

# S5-like Demo Cell

## Update on Solenoid Design

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Marco Statera**

**11/October/2024**

**MuCol-WP8 integration meeting**

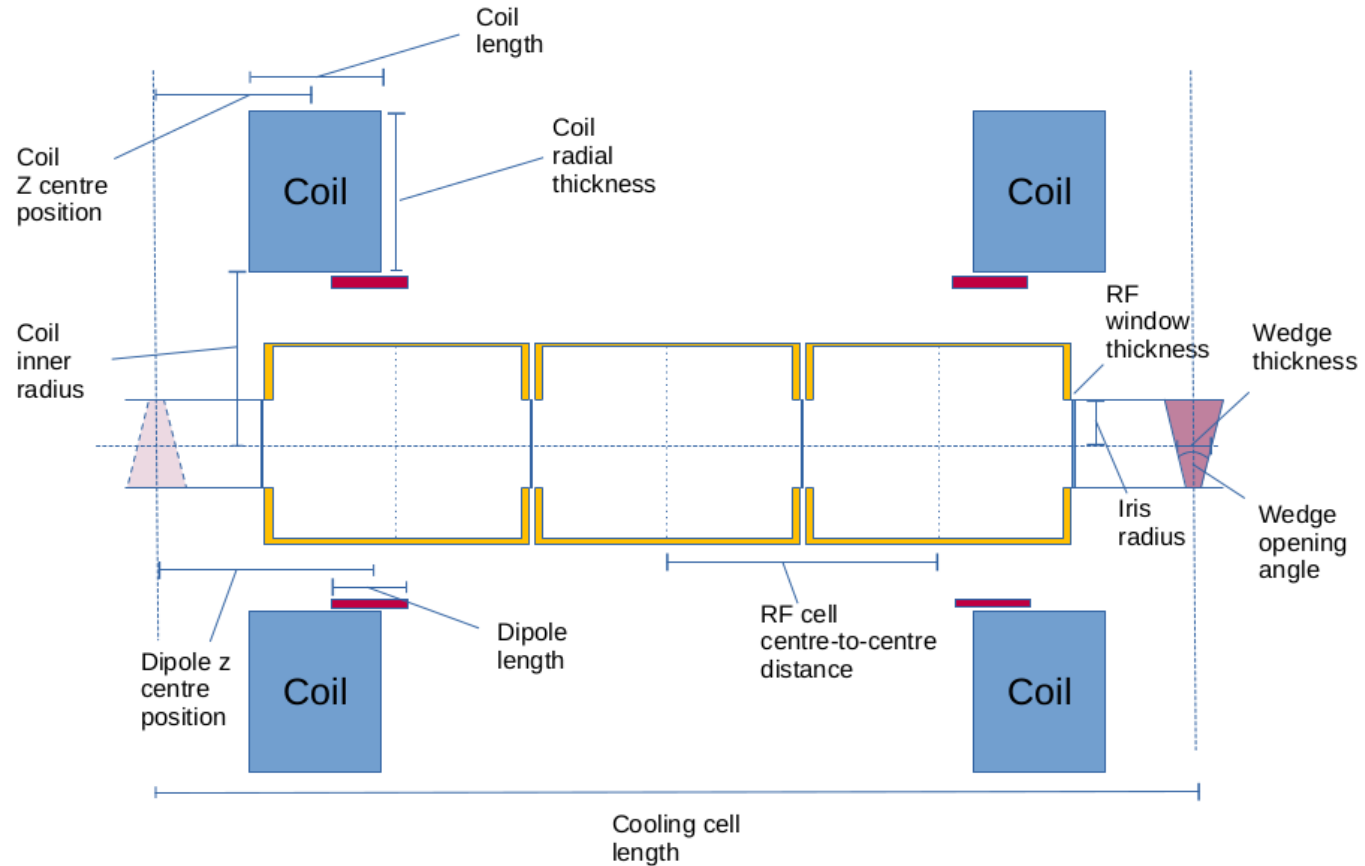
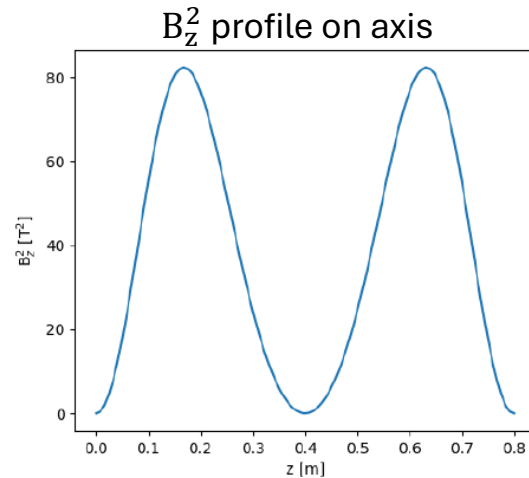
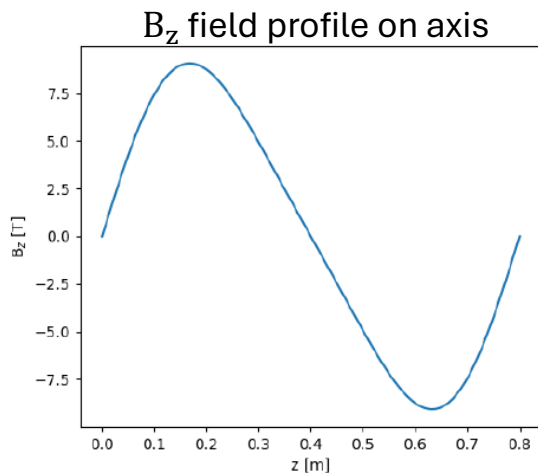
# Outline

- *MuCol Deliverable Report D8.1* solenoid data
- Study of the engineering limits of *D8.1* configuration
- Solenoids design optimization strategy
- Minimum focusing strength error configuration analysis
- Mechanical analyses: *stand-alone* and *lattice* operational modes
- Reduced-current configuration analysis

# S5 demo cell analysis: *MuCol Deliverable Report D8.1*

- Beam optic studies on S5 cell assumed **ideal** solenoids and dipoles.
- Results presented in the *Deliverable Report D8.1*.
- An **engineering design of the stage magnets** is needed.

$$L = 0.8; b_0 = 0; b_1 = 8.75; b_2 = 1.25; b_3 = 0; b_4 = 0; b_5 = 0$$
$$\int B^2(z) dz = 31.25 \text{ T}^2 \text{ m}$$



# S5 demo cell: magnets design

- Design for the target field required by the optics.
- Magnets must be optimized starting from the proposed solenoid configuration.
- **Motivation:** excessive peak field values on the coil section.

MuCol deliverable report  
D8.1 parameters

### Simulated coil geometry

Coil inner radius	250 mm
Coil length	140 mm
Coil radial thickness	169.3 mm
Coil z centre position	100.7 mm
Current Density	500 A/mm <sup>2</sup>

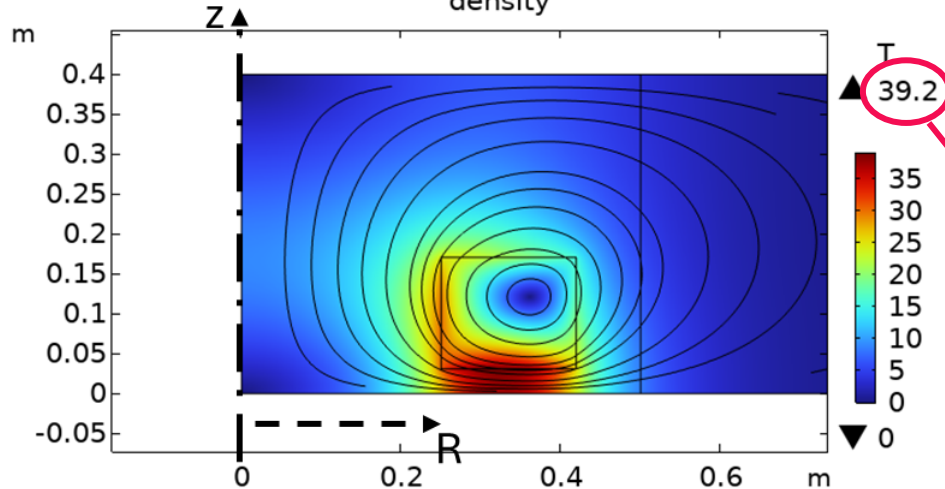
Geometrical radial constraints **not** satisfied\*.  
(RF cavity aperture, cryostat thickness, **dipole radial thickness**)

\*Same solenoid shifted to larger radius, increasing current to keep same profile

### Simulated coil geometry

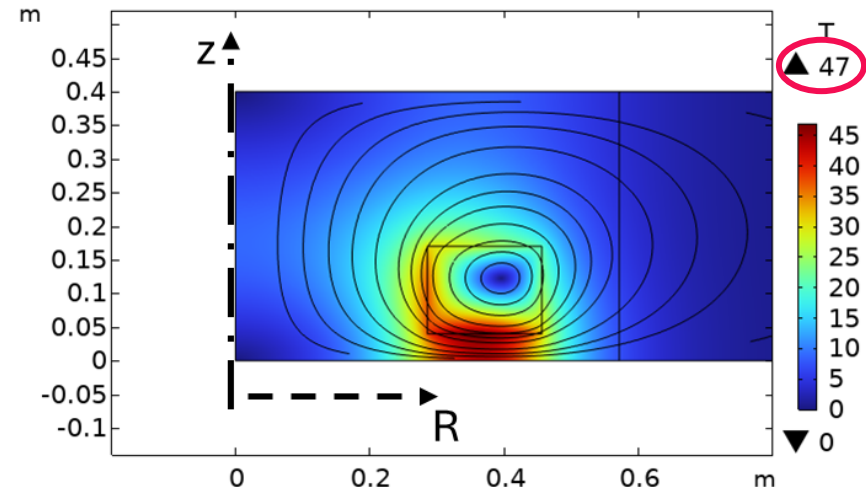
Coil inner radius	285 mm
Coil length	130 mm
Coil radial thickness	170 mm
Coil z centre position	105 mm
Current Density	650 A/mm <sup>2</sup>

Surface: Magnetic flux density norm (T) Streamline: Magnetic flux density



Excessive field at the coil section!!

