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# Status of $vh@nnlo$ and Plans

VH subgroup meeting: Plans for YR5

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**Part I:**  
**vh@nnlo in a nutshell**

vh@nnlo — Higgs Strahlung at hadron colliders<sup>1</sup>Oliver Brein<sup>a</sup>, Robert V. Harlander<sup>b</sup>, Tom J.E. Zirke<sup>b</sup><sup>a</sup>Großbacher Straße 18, D-67256 Weisenheim am Sand, Germany  
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## Abstract

A numerical program for the evaluation of the inclusive cross section for associated Higgs production with a massive weak gauge boson at hadron colliders is described,  $\sigma(pp/\bar{p}\bar{p} \rightarrow HV)$ ,  $V \in \{W, Z\}$ . The calculation is performed in the framework of the Standard Model and includes next-to-next-to-leading order QCD as well as next-to-leading order electro-weak effects.

**Keywords:** Higgs production; hadron collider; higher orders

## PROGRAM SUMMARY

**Program Title:** vhnlo

**Distribution format:** tar.gz

**Programming language:** Fortran 77, C++.

**Computer:** Personal computer.

**Operating system:** Unix/Linux, Mac OS.

**RAM:** 4 or 100 MB.

**External routines/libraries:** LHAPDF (<http://lhapdf.hepforge.org/>),

CUBA (<http://www.tejrnarts.de/cuba/>)

**Nature of problem:**

Calculation of the inclusive total cross section for associated Higgs- and H- or Z-boson production at hadron colliders through next-to-next-to-leading order QCD.

**Solution method:**

Numerical Monte Carlo integration.

**Running time:**

A few seconds for a single set of parameters.

<sup>1</sup>The program is available from <http://particle.uni-wuppertal.de/harlander/software/vhnlo>.

## vh@nnlo-v2: New physics in Higgs Strahlung

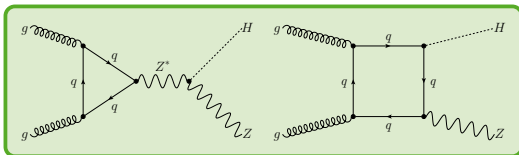
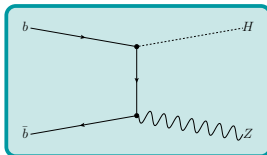
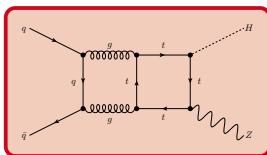
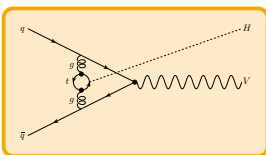
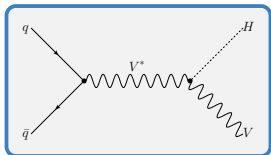
Robert V. Harlander<sup>1</sup>, Jonas Klappert<sup>1</sup>, Stefan Liebler<sup>2</sup>, and Lukas Simon<sup>1</sup><sup>1</sup>Institute for Theoretical Particle Physics and Cosmology,  
RWTH Aachen University, D-52066 Aachen, Germany<sup>2</sup>Institute for Theoretical Physics, Karlsruhe Institute of Technology,  
D-76131 Karlsruhe, Germany

## Abstract

Introducing version 2 of the code `vhnlo` [1], we study the effects of a number of new-physics scenarios on the Higgs-Strahlung process. In particular, the cross section is evaluated within a general 2HDM and the MSSM. While the Drell-Yan-like contributions are consistently taken into account by a simple reweighting of the SM results, the gluon-initiated contribution is supplemented by square-loop mediated amplitudes, and by the  $s$ -channel exchange of additional scalars which may lead to constructive interference effects. The latter holds as well for bottom-quark initiated Higgs-Strahlung, which is also included in the new version of `vhnlo`. Using an orthogonal rotation of the three Higgs CP eigenstates in the 2HDM and the MSSM, `vhnlo` incorporates a simple means of CP mixing in these models. Moreover, the effect of vector-like quarks in the SM on the gluon-initiated contribution can be studied. Beyond concrete models, `vhnlo` allows to include the effect of higher-dimensional operators on the production of CP-even Higgs bosons. Transverse momentum distributions of the final state Higgs boson and invariant mass distributions of the  $V\bar{0}$  final state for the gluon- and bottom-quark initiated contributions can be studied. Distributions for the Drell-Yan-like component of Higgs-Strahlung can be included through a link to `RCF`. `vhnlo` can also be linked to `Pythia8` and `SHiPc` for the calculation of Higgs masses and mixing angles. It can also read these parameters from an SLHA-file as produced by standard spectrum generators. Throughout the manuscript, we highlight new-physics effects in various numerical examples, both at the inclusive level and for distributions.

