

# Search for the critical point in NA61/SHINE

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for NA61/SHINE collaboration

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# Outline

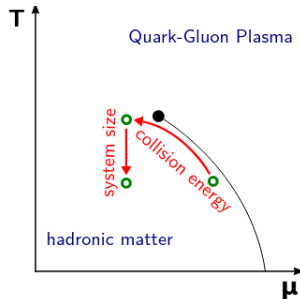
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1. The search for the critical point
2. Multiplicity fluctuations and Net-electric charge fluctuations
3. Femtoscopy (HBT correlations)
4. Intermittency analysis of scaled factorial moments

The search for the critical point

# The search for the Critical Point

- Critical Point (CP): Hypothetical endpoint of the first-order QGP-HM transition, with second-order phase properties.
- What to expect?: 2nd Order Transition  $\rightarrow$  Scale-invariance  $\rightarrow$  power-law form correlation function
- These expectations are for fluctuations and correlations in the configuration space, which are expected to be projected to the momentum space via quantum statistics and/or collective flow.



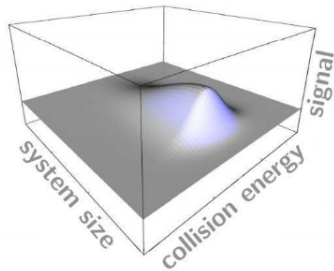
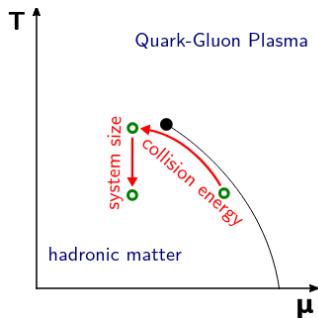
## Who is looking for it?

- *Present*
  - NA61/SHINE at CERN
  - STAR Collaboration at RHIC
- *Future*
  - CBM at FAIR
  - MPD at NICA

Asakawa, Yazaki NPA 504 (1989) 668  
Barducci, Casalbuoni, De Curtis, Gatto, Pettini,  
PLB 231 (1989) 463  
Stephanov, PoS LAT2006 (2006) 024

# The search for the Critical Point

The experimental search for the critical point requires a two-dimensional scan of collision energy and the size of the colliding nuclei (centrality).



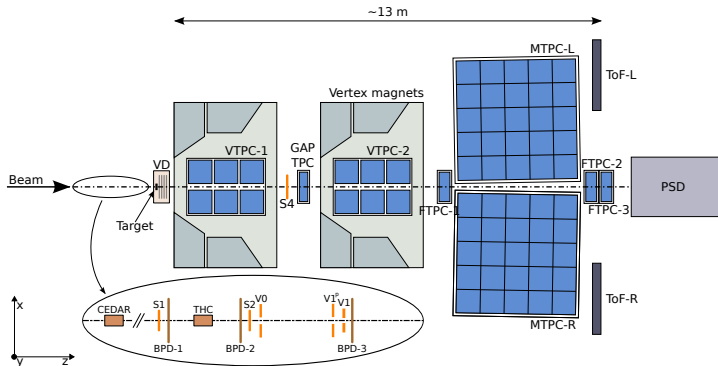
**What do we do to search for the critical point?** We perform a scan of the parameters controlled in the laboratory (collision energy and nuclear mass number, centrality). The idea is that by changing them, we change the freeze-out conditions ( $T, \mu_B$ ).

# The NA61/SHINE experiment

→ Multipurpose fixed target spectrometer with unique capabilities

coverage up to 50%  
of produced charged  
particles starting  
from  $p_T \approx 0$

- Strangeness in quark matter:  
 $K^+$ ,  $K^-$ ,  $K_S^0$ ,  $K^*$ ,  $\Lambda$ ,  $\phi$
- Heavy quarks:  
 $D^0$  and  $\bar{D}^0$
- Correlations, fluctuations, HBT, intermittency...



$$p_{\text{beam}} = 13A - 150A \text{ GeV}/c \Rightarrow \sqrt{s_{NN}} \approx 5 - 17 \text{ GeV}$$

