

# Top Mass Measurements at the Tevatron

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*On behalf of the CDF and DZero collaborations*



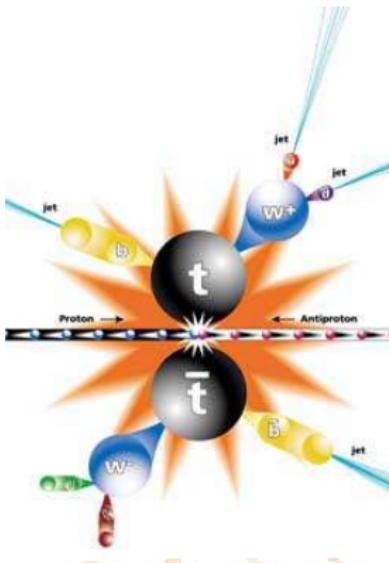
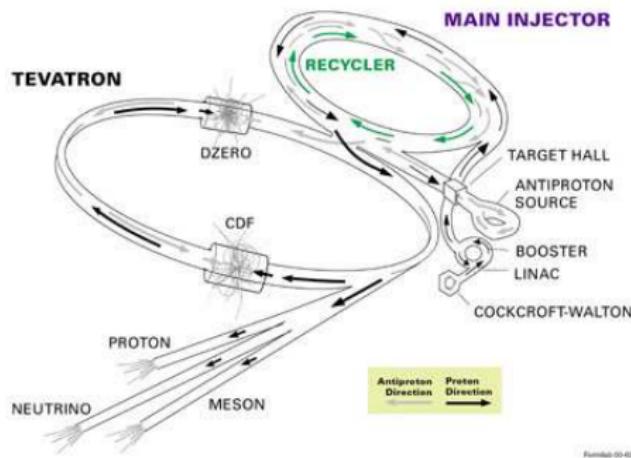
4th International Workshop on Top Quark Physics  
Sant Feliu de Guixols, Spain  
September 28, 2011



# Outline

1. The Top Quark;
2. Mass Measurement Techniques;
3. Mass Measurements;
4. Top-Antitop Mass Difference
5. Combination;

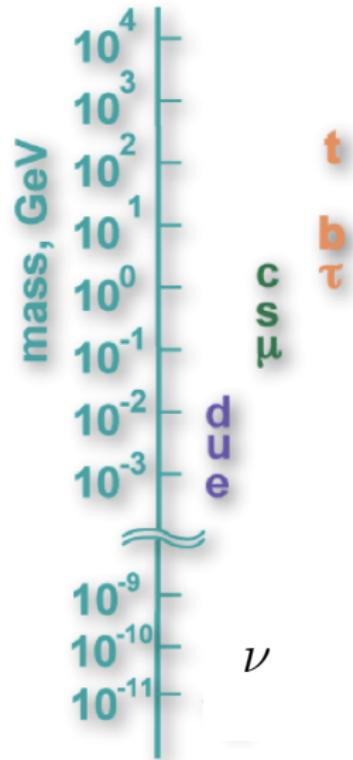
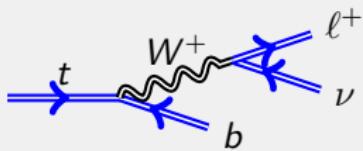
FERMILAB'S ACCELERATOR CHAIN



# The top quark

## What?

- Discovered in 1995 at Fermilab;
- Mass much larger than any other fermion;
- $L_{\text{Yukawa}} = -\lambda \bar{\psi}_L \Phi \psi_R$ ,  $\lambda = 0.996 \pm 0.006$ 
  - What is its role in EWSB?
- Only quark that decays before hadronizing:



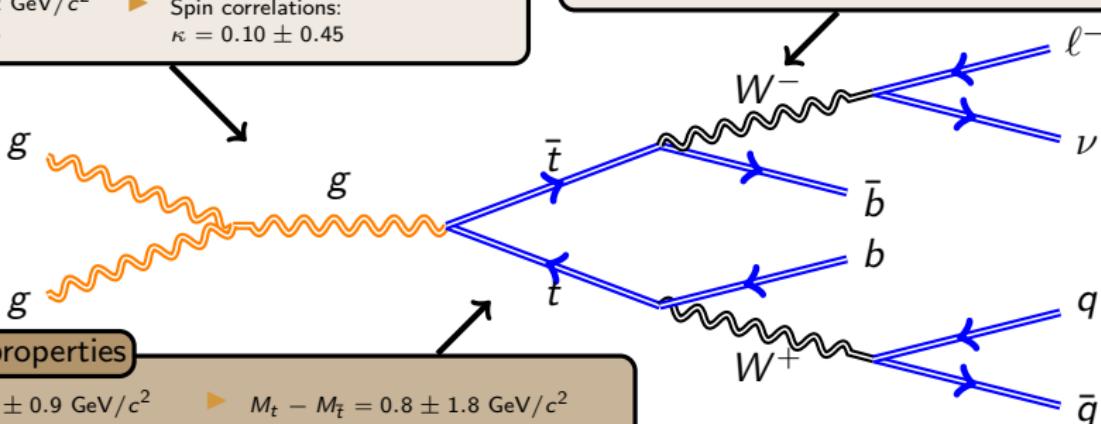
# Top quark physics: intrinsic properties

## Production properties

- $M_{Z'} > 900 \text{ GeV}/c^2$  @ 95% C.L.
- $M_{W'} > 800 \text{ GeV}/c^2$  @ 95% C.L.
- $M_{b'} > 372 \text{ GeV}/c^2$  @ 95% C.L.
- $F_{gg} = 0.07^{+0.15}_{-0.07}$  (stat+sys)
- $A_{fb} = 15 - 40\%$  (parton level)
- Spin correlations:  $\kappa = 0.10 \pm 0.45$

## Decay properties

- $V_{tb} = 0.91 \pm 0.11$  (exp)  $\pm 0.07$  (theory)
- No evidence for charged Higgs
- $f_0 = 0.67 \pm 0.10$  &  $f_+ = 0.02 \pm 0.05$



