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RF-Track



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- Focus on **RF-Track [1]** as a novel simulation tool for final cooling
- Overview of implemented particle-matter interaction models
- Compare **RF-Track** with **ICOOOL[2]** and **G4BL[3]**
- To-Dos
- Conclusion

About the **RF-Track** software



- **C++** code for accelerator physics simulations.
- Utilizes GNU Scientific Library (**GSL**) and the **FFTW** library .
- Software supports **parallel processing** for increased computational efficiency in complex particle tracking within field maps.
- Users have the option to interface with **RF-Track** using **Python** or **Octave**.
- **Collective Effects:**
 - Space charge forces
 - Short- and long-range wakefields
 - Beam loading phenomena
- **Single-Particle Effects:**
 - Incoherent synchrotron radiation
 - Magnetic multipole kicks
 - Multiple Coulomb scattering

Particle-material interactions that are relevant for ionization cooling

Energy loss/ loss fluctuation

Multiple Coulomb scattering

Implementation into the **RF-Track** code

Reference materials for benchmarkings studies

- Performed benchmarkings:
 1. Absorbers
 - I. Liquid hydrogen
 - II. Lithium hydride
 - III. Beryllium
 2. Solenoid
 3. Single final cooling cell

Parameter	Unit	Magnitude
Material		LiH
Thickness	mm	65.37
Density	g cm^{-3}	0.69
Li6 Fraction	by mass	0.814
Li7 Fraction	by mass	0.043
H Fraction	by mass	0.143
Momenta		171.55, 199.93, 239.76
Material		liquid H ₂
Thickness	mm	349.6
Density	g cm^{-3}	0.07053
Momenta	MeV c^{-1}	164.9, 199.0, 237.1
Material		liquid H ₂
Thickness	mm	10
Density	g cm^{-3}	0.07053
Momenta	MeV c^{-1}	30
Number of particles		10^6

Energy loss liquid hydrogen

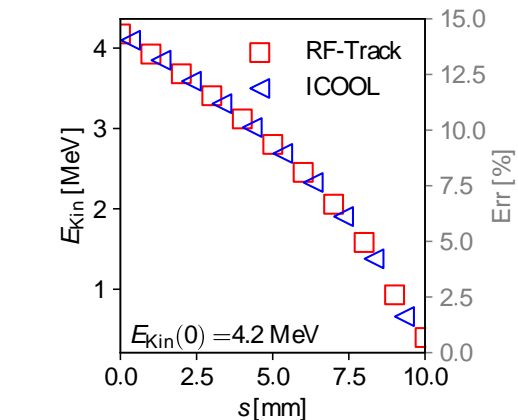
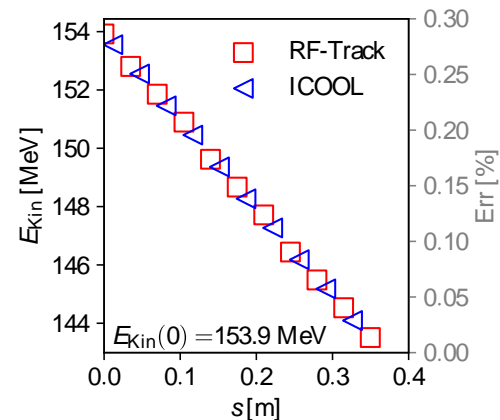
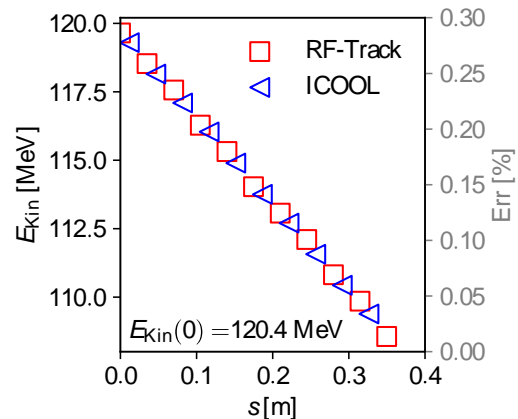
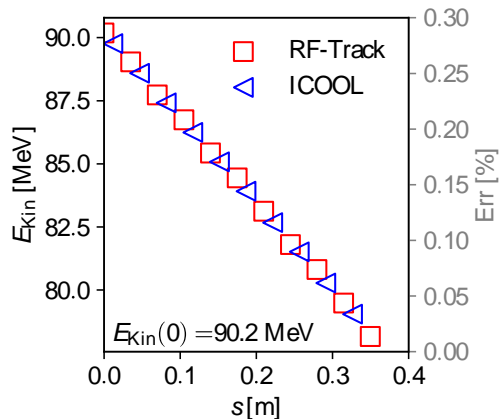
Bethe-Bloch equation

