An experiment for *electron-hadron* scattering at the LHC



Before starting: Personal reflection

Huden Prests & (Proc. Suppl.) 179 + 180 (2008) August 2008

RAPID COMMUNICATIONS

ELSEVIER

PHOTON-LHC-2008

Proceedings of the International Workshop

on High-Energy Photon Collisions at the LHC CERN, Geneva, Switzerland

PHYSICAL REVIEW D, VOLUME 63, 071502(R)

Tagging two-photon production at the CERN Large Hadron Collider

K. Piotrzkowski* CERN, EP Division, CH-1211 Geneva 23, Switzerland and Institute of Nuclear Physics, Kawiory 26A, PL-30055 Kraków, Poland (Received 17 October 2000; published 6 March 2001)

Tagging two-photon interactions offers a significant extension of the CERN LHC physics program. The effective luminosity of high-energy $\gamma\gamma$ collisions reaches 1% of the proton-proton luminosity. The standard detector techniques used for measuring very forward proton scattering will allow a reliable separation of interesting two-photon interactions. Particularly exciting is the possibility of detecting exclusive Higgs boson production via the $\gamma\gamma$ fusion.

This paper was first rejected by *Physics Letters B* and *Zeit. f. Physik C...* and by now has 142 citations on *INSPIRE-HEP*

Edited by D. d'Enterria M. Klasen K. Piotrzkowski

22-28 April 2008

CMS sees first direct evidence for $\gamma\gamma \rightarrow WW$



VOLUME 53 NUMBER 6 JULY/AUGUST 2013

collected at √s=7 TeV and to obtain the first direct evidence of the γγ→WW process. Fully leptonic W-boson decays have been measured in final states characterized by opposite-sign and opposite-flavour lepton pairs where one W decays into an electron and a neutrino, the other into a muon and a neutrino (both neutrinos leave undetected). The leptons were required to have: transverse momenta p,>20 GeV/c and pseudorapidity

www.ebmierohniks.orm

would be expected within the Standard

Model, allows stringent limits on anomalous quartic \gamma \WW couplings to be derived. These surpass the previous best limits, set at the Large Electron—Positron collider and at the Tevatron, by up to two orders of magnitude (figure 3).

 Further reading CMS collaboration 2013 arXiv:1305.5596 [hep-ex] submitted to JHEP.

Lesson learned: it takes time, persistence and hard work to open new directions, but it is very much worth it!



AGH



1st workshop on LHeC/FCC-eh beam dynamics & machine-detector interface Kraków, Poland September 19-21, 2024

Overview
Call for Abstracts
Timetable
Contribution List
My Conference
My Contributions
Registration
Participant List
Practical information
Videoconference

O

Timetable

https://indico.cern.ch/event/1423983/

Thu 19/09	Fri 20/09	All days					>		
			😑 Print	PDF	Full screen	Detailed view	Filter		
09:00 Int	Introduction to the LHeC machine Oliver Bruning								
D-1	D-10 D-czarna (3rd floor), AGH University of Kraków 09:00 - 09:25								
Int	Introduction to the machine-detector interface studies Bernhard Holzer								
D-1	D-10 D-czarna (3rd floor), AGH University of Kraków 09:25 - 09:50								
Pro	Proton optics studies Tiziana Von Witzleben								
10:00 D-1	D-10 D-czarna (3rd floor), AGH University of Kraków 09:50 - 10:								
Ele	Electron optics studies Kevin Daniel Joel Andre								
D-1	D-10 D-czarna (3rd floor), AGH University of Kraków 10:15 - 10:40								
Co	ffee break								
11:00 D-1	10 D-czarna (3r	d floor), AGH Uni	versity of Kraków				10:40 - 11:10		
Sy	nchrotron radi	ations studies				Lauren	t Forthomme 🤞		
D-1	D-10 D-czarna (3rd floor), AGH University of Kraków						11:10 - 11:35		
The HERA ep Interaction Regions - Learned Lessons						Uwe	Schneekloth		
D-1	D-10 D-czarna (3rd floor), AGH University of Kraków 11:35 -								
12:00 EIC	C machine-dete	ector interface e	xperience			Ai	ndrii Natochii 🤞		
D-1	D-10 D-czarna (3rd floor), AGH University of Kraków 12:00 - 12:25								

