

Jets in heavy-ion collisions

24th Zimányi Winter Workshop, 3rd of December 2024



João Barata, CERN-TH

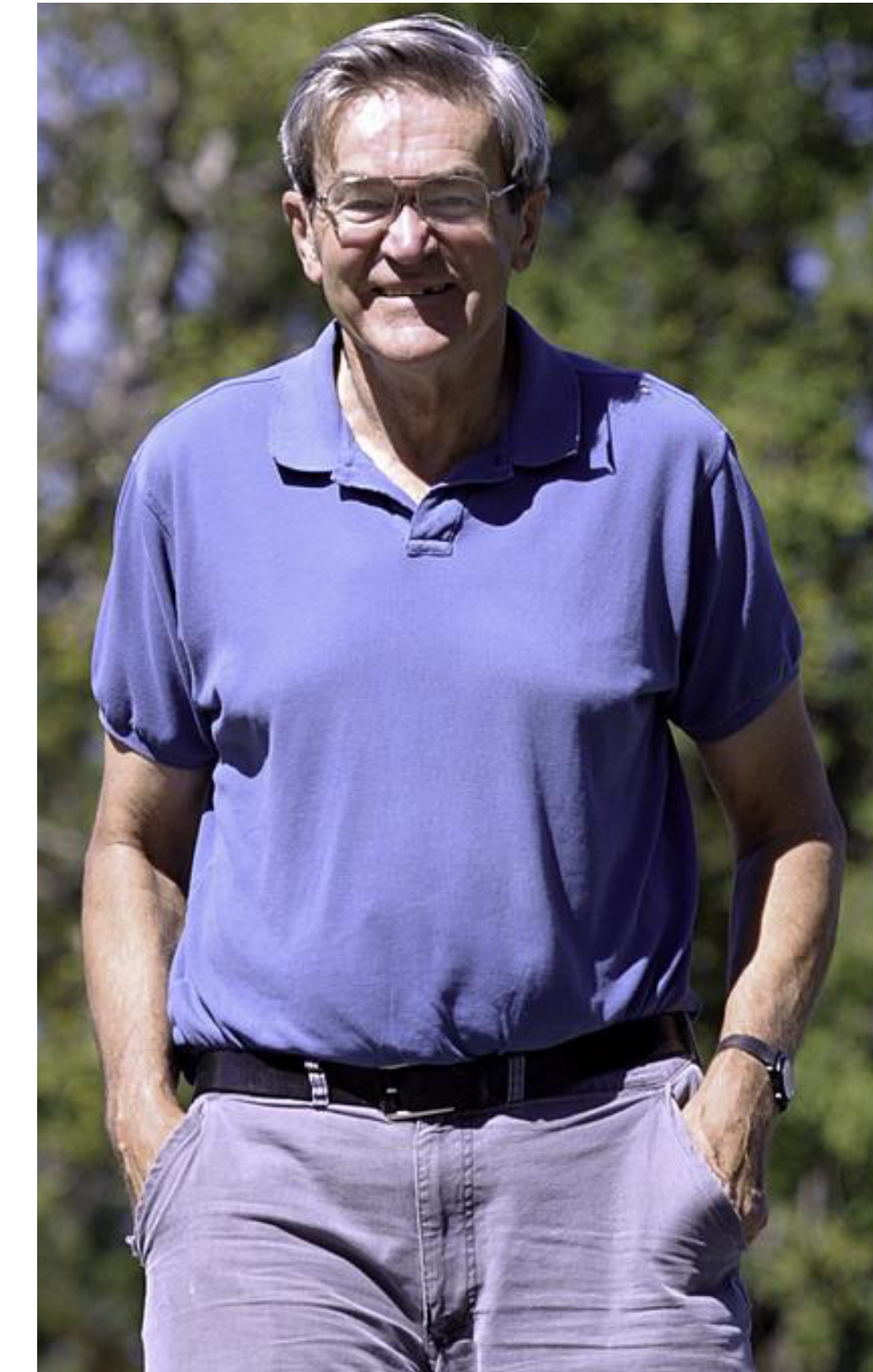
The origins: J. D. Bjorken



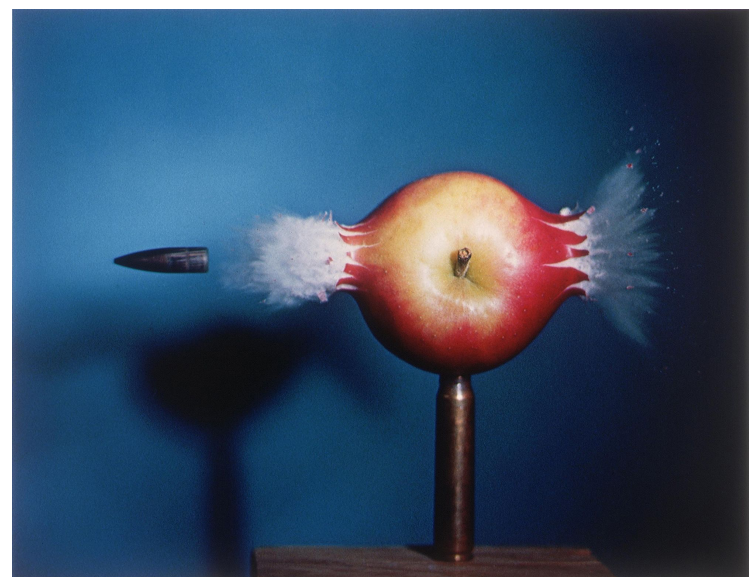
1982

Energy Loss of Energetic Partons in Quark-Gluon Plasma:
Possible Extinction of High p_T Jets in Hadron-Hadron Collisions.

J. D. BJORKEN
Fermi National Accelerator Laboratory
P.O. Box 500, Batavia, Illinois 60510

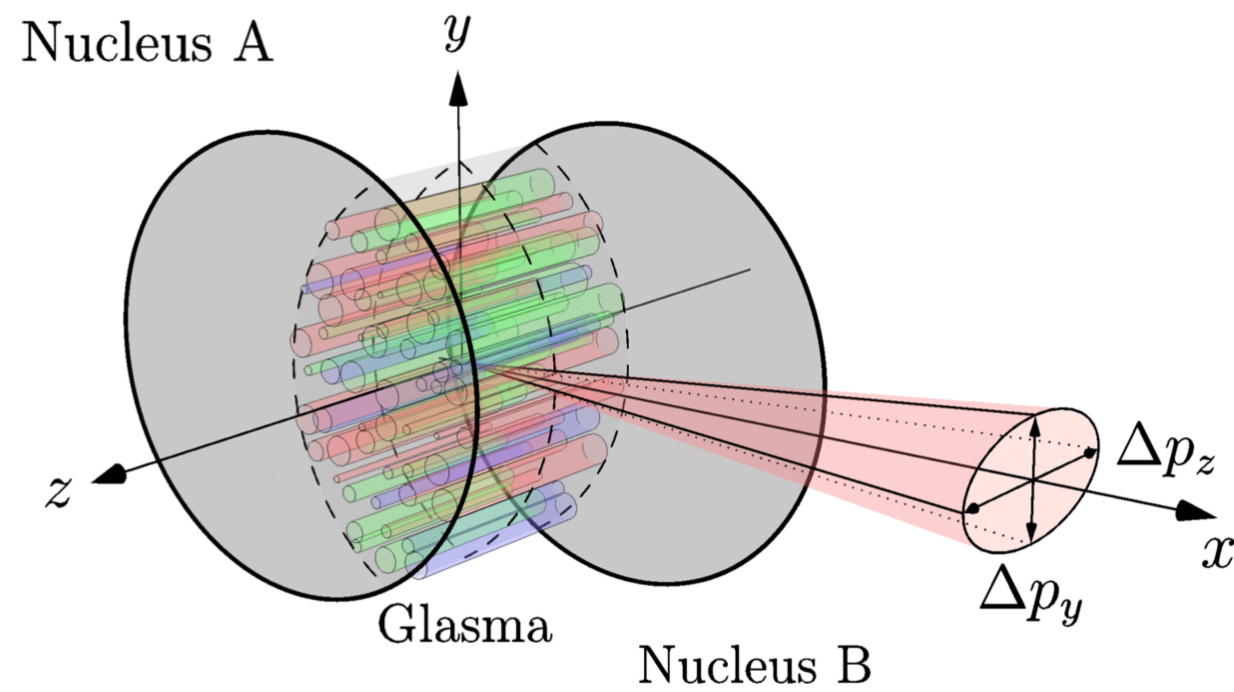
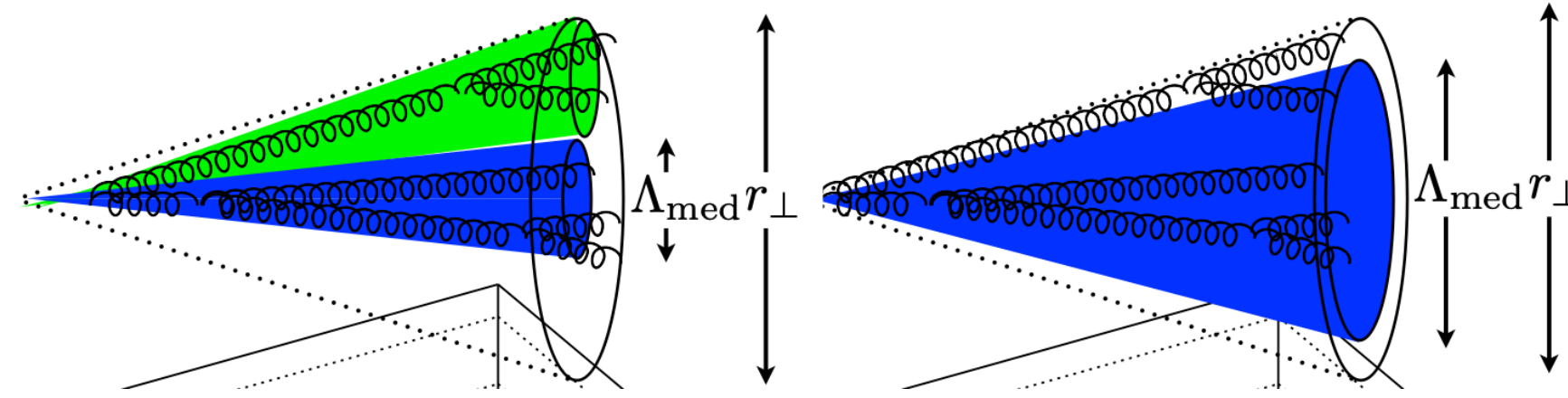
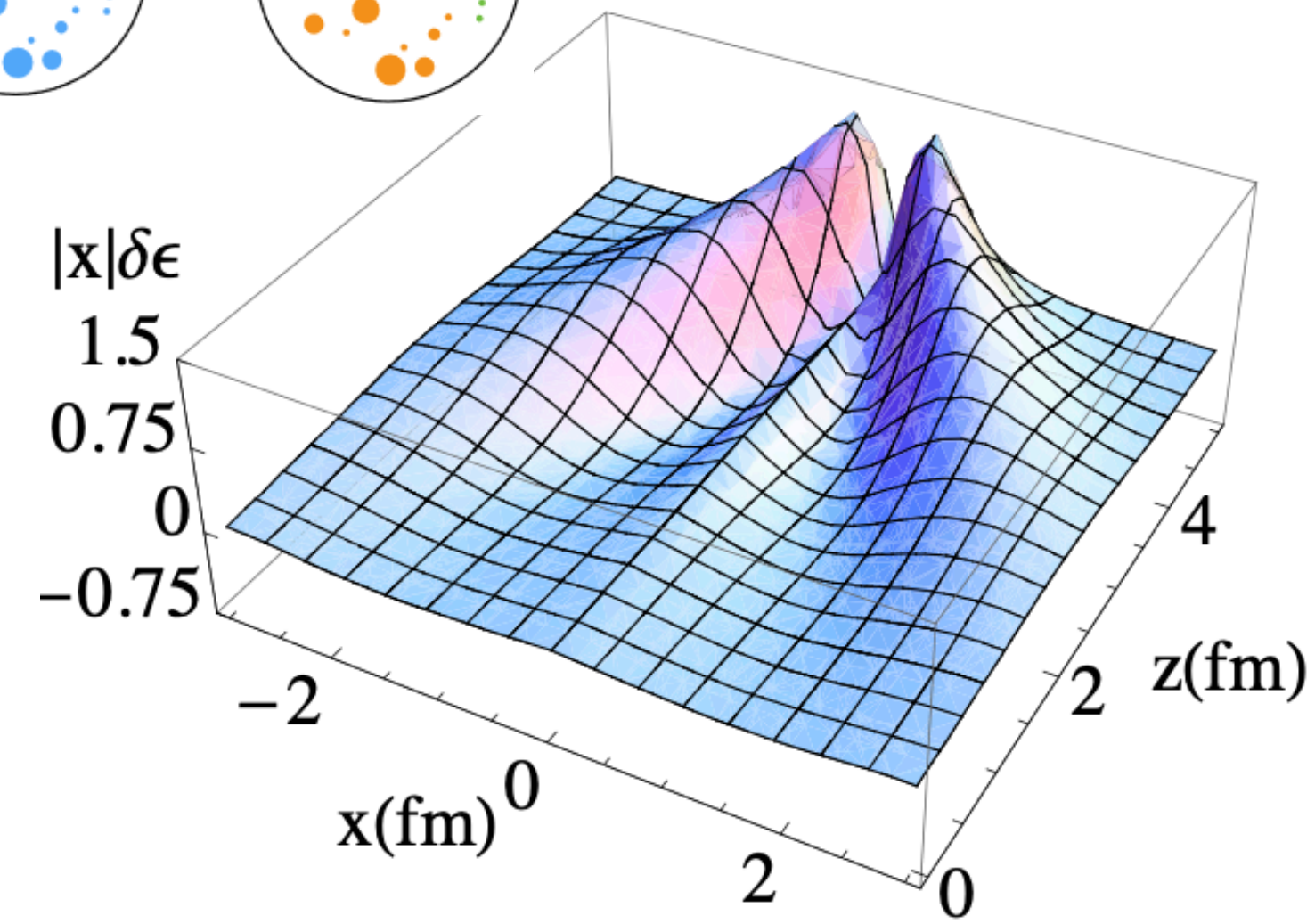
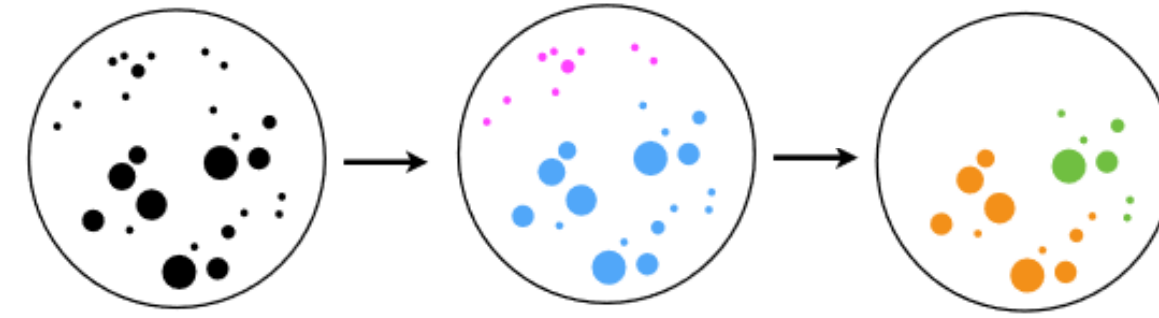
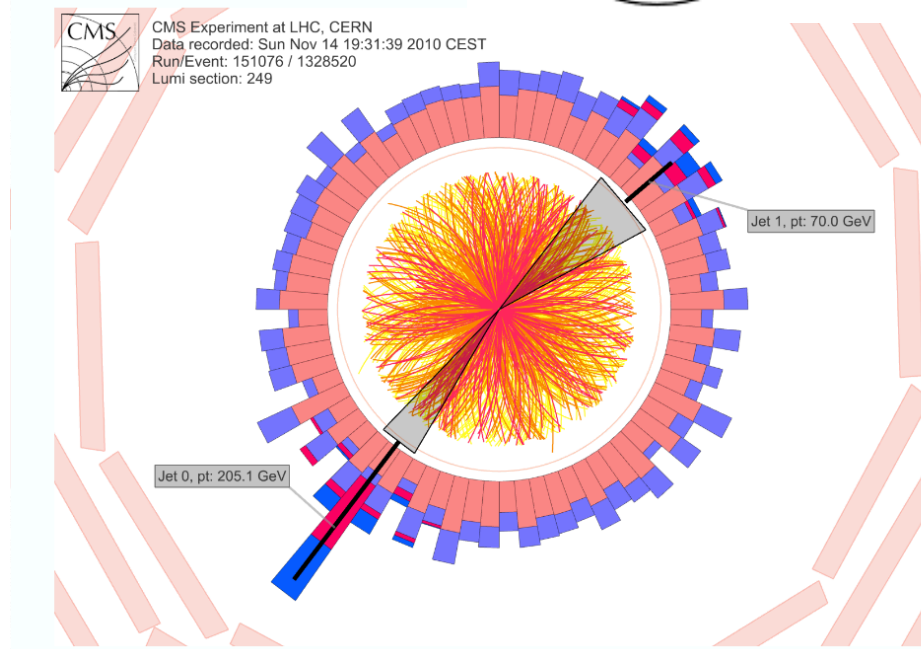
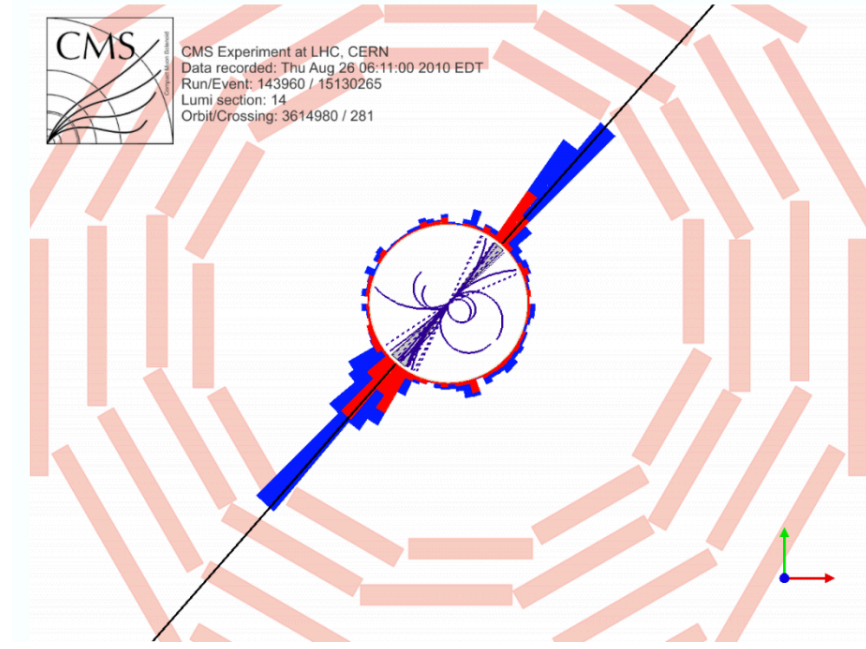
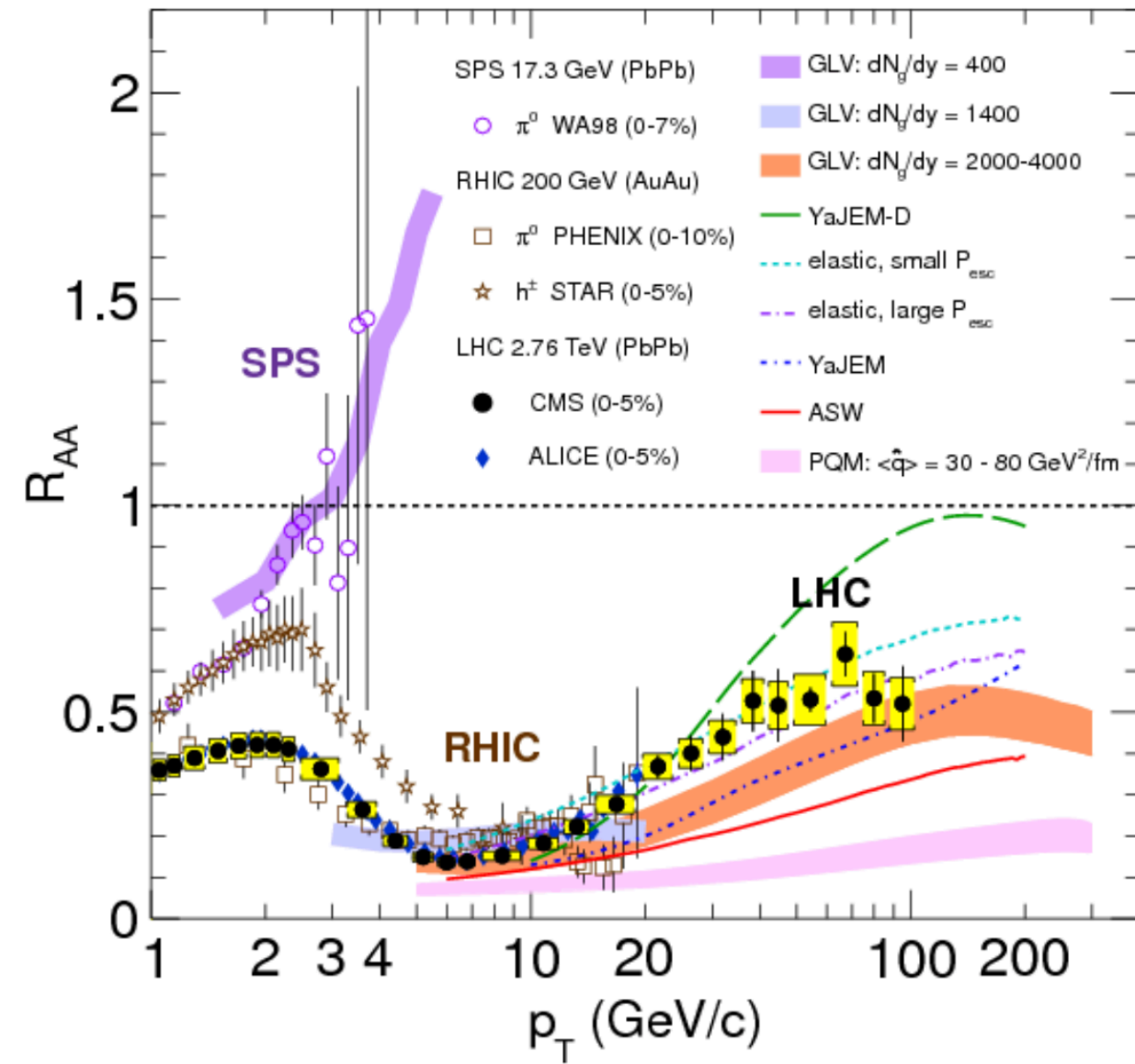


1934-2024



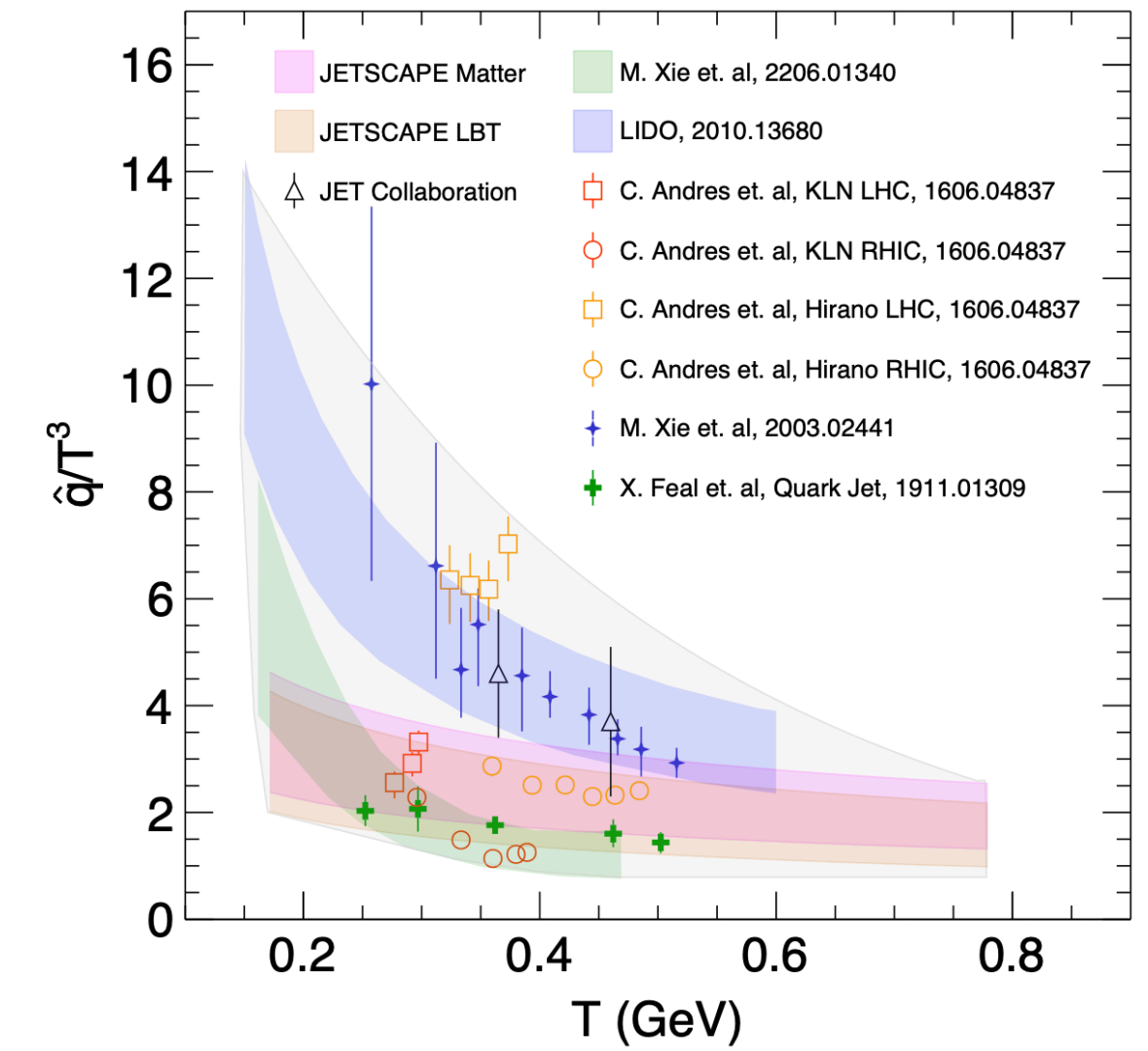
High energy quarks and gluons propagating through quark-gluon plasma suffer differential energy loss via elastic scattering from quanta in the plasma. This mechanism is very similar in structure to ionization loss of charged particles in ordinary matter.

Today: Much more than quarks and gluons



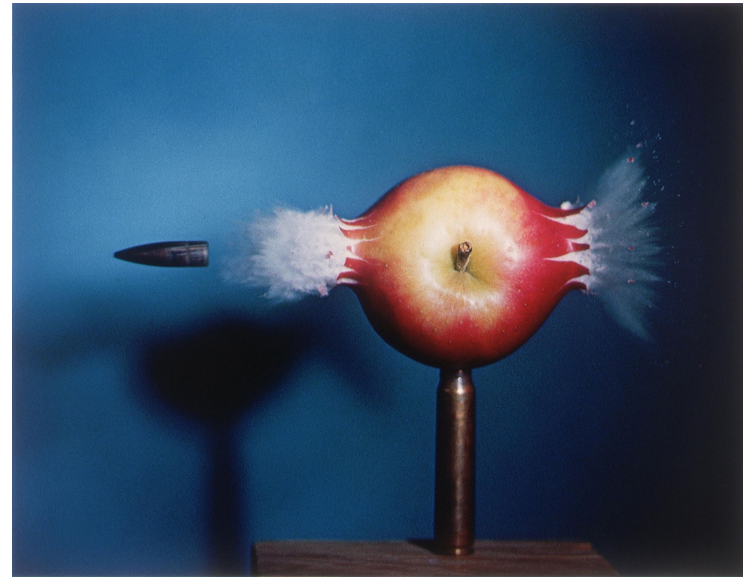
Many theoretical and experimental results !

Very active field in heavy ions collisions (HICs).

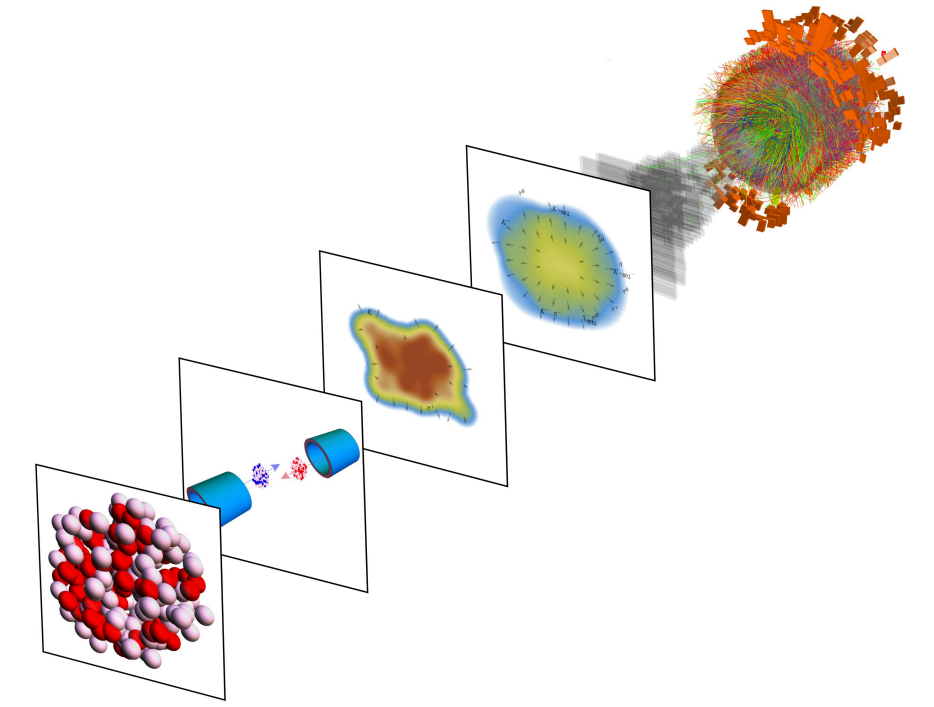


Quark and Gluon jets are the prime spacetime probes of HICs.

Outline

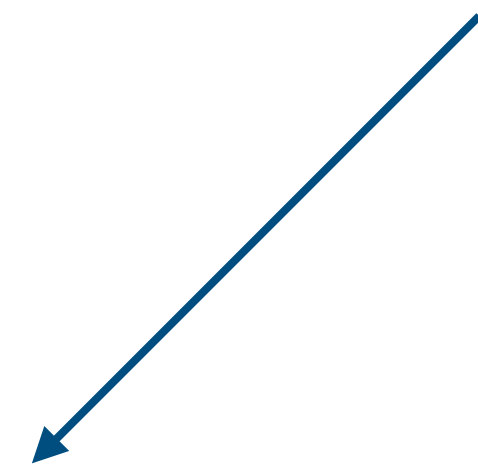
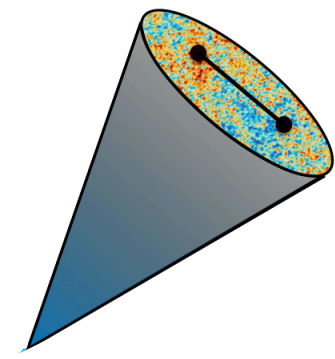


The general picture of jets in HICs



Recent theory developments

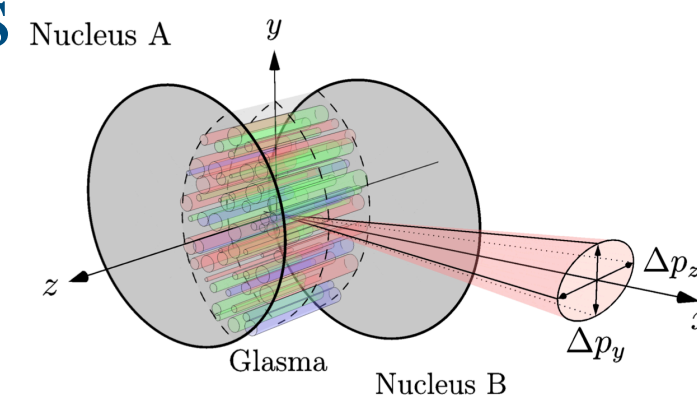
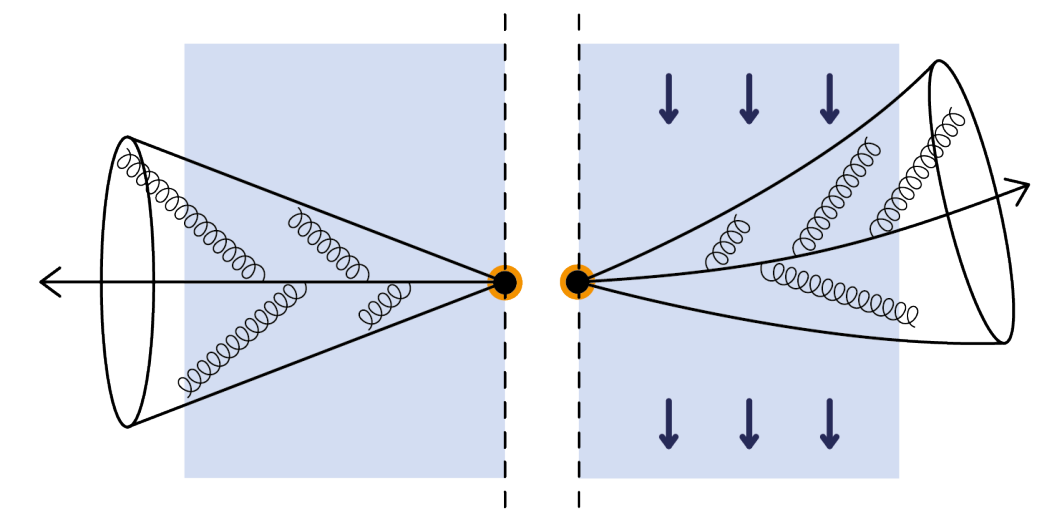
Jet substructure observables



