

François Morellet
Random Distribution of 40,000 Squares using the Odd and Even Numbers of a Telephone Directory 1960



In-Silico generation of random bit streams



the value of unpredictability

Massimo Caccia

Università dell'Insubria & Random Power s.r.l.

massimo.caccia@randompower.eu



AIDAInnova Training Course on Quantum tech
CERN, January 22nd 2025



FALLING WALLS VENTURE

▶ **w h a t w e d o :**

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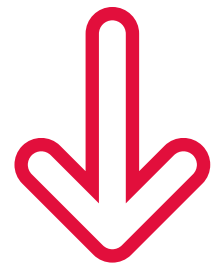


FALLING WALLS VENTURE

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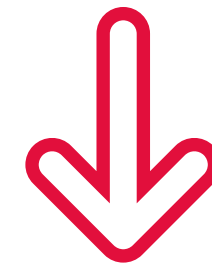
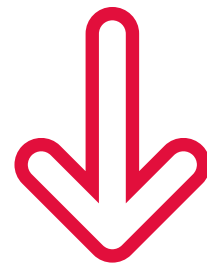
▶ w h a t w e d o :



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FALLING WALLS VENTURE

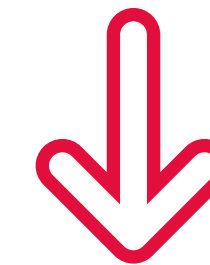
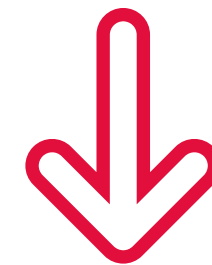
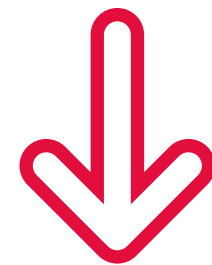
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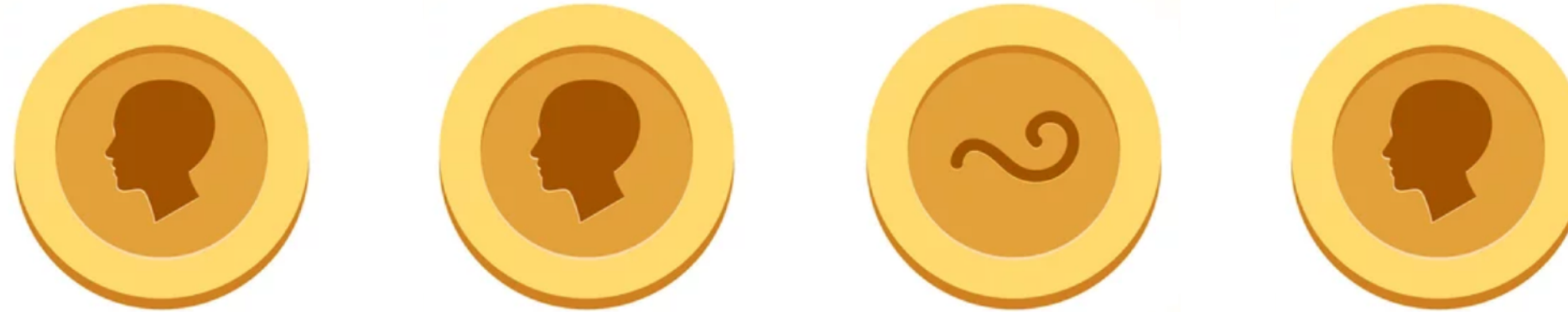
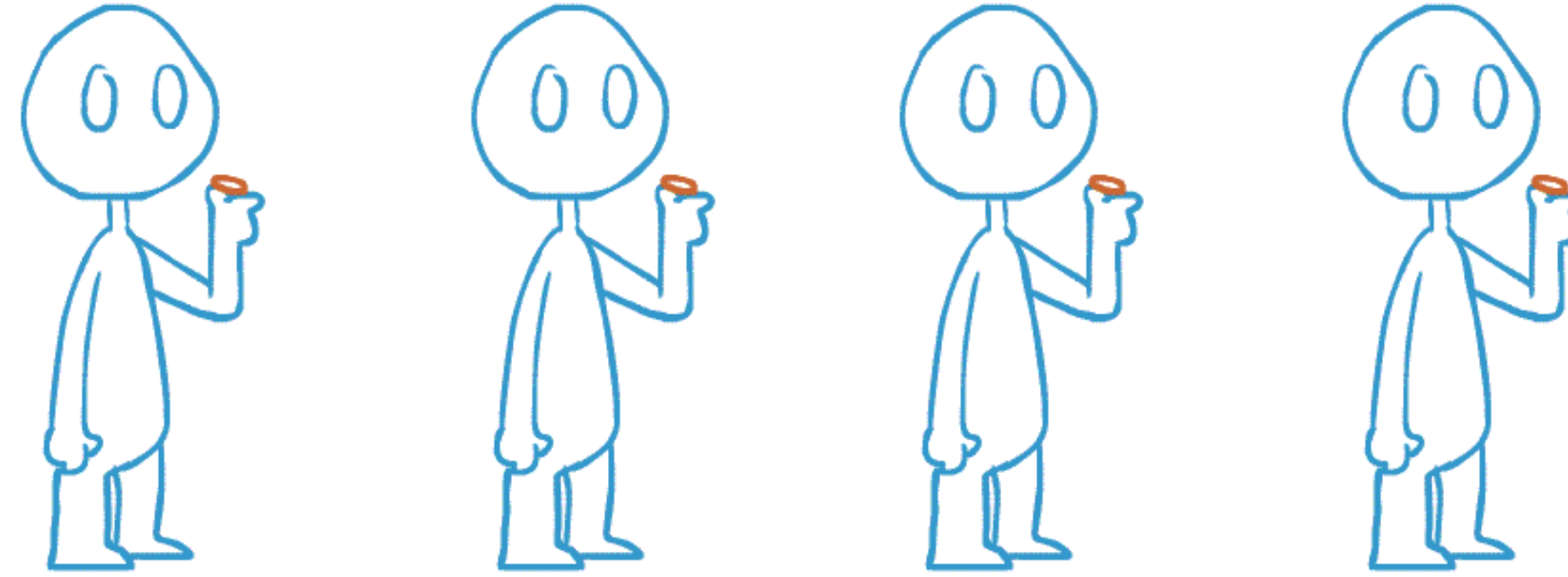
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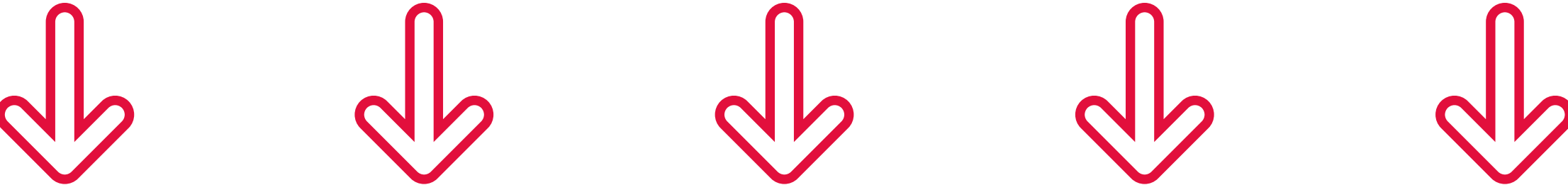
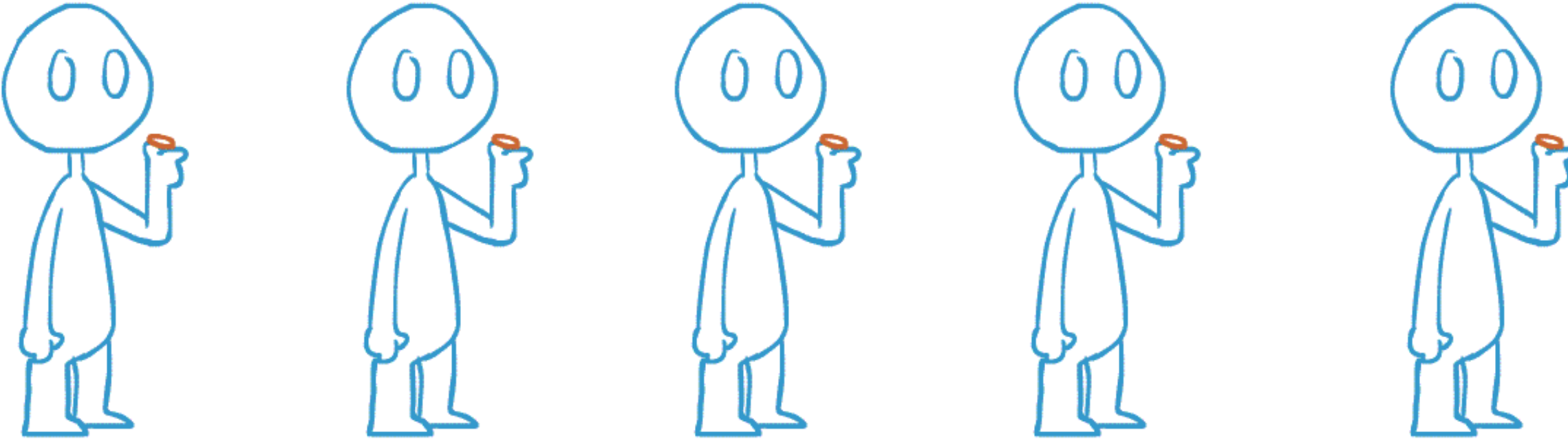
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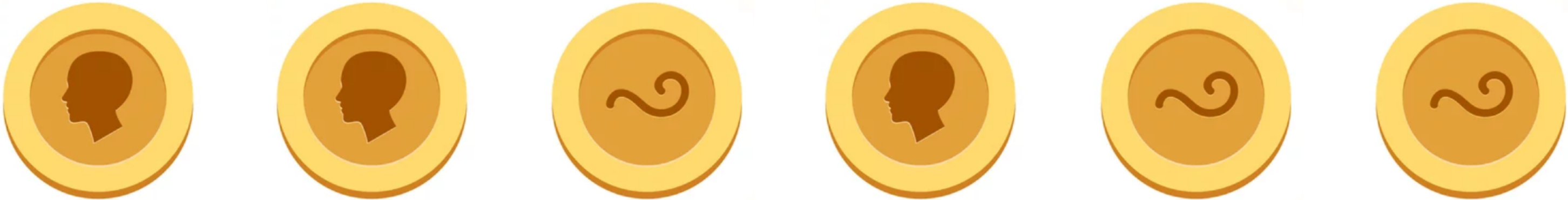
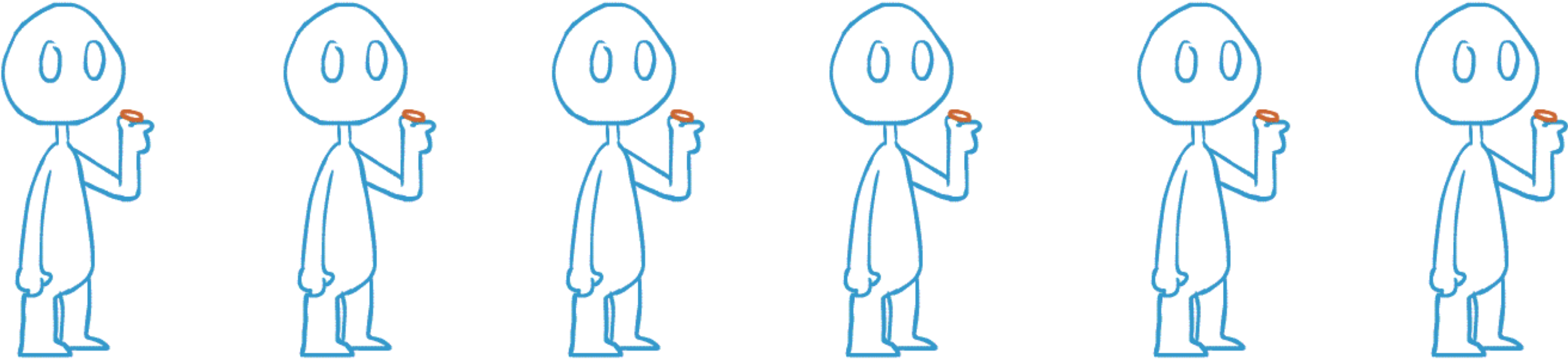
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▶ w h a t w e d o :



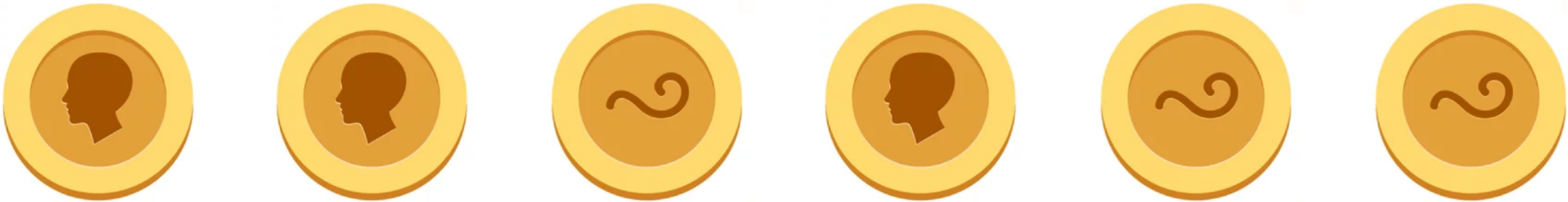
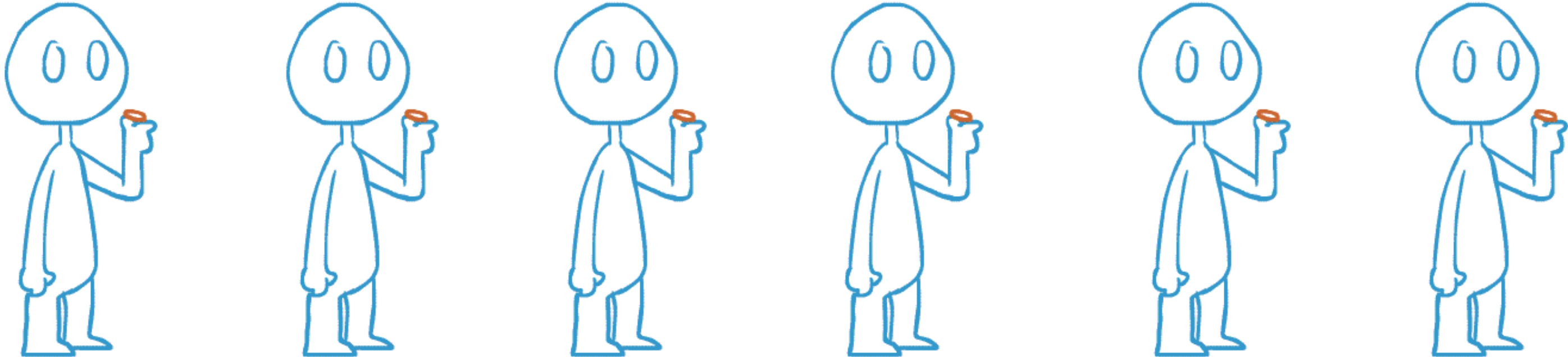
1 1 0 1 0

▶ w h a t w e d o :



1 1 0 1 0 0

▶ w h a t w e d o :



1 1 0 1 0 0



Random Power is developing a platform of Silicon based, patent protected, "QUANTUM coin flippers", generating virtually endless streams of random bits

▶ w h a t f o r :

Unpredictability to preserve the **predictability** of our clockwork world

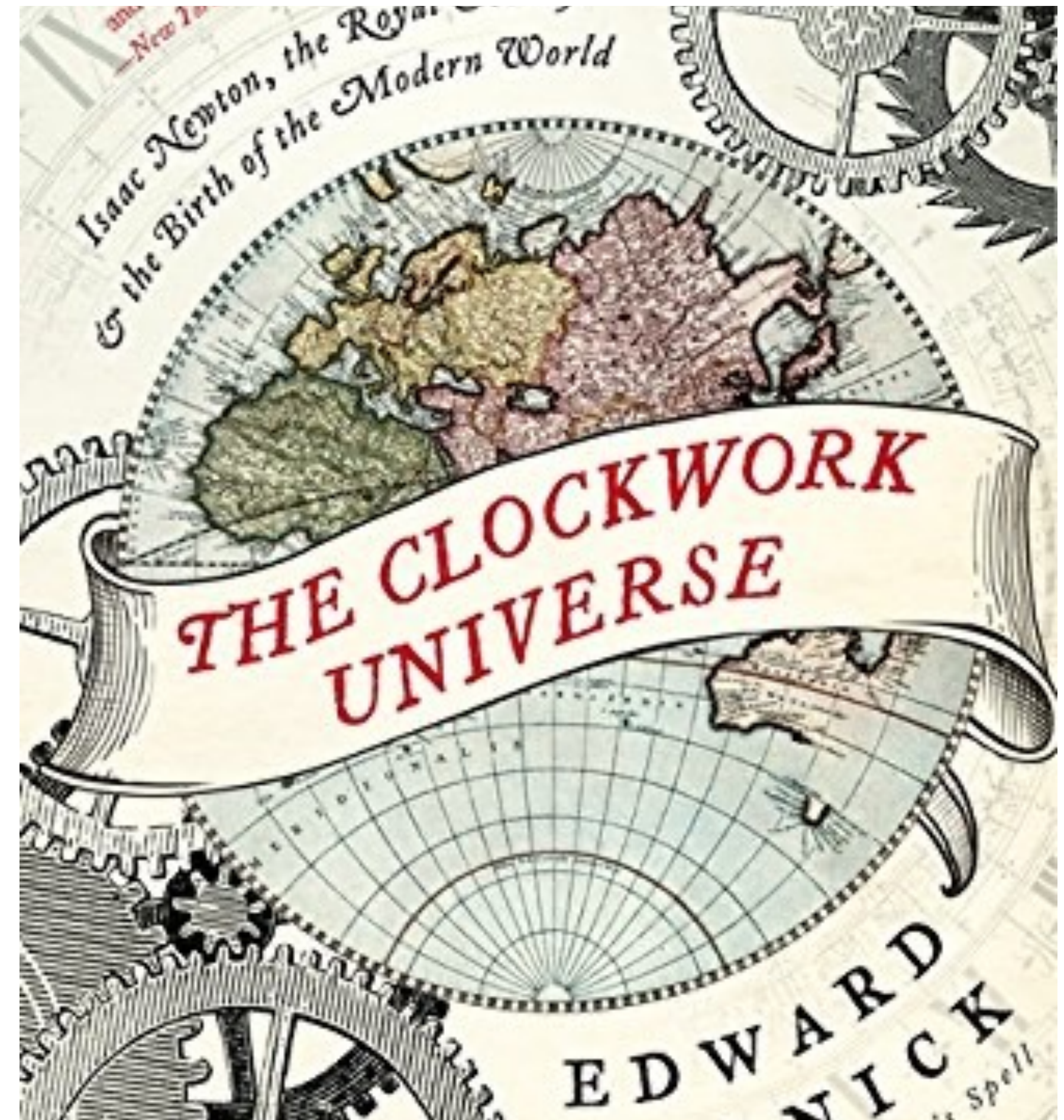
* There is definitely a hype about Random bit streams, not only for **cryptograhya & authentication** but also for **gaming, virtual reality, Monte Carlo simulations** , **Privacy Preservation Procedures and Identity management**

to learn more, watch [this](#) BBC report:

The search for the random numbers that run our lives

6 July 2024

Share 



The Clockwork Universe
Isaac Newton, Royal Society, and the Birth of the Modern World
by Edward Doinick - 2011 Harper Collins

▶ t h e p r o b l e m :

4

Generating REAL, certified and *robust* randomness is far from being trivial, both using algorithmic solutions and exploiting unpredictable natural phenomena based on classical physics

► t h e p r o b l e m :

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Generating REAL, certified and *robust* randomness is far from being trivial, both using algorithmic solutions and exploiting unpredictable natural phenomena based on classical physics

► [1951, John Von Neumann](#) [J. Res. Nat. Bur. Stand. Appl. Math. Series 3, 36-38 (1951)]

Various Techniques Used in Connection With Random Digits

Anyone who considers arithmetical methods of producing random digits is, of course, in a state of sin.

▶ t h e p r o b l e m :

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▶ [a 2013 NSA scandal unveiled by the NYT:](#)



The screenshot shows the New York Times website interface. At the top, there are navigation links for HOME PAGE, TODAY'S PAPER, VIDEO, MOST POPULAR, and U.S. Edition. The main header features the New York Times logo, the word "U.S.", and a search bar. Below the header is a horizontal menu with categories: WORLD, U.S., N.Y./REGION, BUSINESS, TECHNOLOGY, SCIENCE, HEALTH, SPORTS, OPINION, ARTS, STYLE, TRAVEL, JOBS, REAL ESTATE, and AUTOS. Underneath, there are sub-categories: POLITICS, EDUCATION, and TEXAS. The main content area displays the article title "Secret Documents Reveal N.S.A. Campaign Against Encryption" in bold. Below the title is a short summary: "Documents show that the N.S.A. has been waging a war against encryption using a battery of methods that include working with industry to weaken encryption standards, making design changes to cryptographic software, and pushing international encryption standards it knows it can break. [Related Article »](#)". Below the summary are two buttons: "Excerpt from 2013 Intelligence Budget Request" and "Bullrun Briefing Sheet". At the bottom of the article preview, there is a paragraph: "This excerpt from the N.S.A.'s 2013 budget request outlines the ways in which the agency circumvents the encryption protection of everyday Internet communications. The Sigint Enabling Project involves industry relationships, clandestine changes to commercial software to weaken encryption, and lobbying for encryption standards it can crack."

