

# FLAVOR PHYSICS

(PART II: the *B* factories)



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CHIPP Winter School 2012  
Engelberg, Switzerland

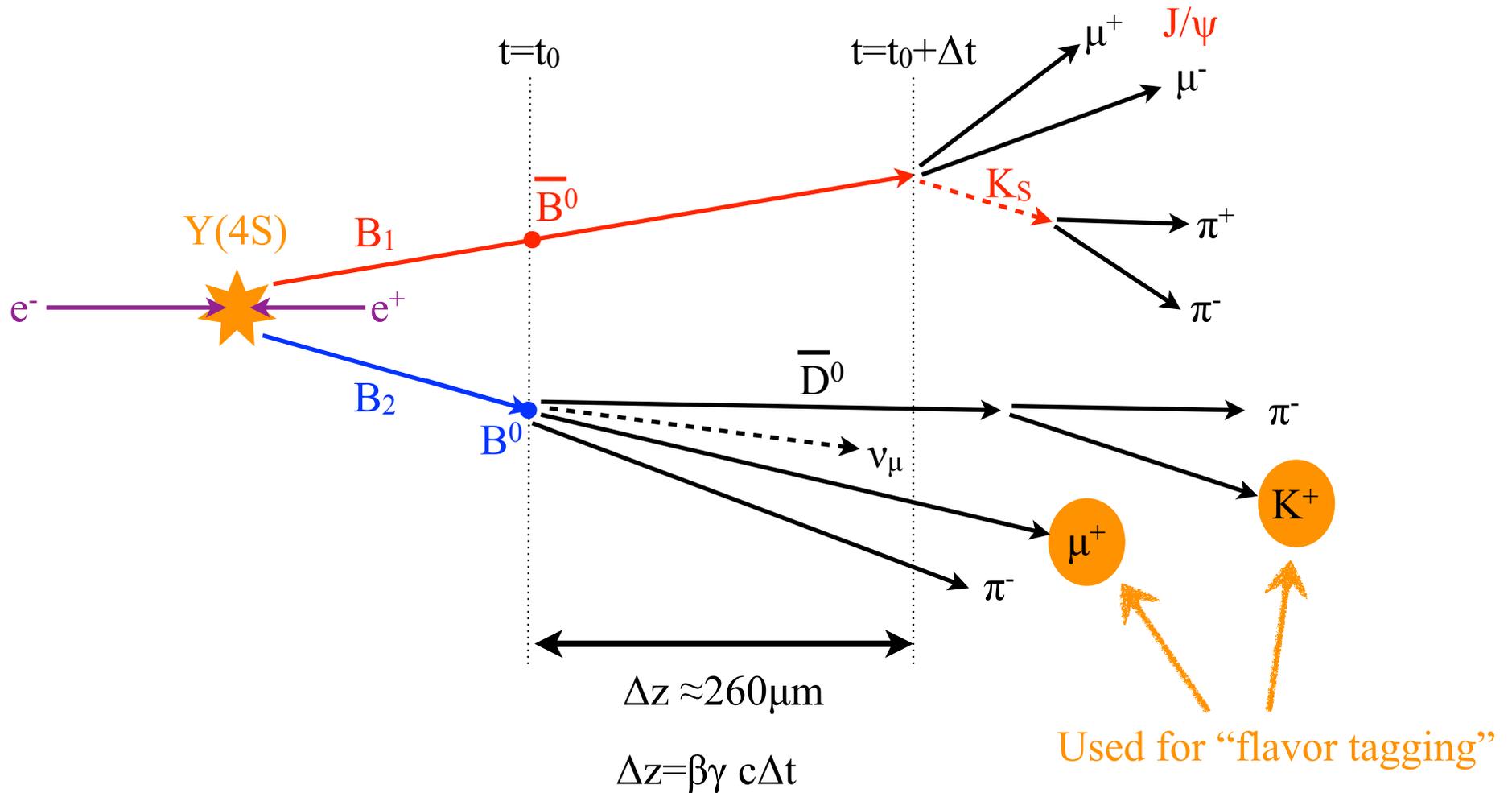
# Flavor physics at the B Factories:

## BELLE & BABAR

# B Factory: requirements

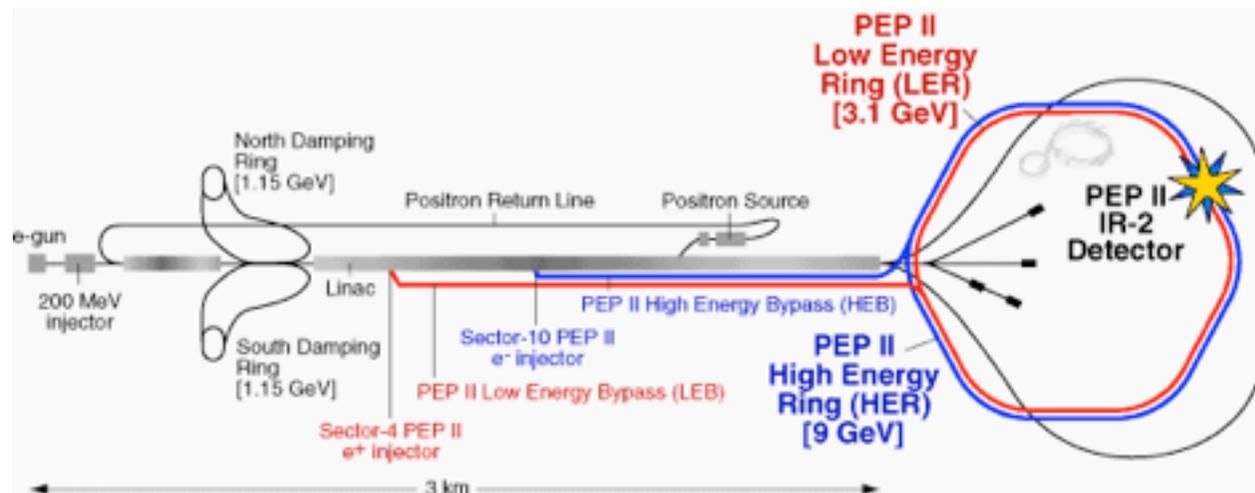
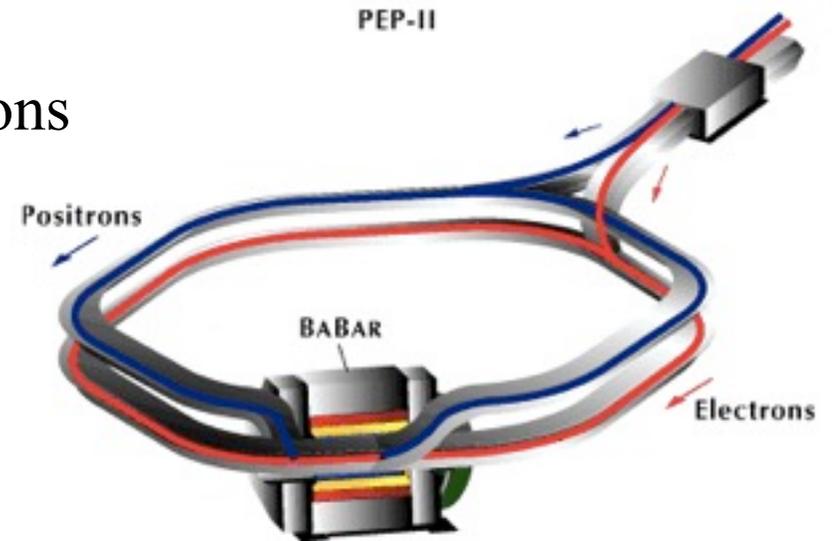
- Primary goal: measure “ $\sin 2\beta$ ” in  $B^0$  decays to  $J/\psi K^0_S$
- Needed:
  - high-statistics sample of  $B^0$  mesons  
=> high-luminosity  $e^+e^-$  collider at the  $Y(4S)$  resonance
  - full kinematical reconstruction of the signal events...  
... + efficient background rejection  
=>  $4\pi$  detector: tracking + calorimetry + particle ID
  - accurate lifetime measurement of the  $B^0$  candidates  
=> boosted  $Y(4S)$  center-of-mass frame + excellent vertexing
  - efficient B-flavor tagging  
=> excellent lepton and kaon identification capabilities

# $B^0$ measurement principle at a B factory



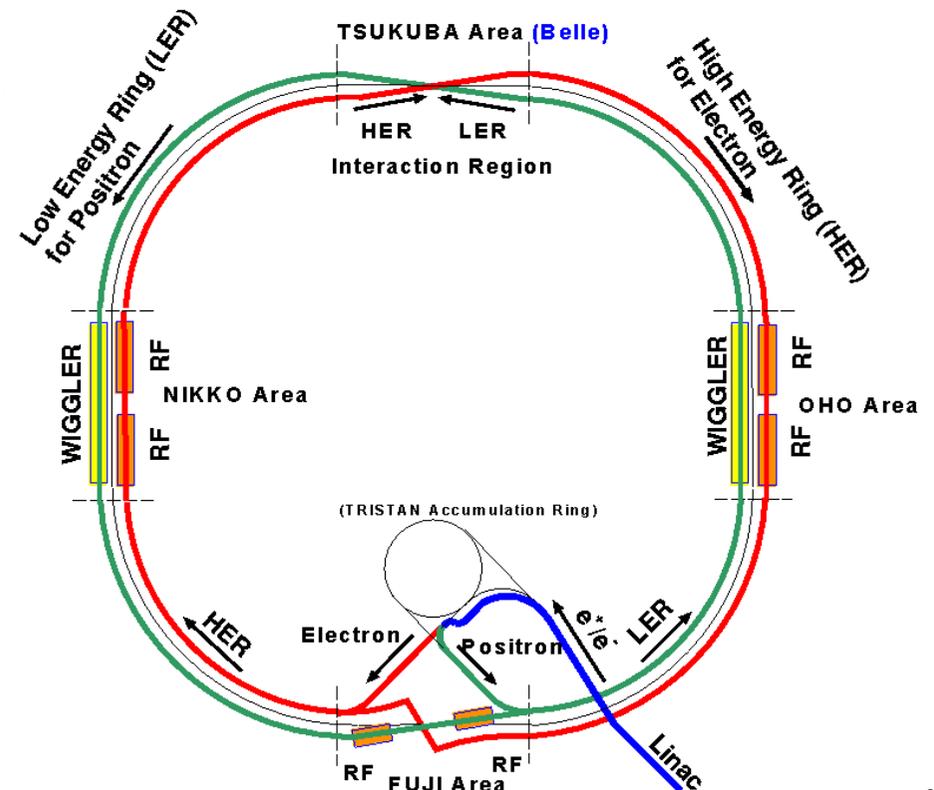
# PEP-II at SLAC

- PEP-II  $e^+e^-$  collider at Stanford Linear Accelerator Center
- 2.2km ring, 1658 bunches
- 9.0GeV electrons on 3.1GeV positrons  
=> boost  $\beta\gamma=0.56$
- Peak luminosity:  $12 \times 10^{33} \text{cm}^{-2}\text{s}^{-1}$
- Integrated luminosity:  $553 \text{fb}^{-1}$
- Operated until 2008

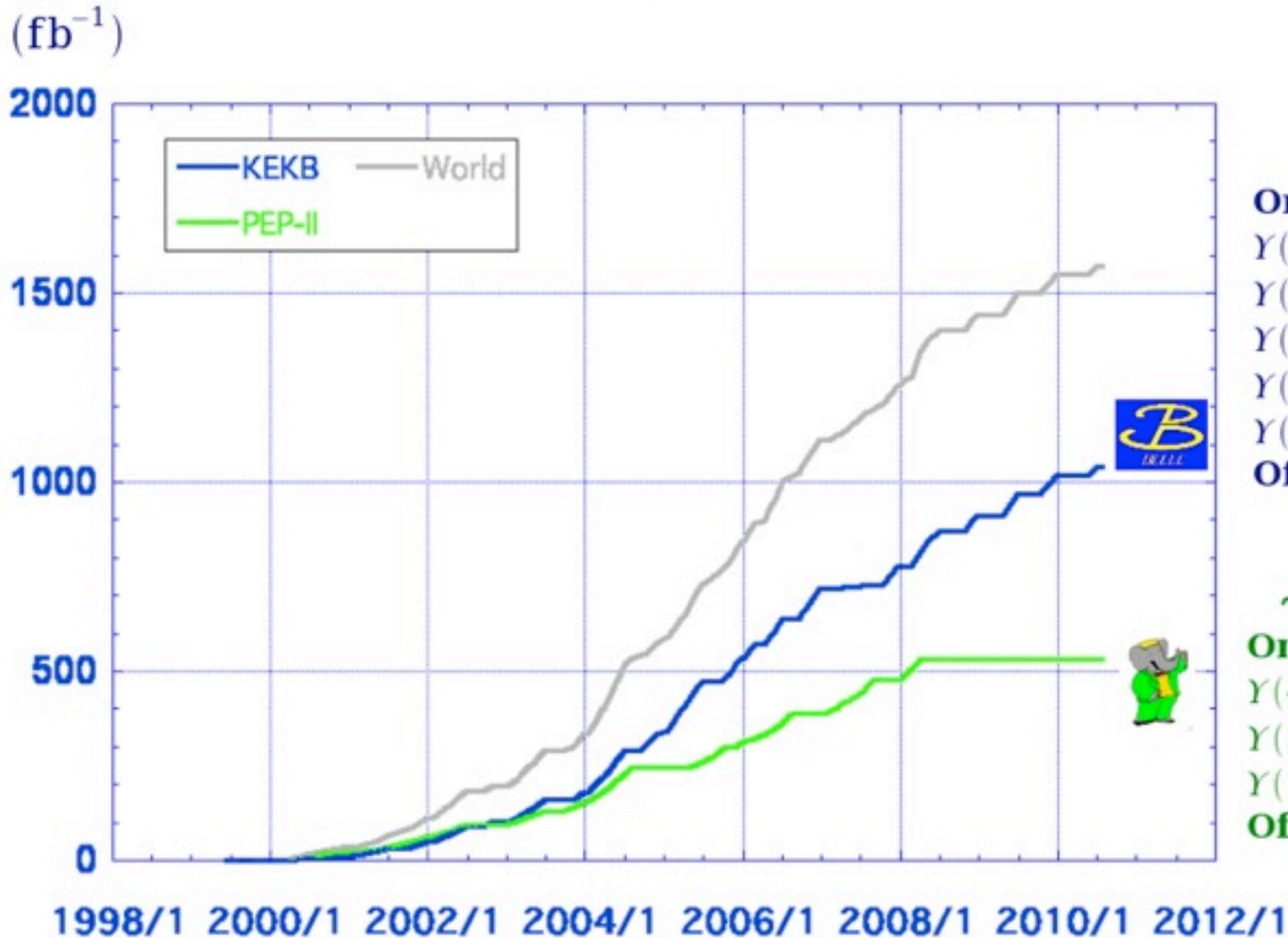


# KEK-B at KEK

- KEK-B  $e^+e^-$  collider at KEK (Japan)
- 3km ring, 5120 bunches
- 8.0GeV electrons on 3.5GeV positrons  
=> boost  $\beta\gamma=0.43$
- Peak luminosity:  $21 \times 10^{33} \text{cm}^{-2}\text{s}^{-1}$
- Integrated luminosity:  $1040 \text{fb}^{-1}$
- Upgrading to Super-KEKB:
  - luminosity:  $8 \times 10^{35} \text{cm}^{-2}\text{s}^{-1}$
  - $50 \text{ab}^{-1}$  by 2020



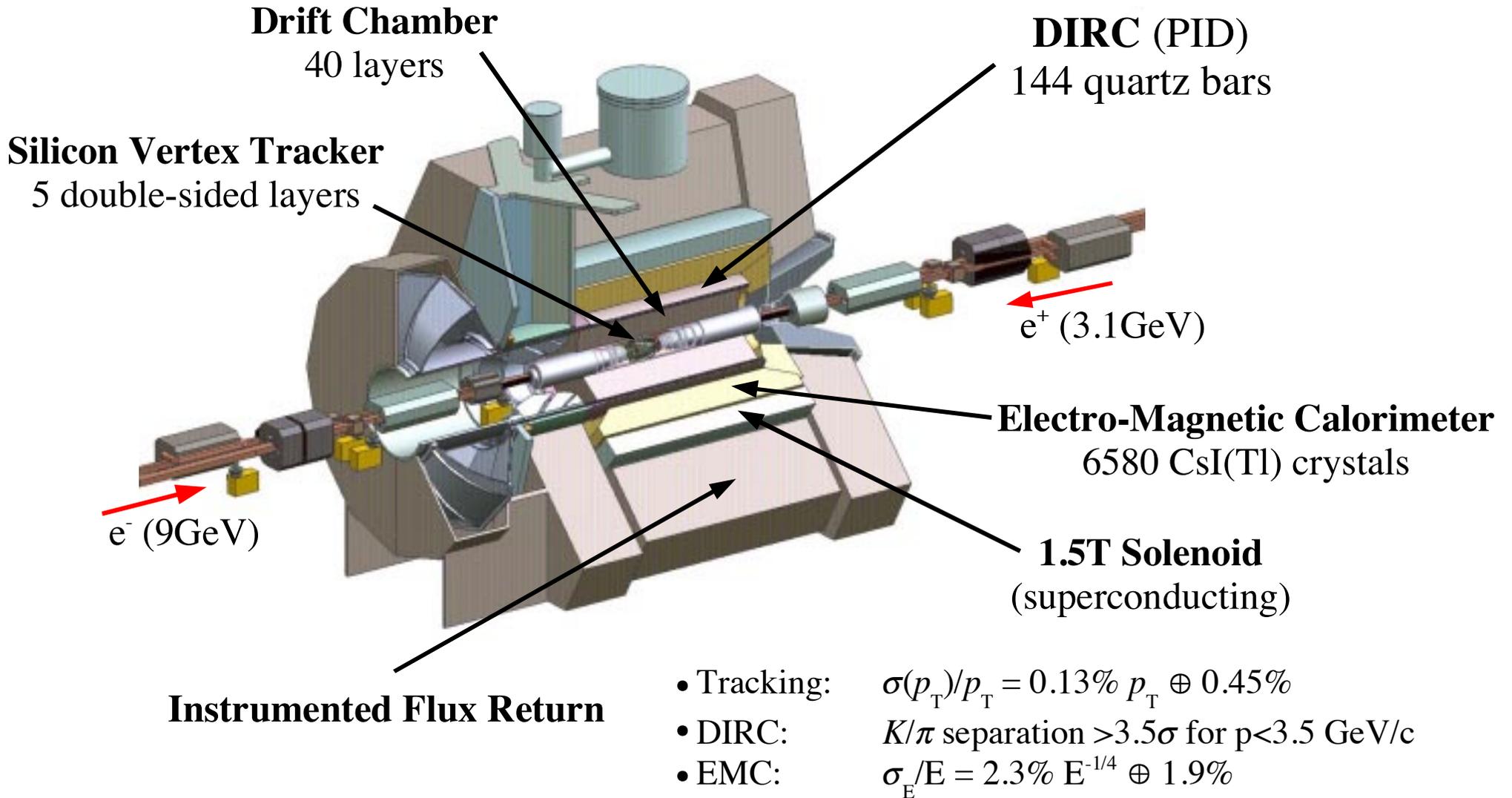
# Luminosity at B factories



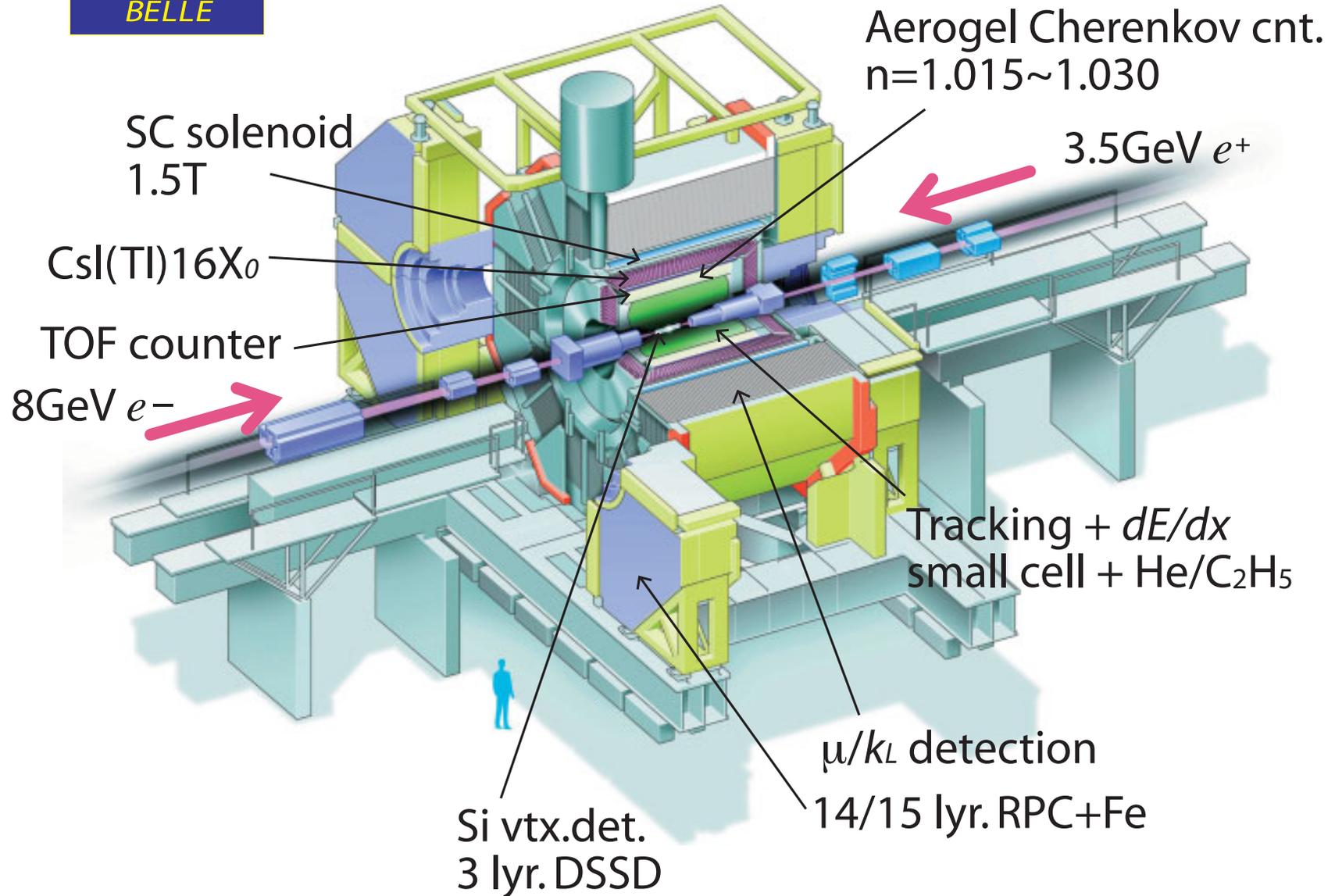
**> 1 ab<sup>-1</sup>**  
**On resonance:**  
 $\Upsilon(5S)$ : 121 fb<sup>-1</sup>  
 $\Upsilon(4S)$ : 711 fb<sup>-1</sup>  
 $\Upsilon(3S)$ : 3 fb<sup>-1</sup>  
 $\Upsilon(2S)$ : 24 fb<sup>-1</sup>  
 $\Upsilon(1S)$ : 6 fb<sup>-1</sup>  
**Off reson./scan:**  
 ~ 100 fb<sup>-1</sup>

**~ 550 fb<sup>-1</sup>**  
**On resonance:**  
 $\Upsilon(4S)$ : 433 fb<sup>-1</sup>  
 $\Upsilon(3S)$ : 30 fb<sup>-1</sup>  
 $\Upsilon(2S)$ : 14 fb<sup>-1</sup>  
**Off resonance:**  
 ~ 54 fb<sup>-1</sup>

# BABAR detector



# Belle Detector



# Backgrounds at the Y(4S)

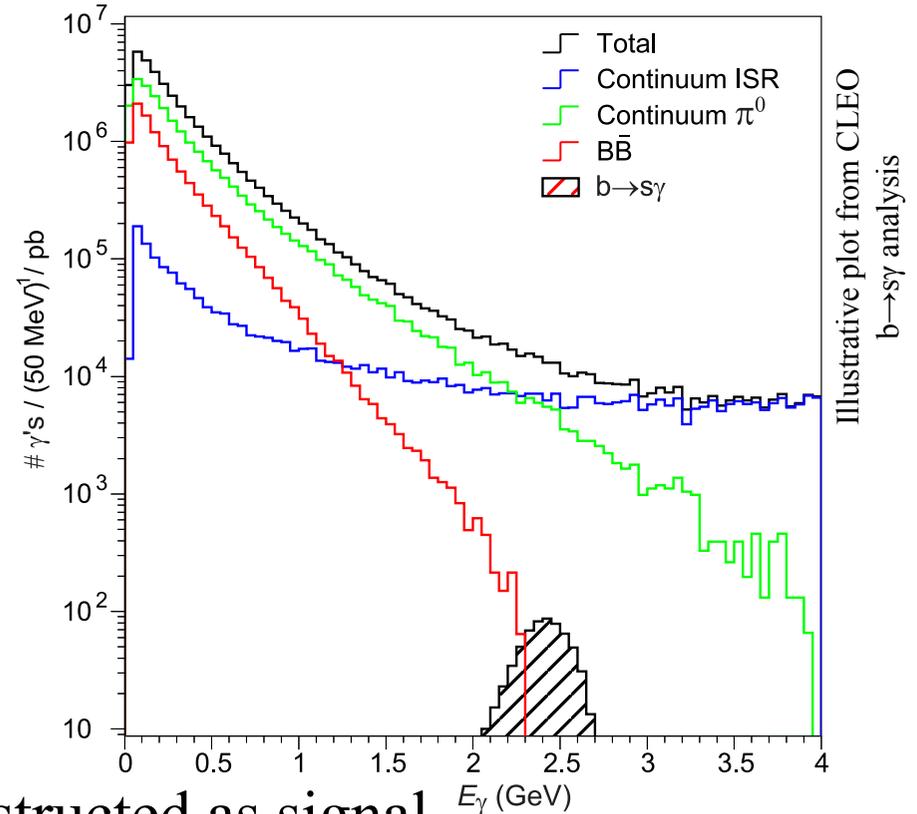
- For B physics analyses, the dominant backgrounds are:

## 1. continuum background

- $e^+e^- \rightarrow qq$ ,  $q=u,d,s,c$
- $e^+e^- \rightarrow e^+e^-, \mu^+\mu^-, \tau^+\tau^-$

## 2. combinatorial background

- other decays of the Y(4S) resonance
- BB events (not signal), reconstructed as signal
- e.g.  $B \rightarrow \rho\pi$  reconstructed as  $B \rightarrow \pi\pi$  (“feed down”) or the opposite (“feed up”)
- e.g.  $B_1 \rightarrow D\pi$  and  $B_2 \rightarrow D(\rightarrow K\pi)lv$  reconstructed as  $B \rightarrow DK$



# Variables for reconstruction of B mesons

## A. Kinematic

- B mass
- B energy
- mass of daughter particles
- decay angle of daughter particles (when applicable)

## B. Particle identification

- Cherenkov angle from ring-imaging Cherenkov detector
- Time-of-flight

## C. Proper time

- decay time information from production and decay vertices

## D. Event shape

- variables characterizing how jetty the event is  
(continuum is jetty, while  $Y(4S) \rightarrow BB$  events are isotropic)

# B mass and energy

- B mass and energy
  - center of mass (CM) energy:  $\sqrt{s}=10.58\text{GeV}$
  - $E^*$  and  $\mathbf{p}^*$  = B energy and momentum in CM

Define: B mass calculated with energy fixed at the beam energy

$$m_{ES} = \sqrt{\frac{1}{4}s - \mathbf{p}_B^{*2}}$$

Define: Energy difference between the B and the beam energy

$$\Delta E = E_B^* - \frac{1}{2}\sqrt{s},$$

- Names for the B mass:
  - beam energy constrained mass  $m_{bc}$  (at Belle)
  - energy-substituted mass  $m_{ES}$  (at BABAR)

