





How Matter Matters:

The Story of Time Invariance Violation in Neutrino Oscillations

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If we follow that CPT is a fundamental symmetry.



- ✓ Charge conjugation
- ✓ Parity
- ✓ Time reversal



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Charge parity transform (CP) alone is <u>violated in the</u> <u>weak sector.</u>







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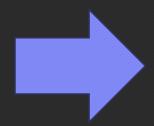
Charge parity transform (CP) alone is <u>violated in the</u> <u>weak sector.</u>

Time reversal transforms alone should also be violated in weak interactions, in order to <u>preserve</u> the overall symmetry.











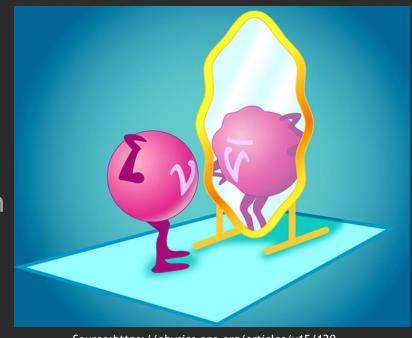
- ✓ Charge conjugation
- ✓ Parity
- ✓ Time reversal



✓ Neutrino physics is a well motivated probe for CP violation, but we are limited to "improper tests" due to our inability to build experiments in an anti-Earth.



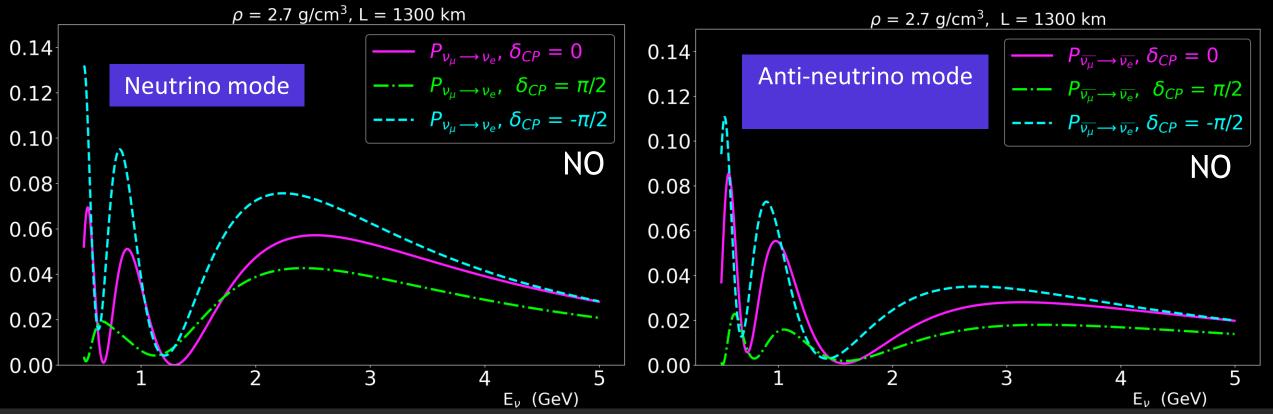
- ✓ Neutrino physics is a well motivated probe for CP violation, but we are limited to "improper tests" due to our inability to build experiments in an anti-Earth.
- ✓ Let us then consider to what extent time invariance violation occurs within the neutrino sector.
- ✓ Why? New physics may not impact both CP and time reversal in the same way.



Source:https://physics.aps.org/articles/v15/120 Credit:APS/Carin Cain

Motivation from the experiments story





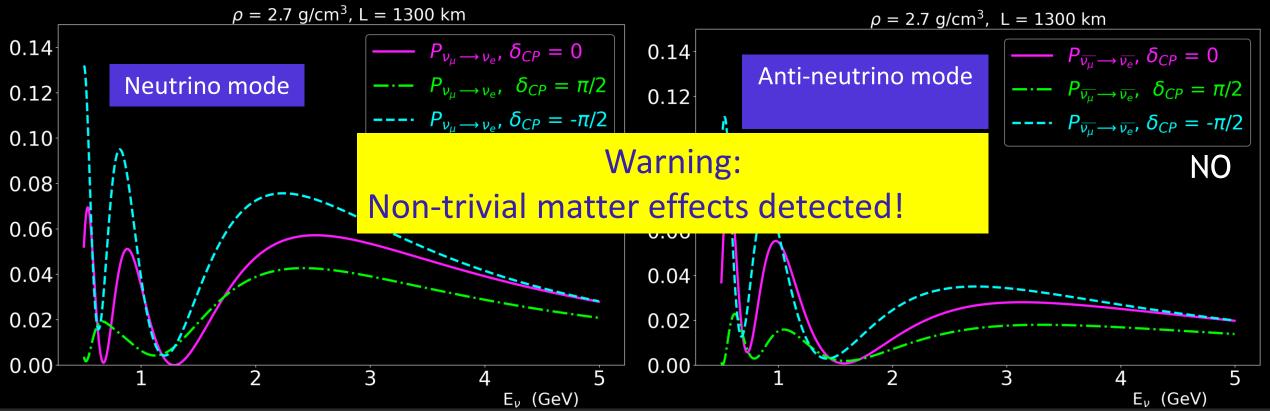
CP conjugate channels are the *most common probes,* as they are more <u>accessible to experiments</u> like long baselines.



Source:https://www.dunescience.org/

Motivation from the experiments story





CP conjugate channels are the *most common probes,* as they are more <u>accessible to experiments</u> like long baselines.



Source:https://www.dunescience.org/





✓ Time invariance violation tests may provide a clearer way* to aid in our understanding of how different matter profiles can affect neutrino oscillations

(i.e. distinguishing between intrinsic & induced time invariance violation)

*dependent upon matter potential profile



Source: (Time-turner) https://tenor.com/view/time-turner-harry-potter-moving-spinning-gif-16031036



Enter Time Invariance Violation Tests

Time invariance tests require comparing

We assume that a new beam capable of producing high energy ν_e 's exists (i.e. muon storage rings as neutrino factories).





Enter Time Invariance Violation Tests

<u>Time invariance tests</u> are *not new*, but the full range of nuances with a variety of different matter profiles, is perhaps not as widely appreciated.

Our aim is to provide a fresh perspective and different insight in this pedagogical study.

For more details about previous work around this topic, please see backup slides.

Recalling 3-Flavor Neutrino Oscillations with Charge-**Current Matter Effects**



$$U = \begin{bmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{bmatrix}$$

(PMNS matrix)



Sources: https://neutrino.syr.edu/research/neutrino-oscillations/& https://neutrino-history.in2p3.fr/neutrino-oscillation/

$$\mathbf{M}^{2} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta \mathbf{m}_{21}^{2} & 0 \\ 0 & 0 & \Delta \mathbf{m}_{31}^{2} \end{pmatrix} \qquad A = \begin{pmatrix} \sqrt{2}G_{F}N_{e} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$A = \begin{pmatrix} \sqrt{2}G_F N_e & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

+/- for neutrinos/antineutrinos





To clarify what "comparisons" we are making in looking for time invariance violation effects, we've specified two distinct measures:

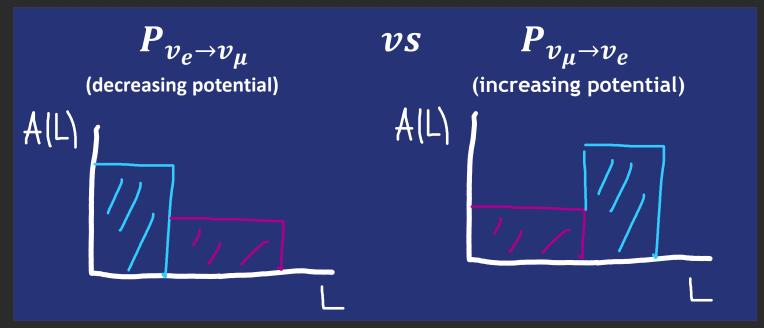
- 1. proper time invariance: (aka: true time invariance violation)
 - Not a good observable, but certainly no harder to calculate than CP conjugate channels.
 - Requires comparing probabilities with final states exchanged and <u>swapping the</u> <u>detector with source.</u>