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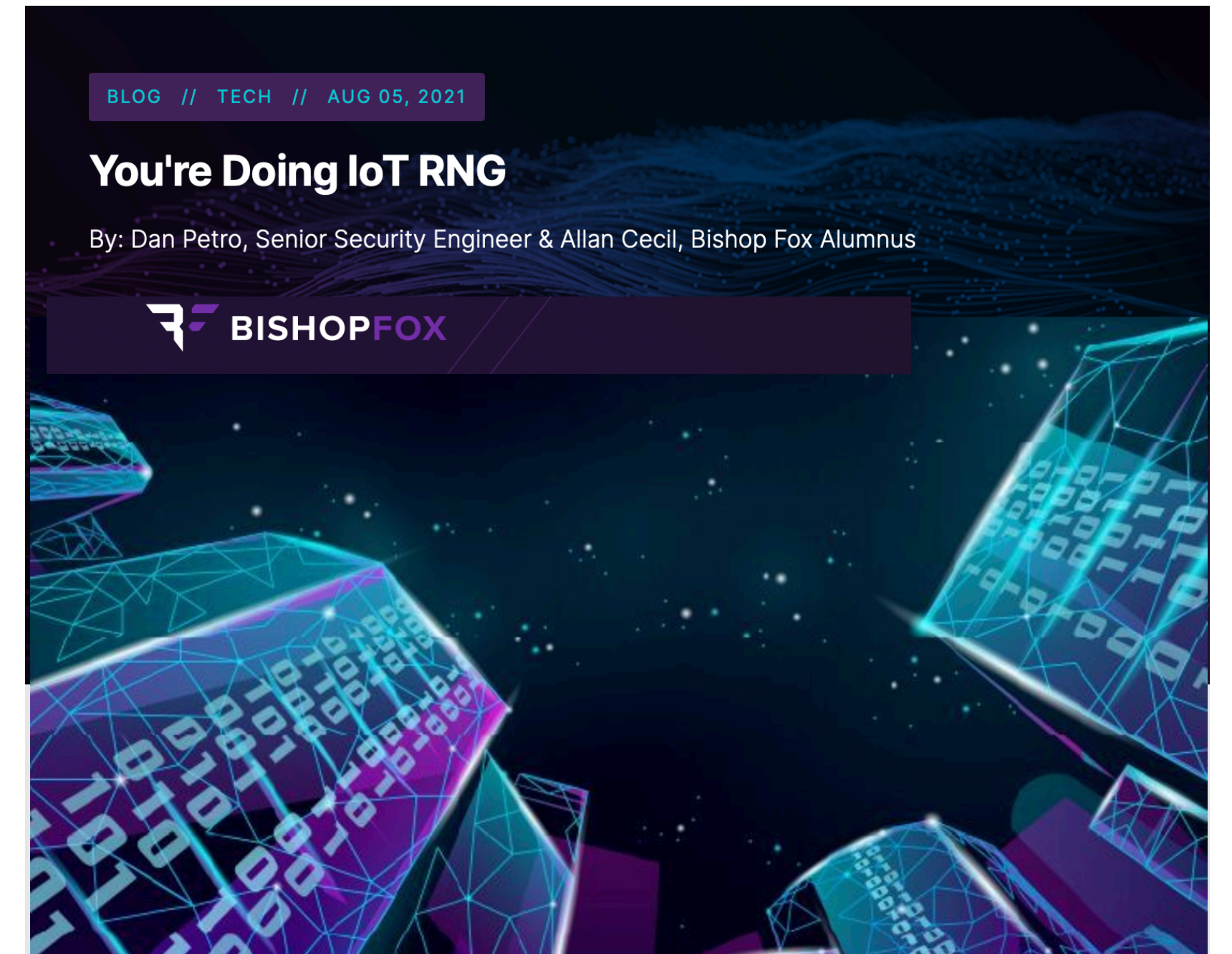
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Generating REAL, certified and *robust* randomness is far from being trivial, both using algorithmic solutions and exploiting unpredictable natural phenomena based on classical physics

▶ [a 2021 finding on weakness in Randomness generation for IoT:](#)



Share



There's a crack in the foundation of Internet of Things (IoT) security, one that affects **35 billion devices worldwide**. Basically, every IoT device with a hardware random number generator (RNG) contains a serious vulnerability whereby it fails to properly generate random numbers, which undermines security for any upstream use.

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Generating REAL, certified and *robust* randomness is far from being trivial, both using algorithmic solutions and exploiting unpredictable natural phenomena based on classical physics

▶ [a 2023 article on FORBES:](#)

Challenges Of Zero-Knowledge Proof Technology For Compliance



Alexander Ray Forbes Councils Member
Forbes Business Council COUNCIL POST | Membership (fee-based)

Problem 2: Vulnerability To Random Number Generator Attacks

▶ **t h e p r o b l e m :**

Generating REAL, certified and *robust* randomness is far from being trivial, both using algorithmic solutions and exploiting unpredictable natural phenomena based on classical physics

▶ [a 2020 paper by the U.S. Census Bureau:](#)

Randomness Concerns When Deploying Differential Privacy

Simson L. Garfinkel
US Census Bureau
Suitland, MD
simson.l.garfinkel@census.gov

Philip Leclerc
US Census Bureau
Suitland, MD
philip.leclerc@census.gov

true data. Thus, while the data for the Decennial Census can be stored in a few tens of gigabytes, protecting its output statistics will require the DAS to use roughly 90TB of random data.

▶ [a 2023 article on FORBES:](#)

Challenges Of Zero-Knowledge Proof Technology For Compliance



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Problem 2: Vulnerability To Random Number Generator Attacks

▶ the *optimal* solution:

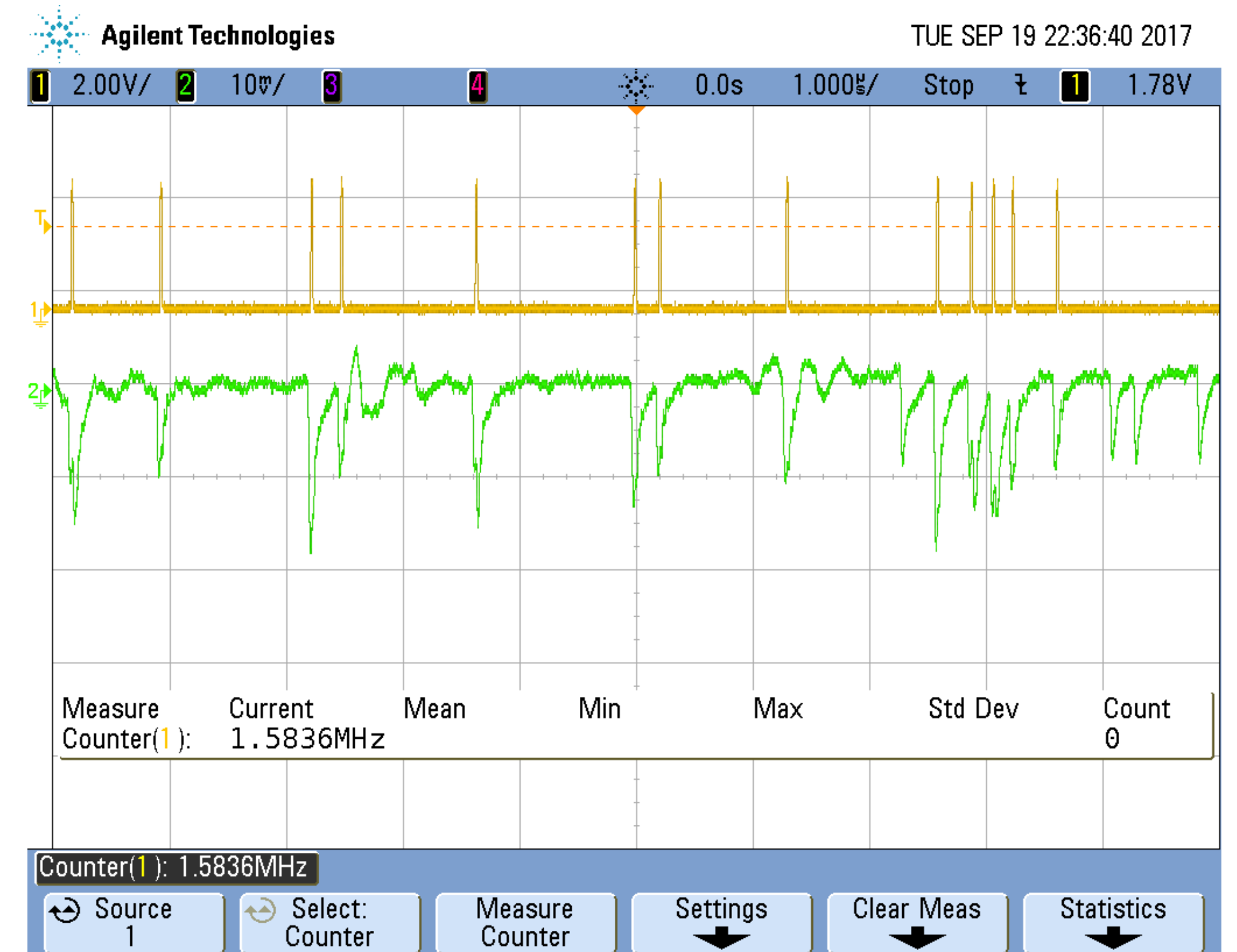
RANDOM NUMBER GENERATION BY OBSERVING UNPREDICTABLE QUANTUM PHENOMENA

where unpredictability is secured by the very same laws of Nature.

▶ the optimal solution:

RANDOM NUMBER GENERATION BY OBSERVING UNPREDICTABLE QUANTUM PHENOMENA

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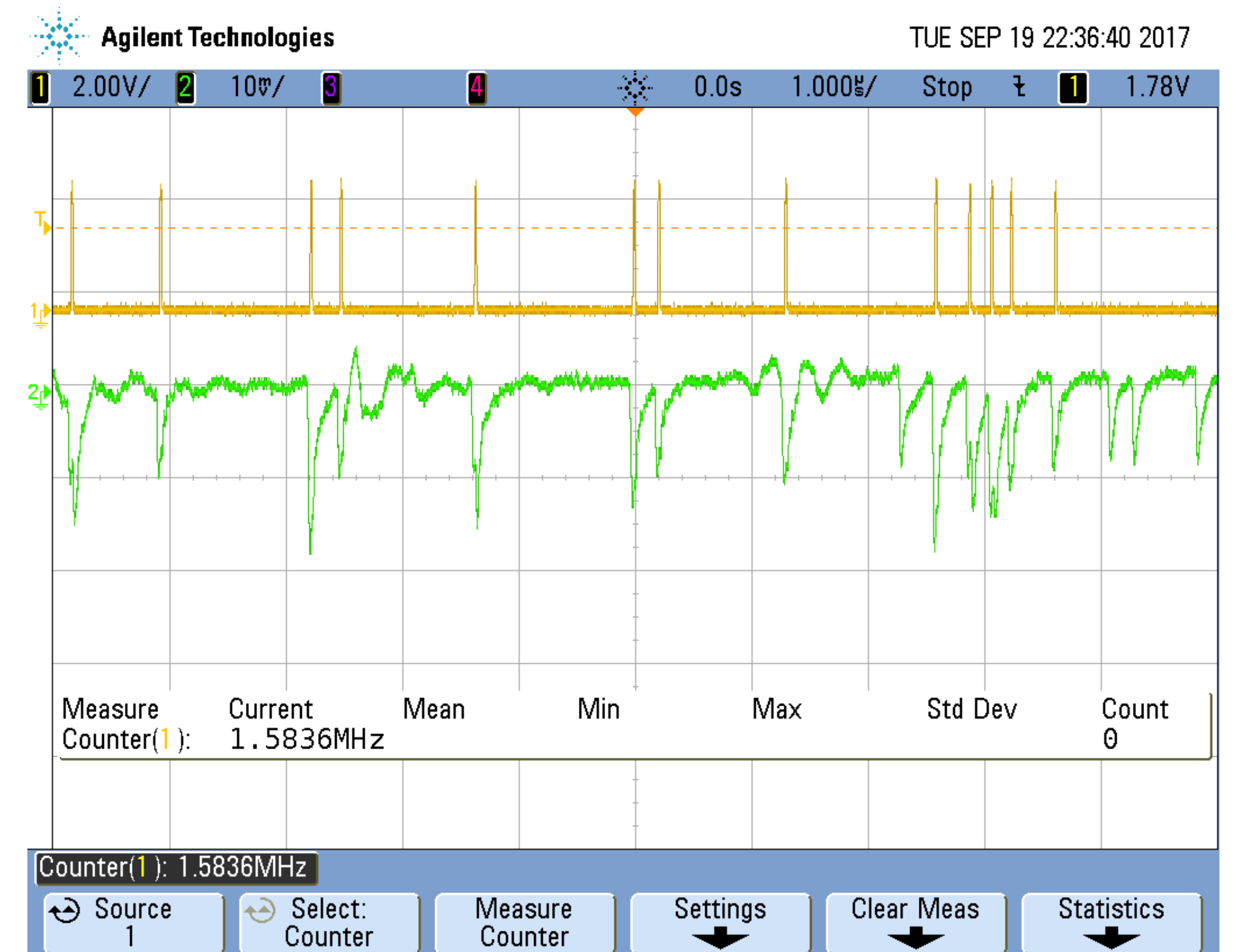
RANDOM NUMBER GENERATION BY OBSERVING UNPREDICTABLE QUANTUM PHENOMENA

where unpredictability is secured by the very same laws of Nature.

* The very first example: exploiting the unpredictability of Radioactive Decays

the sequence of detected decays can be used to generate random bits with different recipes:

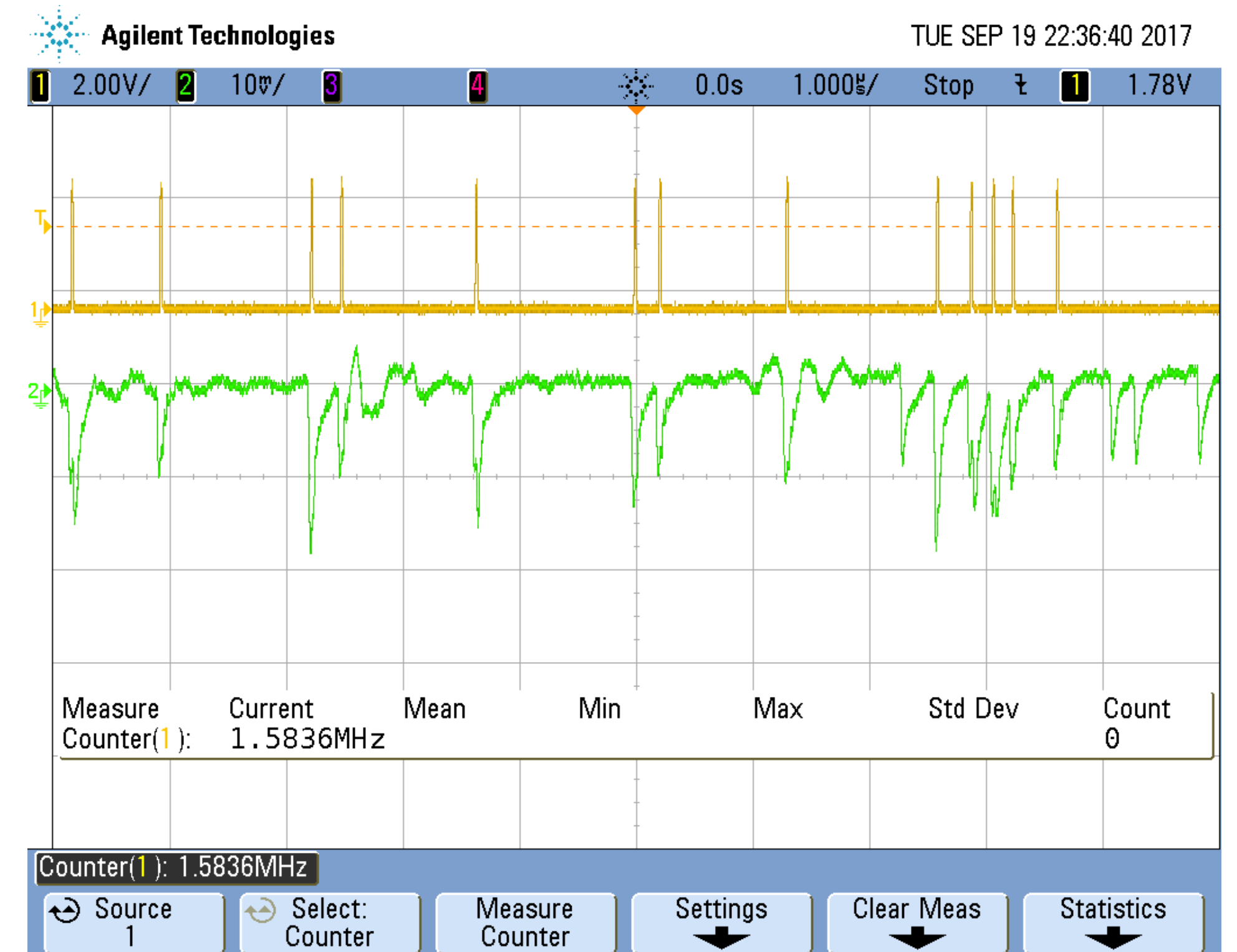
- check the parity of the number of pulses in a time window
- pre-define the time window in a way that is equally like to have or not to have a single pulse



▶ the optimal solution:

RANDOM NUMBER GENERATION BY OBSERVING UNPREDICTABLE QUANTUM PHENOMENA

where unpredictability is secured by the very same laws of Nature.



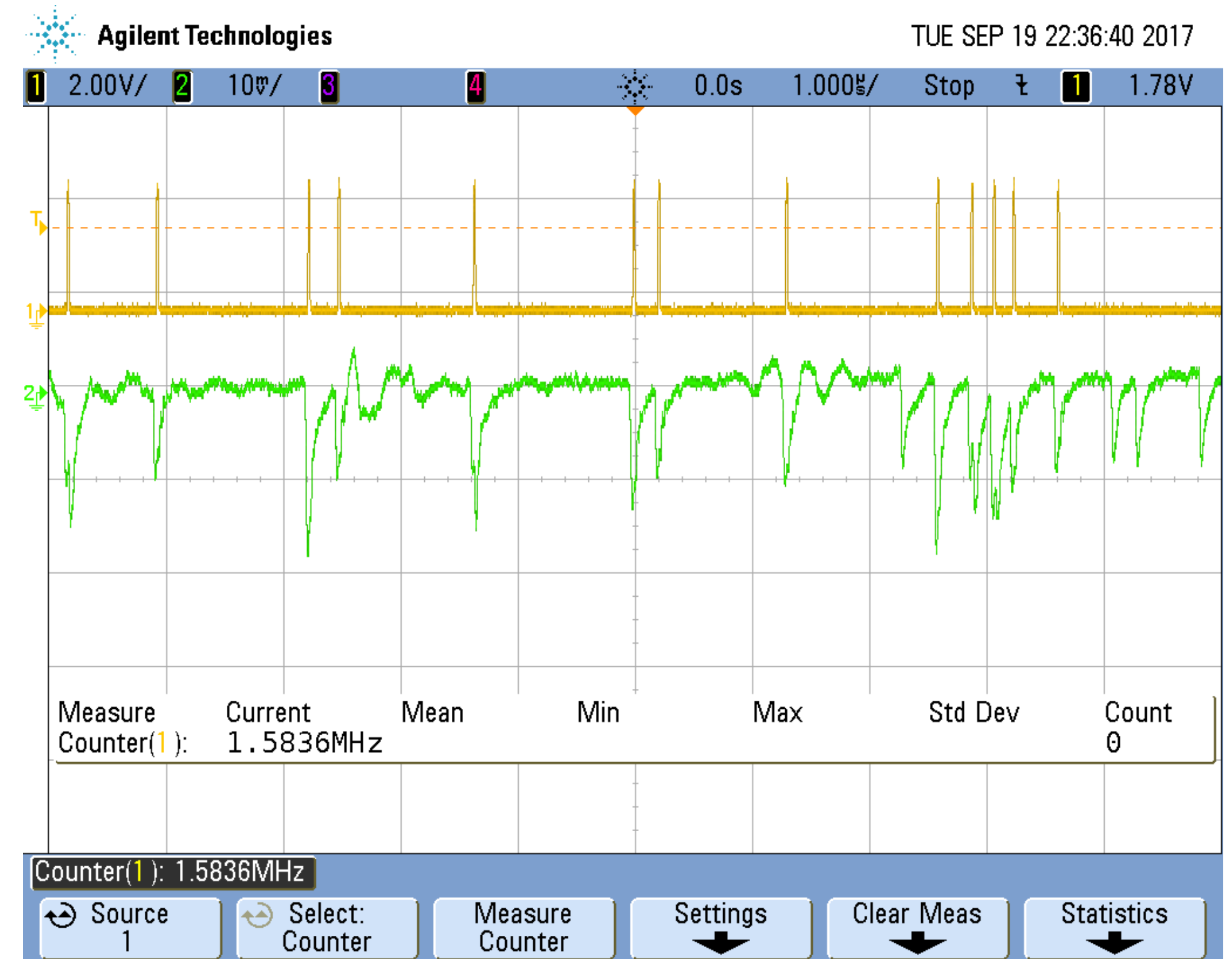
RANDOM NUMBER GENERATION BY OBSERVING UNPREDICTABLE QUANTUM PHENOMENA

where unpredictability is secured by the very same laws of Nature.

Inspired by Forrest Gump, we say:

* RADIOACTIVE IS AS RADIOACTIVE DOES

The idea behind **RANDOM POWER** is to replace a radioactive source with something safer, more handy, cost effective, simple, robust, providing sequences of pulses mimicking radioactive decays.