# B mass and energy

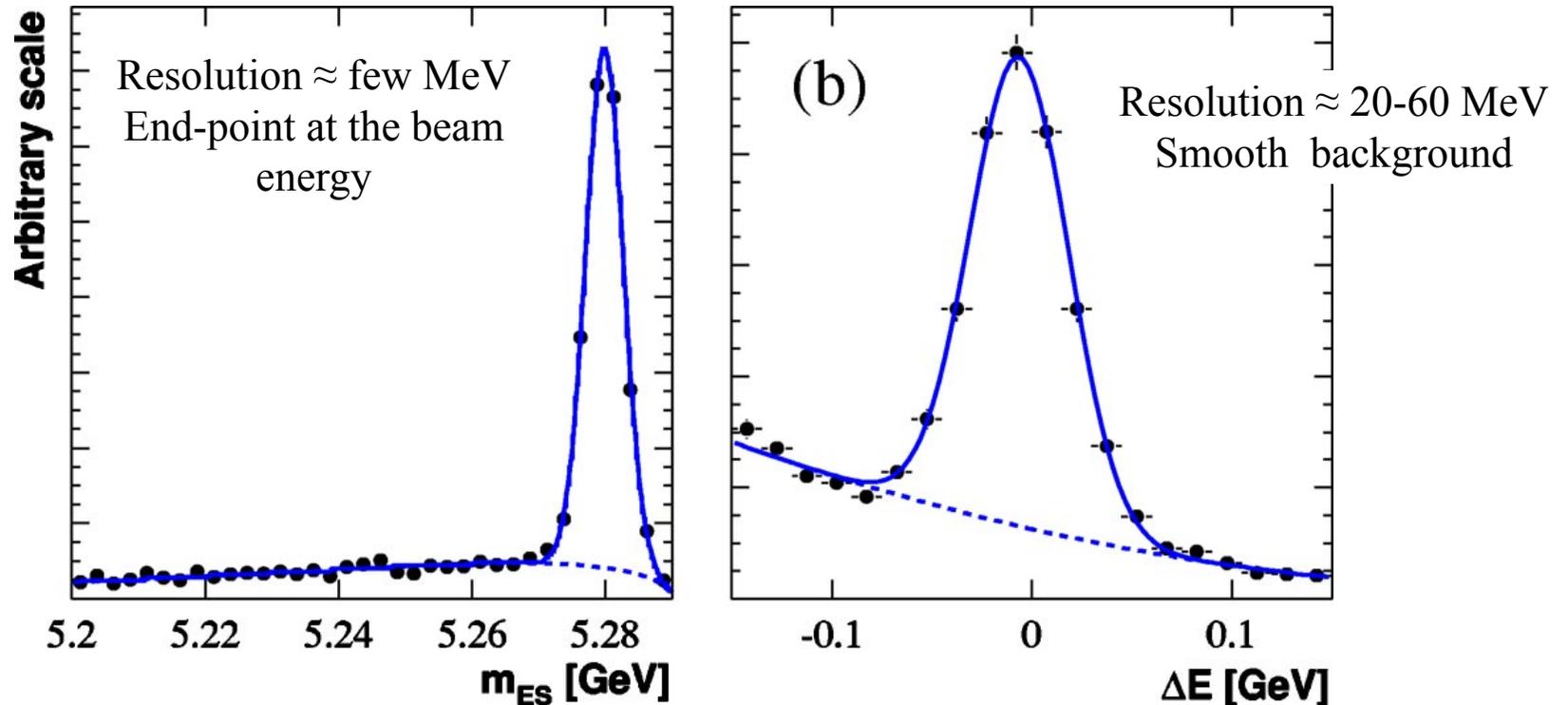
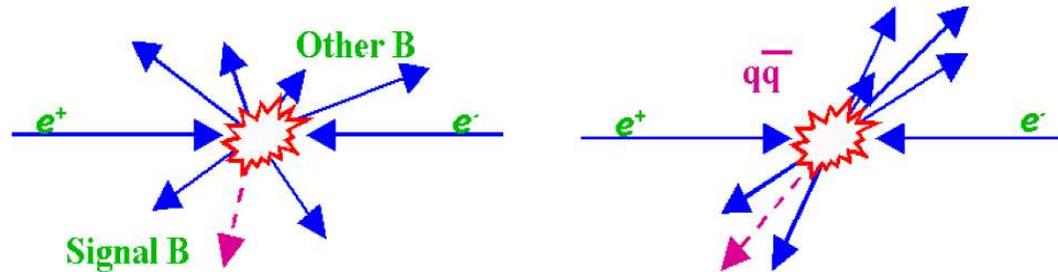
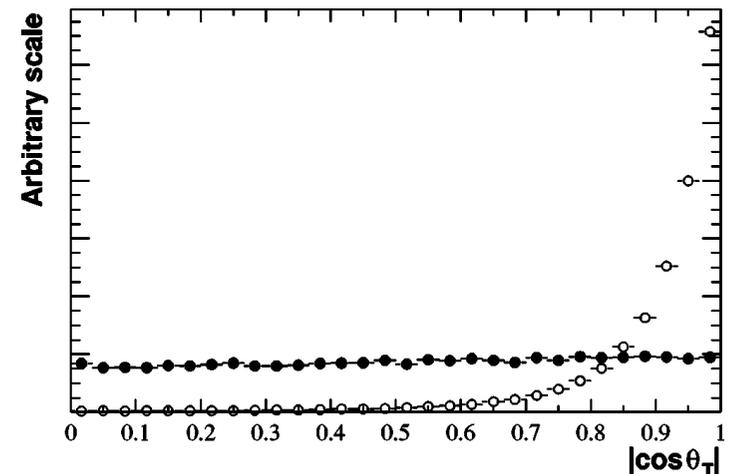


FIG. 7. Distributions of (a)  $m_{ES}$  and (b)  $\Delta E$  from the  $B^- \rightarrow \pi^- D^0$  data sample used to determine the small corrections to signal Monte Carlo PDF shapes.

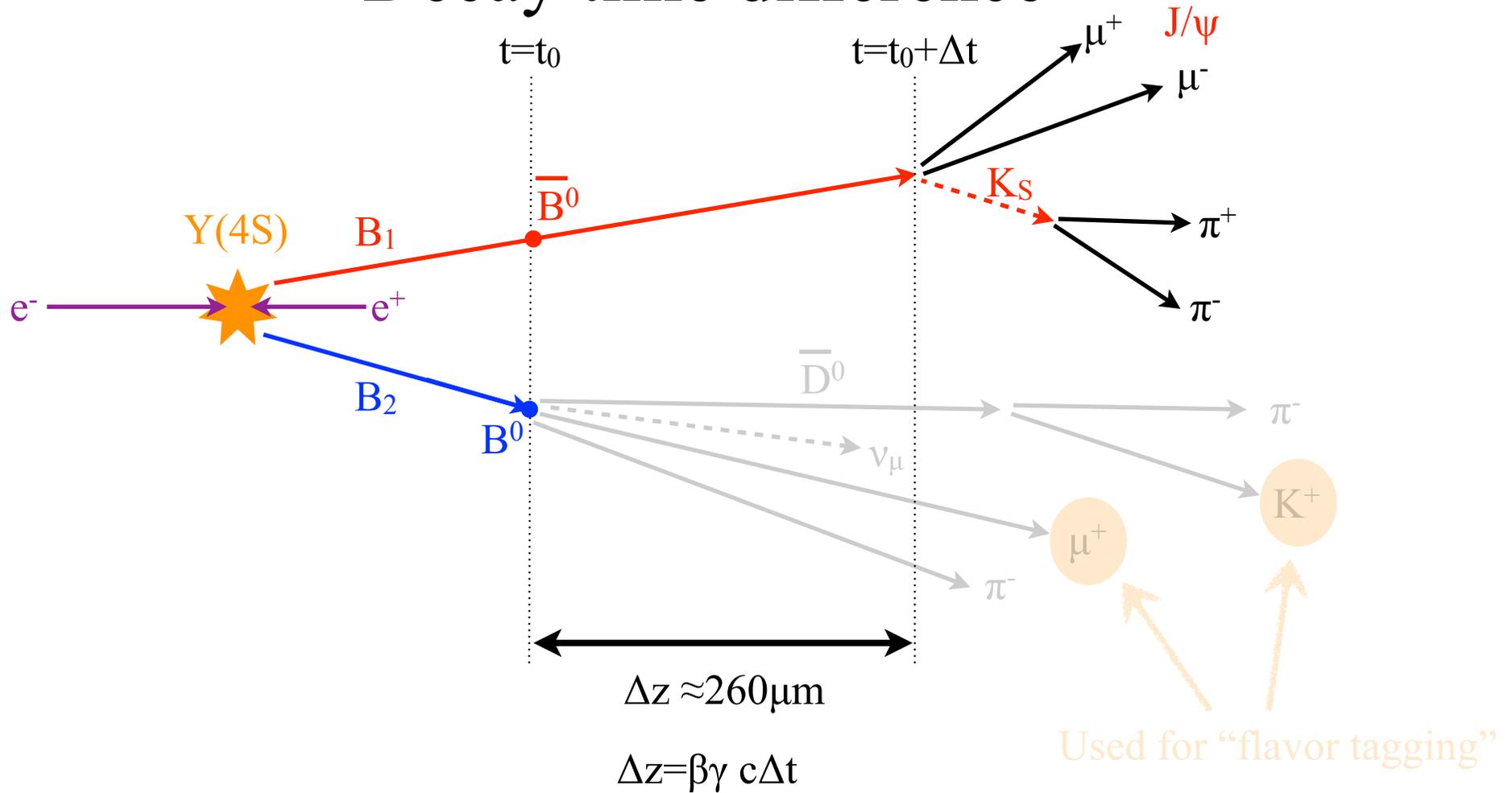
# Event shape



- B mesons are produced (almost) at rest in Y(4S) CM  
=> decay products are isotropic in CM frame
- the light quarks (u,d,s,c) in continuum events have high momentum  
=> decay products are emitted along a main direction
- define the **thrust axis** as the axis that maximizes the sum of momenta projected on this axis
- the cosine of the angle  $\theta_T$  of the thrust axis of the B candidate with respect to the thrust axis of the rest of the event is flat for signal, and sharply peaked at 1.0 for continuum

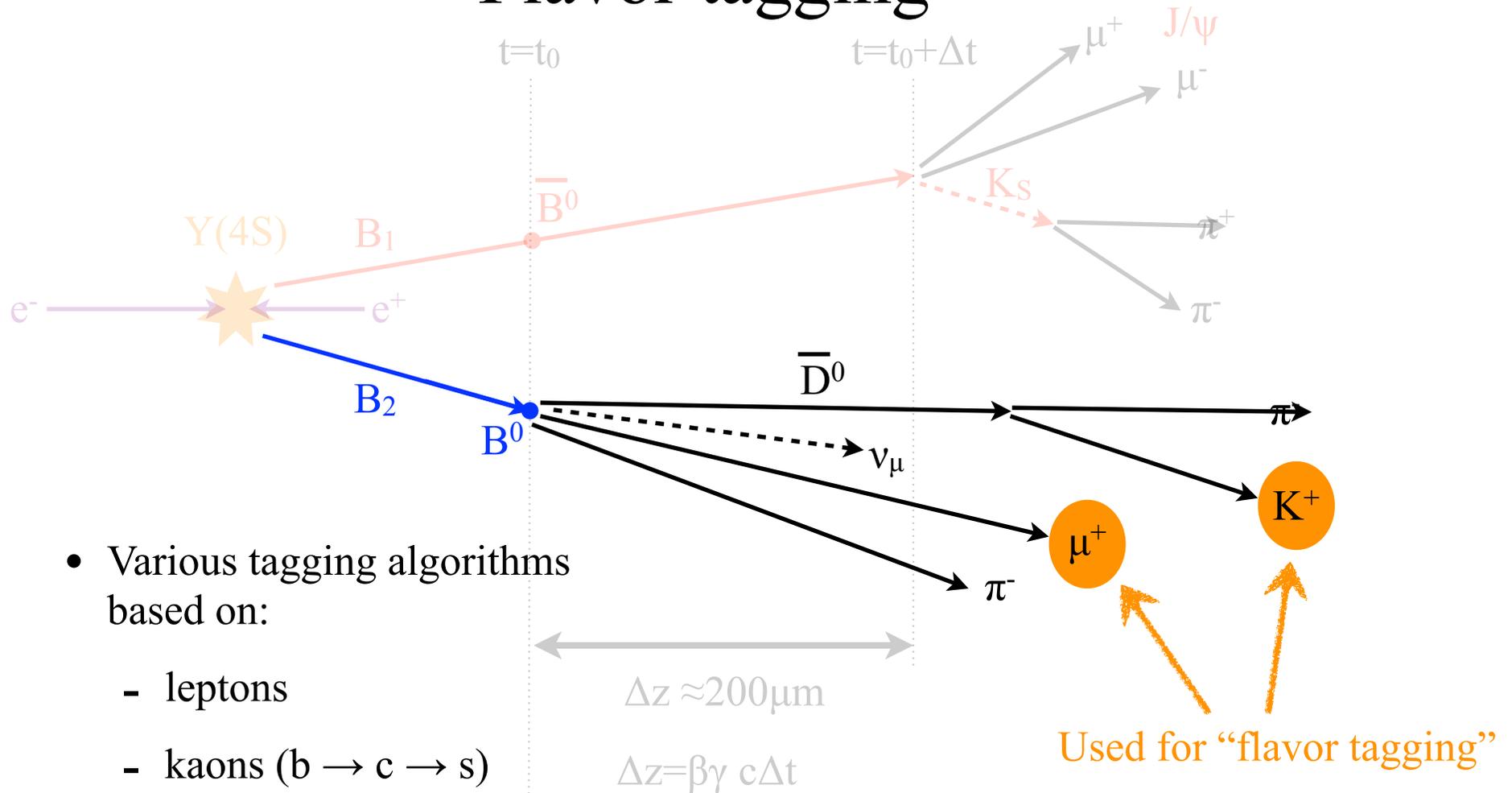


# Decay time difference



- $\sigma(\Delta z) \approx 180 \mu\text{m}$
- $\sigma(\Delta t) \approx 1.1 \text{ps}$  (BABAR) &  $1.4 \text{ps}$  (Belle)

# Flavor tagging



- Various tagging algorithms based on:
  - leptons
  - kaons ( $b \rightarrow c \rightarrow s$ )
  - other global event properties
- Combined in a neural network (BABAR) or likelihood (Belle)
- Mistag from effects such as opposite lepton sign in b or c quark decay

# Tagging performance

- Tagging efficiency depends on
    - fraction of events for which tagging can be obtained:  $\varepsilon$
    - probability to make wrong B flavor identification:  $p_w$
  - $D=1-2p_w$  is the dilution ( $1\equiv$ perfect identification;  $0\equiv$ no flavor identification)
- $\Rightarrow$  effective tagging power:  $\varepsilon D^2 = \varepsilon(1-2p_w)^2$

Category		Efficiency $\varepsilon$ (%)		Effect. dilution $\langle \mathcal{D} \rangle$ (%)		Tagging Power $\varepsilon \mathcal{D}^2$ (%)	
BaBar	Belle ( $r \in$ )	BaBar	Belle	BaBar	Belle	BaBar	Belle
Lepton	0.875–1	$8.96 \pm 0.07$	$14.4 \pm 0.9$	$99.4 \pm 0.3$	$97.0 \pm 0.5$	$7.98 \pm 0.11$	$13.5 \pm 0.9$
Kaon I	0.75–0.875	$10.82 \pm 0.07$	$9.8 \pm 0.7$	$89.4 \pm 0.3$	$78.2 \pm 0.9$	$8.65 \pm 0.3$	$6.0 \pm 0.5$
Kaon II	0.625–0.75	$17.19 \pm 0.09$	$10.7 \pm 0.8$	$71.0 \pm 0.4$	$68.4 \pm 1.0$	$8.68 \pm 0.17$	$5.0 \pm 0.5$
Kaon-Pion	0.5–0.625	$13.67 \pm 0.08$	$10.8 \pm 0.8$	$53.4 \pm 0.4$	$55.0 \pm 1.1$	$3.91 \pm 0.12$	$3.3 \pm 0.4$
Pion	0.25–0.5	$14.18 \pm 0.08$	$14.6 \pm 0.9$	$35.0 \pm 0.4$	$36.0 \pm 0.8$	$1.73 \pm 0.09$	$1.9 \pm 0.2$
Other	0–0.25	$9.54 \pm 0.07$	$39.7 \pm 1.5$	$17.0 \pm 0.5$	$7.2 \pm 0.7$	$0.27 \pm 0.04$	$0.2 \pm 0.1$
Total tagging power						$31.2 \pm 0.3$	$29.9 \pm 1.2$

# Extraction of physics quantities

- Discriminating variables are generally combined in a maximum likelihood (ML) fit
  - use uncorrelated variables
    - correlated variables are combined into a NN or Fisher discriminant
  - extended ML fits are used for branching fraction measurements ( $N$  events,  $Y_j$ =yields,  $P_j^i$ =probability for event  $i$  and event category  $j$ )

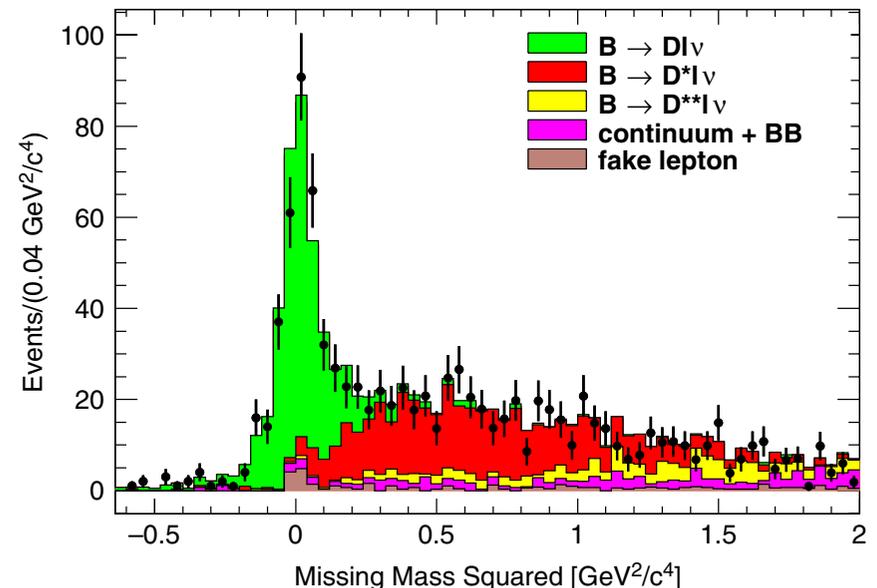
$$\mathcal{L} = \frac{\exp(-\sum_j Y_j)}{N!} \prod_i \sum_j Y_j \mathcal{P}_j^i$$

- time-dependent fits are extensions of the above function
- PDF parameters are determined from control samples, or left floating in the ML fit
- up to  $O(100)$  free parameters in some ML fits!

# Recoil technique

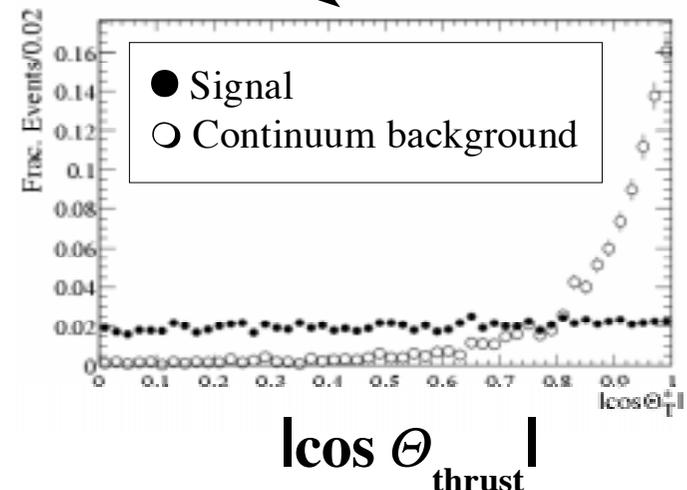
- $Y(4S) \rightarrow BB \Rightarrow$  we can reconstruct one B meson ( $B_{\text{reco}}$ ), and we know the momentum and direction of the other B ( $B_{\text{sig}}$ )
    - this method gives a very clean sample of  $B_{\text{sig}}$  decays recoiling against the reconstructed  $B_{\text{reco}}$
    - but the overall statistics is low
- $\Rightarrow$  Very useful to look for relatively abundant B decays, but which are subject to sizable backgrounds

- For example:
  - inclusive semileptonic B decays
  - $B^0 \rightarrow \nu\bar{\nu}$  (“invisible” decay)
  - inclusive charmless  $b \rightarrow sg$



# Analysis technique: summary

- Use **Maximum Likelihood (ML) fit** technique
- Use **kinematic**, **event shape** and **decay time** variables
- Apply loose cuts  $\Rightarrow$  keep side-bands for background fitting
- Main background:  $e^+e^- \rightarrow q\bar{q}$  continuum ( $q=u,d,s,c$ )
  - Rejected with preliminary cut on thrust angle
- Extract from ML fit:
  - **signal yields**
  - **charge asymmetries**
  - **time dependent asymmetries**
  - **+ several parameters (PDFs, efficiencies, etc...)**
- Several crosschecks:
  - "toy MC"
  - control samples
  - etc...



# Measurement of the angle $\beta$

# Time-dependent asymmetry

- The asymmetry  $A_f(t)$  can be written (assuming  $\Delta\Gamma=0$  and  $|q/p|=1$ )

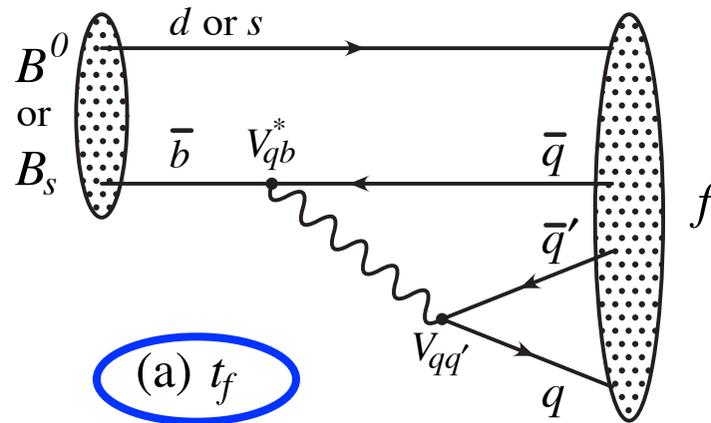
$$A_f(t) = S_f \sin(\Delta mt) - C_f \cos(\Delta mt)$$

where

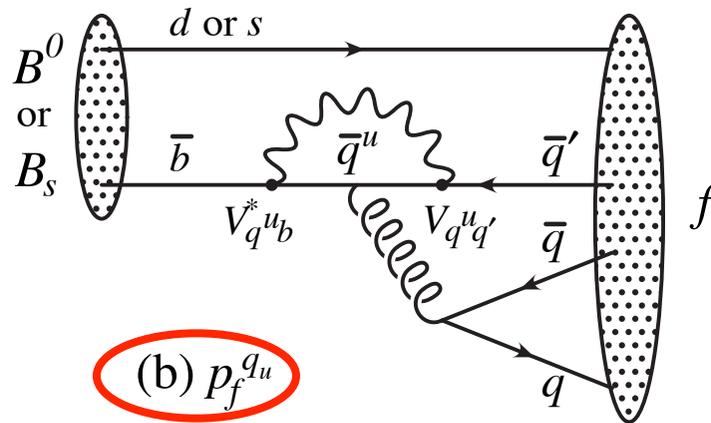
$$S_f \equiv \frac{2\text{Im}(\lambda_f)}{1 + |\lambda_f|^2} \quad C_f \equiv \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2}$$

$$\lambda_f = e^{-i\phi_M} \left( \frac{\bar{A}_f}{A_f} \right)$$

# Feynman diagrams for $b \rightarrow q\bar{q}q'$



Tree



Penguin

# Decay amplitudes

- For  $B \rightarrow J/\psi K_S$  decays, the ratio  $\bar{A}/A$  is

$$\frac{\bar{A}_{\psi K_S}}{A_{\psi K_S}} = \frac{\underbrace{(V_{cb} V_{cs}^*) T_{\psi K}}_{\text{Tree}} + \underbrace{(V_{ub} V_{us}^*) P_{\psi K}^u}_{\text{Penguin}}}{\underbrace{(V_{cb}^* V_{cs}) T_{\psi K}}_{\text{Tree}} + \underbrace{(V_{ub}^* V_{us}) P_{\psi K}^u}_{\text{Penguin}}} \times \underbrace{\frac{V_{cd}^* V_{cs}}{V_{cd} V_{cs}^*}}_{\text{K}^0 \text{ mixing}}$$

- For several B decays, determine the dominant phase in the decay amplitude, and the size of the next contribution

$\bar{b} \rightarrow \bar{q}q\bar{q}'$	$B^0 \rightarrow f$	$B_s \rightarrow f$	CKM dependence of $A_f$	Suppression
$\bar{b} \rightarrow \bar{c}c\bar{s}$	$\psi K_S$	$\psi\phi$	$(V_{cb}^* V_{cs})T + (V_{ub}^* V_{us})P^u$	loop $\times \lambda^2$
$\bar{b} \rightarrow \bar{s}s\bar{s}$	$\phi K_S$	$\phi\phi$	$(V_{cb}^* V_{cs})P^c + (V_{ub}^* V_{us})P^u$	$\lambda^2$
$\bar{b} \rightarrow \bar{u}u\bar{s}$	$\pi^0 K_S$	$K^+ K^-$	$(V_{cb}^* V_{cs})P^c + (V_{ub}^* V_{us})T$	$\lambda^2/\text{loop}$
$\bar{b} \rightarrow \bar{c}c\bar{d}$	$D^+ D^-$	$\psi K_S$	$(V_{cb}^* V_{cd})T + (V_{tb}^* V_{td})P^t$	loop
$\bar{b} \rightarrow \bar{s}s\bar{d}$	$\phi\pi$	$\phi K_S$	$(V_{tb}^* V_{td})P^t + (V_{cb}^* V_{cd})P^c$	$\lesssim 1$
$\bar{b} \rightarrow \bar{u}u\bar{d}$	$\pi^+ \pi^-$	$\pi^0 K_S$	$(V_{ub}^* V_{ud})T + (V_{tb}^* V_{td})P^t$	loop

strongest suppression  
 $\Rightarrow$  negligible contribution  
 from phase of  $V_{ub}$   
 $\Rightarrow$  negligible weak phase in  
 decay amplitude

# Measurement of $\beta$ in $B^0$ decays

- For  $B \rightarrow J/\psi K_S$  and other  $b \rightarrow ccs$  processes:

$$\lambda_{\psi K_S} = e^{-2i\beta} \Rightarrow S_{\psi K_S} = \sin 2\beta \quad \text{and} \quad C_{\psi K_S} = 0$$

- correct to better than 1%

- For  $B \rightarrow \phi K_S$  and other  $b \rightarrow sss$  processes:

$$\lambda_{\phi K_S} = e^{-2i\beta} \Rightarrow S_{\phi K_S} = \sin 2\beta \quad \text{and} \quad C_{\phi K_S} = 0$$

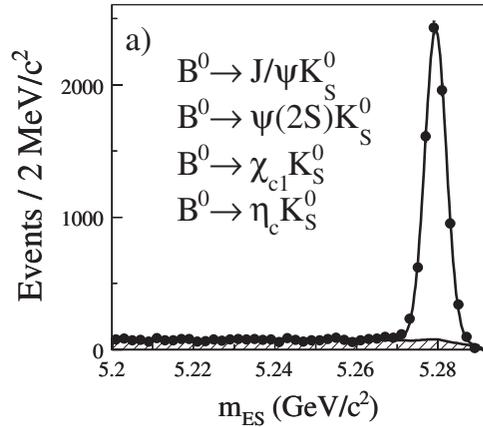
- correct to better than a few percents

- For  $B \rightarrow \pi^+ \pi^-$  and other  $b \rightarrow uud$  processes:

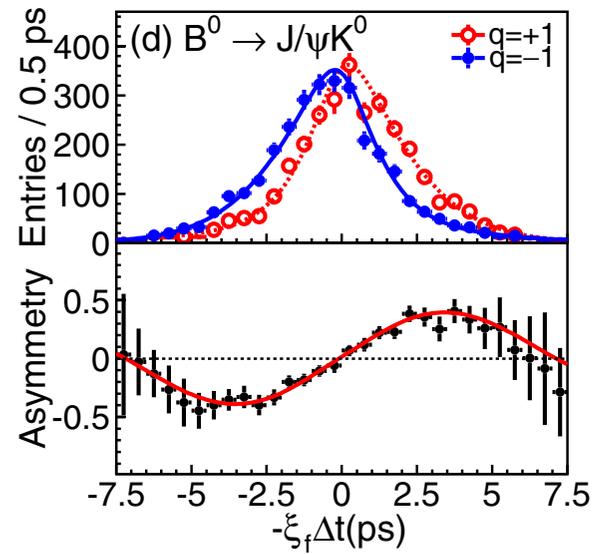
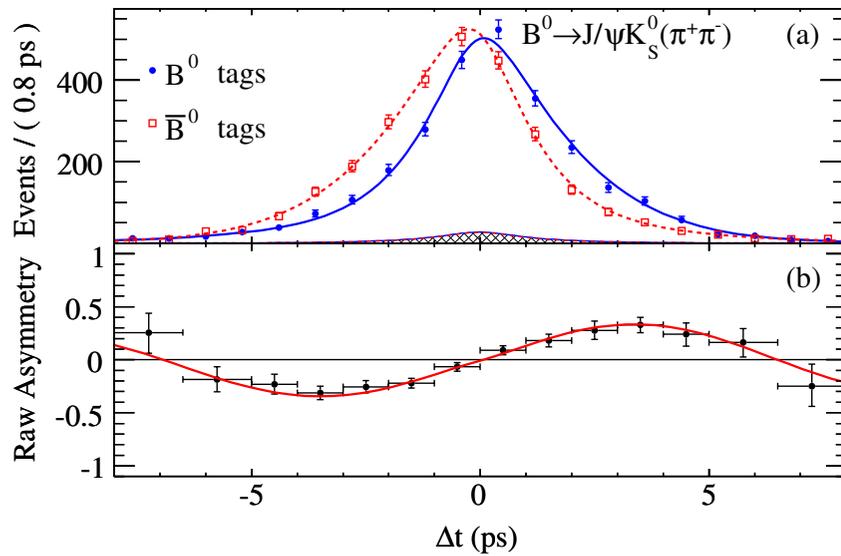
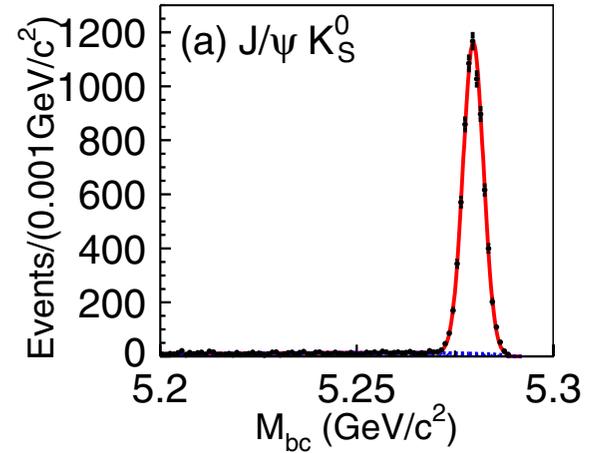
- the dominant decay amplitude contains the phase  $\gamma$ , and are therefore measuring  $\sin(2\beta+2\gamma) = \sin(2\alpha)$

