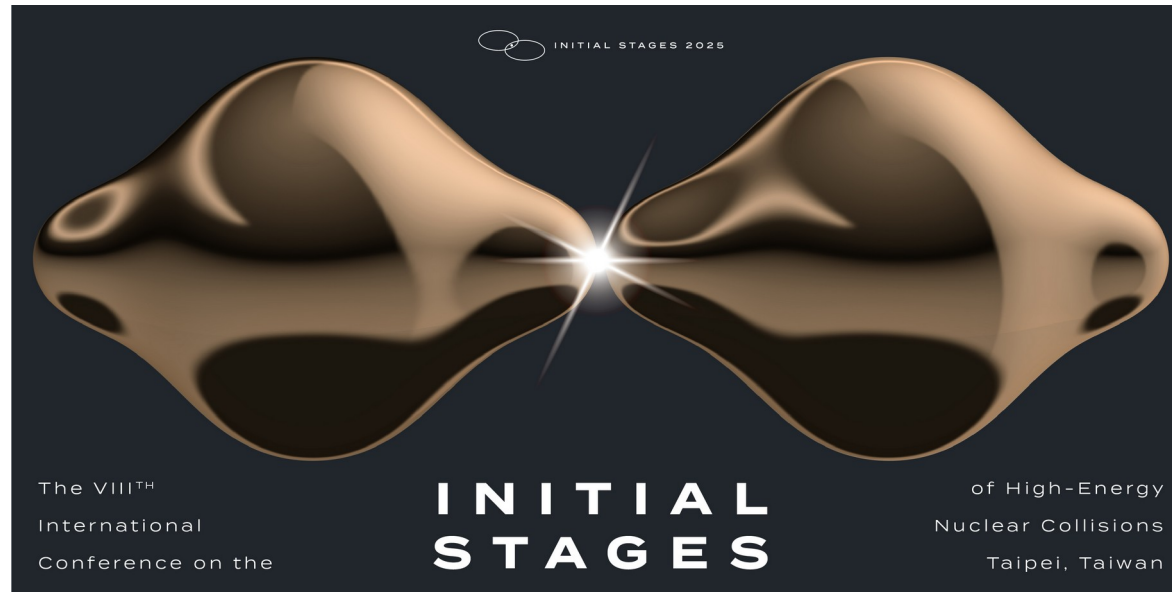


# Emergent many-body dynamics at its limits: from ultracold atoms to high-energy collisions

Giuliano Giacalone



September 12, 2025



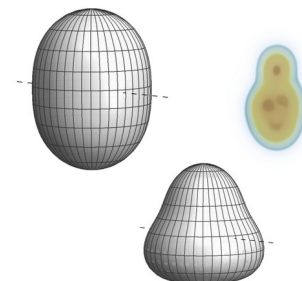
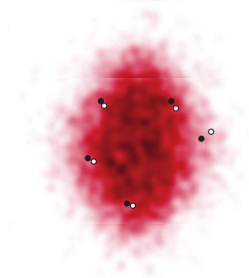
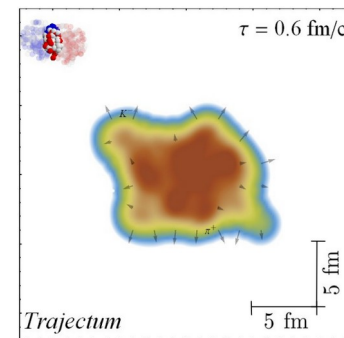
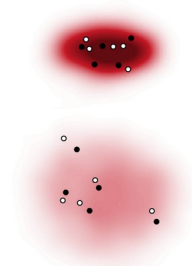
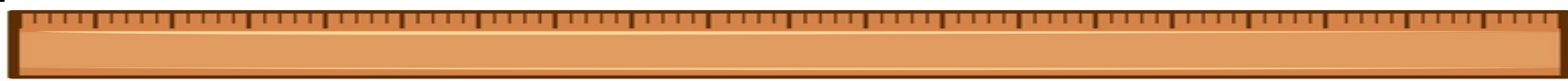
# The physical world as an emergent phenomenon



$10^{15}$  m



$10^{-15}$  m





## More is different ... 50 years later

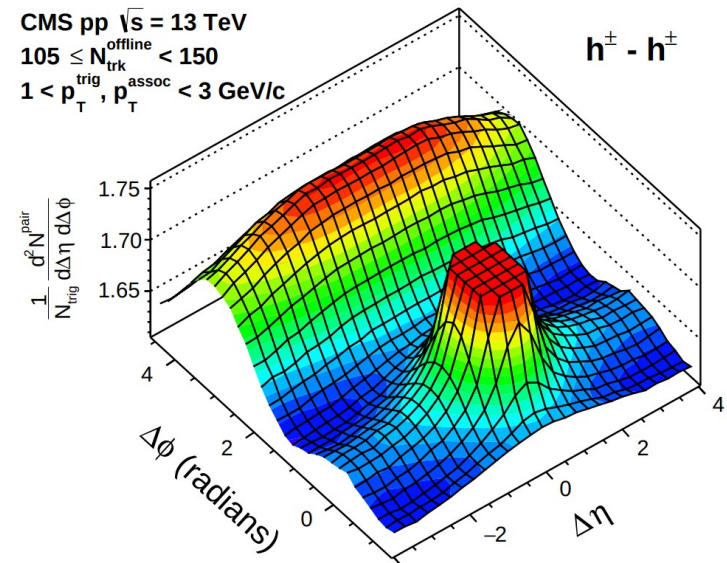
[P. W. Anderson, Science 177 (1972) 4047, 393-396]

**Main point : We are able to dissect that statement and elucidate its meaning**

What is the precise meaning of “more” ?

How does “few” become “more” ?