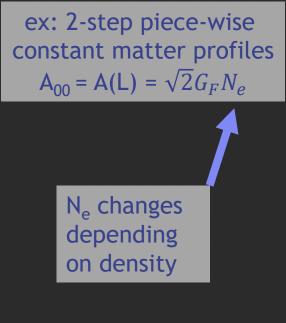




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1. proper time invariance: (aka: true time invariance violation)



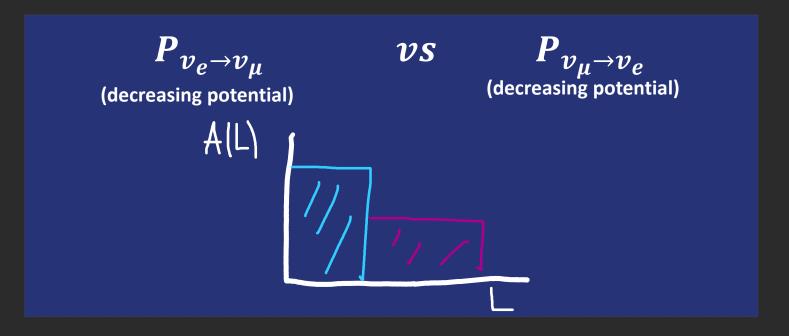




Defining Time Invariance Measures



- 2. improper time invariance: (next best thing!)
 - Compares probabilities with only the final states exchanged.

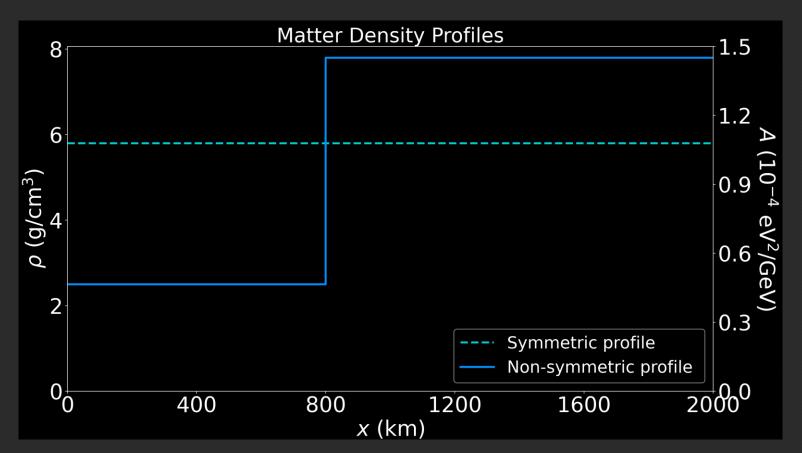


This is what an experiment can measure!

Modeling Matter Effects for 3-Flavors



✓ For the purposes of our study, we separately two types of matter potential profiles.



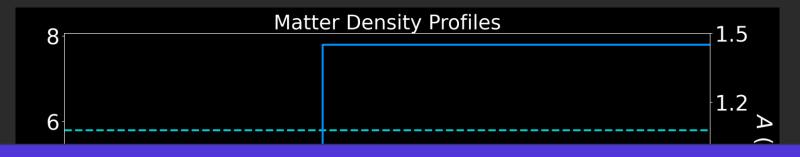
Symmetric: vacuum or single step constant matter potential profile

Non-symmetric: piece-wise matter potential profiles (increasing or decreasing)



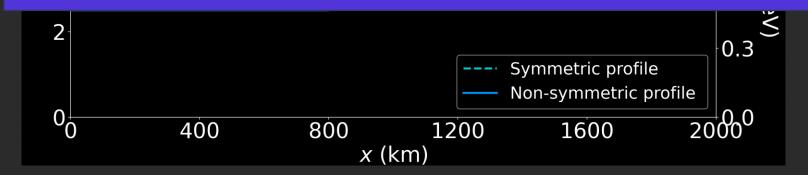


✓ For the purposes of our study, we separately two types of matter potential profiles.



Symmetric: vacuum or single step constant matter potential profile

All mixing parameters (apart from δ_{CP}) have been drawn from NuFIT 2024 global fits: (arXiv:2007.14792 & NuFIT 6.0 (2024), www.nu-fit.org)





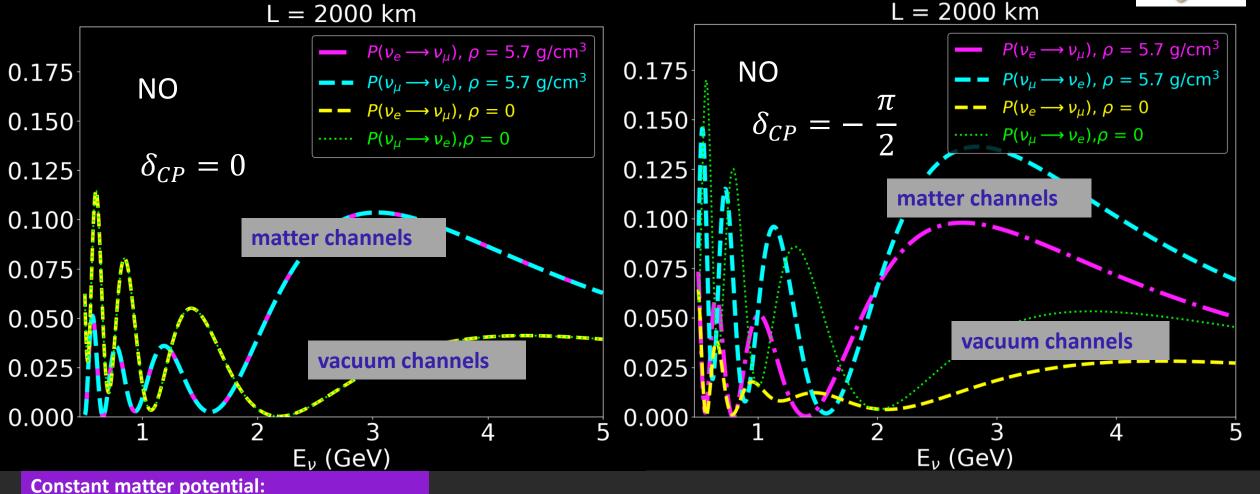
Disclaimer!

The first part of the following analysis is done with hypothetical/fictious matter effects, to get a general sense of how intrinsic versus induced time invariance violation behave with matter effects in cases that the have stronger oscillation differences.



