$B^+ \to K^+ \nu\bar{\nu}$ and other recent Belle II results

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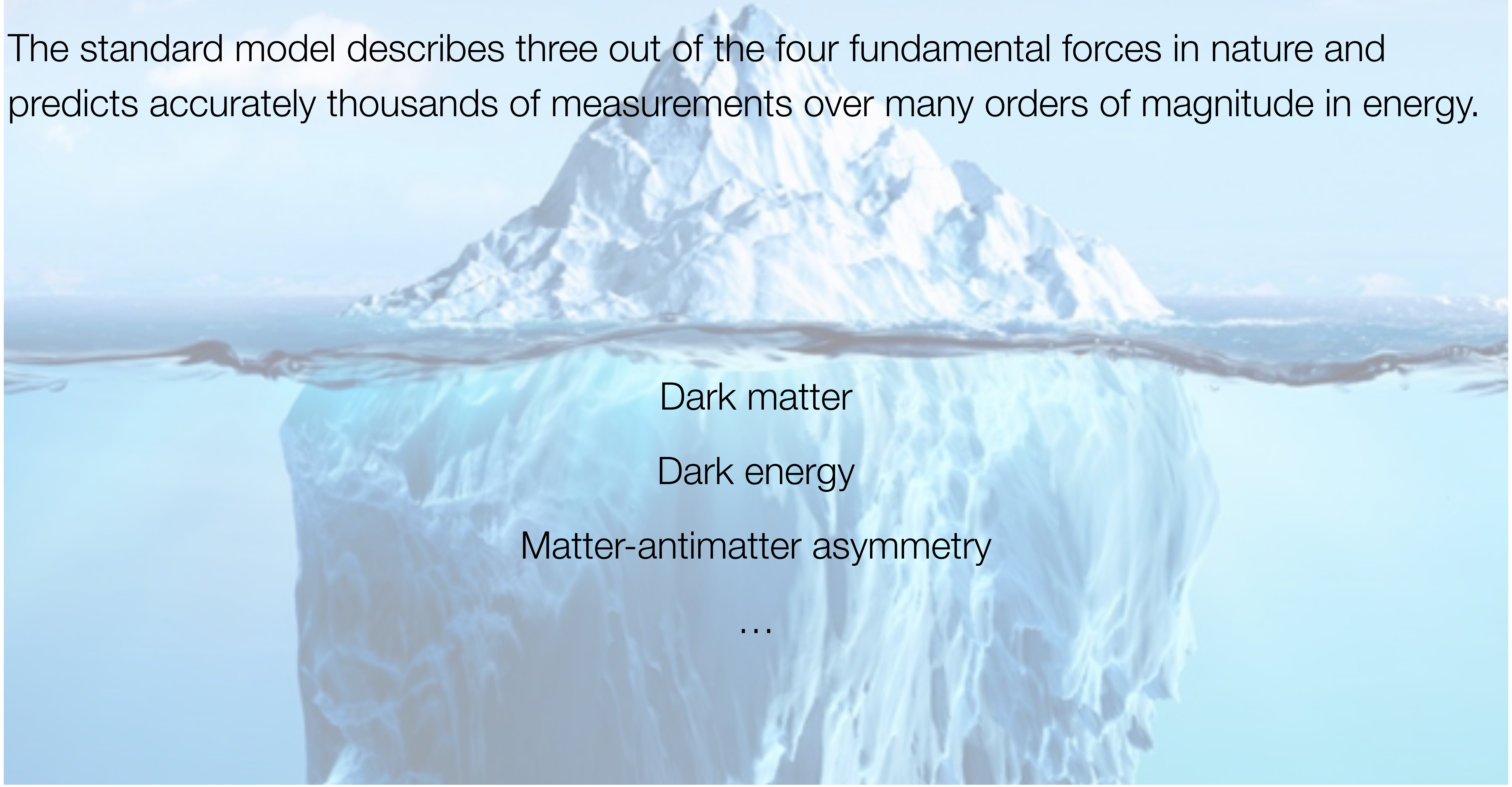
The standard model



The standard model describes three out of the four fundamental forces in nature and predicts accurately thousands of measurements over many orders of magnitude in energy.

Dark matter

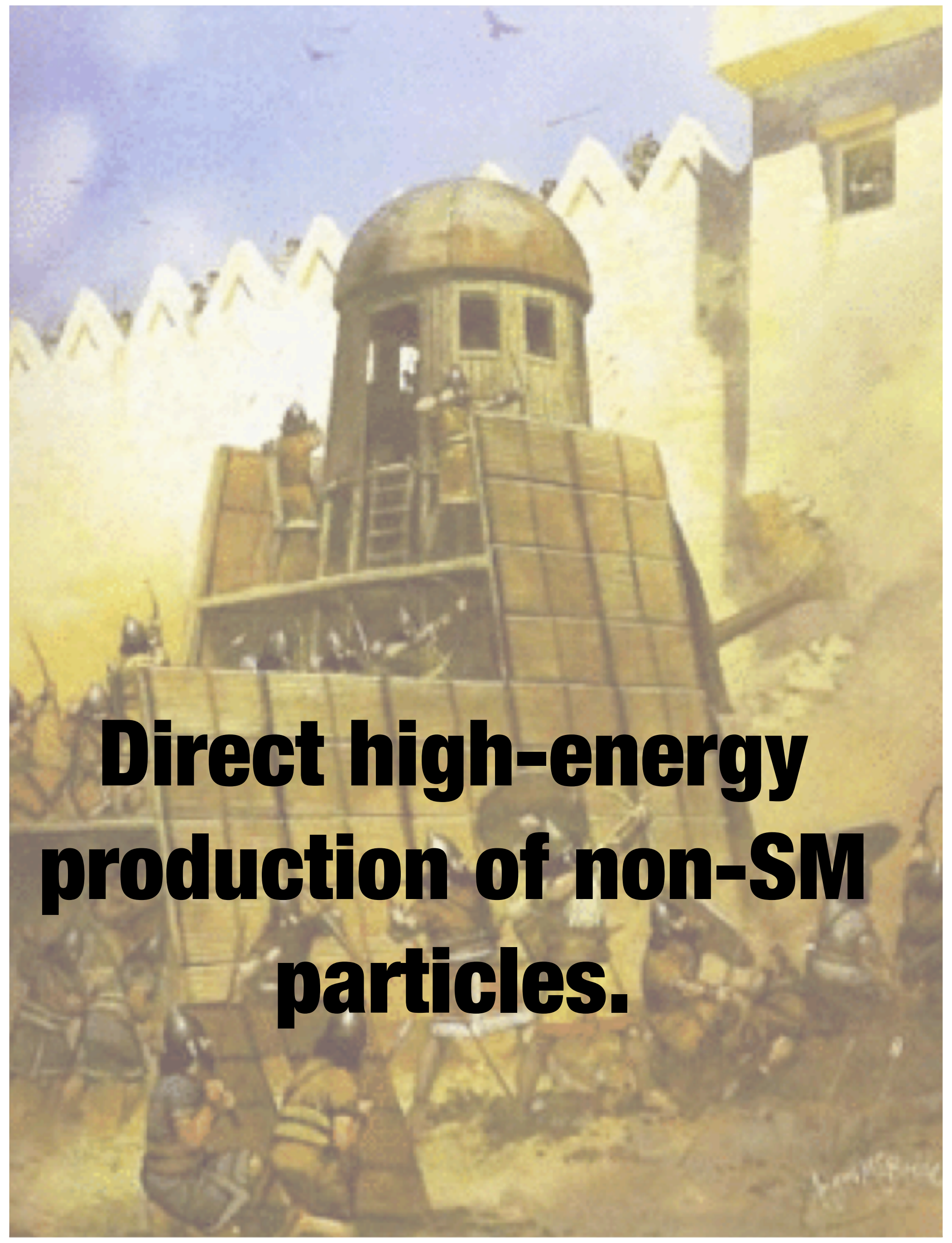
Dark energy

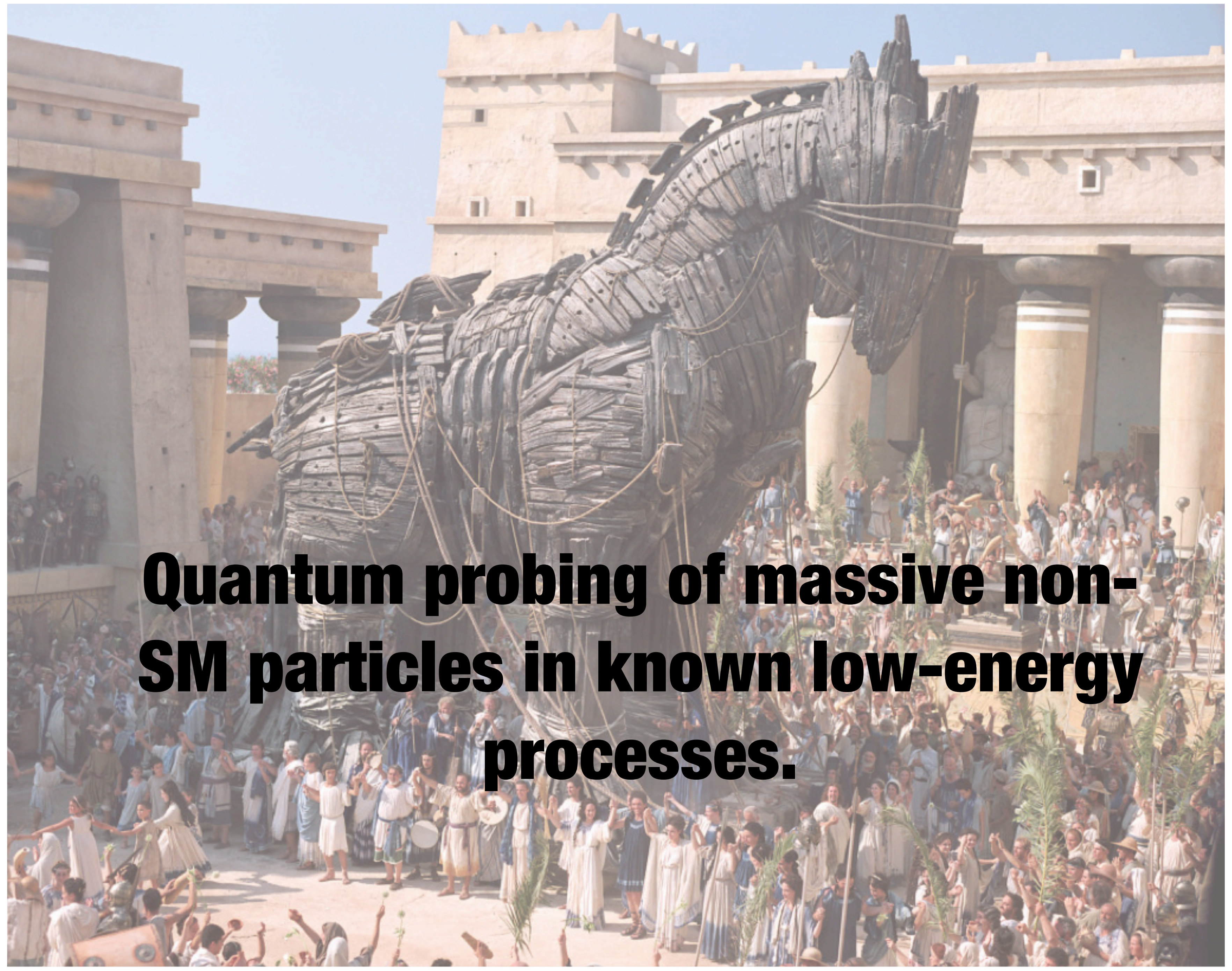
Matter-antimatter asymmetry

…

Determining the theory that completes the SM is the principal goal of today’s particle physics.

Two ways out





Time

Known initial states O(eV÷GeV)	SM or non-SM intermediate states	Measured final states O(eV÷GeV)

Amplitude receives contribution from SM *and* non-SM particles irrespective of mass.

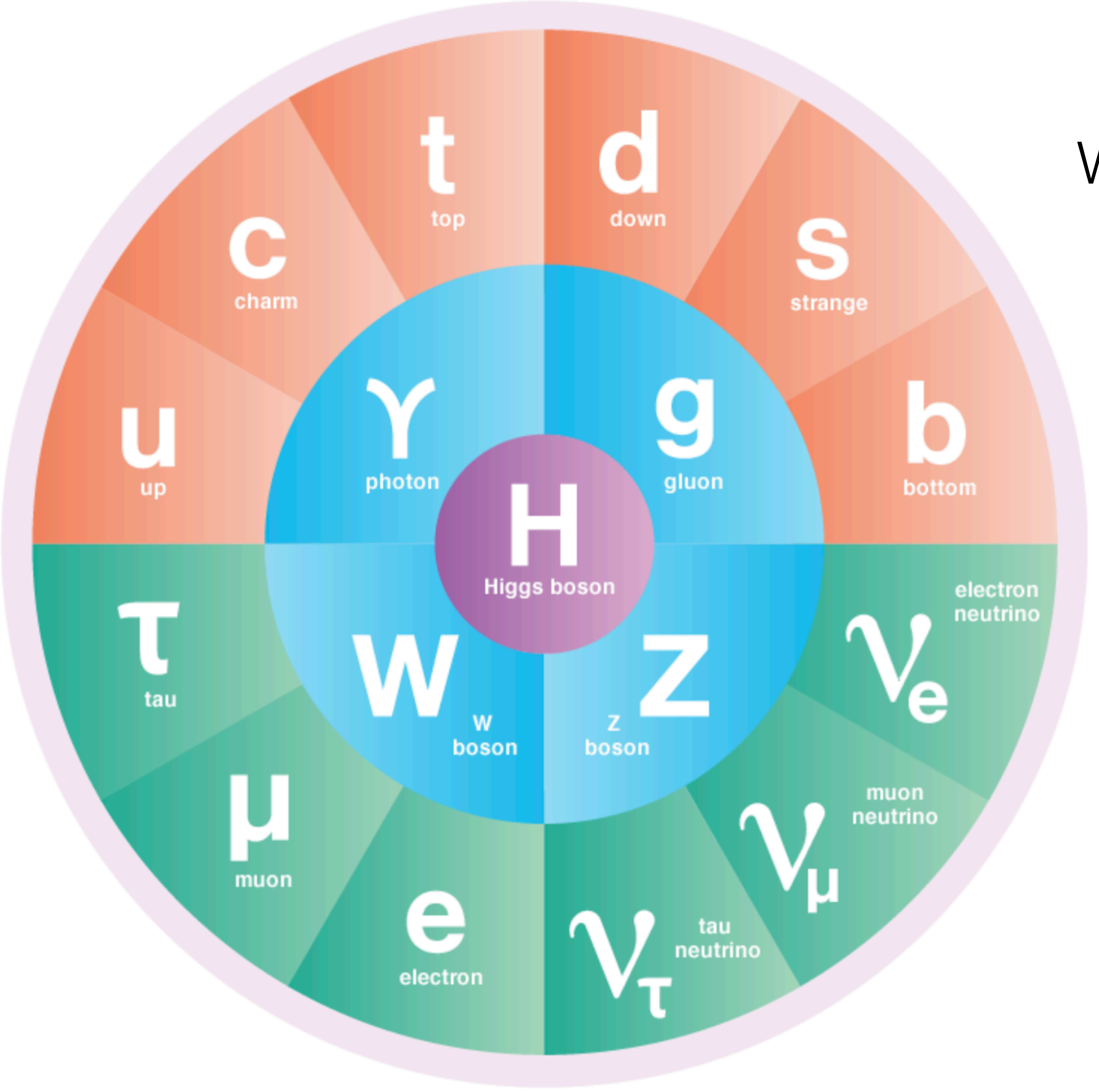
Weak interactions of quarks offer rich opportunities for indirect approach.

Quarks in the standard model

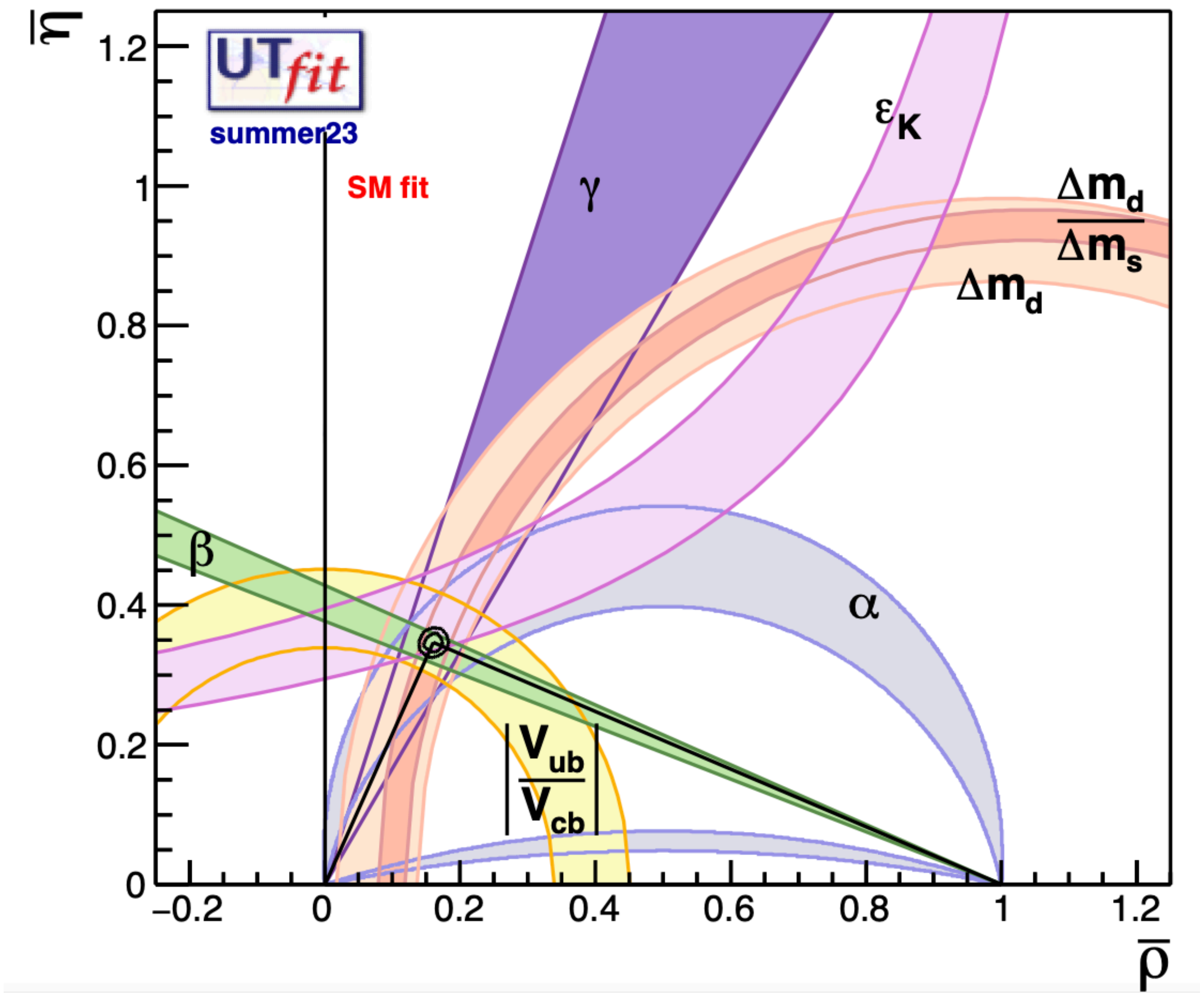
- Transitions of quarks: O(100) accessible processes that are potential for probing non-SM particles
- Violation of charge-parity symmetry

Plenty of opportunities to probe the SM: a rich program ongoing since three decades.

Emerging picture: SM describes well quark-flavor (but within a precision that is still 10-15%).



$$\underbrace{\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix}}_{\text{Weak eigenstates}} = \underbrace{\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}}_{\text{CKM matrix}} \underbrace{\begin{pmatrix} d \\ s \\ b \end{pmatrix}}_{\text{Mass eigenstates}}$$

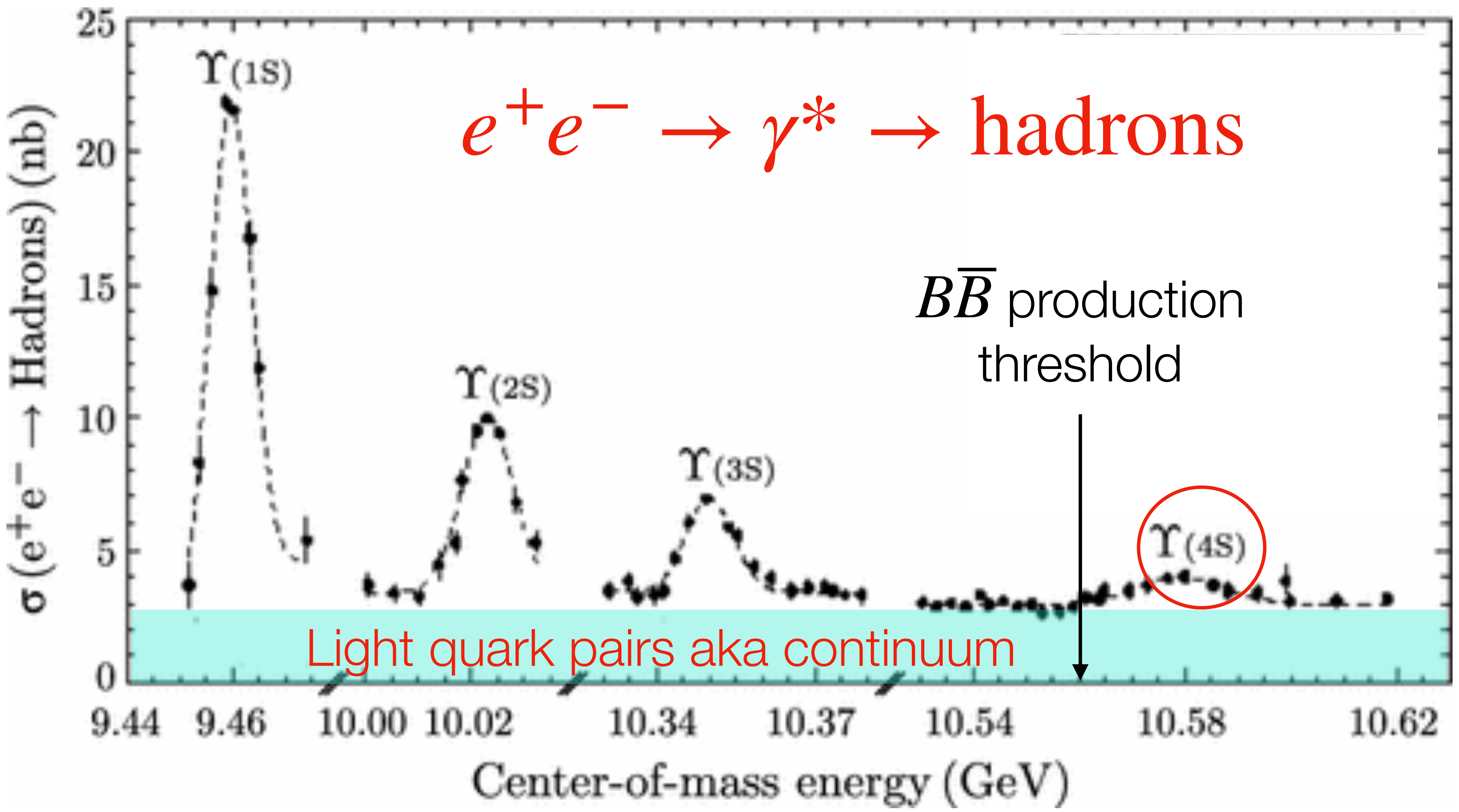


Increase the precision

B factories

Energy-asymmetric electron-positron colliders operating at the energy around the Υ(4S) mass

Aim to produce billions of B and D mesons and τ leptons

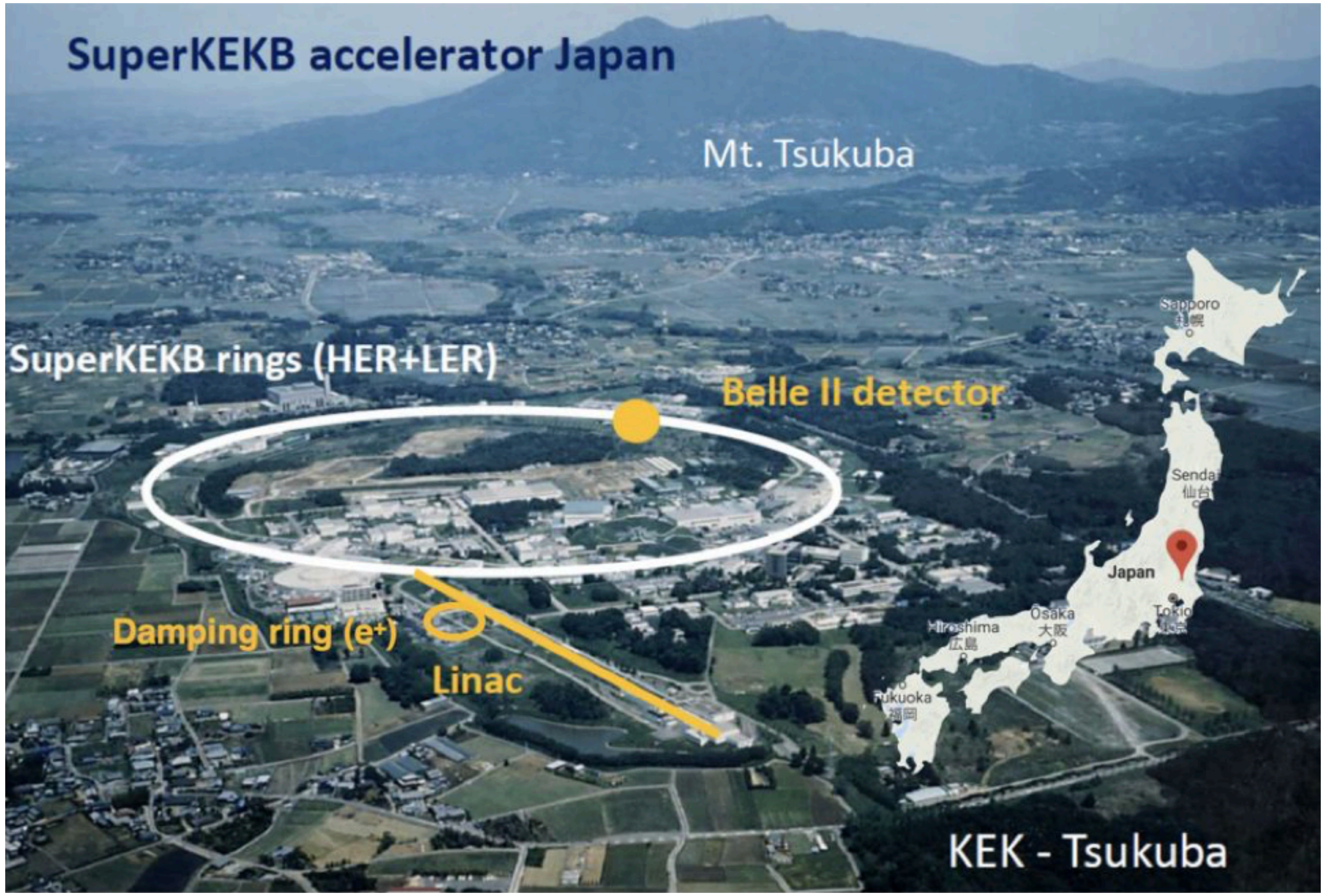


First generation B factories: Belle@KEKB and BaBar@PEP-II

- ~1.5 ab^{-1} collected at and around Υ(4S) mass (roughly 1 ab^{-1} corresponds to 1 billion $B\overline{B}$ pairs)
- Multitude of achievements: confirmation of CKM mechanism, direct charge-parity violation in B decays, $b \to c\tau\nu$ and others

Higher precision requires higher luminosity => Second generation B factory: Belle II@SuperKEKB

Belle II at SuperKEKB

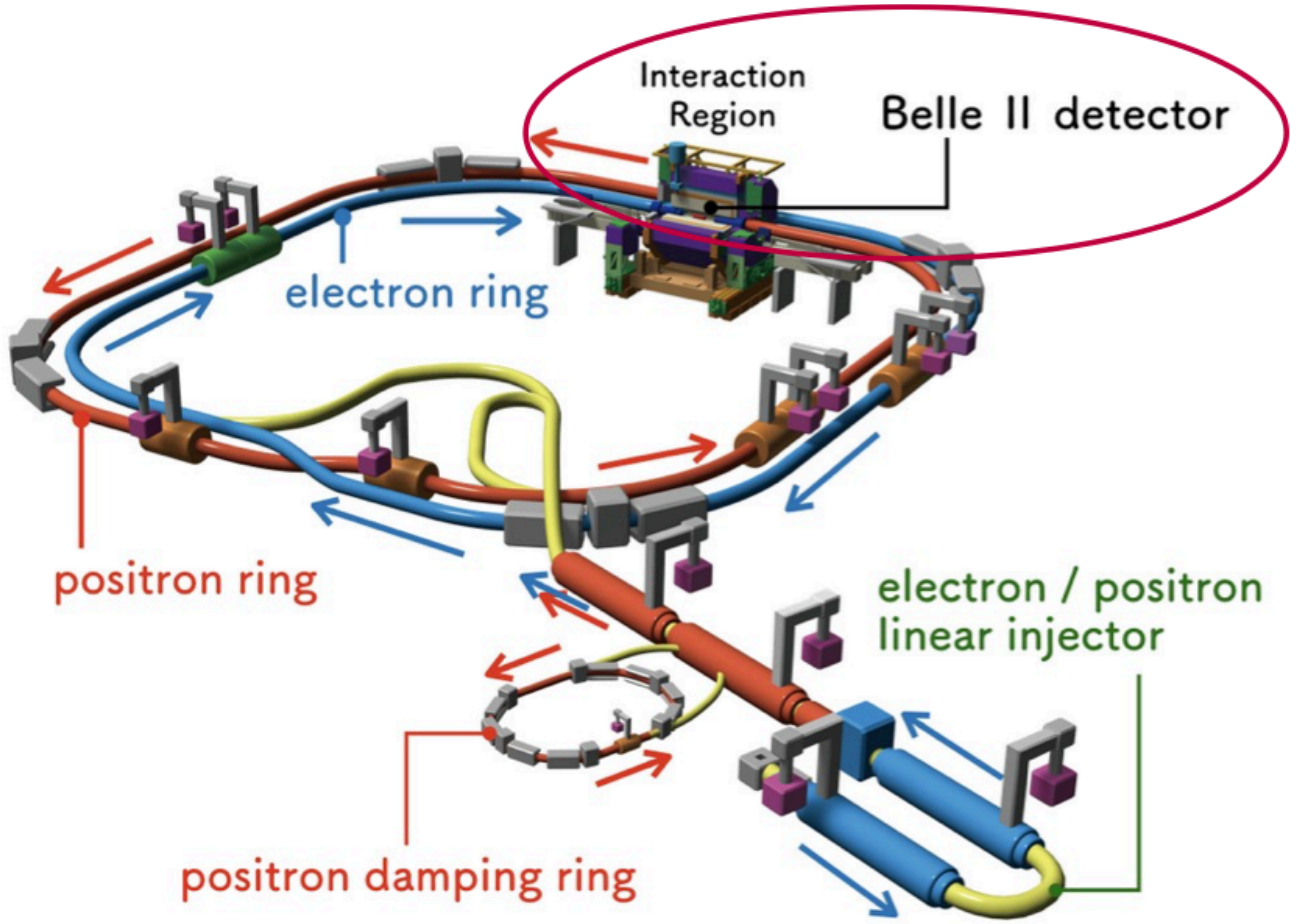


SuperKEKB

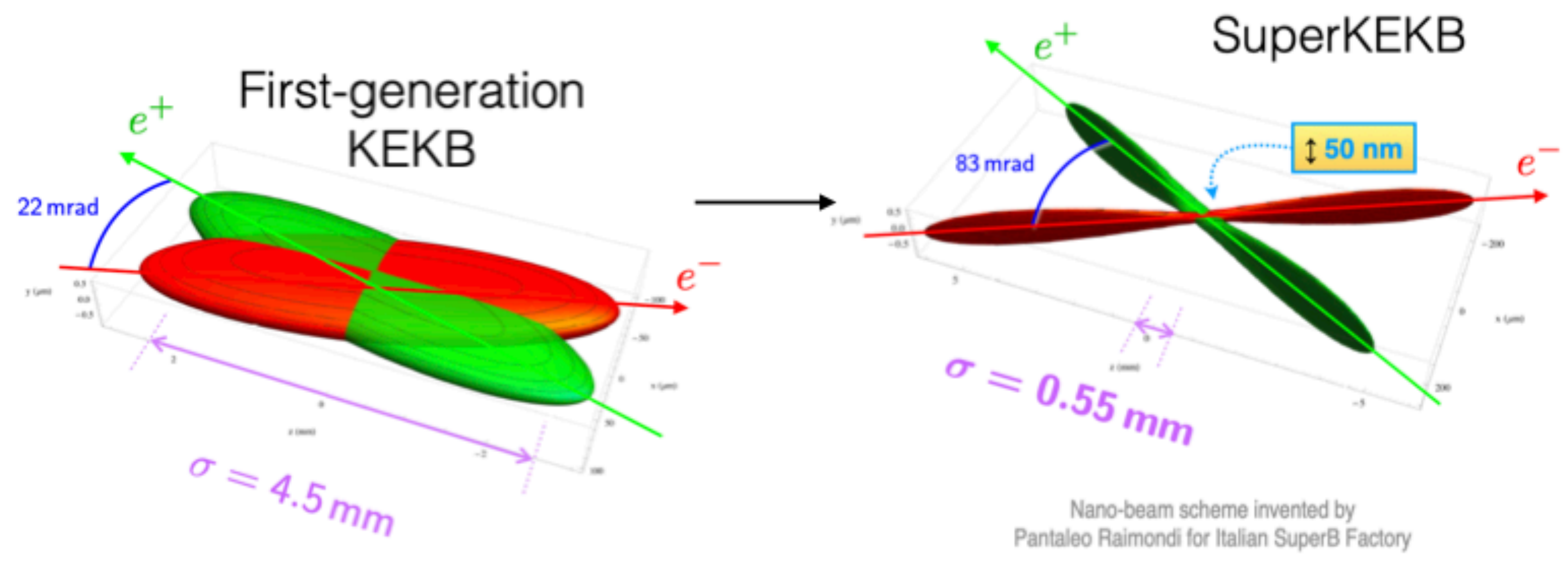
2019 - current

- e^+ (4 GeV) e^-(7 GeV)

