

Aspects of  
**ultralight dark matter**  
for **astrophysical observations**

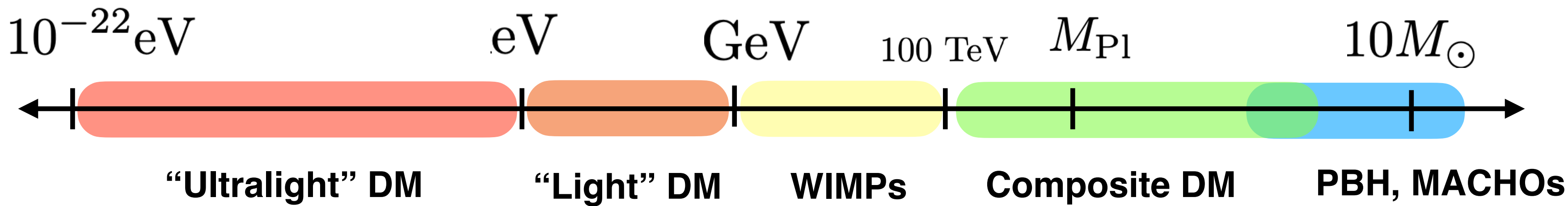


Diego Blas



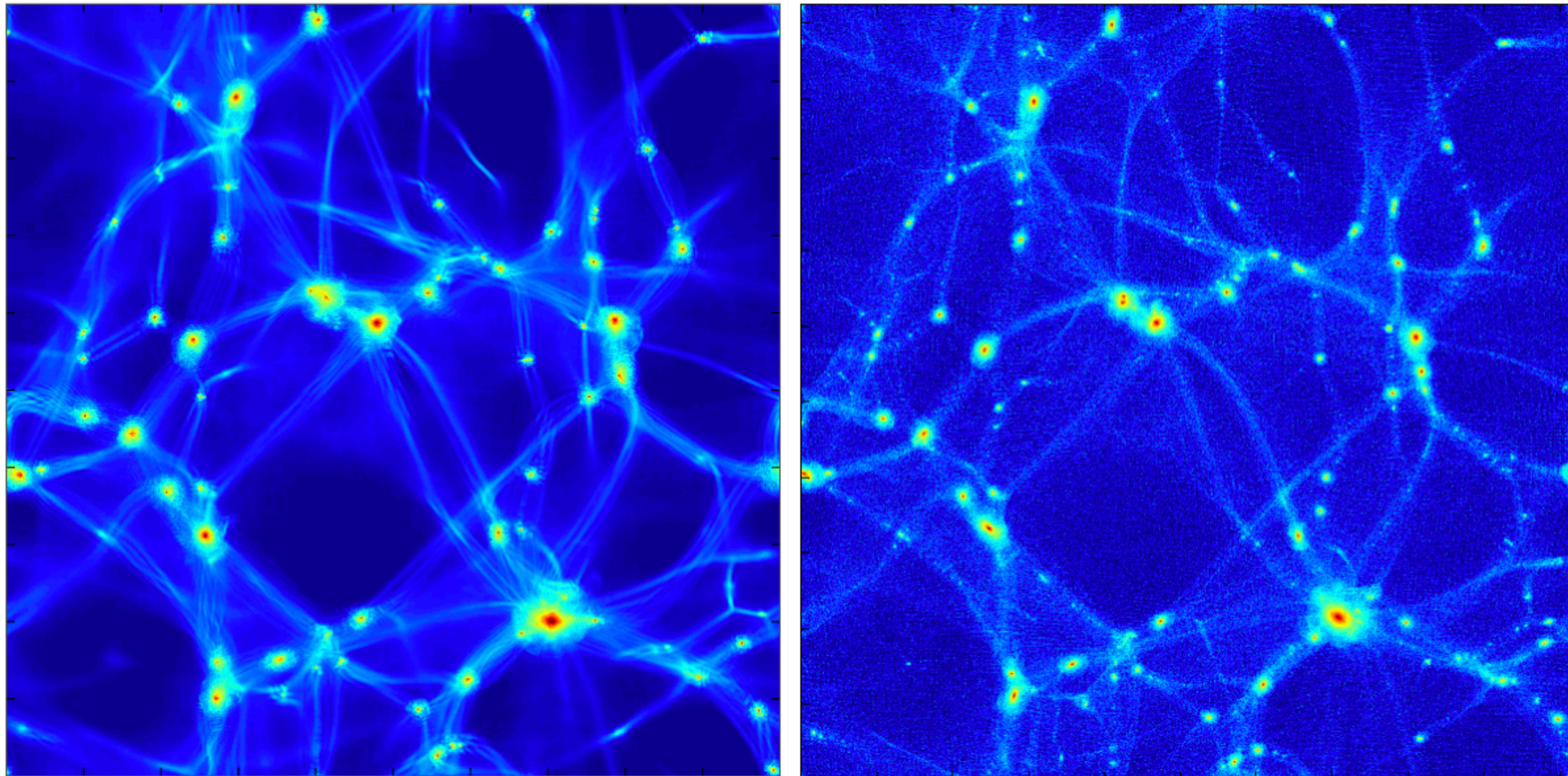
Funded by  
the European Union

# Dark Matter: where to look?



# Similar behaviour at large-scales

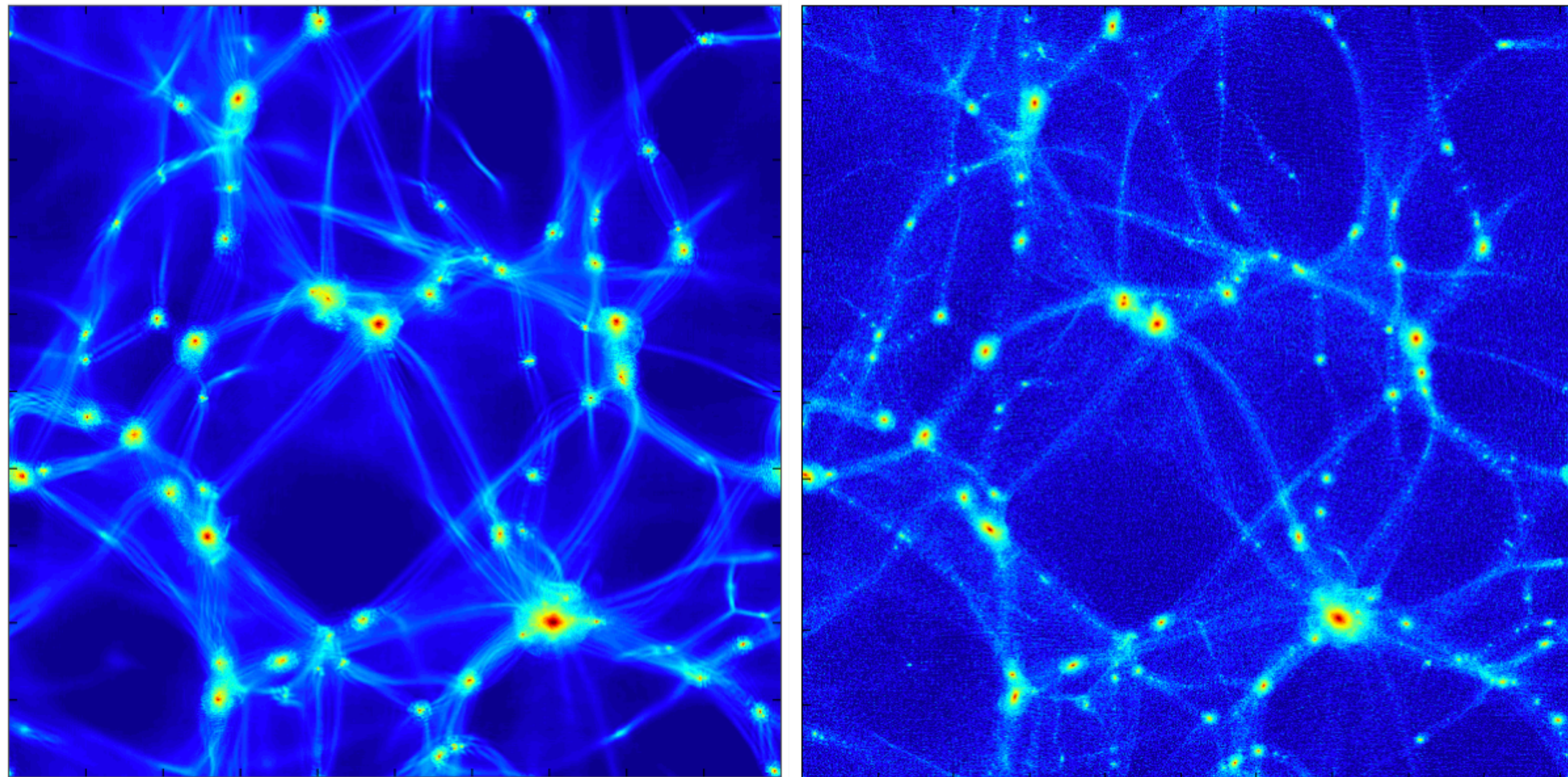
Scale of  $\sim 30$  Mpc, Schive et al. 1406.6586



# Similar behaviour at large-scales

$$m \sim 10^{-22} \text{ eV}$$

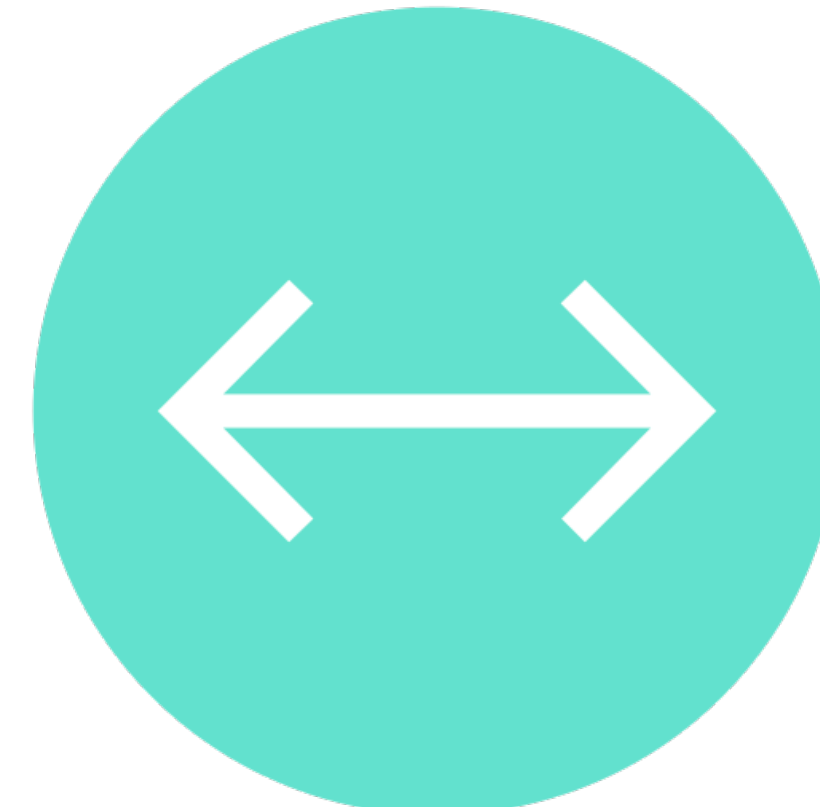
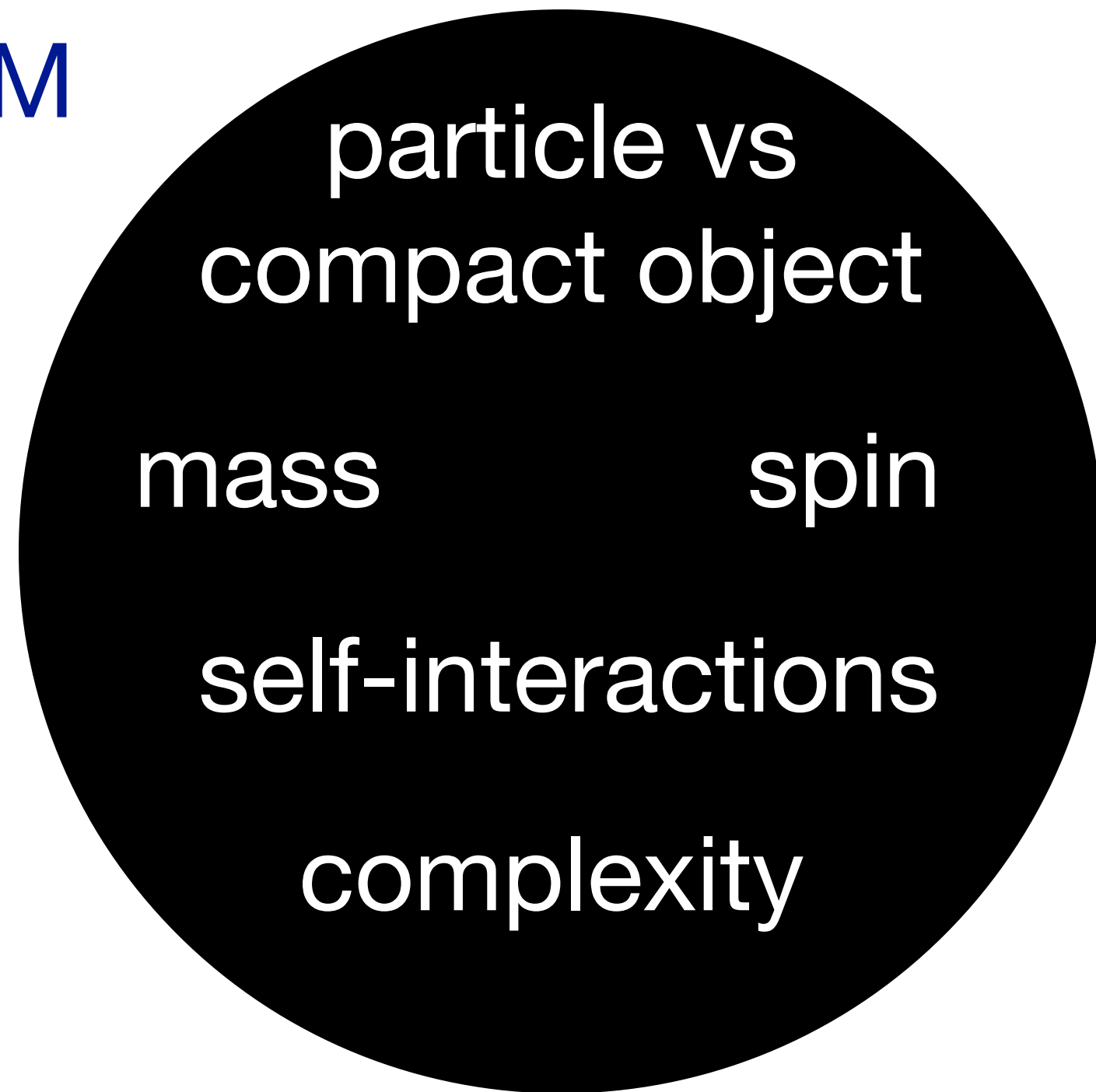
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We see differences at small scales

