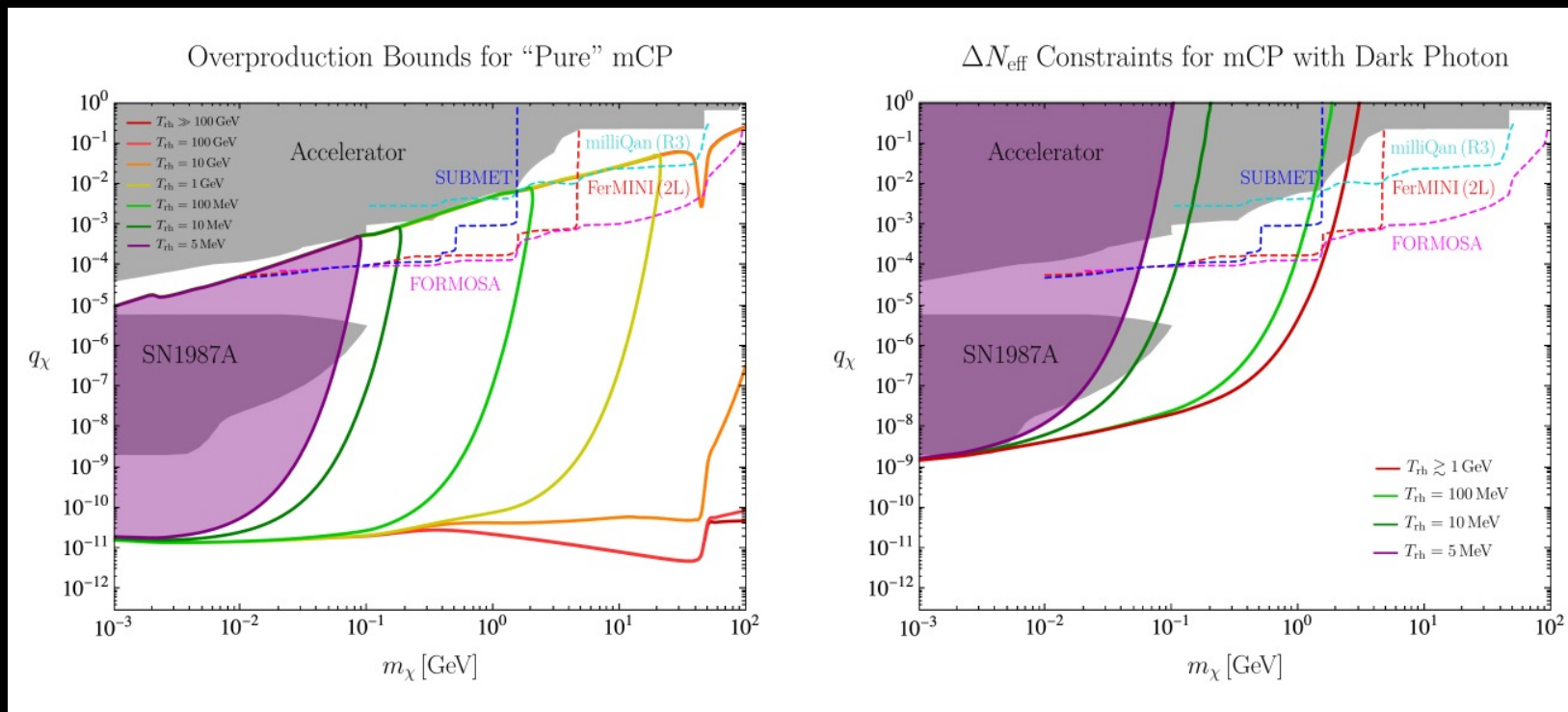


# Cosmic Millicharge Background: Probing Fundamental Theory & Reheating Cosmology



Gan, Tsai, 2308.07951

**Yu-Dai Tsai**

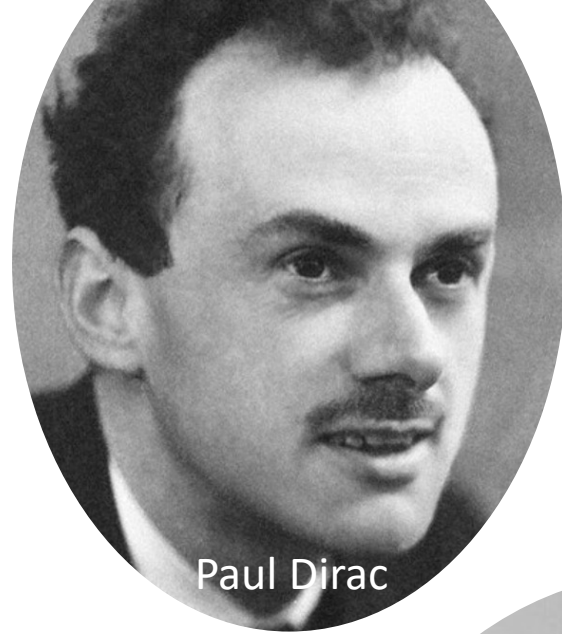
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Gan, Tsai, 2308.07951,

LANL mCP Search: LANSCE-mQ, 2407.07142

# Outline

- Intro & Motivations
- Probing Reheating Cosmology
- Differentiating two types of mCPs



Paul Dirac



Frederick Reines 2

# Theoretical Motivations

**Millicharged particle (mCP)** is a particle  $\chi$  with {mass, electric charge} =  $\{m_\chi, \epsilon e\}$

$$\epsilon = Q_\chi/e$$

## 1. Is electric charge quantized? To what unit? And why?

Long-standing questions:

- Inspired Dirac quantization, Grand Unified Theories (GUTs)
- String theory predicts un-confined fractionally charged particles  
Wen, Witten, Nucl. Phys. B 261 (1985) 651-677  
[Conversation: Salam, Sciama, Witten and Budinich](#) (ICTP, 1986)
- More links to string compactification & quantum gravity (Shiu, Soler, Ye, PRL '13)  
+ new theoretical developments

## 2. Millicharged dark matter Implications & explain CMB absorption spectrum

# Two Kinds of mCP

## “Pure” mCP

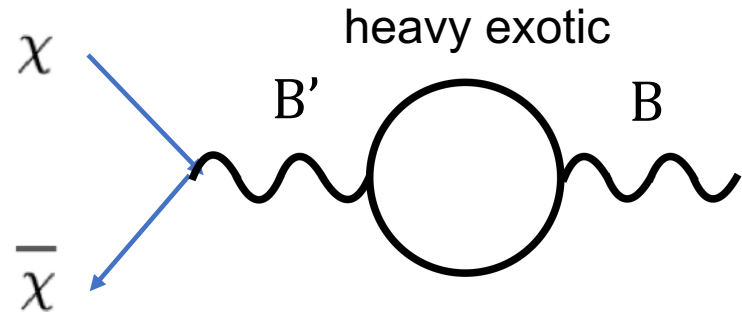
- Theoretical implication of mCP with a **small (irrational) charge without a dark photon**
  - Implications on **GUTs models**
  - Implications on **string compactifications**
- Shiu, Soler, Ye, *PRL* (2013)



$$\mathcal{L}_{\text{MCP}} = i\bar{\chi}(\not{\partial} - i\epsilon'e\not{B} + M_{\text{MCP}})\chi$$

