



Machine-learning VH-bb EFT effects in CMS

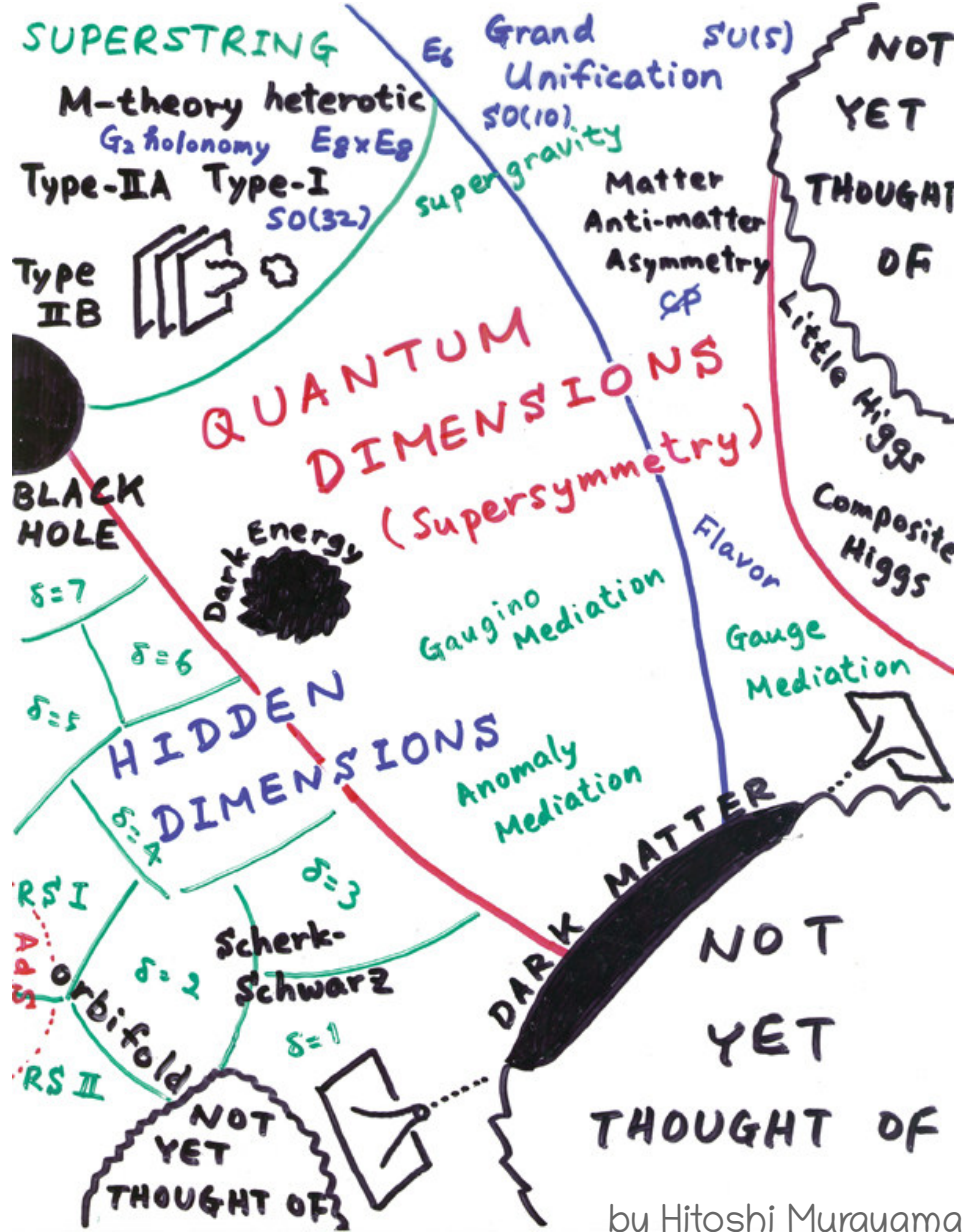
Suman Chatterjee

Deutsches Elektronen-Synchrotron (DESY), Hamburg

20/02/2025

COMETA workshop on
Polarized Perspectives: Tagging and Learning in the SM
Austrian Academy of Sciences, Vienna

Landscape of new physics



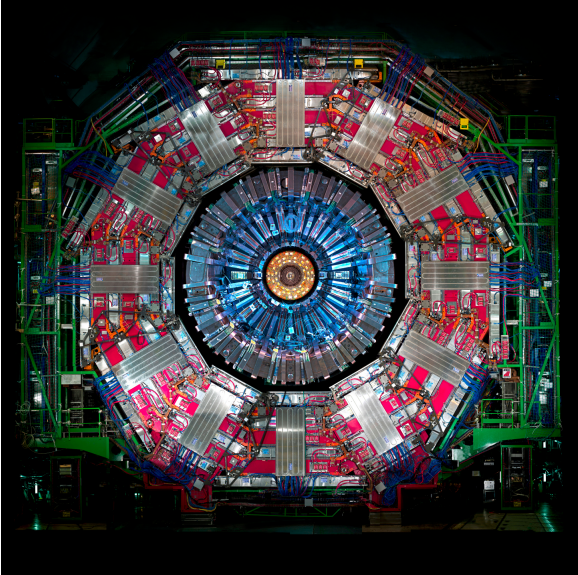
[image link]

Plethora of new ideas → solving one or many problems

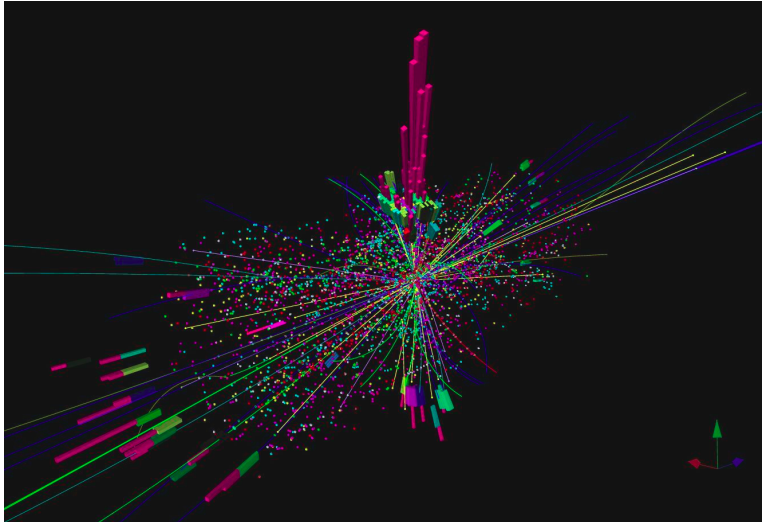
Formulated in terms of Lagrangians

← Parameters: couplings & energy scales

→ Predictions for new phenomena at experiments



Hidden Valley Z' → jets (simulation)



[image link]

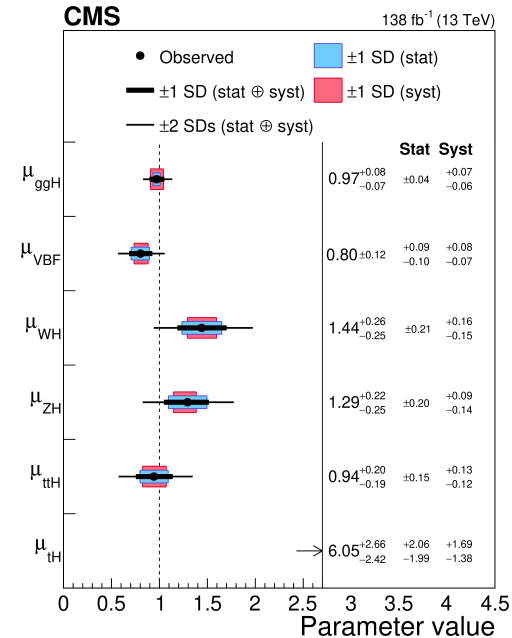
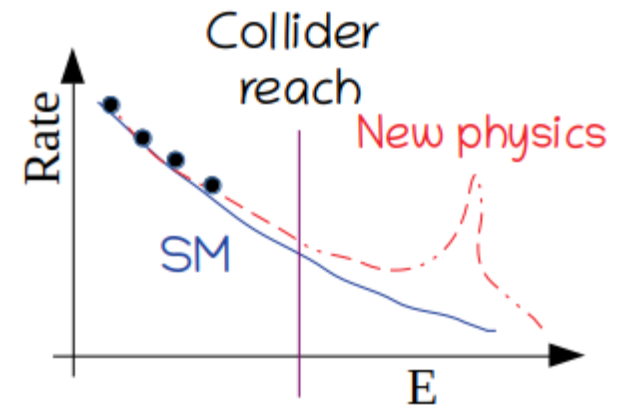
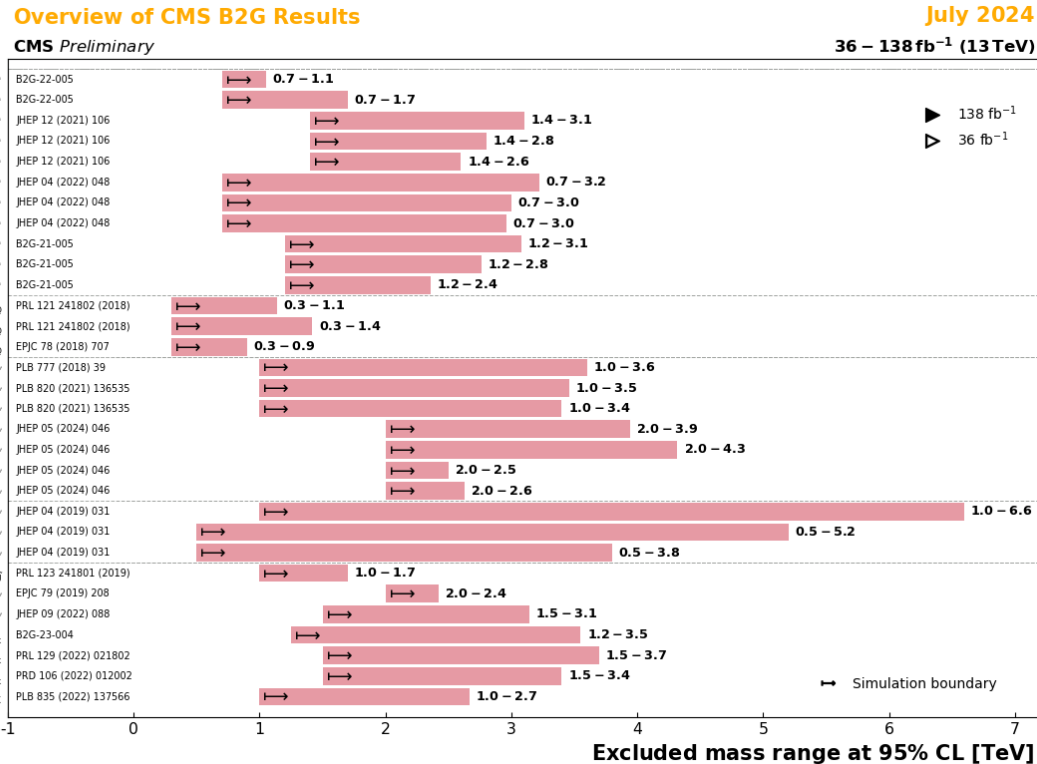
Scale of new physics?



Newest fundamental particle discovered: Last missing piece in standard model (SM)

CMS B2G-Resonances summary plots

Nature 607 (2022) 60-68



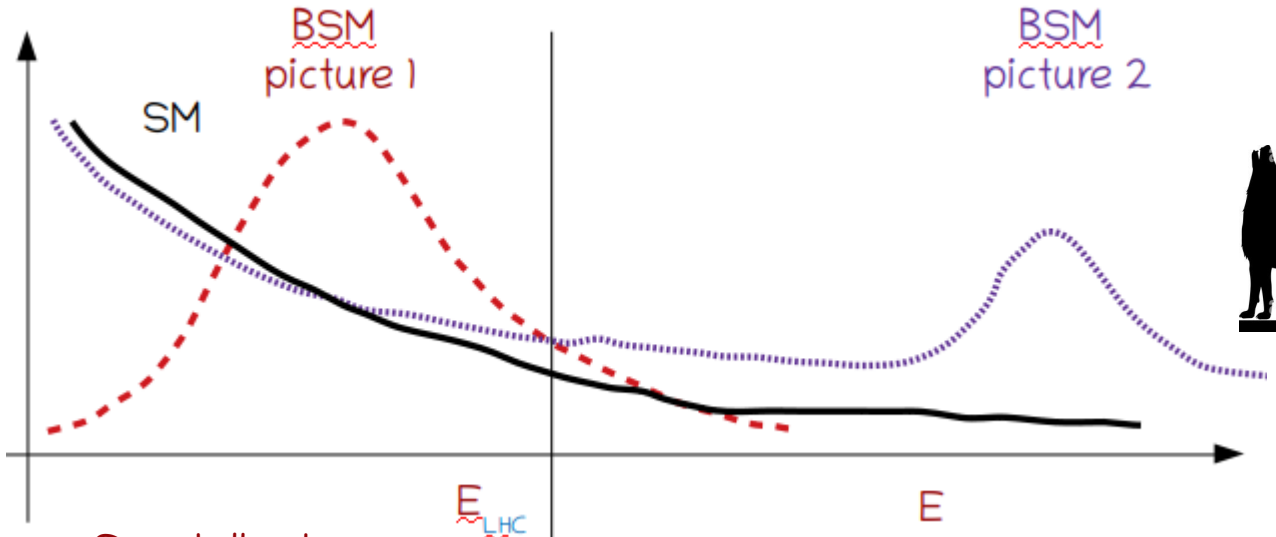
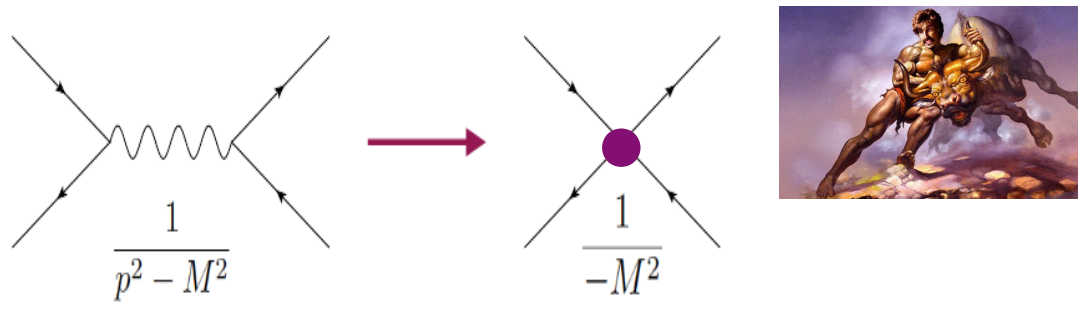
No smoking gun signature of a heavy resonance yet from LHC data

→ Hint for a separation of new physics scale & electroweak scale?

