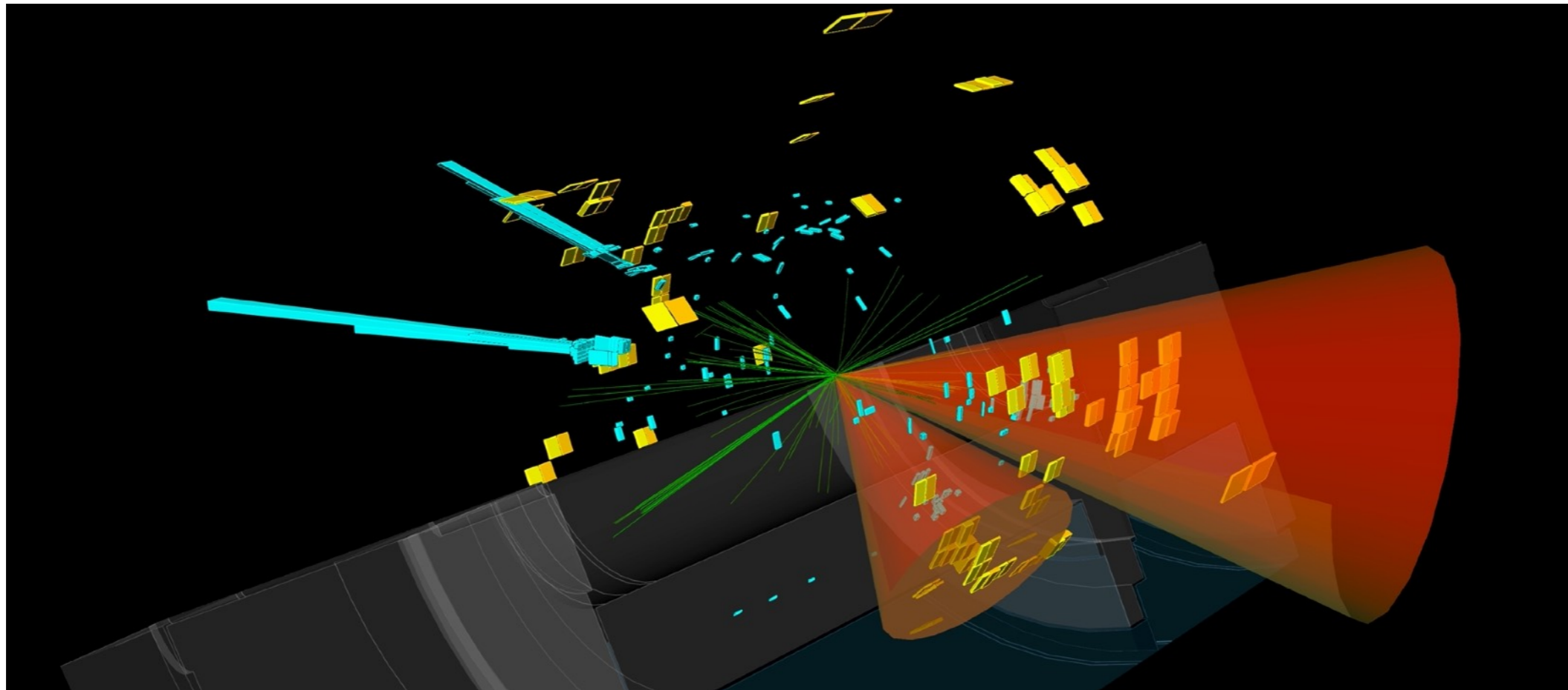


# IMPERIAL

## Interference effects in resonant di-Higgs production at the LHC



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# Overview

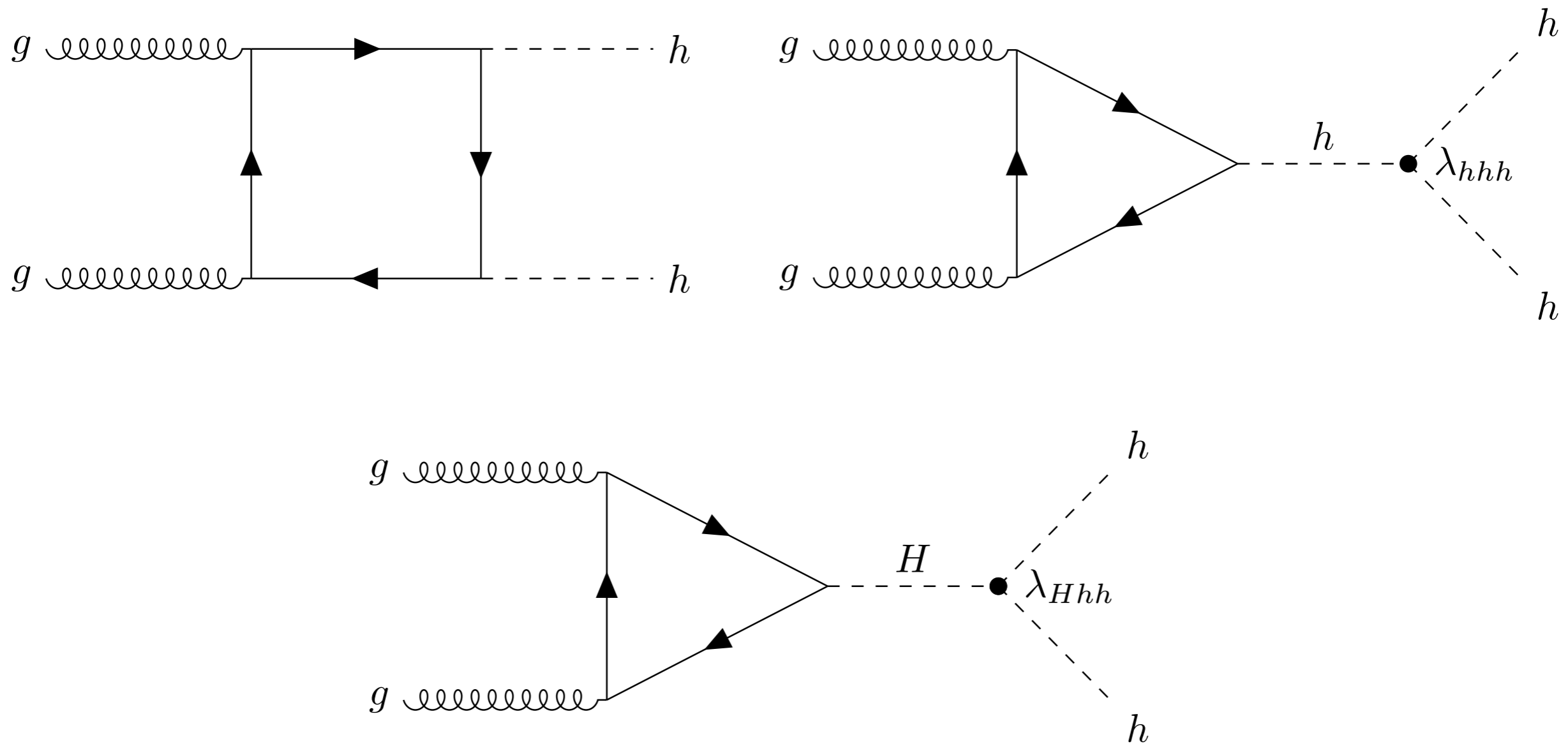
- The material shown today based on the paper “**Interference effects in resonant di-Higgs production at the LHC in the Higgs singlet extension**”, in collaboration with F. Feuerstake, E. Fuchs, and T. Robens
  - [arXiv:2409.06651](https://arxiv.org/abs/2409.06651)
- Latest bounds on Higgs singlet model
- Investigation of interference effects on HH mass spectrum and other variables such as Higgs  $p_T$
- New tool for modelling interference effects using matrix element (ME) reweighting
- Introducing several benchmark scenarios that exhibit interesting features (e.g large interference effects)

# The Higgs singlet model

- Simplest extension of the Standard model (SM) that can provide resonance-enhanced di-Higgs production = Higgs singlet model with softly broken  $\mathbb{Z}_2$  symmetry
- Potential:  $V(\Phi, S) = -m^2\Phi^\dagger\Phi - \mu^2S^2 + \lambda_1(\Phi^\dagger\Phi)^2 + \lambda_2S^4 + \lambda_3\Phi^\dagger\Phi S^2$
- 5 free parameters
  - 2 of them fixed by experiments:  $v$  and  $m_h=125$  GeV
  - 3 remaining parameters chosen as:  $m_H, \sin\alpha, \tan\beta = v/v_S$
  - $\alpha$  is mixing angle that rotates gauge into mass eigenstates, define  $m_H > m_h$
- SM-like  $h$  couplings to fermions and weak gauge bosons modified by  $\cos\alpha$
- Heavy Higgs  $H$  behaves like SM-Higgs with couplings to fermions and gauge bosons scaled by  $\sin\alpha$ , with additional decay channel (if  $m_H > 2m_h$ ):  $H \rightarrow hh$

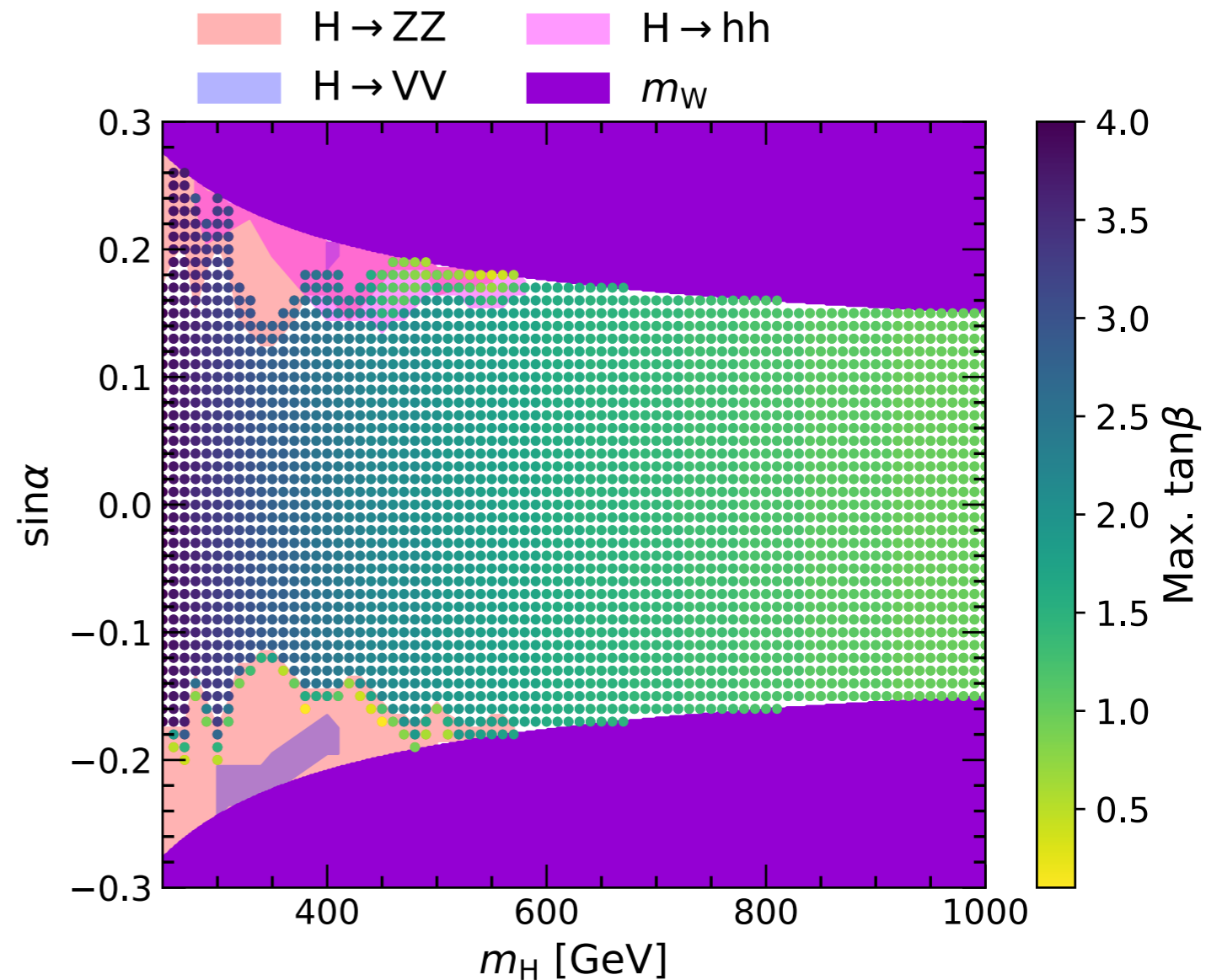
# di-Higgs production at the LHC

- Dominant diagrams contributing to di-Higgs spectrum
- Interference between diagrams as well!



# Allowed parameter space

- Investigate allowed regions
- Theory bounds: unitarity, EW precision data, perturbativity of the couplings, boundedness from below of the potential, local minimum of the potential
- At high  $m_H$ , points excluded by  $W$  mass measurement
- At low  $m_H$  point excluded by experimental searches: mainly  $H \rightarrow ZZ$  and  $H \rightarrow hh$



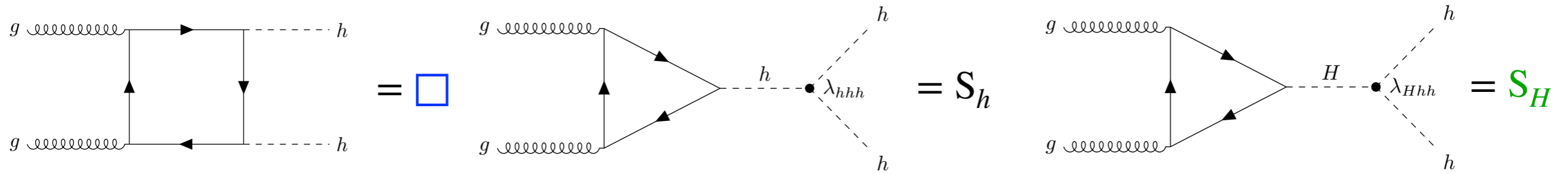
# ME reweighing method

- ME reweighing reweighs events using:

$$w = \frac{|\mathcal{M}_{\text{target}}|^2}{|\mathcal{M}_{\text{ref}}|^2}$$

- $\mathcal{M}_{\text{ref}}$  is ME for the MC you are reweighing and  $\mathcal{M}_{\text{target}}$  is the ME for the process/parameters you want to model
  - $\mathcal{M}_{\text{target}}$  in general model dependent, many options for process and parameters
  - In our method we decompose  $\mathcal{M}_{\text{target}}$  into minimal set of contributions that can scaled and combined to obtain distributions in any model
- Matrix elements computed using MadGraph with TRSM ([A Papaefstathiou, T Robens and G Tetlalmatzi-Xolocotzi JHEP05\(2021\)193](#))

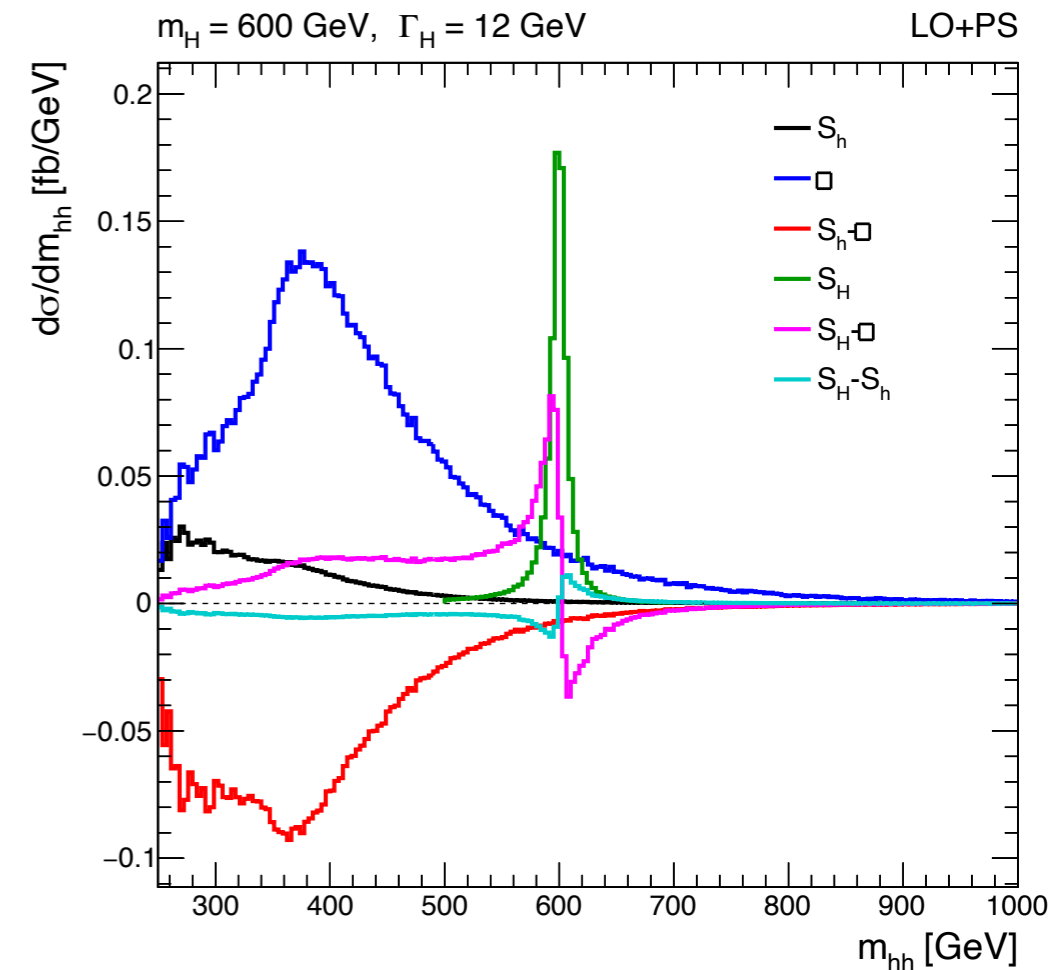
# Decomposing the ME



Parameterise using:  $\lambda_{hhh}, \lambda_{Hhh}, y_q^h, y_q^H, \Gamma_H, m_H$  ( $\kappa_p = p/p_{SM}$ )

