# Precision Measurements of Weak Interaction Parameters

CKM and CP Violation at Belle and Belle II

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BCVSPIN 2024 "Particle Physics and Cosmology in the Himalayas" December 9 - 13, 2024

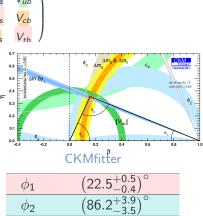
#### **CKM MATRIX & UNITARITY TRIANGLE**

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ts} \\ V_{cd} & V_{cs} & V_{ts} \\ V_{td} & V_{ts} & V_{ts} \end{pmatrix}$$

1/

 $V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$ 

- Overconstrain UT apex through diverse measurements
- goal: precise measurement of all UT angles and sides
- Test the Standard Model and probe BSM
  - Tree-dominated decays: Provide clean SM constraints
  - Loop-dominated decays: Sensitive to BSM contributions



$$\begin{array}{c|c} \phi_1 & (22.5^{+}_{-0.4}) \\ \hline \phi_2 & (86.2^{+3.9}_{-3.5})^{\circ} \\ \phi_3 & (65.9^{+3.3}_{-3.5})^{\circ} \\ \hline |V_{cb}| & (41.6^{+0.2}_{-0.6}) \times 10^{-3} \\ \hline |V_{ub}| & (3.73^{+0.04}_{-0.05}) \times 10^{-3} \end{array}$$

### **CHARGE-PARITY VIOLATION (CPV)**

$$V_{CKM} = \begin{bmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ \lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(\rho - i\eta) & -A\lambda^2 & 1 \end{bmatrix}$$

#### DIRECT CPV

Originates from interference between two amplitudes



 $A_2 \exp(i\phi + \delta)$ 

#### INDIRECT CPV

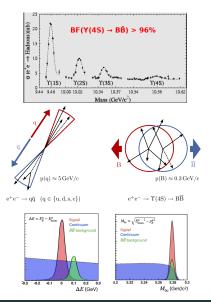
- Measured through interference between mixing and decay
- Time-dependent CPV (TDCPV)  $A^{B \to f}_{CP}(\Delta t) \equiv \frac{\Gamma\left(B^0(\Delta t) \to f\right) - \Gamma\left(\bar{B}^0(\Delta t) \to f\right)}{\Gamma\left(B^0(\Delta t) \to f\right) + \Gamma\left(\bar{B}^0(\Delta t) \to f\right)}$  $= \mathbf{S} \cdot \sin\left(\Delta m_d \Delta t\right) - \mathbf{C} \cdot \cos\left(\Delta m_d \Delta t\right)$ 
  - $S = |sin(2\phi)| = Mixing induced CPV$ C = Direct CPV



Angle	Relation	Measurement Channels	Tree/Loop	CPV Type
$\phi_2(lpha)$	$\arg\left(-\frac{V_{td}V_{tb}^{*}}{V_{ud}V_{ub}^{*}}\right)$	$B^0  ightarrow \pi\pi, B^0  ightarrow  ho^+  ho^-$	Mixed (Tree/Loop)	TDCPV
$\phi_3(\gamma)$	$\arg\left(-rac{V_{ud}V_{ub}^{*}}{V_{cd}V_{cb}^{*}} ight)$	$B^+  ightarrow D^0 K^+$ with various $D^0$ decays	Tree-dominated	Direct

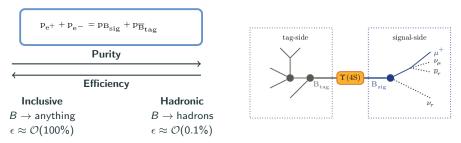
### **B PHYSICS AT BELLE II**

- $e^+e^-$  collision at  $\Upsilon(4S)$  [10.58 GeV]
  - Coherent production of  $B\bar{B}$  pairs
  - Clean environment
- Dominant background:  $e^+e^- o qar q$
- Spherical BB
   events can be discriminated from jet-like qq
- Continuum suppression using Multivariate Analysis (MVA)
- Kinematic constraints: well-known beam energy
  - Δ*E*: Reconstructed *B* and beam energy difference
  - *M*<sub>bc</sub>: Beam constrained mass



