

Double Parton Scattering at ATLAS

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On behalf of the ATLAS Collaboration

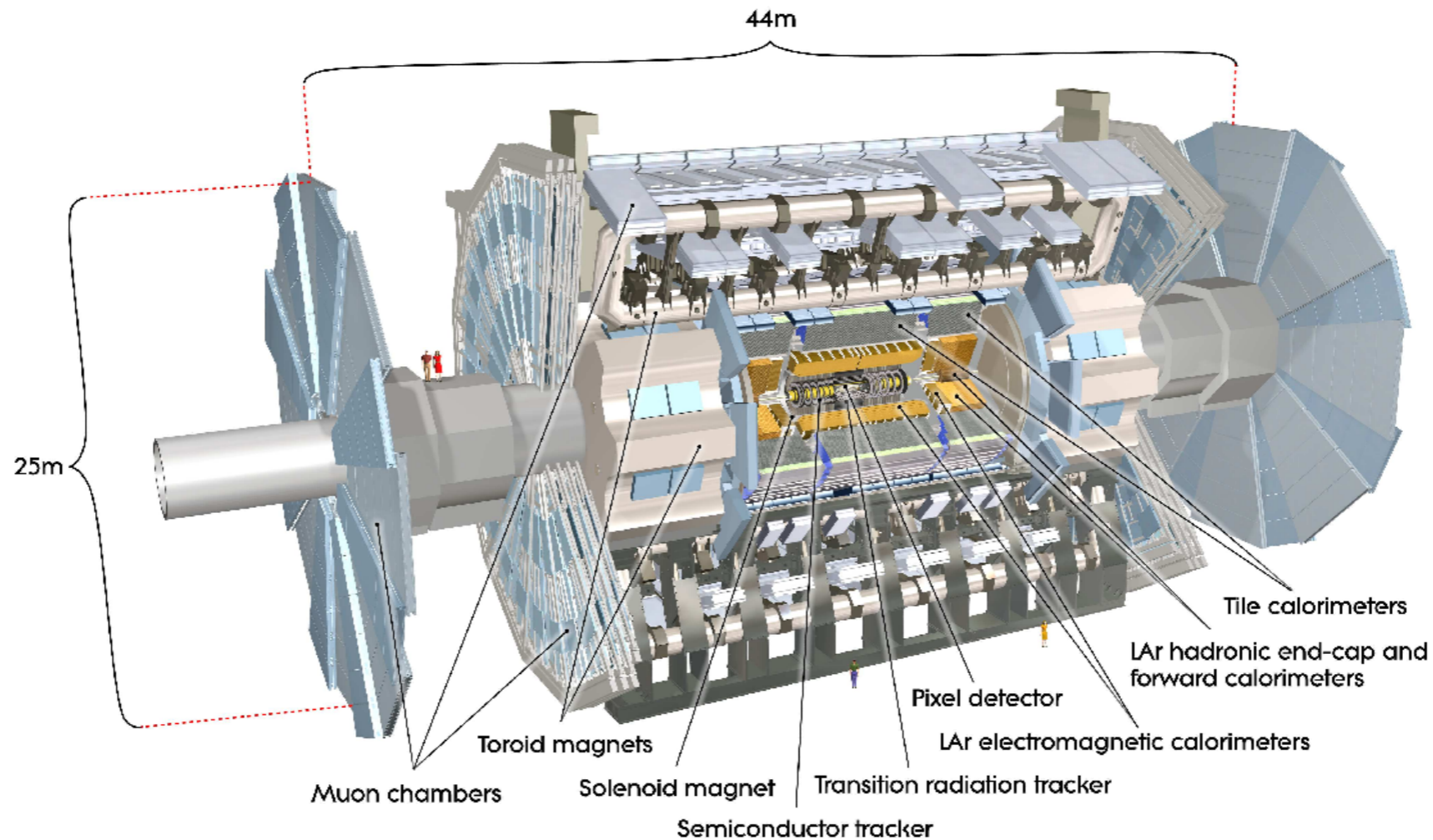
University of Washington

Workshop on Double Parton Scattering
and the 3D structure of hadrons

January 11-15, 2025



The ATLAS detector

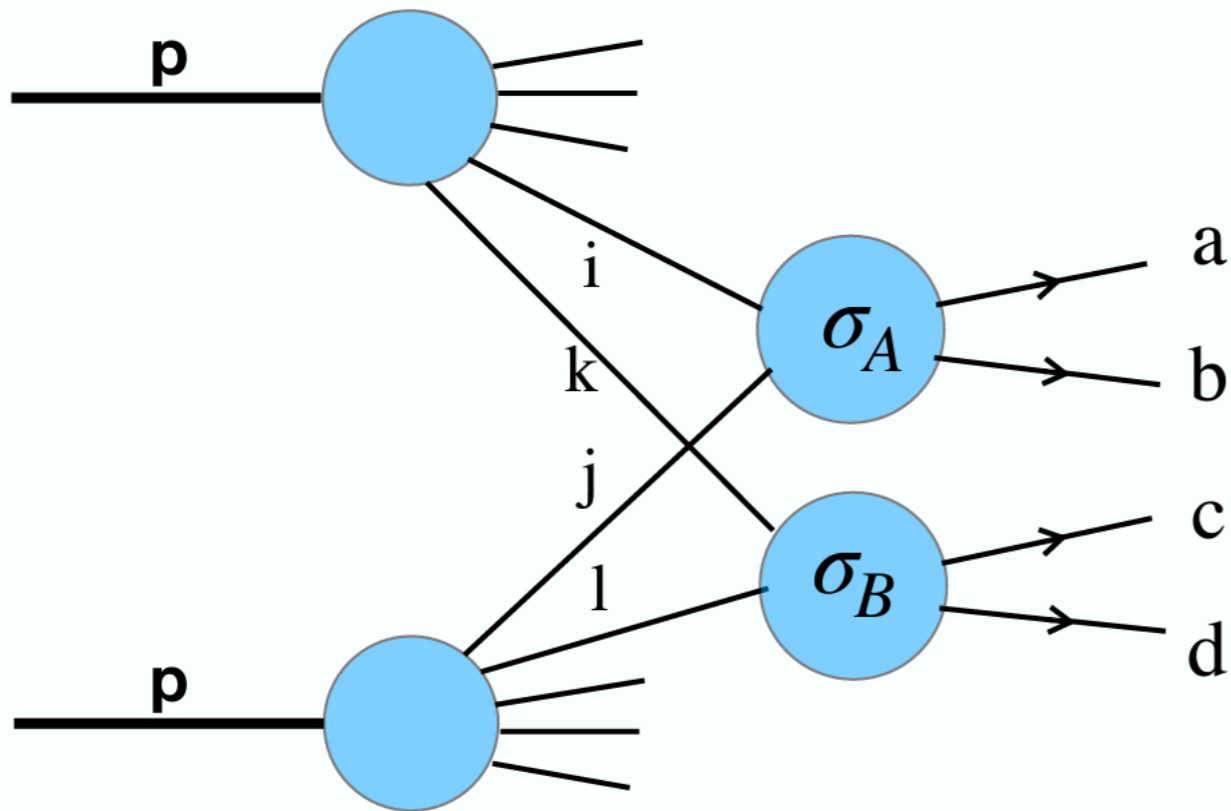


- ATLAS is one of the two general-purpose detectors at the LHC
- At 44 m long, 25 m high and 25 m wide, the 7000-tonne ATLAS detector is the largest volume particle detector ever constructed
- It's designed in layers to observe different types of particles

- Collected a large set of pp-collision data
 - Run 1 (2010-2013): 4.9 fb^{-1} at 7 TeV and 20.2 fb^{-1} at 8 TeV
 - Run 2 (2015-2018): 140 fb^{-1} at 13 TeV
 - Run3 (2022-): 183 fb^{-1} at 13.6 TeV (recorded)

Double parton scattering

- Double parton scattering (DPS): two independent interactions in one pp collision



Cross section:

$$\sigma_{A+B}^{DPS} = \frac{1}{1 + \delta_{AB}} \frac{\sigma_A \sigma_B}{\sigma_{\text{eff}}}$$

If $A=B$, $\delta_{AB} = 1$
 Otherwise, $\delta_{AB} = 0$

- σ_{eff} is the effective area parameter related to the overlap between the interacting hadrons, determining the overall size of DPS cross section
 - Assumed to be independent of process, cut and centre-of-mass energy
- Introduce DPS fraction f_{DPS} : $\sigma_{A+B}^{DPS} = f_{DPS} \cdot \sigma_{A+B}^{\text{tot}}$, where $\sigma_{A+B}^{\text{tot}}$ is the total cross section for A+B final state production, Thus, $\sigma_{\text{eff}} = \frac{1}{1 + \delta_{AB}} \frac{\sigma_A \sigma_B}{f_{DPS} \cdot \sigma_{A+B}^{\text{tot}}}$

In this talk

- Measurement of hard double-parton interactions in $W(\rightarrow \ell\nu) + 2\text{-jet}$ events @ 7 TeV [New J. Phys. 15 \(2013\) 033038](#)
- Study of hard double-parton scattering in four-jet events at 7 TeV [JHEP 11 \(2016\) 110](#)
- Study of the hard double-parton scattering contribution to inclusive four-lepton production @ 8 TeV [Phys.Lett. B 790 \(2019\) 595](#)
- Measurement of prompt J/ψ pair production cross-section @ 8 TeV [Eur. Phys. J. C 77 \(2017\) 76](#)
- Measurement of $Z + J/\psi$ (prompt and non-prompt) @ 8 TeV [Eur. Phys. J. C 75 \(2015\) 229](#)
- Measurement of $W + J/\psi$ (prompt) @ 8 TeV [JHEP 01 \(2020\) 095](#)

$W(\rightarrow \ell\nu) + 2\text{-jet}$ study

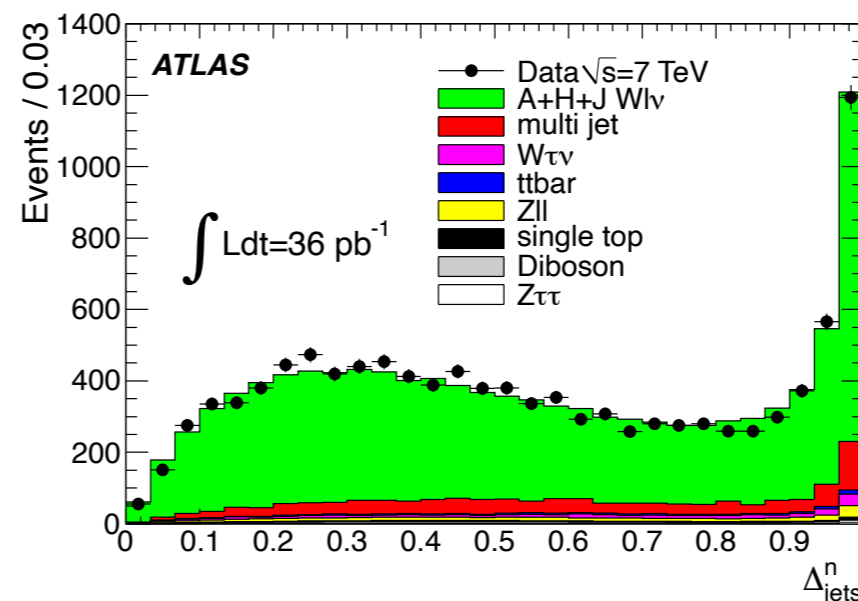
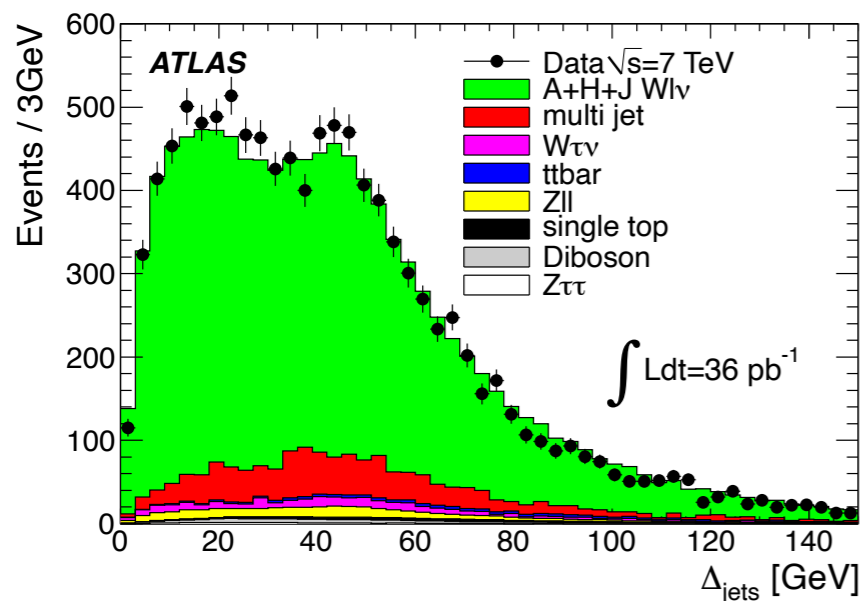
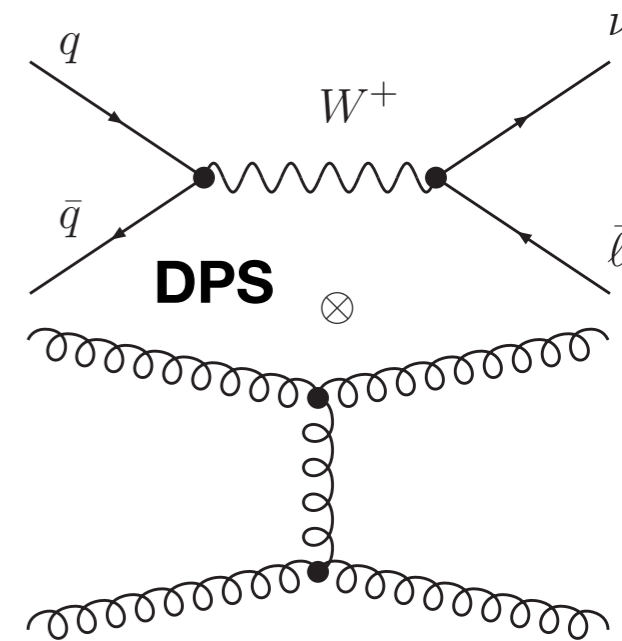
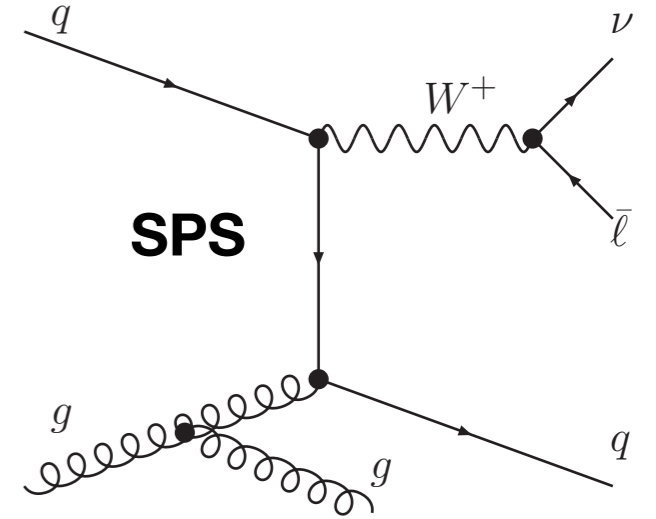
- Measure the hard DPS contribution with the $W(\rightarrow \ell\nu) + 2\text{-jet}$ events
- Dataset: 36 pb^{-1} @ 7 TeV collected in 2010, $\langle \mu \rangle = 0.4$
- Selections:

- Electron/muon: $p_T > 20 \text{ GeV}$ and $|\eta| < 2.47(2.4)$

- $E_T^{\text{miss}} > 25 \text{ GeV}$ and $m_T > 40 \text{ GeV}$ ($m_T = \sqrt{2p_T^\ell E_T^{\text{miss}}(1 - \cos\Delta\phi_{\ell, E_T^{\text{miss}}})}$)