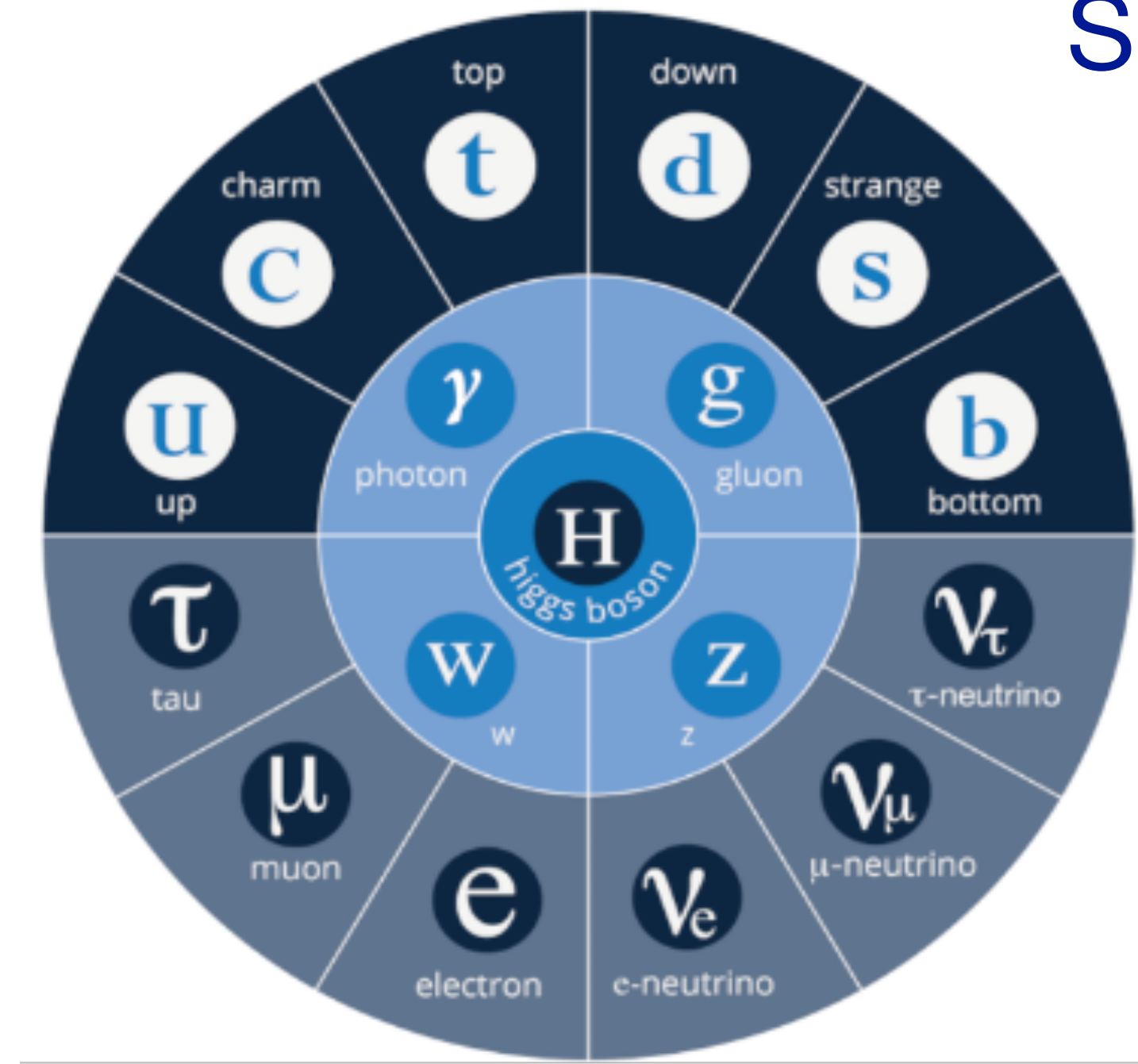
# What can we look for

DM

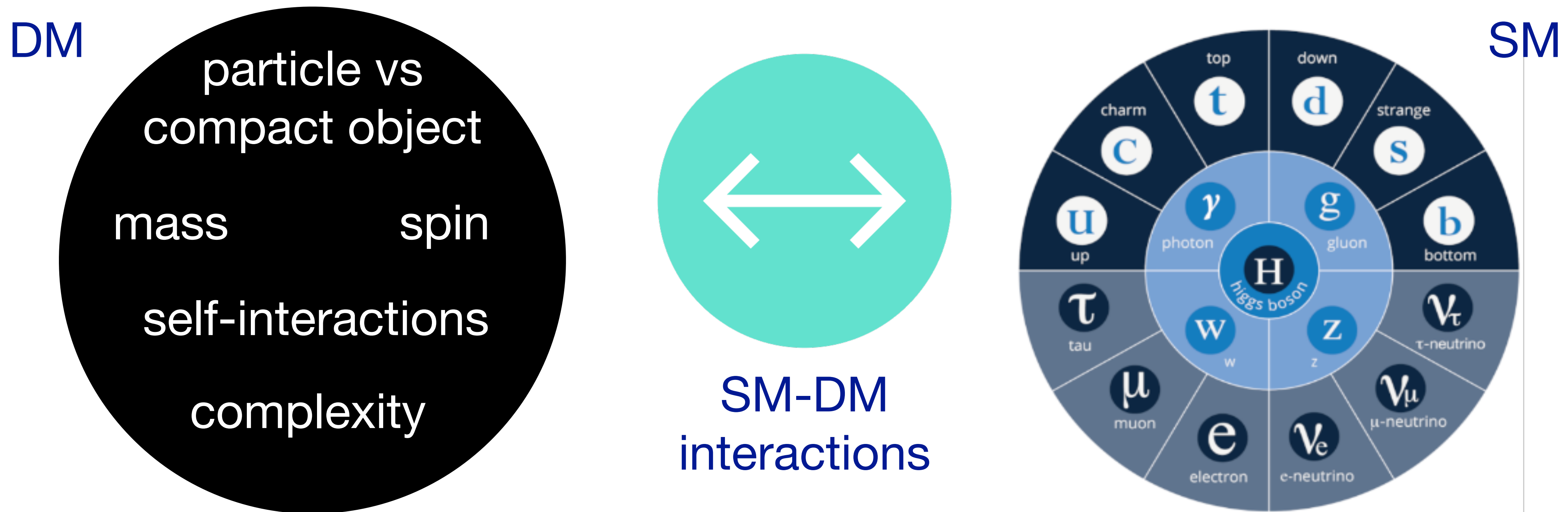


SM-DM interactions

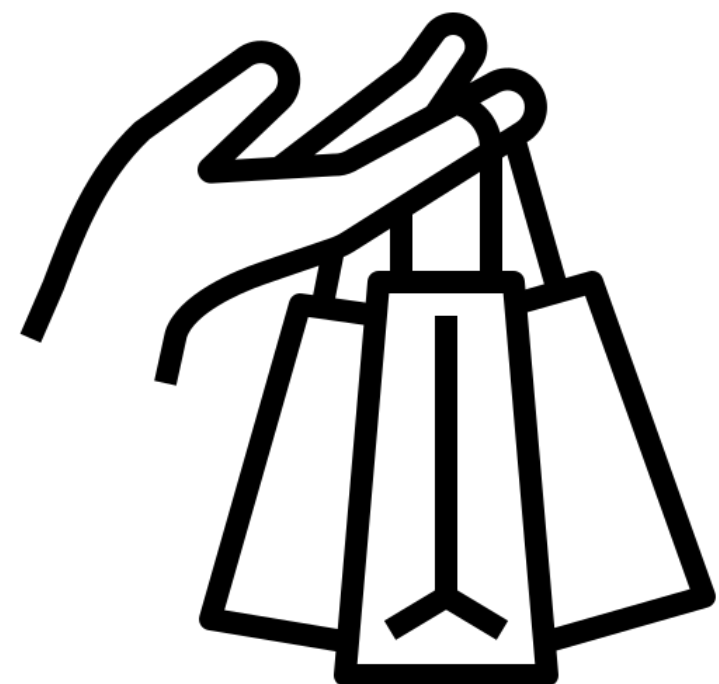
SM



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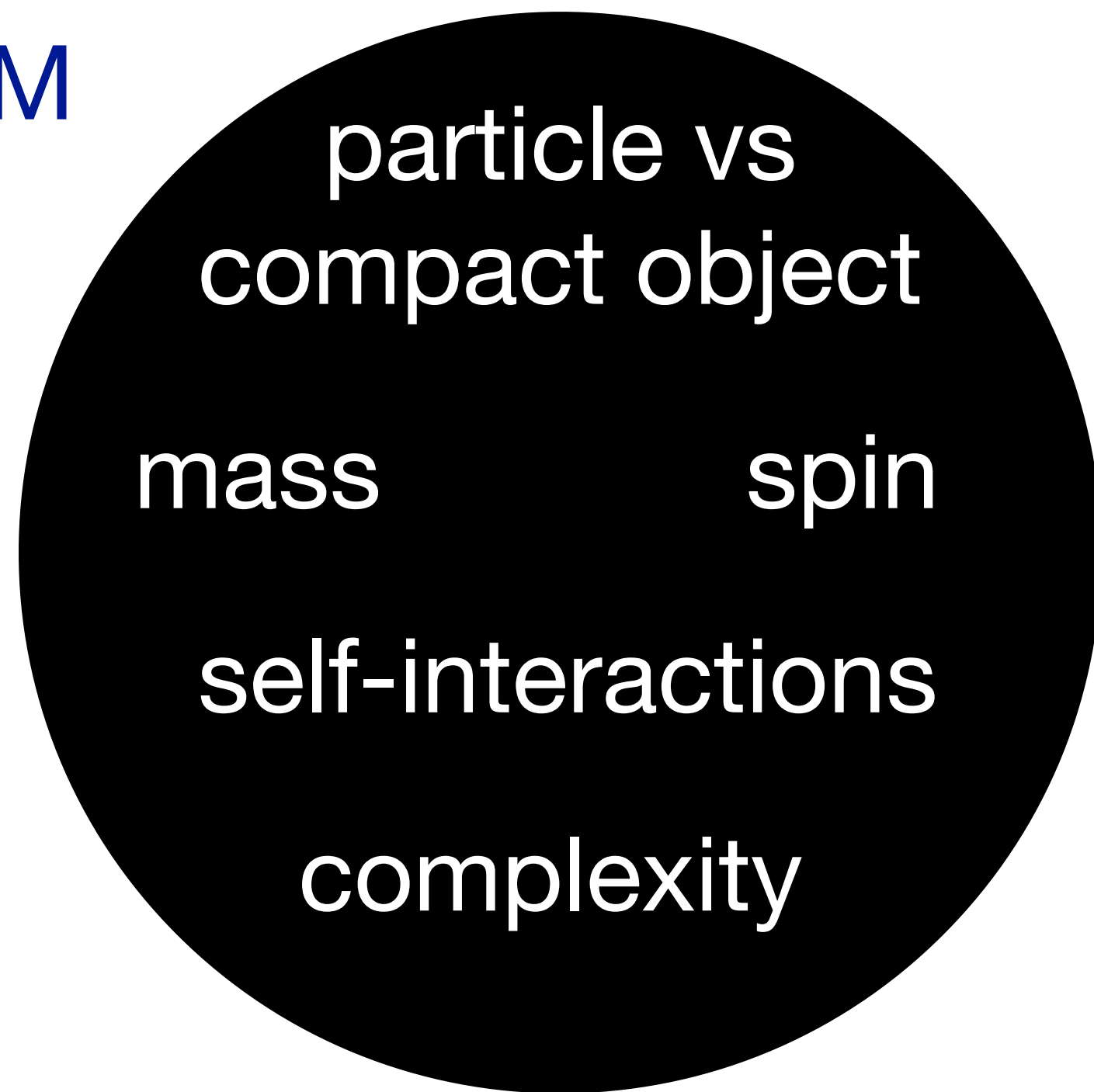
On top this, there are wishful properties ('miracles')



1. does it help in astrophysical observation?
2. is it 'naturally' produced in the early Universe?
3. is it theoretically motivated by other 'principles'/theory concerns?
4. can we detect it in the laboratory?
5. can we single it out in astrophysical data?

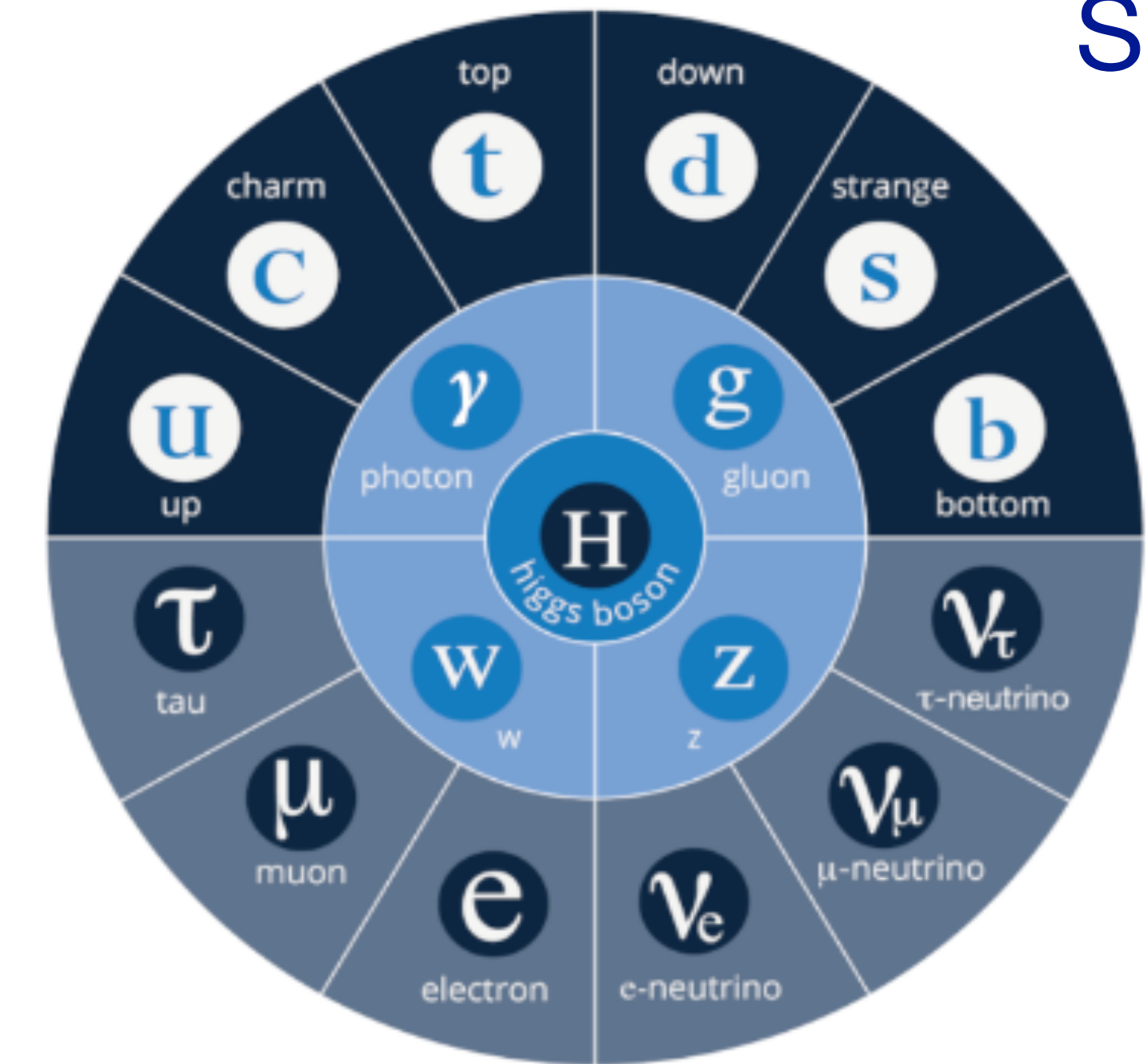
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SM-DM interactions