# $B \rightarrow J/\psi K_S$

BABAR, PRD 79 (2009) 072009



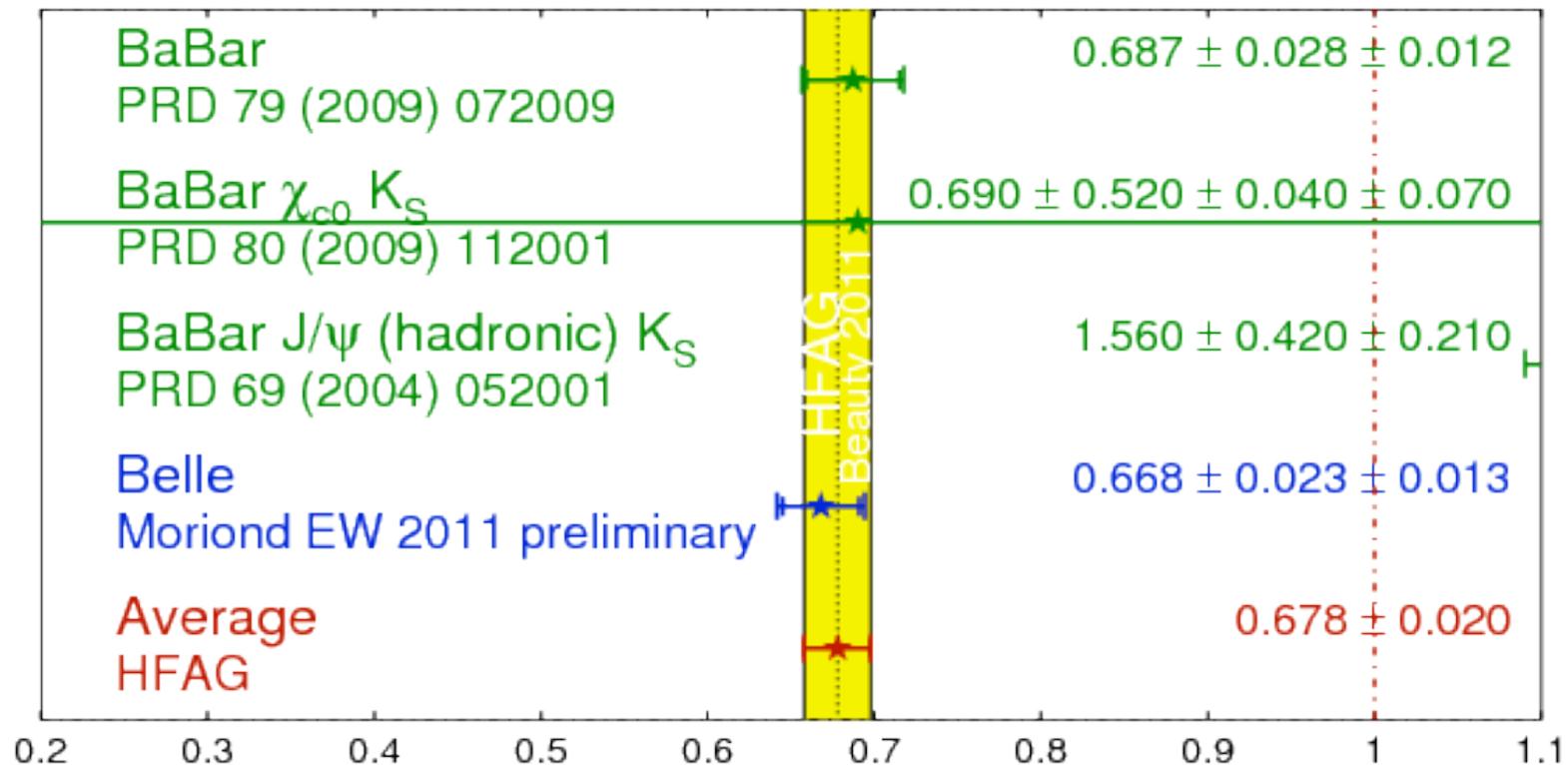
BELLE, PRL 98 (2007) 031802



# $\sin 2\beta$ in $b \rightarrow ccs$ modes

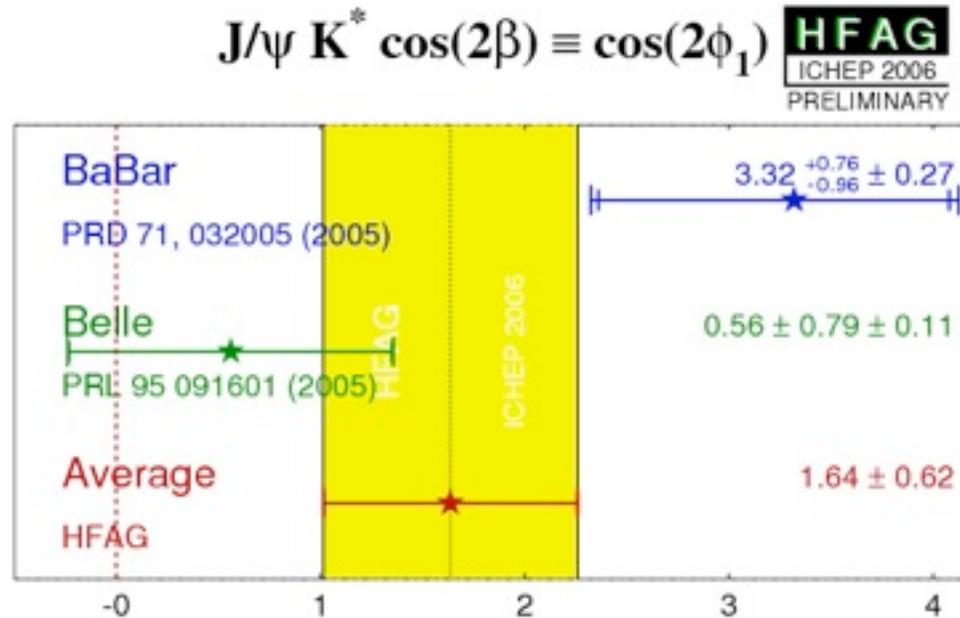
$$\sin(2\beta) \equiv \sin(2\phi_1)$$

**HFAG**  
Beauty 2011  
PRELIMINARY

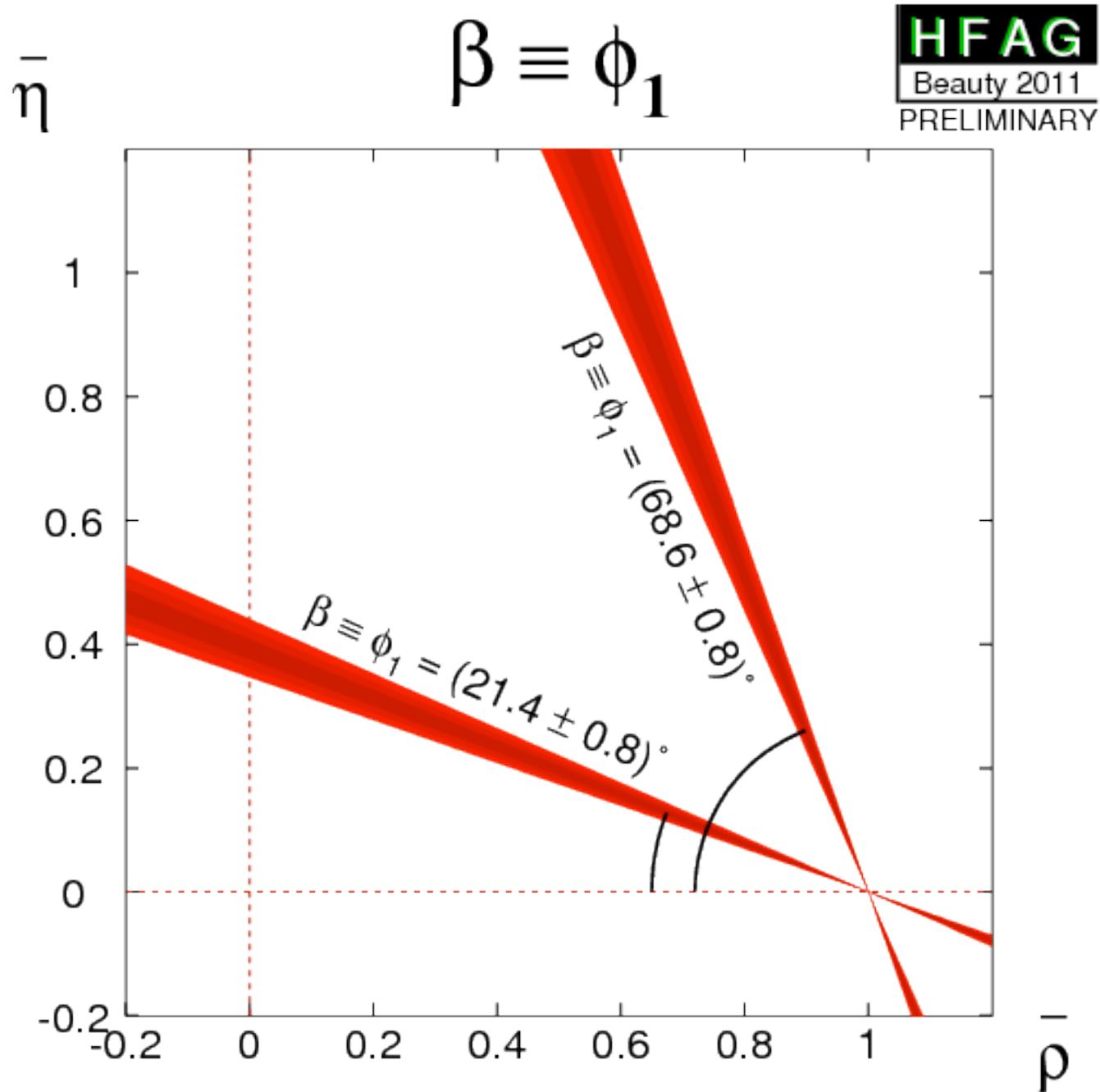


# $\cos 2\beta$

- Time-dependent angular analysis of  $B^0 \rightarrow J/\psi K^{*0}$ 
  - interference between  $CP=+1$  and  $CP=-1$  amplitude  $\Rightarrow \cos 2\beta$
- Results favor one of the solutions for the angle  $\beta$   
 $\Rightarrow \cos 2\beta > 0$



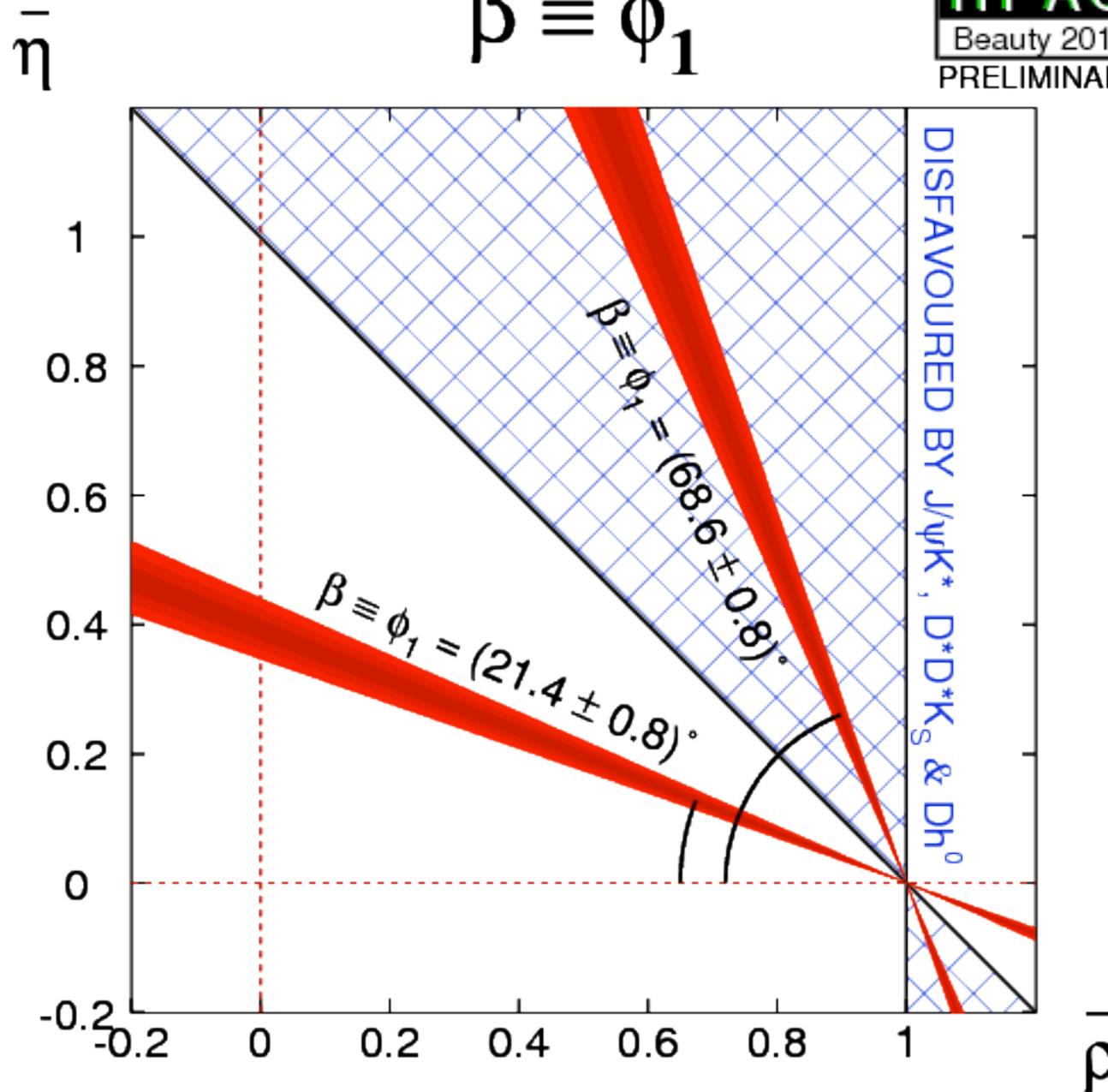
# $\sin 2\beta$ in $b \rightarrow ccs$ modes



# $\sin 2\beta$ in $b \rightarrow ccs$ modes

$$\beta \equiv \phi_1$$

**HFAG**  
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# $\sin 2\beta$ in charmless penguin $B^0$ decays

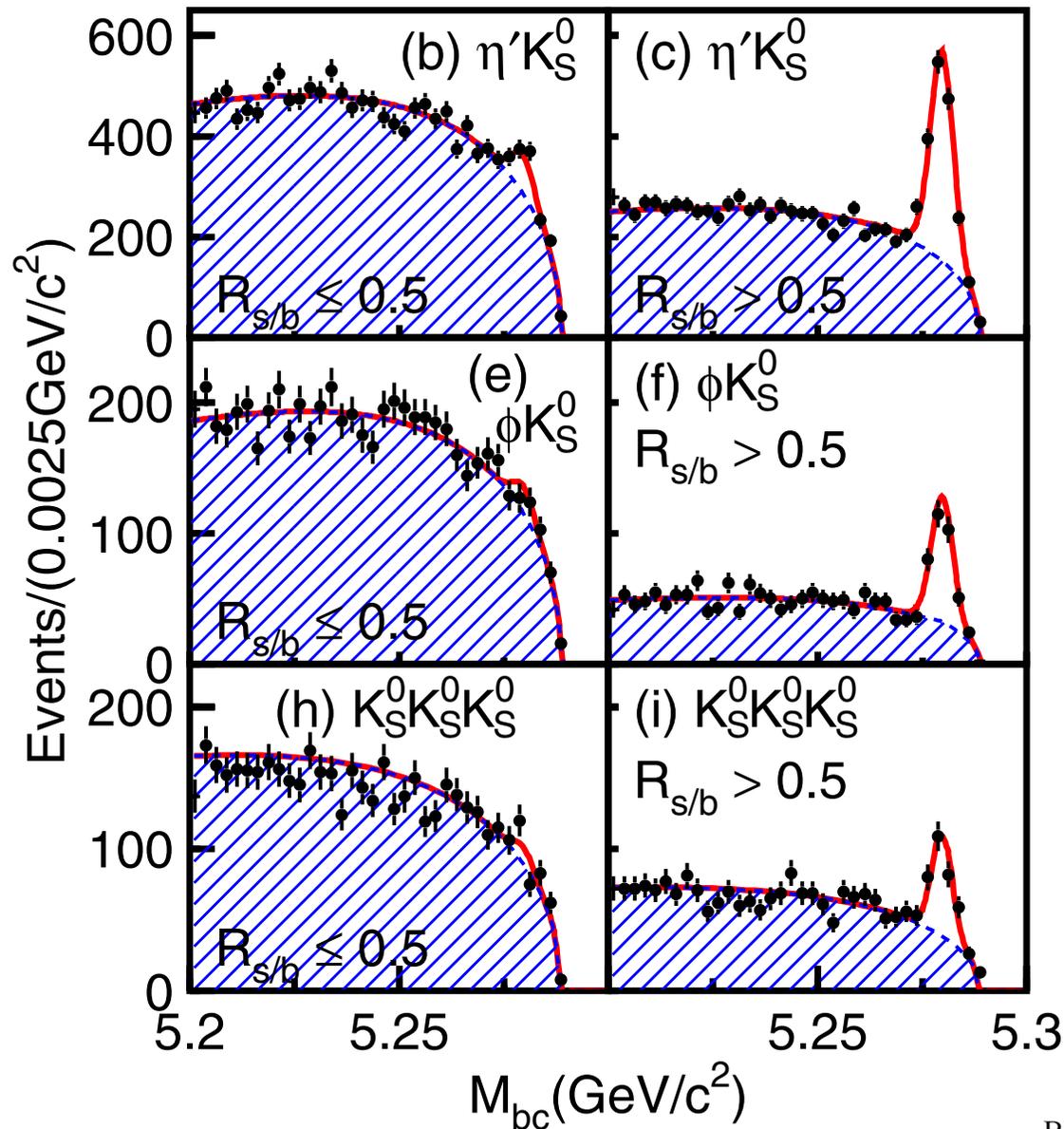
- Weak phase in the decay amplitudes can modify the measured asymmetry

$$\Rightarrow S = \sin 2\beta \quad \rightarrow \quad S = \sin 2\beta^{\text{eff}}$$

- Estimation of the value for  $\Delta S = -\eta S_f - S_{\text{CCS}}$  from QCD
  - Table: prediction for  $\sin 2\beta^{\text{eff}}$  for several modes:

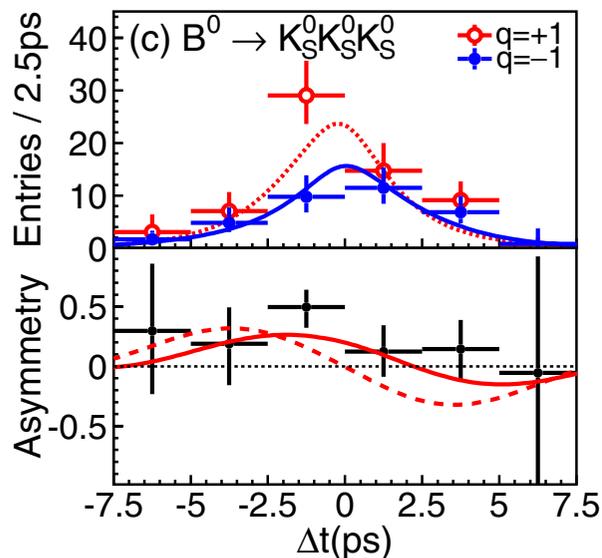
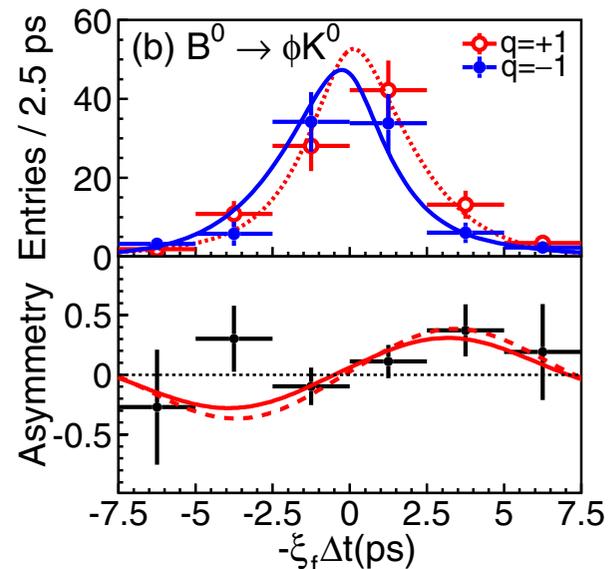
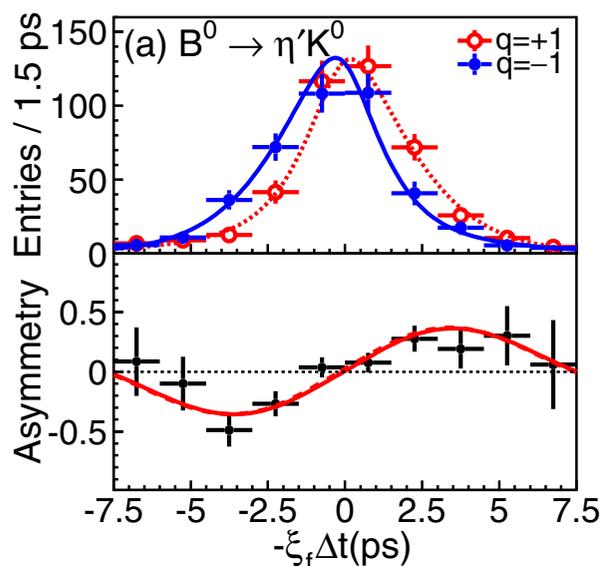
$-\eta_f S_f$	QCDF <sup>a</sup>	pQCD <sup>b</sup>	SCET <sup>c</sup>
$\phi K_S$	$0.75^{+0.00}_{-0.04}$	$0.71 \pm 0.01$	0.69
$\omega K_S$	$0.85^{+0.03}_{-0.06}$	$0.84^{+0.03}_{-0.07}$	$0.50^{+0.05}_{-0.06}$ $0.80 \pm 0.02$
$\rho^0 K_S$	$0.64^{+0.03}_{-0.07}$	$0.50^{+0.10}_{-0.06}$	$0.85^{+0.04}_{-0.05}$ $0.56^{+0.02}_{-0.03}$
$\eta' K_S$	$0.74^{+0.00}_{-0.04}$	–	$0.706 \pm 0.008$ $0.715 \pm 0.008$
$\eta K_S$	$0.79^{+0.02}_{-0.04}$	–	$0.69 \pm 0.16$ $0.79 \pm 0.15$
$\pi^0 K_S$	$0.79^{+0.02}_{-0.04}$	$0.74^{+0.02}_{-0.03}$	$0.80 \pm 0.03$
$f_0(980) K_S$	$0.731^{+0.001}_{-0.001}$	–	–
$K^+ K^- K_S^e$	$0.728^{+0.009}_{-0.020}$	–	–
$K_S K_S K_S$	$0.719^{+0.009}_{-0.020}$	–	–
$K_S \pi^0 \pi^0$	$0.729^{+0.009}_{-0.020}$	–	–

# $m_{bc}$ in $b \rightarrow s$ penguin decays (BELLE)



BELLE, PRL 98 (2007) 031802

# $\sin 2\beta$ in $b \rightarrow s$ penguin decays (BELLE)



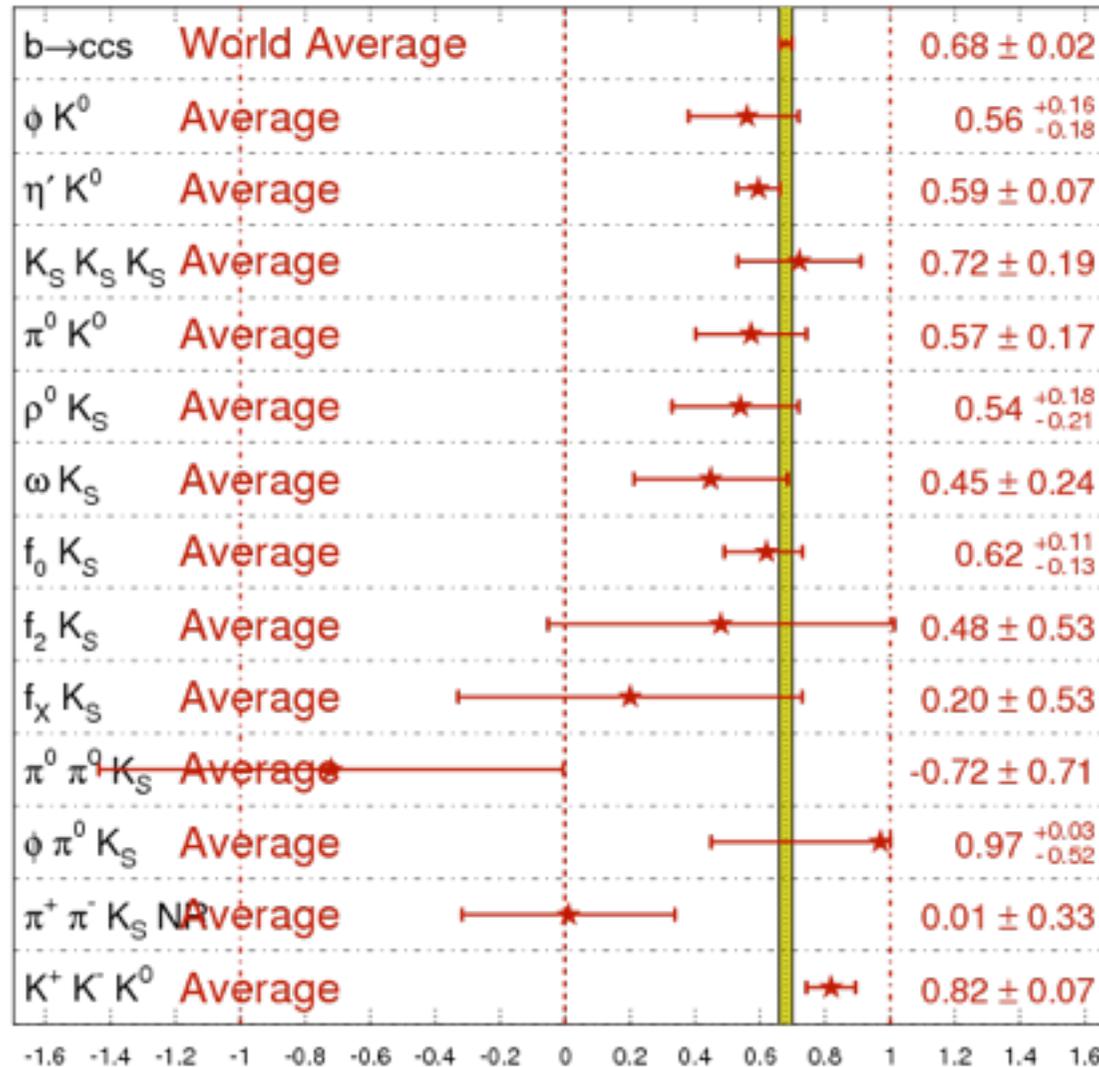
Mode	$\sin 2\phi_1^{\text{eff}}$	$\mathcal{A}_f$
$\phi K^0$	$+0.50 \pm 0.21 \pm 0.06$	$+0.07 \pm 0.15 \pm 0.05$
$\eta' K^0$	$+0.64 \pm 0.10 \pm 0.04$	$-0.01 \pm 0.07 \pm 0.05$
$K_S^0 K_S^0 K_S^0$	$+0.30 \pm 0.32 \pm 0.08$	$+0.31 \pm 0.20 \pm 0.07$
$J/\psi K^0$	$+0.642 \pm 0.031 \pm 0.017$	$+0.018 \pm 0.021 \pm 0.014$