Symmetric Matter Potential Profiles

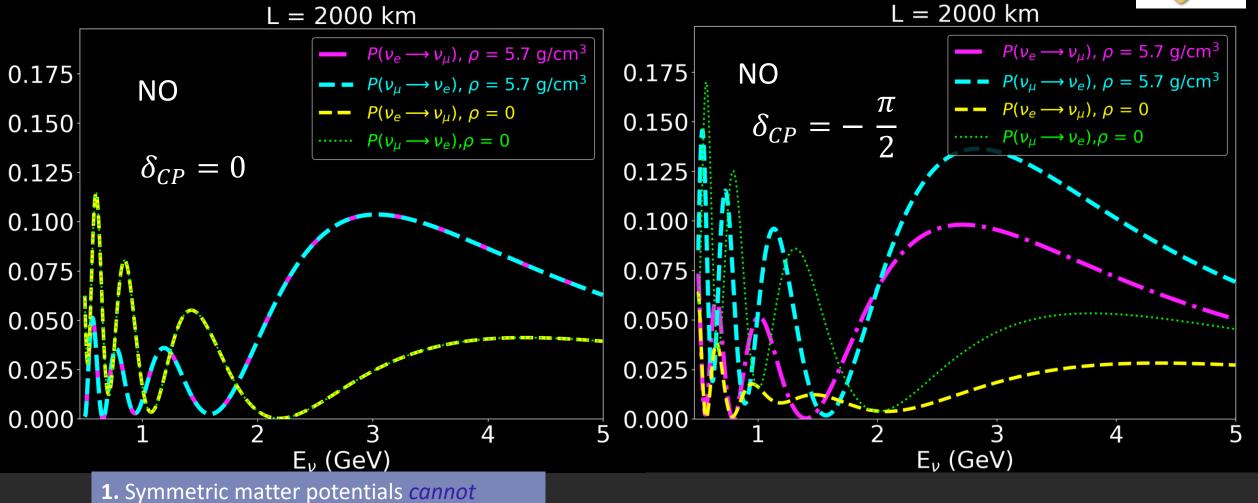




12

 $1.1x10^{-3} \text{ eV}^2/\text{GeV} (5.7 \text{ g/cm}^3)$





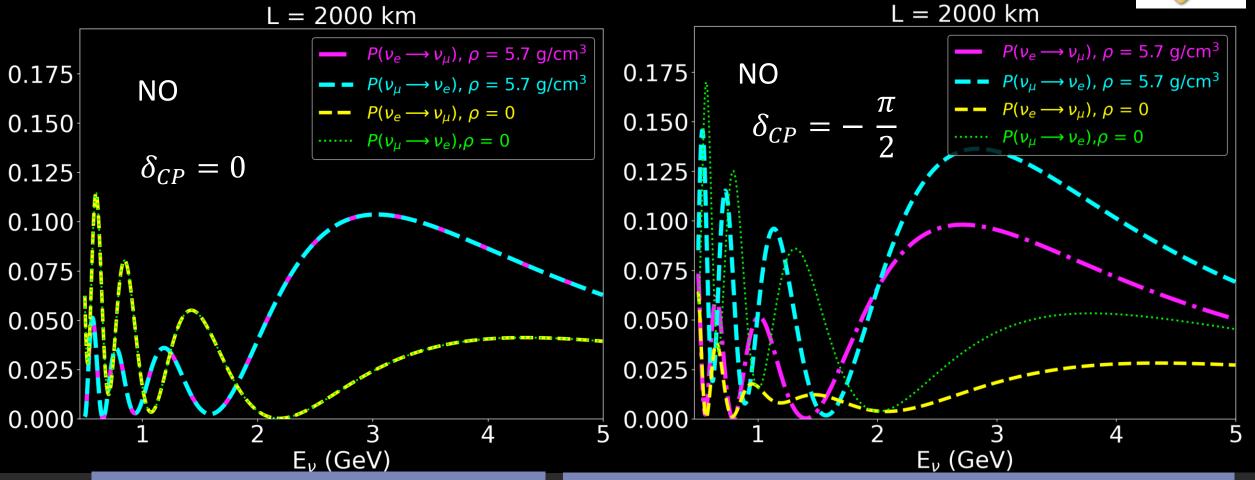
12

induce time invariance violation.

1. Symmetric matter potentials *cannot*

induce time invariance violation.



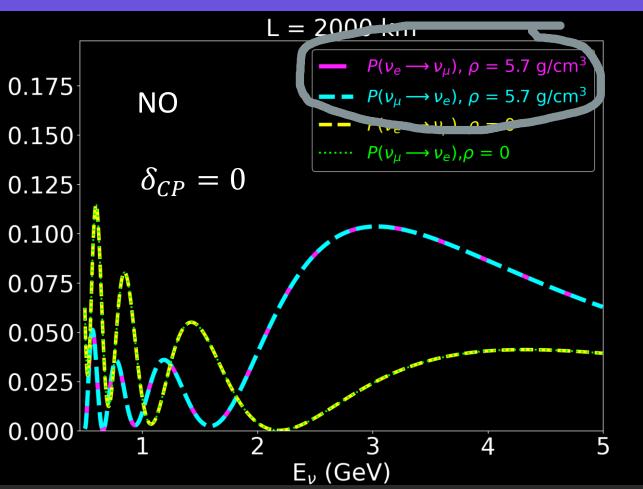


matter potential *modifies the size of the effects*.

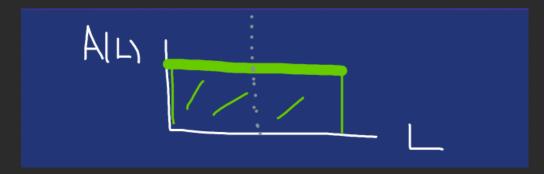
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2. If there is intrinsic time invariance violation from δ_{CP} , then the





If we exchange final states, same matter potential profile.



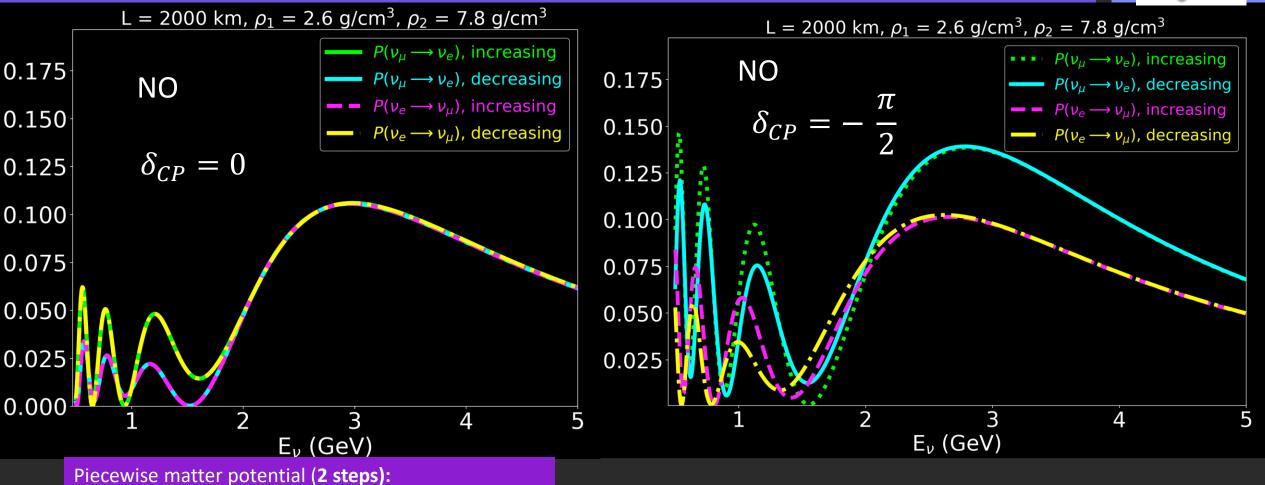
3. Improper and proper comparisons are the same if the *matter potential is symmetric*.



Non-Symmetric Matter Potential Profiles

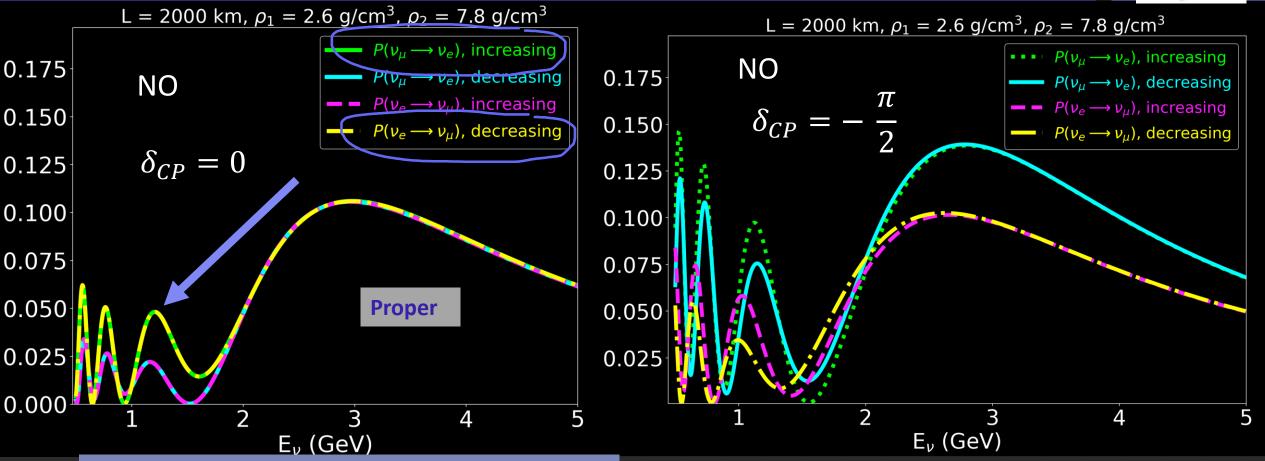
 $A_1 = 5x10^{-4} \text{ eV}^2/\text{GeV} (2.6 \text{ g/cm}^3)$ $A_2 = 1.5 \text{ x}10^{-3} \text{ eV}^2/\text{GeV} (7.8 \text{ g/cm}^3)$





