



SAPIENZA
UNIVERSITÀ DI ROMA



COMBINED FUNCTION MAGNETS

Workshop at LASA

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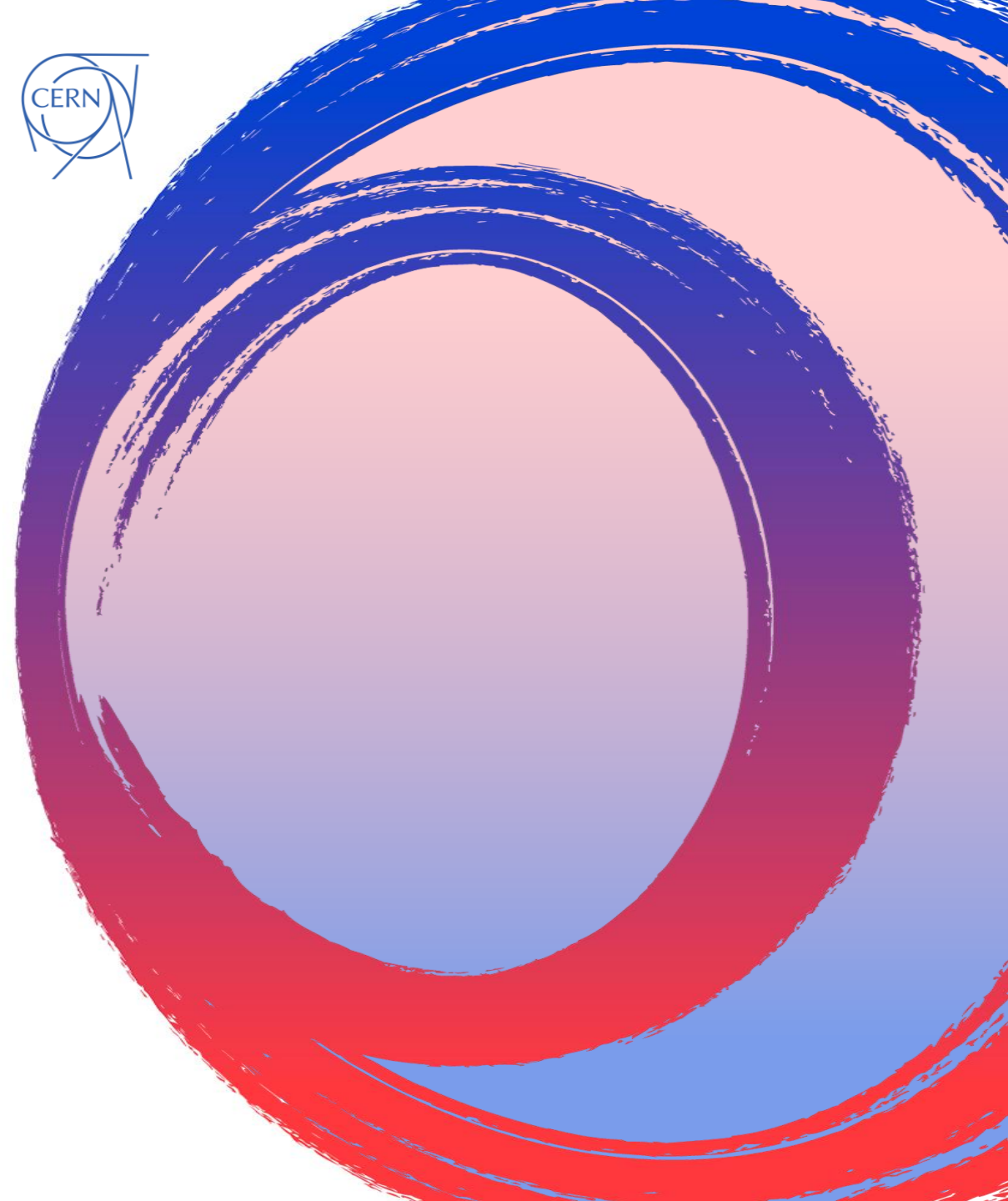
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⁵CERN

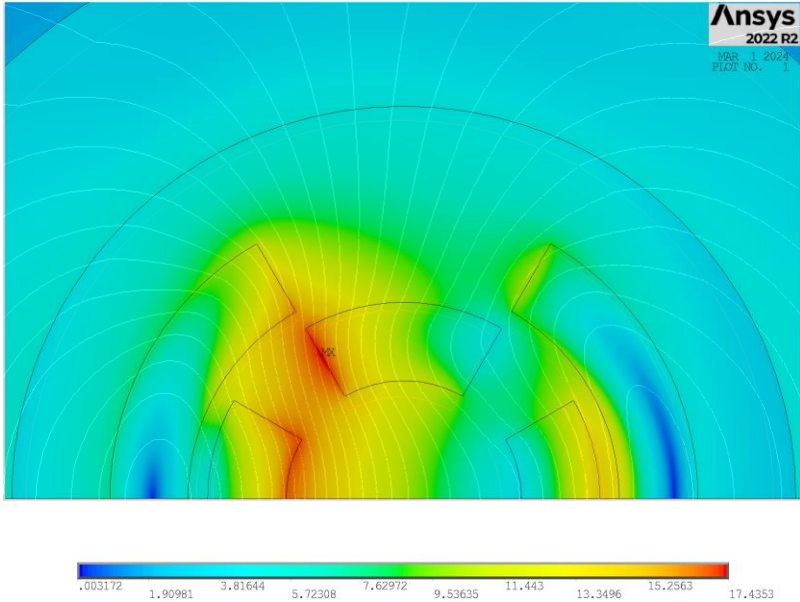


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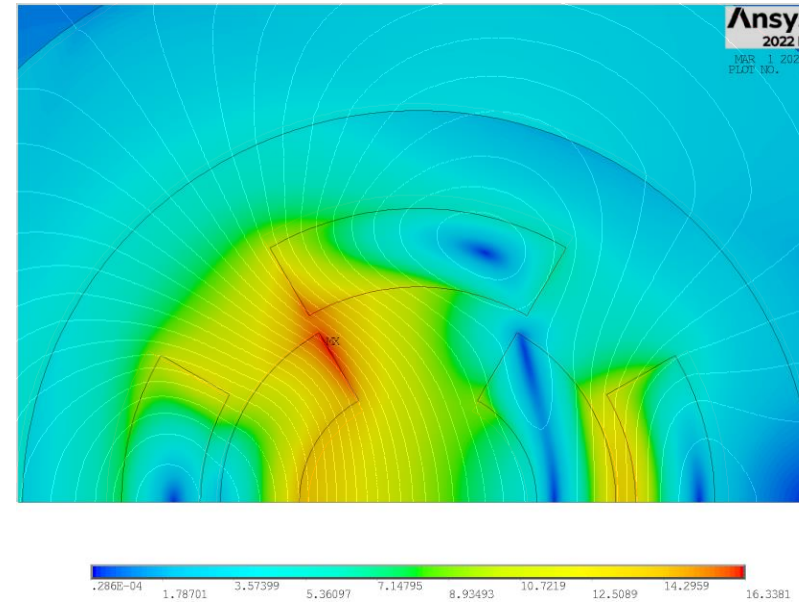


Nested Configurations



Quad into dipole:

(ReBCO @20 K)
 $J = 3.5 \cdot 10^8 \text{ A/m}^2$
 $B \sim 11.7 \text{ T}$
 $G \sim 143.3 \text{ T/m}$



Dipole into quad:

(ReBCO @20 K)
 $J = 3.5 \cdot 10^8 \text{ A/m}^2$
 $B \sim 12.4 \text{ T}$
 $G \sim 90.4 \text{ T/m}$

Arc:

- Combined function magnets: B1, **B1+B2** and **B1+B3**
- $B \approx 8 \dots 16 \text{ T}$; $G \approx 320 \text{ T/m}$; $G' \approx 7100 \text{ T/m}^2$
- Aperture $\approx 160 \text{ mm}$

Final focus:

- Combined function magnets: B1, B2, **B1+B2**, **B1+B3**
- $B \approx 4 \dots 16 \text{ T}$; $G \approx 100 \dots 300 \text{ T/m}$; $G' \approx 12000 \text{ T/m}^2$
- Aperture $\approx 120 \dots 300 \text{ mm}$

The quadrupole into dipole configuration is the most efficient one, in accordance with US-MAP. Additionally, for combined function magnets in the muon collider, quadrupoles are generally required to be stronger than dipoles.

	Dipole	Dipole/Quadrupole	Quadrupole/Dipole
Superconductor	Nb ₃ Sn	Nb ₃ Sn	Nb ₃ Sn
Cable	40x1mm	40x1mm	40x1mm/30x1mm
$B_{coil,max}$, T	15.1	16.6/16.2	16.2/16.1
B_{max}/G_{max} , T/T/m	14.4	9.9/70.1	10.3/89.8
B_{op}/G_{op} , T/T/m	10	8/71	8/81
Margin	~40%	~24%/~20%	~28%/~20%