## Kinetic-mixing mCP

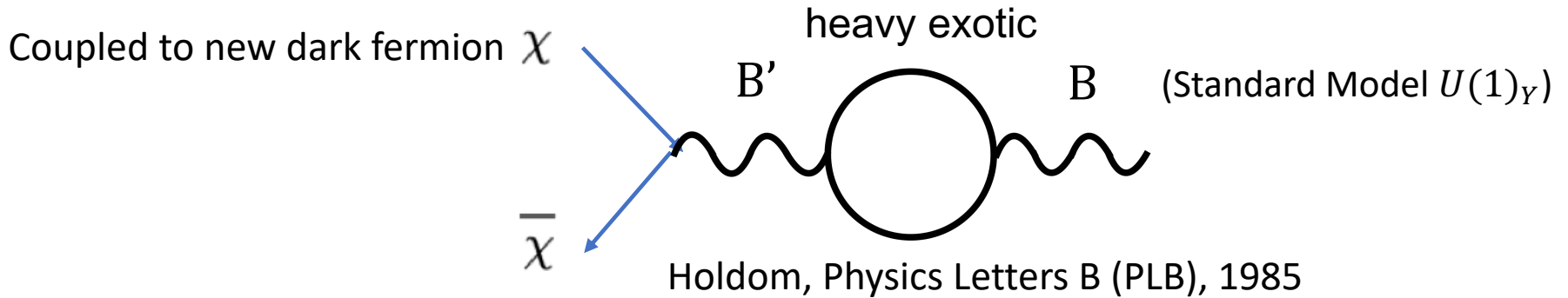
- Compatible with GUTS.



Choose a proper basis:  
**massless dark photon A'**  
**decouple from SM**



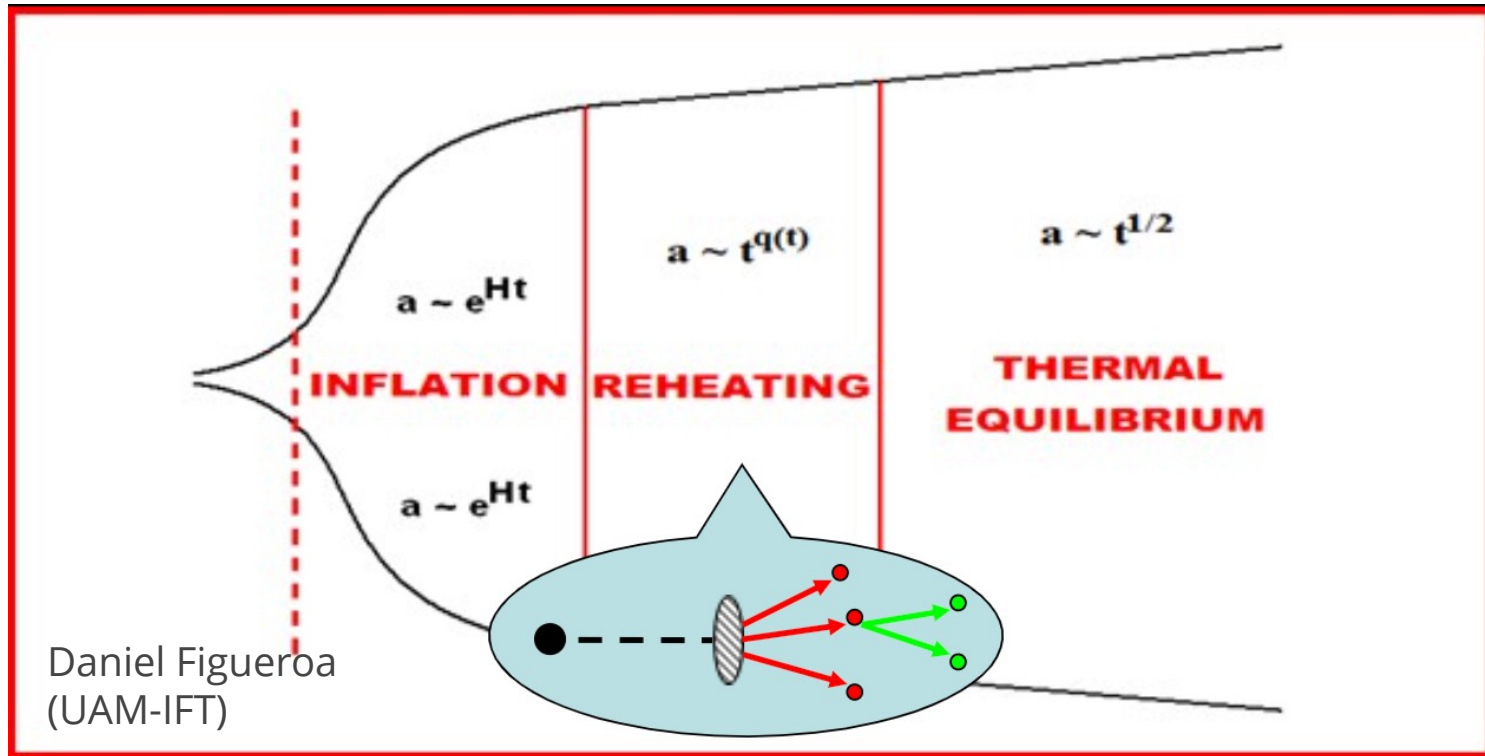
# Kinetic Mixing mCP



$$\mathcal{L} = \mathcal{L}_{\text{SM}} - \frac{1}{4} B'_{\mu\nu} B'^{\mu\nu} - \frac{\kappa}{2} B'_{\mu\nu} B^{\mu\nu} + i\bar{\chi}(\not{\partial} + ie' \not{B}' + iM_{\text{MCP}})\chi$$

- New Fermion  $\chi$  charged under  $U(1)'$
- Field redefinition into a more convenient basis for massless  $B'$ ,  $B' \rightarrow B' + \kappa B$
- new fermion acquires a small EM charge  $Q$  (the charge of mCP  $\chi$ ):  $Q = \kappa e' \cos \theta_W$ ,  $\epsilon \equiv \kappa e' \cos \theta_W / e$ .

