



Metrology requirements for the integrated luminosity measurement at ILC

I. Bozovic

I. Smiljanic & G. Kacarevic

Vinča Institute of Nuclear Sciences - National Institute of the Republic of Serbia

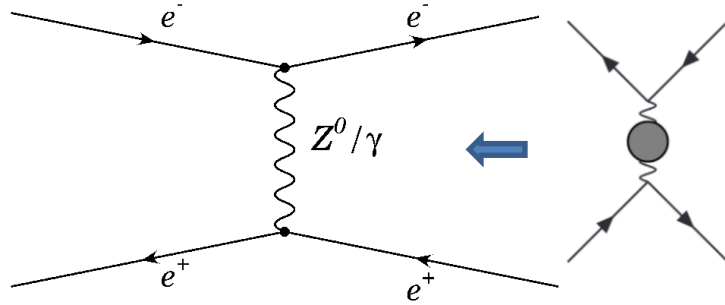
Supported through Grant No. 7699827 Project IDEAS HIGHTONE-P



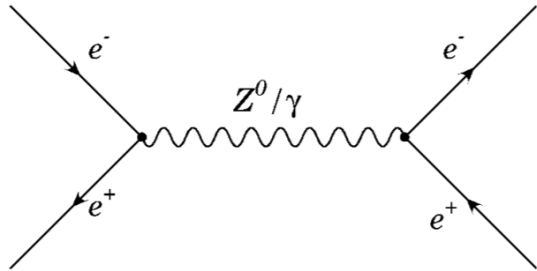
- Small angle Bhabha scattering
- Luminometer at ILC
- Novel metrology study

- Preparing the ECFA Focus Topics paper ([arXiv:2401.07564v2 \[hep-ph\]](https://arxiv.org/abs/2401.07564v2)) we have realized
⇒ NO METROLOGY STUDY EXISTS SINCE TESLA TIMES [LC-DET-2005-004 (2005)]
- We have performed a study at:
Z-pole, 250 GeV, 500 GeV and 1 TeV
(currently under internal ILD review to be submitted to PTEP)

Low angle Bhabha scattering (LABS)



- Dominantly QED scattering at low polar angles
- BHLUMI 4.04: NLO QED corrections; higher-order QED corrections through the exclusive YFS exponentiation; No NLO EW corrections; partial implementation of s-channel γ/Z exchange
- Hadronic vacuum polarization in t-channel photon exchange can be a limiting factor for the x-section precision; Revised $\delta\sigma_B$ for LEP analyses $3.7 \cdot 10^{-4}$ [[Physics Letters B 803 \(2020\) 135319](#)]

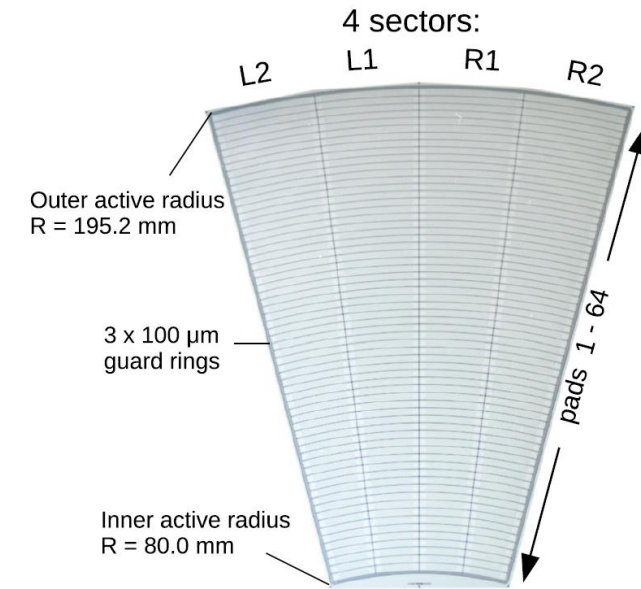
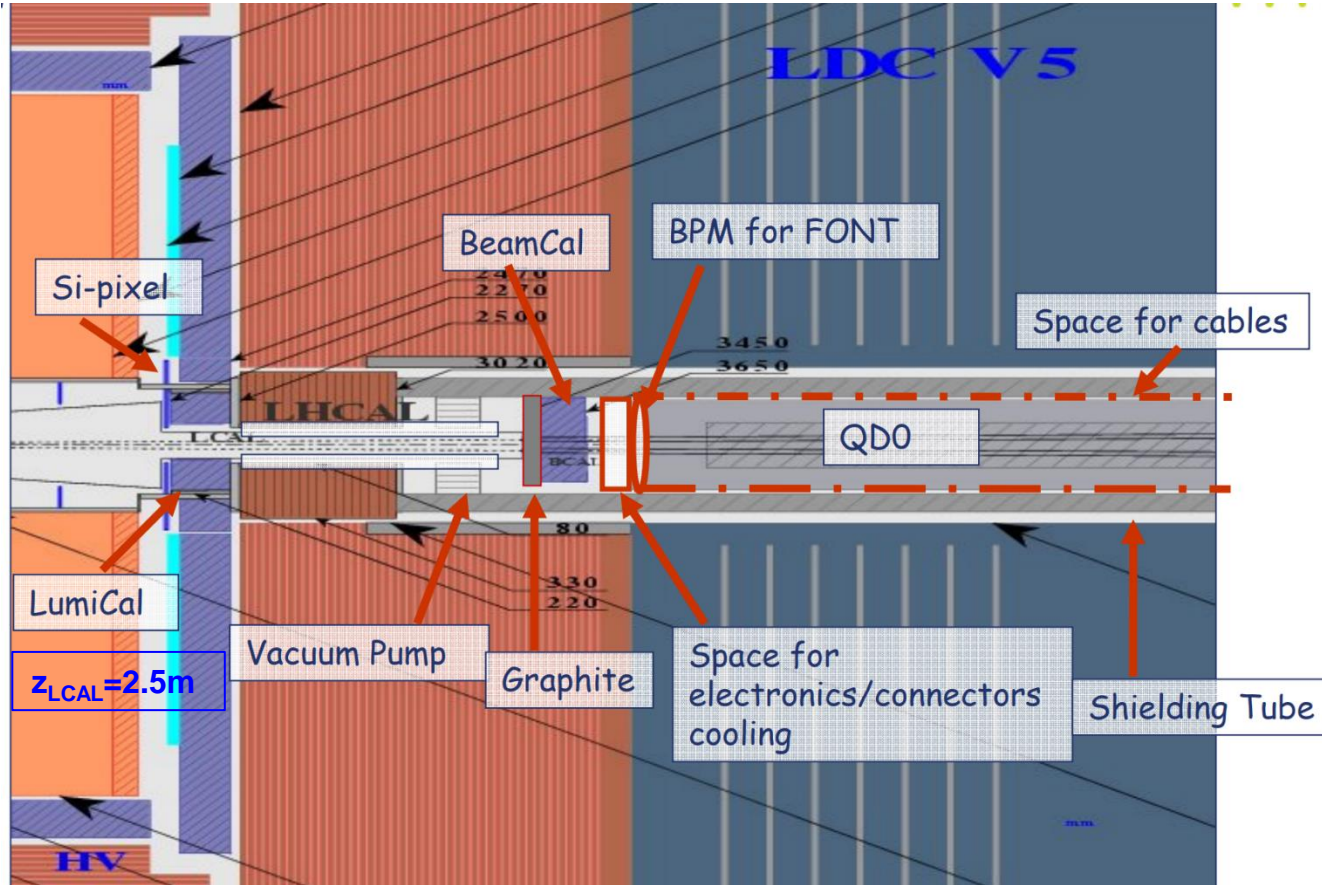


$$\frac{d\sigma_B}{d\theta} = \frac{2\pi\alpha_{em}^2}{s} \frac{\sin\theta}{\sin^4(\theta/2)} \approx \frac{32\pi\alpha_{em}^2}{s} \frac{1}{\theta^3}$$

this is where μm precision of r_{in} is coming from

$$\delta(\sigma_B) \approx \delta(s) = 10^{-4}$$

At the Z-pole, center-of-mass energy should be known at ~ 5 MeV
(up to a few hundreds of MeV at 1 TeV)