International advisory committee B. Holzer (CERN) P. Kostka (DESY & Univ. Liverpool)

Y. Yamazaki (Kobe University) J. d'Hondt (Vrije Univ. Brussel)

Local organising committee

K. Piotrzkowski (AGH) L. Forthomme (ÅGH)

Electron-Hadron collisions at TeV scales

TOPICAL REVIEW • OPEN ACCESS

The Large Hadron–Electron Collider at the HL-LHC

P Agostini¹, H Aksakal², S Alekhin^{3,4}, P P Allport⁵, N Andari⁶, K D J Andre^{7,8}, D Angal-S Antusch¹¹, L Aperio Bella¹², L Apolinario¹³ + Show full author list Published 20 December 2021 • © 2021 The Author(s). Published by IOP Publishing Ltd Journal of Physics G: Nuclear and Particle Physics, Volume 48, Number 11

Reminder:

LHeC CDR in 2012 – proposing **concurrent** *ep* collisions (above 1 TeV) at the LHC

New LH*e*C proposal in 2020 – 337 authors from 156 institutions

5th FCC

Includes discussion of FCC-eh physics (1.2 \rightarrow 3.5 TeV)

Eur. Phys. J. C (2019) 79:474 https://doi.org/10.1140/epjc/s10052-019-6904-3

Derrierry	1.1	Physics scenarios after the LHC and the open questions
Review	1.2	The role of FCC-ee
	1.3	The role of FCC-hh
	1.4	The role of FCC-eh
FCC Phy	sic	s Opportunities

https://indico.cern.ch/event/1066234/

Large Hadron electron Collider Hecluminosity = 1000 × HERA

LHeC is NOT simply super-HERA!

LHeC is not just "super QCD machine" – it is much more:

Novel powerful lab for Electroweak & Higgs physics Sensitivities to **new BSM signatures** High energy eA collider (very complementary to EIC)

Large Hadron electron Collider

Energy Recovery Linac technology, or on-going revolution in high energy electron acceleration techniques

Machine Parameters and Operation - ep

arXiv:2007.14401

	LHeC				Unit	Parameter
ERL technology resulte	Dedicated	Run 6	Run 5	CDR		
in major broaktbrough	50	50	30	60	GeV	E_e
in major breakthough	2.2	2.2	2.2	1.7	10^{11}	N_p
$for \mid Hac (at 100 NANA)$	2.5	2.5	2.5	3.7	$\mu \mathrm{m}$	ϵ_p
	50	20	15	6.4	\mathbf{mA}	I_e
	7.8	3.1	2.3	1	10^{9}	N_e
\rightarrow 10 x luminosity	7	7	10	10	\mathbf{cm}	β^*
	23	9	5	1	$10^{33}{ m cm}^{-2}{ m s}^{-1}$	Luminosity

Energy Recovery Linac (green) technology

"Energy Recovery is at the threshold of becoming a key means for the advancement of accelerators. **Recycling the kinetic energy of a used beam for accelerating a newly injected beam**, i.e. **reducing the power consumption***, utilising the high injector brightness and dumping at injection energy: these are the key elements of a novel accelerator concept, invented half a century ago**. The potential of this technique may be compared with the finest innovations of accelerator technology such as by Widerøe, Lawrence, Veksler, Kerst, van der Meer and others during the past century. Innovations of such depth are rare, and their impact is only approximately predictable. **The fundamental principles of Energy-recovery linacs (ERLs) have now been successfully demonstrated across the globe**. There can no longer be any doubt that an ERL can be built and achieve its goals." *-- European Strategy for Particle Physics – Accelerator R&D Roadmap* (CERN Yellow Report) https://arxiv.org/abs/2201.07895

*) Even by an order of magnitude

**) M. Tigner – A Possible Apparatus for Electron Clashing-Beam Experiments, Nuovo Cimento 10 (1965) 1228 ⇒⇒

Quite surprising gravitational analogy – note 2036 date https://www.youtube.com/watch?v=6RiYXI1Tfu4



ERL@LHeC as Relay Short Track Speed Skating



6×ERL@HL-LHC

ERL geometry



- Two SC linac accelerators
- three-pass return arcs

• ERL main parameters

Parameter	\mathbf{Unit}	Value
Beam energy	GeV	50
Bunch charge	pC	499
Bunch spacing	ns	24.95
Electron current	$\mathbf{m}\mathbf{A}$	20 🔶
trans. norm. emittance	$\mu{ m m}$	30
RF frequency	MHz	801.58
Acceleration gradient	MV/m	20.06
Total length	m	6665