### FULL EVENT INTERPRETATION (FEI)

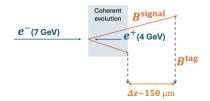
- Essential tool for decays with missing kinematic information
  - eg: Decay involving neutrinos
- FEI algorithm reconstructs second B meson  $(B_{tag})$  in  $\sim 10$ k channels
- Infer kinematics of signal B using well known initial state of  $\Upsilon(4S)$



ComputingandSoftwareforBigScience(2019)

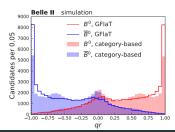
### **FLAVOR TAGGING**

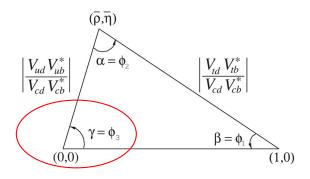
- Distinguish between  $B^0$  and  $\bar{B}^0$
- Signatures of flavor-specific decays grouped into 13 categories
- Quantum correlation allows identification of signal B flavor based on tag B
- $\epsilon = (31.68 \pm 0.45)\%$



#### Graph-neural-network flavor tagging (GFlaT) PhysRevD.110.012001

- Updated from category-based algorithm
- Improved performance by accounting for correlations between final-state particles
- $\epsilon = (37.40 \pm 0.43 \pm 0.36)\%$ 
  - 18% increase in efficiency





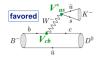
# ANGLE $\phi_3(\gamma)$

 $\phi_3$  is the phase between  $b o u\bar{c}s$  and  $b o c\bar{u}s$  transitions Accessible using B o DK



$$B^{\cdot} \rightarrow D^{\theta} K^{\cdot}$$







$$\frac{A^{\text{suppr.}}(B^- \to \bar{D}^0 K^-)}{A^{\text{favor.}}(B^- \to D^0 K^-)} = r_{\text{B}} \mathrm{e}^{i(\delta_{\text{B}} - \phi_3)}$$

- Common final states give access to phase via interference
- Tree level: No (large) BSM
- SM benchmark

Method	Decay Mode
GLW	$D^0  o K^+ K^-, K^0_s \pi^0$ (CP eigenstates)
BPGGSZ	Self-conjugate multi-body decay, e.g., $D^0  o K^0_s h^+ h^-$
GLS	$D^0  o {\cal K}^0_s {\cal K}^\pm \pi^\mp$ (singly Cabibbo-suppressed decays)
ADS	$D^0  o K^\pm \pi^\mp$

#### $\phi_3$ : Belle + Belle II combination

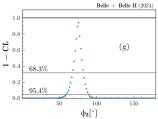
B decay	D decay	Method	Data set (Belle + Belle II)[fb $^{-1}$ ]
$B^+ \to Dh^+$	$D  ightarrow K_{ m s}^0 \pi^0, K^- K^+$	GLW	711 + 189 Bellell
$B^+ \to D h^+$	$D  ightarrow K^+ \pi^-, K^+ \pi^- \pi^0$	ADS	711 + 0
$B^+  ightarrow Dh^+$	$D \rightarrow K_{\rm s}^0 K^- \pi^+$	GLS	711 + 362 Bellell
$B^+ \to D h^+$	$D  ightarrow K_{ m s}^0 h^- h^+$	BPGGSZ (m.i.)	711 + 128 Bellell
$B^+  ightarrow Dh^+$	$D \rightarrow K_{\rm s}^0 \pi^- \pi^+ \pi^0$	BPGGSZ (m.i.)	711 + 0
$B^+  ightarrow D^* K^+$	$D^* \rightarrow D\pi^0, D \rightarrow K^0_s\pi^0, K^0_s\phi,$		
	$K^0_s\omega, K^-K^+, \pi^-\pi^+$	GLW	210 + 0
$B^+  ightarrow D^* K^+$	$D^* \rightarrow D\pi^0, D\gamma, D \rightarrow K^0_s \pi^- \pi^+$	BPGGSZ (m.d.)	605 + 0