x-angle=14 mrad

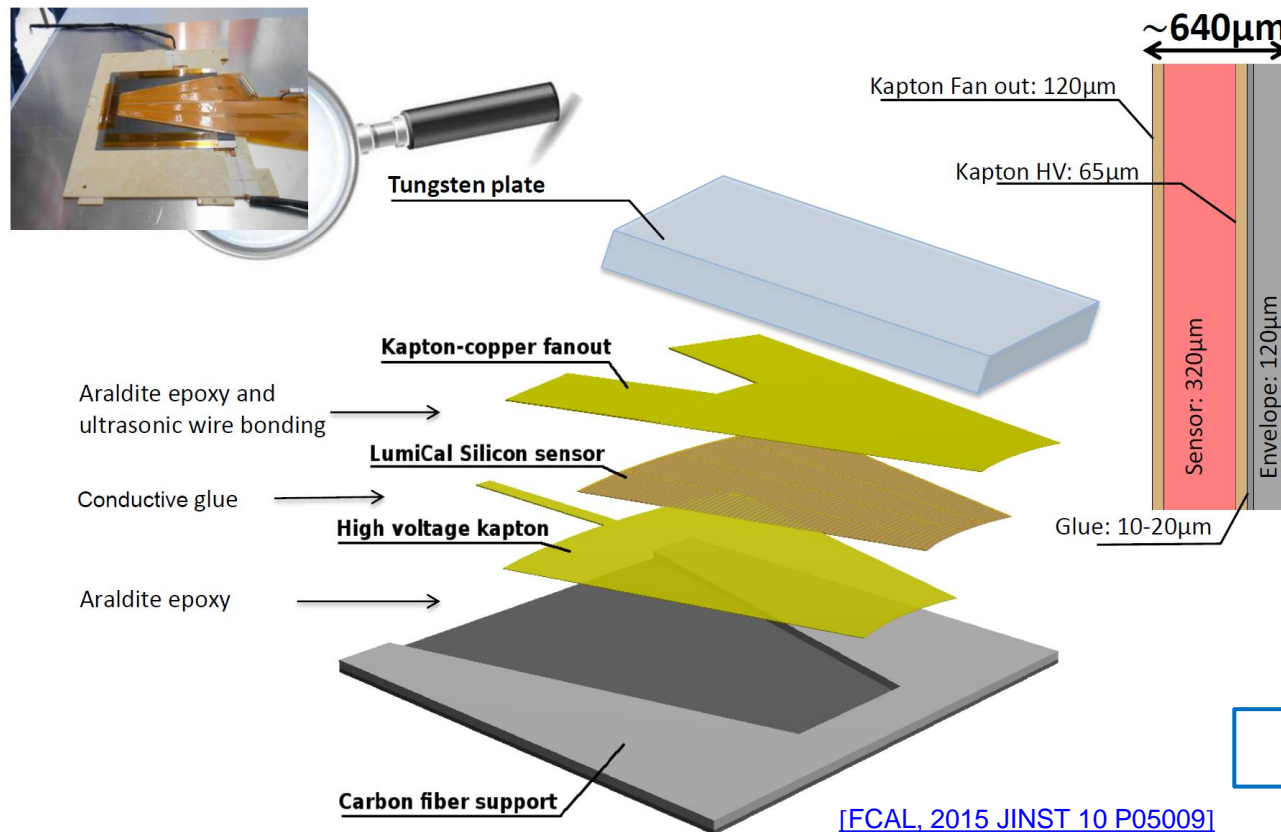
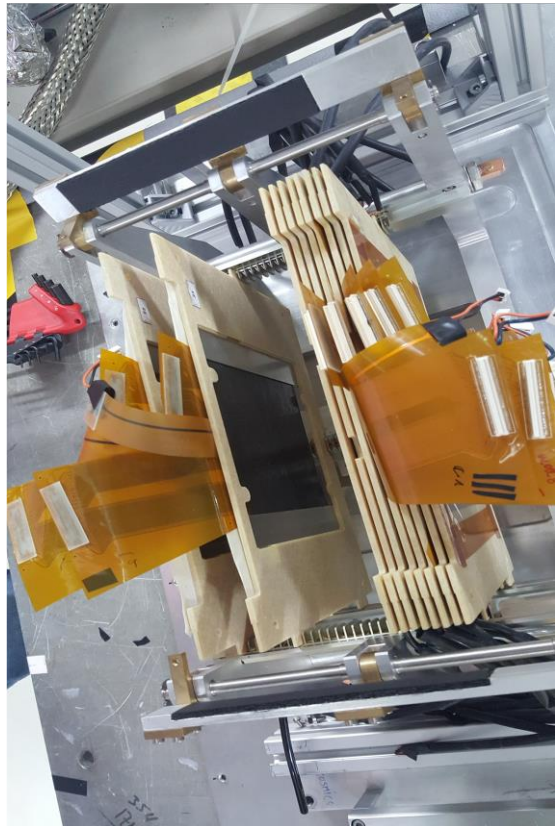


	Parameters	ILD
LumiCal	geometrical acceptance [mrad]	31-77
	fiducial acceptance [mrad]	41-67
	z (from IP) [mm]	2480
	number of layers (W+Si)	30

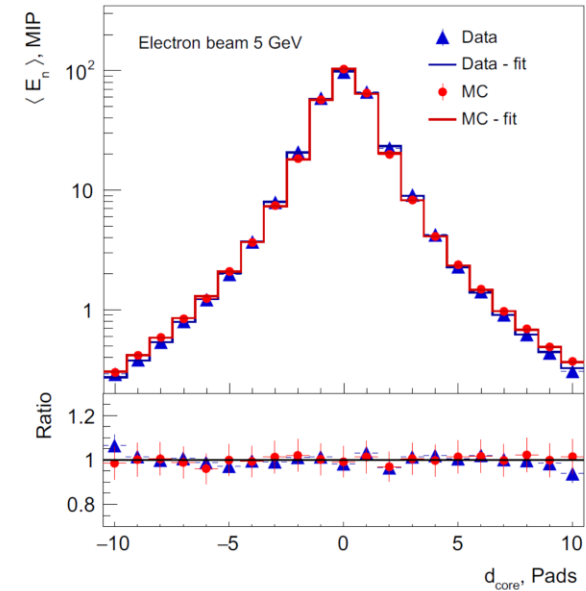
- Cylindrical Silicon-Tungsten sandwich
- 30 $1X_0$ (3.5 mm) absorber planes, 30 sensor planes
- 320 μm sensor thickness/1 mm gap between absorber planes
- Radial segmentation: 64 pads with 1.8 mm pitch
- Azimuthal segmentation: 48 sectors covering 7.5° each
- FE electronics outside the calorimeter

Luminometer prototype

- High precision in polar angle measurement ($\sim 20 \mu\text{rad}$)
 \Rightarrow Shower position and energy measurement on top of widely spread background
- \Rightarrow Compactness - small Moliere radius
- Feasibility demonstrated by the FCAL R&D Collaboration



[FCAL, 2015 JINST 10 P05009]



$$0.9 = \int_0^{2\pi} d\varphi \int_0^{R_M} F_E(r) r dr$$

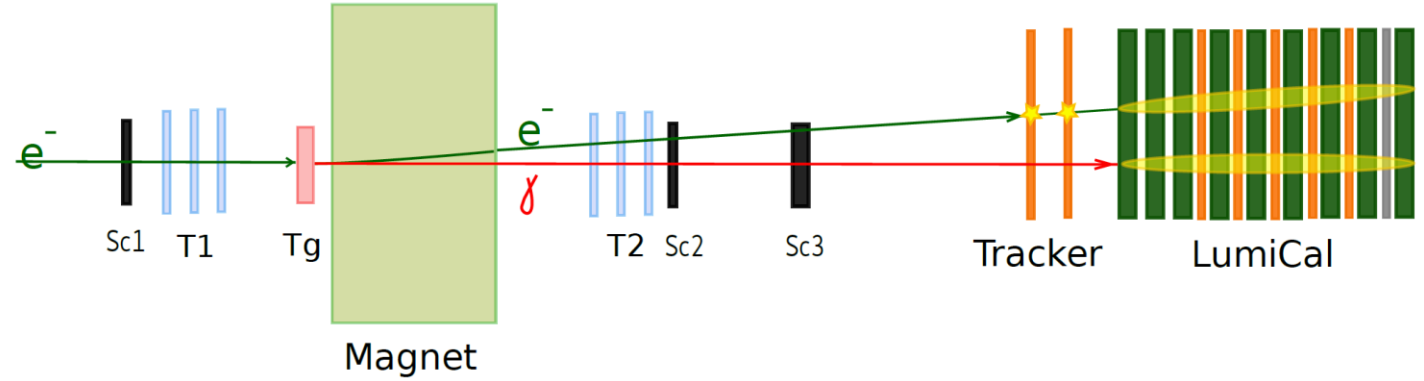
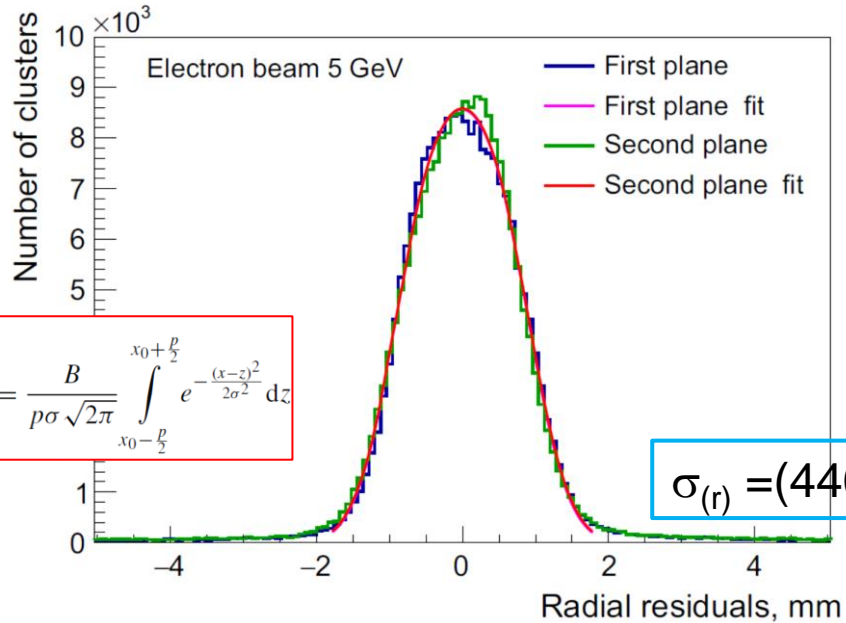
$$R_M = (8.1 \pm 0.1_{\text{stat.}} \pm 0.3_{\text{sys.}}) \text{ mm}$$