• Q-parameter of 5-cell prototype



<u>LHeC Linac-Ring Option: Power & Cost considerations</u>



2 Super Conducting Linacs with Energy Recovery & high current (> 6mA)



Efficient Concept

→ re-circulation implies cost effective use of the SRF investment

 \rightarrow ERL implies efficient operation and higher performance reach

K. Piotrzkowski - HEP Seminar at UW - 8/11/2024



Experiment for *eh* <u>and</u> *hh* scattering @ IP2

Eur. Phys. J. C (2022) 82:40 https://doi.org/10.1140/epjc/s10052-021-09967-z

Regular Article - Experimental Physics



An experiment for electron-hadron scattering at the LHC

K. D. J. André^{1,2}, L. Aperio Bella³, N. Armesto^{4,a}, S. A. Bogacz⁵, D. Britzger⁶, O. S. Brüning¹, M. D'Onofrio², E. G. Ferreiro⁴, O. Fischer², C. Gwenlan⁷, B. J. Holzer¹, M. Klein², U. Klein², F. Kocak⁸, P. Kostka², M. Kumar⁹, B. Mellado^{9,10}, J. G. Milhano^{11,12}, P. R. Newman¹³, K. Piotrzkowski¹⁴, A. Polini¹⁵, X. Ruan⁹, S. Russenschuk¹, C. Schwanenberger³, E. Vilella-Figueras², Y. Yamazaki¹⁶

In 2019 proposal of Alice 3 at IP2 of HL-LHC was presented – our paper showed that it is feasible to make experiments of

ep vs. ppANDeA vs. AAwith SAME (Alice 3e...) detector !

Fig. 17 Schematic view of the three beams in the interaction region. Collisions between electrons and proton beam 1 and a well separated proton beam 2

HL-LHC Upgrade

- Final focusing system is changed from NbTi to Nb3Sn
- D1 magnet superconducting
- crab cavities are inserted in IR 1 and IR 5
- Q4 is moved relative to the IP

Parameter	Unit	Value HL-LHC	LHC IR $1/5$ Q $1/Q2/Q3$
Magnetic field gradient	T/m	132.6	200/205
Magnetic length	m	4.20/7.15	6.3/5.5/6.3
Aperture radius	$\mathbf{m}\mathbf{m}$	75	22.2/28.95
Number of turns per pole		50	
Conductor material		Nb_3Sn	NbTi

Implement this triplet in IR2 -> Gain of aperture!

01/03/2024

Experiment for electron-hadron scattering @ IP2

- The detector is required to have a magnet system consisting of **a central solenoid along with a dipole system** to steer the electron beam allowing for head-on *eh* collisions at the interaction point;

- The **non-interacting proton/ion beam** has to bypass the *ep* interaction yet to be guided through the same beam pipe housing the interacting electron and proton/ion beams;

- The shape of the beam pipe has to allow for the electron beam generated **synchrotron fan** to leave the interaction region unaffected and with minimal back-scattering;

- Good vertex resolution implies a small radius and thin beam pipe optimised in view of synchrotron radiation and background effects;

- The tracking and calorimetry in the forward and backward directions are set up to take into account the extreme asymmetry of the DIS production kinematics, see [1], with multi-TeV energies emitted in the forward, proton beam direction while the electromagnetic and hadron energies emitted backwards are limited by the electron beam energy.

- Very forward and backward detectors have to be set up to access diffractive produced events and to tag photoproduction processes besides measuring the luminosity with high precision in Bether–Heitler scattering, respectively.

https://link.springer.com/article/10.1140/epjc/s10052-021-09967-z

Experiment for eh and hh scattering @ IP2

"As described above in Sect. 4.6, the new accelerator optics is able to provide collisions for eh and hh configurations in the same interaction point. As a consequence and if confirmed by further study, IP2 could indeed house one, common multi-purpose detector serving for all of these, mostly related physics programs, of *ep*, *pp*, *eA*, pA and AA interactions, with high precision and large acceptance, and the **unique** advantage for cross-calibration of performance and physics."