$$-\left\langle \frac{\partial E}{\partial s} \right\rangle = K \frac{Z}{A} \frac{1}{\beta^2} \left[\frac{1}{2} \ln \left(\frac{2m_e c^2 \beta^2 \gamma^2 T_{\max}}{I^2} \right) - \beta^2 - \frac{\delta(\beta\gamma)}{2} \right]$$

Energy loss of muons depends on:

- Energy of the particle
- Material properties
- Path length

- Compare **RF-Track** energy loss of liquid hydrogen with **ICOOOL**
- Error is less than 0.3%
- Results show good agreement.
- Error **increase** in case of particle **losses** (see lower right plot).



Energy loss lithium hydride (LiH)

- The ICOOL manual presents **LiH** with a different density and a varying composition of **Li6** and **Li7** compared to the LiH sample form **MICE**.
- Mixing a specific material with **ICOOL** might require some additional clarification, as the process isn't immediately intuitive.
- Therefore, **RF-Track** energy loss benchmarking of **LiH** with **G4BI**.

How to mix material in **RF-Track** and **G4BL** – code example:

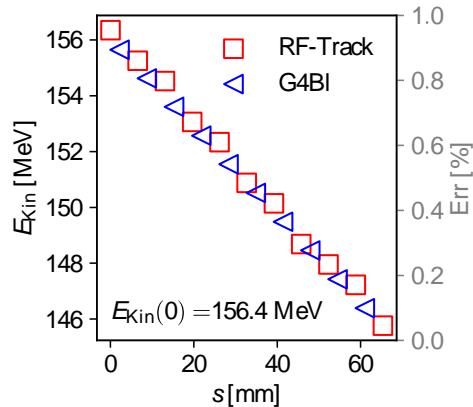
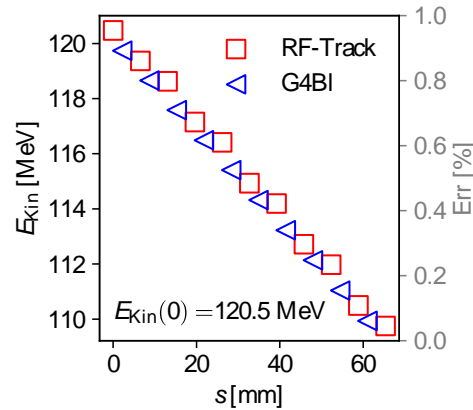
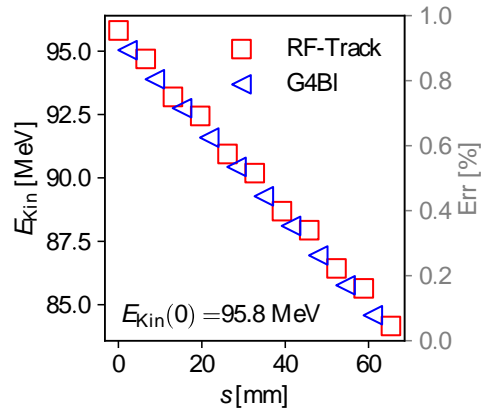
RF-Track

```
frac_Li = 0.86
frac_H = 0.14
A_Li_Mice, A_H = 6.05, 1.0079 #atomic numbers
Li = RF_Track.Absorber(abs_len, X0_Li, Z=3., A=A_Li_Mice, rho_LiH * frac_Li, I=40.)
H = RF_Track.Absorber(abs_len, X0_H, Z=1., A=A_H, rho_LiH * frac_H, I=21.)
V.add(Li, 0, 0, 0, 'entrance')
V.add(H, 0, 0, 0, 'entrance')
```

```
material Li6 Z=3 A=6 density=0.539
material Li7 Z=3 A=7 density=0.534
material LiH Li6,0.814 Li7,0.043 H,0.143 density=0.69
```

