

Precision at Future Colliders

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Fundamental physics at colliders

The main goal of the collider program is to deepen our knowledge of fundamental physics

In practical terms, this means testing the SM

looking for its possible **failures** → evidence of **New Physics** (BSM)

Testing the SM

Complementarity

using different strategies to test the SM predictions
and to cover different types of new physics

- ▶ direct vs indirect searches
- ▶ different collider types (eg. e^+e^- vs hh , low-energy vs high-energy, ...)
- ▶ ...

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improve and optimize the new-physics probes to achieve better sensitivity

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Optimality

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HL-LHC and future colliders will provide a huge amount of data



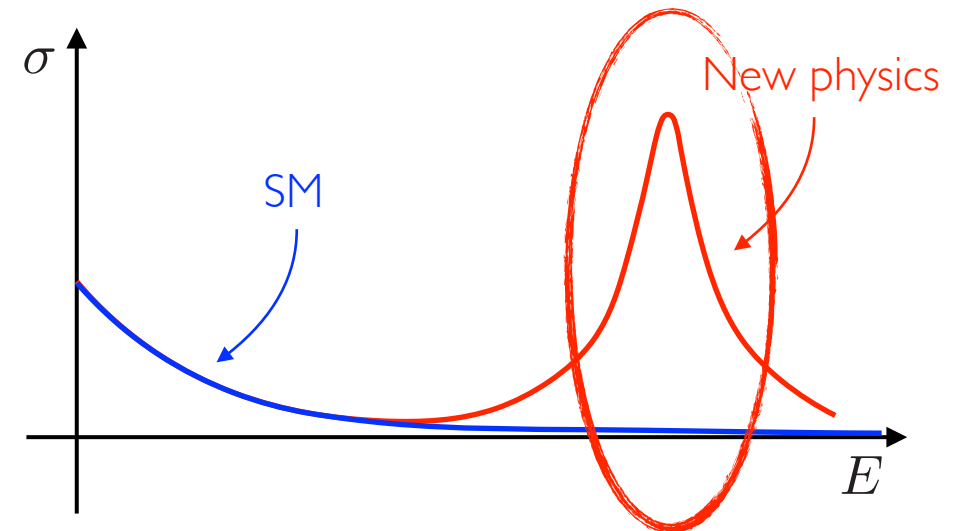
Fine details of the SM can be tested with high precision

How to look for new physics

Direct searches:

look for signals of production
of new particles

- resonant effects in kinematic distributions
- “bump” on top of a smooth SM background
(that can be often extracted from the data)



How to look for new physics

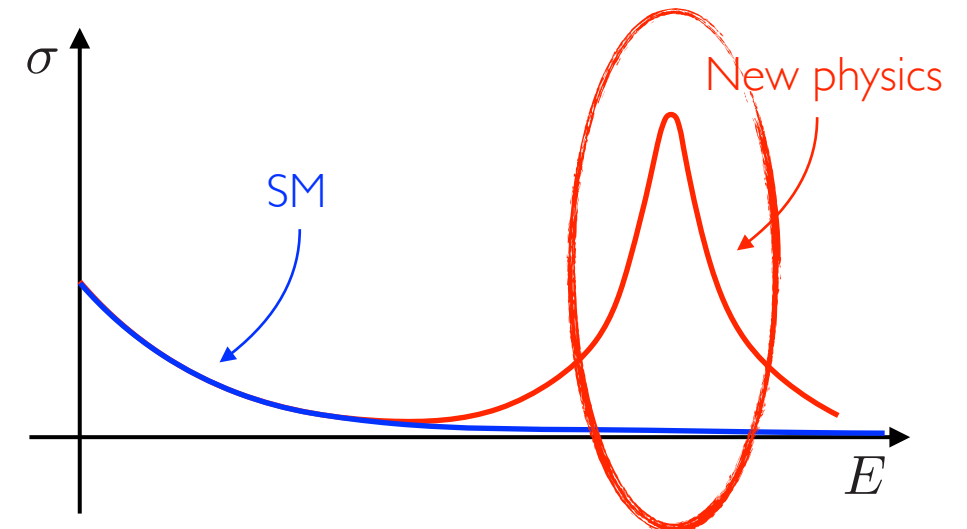
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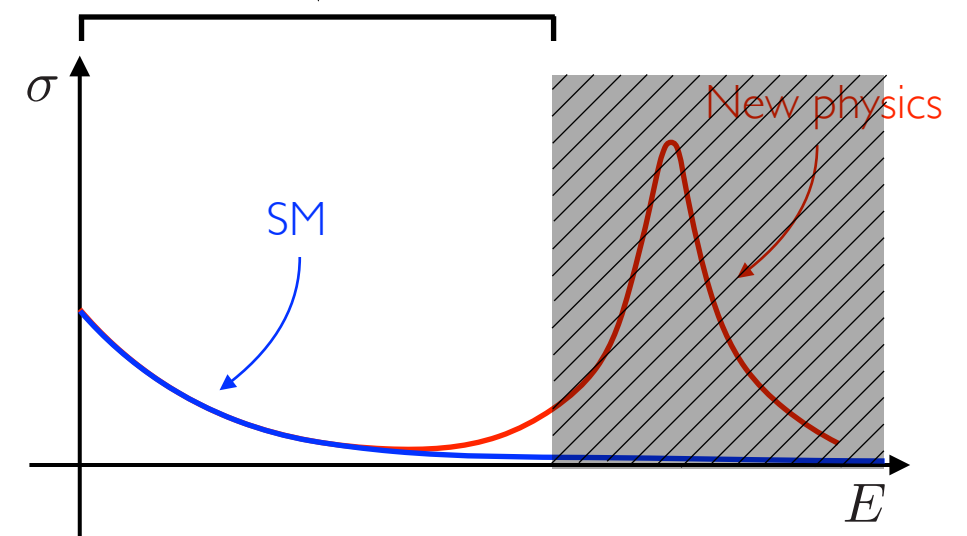
- resonant effects in kinematic distributions
- “bump” on top of a smooth SM background (that can be often extracted from the data)

Limitations:

- new particle must be resonantly produced and must decay to reconstructable final state
- limited by collider energy range



collider energy range



How to look for new physics

Direct searches:

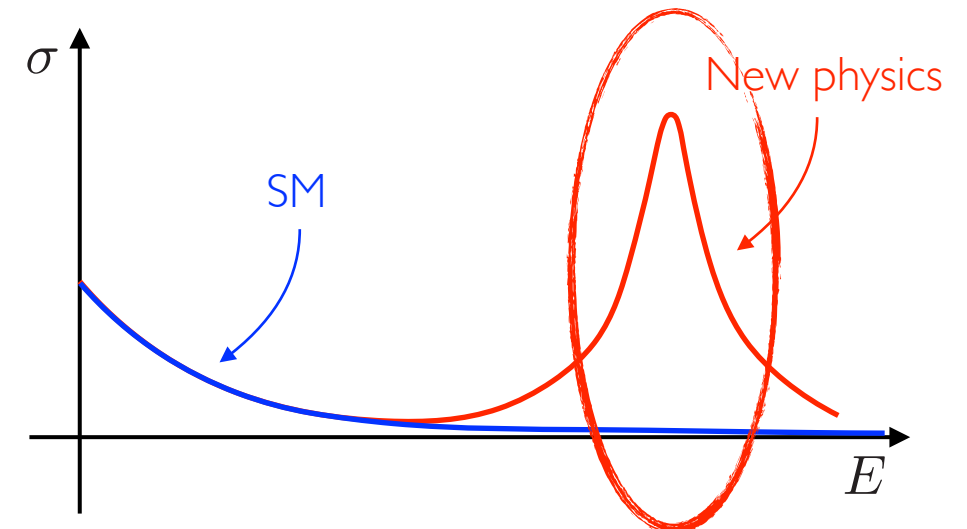
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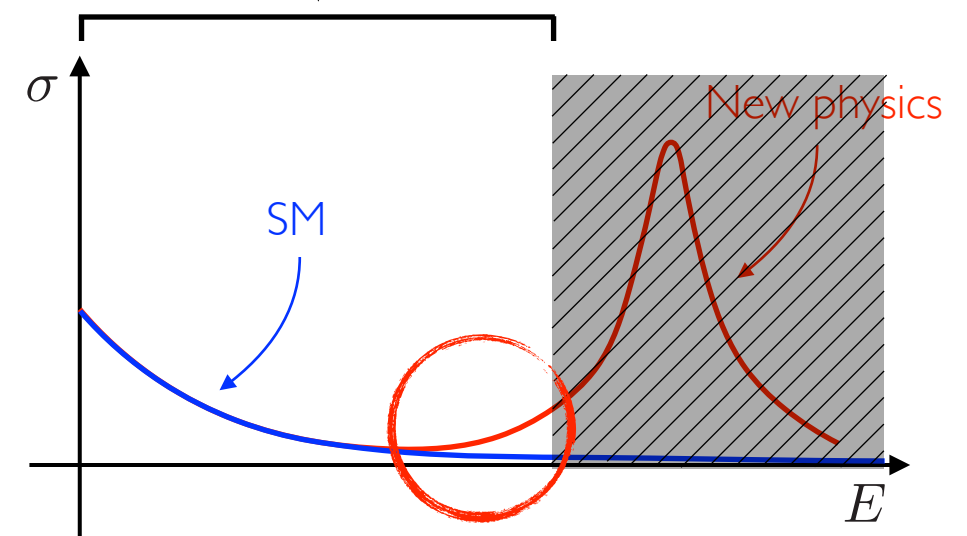
Looking for the tail: Indirect searches

even if we can not directly produce the new particles, we can test their **indirect effects**

- ▶ LEP data at 200 GeV tested new particles with masses up to 3 TeV !

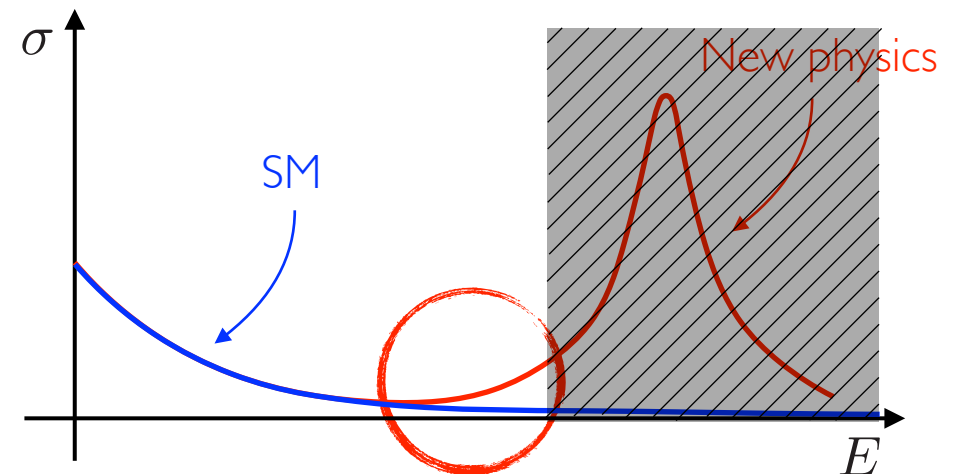


collider energy range



Tails are “universal”

Indirect searches have important advantages



“universality”

- deviations from SM exhibit small number of behaviors dictated by symmetries
- simple parametrization in terms of EFT operators

“model independence”

- captures a huge class of new-physics models

“ubiquity”

- deviations are present also in channels with non-resonant new physics production
- can often be seen also in channels where the final state can not be fully reconstructed

The challenges of indirect searches

Performing indirect searches is a challenging task that requires several key ingredients

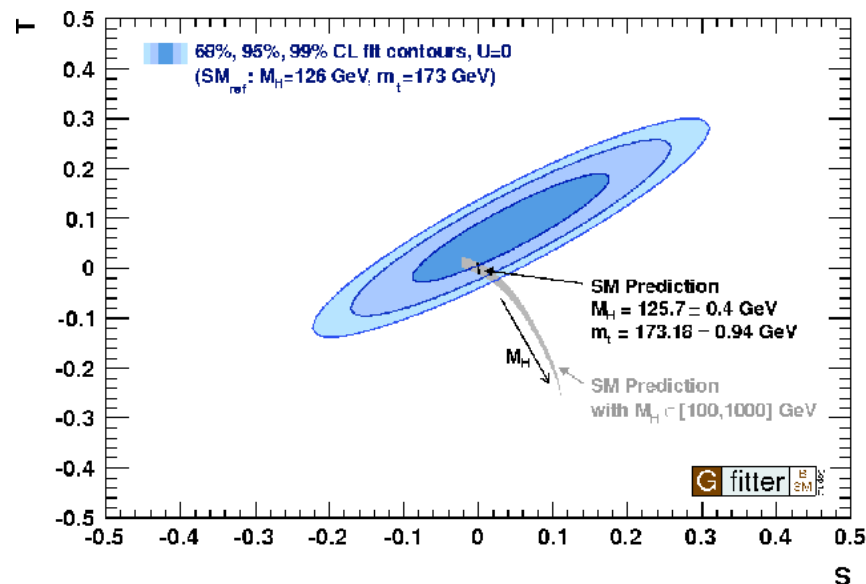
- ▶ Accurate theoretical knowledge of the SM and BSM predictions (i.e. small theoretical systematic uncertainty)
 - ➔ needed to compare theoretical expectation with the experimental data
- ▶ Accurate experimental measurements (i.e. small experimental systematic and statistical uncertainty)
 - ➔ in many cases we expect small deviations with respect to the SM
- ▶ Use of effective search strategies and optimized statistical analysis

*Precision EW measurements
at Lepton Colliders*

Precision at lepton colliders

Precision measurements at lepton colliders have a long and successful history

example: oblique parameters at LEP

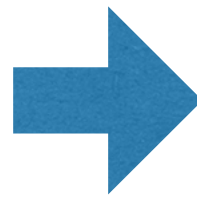
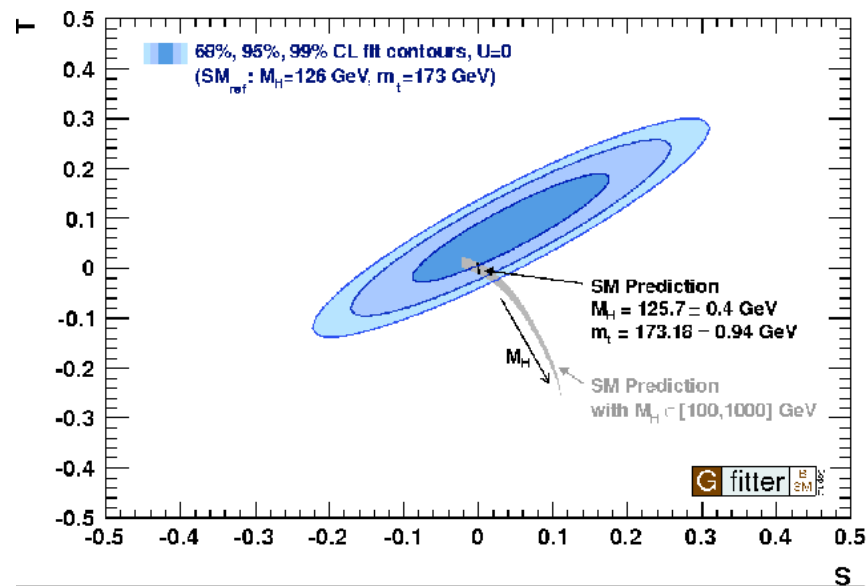


- ◆ 0.1% precision possible thanks to very low systematic errors

Precision at lepton colliders

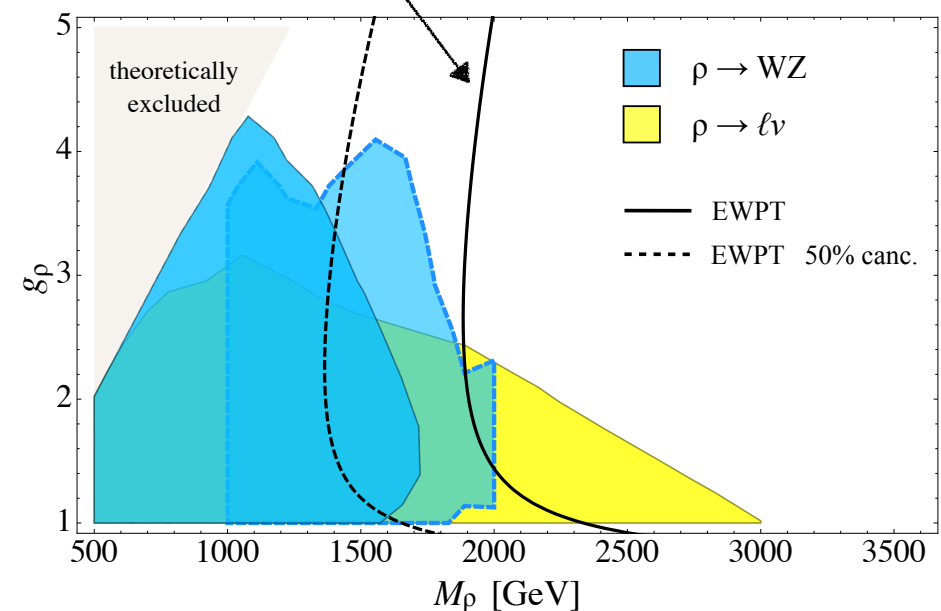
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bounds from S parameter

[Pappadopulo, Thamm et al.]

