

HEAVY NEUTRAL LEPTONS SEARCHES AT FCC-ee

2nd FCC Italy-France workshop
Venice, Nov. 5, 2024

THEORY AND SIMULATION

Heavy neutral leptons

- **Type I seesaw model** with $n > 1$ heavy neutral leptons (HNLs) can address multiple issues of the SM [Phys. Rev. Lett. 128, 051801](#)

$$\mathcal{L}_{type I} = \frac{1}{2} \sum_{i=1}^n \bar{N}_i (i\not{\partial} - M_i) N_i - \frac{g}{\sqrt{2}} \sum_{i=1}^n \sum_{\ell=e,\mu,\tau} \bar{N}_i U_{\ell i}^* W_{\mu}^+ \gamma^{\mu} \ell_L^{-} - \frac{g}{2 \cos \theta_W} \sum_{i=1}^n \sum_{\ell=e,\mu,\tau} \bar{N}_i U_{\ell i}^* Z_{\mu} \gamma^{\mu} \nu_{L,\ell} - \frac{g H M_i}{2 M_W} \sum_{i=1}^n \sum_{\ell=e,\mu,\tau} \bar{N}_i U_{\ell i}^* \nu_{L,\ell} + H.c.$$

- Parameter-dependent **decay length**:

$$L_{N_i} \simeq \frac{1.6}{U_i^2} \left(\frac{M_i}{GeV} \right)^{-6} \left(1 - (M_i/M_Z)^2 \right) \text{ cm}$$

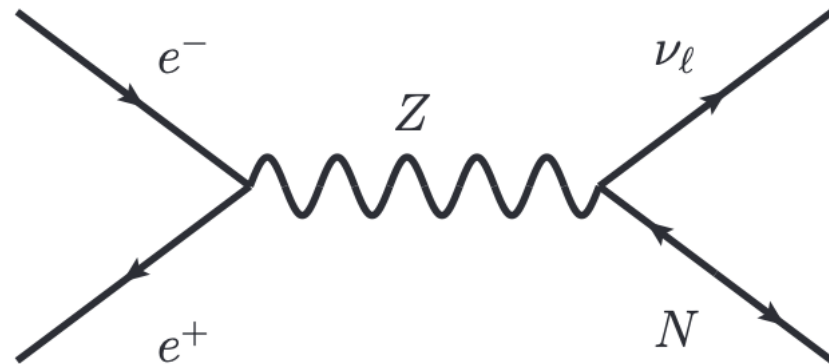
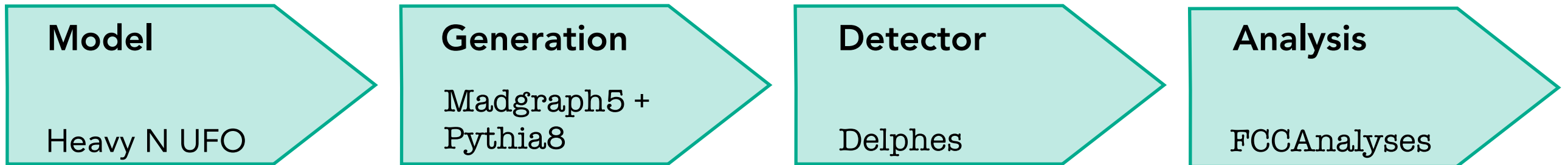
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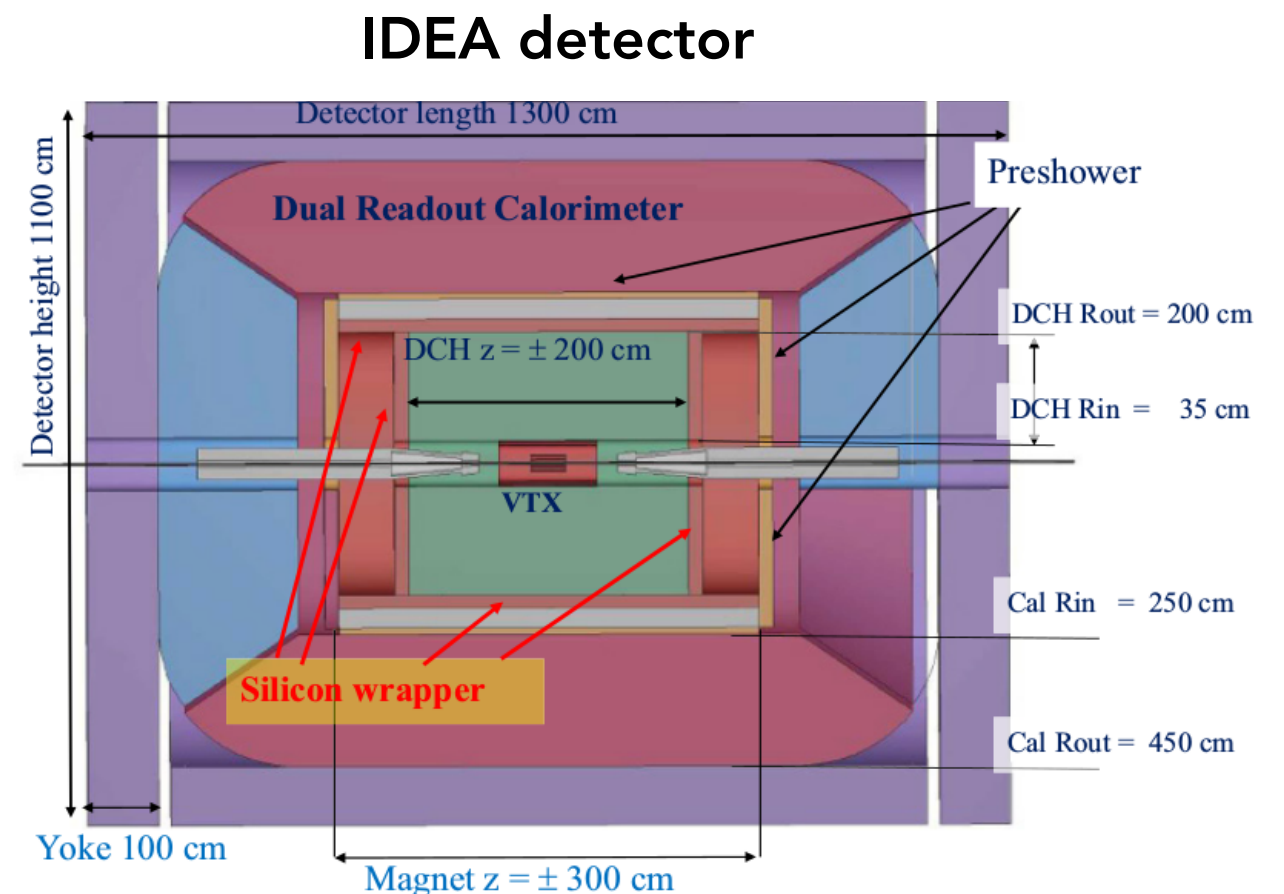
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$$- \frac{g}{2 \cos \theta_W} \sum_{i=1}^n \sum_{\ell=e,\mu,\tau} \bar{N}_i U_{\ell i}^* Z_{\mu} \gamma^{\mu} \nu_{L,\ell} - \frac{g H M_i}{2 M_W} \sum_{i=1}^n \sum_{\ell=e,\mu,\tau} \bar{N}_i U_{\ell i}^* \nu_{L,\ell} + H.c.$$

- Simplified scenario: **one Majorana** or Dirac **HNL**
- Minimal realistic scenarios (lepton number-like symmetry):
 - $M_1 = M_2$ single Dirac HNL
 - $M_1 \approx M_2$ **pseudo-Dirac HNL** [arXiv: 1712.07611](#)
 - $M_1 \neq M_2$ two distinct Majorana HNLs

Simulation setup



- Z pole run at FCC-ee
- SM processes available from Winter '23
[central FCC production](#)
(Pythia8 + Delphes)



