DA studies with Xsuite

K. André

189th FCC-ee Accelerator Design Meeting – July 25th, 2024 Thanks to K. Oide

Oide's DA - Macroparticle grid





'Brute force' grid

Grid resulting from bisection

Resulting DA

As you increase the 'depth' of tracked macroparticle in action J, the central area becomes increasingly whiter, proving the particles survived.

Some parts of the central region appear less white because of the average between phase planes because some planes have no data at this (δ ,J) position.



Reduction to one RF section

From 4 RF cavities at 400MHz evenly distributed in the ring (one in each straight section) to **1 RF section** including 400 MHz RF cavities and 800 MHz RF cavities.

Single RF section for the LCC lattice (nominal)

$$\begin{split} & \text{LCC}_V24.3 \mid \text{E}_{\text{beam}} = 182.5 \text{ GeV}, \ \text{I}_{\text{beam}} = 5\text{mA} \ (\text{N} = 2.02\text{E} + 11\text{pbb}), \ \text{50 turns} \\ & \epsilon_x = 2.12\text{nm.rad}, \ \epsilon_y/\epsilon_x = 2\%, \ \sigma_{\sigma} = 0.148\%, \ \sigma_z = 1.8\text{nm}, \ \beta_{x,y}^* = \{1.00\text{m}, \ 1.6\text{mm}\} \\ & \text{V}_{rf} \ 400|800\text{MHz} = 2.10\text{GV}|9.20\text{GV}, \ \text{Q}_{x|y|s} = \{350.205, \ 266.294, \ 0.115\}, \ \text{Crab waist} = 40\% \end{split}$$



$$\begin{split} & LCC_V24.3 \mid \mathsf{E}_{\mathsf{beam}}=182.5 \text{ GeV}, \ \mathsf{I}_{\mathsf{beam}}=5\mathsf{mA} \ (\mathsf{N}=1.77\mathsf{E}+11\mathsf{ppb}), \ 50 \ \mathsf{turns} \\ & \varepsilon_x=2.12\mathsf{nm}.\mathsf{rad}, \ \varepsilon_y/\varepsilon_x=2\%, \ \sigma_{\delta}=0.148\%, \ \sigma_z=1.9\mathsf{mm}, \ \beta^*_{x,y}=\{1.0\mathsf{om}, \ 1.6\mathsf{mm}\} \\ & \mathsf{V}_{rf} \ 400|800\mathsf{MHz}=2.00\mathsf{GV}|8.74\mathsf{GV}, \ \mathsf{Q}_{\mathsf{x}|\mathsf{v}|s}=\{350.205, \ 266.294, \ 0.107\}, \ \mathsf{Crab} \ \mathsf{waist}=40\% \end{split}$$



 $\begin{array}{l} LCC_V24.3 \mid \mathsf{E}_{\mathsf{beam}}=182.5 \mbox{ GeV, } I_{\mathsf{beam}}=5mA \ (N=1.77E+11ppb), \ 50 \ turns \\ \epsilon_x=2.12nm.rad, \ \epsilon_y/\epsilon_x=2\infty, \ \sigma_5=0.148\%, \ \sigma_z=2.1mm, \ \beta_{x,y}^*=\{1.00m, \ 1.6mm\} \\ V_{rf} \ 400|800MHz=1.87GV|8.19GV, \ Q_{x|y|s}=\{350.205, \ 266.294, \ 0.095\}, \ Crab \ waist=40\% \end{array}$



$$\begin{split} & LCC_V24.3 \mid E_{beam}{=}182.5 \text{ GeV}, \text{ } \text{I}_{beam}{=}5\text{mA} \text{ (N=1.77E+11ppb), 50 turns} \\ & \epsilon_x{=}2.12\text{nm.rad}, \ & \epsilon_y/\epsilon_x = 2\%, \ & \sigma_{\delta}{=}0.148\%, \ & \sigma_z{=}2.4\text{mm}, \ & \beta^*_{x,y}{=}\{1.00\text{m}, \ 1.6\text{mm}\} \\ & V_{rf} \text{ 400}|800\text{MHz}{=}1.78\text{GV}|7.82\text{GV}, \ & Q_{x|y|s}{=}\{350.205, \ 266.294, \ 0.084\}, \ & \text{Crab waist}{=}40\% \end{split}$$



Attempt to get the same synchrotron tune as GHC lattice $(Q_s=0.089)$.