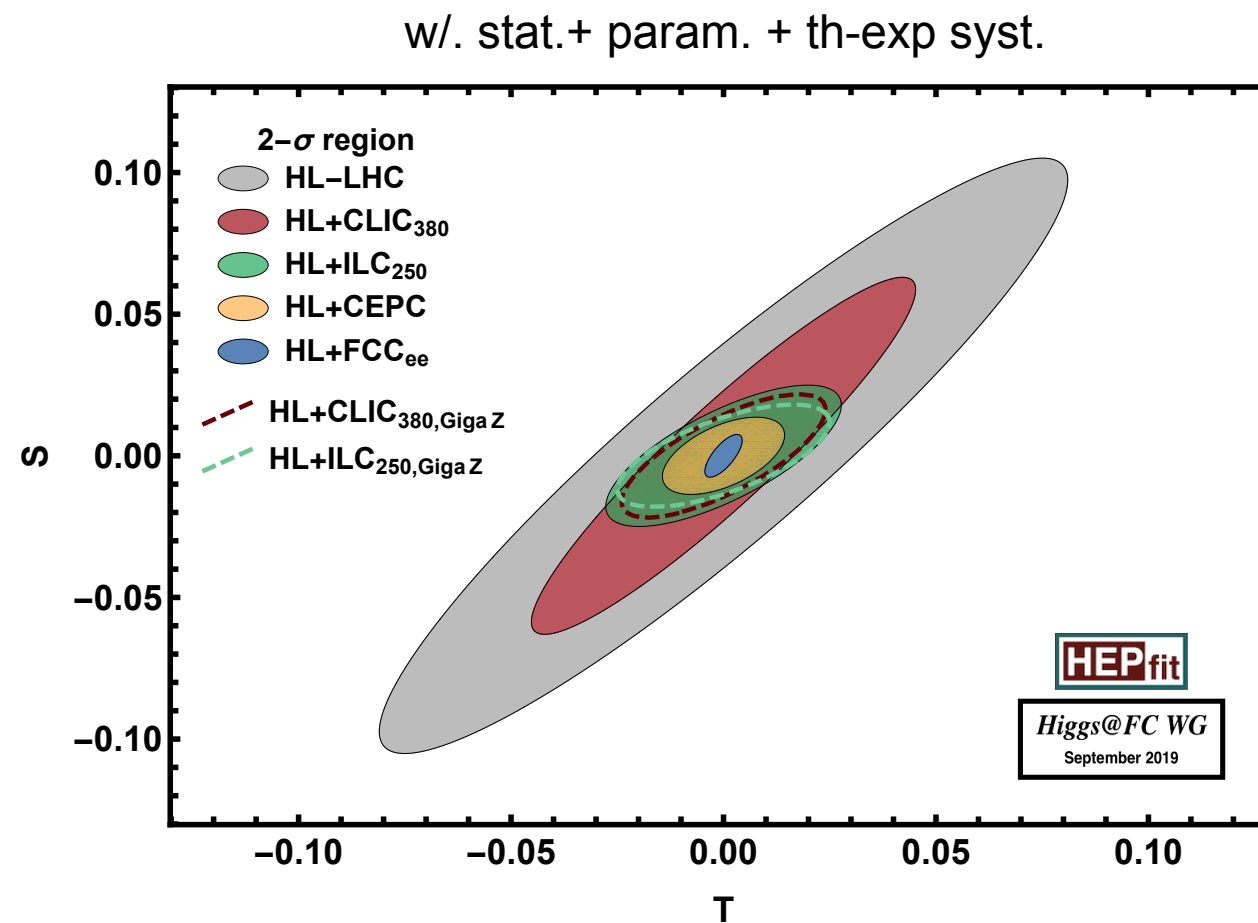


- ◆ 0.1% precision possible thanks to very low systematic errors
- ◆ can probe new physics at the TeV scale

Precision at lepton colliders

Future e^+e^- lepton colliders can significantly improve the reach

- ◆ Bounds on oblique parameters will become one order of magnitude stronger



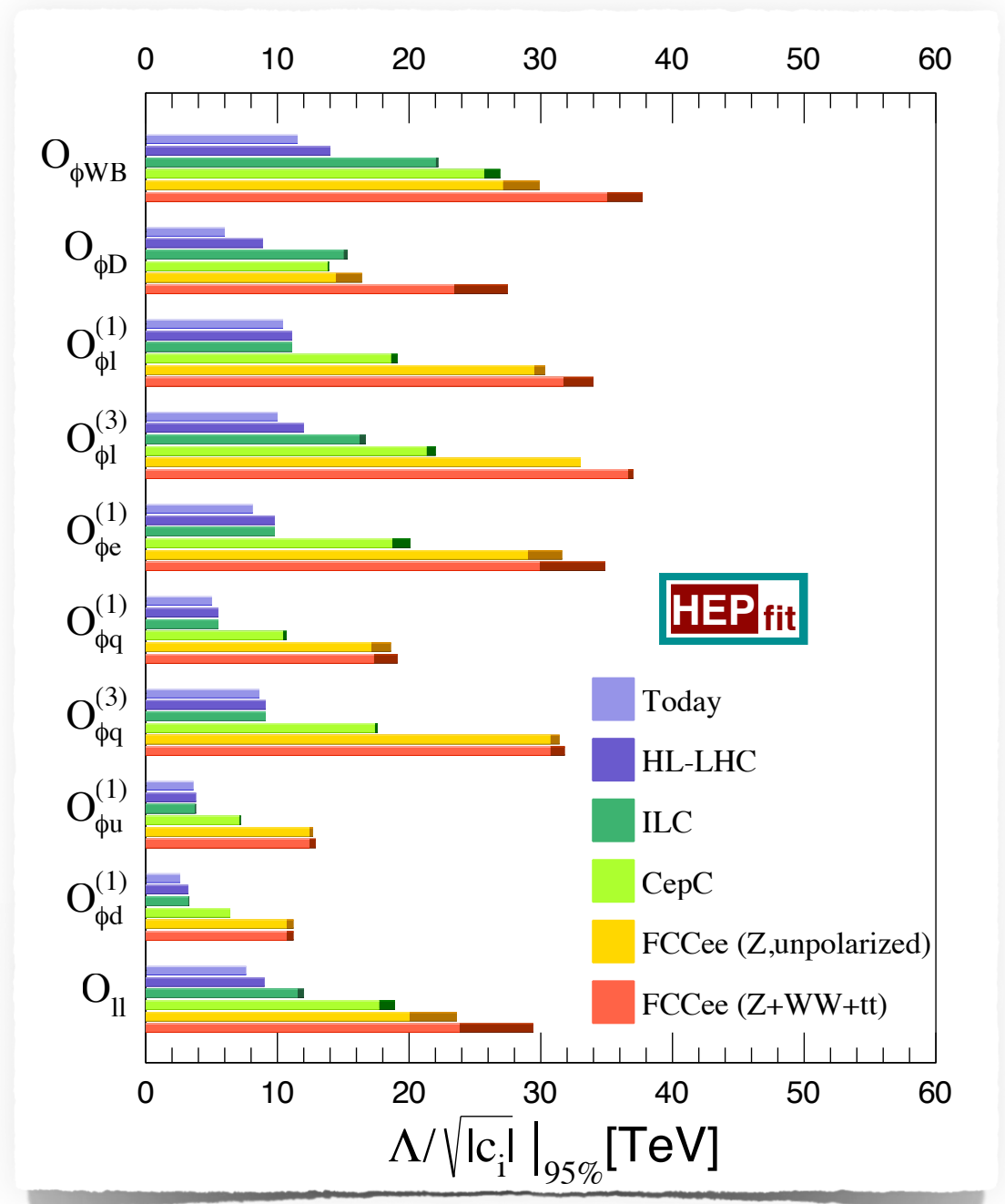
Precision at lepton colliders

Indirect probes of new physics
can test high energy scales

HL-LHC : $\Lambda \sim 10$ TeV

ILC - CepC : $\Lambda \sim 20$ TeV

FCC_{ee} : $\Lambda \sim 30$ TeV



Precision at lepton colliders

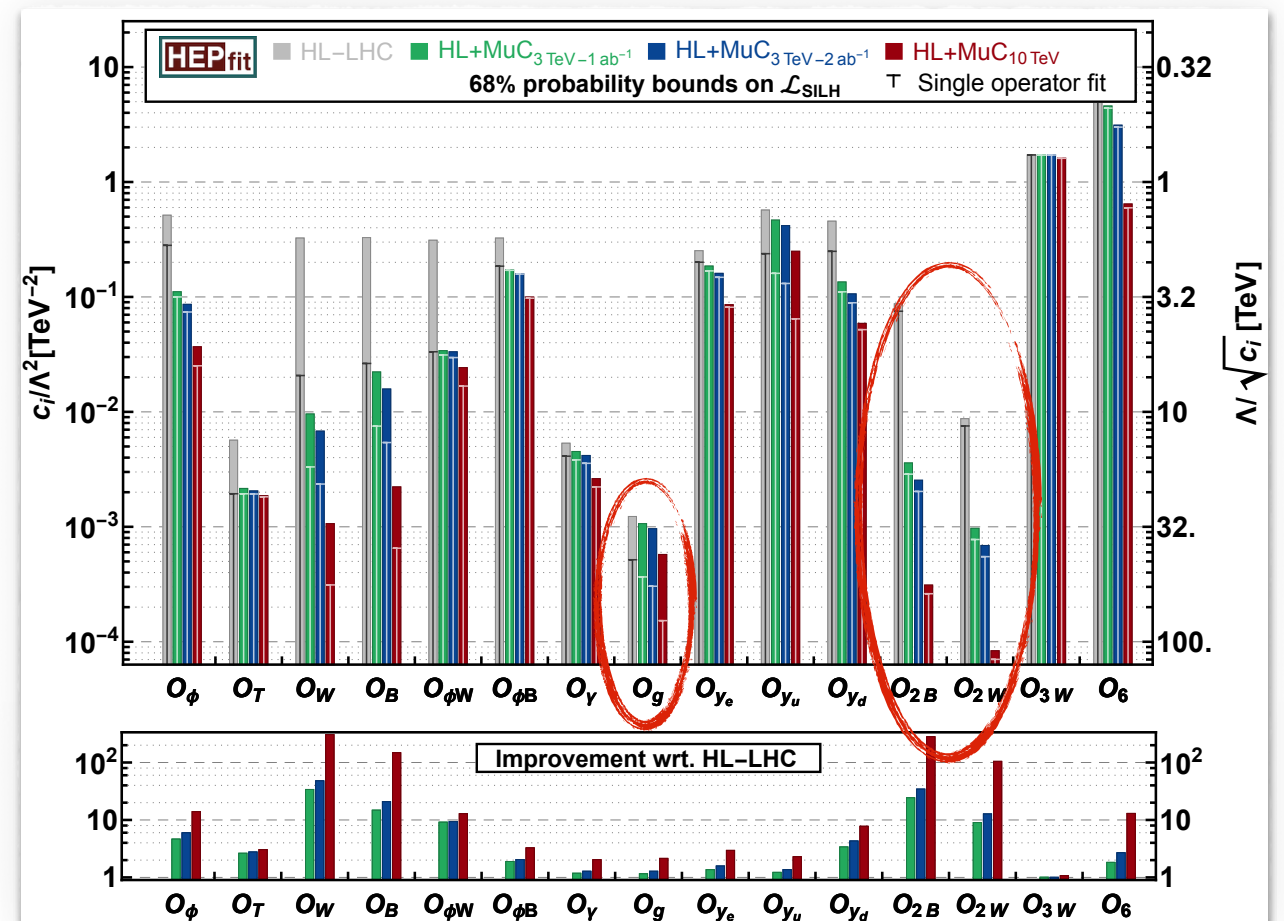
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FCC_{ee} : $\Lambda \sim 30$ TeV

MuC_{10TeV} : $\Lambda \sim 50 - 100$ TeV



Precision vs direct searches

Precision measurements are competitive with direct detection reach

Example: Minimal/Accidental dark matter

[Cirelli, Fornengo, Strumia '05; ...
Del Nobile, Nardecchia, Panci '15;
Di Luzio, Gröber et al. '15;
Mitridate, Redi et al. '17]

New EW multiplets at the TeV scale

- accidentally stable
(no renormalizable χ SM SM interactions)
- viable DM candidates

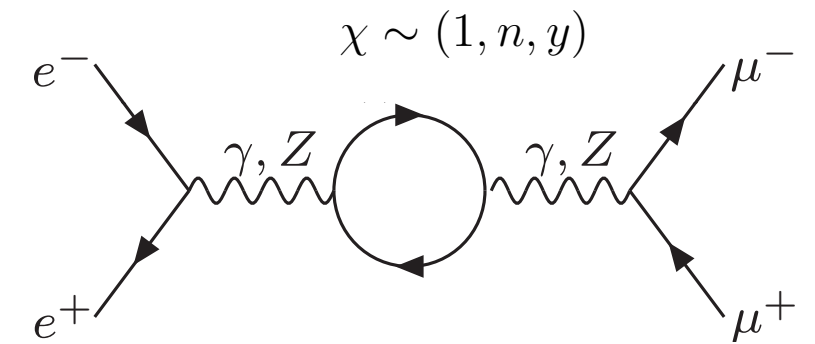
χ / m_χ [TeV]	DM
$(1, 2, 1/2)_{DF}^*$	1.1
$(1, 3, \epsilon)_{CS}$	1.6
$(1, 3, \epsilon)_{DF}$	2.0
$(1, 3, 0)_{MF}^{**}$	2.8
$(1, 5, \epsilon)_{CS}$	6.6
$(1, 5, \epsilon)_{DF}$	6.6
$(1, 5, 0)_{MF}^{***}$	14
$(1, 7, \epsilon)_{CS}$	16
$(1, 7, \epsilon)_{DF}$	16

RS = Real Scalar
CS = Complex Scalar
MF = Majorana Fermion
DF = Dirac Fermion

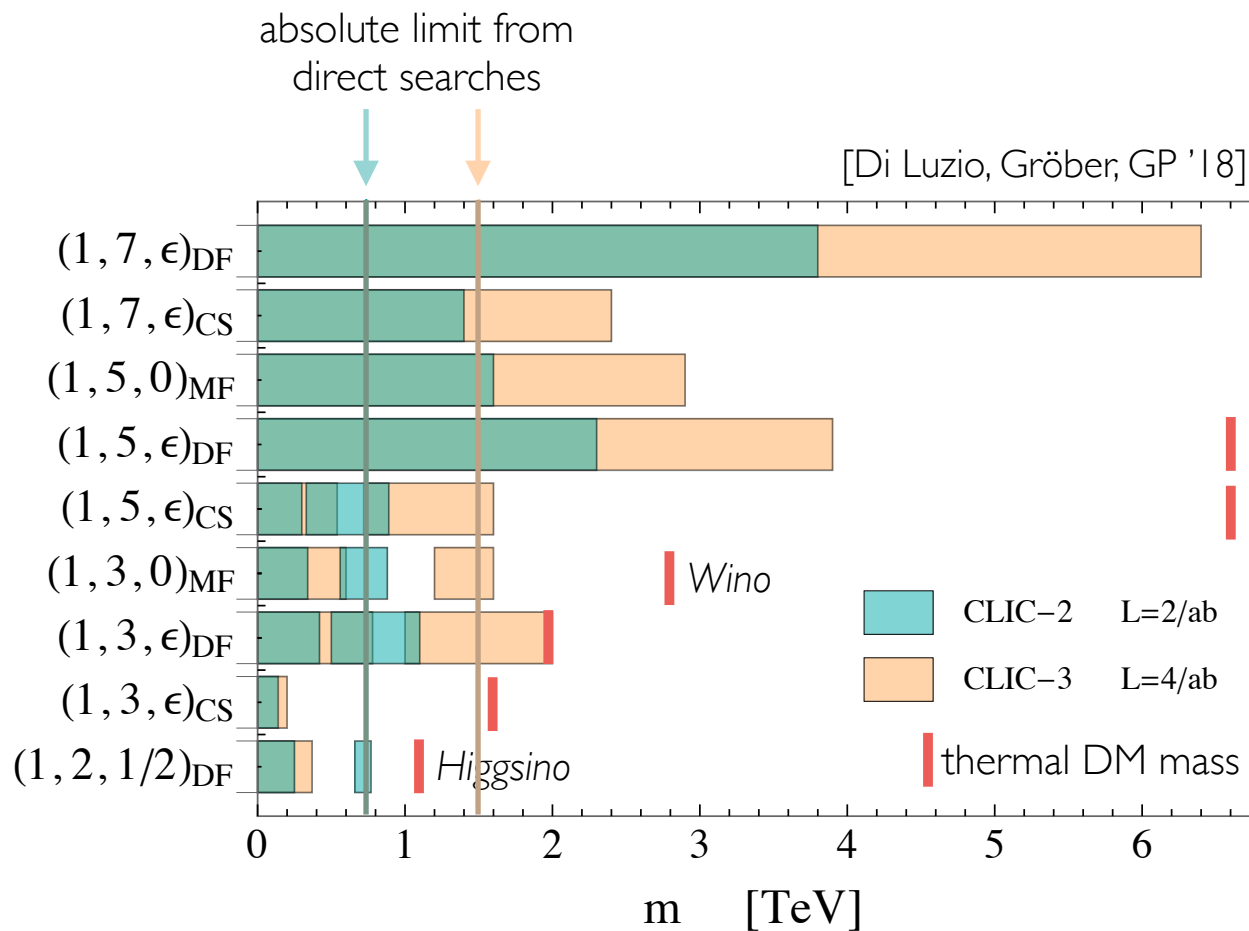
* Higgsino DM
** Wino DM
*** Minimal DM

Minimal dark matter

- ◆ Universal corrections to $2 \rightarrow 2$ fermion scattering
- ◆ Testable deviations in angular distributions