Surface: Magnetic flux density norm (T) Streamline: Magnetic flux density



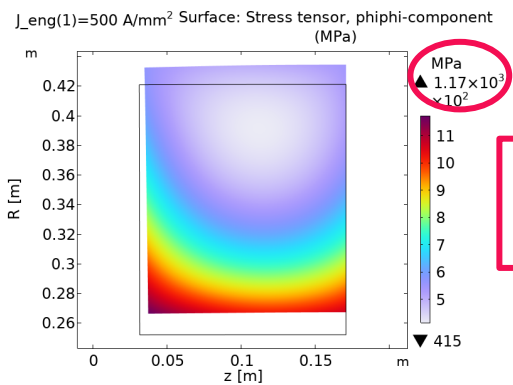
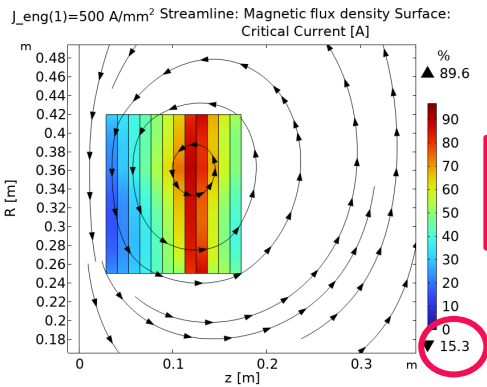
# MuCol D8.1 Report configuration: excessive stresses

→ The engineering limits were investigated on the S5 cell solenoid parameters reported in the MuCol Deliverable Report D8.1.

→ Limit for a feasible solenoid design:

MuCol deliverable report D8.1 parameters

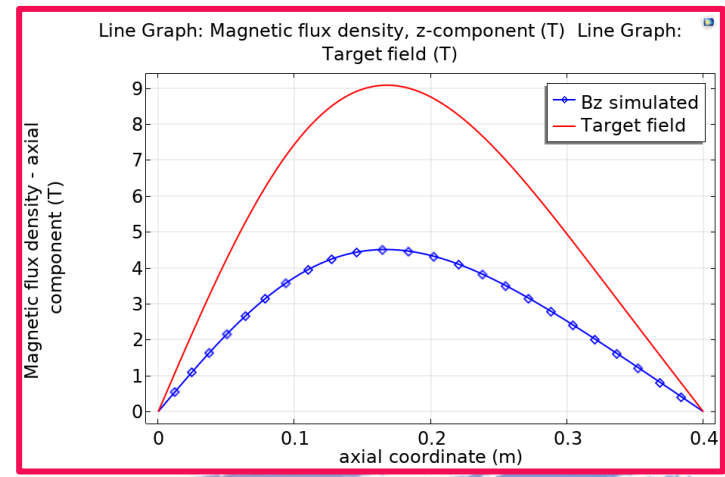
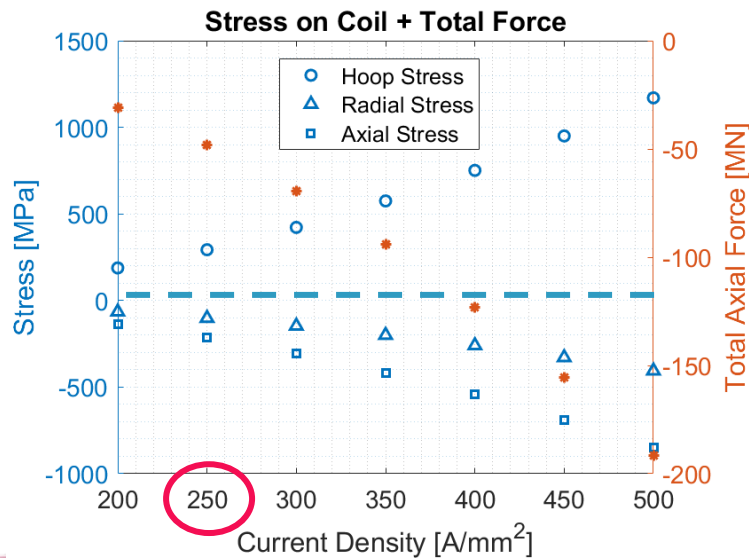
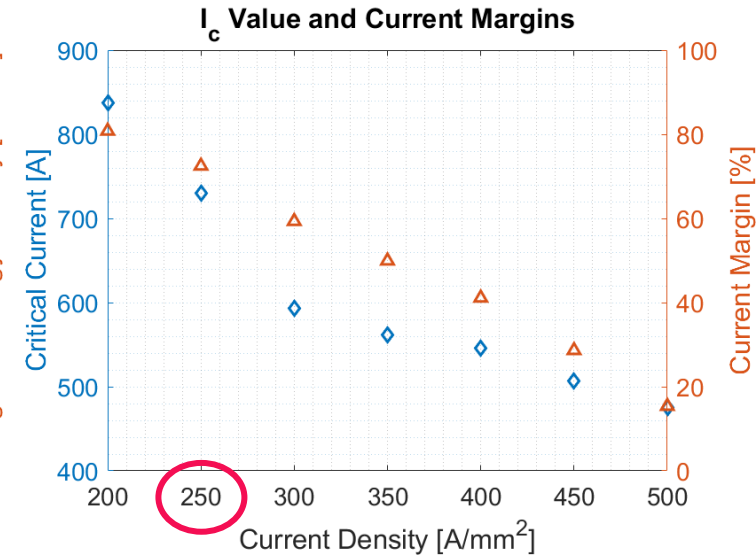
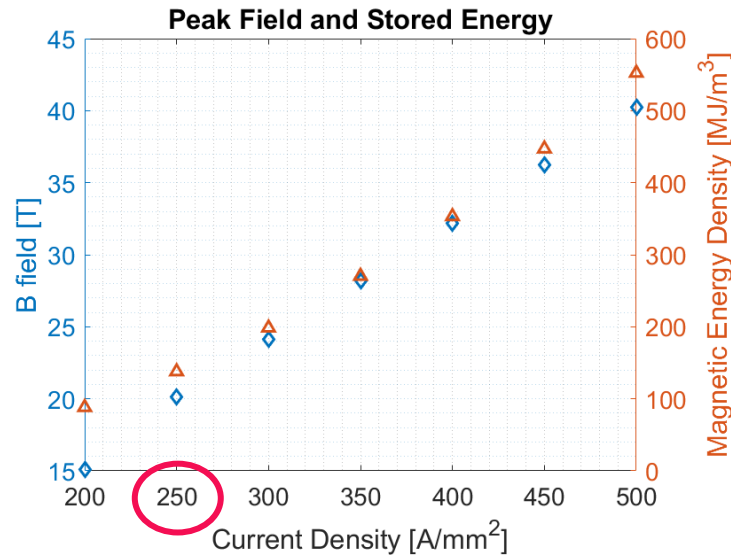
$J_{eng} = 250 \text{ A/mm}^2$



Minimum Current Margin: 15.3%

Max Hoop Stress: 1.2 GPa

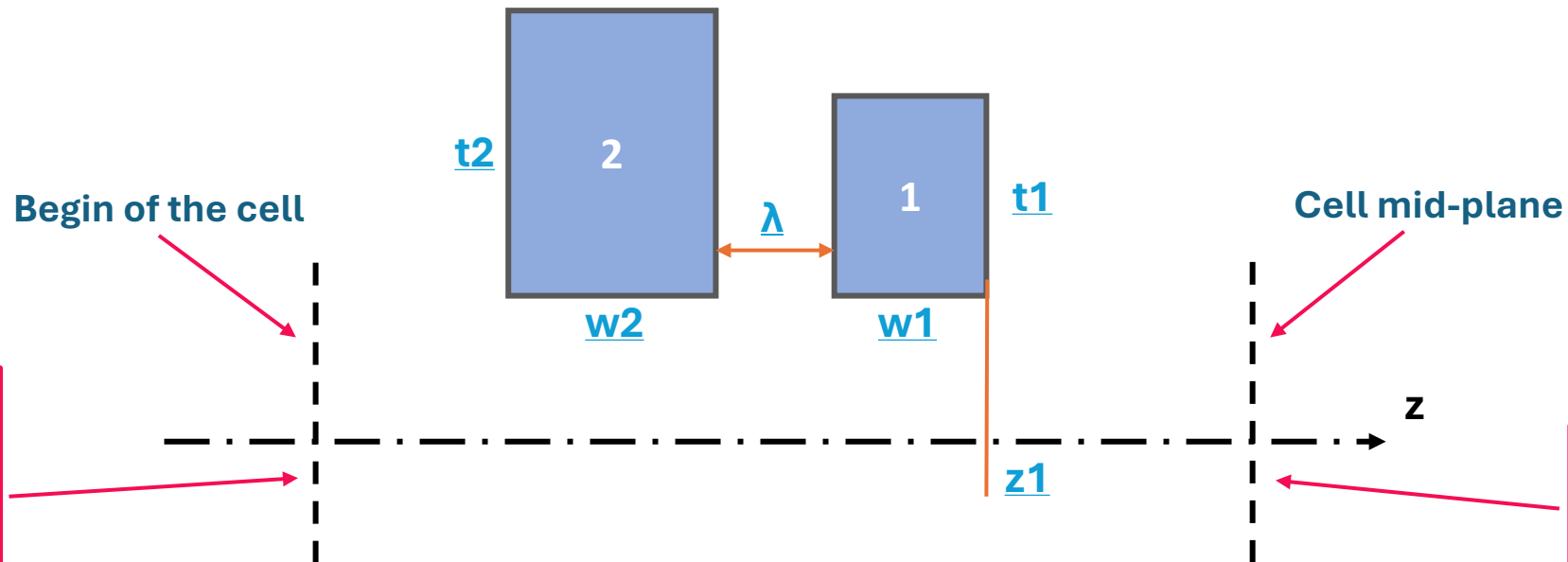
Stresses are the limit!



# Solenoids optimization strategy: lattice configuration

- Divide the coil section in two to reduce the peak field and optimize their shape to produce the same target field.
- Parametric sweep of the coil geometrical parameters:  $6^4$  combinations.

