## Chemical freeze-out of hadrons within the advanced Hadron Resonance Gas Model

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## Motivation

Exploring of the QCD phase diagram:

- detect signals of colour deconfinement
- detect signals of chiral symmetry restoration
- locate critical endpoint of QCD phase diagram

**In order to resolve these tasks we need a good tool to analyze the data.**



## Motivation



3

- Theoretical model should make feed-down corrections consistently with experimental analysis
- Particle ratios should be taken within the same centrality interval

### Induced Surface Tension EOS

System of coupled equations between the pressure p and the induced surface tension coefficient  $\Sigma$ :

$$
p = \sum_{k=1}^{N} p_k^{Id}(T, v_k^P)
$$

$$
\Sigma = \sum_{k=1}^{N} R_k p_k^{Id}(T, v_k^S)
$$

$$
n_k^{Id}(T,\mu) = \frac{g_k}{2\pi^2\hbar^3} \int_{\infty}^{\infty} \frac{p^2 dp}{\exp[(E-\mu)/T] \pm 1}
$$

$$
p_k^{Id}(T,\mu) = \frac{g_k}{2\pi^2\hbar^3} \int_{0}^{\infty} \frac{p^4 dp}{3E} \frac{1}{\exp[(E-\mu)/T] \pm 1}
$$

**V.V. Sagun et al., EPJ Web of [Conferences](https://www.epj-conferences.org/articles/epjconf/pdf/2017/06/epjconf_conf2017_09007.pdf) 137 (2017) 09007 K. A. Bugaev et al., Nucl. Phys. <sup>A</sup> <sup>970</sup> [\(2018\) 133-155](https://doi.org/10.1016/j.nuclphysa.2017.11.008)** <sup>4</sup>

Effective chemical potentials:

$$
v_k^S = \mu_k - pV_k - \alpha \Sigma S_k
$$

$$
\mathbf{v}_k^P = \mu_k - pV_k - \Sigma S_k
$$

#### Induced Surface Tension EOS

Particle number density of kth sort:

$$
n_k = \frac{a_{22}n_k^{ld}(T, v_k^{ld}) - a_{12}R_kn_k^{ld}(T, v_k^S)}{a_{11}a_{22} - a_{12}a_{21}}
$$

$$
a_{11} = 1 + \sum_{k=1}^{N} V_k n_k^{Id} (T, v_k^P)
$$
  
\n
$$
a_{22} = 1 + \alpha \sum_{k=1}^{N} S_k R_k n_k^{Id} (T, v_k^S)
$$
  
\n
$$
a_{12} = \sum_{k=1}^{N} S_k n_k^{Id} (T, v_k^P)
$$
  
\n
$$
a_{21} = \sum_{k=1}^{N} V_k R_k n_k^{Id} (T, v_k^S)
$$

#### **Advantages**

- 2 equations, its number does not depend on the number of different hard core radii
- Allow one to go beyond the Van der Waals approximation, since it reproduces 2nd, 3rd and 4th virial coefficients of the gas of hard spheres for  $\alpha = 1.245$

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## IST EOS settings

Experimental data: STAR Collaboration Energies: **7.7 — 200 GeV**  $\text{Local fit parameters: } \mathbf{T}, \boldsymbol{\mu}_{\mathbf{B}}, \boldsymbol{\mu}_{\mathbf{I3}}, \boldsymbol{\mu}_{\mathbf{S}}, \boldsymbol{\gamma}_{\mathbf{S}}$ Global fit parameters:  $\mathbf{R}_{\pi}$ ,  $\mathbf{R}_{\text{K}}$ ,  $\mathbf{R}_{\text{mesons}}$ ,  $\mathbf{R}_{\text{baryons}}$ ,  $\mathbf{R}_{\Lambda}$ 

Global parameters were fixed as:  $R_{\pi} = 0.15$  fm.  $Rx = 0.395$  fm,  $R$ <sub>mesons</sub>  $= 0.42$  fm. Rbaryons  $=0.365$  fm,  $R_A = 0.085$  fm

**A. Andronic et al., [Nucl. Phys.](https://www.sciencedirect.com/science/article/pii/S0375947409009890) A 834 (2010) 237c K. A. Bugaev et al., Ukr. J. Phys. 61 (2016) no. 8, 659 J. [Cleymans](https://journals.aps.org/prc/abstract/10.1103/PhysRevC.73.034905) et al., Phys. Rev. C 73 (2006) 034905 S. [Borsanyi](https://journals.aps.org/prl/abstract/10.1103/PhysRevLett.125.052001) et al., Phys. Rev. Lett. 125 (2020) 052001**

#### IST EOS fit result of STAR data at 200 GeV



■ Inclusion of weak decays **greatly** improves the description of particle ratios in the experimental data (**50 times better** in this case). 7

## Inclusion of weak decays for STAR data in the IST EOS

Fit by STAR Collaboration for  $\sqrt{s}$  > 200 GeV has T ~ 154 MeV

Inclusion of weak decays **decrease** temperature of chemical freeze-out **on 10 MeV**

**A. Andronic et al., [Nucl. Phys.](https://www.sciencedirect.com/science/article/pii/S0375947409009890) A 834 (2010) 237c K. A. Bugaev et al., Ukr. J. Phys. 61 (2016) no. 8, 659 J. [Cleymans](https://journals.aps.org/prc/abstract/10.1103/PhysRevC.73.034905) et al., Phys. Rev. C 73 (2006) 034905 S. [Borsanyi](https://journals.aps.org/prl/abstract/10.1103/PhysRevLett.125.052001) et al., Phys. Rev. Lett. 125 (2020) 052001**



8

## Results of the IST EOS with weak decays for  $K^{\dagger}/\pi^{\dagger}$  ratio



- $\bullet$  K<sup>+</sup>/ $\pi$ <sup>+</sup> is the most problematic ratio for decription by different models
- Inclusion of weak decays greatly improves the description of particle ratios in the experimental data

## **Conclusions**

- ❑ IST EOS is a good tool to decribe particle yields and to get chemical freeze-out parameters
- ❑ An updated version of this model allows the fitting of ratios, taking into account both inclusive and exclusive feed-down corrections consistently with experimental analysis
- ❑ Brings the chemical freeze-out temperature to the right track. It gets lower than LQCD predictions for pseudocritical T
- ❑ Provides a good description of the particle ratios from the existing experimental data
- ❑ The chemical freeze-out parameters from the IST EOS fits for STAR and NA49 data are close to the LQCD calculations.

# Back up

### Resonances width

 $\blacksquare$  The resonance width is taken into account in thermal densities as it is crucial in a thermal model

■ For instance, description of pion yields cannot be achieved without it inclusion:  $m_{\sigma} = 484 \pm 24$  MeV, width  $\Gamma_{\sigma} = 510 \pm 20$  MeV

$$
n_X^{tot} = n_X^{thermal} + n_X^{decay} = n_X^{th} + \sum_{Y} n_Y^{th} Br(Y \to X)
$$

 $Br(Y \rightarrow X)$  – decay branching of Yth hadron into X

■ Fit of the particle ratios gives smaller systematic uncertainties than fitting of yields