## Intrinsic properties

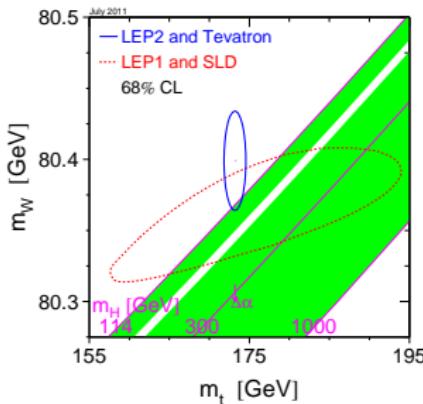
- $M_t = 173.2 \pm 0.9 \text{ GeV}/c^2$
- $M_t - M_{\bar{t}} = -3.3 \pm 1.7 \text{ GeV}/c^2$
- $\Gamma_t < 7.5 \text{ GeV}$  @ 95% C.L.
- $M_t - M_{\bar{t}} = 0.8 \pm 1.8 \text{ GeV}/c^2$
- $\Gamma_t < 1.99^{+0.69}_{-0.55} \text{ GeV}$

# Why is the top quark (mass) so important?

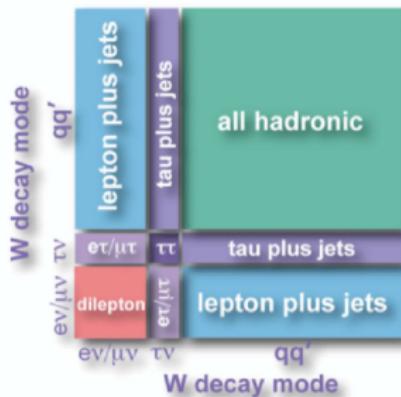
- ▶  $m_t$  is a fundamental parameter of the SM;
- ▶ Its mass ( $m_t$ ) constrains the Higgs mass;

$$\left(\frac{m_W}{m_Z}\right)^2 = (1 - \sin^2 \theta_W) \cdot (1 + \Delta\rho(m_t^2; \ln m_H))$$

- ▶ Relates to many SM observables (loop diagrams)
  - ▶ Strong consistency check on SM parameters
- ▶ The top sector is expected to be sensitive to many new physics processes;



# Pair production decay signatures at Tevatron



## Fully-reconstructed signatures

- Lepton+Jets [ $\mathcal{B} \sim 30\%$ , good  $S/B$ ]
  - ▶ “Golden channel” for top mass;
- All hadronic [ $\mathcal{B} \sim 44\%$ ]
  - ▶ But very large QCD background

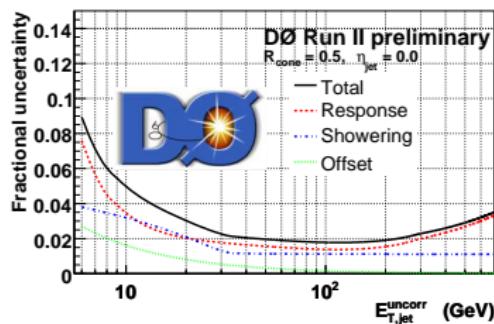
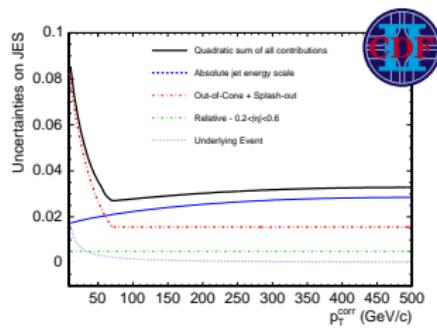
## Experimentally more challenging signatures

- Dilepton [ $\mathcal{B} \sim 5\%$ , highest  $S/B$ ]
  - ▶ Challenge: the two  $\nu$ 's complicate the reconstruction
    - ▶ Neutrino Weighting, Matrix Weighting;
- $\cancel{E}_T +$  jets
  - ▶ Lepton+jets and dilepton decays where  $e/\mu$  is not identified;
  - ▶ Large acceptance to  $\tau$  ( $\sim 40\%$  of sample); large QCD background;
  - ▶ Challenging: even less possibilities to reconstruct the  $m_t$ ;

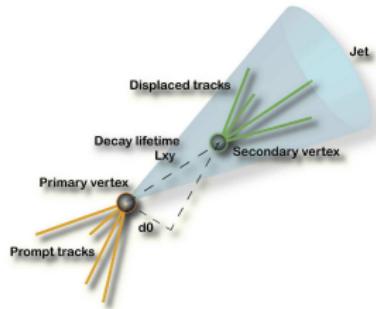
# Experimental Challenges

## Jet Reconstruction

- ▶ Need parton information for  $m_t$ , but we measure calorimeter deposits, thus jets (using a cone algorithm);
- ▶ Jets are further corrected to the particle level;
- ▶ Jet Energy Scale (JES) is the major source of uncertainty;
- ▶ Fortunately, we can measure the JES simultaneously with  $m_t$ ;
  - ▶ **In situ** calibration using  $W \rightarrow jj$  to measure the  $W$  mass;
  - ▶ Transforming a systematic uncertainty into a statistical one;
  - ▶ Can be applied to the  $\ell+jets$  and hadronic topologies.

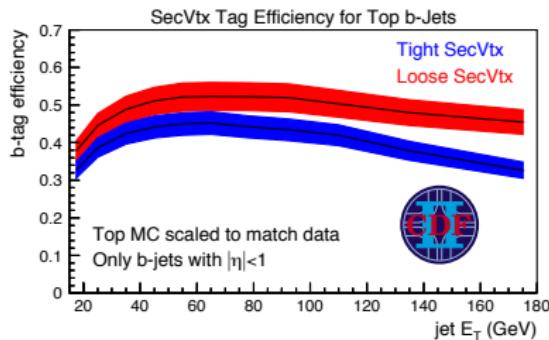
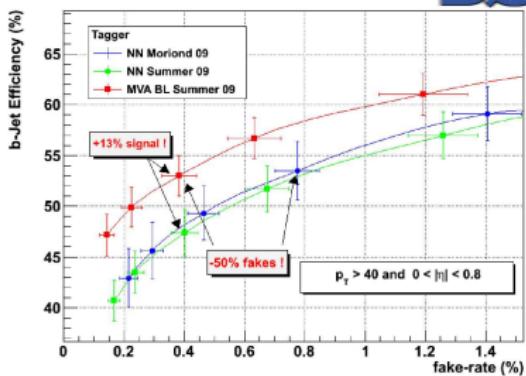