EXCLUSION LIMITS

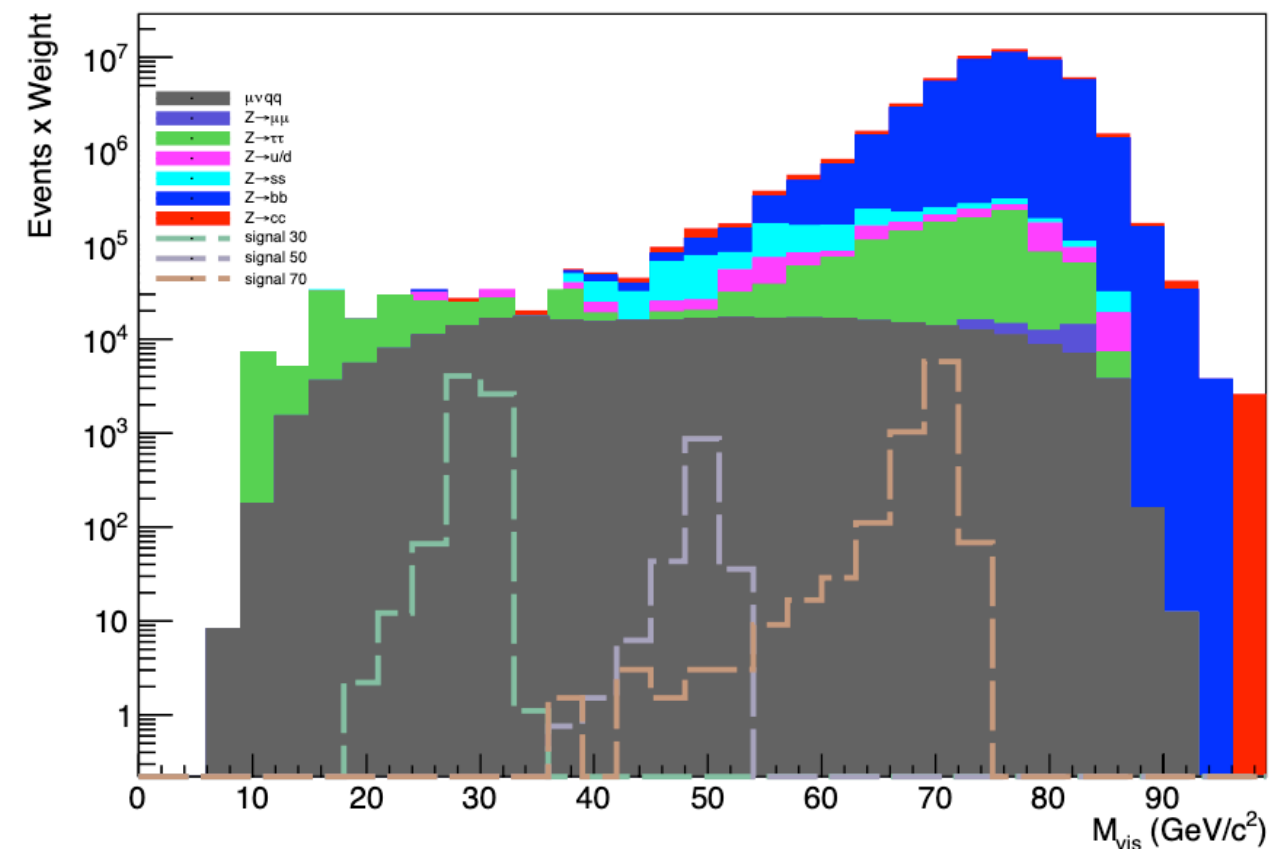
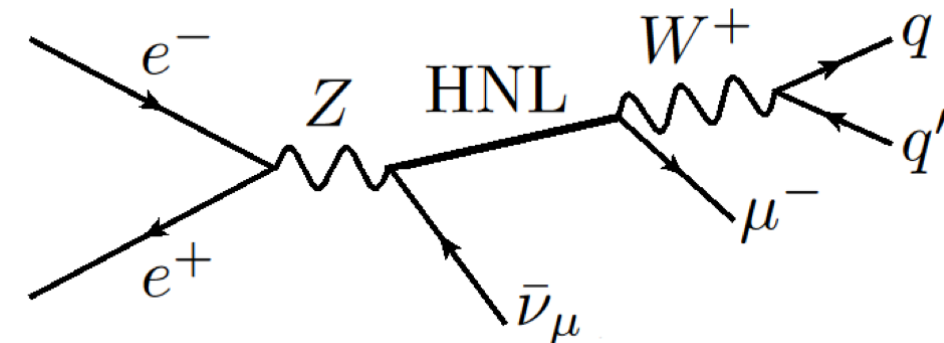
One muon HNL

Polesello and Valle

[doi:10.17181/9pc9x-kcn56](https://doi.org/10.17181/9pc9x-kcn56)



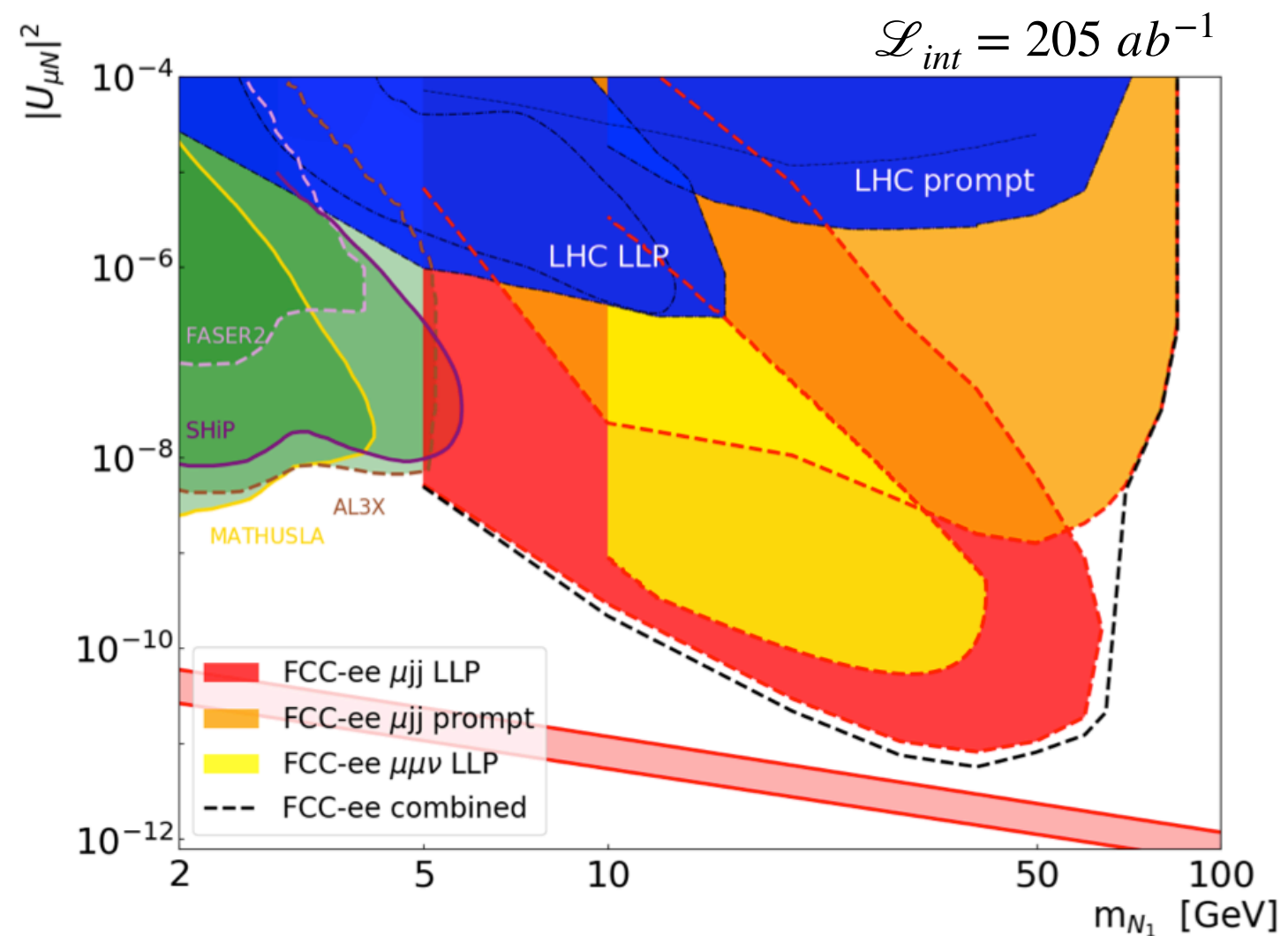
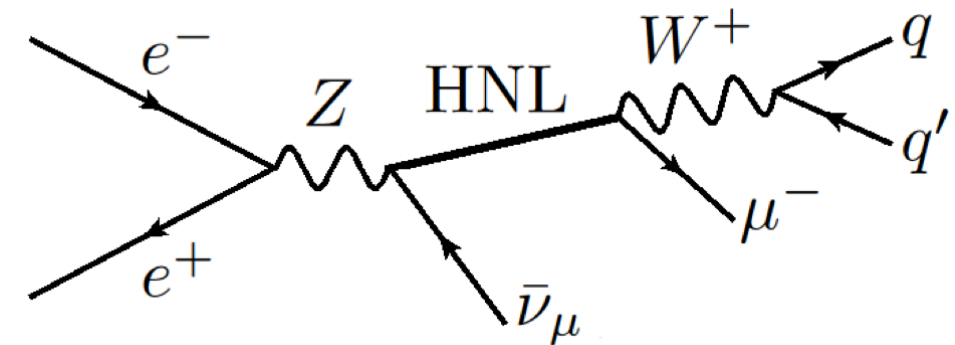
- Majorana $N \rightarrow \mu j j$, coupling to muons
- Privately produced $e^+e^- \rightarrow \nu_\mu \mu j j$ SM background
- At least **three tracks and one muon** not in jets (cut list in backup)
- Exclusive k_T jet clustering $n_{jets} = 2$