Large new physics scale consistent with inclusive measurements

Standard model effective field theory (SMEFT)

New (heavy) particles modify SM interactions



See talks by
A. Malara
A. Agapitos

Discovery through
precision measurements



Deviations from SM ← parameterized by effective field theory operators

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \cancel{\sum_i \frac{c_i^{(5)}}{\Lambda} \mathcal{O}_{5,i}} + \boxed{\sum_i \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_{6,i}} + \cancel{\sum_i \frac{c_i^{(7)}}{\Lambda^2} \mathcal{O}_{7,i}} + \sum_i \frac{c_i^{(8)}}{\Lambda^4} \mathcal{O}_{8,i} + \dots$$

Lepton number violation

Lepton & Baryon number violation

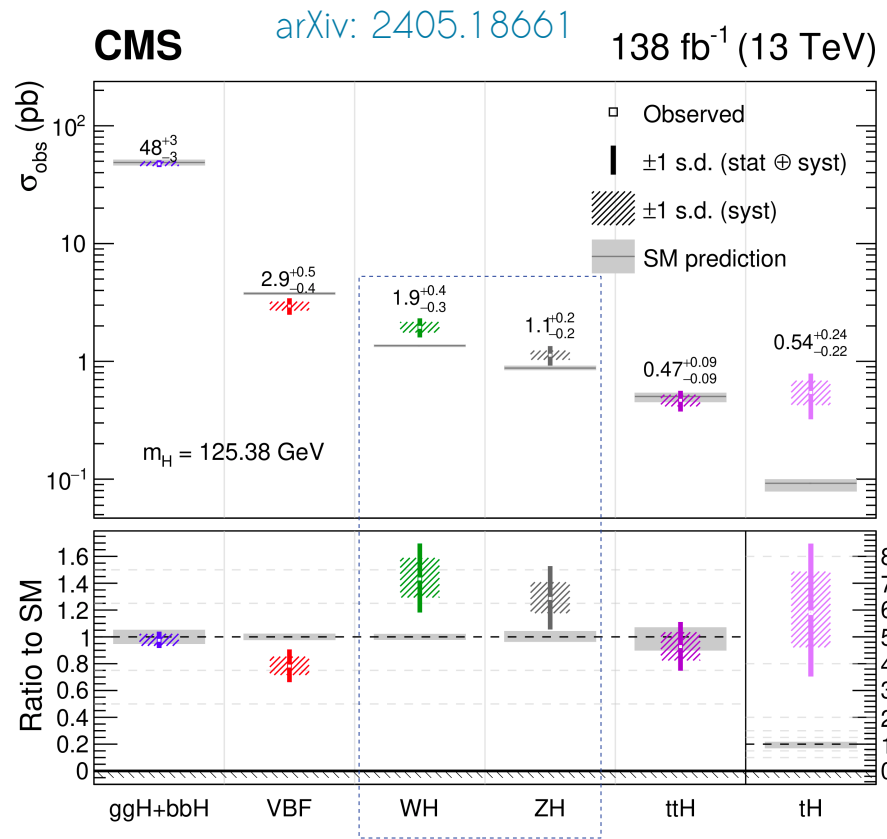
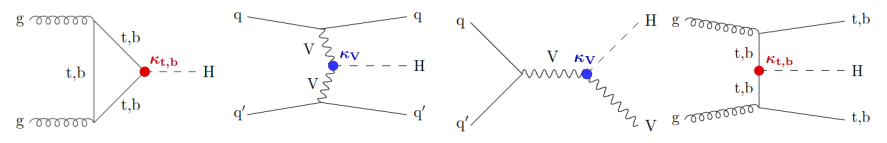
Assumptions:

- Particle content same as in SM
- SM Gauge symmetries $SU(3)_c \times SU(2)_L \times U(1)_y$ respected

59 SMEFT operators @ dim=6 Grzadkowski, Iskrzyński, Misiak, Rosiek (2010)

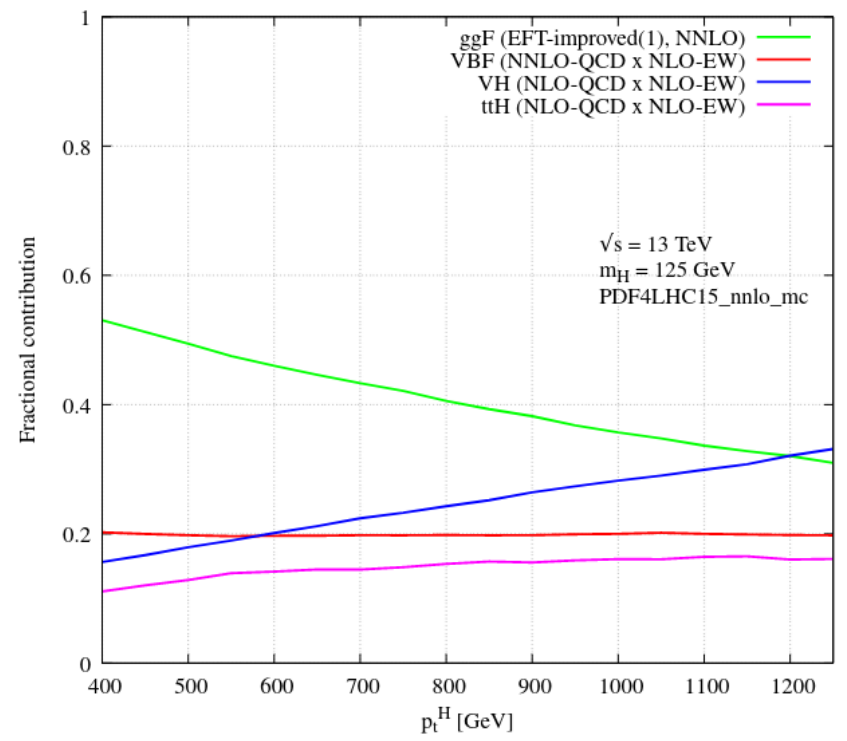
Higgstrahlung: small but important

H production

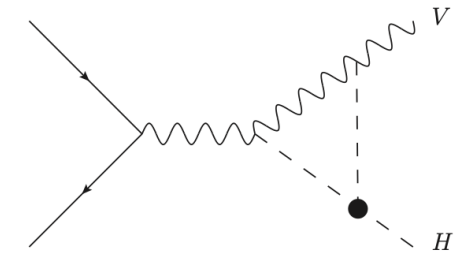


Higgs-strahlung important at high energy

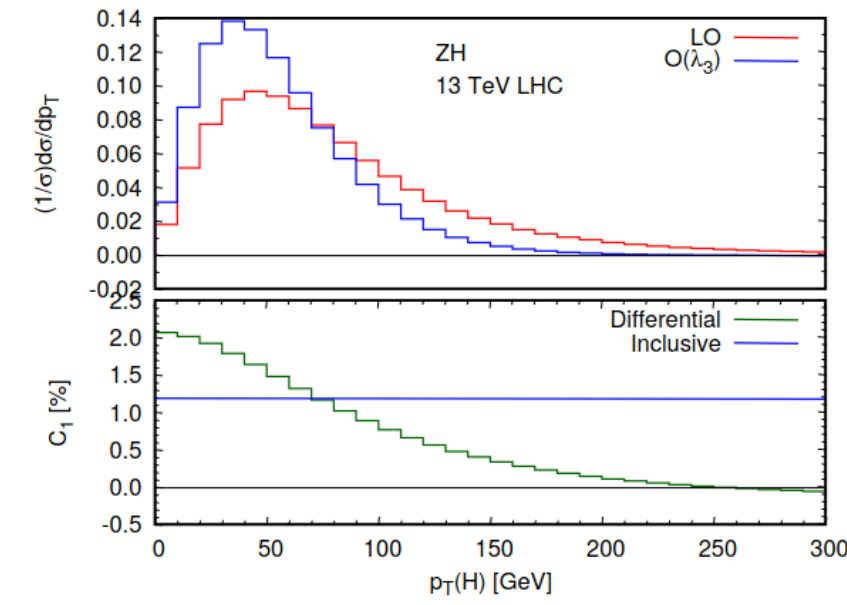
LHCHSWG-2019-002



Sensitive to Higgs self-coupling



Maltoni, Pagani, Shivaji, Zhao (2017)

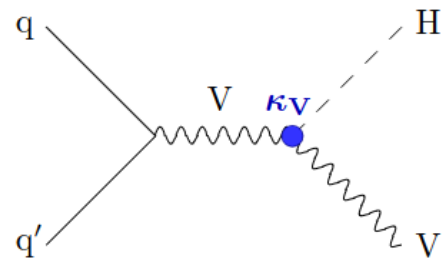


WH/ZH → small production cross section

Cross section measurement of V associated H production @CMS



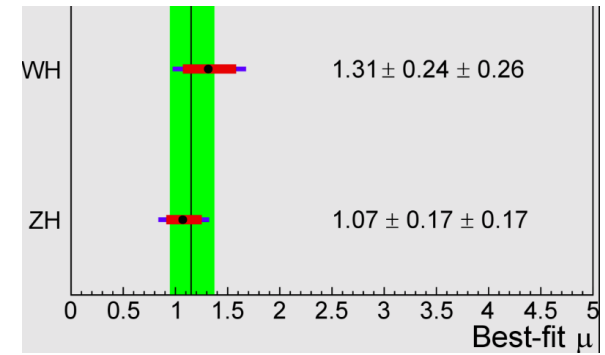
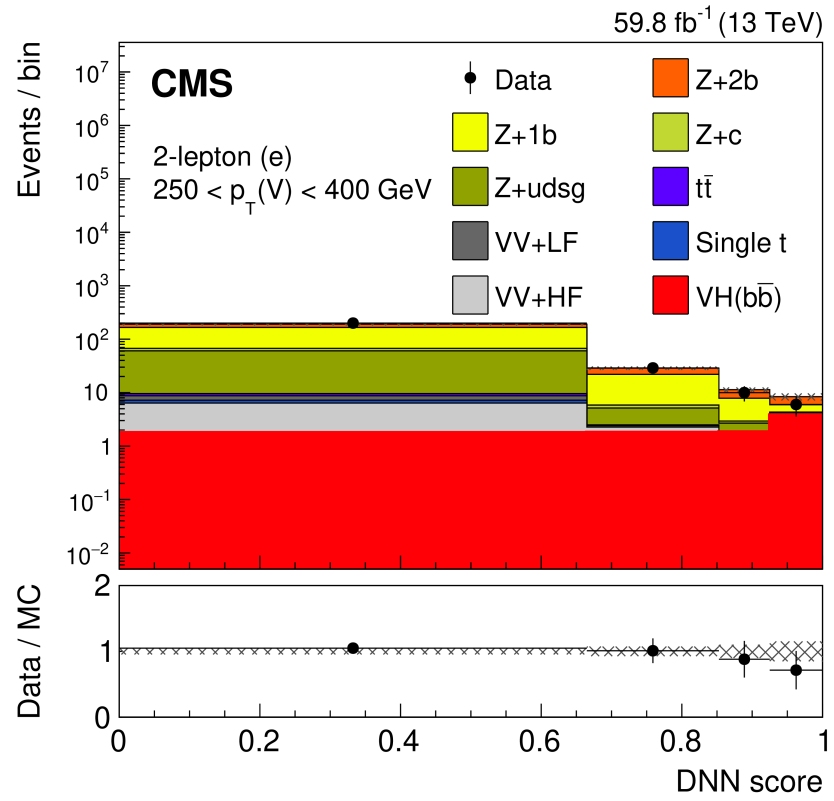
Phys.Rev.D 109 (2024) 9, 092011



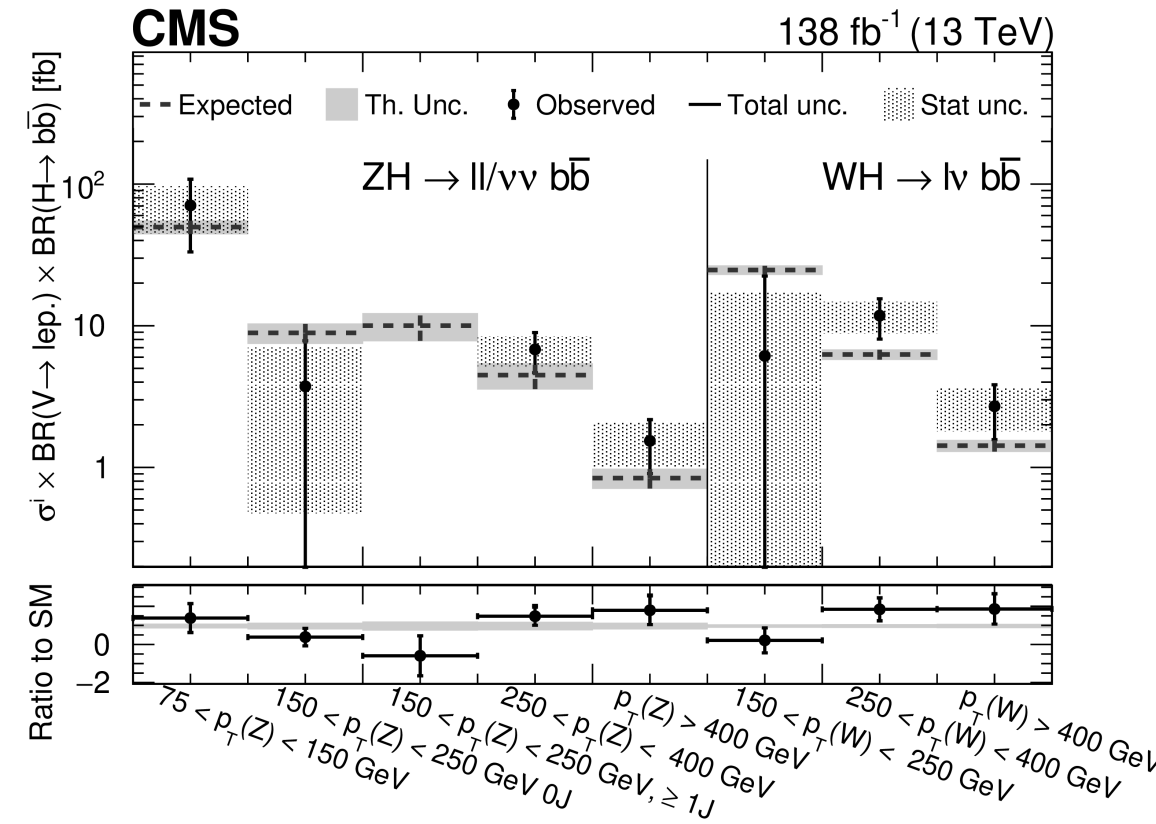
Small production cross section

- $H \rightarrow bb$ decay \leftarrow largest branching ratio
- $V \rightarrow$ leptons \leftarrow clean signature