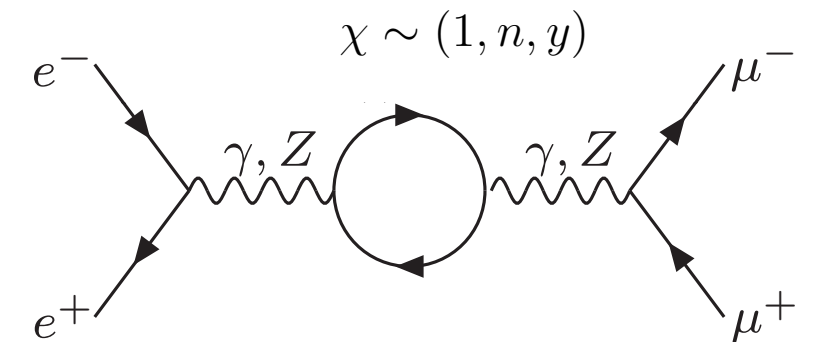
[Harigaya et al. '15;
Matsumoto et al. '17;
Di Luzio, Gröber, GP '18]



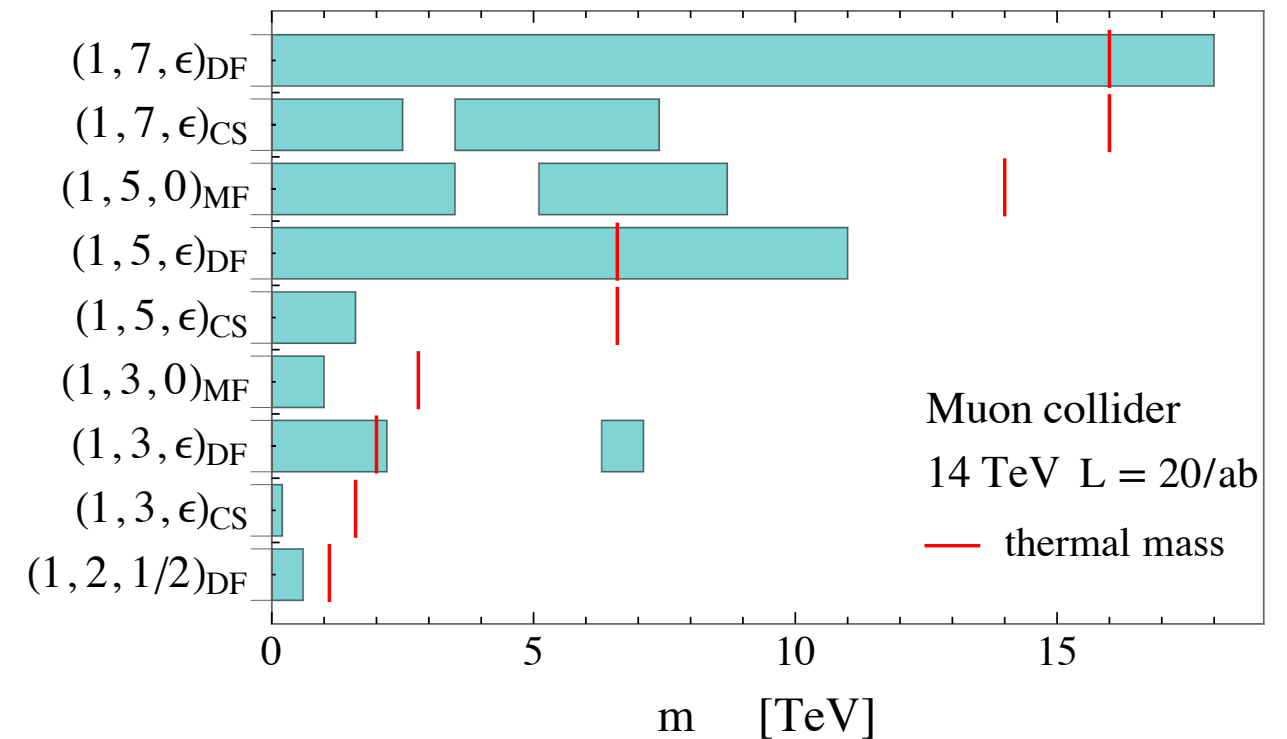
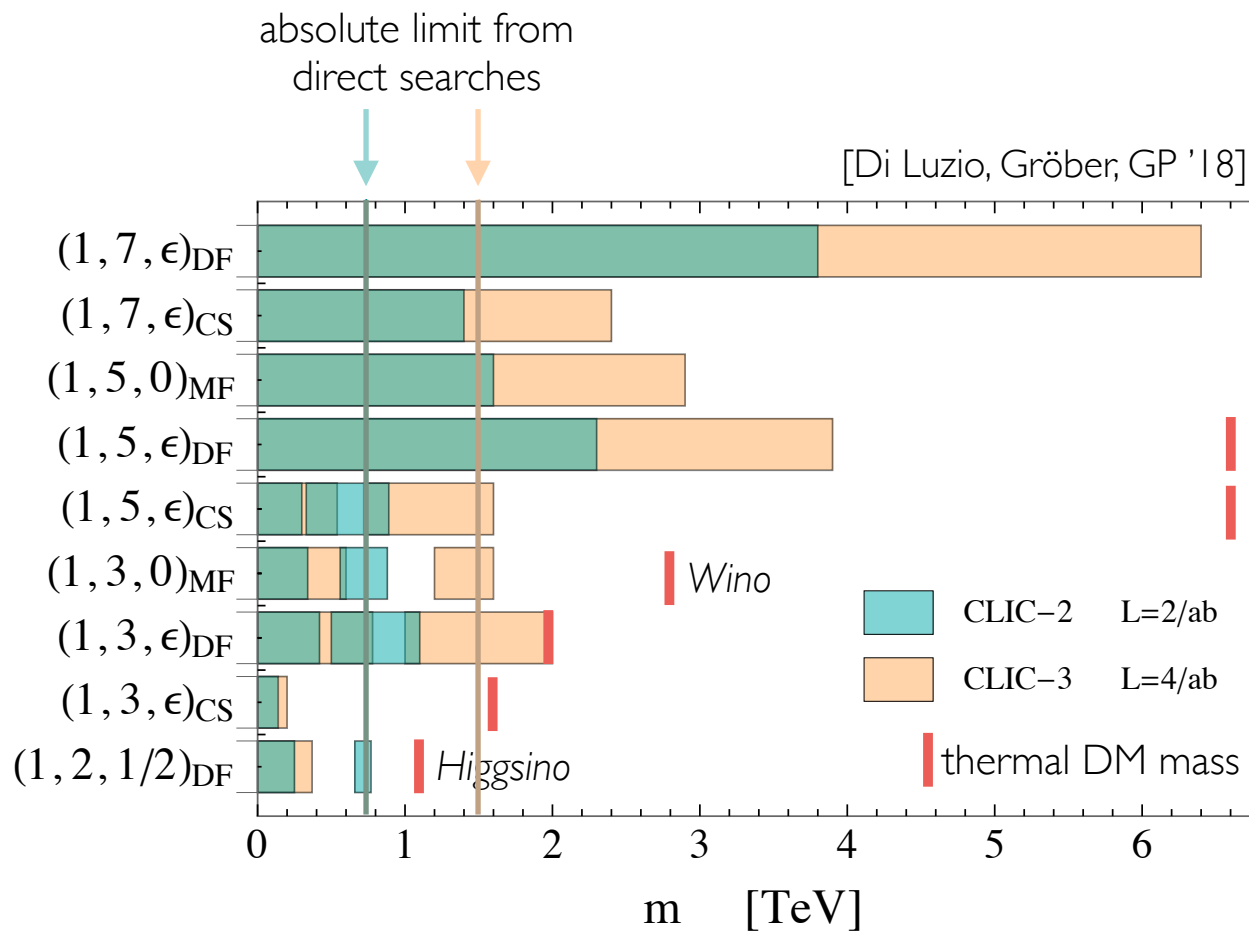
Indirect probes can extend direct detection reach for large multiplets at CLIC

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*Precision EW measurements
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Precision at hadron colliders

New ideas allow us to exploit also **hadron colliders!**

- ◆ sizeable systematic errors in many cases do not allow for pole precision measurements



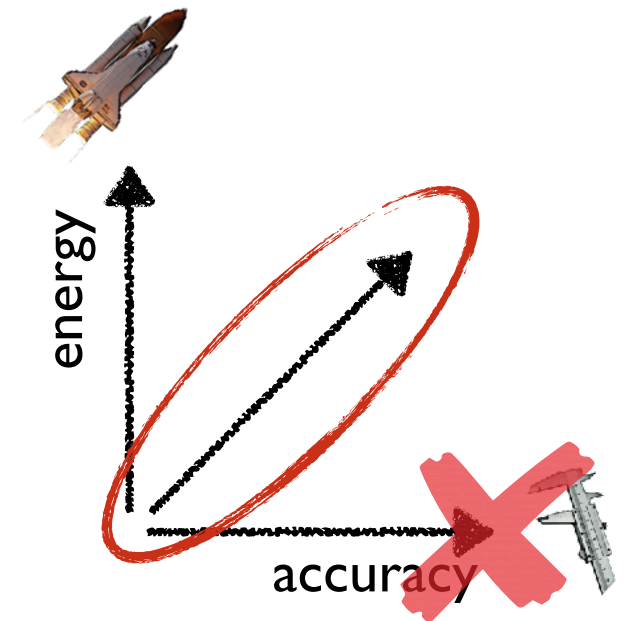
Precision at hadron colliders

New ideas allow us to exploit also **hadron colliders!**

- ◆ sizeable systematic errors in many cases do not allow for pole precision measurements
- ◆ however we can exploit the high energy reach

→ energy helps accuracy!

[Farina, GP, Pappadopulo, Ruderman, Torre, Wulzer '16]



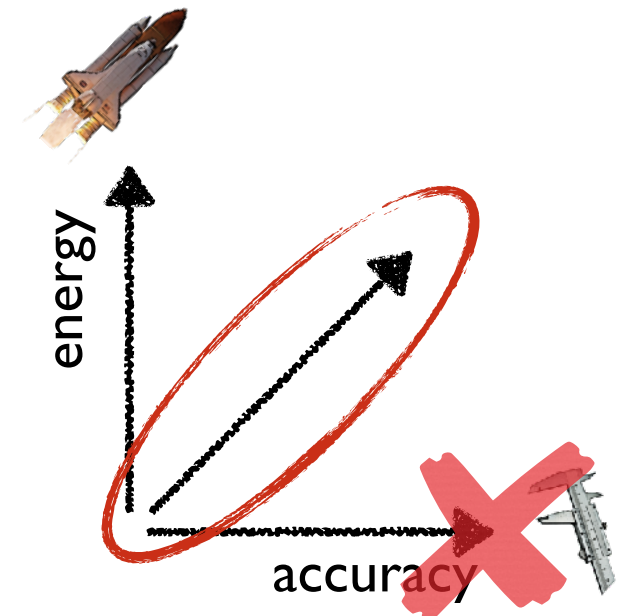
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- ◆ key point: deviations from SM typically **grow with energy**

$$\frac{\mathcal{A}_{\text{SM+BSM}}}{\mathcal{A}_{\text{SM}}} \sim 1 + \# \frac{E^2}{\Lambda^2}$$

→ LHC can match LEP sensitivity exploiting the **high energy** reach

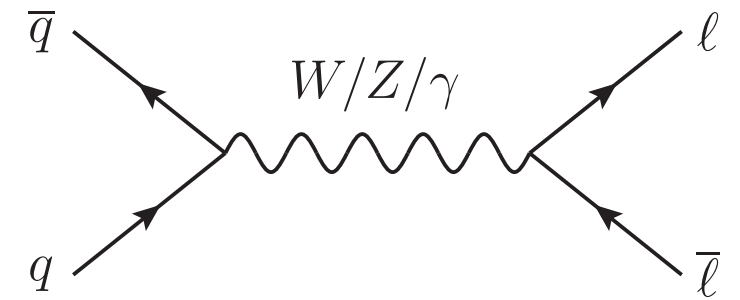
$$0.1 \% \text{ at } 100 \text{ GeV} \xrightarrow{\text{LHC energy}} 10 \% \text{ at } 1 \text{ TeV}$$

LEP energy *LHC energy*

Proof of Principle: Di-lepton DY

Drell-Yan production ($l^+ l^-$ or $l\nu$)

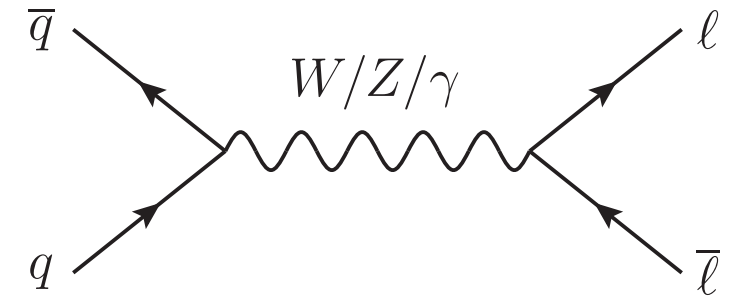
- ▶ large cross section \rightarrow good statistics
- ▶ small theory and exp. systematic uncertainty



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Simple BSM effects: oblique parameters

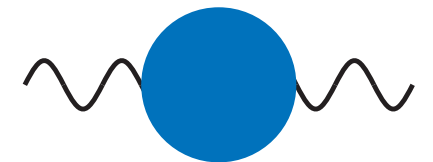
- ◆ Deformation of the gauge propagators from dimension-6 operators

$$\frac{gg'\hat{S}}{16m_W^2} (H^\dagger \sigma^a H) W_{\mu\nu}^a B^{\mu\nu}$$

$$-\frac{g^2\hat{T}}{2m_W^2} |H^\dagger D_\mu H|^2$$

$$-\frac{W}{4m_W^2} (D_\rho W_{\mu\nu}^a)^2$$

$$-\frac{Y}{4m_W^2} (\partial_\rho B_{\mu\nu})^2$$

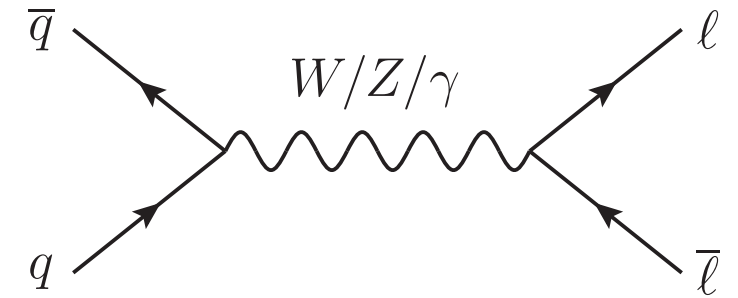


→ **LEP** bounds at the **0.1% level**

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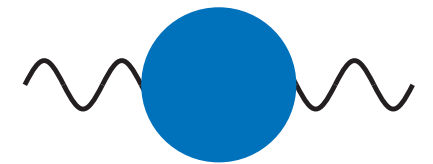
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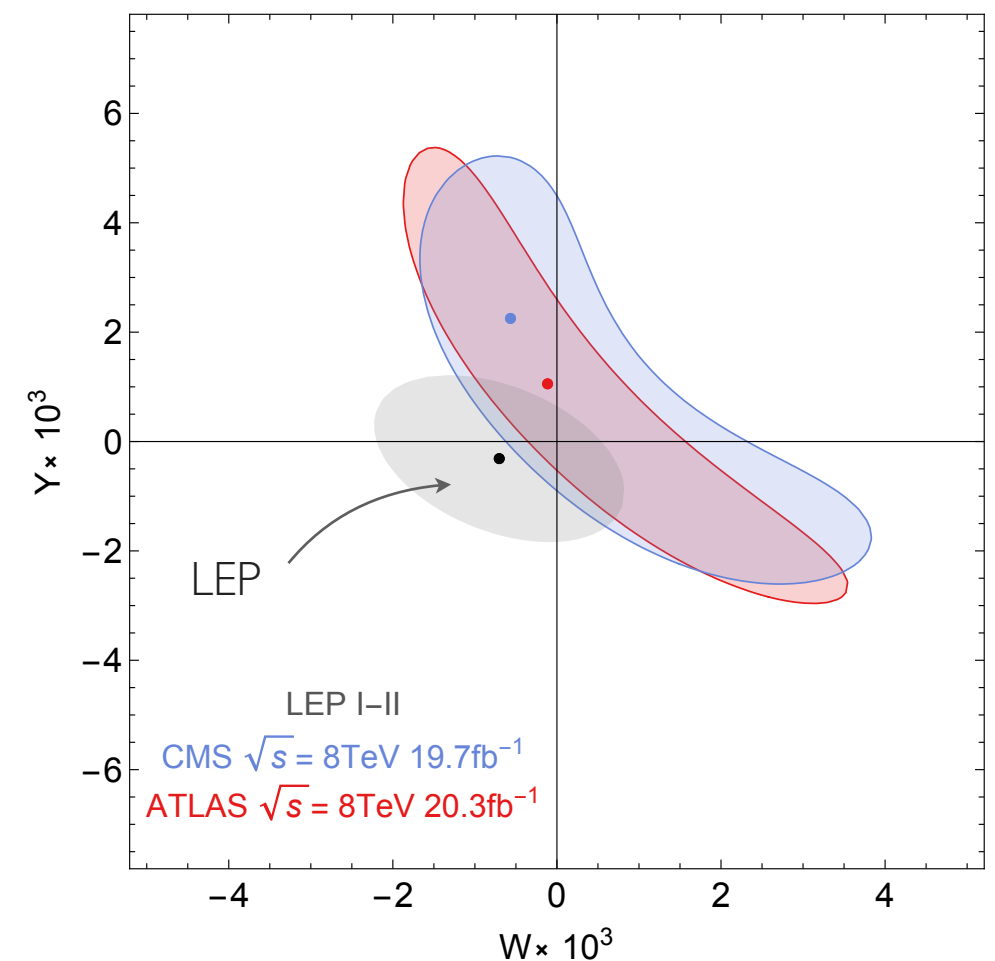
→ **LEP** bounds at the **0.1% level**

