

## **Exercise: Magnetic Field**

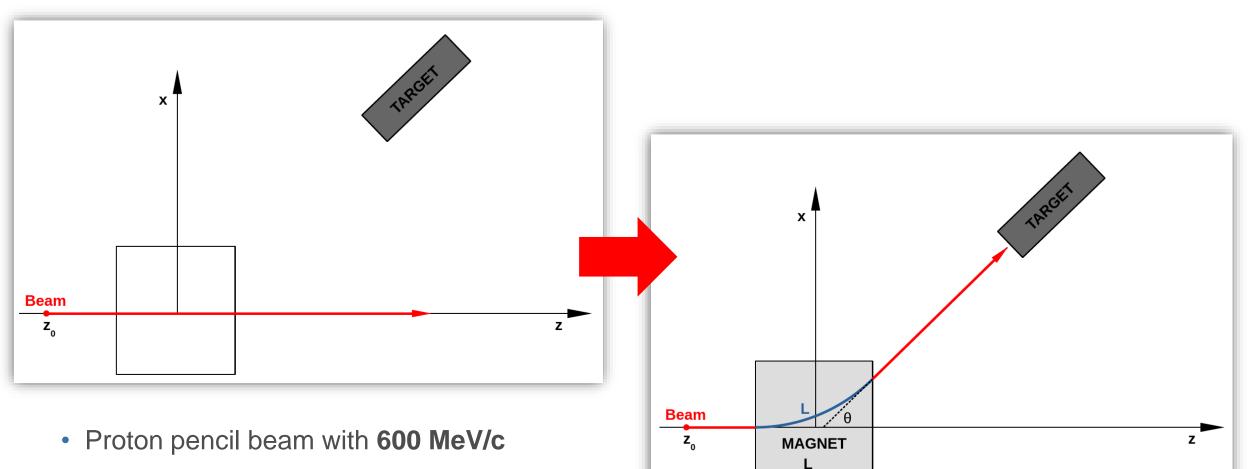
Aim of the exercise:

- Define a dipole field which deviates the beam on a target
- Plot the field
- Visualize the effect of the field on the beam trajectory

#### Beginner course – CERN, December 2024

#### **Goal of the exercise**

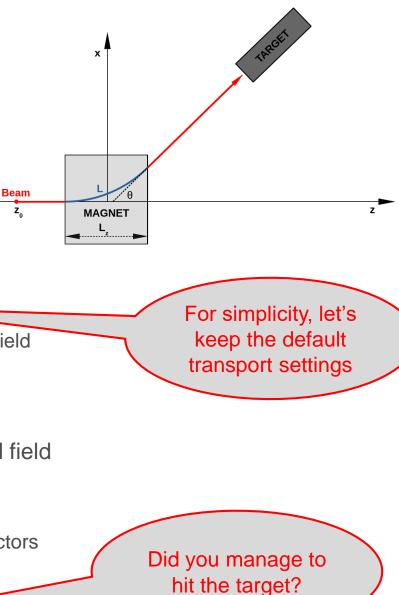
• Introduce a dipole field in order to deflect a given beam on a pre-defined target



• Starts at  $z_0 = -50$  cm, in positive z-direction

### **Steps**

- The beam, regions and scoring is pre-defined
  - Note that all regions except the target are set to VACUUM (including the magnet)
- Exercise steps:
  - 1. Activate a magnetic field in the pre-defined region called **MAGNET** (ASSIGNMA card)
  - 2. Introduce a **MGNFIELD** card and define a B field such that:
    - a. the beam is deflected in the **x-z plane** as illustrated in the figure (hint: the B field direction can be determined from the Lorentz force).
    - b. the deflection angle  $\theta$  is **25 deg**; use the formula on slide 5 to determine the required |B|. Note that the magnet is L<sub>z</sub>=**50 cm** long in z-direction.
  - 3. Verify that the field is correctly activated by plotting the field intensity and field vectors:
    - a. see lecture slides for instructions how to plot a field
    - b. make sure to chose an appropriate plotting plane which contains the field vectors
  - 4. Run one cycle (1 primary) and plot the particle fluence in the x-z plane
    - a. use the *pre-defined* **USRBIN** scoring in the Plot tab of Flair





#### **Lorentz force**

 Use following expression to determine which B field component needs to be set on the MGNFIELD card in order to deflect the beam on the target:

$$\begin{pmatrix} F_{x} \\ F_{y} \\ F_{z} \end{pmatrix} = q \begin{pmatrix} v_{x} \\ v_{y} \\ v_{z} \end{pmatrix} \times \begin{pmatrix} B_{x} \\ B_{y} \\ B_{z} \end{pmatrix} = q \begin{pmatrix} v_{y}B_{z} - v_{z}B_{y} \\ v_{z}B_{x} - v_{x}B_{z} \\ v_{x}B_{y} - v_{y}B_{x} \end{pmatrix}$$

- $(F_x, F_y, F_z) = \text{Lorentz force}$
- q = Particle charge
- $(v_x, v_y, v_z) = Particle velocity$
- $(B_x, B_y, B_z)$  = Magnetic field (magnetic flux density) components



# Required |B|

 Use the following expression to determine the required |B| in order to deviate the beam on the target:

<i>p</i> [ <i>GeV</i> / <i>c</i> ]	$ B [T] L_{z} [m]$
0.299792 Q [ <b>e</b> ]	$\sin \theta$

- p = Particle momentum in GeV/c
- Q = Particle charge (as multiple of elementary charges)
- $|B| = \sqrt{B_x^2 + B_y^2 + B_z^2}$  in Tesla
- $L_z$  = Length of the magnetic field in z-direction (i.e. in the original beam direction)
- $\theta$  = Deflection angle in rad

Note: this formula can be simply derived from the Lorentz force and applies for a homogenous dipole field with  $L_z < R$ , where R is the bending radius.