# Experimental Challenges (2)



## b-tagging

- Background is reduced by identifying jets from  $b$ -quarks;
- Either secondary vertex tagging (most efficient) or ID of semileptonic decays of  $B$  hadrons;



# Methods used at the Tevatron (1)

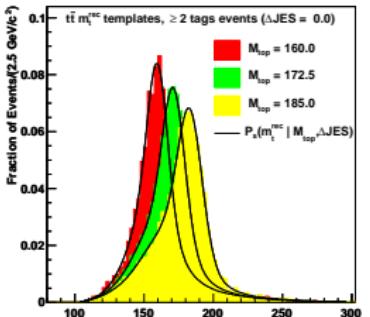
## Template Method

1. Determine  $m_t$ -dependent observables (e.g.  $m_t^{\text{reco}}$ , reconstructed mass);

$$\chi^2 = \underbrace{\sum \left( \frac{p_T^{\text{fit}} - p_T^{\text{meas.}}}{\sigma} \right)^2}_{\text{Kinematic constraints}} + \underbrace{\sum \left( \frac{M_{ff}^{\text{fit}} - M_{W(t)}^{(\text{reco.})}}{\Gamma_{W(t)}} \right)^2}_{\text{Mass constraints}}$$

2. Generate **template** distributions at different  $m_t$  (Monte Carlo);
3. Fit the templates to data to determine  $m_t$ .

- ▶ Does not use the full event information, nor event-by-event differences;
- ▶ Fast but statistical sensitivity worse than other methods;
- ▶ Systematic effects (e.g. JES) can be taken into account in the MC;
- ▶ Lepton  $p_T$  and  $b$ -quark decay length ( $L_{xy}$ ) are also options for the observables, and do not depend on JES;



# Methods used at the Tevatron (2)

## Matrix Element Technique

1. Compute the **event probability density** ( $P_E$ );

$$P_E(x; m_t, f_{t\bar{t}}) = f_{t\bar{t}} \cdot P_{t\bar{t}}(x; m_t) + (1 - f_{t\bar{t}}) \cdot P_b(x)$$

2. Obtain the sample likelihood ( $L = \prod P_E$ ), and extract the most likely mass;

$$P_{t\bar{t}} = \frac{1}{\sigma_{t\bar{t}}(m_t)} \sum_{j=p} \int \sum_{\text{flavors}} dq_1 dq_2 \underbrace{\frac{d\sigma(\mathbf{p}\bar{\mathbf{p}} \rightarrow t\bar{t} \rightarrow \mathbf{y})}{dy}}_{\text{Matrix Element}} \cdot \underbrace{f(q_1)f(q_2)}_{\text{PDFs}} \cdot \underbrace{W(x; y)}_{\text{Resolution}} \cdot dy$$

- ▶ Uses full event information, and event-by-event differences;
- ▶ Very CPU intensive (hours per event);
- ▶ Systematic effects (e.g. JES) can be taken into account when getting  $P_E$ ;
- ▶ Simple version: Dynamical Likelihood, without explicit  $P_b$ .

# Methods used at the Tevatron (3)

## Ideogram Method

- ▶ Similar to the Matrix Element method, except in evaluating  $P_{t\bar{t}}$  and  $P_b$ ;

$$P_E(x; m_t, f_{t\bar{t}}) = f_{t\bar{t}} \cdot P_{t\bar{t}}(x; m_t) + (1 - f_{t\bar{t}}) \cdot P_b(x)$$

- ▶ The probability for a given process ( $P_{\text{proc.}}$ ) obtained from kinematic information to extract  $m_t$  ( $x_\kappa$ ) and other variables ( $x_\tau$ );

$$P_{\text{proc.}}(x; \dots) = P_{\text{proc.}}^\kappa(x_\kappa; \dots) \cdot \underbrace{P_{\text{proc.}}^\tau(x_\tau; \dots)}_{\text{Optional component}}$$

- ▶ Approximation of Matrix Element (ME), less accurate but faster;
- ▶ Cost and performance typically between ME and template method;
- ▶ Requires full  $m_t$  reconstruction: cannot be applied to *dilepton*;
- ▶ Again, systematics can be included in the determination of  $P_E$ .

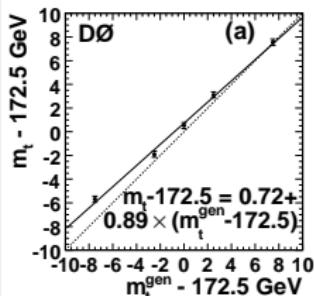
# General considerations for $m_t$ measurements

## Calibration of the measurement

- ▶ Need to quantify the techniques' influence on  $m_T^{\text{meas.}}$ ;
- ▶ Calibration with Monte Carlo pseudo-experiments (ensemble testing), correcting the average mass residual to zero and the width of the pull to unity;

$$m_t^{\text{corr}} = \alpha \times m_t^{\text{meas.}} + \beta$$

- ▶ The calibration is then applied to the measurement.