induce quadratic growth with energy

Oblique parameters

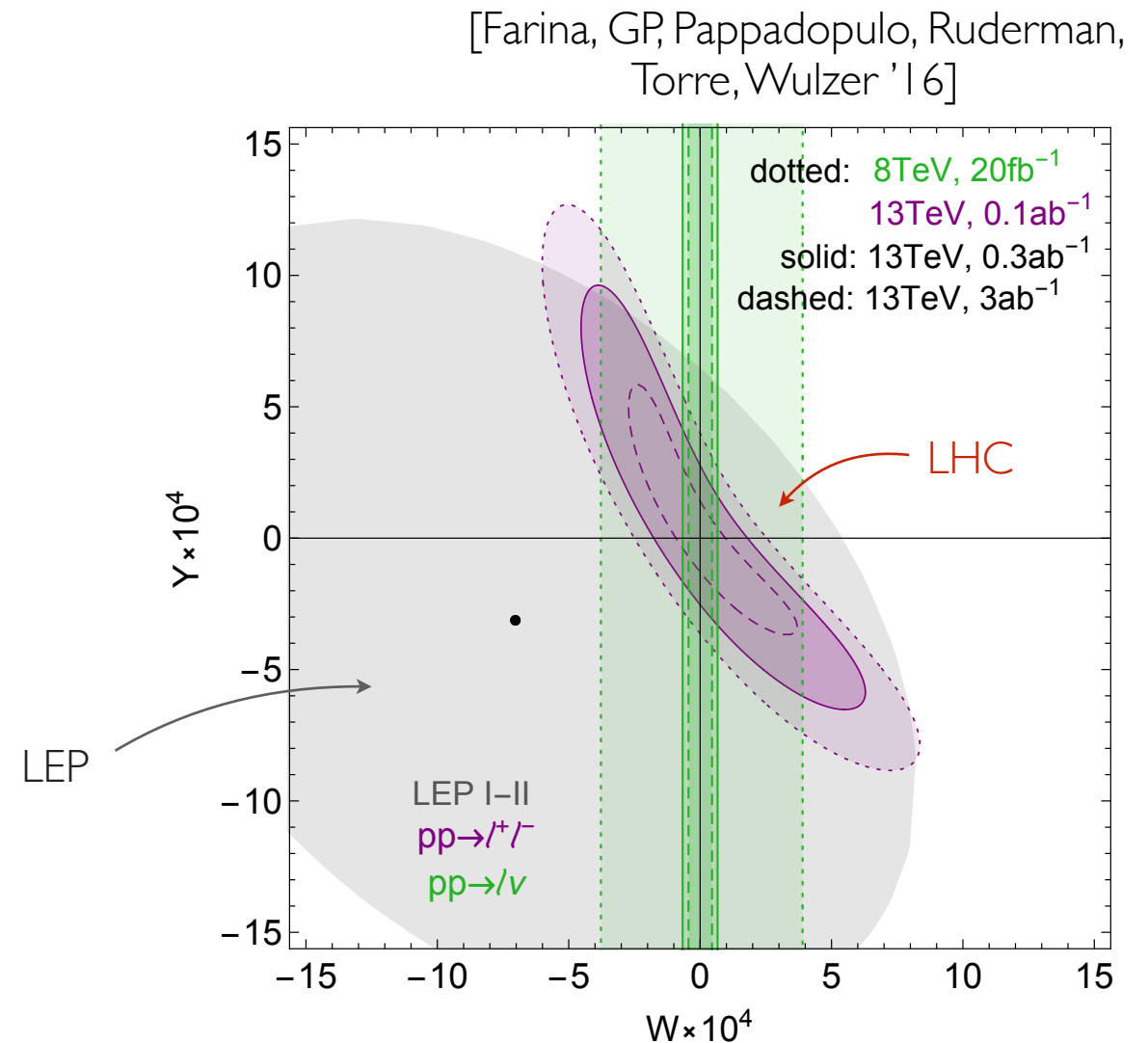
- ◆ **LHC** can significantly **surpass LEP** sensitivity on W and Y !
 - ▶ 8 TeV runs competitive with LEP

[Farina, GP, Pappadopulo, Ruderman, Torre, Wulzer '16]



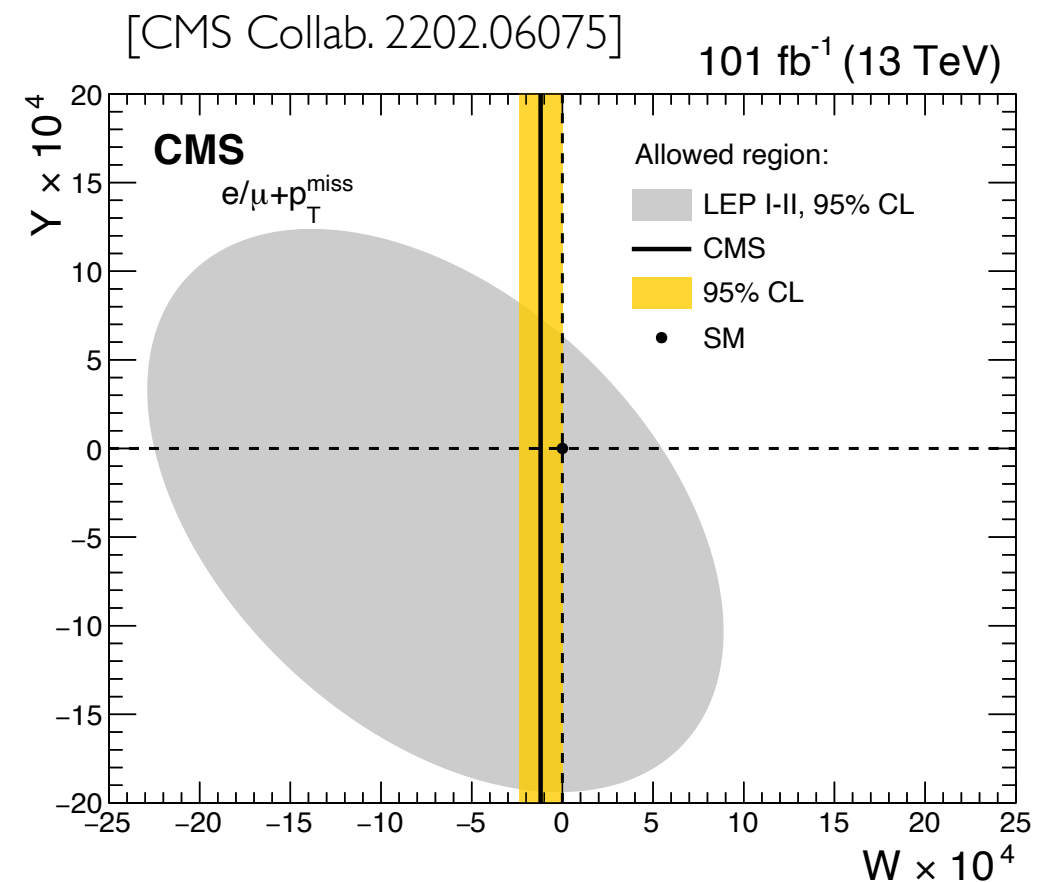
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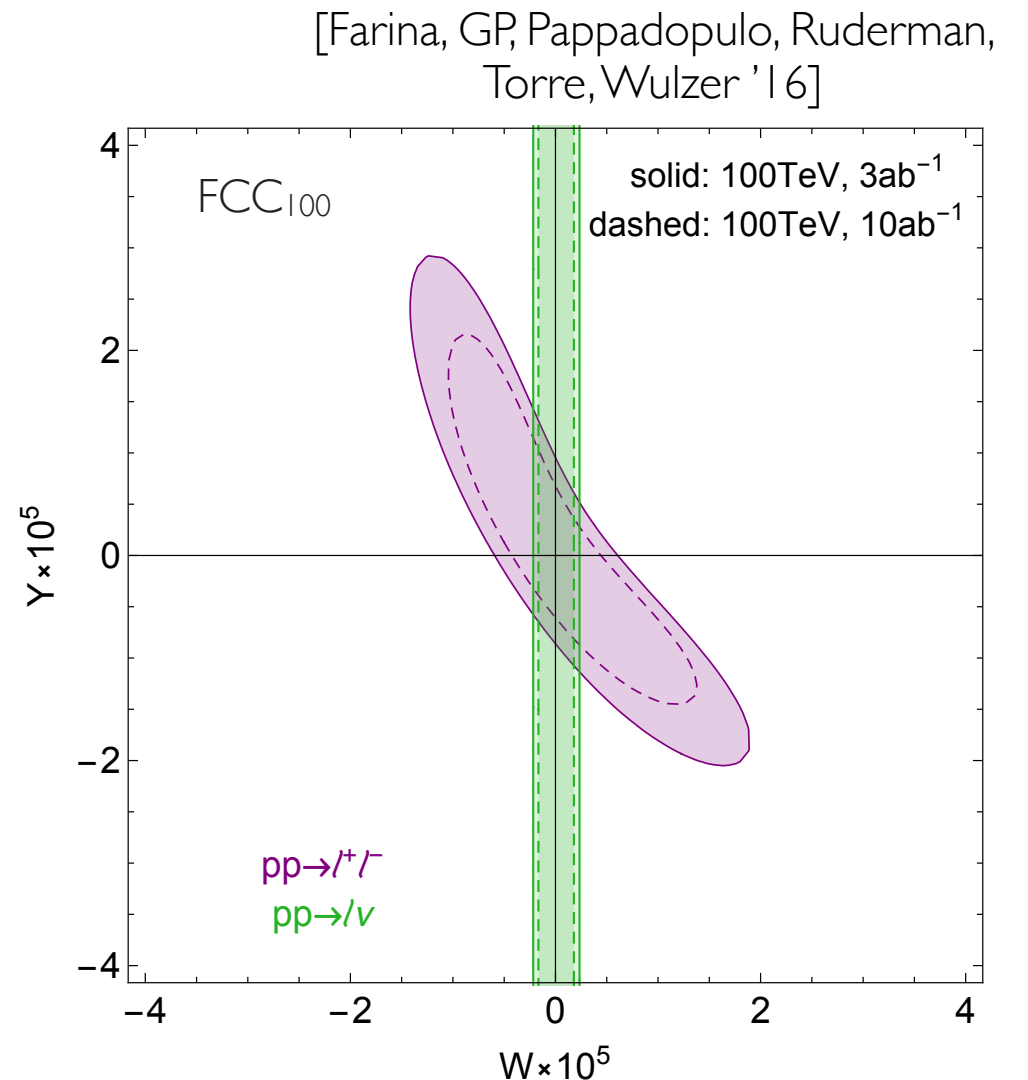
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 - ▶ 8 TeV runs competitive with LEP
 - ▶ high-luminosity 13 TeV will improve the bounds by one order of magnitude
- ◆ Future high-energy hadron colliders can tighten further the bounds
 - ▶ FCC₁₀₀ can reach 10^{-5} precision



Comparison with future colliders

Bounds on W and Y at different colliders

	LEP	LHC 13		FCC 100	ILC	TLEP	CEPC	ILC 500	CLIC 1	CLIC 3
luminosity	$2 \times 10^7 Z$	0.3/ab	3/ab	10/ab	$10^9 Z$	$10^{12} Z$	$10^{10} Z$	3/ab	1/ab	1/ab
$W \times 10^4$	[-19, 3]	± 0.7	± 0.45	± 0.02	± 4.2	± 1.2	± 3.6	± 0.3	± 0.5	± 0.15
$Y \times 10^4$	[-17, 4]	± 2.3	± 1.2	± 0.06	± 1.8	± 1.5	± 3.1	± 0.2	$\sim \pm 0.5$	$\sim \pm 0.15$

- ◆ HL-LHC comparable with TLEP
- ◆ FCC₁₀₀ much better than ILC 500 GeV and CLIC 3 TeV

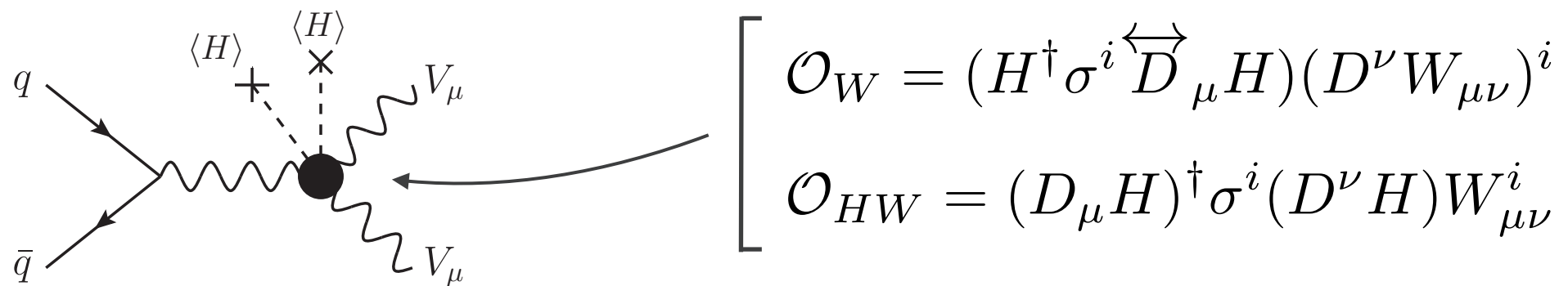
Testing the Higgs dynamics

To **test the Higgs dynamics** we need to probe additional channels

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- ◆ **di-boson** production can probe deviations in the Higgs couplings



More challenging than di-lepton

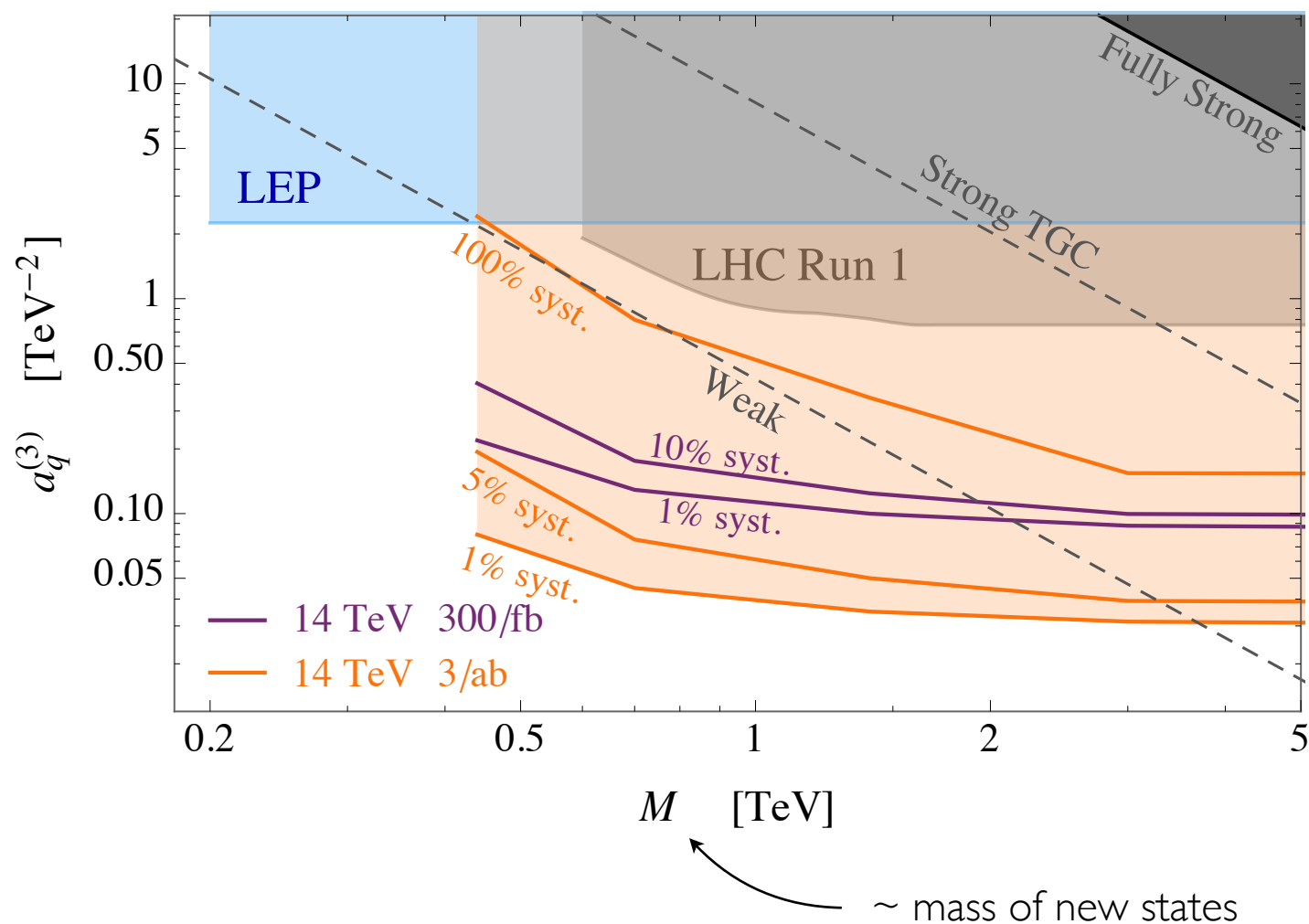
- ▶ energy-growing new physics effects confined to subleading helicity channels (longitudinal) (→ **interference resurrection** via differential measurements)
- ▶ more complex final states

... but **more interesting** → can be used to test a larger set of BSM theories

WZ production: LHC

Estimate of the bounds on $a_q^{(3)} (\bar{q}_L \sigma^a \gamma^\mu q_L) (iH^\dagger \sigma^a \overleftrightarrow{D}_\mu H)$

