



DANIEL WYLER FEST

**ZPW2025**

Particle Physics from Low to High Energies

University of Zurich – January 7, 2025

# The Power of EFTs

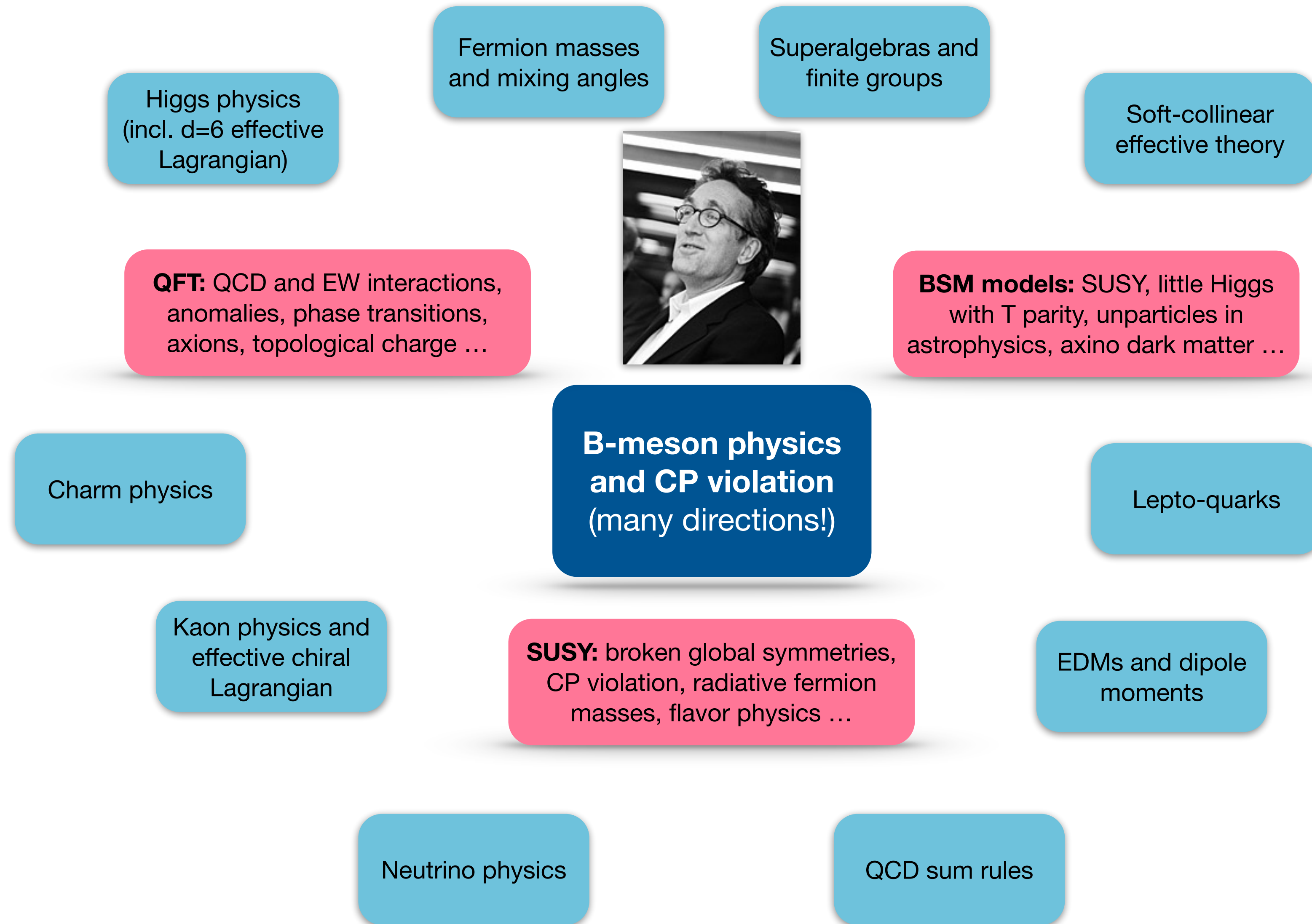
## From HQET to SCET and beyond

Matthias Neubert, Johannes Gutenberg University Mainz

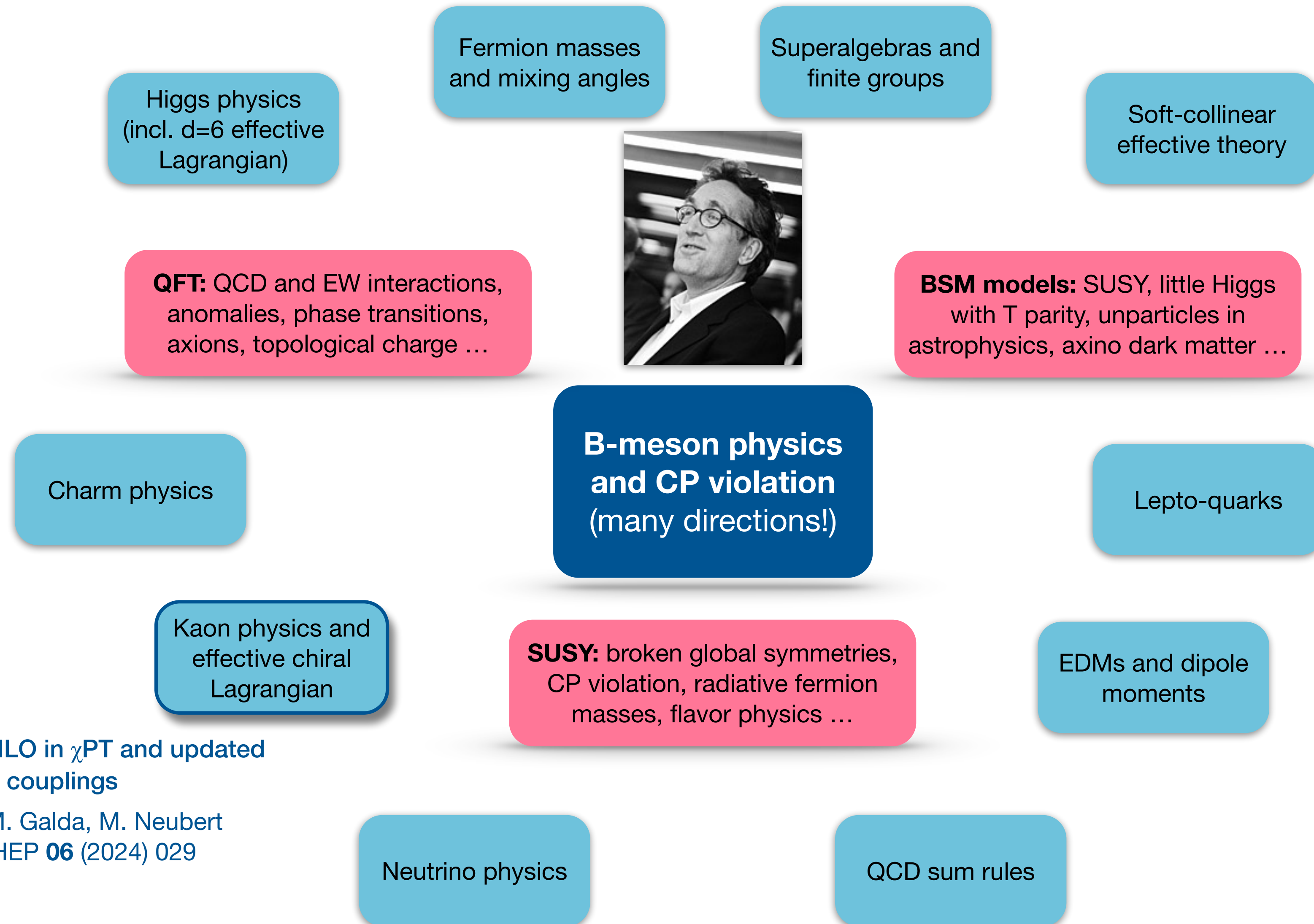




# An oeuvre of enormous breadth and impact



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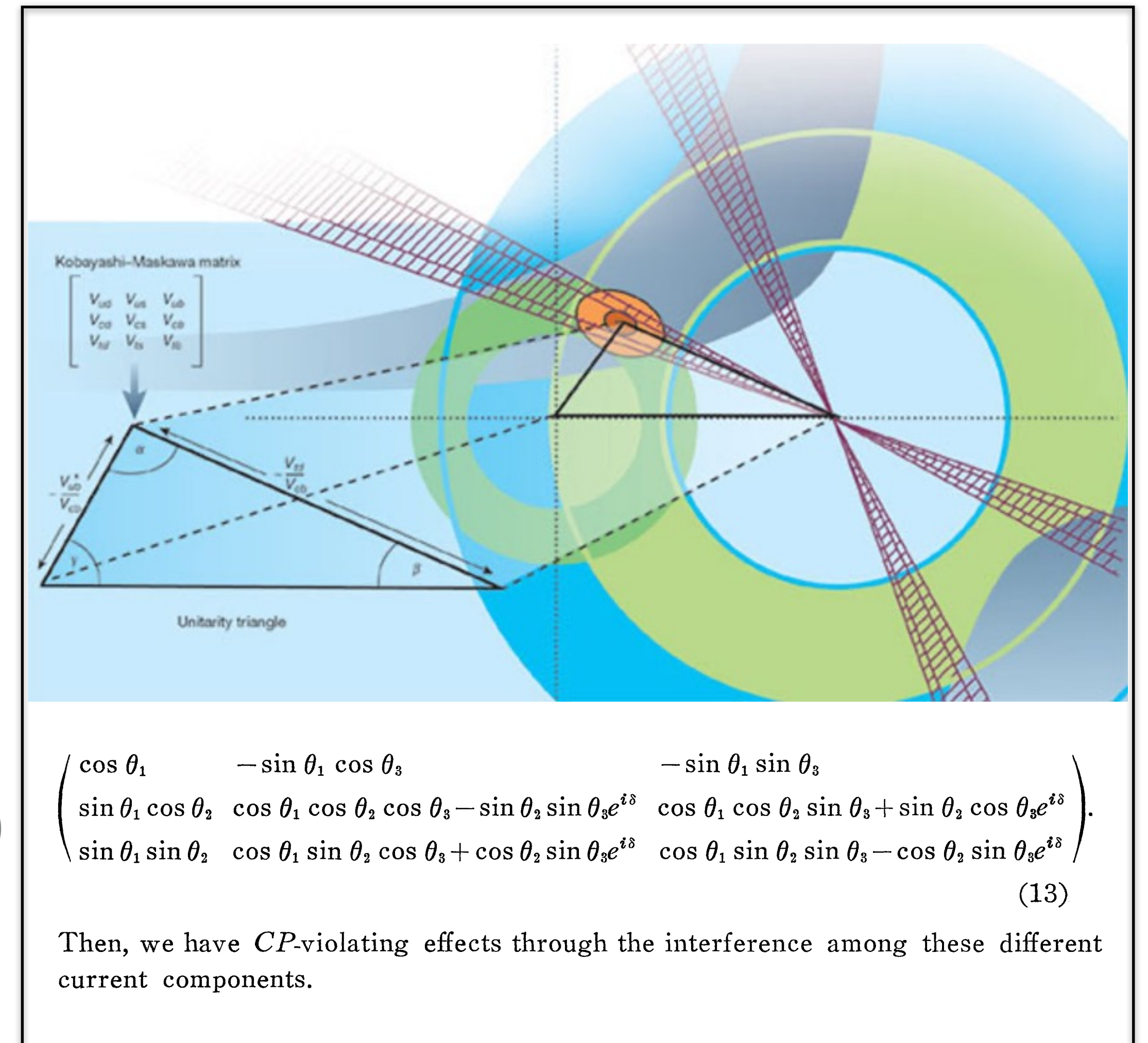


$K^\pm \rightarrow \pi^\pm a$  at NLO in  $\chi$ PT and updated bounds on ALP couplings

C. Cornella, A.M. Galda, M. Neubert and D. Wyler, JHEP **06** (2024) 029

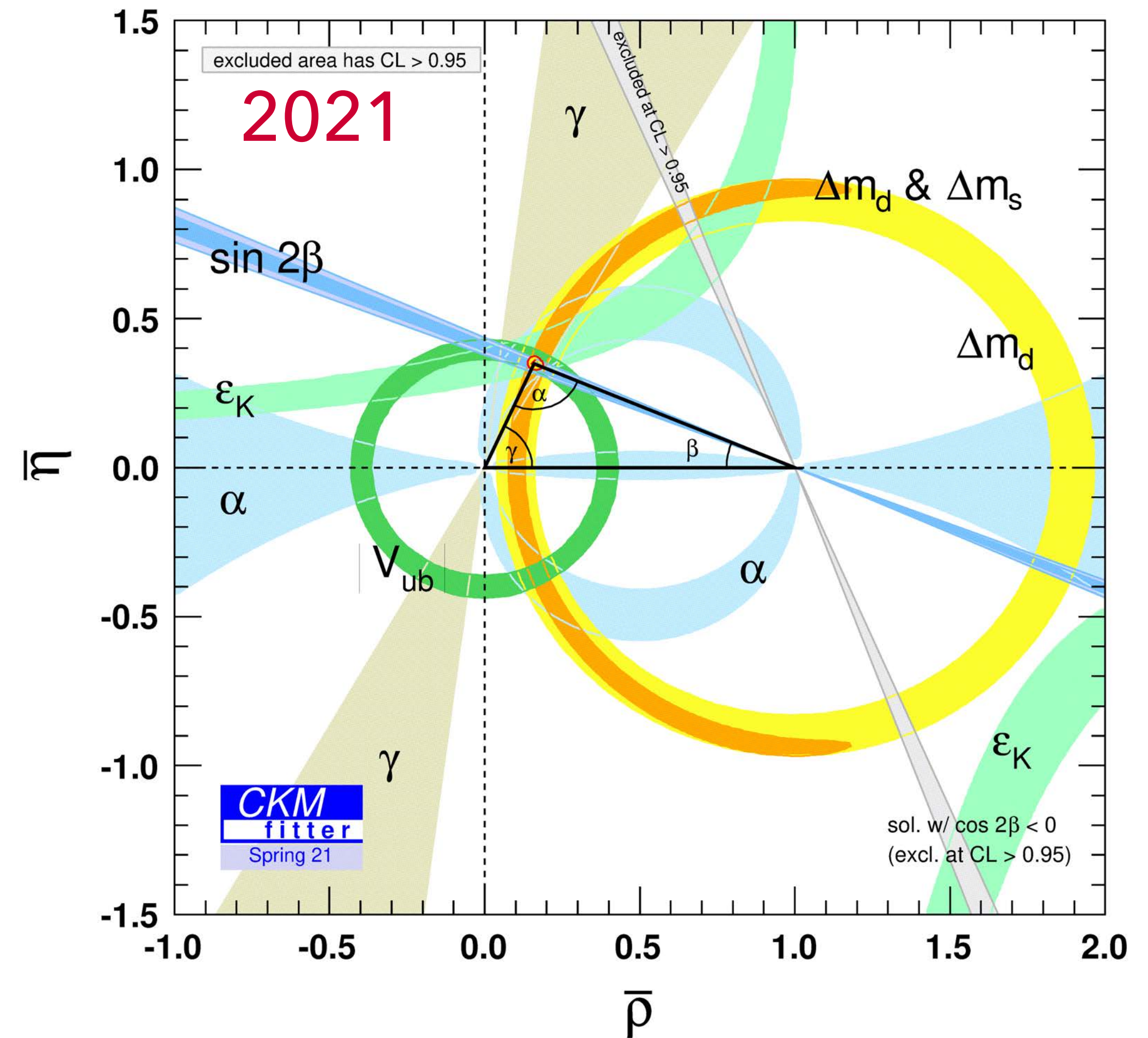
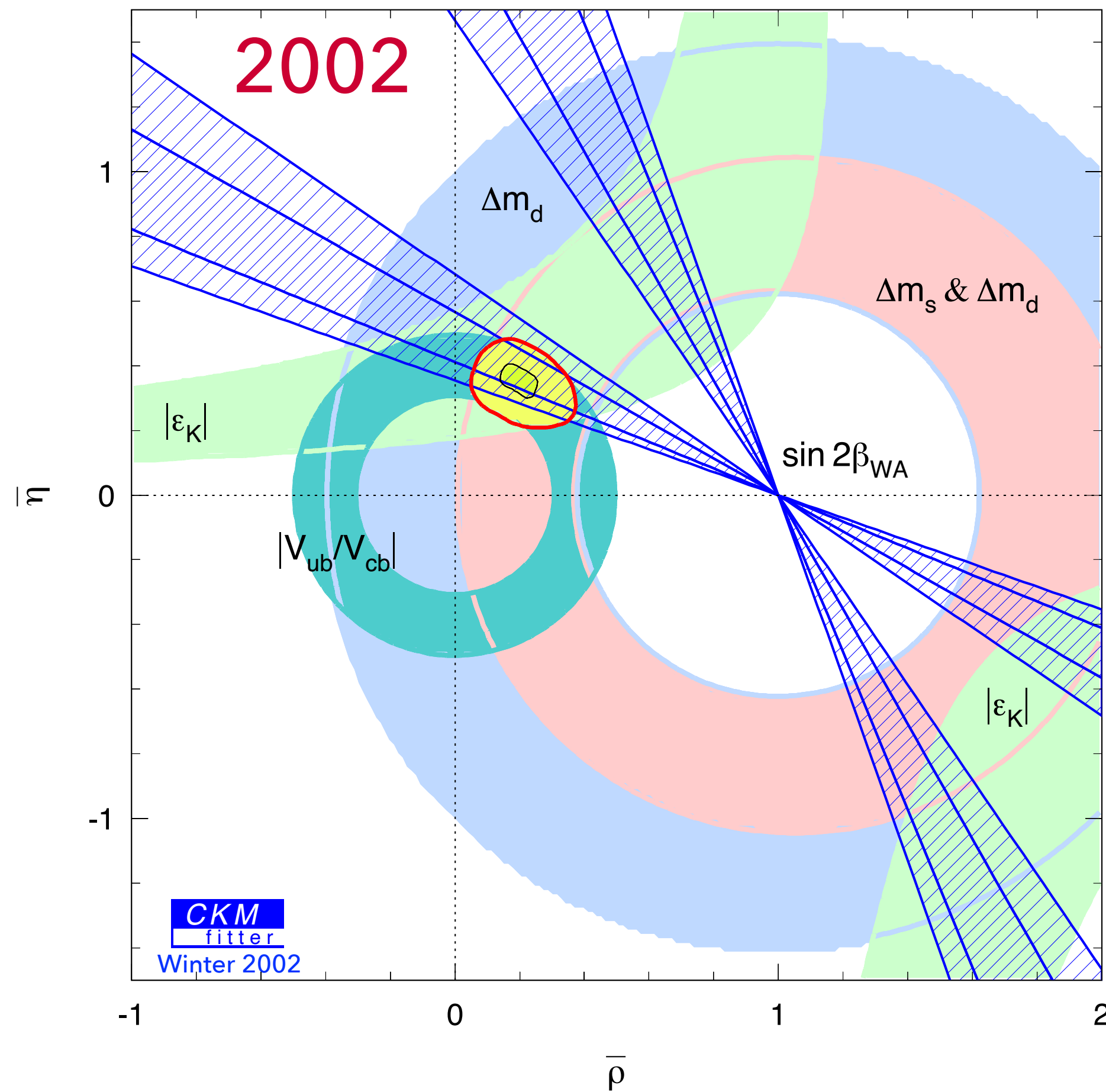
# PUSHING THE LUMINOSITY FRONTIER – GOLDEN AGE OF HEAVY-QUARK THEORY