# VH cross section with vh@nnlo

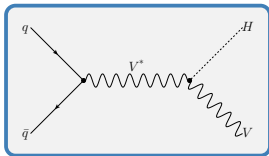
$$\sigma^{VH} = (1 + \delta_{EW}^{VH}) \sigma_{DY}^{VH} + \sigma_I^{VH} + \delta_{VZ} (\sigma_{II}^{ZH} + \sigma_{b\bar{b} \rightarrow ZH} + \sigma_{ggZH})$$



# VH cross section with `vh@nnlo`

Drell-Yan-like contribution

$$\sigma^{VH} = (1 + \delta_{EW}^{VH}) \sigma_{DY}^{VH} + \sigma_I^{VH} + \delta_{VZ} (\sigma_{II}^{ZH} + \sigma_{b\bar{b} \rightarrow ZH} + \sigma_{ggZH})$$



- ▶ **NNLO QCD** corrections have been computed 20 years ago

[Brein, Djouadi, Harlander 2004 (arXiv:hep-ph/0307206)]

- ▶ `vh@nnlo` implementation is based on ZWPROD

[Hamberg, van Neerven, Matsuura 1991]

- ▶ **NLO EW** corrections (including leptonic vector boson decay)

- to inclusive process [Ciccolini, Dittmaier, Krämer 2003 (arXiv:hep-ph/0306234)]

- **HAWK** [Denner, Dittmaier, Kallweit, Mück 2012 (arXiv:1112.5142)]

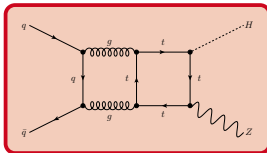
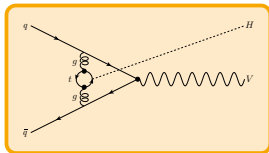
- **HAWK 2.0** [Denner, Dittmaier, Kallweit, Mück 2015 (arXiv:1412.5390)]

„Status of Electroweak Corrections and Plans”

# VH cross section with vh@nnlo

Top-mediated contributions

$$\sigma^{VH} = (1 + \delta_{\text{EW}}^{VH}) \sigma_{\text{DY}}^{VH} + \sigma_{\text{I}}^{VH} + \delta_{\text{VZ}} (\sigma_{\text{II}}^{ZH} + \sigma_{b\bar{b} \rightarrow ZH} + \sigma_{ggZH})$$

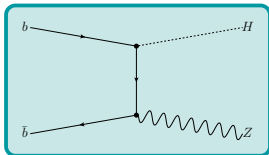


- ▶ top-quark mediated effects with a direct **Higgs-to-top Yukawa coupling** [Brein, Harlander, Wiesemann, Zirke 2012 (arXiv:1111.0761)]
- ▶ corrections of the order of 1 – 3% at LHC energies

# VH cross section with vh@nnlo

Bottom-induced contribution

$$\sigma^{VH} = (1 + \delta_{EW}^{VH}) \sigma_{DY}^{VH} + \sigma_I^{VH} + \delta_{VZ} (\sigma_{II}^{ZH} + \sigma_{b\bar{b} \rightarrow ZH} + \sigma_{ggZH})$$