Achieved 4.7×10^{34} cm^{-2}s^{-1} (current world record)



Belle II at SuperKEKB



$$L = \frac{N_+ N_- n_b f_0}{4\pi \sigma^*_{x,\mathrm{eff}} \sqrt{\varepsilon_y \beta^*_y}}$$

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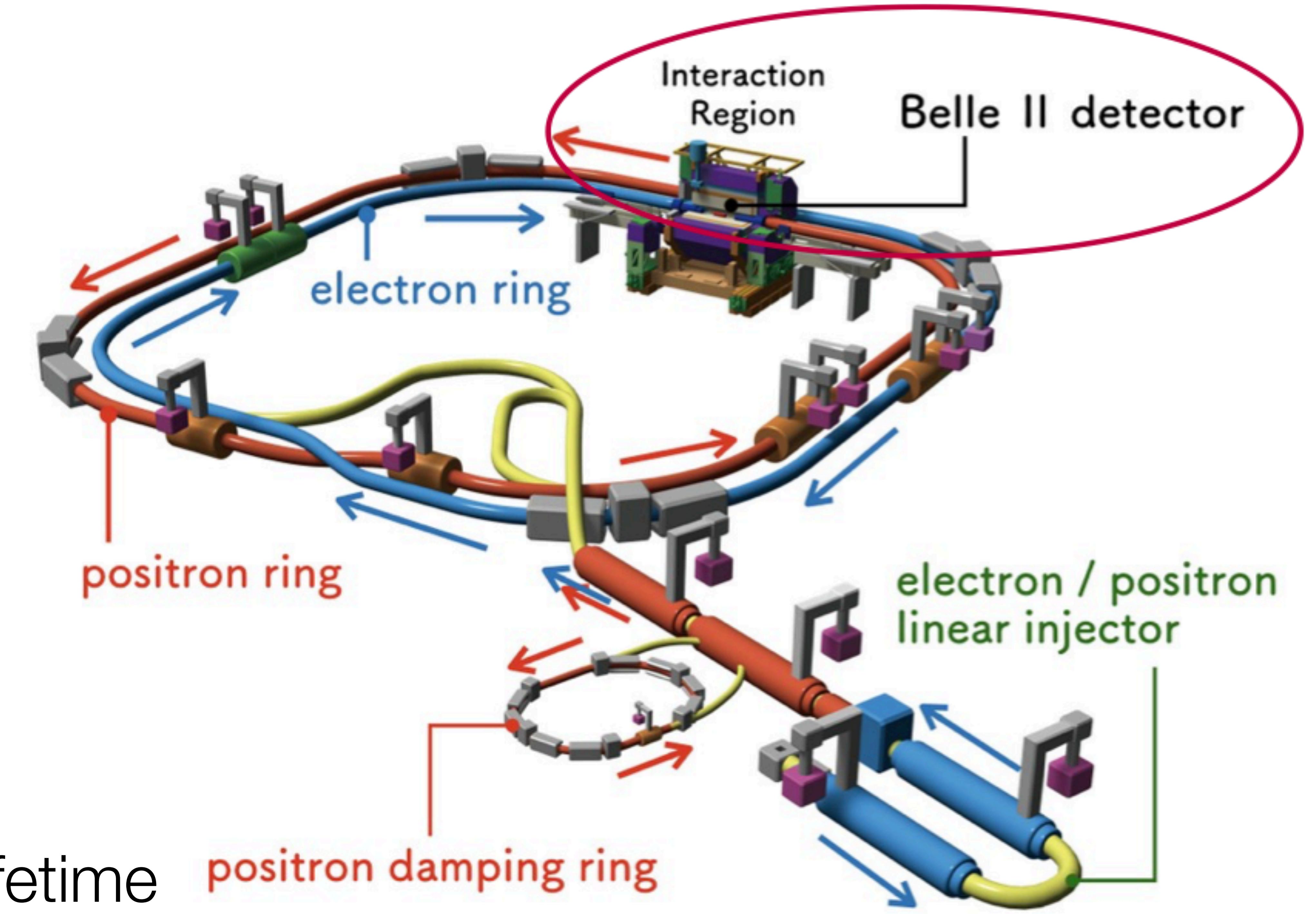
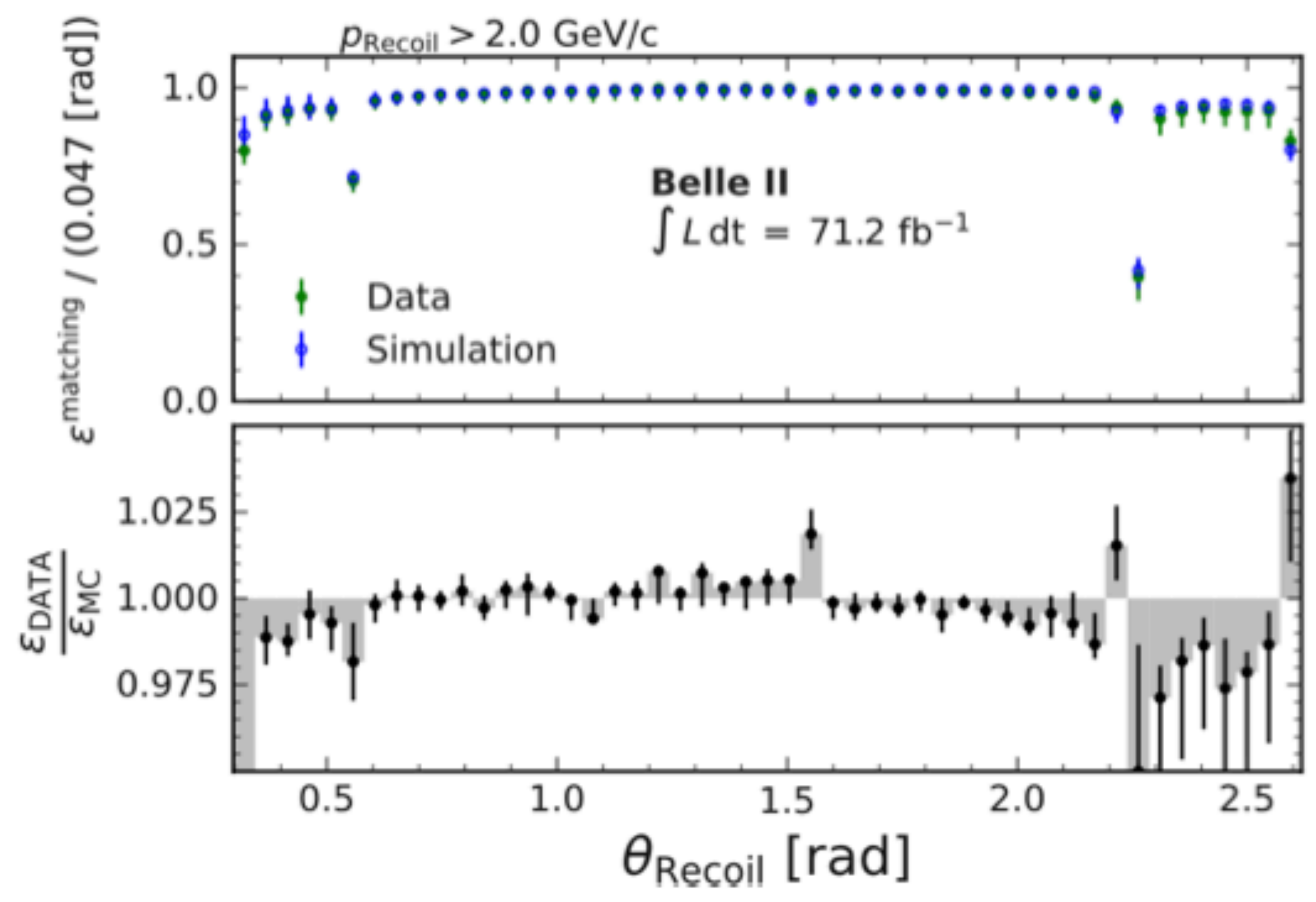


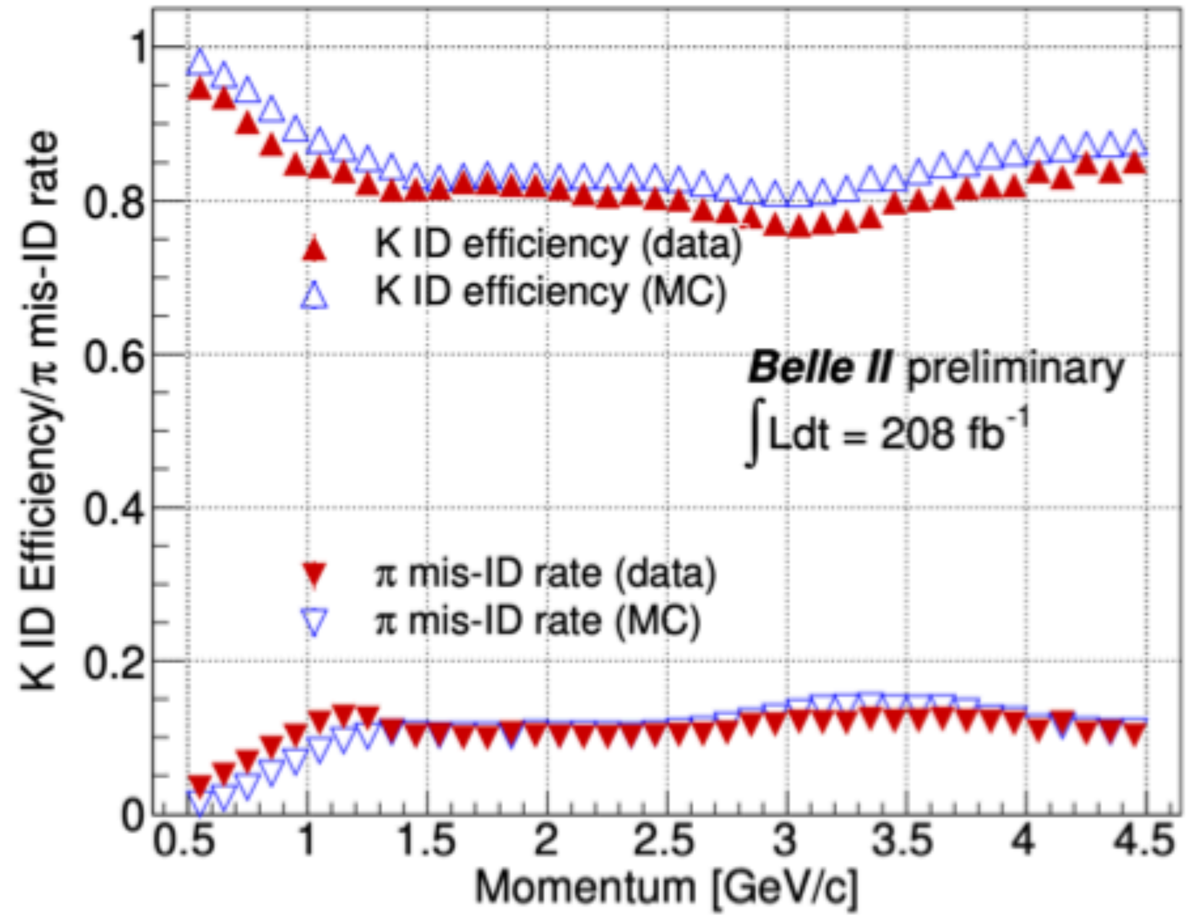
Toward 10^{35} cm^{-2}s^{-1}:

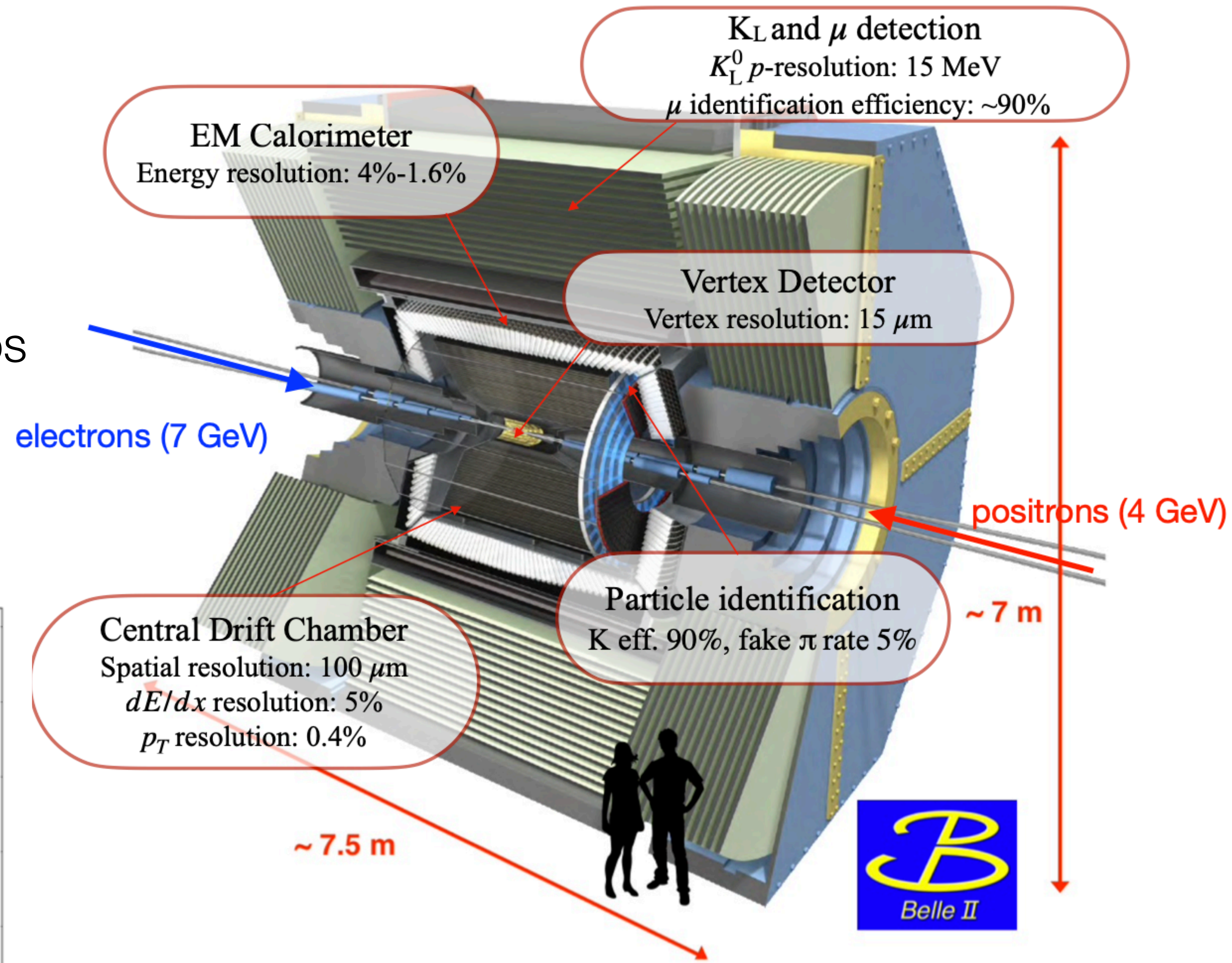
- SuperKEKB integrated luminosity is lower than expected
- Main reasons are low injection efficiency, beam size, beam lifetime
- Working hard to overcome this, e.g. hardware upgrades on collimators and injection system

Belle II

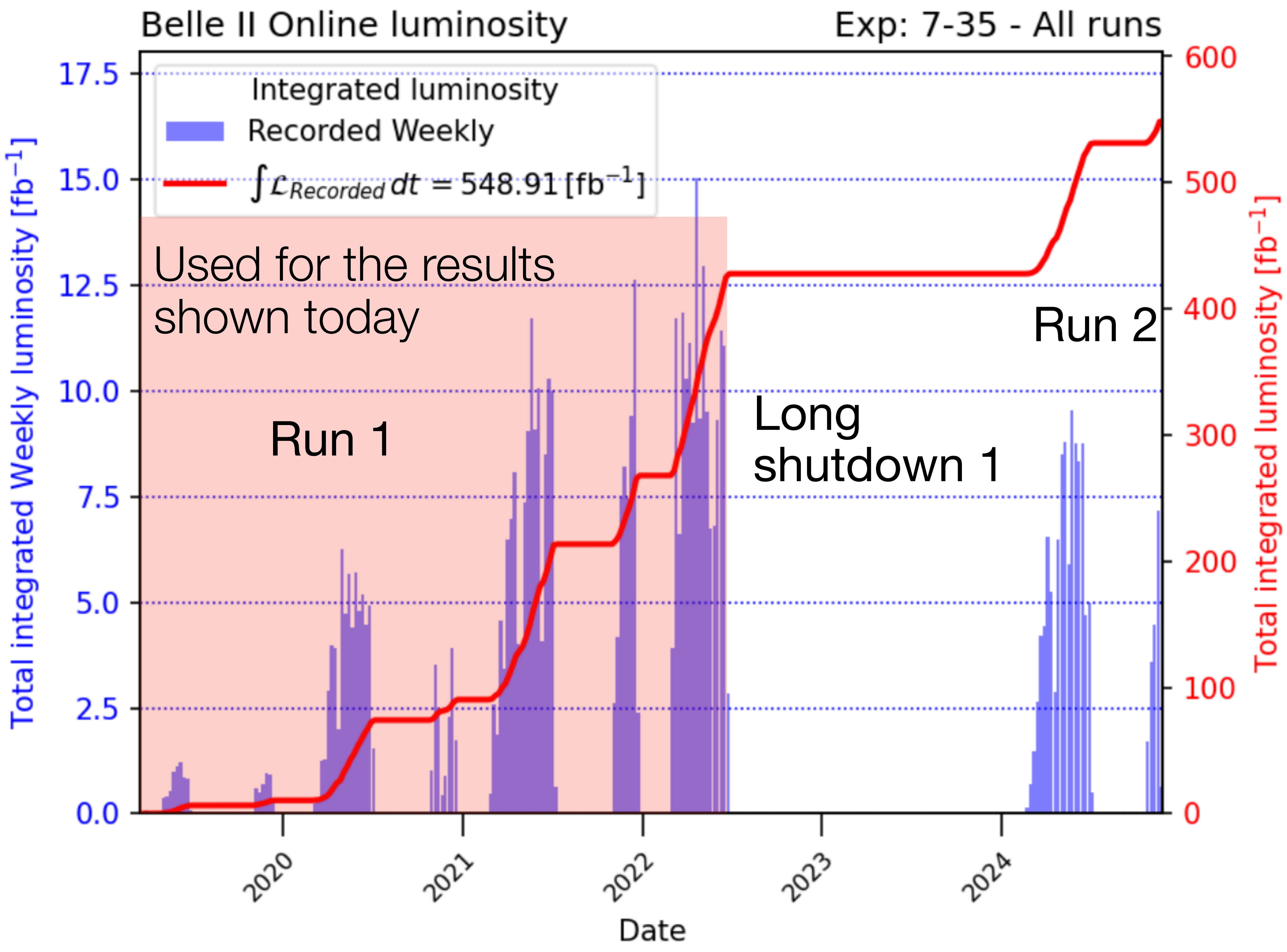
- Well-known initial state
- Production of $B\bar{B}$ at threshold => clean environment
- Boosted centre-of-mass system => essential for time-dependent measurements
- Nearly 4π coverage => covers final states with neutrinos
- High photon detection efficiency => neutral final states
- Good charged particle identification





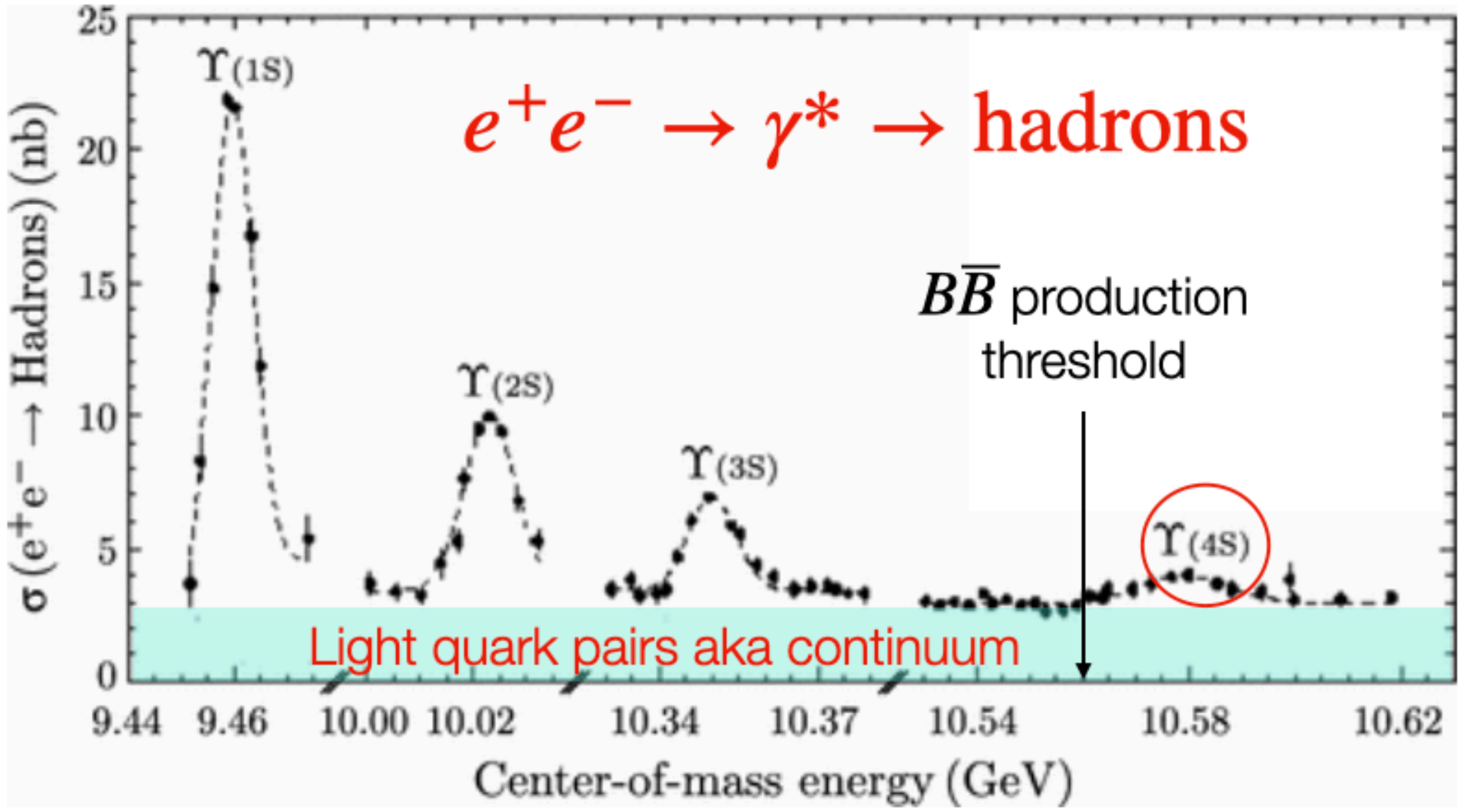


Data taking status

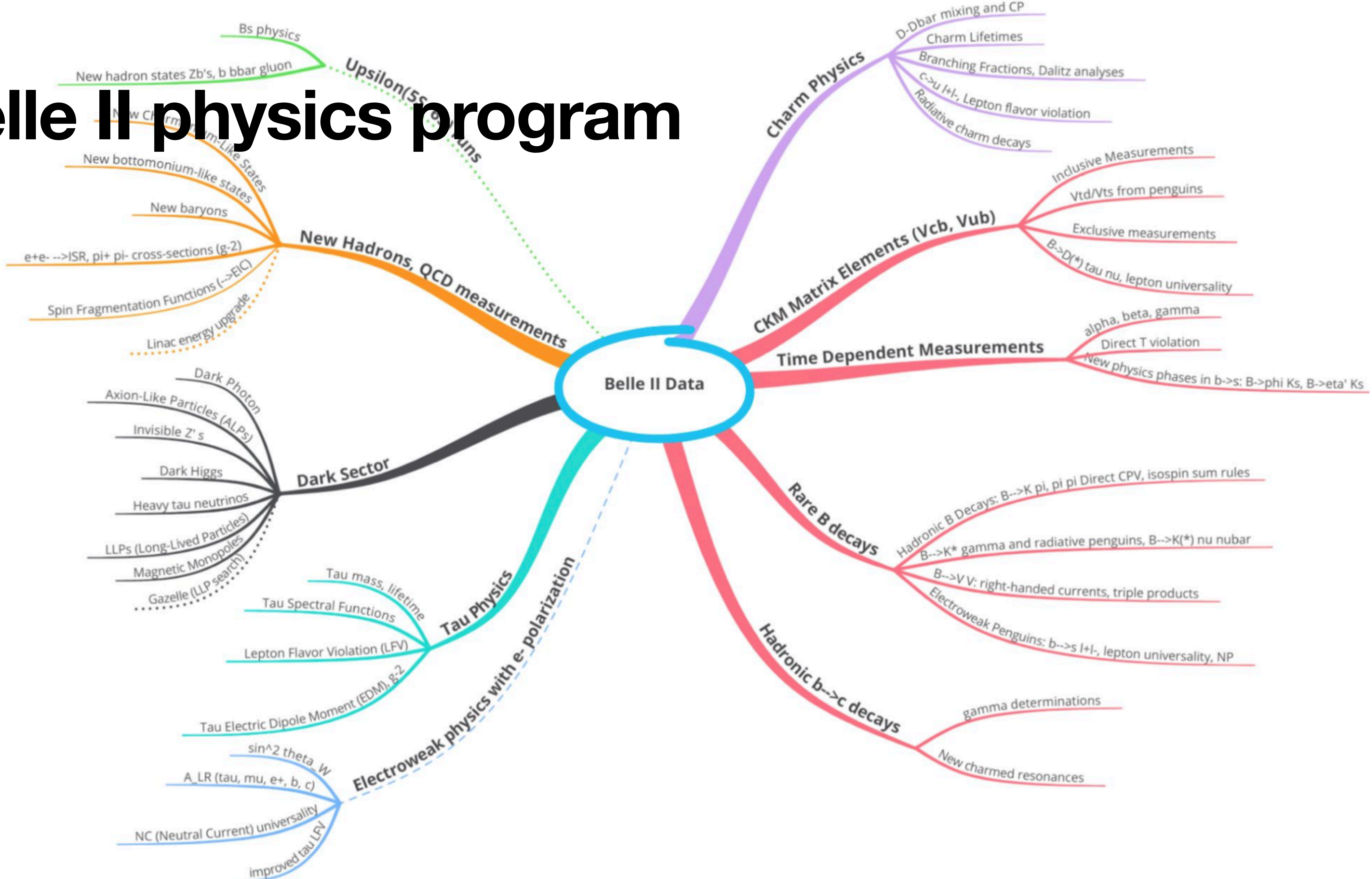


Used for the results shown today

Collision energy	Sample size, fb^{-1}
@$\Upsilon(4S)$	362
60 MeV below $\Upsilon(4S)$	42



Belle II physics program



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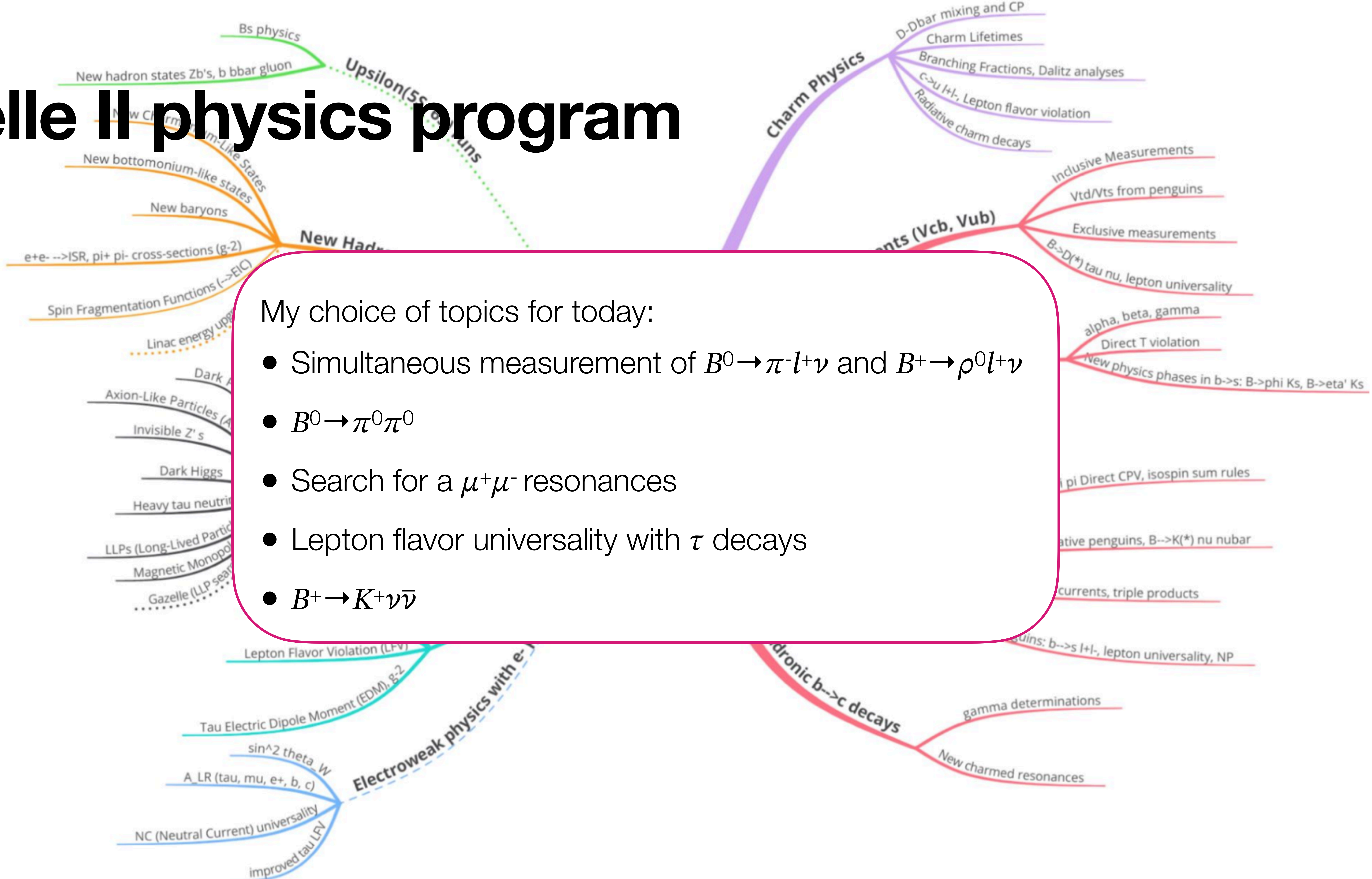


My choice of topics for today:

- Simultaneous measurement of $B^0 \to \pi^- l^+ \nu$ and $B^+ \to \rho^0 l^+ \nu$
- $B^0 \to \pi^0 \pi^0$
- Search for a $\mu^+ \mu^-$ resonances
- Lepton flavor universality with τ decays
- $B^+ \to K^+ \nu \bar{\nu}$

Submitted to PRD
arxiv:2407.17403

Simultaneous measurement of $B^0 \to \pi^- l^+ \nu$ and $B^+ \to \rho^0 l^+ \nu$

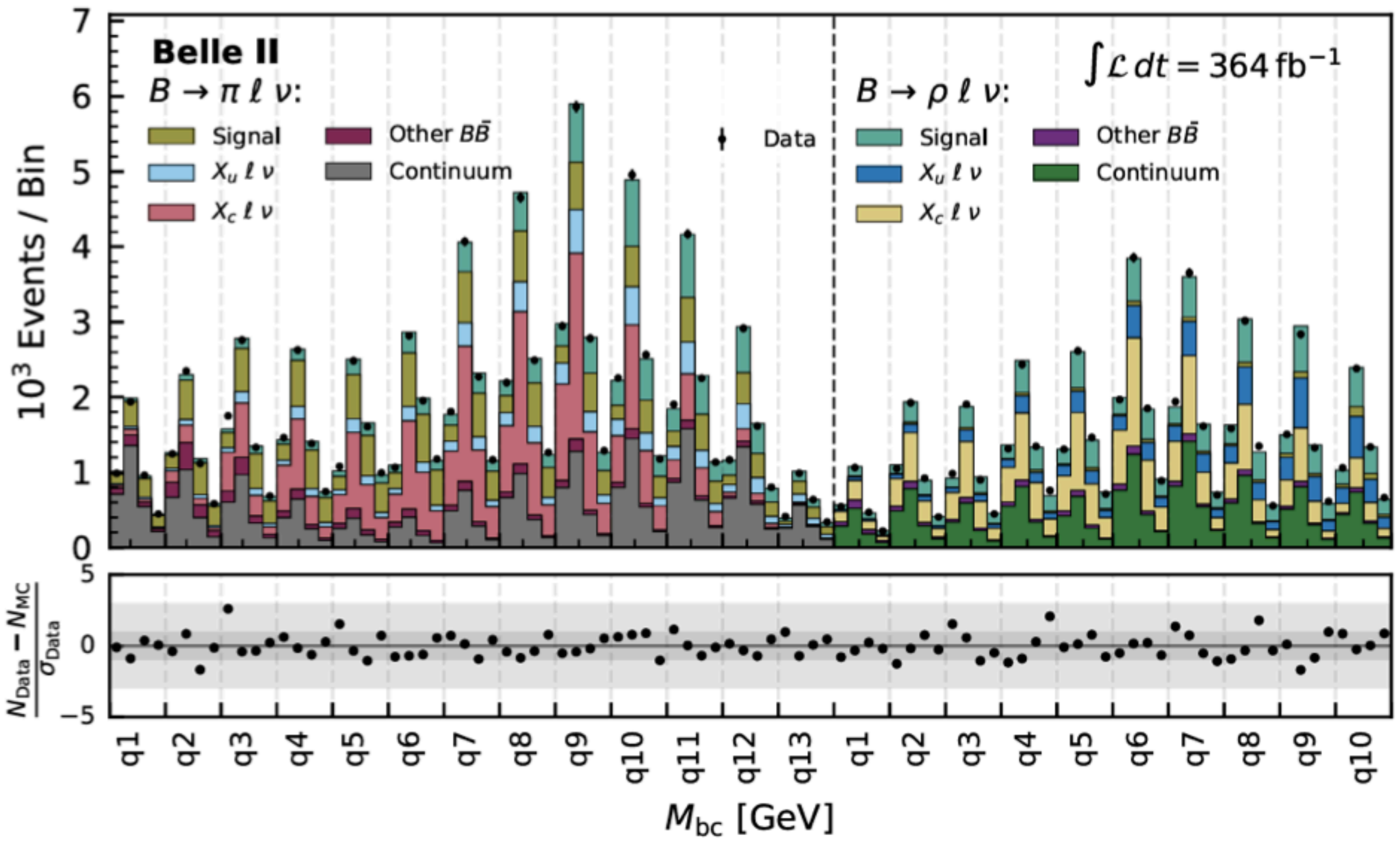
Extract $|V_{ub}|$ from $B^0 \to \pi^- l^+ \nu$ and $B^+ \to \rho^0 l^+ \nu$ decays

