

LATEST THEORETICAL DEVELOPMENTS IN UPC PHYSICS

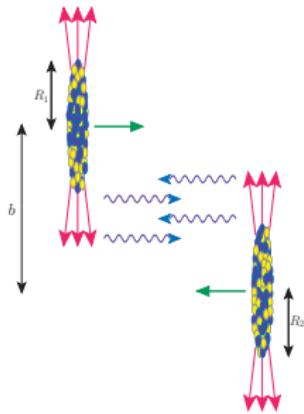
Mariola Kłusek-Gawenda

*The Henryk Niewodniczański Institute of Nuclear Physics
Polish Academy of Sciences*

- Equivalent Photon Approximation
- $\gamma\gamma \rightarrow \gamma\gamma$
- $\ell^+\ell^-\ell^+\ell^-$ production
- $c\bar{c}$ & $b\bar{b}$ production
- $\pi^+\pi^-\pi^+\pi^-$ production
- Electromagnetic excitation of nuclei and neutron evaporation



ULTRAPERIPHERAL COLLISION OF HEAVY IONS

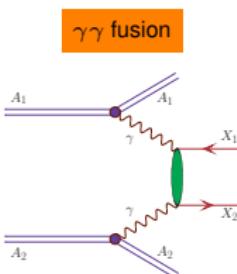
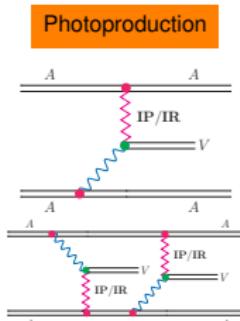


The strong electromagnetic field is a source of photons that can induce electromagnetic reactions in ion-ion collisions. Electromagnetism is a long-range force, so electromagnetic interactions occur even at relatively large ion-ion separations.

$$\text{UPC: } b_{\min} = R_1 + R_2 \approx 14 \text{ fm}$$

$$\text{Photon energy: } \omega = \frac{\gamma}{b_{\min}} \approx \gamma \times 15 \text{ MeV}$$

$$\text{Virtuality: } Q^2 = \frac{1}{R^2} \approx 0.0008 \text{ GeV}^2$$

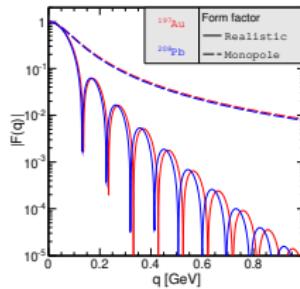
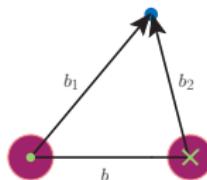


GOAL

- testing QED
- probing the structure of the nucleus and nucleons
- exploration of exotic physics
- minimalization of the QGP production
- bridge the gap between high-energy and nuclear physic

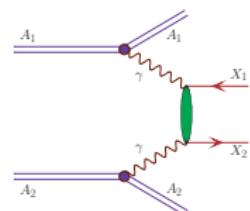
EQUIVALENT PHOTON APPROXIMATION

$$\begin{aligned}
 \sigma_{A_1 A_2 \rightarrow A_1 A_2 X_1 X_2} &= \int \sigma_{\gamma\gamma \rightarrow X_1 X_2}(\omega_1, \omega_2) d\omega_1 d\omega_2 n(\omega_1) n(\omega_2) \rightarrow \dots n(\omega) = \int_{R_{min}}^{\infty} 2\pi b db N(\omega, b) \dots \\
 &= \int \sigma_{\gamma\gamma \rightarrow X_1 X_2} (W_{\gamma\gamma}) N(\omega_1, b_1) N(\omega_2, b_2) S_{abs}^2(b) \frac{W_{\gamma\gamma}}{2} dW_{\gamma\gamma} dY_{X_1 X_2} d\bar{b}_x d\bar{b}_y d^2 b \\
 &= \int \frac{d\sigma_{\gamma\gamma \rightarrow X_1 X_2} (W_{\gamma\gamma})}{d\cos\theta} N(\omega_1, b_1) N(\omega_2, b_2) S_{abs}^2(b) \frac{W_{\gamma\gamma}}{2} dW_{\gamma\gamma} dY_{X_1 X_2} d\bar{b}_x d\bar{b}_y d^2 b \\
 &\times \frac{d\cos\theta}{dy_{X_1} dy_{X_2} dp_t} \times dy_{X_1} dy_{X_2} dp_t .
 \end{aligned}$$



$$N(\omega, b) = \frac{Z^2 \alpha_{em}}{\pi^2 \beta^2} \frac{1}{\omega} \frac{1}{b^2} \times \left| \int d\chi \chi^2 \frac{F\left(\frac{\chi^2 + u^2}{b^2}\right)}{\chi^2 + u^2} J_1(\chi) \right|^2$$

$$F(q^2) = \frac{4\pi}{|\mathbf{q}|} \int \rho(r) \sin(|\mathbf{q}| r) r dr$$



MC EVENT GENERATORS

- ① **STARlight** simulates two-photon and γ -IP interactions between relativistic nuclei and protons. It produces a variety of final states. For two- γ , it simulates lepton pairs and a variety of mesons. For photonuclear interactions, it models coherent and incoherent vector mesons production.

*S.R. Klein, J. Nystrand, J. Seger, Y. Gorbunov, J. Butterworth,
Comp. Phys. Comm. **212** (2017) 258*

- ② **SuperChic** - event generator for exclusive and γ -initiated production in proton and heavy ion collisions. A range of SM final states are implemented, in most cases with spin correlations where relevant, and a fully differential treatment of the soft survival factor is given. Arbitrary user-defined histograms and cuts may be made.

*L.A. Harland-Lang, V.A. Khoze, M.G. Ryskin, W.J. Stirling,
Eur. Phys. J. **C80** (2020) 925*

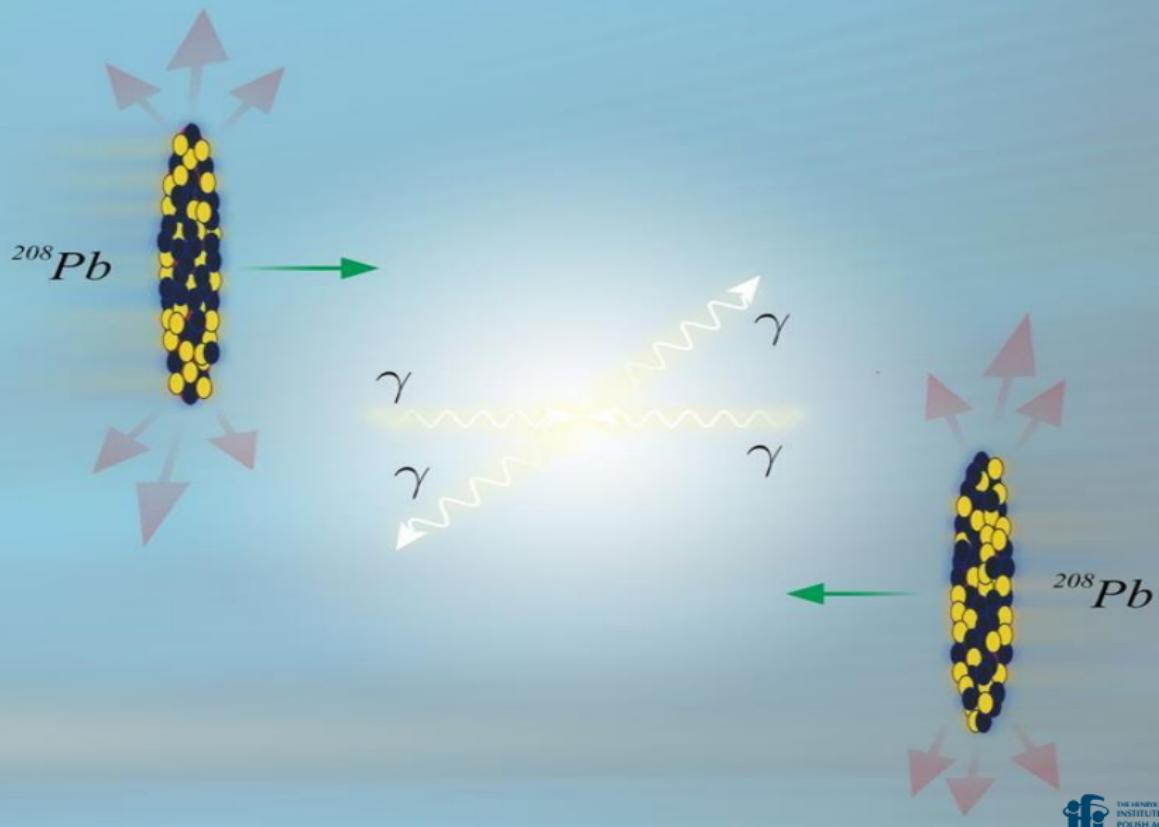
- ③ **UPCgen** - simulation program for $\ell^+ \ell^-$ pair production implements a refined treatment of the γ flux allowing us to improve the agreement with ATLAS data at large dilepton rapidities. Besides, the new generator offers a possibility to study γ polarization effects and set arbitrary values of the lepton anomalous magnetic moment.

