

Neutrino Oscillation Analysis with Combined Data from Super-Kamiokande and T2K



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NuFACT Satellite Workshop

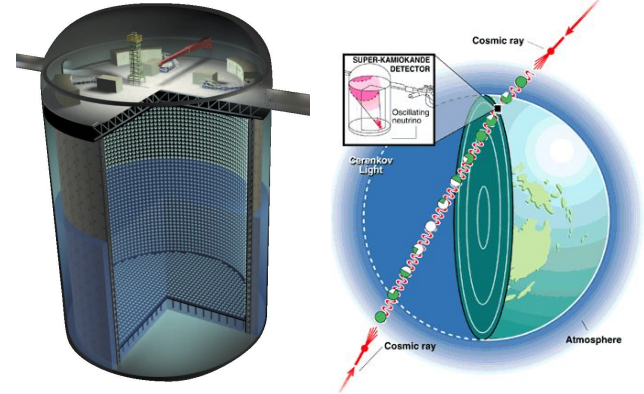
15th September 2024



Experiments

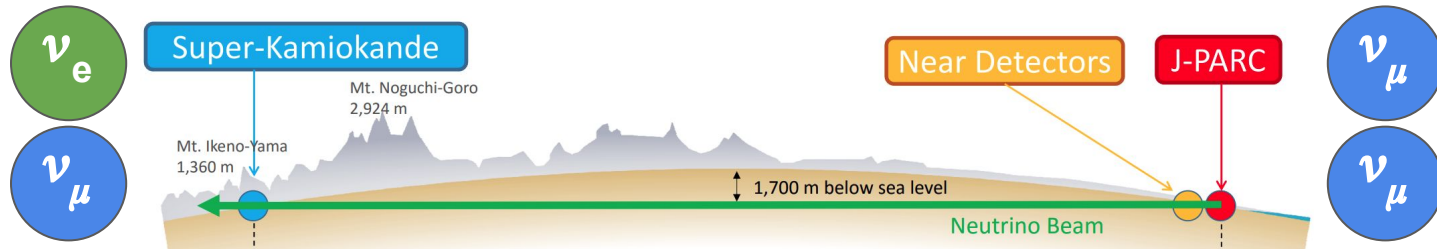
Super-Kamiokande (SK): 50 kton water Cherenkov detector:

- Measure atmospheric neutrinos with large neutrino energy and baseline range
- Good separation of electrons and muons
- No event-by-event neutrino/antineutrino separation

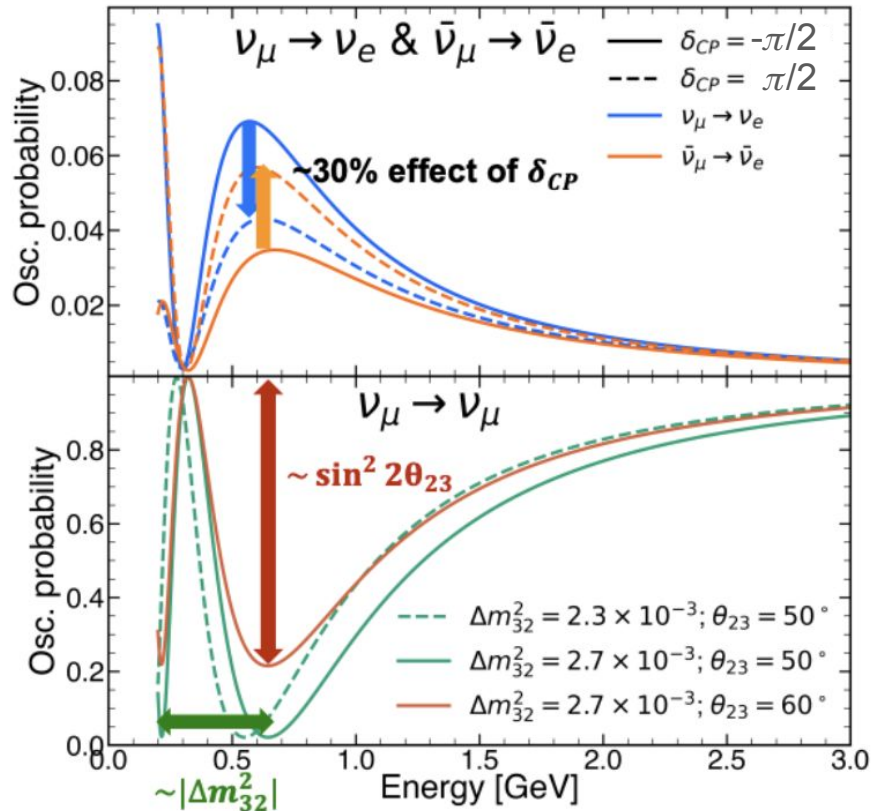


Tokai-to-Kamioka (T2K): Long baseline ($L=295\text{km}$) beam oscillation experiment:

- Primary $\nu_\mu / \bar{\nu}_\mu$ beam peaked at $E_\nu = 0.6 \text{ GeV}/c$
- Near detectors used to constrain flux and cross-section uncertainties
- Far detector oscillated measurement uses SK



Oscillations in T2K



Oscillation probability for T2K:

- Baseline, $L = 295\text{km}$
- Flux peak at 0.6GeV

Disappearance probability ($\nu_\mu \rightarrow \nu_\mu$):

- $\sin^2 2\theta_{23}$ modulates **amplitude**
- **Frequency** of oscillation $\sim |\Delta m_{23}^2|$

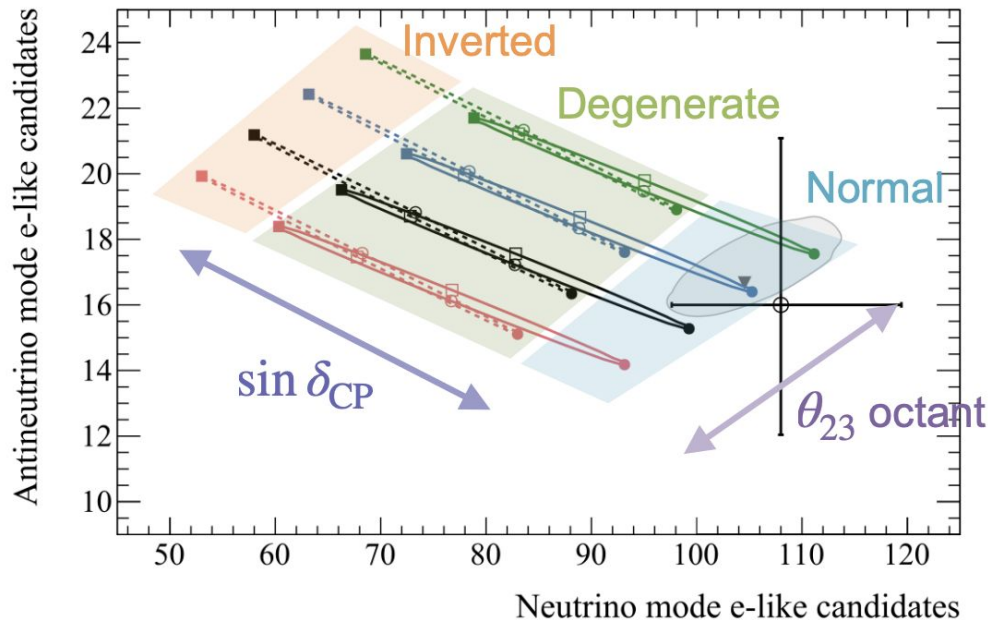
δ_{CP} modifies **neutrino/antineutrino** appearance ($\nu_\mu \rightarrow \nu_e$) probability:

- Circular modulation over 2π period
- Asymmetric effect

Oscillations in T2K

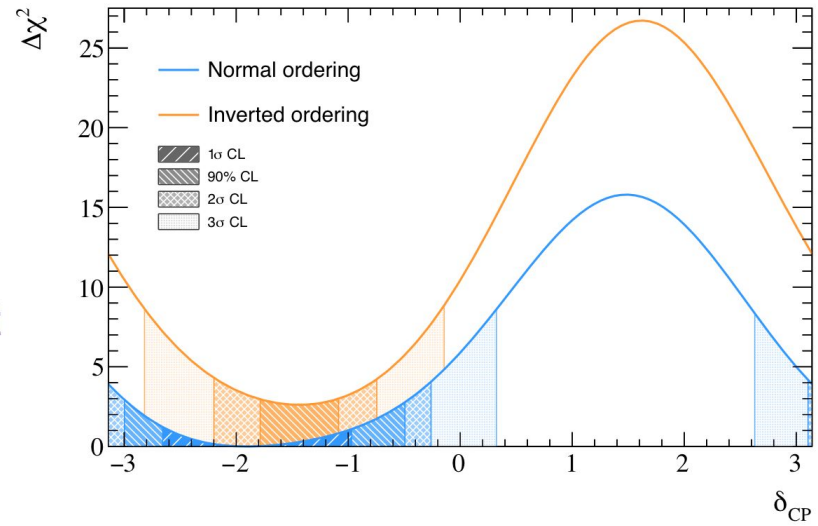
Appearance $\nu_\mu(\bar{\nu}_\mu) \rightarrow \nu_e(\bar{\nu}_e)$

- 68% syst err. at best-fit
- Best-fit
- Data (68% stat err.)
- $\sin^2\theta_{23} = 0.45, 0.50, 0.55, 0.60$
- $\Delta m_{32}^2 = 2.49 \times 10^{-3} \text{ eV}^2 \text{ (NO)}$
- $\Delta m_{31}^2 = -2.46 \times 10^{-3} \text{ eV}^2 \text{ (IO)}$
- $\delta_{\text{CP}} = \pi$
- $\delta_{\text{CP}} = +\pi/2$
- $\delta_{\text{CP}} = 0$
- $\delta_{\text{CP}} = -\pi/2$



Large degenerate region in mass hierarchy (MH) and δ_{CP} :

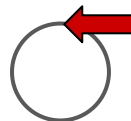
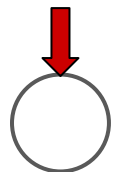
- T2K-only data prefers \sim maximal CP violation