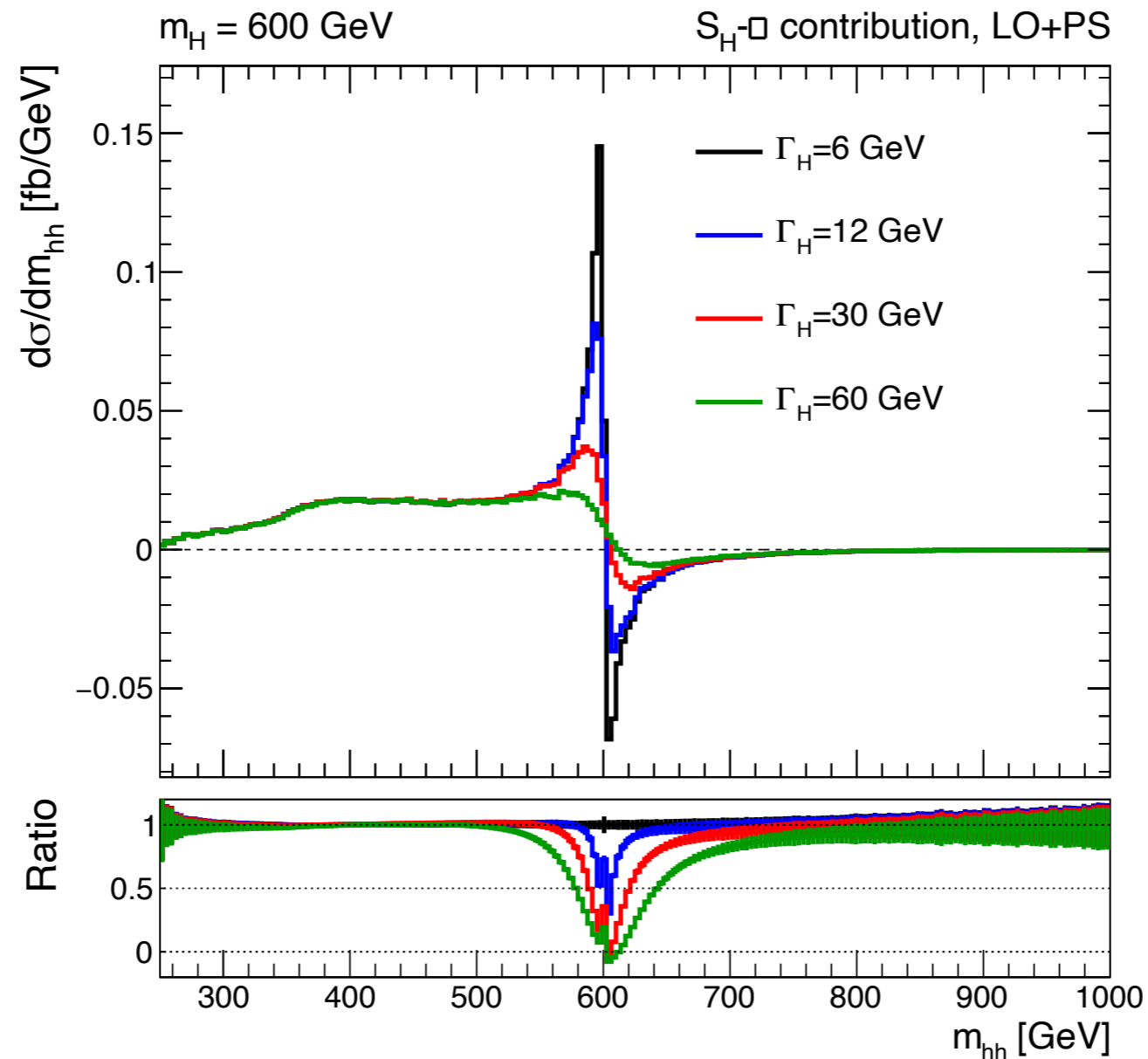
$$\begin{aligned}
 |\mathcal{M}_{\text{total}}|^2 &= \mathcal{M}_{\square}^2 \cdot (\kappa_q^h)^4 \\
 &+ \mathcal{M}_{S_h}^2 \cdot (\kappa_q^h)^2 \kappa_{\lambda_{hhh}}^2 \\
 &+ \mathcal{M}_{S_H}^2(m_H, \Gamma_H) \cdot (\kappa_q^H)^2 \kappa_{\lambda_{Hhh}}^2 \\
 &+ \widetilde{\mathcal{M}}_{S_h-\square}^2 \cdot (\kappa_q^h)^3 \kappa_{\lambda_{hhh}} \\
 &+ \widetilde{\mathcal{M}}_{S_H-\square}^2(m_H, \Gamma_H) \cdot (\kappa_q^h)^2 \kappa_q^H \kappa_{\lambda_{Hhh}} \\
 &+ \widetilde{\mathcal{M}}_{S_H-S_h}^2(m_H, \Gamma_H) \cdot \kappa_q^h \kappa_q^H \kappa_{\lambda_{hhh}} \kappa_{\lambda_{Hhh}},
 \end{aligned}$$

**Interference terms!**



# Dependence on the width

- $S_H$ ,  $\square - S_H$ , and  $S_H - S_h$  depend on the mass and the width of the H

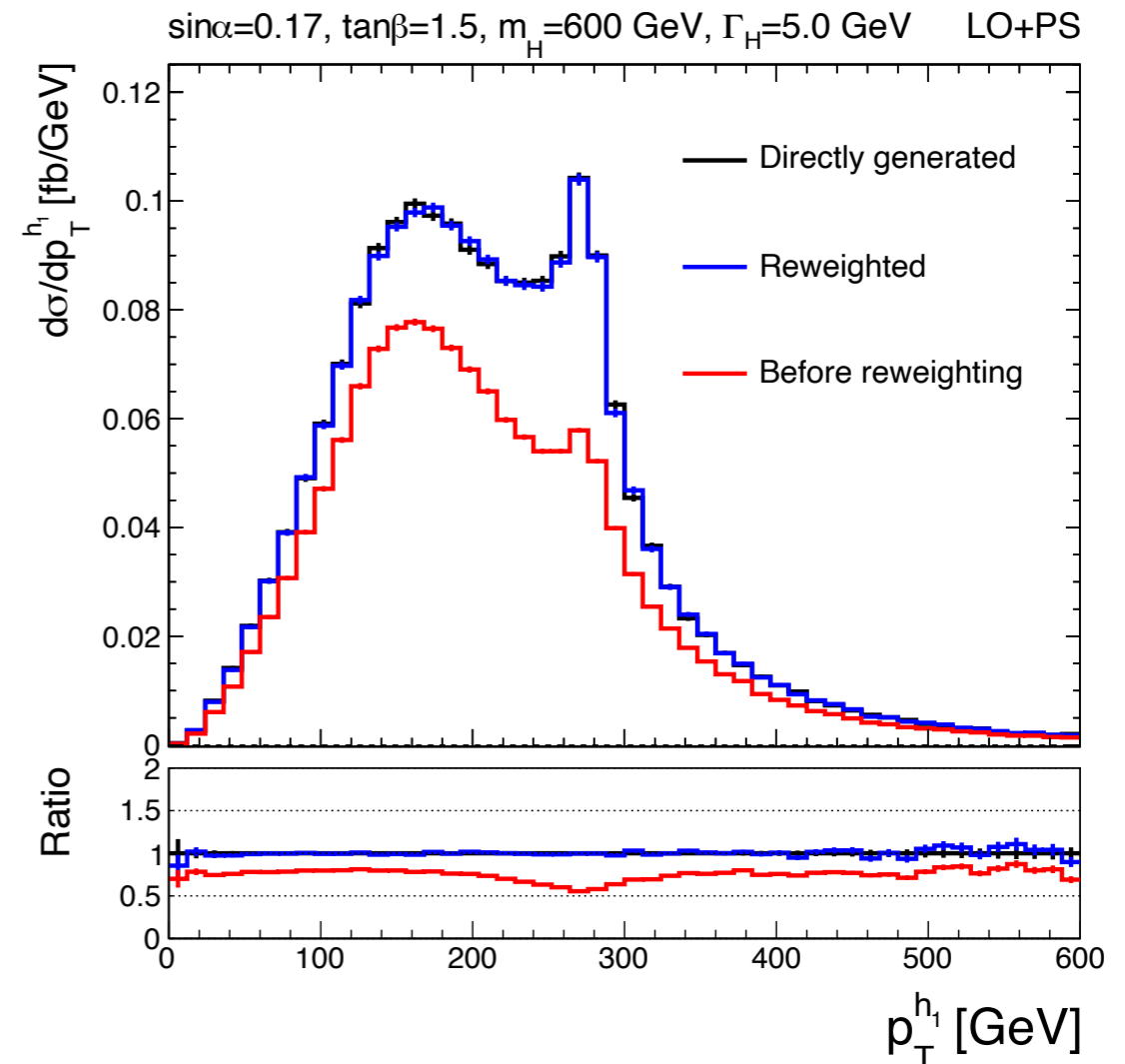
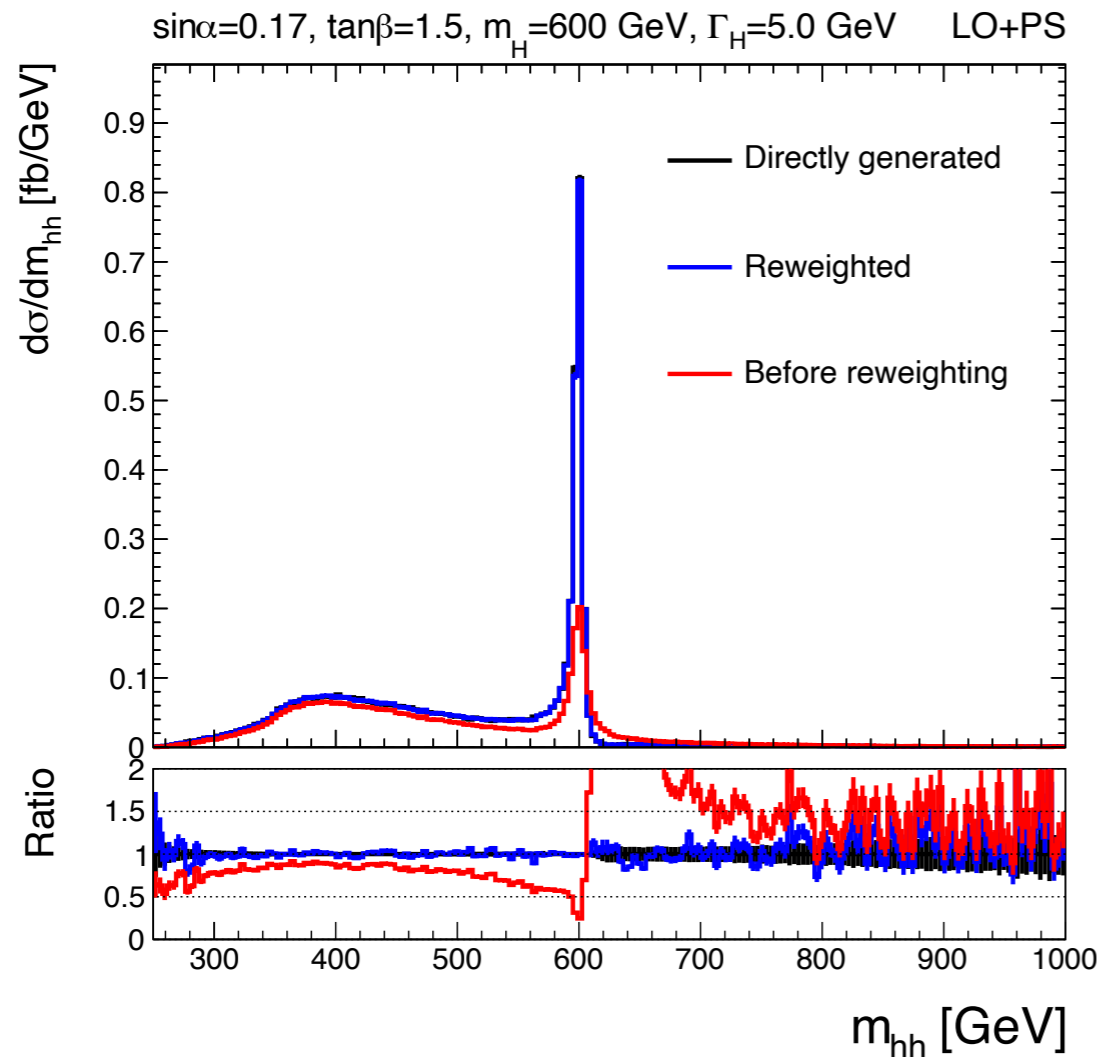




- With ME reweighting you need to make sure your chosen reference sample is populated in all phase-space regions where  $\mathcal{M}_{\text{target}}$  is non-vanishing
- For the  $\square$ ,  $S_h$ ,  $\square - S_h$ ,  $\square - S_H$ , and  $S_H - S_h$  contributions we use a SM di-Higgs sample (non-resonant only)
- For  $S_H$  we use a MC samples of the same  $m_H$  and a width not too far from the target ( $\sim 0.5\text{--}2 \times \text{target } \Gamma_H$ )
- All LO MC sample generated using Madgraph with TRSM

# Validating the reweighting method

- Applying reweighting to LO MC samples give ~perfect agreement with samples generated for a set of model points!



# Including higher-order corrections

- For gluon fusion LO know to under predict cross-section (XS) by ~200-300%
- We can correct for this using K-factors
- K-factors for SM-like terms derived using NNLO XSs from LHCHWG4 ([link](#))
- K-factors for  $S_H$  derived using (NNLO+NNLL) XSs for undecayed H production from LHCHWG ([here](#))
- For interference terms use ansatz:  $K_{i-j} = \sqrt{K_i K_j}$

# Benchmarks

- Several new benchmarks defined that exhibit interesting features

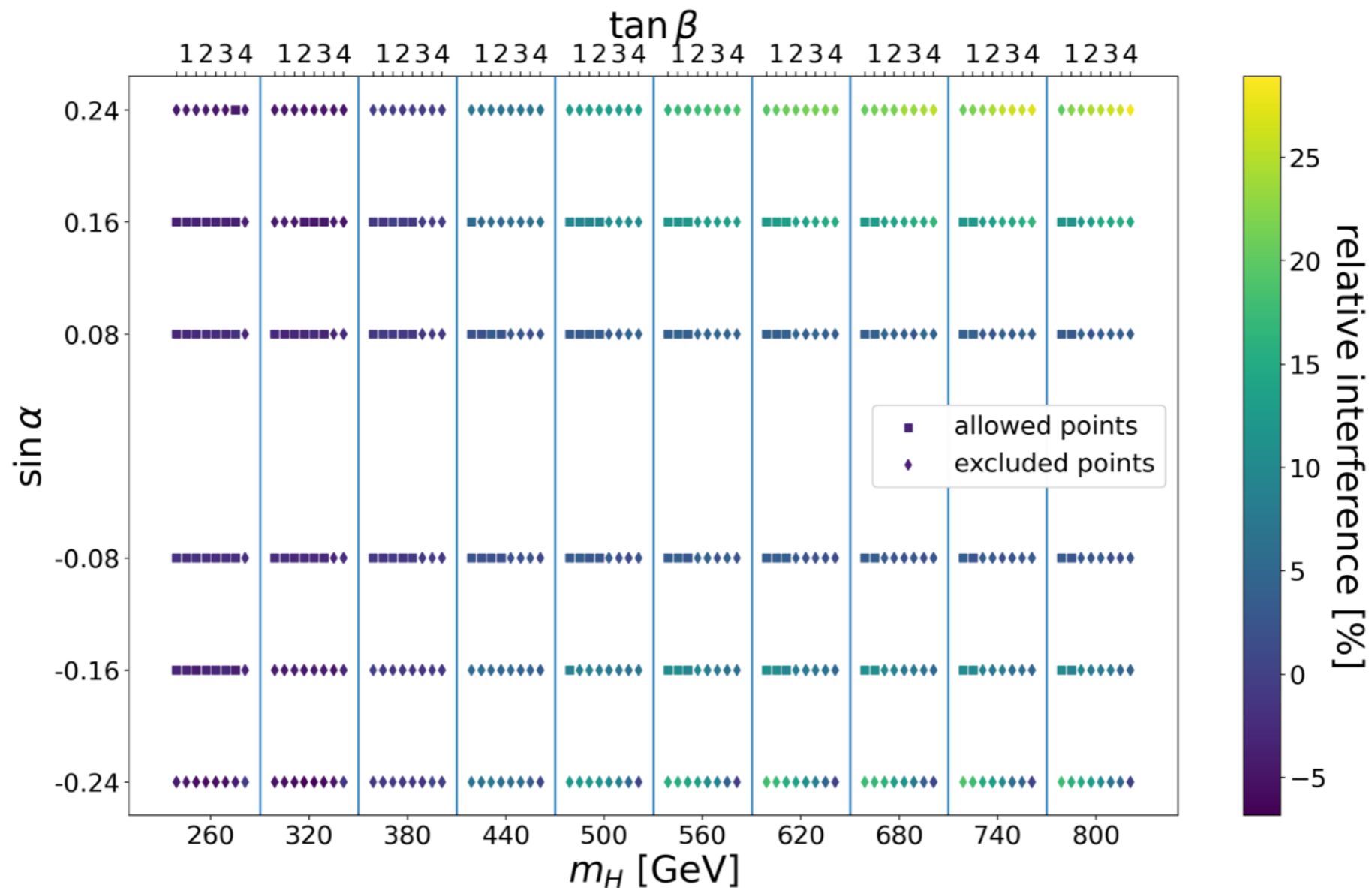
Benchmark	$\sin \alpha$	$\tan \beta$	$m_H$ [GeV]	$\Gamma_H$ [GeV]	$\kappa_{\lambda_{hhh}}$	$\sigma$ [fb]	$\sigma_{SH}$ [fb]	Accessible in Run-3	Feature
BM1	0.16	1.0	620	4.6	0.96	50.5	13.5	✓	Max $(\Delta\sigma)_{\text{rel}}$
BM2	0.16	0.5	440	1.5	0.96	91.6	56.4	✓	Max $(\Delta\sigma)_{\text{rel}}^{\Sigma}$
BM3	0.16	0.5	380	0.8	0.96	119.8	90.1	✓	Max $(\Delta\sigma)_{\text{rel}}^{\Sigma}$ with $(\Delta\sigma)_{\text{rel}} < 1\%$
BM4	-0.16	0.5	560	3.0	0.96	51.4	15.5	✓	Max non-res. within $m_H \pm 10\%$
BM5	0.08	0.5	500	0.6	0.99	40.6	8.1		Max non-res. within $m_H \pm 10\%$
BM6	0.16	1.0	680	6.1	0.96	44.8	8.4	✓	Max $m_H$
BM7	0.15	1.1	870	9.5	0.96	36.8	2.3		Max $m_H$
BM8	0.24	3.5	260	0.6	0.87	374.2	357.3	✓	Max $ \kappa_{\lambda_{hhh}} - 1 $
BM9	0.16	1.0	800	9.8	0.96	38.9	3.6		Max $\frac{\Gamma_H}{m_H}$