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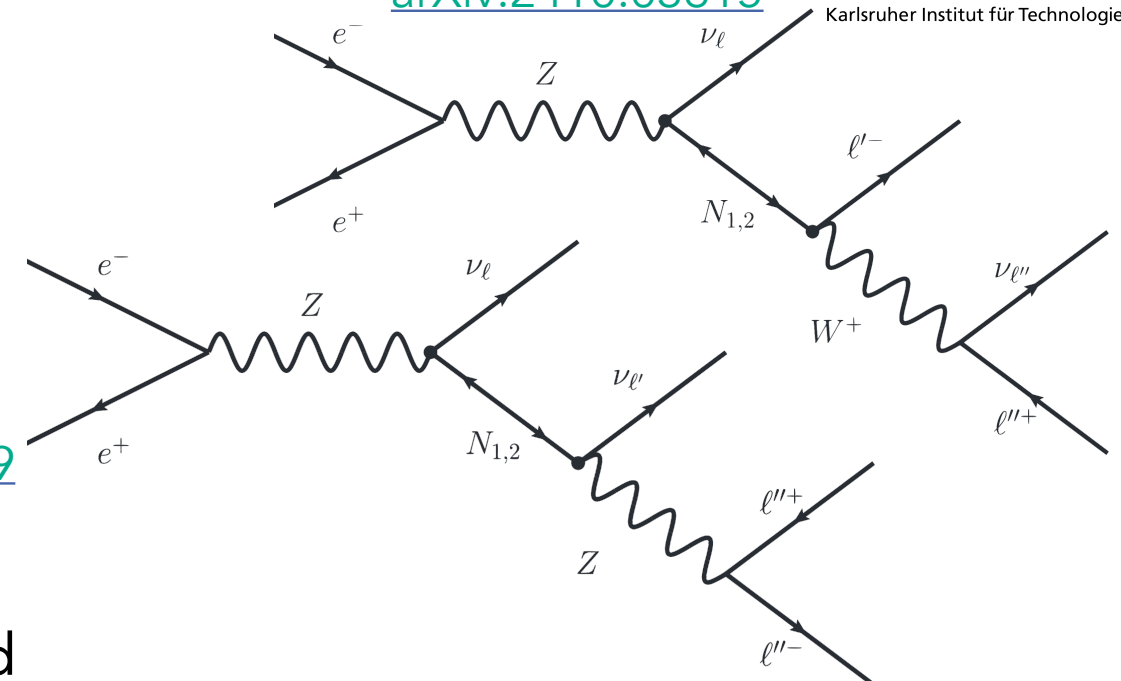
■ **Prompt vs. long-lived HNL**
(background-free): $L_{xy} \lesssim 0.5 \text{ mm}$



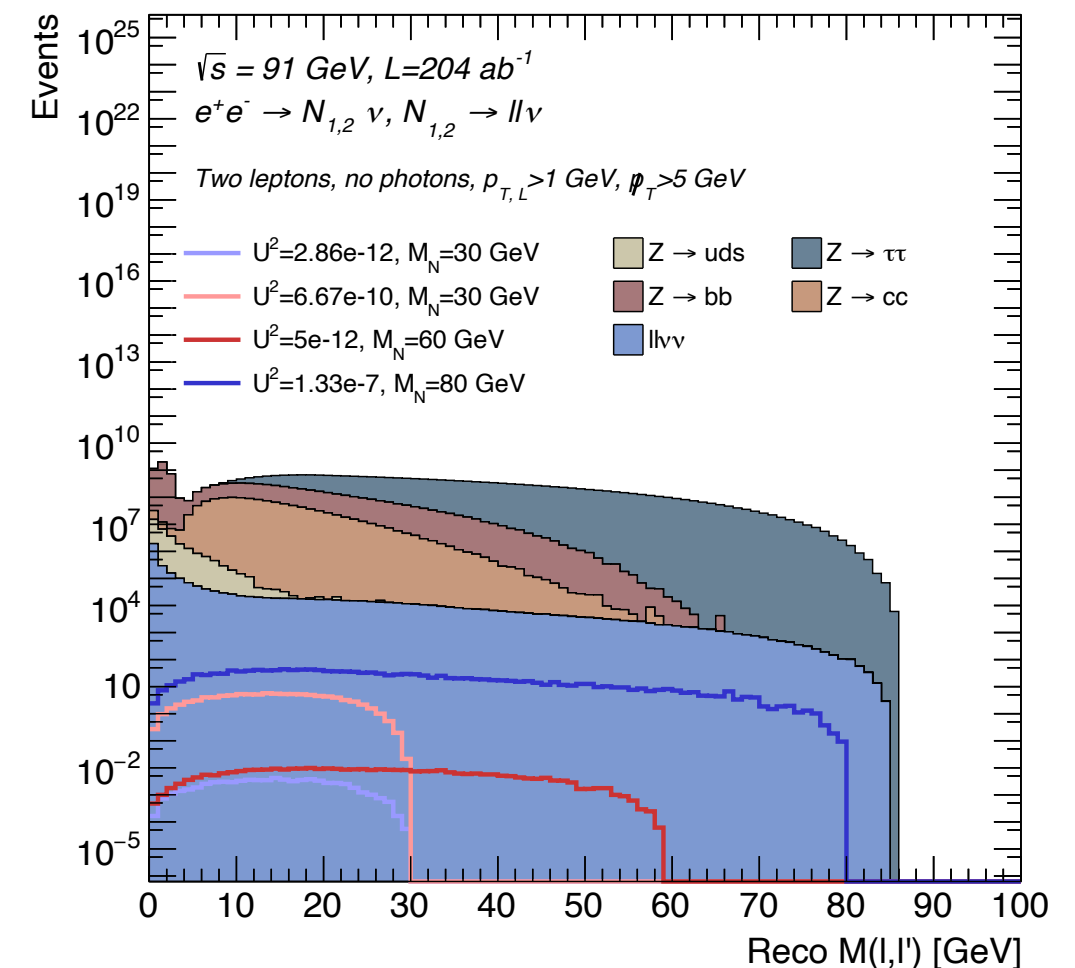
Two HNLs

- Pseudo-Dirac pair $N_{1,2} \rightarrow \ell \ell \nu$, coupling to all leptons
- Parameters in agreement with leptogenesis [Phys. Rev. D 108 \(2023\) L101302](#) and oscillation data [JHEP 09 \(2020\) 178](#)
- Privately produced $e^+e^- \rightarrow \ell \ell \nu \nu$ SM background
- Leptonic τ decays + missing energy (cut list in backup)

Giappichini et al.
[arXiv:2410.03615](https://arxiv.org/abs/2410.03615)



FCCAnalyses: FCC-ee Simulation (Delphes)