The energy loss per turn is smaller for LCC by 10-12%,

but the momentum compaction factor is larger α_{GHC} =7.5e-6 and α_{LCC} = 8.8e-6

Is it important to get to Q_s =0.089 with the LCC lattice ?

MA comparison between SAD & Xsuite for the <u>GHC lattice</u> and against <u>LCC lattice</u>



$$\begin{split} & \mathsf{GHC}_V24 \mid \mathsf{E}_{\mathsf{beam}}{=}45.6 \; \mathsf{GeV}, \mathsf{I}_{\mathsf{beam}}{=}1282\mathsf{mA} \; (\mathsf{N}{=}2.16\mathsf{E}{+}11\mathsf{ppb}), \; 512 \; \mathsf{turns} \\ & \epsilon_x{=}0.70\mathsf{nm}.\mathsf{rad}, \; \epsilon_y/\epsilon_x{=}2\%, \; \sigma_\delta{=}0.039\%, \; \sigma_z{=}5.5\mathsf{mm}, \; \beta^*_{x,\,y}{=}\{0.10\mathsf{m}, \; 0.7\mathsf{mm}\} \\ & \mathsf{V}_{rf} \; 400|800\mathsf{MHz}{=}0.08\mathsf{GV}|0.00\mathsf{GV}, \; \mathsf{Q}_{x|y|s}{=}\{218.156, \; 222.197, \; 0.029\}, \; \mathsf{Crab} \; \mathsf{waist}{=}70\% \end{split}$$













 $\begin{aligned} & \mathsf{GHC_V24} \mid \mathsf{E_{beam}}{=}182.5 \ \mathsf{GeV}, \ \mathsf{I_{beam}}{=}5\mathsf{mA} \ (\mathsf{N}{=}1.47\mathsf{E}{+}11\mathsf{ppb}), \ \mathsf{50} \ \mathsf{turns} \\ & \epsilon_x{=}1.51\mathsf{nm.rad}, \ \epsilon_y/\epsilon_x = 2\%, \ \sigma_{\delta}{=}0.157\%, \ \sigma_z{=}1.8\mathsf{mm}, \ \beta_{x,y}^*{=}\{0.88\mathsf{m}, \ 1.4\mathsf{mm}\} \\ & \mathsf{V_{rf}} \ \mathsf{400}|800\mathsf{MHz}{=}2.10\mathsf{GV}|9.20\mathsf{GV}, \ \mathsf{Q}_{x|y|s}{=}\{398.138, \ 398.208, \ 0.089\}, \ \mathsf{Crab} \ \mathsf{waist}{=}40\% \end{aligned}$



Comparison GHC vs. LCC @ Z energy



$$\begin{split} & \text{LCC}_V24.3 \mid \text{E}_{\text{beam}}=45.6 \text{ GeV}, \text{I}_{\text{beam}}=1456\text{mA} \text{ (N}=2.45\text{E}+11\text{ppb)}, 512 \text{ turns} \\ & \epsilon_x=0.69\text{nm.rad}, \ & \epsilon_y/\epsilon_x=2\infty, \ \sigma_{\sigma}=0.037\%, \ \sigma_z=5.2\text{nm}, \ & \beta_{x,y}^*=\{0.10\text{m}, \ 0.7\text{mm}\} \\ & \text{V}_{rf} \text{ 400}|800\text{MHz}=0.1\text{GV}|0.0\text{GV}, \ & \text{Q}_{x|y|s}=\{198.200, 174.299, \ 0.030\}, \ & \text{Crab waist}=80\% \end{split}$$



$$\label{eq:GHC_V23} \begin{split} & \mathsf{F}_{beam}{=}45.6 \; \mathsf{GeV}, \; \mathsf{I}_{beam}{=}1278\mathsf{mA} \; (\mathsf{N}{=}2.16\mathsf{E}{+}11\mathsf{ppb}), \; 512 \; \mathsf{turns} \\ & \epsilon_x{=}0.70\mathsf{nm}.\mathsf{rad}, \; \epsilon_y/\epsilon_x = 2\%, \; \sigma_{\sigma}{=}0.039\%, \; \sigma_z{=}5.5\mathsf{nm}, \; \beta_{x,y}^*{=}\{0.10\mathsf{m}, \; 0.7\mathsf{mm}\} \\ & \mathsf{V}_{rf} \; 400|800\mathsf{MHz}{=}0.08\mathsf{GV}|0.00\mathsf{GV}, \; \mathsf{Q}_{x|y|s}{=}\{218.156, \; 222.199, \; 0.029\}, \; \mathsf{Crab} \; \mathsf{waist}{=}70\% \end{split}$$