# Inflation and Reheating



$a$ : scale factor, basically quantifying the size of the Universe  
 $t$ : time

**We know very little about reheating. We don't even know what temperature does it reheat to!**

# Cosmic Millicharge Background (CmB)

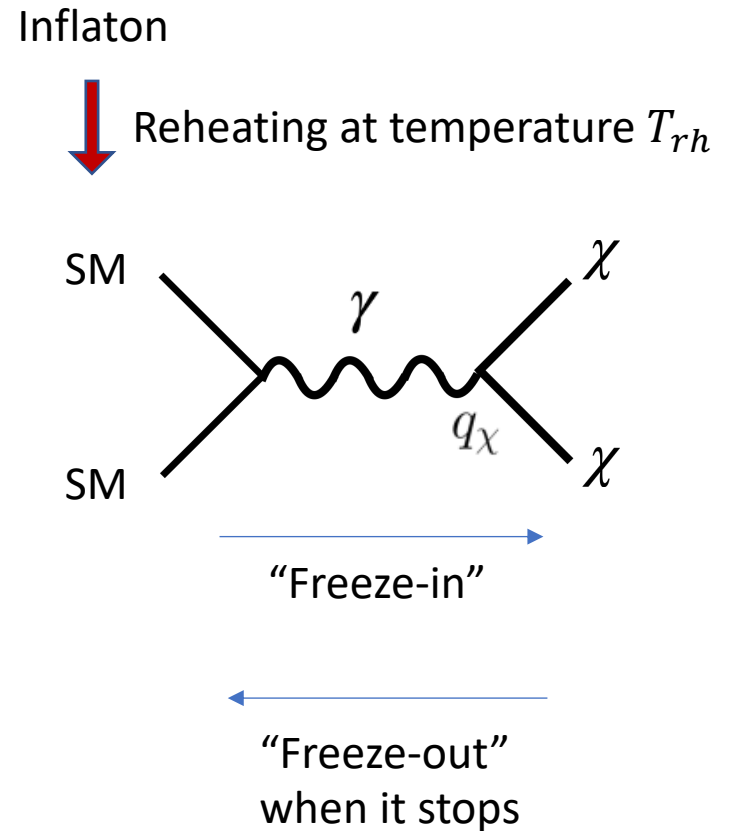
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## “Pure” mCP

- mCP with a **small (irrational) charge & no dark photon**
- **Indirect test of GUTs models**
- **Indirect test of string compactifications**  
Gan, Shiu, Tsai, in progress

$$\mathcal{L}_{\text{MCP}} = i\bar{\chi}(\not{\partial} - i\epsilon'e\cancel{B} + M_{\text{MCP}})\chi$$

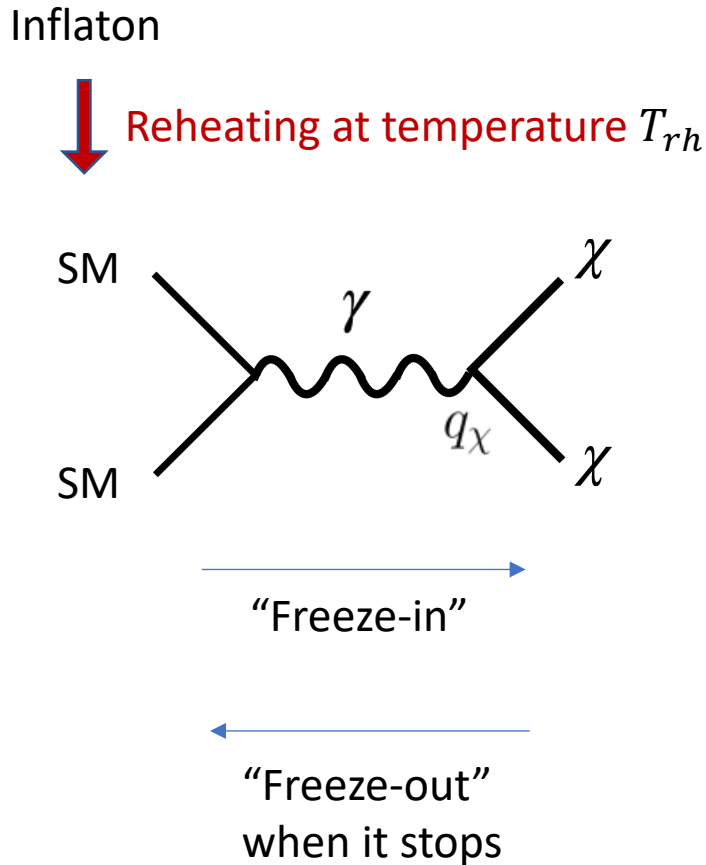
## Irreducible Production during Reheating



# Cosmic Millicharge: Overproduction During Reheating

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## Irreducible Production during Reheating



mCP can be easily “overproduced”,  
to more than that of the observed  
amount of dark matter (DM)

$$\Omega_{\text{DM}} h^2 \sim 0.12$$

Currently measured DM abundance

$$\Omega \equiv \frac{\rho}{\rho_c}$$

Density is normalized by  $\rho_c$ , the critical  
density for a flat Universe;  $h = 0.674$

$$\rho_c = \frac{3H^2}{8\pi G}$$

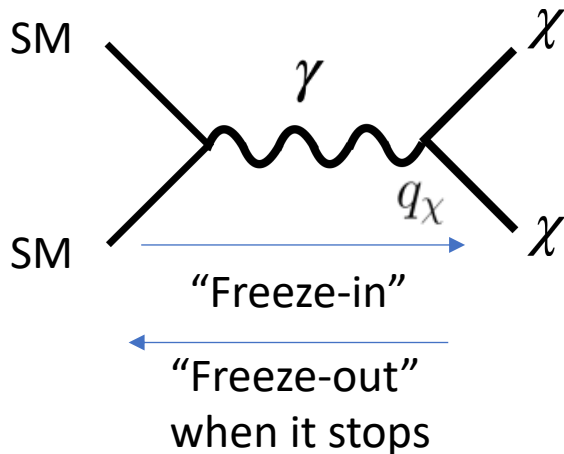
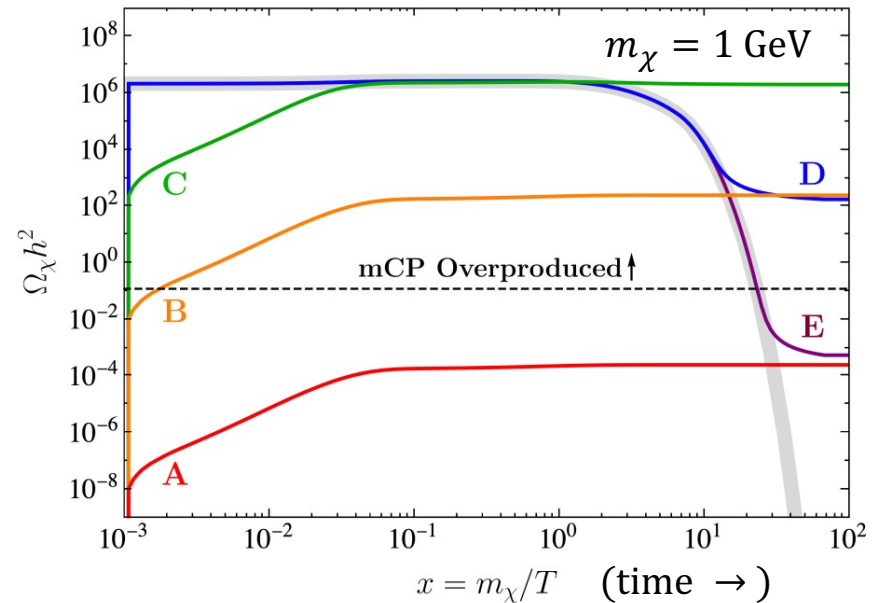
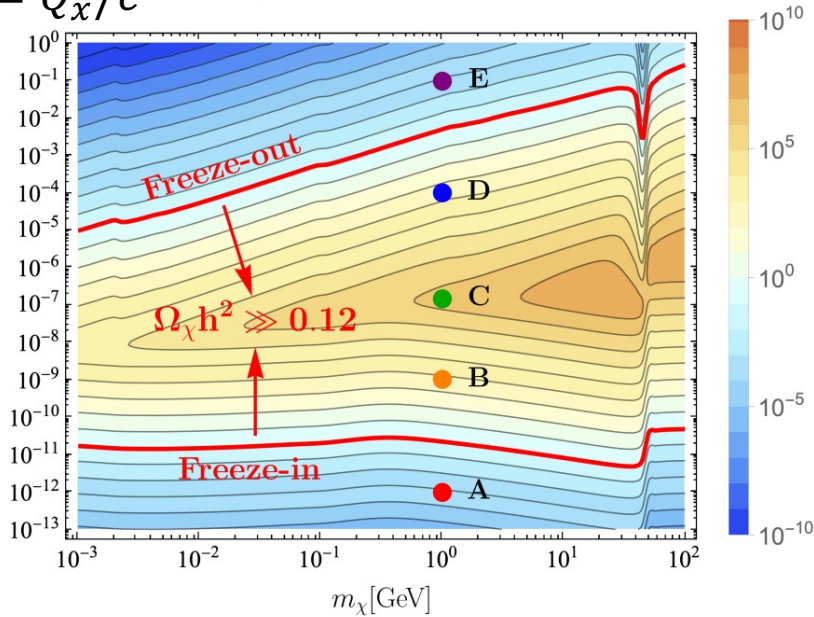