Cross section reported in simplified template cross section framework

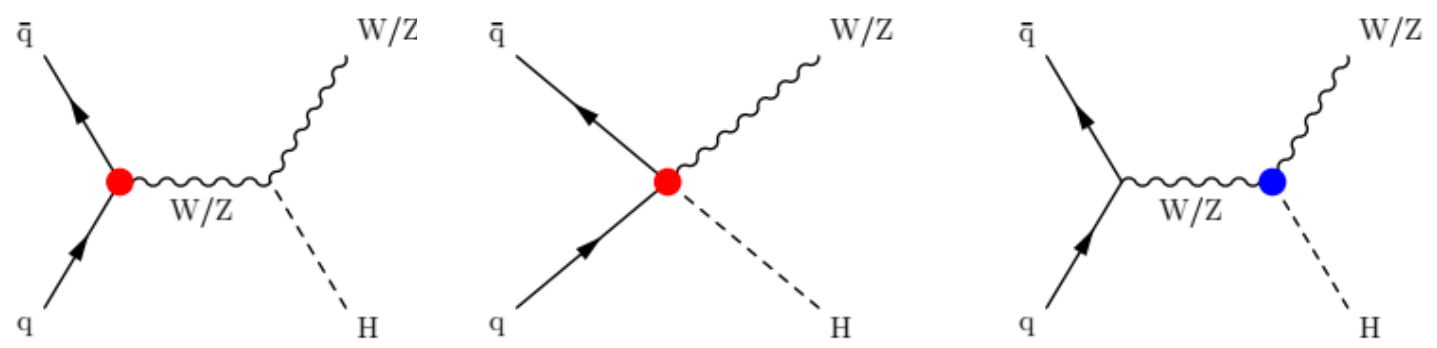


Combined $\mu = 1.15^{+0.22}_{-0.20}$



VH signal extracted using DNN score in signal-enriched regions

EFT effects in V associated H production



Current operators

$$\begin{aligned}
 \mathcal{O}_{\text{Hq}}^{(1)} & iH^\dagger \overleftrightarrow{D}_\mu H \bar{q}_L \gamma^\mu q_L & c_{\text{Hq}}^{(1)} \\
 \mathcal{O}_{\text{Hq}}^{(3)} & iH^\dagger \sigma^a \overleftrightarrow{D}_\mu H \bar{q}_L \sigma^a \gamma^\mu q_L & c_{\text{Hq}}^{(3)} \\
 \mathcal{O}_{\text{Hu}} & iH^\dagger \overleftrightarrow{D}_\mu H \bar{u}_R \gamma^\mu u_R & c_{\text{Hu}} \\
 \mathcal{O}_{\text{Hd}} & iH^\dagger \overleftrightarrow{D}_\mu H \bar{d}_R \gamma^\mu d_R & c_{\text{Hd}}
 \end{aligned}$$

Gauge coupling operators

$$\begin{aligned}
 \mathcal{O}_{\text{HWB}} & H^\dagger \sigma^a H W_{\mu\nu}^a B^{\mu\nu} & c_{\text{HWB}} \\
 \mathcal{O}_{\text{HW}} & (H^\dagger H) W_{\mu\nu}^a W^{a\mu\nu} & c_{\text{HW}} \\
 \mathcal{O}_{\text{HB}} & (H^\dagger H) B_{\mu\nu} B^{\mu\nu} & c_{\text{HB}} \\
 \mathcal{O}_{\text{H}\widetilde{\text{WB}}} & H^\dagger \sigma^a H W_{\mu\nu}^a \widetilde{B}^{\mu\nu} & c_{\text{H}\widetilde{\text{WB}}} \\
 \mathcal{O}_{\text{H}\widetilde{\text{W}}} & (H^\dagger H) W_{\mu\nu}^a \widetilde{W}^{a\mu\nu} & c_{\text{H}\widetilde{\text{W}}} \\
 \mathcal{O}_{\text{H}\widetilde{\text{B}}} & (H^\dagger H) B_{\mu\nu} \widetilde{B}^{\mu\nu} & c_{\text{H}\widetilde{\text{B}}}
 \end{aligned}$$

Rotation to mass eigenstate basis

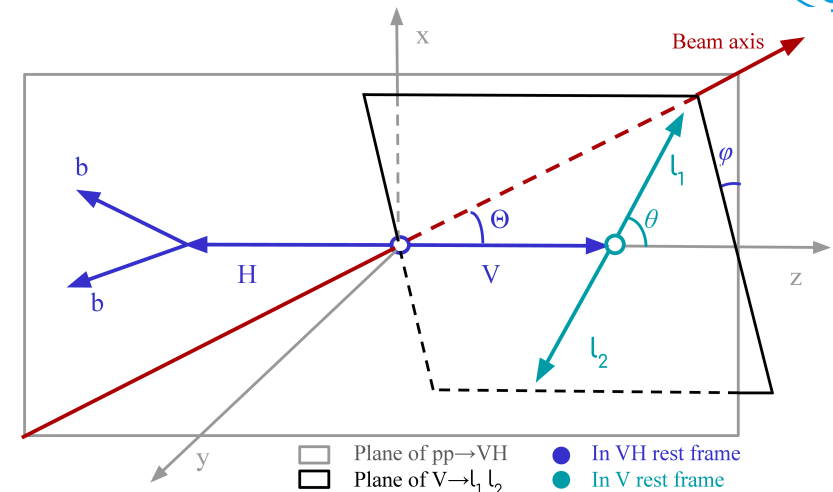
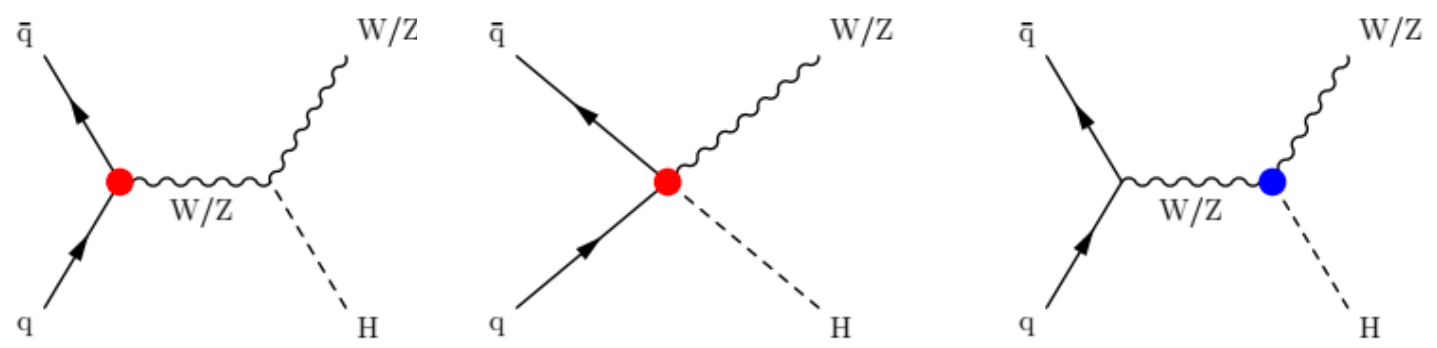
$$\begin{aligned}
 g_2^{ZZ} &= -2 \frac{v^2}{\Lambda^2} (s_w^2 c_{\text{HB}} + c_w^2 c_{\text{HW}} + s_w c_w c_{\text{HWB}}), \\
 g_2^{Z\gamma} &= -2 \frac{v^2}{\Lambda^2} (s_w c_w (c_{\text{HW}} - c_{\text{HB}}) + \frac{1}{2} (s_w^2 - c_w^2) c_{\text{HWB}}), \\
 g_2^{\gamma\gamma} &= -2 \frac{v^2}{\Lambda^2} (c_w^2 c_{\text{HB}} + s_w^2 c_{\text{HW}} - s_w c_w c_{\text{HWB}}), \quad c_w = \cos \theta_W
 \end{aligned}$$

$$\begin{aligned}
 g_4^{ZZ} = \widetilde{g}_2^{ZZ} &= -2 \frac{v^2}{\Lambda^2} (s_w^2 c_{\text{H}\widetilde{\text{B}}} + c_w^2 c_{\text{H}\widetilde{\text{W}}} + s_w c_w c_{\text{H}\widetilde{\text{WB}}}), \\
 g_4^{Z\gamma} = \widetilde{g}_2^{Z\gamma} &= -2 \frac{v^2}{\Lambda^2} (s_w c_w (c_{\text{H}\widetilde{\text{W}}} - c_{\text{H}\widetilde{\text{B}}}) + \frac{1}{2} (s_w^2 - c_w^2) c_{\text{H}\widetilde{\text{WB}}}), \\
 g_4^{\gamma\gamma} = \widetilde{g}_2^{\gamma\gamma} &= -2 \frac{v^2}{\Lambda^2} (c_w^2 c_{\text{H}\widetilde{\text{B}}} + s_w^2 c_{\text{H}\widetilde{\text{W}}} - s_w c_w c_{\text{H}\widetilde{\text{WB}}}).
 \end{aligned}$$

Coefficients targeted in measurement:

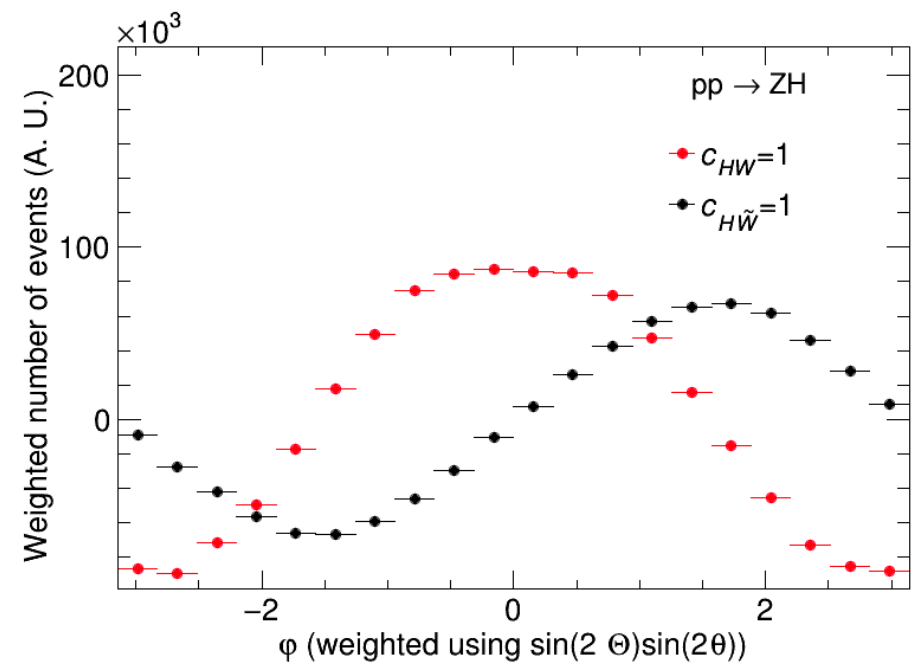
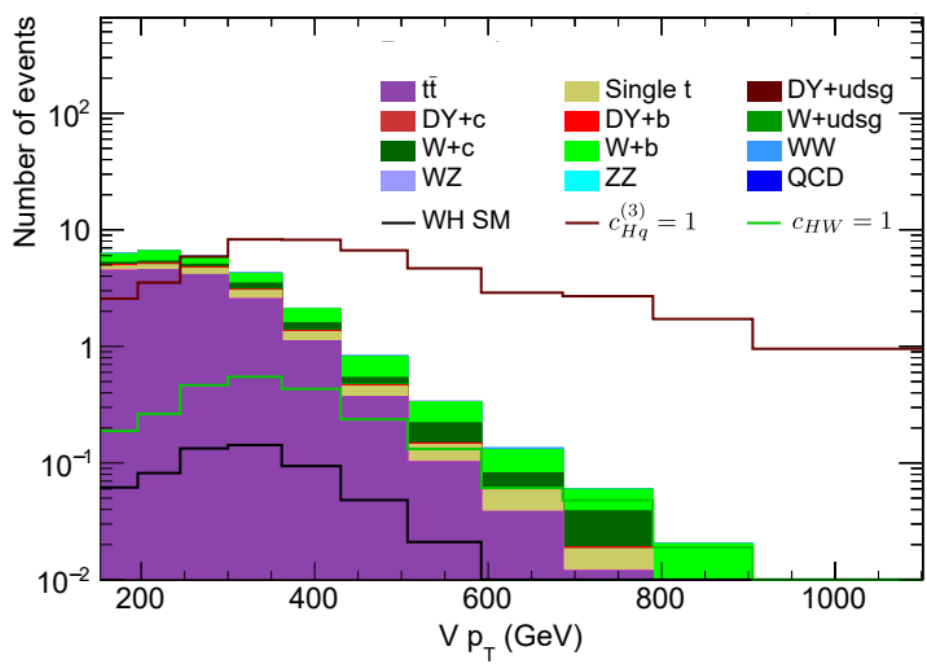
$$c_{\text{Hq}}^{(1)}, c_{\text{Hq}}^{(3)}, c_{\text{Hu}}, c_{\text{Hd}}, g_2^{ZZ}, g_4^{ZZ}$$

EFT effects in V associated H production



Use of angular variables followed from

Banerjee, Gupta, Reiness, Seth, Spanowsky (2019)



EFT effects:
 Changing energy spectra
 +
 Modifying angular correlation

Signal simulation strategy

Polynomial parameterization

$$\mathcal{M}_{\text{SMEFT}} = \mathcal{M}_{\text{SM}} + \sum_i \frac{c_i}{\Lambda^2} \mathcal{M}_{6,i}$$

$$\begin{aligned} \sigma &\sim |\mathcal{M}_{\text{SMEFT}}|^2 \\ &\sim |\mathcal{M}_{\text{SM}}|^2 + \sum_i \frac{c_i}{\Lambda^2} 2\text{Re}(\mathcal{M}_{\text{SM}}^\dagger \mathcal{M}_{6,i}) + \sum_i \frac{c_i^2}{\Lambda^4} |\mathcal{M}_{6,i}|^2 + \sum_i \sum_{j,j>i} \frac{c_i c_j}{\Lambda^4} \mathcal{M}_{6,i} \mathcal{M}_{6,j} \end{aligned}$$

σ is a quadratic function of coefficients!