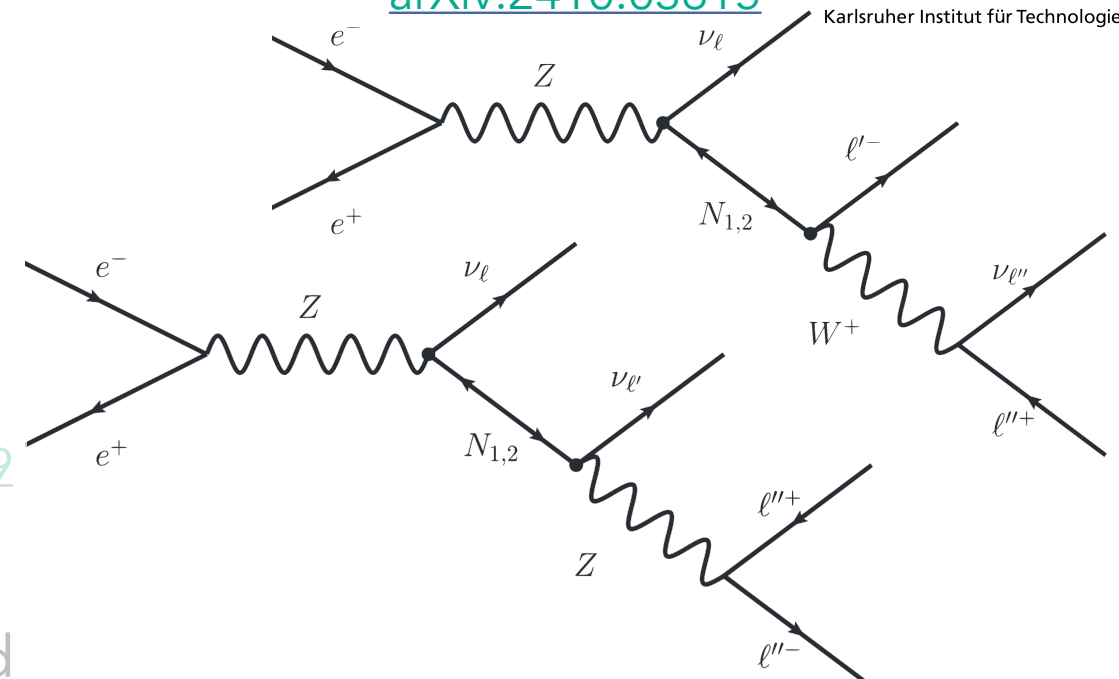


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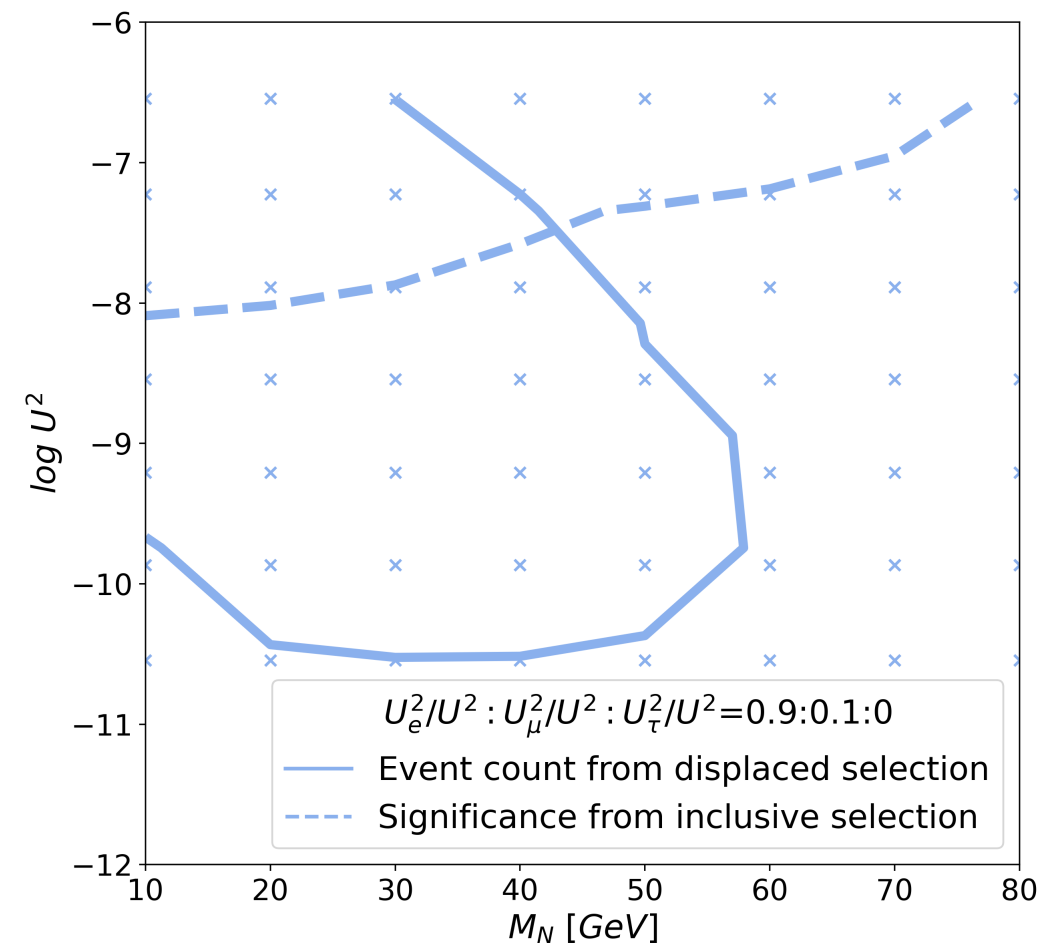
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■ **Inclusive vs. long-lived analysis (background-free): $|d_0| > 0.64 \text{ mm}$**

Giappichini et al.
[arXiv:2410.03615](https://arxiv.org/abs/2410.03615)



$N_{1,2} \rightarrow \ell \ell \nu$ at FCC – ee, $\sqrt{s} = 91 \text{ GeV}$, $\mathcal{L}_{int} = 204 \text{ ab}^{-1}$

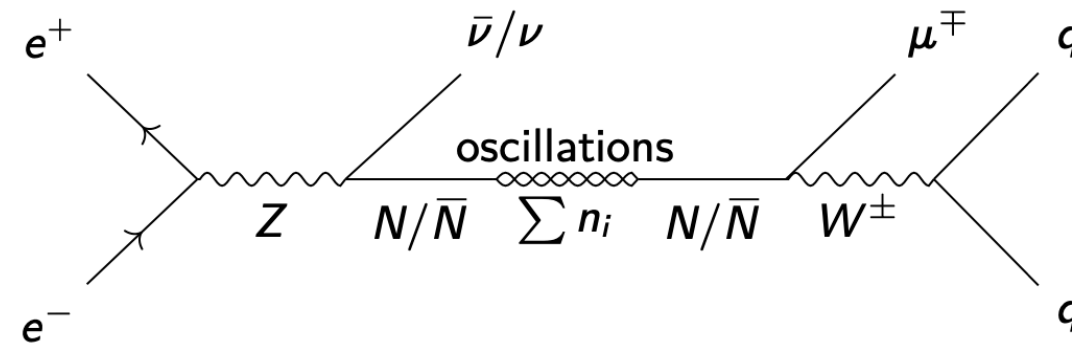


OSCILLATIONS

$N\bar{N}$ oscillations

Hajer et al.

[JHEP 10 \(2023\), p.129](#)

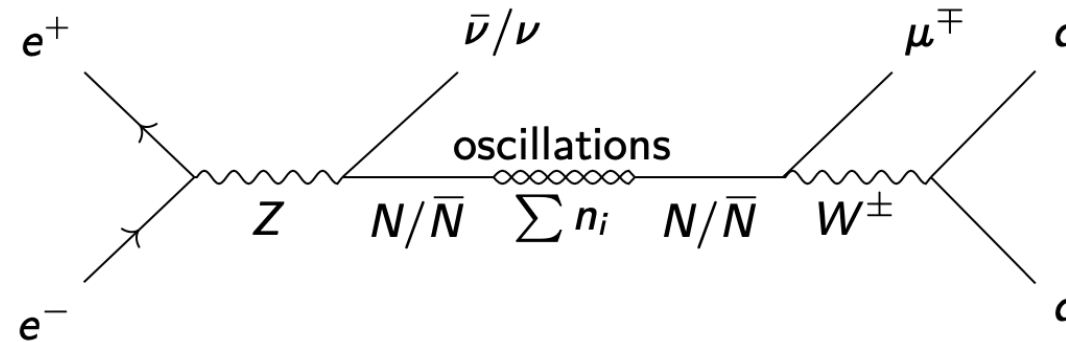


- Pseudo-Dirac pair $\mathbf{N} \rightarrow \mu jj$, coupling to muons
- Oscillations implemented in *pSPSS* [UFO](#) (phenomenological symmetry protected seesaw)

$N\bar{N}$ oscillations

Hajer et al.

[JHEP 10 \(2023\), p.129](#)

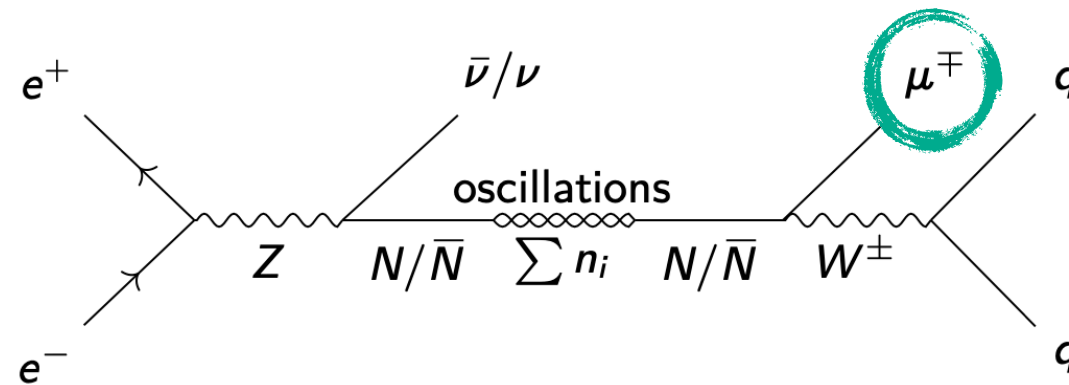


- Pseudo-Dirac pair $\mathbf{N} \rightarrow \mu jj$, coupling to muons
- Oscillations implemented in *pSPSS* [UFO](#)
- $N\bar{N}$ oscillation probability:

$$P_{osc}^{LNCILNV}(\tau) = \frac{1 \pm \cos(\Delta m \tau) \exp(-\lambda)}{2}$$

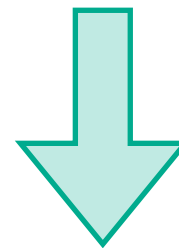
- Damping parameter $\lambda=0$ for long-lived HNLs [JHEP 09 \(2023\), p.170](#)