# “Pure” CmB Cosmology: Freeze-in and Freeze-out

$T_{rh} = 1 \text{ TeV (or above)}$

$$\epsilon = Q_x/e$$

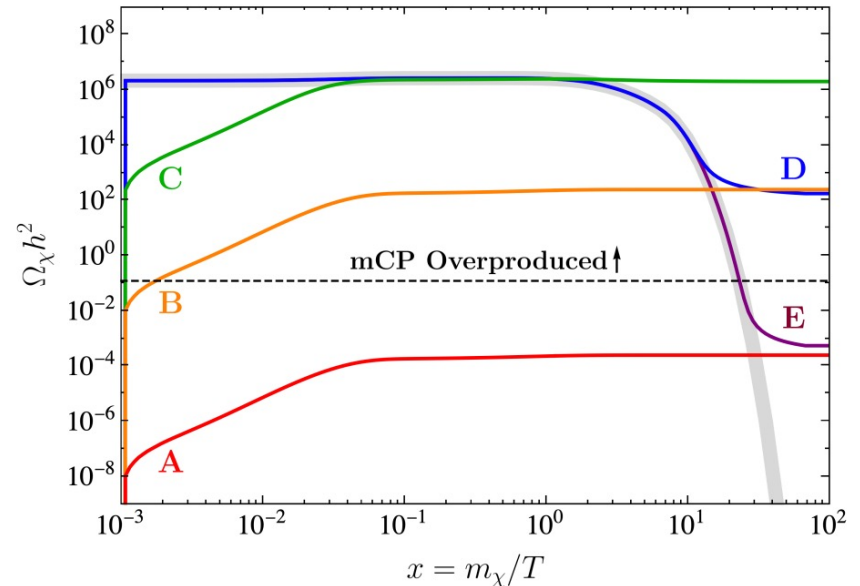
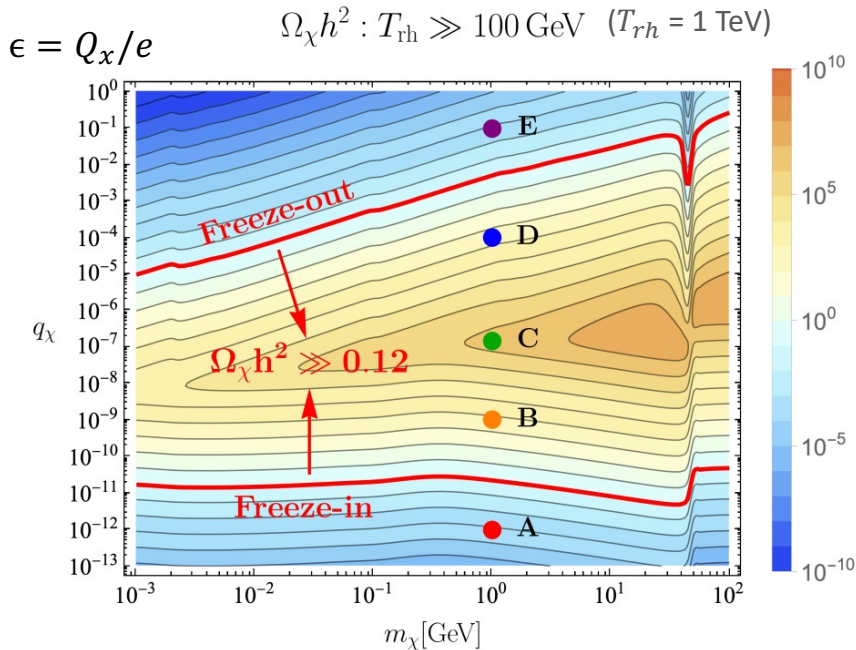
$\Omega_\chi h^2 : T_{rh} \gg 100 \text{ GeV}$



$$\dot{n}_\chi + 3Hn_\chi \simeq C_n(T) \left( 1 - \frac{n_\chi^2}{n_{\chi,eq}^2} \right),$$

$$C_n(T) = 2n_Z \langle \Gamma \rangle_{Z \rightarrow \chi \bar{\chi}} + 2n_f n_{\bar{f}} \langle \sigma v \rangle_{f \bar{f} \rightarrow \chi \bar{\chi}}$$

# “Pure” CmB Cosmology: Freeze-in and Freeze-out



Freeze-in:  $Y_\chi^{\text{FI}} \sim q_\chi^2 \alpha_{\text{em}}^2 \frac{m_{\text{pl}}}{T}, \quad T \gtrsim m_\chi.$

Freeze-out:  $Y_\chi^{\text{FO}} \sim \frac{1}{q_\chi^2 \alpha_{\text{em}}^2} \frac{m_\chi}{m_{\text{pl}}},$

$$\dot{n}_\chi + 3Hn_\chi \simeq C_n(T) \left( 1 - \frac{n_\chi^2}{n_{\chi,\text{eq}}^2} \right),$$