Most efficient configuration

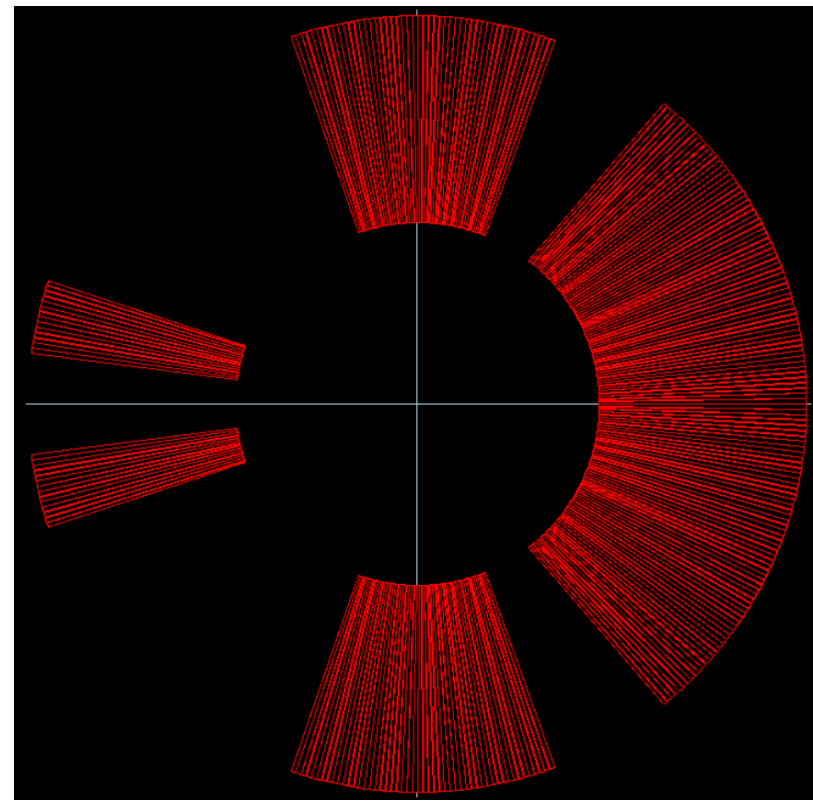
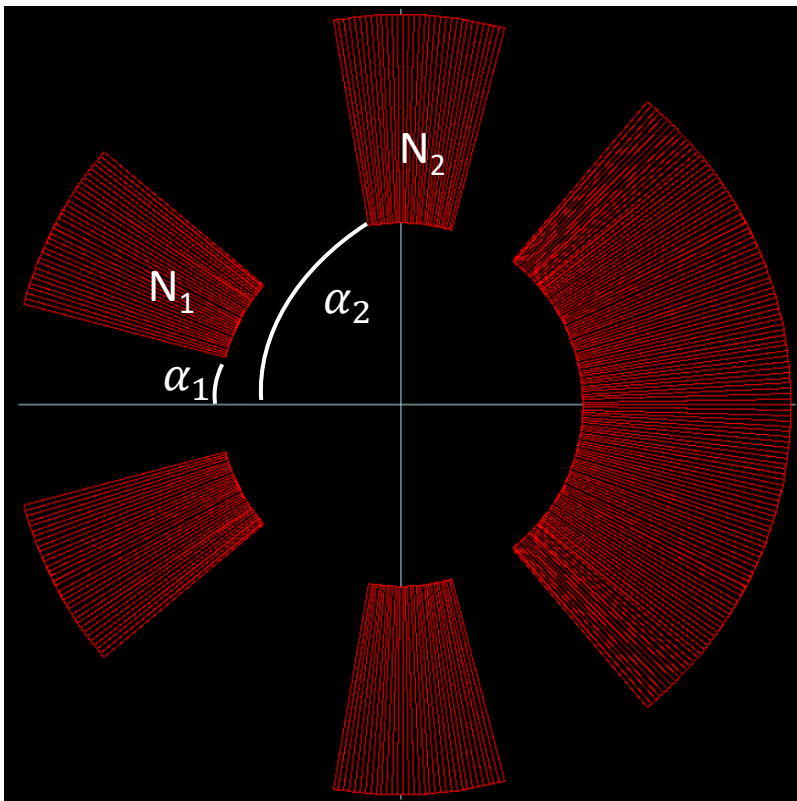
Fermilab

Asymmetric Dipole

No	Type	NCab	X	Y	$\sqrt{u_0^2 b_1}$	Current	Cable name	N1	N2	Imag	Turn
1	Cos	64	70	0	0	48800	REBCO	1	15	0	0
2	Cos	14	70	7,5	7,5	-48800	REBCO	1	15	1	180
3	Cos	50	70	71	71	-48800	REBCO	1	15	1	180

As first approx. I used the same cable assumption of L. Alfonso.

Optimization of α_1, α_2, N_1 and N_2 with ROXIE by maximizing B_2 (@ $R_{ref} = 50 \text{ mm}$) with a weight of 1 and B_1 with a weight of 0.5



$B = 13 \text{ T}$
 $G = 140 \text{ T/m}$
 Ratio = 0.5

$$\text{Ratio} = \frac{B_2 @ R_{ref}}{B_1}$$

Starting from the experience of T.Ogitsu:

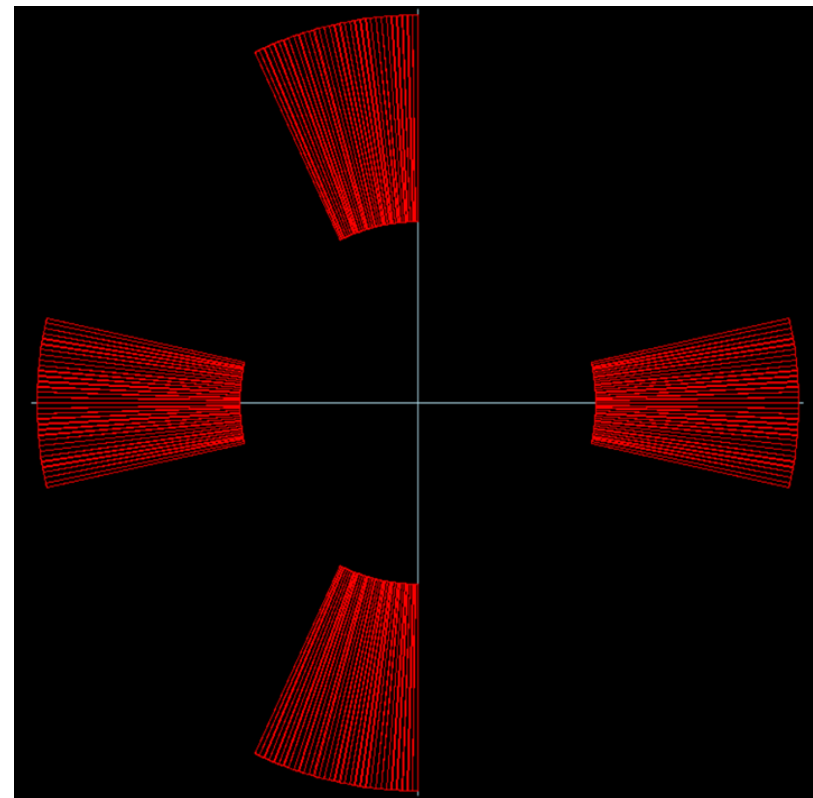
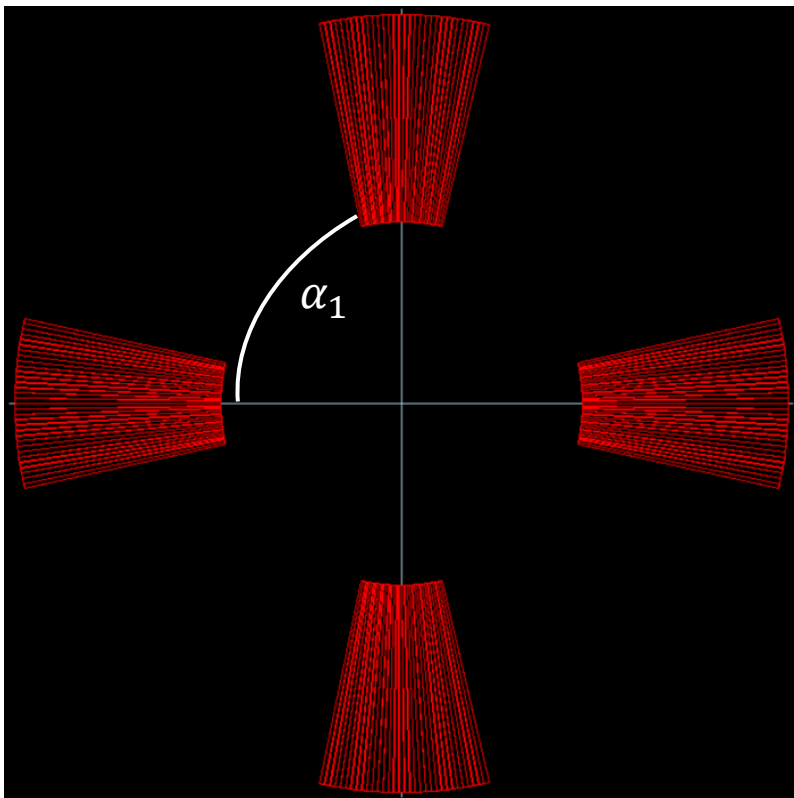
<https://indico.cern.ch/event/1043242/contributions/4448798/attachments/2279860/3873498/MCM20210712SCFM.pdf>

Asymmetric Quadrupole

No	Type	NCab	X	Y	\u03b1	Current	Cable name	N1	N2	Imag	Turn
1	Cos	16	70	0	0	24400	REBCO	1	15	0	0
2	Cos	16	70	0	0	24400	REBCO	1	15	1	180
3	Cos	32	70	89,975	89,975	-48800	REBCO	1	15	0	0

As first approx. I used the same cable assumption of L. Alfonso.

Optimization of α_1 with ROXIE by maximizing B_2 (@ $R_{ref} = 50\text{ mm}$) with a weight of 0.5 and B_1 with a weight of 1



