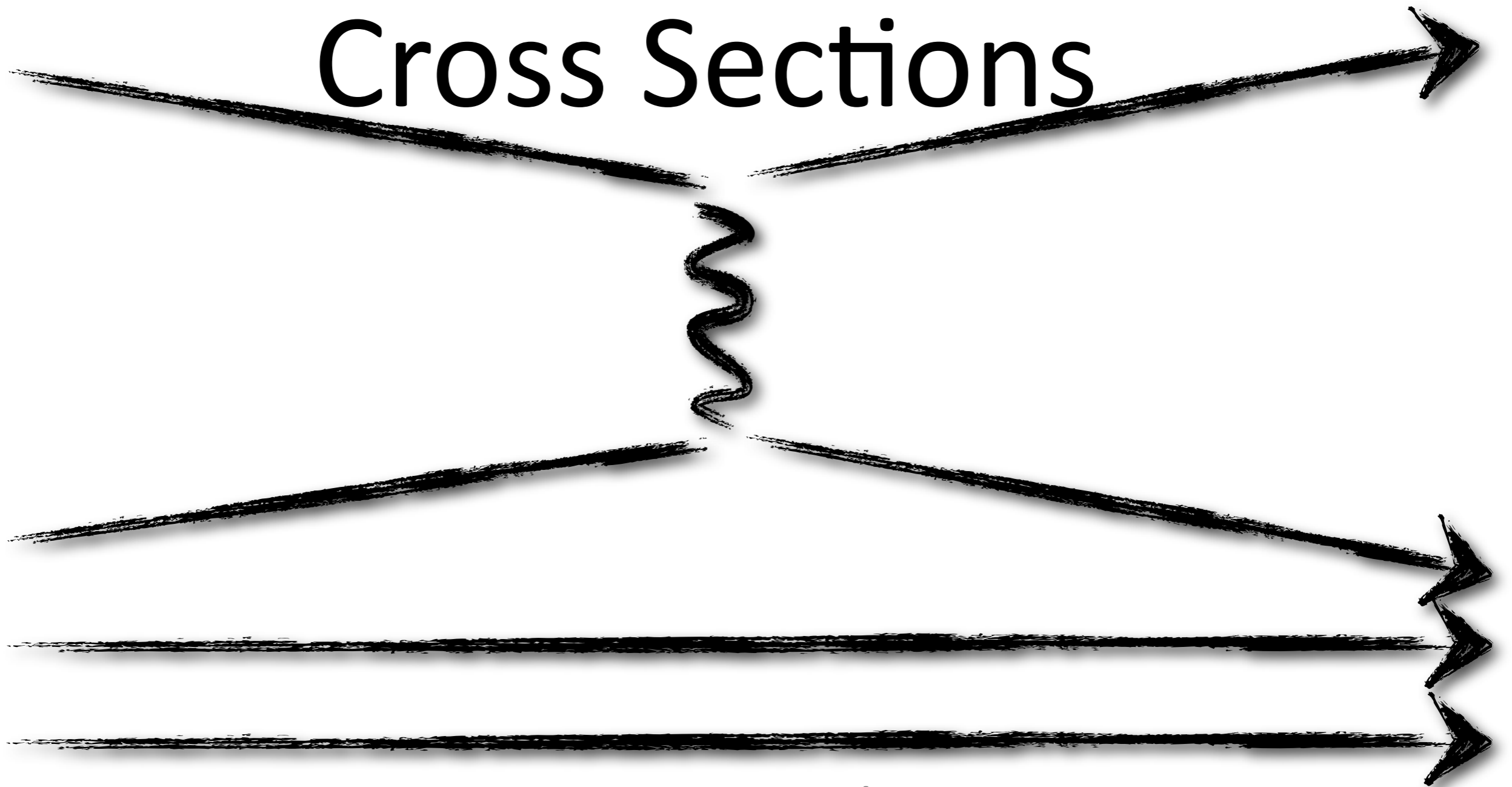


Introduction to

Neutrino Interaction Cross Sections



Morgan Wascko

International Neutrino Summer School 2011

2011 07 23

Outline

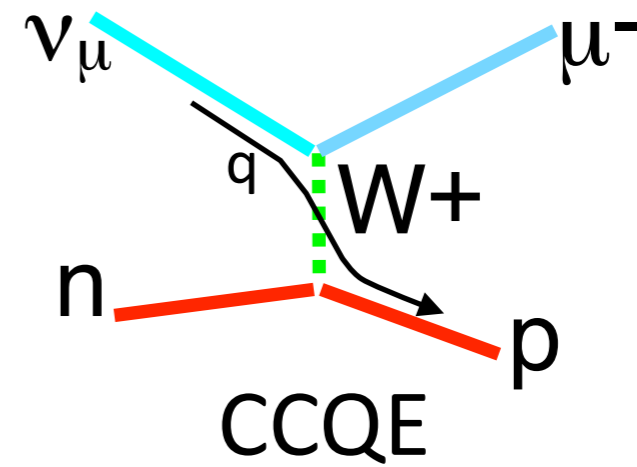
- Introduction to cross section calculations
- Focus on charged current quasi-elastic scattering
- Introduction to cross section experiments
 - Connections to neutrino oscillations
- Focus on CCQE

Lecture 1

Lecture 2

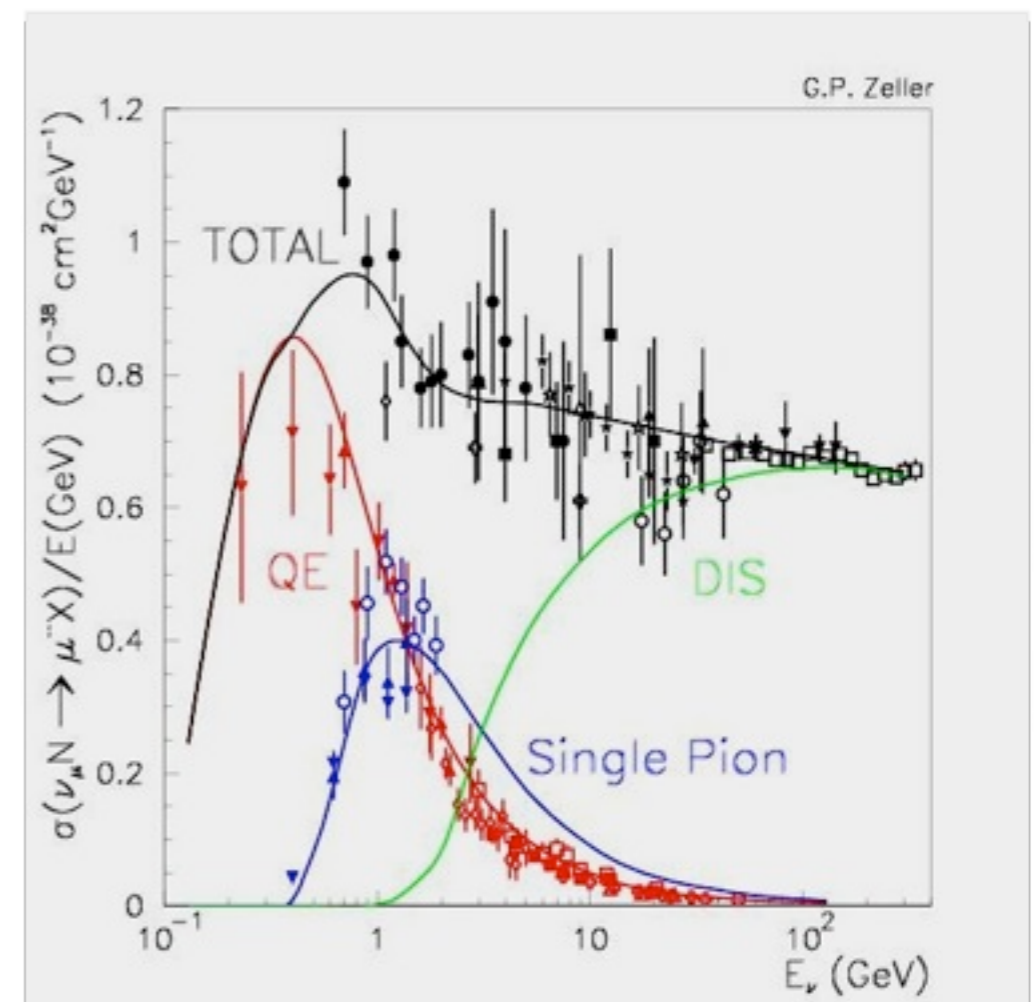
Quasi-Elastic Scattering

- Described by Llewellyn-Smith formalism
- Form-factors parameterise nucleon weak charge distributions
- F_V measured by electron scattering, F_P negligible due to kinematics, F_A assumed to be dipole
- Important for accelerator ν beams
 - Dominant process near 1 GeV
 - Simple energy reconstruction



$$F_A(Q^2) = \frac{F_A(0)}{\left(1 - \frac{Q^2}{M_A^2}\right)^2}$$

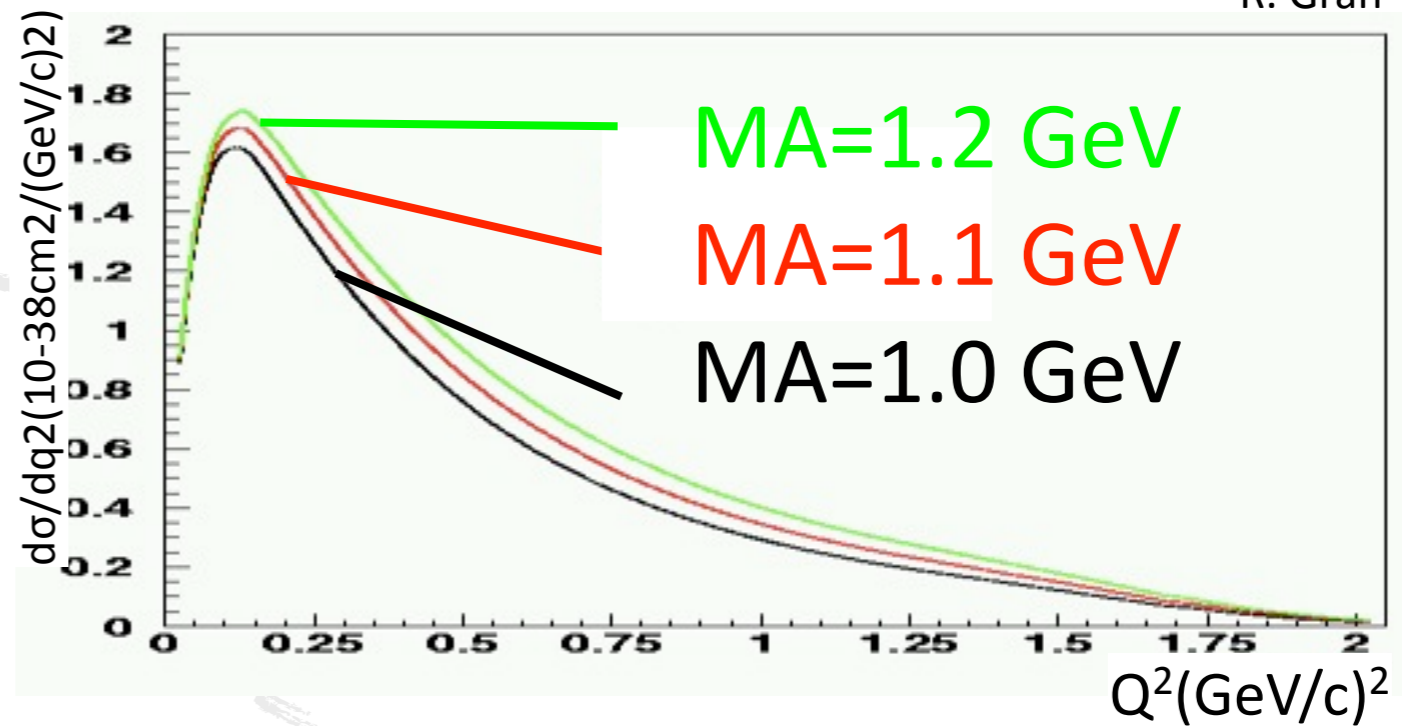
(where $Q^2 = -q^2$)



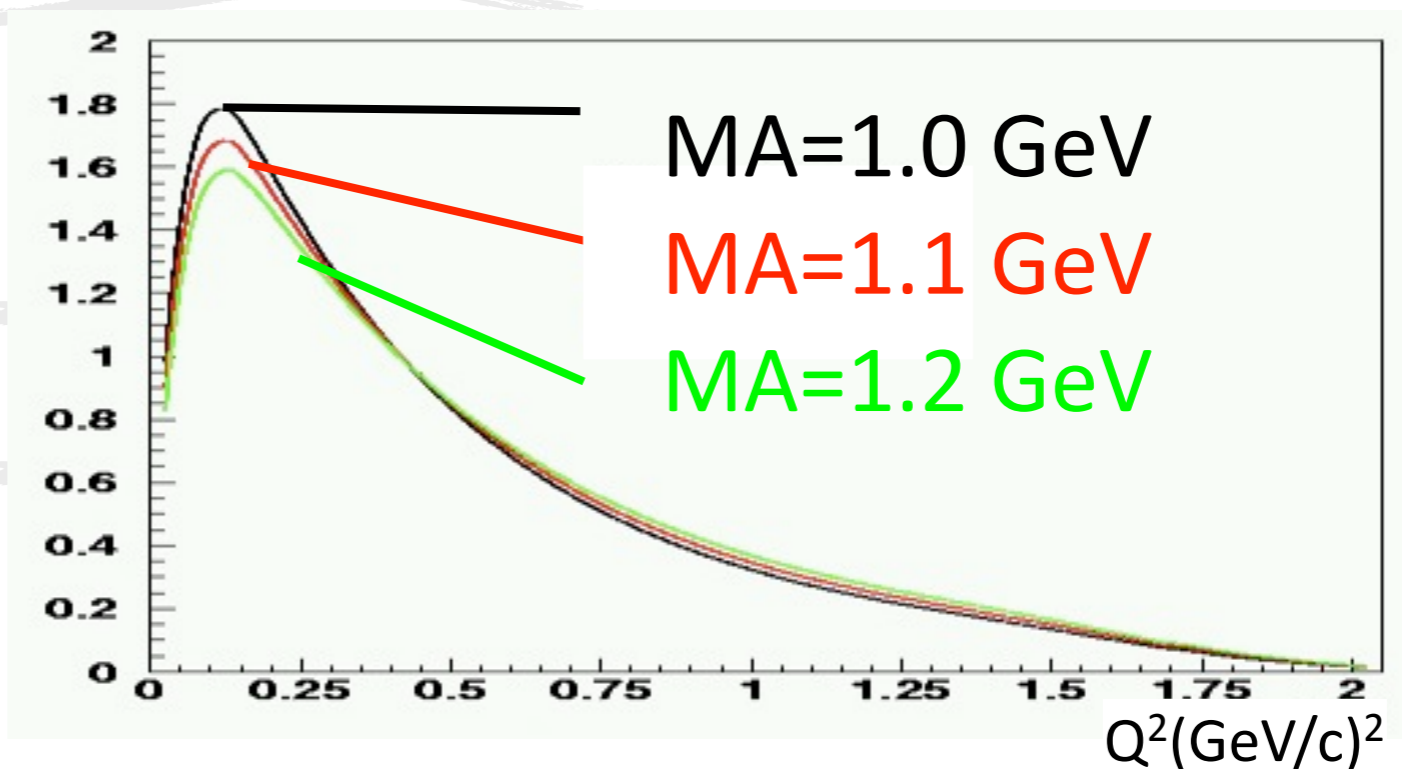
Importance of M_A

R. Gran

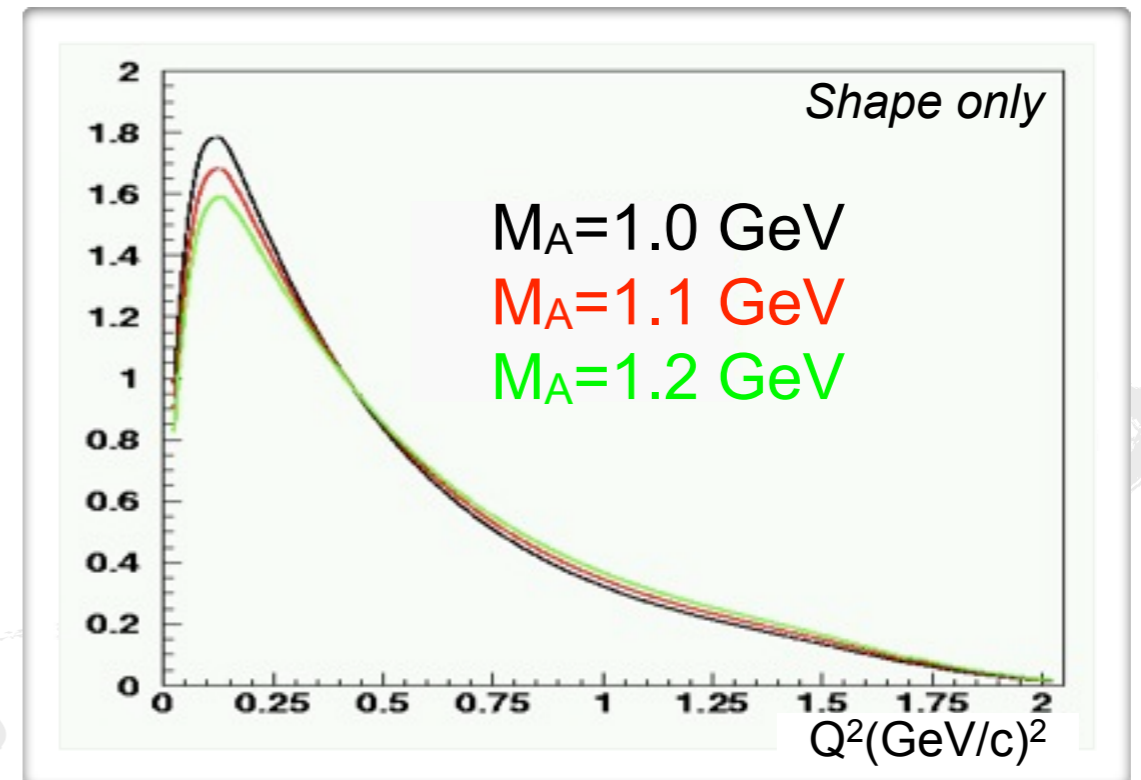
Absolute
Cross-section
(includes normalisation)



Shape only



M_A fit results



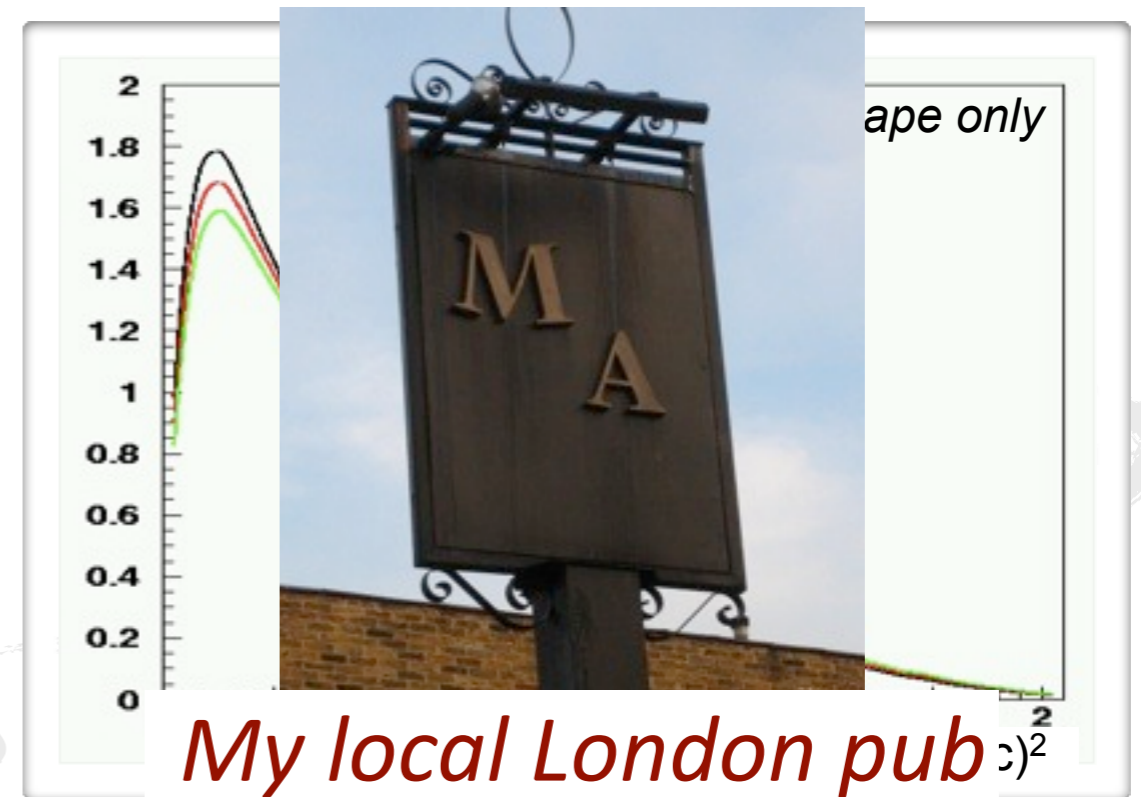
Courtesy of R. Gran

- Value of M_A changes scale & shape of Q^2 distribution
- Recent measurements at low energy on nuclear targets favour high value of M_A
 - But not at high energy!
- Also show increased suppression at low Q^2
- F_A : not dipole form factor?
 - Is M_A an effective parameter?

Experiment	M_A Value (GeV)
World Average(n,p)	1.03 ± 0.03
K2K SciFi (O)	1.20 ± 0.12
K2K SciBar (C)	1.14 ± 0.10
MiniBooNE (C)	1.35 ± 0.17
MINOS (Fe)	1.19 ± 0.17
NOMAD (C)	1.05 ± 0.06

M_A fit results

- Value of M_A changes scale & shape of Q^2 distribution
- Recent measurements at low energy on nuclear targets favour high value of M_A
 - But not at high energy!
- Also show increased suppression at low Q^2
- F_A : not dipole form factor?
 - Is M_A an effective parameter?

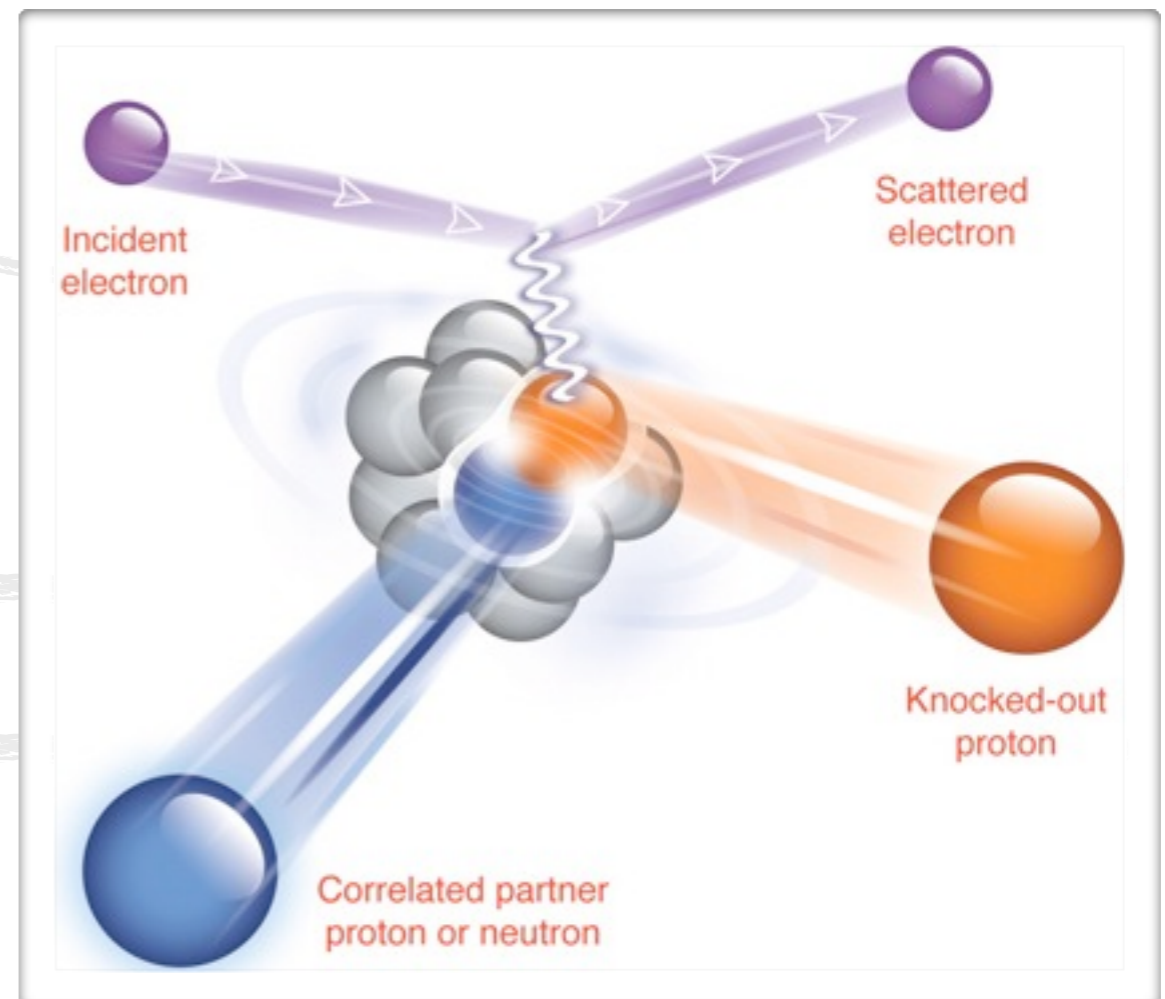
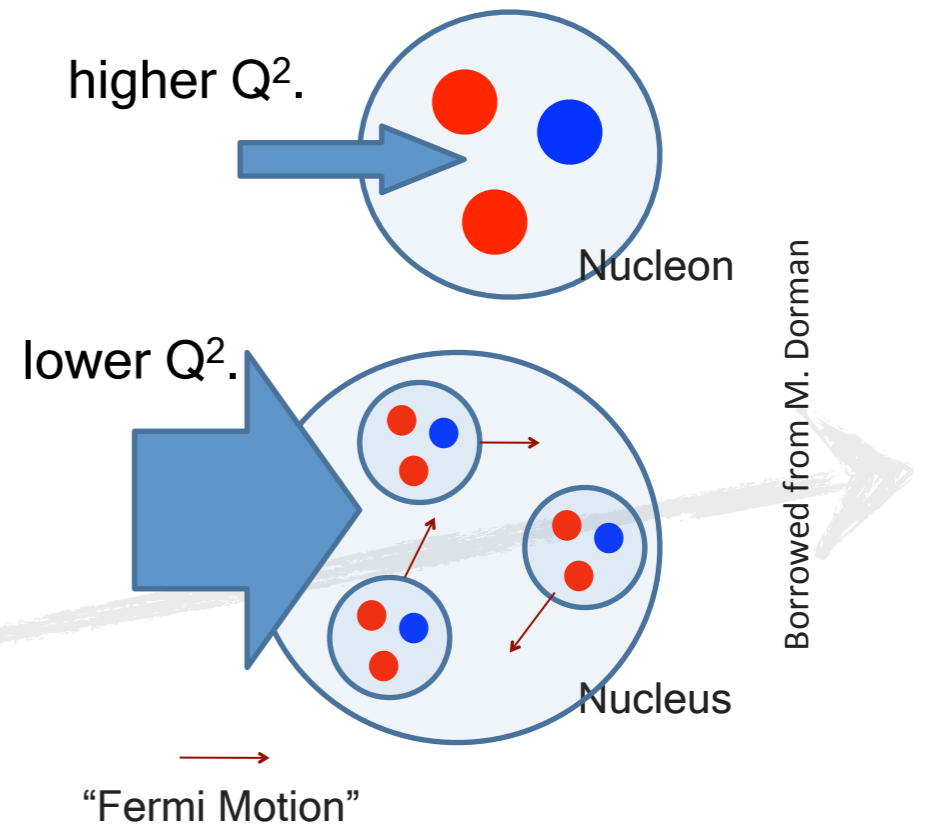