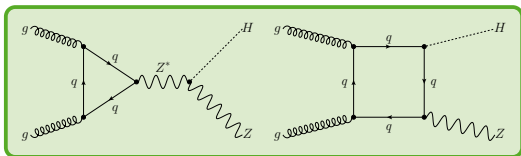


- ▶ only  $b\bar{b}$ -initiated contributions with a direct **Higgs-to-bottom Yukawa coupling**
- ▶ implemented at LO in QCD with massless bottom quarks but non-zero Yukawa coupling
- ▶ contribution negligible in SM (effects at permille level)

# VH cross section with vh@nnlo

Gluon-induced contribution

$$\sigma^{VH} = (1 + \delta_{EW}^{VH}) \sigma_{DY}^{VH} + \sigma_I^{VH} + \delta_{VZ} (\sigma_{II}^{ZH} + \sigma_{b\bar{b} \rightarrow ZH} + \sigma_{ggZH})$$



$$\sigma_{ggZH} = K_{NLO}^{\infty} \sigma_{gg \rightarrow ZH}^{LO} + \sigma_{gg \rightarrow ZH}^{NLL-NLO}$$

- ▶  $K_{NLO}^{\infty}$  is the **NLO K-factor** in the heavy top limit

[Altenkamp, Dittmaier, Harlander, Rzehak, Zirke 2013 (arXiv:1211.5015)]

- ▶  $\sigma_{gg \rightarrow ZH}^{NLL-NLO}$  contains **NLL soft-gluon resummation** effects

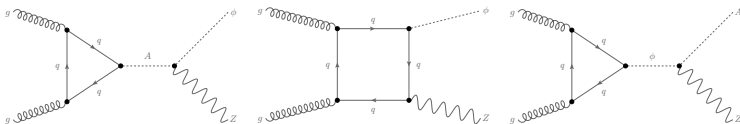
[Harlander, Kulesza, Theeuwes 2014 (arXiv:1410.0217)]



# Beyond the Standard Model

Theories **beyond the Standard Model** in `vh@nnlo`:

- ▶ **Two-Higgs-Doublet Model (2HDM)**

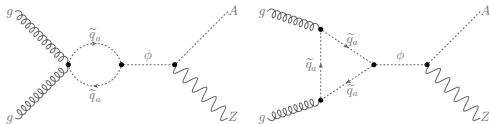


- ▶ **Next-to-Minimal Two-Higgs-Doublet Model (N2HDM)** [not public]
- ▶ **Minimal Supersymmetric Standard Model (MSSM)**
- ▶ **CP-mixing** effects for 2HDM, N2HDM and MSSM
- ▶ **higher-dimensional operators**
- ▶ effects of **vector-like quarks**

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- ▶ Two-Higgs-Doublet Model (**2HDM**)
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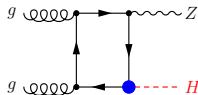
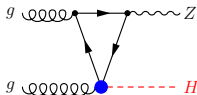
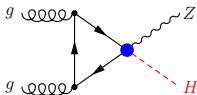
$$\begin{pmatrix} h_1 \\ h_2 \\ h_3 \end{pmatrix} = R \begin{pmatrix} h \\ H \\ A \end{pmatrix}$$

- ▶ **higher-dimensional operators**
- ▶ effects of **vector-like quarks**

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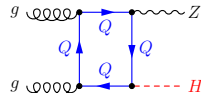
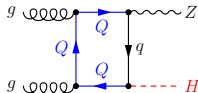
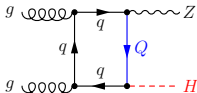


- ▶ effects of **vector-like quarks**

# Beyond the Standard Model

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## Part II:

# Inclusive cross sections for $VH$ production

# WH cross section with leptonic decay

$pp \rightarrow WH \rightarrow \ell\nu H$

Inclusive cross section at **NNLO QCD + NLO EW**

$$\sigma(pp \rightarrow WH \rightarrow \ell\nu H) = ((1 + \delta_{\text{EW}}^{\ell\nu H})\sigma_{\text{DY}}^{\text{WH}} + \sigma_{\text{I}}^{\text{WH}}) \times \text{Br}^{\text{LO}}(W \rightarrow \ell\nu) + \sigma_{\gamma}^{\ell\nu H}$$