14



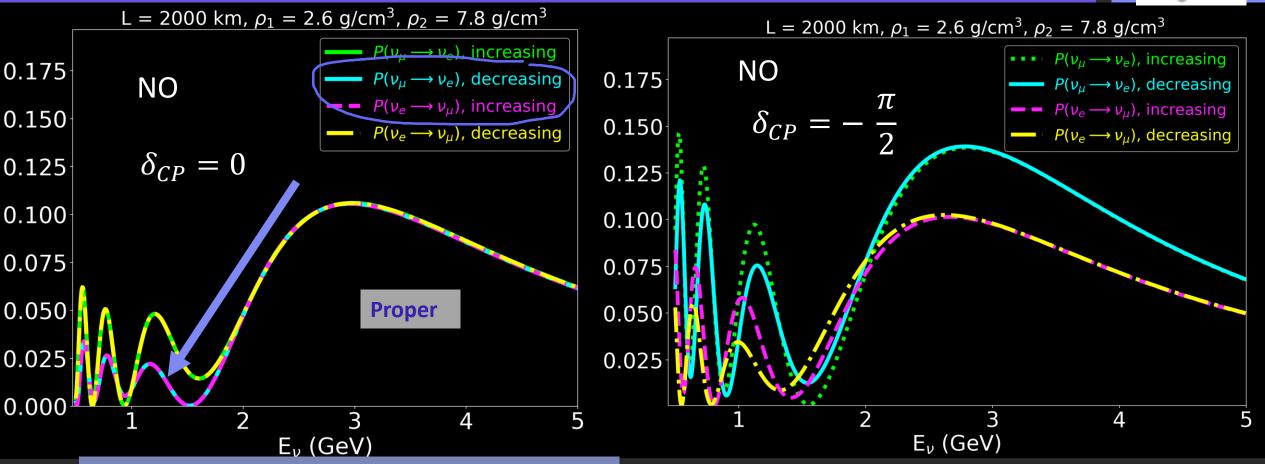


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1. Non-symmetric matter effects are pairwise

degenerate in the proper measure $(\delta_{CP} = 0)$





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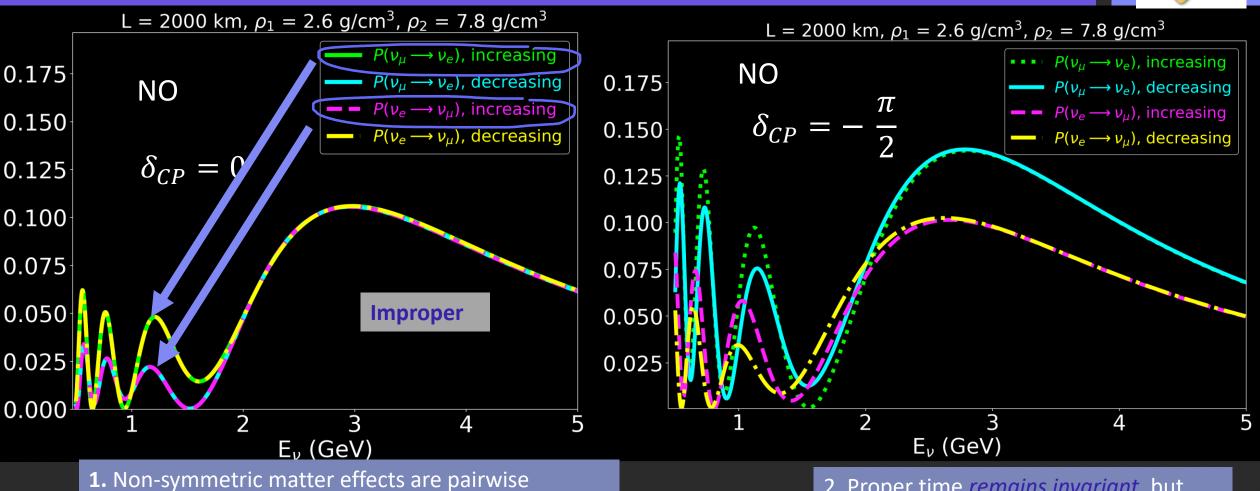
degenerate in the proper measure $(\delta_{CP} = 0)$

14



2. Proper time *remains invariant,* but

improper channels are different.



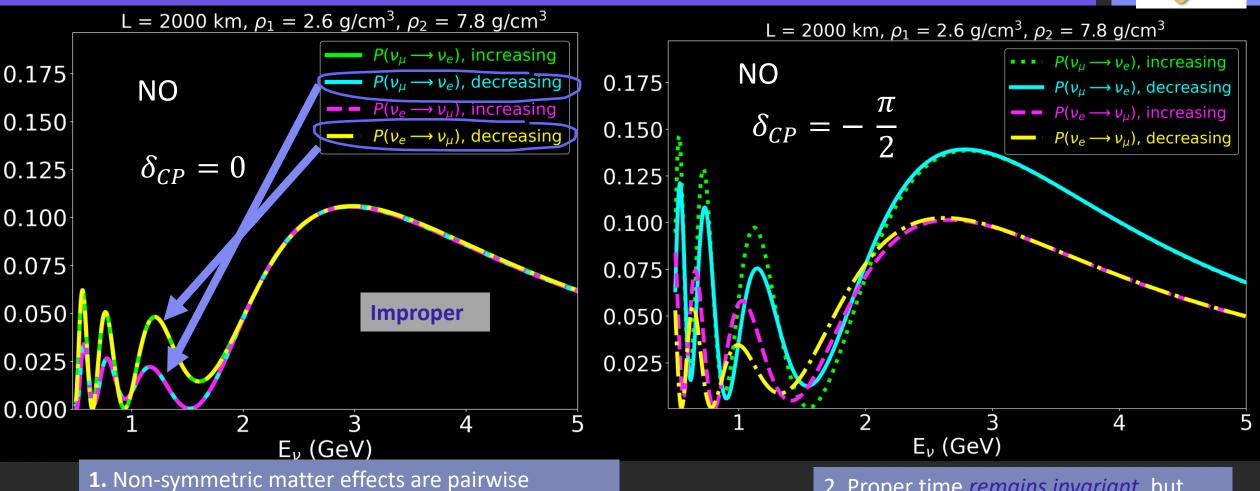
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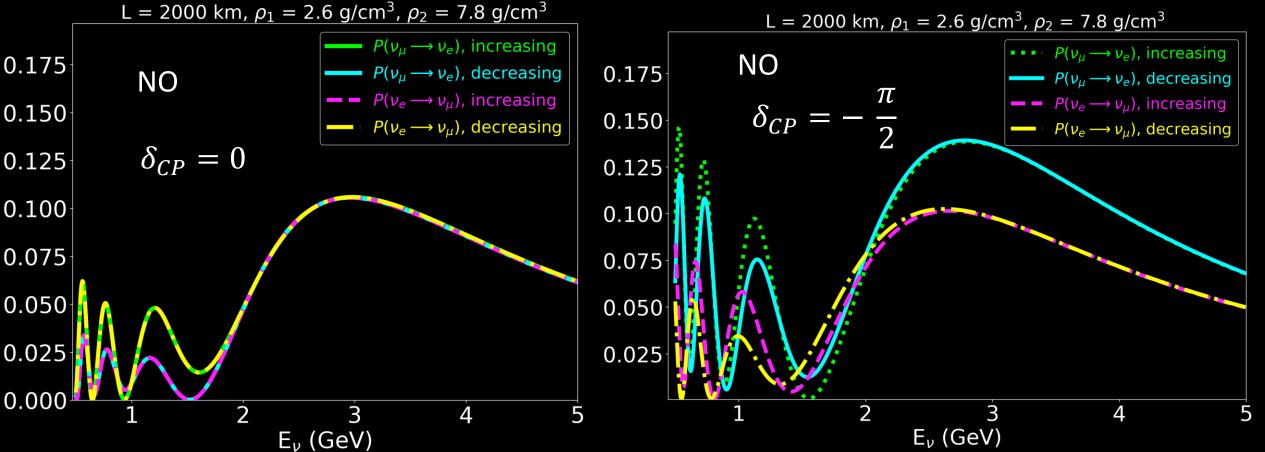
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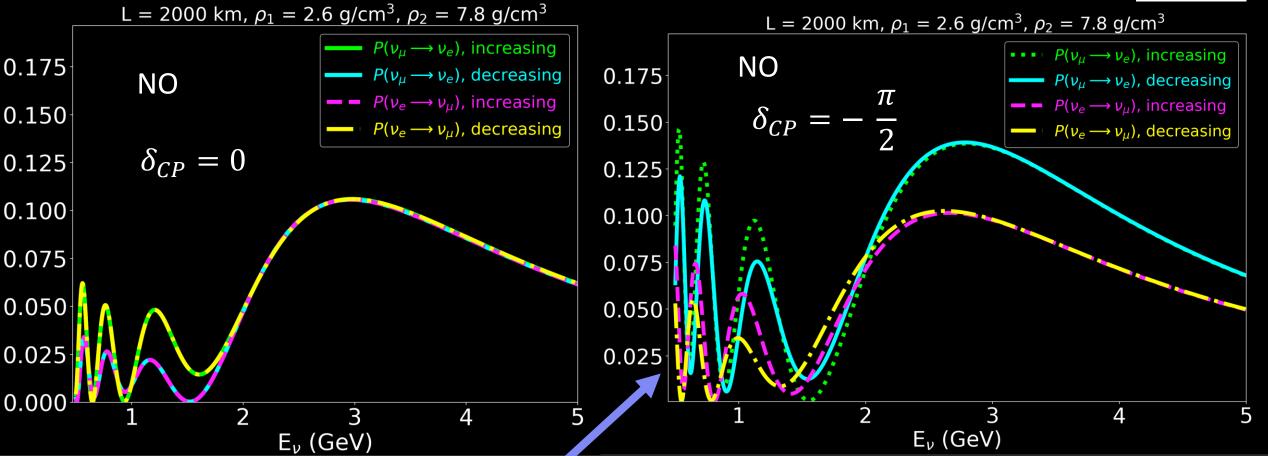
degenerate in the proper measure $(\delta_{CP} = 0)$