Courtesy of R. Gran

Experiment	M_A Value (GeV)
World Average(n,p)	1.03 ± 0.03
K2K SciFi (O)	1.20 ± 0.12
K2K SciBar (C)	1.14 ± 0.10
MiniBooNE (C)	1.35 ± 0.17
MINOS (Fe)	1.19 ± 0.17
NOMAD (C)	1.05 ± 0.06

Impulse approximation

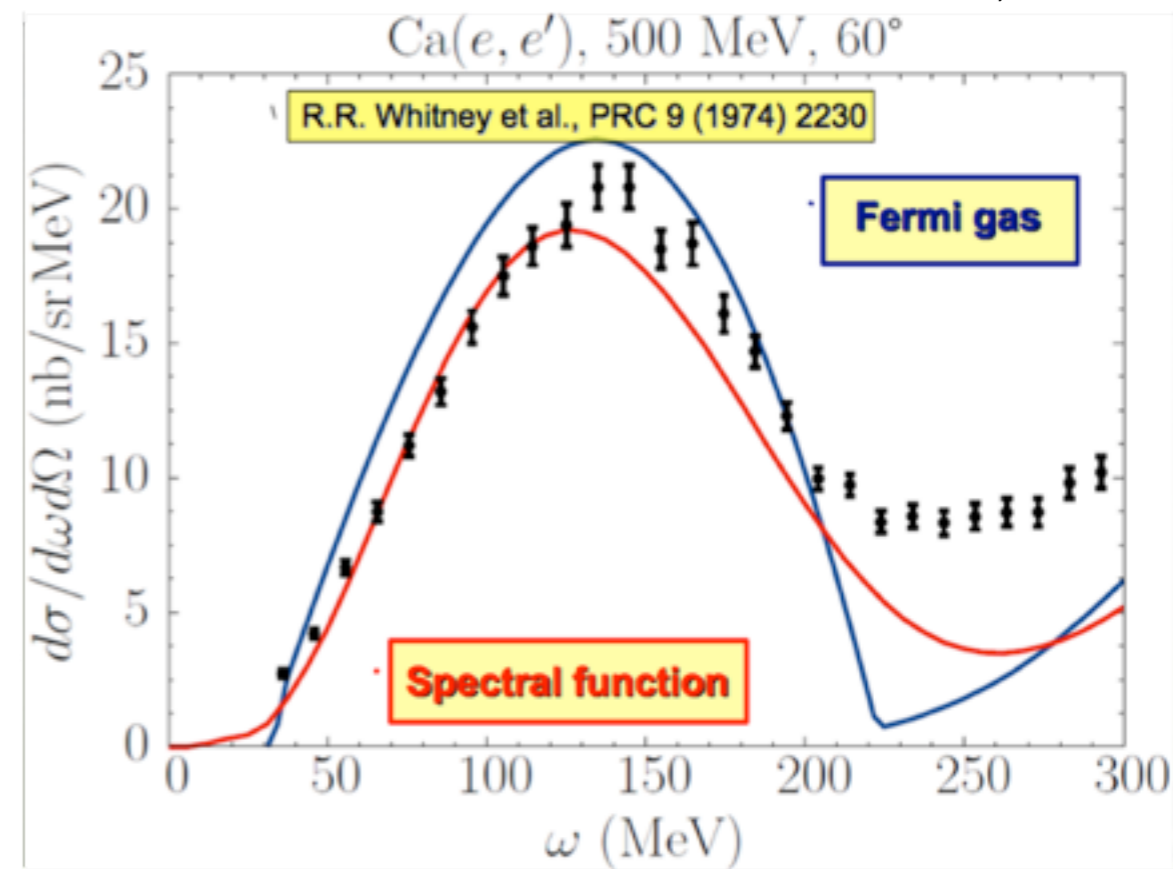
- Assume interaction involves only one nucleon
 - $\lambda > 1 \text{ fm}$ for $Q^2 < 1 (\text{GeV}/c)^2$
- Neutrino experiments assume quasi-free interactions
 - Are nucleons actually quasi-free? If not, could we tell?
- Can low Q^2 region be described by impulse approximation?



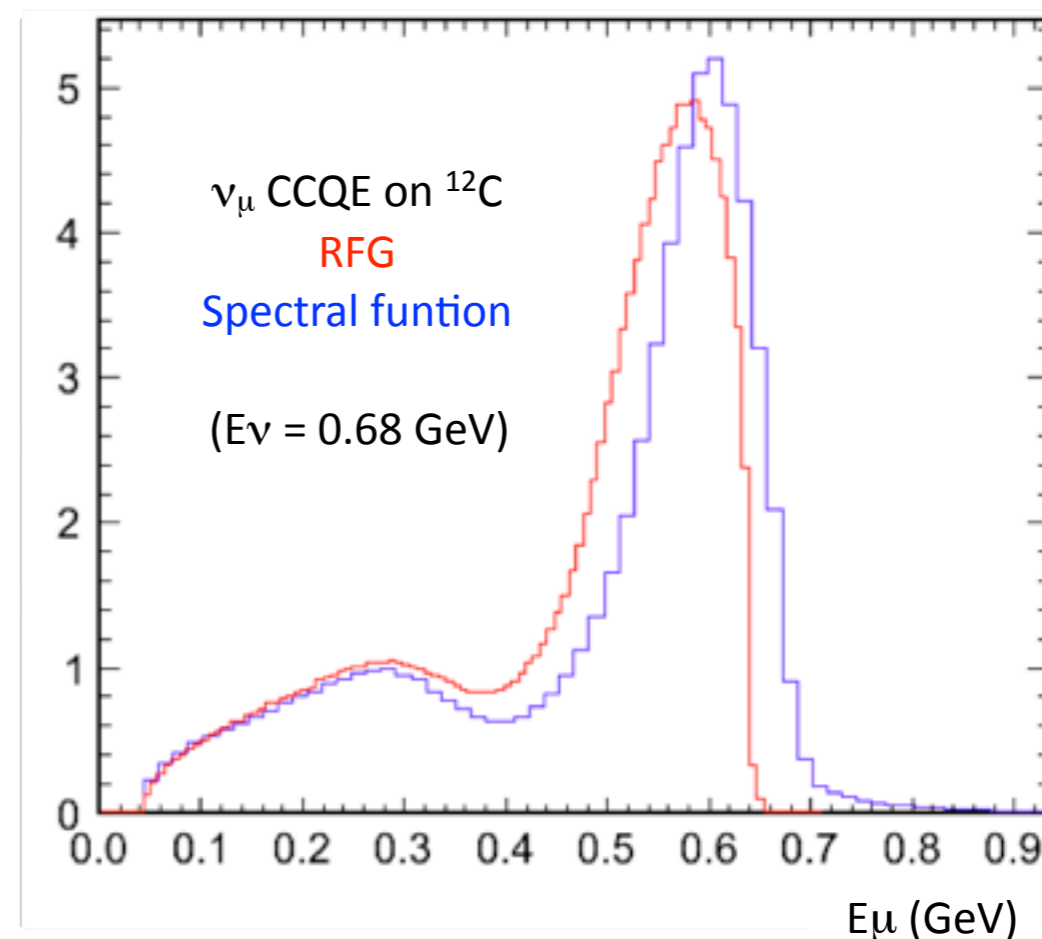
[Science Vol.320. no.5882. pp.1476](#)

Nuclear Models

- Most experiments use RFG
 - Most theorists prefer something else
 - Effects neutrino energy reconstruction!
- ➔ Impacts oscillation experiment!




Prouse (Imperial College London)

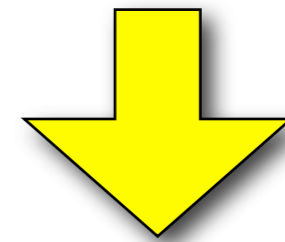


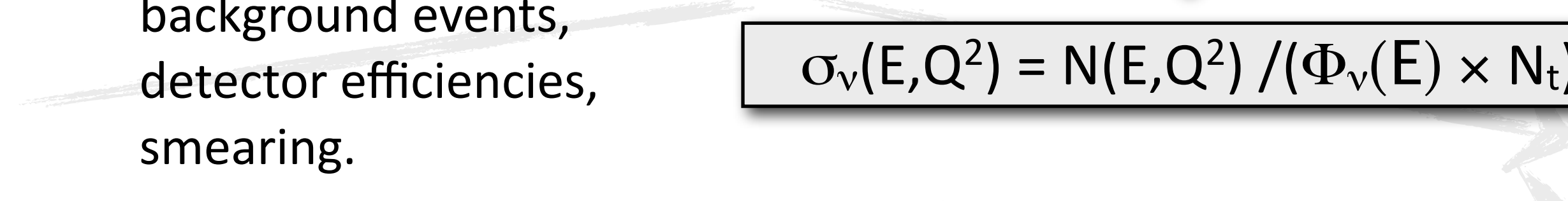
Recent Measurements

Measuring a cross section

- We actually measure an event rate.
- No problem, we can solve for the cross section.
- Need to correct for background events, detector efficiencies, smearing.
- Need to calculate neutrino flux!


$$N(E, Q^2) = \Phi_\nu(E) \times \sigma_\nu(E, Q^2) \times N_t$$




$$\sigma_\nu(E, Q^2) = N(E, Q^2) / (\Phi_\nu(E) \times N_t)$$

Measuring a cross section

- We actually measure an event rate versus E_ν or Q^2 .
- No problem, we can solve for the cross section.
- Need to correct for background events, detector efficiencies, smearing.
- Need to calculate neutrino flux!

Absolute flux-averaged differential cross section formula

U_{ij} : unsmearing matrix

d_j : data vector

$$\sigma_i = \frac{\sum_j U_{ij} (d_j - b_j)}{\varepsilon_i (\Phi T)}$$

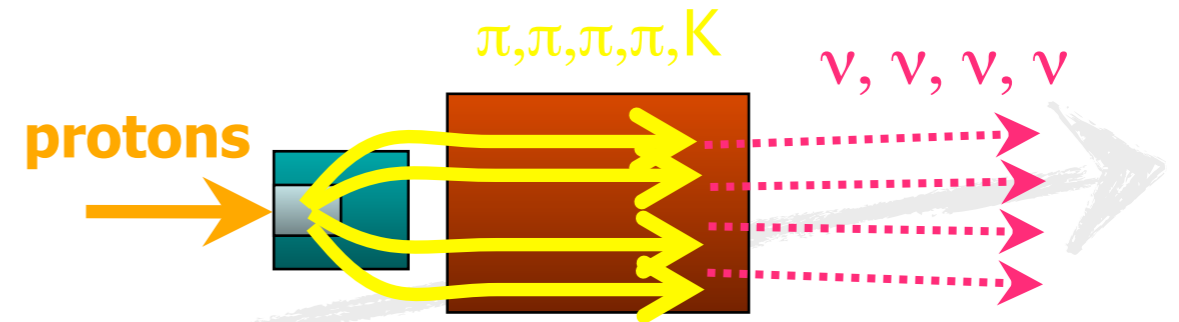
b_j : predicted background

ε_i : efficiency

T : integrated target number

Φ : integrated ν -flux

Flux Predictions



Beam	E_p (GeV)	target	$\langle \delta\Phi/\Phi \rangle$	E range	$\langle E_\nu \rangle$	Hadron prod.exp.
CERN WANF	450	Be	7%	3-100	24.3	SPY (CERN)
NuMI	120	C	~20%?	1-20	4	MIPP (FNAL)
BooNEs	8	Be	9%	0.2-3	0.8	HARP (CERN)

Further Reading:

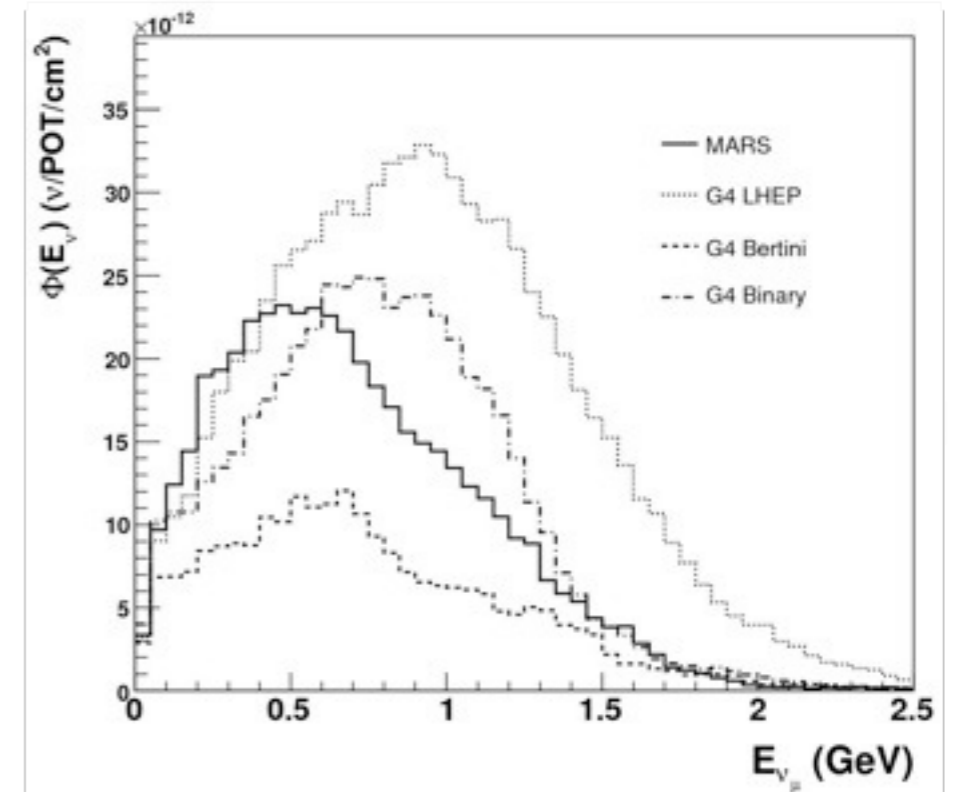
NOMAD: [NIMA 515 \(2003\) 800-828](#)

NuMI: [AIP Conf.Proc.967:49-52,2007](#)

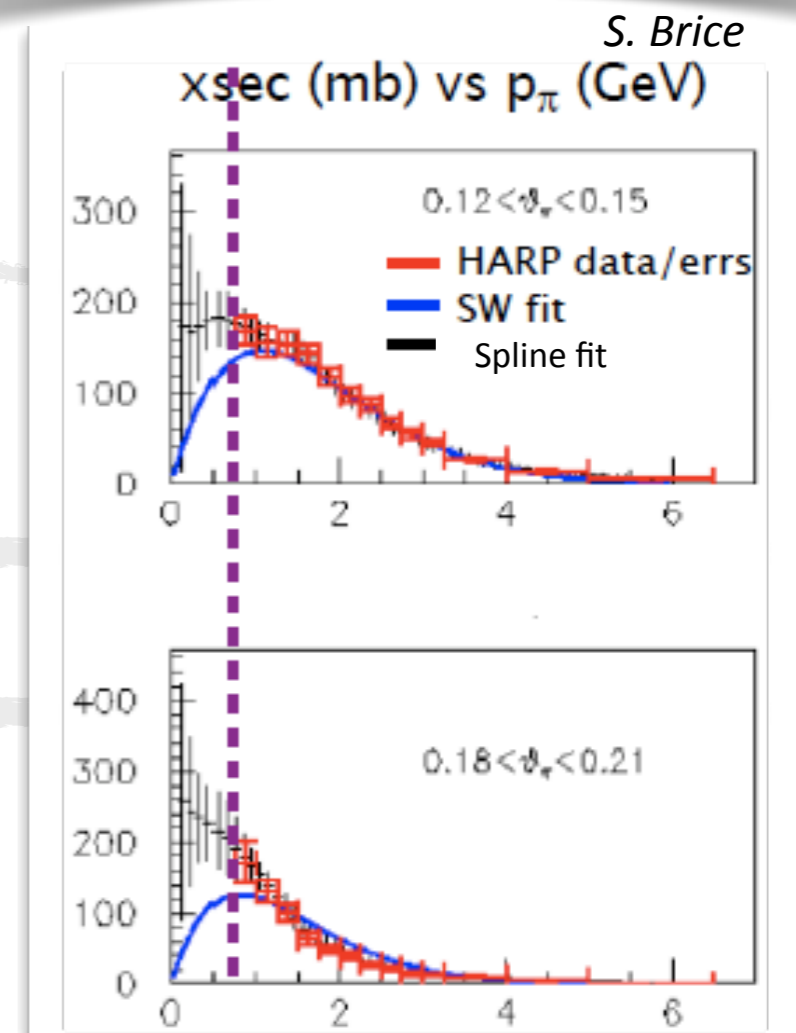
MiniBooNE: [Phys.Rev.D79 072002 \(2009\)](#)

General: [Phys.Rept.439:101-159,2007](#)

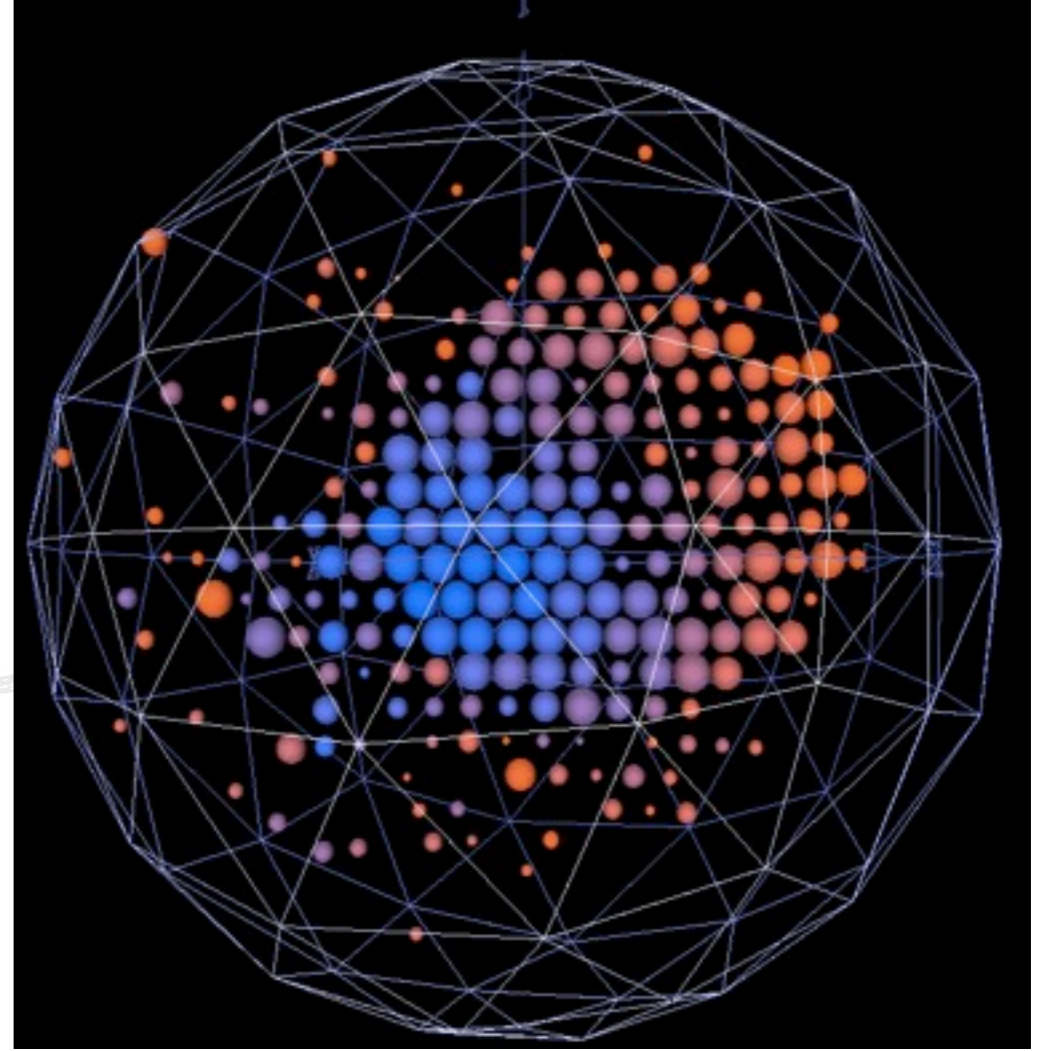
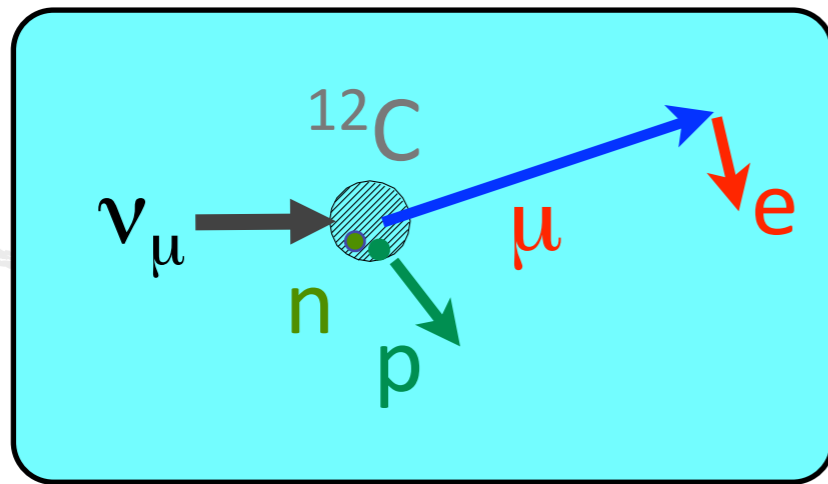
Hadron Production



- *MiniBooNE example*
- Range of MC flux predictions with different hadron models
 - 8 GeV protons on beryllium
- HARP $p\text{Be} \rightarrow \pi^+ X$ data with MiniBooNE fits
 - Spline fit reduces integrated uncertainty from 17% to 9%
- Of course, hadron production isn't magic
 - Still need primary & secondary beam monitoring, etc.

