From Evaporation to Eternity: How Memory Burden Alters Primordial Black Hole Constraints

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Dark matter: where to look?





Dark matter: where to look?





How Special Are Black Holes?

1.Their entropy satisfies the **area law**:

2.They exhibit a (semiclassical) information ho

3.Decay rate is thermal and they have temperature

4. Time-scale required for beginning of the **info** $t_{min} = SR \sim$

5.Their **spin** is bounded

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tion **horizon**.

$$T \sim \frac{1}{R}$$
prmation retrieval is
$$\frac{R^3}{M_p^{-2}} \sim \frac{Volume}{M_p^{-2}}$$

 $J^{max} = S$

S. W. Hawking, 75. D. N. Page, 93.

How Special Are Black Holes?

Does the area law entropy bound extend beyond gravity?

•What is its underlying meaning?



The entropy bound is imposed by **unitarity**

G. Dvali, arXiv:2003.05546. G. Dvali, arXiv:2107.10616

Saturated States: Saturon

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High information storage capacity

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Memory burden effect

G. Dvali, arXiv:1810.02336 [hep-th]; G. Dvali, L. Eisemann, M. Michel, S. Zell, arXiv:2006.00011 [hep-th] The essence of the effect: **Information carried by an object stabilizes it.**



Gapless "memory modes" (Goldstones) live only inside

This has consequences for PBHs DM.

The modes outside are highly gapped. Due to this, information stored in memory modes cannot escape for a long time. This leads to backrection on the configuration itself.

Memory burden is prominent in systems with high information-storage capacity such as black holes.

G. Dvali, J.S.V.B., M. Zantedeschi, arXiv:2405.13117 [hep-th] M. Zantedeschi, L. Visinelli arXiv:2410.07037 [astro-ph.HE]



Memory burden effect

Imagine a room. Inside the room information is written in ladybirds, and outside in elephants.



- AND, NO-LADYBIRD-ZONE OUTSIDE!

State $(0, 3, 3, 0, 0, 3, \dots)$ is much less costly in energy than $(0, 10, 10, 10, 0, 10, 10, \dots)$

Memory burden effect

If the room decays, information cannot escape, because ladybirds cannot live outside and elephants cost very high energy!

Due to this, the room gets stabilized by the burden of memory stored in ladybirds.







State $(0, 3, 3, 0, 0, 3, \dots)$ is much less costly in energy than $(0, 10, 10, 10, 0, 10, \dots)$



A toy model: Saturon as a Vacuum Bubble

Vacuum bubble with high information-storage capacity

- d = 3 + 1
- ϕ in the adjoint representation of SU(N) global symmetry
- $\bullet N \gg 1$
- Theory is renormalizable

$$\mathscr{L} = \frac{1}{2} \operatorname{Tr} \left[(\partial_{\mu} \phi) (\partial^{\mu} \phi) \right] - V[\phi]$$
$$V[\phi] = \frac{\alpha}{2} \operatorname{Tr} \left[\left(f\phi - \phi^2 + \frac{I}{N} \operatorname{Tr}[\phi^2] \right) \right]^2$$

Unitarity requires: $\alpha N \leq 1$

Validity domain of QFT description in terms of ϕ



Vacuum bubble with high information-storage capacity



 $\Phi_{\rm D} \propto \varphi(r)$



Vacuum bubbles:

 $\phi = U^{\dagger} \Phi_{\rm D} U$

- $U = \exp\left[-i\,\theta\,T\right]$
- *T* corresponds to broken generator

 $\theta = \omega t$

- • $\varphi(r)$ is order parameter localizing bubble (Goldstone) region
- Their number correspond to charge $N_{\text{Gold}} = Q$

Some similarities with U(1) Q-balls construction

Vacuum bubble with high information-storage capacity G.Dvali, O. Kaikov, J.S.V.B, '21; G.Dvali, J.S.V.B., M. Zantedeschi, '24. $|\operatorname{Pattern}\rangle = |n_1, n_2, \dots, n_N\rangle$ With: $\sum_{N=1}^{N} n_a = N_{\operatorname{Gold}} = Q$ This stabilizes the bubble

Bubbles rotated by relative SU(N) transformations: $\Phi \rightarrow U^{\dagger}\Phi U$ Due to Goldstone modes, each bubble exhibits an exponentially high microstate degeneracy $S = \log n_{\text{states}}$

$$n_{\text{states}} \simeq \left(1 + \frac{2N}{N_{\text{Gold}}}\right)^{N_{\text{Gold}}} \left(1 + \frac{N_{\text{Gold}}}{2N}\right)^{N}$$

Example of bubble dynamically stabilized by memory.