*N. Burmasov, E. Kryshen, P. Buehler, R. Lavicka,
Comput.Phys.Commun. **277** (2022) 108388*

- ④ **gamma-UPC** is a library for calculating the photon fluxes in the exclusive $\gamma\gamma$ processes in ultraperipheral proton and nuclear collisions. It is derived from electric dipole or charge form factors, and has incorporated hadronic survival probabilities.

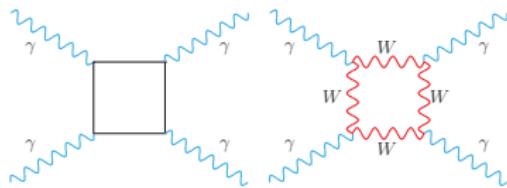
*H.-S. Shao, D. d'Enterria,
J. High Energ. Phys. **2022**, 248 (2022)*

LIGHT-BY-LIGHT SCATTERING



LIGHT-BY-LIGHT SCATTERING

Boxes



Fermionic boxes (LO QED)

FormCalc.

$$|\mathcal{M}_{\gamma\gamma \rightarrow \gamma\gamma}|^2 = \alpha_{em}^4 f(\hat{t}, \hat{u}, \hat{s})$$

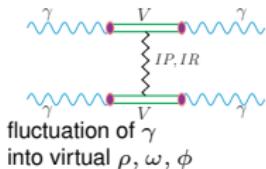
W Box

LoopTools.

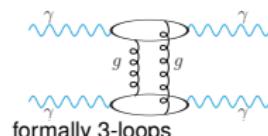
VDM-Regge

WE ADD

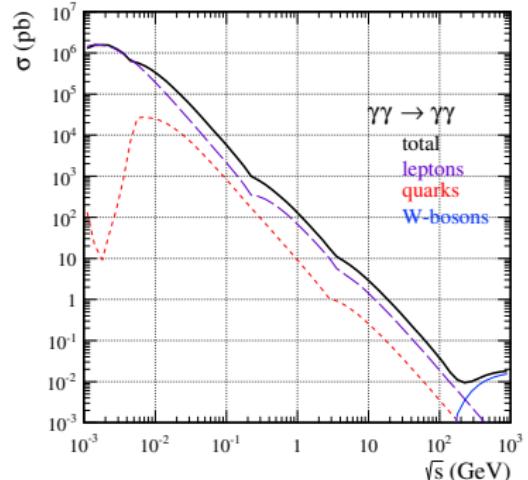
2-gluon exch.



fluctuation of γ
into virtual ρ, ω, ϕ



formally 3-loops



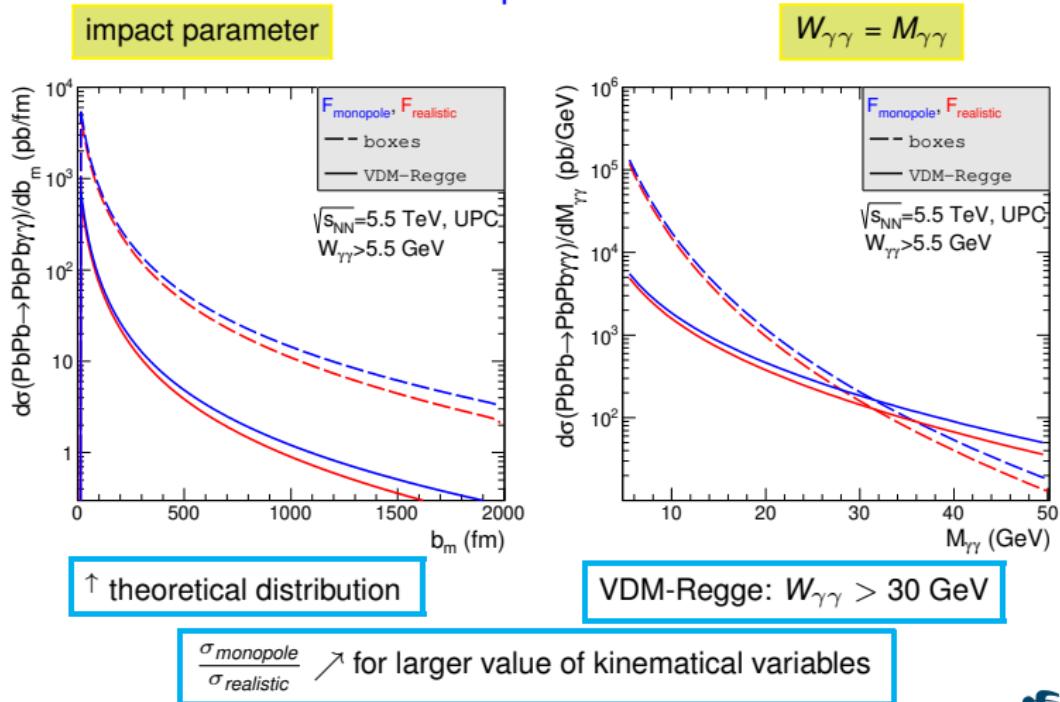
We have compared our results with:

- Jikia et al. (1993),
- Bern et al. (2001),
- Bardin et al. (2009).

Bern et al. consider QCD and QED corrections (two-loop Feynman diagrams) to the one-loop fermionic contributions in the ultrarelativistic limit ($\hat{s}, |\hat{t}|, |\hat{u}| \gg m_f^2$). The corrections are quite small numerically.

AA \rightarrow AA $\gamma\gamma$ - FORM FACTOR

- ⇒ realistic
- ⇒ monopole



AA \rightarrow AA $\gamma\gamma$ - CMS & ATLAS RESULTS

→ ATLAS Collaboration,
PRL **123** (2019) 052001

- $p_{t,\gamma} > 3 \text{ GeV}$
- $|\eta_\gamma| < 2.4$
- $M_{\gamma\gamma} > 6 \text{ GeV}$
- $p_{t,\gamma\gamma} < 2 \text{ GeV}$
- $A_{\text{Co}} < 0.01$

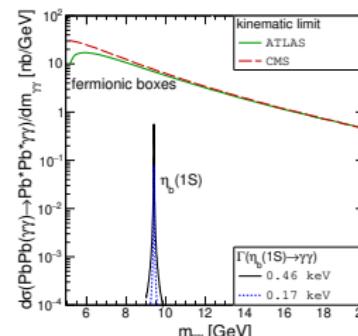
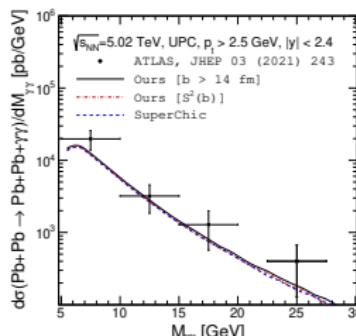
→ ATLAS Collaboration,
JHEP **03** (2021) 243

- $E_{t,\gamma} > 2.5 \text{ GeV}$
- $|\eta_\gamma| < 2.4$
- $M_{\gamma\gamma} > 5 \text{ GeV}$
- $p_{t,\gamma\gamma} < 1 \text{ GeV}$
- $A_{\text{Co}} < 0.01$

→ CMS Collaboration,
PLB **797** (2019) 134826

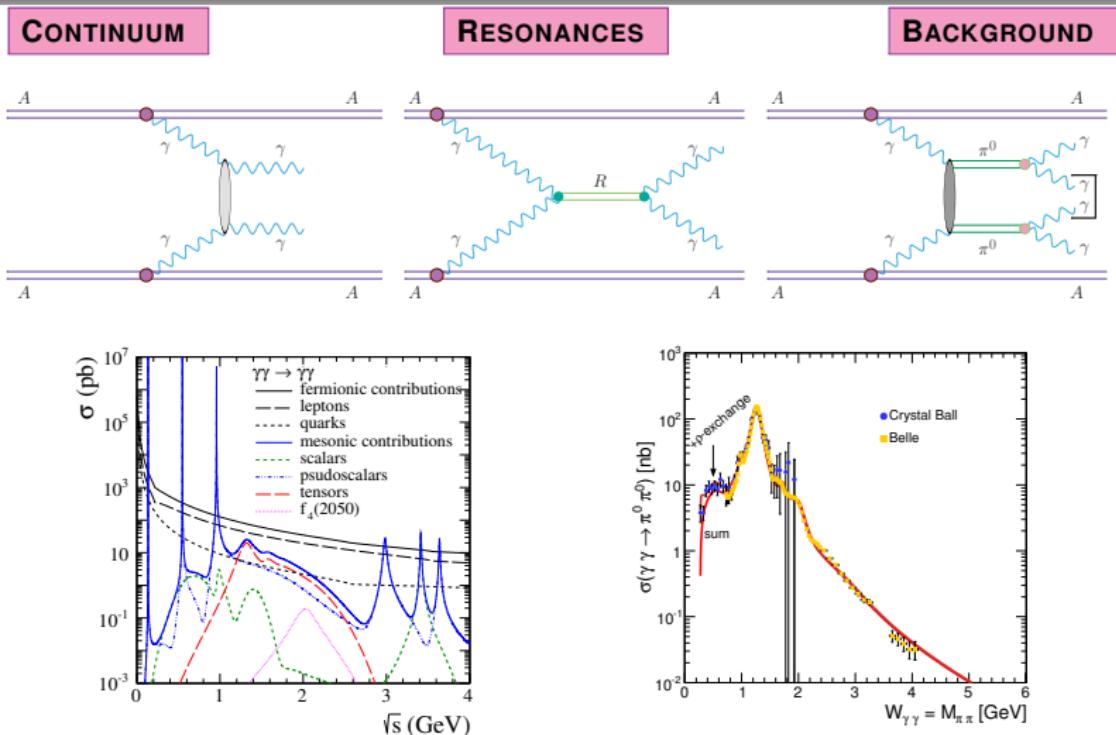
- $E_{t,\gamma} > 2 \text{ GeV}$
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- $M_{\gamma\gamma} > 5 \text{ GeV}$
- $p_{t,\gamma\gamma} < 1 \text{ GeV}$
- $A_{\text{Co}} < 0.01$

Experiment Collaboration	σ [nb]	Theory		
		Vegas	SuperChic	gamma-UPC
ATLAS (2018 data)	$78 \pm 13(\text{stat.}) \pm 7(\text{syst.})$	51	50	–
ATLAS (2015+2018)	$120 \pm 17(\text{stat.}) \pm 13(\text{syst.})$	80	77	70
CMS (2015)	$120 \pm 46(\text{stat.}) \pm 28(\text{syst.})$	103	101	–



- Underestimation:
- tetraquarks X(6900) ?
 - graviton, axion ?
 - coherent sum of higher order processes ?
 - pionic boxes ?

