

Exclusive quarkonium production in photon-photon collisions with gamma-UPC

Quarkonia As Tools

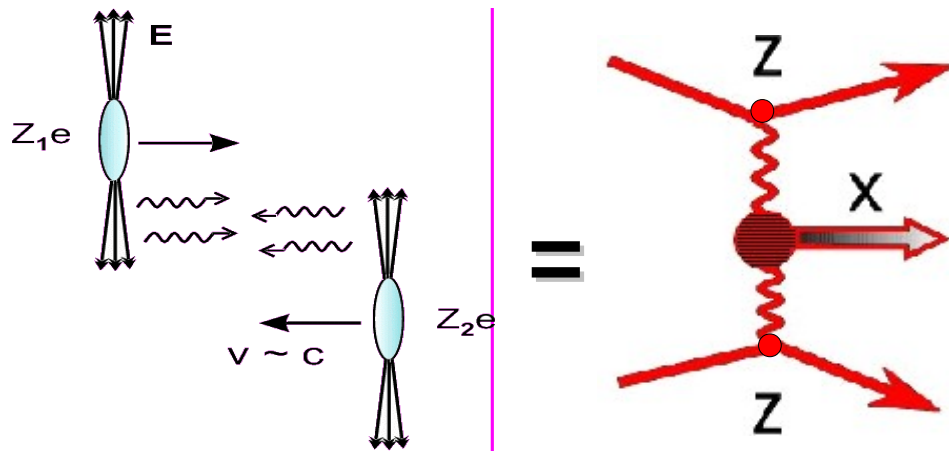
Aussois, Savoie, 10th Jan. 2025

David d'Enterria
(CERN)

Work w/ **Hua-Sheng Shao**: arxiv:2207.03012 [JHEP 09 (2022) 248]
(also DdE & K.Kang, to be submitted)

LHC = Unique photon-photon collider

- **Electromagnetic** ultra-peripheral colls. (UPCs): $b_{\min} > R_A + R_B$, hadrons survive
- **EM field** = Weizsäcker-Williams (Equivalent Photon Approx.) photon flux:



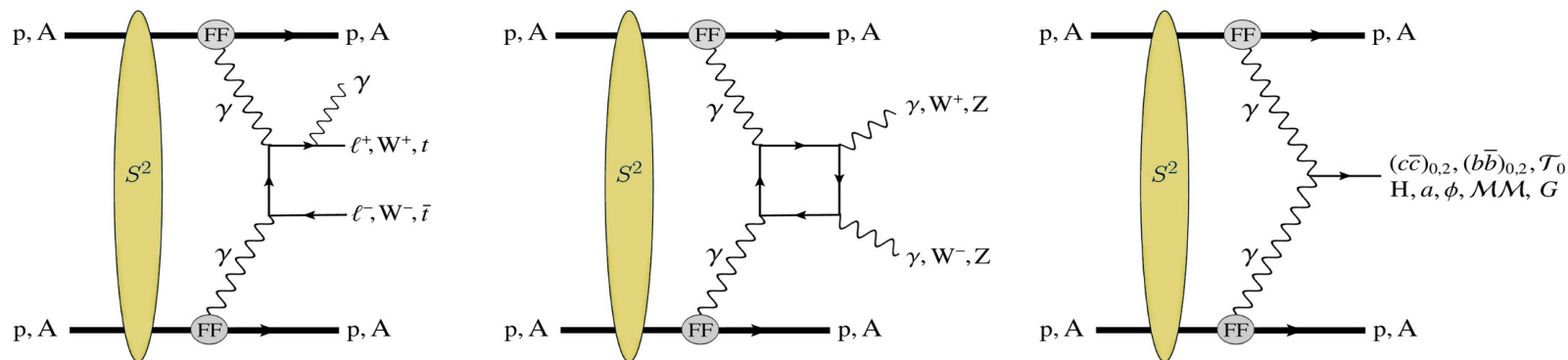
- **Huge photon fluxes:**
 $\sigma(\gamma\gamma) \approx Z^4$ ($\approx 5 \cdot 10^7$ for PbPb)
 times larger than p, e^\pm
- **Beam-energy dependence:**
 Photon-photon luminosities increase as $\propto \log^3(\sqrt{s})$

- **Quasi-real γ** (coherent emission): $Q \approx 1/R \approx 0.03$ GeV (Pb), 0.28 GeV (p)
- **Max. (longitudinal) γ energies:** $\omega < \omega_{\max} \approx \frac{\gamma}{R} \approx 80$ GeV (Pb), 2.5 TeV (p)

System	$\sqrt{s_{NN}}$	\mathcal{L}_{int}	$E_{\text{beam1}} + E_{\text{beam2}}$	γ_L	R_A	E_γ^{\max}	$\sqrt{s_{\gamma\gamma}^{\max}}$
Pb-Pb	5.52 TeV	5 nb ⁻¹	2.76 + 2.76 TeV	2960	7.1 fm	80 GeV	160 GeV
p-Pb	8.8 TeV	1 pb ⁻¹	7.0 + 2.76 TeV	7450, 2960	0.7, 7.1 fm	2.45 TeV, 130 GeV	2.6 TeV
p-p	14 TeV	150 fb ⁻¹	7.0 + 7.0 TeV	7450	0.7 fm	2.45 TeV	4.5 TeV

- ▶ **Single X = C-even (spin 0,2) resonances** only (Landau-Yang + C symmetry)

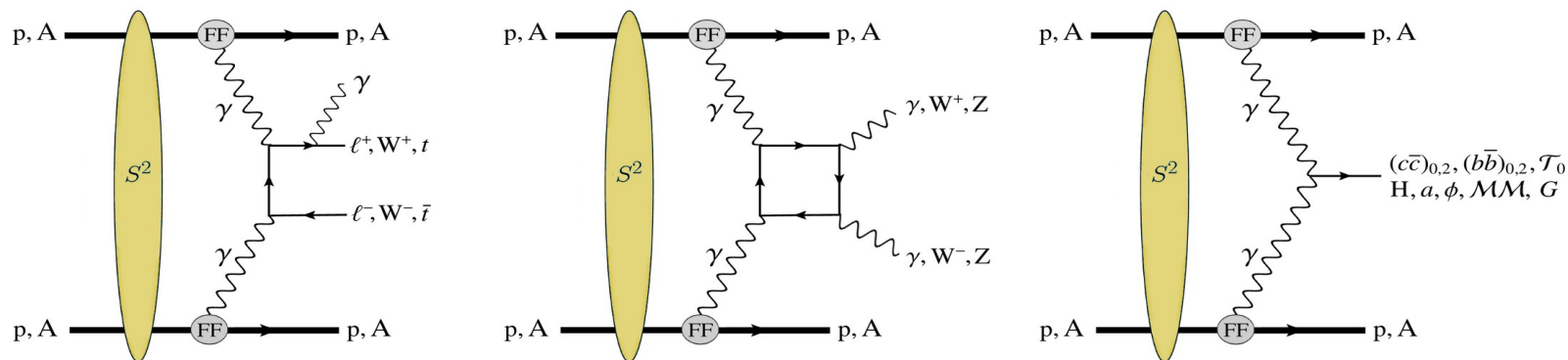
Rich & unique (B)SM $\gamma\gamma$ physics with UPCs at LHC



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Process	Physics motivation
$\gamma\gamma \rightarrow e^+e^-, \mu^+\mu^-$	“Standard candles” for proton/nucleus γ fluxes, EPA calculations, and higher-order QED corrections
$\gamma\gamma \rightarrow \tau^+\tau^-$	Anomalous τ lepton e.m. moments [29–32]
$\gamma\gamma \rightarrow \gamma\gamma$	aQGC [25], ALPs [27], BI QED [28], noncommut. interactions [36], extra dims. [37],...
$\gamma\gamma \rightarrow \mathcal{T}_0$	Ditauonium properties (heaviest QED bound state) [38, 39]
$\gamma\gamma \rightarrow (c\bar{c})_{0,2}, (b\bar{b})_{0,2}$	Properties of scalar and tensor charmonia and bottomonia [40, 41]
$\gamma\gamma \rightarrow XYZ$	Properties of spin-even XYZ heavy-quark exotic states [42]
$\gamma\gamma \rightarrow VMVM$	(with VM = $\rho, \omega, \phi, J/\psi, \Upsilon$): BFKL-Pomeron dynamics [43–46]
$\gamma\gamma \rightarrow W^+W^-, ZZ, Z\gamma, \dots$	anomalous quartic gauge couplings [11, 26, 47, 48]
$\gamma\gamma \rightarrow H$	Higgs- γ coupling, total H width [49, 50]
$\gamma\gamma \rightarrow HH$	Higgs potential [51], quartic $\gamma\gamma HH$ coupling
$\gamma\gamma \rightarrow t\bar{t}$	anomalous top-quark e.m. couplings [11, 49]
$\gamma\gamma \rightarrow \tilde{\ell}\tilde{\ell}, \tilde{\chi}^+\tilde{\chi}^-, H^{++}H^{--}$	SUSY pairs: slepton [11, 52, 53], chargino [11, 54], doubly-charged Higgs bosons [11, 55].
$\gamma\gamma \rightarrow a, \phi, MM, G$	ALPs [27, 56], radions [57], monopoles [58–61], gravitons [62–64],...

Rich & unique SM $\gamma\gamma$ physics with UPCs at LHC



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(this talk)

Dedicated $\gamma\gamma$ MC event generators (up to 2022)

- So far dedicated MC event generators include only **hard-coded $\gamma\gamma$ processes, LO QED/QCD only, no extra γ /gluon FSR, few (“uninteresting”) background processes generated,...**

STARlight (~2000)

Two-Photon Channels	
Particle	Jetset ID
e^+e^- pair	11
$\mu^+\mu^-$ pair	13
$\tau^+\tau^-$ pair	15
$\tau^+\tau^-$ pair, polarized decay	10015*
ρ^0 pair	33
$a_2(1320)$ decayed by PYTHIA	115
η decayed by PYTHIA	221
$f_2(1270)$ decayed by PYTHIA	225
η' decayed by PYTHIA	331
$f_2(1525) \rightarrow K^+K^-(50\%), K^0\bar{K}^0(50\%)$	335
η_c decayed by PYTHIA	441
$f_0(980)$ decayed by PYTHIA	9010221

SuperChic (~2010)

Two-photon collisions	
55	$W^+(\rightarrow \nu_l(8) + l^+(9)) + W^-(\rightarrow \bar{\nu}_l(10) + l^-(11))$
56	$e^+(6) + e^-(7)$
57	$\mu^+(6) + \mu^-(7)$
58	$\tau^+(6) + \tau^-(7)$
59	$\gamma(6) + \gamma(7)$
60	$H(5) \rightarrow b(6) + \bar{b}(6)$
68	$a(5) \rightarrow \gamma(6) + \gamma(7)$
69	$M(5) \rightarrow \gamma(6) + \gamma(7)$ (Dirac Coupling)
70	$M(5) \rightarrow \gamma(6) + \gamma(7)$ (βg Coupling)
71	$m(6) + \bar{m}(7)$ (Dirac Coupling)
72	$m(6) + \bar{m}(7)$ (βg Coupling)
73	$\tilde{\chi}^-(6)(\rightarrow \tilde{\chi}_0^-(8) + \mu^-(9) + \bar{\nu}_\mu(10)) + \tilde{\chi}^+(7)(\rightarrow \tilde{\chi}_0^+(11) + \mu^+(12) + \nu_\mu(13))$
74	$\tilde{\chi}^-(6)(\rightarrow \tilde{\chi}_0^-(8) + \bar{u}(9) + d(10)) + \tilde{\chi}^+(7)(\rightarrow \tilde{\chi}_0^+(11) + u(12) + \bar{d}(13))$
75	$\tilde{\chi}^-(6)(\rightarrow \tilde{\chi}_0^-(8) + \mu^-(9) + \bar{\nu}_\mu(10)) + \tilde{\chi}^+(7)(\rightarrow \tilde{\chi}_0^+(11) + u(12) + \bar{d}(13))$
76	$\tilde{l}^-(5)(\rightarrow \tilde{\chi}_0^-(8) + \mu^-(9)) + \tilde{l}^+(6)(\rightarrow \tilde{\chi}_0^+(10) + \mu^+(11))$
77	$\phi(5) \rightarrow \mu^+(6)\mu^-(7)$
78	$J/\psi(5) \rightarrow e^+(6)e^-(7)$
79	$\psi_{2S}(5) \rightarrow e^+(6)e^-(7)$