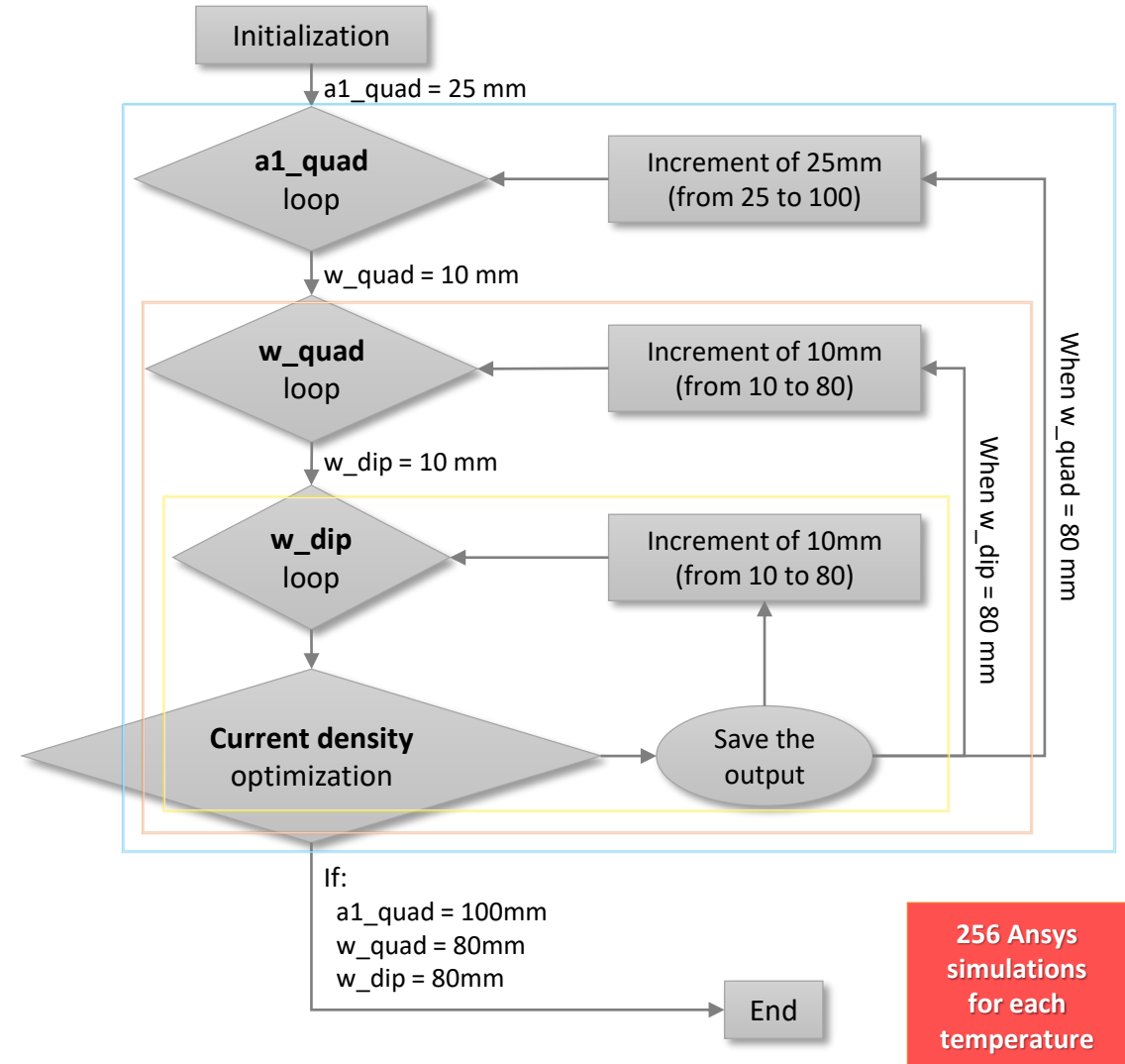
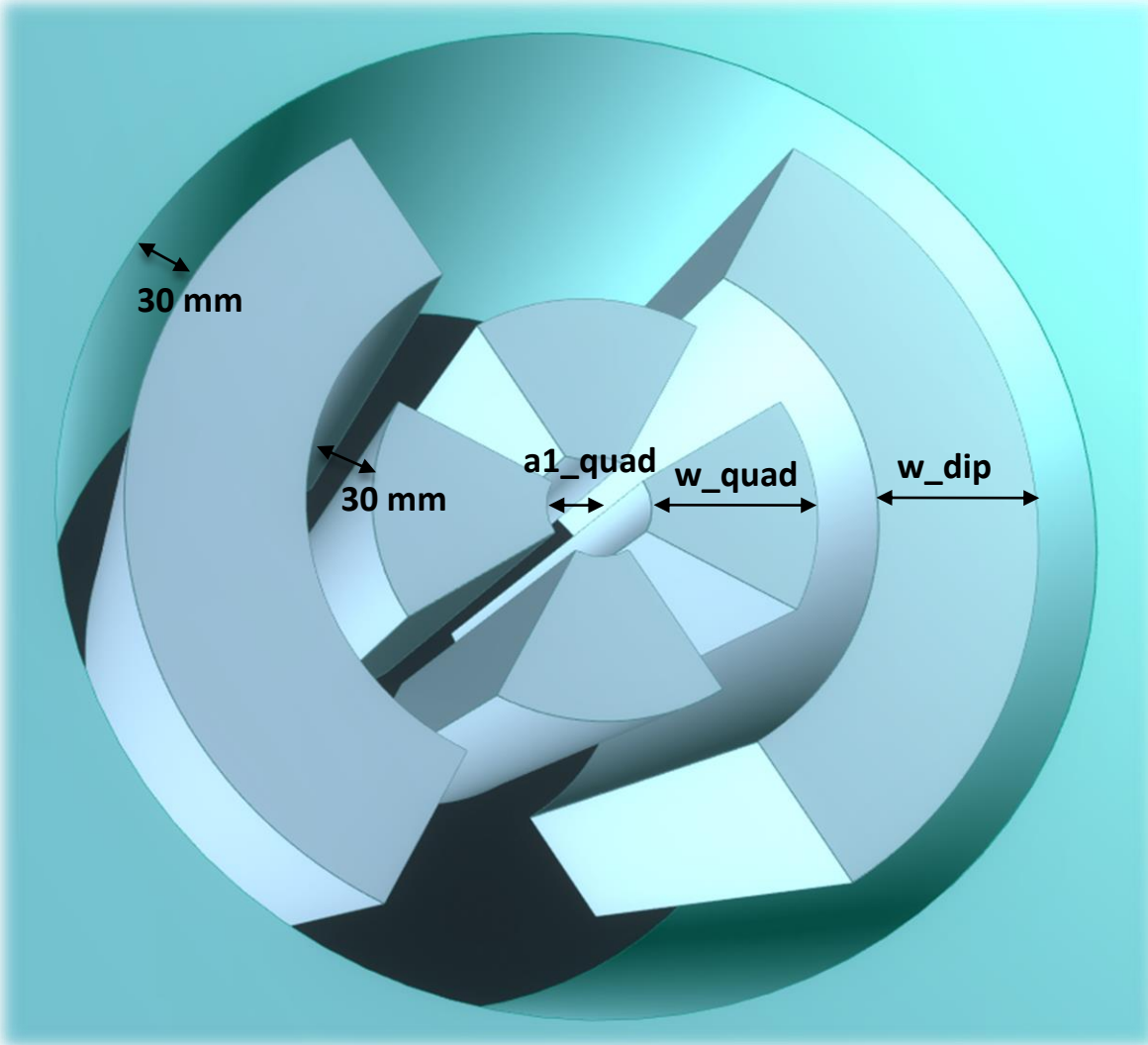
$$B = 4\text{ T}$$

$$G = 80\text{ T/m}$$

$$\text{Ratio} = 0.2$$

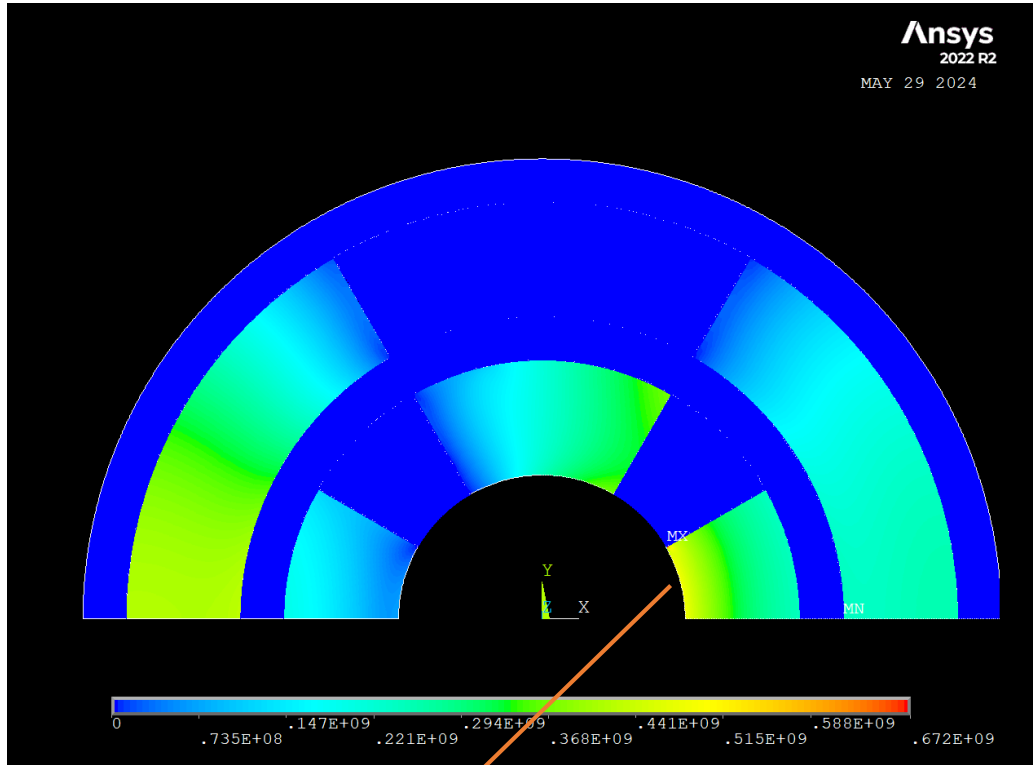
$$\text{Ratio} = \frac{B_1}{B_2 @ R_{ref}}$$

By also allowing the number of conductors to vary, it becomes again an asymmetric dipole.