Design and performance

Dissipation of reconstructed hits
in the luminometer front plane

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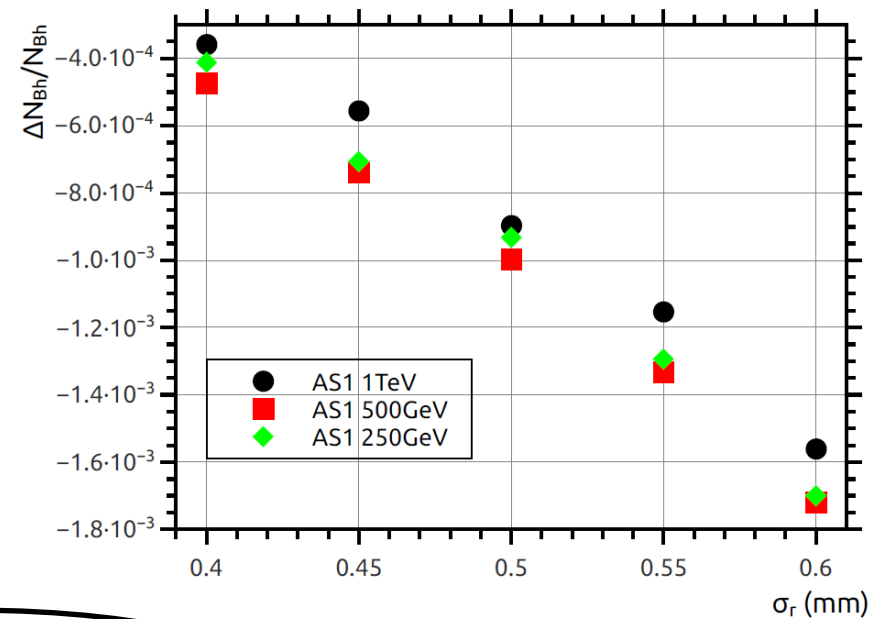
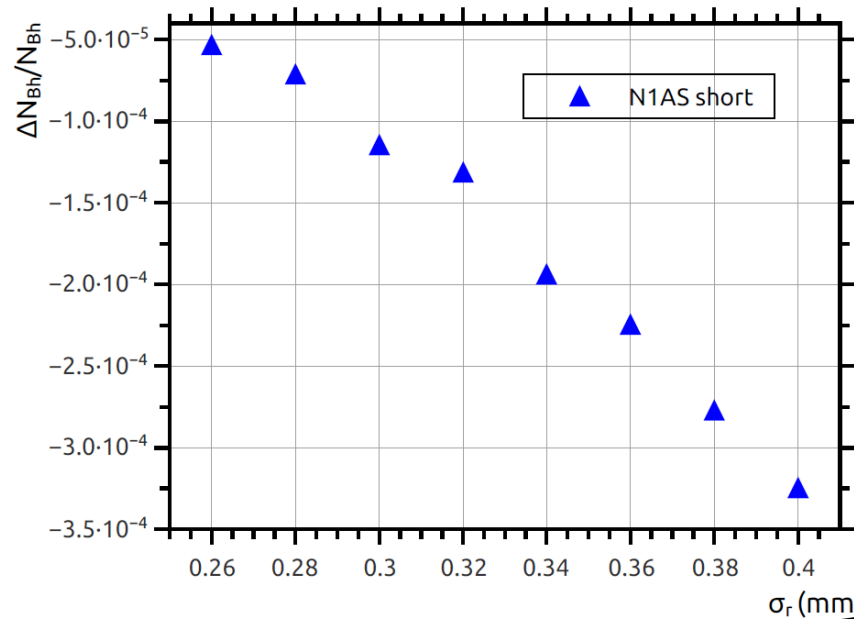


- DESY-II Synchrotron electron beam 1-5 GeV (beam size 5x5 mm²)
 - T1, T2 Eudet telescopes each with 3 MIMOSA Si-pixel planes
 - Sc1,2,3 scintillator trigger
 - Tg copper target
- Dipole magnet –13 kGs for e/γ separation
- 8 detector planes (6 -LumiCal, 2-tracker)
 - 128 read-out channels per plane
 - 8 W absorber plates
 - External electronics



- 10 million low angle Bhabha scattering events using BHLUMI V4.04
- (20-200) mrad to allow events with non-collinear final state radiation to contribute
- No full detector simulation, no beam-beam effects, only FV (41-67) mrad
- s-axis, asymmetric counting ($\Delta r=1\text{mm}$)

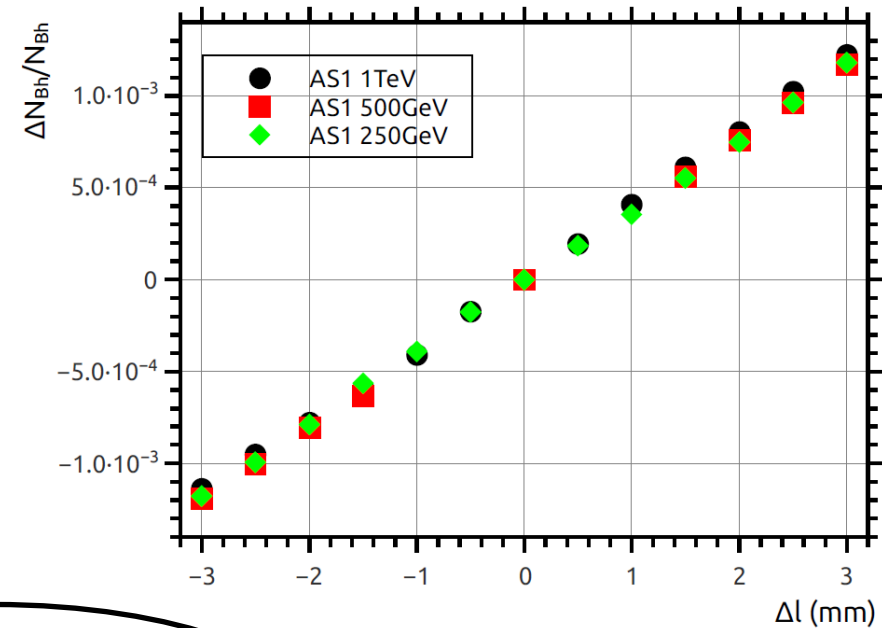
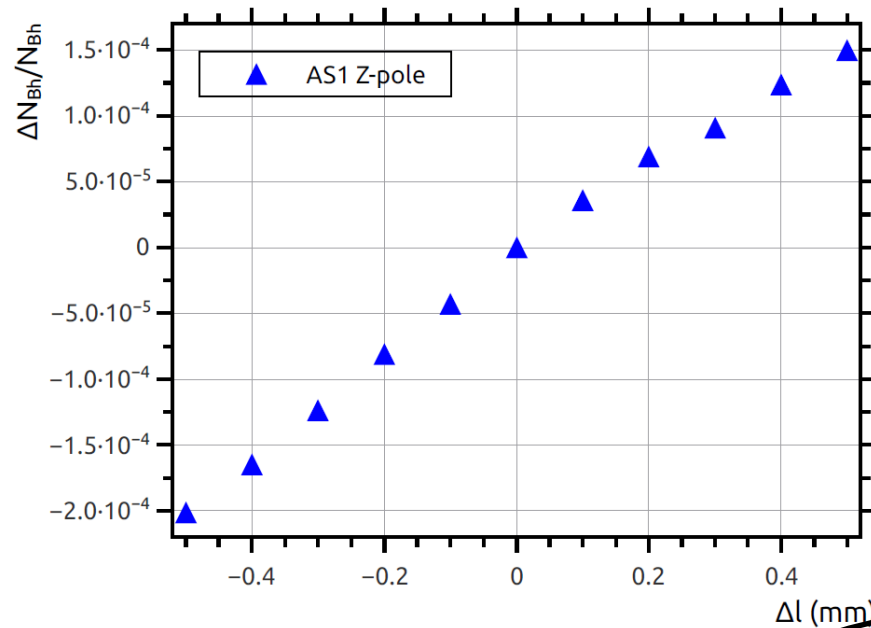
Dissipation of reconstructed hits in the luminometer front plane