FPMC (~2010)

IPROC	Description
16006	$\gamma\gamma \rightarrow ll$
16010	$\gamma\gamma \rightarrow W^+W^-$
16010	$\gamma\gamma \rightarrow W^+W^-$ beyond SM
16015	$\gamma\gamma \rightarrow ZZ$ beyond SM

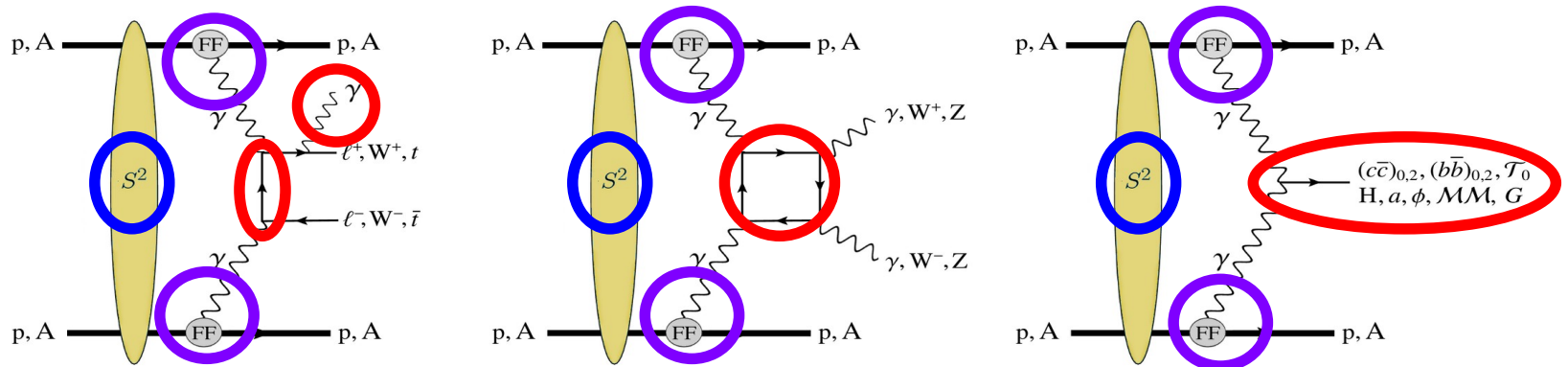
only pp UPC

UPCgen, LPAIR/CepGen (~2020)

$$\gamma\gamma \rightarrow l^+l^-$$

gamma-UPC $\gamma\gamma$ MC event generator

- gamma-UPC features: [\[H.S.Shao/DdE, JHEP09\(2022\)248. http://cern.ch/hshao/gammaupc.html\]](http://cern.ch/hshao/gammaupc.html)
 - Arbitrary (B)SM & $Q\bar{Q}$ matrix elements with MG5@NLO & HelacOnia
 - N γ /gluon FSR out-of-the-box. Extendable to NLO QCD & EW
 - LHE output: FSR+shower+hadronization via PS (PY8, HERWIG,...)
 - 2 different form factors (γ fluxes) coded. Glauber MC for the non-overlap
 - Any colliding combination: p-p,p-A,A-A (for any A)



- gamma-UPC key properties:
 - 1) Matrix elements: MG5@NLO, HelacOnia, custom (N γ /g FSR's, NLO QCD/EW)
 - 2) p,A form factors: Charge (ChFF) (and Electric Dipole, EDFF) γ fluxes
 - 3) p,A survival probability: Glauber-MC $T_{AA}(b)$ (and optical Glauber) eikonal

Heavy-ion γ fluxes: ChFF vs. EDFF

■ Electric dipole form factor (EDFF)

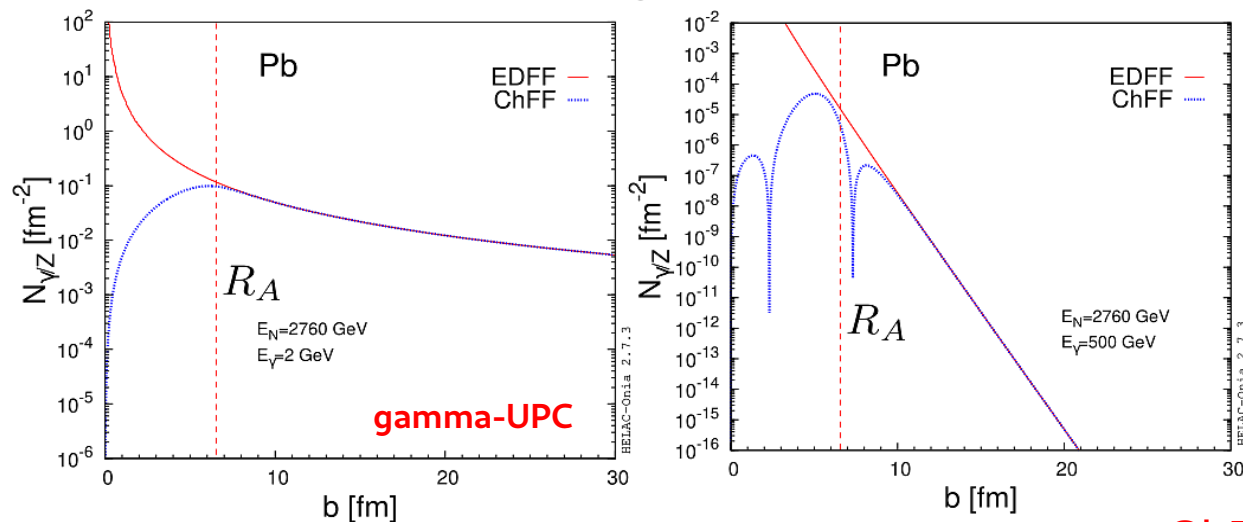
- Same as STARlight

$$N_{\gamma/Z}^{\text{EDFF}}(E_\gamma, b) = \frac{Z^2 \alpha}{\pi^2} \frac{\xi^2}{b^2} \left[K_1^2(\xi) + \frac{1}{\gamma_L^2} K_0^2(\xi) \right] \quad \xi = \frac{E_\gamma b}{\gamma_L}$$

■ Charge form factor (ChFF) (same as SuperChic)

$$N_{\gamma/Z}^{\text{ChFF}}(E_\gamma, k_\perp) = 2\pi k_\perp \frac{Z^2 \alpha}{\pi^2} \left| \int_0^\infty \frac{db k_\perp^2}{k_\perp^2 + E_\gamma^2/\gamma_L^2} F_{\text{ch},A} \left(\sqrt{k_\perp^2 + E_\gamma^2/\gamma_L^2} \right) J_1(bk_\perp) \right|^2 = \frac{2Z^2 \alpha}{\pi} \frac{k_\perp^3}{(k_\perp^2 + E_\gamma^2/\gamma_L^2)^2} \left[F_{\text{ch},A} \left(\sqrt{k_\perp^2 + E_\gamma^2/\gamma_L^2} \right) \right]^2$$

$$F_{\text{ch},A}(q) = \int d^3\mathbf{r} e^{i\mathbf{q}\cdot\mathbf{r}} \rho_A(\mathbf{r}) = \frac{4\pi}{q} \int_0^{+\infty} dr \rho_A(r) r \sin(qr) \quad \rho_A(\mathbf{r}) = \rho, A \text{ matter density}$$



- Main difference comes from the $b < R_A$ regime
- EDFF photon number density is divergent at $b = 0$
 - Need a (arbitrary) cutoff when convoluting with ME

■ ChFF is more realistic & also agrees better with $\gamma\gamma \rightarrow \ell\ell$ UPC data at LHC.

Proton γ fluxes: ChFF vs. EDFF

■ Electric dipole form factor (EDFF)

- Same as STARlight

$$N_{\gamma/Z}^{\text{EDFF}}(E_\gamma, b) = \frac{Z^2 \alpha}{\pi^2} \frac{\xi^2}{b^2} \left[K_1^2(\xi) + \frac{1}{\gamma_L^2} K_0^2(\xi) \right] \quad \xi = \frac{E_\gamma b}{\gamma_L}$$

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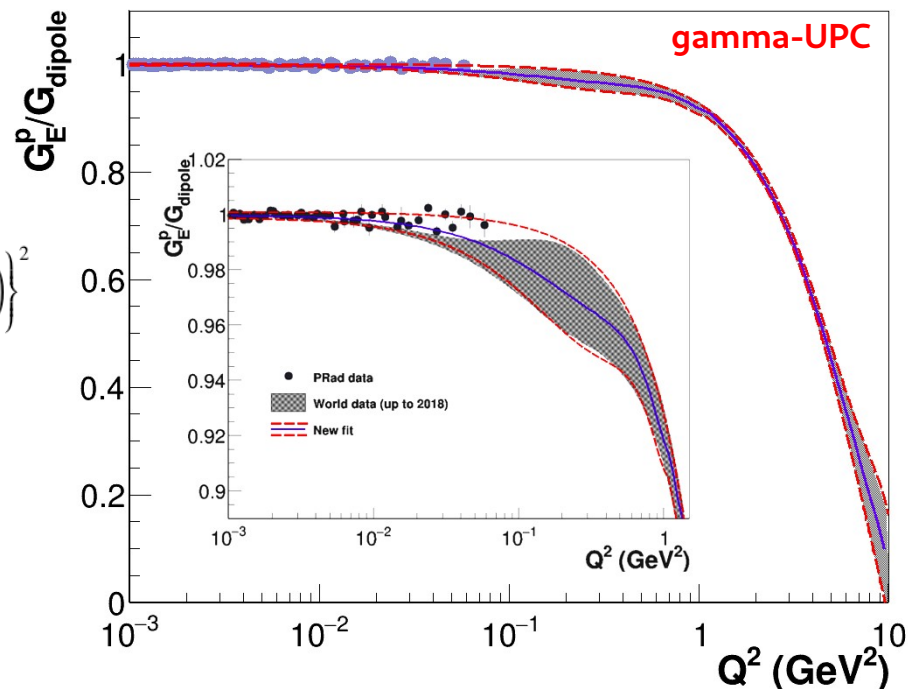
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■ Proton dipole form-factor:

$$F_{\text{ch},p}(q) = \frac{1}{(1 + q^2 a_p^2)^2} \quad \text{with } a_p^{-2} = Q_0^2 = 0.71 \text{ GeV}^2$$

$$N_{\gamma/p}^{\text{ChFF}}(E_\gamma, b) = \frac{\alpha}{\pi^2} \frac{\xi^2}{b^2} \left\{ \left[K_1(\xi) - \sqrt{1 + \tilde{a}_p^{-2}} K_1 \left(\xi \sqrt{1 + \tilde{a}_p^{-2}} \right) \right] - \frac{\xi}{2\tilde{a}_p^2} K_0 \left(\xi \sqrt{1 + \tilde{a}_p^{-2}} \right) \right\}^2$$

