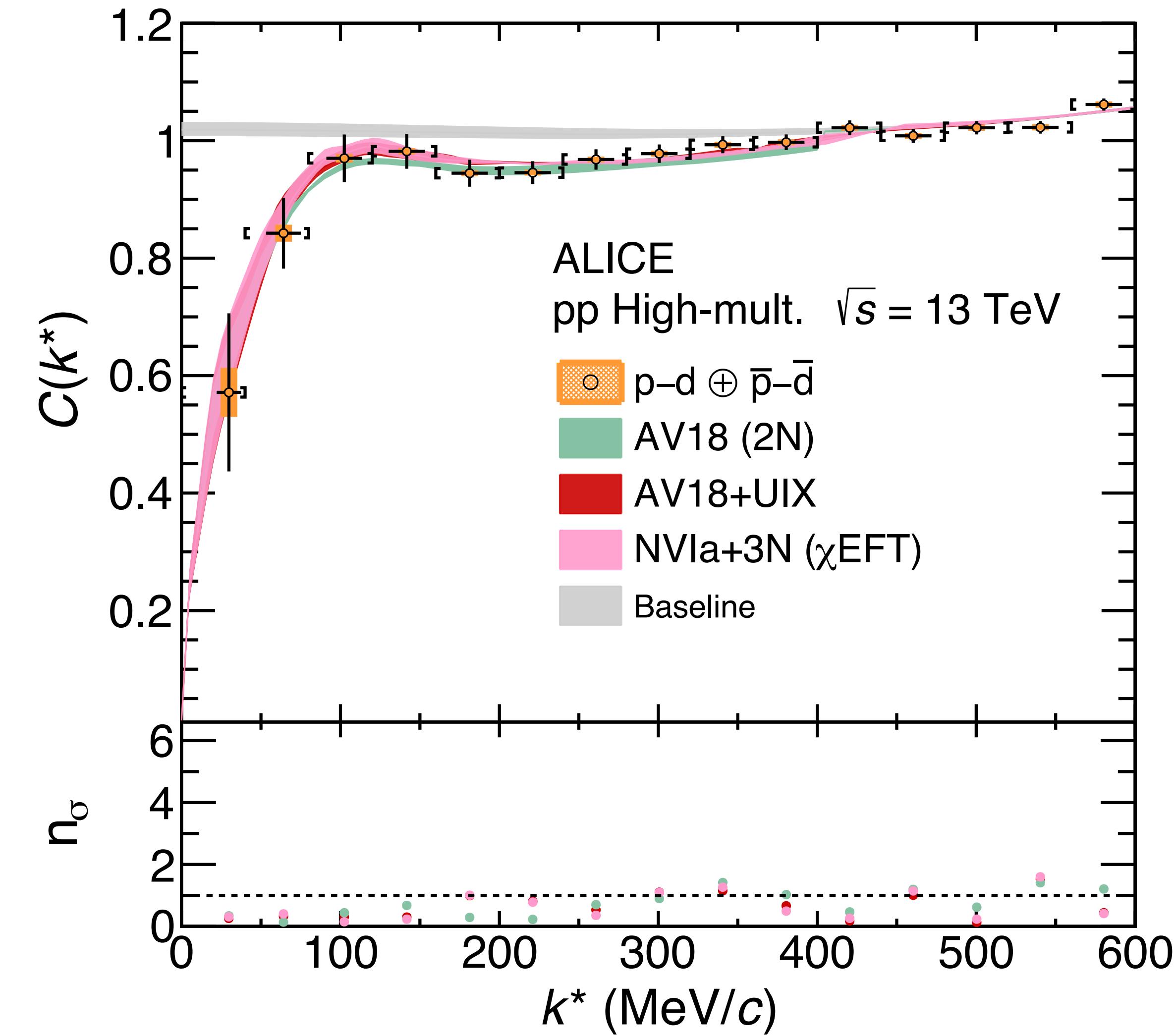
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# AV18+UIX vs NVla3 3N Chiral potentials

- Comparision with Chiral potentials (**Full three-body dynamics**)<sup>[1]</sup>
- Argonne v18+Urbana IX interaction<sup>[2,3]</sup>
- **All partial waves upto d-waves:** describes data within  $n_\sigma \sim 1$  for  $k^*$  up to 400 MeV/c
- Calculations using chiral potential from NVla+3N
  - Very good agreement with AV18+UIX
- AV18 alone: just two-body NN interaction
- Current data cannot resolve the effect of three-body force



# The p $\Lambda$ interaction in the femtoscopy

- **Improvement:** combined analysis of femtoscopic and scattering data