- Jets: $p_T > 20 \text{ GeV}$ and $|y| < 2.8$

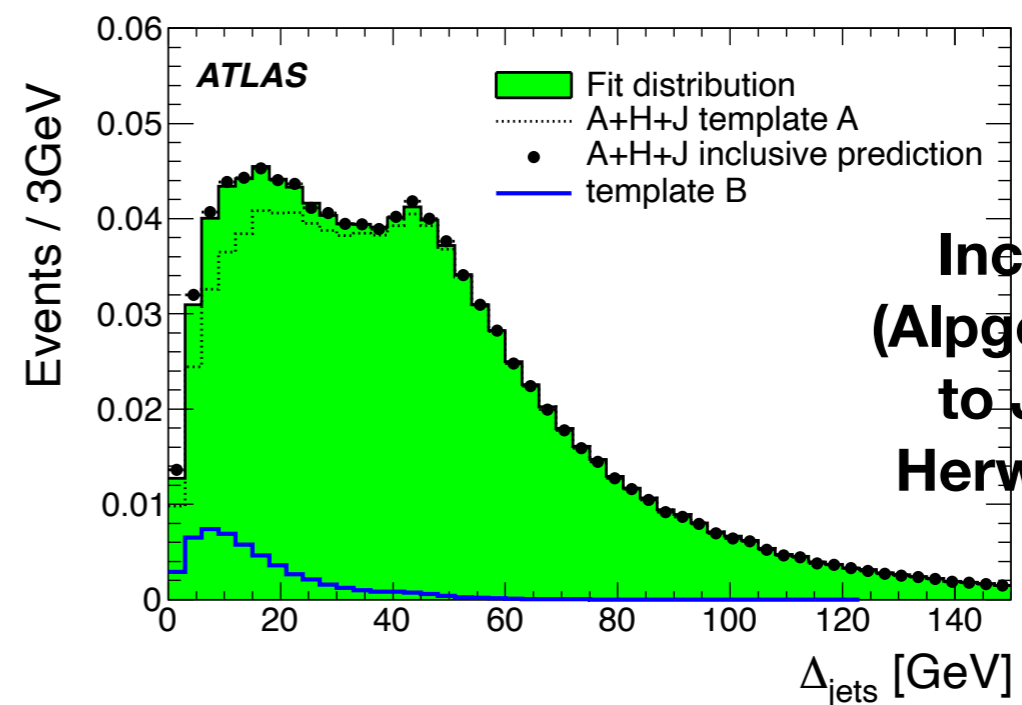
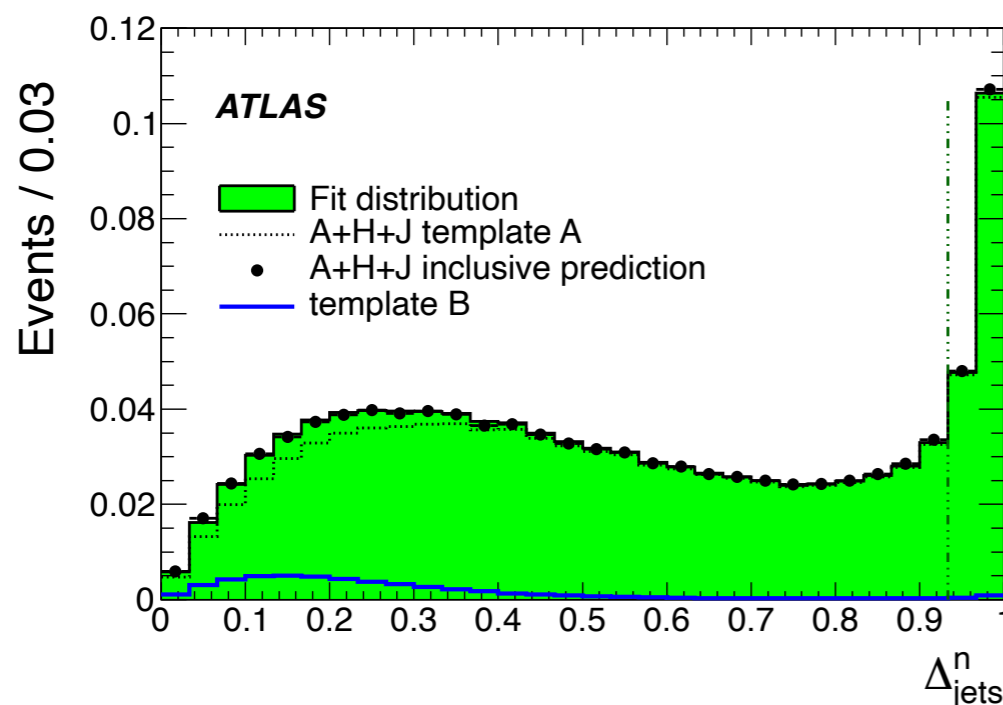
- Observables: $\Delta_{\text{jets}} = |\vec{p}_T^{J_1} + \vec{p}_T^{J_2}|$ and $\Delta_{\text{jets}}^n = \frac{|\vec{p}_T^{J_1} + \vec{p}_T^{J_2}|}{|\vec{p}_T^{J_1}| + |\vec{p}_T^{J_2}|}$



$W(\rightarrow \ell\nu) + 2\text{-jet}$ study

- To extract $f_{DP}^{(D)}$, a fit is performed by comparing the Δ_{jets}^n distribution at detector level in background-corrected data with two templates:
 - Template A “DPI-off”: two jets originate from a primary scatter (SPS). Constructed by removing hard MPI candidate events from generated sample
 - Template B “DPI-only”: both jets originate from a DPI scatter (DPS). Constructed by minimum bias dijet data

$$f = (1 - f_{DP}^{(D)}) \cdot A + f_{DP}^{(D)} \cdot B$$



**Inclusive AHJ
(AlpGen interfaced
to Jimmy and
Herwig) pseudo-
data**

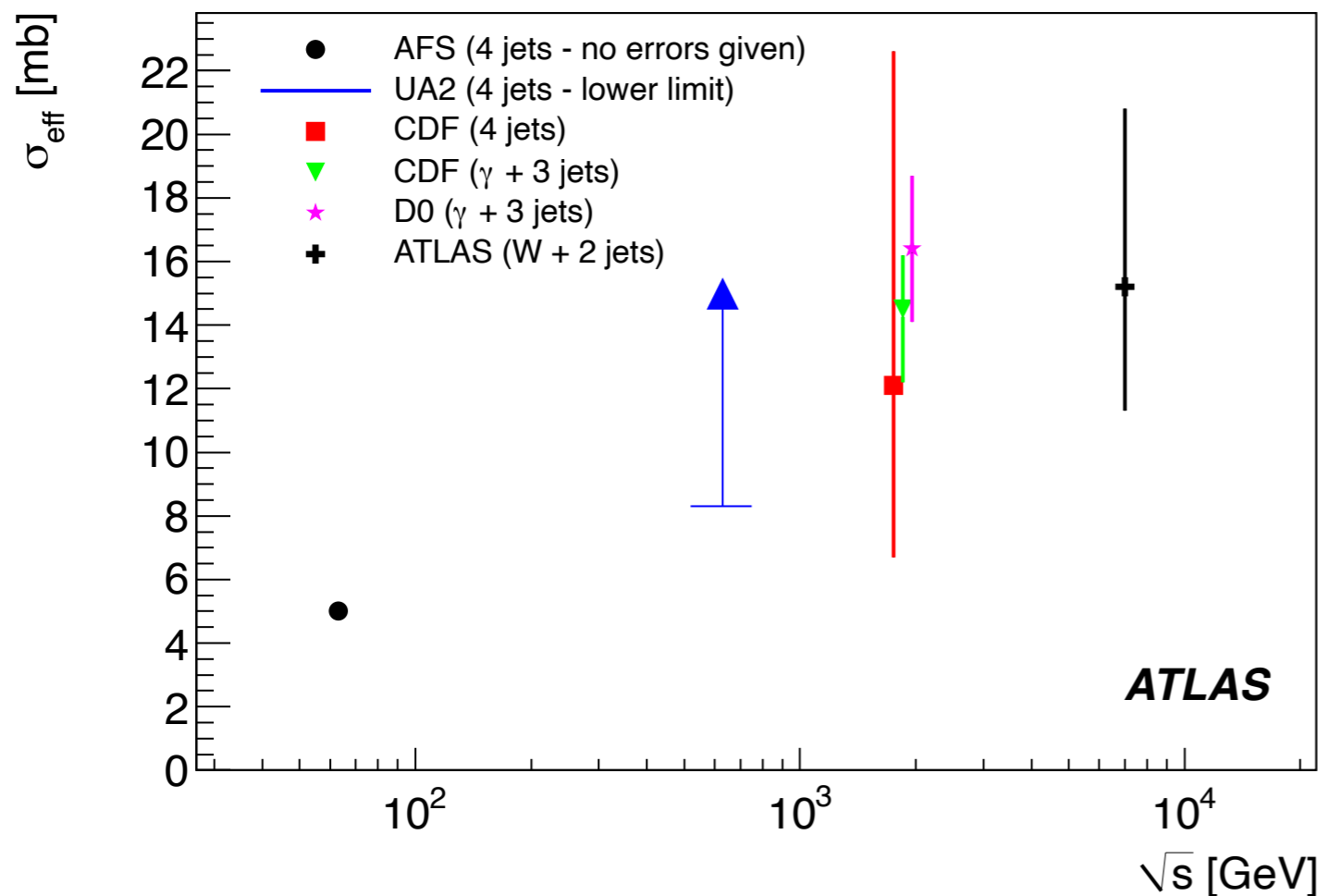
$W(\rightarrow \ell\nu) + 2\text{-jet}$ study

- For jets with $p_T > 20$ GeV and $|y| < 2.8$, the double-parton interaction rate $f_{DP}^{(D)}$ is measured to be:

$$f_{DP}^{(D)} = 0.08 \pm 0.01(\text{stat.}) \pm 0.02(\text{sys.})$$

- The effective area parameter σ_{eff} extracted from data is:

$$\sigma_{\text{eff}}(7 \text{ TeV}) = 15 \pm 3(\text{stat.})_{-3}^{+5}(\text{sys.}) \text{ mb}$$



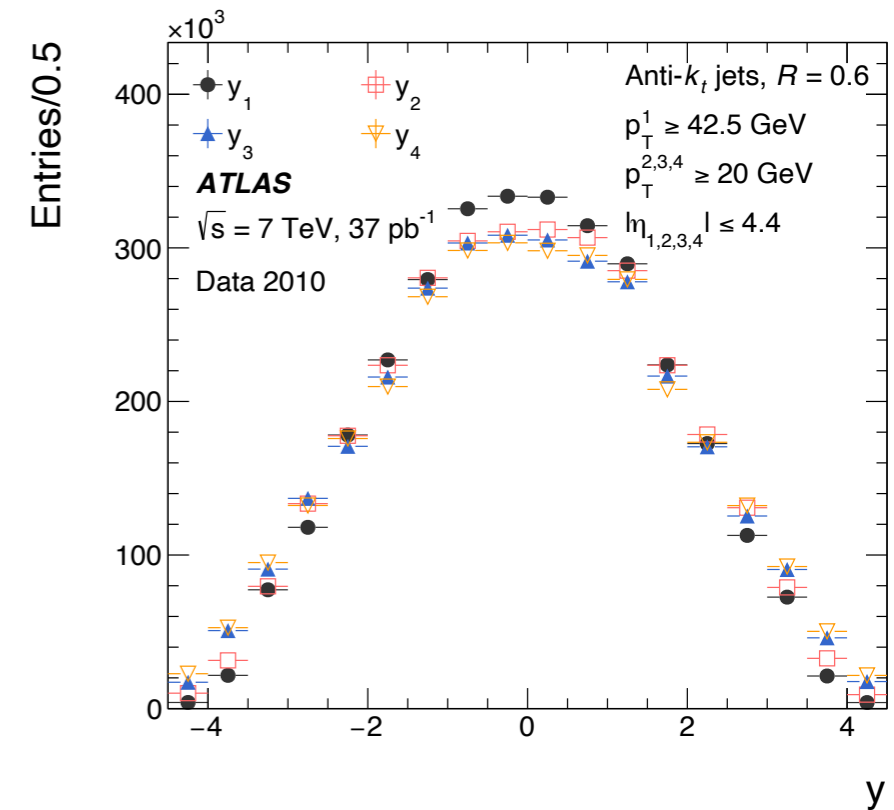
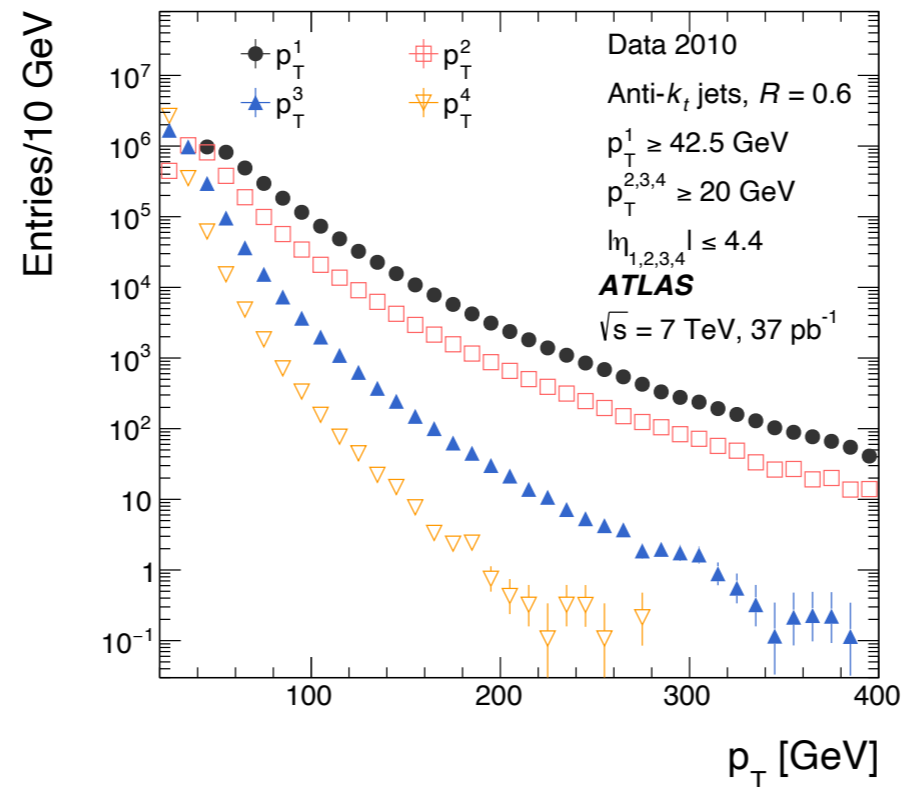
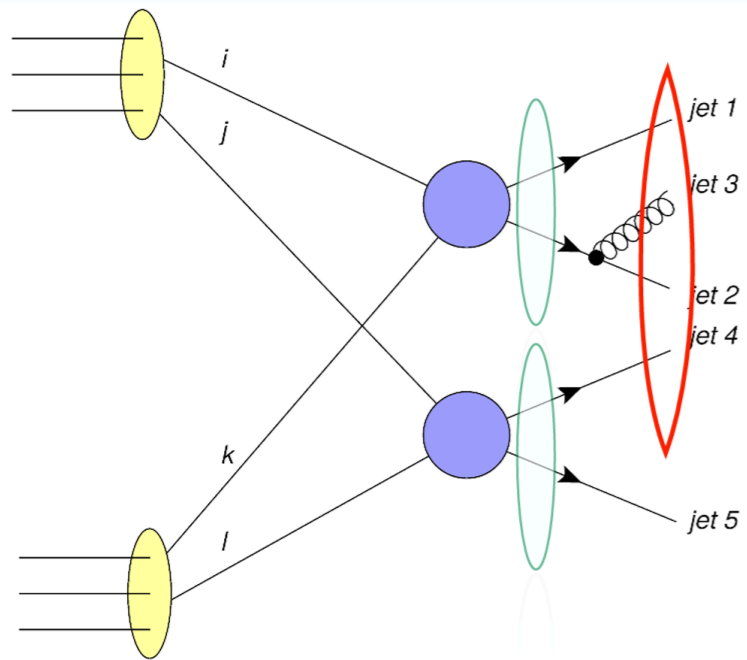
- This value of σ_{eff} is consistent with values previously measured in other experiments at lower centre-of-mass energies

Four-jet study

[JHEP 11 \(2016\) 110](#)

- Measure the hard DPS contribution with the inclusive 4-jet events
- Dataset: 36 pb^{-1} @ 7 TeV collected in 2010, $\langle \mu \rangle = 0.4$
- Anti-kt jets with $R = 0.6$, $p_T > 20 \text{ GeV}$ and $|\eta| \leq 4.4$
- Event categories:
 - SPS: No jets matched to secondary scatter parton
 - sDPS: 1 jet matched to secondary scatter parton
 - cDPS: 2 jet matched to secondary scatter parton