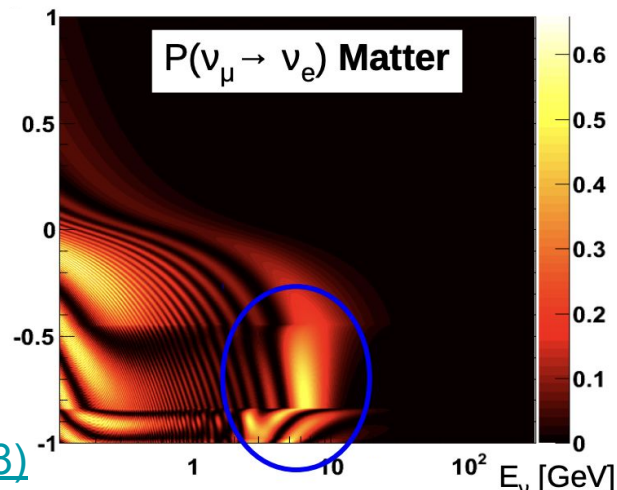
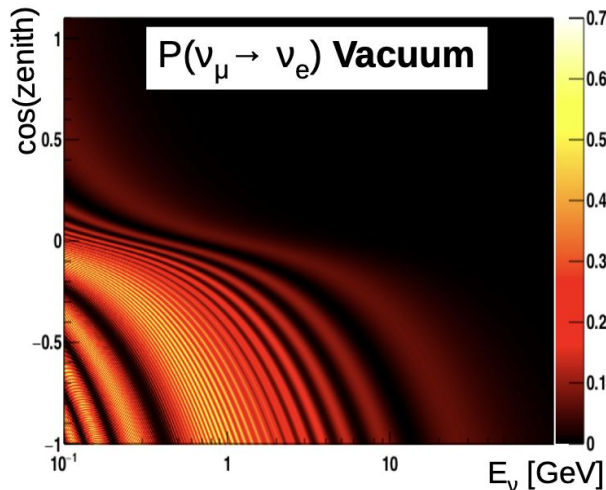
Atmospheric Oscillations in SK

SK has discriminating power of mass ordering due to resonant-induced matter effects between 2 and 10 GeV in upgoing-neutrinos [$\cos(\text{zenith}) < 0$]:

- Enhancement of ν in NO; enhancement of $\bar{\nu}$ in IO
- Amplitude of effect depends on $\sin^2\theta_{23} \rightarrow$ sensitive to θ_{23} octant



Atmospheric neutrino oscillation probability (normal ordering)

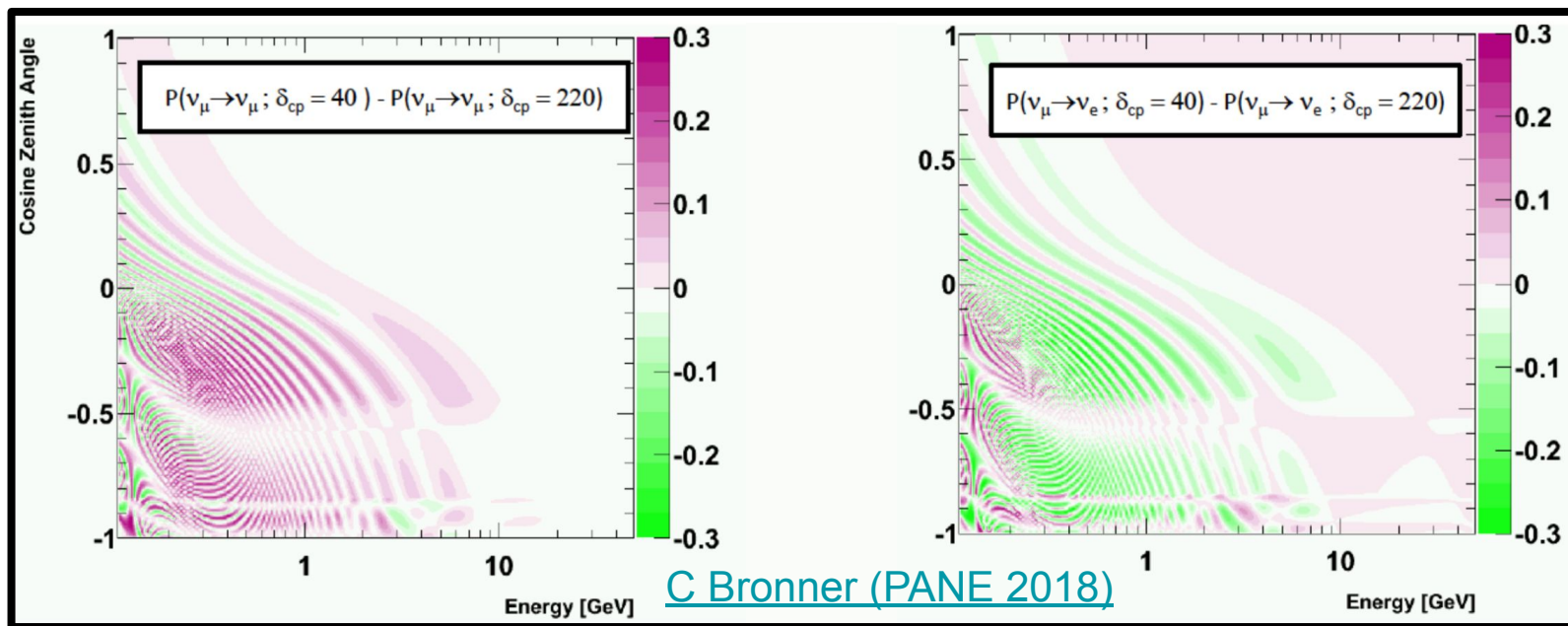


[C Bronner \(PANE 2018\)](#)

Atmospheric Oscillations in SK

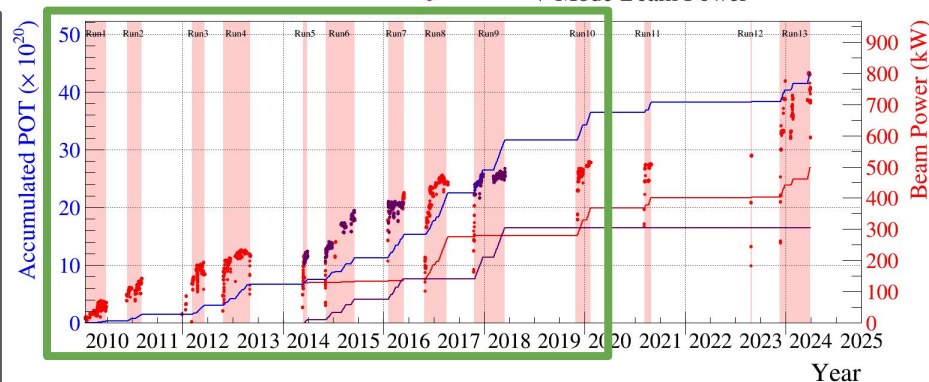
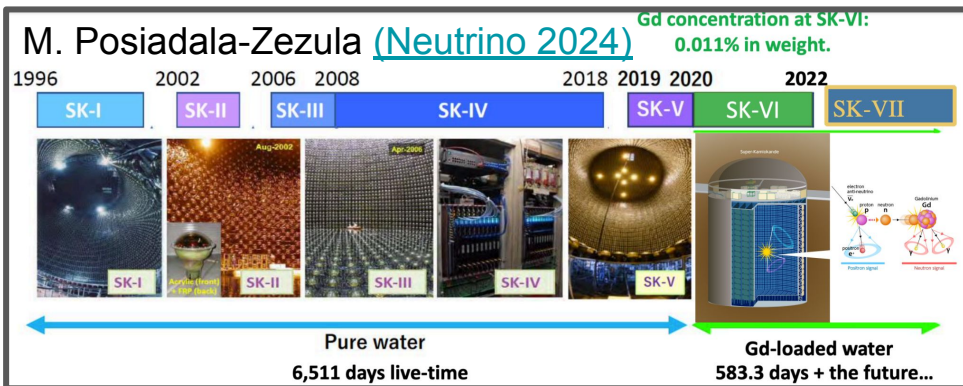
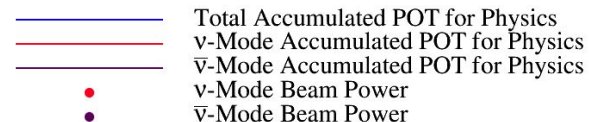
SK has limited sensitivity to δ_{CP} through the normalisation of sub-GeV e-like events:

- Overall normalisation due to detector energy and angular resolution
- More ν_e events at $\delta_{\text{CP}} \sim 220^\circ$, fewer at $\delta_{\text{CP}} \sim 40^\circ$



Two joint analyses released in 2023:

- T2K (beam) + NOvA (beam) → See the previous talks
- T2K (beam) + SK (atmospherics) → [Arxiv 2405.12488](#)
 - T2K data (5 samples) POT: 3.6×10^{21} - [Eur. Phys. J. C 83, 782](#)
 - SK-IV data (18 samples) 3244 days - [PTEP 2019 5, 054F01](#)



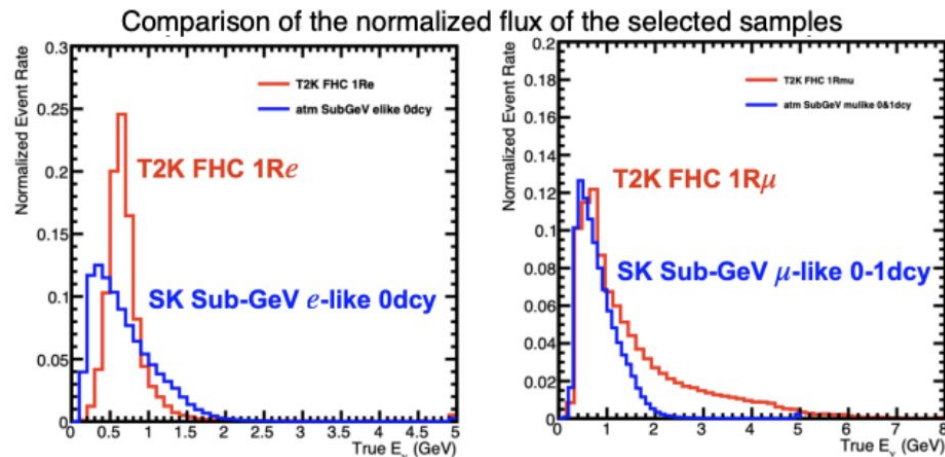
Motivation of T2K+SK Joint Analysis



Combining experiments should provide us with:

- Better sensitivity to oscillation parameters and mass ordering due to increased stats
- SK helps **break degeneracy** between δ_{CP} and **mass ordering** in T2K
- T2K can constrain $\sin^2\theta_{23}$ better \rightarrow improve sensitivity to **mass ordering** in SK