■ Updated proton elastic ChFF, from fit to latest A1+PRad e-p elastic data:



$\gamma\gamma$ EPA cross sections & A-A survival probability

■ Cross section:

$$\sigma(A B \xrightarrow{\gamma\gamma} A X B) = \int \frac{dE_{\gamma_1}}{E_{\gamma_1}} \frac{dE_{\gamma_2}}{E_{\gamma_2}} \frac{d^2 N_{\gamma_1/Z_1, \gamma_2/Z_2}^{(AB)}}{dE_{\gamma_1} dE_{\gamma_2}} \sigma_{\gamma\gamma \rightarrow X}(W_{\gamma\gamma})$$

■ Effective two-photon luminosity:

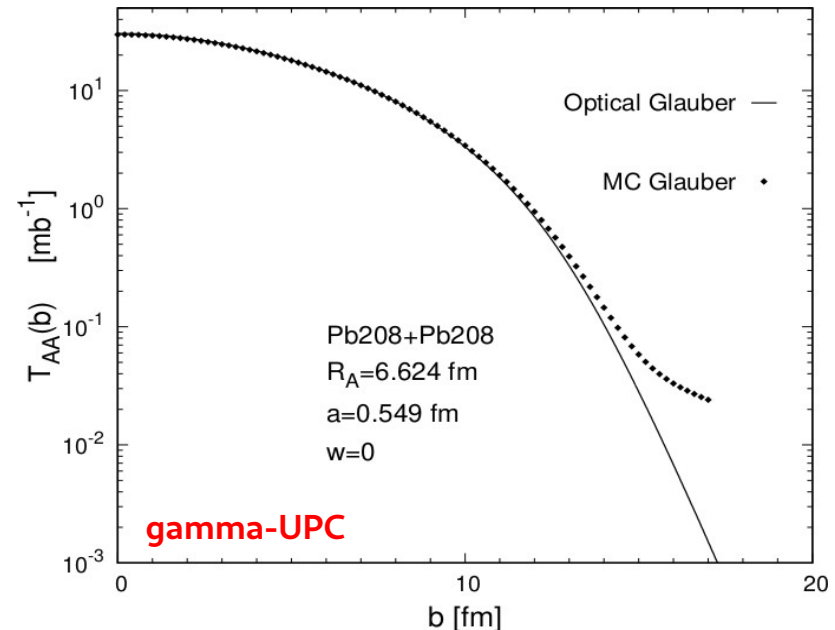
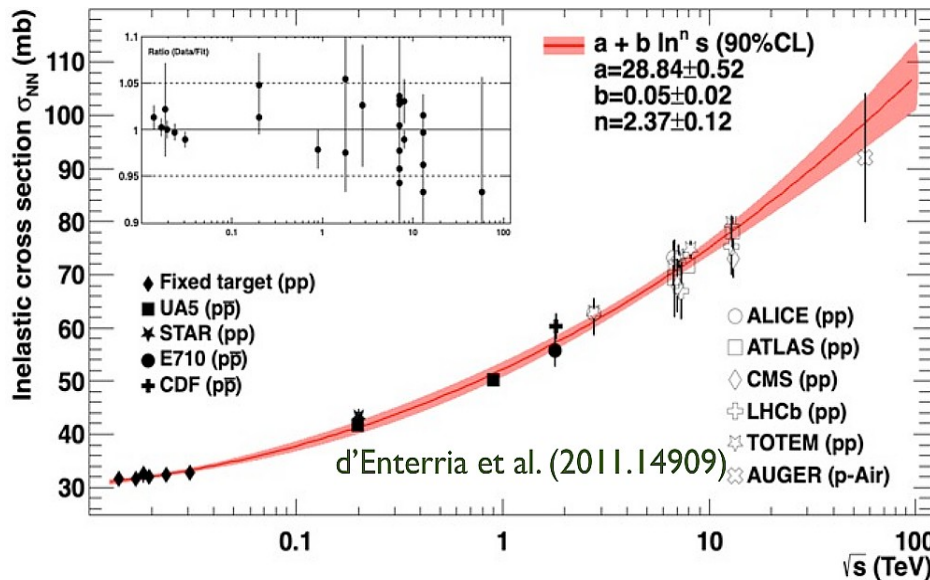
$$\frac{d^2 N_{\gamma_1/Z_1, \gamma_2/Z_2}^{(AB)}}{dE_{\gamma_1} dE_{\gamma_2}} = \int d^2 \mathbf{b}_1 d^2 \mathbf{b}_2 P_{\text{no inel}}(\mathbf{b}_1, \mathbf{b}_2) N_{\gamma_1/Z_1}(E_{\gamma_1}, \mathbf{b}_1) N_{\gamma_2/Z_2}(E_{\gamma_2}, \mathbf{b}_2)$$

■ No hadronic/inelastic interaction probability density:

$$P_{\text{no inel}}(b) = \begin{cases} e^{-\sigma_{\text{inel}}^{\text{NN}} \cdot T_{AB}(b)}, \\ e^{-\sigma_{\text{inel}}^{\text{NN}} \cdot T_A(b)}, \\ |1 - \Gamma(s_{\text{NN}}, b)|^2, \text{ with } \Gamma(s_{\text{NN}}, b) \propto e^{-b^2/(2b_0)} \end{cases}$$

nucleus-nucleus
proton-nucleus
p-p

$T_{AB}(b)$ overlap from
parametrized
Glauber MC:



$\gamma\gamma$ EPA cross sections & p-p survival probability

■ Cross section:

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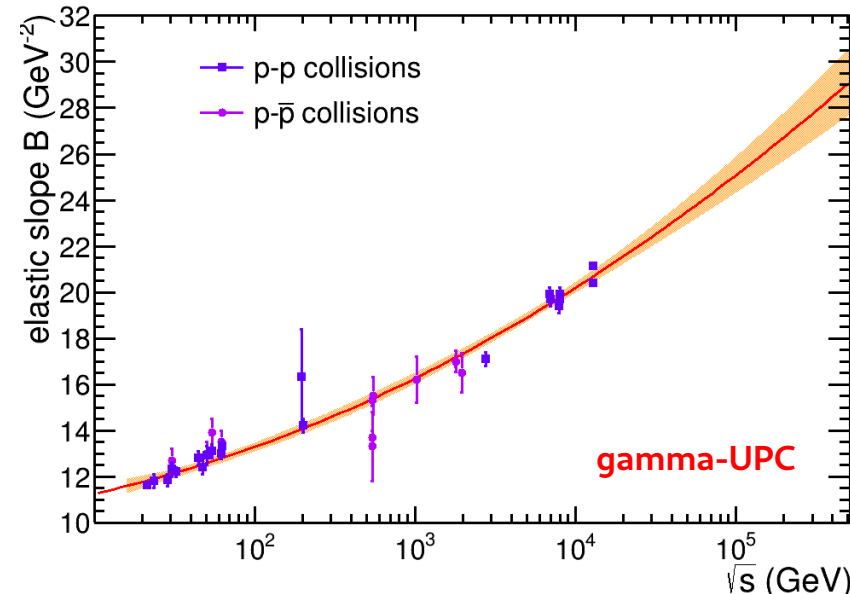
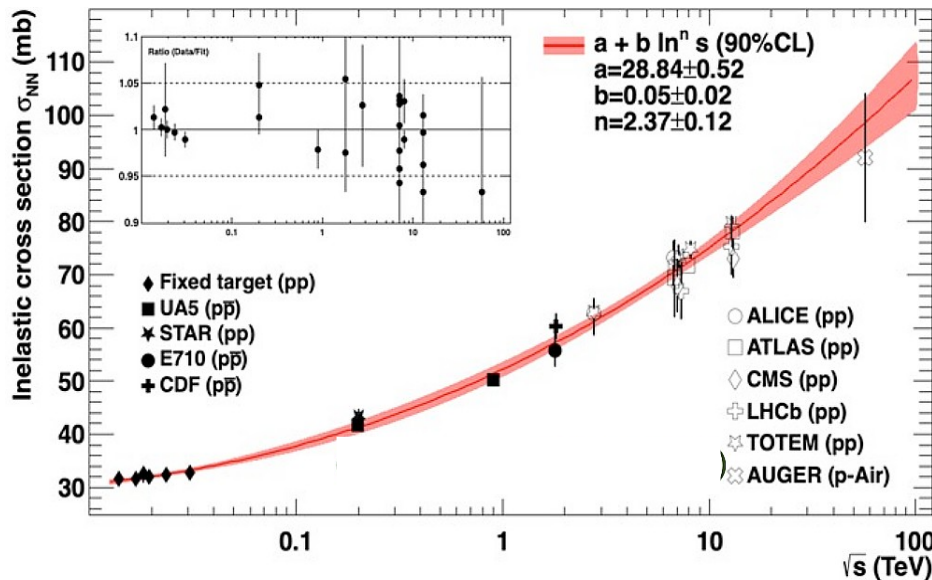
$$P_{\text{no inel}}(b) = \begin{cases} e^{-\sigma_{\text{inel}}^{\text{NN}} \cdot T_{AB}(b)}, & \text{nucleus-nucleus} \\ e^{-\sigma_{\text{inel}}^{\text{NN}} \cdot T_A(b)}, & \text{proton-nucleus} \\ |1 - \Gamma(s_{\text{NN}}, b)|^2, & \text{with } \Gamma(s_{\text{NN}}, b) \propto e^{-b^2/(2b_0)} \end{cases}$$

nucleus-nucleus

proton-nucleus

p-p

Parametrized proton elastic slope data:



How peripheral are Pb-Pb UPCs at the LHC?

■ Average $|\vec{b}_1 - \vec{b}_2|$ vs. $m_{\gamma\gamma}$:

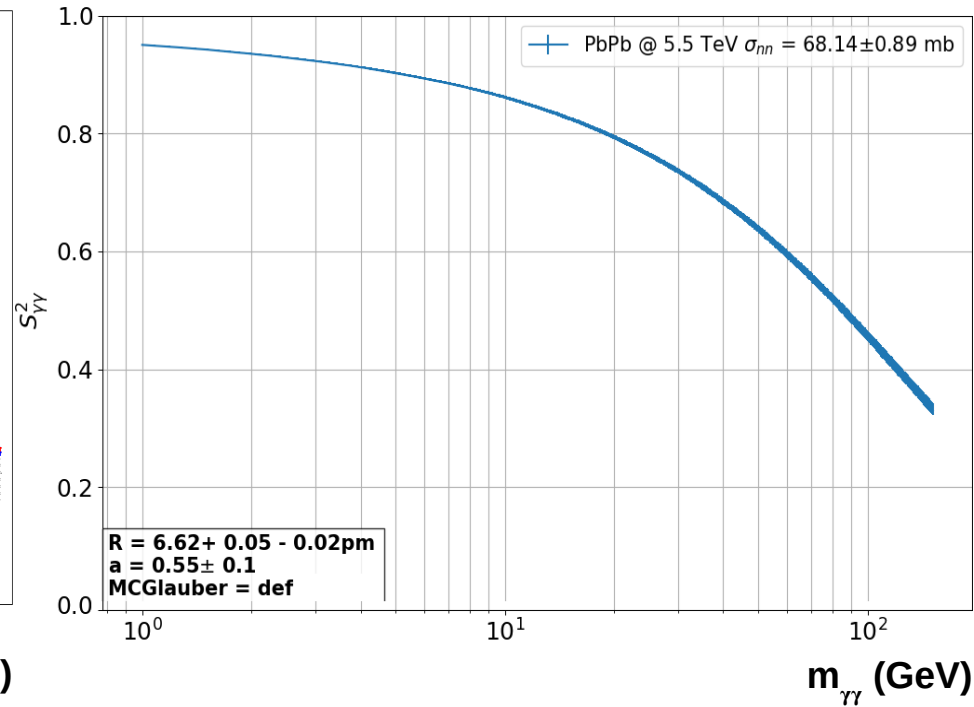
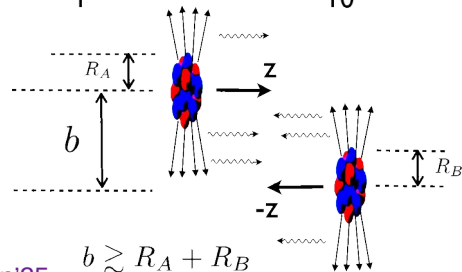
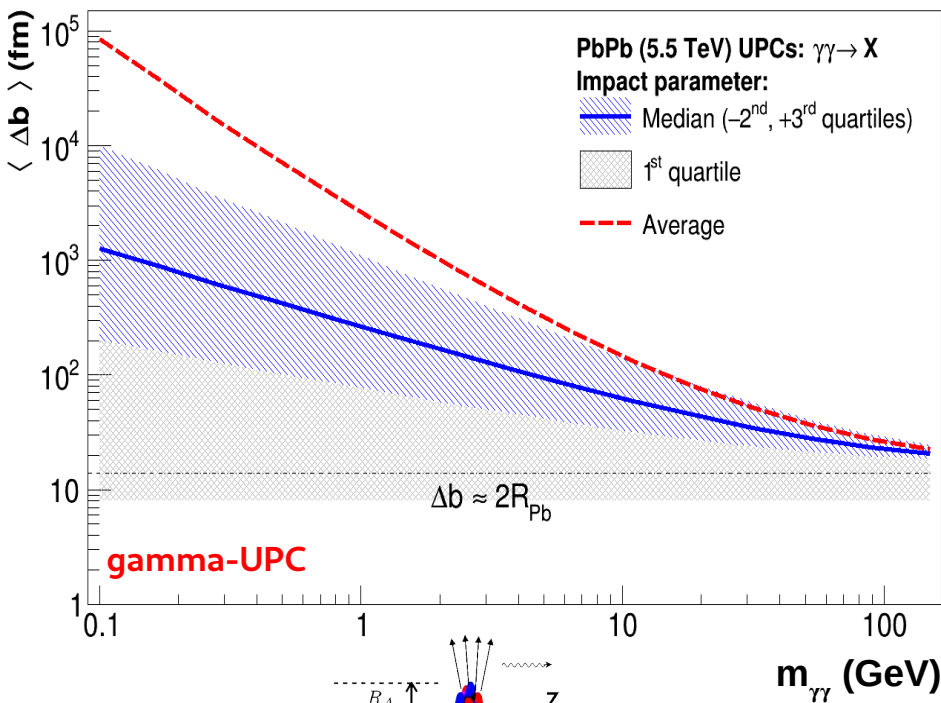
$m_{\gamma\gamma} < 5$ GeV: $\langle \Delta b \rangle > 100$ fm

$m_{\gamma\gamma} > 100$ GeV: $\langle \Delta b \rangle \sim 20$ fm

■ Pb-Pb survival probab. vs. $m_{\gamma\gamma}$:

$m_{\gamma\gamma} < 5$ GeV: $\langle P_{\text{non-overlap}} \rangle > 90\%$

$m_{\gamma\gamma} > 100$ GeV: $\langle P_{\text{non-overlap}} \rangle < 40\%$



$$S_{\gamma\gamma}^2 = \frac{\int d^2\mathbf{b}_1 d^2\mathbf{b}_2 P_{\text{no inel}}(\mathbf{b}_1, \mathbf{b}_2) N_{\gamma_1/Z_1}(E_{\gamma_1}, \mathbf{b}_1) N_{\gamma_2/Z_2}(E_{\gamma_2}, \mathbf{b}_2)}{\int d^2\mathbf{b}_1 d^2\mathbf{b}_2 N_{\gamma_1/Z_1}(E_{\gamma_1}, \mathbf{b}_1) N_{\gamma_2/Z_2}(E_{\gamma_2}, \mathbf{b}_2)}$$

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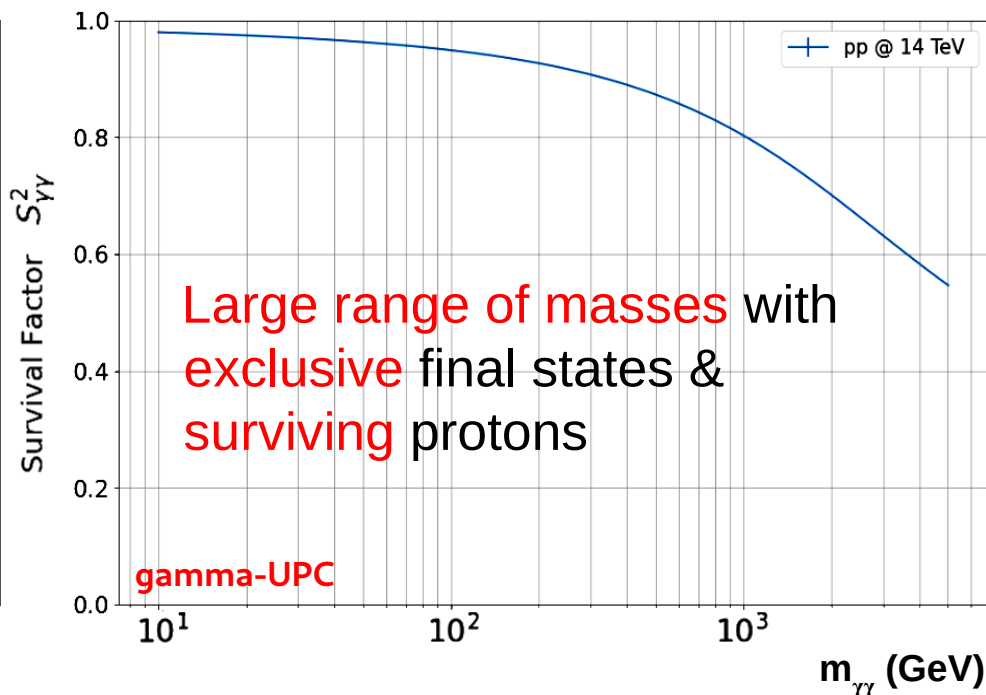
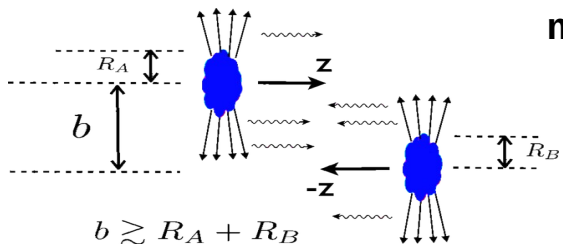
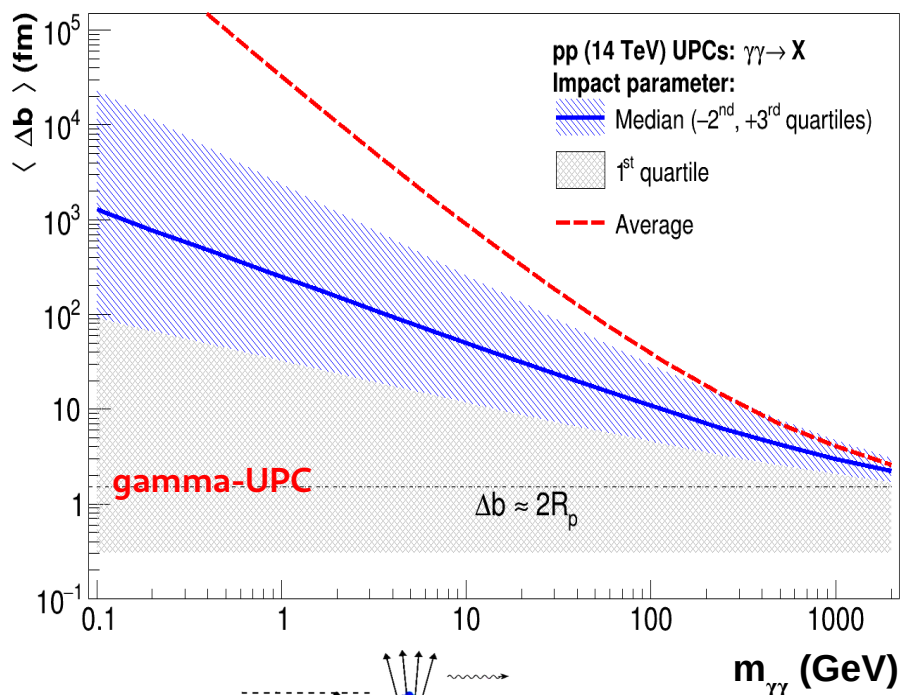
$m_{\gamma\gamma} < 10$ GeV: $\langle \Delta b \rangle > 50$ fm

$m_{\gamma\gamma} > 1$ TeV: $\langle \Delta b \rangle < 3$ fm

■ p-p survival probab. vs. $m_{\gamma\gamma}$:

$m_{\gamma\gamma} < 10$ GeV: $\langle P_{\text{non-overlap}} \rangle > 95\%$

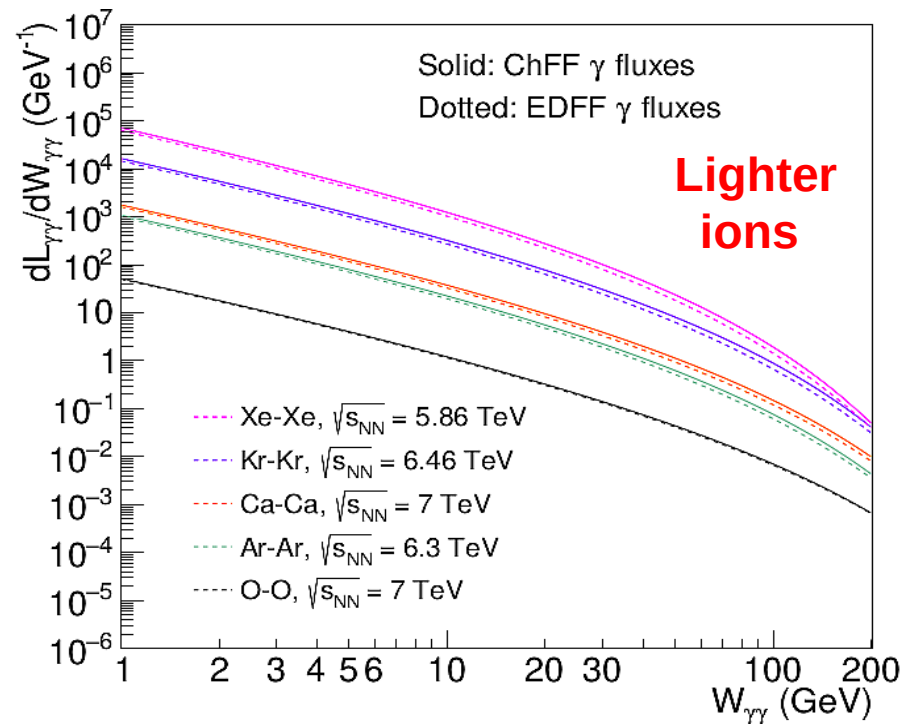
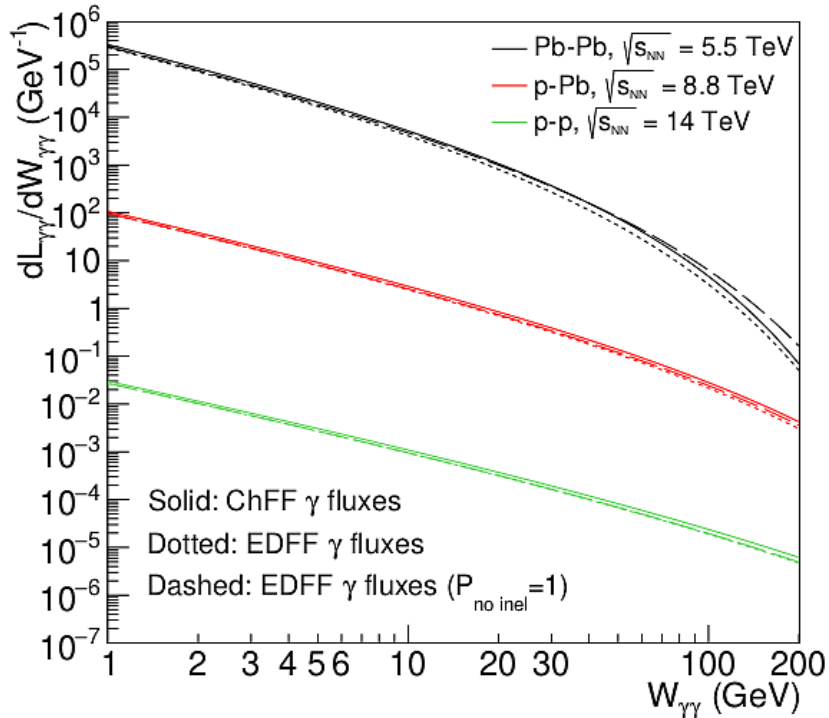
$m_{\gamma\gamma} > 1$ TeV: $\langle P_{\text{non-overlap}} \rangle < 80\%$



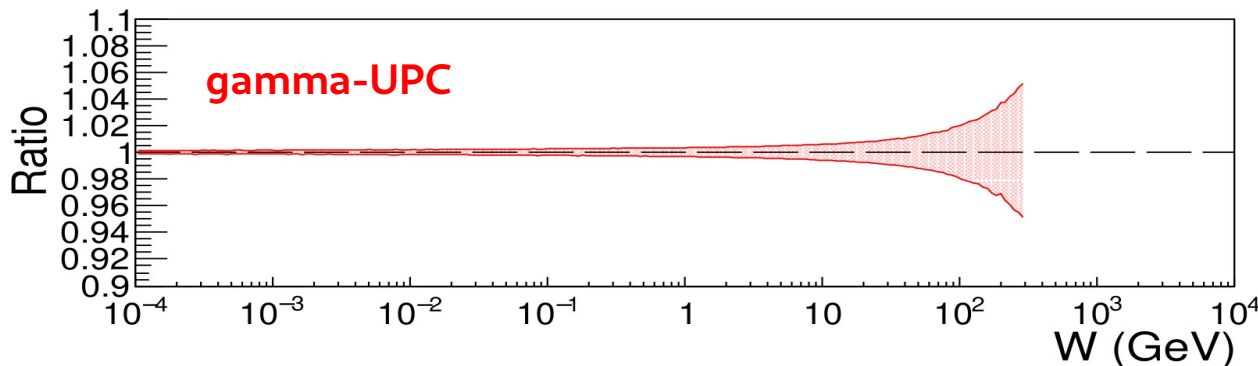
$$S^2_{\gamma\gamma} = \frac{\int d^2\mathbf{b}_1 d^2\mathbf{b}_2 P_{\text{no inel}}(\mathbf{b}_1, \mathbf{b}_2) N_{\gamma_1/Z_1}(E_{\gamma_1}, \mathbf{b}_1) N_{\gamma_2/Z_2}(E_{\gamma_2}, \mathbf{b}_2)}{\int d^2\mathbf{b}_1 d^2\mathbf{b}_2 N_{\gamma_1/Z_1}(E_{\gamma_1}, \mathbf{b}_1) N_{\gamma_2/Z_2}(E_{\gamma_2}, \mathbf{b}_2)}$$

Effective $\gamma\gamma$ luminosities (p-p, p-A, A-A)

■ Thanks to Z^4 boost, **A-A $\gamma\gamma$ lumis (per collision) much above p-p ones:**



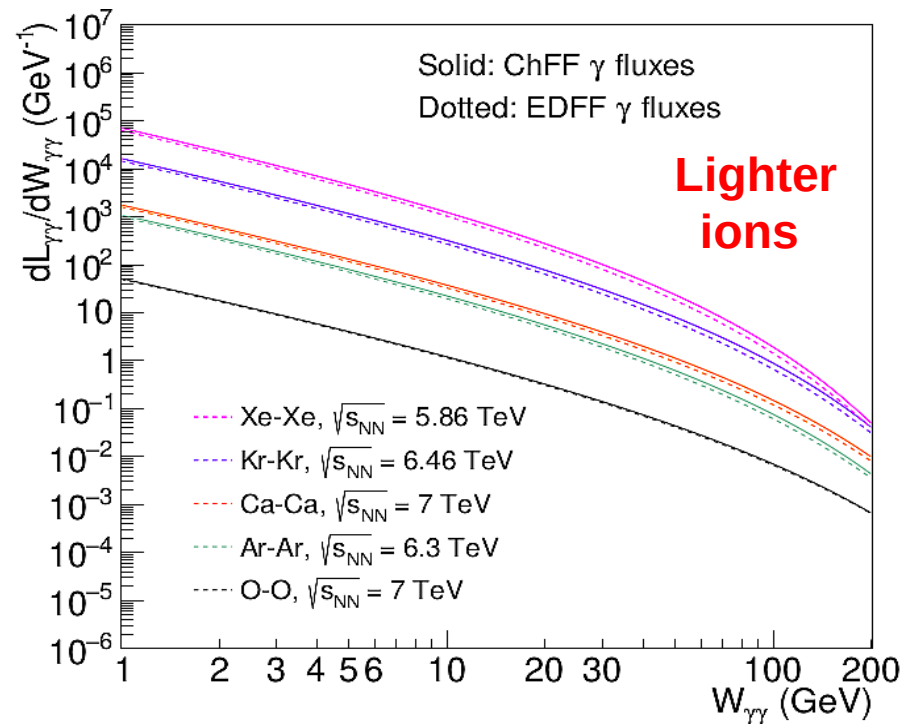
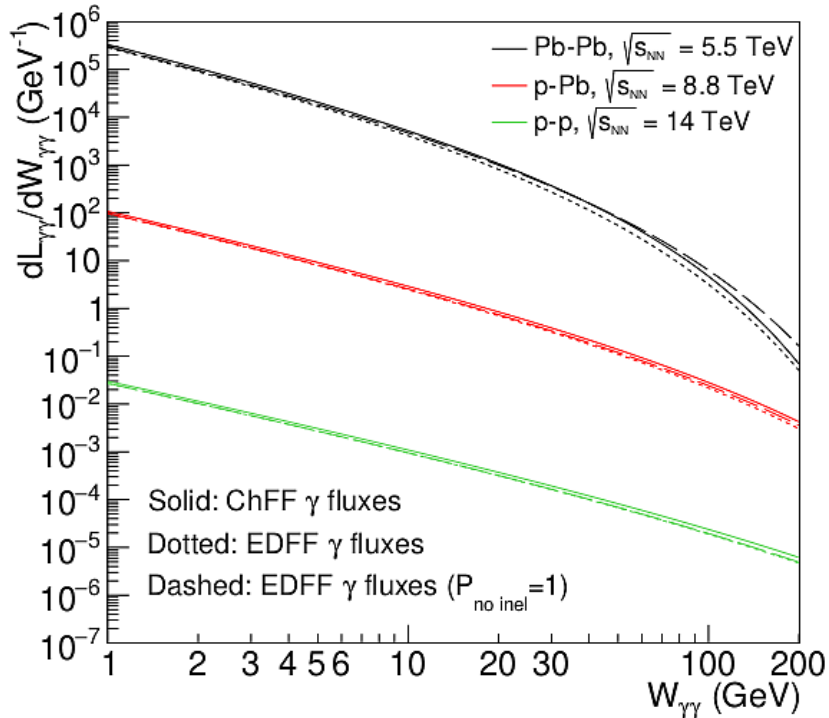
■ ChFF $\gamma\gamma$ luminosity uncertainties (PbPb): **Low-mass: <1%. High mass: ~5%**



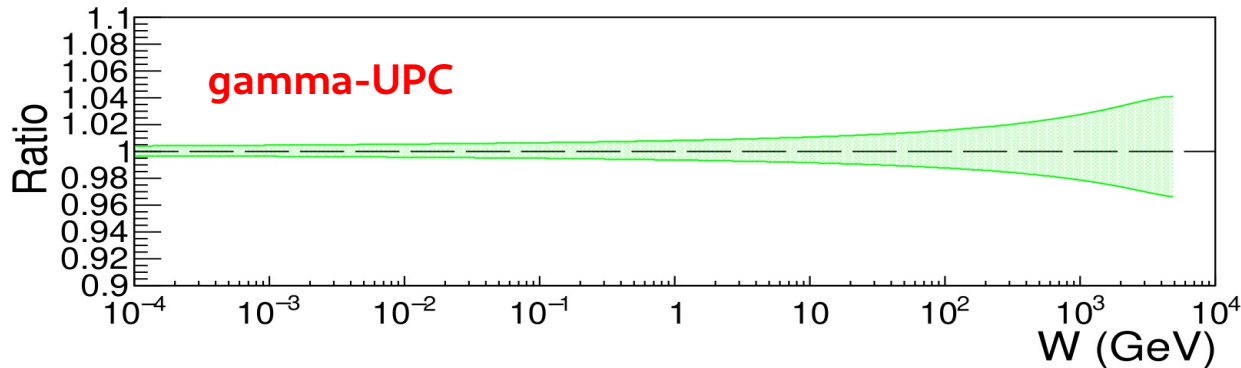
ChFF γ spectra.
 Glauber MC:
Variations of R, a, σ_{NN}

Effective $\gamma\gamma$ luminosities (p-p, p-A, A-A)

■ Thanks to Z^4 boost, **A-A $\gamma\gamma$ lumis (per collision) much above p-p ones:**