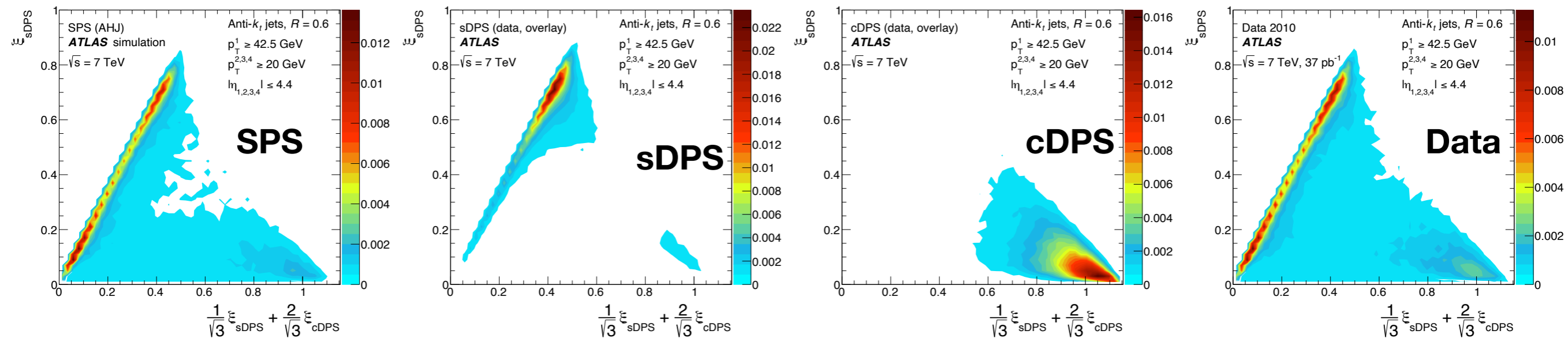
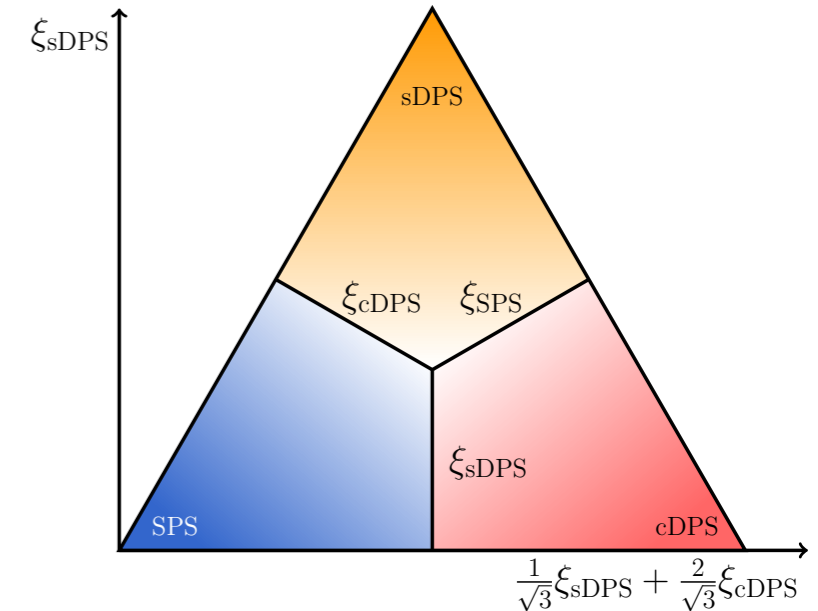
$$f_{\text{DPS}} = f_{\text{sDPS}} + f_{\text{cDPS}}$$



Four-jet study

- An artificial neural network (NN) is trained to perform event classification
 - Input: 21 variables consisting of all possible dijet combinations
 - Output: probabilities for an event to be more like SPS(δ_{SPS}), cDPS(δ_{sDPS}) or sDPS(δ_{cDPS}), with $\delta_{SPS} + \delta_{sDPS} + \delta_{cDPS} = 1$

JHEP 11 (2016) 110



- Good separation between event categories
 - The separation between SPS and sDPS is difficult
- Fit MC profiles to data: $D = (1 - f_{cDPS} - f_{sDPS})M_{SPS} + f_{cDPS}M_{cDPS} + f_{sDPS}M_{sDPS}$

Four-jet study

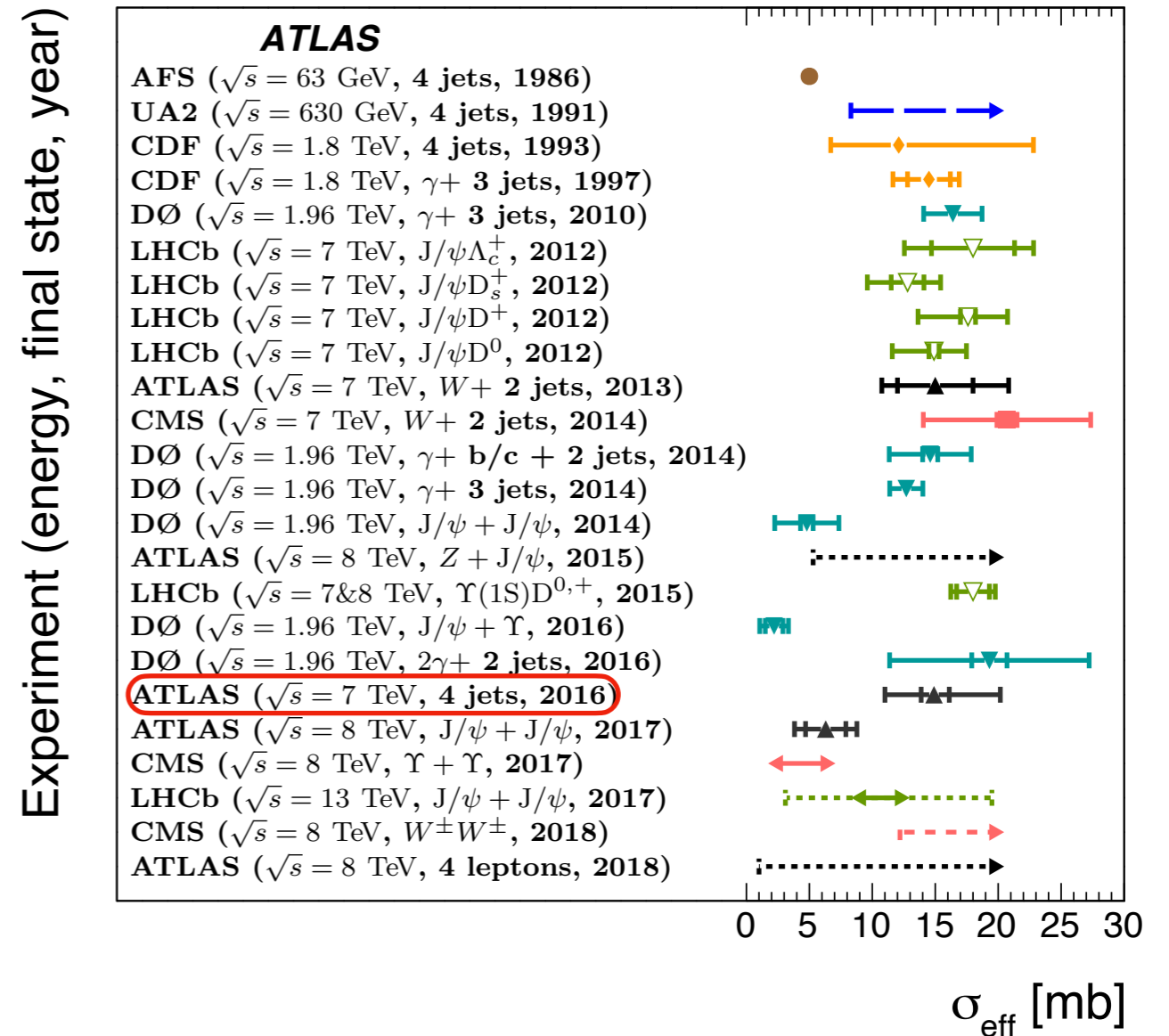
[JHEP 11 \(2016\) 110](#)

- The extracted f_{DPS} is $f_{\text{DPS}} = 0.092^{+0.005}_{-0.011}(\text{stat.})^{+0.033}_{-0.037}(\text{syst.})$, with $\sim 40\%$ contribution from f_{sDPS}

- The measurements of the dijet and four-jet cross sections can be used to calculate the effective cross section:

$$\sigma_{\text{eff}} = 14.9^{+1.2}_{-1.0}(\text{stat.})^{+5.1}_{-3.8}(\text{syst.}) \text{ mb}$$

- It is consistent within the quoted uncertainties with previous measurements



Four-lepton study

- Measure the hard DPS contribution with the inclusive 4-lepton events
- Dataset: 20.2 fb^{-1} @ 8 TeV
- Events with at least four leptons (electrons or muons) which can form two same-flavor opposite-charge (SFOC) lepton pairs are selected

- **Pairing:**

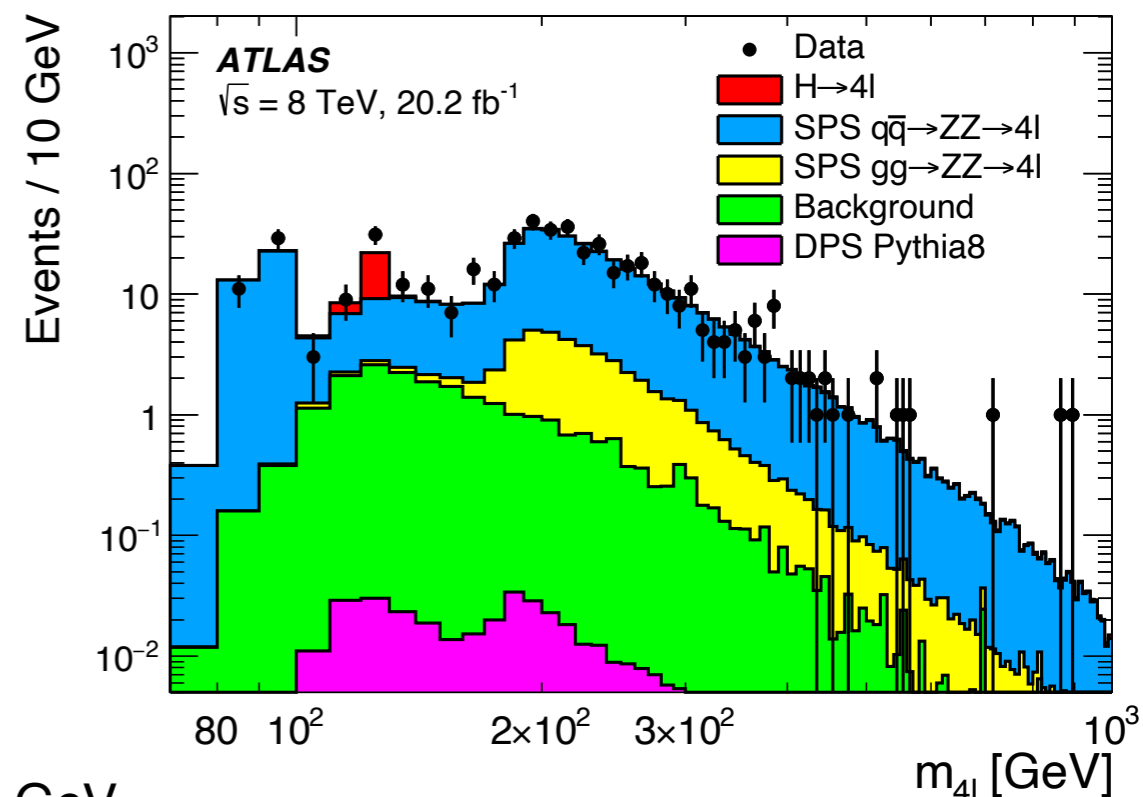
- Leading pair: SFOC lepton pair with smallest $|m_Z - m_{\ell\ell}|$
- Second pair: remaining SFOC with largest $m_{\ell\ell}$

- **Lepton selection:**

- $p_T > 7$ (6 if muon) GeV, $|\eta| < 2.5$ (2.7 if muon)

- **Event selection:**

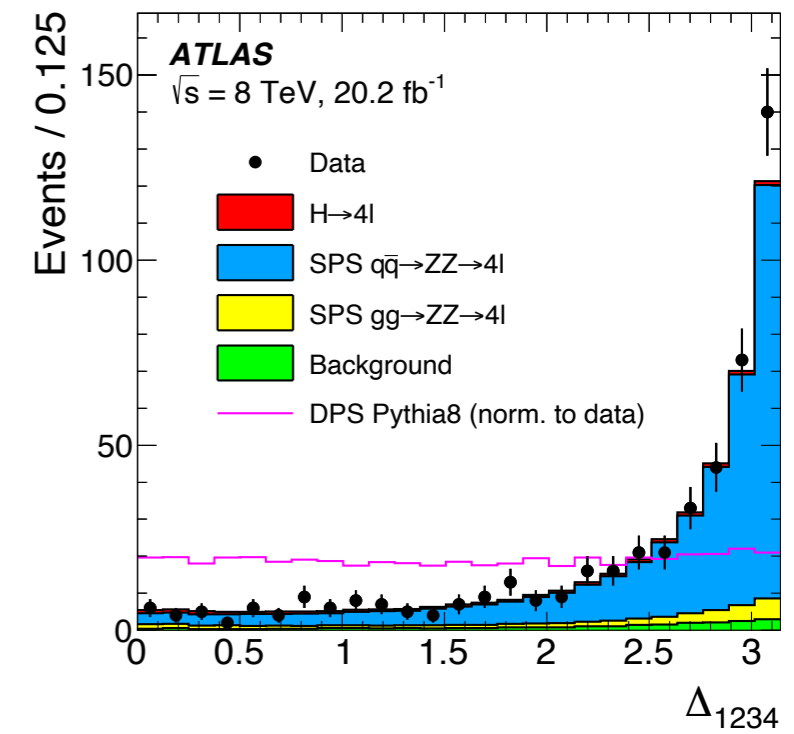
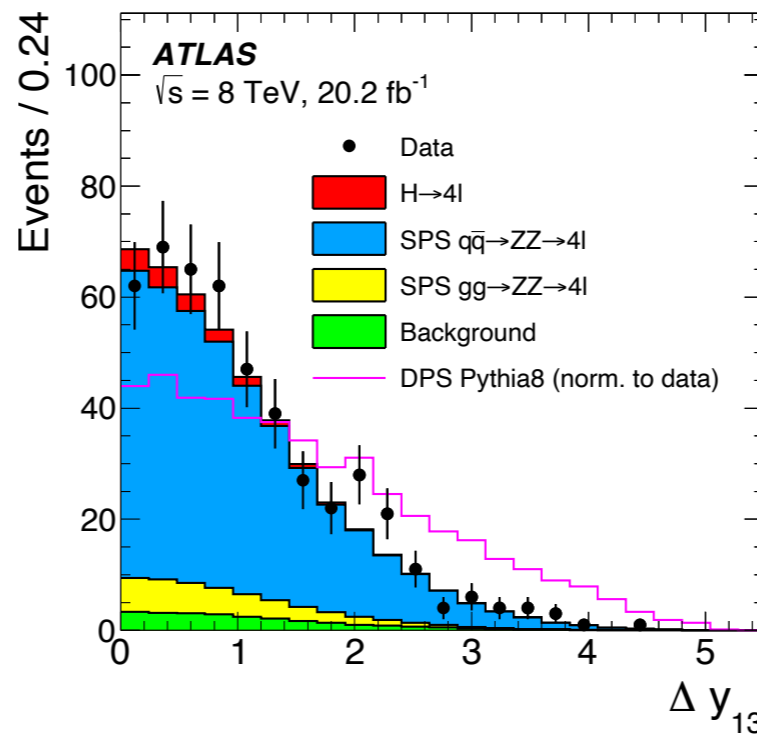
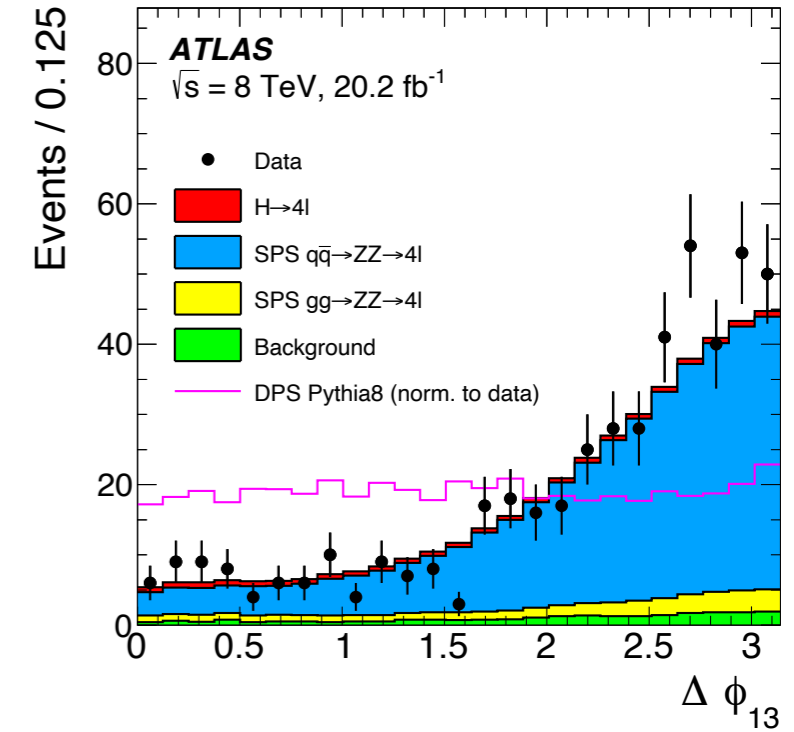
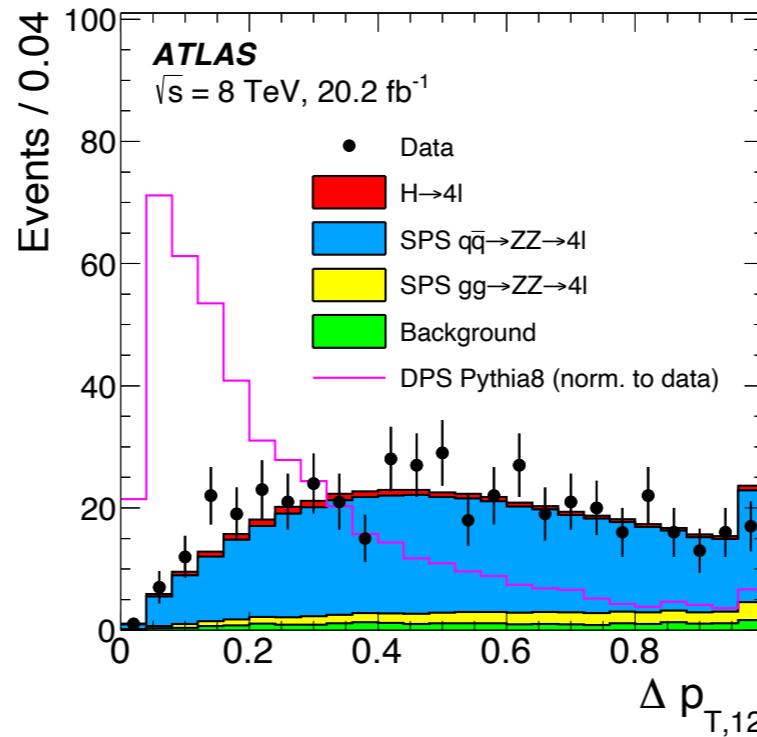
- Lepton $p_T^{\ell_1, \ell_2, \ell_3, \ell_4} > 20, 15, 10$ (8 if muon), 7 (6 if muon) GeV
- Lepton pair mass: $50 < m_{\text{leading}} < 120$ GeV, $12 < m_{\text{sub-leading}} < 120$ GeV
- Separation: $\Delta R(\ell_i, \ell_j) > 0.1(0.2)$ for same (different) flavor leptons
- J/ψ veto: $m(\ell_i^+, \ell_j^-) > 5$ GeV
- Four-lepton mass: $80 < m_{4\ell} < 1000$ GeV