## What is being measured (theoretical interpretation)?

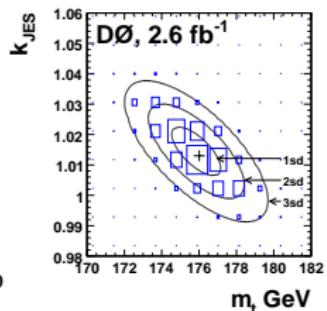
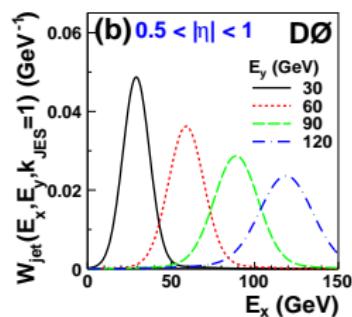
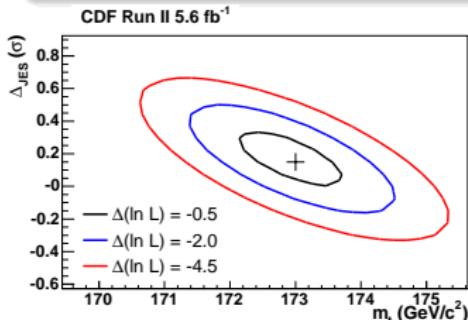
- ▶ Free particle: the physical mass usually is the **pole** of its renormalized propagator;
- ▶ Ambiguous for quarks, due to non-perturbative QCD effects,  $\mathcal{O}(\Lambda_{QCD})$ ;
- ▶ Alternatives:  $m_{\overline{MS}}$ , only sensitive to short distance QCD (used for light quarks);
- ▶ Experiment: measurement (usually) through the **reconstruction of the decay products**, based on MC; is this the pole mass? [Will discuss later]
- ▶ Calibration: MC generators include model-dependent descriptions of the parton shower and the hadronization; effect of  $\mathcal{O}(\Lambda_{QCD})$ ;

# Lepton + Jets

- Most precise  $m_t$  measurements from single channel;
- Using matrix elements with in-situ JES to maximise sensitivity;
- $p_T(e, \mu) > 20 \text{ GeV}/c$ ,  $\cancel{E}_T > 20 \text{ GeV}$ , 4 jets with  $p_T > 20 \text{ GeV}/c$ ,  $\geq 1 b\text{-tag}$ ;
- CDF: NN to weight background contribution; Quasi-MC integration over 19 var.;
- DØ:  $q\bar{q} \rightarrow t\bar{t}$  ME for signal, background ME from VECBOS;

## Latest results

- CDF [5.6 $\text{fb}^{-1}$ ]:  $m_t = 173.0 \pm 1.2 \text{ GeV}/c^2$   
[ Phys.Rev.Lett. 105 (2010) 252001; arXiv:1010.4582 [hep-ex] ]
- DØ [1.0+2.6 $\text{fb}^{-1}$ ]:  $m_t = 174.9 \pm 1.5 \text{ GeV}/c^2$   
[ Phys.Rev.D 84 (2011) 032004; arXiv:1105.6287 [hep-ex] ]

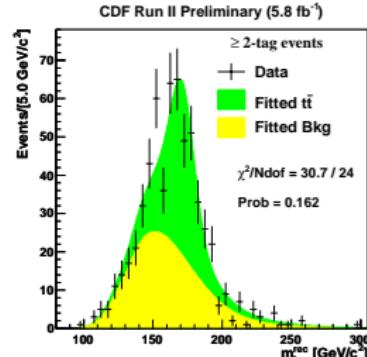
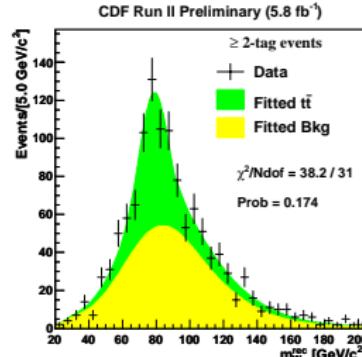
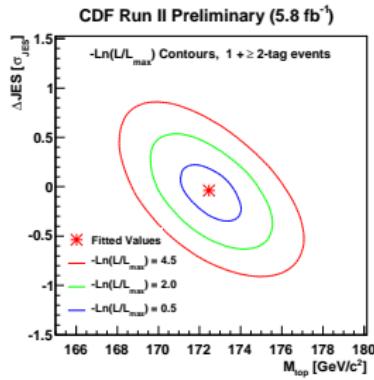


# All-Hadronic

- ▶ 6 – 8 jets with  $p_T > 15 \text{ GeV}/c$ ,  $\geq 1b\text{-tags}$ , no leptons, small  $\cancel{E}_T$ ;
- ▶ NN background suppression;
- ▶ Uses jet shapes to distinguish quark jets from gluon jets;
- ▶ Template method with kinematic fitter, and in-situ JES calibration;

## Latest results

- ▶ CDF [5.8 $\text{fb}^{-1}$ ]:  $m_t = 172.5 \pm 2.0 \text{ GeV}/c^2$   
[ CDF/PHYS/TOP/PUBLIC/10456 ]

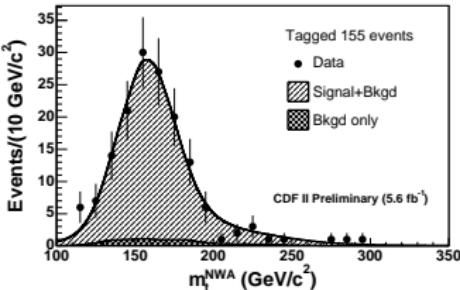


# Dilepton

- ▶ No in-situ JES calibration possible (no hadronic  $W$ );
- ▶ System is underconstrained: two  $\nu$ s, one  $\cancel{E}_T$ ;
- ▶ CDF: Templates using neutrino weighting algorithm (NWA); [also for DØRun IIa]

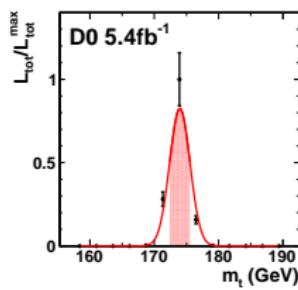
## Latest results

- ▶ DØ [5.4 $\text{fb}^{-1}$ ]:  $m_t = 174.0 \pm 3.1 \text{ GeV}/c^2$  [Matrix Element]  
[ Phys. Rev. Lett. 107 (2011) 082004; arXiv:1105.0320v2 [hep-ex] ]
- ▶ CDF [5.6 $\text{fb}^{-1}$ ]:  $m_t = 170.3 \pm 3.7 \text{ GeV}/c^2$  [Template Method]  
[ Phys.Rev.D 83 (2011) 111101; arXiv:1105.0192 [hep-ex] ]
- ▶ CDF [2.0 $\text{fb}^{-1}$ ]:  $m_t = 172.3 \pm 4.0 \text{ GeV}/c^2$  [Dalitz-Goldstein Method]  
[ CDF/PUB/TOP/PUBLIC/10635 ]