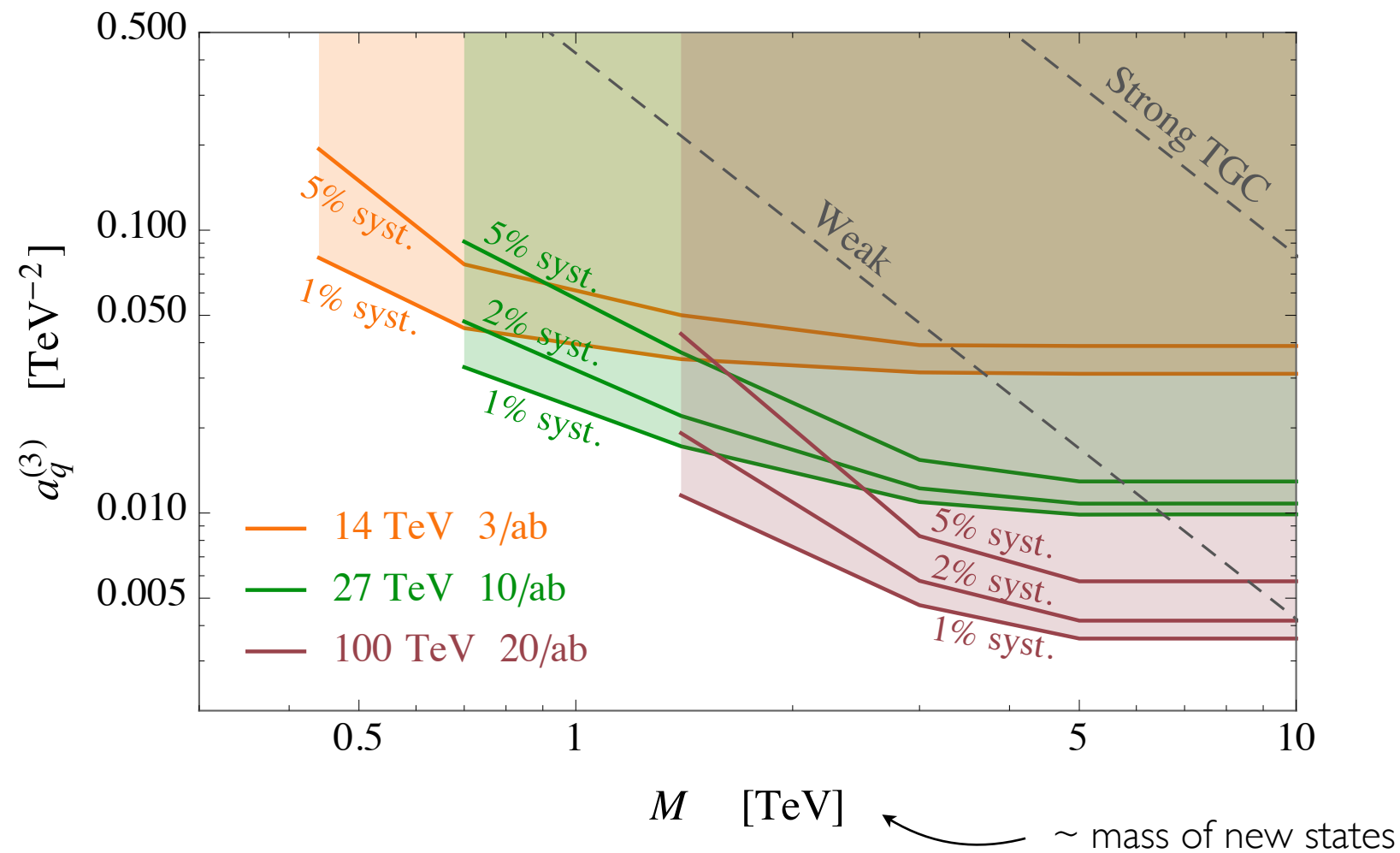
[Franceschini, GP, Pomarol, Riva, Wulzer '17]



- ◆ Non-trivial analysis: longitudinal channels small → exploit transverse zeroes
- ◆ Big improvement with respect to LEP

WZ production: Future colliders

Estimate of the bounds on $a_q^{(3)} (\bar{q}_L \sigma^a \gamma^\mu q_L) (iH^\dagger \sigma^a \overleftrightarrow{D}_\mu H)$



- ◆ additional improvement possible at future colliders
- ◆ reach at FCC-hh comparable with CLIC see [Ellis, Roloff, Sanz, You '17]

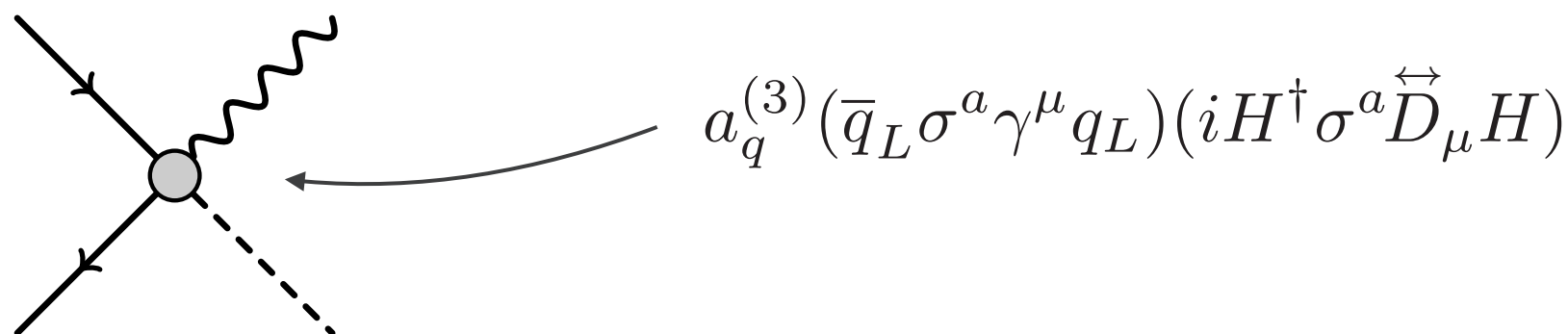
High luminosity and rare channels

High integrated luminosity → **very rare** but **very clean** channels

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High integrated luminosity \rightarrow very rare but very clean channels

Example: VH production



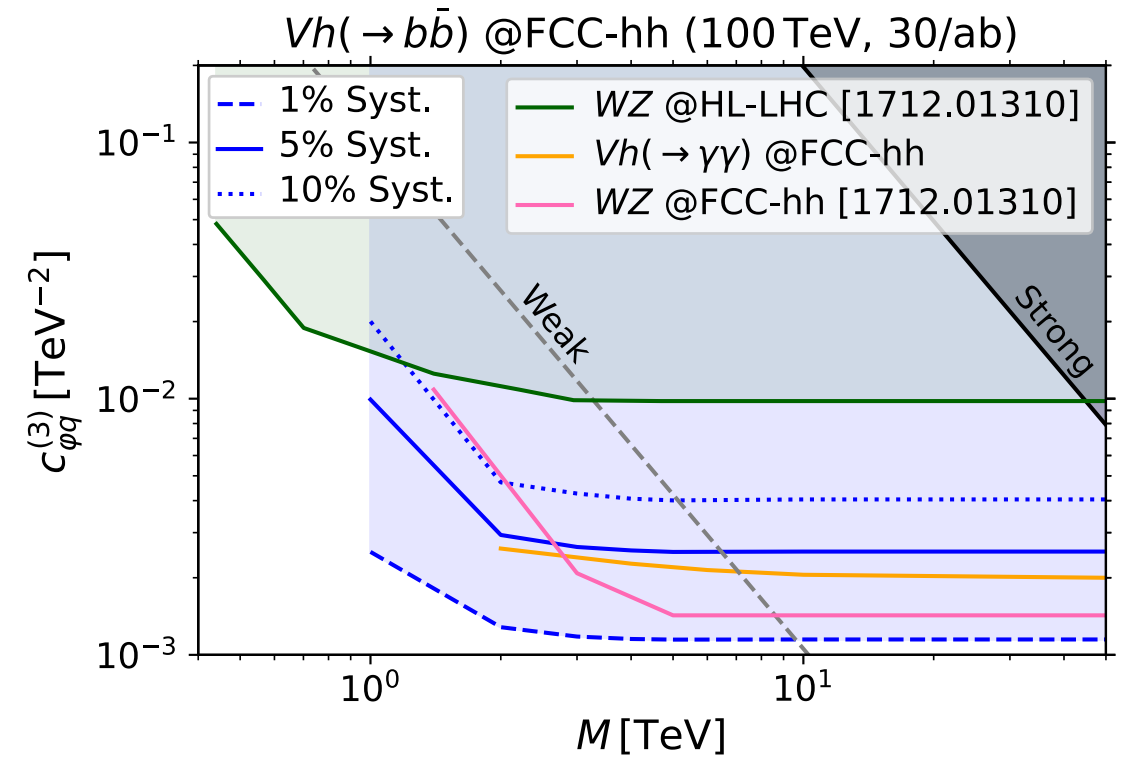
Different decay channels:

- ▶ $H \rightarrow bb$ \rightarrow large cross section, but sizeable background
- ▶ $H \rightarrow \gamma\gamma$ \rightarrow tiny cross section (only accessible at FCC-hh), but very clean

VH at FCC-hh

[Bishara, Englert et al. '22]

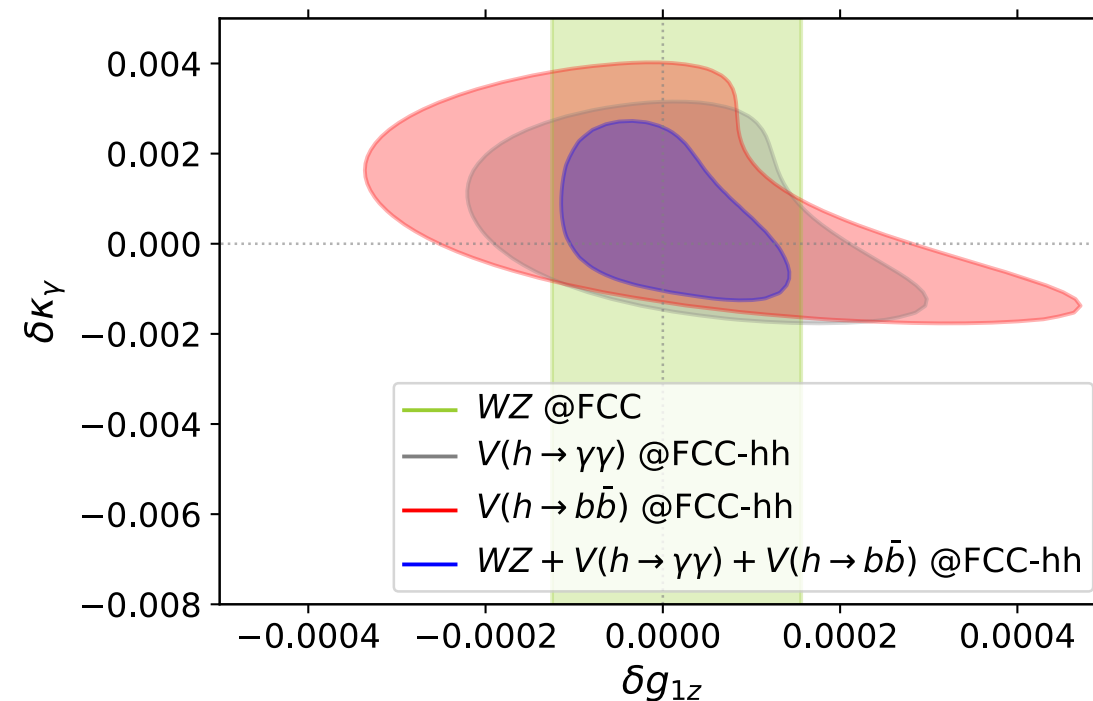
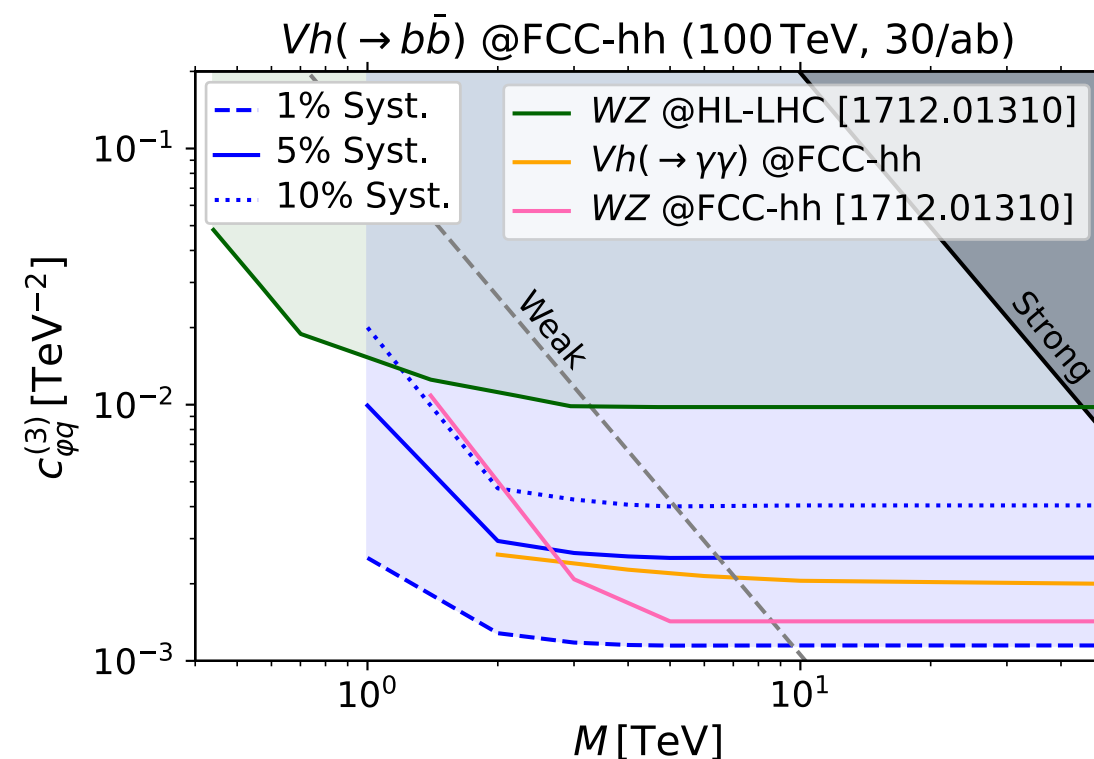
- ◆ $VH(\rightarrow bb)$ and $VH(\rightarrow \gamma\gamma)$ provide similar sensitivity
- ◆ Bounds competitive with WZ



VH at FCC-hh

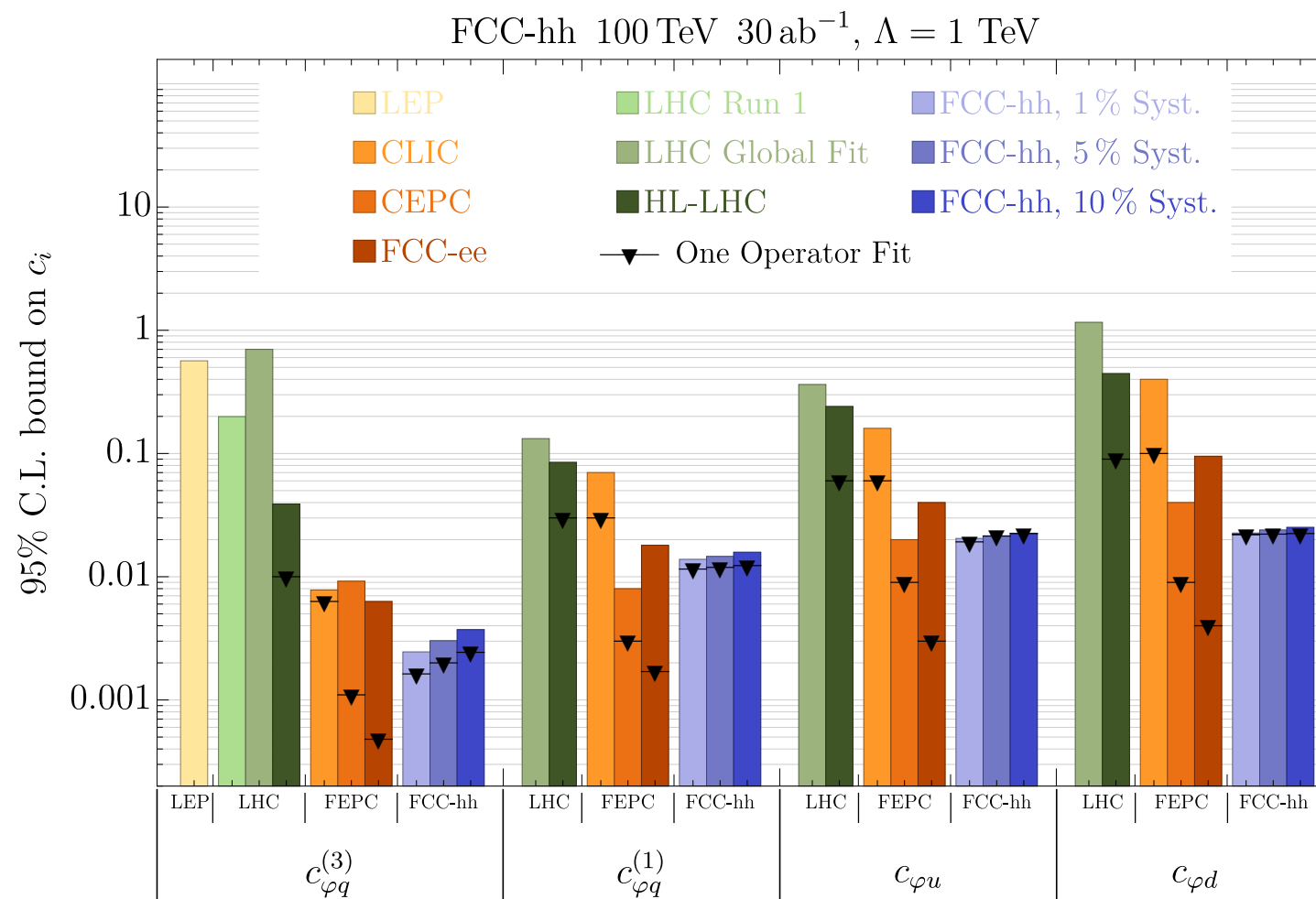
[Bishara, Englert et al. '22]