Why are p-p collisions “different” ?



arXiv:2509.05049

<https://indico.gsi.de/event/19234/>

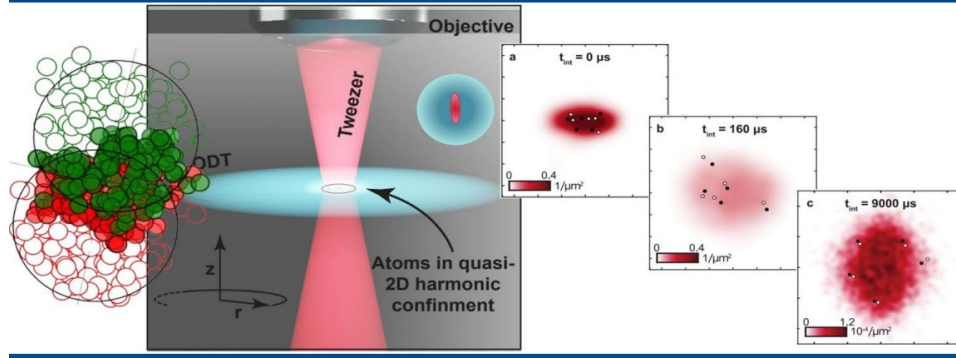
## ExtreMe Matter Institute EMMI

EMMI Rapid Reaction Task Force

### Deciphering Many-Body Dynamics in Mesoscopic Quantum Gases

March 18-21, 2024

Heidelberg University, Germany



## Heavy Ions

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Jasmine Brewer  
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Giuliano Giacalone  
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Alice Ohlson

Aleksas Mazeliauskas  
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## Cold atoms

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Meera Parish  
Nir Navon  
Stephanie Reimann  
Francesco Scazza  
Joseph Thywissen  
Yangqian Yan  
Matteo Zaccanti  
Torsten Zache

*“... emerging area of research, which we believe holds the promise of establishing a new frontier within the discipline of physics as a whole”*

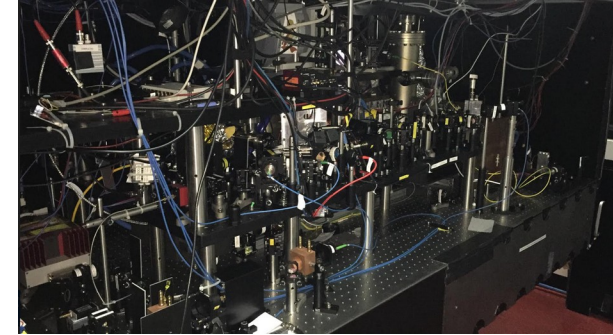
... why these two fields ?

particle number

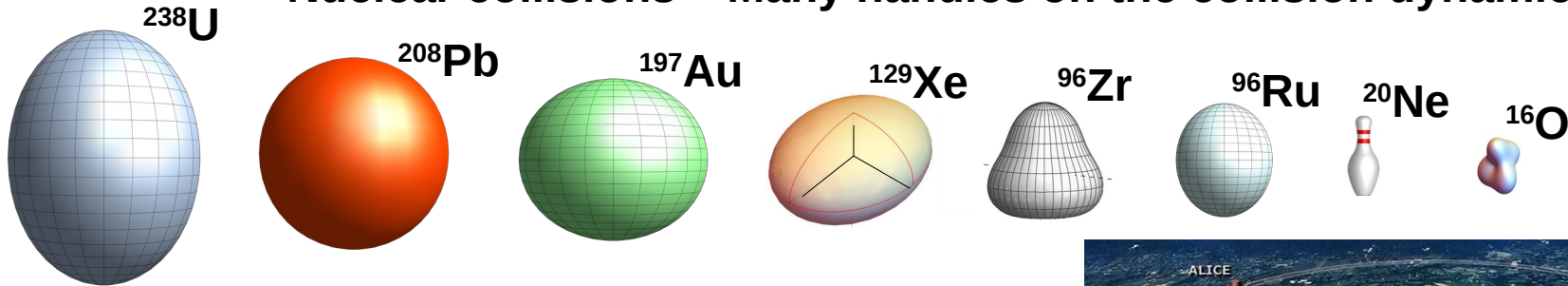
Ultracold atoms – Highly controllable quantum systems

$$\mathcal{H} = - \sum_{i=1}^N \frac{\hbar^2}{2m} \nabla_i^2 + \sum_{i<j} \frac{\hbar^2}{2m} g_0 \delta^{(d)}(\mathbf{r}_i - \mathbf{r}_j) + \sum_{i=1}^N \mathcal{V}_{\text{ext}}(\mathbf{r}_i)$$

interaction strength      geometry



Nuclear collisions – Many handles on the collision dynamics

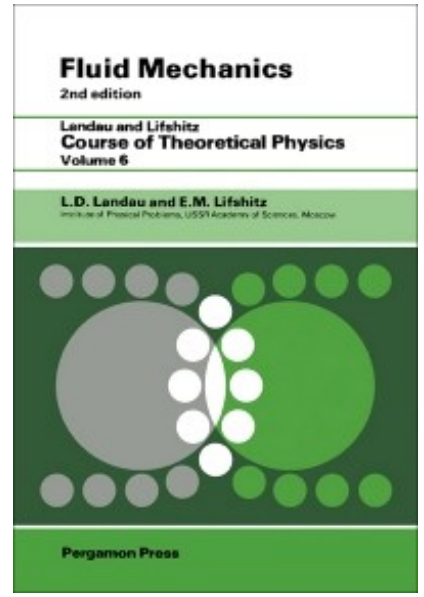
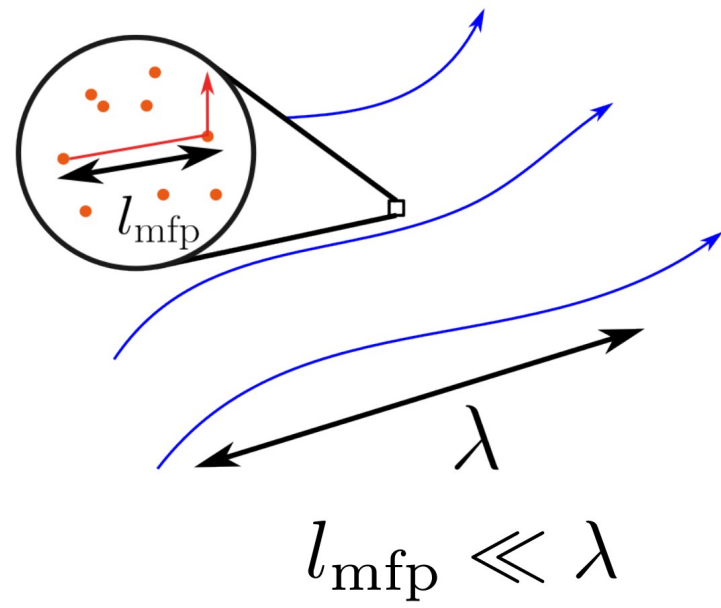


multiplicity, rapidity, collision energy ...