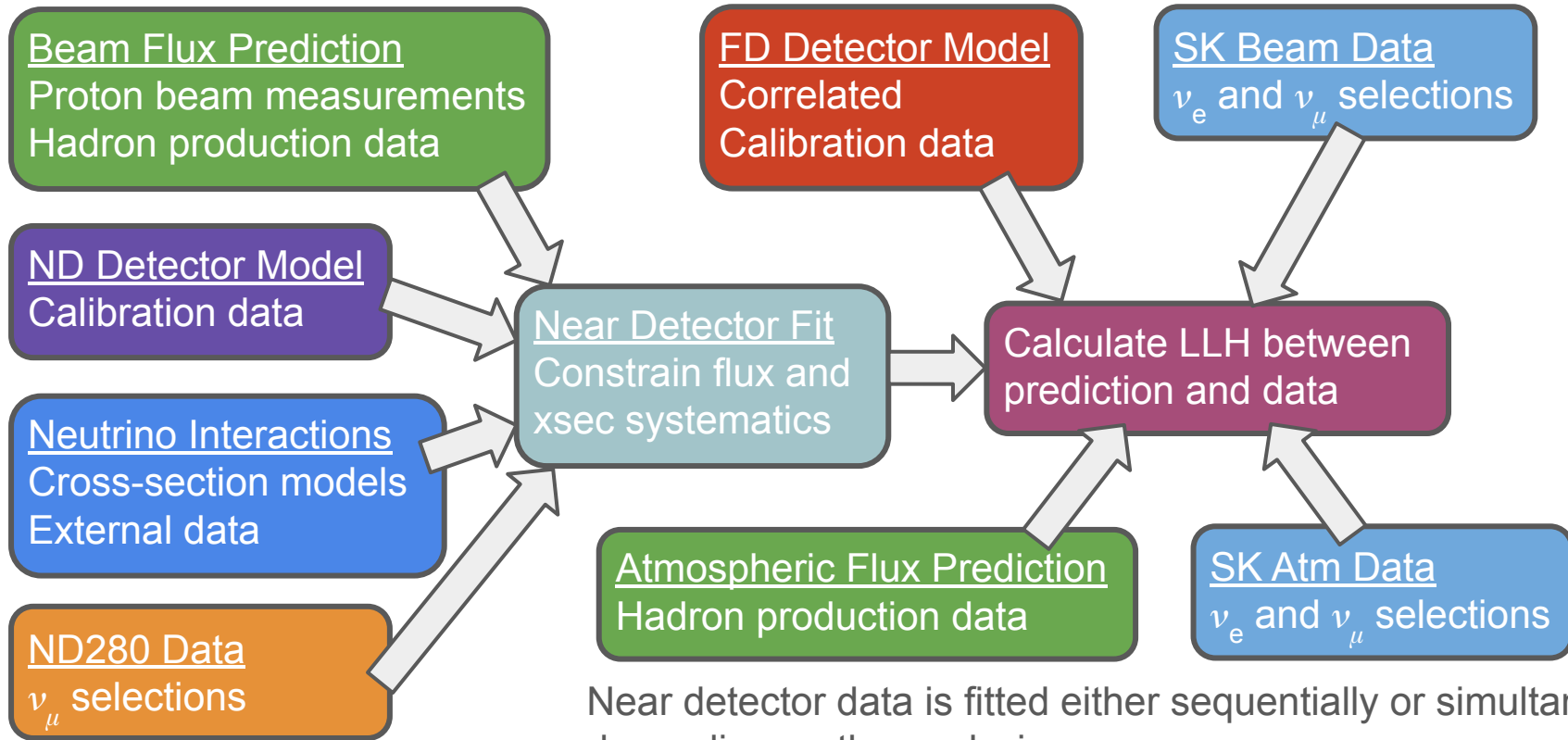
Both experiments have **overlapping energy spectrum**:



Correlated systematics

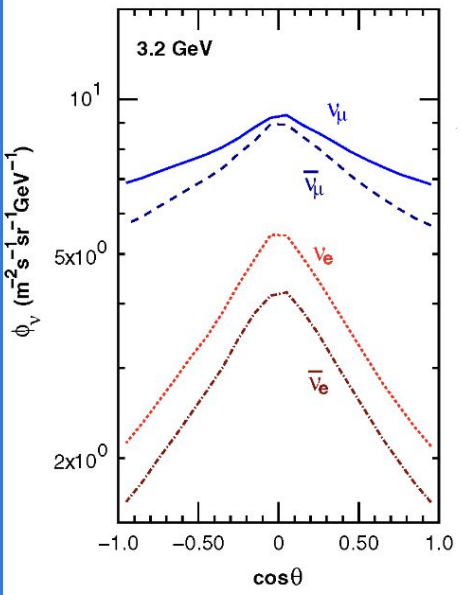
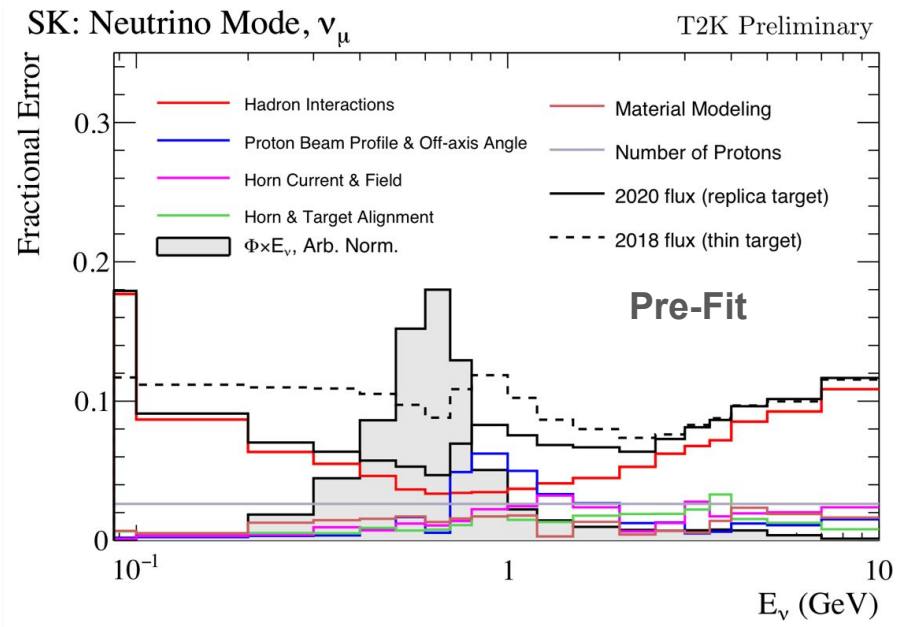
T2K near detector can be used to constrain cross-section uncertainties for low-energy atmospheric samples

Analysis Methodology in Joint Analysis

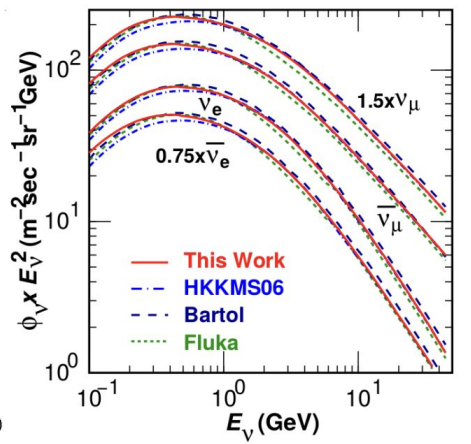


Near detector data is fitted either sequentially or simultaneously, depending on the analysis

Neutrino Flux Modelling



Flux: **Honda 2011**
(PRD 83, 123001 (2011))



Flux uncertainty $\sim 6\%$ at peak of spectrum:

- External hadron production data (e.g NA61)

No correlations included in flux modeling

Use downgoing neutrino (un-oscillated) flux to control the flux uncertainties

- Large overlap in the neutrino energy range

Cross Section Modelling



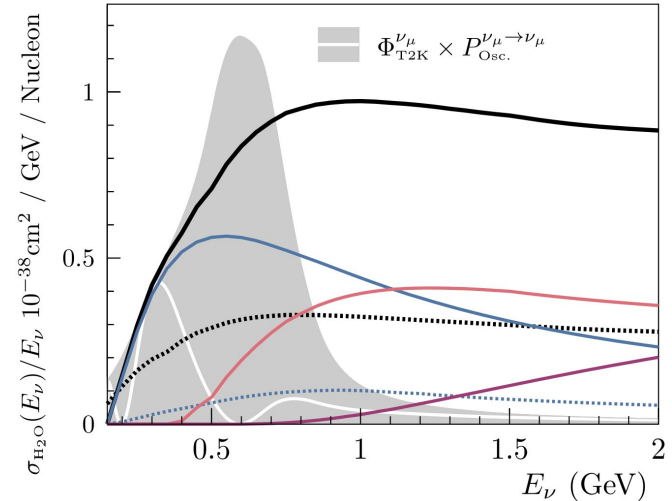
Interaction model:

Interaction Model Summary		
	“Low-energy” samples SK FC sub-GeV and T2K	“High-energy” samples SK FC multi-GeV, PC, Upmu
Charged Current Quasi-Elastic (CCQE)	T2K model with ND280 constraint, correlated in low-E/highE (except for high-Q ² parameters)	
	high-Q ² params w/ND280 + extra ν_e/ν_μ xsec diff. error	high-Q ² params w/o ND
Two particles two holes (CC2p2h)	T2K model w/ND280	SK model (100% error) + T2K-style shape error
Resonant Interactions	T2K model w/ND280 + new p_n shape uncertainty + extra NC1 π^0 uncertainties	SK model for 3 dials also in T2K model, use more recent, larger T2K priors
Deep inelastic	T2K model w/ND280	SK model
Tau neutrino interactions	SK model (25% normalization error) correlated in low-E/highE	
Final State Interactions	T2K model w/ND280	T2K model w/o ND280 (mostly same as SK model)
Secondary Interactions	T2K model, correlated in low-E/high-E not applied to SK Upmu samples	

Correlated in beam and low energy atmospheric: NEUT

- High energy uses SK model

- CC Inclusive
- CC Quasi-elastic
- CC Resonant 1 π
- ⋯ NC Inclusive
- ⋯ CC 2p2h
- CC Multi- π + DIS



Low energy interactions dominated by CCQE:

- Significant 2p2h and resonant contributions
- Mis-modelling may bias neutrino energy reconstruction - Near Detector constraint