- ▶ Tremendous experimental advances:
  - ▶ 1. generation: ARGUS & CLEO, LEP expts.
  - ▶ 2. generation: BaBar & Belle, LHCb, CMS, ...
  - ▶ 3. generation: Belle II, LHCb upgrade, ...
- ▶ Precise measurement of CKM elements  $|V_{cb}|, |V_{ub}|, |V_{td}|, |V_{ts}|$  involving third-generation quarks
- ▶ Precise determinations of angles (CP violation)
- ▶ New-physics searches using FCNC processes





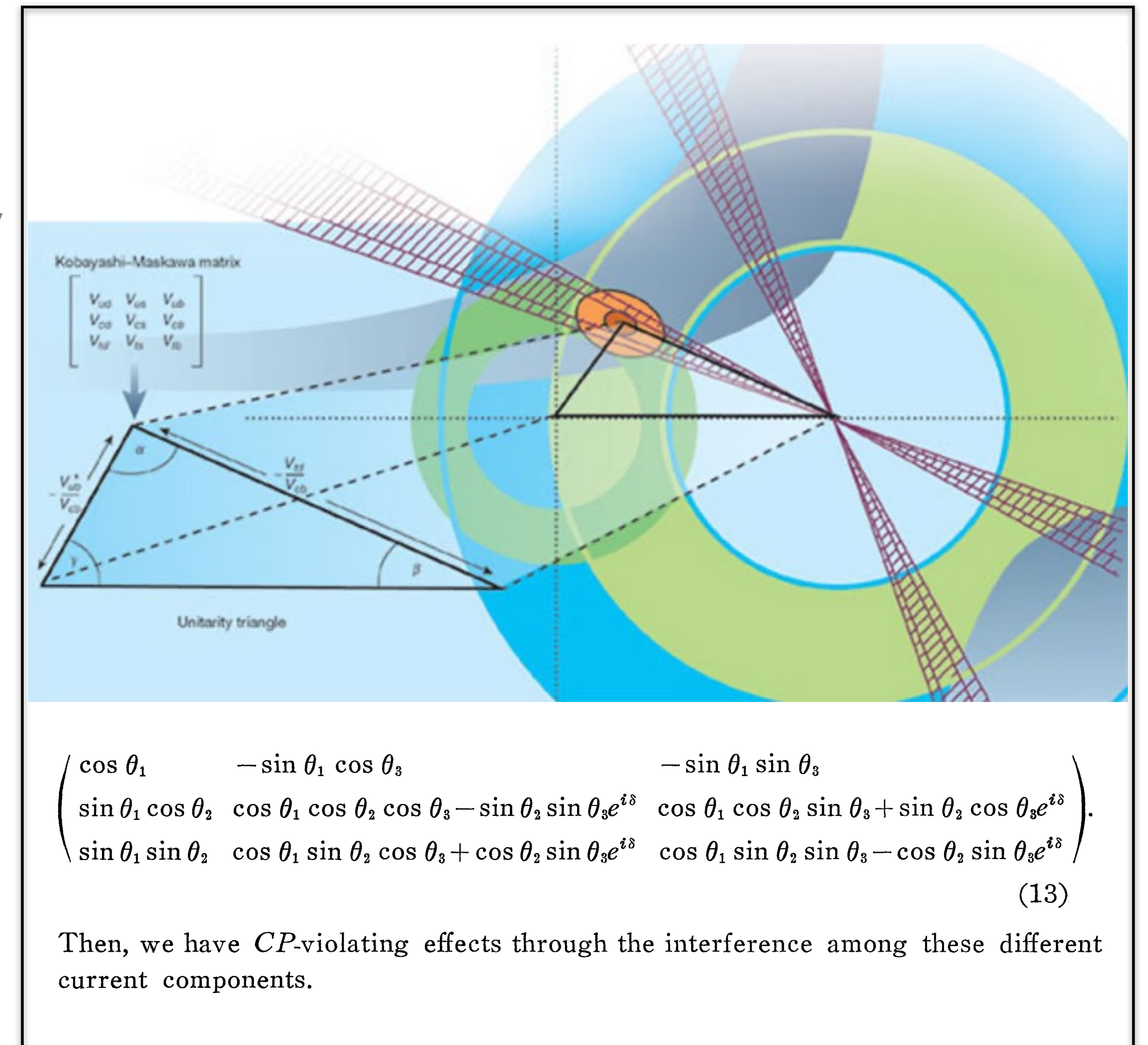
# PUSHING THE LUMINOSITY FRONTIER – GOLDEN AGE OF HEAVY-QUARK THEORY





# PUSHING THE LUMINOSITY FRONTIER – GOLDEN AGE OF HEAVY-QUARK THEORY

- ▶ Matching the incredible precision of the  $B$ -factories required a revolution in theory
- ▶ Concerted effort of theory community was an important consequence
- ▶ Breakthrough came from using **effective field theories** (EFTs):
  - ▶  $\mathcal{H}_{\text{eff}}^{\text{weak}}$ , HQET, NRQCD, QCDF, SCET
- ▶ SCET later became a versatile tool for addressing difficult QCD problems



# EFFECTIVE WEAK HAMILTONIAN

- ▶ Systematic method to separate short-distance effects (weak scale and beyond) from long-distance hadronic dynamics
- ▶ Nowadays embedded into SMEFT and its low-energy variant LEFT
- ▶ **But:** challenge is to evaluate hadronic matrix elements of the quark-gluon operators  $Q_i(\mu)$  in all but simplest cases

$$Q_1^q = (\bar{b}_i q_j)_{V-A} (\bar{q}_j d_i)_{V-A}$$

$$Q_2^q = (\bar{b} q)_{V-A} (\bar{q} d)_{V-A}$$

$$Q_3 = (\bar{b} d)_{V-A} \sum_q (\bar{q} q)_{V-A}$$

$$Q_4 = (\bar{b}_i d_j)_{V-A} \sum_q (\bar{q}_j q_i)_{V-A}$$

$$Q_5 = (\bar{b} d)_{V-A} \sum_q (\bar{q} q)_{V+A}$$

$$Q_6 = (\bar{b}_i d_j)_{V-A} \sum_q (\bar{q}_j q_i)_{V+A}$$

$$Q_7 = \frac{3}{2} (\bar{s} d)_{V-A} \sum_q e_q (\bar{q} q)_{V+A}$$

$$Q_8 = \frac{3}{2} (\bar{s}_i d_j)_{V-A} \sum_q e_q (\bar{q}_j q_i)_{V+A}$$

$$Q_9 = \frac{3}{2} (\bar{s} d)_{V-A} \sum_q e_q (\bar{q} q)_{V-A}$$

$$Q_{10} = \frac{3}{2} (\bar{s}_i d_j)_{V-A} \sum_q e_q (\bar{q}_j q_i)_{V-A}$$

$$\mathcal{H}_{\text{eff}}(\Delta S = 1) = \frac{G_F}{\sqrt{2}} V_{us}^* V_{ud} \sum_{i=1}^{10} (z_i(\mu) + \tau y_i(\mu)) Q_i(\mu)$$

[Gilman, Wise (1979); Buras et al. (1990s)]

## HEAVY QUARK SYMMETRY

- ▶ Hadronic bound states containing a heavy quark obey an approximate **spin-flavor symmetry**
- ▶ Many predictions for spectroscopy of heavy hadrons [Shuryak (1980)]
- ▶ Symmetry relations among  $B \rightarrow D^{(*)}$  form factors, including symmetry-breaking corrections  $\sim \alpha_s(m_Q)$  or  $\Lambda_{\text{QCD}}/m_Q$  [Isgur, Wise (1990)]

Relations between level spacings in bottom and charm systems, e.g.:

- ▶  $m_{B^*}^2 - m_B^2 \approx 0.49 \text{ GeV}^2$  vs.  $m_{D^*}^2 - m_D^2 \approx 0.55 \text{ GeV}^2$
- ▶  $m_{B_s} - m_B \approx m_{D_s} - m_d \approx 0.10 \text{ GeV}$
- ▶  $m_{B_2^*}^2 - m_{B_1}^2 \approx m_{D_2^*}^2 - m_{D_1}^2 \approx 0.17 \text{ GeV}^2$

Form-factor relations:

$$\langle D(v') | V^\mu | B(v) \rangle = h_+(w) (v + v')^\mu + h_-(w) (v - v')^\mu$$

$$\langle D^*(v', \epsilon) | V^\mu | B(v) \rangle = i h_V(w) \epsilon^{\mu\nu\alpha\beta} \epsilon_\nu^* v'_\alpha v_\beta$$

$$\langle D^*(v', \epsilon) | A^\mu | B(v) \rangle = h_{A_1}(w) (w + 1) \epsilon^{*\mu} - [h_{A_2}(w) v^\mu + h_{A_3}(w) v'^\mu] \epsilon^* \cdot v$$

with  $w = v \cdot v'$ :

$$h_+(w) = h_V(w) = h_{A_1}(w) = h_{A_3}(w) = \xi(w) \quad \text{and} \quad \xi(1) = 1$$

$$h_-(w) = h_{A_2}(w) = 0$$



# MODEL-INDEPENDENT DETERMINATION OF $|V_{cb}|$

- ▶ Extrapolate observed spectrum in  $w = v \cdot v'$  to zero recoil:

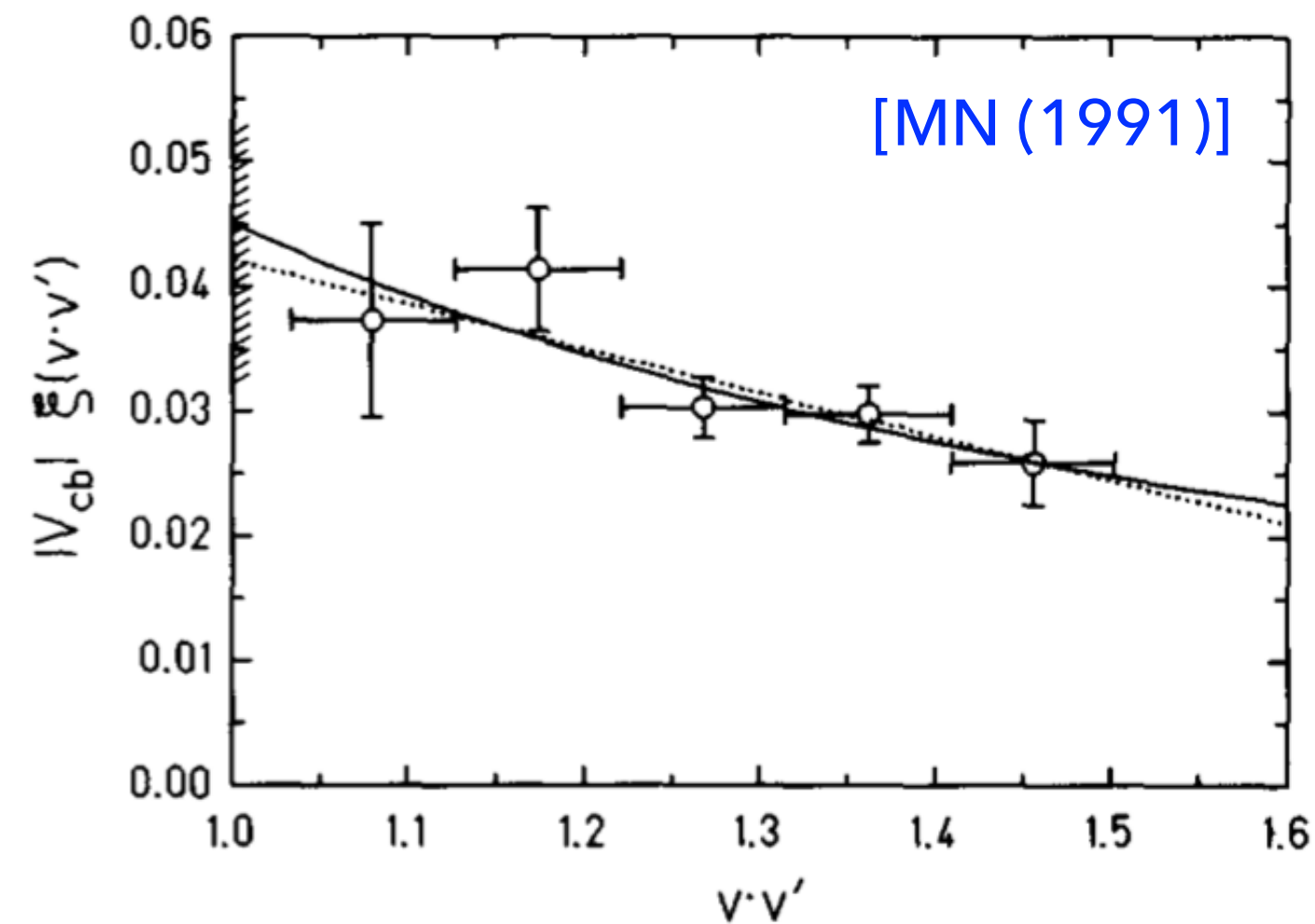
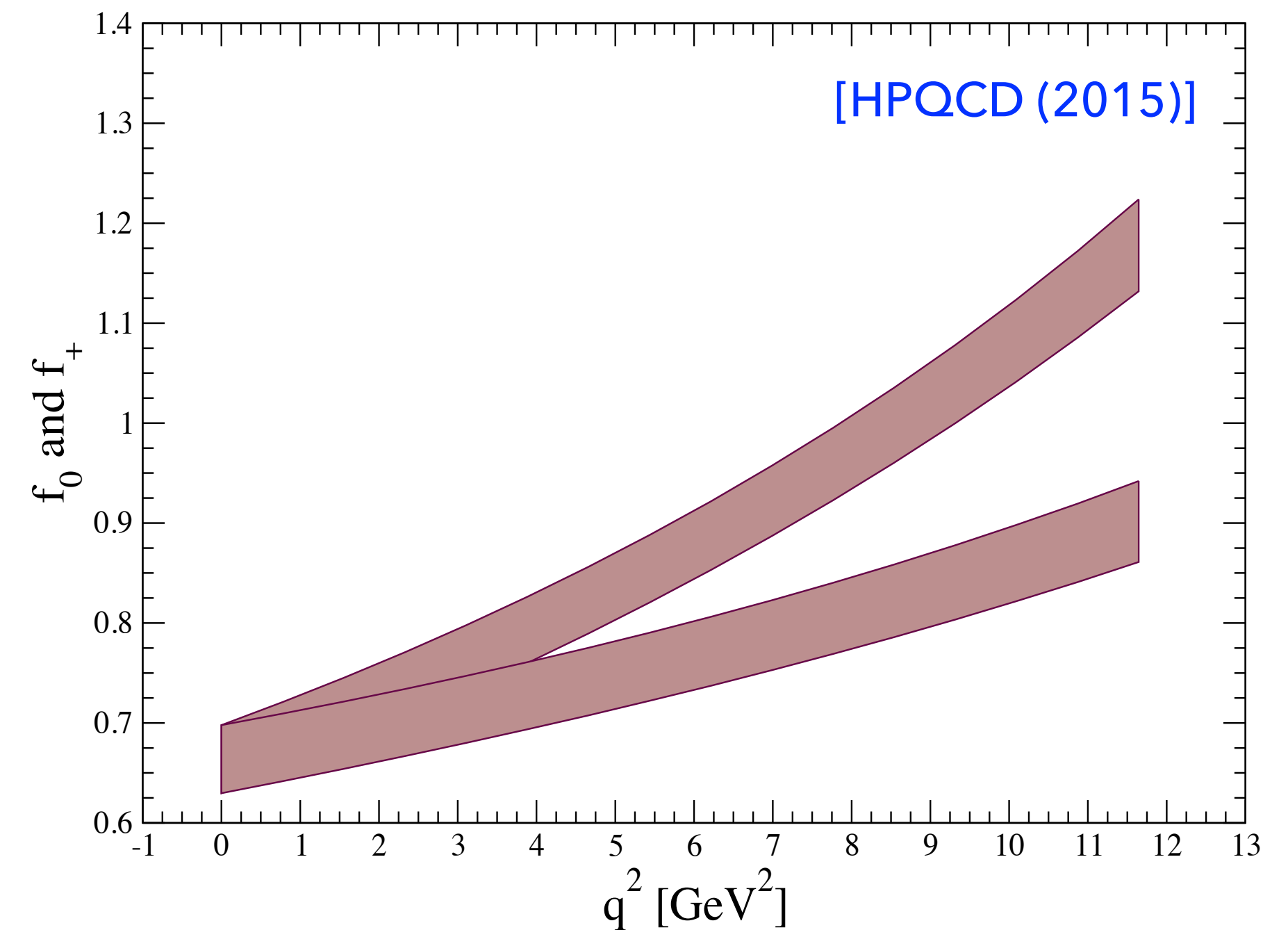


Fig. 1. Extraction of  $|V_{cb}|$  and the Isgur-Wise function from  $\bar{B}^0 \rightarrow D^{*+} \ell \bar{\nu}_\ell$  decays. The data are taken from ref. [16].  $\tau_{B^0} = 1.18$  ps is assumed.  $|V_{cb}|$  follows from an extrapolation of the data to  $v \cdot v' = 1$ . Its currently best value is indicated as a shaded area on the vertical axis.