3. No intrinsic time invariance violation but *matter* induced time invariance violation occurs.

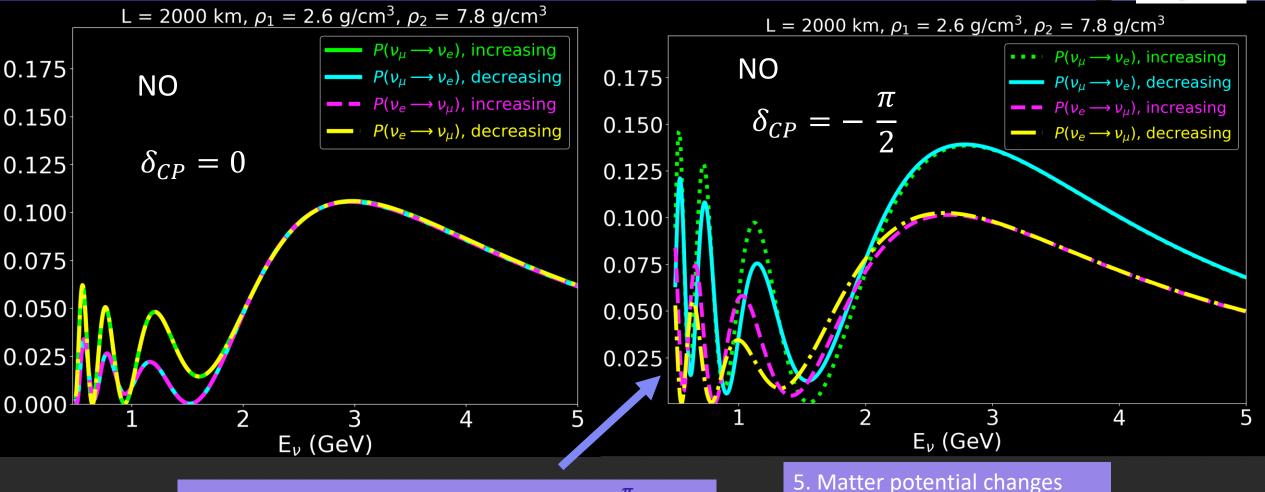




4. No longer pairwise degenerate if $(\delta_{CP} = -\frac{\pi}{2})$.

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magnitude of oscillations.

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Realistic Matter Potential Profiles

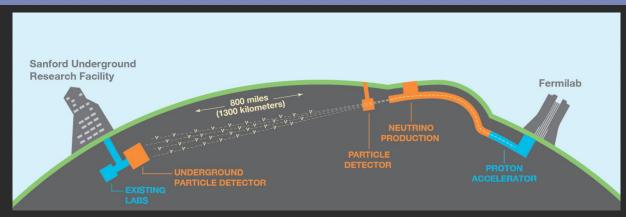
Realistic Considerations

We can play the same games for a more realistic model!



Our main model ingredients:

- ✓ Assume the high energy neutrino factory beamline as before
- ✓ Pick a well motivated baseline to test (ex: Fermilab DUNE baseline at 1300 km)
- ✓ Find the variations in Earth's crust densities







Realistic Considerations



Remember!

We are testing for possible time invariance violation

Let's call this "derived" observable:

Realistic Considerations

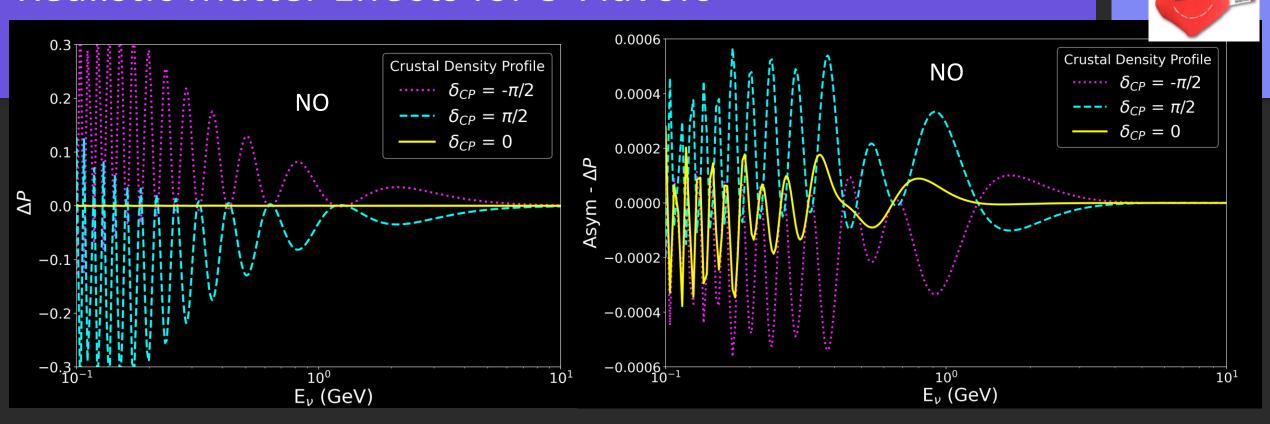


But let's also be clever in how we ask our question!

Can we meaningfully extract how much a possible time invariance violation is <u>dependent upon the asymmetry in the potential</u>? YES!