## Parameter scan

- ▶ center of mass energies:  $\sqrt{s} \in \{7, 8, 13, 13.6, 14\}$  TeV
- ▶ Higgs masses:  $M_H \in \{120, 122, 124, 124.6, 124.8, 125, 125.09, 125.2, 125.3, 125.38, 125.6, 126, 128, 130\}$  GeV

# WH cross section with leptonic decay

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## vh@nnlo

- ▶ central scales:  $\mu_R = \mu_F = M_{WH}$
- ▶ PDF set: PDF4LHC21\_40

## HAWK 2.0

- ▶ PDF set for computing  $\delta_{EW}$ : PDF4LHC21\_40
- ▶ PDF set for computing  $\sigma_{\gamma}$ : LUXqed17\_plus\_PDF4LHC15\_nnlo\_100



# Uncertainty estimate

$pp \rightarrow WH \rightarrow \ell\nu H$

Uncertainties have been computed following the recommendations for  
„Higgs Production Cross Section for Run III”

1. **QCD scale uncertainty:** 7-point scale variation

$$\frac{1}{3}M_{WH} < \mu_{\text{R}}, \mu_{\text{F}} < 3M_{WH} \quad \wedge \quad \frac{1}{3} < \frac{\mu_{\text{R}}}{\mu_{\text{F}}} < 3$$

2. **PDF uncertainty:** following the [PDF4LHC recommendation](#) for a symmetric Hessian PDF set
3.  $\alpha_s$  **uncertainty:** we have varied  $\alpha_s(M_Z) = 0.1180 \pm 0.0010$  (as provided by the PDF set)

Note: Uncertainties have not been computed for the photon induced contribution  $\sigma_\gamma$ .

# VH cross section values

$$\sqrt{s} = 13.6 \text{ TeV}, \quad M_H = 125.09 \text{ GeV}$$

	$\sigma$ [pb]	scale [%]	PDF [%]	$\alpha_s$ [%]	PDF+ $\alpha_s$ [%]
$\ell^+ \nu H$	0.10180	+0.49 -0.74	1.69	0.54	1.78
$\ell^- \bar{\nu} H$	0.064475	+0.42 -0.66	1.73	0.54	1.81
$W^+ H$	0.89750	+0.51 -0.77	1.76	0.57	1.85
$W^- H$	0.56684	+0.43 -0.69	1.81	0.57	1.90

	$\sigma$ [pb]	scale [%]	PDF [%]	$\alpha_s$ [%]	PDF+ $\alpha_s$ [%]
$\ell^+ \ell^- H$	0.032152	+3.90 -3.27	1.52	0.50	1.60
$\nu \bar{\nu} H$	0.19111	+3.89 -3.26	1.52	0.50	1.60
$ZH$	0.95187	+3.92 -3.28	1.53	0.50	1.61

# **Part III: Beyond vh@nnlo**

## Production cross section at $N^3LO$

- ▶ inclusive cross section and invariant mass distribution for  $DY$ -like contributions available in literature [Baglio, Duhr, Mistlberger, Szafron 2022 (arXiv:2209.06138)]
- ▶ public code `n3loxS` available

## Fully-differential cross sections at NNLO

fully-differential cross sections at NNLO (including various decay channels of the Higgs and/or vector boson)

- ▶ for  $WH$  production [Ferrera, Grazzini, Tramontano 2014 (arXiv:1312.1669)]
- ▶ for  $ZH$  production [Ferrera, Grazzini, Tramontano 2015 (arXiv:1407.4747)]
- ▶ for  $VH$  production [Ferrera, Somogyi, Tramontano 2018 (arXiv:1705.10304)]
- ▶ with Nested Soft-Collinear Subtraction [Caola, Melnikov, Röntsch 2019 (arXiv:1902.02081)]
  - we also have an implementation based on Nested Soft-Collinear Subtraction for fully-differential  $VH$  cross sections
- ▶ many more ...