# Example for heavy ions : Collisional hydrodynamics ( $T > 0$ )

Large N, separation of scales, equilibrium, ...



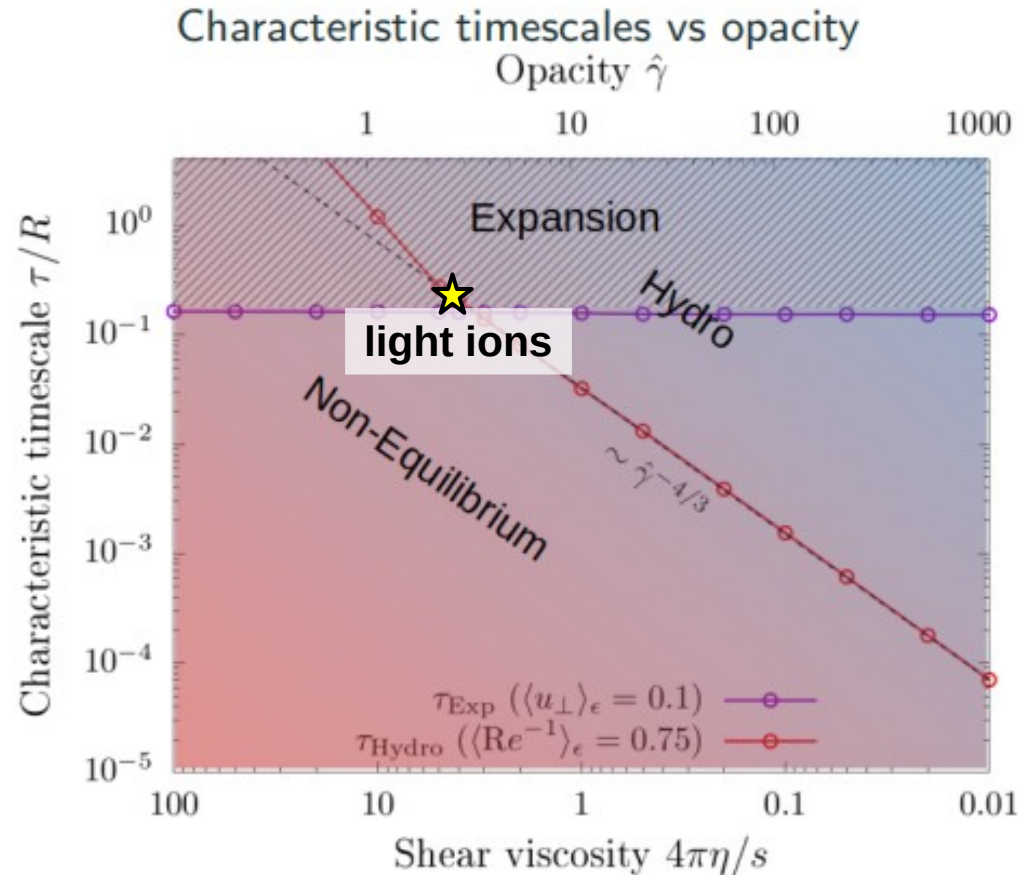
$$\rho \left( \partial_t + \vec{u} \cdot \vec{\nabla} \right) \vec{u} = -\vec{\nabla} p + \eta \nabla^2 \vec{u}$$

density
pressure
shear

$$\text{Kn} \equiv \frac{\eta}{\rho v R} \ll 1$$

# Breaking textbook criteria – Since 2018

[Kurkela, Wiedemann, Wu, EPJC 79 (2019) 11, 965]



**Boltzmann eq. in relaxation time approximation (RTA)**

$$\hat{\gamma} = \frac{1}{5\eta/s} \left( \frac{R}{\pi a} \frac{dE_{\perp}^0}{d\eta} \right)^{1/4}$$

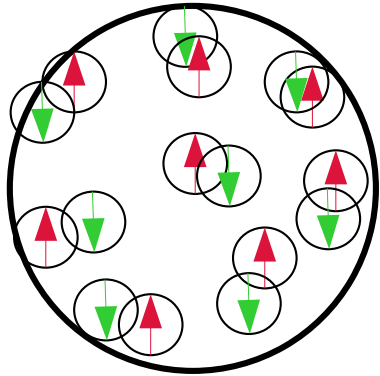
**Detailed numerical solutions to assess hydro applicability**

[Ambrus, Schlichting, Werthmann, PRL 130 (2023) 15, 152301]

Talk by Clemens Werthmann

Talk by Aleks Kurkela

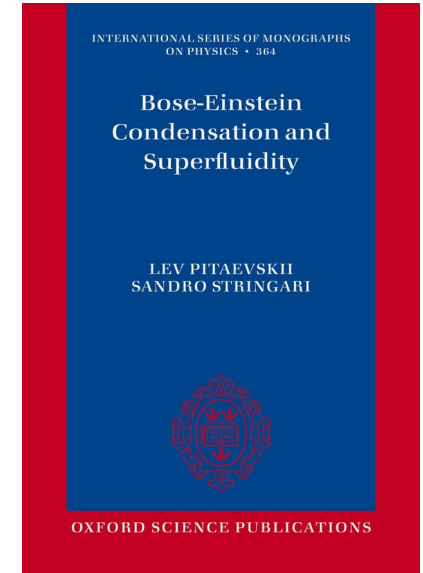
# Example for cold atoms : Superfluid hydrodynamics (T~0)



large system of bosons  $N \gg 1$

separation of scales  $na_s^3 \ll 1$

molecule size  $\ll$  inter-molecule distance



Gross-Pitaevskii equation

$$\hat{\Psi}(r,t) = \Psi(r,t) + \cancel{\delta\hat{\Psi}(r,t)}$$

$$i\hbar \frac{\partial \Psi}{\partial t} = \left( -\frac{\hbar^2}{2m} \nabla^2 + V_{\text{ext}}(\mathbf{r}) + g|\Psi|^2 \right) \Psi$$