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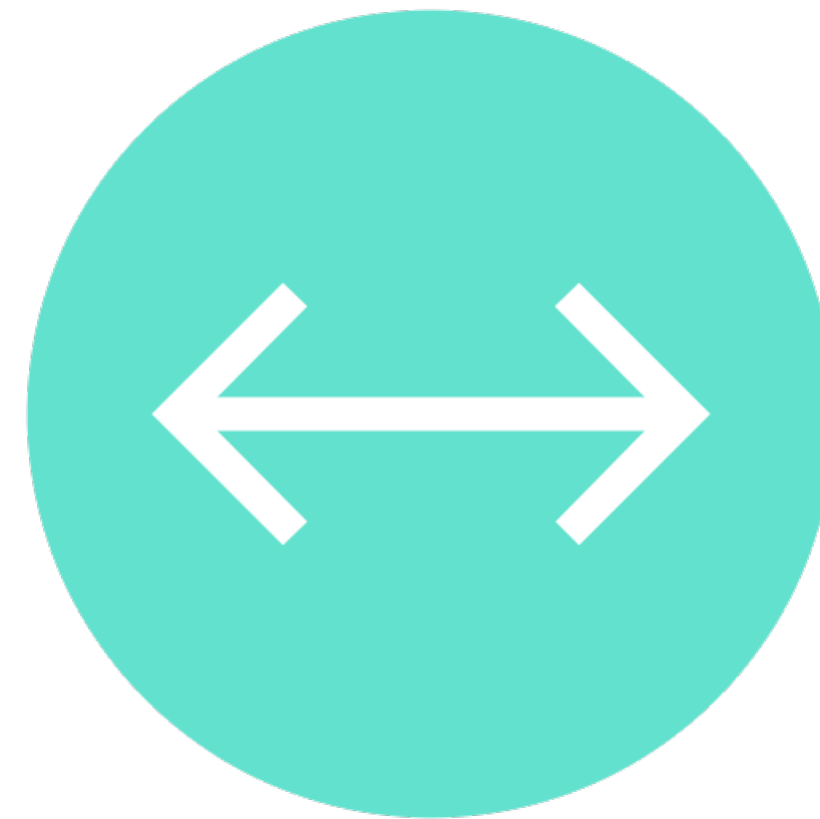
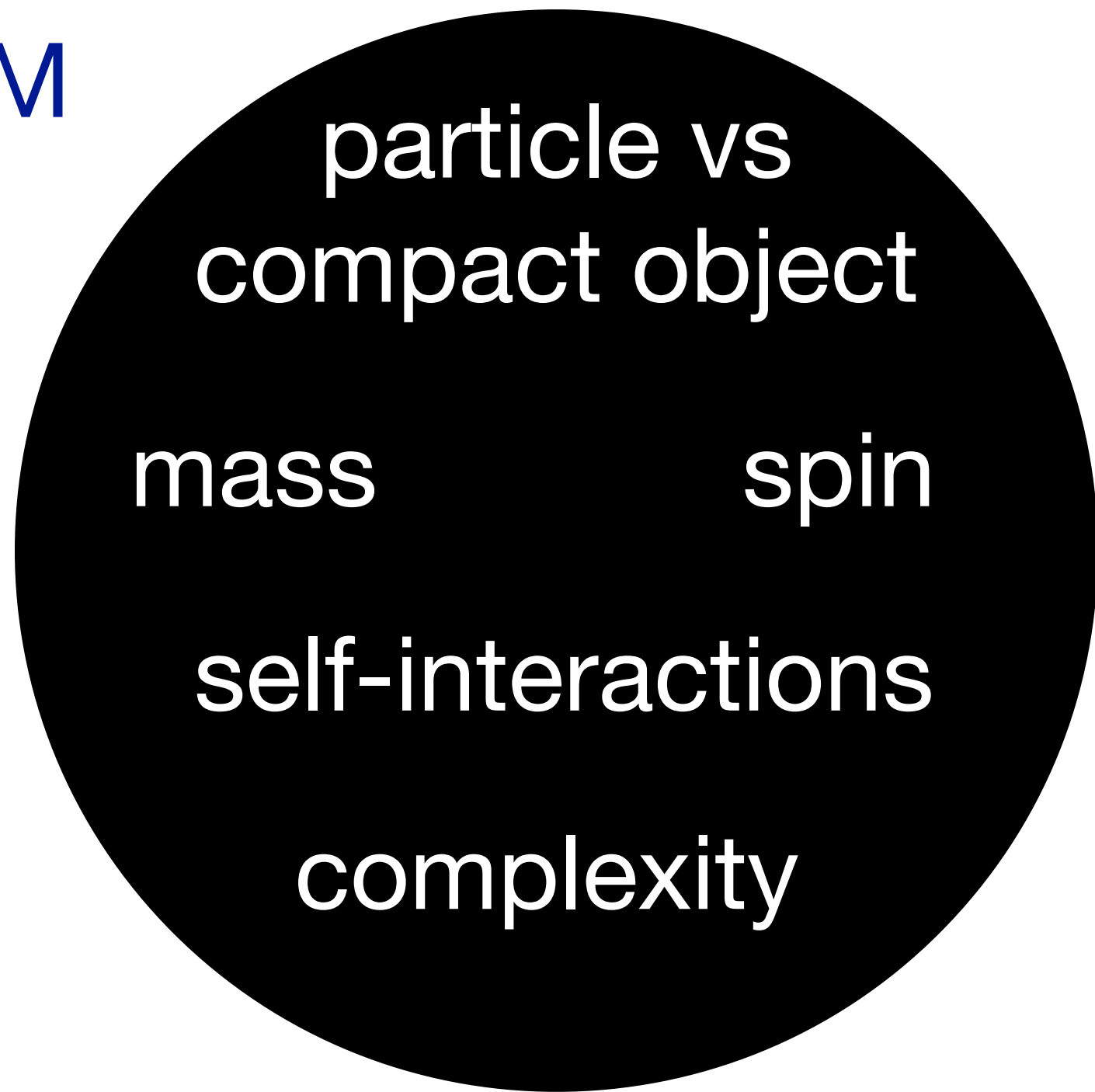
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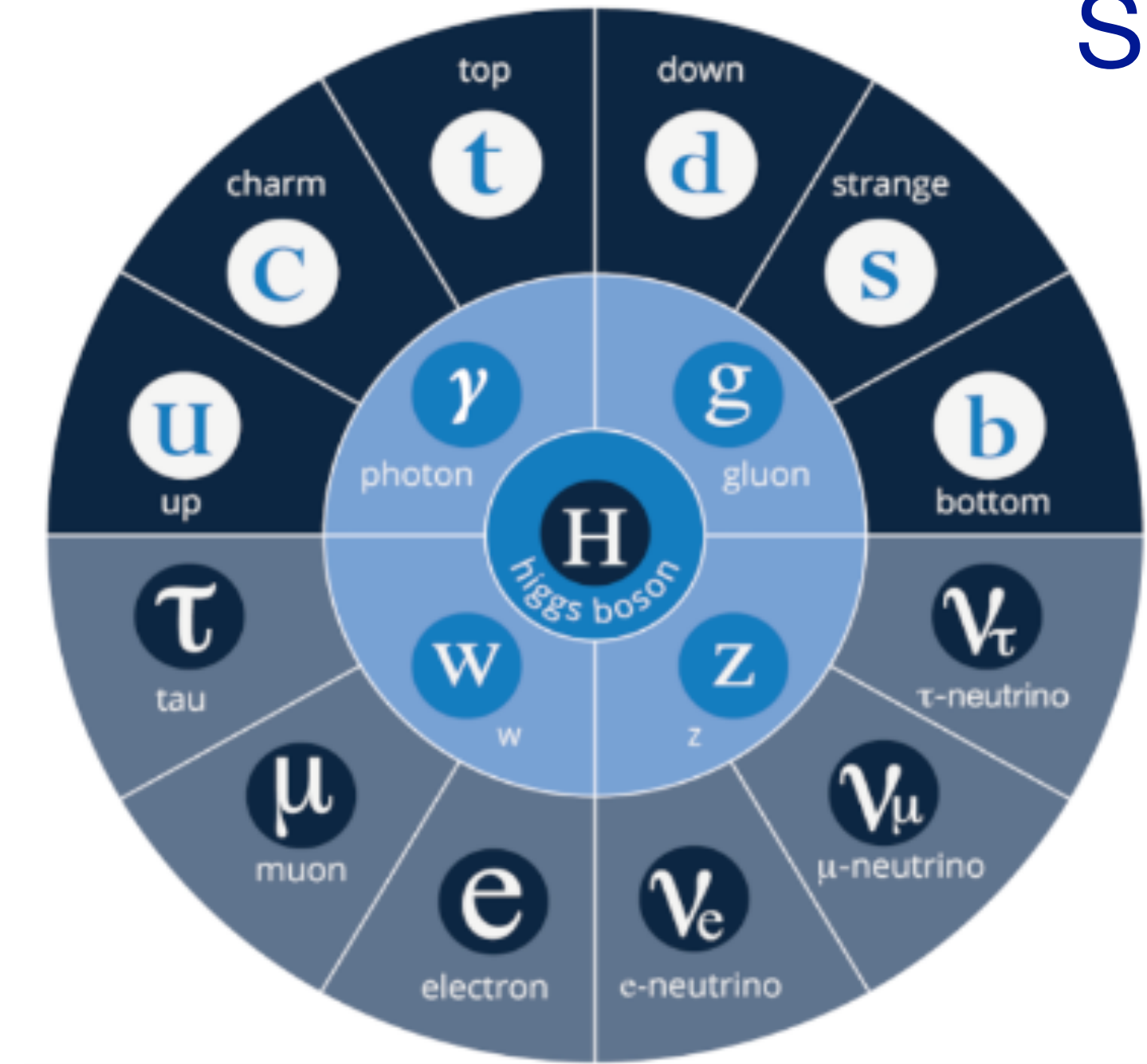
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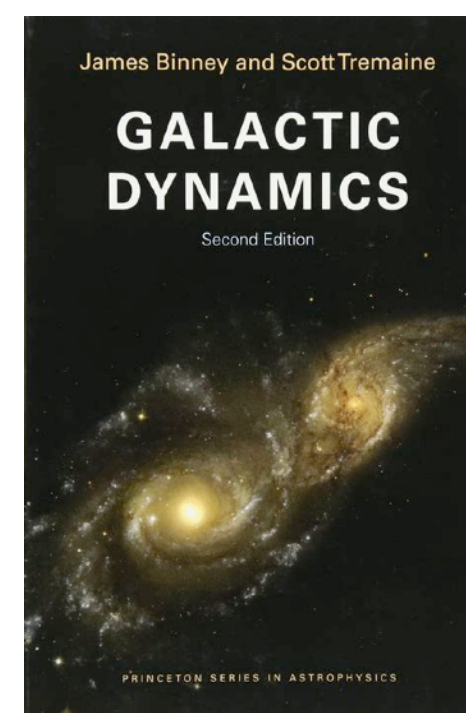
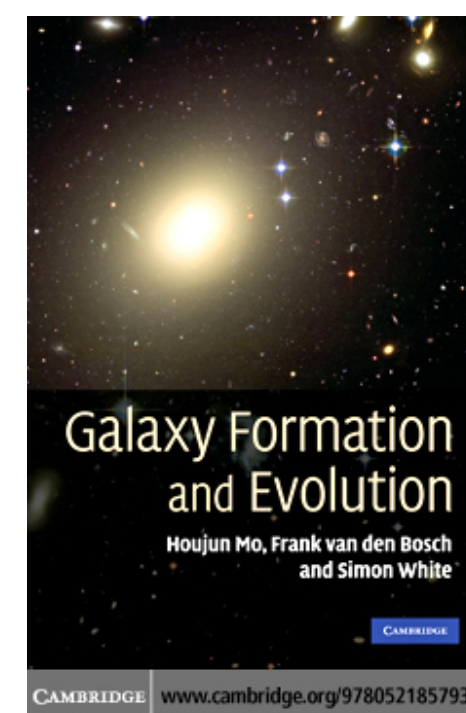
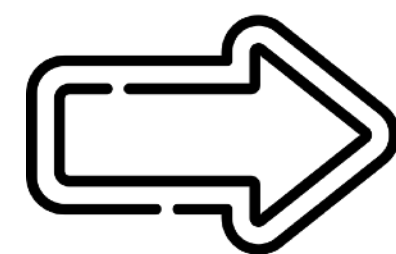
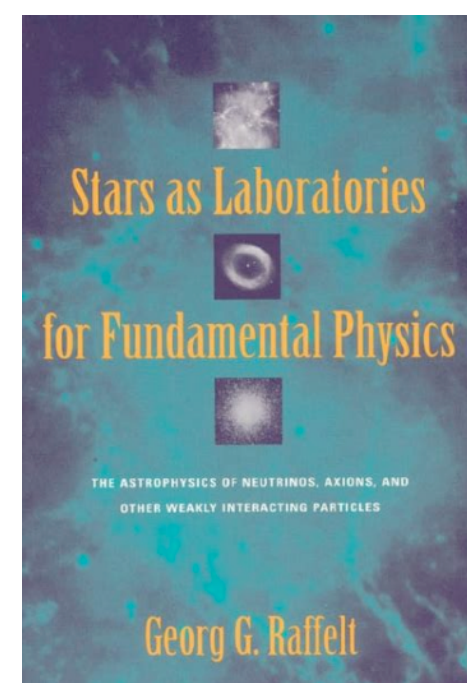


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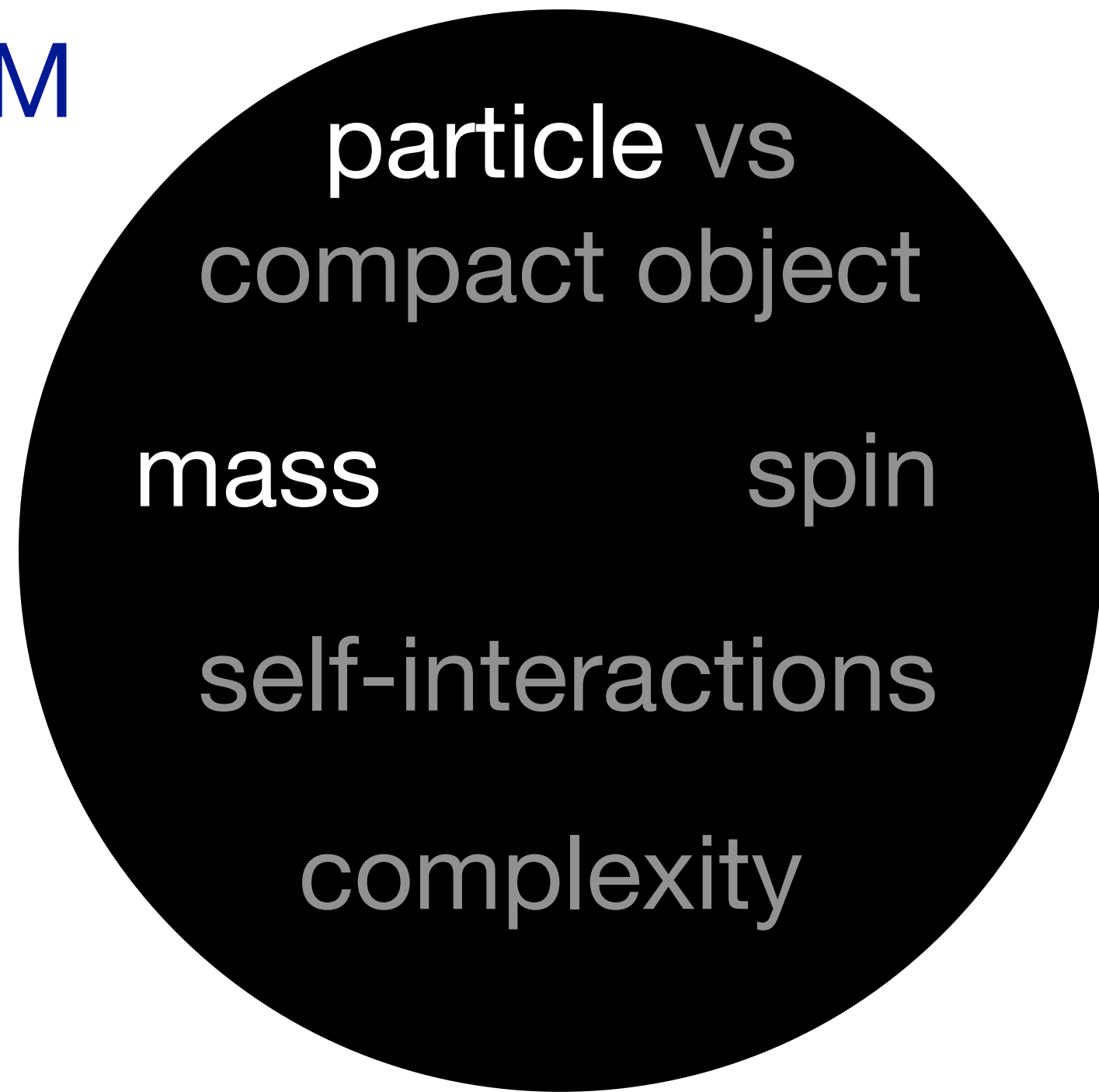