Coil scheme & geom. parameters considered:



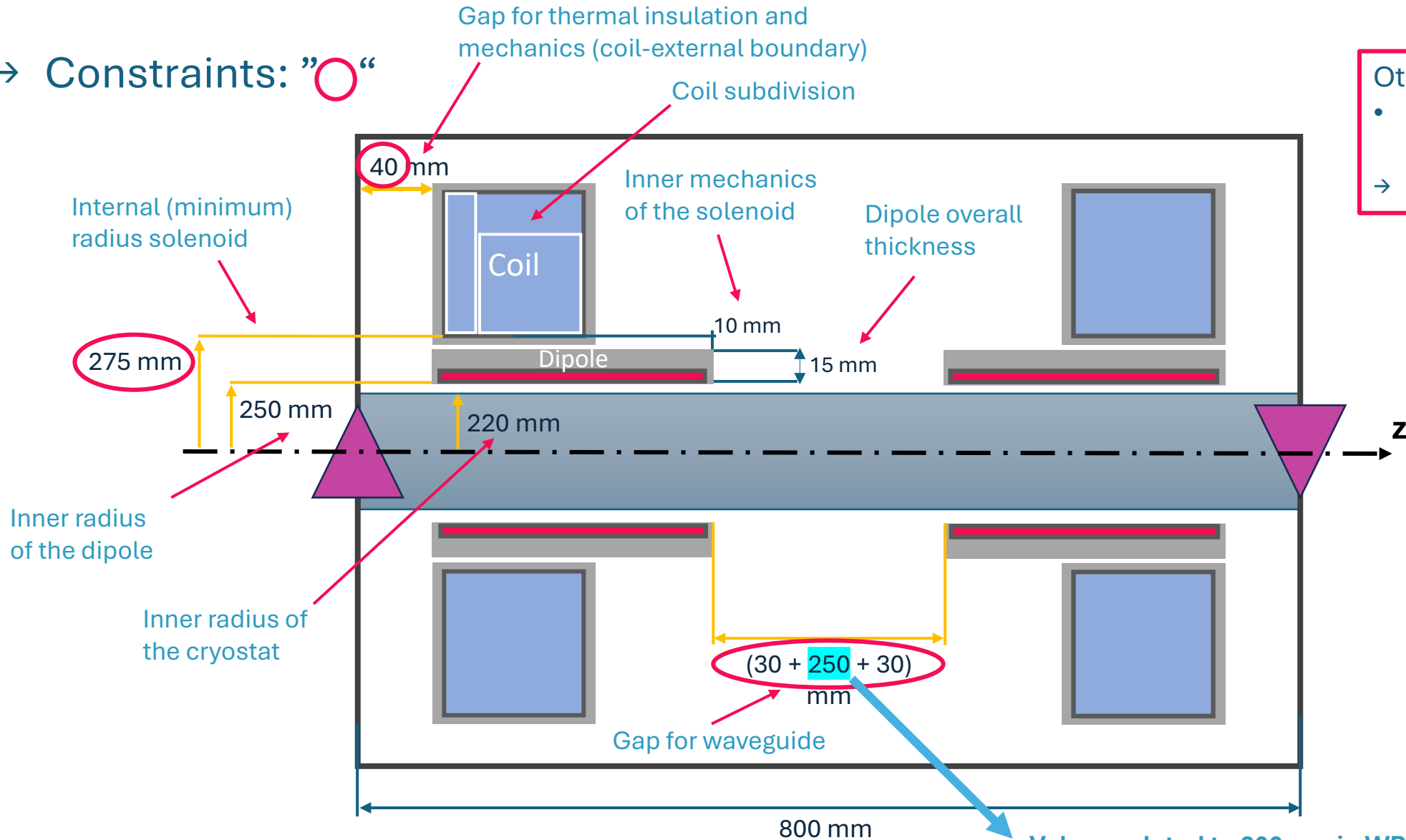
**Nota Bene:**

- Periodicity accounted in the stage modelling.

**Symmetry condition on the cell mid-plane**

# Constraints

→ Constraints: "○"



Other constraint:  
• Aspect ratio of the coil section:  
→  $1/3 < w_x/t_x < 3$

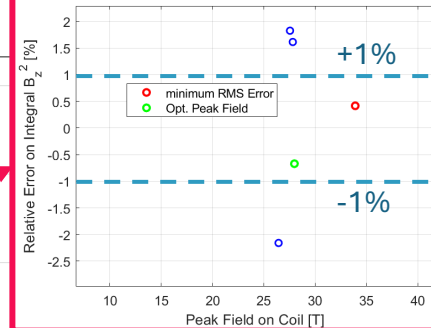
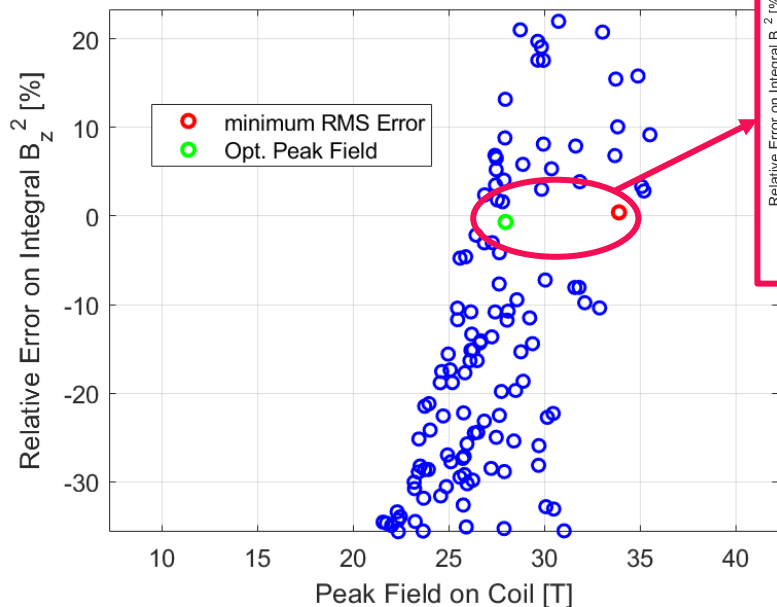
Value updated to 200mm in WP8 meeting #22

# Optimization targets

- The search of the **optimal solenoid configuration** should target the following:
  - Minimum peak field on the coil section.
  - Minimum RMS error of the axial field w.r.t. the target field expansion.
  - Minimum error on the focusing strength on the cell length (integral of  $B_z^2$  along the cell axis).
  - From results considerations: maximum B2 field harmonic component.

2 configuration found:

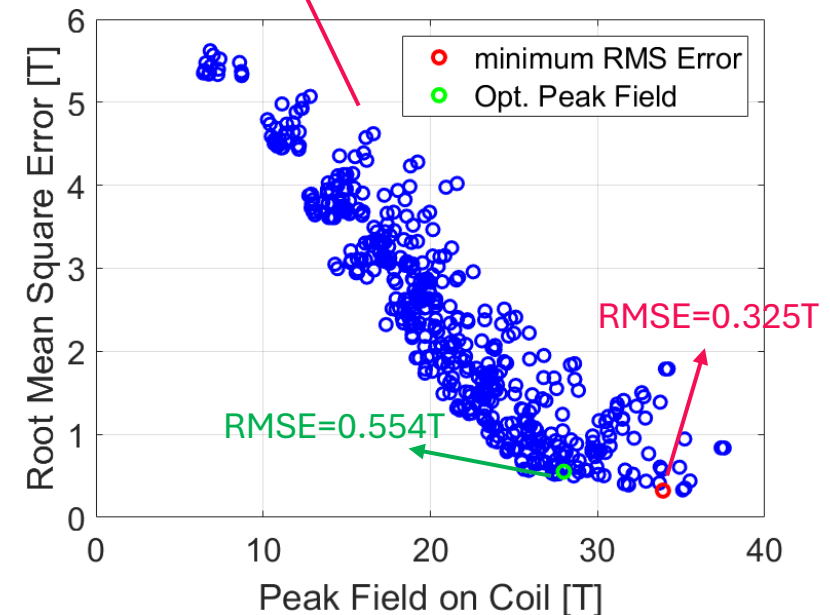
- Minimum RMSE.
- Optimized: lower peak field.



Focusing  
Strength  
error within  
1%

Each point corresponds to a unique combination of the geometrical parameters

$$RMSE = \sqrt{\frac{\sum_{i=1}^N \|y(i) - \hat{y}(i)\|^2}{N}}$$





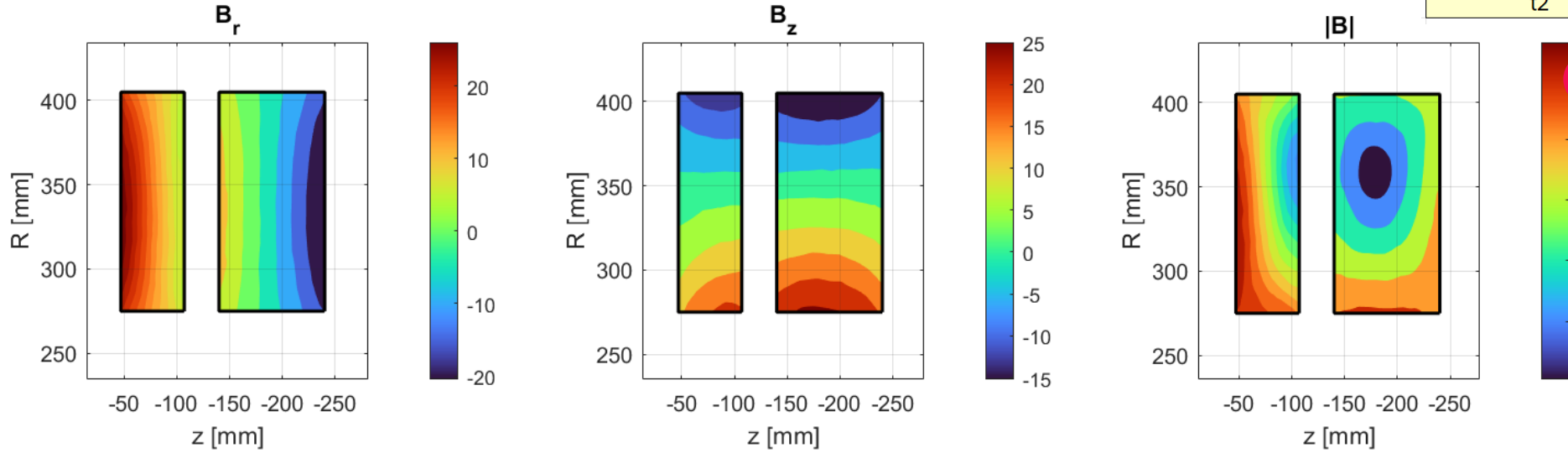
# Results

$$J_{eng} = 500 \text{ A/mm}^2$$

→ Lower peak field configuration: RMSE = 0.554 T.

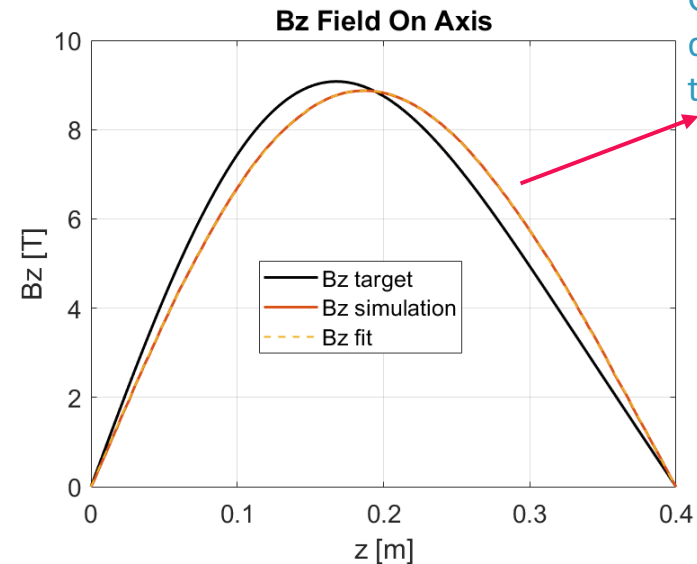
Simulated coil geometry	
z1	240 mm
w1	100 mm
t1	130 mm
z2	107 mm
w2	60 mm
t2	130 mm

N.B:  
6D stage  
lattice  
considered!