Jets in the early stages of HICs



Jets in anisotropic and flowing matter





The general picture of jets in HICs

The spacetime picture of HICs

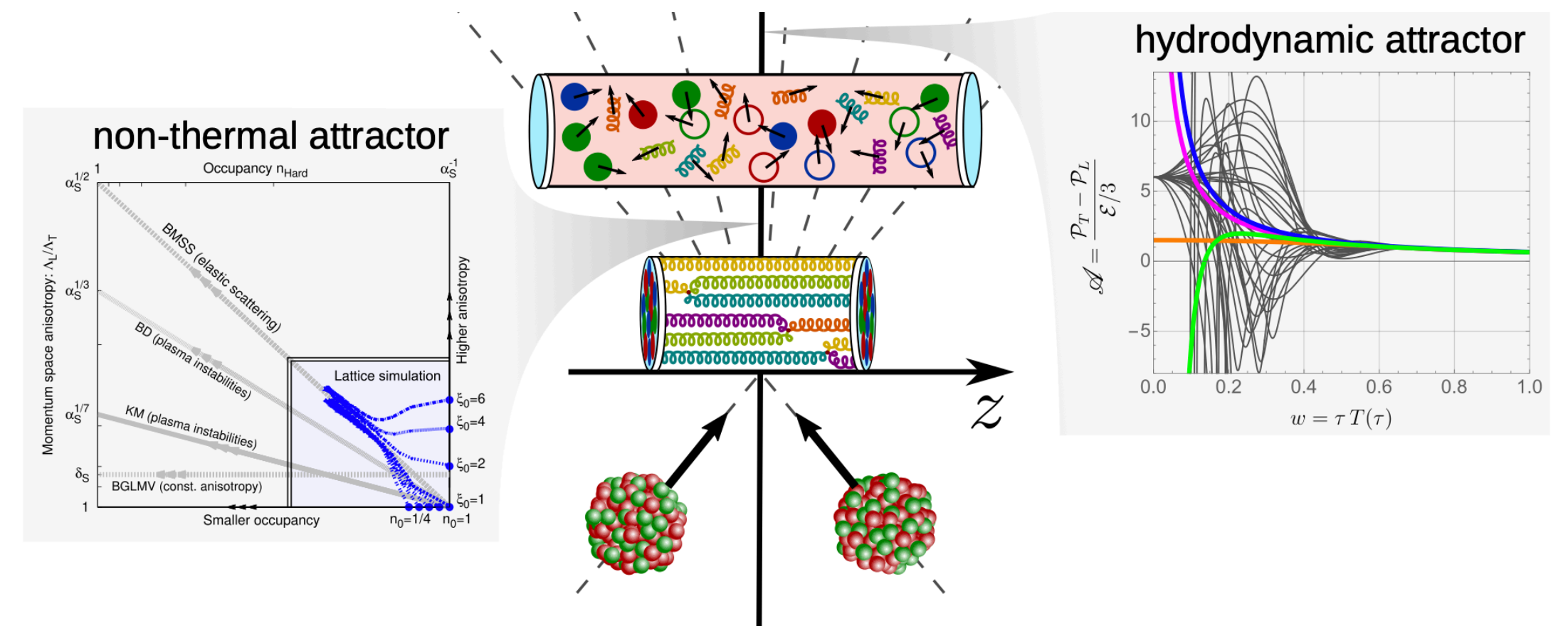
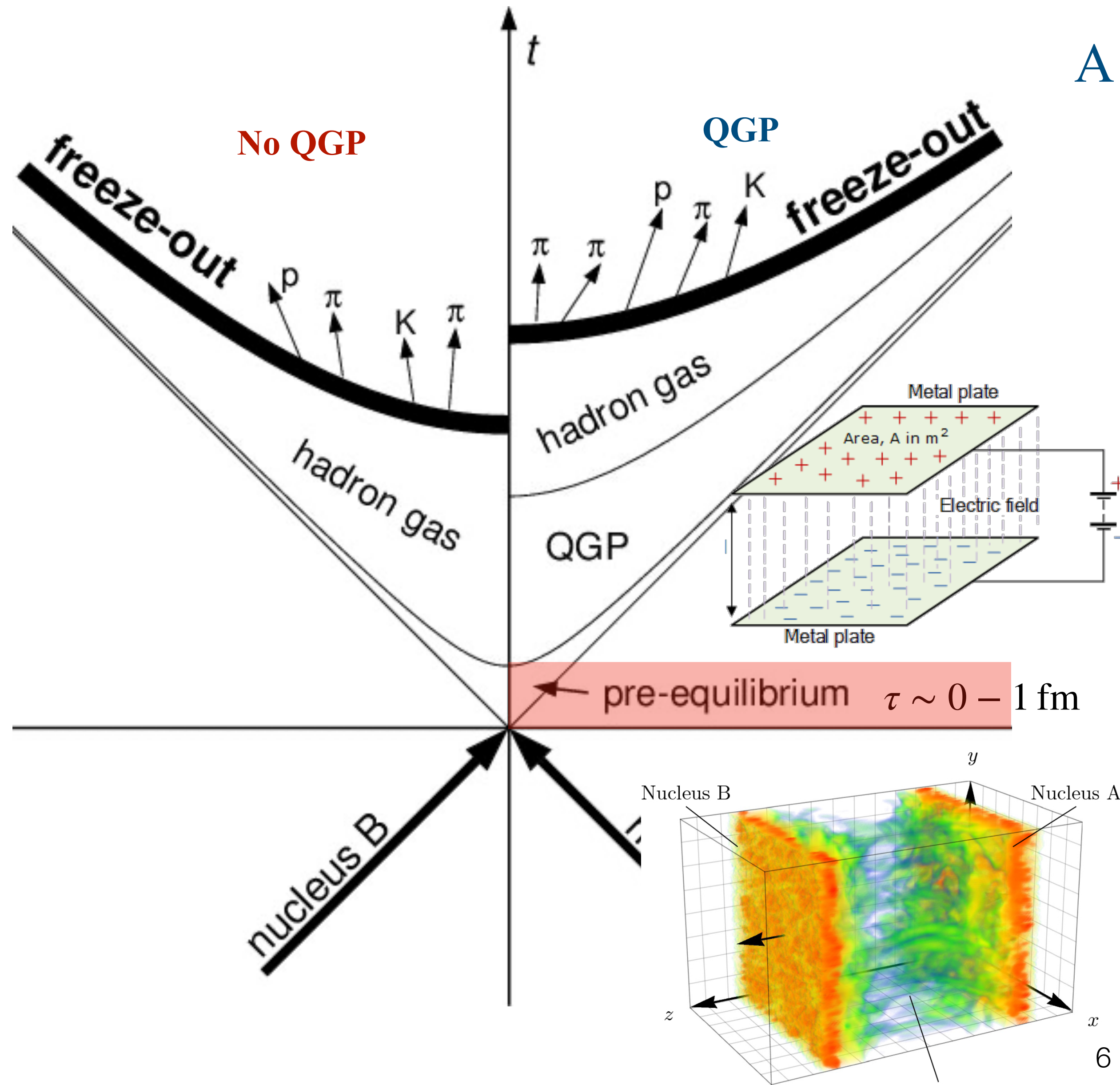


1 fm $\sim 10^{-24}$ s

A brief summary of the different epochs in HICs

Early times: Out of equilibrium matter (Glasma)

Short lived and dominated by classical configurations



[Berges, Heller, Mazeliauskas, Venugopalan, 2005.12299]

$$1 \text{ fm} \sim 10^{-24} \text{ s}$$

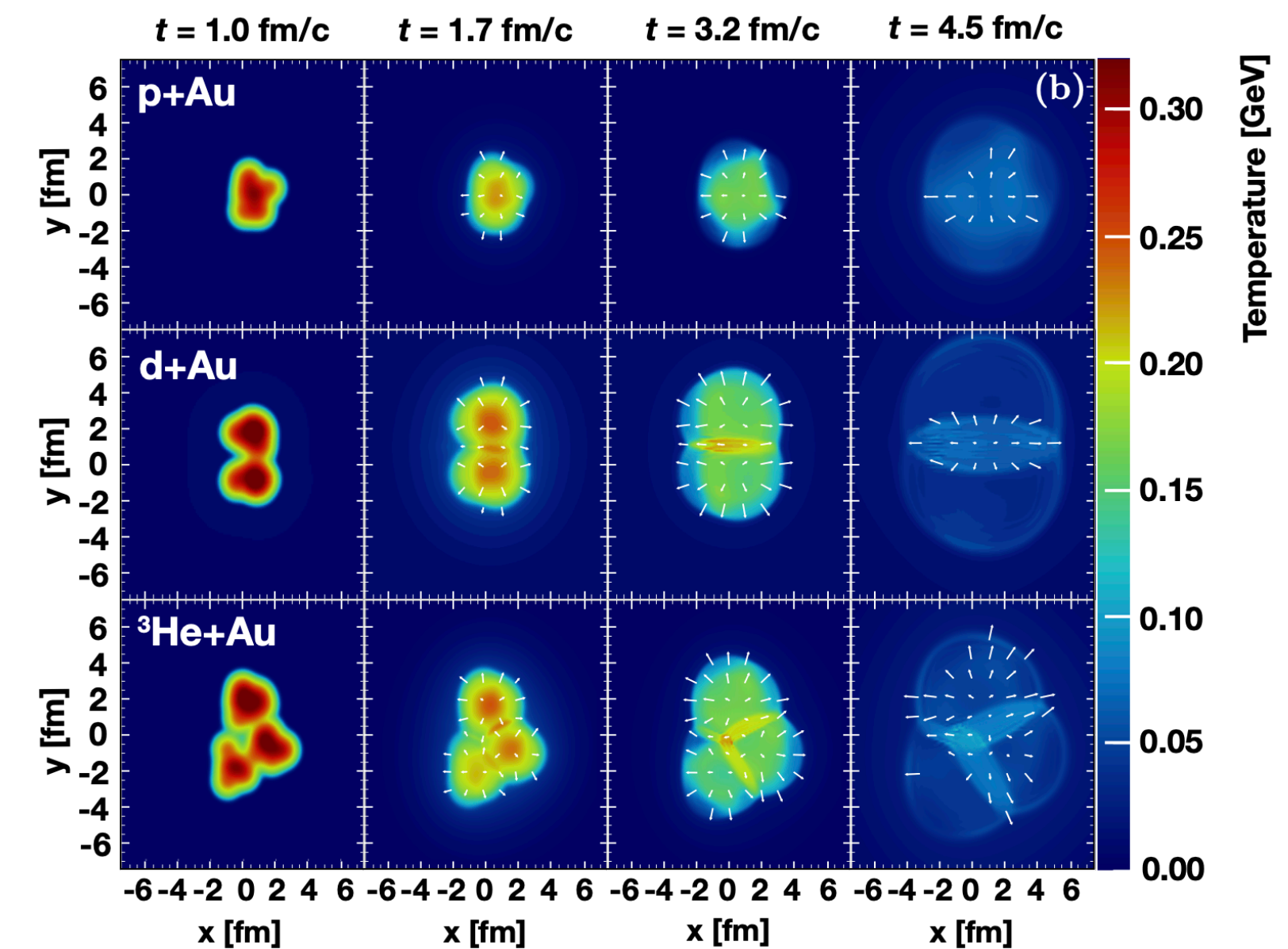
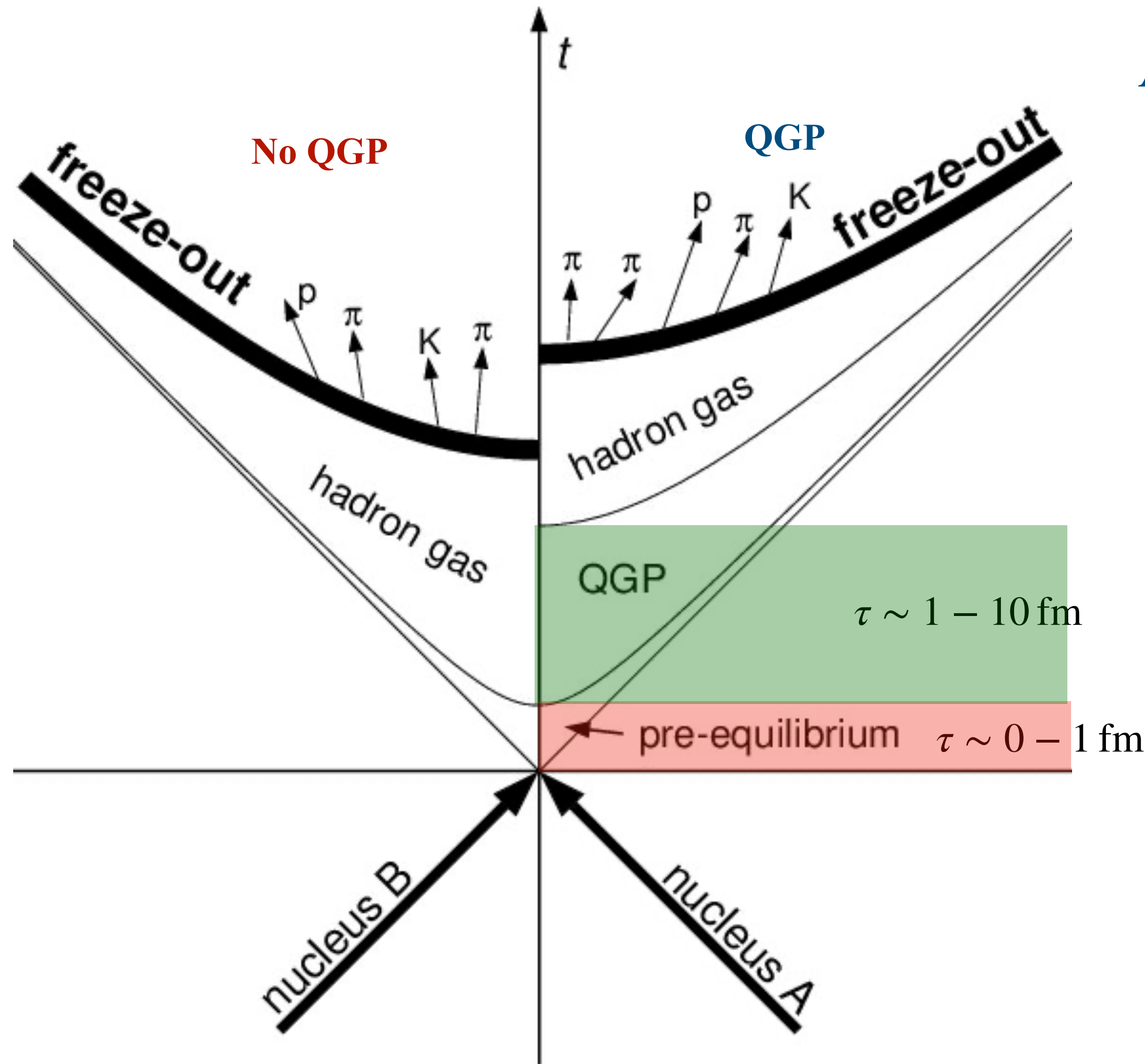
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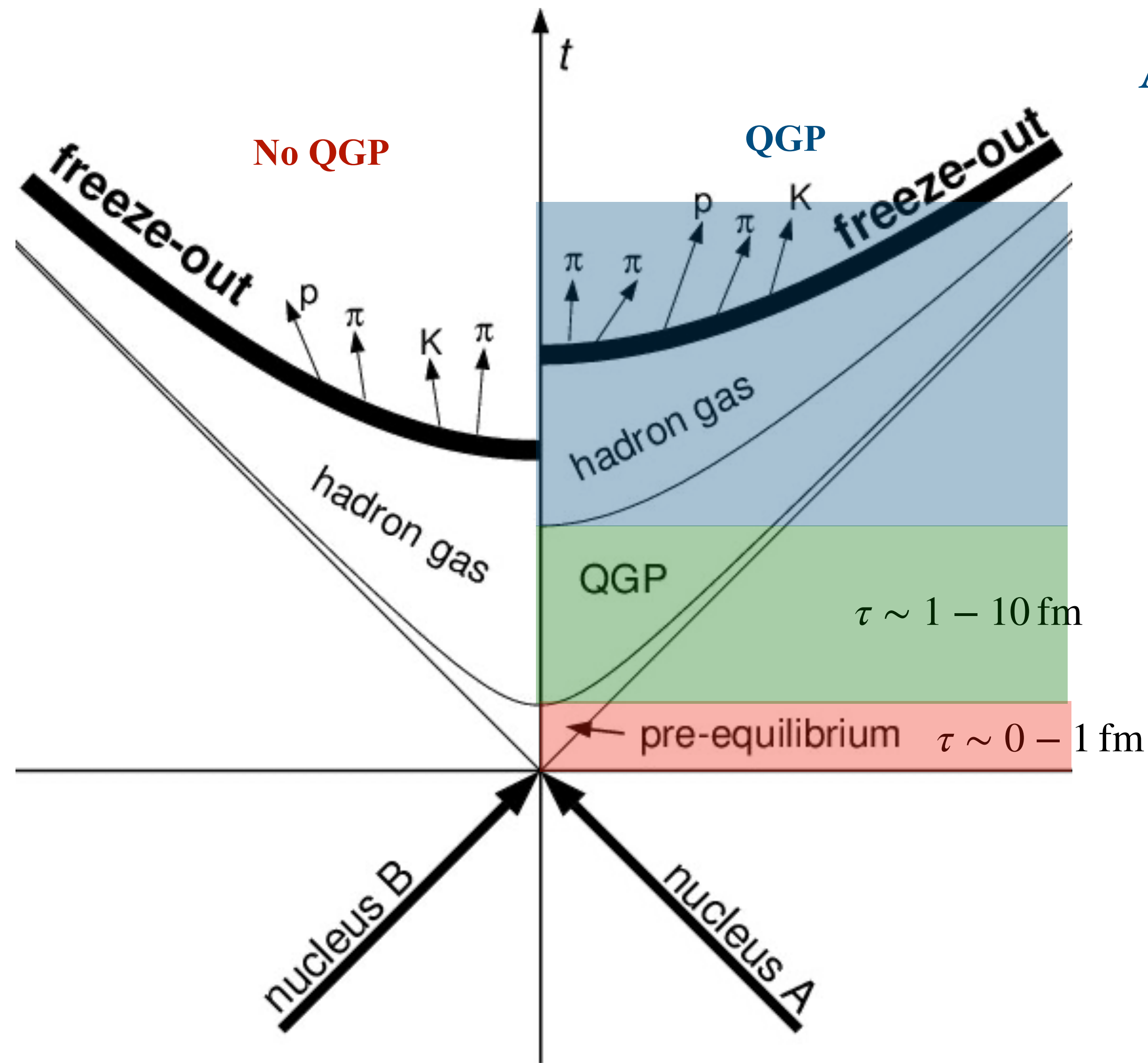
Intermediate times: Quark Gluon Plasma phase

Long lived, expanding hydro system where quarks and gluons are not confined inside hadrons



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A brief summary of the different epochs in HICs



Early times: Out of equilibrium matter (Glasma)

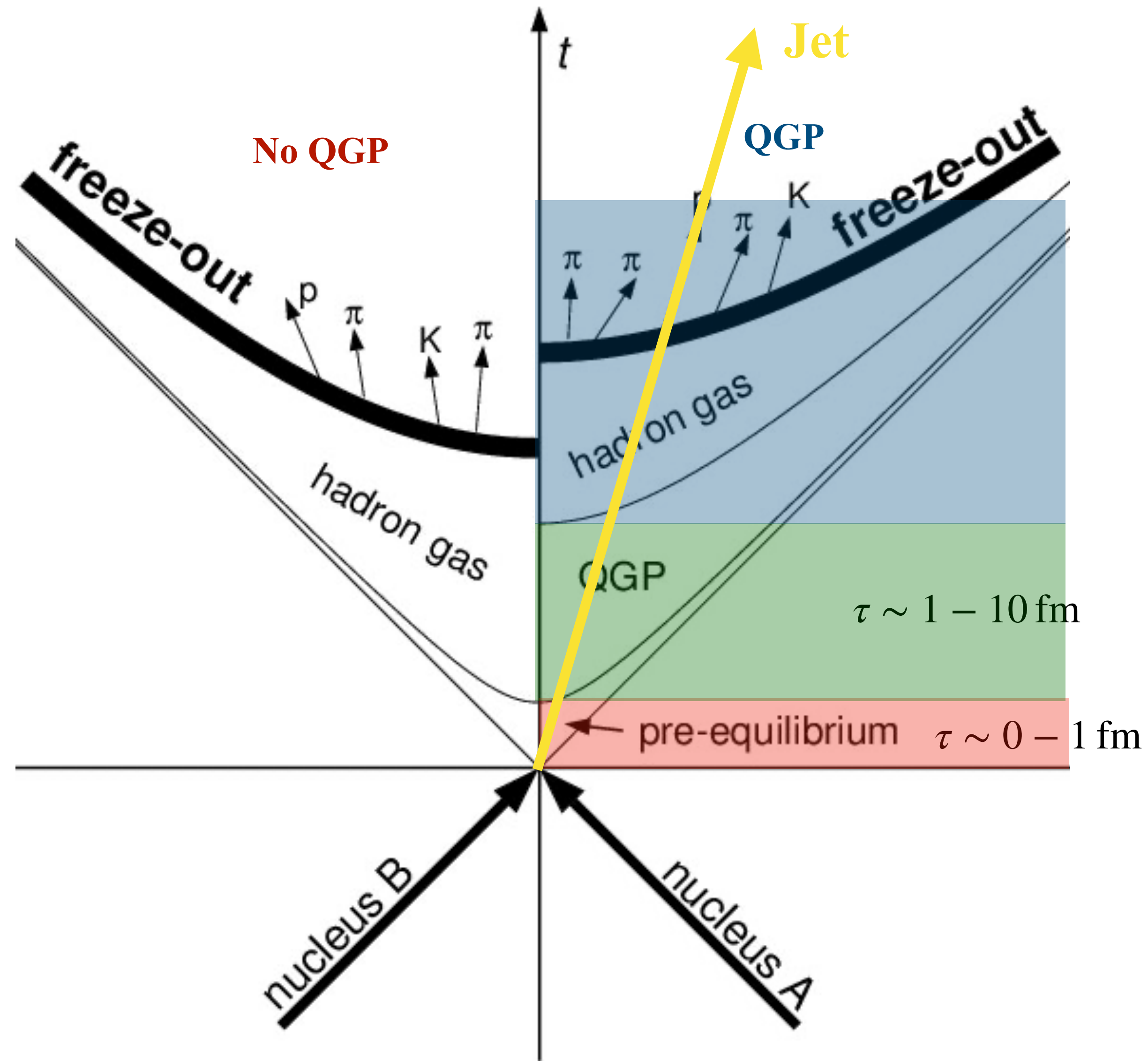
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Intermediate times: Quark Gluon Plasma phase

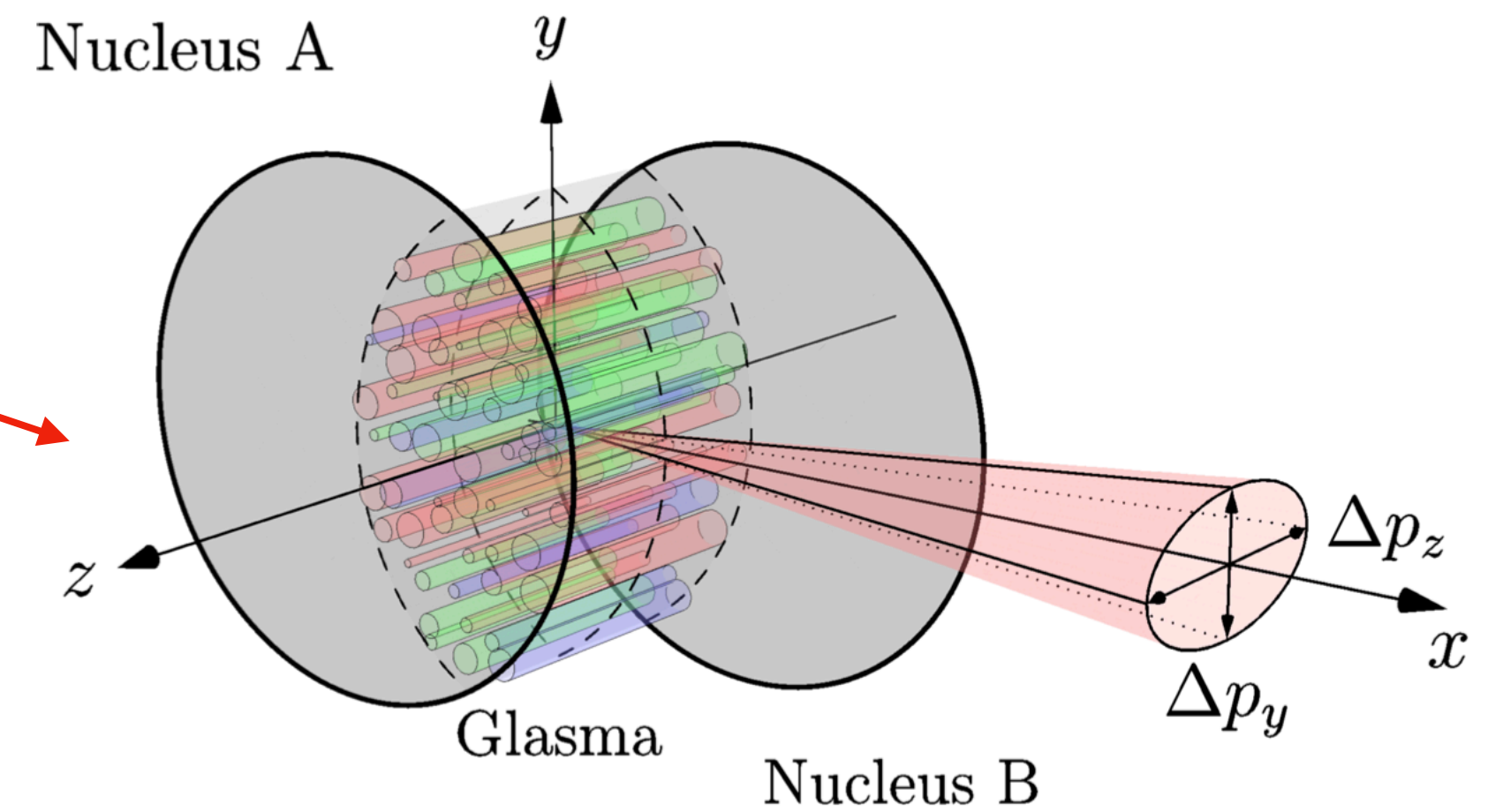
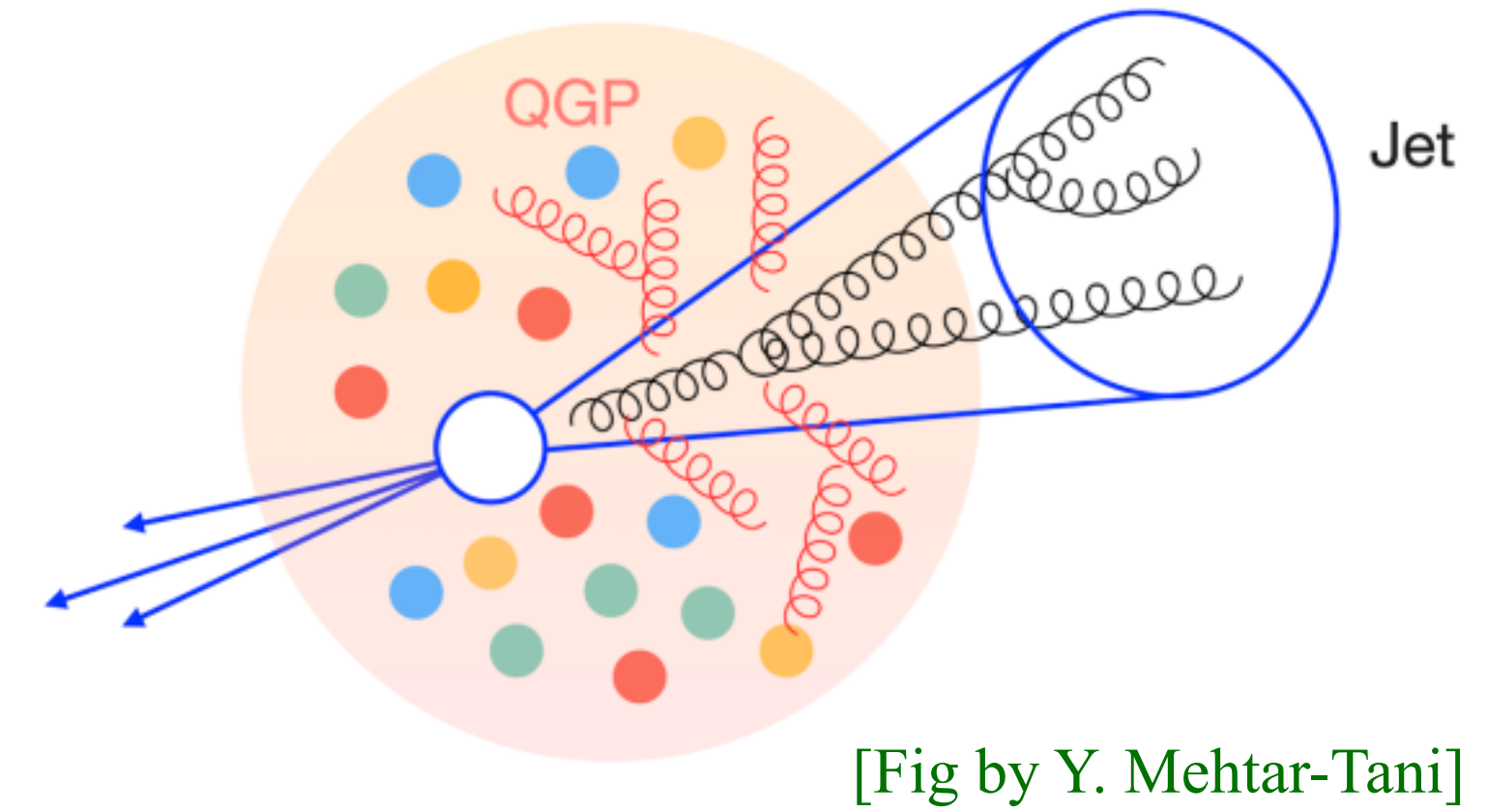
Long lived, expanding hydro system where quarks and gluons are not confined inside hadrons

Hadronic phase: Temperature below critical value

Gas of hadrons, which eventually free streams to the detectors

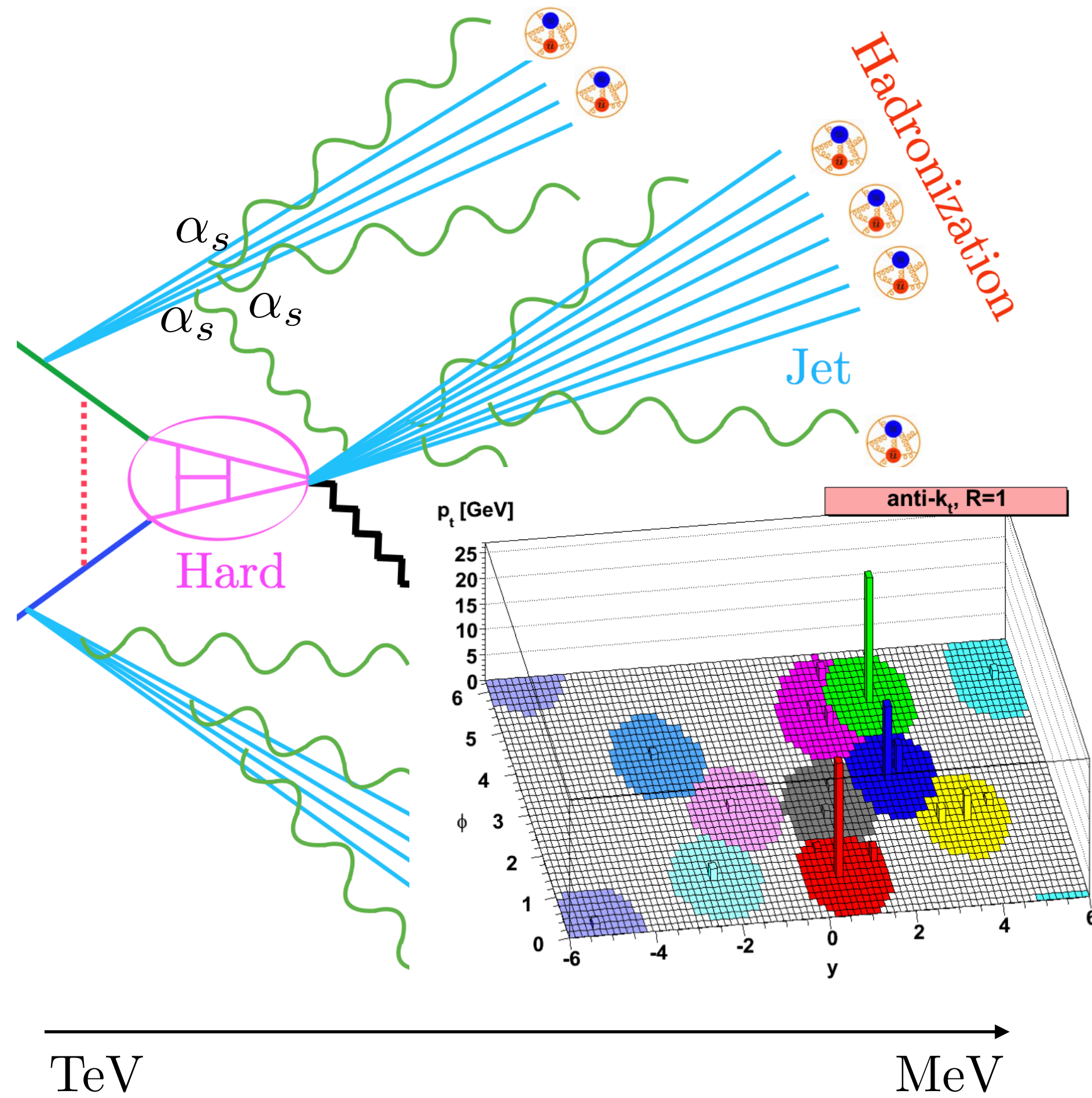


An ideal probe: QCD jets



[A. App, D. I. Muller, D. Schuh, 2009.14206]

In general, an event is decomposed as



The probability to branch takes the form

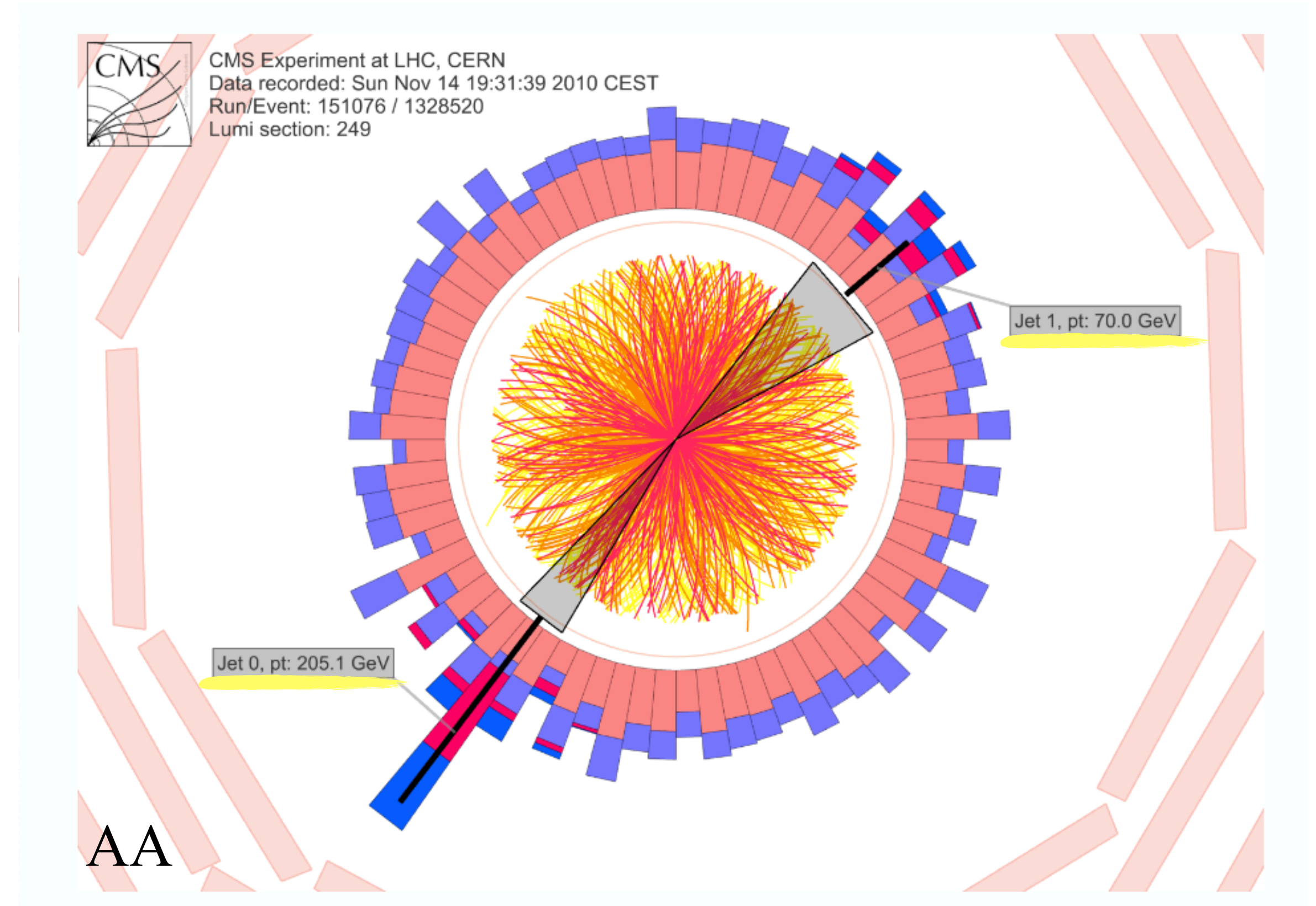
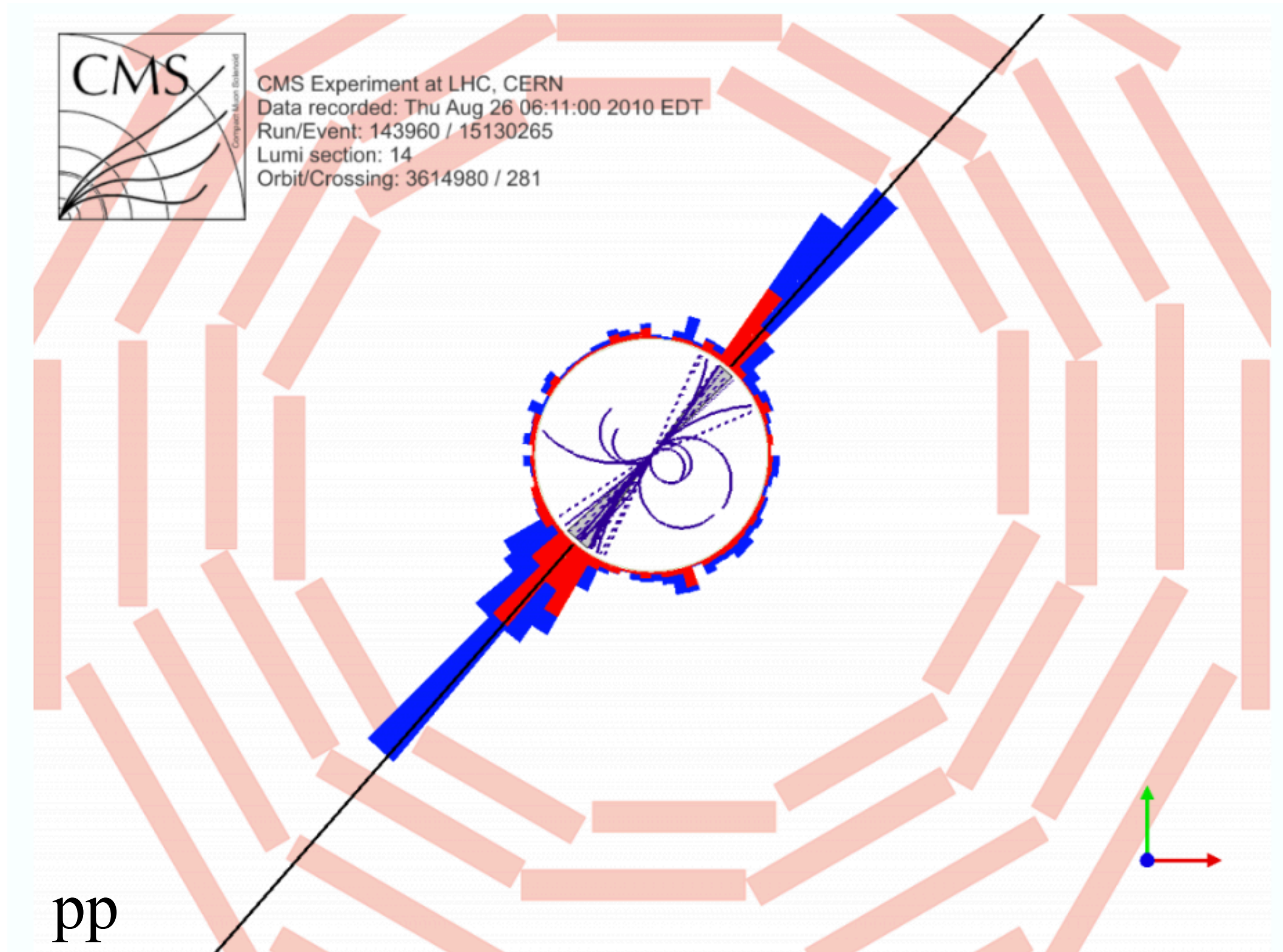
$$\alpha_s \ll 1 \quad \sim \alpha_s d \log \theta d \log z$$

The diagram shows a branching process where a line splits into two lines at an angle θ . The energy fraction of the upper branch is z and the lower branch is $1-z$.