*'Try to extend the diversity of DM models to astrophysical modelling'*



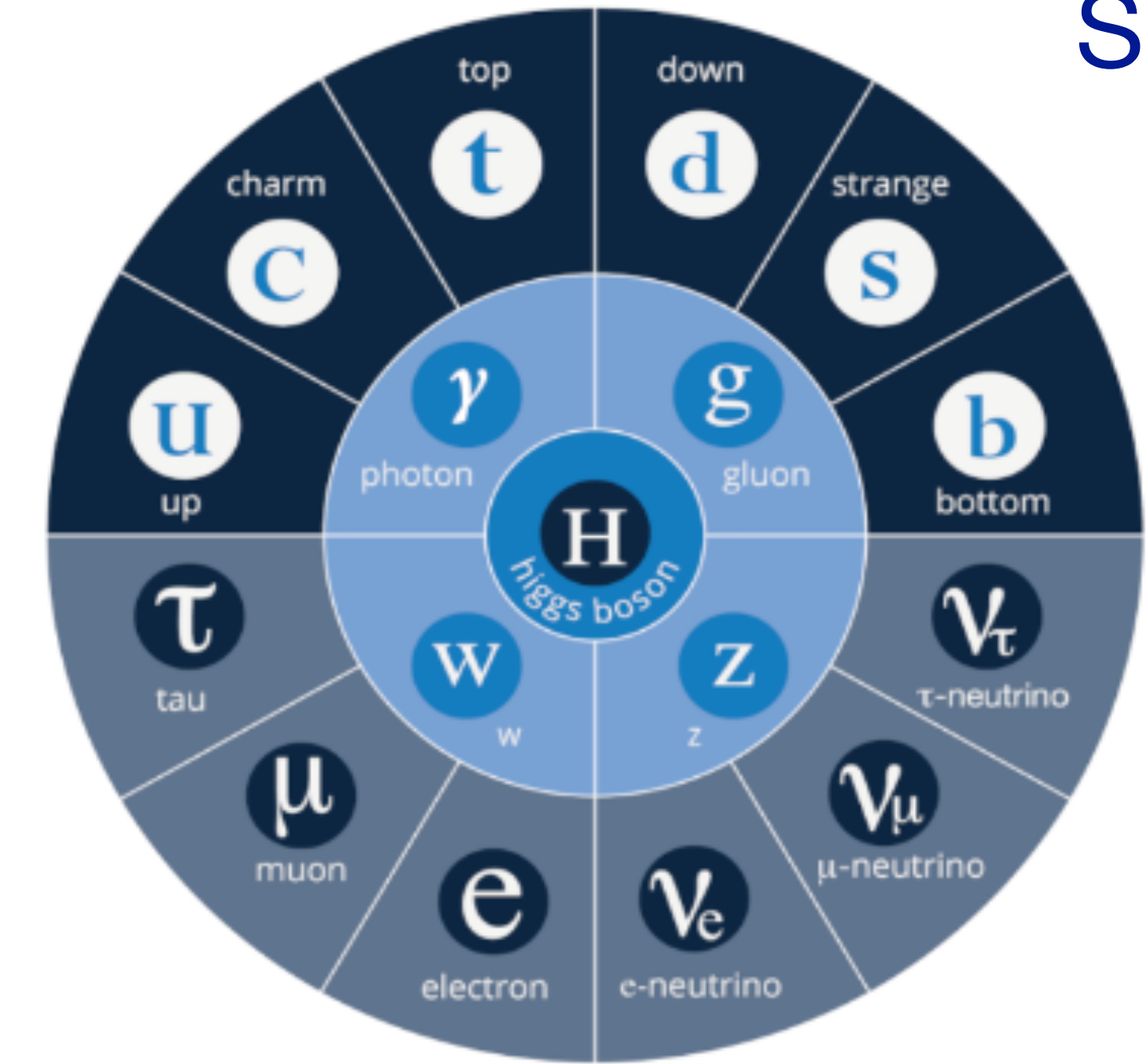
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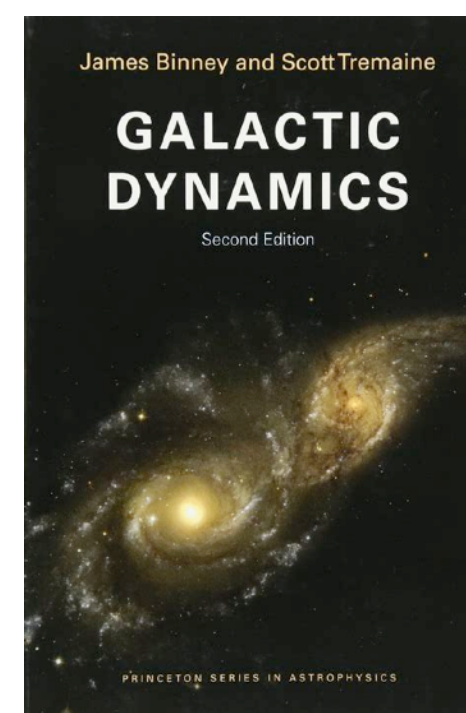
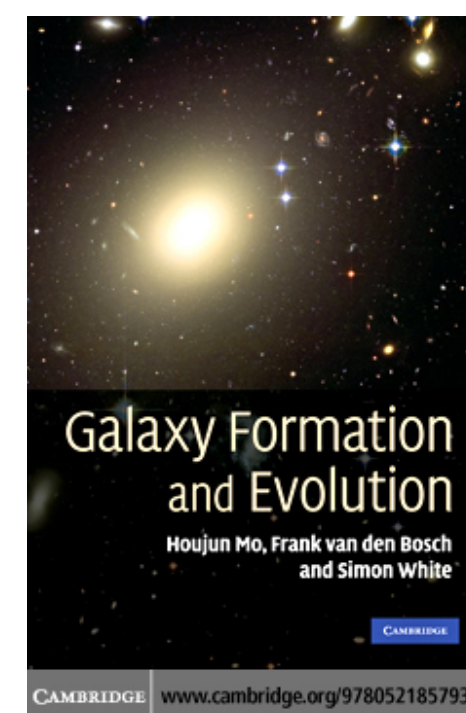
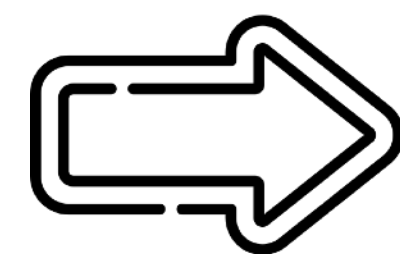
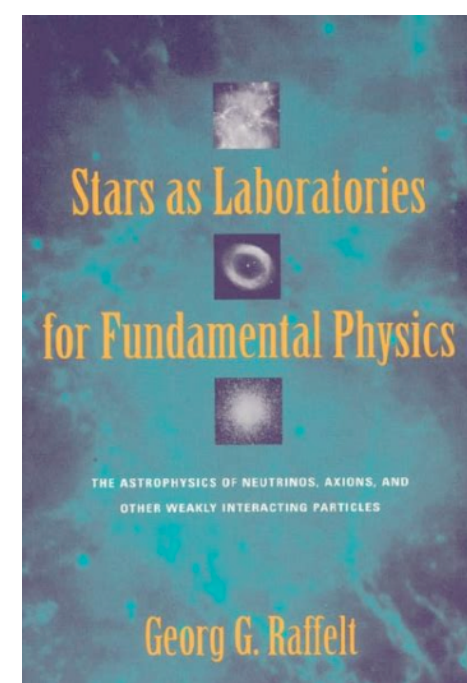


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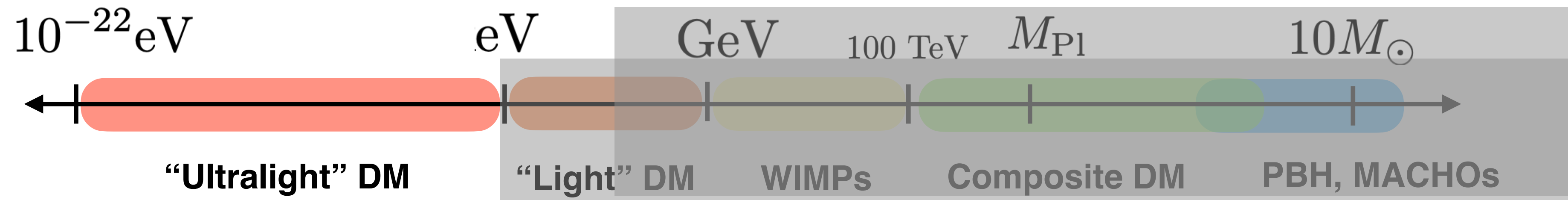


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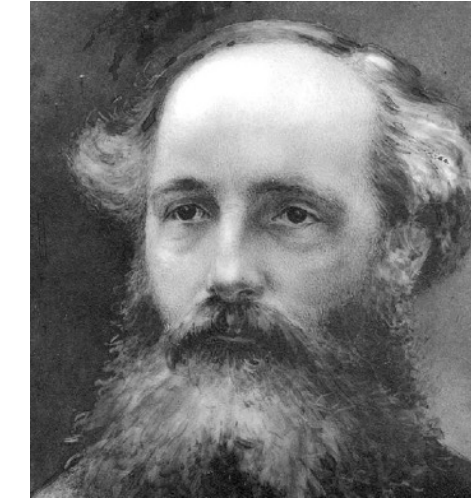
# 2 natural barriers: ULDM and Tremaine-Gunn



# (U)LDM does not behaves as CDM at small-scales

Description as a particle, as a classical field or as DF?

$\hbar\omega$



$F_{\mu\nu}$

e.g. Milky way DM halo

i) typical **distance** between particles  $d \sim n^{-1/3} \sim (M/(mV))^{-1/3} \sim 20 \text{ kpc}/(10^9 M_\odot)^{1/3} m^{1/3}$

ii) typical **size** of particle wavepacket in the halo  $L \gtrsim 1/(mv_{\text{esc}}) \approx 190 \left(\frac{m}{10^{-22} \text{eV}}\right)^{-1} \text{ pc}$

particles overlap for  $d \lesssim L$

$m_{MW} \sim 1 \text{ eV}$

## fermions

become degenerate close to this limit

**a**  $m_f \gtrsim \text{keV}$  Tremaine-Gunn bound

**b** 'condensed dark matter' Bar et al 2102.11522  
Garani et al 2207.06928

field theory description

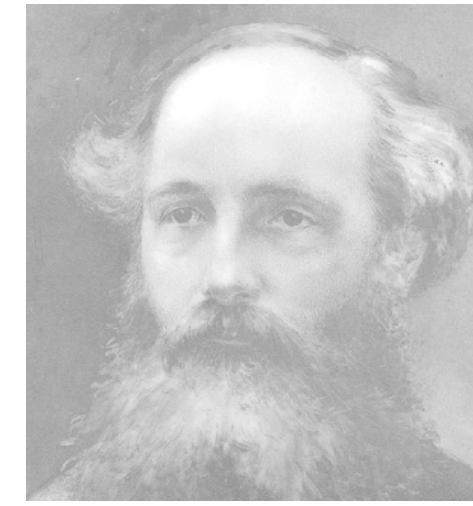
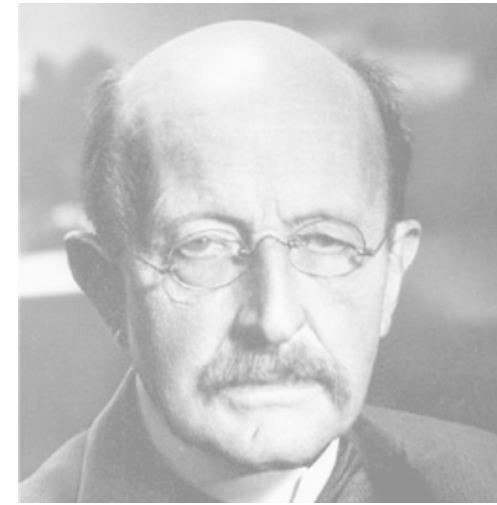
**c**  $\mathcal{L} = \frac{1}{2} \left[ (\partial_\mu \phi)^2 - m^2 \phi^2 \right] + \text{gravity}$   
(spin 0, 1 or 2)

## bosons

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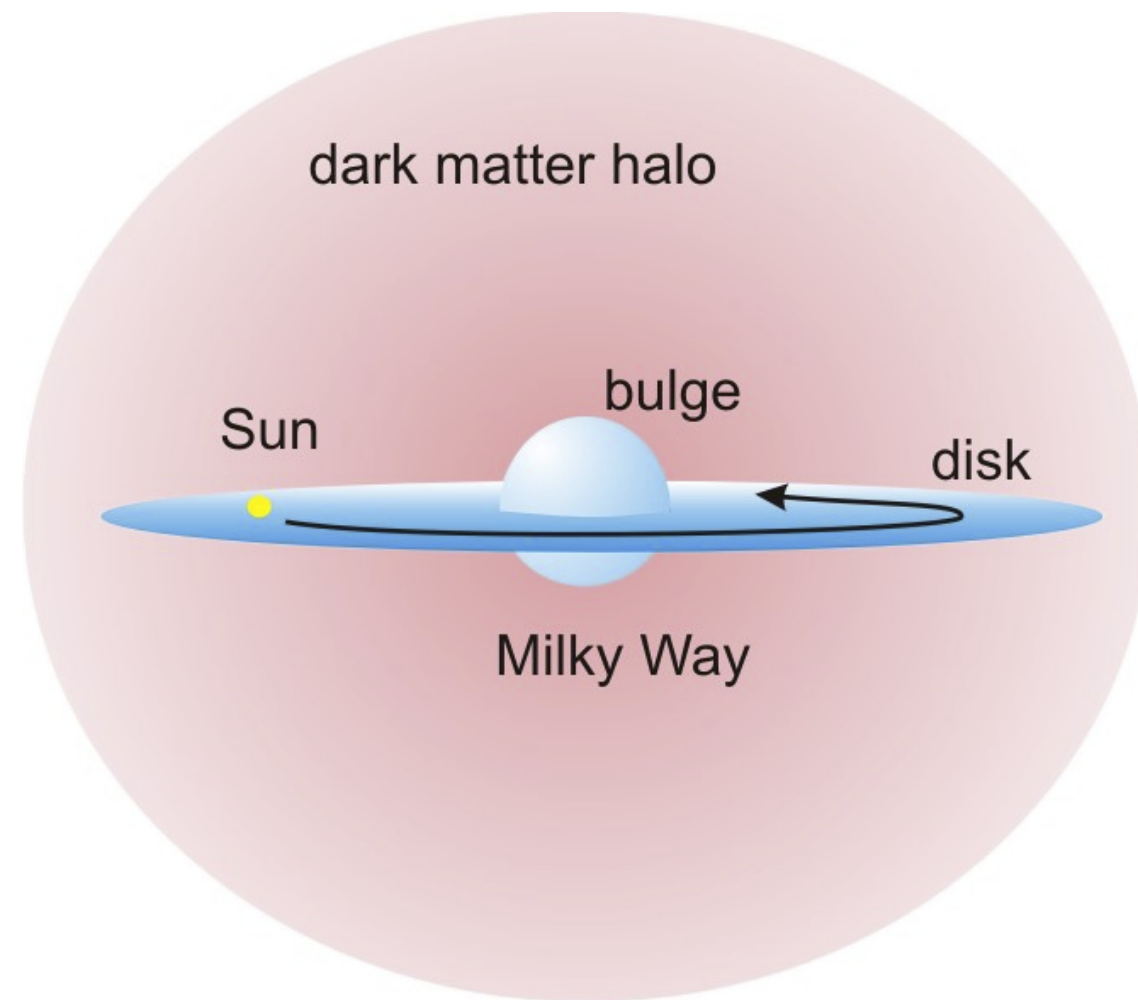
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**bosons**

# ULDM does not behaves like CDM at small-scales



$$\mathcal{L} = \frac{1}{2} \left[ (\partial_\mu \phi)^2 - m^2 \phi^2 \right] + \text{gravity}$$

$$\lambda_{dB} \sim \frac{10^{-22} \text{eV}}{m} \frac{10^{-3}}{v} \text{kpc}$$

Close to  $\lambda_{db}$

In terms of **fluid variables (e.g.  $\rho \propto m^2 \phi^2$ )**:

gravitational potential

$$\phi_k \sim e^{i(\omega t - kx)}$$

**Virialized configuration:** collection of waves with distribution determined by properties from the galaxy

$$\phi \propto \int_0^{v_{max}} d^3v e^{-v^2/\sigma_0^2} e^{i\omega_v t} e^{-im\vec{v}\cdot\vec{x}} e^{if_{\vec{v}}} + c.c.$$

$$\sigma_0 \sim 10^{-3} c \quad \text{in the MW}$$

free wave

The DM potential has coherent oscillations in  $\lambda_{db}$

$$t \sim \frac{10^6}{m} \left( \frac{10^{-6}}{\sigma_0^2} \right)$$

$$\begin{aligned} \dot{\rho} + 3H\rho + \frac{\nabla}{a} (\rho \vec{v}) &= 0 \\ \dot{\vec{v}} + H\vec{v} + \left( \vec{v} \cdot \frac{\nabla}{a} \right) \vec{v} &= -\frac{\nabla}{a} \left( V + \frac{1}{2m^2 a^2} \frac{\nabla^2 \sqrt{\rho}}{\sqrt{\rho}} \right) \end{aligned}$$

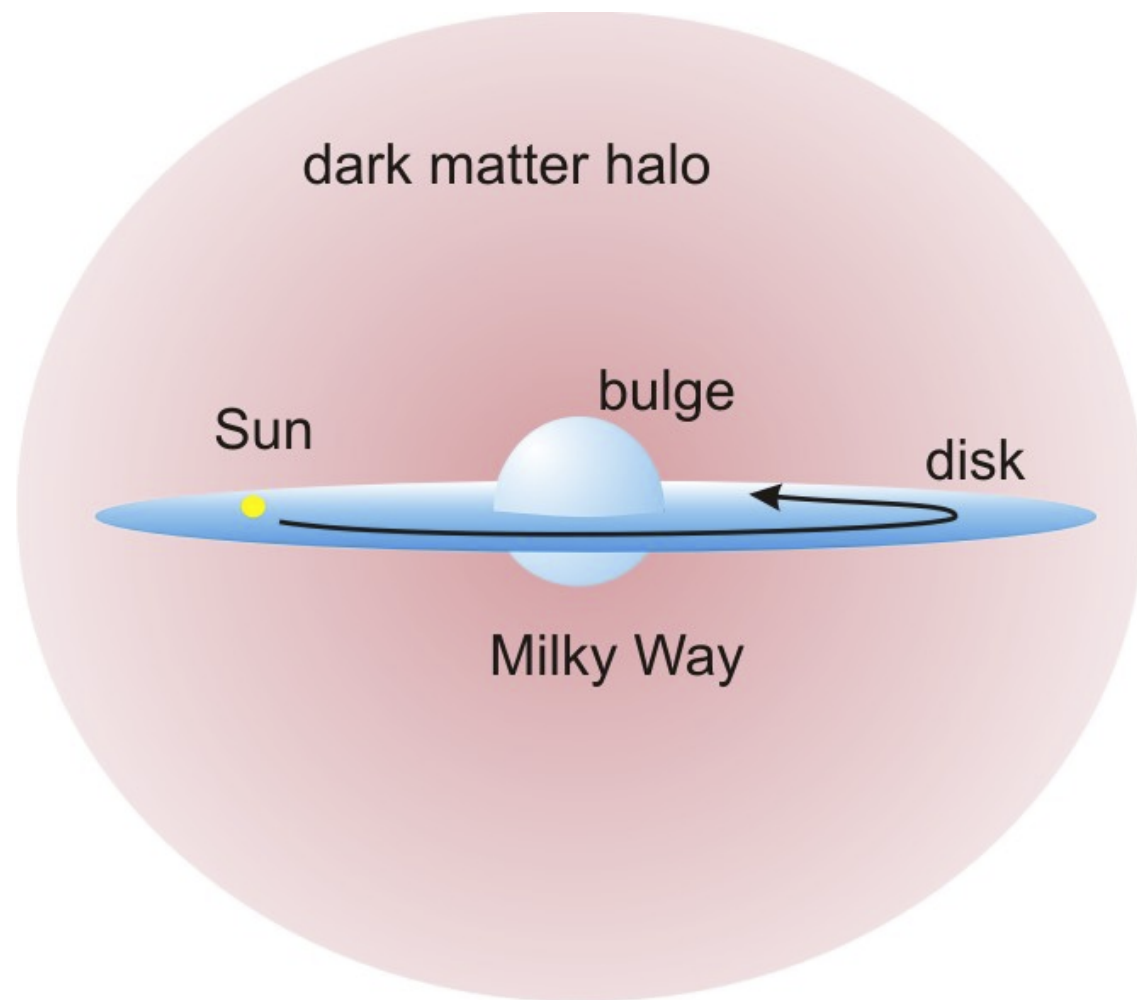
pure CDM part

new phenomena at small scales!