Vacuum bubble stabilisation

 $\dot{\boldsymbol{ heta}} = \mathbf{0}$



 $\dot{\boldsymbol{\theta}} = \boldsymbol{\omega}$



- The bubble without memory (left panel) simply annihilates (zero charge).
- The bubble with charge central and right panel is stabilized.
- The stabilisation is independent on other d couplings to new degrees of freedom.

mply annihilates (zero charge). panel - is stabilized.

• The stabilisation is independent on other details such as vorticity, width of the bubble wall or

n³ 0.4 0.3 0.2 0.1



- storing information
- Presence of information horizon in Goldstone flavour space
- configuration

• Charge is conserved within 1%. These configurations are, in fact, highly efficient at

• Different asymptotic energies depending on the initial information stored in the

G. Dvali, J.S.V.B., M. Zantedeschi, '24

- Memory burden effects seems inevitable in all configurations with a high-information storage capacity, such as saturons.
- Black holes are indeed saturated configurations.
- It is therefore expected that black holes experience the memory burden effect.

holes are described in terms of condensate of marginally bounded gravitons

This is also supported by the so-called black hole N-portrait (Dvali, Gomez '11), where black

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After this point, the evaporation / decay is slowed down so that the lifetime is extended as:

modes as well as in the coupling, which scale as:

up for masses $10^3 g \lesssim M_{\text{PRH}} \lesssim 10^{14} g$.

Dvali, Eisemann, Michel, Zell, '21; Dvali, Kühnel, M. Zantedeschi, '21 Alexandre, Dvali, Koutsangelas, '24; Thoss, Burkert, Kohri, '24;

The detailed analysis shows that the memory burden effect sets-in latest by half-decay.

 $t \sim R S^{n+1}$

- n =positive integer. This is because the decay rate is analytic both in number of memory
 - $\alpha \sim 1/S$, $N_{\text{Gold}} \sim S$

Already for n = 1 - seemingly the most motivated value - new window for PBHs DM opens

 $|\operatorname{Pattern}\rangle = |n_1, n_2, .$

The spread in masses of stabilised remnants is determined by the statistical distribution of $N_{\rm G}$ among the initial black holes. Assuming no energy bias



...,
$$n_S$$
 With: $\sum_{a}^{S} n_a = N_G$

$$\mathcal{P}_{N_{\rm G}} = 2^{-S} \frac{S!}{(S - N_{\rm G})!N_{\rm G}!}$$

which is maximal for $N_{\rm G} \simeq S/2$, $\mathcal{P}_{S/2} \sim 1/\sqrt{S}$, while the width is $\sqrt{S/2}$.

On the other hand, for $N_G \ll S$, the probability is exponentially suppressed as,

$$\mathcal{P}_{N_{\rm G}\ll S} \sim 2^{-S} \left(\frac{S\,{\rm e}}{N_{\rm G}}\right)^{N_{\rm G}}$$

Consequences for black holes as dark matter



- A new mass window for dark-matter PBHs stabilised by their memory opens up below 10^{14} g
 - In such mass widnow, PBHs are normally discarded as potential dark matter candidates because they are naively tooshort lived. However memory burden effect stabilizes them.
 - Novelty of our work: any initial distribution in such region will observe a natural spread, of width of order initial mass, on time scales longer than the memory burden back reaction time *t*_M
 - An example of this is depicted in the figure. Shaded areas denote existing constraint, while dotted lines correspond to two monochromatic distribution of mass M_* formed at time t_f
- The distribution in the light mass region, is stabilised and spread by the memory burden effect, resulting in the pictorially denoted dashed-red distribution at late times