LO	1		
NLO	αL	α	
NNLO	$\alpha^2 L^2$	$\alpha^2 L$	α^2
...
$N^k \text{LO}$	$\alpha^k L^k$	$\alpha^k L^{k-1}$	$\alpha^k L^{k-2}$

L is some large logarithm of scales' ratios

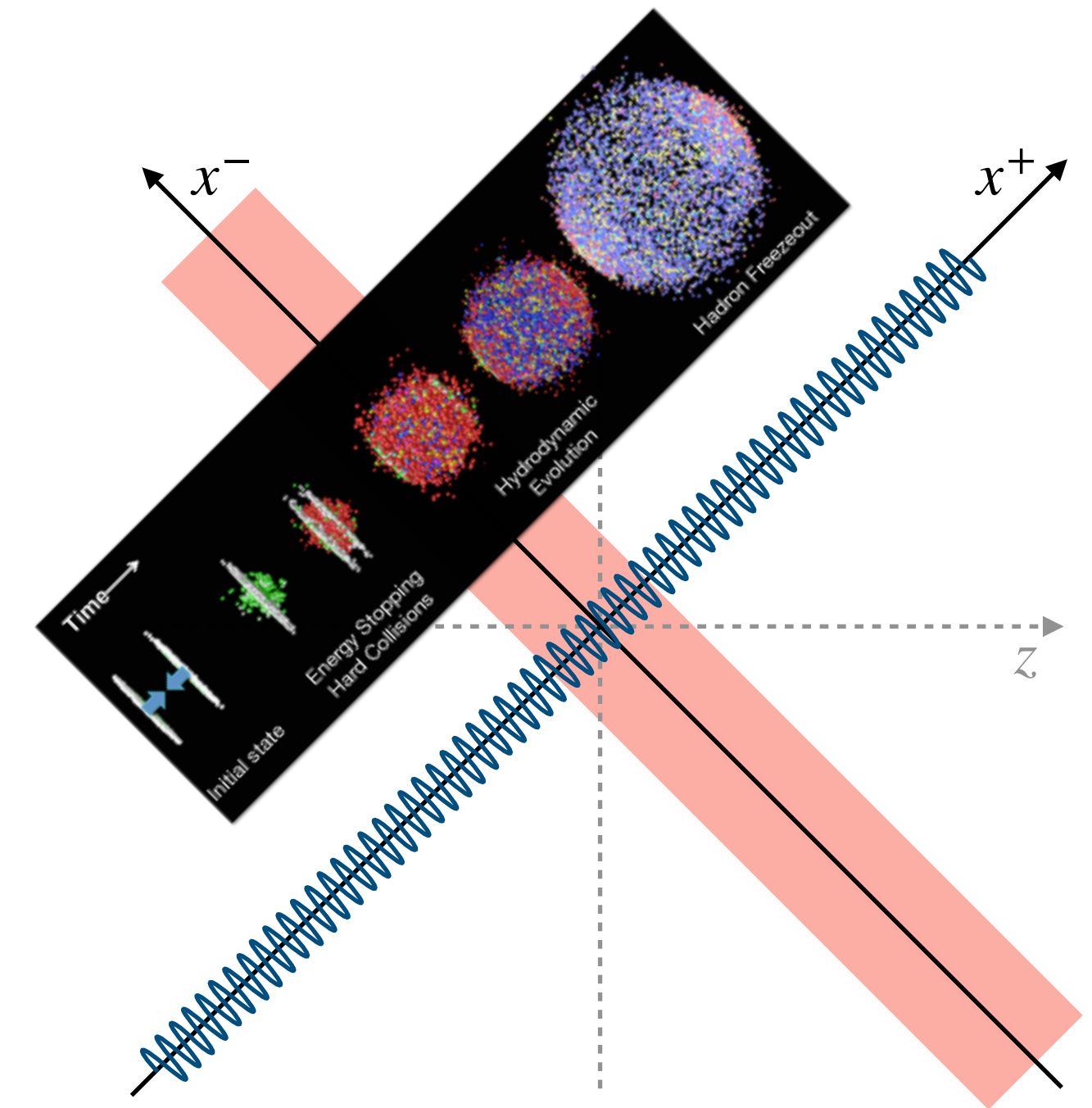
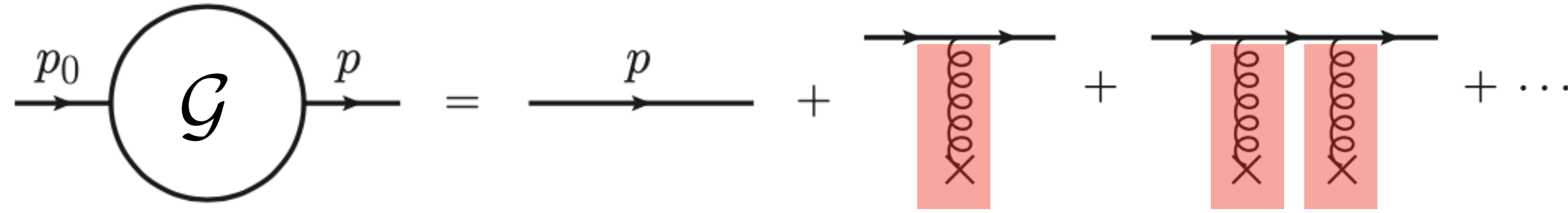
What happens to jets in HICs ?



The modification of jets due to the propagation in the QGP is generally referred to as **jet quenching**

How does one compute these modifications ?

In the medium, one needs to account for interactions with the QGP:



For very energetic particles there is a simple solution:

$$\mathcal{G}(\mathbf{x}_2, t_2; \mathbf{x}_1, t_1) = \text{Positional kicks from medium particles} + \text{Color rotation} + \dots$$

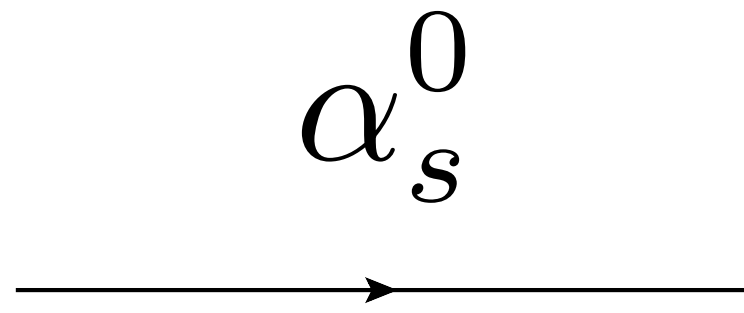
[Higher-Twist, early 2000s]
 [BDMPS-Z, early 2000s]
 [GLV, early 2000s]
 [AMY, early 2000s]

Any process reduces to computing correlators of these objects

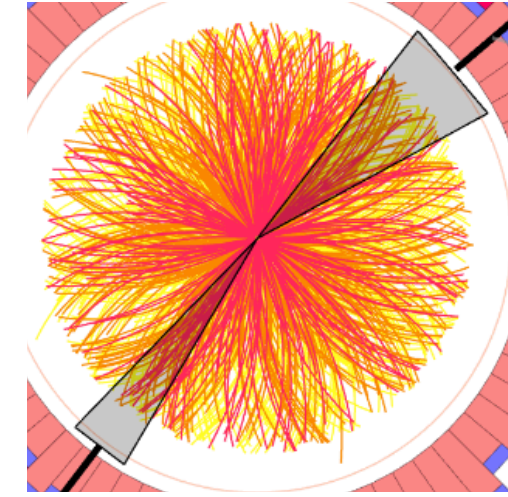
$$d\sigma \sim \langle \mathcal{T} \prod_{\text{QCD vertices}} \{ \mathcal{G}, \Gamma \} \rangle_{\text{matter}}$$

Simplest example, consider just 1 particle

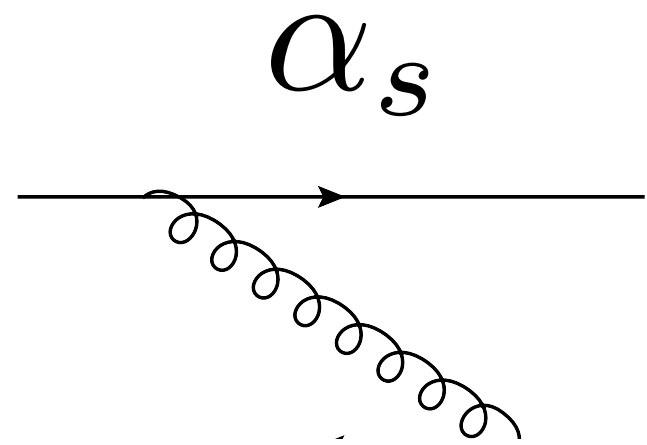
$$d\sigma^{(1)} \sim \langle \mathcal{G} \mathcal{G}^\dagger \rangle_{\text{matter}}$$



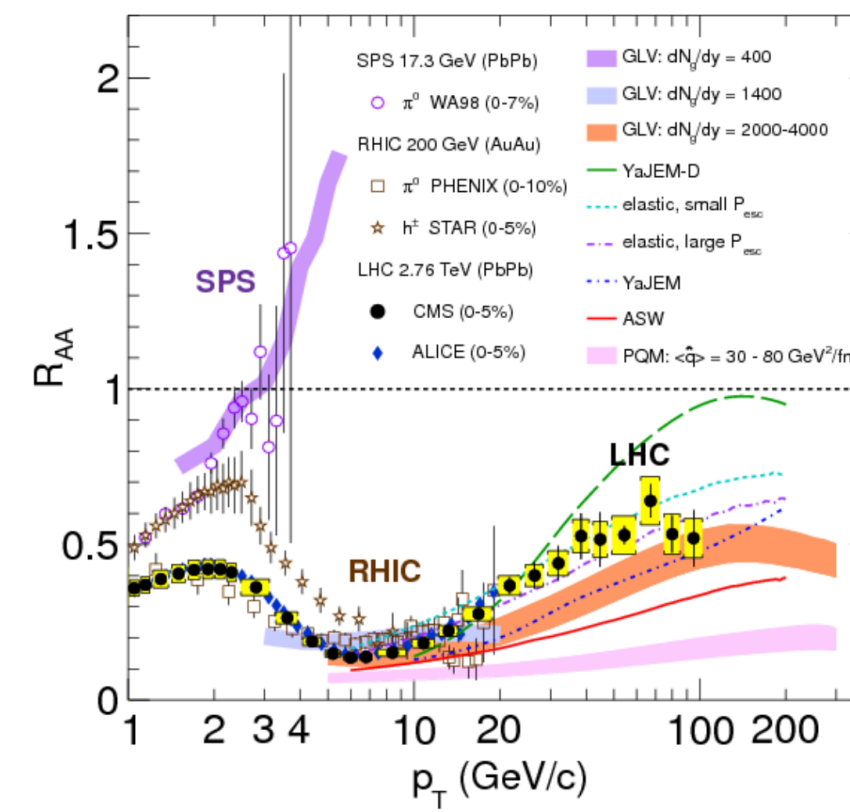
Momentum broadening



Known from pre-QCD era

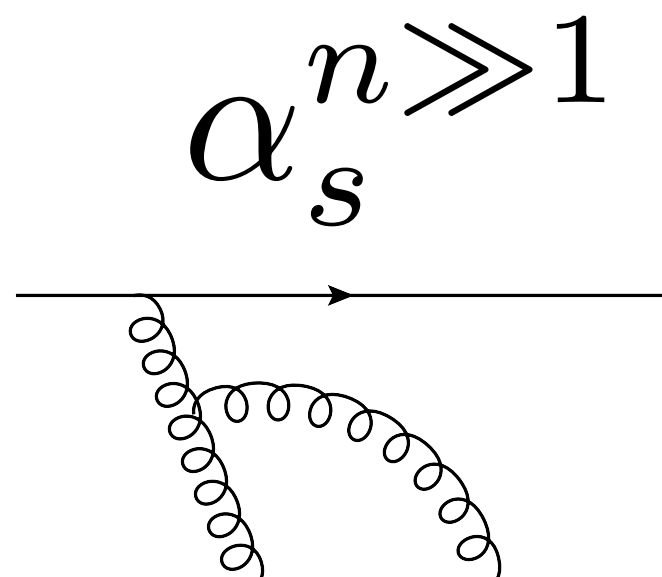


Energy loss

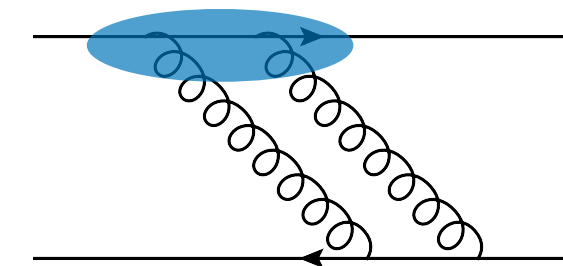


First studies, early 2000's

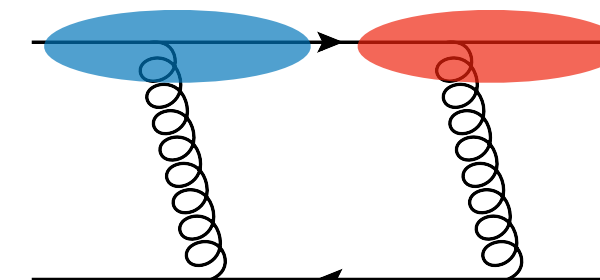
Full kinematics, 2000-ongoing



Medium modified partonic cascades



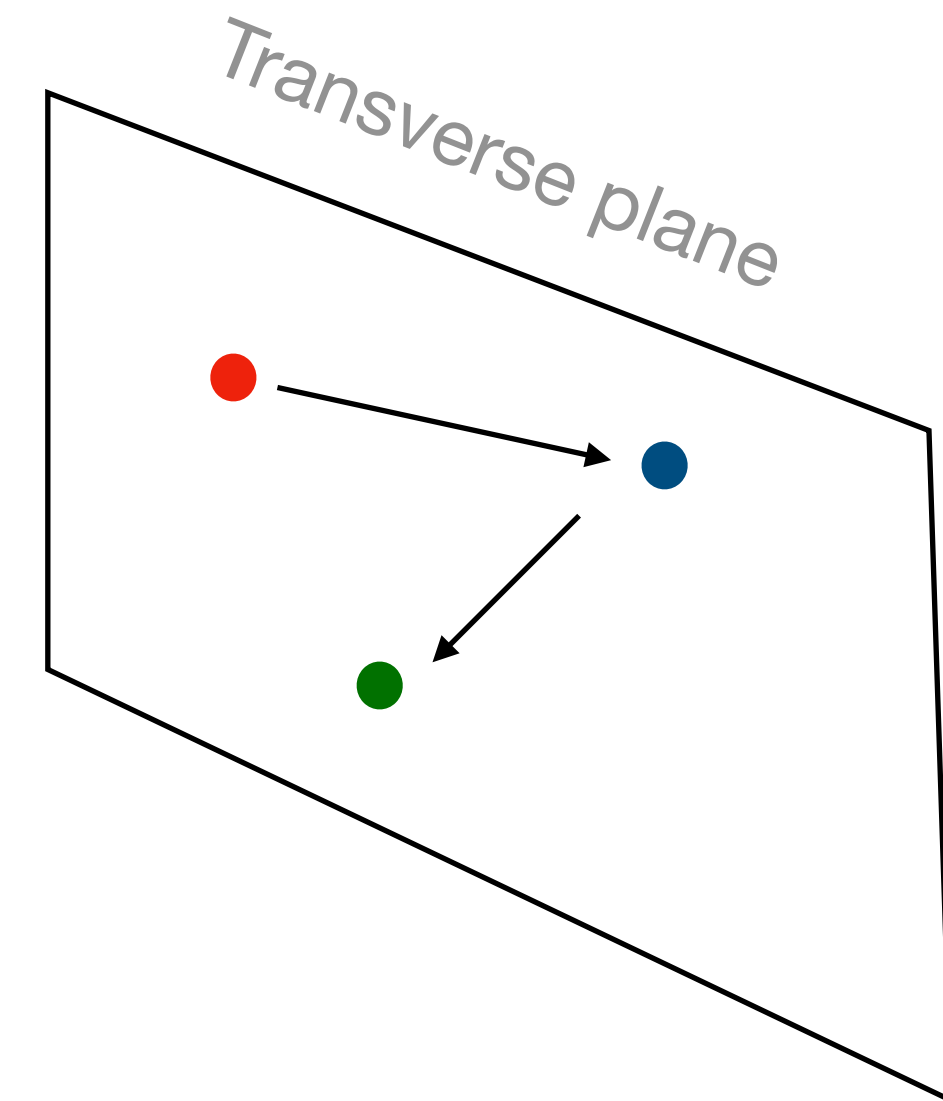
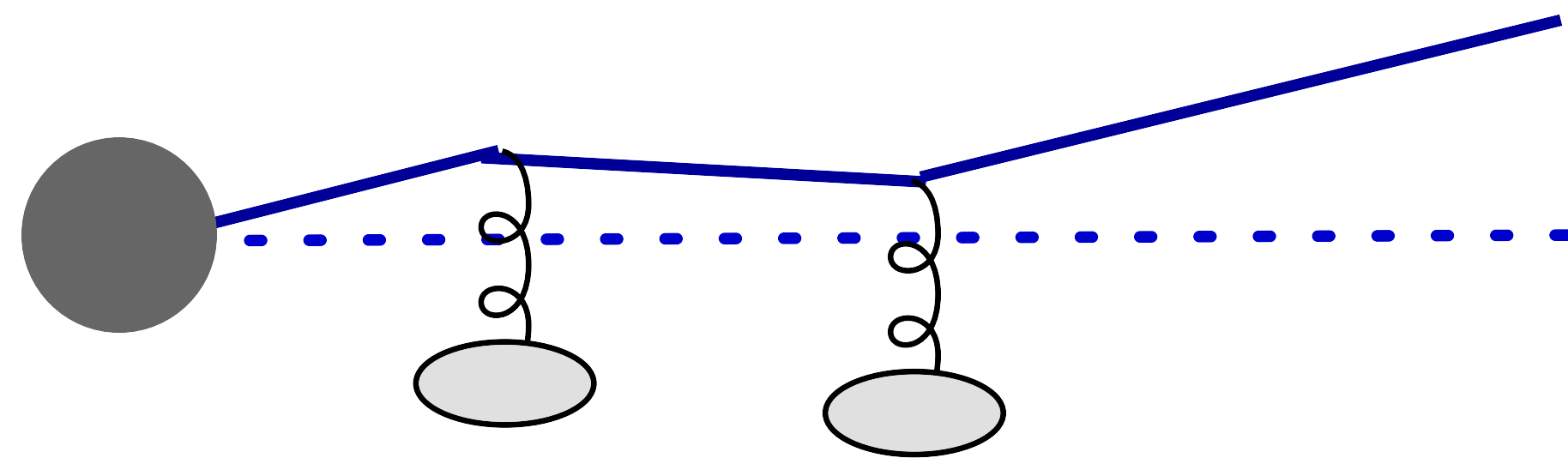
vs



Simple set ups, 2010-ongoing

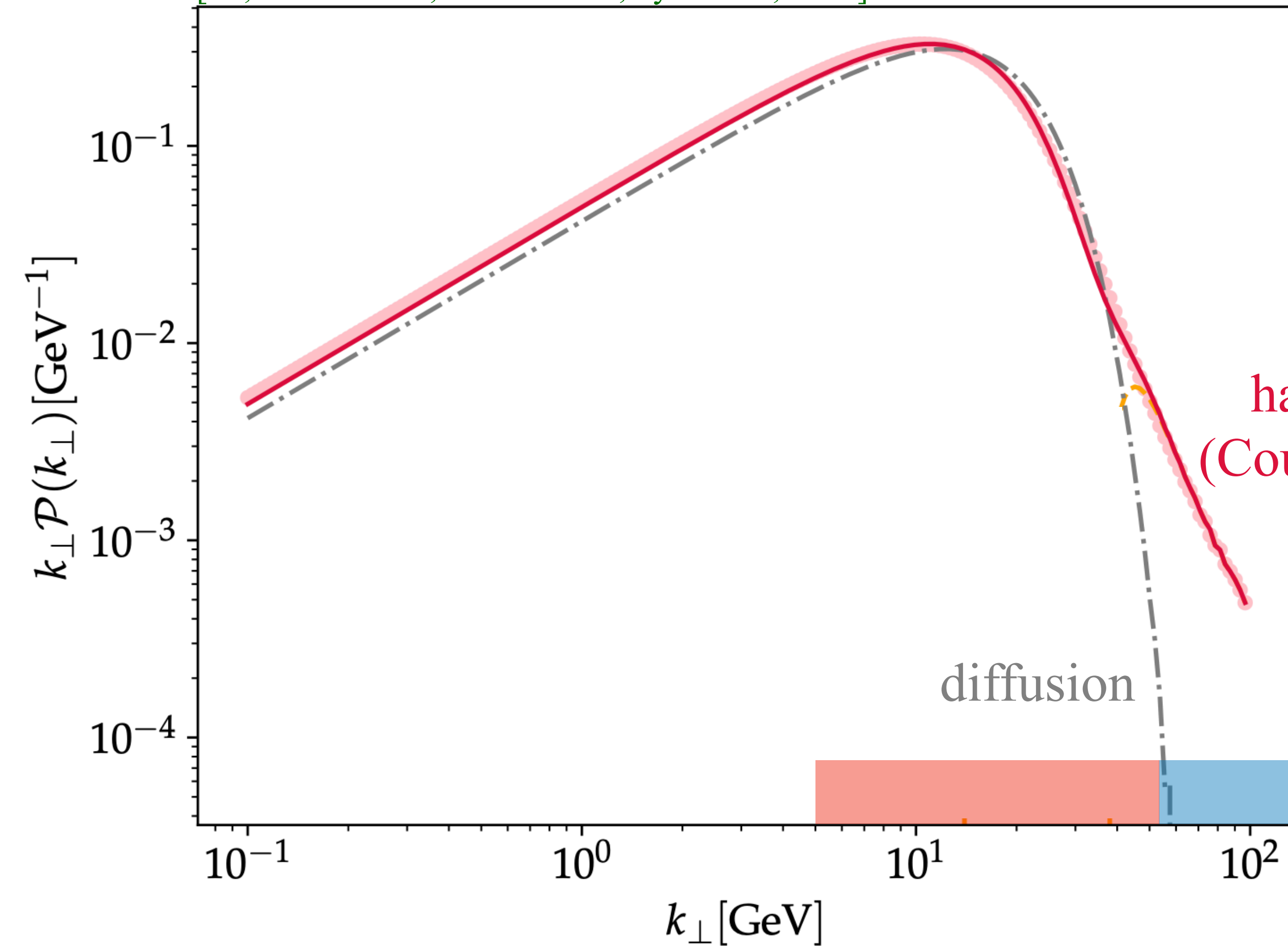
Momentum broadening

$\mathcal{O}(\alpha_s^0)$



How is momentum transferred to the parton ?

[JB, Mehtar-Tani, Soto-Ontoso, Tywoniuk, 2022]



Two regimes :

Diffusive broadening

= many soft kicks

$$\partial_t \mathcal{P}(\mathbf{k}) = -\frac{\hat{q}}{4} \partial_{\mathbf{k}}^2 \mathcal{P}(\mathbf{k})$$

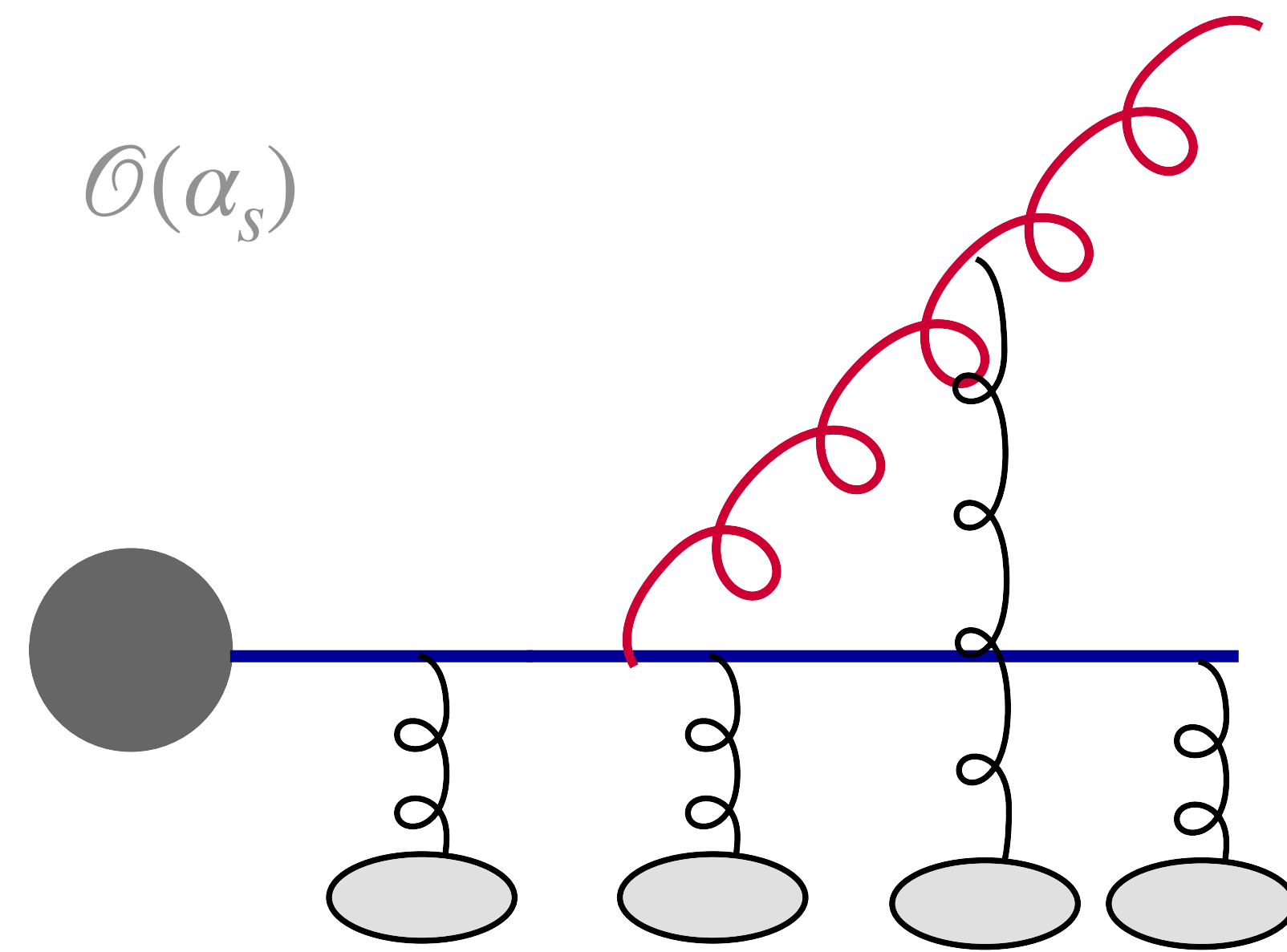
jet quenching parameter

Single hard interaction

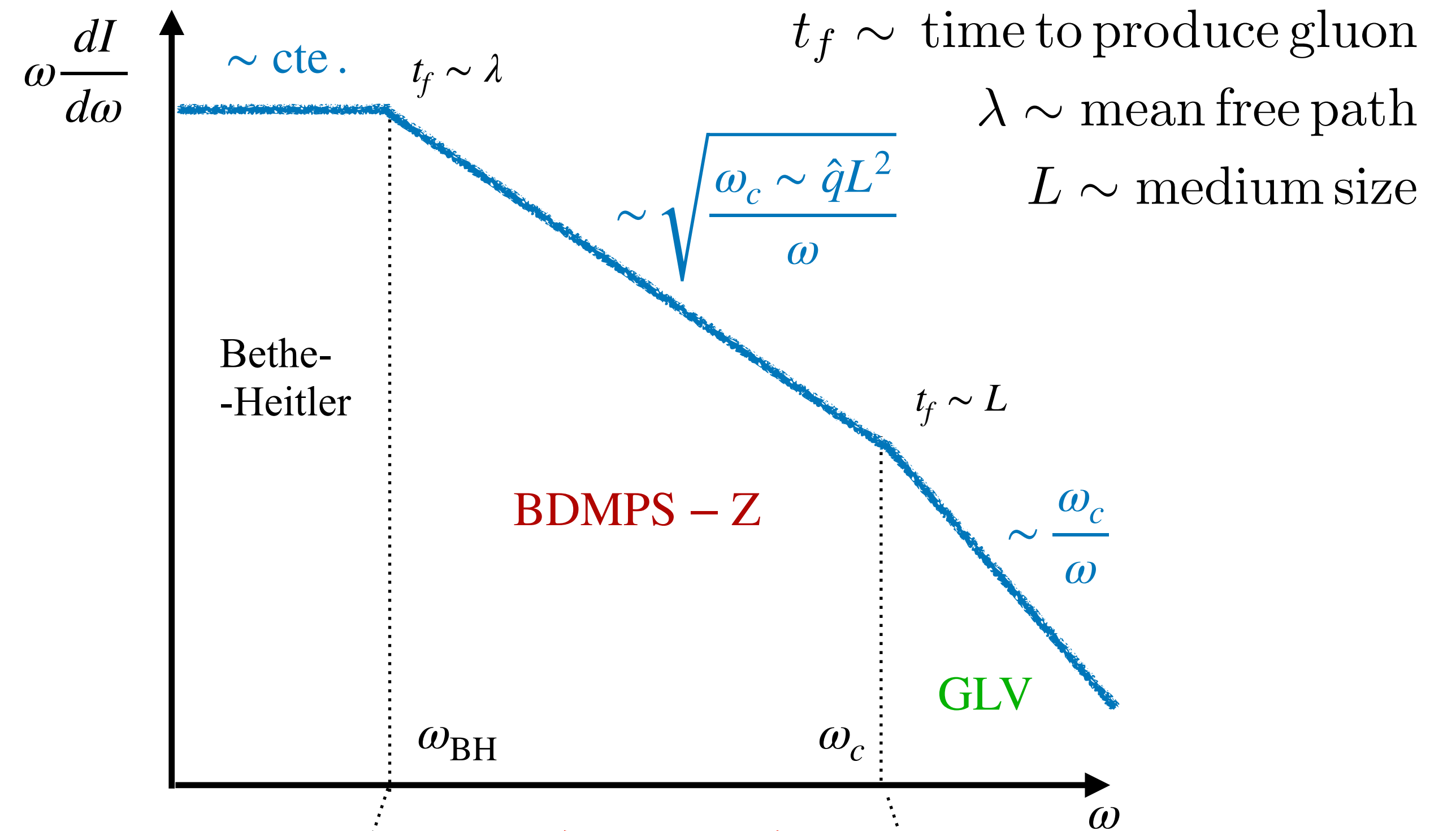
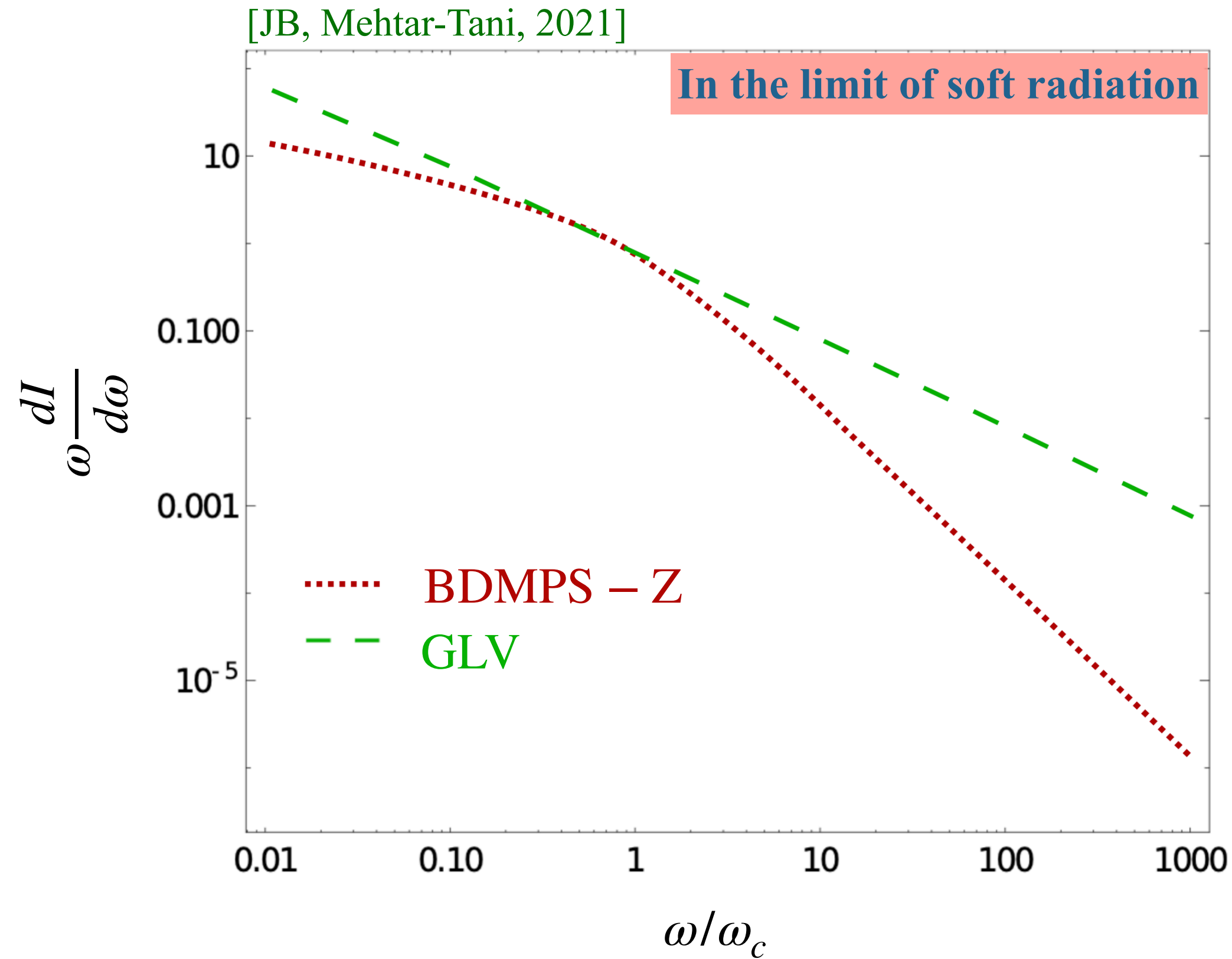
= one hard kick

$$\mathcal{P}(\mathbf{k}) \propto \frac{1}{k^4}$$

Medium induced radiation



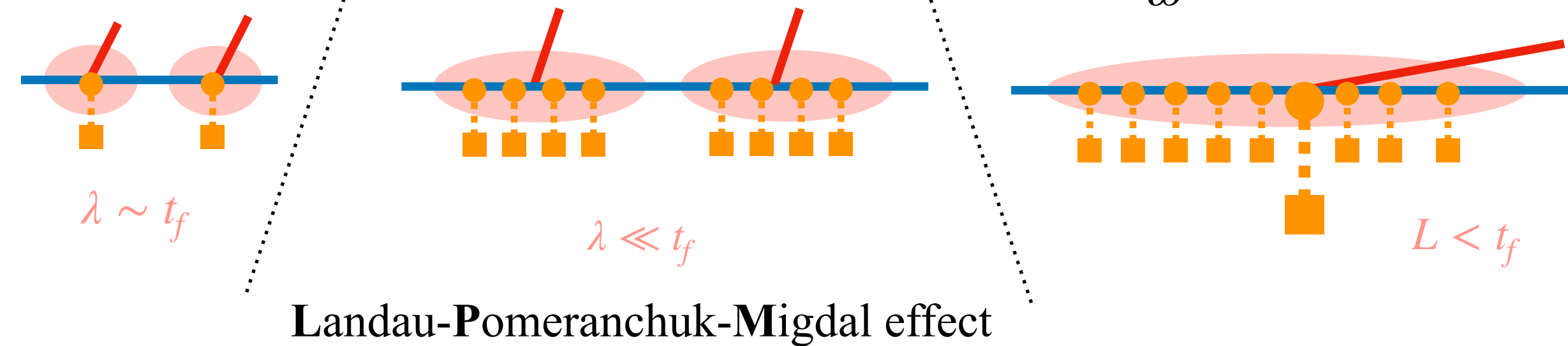
How do particles radiate in-medium ?