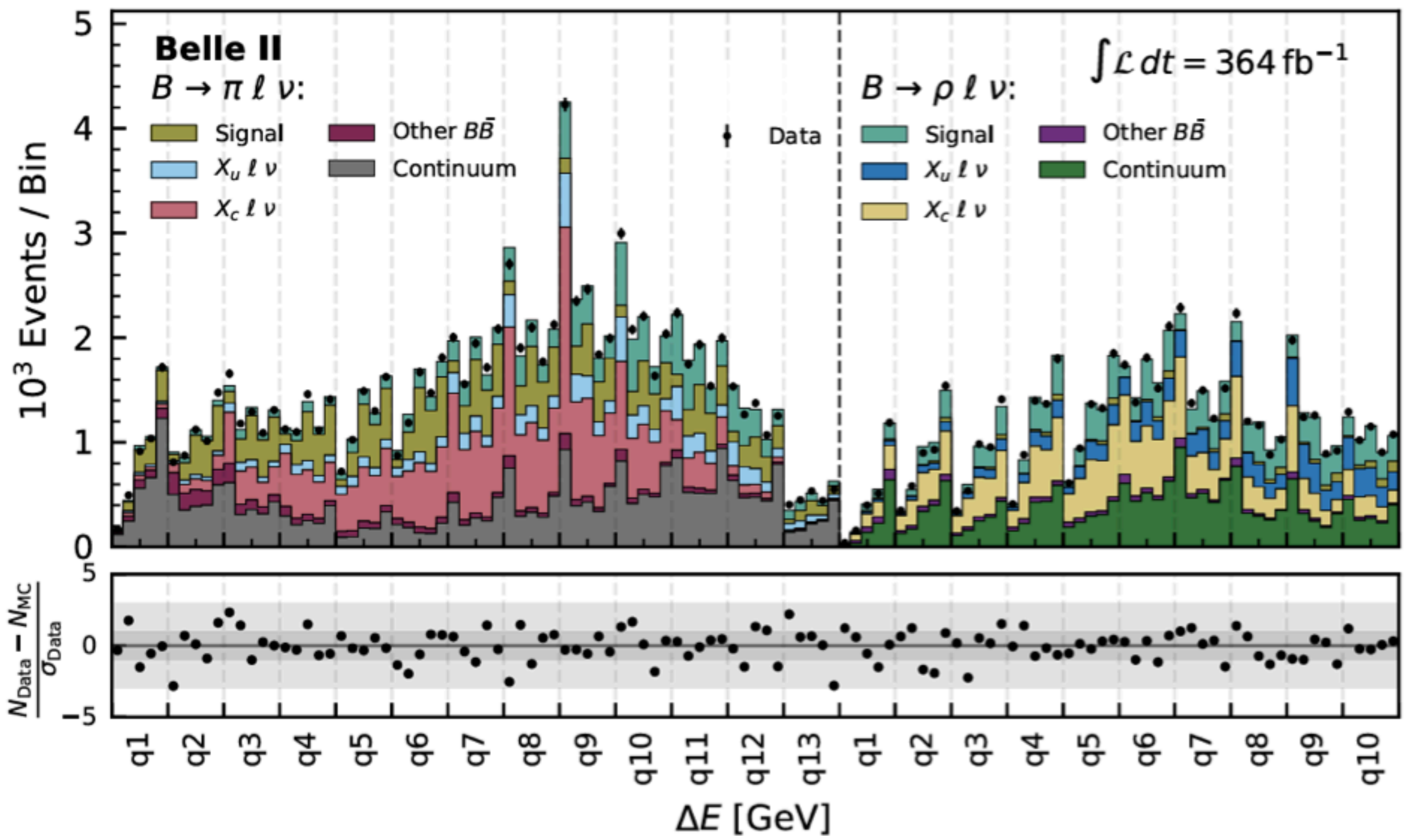
$$M_{bc}c^2 = \sqrt{E_{beam}^{*2} - c^2 \left|\overrightarrow{p_B^*}\right|^2}$$

$$\Delta E = E_B^* - E_{beam}^*$$

- Suppress $e^+e^- \to q\bar{q}$ and background from other B decays using BDTs
- Extract signal yields from a fit of 2 kinematic variables in bins of $q^2 = (p_B - p_{\rho,\pi})^2$ simultaneously for $B^0 \to \pi^- l^+ \nu$ and $B^+ \to \rho^0 l^+ \nu$ => (13 + 10) × 4 × 5 bins

q^2 M_{bc} $|\Delta E|$





Simultaneous measurement of $B^0 \to \pi^- l^+ \nu$ and $B^+ \to \rho^0 l^+ \nu$

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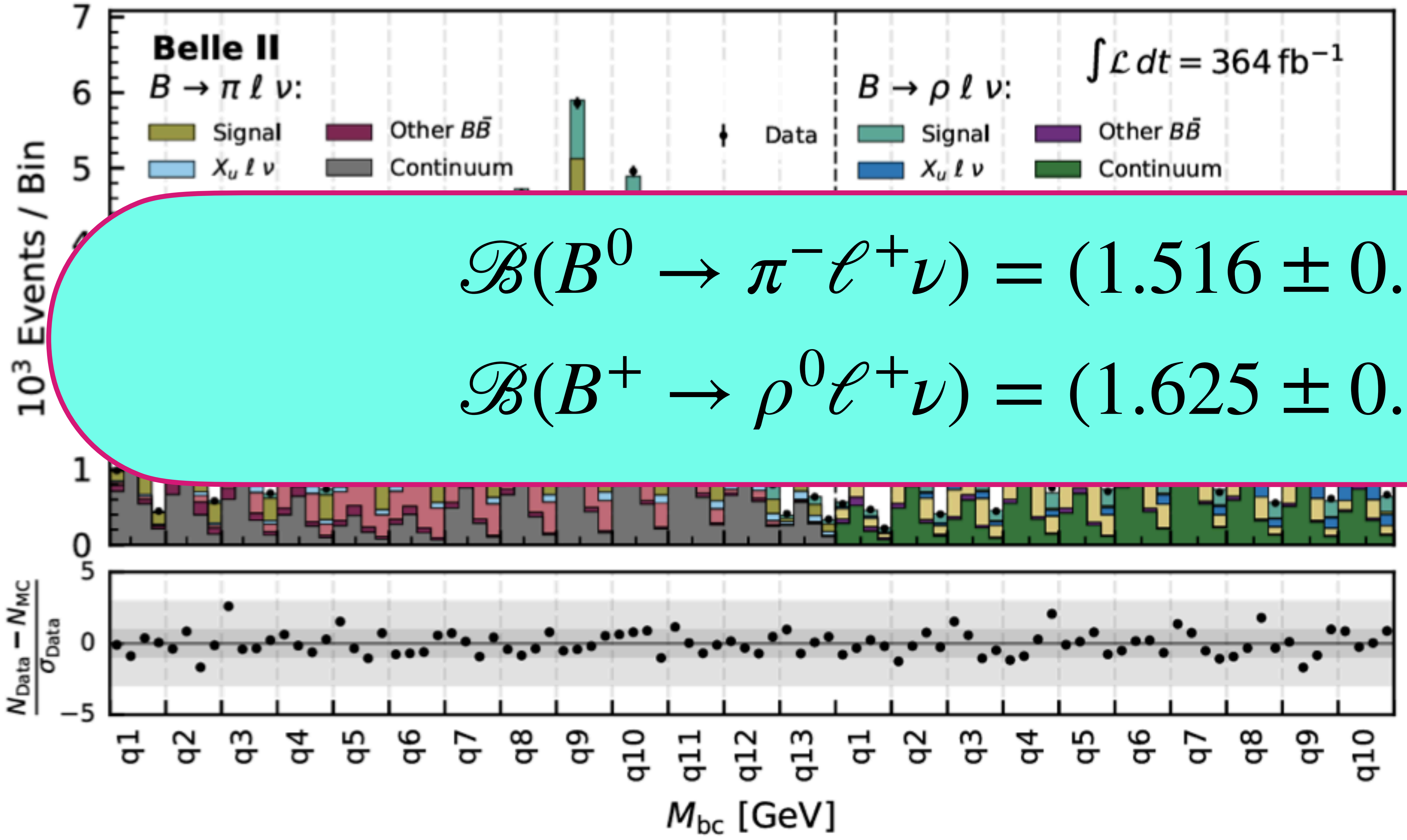
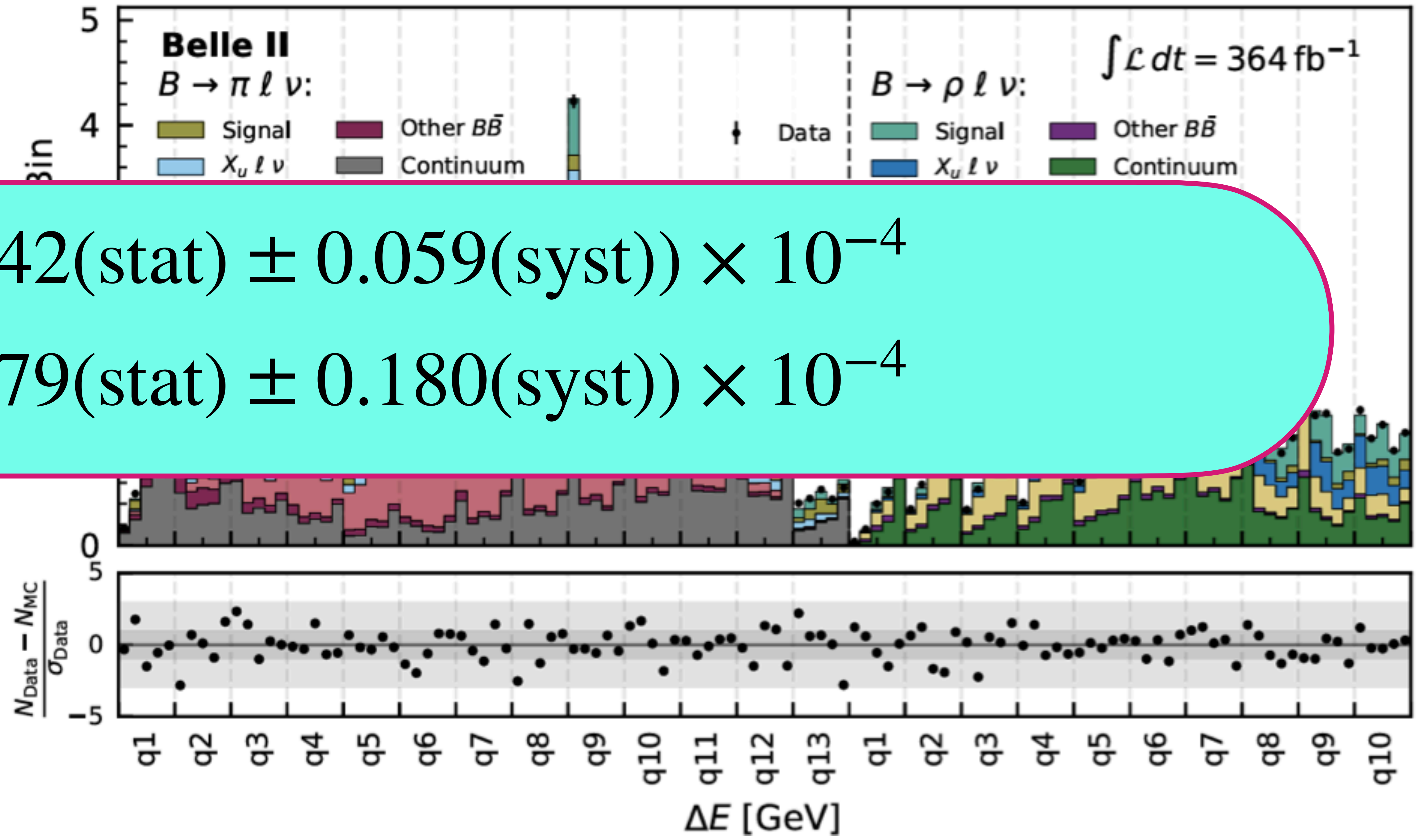




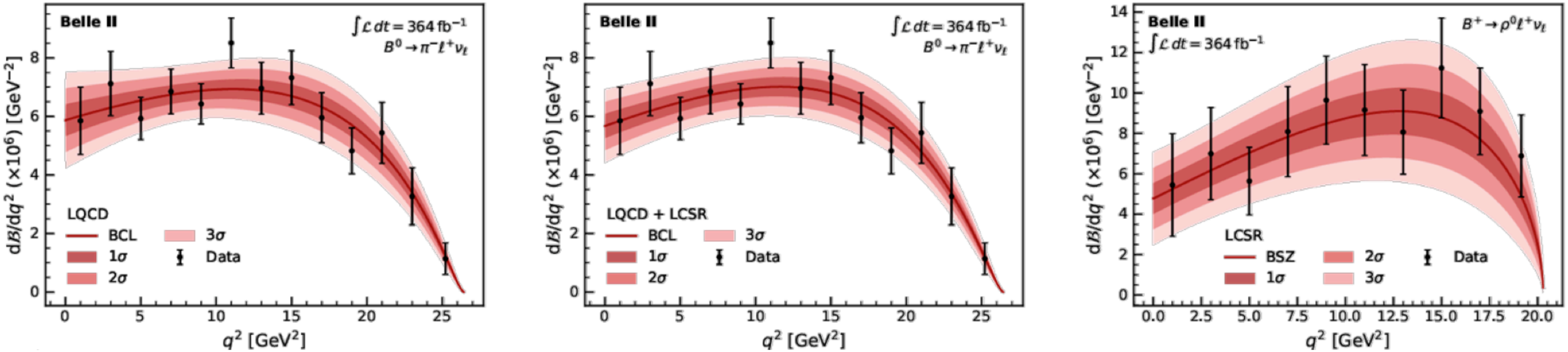
$$\mathcal{B}(B^0 \to \pi^- \ell^+ \nu) = (1.516 \pm 0.042(\mathrm{stat}) \pm 0.059(\mathrm{syst})) \times 10^{-4}$$

$$\mathcal{B}(B^+ \to \rho^0 \ell^+ \nu) = (1.625 \pm 0.079(\mathrm{stat}) \pm 0.180(\mathrm{syst})) \times 10^{-4}$$

$|V_{ub}|$ from $B^0 \to \pi^- l^+ \nu$ and $B^+ \to \rho^0 l^+ \nu$

$$\frac{d\mathscr{B}}{dq^2} \propto |V_{ub}|^2 \times |FF(q^2)|^2$$

Set up χ^2 fits and use FF parametrizations and Lattice/LCSR constraints as nuisance parameters



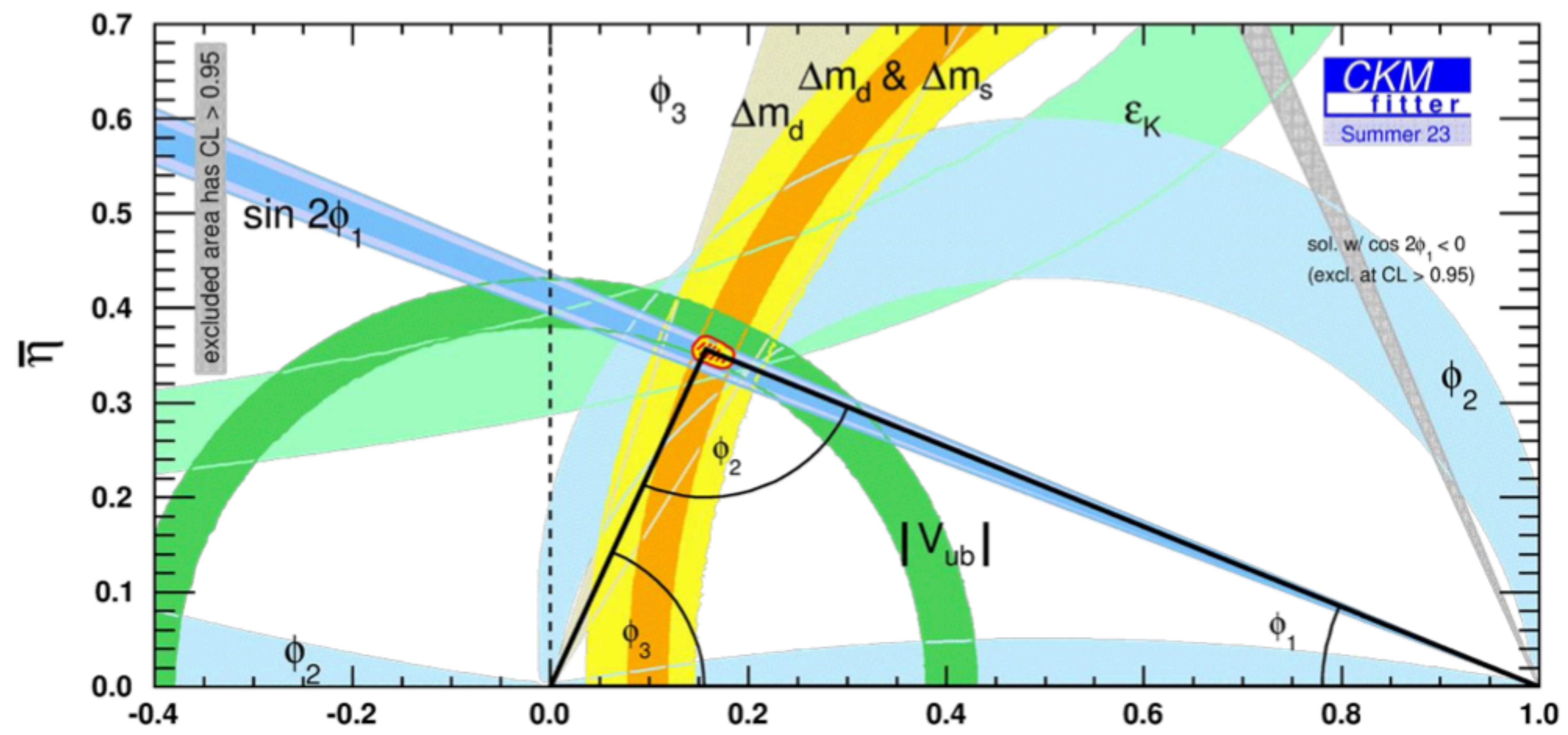
$|V_{ub}|_{B^0 \to \pi^- \ell^+ \nu} = (3.93 \pm 0.09(\mathrm{stat}) \pm 0.13(\mathrm{syst}) \pm 0.19(\mathrm{theo})) \times 10^{-3}$ LQCD constraints

$|V_{ub}|_{B^0 \to \pi^- \ell^+ \nu} = (3.73 \pm 0.07(\mathrm{stat}) \pm 0.07(\mathrm{syst}) \pm 0.16(\mathrm{theo})) \times 10^{-3}$ LQCD+LCSR constraints

$|V_{ub}|_{B^+ \to \rho^0 \ell^+ \nu} = (3.19 \pm 0.12(\mathrm{stat}) \pm 0.17(\mathrm{syst}) \pm 0.26(\mathrm{theo})) \times 10^{-3}$ LCSR constraints

Preliminary

$B^0 \to \pi^0\pi^0$

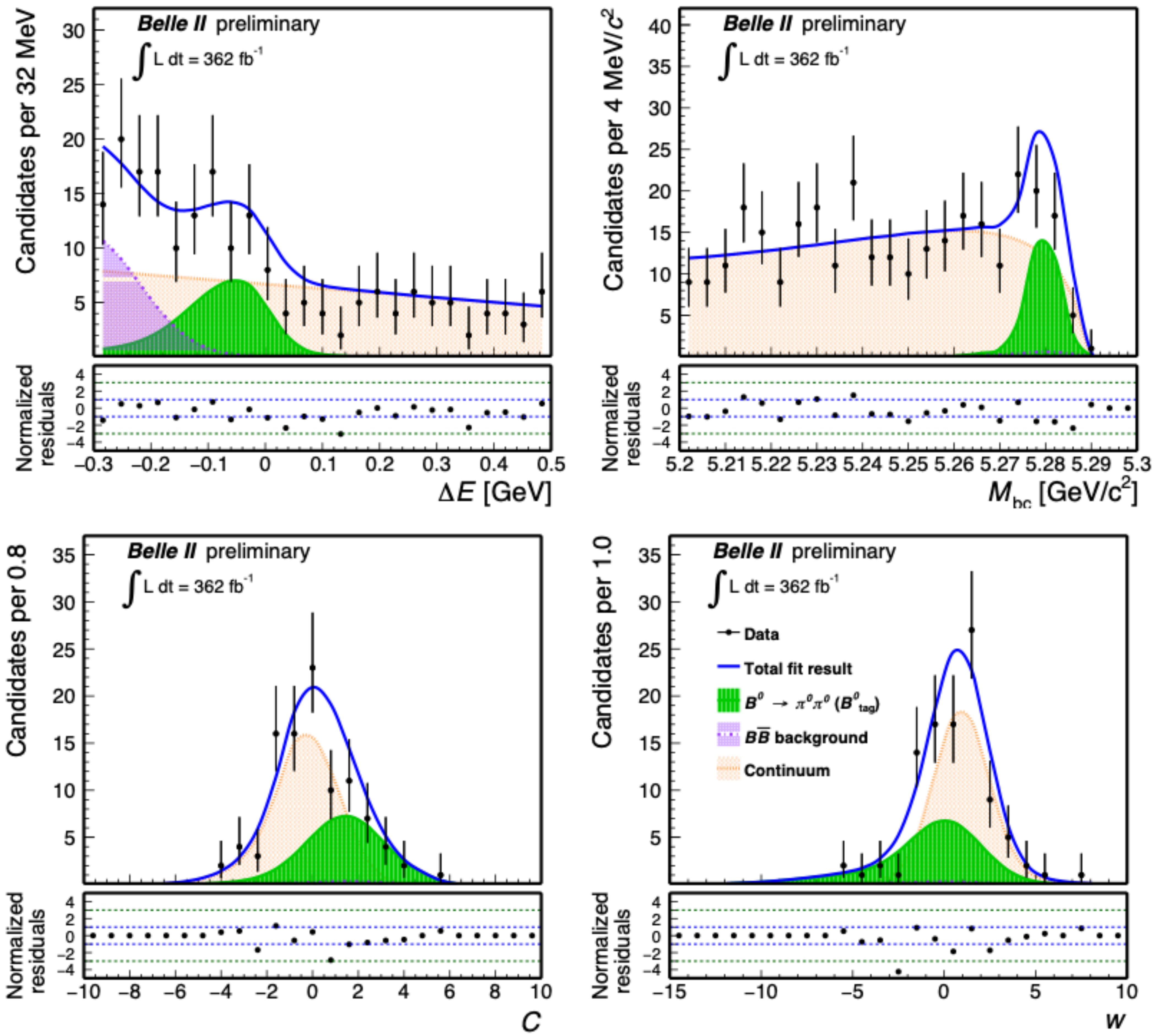


Extract α/φ_2 (least-known CKM angle) using inputs from $B^0 \to \pi^0\pi^0$

- Purely neutral final state => develop robust photon selection against beam-induced background
- Large contamination from $e^+e^- \to q\bar{q}$ => train a MVA
- Need to know the flavor of the neutral B for the measurement the *CP*-violating asymmetry => apply a flavor tagger
- Requires a multidimensional fit => ΔE, M_{bc}, MVA output (*C*) and transformed probability of wrong tag (*w*)

$$\mathscr{B}(B^0 \to \pi^0\pi^0) = (1.26 \pm 0.20(\text{stat}) \pm 0.11(\text{syst})) \times 10^{-6}$$

$$A_{CP}(B^0 \to \pi^0\pi^0) = 0.03 \pm 0.30(\text{stat}) \pm 0.05(\text{syst})$$

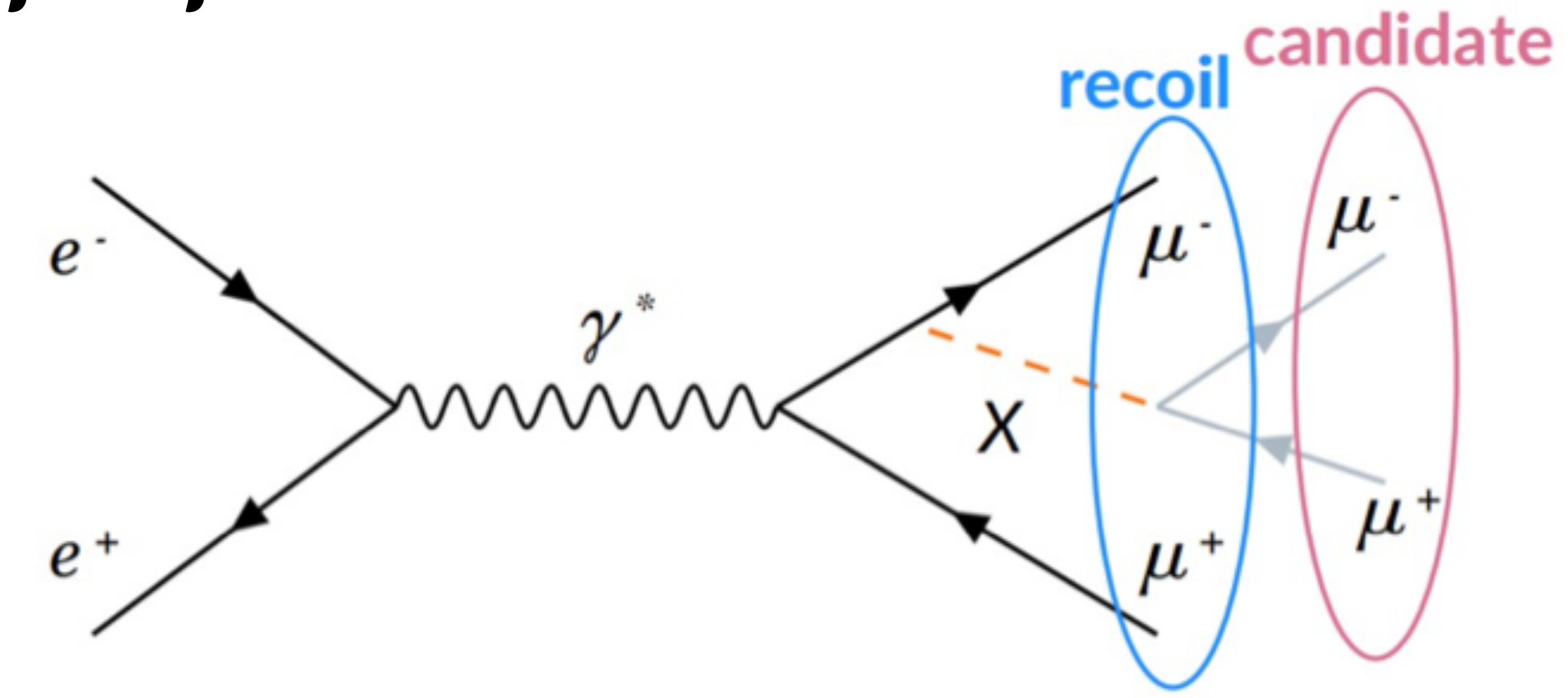


PRD 109, 112015 (2024)

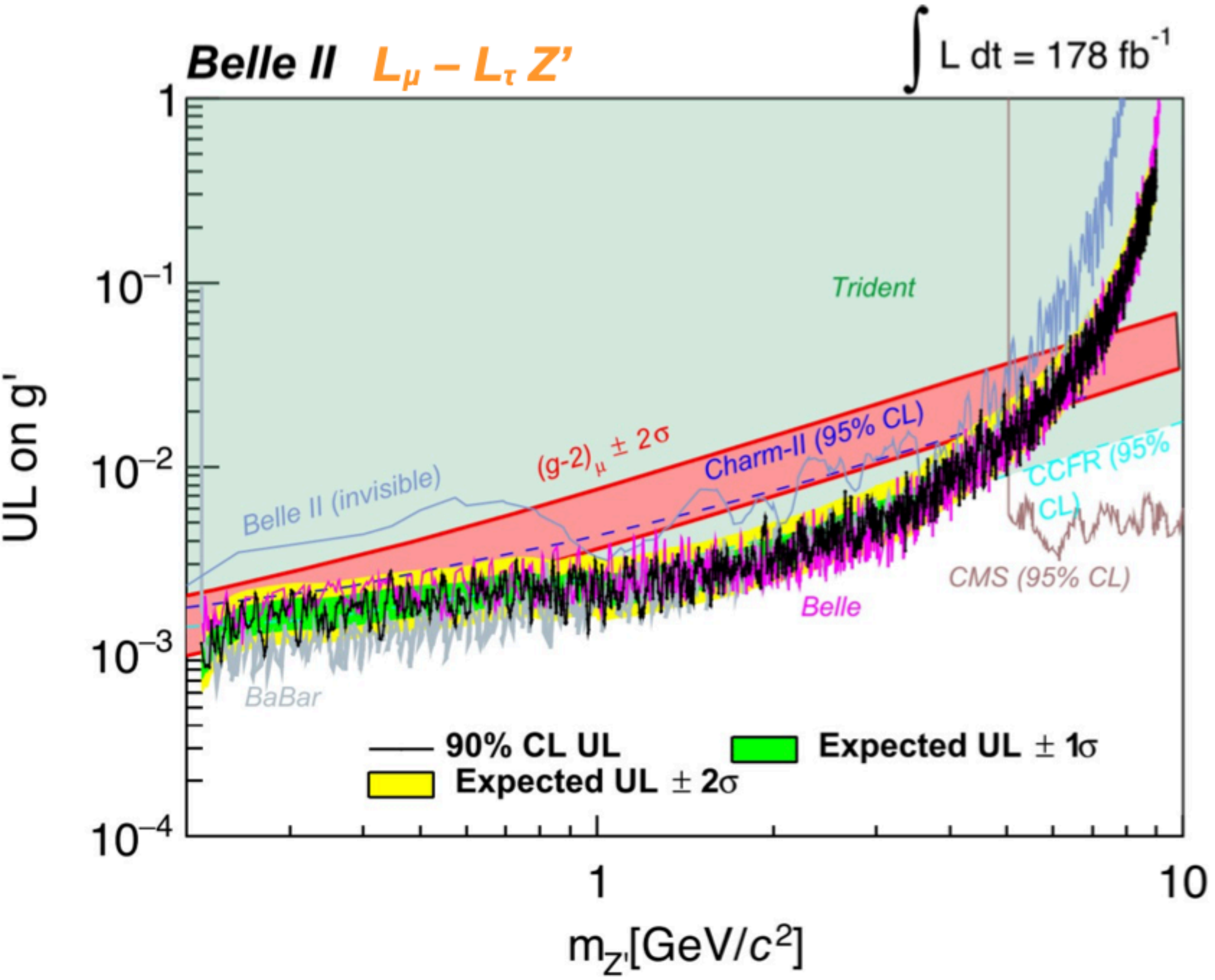
$\mu^+\mu^-$ resonances in $e^+e^-\to\mu^+\mu^-\mu^+\mu^-$

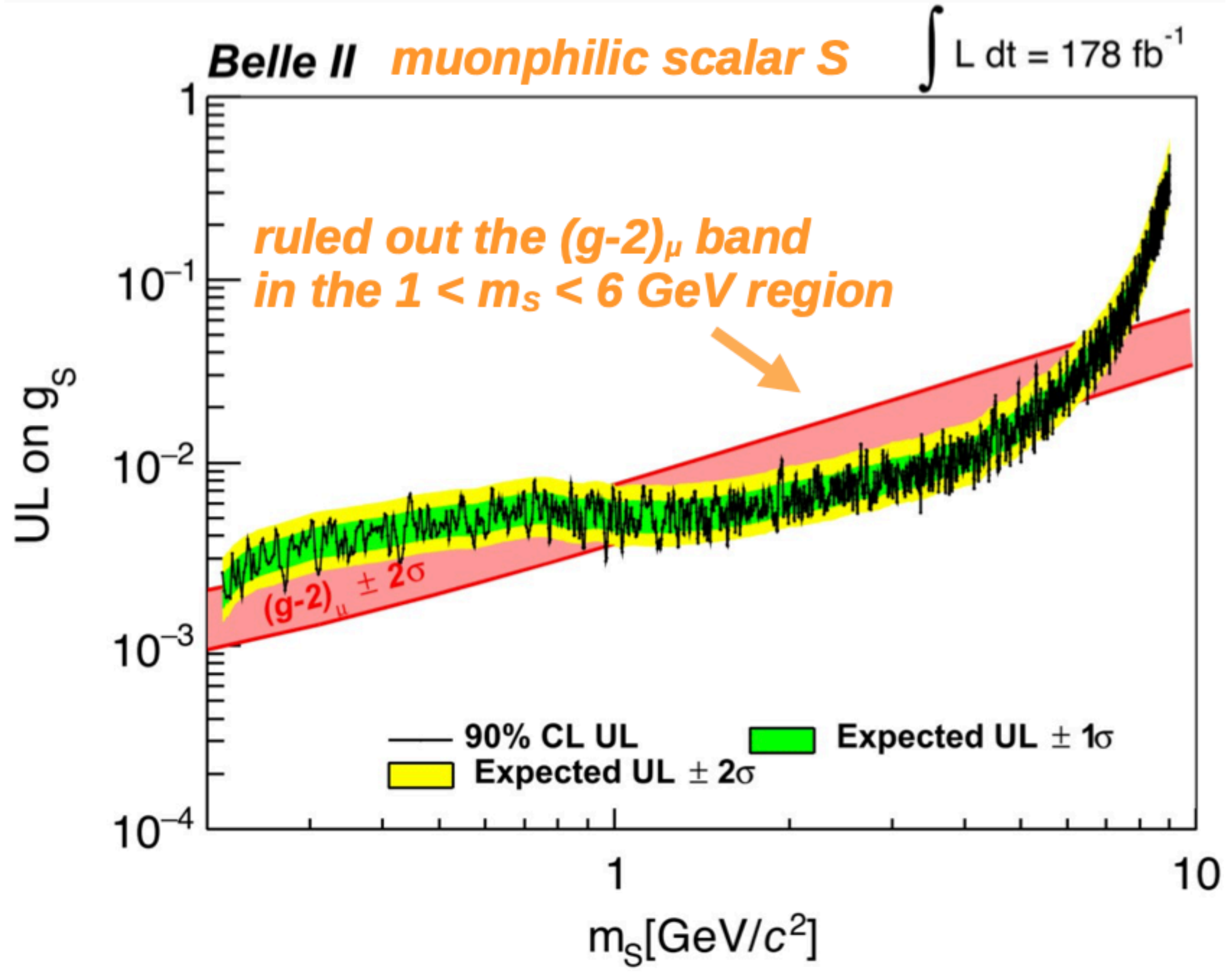
Search for the process $e^+e^-\to\mu^+\mu^-X$, where $X\to\mu^+\mu^-$