Today I will  
show this one

$$(\Delta\sigma)_{\text{rel}} = \frac{\sigma_{\text{total}} - \sigma_{\text{res}} - \sigma_{\text{non-res}}}{\sigma_{\text{total}}}$$

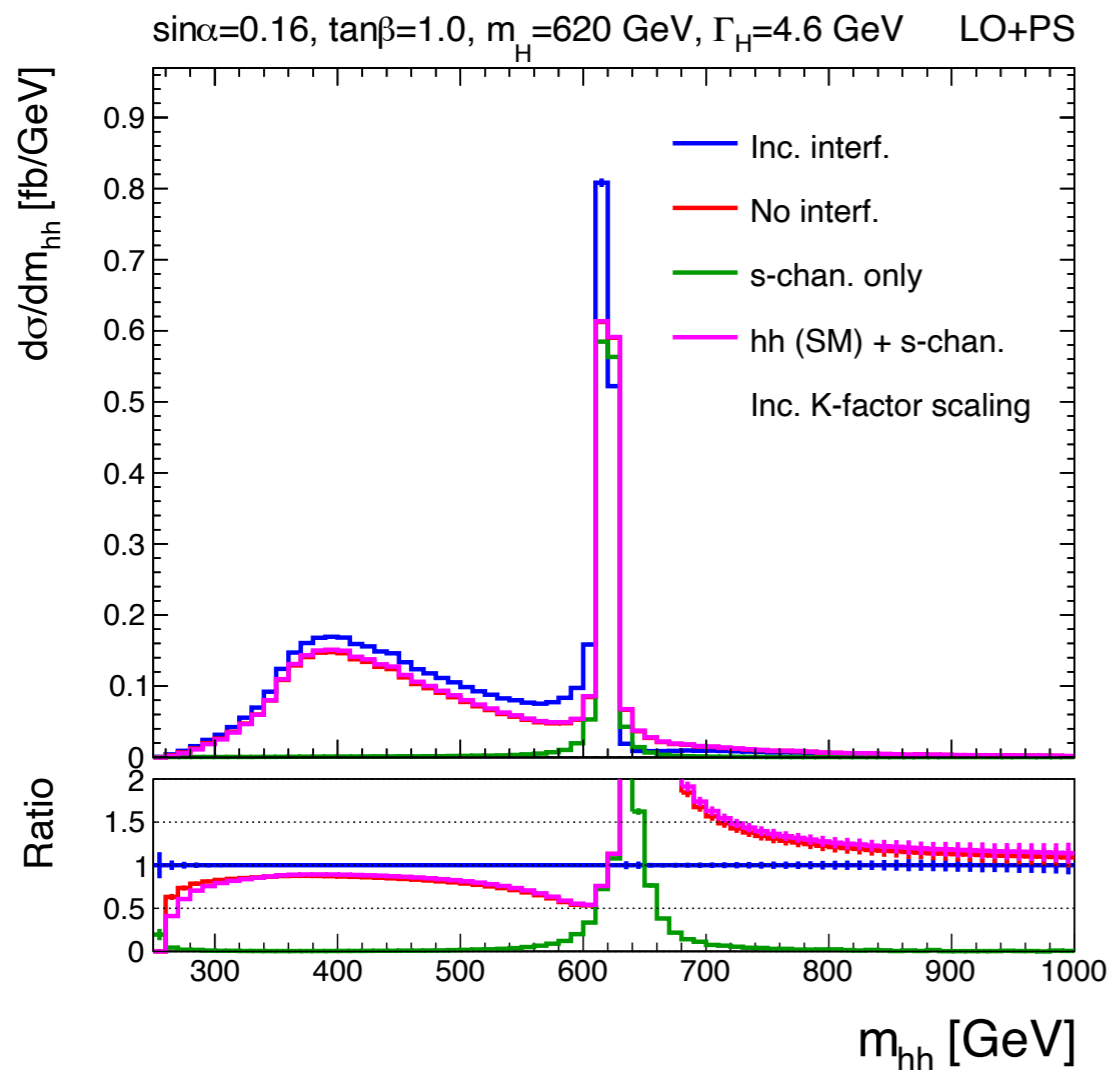
# Parameter scans

- We perform scans to determine regions where the interference effect in the total cross-section is large
- Squares = allowed points, diamonds are excluded

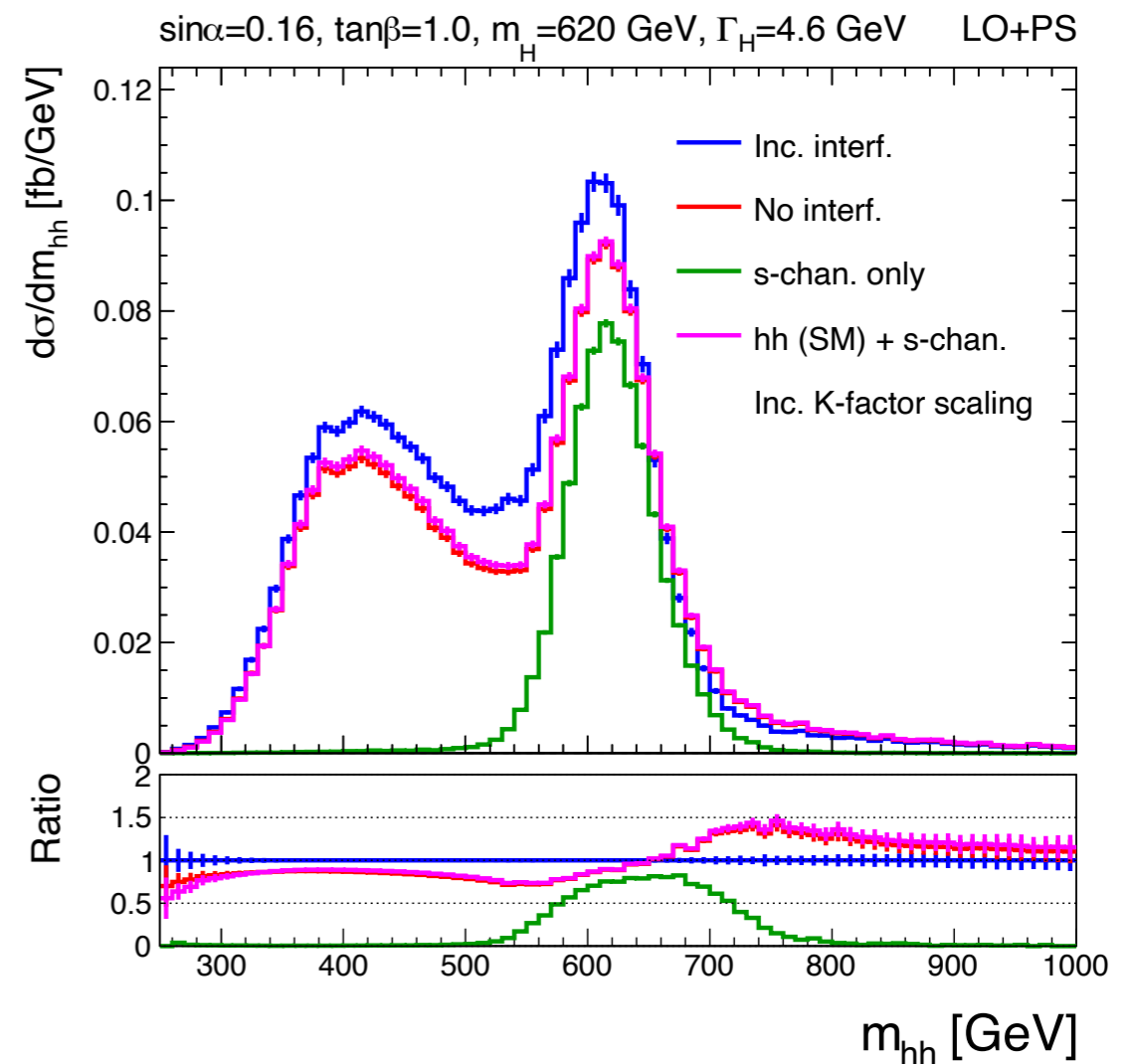


# Benchmark distributions (BM1)

- di-Higgs mass distributions
- We show different assumptions for the modelling
  - Blue = full, correct description, Green = resonant-only (most CMS and ATLAS results so far), magenta = SM non-resonant + resonant with no interference (few analyses do this already)



**Before smearing**



**HH → 4b-like smearing**

# Conclusions

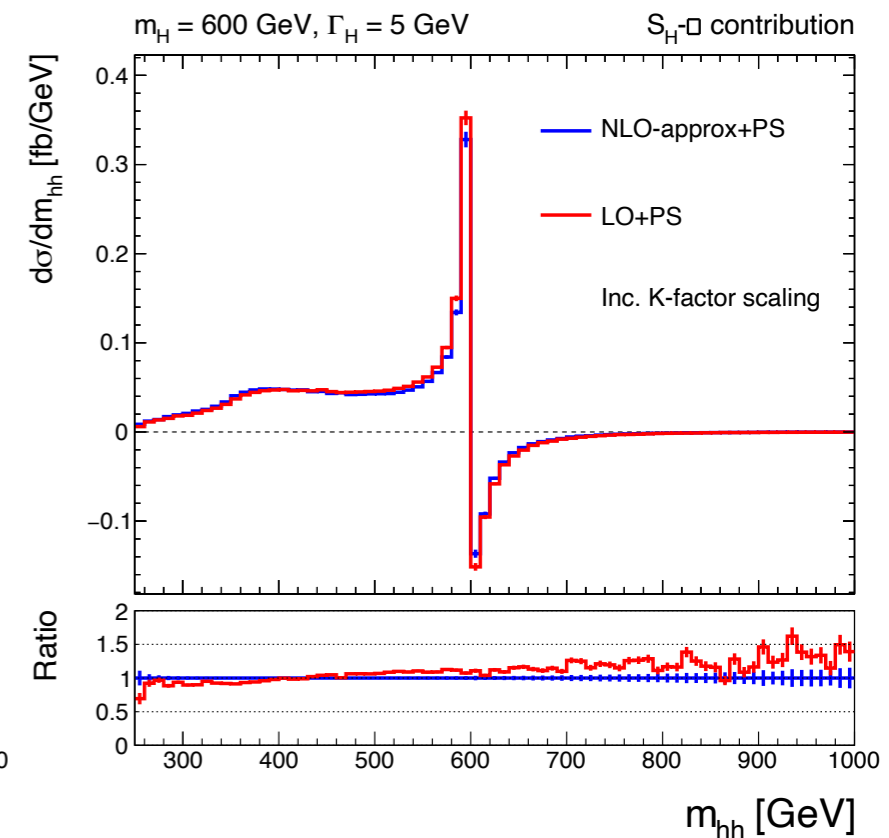
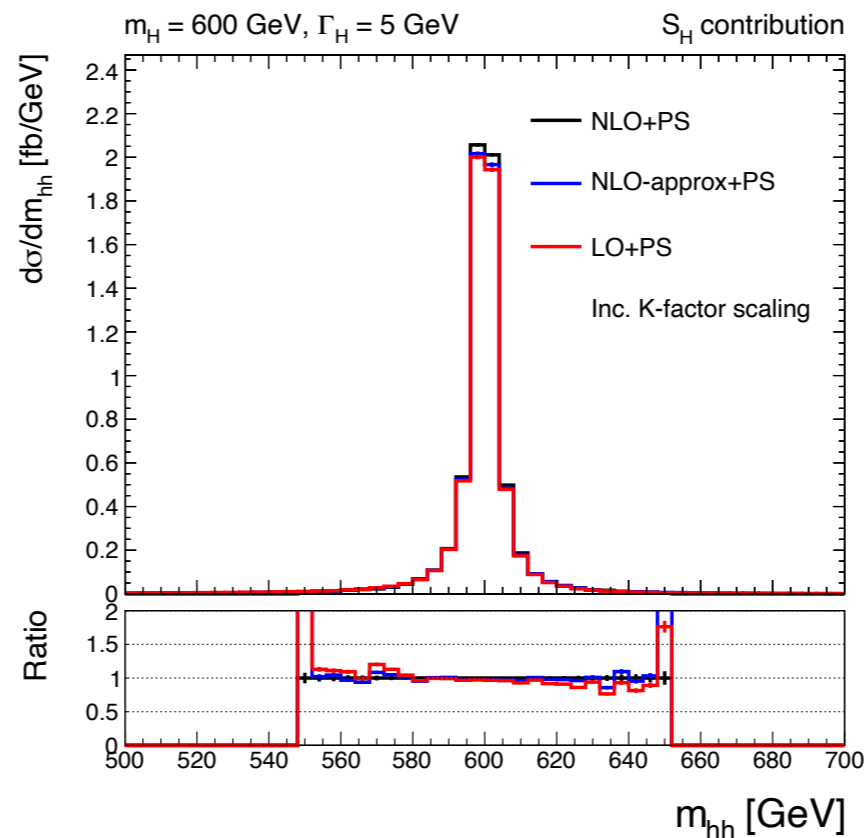
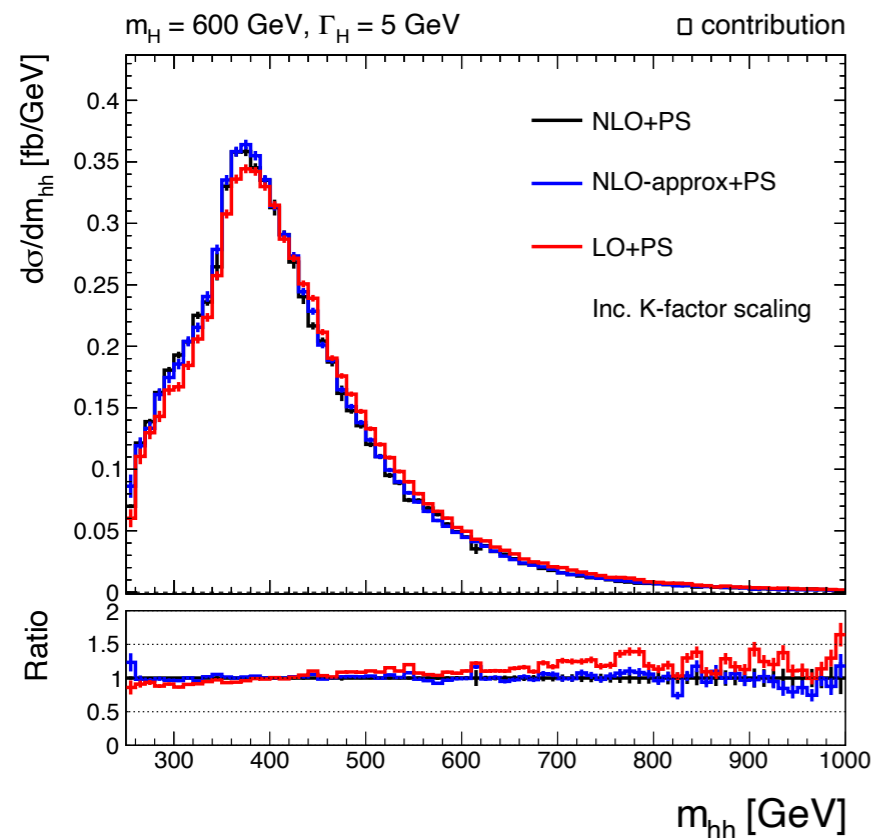
- Showed latest bounds on Higgs singlet model and investigated interference effects on cross-sections and distributions
- Interference effects are important for resonant di-Higgs searches
- Even without interference, the non-resonant contribution to the spectrum is sizeable and should be accounted for
- Martix element reweight tool developed to provide a convenient method for handling interference effects
  - Available on Gitlab: <https://gitlab.com/danielwinterbottom/HHReweigher>
- More details are provided in the publication: [arXiv:2409.06651](https://arxiv.org/abs/2409.06651)