- ▶ Direct calculation of the  $B \rightarrow D \ell \nu$  form factors (HPQCD):





## HEAVY QUARK EFFECTIVE THEORY (HQET)

[Eichten, Hill (1990); Georgi (1990)]

- ▶ Firm theoretical basis for deriving heavy-quark symmetry and its consequences

$$\mathcal{L}_{\text{HQET}} = \bar{h}_v i v \cdot D h_v + \mathcal{O}\left(\frac{1}{m_Q}\right) + \frac{1}{2m_Q} \left[ \bar{h}_v (iD)^2 h_v + \frac{g_s}{2} \bar{h}_v \sigma_{\mu\nu} G^{\mu\nu} h_v \right] + \dots$$



## THE GRAND CHALLENGE: NON-LEPTONIC DECAYS

- ▶ Georgi: *“Why we can’t calculate ...”* [Georgi: *Weak Interactions and Modern Particle Theory* (1984)]
- ▶ Naive factorization approach was semi-successful in describing early data, but lacked a firm theoretical foundation [Bauer, Stech, Wirbel (1986)]

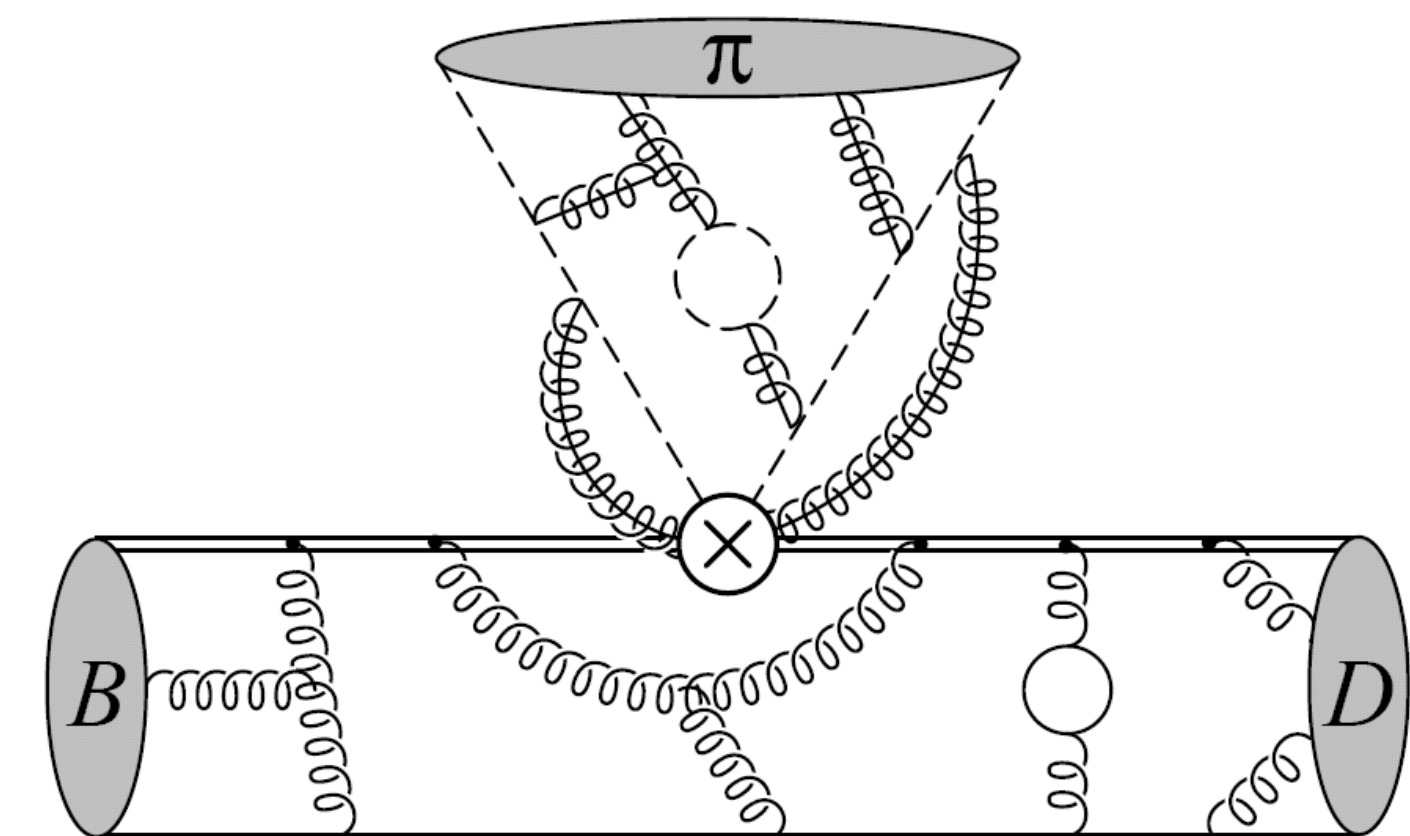


# THE GRAND CHALLENGE: NON-LEPTONIC DECAYS

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- ▶ **QCD factorization approach (BBNS):**
  - ▶ First model-independent calculation of  $B \rightarrow M_1 M_2$  decay amplitudes from first principles (including strong- and weak-interaction phases) in heavy-quark limit

[Beneke, Buchalla, MN, Sachrajda (1999–2001)]

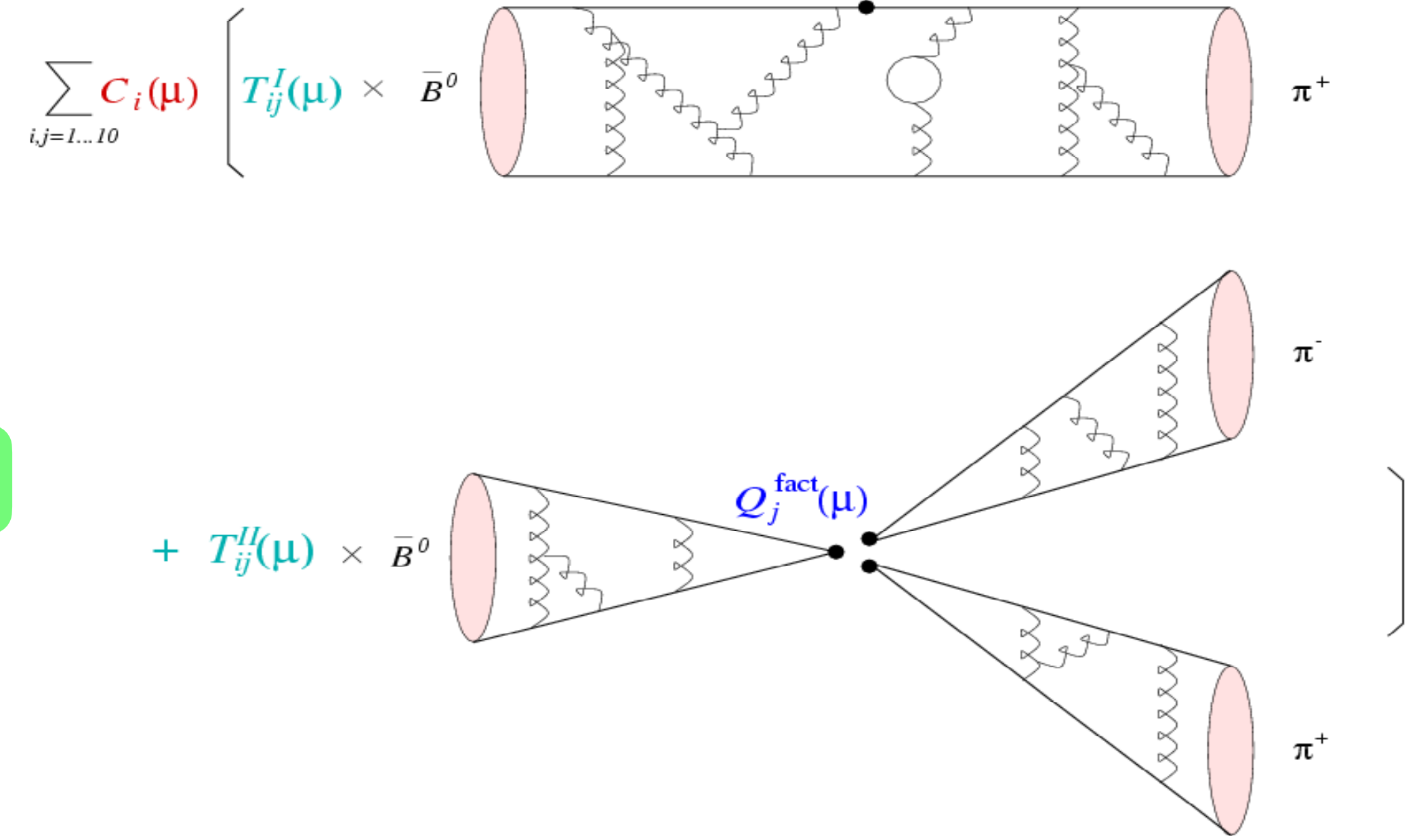
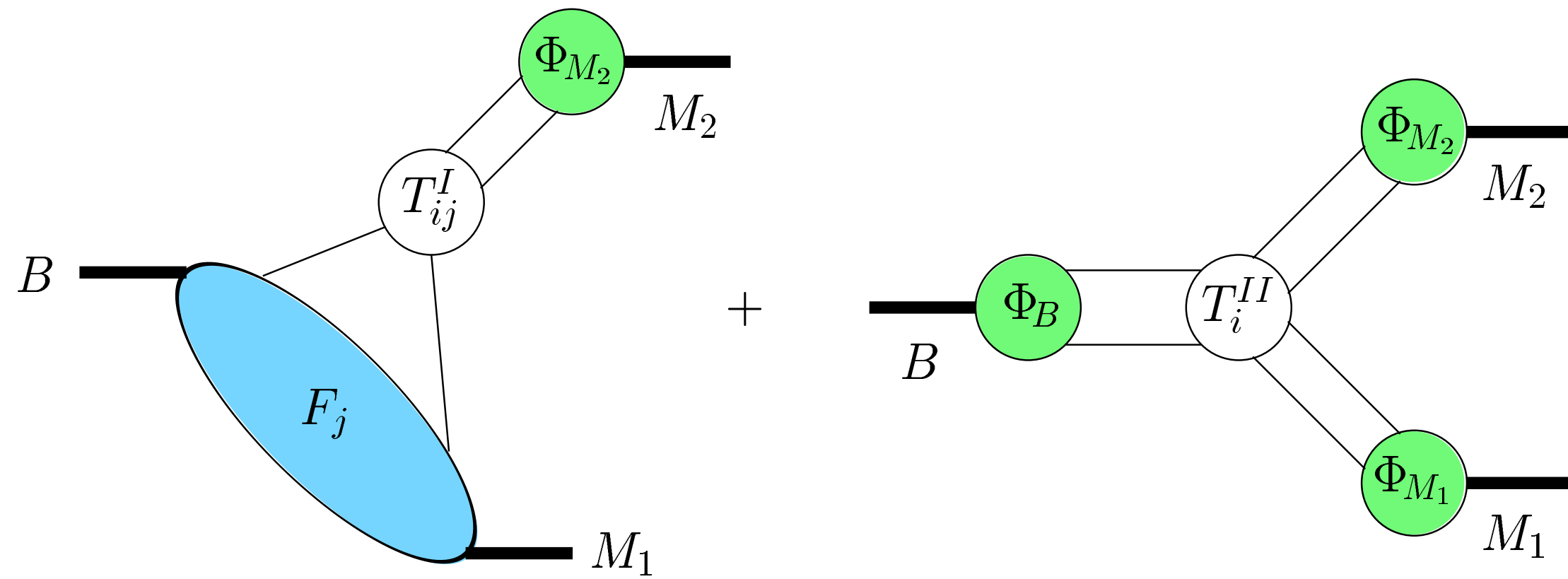


Factorization proof at two-loop order based on method of regions, see pp. 48-79 in BBNS (2000)



# QCD FACTORIZATION IN NONLEPTONIC B DECAYS INTO LIGHT MESONS

QCD factorization theorem: [Beneke, Buchalla, MN, Sachrajda (1999–2001)]

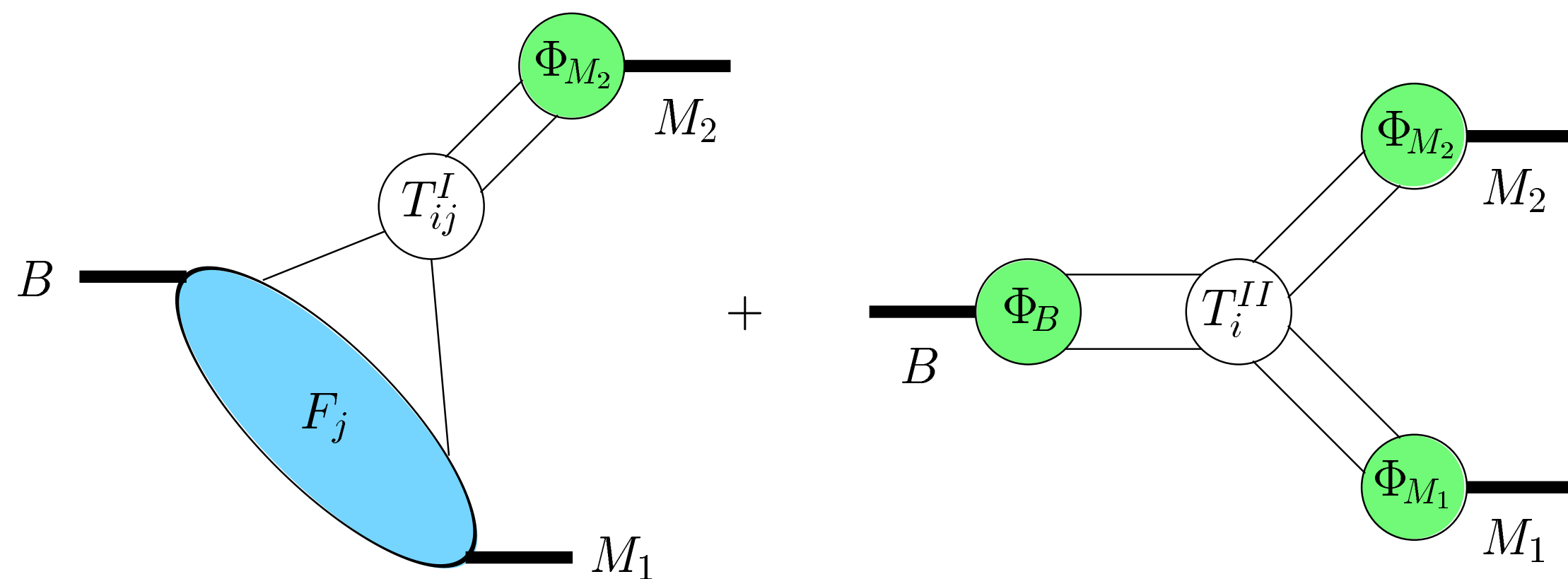


$$\langle \pi K | Q_i | B \rangle = F_0^{B \rightarrow \pi} T_{K,i}^I * f_K \Phi_K + F_0^{B \rightarrow K} T_{\pi,i}^I * f_\pi \Phi_\pi + T_i^{II} * f_B \Phi_B * f_K \Phi_K * f_\pi \Phi_\pi + \mathcal{O}\left(\frac{\Lambda_{\text{QCD}}}{m_b}\right)$$