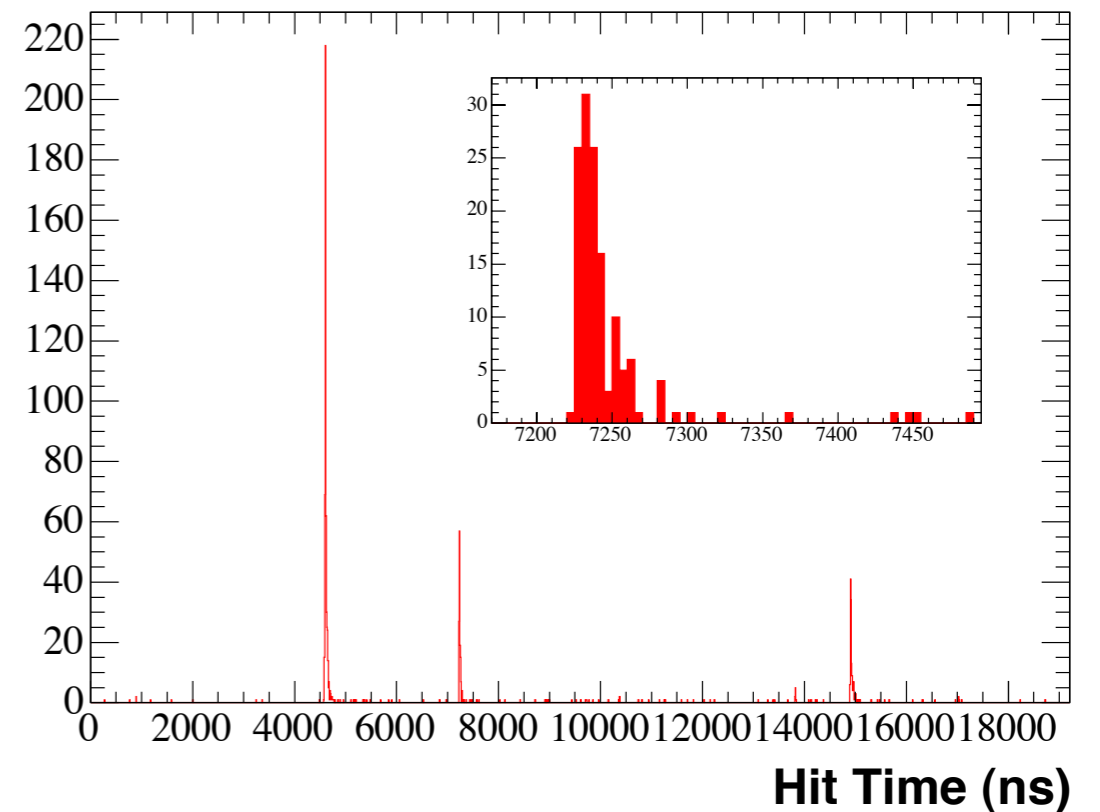


MiniBooNE

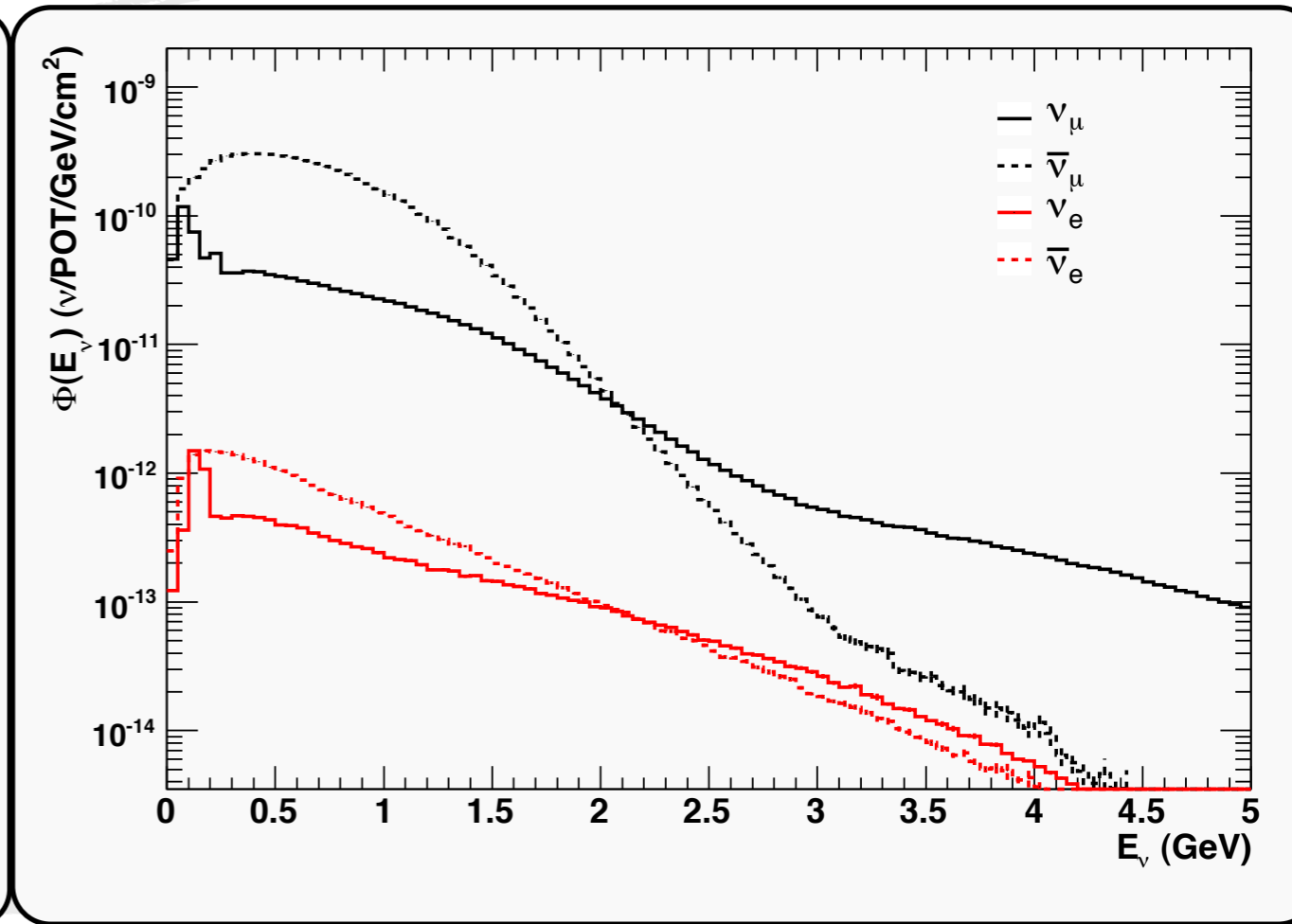
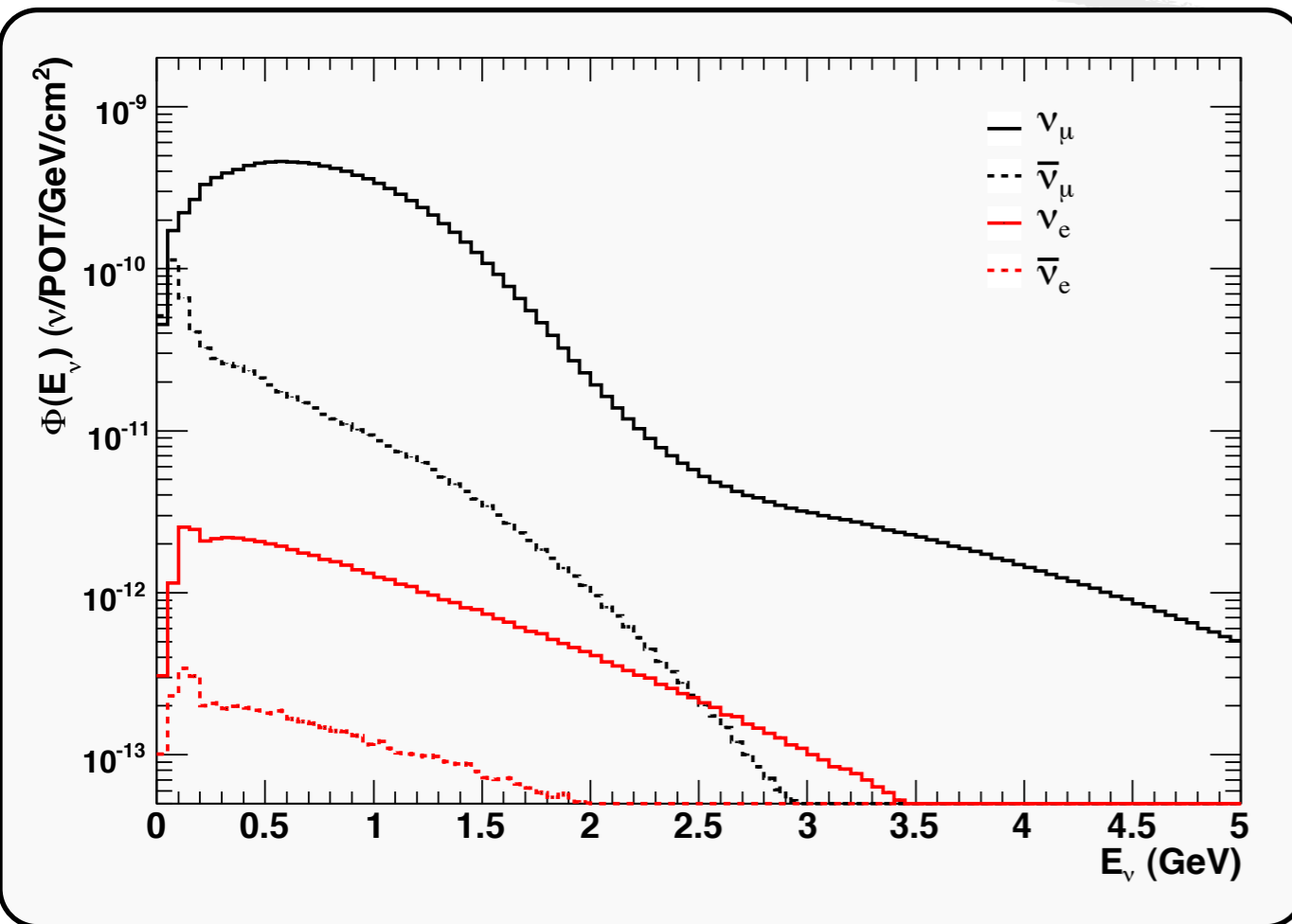


- PMT hits separated into time clusters (“subevents”)
- Reconstruct muon Cherenkov ring
 - First subevent
- Find decay electrons
 - Late subevents
- CCQE requires 1 late subevent

27% efficiency
77% purity
146,070 events
with 5.58E20 POT

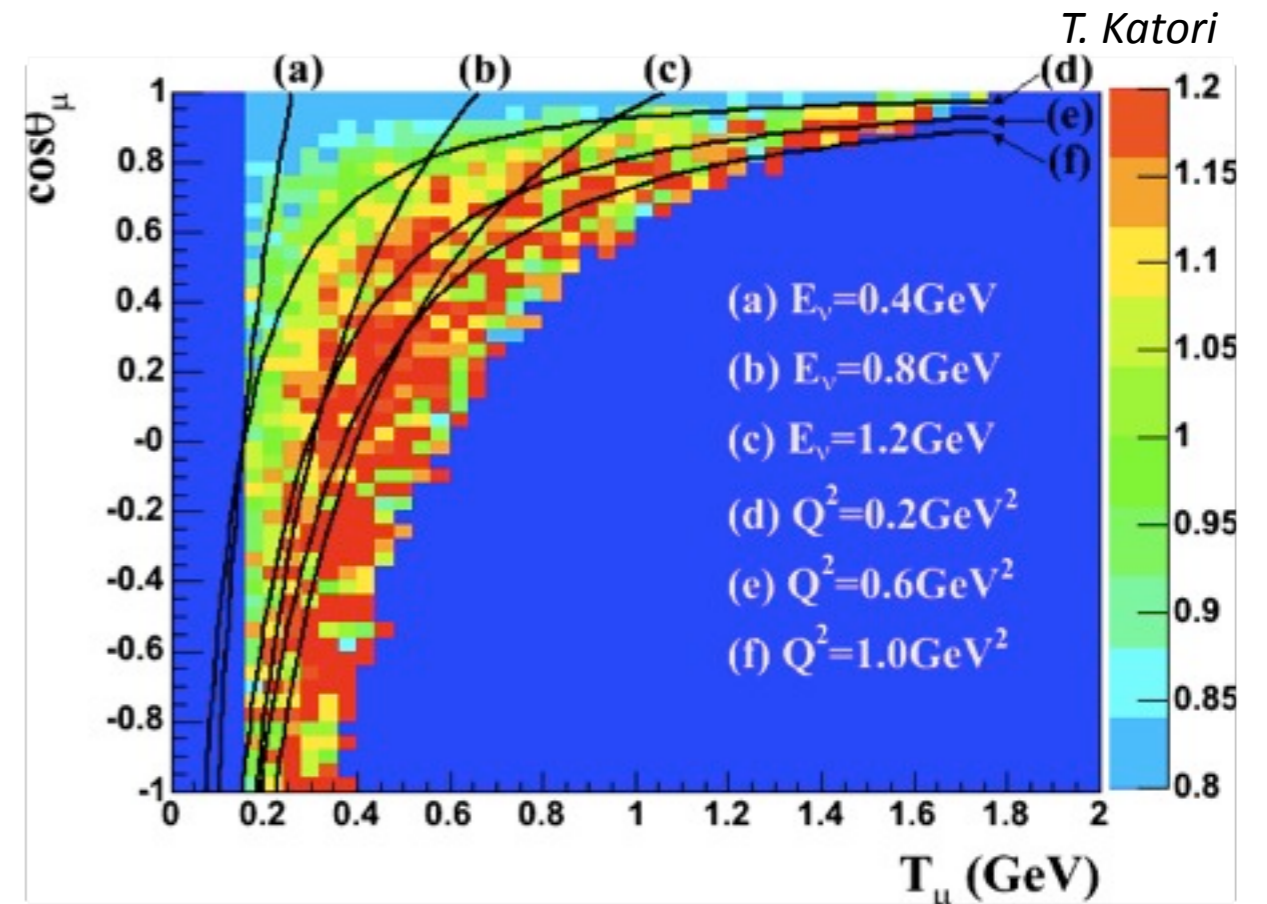


MB fluxes

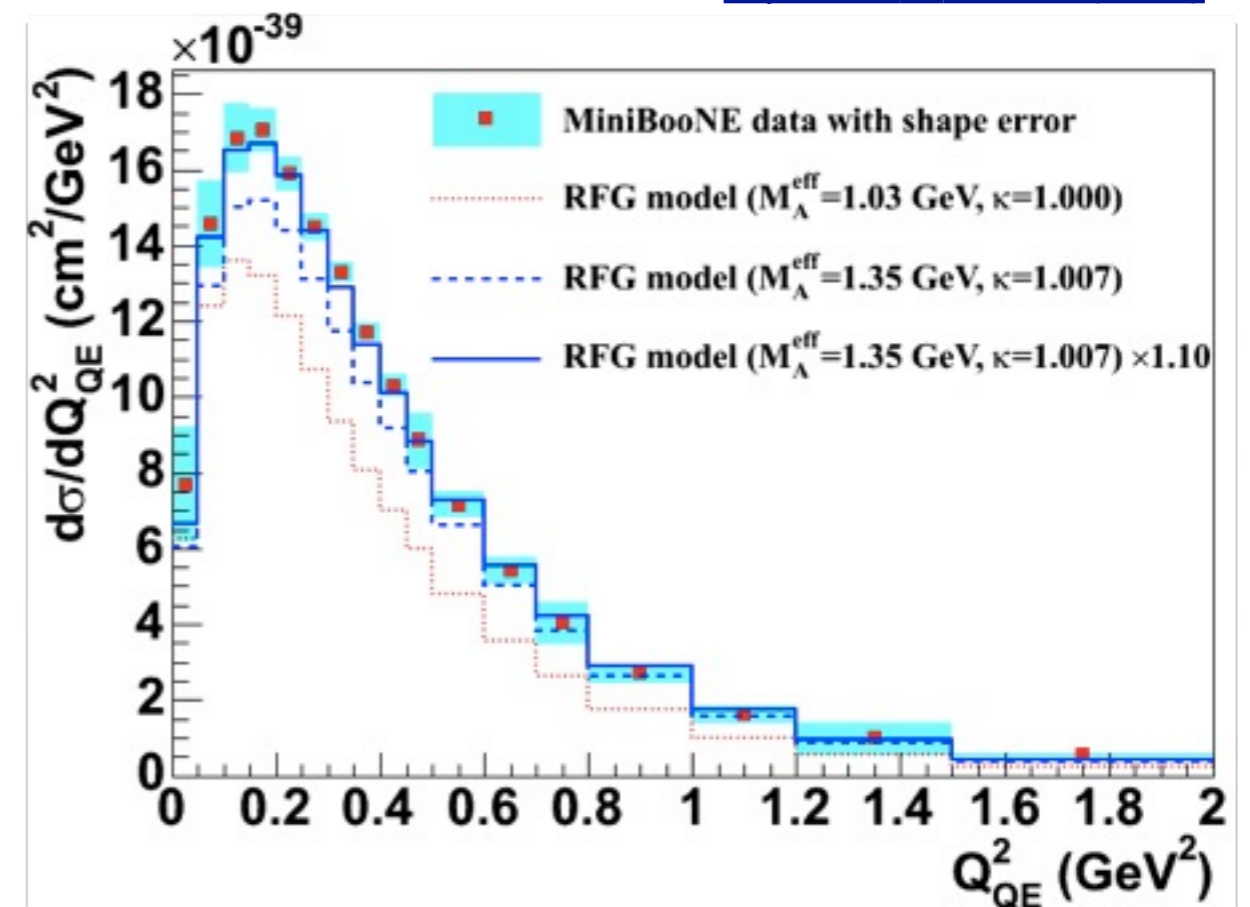


MiniBooNE

- CCQE selection: require clean μ ring with matched decay electron
 - 1.4E5 events after cuts!
- Q^2 shape fits for M_A
 - discrepancies at high & low Q^2 !
 - $M_A = 1.35 \pm 0.17$ GeV
- Low Q^2 deficit addressed with $CC\pi^+$ BG with data constraint
- First POT normalised cross-section!



[PhysRevD 81 092005 \(2010\)](#)

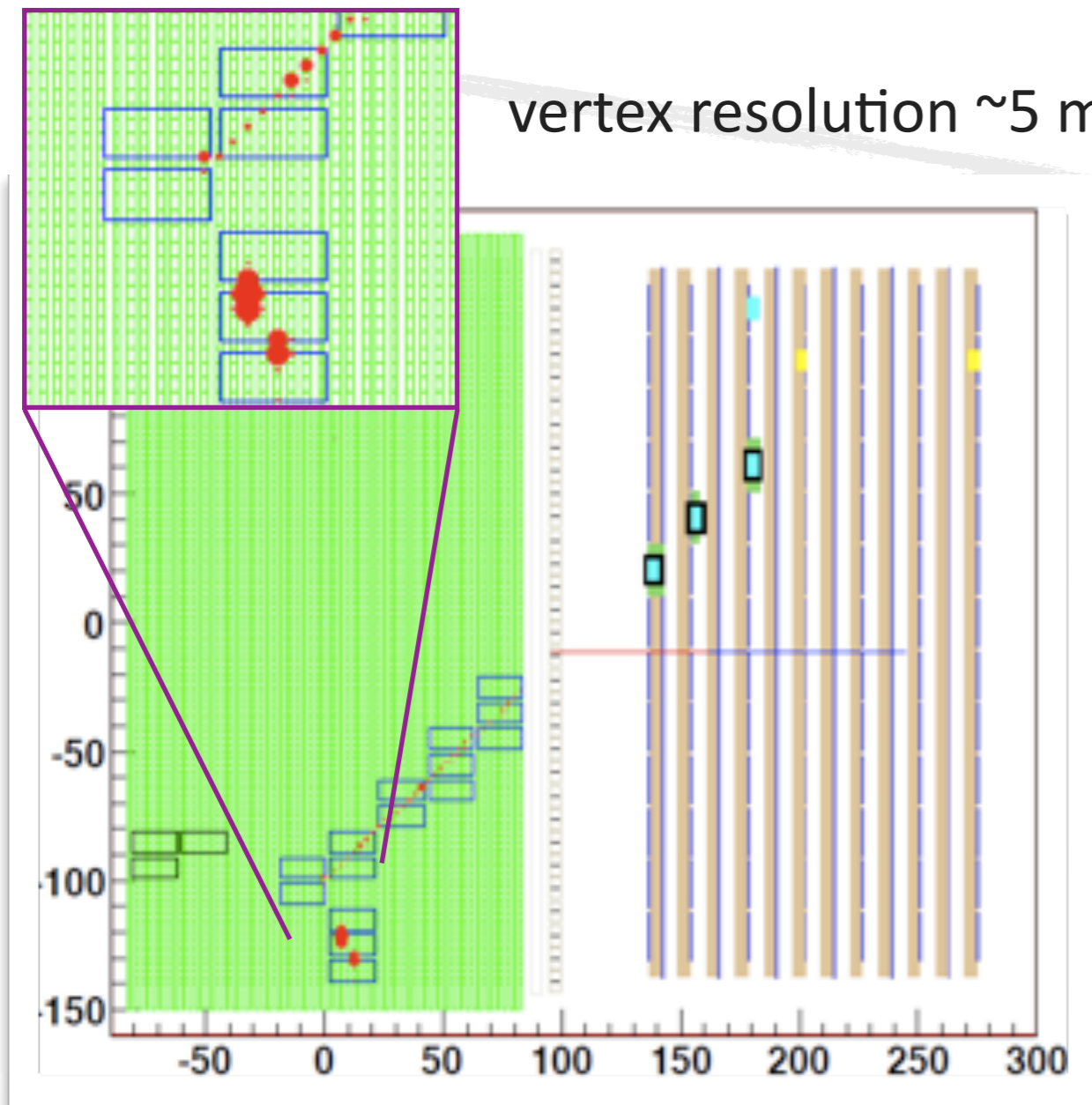


SciBooNE event displays

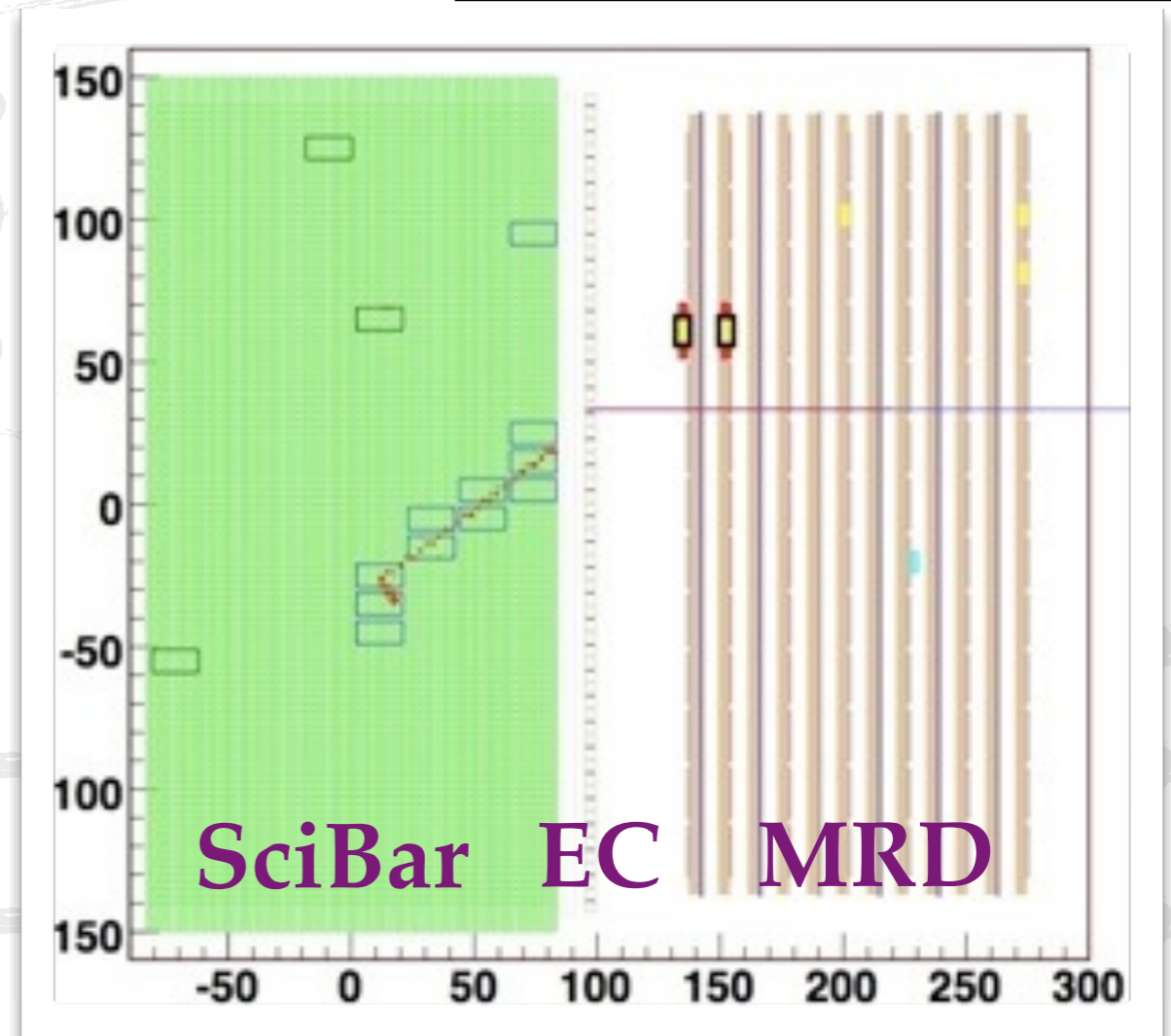
Real SciBooNE Data

vertex resolution ~ 5 mm

- ADC hits (area \propto charge)
- TDC hits (32ch "OR")