# Backup



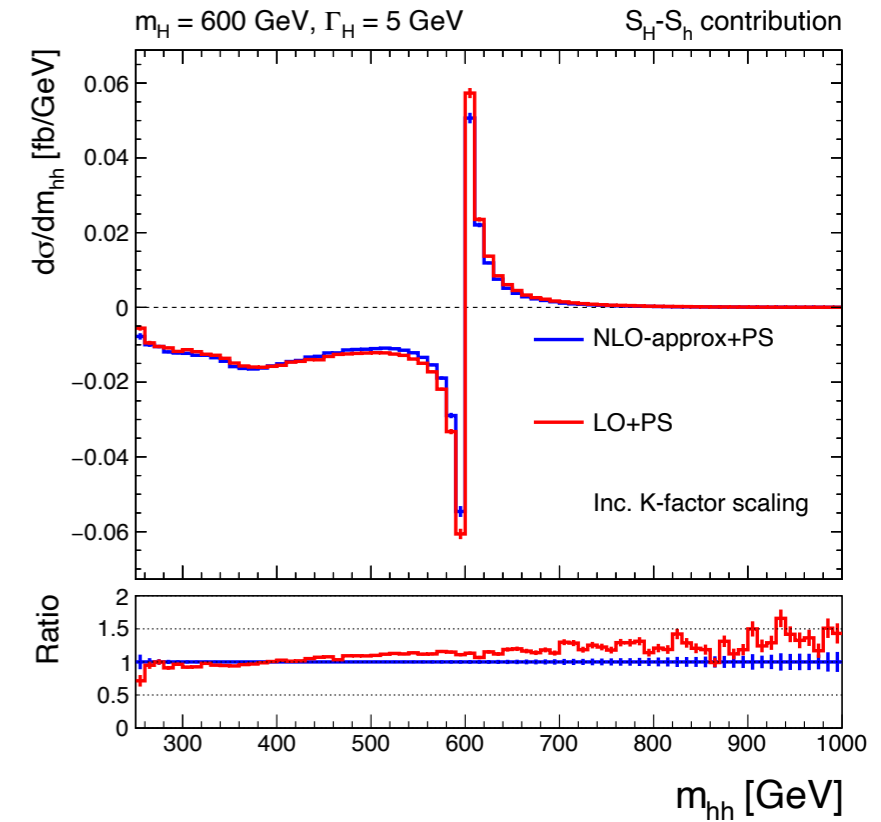
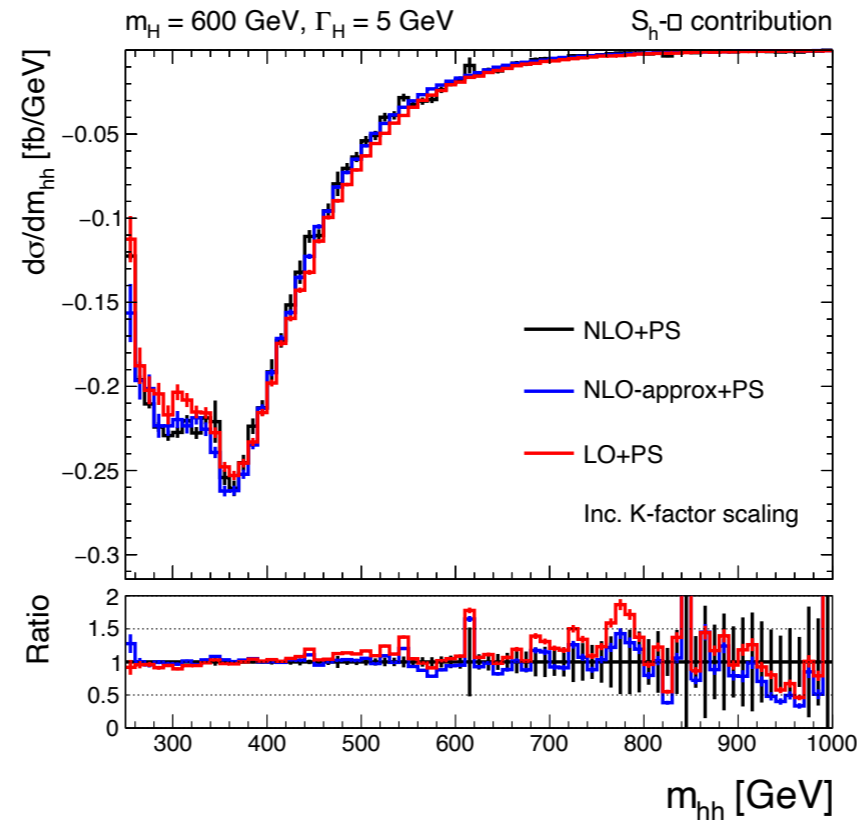
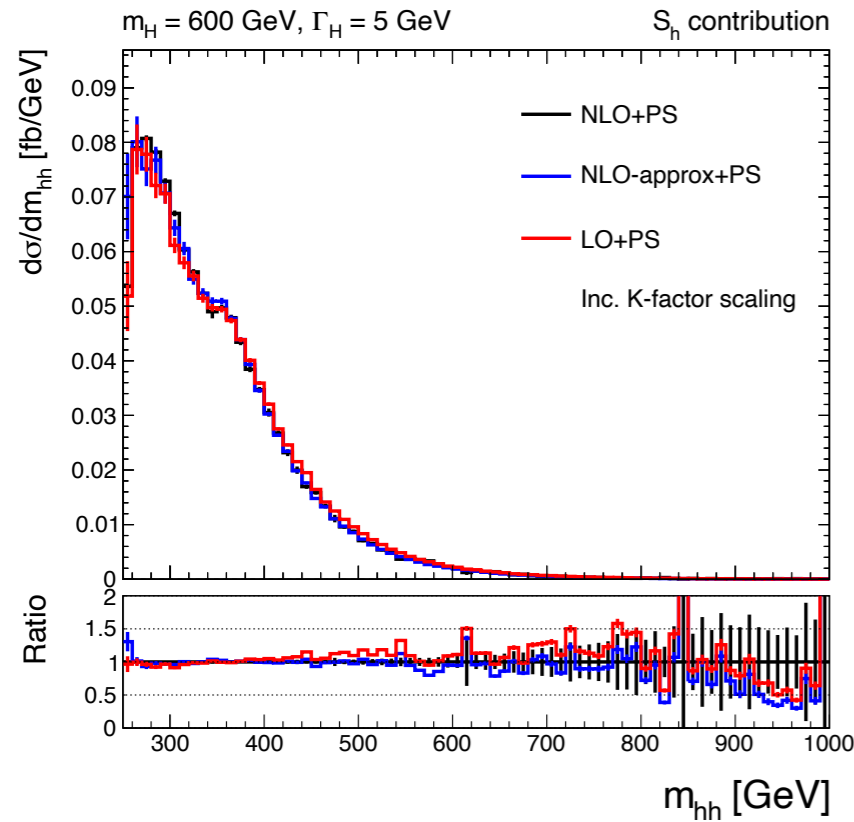
# Including higher order corrections

- Define approximate-method for reweighting NLO samples
  - Ignore additional radiation and compute MEs at LO
- NLO samples generated using POWHEG
  - No model currently available that can generate nonresonant+resonant di-Higgs with interference
  - We generate  $\square$ ,  $S_h$ ,  $\square - S_h$  for non-resonant, and  $S_H$  resonant samples and compare to reweighting where possible
  - We can also use reweighting to obtain approximate  $\square - S_H$ , and  $S_H - S_h$  predictions - agree well with LO, to be checked once proper NLO MC is available



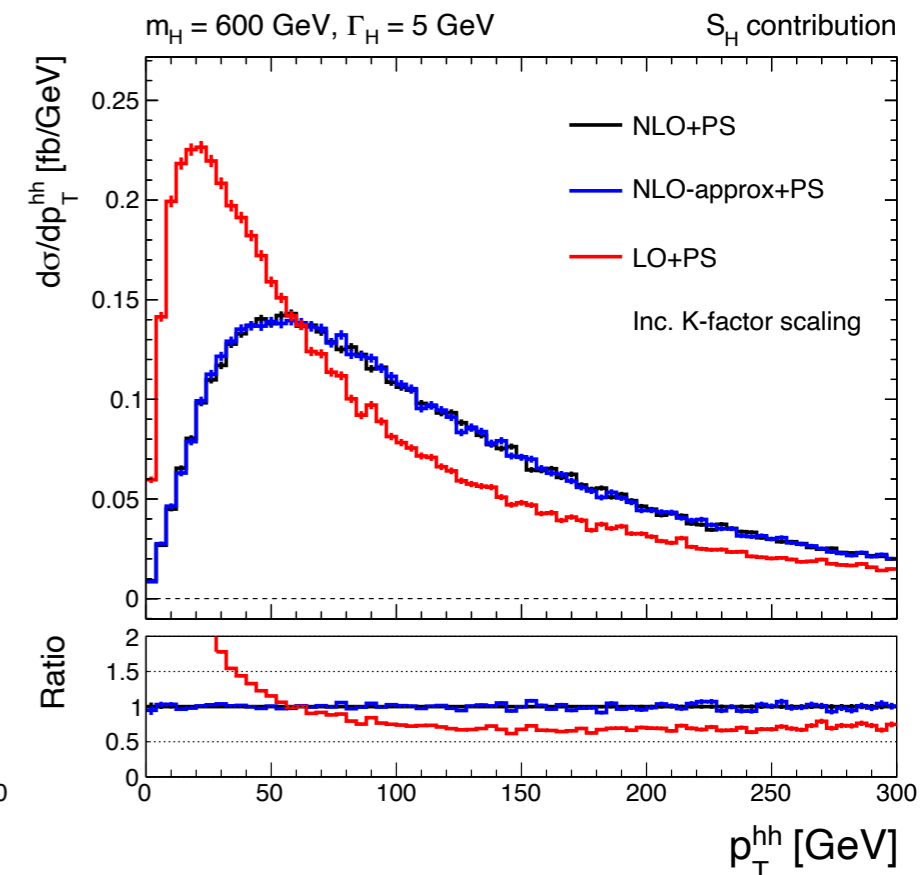
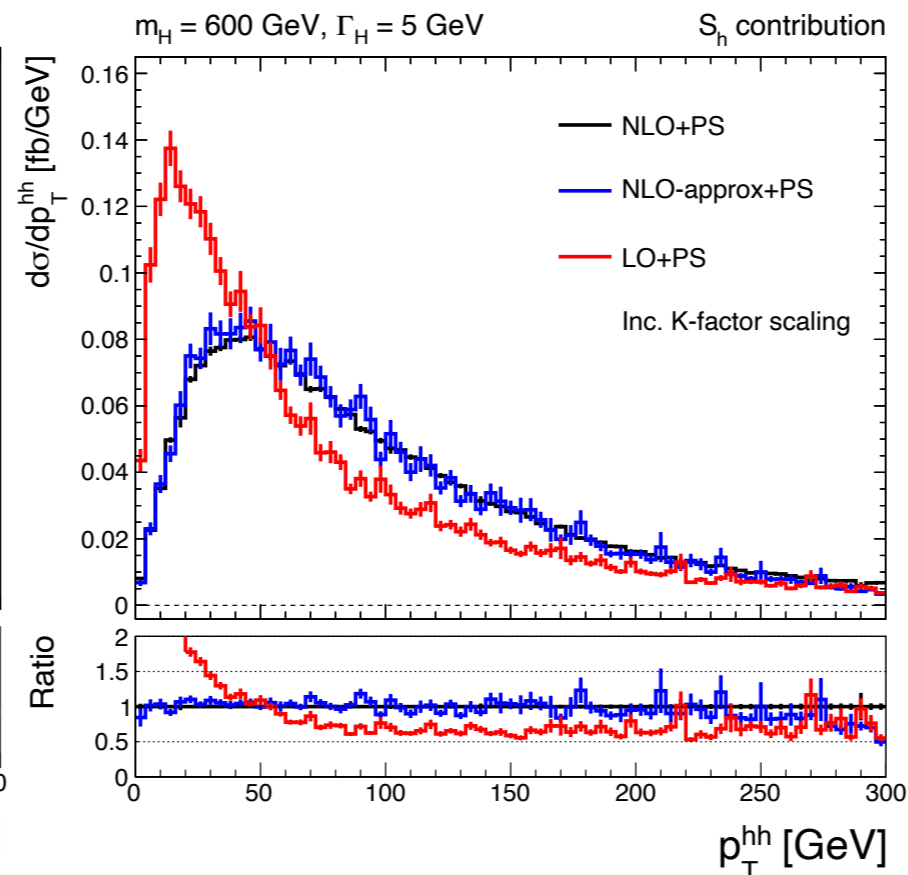
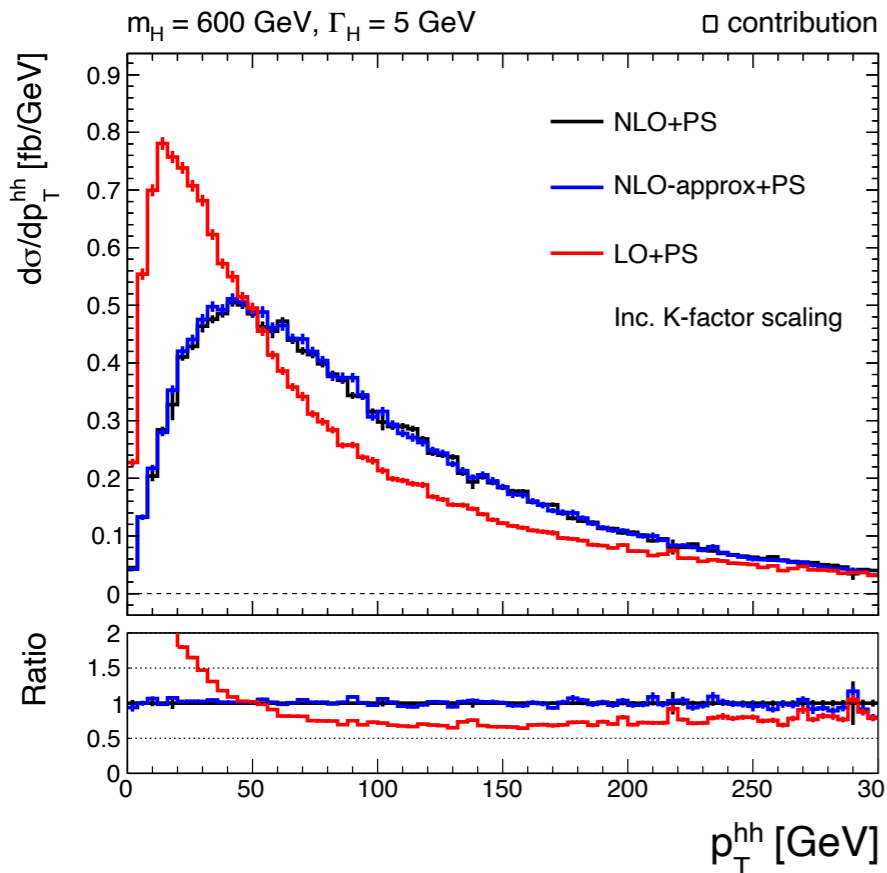
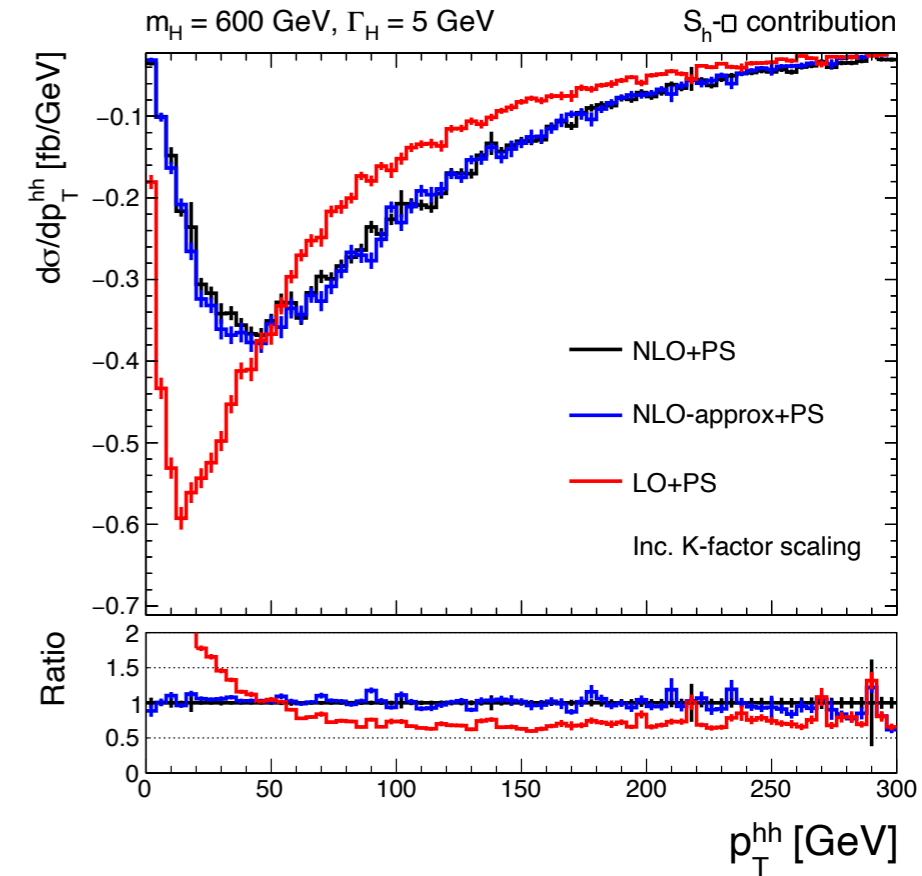
# Additional plots of NLO validations

- Plots of di-Higgs mass for other terms



# Additional plots of NLO validations

- Plots of di-Higgs  $p_T$



# More details on approximate NLO reweighting

When reweighting NLO samples we “ignore” the additional radiation if there is any as follows:

- We take the two outgoing  $h$  four-momenta from the ME and boost to the di-Higgs rest frame
- We then obtain the four-momenta for the incoming gluons by requiring both gluons to have zero transverse momentum, and equal and opposite longitudinal momentum, also requiring four-momentum conservation between incoming and outgoing particles
- When estimating the MEs we also average over all possible spin-states of the incoming gluons
- If there is no radiation, then we compute ME in the usual way as if the event is from a LO generator