AA \rightarrow AA $\gamma\gamma$ FOR $M_{\gamma\gamma} < 5$ GEV ?



- P. Lebiedowicz, A. Szczurek, *Phys. Lett. B772* (2017) 330,
The role of meson exchanges in light-by-light scattering

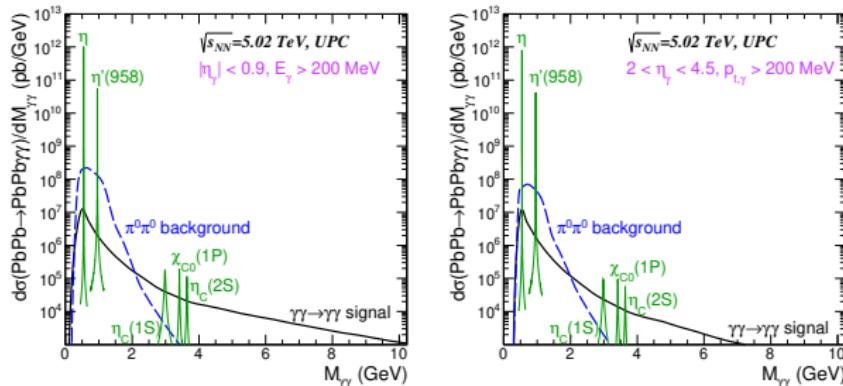
- M. K-G, A. Szczurek, *Phys. Rev. C87* (2013) 054908;
 $\pi^+\pi^-$ and $\pi^0\pi^0$ pair production in photon-photon and in ultraperipheral ultrarelativistic heavy-ion collisions

UPC OF AA...

ALICE cuts

- boxes
- bkg
- mesons

LHCb cuts



Total nuclear cross section [nb]

Energy	$W_{\gamma\gamma} = (0 - 2)$ GeV		$W_{\gamma\gamma} > 2$ GeV		
	Fiducial region	ALICE	LHCb	ALICE	LHCb
Boxes		4 890	3 818	146	79
$\pi^0\pi^0$ bkg		135 300	40 866	46	24
η		722 573	568 499		
$\eta'(958)$		54 241	40 482		
$\eta_c(1S)$				9	5
$\chi_{c0}(1P)$				4	2
$\eta_c(2S)$				2	1

AA \rightarrow AA $\gamma\gamma$ @ FORWARD REGION ?

✓ ALICE Collaboration,

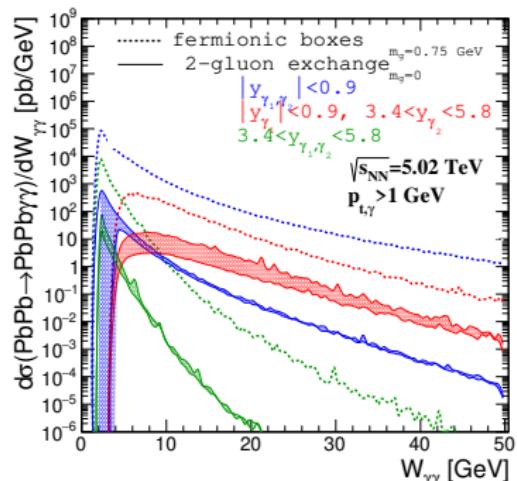
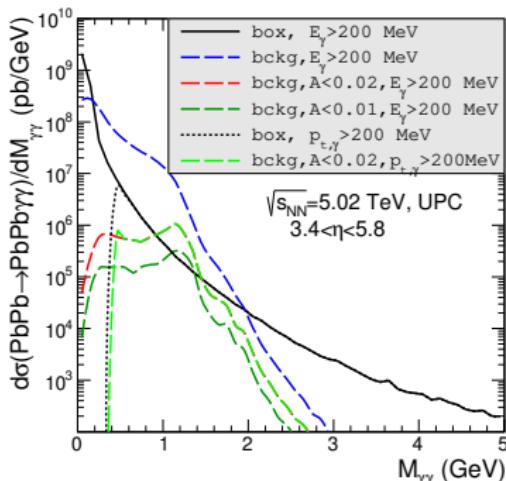
*Letter of Intent: A Forward Calorimeter (FoCal) in the ALICE experiment,
CERN-LHCC-2020-009*

FOCAL → $3.4 < \eta < 5.8$

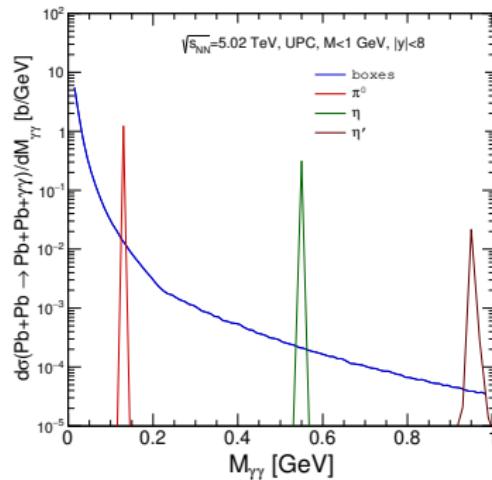
The forward electromagnetic and hadronic calorimeter is an upgrade to the ALICE experiment, to be installed during LS3 for data-taking in 2027–2029 at the LHC.

$E_\gamma > 0.2$ GeV

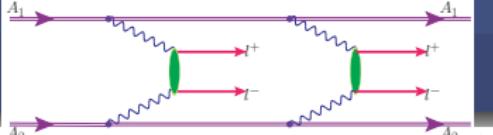
$p_{t,\gamma} > 1$ GeV



Boxes & Pionic bkgr & 2-gluon exchange (with effective gluon mass)

AA \rightarrow AA $\gamma\gamma$ @ LOW p_t REGION ? $M_{\gamma\gamma} < 1 \text{ GeV}$  $\gamma\gamma \rightarrow \pi^0 \rightarrow \gamma\gamma$

FOUR-LEPTON PRODUCTION



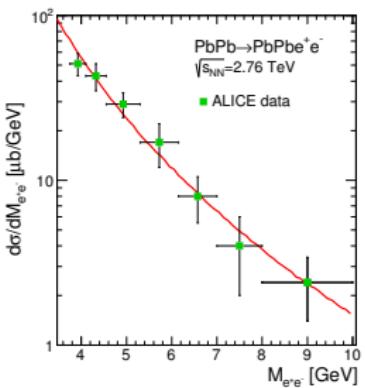
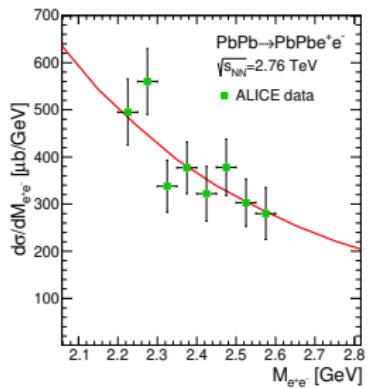
$$\frac{d\sigma_{A_1 A_2 \rightarrow A_1 A_2 (\ell^+ \ell^-)(\ell^+ \ell^-)}}{dy_{\ell^+}^I dy_{\ell^-}^I dy_{\ell^+}^{II} dy_{\ell^-}^{II}} = \frac{1}{2} \int \left(\frac{dP_{\gamma\gamma \rightarrow \ell^+ \ell^-}^I(b, y_{\ell^+}^I, y_{\ell^-}^I; p_{t,\ell})}{dy_{\ell^+}^I dy_{\ell^-}^I} \times \frac{dP_{\gamma\gamma \rightarrow \ell^+ \ell^-}^{II}(b, y_{\ell^+}^{II}, y_{\ell^-}^{II}; p_{t,\ell})}{dy_{\ell^+}^{II} dy_{\ell^-}^{II}} \right) \times 2\pi b db$$

$$P_{\gamma\gamma \rightarrow \ell^+ \ell^-}(b; y_{\ell^+}, y_{\ell^-}, p_{t,\ell}) = \int N(\omega_1, \mathbf{b}_1) N(\omega_2, \mathbf{b}_2) S_{abs}^2(\mathbf{b}) \times \frac{d\sigma_{\gamma\gamma \rightarrow \ell_1 \ell_2} (W_{\gamma\gamma})}{d \cos \theta} d\bar{b}_x d\bar{b}_y \frac{W_{\gamma\gamma}}{2} dW_{\gamma\gamma} dY_{\ell_1 \ell_2}$$