$$t_f \sim \frac{2\omega}{k_{\perp}^2} \sim \frac{2\omega}{\hat{q}t_f} \longrightarrow \omega \frac{dI}{d\omega} \sim \alpha_s \frac{L}{t_f} \sim \alpha_s \sqrt{\frac{\hat{q}L^2}{\omega}}$$

$\langle k_{\perp}^2 \rangle \sim \hat{q}t$

LPM effect



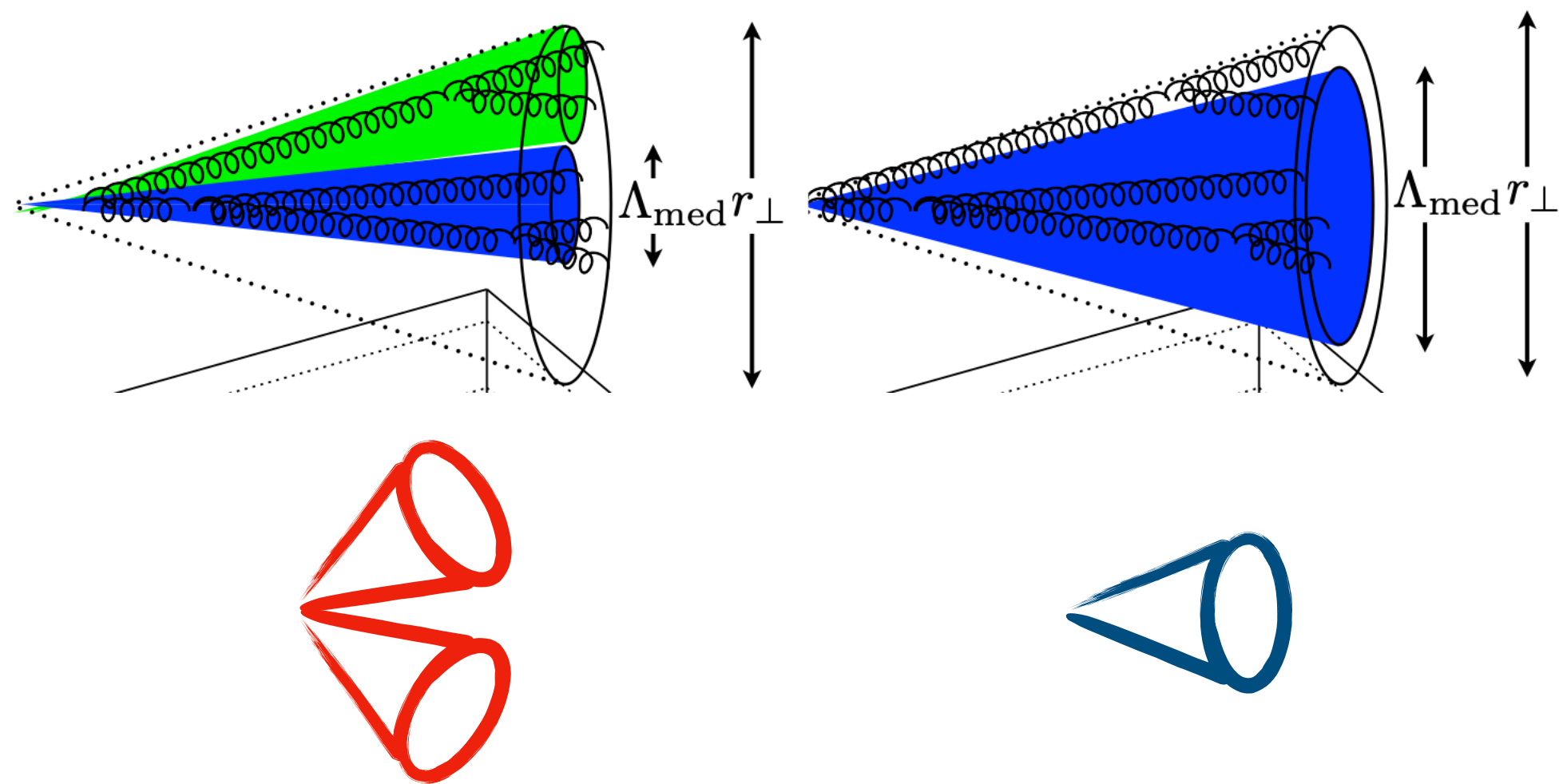
Energy loss in the quenching weight approximation

$$\frac{d\sigma_q^{\text{med}}}{dp_t d\theta} = \int_0^\infty d\varepsilon D_q(\varepsilon) \left. \frac{d\sigma_q^{\text{vac}}}{dp'_t d\theta} \right|_{p'_t = p_t + \varepsilon}$$

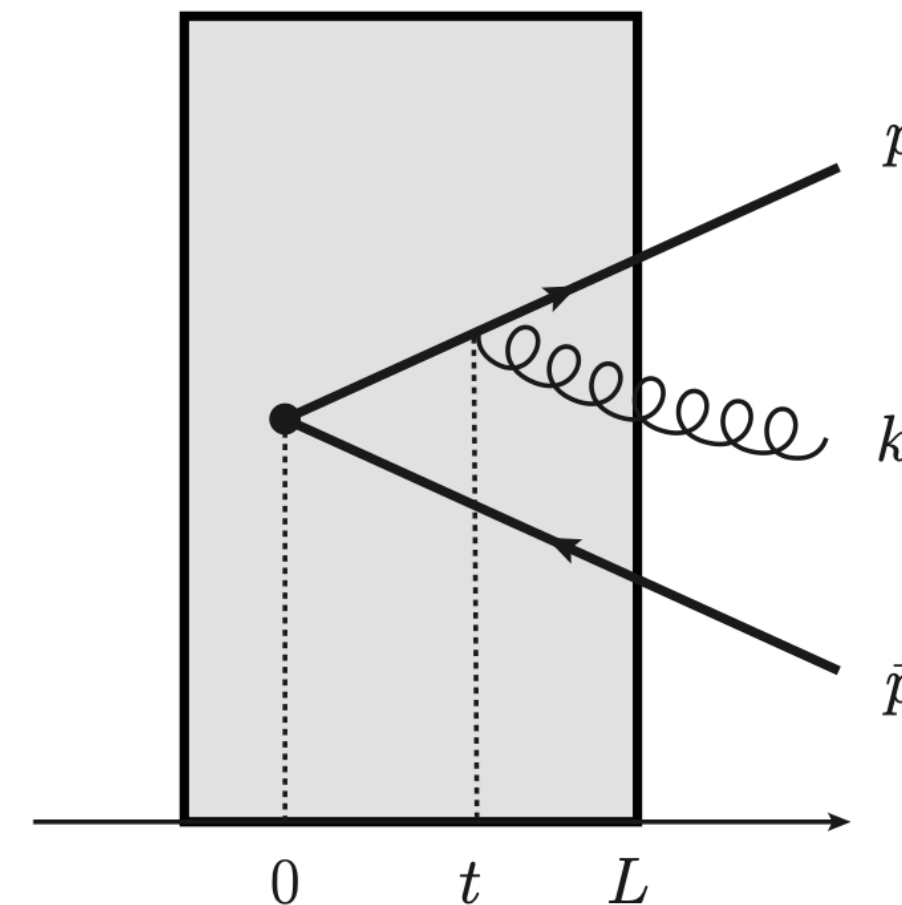
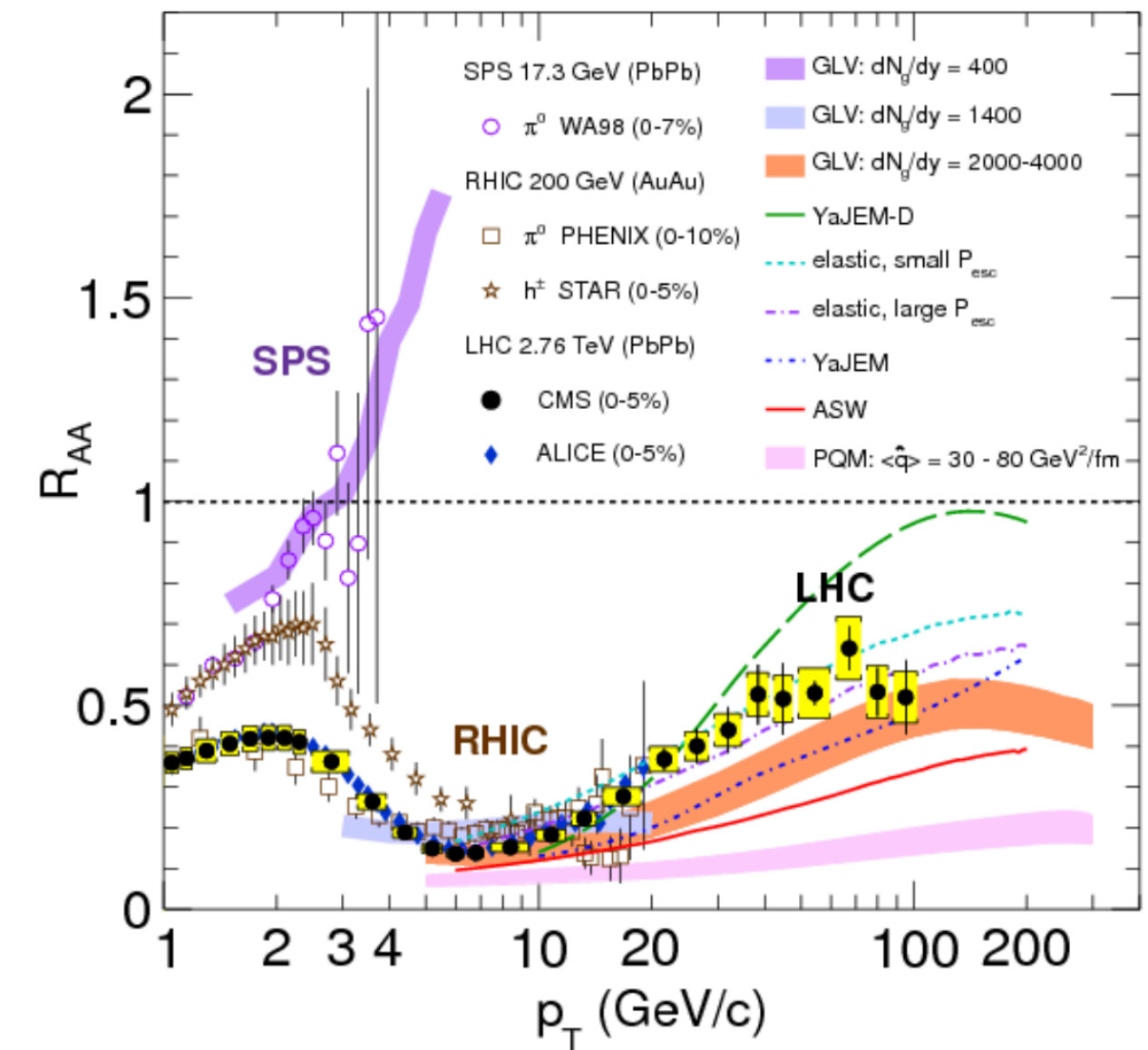
$$\frac{d\sigma_q^{\text{med}}}{dp_t d\theta} \approx \frac{d\sigma_q^{\text{vac}}}{dp_t d\theta} \int_0^\infty d\varepsilon D_q(\varepsilon) e^{-\frac{n\varepsilon}{p_t}} \equiv Q_q(p_t) \frac{d\sigma_q^{\text{vac}}}{dp_t d\theta}$$

[R. Baier, Y. Dokshitzer, A. H. Mueller, hep-ph/0106347]

Color coherence and anti-angular ordering



$$0 < Q_q < 1$$



vacuum \longrightarrow angular ordering

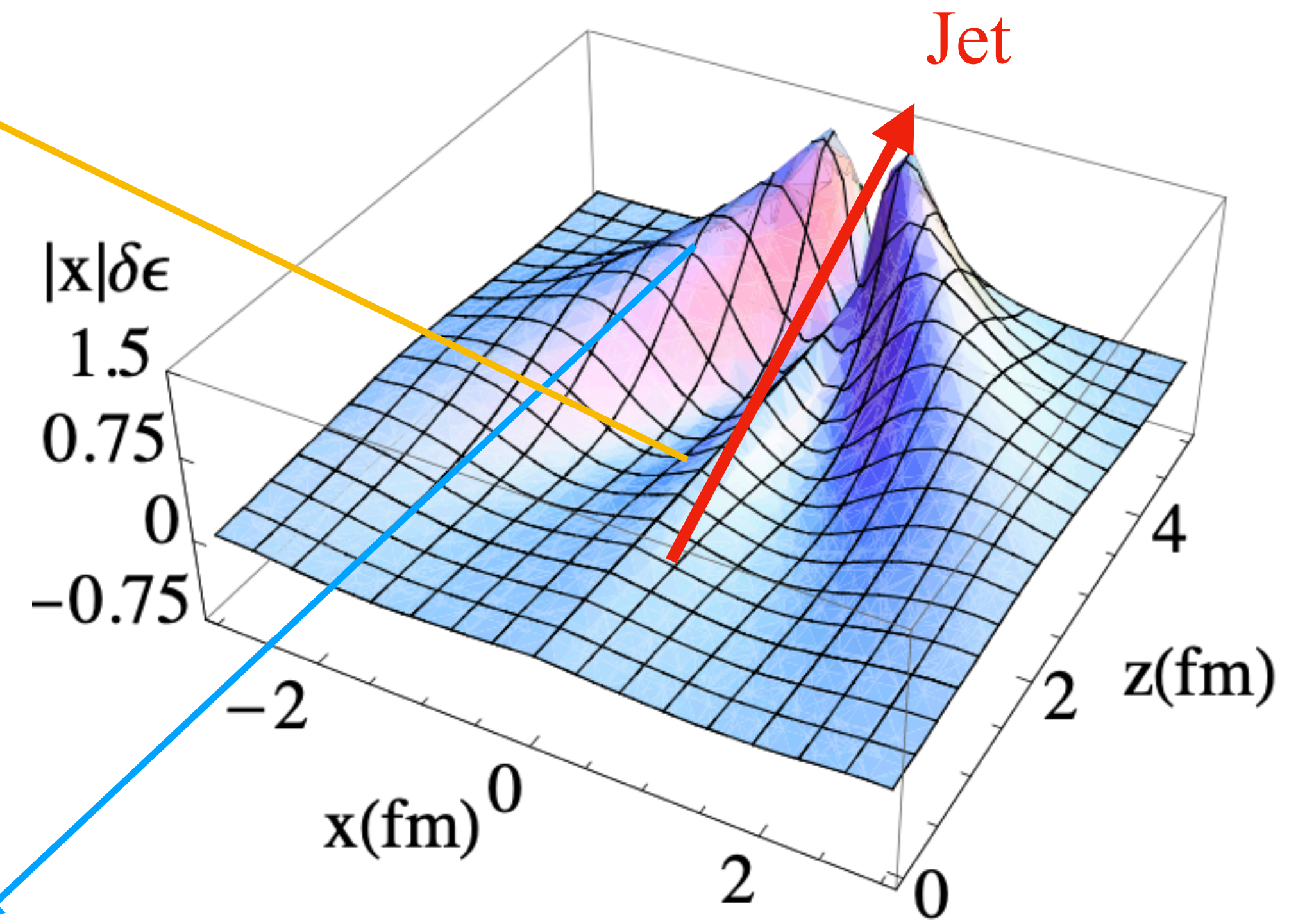
medium \longrightarrow anti-angular ordering

Back-reaction: Jet induced wake on the plasma

Depletion of energy

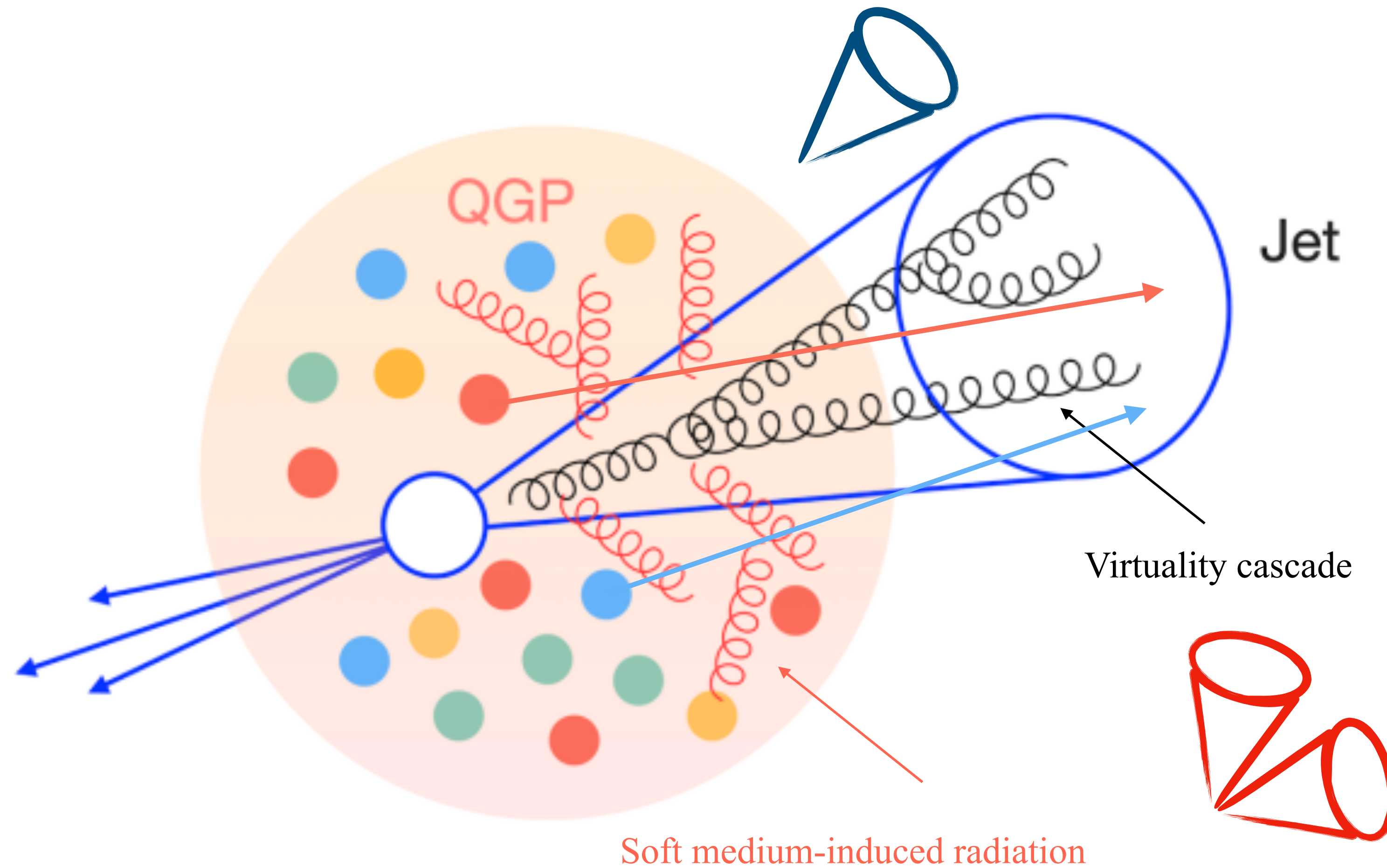


[G.-Y. Qin, A. Majumder, H. Song, U. Heinz, 0903.22255]



Excess of soft particles

These results form the basis for jet quenching phenomenology





Jet substructure observables

How to understand the structure of jets

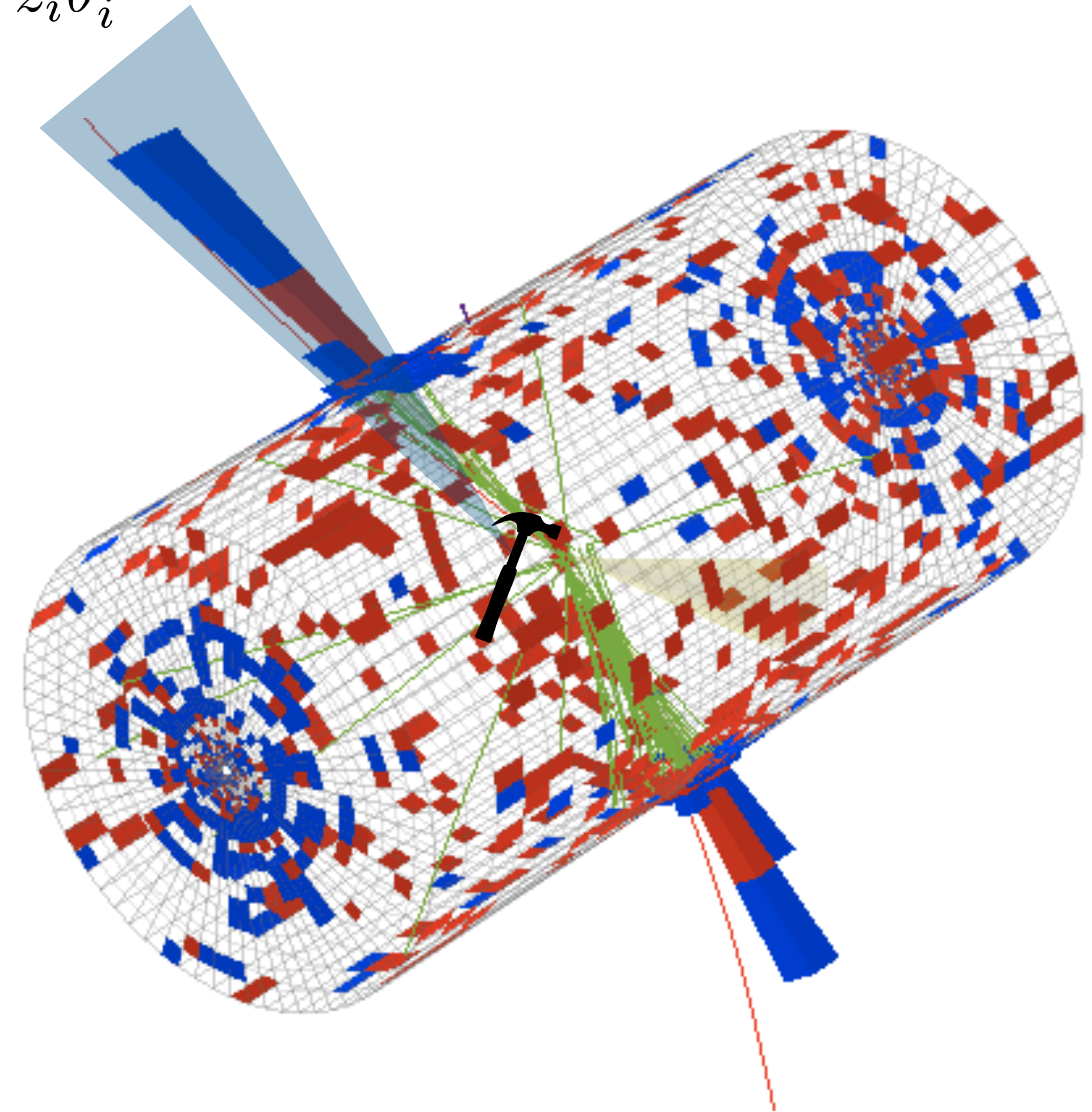


$$O_{m^2} = \sum_i z_i \theta_i^2$$



[Caron-Huot, et al, 2209.00008]

≈



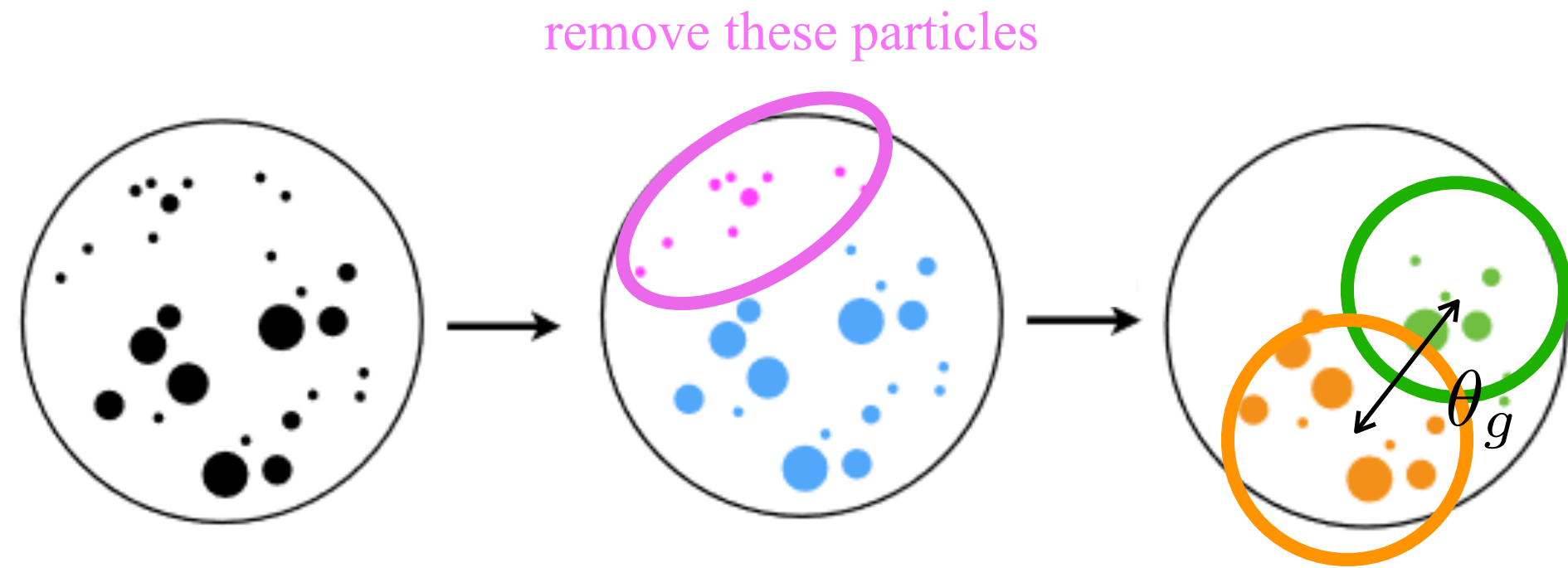
Schematically, one can compute “shapes” of the underlying distribution

$$\frac{d\sigma}{do} = \int d^4x e^{iq^\mu x_\mu} \langle \Omega | \hat{O}(x) \mathcal{M}[\hat{o}] O^\dagger(0) | \Omega \rangle, \quad \text{e.g.} \quad \mathcal{M}[\hat{o}] = \delta(\hat{o} - o)$$

How to understand the structure of jets: jet shapes

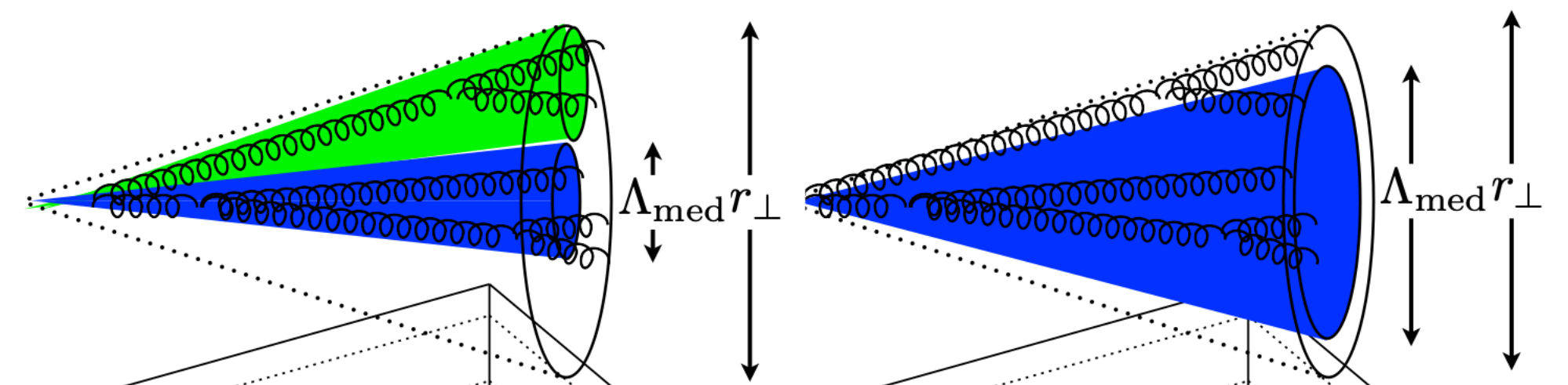
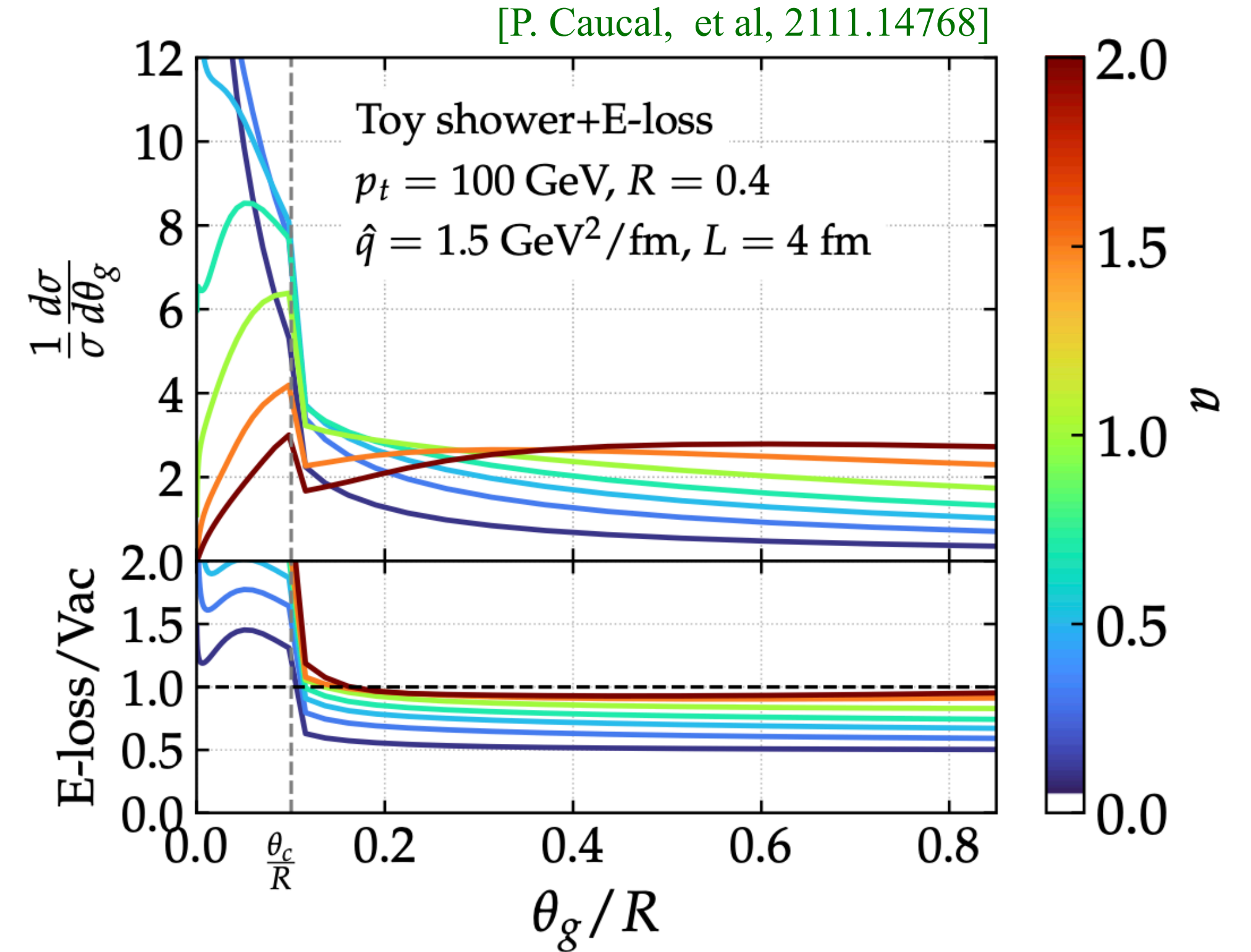


The common strategy boils down to reclustering the jet and then selecting only a subset of constituents



Allows to explore the details of the jet cascade. However, formally the treatment is not trivial even in vacuum.