BELLE, PRL 98 (2007) 031802

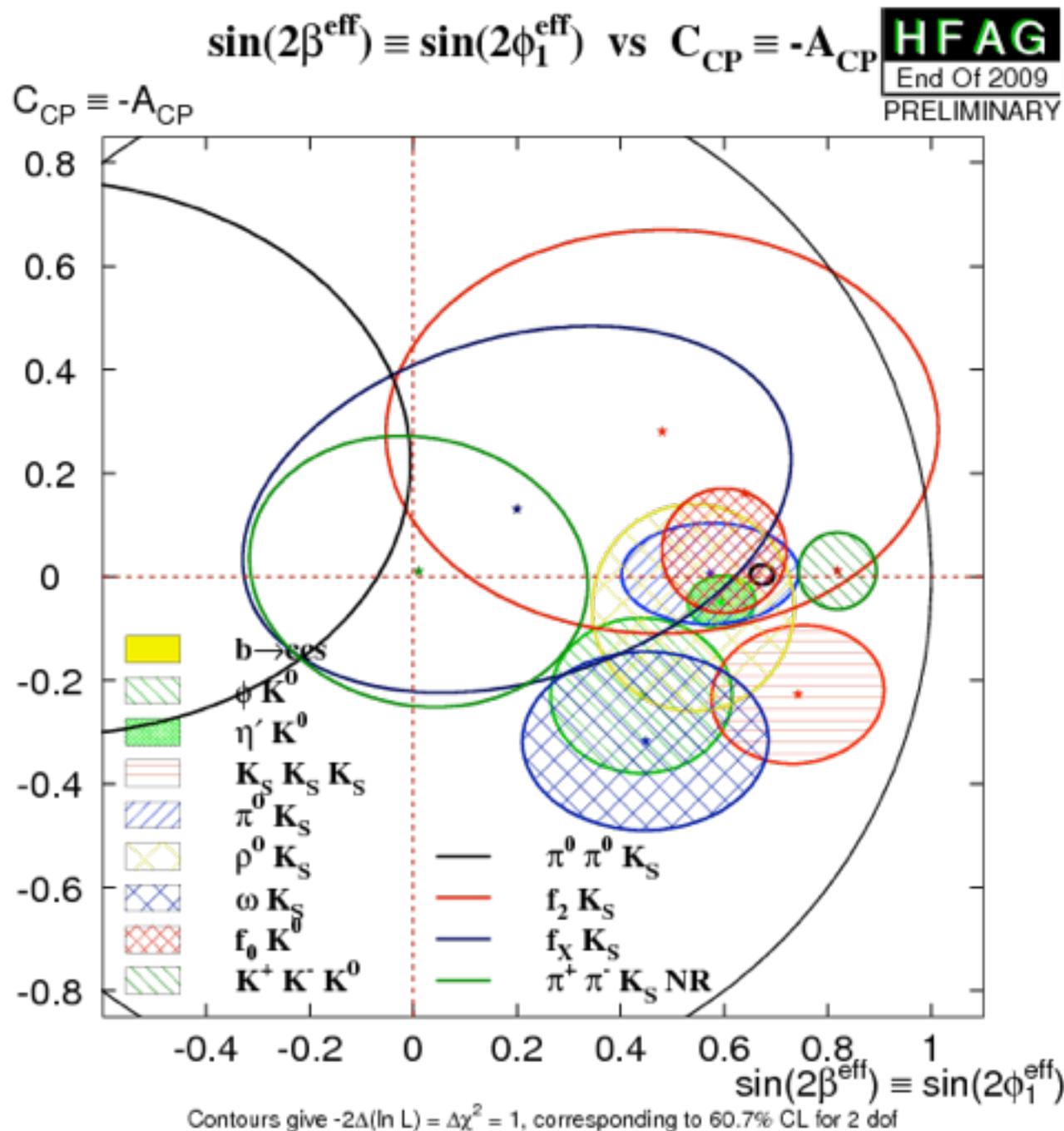
# $\sin 2\beta^{\text{eff}}$ in $b \rightarrow s$ penguin decays: summary

$$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$$

**HFAG**  
EndOfYear 2011  
PRELIMINARY



# $\sin 2\beta^{\text{eff}}$ in $b \rightarrow s$ penguin decays: C vs S



# $\Delta S$ and the $2\sigma$ discrepancy

- Since around  $\sim 2005$ , the naïve average of  $\sin 2\beta^{\text{eff}}$  in  $b \rightarrow s$  penguin decays has been  $\approx 2\sigma$  low relative to  $\sin 2\beta$  measured in charmonium modes
- The average has slowly moved towards  $\sin 2\beta$  with more data and more decay modes (regression to the mean?)
- QCD uncertainties are large, and no new physics can be invoked at this point
- More data, and more modes ( $B_s$  decays?) should help clarify the situation

Year	$\sin 2\beta^{\text{eff}}$ naïve average
2005	$0.50 \pm 0.06$
2006	$0.53 \pm 0.05$
2007	$0.56 \pm 0.05$
2008	$0.64 \pm 0.04$
2009	$0.62 \pm 0.04$
2010-11	$0.64 \pm 0.04$

$$\sin(2\beta+\gamma)$$

- $B^0$  decays to open charm are sensitive to  $\sin(2\beta+\gamma)$ 
  - interference between
    - CKM-favored  $b \rightarrow c$  decay amplitude  $A_{\text{fav}}$  (no weak phase)
    - and
    - CKM-suppressed  $b \rightarrow u$  decay amplitude  $A_{\text{supp}}$  (weak phase  $\gamma$ )
  - with and without mixing (phase  $2\beta$ )  
 $\Rightarrow$  overall phase difference  $2\beta+\gamma$
- Final states are not CP eigenstates. For example:
  - $B^0 \rightarrow D^- \pi^+$  (CKM-favored)
  - $B^0 \rightarrow D^+ \pi^-$  (CKM-suppressed)

$$\sin(2\beta + \gamma)$$

- Coefficient of the sine term in time-dependent asymmetry

$$S_f = -2r_f \sin(2\beta + \gamma - \delta_f)$$

$$S_{\bar{f}} = -2r_f \sin(2\beta + \gamma + \delta_f)$$

where

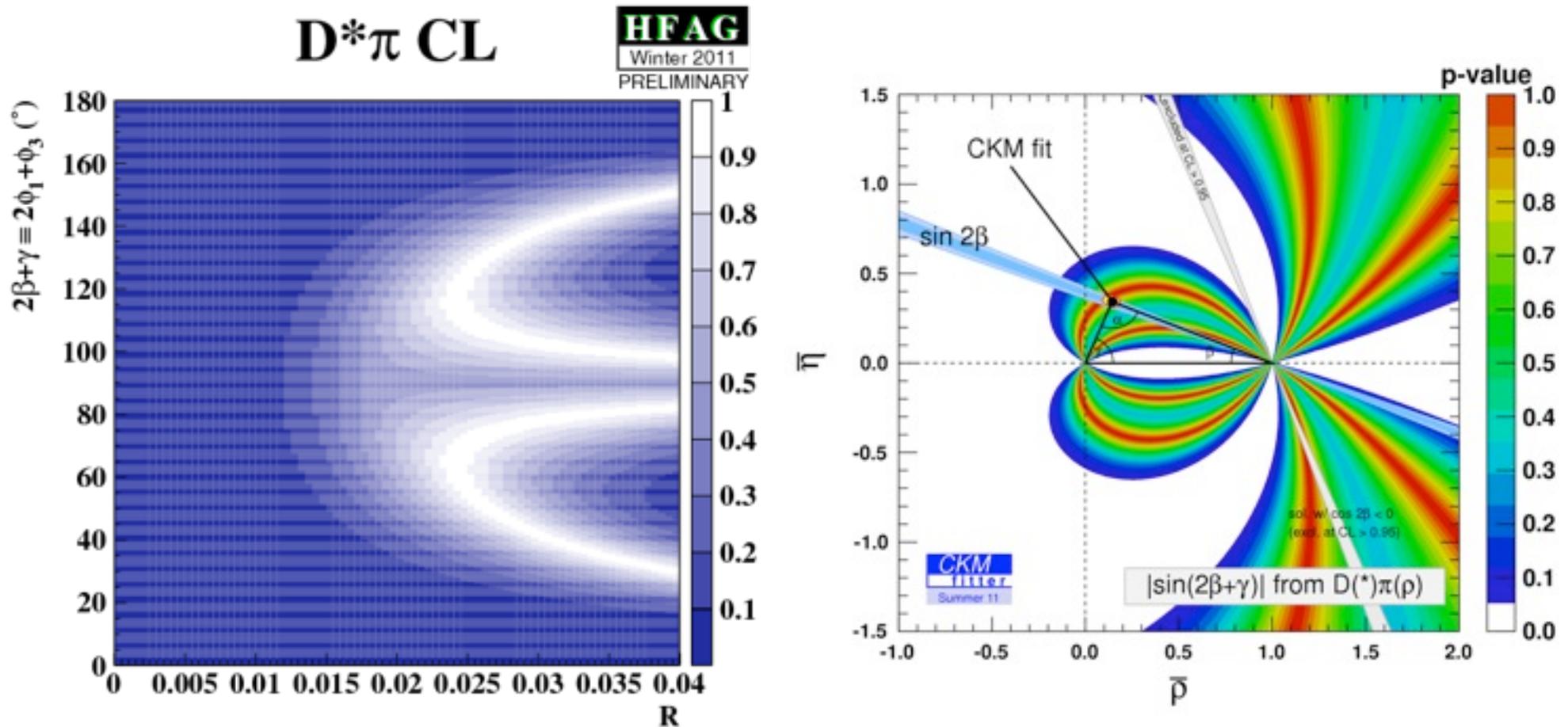
$$r_f = \left| \frac{A_{\text{CKM-suppressed}}}{A_{\text{CKM-favored}}} \right| \quad (\approx 0.01)$$

$\delta_f =$  strong phase

- Measure  $r_f$  in charged B decays, and use isospin relations
- Measure  $S_f$  and  $S_{\bar{f}}$   $\Rightarrow$  clean extraction of  $(2\beta + \gamma)$  and  $\delta_f$

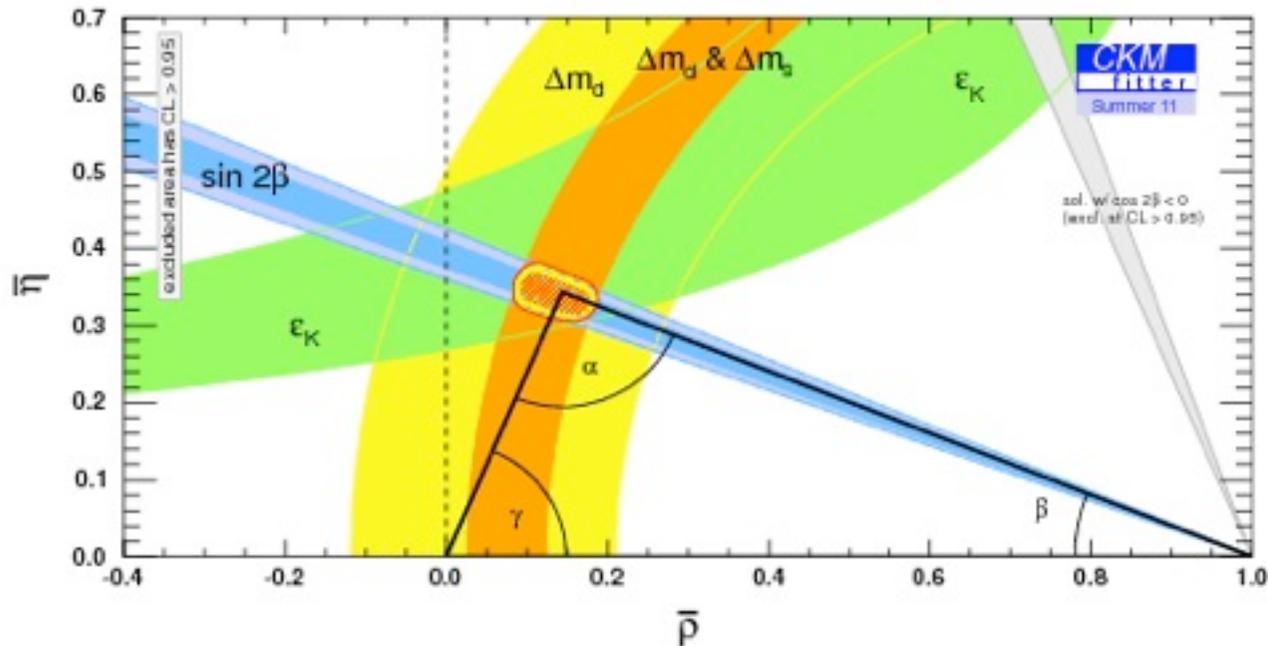
$$\sin(2\beta+\gamma)$$

- The uncertainty on  $r_f$  is large
- In practice, we plot  $\sin(2\beta+\gamma)$  as a function of  $r_f$



# Summary on angle $\beta$

- $\beta$  is the most accurately measured CKM triangle property
- Several modes contribute to the measurement of  $\beta$ 
  - $B \rightarrow (cc)K_S$  decays:
    - all consistent
    - with small theoretical uncertainties
  - $b \rightarrow s$  penguin decays:
    - inconsistencies at the level of  $1-2\sigma$
    - but large theoretical uncertainties



# Measurement of the angle $\alpha$

# Measurement of $\alpha$ in $B^0$ decays

- Measure  $\alpha$  in  $B^0 \rightarrow \pi^+ \pi^-$  and other  $b \rightarrow u \bar{u} d$  processes:
  - the dominant decay amplitude contains the phase  $\gamma$ , and are therefore measuring the relative phase between  $V_{tb}^* V_{td}$  and  $V_{ub}^* V_{ud}$
- Problem in the decay amplitude:
  - the “penguin pollution” has another weak phase ( $\beta$ ) than the dominant tree channel ( $\gamma$ )...
  - ...and is only suppressed at the loop level (and no additional CKM suppression)
- Solution:
  - determine the penguin amplitude from SU(3)-related decays:
    - $B^0(B^0) \rightarrow \pi^+ \pi^-$ ,  $B^\pm \rightarrow \pi^\pm \pi^0$  and  $B^0(B^0) \rightarrow \pi^0 \pi^0$
    - $B^0(B^0) \rightarrow \rho^+ \rho^-$ ,  $B^\pm \rightarrow \rho^\pm \rho^0$  and  $B^0(B^0) \rightarrow \rho^0 \rho^0$

# $\sin 2\alpha$ in presence of penguin pollution (I)

- Define the ratio of the penguin over the tree amplitudes:

$$R_{PT} = \frac{|V_{tb}V_{td}| P_{\pi\pi}^t}{|V_{ub}V_{ud}| T_{\pi\pi}}$$

- $R_{PT}$  can be different for  $\pi^+\pi^-$ ,  $\pi^+\pi^0$  and  $\pi^0\pi^0$
  - $R_{PT}$  can also be defined for  $\rho\rho$  final states
- The parameter  $\lambda$  can then be written as:

$$\lambda_{\pi\pi} = e^{2i\alpha} \left[ \frac{1 - R_{PT}e^{-i\alpha}}{1 - R_{PT}e^{+i\alpha}} \right]$$

- The amplitude of the sine and cosine terms become:

$$S_{\pi\pi} \approx \sin 2\alpha + 2\mathcal{R}e(R_{PT}) \cos 2\alpha \sin \alpha$$

$$C_{\pi\pi} \approx 2\mathcal{I}m(R_{PT}) \sin \alpha$$

# $\sin 2\alpha$ in presence of penguin pollution (II)

$$S_{\pi\pi} \approx \sin 2\alpha + 2\mathcal{R}e(R_{PT}) \cos 2\alpha \sin \alpha$$

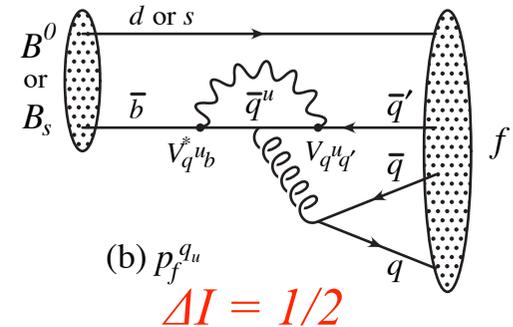
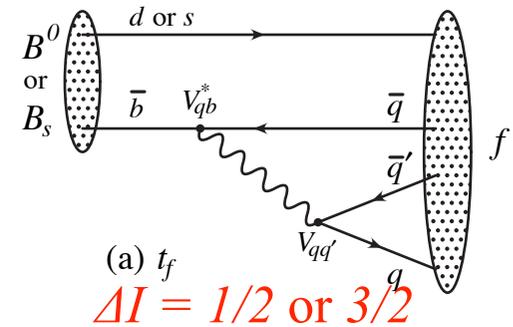
$$C_{\pi\pi} \approx 2\mathcal{I}m(R_{PT}) \sin \alpha$$

- Remarks:

- if relative strong phase  $\delta_{\text{strong}} = 0$  between  $P_{\pi\pi}$  and  $T_{\pi\pi}$ 
  - $\Rightarrow R_{PT}$  is real  $\Rightarrow C_{\pi\pi} = 0$
  - $\Rightarrow$  the size of  $C_{\pi\pi}$  is a measure of  $\delta_{\text{strong}}$
- the measure of  $\sin 2\alpha$  relies on the knowledge of  $R_{PT}$ 
  - $\Rightarrow$  this is the problem of the “penguin pollution”
  - solution by Gronau and London, using isospin relations between measurable amplitudes

# Gronau-London isospin analysis (I)

- The amplitudes for  $B \rightarrow \pi\pi$  are related by isospin symmetry
- Pseudo-scalar  $B$  meson  $\Rightarrow \pi\pi$  system must be in state  $L=0$
- $L=0$  and Bose-Einstein symmetry  $\Rightarrow$  even isospin state ( $I=0$  or  $I=2$ )
- Tree amplitude:  $\Delta I = 1/2$  or  $3/2$   $\Rightarrow I=0$  or  $I=2$  are possible
- $I_{gluon}=0 \Rightarrow$  Penguin amplitude:  $\Delta I = 1/2$   $\Rightarrow I=0$  (and not  $I=2$ )
  - assume electroweak penguins can be neglected ( $\Delta I=3/2$  allowed)
- Accessible isospin states:
  - $B^0(B^0) \rightarrow \pi^+\pi^-$  and  $B^0(B^0) \rightarrow \pi^0\pi^0$  are  $I=0$  or  $I=2$
  - $B^\pm \rightarrow \pi^\pm\pi^0$  is  $I=2$  only



# Gronau-London isospin analysis (II)

- $B \rightarrow \pi\pi$  amplitudes, including Clebsch-Gordan coefficients:

$$A(B^+ \rightarrow \pi^+\pi^0) = \frac{\sqrt{3}}{2} A_{3/2,2}$$

$$\frac{1}{\sqrt{2}} A(B^0 \rightarrow \pi^+\pi^-) = \frac{1}{\sqrt{12}} A_{3/2,2} - \sqrt{\frac{1}{6}} A_{1/2,0}$$

$$A(B^0 \rightarrow \pi^0\pi^0) = \frac{1}{\sqrt{3}} A_{3/2,2} + \sqrt{\frac{1}{6}} A_{1/2,0}$$


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- Therefore, we have the relation

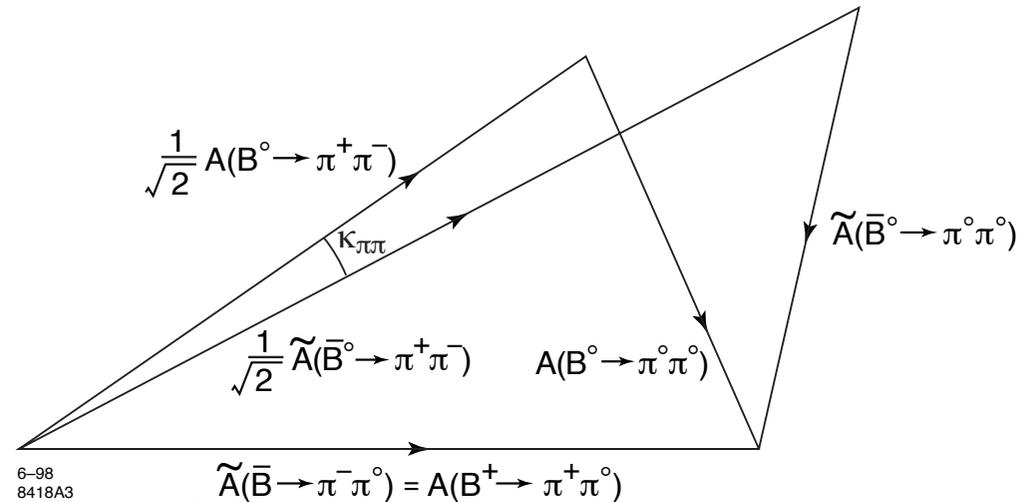
$$\frac{1}{\sqrt{2}} A^{+-} + A^{00} = A^{+0}$$

and its conjugate

$$\frac{1}{\sqrt{2}} \bar{A}^{+-} + \bar{A}^{00} = A^{-0}$$

$\Rightarrow$  build 2 triangles in the complex plane:

- 6 sides can (in principle) be measured
- and the angle  $\kappa$  be determined



Gronau and London, Phys.Rev.Lett. 65 (1990) 3381

# Gronau-London isospin analysis (II)

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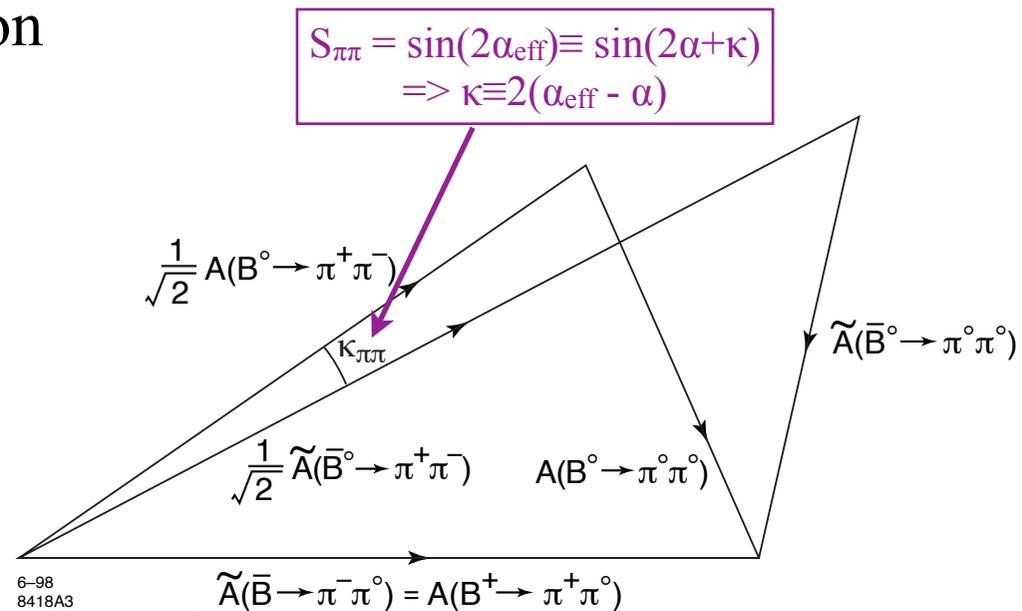
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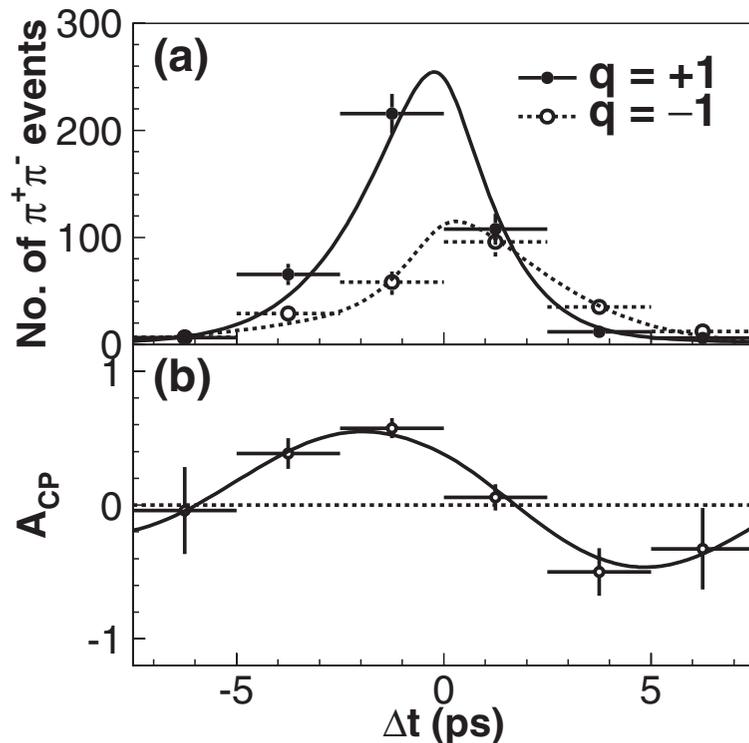
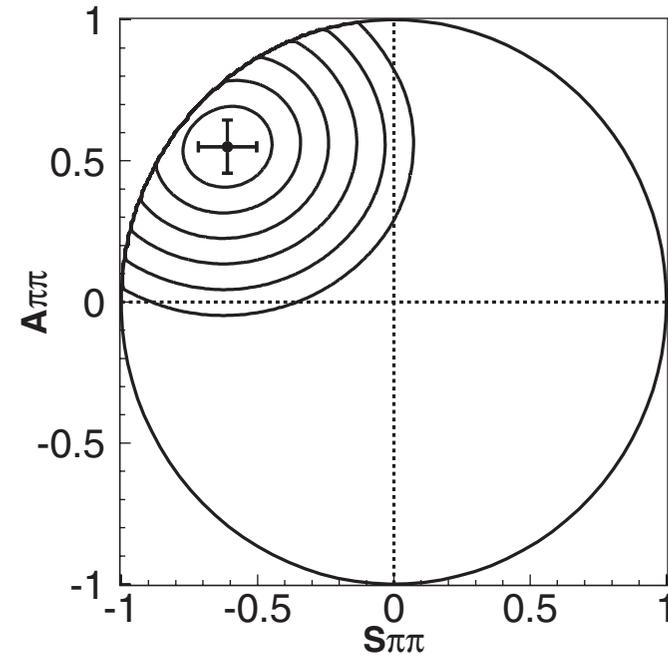
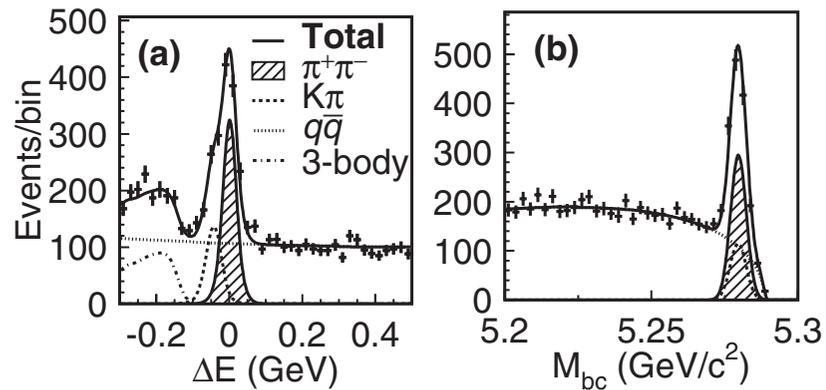
$\Rightarrow$  build 2 triangles in the complex plane:

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# $B^0 \rightarrow \pi^+ \pi^-$ : Belle results