$2.2 \text{ GeV} < M_{ee} < 2.6 \text{ GeV}$

$|y_e| < 0.9$

$3.7 \text{ GeV} < M_{ee} < 10 \text{ GeV}$

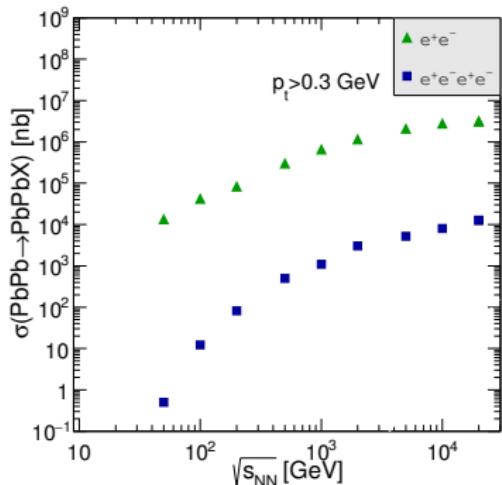


Good description of single pair production \Rightarrow two $e^+ e^-$ pair production...?

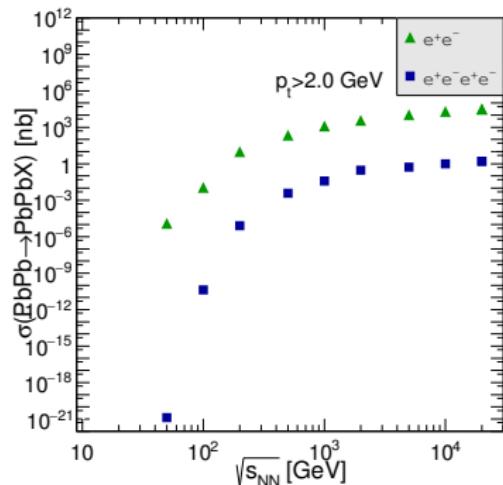
$$AA \rightarrow AAe^+e^- \text{ & } AA \rightarrow AAe^+e^-e^+e^-$$

**Single e^+e^- pair production
vs.
double scattering production of two e^+e^- pairs**

$p_t > 0.3 \text{ GeV}$

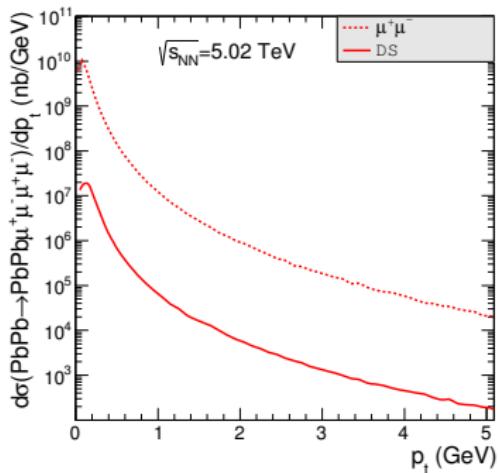
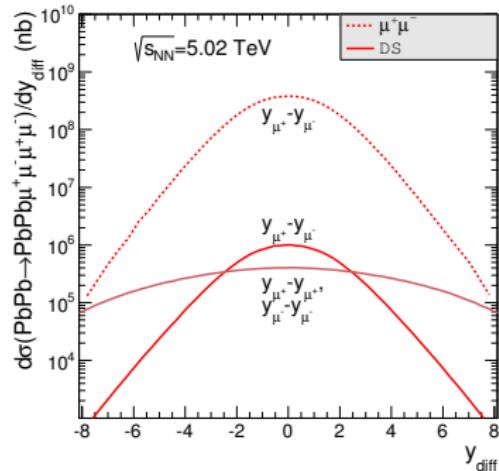


$p_t > 2.0 \text{ GeV}$



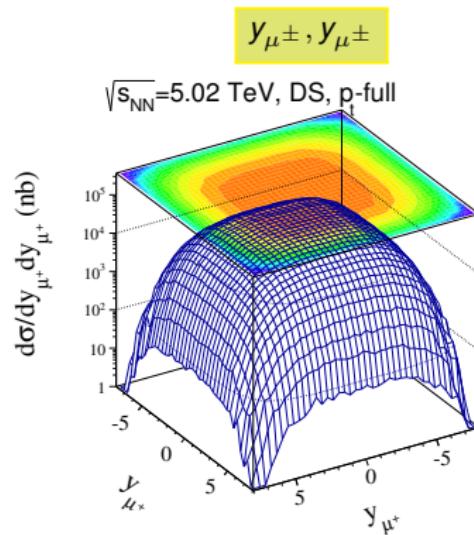
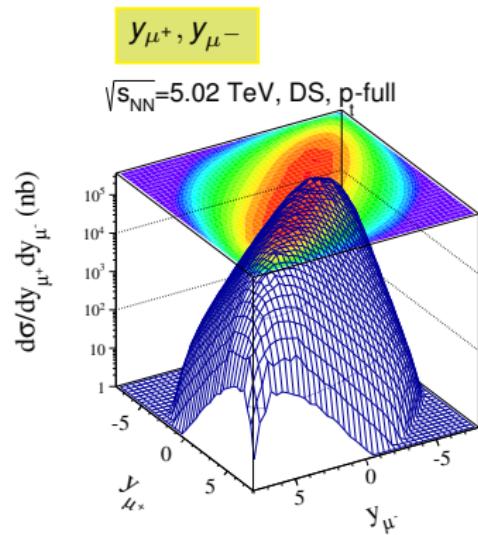
$$AA \rightarrow AA\mu^+\mu^- \text{ & } AA \rightarrow AA\mu^+\mu^-\mu^+\mu^-$$

**Single $\mu^+\mu^-$ pair production
vs.
double scattering production of two $\mu^+\mu^-$ pairs**

 $p_{t,\mu}$  **y_{diff}** 

$$\sigma_{\ell^+\ell^-} \simeq 1000 \times \sigma_{(\ell^+\ell^-)(\ell^+\ell^-)} \simeq 1000000 \times \sigma_{\ell^+\ell^-\ell^+\ell^-}$$

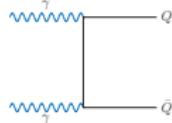
$\text{AA} \rightarrow \text{AA} \mu^+ \mu^- \mu^+ \mu^-$



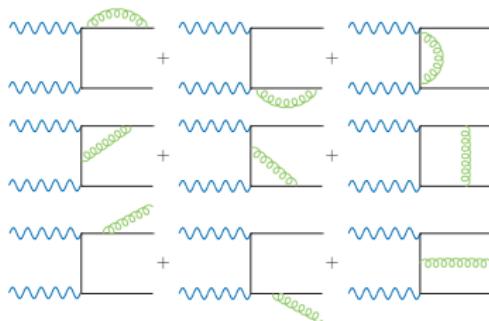
creation of similar distributions by ALICE or CMS?

QUARKS PRODUCTION

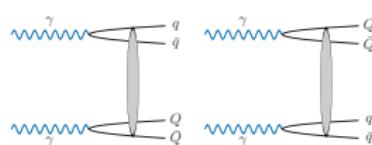
❶ $2 \rightarrow 2$ process (Born amplitude)



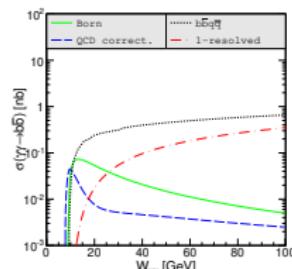
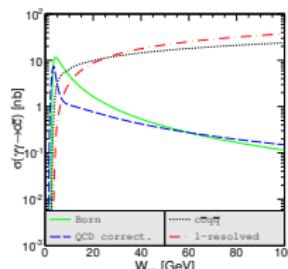
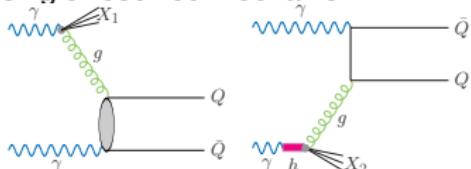
❷ LO QCD corrections



❸ $Q\bar{Q}q\bar{q}$ production



❹ single-resolved mechanism



	σ_{tot}	Ad.1	Ad.2	Ad.3	Ad.4
$c\bar{c}$	2.47 mb	42.5%	14.6%	27.1%	15.8%
$b\bar{b}$	$10.83 \mu b$	18.9%	7.7%	64.5%	8.9%

$$AA \rightarrow AA\pi^+\pi^-\pi^+\pi^-$$

H1 DATA

H1prelim-18-011
April 10, 2018

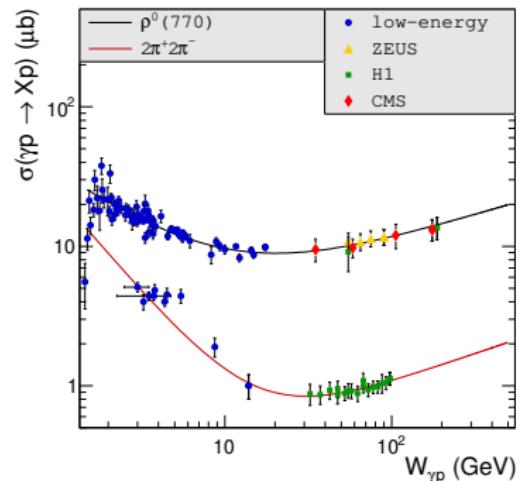
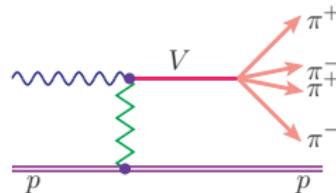
Submitted to **DIS-2018**, Kobe, 16–20 April, 2018