Four-lepton study

- NN is applied to discriminate SPS and DPS
- Input: 21 variables with all the lepton combinations ($\Delta p_{T,ij}$, $\Delta\phi_{ij}$, Δy_{ij} and $\Delta_{ijkm} = |\phi_{i+j} - \phi_{k+m}|$)

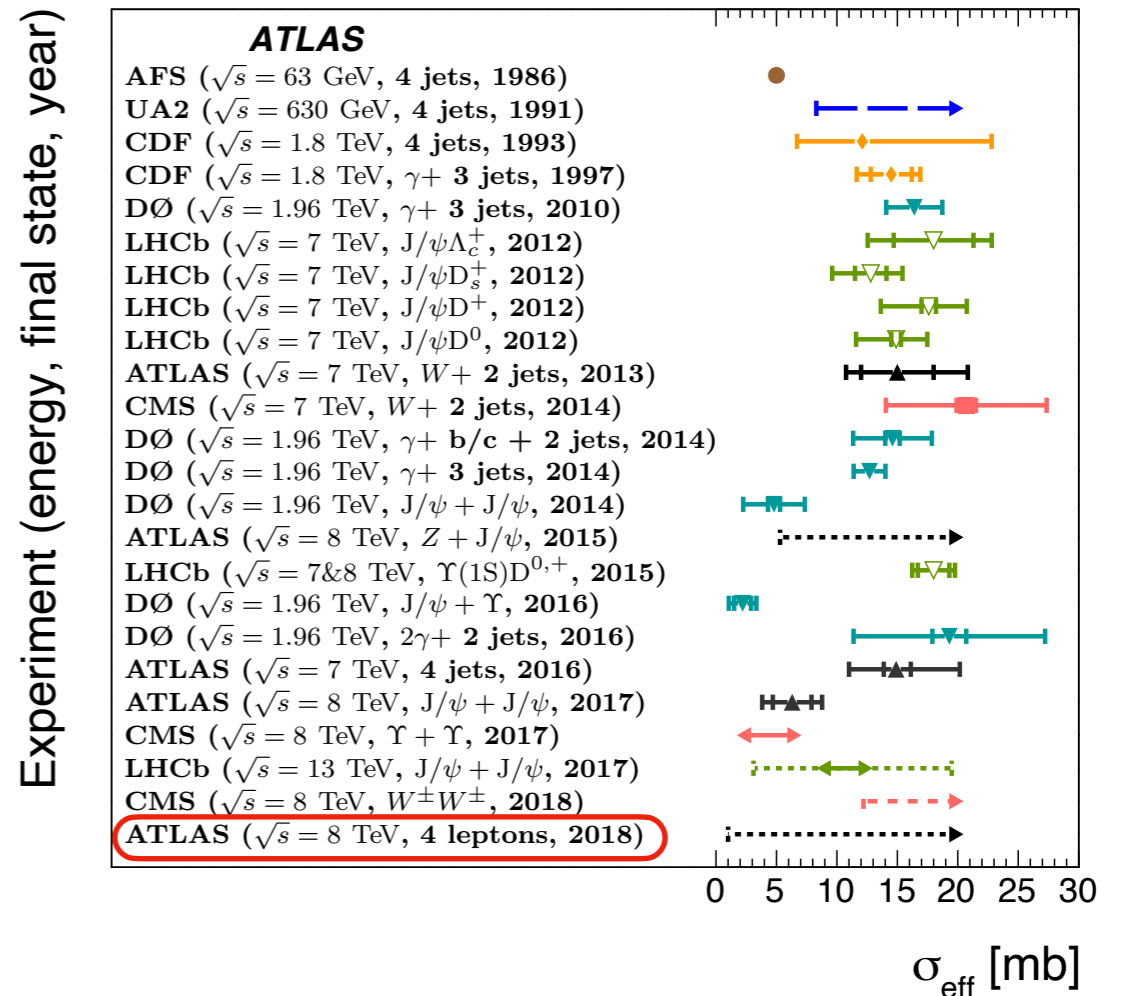
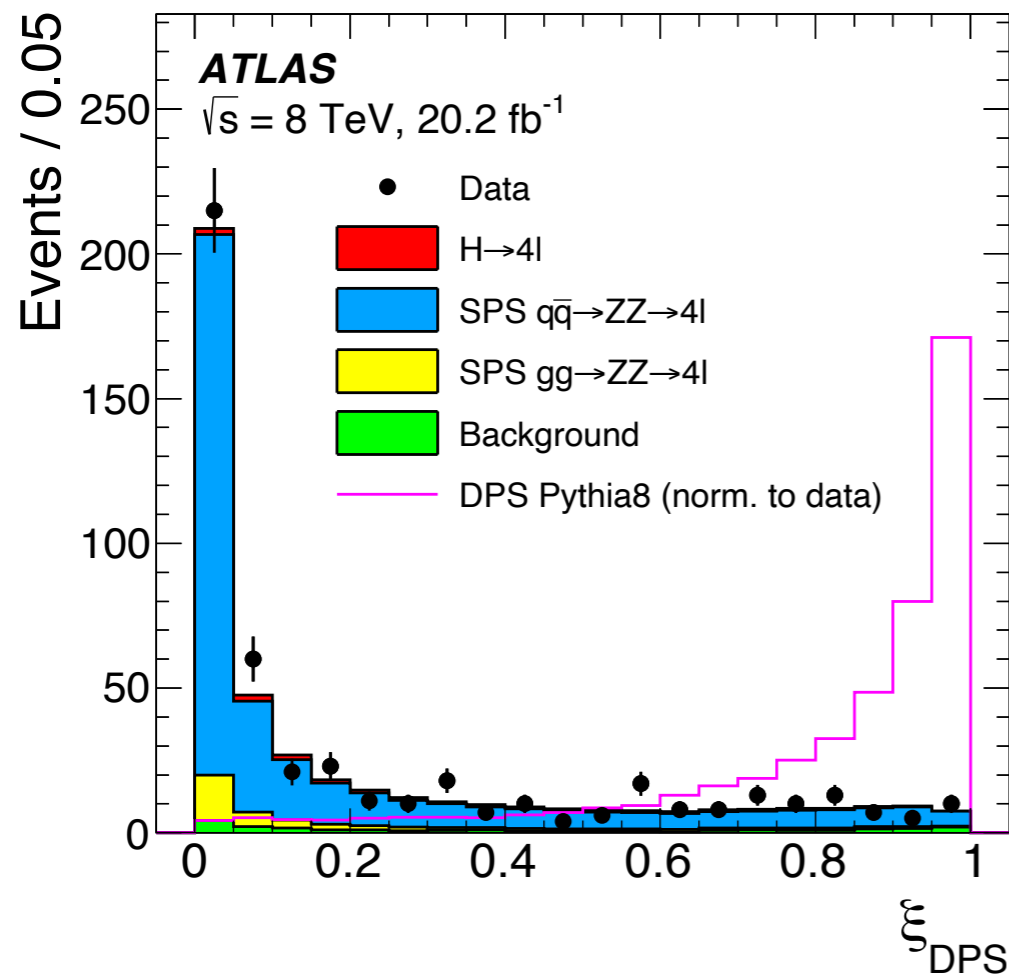
Phys.Lett. B 790 (2019) 595



Four-lepton study

[Phys.Lett. B 790 \(2019\) 595](#)

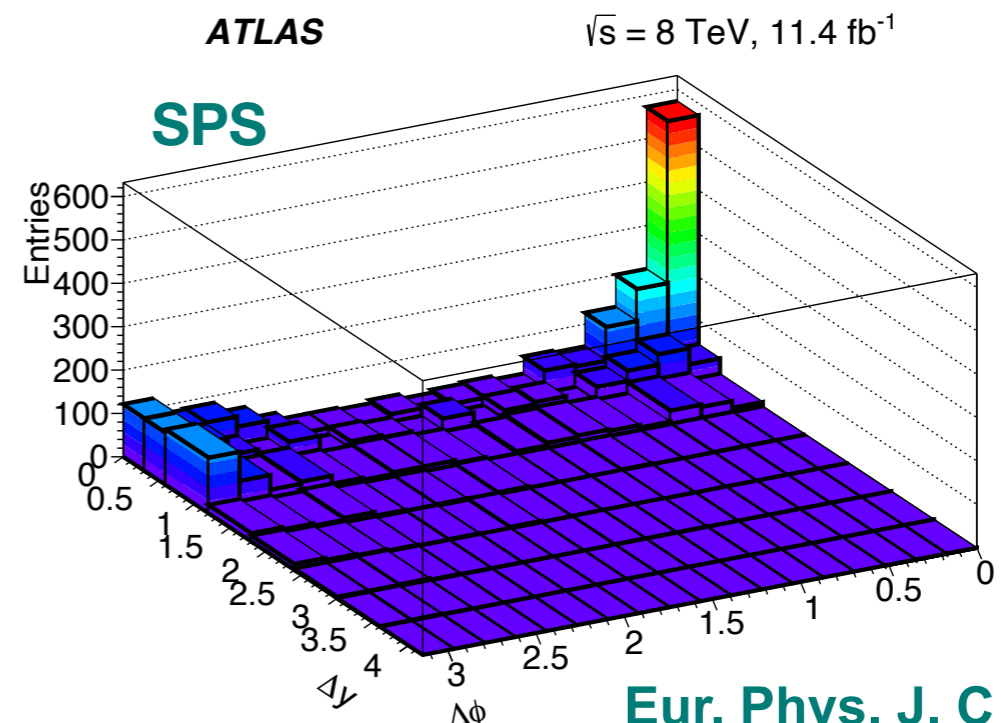
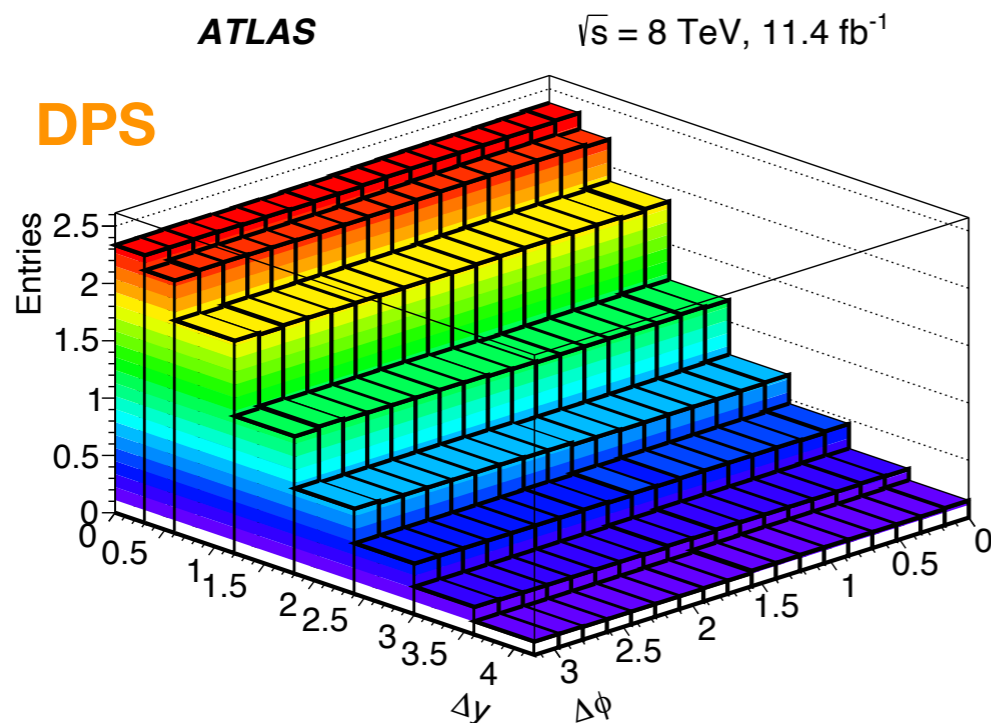
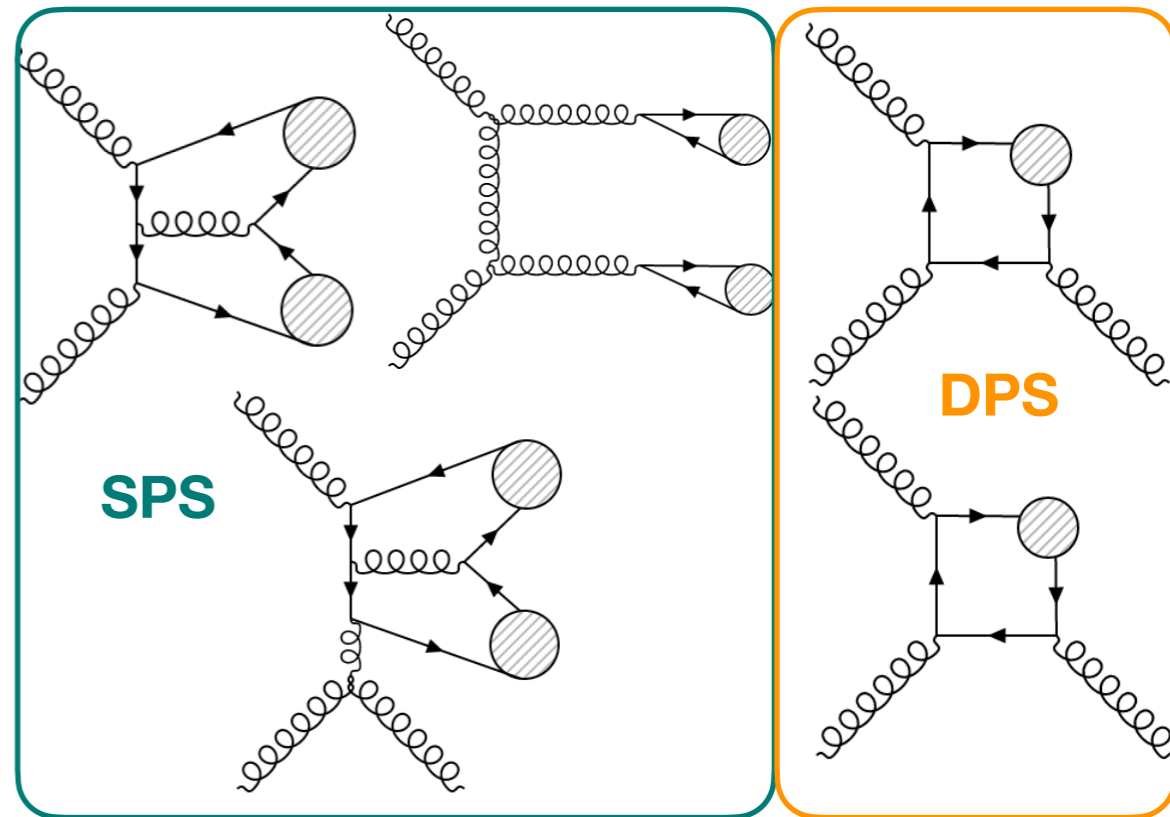
- Perform fit on NN output variable ξ_{DPS} to determine DPS fraction
 $f_{\text{DPS}} = -0.009 \pm 0.017(\text{stat.}) \pm 0.003(\text{sys.})$
- Translate into the upper limit $f_{\text{DPS}} < 0.042$ at 95% CL
- The lower limit on σ_{eff} is extracted to be >1.0 mb at 95% CL