(repulsive effect: "quantum pressure")

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**A) coherent oscillations +  
B) stochastic 'narrow' piece**

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**C) changes dynamics at smaller scales**

$$\frac{10^{-3}}{v} \text{kpc}$$

# New phenomenology from ULDM

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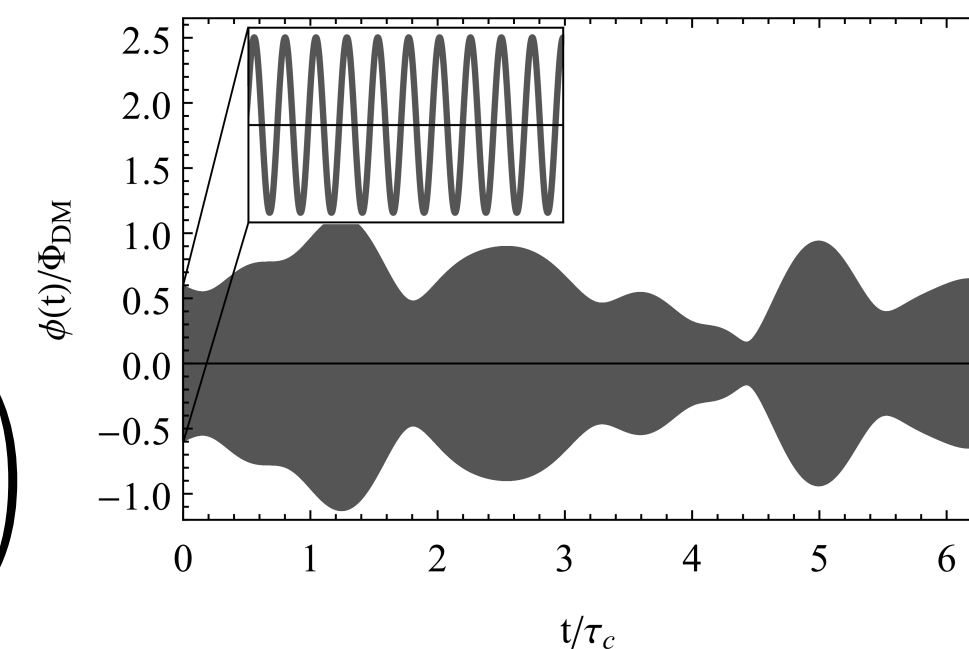
Centers et al 19

**DM halo**

$$\phi \propto \int_0^{v_{max}} d^3v e^{-v^2/\sigma_0^2} e^{i\omega_v t} e^{-im\vec{v}\cdot\vec{x}} e^{if\vec{v}} + c.c.$$

**A) coherent oscillations**

$$\omega \sim m \approx \frac{m}{10^{-22} \text{ eV}} \frac{1}{76 \text{ days}} \quad t \sim \frac{10^6}{m} \left( \frac{10^{-6}}{\sigma_0^2} \right)$$



$$\phi \approx \phi_0 \cos(\omega t + \psi_0)$$

**SM-DM interactions**

$$\phi F_{\mu\nu} \tilde{F}^{\mu\nu}$$

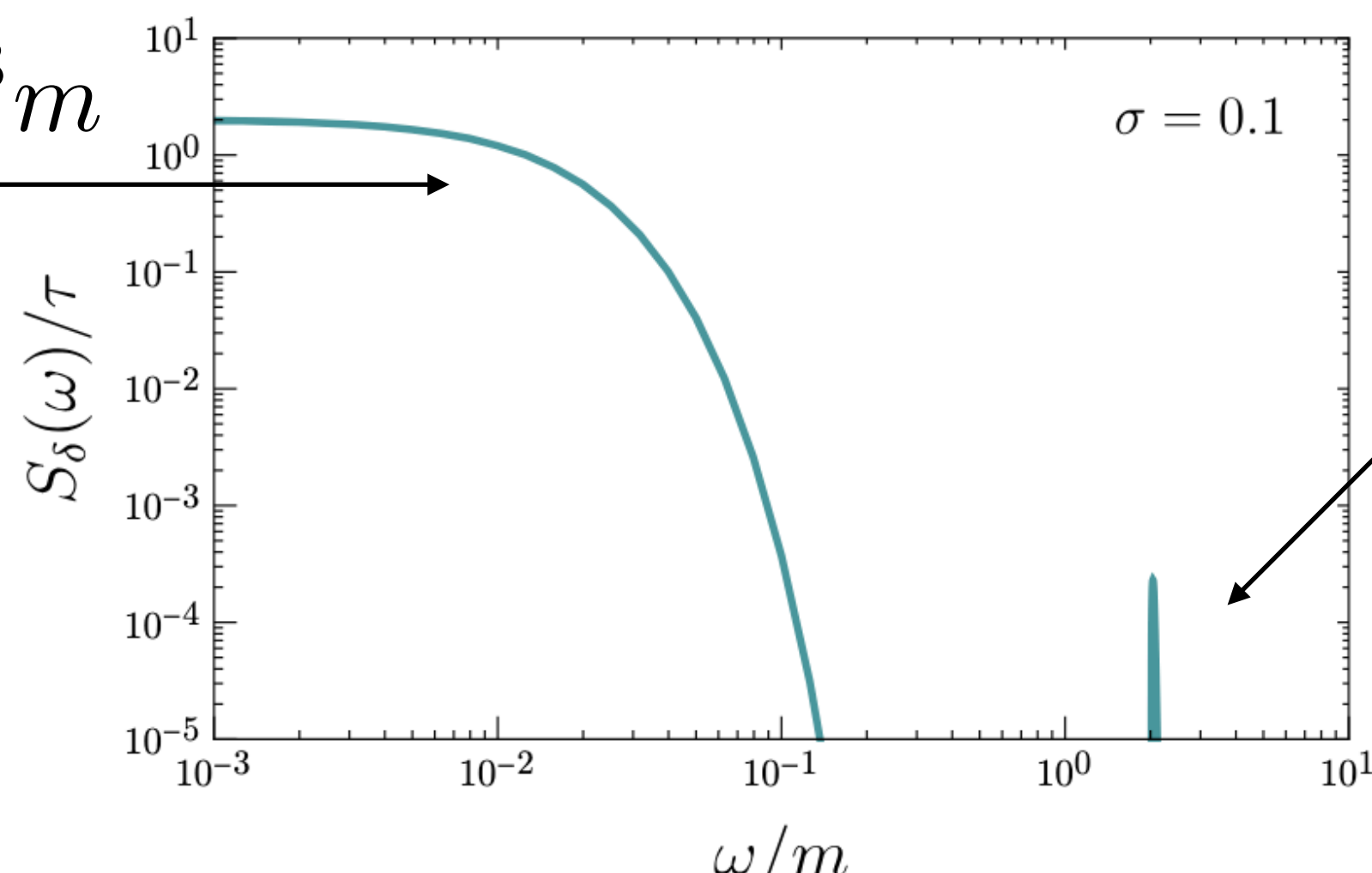
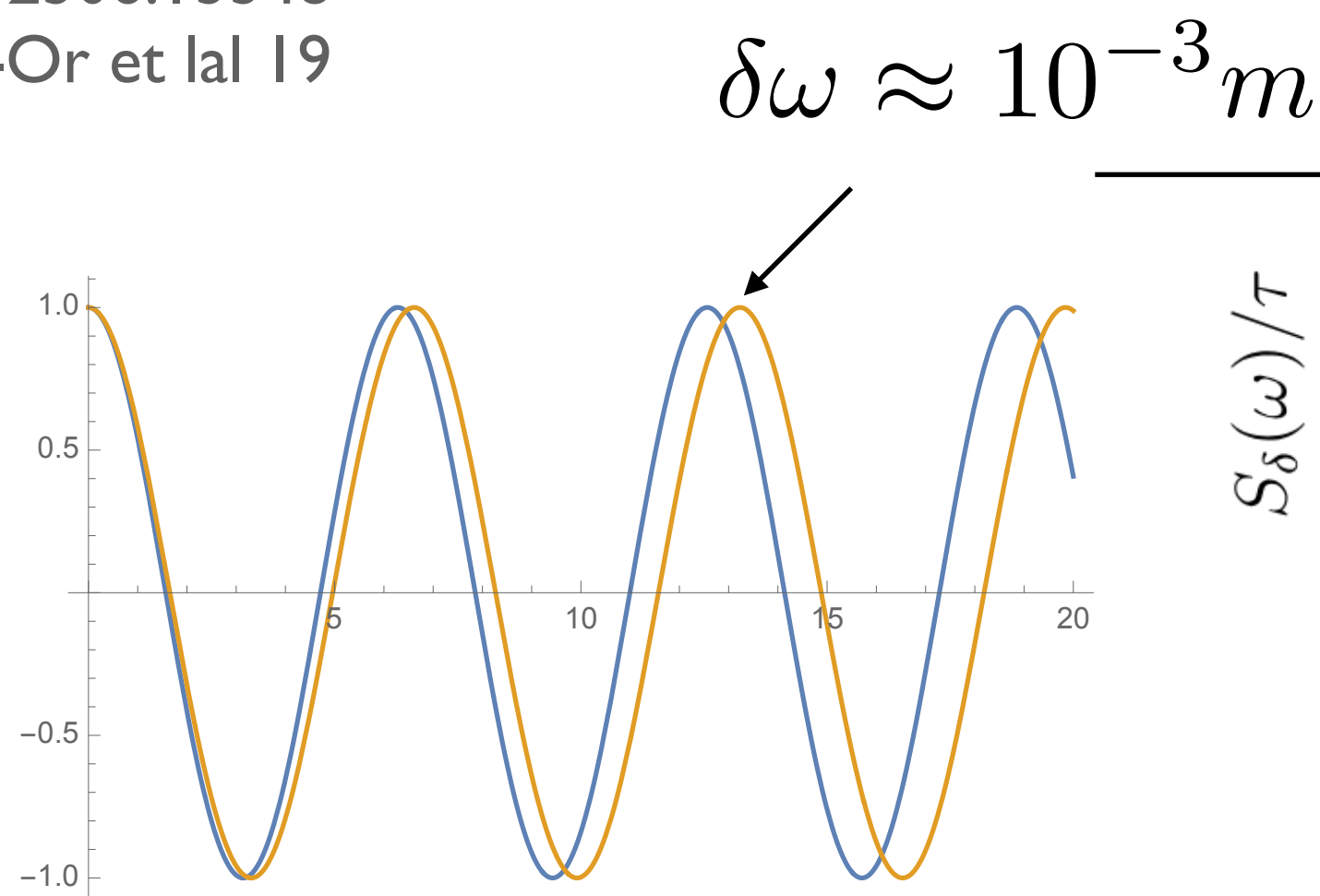
$$m_{\text{SM}} \phi \psi_{\text{SM}}^2$$

**B) stochastic 'narrow' piece**

$$\sim \langle \phi^* \phi \rangle$$

these fluctuations  
heat, decorrelate (interf),  
friction

Kim 2306.13348  
Ban-Or et al 19



$$\omega = 2m$$

Marsh, Niemeyer 18  
Dalal, Kravtsov 22  
Ban-Or et al 19  
Bar-Or et al 1809.07673





# New phenomenology from ULDM: 3 examples

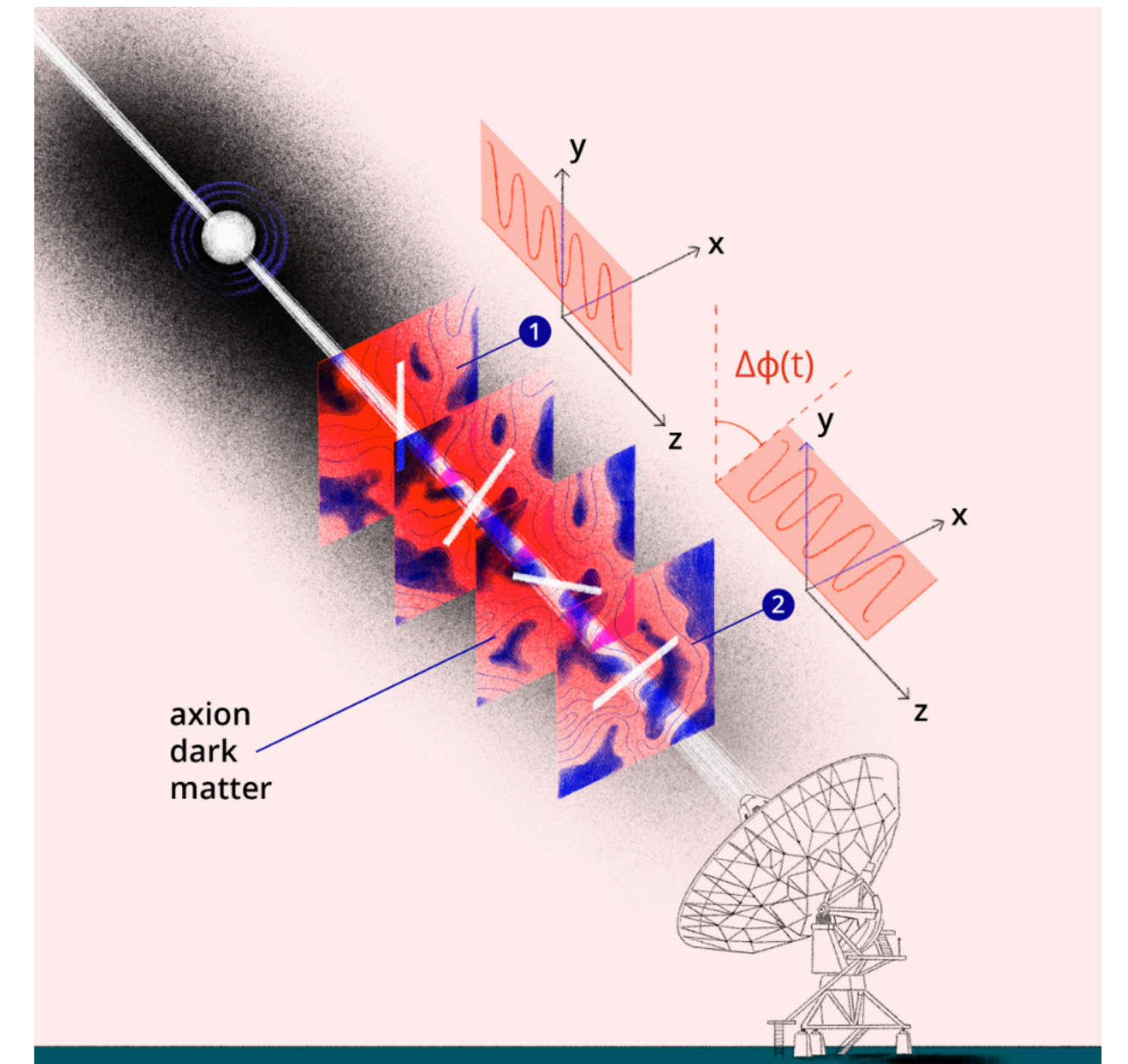
## A) coherent oscillations

Searching for dark-matter waves with PPTA and QUIJOTE pulsar polarimetry

Andrés Castillo (Laguna U., Tenerife), Jorge Martín-Camalich (Laguna U., Tenerife), Jorge Terol-Calvo (Laguna U., Tenerife), Diego Blas (Barcelona, Autònoma U. and Barcelona, IFAE), Andrea Caputo (Tel Aviv U. and Weizmann Inst.) et al. (Jan 10, 2022)

$$\mathcal{L} = \frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \frac{g_{a\gamma}}{4} a F_{\mu\nu} \tilde{F}^{\mu\nu} + \frac{1}{2} (\partial_\mu a \partial^\mu a - m_a^2 a^2)$$