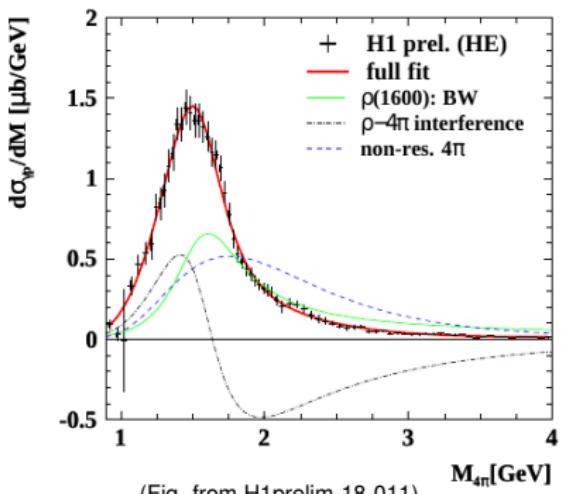
Exclusive Photoproduction of $2\pi^+2\pi^-$ Final State at H

Abstract

Exclusive production of four charged pions at the ep collider HERA is studied at small photon virtualities $Q^2 < 2 \text{ GeV}^2$. The data were taken with the H1 detector in the years 2006 and 2007 at a centre-of-mass energies of $\sqrt{s} = 319 \text{ GeV}$ and $\sqrt{s} = 225 \text{ GeV}$ and correspond to an integrated luminosity of 7.6 pb^{-1} and 1.7 pb^{-1} respectively. The cross section of the reaction $\gamma p \rightarrow (2\pi^+2\pi^-)Y$ is determined in the phase space of $35 < W_{\gamma p} < 100 \text{ GeV}$, $|t| < 1 \text{ GeV}^2$ and $M_Y < 1.6 \text{ GeV}$. The 4π mass spectra indicate that the reaction proceeds predominantly via production and decay of ρ' resonances. The fit however did not allow yet to distinguish unambiguously between the hypotheses of one or two broad overlapping ρ' resonances.

vector meson ?





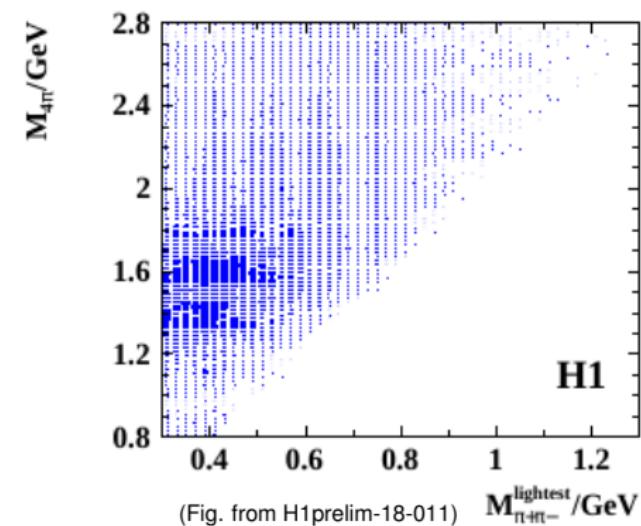
(Fig. from H1prelim-18-011)

77. The $\rho(1450)$ and the $\rho(1700)$

Updated November 2015 by S. Eidelman (Novosibirsk), C. Hanhart (Juelich) and G. Venanzoni (Frascati).

In our 1988 edition, we replaced the $\rho(1600)$ entry with two new ones, the $\rho(1450)$ and the $\rho(1700)$, because there was emerging evidence that the 1600-MeV region actually contains two ρ -like resonances. Erkal [1] had pointed out this possibility with a theoretical analysis on the consistency of 2π and 4π electromagnetic form factors and the $\pi\pi$ scattering length. Donnachie [2], with a full analysis of data on the 2π and 4π final states in e^+e^- annihilation and photoproduction reactions, had also argued that in order to obtain a consistent picture, two resonances were necessary. The existence of $\rho(1450)$ was supported by the analysis of $\eta\rho^0$ mass spectra obtained in photoproduction and e^+e^- annihilation [3], as well as that of $e^+e^- \rightarrow \omega\pi$ [4].

The analysis of [2] was further extended by [5,6] to include new data on 4π -systems produced in e^+e^- annihilation, and in τ -decays (τ decays to 4π , and e^+e^- annihilation to 4π can be related by the Conserved Vector Current assumption). These systems were successfully analyzed using interfering contributions from two ρ -like states, and from the tail of the $\rho(770)$ decaying into two-body states. While specific conclusions on $\rho(1450) \rightarrow 4\pi$ were obtained, little could be said about the $\rho(1700)$.



(Fig. from H1prelim-18-011)

DECAY MODE

$$M_{4\pi} = 1.6 \text{ GeV}$$

or

$$M_{4\pi} = 1.45 \text{ GeV} \quad \& \quad M_{4\pi} = 1.7 \text{ GeV}$$

RESONANCES SKETCH PDG

$\rho(1570)$

$$\rho^G(J^PC) = 1^+(1^{--})$$

$\rho(1570)$ MASS

VALUE (MeV)	EVTS	DOCUMENT ID	TECN	COMMENT
$1570 \pm 36 \pm 62$	54	1 AUBERT 085	BABR	$10.6 e^+ e^- \rightarrow \phi\pi^0\gamma$

$\rho(1570)$ WIDTH

VALUE (MeV)	EVTS	DOCUMENT ID	TECN	COMMENT
$144 \pm 75 \pm 43$	54	3 AUBERT 085	BABR	$10.6 e^+ e^- \rightarrow \phi\pi^0\gamma$

$\rho(1570)$ DECAY MODES

Mode	Fraction (Γ_i/Γ)
$\Gamma_1 e^+ e^-$	
$\Gamma_2 \phi\pi$	not seen
$\Gamma_3 \omega\pi$	

$\rho(1450)$ [r]

$$\rho^G(J^PC) = 1^+(1^{--})$$

Mass $m = 1465 \pm 25$ MeV [l]
 Full width $\Gamma = 400 \pm 60$ MeV [l]

$\rho(1450)$ DECAY MODES	Fraction (Γ_i/Γ)	p (MeV/c)
$\pi\pi$	seen	720
$\pi^+\pi^-$	seen	719
4π	seen	669

$\rho(1700)$ [r]

$$\rho^G(J^PC) = 1^+(1^{--})$$

Mass $m = 1720 \pm 20$ MeV [l] ($\eta\rho^0$ and $\pi^+\pi^-$ modes)
 Full width $\Gamma = 250 \pm 100$ MeV [l] ($\eta\rho^0$ and $\pi^+\pi^-$ modes)

$\rho(1700)$ DECAY MODES	Fraction (Γ_i/Γ)	p (MeV/c)
$2(\pi^+\pi^-)$	seen	803

$\rho(770)$ [h]

$$\rho^G(J^PC) = 1^+(1^{--})$$

Mass $m = 775.26 \pm 0.25$ MeV

Full width $\Gamma = 149.1 \pm 0.8$ MeV

$\Gamma_{ee} = 7.04 \pm 0.06$ keV

$\rho(770)$ DECAY MODES	Fraction (Γ_i/Γ)	Scale factor/ Confidence level	p (MeV/c)
$\pi\pi$	~ 100	%	363

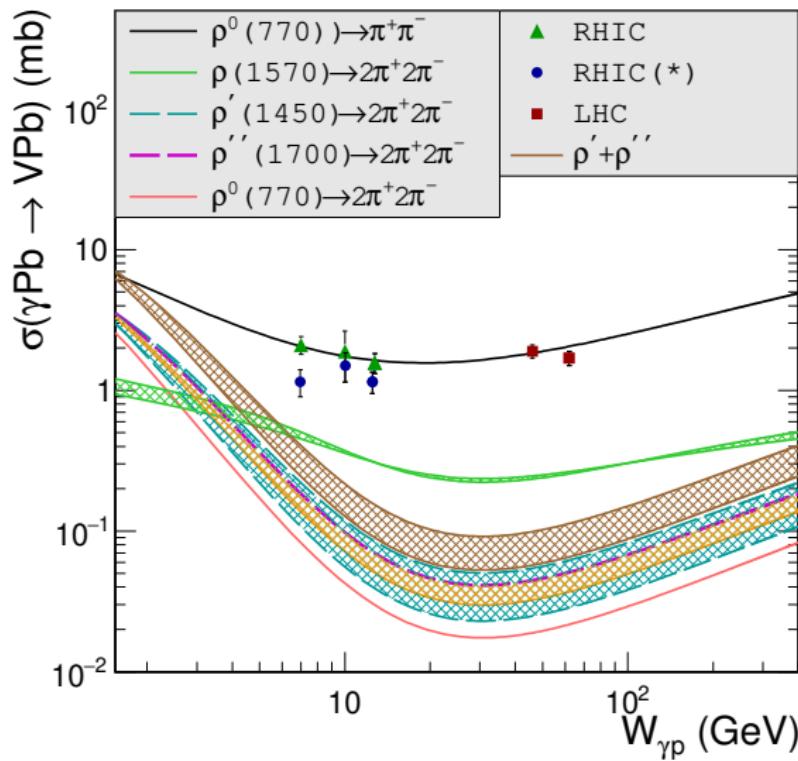
$$\pi^+ \pi^- \pi^+ \pi^- \quad (1.8 \pm 0.9) \times 10^{-5}$$