Peak field still high, but improved w.r.t. single coil stack (>40T)!

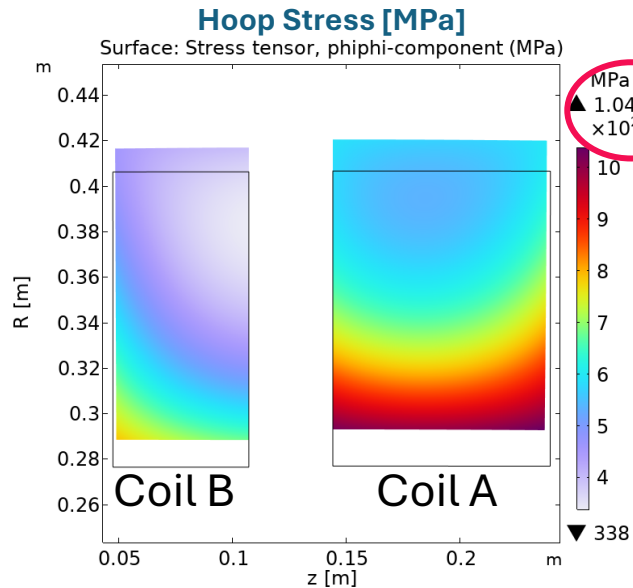
Coil Parameters	
Current Margin [%]	30.9
Minimum Critical current [A]	582
Temperature Margin [K]	27.2
Total magnetic energy in cell [MJ]	47.4



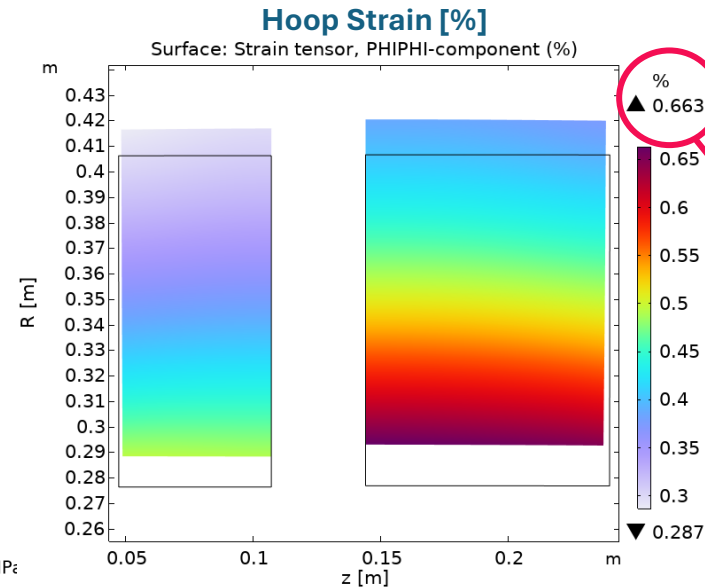
Computed field disaligned w.r.t. the target...

# Mechanical Analysis: No prestress, no radial constraints

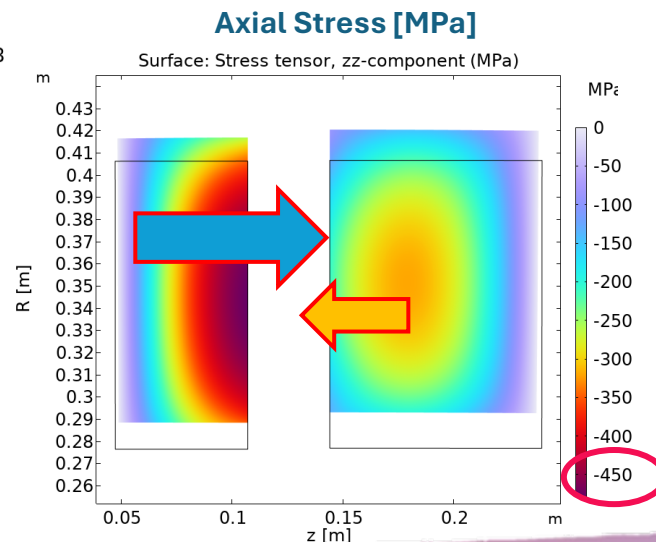
- Mechanical analysis of the **free-expanding coils**.
- **Limiting hoop stress values!**
- Resulting force on the coils points towards the center of the cell (**attractive force**).



No radial constraints applied.  
→ The coils are **not self-sustaining**



>> Limit value of **0.3 %**



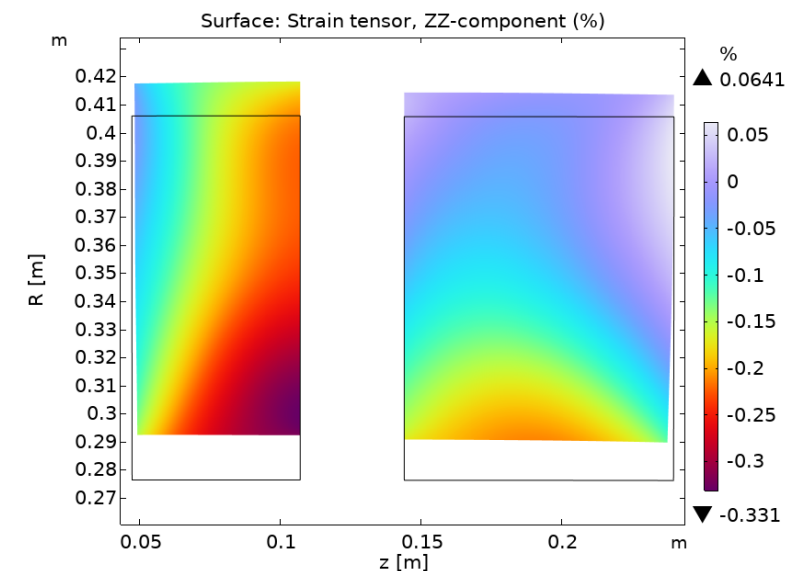
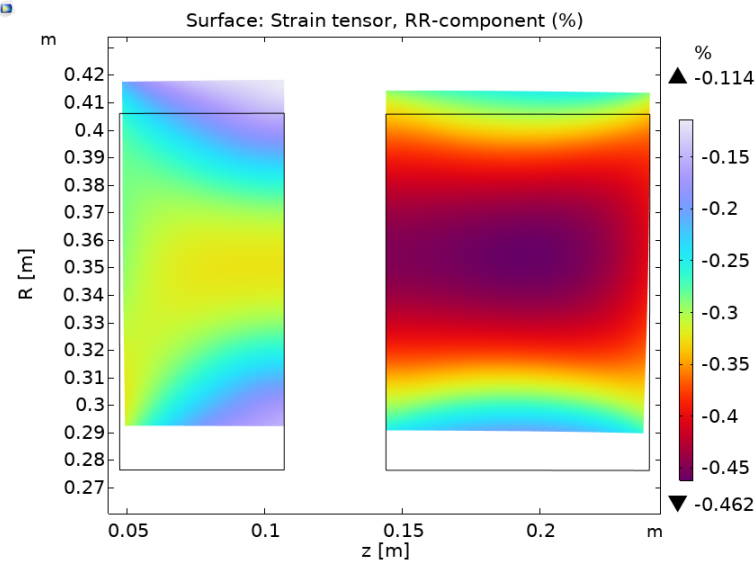
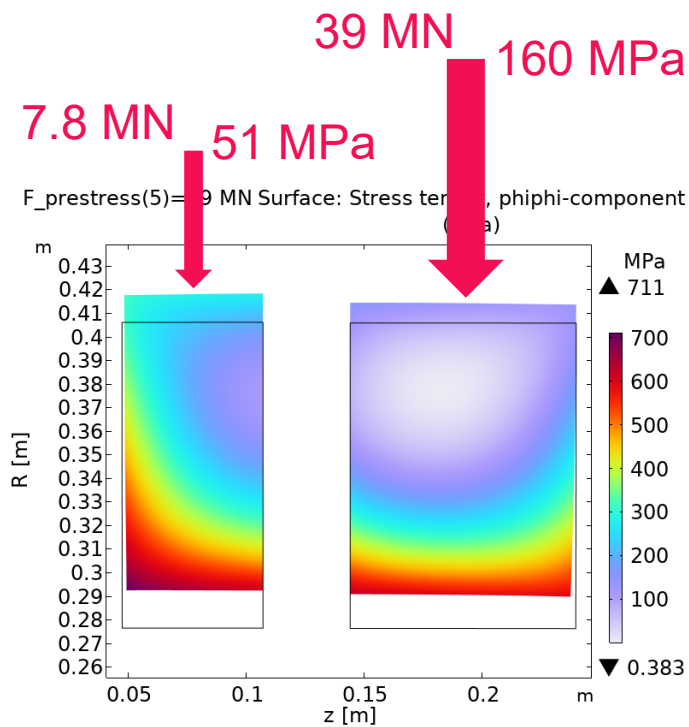
**Coil Axial Forces:**  
→ Coil A: **47.5 MN**  
→ Coil B: **-119 MN**  
**Net Force:**  
→ **-71.5 MN**

N.B:  
6D stage **lattice** considered!

# Prestress Study: Pressure on free boundary (I)

- Free radial expansion, pre-stress added as an external uniform pressure acting on the  $R = R_{ext}$  plane.
- Parametric sweep of the applied force on the boundary stopped when hoop stress started to get negative values. Last step: 39 MN on Coil1, 7.8 MN on Coil2.
- Max hoop stress still **>700 MPa** 😞. Max hoop strain 0.5% > limit hoop strain! 😞

First approach:  
avoid negative  
hoop stress  
values!