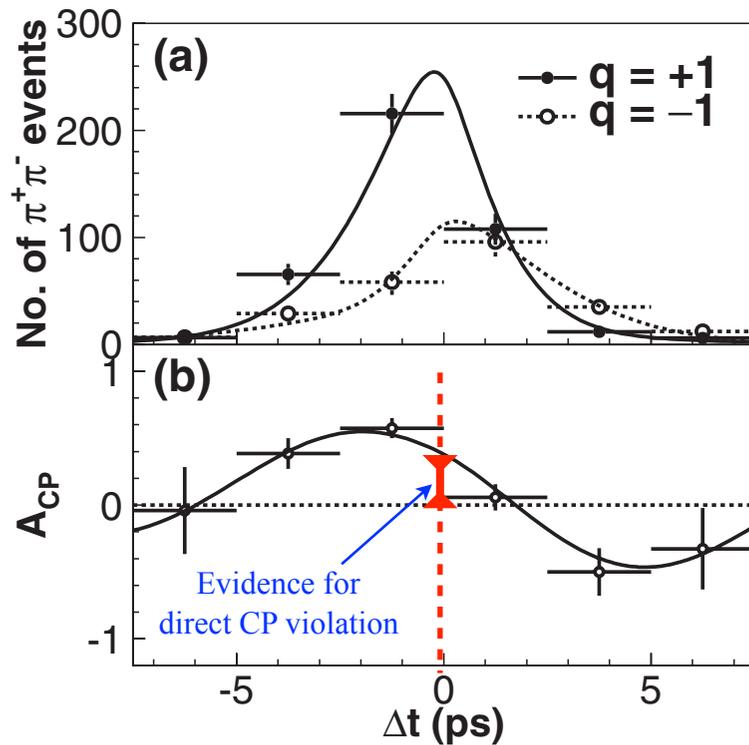
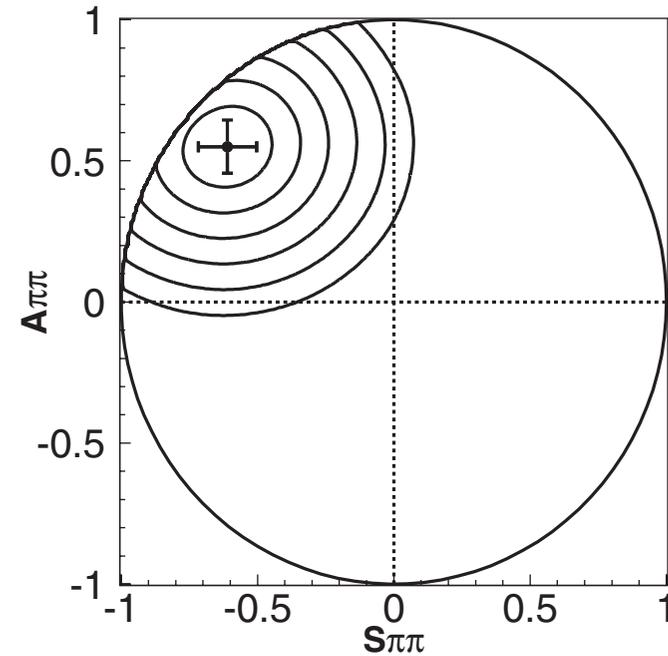
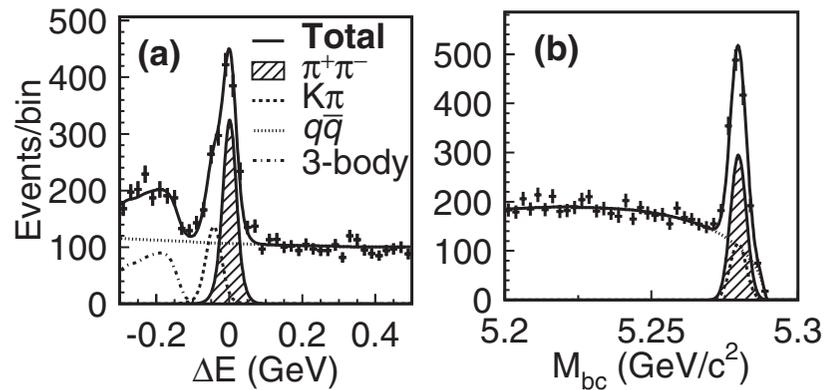
BELLE, PRL 98 (2007) 211801



- Based on  $535 \times 10^6$   $B\bar{B}$  pairs
- $S_{\pi\pi} = -0.61 \pm 0.10_{\text{stat}} \pm 0.04_{\text{syst}}$
- $A_{\pi\pi} = -C_{\pi\pi} = 0.55 \pm 0.08_{\text{stat}} \pm 0.05_{\text{syst}}$

# $B^0 \rightarrow \pi^+ \pi^-$ : Belle results

BELLE, PRL 98 (2007) 211801

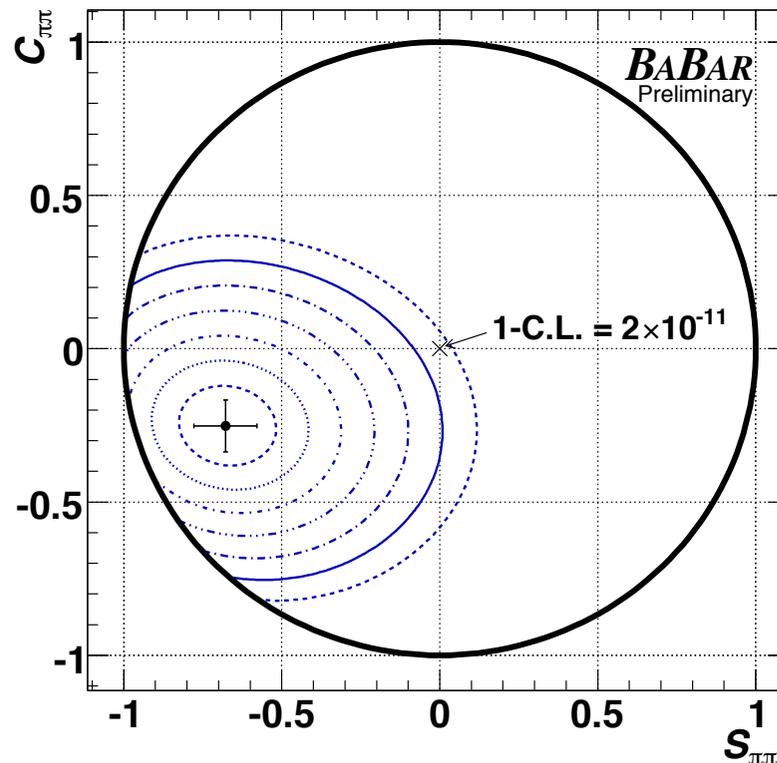
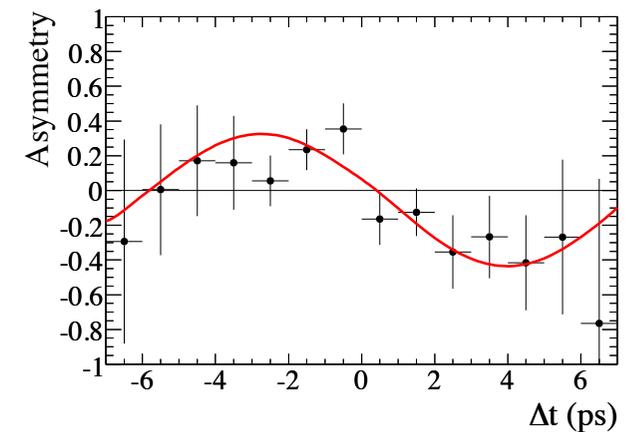
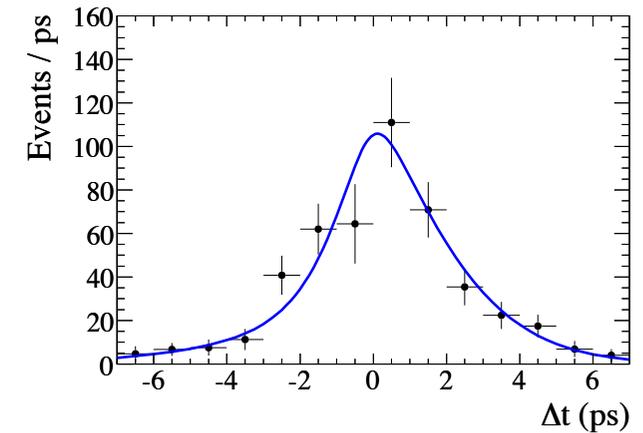
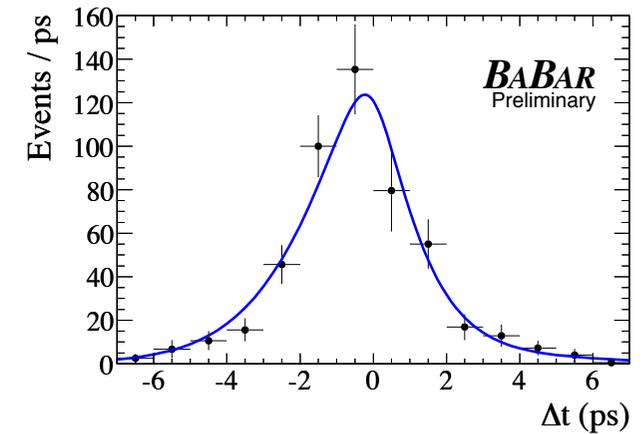


- Based on  $535 \times 10^6$   $B\bar{B}$  pairs
- $S_{\pi\pi} = -0.61 \pm 0.10_{\text{stat}} \pm 0.04_{\text{syst}}$
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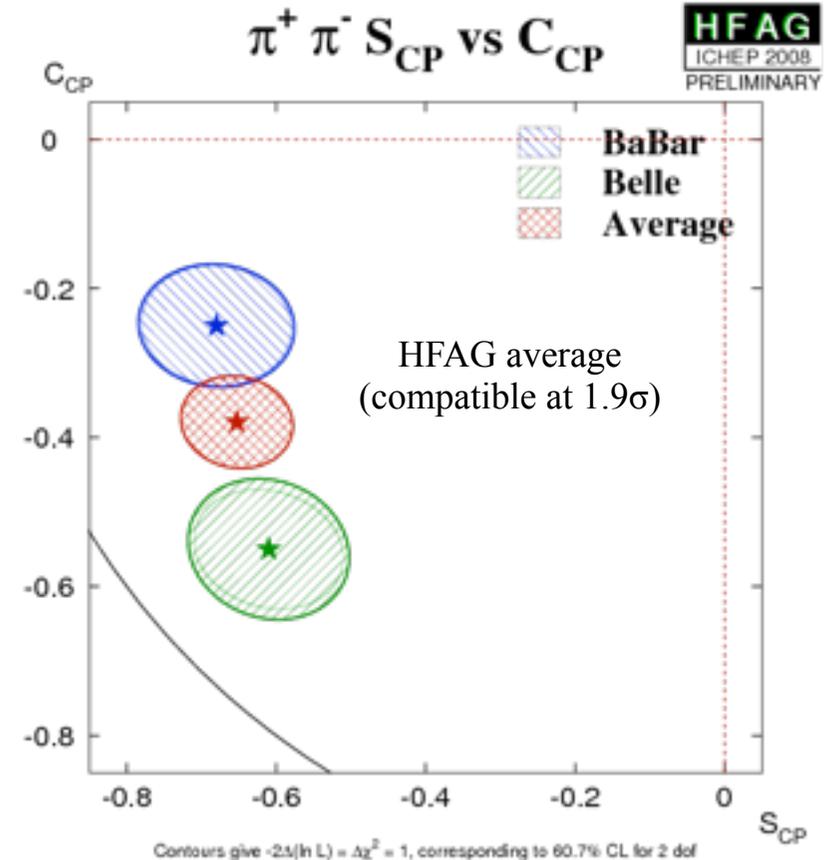
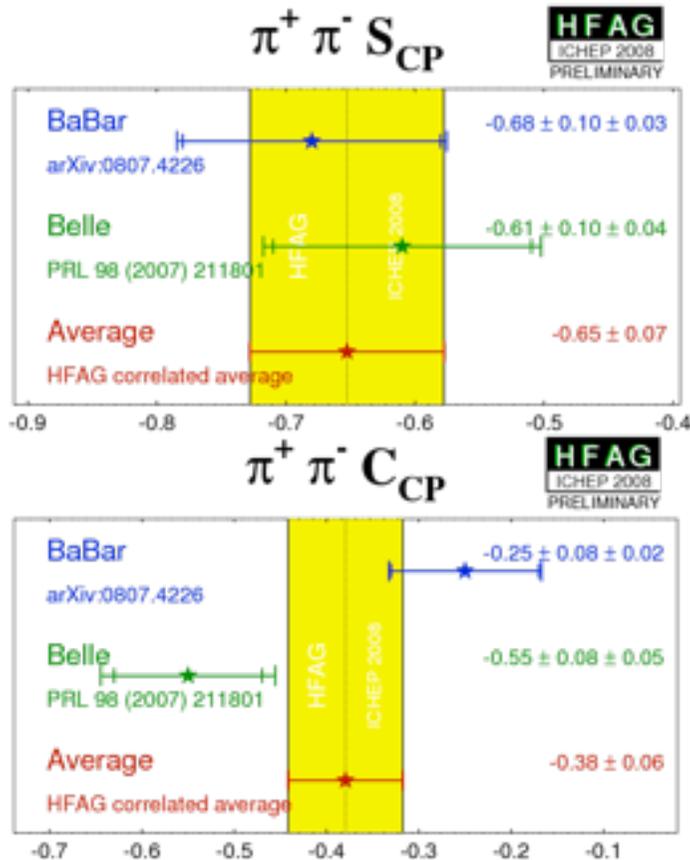
# $B^0 \rightarrow \pi^+ \pi^-$ : BABAR results

BABAR, arXiv:0807.4226

- Based on  $467 \times 10^6$  BB pairs
- $S_{\pi\pi} = -0.68 \pm 0.10_{\text{stat}} \pm 0.03_{\text{syst}}$
- $C_{\pi\pi} = -0.25 \pm 0.08_{\text{stat}} \pm 0.02_{\text{syst}}$



# Combined $B^0 \rightarrow \pi^+ \pi^-$ results



- $C \neq 0 \Rightarrow$  non-zero strong phase between the tree and penguin amplitudes
- $\sin 2\alpha_{eff} = S/(1+C) = -1.05$   
 $\Rightarrow \alpha_{eff} = \sin^{-1}(-0.703)/2 = 135^\circ$  (+3 other solutions...)

# Related $B \rightarrow \pi\pi$ modes

- Branching fractions + charge asymmetries:

$$\mathcal{B}(B^0 \rightarrow \pi^+\pi^-) = (5.16 \pm 0.22) \times 10^{-6}$$

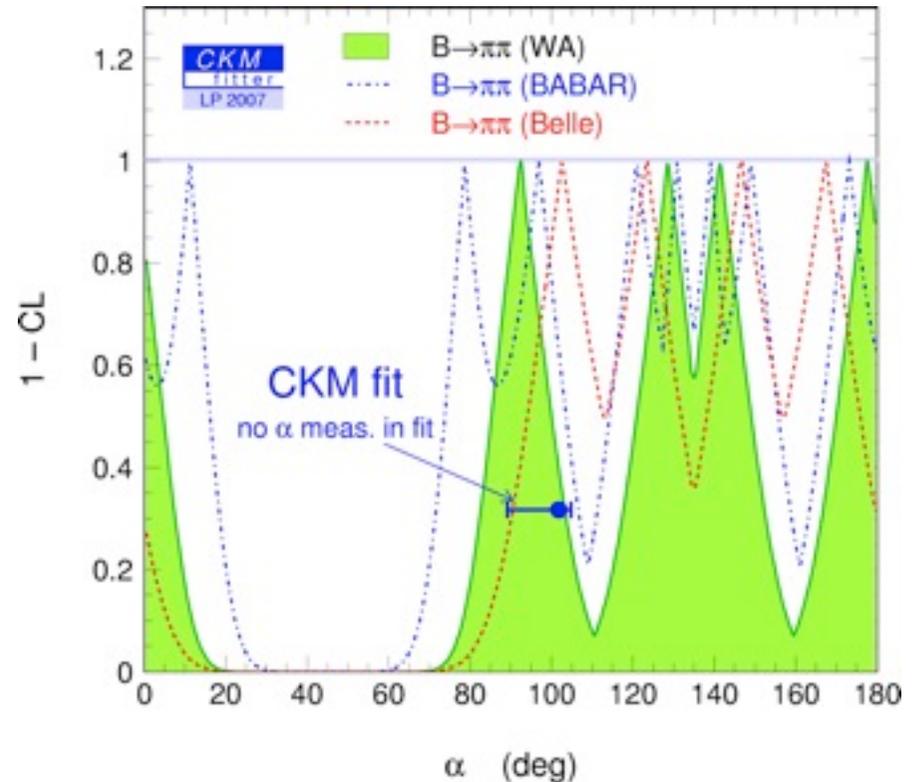
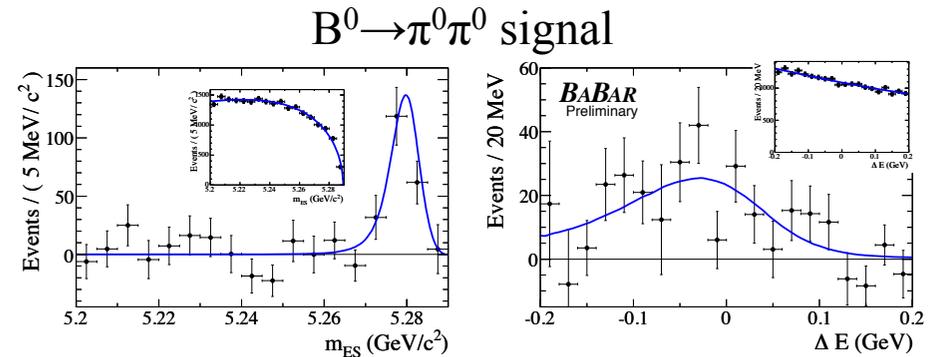
$$\mathcal{B}(B^\pm \rightarrow \pi^\pm\pi^0) = (5.59^{+0.41}_{-0.40}) \times 10^{-6}$$

$$\mathcal{A}_{CP}(B^\pm \rightarrow \pi^\pm\pi^0) = 0.06 \pm 0.05$$

$$\mathcal{B}(B^0 \rightarrow \pi^0\pi^0) = (1.55 \pm 0.19) \times 10^{-6}$$

$$\mathcal{A}_{CP}(B^0 \rightarrow \pi^0\pi^0) = 0.43^{+0.25}_{-0.24}$$

- Combined result for  $\alpha$  determined using method derived from global fit to isospin-related modes (CKM Fitter group, 2007)
  - notice the 4-fold ambiguity
  - main uncertainty from relatively large  $B^0 \rightarrow \pi^0\pi^0$  branching fraction



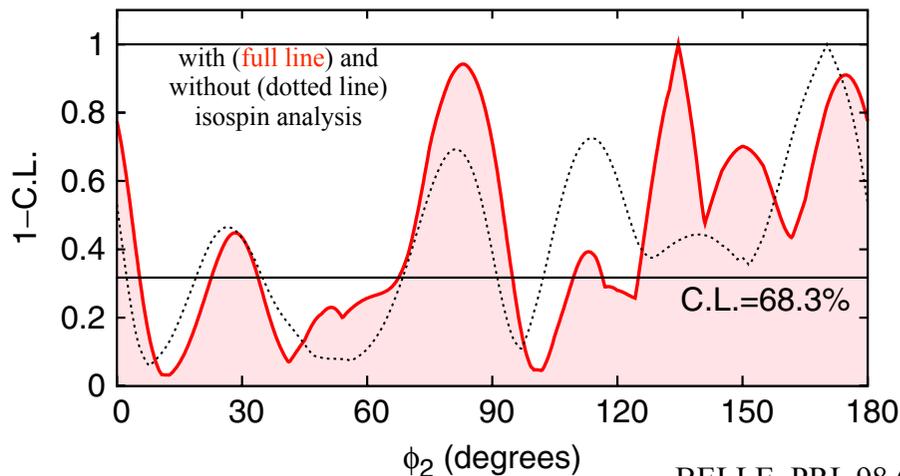
$$B^0 \rightarrow \rho^+ \pi^-$$

- Snyder and Quinn (PRD 48 (1993) 2139) propose a time-dependent Dalitz plot analysis of  $B^\pm \rightarrow \pi^\pm \pi^+ \pi^-$  decays:
  - not a CP eigenstate! 4 decay rates:  $B^+/B^- \rightarrow \pi^+ \pi^+ \pi^- / \pi^- \pi^+ \pi^-$
  - determine the complex amplitudes and the UT angle  $\alpha$
  - fit the time- and Dalitz-plot-dependent decay rate:

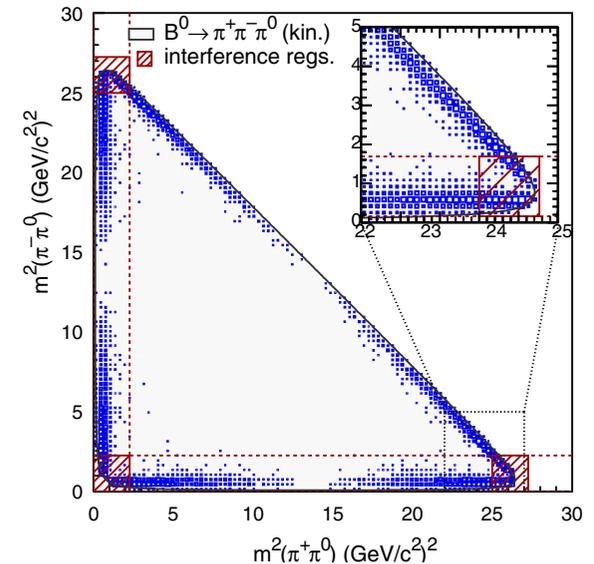
$$\frac{d\Gamma}{d\Delta t ds_+ ds_-} \sim e^{-|\Delta t|/\tau_{B^0}} \left\{ (|A_{3\pi}|^2 + |\bar{A}_{3\pi}|^2) - q_{\text{tag}} (|A_{3\pi}|^2 - |\bar{A}_{3\pi}|^2) \cos(\Delta m_d \Delta t) + q_{\text{tag}} 2\text{Im} \left[ \frac{q}{p} A_{3\pi}^* \bar{A}_{3\pi} \right] \sin(\Delta m_d \Delta t) \right\}$$

- determine 27 observable parameters!

- Belle and BABAR have applied this method



BELLE, PRL 98 (2007) 211801



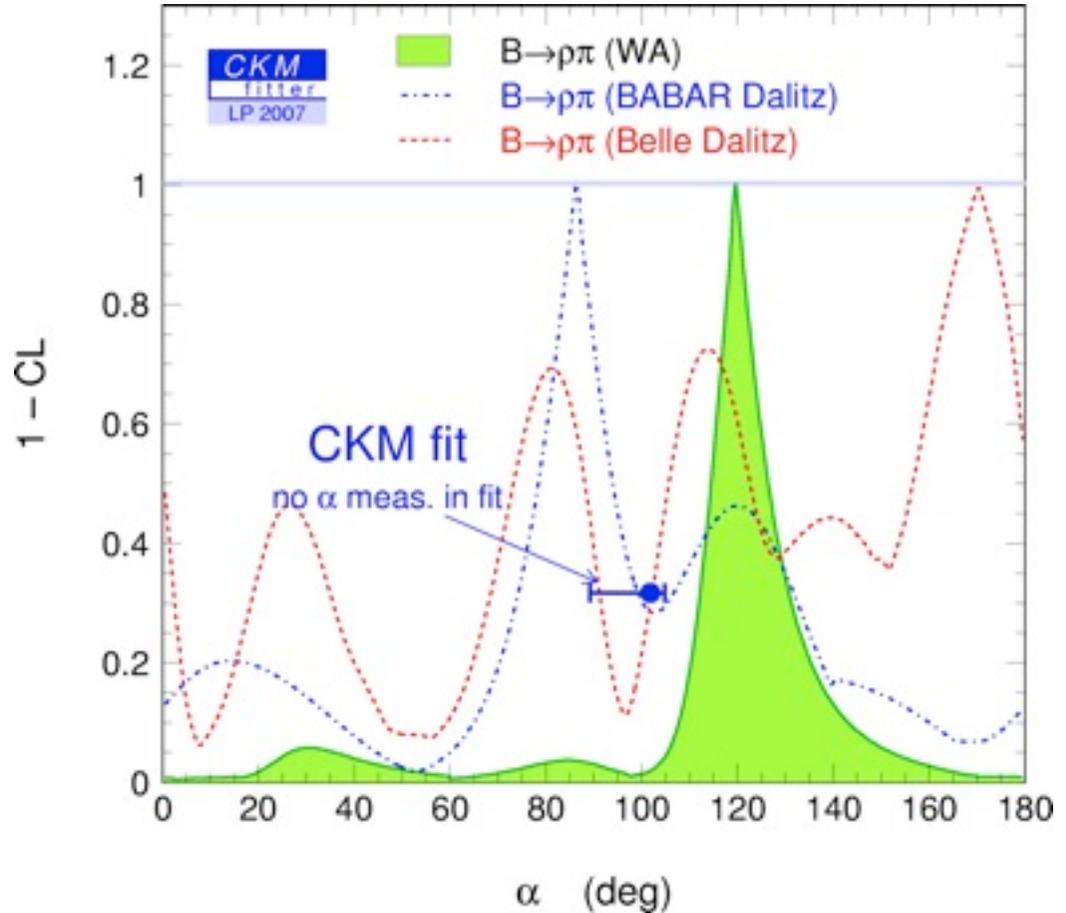
BABAR, PRD 76 (2007) 012004

# $B^0 \rightarrow \rho^+ \pi^-$ combined results

- Combination of the results (CKMFitter group)
  - combine measured parameters from Belle and BABAR
  - use correlation matrices between parameters

TABLE IV. Correlation matrix of statistical uncertainties for the  $U$  and  $I$  coefficients. Since the matrix is symmetric, all elements above the diagonal are omitted.

	$N_{\rho^+}$	$I_0$	$I_+$	$\rho_{\rho^+}^+$	$\rho_{\rho^+}^0$	$I_+$	$\rho_{I_+}^+$	$\rho_{I_+}^0$	$\rho_{I_+}^-$	$\rho_{I_+}^+$	$U_0^+$	$U_0^0$	$U_0^-$	
$N_{\rho^+}$	1.00													
$I_0$	-0.02	1.00												
$I_+$	-0.04	-0.04	1.00											
$\rho_{\rho^+}^+$	-0.09	-0.11	0.28	1.00										
$\rho_{\rho^+}^0$	-0.03	0.28	-0.18	-0.15	1.00									
$I_+$	0.06	-0.04	-0.20	-0.21	0.17	1.00								
$\rho_{I_+}^+$	0.06	-0.03	-0.11	-0.14	0.09	0.38	1.00							
$\rho_{I_+}^0$	-0.17	0.30	0.18	0.17	-0.06	-0.35	-0.45	1.00						
$\rho_{I_+}^-$	0.09	0.11	0.14	-0.17	0.10	0.21	0.11	-0.03	1.00					
$U_0^+$	-0.24	0.04	0.36	0.28	-0.15	-0.46	-0.25	0.43	-0.01	1.00				
$U_0^0$	-0.03	0.07	0.08	-0.05	-0.11	-0.06	-0.02	0.13	0.09	0.15	1.00			
$U_0^-$	0.04	-0.02	0.20	0.32	-0.19	-0.24	-0.19	0.30	-0.13	0.35	0.11	1.00		
$U_{\rho^+}^{++}$	0.01	0.13	-0.11	-0.14	0.42	0.14	0.08	-0.07	0.10	-0.13	-0.36	-0.18	1.00	
$U_{\rho^+}^{+0}$	0.02	0.07	-0.05	-0.44	0.03	0.06	0.05	0.01	0.17	-0.06	0.04	-0.19	0.13	
$U_{\rho^+}^{+ -}$	0.07	0.18	-0.14	-0.39	0.21	0.22	0.18	-0.14	0.27	-0.26	0.03	-0.56	0.31	
$U_{\rho^+}^{0+}$	-0.05	0.16	0.07	-0.21	0.07	-0.01	-0.01	0.14	0.25	0.08	0.09	-0.05	0.19	
$U_{\rho^+}^{00}$	0.11	-0.01	-0.03	-0.06	0.01	0.01	0.02	-0.06	0.01	-0.08	-0.09	-0.08	0.12	
$U_{\rho^+}^{0 -}$	-0.12	0.14	0.08	-0.02	0.08	-0.06	-0.06	0.22	0.06	0.20	0.11	0.18	0.10	
$U_{\rho^+}^{-+}$	0.26	0.03	-0.17	-0.19	0.10	0.17	0.11	-0.20	0.08	-0.40	-0.26	-0.31	0.15	
$U_{\rho^+}^{0+}$	0.13	-0.02	0.00	0.08	-0.18	-0.13	-0.23	0.07	-0.05	-0.05	-0.04	0.03	-0.11	
$U_{\rho^+}^{+-}$	0.03	0.12	-0.17	-0.41	0.36	0.34	0.34	-0.31	0.25	-0.29	-0.02	-0.54	0.29	
$U_{\rho^+}^{++}$	0.23	-0.03	-0.16	-0.25	0.13	0.25	0.28	-0.49	0.16	-0.44	-0.12	-0.36	0.12	
$U_{\rho^+}^{+0}$	-0.14	-0.04	0.03	0.15	-0.04	-0.08	-0.07	0.09	-0.11	0.19	0.01	0.13	-0.08	
$U_{\rho^+}^{+ -}$	-0.12	-0.10	-0.05	0.14	-0.05	-0.01	-0.04	-0.01	-0.20	0.07	-0.10	0.09	-0.04	
$U_{\rho^+}^{0+}$	0.12	-0.20	-0.09	0.18	-0.21	-0.03	-0.01	-0.17	-0.18	-0.22	-0.17	0.02	-0.17	
$U_{\rho^+}^{00}$	-0.15	0.05	0.07	0.01	0.06	0.00	-0.03	0.12	0.22	0.13	0.10	0.10	0.03	
$U_{\rho^+}^{0 -}$	-0.05	-0.01	0.00	0.05	-0.06	-0.07	-0.05	0.05	-0.03	0.04	-0.03	0.05	-0.04	
$U_{\rho^+}^{++}$	1.00													
$U_{\rho^+}^{+0}$	0.36	1.00												
$U_{\rho^+}^{+ -}$	0.34	0.25	1.00											
$U_{\rho^+}^{0+}$	0.19	0.06	0.03	1.00										
$U_{\rho^+}^{00}$	0.11	0.20	0.28	-0.13	1.00									
$U_{\rho^+}^{0 -}$	0.07	0.22	-0.04	0.10	-0.16	1.00								
$U_{\rho^+}^{++}$	-0.01	-0.08	-0.05	0.07	-0.05	0.32	1.00							
$U_{\rho^+}^{+0}$	0.22	0.56	0.17	-0.00	0.05	0.20	-0.25	1.00						
$U_{\rho^+}^{+ -}$	0.08	0.23	0.02	0.11	-0.31	0.37	-0.06	0.41	1.00					
$U_{\rho^+}^{0+}$	-0.15	-0.20	-0.11	-0.27	-0.05	-0.15	-0.03	-0.12	-0.17	1.00				
$U_{\rho^+}^{00}$	-0.12	-0.19	-0.21	0.08	0.02	-0.07	0.03	-0.16	-0.16	0.09	1.00			
$U_{\rho^+}^{0 -}$	-0.22	-0.33	-0.35	0.06	-0.48	0.15	0.22	-0.33	0.12	0.10	0.12	1.00		
$U_{\rho^+}^{++}$	0.03	-0.04	0.17	-0.02	0.10	-0.19	-0.19	0.05	-0.07	0.03	-0.15	-0.24	1.00	
$U_{\rho^+}^{+0}$	-0.02	-0.03	-0.03	-0.07	0.11	0.14	0.30	-0.11	-0.11	0.18	0.20	0.02	-0.12	1.00