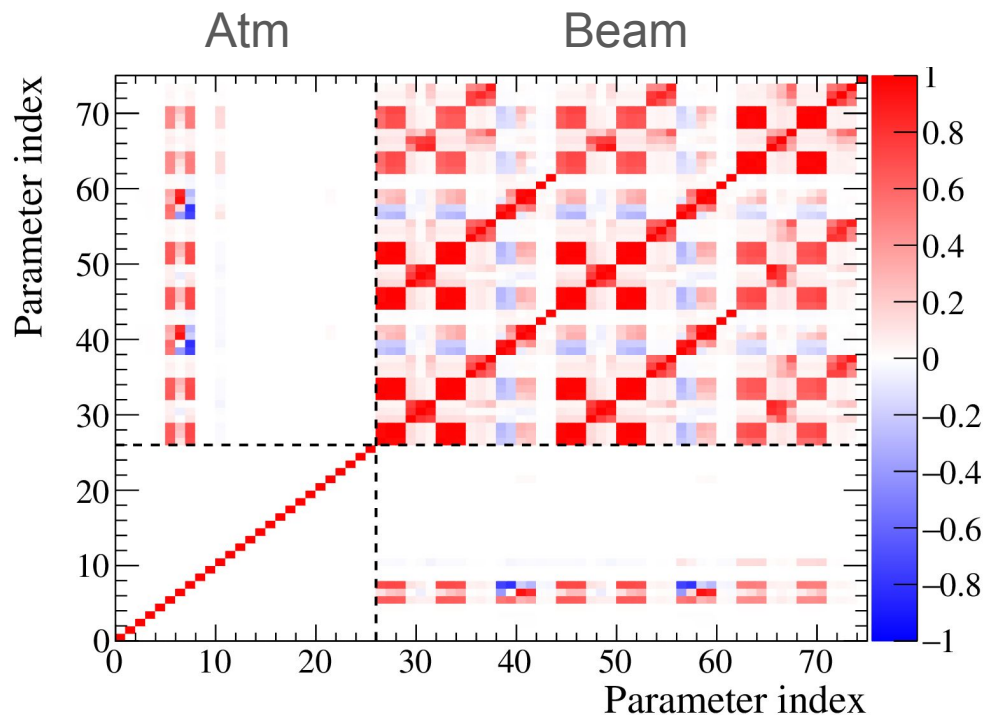
Correlated Detector Modelling

Correlated detector model developed in joint analysis:

- Larger range in energy in SK
- Larger number of multi-ring events
- Better constraint of the uncertainties

Based on SK model, with additional beam uncertainties added for T2K part

Detector model:

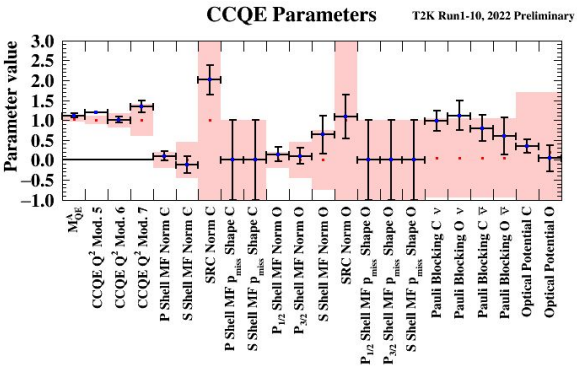
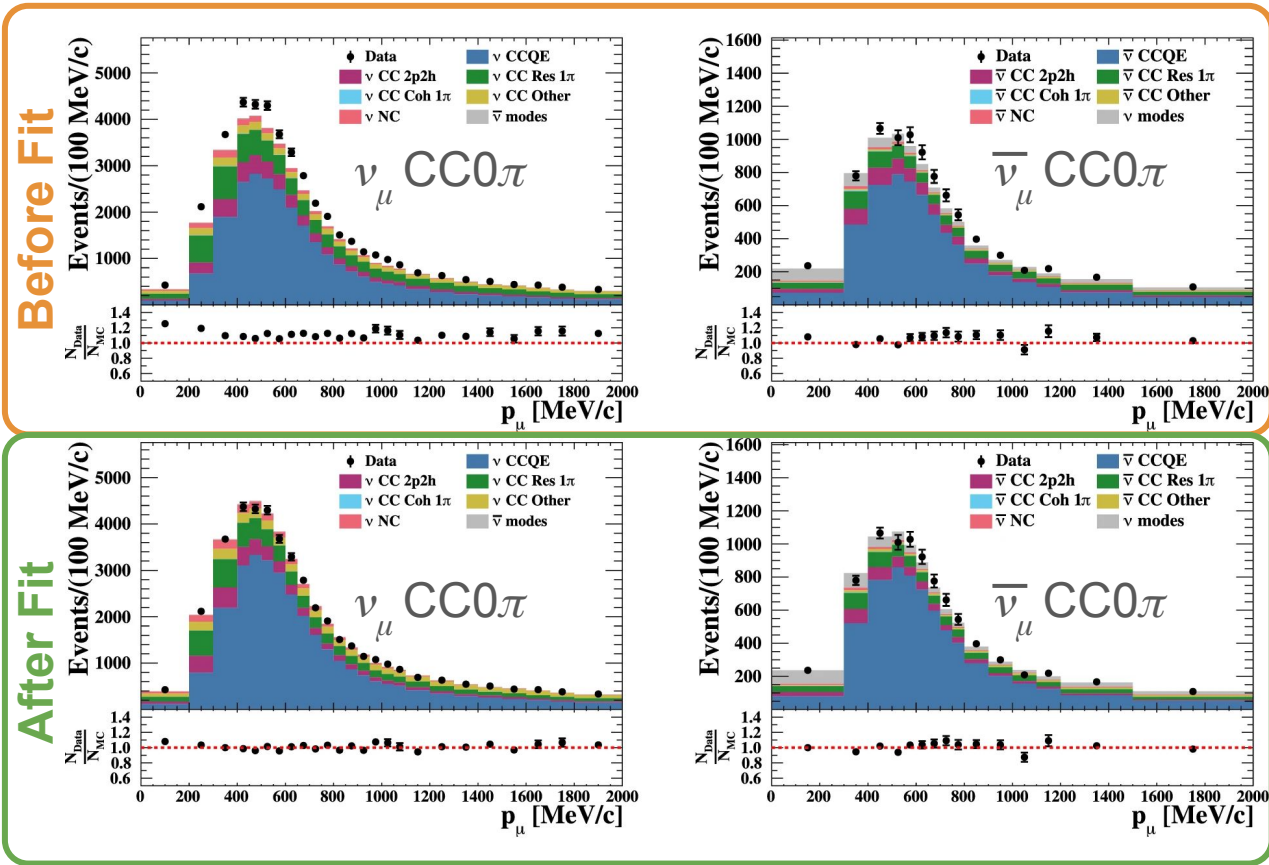


ND280 Fit

18 Samples based on:

- Horn current
- Target (CH/H₂O)
- Number of pions and protons

Tune and reduce flux and cross-section uncertainty:



T2K Beam Selections

5 samples, split by:

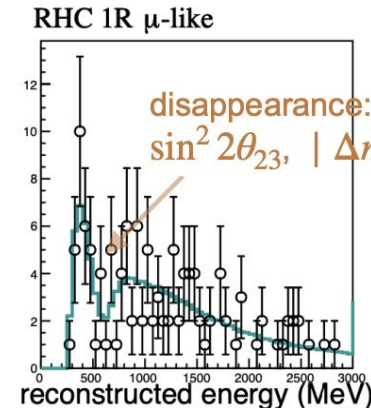
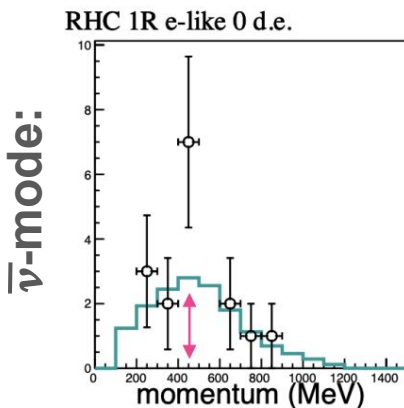
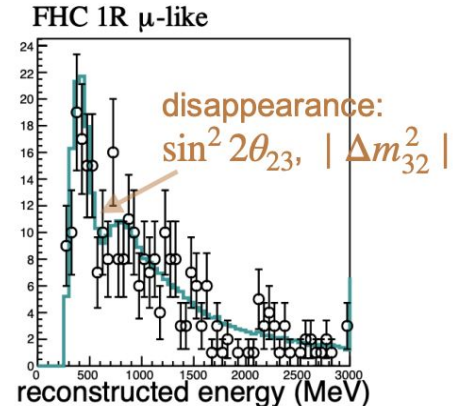
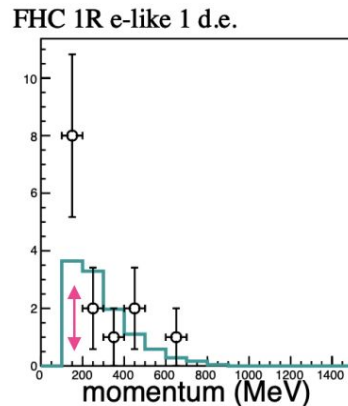
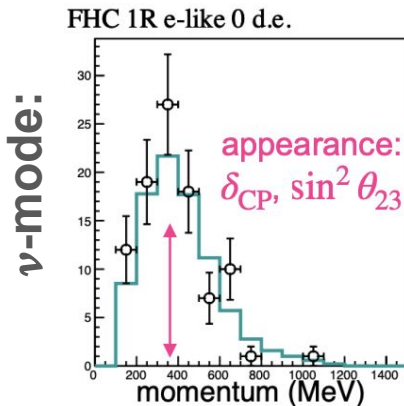
- Beam configuration
- Electron/Muon PID
- Number of decay electrons

3.6×10^{21} Protons on Target

- 55%:45% split in $\nu:\bar{\nu}$

Consistency shows good agreement between SK and T2K samples:

- Agreement between systematic parameters favored by the two datasets, p-val = 0.24



○ Data
— MC

SK Atmospheric Samples

18 SK atmospheric samples with 3244.4 days of data taking:

Multi-GeV samples:

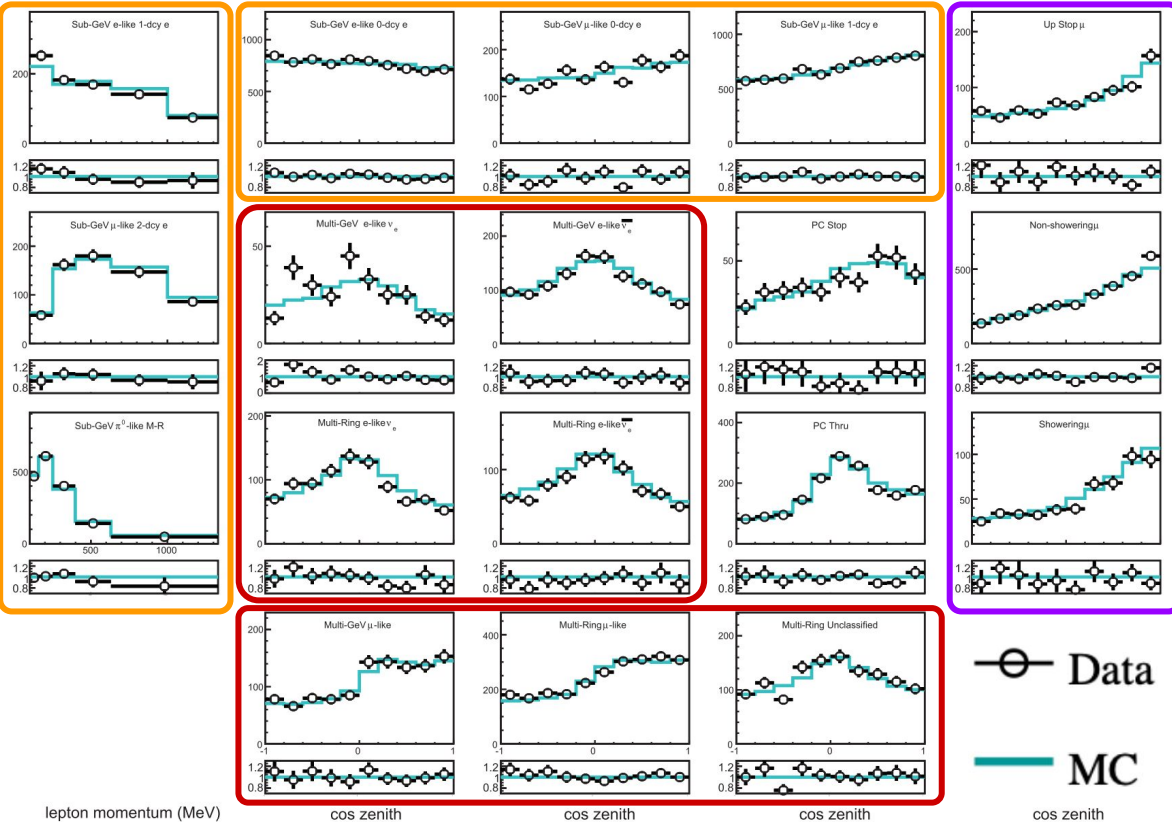
- Sensitive to mass ordering and θ_{23} octant

Sub-GeV samples:

- Electron CCQE-like sample normalisation sensitive to δ_{CP}

Upward going muons:

- Sensitive to $|\Delta m_{32}^2|$ and $\sin^2 2\theta_{23}$ due to ν_{μ} disappearance



[PTEP 2019 5, 054F01](#)

Oscillation Parameter Measurements

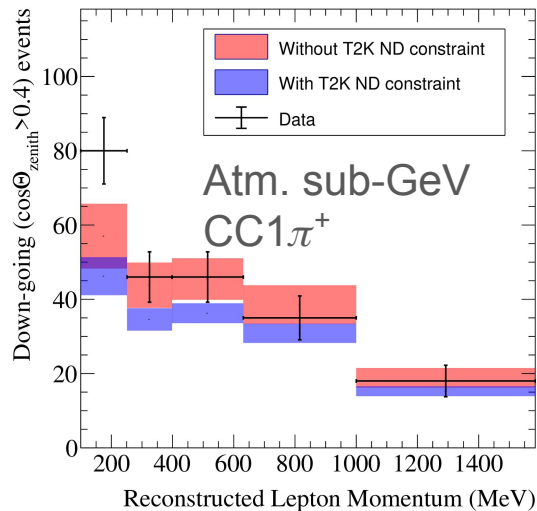
Robustness Studies

Predict potential biases from out-of-model effects

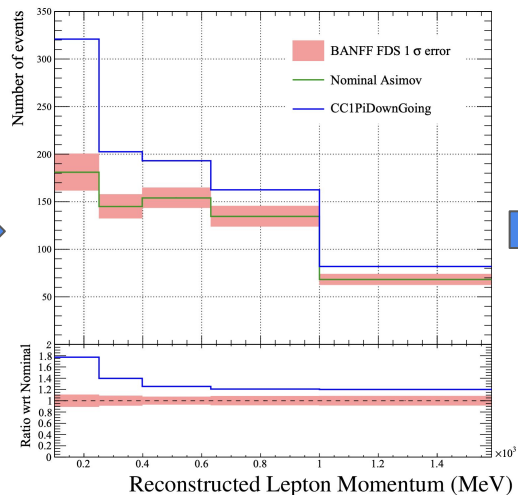
- Test 14 alternative models or data-driven effects to estimate the bias
- Biases on Δm^2_{32} are included via Gaussian smearing

Example: Excess in down-going (un-oscillated) atmospheric data after applying ND constraints

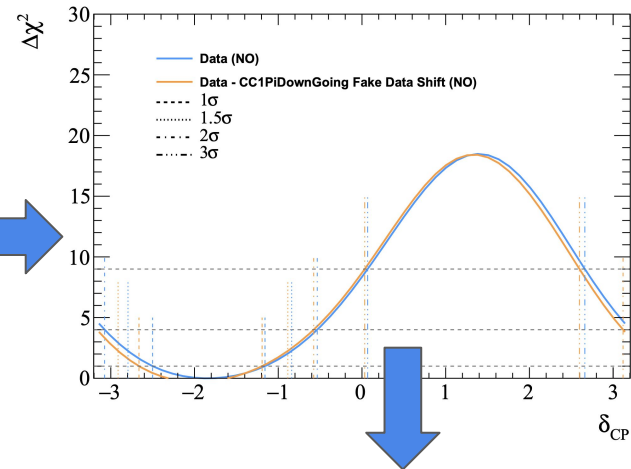
Effect:



Construct fake data
with excess:



Evaluate effect using difference
between nominal and fake data fit



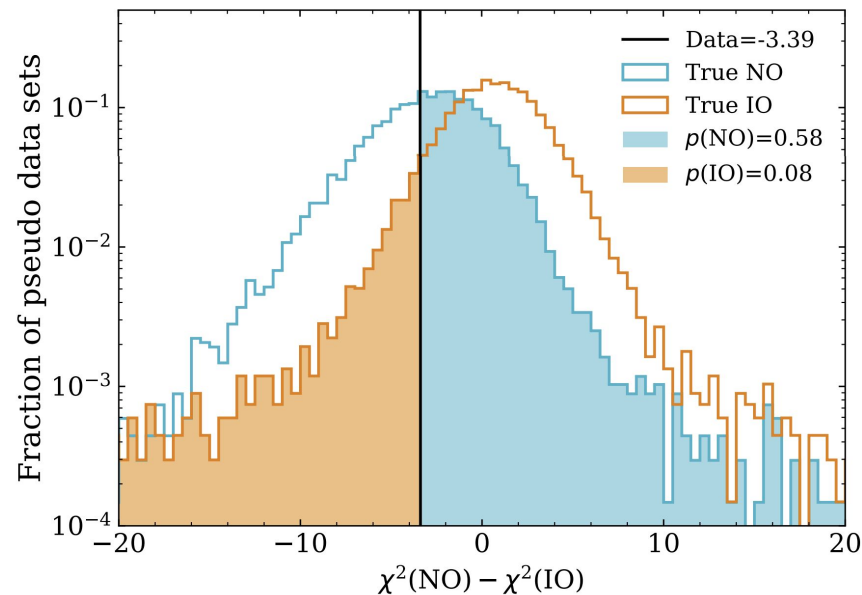
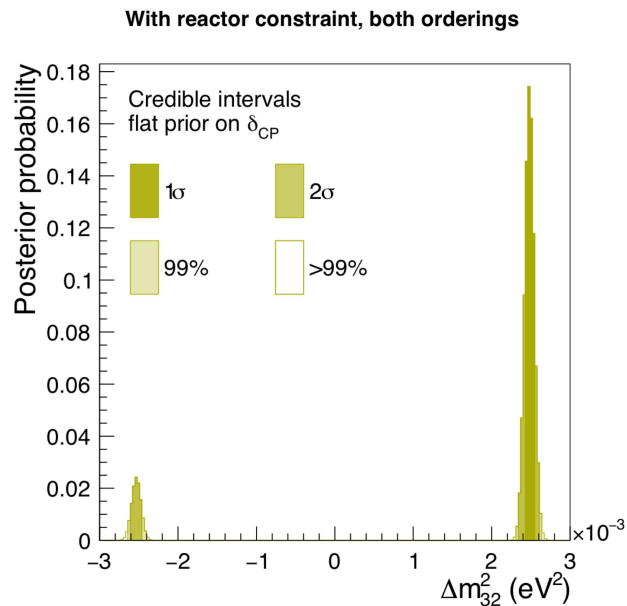
Apply difference to data results

T2K+SK Oscillation Analysis Results



Slight preference for normal ordering:

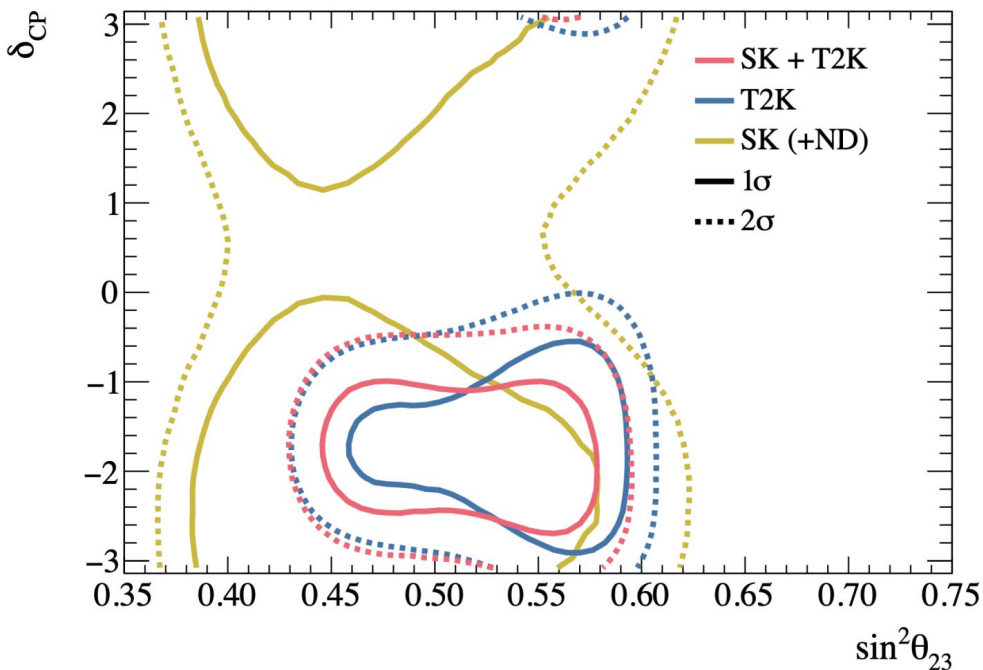
- Bayes factor $\mathbf{B(NO/IO) = 8.98}$
- Normal ordering preferred, with **p-value** for IO = **0.08**
 - Corresponds to 1.2σ deviation using one-sided test