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Top Mass @ Tevatron



September 28, 2011

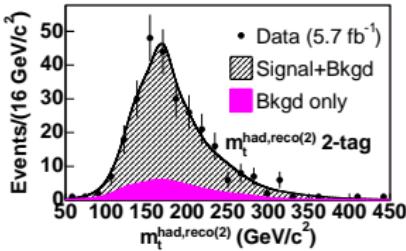
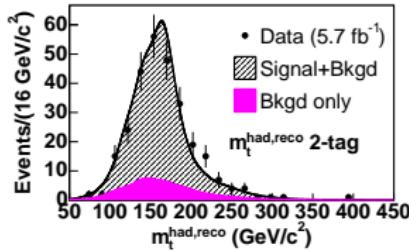
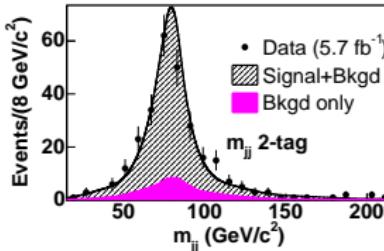
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# $\cancel{E}_T + \text{jets}$

- ▶ Analyzes events without reconstructed  $e$  or  $\mu$ ; sensitive to  $\tau$ 's (40% of signal);
- ▶ Sensitive to new physics in the  $\tau$  sector;
- ▶ 4 – 6 jets ( $E_T > 15$  GeV), lepton veto ( $p_T > 20$  GeV/c),  $\cancel{E}_T / \sum E_T^{\text{jets}} > 3$  GeV $^{1/2}$
- ▶ NN event selection, data-driven background model;
- ▶ Only the hadronically decaying top is reconstructed (in two ways):
  - ▶ 3D p.d.f.s to extract  $m_t$ ;

## Latest results

- ▶ CDF [5.7 fb $^{-1}$ ]:  $m_t = 172.3 \pm 2.6$  GeV/c $^2$  [Template Method]  
[ arXiv:1109.1490v1 [hep-ex] ]

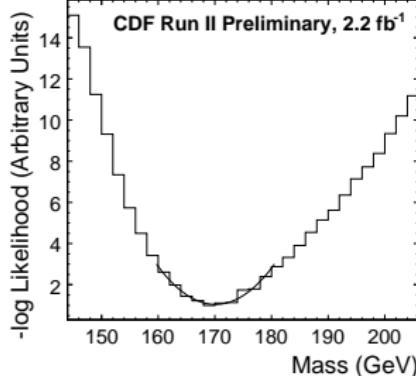
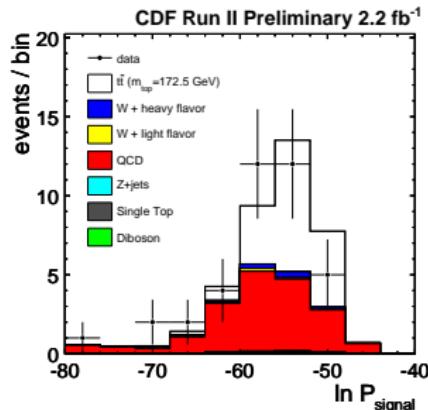
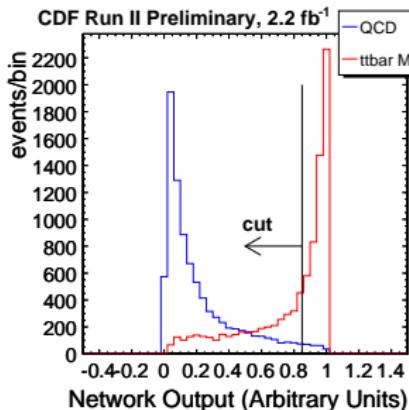


# Hadronic $\tau$ + jets

- ▶ Cross-section and first  $m_t$  measurement in  $\tau$ +jets;
- ▶ Tests lepton universality; probes a channel possibly sensitive to NP;
- ▶  $p_T(\tau) > 25$  GeV/c, jets with  $E_T > 20$  GeV,  $\cancel{E}_T > 20$  GeV,  $\geq 1$  b-tag;
- ▶ JES is largest systematic ( $3.4$  GeV/c $^2$ );

## Latest results

- ▶ CDF [2.2fb $^{-1}$ ]:  $m_t = 172.7 \pm 10.0$  GeV/c $^2$  [Matrix Element]  
[ CDF/PUB/TOP/PUBLIC/10562 ]

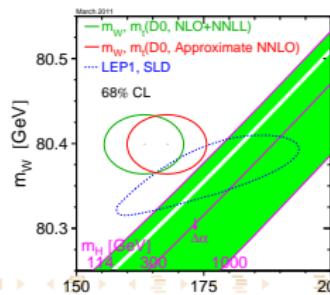
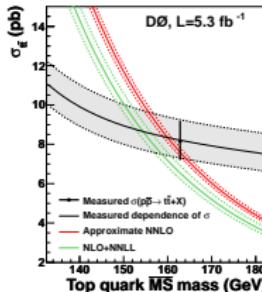
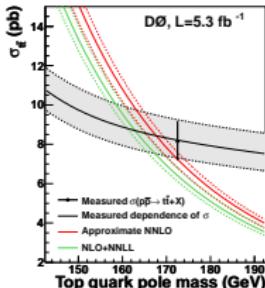


# Top mass from cross-section measurement

- Acceptance from MC (as a function of  $m_t$ ) used to determine  $\sigma_{t\bar{t}}(m_t)$ ;
- $\sigma_{t\bar{t}}$  compared to higher-order predictions (NLO+(N)NLL)/Approx. NNLO);
- Most likely  $m_t$  from  $L(m_t) = \int f_{\text{exp}}(\sigma|m_t) [f_{\text{scale}}(\sigma|m_t) \otimes f_{\text{PDF}}(\sigma|m_t)] d\sigma$ ;
- Performed for two assumptions for  $m_t^{\text{MC}} = m_t^{\text{pole}}$  and  $m_t^{\text{MC}} = m_t^{\overline{\text{MS}}}$ .