▶ the *R a n d o m P o w e r* way :

A THREE STEP DANCE:

► the **R a n d o m P o w e r** way :

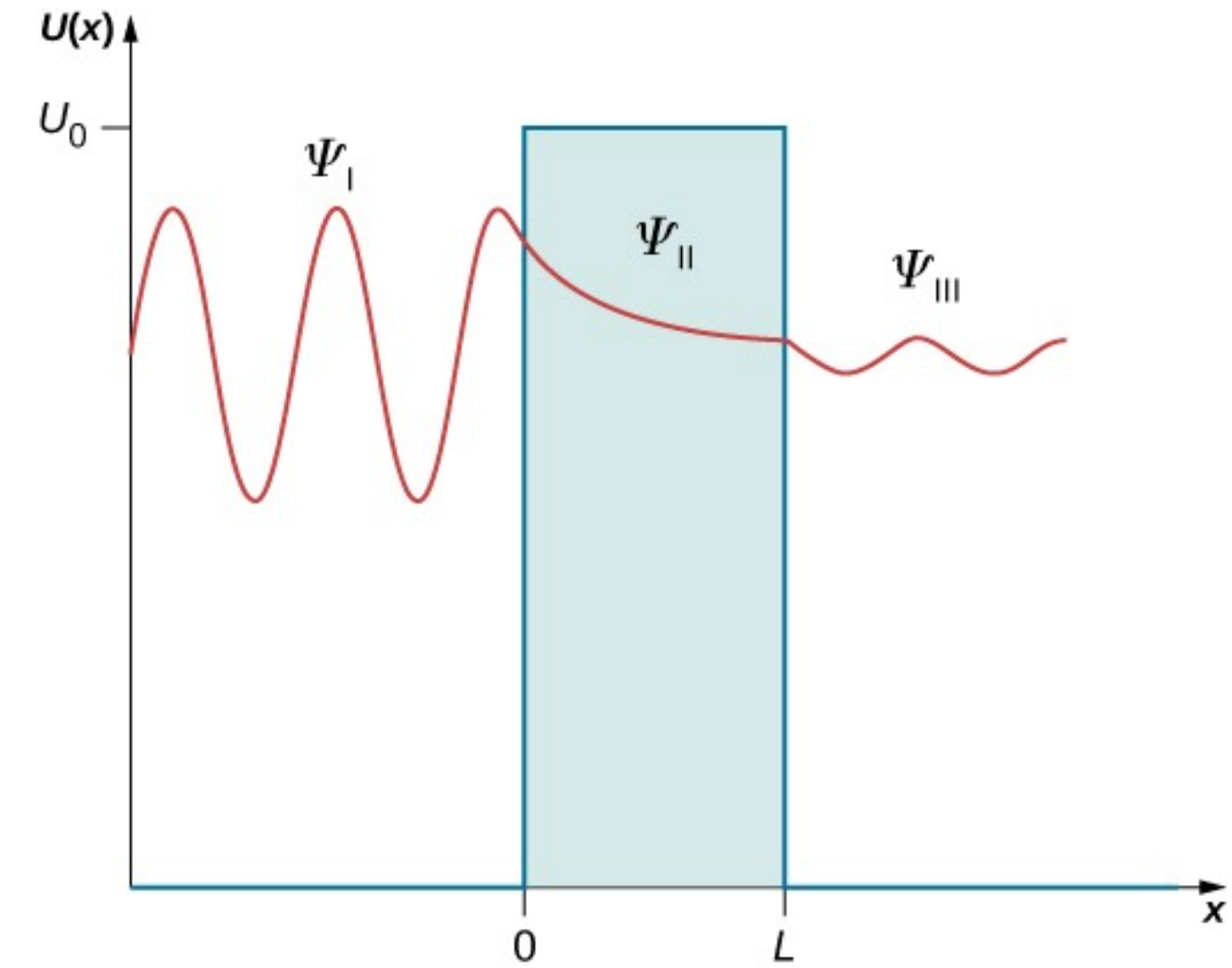
A THREE STEP DANCE:

The name of the game is **QUANTUM TUNNELING:**

* **Electrons** and quantum entities in general are not like a  but they rather appear as a



when they bounce against a [potential] barrier, they can occasionally go through in an unpredictable way.



► the **R a n d o m P o w e r** way :

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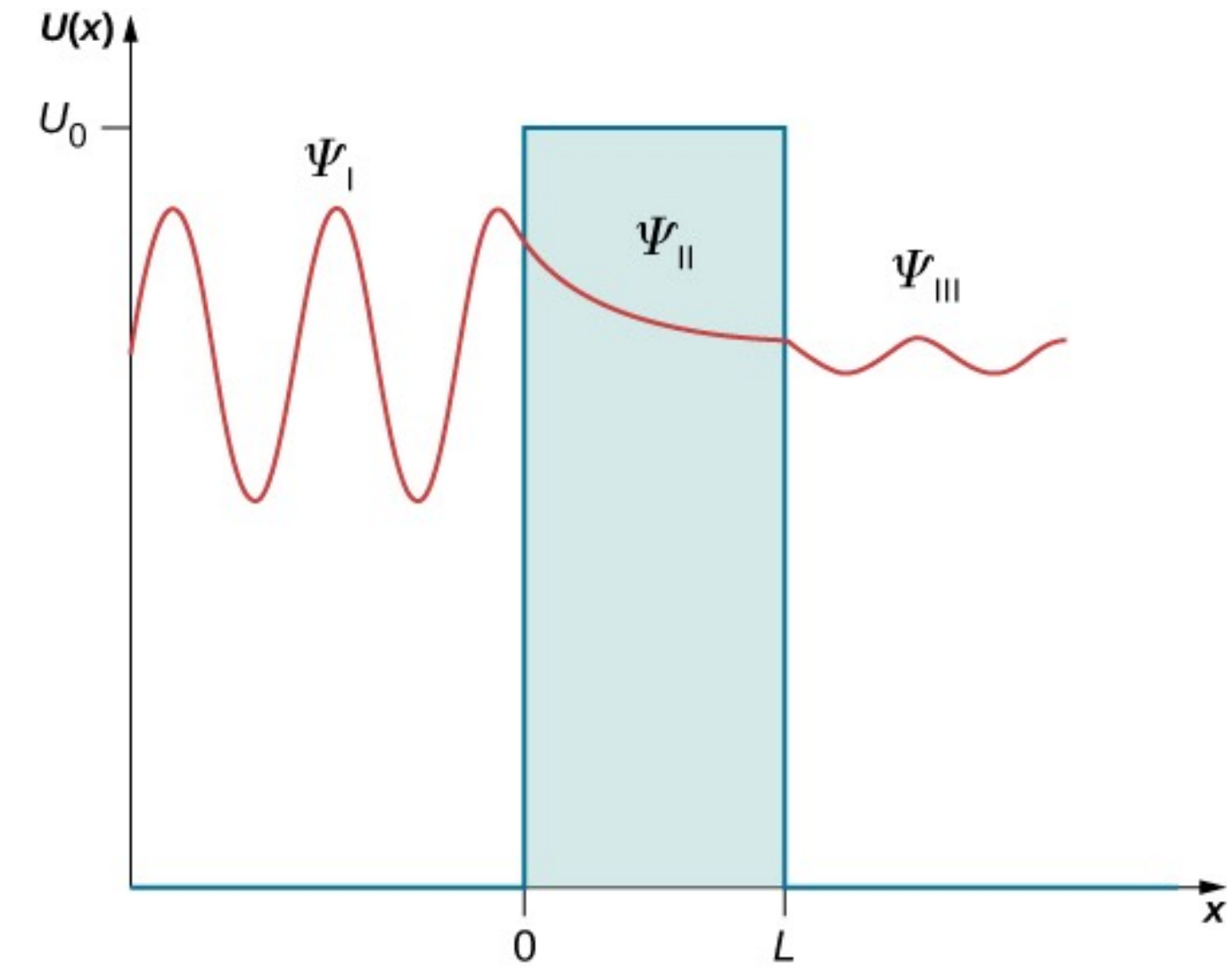
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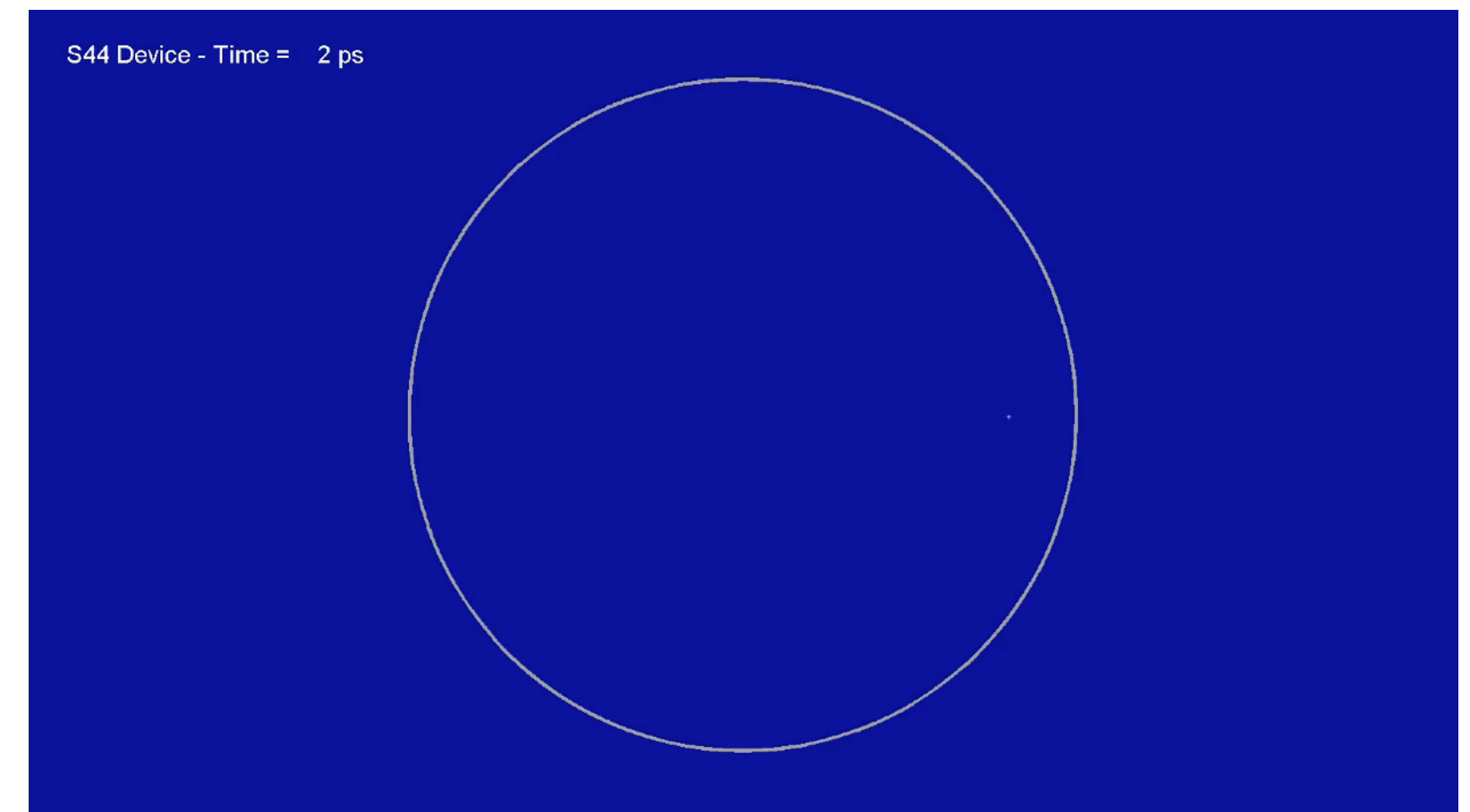
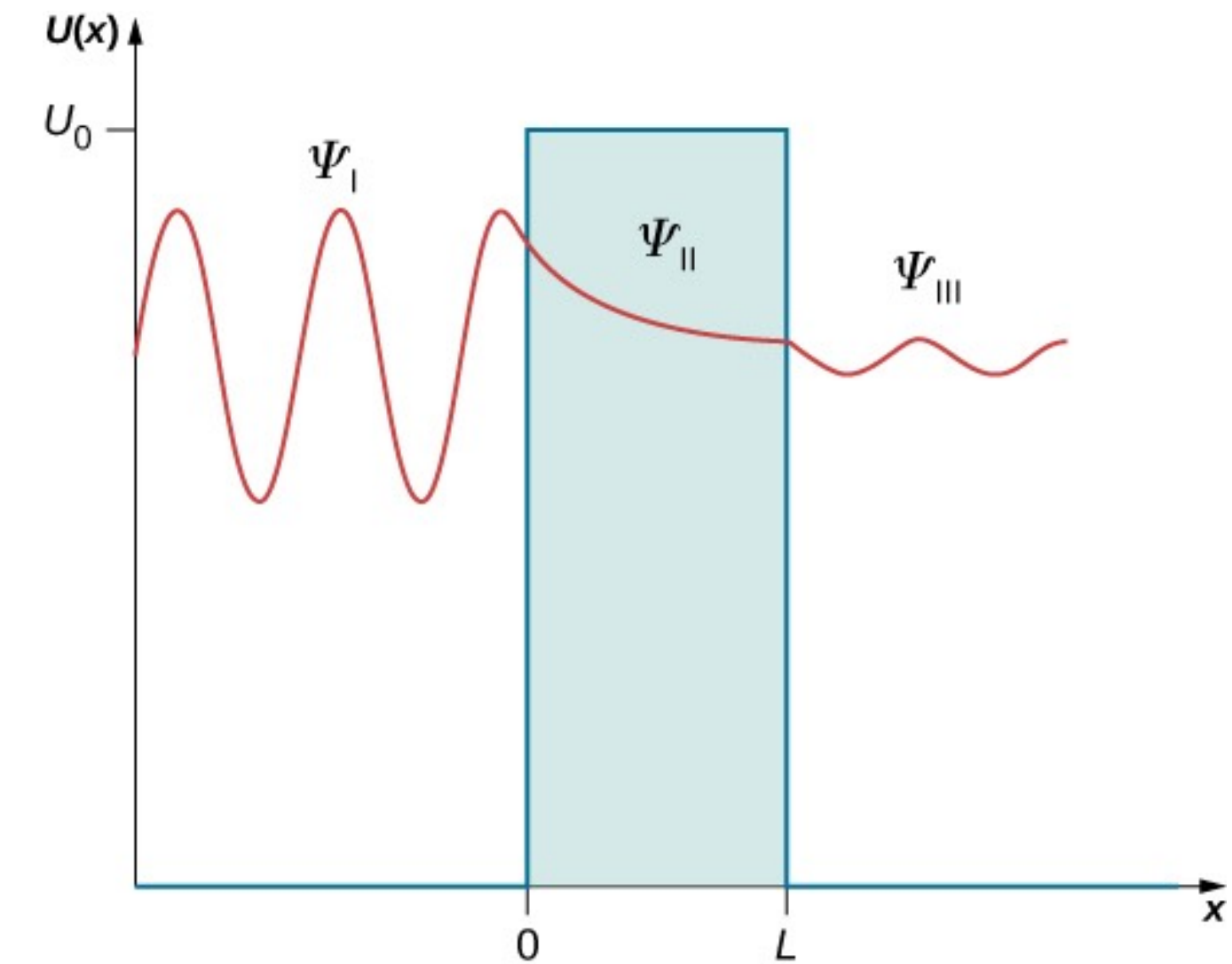
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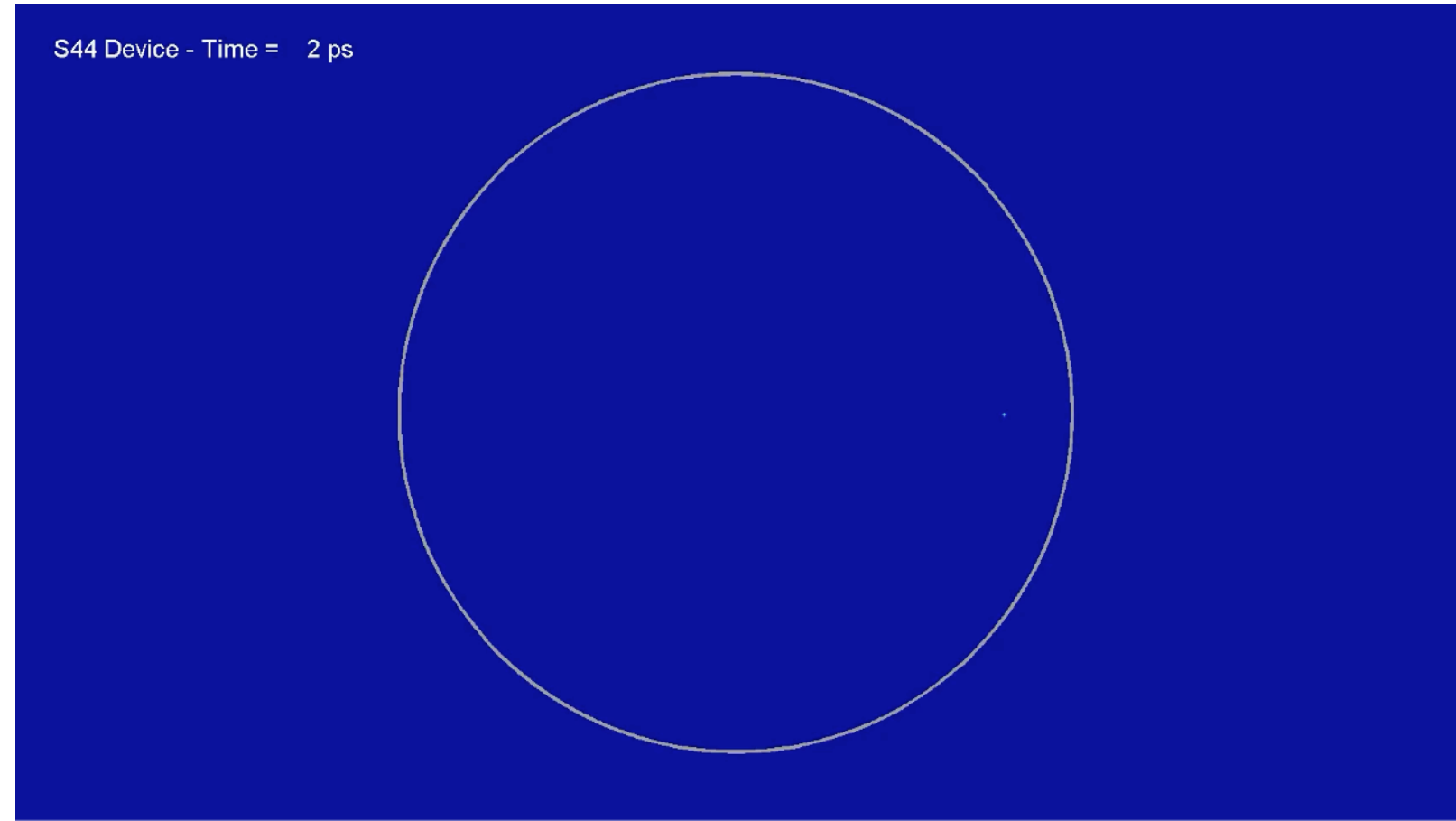
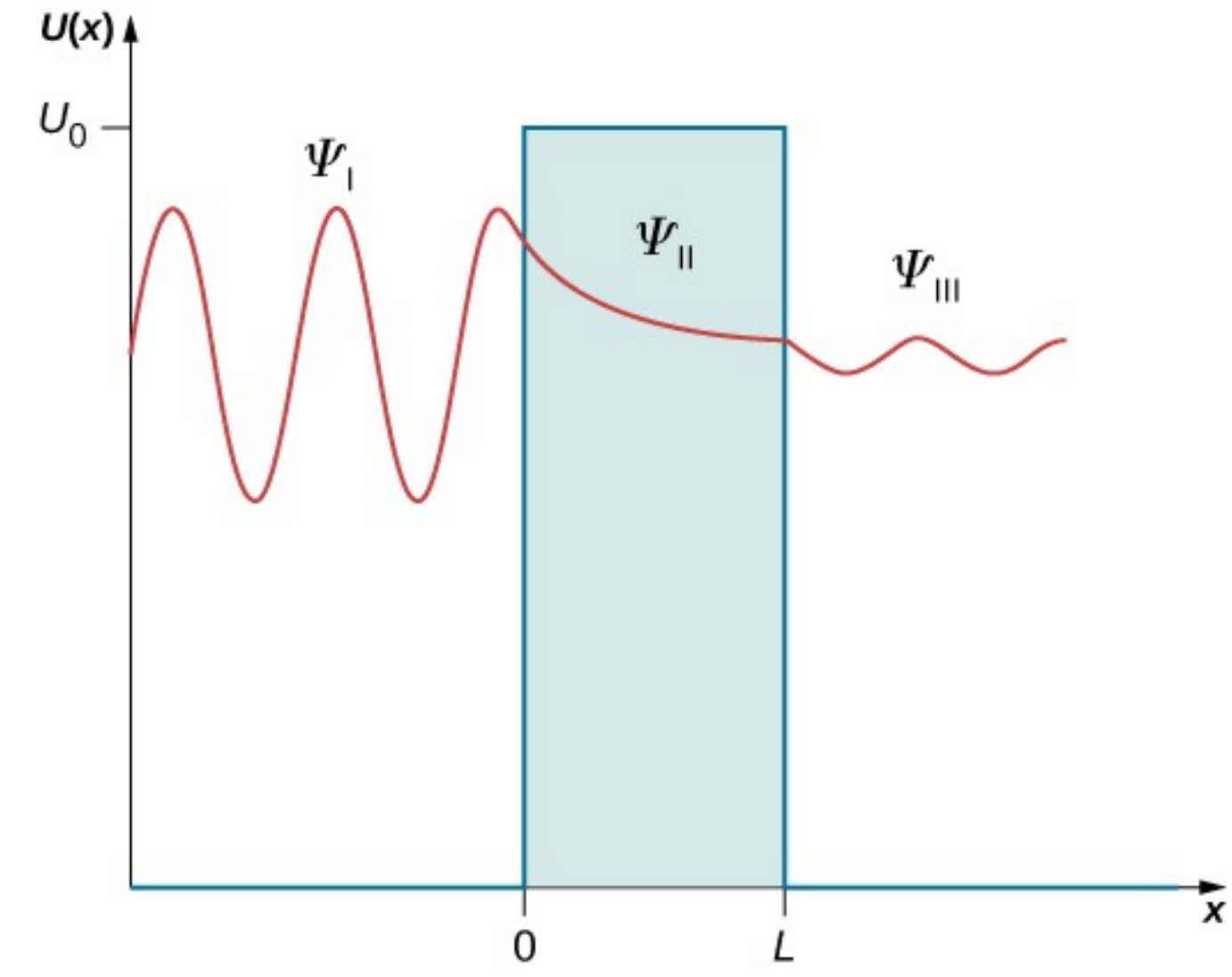
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Courtesy of Ivan Rech, Politecnico di Milano
[50 μm cell size]