di- J/ψ study

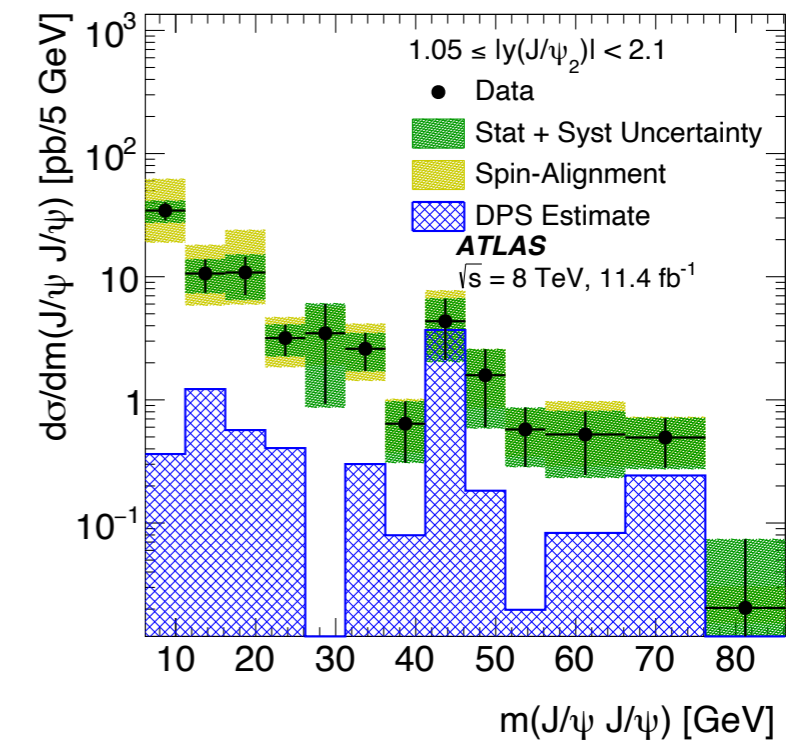
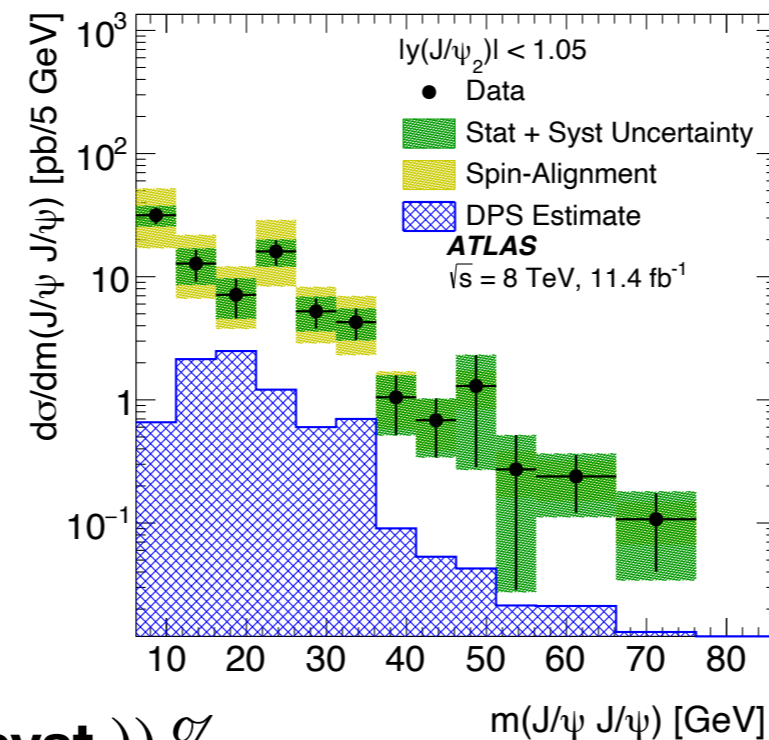
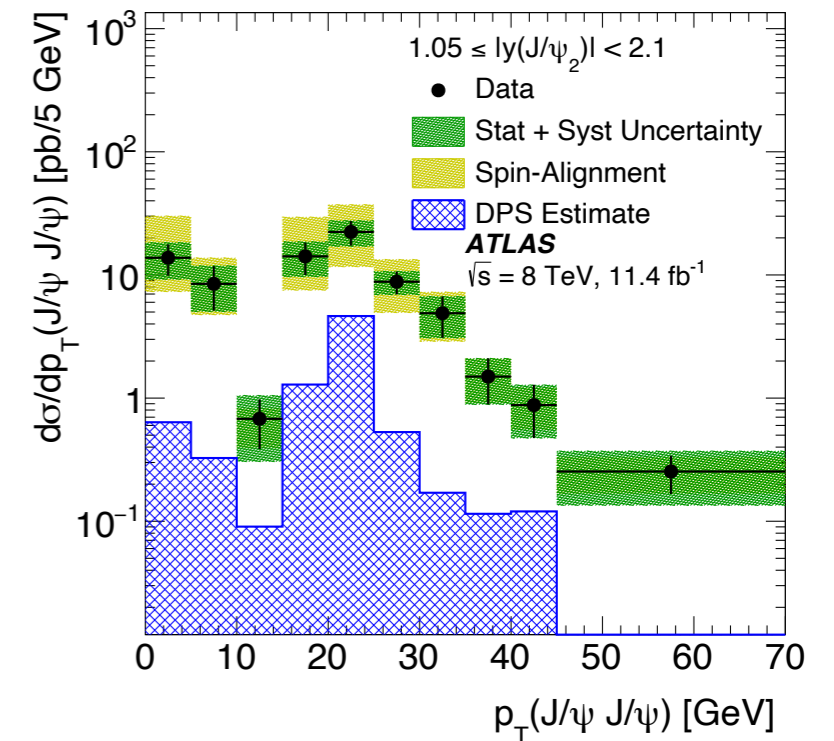
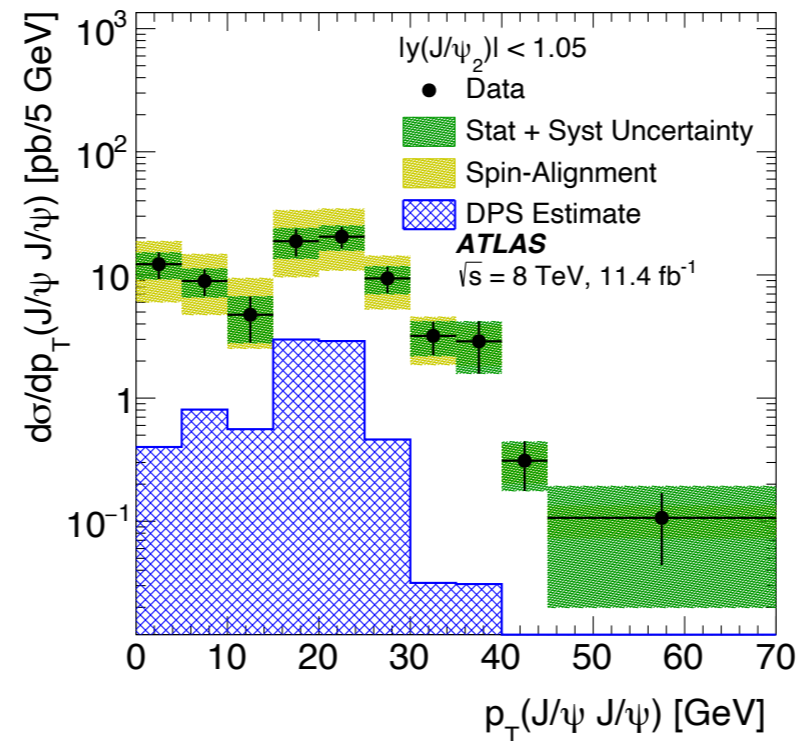
- Measure the hard DPS contribution with prompt di- J/ψ events
- Dataset: 11.4 fb^{-1} @ 8 TeV collected in 2012
- Selections:
 - J/ψ dimuon trigger with muon p_T threshold of 4 GeV
 - $p_T^\mu > 2.5 \text{ GeV}$ and $|\eta^\mu| < 2.3$
 - $2.8 \leq m(\mu\mu) \leq 3.4 \text{ GeV}$
 - $|y^{J/\psi}| < 2.1$ and $p_T^{J/\psi} > 8.5 \text{ GeV}$
 - The distance between the two J/ψ decay vertices along the beam direction $|d_z| < 1.2 \text{ mm}$
 - L_{xy} uncertainty $< 0.3 \text{ mm}$
- SPS and DPS event weights are derived with 2D data-driven templates of Δy and $\Delta\phi$ between the two J/ψ candidates

$$J/\psi \rightarrow \mu^+ \mu^-$$



di- J/ψ study

- The cross-section is measured in two rapidity regions as a function of the di- J/ψ p_T and invariant mass with assumption of unpolarised J/ψ mesons
- There are two peaks in the di- J/ψ p_T distribution
 - Low p_T : two J/ψ are produced back-to-back in an away topology
 - High p_T : two J/ψ are produced in the same direction in a towards topology



$$f_{\text{DPS}} = (9.2 \pm 2.1(\text{stat.}) \pm 0.5(\text{syst.})) \%$$

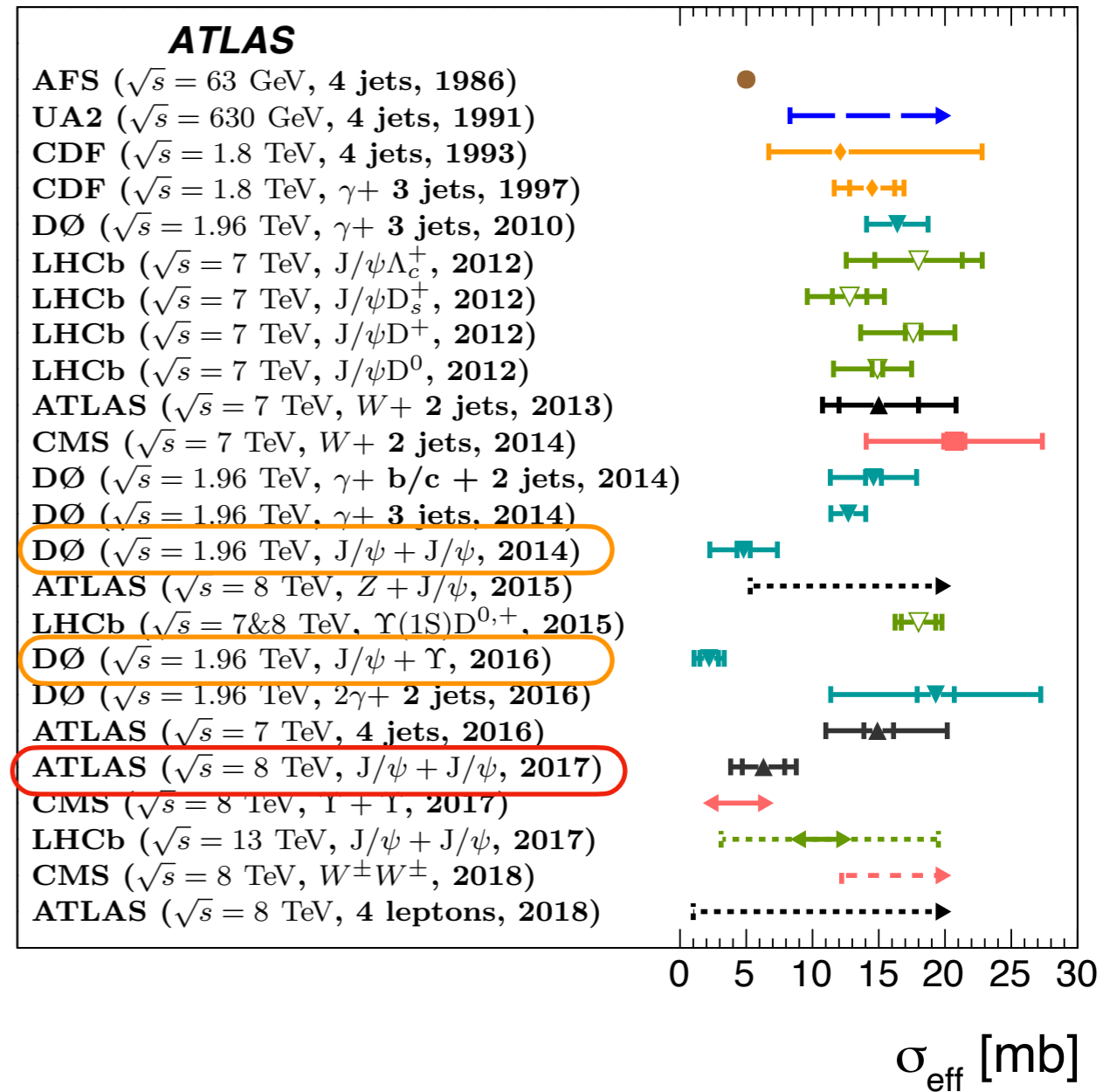
di- J/ψ study

- With $\sigma_{J/\psi}$ obtained from ATLAS measurements (Eur. Phys. J. C 76 (2016) 283) and f_{DPS} as inputs, the effective cross-section is measured to be:

$$\sigma_{\text{eff}} = 6.3 \pm 1.6(\text{stat.}) \pm 1.0(\text{syst.}) \pm 0.1(\text{BF}) \pm 0.1(\text{lumi}) \text{ mb}$$

- Close to **D0 results** and lower than other measurements

Experiment (energy, final state, year)



Z + J/ψ study

Eur. Phys. J. C 75 (2015) 229

- Study DPS in the production of prompt and non-prompt J/ψ (→ μ⁺μ⁻) in association with a Z boson (→ ℓ⁺ℓ⁻)
- Dataset: 20.3 fb⁻¹ @ 8 TeV

Event selections

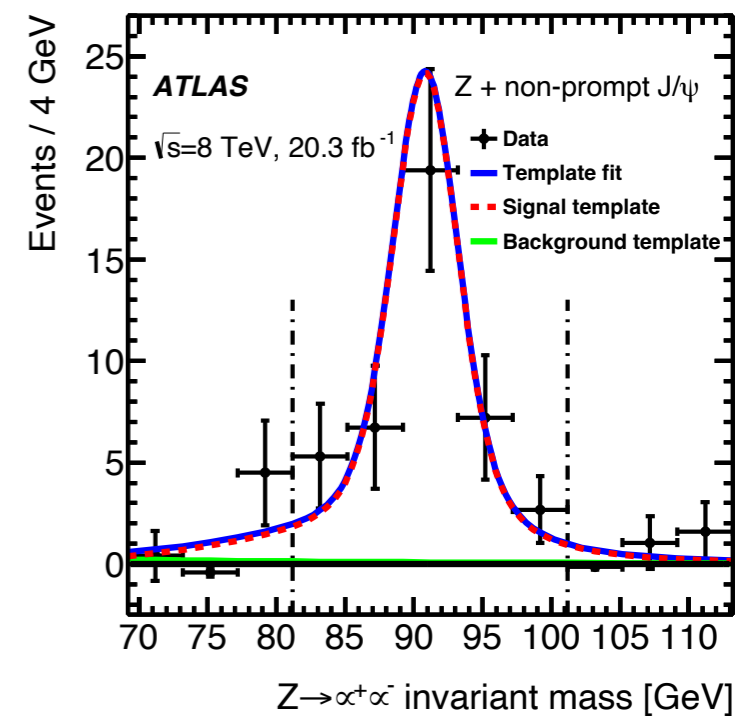
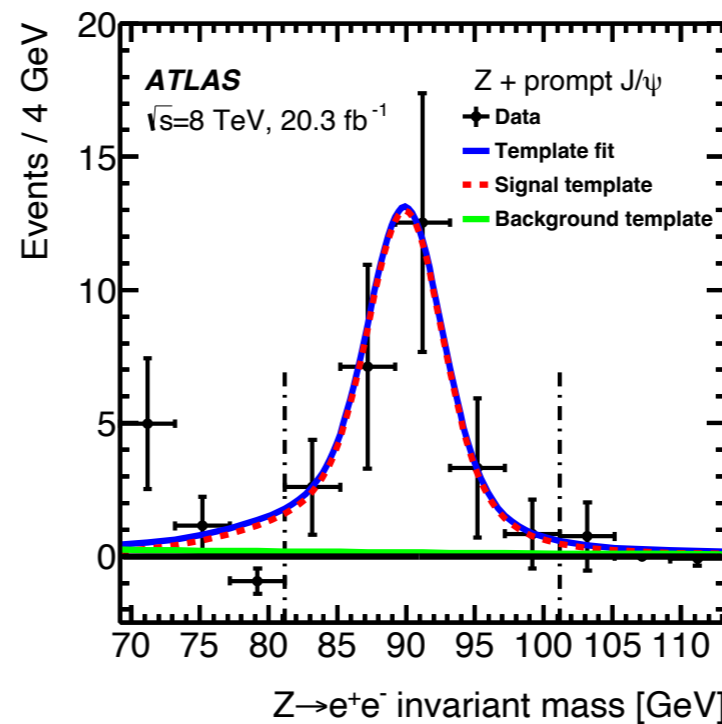
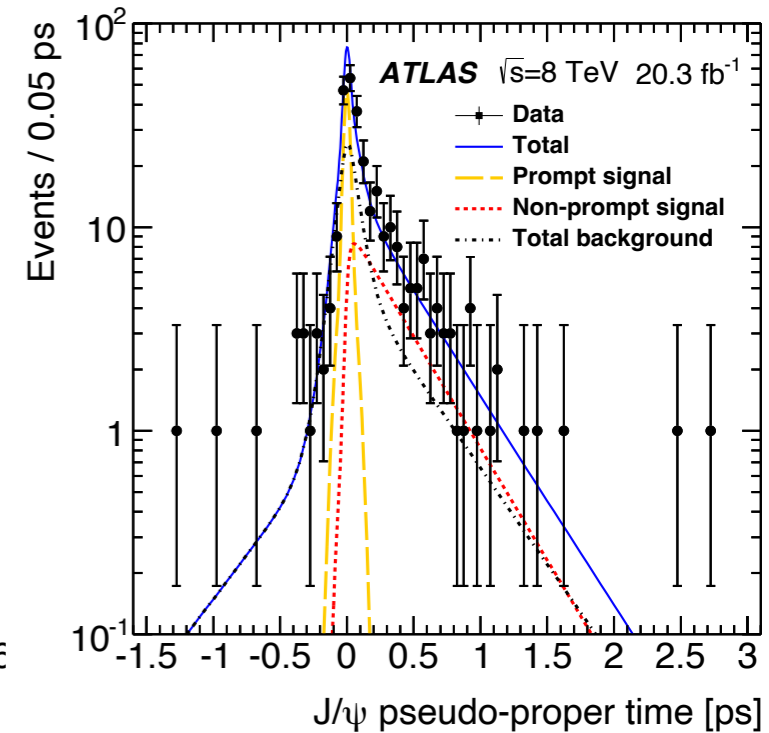
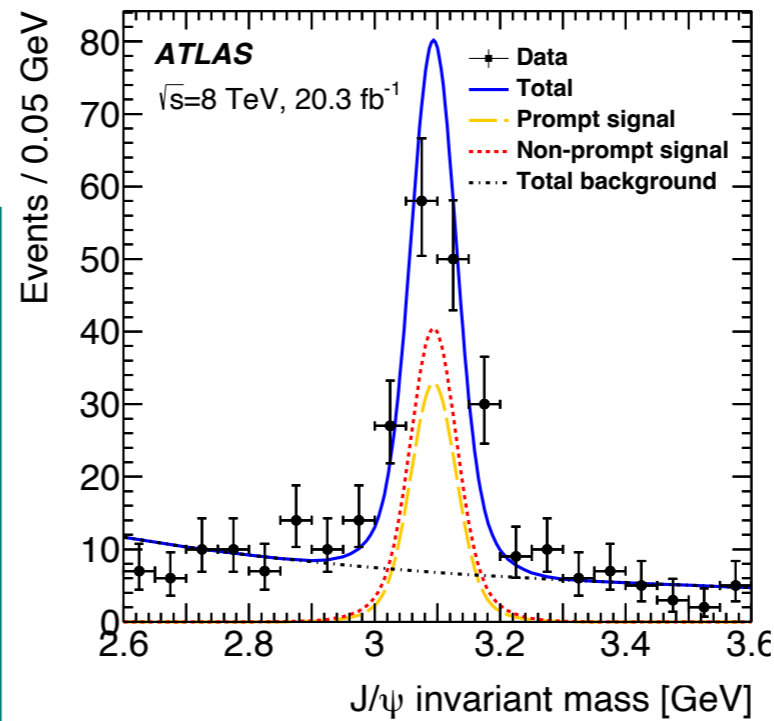
Z boson:

- $p_T^{\text{trigger } \ell} > 25 \text{ GeV}, p_T^{\text{sub-leading } \ell} > 15 \text{ GeV},$
- $|\eta^\ell| < 2.5, |m^Z - 91.1876| < 10 \text{ GeV}$

J/ψ:

- $2.6 < m^{J/\psi} < 3.6 \text{ GeV}$
- $8.5 < p_T^{J/\psi} < 100 \text{ GeV}, |y_{J/\psi}| < 2.1$
- $p_T(\text{leading } \mu) > 4 \text{ GeV}, |\eta(\text{leading } \mu)| < 2.5$
- Either $p_T(\text{sub-leading } \mu) > 2.5 \text{ GeV}, 1.3 \leq |\eta(\text{sub-leading } \mu)| < 2.5$
- Or $p_T(\text{sub-leading } \mu) > 3.5 \text{ GeV}, |\eta(\text{sub-leading } \mu)| < 1.3$

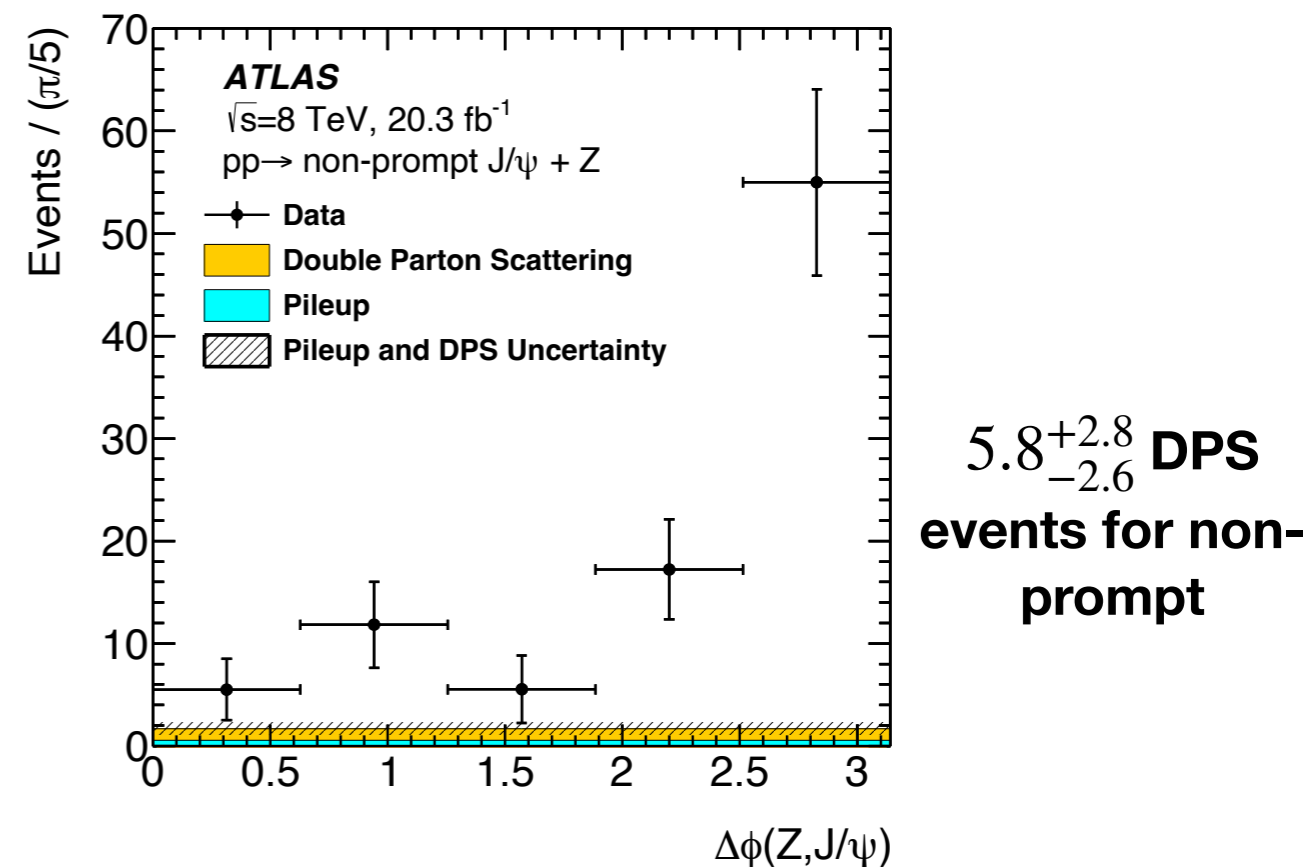
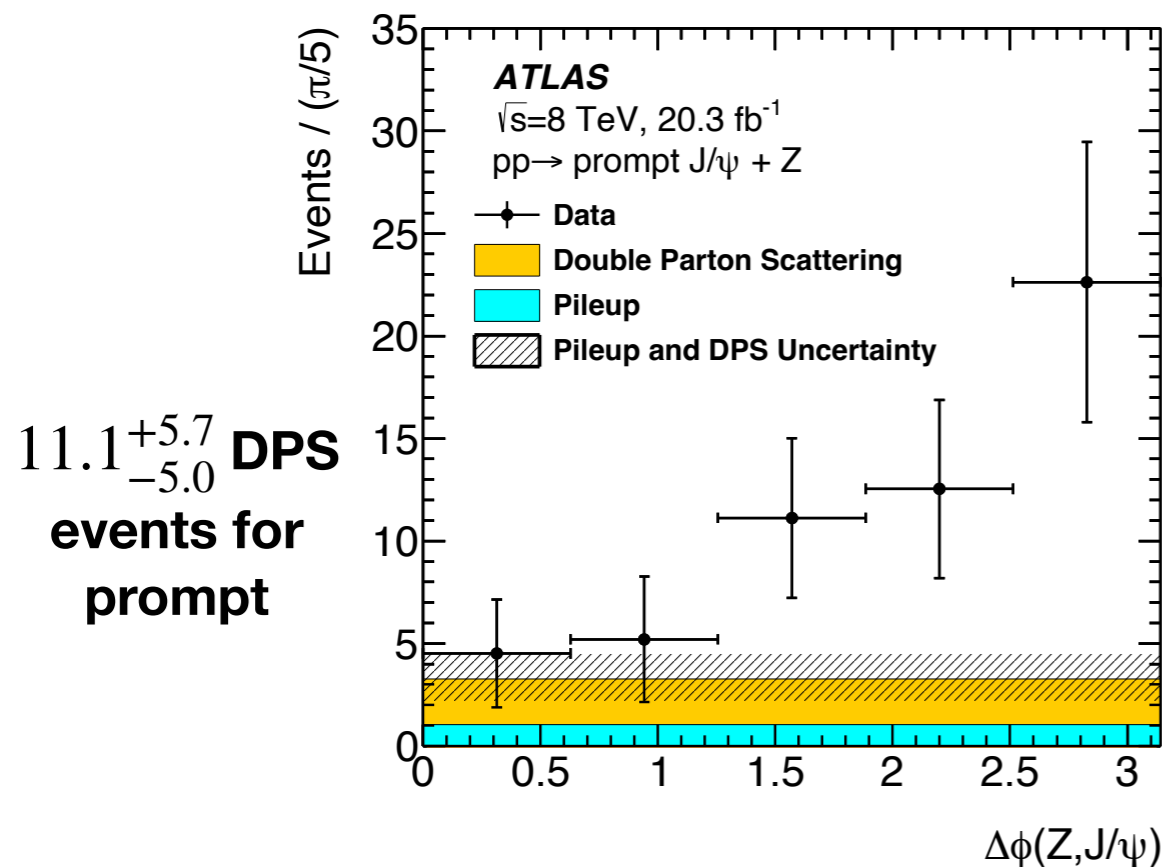
$$\text{Pseudo-proper time: } \tau = \frac{L_{xy} m^{J/\psi}}{p_T^{J/\psi}}$$



Z + J/ψ study

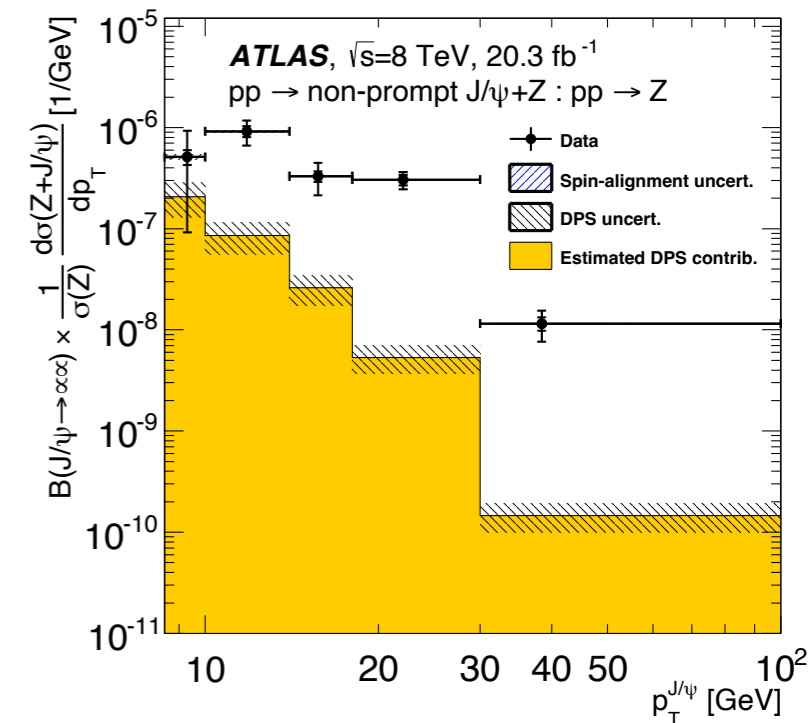
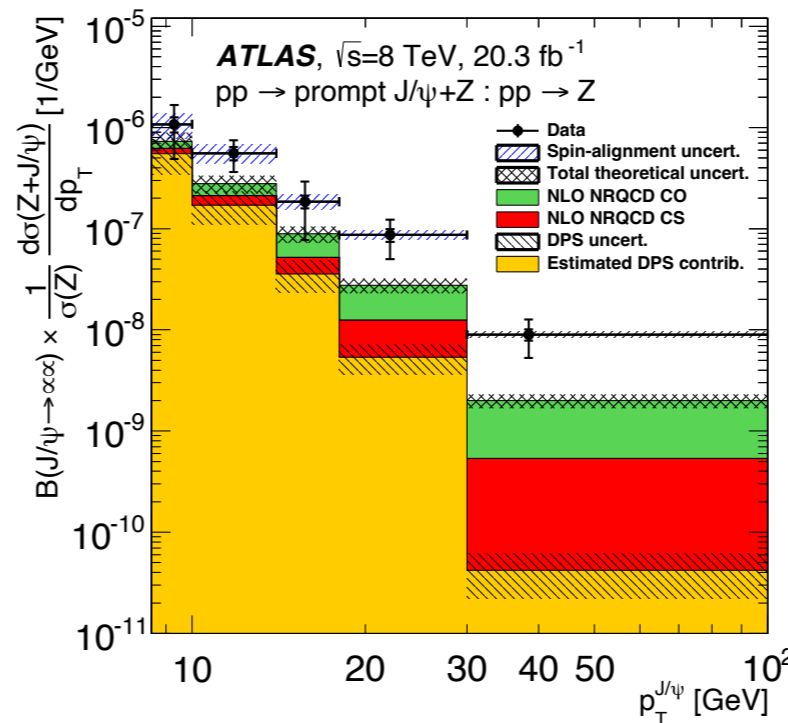
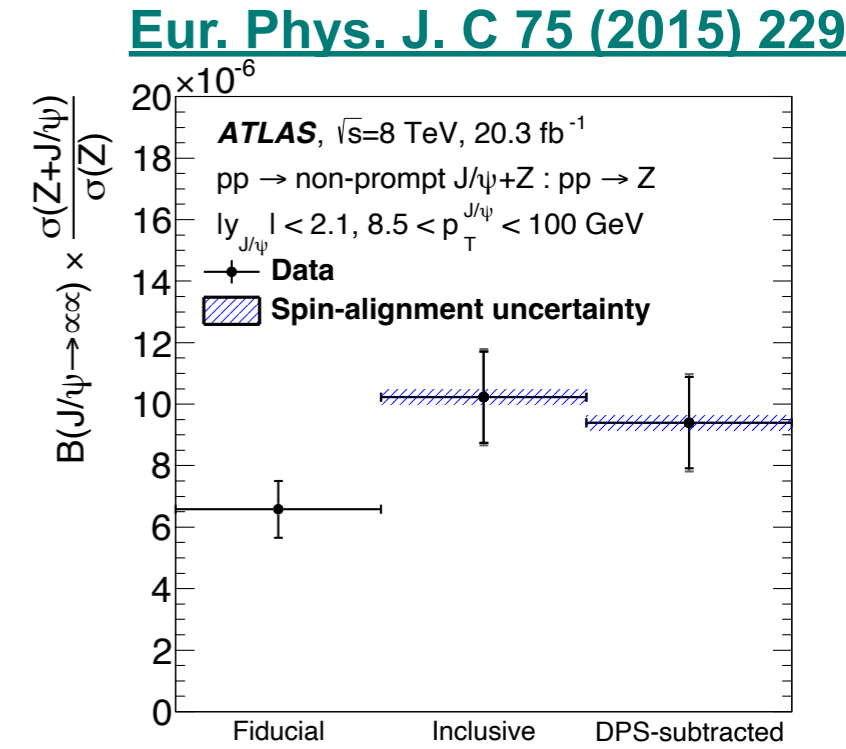
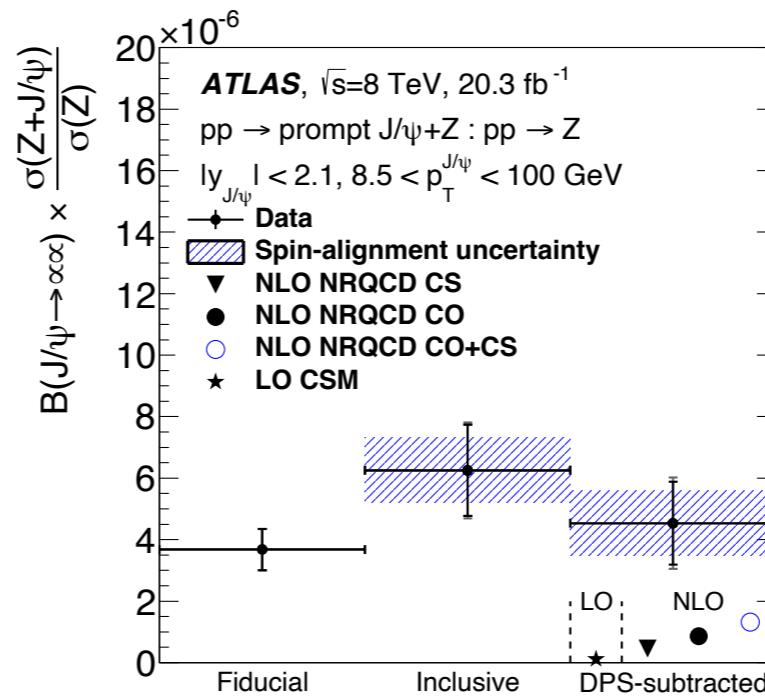
[Eur. Phys. J. C 75 \(2015\) 229](#)