Consequences for black holes as dark matter



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 $m_{\rm PBH}[g]$

M. Zantedeschi, L. Visinelli, '24



Thank you

Backup

Vorticity in saturons

G. Dvali, F. Kühnel, M. Zantedeschi, PRL 129 (2022) 6, 06130

 $\theta = \omega t + n \varphi$

Profile for n = 1

Construction has similarities with spinning U(1) Q-ball see Volkov, Wohnert '02

There is a way to spin a saturon bubble in an axial-symmetric way: Vorticity

winding number = $n = 0, \pm 1, \pm 2, \dots, \varphi$ = polar angle



Vorticity in saturons

	Saturon bubble	Black hole
Maximal spin	$S \\ n \sim \mathcal{O}(1)$	$S_{ m BH}$

- Saturon of a renormalizable QFT and black holes obey the same bound on spin
- Microscopic interpretation of extremality bound in terms of vorticity
- nature of the vortex

• Topological explanation of the absence of Hawking (soft) radiation due to macroscopic integer

• Can vorticity be a property manifesting in highly spinning black holes? If so, pheno consequences?

Vorticity in saturons

G. Dvali, O. Kaikov, J.S.V.B., F. Kühnel, M. Zantedeschi, '24 features emerge in black hole mergers?



Example: Study the impact of vorticity in saturated configurations. Could similar

 m^{-3}

- 0.4

0.3

- 0.2

- 0.1

• Due to the integer nature of the vortex, its emergence leads to macroscopic deviations in the emitted radiation.

1. Similar behaviours are expected in black hole mergers if vorticity localizes in the intermediate configuration.

Vacuum bubble with high information-storage capacity





 $\Phi_{\rm D} \propto \varphi(r) \, {\rm diag} \, (N-1, -1, -1, ..., -1)$



Memory burden in many body approach

G. Dvali, arXiv:1810.02336 [hep-th]; G. Dvali, L. Eisemann, M. Michel, S. Zell, arXiv:2006.00011 [hep-th];

Consider the following simple prototype Hamiltonian → Positive factor $n_{j}\hat{n}_{j} + \frac{\tilde{m}}{\sqrt{N_{\phi}}}\hat{b}^{\dagger}\hat{a}_{\phi} + \frac{\tilde{m}^{*}}{\sqrt{N_{\phi}}}\hat{a}_{\phi}^{\dagger}\hat{b} + m_{\phi}\hat{n}_{b}$

$$\hat{H} = m_{\phi} \hat{n}_{\phi} + \left(1 + \frac{\hat{n}_{\phi}}{N_{\phi}}\right)^{q} \sum_{j} m_{j}$$
Memory modes - C

Master mode - profile mode " $|\varphi(r)|$ "

• Memory is stored in a pattern $|n_1, n_2, ..., n_N\rangle =$

The effective gap of memory mode is $\omega_j \equiv \left(1 - \frac{1}{2}\right)^{-1}$

- As n_{ϕ} decreases, the memory modes backrest on the master modes, stopping its mixing with b modes
- Mapping of above system to bubble case: $q = 2/3, \ldots$

harge of the bubble

Hawking emission - added dof for relaxation

$$\left(\frac{n_{\phi}}{N_{\phi}}\right)^{q} m_{j} \text{ , gapless for initial condition } \langle \hat{n}_{\phi} \rangle = N_{\phi}$$

- The universality of memory burden effect shows that it must be shared by all systems of enhanced capacity of information storage (saturons), including black holes.
- This statement is independent of a particular microscopic theory of a black hole. However it is always useful to have one, in order to make things explicit.
- Such a framework is provided by ``black hole's quantum N-portrait'' (Dvali, Gomez '11).
- This theory describes a black hole of radius *R* as saturated coherent state of soft gravitons of wavelengths *R* and occupation number: $N_{\rm g} = (RM_{\rm P})^2$
- These gravitons are analogous to the radial (profile) mode "master mode" localizing the symmetry broken region in the bubble case. This picture makes the origin of memory modes explicit: They represent Goldstone-type excitations of very short wavelength gravitons. In black hole background, they are gapless in the way very similar to Goldstones of a vacuum bubble.

Dvali, Gomez '12,'13; Dvali, Franca, Gomez, Wintergerst, '13; Averin, Dvali, Gomez, Lust, '15, Dvali '17,'18,...