# QCD FACTORIZATION IN NONLEPTONIC B DECAYS INTO LIGHT MESONS

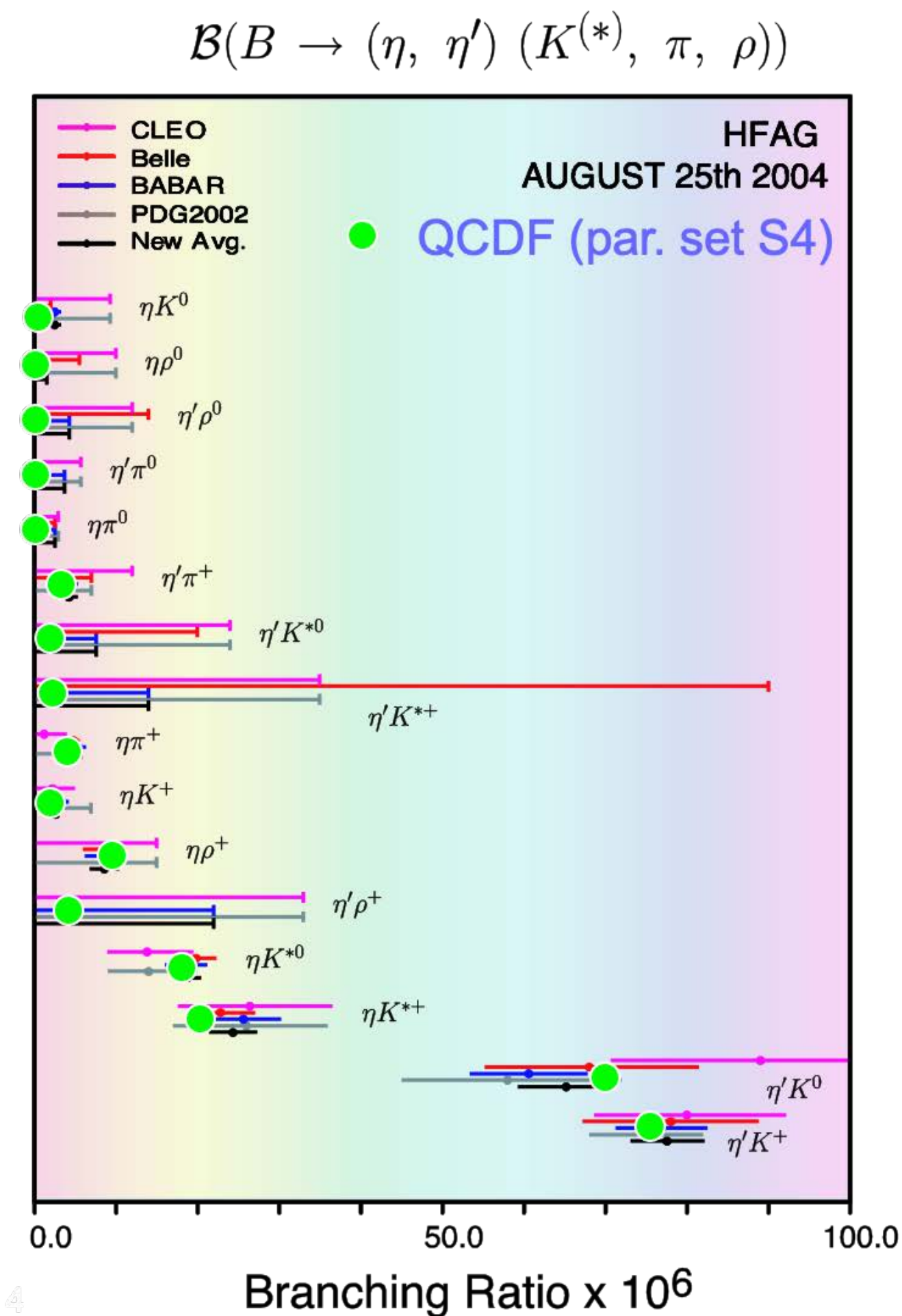
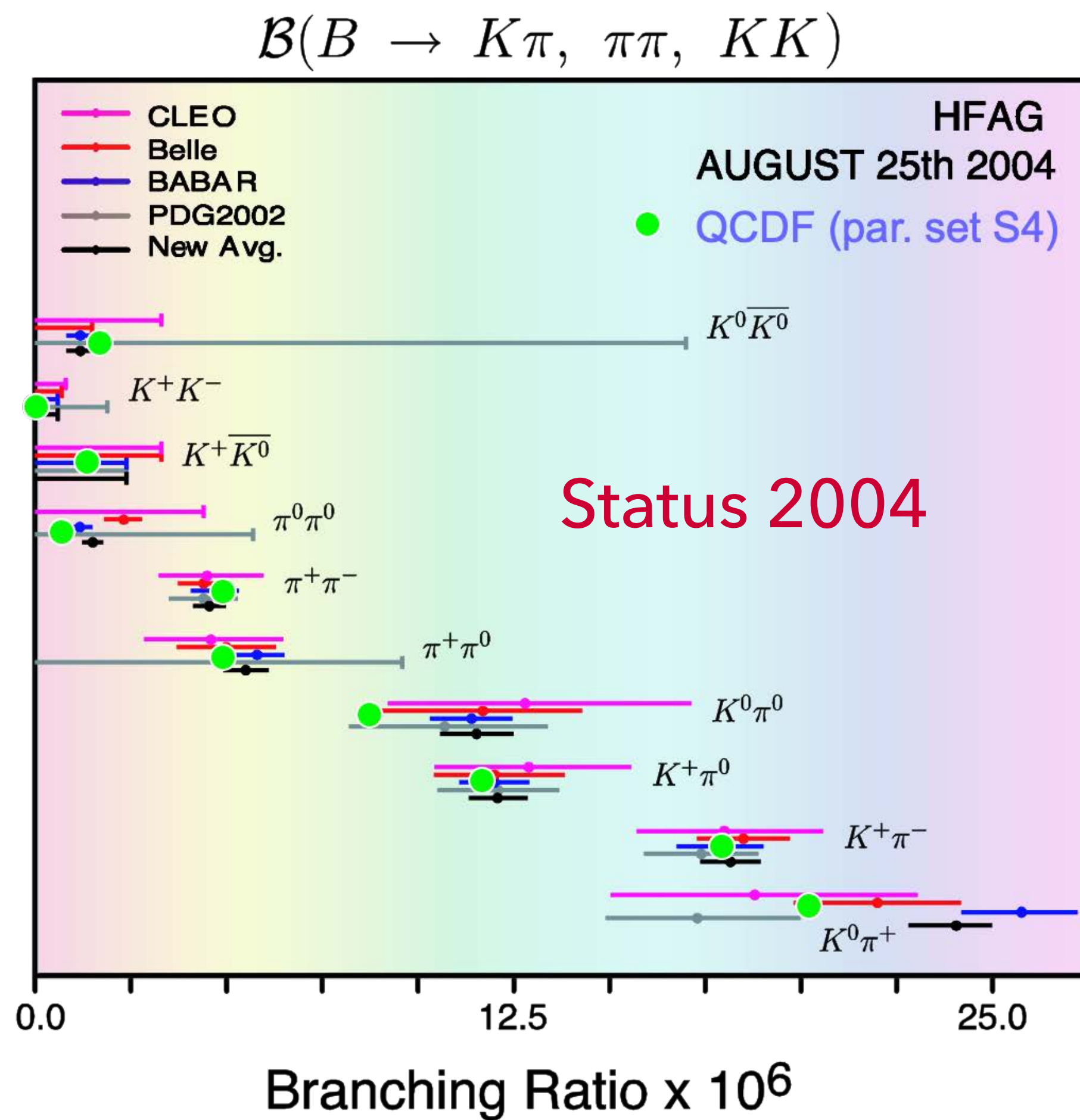
QCD factorization theorem: [Beneke, Buchalla, MN, Sachrajda (1999–2001)]



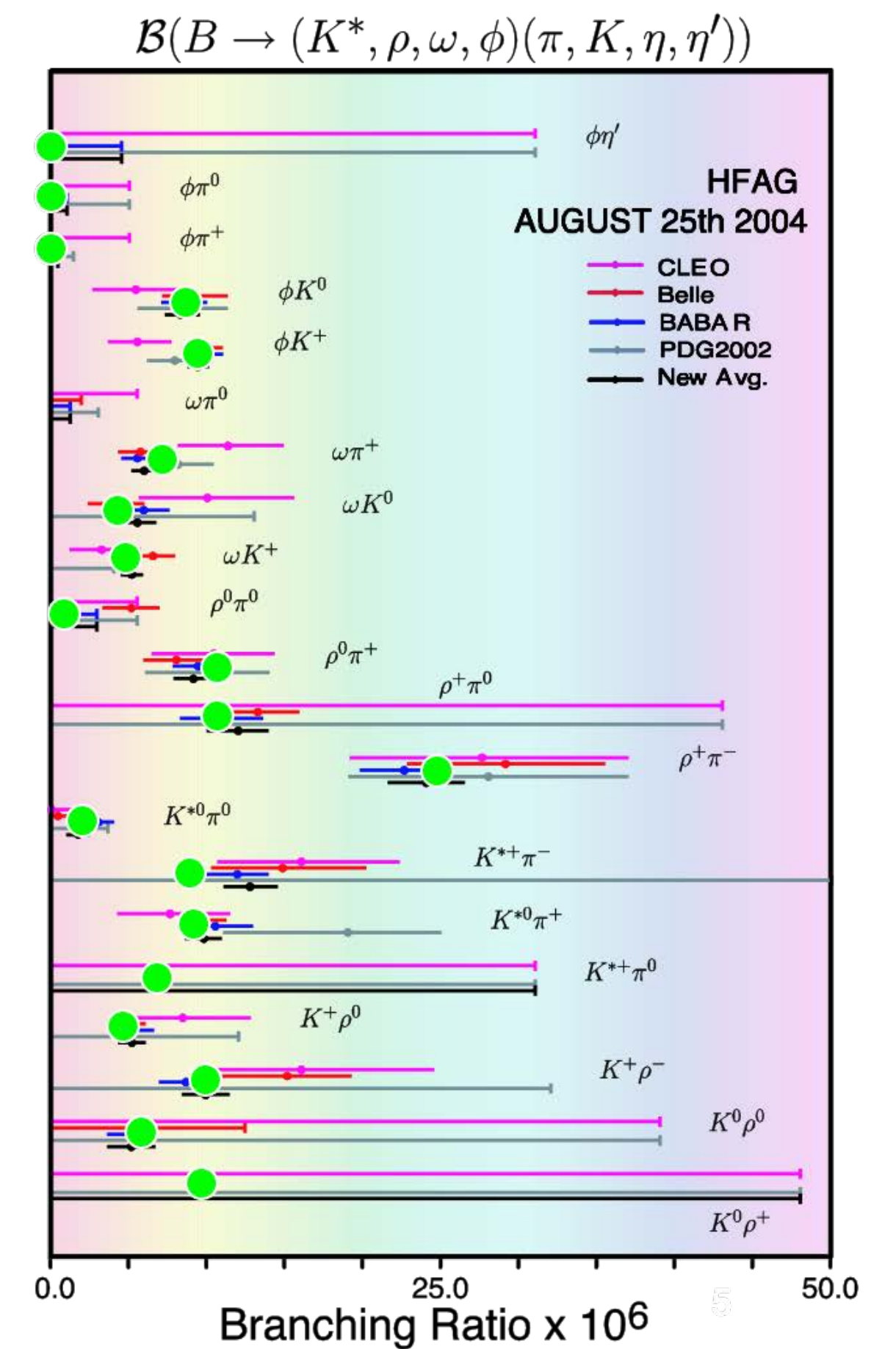
$$\langle \pi K | Q_i | B \rangle = F_0^{B \rightarrow \pi} T_{K,i}^I * f_K \Phi_K + F_0^{B \rightarrow K} T_{\pi,i}^I * f_\pi \Phi_\pi + T_i^{II} * f_B \Phi_B * f_K \Phi_K * f_\pi \Phi_\pi + \mathcal{O}\left(\frac{\Lambda_{\text{QCD}}}{m_b}\right)$$

- ▶ Importance of **non-local hadronic matrix elements**, in particular light-cone distribution amplitudes (LCDAs), to account for hadronic dynamics
- ▶ Second term corresponds to Brodsky-Lepage (1980), while the first term is specific for  $B$ -meson decays and contributes at the same order in  $\Lambda_{\text{QCD}}/m_b$

# QCD FACTORIZATION IN NONLEPTONIC B DECAYS INTO LIGHT MESONS



[Beneke, MN (2003)]





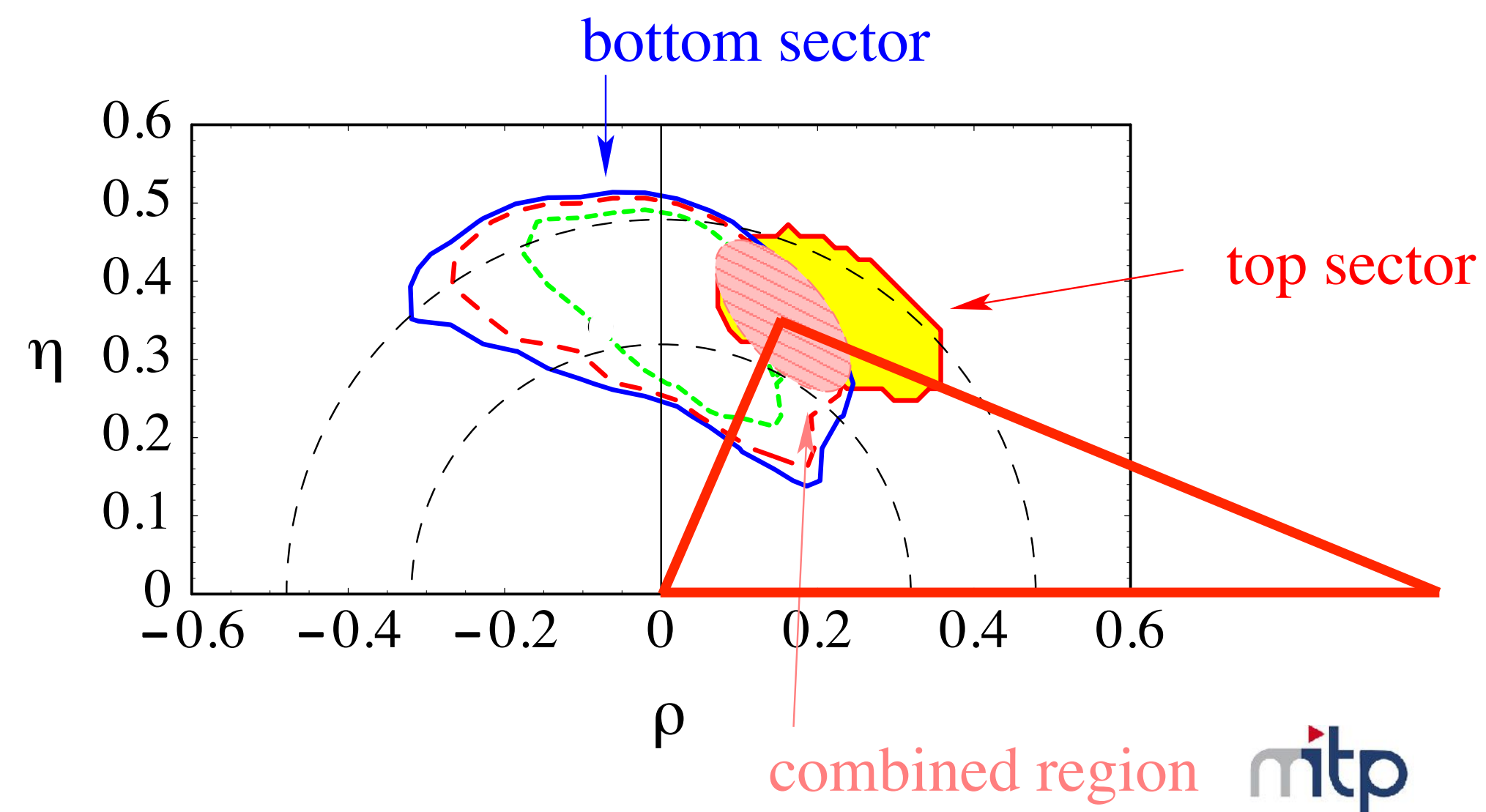
# CONFIRMATION OF KM RELATION BETWEEN $\text{Im}(V_{UB})$ AND $\text{Im}(V_{TB})$

- ▶ In 2001, fact that  $\text{Im}(V_{td}) \neq 0$  had been established by studies of  $K-\bar{K}$  and  $B-\bar{B}$  mixing and first measurements of  $\sin 2\beta$
- ▶ Fact that  $\text{Im}(V_{ub}) \neq 0$  has been established by studying rare hadronic decays  $B \rightarrow \pi K, \pi\pi$  in QCD factorization [BBNS (2001), here updated to 2004 data]
- ▶ **KM relation confirmed;** most stringent test of KM mechanism at the time

2004 analysis:  $\bar{\rho} = 0.15 \pm 0.08$ ,  $\bar{\eta} = 0.36 \pm 0.09$   
 $\gamma = (67 \pm 15)^\circ$ ,  $\beta = (24 \pm 2)^\circ$