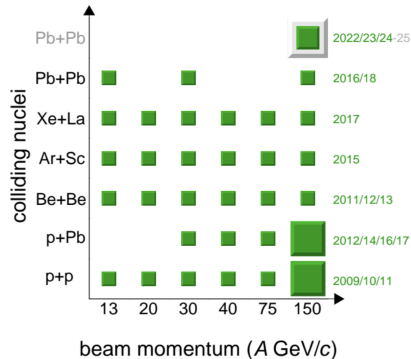
# The physics program

## Strong interactions physics:

- Study the onset of deconfinement
- Search for the **critical point**
- Measurement of open charm

## Neutrino and cosmic-ray physics

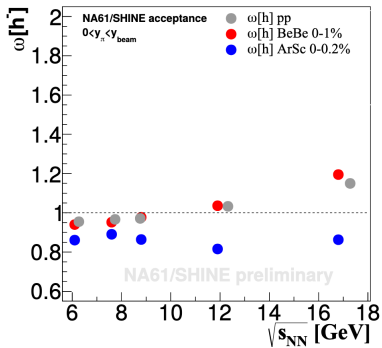
- measurements for **neutrino programs** at J-PARC and Fermilab
- measurements of **nuclear fragmentation** cross-section for cosmic rays physics



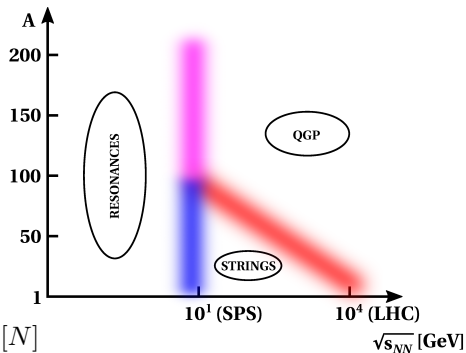
# Multiplicity fluctuations and Net-electric charge fluctuations



# Multiplicity fluctuations



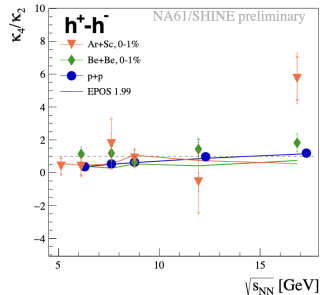
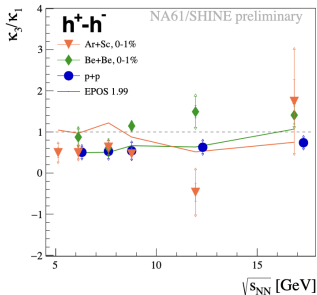
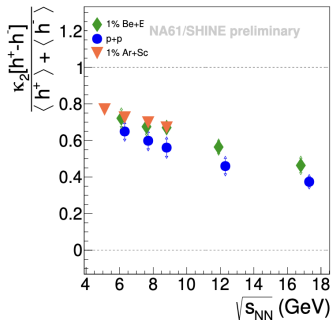
$$\omega[N] = \frac{\text{Var}[N]}{\langle N \rangle}$$



Be+Be similar to p+p, Ar+Sc different  $\rightarrow$  onset of fireball ?

No collision energy dependence has been observed in Ar+Sc data that could be related to the critical point

# Net-electric charge fluctuations



$$\kappa_1 = \langle N \rangle$$

$$\kappa_2 = \langle (\delta N)^2 \rangle$$

$$\kappa_3 = \langle (\delta N)^3 \rangle$$

$$\kappa_4 = \langle (\delta N)^4 \rangle$$

$$\langle N_2 \rangle \sim \xi^2$$

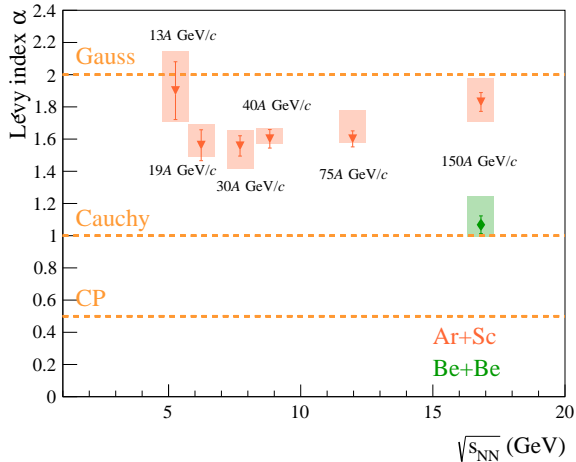
$$\langle N_4 \rangle \sim \xi^7$$

NA61/SHINE,  
PoS(PANIC2021)238  
NA61/SHINE,  
Status Report 2022

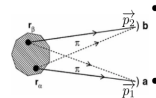
**No significant non-monotonic signal  
observed**