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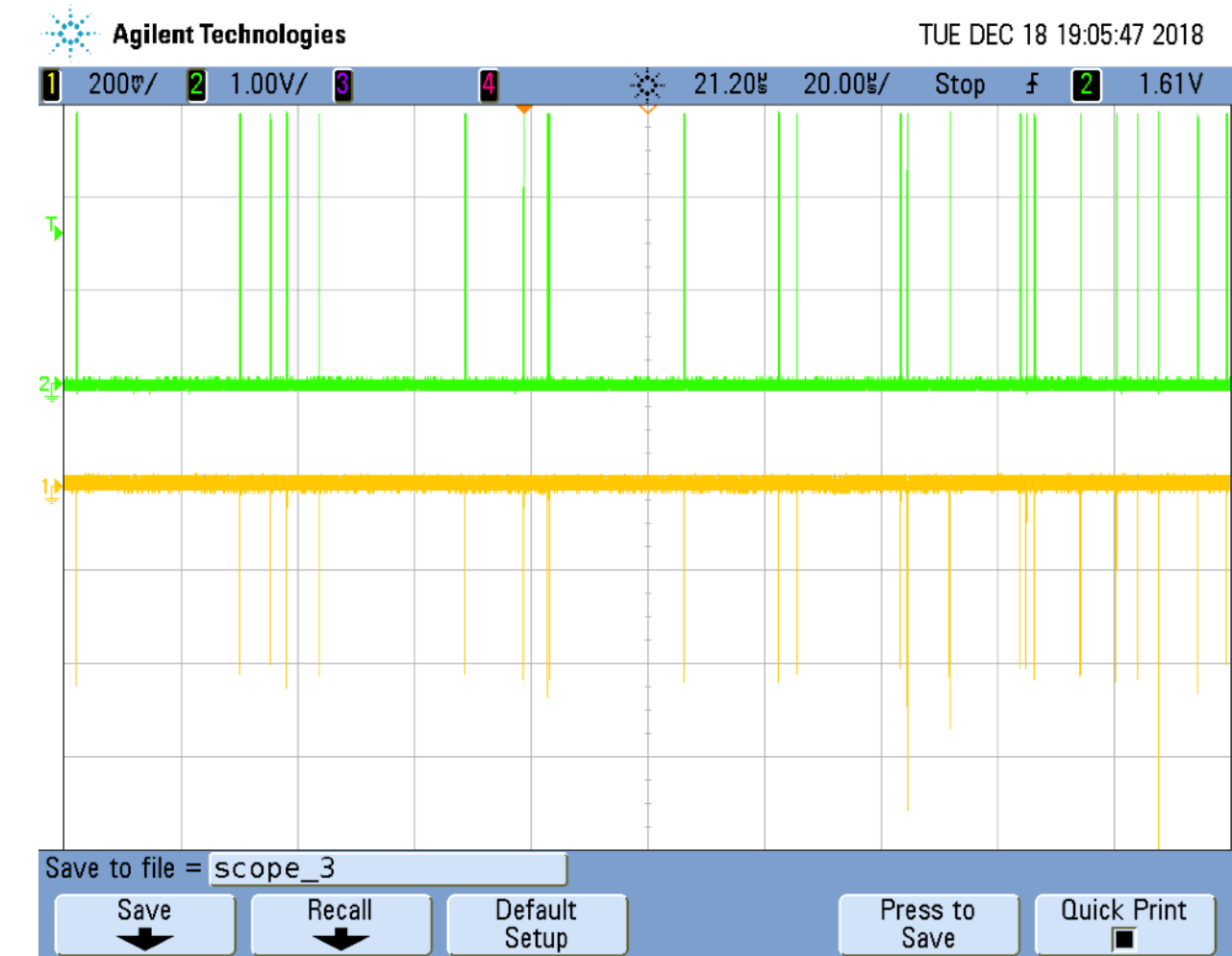
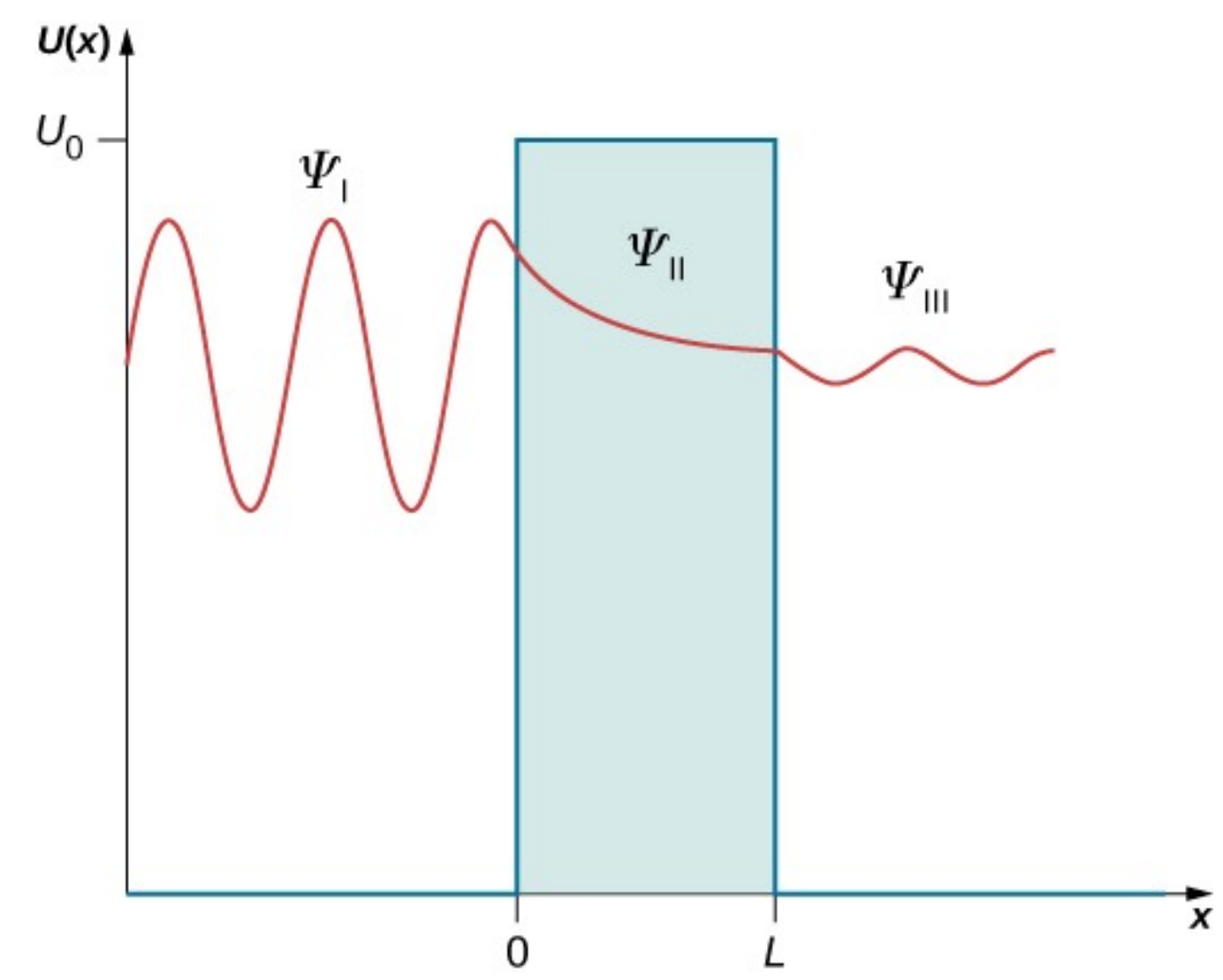
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* When this is happening, the “ghost” electron enters a region of high electric field, generating a **current pulse** by impact ionisation

* By **time stamping** the pulses the analysing the time series, we turn unpredictable occurrence of the pulses into **bits**

and we embody the principle in a platform of Silicon-based devices



This is the **PATENTED** essence of



Ministero dello Sviluppo Economico

Direzione generale per la tutela della proprietà industriale

Ufficio Italiano Brevetti e Marchi

ATTESTATO DI BREVETTO PER INVENZIONE INDUSTRIALE

Il presente brevetto viene concesso per l'invenzione oggetto della domanda:

N. 102018000009064



(11) EP 3 861 431 B8

(12) CORRECTED EUROPEAN PATENT SPECIFICATION

(15) Correction information:
Corrected version no 1 (W1 B1)
Corrections, see
Bibliography INID code(s) 73

(51) International Patent Classification (IPC):
G06F 7/58 (2006.01) H04L 9/08 (2006.01)

(52) Cooperative Patent Classification (CPC):
H04L 9/0852; G06F 7/588; Y04S 40/20

(48) Corrigendum issued on:
16.11.2022 Bulletin 2022/46

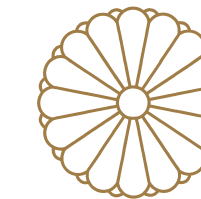
(86) International application number:
PCT/IB2019/058340

(45) Date of publication and mention
of the grant of the patent:
05.10.2022 Bulletin 2022/40

(87) International publication number:
WO 2020/070641 (09.04.2020 Gazette 2020/15)

(21) Application number: 102018000009064

(22) Date of filing: 01.10.2019



特許証

(CERTIFICATE OF PATENT)

特許第7568297号

(PATENT NUMBER)

発明の名称
(TITLE OF THE INVENTION)

ランダムビットシーケンスを生成するための装置及び方法

特許権者
(PATENTEE)

イタリア20129ミラノ、ヴィア・マセドニ
オ・メローニ40

国籍・地域 イタリア共和国

発明者
(INVENTOR)

ランダム・パワー・ソチエタ・ア・レ
スポンサビリタ・リミタータ・イン・
フォルマ・アッブレヴィアータ・ラッ
プ!・ソチエタ・ア・レス (その他別紙記載)
マッシモ・ルイージ・マリア・カッチ
ア

RANDOM
POWER

- Italian Patent granted in Sept. 2020
- EU patent granted in 2022
- Japanese patent granted in 2024
- in the examination phase in China, Korea and U.S. (since April 2021)

This is the **PATENTED** essence of

9

RANDOM POWER

where the key issues are:

- ▶ **endogenous in-silico seeding of the pulses**
- ▶ self-amplification of the seeds in excess of a factor 1 000 000, **making pulse tagging robust**
- ▶ **bit extraction through a non parametric local analysis of the time series of pulses**
- ▶ no influence of temperature on the randomness of the occurrences
- ▶ **no need of post-processing to correct left-over bias**
- ▶ maximum bit/occurrence rate = 40% [2 random bits every 5 pulses]
- ▶ **current rate at the 5-10 Mbps rate for every mm² of Silicon sensor**
- ▶ potential to embed the generator into an ASIC [Application Specific Integrated Circuit]

a. Our principle is actually a lesson from the past. This effect was known since the early days of the Silicon technology development:

1. INTRODUCTION

MOST reverse biased $p-n$ junctions in silicon have their avalanche breakdown caused by microplasma effects. Microplasmas are small regions within the junction,¹ where a local disturbance of the electrical field is believed to reduce the breakdown voltage to a value below the breakdown voltage of the surrounding uniform junction.²⁻⁵ As voltage is increased from low values microplasma breakdown is generally characterized by random "on-off" current fluctuations so long as currents remain below a critical value (40 to 120 μA).⁶⁻⁸

from paper 2

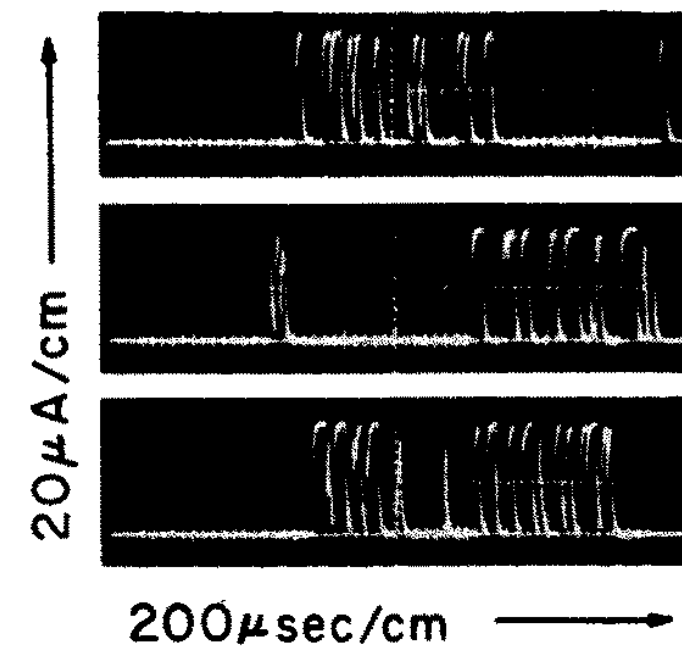


FIG. 5. Avalanche current as a function of time at low temperatures. The group character of the avalanche pulses is obvious.

from paper 3

1

Avalanche Breakdown in Silicon

K. G. MCKAY
Bell Telephone Laboratories, Murray Hill, New Jersey
(Received December 23, 1953)

2

Model for the Electrical Behavior of a Microplasma*

ROLAND H. HAITZ†
Shockley Laboratory, Clevite Corporation Semiconductor Division, Palo Alto, California
(Received 5 November 1963)

The complex current fluctuations observed in connection with microplasma breakdown can be explained by a simple model containing two constants: extrapolated breakdown voltage V_b and series resistance R_s ; and two continuous probability functions: turnoff probability per unit time $p_{10}(I)$ as a function of pulse current I and turn-on probability per unit time p_{01} . Experimental methods allowing an accurate measurement of these four quantities are described. The new concept of an extrapolated breakdown voltage V_b is discussed based on two independent measurements: one of secondary multiplication and the other of instantaneous current, both as a function of voltage. Within the experimental accuracy of 20 mV both methods extrapolated to one and the same breakdown voltage. The turnoff probability $p_{10}(I)$ is determined by a new combination of experimental techniques to cover the current range from 5 to 70 μA with a variation of 11 decades for $p_{10}(I)$. The observation of a narrow turnoff interval is explained quantitatively.

3

Mechanisms Contributing to the Noise Pulse Rate of Avalanche Diodes*

ROLAND H. HAITZ†
Shockley Research Laboratory, Semiconductor Division of Clevite Corporation, ‡ Palo Alto, California
(Received 16 November 1964)

► **The phenomenology is by now quite well known** [even if large uncertainties are still there, requiring somehow a “cook & look” approach]

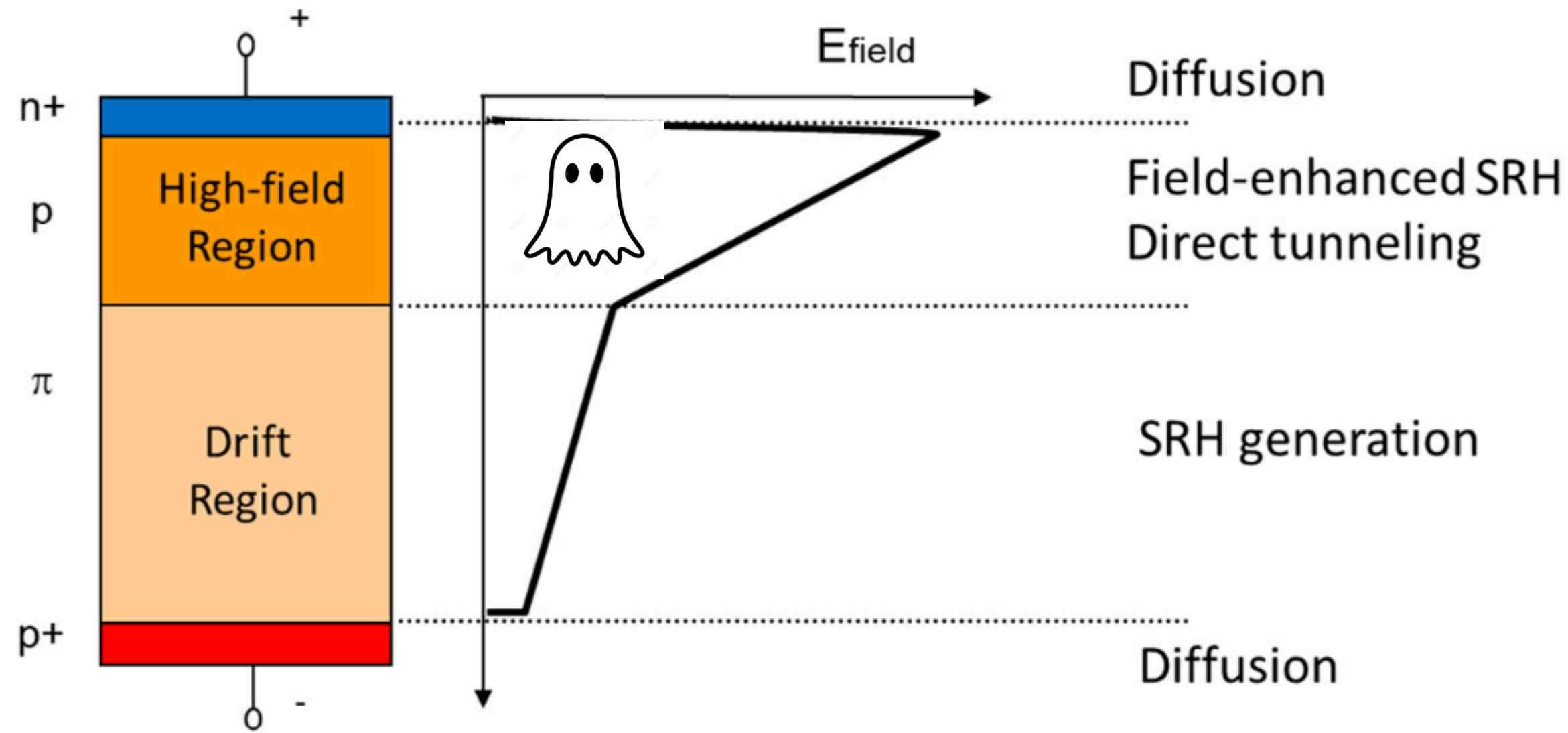


Fig. 8. Representation of the different sources of primary dark events and their location in the SPAD structure.

after A. Gola, C. Piemonte, NIM A926 (2019) 2-15

Key issues:

- * **the Pulse Rate is O(1 KHz)/cell, 50 μm pitch (it may be higher for SPAD arrays in CMOS technology)**
- * provided the nature of the “Dark Pulses”, we have a significant dependence on Temperature
- * forget-me-not: the Over-voltage is affecting the triggering probability

Thermal generation of carriers by states in the bang-gap

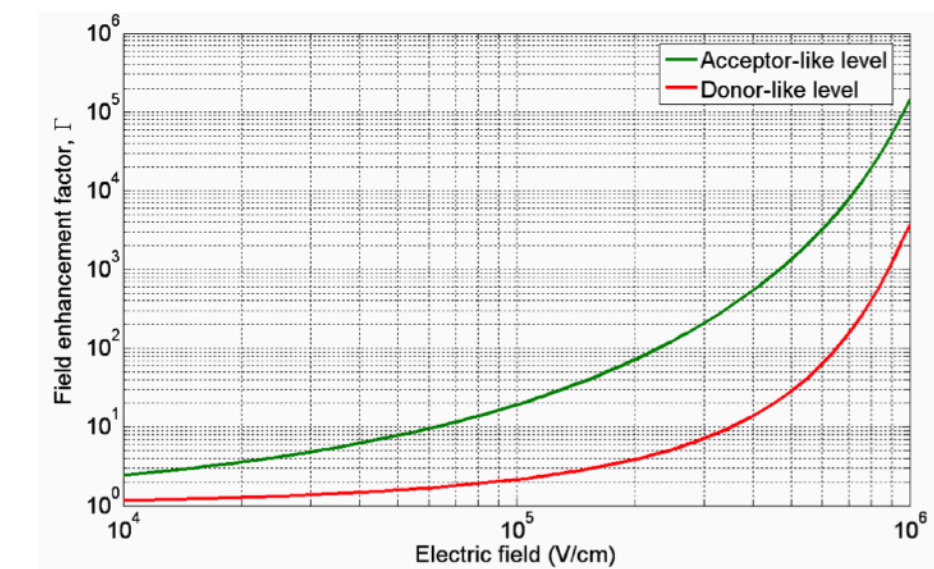
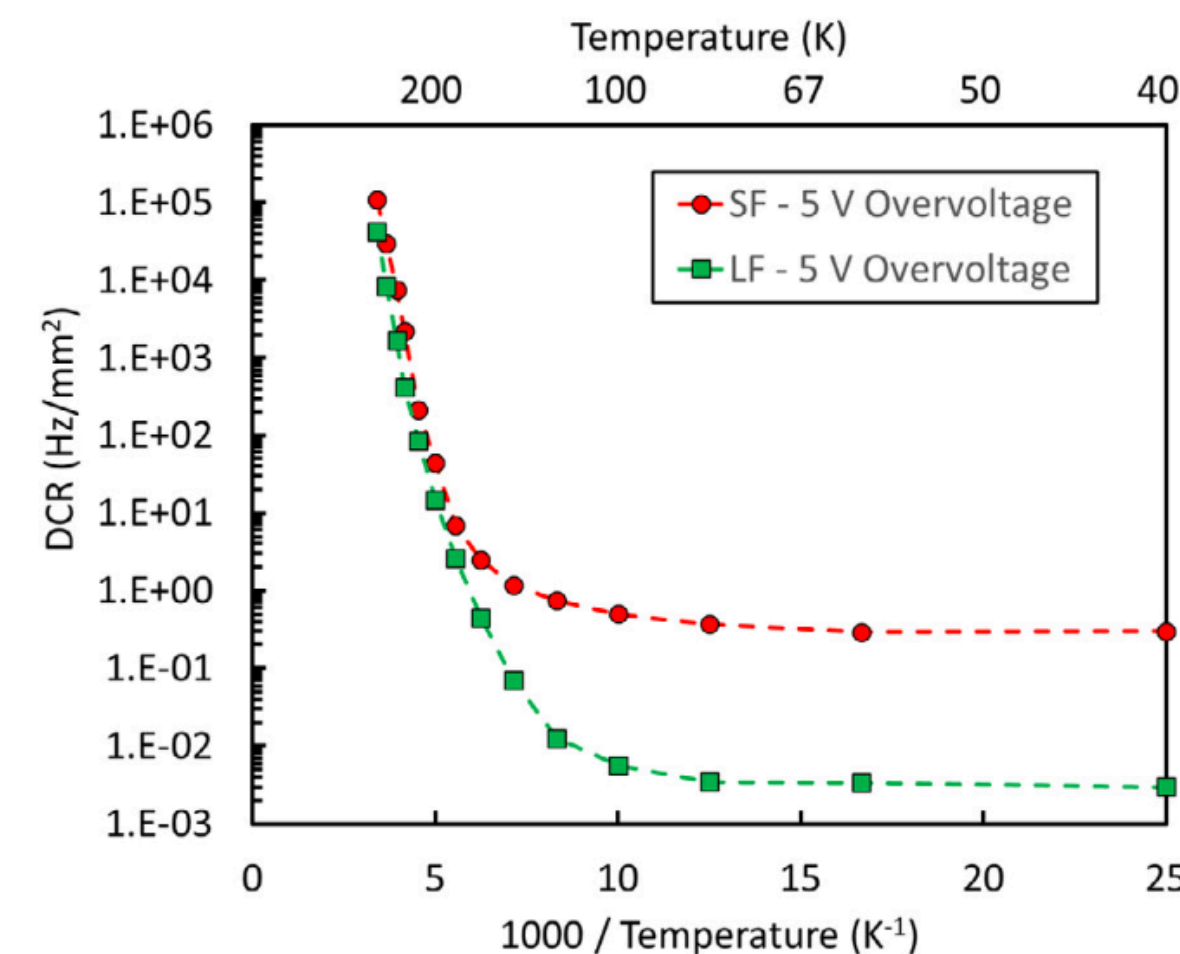
(Shockley-Read-Hall statistics), where trapping and de-trapping is increased by the high electric field in the junction. The