Let's call this: Asymmetrically-Induced -

or Asym - $\triangle P$

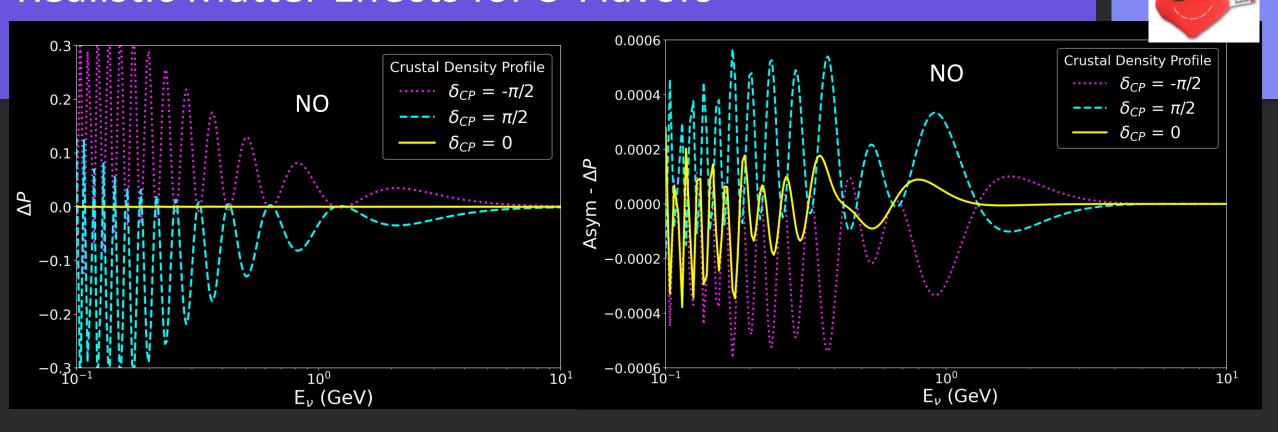


Details for Crustal Density Profile:

- 1) https://ui.adsabs.harvard.edu/abs/2013EGUGA..15.2658L/abstract
- 2) K J Kelly and S J Parke (2018) arXiv:1802.06784

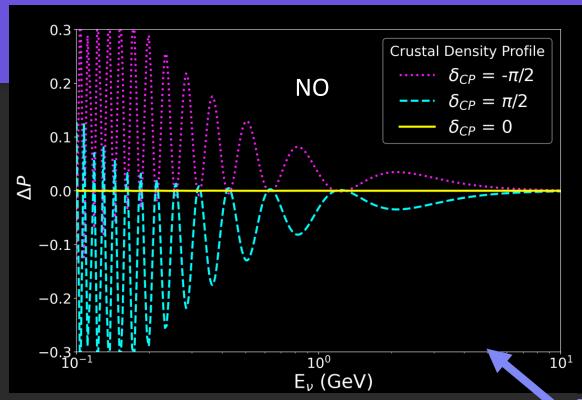
1300 km (DUNE-like baseline)
Asymmetric matter density profile

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1. No T violation if $(\delta_{CP} = 0)$ but matter induced T violation if $(\delta_{CP} \not\equiv 0)$.

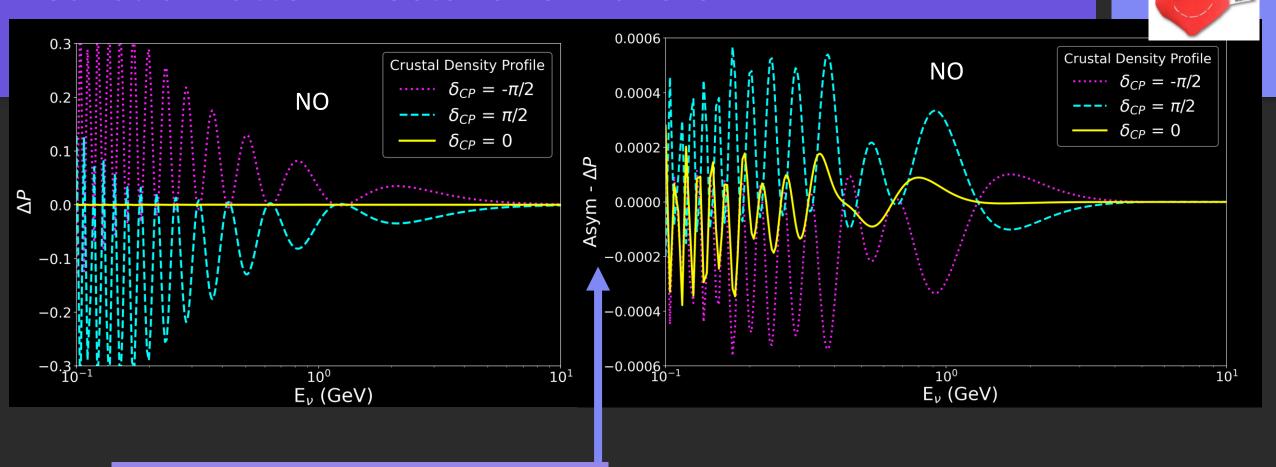
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0.0006 Crustal Density Profile NO $\delta_{CP} = -\pi/2$ 0.0004 $\delta_{CP} = \pi/2$ $\delta_{CP}=0$ 0.0002 ΔD Asym 0.0000 -0.0002-0.0004-0.000610⁰ E_{ν} (GeV)

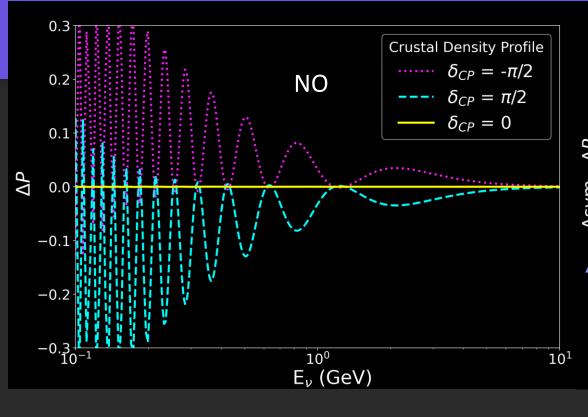
1. No T violation if $(\delta_{CP} = 0)$ but matter induced T violation if $(\delta_{CP} \not\equiv 0)$.

2. Meaning: for *DUNE-like parameters*, even in an extreme asymmetric matter, the density profile is <u>symmetric enough not</u> to induce any meaningful T-invariance violation if there is no intrinsic CP violation.

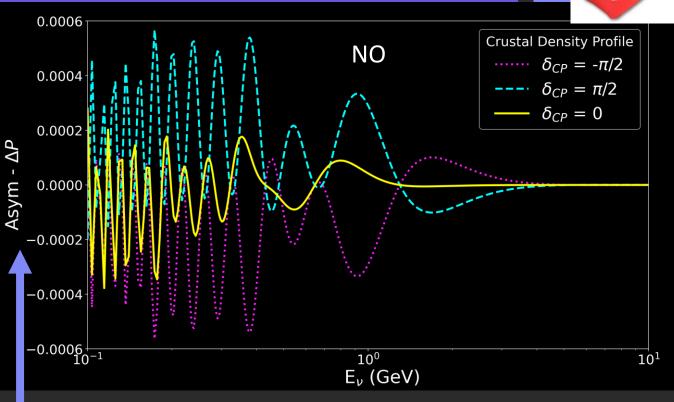


3. T-invariance violation that is induced by the matter profile's asymmetry.

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3. T-invariance violation that is induced by the matter profile's asymmetry.