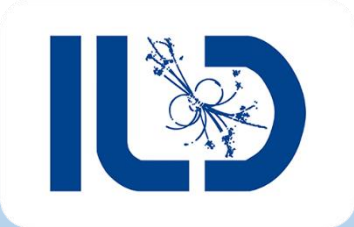
< 500 μm ok at higher energies
 $\leq 300 \mu\text{m}$ needed at the Z-pole



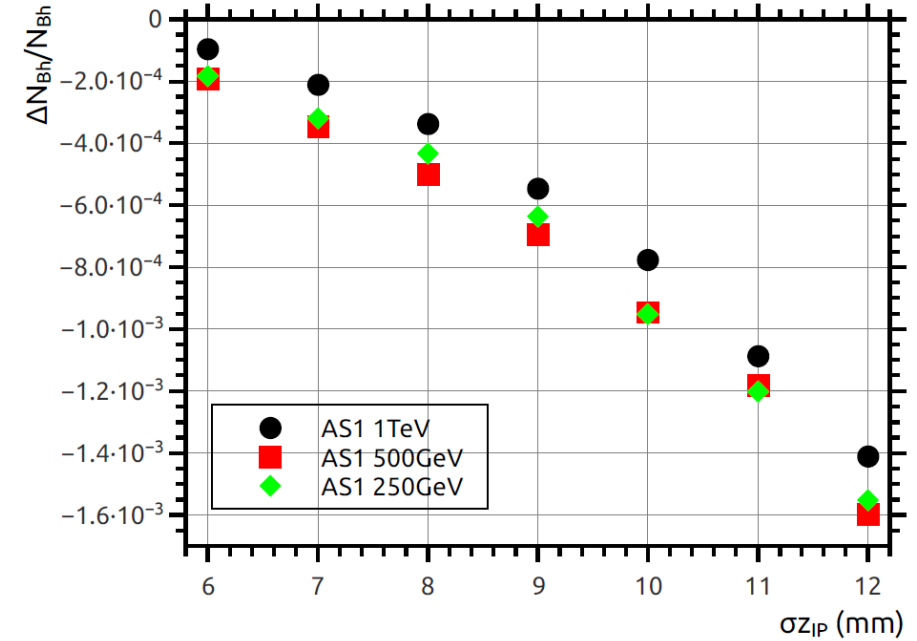
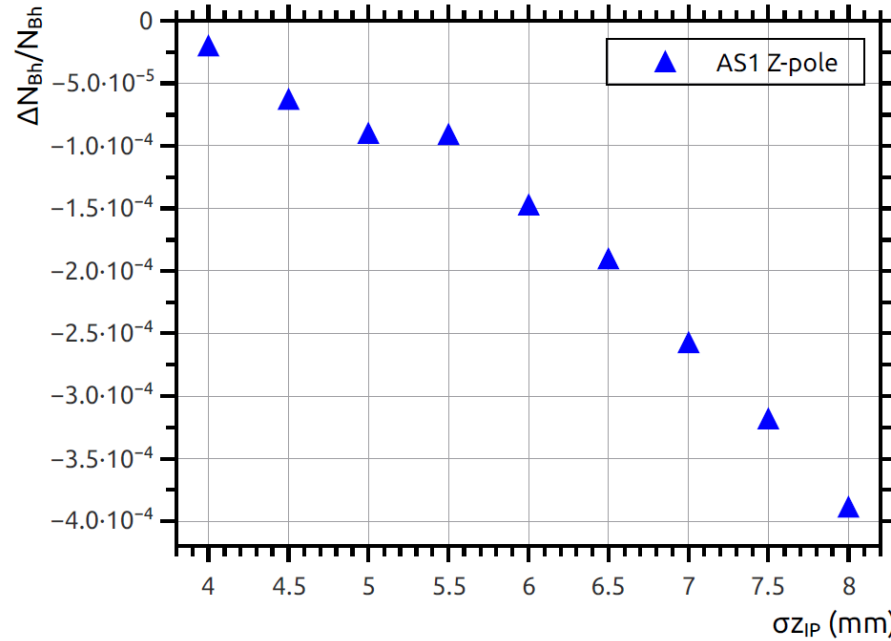
Distance between luminometer halves (symmetric)



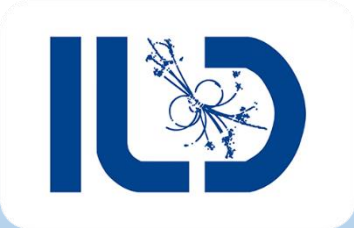
~ 2.5 mm at higher energies
 ~ 200 μ m at the Z-pole
 (feasible with FSI)



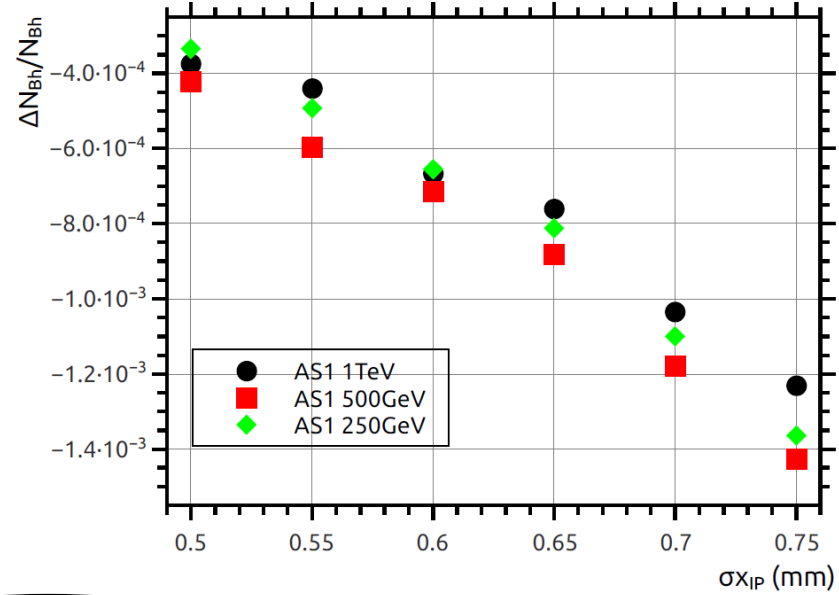
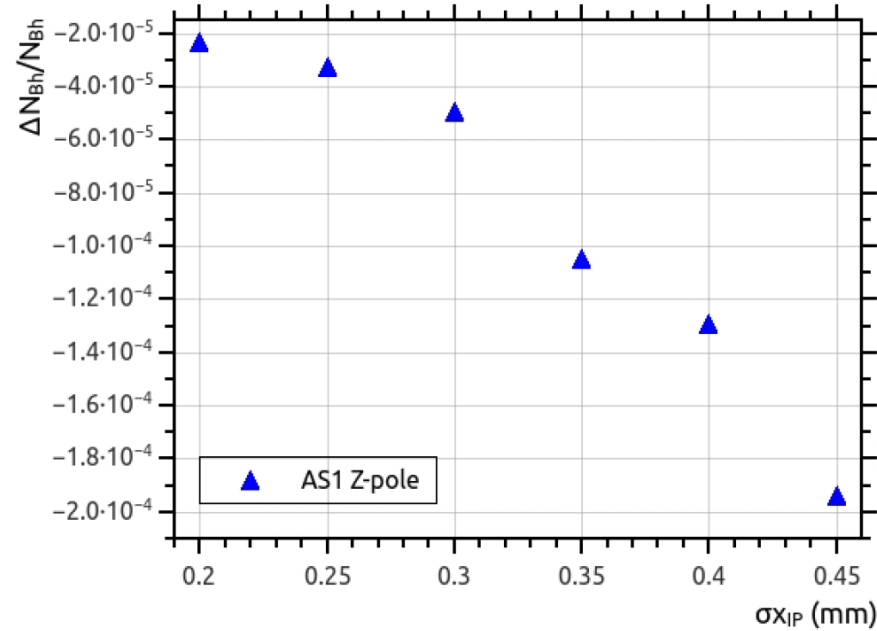
Axial vibrations of the luminometer