Latest results from DØ [5.3fb<sup>-1</sup>]: experimental  $m_t$  closer to pole mass

- $m_t^{\text{pole}} = 167.5 \pm 5.0 \text{ GeV}/c^2$ ;  $m_t^{\overline{\text{MS}}} = 160.0 \pm 4.6 \text{ GeV}/c^2$  [Approx. NNLO]  
[ arXiv:1104.2887v1 [hep-ex] ]

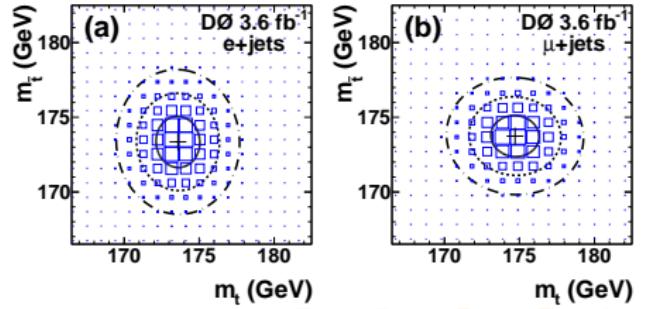
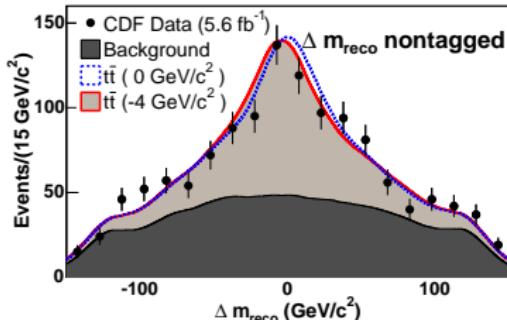


# Top-Antitop Mass Difference

- If CPT is conserved,  $\Delta m = M_t - M_{\bar{t}} = 0$ ;
- This assumption is used in top mass measurements till now;
- Good agreement with SM, but still statistically limited.

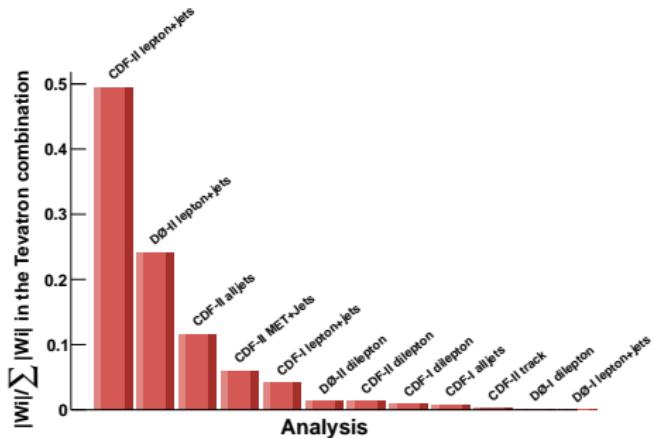
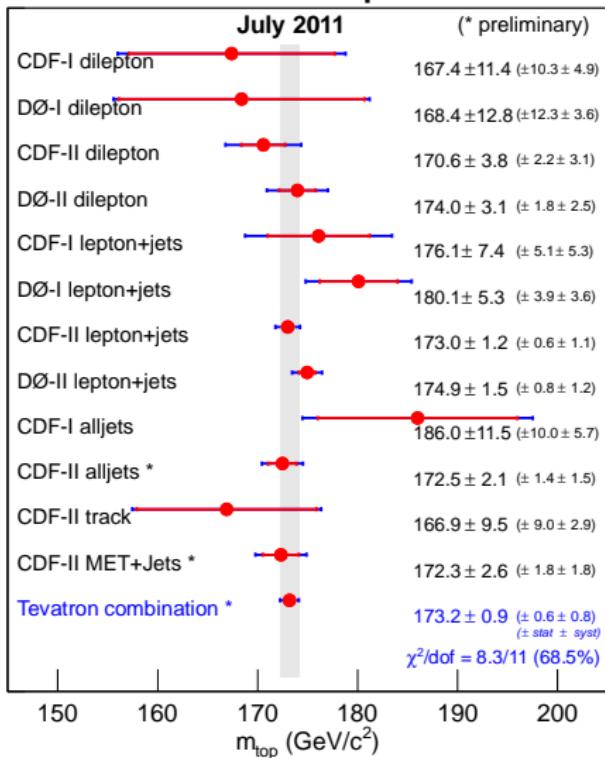
## Latest results

- CDF [5.6 $\text{fb}^{-1}$ ]:  $\Delta m = -3.3 \pm 1.7 \text{ GeV}/c^2$  [ $\Delta m$  Templates]  
[ Phys.Rev.Lett. 106 (2011) 152001; arXiv:1103.2782 [hep-ex] ]
- DØ [3.6 $\text{fb}^{-1}$ ]:  $\Delta m = 0.8 \pm 1.9 \text{ GeV}/c^2$  [Measures  $m_t$  and  $m_{\bar{t}}$ , ME]  
[ arXiv:1106.2063v2 [hep-ex] ]



# Combination

## Mass of the Top Quark



$$m_t = 173.2 \pm 0.6(\text{stat}) \pm 0.8(\text{syst}) \\ = 173.2 \pm 0.9 \text{ GeV}/c^2$$

Combination of 12 measurements.

Uncertainty below 1  $\text{GeV}/c^2$   
for the first time!