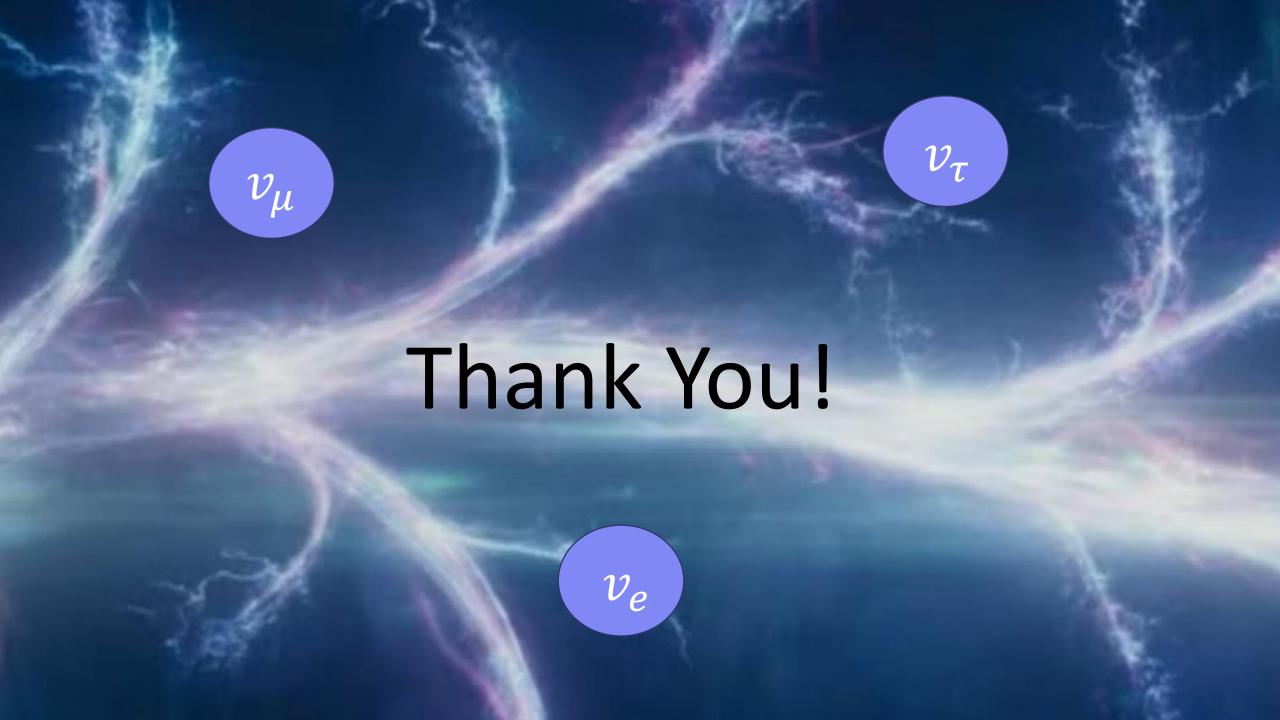


4. The amount of T-violation due to the matter profile's asymmetry, regardless of intrinsic CP violation, is insignificant and immeasurable at DUNE-like experiments.

Main Takeaways



- This study looked at how much time invariance violation (if at all) can be observed in neutrino oscillations, and their relation to simple neutrino matter potential models.
- Symmetric potentials cannot induce time violation, but if time invariance is intrinsically violated, the matter potential simply changes the degree of the observed effects.
- Symmetric potentials provide probes into proper time invariance.
- Non-symmetric matter potentials can induce improper time violation, while proper time violation is more protected.
- Realistic matter profiles induce immeasurable T violation effects for DUNE-like parameters.



Backups

Past T invariance studies include:

This list is far from complete, but just to get a sense of the progress made over the years...



Formalism developed in the late 1980s:

T.K. Kuo & J. Pantaleone (Phys. Lett. B 198 (1987))

S. Toshev (Phys. Lett. B 226 (1989))

Details relating to characteristics extracted from neutrino probabilities developed (including oscillation parameters, Jarlskog invariant etc):

M. Blom & H. Minakata (arXiv: 0404142)

P. F. Harrison & W. G. Scott (arXiv: 9912435)

S. T. Petcov & Y-L. Zhou (arXiv: 1806.09112)

Z-Z. Xing (arXiv: 1304.7606)

S. J. Parke & T. J. Weiler (arXiv: 0011247)

E.Kh. Akhmedov, P. Huber, M. Lindner, T. Ohlsson (arXiv: 0105029)

J. Bernabeu & A. Segarra (arXiv: 1901.02761)

Discussions on possible Long-Baseline tests and future neutrino factories:

J. Arafune & J. Sato (arXiv: 9607437))

T. Miura, E. Takasugi, Y. Kuno, M. Yoshimura (arXiv: 0102111)

T. Schwetz & A. Segarra

(arXiv: 2106.16099 & arXiv: 2112.08801)

S. S. Chatterjee, S. Patra, T. Schwetz, K. Sharma (arXiv: 2408.06419)

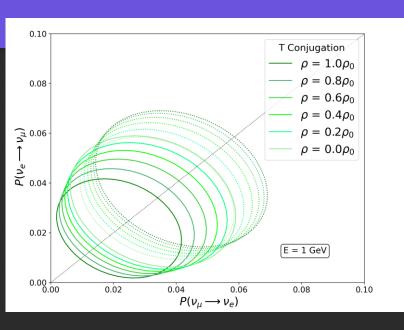
Exact formulaic derivations:

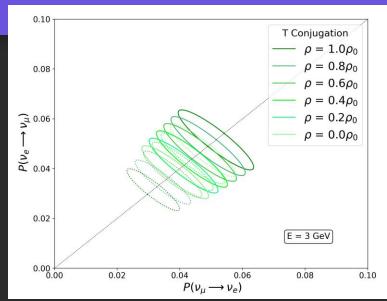
T K. Kimura, A. Takamura, H. Yokomakura (Physics Letters B 537 (2002))

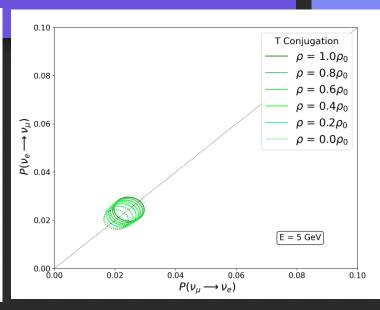
O. Yasuda (https://doi.org/10.3390/e26060472)

Bi-Probability Plots







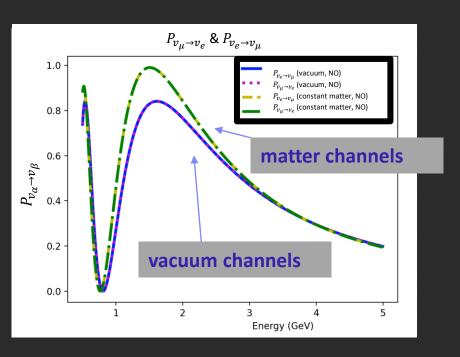


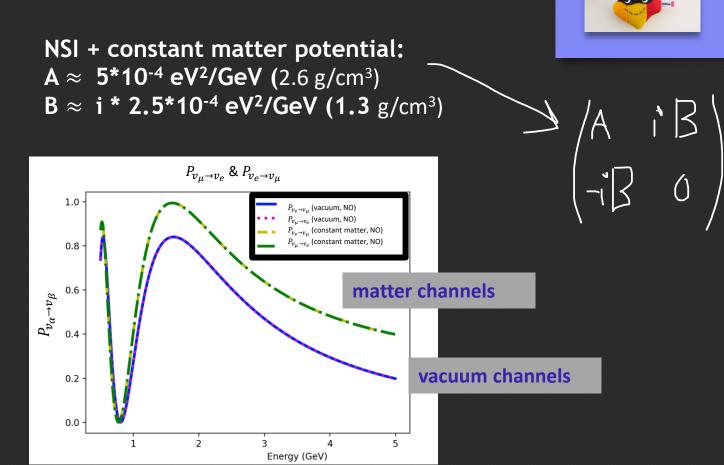
Solid lines: NO Dashed lines: IO $\rho_0 = 2.84 \text{ g/cm}^3$

Showing the impact of neutrino mass ordering and energy on T-conjugation via bi-probability plots

Symmetric matter effects for 2-Flavors (Normal Ordering, Baseline: 2000 km)