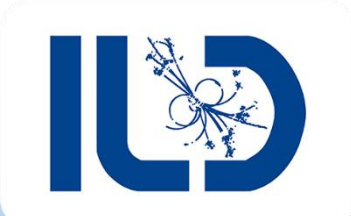
~ 10 mm at higher energies
 ~ 5 mm at the Z-pole



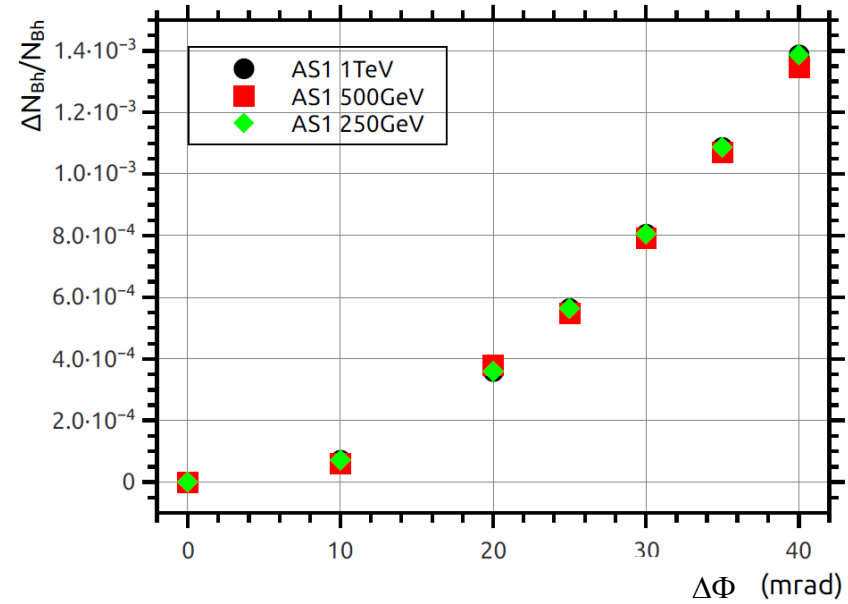
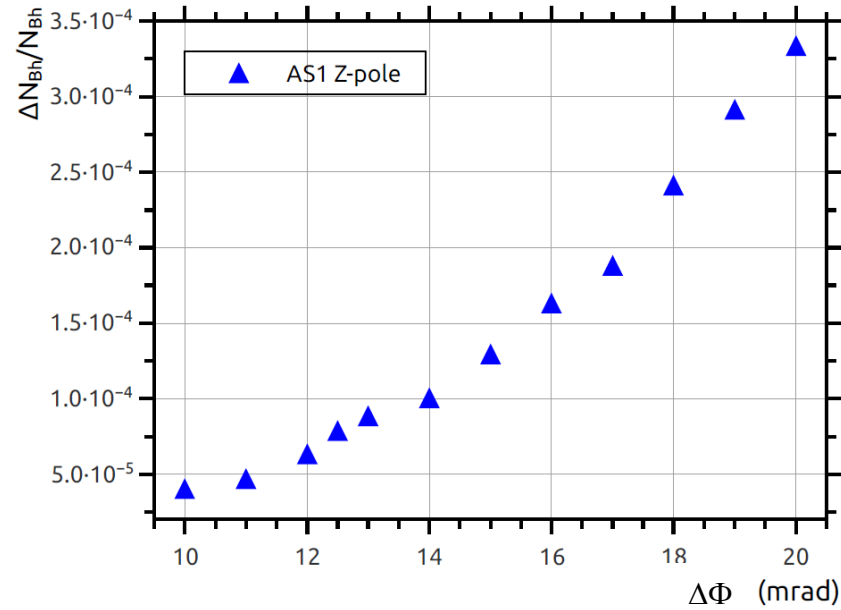
Radial vibrations of the luminometer



*< 700 μ m at higher energies
 ~ 350 μ m at the Z-pole*



Tilt (rotation around y-axis) of the luminometer



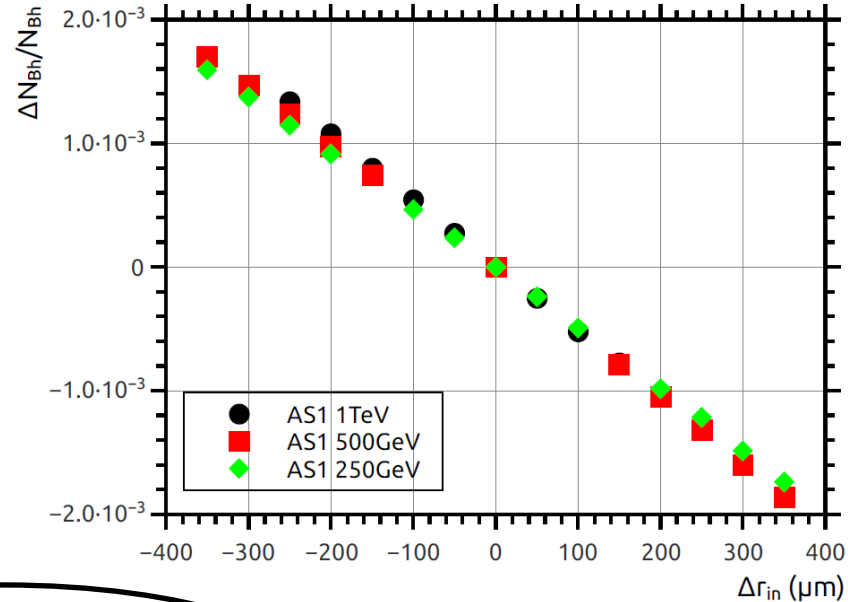
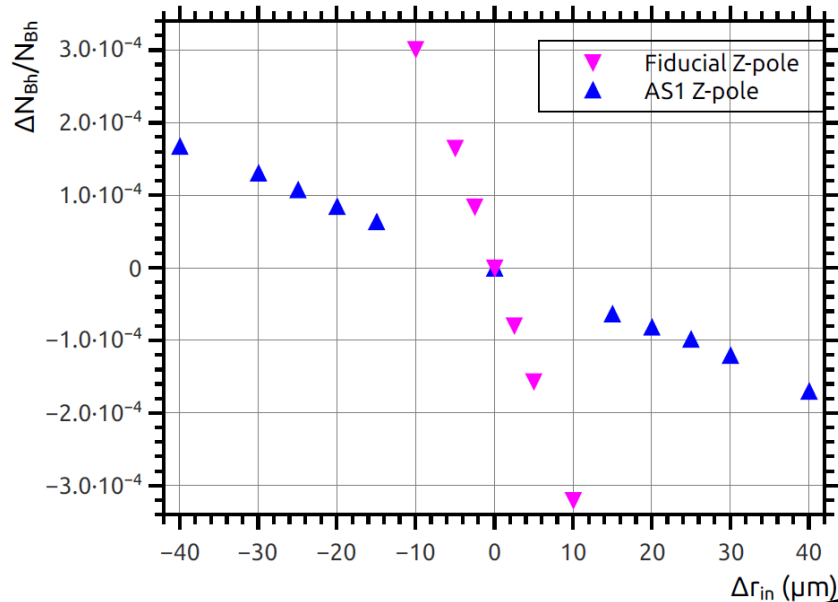
*~ 35 mrad at higher energies
~ 14 mrad at the Z-pole*



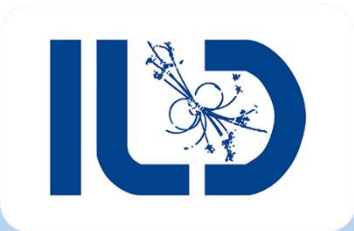
- Metrology for **the inner aperture** depends on:
 - What is a counting volume: full acceptance, FV?
 - Way of counting (LEP-style, full FV)?