 $\label{eq:GHC_V23} \begin{array}{l} | \ E_{beam}{=}45.6 \ \text{GeV}, \ I_{beam}{=}1278\text{mA} \ (\text{N}{=}2.16\text{E}{+}11\text{ppb}), \ 512 \ \text{turns} \\ \epsilon_x{=}0.70\text{nm.rad}, \ \epsilon_y/\epsilon_x{=}2\%, \ \sigma_{\delta}{=}0.039\%, \ \sigma_z{=}5.5\text{nm}, \ \beta_{x,y}^*{=}\{0.10\text{m}, \ 0.7\text{mm}\} \\ V_{rf} \ 400|800\text{MHz}{=}0.08\text{GV}|0.00\text{GV}, \ Q_{x|y|s}{=}\{218.156, \ 222.199, \ 0.029\}, \ \text{Crab waist}{=}70\% \end{array}$



Nominal magnet strengths (v92a)

Comparison GHC vs. LCC (opti) @ Z energy



LCC_V24.3 | Ebeam = 45.6 GeV, Ibeam = 1456mA (N=2.45E+11ppb), 512 turns

$$\begin{split} & \text{LCC_V24.3} \mid \text{E}_{\text{beam}} = 45.6 \text{ GeV}, \text{I}_{\text{beam}} = 1456\text{mA} \text{ (N=2.45E+11ppb)}, 512 \text{ turns} \\ & \epsilon_x = 0.69\text{nm.rad}, \ \epsilon_y / \epsilon_x = 2\%, \ \sigma_\sigma = 0.037\%, \ \sigma_z = 5.3\text{mm}, \ \beta^*_{x,y} = \{0.10\text{m}, \ 0.7\text{mm}\} \\ & \text{V}_{rf} \text{ 400} \mid 800\text{MHz} = 0.08\text{GV} \mid 0.00\text{GV}, \ Q_{x|y|s} = \{198.200, \ 174.299, \ 0.030\}, \ \text{Crab waist} = 80\% \end{split}$$



$$\label{eq:GHC_V23} \begin{split} & \mathsf{F}_{beam}{=}45.6 \; \mathsf{GeV}, \; \mathsf{I}_{beam}{=}1278\mathsf{mA} \; (\mathsf{N}{=}2.16\mathsf{E}{+}11\mathsf{ppb}), \; 512 \; \mathsf{turns} \\ & \epsilon_x{=}0.70\mathsf{nm}.\mathsf{rad}, \; \epsilon_y/\epsilon_x = 2\%, \; \sigma_{\sigma}{=}0.039\%, \; \sigma_z{=}5.5\mathsf{nm}, \; \beta^*_{x,y}{=}\{0.10\mathsf{m}, \; 0.7\mathsf{mm}\} \\ & \mathsf{V}_{rf} \; 400|800\mathsf{MHz}{=}0.08\mathsf{GV}|0.00\mathsf{GV}, \; \mathsf{Q}_{x|y|s}{=}\{218.156, \; 222.199, \; 0.029\}, \; \mathsf{Crab} \; \mathsf{waist}{=}70\% \end{split}$$



 $\begin{array}{l} \label{eq:GHC_V23} \mathsf{GHC_V23} \mid \mathsf{E}_{\mathsf{beam}}{=}45.6 \; \mathsf{GeV}, \; \mathsf{I}_{\mathsf{beam}}{=}1278\mathsf{mA} \; (\mathsf{N}{=}2.16\mathsf{E}{+}11\mathsf{ppb}), \; 512 \; \mathsf{turns} \\ \epsilon_x{=}0.70\mathsf{nm}.\mathsf{rad}, \; \epsilon_y/\epsilon_x = 2\%, \; \sigma_{\delta}{=}0.039\%, \; \sigma_z{=}5.5\mathsf{nm}, \; \beta_{x,y}^*{=}\{0.10\mathsf{m}, \; 0.7\mathsf{nm}\} \\ \mathsf{V}_{rf}\; 400|800\mathsf{MHz}{=}0.08\mathsf{GV}|0.00\mathsf{GV}, \; \mathsf{Q}_{x|y|s}{=}\{218.156, \; 222.199, \; 0.029\}, \; \mathsf{Crab}\; \mathsf{waist}{=}70\% \end{array}$