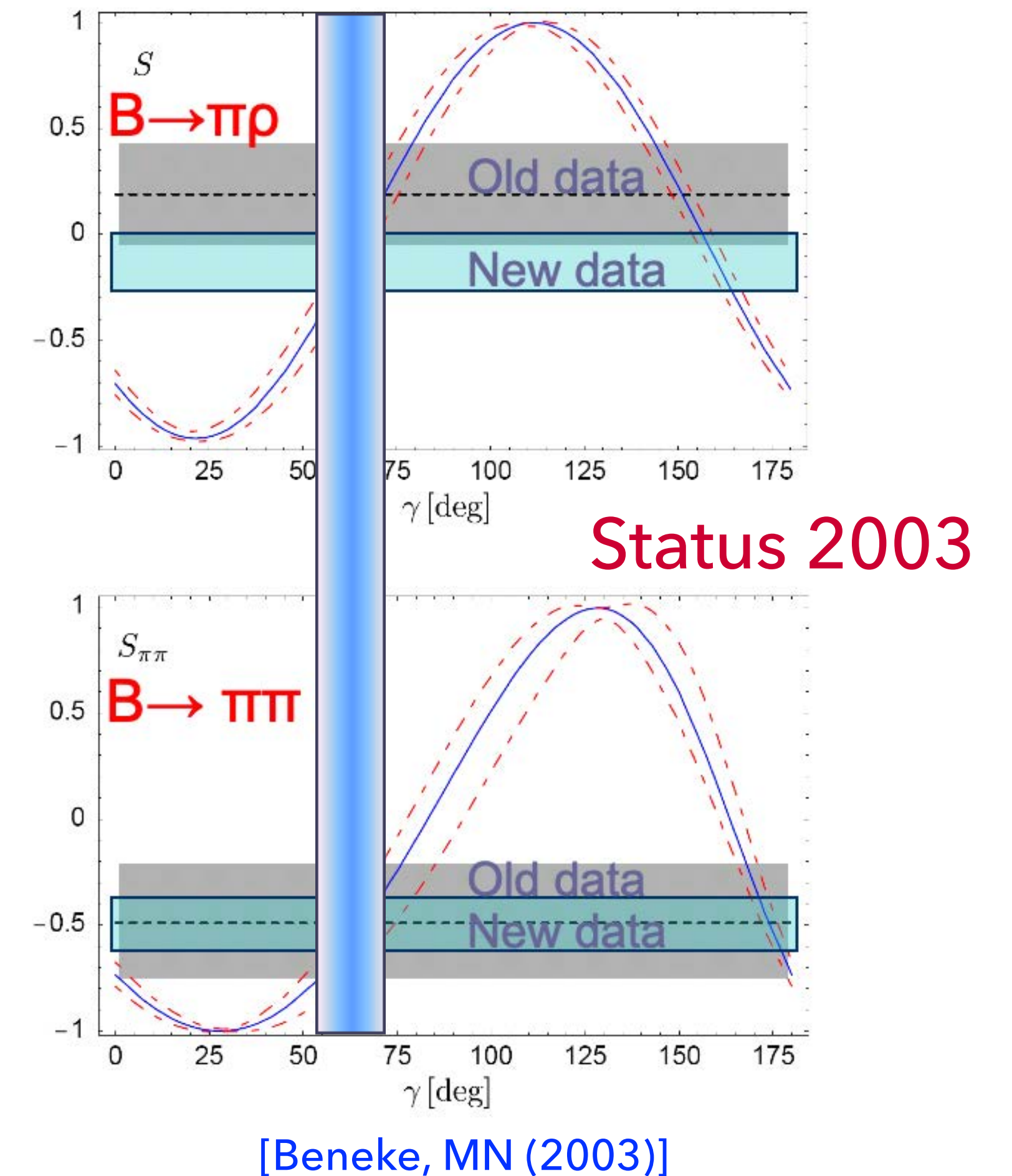
2021 values:  $\bar{\rho} = 0.157^{+0.009}_{-0.005}$ ,  $\bar{\eta} = 0.347^{+0.012}_{-0.005}$   
 $\gamma = (65.5^{+1.3}_{-1.2})^\circ$ ,  $\beta = (22.42^{+0.64}_{-0.37})^\circ$

[CKMfitter global fit, spring 2021]



# CONFIRMATION OF KM RELATION BETWEEN $\text{IM}(V_{UB})$ AND $\text{IM}(V_{TB})$

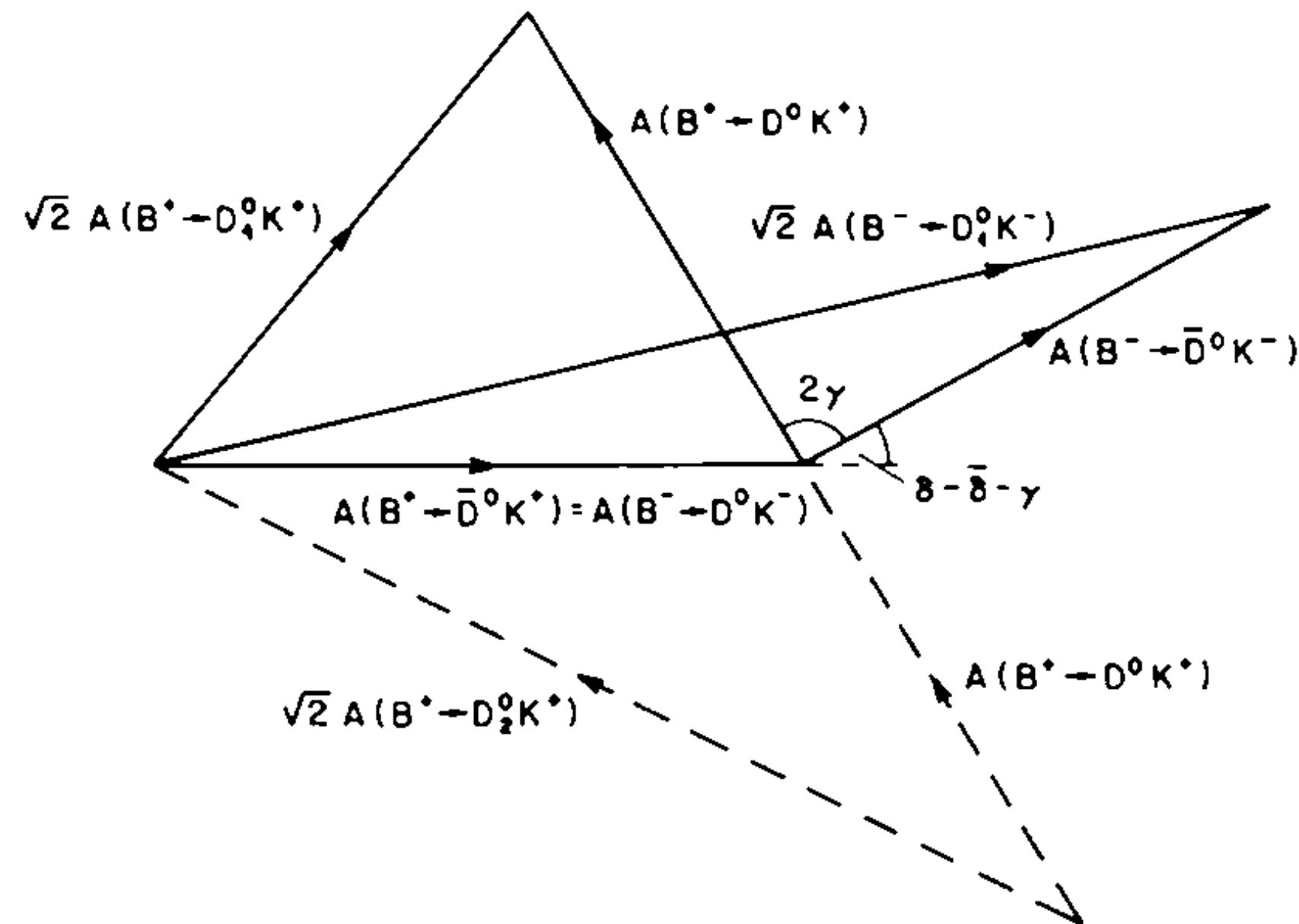
- ▶ Measuring time-dependent CP asymmetries in  $B \rightarrow \pi\pi$  and  $B \rightarrow \pi\rho$  decays one obtains an internally consistent determination of  $\gamma$
- ▶ 2003 analysis found:  $\gamma = (62 \pm 8)^\circ$
- ▶ 2021 value:  $\gamma = (65.5^{+1.3}_{-1.2})^\circ$   
 ↪ Gronau–Wyler method





# GRONAU-WYLER METHODE

[Gronau, Wyler (1991)]



$$\sin \gamma = \frac{1}{4|A\bar{A}|} \left( \pm \left\{ \left[ (|A| + |\bar{A}|)^2 - 2|A_1^+|^2 \right] \times [2|A_1^-|^2 - (|A| - |\bar{A}|)^2] \right\}^{1/2} \pm \left\{ \left[ (|A| + |\bar{A}|)^2 - 2|A_1^-|^2 \right] \times [2|A_1^+|^2 - (|A| - |\bar{A}|)^2] \right\}^{1/2} \right),$$

Physics Letters B 265 (1991) 172–176  
North-Holland

**A pioneering paper!**  
(1141 citations)

PHYSICS LETTERS B

## On determining a weak phase from charged B decay asymmetries

Michael Gronau

*Technion – Israel Institute of Technology, Haifa 32000, Israel*

and

Daniel Wyler

*Institute for Theoretical Physics, University of Zurich, Schönberggasse 9, CH-8001 Zurich, Switzerland*

Received 27 May 1991

We demonstrate a possible determination of the weak phase  $\gamma$  from the  $CP$  asymmetry in  $B^+ \rightarrow D_{1(2)}^0 X^+$ , where  $D_{1(2)}^0$  is a  $CP$ -even (odd) state and  $X^+$  is any hadronic state with the flavor of a  $K^+$ . To obtain the phase one needs separate measurements of the rates  $\Gamma(B^+ \rightarrow D_{1(2)}^0 X^+)$  and of the equal rates  $\Gamma(B^\pm \rightarrow D^0 X^\pm) = \Gamma(B^\pm \rightarrow \bar{D}^0 X^\mp)$ . Certain ambiguities are discussed and resolutions are proposed.

$$\begin{aligned} \sqrt{2} A(B^+ \rightarrow D_1^0 K^+) &= |A| \exp(i\gamma) \exp(i\delta) + |\bar{A}| \exp(i\delta), \\ \sqrt{2} A(B^- \rightarrow D_1^0 K^-) &= |A| \exp(-i\gamma) \exp(i\delta) + |\bar{A}| \exp(i\delta). \end{aligned}$$

$$\begin{aligned} \sqrt{2} A(B^+ \rightarrow D_1^0 K^+) &= A(B^+ \rightarrow D^0 K^+) + A(B^+ \rightarrow \bar{D}^0 K^+), \\ \sqrt{2} A(B^- \rightarrow D_1^0 K^-) &= A(B^- \rightarrow \bar{D}^0 K^-) + A(B^- \rightarrow D^0 K^-). \end{aligned}$$

## LIMITATIONS OF QCD FACTORIZATION

- ▶ Lots of predictive power, but uncertainties due to hadronic input quantities: form factors, decay constants, and LCDAs (reducible to some extent)
- ▶ **Power corrections in  $\Lambda_{\text{QCD}}/m_b$  do not (naively) factorize due to endpoint divergences** ( $\Rightarrow$  different meanings of “factorization”)
- ▶ In some cases, power-suppressed effects can be enhanced by large Wilson coefficients (e.g. “color-suppressed” decay modes)
- ▶ To make progress, one needed an EFT implementation of QCD factorization



# SOFT-COLLINEAR EFFECTIVE THEORY (SCET)

[Bauer, (Fleming,) Pirjol, Stewart (2001); Beneke, Chapovski, Diehl, Feldmann (2002)]

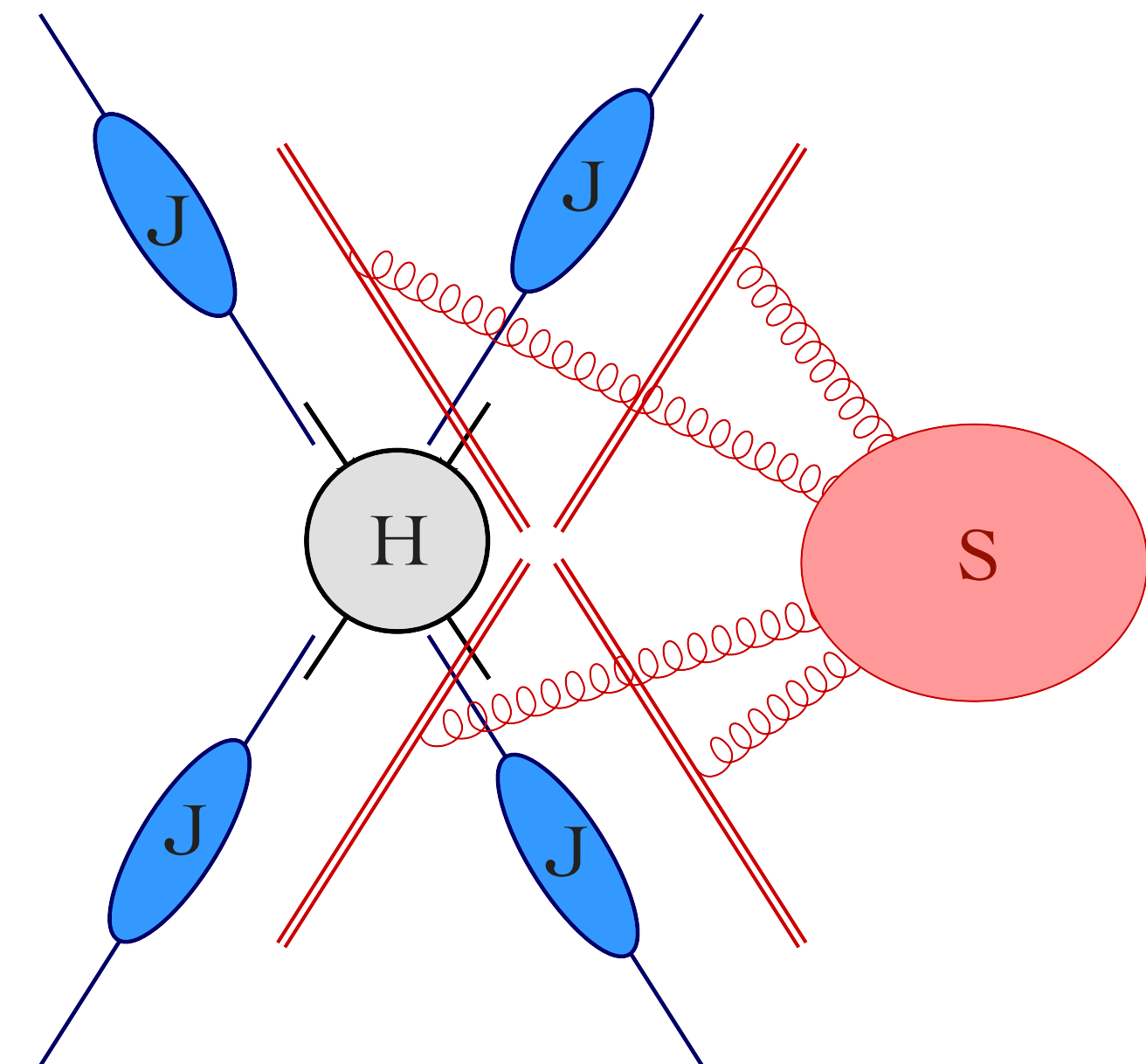
- ▶ Firm theoretical basis for deriving QCD factorization theorems in heavy-quark and collider physics for processes involving light energetic particles

- ▶ Collinear effective Lagrangian:

$$\mathcal{L}_n = \bar{\xi}_n(x) \left[ i\not{n} \cdot D_n + g\not{n} \cdot A_s + i\not{\mathcal{D}}_n^\perp \frac{1}{i\not{\bar{n}} \cdot \mathcal{D}_n} i\not{\mathcal{D}}_n^\perp \right] \frac{\not{n}}{2} \xi_n(x) + \dots$$

eikonal interaction, can be removed by  
the field redefinition  $\xi_n \rightarrow S_n \xi_n^{(0)}$