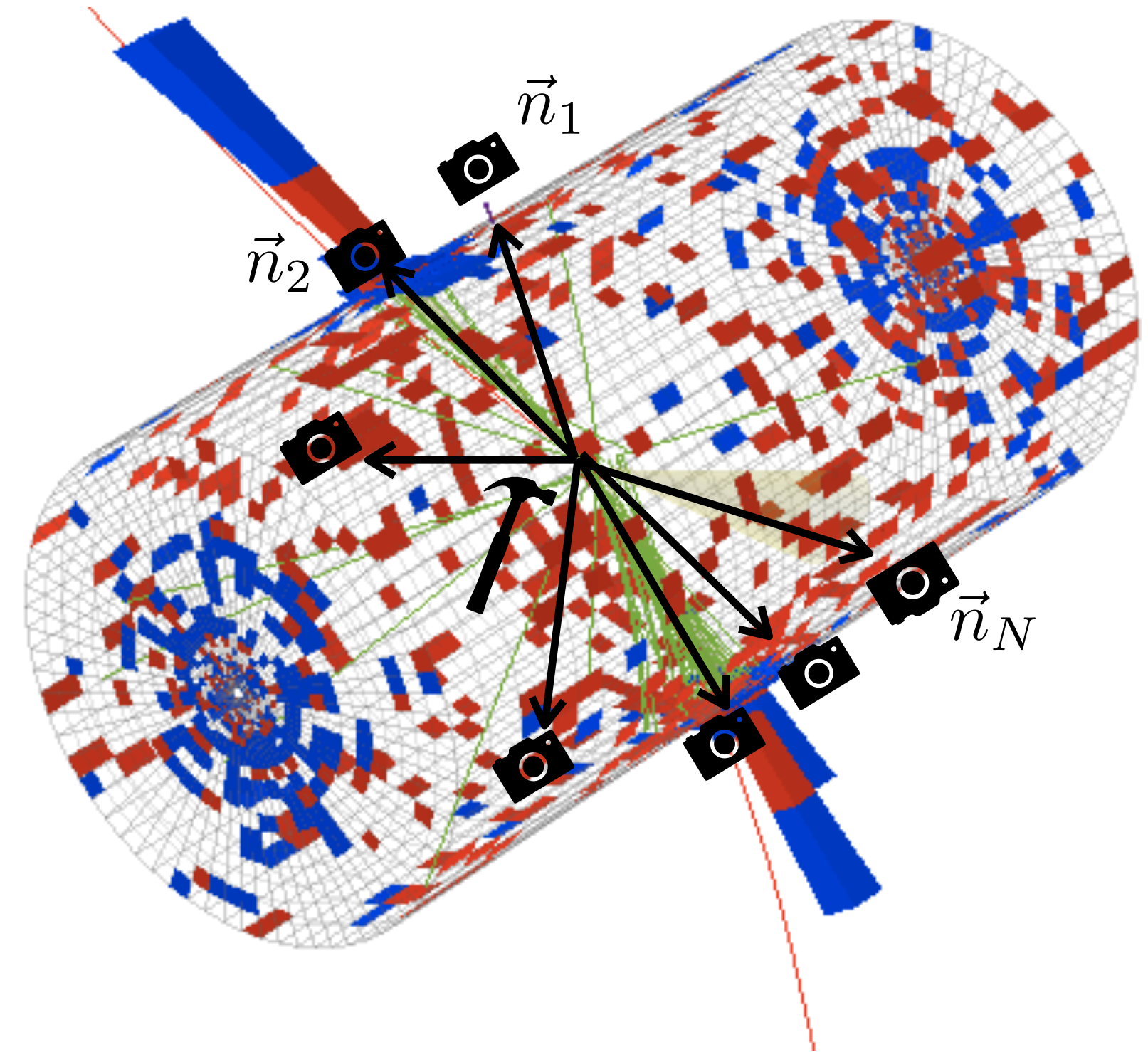
[See Takao and Monika's talk in this session for more substructure studies]





[Caron-Huot, et al, 2209.00008]

≈



Another option is to weight the final state by the energy of particles

$$\sigma = \int d^4x e^{iq^\mu x_\mu} \langle \Omega | \hat{O}(x) \mathcal{E}(\vec{n}_1) \cdots \mathcal{E}(\vec{n}_N) \hat{O}(0) | \Omega \rangle, \quad \text{where} \quad \mathcal{E}(\vec{n}) | P \rangle = \sum_i E_i \delta(\Omega_{\vec{n}} - \Omega_{\vec{k}_i}) | P \rangle$$

How to understand the structure of jets: Energy Correlators

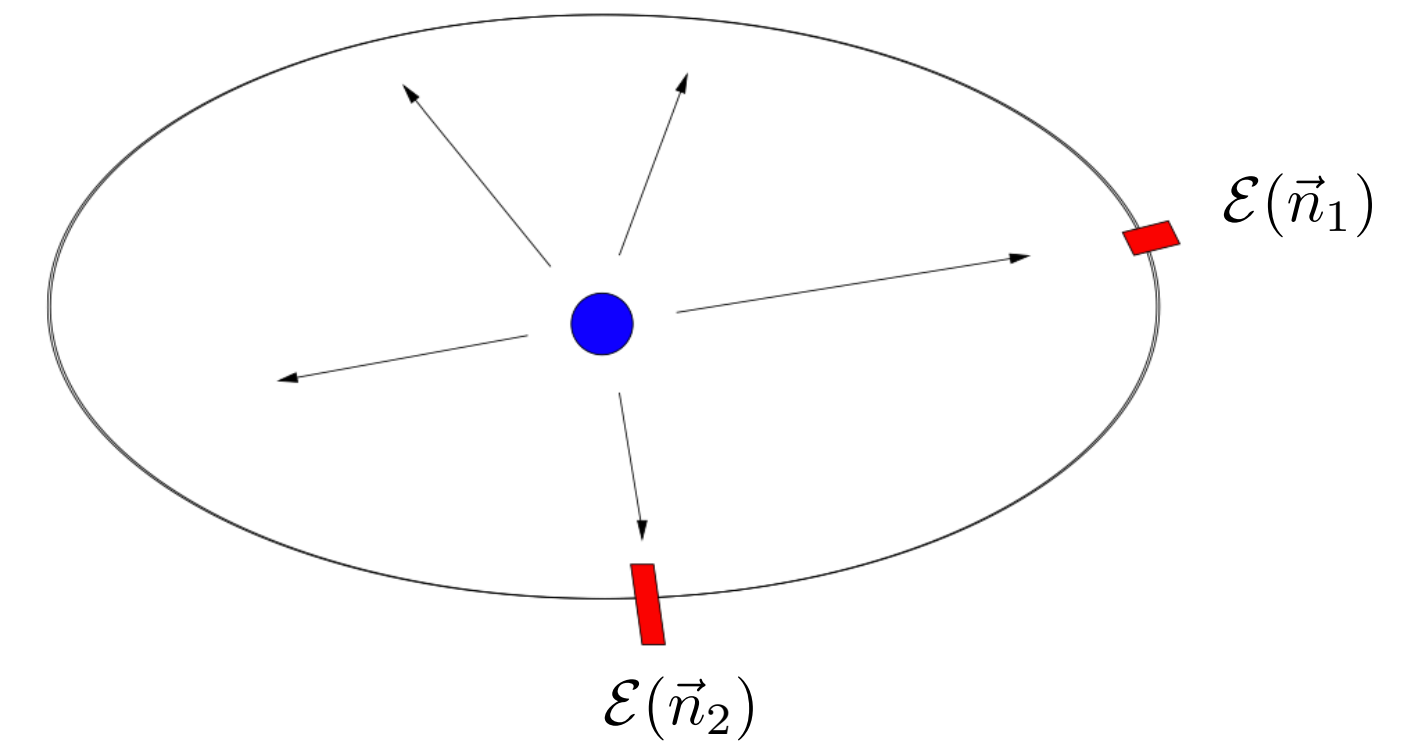
Energy correlators were first proposed in QCD in the late 1970s

Energy Correlations in Electron-Positron Annihilation: Testing Quantum Chromodynamics

C. Louis Basham, Lowell S. Brown, Stephen D. Ellis, and Sherwin T. Love

Department of Physics, University of Washington, Seattle, Washington 98195

(Received 21 August 1978)



1-point correlator

$$\frac{d\Sigma}{d\Omega} = \sum_{N=2}^{\infty} \int \sum_{a=1}^N E_a^{-1} d^3p_a \frac{d^N\sigma}{E_1^{-1} d^3p_1 \cdots E_N^{-1} d^3p_N} S_N \left[\sum_{b=1}^N \frac{E_b}{W} \delta(\Omega_b - \Omega) \right]$$

2-point correlator

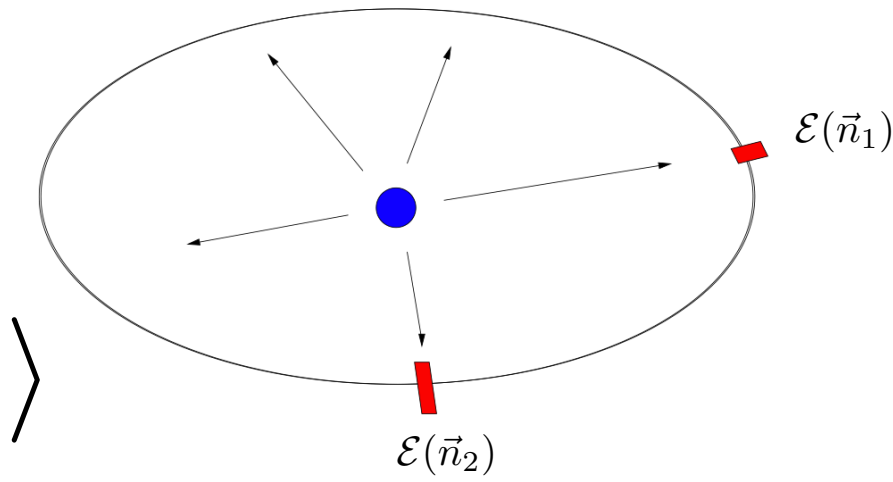
$$\frac{d^2\Sigma}{d\Omega d\Omega'} = \sum_{N=2}^{\infty} \int \prod_{a=1}^N E_a^{-1} d^3p_a \frac{d^N\sigma}{E_1^{-1} d^3p_1 \cdots E_N^{-1} d^3p_N} S_N \left[\sum_{b,c=1}^N \frac{E_b E_c}{W^2} \delta(\Omega_b - \Omega) \delta(\Omega_c - \Omega') \right]$$

- N-particle cross-section
- Energy weighting
- Restricted angular region
- Form pairs out of N partons

It should be emphasized that the measurement of the energy cross section, Eq. (1), does not require any detailed event-by-event analysis as is the case for tests which specify a quantity involving the definition of a jet axis in each event.⁵

ENCs boil down to measuring correlation functions of the **energy flow operator** $\mathcal{E}(\vec{n})$

$$\mathcal{E}(\vec{n}) = \lim_{r \rightarrow \infty} \int dt r^2 n^i T^{0i}(t, r \vec{n}) \longrightarrow \langle 0 | \bar{\psi}(x) \mathcal{E}(\vec{n}_1) \mathcal{E}(\vec{n}_2) \psi(0) | 0 \rangle$$



In the simplest case, we can consider the one dimensional projection

$$\frac{d\Sigma}{d\theta} = \int_{\vec{n}_1, \vec{n}_2} \frac{\langle \mathcal{E}(\vec{n}_1) \mathcal{E}(\vec{n}_2) \rangle}{p_t^2} \delta(\vec{n}_1 \cdot \vec{n}_2 - \cos \theta)$$

$$\frac{d\Sigma}{d\theta} = \int_z \frac{d\sigma}{\sigma d\theta dz} z(1-z)$$

IR safe

$$\sim \frac{1}{\theta^\alpha}$$

In summary: *The small angle behavior of the energy correlation functions is determined by the spin $j = 3$ non-local operators that appear in the OPE*

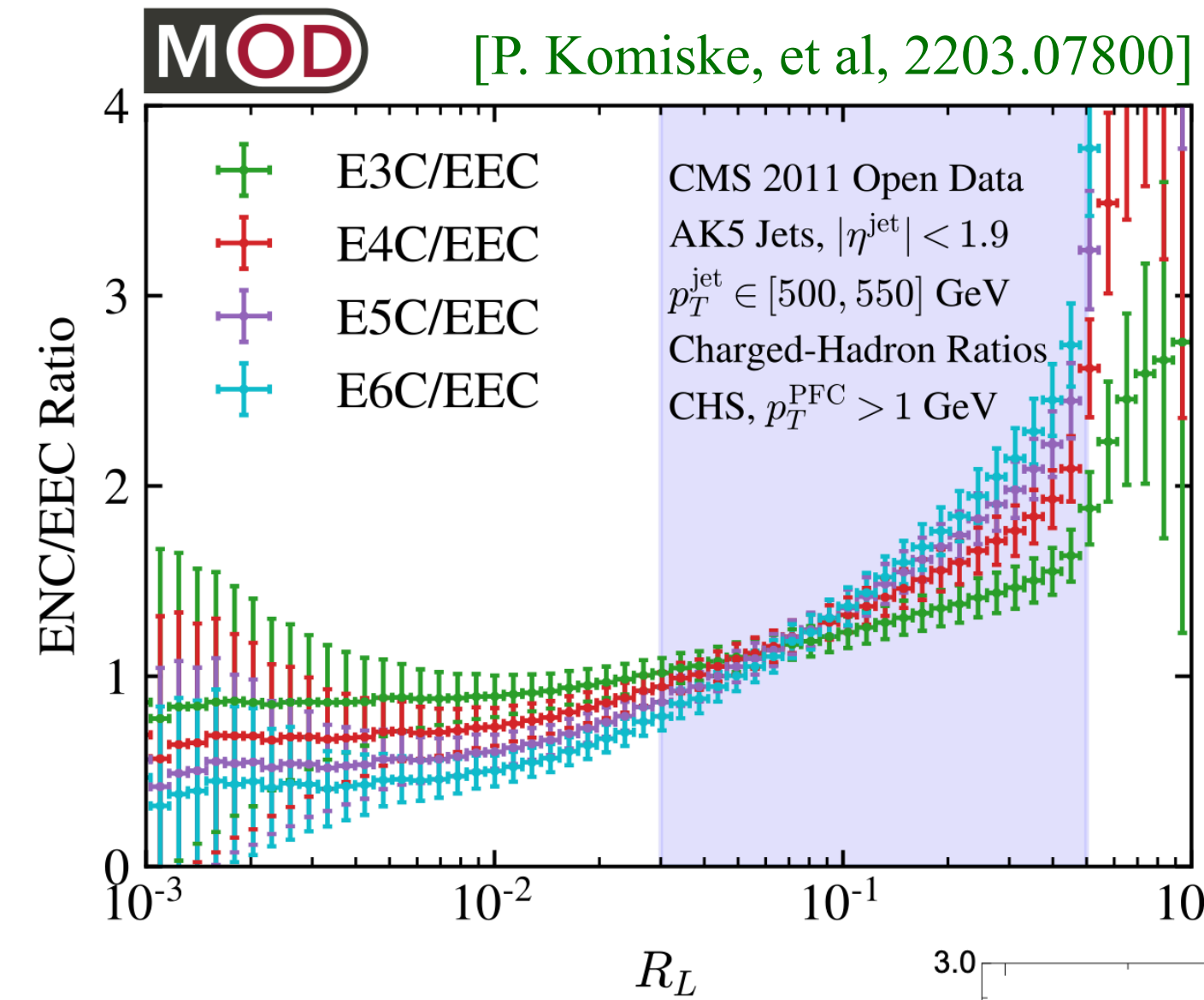
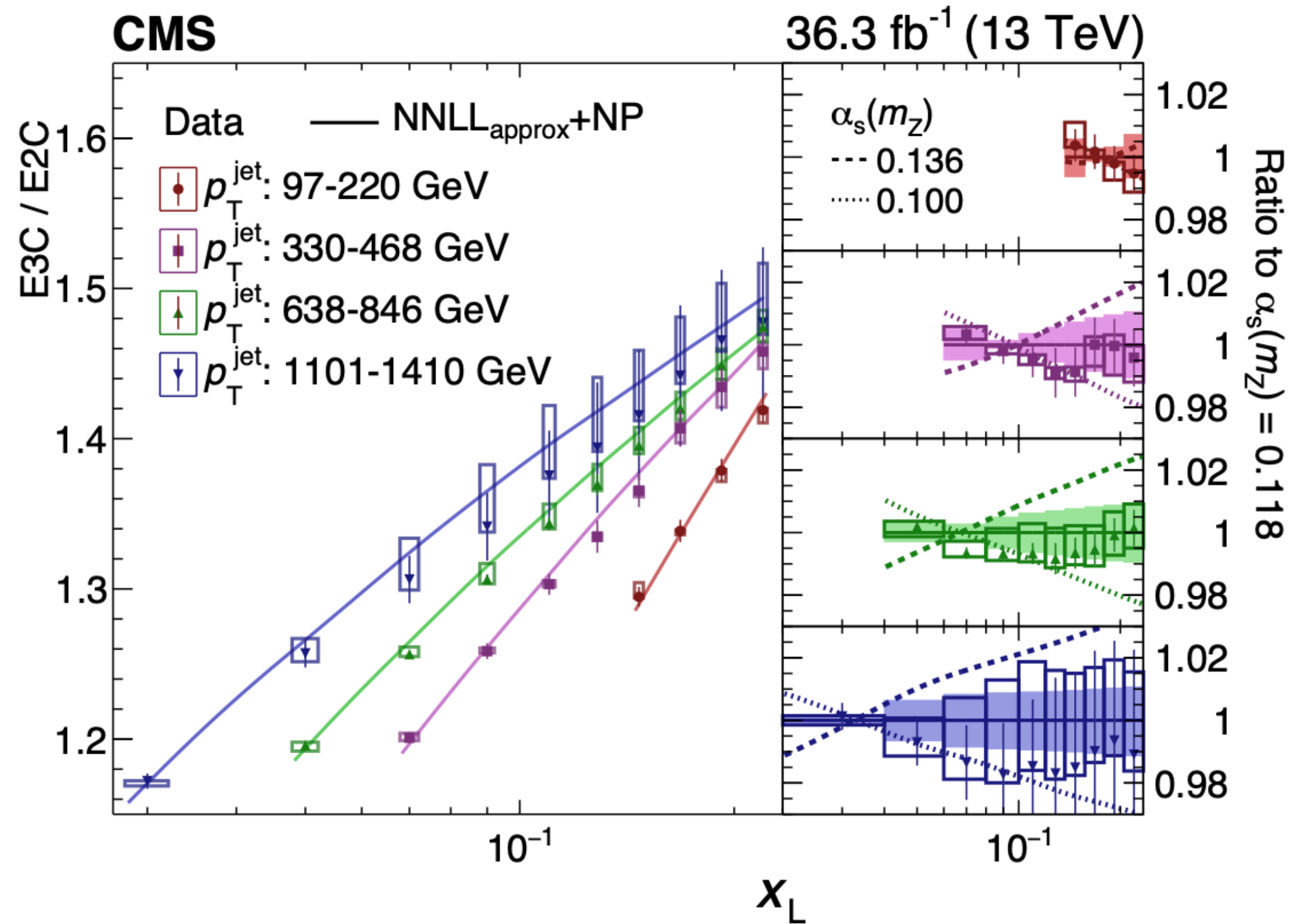
$$\langle \mathcal{E}(\theta_1) \mathcal{E}(\theta_2) \dots \rangle \sim \sum |\theta_{12}|^{\tau_n - 4} \langle \mathcal{U}_{3-1,n}(\theta_2) \dots \rangle \quad (2.19)$$

at LO : $\alpha = 1$, deviations controlled by **quantum theory**

How to understand the structure of jets: Energy Correlators

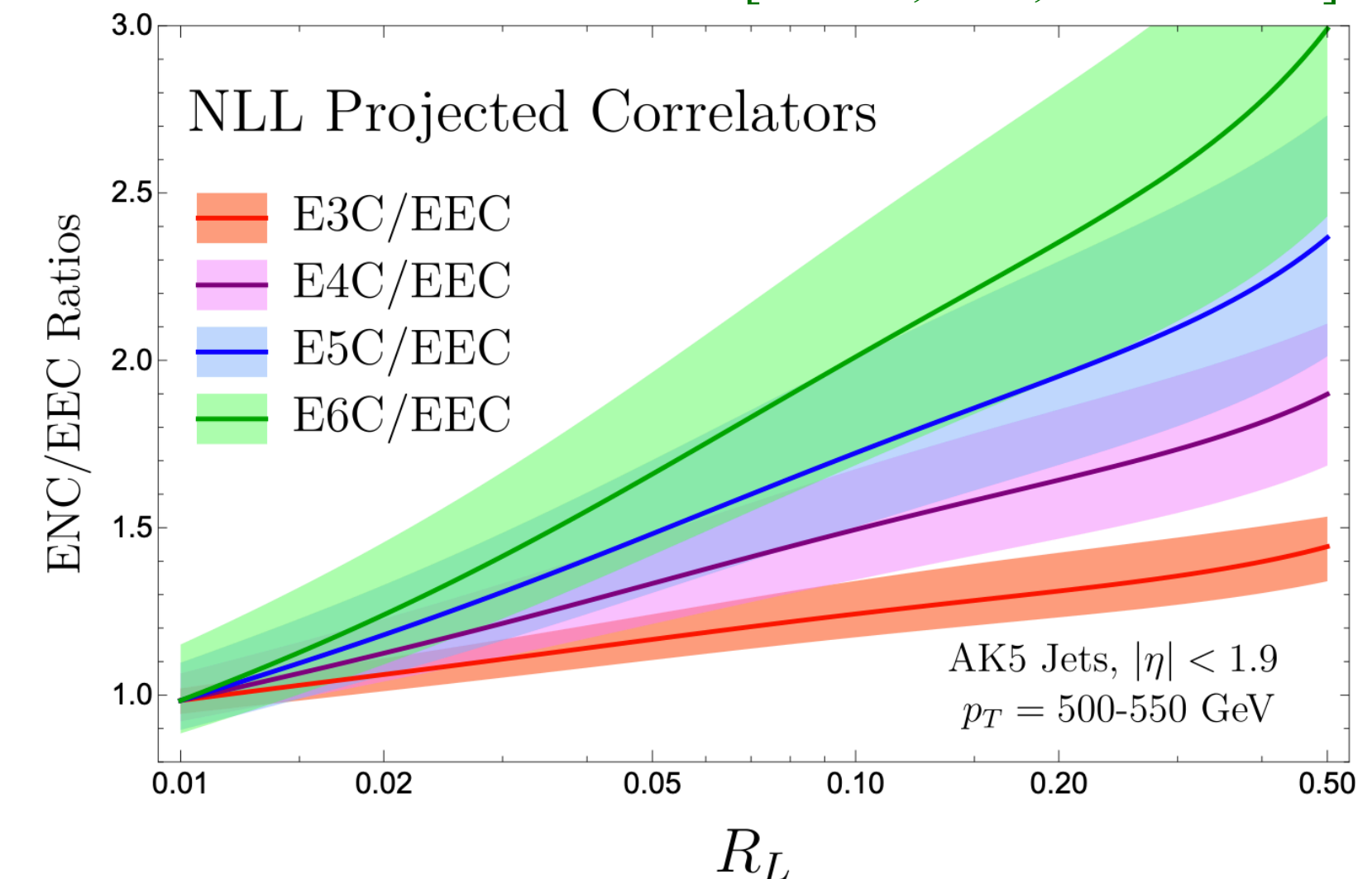


ENCs have been measured in QCD and they provide a wealth of interesting information about the theory



$$\frac{\text{ENC}}{\text{EEC}} \propto R_L^{\gamma(N+1) - \gamma(3)}$$

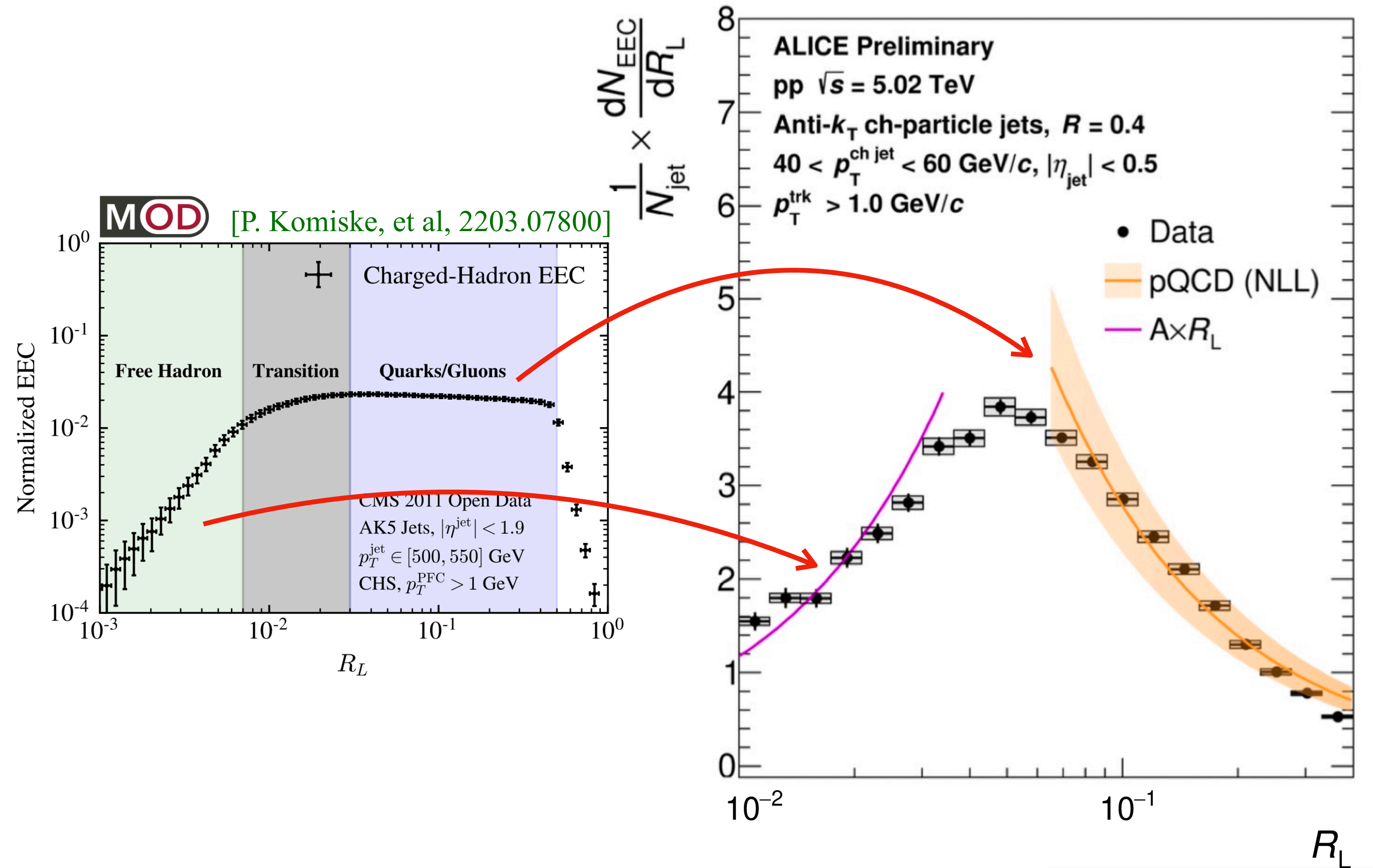
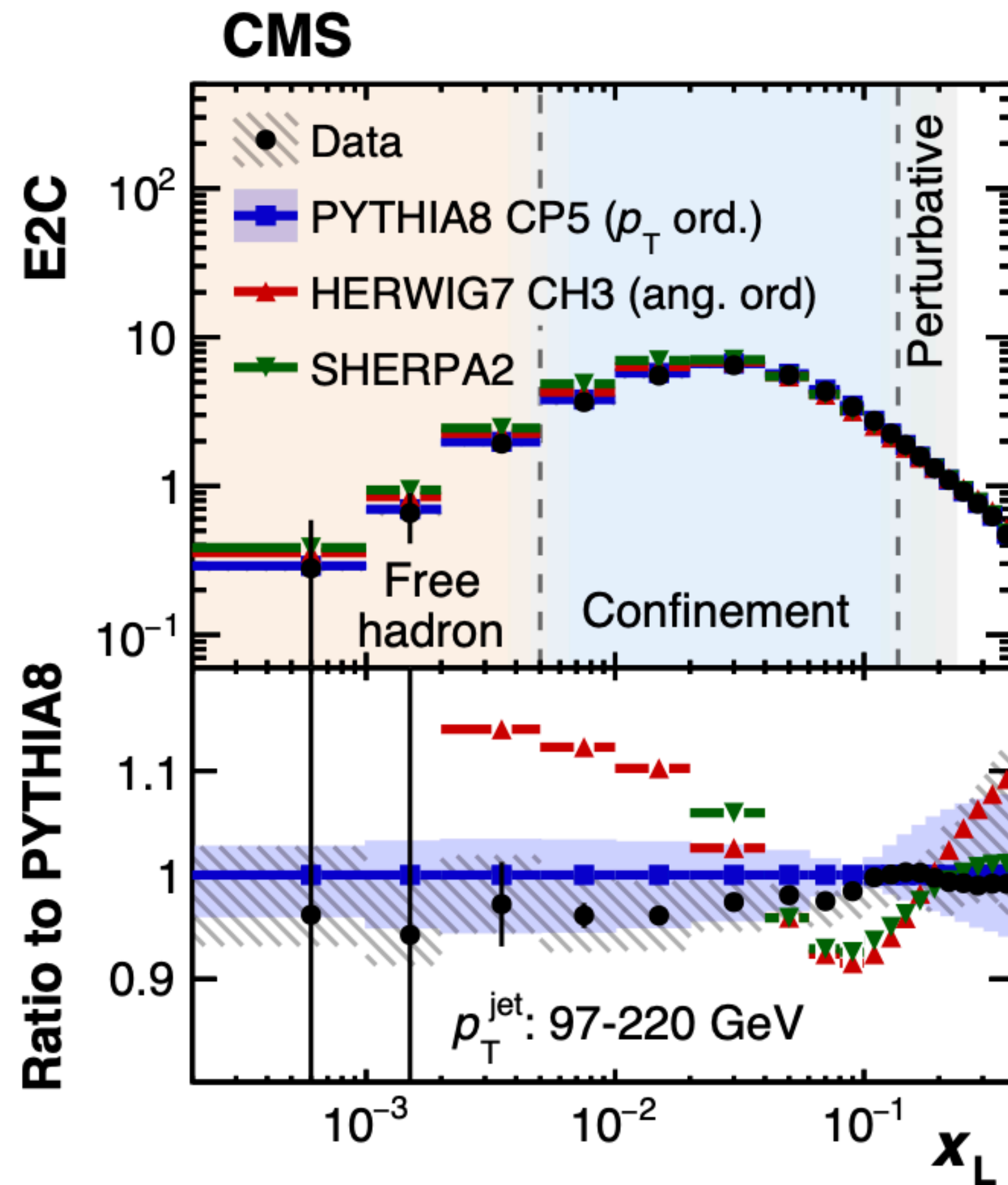
[K. Lee, et al, 2205.03414]



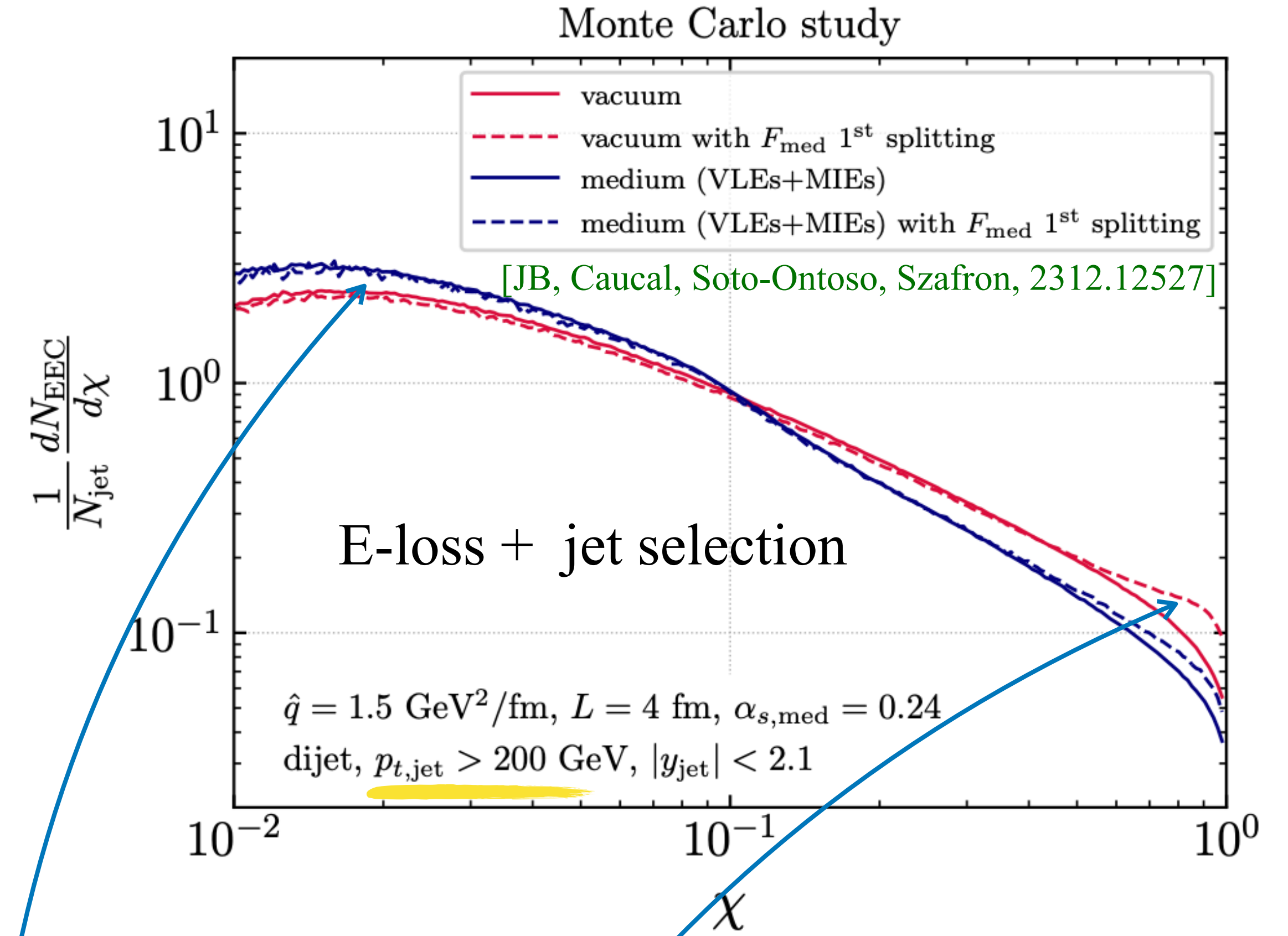
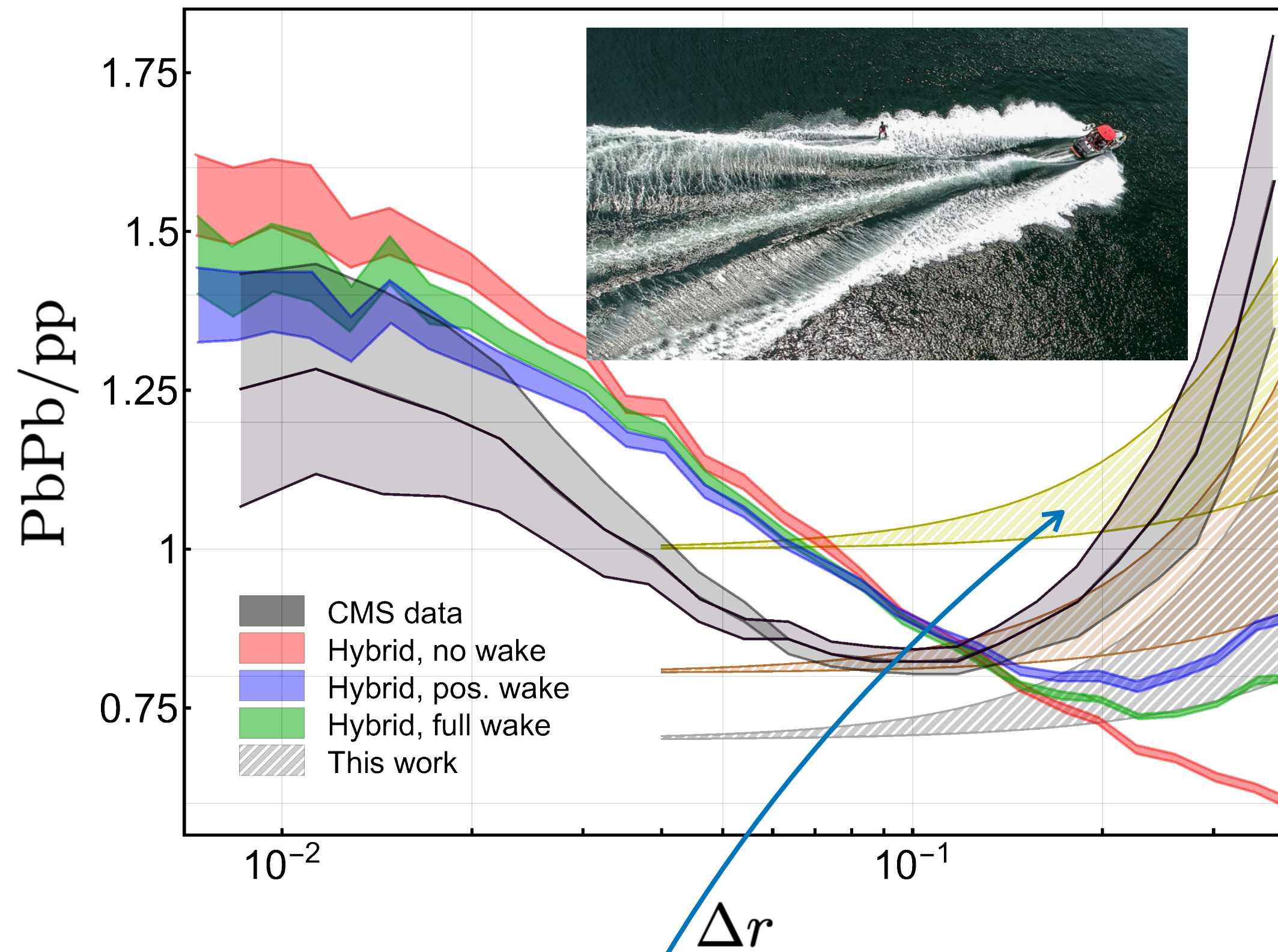
How to understand the structure of jets: Energy Correlators



ENCs have been measured in QCD and they provide a wealth of interesting information about the theory



How to understand the structure of jets: Energy Correlators



- Energy loss leads to suppression at large angles and enhancement at small ones (solid lines)
- Medium introduces slight enhancement at large angles, which competes with E-loss. The soft contribution can overwhelm this signal.