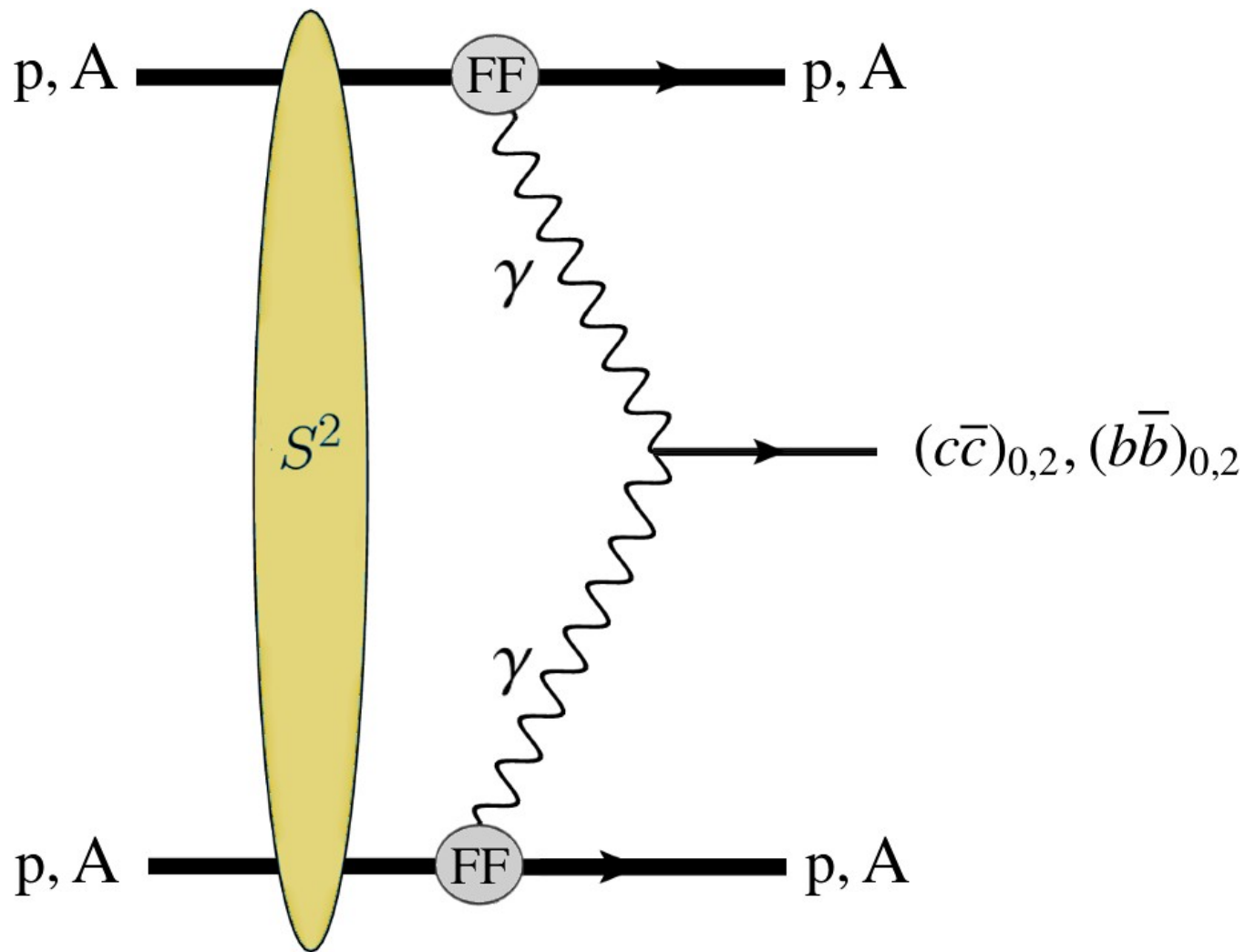


■ ChFF $\gamma\gamma$ luminosity uncertainties (pp): **Low-mass: <1%. High mass: ~4%**



ChFF γ spectra.
Glauber MC:
Variations of b_0

$\gamma\gamma \rightarrow$ even-spin quarkonium production



$\gamma\gamma \rightarrow$ even-spin quarkonium production

- Breit-Wigner cross section for the $\gamma\gamma$ production of resonance X with mass m_X , even-spin J, total width Γ_{tot} , and two-photon width $\Gamma_{\gamma\gamma}$:

$$\hat{\sigma}_{\gamma\gamma \rightarrow X}(\hat{s}_{\gamma\gamma}) = 8\pi^2(2J+1) \frac{\Gamma_{\gamma\gamma}\Gamma_{\text{tot}}}{(\hat{s}_{\gamma\gamma} - m_X^2)^2 + (m_X\Gamma_{\text{tot}})^2} = 4\pi^2(2J+1) \frac{\Gamma_{\gamma\gamma}}{m_X^2} \delta(\hat{s}_{\gamma\gamma} - m_X^2)$$

- "Pocket-formula" x-section in UPCs: $\sigma(\text{AB} \xrightarrow{\gamma\gamma} \text{A X B}) = 4\pi^2(2J+1) \frac{\Gamma_{\gamma\gamma}}{m_X^2} \frac{d\mathcal{L}_{\gamma\gamma}^{(\text{AB})}}{d\hat{s}_{\gamma\gamma}} \Big|_{\hat{s}_{\gamma\gamma}=m_X^2}$
- 8 scalar & tensor $Q\bar{Q}$ states producible in UPCs (not all have measured $\Gamma_{\gamma\gamma}$):

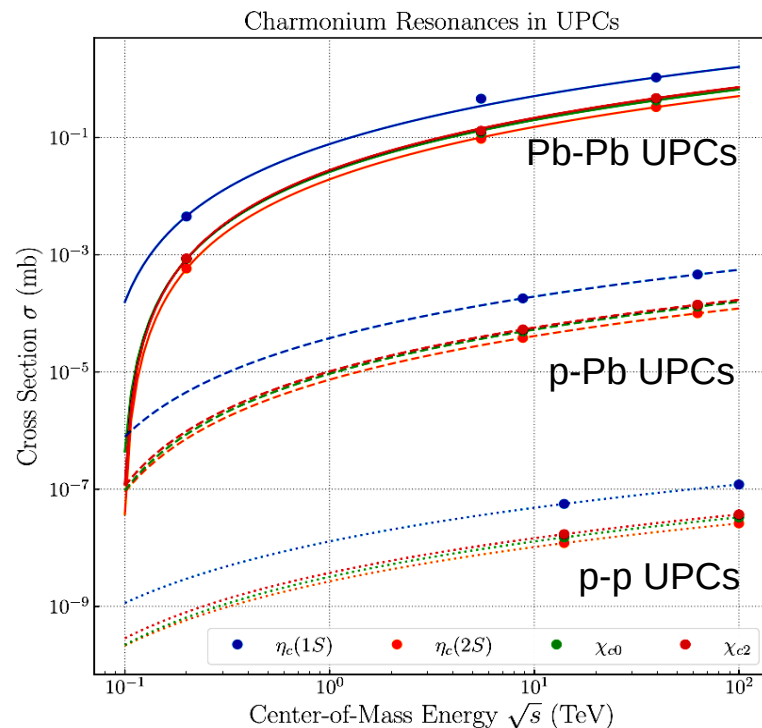
Resonance	J^{PC}	m_X (GeV)	Γ_{tot} (MeV)	$\Gamma_{\gamma\gamma}$ (MeV)	Dominant decay (\mathcal{B})
$\eta_c(1S)$	0^{-+}	2.9841 ± 0.0004	30.5 ± 0.5	$(6.788 \pm 0.061) \cdot 10^{-3}$ (*)	$2(\pi^+\pi^-\pi^0)$ ($15.9 \pm 2.0\%$)
$\eta_c(2S)$	0^{-+}	3.6377 ± 0.0009	11.8 ± 1.6	$(2.12 \pm 1.45) \cdot 10^{-3}$	$K\bar{K}\pi$ ($1.9 \pm 1.2\%$)
χ_{c0}	0^{++}	3.41471 ± 0.00030	10.7 ± 0.6	$(2.1828 \pm 0.16) \cdot 10^{-3}$	$\pi^+\pi^-\pi^0\pi^0$ ($3.3 \pm 0.4\%$)
χ_{c2}	2^{++}	3.55617 ± 0.0007	1.98 ± 0.09	$(5.781 \pm 0.354) \cdot 10^{-4}$	$\gamma J/\psi(1S)$ ($19.0 \pm 0.5\%$)
$\eta_b(1S)$	0^{-+}	9.3987 ± 0.0020	10_{-4}^{+5}	$(5.57 \pm 0.32) \cdot 10^{-4}$ (*)	gg ($\approx 100\%$)
$\eta_b(2S)$	0^{-+}	9.999 ± 0.004	5_{-2}^{+3}	$(2.4_{-1.0}^{+1.2}) \cdot 10^{-4}$ (**)	gg ($\approx 100\%$)
χ_{b0}	0^{++}	9.85944 ± 0.00052	$2.60_{-0.57}^{+0.79}$	$(0.15_{-0.03}^{+0.05}) \cdot 10^{-3}$ (**)	$\Upsilon(2S)\gamma$ ($1.94 \pm 0.27\%$)
χ_{b2}	2^{++}	9.91221 ± 0.00040	$0.180_{-0.057}^{+0.016}$	$(9.3_{-6.2}^{+1.3}) \cdot 10^{-6}$ (**)	$\Upsilon(1S)\gamma$ ($18.0 \pm 1.0\%$)

(*) Lattice QCD (**) NRQCD: $\frac{\Gamma(\Upsilon(1S) \rightarrow e^+e^-)}{\Gamma(\eta_b(1S) \rightarrow \gamma\gamma)} = \frac{1}{3Q_b^2} (1 - 0.302 - 0.115)$

$\gamma\gamma \rightarrow (c\bar{c})_{0,2}$ production in UPCs at the LHC

- Large LHC production rates for all C-even charmonium ($m_X = 2.98\text{--}3.55$ GeV):
 - Cross sections: $100\text{--}500$ μb ($10\text{--}60$ pb) for Pb-Pb (p-p).
 - Yields (mostly soft hadronic decays): $\mathcal{O}(10^6)$ for Pb-Pb, $\mathcal{O}(10^4)$ for p-Pb & p-p UPCs

Colliding system, $\sqrt{s_{NN}}$	$\sigma(\gamma\gamma \rightarrow X)$			
	$\eta_c(1S)$	$\eta_c(2S)$	χ_{c0}	χ_{c2}
Au-Au, 0.2 TeV	5.65 ± 0.05 μb	0.58 ± 0.38 μb	0.85 ± 0.04 μb	0.86 ± 0.03 μb
$N_{\text{evts}}(\mathcal{L}=1 \text{ nb}^{-1})$	5.6×10^4	5.6×10^3	8.5×10^3	8.8×10^3
Pb-Pb, 5.5 TeV	0.62 ± 0.01 mb	96 ± 63 μb	0.12 ± 0.01 mb	0.13 ± 0.01 mb
$N_{\text{evts}}(\mathcal{L}=10 \text{ nb}^{-1})$	6.2×10^6	9.1×10^5	1.2×10^6	1.4×10^6
p-Pb, 8.8 TeV	220 ± 2 nb	35.2 ± 23.0 nb	43.9 ± 2.0 nb	53.0 ± 1.9 nb
$N_{\text{evts}}(\mathcal{L}=1 \text{ pb}^{-1})$	2.2×10^5	3.4×10^4	4.4×10^4	5.0×10^4
p-p, 14 TeV	56.0 ± 4.1 pb	12.0 ± 7.8 pb	15.0 ± 0.7 pb	17.0 ± 0.6 pb
$N_{\text{evts}}(\mathcal{L}=1 \text{ fb}^{-1})$	5.6×10^4	1.2×10^4	1.5×10^4	1.7×10^4