**Backup**

# WH cross section

$pp \rightarrow WH$

Inclusive cross section at **NNLO QCD + NLO EW**

$$\sigma(pp \rightarrow WH) = (1 + \delta_{\text{EW}}^{WH})\sigma_{\text{DY}}^{WH} + \sigma_{\text{I}}^{WH}$$

with

$$\delta_{\text{EW}}^{WH} = (1 + \delta_{\text{EW}}^{\ell\nu H}) \frac{\text{Br}^{\text{LO}}(W \rightarrow \ell\nu)}{\text{Br}^{\text{NLO}}(W \rightarrow \ell\nu)} - 1$$

Note: Photon induced contribution has not been included.

# ZH cross section with leptonic decay

$pp \rightarrow ZH \rightarrow \ell\ell Z$

Inclusive cross section at **NNLO QCD + NLO EW**

$$\sigma(pp \rightarrow ZH \rightarrow \ell\ell H) = ((1 + \delta_{EW}^{\ell\ell H})\sigma_{DY}^{ZH} + \sigma_I^{ZH} + \sigma_{II}^{ZH} + \sigma_{ggZH}) \\ \times \text{Br}^{\text{LO}}(Z \rightarrow \ell\ell) + \sigma_{\gamma}^{\ell\ell H}$$

## vh@nnlo

- ▶ central scales:  $\mu_R = \mu_F = M_{ZH}$
- ▶ PDF set: PDF4LHC21\_40

## HAWK 2.0

- ▶ PDF set for computing  $\delta_{EW}$ : PDF4LHC21\_40
- ▶ PDF set for computing  $\sigma_{\gamma}$ : LUXqed17\_plus\_PDF4LHC15\_nnlo\_100

# Uncertainty estimate

$pp \rightarrow ZH \rightarrow \ell\ell H$

Uncertainties have been computed following the recommendations for  
„[Higgs Production Cross Section for Run III](#)”

## 1. QCD scale uncertainty: 7-point scale variation

$$\frac{1}{3}M_{ZH} < \mu_{\text{R}}, \mu_{\text{F}} < 3M_{ZH} \quad \wedge \quad \frac{1}{3} < \frac{\mu_{\text{R}}}{\mu_{\text{F}}} < 3$$

## 2. PDF uncertainty: following the [PDF4LHC recommendation](#) for a symmetric Hessian PDF set

## 3. $\alpha_s$ uncertainty: we have varied $\alpha_s(M_Z) = 0.1180 \pm 0.0010$ (as provided by the PDF set)

Note: Only QCD scale uncertainty, but no PDF and  $\alpha_s$  uncertainties, have been computed for the resummation contribution  $\sigma_{gg \rightarrow ZH}^{\text{NLL-NLO}}$ . Moreover, uncertainties have not been computed for the photon induced contribution  $\sigma_\gamma$ .



# ZH cross section with leptonic decay

$$pp \rightarrow ZH \rightarrow \ell\ell H$$

Inclusive cross section at **NNLO QCD + NLO EW**

$$\sigma(pp \rightarrow ZH) = (1 + \delta_{\text{EW}}^{\text{ZH}})\sigma_{\text{DY}}^{\text{ZH}} + \sigma_{\text{I}}^{\text{ZH}} + \sigma_{\text{II}}^{\text{ZH}} + \sigma_{gg\text{ZH}}$$

with

$$\delta_{\text{EW}}^{\text{ZH}} = \frac{1}{2} \left[ (1 + \delta_{\text{EW}}^{\ell\ell H}) \frac{\text{Br}^{\text{LO}}(Z \rightarrow \ell\ell)}{\text{Br}^{\text{NLO}}(Z \rightarrow \ell\ell)} - 1 \right. \\ \left. + (1 + \delta_{\text{EW}}^{\nu\nu H}) \frac{\text{Br}^{\text{LO}}(Z \rightarrow \nu\nu)}{\text{Br}^{\text{NLO}}(Z \rightarrow \nu\nu)} - 1 \right]$$

Note: Photon induced contribution has not been included.