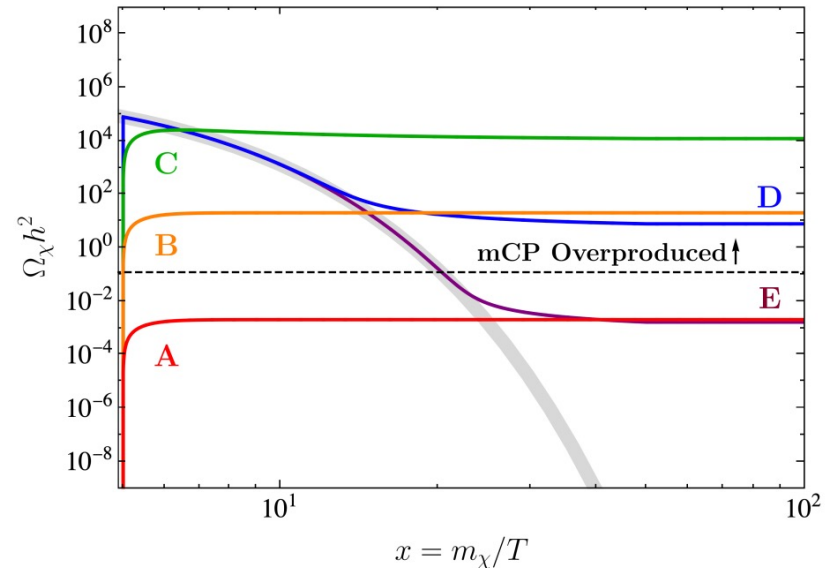
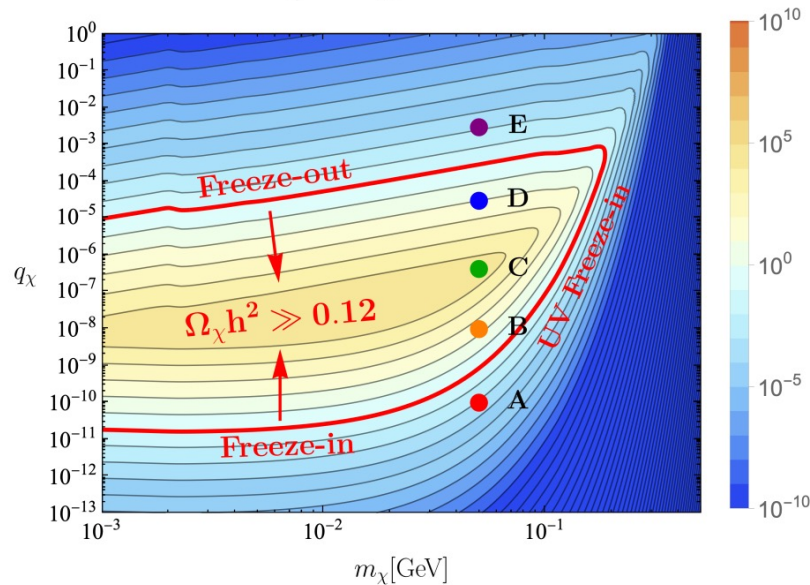
$$C_n(T) = 2n_Z \langle \Gamma \rangle_{Z \rightarrow \chi \bar{\chi}} + 2n_f n_{\bar{f}} \langle \sigma v \rangle_{f \bar{f} \rightarrow \chi \bar{\chi}}$$

See, e.g., Vogel, Redondo, JCAP (2014), Dvorkin+, PRD (2019)

# “Pure” CmB Cosmology: Low-Reheat Temperature

$$T_{rh} = 10 \text{ MeV}$$

$$\Omega_\chi h^2 : T_{rh} = 10 \text{ MeV}$$

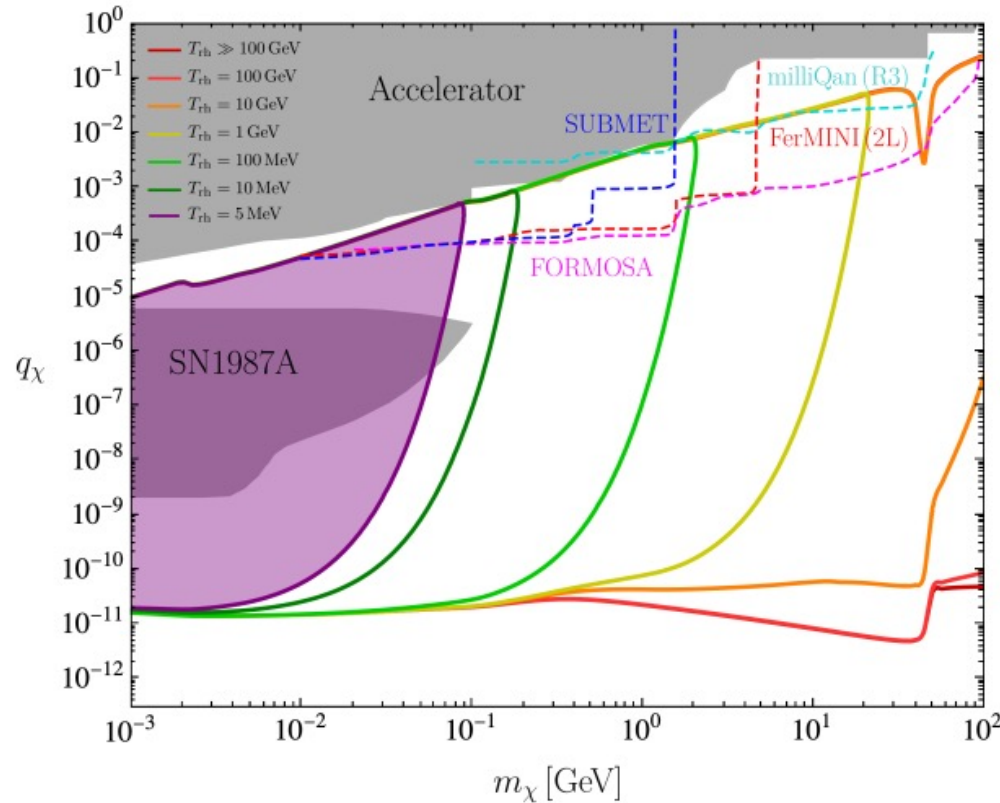


For the freeze-in at low  $T_{rh}$ , mCP-SM interaction is suppressed exponentially: the coupling has to increase exponentially to compensate it

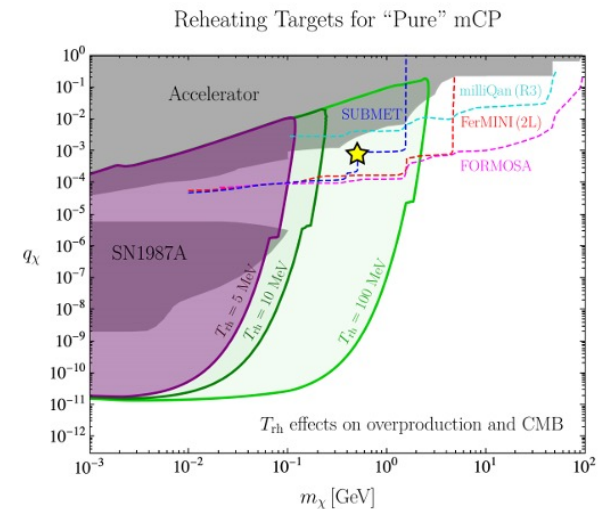
The freeze-in curve holds the approximate relation:  $q_\chi \propto \exp\left(\frac{m_\chi}{T_{rh}}\right)$