- Asymmetric counting ($\Delta r=1$ mm at one side) compensates for smaller variations $\sim 20 \mu\text{m}$ (of the counting volume) at the other
- Symmetrical counting requires $\sim 1 \mu\text{m}$ precision at the Z-pole
- Asymmetric counting only applicable with luminometer on the s-axis

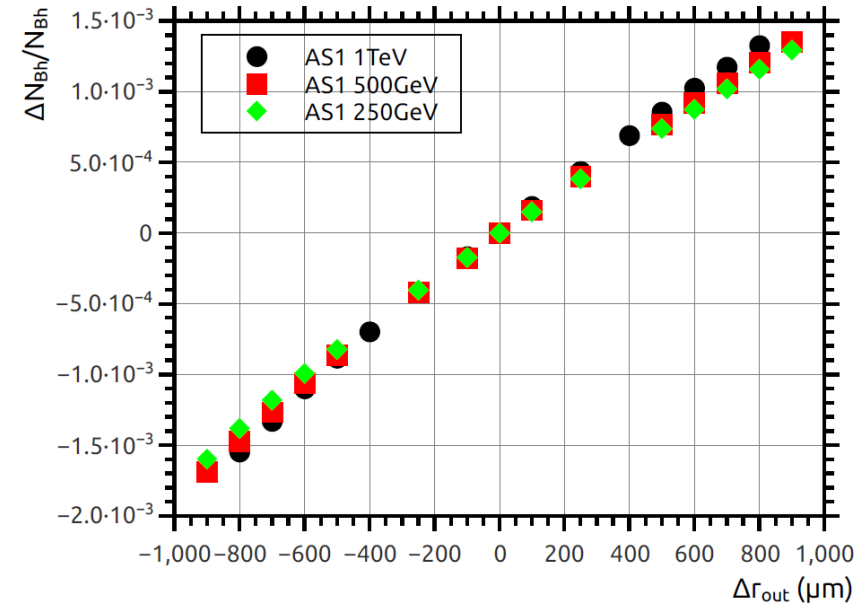
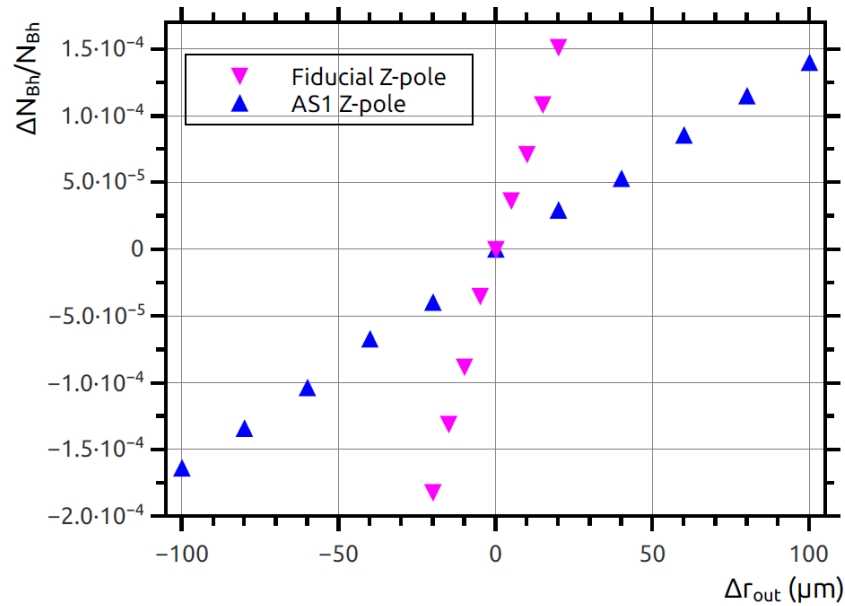
Inner aperture of the counting (FV) volume



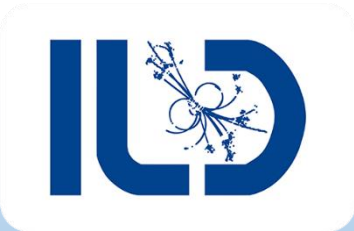
*~ 200 μm at higher energies
~ 20 μm at the Z-pole*



Outer aperture of the counting (FV) volume

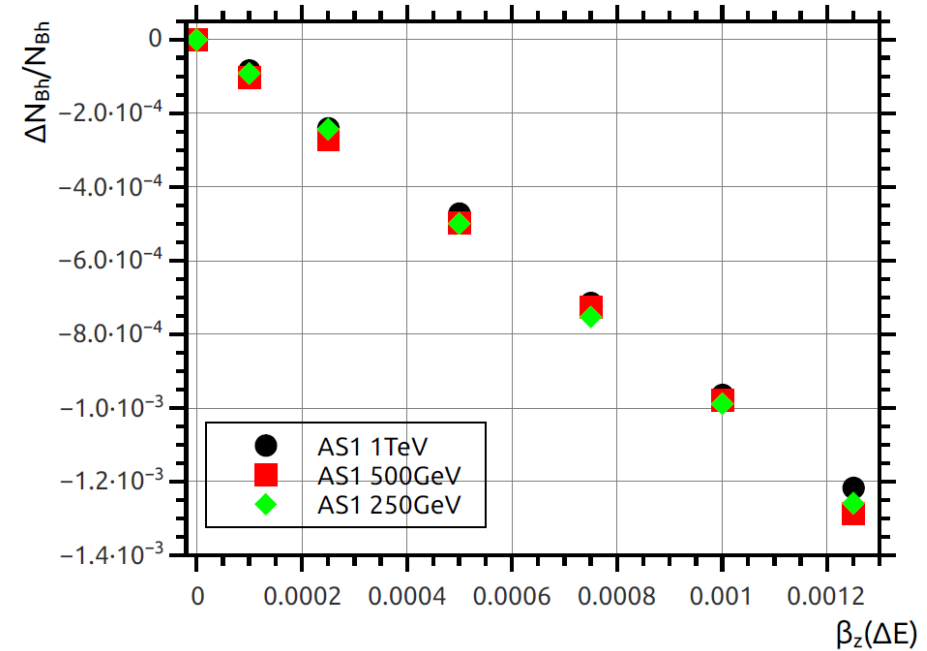
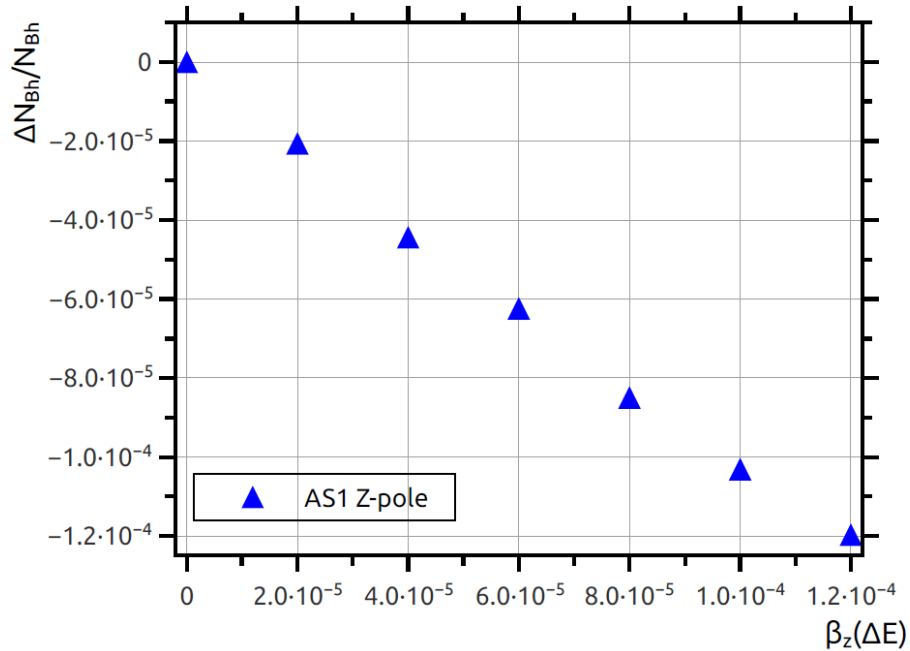