- Result:  $\alpha = (120^{+11}_{-7})^\circ$

$$B^0 \rightarrow \rho^+ \rho^-$$

- $B^0 \rightarrow \rho^+ \rho^-$  is sensitive to  $\alpha$  (similar to  $\pi^+ \pi^-$  mode)
  - penguin amplitude separated using  $B^\pm \rightarrow \rho^\pm \rho^0$  and  $B^0 \rightarrow \rho^0 \rho^0$
  - difference with  $\pi^+ \pi^-$  : the rho meson is a vector
    - => mixture of CP-odd and CP-even components in final state
    - => thought to make the analysis difficult
- However
  1. the longitudinal polarization fraction  $f_L$  are measured to be close to unity => final state mostly CP-even!
  2. in addition, the branching fraction for  $B^0 \rightarrow \rho^0 \rho^0$  is small

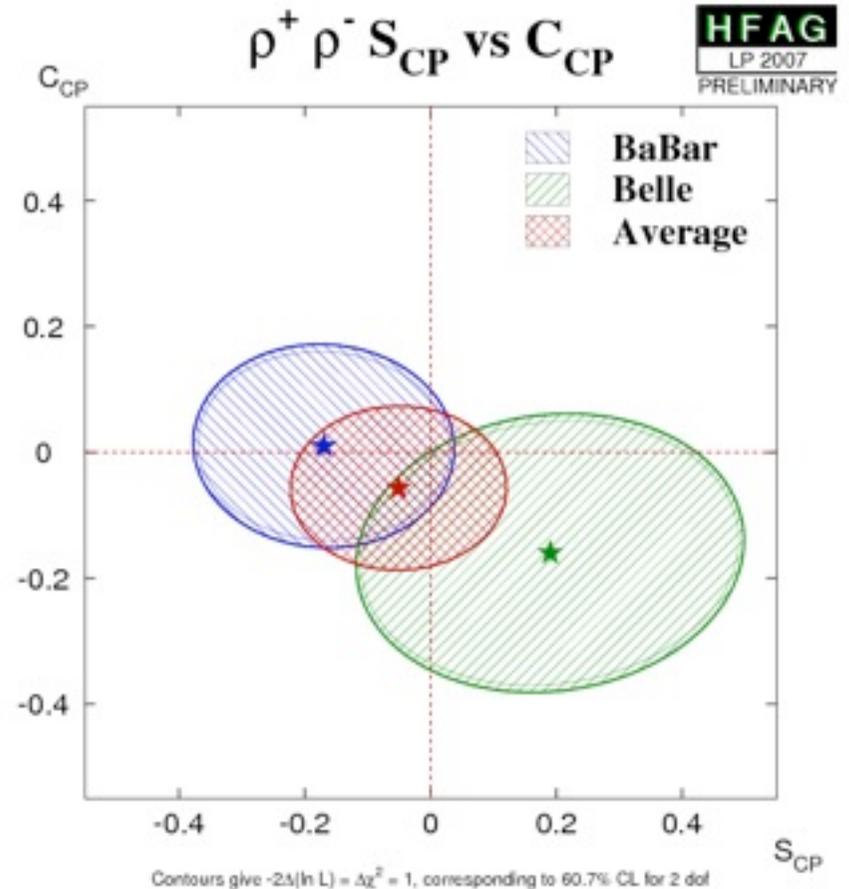
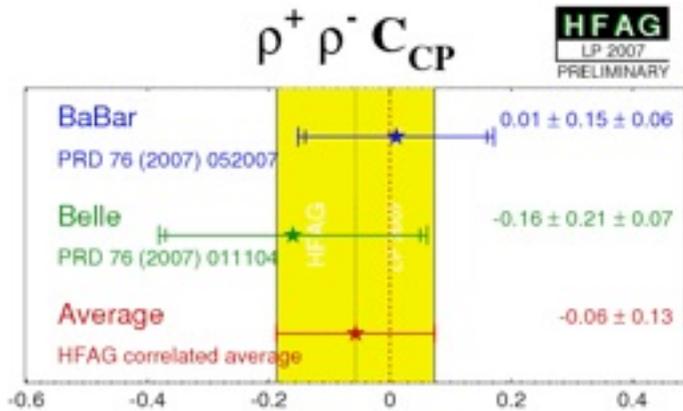
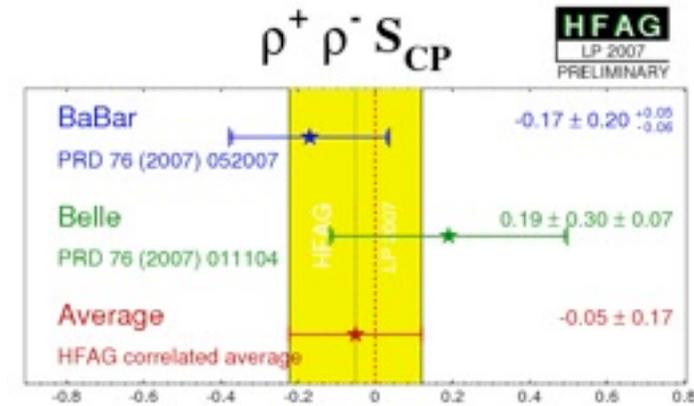
$$\mathcal{B}(B^0 \rightarrow \rho^+ \rho^-) = (24.2_{-3.2}^{+3.1}) \times 10^{-6}$$

$$\mathcal{B}(B^\pm \rightarrow \rho^\pm \rho^0) = (24.0_{-2.0}^{+1.9}) \times 10^{-6}$$

$$\mathcal{B}(B^0 \rightarrow \rho^0 \rho^0) = (0.73_{-0.28}^{+0.27}) \times 10^{-6}$$

- => the penguin amplitude is negligible
- => clean measurement of  $\alpha$ ! ( $\alpha \approx \alpha_{eff}$ )

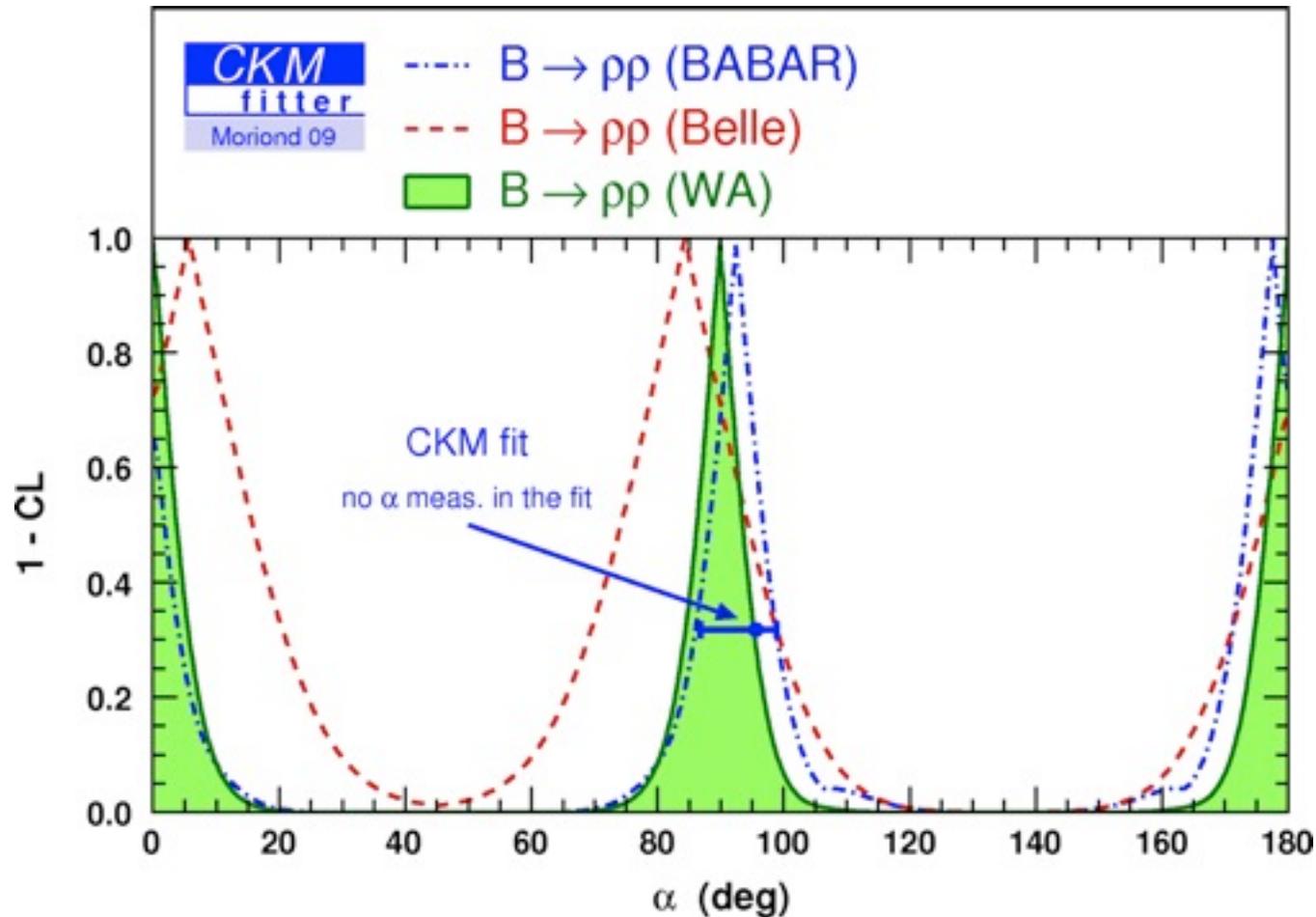
# $B^0 \rightarrow \rho^+ \rho^-$ combined results



- $C \approx 0 \Rightarrow \sin 2\alpha_{eff} = S/(1+C) \approx S = -0.05$
- Penguin amplitude  $\approx 0 \Rightarrow \alpha_{eff} \approx \alpha$   
 $\Rightarrow \alpha \approx \sin^{-1}(-0.05)/2 = 89^\circ (+3 \text{ other solutions...})$

# Angle $\alpha$ from $B^0 \rightarrow \rho^+ \rho^-$

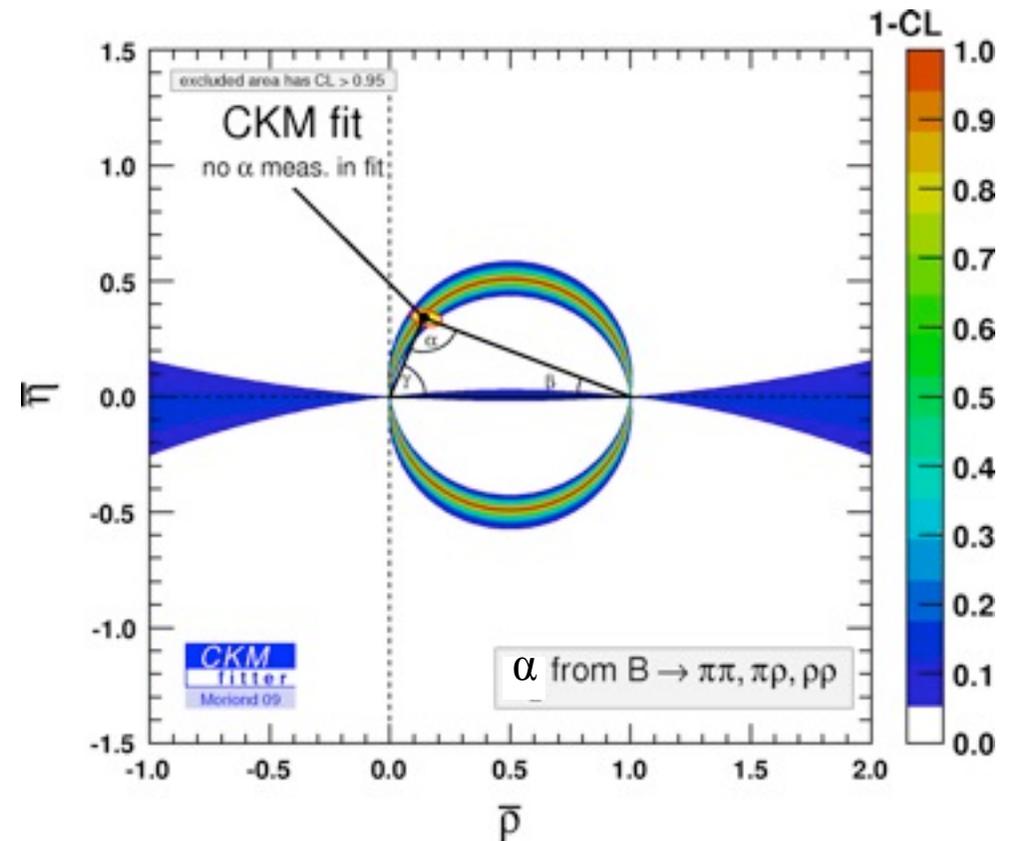
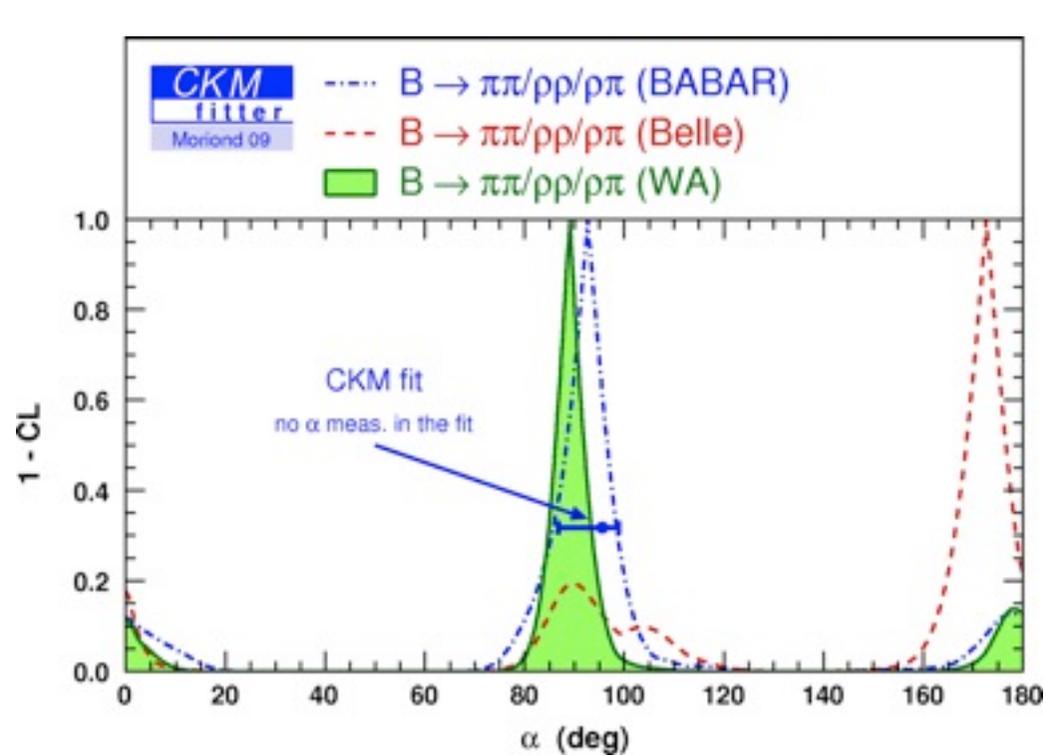
- Combined result for  $\alpha$  (CKMFitter group)



- Result:  $\alpha = (89.9 \pm 5.4)^\circ$   
=> most accurate measurement for  $\alpha$ !!!

# Summary on angle $\alpha$

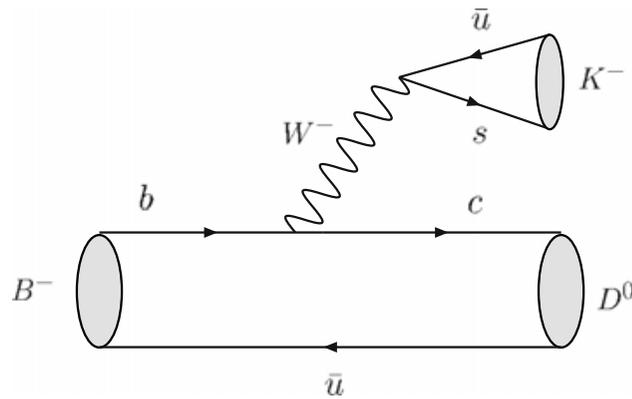
- The UT angle  $\alpha$  is measured in several modes, most noticeably in  $B \rightarrow \pi\pi$ ,  $\rho\pi$ , and  $\rho\rho$
- Average from CKMFitter:  $\alpha = (89.0^{+4.4}_{-4.2})^\circ$ 
  - compare to  $\alpha = (97.5^{+1.6}_{-8.1})^\circ$  from indirect measurement



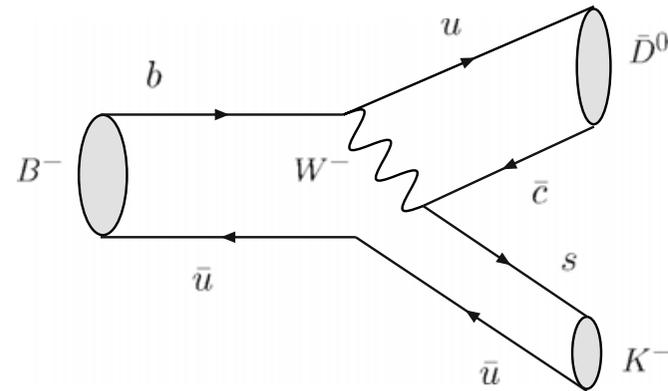
# Measurement of the angle $\gamma$

# Measurement of $\gamma$ in $B$ decays

- Measure  $\gamma$ , the relative phase between  $V_{ub}^* V_{ud}$  and  $V_{cb}^* V_{cd}$ , in  $B \rightarrow DK$  decays
  - exploit the interference between  $D^0$  and  $D^{\bar{0}}$  decays to a common CP eigenstate



no weak phase



weak phase of  $V_{ub}$  ( $=\gamma$ )

- Only UT angle measurable with tree processes only

# Extracting $\gamma$ from $B \rightarrow DK$ measurements

- Define the ratio of amplitudes

$$r_B e^{i\delta_B} = \frac{\mathcal{A}(B^+ \rightarrow D^0 K^+)}{\mathcal{A}(B^+ \rightarrow \bar{D}^0 K^+)}$$

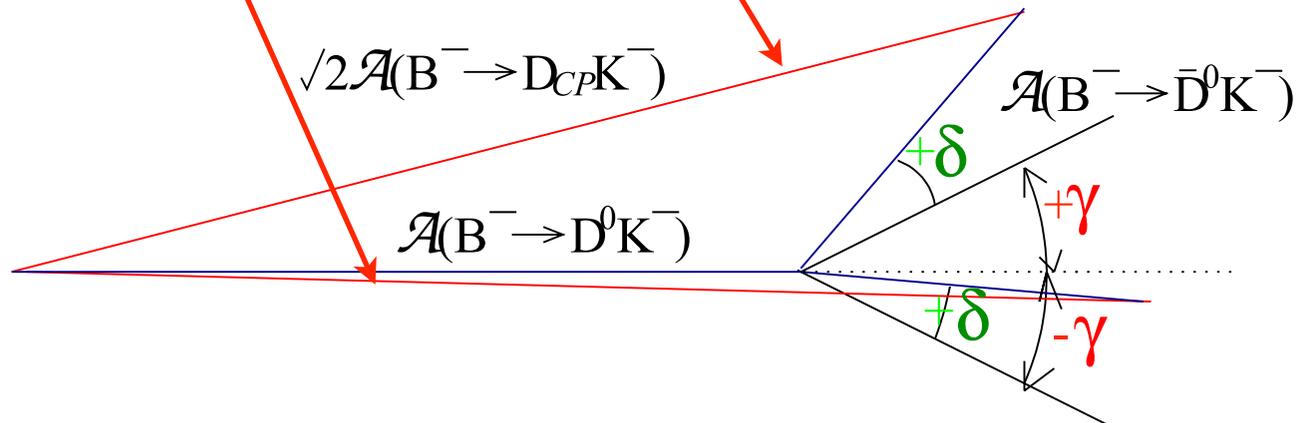
- Determine the decay rates to neutral D mesons in CP-even ( $D_1$ ) and CP-odd ( $D_2$ ) states

$$\mathcal{A}(B^- \rightarrow D_1 K^-) \propto \frac{1}{2} (1 + r_B e^{i(\delta_B - \gamma)}) \longrightarrow \Gamma(B^- \rightarrow D_1 K^-) \propto 1 + r_B^2 + 2r_B \cos(\delta_B - \gamma)$$

$$\mathcal{A}(B^- \rightarrow D_2 K^-) \propto \frac{1}{2} (1 - r_B e^{i(\delta_B - \gamma)}) \longrightarrow \Gamma(B^- \rightarrow D_2 K^-) \propto 1 + r_B^2 - 2r_B \cos(\delta_B - \gamma)$$

$$\mathcal{A}(B^+ \rightarrow D_1 K^+) \propto \frac{1}{2} (1 + r_B e^{i(\delta_B + \gamma)}) \longrightarrow \Gamma(B^+ \rightarrow D_1 K^+) \propto 1 + r_B^2 + 2r_B \cos(\delta_B + \gamma)$$

$$\mathcal{A}(B^+ \rightarrow D_2 K^+) \propto \frac{1}{2} (1 - r_B e^{i(\delta_B + \gamma)}) \longrightarrow \Gamma(B^+ \rightarrow D_2 K^+) \propto 1 + r_B^2 - 2r_B \cos(\delta_B + \gamma)$$



# Extracting $\gamma$ from $B \rightarrow DK$ : remarks

- CP violating effects will be most visible for large  $r_B$ 
  - $r_B$  is typically 0.1-0.2
- Rate ( $\Gamma$ ) measurements alone  $\Rightarrow r_B \cos(\delta_{B\pm\gamma})$   
 $\Rightarrow$  ambiguities in determination of  $\gamma$ 
  - resolved in Dalitz plot analyses  $\Rightarrow r_B \sin(\delta_{B\pm\gamma})$
- Various methods:
  - “GLW” analyses
  - “ADS” analyses
  - Dalitz analyses

# GLW analyses

- Use  $D^0$  decays to
  - $\pi^+\pi^-, K^+K^-$  (CP even)
  - $K_S\pi^0, K_S\phi$  (CP odd)
- Observables:

Gronau and London, PLB 253 (1991) 483  
 Gronau and Wyler, PLB 265 (1991) 172

- the asymmetry

$$\begin{aligned} \mathcal{A}_{1,2} &\equiv \frac{\mathcal{B}(B^- \rightarrow D_{1,2}K^-) - \mathcal{B}(B^+ \rightarrow D_{1,2}K^+)}{\mathcal{B}(B^- \rightarrow D_{1,2}K^-) + \mathcal{B}(B^+ \rightarrow D_{1,2}K^+)} \\ &= \frac{2r_B \sin \delta' \sin \gamma}{1 + r_B^2 + 2r_B \cos \delta' \cos \gamma} \end{aligned}$$

- and the double ratio

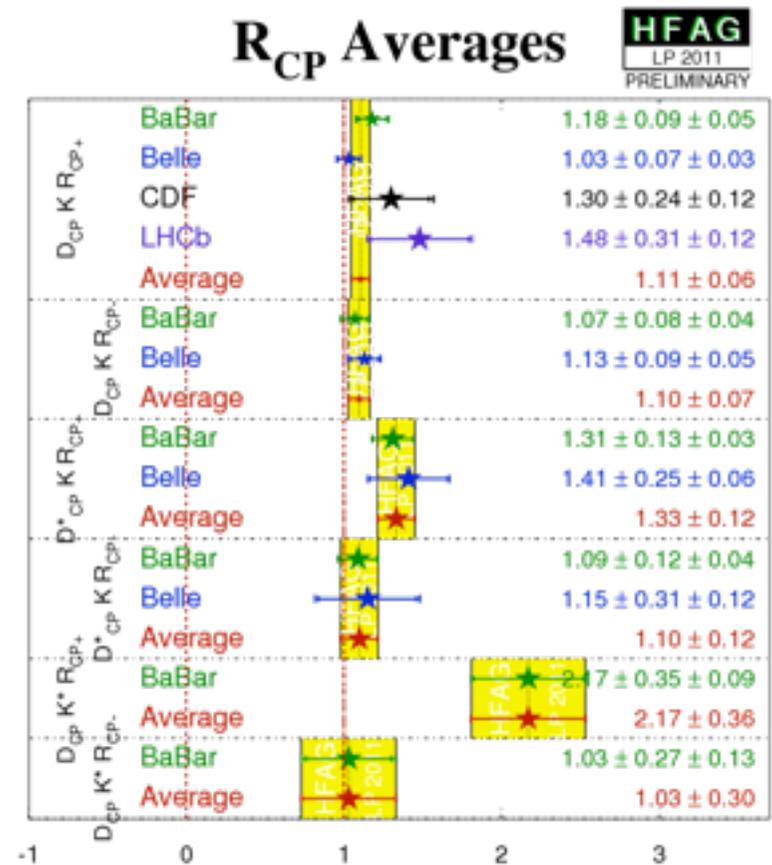
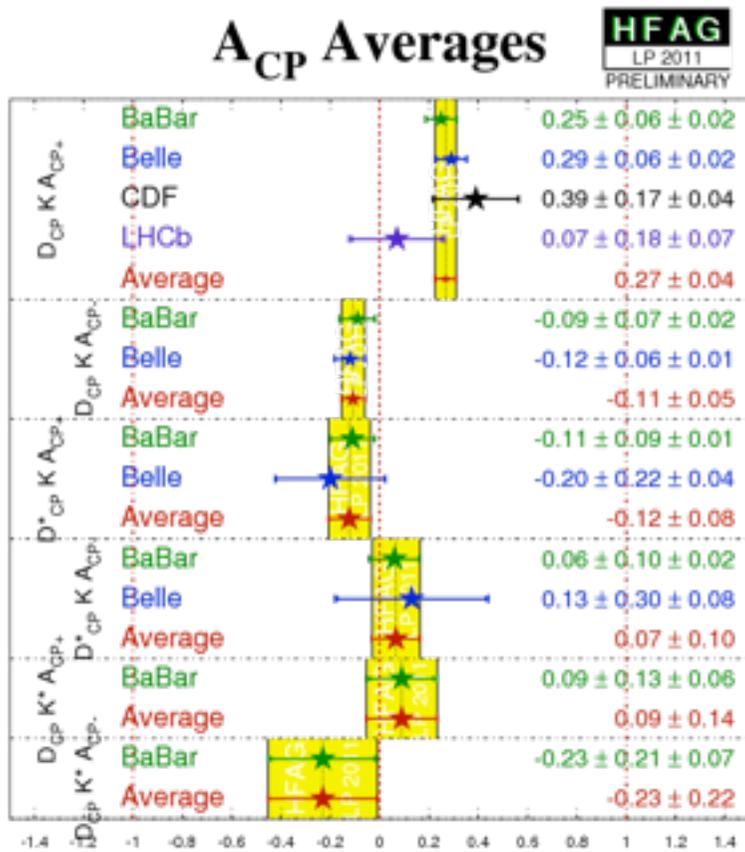
$$\begin{aligned} \mathcal{R}_{1,2} &\equiv \frac{\mathcal{B}(B^- \rightarrow D_{1,2}K^-) + \mathcal{B}(B^+ \rightarrow D_{1,2}K^+)}{\mathcal{B}(B^- \rightarrow D^0K^-) + \mathcal{B}(B^+ \rightarrow D^0K^+)} \\ &= 1 + r_B^2 + 2r_B \cos \delta' \cos \gamma, \end{aligned}$$

$$\delta' = \begin{cases} \delta_B & \text{for } D_1 \\ \delta_B + \pi & \text{for } D_2, \end{cases}$$

- Main difficulty:
  - small  $r_B \Rightarrow$  small measurable CP asymmetry

# GLW analyses: results

- Belle, BABAR, CDF, and LHCb measured the asymmetries  $A$  and ratios  $R$



# ADS analyses

Atwood et.al., PRL 78 (1997) 3257  
Atwood et.al., PRD 63 (2001) 036005

- To alleviate the problem of the small value of  $r_B$ , consider  $D^0$  decays to  $K^+\pi^-$  (and  $K^-\pi^+$ ) such that:
  - suppressed  $B$  decay correspond to Cabibbo-allowed  $D^0$  decay
  - and vice versa
    - $\Rightarrow$  interference from processes with similar amplitudes
    - $\Rightarrow$  larger CP violation is expected