G4BI

Energy loss lithium hydride (LiH)



- Error slightly higher, than compared to LH
- Might come from different mixing techniques

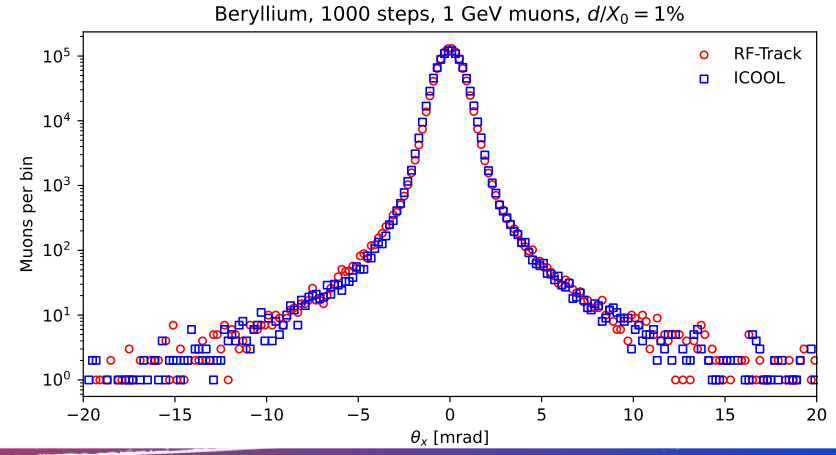
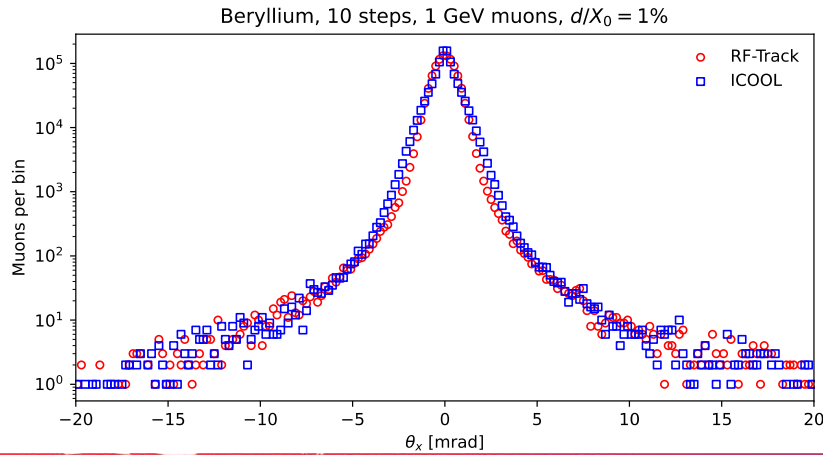
Semi-Gaussian distribution as scattering model in **RF-Track** [9,10]

$$f(\theta) = (1 - \epsilon) \frac{\theta e^{-\frac{\theta^2}{2\sigma^2}}}{\sigma^2} + \epsilon \frac{2a^2\theta}{(\theta^2 + a^2)^2}$$

- The tail weight factor ϵ indicates the probability of a particle to be long ranged scattered
- The first term represents the **core** Gaussian of the distribution
- Term 2 shows a non-Gaussian single scattering distribution (**tails**)
- **ICool** and **G4BI** use the **Moliér** algorithm from the Gant4 library.