Optimized magnet strengths (v92a)

Comparison GHC vs. LCC @ tt energy



GHC V24 | E_{beam}=182.5 GeV, I_{beam}=5mA (N=1.47E+11ppb), 50 turns $\varepsilon_x = 1.51$ nm.rad, $\varepsilon_v / \varepsilon_x = 2\%$, $\sigma_{\delta} = 0.157\%$, $\sigma_z = 1.8$ nm, $\beta_{x,v}^* = \{0.88$ m, 1.4 nm} V_{rf} 400|800MHz=2.10GV|9.20GV, Q_{xlvis}={398.138, 398.208, 0.089}, Crab waist=40%



LCC_V24.3 | E_{beam}=182.5 GeV, I_{beam}=5mA (N=2.02E+11ppb), 50 turns $\varepsilon_x = 2.12$ nm.rad, $\varepsilon_v / \varepsilon_x = 2$ %, $\sigma_{\delta} = 0.148$ %, $\sigma_z = 1.8$ nm, $\beta_{x,v}^* = \{1.00$ m, 1.6 nm $\}$ V_{rf} 400|800MHz=2.10GV|9.20GV, $Q_{x|y|s}$ ={350.205, 266.294, 0.115}, Crab waist=40% 100 50 75 40 plitude $A_y(\phi)$ 50 survived 25 tŦ 0 DA - 20 SU -25 Normalis -50 10 -75 -100-30 -20 -100 10 20 30 X [σ_x] -10-5 0 5 10 X [mm]

> LCC V24.3 | Ebeam=182.5 GeV, Ibeam=5mA (N=2.02E+11ppb), 50 turns $\varepsilon_x = 2.12$ nm.rad, $\varepsilon_v / \varepsilon_x = 2\infty$, $\sigma_{\delta} = 0.148\%$, $\sigma_z = 1.8$ nm, $\beta_{x,v}^* = \{1.00$ nm, 1.6 nm $\}$ V_{rf} 400|800MHz=2.10GV|9.20GV, $Q_{x|y|s}$ ={350.205, 266.294, 0.115}, Crab waist=40%



50

40

survived

20 Sun

- 10

- 0

MA comparison between SAD and Xsuite for the LCC lattice

Differences between Xsuite and SAD (CW=0%)

- I spotted differences (in the converted MADX file, Oide-san sent me) in which the variable cs_comp is not used and the decapoles not defined.
- It could explain the differences observed with and without crab waist as the decapoles are turned on also without crab waist.





Differences between Xsuite and SAD (CW=80%)

- I spotted differences (in the converted MADX file, Oide-san sent me) in which the variable cs_comp is not used and the decapoles not defined.
- It could explain the differences observed with and without crab waist as the decapoles are turned on also without crab waist.



MA study comparison between relaxed vs. nominal optics

-- GHC lattice detuned to $\beta_x^* = 0.33 \text{ m \& } \beta_y^* = 7 \text{ mm}$

-- LCC lattice detuned to $\theta_x^* = 0.30 \text{ m \& } \theta_y^* = 7 \text{ mm}$

Momentum Acceptance of the relaxed optics

LCC_V24.3 | Ebeam = 45.6 GeV, Ibeam = 1456mA (N=2.45E+11ppb), 512 turns $\varepsilon_x = 0.69$ nm.rad, $\varepsilon_v / \varepsilon_x = 2\%$, $\sigma_{\delta} = 0.037\%$, $\sigma_z = 5.2$ nm, $\beta_{x,v}^* = \{0.10$ m, 0.7 nm} V_{rf} 400|800MHz=0.1GV|0.0GV, $Q_{x|y|s}$ ={198.200, 174.299, 0.030}, Crab waist=80% $\phi = 0$ 20 - $\phi = \pi/4$ $\phi = \pi/2$ 400 $A_{x}(\phi)$ $\phi = 3\pi/4$ 10 amplitude survived Ω - 200 Sunj ed ma -10Nor 100 Nomina -20 -0.50.0 0.5 1.0 -1.5-1.01.5 δ[%] -30 -20 -1010 20 30 -400 $\delta \left[\sigma_{5}^{SR} \right]$