$$a = a_0 \cos(mt + \psi_0)$$



Huge landscape of possibilities

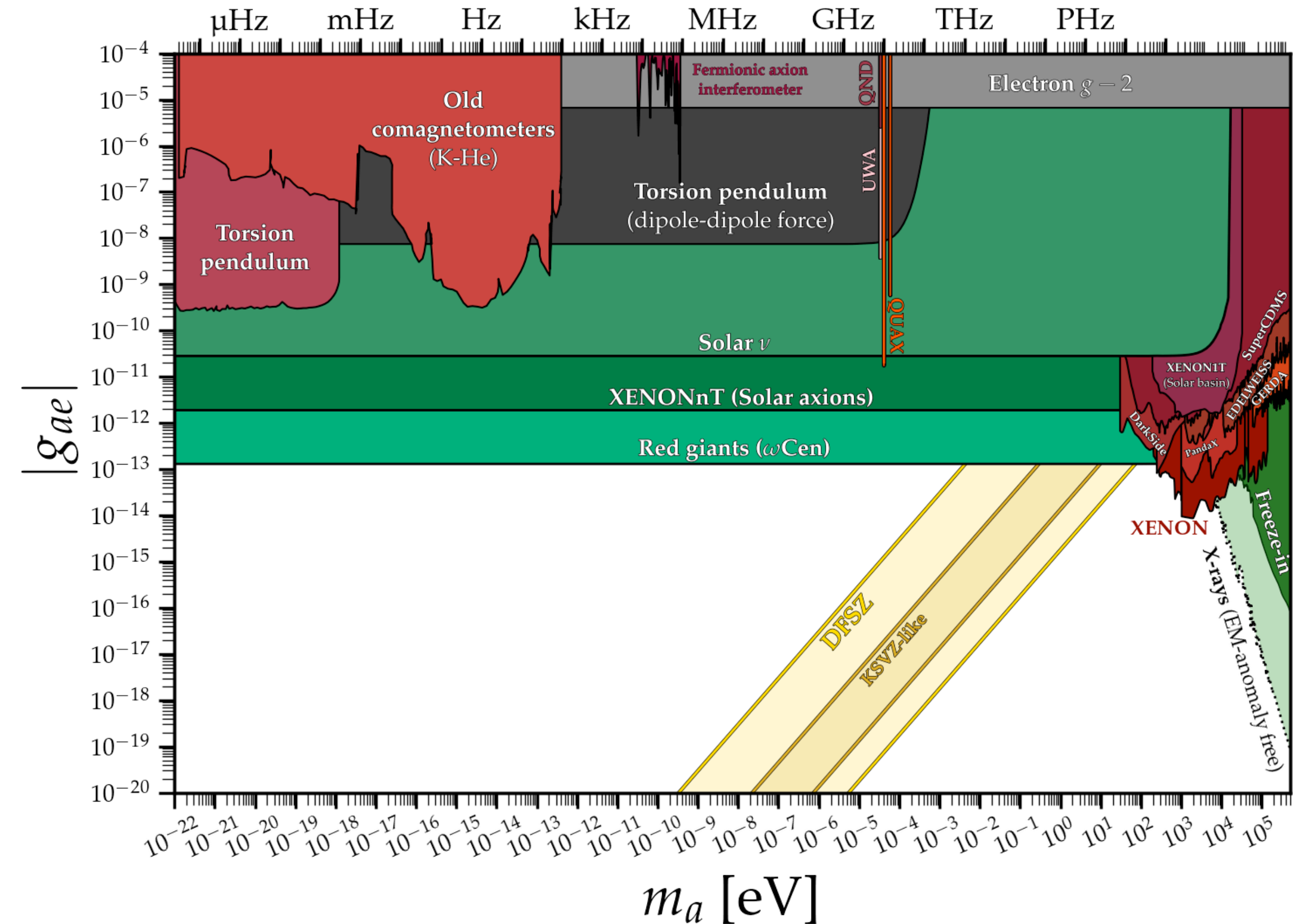
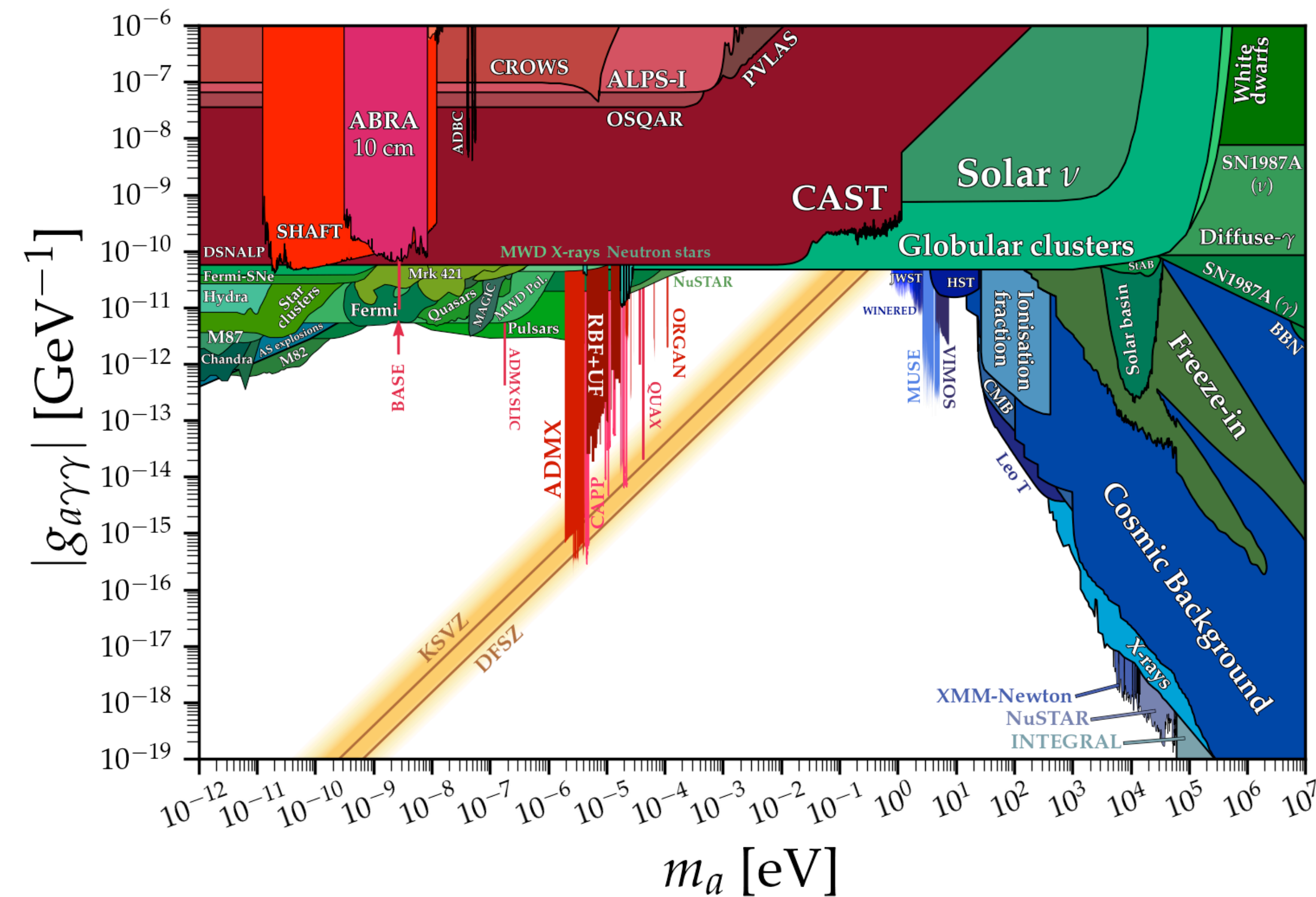
$$\mathcal{L}_{\text{int}} = \frac{\phi}{\sqrt{2}} \left( \frac{d_e}{4\mu_0} F_{\mu\nu} F^{\mu\nu} - \frac{d_g \beta_3}{2g_3} G_{\mu\nu}^a G^{a\mu\nu} - \sum_{i=e,u,d} (d_{m_i} + \gamma_{m_i} d_g) m_i \bar{\psi}_i \psi_i \right),$$

# New phenomenology from ULDM: 3 examples

## A) coherent oscillations

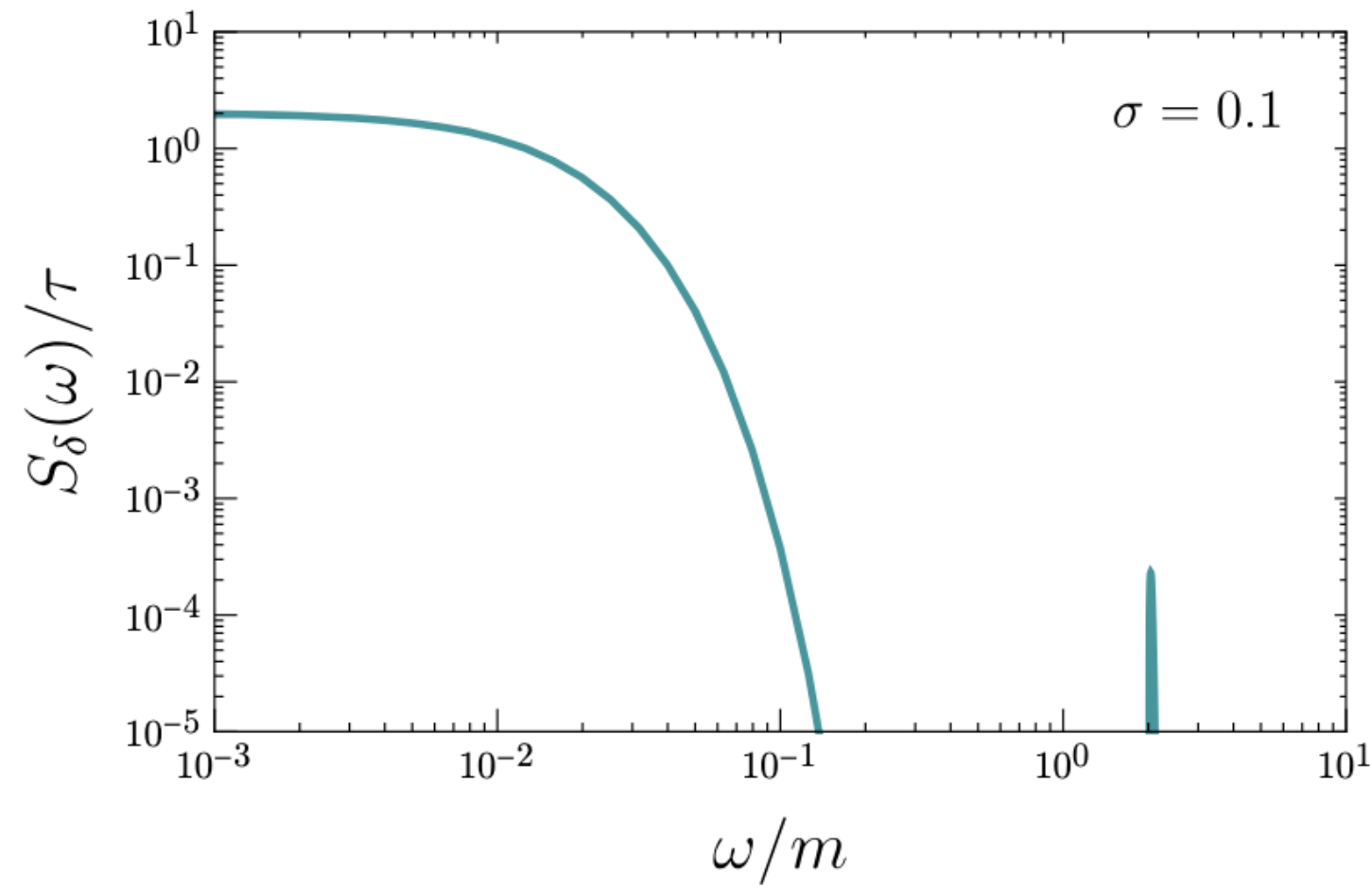
<https://cajohare.github.io/AxionLimits/>

Huge landscape of possibilities



# New phenomenology from ULDM: 3 examples

## B) stochastic 'narrow' piece

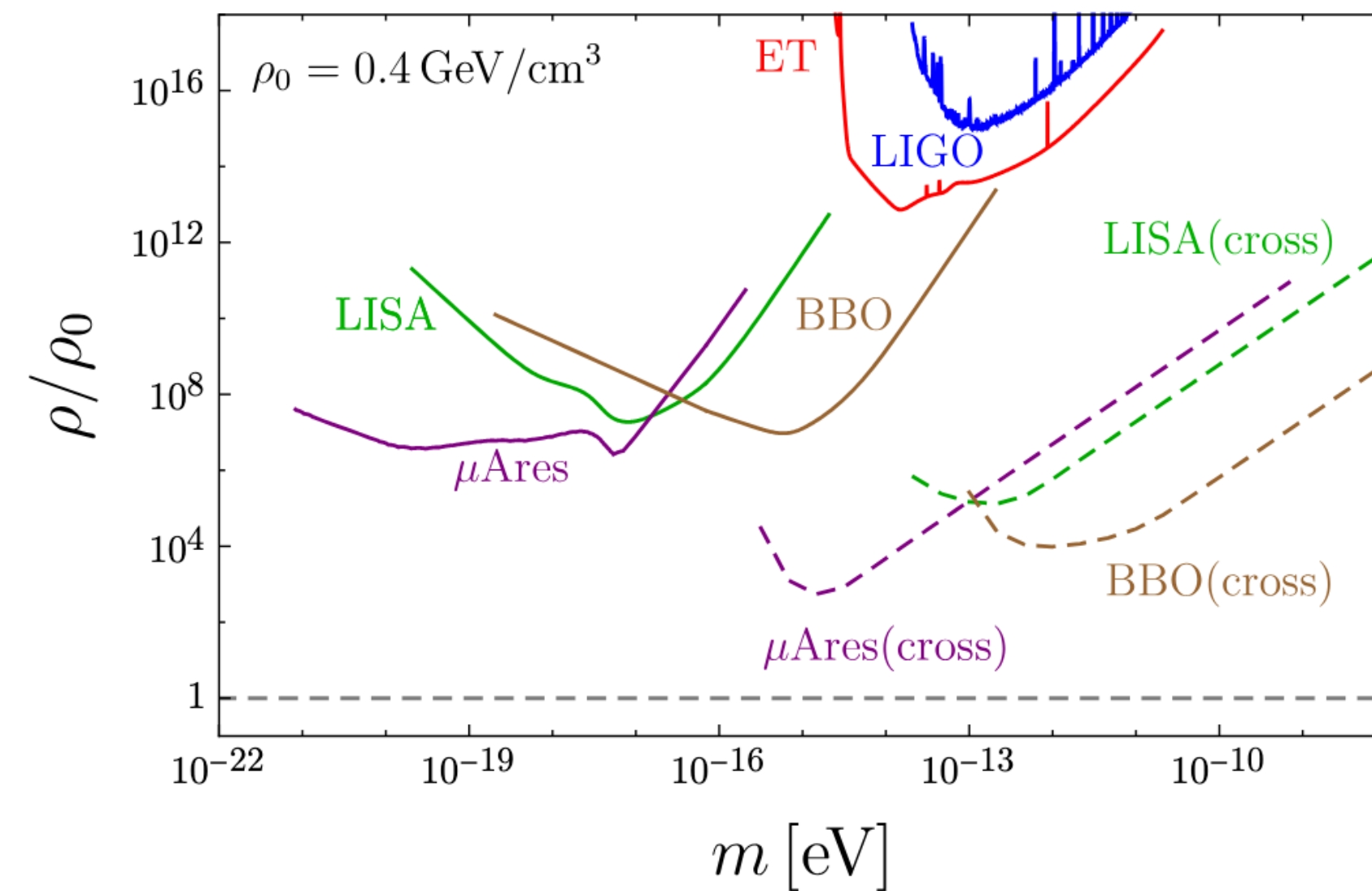
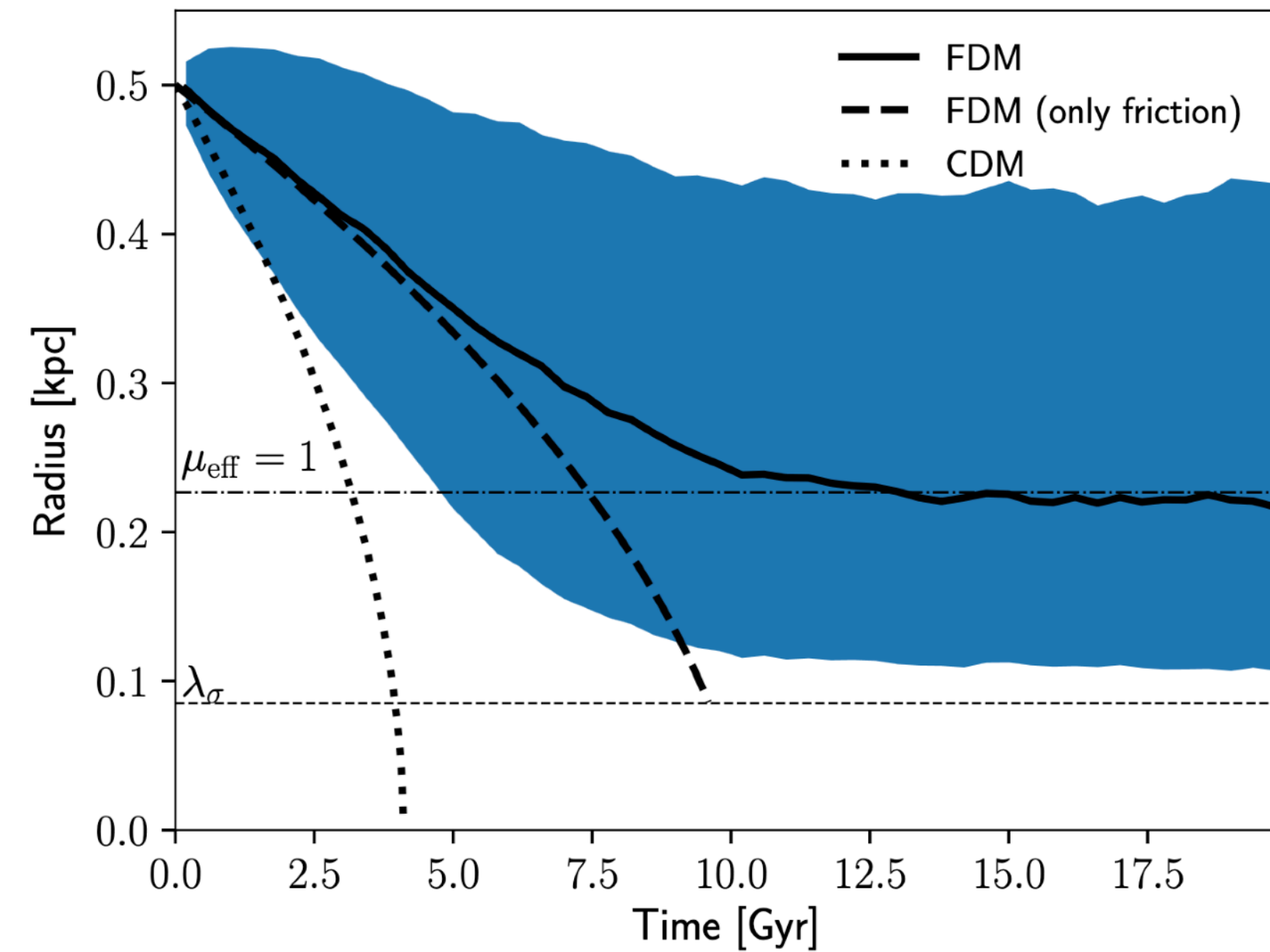
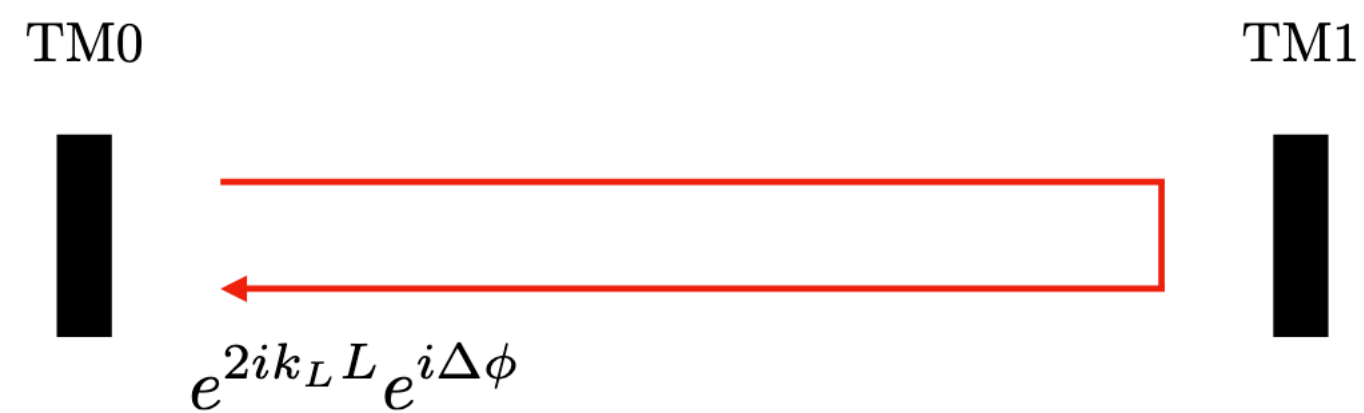