$$\Psi = \sqrt{n} e^{iS(r,t)}$$

$$v_S = \frac{\hbar}{m} \nabla S$$



ideal (superfluid) hydrodynamics

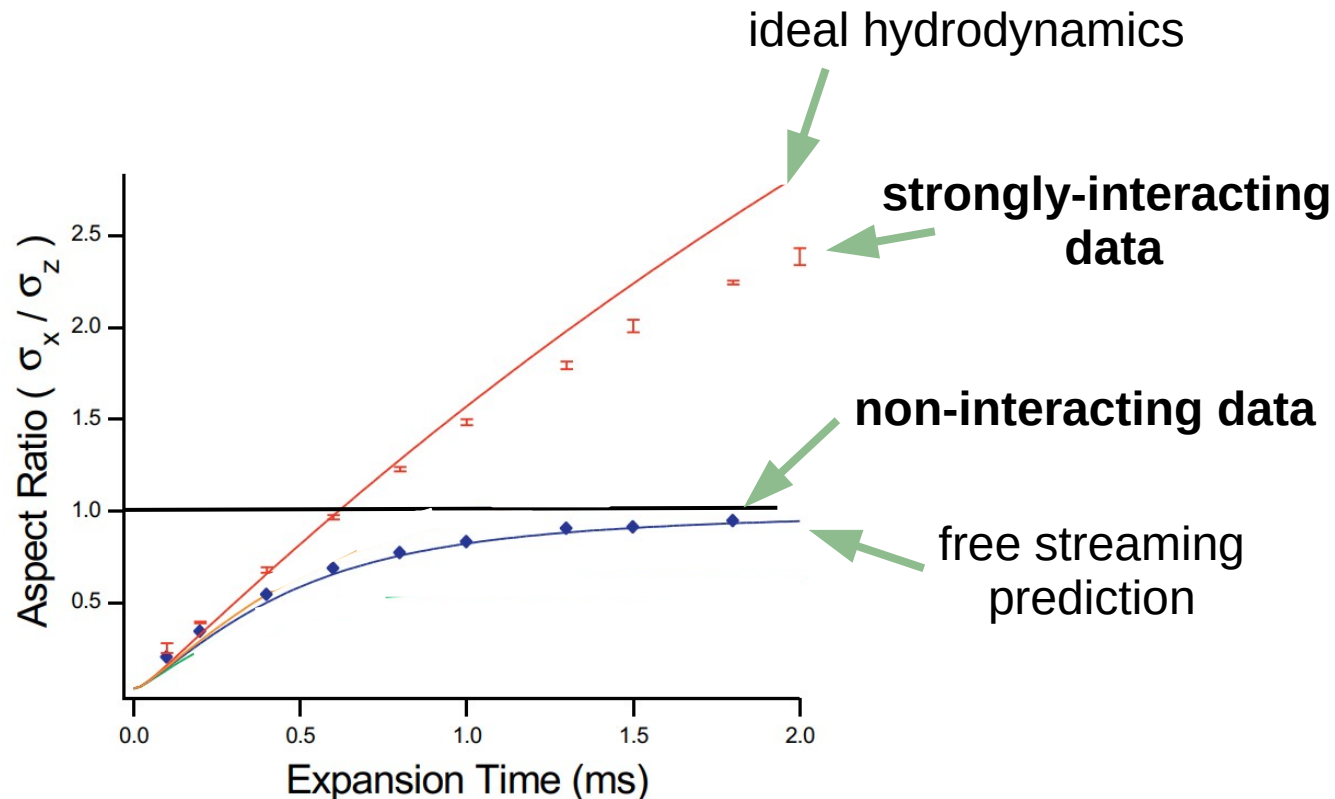
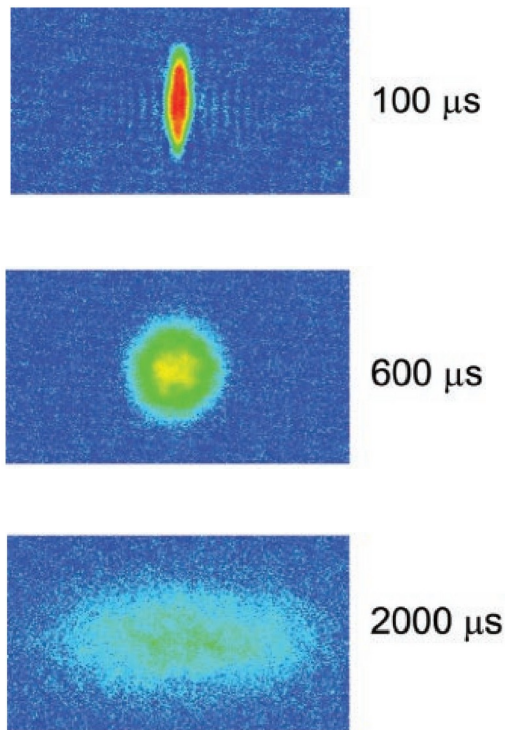
$$\begin{aligned} \frac{\partial}{\partial t} n + \nabla(v_S n) &= 0 \\ m \frac{\partial}{\partial t} v_S + \nabla \left( \frac{1}{2} m v_S^2 + \mu(n) + V_{\text{ext}} \right) &= 0 \end{aligned}$$