- Coupling modifiers (wrt SM couplings) in the singlet model

$$\kappa_{f/V}^h = \cos \alpha,$$

$$\kappa_{f/V}^H = \sin \alpha,$$

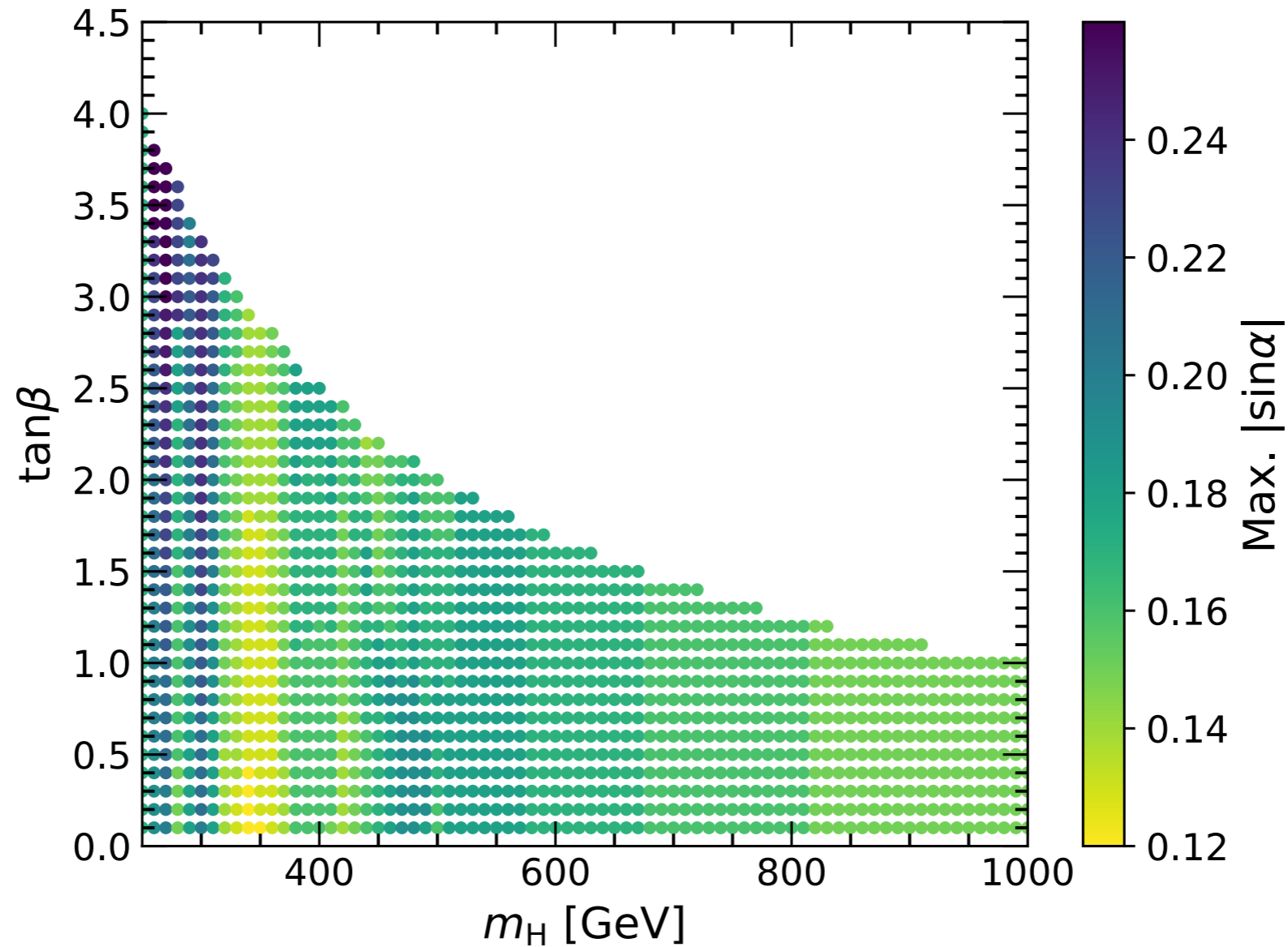
$$\kappa_{\lambda_{hhh}} = \cos^3 \alpha - \tan \beta \sin^3 \alpha,$$

$$\kappa_{\lambda_{Hhh}} = \frac{2m_h^2 + m_H^2}{m_h^2} \frac{\sin(2\alpha)}{2} (\cos \alpha + \tan \beta \sin \alpha),$$

$$\Gamma_H = \sin^2 \alpha \Gamma_{\text{SM}}(m_H) + \frac{\kappa_{\lambda_{Hhh}}^2 \sqrt{1 - 4m_h^2/m_H^2}}{8\pi m_H}$$

# Allowed points

- Allowed points in  $\tan\beta$ - $m_H$  plane

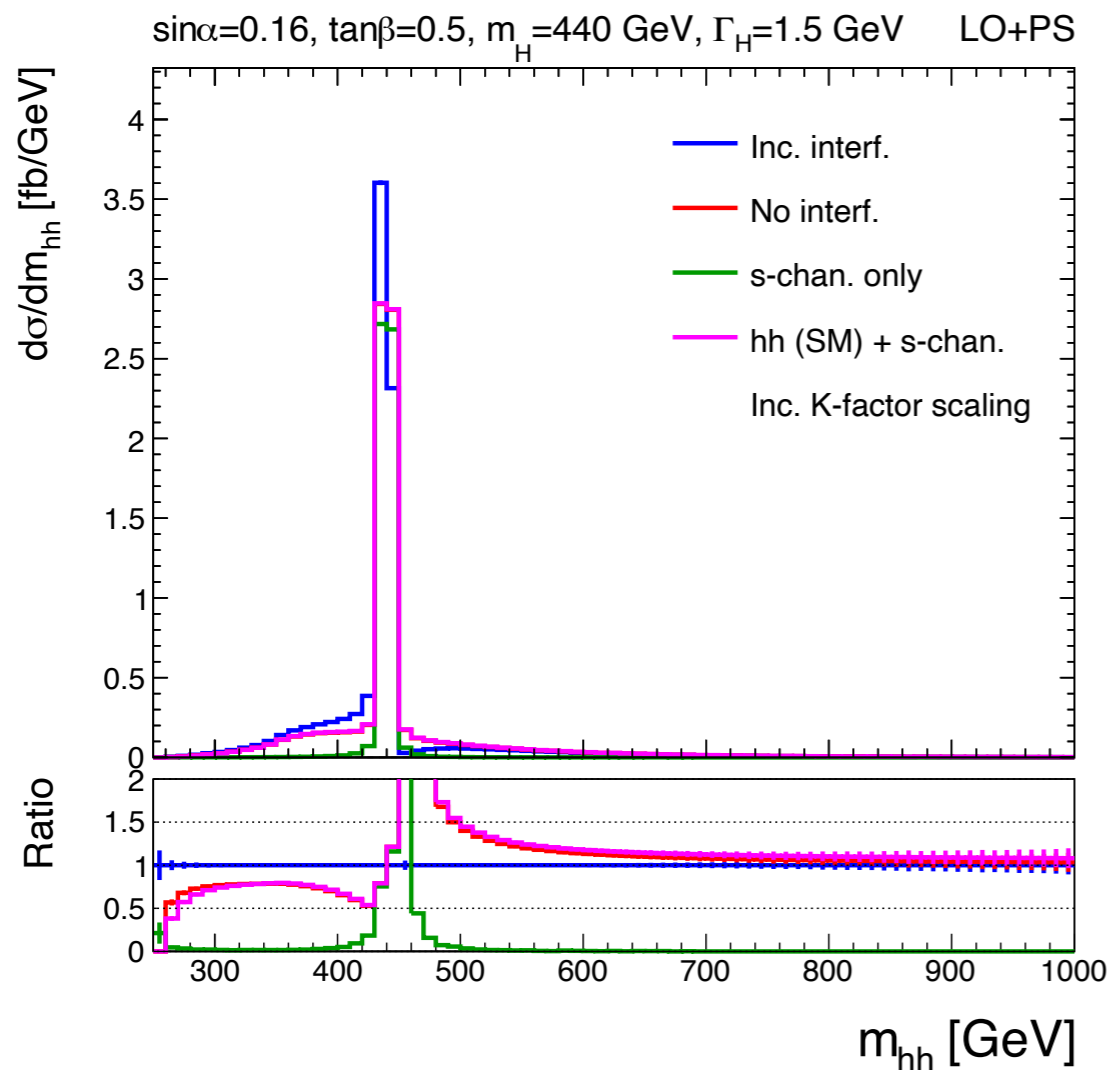


# Smearing

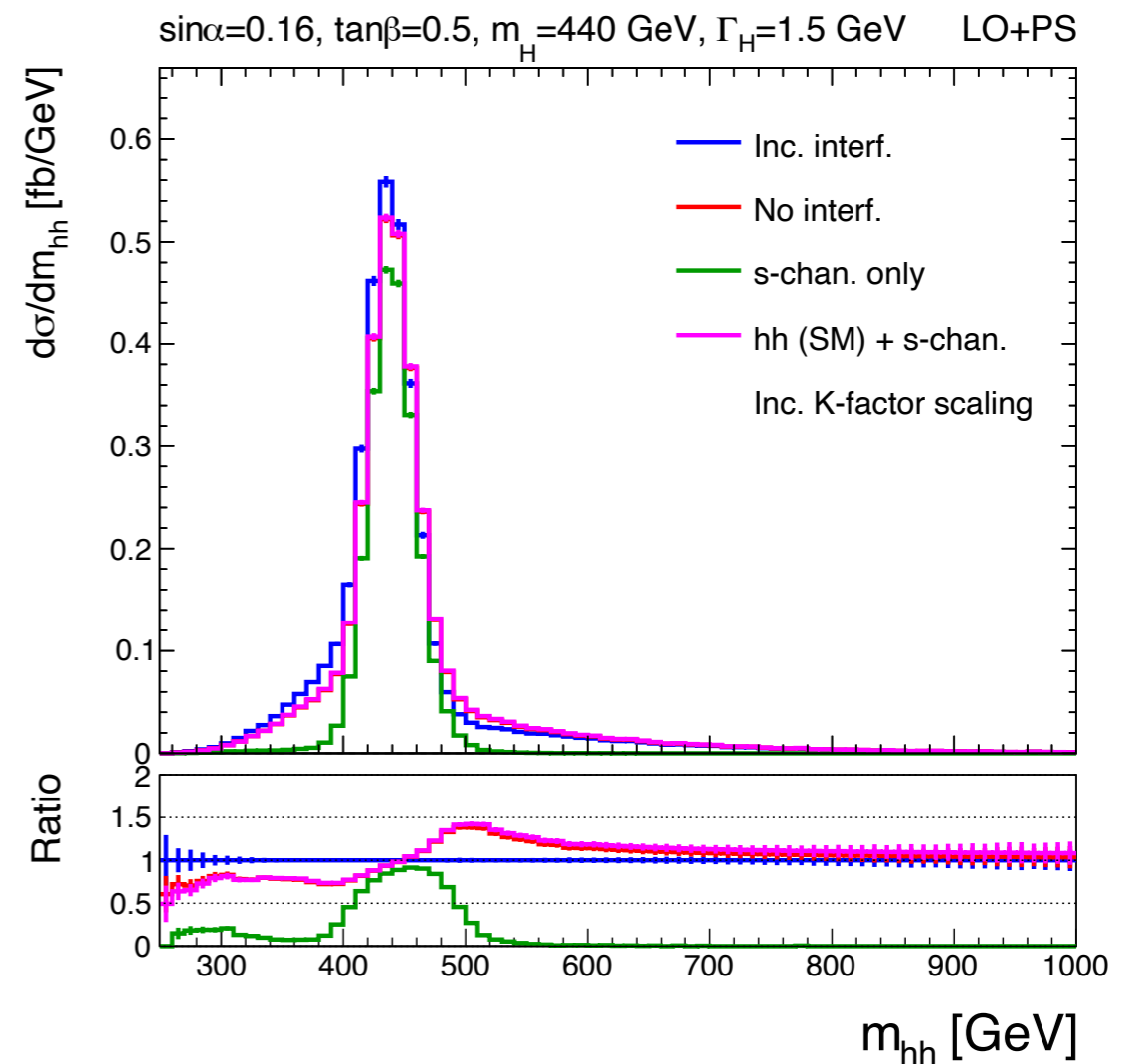
- Assume  $HH \rightarrow 4b$  like smearing by the CMS detector
- Angular smearing: smear  $\phi$  and  $\eta$  by randomly sampling a Gaussian with mean=0 and  $\sigma=0.05$
- Energy: smear energies by randomly sampling a Gaussian with mean=0 and  $\sigma=0.15$  - this is to match the Higgs mass resolutions quoted in [arXiv:1912.06046](https://arxiv.org/abs/1912.06046)
- Additional cuts to match CMS Run-3 trigger requirements: b-jet  $p_T > 30$  GeV, b-jet  $|\eta| < 2.5$ , and  $H_T > 280$  GeV (<https://cds.cern.ch/record/2868787>)

# Benchmark distributions (BM2)

- di-Higgs mass distributions
- We show different assumptions for the modelling
  - Blue = full, correct description, Green = resonant-only (most CMS and ATLAS results so far), magenta = SM non-resonant + resonant with no interference (few analyses do this already)



**Before smearing**

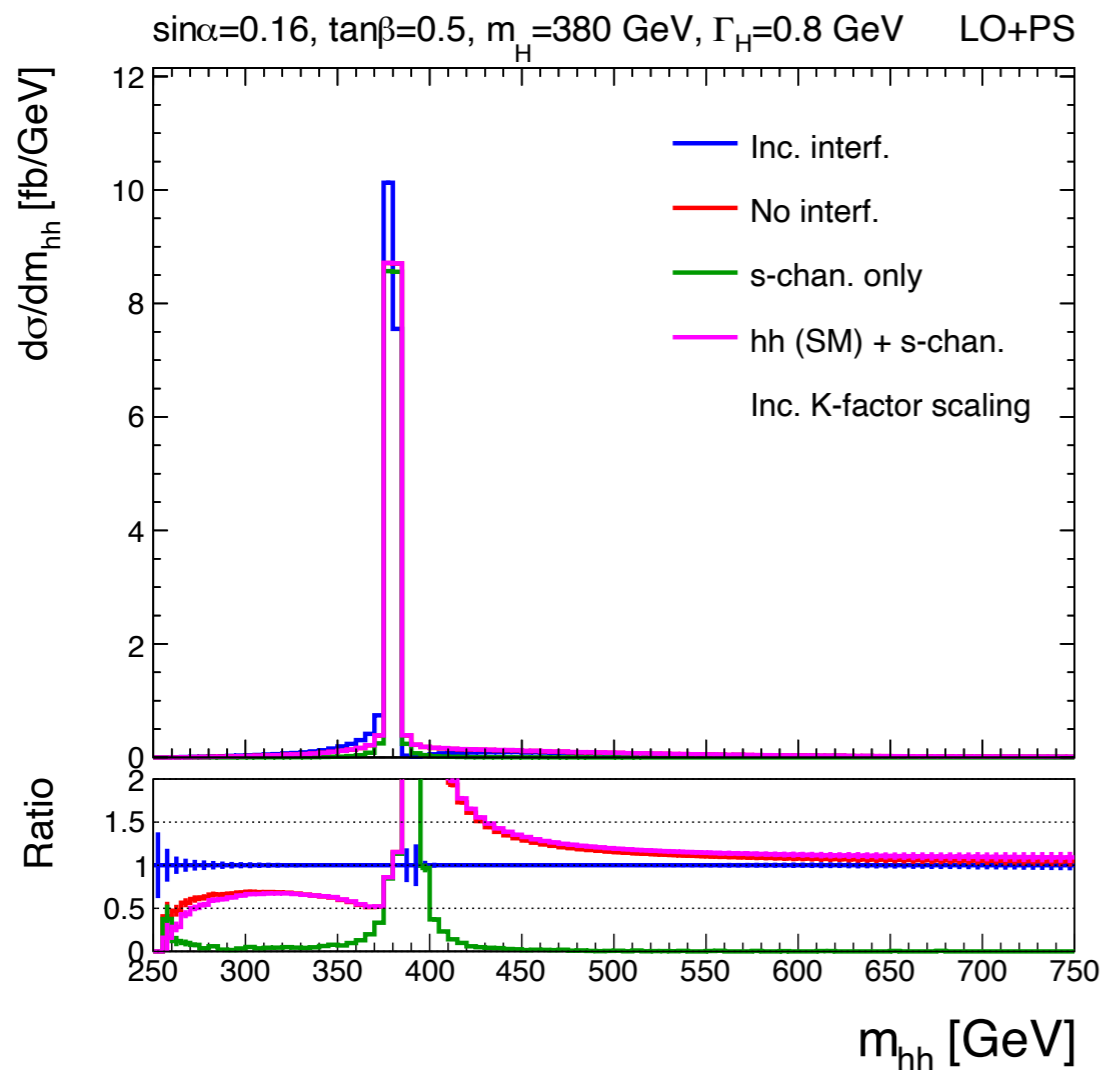


**HH → 4b-like smearing**

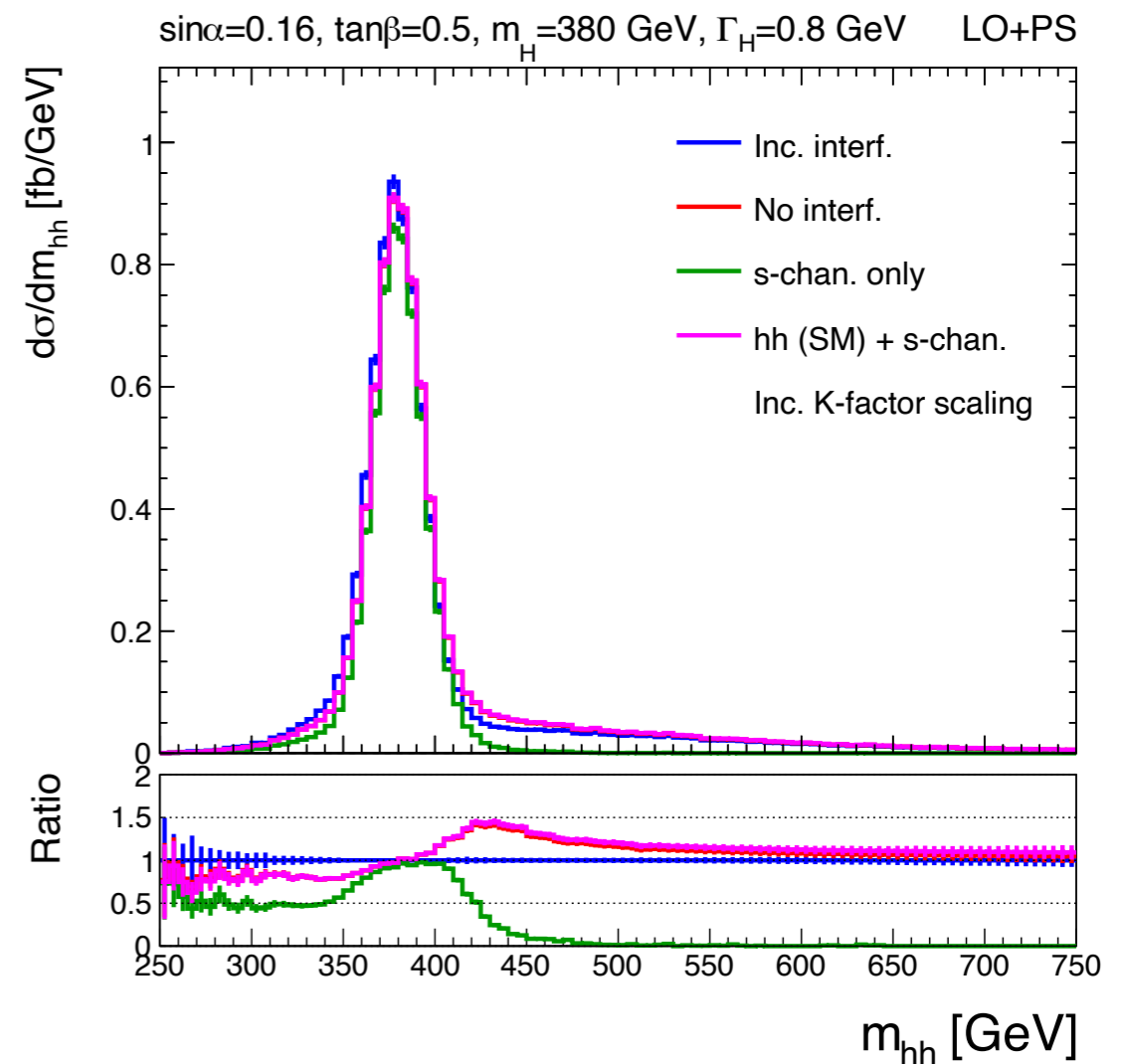


# Benchmark distributions (BM3)

- di-Higgs mass distributions
- We show different assumptions for the modelling
  - Blue = full, correct description, Green = resonant-only (most CMS and ATLAS results so far), magenta = SM non-resonant + resonant with no interference (few analyses do this already)