Bar-Or et al 1809.07673

*Stalling of dynamical friction*

Kim 2306.13348

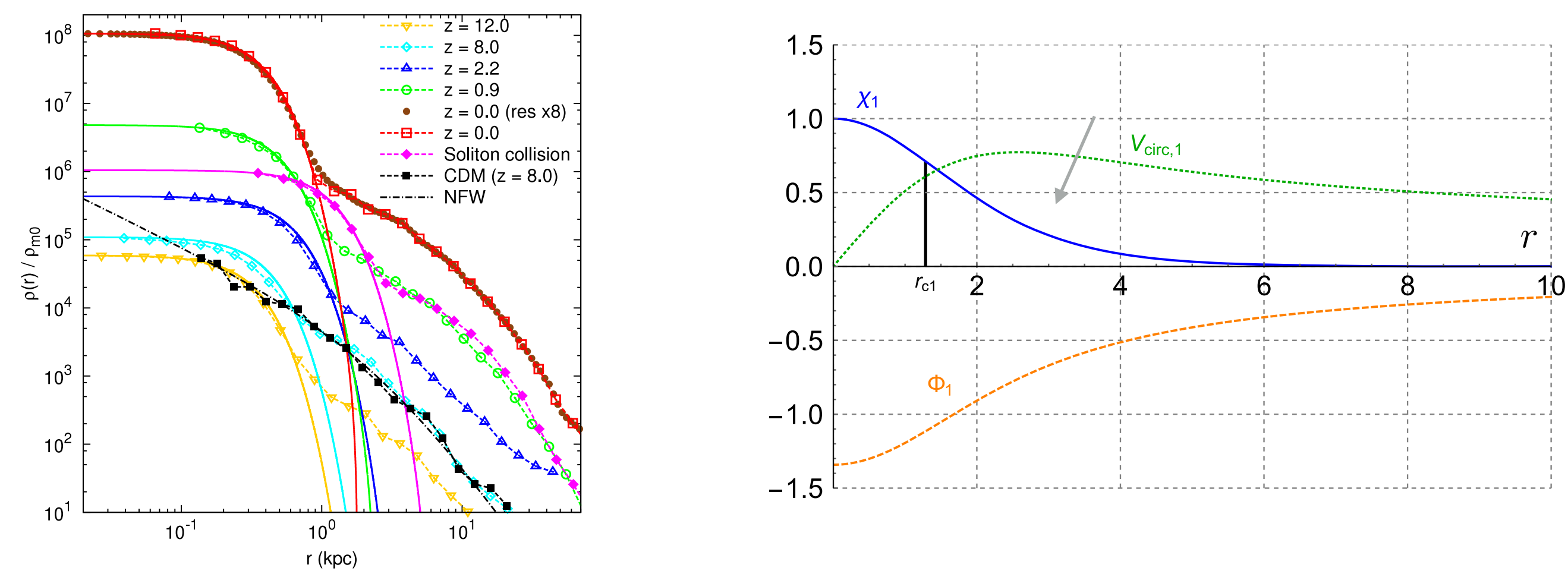
*Impact on interferometers*



# New phenomenology from ULDM: 3 examples

## C) changes dynamics at smaller scales

Velocity curves in the presence of solitons



Modulation of signals of known spectrum

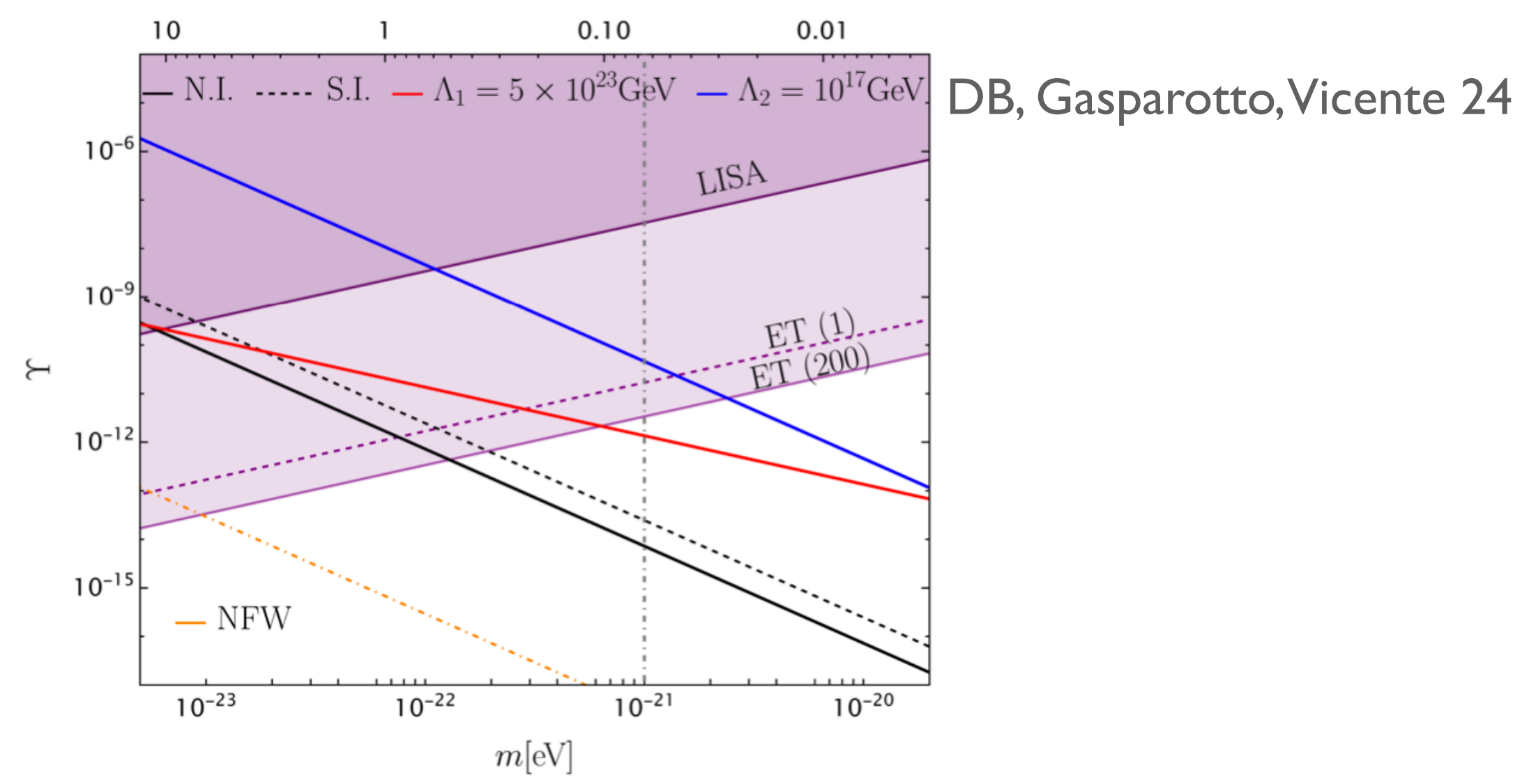
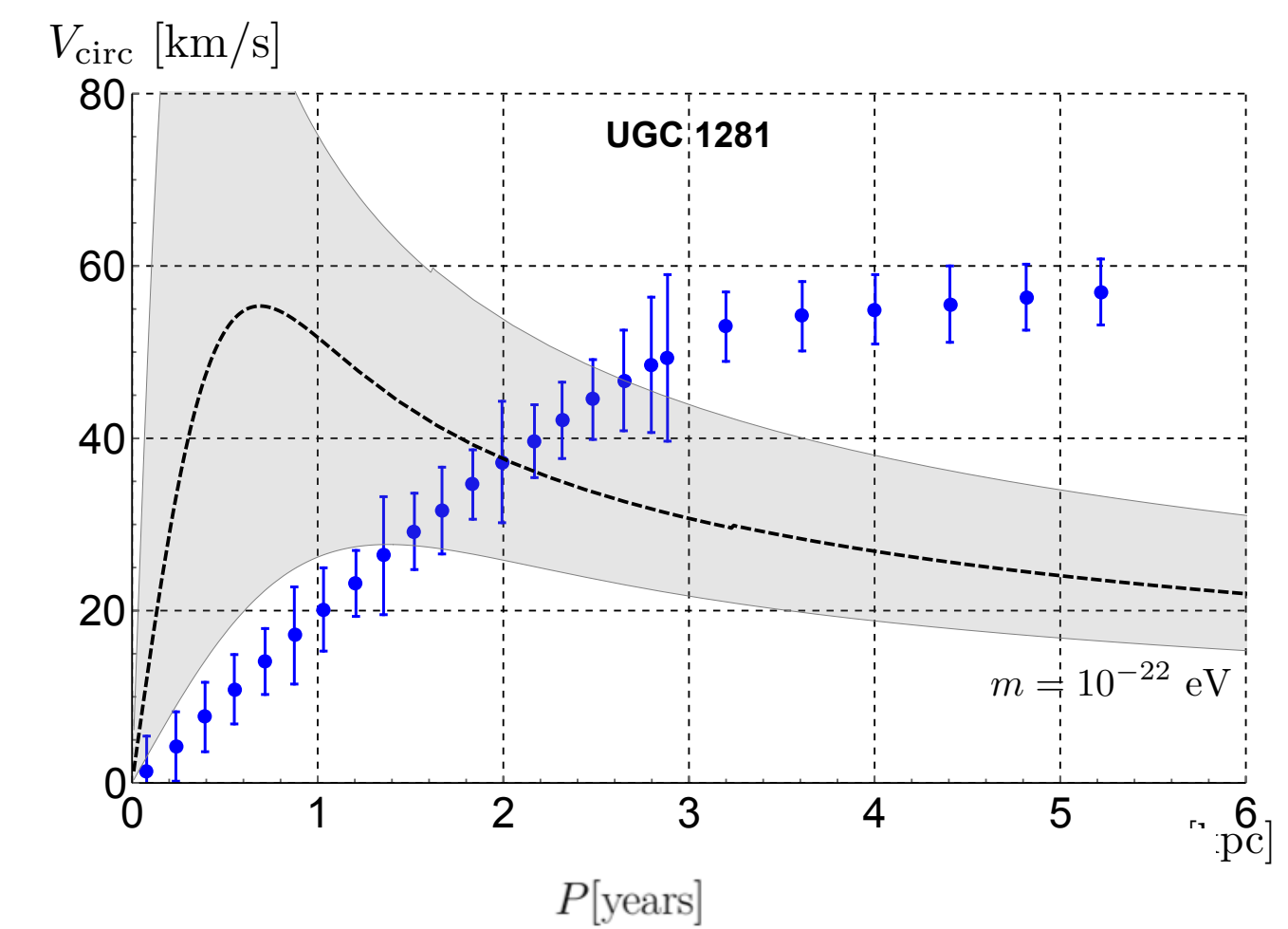
Time depending gravitational redshift

$$\frac{\Delta\omega_e}{\omega_e} \simeq \Phi \Big|_e^r + n^i v_i \Big|_e^r - I_{iSW} \text{ where}$$

$$I_{iSW} = (\Phi + \Psi) \Big|_e^r + n^i \int_e^r \partial_i(\Phi + \Psi) d\lambda$$

Sources at the center include **LISA** binaries!