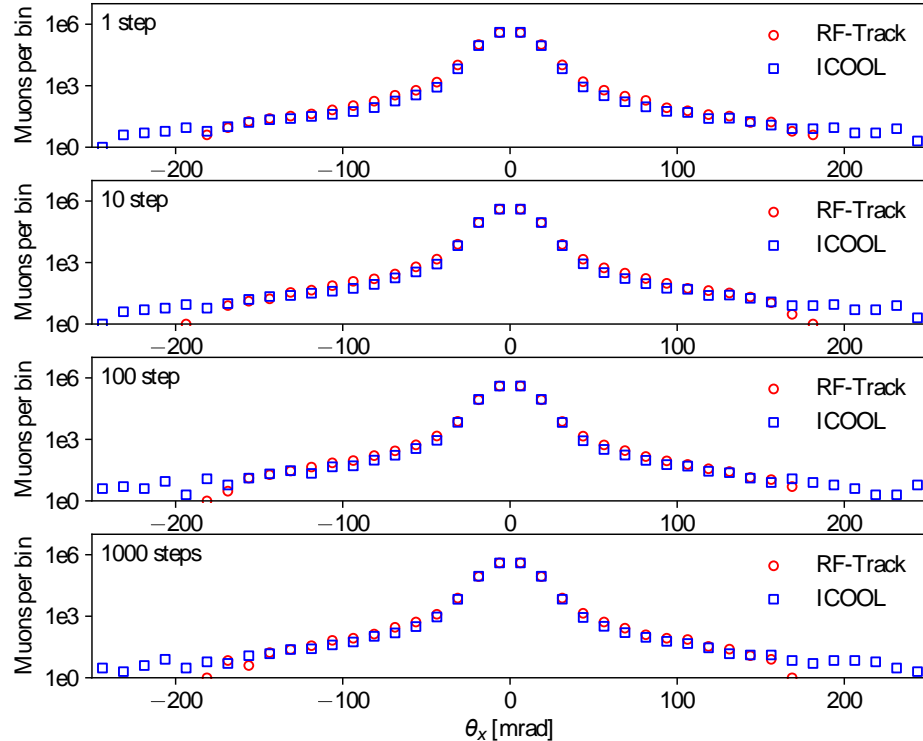
First try: ICool vs RF-track: Beryllium

- 1E6 muons for each simulation
- Start: 1 GeV mono energetic pencil beam
- Absorber length: 1% of radiation length
- The shape of the distribution changes minimally with the number of integration steps.
- The Moliér model lacks on the convolution property, indicating potential for further improvement.

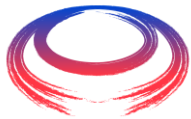


ICOOOL vs RF-Track: Liquid hydrogen

LH length: 349.5mm, $p = 164.9$ MeV



- 1E6 muons for each simulation.
- Example with 1, 10, 100 and 1000 steps.
- Excellent agreement is observed with **ICOOOL**.
- Exception: the **ICOOOL** model overestimates the tails slightly .

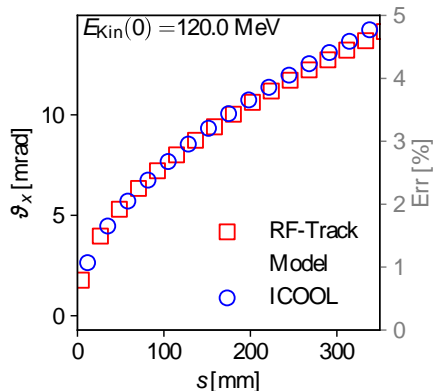
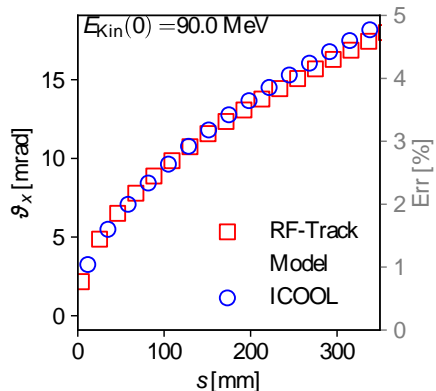


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Std. scatter angle benchmarks