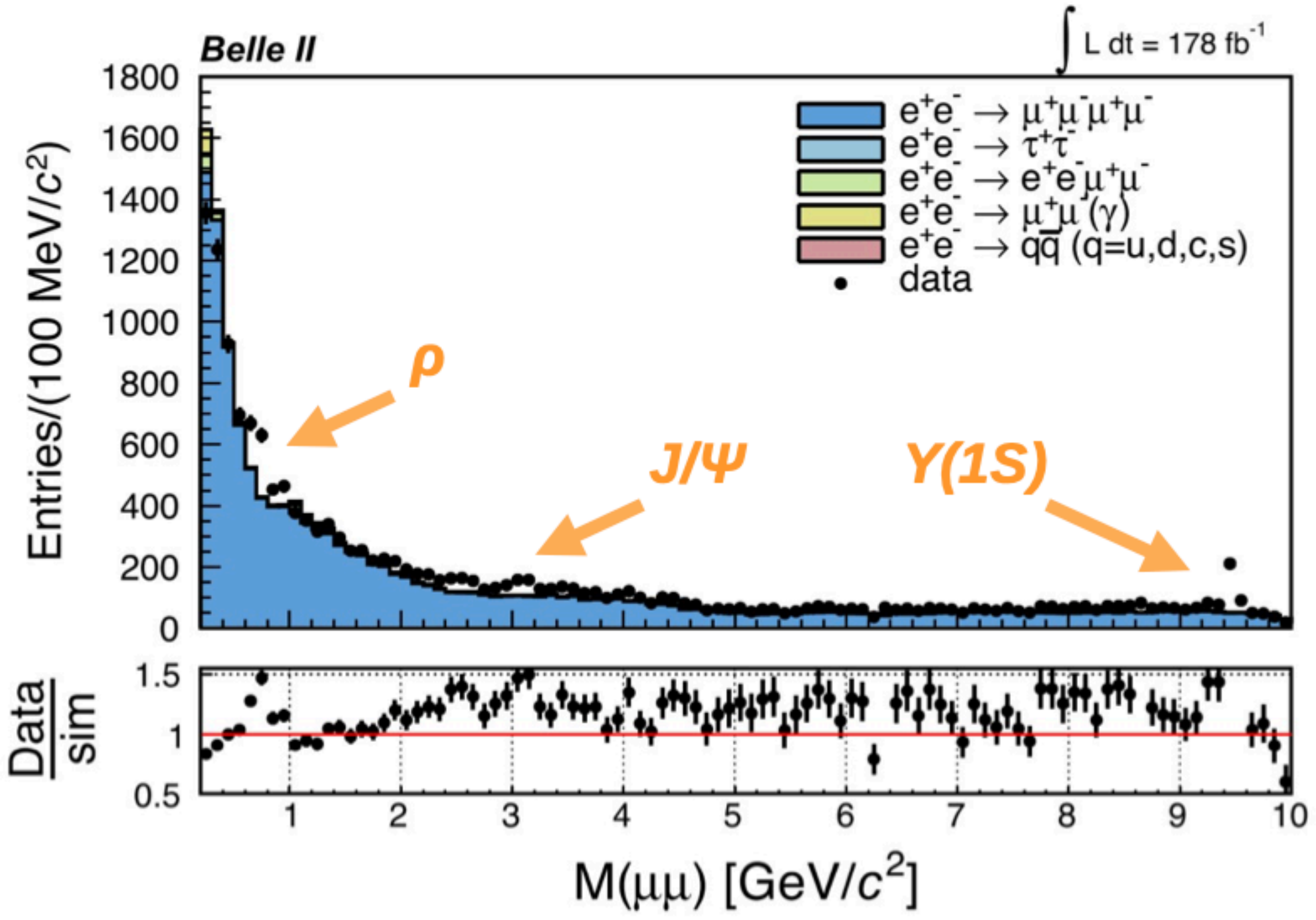
- Look for a narrow peak in the $\mu^+\mu^-$ mass distribution.
  Probing two different models:
  - L_μ-L_τ vector mediator (Z') [W. Altmanshofer et al., JHEP. 2016, 106]
  - Muonphilic dark scalar (S) [R. Capdevilla et al., JHEP 2022, 129]



- Agressive background suppression using Neural Nets







First 90% CL upper limits for the muonphilic dark scalar (S)

Light lepton flavor universality with τ decays

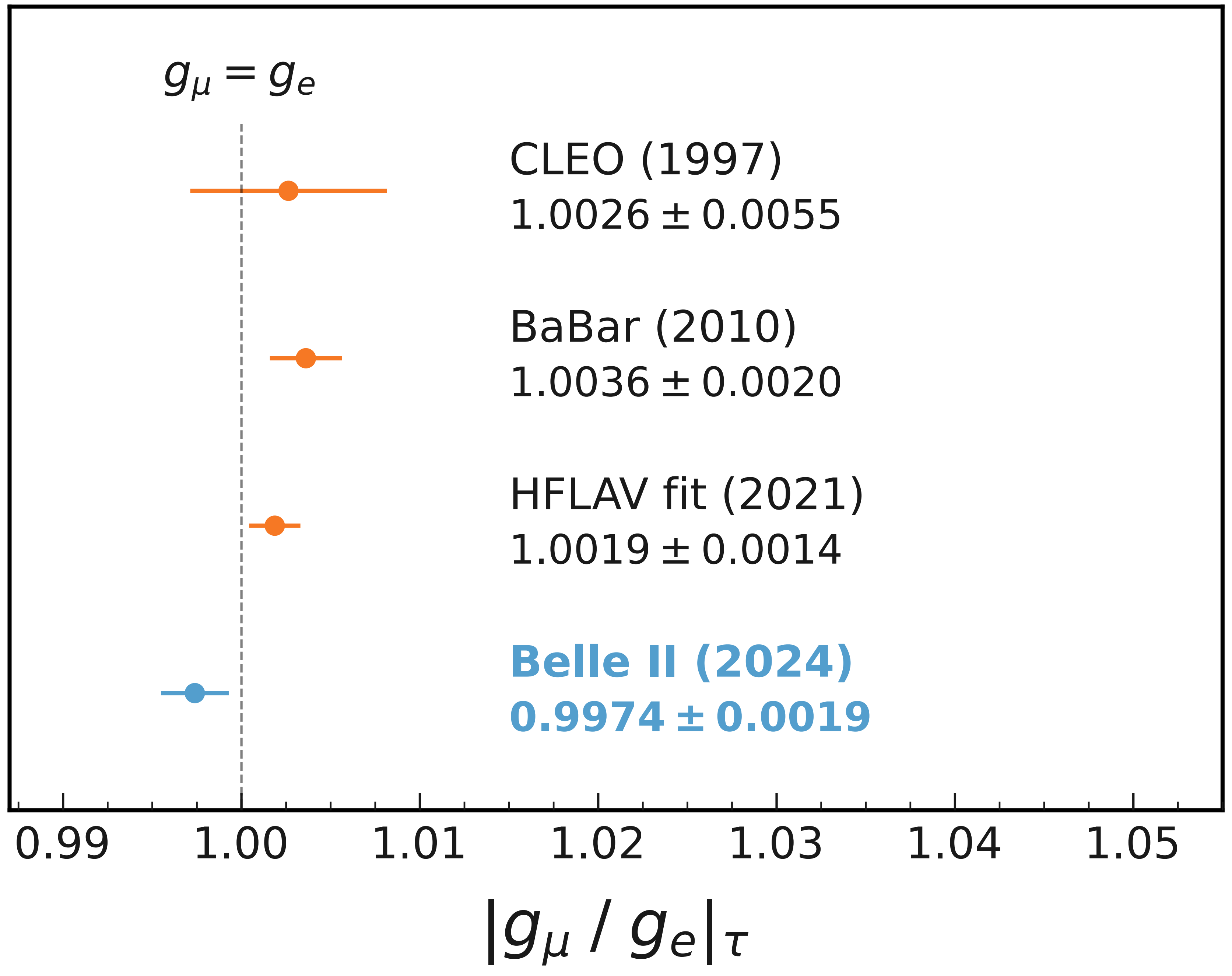
Same coupling g of electroweak gauge bosons to all generations of leptons in the standard model

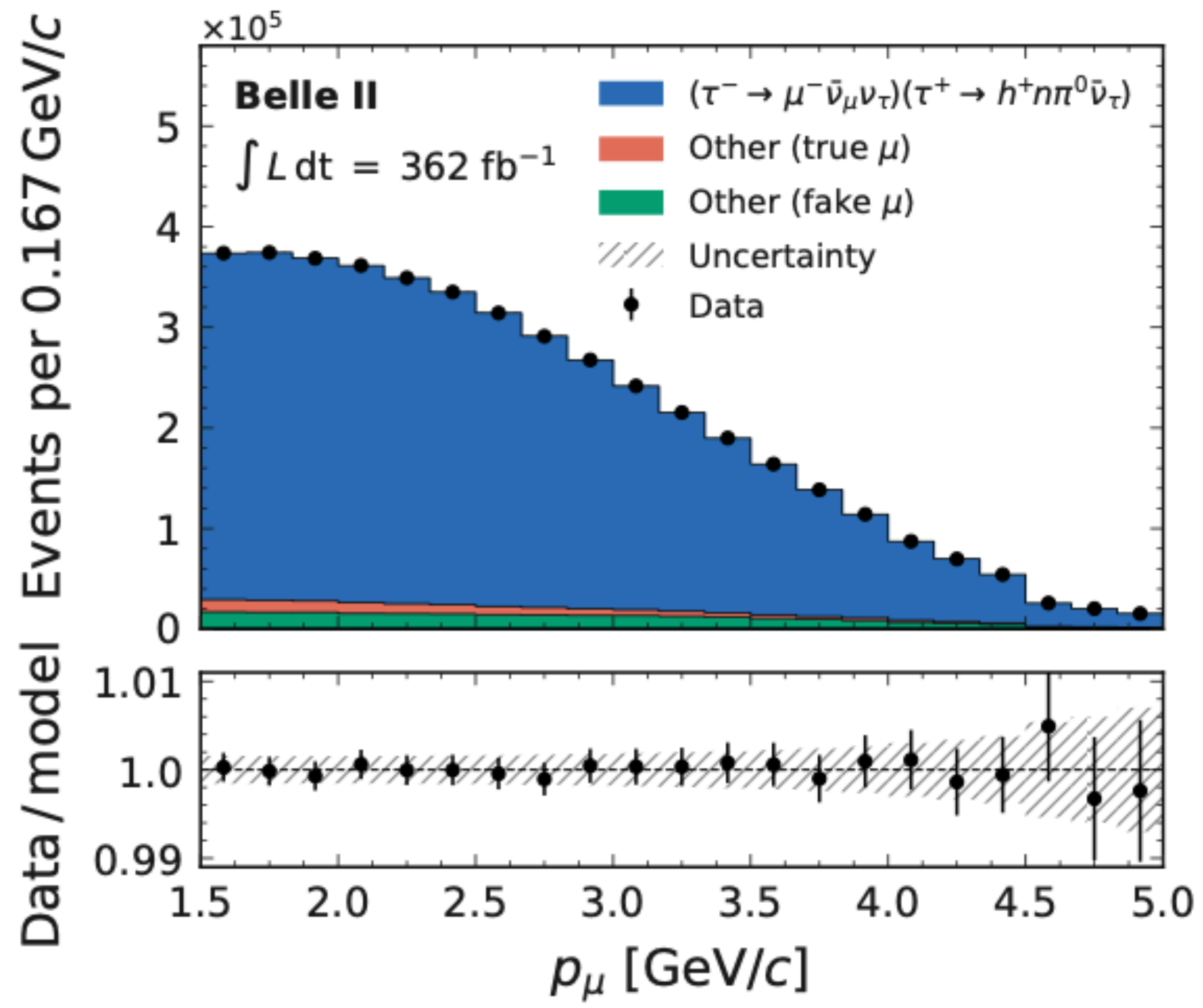
- Common selection to both modes -> many systematic uncertainties cancel out
- Neural network to suppress background

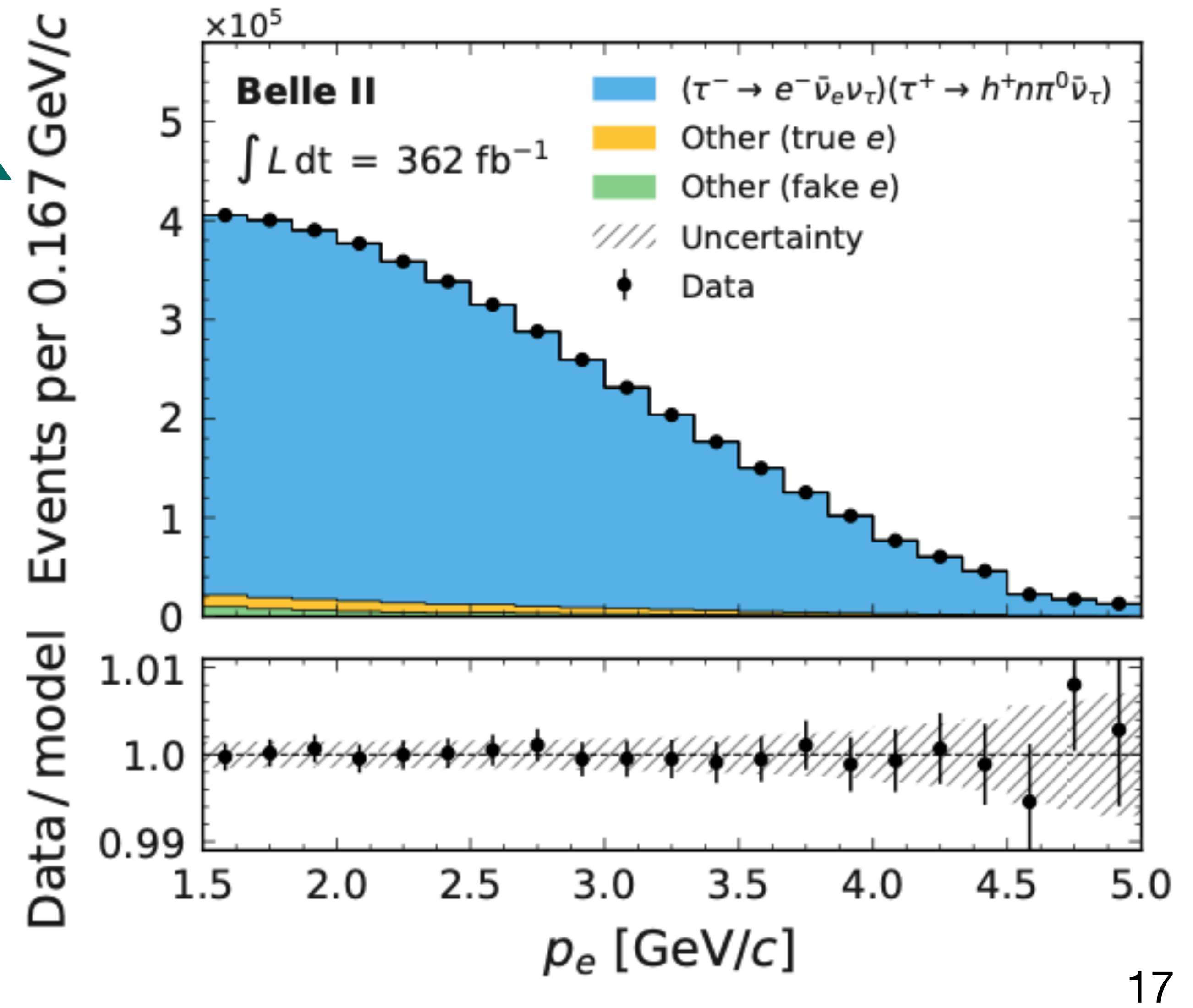
Most precise test of light lepton flavor universality in τ decays

$$\left(\frac{g_\mu}{g_e}\right)_\tau = \sqrt{R_\mu \frac{f(m_e^2/m_\tau^2)}{f(m_\mu^2/m_\tau^2)}}$$

$$R_\mu = \frac{\mathscr{B}(\tau^- \to \mu^- \bar{\nu}_\mu \nu_\tau)}{\mathscr{B}(\tau^- \to e^- \bar{\nu}_e \nu_\tau)}$$







PRD 109, 012001 (2024)

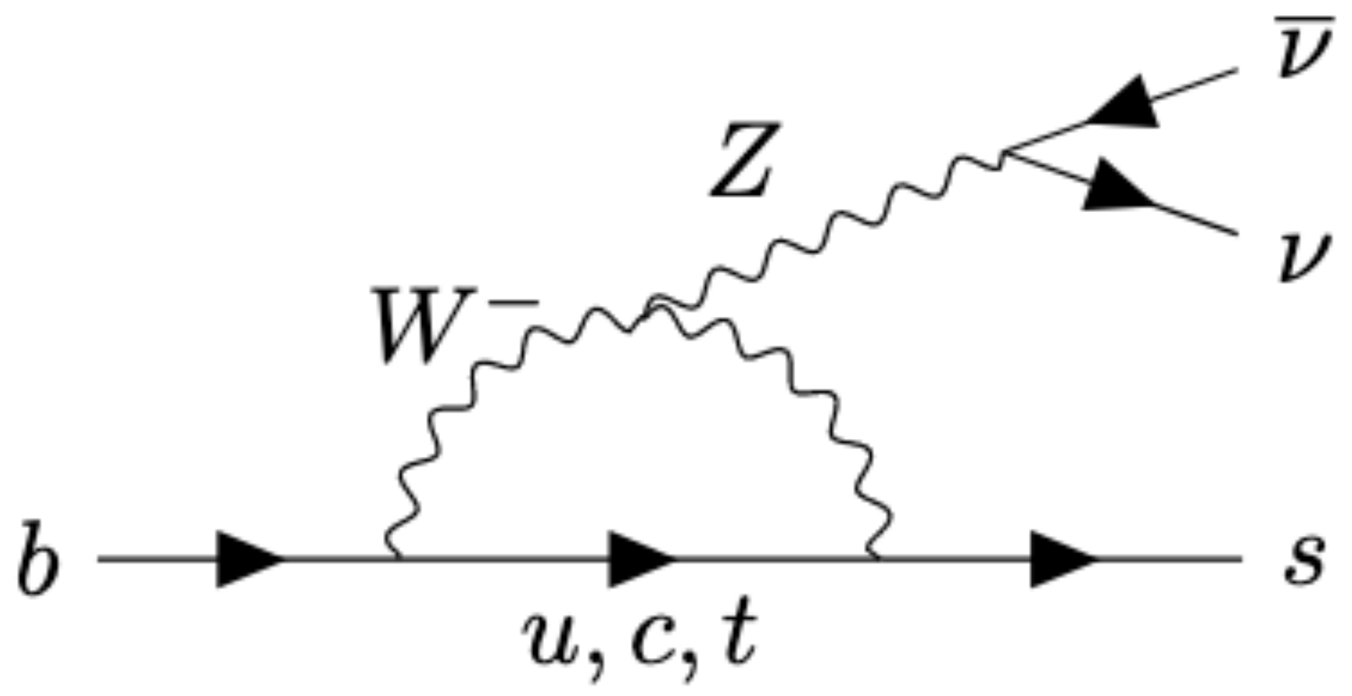
Flavour-changing-neutral current $b \to s\nu\bar{\nu}$

FCNC $b \to s\nu\bar{\nu}$ transitions offer a powerful probe of the SM

- Occur only at the loop level ➞ highly suppressed
- Only W, Z bosons involved ➞ clean theoretical predictions

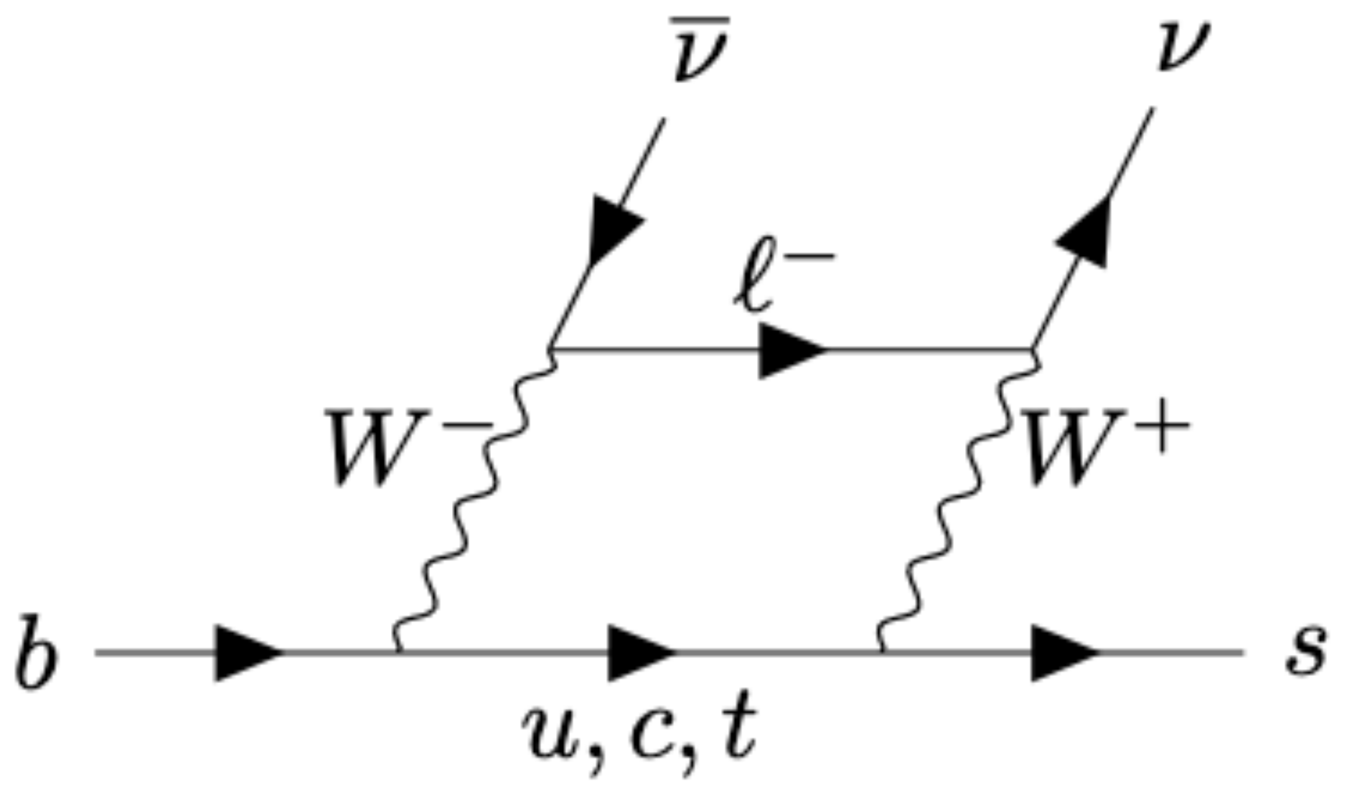
  $\mathcal{B}(B \to K\nu\bar{\nu}) = (4.97 \pm 0.38) \times 10^{-6}$ [arxiv:2207.13371]

  (no $B \to \tau(\to K\bar{\nu})\nu$ contribution)



Highly sensitive to potential new physics (NP) contribution

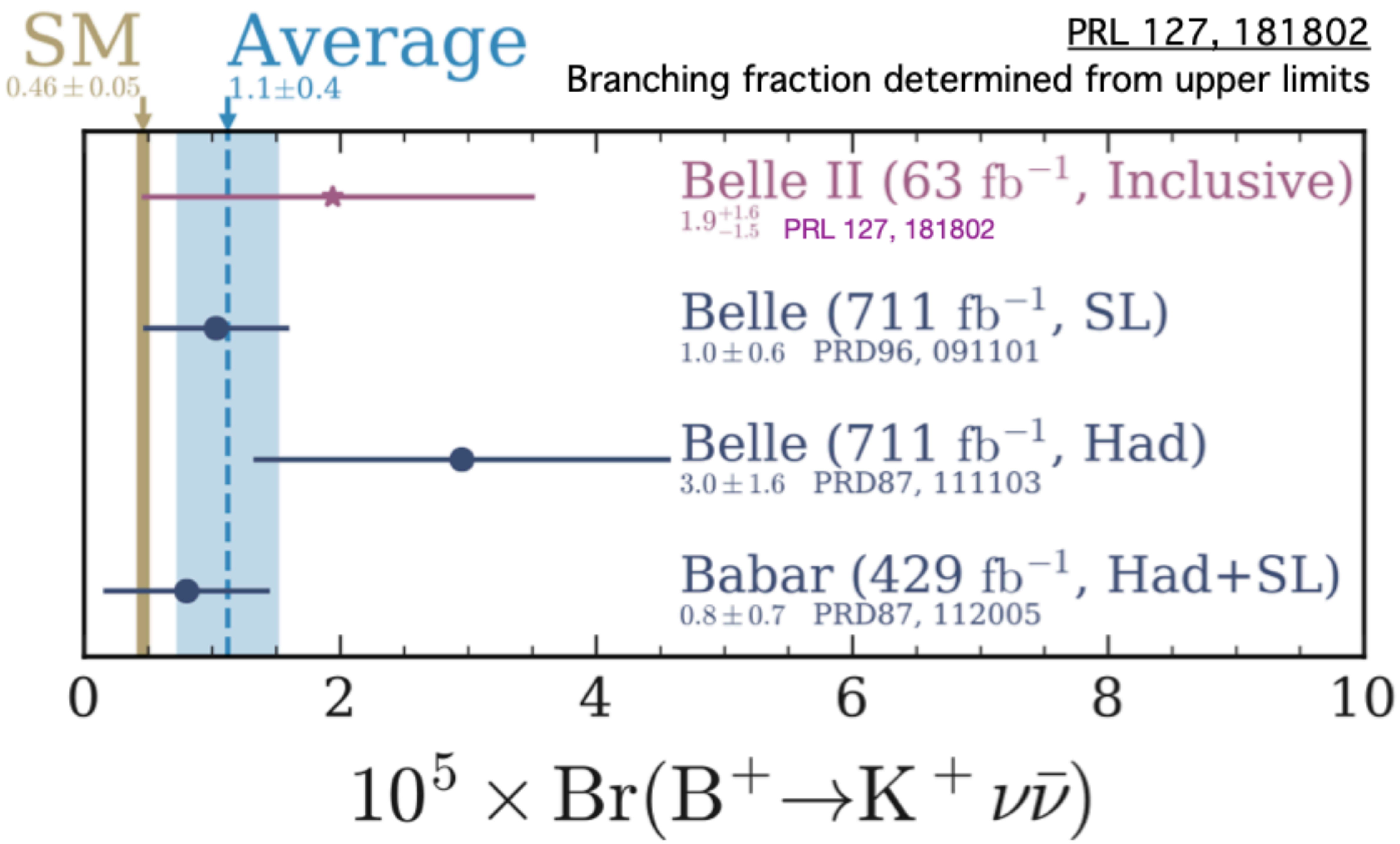
- Mediators in loops or **new tree level diagrams**
- Sources of missing energy (e.g. b ➞ s + DM)



<u>Measure $B^+ \to K^+\nu\bar{\nu}$ decay branching fraction in Run-1 Belle II data</u>

Experimental status before our measurement

- Challenges:
  - Expected low branching fraction
  - Two neutrinos in the final state
    => large background
  - Continuous spectrum for the signal kaon
    => no good variable to fit
- No signal observed in previous searches:
  - Competitive result from Belle II already with sample corresponding to 63 fb^{-1}
  - **Unique for Belle II**



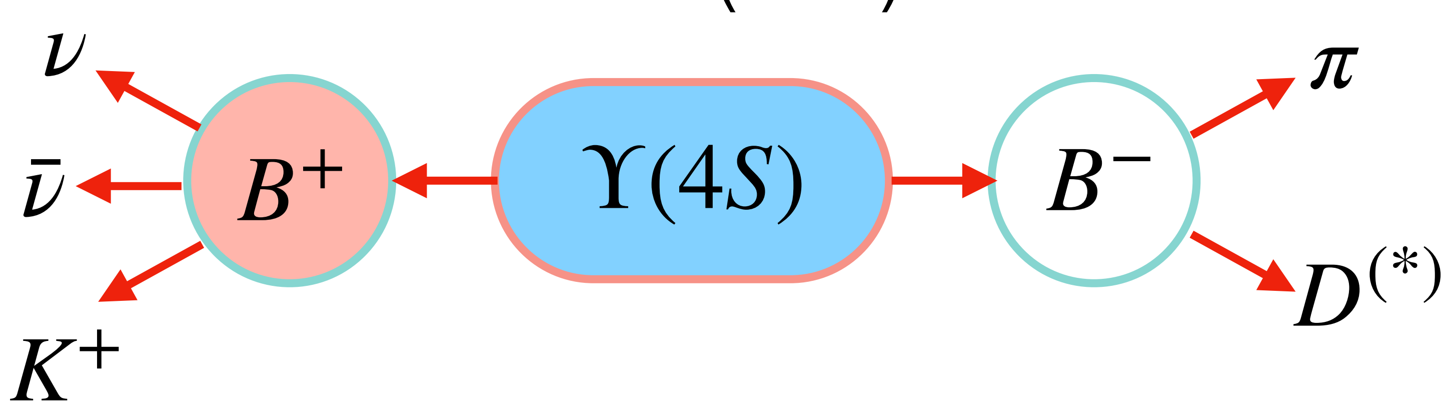
Reconstruction techniques

Specific for B-factories: information from partner B (tag) provides insight about signal B

Hadronic tag

$$B_{\text{tag}} \to \text{hadrons, e.g } B \to D^{(*)} n\pi$$

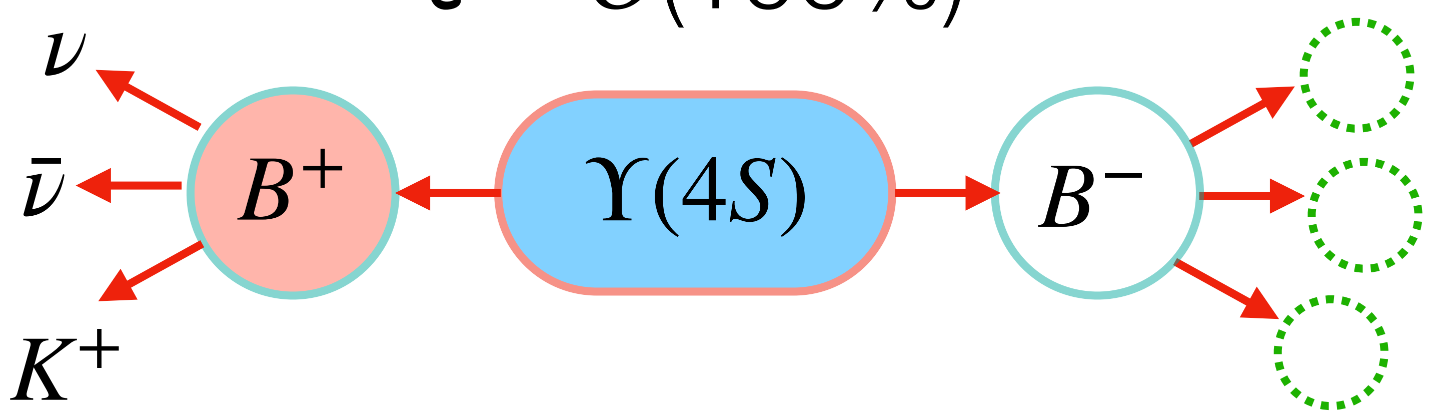
$$\epsilon = \mathcal{O}(2\%)$$



Inclusive tag

$$B_{\text{tag}} \to \text{anything}$$

$$\epsilon = \mathcal{O}(100\%)$$



← Purities of the tagged samples, available physics observables

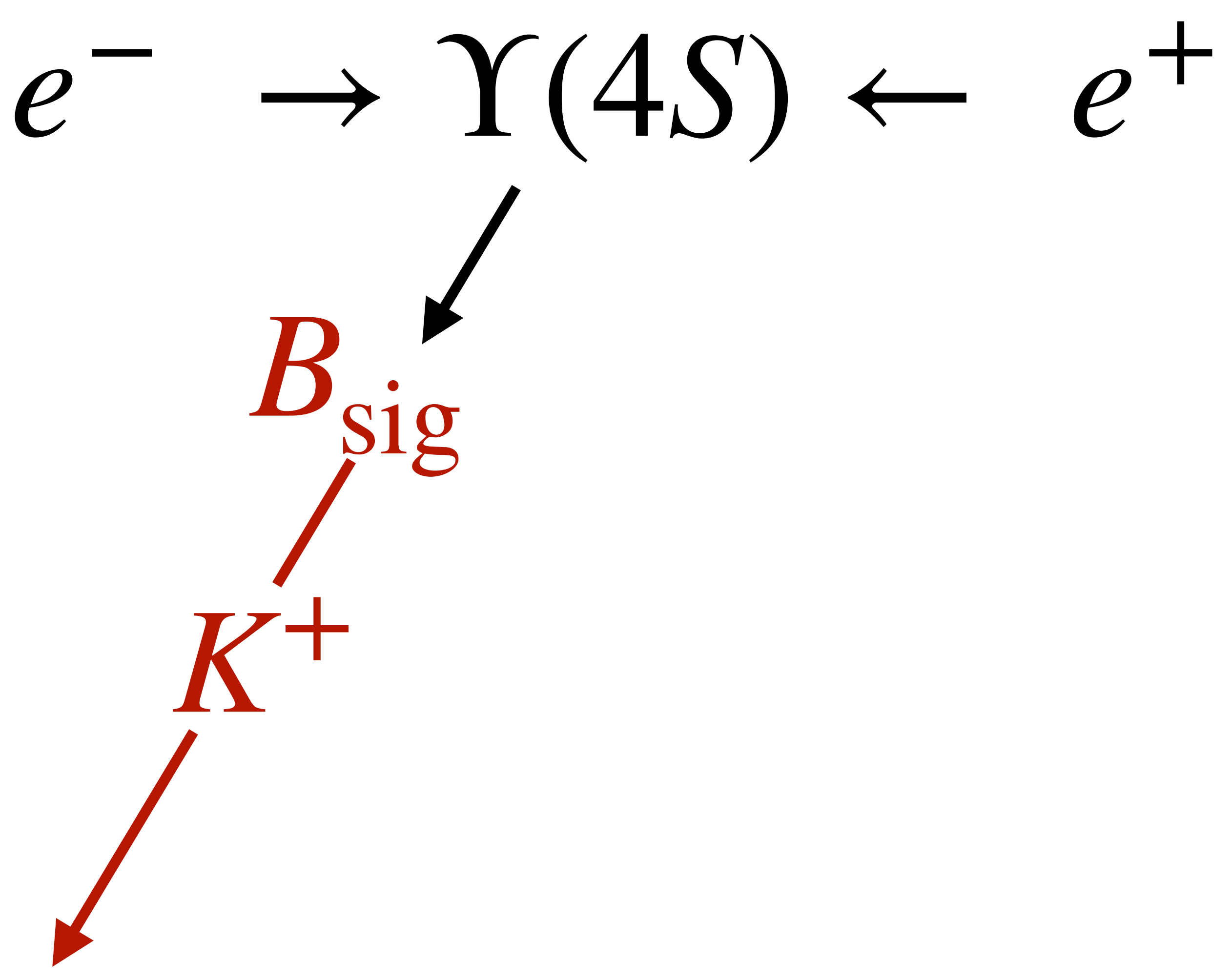
Tagging efficiencies, achievable yields →