- ◆ $VH(\rightarrow bb)$ and $VH(\rightarrow \gamma\gamma)$ provide similar sensitivity
- ◆ Bounds competitive with WZ
- ◆ Combination of the two channels can significantly improve the bounds



VH at FCC-hh

[Bishara, De Curtis et al. '20]



FCC-hh can match (or surpass) sensitivity at e^+e^- colliders

Higgs “pole” measurements

Low-energy e^+e^- colliders

Low-energy e^+e^- colliders can test several Higgs “pole” properties

- ▶ determination of **absolute normalization of couplings**
(via recoil method $HZ(\rightarrow \ell^+\ell^-)$)

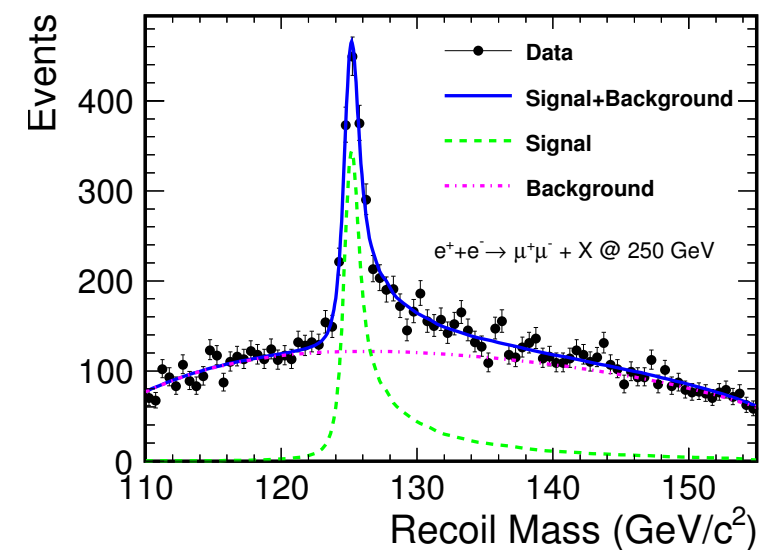
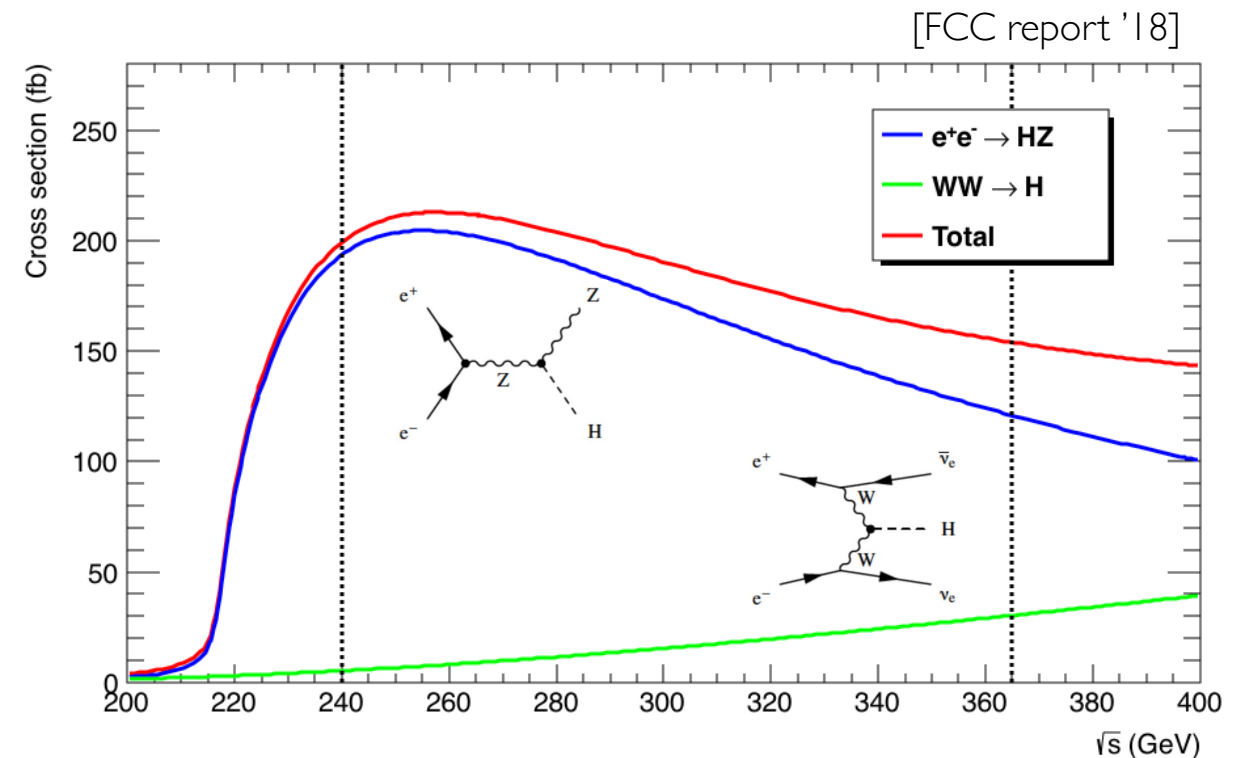
- ▶ sensitivity to **invisible decays**

- ▶ measurement of Higgs **width**

$$\delta\Gamma_H \sim 1\%$$

- ▶ measurement of Higgs **mass**

$$\delta m_H \sim 3 \text{ MeV}$$



Low-energy e^+e^- colliders

Higgs coupling sensitivity

Coupling	HL-LHC	FCC-ee (240–365 GeV) 2 IPs / 4 IPs
κ_W [%]	1.5*	0.43 / 0.33
κ_Z [%]	1.3*	0.17 / 0.14
κ_g [%]	2*	0.90 / 0.77
κ_γ [%]	1.6*	1.3 / 1.2
$\kappa_{Z\gamma}$ [%]	10*	10 / 10
κ_c [%]	–	1.3 / 1.1
κ_t [%]	3.2*	3.1 / 3.1
κ_b [%]	2.5*	0.64 / 0.56
κ_μ [%]	4.4*	3.9 / 3.7
κ_τ [%]	1.6*	0.66 / 0.55
BR _{inv} (<%, 95% CL)	1.9*	0.20 / 0.15
BR _{unt} (<%, 95% CL)	4*	1.0 / 0.88




[Table from mid-term report, from C. Grojean, Corfu '24]

- ▶ Model-independent measurement of linear Higgs couplings
- ▶ Significant improvement with respect to HL-LHC in

$$g_{HZZ}^{eff}, g_{HWW}^{eff}, g_{Hgg}^{eff}, g_{Hbb}^{eff}, g_{Hcc}^{eff}, g_{H\tau\tau}^{eff}$$

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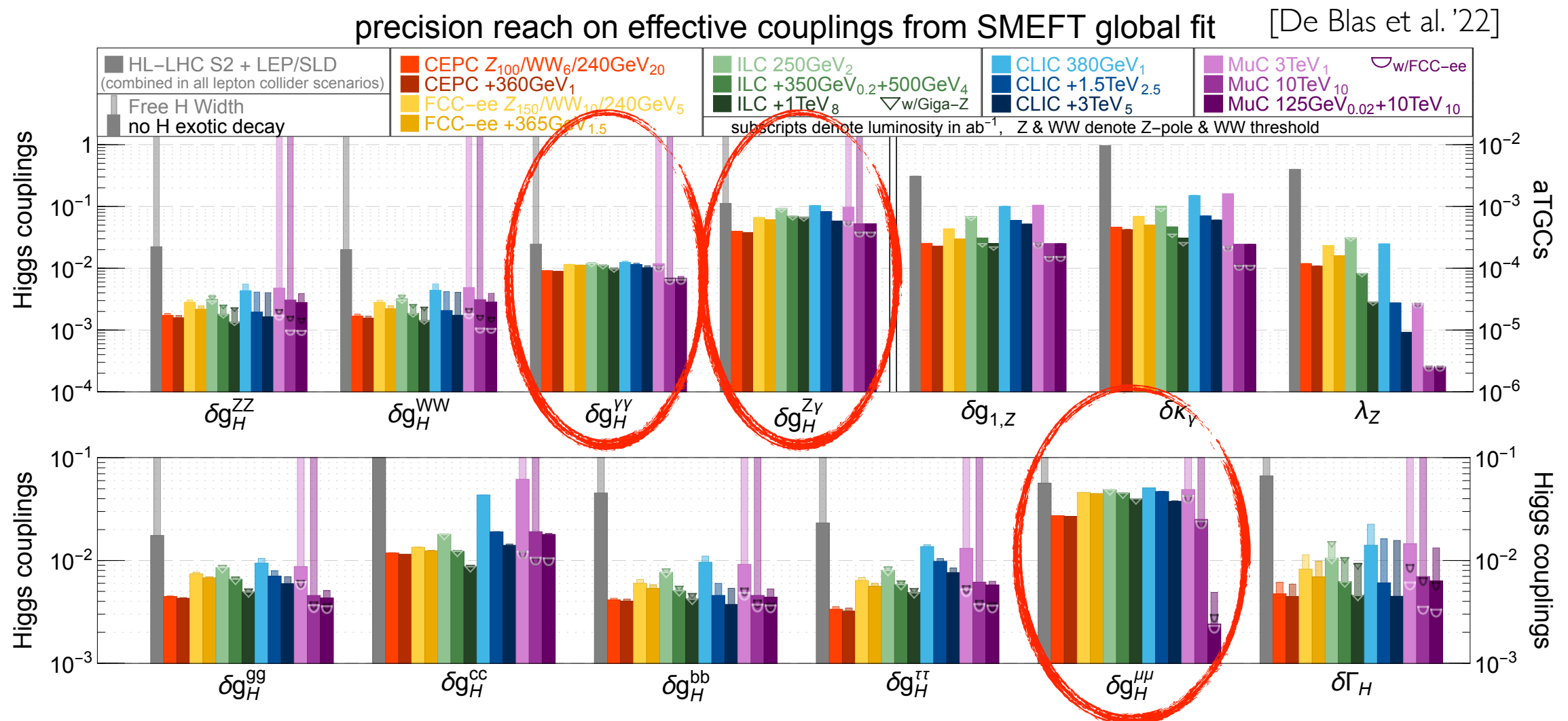
- ▶ **Exception:** decay channels with low BR

$$g_{H\gamma\gamma}^{eff}, g_{H\mu\mu}^{eff}, g_{HZ\gamma}^{eff}$$

Muon collider

A muon collider can improve the determination of some couplings

- ▶ improvement in $g_{H\gamma\gamma}^{eff}$ (and $g_{HZ\gamma}^{eff}$) with 10 TeV (and 125 GeV) run
- ▶ improvement in $g_{H\mu\mu}^{eff}$ with 10 TeV run; excellent determination with 125 GeV run

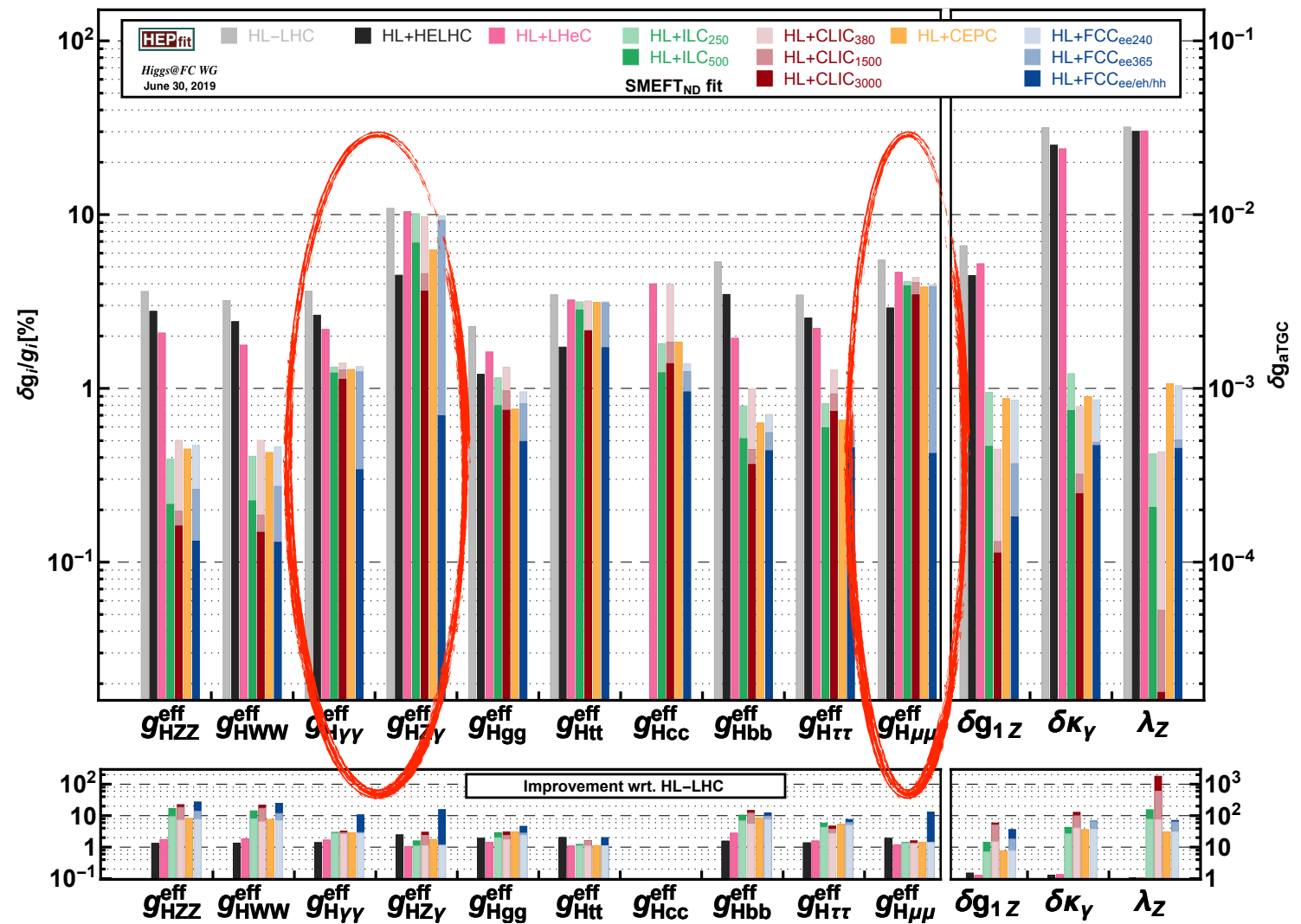


High-energy hadron collider

FCC-hh can test $g_{H\gamma\gamma}^{eff}$, $g_{H\mu\mu}^{eff}$, $g_{HZ\gamma}^{eff}$
with high precision

$g_{H\gamma\gamma}^{eff} \rightarrow 0.4\%$
 $g_{H\mu\mu}^{eff} \rightarrow 0.7\%$
 $g_{HZ\gamma}^{eff} \rightarrow 0.9\%$

[De Blas et al. '22]



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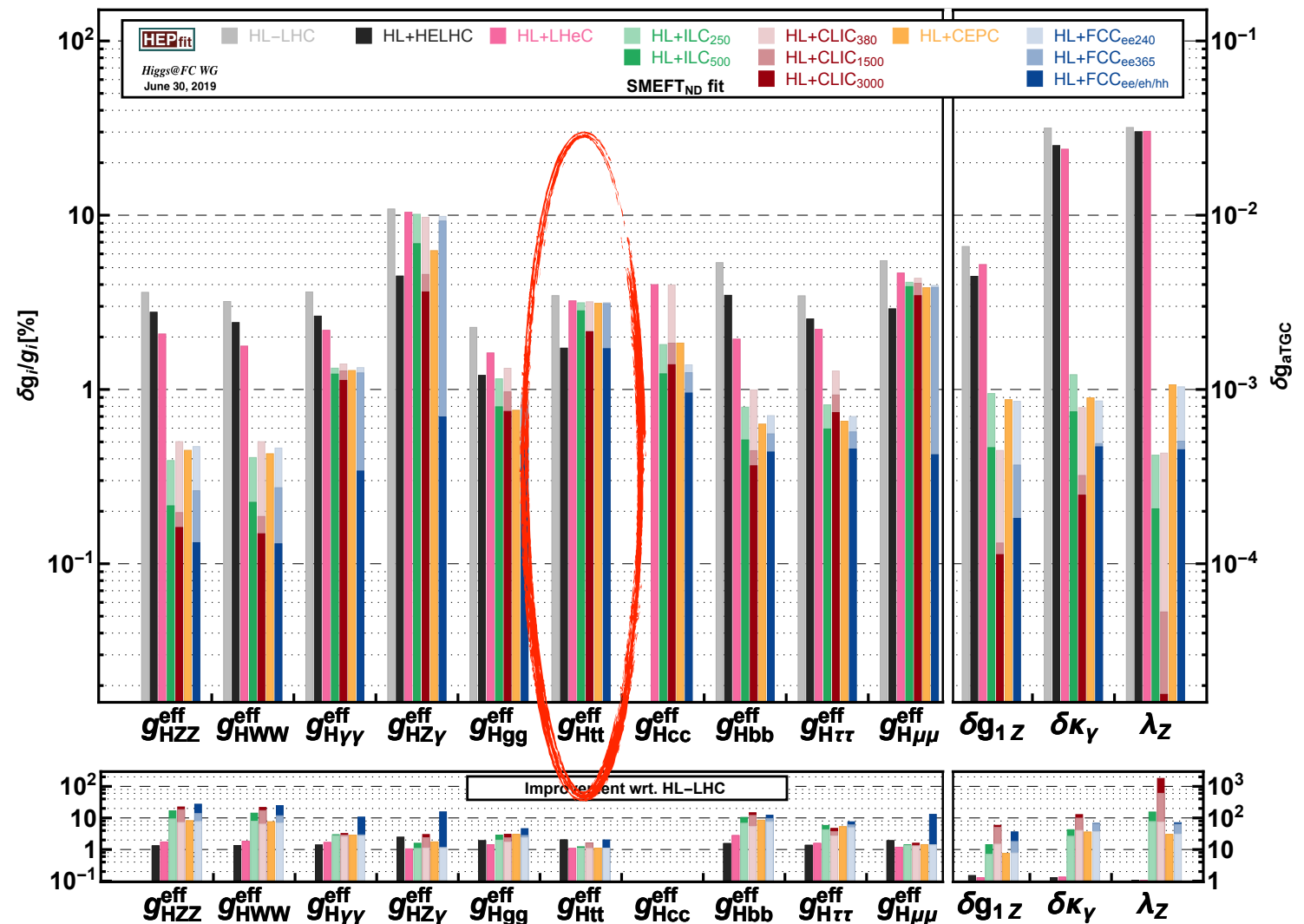
$$g_{HZ\gamma}^{eff} \longrightarrow 0.9\%$$