## Bits of history ...

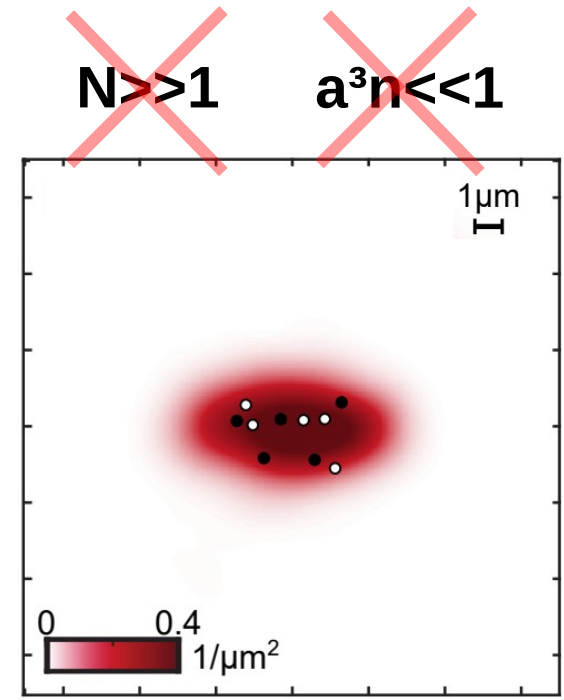
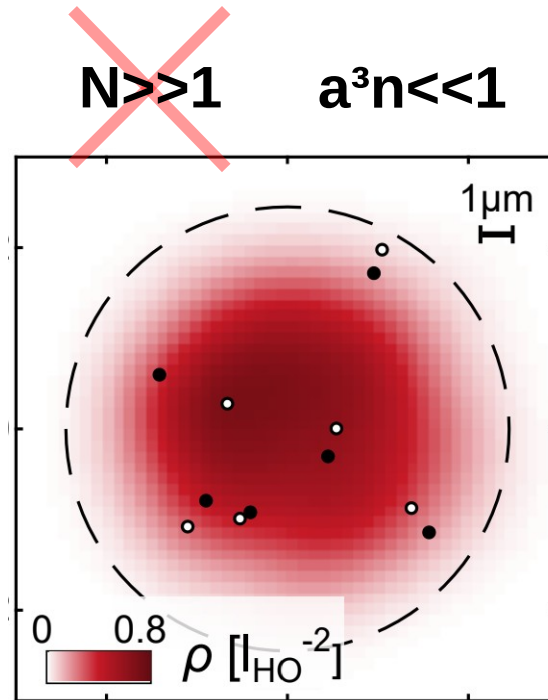
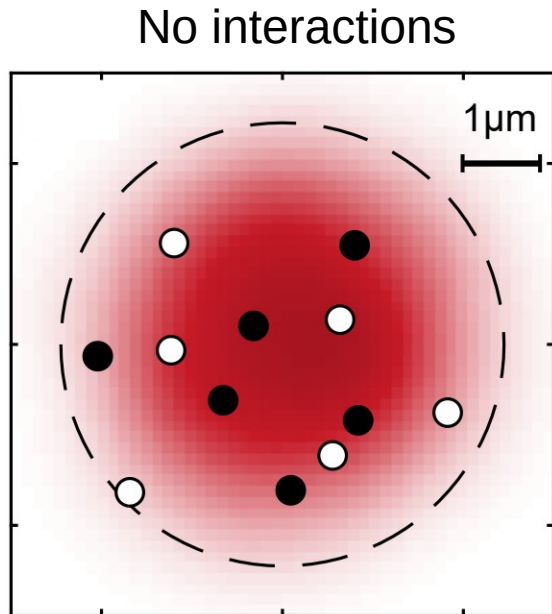
# Control of geometry and interactions – Elliptic flow to probe superfluid hydrodynamics

[O'Hara et al., Science **298** (2002) 2179-2182]

[Menotti, Pedri, Stringari, PRL **89**, 250402 (2002)]



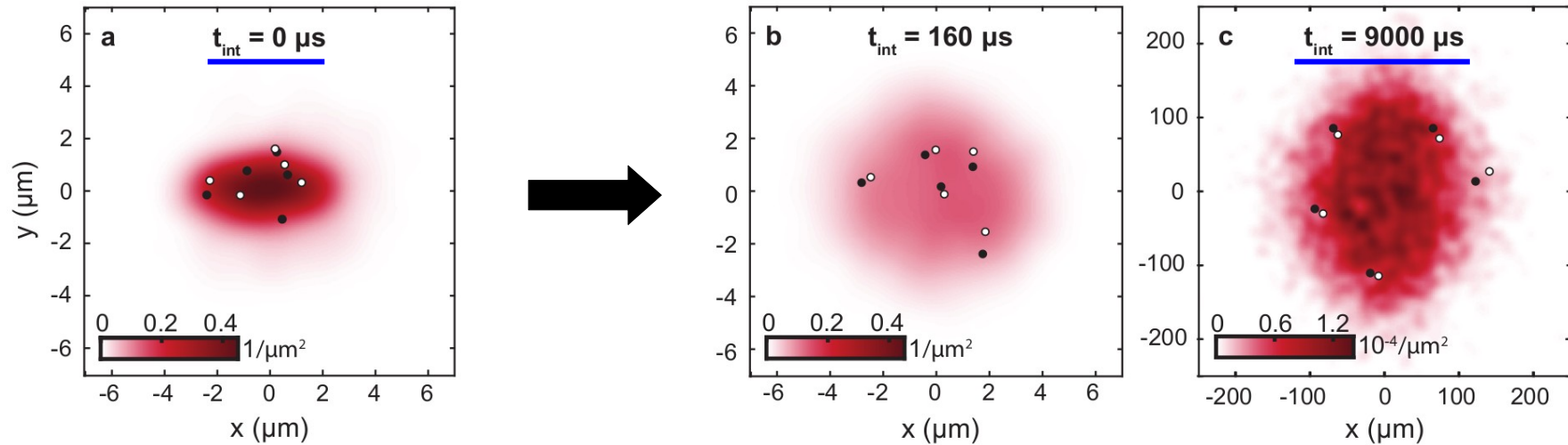
## Breaking textbook criteria – One by one



???

# Criteria for applicability of many-body description fail

## Yet ... Observed inversion of the initial anisotropy



nature physics

Article

<https://doi.org/10.1038/s41567-024-02705-8>

## Emergent interaction-driven elliptic flow of few fermionic atoms

... fluid of 10 atoms !?