Inclusive tag analysis drives the precision

Hadronic tag is an auxiliary measurement

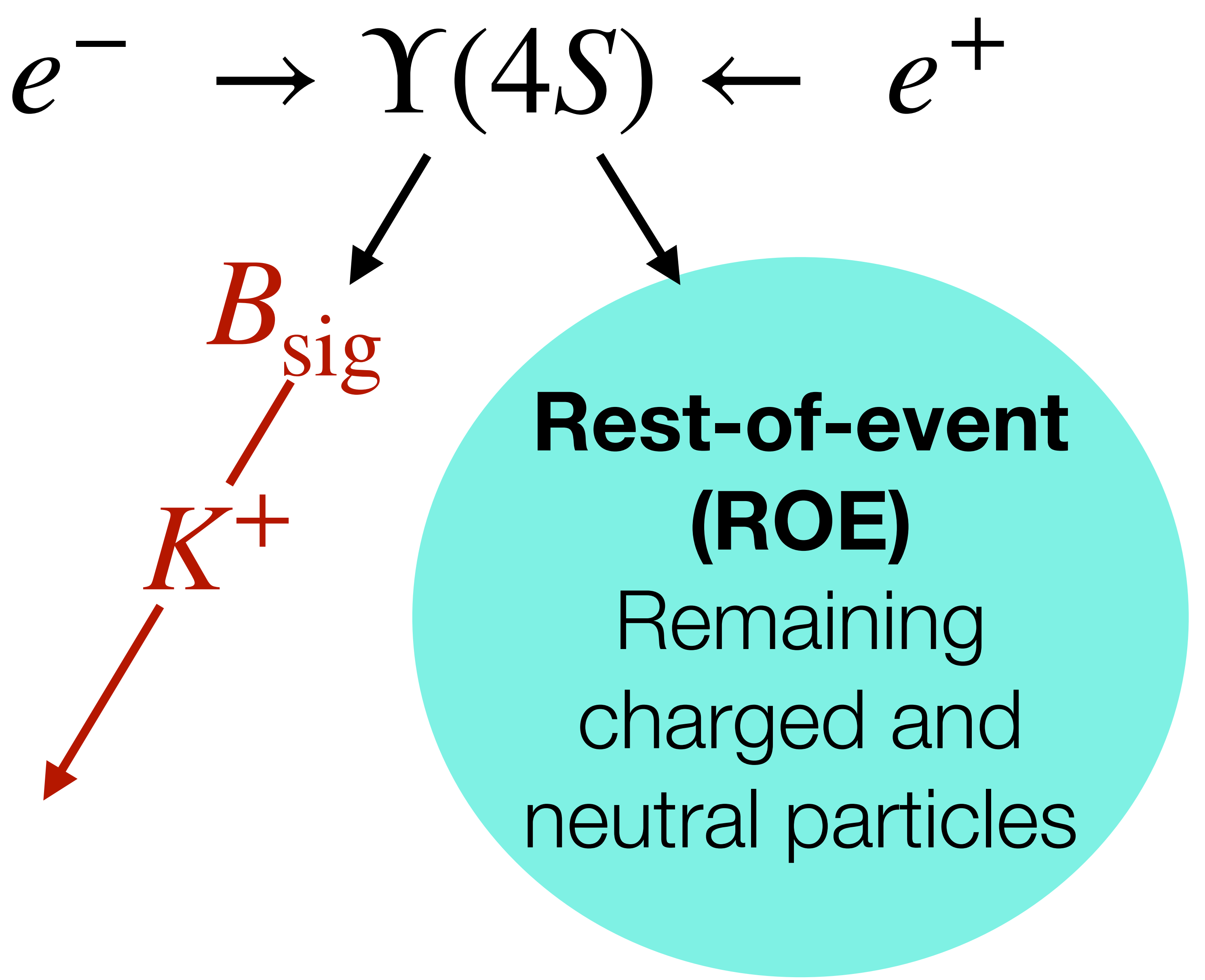
Baseline reconstruction

- Signal candidate: identified charged kaon



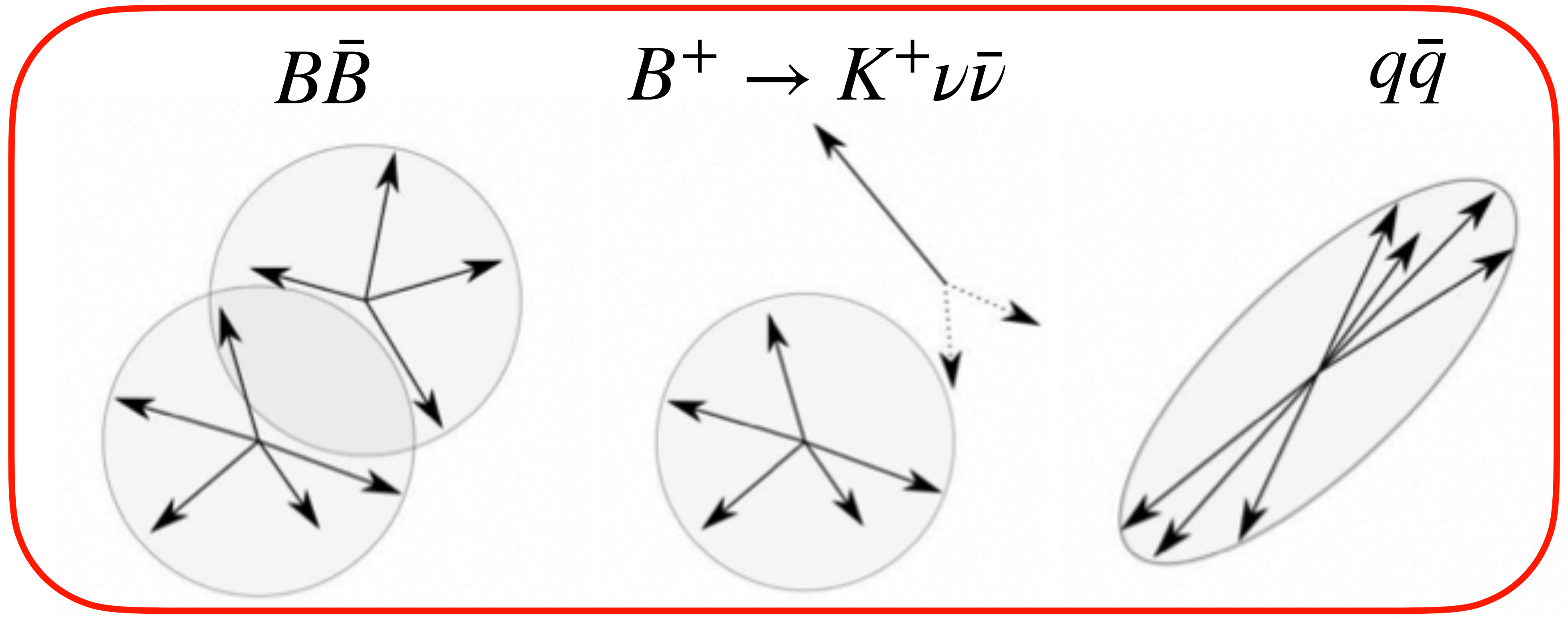
Baseline reconstruction

- Signal candidate: identified charged kaon
- No explicit tag reconstruction
- Charged particles: p_T > 100 MeV/c, close to collision point, in the central part of the detector
  => Pure tracks
- Neutral particles: E > 100 MeV, in the central part of the detector
  => Includes real photons, fake photons, K_L^0 etc.



Signal discrimination

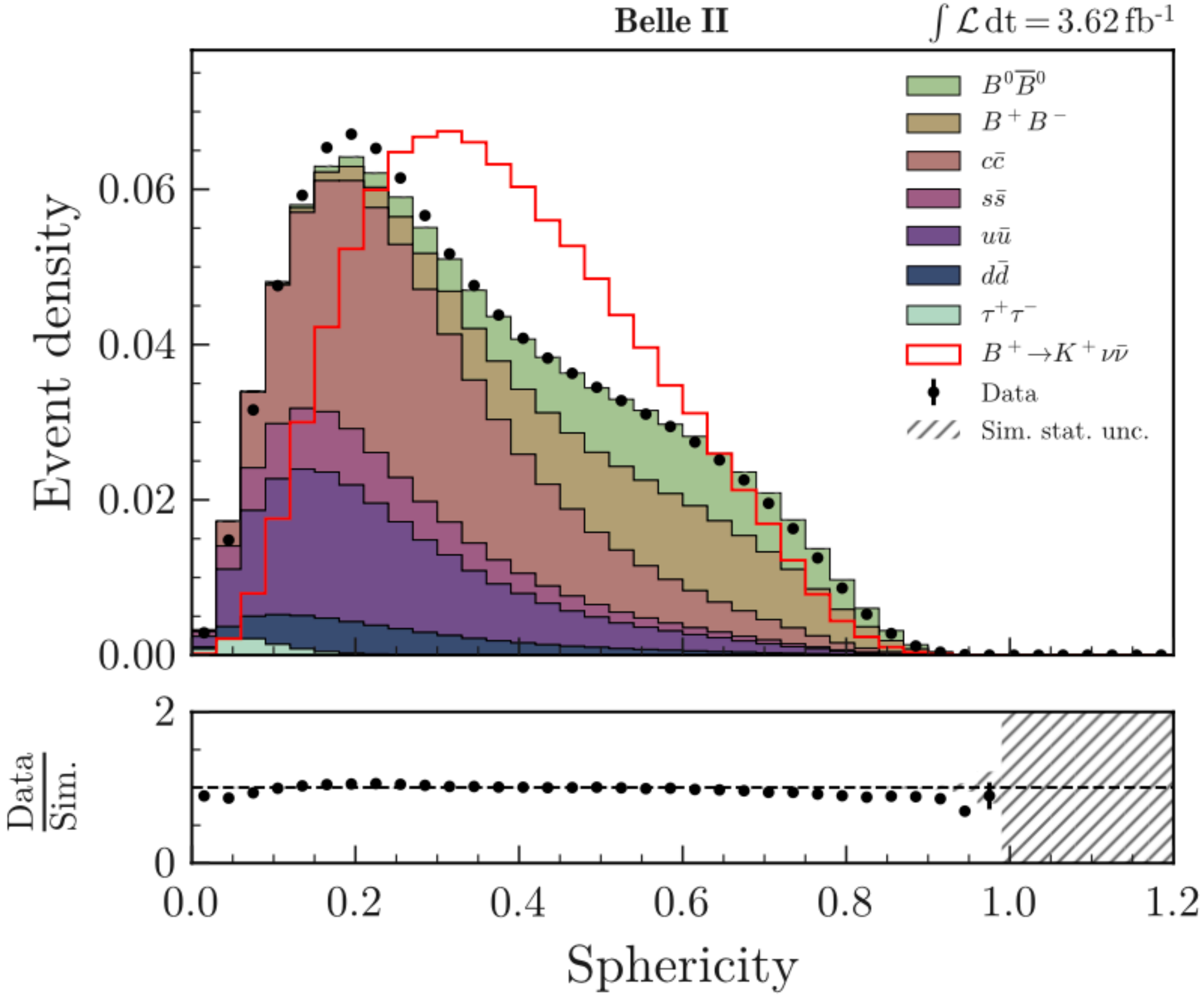
Combine signal kaon, event topology, rest-of-event information in two subsequent MVA classifiers distinguishing signal and background



Backgrounds:

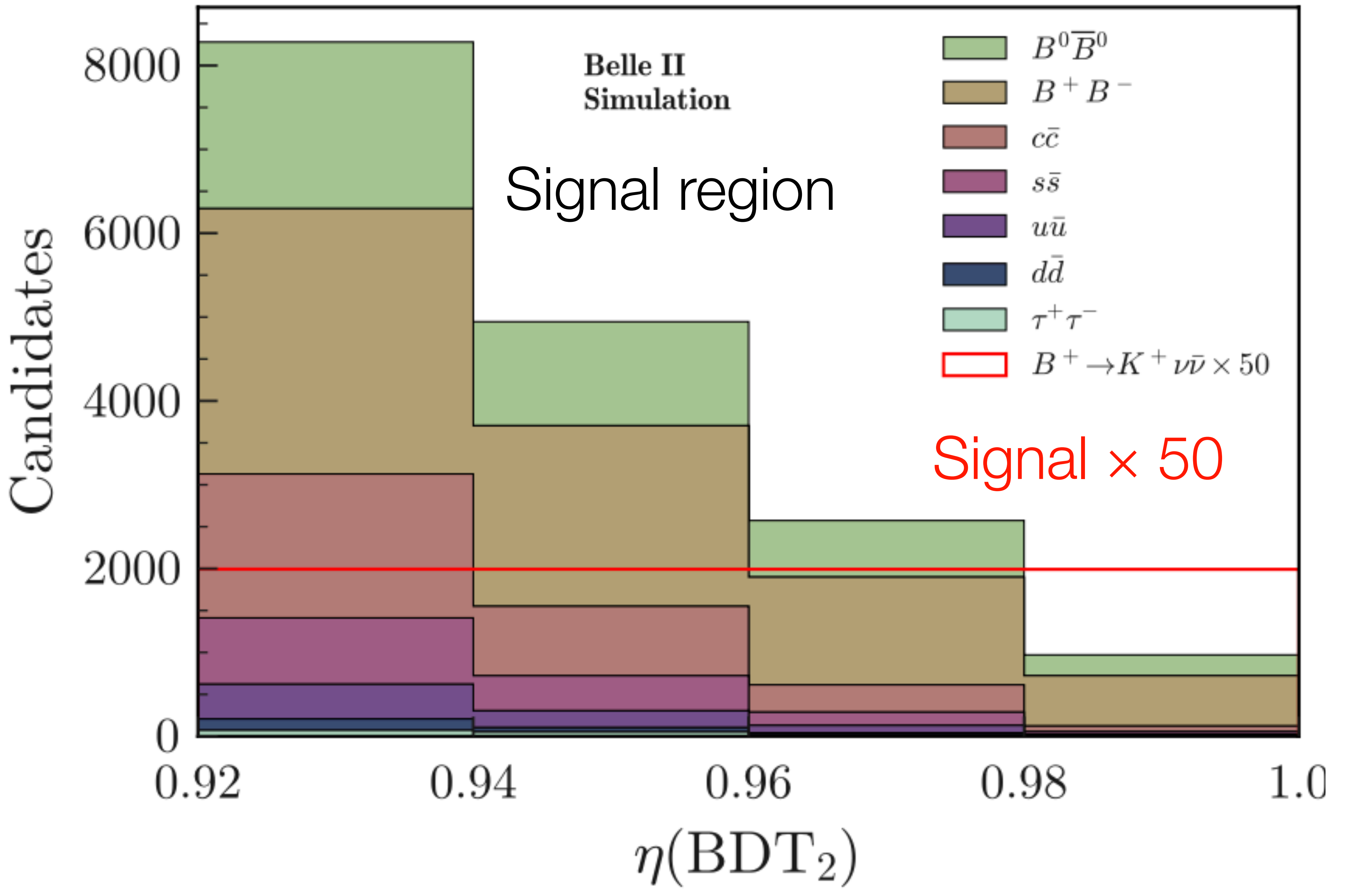
- $e^+e^- \to u\bar{u}$
- $e^+e^- \to d\bar{d}$
- $e^+e^- \to s\bar{s}$
- $e^+e^- \to c\bar{c}$
- $e^+e^- \to \tau^+\tau^-$
- B^+B^- events
- $B^0\bar{B}^0$ events

(the first five: continuum)



Background suppression

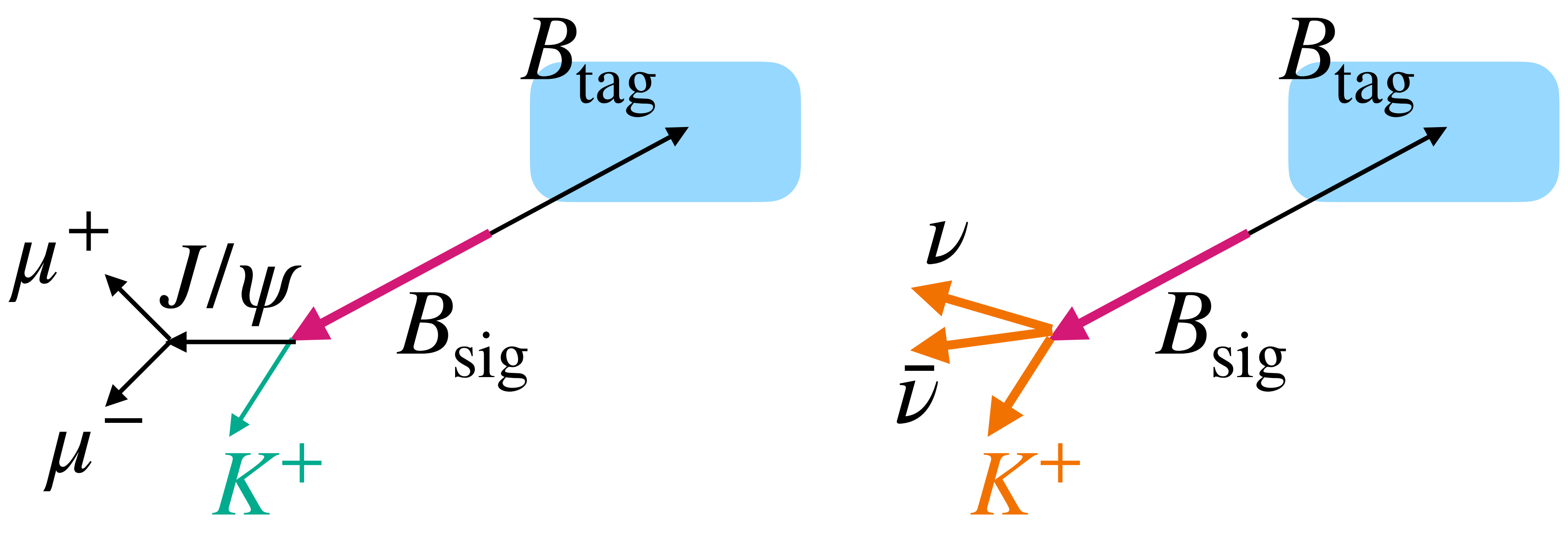
- Train two subsequent multivariate binary classifiers based on boosted decision tree (BDT)
  - BDT_1 used as a filter and trained with fewer variables. Restrict the sample to higher BDT_1 output values
  - BDT_2 provides the main signal-background separation → x3 sensitivity increase wrt BDT_1
- Transform BDT_2 output to $\eta(\mathrm{BDT}_2)$ such that the signal efficiency is flat
- Signal region defined within 8% of signal efficiency

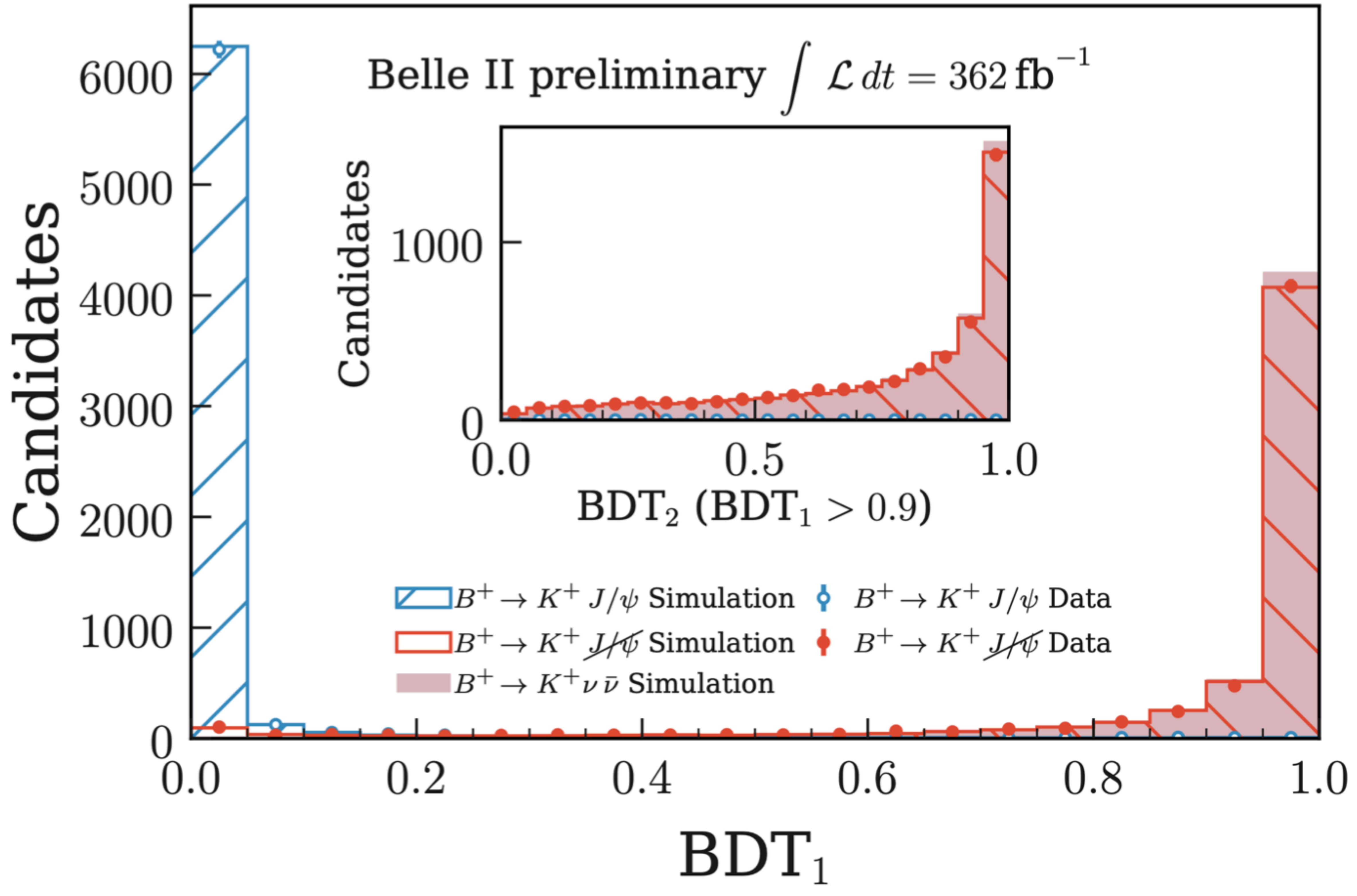


Analysis heavily relies on the simulation
=> Crucial to validate it in data

Signal efficiency validation

- Use clean signature and abundant $B^+ \to J/\psi K^+$ decay reconstructed in data and simulation
- Remove J/ψ products and substitute K^+ with K^+ from signal simulation
- Apply signal selection and check data-simulation agreement for relevant variables and efficiency

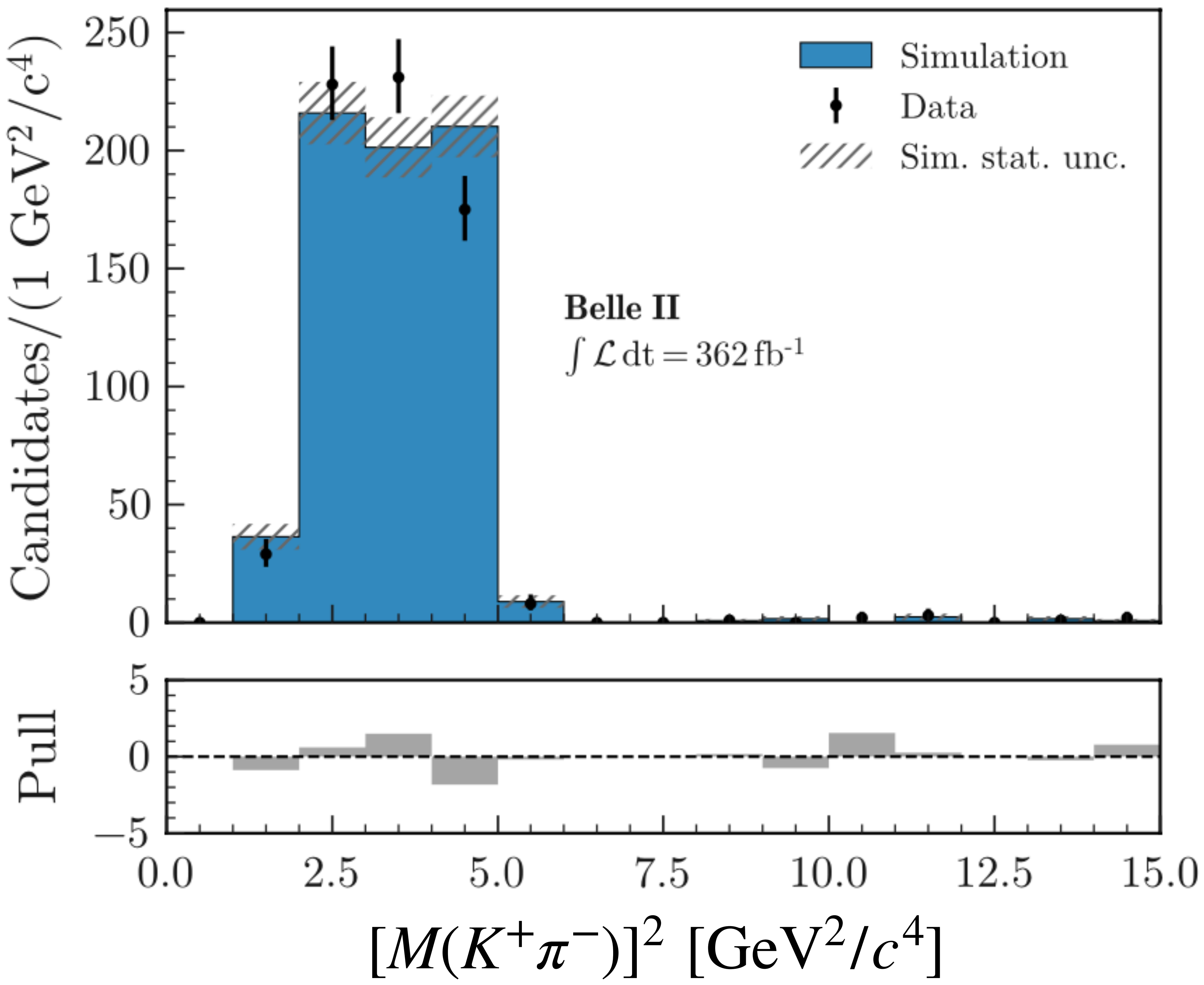




Data-simulation efficiency ratio 1.00±0.03 - good agreement within 3% which is included in systematics

Validation of particle identification

- Particle identification selection on kaon is the sole strong signal requirement
- Check data-simulation agreement
  => Apart from kaon identification efficiency also worried about pion-kaon misidentification
  => Use abundant and low-background $D^{*+} \to D^0(\to K^-\pi^+)\pi^+$ decay
  => Corrections: ~0.9 for kaon ID efficiency, ~2 for pion-to-kaon fake rate
- Validate corrections using $B^+ \to \bar{D}^0(\to K^+\pi^-)h^+,\ (h = K/\pi)$



Validation of $e^+e^- \to q\bar{q}$ modeling

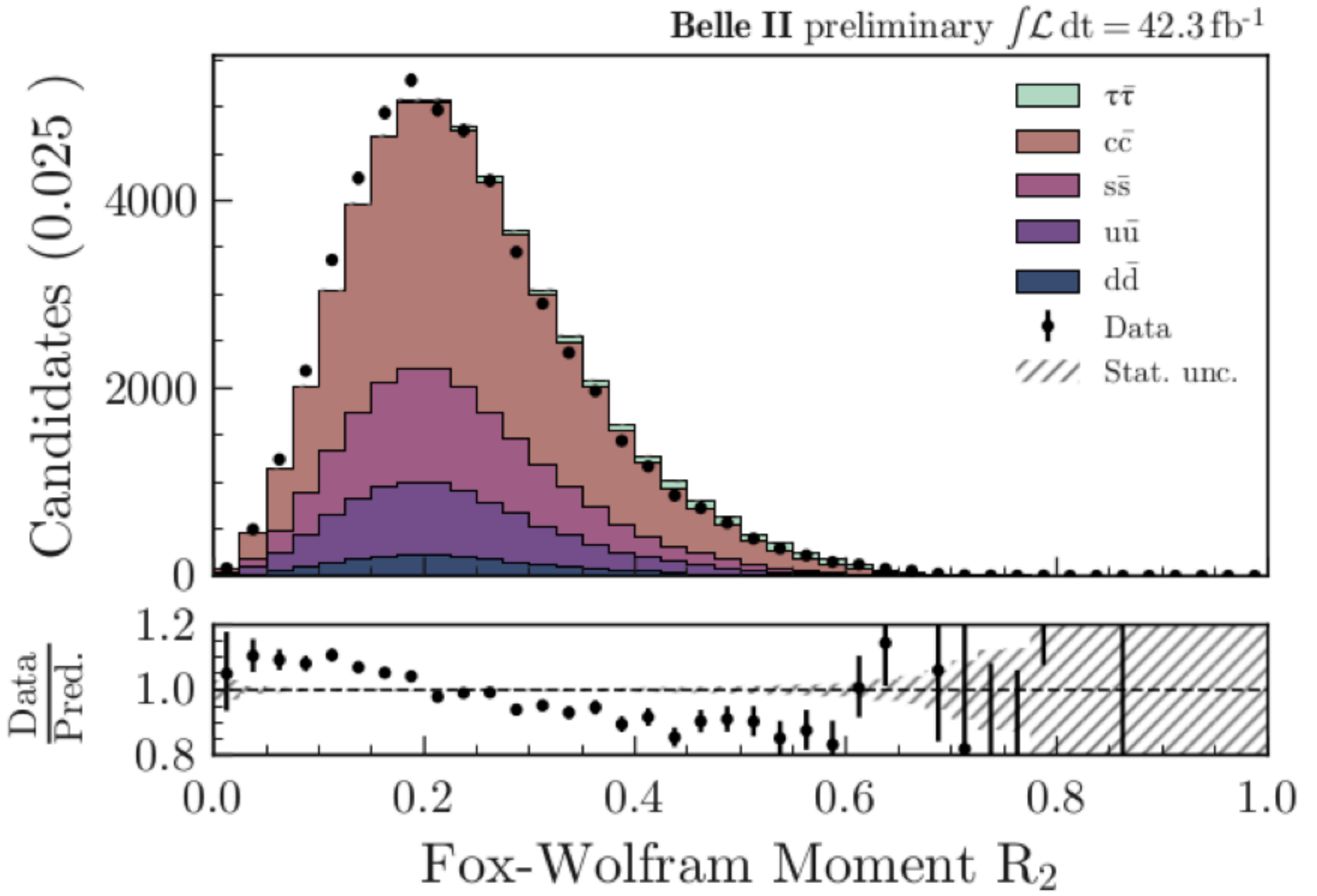
- Compare pure continuum data (off-resonance) and continuum simulation
- Normalization in data 40% larger than in simulation
- Several discrepancies in shapes of relevant variables
  => Reweight simulation using J. Phys.: Conf. Ser. 368 012028
- Train a classifier $\mathrm{BDT_c}$ that distinguishes data from simulation
- Introduce a weight that suppresses events in simulation that do not resemble the data