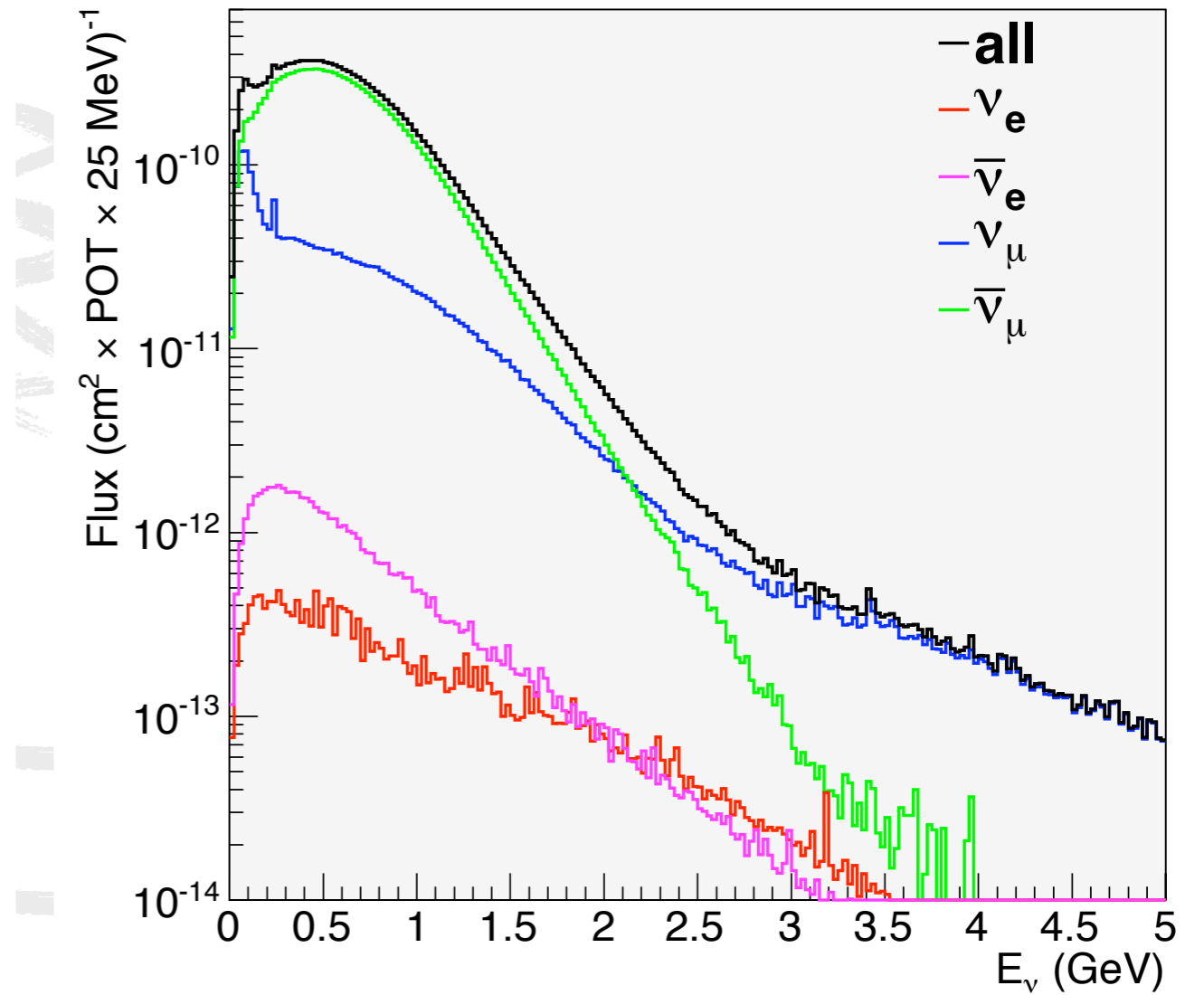
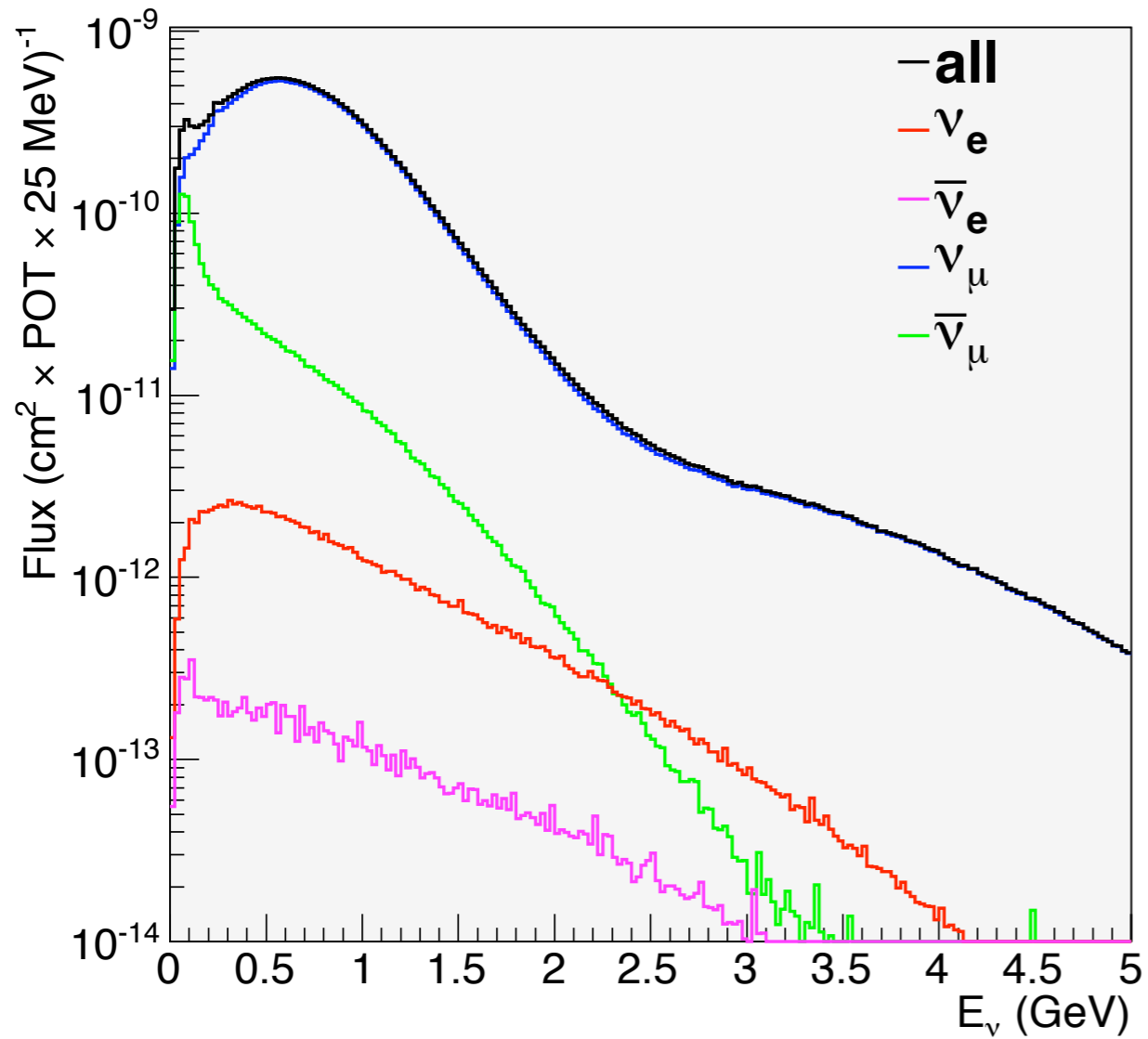


anti- ν_μ CC-QE candidate
 $(\bar{\nu}_\mu + p \rightarrow \mu + n)$



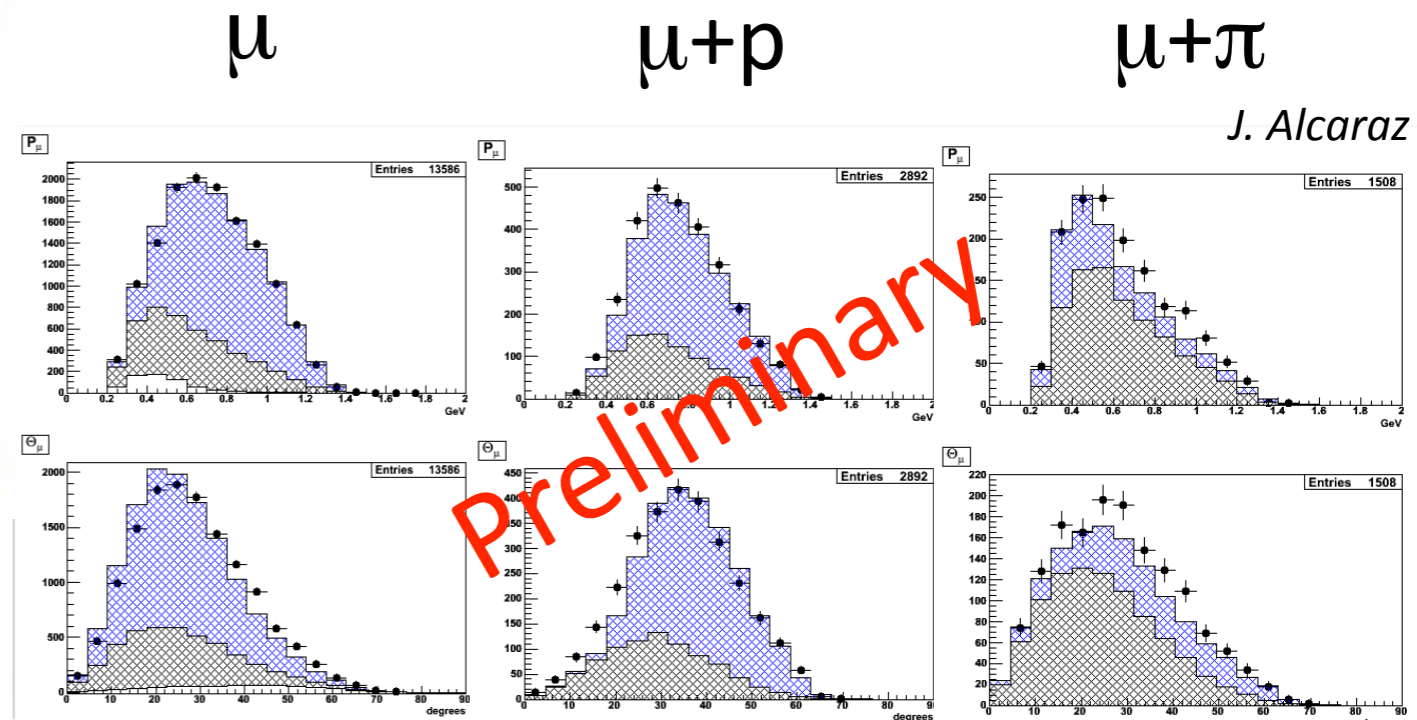
ν_μ CC-QE candidate
 $(\nu_\mu + n \rightarrow \mu + p)$

SB fluxes



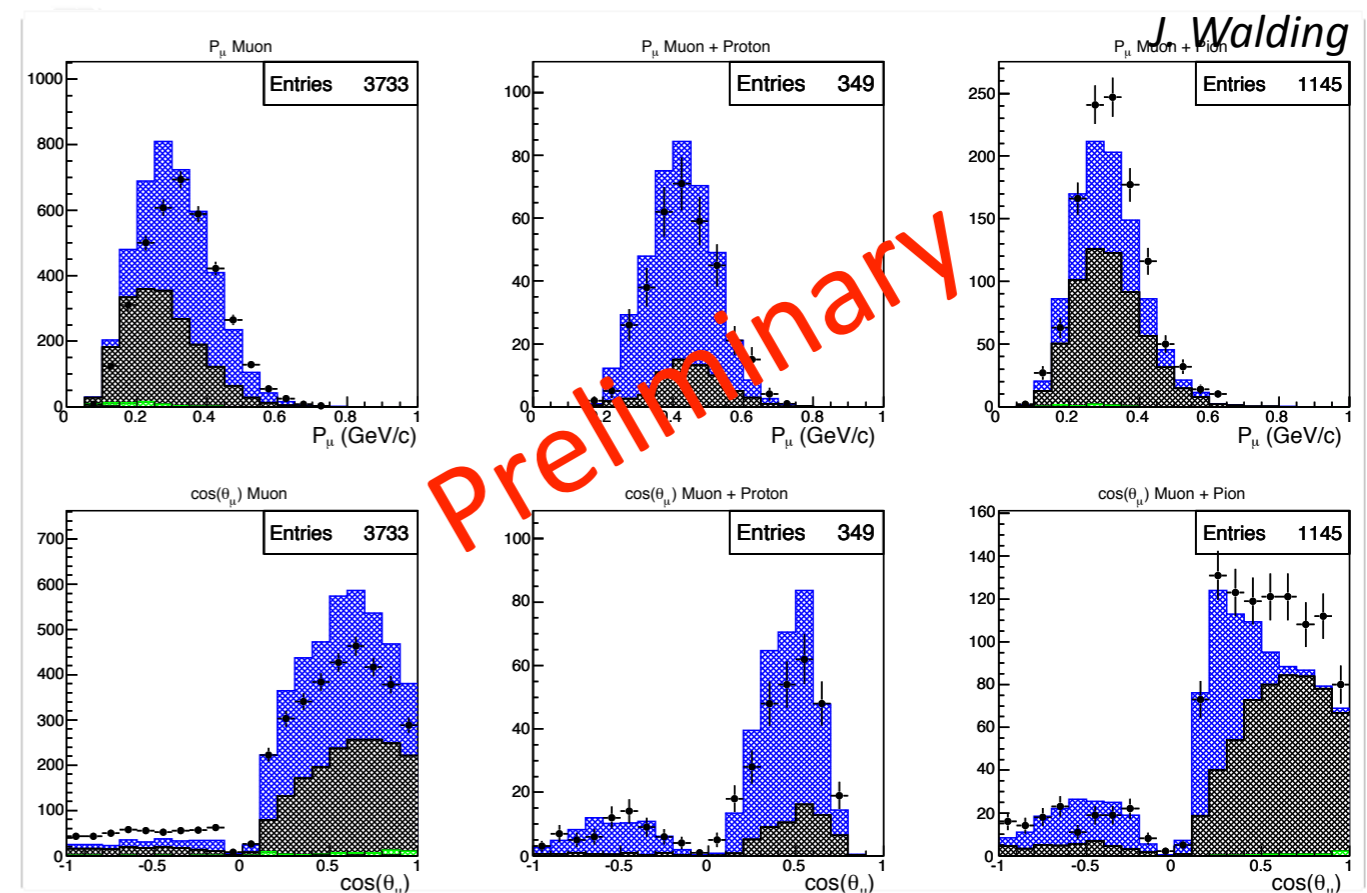
SciBooNE

- Fine-grained vertex detector
- Carbon target
- Sensitivity to secondary tracks
- simultaneously fit μ , $\mu+p$, $\mu+\pi$ samples
- Extract $\sigma_{QE}(E_\nu)$
- Also producing POT normalised cross-sections
- Similar discrepancies as seen by MiniBooNE

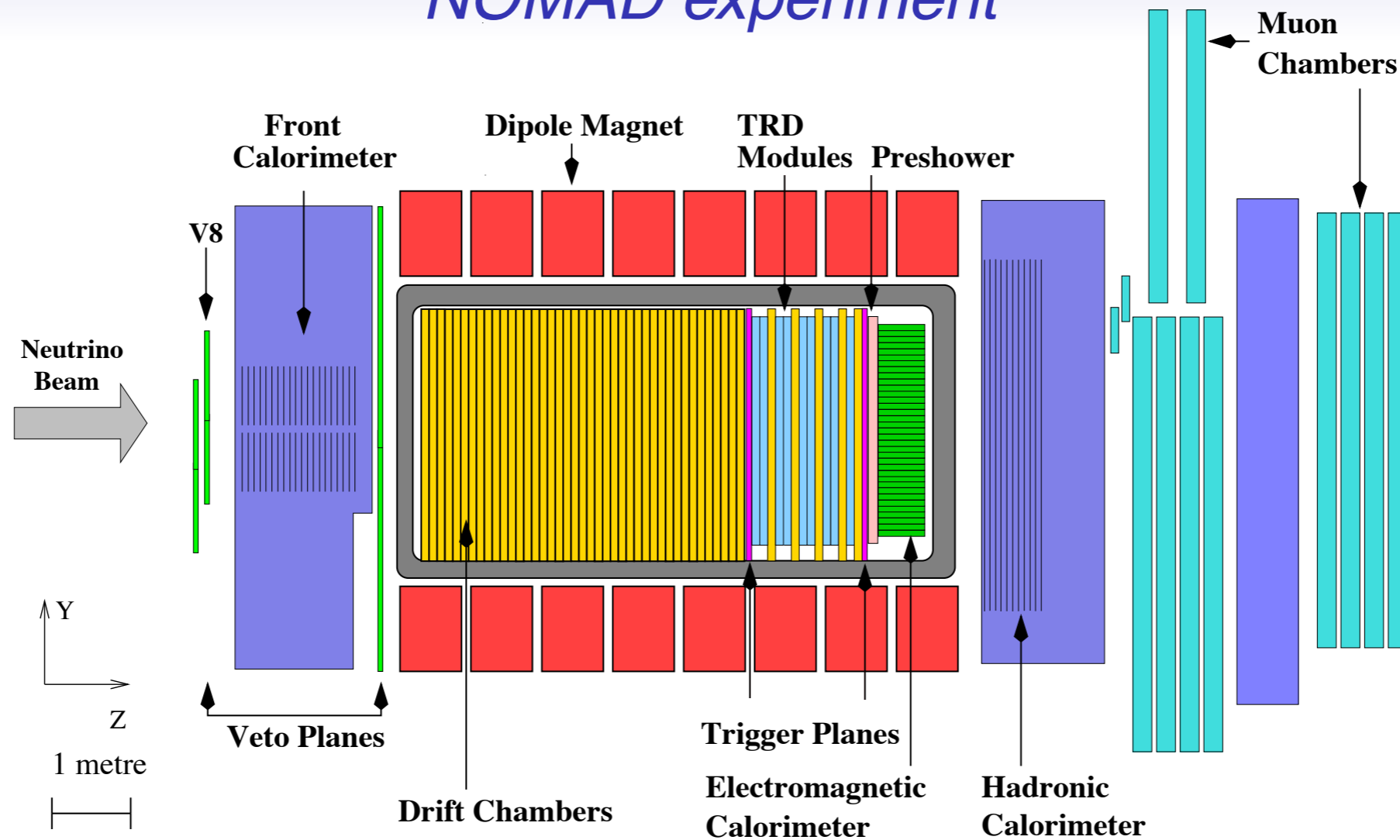


CCQE signal ; Backgrounds

AIP Conf.Proc.1189:145-150,2009

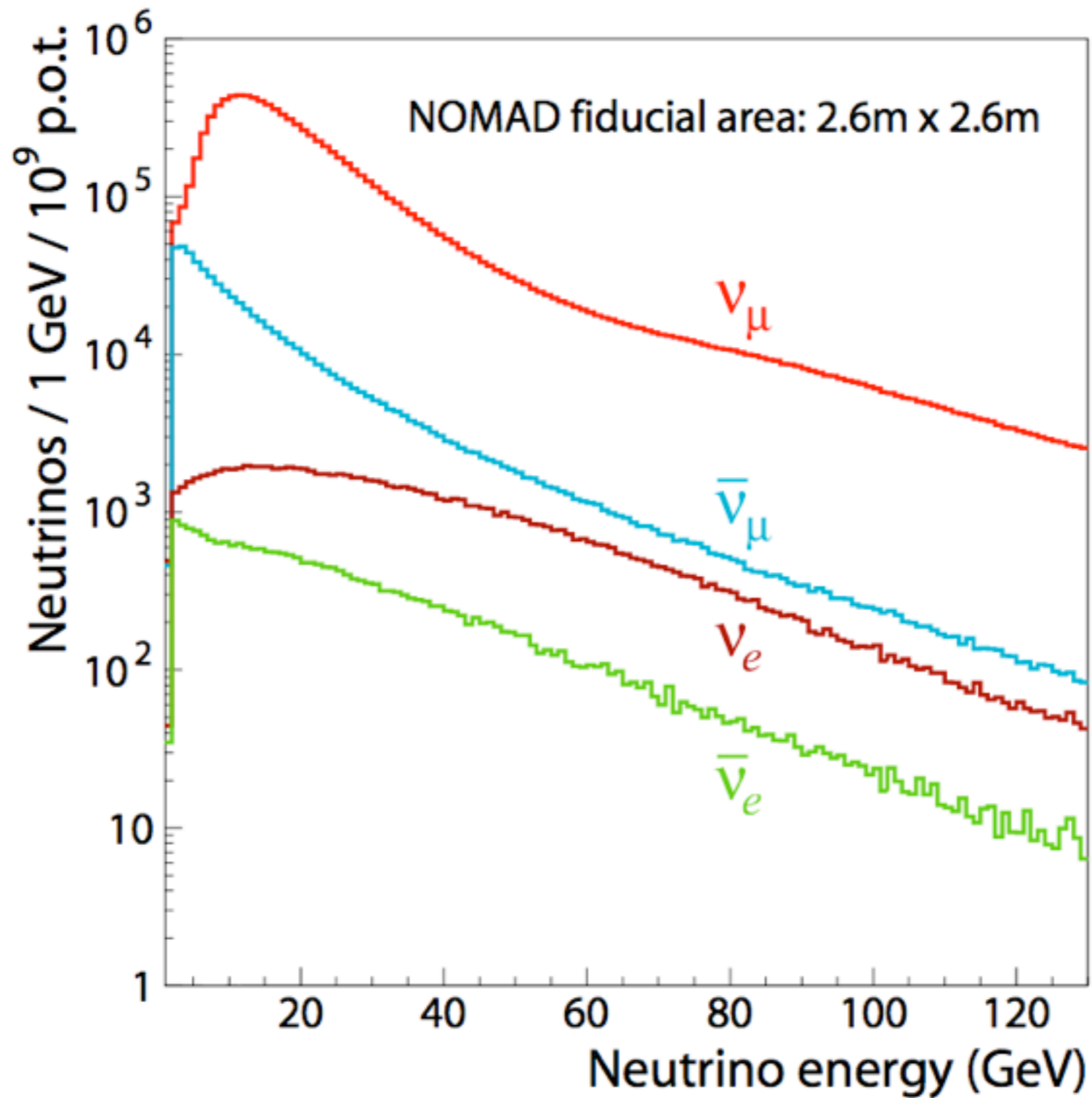


NOMAD experiment



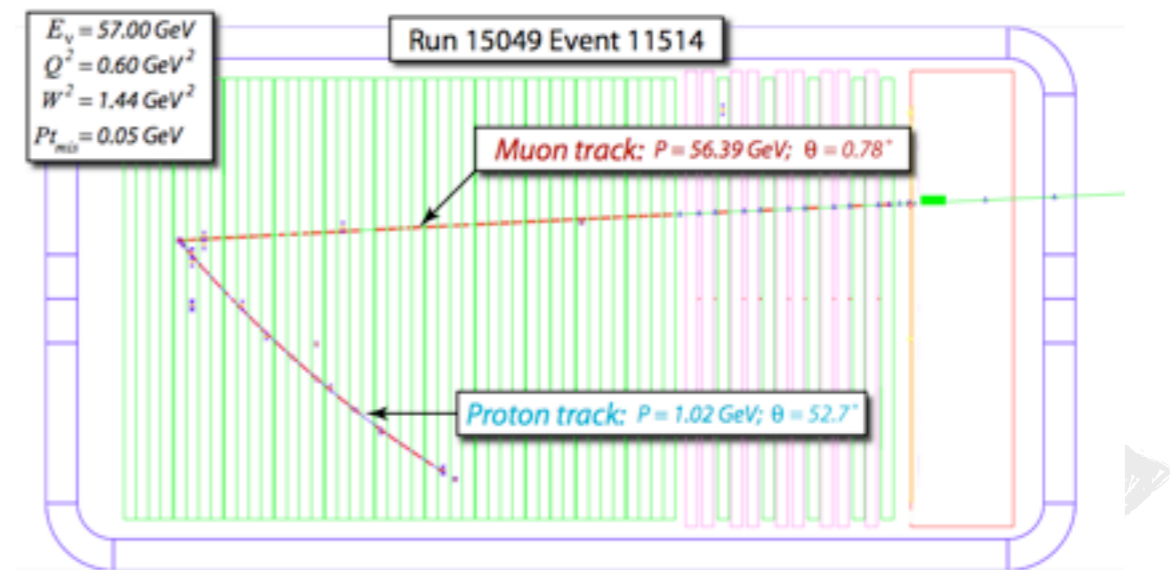
- **Drift Chambers** (target and momentum measurement) Position resolution $< 200 \mu\text{m}$ (small angle tracks)
Momentum resolution $\sim 3.5\%$ ($p < 10 \text{ GeV}/c$)
- **Transition Radiation Detector** for e^\pm identification: π rejection $\sim 10^3$ for electron efficiency $\geq 90\%$
- **Lead glass Electromagnetic Calorimeter** $\frac{\sigma(E)}{E} = (1.04 \pm 0.01)\% + \frac{(3.22 \pm 0.07)\%}{\sqrt{E \text{ (GeV)}}}$
- **Muon Chambers** for μ^\pm identification: efficiency $\approx 97\%$ ($p_\mu > 5 \text{ GeV}/c$)
- **Hadronic Calorimeter** for n and K_L^0 veto

NOMAD fluxes

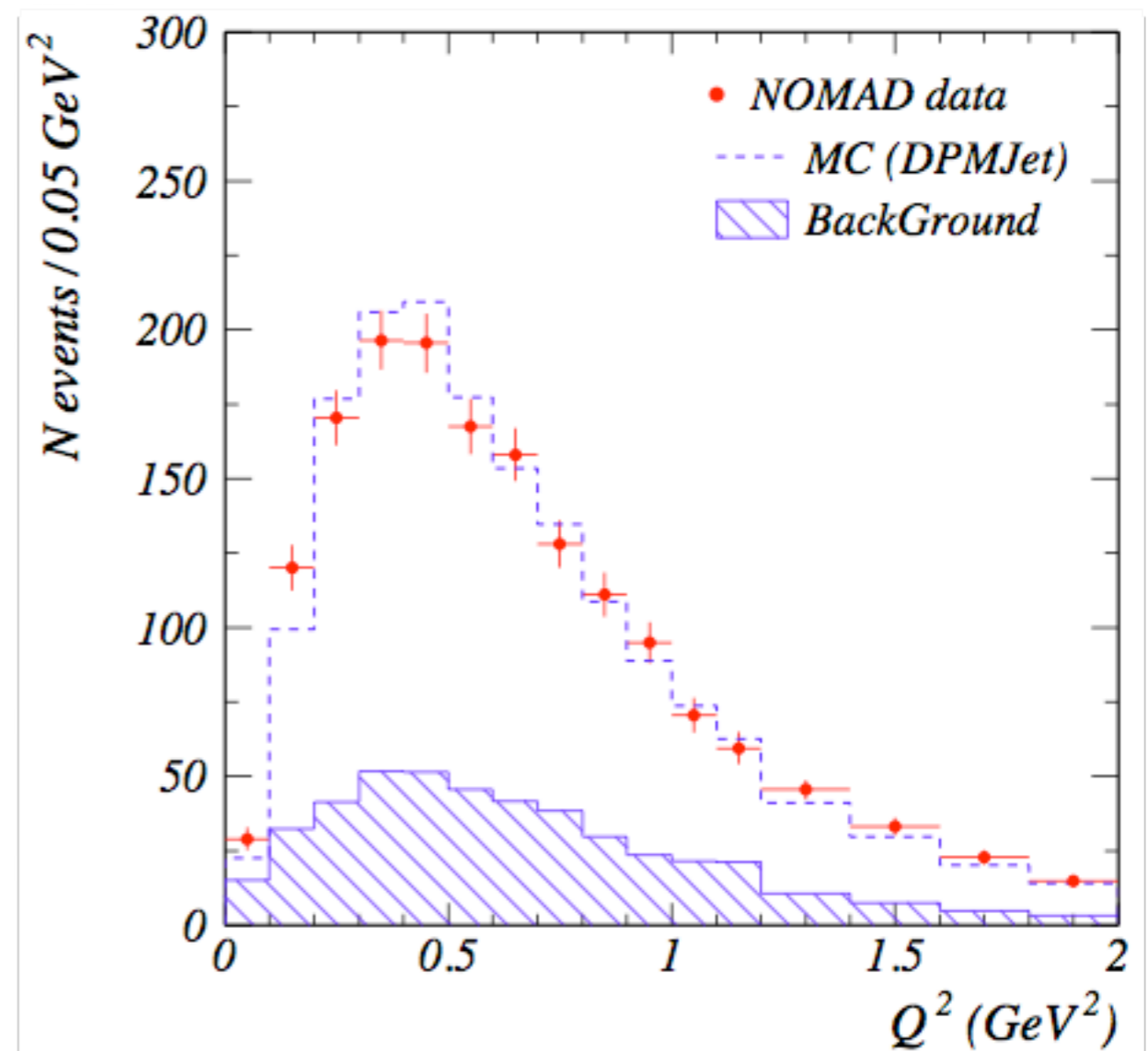


NOMAD

- Drift chambers in magnetic field
 - “Mainly carbon” target
- Select ν_μ and $\bar{\nu}_\mu$ CCQE events using strict PID and final state cuts
- Extract σ_{QE} with cross section ratios (DIS)
 - Use extracted σ_{QE} to infer value of M_A
 - Also fit Q^2 shape to check M_A
- $M_A = 1.05 \pm 0.06$ GeV

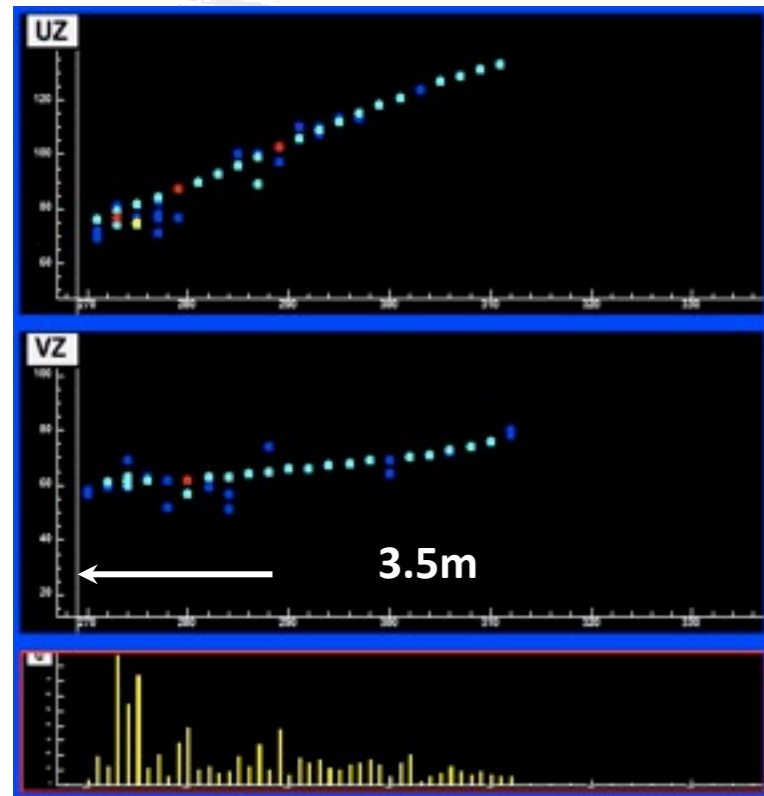


[Eur.Phys.J.C63:355-381,2009](#)



Events in the MINOS Detectors

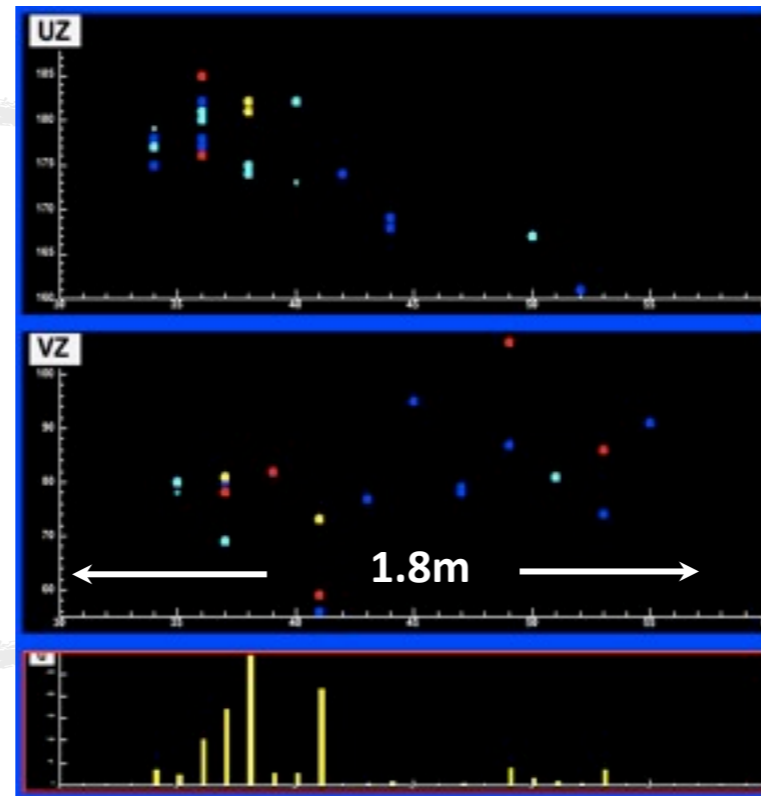
ν_μ CC Event



Long muon track with hadronic activity at the vertex.