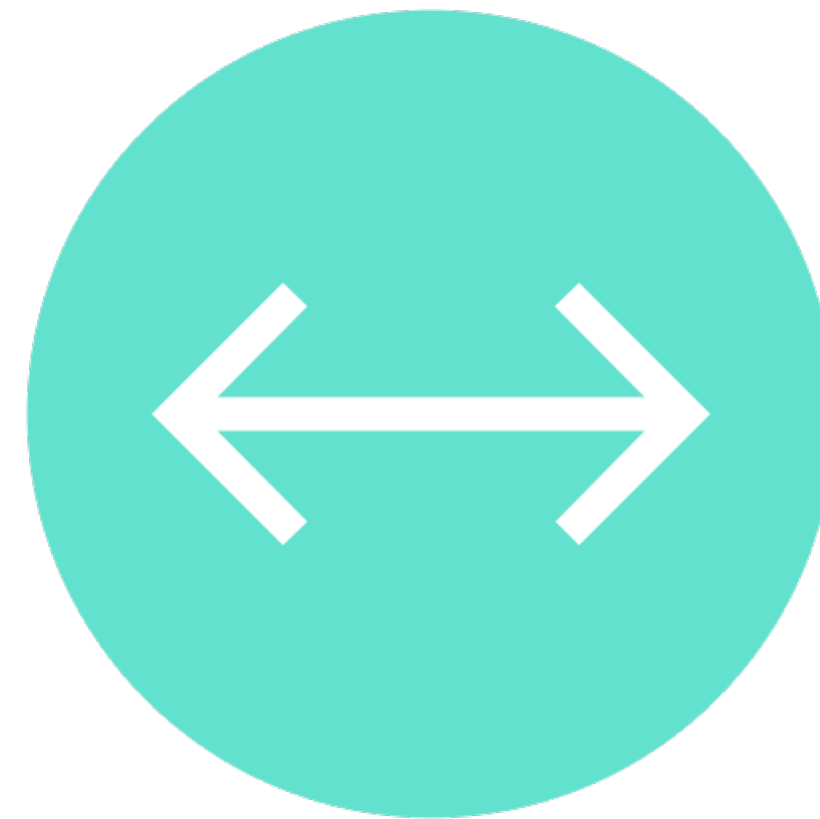
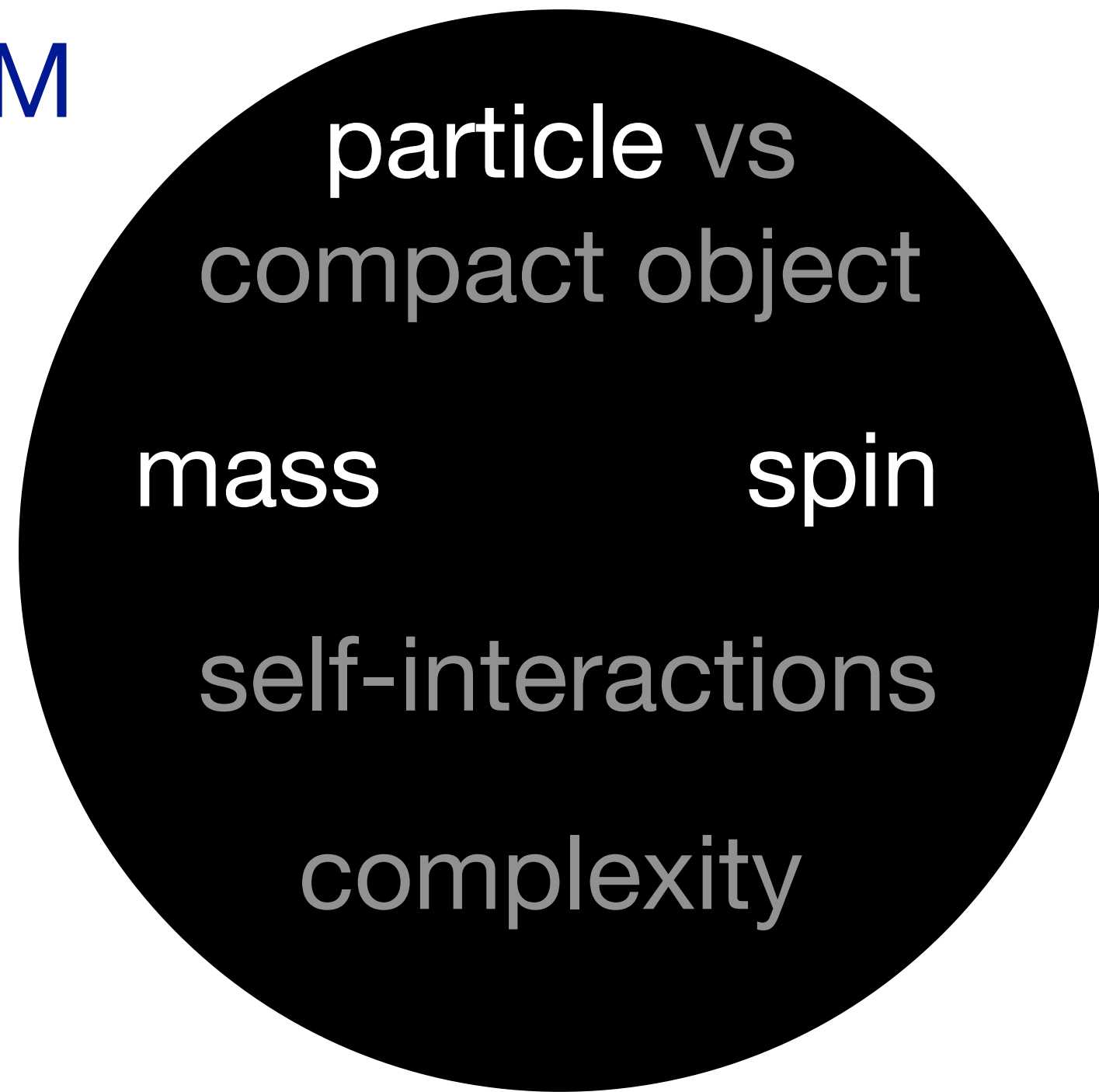
$m \sim 10^{-22}$  eV Bar, DB, Blum, Sibiryakov 1805.00122



DB, Gasparotto, Vicente 24

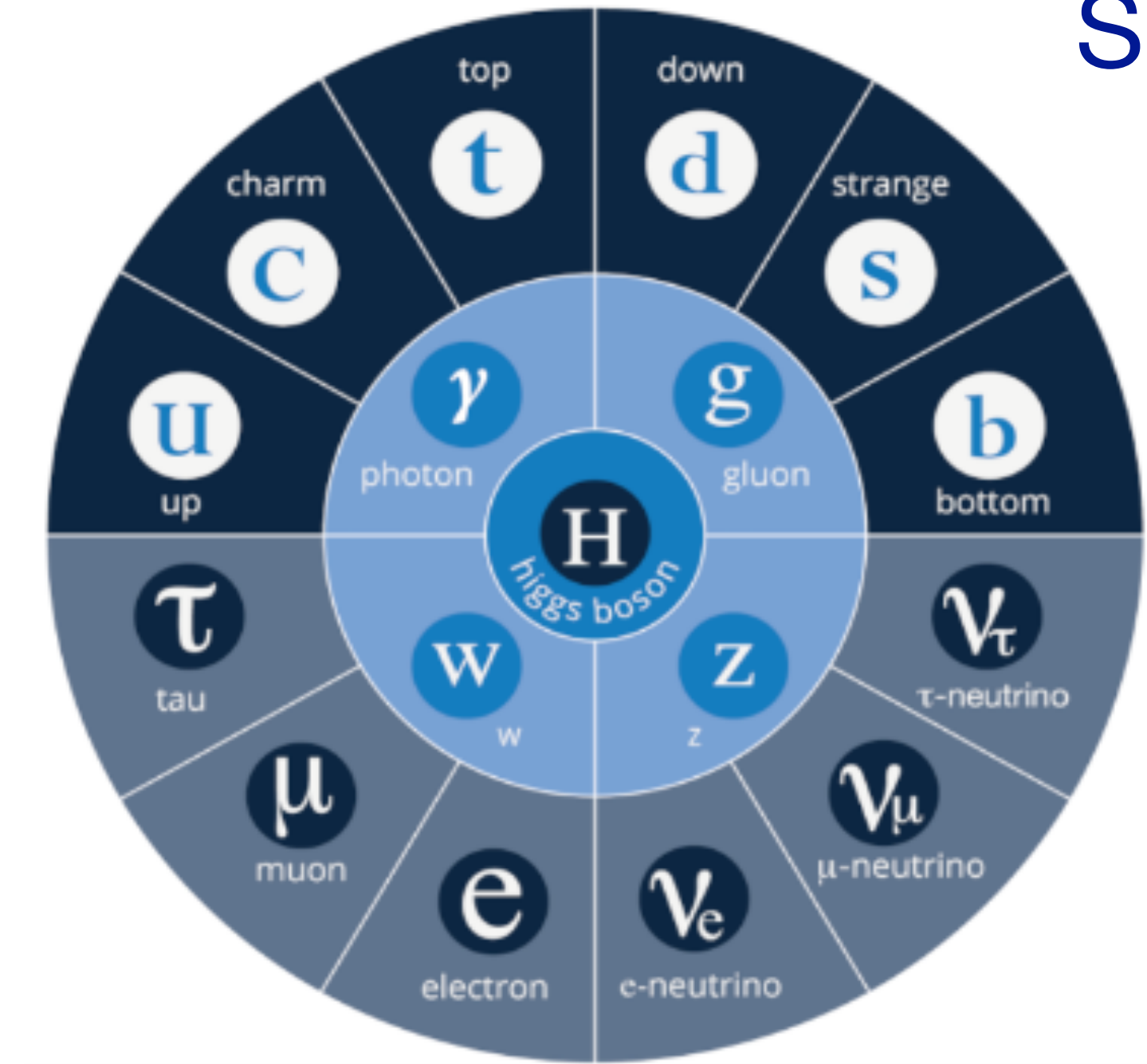
# What can we look for

DM

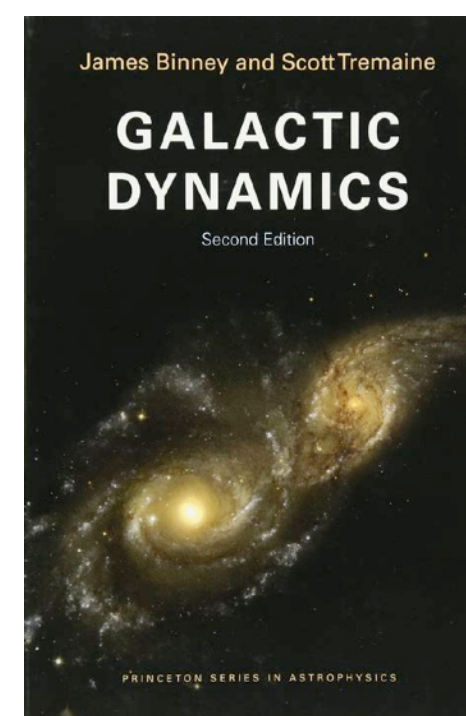
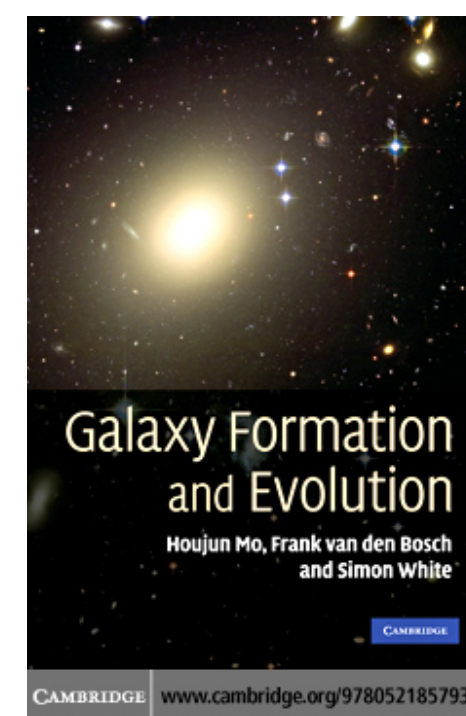
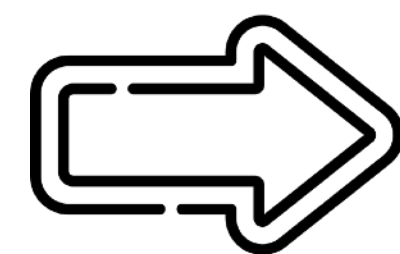
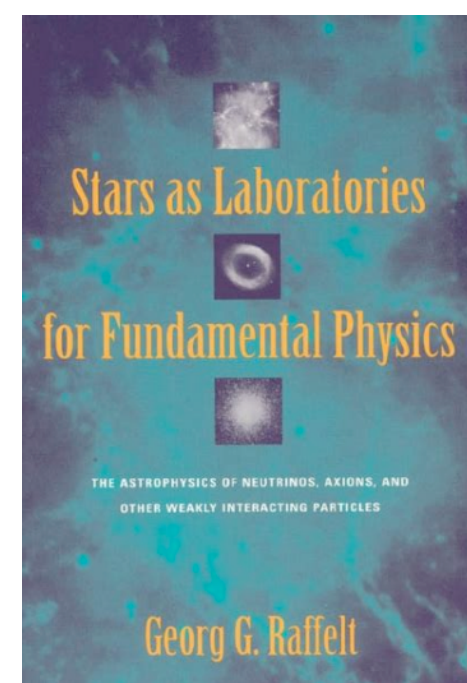


SM-DM interactions

SM



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# Conclusions

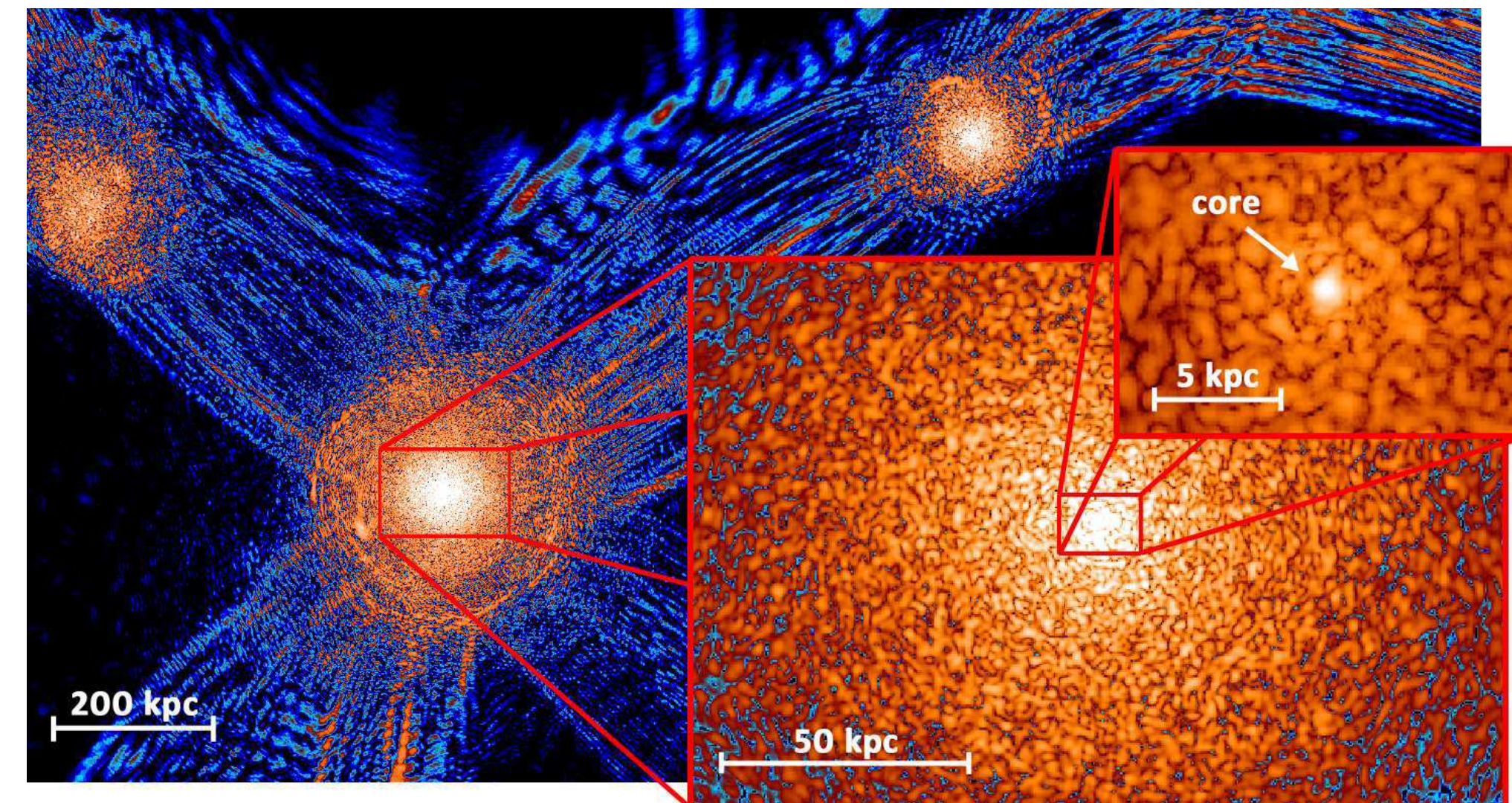
*Ultra-light* bosonic DM (or light fermionic DM)

- Includes new dynamics that open new phenomenological windows
- Two directions
  - explore all possible masses, with different time scales
  - explore direction of possible couplings

**A) coherent oscillations**

**B) stochastic 'narrow' piece**

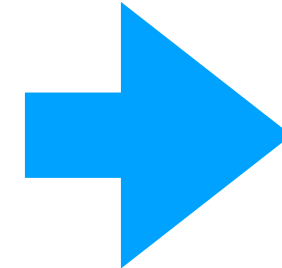
**C) changes dynamics at smaller scales**



# Properties of the soliton

$$\phi(x, t) = \frac{1}{\sqrt{2m}} e^{-imt} \psi(x, t) + c.c.$$

$$v \ll c, \omega \ll m$$



$$i\partial_t \psi = -\frac{1}{2m} \Delta \psi + m\Phi_N \psi$$

$$\Delta \Phi_N = 4\pi G |\psi|^2$$

spherically symmetric stationary, non-relativistic solution:

e.g. Bar, DB, Blum, Sibiryakov 18

$$\phi(x, t) = \frac{M_{pl}}{2\sqrt{2\pi}} e^{-imt} e^{-i\gamma t} \chi(x) + h.c.$$

scaling solution

$$\chi_\lambda(r) = \lambda^2 \chi_1(\lambda r)$$

$$x_{c\lambda} = \lambda^{-1} x_{c1}$$

$$M_\lambda = \lambda M_1$$

$$\gamma_\lambda = \lambda^2 \gamma$$

$$\rho_{c\lambda} = \lambda^4 \rho_{c1}$$

What fixes  $\gamma$ ?