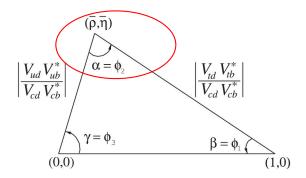
- First combination of all Belle and Belle II φ<sub>3</sub> measurements
- 59 input observables and 18 free parameters
- Belle + Belle II is improving the precision!

#### JHEP10(2024)143

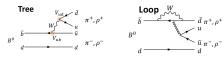
Experiment	φ <sub>3</sub> (°)
Belle + Belle II	$(75.2\pm7.6)$
LHCb LHCb-CONF	$(64.6\pm2.8)$





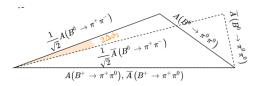


### EXTRACTION OF $\phi_2$ : ISOSPIN ANALYSIS



- TDCPV measurement
- $b \rightarrow u \bar{u} d$ : sensitive to  $\phi_2$
- b 
  ightarrow d loop contributions add an extra phase  $\Delta \phi_2$
- Interference of tree and loop:  $S = \sin(2\phi_2 + 2\Delta\phi_2), C \neq 0$

Key Observables:	
$\pi^+\pi^-, \rho^+\rho^-$	BF, $S$ , $C$
$\pi^+\pi^0, \rho^+\rho^0$	BF, $A_{\rm CP}$
$\pi^{0}\pi^{0}, \rho^{0}\rho^{0}$	BF, $A_{\rm CP}$ or C
	$S$ (only for $\rho^0 \rho^0$ )



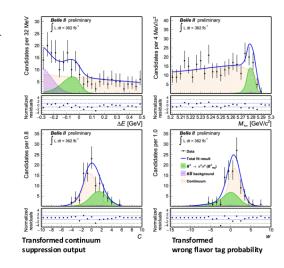
- Isospin symmetry allows for separating tree and penguin contributions
- Determining  $\phi_2$  from  $B \to \pi\pi$  requires BFs and  $A_{CP}$  of  $B^0 \to \pi^+\pi^-$ ,  $B^+ \to \pi^+\pi^0$ ,  $B^0 \to \pi^0\pi^0$
- $\pi^0 \pi^0, \rho^+ \rho^0, \rho^+ \rho^-$  requires  $\pi^0$  reconstruction:
  - Belle II has an advantage.
- $\rho\rho$  with smaller loop contribution dominates  $\phi_2$  precision

### $\phi_2:B^0 o\pi^0\pi^0$

- Experimentally challenging: 4 photons and no tracks
- Updated measurements of BF and A<sub>CP</sub> with full Run-1 statistics:
  - GFlat for flavor tagging
  - MVA dedicated for photon selections
- Fit to four variables

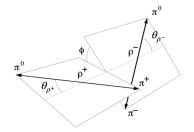
	${f BF}  imes 10^{-6}$	A <sub>CP</sub>
BelleII	$1.26 \pm 0.20 \pm 0.12$	$-0.06 \pm 0.30 \pm 0.05$
WA	$1.59\pm0.26$	$\textbf{0.30} \pm \textbf{0.20}$

- World best BF
- A<sub>CP</sub> comparable with WA
- Paper in preparation



 $\phi_2: B^0 \to \rho^+ \rho^-$ 

- Small contribution from loops: gives most stringent constraints on  $\phi_2$
- Reconstruction:  $\rho \rightarrow \pi^+(\pi^0 \rightarrow \gamma \gamma)$
- MVA to identify real photons in  $\pi^0$
- $q\bar{q}$  suppressed by TabNet (arxiv:1908.07442)
- Psuedoscalar  $\rightarrow$  Vector Vector decay:



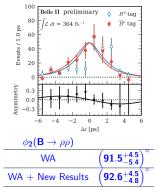
- Longitudinal and two transverse polarization states
- The fraction of longitudinal polarization *f*<sub>L</sub> determines the sensitivity of the CPV parameters
- $f_L$  is extracted from the helicity angle  $\theta_{
  ho}$

$$f_L = rac{\mathcal{B}(Long.)}{\mathcal{B}(Long.) + \mathcal{B}(Trans.)}$$

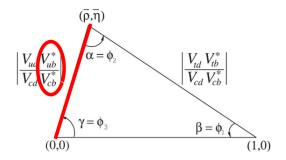
### $\phi_2:B^0 o ho^+ ho^-$

 Improved precision by GFlat flavor-tagger and better selection criteria

Fit to 6 observables to extract  $\mathcal{B}$  and  $f_L$ Long, signal ---- Self-crossfeed Data Trans, signal ····· Peaking backgrounds BB— Total Belle II preliminary Belle II preliminary 150 Events / 0.01 GeV/c Events / 0.01 GeV = 364 fb $L dt = 364 \text{ fb}^-$ 150 100 100 50 50 Pull Pull 30 ŏ -0.10.0 0.1 0.6 0.8 1.0  $\Delta E[GeV]$  $m_{\pi^+\pi^0}[GeV/c^2]$  $\mathcal{B} = \left(29.0^{+2.3}_{-2.2} \pm 3.1\right) \times 10^{-6}$  $f_L = 0.921^{+0.024}_{-0.022}_{-0.015}$  $S = (-0.26 \pm 0.19 \pm 0.08)$  $\mathcal{C}{=}{-}0.02 \pm 0.12^{+0.06}$ 

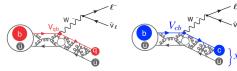


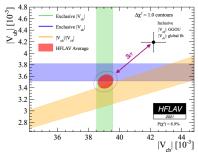
- 6% improvement by Belle II results!
- Consistent with previous measurements
- Paper in preparation



# DETERMINATION OF $|V_{ub}| \& |V_{cb}|$

- $|V_{ub}|$  and  $|V_{cb}|$  are important to constrain CKM unitarity
- Precisely measured via semileptonic *B* decays.
- Significant tension between inclusive & exclusive determinations

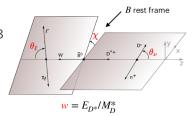




Exclusive $ V_{xb} $	Inclusive $ V_{xb} $
<b>Exclusive</b> $ V_{ub} : \bar{B} \to \pi \ell \bar{\nu}_{\ell}$	Inclusive $ V_{ub} : \ ar{B}  o X_u \ell ar{ u}_\ell$
<b>Exclusive</b> $ V_{cb} : \ \bar{B} \to D\ell\bar{\nu}_{\ell}, \ \bar{B} \to D^*\ell\bar{\nu}_{\ell}$	Inclusive $ V_{cb} : \ \bar{B}  o X_c \ell \bar{ u}_\ell$
$\mathcal{B} \propto  V_{qb} ^2 f^2$	$\mathcal{B} =  V_{qb} ^2 \left[ \Gamma(b \to q \ell \bar{\nu}_\ell) + \frac{1}{m_{c,b}} + \alpha_s + \ldots \right]$
$f \rightarrow$ Form Factors	Heavy Quark Expansion

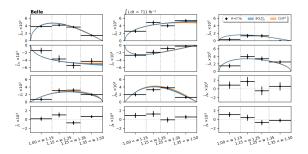
 $|V_{cb}|$  from  $\bar{B} \to D^* \ell \bar{\nu}_{\ell}$ 

- $|V_{cb}|$  from angular analysis of  $B o D^* \ell \bar{
  u}_\ell$
- Full Belle dataset (711  ${\rm fb}^{-1}$ ) with hadronic B tagging
- Reconstruct both charged and neutral B
  - $\bar{B}^0 \to D^{*+} \ell \bar{\nu}_{\ell}, \ D^{*+} \to D^0 \pi^+ / D^+ \pi^0$
  - $B^- \rightarrow D^{*0} \ell \bar{\nu}_\ell$ ,  $D^{*0} \rightarrow D^0 \pi^0$