$$\frac{\mathrm{BDT_c}}{1 - \mathrm{BDT_c}}$$

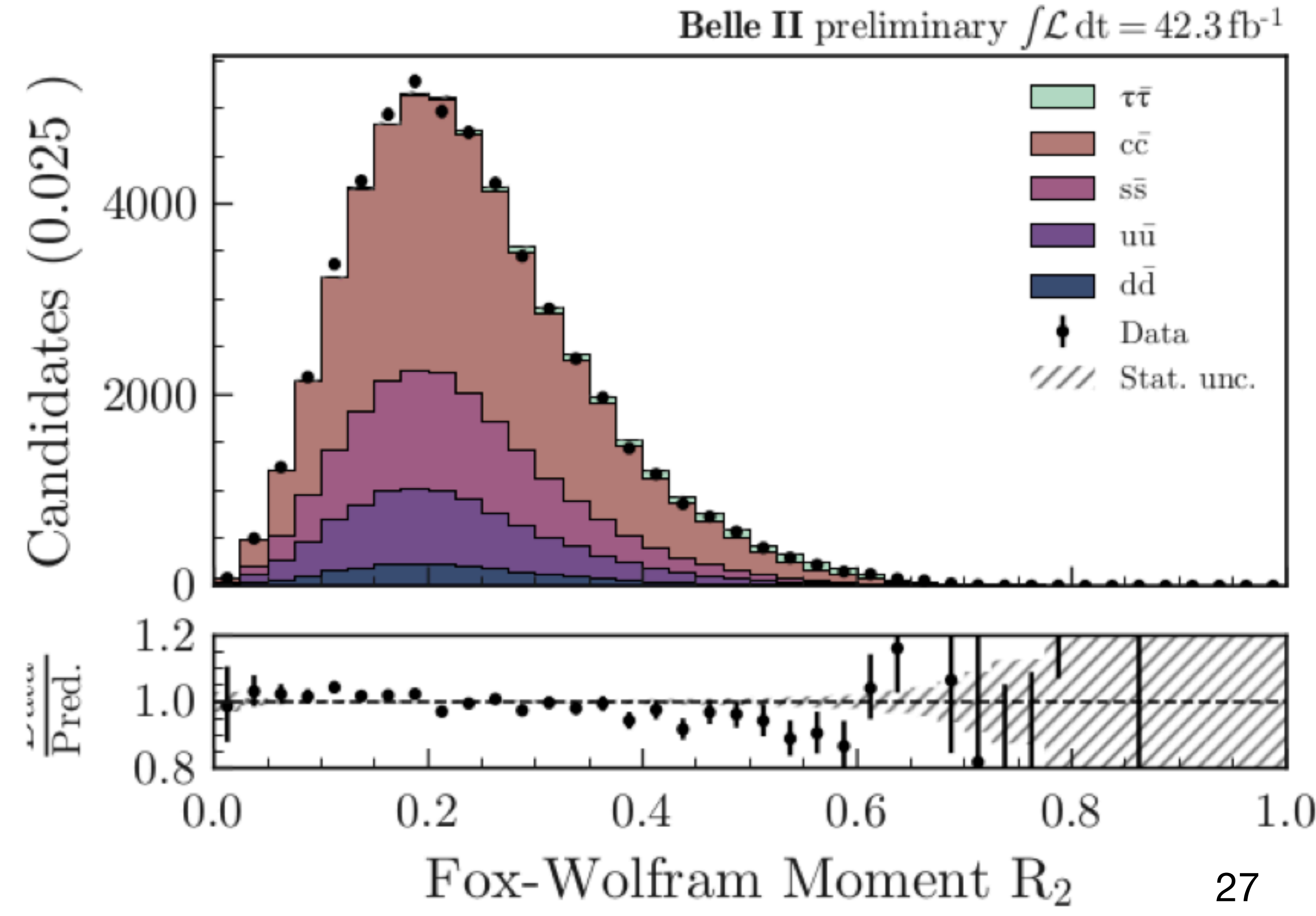
- Correct simulation using this weight

Agreement improved after the corrections

Before corrections



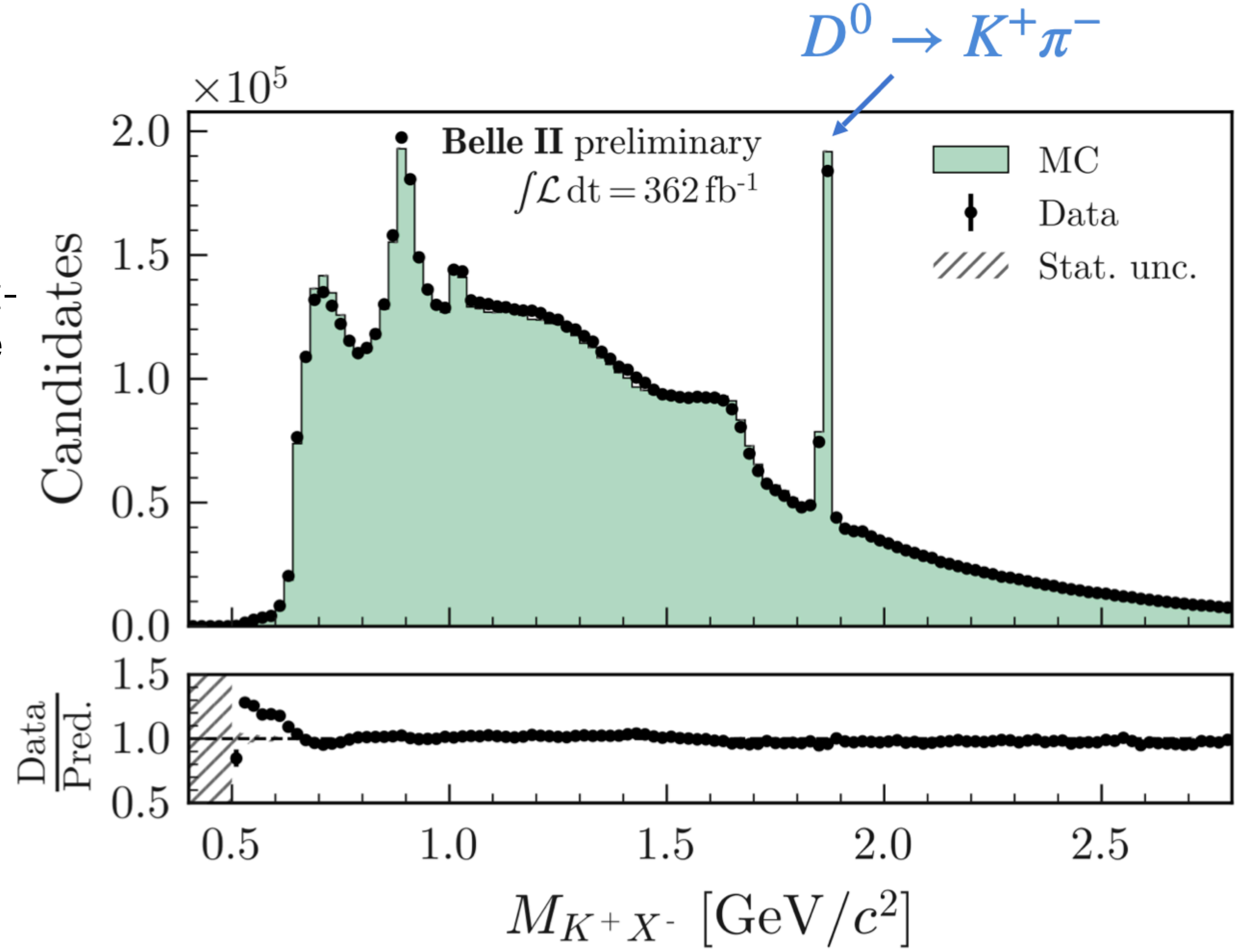
After corrections



Validation of $B\bar{B}$ modeling: kaons from D

- Semileptonic B decays with kaons coming from a D decay
- Check invariant mass of the signal kaon combined with a charged particle from the rest-of-event (before applying strict selection on the BDT output)

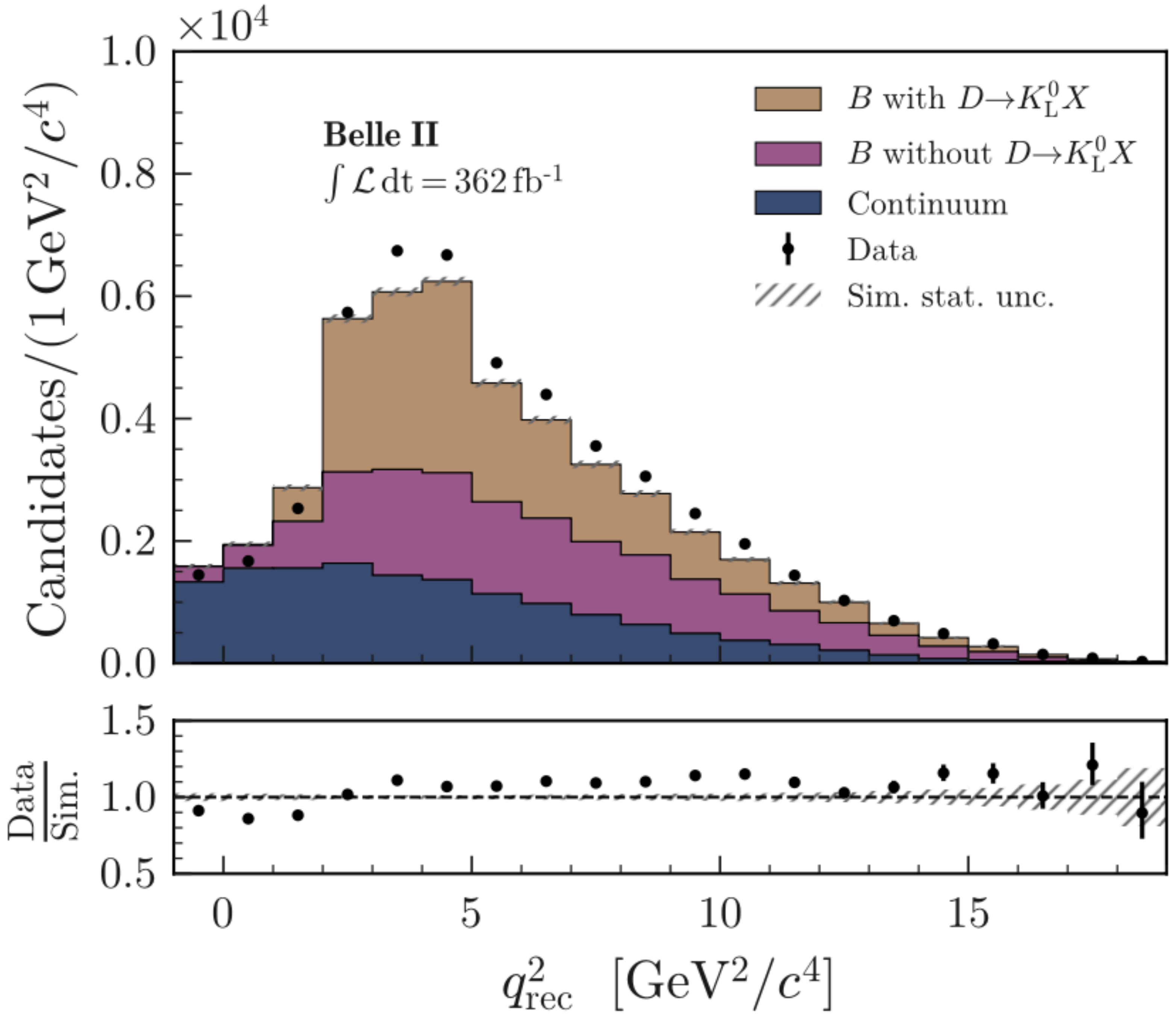
Good agreement

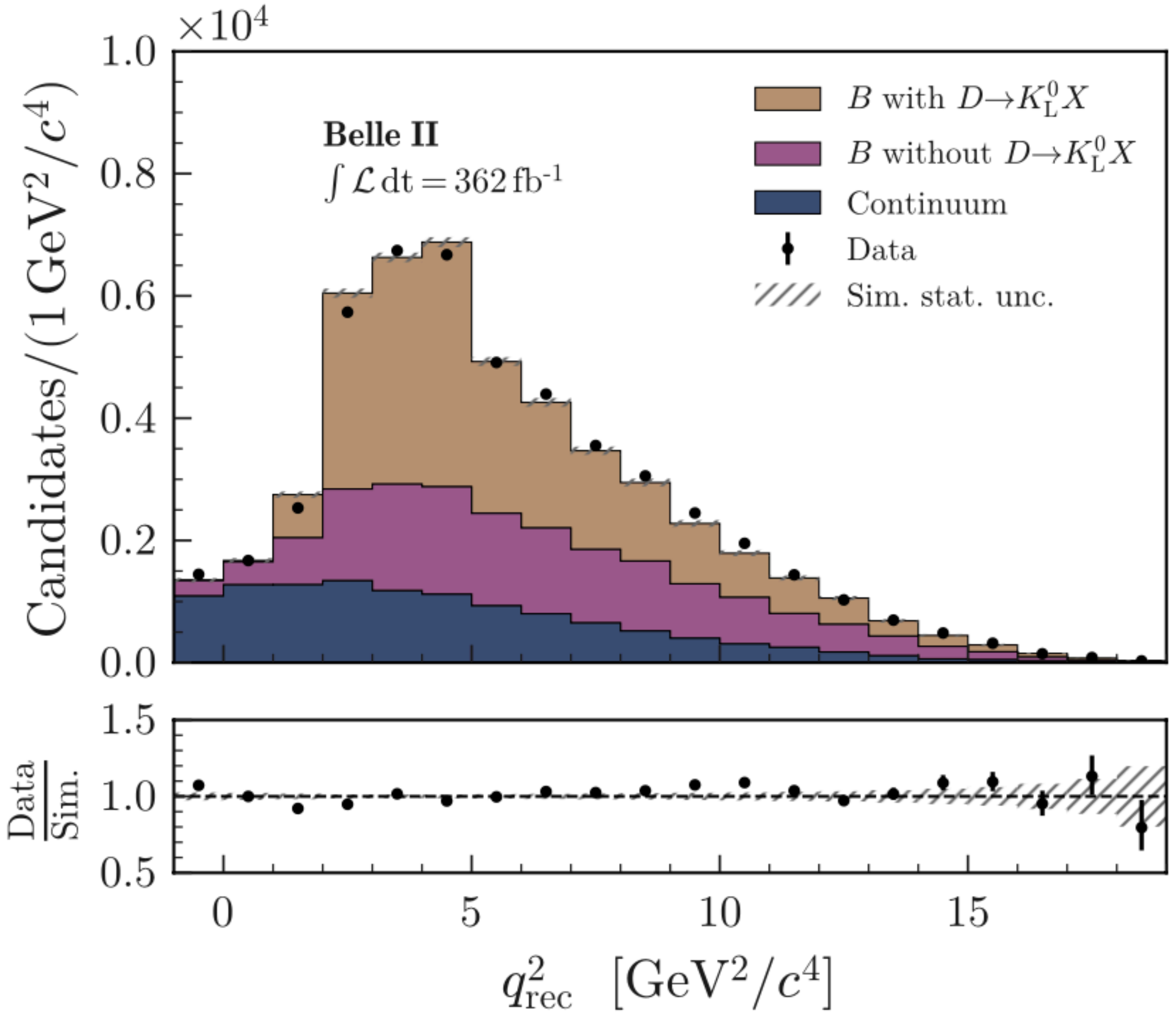


Validation of $B\bar{B}$ modeling: $B \to D(\to K_L^0 X)X$

$$q^2_{\rm rec} = s/(4c^4) + M_K^2 - \sqrt{s}E_K^*/c^4$$

- Contribution from $B^+ \to K^+\bar{D}^{(*)0}$ and $B^0 \to K^+\bar{D}^{(*)-}$ decays can be underestimated in simulation due to the poorly known fraction of D meson decays involving $K_{\rm L}^0$
- Use sample enriched in pions to check the modeling
- Perform 3-components fit of $q^2_{\rm rec}$ to find the scale for $B \to D \to K_{\rm L}^0$ decays



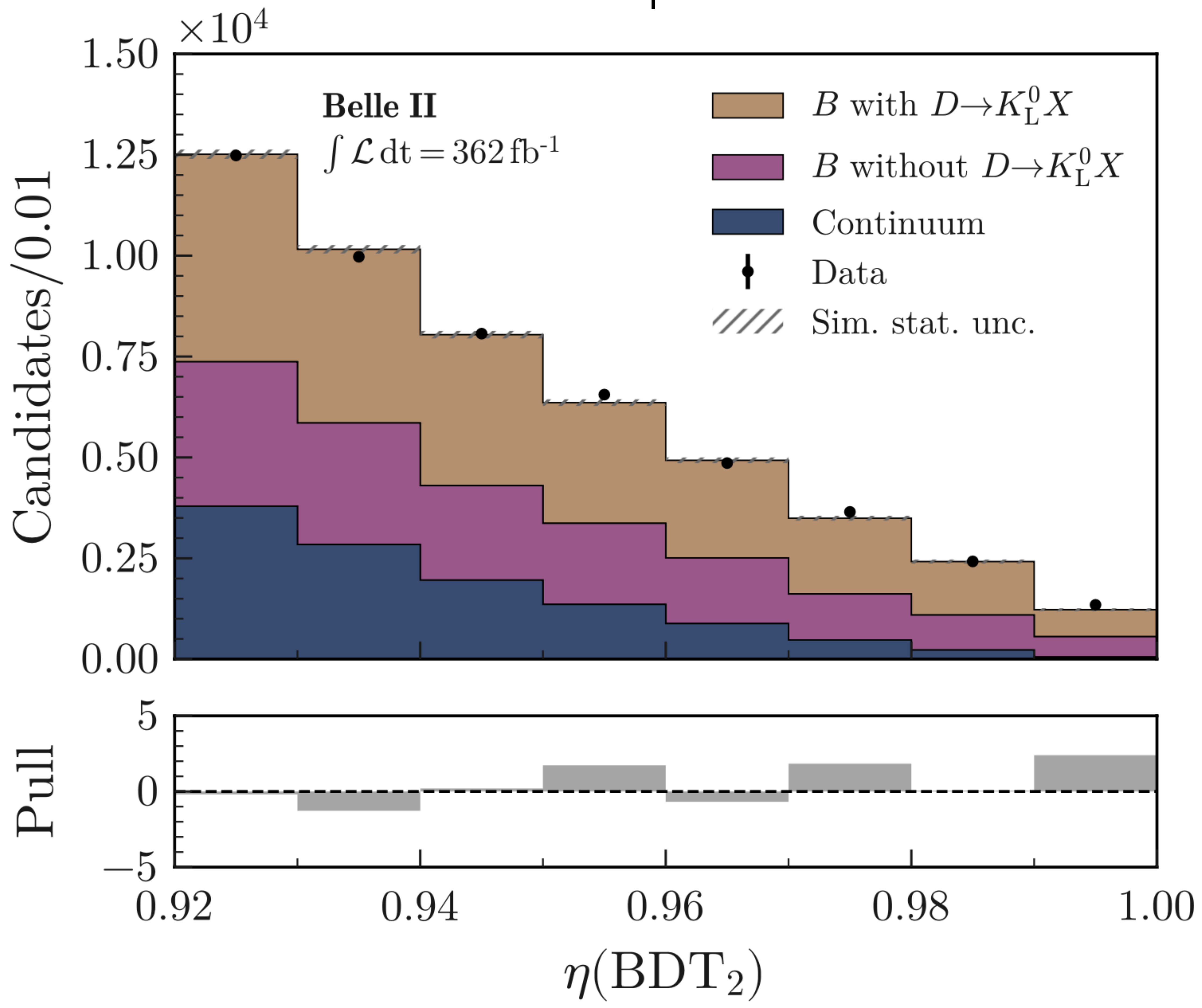


Scaling up $B \to D \to K_{\rm L}^0$ decays by factor of 1.35 in simulation results in better agreement
=> Similar correction of 1.38 obtained in muon and electron enriched control samples
=> Scale up $B \to D \to K_{\rm L}^0$ decays by 1.3±0.1

Validation of $B\bar{B}$ modeling: $B \to D(\to K_L^0 X)X$

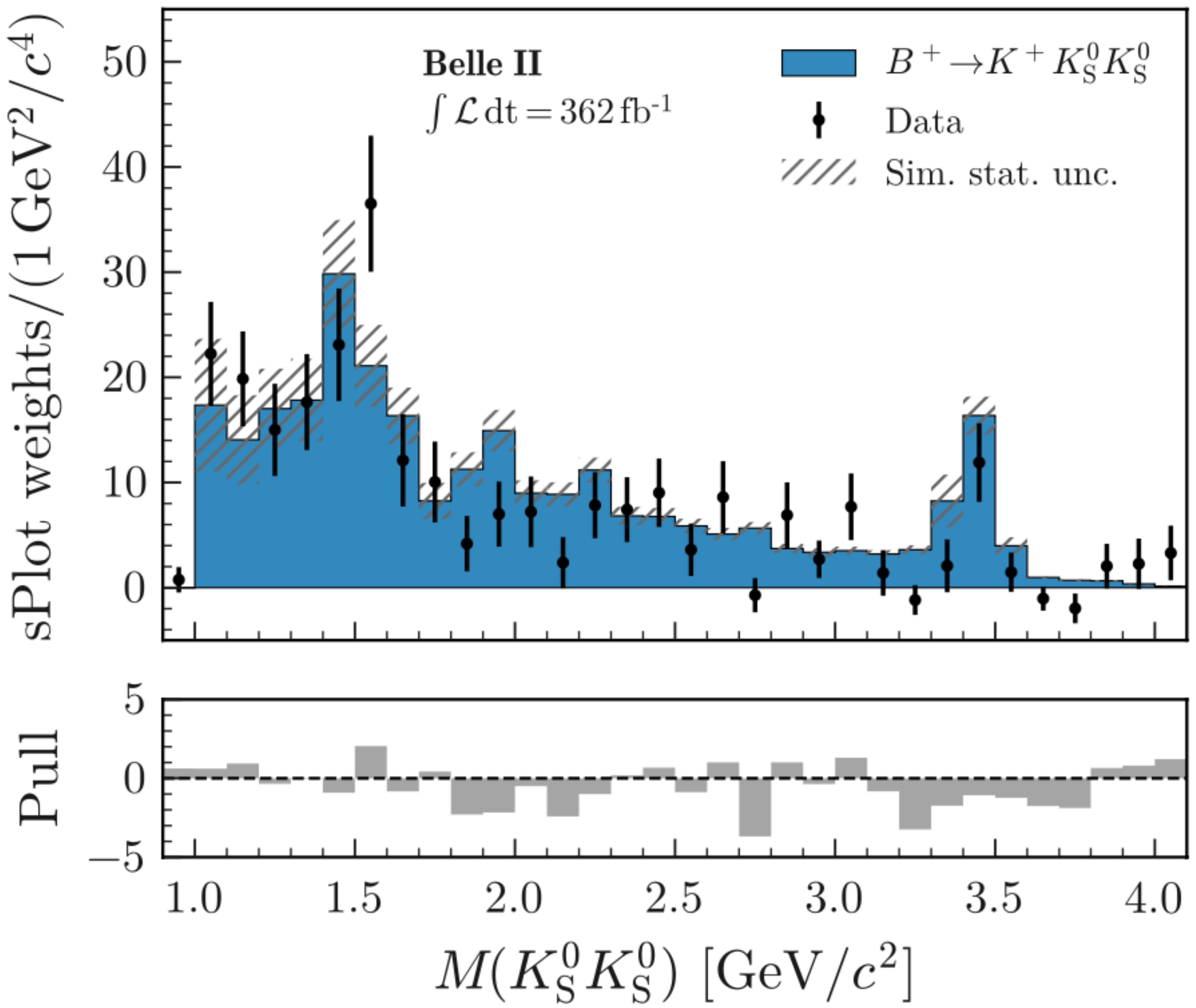
Well described! ✓

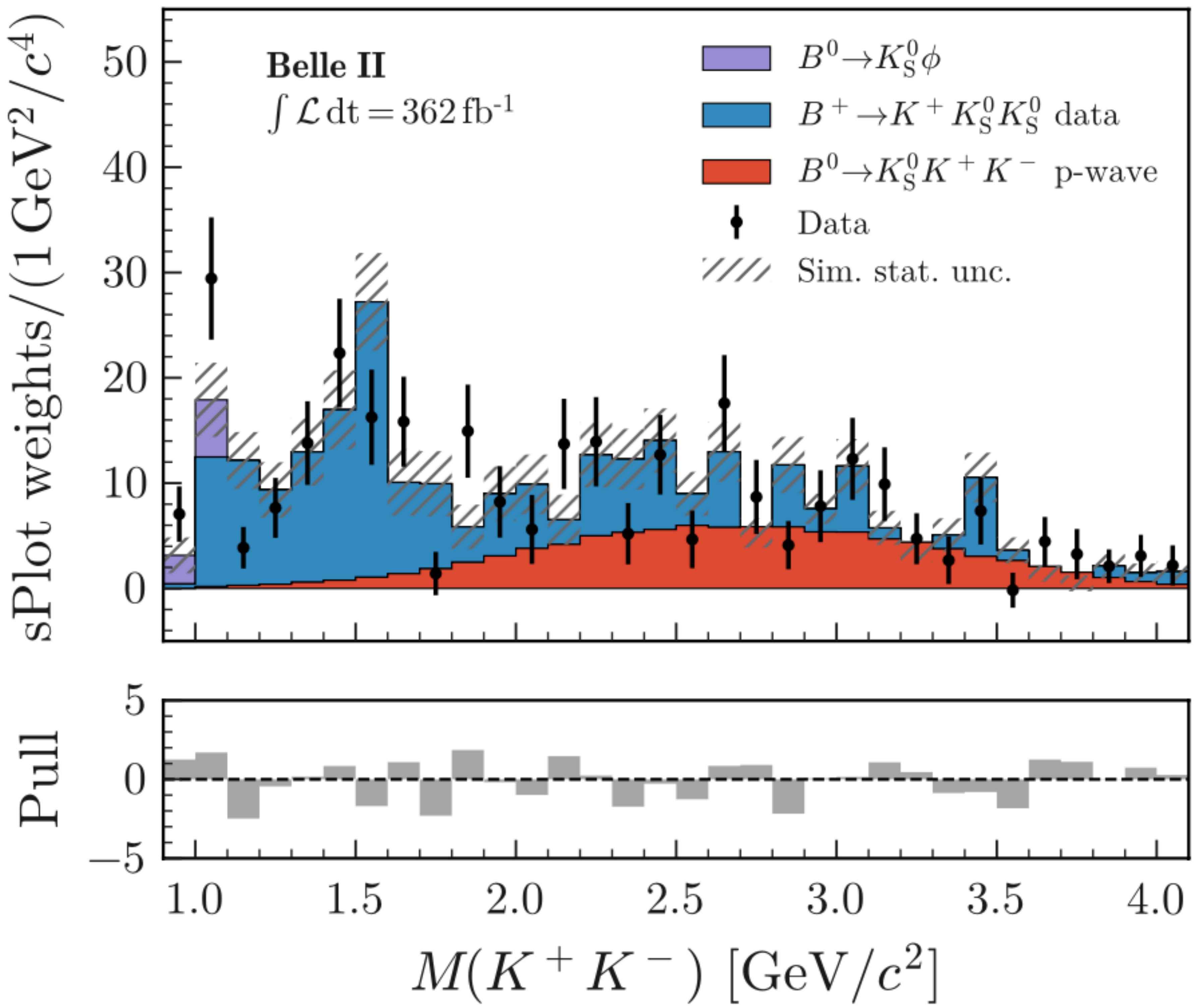
Pion enriched sample after correction



Validation of signal-like background

- $B^+ \to K^+ K^0 \bar{K}^0$can mimic the signal and is poorly constrained
- Use BaBar [PRD85, 112010] $B^+ \to K^+ K_S^0 K_S^0$ to model $B^+ \to K^+ K_L^0 K_L^0$
- Model $B^+ \to K^+ K_S^0 K_L^0$ by using inputs from $B^+ \to K^+ K_S^0 K_S^0$ and $B^0 \to K_S^0 K^+ K^-$ decays

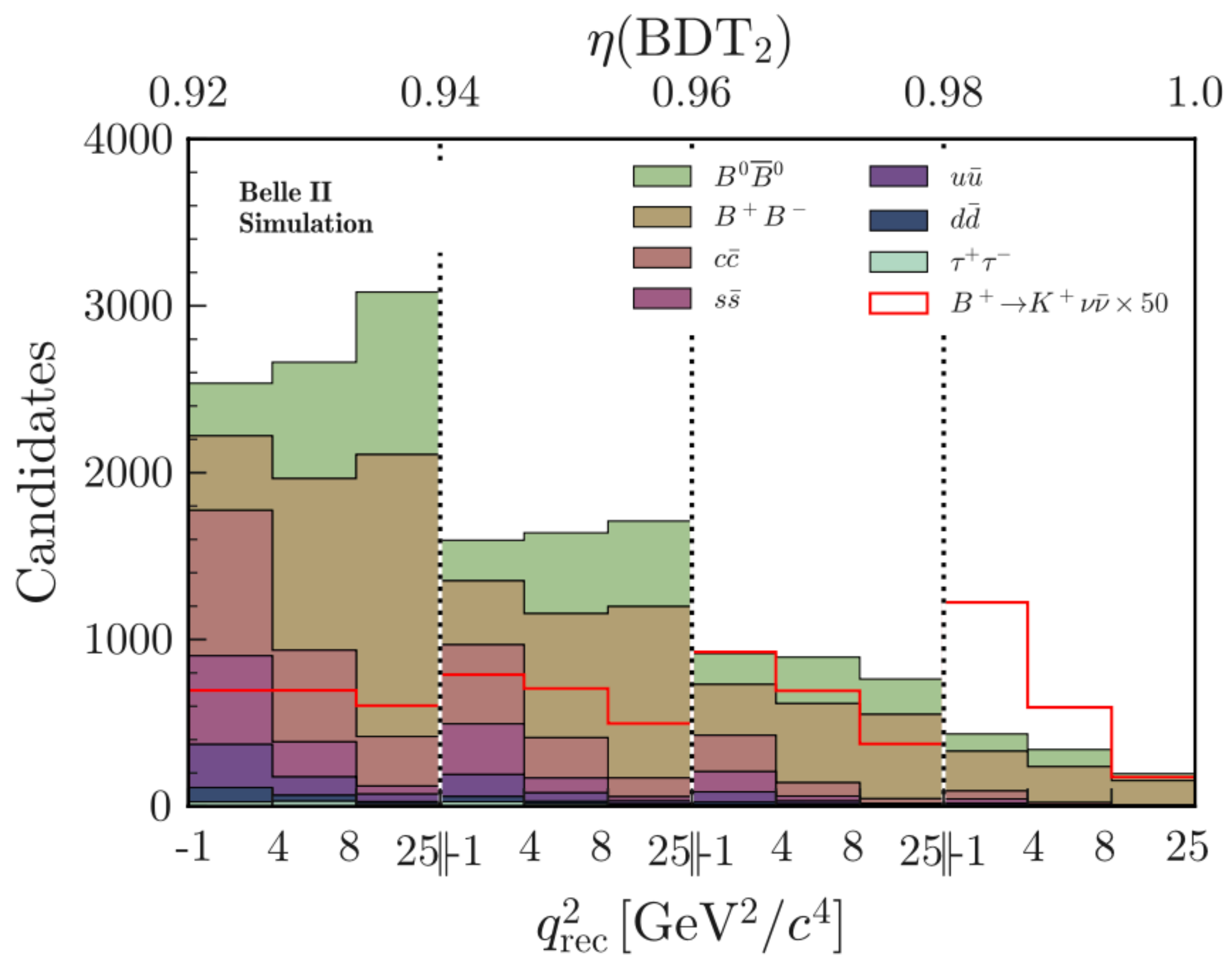




Good agreement

Signal extraction

- Signal region divided into 4 bins of $\eta(\mathrm{BDT}_2)$ and 3 bins of q^2_{rec}
- Also fit off-resonance data to constrain continuum background
- 24 bins in total: $\underbrace{\eta(\mathrm{BDT}_2)}_{\text{4 bins}} \times \underbrace{q^2_{\mathrm{rec}}}_{\text{3 bins}} \times \underbrace{[\text{on/off res}]}_{\text{2 bins}}$
- Binned likelihood fit with one signal and 7 background components
    - Poisson uncertainties for data counts
    - Systematic uncertainties included in the fit as predicted rate modifiers with Gaussian likelihoods
    - Simulated sample size uncertainties are included as nuisance parameters, per each bin and each fit category



193 nuisance parameters and the parameter of interest: signal strength $\mu = BR/BR_{SM}$, with $BR_{SM} = 4.97 \times 10^{-6}$ ($B \to \tau(\to K\bar{\nu})\nu$ treated as background)

Systematics

Source	Uncertainty size	Impact on σ_μ
Normalization of $B\bar{B}$ background	50%	0.90
Normalization of continuum background	50%	0.10
Leading B-decay branching fractions	$O(1\%)$	0.22
Branching fraction for $B^+ \to K^+ K^0_L K^0_L$	20%	0.49
p-wave component for $B^+ \to K^+ K^0_S K^0_L$	30%	0.02
Branching fraction for $B \to D^{**}$	50%	0.42
Branching fraction for $B^+ \to K^+ n\bar{n}$	100%	0.20
Branching fraction for $D \to K^0_L X$	10%	0.14
Continuum-background modeling, $\mathrm{BDT_c}$	100% of correction	0.01
Integrated luminosity	1%	< 0.01
Number of $B\bar{B}$	1.5%	0.02
Off-resonance sample normalization	5%	0.05
Track-finding efficiency	0.3%	0.20
Signal-kaon PID	$O(1\%)$	0.07
Photon energy	0.5%	0.08
Hadronic energy	10%	0.37
K^0_L efficiency in ECL	8.5%	0.22
Signal SM form factors	$O(1\%)$	0.02
Global signal efficiency	3%	0.03
Simulated-sample size	$O(1\%)$	0.52

Statistical uncertainty on μ is 1.0

- For the hadronic-tag, use similar set of systematic uncertainties.
- Dominant are background normalization, simulation statistics, and systematic on mismodeling of photon multiplicity in the rest of event..