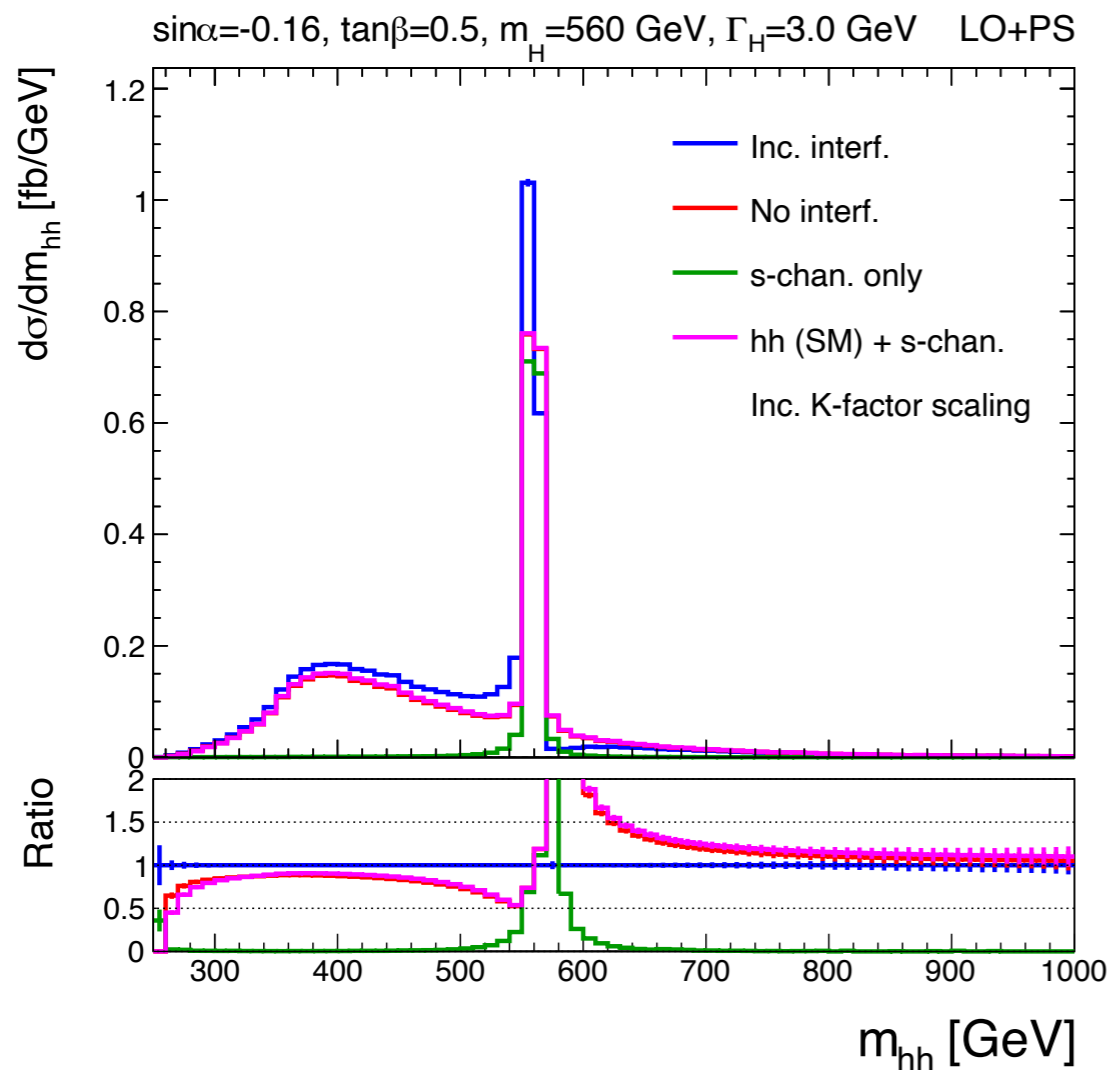
**Before smearing**



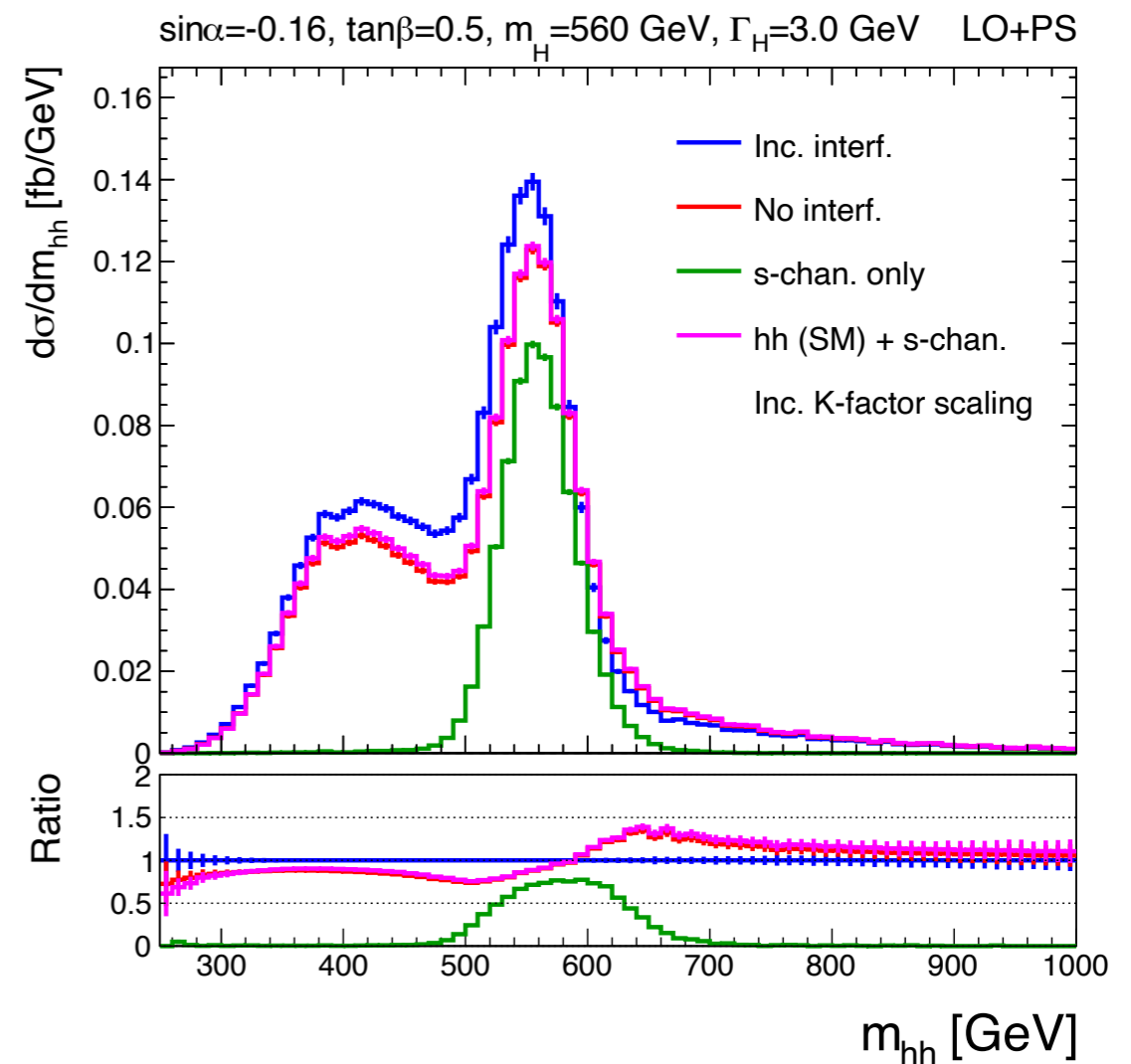
**HH → 4b-like smearing**

# Benchmark distributions (BM4)

- di-Higgs mass distributions
- We show different assumptions for the modelling
  - Blue = full, correct description, Green = resonant-only (most CMS and ATLAS results so far), magenta = SM non-resonant + resonant with no interference (few analyses do this already)



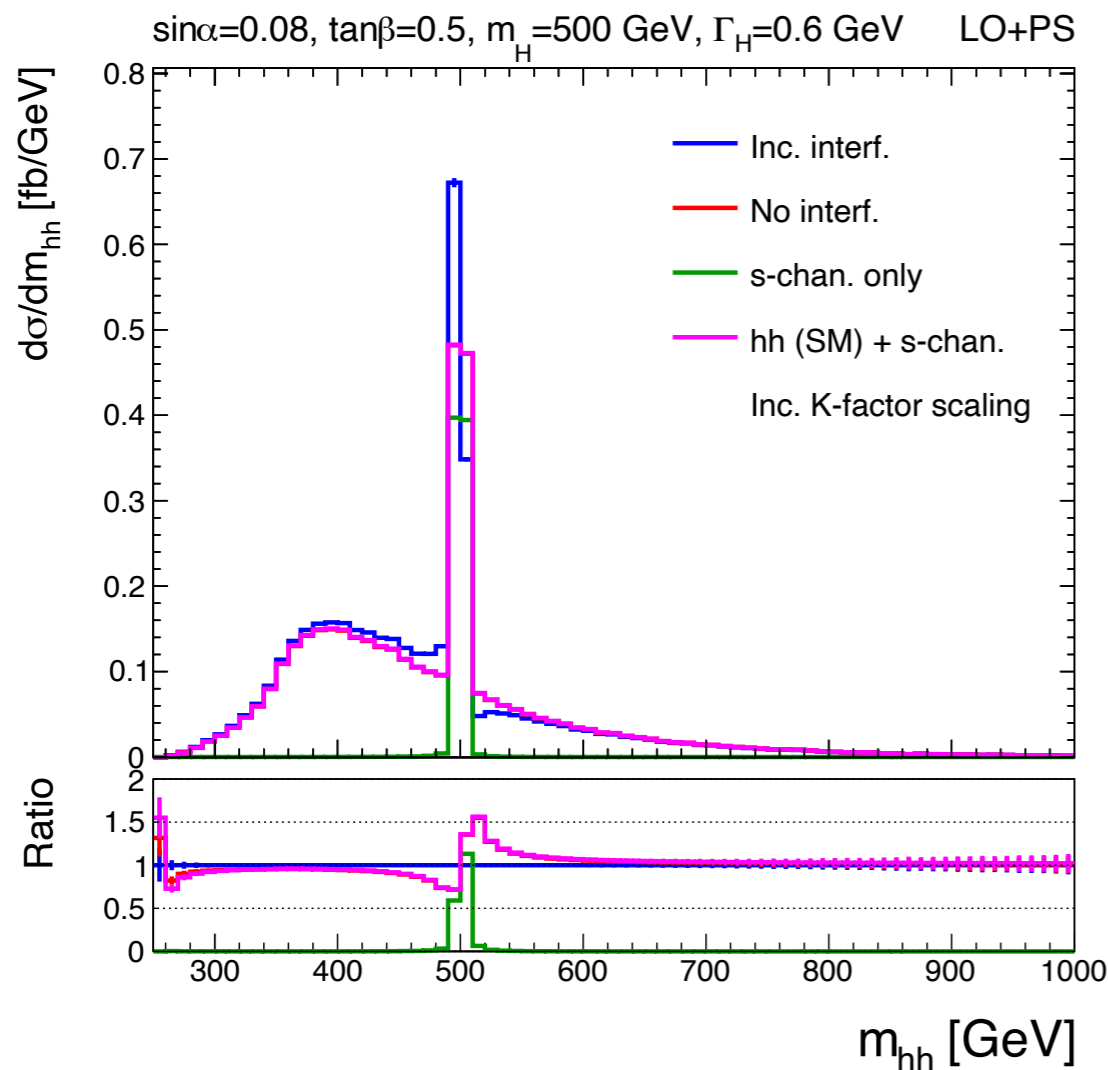
**Before smearing**



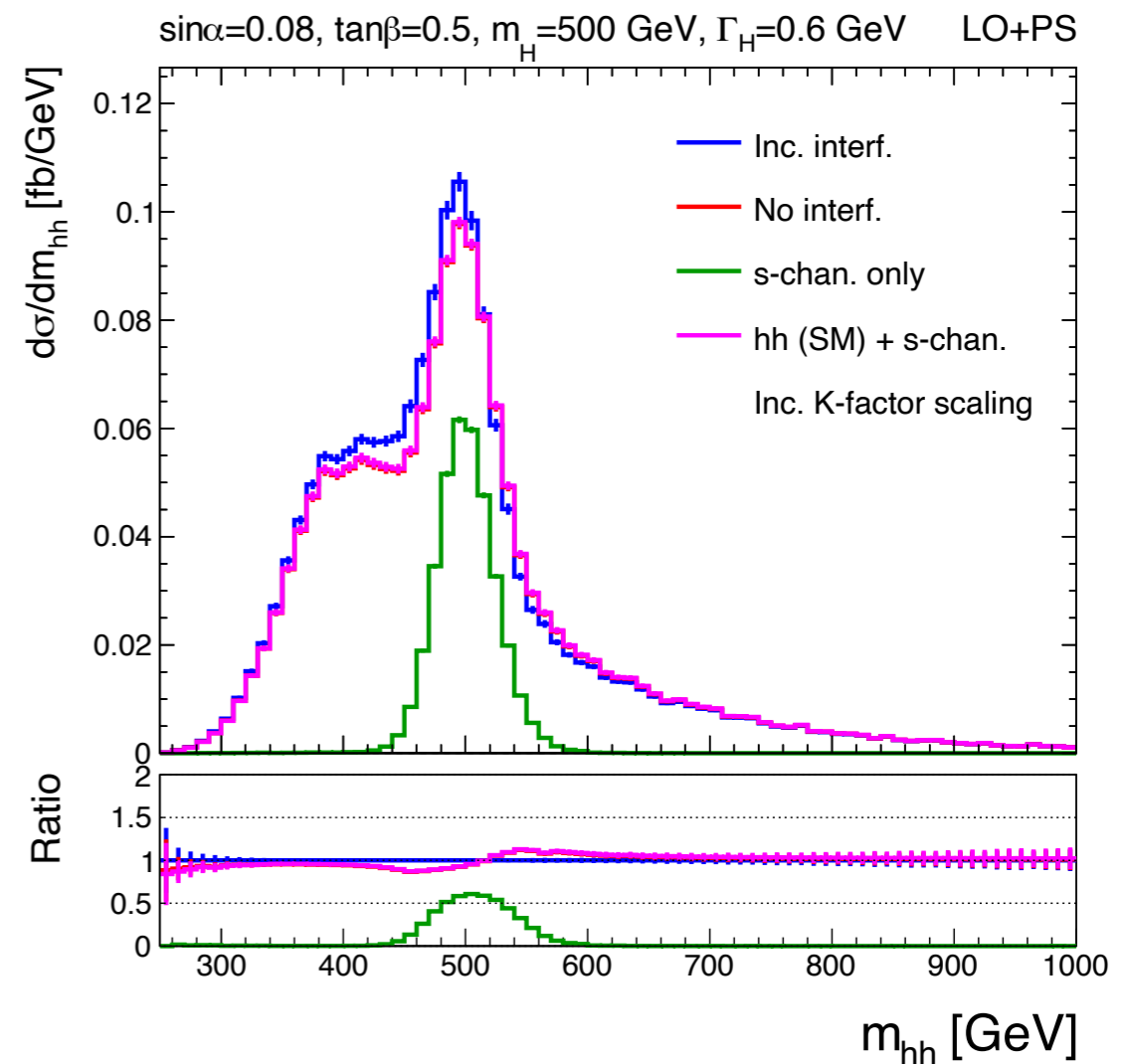
**HH → 4b-like smearing**

# Benchmark distributions (BM5)

- di-Higgs mass distributions
- We show different assumptions for the modelling
  - Blue = full, correct description, Green = resonant-only (most CMS and ATLAS results so far), magenta = SM non-resonant + resonant with no interference (few analyses do this already)