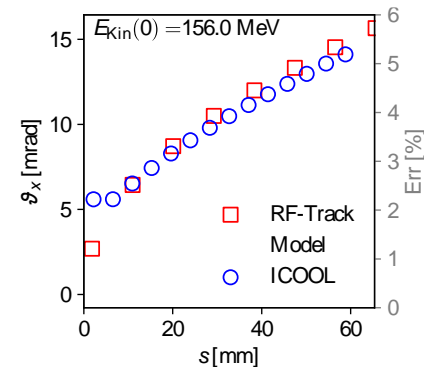
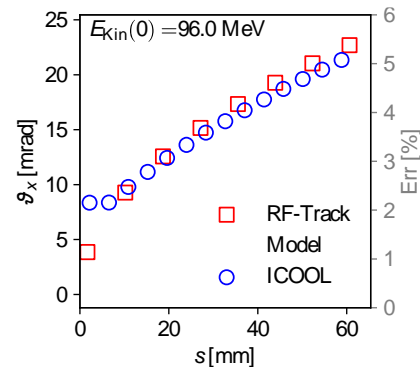
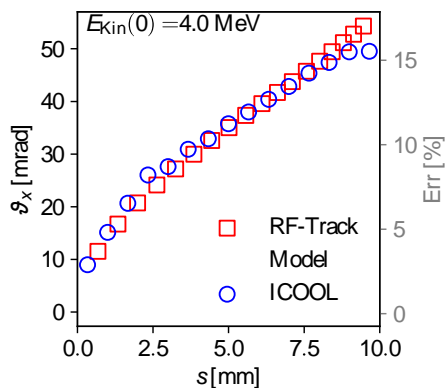
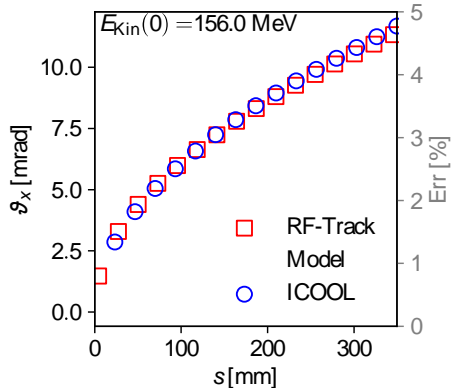


Liquid hydrogen Examples

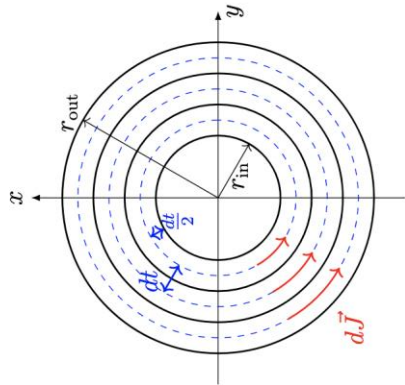
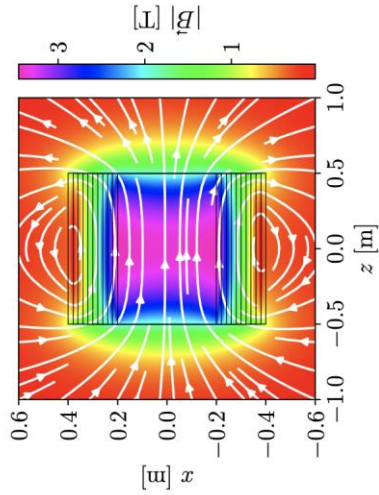


- Error are in the range of 5%.
- Exception: low energy example, due to high losses.