## Femtoscscopy (HBT correlations)

# Bose-Einstein (HBT) correlations (femtoscscopy)



- Femtoscopy reveals the space-time structure of hadron production
- The **Levy parameter**  $\alpha$  describes the shape of the source and is sensitive to the system freezing out at the CP
- The new Ar+Sc results are close to Gaussian and far from the CP



Levy-shaped source (1-D):

$$C(q) \cong 1 + \lambda \cdot e^{(-qR)^\alpha}$$

where  $q = |\vec{p}_1 - \vec{p}_2|_{LCMS}$ ,  $\lambda$  describes correlation strength,  $R$  determines the length of homogeneity.

[Csörgo, Hegyi, Novak, Zajc, AIP Conf. Proc. 828 (2006) 525]

Ar+Sc, 0-10% central, NA61/SHINE preliminary  
 Be+Be, 0-20% central, NA61/SHINE, EPJC 83 (2023) 919

# Intermittency analysis of scaled factorial moments

# Fluctuations as a function of the momentum bin size

Scaled factorial moments  $F_r(M)$  of the order  $r$

$$F_r(M) = \frac{\left\langle \frac{1}{M} \sum_{i=1}^M N_i \dots (N_i - r + 1) \right\rangle}{\left\langle \frac{1}{M} \sum_{i=1}^M N_i \right\rangle^r}$$

$M$  – sub-division intervals

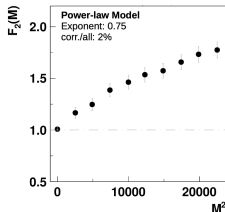
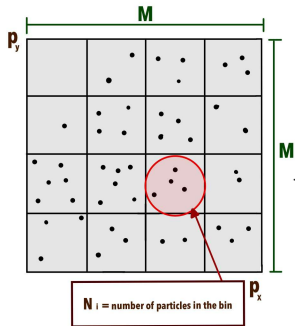
$N_i$  – number of particles in  $i$ -th bin

When the system **freezes out near or at CP**, its properties are expected to be different from an ideal gas

- System represents a simple fractal
- Scaled factorial moments  $F_r(M)$  are expected to follow a **power-law** behaviour

$$F_r(M) \sim (M^2)^{\phi_r}$$

N. Antoniu et al., Phys.Rev.Lett.97 (2006) 032002



Bialas, Peschanski, NPB 273 (1986) 703  
 Wosiek, APPB 19 (1988) 863  
 Asakawa, Yazaki, NPA 504 (1989) 668  
 Barducci et al., PLB 231 (1989) 463  
 Satz, NPB 326 (1989) 613  
 Antoniou et al., PRL 97 (2006) 032002  
 Czopowicz, arxiv:2309.13706

# Current methodologies

$F_r(M)$  depends on the shape of inclusive single particle  $p_T$  distribution. To eliminate this dependence, we have two approaches

## $p_T$ binning

Instead of studying  $F_2(M)$  we study  $\Delta F_2$ . The quantity defined as:<sup>1</sup>