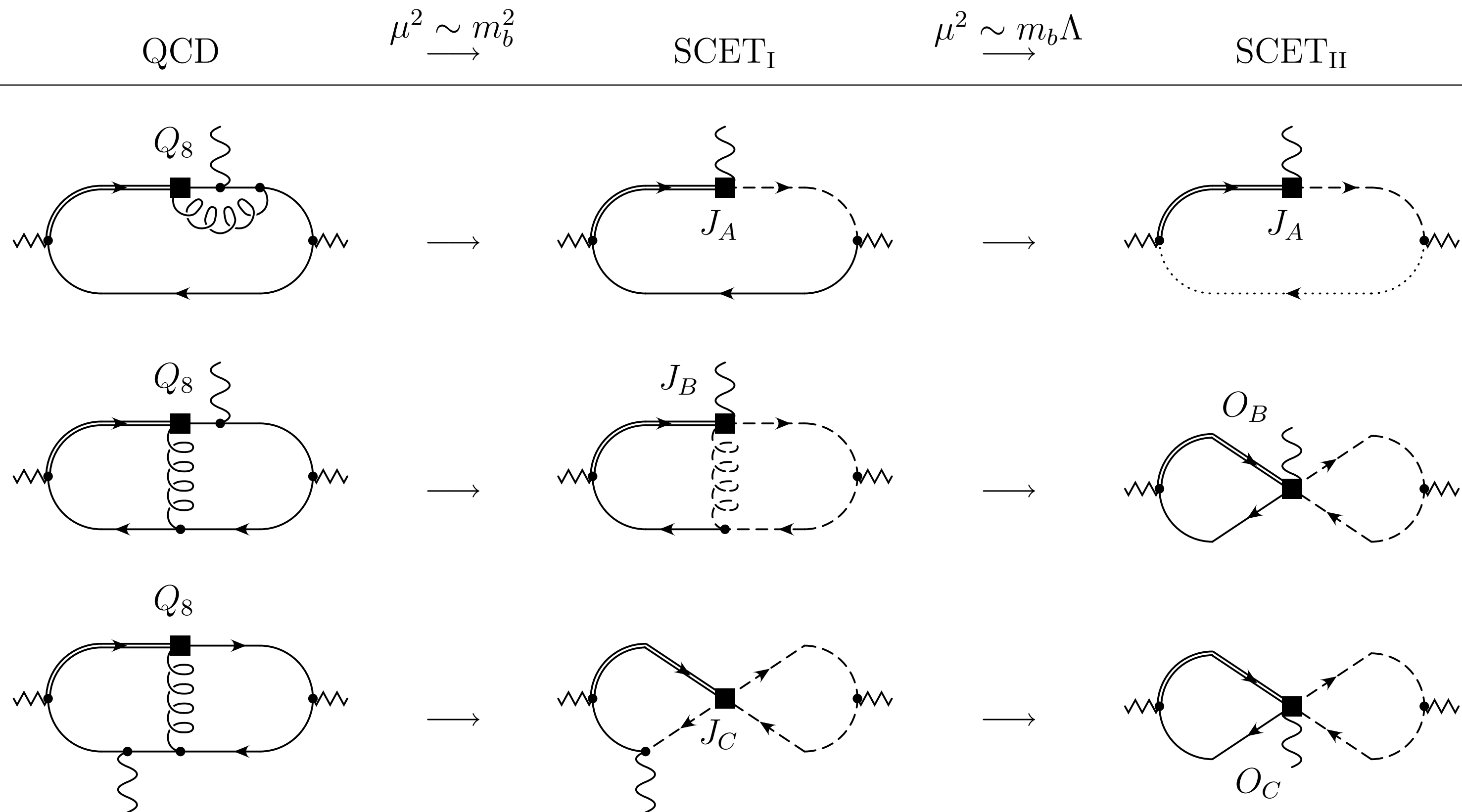
- ▶ Soft-collinear factorization at Lagrangian level
- ▶ Scale separation and resummation accomplished using powerful EFT tools



# SCET PROOF OF QCD FACTORIZATION FOR $B \rightarrow K^* \gamma$ DECAY

[Becher, Hill, MN (2005)]

Two-step matching procedure QCD  $\rightarrow$  SCET-I  $\rightarrow$  SCET-II:

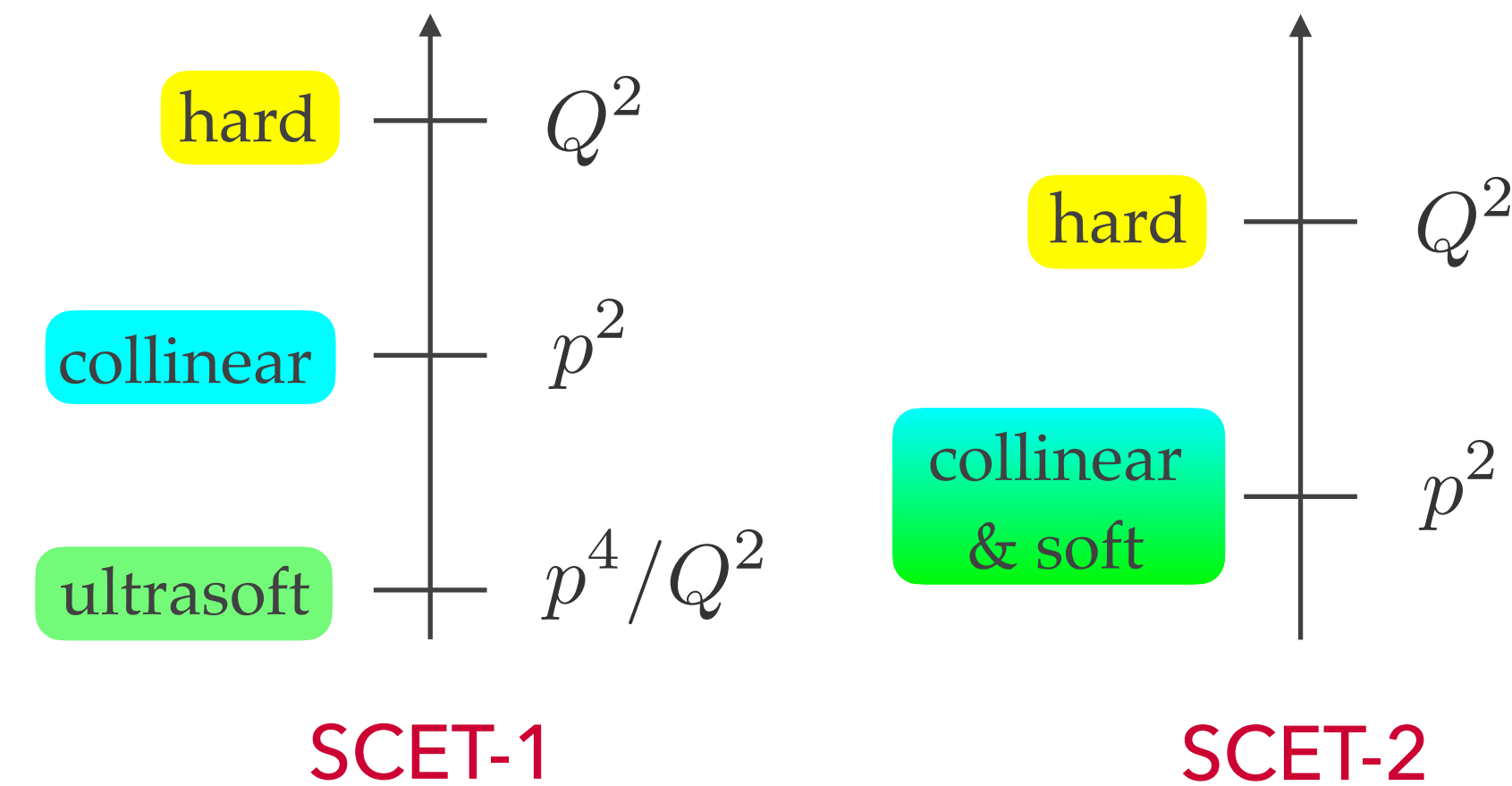




# PROTOTYPICAL SCET FACTORIZATION THEOREM

Product/convolution of component functions each depending on a single scale:

$$\sigma \sim \underset{\text{hard}}{H} \int \underset{\text{collinear}}{J \otimes J} \otimes \underset{\text{soft}}{S}$$



- ▶ Extension to next-to-leading power is a hard problem, due to **endpoint-divergent convolution integrals** [Beneke et al. ; Moult et al.; Stewart et al.; Bell et al. (2018–2022)]

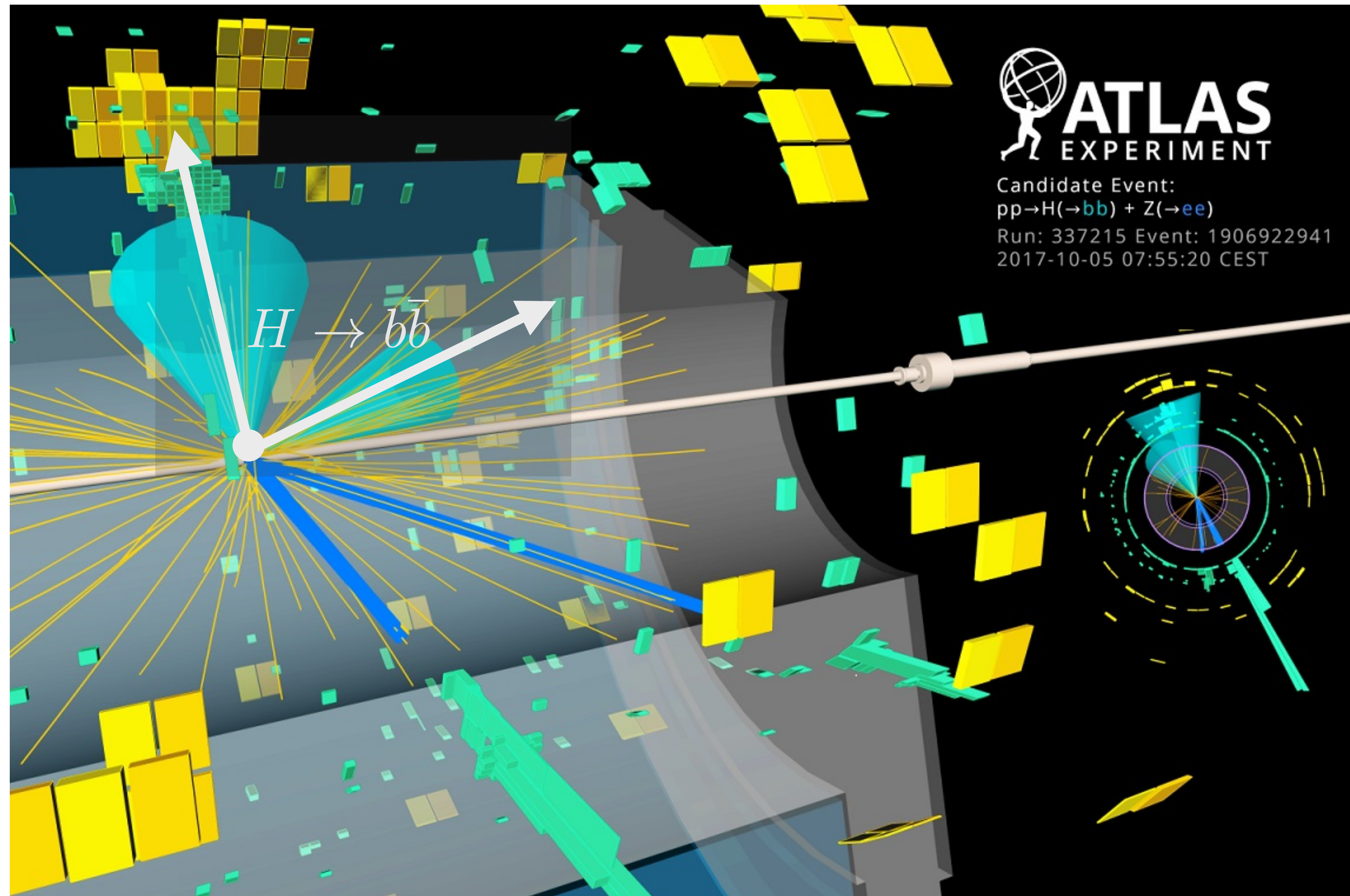
- ▶ **Refactorization-based subtraction (RBS)** scheme provides a consistent framework for dealing with this problem [Liu, MN (2019, 2020); Liu, Mecaj, MN, Wang (2021); Liu, MN, Schnubel, Wang (2022)]

**ZPW2025**

Particle Physics from Low to High Energies



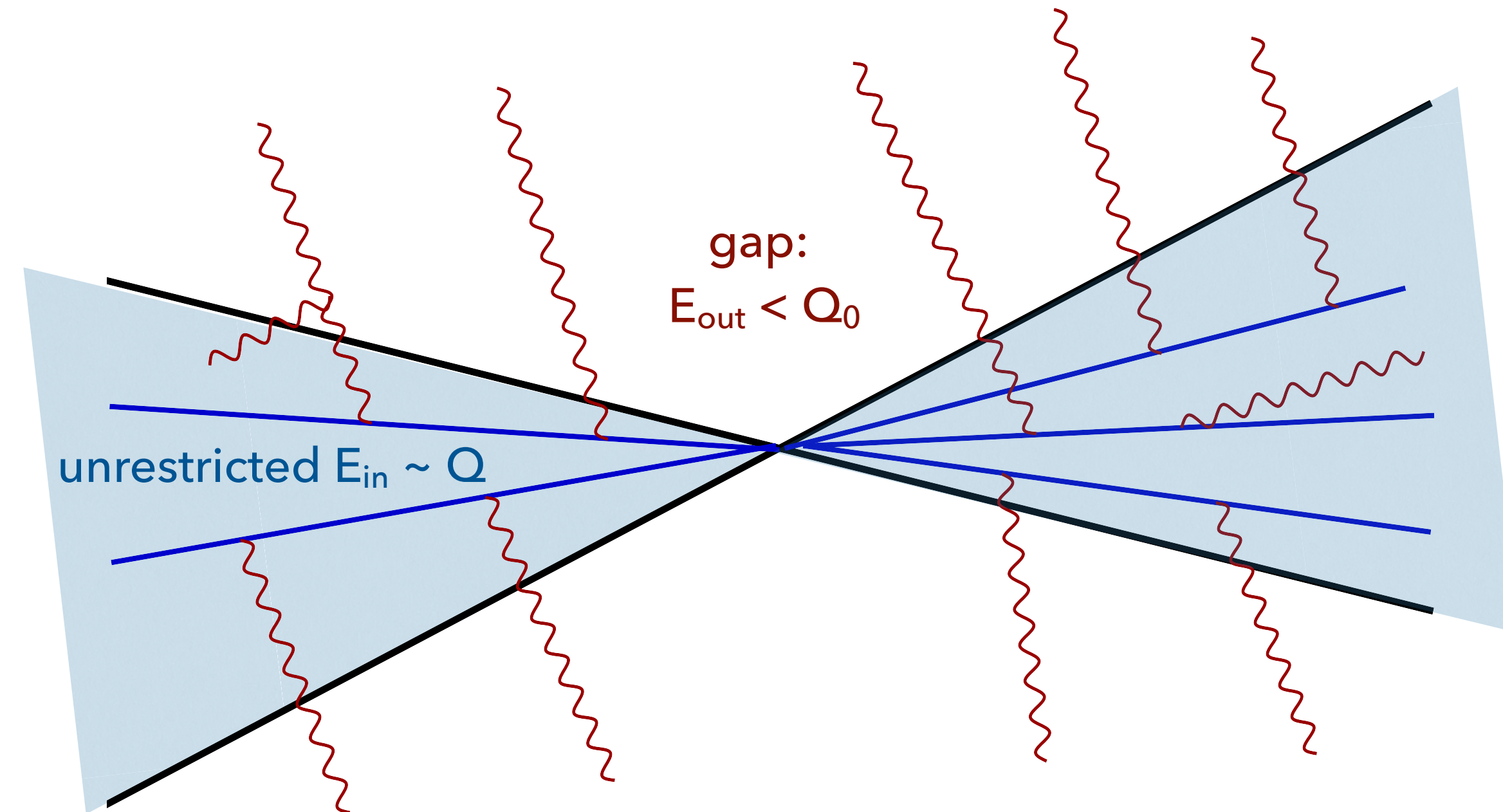
# GAP-BETWEEN-JETS OBSERVABLES



CERN Document Server, ATLAS-PHOTO-2018-022-6



# LARGE LOGARITHMS IN JET PROCESSES



Perturbative expansion includes "super-leading" logarithms:

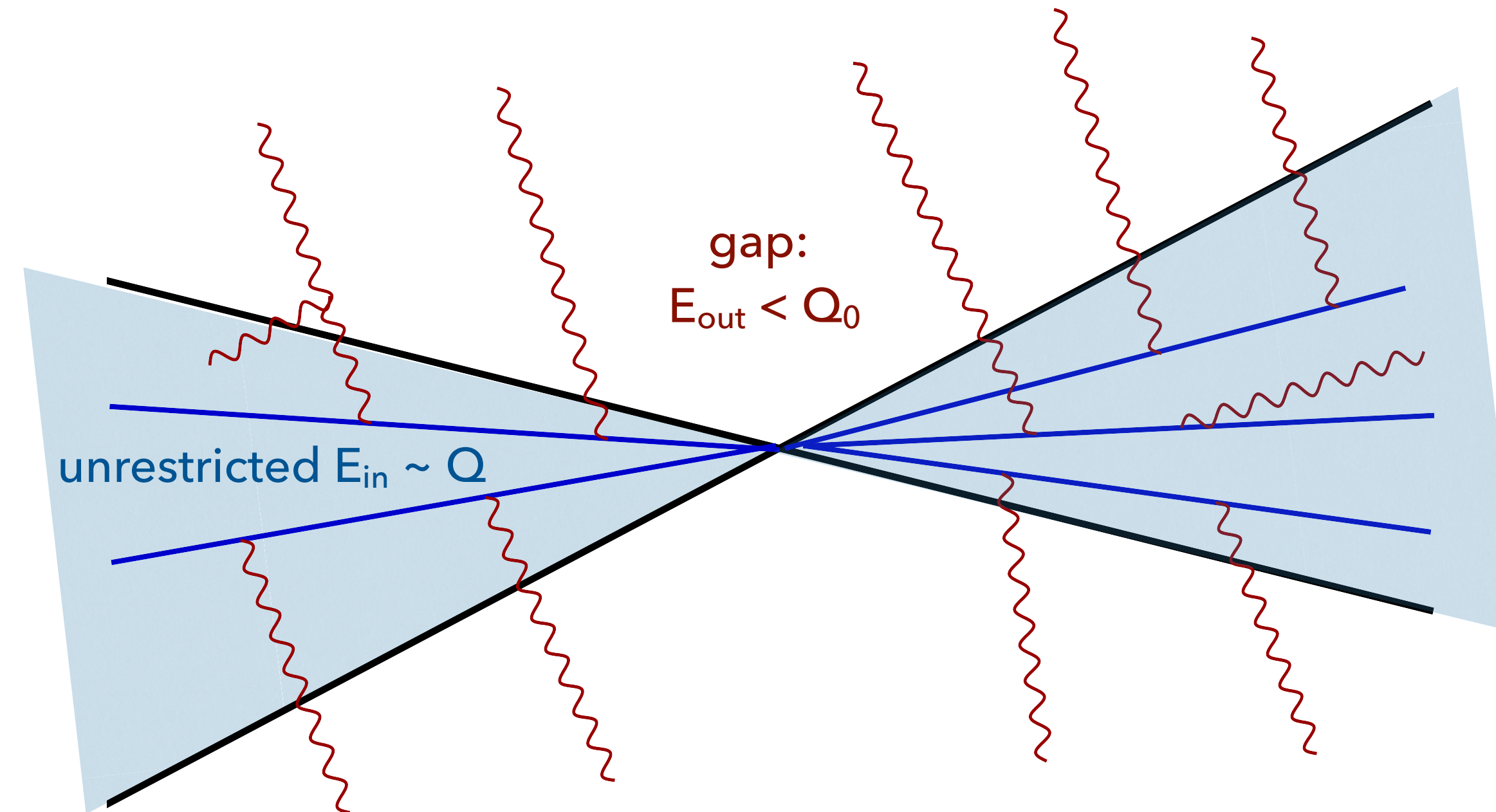
$$\sigma \sim \sigma_{\text{Born}} \times \left\{ 1 + \alpha_s L + \alpha_s^2 L^2 + \alpha_s^3 L^3 + \underbrace{\alpha_s^4 L^5 + \alpha_s^5 L^7 + \dots}_{\text{formally larger than } O(1)} \right\}$$