# “Pure” CmB from Irreducible Production

$\epsilon = Q_x/e$  Overproduction Bounds for “Pure” mCP



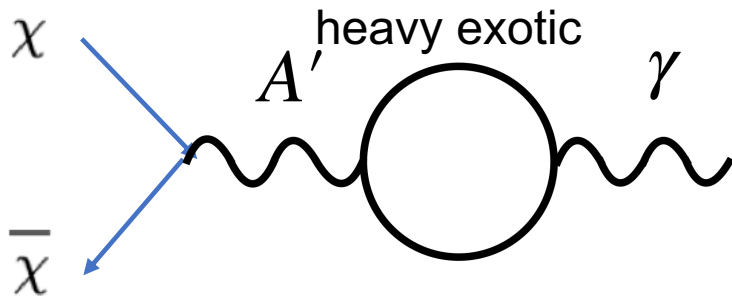
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- Minimal reheating temperature larger than  $T_{BBN}$  (e.g., Hasegawa+, JCAP19; Hannestad, PRD04)
- **Our purple bound is covering the SN1987A constraint** (gray region from Chang+, JHEP18)

# Kinetic-Mixing Cosmic Millicharge Background (CmB)

## Kinetic-mixing mCP



$$\mathcal{L} = \mathcal{L}_{\text{SM}} - \frac{1}{4} B'_{\mu\nu} B'^{\mu\nu} - \frac{\kappa}{2} B'_{\mu\nu} B^{\mu\nu} + i\bar{\chi}(\not{\partial} + ie'\not{B}' + iM_{\text{MCP}})\chi$$

Choose a proper basis:  
massless dark photon  $A'$  decouple from SM

$$q_\chi = \frac{\epsilon g_d}{e}$$

$$\mathcal{L}_{\text{MCP}} = i\bar{\chi}(\not{\partial} - i\epsilon'e\not{B} + M_{\text{MCP}})\chi$$

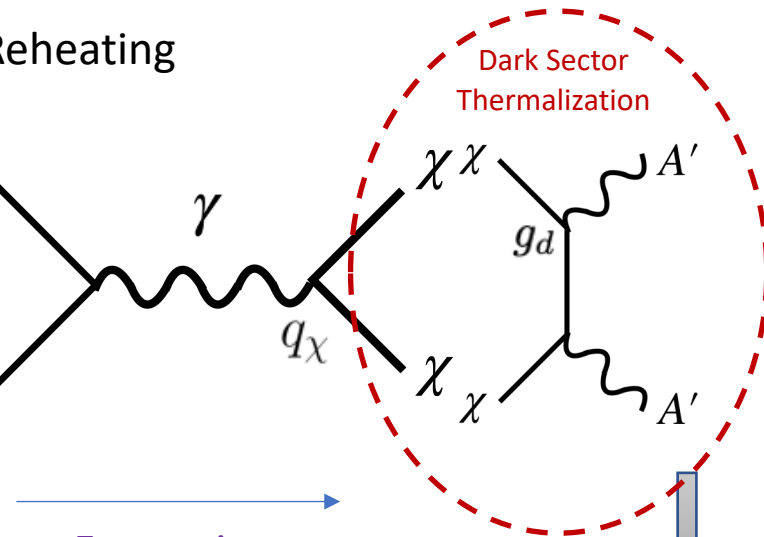
## Kinetic-mixing mCP

Inflaton

Reheating

SM

SM



Freeze-in:

Freeze-out:

massless dark photon  $A'$  will affect  $N_{\text{eff}}$   
See Vogel, Redondo, JCAP (2014),  
Adshead, Ralegankar, Shelton JCAP (2022)

# Kinetic-Mixing CmB Cosmology:

## $N_{eff}$ Effects from Dark Photon

- Freeze-in from the heat bath
- $\chi$  thermalizing with dark photon: Require effective transfer of  $\chi$  entropy to dark radiation  $A'$  here

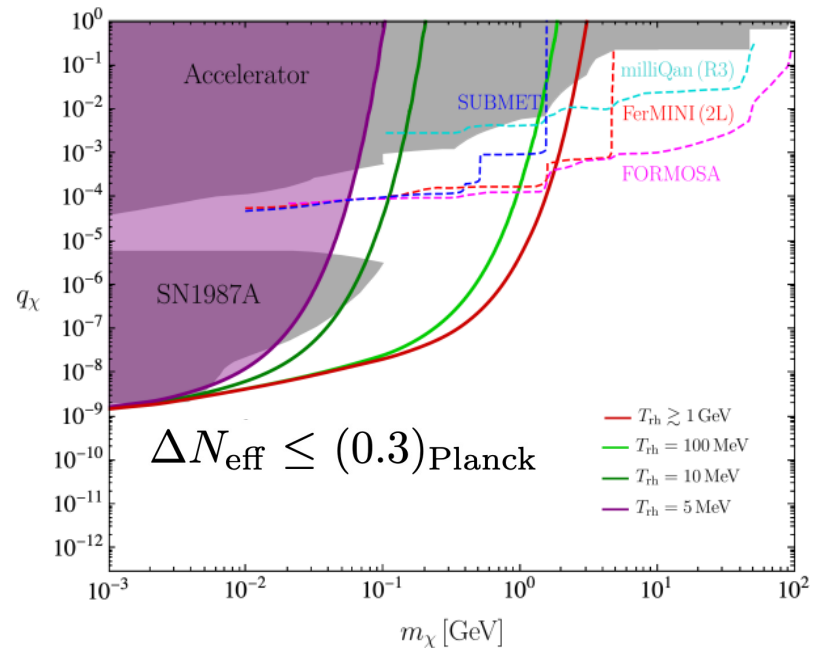
$$\frac{n_{\chi}^{\text{FI}} \langle \sigma v \rangle_{\text{dth}}}{H} \sim q_{\chi}^2 \alpha_{\text{em}}^2 \alpha_d^2 \left( \frac{m_{\text{pl}}}{T} \right)^2 \gg 1.$$

$$\alpha_d \gg 10^{-4}$$

- A quick  $\Delta N_{eff}$  estimation:

$$\Delta N_{\text{eff}} \sim q_{\chi}^2 \alpha_{\text{em}}^2 \frac{m_{\text{pl}}}{m_{\chi}}$$