Generation rate can be written as:

$$G = \frac{n_i}{2 \cdot \cosh\left(\frac{E_0 - E_t}{kT}\right)} N_t \sigma v_{th} = \frac{n_i}{\tau_{g0}}$$

- E₀ = Fermi level
- E_t = trapping level
- n_i = intrinsic carrier concentration
- N_t = trapping concentration
- σ = trapping cross section
- v_{th} = thermal velocity

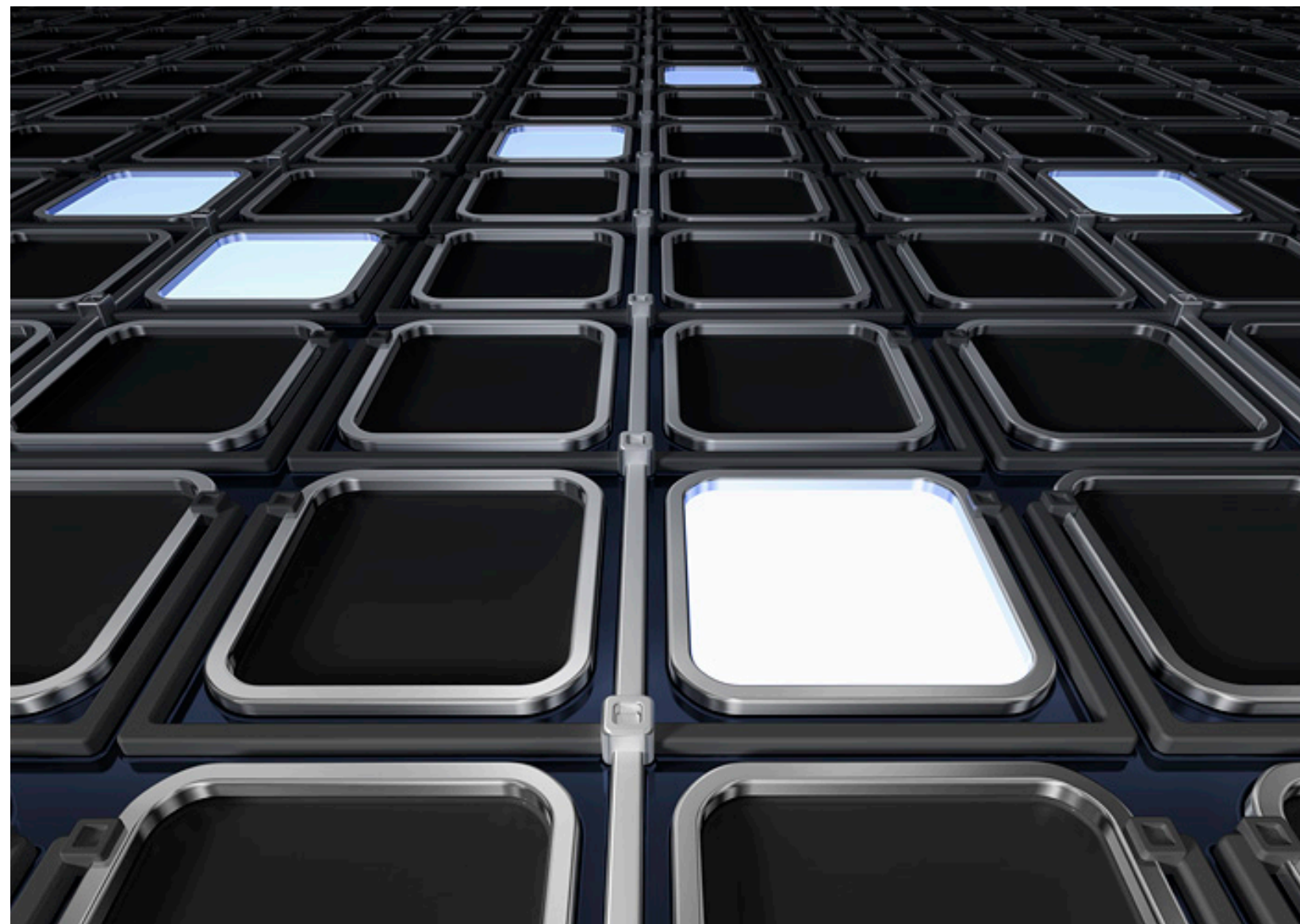
$$G = \frac{(1 + \Gamma) n_i}{\tau_{g0}} \quad \Gamma \text{ “boost” by the field}$$



F. Acerbi, et al., IEEE Trans. Electron Devices 64 (2) (2017) 521-526.

► a few notes :

b. The idea flashed as a genuine act of serendipity, while studying the properties of Dark Counts in Silicon Photomultipliers (SiPM)



► SiPM may be seen as a collection of binary cells, p-n junctions operated beyond the breakdown voltage [SPAD], fired when a photon is absorbed

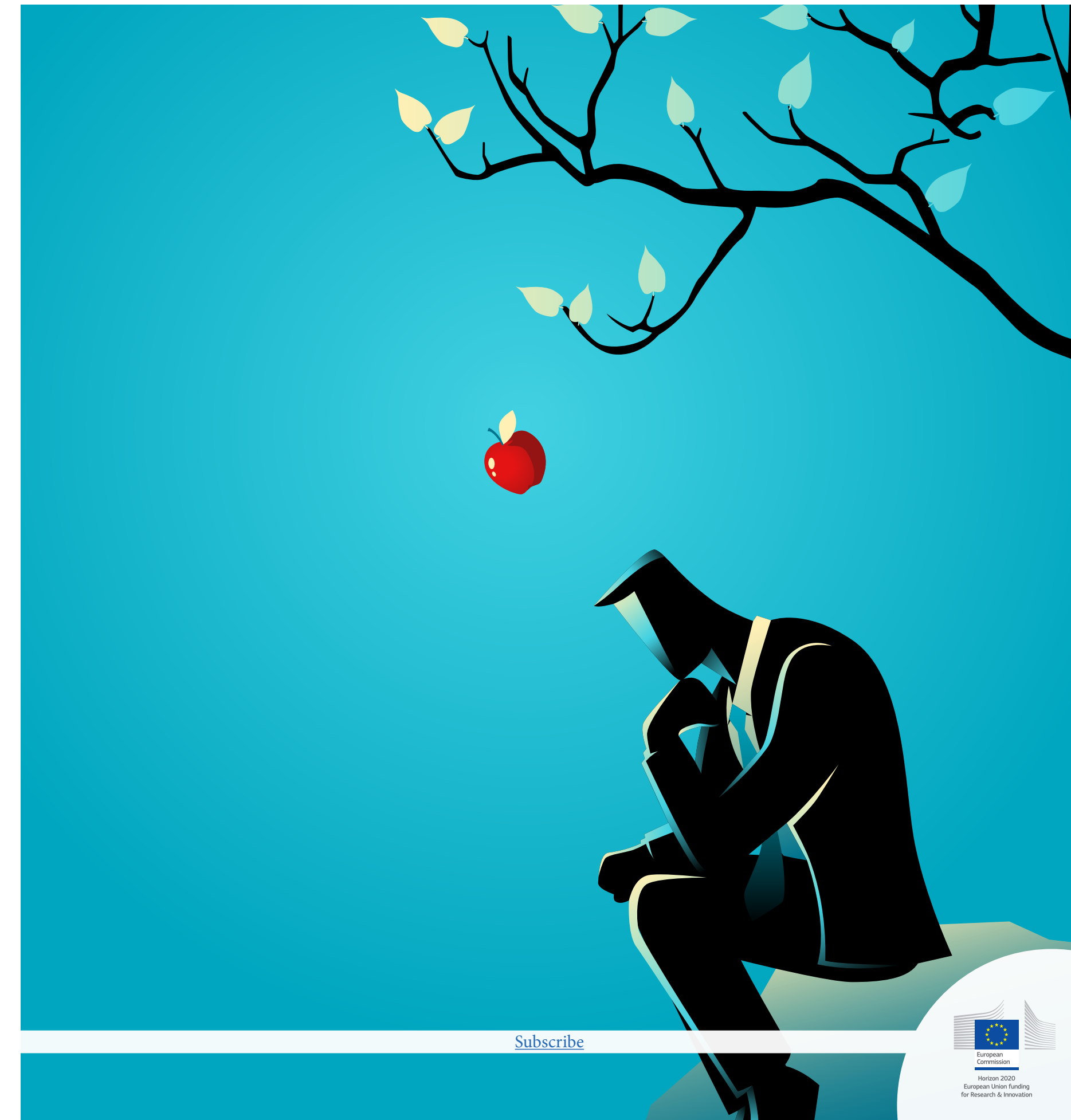
[in principle, a NATIVE DIGITAL DEVICE]



Impact:
73% breakthroughs/
major advances

Tales of serendipity

10th anniversary
celebrations continue

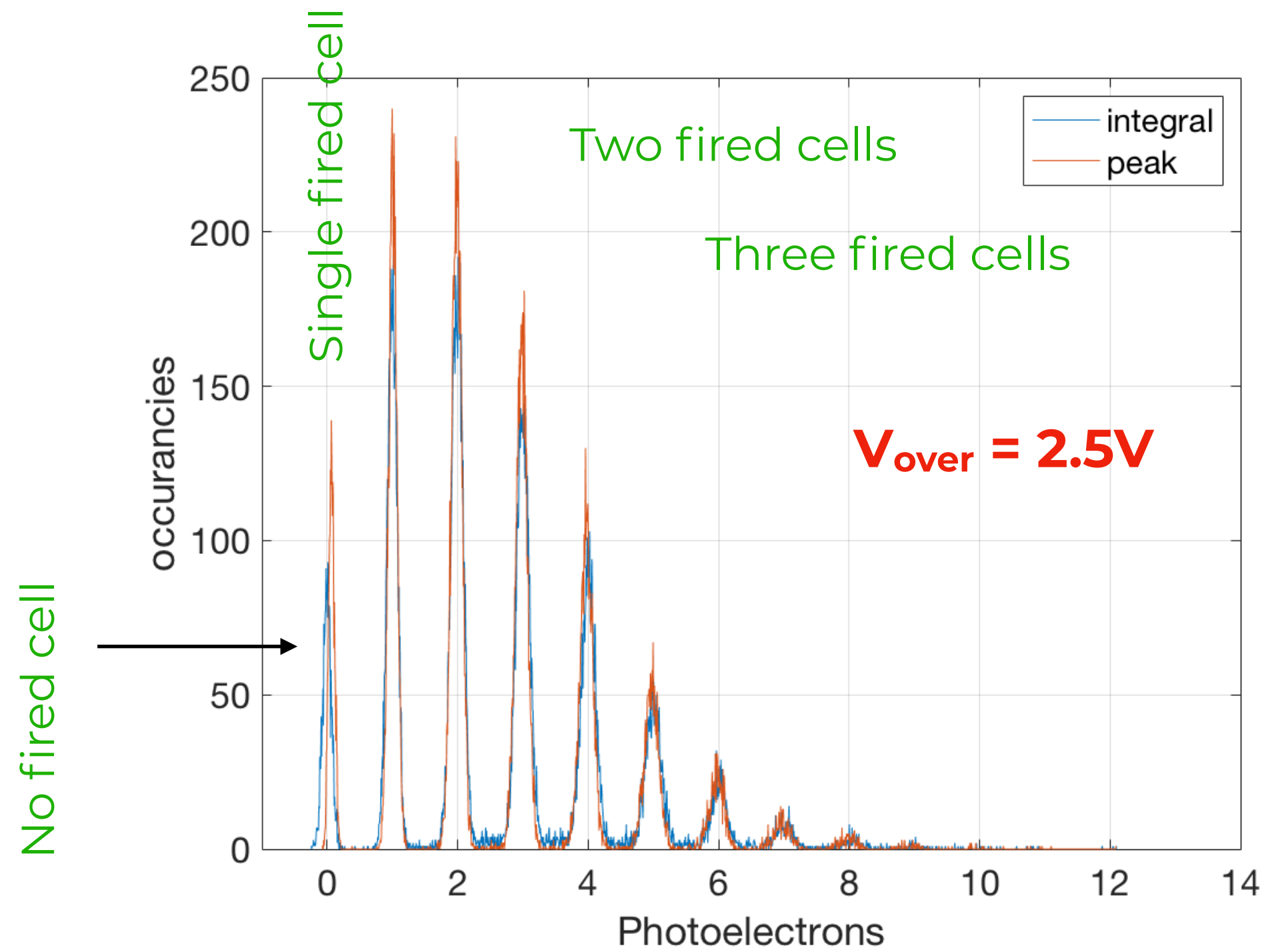


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► a few notes :

b. The idea flashed as a genuine act of serendipity, while studying the properties of Dark Counts in Silicon Photomultipliers (SiPM)



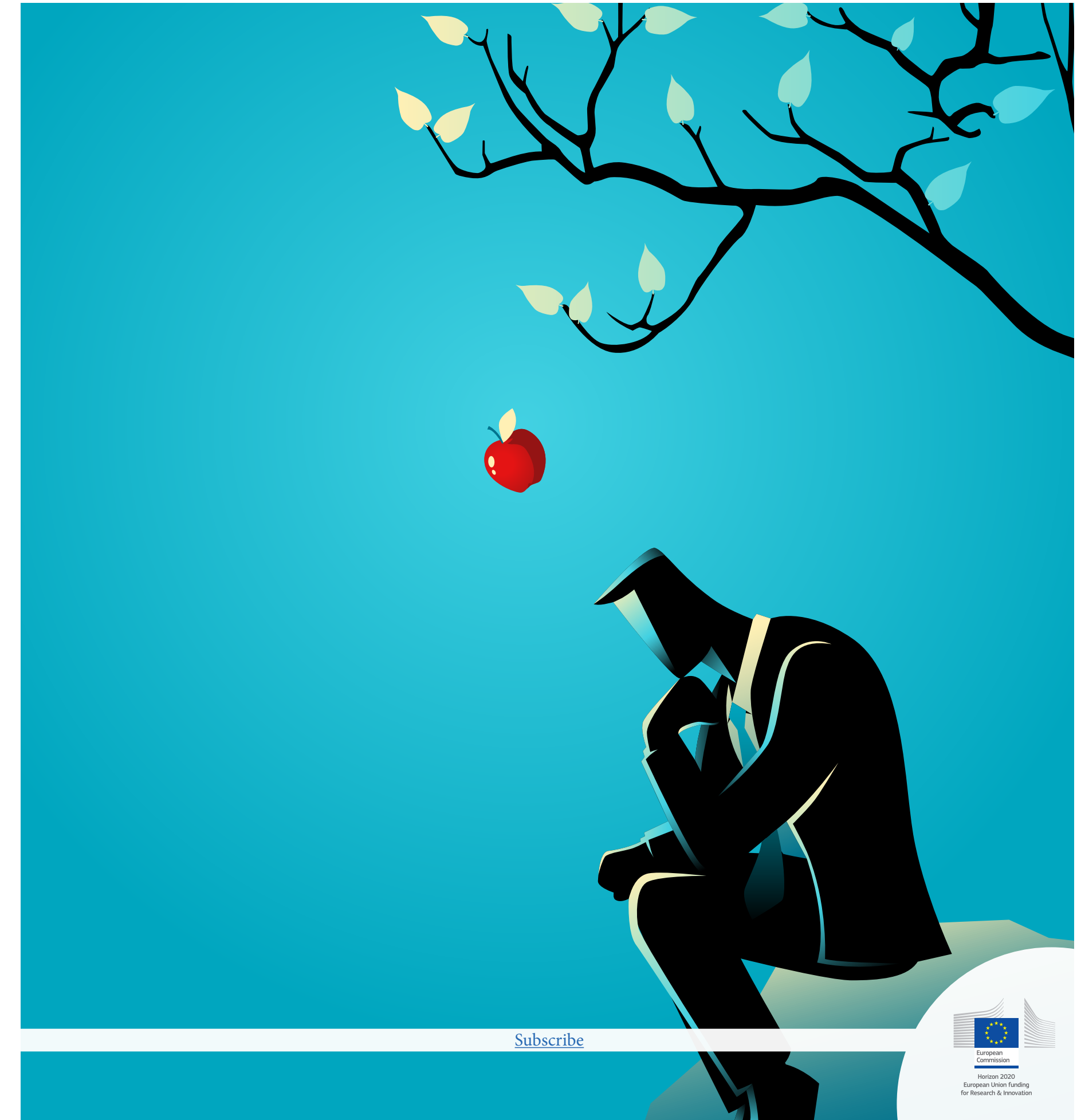
► histogram of the response to a high statistics of low intensity light pulses



Impact: 73% breakthroughs/major advances

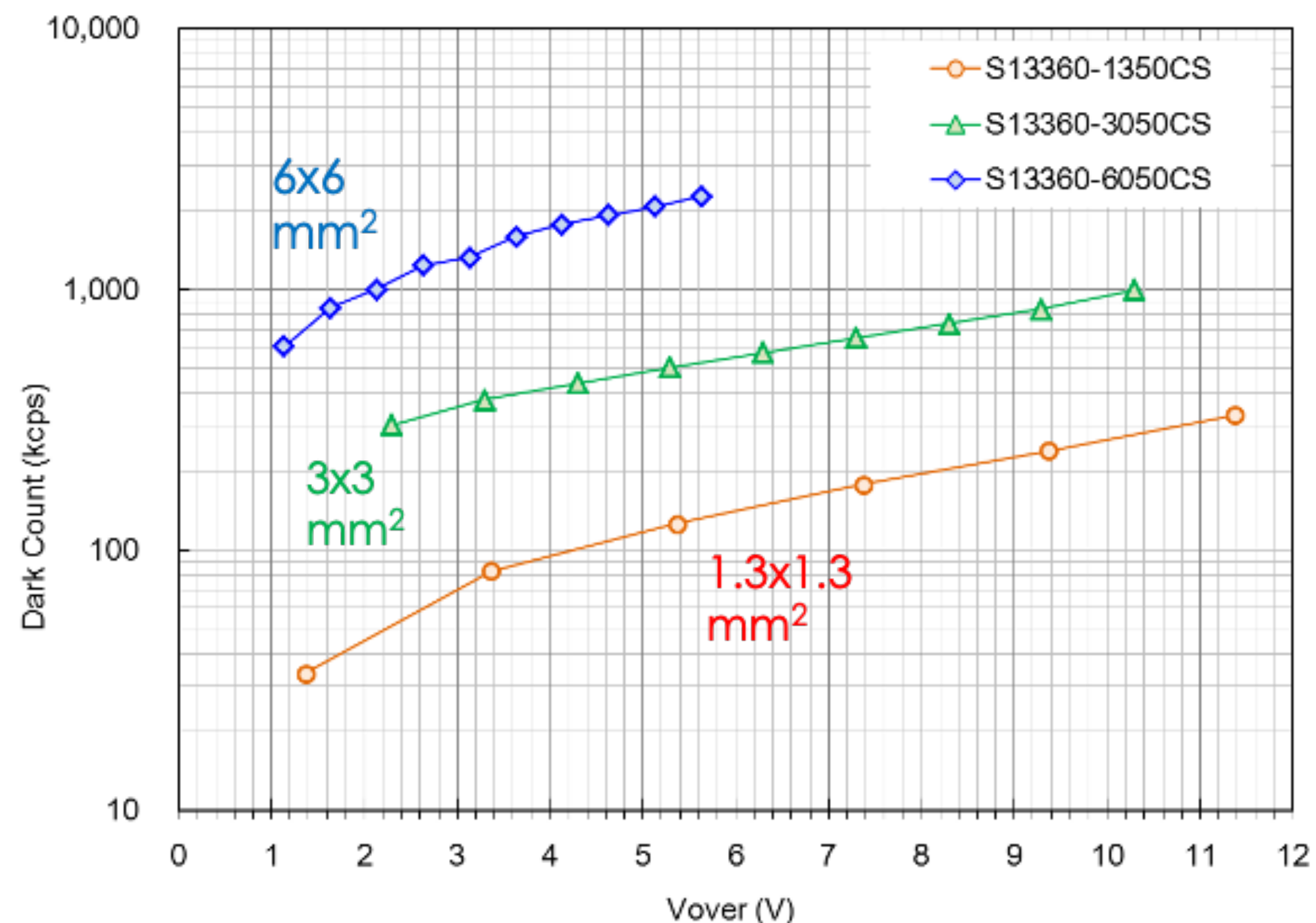
Tales of serendipity

10th anniversary celebrations continue



► a few notes:

b. The idea flashed as a genuine act of serendipity, while studying the properties of Dark Counts in Silicon Photomultipliers (SiPM)