↑  
state-of-the-art

[Forshaw, Kyrieleis, Seymour (2006)]



# LARGE LOGARITHMS IN JET PROCESSES



Really, a double-logarithmic series starting at 3-loop order:

$$\sigma \sim \sigma_{\text{Born}} \times \left\{ 1 + \alpha_s L + \alpha_s^2 L^2 + (\alpha_s \pi^2) \left[ \alpha_s^2 L^3 + \alpha_s^3 L^5 + \dots \right] \right\}$$

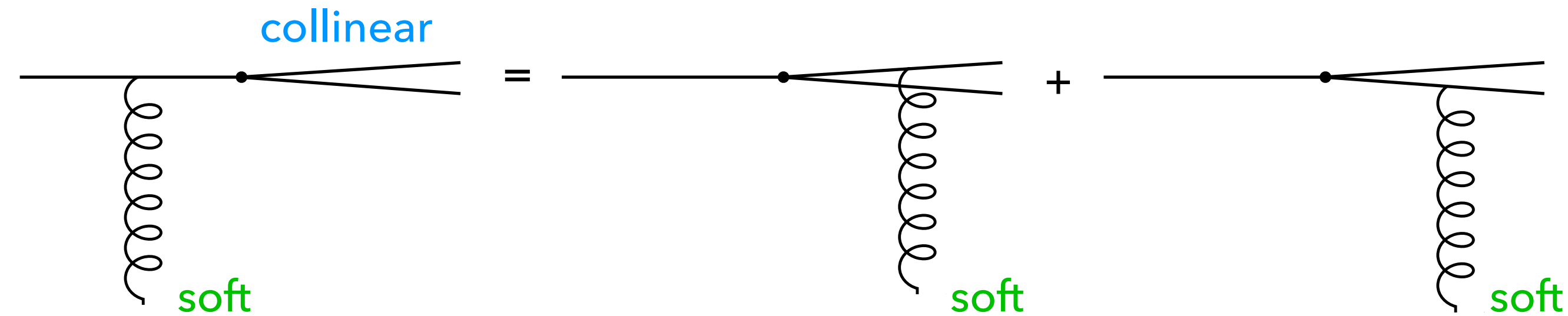
$(\Im m L)^2$

formally larger than  $O(1)$

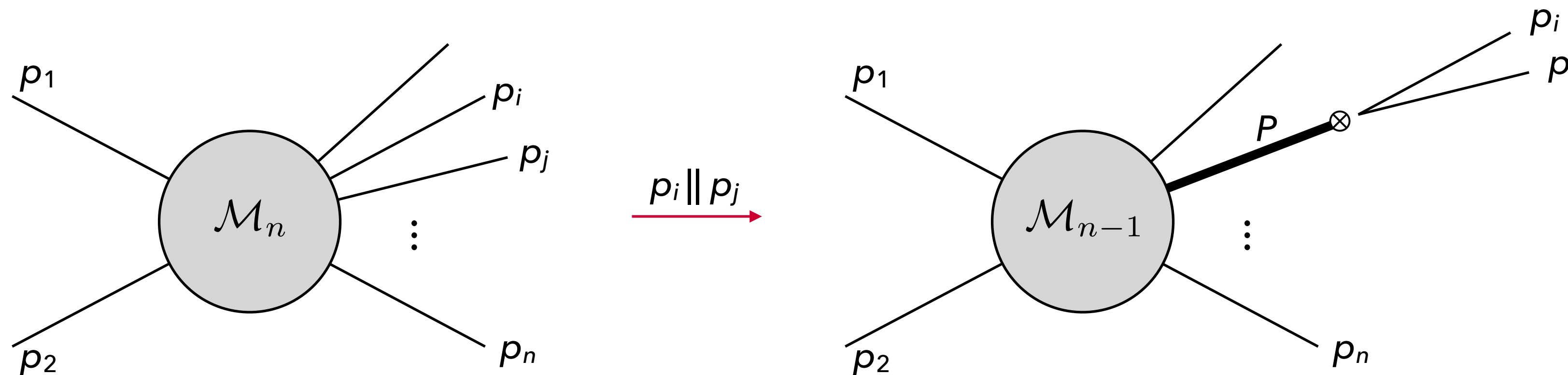
[Forshaw, Kyrieleis, Seymour (2006)]

# BREAKING OF COLOR COHERENCE

- ▶ **Color coherence holds** if all three particles are incoming or outgoing (time-like splitting):



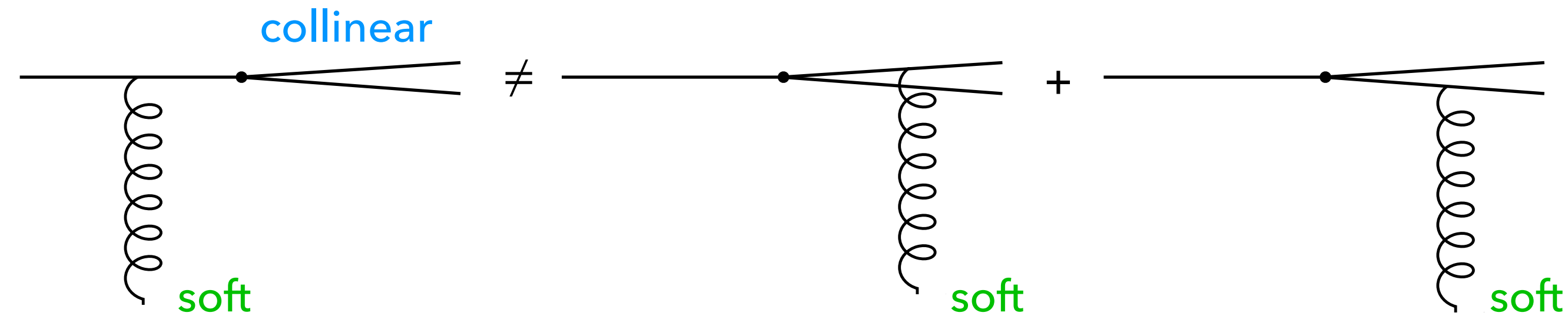
- ▶ **Then collinear factorization holds:**



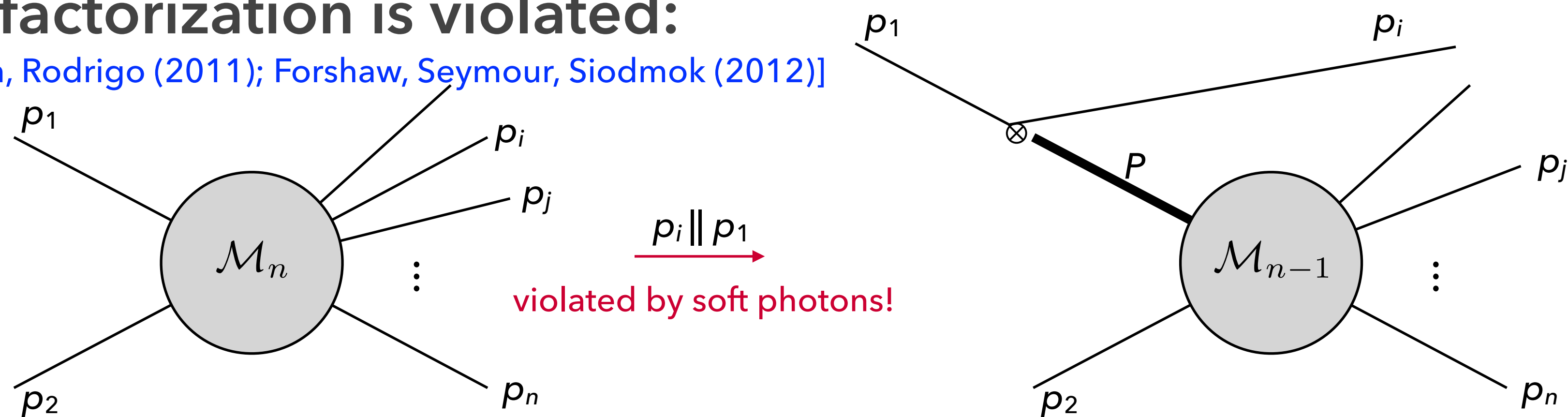


# BREAKING OF COLOR COHERENCE

- ▶ **Color coherence is broken** if not all particles are incoming/outgoing (space-like splitting), since both sides receive different phase factors:



- ▶ **Collinear factorization is violated:**  
[Catani, de Florian, Rodrigo (2011); Forshaw, Seymour, Siodmok (2012)]



# GAP-BETWEEN-JETS OBSERVABLES

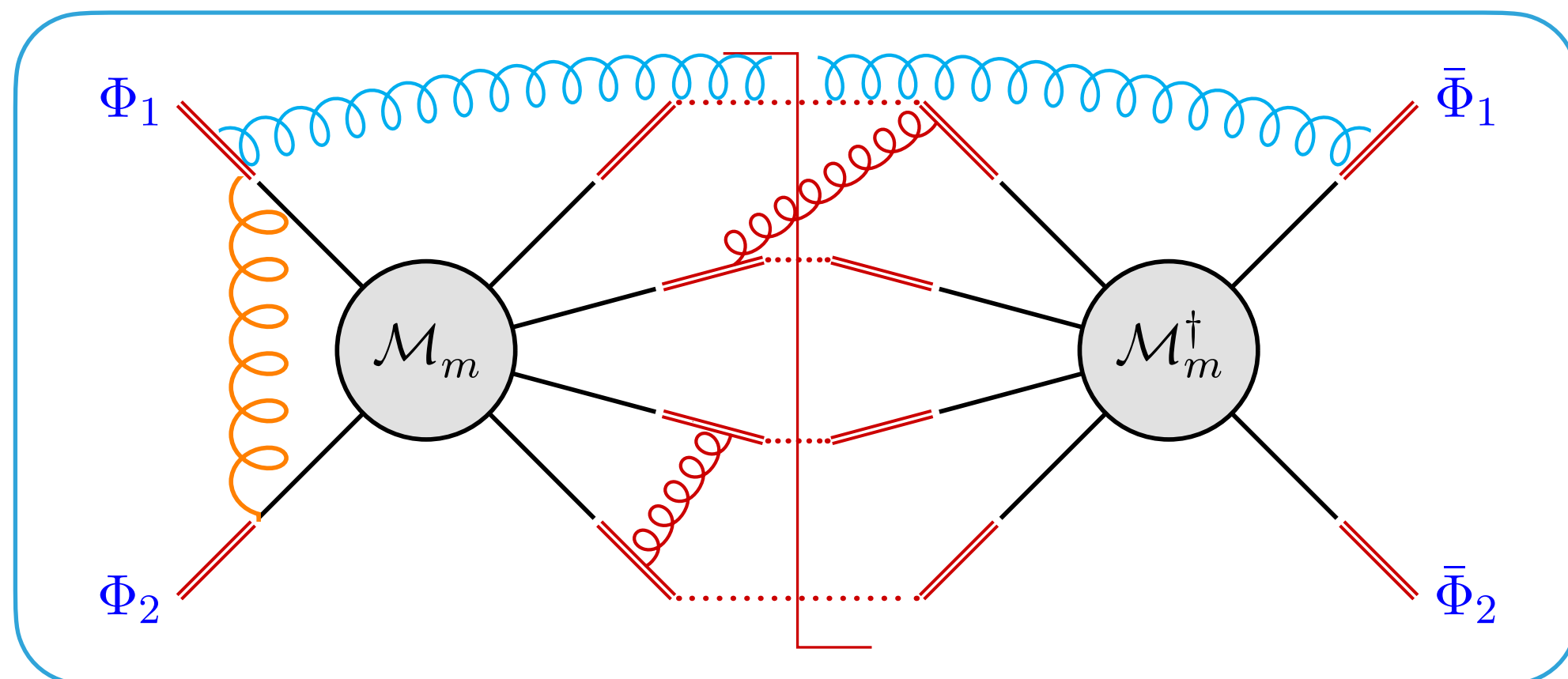
## SCET factorization theorem for $M$ -jet production at the LHC

$$\sigma(Q_0) = \sum_{m=m_0}^{\infty} \int d\xi_1 d\xi_2 \langle \mathcal{H}_m(\{\underline{n}\}, Q, \xi_1, \xi_2, \mu) \otimes \mathcal{W}_m(\{\underline{n}\}, Q_0, \xi_1, \xi_2, \mu) \rangle$$

[Becher, MN, Shao (2021);  
+ Stillger (2023)]

high scale

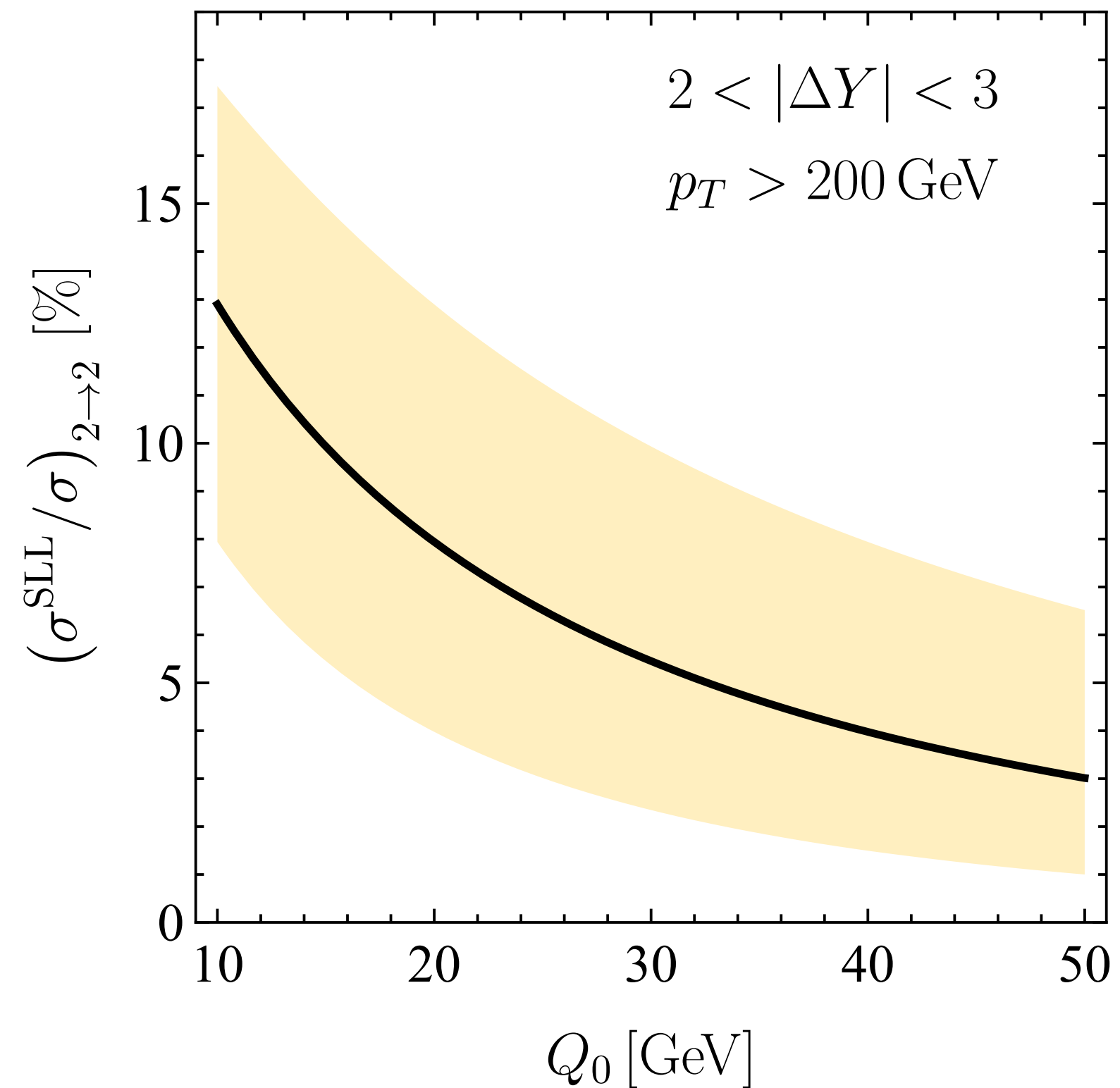
low scales  $Q_0$  and  $\Lambda_{\text{QCD}}$