of signal samples (for 'n' coefficients): $N(n) = 1 + n + n(n+1)/2$ ← Sufficient

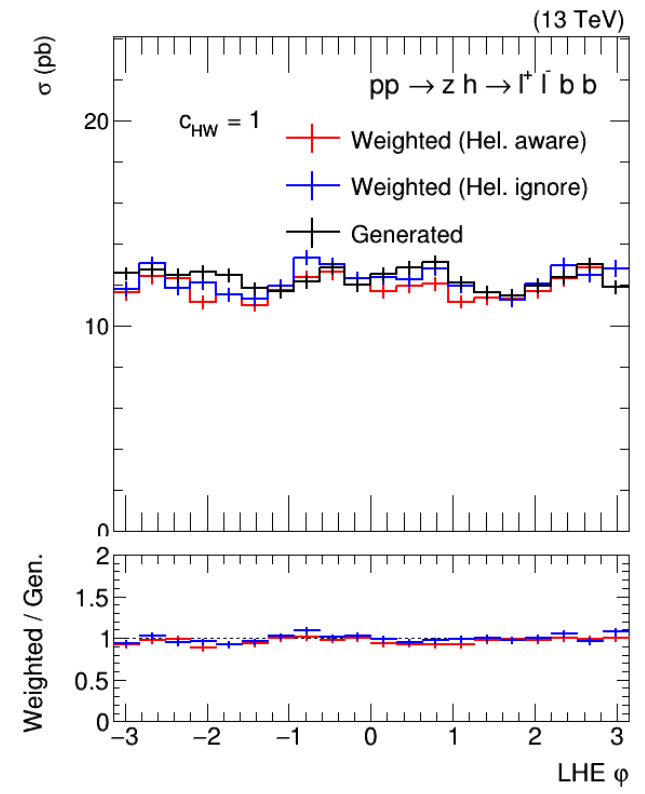
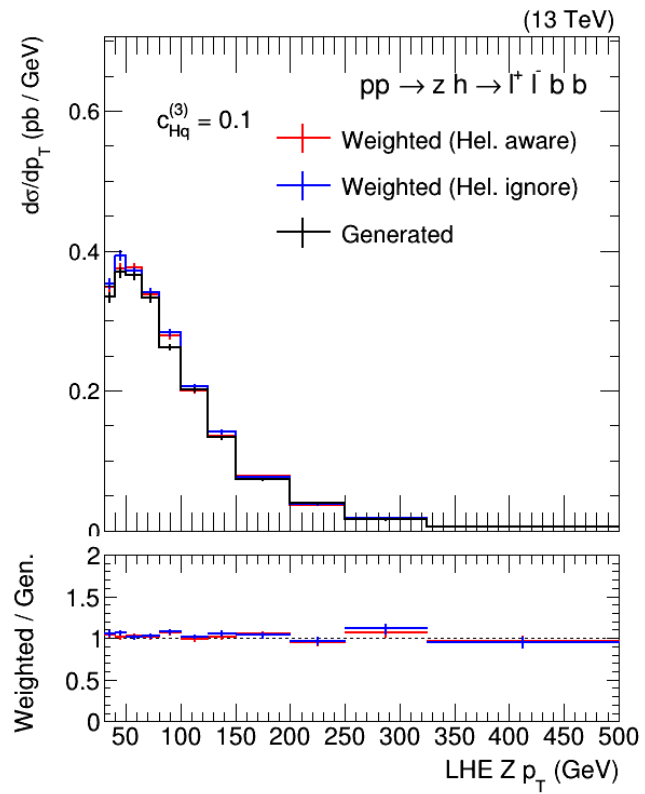
Possible to encode SMEFT prediction in event weights

$$\omega = \frac{|\mathcal{M}_{\text{SMEFT}}(c = c_1)|^2}{|\mathcal{M}_{\text{SMEFT}}(c = c_0)|^2}$$

$$\omega(\mathbf{z}|\mathbf{c}) \sim \frac{d\sigma}{dz} = \text{Const}(\mathbf{z}) + \text{LIN}_a(\mathbf{z})c_a + \frac{1}{2}\text{QUAD}_{ab}(\mathbf{z})c_a c_b$$

Store $N(n)$ weights per event
 → obtain EFT prediction for any coefficient value

SciPost Phys.Comm.Rep. (2024) 4



Observable: likelihood-free inference

Likelihood ratio trick in classification

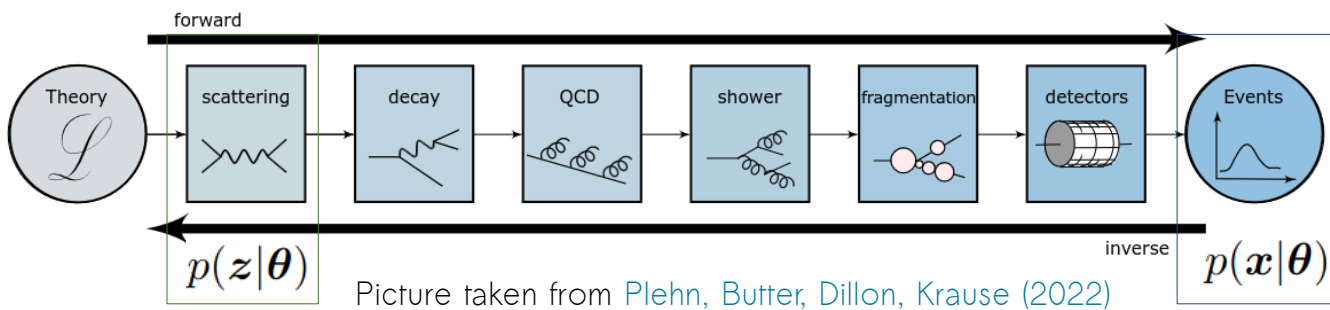
$$L = \int d\mathbf{x} \sum_{z \in \{0,1\}} p(\mathbf{x}, z) (z - f(\mathbf{x}))^2 \xrightarrow{\text{Minimizing } L} f^*(\mathbf{x}) = \frac{p(\mathbf{x}|\text{SM})}{p(\mathbf{x}|\text{SM}) + p(\mathbf{x}|\theta)} = \frac{1}{1 + \frac{\sigma(\theta)}{\sigma(\text{SM})} r(\mathbf{x})}$$

0 → SM, 1 → θ

Optimal test statistic:
Likelihood ratio (LLR)

$$r(\mathbf{x}) = \frac{p(\mathbf{x}|\theta)}{p(\mathbf{x}|\text{SM})} \rightarrow R(\mathbf{x}|\theta_1, \theta_0)$$

x ← observable



$$p(\mathbf{x}|\theta) = \int \int \int p(\mathbf{x}|z_{\text{Det}}) p(z_{\text{Det}}|z_{\text{Had}}) p(z_{\text{Had}}|z_{\text{PS}}) p(z_{\text{PS}}|z) dz_{\text{Det}} dz_{\text{Had}} dz_{\text{PS}} p(z|\theta) dz$$

$$p(\mathbf{x}|\theta) = \int p(\mathbf{x}|z) p(z|\theta) dz$$

intractable

tractable

Inverse problem: Estimate θ from p(x)

LLR between two EFT hypotheses → learned by regressing on joint LLR

Brehmer, Cranmer, Louppe, Pavez (2018)

$$R(\mathbf{x}, z|\theta_1, \theta_0) = \frac{p(\mathbf{x}, z|\theta_1)}{p(\mathbf{x}, z|\theta_0)} = \frac{p(\mathbf{x}|z)p(z|\theta_1)}{p(\mathbf{x}|z)p(z|\theta_0)} = \frac{p(z|\theta_1)}{p(z|\theta_0)}$$

$$L[\hat{F}] = \int d\mathbf{x} dz p(\mathbf{x}, z|\theta_0) |F(\mathbf{x}, z) - \hat{F}(\mathbf{x})|^2$$

$$F(\mathbf{x}, z) = \frac{\sigma(\theta_1)}{\sigma(\theta_0)} R(\mathbf{x}, z) = \frac{\sigma(\theta_1)}{\sigma(\theta_0)} \frac{p(\mathbf{x}, z|\theta_1)}{p(\mathbf{x}, z|\theta_0)}$$

$$\hat{R}(\mathbf{x}) = \frac{\int dz p(\mathbf{x}, z|\theta_0) \frac{\sigma(\theta_1)}{\sigma(\theta_0)} \frac{p(\mathbf{x}, z|\theta_1)}{p(\mathbf{x}, z|\theta_0)}}{\int dz p(\mathbf{x}, z|\theta_0)} = \frac{\sigma(\theta_1)}{\sigma(\theta_0)} \frac{p(\mathbf{x}|\theta_1)}{p(\mathbf{x}|\theta_0)} = R(\mathbf{x}|\theta_1, \theta_0)$$

Likelihood-free / simulation-based inference

Boosted information tree (BIT)

Using decision trees to regress on learn likelihood ratio terms

→ **very fast!**

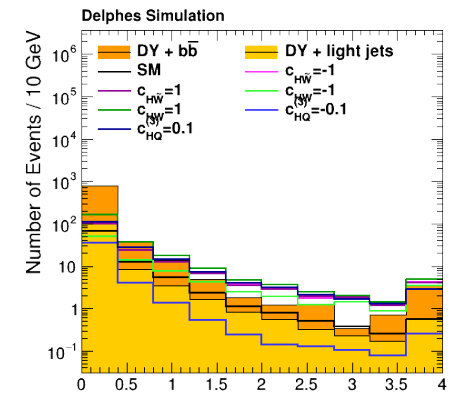
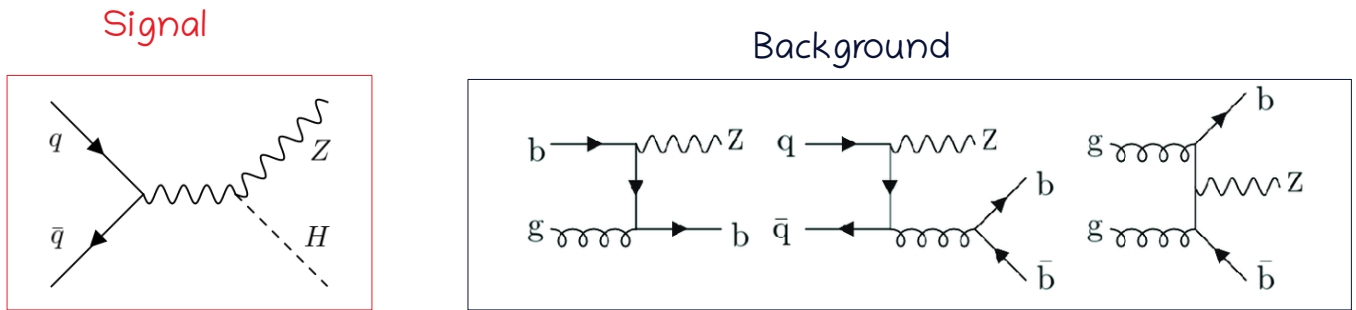
SC, N. Frohner, L. Lechner, R. Schoefbeck, D. Schwarz (2021)

of trainings = N + N + N(N-1)/2

$$R(\mathbf{x}|\theta_1, \theta_0) = 1 + (\theta_1 - \theta_0)_a R_a(\mathbf{x}) + \frac{1}{2} (\theta_1 - \theta_0)_a (\theta_1 - \theta_0)_b R_{a,b}(\mathbf{x})$$

Learning SMEFT likelihood ratio

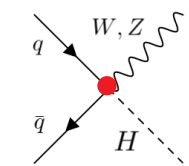
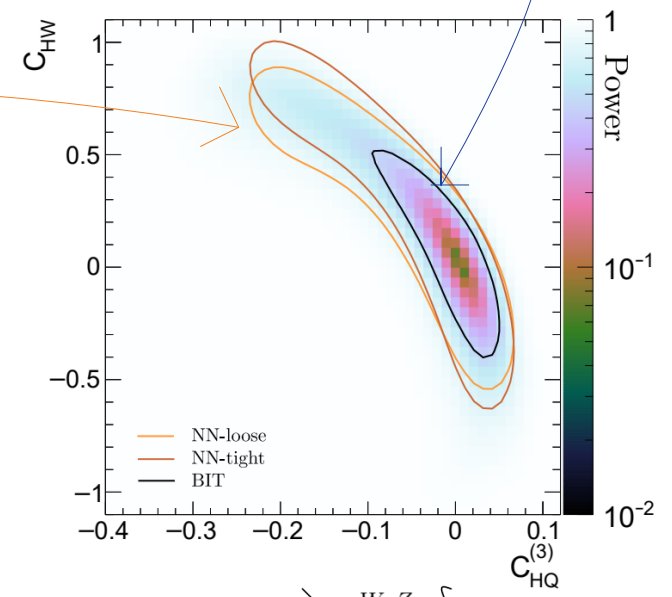
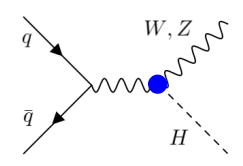
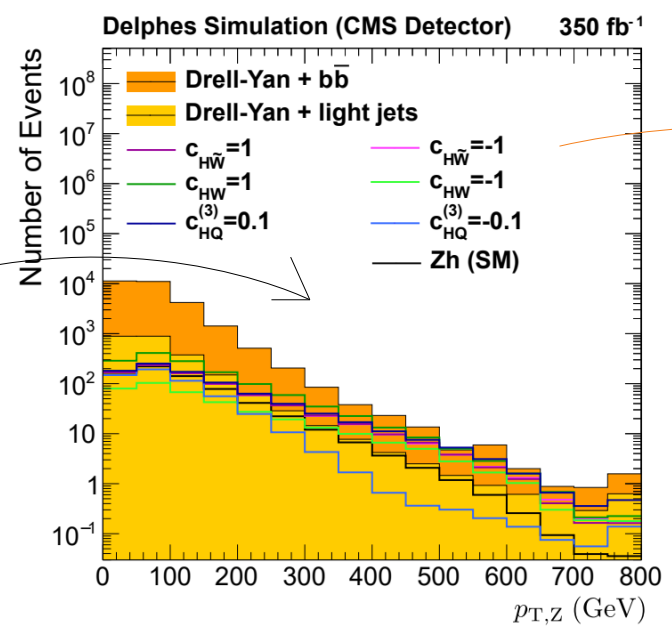
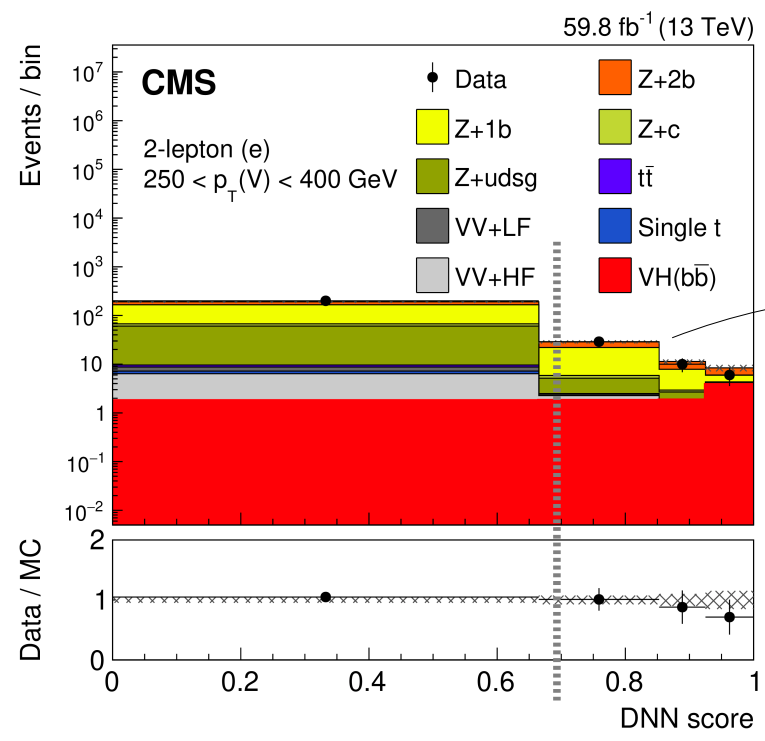
SC, S. Roshap, R. Schoefbeck, D. Schwarz (2022)