What we look for in the muon neutrino / anti-neutrino analyses.

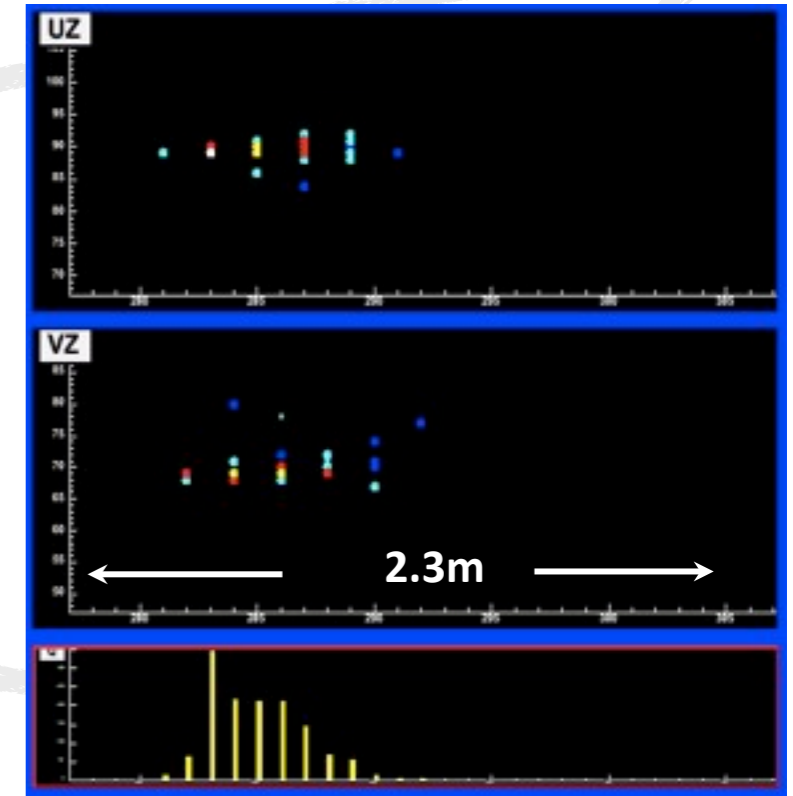
NC Event



Short event often with a diffuse shower.

What we use for the sterile neutrino analysis.

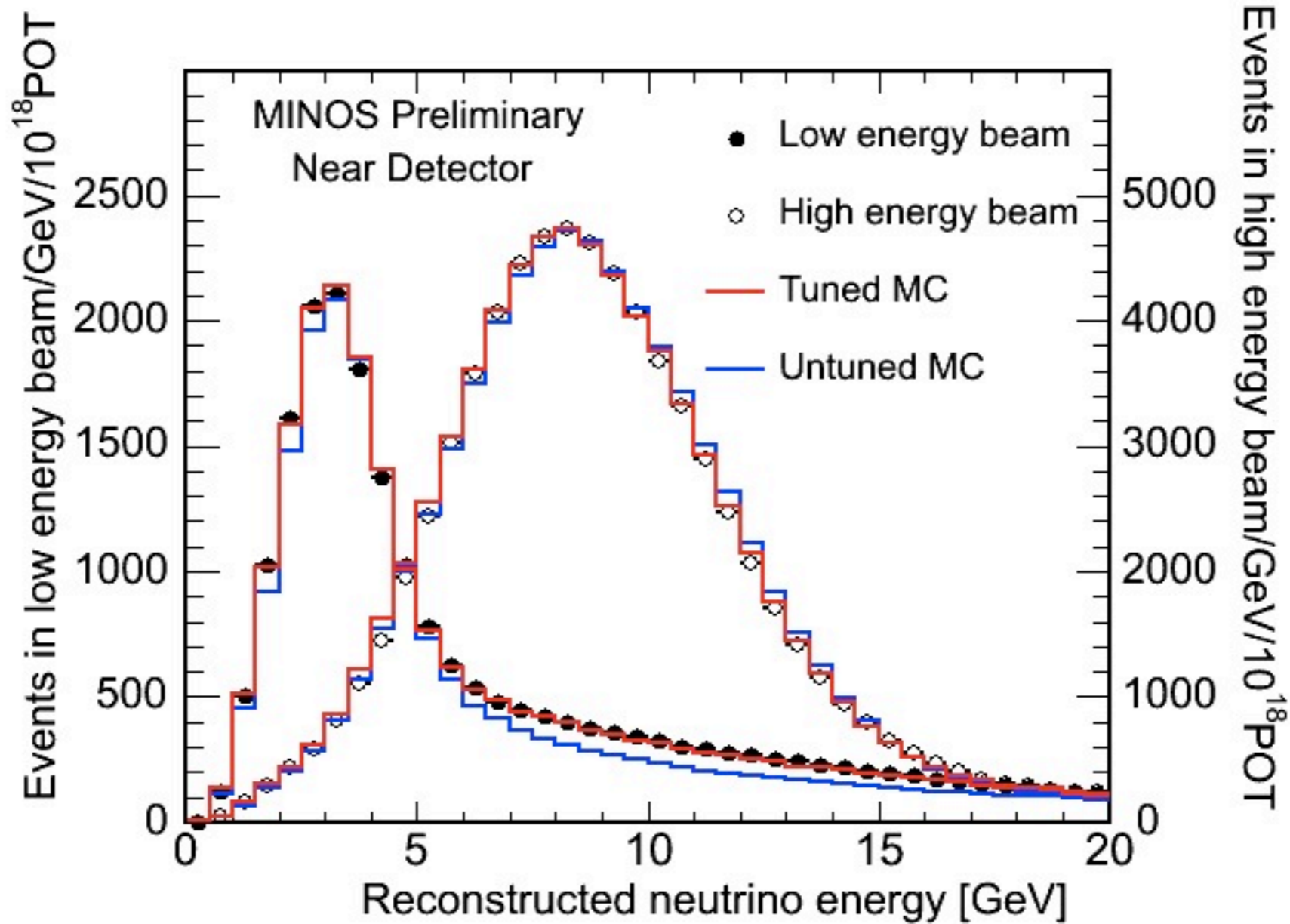
ν_e CC Event



Short event with a compact, EM-like shower profile.

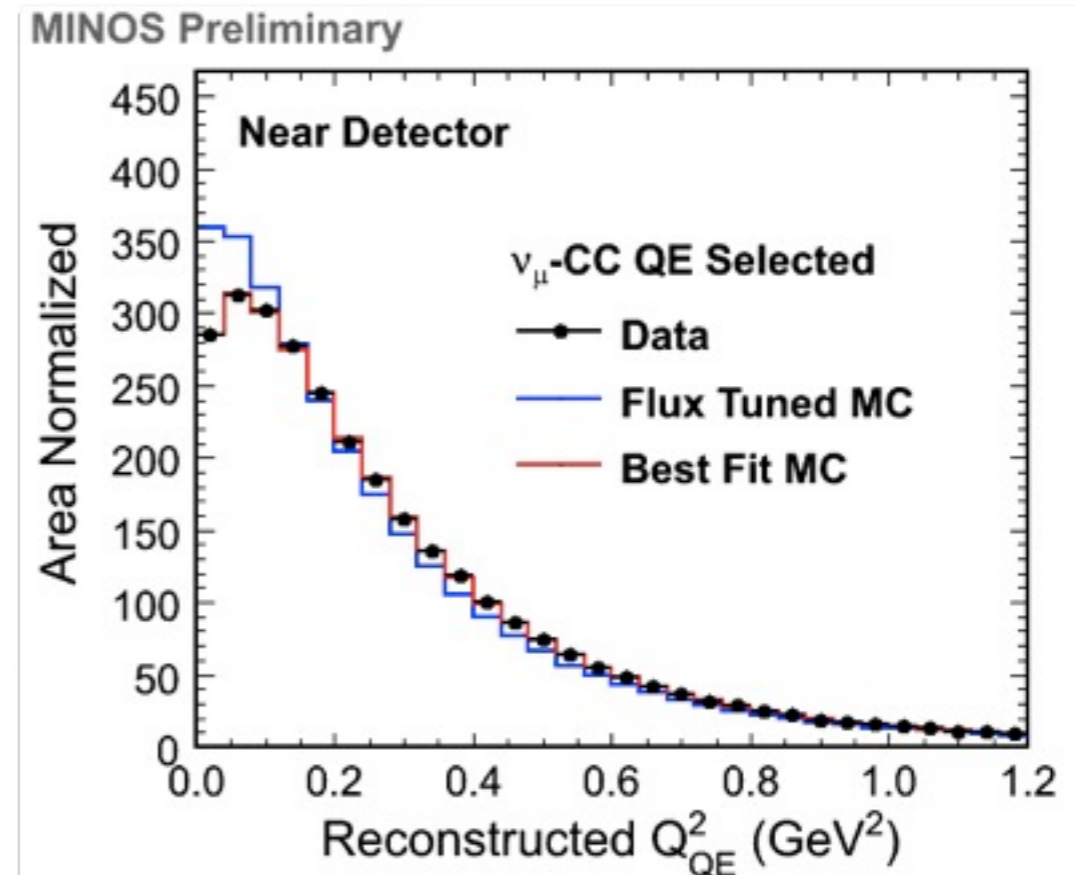
What we look for in the electron neutrino analysis.

MINOS fluxes

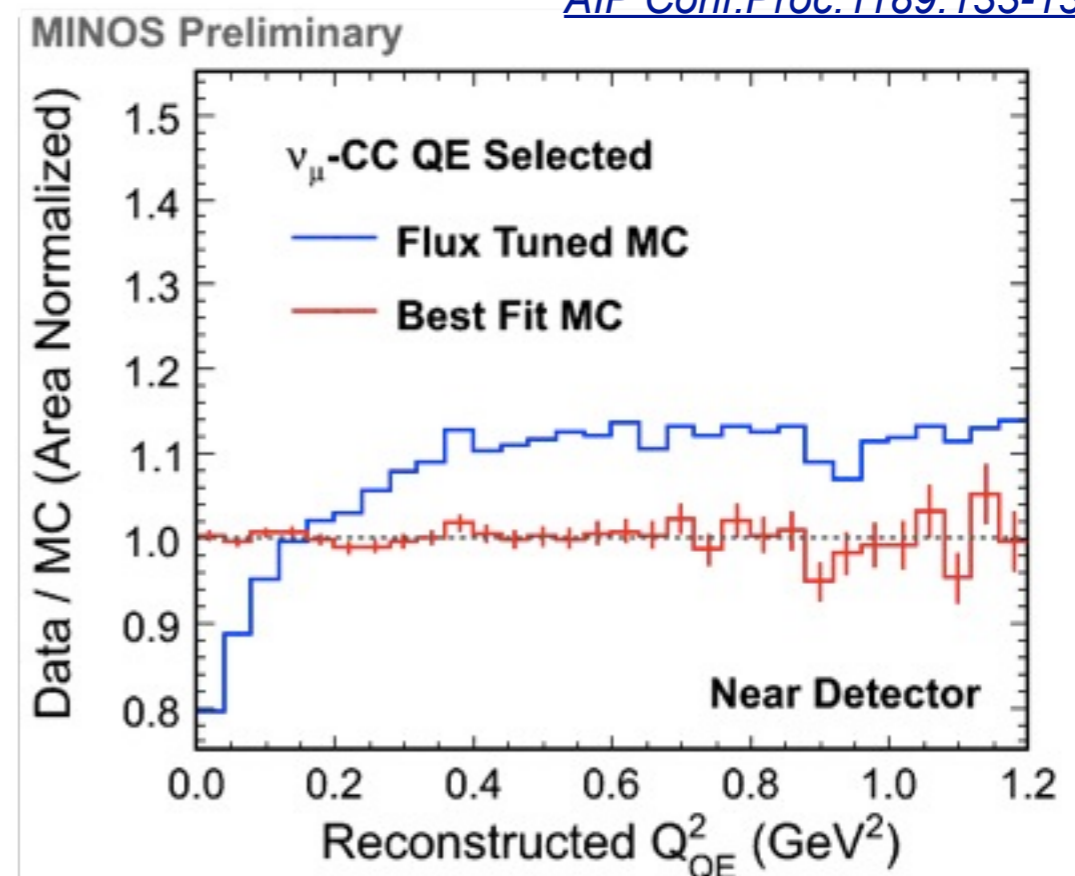


MINOS

- Iron calorimeter with magnetic field
- Intense flux \Rightarrow high statistics
- (Already published CC inclusive $\sigma_{\nu S}$ [[Phys.Rev.D 81, 072002 \(2010\)](#)])
- Select ν_{μ} events with low hadronic shower energy
- Fit Q^2 distribution for M_A
 - $M_A = 1.19 \pm 0.17$ GeV
- Non-dipole F_A fits ongoing.

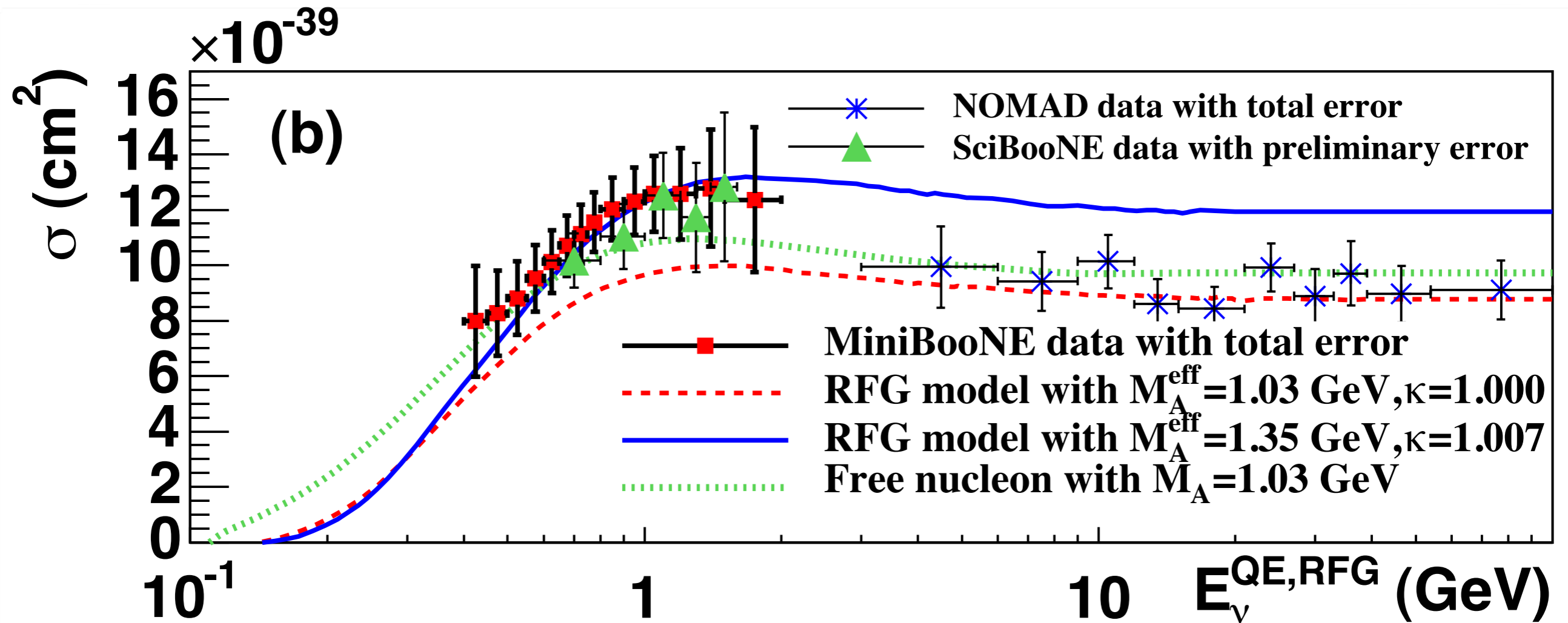


[AIP Conf.Proc.1189:133-138,2009](#)