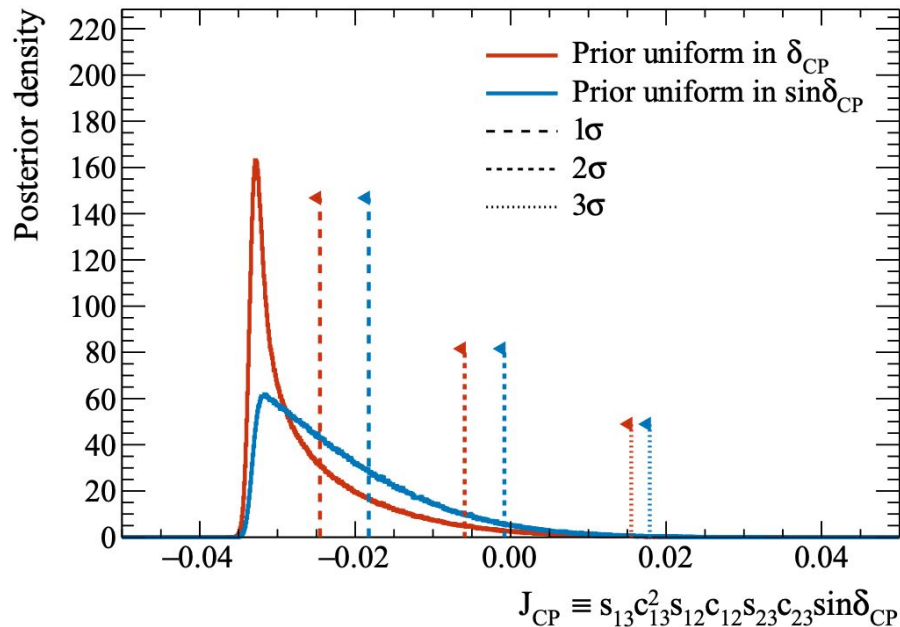
T2K+SK Oscillation Analysis Results



Conclusion: between 1.9σ and 2.0σ exclusion of CP symmetry

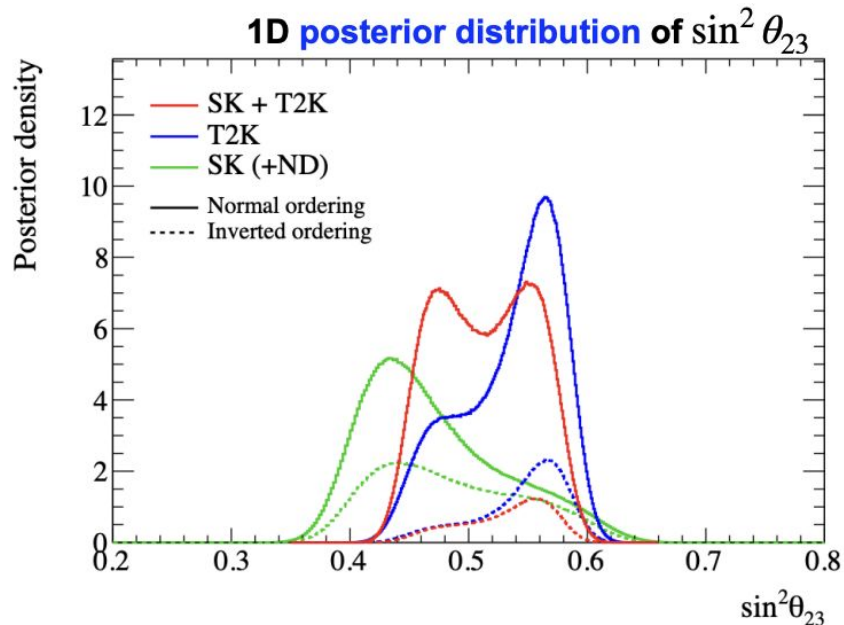


SK has significant contribution to preference of octant



Exclusion of CP-conserving values of $J_{CP}=0$ is 2.2σ (1.9σ) for flat δ_{CP} ($\sin\delta_{CP}$) prior

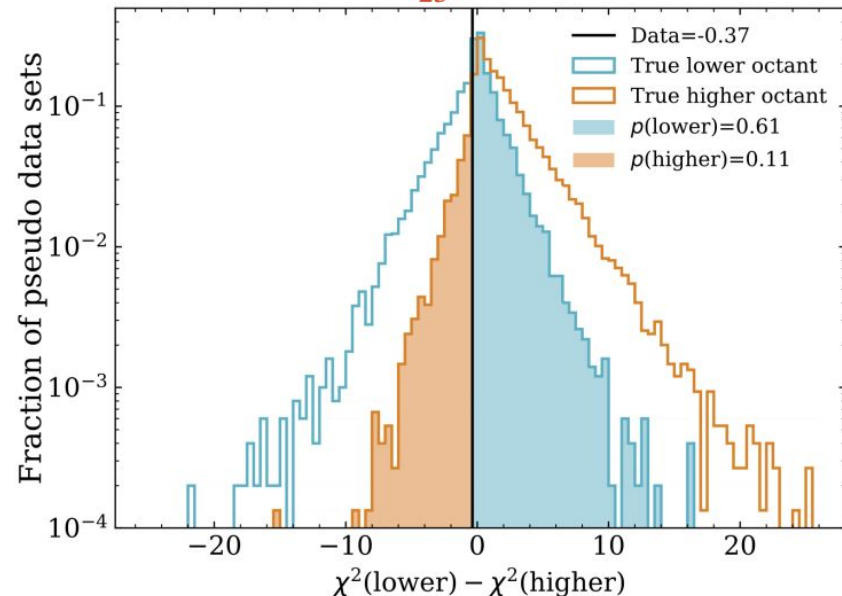
T2K+SK Oscillation Analysis Results



Different octant preference by each experiment:

- Combined analysis: Bayesian posterior probability prefers UO (0.64)
- Corresponds to $\sim 0.9\sigma$ fluctuation of LO

Distribution of the θ_{23} Octant test statistic



P-value (CLs) for UO from Frequentist analysis is 0.11 (0.28)

- **Conclusion:** no obvious preference for octant

First joint oscillation analysis of T2K beam + SK atmospheric neutrinos has been performed:

Both Bayesian and Frequentist results provided, with additional robustness studies:

- Limited rejection of inverse hierarchy at **90% CL**
- Charge-Parity conservation rejected between **1.9σ** and **2.0σ** exclusion
- No preference on the θ_{23} octant

Potential for future updates:

- SKIV (3244.4 days) \rightarrow SKI to SKV (6511.3 days)
- T2K Run 1-10 \rightarrow Run 1-11 (10% increase in ν -mode data)
- Updates to flux and interaction models

Results from the analysis presented in [Arxiv 2405.12488](#)

Backup Slides

LBL experiments sensitive to these parameters

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{23} & \sin \theta_{23} \\ 0 & -\sin \theta_{23} & \cos \theta_{23} \end{pmatrix} \begin{pmatrix} \cos \theta_{13} & 0 & \sin \theta_{13} e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -\sin \theta_{13} e^{i\delta_{CP}} & 0 & \cos \theta_{13} \end{pmatrix} \begin{pmatrix} \cos \theta_{12} & \sin \theta_{12} & 0 \\ -\sin \theta_{12} & \cos \theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Atmospherics and LBL

$$\theta_{23} \sim 45^\circ$$

$$|\Delta m_{32}^2| \sim 2.5 \times 10^{-3} \text{eV}^2$$

Reactors

$$\theta_{13} \sim 10^\circ$$

$$\delta_{CP} \text{ unknown}$$

Solar and Reactors

$$\theta_{12} \sim 35^\circ$$

$$\Delta m_{21}^2 \sim 7.5 \times 10^{-5} \text{eV}^2$$

Long baseline accelerator (LBL) experiments:

- Make the most precise measurements of θ_{23} , $|\Delta m_{32}^2|$
- Sign of $|\Delta m_{32}^2|$ and δ_{CP} still unknown and accessible to LBL

C. Giganti (Neutrino 2024)

Physics case

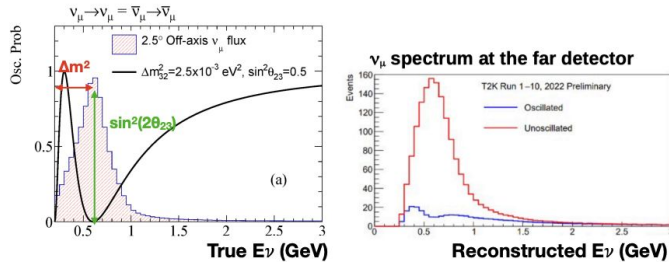


ν_μ and $\bar{\nu}_\mu$ disappearance

$$P(\nu_\mu \rightarrow \nu_\mu) = P(\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu) = 1 - \sin^2(2\theta_{23}) \sin^2\left(1.27 \frac{\Delta m^2 L}{E}\right)$$

Same oscillation probability for ν and $\bar{\nu}$

Sensitive to $|\Delta m^2_{32}|$ and to $\sin^2(2\theta_{23}) \rightarrow$ no sensitivity to mass ordering and δ_{CP}



ν_e and $\bar{\nu}_e$ appearance

$$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) \simeq \sin^2\theta_{23} \frac{\sin^2 2\theta_{13}}{(A-1)^2} \sin^2[(A-1)\Delta_{31}]$$

$$+ \alpha \frac{J_0 \sin \delta_{CP}}{A(1-A)} \sin \Delta_{31} \sin(A\Delta_{31}) \sin[(1-A)\Delta_{31}]$$

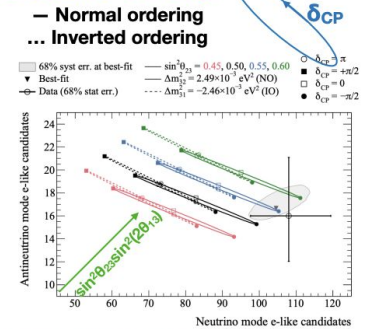
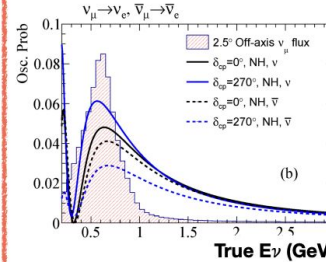
$$+ \alpha \frac{J_0 \cos \delta_{CP}}{A(1-A)} \cos \Delta_{31} \sin(A\Delta_{31}) \sin[(1-A)\Delta_{31}] + O(\alpha^2)$$

$$\alpha = \Delta m^2_{21} / \Delta m^2_{31} \sim 1/30$$

$$J_0 = \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23} \cos \theta_{13}$$