Fig. 24 Side view of a first design of the LHeC detector for both eh and hh collisions, where the detector coverage of the backward (electron) direction is extended to match that for the forward (hadron) direction.

Experiment for *eh* (and *hh*) scattering @ IP2

Huge advantage for *eh* experiments \Rightarrow **total inelastic cross-section**:

Event pileup is very small/negligible at LHeC

Data streaming aka "no triggering" is possible (as at EIC)

Much broader types of final states/decay channels are feasible!

Unique capabilities (with about 1000 fb⁻¹ of collected data in total)

Electron-Hadron Scattering @ LHC

LHeC

- Rich physics program at all scales
 - Higgs physics in NC and CC DIS
 - Top quark production
 - BSM physics and searches
 - Precision QCD
 - Proton structure, substructure, strong coupling constant, jet physics, heavy quarks, ...
 - Electroweak physics
 - Heavy ion programme

Several highlights $\Rightarrow \Rightarrow$

DIS @ LHeC

Deep-inelastic electron-proton scattering mediated in spacelike regime, by γ, γΖ, Ζ or W-boson exchange

10⁵

 Q^2 [GeV²]

10⁴

10³

LHeC as Gauge Boson Collider

WW, ZZ and $\gamma\gamma$ fusion

(in clean environment)

(Clean) Higgs factory @ LHeC

DIS Higgs Production Cross Section 4 Log(ep→HX) 3 FCC-eh 2 LHeC 1 HERA 0 -1 -2 -3 -4 -5 EIC -6 -7 cms energy /TeV

- Higgs-production cross section ~ 200pb
- Sensitivity to six decay channels bb, WW, gg, ττ, cc, ZZ

Higgs in CC and NC DIS

K. Piotrzkowski - HEP Seminar at UW - 8/11/2024

Electron-Hadron Scattering @ LHC

- Parton distribution functions (PDFs) of the proton with unprecedented precision
- Full determination of all flavors

eA scattering at LHeC

Unprecedented access to (x,Q^2) kinematic plane in *eA*:

• coverage extended with respect to EIC by up to **2 orders of magnitude**

• DIS with nuclei down to and below $x = 10^{-5}$ in **perturbative** regime \Rightarrow saturation scale (non-linearities) in fully perturbative regime

LHeC updates in Praha @ ICHEP2024

The LHeC and FCC-eh experimental program, Jorgen D'Hondt

https://indico.cern.ch/event/1291157/contributions/5890135/

A detector for future DIS at the energy frontier, Laurent Forthomme

https://indico.cern.ch/event/1291157/contributions/5888179/

The general-purpose LHeC and FCC-eh high-energy precision programme: Top and EW measurements, Daniel Britzger <u>https://indico.cern.ch/event/1291157/contributions/5896101/</u>

Higgs precision physics in electron-proton scattering at CERN, Uta Klein

https://indico.cern.ch/event/1291157/contributions/5876815/

Proton and nuclear structure from EIC and HERA to LHeC and FCC-eh, Claire Gwenlan <u>https://indico.cern.ch/event/1291157/contributions/5876815/</u>

High energy γγ interactions at the LHeC, Krzysztof Piotrzkowski https://indico.cern.ch/event/1291157/contributions/5905430/

Event display of a DDG4/Geant4 simulation of a central exclusive $ep \rightarrow e(\gamma \gamma \rightarrow \mu^+ \mu^-)p$ event as generated by CepGen inside the LHeC detector.

K. Piotrzkowski - HEP Seminar at UW - 8/11/2024

Aftermath of two "earthquakes" last winter...

Bottom line

FCC-ee (in 2048)

VS.

CEPC (in 2037)

"issue" to be

resolved by

end of 2025

CERN SUPERCOLLIDER IN QUESTION AS TOP FUNDER CRITICIZES COST

Germany has raised doubts about the affordability of the Large Hadron Collider's planned successor.

By Davide Castelvecchi

lans for a 91-kilometre European particle accelerator are facing a challenge after the German government said that the project was unaffordable.

CERN, the European particle-physics laboratory outside Geneva, Switzerland, has embarked on a feasibility study for the first stage of its Future Circular Collider (FCC). This stage, known as FCC-ee, would involve a machine to smash electrons together with antielectrons, and could cost 15 billion Swiss francs (US\$17 billion) by the time it is completed in the mid-2040s. The initial phase of that study, focusing on the technical aspects, had a positive outcome, CERN said in February.