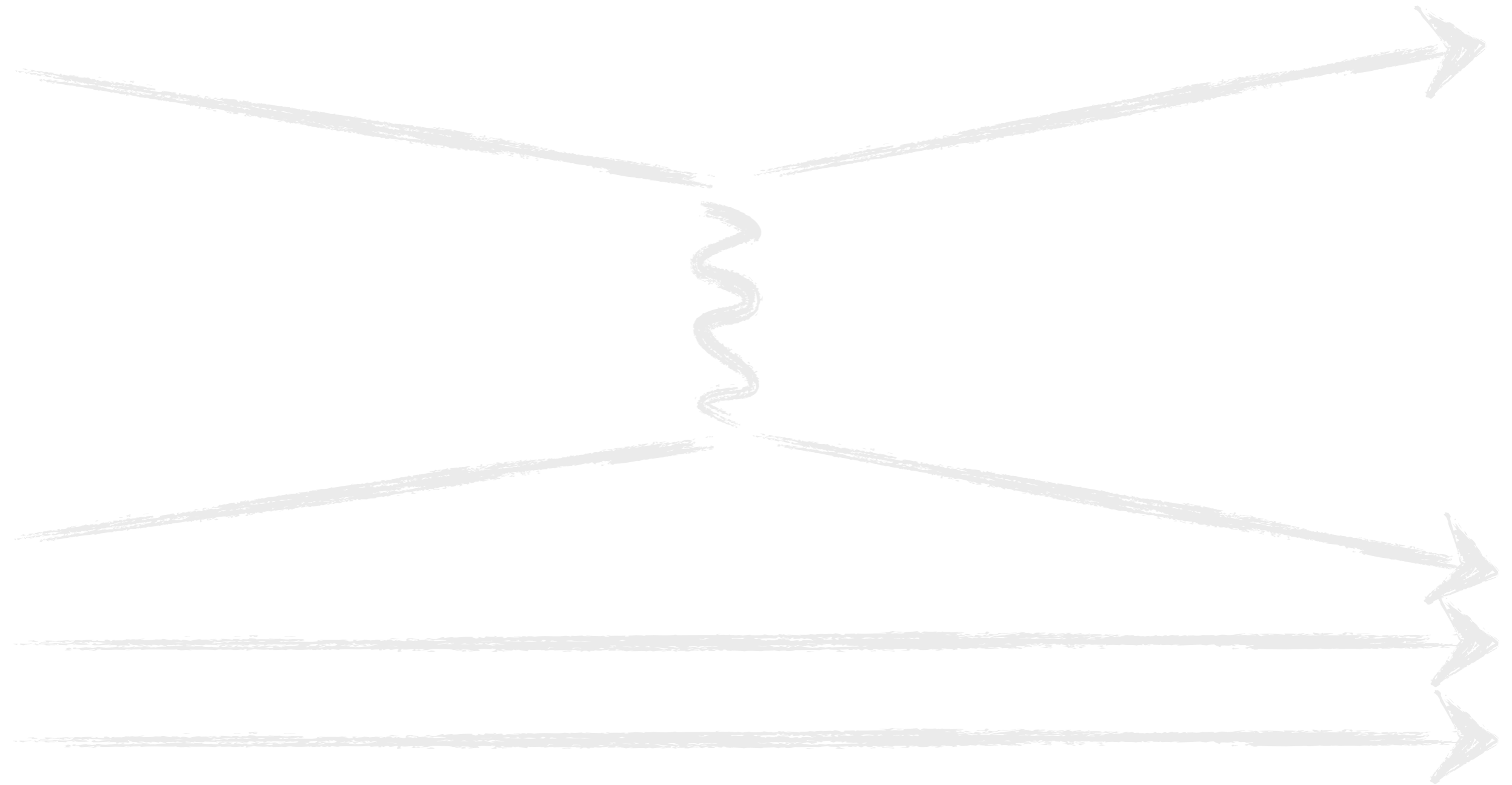


CCQE comparisons

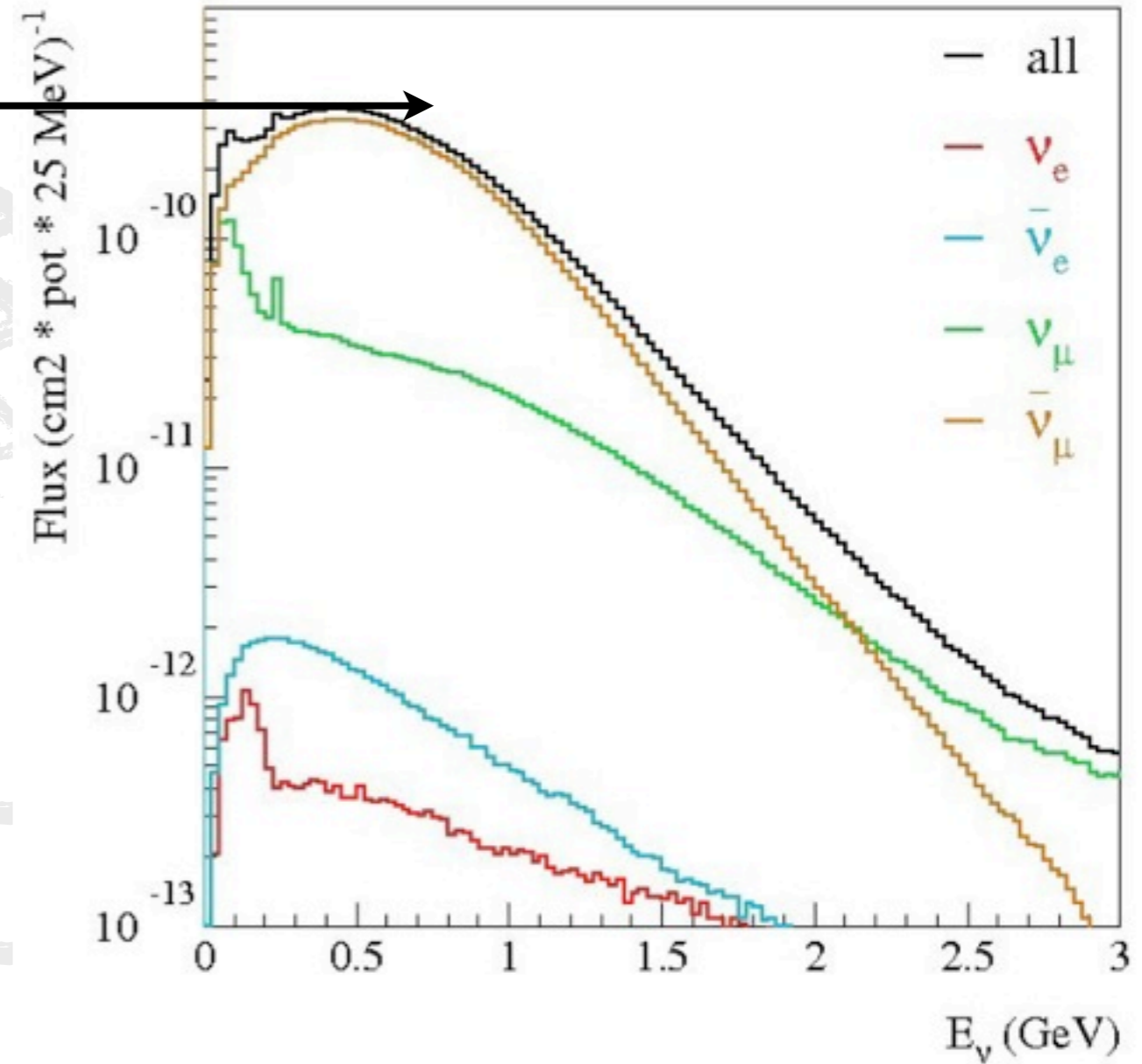
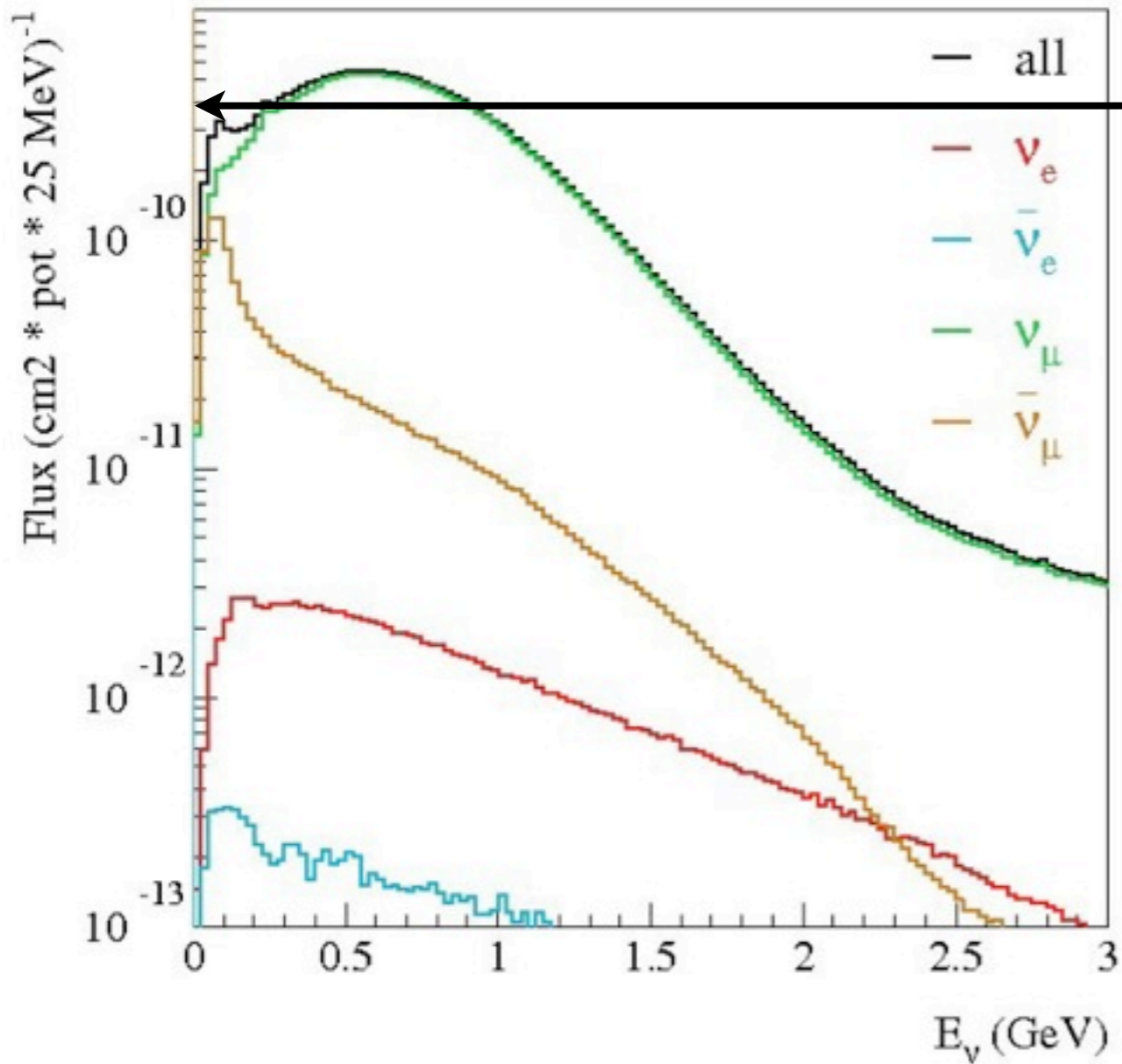
Plot courtesy of Teppei Katori (MIT)



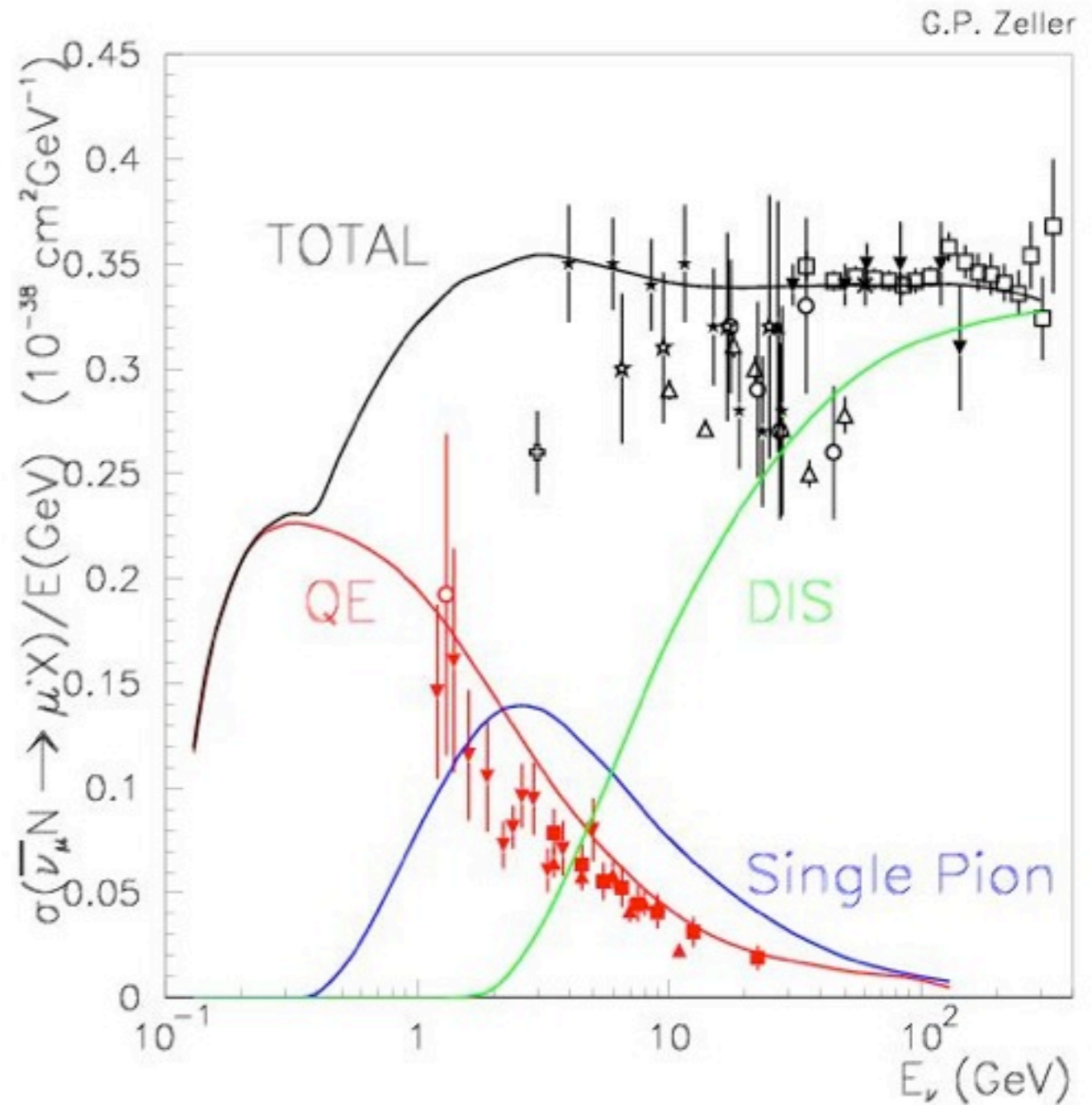
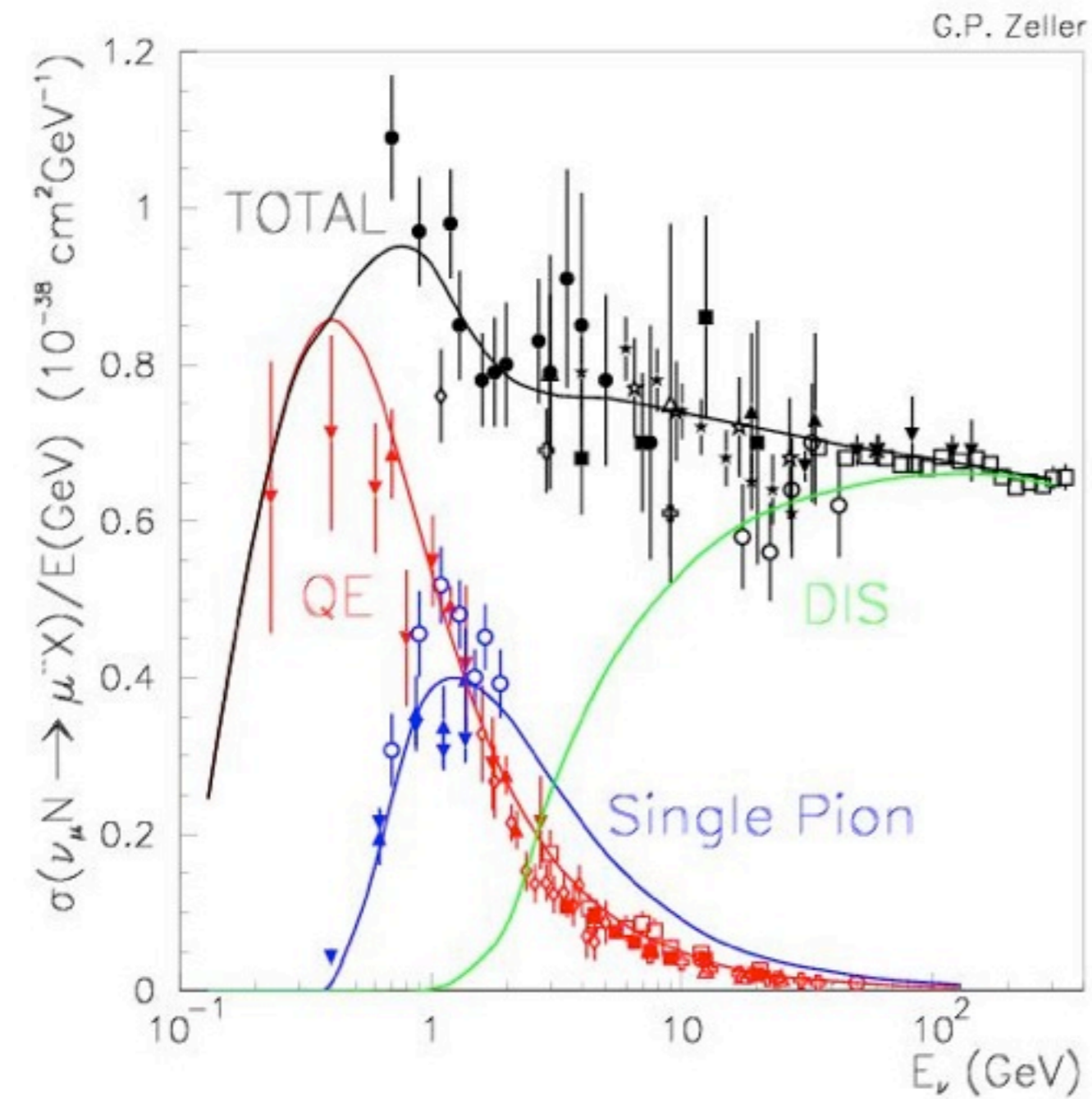
Antineutrino intro



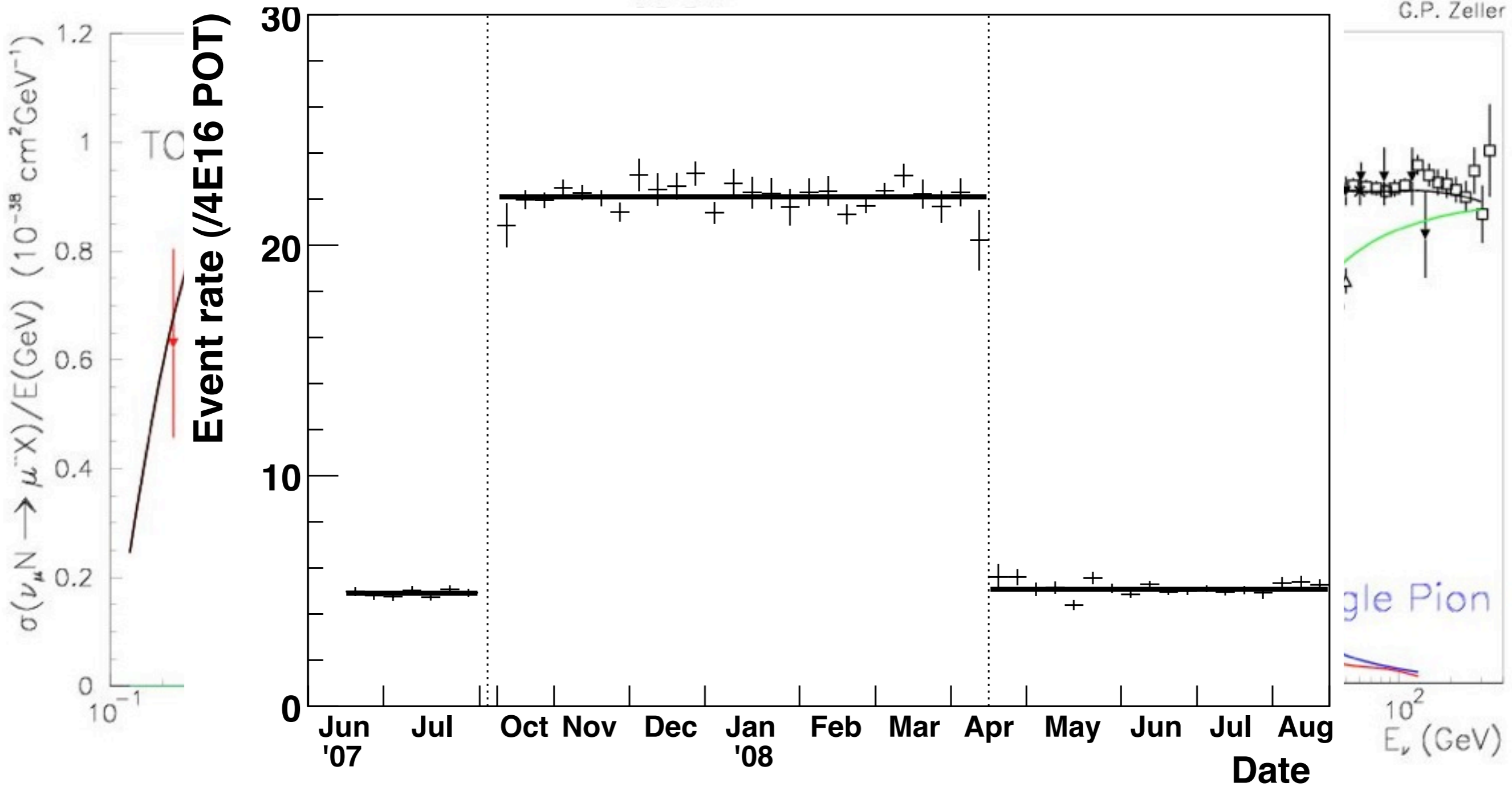
Size Matters



Size Matters



Size Matters



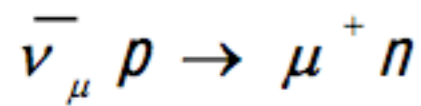
G.P. Zeller

MINERvA

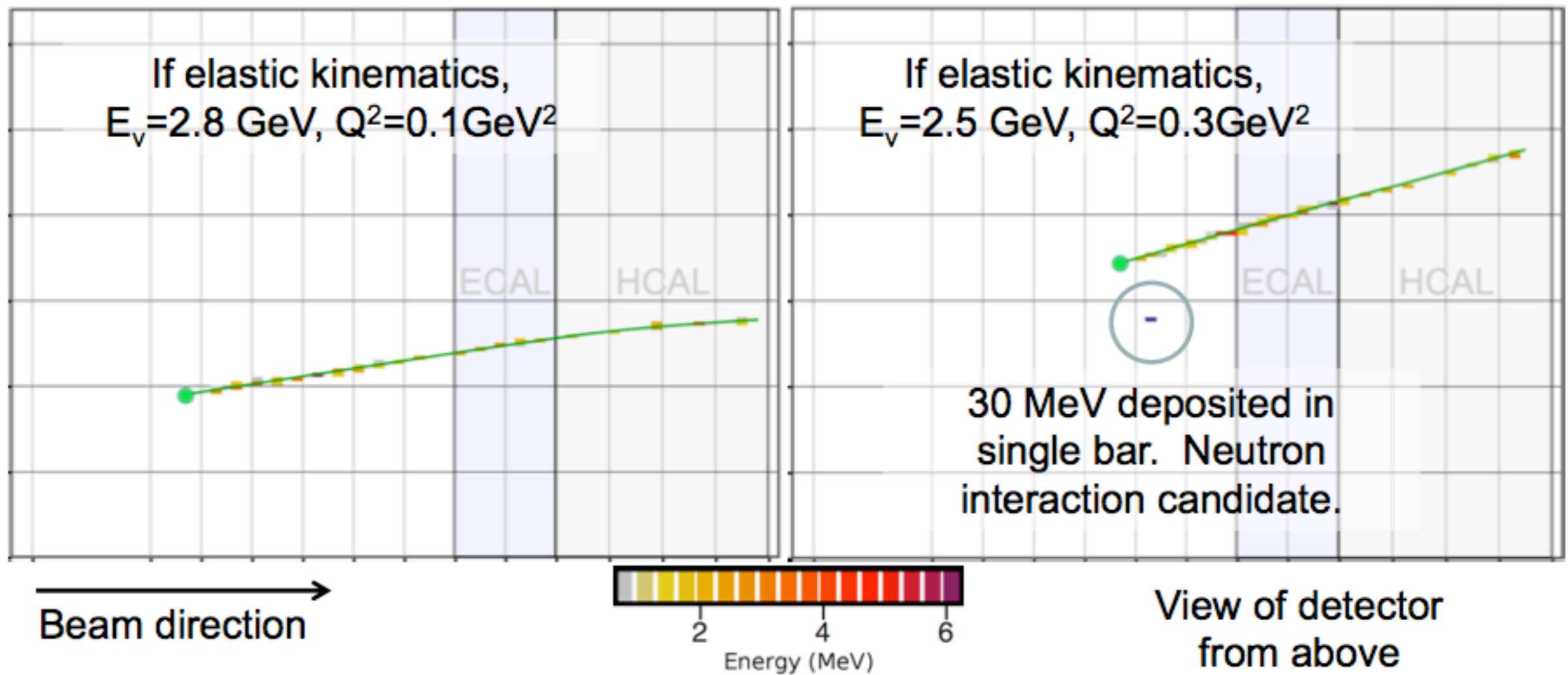
Quasi-Elastic Scattering on MINERvA



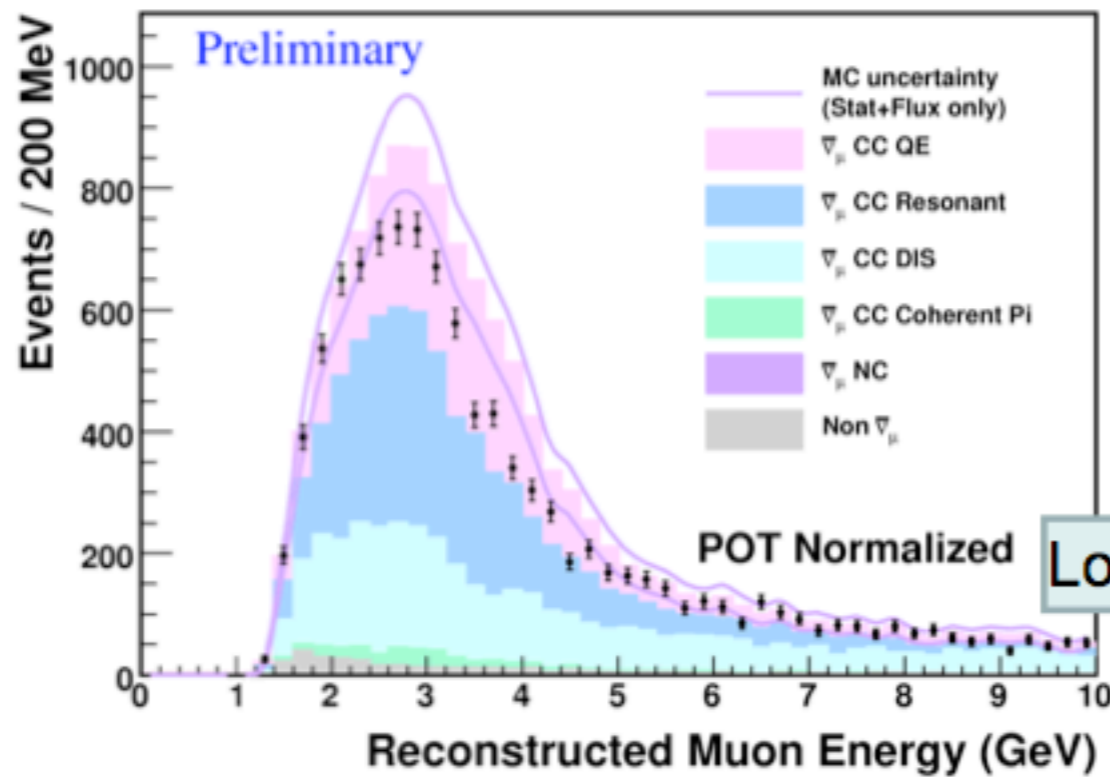
Kevin McFarland
University of Rochester
NuINT11, Dehradun
8 March 2011



- Muon is a long, penetrating track
- Neutron may or may not appear in the detector



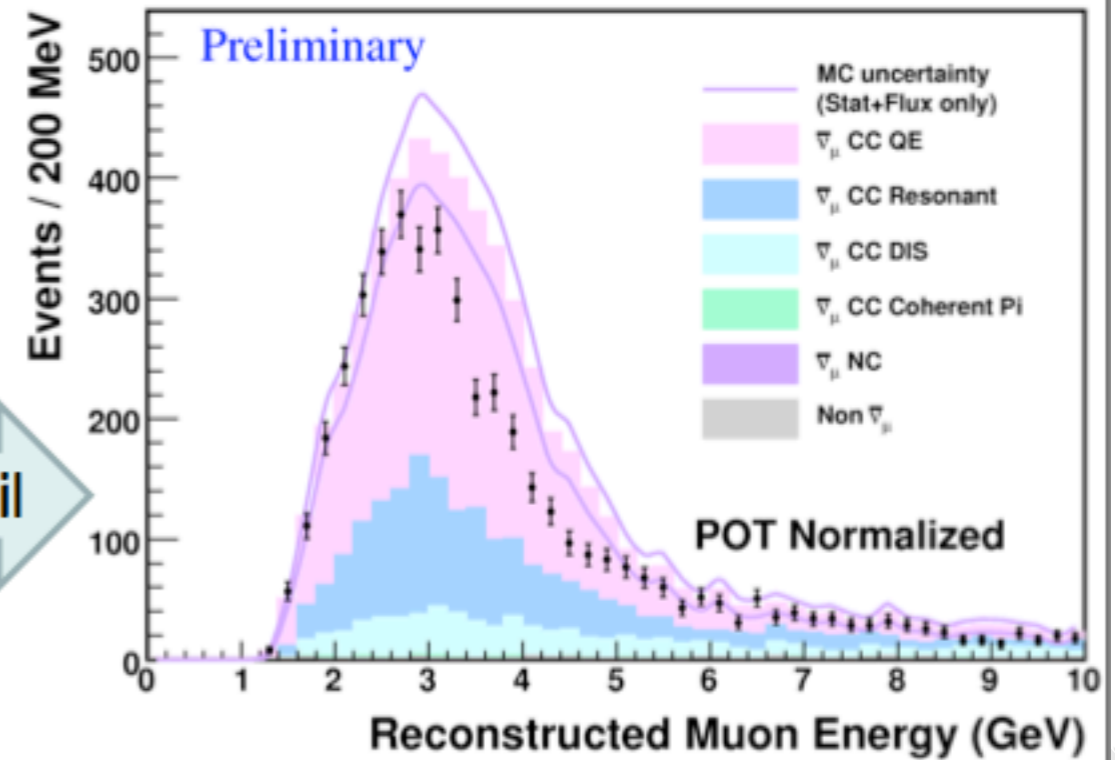
MINERvA



Inclusive μ^+

0.4E20 POT,
partial detector

Low Recoil



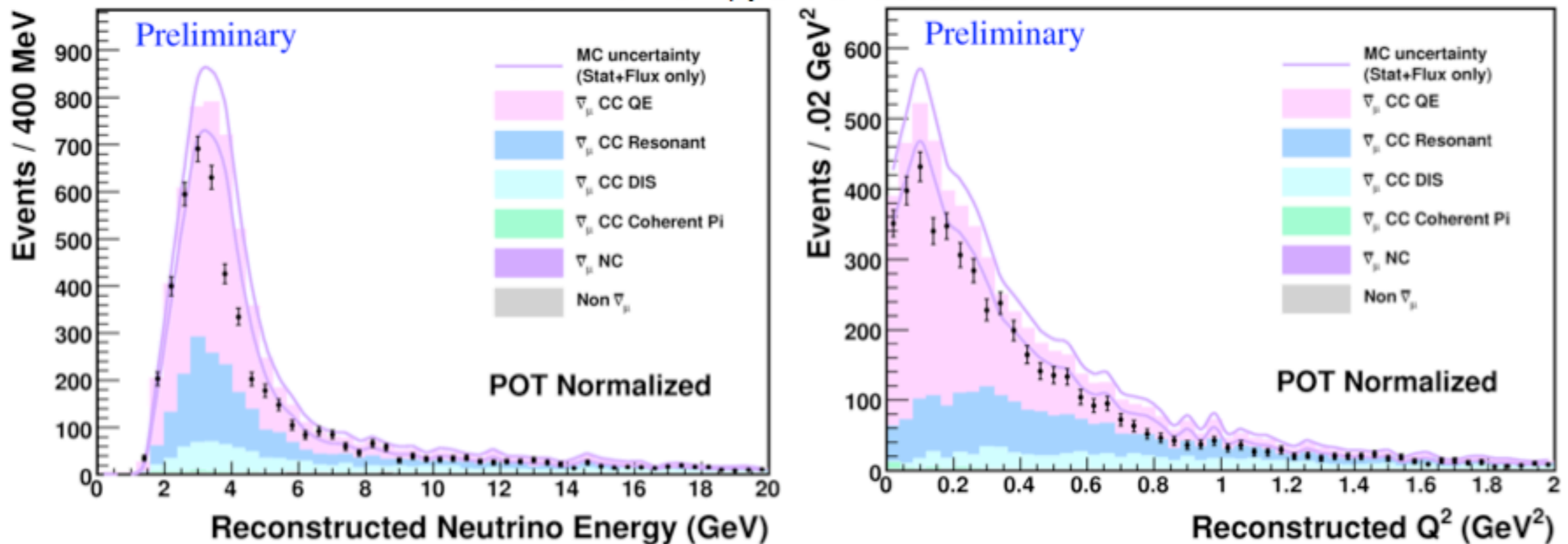
$\bar{\nu}_\mu p \rightarrow \mu^+ n$ candidates