- For a collision where a Z boson is produced, the probability that a J/ψ is produced in addition due to a second hard process is $P_{J/\psi|Z} = \sigma_{J/\psi} / \sigma_{\text{eff}}$
 - $\sigma_{J/\psi}$ is taken from ATLAS J/ψ cross-section measurement
 - σ_{eff} is taken to be $\sigma_{\text{eff}} = 15 \pm 3(\text{stat.})_{-3}^{+5}(\text{sys.})$ mb according to ATLAS measurement in W+2-jet events



Z + J/ψ study

- For prompt and non-prompt production, the cross-section ratios were measured for $8.5 < p_T^{J/\psi} < 100$ GeV and $|y_{J/\psi}| < 2.1$
- Production of a $J/\psi \rightarrow \mu^+ \mu^-$ meson in association with a Z boson occurs approximately 10 times per million Z boson
- The inclusive differential cross-section ratio is measured as a function of $J/\psi p_T$ for both prompt and non-prompt
 - The observed p_T dependence is significantly harder than the inclusive J/ψ production [Nucl. Phys. B 850, 387–444 (2011)]
- For prompt, it's compared to NLO colour-singlet and colour-octet predictions
 - CO contribution is larger than CS by a factor of ~ 2 , and becomes increasingly dominant for higher p_T



W + J/ψ study

JHEP 01 (2020) 095

- Study DPS in the production of prompt J/ψ ($\rightarrow \mu^+ \mu^-$) in association with a W boson ($\rightarrow \mu\nu$)
- Dataset: 20.3 fb^{-1} @ 8 TeV collected

W boson

W^\pm boson selection

At least one isolated muon that originates < 1 mm from primary vertex along z -axis

$$p_T (\text{trigger muon}) > 25 \text{ GeV}$$

$$|\eta^\mu| < 2.4$$

Missing transverse momentum $> 20 \text{ GeV}$

$$m_T(W^\pm) > 40 \text{ GeV}$$

$$|d_0|/\sigma_{d_0} < 3$$

J/ψ

J/ψ selection

$$2.4 < m(\mu^+ \mu^-) < 3.8 \text{ GeV}$$

$$8.5 < p_T^{J/\psi} < 150 \text{ GeV}, |y_{J/\psi}| < 2.1$$

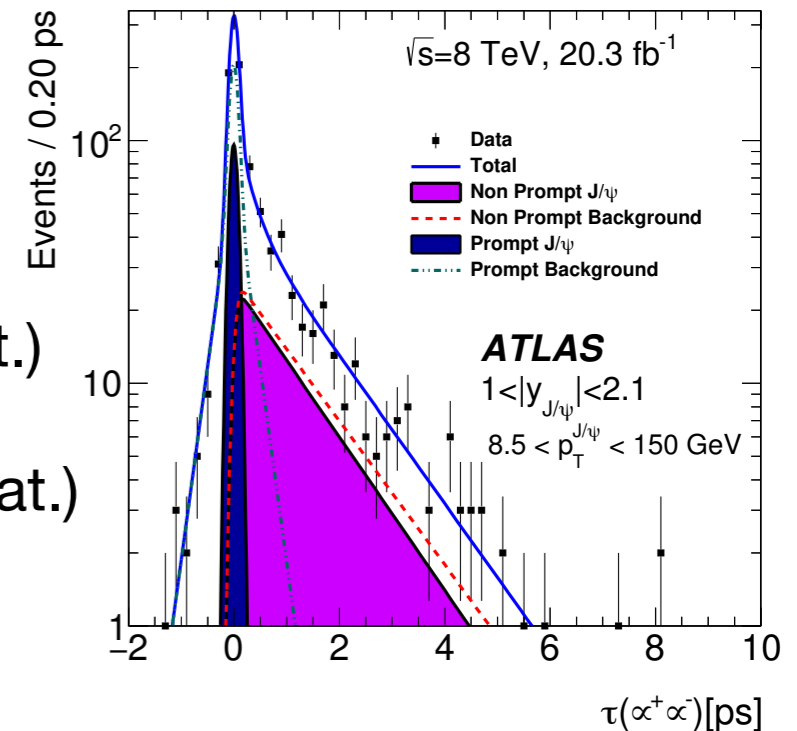
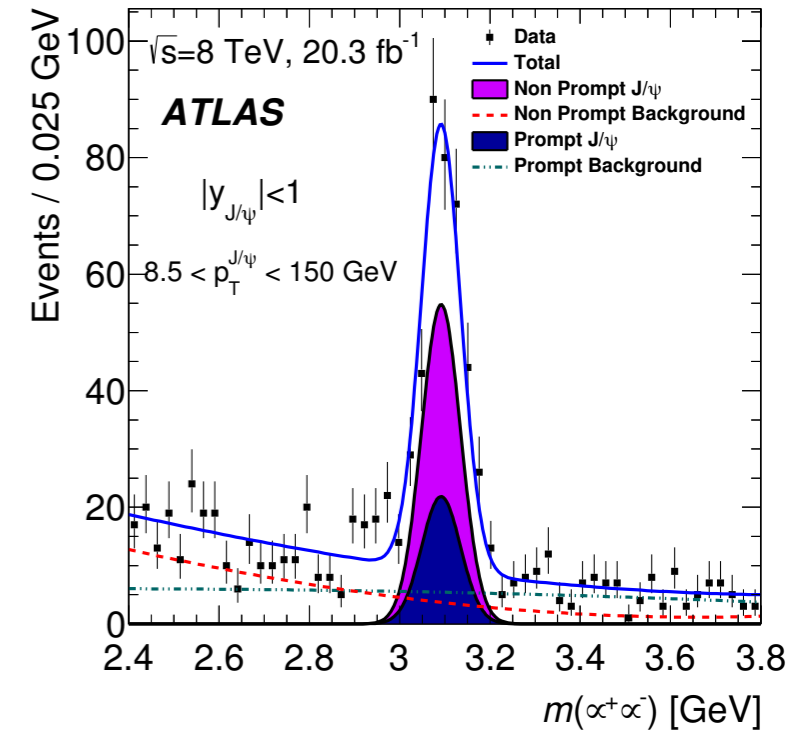
$$p_T^{\mu_1} > 4 \text{ GeV}, |\eta^{\mu_1}| < 2.5$$

$$\left\{ \begin{array}{l} \text{either } p_T^{\mu_2} > 2.5 \text{ GeV}, \quad 1.3 \leq |\eta^{\mu_2}| < 2.5 \\ \text{or } p_T^{\mu_2} > 3.5 \text{ GeV}, \quad |\eta^{\mu_2}| < 1.3 \end{array} \right\}$$

- Prompt signal yields:

- $|y_{J/\psi}| < 1$: 91 ± 14 (stat.)

- $1 < |y_{J/\psi}|$: 102 ± 17 (stat.)



$W + J/\psi$ study

[JHEP 01 \(2020\) 095](#)

- Based on the assumption that the two hard scatters are uncorrelated, the probability that a J/ψ is produced by a second hard process in an event containing a W boson is:

$$P_{J/\psi|W} = \frac{\sigma_{J/\psi}}{\sigma_{\text{eff}}}$$

- As it's unclear which σ_{eff} value to use, two values are chosen:

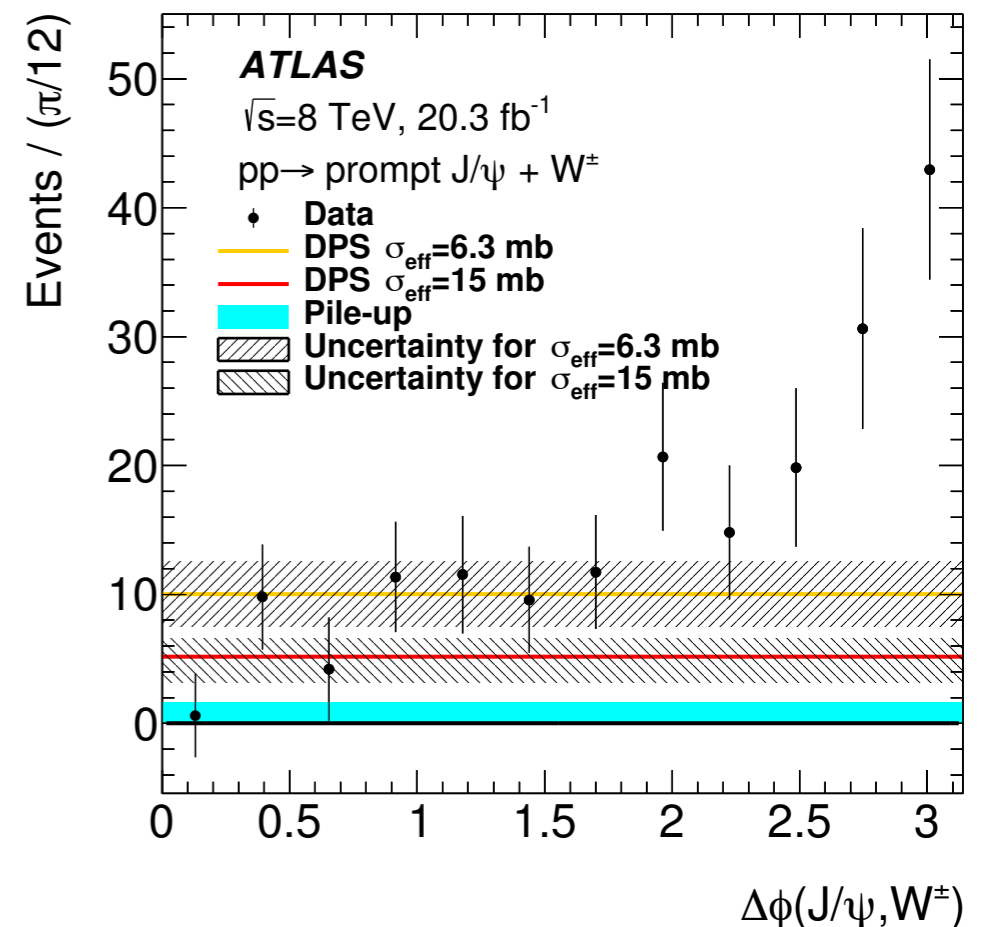
- $\sigma_{\text{eff}} = 15 \pm 3(\text{stat.})_{-3}^{+5}(\text{sys.})$ mb from $W+2$ -jet events
- $\sigma_{\text{eff}} = 6.3 \pm 1.6(\text{stat.}) \pm 1.0(\text{sys.})$ mb from prompt J/ψ pair production

- The estimated DPS fraction among inclusive signal yield is between $(31_{-12}^{+9})\%$ ($\sigma_{\text{eff}} = 15$ mb) and $(75 \pm 23)\%$

($\sigma_{\text{eff}} = 6.3$ mb)

- $\Delta\phi(J/\psi, W)$ distribution is measured with estimated DPS contribution

- DPS component should almost be flat, while SPS events peak at $\Delta\phi \approx \pi$ due to momentum conservation
- Both values of σ_{eff} are consistent with the data at low $\Delta\phi$



$W + J/\psi$ study

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- Cross-section ratios ($R_{J/\psi}$) are measured in the region $8.5 < p_T^{J/\psi} < 150$ GeV and $|y_{J/\psi}| < 2.1$

- **Fiducial** (in the J/ψ fiducial region):

$$R_{J/\psi}^{\text{fid}} = (2.2 \pm 0.3 \pm 0.7) \times 10^{-6}$$

- **Inclusive** (with J/ψ acceptance and the unknown J/ψ spin-alignment taken into account):

$$R_{J/\psi}^{\text{incl}} = (5.3 \pm 0.7 \pm 0.8_{-0.7}^{+1.5}) \times 10^{-6}$$

$$\sigma_{\text{eff}} = 15_{-4.2}^{+5.8} \text{ mb}$$

- **DPS subtracted:**

$$R_{J/\psi}^{\text{DPSsub}} = (3.6 \pm 0.7_{-1.0}^{+1.1} \pm 1.5_{-0.7}^{+1.5}) \times 10^{-6},$$

$$[\sigma_{\text{eff}} = 15_{-4.2}^{+5.8} \text{ mb}]$$

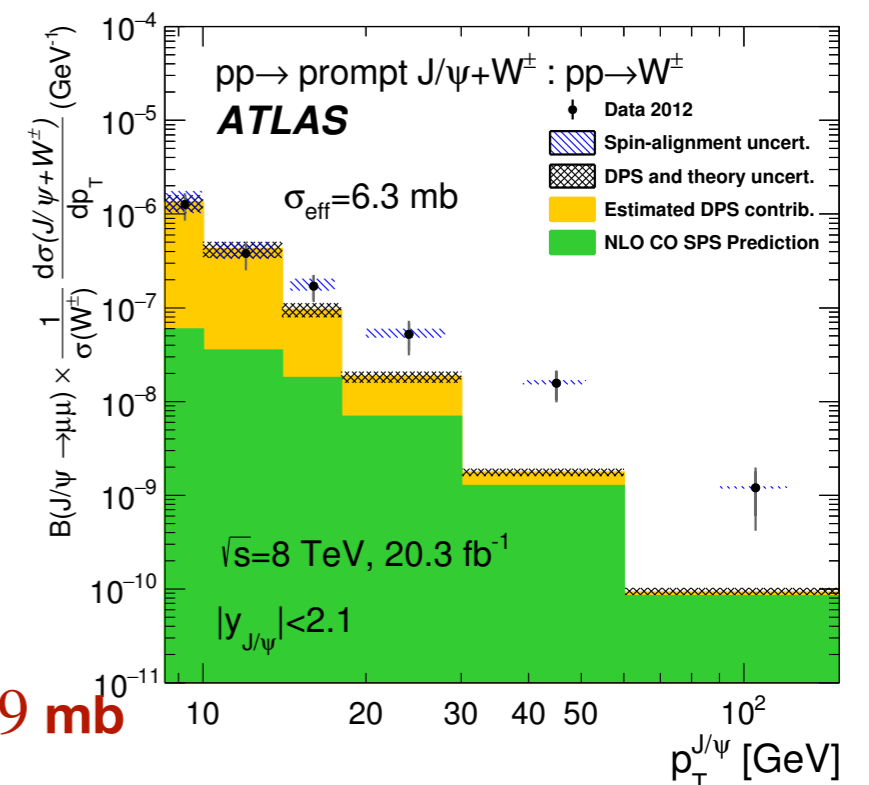
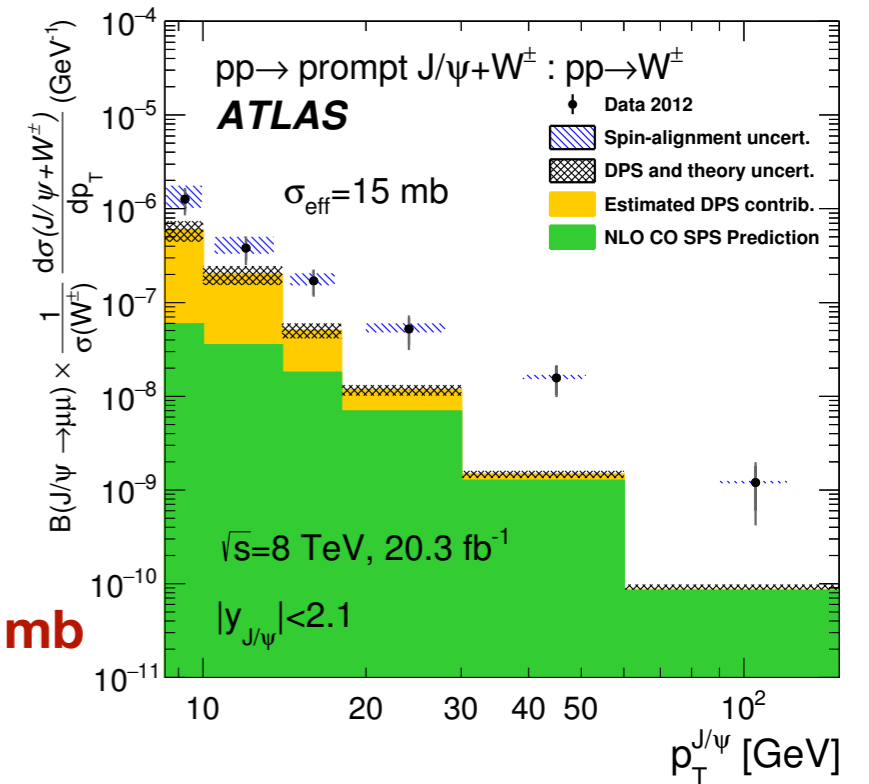
$$R_{J/\psi}^{\text{DPSsub}} = (1.3 \pm 0.7 \pm 1.5_{-0.7}^{+1.5}) \times 10^{-6},$$