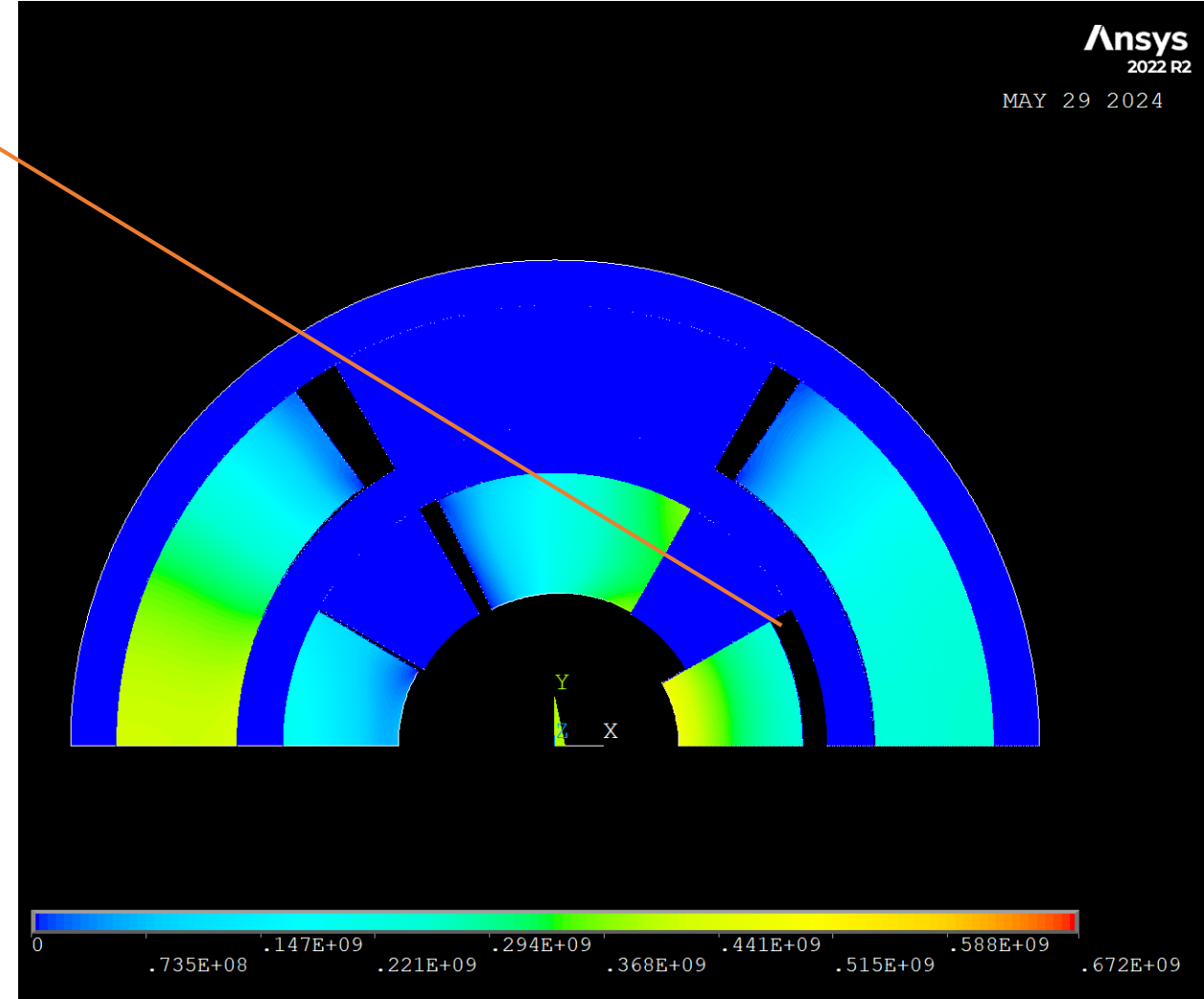


Stress Issue

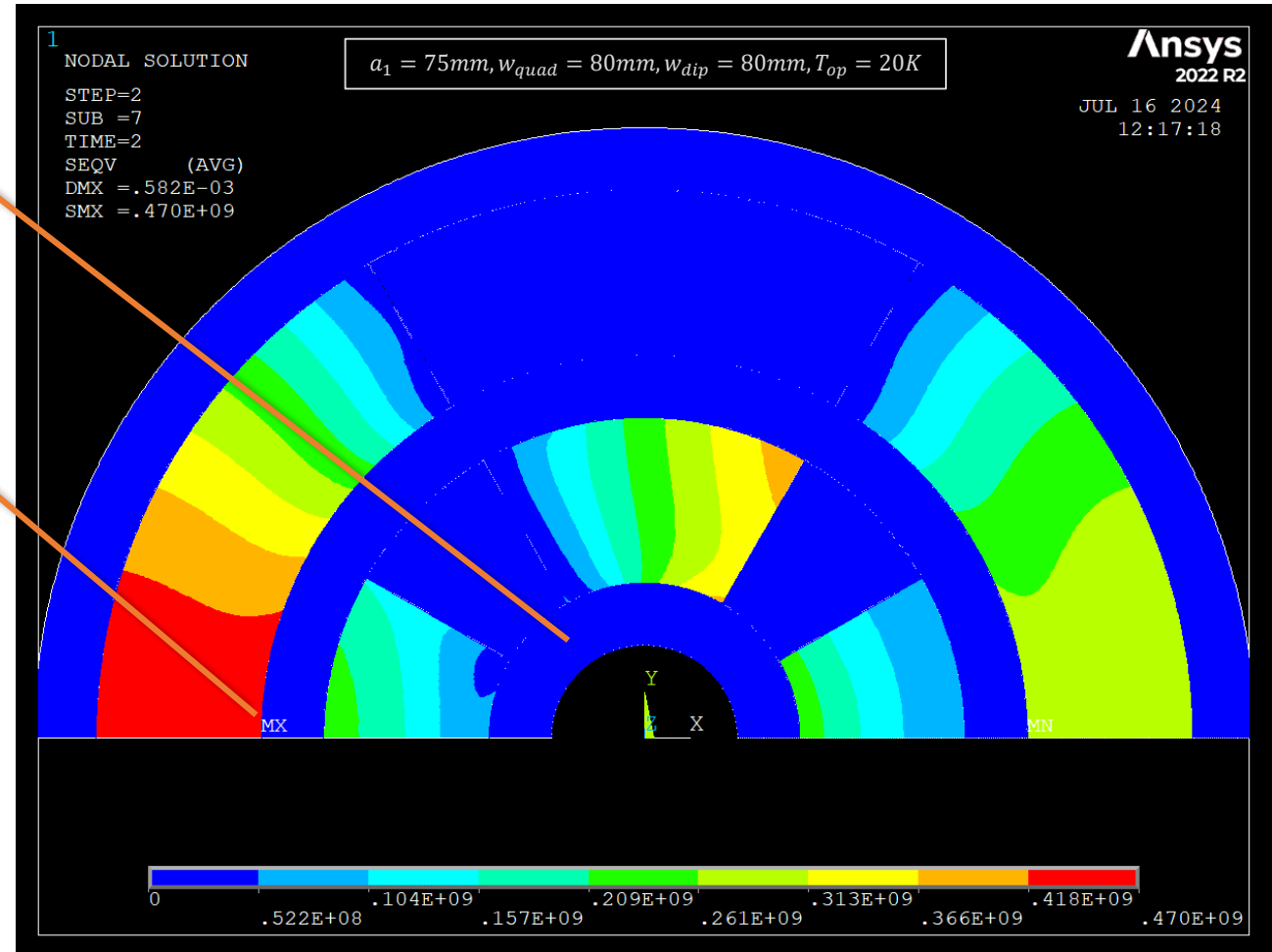
- Zoom-in on the displacements shows that this sector of the quadrupole moves inward



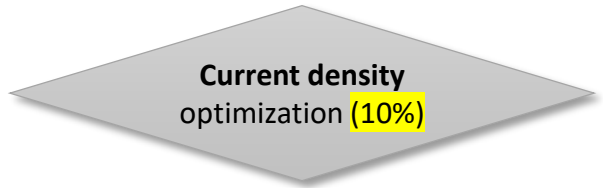
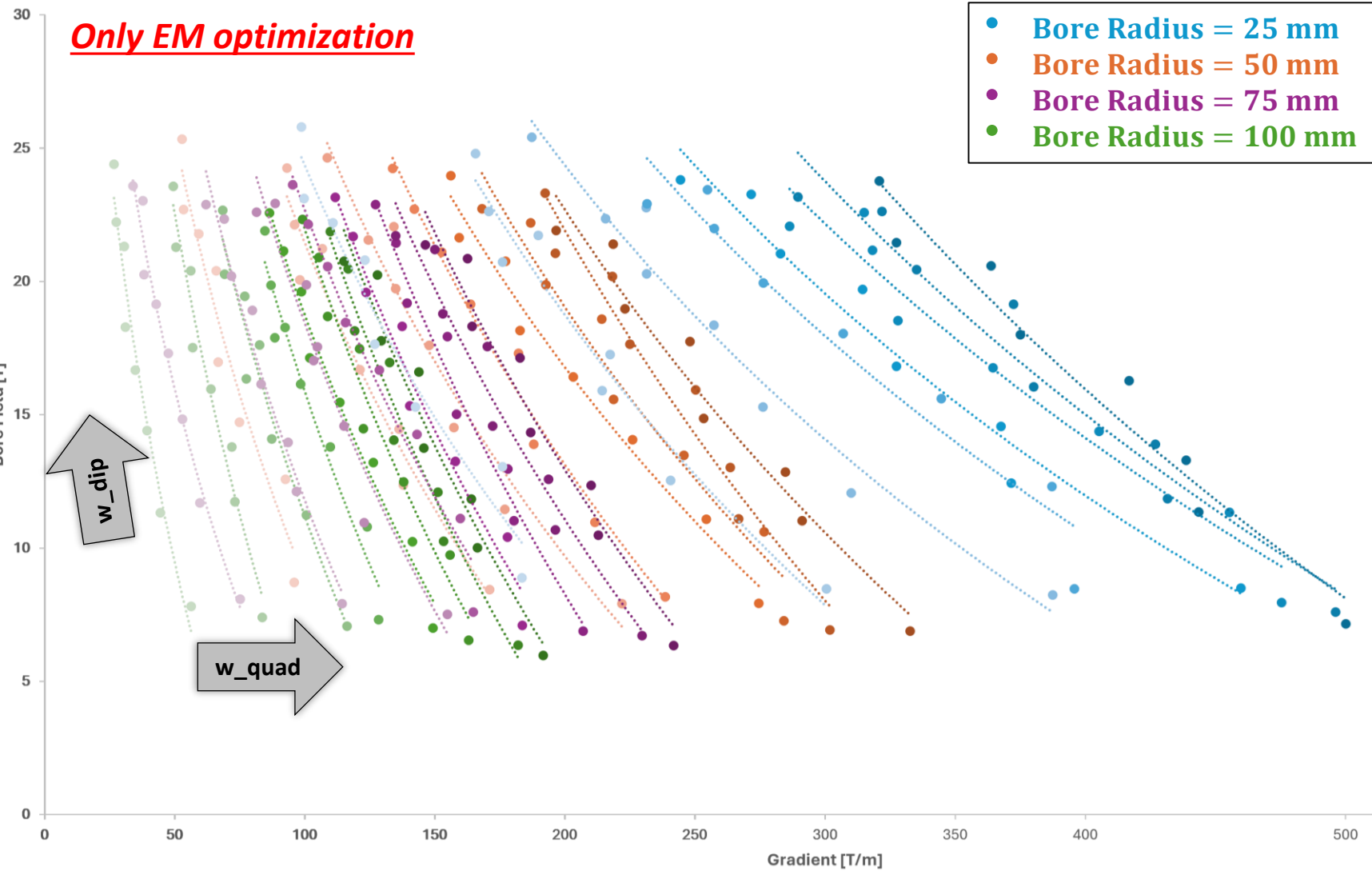
The Von Mises peak stress is on the inner part of the coil



- To address the issue, we insert an **infinitely rigid internal structure** to enable the study of stress behavior in the coils.
- Now the **peak stress**, in the same configuration discussed so far, is on the dipole in compression on the midplane (by changing the parameters, the maximum could be shifted).
- Now that we have a stress distribution in the coils, we can run the code and add a column with the peak stress to the data.
- With all information we will try to create B-G plots for the combined.