~ 600 μm at higher energies
 ~ 60 μm at the Z-pole

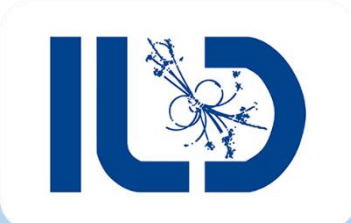


ΔE - asymmetry (bias) in beam energies

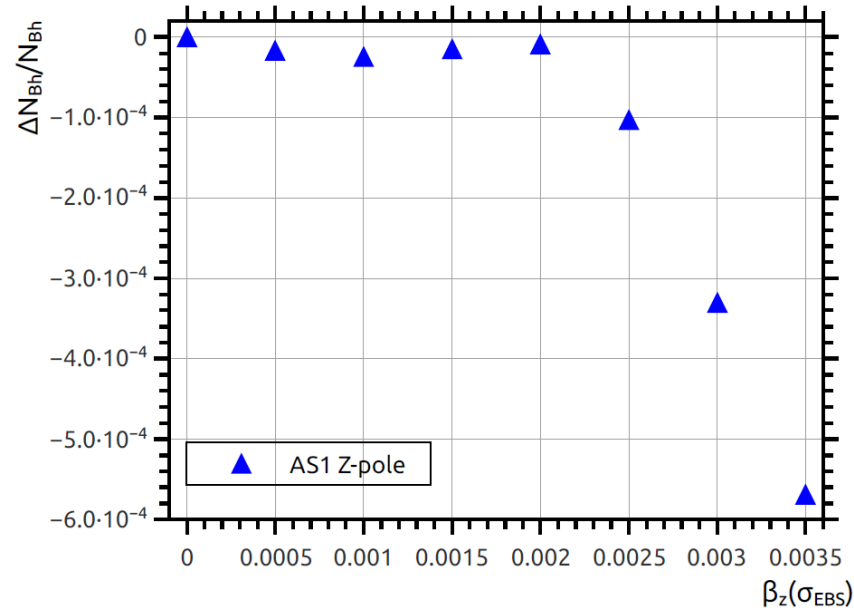
$$\beta_z = 2\Delta E / \sqrt{s}$$



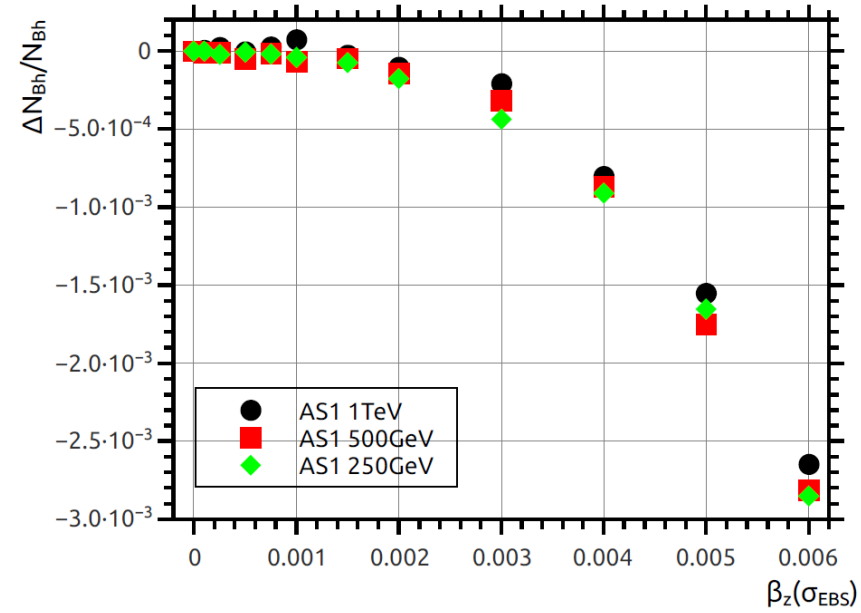
125 MeV, 250 MeV and 500 MeV
 at 250 GeV, 500 GeV and 1 TeV
 ~ 5 MeV needed at the Z-pole



BES - beam energy spread

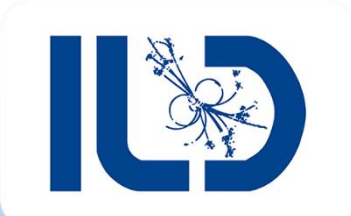


current BES (250 GeV) 0.019: $\Delta \mathcal{L}/\mathcal{L} \sim 3 \cdot 10^{-5}$

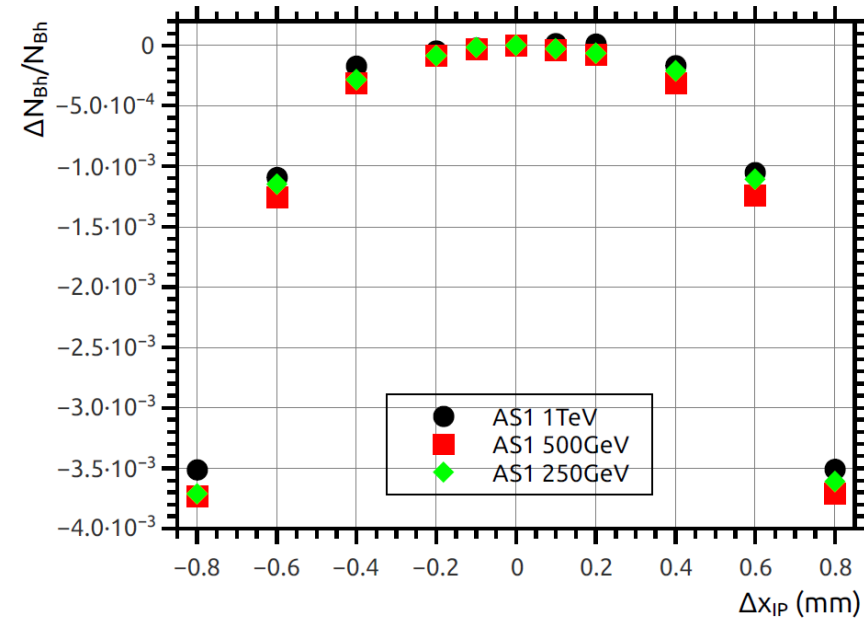
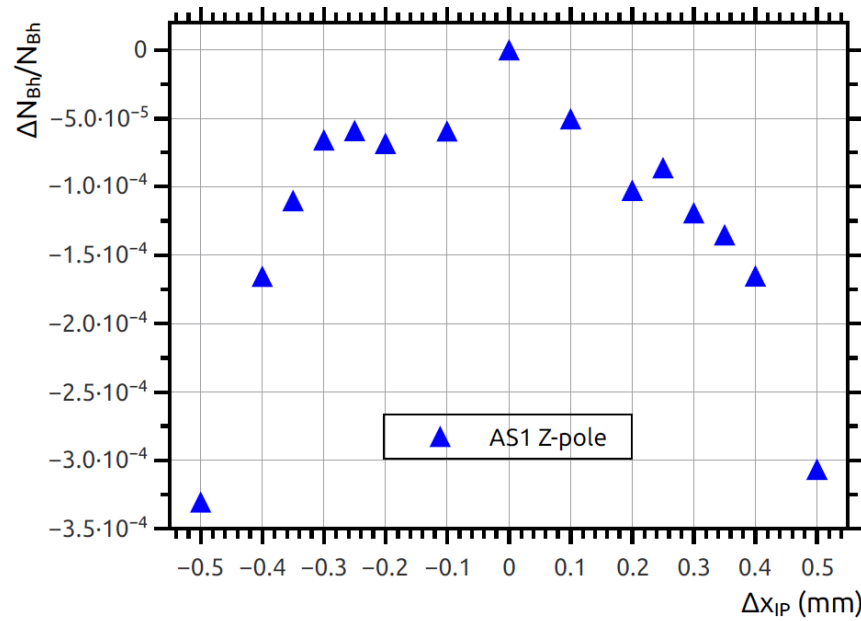


500 MeV, 1 GeV and 2 GeV
at 250 GeV, 500 GeV and 1 TeV

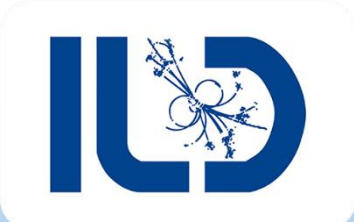
~ 110 MeV needed at the Z-pole
(<0.2% BES should be ok)