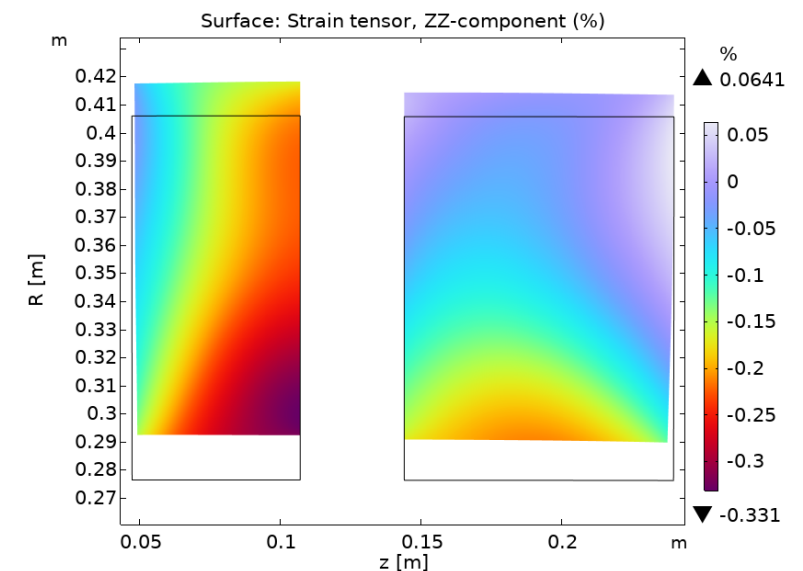
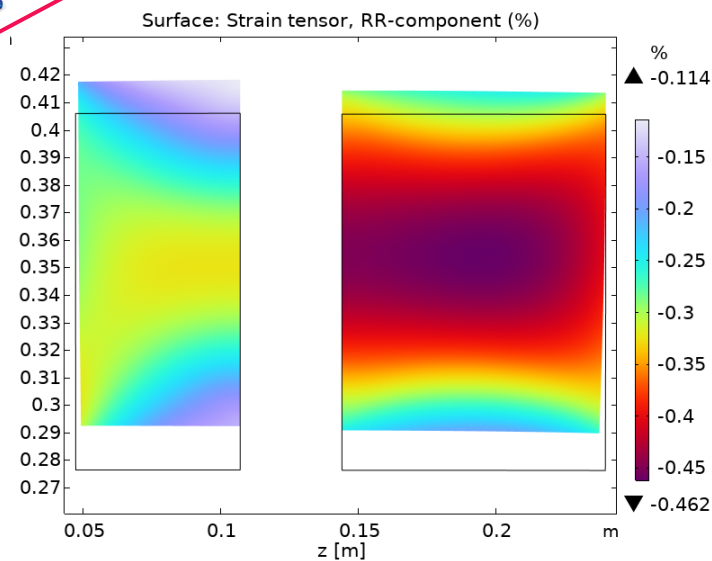
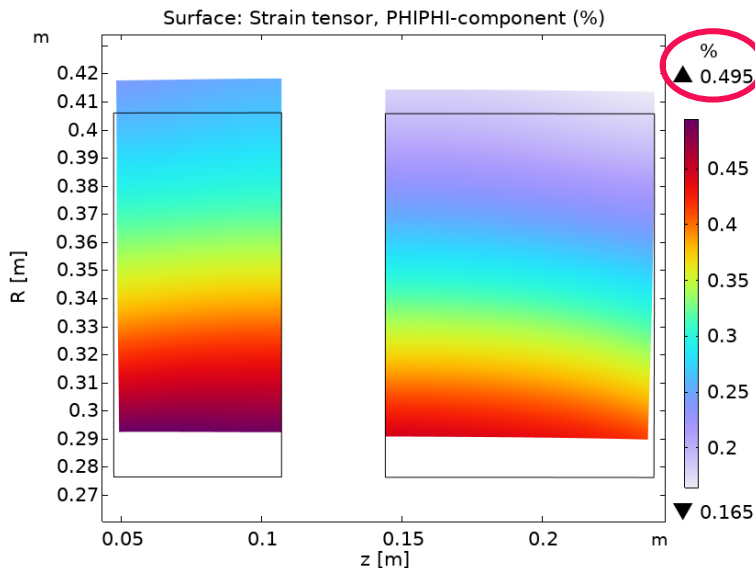
N.B: 6D stage lattice considered!

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First approach:  
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Max hoop strain > 0.3 %...

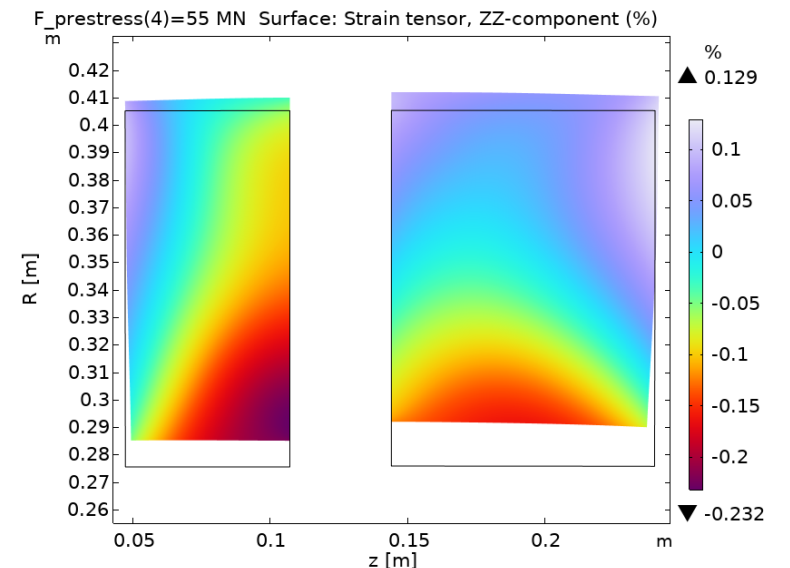
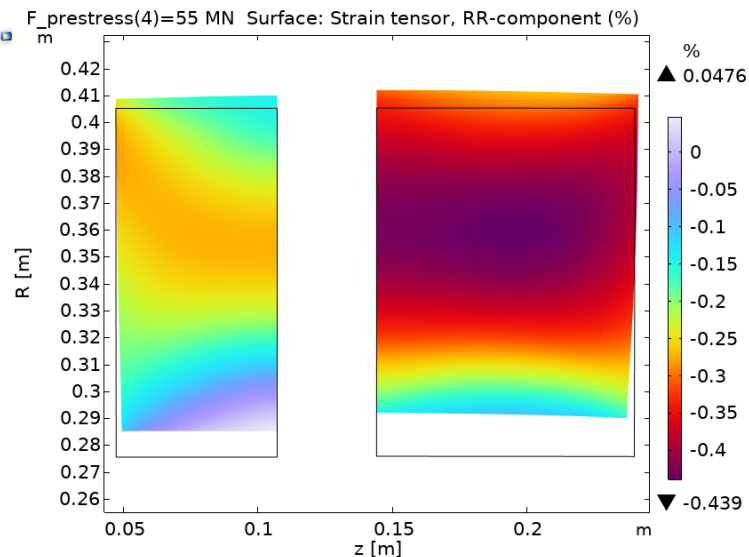
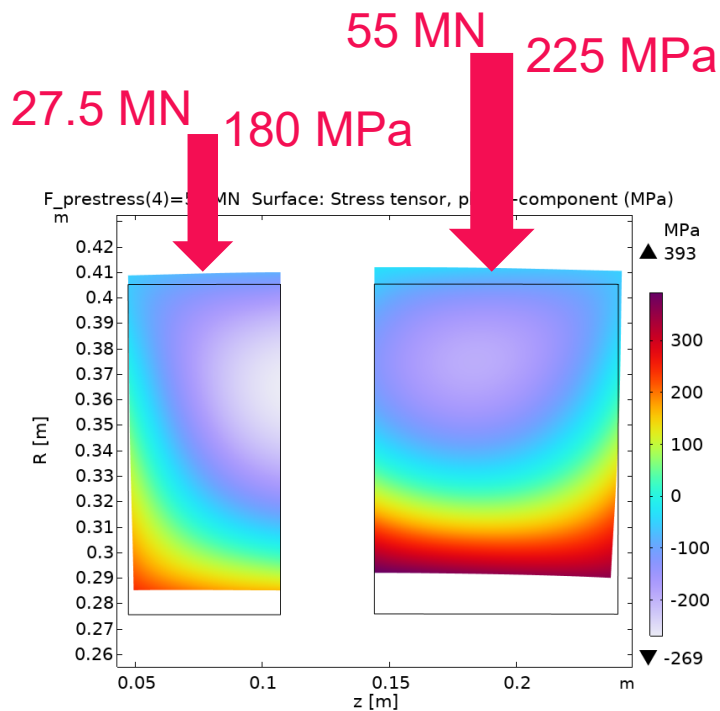


N.B: 6D stage **lattice** considered!

# Prestress Study: Pressure on free boundary (II)

- Free radial expansion, pre-stress added as an external uniform pressure acting on the  $R = R_{ext}$  plane.
- Parametric sweep of the applied force on the boundary stopped when hoop strain  $< 0.3\%$  reached... BUT negative hoop stress. → Last step: 55 MN on Coil1, 27.5 MN on Coil2.
- Max hoop stress 393 MPa / -269 MPa, Max hoop strain  $0.28\% < \text{limit hoop strain!}$