B-G plot at 4.5K



Optimize J_{quad} and J_{dip} to be close to the critical current density:

```

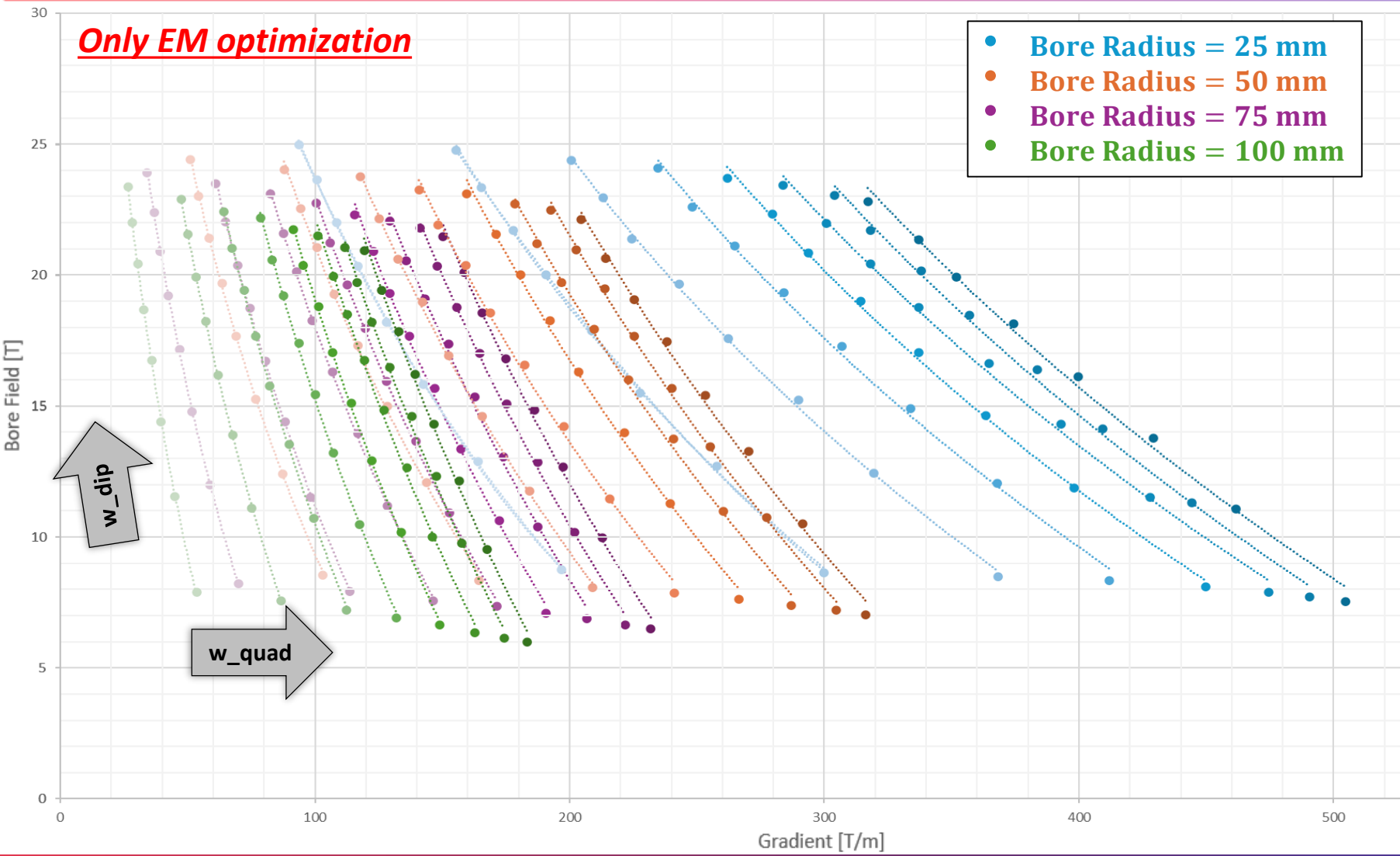
.....
while not ( 0.9 < f < 1.1 ):
.....
    → ANSYS input (a1, w_quad, J_quad, w_dip, J_dip)
    Run ANSYS
    ANSYS output →
    f = J_c (B_peak) / J
    if f > 1: J = J * 1.1
    else: J = J * 0.9
.....
    
```

the optimization acts on J_{quad} and J_{dip} with corrections of 10%, and the cycle closes when either J_{quad} or J_{dip} is within 10% of J_c



What if we performed a 1% optimization ?

B-G plot at 4.5K



Current density
Optimization (1%)

Optimize J_{quad} and J_{dip} to be close to the critical current density:

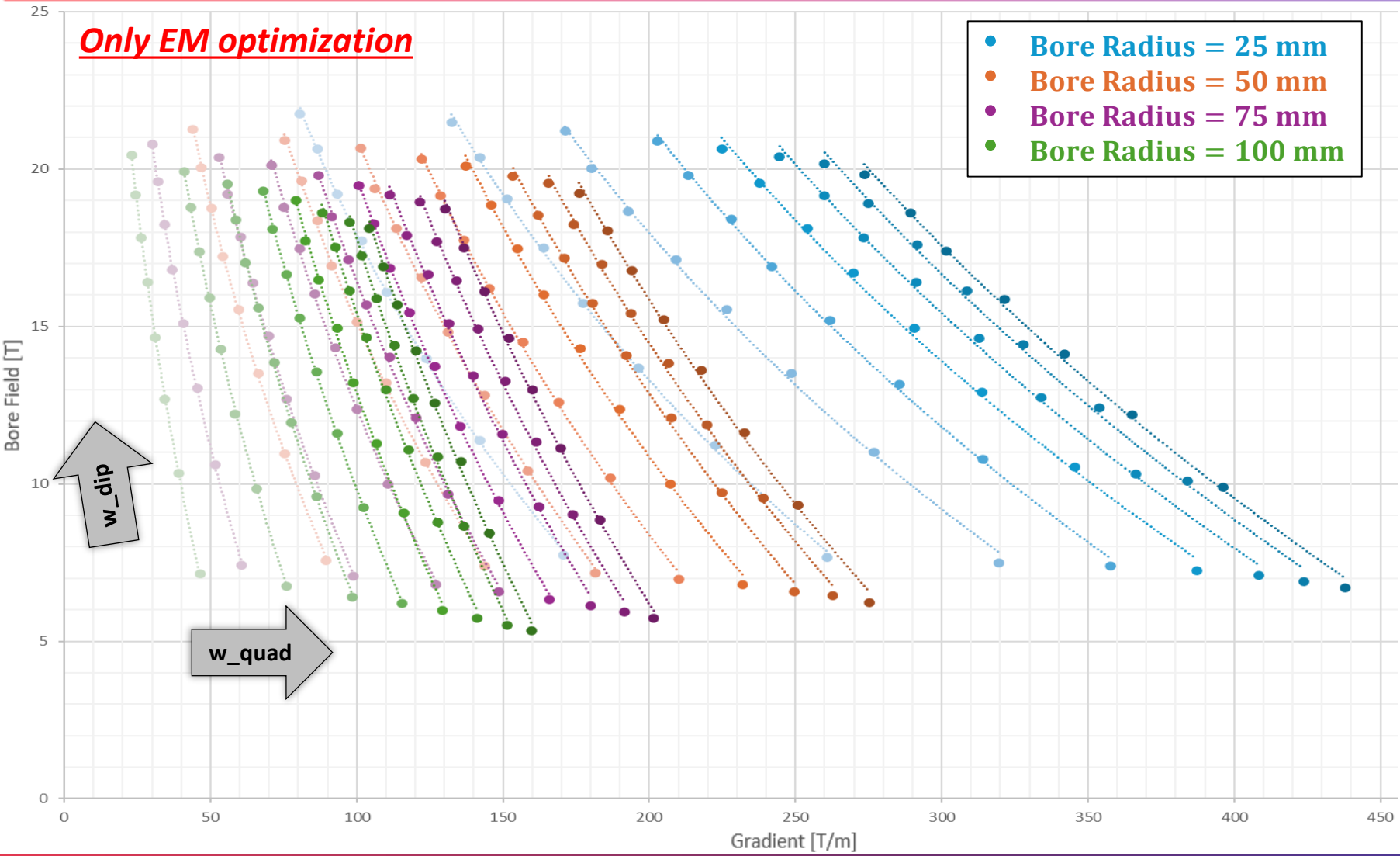
```

....
while not ( 0.99 < f < 1.01 ):
....
  → ANSYS input (a1, w_quad, J_quad, w_dip, J_dip)
  Run ANSYS
  ANSYS output →
  f = J_c (B_peak) / J
  if f > 1: J = J*1.01
  else: J = J*0.99
....
the optimization acts on J_quad and J_dip
with corrections of 1%,
and the cycle closes when either
J_quad or J_dip is within 1% of J_c
  
```



This optimization requires more computational effort, but the result is more understandable graphs.