- Absolute normalization: protons + flux + cross-sections
- Recoil cut leaves Quasi-Elastic sample largely untouched, but reduces backgrounds significantly

MINERvA

$\bar{\nu}_{\mu} p \rightarrow \mu^{+} n$ candidates

0.4E20 POT, partial detector



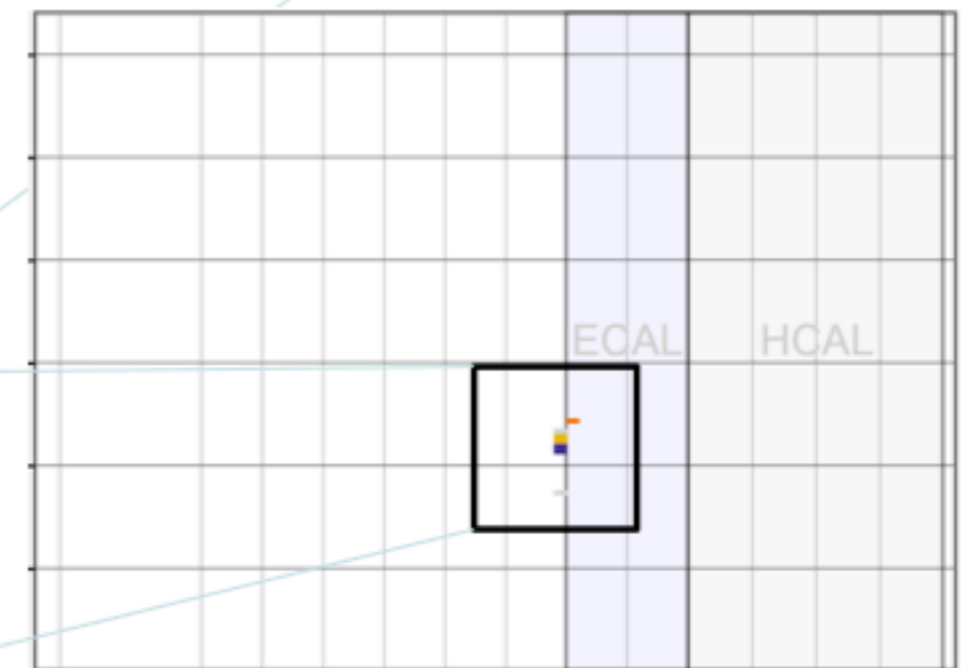
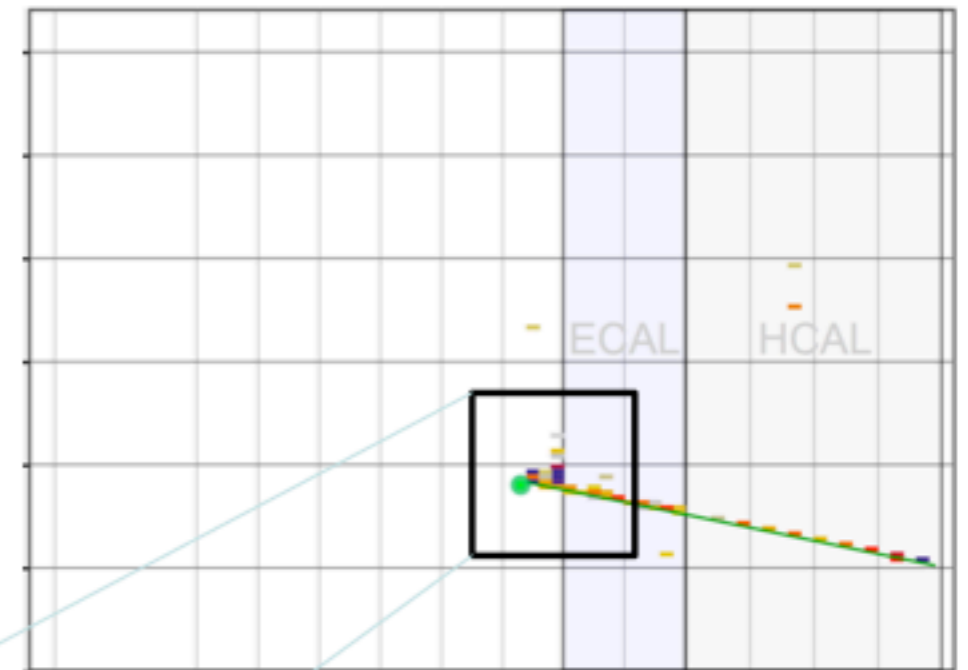
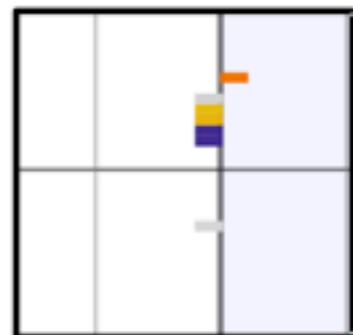
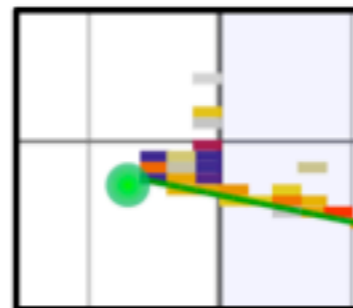
- Reminder: absolute predictions from flux simulation, GENIE 2.6.2, MINERvA simulation
- Event deficit is flat in Q^2 and not flat in E_{ν}

Ways to improve purity

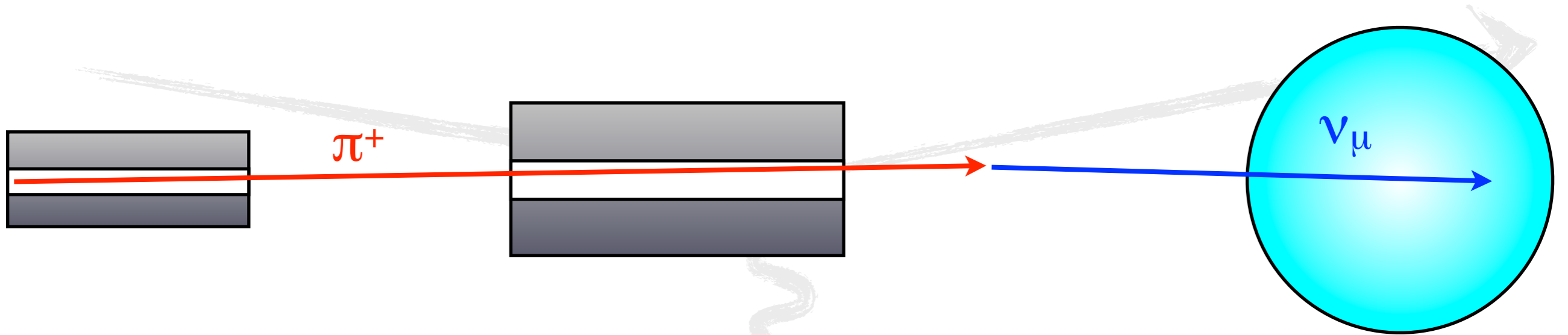
- The current strategy is generous in keeping signal events,
 - at the price of leaving a significant background, particularly at high Q^2 .
- This event illustrates two future background reduction techniques

- Recoil energy near the track

- Michel electron veto to remove π^\pm



Wrong sign BGs



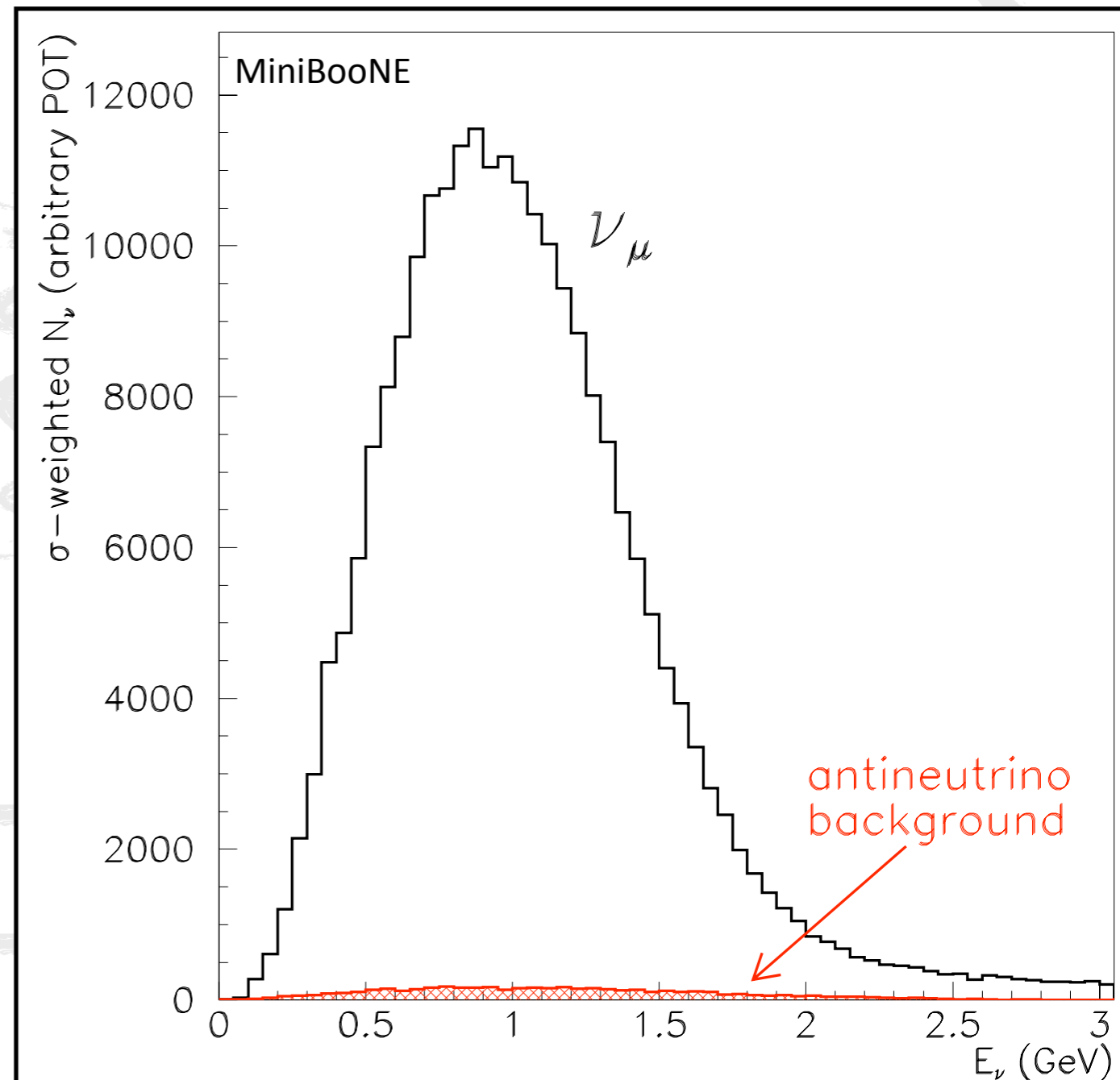
Neutrino horns cannot focus (or sign-select) pion passing *inside* the inner conductor.

More π^+ produced than π^- , so unfocused beam is predominantly ν_μ not $\bar{\nu}_\mu$.

Wrong Sign BGs

Gang of Four

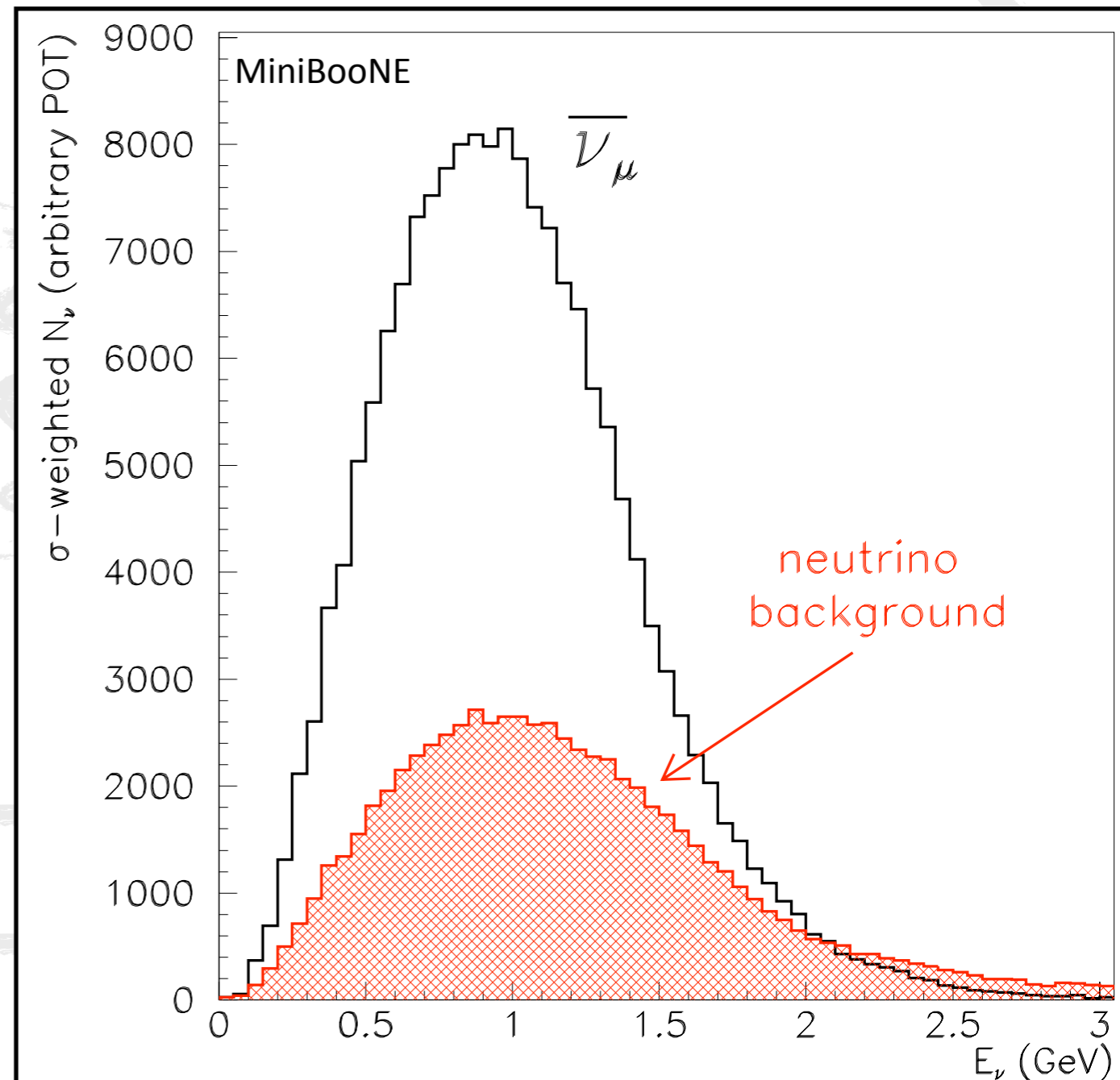
- In neutrino running, wrong sign backgrounds are very small (2%)
- In antineutrino running they are much larger (~30%)
- Cherenkov calorimeters cannot distinguish μ^- from μ^+
- Need a way to extract the WS BGs!



Wrong Sign BGs

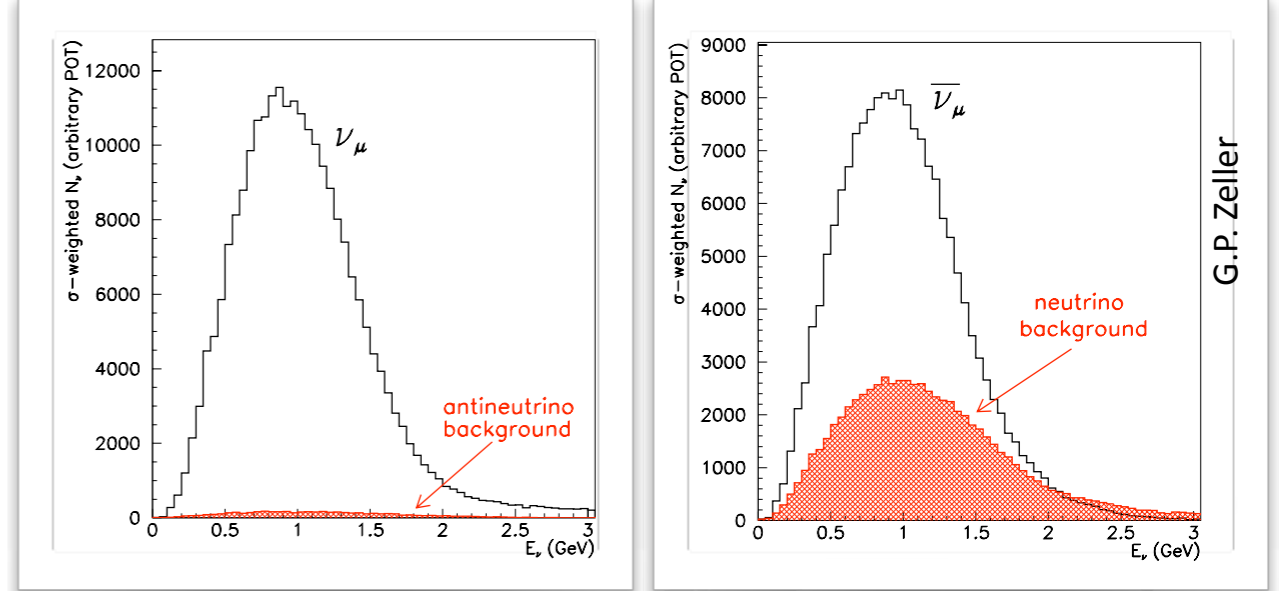
Gang of Four

- In neutrino running, wrong sign backgrounds are very small (2%)
- In antineutrino running they are much larger (~30%) for BooNEs
- Cherenkov calorimeters cannot distinguish μ^- from μ^+ (event by event)
- Need a way to extract the WS BGs!



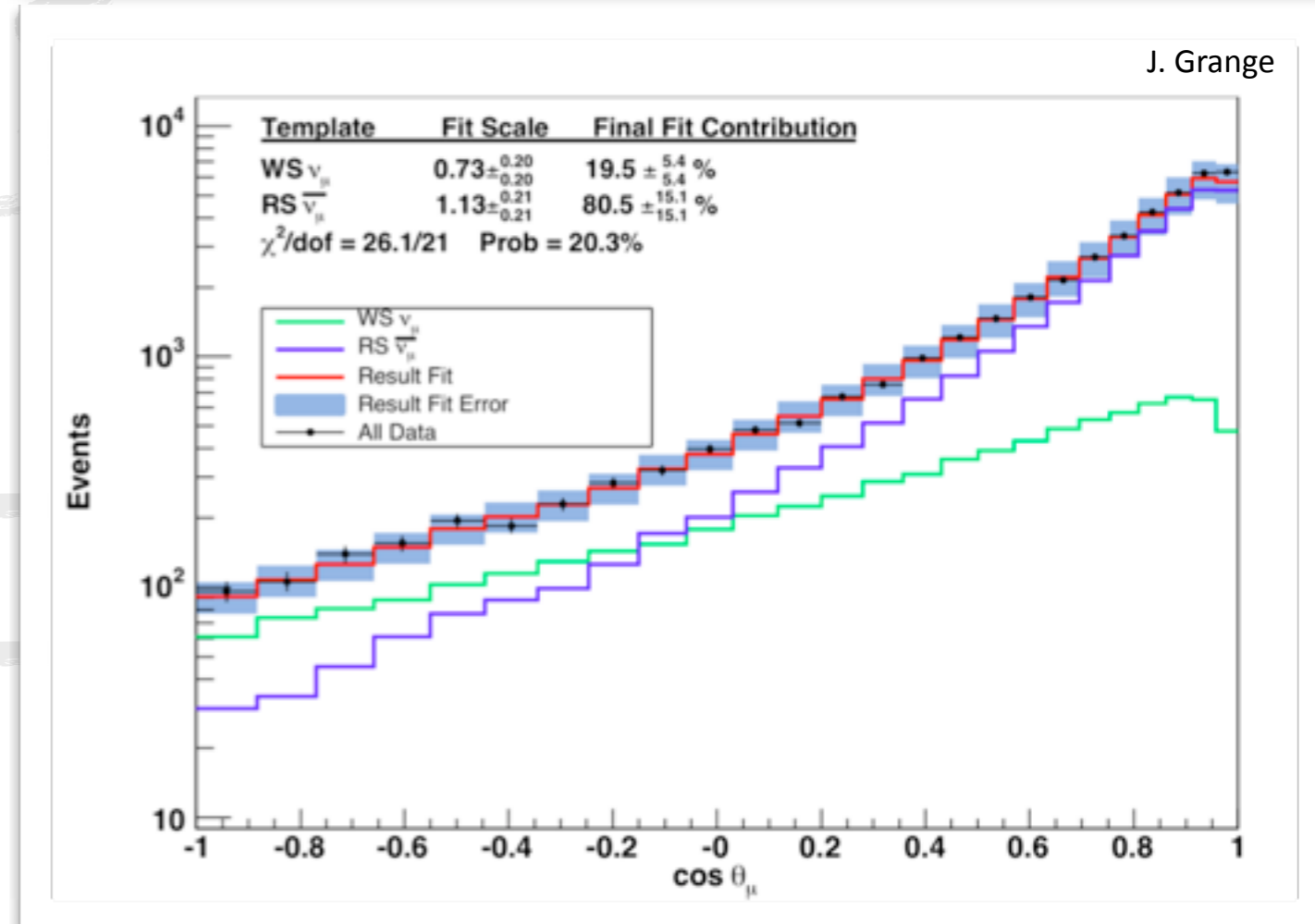
MiniBooNE Antineutrinos

- Very few measurements of nubar CCQE near 1 GeV
- Horn focussing leads to wrong sign (WS) backgrounds
 - neutrinos in antineutrino mode
- MiniBooNE has sophisticated analysis to constrain WS BGs
- Different angular distributions

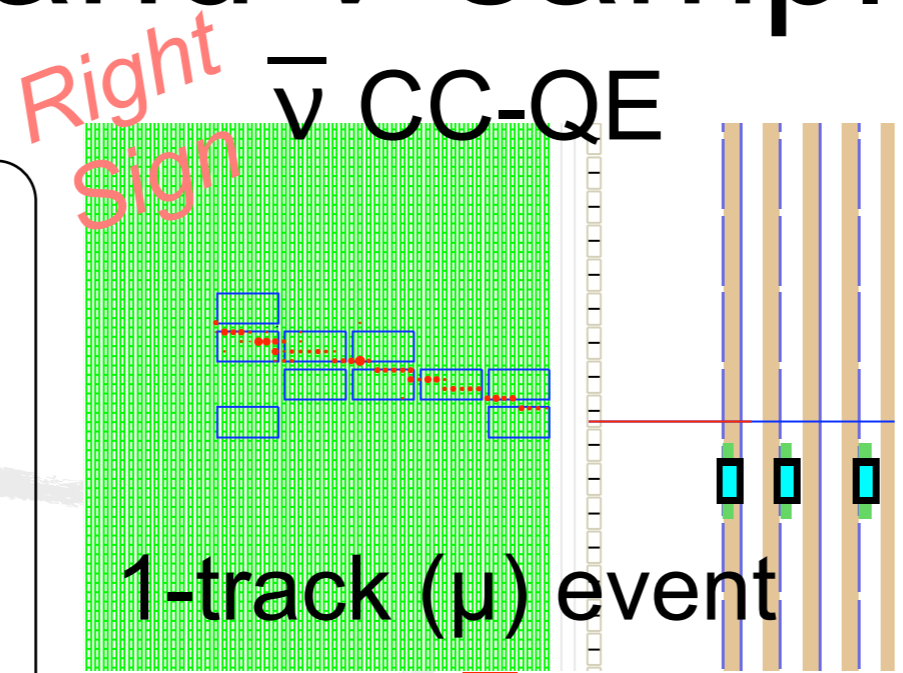
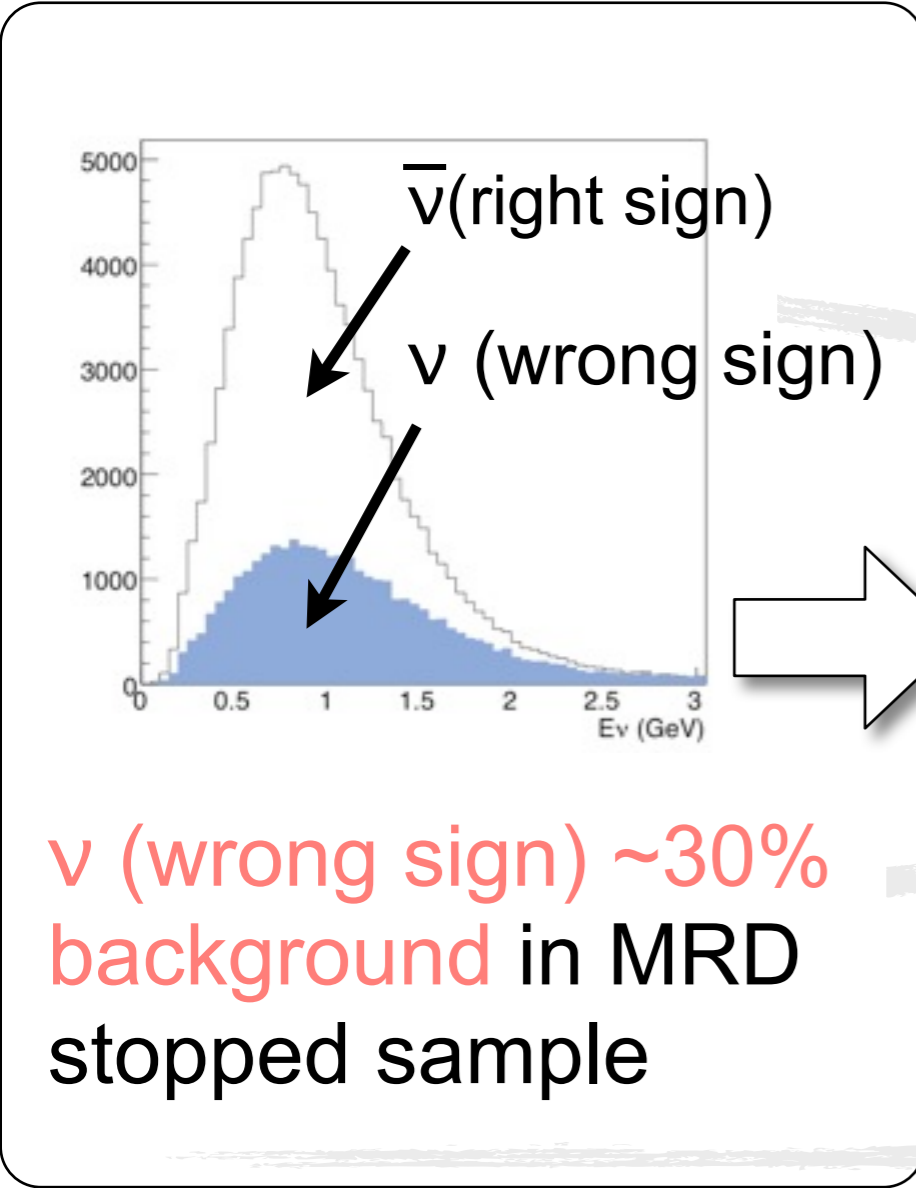


$$\frac{d\sigma^{QE}}{dQ^2} = \frac{M^2 G_F^2 |V_{ud}|^2}{8\pi E_\nu^2} \left[A(Q^2) \pm B(Q^2) \times \left(\frac{s-u}{M^2}\right) + C(Q^2) \times \left(\frac{s-u}{M^2}\right)^2 \right]$$