- Observables:

$$\begin{aligned}\mathcal{R}_{ADS} &= \frac{\mathcal{B}(B^\pm \rightarrow [K^\mp \pi^\pm]_D K^\pm)}{\mathcal{B}(B^\pm \rightarrow [K^\pm \pi^\mp]_D K^\pm)} \\ &= r_B^2 + r_D^2 + 2r_B r_D \cos \gamma \cos \delta\end{aligned}$$

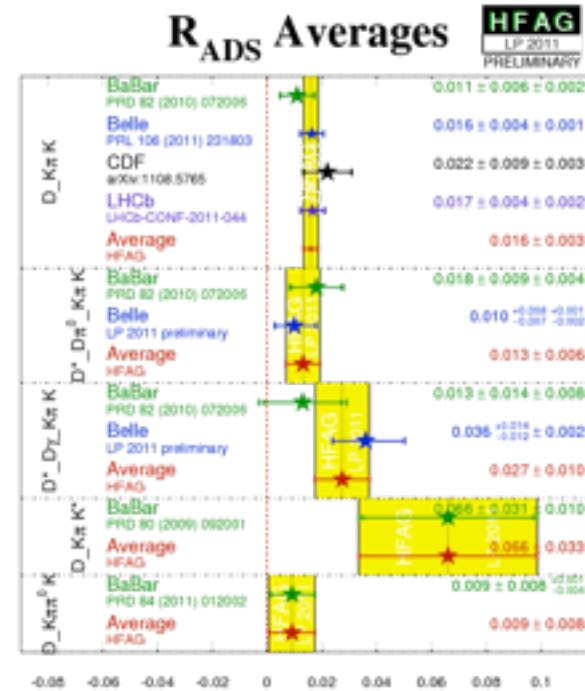
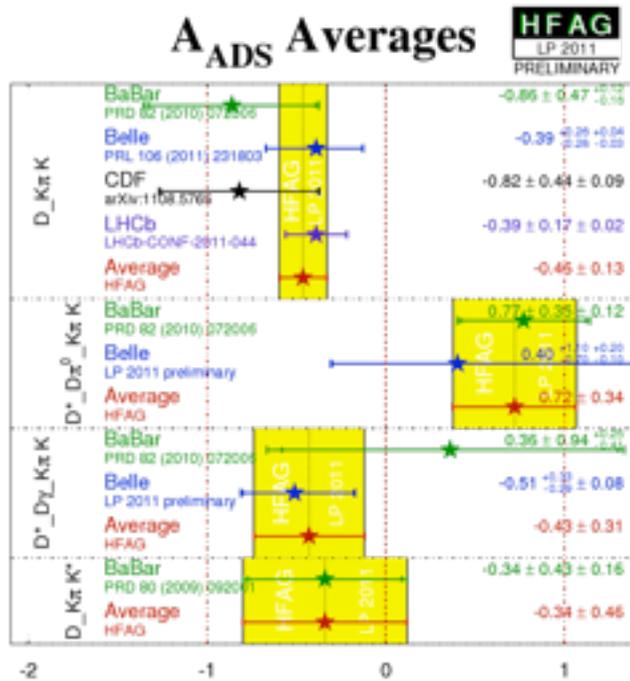
$$r_D = \left| \frac{A(D^0 \rightarrow K^+\pi^-)}{A(D^0 \rightarrow K^-\pi^+)} \right| = 0.058 \pm 0.001$$

$$\delta = \delta_B + \delta_D$$

$$\begin{aligned}\mathcal{A}_{ADS} &= \frac{\mathcal{B}(B^- \rightarrow [K^+\pi^-]_D K^-) - \mathcal{B}(B^+ \rightarrow [K^-\pi^+]_D K^+)}{\mathcal{B}(B^- \rightarrow [K^+\pi^-]_D K^-) + \mathcal{B}(B^+ \rightarrow [K^-\pi^+]_D K^+)} \\ &= \frac{2r_B r_D \sin \gamma \sin \delta}{r_B^2 + r_D^2 + 2r_B r_D \cos \gamma \cos \delta}.\end{aligned}$$

# ADS analyses: results

- Results by Belle, BABAR, CDF, and LHCb



- Currently not sensitive to angle  $\gamma$   
...but useful constraint on  $r_B$

$$r_B < 0.19 \text{ at } 90\% \text{ CL}$$

# $\gamma$ from Dalitz plot analyses

- $B \rightarrow D^0 K$  with  $D^0 \rightarrow K_S \pi^+ \pi^-$ 
  - Dalitz plot analysis of the  $D^0$  decay allows to determine all the information in a single mode  
=> measure of  $\gamma$  with 2-fold ambiguity
- Evidence for direct CP violation from BABAR and Belle

BABAR

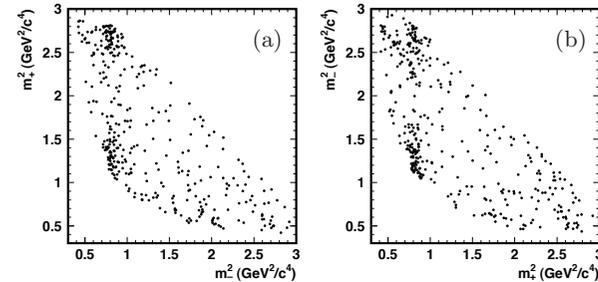
$$\gamma = (68 \pm 14 \pm 4 \pm 3)^\circ$$

Parameter	68.3% CL	95.4% CL
$\gamma$ ( $^\circ$ )	$68_{-14}^{+15}$ {4, 3}	[39, 98]
$r_B$ (%)	$9.6 \pm 2.9$ {0.5, 0.4}	[3.7, 15.5]
$r_B^*$ (%)	$13.3_{-3.9}^{+4.2}$ {1.3, 0.3}	[4.9, 21.5]
$\kappa r_s$ (%)	$14.9_{-6.2}^{+6.6}$ {2.6, 0.6}	< 28.0
$\delta_B$ ( $^\circ$ )	$119_{-20}^{+19}$ {3, 3}	[75, 157]
$\delta_B^*$ ( $^\circ$ )	$-82 \pm 21$ {5, 3}	[-124, -38]
$\delta_s$ ( $^\circ$ )	$111 \pm 32$ {11, 3}	[42, 178]

BABAR, arXiv:1005.1096

Belle

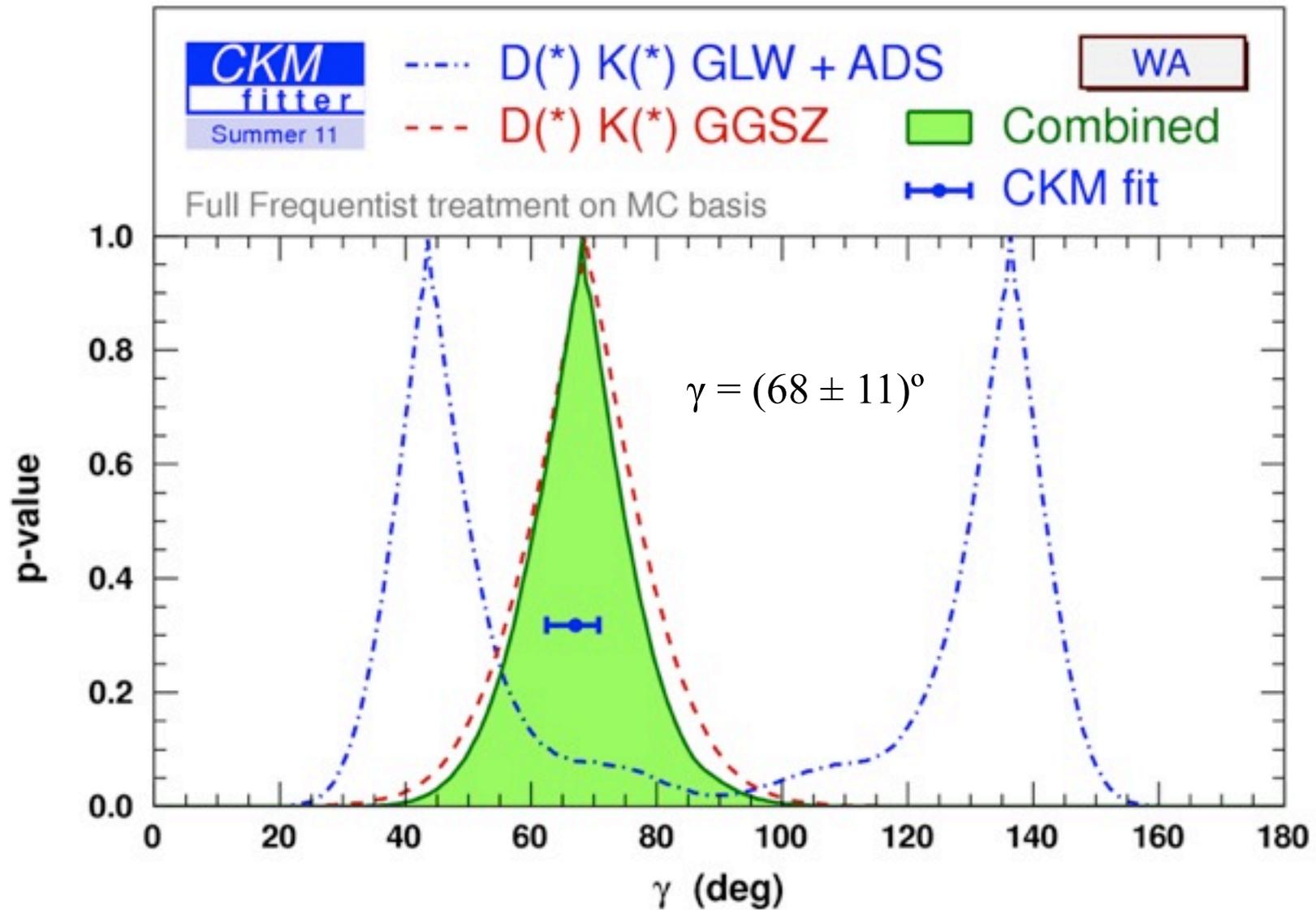
$$\gamma = (78.4^{+10.8}_{-11.6} \pm 3.6 \pm 8.9)^\circ$$



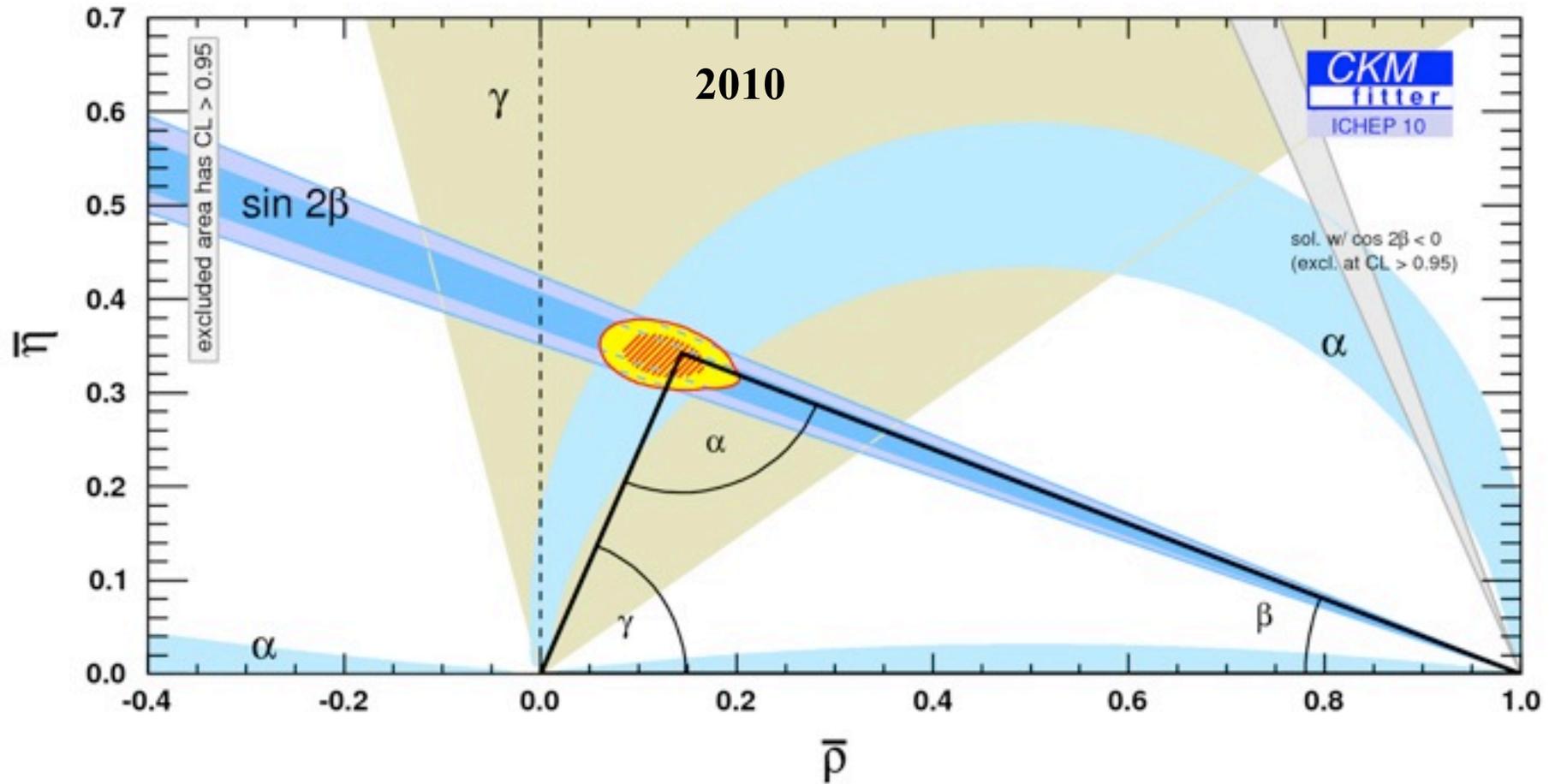
Parameter	$1\sigma$ interval	$2\sigma$ interval	Systematic error	Model uncertainty
$\phi_3$	$(78.4_{-11.6}^{+10.8})^\circ$	$54.2^\circ < \phi_3 < 100.5^\circ$	$3.6^\circ$	$8.9^\circ$
$r_{DK}$	$0.160_{-0.038}^{+0.040}$	$0.084 < r_{DK} < 0.239$	0.011	+0.050 -0.010
$r_{D^*K}$	$0.196_{-0.069}^{+0.072}$	$0.061 < r_{D^*K} < 0.271$	0.012	+0.062 -0.012
$\delta_{DK}$	$(136.7_{-15.8}^{+13.0})^\circ$	$102.2^\circ < \delta_{DK} < 162.3^\circ$	$4.0^\circ$	$22.9^\circ$
$\delta_{D^*K}$	$(341.9_{-19.6}^{+18.0})^\circ$	$296.5^\circ < \delta_{D^*K} < 382.7^\circ$	$3.0^\circ$	$22.9^\circ$

BELLE, arXiv:1003.3360

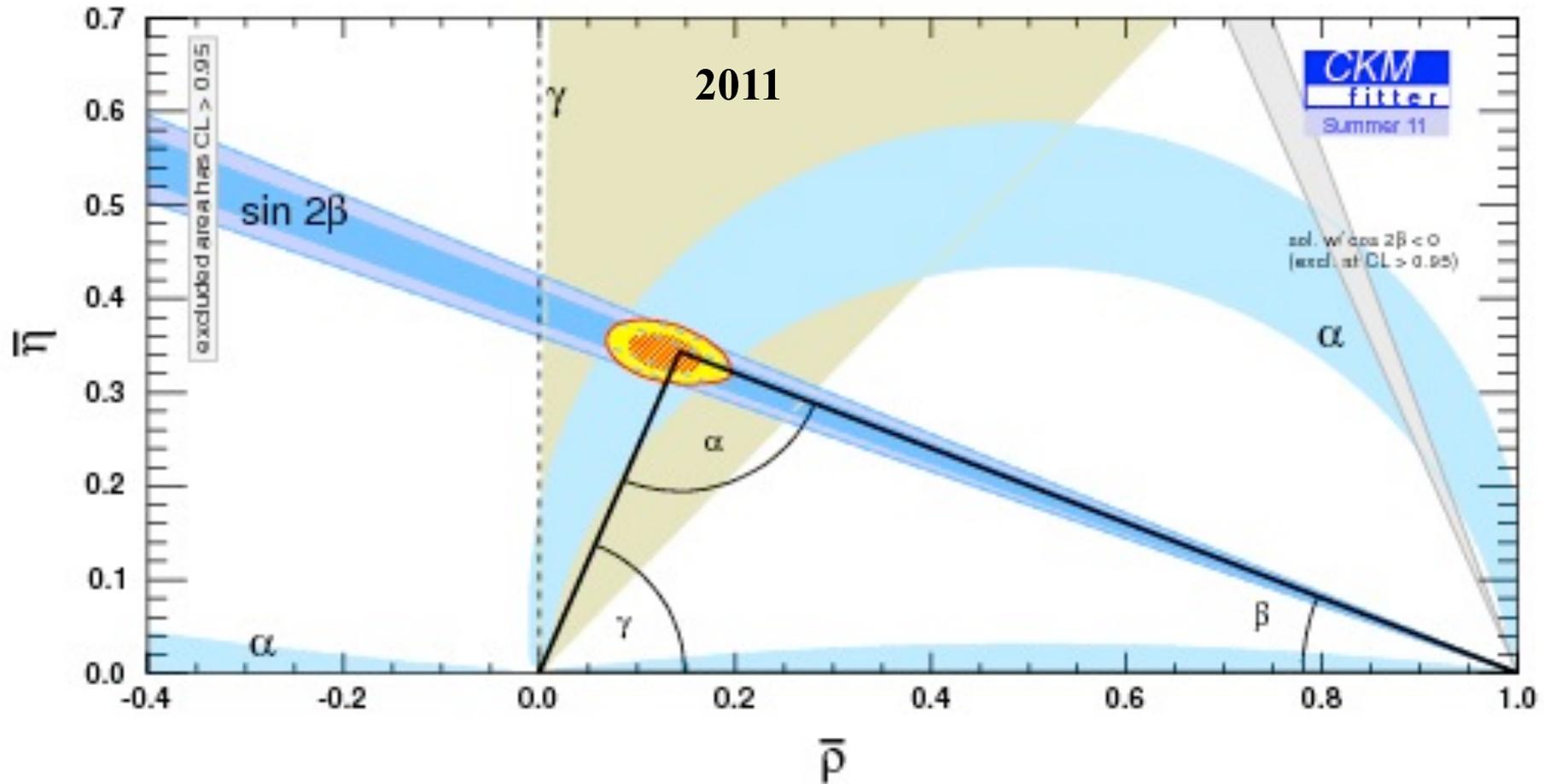
# Summary on angle $\gamma$



# Combined measurements of $\alpha$ , $\beta$ , $\gamma$



# Combined measurements of $\alpha$ , $\beta$ , $\gamma$



Strong activity in the measurement of angle  $\gamma$

# Magnitude of the CKM elements $V_{ub}$ and $V_{cb}$

# CKM matrix element $V_{ub}$ and $V_{cb}$ in semileptonic decays

- The magnitude of  $V_{(u/c)b}$  is measured in semileptonic decays
  - exclusive  $B \rightarrow \pi l \nu$  and  $B \rightarrow D^{(*)} l \nu$
  - inclusive  $b \rightarrow u l \nu$  and  $b \rightarrow c l \nu$
- For light leptons ( $e, \mu$ ), the decay rate for the process  $H \rightarrow P l \nu$  can be written as

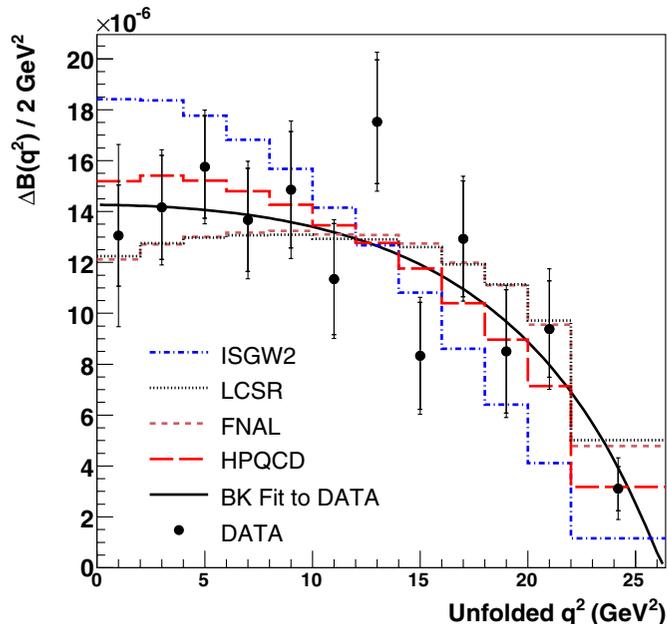
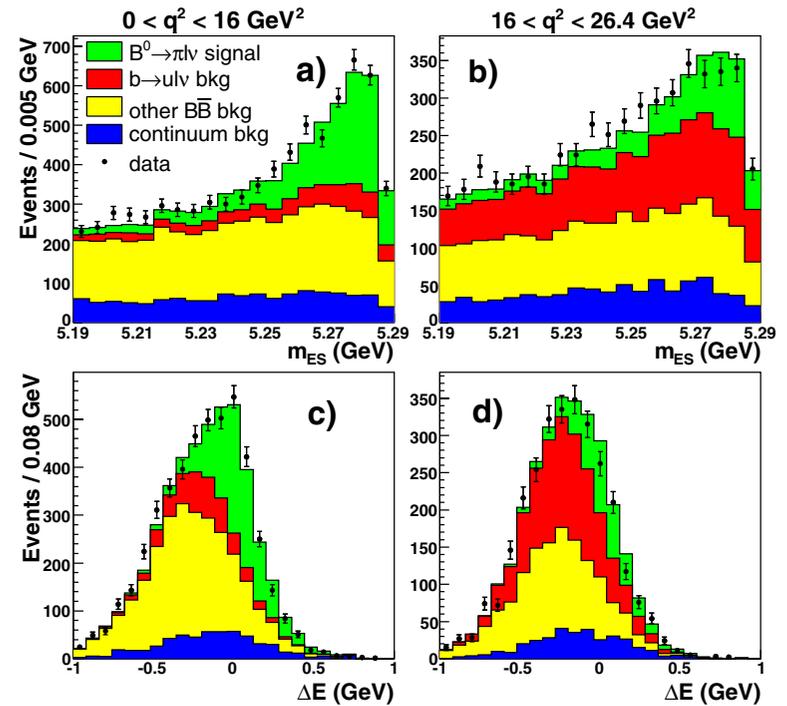
$$\frac{d\Gamma}{dq^2} = \frac{G_F^2 |V_{qQ}|^2}{192\pi^3 m_H^3} \left[ (m_H^2 + m_P^2 - q^2)^2 - 4m_H^2 m_P^2 \right]^{3/2} |f_+(q^2)|^2$$

CKM element form factor

- Clean determination of the CKM matrix element from
  1. measurement of  $d\Gamma/dq^2$
  2. theoretical calculation of the form factor  $f_+(q^2)$  [e.g. Lattice QCD]
  3. determine  $|V_{qQ}|$  from integration of the decay rate over the  $q^2$  range

# CKM element $V_{ub}$

- Measure  $B \rightarrow \pi \ell \nu$  branching fraction and  $q^2$  spectrum
- Extract signal from  $m_{ES} : \Delta E$  distributions
- $q^2$  spectrum for signal
- Results:



$$\mathcal{B}(B^0 \rightarrow \pi^- \ell^+ \nu) = (1.46 \pm 0.07_{\text{stat}} \pm 0.08_{\text{syst}}) \times 10^{-4}$$

$$|V_{ub}| = (4.1 \pm 0.2_{\text{stat}} \pm 0.2_{\text{syst}}^{+0.6}_{-0.4\text{FF}}) \times 10^{-3}$$

BABAR, PRL 98 (2007) 091801

# CKM element $V_{ub}$ (Belle and BABAR)

- Many measurement of  $B \rightarrow \pi \ell \nu$  branching fractions

	$\mathcal{L}$ (fb $^{-1}$ )	$\mathcal{B} \times 10^4$	$\Delta\mathcal{B}(q^2 < 16) \times 10^4$	$\Delta\mathcal{B}(q^2 > 16) \times 10^4$
BaBar no tag ( $\pi^-$ ) [466]	206	$1.45 \pm 0.07 \pm 0.11$	$1.08 \pm 0.06 \pm 0.09$	$0.38 \pm 0.04 \pm 0.05$
CLEO no tag ( $\pi^-, \pi^0$ ) [464]	16	$1.38 \pm 0.15 \pm 0.11$	$0.97 \pm 0.13 \pm 0.09$	$0.41 \pm 0.08 \pm 0.04$
BaBar sl. tag ( $\pi^-$ ) [467]	348	$1.39 \pm 0.21 \pm 0.08$	$0.92 \pm 0.16 \pm 0.05$	$0.46 \pm 0.13 \pm 0.03$
Belle sl. tag ( $\pi^-$ ) [471]	253	$1.38 \pm 0.19 \pm 0.15$	$1.02 \pm 0.16 \pm 0.11$	$0.36 \pm 0.10 \pm 0.04$
BaBar sl. tag ( $\pi^0$ ) [467]	348	$1.80 \pm 0.28 \pm 0.15$	$1.38 \pm 0.23 \pm 0.11$	$0.45 \pm 0.17 \pm 0.06$
Belle sl. tag ( $\pi^0$ ) [471]	253	$1.43 \pm 0.26 \pm 0.15$	$1.05 \pm 0.23 \pm 0.12$	$0.37 \pm 0.15 \pm 0.04$
BaBar had. tag ( $\pi^-$ ) [468]	211	$1.07 \pm 0.27 \pm 0.19$	$0.42 \pm 0.18 \pm 0.06$	$0.65 \pm 0.20 \pm 0.13$
Belle had. tag ( $\pi^-$ ) [472]	605	$1.12 \pm 0.18 \pm 0.05$	$0.85 \pm 0.16 \pm 0.04$	$0.26 \pm 0.08 \pm 0.01$
BaBar had. tag ( $\pi^0$ ) [468]	211	$1.54 \pm 0.41 \pm 0.30$	$1.05 \pm 0.36 \pm 0.19$	$0.49 \pm 0.23 \pm 0.12$
Belle had. tag ( $\pi^0$ ) [472]	605	$1.24 \pm 0.23 \pm 0.05$	$0.85 \pm 0.16 \pm 0.04$	$0.41 \pm 0.11 \pm 0.02$
Average		$1.36 \pm 0.05 \pm 0.05$	$0.94 \pm 0.05 \pm 0.04$	$0.37 \pm 0.03 \pm 0.02$

- ...and with other light resonances

Decay mode	$\mathcal{B} \times 10^4$	$\sigma_{\text{stat}} \times 10^4$	$\sigma_{\text{syst}} \times 10^4$
$B^+ \rightarrow \eta \ell^+ \nu$ (BaBar average) [469]	0.37	0.06	0.07
$B^+ \rightarrow \eta' \ell^+ \nu$ (CLEO no tag) [464] <sup>a</sup>	2.66	0.80	0.56
$B^0 \rightarrow \rho^- \ell^+ \nu$ (average)	2.80	0.18	0.16
$B^+ \rightarrow \omega \ell^+ \nu$ (BaBar no tag) [469]	1.14	0.16	0.08

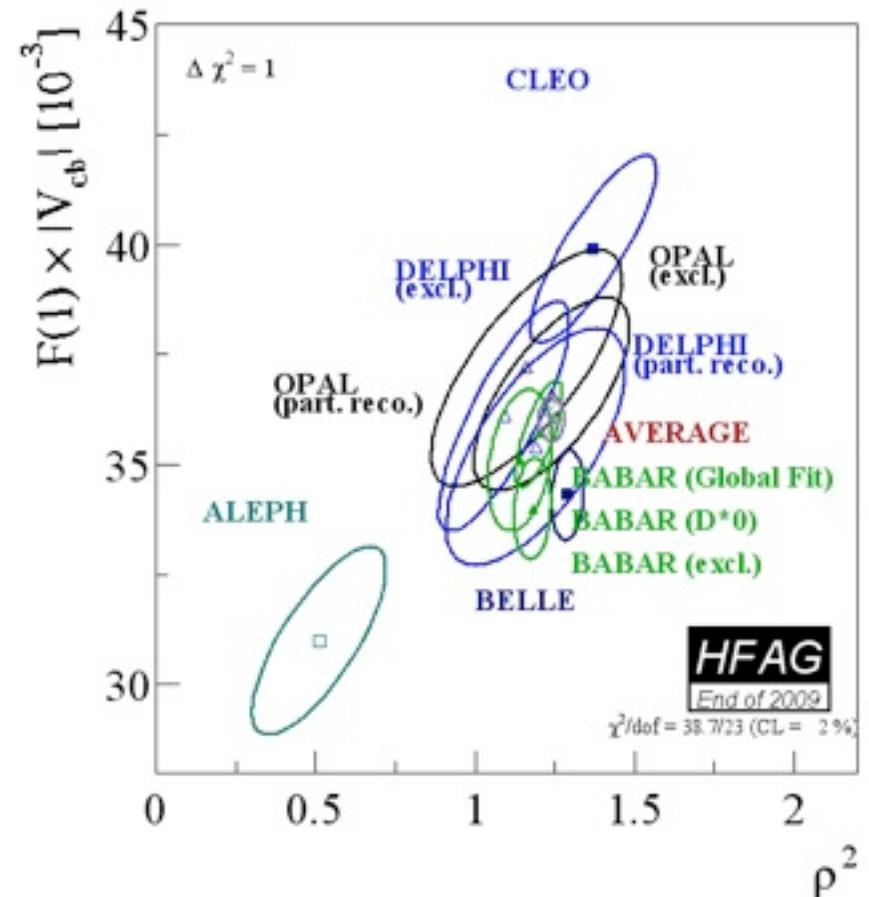
- $|V_{ub}|$  from exclusive decays yields:

$$|V_{ub}| = (3.38 \pm 0.36) \times 10^{-3}$$

# CKM element $V_{cb}$ from exclusive decays

- Measure  $B \rightarrow D^{(*)} l \nu$  branching fraction and  $q^2$  spectrum (similar to  $B \rightarrow \pi l \nu$ )
- Several measurements from
  - B factories
  - LEP
- Most accurate results from Belle and BABAR
- Average:

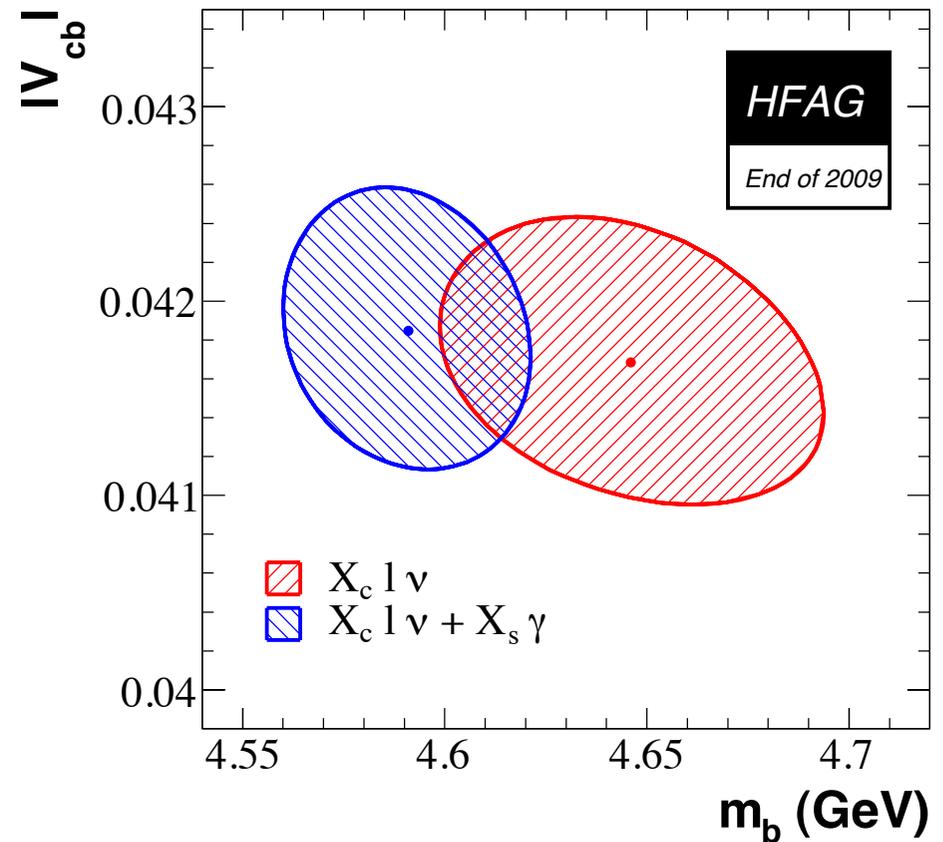
$$|V_{cb}| = (36.0 \pm 0.5) \times 10^{-3}$$



# CKM element $V_{cb}$ from inclusive decays

- In inclusive measurements of  $b \rightarrow cl\nu$ , determine
  - branching fraction
  - lepton energy spectrum
- Global fit for  $V_{cb}$  and  $m_b$
- Average:

$$|V_{cb}| = (41.7 \pm 0.7) \times 10^{-3}$$



# $V_{ub}$ from leptonic $B^\pm \rightarrow \tau^\pm \nu_\tau$ decays

- The  $B^\pm \rightarrow \tau^\pm \nu_\tau$  decay already occurs at the tree level
    - in SM
    - in new physics with extended Higgs sector
- => sensitivity to new physics

- From SM and Unitarity Triangle properties, expect

$$\mathcal{B}(B \rightarrow \tau \nu)_{\text{SM}} = (0.87 \pm 0.19) \times 10^{-4}$$

- In minimal flavor violation (MFV) supersymmetry models, define ratio of branching ratios (effective coupling  $\epsilon_0 \approx 10^{-2}$ )

$$R_{P\ell\nu} = \frac{\mathcal{B}^{\text{SM}}(P \rightarrow \ell \nu)}{\mathcal{B}^{\text{SUSY}}(P \rightarrow \ell \nu)} = \left[ 1 - \left( \frac{m_P^2}{m_{H^\pm}^2} \right) \frac{\tan^2 \beta}{1 + \epsilon_0 \tan \beta} \right]^2$$

- MSSM => O(10%) suppression relative to SM  $BF(B \rightarrow \tau \nu)$

# $B^\pm \rightarrow \tau^\pm \nu_\tau$ measurements

- At least 3 neutrinos in the final state ( $B \rightarrow \tau \nu_\tau$ , followed by (e.g.)  $\tau \rightarrow \mu \nu_\mu \nu_\tau$ )  
=> use the recoil technique
  - reconstructed  $B$  (tagging  $B$ ) as
    - semileptonic => high statistics, but non-negligible background
    - hadronic => cleaner, but lower statistics
  - on signal side:
    - reconstruct all visible particles
    - reject events with larger energy deposited in the calorimeter
- Belle and BABAR have observed the decay  $B^\pm \rightarrow \tau^\pm \nu_\tau$  :
  - Belle:  $\text{BF}(B^\pm \rightarrow \tau^\pm \nu) = (1.54 \pm 0.38 \pm 0.30) \times 10^{-4}$
  - BABAR:  $\text{BF}(B^\pm \rightarrow \tau^\pm \nu) = (1.76 \pm 0.49) \times 10^{-4}$
  - Average (HFAG):  $\text{BF}(B^\pm \rightarrow \tau^\pm \nu) = (1.64 \pm 0.34) \times 10^{-4}$

# $B^\pm \rightarrow \tau^\pm \nu_\tau$ : comparison to SM

- Average  $B^\pm \rightarrow \tau^\pm \nu_\tau$  branching fraction:

$$\mathcal{B}(B \rightarrow \tau \nu)_{\text{exp}} = (1.64 \pm 0.34) \times 10^{-4}$$

- SM prediction:

$$\mathcal{B}(B \rightarrow \tau \nu)_{\text{SM}} = (0.87 \pm 0.19) \times 10^{-4}$$

- Difference =  $(0.77 \pm 0.39) \times 10^{-4} \Rightarrow 2.0\sigma$  discrepancy

- Remarks:

- SM systematic uncertainty from lattice calculation is missing
- experimental uncertainty is statistics dominated

$\Rightarrow$  new more data at next-generation B factory(ies)!

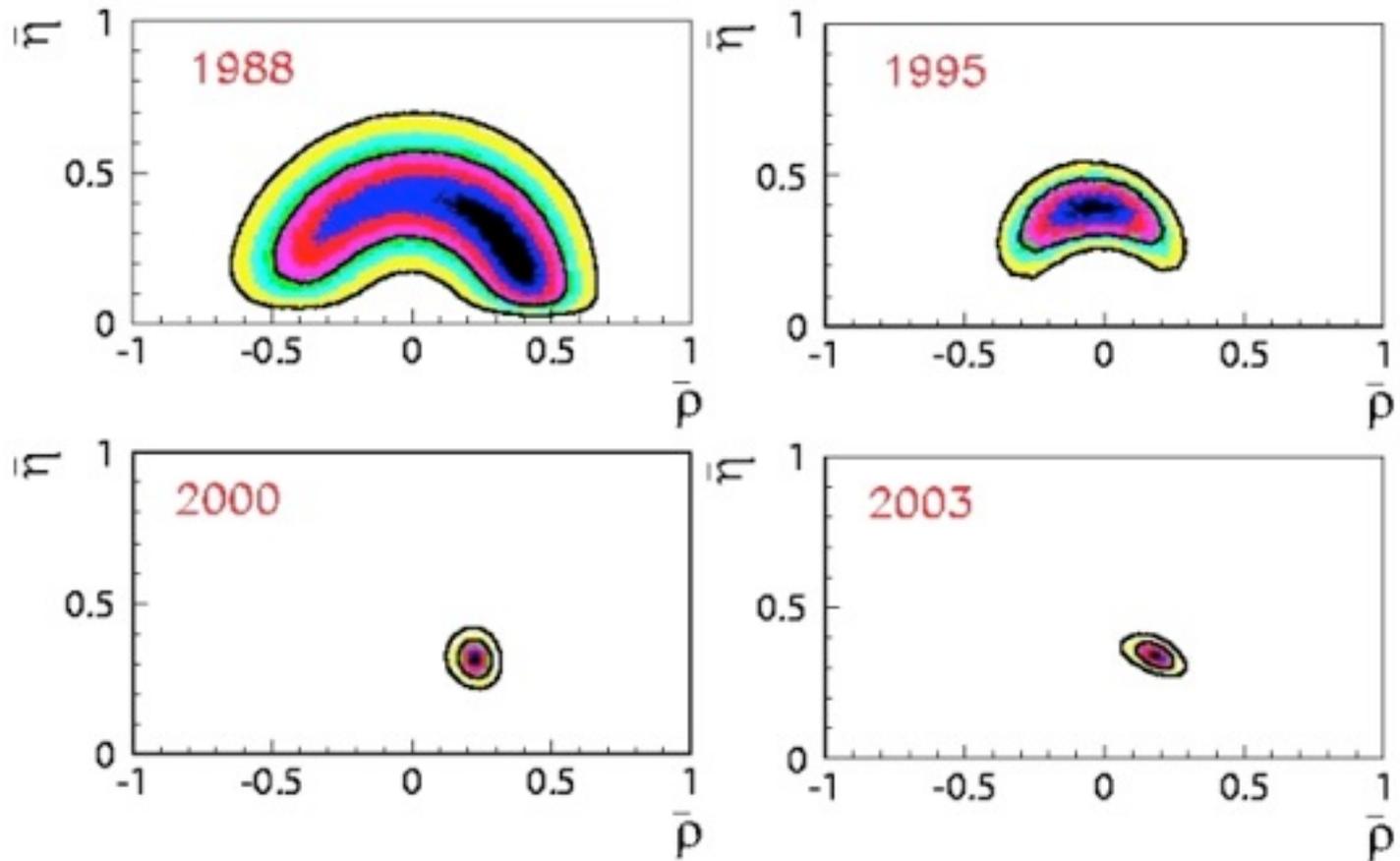
# Global fits

# Global fit strategy

- CKM matrix elements can be determined from global fit using all available measurements:
  - 4 parameters
  - 100's of measurements

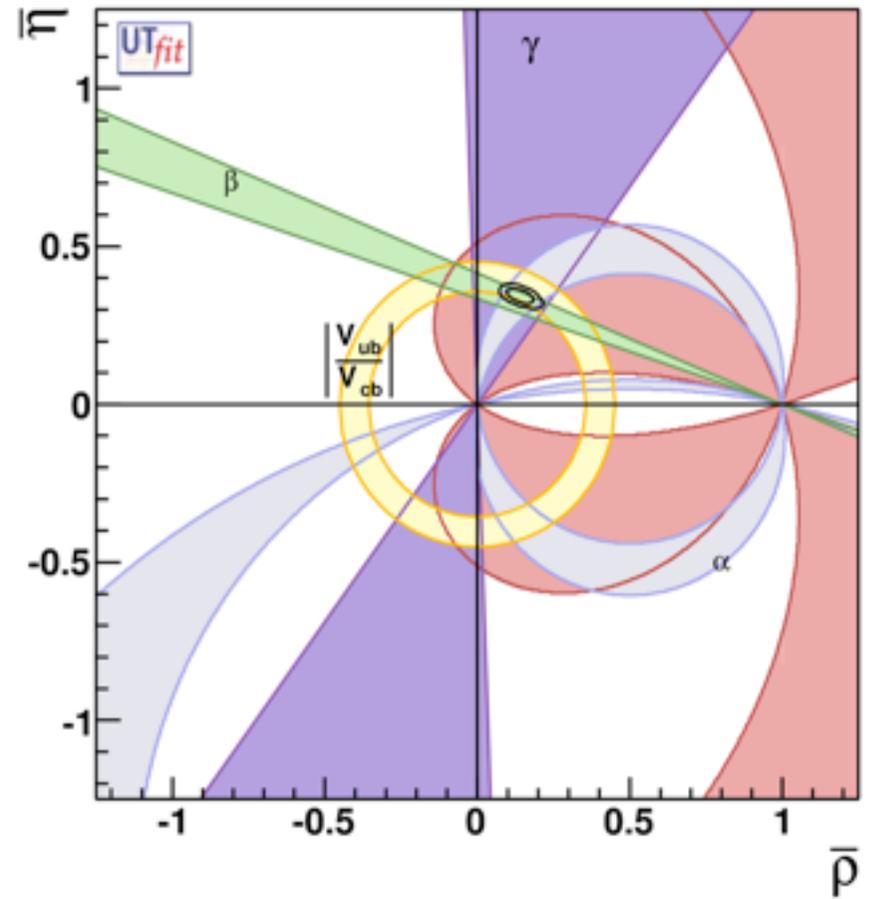
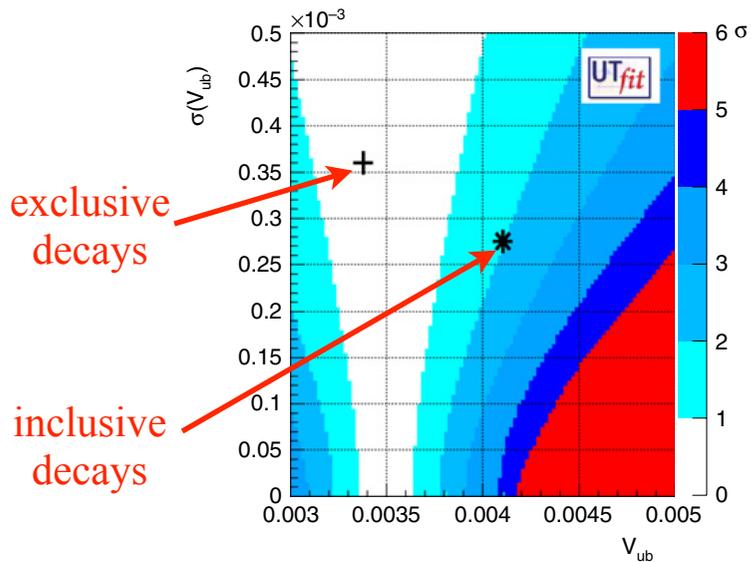
⇒ strong constraints on parameters
- Any discrepancy not explainable within the standard model would be a sign of new physics!
- Two main strategies:
  - frequentist
    - applied by the CKMFitter group [ <http://ckmfitter.in2p3.fr> ]
  - bayesian
    - applied by the UTFit group [ <http://www.utfit.org/UTFit> ]

# UTFit: evolution over time



# UTfit: results 2010

- Overall very good agreement between measurements
  - small discrepancy between  $|V_{ub}|$  measurements from inclusive and exclusive modes

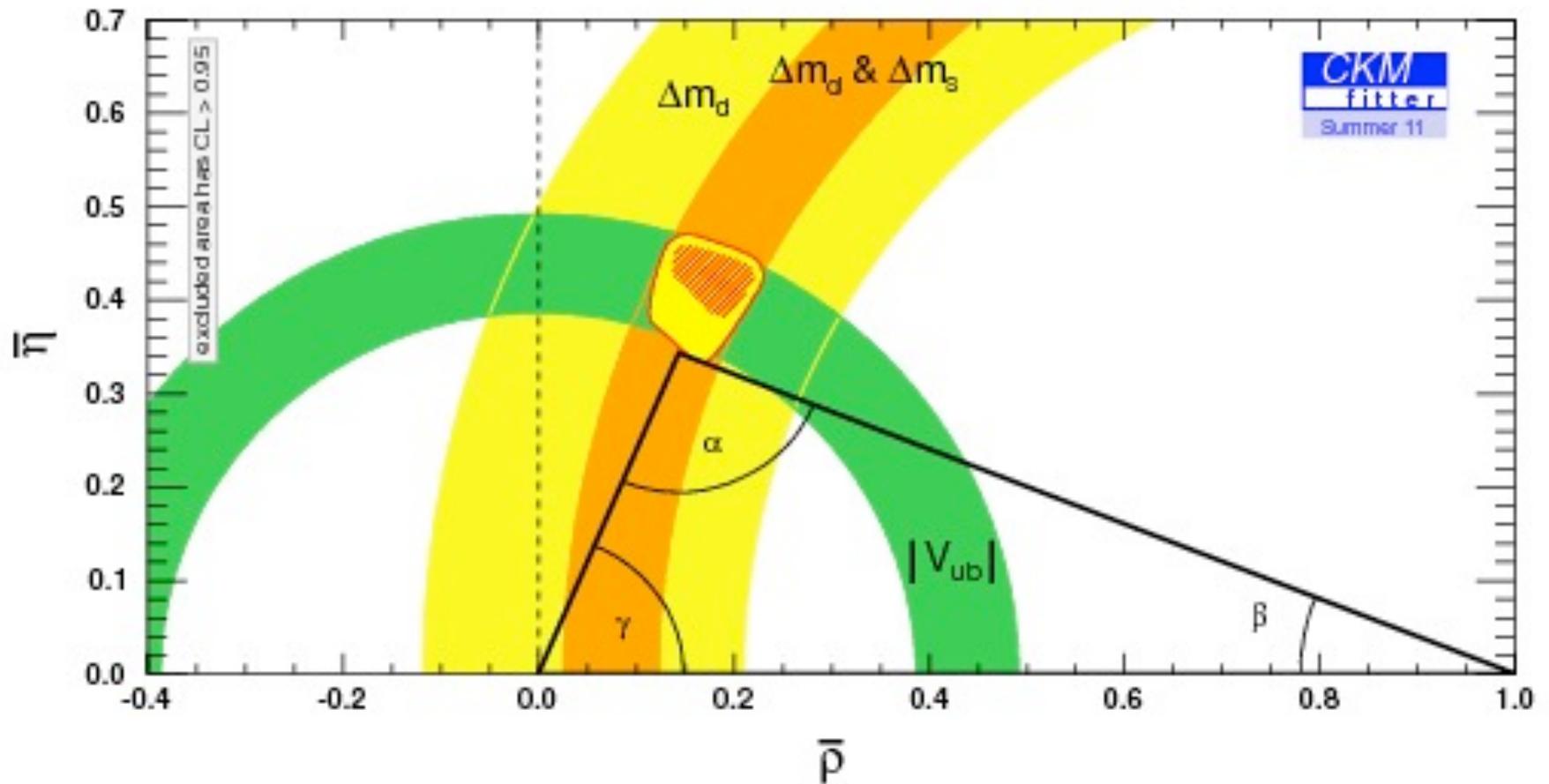


$$V_{CKM} = \begin{pmatrix} 0.97425 \pm 0.00015 & 0.22545 \pm 0.00065 & 0.00352 \pm 0.00011 e^{i(-67.7 \pm 4.4)} \\ -0.2253 \pm 0.00065 e^{i(-0.033 \pm 0.0016)} & 0.97342 \pm 0.00015 & 0.04099 \pm 0.00046 \\ 0.00854 \pm 0.00031 e^{i(-21.86 \pm 0.73)} & -0.04024 \pm 0.00045 e^{i(-1.04 \pm 0.048)} & 0.999154 \pm 1.8 \times 10^{-05} \end{pmatrix}$$



# CKMFitter: CP conserved quantities

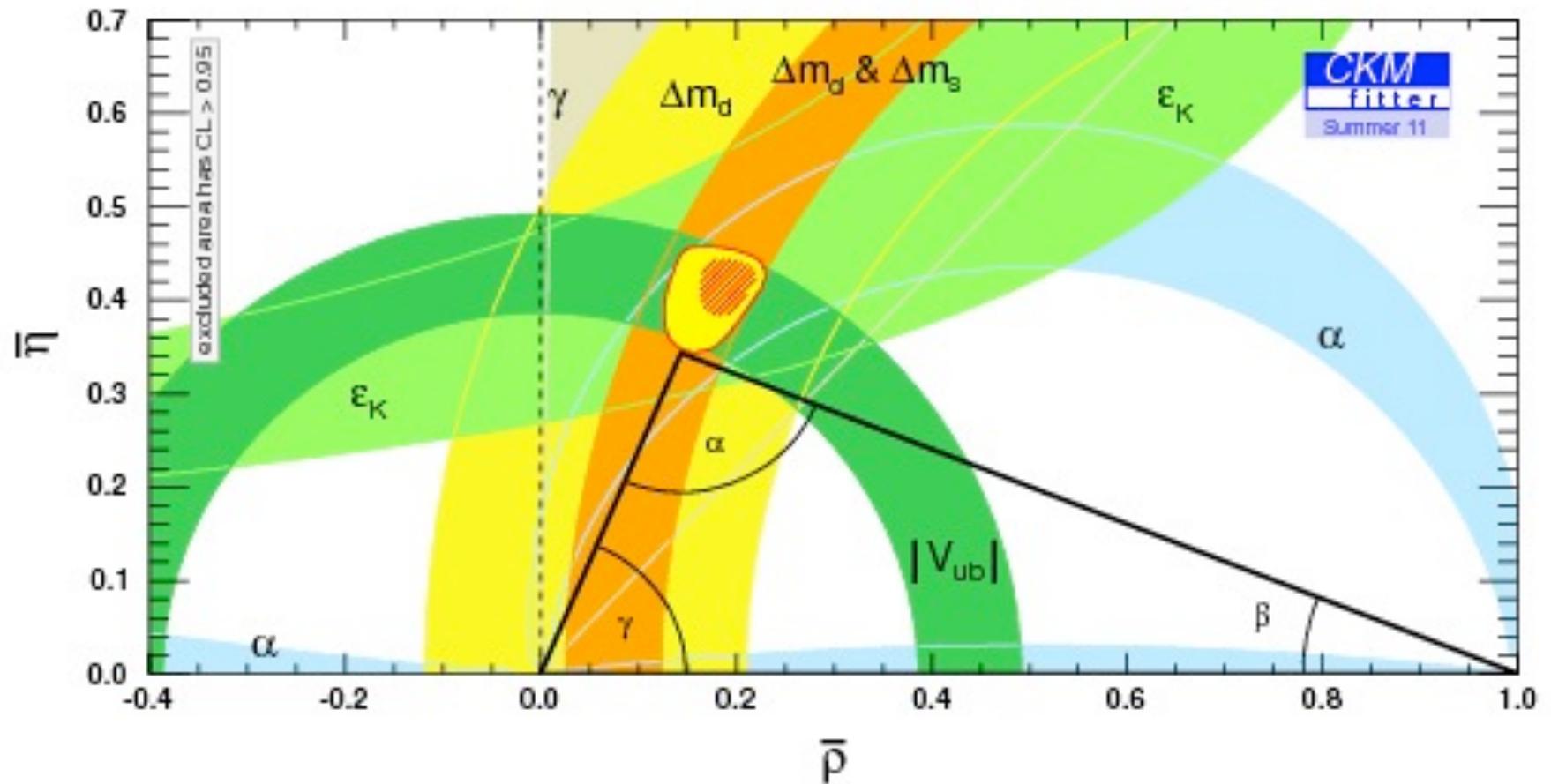
$|V_{ub}|$  (with  $B \rightarrow \tau\nu$ ),  $\Delta m$





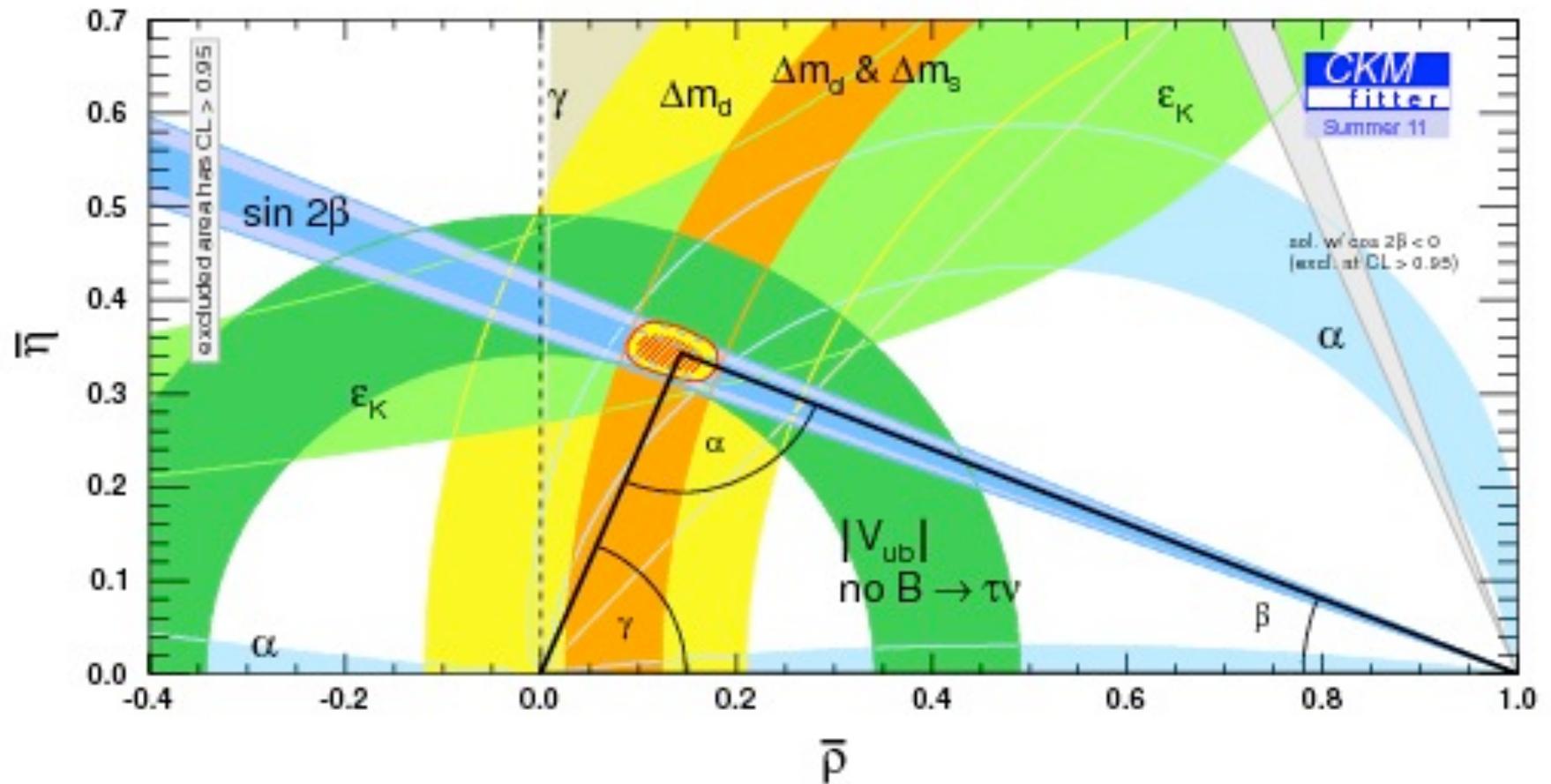
# CKMFitter: global fit result

without  $\sin 2\beta$ , with  $B \rightarrow \tau \nu$



# CKMFitter: global fit result

with  $\sin 2\beta$ , without  $B \rightarrow \tau\nu$



# Comparison UFit / CKMFitter

- Compare results from UFit and CKMFitter groups

	UFit	CKMFitter
$\bar{\rho}$	$0.158 \pm 0.021$	$0.139^{+0.025}_{-0.027}$
$\bar{\eta}$	$0.343 \pm 0.013$	$0.341^{+0.016}_{-0.015}$
$A$	$0.802 \pm 0.015$	$0.812^{+0.010}_{-0.024}$
$\lambda$	$0.2259 \pm 0.0016$	$0.2252 \pm 0.0008$
$\alpha$ ( $^\circ$ )	$92.6 \pm 3.2$	$90.6^{+3.8}_{-4.2}$
$\sin 2\beta$	$0.698 \pm 0.019$	$0.684^{+0.023}_{-0.021}$
$\gamma$ ( $^\circ$ )	$65.4 \pm 3.1$	$67.8^{+4.2}_{-3.9}$
$ V_{ub} $	$0.00359 \pm 0.0012$	$0.00350^{+0.00015}_{-0.00014}$
$ V_{cb} $	$0.0409 \pm 0.0005$	$0.04117^{+0.00038}_{-0.00115}$
$ V_{td} $	$0.00842 \pm 0.00021$	$0.00859^{+0.00027}_{-0.00029}$

- The fitted values are all compatible within their uncertainties
- Both fitters agree on the tension between  $\sin 2\beta$  and  $B \rightarrow \tau \nu$

# Summary