More on memory modes in black holes

The number of flavours of memory mode should be of order

harmonics $Y_{l.m}$.

All modes up to the cutoff $M_{\rm Pl}$ ought to be included in the counting. Notice that these correspond to modes of angular momentum of order $RM_{\rm Pl}$.

Their multiplicity is therefore the needed one

These modes have a gap of order $M_{\rm Pl}$. However, they are rendered gapless by the black hole master mode with occupation number N_{g} (order parameter). These are effectively the Goldstones associated to the Poincaré symmetry broken by the black hole itself.

- $N \sim S_{\rm BH}$.
- A suitable candidates are the graviton modes corresponding to various spherical

- $N \sim l^2 \sim (RM_{\rm Pl})^2 \simeq S_{\rm BH}$

Averin, Dvali, Gomez, Lust, '15, Dvali '18

Classical vs quantum memory

G. Dvali, C. Gomez '11;

When the above bound is saturated in black hole, it reaches extremality. This corresponds to presence of some long-range classical hair. The quantum pattern plays no role. However, the extremal black holes of the same electric charge and mass can carry information patterns of very different content.

In contrast, when a black hole is stabilized by a quantum memory burden, no classical charge associated with a long-range gauge field is required. Of course, a macroscopic ``hair'' emerges in form of a memory burden parameter, $S_{\rm BH}$. This parameter is in principle measurable by a scattering experiment, but there is no inconsistency with the no-hair properties: it is a quantum object.

Bubble unifies these features as the memory burden corresponds to macroscopic occupation of memory mode. However, it connects to quantum states via SU(N) rotation to other degenerate states.





Hawking emission vs retrieval of memory

G. Dvali, J. S.V.B., M. Zantedeschi, '24

Black hole can emit master modes - initially - reproducing Hawking entropy. The coupling suppression is compensated by the large occupation number

 $\Gamma_{\text{master mode}}$

compensation. Their annihilation is very rare: $\Gamma_{\rm memory}$ ~

As a consequence, it is natural to expect that, due to memory burden effect, the lifetime of the black hole is enhanced as

 $\tau_{\rm semiclassical} \sim R$

Model dependent different scalings are possible

$$a \sim \alpha_{\rm gr}^2 N_{\rm g}^2 \frac{1}{R} \sim \frac{1}{R}$$

Quantum memory modes $|n_1, \ldots, n_S\rangle$ do not have large occupation number, i.e., no

$$\sim \alpha_{\rm gr}^2 \frac{1}{R} \sim \frac{1}{S^2 R}$$

$$S \rightarrow \tau \gtrsim \tau_{\text{semiclassical}} S^2$$

•Analogous dynamics is observed if a SU(N)-singlet χ is derivatively coupled to the bubble with interaction $\chi \operatorname{Tr} \left[(\partial_{\mu} \phi) (\partial^{\mu} \phi) \right]$

2+1 dimensional perspective



















The same mechanism of stabilisation takes place in the case of bubble endowed with vorticity, characterised by integer winding number n = 1



Energy density as a function of time for different initial memories, $Q = 3Q_s/4$ (left column) and $Q = Q_s/2$ (right column), for winding number n = 0 (top row) and n = 1 (bottom row). Energy is emitted in χ quanta, relaxing the configuration.

It carries no information.





- Analogous dynamics is observed for bubbles in thick-wall regime
- In the case of vorticity, at late times the bubble sometimes ejects the vortex (bottom panel) or fragments
- In the former case, the residual configuration is left with vanishingly small angular momentum we characterised this phenomenon already in arXiv:2310.02288 - Dvali, Kaikov, Kühnel, Valbuena Bermúdez, Zantedeschi, *Phys. Rev. Lett.* 132 (2024) 15, 151402

Example of fragmentation







No-Vortex Case

Ejected-Vortex Case

Vortex Case

Energy and Spin evolve in a similar manner

- Ejected Vortex: the resulting soliton possesses a vortex for a while. Eventually it is ejected resulting in a close-to-zero spin configuration
- Vortex: almost no emission takes place in this case. The energy and angular momentum are invested in vortex formation