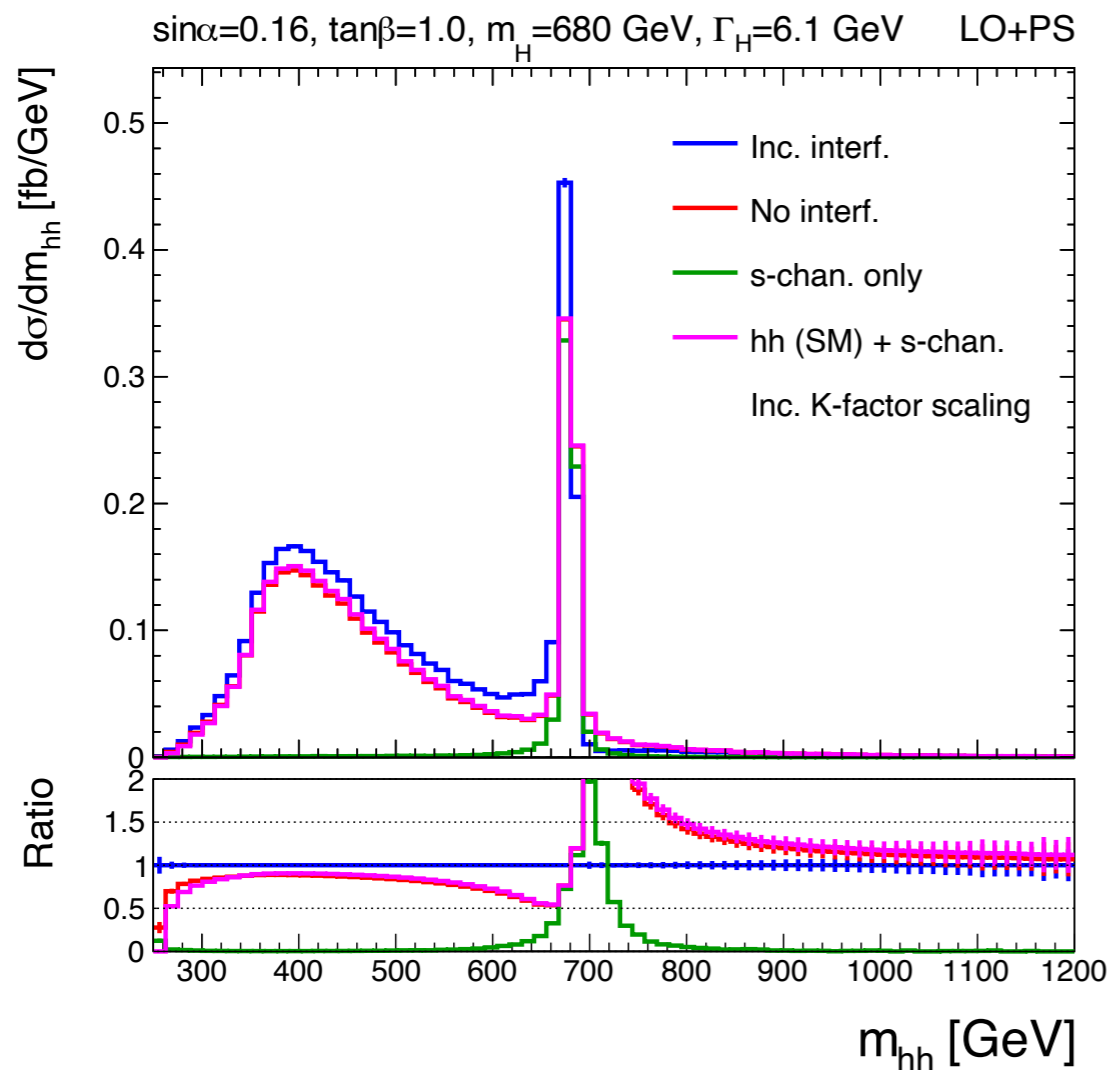
**Before smearing**



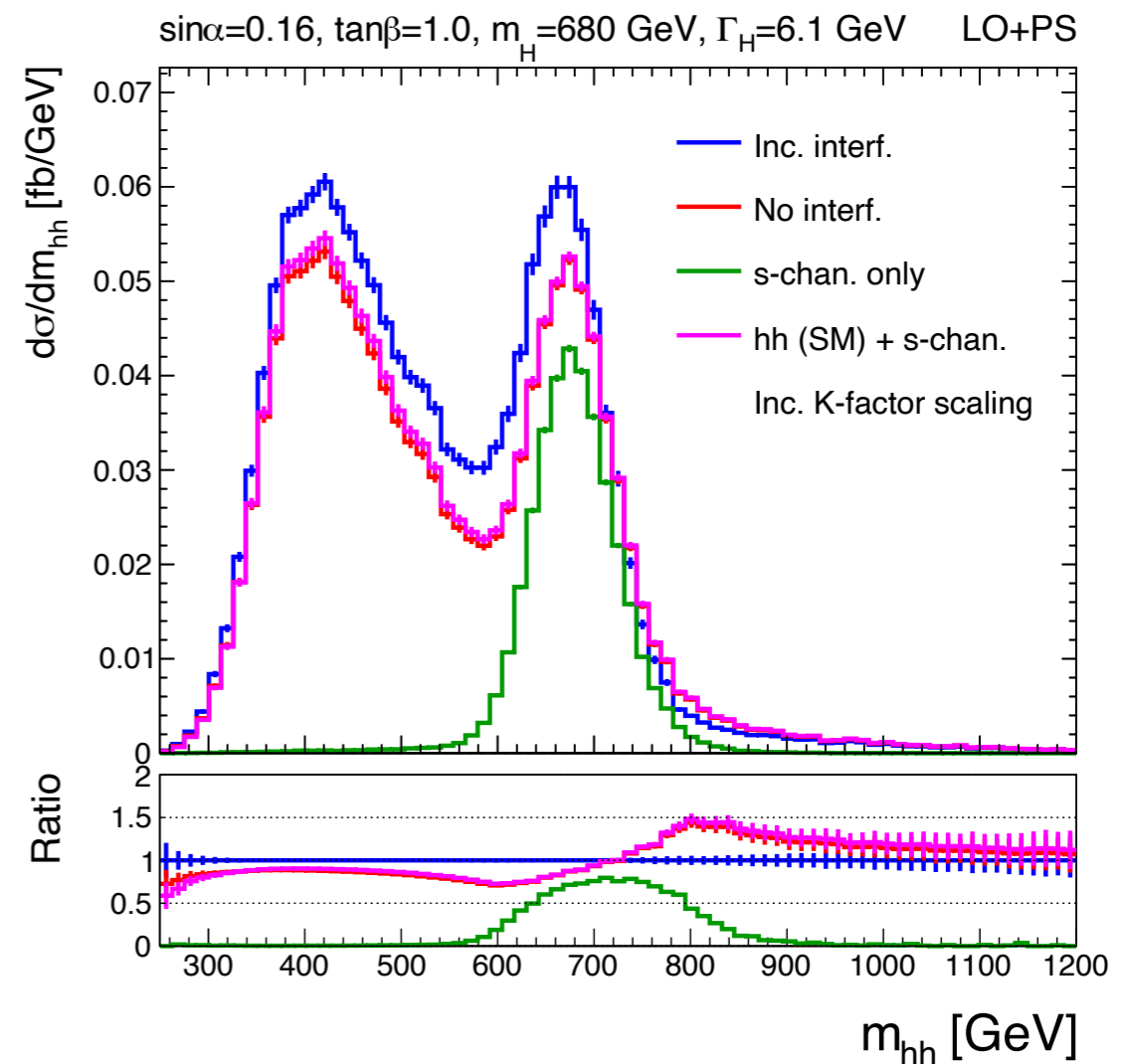
**HH → 4b-like smearing**

# Benchmark distributions (BM6)

- di-Higgs mass distributions
- We show different assumptions for the modelling
  - Blue = full, correct description, Green = resonant-only (most CMS and ATLAS results so far), magenta = SM non-resonant + resonant with no interference (few analyses do this already)



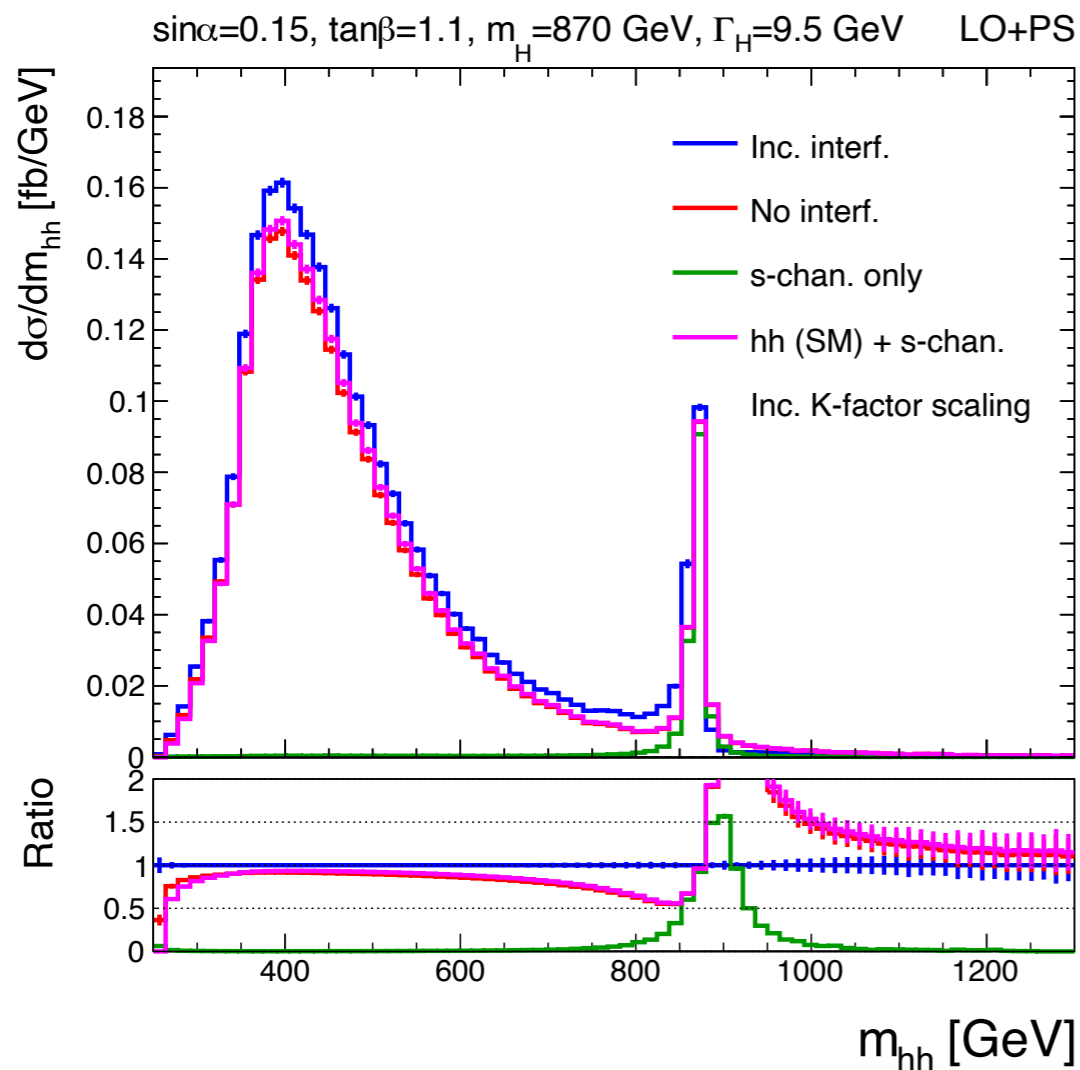
**Before smearing**



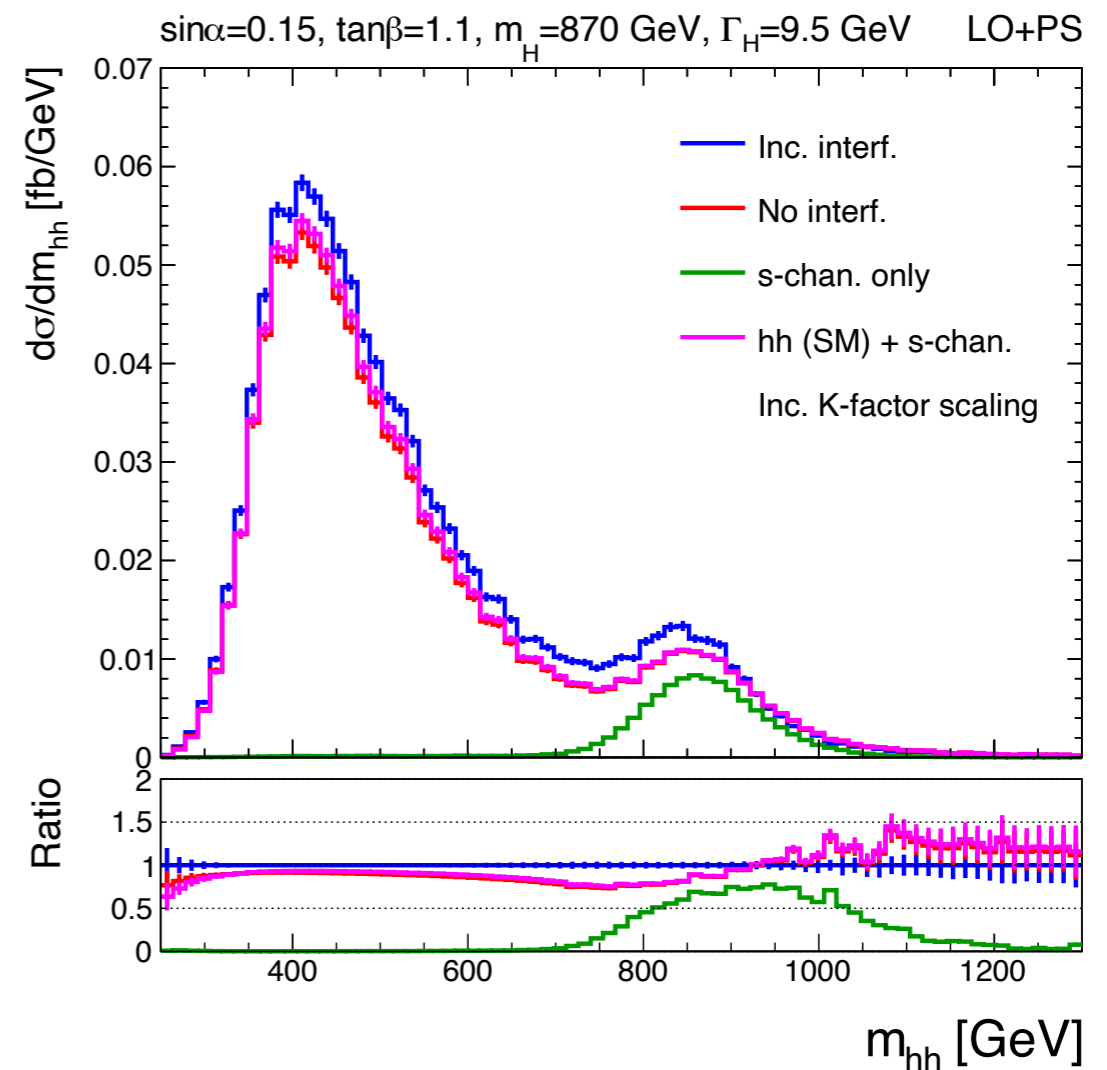
**HH → 4b-like smearing**

# Benchmark distributions (BM7)

- di-Higgs mass distributions
- We show different assumptions for the modelling
  - Blue = full, correct description, Green = resonant-only (most CMS and ATLAS results so far), magenta = SM non-resonant + resonant with no interference (few analyses do this already)