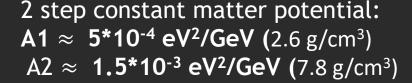
constant matter potential: $A \approx 5*10^{-4} \text{ eV}^2/\text{GeV}$ (2.6 g/cm³)

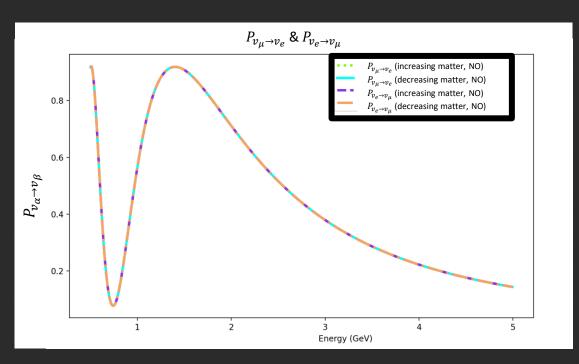




Non-symmetric matter effects for 2-Flavors (Normal Ordering, Baseline: 2000 km)

r potential:





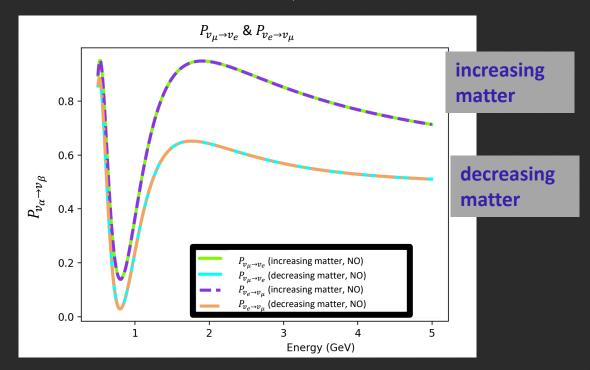


 $A1 \approx 5*10^{-4} \text{ eV}^2/\text{GeV} (2.6 \text{ g/cm}^3)$

B1 \approx i * 2.5*10⁻⁴ eV²/GeV (1.3 g/cm³)

 $A2 \approx 1.5*10^{-3} \text{ eV}^2/\text{GeV} (7.8 \text{ g/cm}^3)$

 $B2 \approx i * 7.5*10^{-4} eV^2/GeV (3.9 g/cm^3)$



Non-symmetric matter effects for 3-Flavors, 3-Steps (Normal

Ordering, Baseline: 2000 km)

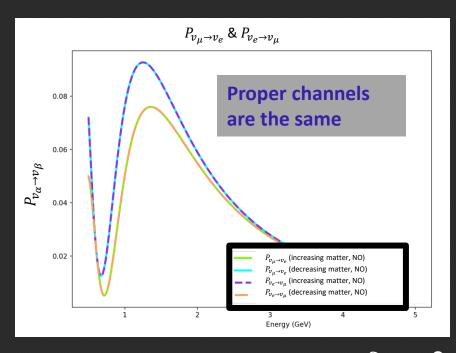


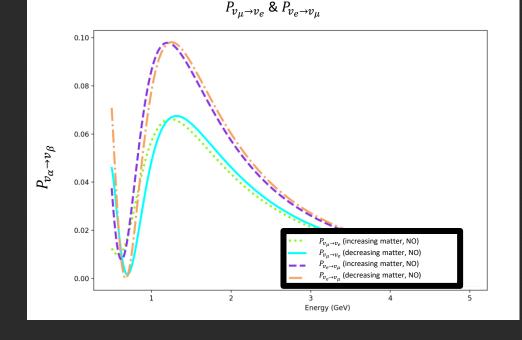
3 step constant matter potential:

 $A1 \approx 5.0*10^{-4} \text{ eV}^2/\text{GeV} (2.6 \text{ g/cm}^3)$

 $A2 \approx 1.5*10^{-3} \text{ eV}^2/\text{GeV} (7.8 \text{ g/cm}^3)$

 $A3 \approx 3.0*10^{-3} \text{ eV}^2/\text{GeV} (15.6 \text{ g/cm}^3)$





$$\delta_{CP}$$
 = 90

$$\delta_{CP} = 0$$

$$\alpha, \beta \rightarrow [\mu, e]$$



We include matter effects explicitly from the following prescription for the probabilities (useful in the context of this study):

$$P_{v_{\alpha} \to v_{\beta}} = \left| \langle \mathbf{v}_{\beta}(\mathbf{0}) | \mathbf{v}_{\alpha}(\mathbf{L}) \rangle \right|^{2}$$
 where $|\mathbf{v}_{\alpha}(\mathbf{L}) \rangle = \mathbf{U} | \mathbf{v}_{\alpha}(\mathbf{0}) \rangle$

with
$$U = e^{-iLH}$$
 (H = H_{vacuum} + H_{matter})



As an example for a Baseline L, let's break L up into 2 steps: L_1 and $L_{2,}$ where each evolution U(L) will model different matter potentials A_1 and A_2 respectively.



As an example for a Baseline L, let's break L up into 2 steps: L_1 and L_2 , where each evolution U(L) will model different matter potentials A_1 and A_2 respectively.

$$U_1 = e^{-iL_1H_1}$$
 & $U_2 = e^{-iL_2H_2}$

where H_i contain different matter effects in the form: $A_i = \sqrt{2}G_FN_e$ -> constant



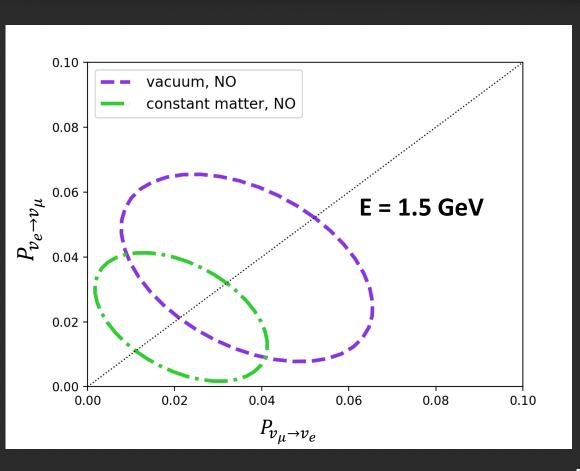
In principle, one could consider an n multistep matter potential A = matter potential (piecewise constant).

where $e_{i=1}^{n}$ step is itself a constant





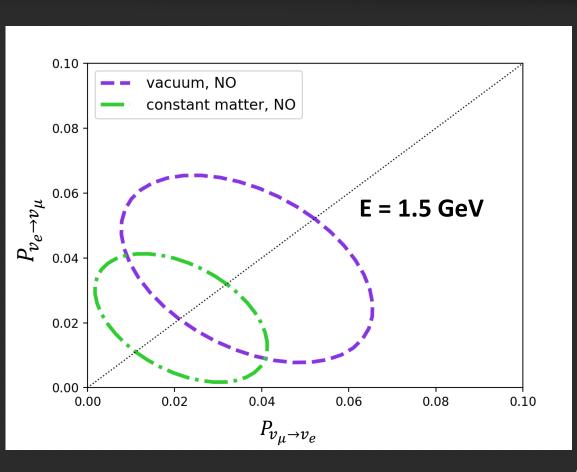




- ✓ Symmetric matter potentials *cannot induce time violation*.
- If there is intrinsic $P_{v_{\mu} \to v_{e}} \neq P_{v_{e} \to v_{\mu}}$ from δ_{CP} , then the matter potential simply changes the degree of the observed effects.







- ✓ Note: Improper and proper comparisons are the same if the matter potential is symmetric.
- ✓ Why?
 - A single constant matter potential is by construction symmetric.
 - → We cannot tell the two measures apart if "exchanging source and detector" gives the *same* results.

Future Studies



- ✓ Interesting probes in cases where matter induced time violation occurs and/or realistic models are non-symmetric:
 - Center of the Earth (annihilating dark matter to neutrinos scenario)
 - Geo neutrinos (properties/applications)
- ✓ Next steps include *NSI time invariance* probes applicable to DUNE, (a follow-up to previous work).