- Four-dimensional differential decay rate for  $\bar{B} \to D^* \ell \bar{\nu}_\ell$  can be expressed in terms of 12 functions
- Angular coefficients obtained from data in bins of the hadronic recoil parameter  $w = \frac{m_B^2 + m_{D^*}^2 q^2}{2m_B m_{D^*}}$
- Measure 12 angular coefficients  $J_i$  in four bins of w
- Determine signal yields by fitting the mass of undetected neutrinos in the event:  $M_{\text{miss}}^2 = \left(p_{e^+} + p_{e^-} - p_{B_{B_{tag}}} - p_{D^*} - p_{\ell}\right)^2$

# $|V_{cb}|$ from $ar{B} ightarrow D^* \ell ar{ u}_\ell$



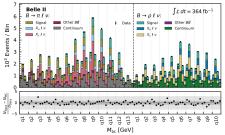
Phys.Rev.Lett.133(2024)131801  $|V_{cb}|_{BGL} = (41.0 \pm 0.3 \pm 0.4 \pm 0.5) \times 10^{-3}$ 

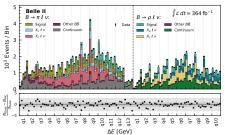
 $|V_{cb}|_{
m CLN} = (40.9 \pm 0.3 \pm 0.4 \pm 0.4) \times 10^{-3}$ 

- Agrees with the latest and most precise determinations of inclusive  $\left|V_{cb}\right|$
- Results in agreement with fits to 1D partial rates on the same data set PhysRevD.108.012002 as well as on Belle II data arXiv:2310.01170v2

 $|V_{\mu b}|$  from  $B^0 \to \pi^- \ell^+ \nu_\ell$  &  $B^+ \to \rho^0 \ell^+ \nu_\ell$ 

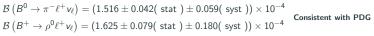
- The rates of  $b \rightarrow u$  decays is proportional to  $|V_{ub}|^2$
- Full Belle II Run1 dataset of 364 fb-1, untagged
- Extract signal yields from fit to binned MC templates
  - 2 kinematic variables in bins of q<sup>2</sup> simultaneously for πℓν and ρℓν
  - $q^2 = (P_B P_{\pi/\rho})^2$
- Background suppressed using BDTs
- Total branching ratio is the sum of all the partial  $\Delta B_i$  in each  $q^2$  bin

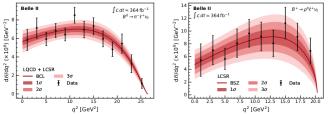




$$|V_{ub}|$$
 from  $B^0 o \pi^- \ell^+ 
u_\ell$  &  $B^+ o 
ho^0 \ell^+ 
u_\ell$ 

#### arxiv:2407.17403 [PRD]





$$\begin{split} B^0 &\rightarrow \pi^- \ell^+ v_\ell : |V_{ub}| = (3.73 \pm 0.07 (\text{stat}) \pm 0.07 (\text{syst}) \pm 0.16 (\text{theo})) \times 10^{-3} \text{ LQCD+LCSR constraints} \\ B^+ &\rightarrow \rho^0 \ell^+ v_\ell : |V_{ub}| = (3.19 \pm 0.12 (\text{stat}) \pm 0.17 (\text{syst}) \pm 0.26 (\text{theo})) \times 10^{-3} \text{ LCSR constraints} \end{split}$$

- Consistent with WA
- Comparable precision with Belle/Babar

#### **SUMMARY**

- Belle II has already recorded a total of 531  ${\rm fb}^{-1}$  of data
- Precise measurements of CKM angles and sides are crucial for increasing the constraining power of the Unitarity Triangle fit.
- The new GNN-based flavor tagger has achieved an 18% improvement in effective tagging efficiency