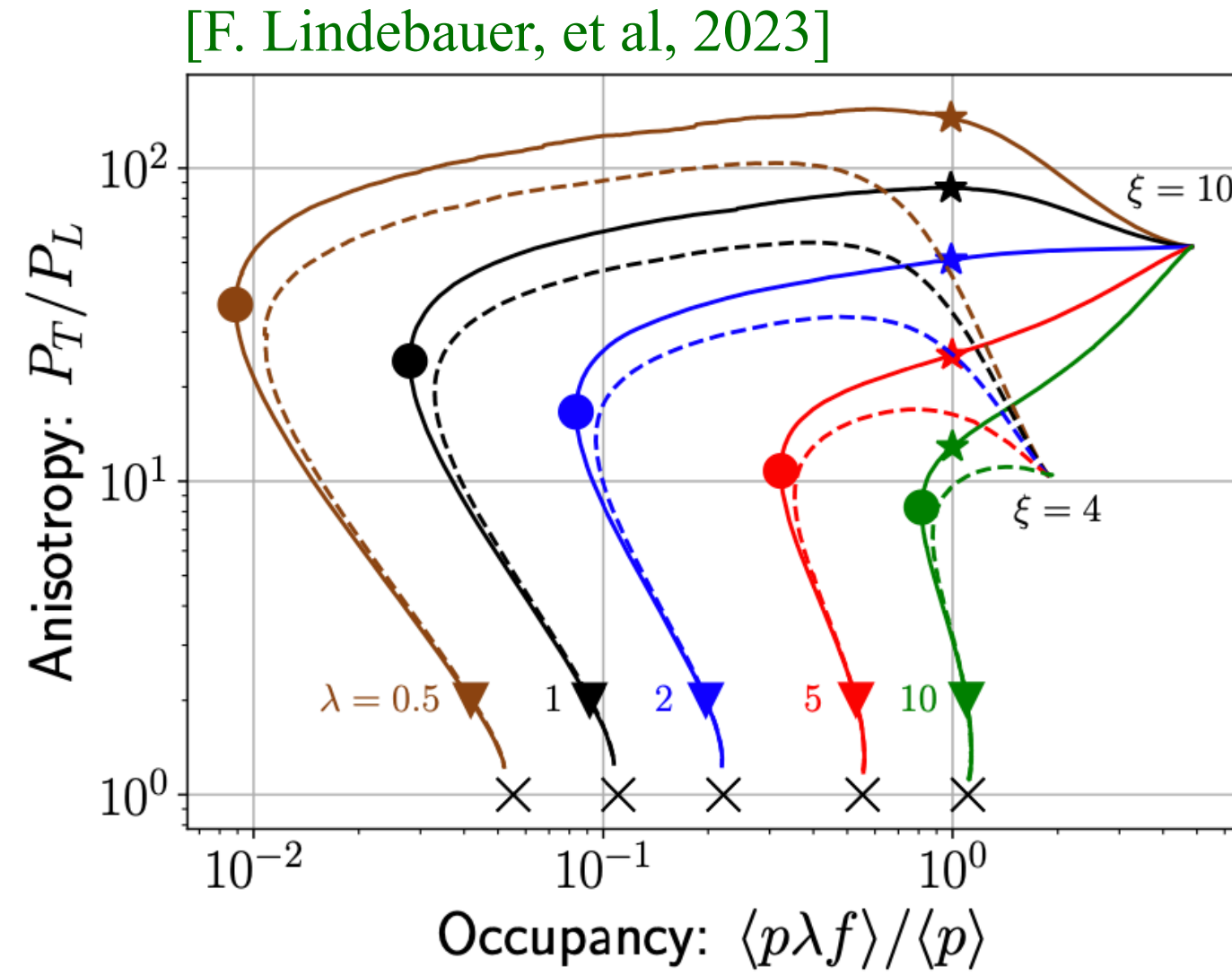


Jets in the early stages of HICs

Why are the early stages “different”



[See talk by Kirill later this week]



- At early times there is a big pressure anisotropy

- This reflects in an anisotropic transport coefficient

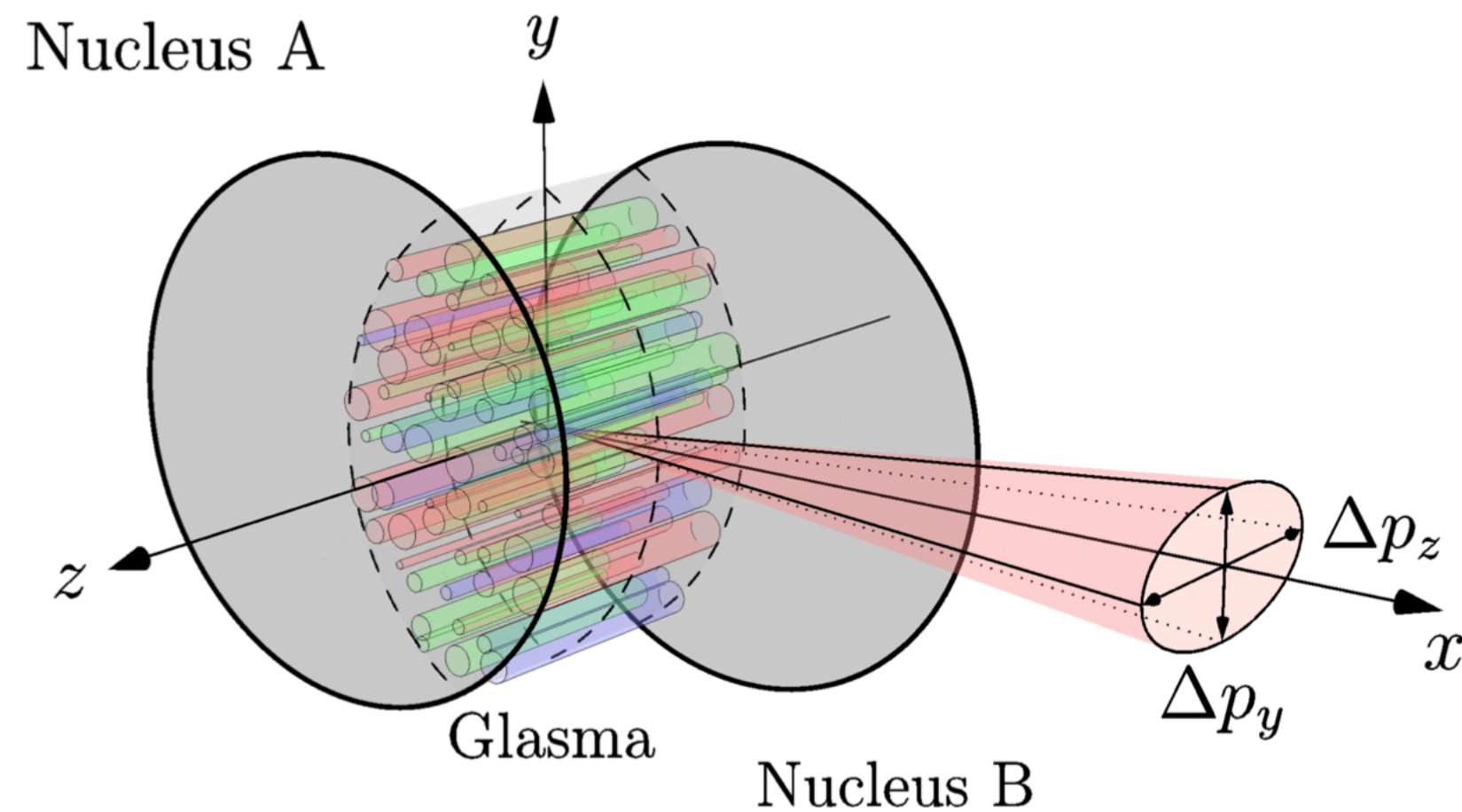
[Can be washed out by hydro expansion]

$$\hat{q}_x \gg \hat{q}_y$$

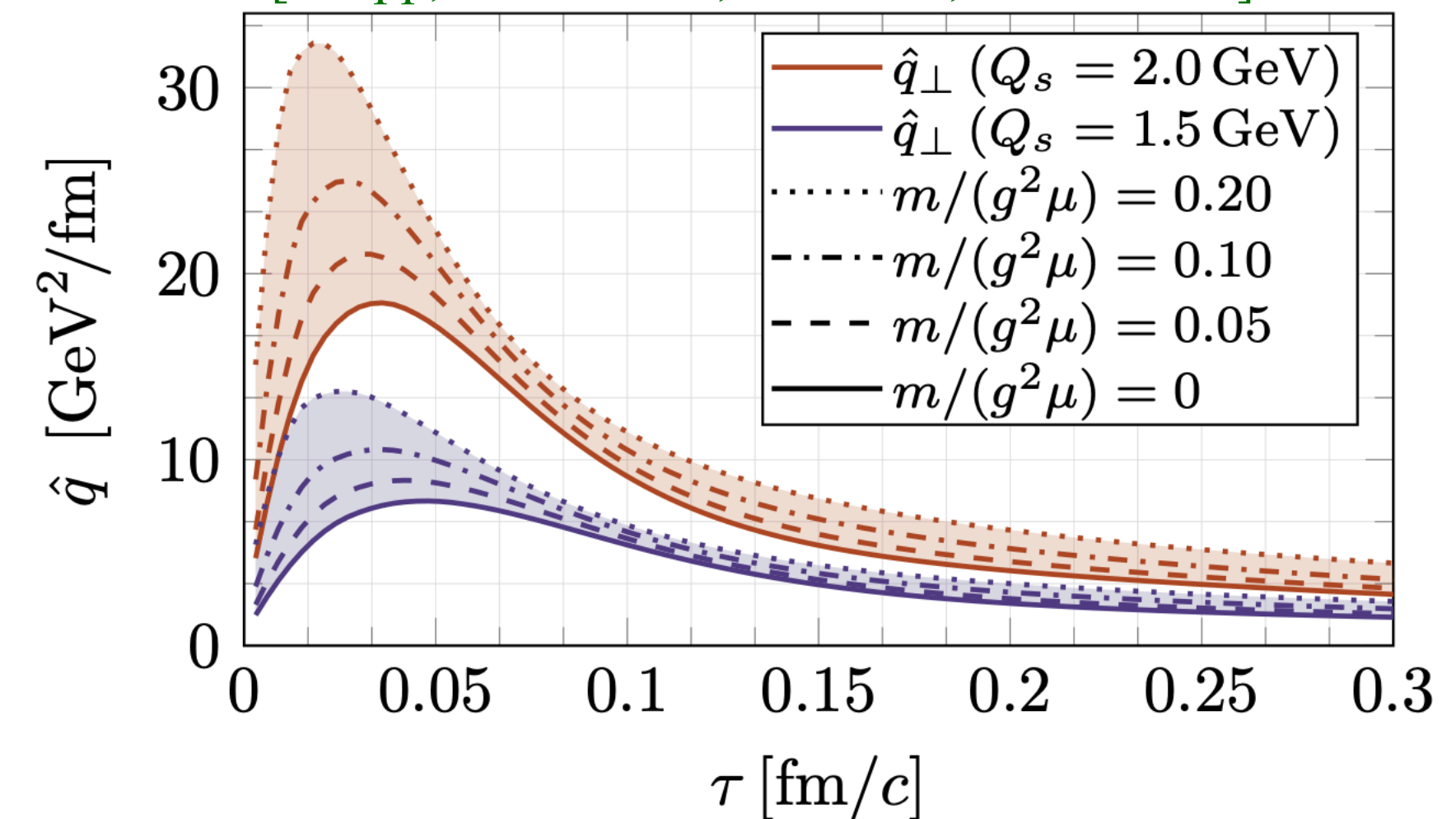
- Furthermore, the observed jet quenching coefficient seems to be much larger than the hydro one

[Observables integrate over jet path]

$$\hat{q}_{\text{early}} \gg \hat{q}_{\text{hydro}}, \tau_{\text{hydro}} \gg \tau_{\text{early}}$$



[A. Ipp, D. I. Muller, D. Schuh, 2009.14206]



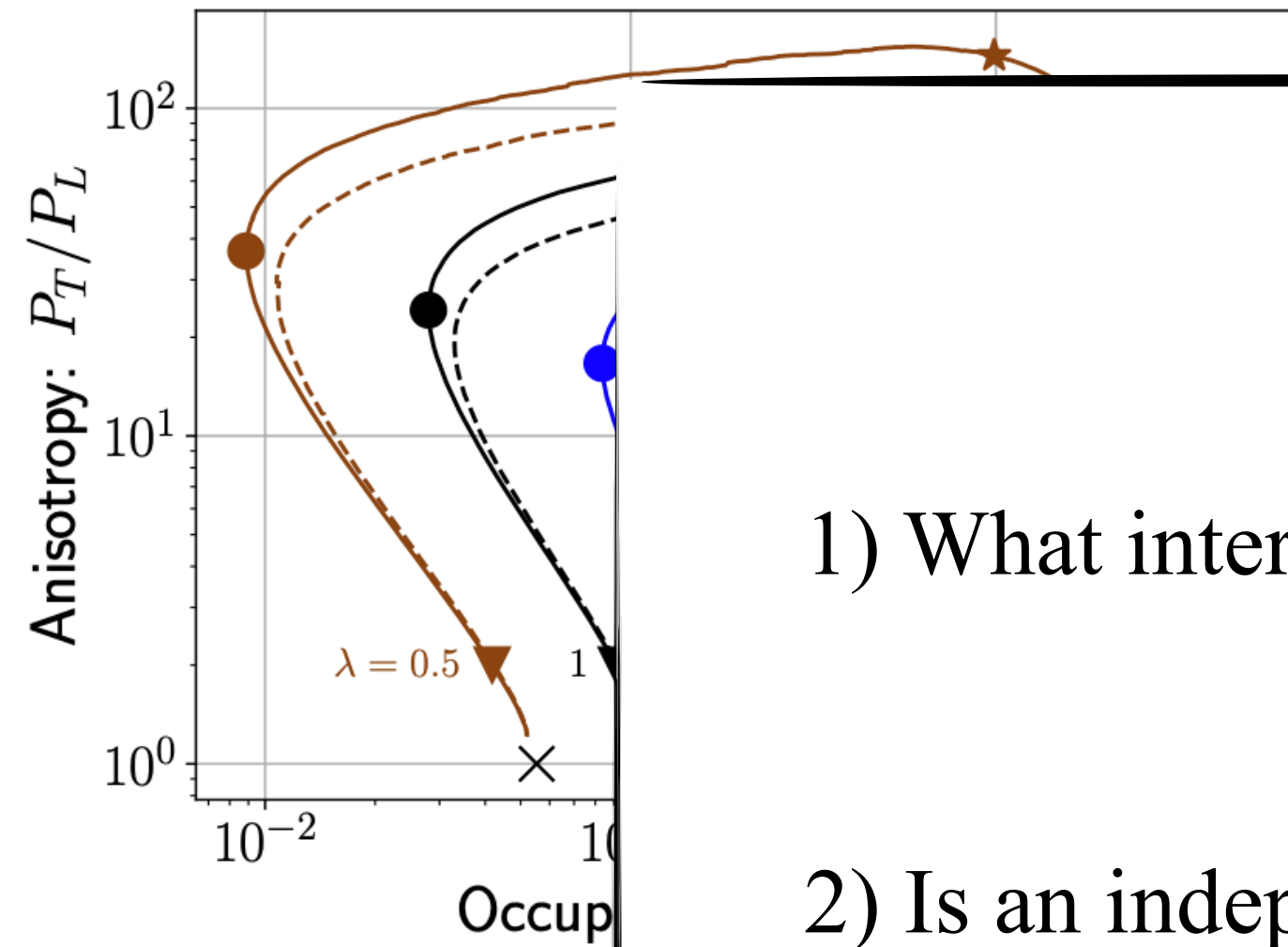
Why are the early stages “different”

[See talk by Kirill later this week]



- At early times there is a big pressure anisotropy

[F. Lindebauer, et al, 2023]



1) What interesting features can we see from early time anisotropies?

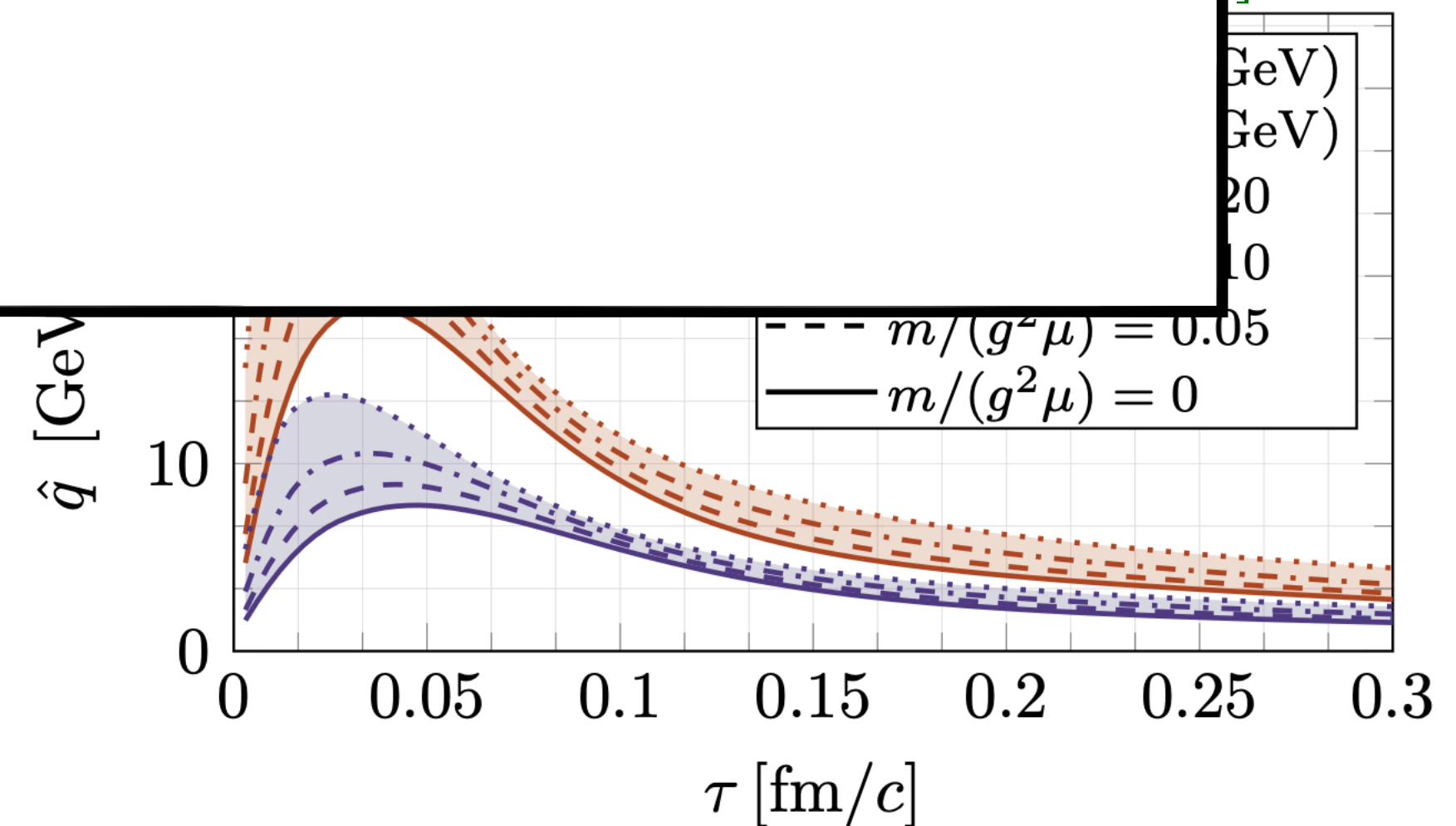
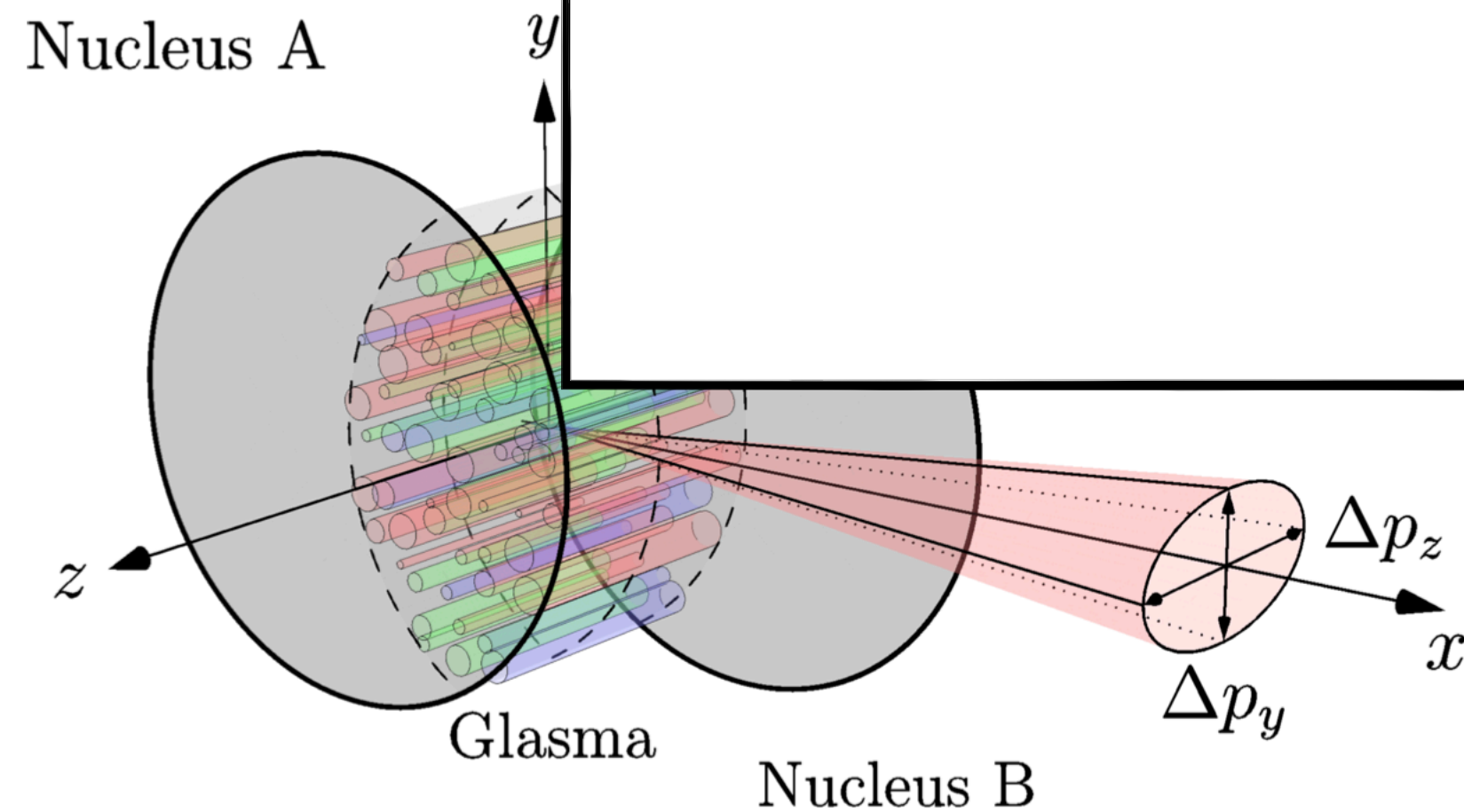
2) Is an independent multiple scattering picture still meaningful ?

coefficient
[d out by hydro expansion]

coefficient

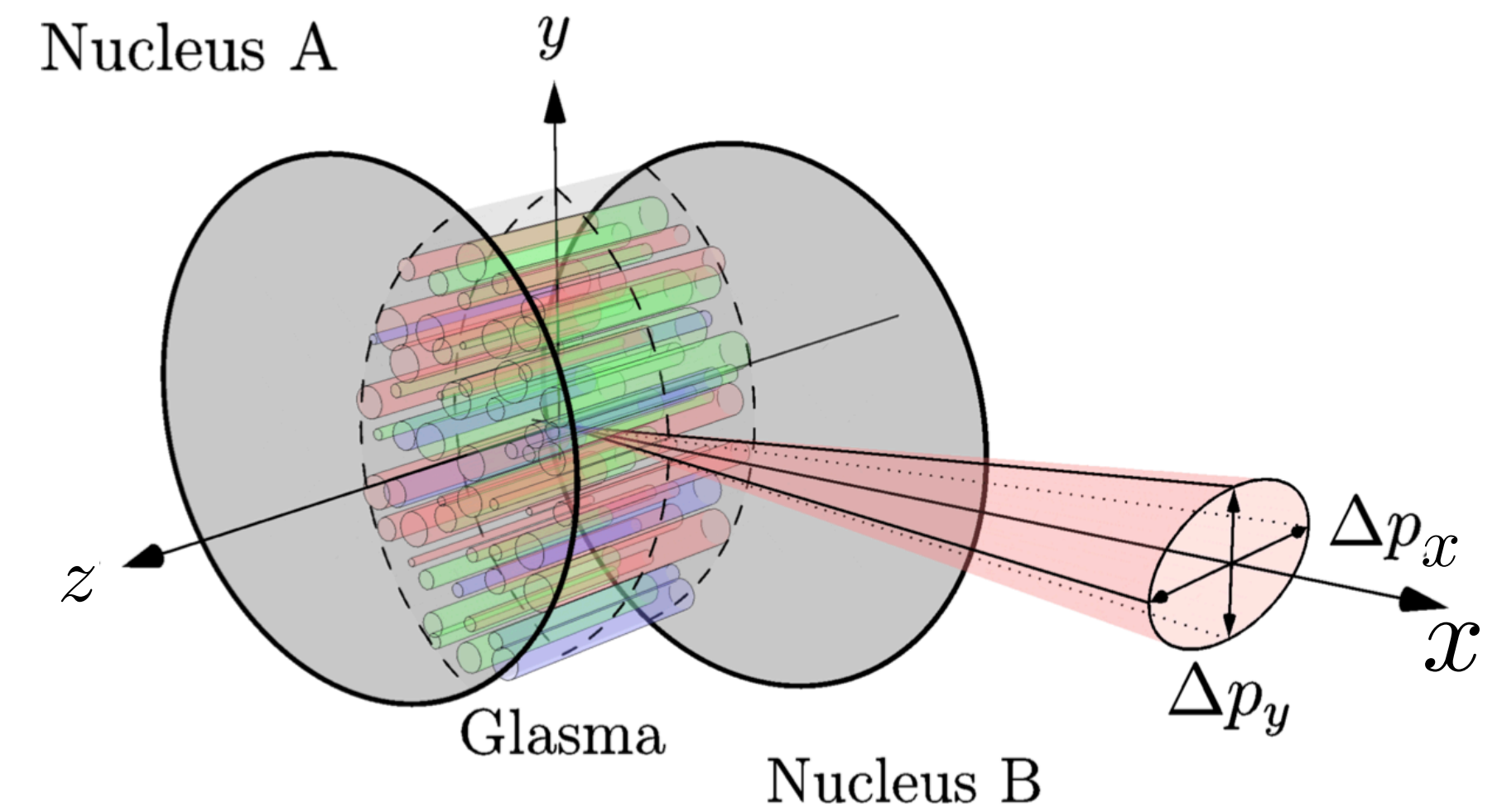
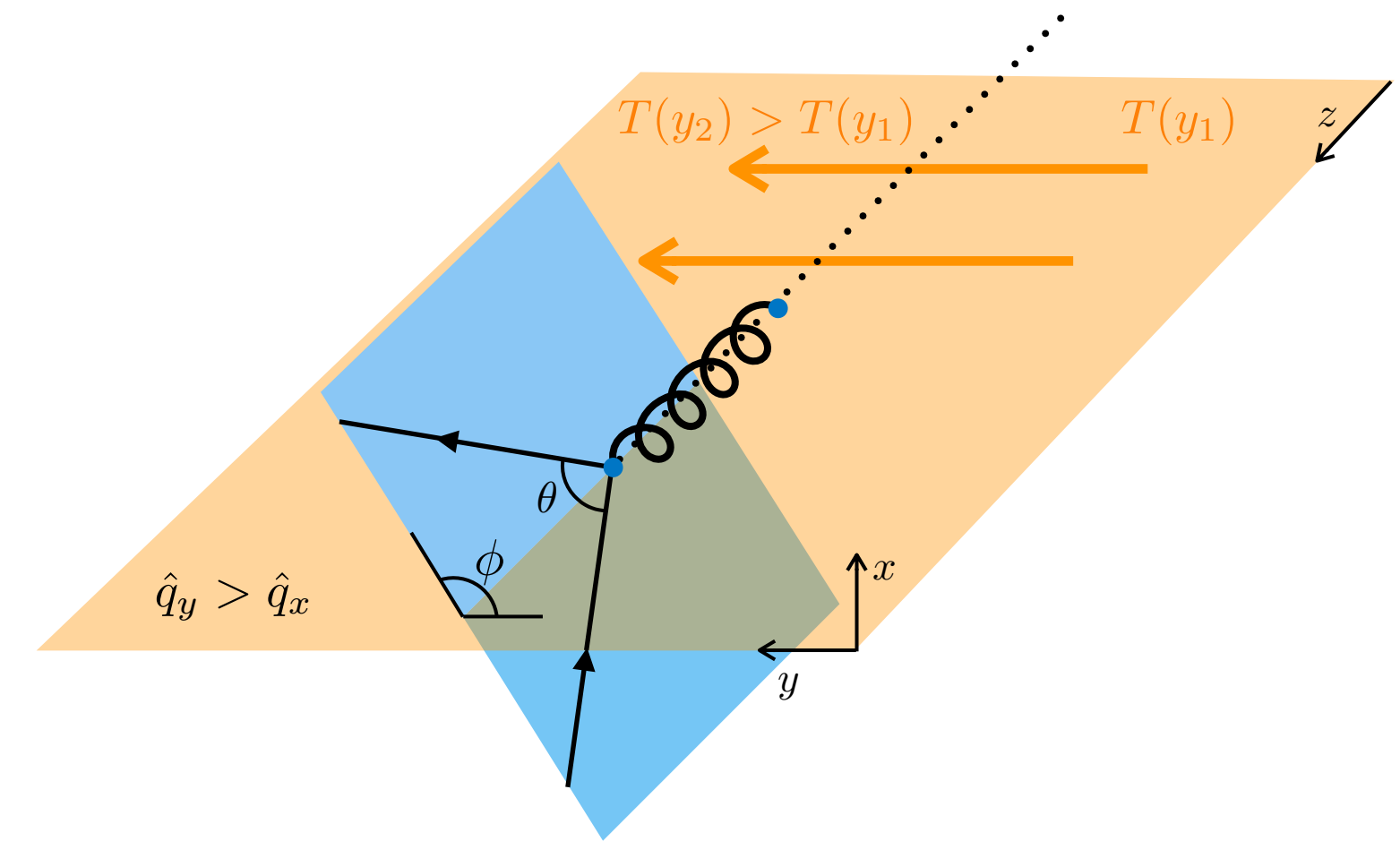
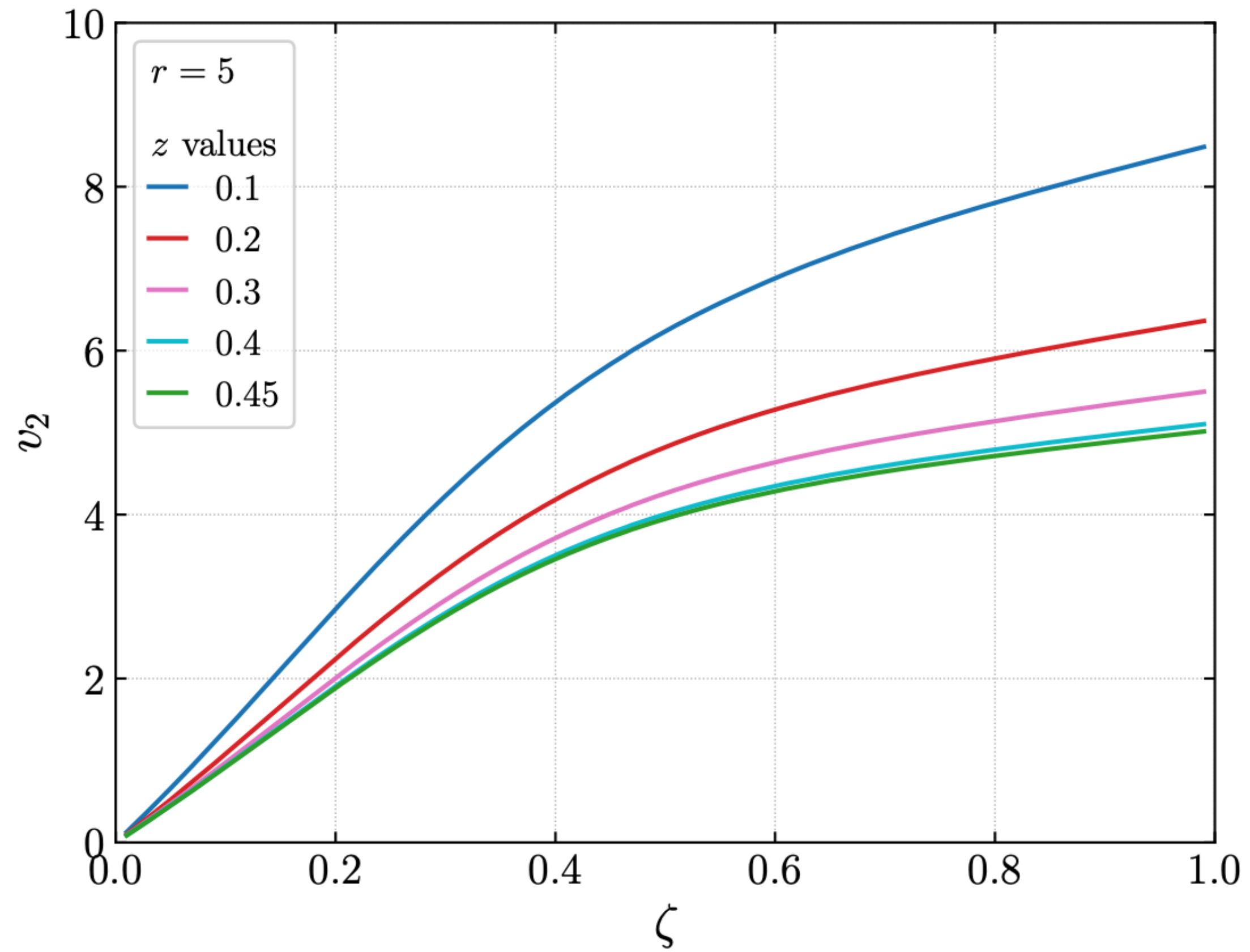
observables integrate over jet path]

early



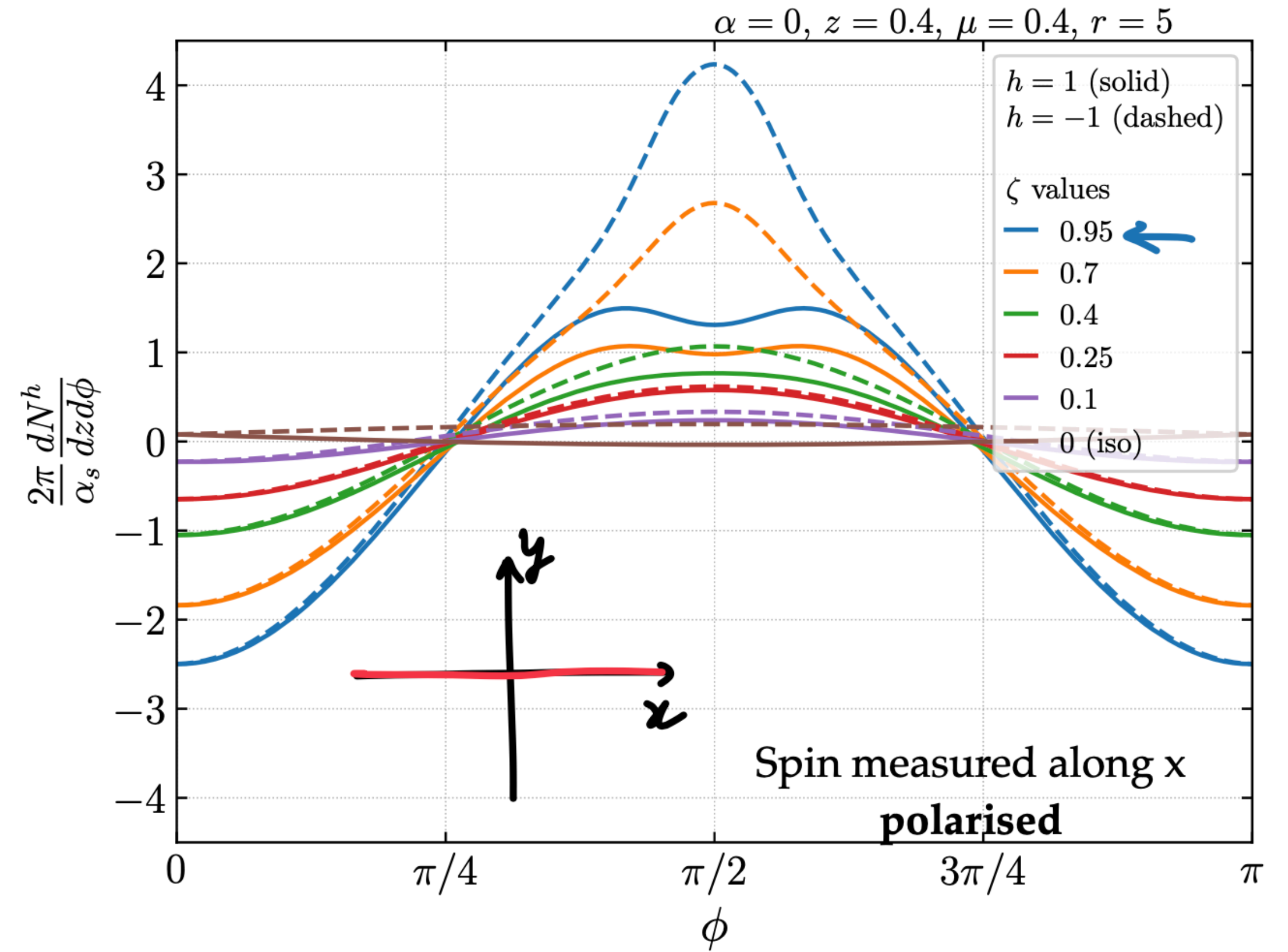
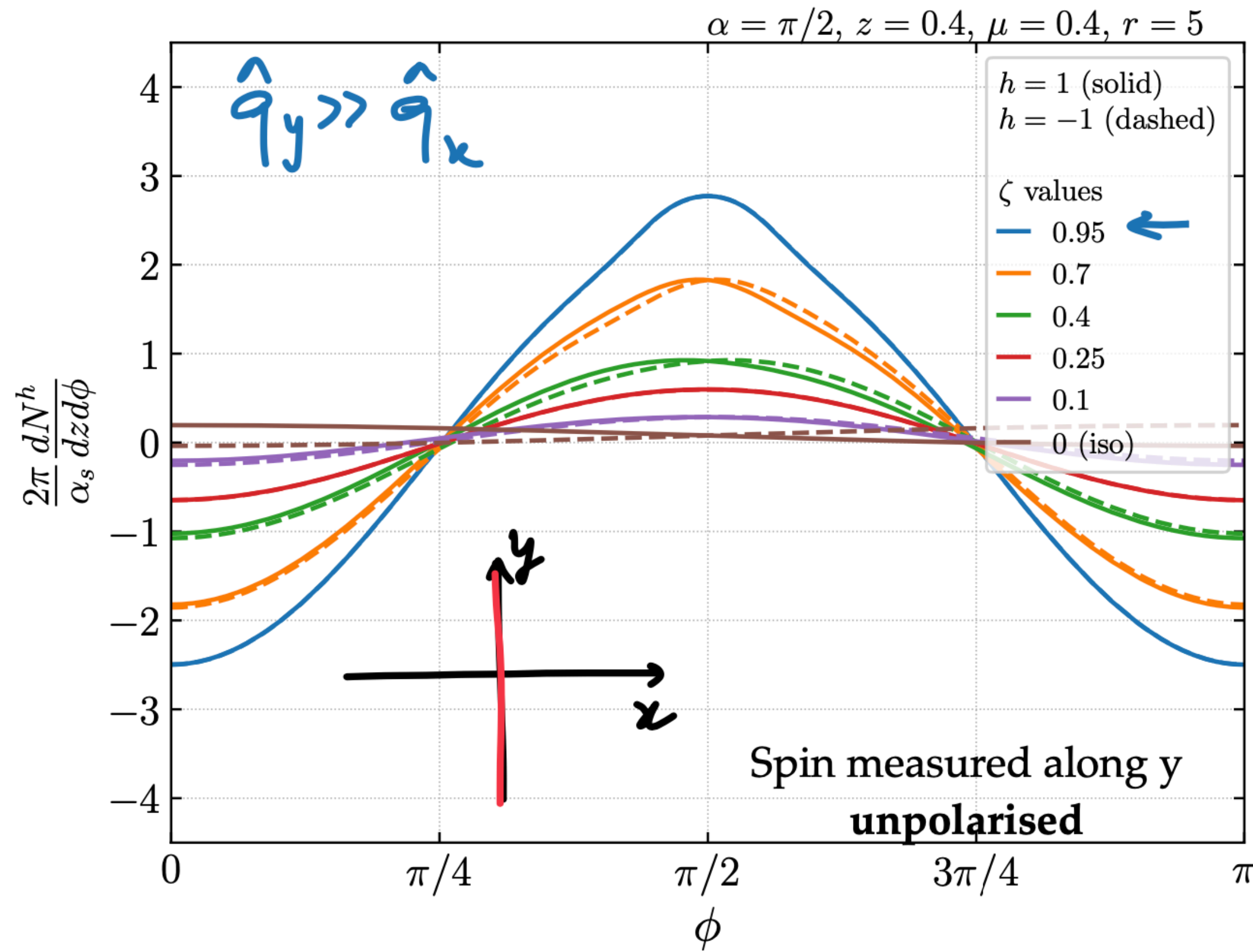