Traditional approach

BIT approach

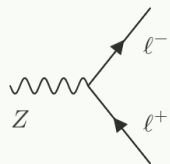
$$R(x|\theta_1, \theta_0) = 1 + (\theta_1 - \theta_0)_a R_a(x) + \frac{1}{2}(\theta_1 - \theta_0)_a(\theta_1 - \theta_0)_b R_{a,b}(x)$$



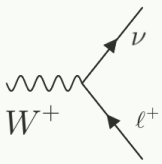
Event selection & categorization

Final state

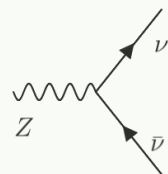
2-lepton



1-lepton

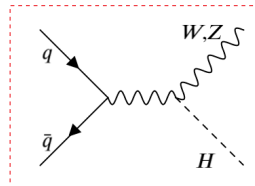


0-lepton

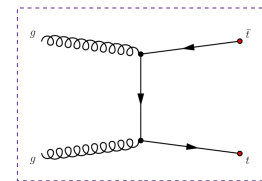


Regions

Signal region (SR)

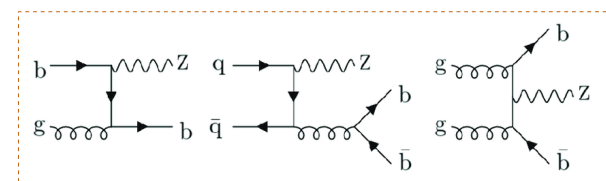


$t\bar{t}$



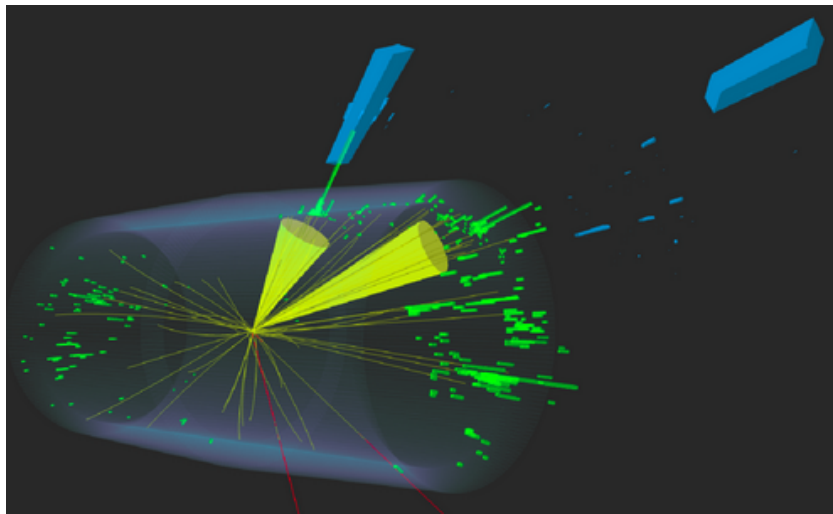
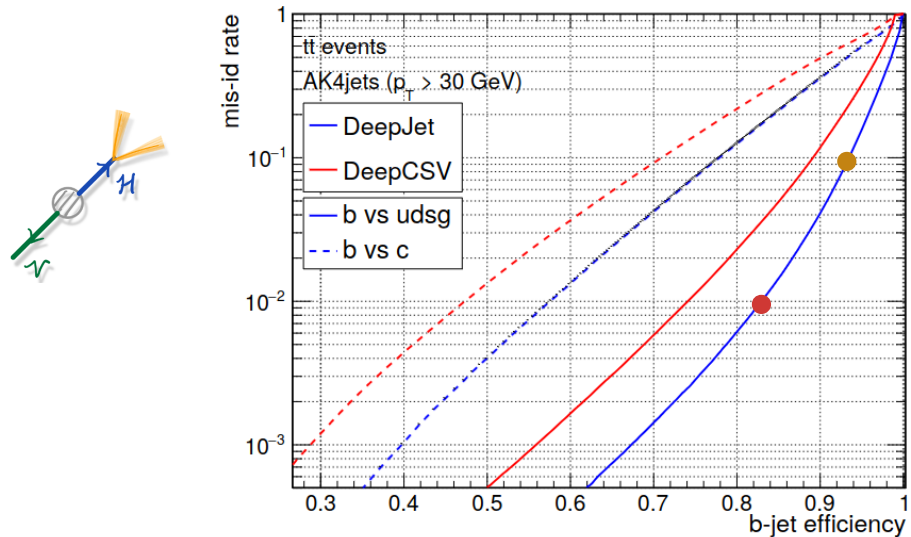
Control regions (CRs)

V+ heavy-flavor jets

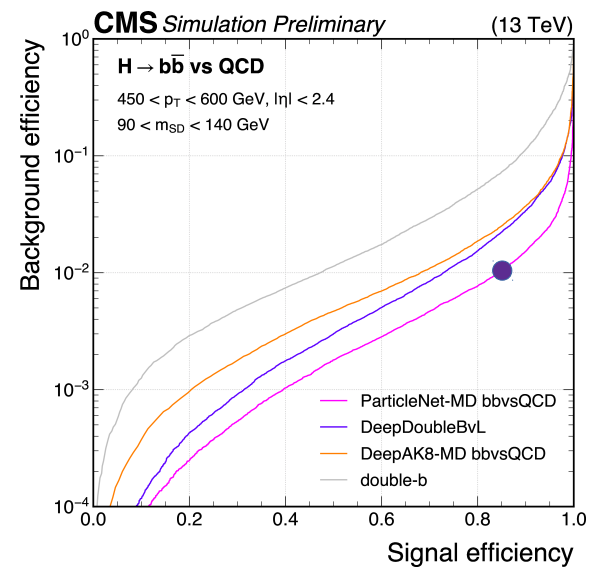


Used to measure background

Bols, Kieseler, Verzetti, Stoye, Stakia (2020)



CMS-PAS-BTV-22-001



BIT training & template optimization



Objective:

- SMEFT effects vs
- SM VH
- Background

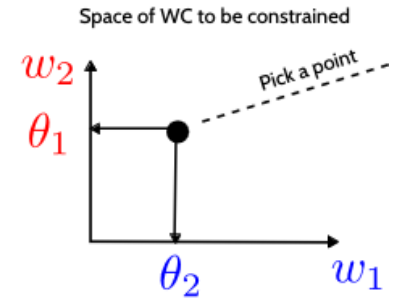
Inputs:

- Object kinematics
- Jet tagging scores
- Angular variables

Template optimization

Optimal performance guaranteed
if binning is chosen at each point in EFT space

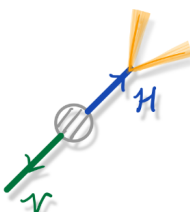
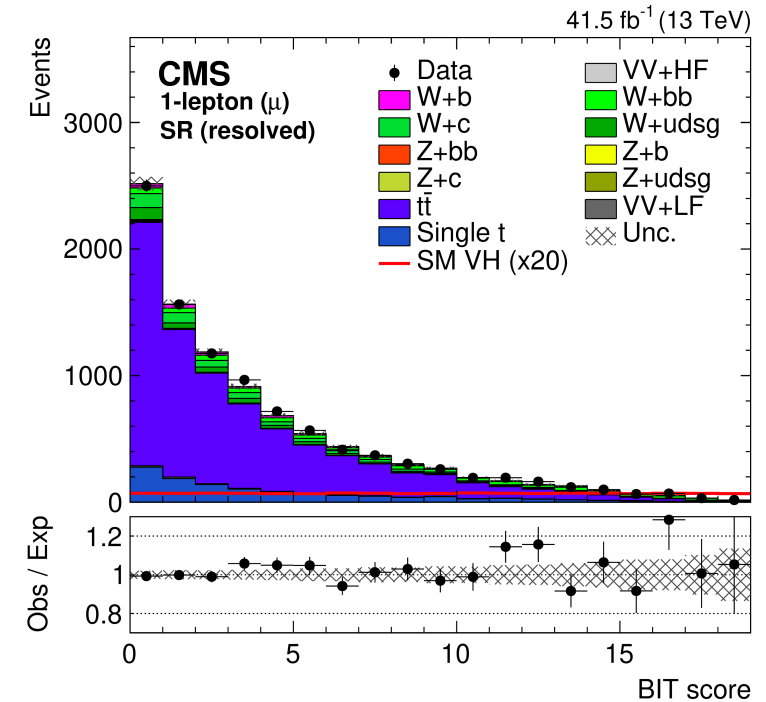
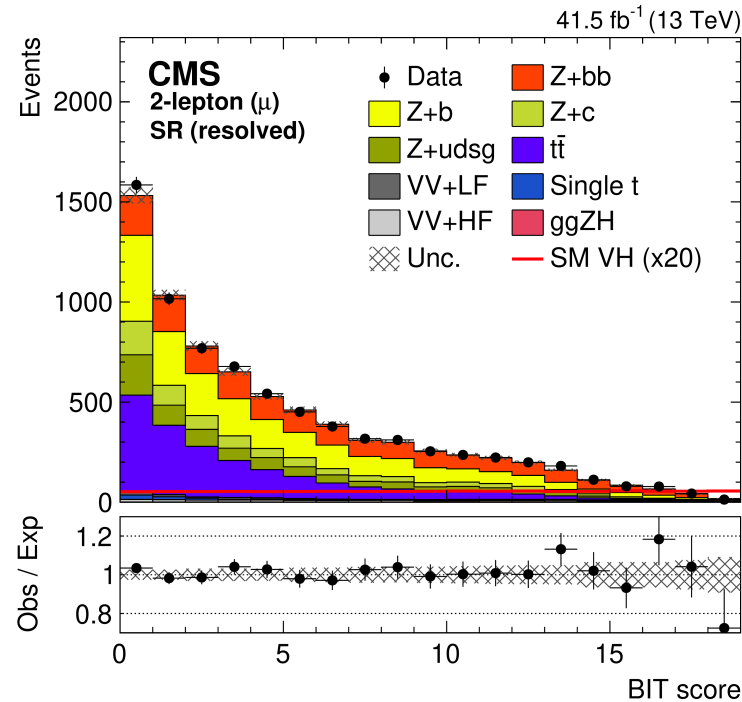
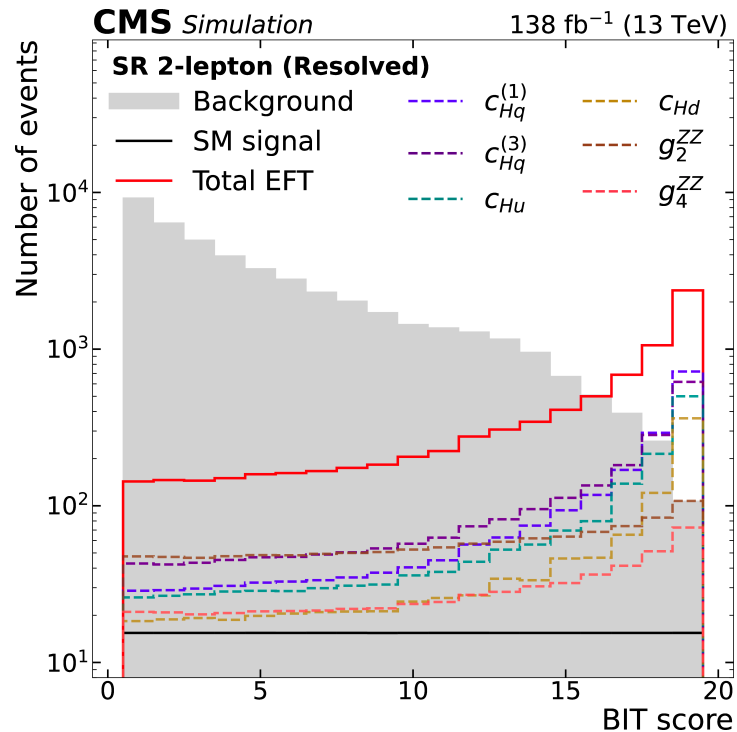
very challenging



No EFT effects considered in background

Template is chosen minimizing $\prod 2\sigma$ intervals (profiled)

← Find the point in EFT space



BIT training & template optimization



Objective:

- SMEFT effects vs
- SM VH
- Background

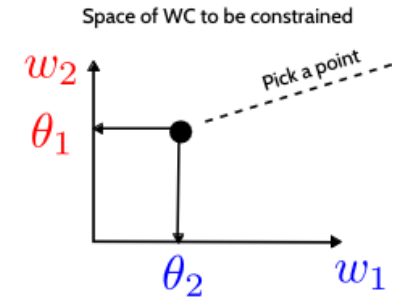
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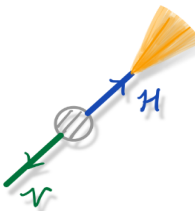
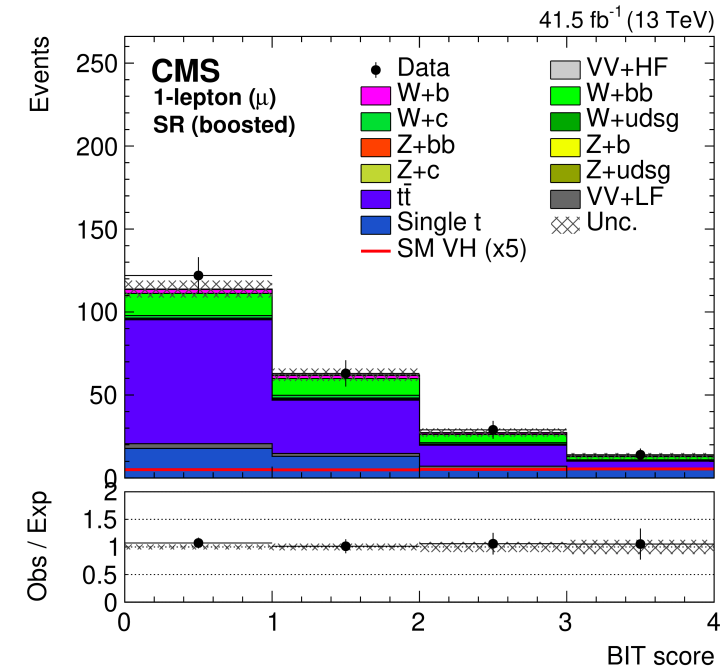
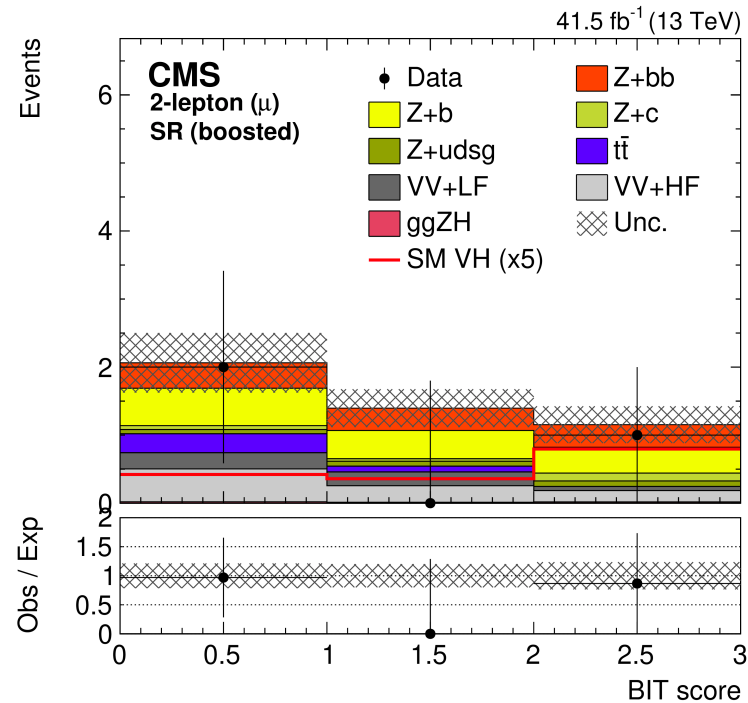
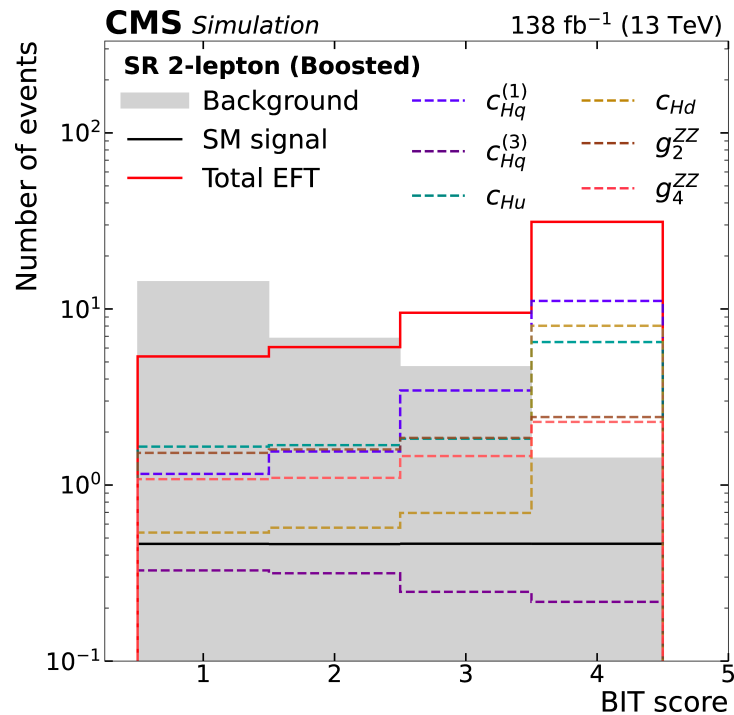
very challenging



No EFT effects considered in background

Template is chosen minimizing $\prod 2\sigma$ intervals (profiled)

← Find the point in EFT space



EFT interpretation: Wilson coefficients

With **linear** or **full quadratic** expansion

$$\sigma \sim |\mathcal{M}_{\text{SMEFT}}|^2$$

$$\sim |\mathcal{M}_{\text{SM}}|^2 + \sum_i \frac{c_i}{\Lambda^2} 2\text{Re}(\mathcal{M}_{\text{SM}}^\dagger \mathcal{M}_{6,i}) + \sum_i \frac{c_i^2}{\Lambda^4} |\mathcal{M}_{6,i}|^2 + \sum_i \sum_{j,j>i} \frac{c_i c_j}{\Lambda^4} \mathcal{M}_{6,i} \mathcal{M}_{6,j}$$

$\Lambda = 1 \text{ TeV}$

Compatibility with SM while varying all coefficients together

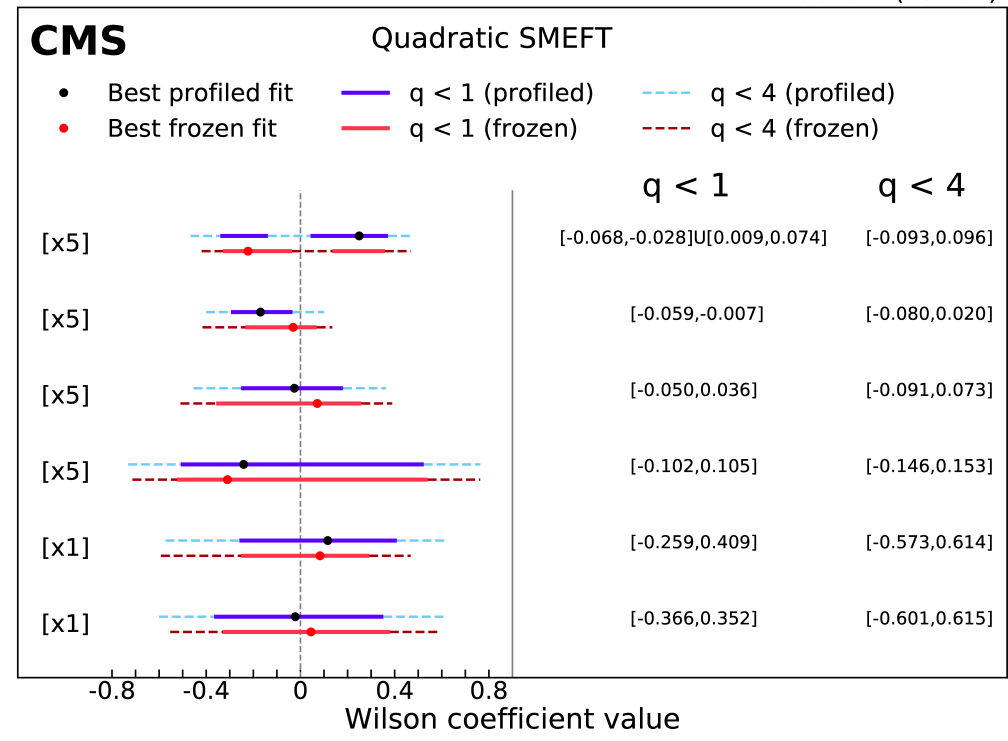
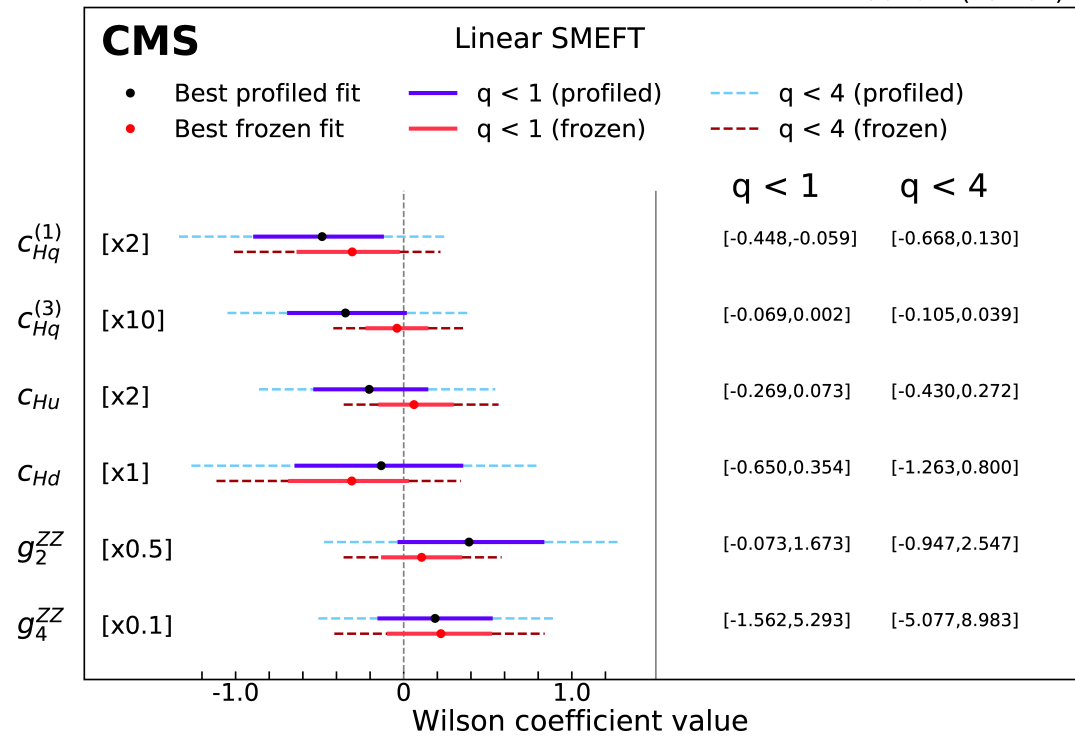
arXiv: 2411.16907

p-value = 73%

p-value = 84%

138 fb⁻¹ (13 TeV)

138 fb⁻¹ (13 TeV)



Quadratic component dominates sensitivity for most coefficients

EFT interpretation: energy scale

With **linear** or **full quadratic** expansion

$$\sigma \sim |\mathcal{M}_{\text{SMEFT}}|^2$$

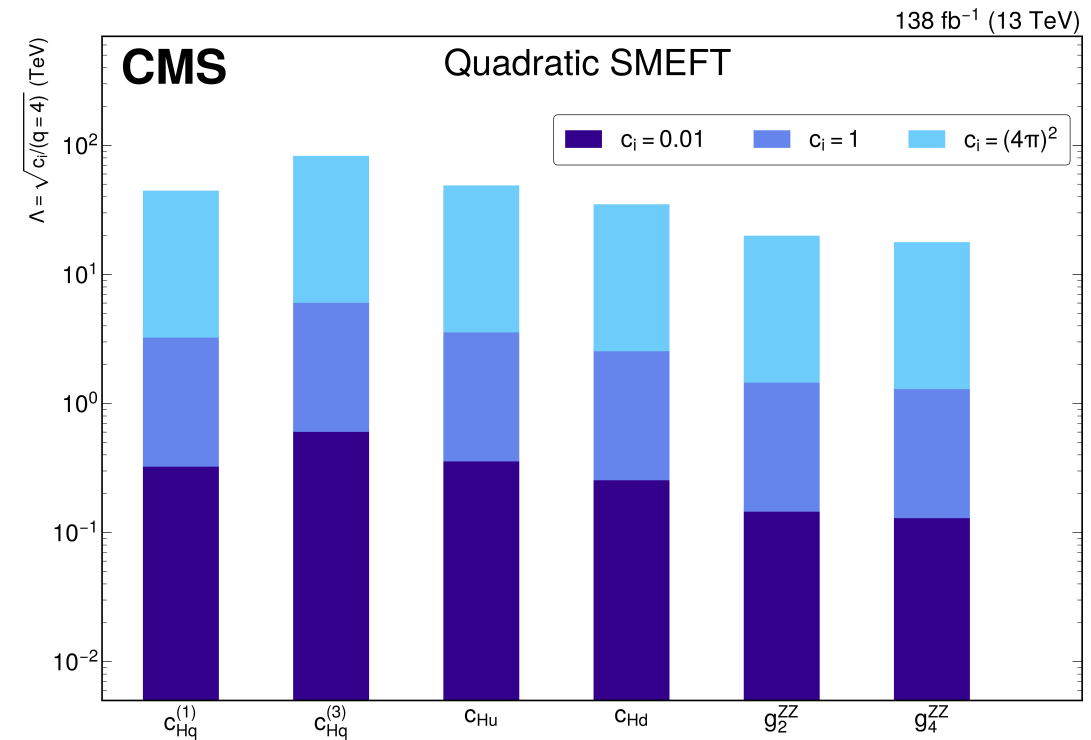
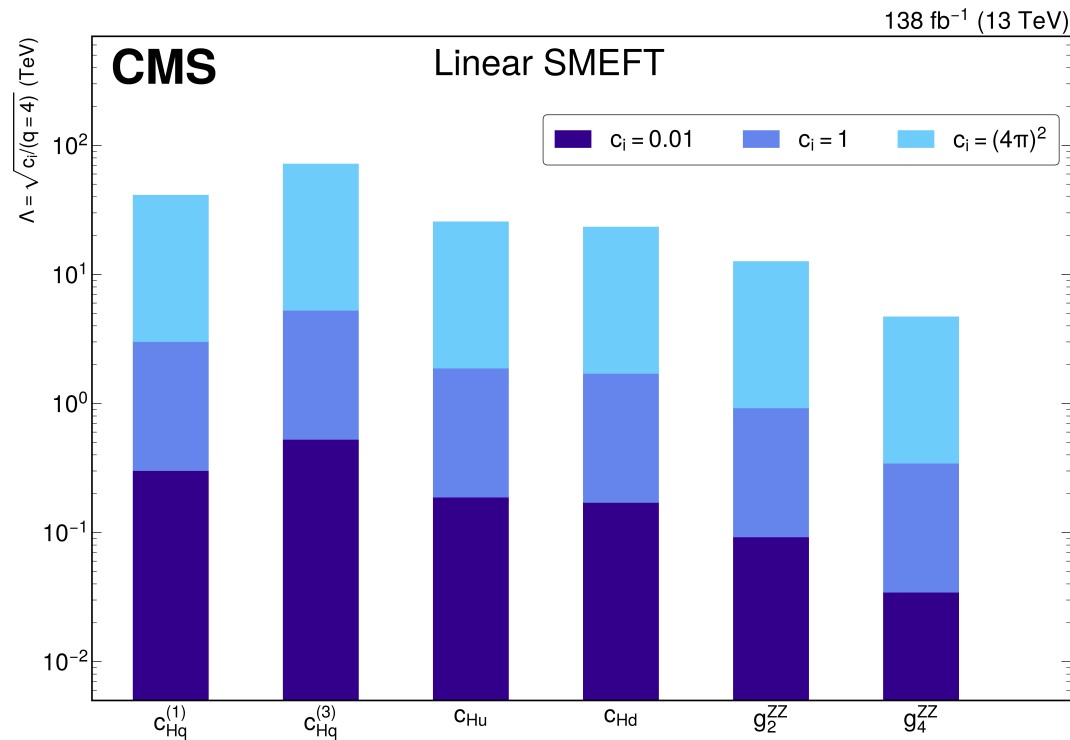
$$\sim |\mathcal{M}_{\text{SM}}|^2 + \sum_i \frac{c_i}{\Lambda^2} 2\text{Re}(\mathcal{M}_{\text{SM}}^\dagger \mathcal{M}_{6,i}) + \sum_i \frac{c_i^2}{\Lambda^4} |\mathcal{M}_{6,i}|^2 + \sum_i \sum_{j,j>i} \frac{c_i c_j}{\Lambda^4} \mathcal{M}_{6,i} \mathcal{M}_{6,j}$$