Approach:  
hoop strain  
 $< 0.3\% !!$



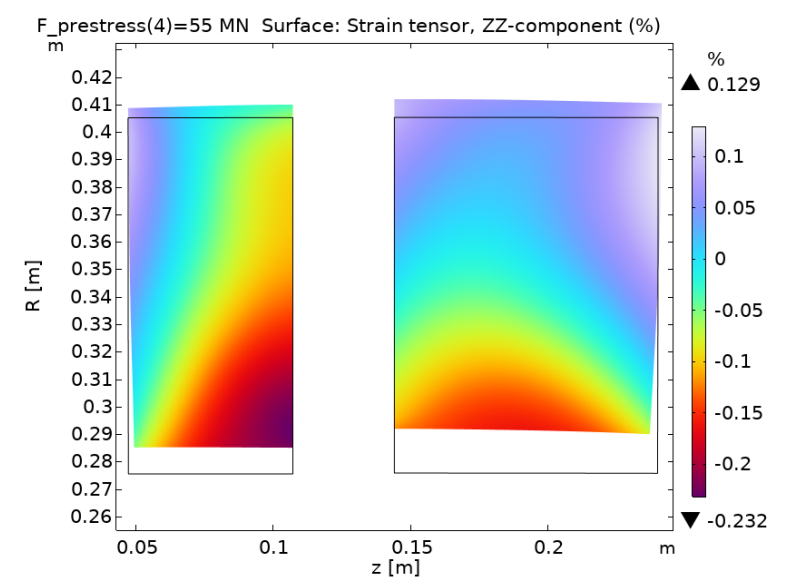
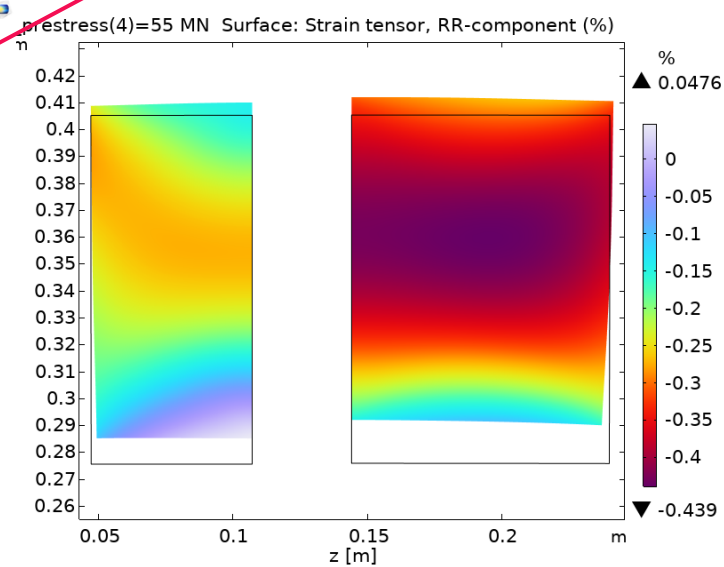
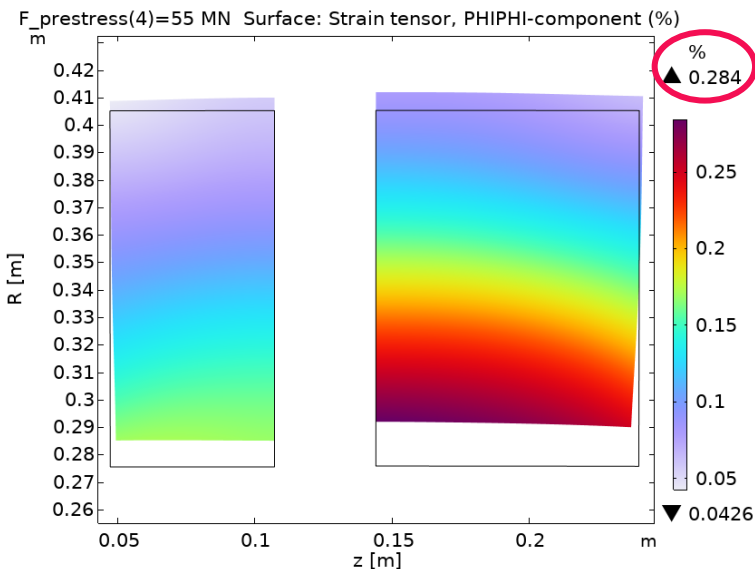
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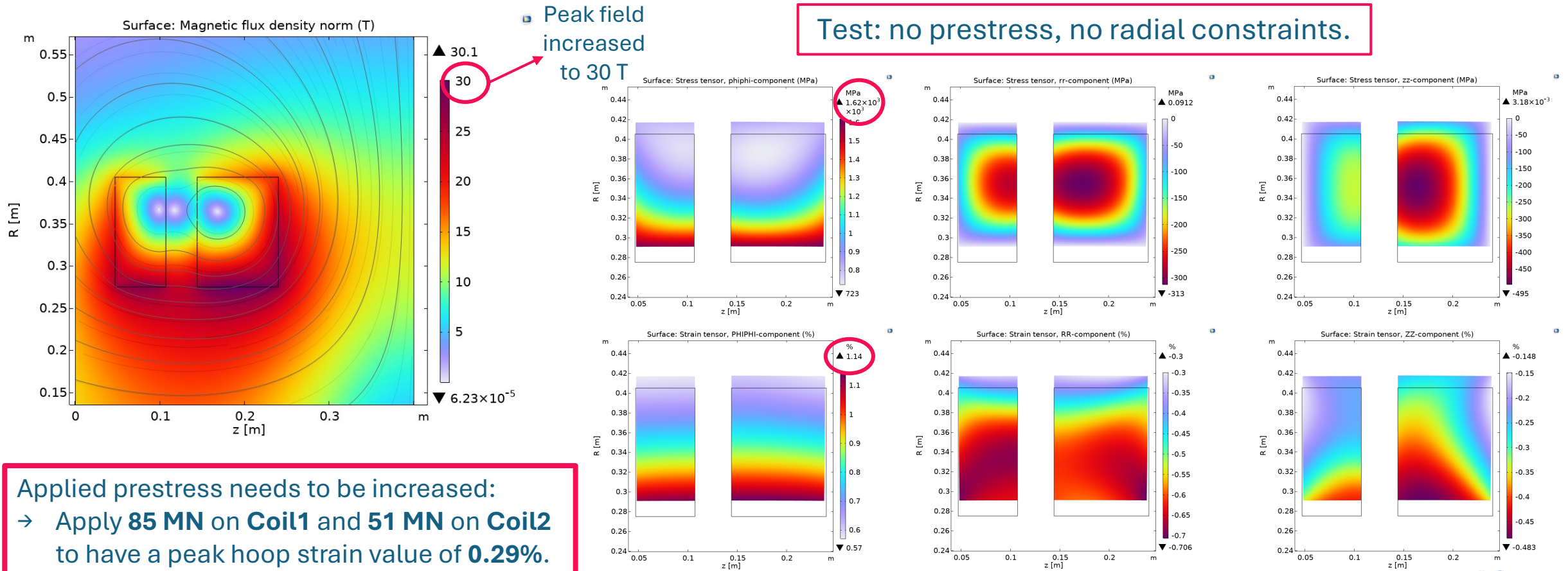
Max hoop strain  $< 0.3\% !!$



N.B: 6D stage lattice considered!

# Mechanical Analysis: stand-alone demonstrator

- Results for the **stand-alone** demonstrator stage.
- This case is representative of the steady-state condition on an S5 stage following a fault shutdown on subsequent stages.



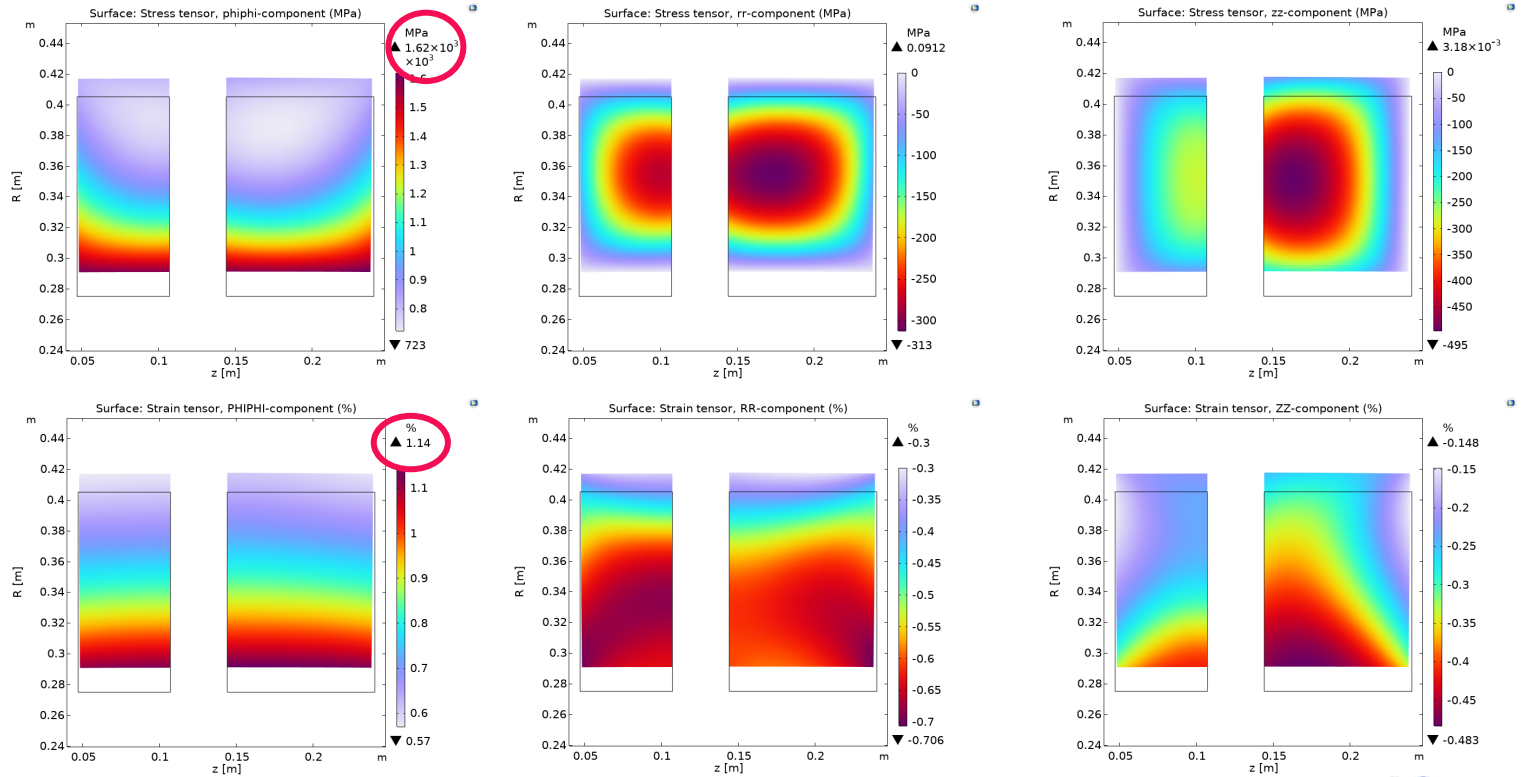
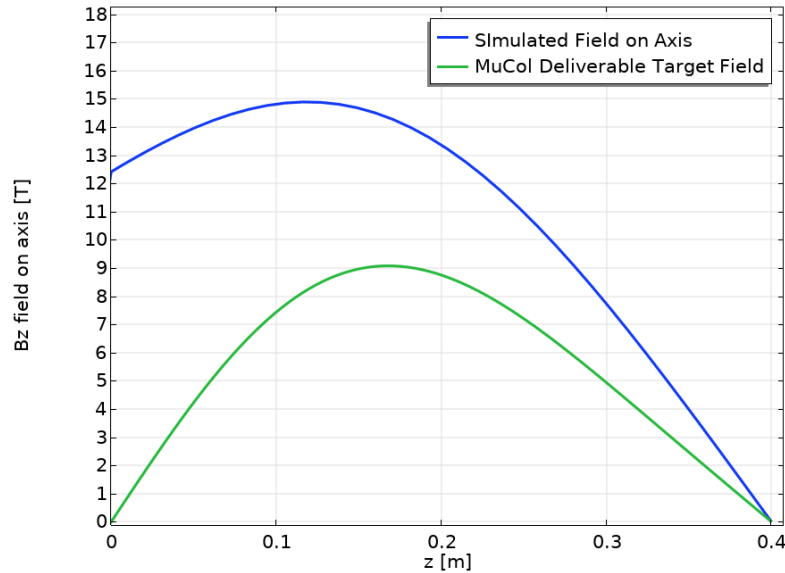
Applied prestress needs to be increased:  
→ Apply **85 MN** on **Coil1** and **51 MN** on **Coil2** to have a peak hoop strain value of **0.29%**.  
Still **negative hoop stress** regions.

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- Results for the **stand-alone** demonstrator stage.
- This case is representative of the steady-state condition on an S5 stage following a fault shutdown on subsequent stages.

Test: no prestress, no radial constraints.