B-G plot at 10K



Current density
Optimization (1%)

Optimize J_{quad} and J_{dip} to be close to the critical current density:

```

.....
while not ( 0.99 < f < 1.01 ):
.....
    → ANSYS input (a1, w_quad, J_quad, w_dip, J_dip)
    Run ANSYS
    ANSYS output →
    f = J_c (B_peak) / J
    if f > 1: J = J * 1.01
    else: J = J * 0.99
.....

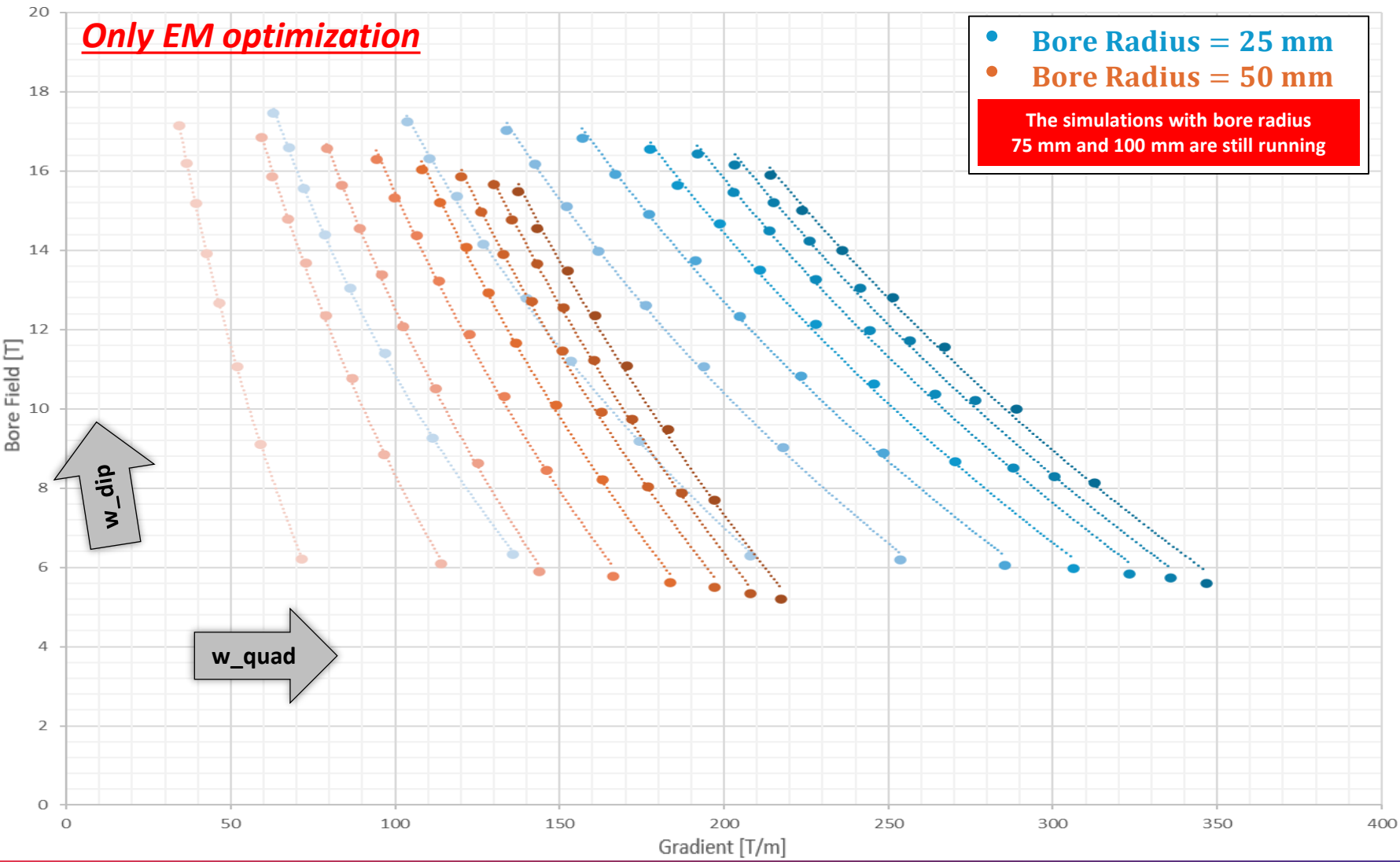
```

the optimization acts on J_{quad} and J_{dip} with corrections of 1%, and the cycle closes when either J_{quad} or J_{dip} is within 1% of J_c



This optimization requires more computational effort, but the result is more understandable graphs.

B-G plot at 20K



Current density Optimization (1%)

Optimize J_{quad} and J_{dip} to be close to the critical current density:

```

....
while not ( 0.99 < f < 1.01 ):
    ....
    → ANSYS input (a1, w_quad, J_quad, w_dip, J_dip)
    Run ANSYS
    ANSYS output →
    f = J_c (B_peak) / J
    if f > 1: J = J * 1.01
    else: J = J * 0.99
    ....
    ....
    
```

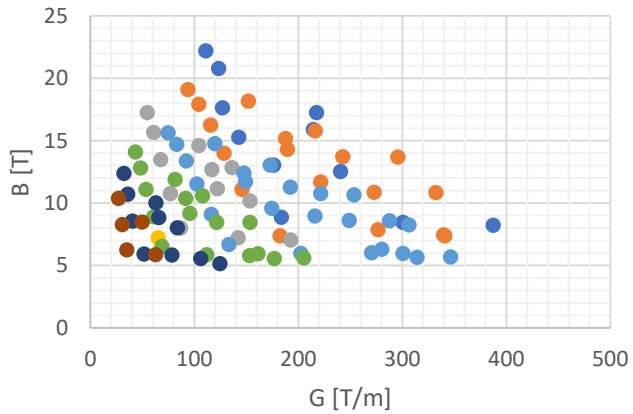
the optimization acts on J_{quad} and J_{dip} with corrections of 1%, and the cycle closes when either J_{quad} or J_{dip} is within 1% of J_c



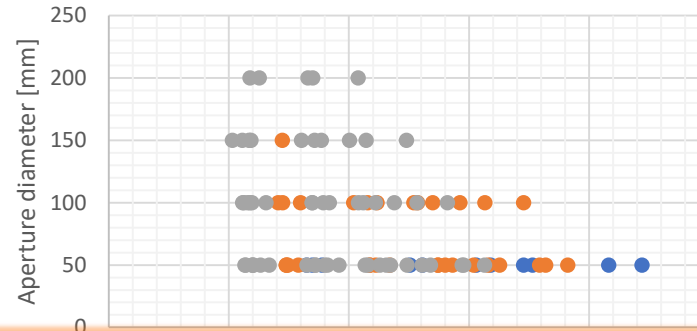
This optimization requires more computational effort, but the result is more understandable graphs.

Manually excluding the points that exceed the cost (400 kEUR/m) and the stress (400 MPa) limits

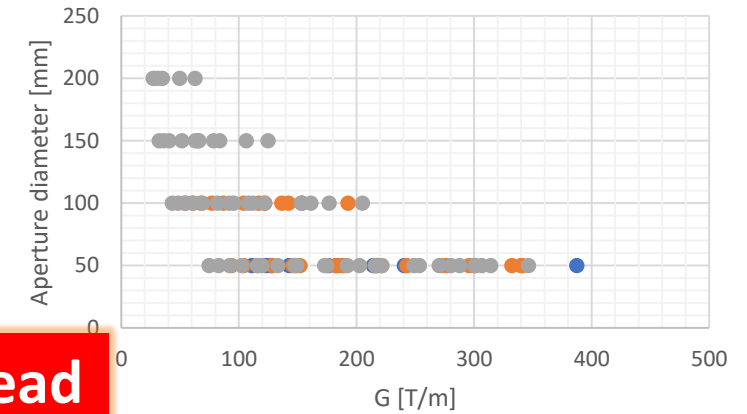
B vs G – Cost and Stress limits



A vs B – Cost and Stress limits

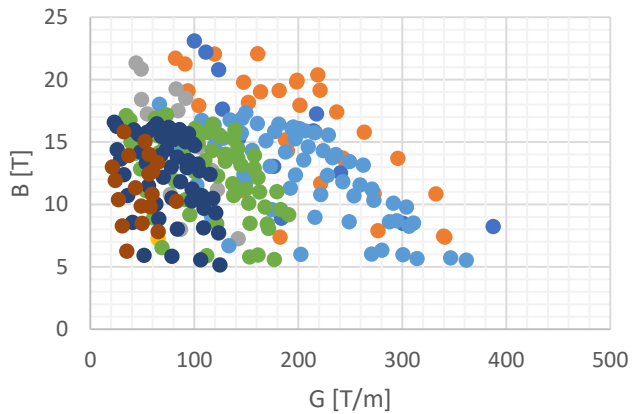


A vs G – Cost and Stress limits

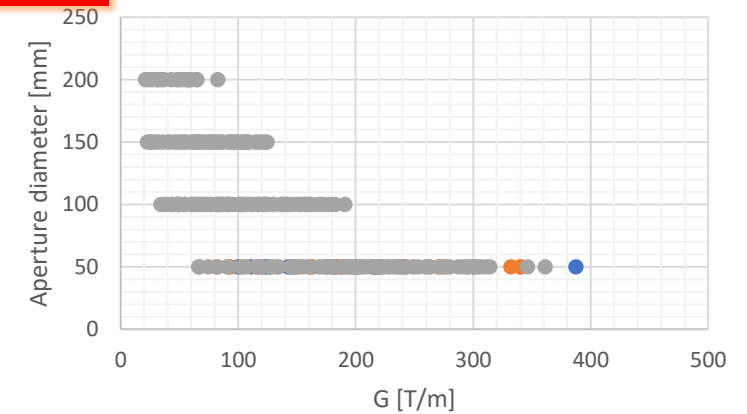
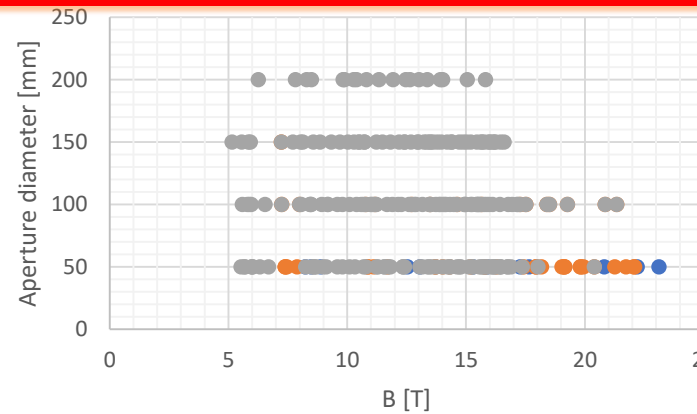