LiH Examples



Solenoid model

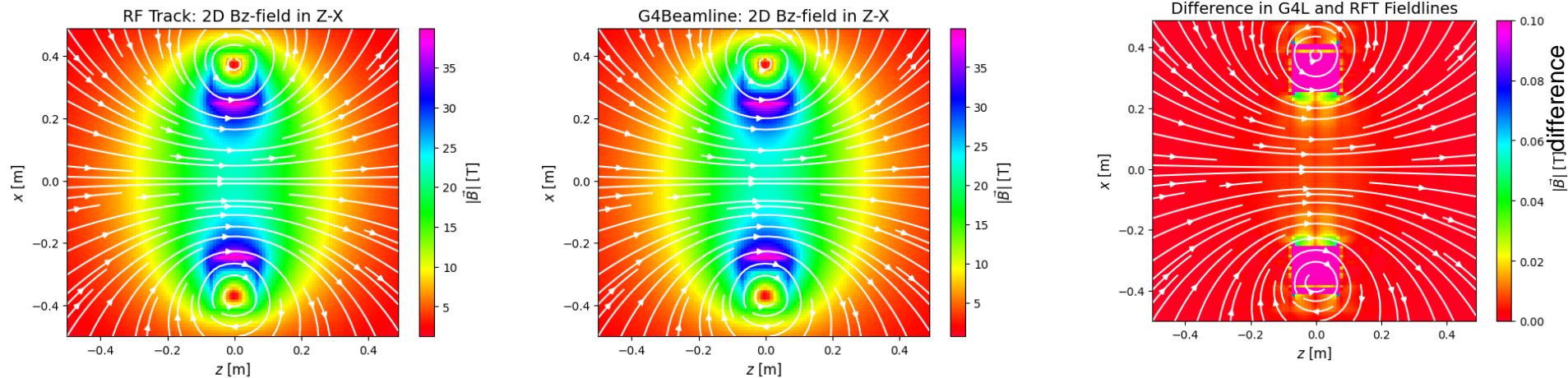


- **RF-Track** uses the current sheet model for solenoids.
- The model is based on **elliptical integral functions**.
- These functions come from GSL but require more computational time to evaluate field strength for all particle positions.
- **Solution:** **RF-Track** creates a meshgrid of the 3D solenoid field and uses an interpolation function to provide field strengths during particle tracking.

Solenoid field benchmarking

- Comparison **RT-Track** with **G4BL**.
- Sheet number: 200
- We find slightly differences in the off-axis and coil regions.

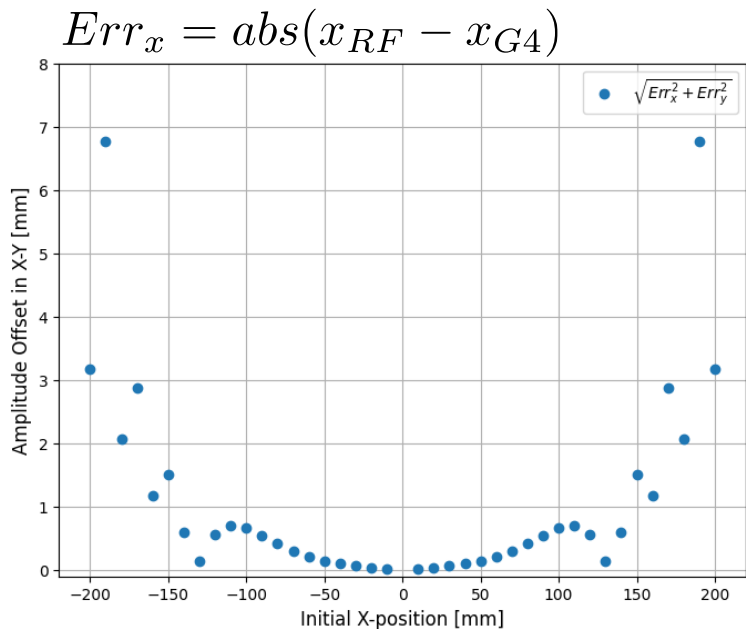
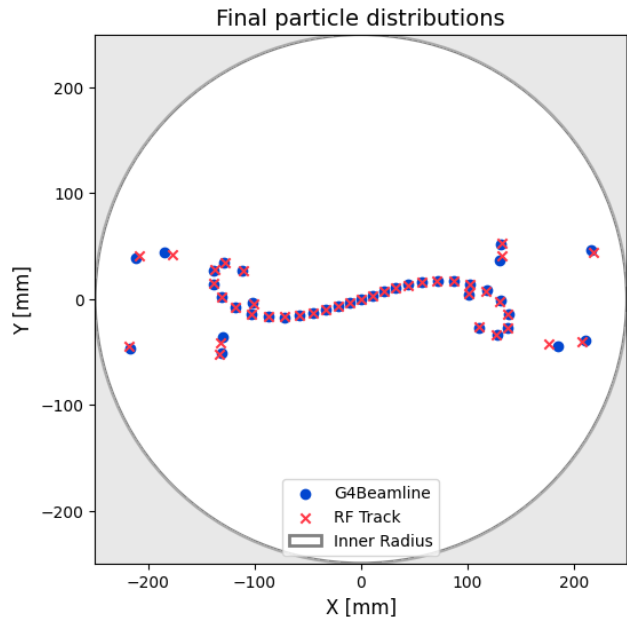
Parameter	Unit	Magnitude
Coil inner radius	mm	250.0
Coil radial thickness	mm	169.3
Coil outer radius	mm	419.3
Coil length	mm	140.0
Current density	A/mm ²	500.0
Particle species		μ^+
Particle momentum	MeV/c	200.0
Particle z start	mm	-500.0
Particle z end	mm	500.0
Particle radial step	mm	10.0
Particle maximum radius	mm	200.0