Lower bound on Λ

Three BSM scenarios:

- weakly coupled model ($c=0.01$)
- no assumption ($c=1$)
- strongly-coupling perturbativity limit ($c=16\pi^2$)

arXiv: 2411.16907



Sensitivity: ~ few TeV for $c=1$

EFT interpretation: Wilson coefficients in 2D

With
full quadratic
expansion

$$\sigma \sim |\mathcal{M}_{\text{SMEFT}}|^2$$

$$\sim |\mathcal{M}_{\text{SM}}|^2 + \sum_i \frac{c_i}{\Lambda^2} 2\text{Re}(\mathcal{M}_{\text{SM}}^\dagger \mathcal{M}_{6,i}) + \sum_i \frac{c_i^2}{\Lambda^4} |\mathcal{M}_{6,i}|^2 + \sum_i \sum_{j,j>i} \frac{c_i c_j}{\Lambda^4} \mathcal{M}_{6,i} \mathcal{M}_{6,j}$$

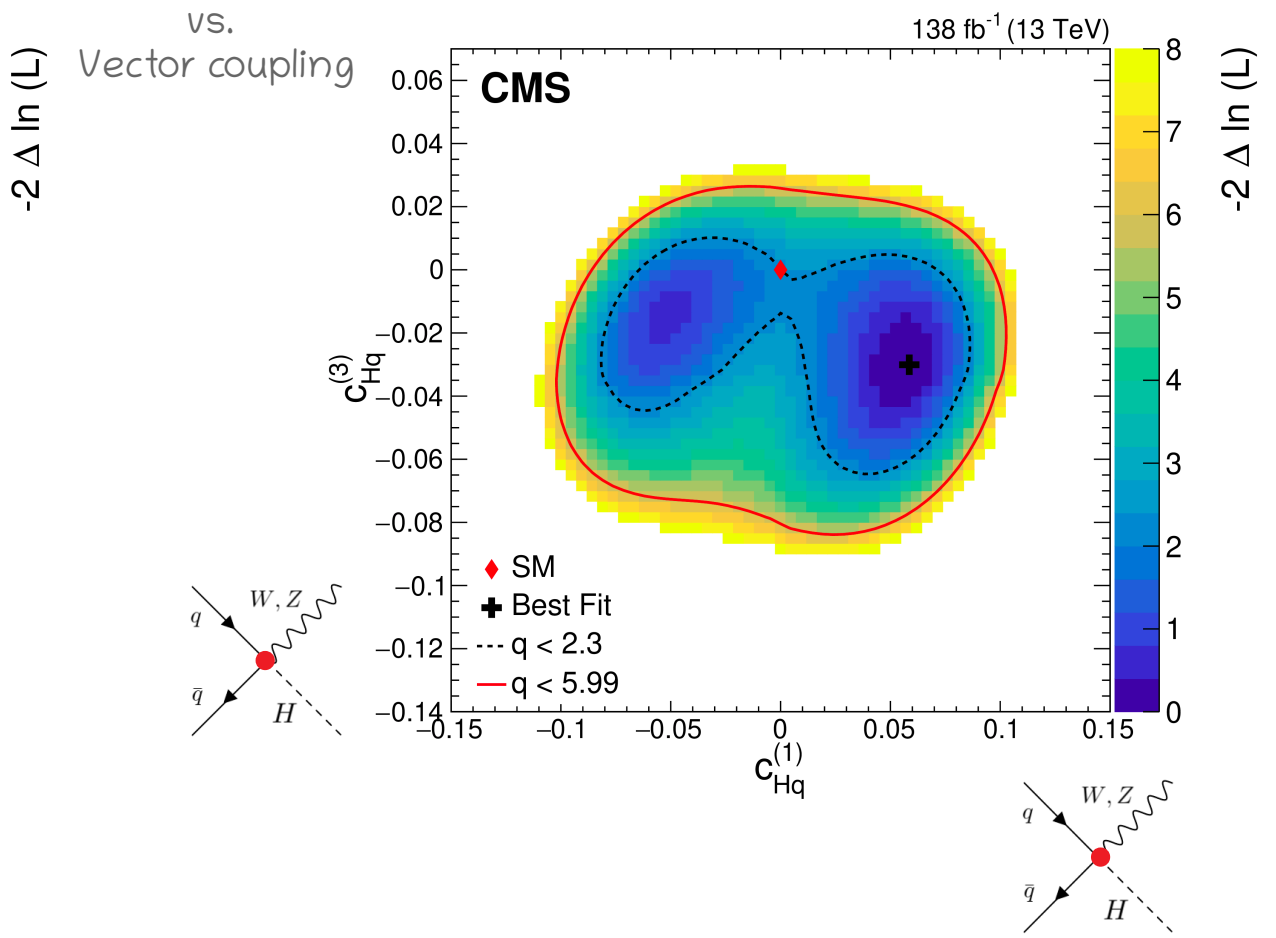
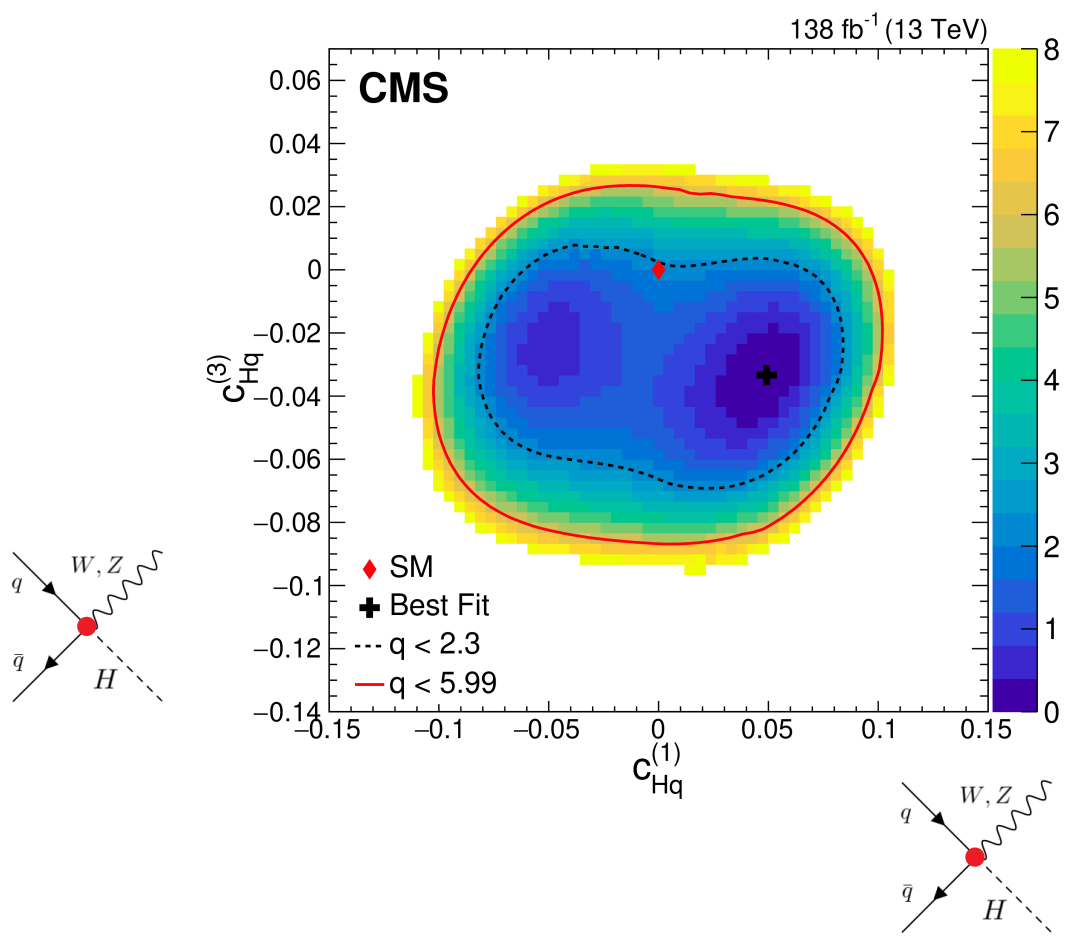
$\Lambda = 1 \text{ TeV}$

Other coefficients profiled

Vector coupling
vs.
Vector coupling

Other coefficients fixed at 0

arXiv: 2411.16907



EFT interpretation: Wilson coefficients in 2D

With
full quadratic
expansion

$$\sigma \sim |\mathcal{M}_{\text{SMEFT}}|^2$$

$$\sim |\mathcal{M}_{\text{SM}}|^2 + \sum_i \frac{c_i}{\Lambda^2} 2\text{Re}(\mathcal{M}_{\text{SM}}^\dagger \mathcal{M}_{6,i}) + \sum_i \frac{c_i^2}{\Lambda^4} |\mathcal{M}_{6,i}|^2 + \sum_i \sum_{j,j>i} \frac{c_i c_j}{\Lambda^4} \mathcal{M}_{6,i} \mathcal{M}_{6,j}$$

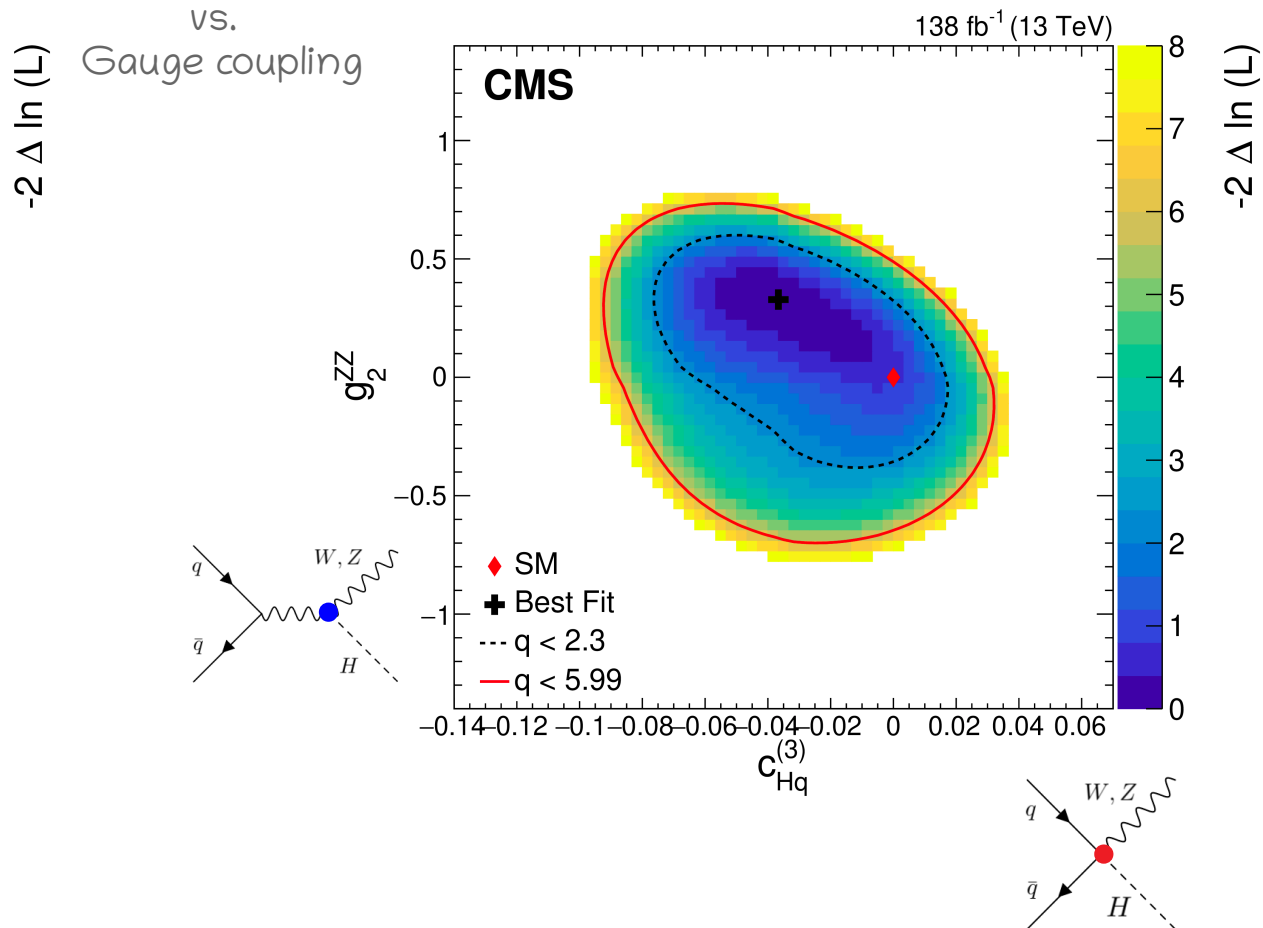
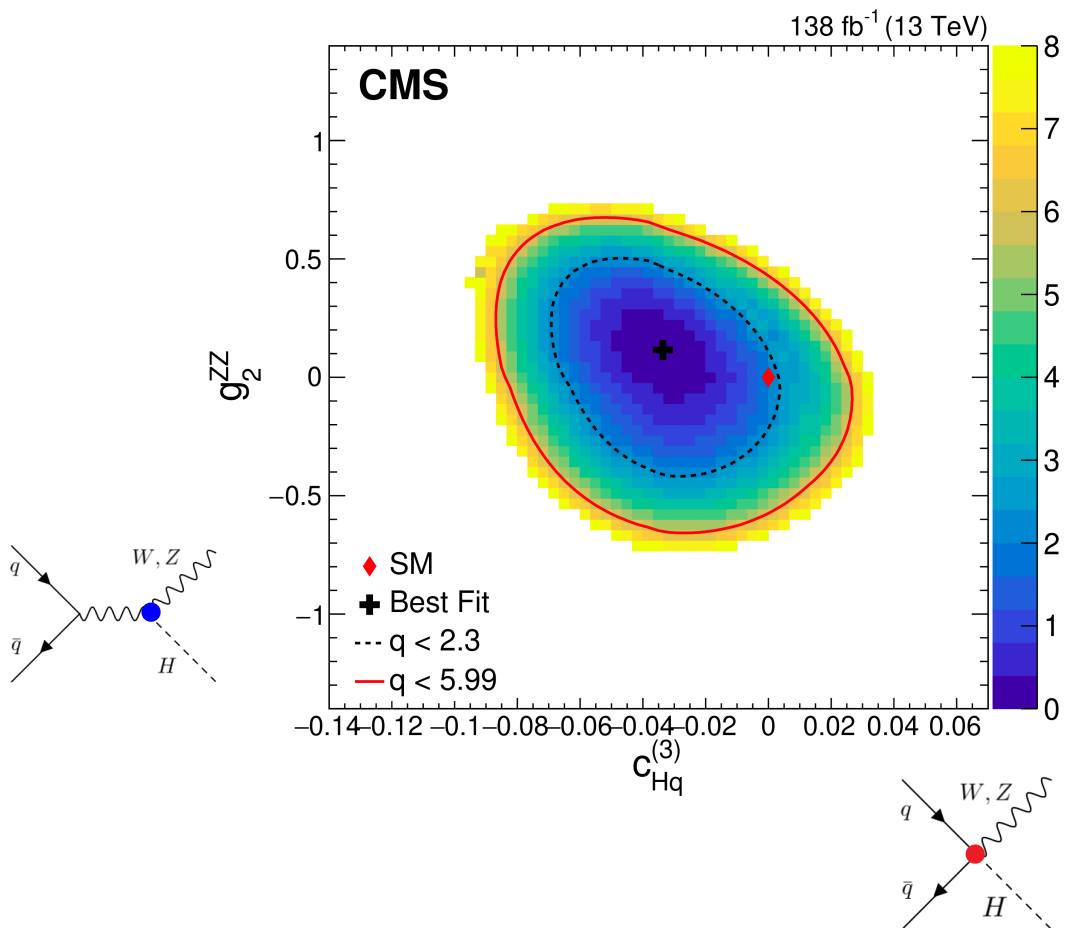
$\Lambda = 1 \text{ TeV}$