Final state distributions

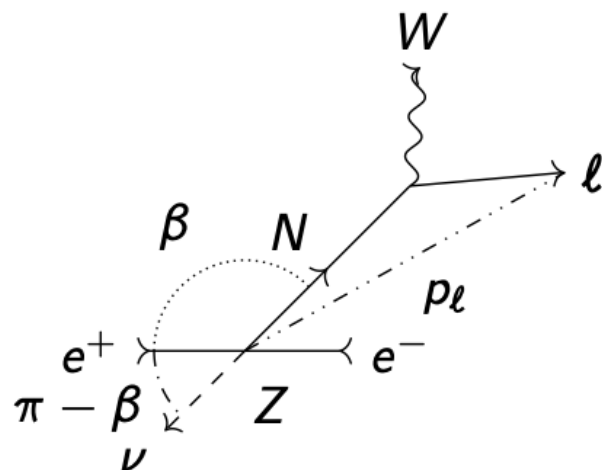


- Angular-dependent probability

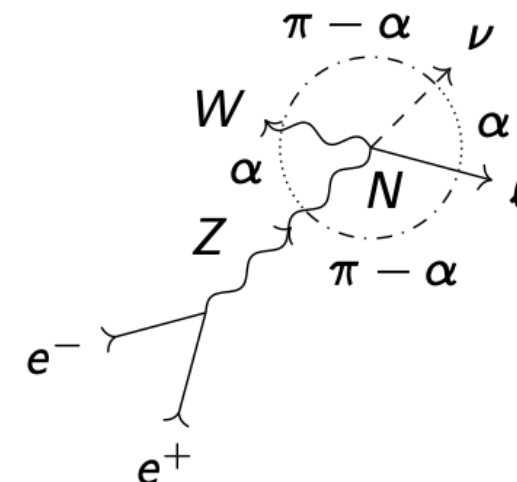
$$P_{\ell^\pm}(\cos\theta, \tau) = \frac{1}{\sigma} \frac{d\sigma(\cos\theta)}{d\cos\theta} P_{osc}^{LNC/LNV}(\tau)$$



- Forward-backward asymmetry



- Opening angle asymmetry



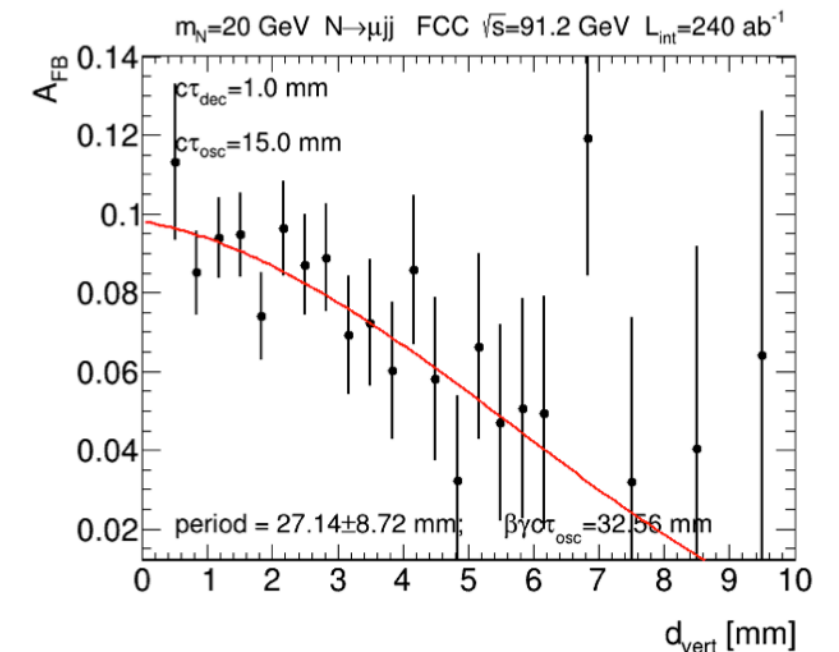
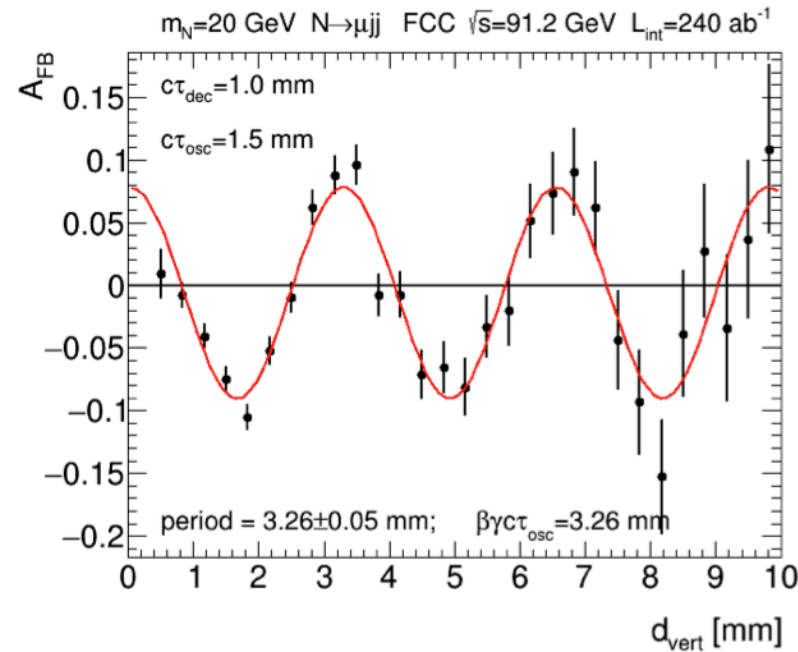
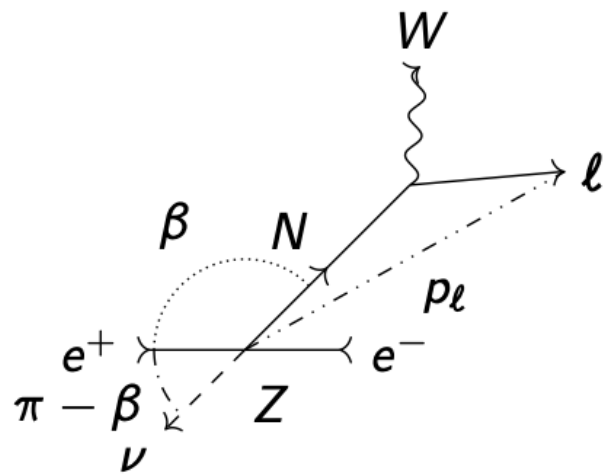
Final state distributions

Polesello and Valle

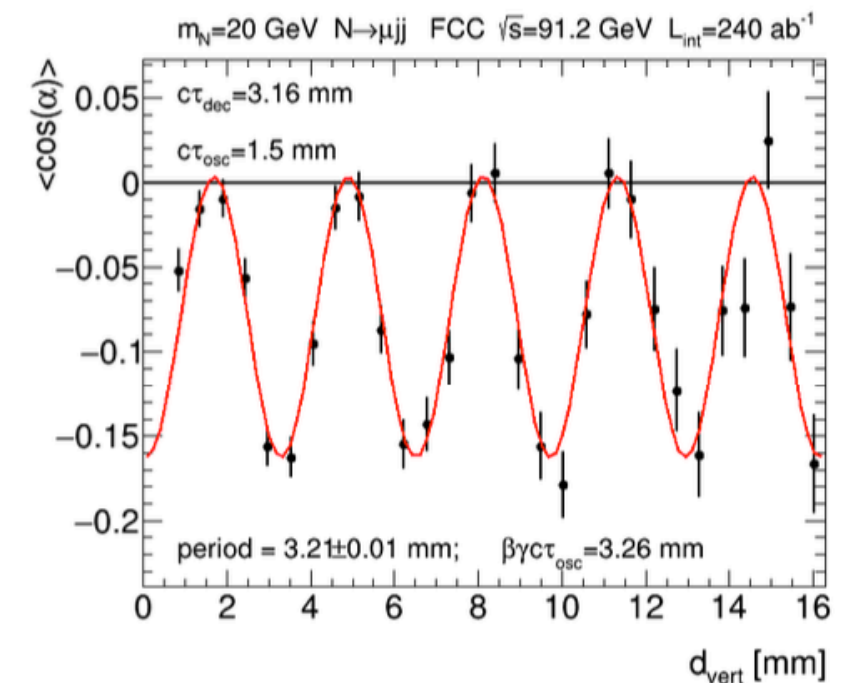
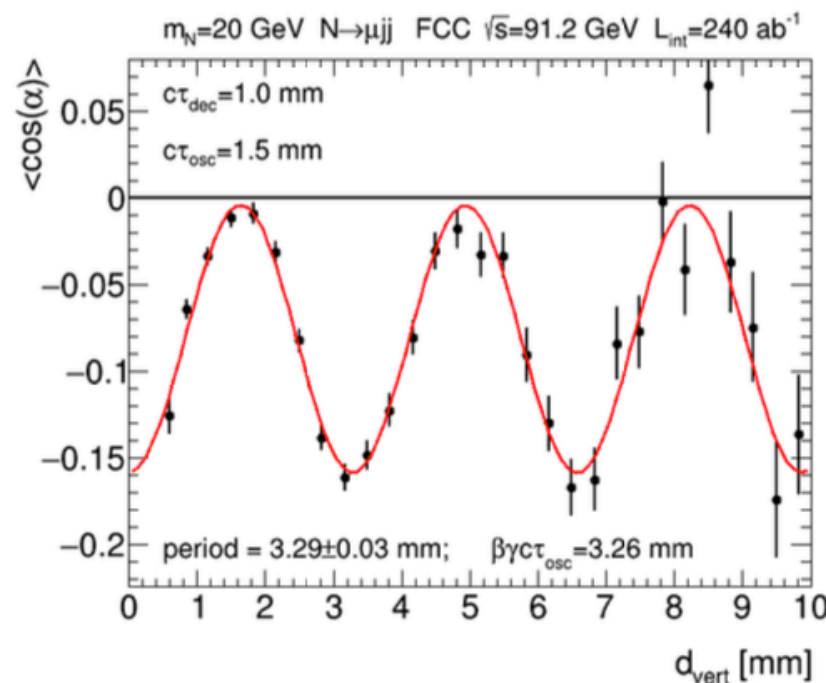
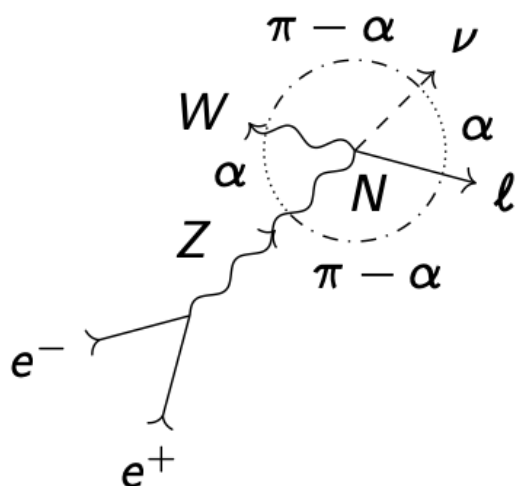
[doi:10.17181/recsm-v3k46](https://doi.org/10.17181/recsm-v3k46)