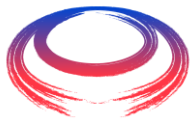




Solenoid field: particle tracking benchmarking

Parameter	Unit	Magnitude
Coil inner radius	mm	250.0
Coil radial thickness	mm	169.3
Coil outer radius	mm	419.3
Coil length	mm	140.0
Current density	A/mm ²	500.0
Particle species		μ^+
Particle momentum	MeV/c	200.0
Particle z start	mm	-500.0
Particle z end	mm	500.0
Particle radial step	mm	10.0
Particle maximum radius	mm	200.0

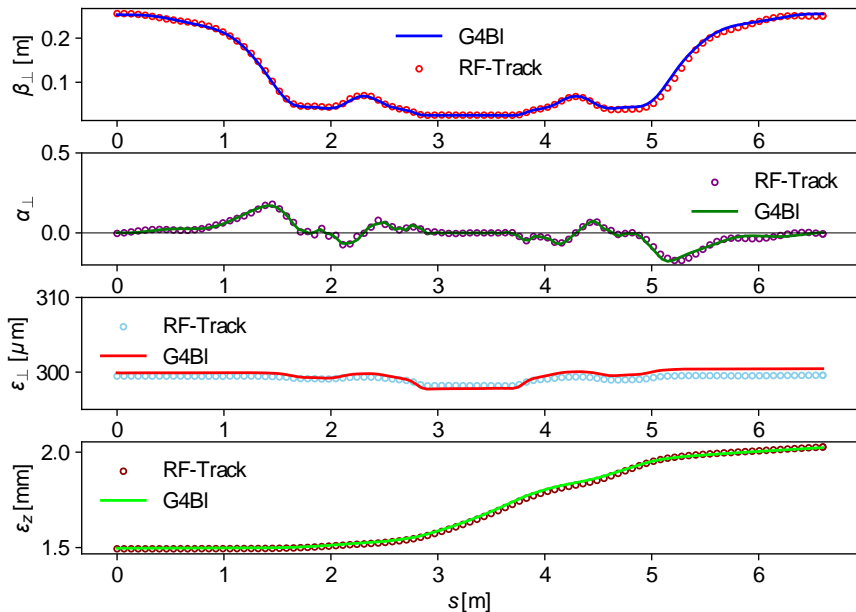




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Final cooling cell example

No absorber

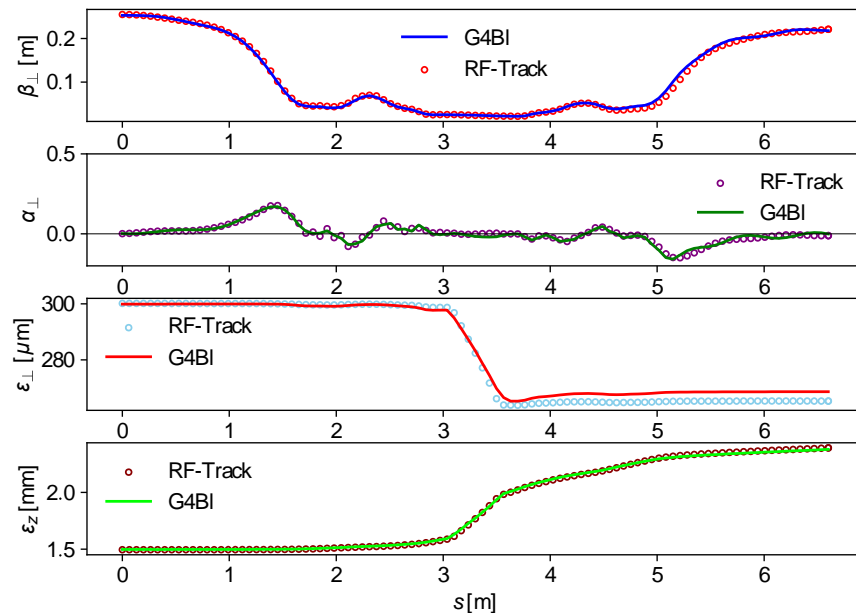


Computation time

	RF-Track	G4Beamline
time	5 min 1 s	15 min 55 s

Slightly higher cooling with **RF-Track**, which must be investigated.