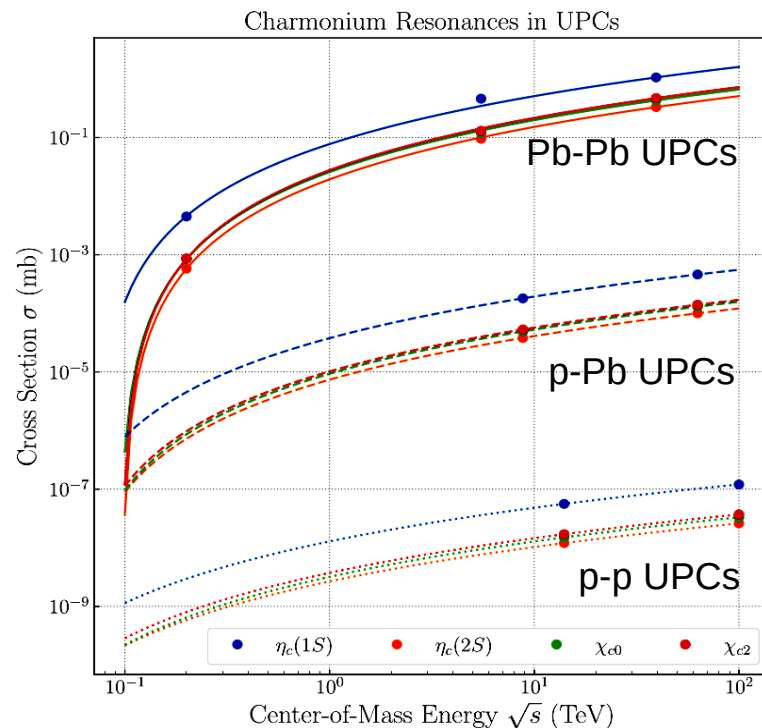


- No existing measurement in UPCs !
- UPC measurements would help solve two issues:
 - Inconsistency between $\Gamma(\eta_c(1S) \rightarrow \gamma\gamma) \approx 11$ keV decay measurement (BES-III) and lattice-QCD result: $\Gamma(\eta_c(1S) \rightarrow \gamma\gamma) \approx 6$ keV.
 - Badly known $\eta_c(2S)$ diphoton width: $\pm 60\%$ uncertainty

$\gamma\gamma \rightarrow (c\bar{c})_{0,2}$ production in UPCs at the LHC

- Large LHC production rates for all C-even charmonium ($m_X = 2.98\text{--}3.55$ GeV):
 - Cross sections: 100–500 μb (10–60 pb) for Pb-Pb (p-p).
 - Yields (mostly soft hadronic decays): $\mathcal{O}(10^6)$ for Pb-Pb, $\mathcal{O}(10^4)$ for p-Pb & p-p UPCs

Colliding system, $\sqrt{s_{NN}}$	$\sigma(\gamma\gamma \rightarrow X)$			
	$\eta_c(1S)$	$\eta_c(2S)$	χ_{c0}	χ_{c2}
Au-Au, 0.2 TeV	$5.65 \pm 0.05 \mu\text{b}$	$0.58 \pm 0.38 \mu\text{b}$	$0.85 \pm 0.04 \mu\text{b}$	$0.86 \pm 0.03 \mu\text{b}$
$N_{\text{evts}}(\mathcal{L}=1 \text{ nb}^{-1})$	5.6×10^4	5.6×10^3	8.5×10^3	8.8×10^3
Pb-Pb, 5.5 TeV	$0.62 \pm 0.01 \text{ mb}$	$96 \pm 63 \mu\text{b}$	$0.12 \pm 0.01 \text{ mb}$	$0.13 \pm 0.01 \text{ mb}$
$N_{\text{evts}}(\mathcal{L}=10 \text{ nb}^{-1})$	6.2×10^6	9.1×10^5	1.2×10^6	1.4×10^6
p-Pb, 8.8 TeV	$220 \pm 2 \text{ nb}$	$35.2 \pm 23.0 \text{ nb}$	$43.9 \pm 2.0 \text{ nb}$	$53.0 \pm 1.9 \text{ nb}$
$N_{\text{evts}}(\mathcal{L}=1 \text{ pb}^{-1})$	2.2×10^5	3.4×10^4	4.4×10^4	5.0×10^4
p-p, 14 TeV	$56.0 \pm 4.1 \text{ pb}$	$12.0 \pm 7.8 \text{ pb}$	$15.0 \pm 0.7 \text{ pb}$	$17.0 \pm 0.6 \text{ pb}$
$N_{\text{evts}}(\mathcal{L}=1 \text{ fb}^{-1})$	5.6×10^4	1.2×10^4	1.5×10^4	1.7×10^4



- Measurable in PbPb, pPb, pp w/o pileup with low- p_T charged particle & photon PID/reco (ALICE, LHCb).

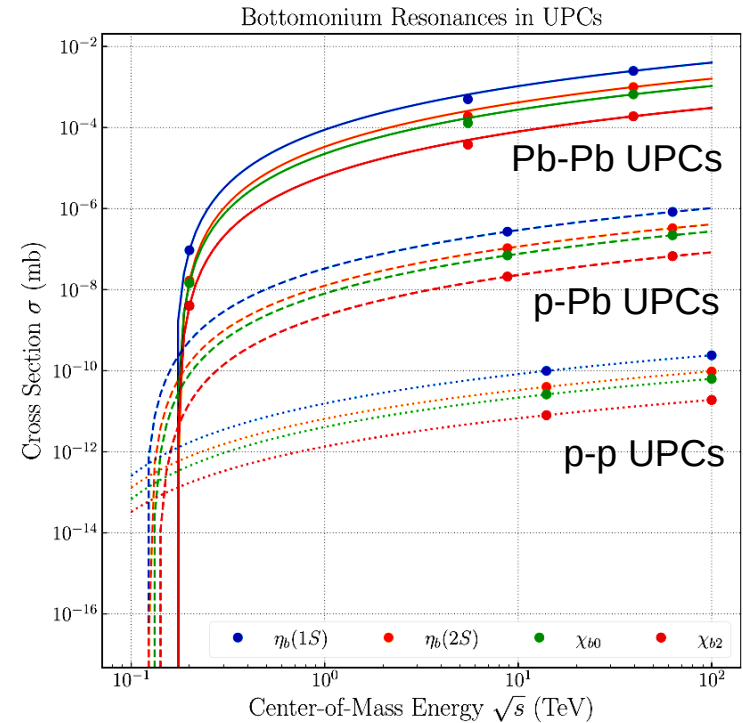
- Badly known $\eta_c(1S)$, $\eta_c(2S)$ diphoton widths can be extracted from the measured UPC x-section & known $\gamma\gamma$ luminosity:

$$\Gamma_{X \rightarrow \gamma\gamma} = \frac{\sigma(\text{AB} \xrightarrow{\gamma\gamma} \text{A X B})}{4\pi^2(2J+1)} m_X^2 \left[\frac{d\mathcal{L}_{\gamma\gamma}^{(\text{AB})}}{d\hat{s}_{\gamma\gamma}} \Big|_{\hat{s}_{\gamma\gamma}=m_X} \right]^{-1}$$

$\gamma\gamma \rightarrow (b\bar{b})_{0,2}$ production in UPCs at the LHC

- All **C-even bottomonium mesons** ($m_X = 9.4\text{--}9.99$ GeV) are producible at the LHC:
 - Cross sections: **40–500 nb (10–100 fb)** for Pb-Pb (p-p).
 - Yields (mostly soft hadronic decays): $\mathcal{O}(1000)$ for Pb-Pb, $\mathcal{O}(10\text{--}100)$ for p-Pb & p-p

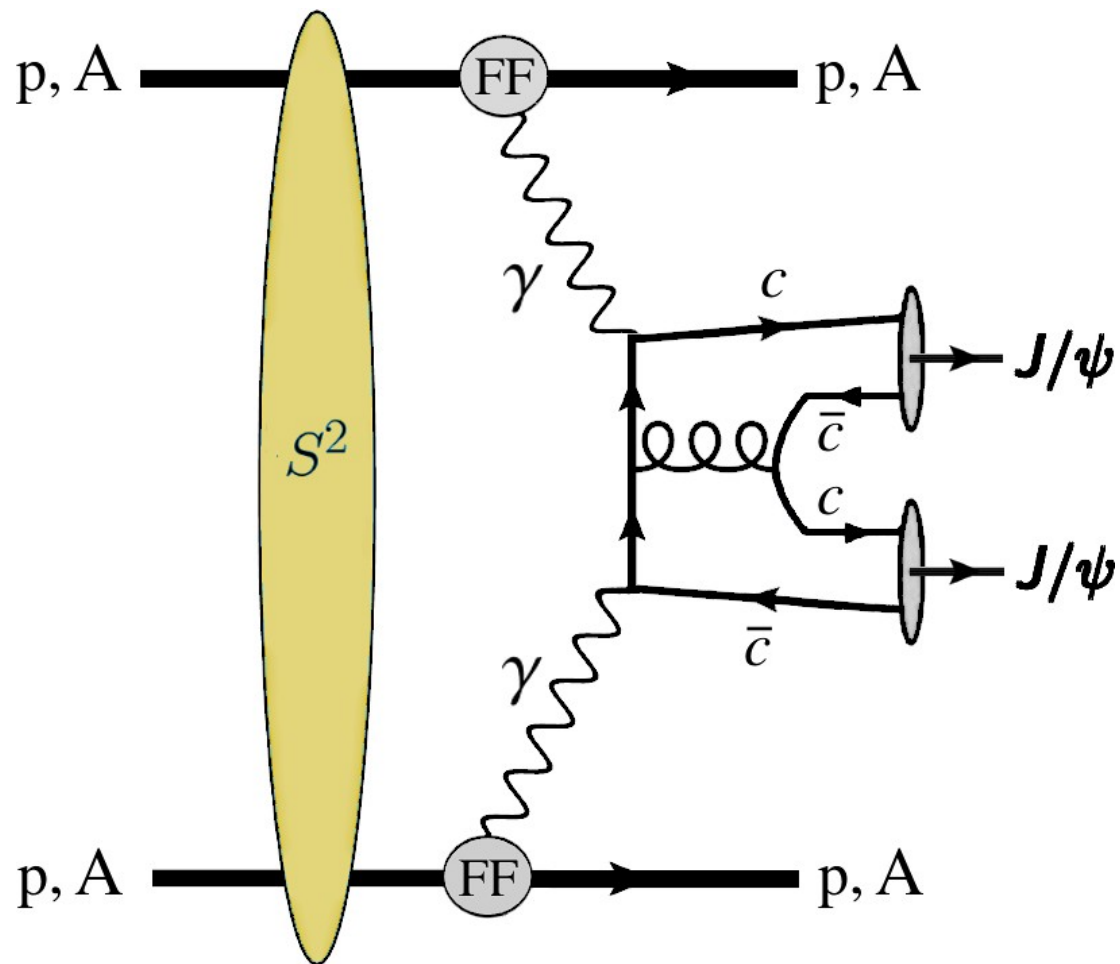
Colliding system, $\sqrt{s_{NN}}$	$\sigma(\gamma\gamma \rightarrow X)$			
	$\eta_b(1S)$	$\eta_b(2S)$	χ_{b0}	χ_{b2}
Au-Au, 0.2 TeV	0.11 ± 0.01 nb	$16.8^{+8.4}_{-7.0}$ pb	$14.5^{+4.8}_{-2.9}$ pb	$4.0^{+0.6}_{-2.7}$ pb
$N_{\text{evts}}(\mathcal{L}=1 \text{ nb}^{-1})$	1	0.1	0.15	0.04
Pb-Pb, 5.5 TeV	0.57 ± 0.03 μb	$0.19^{+0.10}_{-0.08}$ μb	$0.13^{+0.04}_{-0.03}$ μb	38^{+5}_{-25} nb
$N_{\text{evts}}(\mathcal{L}=10 \text{ nb}^{-1})$	5700	1900	1300	380
p-Pb, 8.8 TeV	0.27 ± 0.02 nb	106^{+53}_{-44} pb	70^{+23}_{-14} pb	21^{+3}_{-14} pb
$N_{\text{evts}}(\mathcal{L}=1 \text{ pb}^{-1})$	270	100	70	20
p-p, 14 TeV	99^{+56}_{-41} fb	40^{+20}_{-16} fb	26^{+8}_{-5} fb	$8.0^{+1.1}_{-5.3}$ fb
$N_{\text{evts}}(\mathcal{L}=1 \text{ fb}^{-1})$	100	40	26	8



- **No existing measurement** in UPCs.
- Potentially measurable in PbPb with **charged particle & γ PID/reco** (all LHC exps.)