Radial displacements of the IP

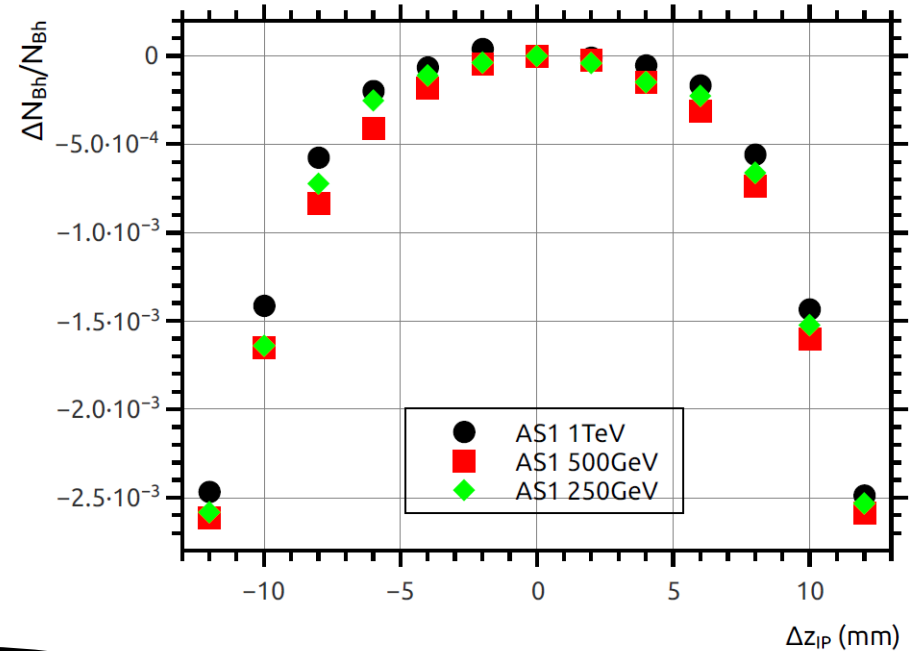
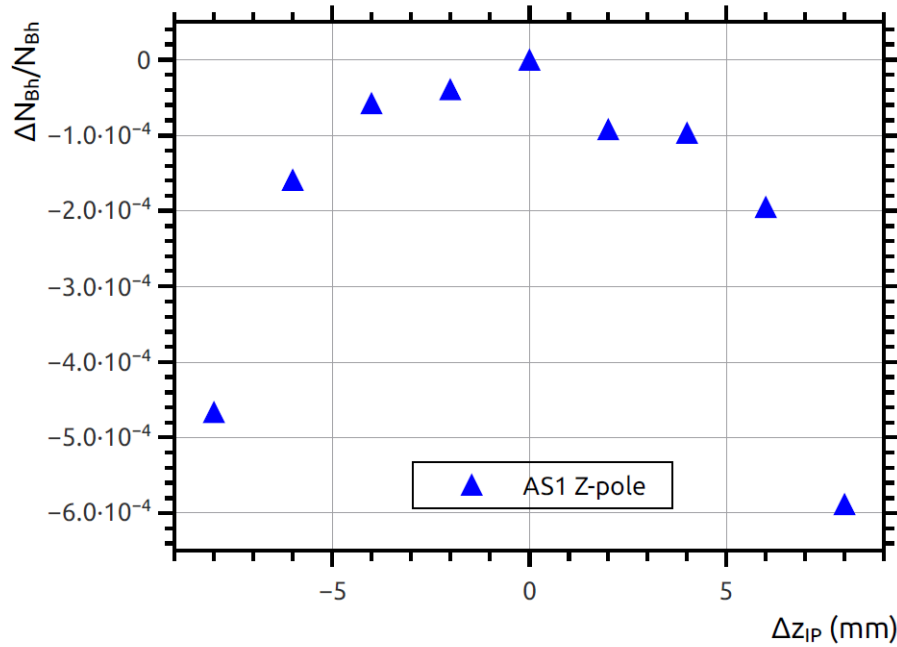


~ 600 μm at higher energies
 ~ 300 μm at the Z-pole

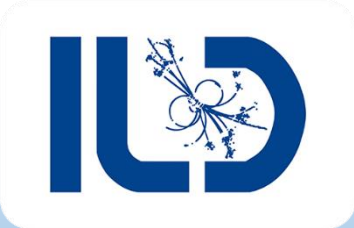


- Axial displacement of the IP \Rightarrow beam synchronization

Axial displacements of the IP



~ 9 mm (30 ps) at higher energies
 ~ 4 mm (13 ps) needed at the Z-pole



Conclusion on metrology

parameter	Z-pole	250 GeV	500 GeV	1 TeV
Δr_{in} (μm)	20	200	200	200
Δr_{out} (μm)	60	600	600	550
σ_r (mm)	0.3	0.5	0.5	0.5
Δl (mm)	0.2	2.5	2.5	2.5
$\sigma_{x_{IP}}$ (mm)	0.3	0.6	0.6	0.6
$\sigma_{z_{IP}}$ (mm)	5	10	10	10
tilt (mrad)	14	35	35	35
Δx_{IP} (mm)	0.3	0.6	0.6	0.6
Δz_{IP} (mm)	4	8	8	8
$\Delta\tau$ (ps)	13	27	27	30
$\sigma_{E_{BS}}$ (MeV)	110	500	1000	2000
ΔE (MeV)	5	125	250	500
$\Delta\mathcal{L}/\mathcal{L}$	$< 3.3 \cdot 10^{-4}$	$< 3.3 \cdot 10^{-3}$		

- **The major challenges only at the Z-pole**
- Inner aperture of the luminometer relaxed with the asymmetric counting
- Position reconstruction in the first plane (300 μm) slightly below prototyped performance (440 μm); Can be resolved with a tracker plane in front of the luminometer
- Beam energy spread should be kept $\leq 0.2\%$
- Asymmetric bias in beam energies (~ 5 MeV)

- $\Delta(\sqrt{s})$ for the cross-section calculation ($\sim 5 \cdot 10^{-4}$)
- Theoretical uncertainty for the revised LEP analyses $3.7 \cdot 10^{-4}$ [[Physics Letters B 803 \(2020\) 135319](#)]



- ILC/ILD has a past of extensive simulation studies on integrated luminosity measurement by the FCAL Collaboration
- FCAL Collaboration has demonstrated in prototype a feasibility of the compact calorimetry for the very forward region of an e^+e^- collider
- Completed with the metrology study at ILC energies – aiming to derive precision limits on individual parameters, not on the integrated luminosity itself
- Input to the ECFA study on Higgs / Top / EW factories prepared, topical paper under ILD review





Complementing the existing results

Source of uncertainty	$\Delta L/L$ (500 GeV)	$\Delta L/L$ (1 TeV)	Comment			
Bhabha cross-section σ_B	$5.4 \cdot 10^{-4}$	$5.4 \cdot 10^{-4}$	If needed, can be resolved with Si-tracker plane			
Polar angle resolution σ_θ	$1.6 \cdot 10^{-4}$	$1.6 \cdot 10^{-4}$				
Bias of polar angle $\Delta\theta$	$1.6 \cdot 10^{-4}$	$1.6 \cdot 10^{-4}$				
IP lateral position uncertainty	$1 \cdot 10^{-4}$	$1 \cdot 10^{-4}$	Quantified to 200 μm			
Energy resolution a_{res}	$1.0 \cdot 10^{-4}$	$1.0 \cdot 10^{-4}$	Unchanged			
Energy scale	$1.0 \cdot 10^{-3}$	$1.0 \cdot 10^{-3}$				
Beam polarization	$1.9 \cdot 10^{-4}$	$1.9 \cdot 10^{-4}$				
Physics background B/S	$2.2 \cdot 10^{-3}$	$0.8 \cdot 10^{-3}$				
Beamstrahlung + ISR ¹	$-1.1 \cdot 10^{-3}$	$-0.7 \cdot 10^{-3}$				
Beamstrahlung + ISR ²	$0.4 \cdot 10^{-3}$	$0.7 \cdot 10^{-3}$				
EMD ¹	$-2.4 \cdot 10^{-3}$	$-1.1 \cdot 10^{-3}$				
EMD ²	$0.5 \cdot 10^{-3}$	$0.2 \cdot 10^{-3}$				
$(\Delta L/L)^1$	$4.3 \cdot 10^{-3}$	$2.3 \cdot 10^{-3}$			(< $3.3 \cdot 10^{-3}$ from metrology)	
$(\Delta L/L)^2$	$2.6 \cdot 10^{-3}$	$1.6 \cdot 10^{-3}$			$5.4 \cdot 10^{-3}$	$4.0 \cdot 10^{-3}$
			$4.2 \cdot 10^{-3}$	$3.7 \cdot 10^{-3}$		

[FCAL, 2010 JINST 5 P12002] and
 [IBJ et al., 2013 JINST 8 P08012]



ILC beam parameters

Machine	ILC			
mode	Z-pole*	Higgs	500 GeV	1 TeV
Half crossing angle at IP (mrad)	7	7	7	7
Beam energy (GeV)	45	125	250	500
Bunch population (10^{11})	0.2	0.2	0.2	1.74
Bunch length (mm)	0.3	0.3	0.3	0.225
Beam size at IP σ_x/σ_y ($\mu\text{m}/\text{nm}$)	1.35/11.6	0.729/0.7	0.474/5.9	0.335/2.7
Energy spread (natural) (%)	0.42	0.19	0.124	0.085
Luminosity per IP ($10^{34} \text{ cm}^{-2}\text{s}^{-1}$)	0.23	0.75	3.6	4.9