$\Delta N_{\text{eff}}$  Constraints for mCP with Dark Photon

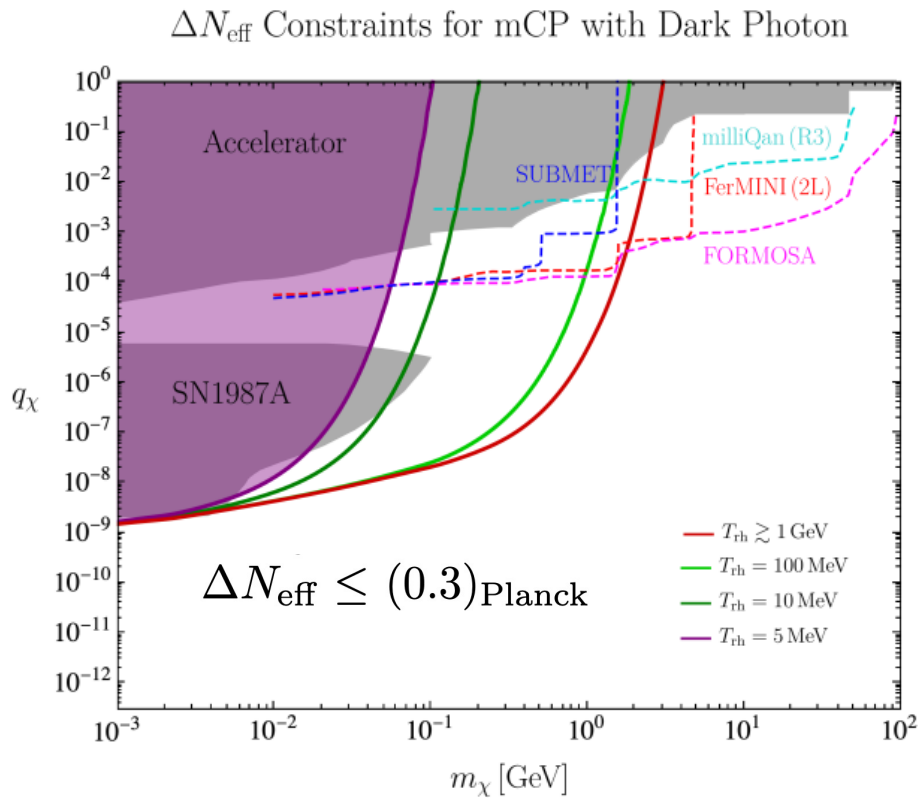


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- **Our purple bound is again covering the SN1987A constraint**



# Kinetic-Mixing CmB Cosmology



$$q_\chi \sim 10^{-7} \left( \frac{m_\chi}{1 \text{ GeV}} \right)^{1/2} \left( \frac{\Delta N_{\text{eff}}}{0.3} \right)^{1/2} \cdot m_\chi \leq T_{\text{rh}}$$

$$q_\chi \propto \exp\left(\frac{m_\chi}{T_{\text{rh}}}\right) \cdot m_\chi > T_{\text{rh}}$$

Considering higher reheating temperatures for region to the right of the red curve:

$$\Delta N_{\text{eff}} \lesssim g_{A'} \frac{4}{7} \left( \frac{g_{*,S}(T \ll T_{\text{QCD}})}{g_{*,S}(T \gg T_{\text{QCD}})} \right)^{4/3} \simeq 0.1,$$

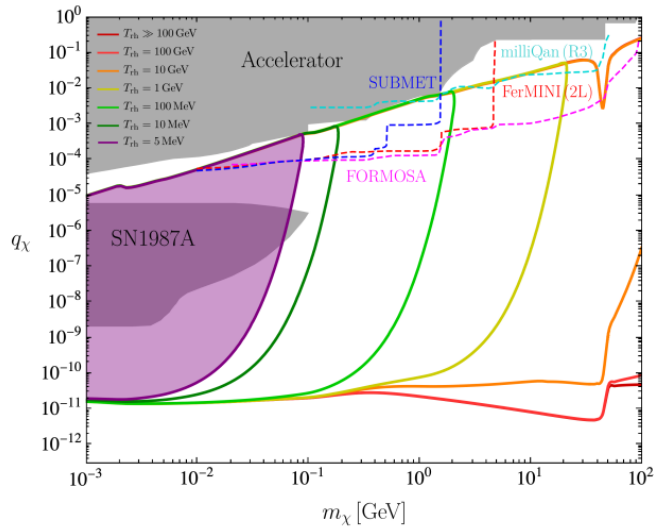
See Gan, Tsai, [2308.07951](#) for detailed discussions

Current:  $\Delta N_{\text{eff}} \leq (0.3)_{\text{Planck}}$

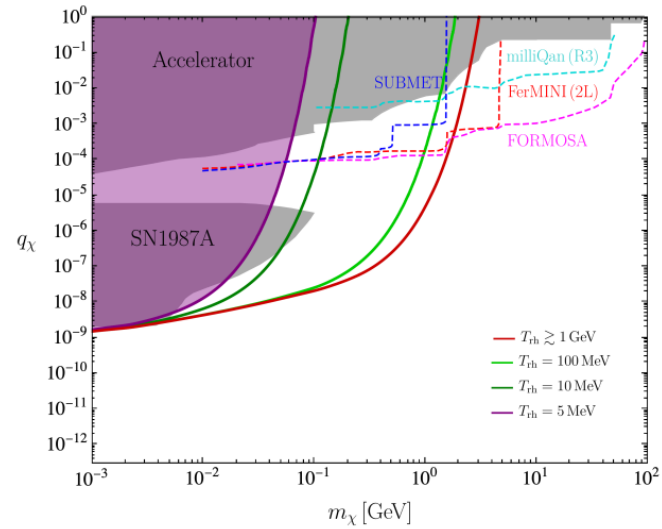
Future:  $\Delta N_{\text{eff}} \leq (0.06)_{\text{CMB-S4}}$

# Testing Reheat Temperatures in Both Cases

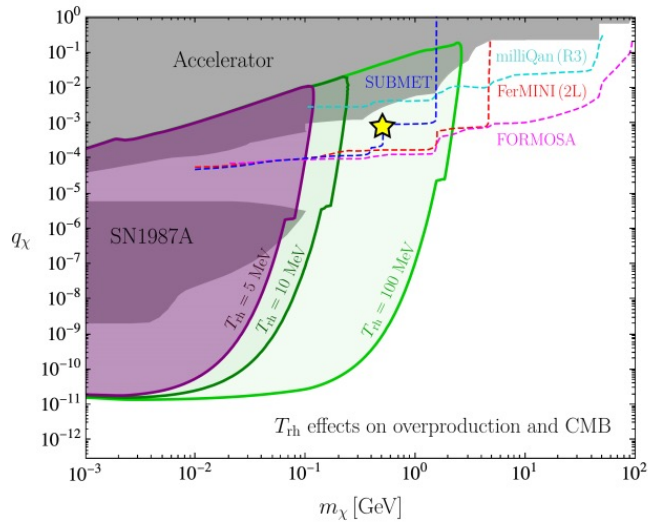
Overproduction Bounds for “Pure” mCP



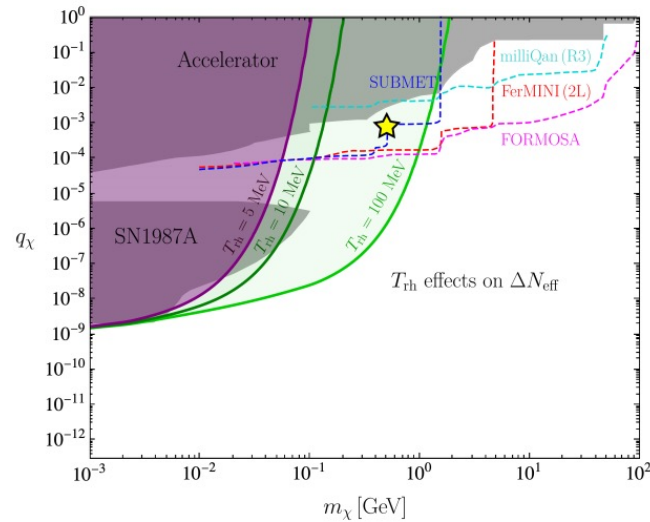
$\Delta N_{\text{eff}}$  Constraints for mCP with Dark Photon