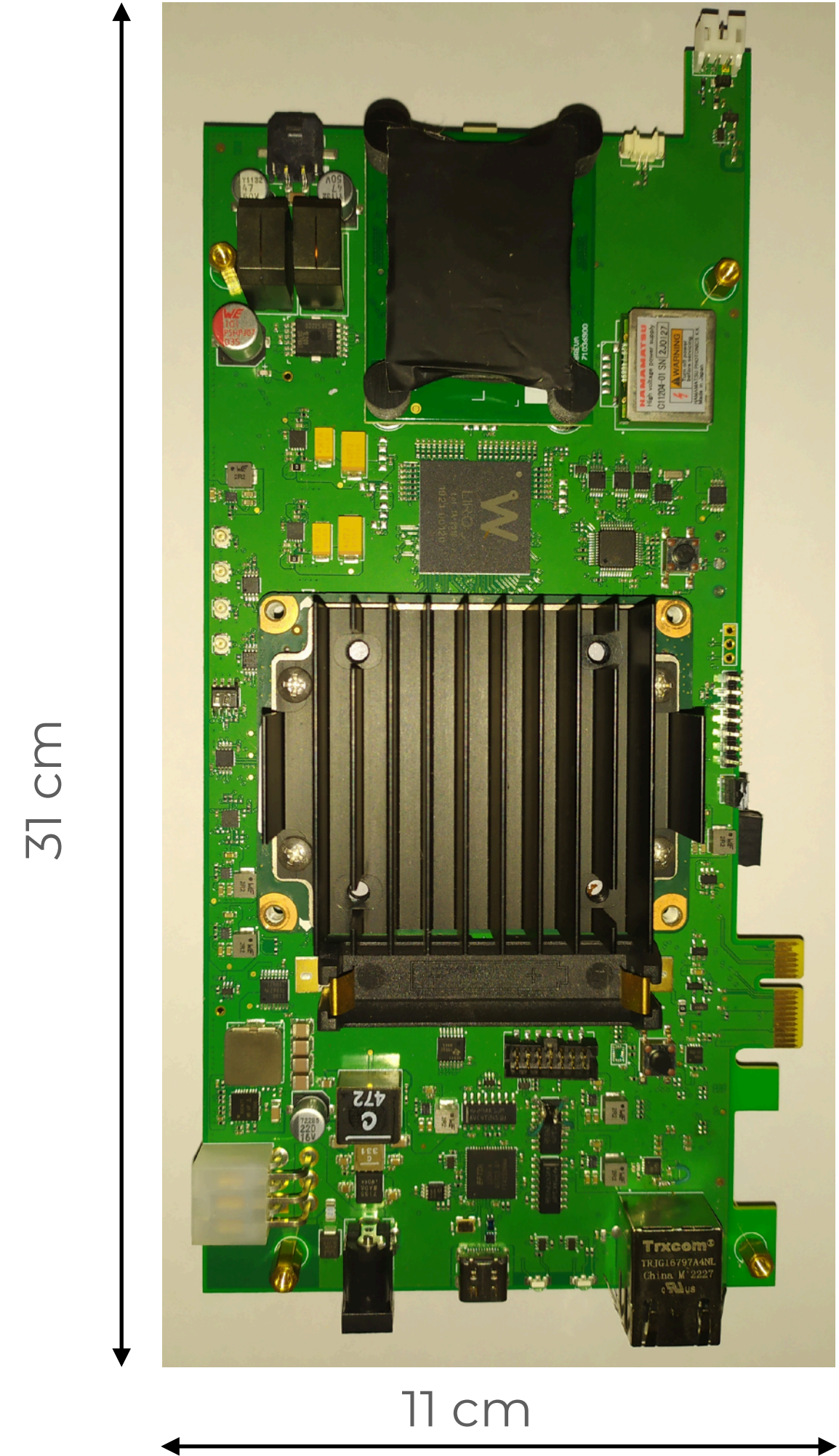
► Dependence of the Dark Count Rate on the Overvoltage (wrt Breakdown) in different HAMAMATSU SiPM

The newsletter cover features the ERC 10 years logo and the title 'ideas #3 AUTUMN 2017'. It highlights 'Impact: 73% breakthroughs/major advances', 'Tales of serendipity', and '10th anniversary celebrations continue'. The main illustration shows a silhouette of a person in a suit sitting on a rock, looking up at a red apple falling from a tree branch against a blue sky. At the bottom, there is a 'Subscribe' link and the European Commission logo.

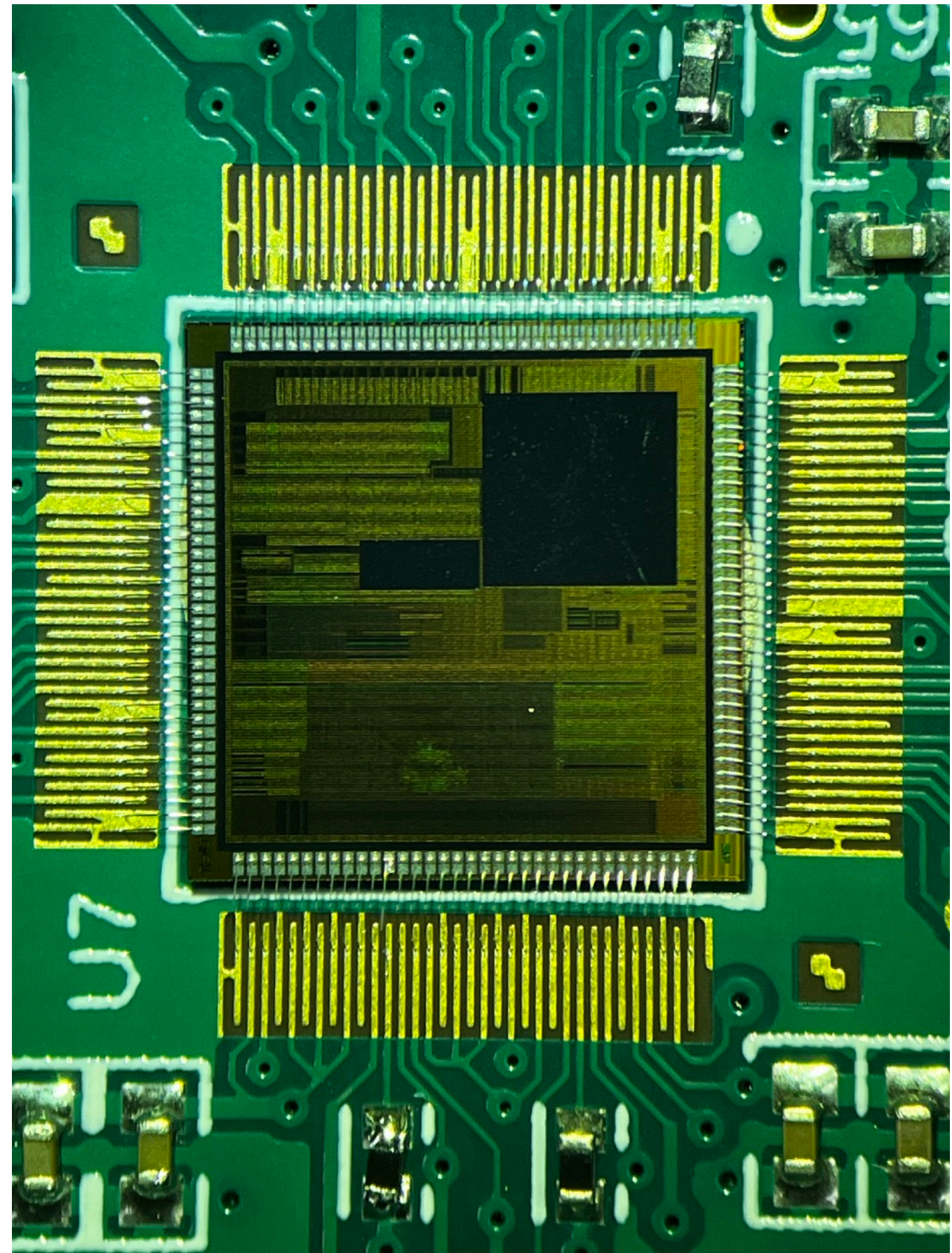
Three elements of the platform have been developed and will be **ready for the market by Q1 2025:**



A **single generator board**, for **qualification and the educational market**

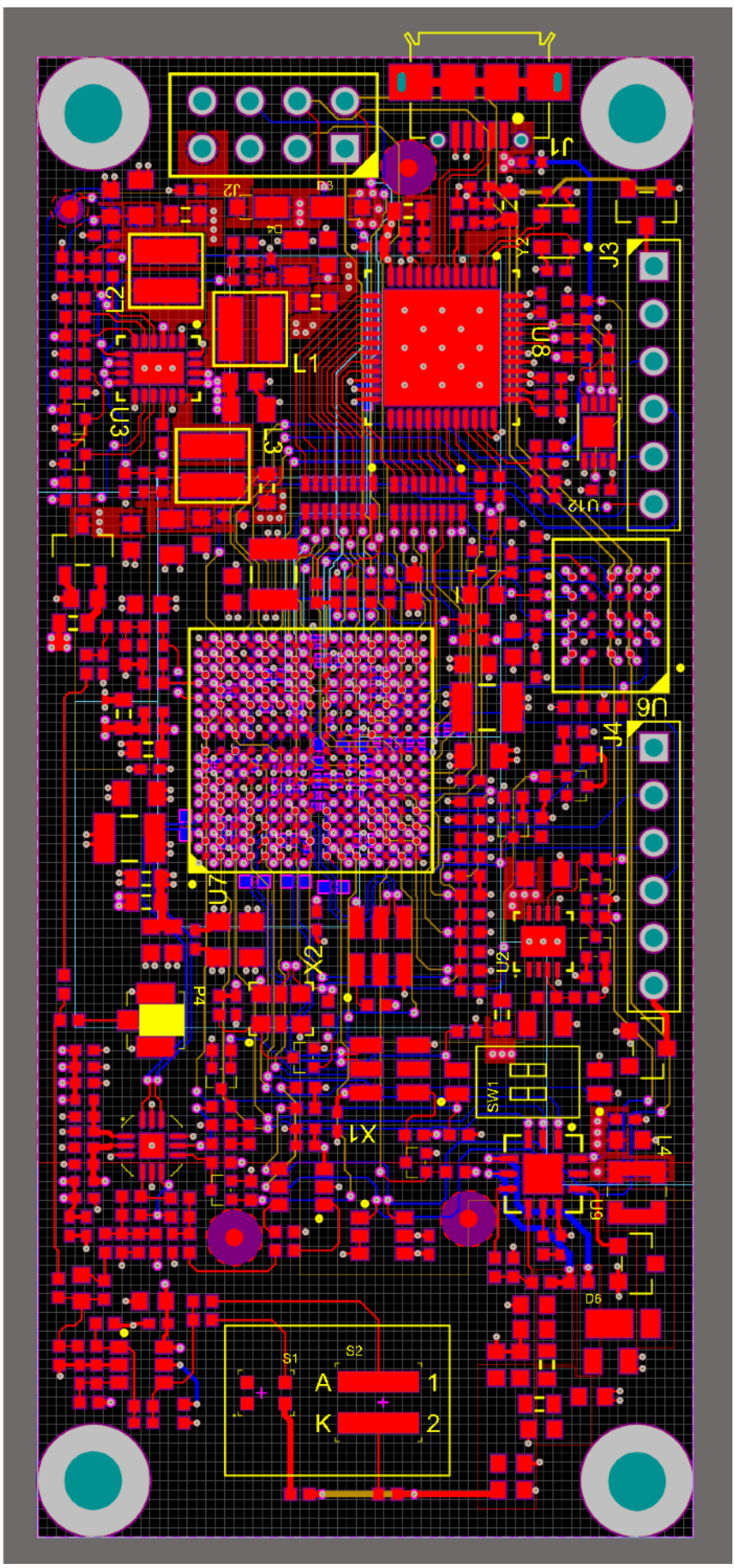


A **64 generator computer on a board**, for **Data Centers** (e.g. simulations & AI training)



A **full custom ASIC (a chip!)** for IoT, Authentication, gaming&gambling

THE SINGLE GENERATOR BOARD



Dimensions [cm²]	8x3.5
No. generators	1 array
Raw bit stream:	100 kbps
NIST DRBG output (SP800-90 A,B,C)	NA
Control:	Xilinx Spartan 7
I/O:	USB or bits-on-pin
Power supply:	through the USB (5V, 0.5A)
Power consumption:	<2.5W
Encryption of the bit stream:	No
Specific Features:	<ul style="list-style-type: none"> • Firmware implemented Real-Time sanity checks (MONOBIT and RUNS) • Auxiliary post-processing through a SHA256 function
State of development:	<ul style="list-style-type: none"> • Completed • Full qualification of 2 Tb through the NIST and TESTU01 protocols • Single board control through a GUI or mini-farm control implementing also the NIST DRBG procedure (SP800-90 A,B,C)

Main output of the

```

finalAnalysisReport_PART2.txt
RESULTS FOR THE UNIFORMITY OF P-VALUES AND THE PROPORTION OF PASSING SEQUENCES
generator is </Users/luca/Documents/Random_Power/ProgramAndTechnical/ATTRACT_Eu_Board_Fw8/
TestFW8_4BitNoReshape_1GB_Part2.bin>
-----
C1 C2 C3 C4 C5 C6 C7 C8 C9 C10 P-VALUE PROPORTION STATISTICAL TEST
-----
100 110 95 93 90 90 114 101 98 109 0.682823 986/1000 Frequency
97 102 94 103 107 97 105 106 102 87 0.941144 993/1000 BlockFrequency
95 95 101 100 113 106 93 100 89 108 0.842937 989/1000 CumulativeSums
94 112 117 90 93 91 89 96 123 95 0.125927 987/1000 CumulativeSums
100 93 91 112 93 112 99 110 101 89 0.647530 992/1000 Runs
105 91 96 80 121 99 85 100 107 116 0.092597 989/1000 LongestRun
100 104 89 110 97 88 126 84 99 103 0.148653 992/1000 Rank
95 109 103 113 85 94 90 100 106 105 0.630872 995/1000 FFT
104 98 91 89 104 90 110 104 115 95 0.632955 987/1000 NonOverlappingTemplate
111 93 112 88 96 95 100 101 106 98 0.798139 981/1000 NonOverlappingTemplate
111 100 93 94 101 109 93 87 117 95 0.514124 986/1000 NonOverlappingTemplate
86 94 119 101 107 98 93 103 98 101 0.626709 998/1000 NonOverlappingTemplate
93 112 93 103 91 89 94 99 115 111 0.498313 989/1000 NonOverlappingTemplate
84 106 101 109 86 119 111 96 94 94 0.249284 988/1000 NonOverlappingTemplate
114 92 98 96 105 105 101 100 83 106 0.682823 992/1000 NonOverlappingTemplate
117 87 98 101 100 106 91 94 105 101 0.697257 991/1000 NonOverlappingTemplate
90 93 97 107 99 89 100 116 108 101 0.689019 994/1000 NonOverlappingTemplate
99 108 98 99 116 104 98 85 96 97 0.743915 991/1000 NonOverlappingTemplate
88 93 103 101 112 94 111 99 100 99 0.829047 988/1000 NonOverlappingTemplate
96 97 103 103 106 108 114 97 93 83 0.651693 987/1000 NonOverlappingTemplate
108 95 97 109 84 94 101 101 91 120 0.388990 988/1000 NonOverlappingTemplate

```

series of tests on non-overlapping templates

```

80 98 115 100 98 115 107 91 83 113 0.106877 993/1000 OverlappingTemplate
86 116 121 101 91 87 96 101 87 114 0.084037 990/1000 Universal
97 90 107 116 110 95 103 93 92 97 0.668321 987/1000 ApproximateEntropy
70 62 54 60 55 66 60 63 77 65 0.668486 626/632 RandomExcursions
62 69 58 70 58 61 56 71 63 64 0.909311 626/632 RandomExcursions
60 53 59 62 76 72 60 59 66 65 0.681642 620/632 RandomExcursions
70 64 83 45 62 69 70 65 51 53 0.040275 622/632 RandomExcursions
66 69 69 73 73 73 38 49 52 70 0.009611 627/632 RandomExcursions
65 52 67 82 68 54 51 63 72 58 0.136536 627/632 RandomExcursions
61 55 60 72 66 71 67 56 55 69 0.711017 626/632 RandomExcursions
47 61 62 58 71 63 71 61 68 70 0.553450 625/632 RandomExcursions
60 57 66 62 58 61 67 67 73 61 0.941564 624/632 RandomExcursionsVariant
60 70 43 60 64 58 58 88 64 67 0.030676 622/632 RandomExcursionsVariant
66 58 51 65 51 61 72 72 71 65 0.447593 624/632 RandomExcursionsVariant
63 67 59 46 67 60 68 70 73 59 0.483876 623/632 RandomExcursionsVariant
61 67 58 69 63 74 48 60 66 66 0.615645 624/632 RandomExcursionsVariant
75 62 63 58 63 55 66 54 71 65 0.717488 624/632 RandomExcursionsVariant
68 63 66 54 57 65 63 67 56 73 0.827336 620/632 RandomExcursionsVariant
75 54 64 57 65 64 56 62 64 71 0.733547 623/632 RandomExcursionsVariant
76 68 70 56 55 50 66 52 64 75 0.176734 624/632 RandomExcursionsVariant
89 63 57 59 59 55 58 68 63 61 0.134074 624/632 RandomExcursionsVariant
67 68 61 57 60 69 66 63 63 58 0.979797 624/632 RandomExcursionsVariant
65 64 62 71 58 68 67 53 60 64 0.917568 626/632 RandomExcursionsVariant
71 58 56 62 75 62 67 64 53 64 0.701268 626/632 RandomExcursionsVariant
64 71 49 62 61 69 69 59 59 69 0.694743 626/632 RandomExcursionsVariant
61 65 54 59 63 63 64 76 62 65 0.879806 626/632 RandomExcursionsVariant
58 55 57 67 65 66 54 66 76 68 0.642077 629/632 RandomExcursionsVariant
46 64 65 61 64 61 81 59 75 56 0.150772 624/632 RandomExcursionsVariant
50 56 65 67 74 67 51 63 73 66 0.353061 629/632 RandomExcursionsVariant
106 107 87 107 94 109 100 83 92 115 0.352107 989/1000 Serial
105 100 94 98 96 95 96 101 95 120 0.790621 991/1000 Serial
105 97 89 101 96 106 92 112 105 97 0.875539 991/1000 LinearComplexity

```

The minimum pass rate for each statistical test with the exception of the random excursion (variant) test is approximately = 980 for a sample size = 1000 binary sequences.
The minimum pass rate for the random excursion (variant) test is approximately = 618 for a sample size = 632 binary sequences.
For further guidelines construct a probability table using the MAPLE program provided in the addendum section of the documentation.

▶ A proto-randomness farm based on 10 boards have been collecting about 1.5 Tb, qualified through the NIST and TESTU01 suites.

Results show that the stream looks extremely “white”, essentially with no failures on the raw data beside what can be statistically expected.