With absorber

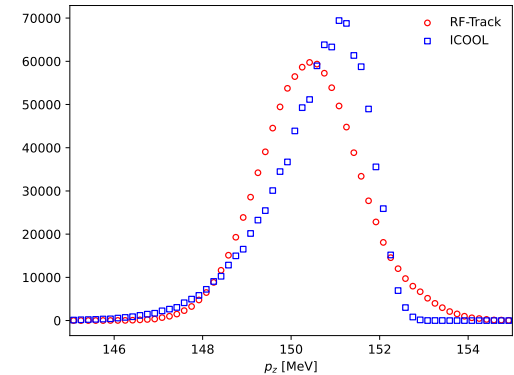
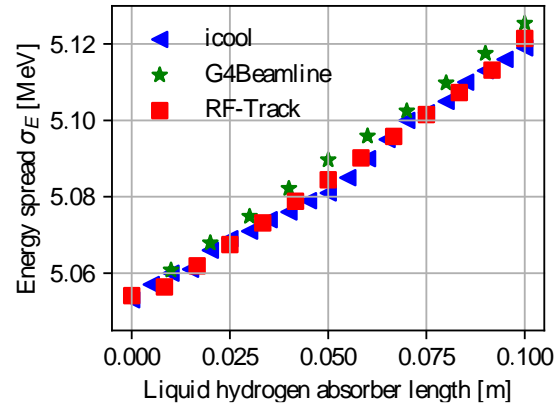


Computation time

	RF-Track	G4Beamline
time	9 min 3 s	16 min 57 s

To-do list for RF-Track

- **RF-Track** assumes the energy fluctuation as normal distributed.
- It must be Vavilov/Landau distributed.
- The Gauss approximation is valid for very thick materials.



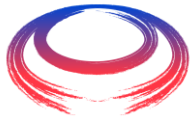
- Comparison of tracking in cavities.
- RF-Track uses TM011 mode; G4BL uses TM010 mode.
- TM011 is the better option, since we consider window less cavities in final cooling.

Summary & outlook

- Energy loss model **in RF-Track** show high agreement with **ICOOL** and **G4BL**
- A multiple Coulomb scattering model based on a semi-Gaussian mixture model was added in **RF-Track** and compared with **ICOOL**.
- Results were compared with **ICOOL**, showing excellent benchmarking results.
- This new tool enables an optimized design of ionization cooling channels for a future muon collider.
- Next step: Focus on longitudinal beam distributions

Thank you for your attention





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Reference list

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- [2] R. Fernow, "COOL: a simulation code for ionization cooling of muon beams", *Proc. of the 1999 Particle Accelerator Conference*, New York, NY, USA, 1999, pp. 3020-3022 vol.5, doi:10.1109/PAC.1999.792132.
- [3] T.J. Roberts, "G4beamline simulation program for matter-dominated beamline", *IEEE Particle Accelerator Conference (PAC)*, Albuquerque, NM, USA, 2007, pp. 3468-3470, 2007, doi: 10.1109/PAC.2007.4440461.
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- [5] C. Rossi et al., "The deep electron flash therapy facility"
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- [7] Y. Zhao et al., "Comparison of Different Matching Device Field Profiles for the FCC-ee Positron Source,"
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- [9] R. Frühwirth, M. Liendel: Mixture models of multiple scattering: computation and simulation.
- [10] R. Frühwirth, M. Regler: On the quantitative modelling of core and tails of multiple scattering by Gaussian mixtures .
- [11] B. Palmer: Muon final cooling in 30-50T solenoids.