Reheating Targets for “Pure” mCP

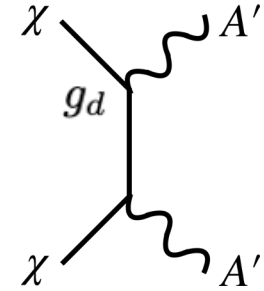


Reheating Targets for mCP with Dark Photon





# Another Key Objective: Differentiate Two Types of MCPs

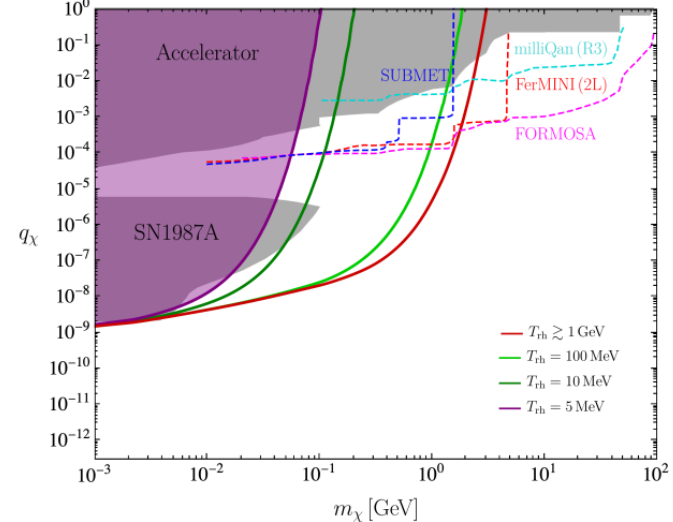
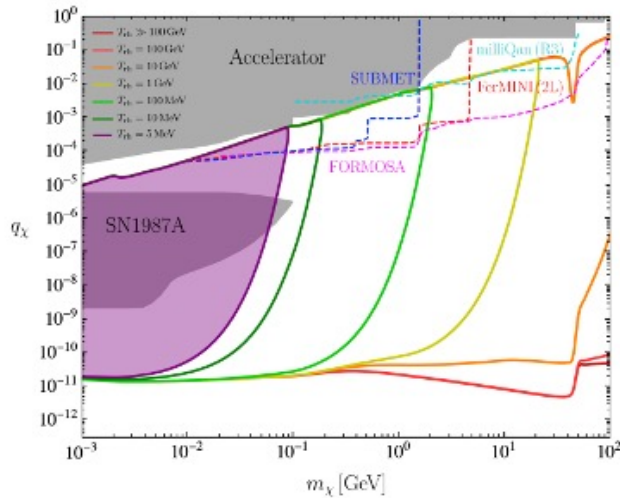


$$g_d = 0$$

Sizable  $g_d$

Overproduction Bounds for "Pure" mCP

$\Delta N_{\text{eff}}$  Constraints for mCP with Dark Photon



modifying  $g_d$   
 $\longleftrightarrow$   
 Interpolate between the two

Theoretically, there is a limit on how small  $g_d$  can be, for a given  $q_\chi$

# “Distinguishability” Conditions

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- Turning down thermalization between  $\chi - A'$ :  $g_d \lesssim (16\pi^2 m_\chi / \mathcal{F} m_{\text{pl}})^{1/4}$

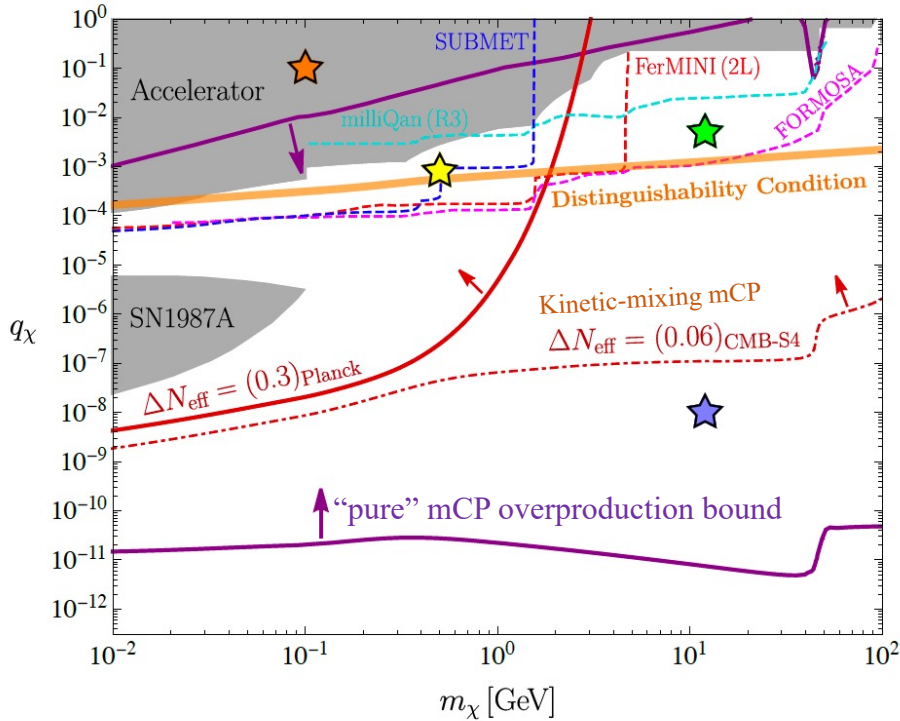
- **Requirement for kinetic mixing:**  $\epsilon < 1 \Rightarrow g_d > e q_\chi$ ,  $q_\chi = \frac{\epsilon g_d}{e}$   
Burgess *et al*, JCAP (2008)

- Considering these two inequalities for  $g_d$ , we can roughly determine that:

$$q_\chi \gtrsim \frac{1}{\alpha_{\text{em}}^{1/2}} \left( \frac{m_\chi}{\mathcal{F} m_{\text{pl}}} \right)^{1/4}$$

One CANNOT de-thermalize  $\chi - A'$  interaction rate to mimic “pure” mCP!

# Regions of Interests



- **Orange Star:** favoring “pure” mCP
- **Yellow Star:** testing reheat temperatures
- **Green Star:**
  - 1) testing reheat temperatures with CMB-S4
  - 2) currently favoring kinetic-mixing mCP
- **Purple Star:** favoring kinetic-mixing mCP (can be reached by direct-detection exps.)



## Frederick Reines

**Nobel Prize Laureate; Professor at UC Irvine**

**Utilized a nuclear reactor to study free neutrinos**

**We have an opportunity to explore the millicharge dark sector  
and unveil deep mysteries of the Universe**

# Thank you!