[ arXiv:1107.5255v3 [hep-ex] ]

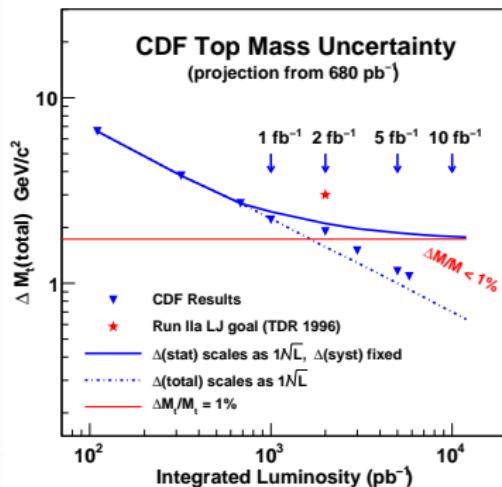
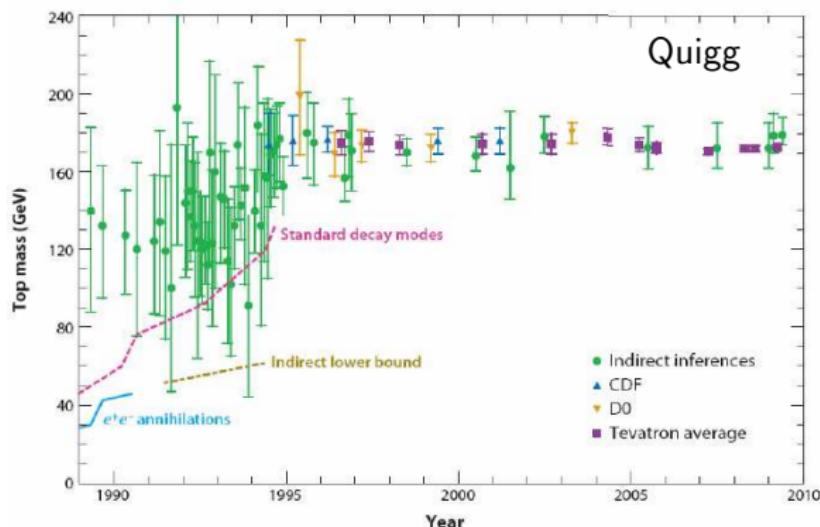
# A word on systematic uncertainties

- ▶ Results are systematically limited;
- ▶ Main systematics: JES, Singal (Generator, ISR/FSR).

Tevatron combined values ( $\text{GeV}/c^2$ )	
$m_t$	173.18
<b>iJES</b>	<b>0.39</b>
aJES	0.09
bJES	0.15
cJES	0.05
<b>dJES</b>	<b>0.20</b>
rJES	0.12
Lepton $p_T$	0.10
<b>Signal</b>	<b>0.51</b>
Detector Modeling	0.10
UN/MI	0.00
Background from MC	0.14
Background from Data	0.11
Method	0.09
MHI	0.08
Systematics	0.75
Statistics	0.56
Total	0.94

[ arXiv:1107.5255v3 [hep-ex] ]

# History of Top Mass Measurements



A long way to reach a precision of  $< 0.5\% (< 1 \text{ GeV}/c^2)$

# Summary

- ▶ The precise determination of the top quark mass,  $m_t$ , will be a legacy of the Tevatron;  
 $m_t = 173.2 \pm 0.6(\text{stat}) \pm 0.8(\text{syst}) = 173.2 \pm 0.9 \text{ GeV}/c^2$
- ▶ Top-Antitop mass difference compatible CPT invariance;  
 $\Delta m = -3.3 \pm 1.7 \text{ GeV}/c^2$  (CDF);  $\Delta m = 0.8 \pm 1.9 \text{ GeV}/c^2$  (DØ)
- ▶ Top mass measurement dominated by systematic uncertainties;  
 $\sim 0.5 \text{ GeV}/c^2$  Signal (Generator, ISR/FSR);  $\sim 0.5 \text{ GeV}/c^2$  JES

Too many results to describe here

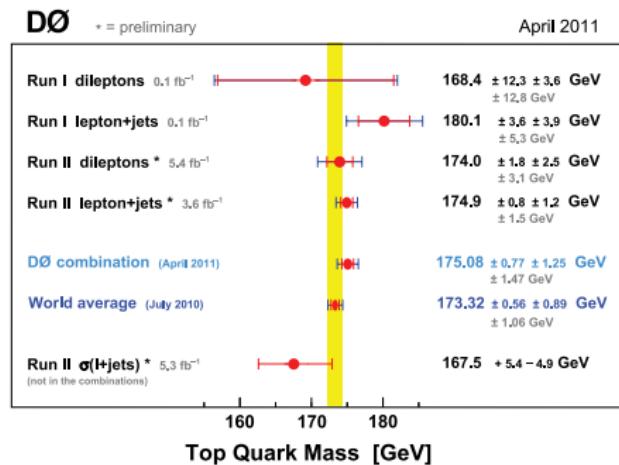
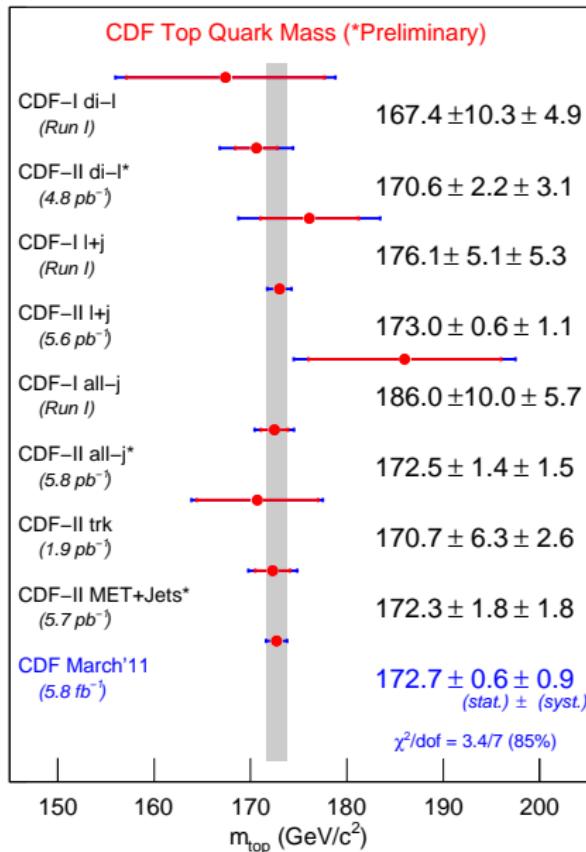
DØ <http://www-d0.fnal.gov/Run2Physics/top/>

CDF [http://www-cdf.fnal.gov/physics/new/top/public\\_mass.html](http://www-cdf.fnal.gov/physics/new/top/public_mass.html)

Thank you!