Closure test

Measure known decay mode to validate the method

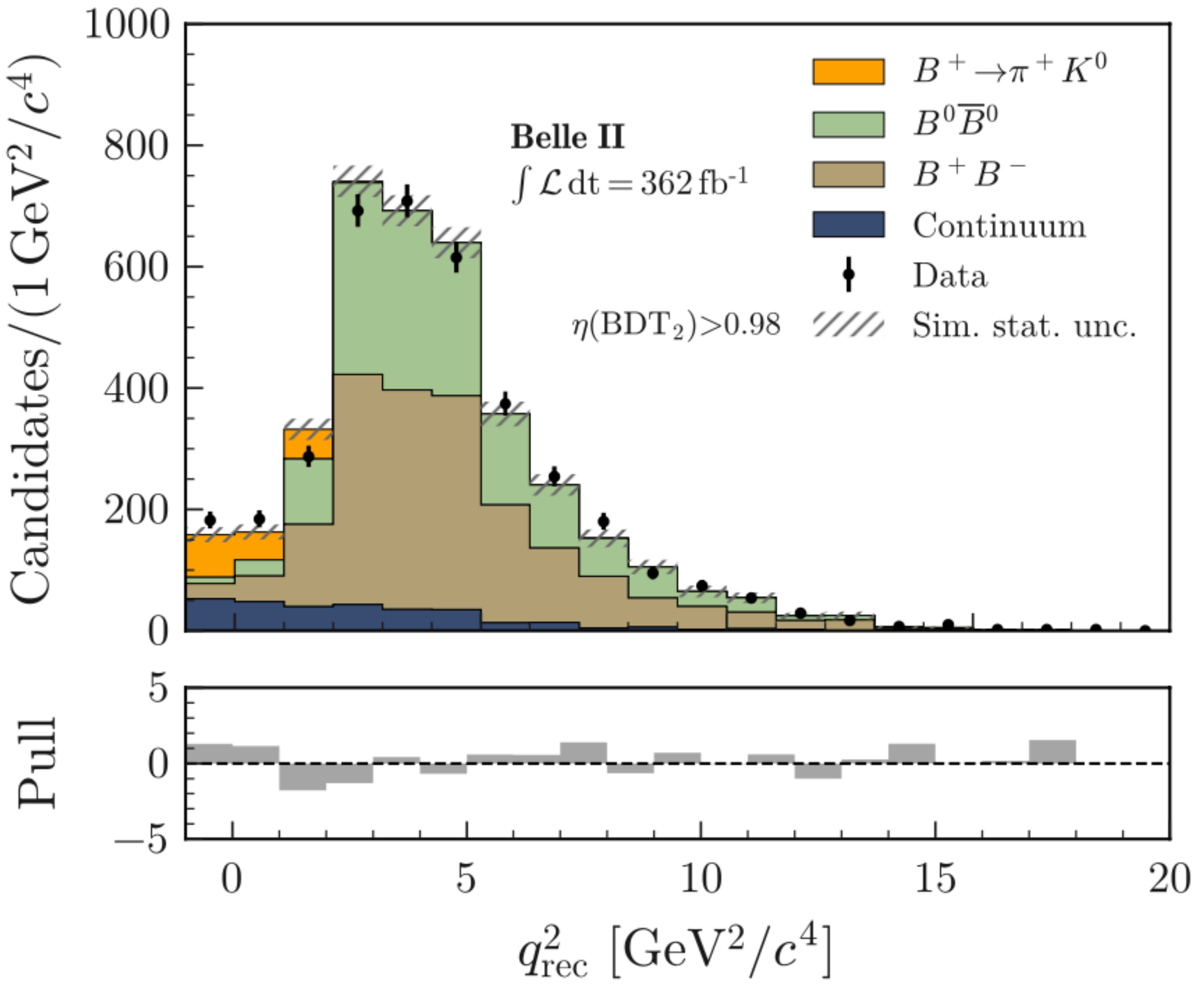
Minimally adapt $B^+ \to K^+ \nu \bar{\nu}$ to measure BF($B^+ \to \pi^+ K^0$)

$B^+ \to \pi^+ K^0$ has similar branching fraction to SM $B^+ \to K^+ \nu \bar{\nu}$

BF($B^+ \to \pi^+ K^0$) = (2.5 ± 0.5) x 10^{-5}

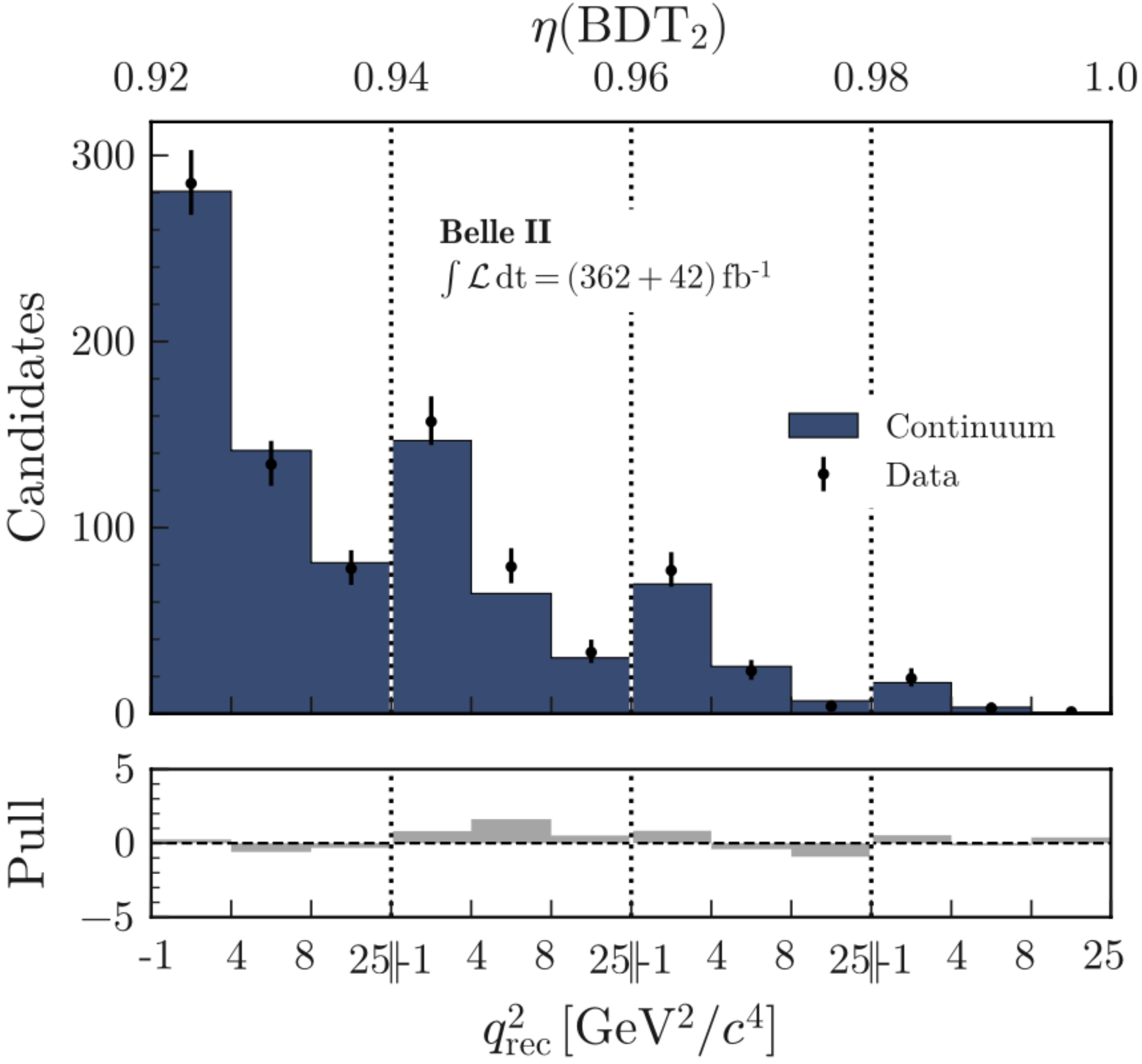
consistent with PDG [(2.38 ± 0.08) x 10^{-5}]

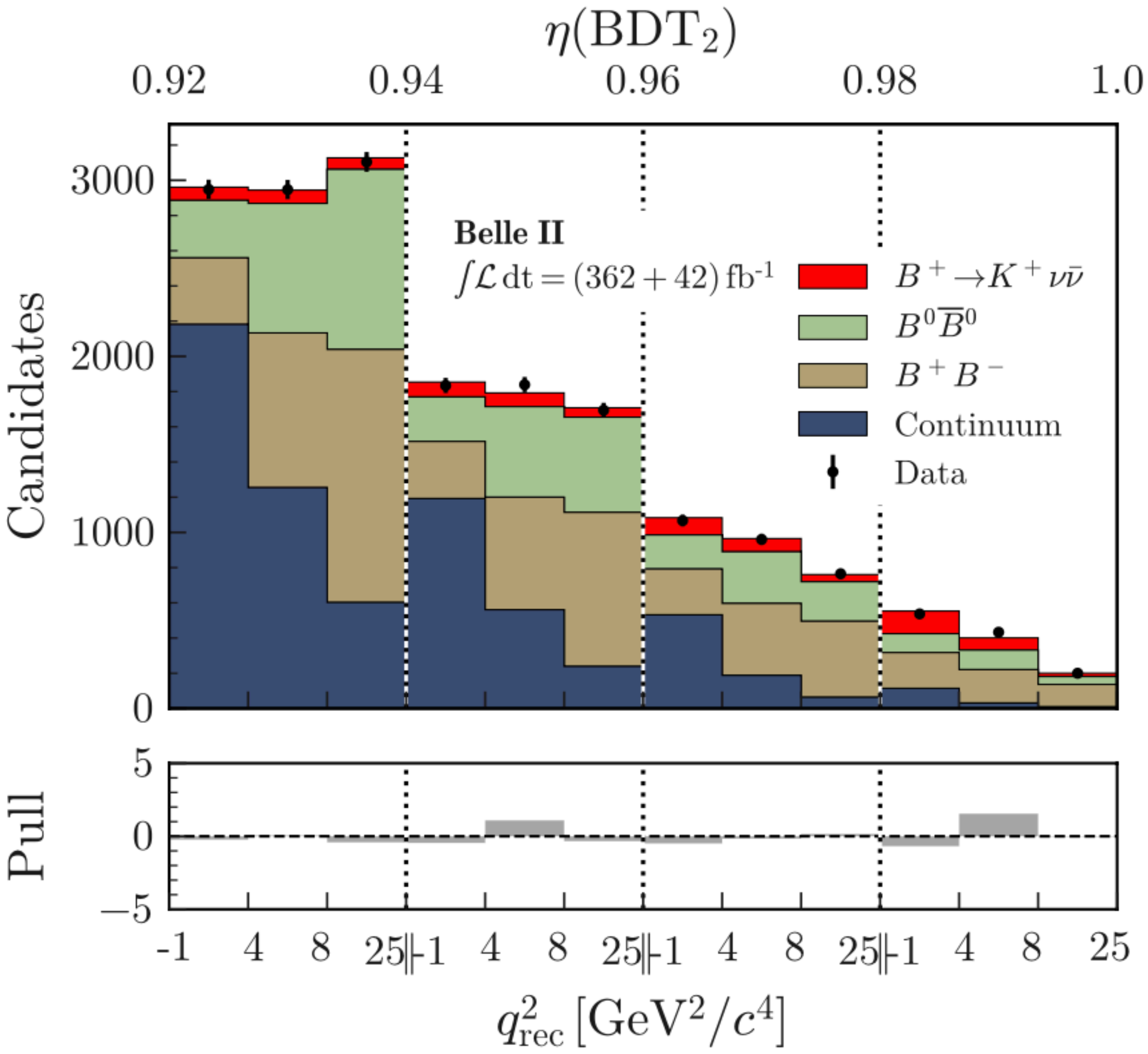
Test passed ✓



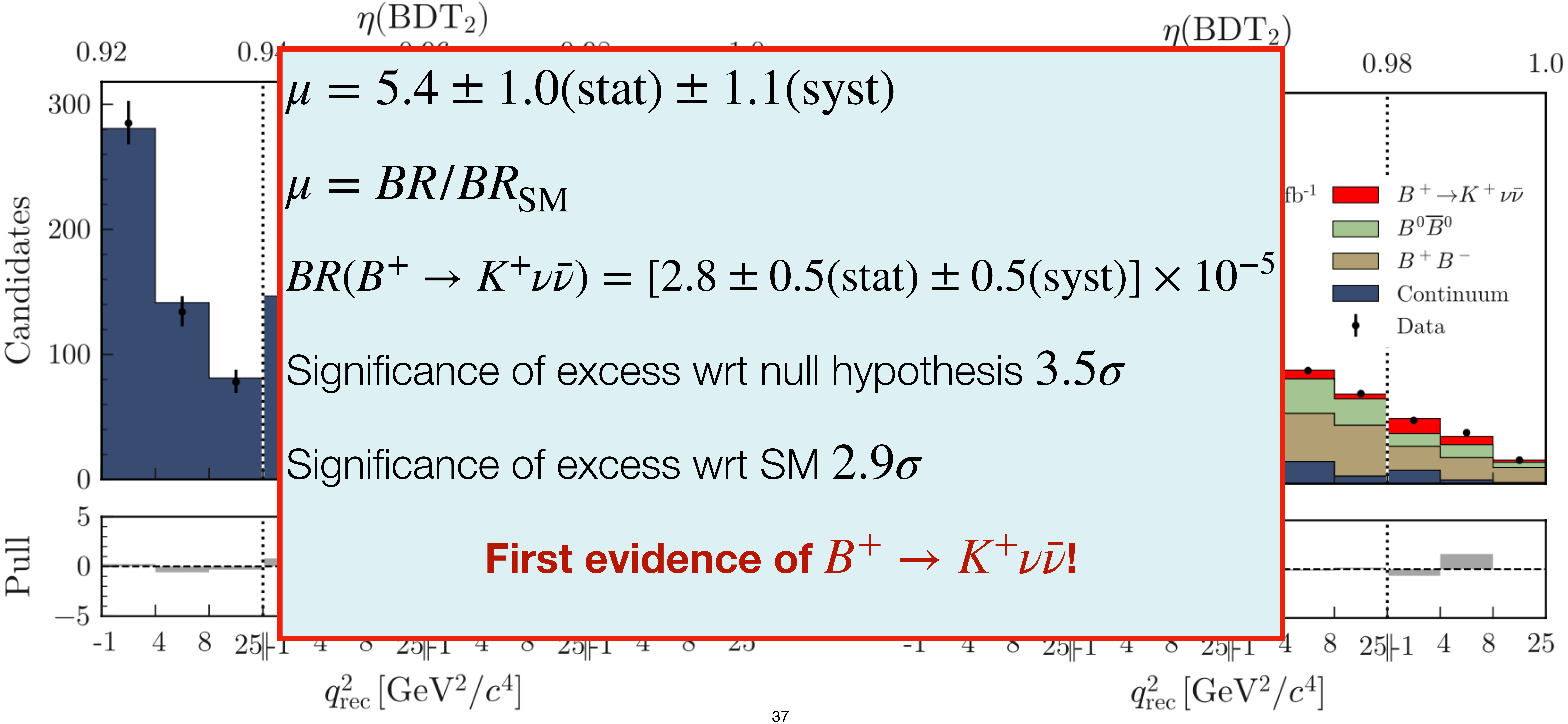
Results

Inclusive tag results





Inclusive tag results



$\mu = 5.4 \pm 1.0(\text{stat}) \pm 1.1(\text{syst})$

$\mu = BR/BR_{\text{SM}}$

$BR(B^+ \to K^+\nu\bar{\nu}) = [2.8 \pm 0.5(\text{stat}) \pm 0.5(\text{syst})] \times 10^{-5}$

Significance of excess wrt null hypothesis 3.5σ

Significance of excess wrt SM 2.9σ

First evidence of $B^+ \to K^+\nu\bar{\nu}$!

Hadronic tag results

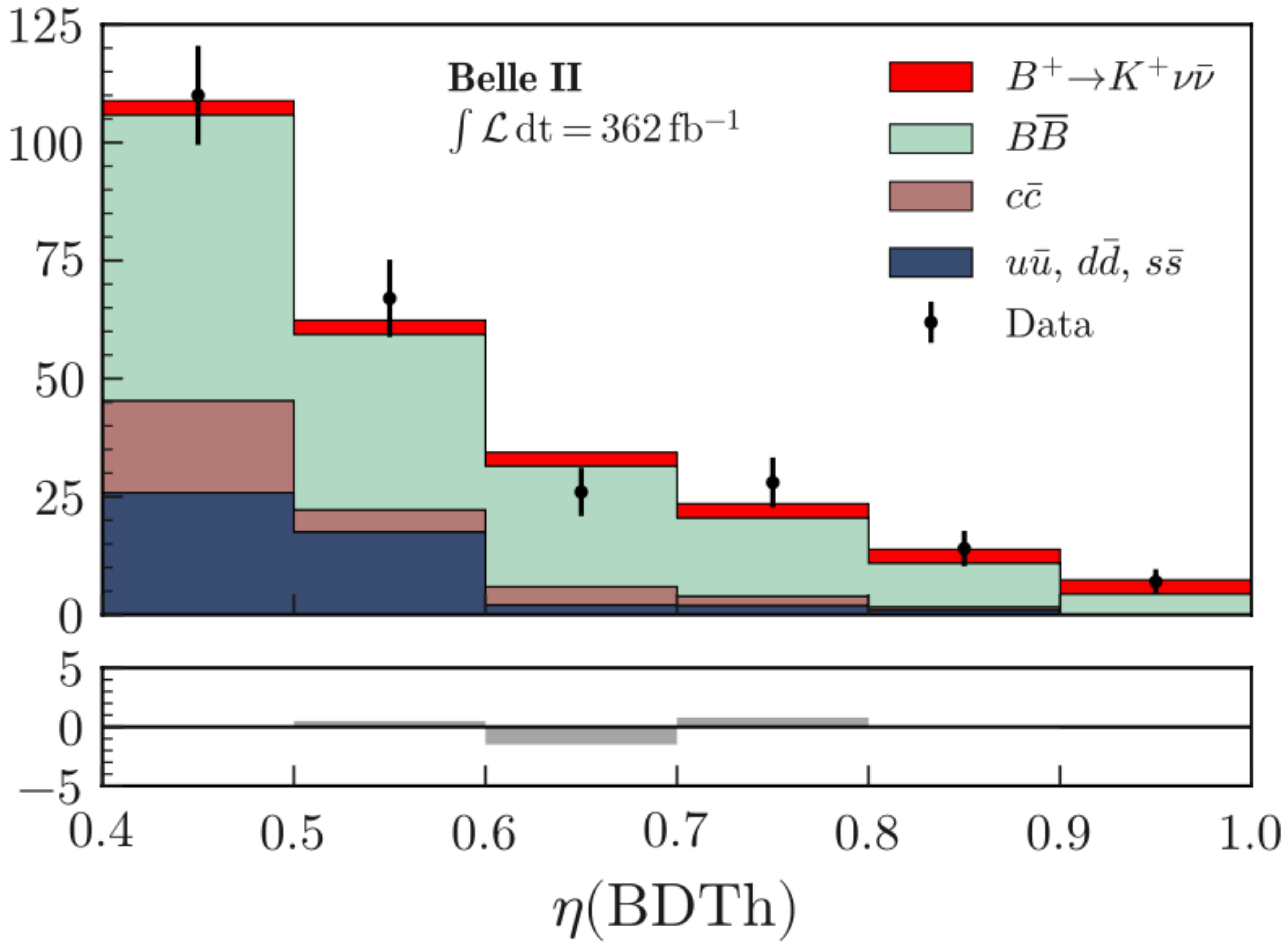
$\mu = 2.2^{+1.8}_{-1.7}(\text{stat})^{+1.6}_{-1.1}(\text{syst})$

$\mu = BR/BR_{\text{SM}}$

$BR(B^+ \to K^+\nu\bar{\nu}) = [1.1^{+0.9}_{-0.8}(\text{stat})^{+0.8}_{-0.5}(\text{syst})] \times 10^{-5}$

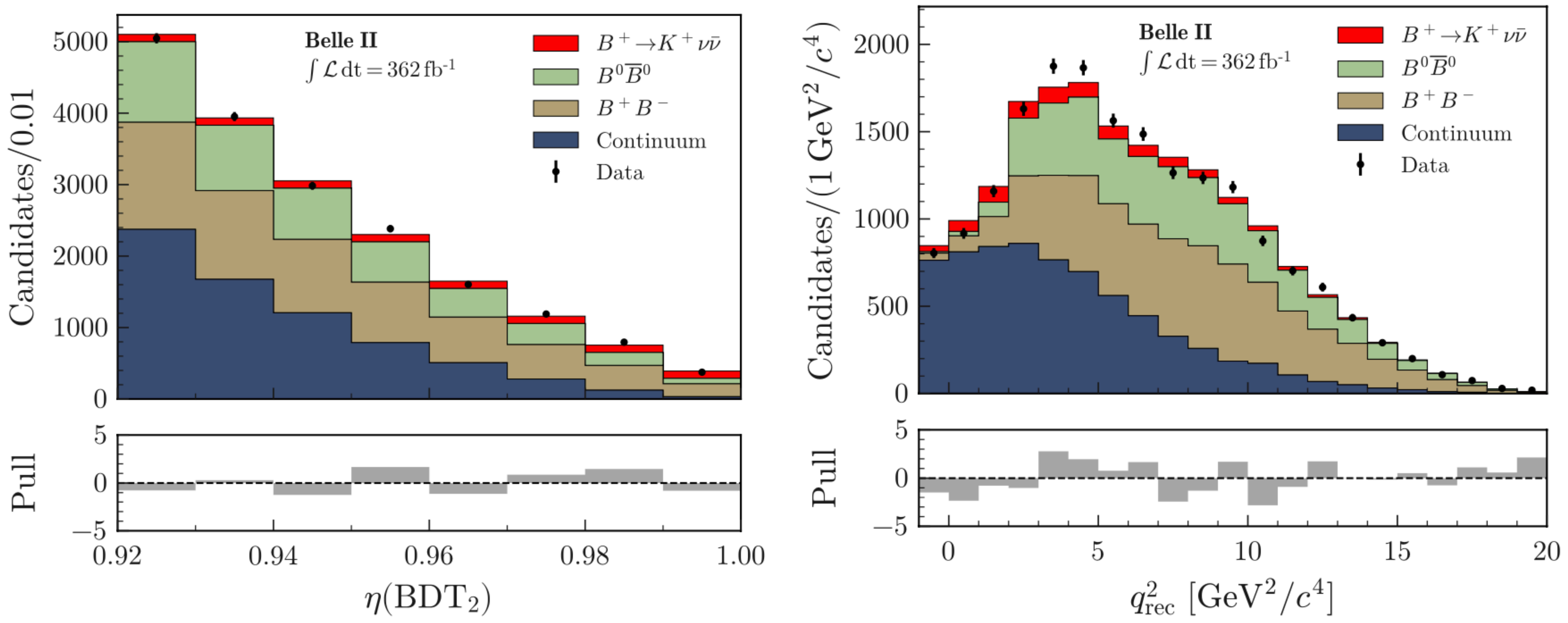
Significance wrt null hypothesis 1.1σ

Significance wrt SM 0.6σ

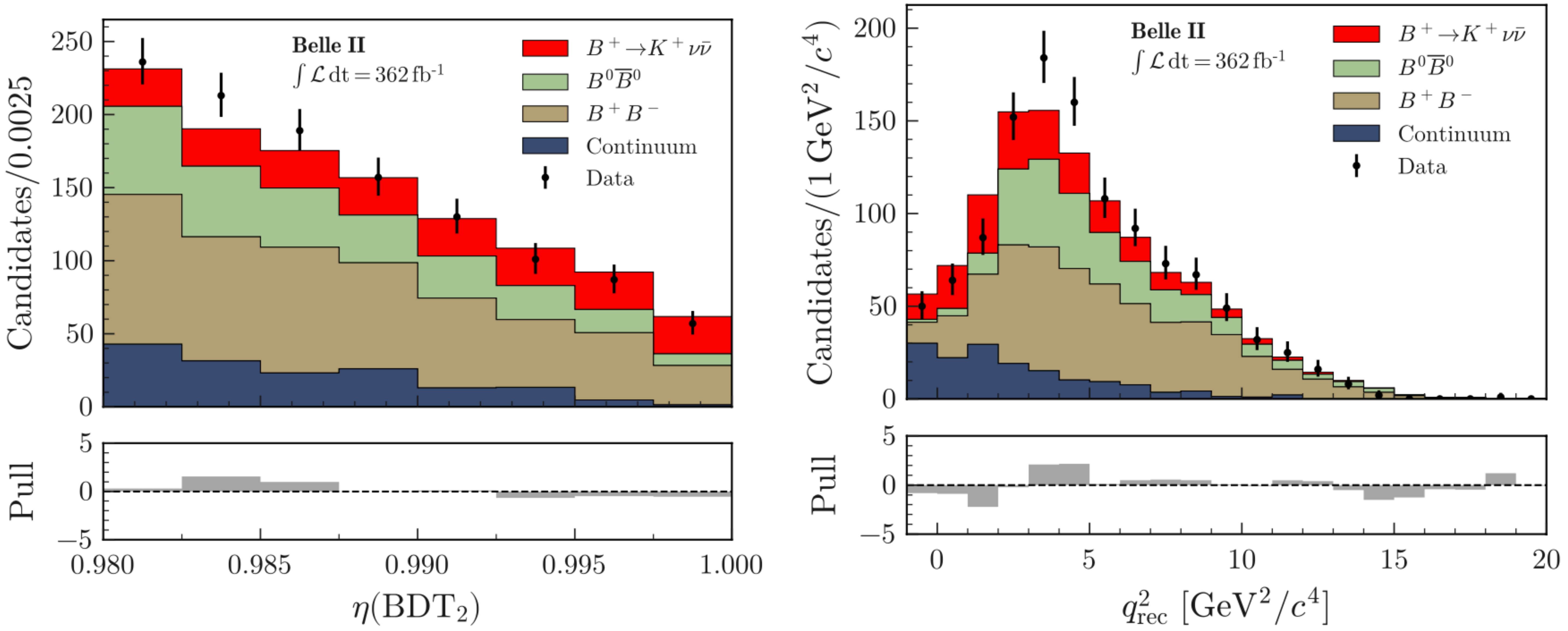


Inclusive tag post-fit distributions

Full signal region:

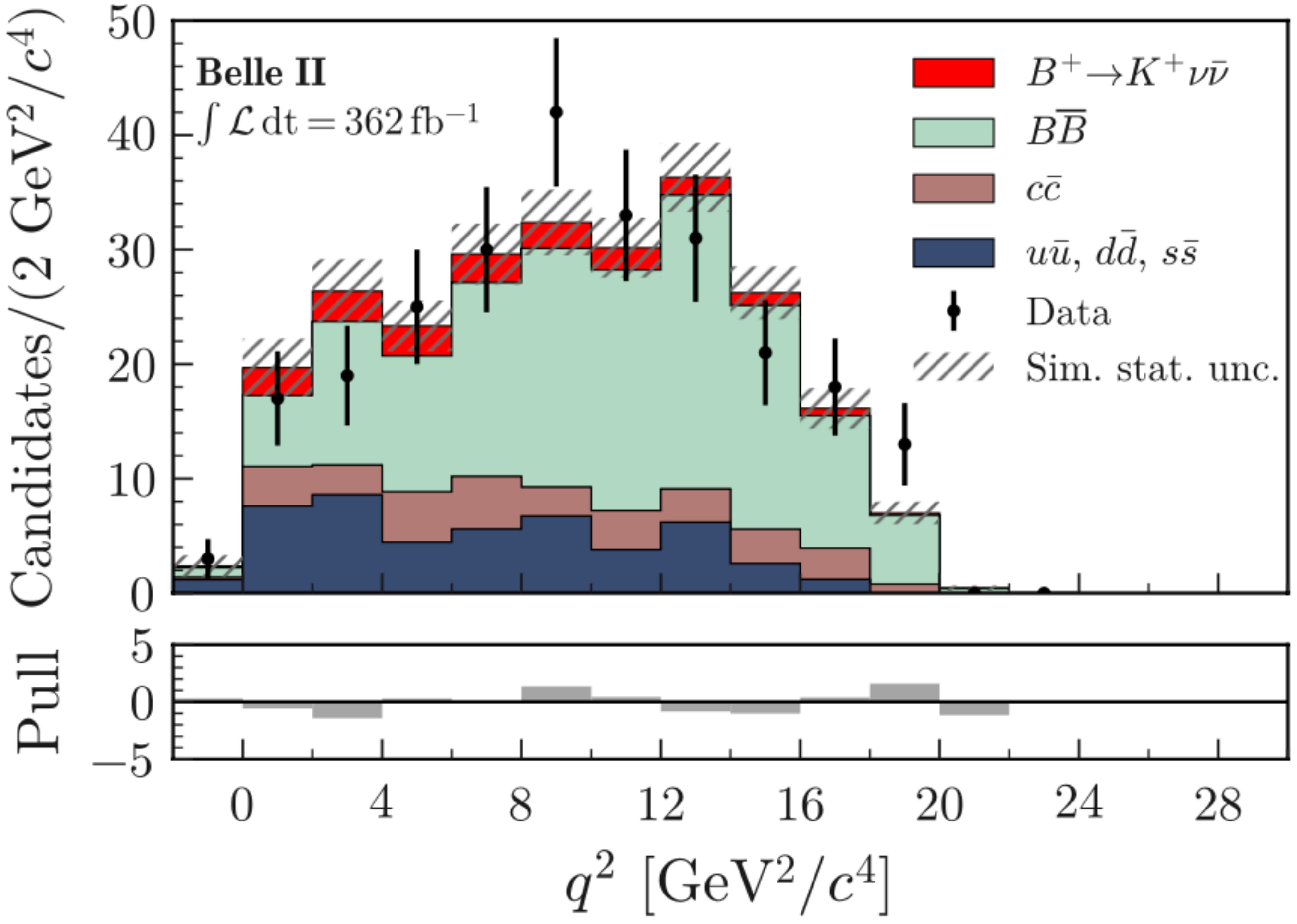


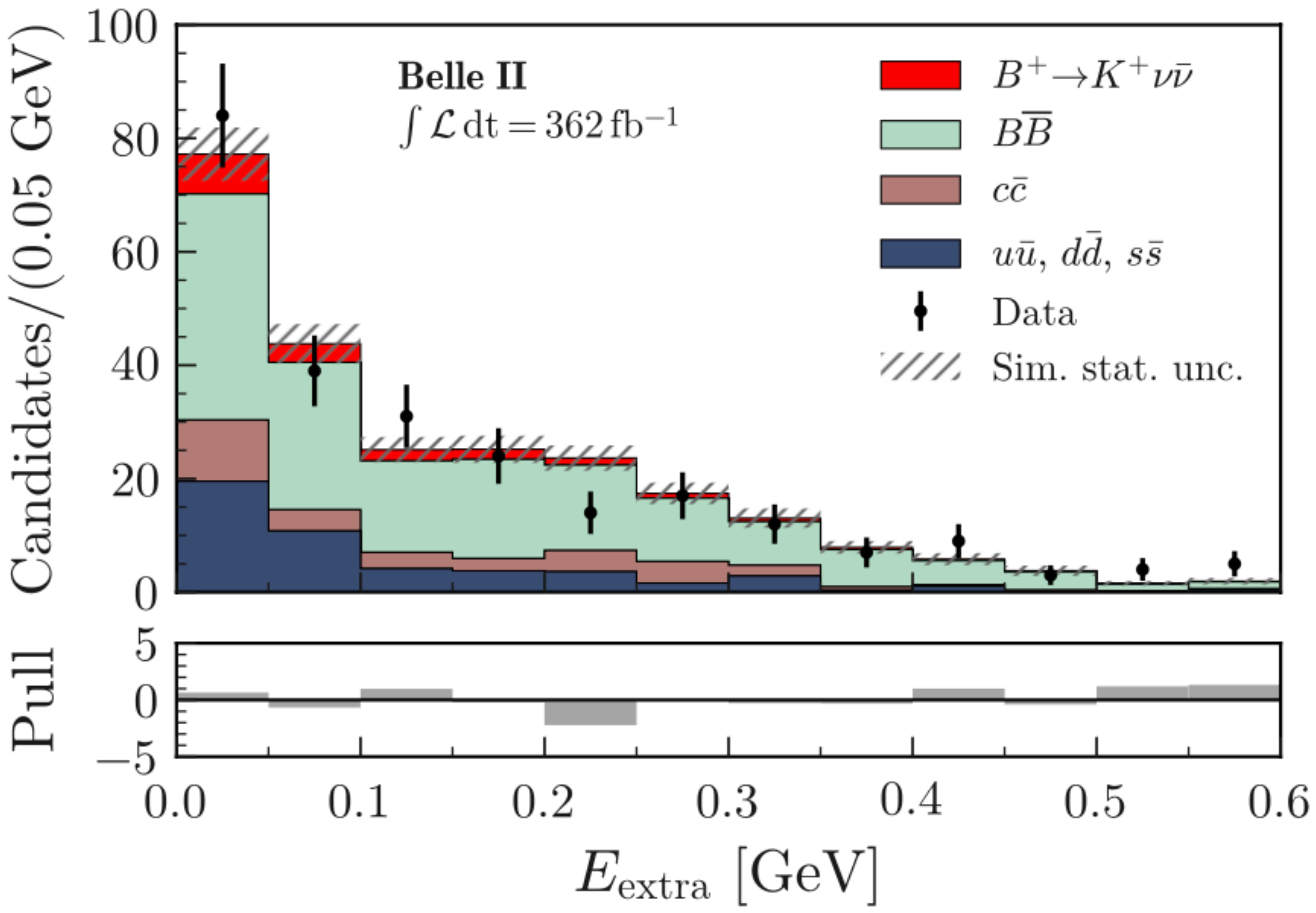
Most sensitive $\eta(\mathrm{BDT}_2)$ bin:



Hadronic tag post-fit distributions

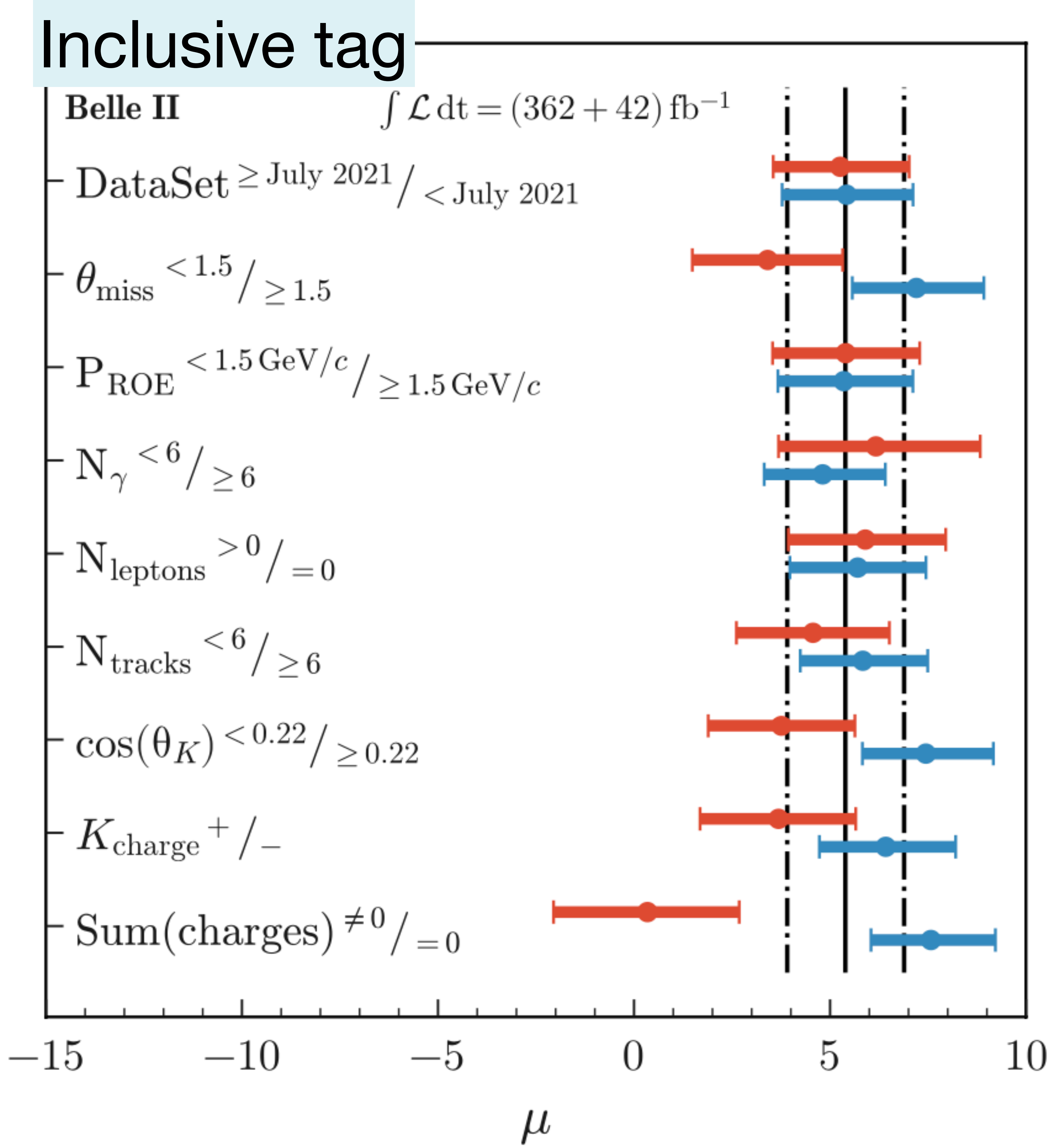
Full signal region:

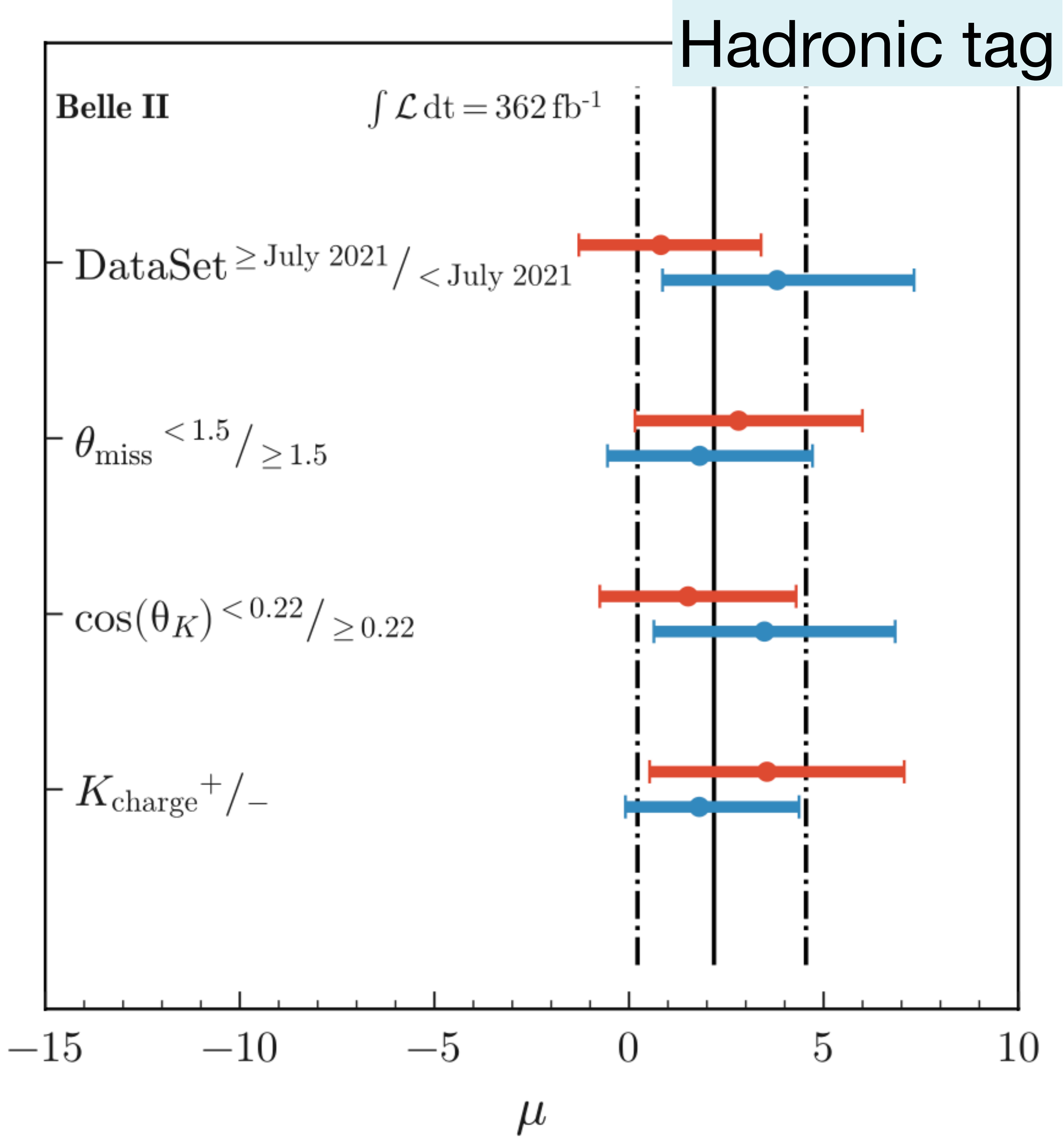




Stability checks

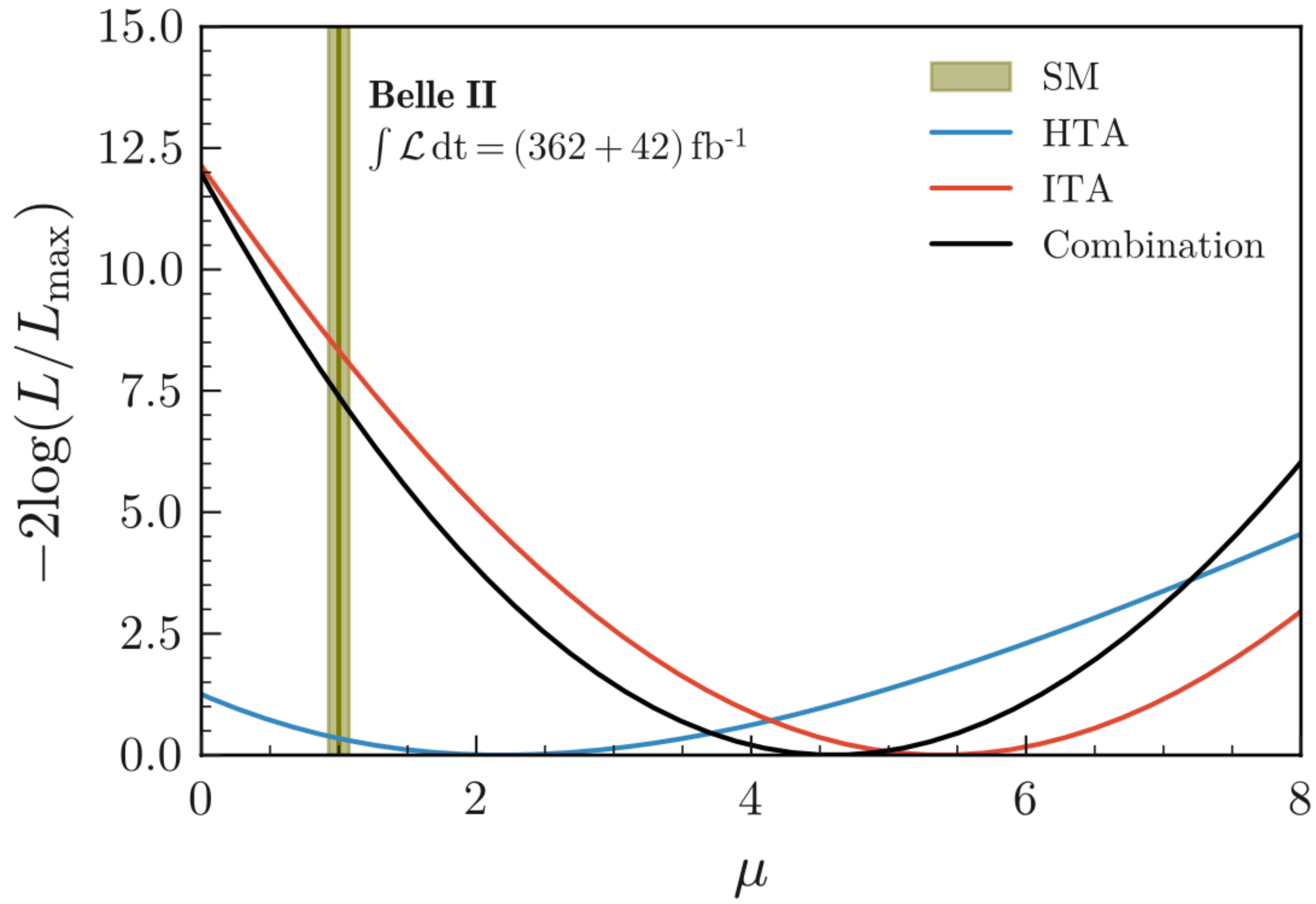
Split the sample into pairs of statistically independent datasets





Combination

- Consistency between two methods
- Events from hadronic tag represent only 2% of events in the inclusive tag signal region
- For the combination, correlations among common systematic uncertainties included and common data events excluded from the inclusive tag sample



Combination

- Consistency bet
- Events from had events in the incl
- For the combina common system and common da inclusive tag sam

$$\mu = 4.6 \pm 1.0(\text{stat}) \pm 0.9(\text{syst})$$

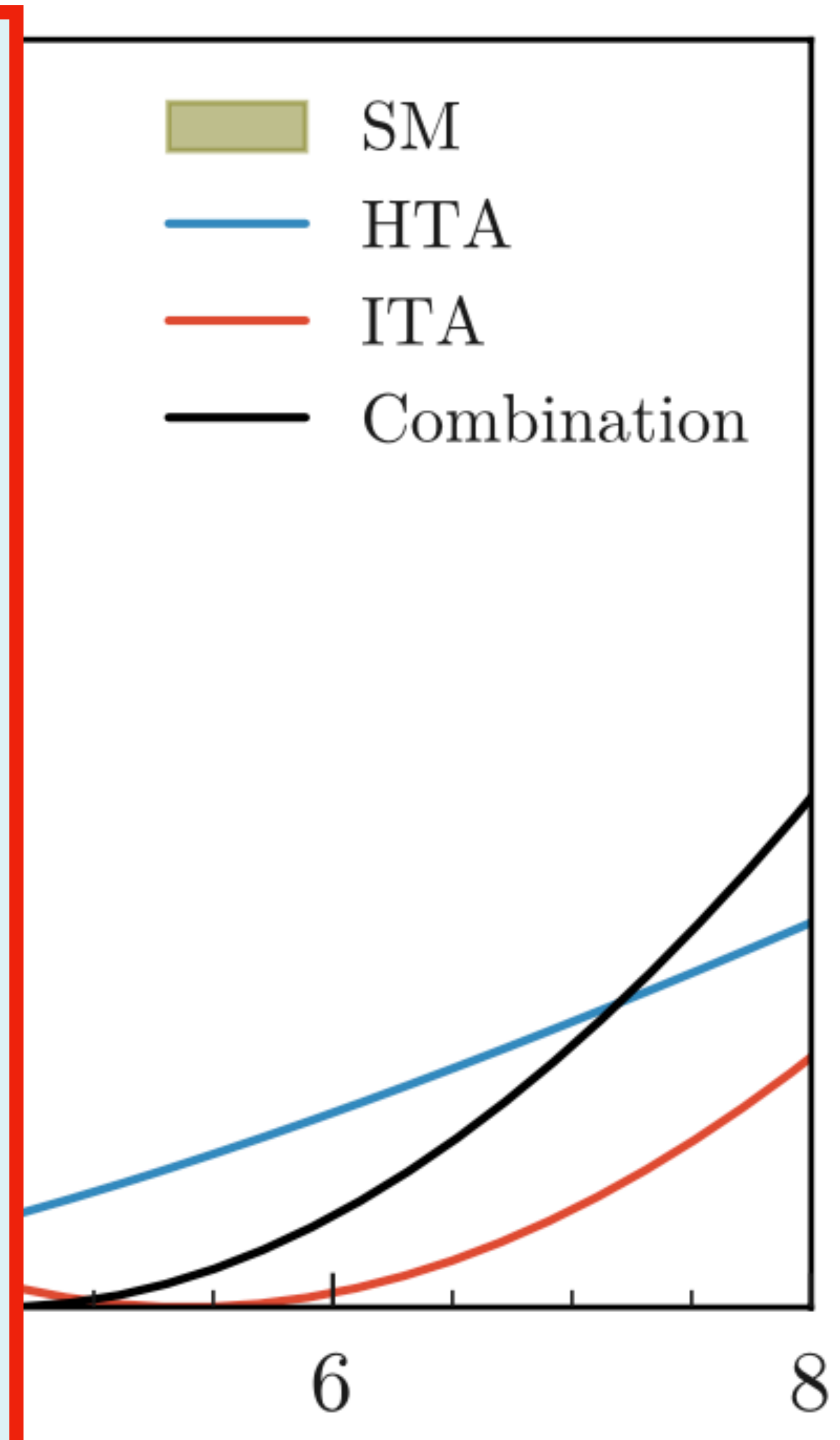
$$\mu = BR/BR_{\text{SM}}$$

$$BR(B^+ \to K^+\nu\bar{\nu}) = [2.3 \pm 0.5(\text{stat})^{+0.5}_{-0.4}(\text{syst})] \times 10^{-5}$$

Significance of excess wrt null hypothesis 3.5σ

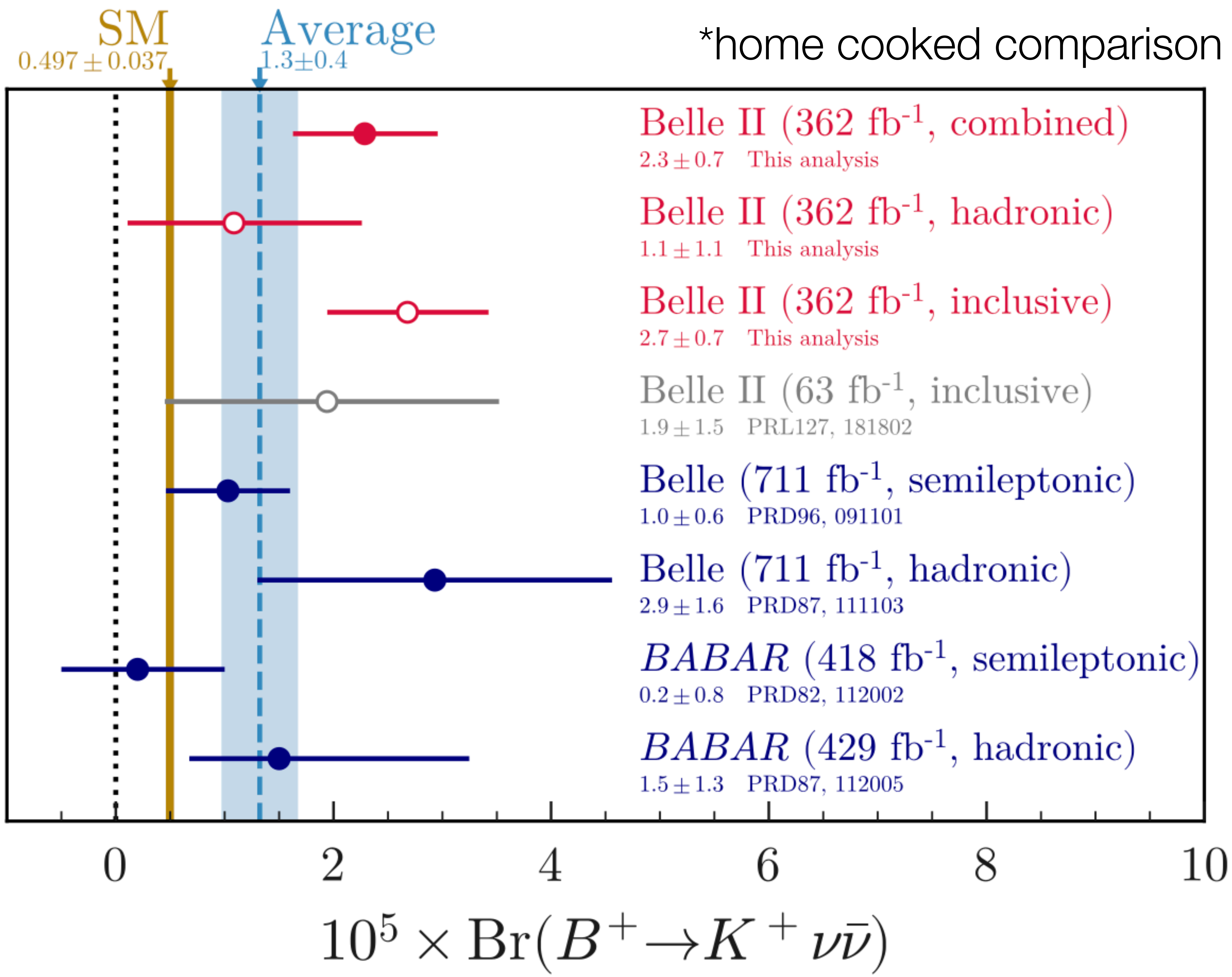
Significance of excess wrt SM 2.7σ

First evidence of $B^+ \to K^+\nu\bar{\nu}$!



Current experimental status

*home cooked comparison



Summary

- Belle II @ SuperKEKB offers unique experimental environment to probe new physics in an indirect way
- About 500 fb^{-1} collected at $\Upsilon(4S)$ which corresponds to ~500M $B\bar{B}$ pairs
- A small fraction of results obtained with Run 1 dataset is shown today
  - World-leading results even with smaller dataset than expected
  - Unique for Belle II measurements
  - **First evidence of $B^+ \to K^+\nu\bar{\nu}$ decay**

Back up

SELECTION: INCLUSIVE TAG

Tracks

- $4 \leq N_{tracks} \leq 10$
- $|dr| < 0.5$ cm, $|dz| < 3$ cm
- $p_T > 0.1$ GeV/c, $E < 5.5$ GeV

K^+: $N_{PXDHits} > 0$, $\theta \in$ CDC, $N_{CDCHits} > 20$, kaonID > 0.9

ROE:

- K^0_S: 'merged' + $0.495 < m(\pi^+\pi^-) < 0.500$ GeV/c^2 + $\cos\theta(p, v) > 0.98$ + flightTime > 0.007 ns + kFit > 0.001
- γ: $0.1 < E < 5.5$ GeV, $\theta \in$ CDC

$0.3 < \theta(p_{miss}) < 2.8$, $E_{visible} > 4$ GeV

One B candidate per event with lowest $q^2_{\mathrm{rec}} = s/4 + M_K^2 - \sqrt{s}E_K^*$.

SELECTION: HADRONIC TAG (I)

- **Hadronic FEI skim requirements:**
  - At least 3 tracks with |dz| < 2cm, dr < 0.5cm and p_t > 0.1 GeV/c
  - At least 3 ECL clusters with E < 0.1 GeV and 0.297 < θ < 2.62
  - E_{vis} > 4 GeV
  - B_{tag} M_{bc} > 5.20 GeV/c^2
  - |B_{tag} Δ_E|< 0.3 GeV
  - B_{tag} FEI probability > 0.001

- **Event requirements:**
  - Less than 12 tracks with dr < 2cm, |dz| < 4cm

SELECTION: HADRONIC TAG (II)

- **K^+ signal candidates requirements:**
  - $|dz| < 2$cm and $dr < 0.5$cm
  - Track in CDC acceptance ($17° < \theta < 170°$)
  - nCDCHits > 20
  - nPXDHits > 0
  - KaonID > 0.9

- $B^+ \to K^+$**$\nu\nu$** reconstructed from signal K^+ candidate

- Require right B_{sig}-B_{tag} charge conjugation

- Additional requirement on tag-side applied at this stage: B_{tag} $M_{bc} > 5.27$ GeV/c^2

- Requirements for missing energy: **$0.3 < \theta_{miss} < 2$**
  - Sum of missing energy and momentum → input of final BDT

SELECTION: HADRONIC TAG (III)

- ROEh: deposits not associated with B_{tag} nor B_{sig} (empty for signal events)
- Reconstructed in ROEh:
  - π^0 from eff20_May2020
  - K_S^0 from stdKshorts
  - Λ from stdLambads
- **Multiplicity of all of the above requested to be 0**

- Require **0 "good tracks" in rest of event of B_{sig}-B_{tag} system** (good track: dr < 2cm, |dz| < 4cm in CDC acceptance, nCDC hits > 20)
  - Tracks in ROEh not passing "good track" selection → input of final BDT

- Neutral Extra ECL clusters → input of final BDT
  - dedicated extra photon cleaning (next slides)

- Photons in ROEh:
  - E > (100, 60, 150) MeV for photons in (FWD, Barrel, BWD)
  - Acceptance within CDC
  - Minimum distance-to-the-closest-track > 50 cm

MVA CLASSIFIERS: INCLUSIVE TAG

First, train BDT_1 using 12 discriminating variables. Then, restrict sample to high BDT_1 values and train BDT_2 using 35 discriminating variables.

Parameter	Value
Number of trees	2000
Tree depth	2/3 ($BDT_{1/2}$)
Shrinkage	0.2
Sampling rate	0.5
Number of equal-frequency bins	256

Variables related to the D^0/D^+ suppression

D^0 candidates are obtained by fitting the kaon candidate track and each track of opposite charge in the ROE to a common vertex; D^+ candidates are obtained by fitting the kaon candidate track and two ROE tracks of appropriate charges. In both cases, the best candidate is the one having the best vertex fit quality.

- Radial distance between the best D^+ candidate vertex and the IP (BDT_2)
- χ^2 of the best D^0 candidate vertex fit and the best D^+ candidate vertex fit (BDT_2)
- Mass of the best D^0 candidate (BDT_2)
- Median p-value of the vertex fits of the D^0 candidates (BDT_2)

Variables related to the entire event

- Number of charged lepton candidates ($e^\pm$ or $\mu^\pm$) (BDT_2)
- Number of photon candidates, number of charged particle candidates (BDT_2)
- Square of the total charge of tracks in the event (BDT_2)
- Cosine of the polar angle of the thrust axis in the c.m. (BDT_1, BDT_2)
- Harmonic moments with respect to the thrust axis in the c.m. [44] (BDT_1, BDT_2)
- Modified Fox-Wolfram moments calculated in the c.m. [45] (BDT_1, BDT_2)
- Polar angle of the missing three-momentum in the c.m. (BDT_2)
- Square of the missing invariant mass (BDT_2)
- Event sphericity in the c.m. [43] (BDT_2)
- Normalized Fox-Wolfram moments in the c.m. [44] (BDT_1, BDT_2)
- Cosine of the angle between the momentum line of the signal kaon track and the ROE thrust axis in the c.m. (BDT_1, BDT_2)
- Radial and longitudinal distance between the POCA of the K^+ candidate track and the tag vertex (BDT_2)

Variables related to the tracks and energy deposits of the rest of the event (ROE)

- Two variables corresponding to the x, z components of the vector from the average interaction point to the ROE vertex (BDT_2)
- p-value of the ROE vertex fit (BDT_2)
- Variance of the transverse momentum of the ROE tracks (BDT_2)
- Polar angle of the ROE momentum (BDT_1, BDT_2)
- Magnitude of the ROE momentum (BDT_1, BDT_2)
- ROE-ROE (oo) modified Fox-Wolfram moment calculated in the c.m. (BDT_1, BDT_2)
- Difference between the ROE energy in the c.m. and the energy of one beam of c.m. ($\sqrt{s}/2$) (BDT_1, BDT_2)

Variables related to the kaon candidate

- Radial distance between the POCA of the K^+ candidate track and the IP (BDT_2)
- Cosine of the angle between the momentum line of the signal kaon candidate and the z axis (BDT_2)

MVA CLASSIFIERS: HADRONIC TAG

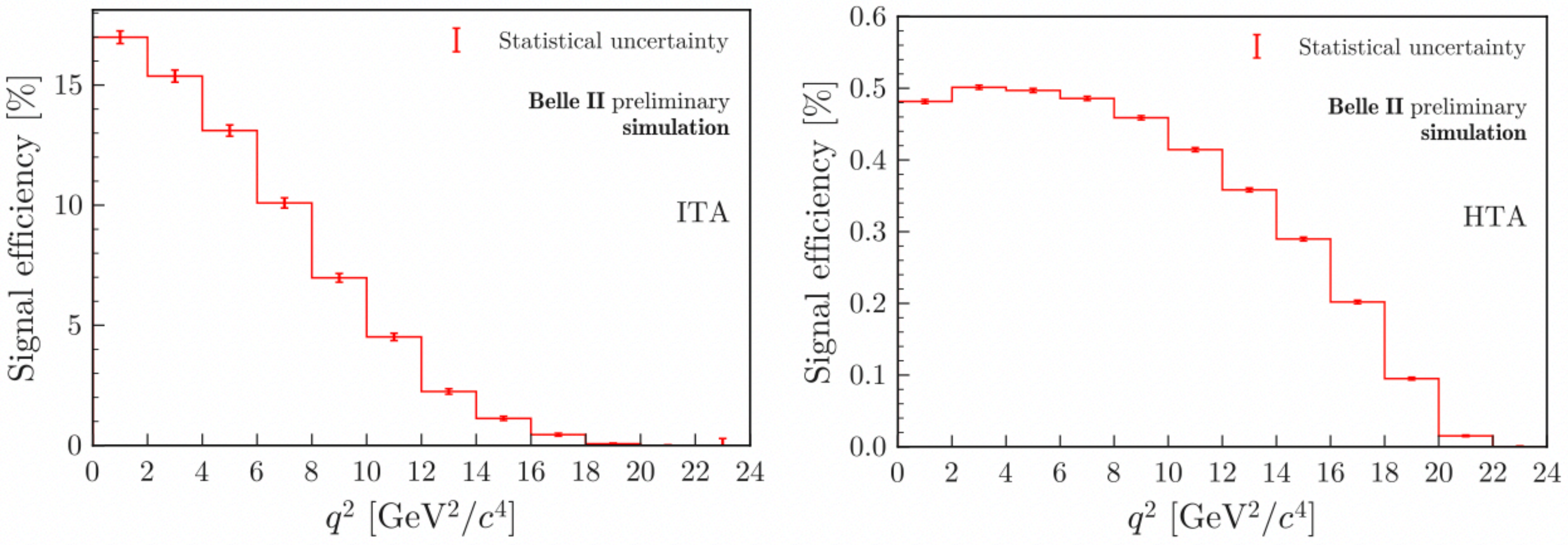
Train single BDT using 12 variables

Parameter	Value
Number of trees	1300
Tree depth	3
Shrinkage	0.03
Sampling rate	0.8
Number of equal-frequency bins	256

- Sum of photon energy deposits in ECL in ROEh
- Number of tracks in ROEh
- Sum of the missing energy and absolute missing three-momentum vector
- Azimuthal angle between the signal kaon and the missing momentum vector
- Cosine of the angle between the thrust axis of the signal kaon candidate and the thrust axis of the ROEh
- Kakuno-Super-Fox-Wolfram moments H_{22}^{so}, H_{02}^{so}, H_0^{oo}
- Invariant mass of the tracks and energy deposits in ECL in the recoil of the signal kaon
- p-value of B_{tag}
- p-value of the vertex fit of the signal kaon and one or two tracks in the event to reject fake kaons coming from D^0 or D^+ decays

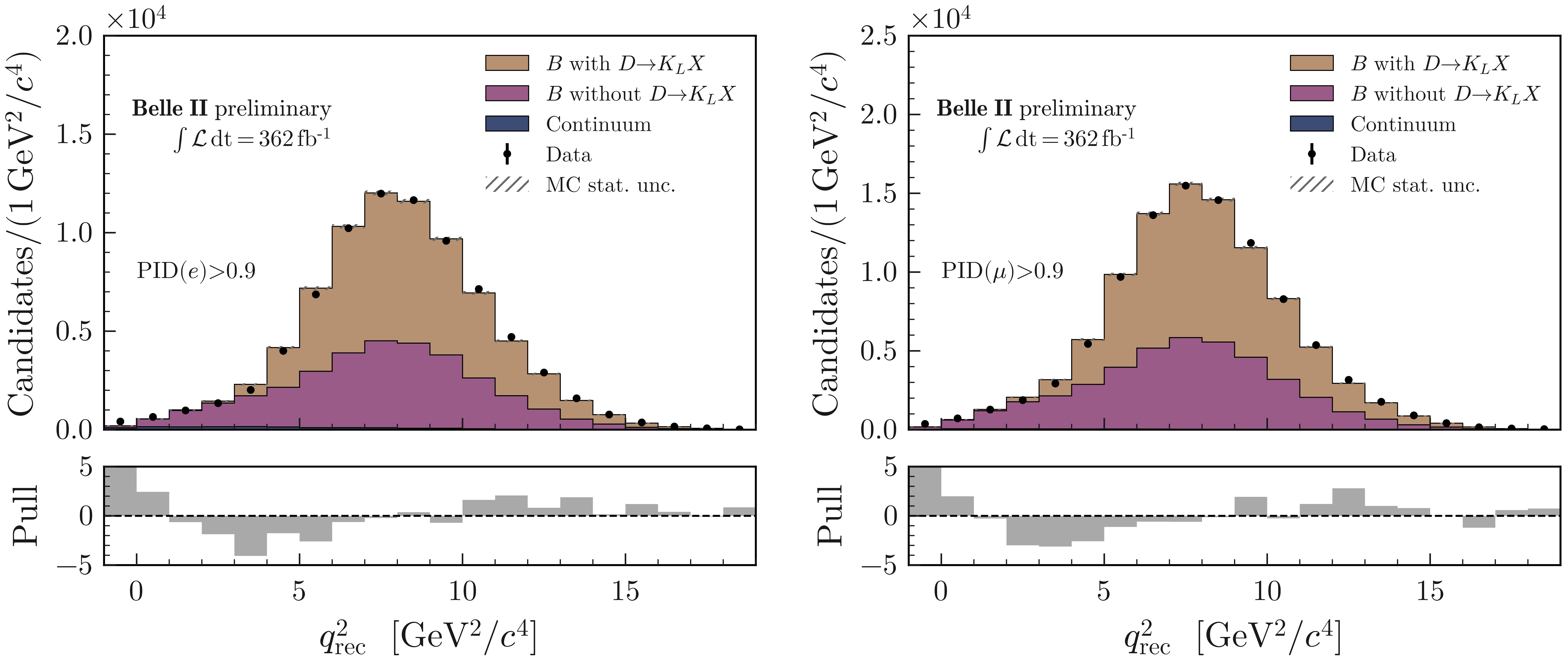
EFFICIENCIES

Inspect signal efficiencies as a function of true generated q^2



LEPTON SIDEBANDS

Inclusive-tag analysis with lepton-enriched selection.



$B^+ \to K^+ n\bar{n}$ MODELING

$B^+ \to K^+ n\bar{n}$ can mimic our signal.

https://arxiv.org/pdf/0707.1648.pdf shows an enhancement close to the $p\bar{p}$ production threshold in $B^0 \to K^0 p\bar{p}$.

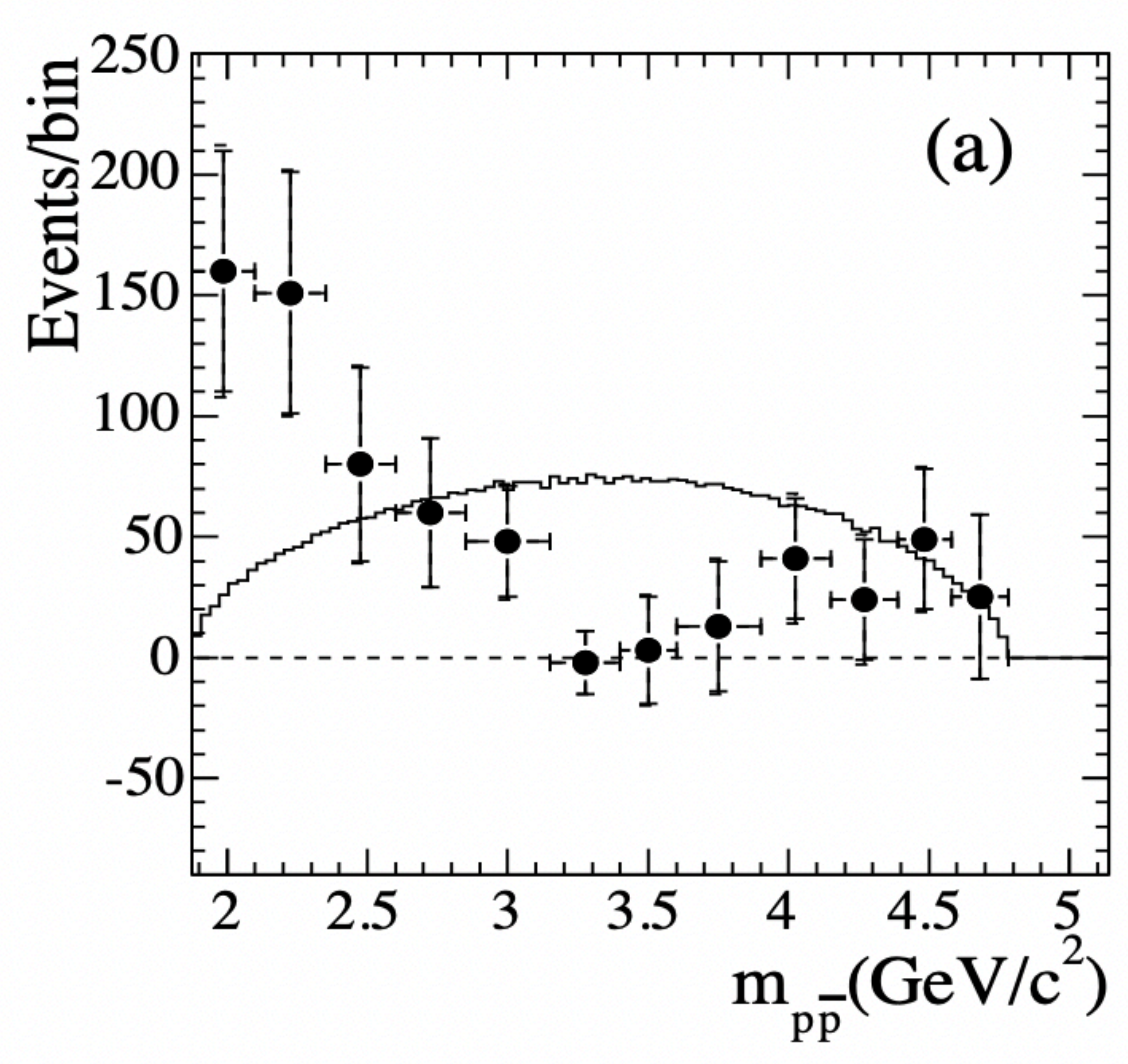
=> Reweight phase space m_{nnbar} to include the enhancement

=> Use BF of proper isospin partner $B^0 \to K^0 p\bar{p}$ scaled by τ_{B^+}/τ_{B^0}

Br = 2.9×10^{-6}

Keep 100% systematic due to

- isospin violation effects
- uncertainties in m_{ppbar} shape
- presence of additional unmeasured baryonic states
- modeling of $n/\bar{n}$ in ECL



VALIDATING $B^+ \to K^+ K^0_L K^0_S$ MODEL

The decay has not been measured

- $K_L K_S$ pair is in CP-odd state: assume that $B^+ \to K^+ K_L K_S$ decay has a rate as a p-wave component of the isospin partner $B^0 \to K_S K^+ K^-$
- Use the same BaBar analysis as for $B^+ \to K^+ K_S K_S$, estimate the rate as a sum of $B^+ \to K^+ \varphi(\to K_L K_S)$ and p-wave non-resonant contribution
- Validate using Belle II data; model s-wave component using Belle II data for $B^+ \to K^+ K_S K_S$