Other coefficients profiled

Vector coupling
vs.
Gauge coupling

Other coefficients fixed at 0

arXiv: 2411.16907



Highlights

In K. Cranmer's [DESY Colloquium](#)



ATLAS CONF Note

ATLAS-CONF-2024-015

28th October 2024



Available on the CERN CDS information server

CMS PAS HIG-23-016

CMS Physics Analysis Summary

Contact: cms-pag-conveners-higgs@cern.ch

2024/09/20

An implementation of Neural Simulation-Based Inference for Parameter Estimation in ATLAS

The ATLAS Collaboration

Neural Simulation-Based Inference (NSBI) is a powerful class of machine learning (ML)-based methods for statistical inference that naturally handles high-dimensional parameter estimation without the need to bin data into low-dimensional summary histograms. Such methods are promising for a range of measurements, including at the Large Hadron Collider (LHC), where no single observable may be optimal to scan over the entire theoretical phase space under consideration, or where binning data into histograms could result in a loss of sensitivity. This work develops an NSBI framework for statistical inference, using neural networks to estimate probability density ratios, which enables the application of NSBI to a full-scale LHC analysis. It incorporates a large number of systematic uncertainties, quantifies the uncertainty coming from finite training statistics, develops a method to construct confidence intervals, and demonstrates a series of intermediate diagnostic checks that can be performed to validate the robustness of the method. As an example, the power and feasibility of the method are demonstrated on simulated data for a simplified version of an off-shell Higgs boson couplings measurement in the four-leptons final states. This NSBI framework is an extension of the standard statistical framework used by LHC experiments and can benefit a large number of physics analyses.

Constraints on standard model effective field theory effects with Higgs bosons produced in association with W or Z bosons in the $H \rightarrow b\bar{b}$ decay channel in proton-proton collisions at $\sqrt{s} = 13$ TeV

The CMS Collaboration

Abstract

A standard model effective field theory (SMEFT) analysis with dimension-six operators is performed in the Higgsstrahlung process, where the Higgs boson is produced in association with a W or Z boson, in proton-proton collisions at a center-of-mass energy of 13 TeV. The final states where the W or Z boson decay leptonically and the Higgs boson decays to a pair of bottom quarks are considered. The analyzed data were collected by the CMS experiment between 2016 and 2018 and correspond to an integrated luminosity of 138 fb^{-1} . An approach targeted to optimize simultaneously the sensitivity to Wilson coefficients of multiple SMEFT operators is employed. The observed results are consistent with the predictions of the standard model.

ATLAS-CONF-2024-015
28 October 2024

ATLAS used simulation-based inference for off-shell H production

Neural network-based approach: [arXiv: 2412.01548](https://arxiv.org/abs/2412.01548)



Summary

- Detailed effective field theory analysis in Higgs production in association with W/Z boson with full Run 2 data
 - *Follow-up & complementary to cross section measurements*
- Probed effects of both **vector** and **gauge** coupling operators
- First application of **likelihood-free/simulation-based inference** at colliders
 - *Developed outside collaboration & technology available for any EFT analysis*
 - *Road towards fully unbinned EFT analysis using optimal observables [see Schöfbeck (2024)]*
- Results reported as constraints on Wilson coefficients
 - *in 1D with other coefficients profiled or set to SM values*
 - *in 2D with other coefficients profiled or set to SM values*
 - ← *findings consistent with SM*
- Best SMEFT sensitivity reported in **VH(bb) channel** till date

Documentation
 arXiv: 2411.16907
 (Accepted in JHEP)



Extra Material

Learning SMEFT likelihood with decision trees (1)

Tree prediction $\hat{F}(\mathbf{x}) = \sum_{j \in \mathcal{J}} \mathbb{1}_{\alpha_j}(\mathbf{x}) F_j$

\mathbf{x} : Feature vectors
 j : Terminal nodes
 α_j : Requirements on \mathbf{x} for node j
 F_j : Prediction for node j

Phase space partitioning Prediction

Minimization of loss function w.r.t. α_j and F_j

Linear term in SMEFT expansion

$$\text{MSE}[\hat{F}_a] = \sum_{j \in \mathcal{J}} \sum_{i \in j} w_i \left| \frac{w_{i,a}}{w_i} - F_j \right|^2 = \sum_{i=1}^{N_{\text{sim}}} \frac{w_{i,a}^2}{w_i} - 2 \sum_{j \in \mathcal{J}} F_j \sum_{i \in j} w_{i,a} + \sum_{j \in \mathcal{J}} F_j^2 \sum_{i \in j} w_i.$$

Integral replaced by summation

$$\lambda_j = \sum_{i \in j} w_i$$

$$\frac{\partial}{\partial F_j} \text{MSE}[\hat{F}_a] = 0 \rightarrow F_j = \frac{\sum_{i \in j} w_{i,a}}{\sum_{i \in j} w_i} = \frac{\partial_a \lambda_j}{\lambda_j} \Big|_{\theta=\theta_0} = \partial_a \log \lambda_j \Big|_{\theta=\theta_0}$$

$$\text{MSE}[\hat{F}_a] = - \sum_{j \in \mathcal{J}} \frac{\left(\sum_{i \in j} w_{i,a} \right)^2}{\sum_{i \in j} w_i} = - \sum_{j \in \mathcal{J}} \frac{(\partial_a \lambda_j)^2}{\lambda_j} \Big|_{\theta=\theta_0} = - \sum_{j \in \mathcal{J}} I^{(\lambda_j)}$$

Fisher information for measurement of θ

Fisher information = Variance of score (= derivative of log-likelihood)

Cramér-Rao bound: $\text{Variance}(\hat{\theta}) \geq \frac{1}{I(\theta)}$ [wiki](#)

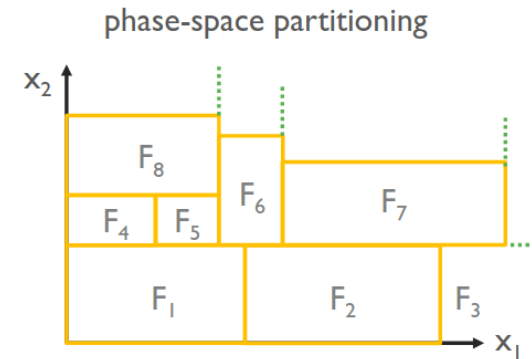
Node-split criterion maximizes Fisher information → Optimal in precision

$$\lambda_j = b_j + \theta s_j \quad \rho_j = \frac{\theta s_j}{b_j + \theta s_j}$$

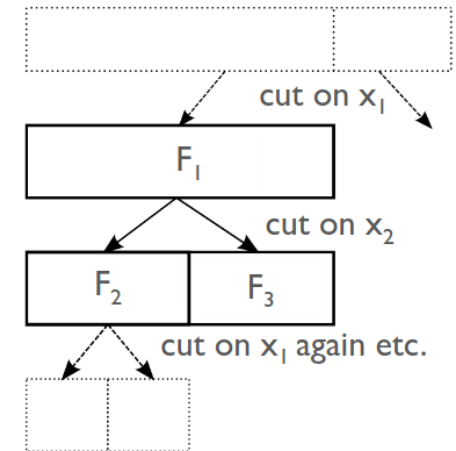
$$L = - \sum_j \frac{(\partial_\theta \lambda_j)^2}{\lambda_j} = - \sum_j \frac{s_j^2}{b_j + \theta s_j} = - \frac{1}{\theta^2} \sum_j \lambda_j \rho^2 \equiv \sum_j \lambda_j \rho(1 - \rho)$$

Starting point of SC, N. Frohner, L. Lechner, R. Schoefbeck, D. Schwarz (2021)

Gini index implemented in TMVA for classification



Training phase



Quadratic term in SMEFT expansion

$$F_j = \frac{\sum_{i \in j} w_{i,ab}}{\sum_{i \in j} w_i} = \frac{\partial_a \partial_b \lambda_j}{\lambda_j} \Big|_{\theta=\theta_0}$$

$$\text{MSE}[\hat{F}_{ab}] = - \sum_{j \in \mathcal{J}} \frac{\left(\sum_{i \in j} w_{i,ab} \right)^2}{\sum_{i \in j} w_i} = - \sum_{j \in \mathcal{J}} \frac{(\partial_a \partial_b \lambda_j)^2}{\lambda_j} \Big|_{\theta=\theta_0}$$

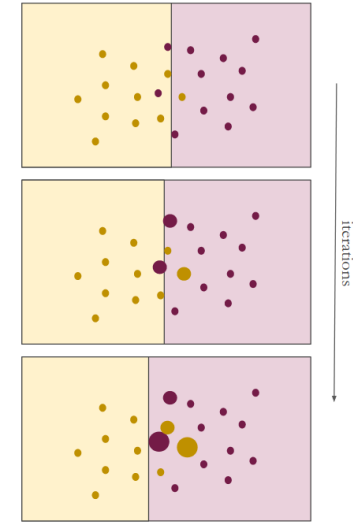
Learning SMEFT likelihood with decision trees (2)

Boosting: Provides a strong learner by iteratively training an ensemble of weak learners to pseudo-residuals of previous iteration

$$\hat{F}^b(x) = \hat{f}^b(x) + \eta \hat{F}^{b-1}(x) \quad \text{Minimize loss function loss w.r.t. } f(x) \quad \leftarrow \text{Goes on till a pre-defined number } B$$

$$\text{MSE}[\hat{F}_a] = \sum_{j \in \mathcal{J}} \sum_{i \in j} w_i \left| \frac{w_{i,a}}{w_i} - \hat{f}^b(x) - \eta \hat{F}^{b-1}(x) \right|^2 = \sum_{j \in \mathcal{J}} \sum_{i \in j} w_i \left| \frac{w_{i,a} - \eta \hat{F}^{b-1}(x) w_i}{w_i} - \hat{f}^b(x) \right|^2$$

Weak learner needs to fit $w - \eta F$ \leftarrow Target needs to be updated in each iteration



Final outcome of algorithm $\hat{R}(x|\theta, \theta_0) = 1 + (\theta - \theta_0)_a \hat{F}_a^{(B)}(x) + \frac{1}{2}(\theta - \theta_0)_a(\theta - \theta_0)_b \hat{F}_{ab}^{(B)}(x)$ Boosted information tree (BIT)

SC, S. Roshap, R. Schoefbeck, D. Schwarz (2022)

Separate training for each linear ('a') & quadratic terms ('ab') \rightarrow Total # of trainings = $n + n(n+1)/2$

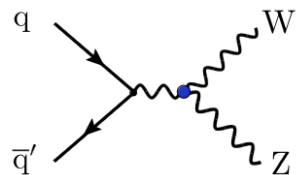
$$q(\mathcal{D}(N_{\text{obs}}, x)|\theta_1, \theta_0) \stackrel{\text{LLR to achieve}}{=} -2 \left[\mathcal{L}(\sigma(\theta_1) - \sigma(\theta_0)) - \sum_{i=1}^{N_{\text{obs}}} \ln R(x|\theta_1, \theta_0) \right] \stackrel{\text{(in large sample limit)}}{=} \hat{q}(\mathcal{D}(N_{\text{obs}}, x)|\theta_1, \theta_0) \stackrel{\text{LLR obtained}}{=} -2 \left[\mathcal{L}(\sigma(\theta_1) - \sigma(\theta_0)) - \sum_{i=1}^{N_{\text{obs}}} \ln \hat{R}(x|\theta_1, \theta_0) \right]$$

Simulation strategy for SMEFT

Possible to encode SMEFT prediction in event weights $\omega = \frac{|\mathcal{M}_{SMEFT}(c = c_1)|^2}{|\mathcal{M}_{SMEFT}(c = c_0)|^2}$

$$\omega(\mathbf{z}|\mathbf{c}) \sim \frac{d\sigma}{dz} = \text{Const}(\mathbf{z}) + \text{LIN}_a(\mathbf{z})c_a + \frac{1}{2}\text{QUAD}_{ab}(\mathbf{z})c_ac_b$$

Store N(n) weights per event \rightarrow obtain EFT prediction for any coefficient value



\rightarrow EFT operator changes helicity configuration

SM: +/-/-+ EFT: ++/--

Helicity-aware reweighting $\omega = \frac{|\mathcal{M}(z_p, h|c_1)|^2}{|\mathcal{M}(z_p, h|c_0)|^2}$

Needs careful choice of reference point

Helicity-ignorant reweighting $\omega = \frac{\sum_h |\mathcal{M}(z_p, h|c_1)|^2}{\sum_h |\mathcal{M}(z_p, h|c_0)|^2}$

Robust option

SC & others (2024)