Forward-backward asymmetry



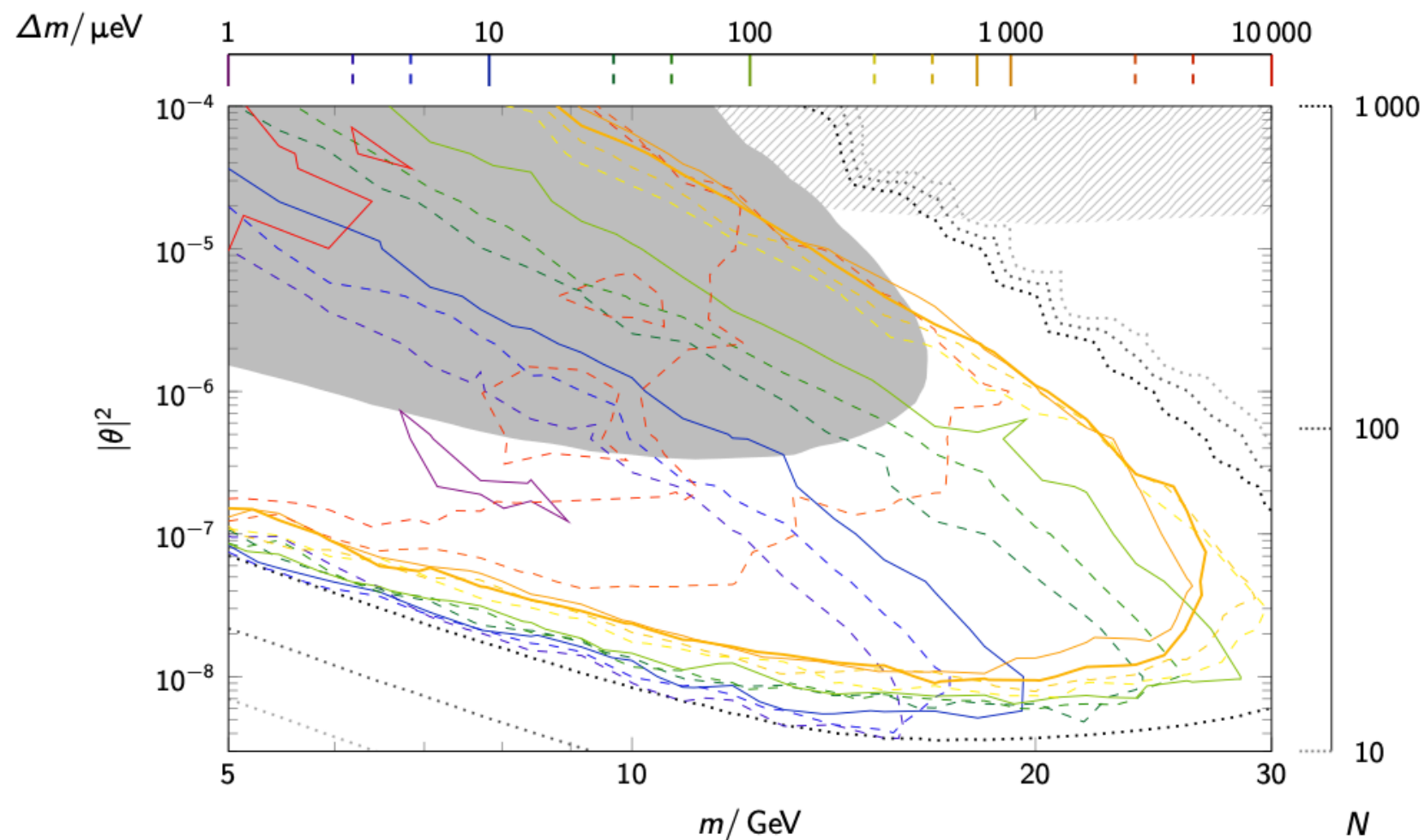
Opening angle asymmetry



$N\bar{N}$ oscillations sensitivity

Hajer et al.
[arxiv:2408.01389](https://arxiv.org/abs/2408.01389)