251

MY CALCULATION

m [GeV]	Γ [GeV]	$\Gamma(e^+e^-)$ [keV]
$\rho(1570)$		
1.57 ± 0.07	0.144 ± 0.09	$0.35 - 0.5^*$
$\rho(1450) \equiv \rho'$		
1.465 ± 0.025	0.40 ± 0.05	$4.3 - 6^*$
$\rho(1700) \equiv \rho''$		
1.72 ± 0.02	0.25 ± 0.01	7.6 ± 1.3

COHERENT VECTOR MESON PHOTOPRODUCTION



$$\sigma_{tot}(VA) = \int \left[1 - \exp \left(-\sigma_{tot}(Vp) T_A(\vec{b}) \right) \right] d^2 b$$

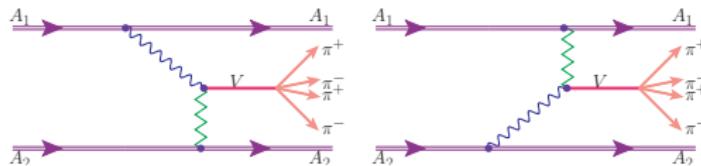
$$T_A(\vec{b}) = \int_{-\infty}^{+\infty} \rho(\vec{b}, z) dz$$

$$\sigma(\gamma A \rightarrow VA) =$$

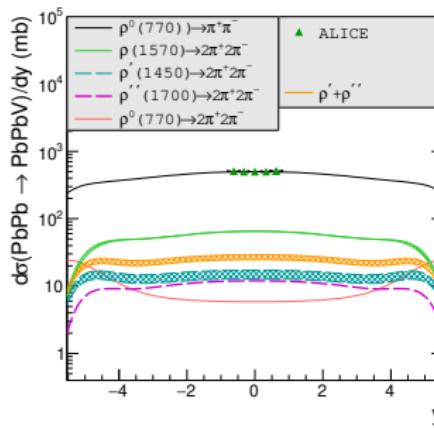
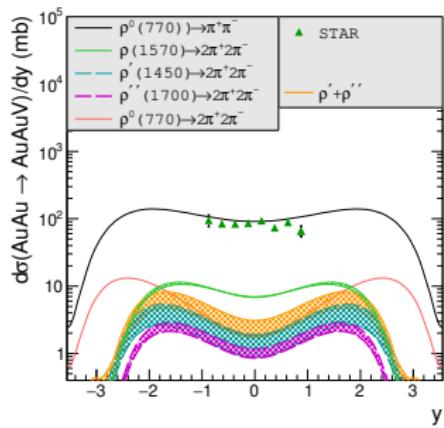
$$\frac{1}{16\pi} \frac{e^2}{f_V^2} \sigma_{tot}^2(VA) \int |F(t)|^2 dt$$

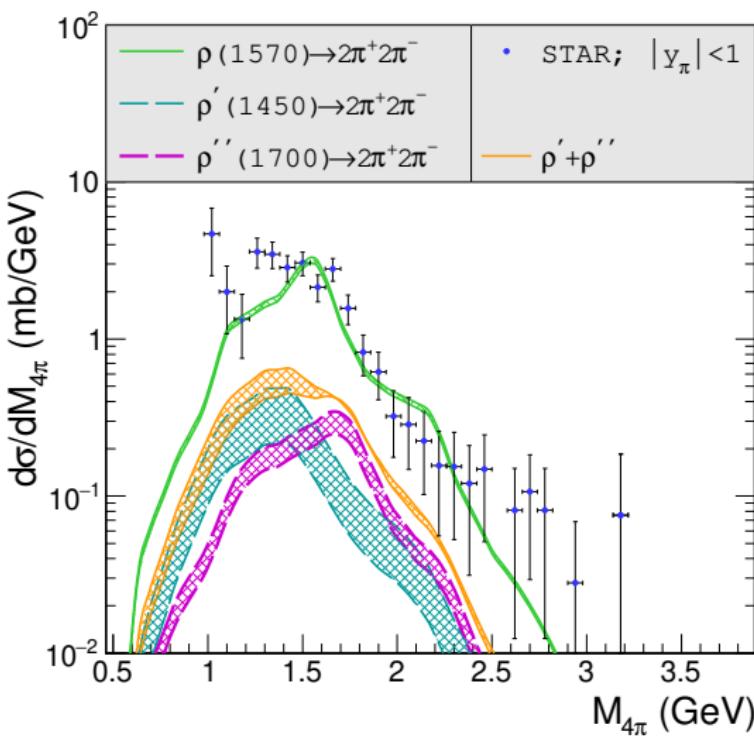
$$F(\mathbf{q}^2) = \frac{4\pi}{|\mathbf{q}|} \int \rho(r) \sin(|\mathbf{q}| r) r dr$$

DIFFERENTIAL CROSS SECTION



$$\frac{\sigma(A_1 A_2 \rightarrow A_1 A_2 2\pi^+ 2\pi^-)}{dy_V} = d^2 b \times \left[\int \omega_1 \frac{dN(\omega_1, b)}{d^2 b d\omega_1} \sigma_{\gamma A_2 \rightarrow V A_2} (W_{\gamma A_2}) \right. \\ \left. + \int \omega_2 \frac{dN(\omega_2, b)}{d^2 b d\omega_2} \sigma_{\gamma A_1 \rightarrow V A_1} (W_{\gamma A_1}) \right]$$

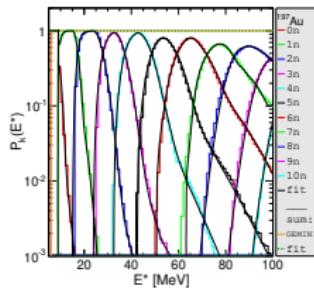




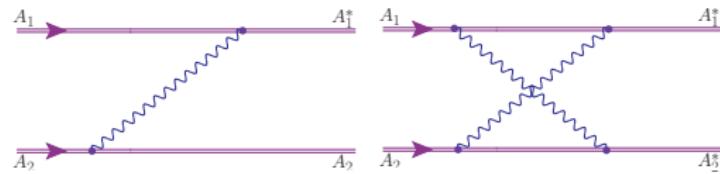
Success of $\rho(1570)$ for STAR. New ALICE-LHC data!

ELECTROMAGNETIC EXCITATION

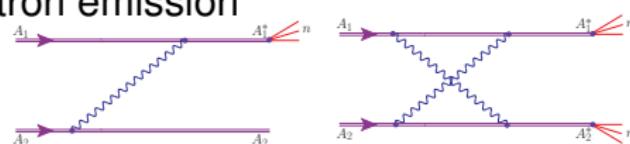
$P_k(E^*)$



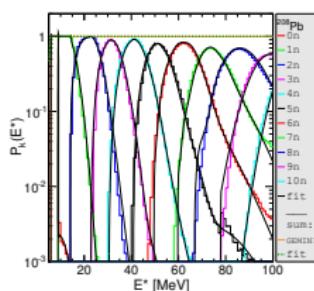
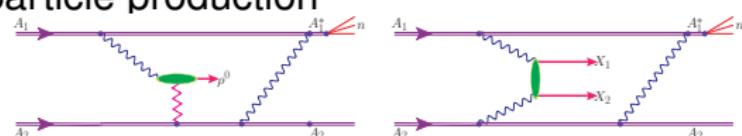
► Photon → nucleus excitation

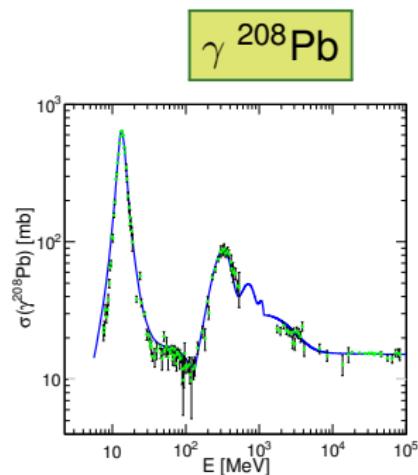
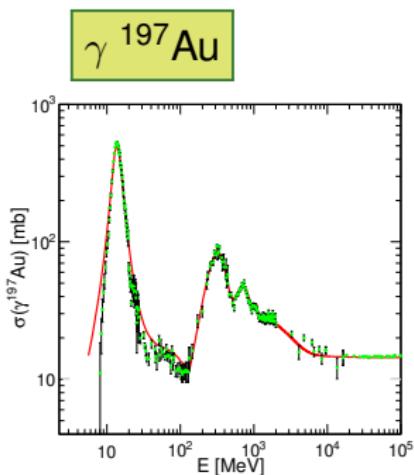