Line Graph: Magnetic flux density, z-component (T) Line Graph: Target Field

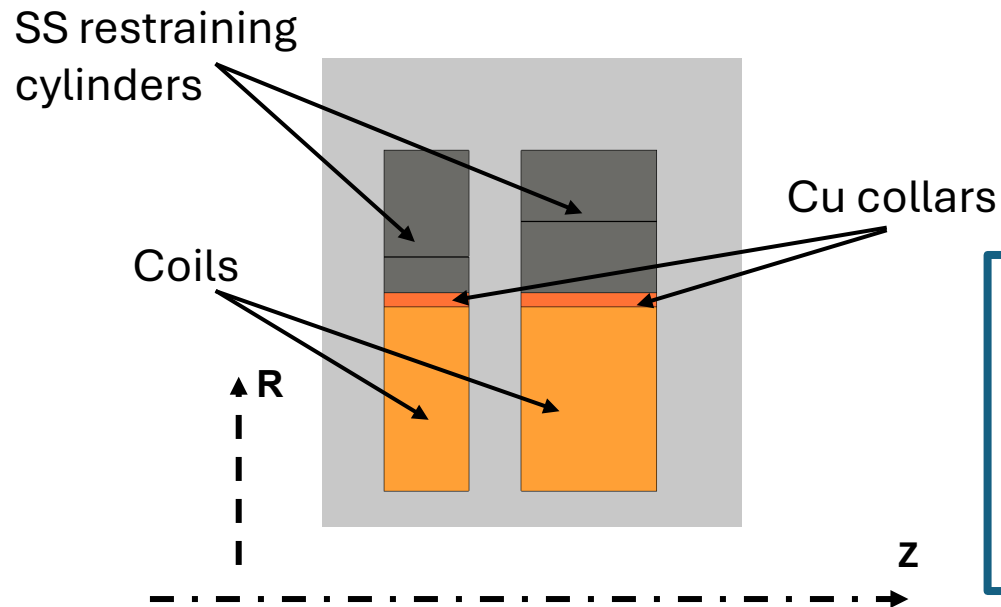


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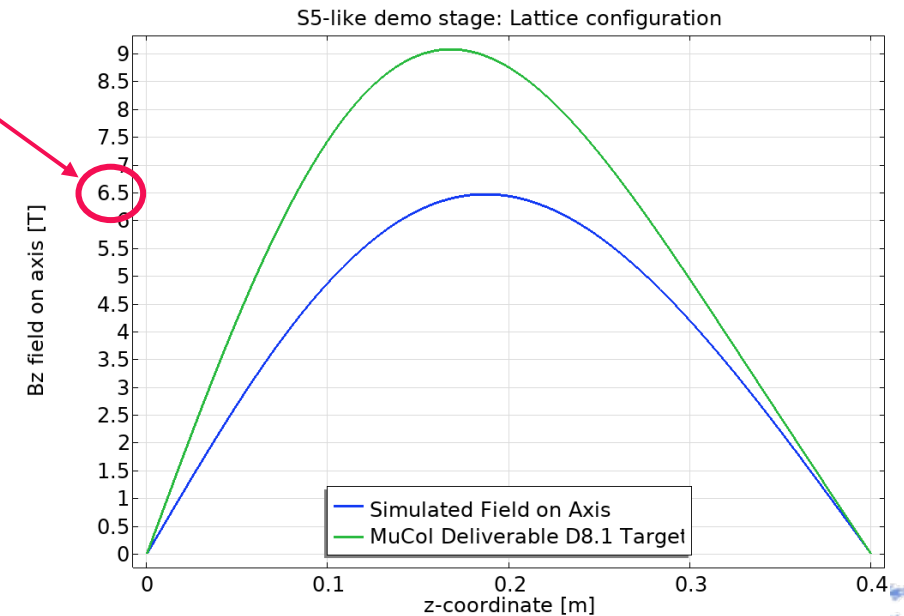
# Reduced-current solenoid for first integration exercise

- Considering the required field targets, the **proposed solenoid configuration still does not respect the mechanical limits** of HTS-based coils.
- A **reduced-current configuration** has been studied:  $J_{\text{eng}} = 375 \text{ A/mm}^2$  (25% reduction).
- The **magnet design and cell integration** has been conducted on this configuration. The displayed **results does not meet the requested field targets on the beam axis**.
- Both configurations (*stand-alone, lattice*) has been considered in the mechanical design.



Reduced peak field  
on axis: 6.5 T.

Two separated AISI 316LN steel restraining collars has been added: in case of stand-alone stage operation, the coil-structure deformation will be contained by the most external SS ring.

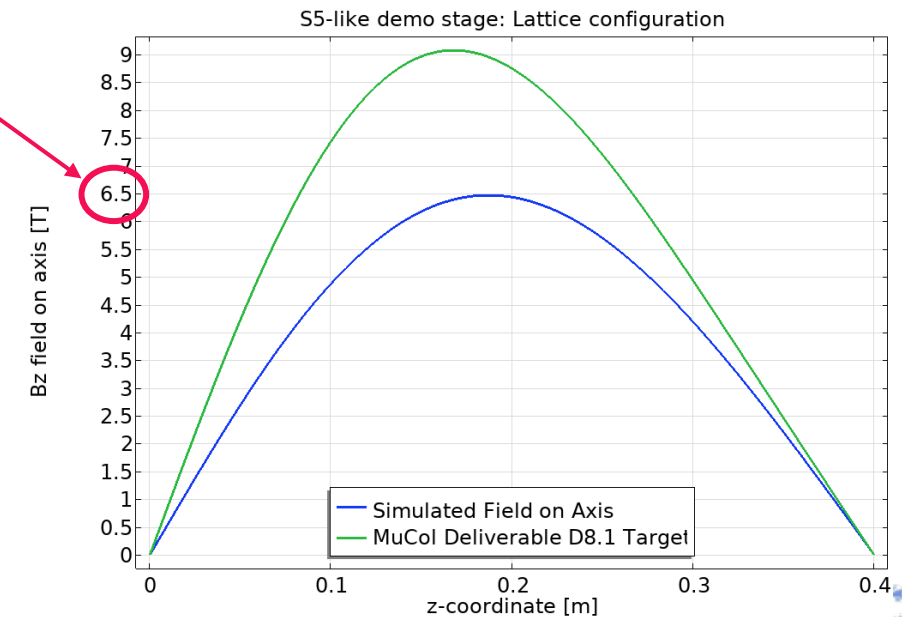


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Figures of Merit	Value
RMS difference [T]	1.67
Reduction on Integral $B_z^2$ along the axis [%]	47.03

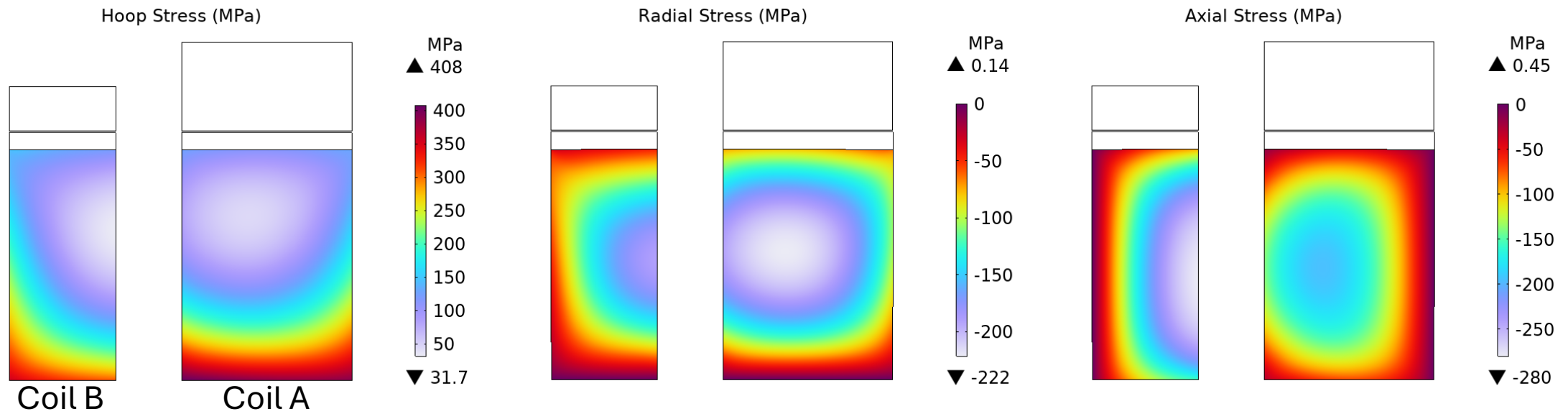
Reduced peak field  
on axis: 6.5 T.



# Reduced-current solenoid design: lattice operation (I)

- The mechanical design of the S5-like solenoids converged to a **25% reduced current configuration**.
- To limit the stresses in the solenoids in lattice operation, SS collars must be fit on the **10 mm Cu rings** containing the coils. A **50 mm SS collar** is needed for **coil A**, **25 mm SS collar** for **coil B**.
- A **0.8 mm interference** between the two collars is **required** to contain the stresses in a **self-sustaining coil configuration**.

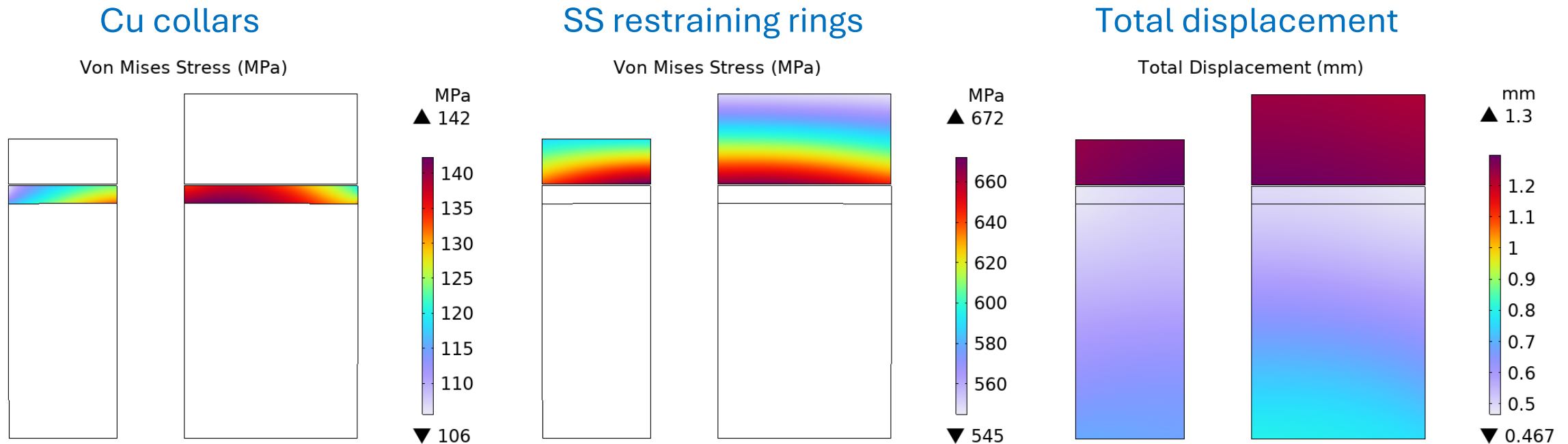
## Coil stress components: lattice configuration



**Stresses are within the mechanical limits!**

# Reduced-current solenoid design: lattice operation (II)

- The **Von Mises stress** was assessed in the **Cu collars** and **SS restraining rings**.
- The resulting stresses are **compatible with the elastic limits of the materials** considered.
- The **total radial displacement** is needed to determine the radial gap with the external SS ring required for the stand-alone cell operation.