FCC-hh can improve the
measurement of the top Yukawa

$$g_{Htt}^{eff} \longrightarrow 1\%$$

(improvement also possible at HE-LHC and CLIC 3TeV)

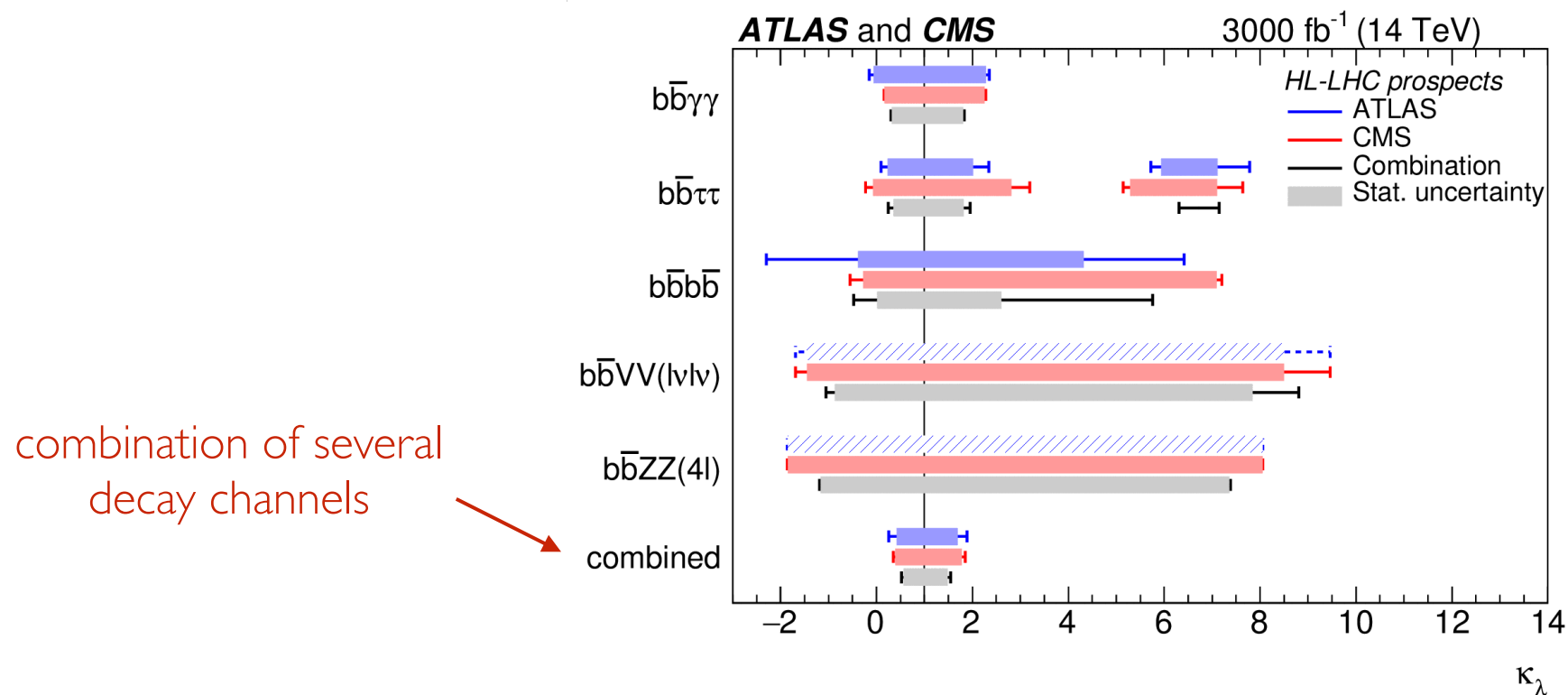
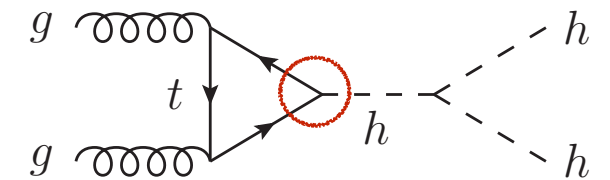
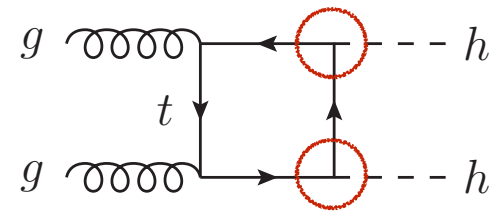
[De Blas et al. '22]



Higgs trilinear coupling

High-luminosity LHC

Main sensitivity from $gg \rightarrow HH$



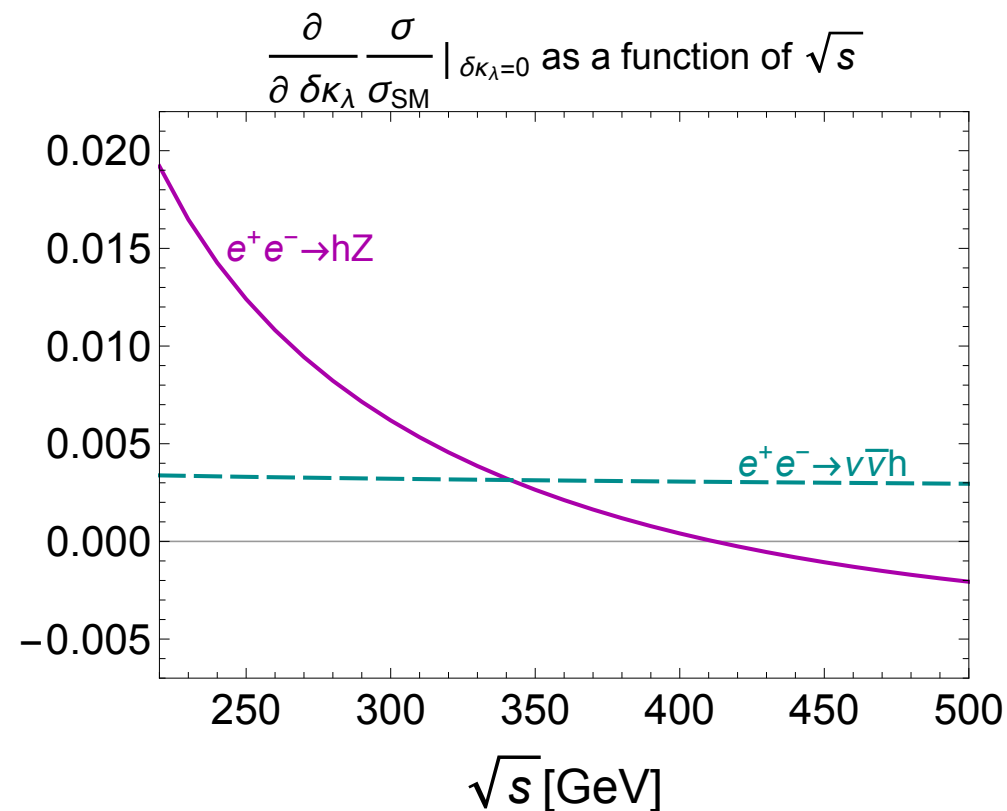
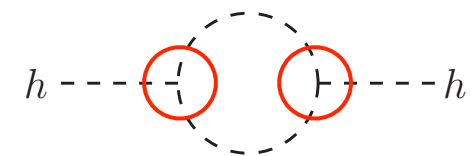
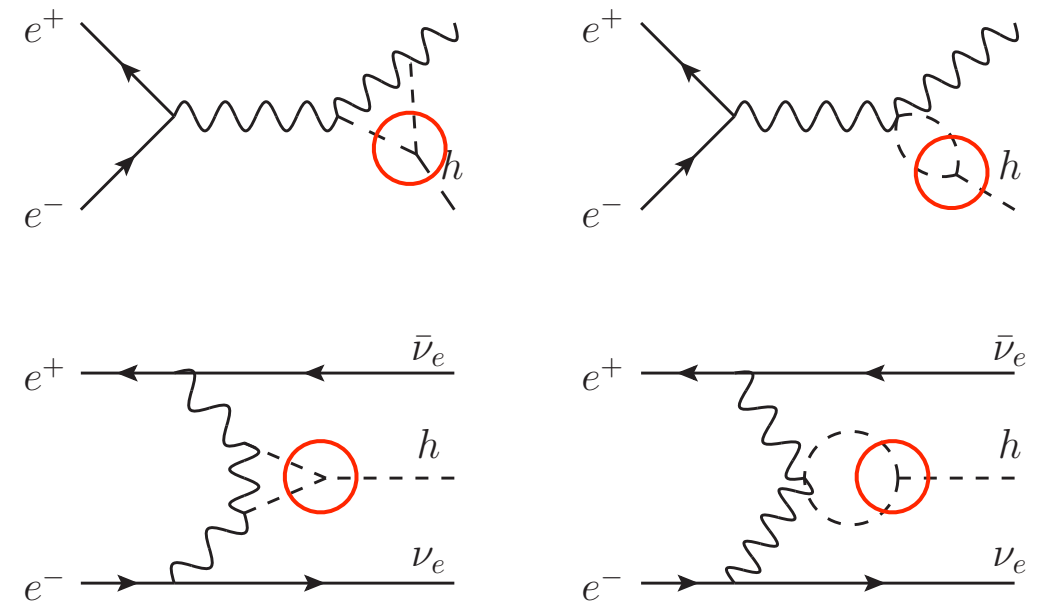
◆ HL-LHC can test the Higgs trilinear with $O(50\%)$ precision [See Di Micco et al. '19]

$$-0.43 \leq \delta\kappa_\lambda \leq 0.5 \quad \text{at} \quad 68\% \text{ C.L.}$$

Low-energy e^+e^- colliders

Higgs self-interaction can be probed indirectly through one-loop corrections to **single-Higgs processes**

[McCullough '13]



Good sensitivity at low energy in HZ (and $\nu\bar{\nu}H$) channels

Low-energy e^+e^- colliders

Expected precision from 1-parameter fit (1σ bounds)

collider	1-parameter
CEPC 240	18%
FCC-ee 240	21%
FCC-ee 240/365	21%
FCC-ee (4IP)	15%
ILC 250	36%
ILC 250/500	32%
ILC 250/500/1000	29%
CLIC 380	117%
CLIC 380/1500	72%
CLIC 380/1500/3000	49%

CEPC and FCC-ee
provide fair
sensitivity

[Di Micco et al. '19]

collider	Full \mathcal{L} [ab^{-1}]
CEPC 240	5.6
FCC-ee 240	5.0
FCC-ee 365	1.5
FCC-ee (4IP)	12.0 + 5.5
ILC 250	2.0
ILC 500	4.0
ILC 1000	8.0
CLIC 380	1.0
CLIC 1500	2.5
CLIC 3000	5.0

Low-energy e^+e^- colliders

Expected precision from global fit (1σ bounds)

collider	1-parameter	full SMEFT
CEPC 240	18%	-
FCC-ee 240	21%	-
FCC-ee 240/365	21%	44%
FCC-ee (4IP)	15%	27%
ILC 250	36%	-
ILC 250/500	32%	58%
ILC 250/500/1000	29%	52%
CLIC 380	117%	-
CLIC 380/1500	72%	-
CLIC 380/1500/3000	49%	-

← runs at single energy
do not provide
significant bounds

collider	Full \mathcal{L} [ab^{-1}]
CECP 240	5.6
FCC-ee 240	5.0
FCC-ee 365	1.5
FCC-ee (4IP)	12.0 + 5.5
ILC 250	2.0
ILC 500	4.0
ILC 1000	8.0
CLIC 380	1.0
CLIC 1500	2.5
CLIC 3000	5.0

[Di Micco et al. '19]

Low-energy e^+e^- colliders

Expected precision from global fit (1σ bounds)

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CEPC 240	18%	-
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FCC-ee 240/365	21%	44%
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ILC 250	36%	-
ILC 250/500	32%	58%
ILC 250/500/1000	29%	52%
CLIC 380	117%	-
CLIC 380/1500	72%	-
CLIC 380/1500/3000	49%	-

← runs at single energy
do not provide significant bounds

←

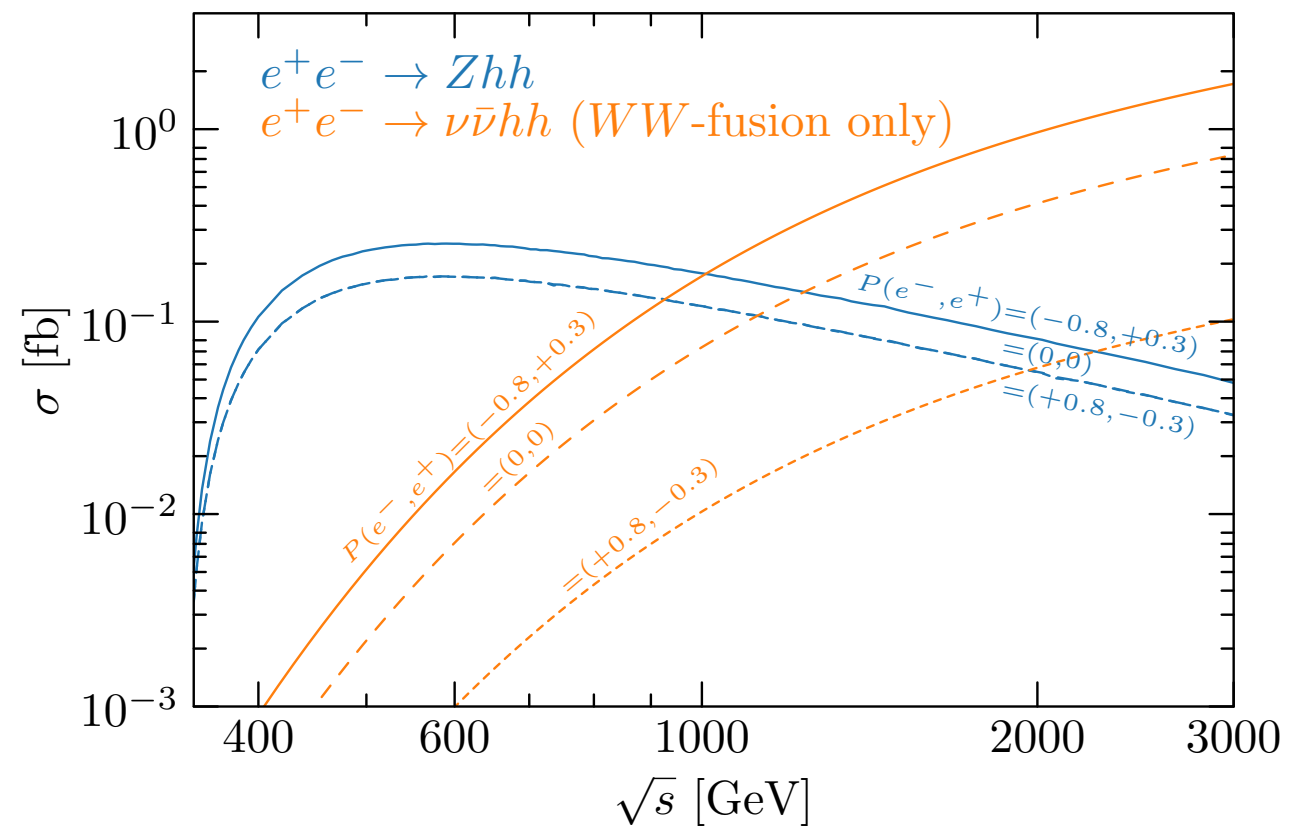
← determination can reach 27% at FCC-ee with 4 interaction points

collider	Full \mathcal{L} [ab^{-1}]
CECP 240	5.6
FCC-ee 240	5.0
FCC-ee 365	1.5
FCC-ee (4IP)	12.0 + 5.5
ILC 250	2.0
ILC 500	4.0
ILC 1000	8.0
CLIC 380	1.0
CLIC 1500	2.5
CLIC 3000	5.0

[Di Micco et al. '19]