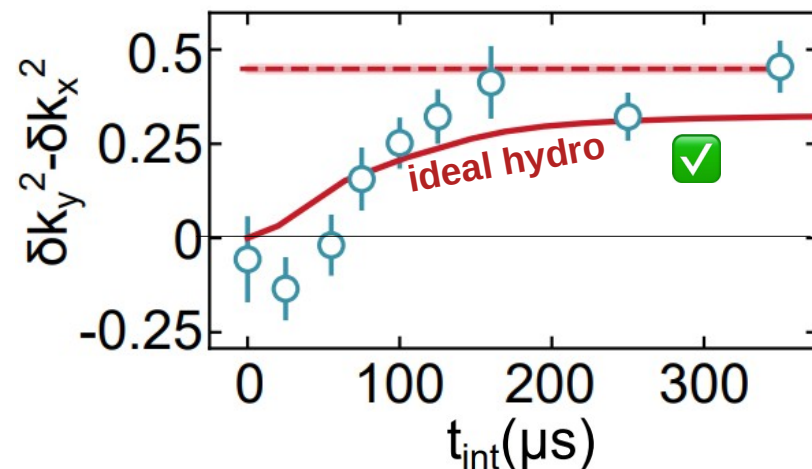
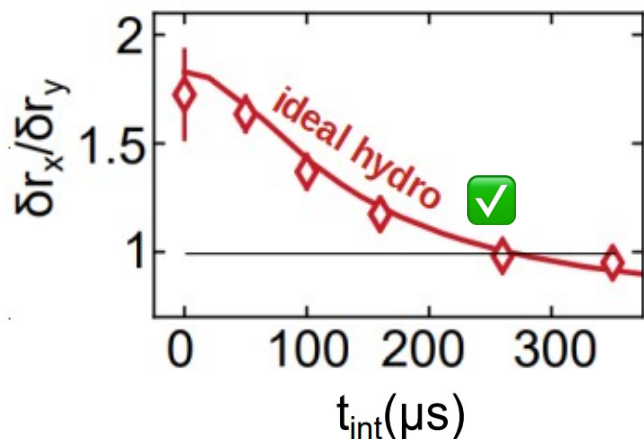
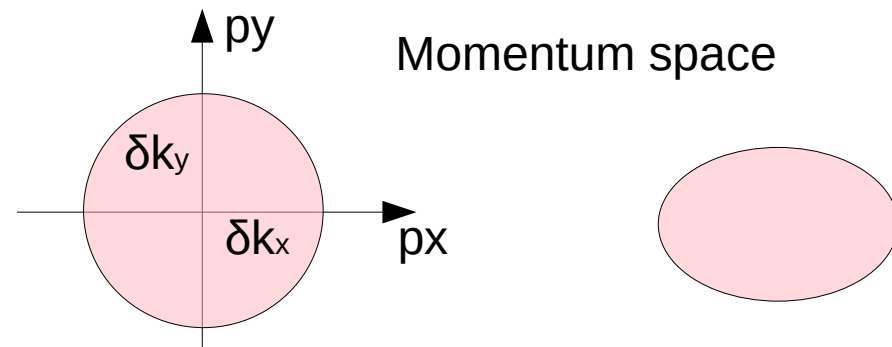
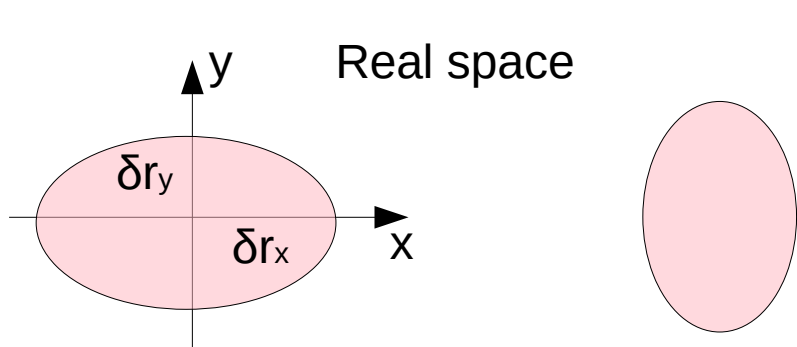
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Giuliano Giacalone<sup>2</sup>, Lars H. Heyen<sup>2</sup>, Maciej Gafka<sup>1</sup>,  
Keerthan Subramanian<sup>1</sup>, Marvin Holten<sup>1,4</sup>, Philipp M. Preiss<sup>1,5</sup>,  
Stefan Floerchinger<sup>3</sup> & Selim Jochim<sup>1</sup>

# Ideal hydro model based on the many-body gas (EOS, $N \gg 1$ )



**Bonus :** Tails of the trapped density nicely captured by Gross-Pitaevskii framework

[Floerchinger, Giacalone, Heyen, PRC **112** (2025) 1, 014003]