$$\Delta F_2(M) = F_2^{data}(M) - F_2^{mixed}(M)$$

<sup>1</sup>NA49 collaboration. In: Eur. Phys. J. C 75.2 (2015), p. 587m

<sup>2</sup>Bialas; Gazdzicki. In: Physics Letters B 252.3 (1990), pp. 483–486

<sup>3</sup>Antoniou; Diakonou. url: <https://indico.cern.ch/event/818624>

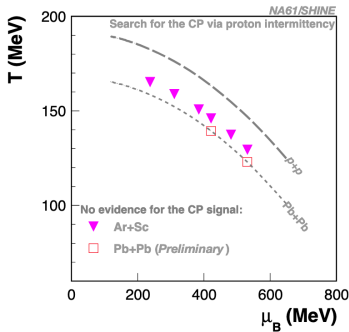
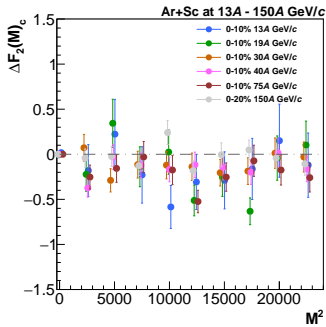
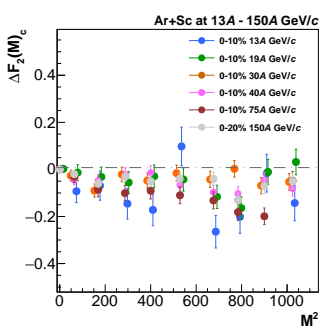
## Cumulative $p_T$ binning

Instead of using  $p_x, p_y$  we use cumulative quantities  $Q_x, Q_y$ :

$$Q_x = \int_{x_{min}}^x \rho(x)dx / \int_{x_{min}}^{x_{max}} \rho(x)dx$$
$$Q_y = \int_{y_{min}}^y P(x, y)dy / P(x)$$

- Transforms any distribution into uniform <sup>2</sup> and removes the dependence of  $F_r$  on the shape of single particle distribution.
- Intermittency index of an ideal power law correlation function remain invariant <sup>3</sup>
- Results are displayed in:
  - $\Delta F_r(M)_c = F_r(M) - F_r(1)$  (where  $F_r(M)$  and  $F_r(1)$  by employing the cumulative  $p_T$  binning.  
 $F_r(1) = F_r(M)$  for uncorrelated particles in  $p_T$ )

# Proton intermittency results for Ar+Sc

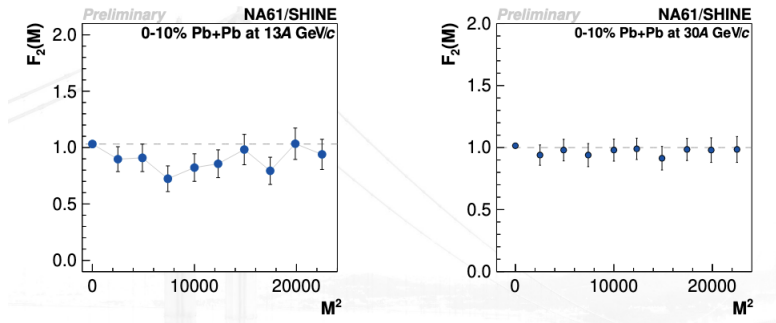


No indication for power-law increase with cumulative  $p_T$  binning

NA61/SHINE, EPJC 83 (2023) 881  
NA61/SHINE, EPJC 84 (2024) 7, 741

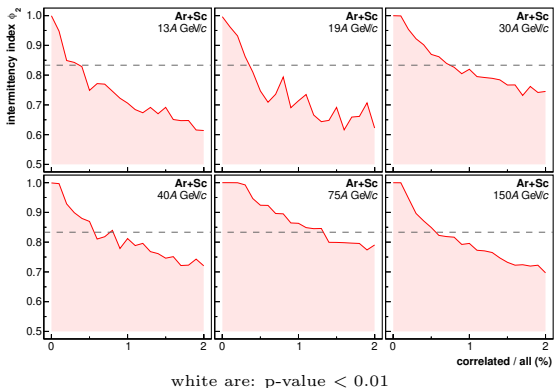


# Proton intermittency results for Pb+Pb



No indication for power-law increase with cumulative  $p_T$  binning

# Exclusion plots

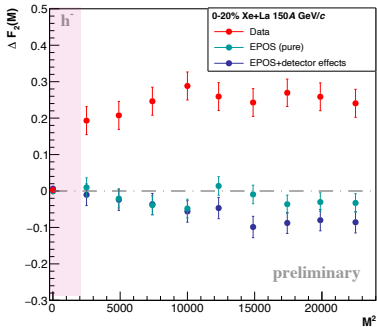


Exclusion plots for parameters of simple power-law model:

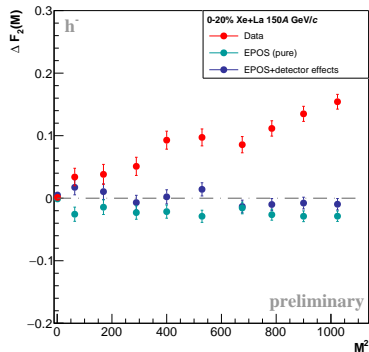
- power-law exponent  $\phi$  in  $|\Delta\vec{p}_T|$  correlation function  $\rho(|\Delta\vec{p}_T|) = |\Delta\vec{p}_T|^{-\phi}$ ,  $\varphi_2 = (\phi + 1)/2$
- fraction of correlated particles

The intermittency index  $\varphi_2$  for a system freezing out at the QCD critical endpoint is expected to be  $\varphi_2 = 5/6$  assuming that the latter belongs to the 3D Ising universality class.