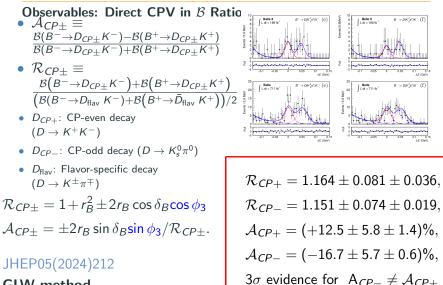
• 
$$\phi_2$$
:  $B \to \pi^0 \pi^0$ ,  $B^0 \to \rho^+ \rho^-$ 

- New results with improved precision, the first  $\phi_2$  extraction with improved precision
- $\phi_3$ : First combined Belle and Belle II analysis, achieving improved sensitivity
- Belle and Belle II continue to produce updated and improved measurements of |V<sub>cb</sub>| and |V<sub>ub</sub>|

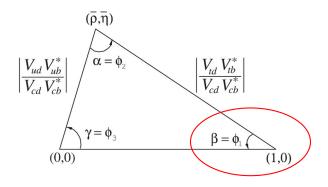
Thank You!

BACKUP

### $\phi_3: B^{\pm} \rightarrow D_{CP}K^{\pm}$ in Belle + Belle II Data



**GLW** method



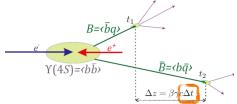
# ANGLE $\phi_1(\beta)$

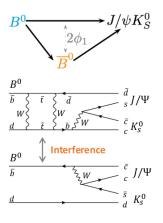
#### Time-dependent CPV

- Oscillation-induced CPV as a function of  $\Delta t$
- Boosted CMS to measure  $\Delta t$  from decay length

$$\begin{split} A^{B \to f}_{CP}(\Delta t) &\equiv \frac{\Gamma\left(B^0(\Delta t) \to f\right) - \Gamma\left(\bar{B}^0(\Delta t) \to f\right)}{\Gamma\left(B^0(\Delta t) \to f\right) + \Gamma\left(\bar{B}^0(\Delta t) \to f\right)} \\ &= \frac{S \cdot \sin\left(\Delta m_d \Delta t\right) - C \cdot \cos\left(\Delta m_d \Delta t\right)}{} \end{split}$$

 $S = |sin(2\phi_1)| = Mixing induced CPV C = Direct CPV$ 



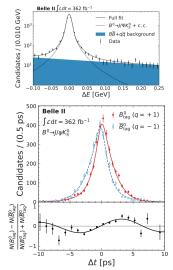


 $\phi_1: B^0 
ightarrow {\sf J}/\psi {\sf K}^0_{\sf S}$ 

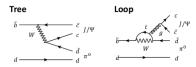
- $b \rightarrow c\bar{c}s$  transition
- Uses the GFlat flavor-tagging algorithm
- Yield extraction fit to  $\Delta E$
- Fit background-free Δt for parameters of interest
- Improved statistical uncertainty 8% (S) and 7% (C) compared to category-based FBDT flavor tagger

$$\begin{split} S = & 0.724 \pm 0.035 \pm 0.009 \\ & \rightarrow \phi_1 = (23.2 \pm 1.5 \pm 0.6)^{\circ} \\ & \mathrm{C} = & -0.035 \pm 0.026 \pm 0.029 \end{split}$$

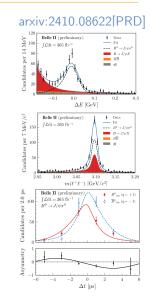
#### PhysRevD.110.012001



### $\phi_1:B^0 o J/\psi\pi^0$



- CKM & color-suppressed tree-level  $b 
  ightarrow c ar{c} d$
- Constrain the loop contributions in  $B^0 \rightarrow J/\psi K^0$  $(b \rightarrow c\bar{c}s)$  to determine  $\phi_1$
- Fit ΔE & m(II) for background subtraction and extract yields
- Fit  $\Delta t$  to extract CPV parameters
- $1^{st}$  5  $\sigma$  observation TDCPV in this mode BF =  $(2.00 \pm 0.12 \pm 0.10) \times 10^{-5}$ S<sub>CP</sub> =  $-0.88 \pm 0.17 \pm 0.03$ C<sub>CP</sub> =  $0.13 \pm 0.12 \pm 0.03$
- Most precise and comparable with previous measurements