- ▶ **new perspective** to think about non-global observables
- ▶ large logs can be **resummed using RGEs**
- ▶ **all-order understanding** of super-leading logarithms for arbitrary processes



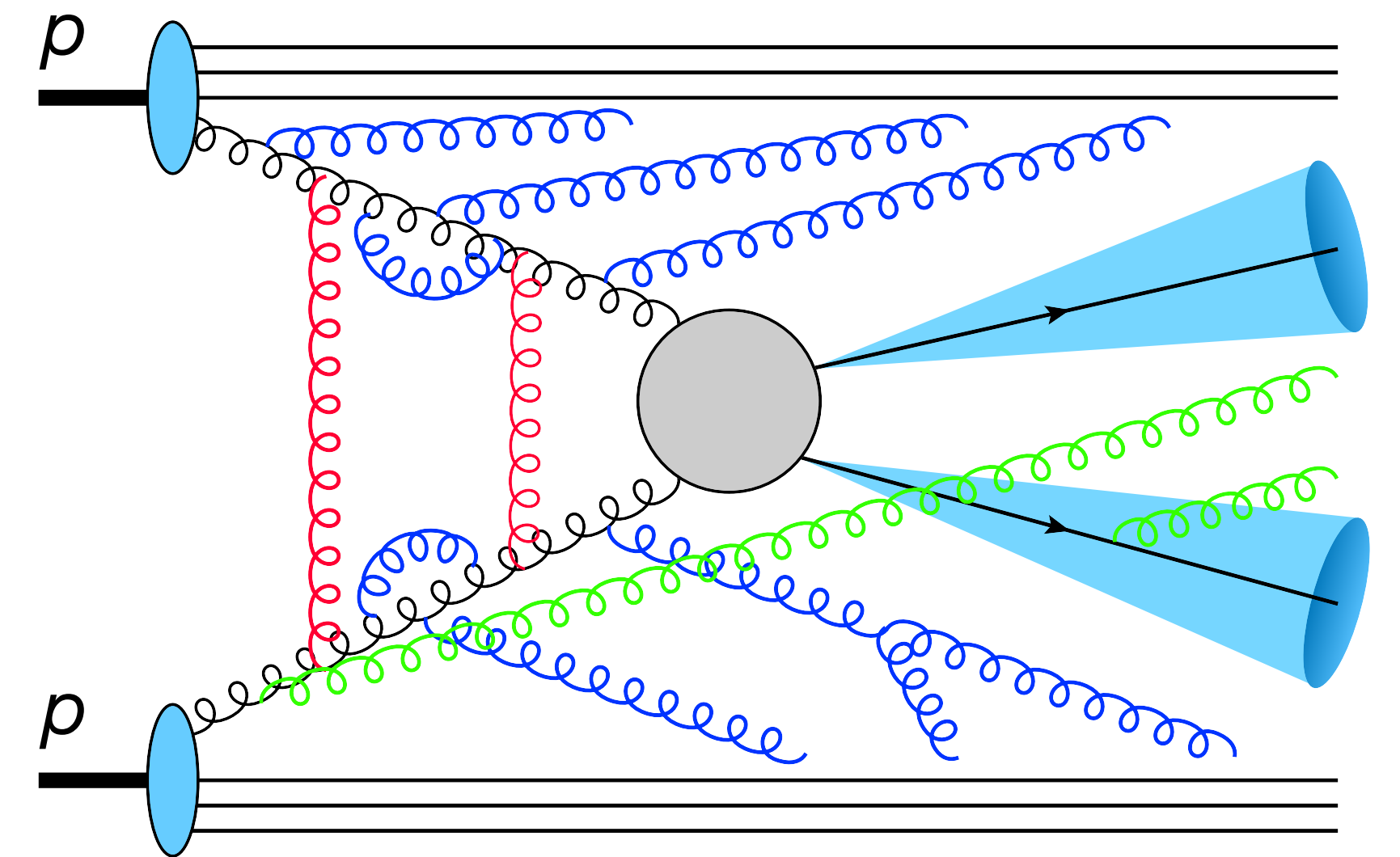
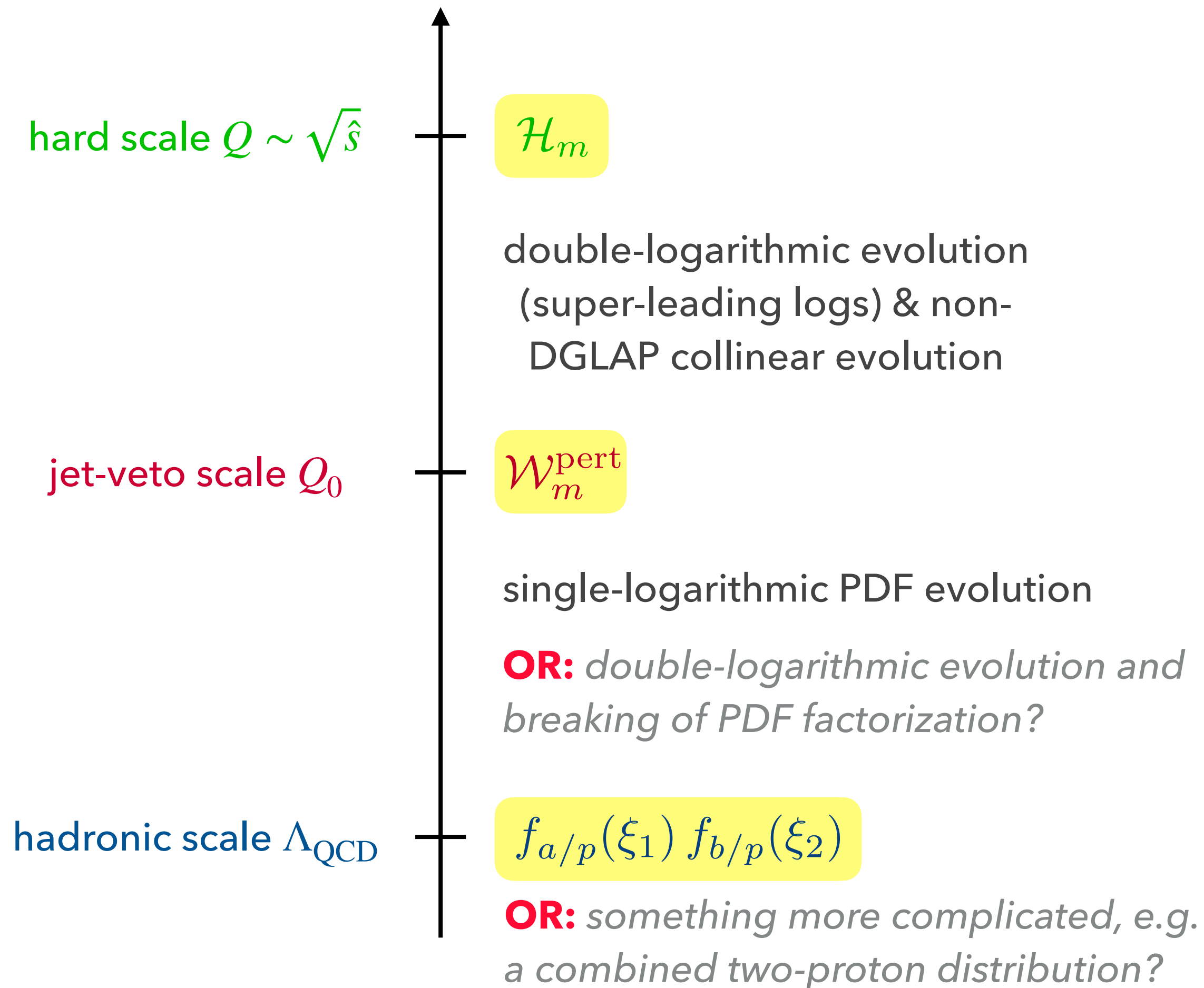
# GAP-BETWEEN-JETS OBSERVABLES



[Becher, Martinelli, MN, Schwienbacher (2024)]

**Figure 2:** SLL contribution to the  $pp \rightarrow 2$  jets cross section at the LHC as a function of the veto scale  $Q_0$ , for a center-of-mass energy  $\sqrt{s} = 13 \text{ TeV}$  and jet radius  $R = 0.6$ . The black curve shows the central result obtained in RG-improved perturbation theory. The perturbative uncertainties indicated by the yellow bands are obtained from the variation of the soft scale  $\mu_s$  by a factor 2 about its default value  $Q_0$ .

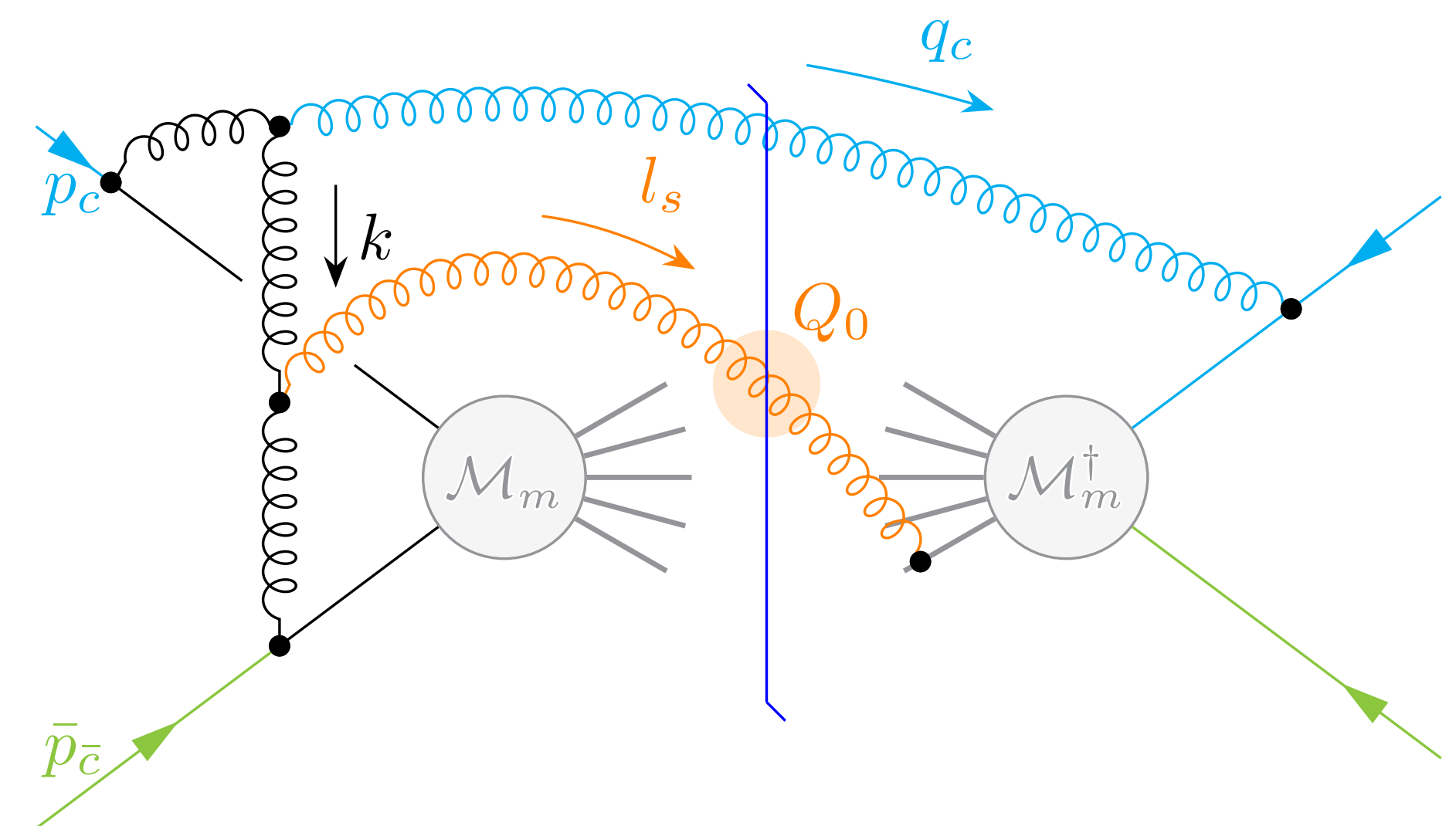
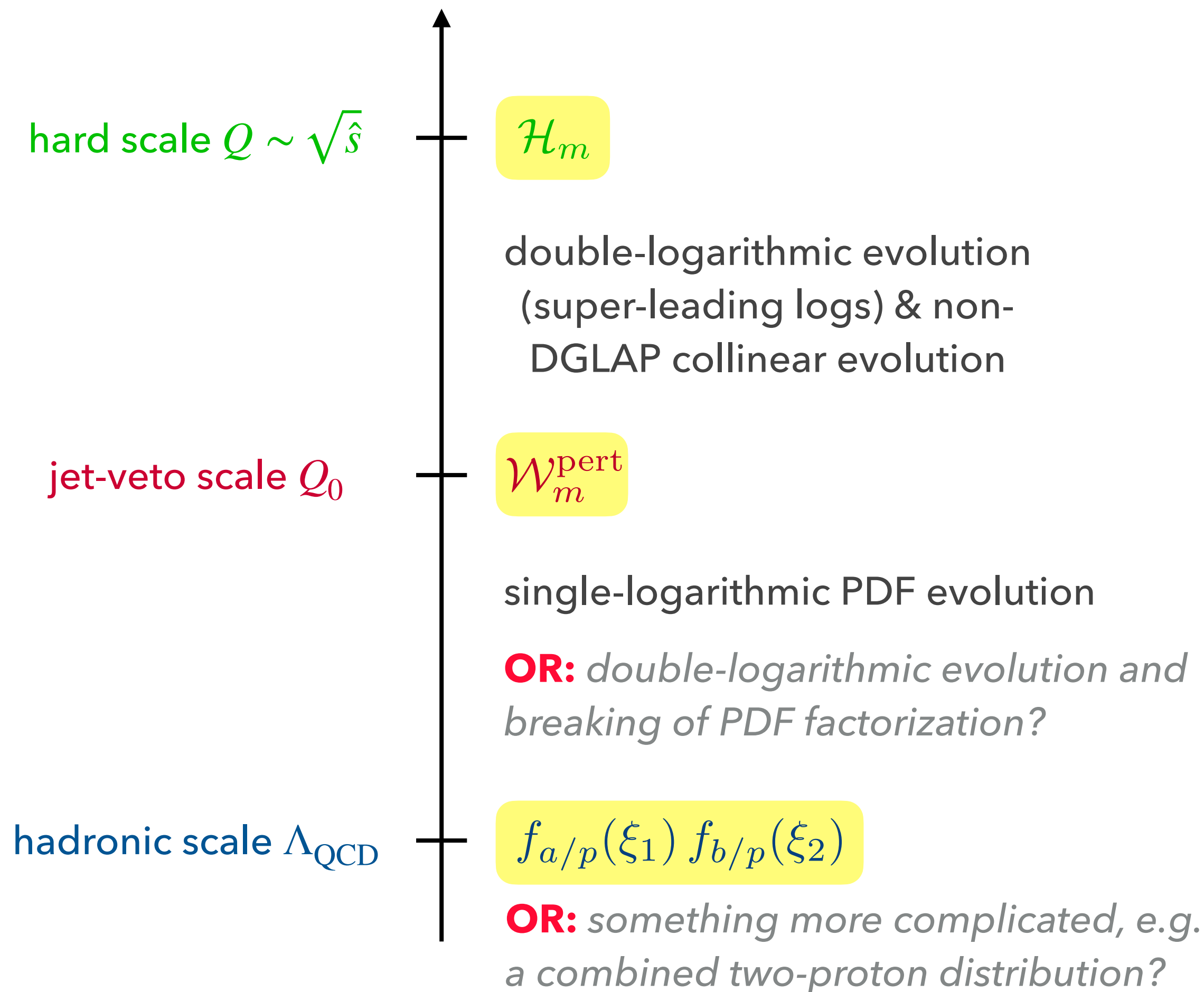
# STRUCTURE OF THE FACTORIZATION THEOREM ?



$$\sigma \stackrel{?}{\sim} \sum_m \mathcal{H}_m \otimes \mathcal{W}_m^{\text{pert}} \otimes f_{a/p} \otimes f_{b/p}$$



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[Becher, Hager, Jaskiewicz, MN, Schwienbacher (2024)]

## NEW INSIGHTS

- ▶ We have uncovered a new mechanism that reconciles the breaking of collinear factorization with unbroken PDF factorization
- ▶ In an interplay of space-like collinear splittings and soft emissions, perturbative Glauber gluons restore the factorization of the cross section by converting double-logarithmic into single-logarithmic evolution below the veto scale  $Q_0$  (shown explicitly up to 3-loop order) [\[Becher, Hager, Jaskiewicz, MN, Schwienbacher \(2024\)\]](#)
- ▶ In the future, it will be important to understand the all-order structure of these effects, paving the way for a proof of PDF factorization for a much wider class of observables!





Thank you for your friendship, Daniel