**10 is “different” !?**

# More prospects [from arXiv:2509.05049] – ideas welcome!

## We can play with

Initial geometry/size

Interaction strength

Number of atoms

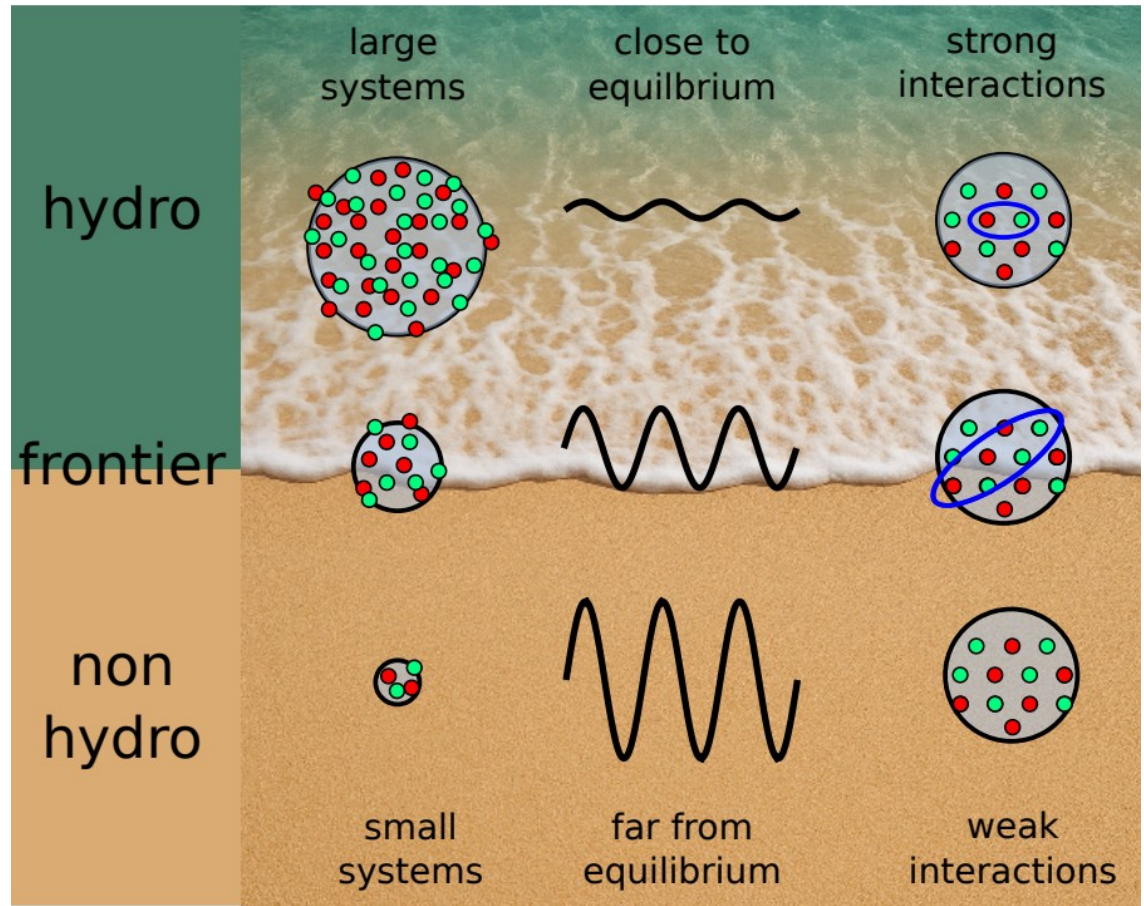
Perturbations

## We can measure

Response/relaxation

Two- and multi-particle correlations

Transport/EOS



## Much activity on the “equilibrium front” ... hydrodynamic attractors

New platform operational in Huzhou for studying thermal gas across opacities

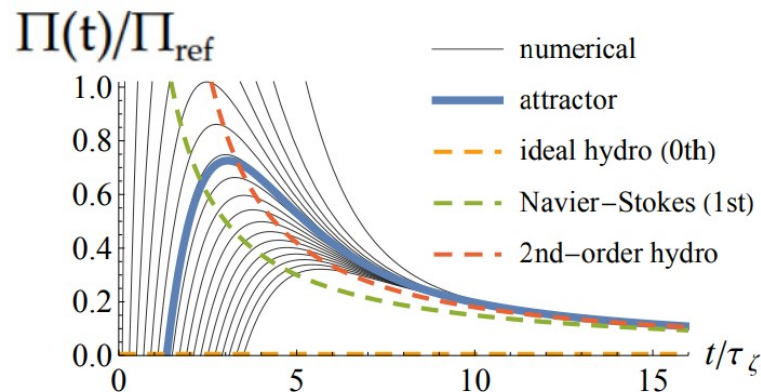
[Li *et al.*, arXiv:2405.02847] **Talk by Fuqiang Wang**

Protocol to look for attractor in cold gases

[Fuii, Enss, PRL **133** (2024) 17, 173402]

Seeing cyclic attractor behavior

[Mazeliauskas, Enss, arXiv:2501.19240]



**Talk by Clemens Werthmann**

Far-from-equilibrium dynamics in thermal near-unitary gas

[Werthmann, Heller, arXiv:2507.02838]

**Ultracold atom setup ideally suited for experimental discovery of the attractor**

# Frontier with ultra-cold atom gases – Spatial imaging

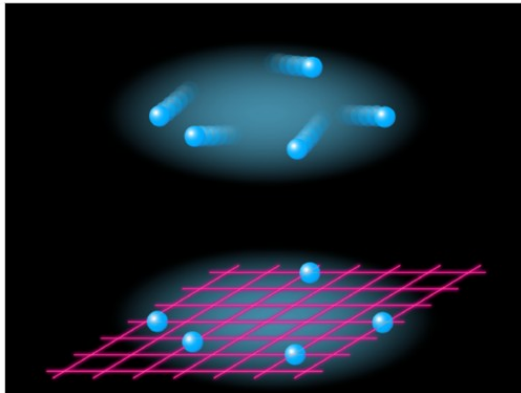
## A Glimpse at the Quantum Behavior of a Uniform Gas

Meera Parish

School of Physics and Astronomy, Monash University, Melbourne, Australia

May 5, 2025 • *Physics* 18, 89

An innovative way to image atoms in cold gases could provide deeper insights into the atoms' quantum correlations.



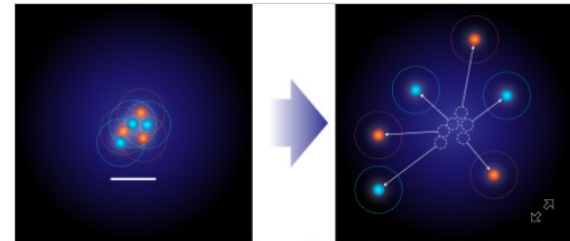
## Magnifying Atomic Images

Tarik Yefsah

French National Centre for Scientific Research (CNRS) and École Normale Supérieure, Paris, France

September 2, 2025 • *Physics* 18, 152

A new technique allows the imaging of an atomic system in which the interatomic spacing is smaller than the optical-resolution limit.



# Many-body correlations of atoms – Snapshots of the ground-state wave function

$$|\Psi(\mathbf{r}_1, \mathbf{r}_2, \dots, \mathbf{r}_A)|^2 \text{ atoms}$$

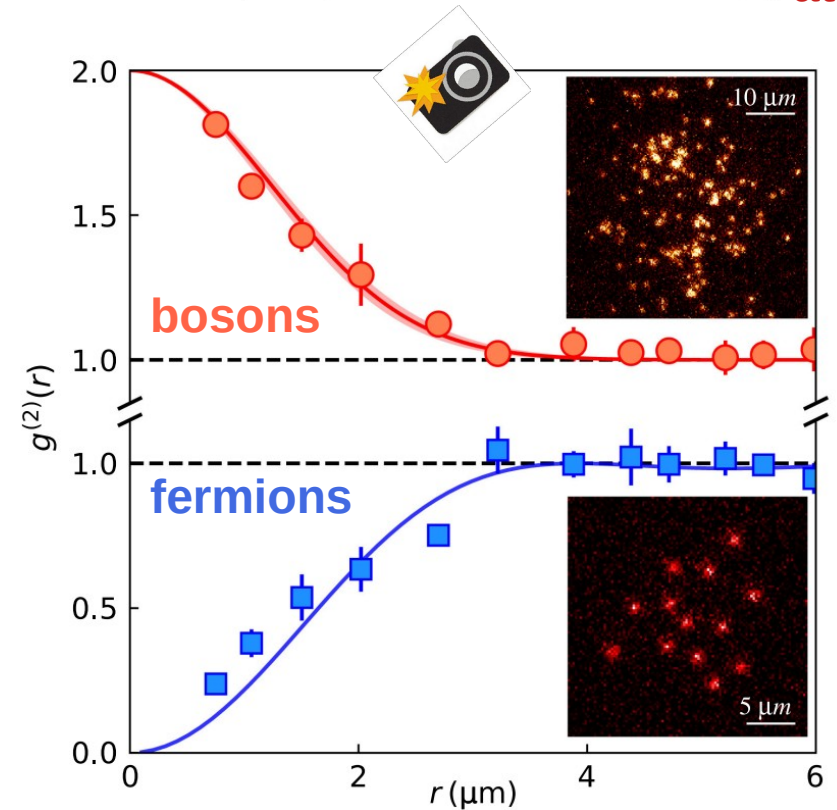
two-body correlation function

$$g_2(\mathbf{r}_1, \mathbf{r}_2) = \frac{\langle \psi^\dagger(\mathbf{r}_2)\psi^\dagger(\mathbf{r}_1)\psi(\mathbf{r}_1)\psi(\mathbf{r}_2) \rangle}{n^2}$$

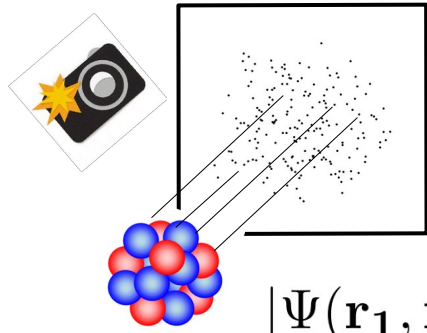


[Yao et al., PRL **134** (2025) 18, 183402]

Connection with nuclear physics?