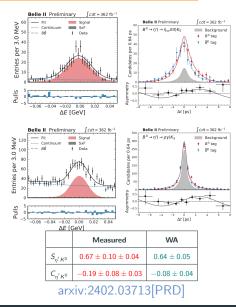
 $\phi_1: B^0 \to n' K_s$ 

 $\overline{b} \underbrace{k}_{W} \underbrace{k}_{W} \underbrace{k}_{K_{S}} \underbrace{k}_{$ 

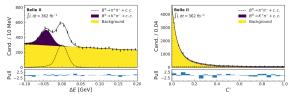
- Dominated by the Loop process: BSM could shift S & C
- Relatively large BF and limited contribution from tree amplitudes compared to other  $b \to sq\bar{q}$

• 
$$\eta^{'} 
ightarrow \eta(\gamma\gamma)\pi\pi \And \eta^{'} 
ightarrow 
ho(\pi\pi)\gamma$$

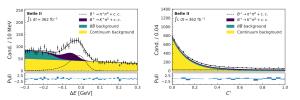
- SM prediction:
  - $|sin(2\phi_1) S_{\eta'K_S}| = 0.01 \pm 0.01$ •  $C_{\eta'K_S} = 0$
- Fits to  $\Delta E$ ,  $M_{\rm bc}$ ,  $C_{BDT}$  &  $\Delta t$
- Agreement with WA and compatible with Belle/Babar precision



#### $\phi_2: B^0 \to \pi^+\pi^-$ and $B^+ \to \pi^+\pi^0$



 $B^0 
ightarrow \pi^+\pi^-$ : BR =  $(5.83 \pm 0.22 \pm 0.17)10^{-6}$ 

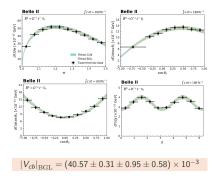


#### PhysRevD.109.012001

- Good agreement with previous measurements
- Sensitivity is comparable with Belle using only half of Belle's data!

 $B^+ \to \pi^+ \pi^0$ : BR = (5.10 ± 0.29 ± 0.27)10<sup>-6</sup>  $A_{CP} = -0.081 \pm 0.054 \pm 0.008$ 

 $|V_{cb}|$  from  $\bar{B} \to D^* \ell \bar{\nu}_{\ell}$ 



- Using 189  ${\rm fb}^{-1}$  of Belle II data
- Partial decay rates are reported as a function of the recoil parameter and three decay angles

$$\mathcal{B}\left(\bar{B}^{0} \to D^{*+}e^{-}\bar{\nu}_{e}\right) = (4.917 \pm 0.032 \pm 0.216)\%,$$

$$\mathcal{B}(\bar{B}^0 \to D^{*+} \mu^- \bar{\nu}_{\mu}) = (4.920 \pm 0.032 \pm 0.231)\%,$$
  
 $\mathcal{B}(\bar{B}^0 \to D^{*+} \mu^- \bar{\nu}_{\mu}) = (4.922 \pm 0.023 \pm 0.220)\%$ 

 $|V_{cb}|_{\rm CLN} = (40.13 \pm 0.27 \pm 0.93 \pm 0.58) \times 10^{-3}$ 

- Signal extraction with fit to cos θ<sub>BY</sub> and ΔM in bins of w, cos θ<sub>ℓ</sub>, cos θ<sub>ν</sub> and χ
- Good agreement with the world average of the exclusive and inclusive determinations
- Agrees with the recent Belle measurement PhysRevD.108.012002