+ neutron emission



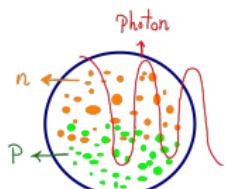
+ particle production



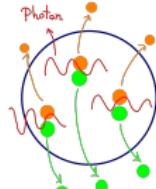


$$\sigma_\gamma A = \sigma_{\text{GDR}} + \sigma_{\text{QD}} + \sigma_{\text{nucleon res.}} + \sigma_{\text{nucleon cont.}}$$

- ① Giant Dipole Resonance
 $E_\gamma < 40 \text{ MeV}$



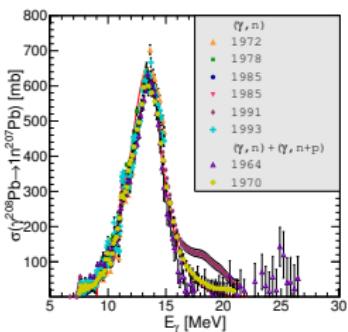
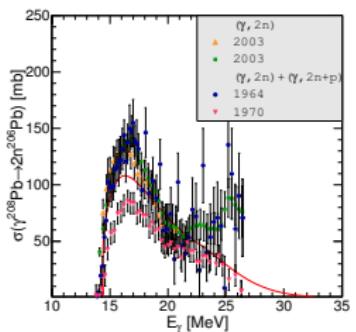
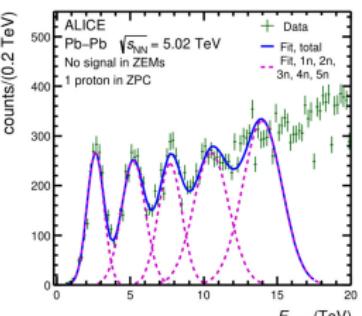
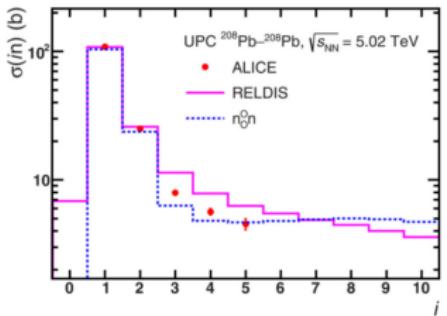
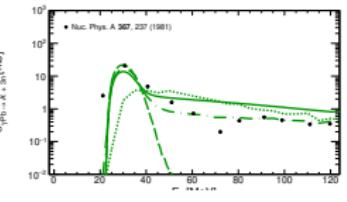
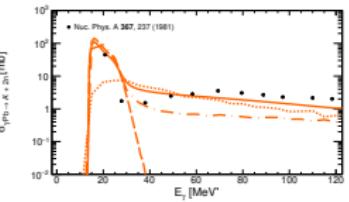
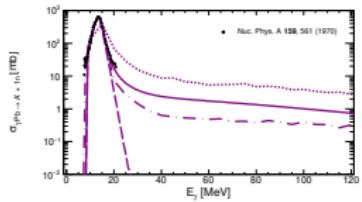
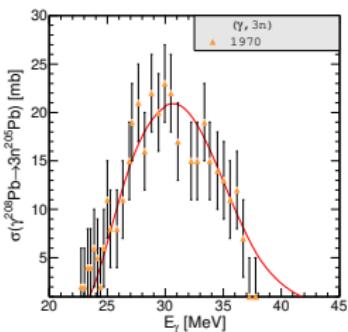
- ② quasi-deuteron contribution
 $E_\gamma = (40 - 100) \text{ MeV}$



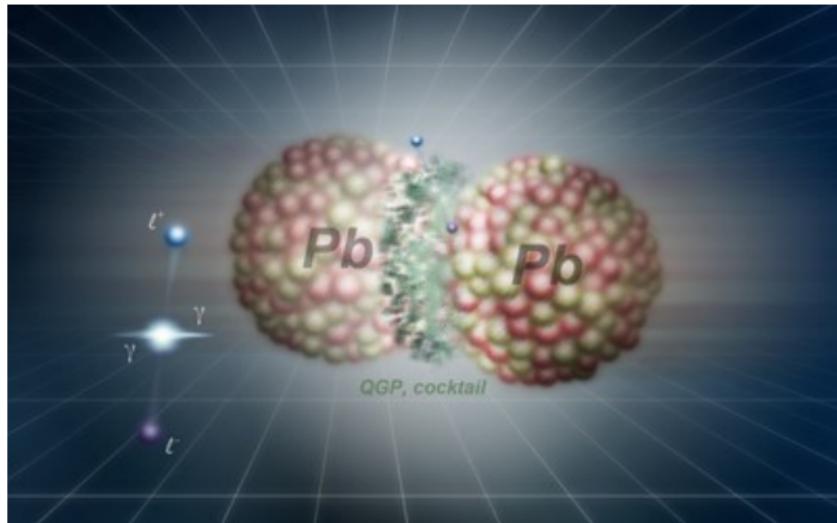
- ③ nucleon resonances
 $E_\gamma = (0.1 - 1) \text{ GeV}$



- ④ break-up of nucleons
 $E_\gamma > 1 - 8 \text{ GeV}$

$\gamma^{208}\text{Pb} \rightarrow 1n^{207}\text{Pb}$  $\gamma^{208}\text{Pb} \rightarrow 2n^{206}\text{Pb}$  $\gamma^{208}\text{Pb} \rightarrow 3n^{205}\text{Pb}$ 

SEMICENTRAL HEAVY-ION COLLISIONS



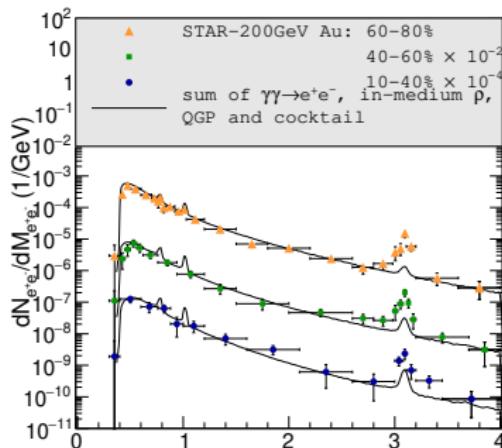
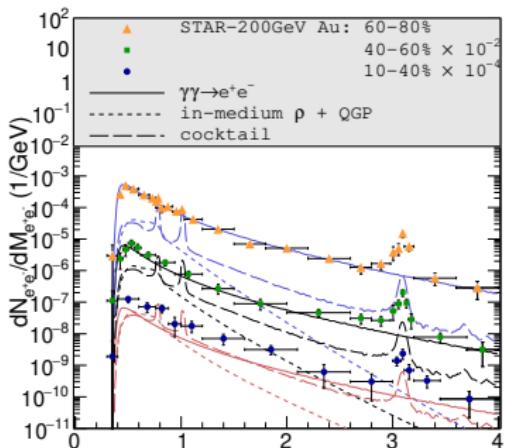
- From ultraperipheral to semicentral collisions → dilepton sources
 - $\gamma\gamma$ fusion mechanism
- Invariant mass
 - SPS (NA60 data)
 - RHIC (STAR data)
 - LHC (ALICE data)
- Low- P_T dilepton spectra
 - RHIC (STAR data)
 - LHC (ALICE data)
- Acoplanarity
 - LHC (ATLAS data)

DIELECTRON INVARIANT-MASS SPECTRA - RHIC

 $p_t > 0.2 \text{ GeV}$ $|\eta_e| < 1$ $|y_{e^+ e^-}| < 1$

- ✓ $\gamma\gamma$ -fusion
- ✓ thermal radiation
- ✓ hadronic cocktail

3 centrality classes



The coherent emission dominates for the two peripheral samples

and is comparable to the cocktail and thermal radiation yields in semi-central collisions.

EPA in the impact parameter space - the pair transverse momentum $P_T^{\ell^+\ell^-}$ is neglected

$$\sigma_{A_1 A_2 \rightarrow A_1 A_2 \ell^+ \ell^-} = \int N(\omega_1, \mathbf{b}_1) N(\omega_2, \mathbf{b}_2) \delta^{(2)}(\mathbf{b} - \mathbf{b}_1 - \mathbf{b}_2) \int d^2 \mathbf{b}_1 d^2 \mathbf{b}_2 d^2 \mathbf{b} dy_{\ell^+} dy_{\ell^-} dp_{t,\ell}^2 \frac{d\sigma(\gamma\gamma \rightarrow \ell^+ \ell^-; \hat{s})}{d(-\hat{t})}$$

⇒ k_t -factorization

$$\frac{dN_{II}}{d^2 \mathbf{P}_T^{\ell^+ \ell^-}} = \int \frac{d\omega_1}{\omega_1} \frac{d\omega_2}{\omega_2} d^2 \mathbf{q}_{1t} d^2 \mathbf{q}_{2t} \frac{dN(\omega_1, q_{1t}^2)}{d^2 \mathbf{q}_{1t}} \frac{dN(\omega_2, q_{2t}^2)}{d^2 \mathbf{q}_{2t}} \delta^{(2)}(\mathbf{q}_{1t} + \mathbf{q}_{2t} - \mathbf{P}_T^{\ell^+ \ell^-}) \hat{\sigma}(\gamma\gamma \rightarrow \ell^+ \ell^-) \Big|_{\text{cuts}},$$