# Backup Slides

# Collaboration averages

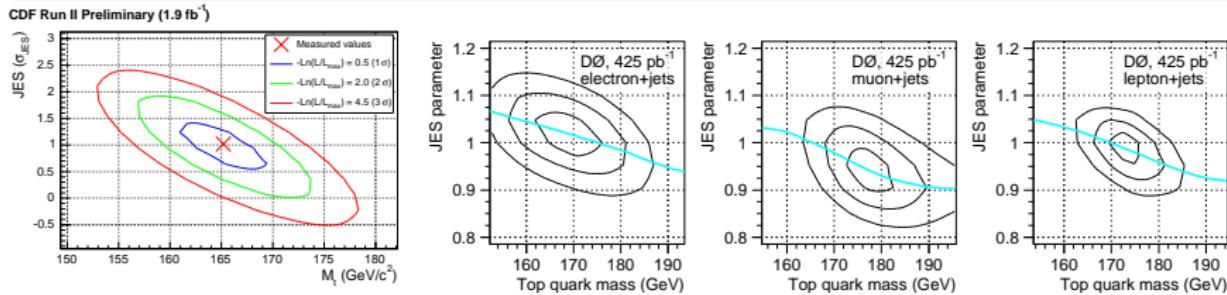


# Ideogram Method

- ▶ Using in-situ JES calibration;

## Latest results

- ▶ CDF [1.9 $\text{fb}^{-1}$ ]:  $m_t = 162.7 \pm 4.7 \text{ GeV}/c^2$  [All-Hadronic]  
[ CDF/PHYS/TOP/PUBLIC/8233 ]
- ▶ DØ [0.43 $\text{fb}^{-1}$ ]:  $m_t = 173.7 \pm 4.8 \text{ GeV}/c^2$  [Lepton+Jets]  
[ Phys.Rev.D 75 (2007) 092001; arXiv:0702018v1 [hep-ex] ]



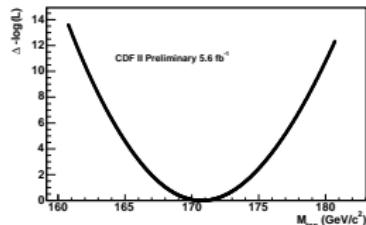
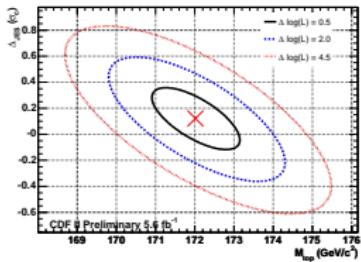
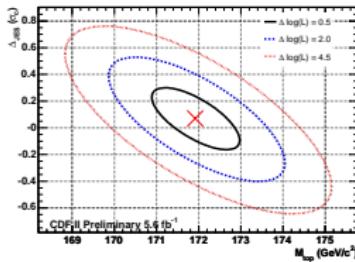
# Simultaneous Fit of Lepton + Jets and Dilepton

- ▶ Main idea: bring **in-situ** JES calibration from lepton + jets to the dilepton channel;
- ▶ Dominated by lepton + jets;

## Results (CDF [5.6 $\text{fb}^{-1}$ ])

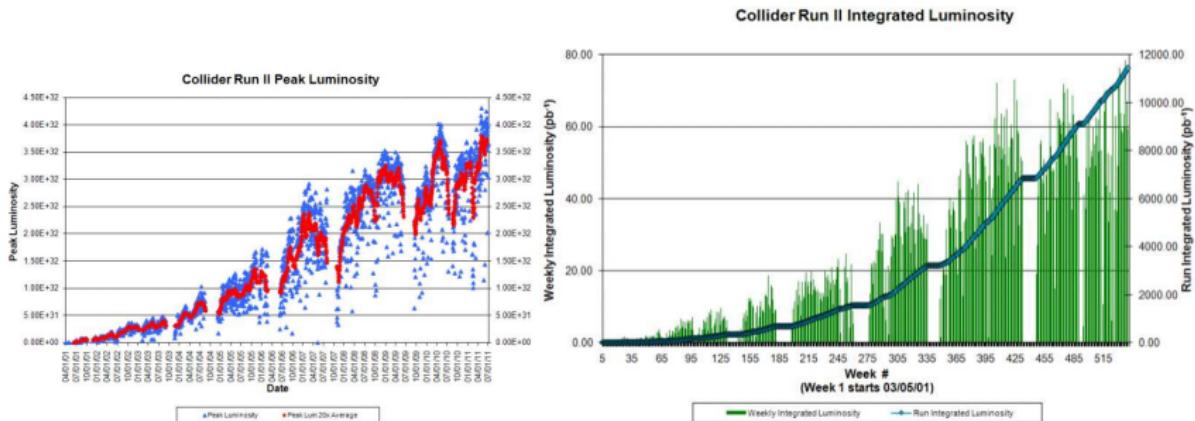
- ▶ Dilepton:  $170.3 \pm 3.7 \text{ GeV}/c^2$
- ▶ Lepton+Jets:  $172.2 \pm 1.5 \text{ GeV}/c^2$
- ▶ Combined:  $172.1 \pm 1.4 \text{ GeV}/c^2$

[ Phys.Rev.D 83 (2011) 111101; arXiv:1105.0192 [hep-ex] ]



# Tevatron luminosity

- ▶ Tevatron doing great in providing collisions to experiments.
- ▶ Today's talk: up to  $7.8\text{fb}^{-1}$  of data;



# CDF and DZero, two general purpose detectors



Tracking	Silicon Drift cell	$ \eta  < 2 - 2.5$ $ \eta  < 1.1$	Silicon Fiber	$ \eta  < 3$ $ \eta  < 1.7$
Calorimetry	Scintillators	$ \eta  < 3.6$	LAr/DU	$ \eta  < 4$
Muon chambers	Drift Scintillators	$ \eta  < 1.5$	Drift Scintillators	$ \eta  < 2.0$