$$[\sigma_{\text{eff}} = 6.3 \pm 1.9 \text{ mb}]$$

- Neither value of σ_{eff} is able to correctly model the J/ψ

p_T dependence

$$\sigma_{\text{eff}} = 6.3 \pm 1.9 \text{ mb}$$



Summary

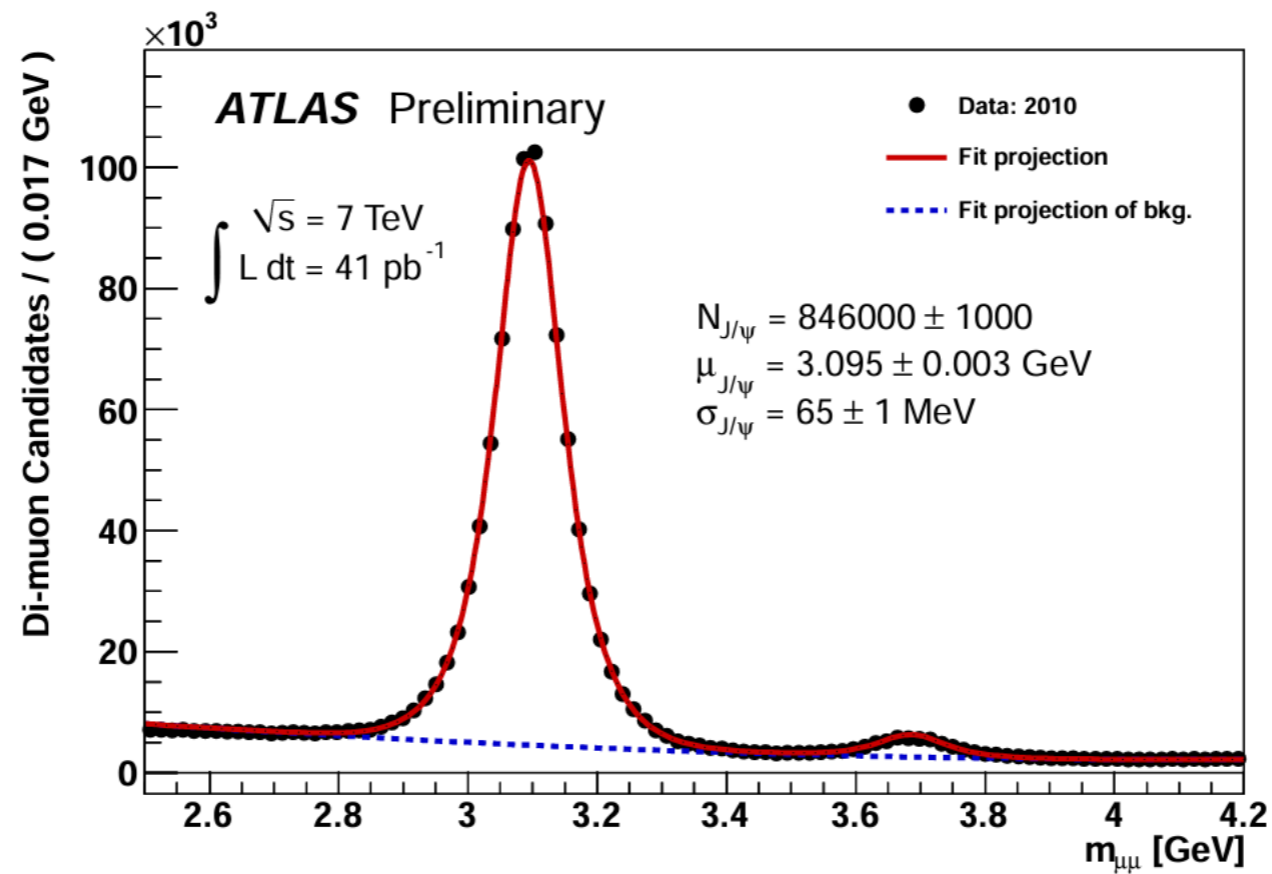
- DPS contribution with ATLAS Run 1 data are studied in various processes:
 - $W(\rightarrow \ell\nu) + 2\text{-jet}$
 - Four-jet
 - Four-lepton
 - Prompt J/ψ pair
 - $Z + J/\psi$ (prompt and non-prompt)
 - $W + J/\psi$
- The measured values of σ_{eff} are consistent within uncertainties
- New measurements with Run 2 data are on-going: stay tuned!

Thanks

BACKUP

Bphys di-muon trigger

- Dimuon invariant mass around the J/ψ mass based on the full sample collected in 2010 using single- and di-muon triggers



$W(\rightarrow \ell\nu) + 2\text{-jet study}$

Table 1. Summary of the fractional uncertainties on $f_{\text{DP}}^{(\text{D})}$.

Systematic source	Uncertainty (%)
Theory	10
Pile-up	13
Jet energy scale	12
Jet energy resolution	8
Background modelling and lepton response	11
Total systematic	24
Total statistical	17

- Various systematic sources are considered
 - The systematic uncertainty of pileup has the largest impact

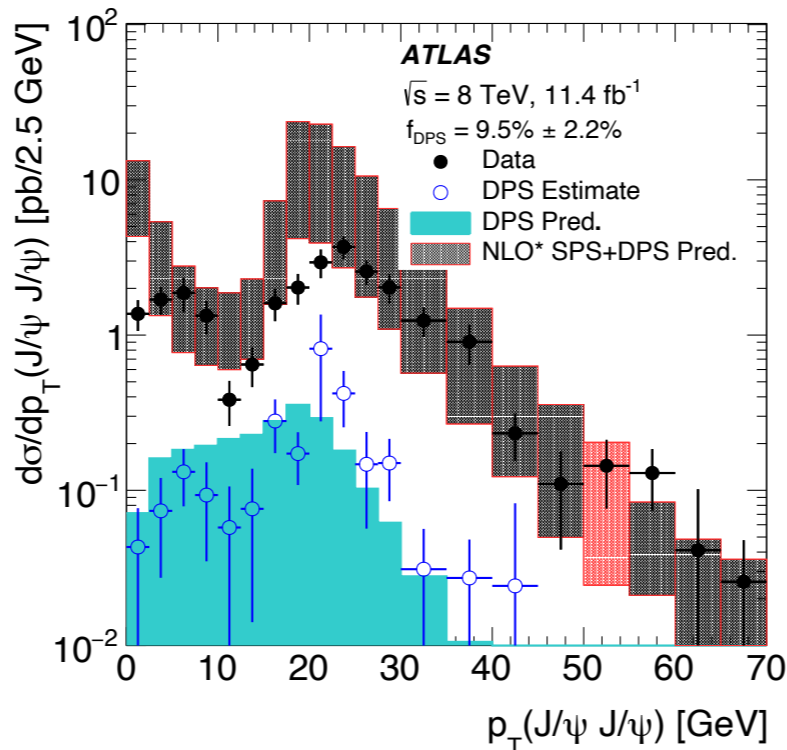
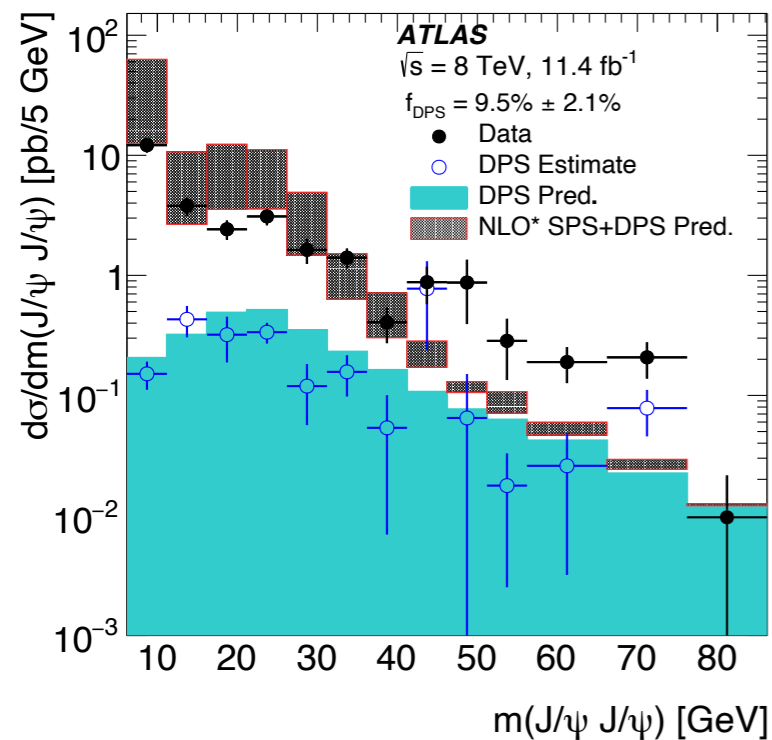
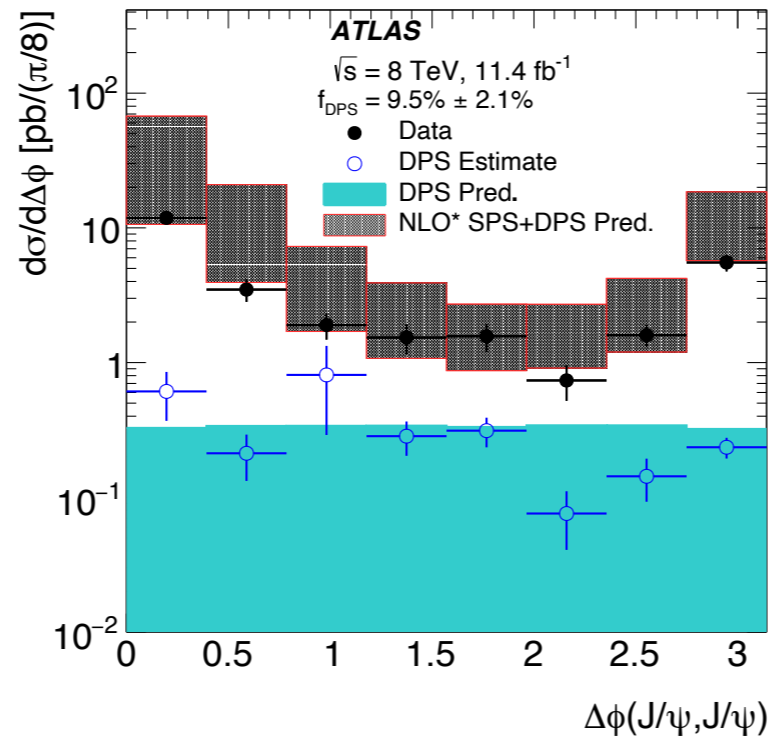
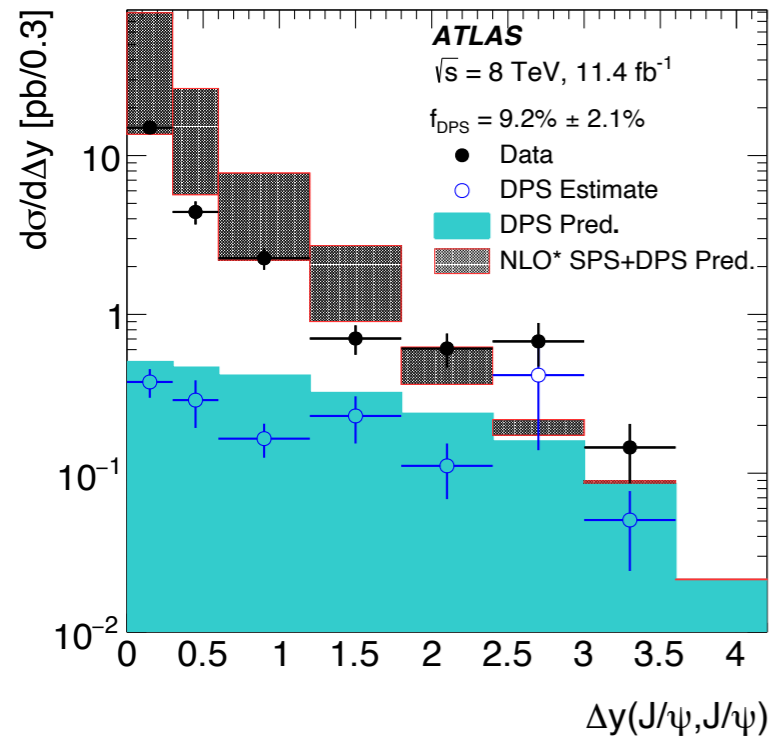
Four-jet study

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- Summary of the relative systematic uncertainties in f_{DPS} , α_{2j}^{4j} and σ_{eff}

Source of systematic uncertainty	Δf_{DPS}	$\Delta \alpha_{2j}^{4j}$	$\Delta \sigma_{\text{eff}}$
Luminosity			$\pm 3.5 \%$
Model dependence for detector corrections		$\pm 2 \%$	$\pm 2 \%$
Reweighting of AHJ	$\pm 6 \%$		$\pm 6 \%$
Jet reconstruction efficiency			$\pm 0.1 \%$
Single-vertex events selection			$\pm 0.1 \%$
Jet energy and angular resolution	$\pm 15 \%$	$\pm 3 \%$	$\pm 15 \%$
JES uncertainty	$+32 \%$ -37%	$\pm 12 \%$	$+31 \%$ -19%
Total systematic uncertainty	$+36 \%$ -40%	$\pm 13 \%$	$+35 \%$ -25%

di- J/ψ study



- DPS predictions are normalised to measured f_{DPS}
- NLO SPS is scaled by 1.85 to account for feed-down
- Data deviates from NLO*SPS+DPS prediction at large Δy , large invariant mass and low p_T regions

di- J/ψ study

Systematic uncertainty: di- J/ψ cross-section [%]

Source	$ y(J/\psi_2) < 1.05$	$1.05 \leq y(J/\psi_2) < 2.1$
Trigger	± 7.5	± 8.3
Muon reconstruction	± 1.1	± 1.3
Kinematic acceptance	± 0.4	± 1.1
Mass model	± 0.1	± 0.1
Mass bias	± 0.2	± 0.2
Prompt-prompt model	± 0.2	± 0.01
Differential f_{PP} corr.	± 0.6	± 0.3
Pile-up	± 0.03	± 0.4
Total	± 7.7	± 8.5
Branching fraction		± 1.1
Luminosity		± 1.9

Systematic uncertainty: f_{DPS} [%]

Source	Relative uncertainty [%]
Trigger	± 0.7
Muon reconstruction	± 0.1
Mass model	± 0.01
Mass bias	± 0.02
Prompt-prompt model	± 0.1
Differential f_{PP} corr.	± 0.1
Pile-up	± 0.8
DPS model	± 5.6
Total	± 5.7

Z + J/ψ study

[Eur. Phys. J. C 75 \(2015\) 229](#)

Source	Prompt		Non-prompt	
	$ y_{J/\psi} < 1.0$	$1.0 < y_{J/\psi} < 2.1$	$ y_{J/\psi} < 1.0$	$1.0 < y_{J/\psi} < 2.1$
Fit procedure	3%	3%	4%	8%
Z boson kinematics	1%	1%	1%	1%
$\mu_{J/\psi}$ efficiency	1%	1%	1%	1%
Vertex separation	7%	16%	2%	15%

Process	$ y_{J/\psi} < 1.0$	$1.0 < y_{J/\psi} < 2.1$	Total	
			Events found	From pileup
Prompt signal	$24 \pm 6 \pm 2$	$32 \pm 8 \pm 5$	$56 \pm 10 \pm 5$	$5.2^{+1.8}_{-1.3}$
Non-prompt signal	$54 \pm 9 \pm 3$	$41 \pm 8 \pm 7$	$95 \pm 12 \pm 8$	$2.7^{+0.9}_{-0.6}$
Background	$61 \pm 11 \pm 6$	$77 \pm 13 \pm 7$	$138 \pm 17 \pm 9$	

$W + J/\psi$ study

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Source of Uncertainty	Uncertainty [%]	
	$ y_{J/\psi} < 1$	$1 < y_{J/\psi} < 2.1$
J/ψ mass fit	8.7	4.9
Vertex separation	12	15
$\mu_{J/\psi}$ efficiency	2.0	1.6
Pile-up	1.1	1.4
$J/\psi + Z$ and $J/\psi + W^\pm (\rightarrow \tau^\pm \nu)$	3.5	4.8
Efficiency correction	2.3	2.3