We should optimize the stress instead of excluding the points manually

B vs G – only Stress limit



A vs G – only Stress limit

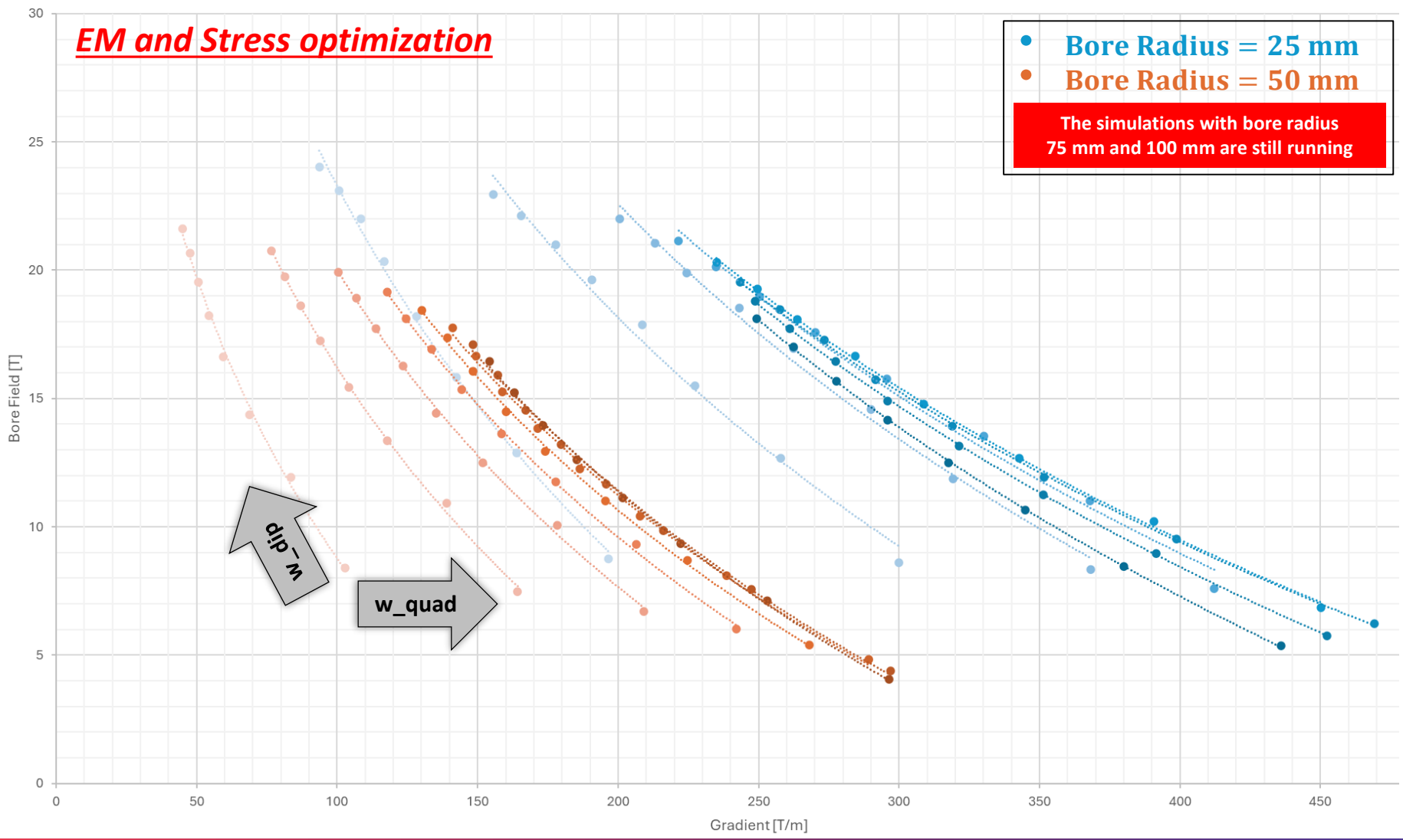


B-G plot at 4.5K

EM and Stress optimization

- Bore Radius = 25 mm
- Bore Radius = 50 mm

The simulations with bore radius 75 mm and 100 mm are still running



Optimize (decrease) J_{quad} and J_{dip} to not exceed the maximum stress (400 MPa)

```

.....
while not ( 0.99 < f < 1.01 ):
.....
  read the J from 1% optimization
  → ANSYS input (a1, w_quad, J_quad, w_dip, J_dip)
  Run ANSYS
  ANSYS output →
  if stress > 400:
    f = 400/stress
    J = J * √f
.....

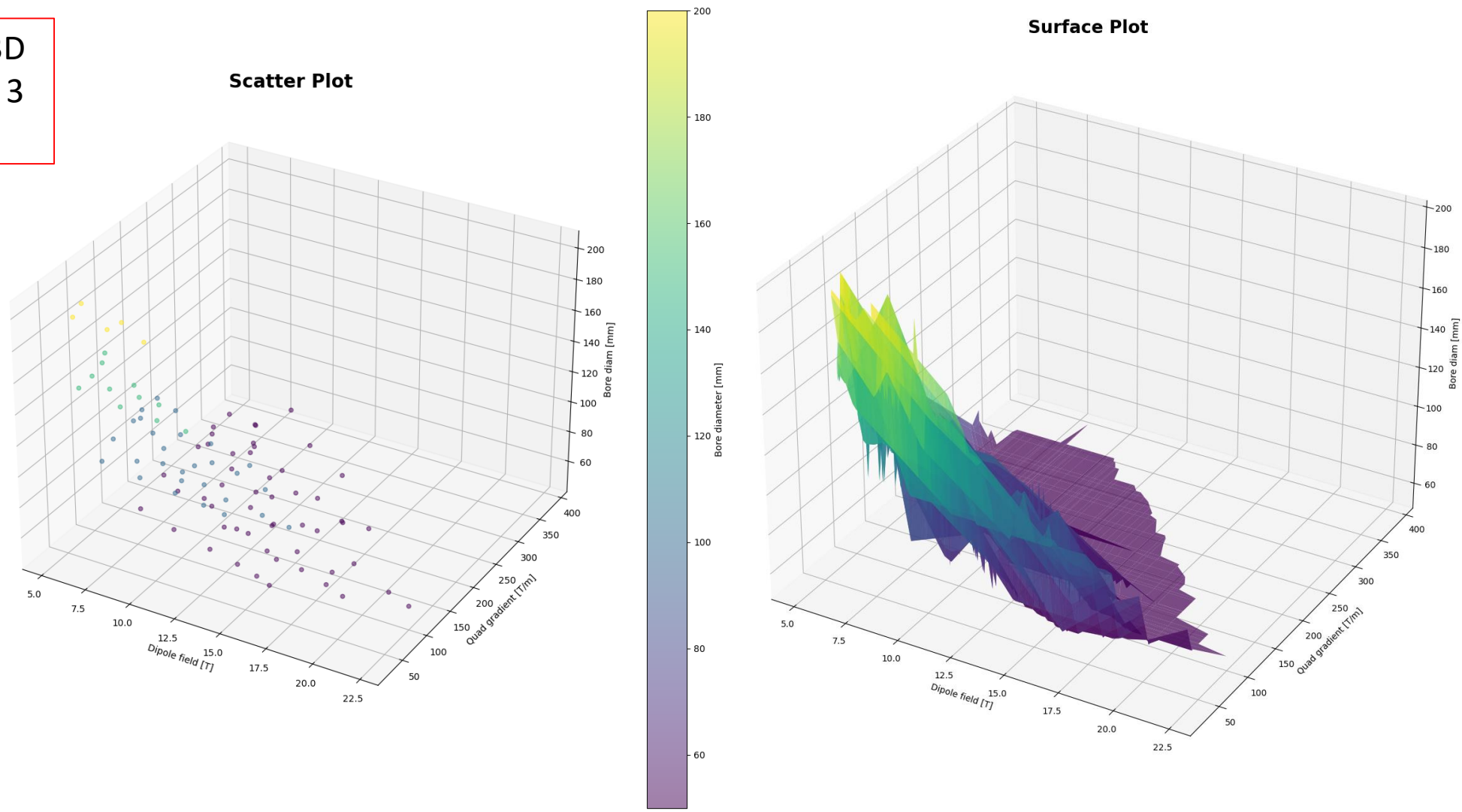
```

the optimization acts on J_{quad} and J_{dip} with quadratic dependence of J on stress, and the cycle closes when the stress is below 400 MPa on both the dipole and the quadrupole.



Limitations on cost are still missing

Is it useful to have a 3D representation of the 3 planes of interest?



Conclusions

- Do we exclude the asymmetric configuration a priori? We have seen the cos-theta, but what about the CCT? The nested configuration may be best for the B-G plot, allowing B2 values greater than B1, but to study specific configurations the asymmetric might be better.
- We inserted an internal support to solve the problem of the coil wanting to enter the aperture. I assumed an internal support with infinitely rigid structure, so the thickness does not matter for the code, but it is relevant to the results. How thick do we consider the inner support?
- The code throws simulations with w from 10 to 80 mm (step 10mm), bore diameter from 50 to 200 (step 50mm). How can we make the graphs more accessible? Could it be useful to add points with w from 1 to 10 mm in 1mm steps? Add aperture points?
- Now I'm considering roebel cable, 150 MPa as Young module of the ReBCO tape, etc. Should I align with the dipole design considerations? What about the protection of these kind of magnets?
- Is it possible to interface the new plots with the old A-B plots? It might be useful to have a relationship between the new work with the old work. Is there a way to analytically assess if we are on the right path with the combined?
- Should we start focusing on a specific configuration? If so, nested or asymmetric?