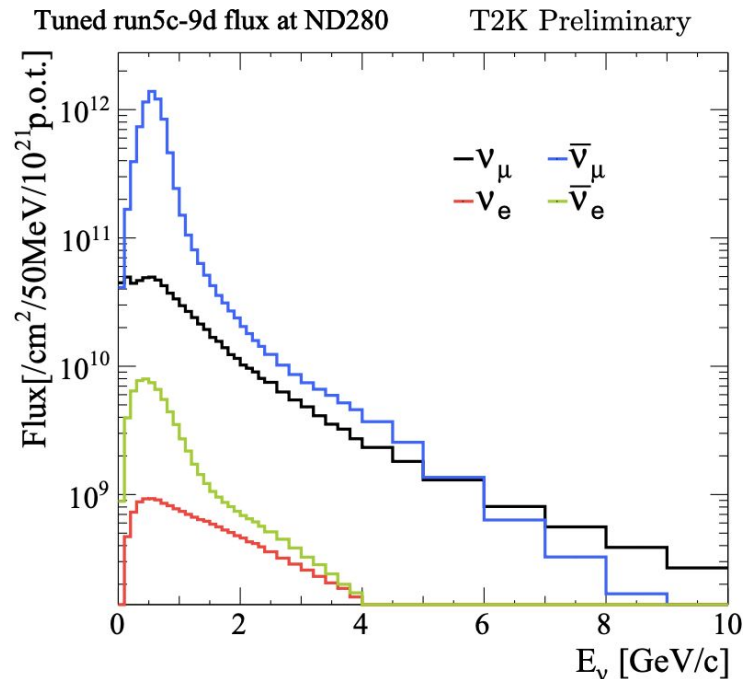
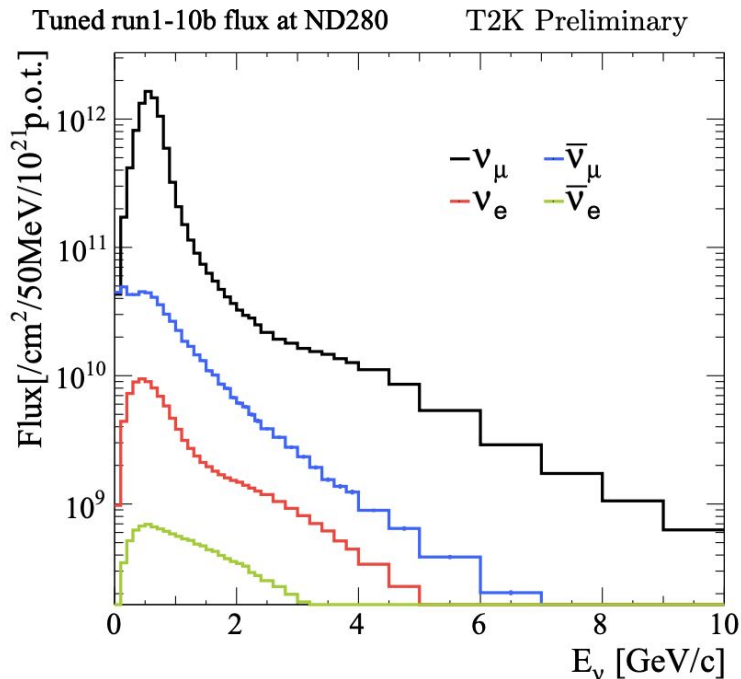
$$A = (\mp) 2\sqrt{2} G_F n_e E / \Delta m^2_{31}$$

Sensitivity to δ_{CP} , to the mass ordering and to the octant of θ_{23}

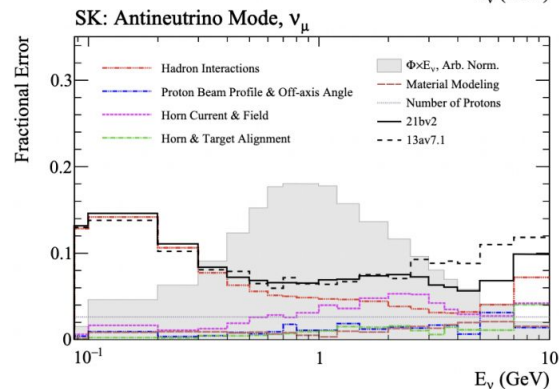
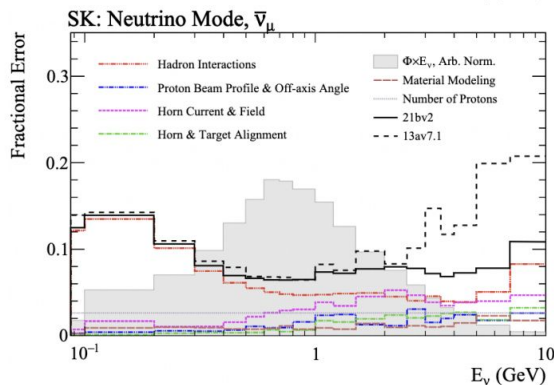
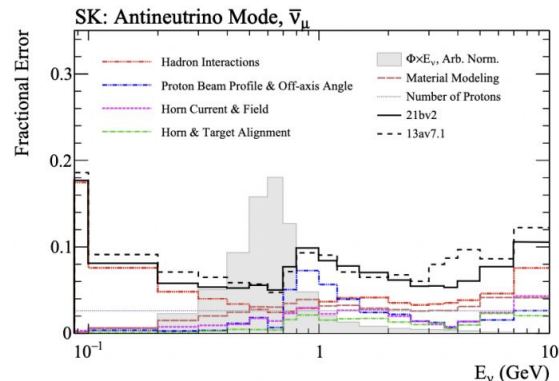
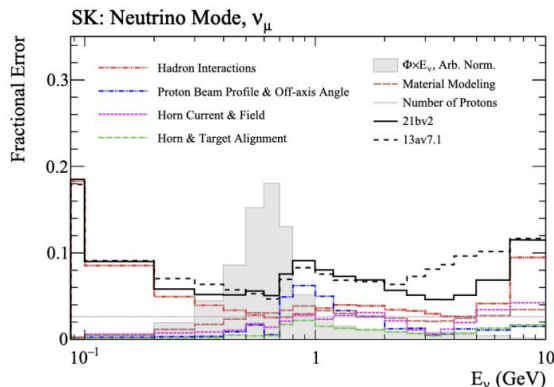


ν -mode

$\bar{\nu}$ -mode



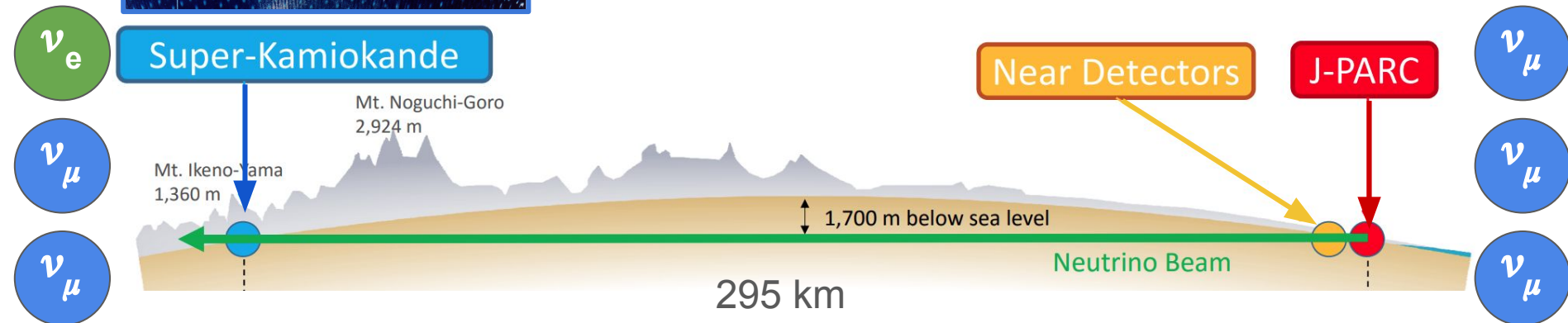
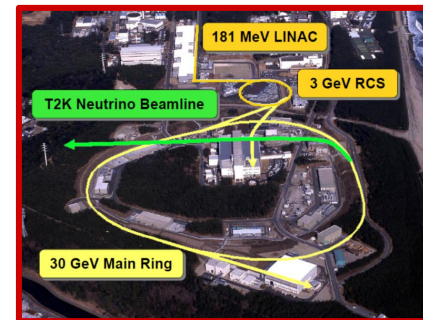
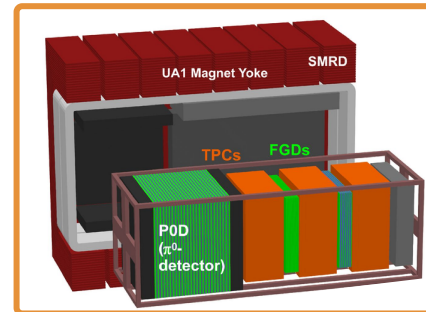
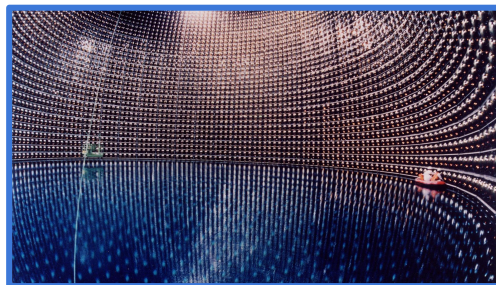
Neutrino Flux Uncertainties



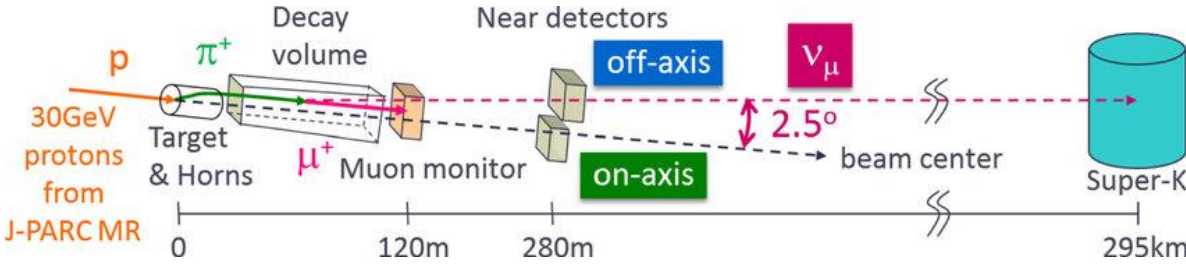
T2K Experiment

High intensity neutrino(antineutrino) beam produced at **J-PARC**:

- Use **Near** and **Far** detector



Beamline



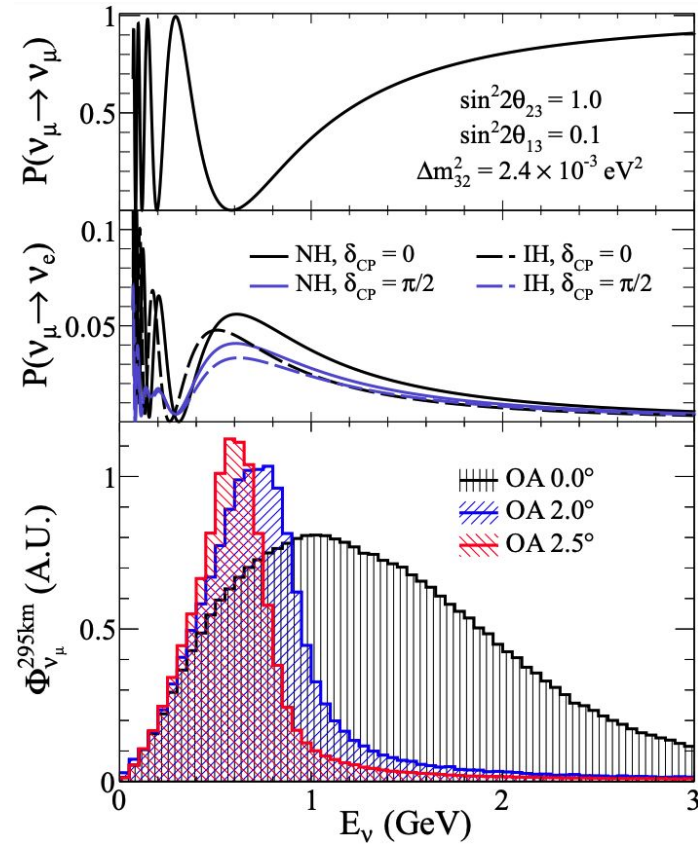
30 GeV proton beam extracted onto graphite target:

- p+C interactions produce hadron beam (π^\pm and K^\pm)

Hadrons focused by 3 electromagnetic horns:

- Focusing π^+ produces ν_μ via $\pi^+ \rightarrow \mu^+ + \nu_\mu$
- Changing horn current produces antineutrino beam

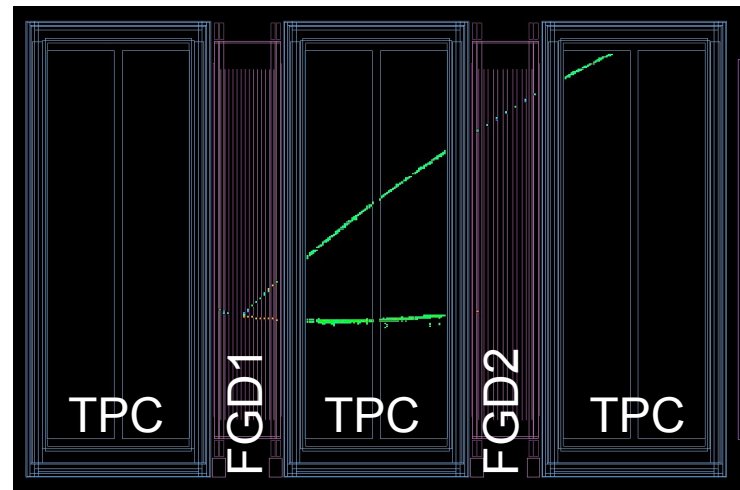
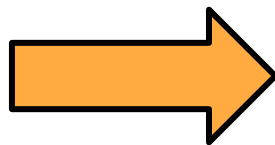
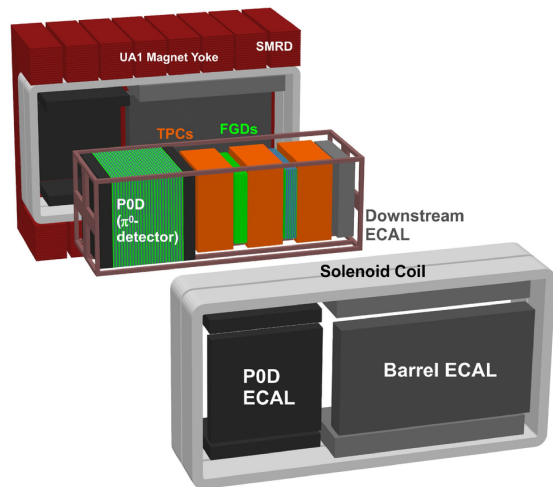
Off axis technique produces narrow-band beam



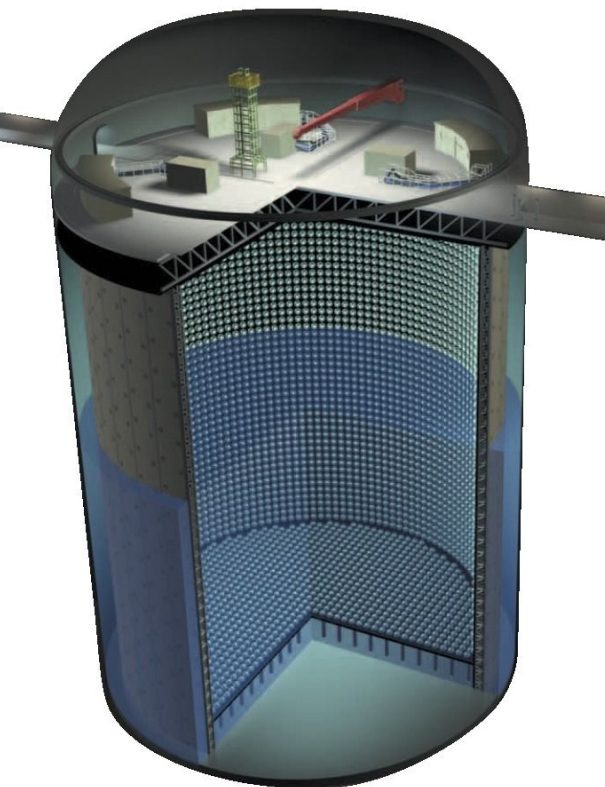
Near Detector (ND280)

Measure beam spectrum and flavour composition pre-oscillation:

- 0.2T magnetic field
- Electromagnetic calorimeter to distinguish showers/tracks
- 2 Fine Grain Detectors (FGDs): Primary neutrino target
- 3 Time Projection Chambers (TPCs): Reconstruct momentum, charge and PID
- Recent upgrades (SFGD, high-angle TPCs, time of flight): **Not** used within analyses shown



Super Kamiokande (SK)

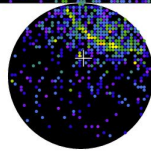
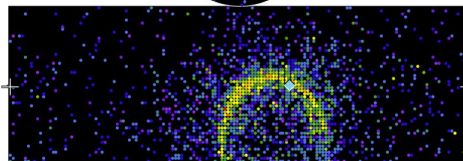
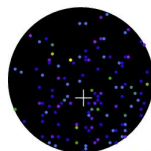


Large underground 50 kton water Cherenkov detector:

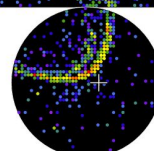
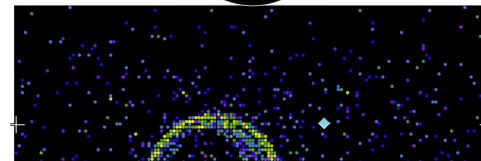
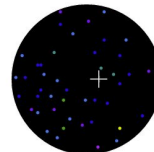
- ~11k 20" PMTs in the inner detector
- ~2k 8" PMTs in the outer detector, used as veto

Doped with 0.03% Gd in 2022 for improved neutron tagging efficiency: **Not** used within analyses shown

Electron:



Muon:



(See A. Beauchêne's talk)

Sample Breakdown

FHCCC1pi-2020	0.03	0.83	0.02	0.03	0.00	0.01	0.01	0.00	0.01	0.02	0.00	0.00	0.01	0.00	0.03
RHC1Re-2020	0.58	0.12	0.01	0.01	0.00	0.07	0.01	0.01	0.00	0.13	0.03	0.00	0.01	0.00	0.02
FHC1Re-2020	0.65	0.11	0.00	0.00	0.00	0.04	0.01	0.00	0.00	0.13	0.02	0.00	0.00	0.00	0.02
RHC1Rmu-2020	0.59	0.18	0.00	0.02	0.00	0.00	0.02	0.00	0.00	0.14	0.00	0.00	0.00	0.00	0.03
FHC1Rmu-2020	0.59	0.18	0.00	0.03	0.00	0.00	0.03	0.00	0.00	0.13	0.00	0.00	0.01	0.00	0.03
SubGeV-pi0like	0.05	0.02	0.00	0.00	0.00	0.68	0.06	0.06	0.03	0.01	0.00	0.00	0.07	0.00	0.01
SubGeV-mulike-2dcy	0.03	0.80	0.01	0.10	0.00	0.00	0.00	0.00	0.00	0.01	0.00	0.00	0.00	0.00	0.03
SubGeV-mulike-1dcy	0.70	0.13	0.00	0.01	0.00	0.00	0.01	0.00	0.00	0.13	0.00	0.00	0.00	0.00	0.02
SubGeV-mulike-0dcy	0.65	0.11	0.00	0.01	0.00	0.01	0.05	0.00	0.02	0.12	0.00	0.00	0.01	0.00	0.02
SubGeV-elike-1dcy	0.05	0.75	0.01	0.10	0.00	0.00	0.01	0.00	0.01	0.01	0.00	0.00	0.02	0.01	0.03
SubGeV-elike-0dcy	0.69	0.11	0.00	0.01	0.00	0.03	0.00	0.00	0.00	0.12	0.00	0.00	0.00	0.00	0.02
	CCQE	CC1pipm	CCcoh	CCmpi	CCDIS	NC1pi0	NC1pipm	NCcoh	NCoth	2p2h	NC1gam	CCMisc	NCmpi	NCDIS	CC1pi0