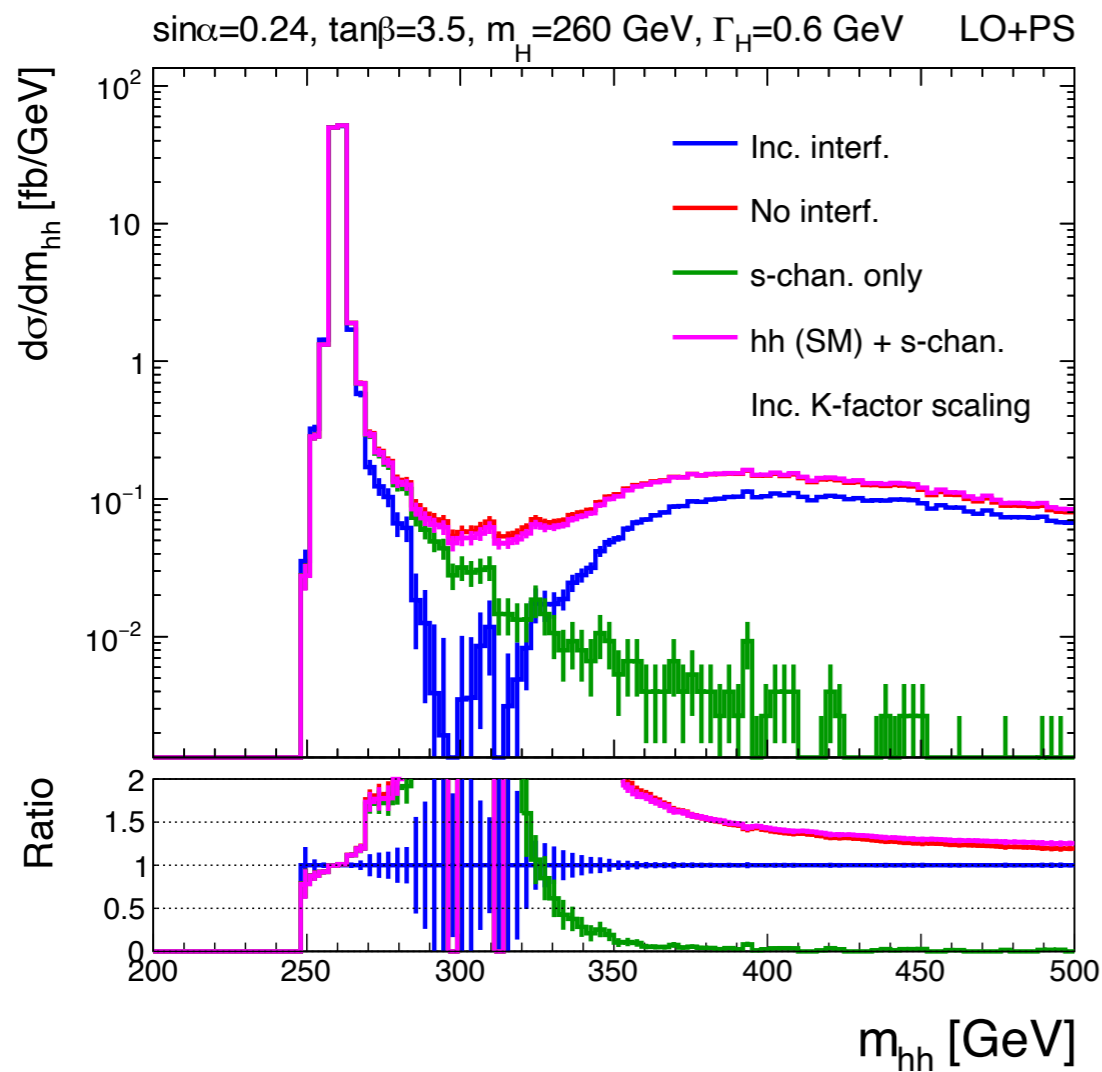
**Before smearing**



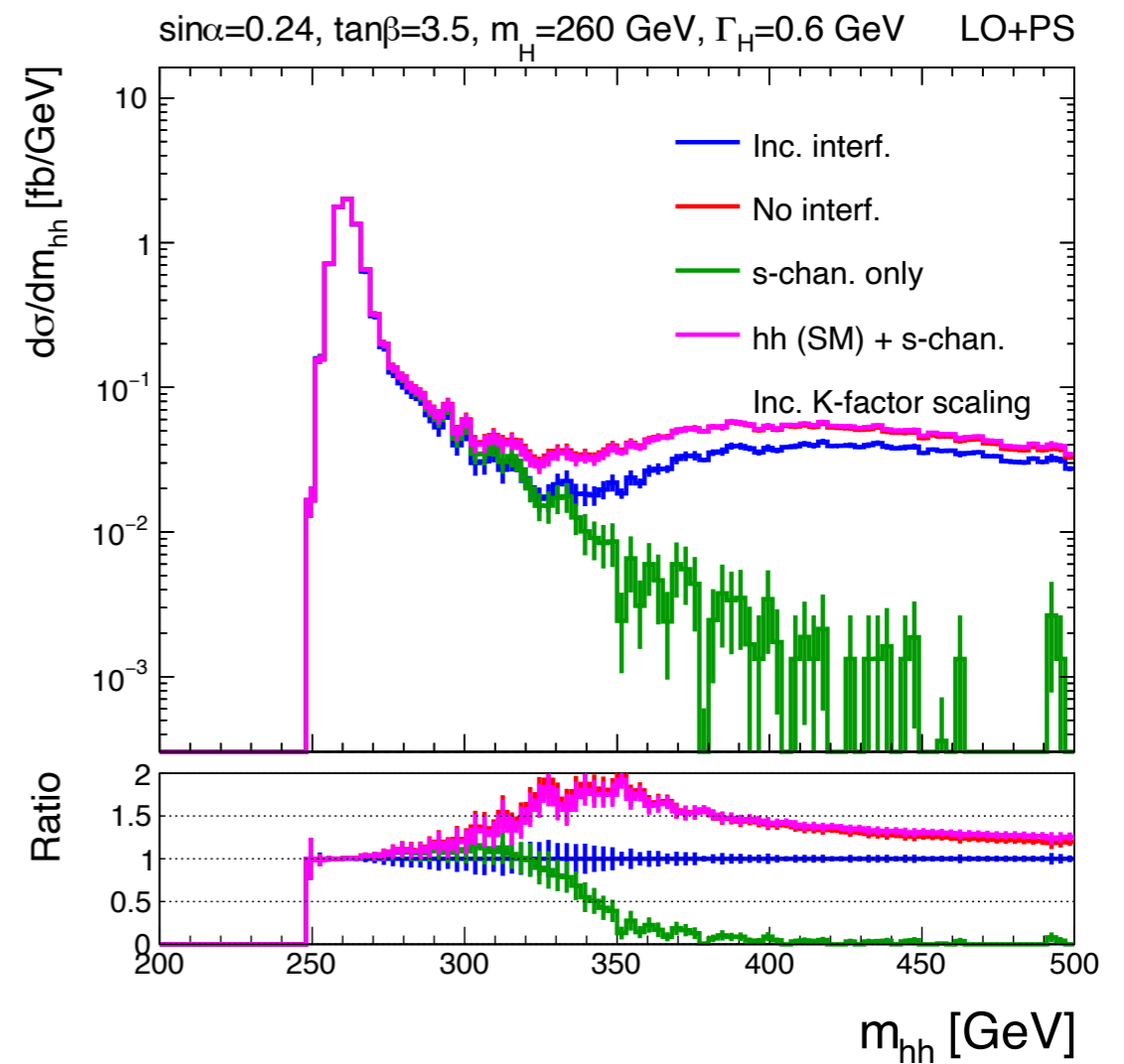
**HH → 4b-like smearing**

# Benchmark distributions (BM8)

- di-Higgs mass distributions
- We show different assumptions for the modelling
  - Blue = full, correct description, Green = resonant-only (most CMS and ATLAS results so far), magenta = SM non-resonant + resonant with no interference (few analyses do this already)



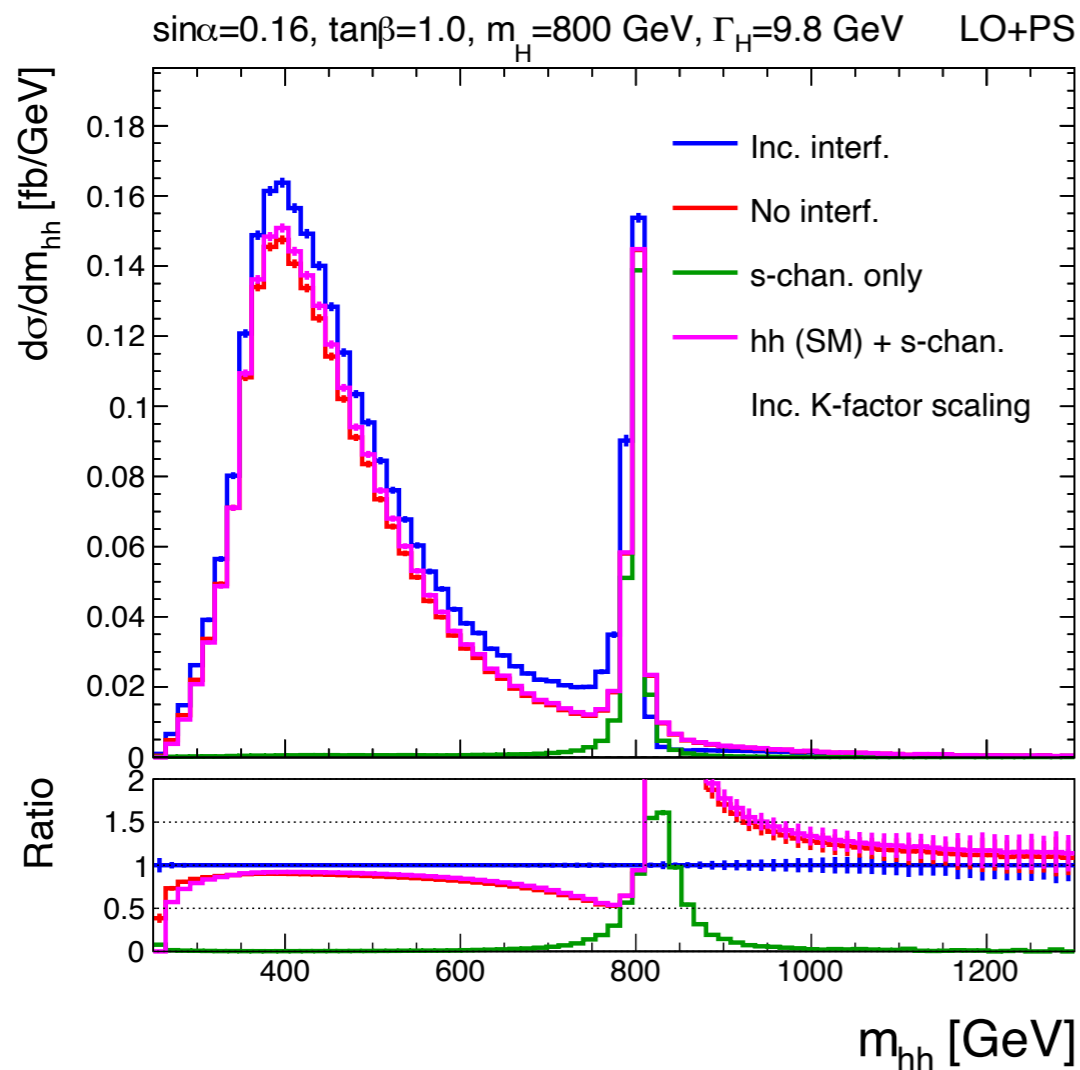
**Before smearing**



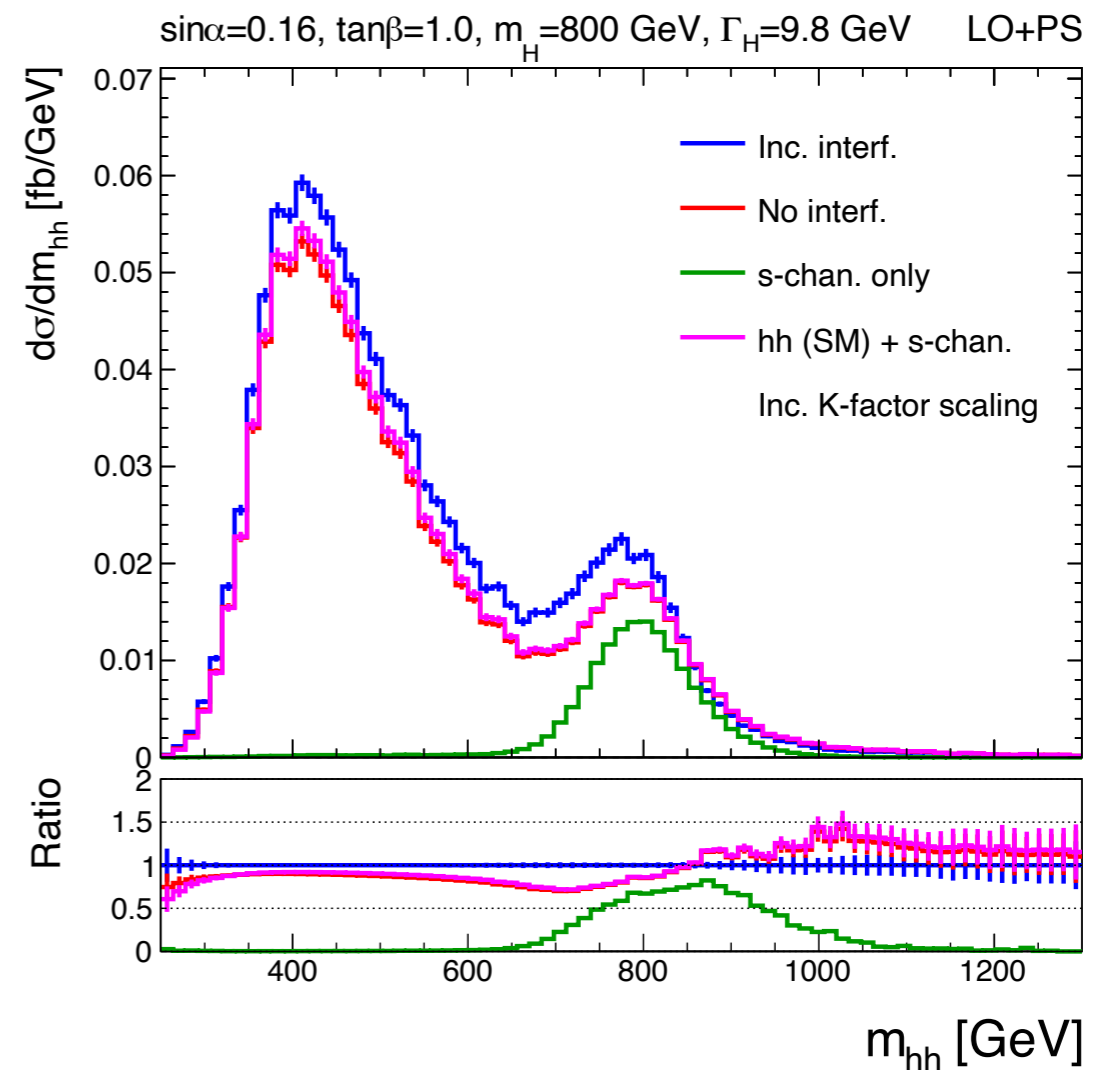
**HH → 4b-like smearing**

# Benchmark distributions (BM9)

- di-Higgs mass distributions
- We show different assumptions for the modelling
  - Blue = full, correct description, Green = resonant-only (most CMS and ATLAS results so far), magenta = SM non-resonant + resonant with no interference (few analyses do this already)



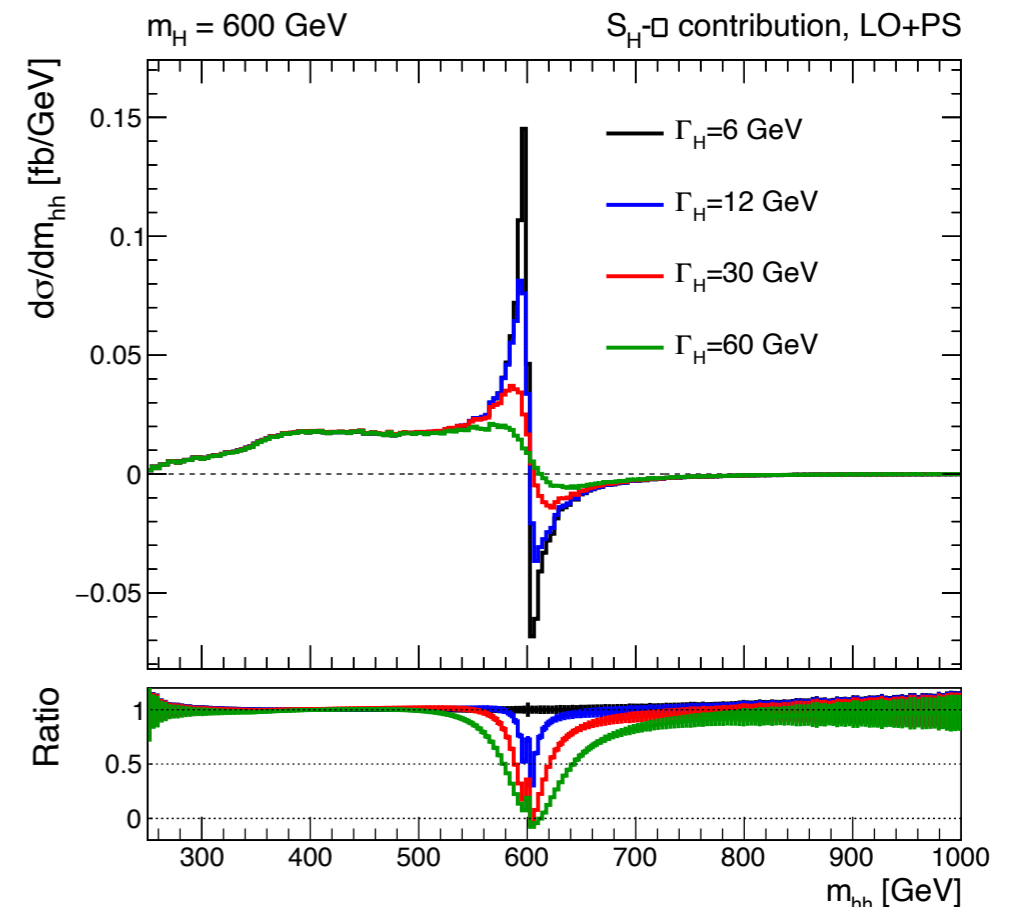
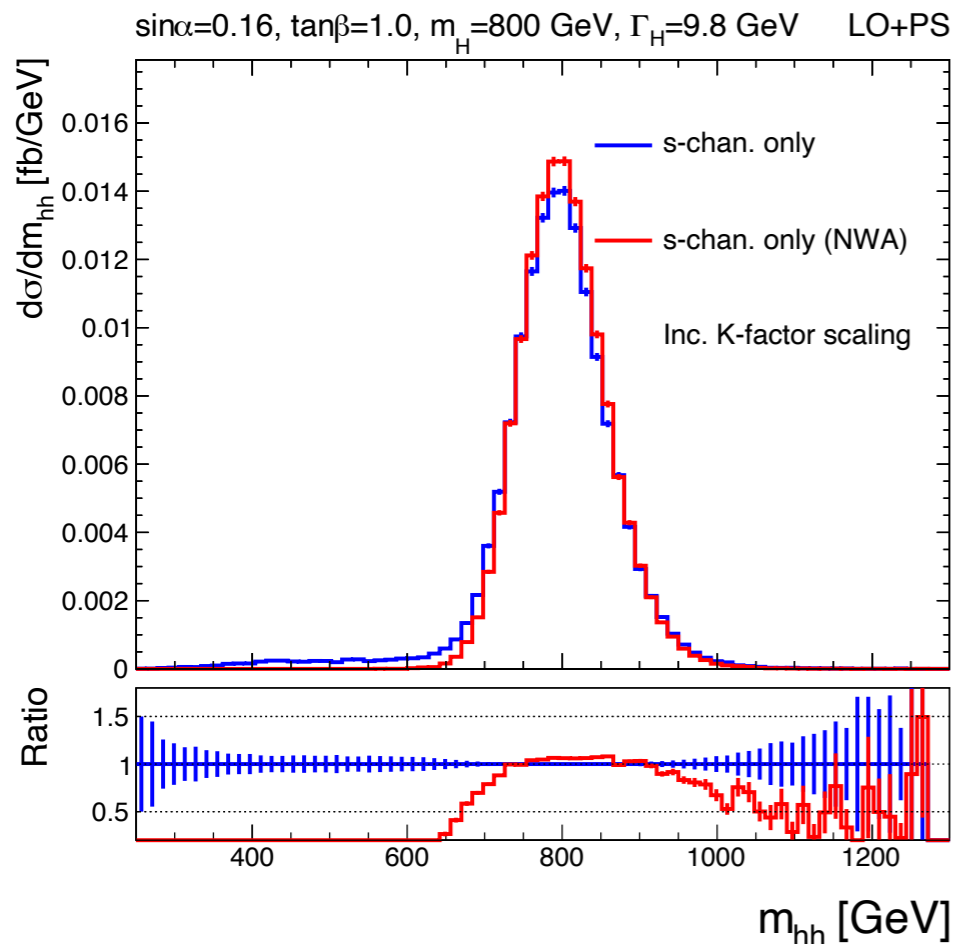
**Before smearing**



**HH → 4b-like smearing**

# Narrow width approximation (NWA) validity

- In singlet model, largest relative width we found was 1.2% - BM9
- Usually this is within experimental resolution so NWA for generation of  $S_H$  is valid
  - Generate sample with narrow width (e.g 20 MeV as below) and then rescale the branching ratio by  $(20 \text{ MeV})/\Gamma_H$  (left plot)
  - Caution: this is specific to singlet model, other models can accommodate larger widths  $O(10\%)$
- But such a re-scaling is not possible for interference terms!
  - Shapes of distributions depends on width in non-trivial way (e.g right plot)





# Benchmark distributions (BM1)

- Some other example of variables after smearing
- We show different assumptions for the modelling
  - Blue = full, correct description, Green = resonant-only (most CMS and ATLAS results so far), magenta = SM non-resonant + resonant with no interference (few analyses do this already)