FCC-ee (IDEA) 5σ discovery reach

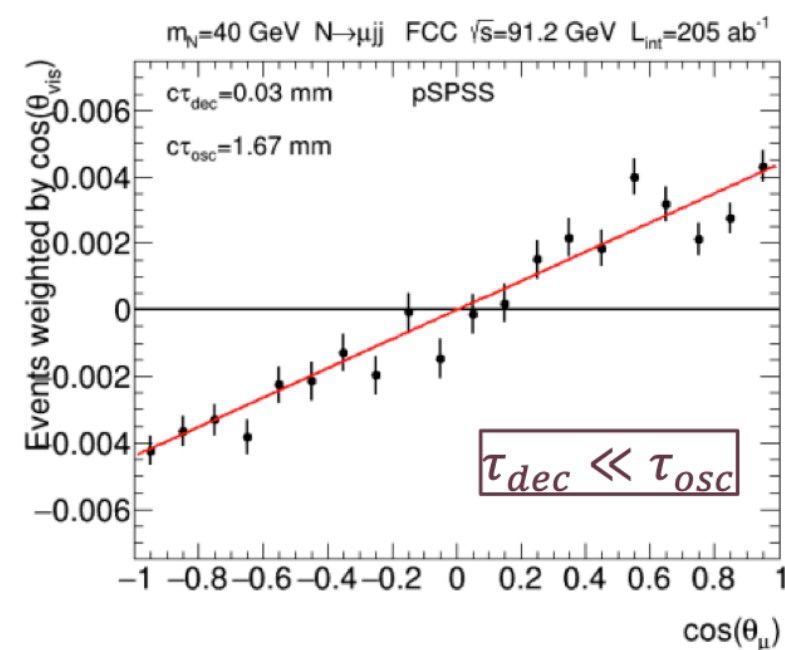
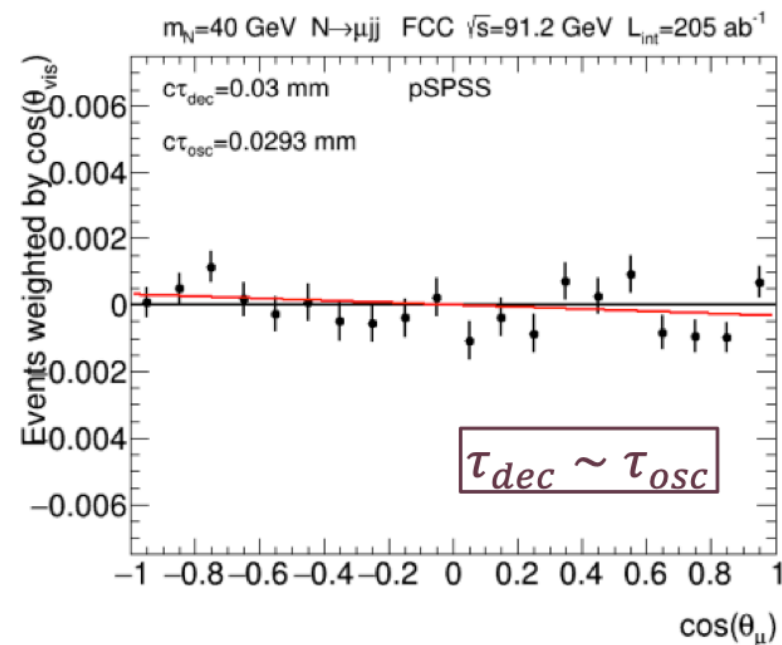
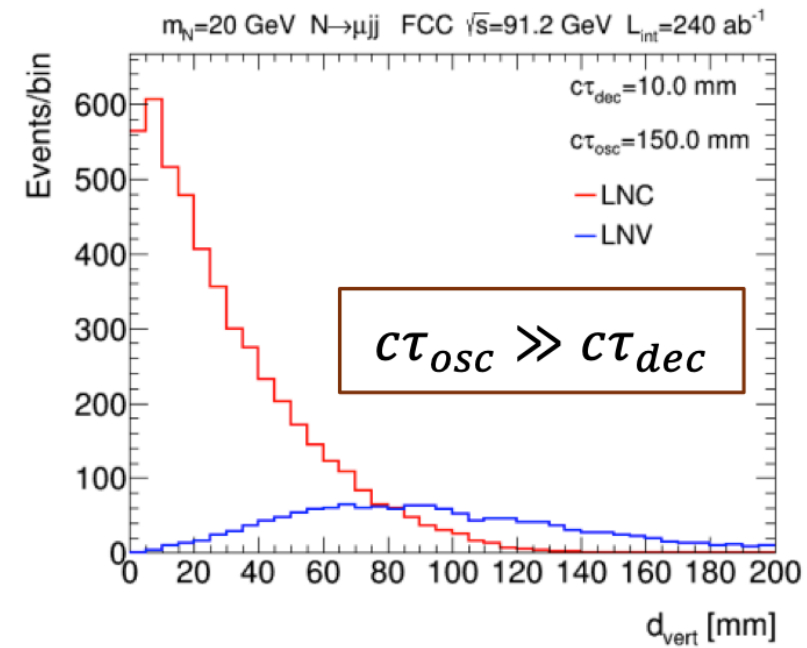
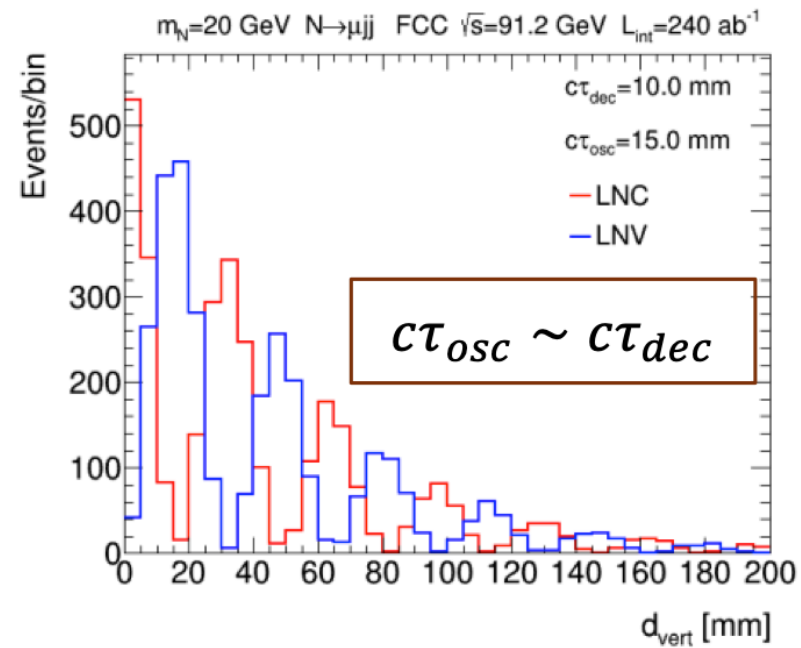


- Assuming background-free analysis (cut list in backup)
- Likelihood ratio test on the opening angle asymmetry

Dirac vs. Majorana

$\Delta m\tau \gg 1$ two Majorana HNLs

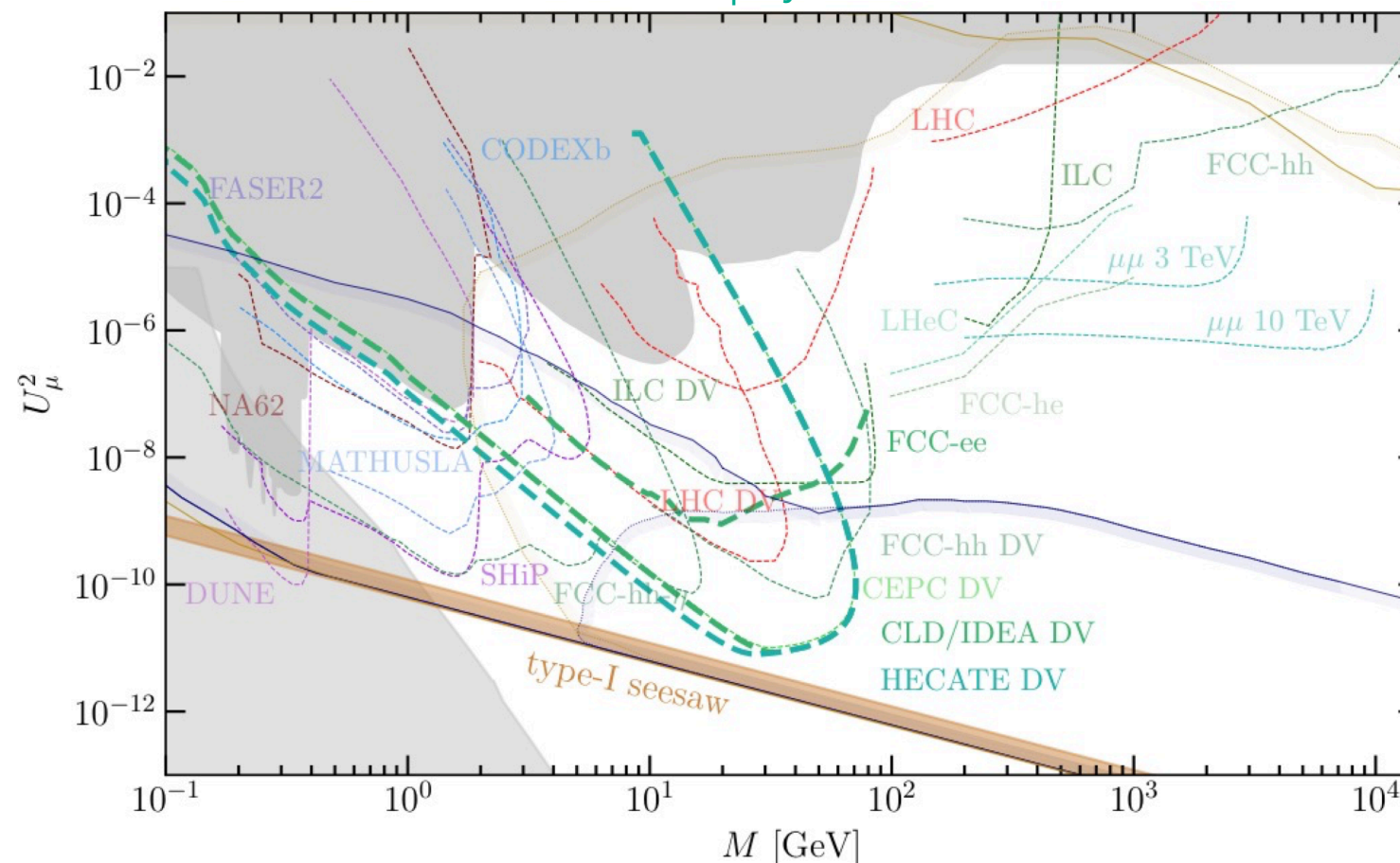
$\Delta m\tau \approx 1$ single Dirac HNL



Conclusions

- Analyses of different **HNL coupling scenarios** show FCC-ee great potential for direct searches in both **prompt** and **long-lived** channels
- $N\bar{N}$ oscillations could also be observed and their period measured in a sub-region of the accessible parameter space
- If not, **Dirac and Majorana** limits can be used to assess the phenomenon

[doi:10.3389/fphy.2022.967881](https://doi.org/10.3389/fphy.2022.967881)