But Germany, which already contributes €267 million (US\$290 million) annually to CERN – some 20% of the lab's budget – cannot afford to spend more, said Eckart Lilienthal of the country's Federal Ministry of Education and Research (BMBF) on 23 May, at a workshop for particle physicists in Bonn, Germany.

The preliminary cost estimates for the FCC-ee "are subject to a large number of uncertainties, the effects of which are still largely unknown", a BMBF spokesperson told *Nature*. "The financing plan is extremely vague and requires a high level of commitment from external partners, which is neither assured nor even in prospect at the present time. Given these conditions, Germany cannot support funding of the project at this point."

The German government had already made its position known to CERN at a closed meeting in February. But Lilienthal's remarks surprised some researchers, says Jenny List, a particle physicist at the German Electron Synchrotron (DESY) in Hamburg, who presented alternatives to the FCC-ee at the Bonn workshop. "Clearly, this is still sinking in with the German particle-physics community," she says.

CERN's research director, Joachim Mnich, played down the implications of Lilienthal's remarks. "The questions and concerns he raised about the FCC are not new to us and they are all being addressed in the FCC feasibility study," he says.

"All comments and feedback received from our member states will be taken into account in the preparation for the final report," says CERN spokesperson Arnaud Marsollier.

Future Higgs factory

The main goal of the FCC-ee would be to mass-produce the Higgs boson, the particle that was discovered in 2012 at CERN's

CHINA HOPES TO BUILD WORLD'S BIGGEST PARTICLE COLLIDER

The facility would be cheaper, bigger and faster to construct than one proposed by European scientists.

By Gemma Conroy

hina hopes to build a US\$5-billion particle smasher in the next three years, beating Europe's proposed mega-collider to the punch. The 100-kilometre Circular Electron Positron Collider (CEPC) would aim to measure the Higgs boson – a mysterious particle that gives everything mass – in exquisite detail. Such information could answer fundamental questions about how the Universe evolved and why particles interact in the way that they do.

Next year, the proposal for the CEPC will go before the Chinese government for possible inclusion in the country's next five-year plan. If it can win government support, construction could begin in 2027 and would take around a decade, according to a technical-design report published on 3 June (J. Gao Radiat. Detect. Technol. Methods https://doi.org/ m4kg; 2024). The report estimates that the supersized collider would cost 36.4 billion yuan (US\$5.2 billion), making it considerably cheaper to build and run than Europe's US\$17-billion Future Circular Collider (FCC). Construction on the European facility will begin in the 2030s if it receives government approval.

Inside its enormous underground tunnel, the CEPC would smash together electrons and their antiparticles, positrons, at extraordinarily high energies to generate millions of Higgs bosons. The sheer number of these would allow researchers to study the particle in greater detail than ever before, says Andrew Cohen, a theoretical physicist at the Hong Kong University of Science and Technology. By measuring the Higgs more precisely, researchers will be able to explore questions that reach beyond the Standard Model - the leading but incomplete theory of what the cosmos is made of – such as the nature of dark matter and why there is more ordinary matter than antimatter in the Universe.

The latest report includes a detailed blueprint of the accelerator's layout design and component prototypes, says physicist Wang Yifang, director of the Chinese Academy of Science's Institute of High Energy Physics (IHEP) in Beijing. It also includes assessments of three potential sites: Qinhuangdao, Changsha and Huzhou. "We are now confident this is a real machine that we can build," says Wang.

Many of the components that are planned for China's mega machine are already being tested at other facilities in the country, says

Nature | Vol 630 | 20 June 2024 | 539 Piotrzkowski - HEP Seminar at UW - 8/11/202

LHeC: very personal outlook

[It is likely CEPC funding will be approved in 2025]

LHeC concept is fully developed and is ready to be thoroughly considered by ESPP Update as next big project at CERN

If by 2027 CERN/Europe decide to make LHeC, it seems feasible by 2036 to get 20 GeV electron beam at IP2 for concurrent *ep* (and *eA*) collisions at 0.75 TeV, and final "stand-alone" LH*e*C at 1.2 TeV in 2040s

In parallel, novel acceleration techniques can be vigorously pursued, as acceleration in plasma, or/and concept of multi-TeV muon collider

LHeC: very personal outlook

If by 2027 CERN/Europe decide to make LHeC, it seems feasible by 2036 to get 20 GeV electron beam at IP2 for **concurrent** *ep* (and *eA*) collisions at **0.75 TeV**, providing also perfect LHeC staging

win-win-win for LHC science programme

making unique LHeC science + improving precision of pp experiments
+ enhancing HI research with Alice 3e [data streaming already in use in Alice!]