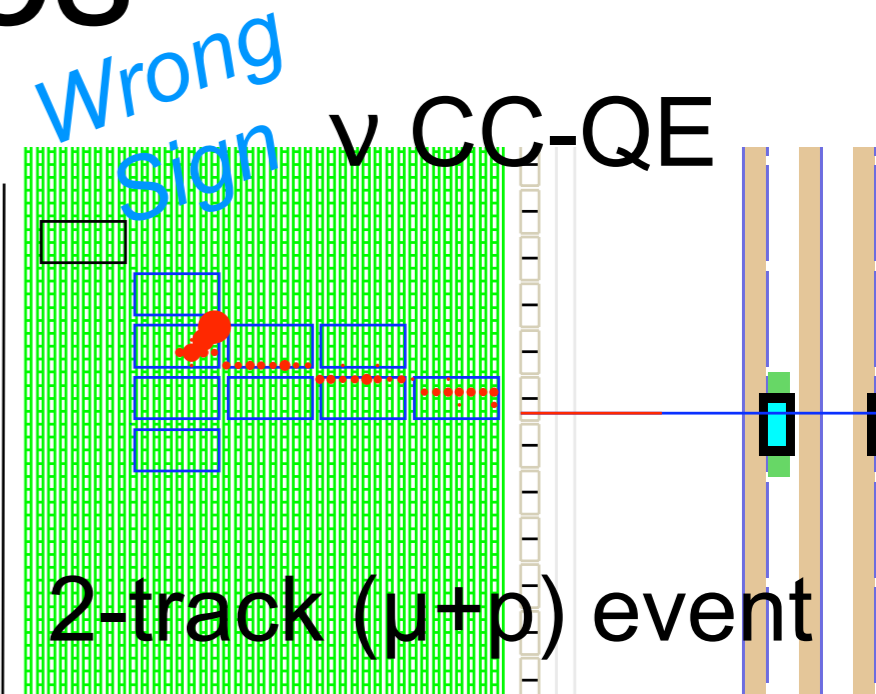
+ for ν , - for $\bar{\nu}$



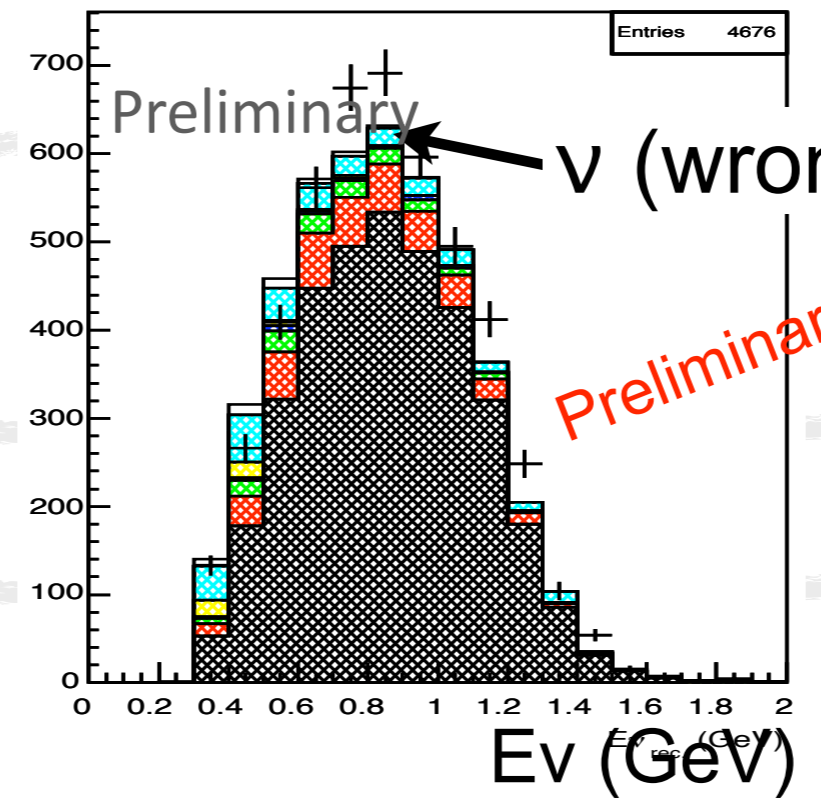
$\bar{\nu}$ and ν samples



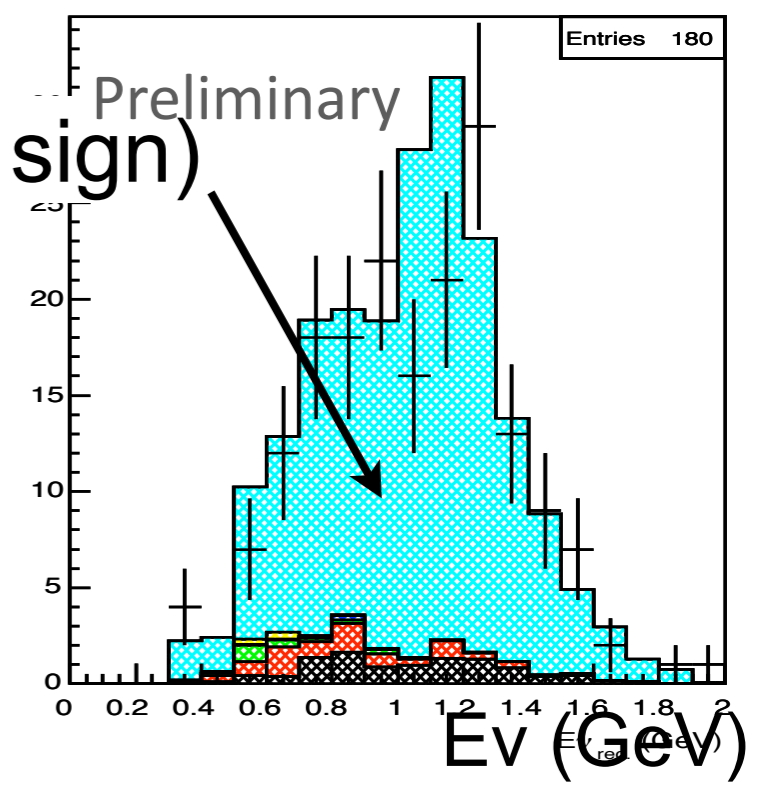
~90% $\bar{\nu}$ purity
 ($\bar{\nu}$ CC-QE: 80%)



~90% ν purity
 (ν CC-QE: 75%)



1-track w/o activity sample



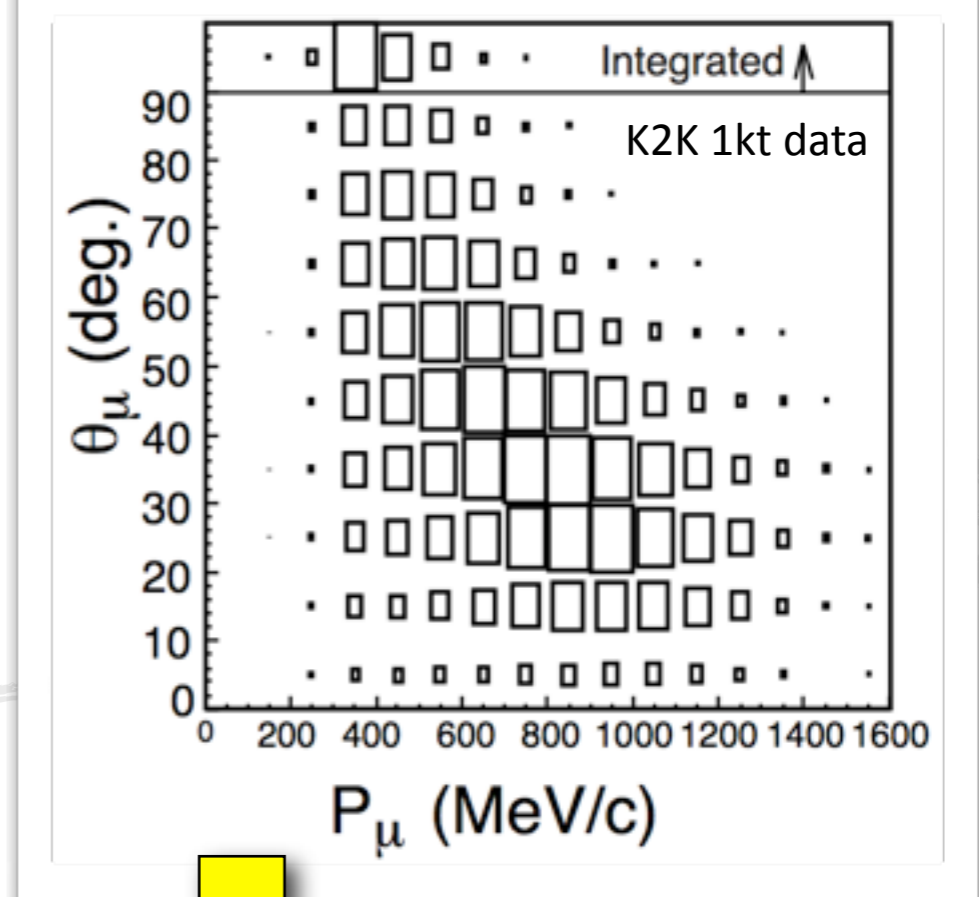
2-track QE-like sample

- $\bar{\nu}$ CC QE
- $\bar{\nu}$ CC resonant π
- $\bar{\nu}$ CC coherent π
- $\bar{\nu}$ CC other
- $\bar{\nu}$ NC
- ν (wrong sign)
- BG (EC/MRD events)

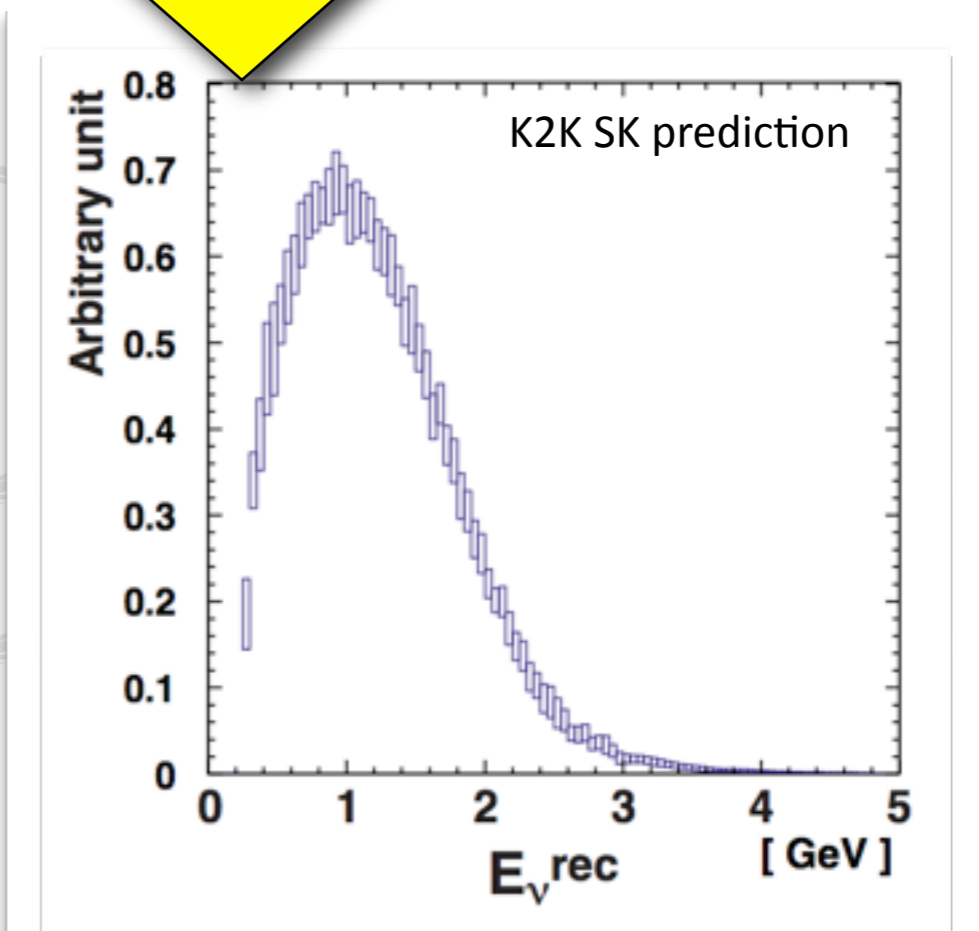
Putting these in context

What do we need?

- Need to predict event rates and kinematics of final state particles
- Need to reconstruct neutrino energy accurately
- Need to accurately predict background contamination
- ➔ Need precise neutrino-nucleus cross-sections
- ➔ Need good models



[Phys.Rev.D 74 072003 \(2006\)](#)



CCQE and Oscillations

- Current models cannot describe K2K, MiniBooNE, SciBooNE observations.
- Model dependence will always be injected into data analysis
 - Energy, Q^2 reconstruction
 - Background subtraction
- Using current models will always give such uncertainties.
 - Need better models!

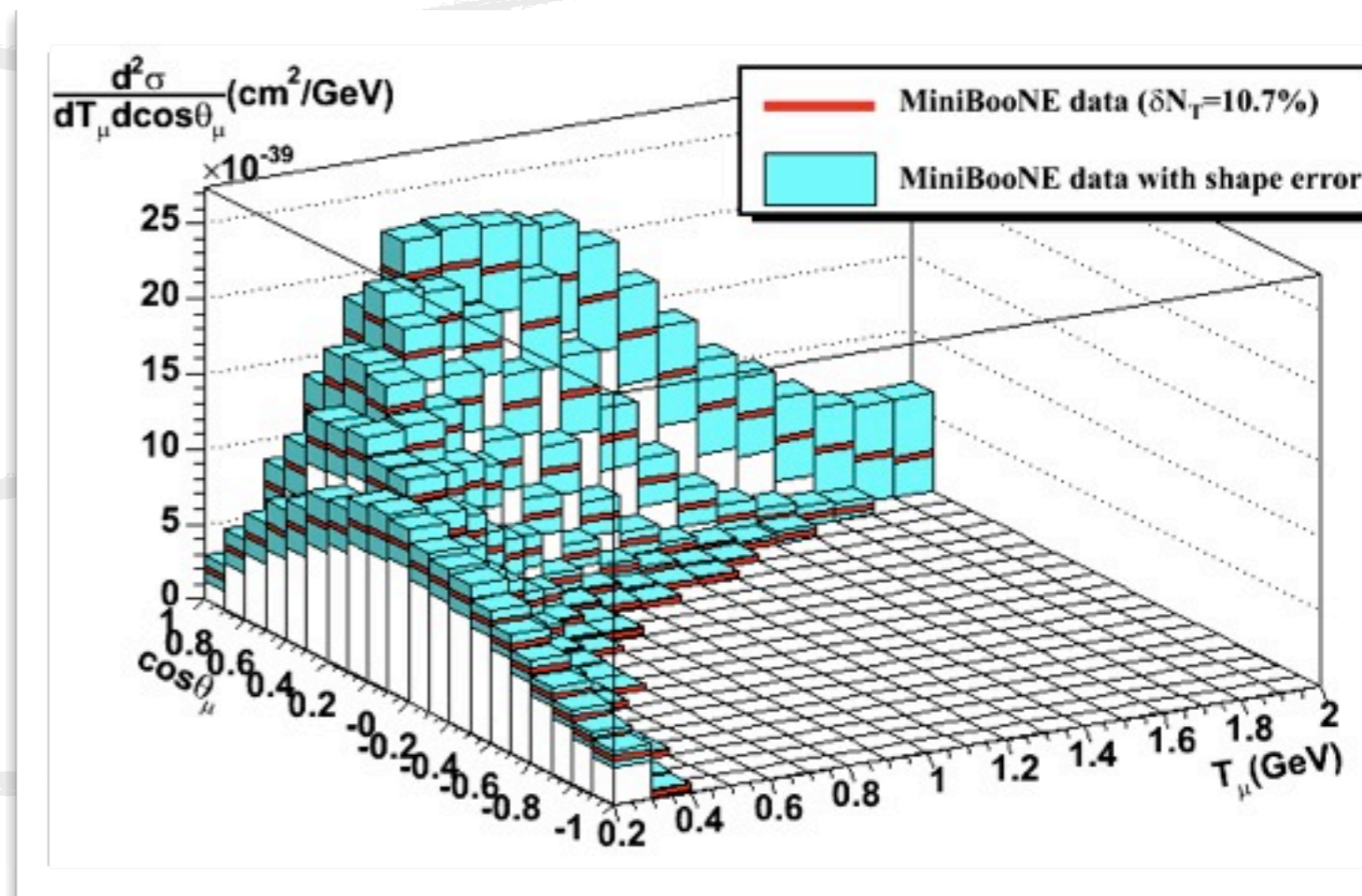
MiniBooNE ν_e appearance systematic uncertainties

Source	Error(%)
Flux from π^+/μ^+ decay	6.2
Flux from K^+ decay	3.3
Flux from K^0 decay	1.5
Target and beam models	2.8
ν-cross section	12.3
NC π^0 yield	1.8
External interactions ("Dirt")	0.8
Optical model	6.1
DAQ electronics model	7.5

[Conrad & Louis, FNAL Wine and Cheese Apr 11 2007](#)

MiniBooNE's final ν_μ CCQE result

- Flux averaged double differential CCQE cross section
- Most complete, and least biased, information possible about the cross section based on the muon kinematics
- Also being pursued for multi-particle final states
- Crucial input for theorists!



[PhysRevD 81 092005 \(2010\)](#)

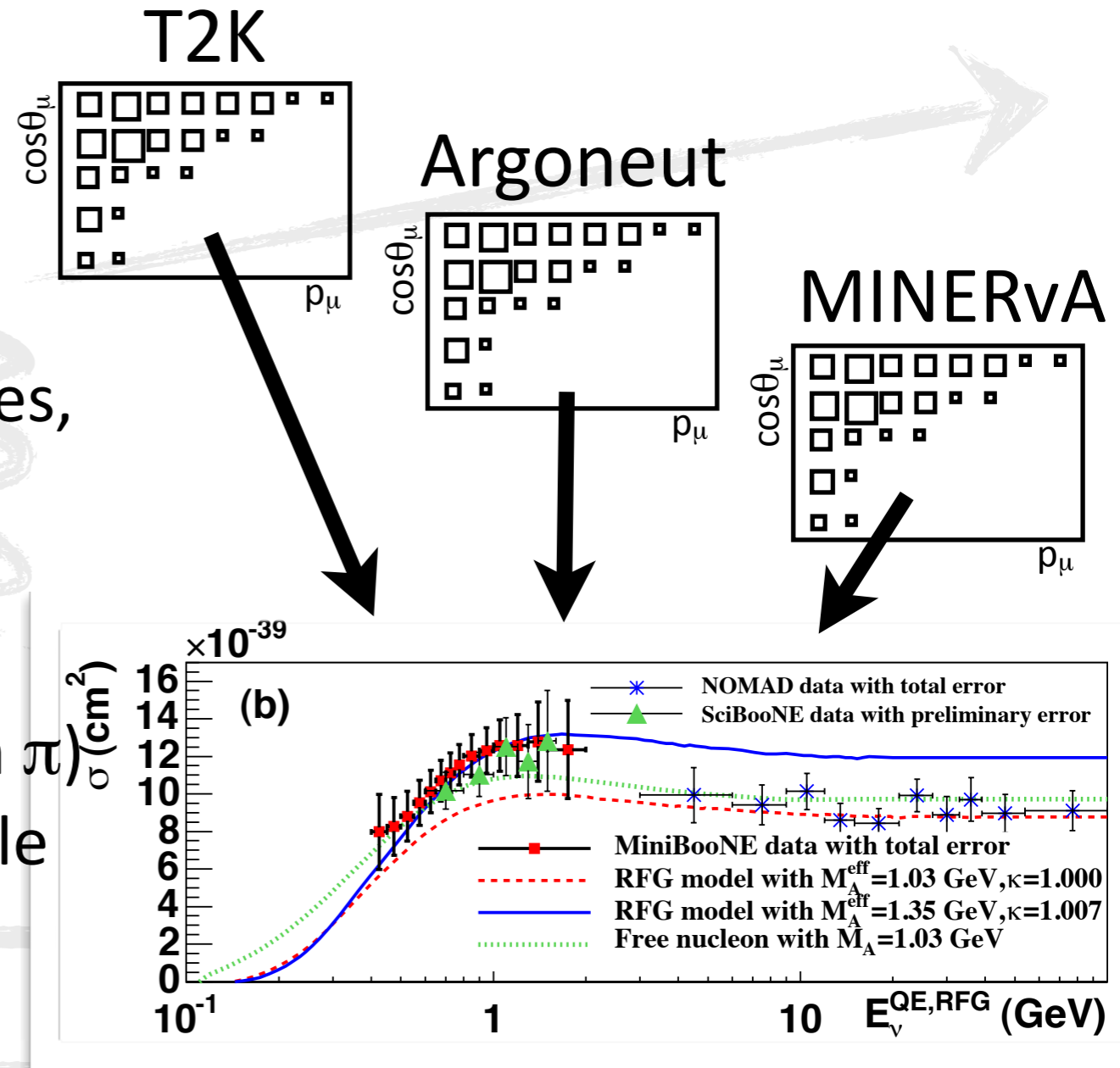
Wrap up

Summary of measurements

- Recent measurements of ν_μ CCQE scattering have much higher statistics and better controlled flux systematics than past.
- In 1 GeV region, experiments on nuclear targets show increased cross-section, harder Q^2 spectrum, and large suppression at low Q^2 ($<0.2 \text{ GeV}^2$).
 - Higher M_A ? Non-dipole F_A ? Nuclear model? Impulse approximation? Many body effects?
- At higher energy, world average model with RFG seems to work fine.

Growing Consensus

- We need broad coverage
 - Model independent measurements at many energies, nuclei
- Move away from process cross-sections
 - $\sigma(\text{CCQE})$, $\sigma(\text{CC res } \pi)$, $\sigma(\text{CC coh } \pi)$
- Instead measure final state particle cross-sections
 - $\sigma(\text{CC})$, $\sigma(\mu)$, $\sigma(\mu+p)$, $\sigma(\mu+\pi)$
 - (CC Inclusive measurements offer most robust confrontation of theory and experiment)



Same goes for NC...

What does model dependence mean?

- Distinguish between σ model and detector model
 - Any MC-derived quantity is, of course, model-dependent
- Restricting unsmearing, BG corrections, and efficiencies to detector MC quantities, not cross section processes is probably the best we can do
- This is why we push the idea of final state particle cross sections over process measurements

Absolute flux-averaged differential cross section formula

U_{ij} : unsmearing matrix

d_j : data vector

$$\sigma_i = \frac{\sum_j U_{ij} (d_j - b_j)}{\varepsilon_i (\Phi T)}$$

b_j : predicted background

ε_i : efficiency

T : integrated target number

Φ : integrated ν -flux

Best way to present data?

- To get better models, we need theorists to use our data effectively
 - It's in our best interest to make that as easy as possible
- Typically, our goal is to produce cross section measurements
 - We use the detector MC to model the efficiency and smearing,
 - We then correct those effects with unfolding matrices and efficiency functions

Best way to present data?

- We could alternatively provide theorists with the tools to analyze our data the way that we do
 - For example, when fitting for M_A , we use the detector MC to make fake data sets, and modify the fake data sets until the MC matches data
 - For example, numbers of events in bins of p_μ, θ_μ
 - We obviously don't want to give away the detector MC, but we could provide efficiency functions (including smearing) with systematics and our measured data
 - The efficiency function could be applied to inclusive fake data samples, allowing theorists to perform analysis the way we do
 - Obviously need to provide fluxes, too, but we already do that.

CCQE Conclusions

- We observe discrepancies between CCQE data and models, & between experiments.
- Flux constraints are crucial for cross section measurements.
- Need model independent measurements so that new models can be tested.
 - MiniBooNE has published world's first absolutely normalised double differential cross section!
 - New measurements from Fermilab can and should provide the needed data for better models.

Conclusions

- Cross section measurements are needed to interpret neutrino oscillation data.
- New measurements are revealing problems left unseen by previous experiments.
- These problems have consequences for oscillation experiments.
- New data analysis philosophies are needed so we can improve theoretical models.
- Observing CP violation relies on this!!



Thank you for your attention!

ご清聴ありがとうございました

水戸の梅の花