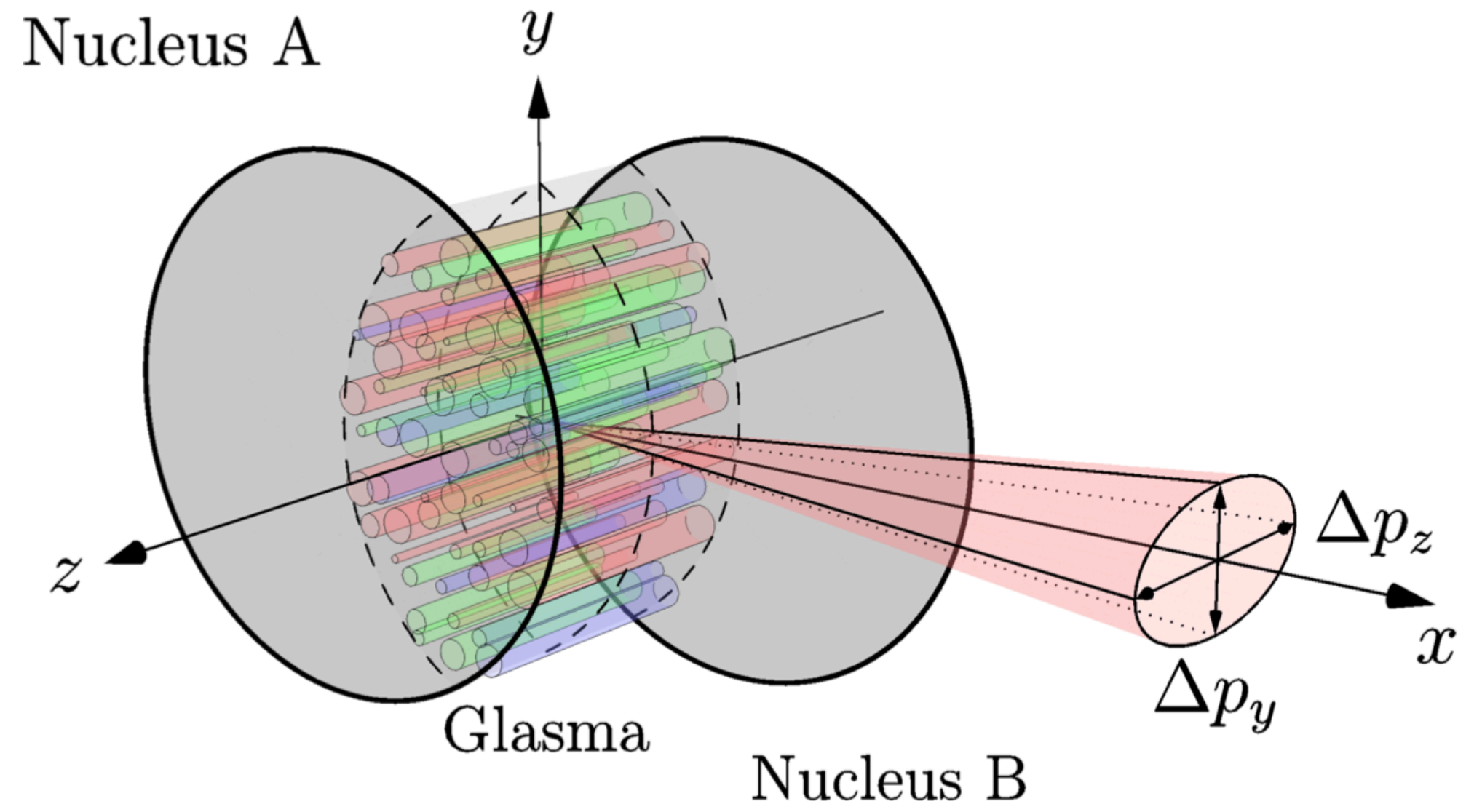
$$\zeta = \frac{\sqrt{\hat{q}_y} - \sqrt{\hat{q}_x}}{\sqrt{\hat{q}_y} + \sqrt{\hat{q}_x}}, \quad r = L^+ \frac{(\sqrt{\hat{q}_y} + \sqrt{\hat{q}_x})}{2\sqrt{q_0^+}}$$



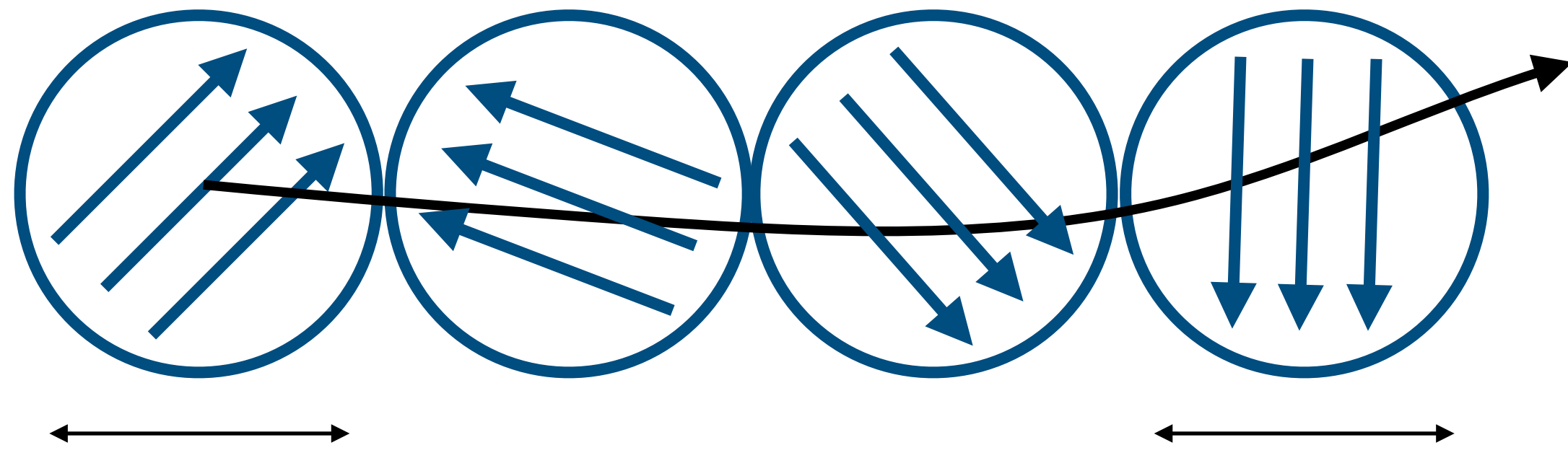
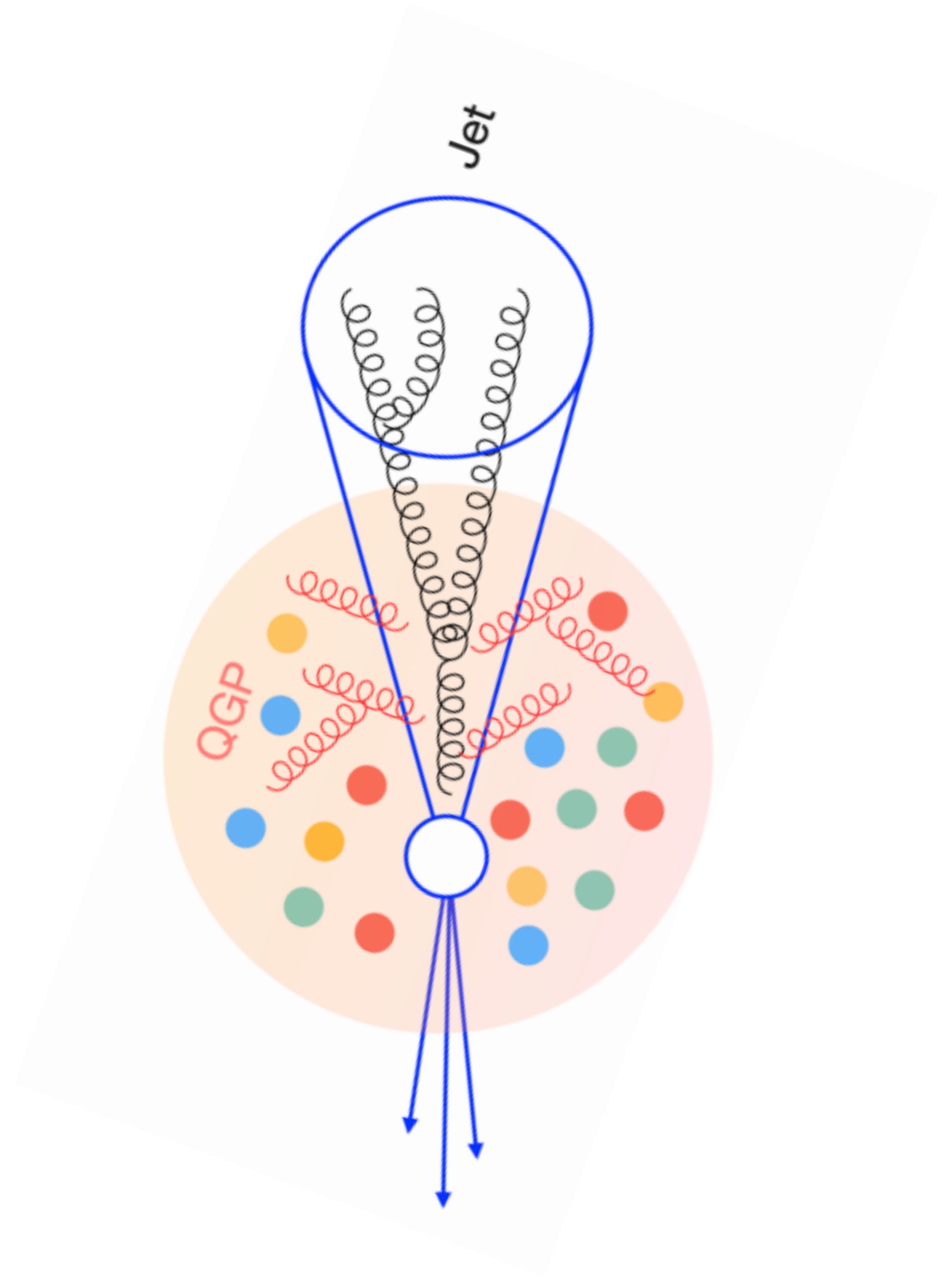


$$\zeta = \frac{\sqrt{\hat{q}_y} - \sqrt{\hat{q}_x}}{\sqrt{\hat{q}_y} + \sqrt{\hat{q}_x}}, \quad r = L^+ \frac{(\sqrt{\hat{q}_y} + \sqrt{\hat{q}_x})}{2\sqrt{q_0^+}}, \quad \mu = \frac{\sqrt{2}m^2}{(\sqrt{\hat{q}_y} + \sqrt{\hat{q}_x})\sqrt{q_0^+}}$$





??
=

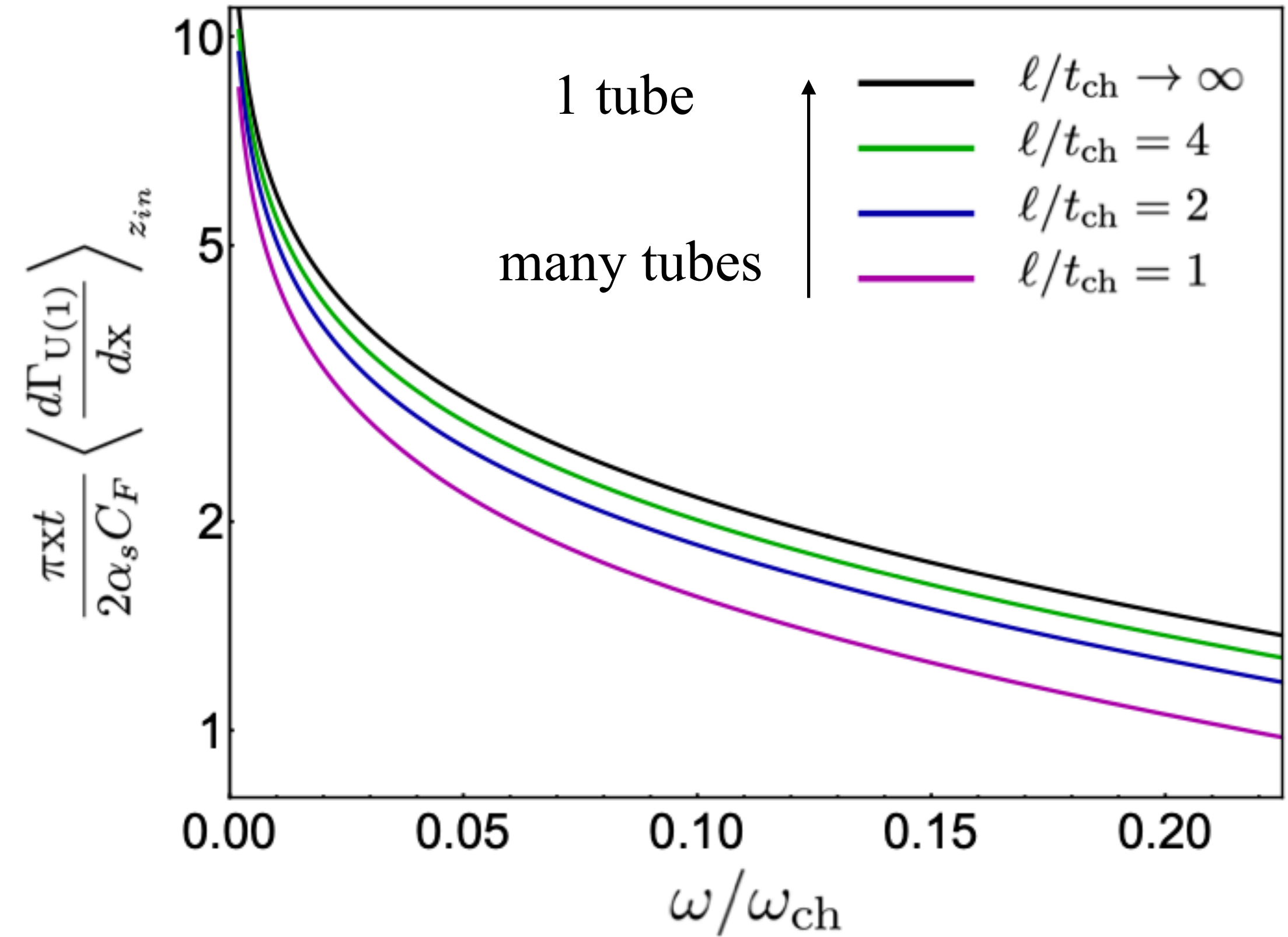
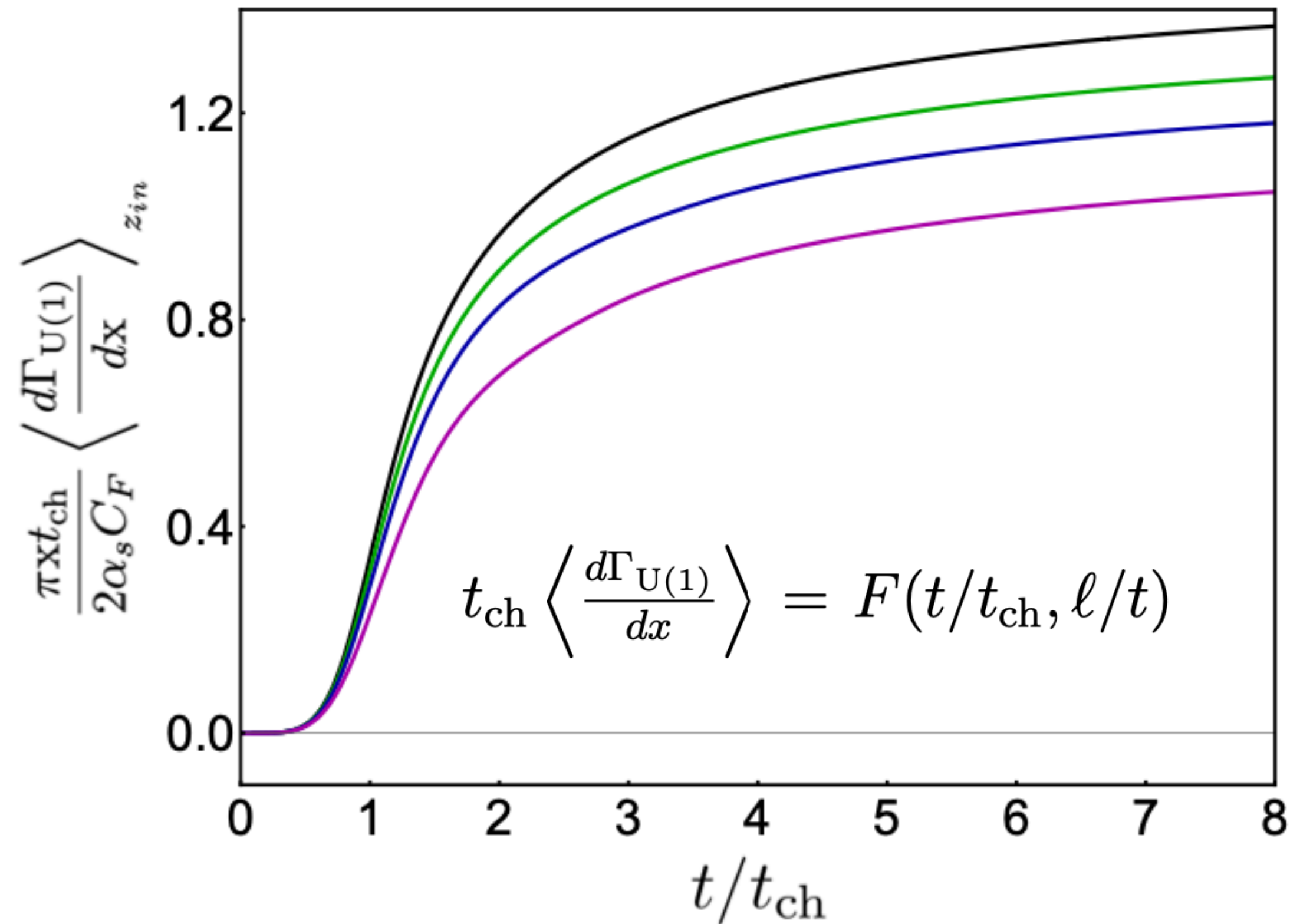


Synchrotron like scenario

$$l \sim 1/Q_s$$



More flux tubes = longer formation time = lower rate



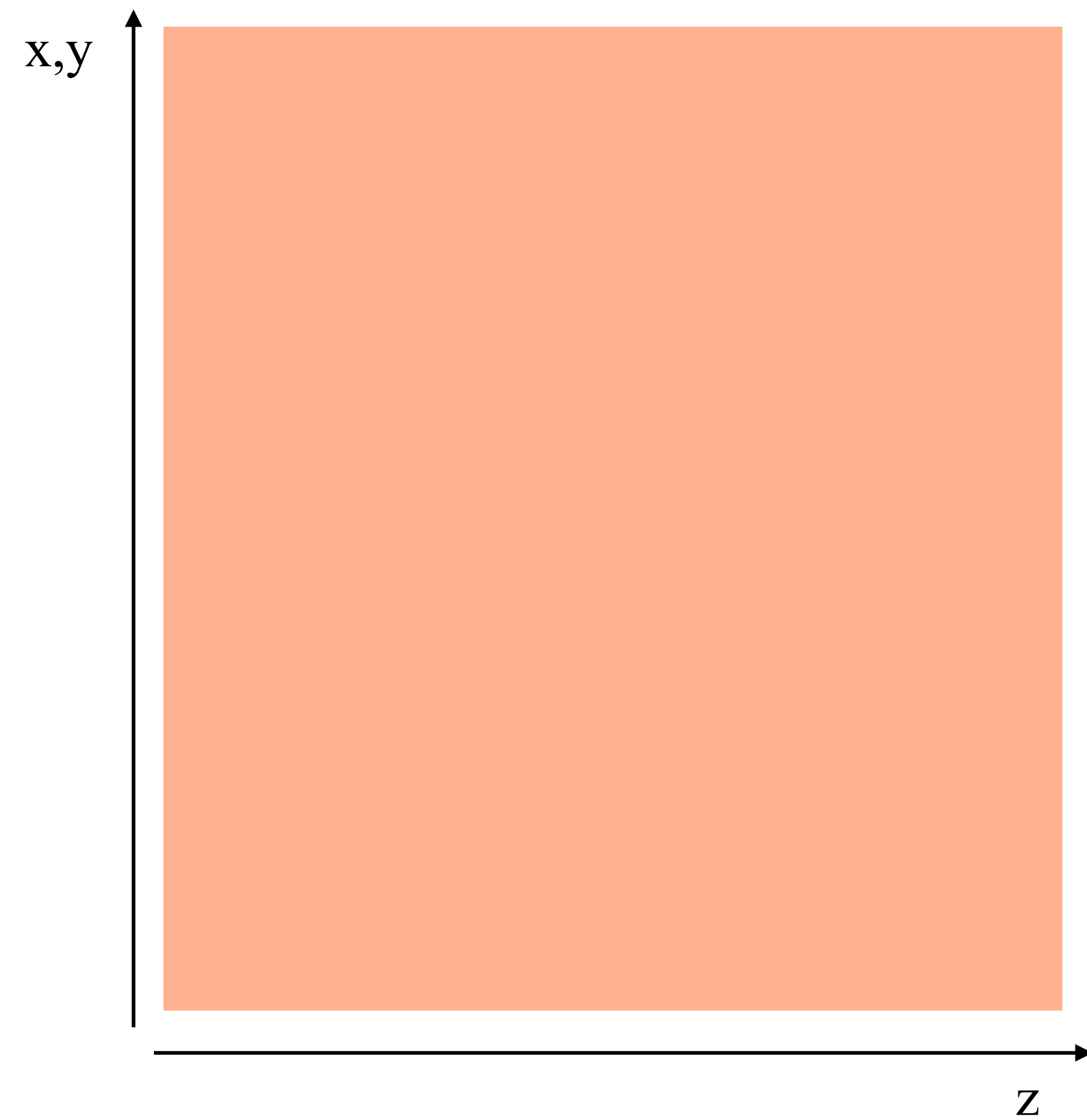
It is very important to go beyond QGP-like picture for these stages !



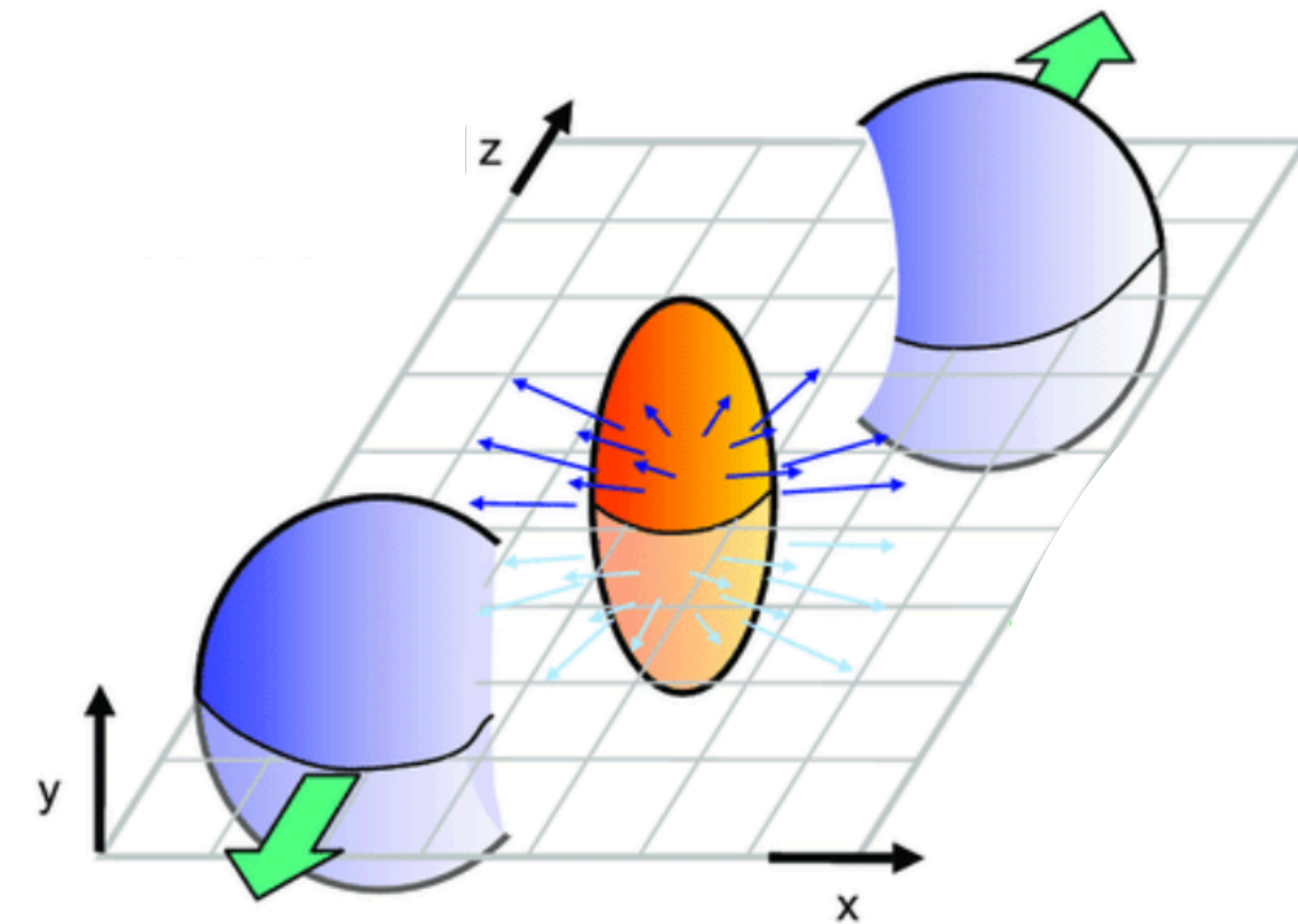
Jets in anisotropic and flowing matter

Why?

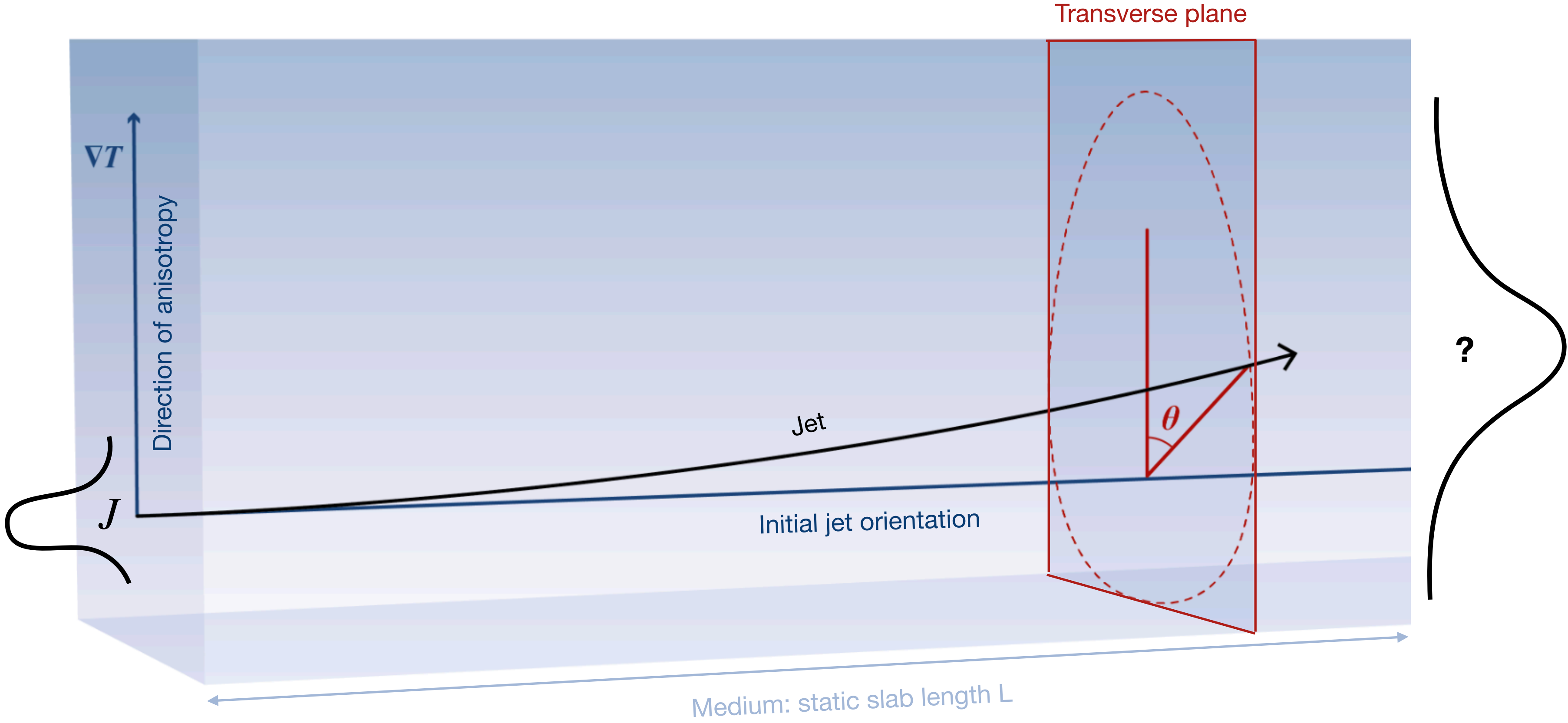
An infinitely long static medium as used in model calculations...