20

10

-10

-20 -

-1.5

-40

-1.0

-30

-0.5

-20

-10

 $A_x(\phi)$

amplitude

Normalised

 $\begin{array}{l} \label{eq:GHC_V24} GHC_V24 \mid E_{beam}{=}45.6 \mbox{ GeV}, \mbox{ I}_{beam}{=}1282\mbox{mA} \mbox{ (N=2.16E+11ppb), 512 turns} \\ \epsilon_x{=}0.70\mbox{nm.rad}, \ \epsilon_y/\epsilon_x {=}2\%, \ \sigma_{\sigma}{=}0.039\%, \ \sigma_z{=}5.5\mbox{mm}, \ \beta_{x,y}^*{=}\{0.10\mbox{m}, 0.7\mbox{mm}\} \\ V_{rf} \mbox{ 400}|800\mbox{MHz}{=}0.08\mbox{GV}|0.00\mbox{GV}, \ Q_{x|y|s}{=}\{218.156, 222.197, 0.029\}, \ Crab \ waist{=}70\% \end{array}$



$$\label{eq:GHC_V24} \begin{split} & \mbox{GHC_V24} \mid \mbox{E}_{beam} = 45.6 \mbox{ GeV}, \mbox{ } \mbox{I}_{beam} = 1282 \mbox{mA} \mbox{ (N=2.16E+11ppb)}, \mbox{ 512 turns} \\ & \mbox{ } \mbox{$$



 $\begin{array}{l} LCC_V24.3 \mid E_{beam} = 45.6 \ \text{GeV}, \ I_{beam} = 1456\text{mA} \ (\text{N} = 2.45\text{E} + 11\text{ppb}), \ 512 \ \text{turns} \\ \epsilon_x = 0.68\text{nm.rad}, \ \epsilon_y/\epsilon_x = 2\%, \ \sigma_\sigma = 0.037\%, \ \sigma_z = 5.2\text{mm}, \ \beta_{x,y}^* = \{0.30\text{m}, \ 7.0\text{mm}\} \\ V_{rf} \ 400 \mid 800\text{MHz} = 0.08\text{GV} \mid 0.00\text{GV}, \ Q_{x\mid y\mid s} = \{198.200, \ 174.300, \ 0.030\}, \ \text{Crab} \ \text{waist} = 0\% \end{array}$

0.0

δ [%]

0

 $\delta [\sigma_5^{SR}]$

0.5

20

10

1.0

30

LCC V24.3 | Ebeam = 45.6 GeV, Ibeam = 1456mA (N=2.45E+11ppb), 512 turns

 $\epsilon_x = 0.68$ nm.rad, $\epsilon_v / \epsilon_x = 2$ ‰, $\sigma_{\delta} = 0.037$ %, $\sigma_z = 5.2$ nm, $\beta_{x,v}^* = \{0.30$ m, 7.0 nm}

V_{rf} 400|800MHz=0.08GV|0.00GV, Q_{xlvls}={198.200, 174.300, 0.030}, Crab waist=0%

 $\phi = 0$

 $\phi = \pi/4$

 $\phi = \pi/2$

 $\phi = 3\pi/4$

400

survived

- 200 5

- 100

1.5

Momentum Acceptance of the relaxed optics



Summary and outlook

- One RF section: Decreasing by about 5% the total RF voltage of LCC at tt energy still result in \pm 3% MA and Q_s=0.107. 10% is too much though.
- Xsuite/SAD MA comparison: The MA results for the GHC lattice agree well with CW. The MA results for the LCC lattice agree well without CW.
- **Detuned optics**: The MA of the GHC detuned optics goes beyond $40\sigma_x$ onenergy and $10\sigma_x$ at ±1%, whereas LCC detuned optics goes beyond $60\sigma_x$ onenergy and $20\sigma_x$ at ±1%.

Outlook:

- Implement the DA/MA with Xsuite as a test in the Gitlab lattice repository, along with SAD?
- Compare Xsuite/SAD MA results for the LCC lattice including decapoles (and cs_comp with CW).
- Implement the optimum magnet strengths for the LCC lattice at ttbar energy.