- **Unknown diphoton widths measurable:** $\Gamma_{X \rightarrow \gamma\gamma} = \frac{\sigma(AB \xrightarrow{\gamma\gamma} A X B)}{4\pi^2(2J+1)} m_X^2 \left[\frac{d\mathcal{L}_{\gamma\gamma}^{(AB)}}{d\hat{s}_{\gamma\gamma}} \Big|_{\hat{s}_{\gamma\gamma}=m_X} \right]^{-1}$

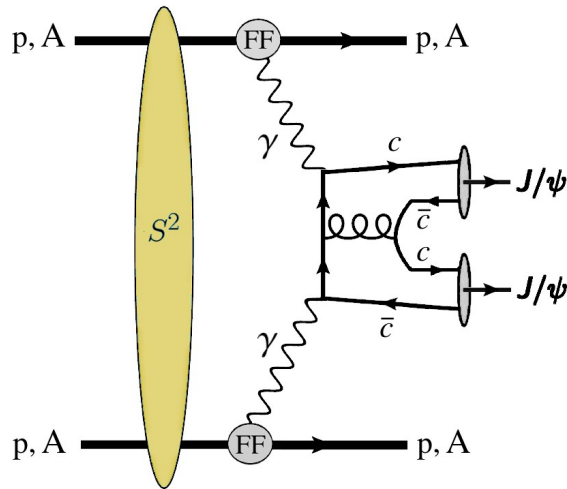
$\gamma\gamma \rightarrow$ double-quarkonium production



$\gamma\gamma \rightarrow$ double-quarkonium production

- Process computed with **gamma-UPC+HelacOnia** at LO accuracy:

$$\sigma \propto q_Q^4 \cdot \alpha^2 \cdot \alpha_s(m_{QQ})^2 \cdot |R(0)|^4 \cdot d\mathcal{L}_{\gamma\gamma}/dm|_{m=2m} \cdot [2m_{QQ}]^{-4}$$



Process: $\gamma\gamma \rightarrow J/\psi J/\psi$ Colliding system, c.m. energy	gamma-UPC	
	σ	N_{evts}
p-p at 14 TeV ($\mathcal{L}=1 \text{ fb}^{-1}$)	23_{-7}^{+13} fb	20
p-Pb at 8.8 TeV ($\mathcal{L}=1 \text{ pb}^{-1}$)	$64_{-18}^{+35} \text{ pb}$	60
Pb-Pb at 5.52 TeV ($\mathcal{L}=10 \text{ nb}^{-1}$)	$128_{-36}^{+71} \text{ nb}$	1300

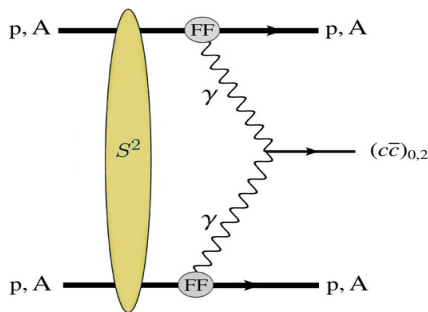
Dominant theoretical uncertainties: +50%, -20%
(varying renormalization scale within $\times 2$)

- Double- J/ψ has relative low x-sections in UPCs:
 - Cross sections: **100 nb for Pb-Pb, 60 pb for p-Pb, and 20 fb for p-p.**
 - Yields: **~15 exclusive 4-lepton ($4\mu, 4e, 2\mu 2e$) events expected in PbPb UPCs**
- Double- η_c is of the same order (given same $|R(0)|^2$), but **double- Υ & double- η_b** rates are **negligible**: (much) smaller q_Q^4 , $\alpha_s(m_{QQ})^2$, $\mathcal{L}_{\gamma\gamma}$, m_{QQ}^{-4} factors
- Note **$\gamma\gamma \rightarrow J/\psi + \gamma$, $\Upsilon + \gamma$ also calculable** with gamma-UPC+HelacOnia.

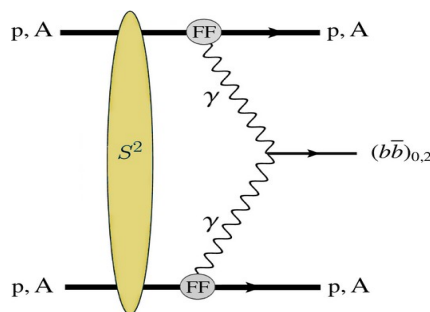
Exclusive quarkonia in $\gamma\gamma$ collisions: Summary

- LHC is a **unique $\gamma\gamma$ collider** thanks to PbPb, pPb, pp UPCs. Any photon-coupled object is producible with masses $m_{\gamma\gamma} < 0.16, 2.5, 4.5$ TeV, respectively.
- **gamma-UPC** (+MG5, +HelacOnia) is available to compute x-sections & generate UPC events for any colliding system & final state:
 - Two different γ fluxes (but **ChFF** preferred).
 - Realistic hadron survival probabilities with **few % parametric** uncertainties.
 - **NLO** QED and/or QCD corrections implementable.
- **Quarkonia** states can be produced **singly (even spin) or in pairs (spin-1)**:

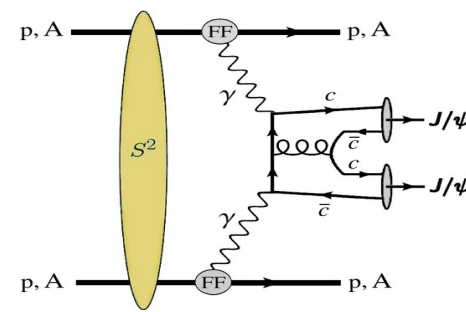
Spin-0,2 **charmonia**:



Spin-0,2 **bottomonia**:



Double-J/psi:



- Large yields: $\mathcal{O}(10^6)$ for Pb-Pb
- (Soft) hadron decays measurable in ALICE/LHCb.
- Improve badly known $\eta_c(1S,2S)$ **diphoton widths**

- Moderate yields: $\mathcal{O}(1000)$ for Pb-Pb
- Decays measurable by all LHC expts.
- Measure all unknown **diphoton widths**

$$\Gamma_{X \rightarrow \gamma\gamma} = \frac{\sigma(AB \xrightarrow{\gamma\gamma} A X B)}{4\pi^2(2J+1)} m_X^2 \left[\frac{d\mathcal{L}_{\gamma\gamma}^{(AB)}}{d\hat{s}_{\gamma\gamma}} \Big|_{\hat{s}_{\gamma\gamma}=m_X} \right]^{-1}$$

~15 exclusive 4-lepton events expected in PbPb

- All these processes are interesting & measurable at the LHC!

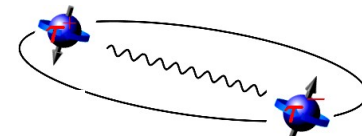
Backup slides

Para-ditauonium via $\gamma\gamma \rightarrow \tau_0 \rightarrow \gamma\gamma$?

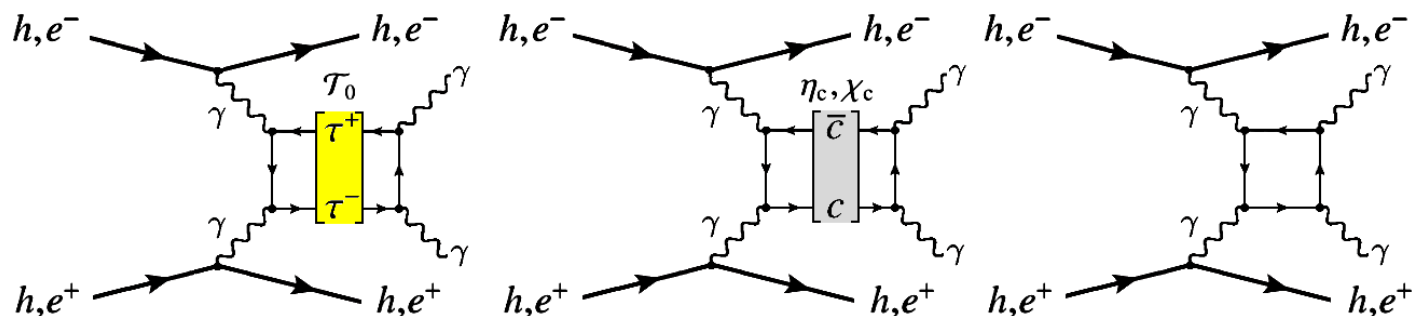
- Ditauonium $\tau \equiv (\tau^+\tau^-)$, never observed, is **smallest & most-bound leptonium** state:

Mass: $m_\tau = 2m_\tau + E_{\text{bind}} = 3553.6962 \pm 0.2400 \text{ MeV}$, $E_{\text{bind}} = -\alpha^2 m_\tau / (4n^2) = -23.7 \text{ keV}$

Bohr radius: $a_0 = 2/(\alpha m_\tau) = 30.4 \text{ fm}$ ($\times 3500$ smaller than positronium)



- Signal & background x-sections: $\sigma(ab \rightarrow ab + X) = 4\pi^2(2J + 1) \frac{\Gamma_{\gamma\gamma}(X)}{m_X^2} \left. \frac{d\mathcal{L}_{\gamma\gamma}^{(ab)}}{dW_{\gamma\gamma}} \right|_{W_{\gamma\gamma}=m_X}$



[DdE, H-S. Shao, PRD105 (2022)093008]

Colliding system, c.m. energy, \mathcal{L}_{int} , exp.	$\sigma \times \mathcal{B}_{\gamma\gamma}$					$N \times \mathcal{B}_{\gamma\gamma}$		
	$\eta_c(1S)$	$\eta_c(2S)$	$\chi_{c,0}(1P)$	$\chi_{c,2}(1P)$	LbL	\mathcal{T}_0	\mathcal{T}_0	$\chi_{c,2}(1P)$
e^+e^- at 3.78 GeV, 20 fb^{-1} , BES III	120 fb	3.6 ab	15 ab	13 ab	30 ab	0.25 ab	–	–
e^+e^- at 10.6 GeV, 50 ab^{-1} , Belle II	1.7 fb	0.35 fb	0.52 fb	0.77 fb	1.7 fb	0.015 fb	750	38 500
e^+e^- at 91.2 GeV, 50 ab^{-1} , FCC-ee	11 fb	2.8 fb	3.9 fb	6.0 fb	12 fb	0.11 fb	5 600	$3 \cdot 10^5$
p-p at 14 TeV, 300 fb^{-1} , LHC	7.9 fb	2.0 fb	2.8 fb	4.3 fb	6.3 fb	0.08 fb	24	1290
p-Pb at 8.8 TeV, 0.6 pb^{-1} , LHC	25 pb	6.3 pb	8.7 pb	13 pb	21 pb	0.25 pb	0.15	8
Pb-Pb at 5.5 TeV, 2 nb^{-1} , LHC	61 nb	15 nb	21 nb	31 nb	62 nb	0.59 nb	1.2	62

Largest x-sections (**0.6 nb**) in **PbPb UPC** but only ~ 1 evt expected. Visible at e^+e^-