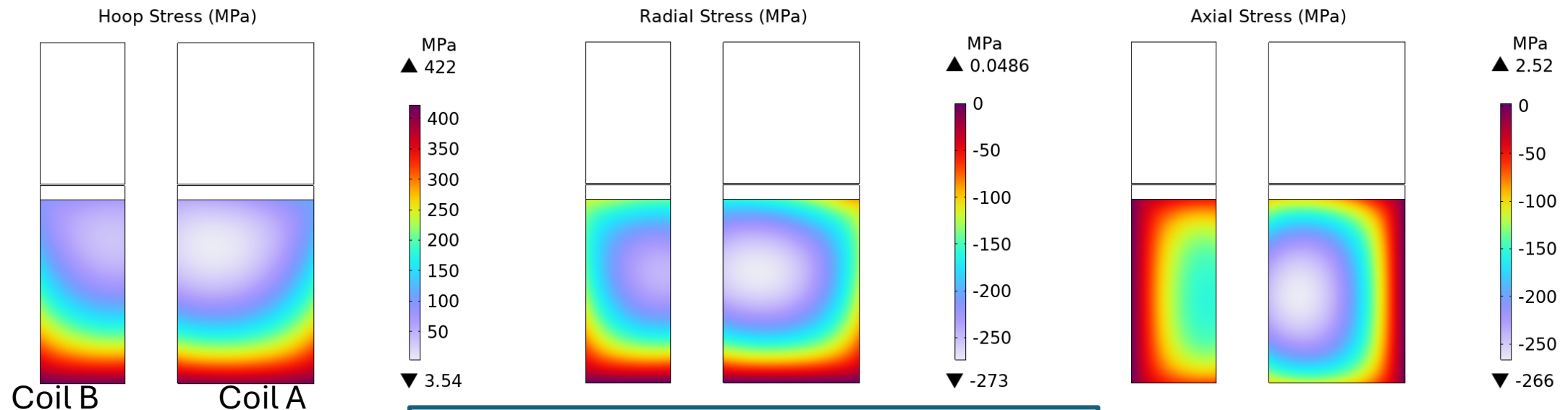


**Stresses are within the mechanical limits!**

# Reduced-current design: stand-alone operation (I)

- The load conditions in the stand-alone cell operation are remarkably different to the analyzed lattice configuration.
- To limit the stresses in stand-alone operation, **additional SS collars must be fit** on the coils structure. Addittional **50 mm SS collar** is needed for **coil A**, **75 mm SS collar** for **coil B**.
- A **0.8 mm interference** between the two collars is **assumed**.

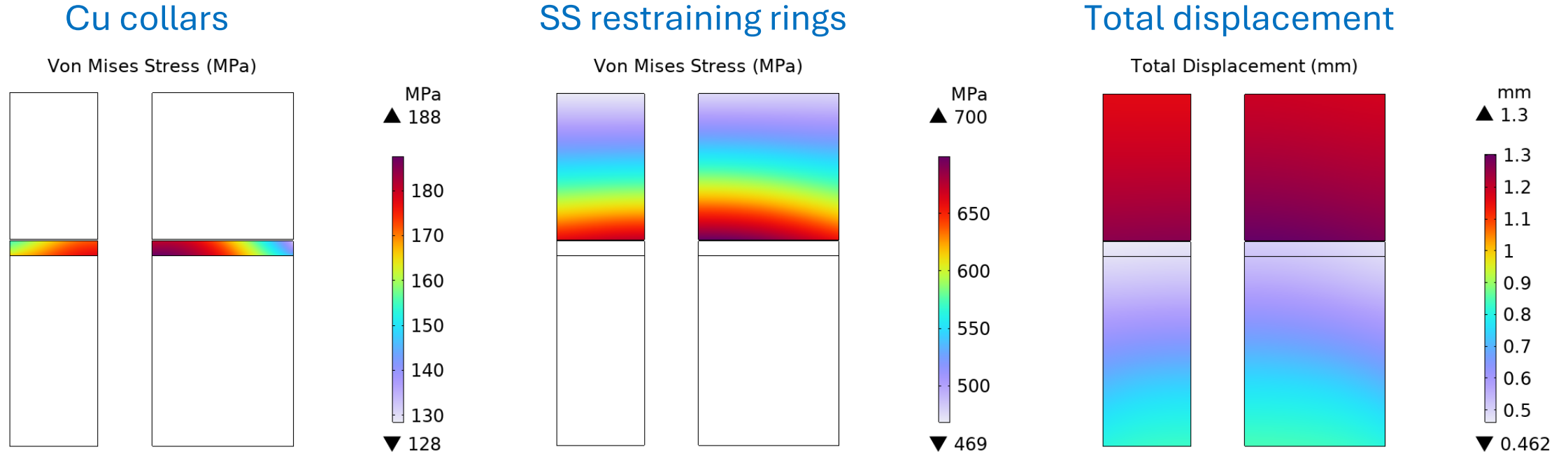
## Coil stress components: lattice configuration



**Stresses are within the mechanical limits!**

# Reduced-current design: stand-alone operation (II)

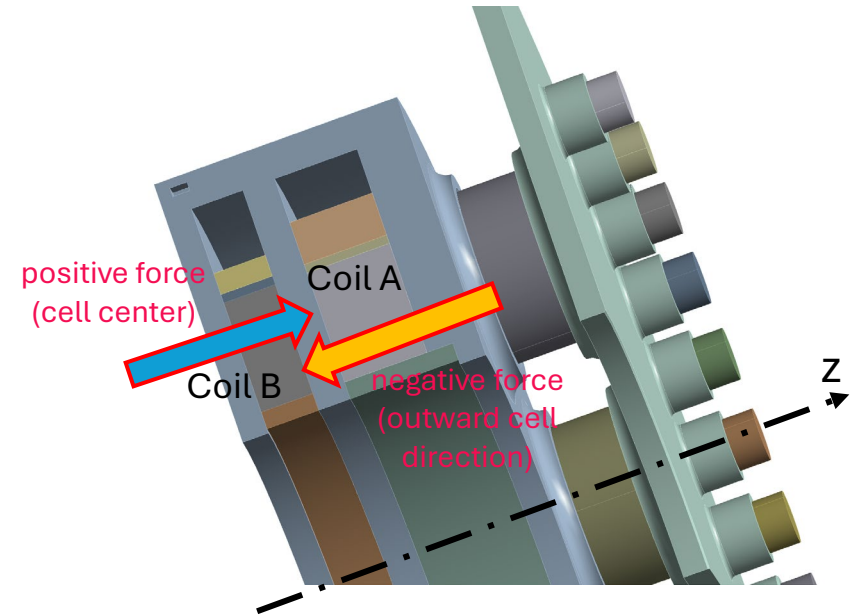
- The **Von Mises stress** was assessed in the **Cu collars** and **SS restraining rings**.
- The resulting stresses are **compatible with the elastic limits of the materials** considered.
- The **total radial displacement** has been assessed on the structure.



**Stresses are within the mechanical limits!**

# Reduced-current design: support structure design

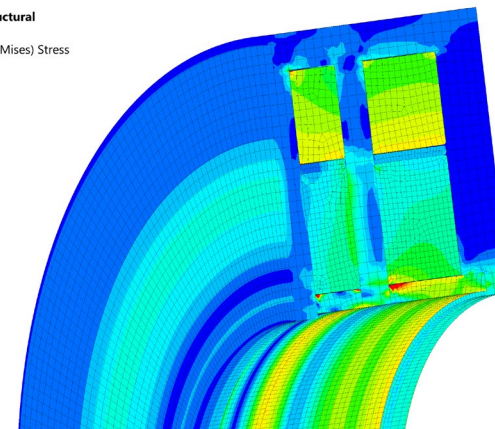
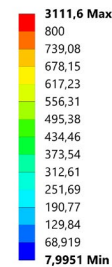
- The coil support structure has been designed to sustain the coil axial forces in the two configurations: **stand-alone**, **lattice**.
- Thick AISI 316LN shell is needed to sustain the axial forces in normal out-of-cell direction.
- Even in the reduced-current configuration, **the mechanical design of the support structure is not trivial.**



Coil Axial Forces	Coil A/Coil B Value [MN]	Net Force Value [MN]
<b>Lattice configuration</b>	-27 / +67	+50
<b>Stand-alone configuration</b>	-55 / +35	-20

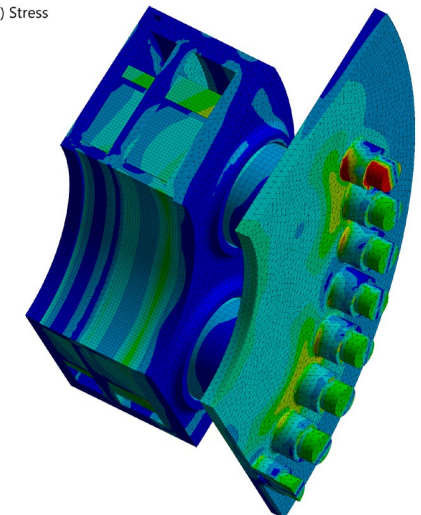
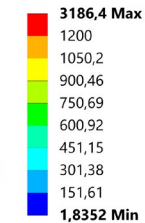
Stand-alone configuration:  
Von Mises Stress [Mpa]

C: Copy of Static Structural  
Equivalent Stress  
Type: Equivalent (von-Mises) Stress  
Unit: MPa  
Time: 1 s  
11/10/2024 13:37



Lattice configuration:  
Von Mises Stress [Mpa]

D: Static Structural  
Equivalent Stress  
Type: Equivalent (von-Mises) Stress  
Unit: MPa  
Time: 1 s  
11/10/2024 13:40



# Summary and next steps

- The magnet design for the S5-like demonstrator cell looks challenging, in particular from a mechanical point of view.
- The **search for an optimized solenoid configuration**, respecting the required focusing strength, converged to the two-coil-subdivision configuration presented.
- The **mechanical limits** of the materials constituting the assembly are **not respected**, thus a reduced-current configuration has been studied.
- A **25% coil current reduction** (from 500 A/mm<sup>2</sup> to 375 A/mm<sup>2</sup>) decrease the coil stresses within their mechanical limits: a **collar and support structure design** has been **proposed**.
- The **support structure** design **still presents criticalities** to be solved, the stresses appear excessive, requiring 60 mm Inconel bolts and a thick shell (with **associated increased cost and manufacturing complications...**).
- **Further iterations are needed**, both on the **magnets design** and on the **cell integration** study!





***Thank you for your attention!***