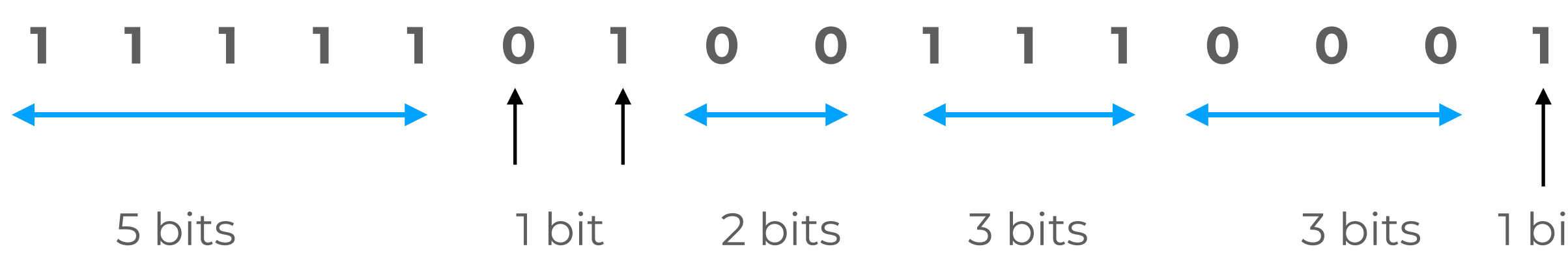
▶ A SHA256 vetted conditioning function firmware implemented

▶ Two tests have been implemented in firmware to guarantee real-time sanity checks:

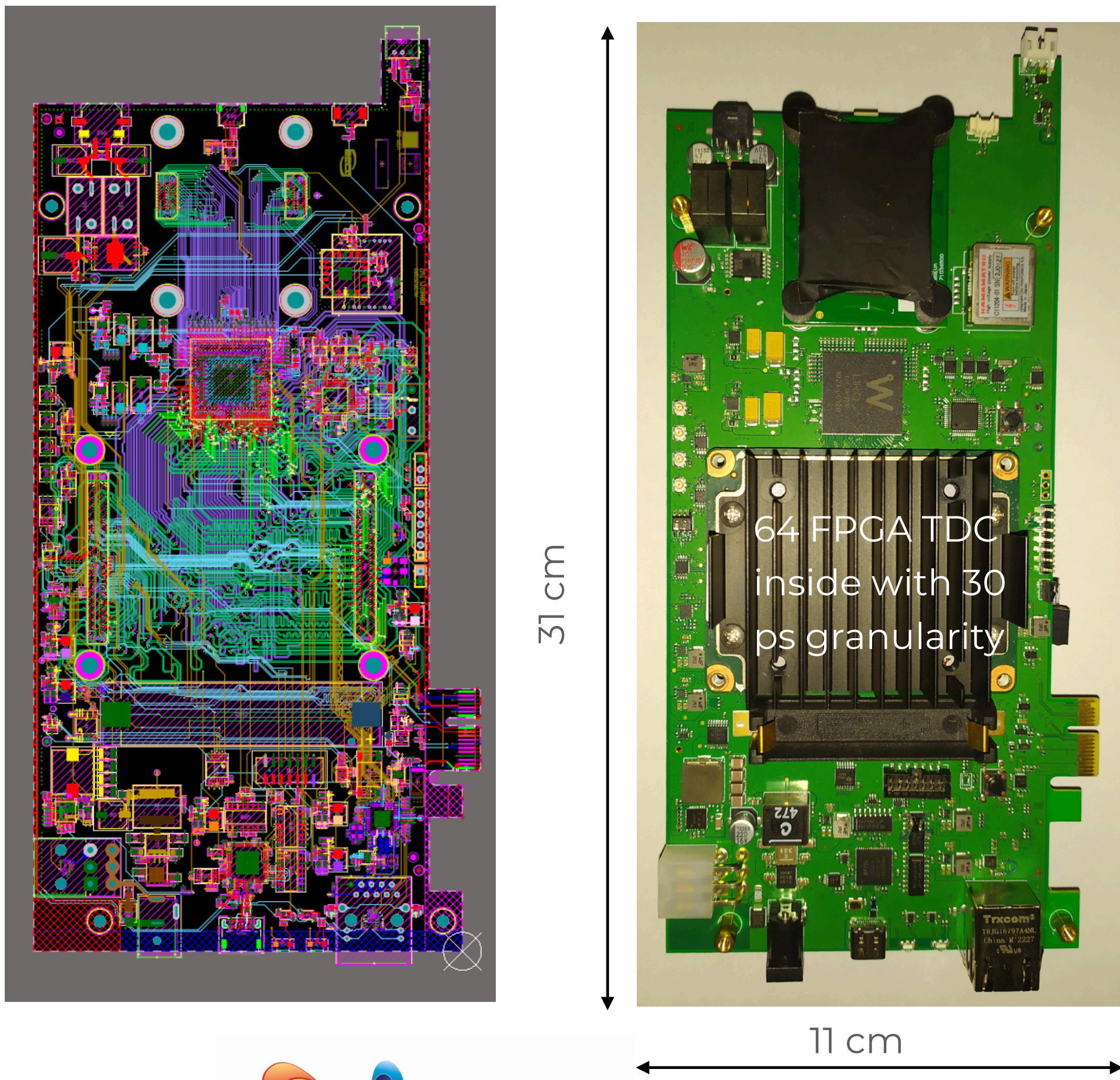
* **MONOBIT**: essentially testing the asymmetries between 0’s and 1’s in a bit string:



* **RUNS**: testing the statistics of the number of sequences of identical bits in a string



THE 64 GENERATORS BOARD



Dimensions [cm²]	11.1x31.2x2.0
No. generators	64 arrays
Raw bit stream:	32 Mbps
NIST DRBG output (SP800-90 A,B,C)	1 Gbps
Control:	Xilinx KRIA K26 SOM
I/O:	Eth or PCI-Express
Power supply:	12V, 8A
Power consumption:	20W
Encryption of the bit stream:	Yes (AES-256)
Specific Features:	<ul style="list-style-type: none"> • Firmware implemented Real-Time sanity checks (MONOBIT, RUNS, Adaptive proportion test, Repetition Count Test) • Auxiliary post-processing through a SHA256 function • Interface through the Trusted Execution Environment • Temperature control through a Peltier cooler • FIPS-140-3 compliant by design
State of development:	<ul style="list-style-type: none"> ▶ v1.0 delivered in July 2023, qualified ▶ v2.0, product grade, delivered in September 2024, being qualified ▶ software architecture under development

Goal of the



Phase 2 project (May 2022-Fall.2023)



BEYOND A PURE TRUE RANDOM NUMBER GENERATOR (TRNG)

NIST Special Publication 800-90B

Recommendation for the Entropy Sources Used for Random Bit Generation

How to design and test entropy sources to be used to feed Deterministic Random Bit Generators (DRBG)

NIST Special Publication 800-90A
Revision 1

Recommendation for Random Number Generation Using Deterministic Random Bit Generators

Approved DRBG mechanisms

1 (Second Draft) NIST Special Publication 800-90C

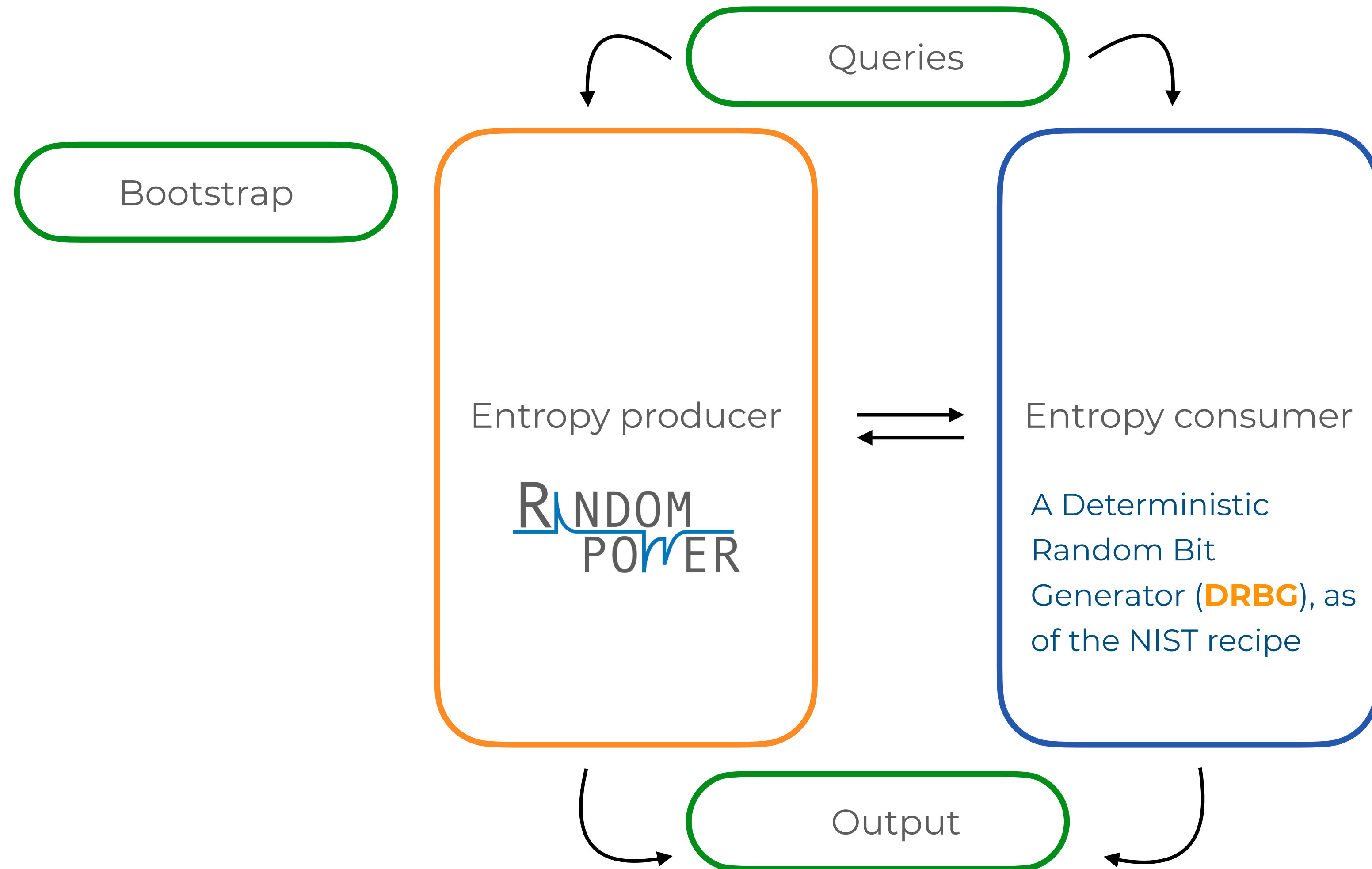
2
3
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7

Recommendation for Random Bit Generator (RBG) Constructions

Construction of RBG from A+B

- * pre-requisites for entering the programs eventually leading to the FIPS-140-3 certification
- * impacting on the design of both the ASIC, the multiple generator board and its embodiment in a “system”

GO BEYOND A PURE TRUE RANDOM NUMBER GENERATOR (TRNG)



* Essentially, the True Random Bits generated by Random Power are used to seed a NIST approved Pseudo Random Bit Generator

* when reseeding occurs after EVERY iteration of the Deterministic machine, you obtain the highest level of security, namely **Prediction Resistance***

* QUOTING NIST: Prediction resistance means that a compromise of the DRBG internal state has no effect on the security of future DRBG outputs.

BEYOND A PURE TRUE RANDOM NUMBER GENERATOR (TRNG)

Why this is done? in principle, the majority of the randomness tests qualify the stream against modelled pitfalls but you cannot exclude a priori unknown deviations.

“Universal tests” have been proposed, connected to “compression” algorithms but even Maurer’s test, the most widely known, in its practical implementation can possibly have a reduced diagnostics power:

J. Cryptology (1992) 5: 89–105

Journal of Cryptology
© 1992 International Association for
Cryptologic Research

A Universal Statistical Test for Random Bit Generators*

Ueli M. Maurer

Institute for Theoretical Computer Science, ETH Zürich,
CH-8092 Zürich, Switzerland

Communicated by Rainer A. Rueppel

Received 2 April 1990 and revised 23 June 1991

Abstract. A new statistical test for random bit generators is presented which, in contrast to presently used statistical tests, is universal in the sense that it can detect any significant deviation of a device’s output statistics from the statistics of a truly random bit source when the device can be modeled as an ergodic stationary source with finite memory but arbitrary (unknown) state transition probabilities. The test parameter is closely related to the device’s per-bit entropy which is shown to be the correct quality measure for a secret-key source in a cryptographic application. The test hence measures the cryptographic badness of a device’s possible defect. The test is easy to implement and very fast and thus well suited for practical applications. A sample program listing is provided.

AN ACCURATE EVALUATION OF MAURER’S UNIVERSAL TEST

Jean-Sébastien Coron

Ecole Normale Supérieure
45 rue d’Ulm
Paris, F-75230, France
coron@clipper.ens.fr

David Naccache

Gemplus Card International
34 rue Guynemer
Issy-les-Moulineaux, F-92447, France
naccache@compuserve.com

Abstract. Maurer’s universal test is a very common randomness test, capable of detecting a wide gamut of statistical defects. The algorithm is simple (a few Java code lines), flexible (a variety of parameter combinations can be chosen by the tester) and fast.

Although the test is based on sound probabilistic grounds, one of its crucial parts uses the heuristic approximation :

$$c(L, K) \cong 0.7 - \frac{0.8}{L} + \left(1.6 + \frac{12.8}{L}\right) K^{-4/L}$$

In this work we compute the precise value of $c(L, K)$ and show that the inaccuracy due to the heuristic estimate can make the test 2.67 times more permissive than what is theoretically admitted.

BEYOND A PURE TRUE RANDOM NUMBER GENERATOR (TRNG)

Why this is done? in principle, the majority of the randomness tests qualify the stream against modelled pitfalls but you cannot exclude a priori unknown deviations.

On the other hand, if you can mathematically prove the strength of an algorithm, you can feel relieved. **Maybe:**

Security Analysis of NIST CTR-DRBG

Viet Tung Hoang¹ and Yaobin Shen²

¹ Dept. of Computer Science, Florida State University

² Dept. of Computer Science & Engineering, Shanghai Jiao Tong University, China


Abstract. We study the security of CTR-DRBG, one of NIST’s recommended Pseudorandom Number Generator (PRNG) designs. Recently, Woodage and Shumow (Eurocrypt’ 19), and then Cohn et al. (S&P’ 20) point out some potential vulnerabilities in both NIST specification and common implementations of CTR-DRBG. While these researchers do suggest counter-measures, the security of the patched CTR-DRBG is still questionable. Our work fills this gap, proving that CTR-DRBG satisfies the robustness notion of Dodis et al. (CCS’13), the standard security goal for PRNGs.

An Analysis of the NIST SP 800-90A Standard

Joanne Woodage¹, Dan Shumow²

¹Royal Holloway, University of London
² Microsoft Research

Abstract. We investigate the security properties of the three deterministic random bit generator (DRBG) mechanisms in the NIST SP 800-90A standard [2]. This standard received a considerable amount of negative attention, due to the controversy surrounding the now retracted DualEC-DRBG, which was included in earlier versions. Perhaps because of the attention paid to the DualEC, the other algorithms in the standard have received surprisingly patchy analysis to date, despite widespread deployment. This paper addresses a number of these gaps in analysis, with a particular focus on HASH-DRBG and HMAC-DRBG. We uncover a mix of positive and less positive results. On the positive side, we prove (with a caveat) the robustness [16] of HASH-DRBG and HMAC-DRBG in the random oracle model (ROM). Regarding the caveat, we show that if an optional input is omitted, then – contrary to claims in the standard — HMAC-DRBG does not even achieve the (weaker) property of forward security. We also conduct a more informal and practice-oriented exploration of flexibility in implementation choices permitted by the standard. Specifically, we argue that these DRBGs have the property that partial state leakage may lead security to break down in unexpected ways. We highlight implementation choices allowed by the overly flexible standard that exacerbate both the likelihood, and impact, of such attacks. While our attacks are theoretical, an analysis of two open source implementations of CTR-DRBG shows that potentially problematic implementation choices are made in the real world.



EMV-SWG-NC62r3

EMVCo Position Statement on
The Alleged backdoor in a NIST Random Number Generator (Dual EC DRBG)

January 2014

This paper provides the EMVCo position regarding an alleged backdoor in the NIST Dual Elliptic Curve Deterministic Random Bit Generator (Dual EC-DRBG).

Background

Recent allegations arising from Snowden-NSA disclosures are in fact a re-surfacing of publicly aired concerns dating back to 2007 regarding a random number generator being standardised by NIST, ANSI and ISO. This random number generator uses elliptic curve cryptography to produce an output sequence of pseudo random bits. However researchers showed that anyone knowing the inverse of one of the ECC parameters of the generator and also knowing just 32 bytes of the generator's output will be able to determine the secret internal state of the generator and thus be able to predict all the generator's output bits.

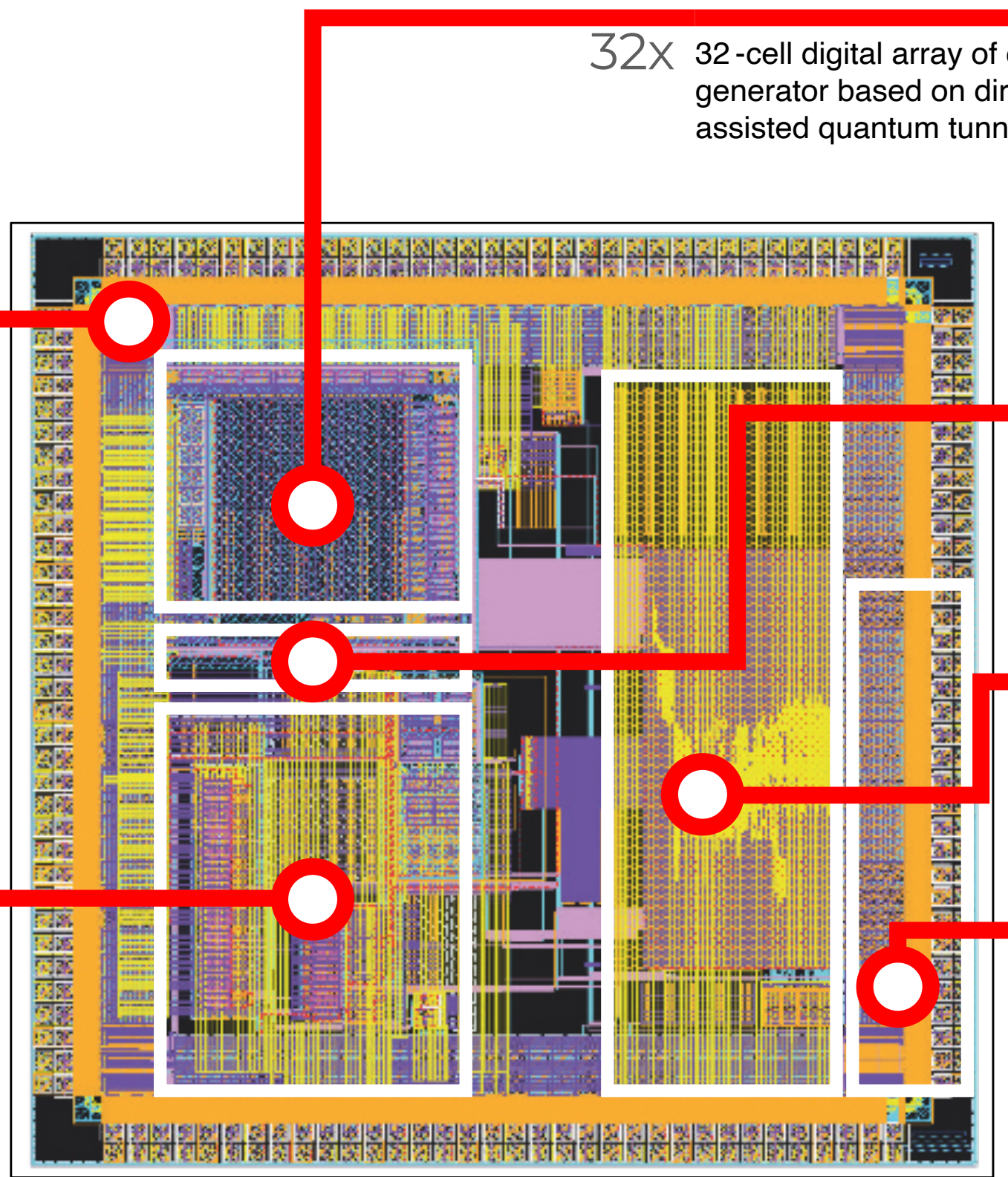
Thus the security of the Dual EC-DRBG rests on the secrecy of the inverse of the ECC parameter. NIST, ANSI and ISO Standards specify the use of a parameter originating from the NSA and the allegations are that the NSA knows its inverse. Note that in the NIST, ANSI and ISO Standards the Dual EC-DRBG is just one of multiple ways of generating random bits.