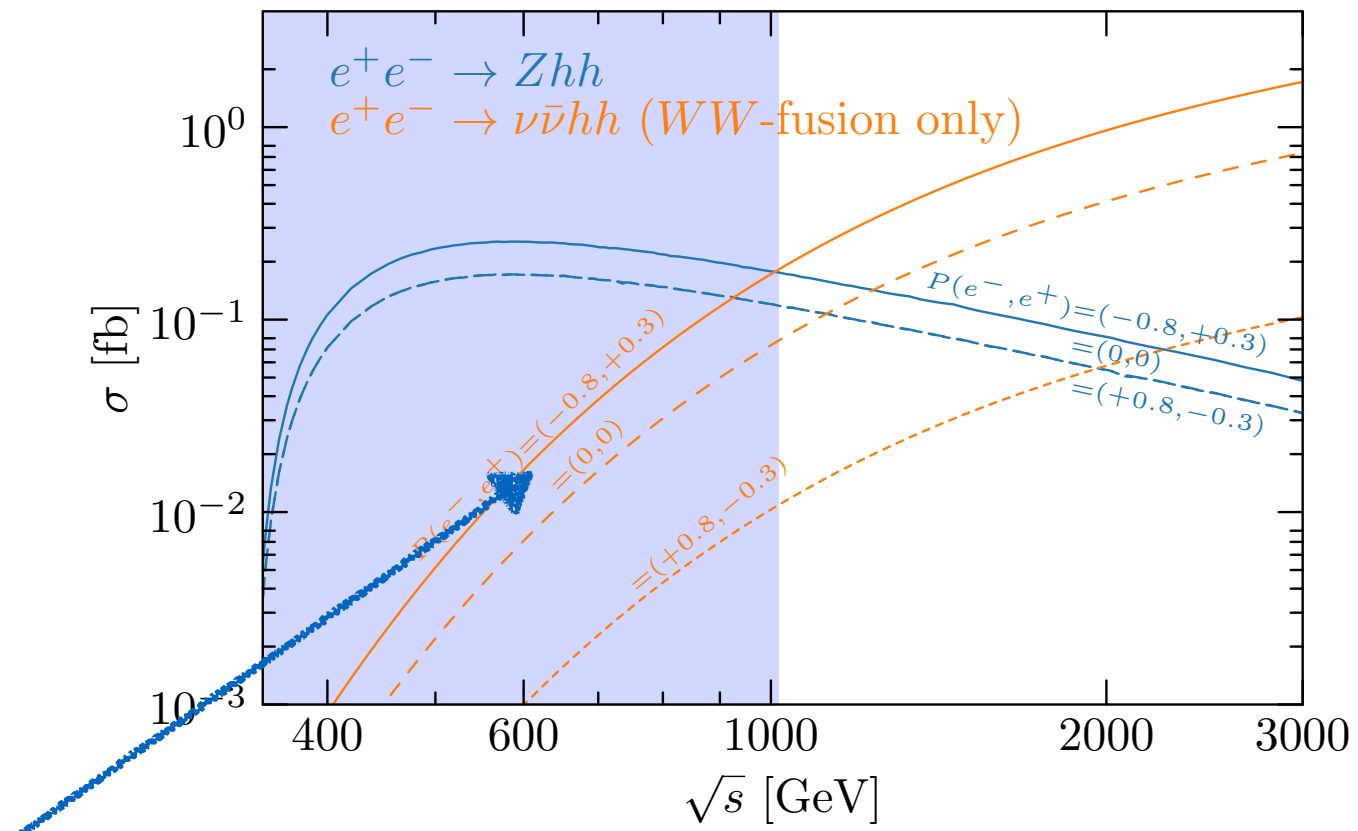
High-energy e^+e^- colliders

Two main channels
 ZHH and $\nu\bar{\nu}HH$



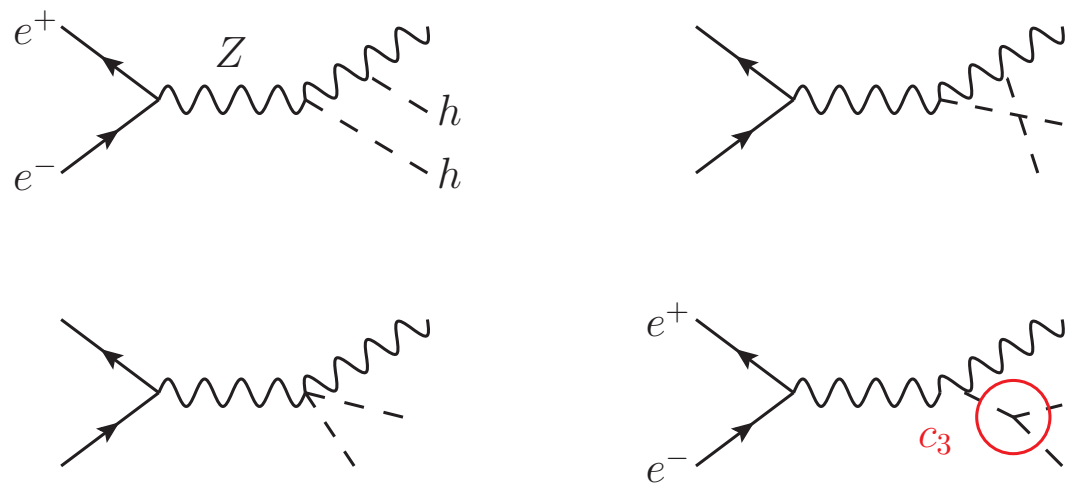
High-energy e^+e^- colliders

Two main channels
 ZHH and $\nu\bar{\nu}HH$



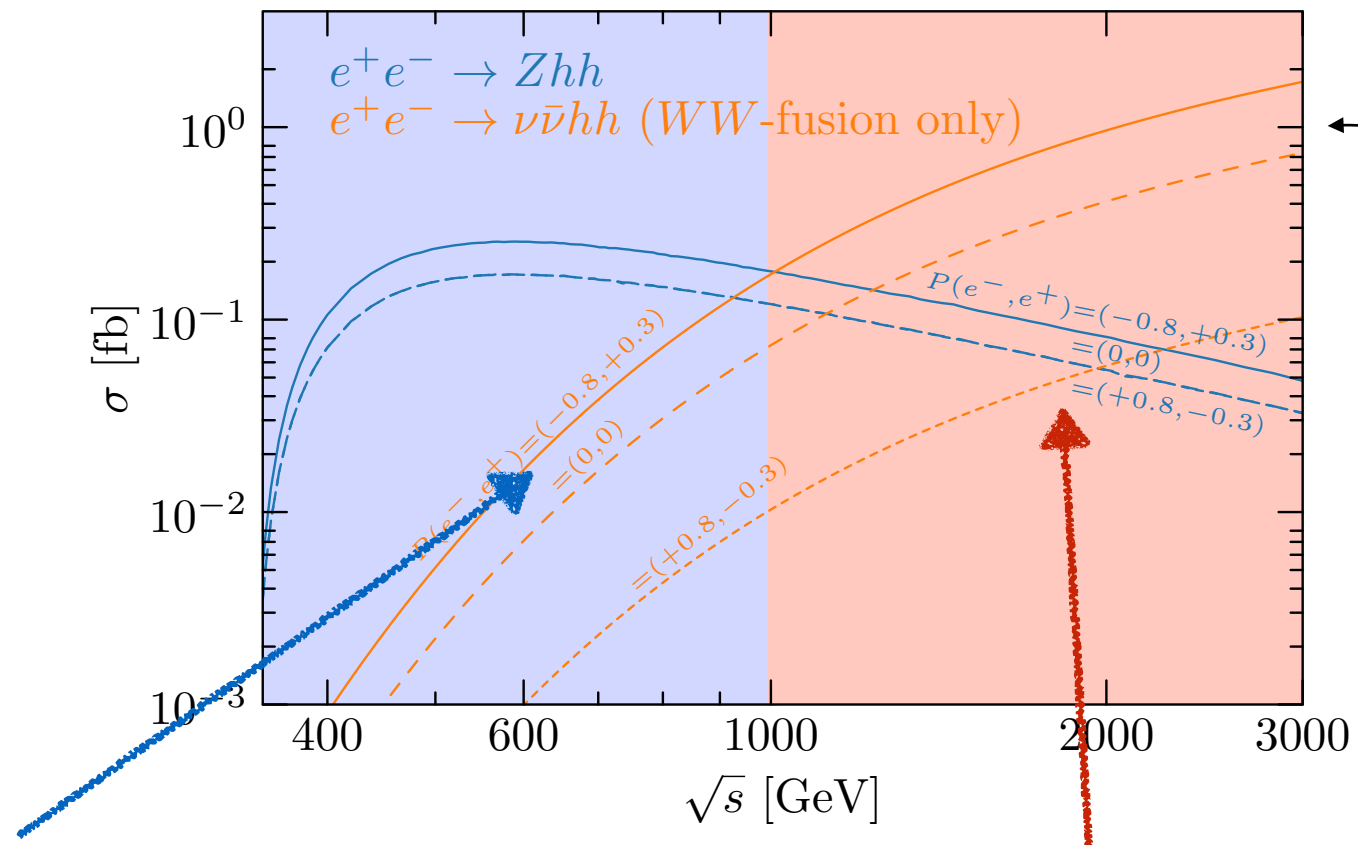
Double Higgs-strahlung (DHS)

dominant below 1 TeV



High-energy e^+e^- colliders

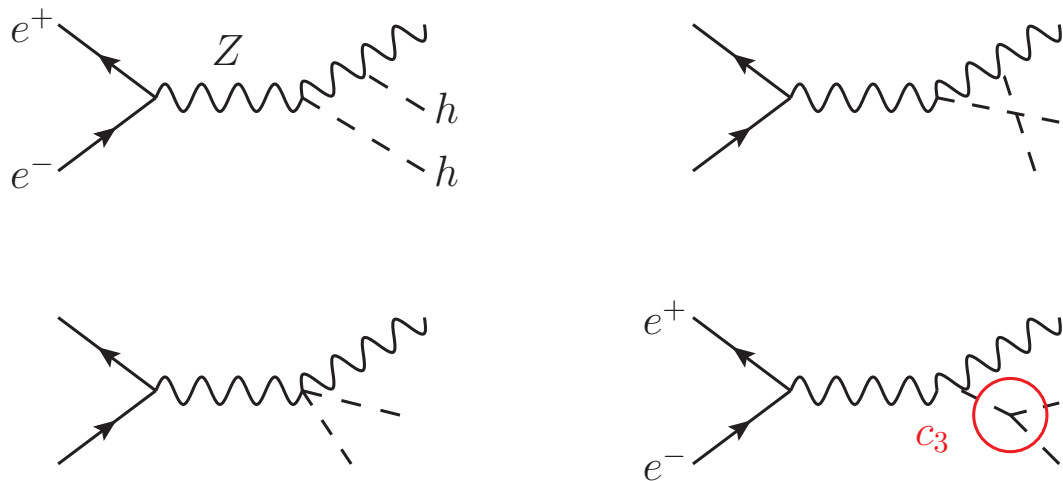
Two main channels
 ZHH and $\nu\bar{\nu}HH$



beam polarization
can enhance
cross-section

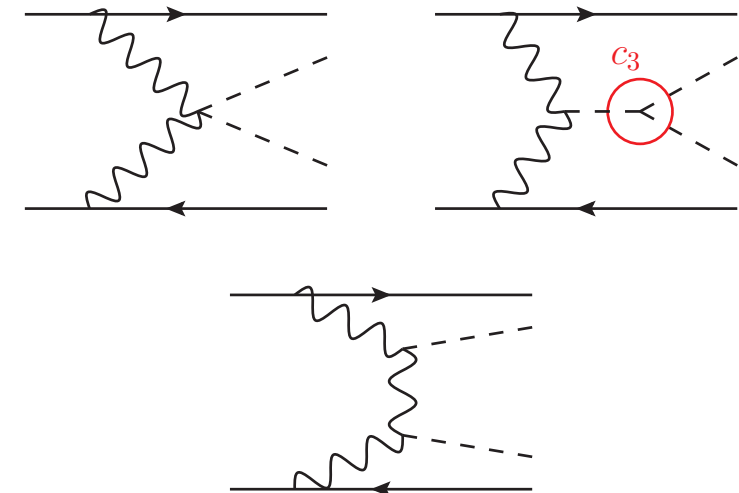
Double Higgs-strahlung (DHS)

dominant below 1 TeV



Vector Boson Fusion (VBF)

dominant above 1 TeV



Precision reach at ILC and CLIC

Expected precision from HH production channels
(1σ bounds)

collider	excl. from HH
HL-LHC	50%
ILC 500	27%
ILC 1000	10%
CLIC 1500	36%
CLIC 3000	[-7%, 11%]

Can reach the 10% threshold

FCC-hh

Exclusive fit on $\delta\kappa_\lambda$

$$\sqrt{s} = 100 \text{ TeV} \quad \mathcal{L} = 30 \text{ ab}^{-1}$$

	$b\bar{b}\gamma\gamma$	$b\bar{b}\tau^+\tau^-$	$b\bar{b}ZZ^* (4\ell)$	$b\bar{b}WW^* (2j\ell\nu)$	$b\bar{b}b\bar{b} + \text{jet}$
$\delta\kappa_\lambda$	6%	8%	14%	40%	30%

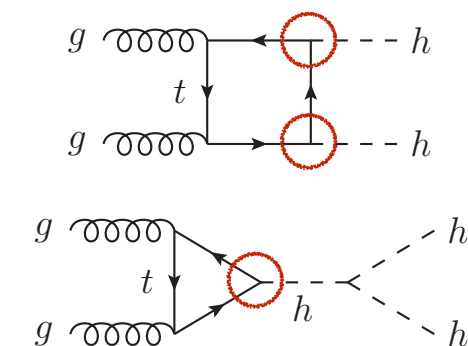
[Di Micco et al. '19]

- ▶ precision likely to be limited by systematics
(theory systematics dominant for $\Delta_S \gtrsim 2.5\%$, leading to $\delta\kappa_\lambda \simeq 2\Delta_S$)

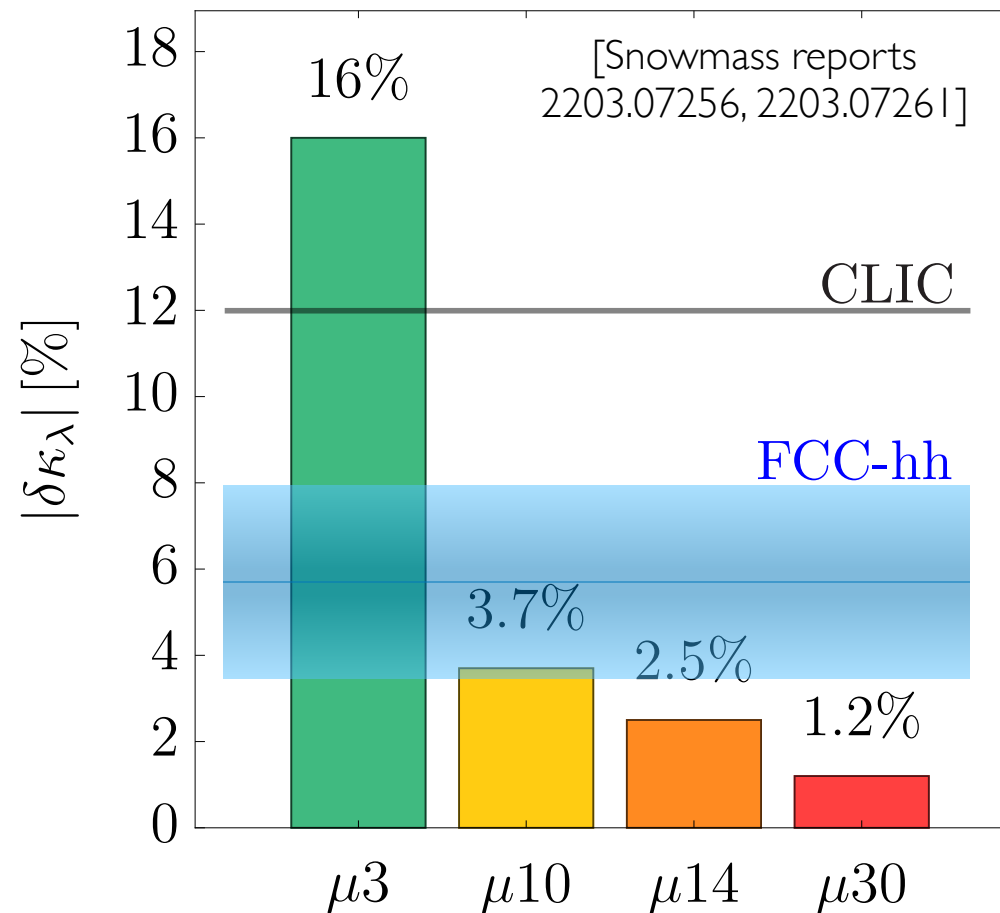
- ▶ ultimate FCC-hh reach in the 3.4 - 7.8% range

[Mangano et al. 2004.03505]

- ▶ global fit could affect the prediction
(strong dependence on top Yukawa coupling)



Muon collider



energy	Full \mathcal{L} [ab^{-1}]
3 TeV	≈ 2
10 TeV	10
14 TeV	≈ 20
30 TeV	90

- ▶ High-energy muon collider can be competitive with FCC-hh

Conclusions and Outlook

Conclusions and outlook

Precision measurements can provide promising information at HL-LHC and future colliders

- ▶ complements direct searches
- ▶ can extend reach beyond collider energy threshold (eg. e^+e^- machines)

Can be performed both at **lepton** and at **hadron colliders**

Challenging aspects:

- ▶ good statistics (especially in the high-energy tails)
- ▶ good control on theoretical and experimental systematics

Conclusions and outlook

Crucial aspect: approaching **optimality**

- ▶ important to fully exploit data and reach maximal sensitivity

Challenging aspects:

- ▶ huge amount of data
- ▶ information 'hidden' in high-dimensional kinematic distributions
- ▶ need for simultaneous fit of several quantities
(eg. PDF determination together with fit of SMEFT operators)

Promising approaches through **machine learning**