Old theoretical prediction for one HNL coupling to electrons

BACKUP

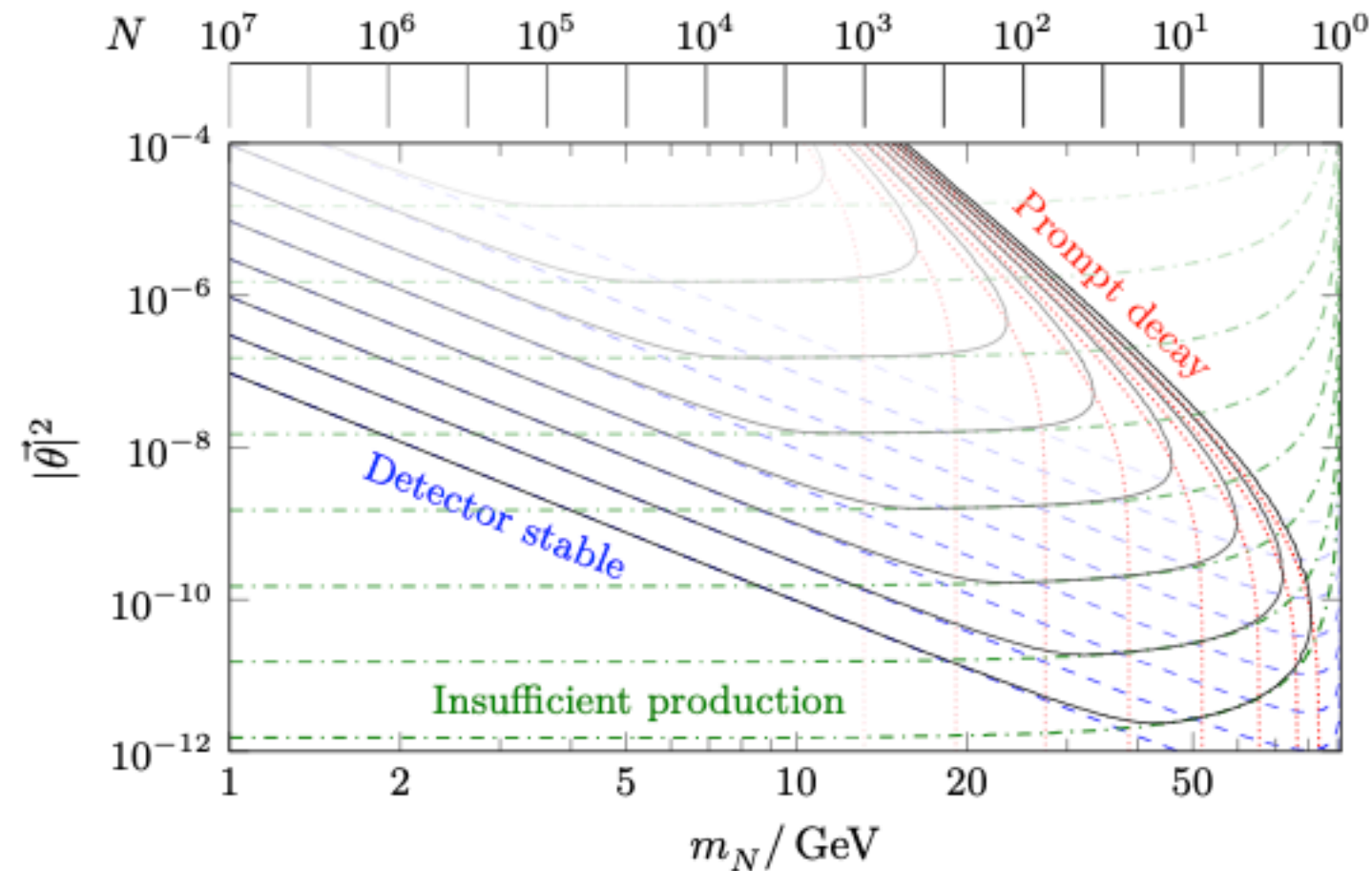


Figure 3: The testable parameter space in displaced vertex searches is constrained by the geometry of the detector. The minimal displacement cut limits the mass range from above (-----), while the maximal displacement of the reconstructed vertices limits the mass range from below (- - -). Finally, the cross section of the model imposes a lower limit on the testable couplings (-·-·-). The corresponding analytic approximations are given in [31].

Table A1 Steps of event selection implemented in this analysis. The details are given in the text. The name given to each step can be used to interpret the following tables and figures.

1. Event Filter	2. Event Selection	3. Vertex selection
1 muon ≥ 3 tracks $E_\mu \geq 3$ GeV $E_{miss} \geq 5$ GeV	1 lepton (muon) Cuts on p_{miss} , jets, μ and visible mass	$N_{tracks} - N_{tracks}^{primary} < 5$ $\chi_{vtx,primary}^2 < 10$
4. Mass-dependent kin. selection	5a. Displacement: prompt	5b. Displacement: LL
M_{vis} within $2 \times 10\% \sqrt{M}$ E_{miss} within $2 \times 10\% \sqrt{p_\nu}$	$r_{vert}^{primary} > 0.5$ mm $D_{0,\mu} < 8\sigma$ if $M_{N_1} > 70$	$r_{vert}^{primary} < 0.5$ mm

Cut list - two HNLs

Giappichini et al.
[arXiv:2410.03615](https://arxiv.org/abs/2410.03615)



Inclusive selection:

Two leptons, no photons

$$p_{T,miss} > 5 \text{ GeV}, p_{T,\ell} > 1 \text{ GeV}, E_\ell > 2 \text{ GeV}$$

No other track and no neutral hadron

$$p_{T,miss} > 10 \text{ GeV}$$

$$\cos\theta_{ll} > 0$$

$$E_{miss} > 45 \text{ GeV}$$

$$E_{l, leading} < 35 \text{ GeV}$$

$$M(l, l') < M_{HNL}$$

Displaced selection:

Two leptons, no photons

$$p_{T,miss} > 5 \text{ GeV}, p_{T,\ell} > 1 \text{ GeV}, E_\ell > 2 \text{ GeV}$$

No other track and no neutral hadron

$$p_{T,miss} > 10 \text{ GeV}$$

$$\cos\theta_{ll} > -0.8$$

$$M(l, l') < 80 \text{ GeV}$$

$$\chi^2 < 10$$

$$|d_0| > 0.64 \text{ mm}$$

Efficiencies - two HNLs

Giappichini et al.
[arXiv:2410.03615](https://arxiv.org/abs/2410.03615)



	Cross-section (pb)	N_{gen}	Inclusive selection	Displaced selection
$Z \rightarrow ee$	1462.09	100000000	$\leq 3.42e-13$	$\leq 4.38e-17$
$Z \rightarrow \mu\mu$	1462.08	100000000	$1.20e-08$	$\leq 4.69e-16$
$Z \rightarrow \tau\tau$	1476.58	100000000	$2.41e-06$	$\leq 8.29e-11$
$Z \rightarrow bb$	6645.46	438738637	$\leq 4.08e-14$	$\leq 4.23e-14$
$Z \rightarrow cc$	5215.46	499786495	$\leq 7.65e-12$	$\leq 4.10e-13$
$Z \rightarrow ud$	11870.5	497658654	$\leq 2.04e-15$	$\leq 6.18e-16$
$Z \rightarrow ss$	5215.46	499842440	$\leq 7.03e-15$	$\leq 3.46e-15$
$ee\nu\nu$	$1.09e-02$	1000000	$2.25e-01$	$\leq 1.23e-07$
$\mu\mu\nu\nu$	$4.78e-03$	1000000	$2.27e-01$	$\leq 1.12e-07$
$\tau\tau\nu\nu$	$1.42e-03$	1000000	$1.04e-01$	$\leq 2.92e-07$
$ll'\nu\nu$	$4.59e-03$	1000000	$2.66e-01$	$\leq 7.43e-09$
$U^2 = 2.86e-12, M_N = 30 \text{ GeV}$	$4.48e-09$	50000	$6.01e-01$	$7.83e-01$
$U^2 = 6.67e-10, M_N = 30 \text{ GeV}$	$1.04e-06$	50000	$5.79e-01$	$6.27e-01$
$U^2 = 5e-12, M_N = 60 \text{ GeV}$	$3.75e-09$	50000	$3.11e-01$	$5.89e-01$
$U^2 = 1.33e-7, M_N = 80 \text{ GeV}$	$2.27e-05$	50000	$2.98e-01$	$\leq 3.59e-06$

- Forward-backward asymmetry:

$$P_{N/\bar{N}}(\cos \beta) = P_+(\cos \beta) \pm P_-(\cos \beta)$$

$$P_+(\cos \beta) = \frac{3}{4} \frac{(1 + \cos^2 \beta)m_Z^2 + (a - \cos^2 \beta)m_N^2}{2m_Z^2 + m_N^2}, \quad P_-(\cos \beta) = \frac{b}{2} \cos \beta$$

- Opening angle asymmetry:

$$P_{c/v}(\cos \alpha) = P_+(\cos \alpha) \pm P_-(\cos \alpha)$$

$$P_+(\cos \alpha) = \frac{1}{2}, \quad P_-(\cos \alpha) = -\frac{a(m_N, m_Z, m_W)}{2} \cos \alpha$$

- where a and b are the corresponding analysis power

Cut list - oscillations

Hajer et al.
[arxiv:2408.01389](https://arxiv.org/abs/2408.01389)



- One displaced muon ($400 \mu m < L_{xyz} < 1 m$)
- One jet (soft quarks, at least two tracks within $100 \mu m$ of the muon vertex)
- Displaced vertex collinear with the HNL momentum $\Delta R \geq 0.1$
- Reconstructed HNL mass in window $\pm 2 GeV$ of generated HNL mass

	Events	
	Simulated	
	497068	100 %
Exactly one muon	-56228	-11.3 %
Exactly one jet	-2271	-0.515 %
N mass window	-70177	-16.0 %
Displaced muon	-5444	-1.48 %
Single vertex	-13812	-3.81 %
Vertex direction	-3152	-0.903 %
Remaining	345984	69.6 %