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THANK YOU FOR YOUR ATTENTION

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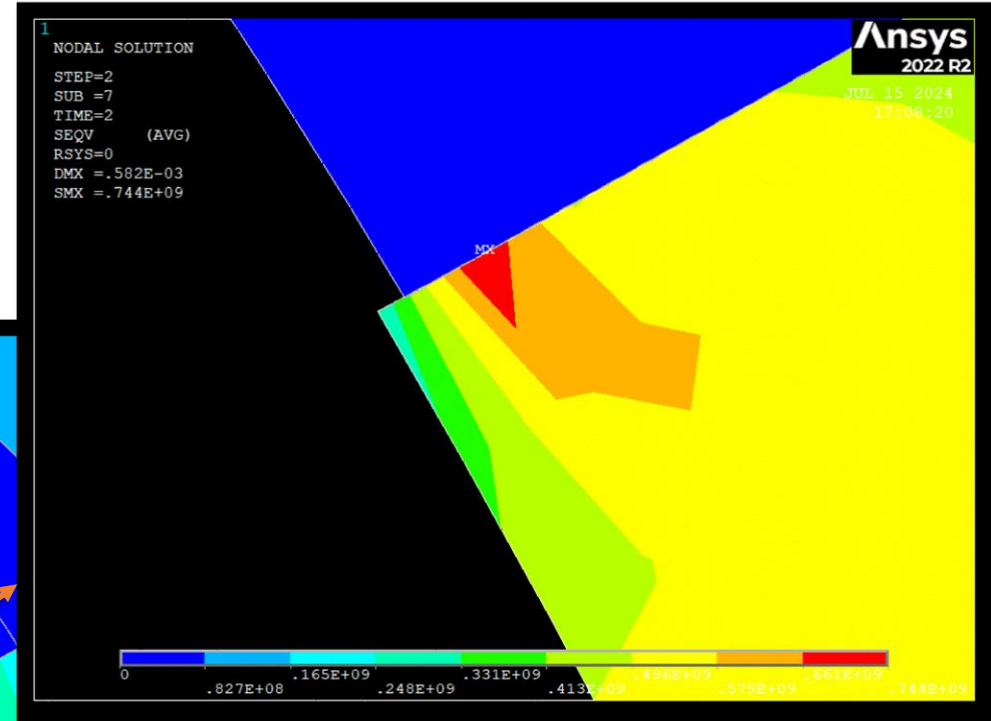
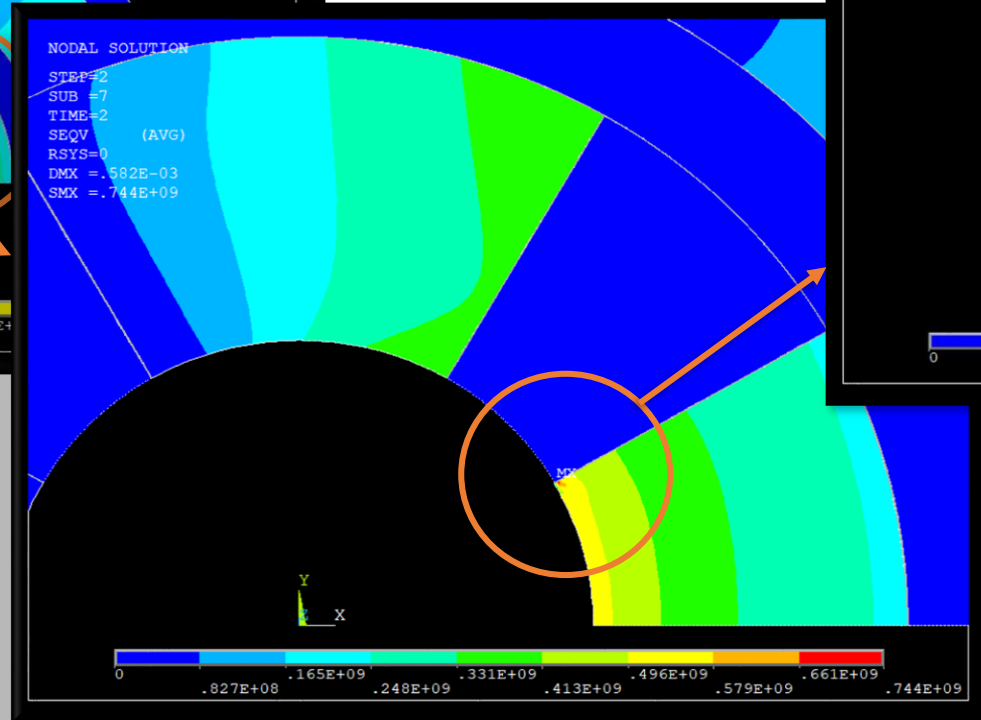
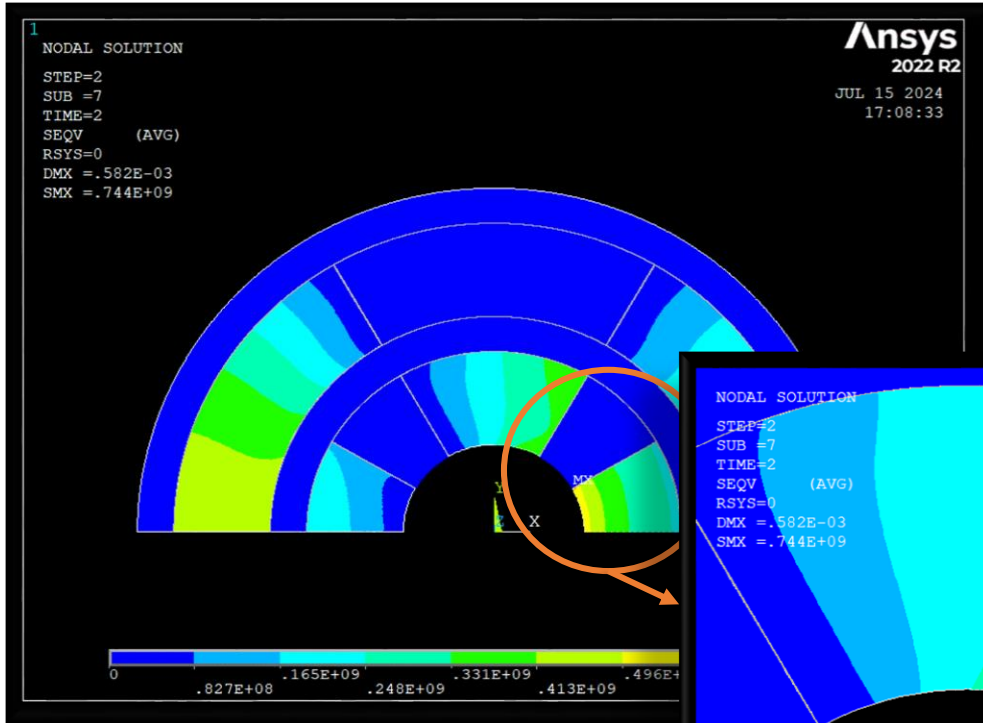
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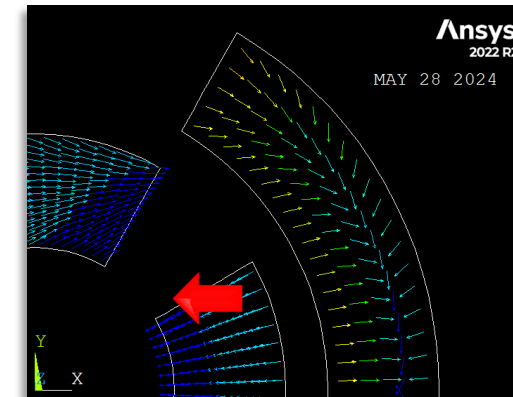
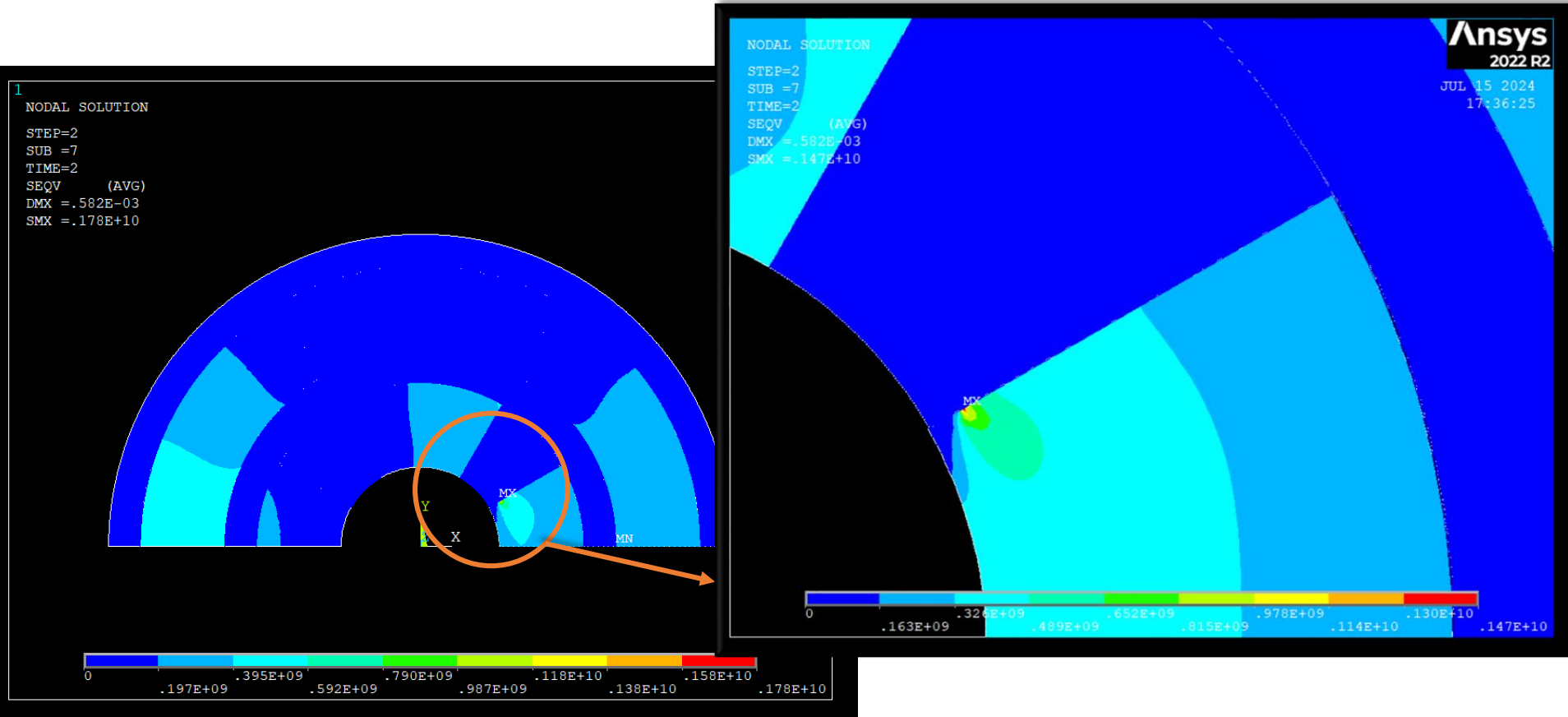
⁴Tampere University

⁵CERN



➤ A “tooth” is formed that undergoes a peak of stress.

➤ If we manually remove the “tooth,” it moves to the first zone not excluded.



➤ This is due to the fact that wedges are infinitely rigid, and the coil wants to move inside.

Bsum + plf2d