# $h^-$ intermittency: an unexpected increase



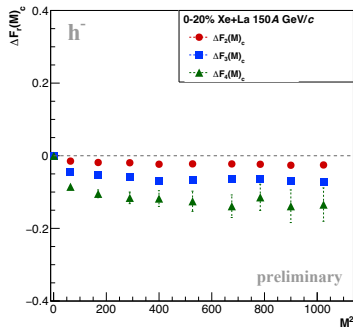
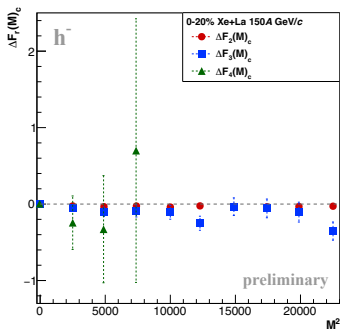
full range –  $p_T$  binning



small range –  $p_T$  binning

Motivated by STAR collaborations results from 2023, we follow the NA49 methodology and found an unexpected increase when analyzing negatively charged hadrons in central Xe+La collisions at 150A GeV/c. However, this increase does not follow a proper power law.

# $h^-$ intermittency in Xe+La



**No indication for power-law increase with cumulative  $p_T$  binning**

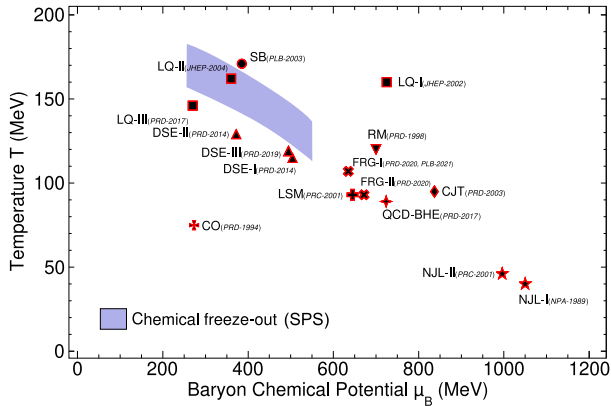
Therefore, we attribute the seen increase to short-range correlations of HBT type.

V. Reyna, CPOD 2024, Berkeley, California

# Summary

In this talk, I resumed results on:

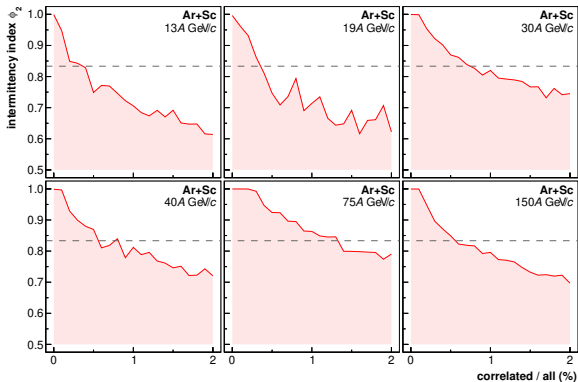
- Multiplicity fluctuations and net-charge fluctuations in Be+Be, p+p and Ar+Sc
- Femtoscopy analysis in Be+Be and Ar+Sc
- Proton intermittency using cumulative  $p_T$  in Ar+Sc and Pb+Pb
- Negatively charged hadron intermittency using  $p_T$  binning and cumulative  $p_T$  binning in Xe+La



# Summary

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- A huge amount of data has been analyzed, resulting in better insight and physics comprehension related to the critical point
- New methods were developed
- None of the results show indication of the Critical Point
- We were able to establish exclusion limits on a simple model of the critical point
- And we are working on more...



Thanks