ESPP white paper preparation meeting for LHeC

- Friday 15 Nov 2024, 08:00 → 18:30 Europe/Zurich
- 6/2-024 BE Auditorium Meyrin (CERN)

Jorgen D'Hondt (Vrije Universiteit Brussel (BE)), Nestor Armesto Perez (Universidade de Santiago

Yannis Papaphilippou (CERN)

ZOOM ESPP white paper preparation meeting for ep/eA

https://indico.cern.ch/event/1456583/

LHeC: Summary

LHeC will complete the HL-LHC science in profound & relevant ways – in **QCD**, HF, top, **Higgs** & Electroweak sectors

In addition, PDF determined at LHeC will **significantly decrease systematic uncertainties** of *pp* experiments at HL-LHC

LHeC offers practically ideal conditions for studying high energy $\gamma\gamma$ interactions (and other exclusive processes) and will open new era in eA studies

NEW detector and beamline designs have been developed for IP2, accommodating both *eh* <u>and</u> *hh* collisions (\Rightarrow stage 1 LH*e*C "includes" ALICE 3)

LHeC: Final personal remarks

Extracting best science at LHC is our **duty** – LH*e*C will open vast new fields of research <u>and</u> significantly strengthen **concurrent** hadron-hadron research at **cost below that of EIC!**

Join us! For example, by checking how much **your** HL-LHC research would profit from LHeC!

Or, just help it happen...remember – ESPP update will shape HEP for next >25 years

Reminder: LHeC has been driving developments of **green** ERL technology for future colliders [**very appropriate response to demands of our time**] \Rightarrow strong hadron cooling at EIC, new designs of Next Linear Collider & **electron beam injector for FCC**-*ee* + electron beam for FCC-*eh*

Timeline for the update of the European Strategy for Particle Physics

Thank you for attention!

For interested...

Two very well financed four-year scholarships for doctoral students are available at AGH from October 2025, dedicated to the LHeC (and CMS) research – one more phenomenology- and one more detector-oriented

Contact: piotrzkowski@agh.edu.pl

In addition, **up to six-months LHeC project positions** (including extended stays at CERN) can be offered to both undergraduate and graduate candidates – starting from January 2025!

Backup slides

Summary LHeC / FCC-eh

- Unique machine for exploring the TeV Center of Mass region of HEP with ep
- Maximum Infrastructure exploitation of the LHC and FCC!
- Moderate cost [compared to ILC, CLIC or FCC]
- Unique oportunity no other machine can provide ep @ TeV CME
- Technology driver with many spin off benefits ERL & SRF
 - → Sustainable accelerator operation!
- Unique physics program
- Modular design with several operation phases!

→ LHeC, FCC-ee injector, FCC-eh

LHeC demonstrator: Powerful ERL for Experiments (PERLE)

in <u>Orsay</u>

[J. Phys G]

Nuclear particle physics with electron-ion scattering at the LHeC

• "The LHeC will be able to test and establish or exclude the phenomenon of parton saturation at low *x* in protons and nuclei. [...] The LHeC will be a unique machine with which to address both of their variations, such that the saturation concepts can be precisely tested."

• "LHeC machine in *eA* mode will have a huge impact on physics explored in *pA* and *AA* collisions, see section 9.7, where it will provide vital input and constraints on the 'baseline' initial state in nuclear collisions and measurements of the impact of a cold nuclear medium on hard probes and the effects of hadronisation. It will also explore the effect of the initial-state correlations on the final-state observables, which are relevant in order to understand collectivity in small systems explored in *pp* or *pA* collisions."

• "The measurements of diffraction of protons and nuclei as well as the inclusive structure functions in the nuclear case will allow us to explore the very important relation between nuclear shadowing and diffraction [...]

• Similarly to the proton case, DVCS and exclusive vector-meson production will provide unique insight into 3D nuclear structure."

https://iopscience.iop.org/article/10.1088/1361-6471/abf3ba