THE ASIC:

Authentication at 3 levels, starting by a Silicon embedded primary key and a Key Derivation Function

High-resolution sub-nanosecond-level time to digital converters with near-zero dead time. Logic for the patented random bit generation

On-chip secure eFuses for key storage



Dimensions [cm²]	1x1
No. generators	1 array
Raw bit stream:	2-8 Mbps
NIST DRBG output (SP800-90 A,B,C)	32 Mbps
Control:	SPI at 24 MHz
I/O:	SPI at 24 MHz
Power supply:	5V, 1.8V
Power consumption:	100 mW
Encryption of the bit stream:	Yes (AES-256)

- Specific Features:**
- On Silicon implementation of the NIST Real-Time sanity checks (Adaptive Proportion Test and Repetition Count Test)
 - On Silicon implementation of the NIST DRBG protocol
 - Package: QFN100
 - FIPS 140-3 compliancy by design;
 - CAVP (Cryptographic Algorithm Validation Program) granted

- ▶ Out-of-the fab in June 2024, result of an engineering run
- ▶ Full qualification close to completion

THE ASIC:

On-chip secure eFuses for key storage

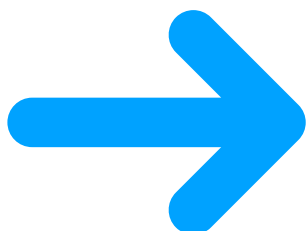
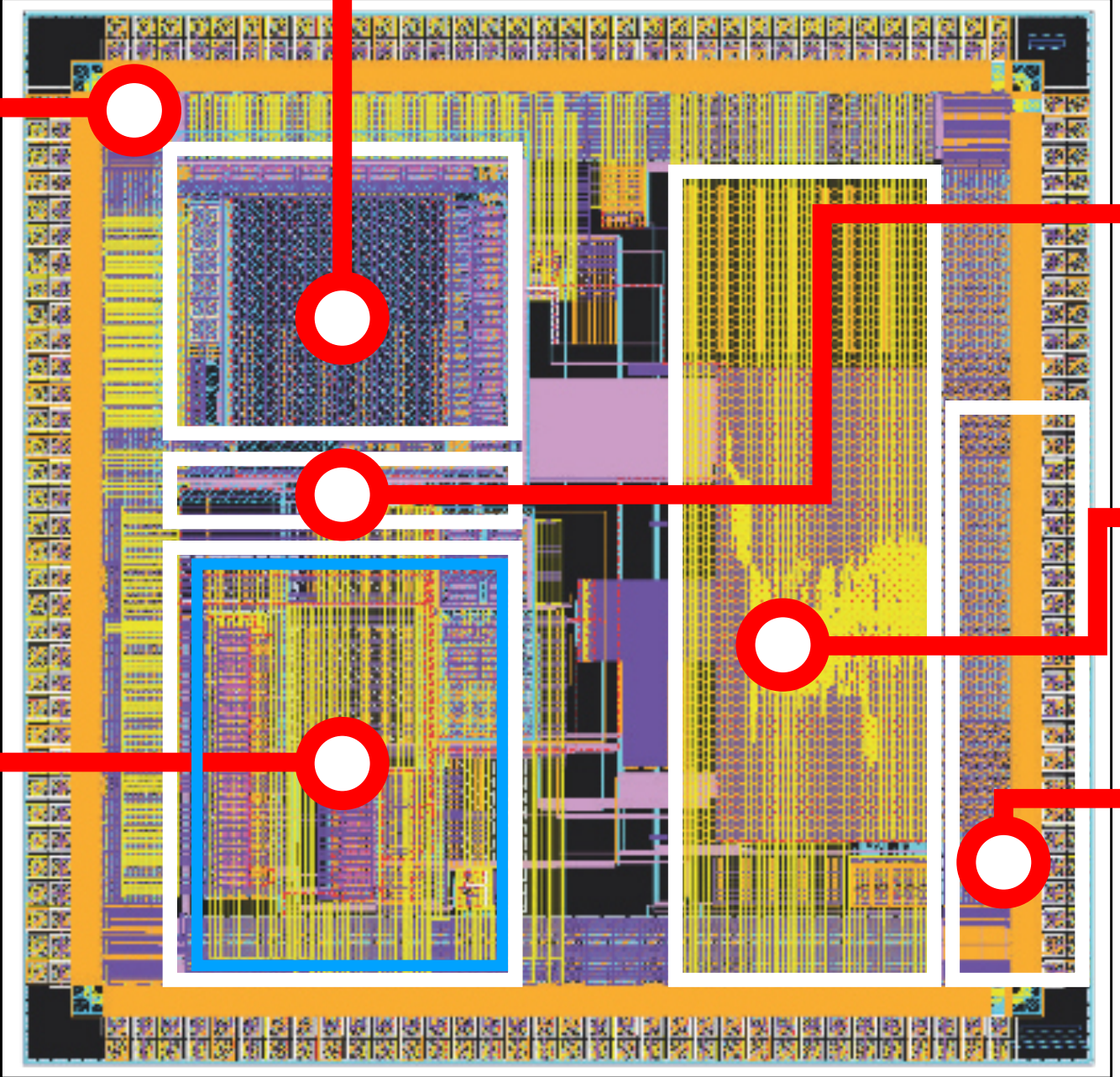
High-resolution sub-nanosecond-level time to digital converters with near-zero dead time. Logic for the patented random bit generation

32x 32-cell digital array of quantum entropy generator based on direct and trap assisted quantum tunneling

High-throughput streaming of the pulses to the readout electronics

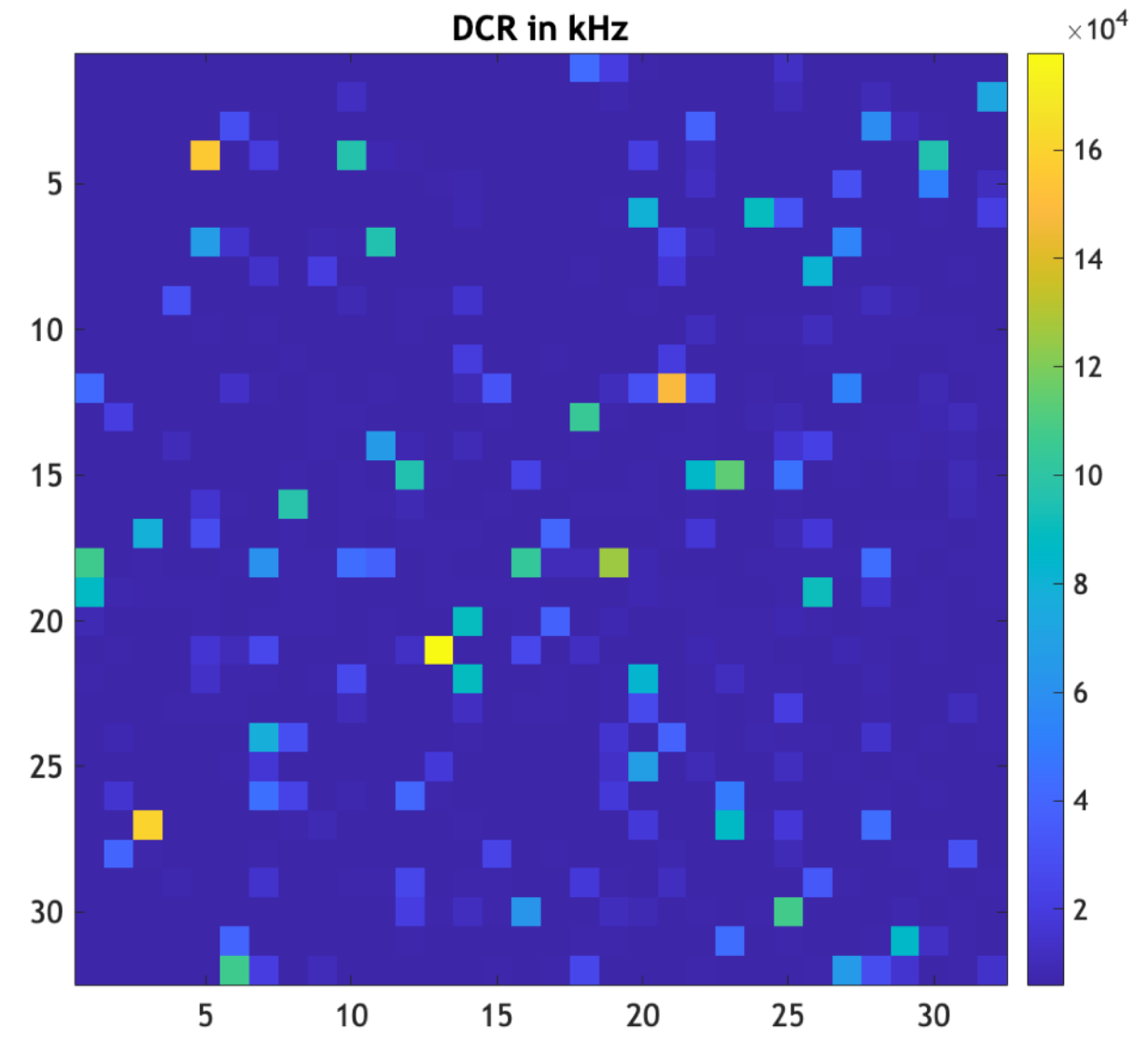
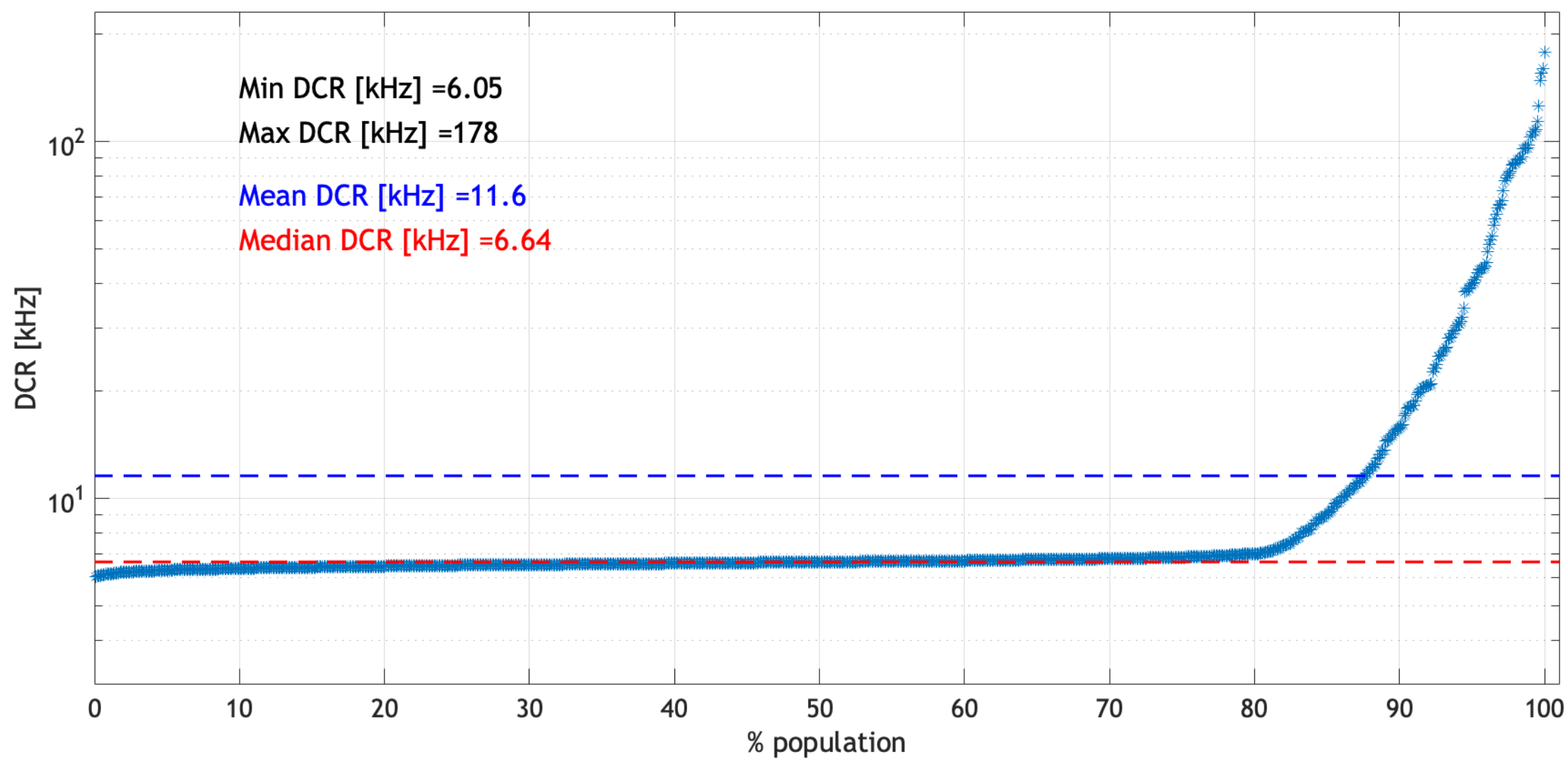
FIPS compliant DRGB, realtime AES256 bitstream encryption

2x24 MHz SPI Interface for easy integration with any commercial SoC, CPU, Microcontroller and FPGA



It embodies also:

- * two different TDC architectures
- * a two stage mechanism to implement “screamers identification” and a procedure for the rate stabilisation:



Beside hardware:



▶ how did we do it?

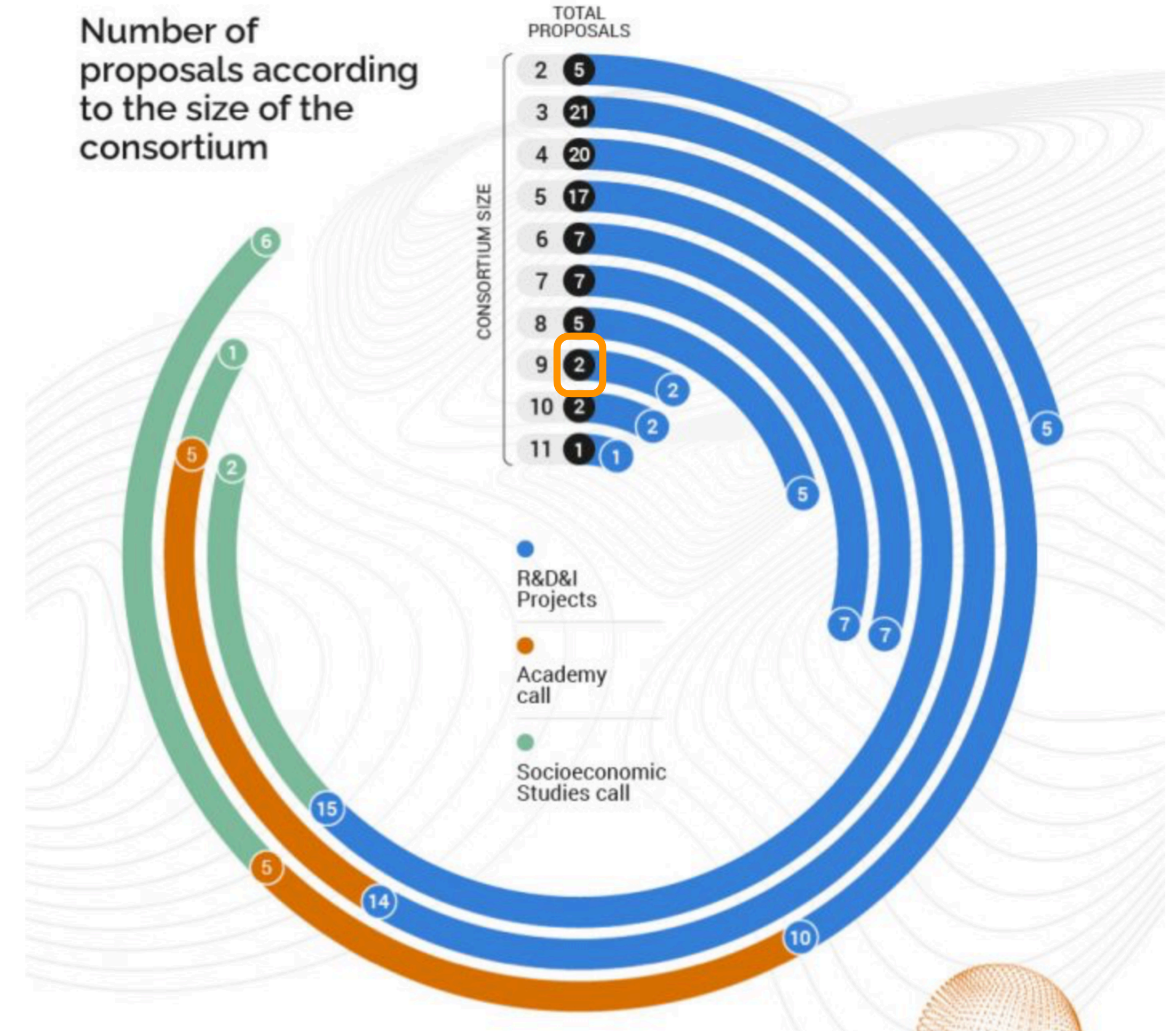
Essentially, Thanks to the EC



Our consortium:



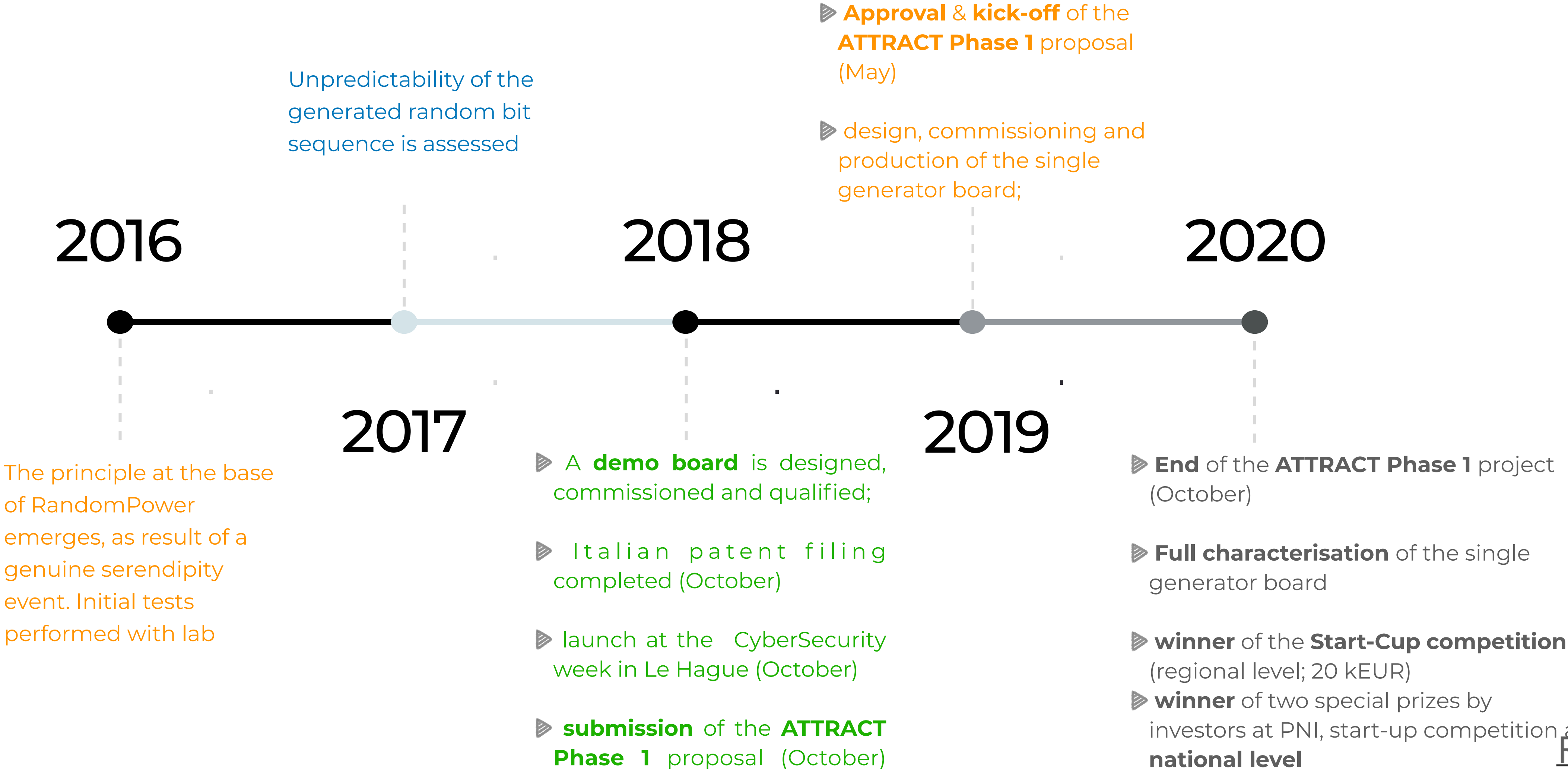
leading party



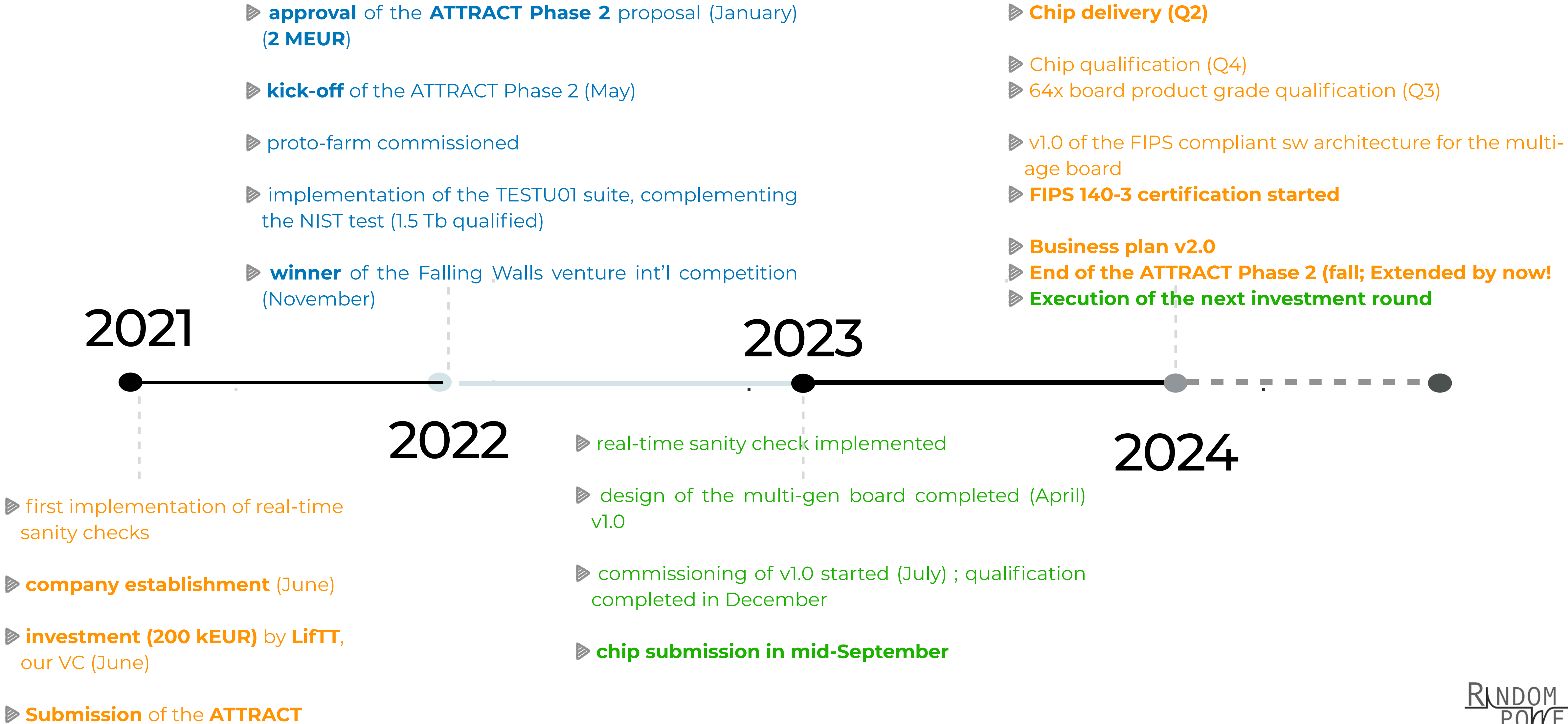
18 man-years dedicated to the project



HISTORY & TEAM: pre-incorporation



HISTORY & TEAM: post-incorporation (2021)





Join us, we will be happy to walk with you!

RANDOM POWER

www.randompower.eu

Established in June 2021



This project has received funding from the ATTRACT project funded by the EC under Grant Agreement 777222



2020-10 Winner - ICT

2020-11 Winner of 2 "special prizes"



2021-06 PoC investment by LifTT, a VC located in Torino (ITALY)

2022-11 winner @the Falling Walls venture competition for curious people: [here](#) & [and there](#)

I AM A FALLING WALLS WINNER



embeddedworld
Exhibition&Conference

2024-03 Random Power goes to the most important trade fair on IoT technologies, hosted at the SECO booth.