## Imaging nuclear ground states at colliders – Same strategy



$$|\Psi(\mathbf{r}_1, \mathbf{r}_2, \dots, \mathbf{r}_A)|^2$$

$$t(\mathbf{x}) = \sum_i^A \delta(\mathbf{x} - \mathbf{x}_i) \quad \text{THICKNESS FUNCTION} \quad \text{ULTRA-CENTRAL ENTROPY}$$

$$s(\mathbf{x}) \propto t(\mathbf{x})$$

### Mean squared eccentricity

$$\langle \varepsilon_n^2 \rangle \propto \frac{1}{A} \int_{\mathbf{x}} \rho_{\perp}^{(1)}(\mathbf{x}) (x^2 + y^2)^n \quad + \quad \int_{\mathbf{x}_1, \mathbf{x}_2} \rho_{\perp}^{(2)}(\mathbf{x}_1, \mathbf{x}_2) (x_1 + iy_1)^n (x_2 - iy_2)^n$$

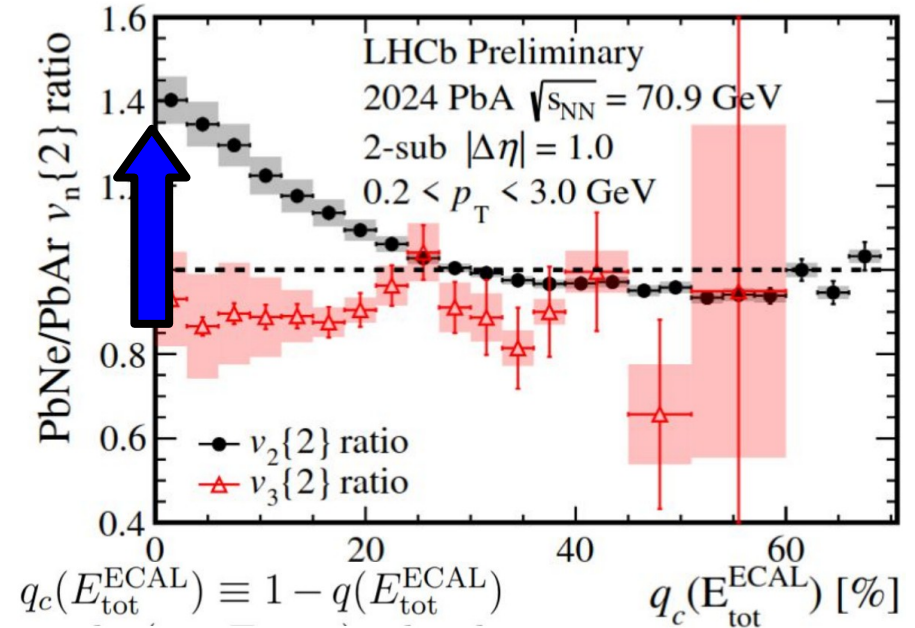
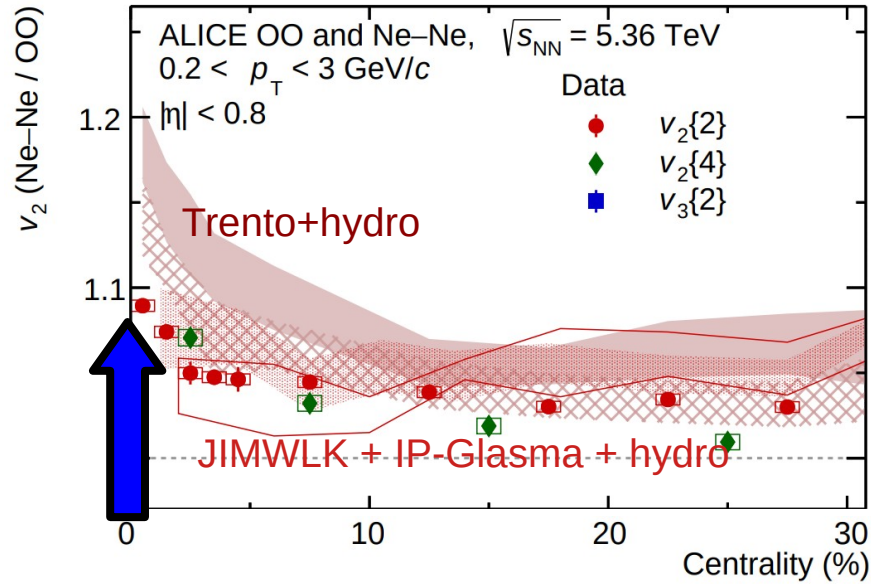
FINITE NUMBER OF NUCLEONS ⚠ TWO-BODY CORRELATIONS

### New “eccentricity operator” for many-body quantum systems

$$\hat{\mathcal{E}}_n(\mathbf{x}_1, \mathbf{x}_2) = (x_1 + iy_1)^n (x_2 - iy_2)^n$$

[Duguet, Giacalone, Jeon, Tichai, arXiv:2504.02481]

## Highlights from ALICE and LHCb at this conference



Upward correction from the ground-state expectation  $\langle \Psi_0 | \hat{\mathcal{E}}_2 | \Psi_0 \rangle$

Neon has stronger angular correlations than oxygen (e.g. deformation)

**Implications for nuclear forces in chiral EFT? Interplay with QCD effects?**

[work in progress with *ab initio* nuclear structure community]

# Conclusion

Fully controllable quantum systems are available (particle number, interactions, geometry)

Understanding emergence – Re-examining textbook criteria, new language/interpretation

**Heavy/Light ions (or?) and ultracold atoms at the forefront of these developments!**