⇒ Exact calculation

$$\begin{aligned} \frac{d\sigma[C]}{d^2 \mathbf{P}_T^{\ell^+ \ell^-}} &= \int \frac{d^2 \mathbf{Q}}{2\pi} w(Q; b_{\max}, b_{\min}) \int \frac{d^2 \mathbf{q}_1}{\pi} \frac{d^2 \mathbf{q}_2}{\pi} \delta^{(2)}(\mathbf{P}_T^{\ell^+ \ell^-} - \mathbf{q}_1 - \mathbf{q}_2) \int \frac{d\omega_1}{\omega_1} \frac{d\omega_2}{\omega_2} \\ &\times E_i\left(\omega_1, \mathbf{q}_1 + \frac{\mathbf{Q}}{2}\right) E_j^*\left(\omega_1, \mathbf{q}_1 - \frac{\mathbf{Q}}{2}\right) E_k\left(\omega_2, \mathbf{q}_2 - \frac{\mathbf{Q}}{2}\right) E_l^*\left(\omega_2, \mathbf{q}_2 + \frac{\mathbf{Q}}{2}\right) \frac{1}{2\hat{s}} \sum_{\lambda \bar{\lambda}} M_{ik}^{\lambda \bar{\lambda}} M_{jl}^{\lambda \bar{\lambda} \dagger} d\Phi(\ell^+ \ell^-). \end{aligned}$$

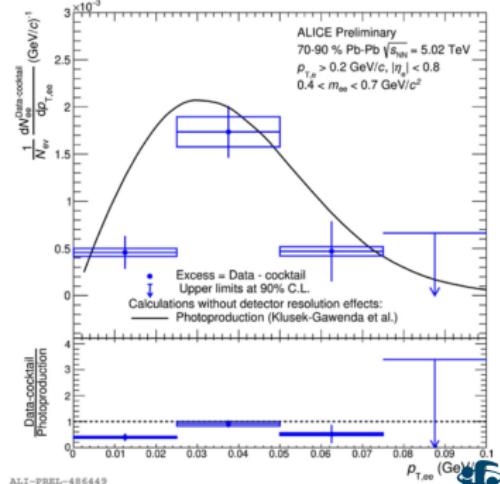
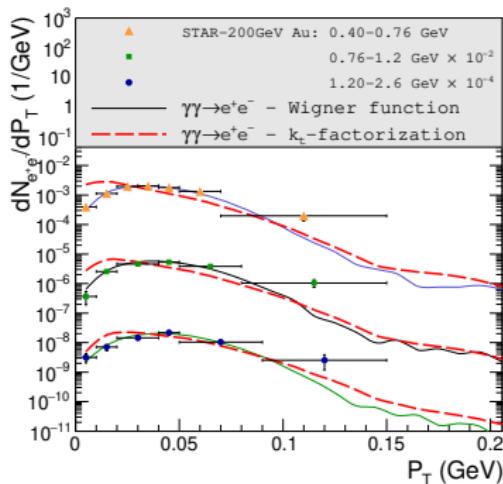
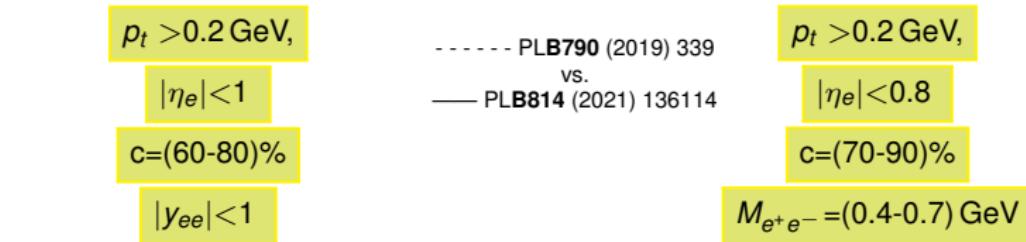
The factorization formula is written in terms of the Wigner function:

$$N_{ij}(\omega, \mathbf{b}, \mathbf{q}) = \int \frac{d^2 \mathbf{Q}}{(2\pi)^2} \exp[-i\mathbf{b}\mathbf{Q}] E_i\left(\omega, \mathbf{q} + \frac{\mathbf{Q}}{2}\right) E_j^*\left(\omega, \mathbf{q} - \frac{\mathbf{Q}}{2}\right) = \int d^2 \mathbf{s} \exp[i\mathbf{qs}] E_i\left(\omega, \mathbf{b} + \frac{\mathbf{s}}{2}\right) E_j^*\left(\omega, \mathbf{b} - \frac{\mathbf{s}}{2}\right),$$

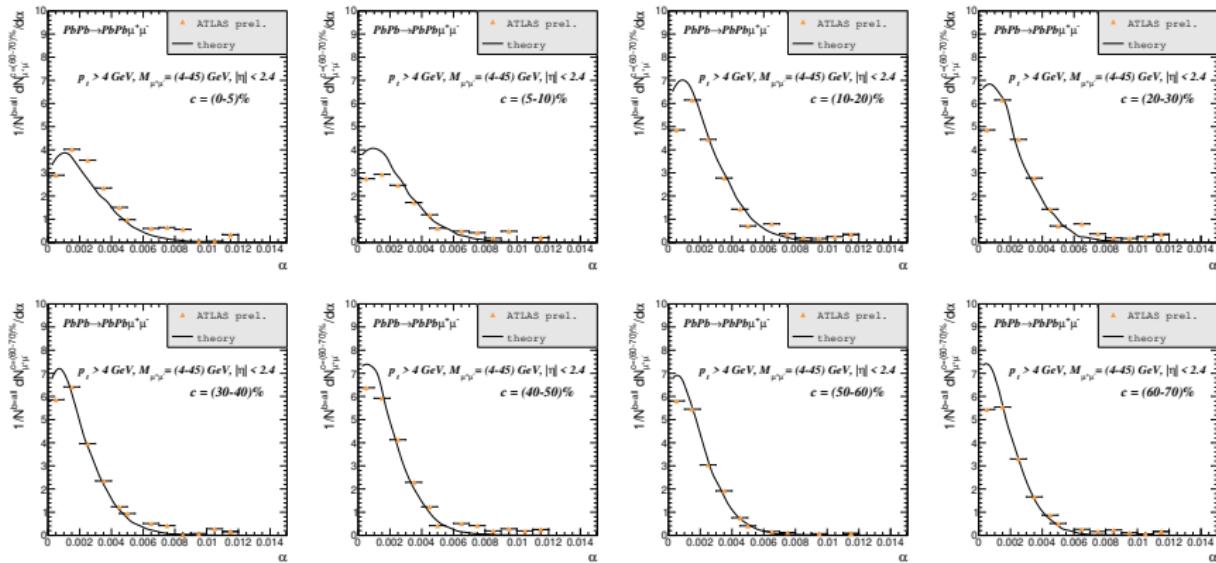
$$N(\omega, \mathbf{q}) = \delta_{ij} \int d^2 \mathbf{b} N_{ij}(\omega, \mathbf{b}, \mathbf{q}) = \delta_{ij} E_i(\omega, \mathbf{q}) E_j^*(\omega, \mathbf{q}) = |\mathbf{E}(\omega, \mathbf{q})|^2,$$

$$N(\omega, \mathbf{b}) = \delta_{ij} \int \frac{d^2 \mathbf{q}}{(2\pi)^2} N_{ij}(\omega, \mathbf{b}, \mathbf{q}) = \delta_{ij} E_i(\omega, \mathbf{b}) E_j^*(\omega, \mathbf{b}) = |\mathbf{E}(\omega, \mathbf{b})|^2.$$

PAIR TRANSVERSE MOMENTUM - RHIC & LHC



ACOPLANARITY - ATLAS DATA



A successful description of ATLAS data by $\gamma\gamma$ -fusion alone

A correct normalization and shape of the distributions

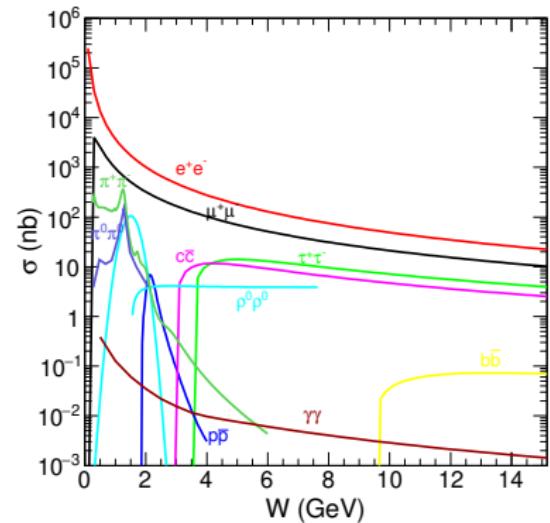
$p_t > 4 \text{ GeV},$

$M_{\mu^+\mu^-} = (4-45) \text{ GeV},$

$|\eta_\mu| < 2.4$

CONCLUSION

- EPA in the impact parameter space
- Fourier transform of the charge distribution
- Multidimensional integrals → differential cross section
- Description of experimental data for UPC
- Predictions include the experimental acceptance
- Electromagnetic excitation - ZDC
- Collaboration - theoreticians and experimenters
- Future:
 - more forward/backward region
 - lower p_t



Thank you