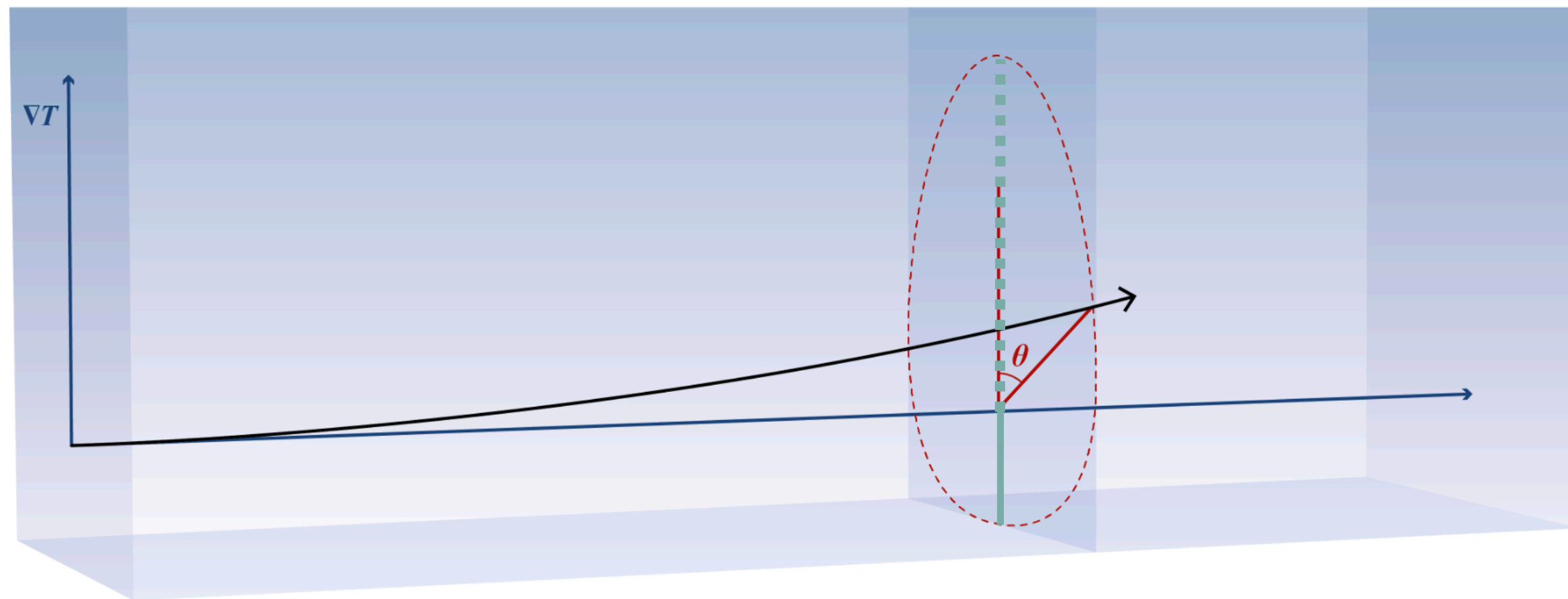
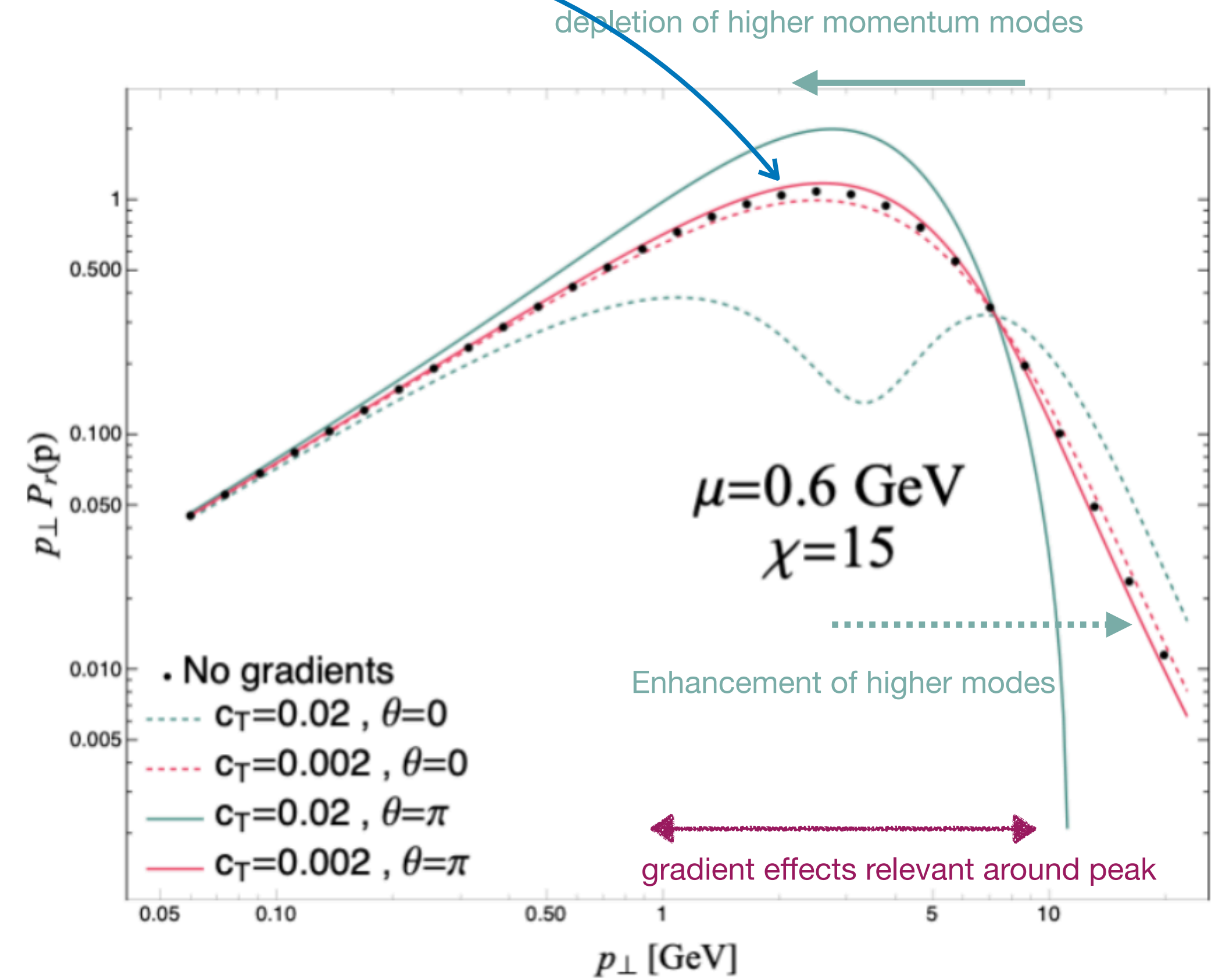
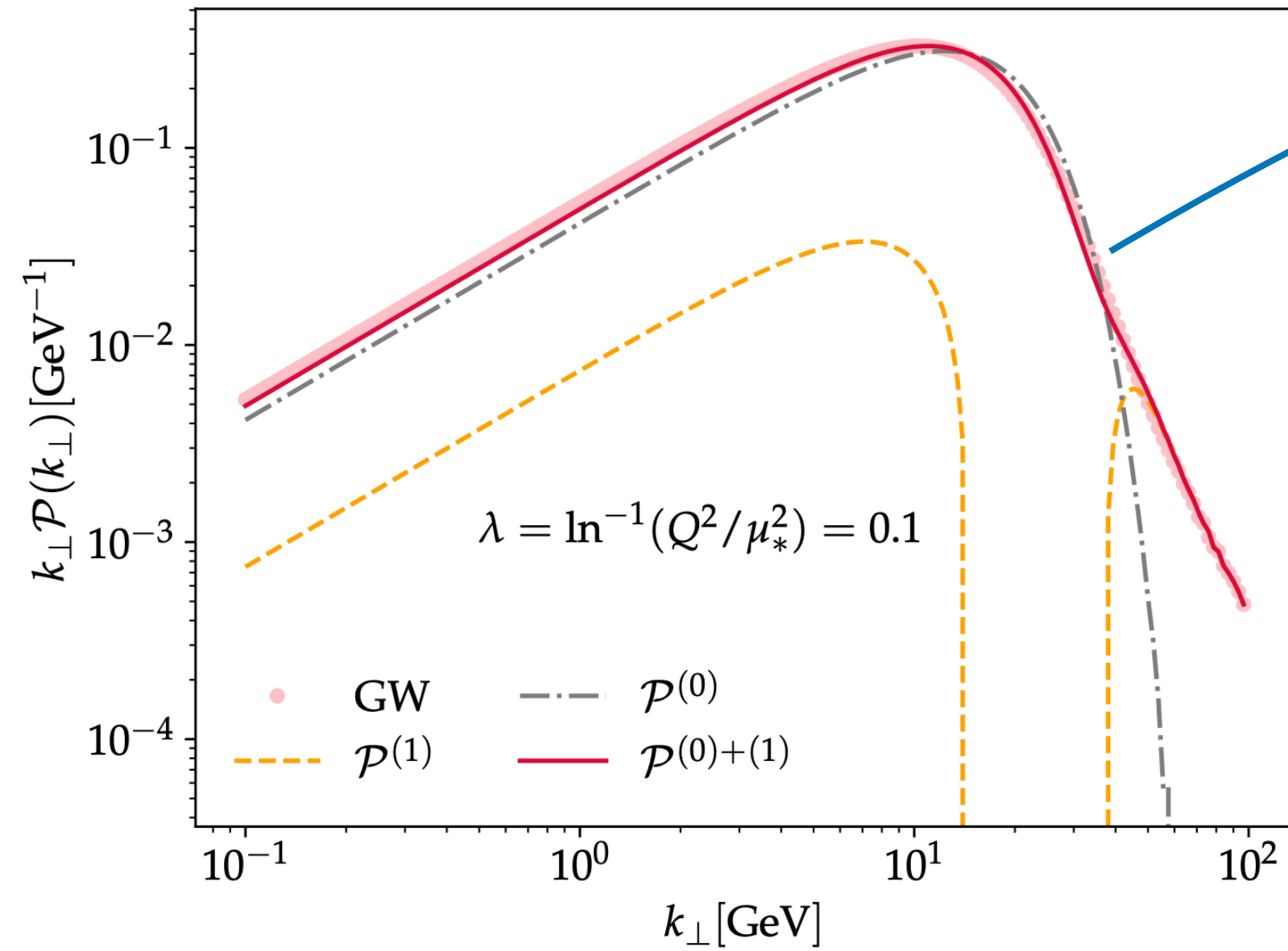
... might not be a good approximation to a real droplet



Jet evolution in structured matter: momentum broadening

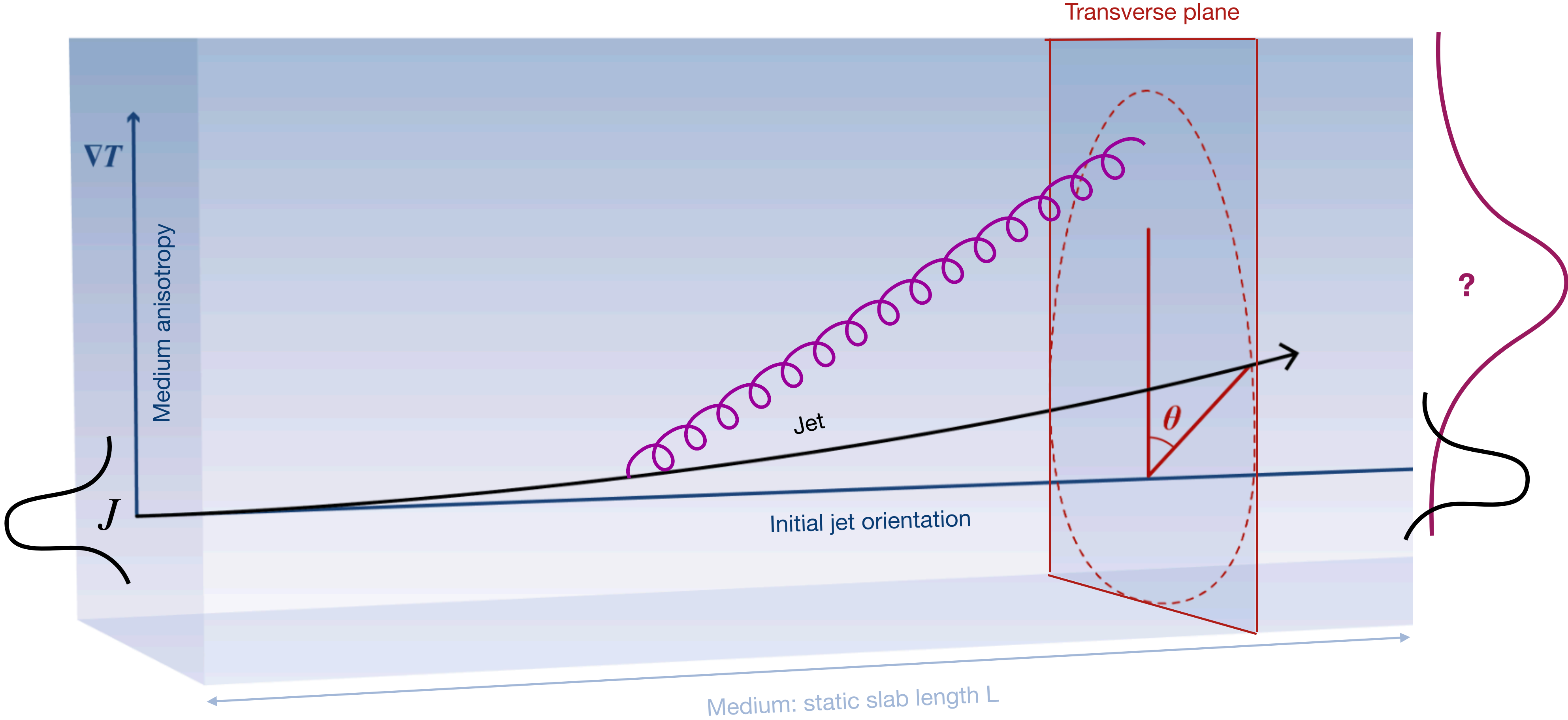


Jet evolution in structured matter: momentum broadening



The full distribution is written in terms of the angle θ and parameter $c_T \equiv \left| \frac{\nabla T}{ET} \right|$.

Jet evolution in structured matter: gluon radiation



Jet evolution in structured matter: momentum broadening

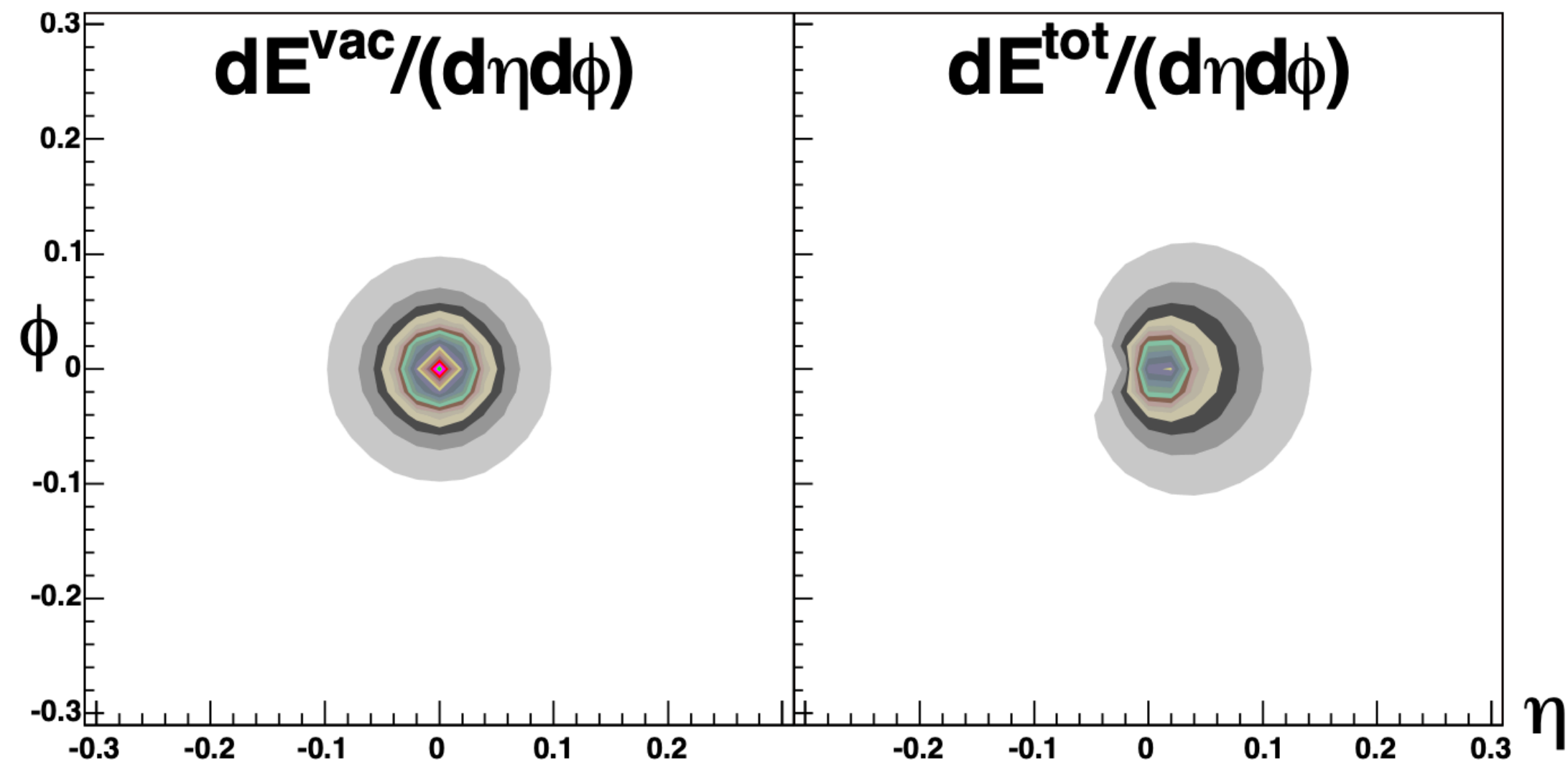


The presence of anisotropies leads to a non-trivial azimuthal structure for radiation flow. The same occurs with flowing matter.

Observable: jet shape density

$$(2\pi)p_t^{\text{jet}} \frac{d\rho(r)}{d\omega d\alpha} = 1 - 2\pi \int_{\omega r}^{\omega} dk k \omega \frac{dI}{d\omega d^2k}$$

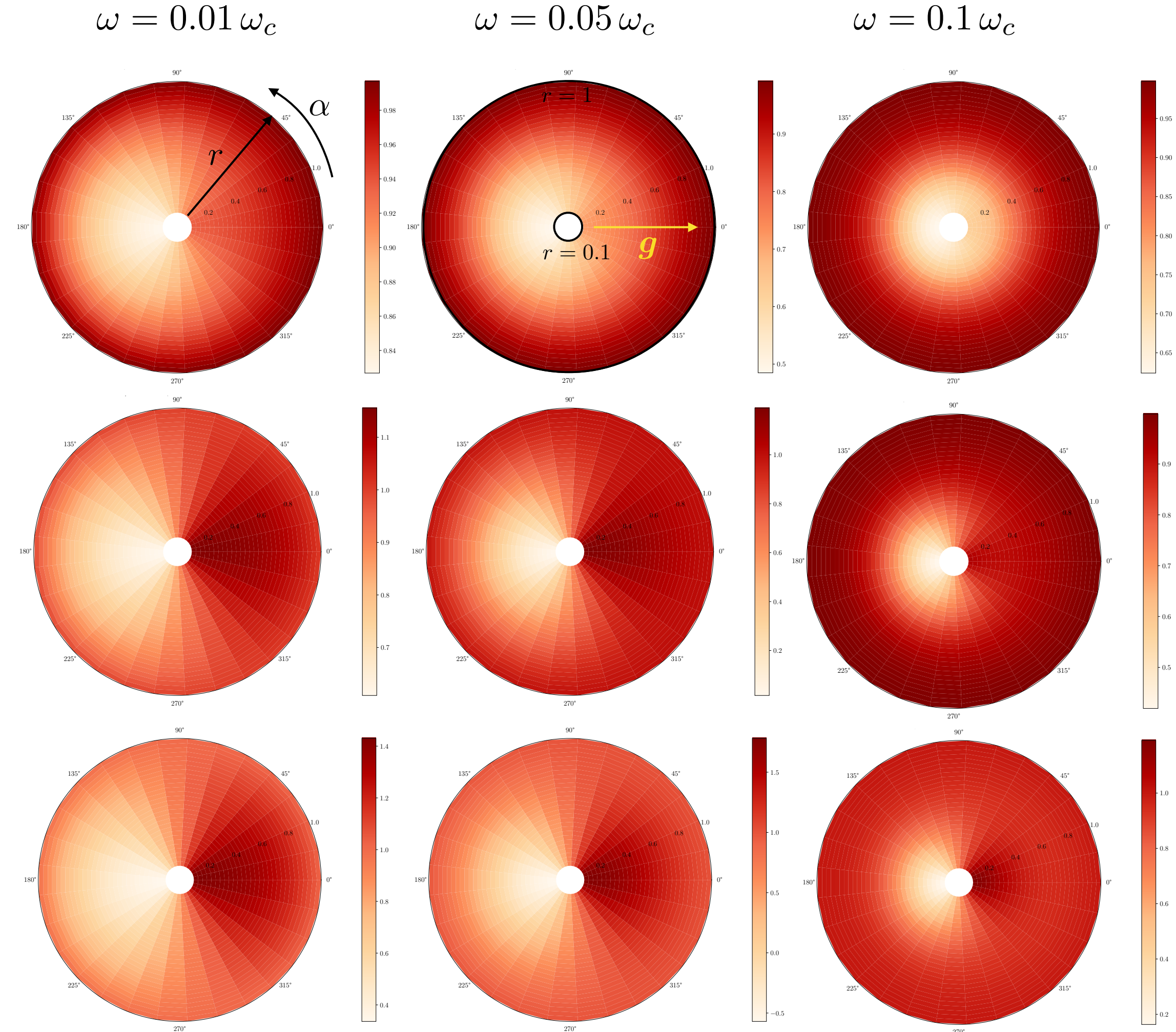
[Armesto, Salgado, Wiedemann, 2004]



$\gamma_T = 0.1$

$\gamma_T = 0.5$

$\gamma_T = 1$



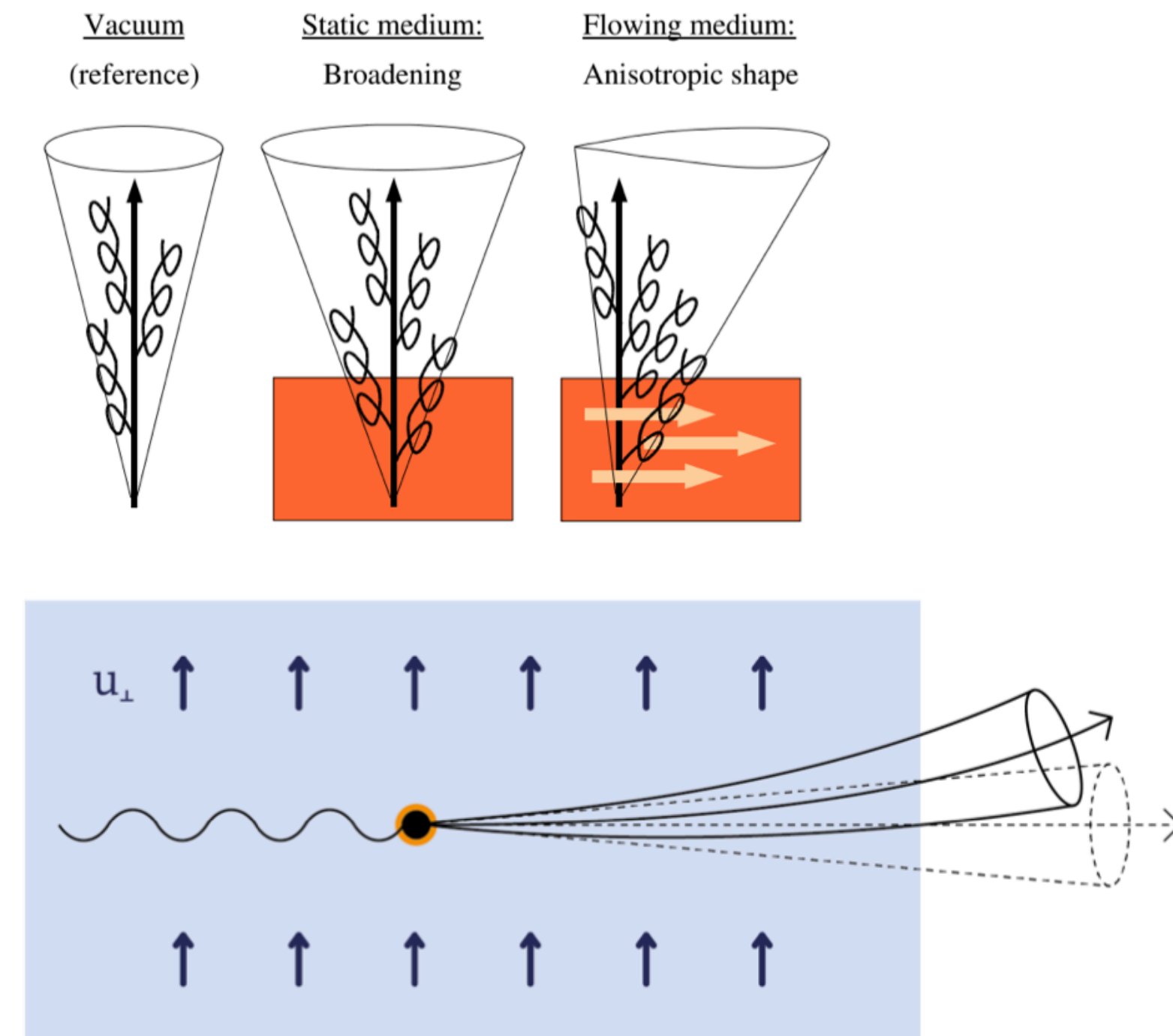
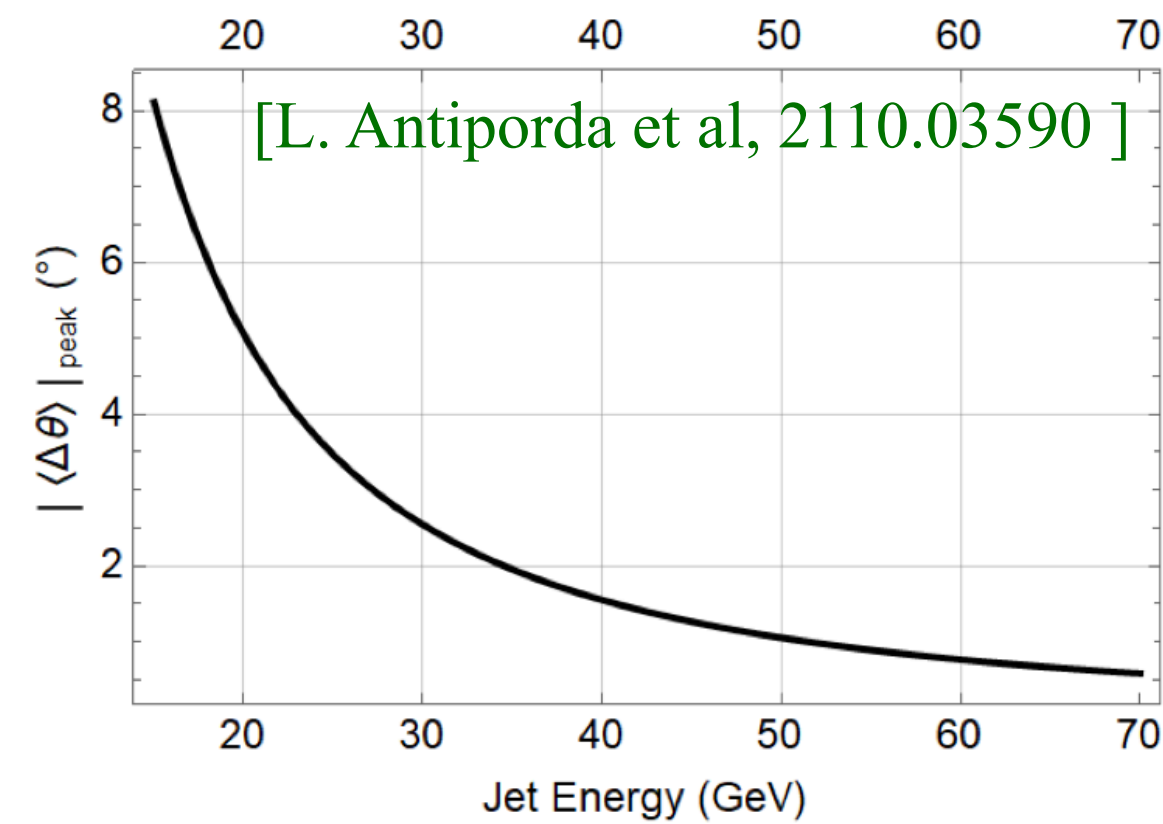
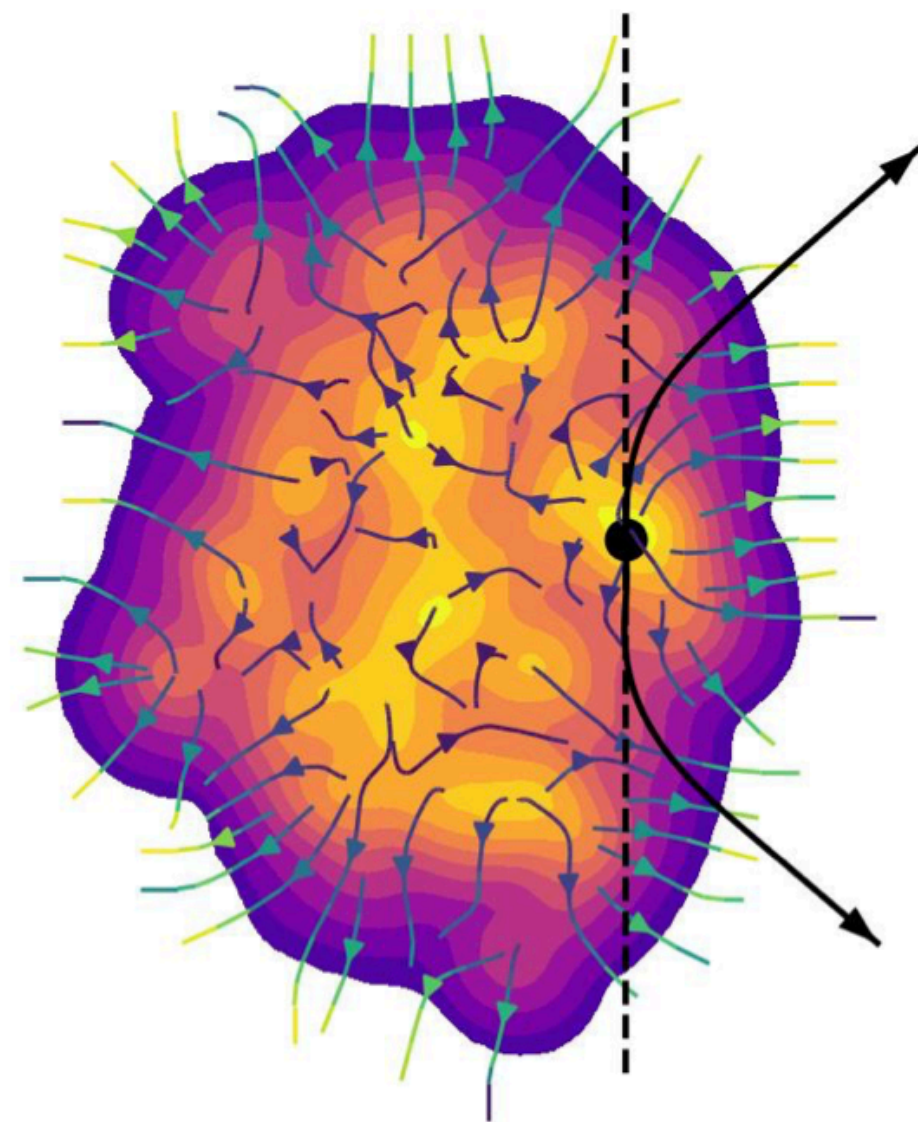
The Landscape

Jet evolution in hydrodynamical phase

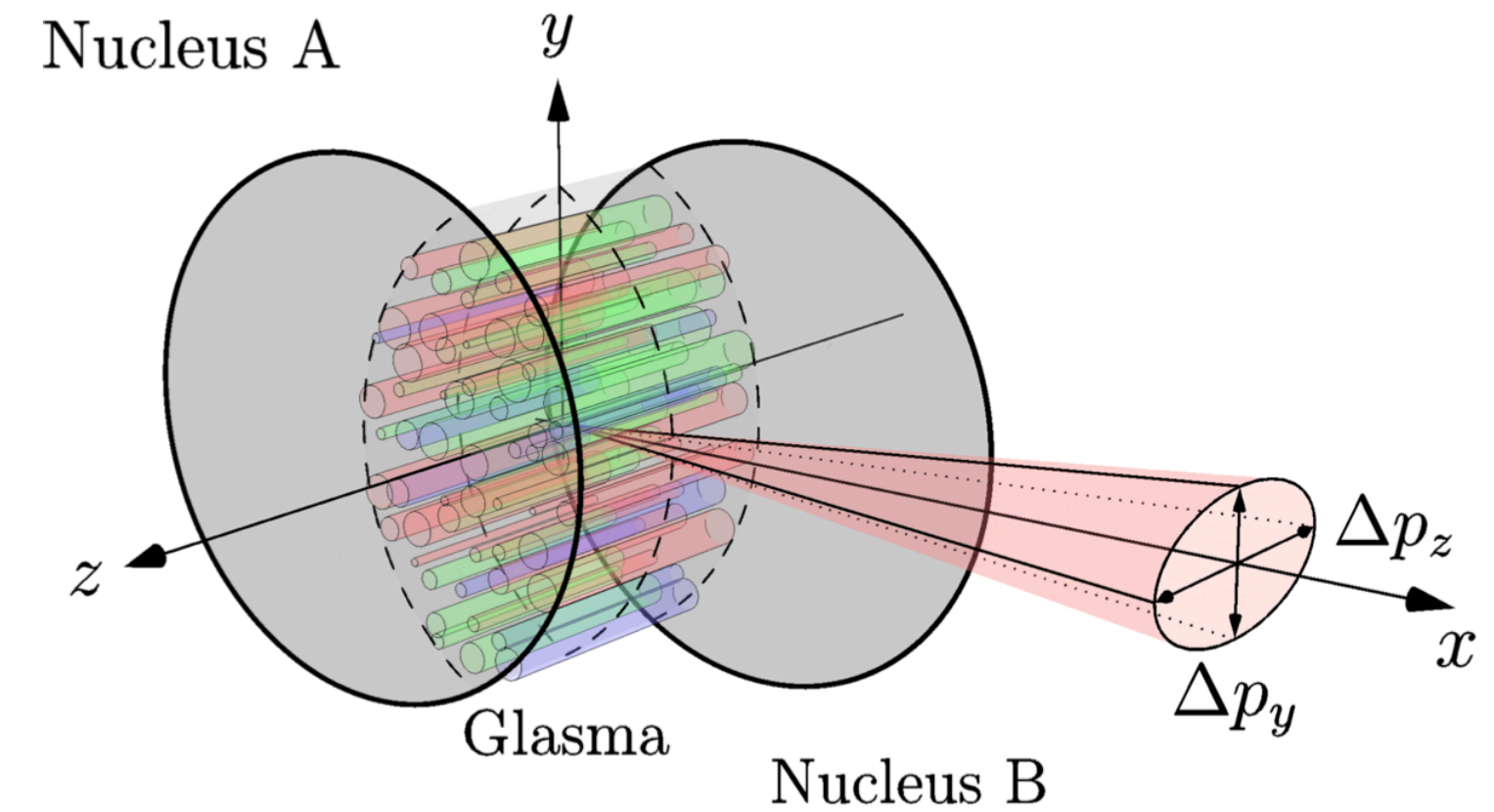
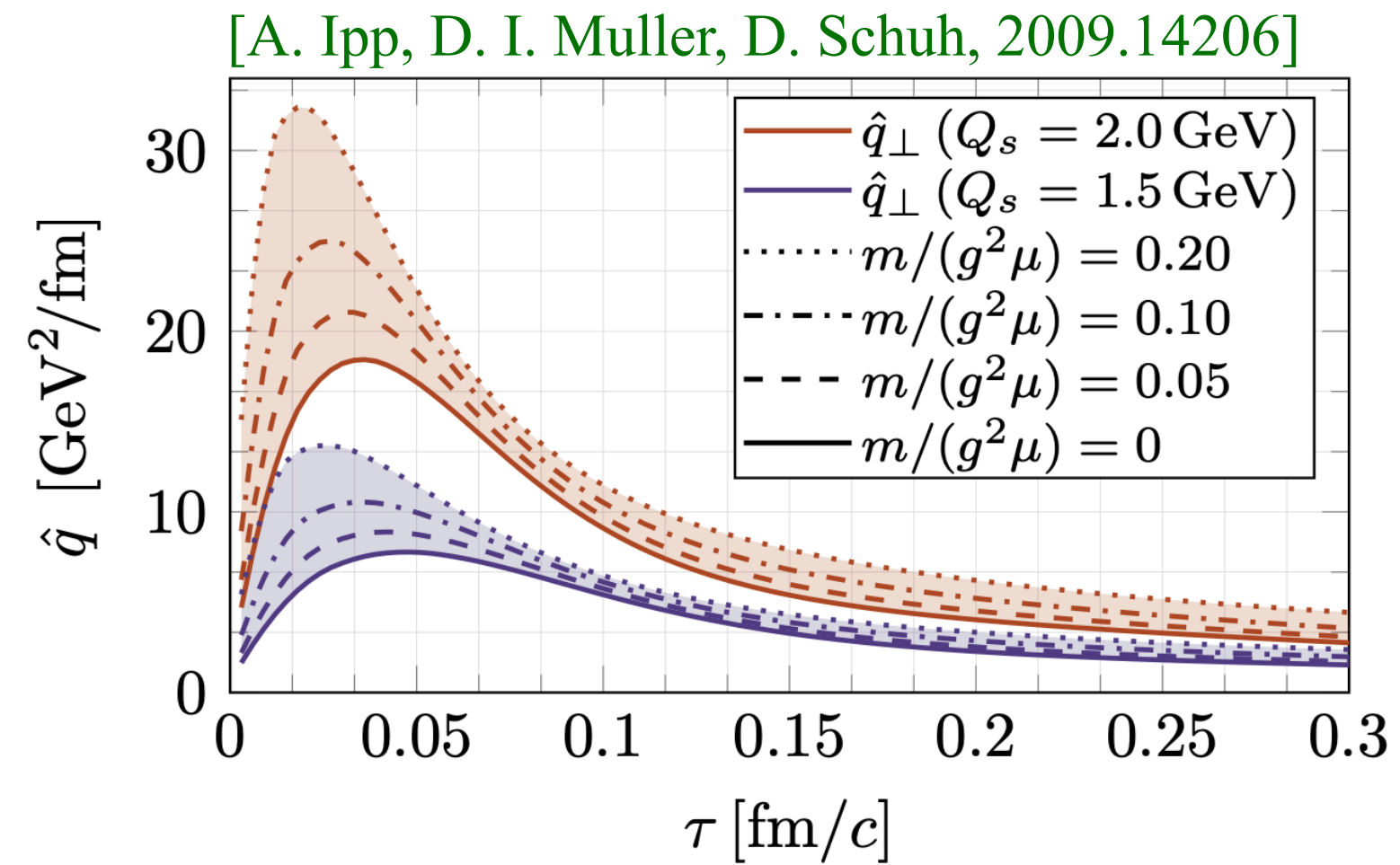
Flowing matter: 2104.09513 [N=1], 2207.07141 [Resummation], 2406.14628 [Gluon radiation], 2309.00683 [Flowing anisotropic matter], ...

Matter gradients: 2104.09513 [N=1], 2202.08847 [Resummation], 2210.06519 [Kinetic Th.], 2304.03712 [Gluon Radiation], 2204.05323 [Broadening]

Jet observables/Pheno: 2110.03590 [Jet drift], 2308.01294 [Jet substructure], DREENA, ...



The Landscape



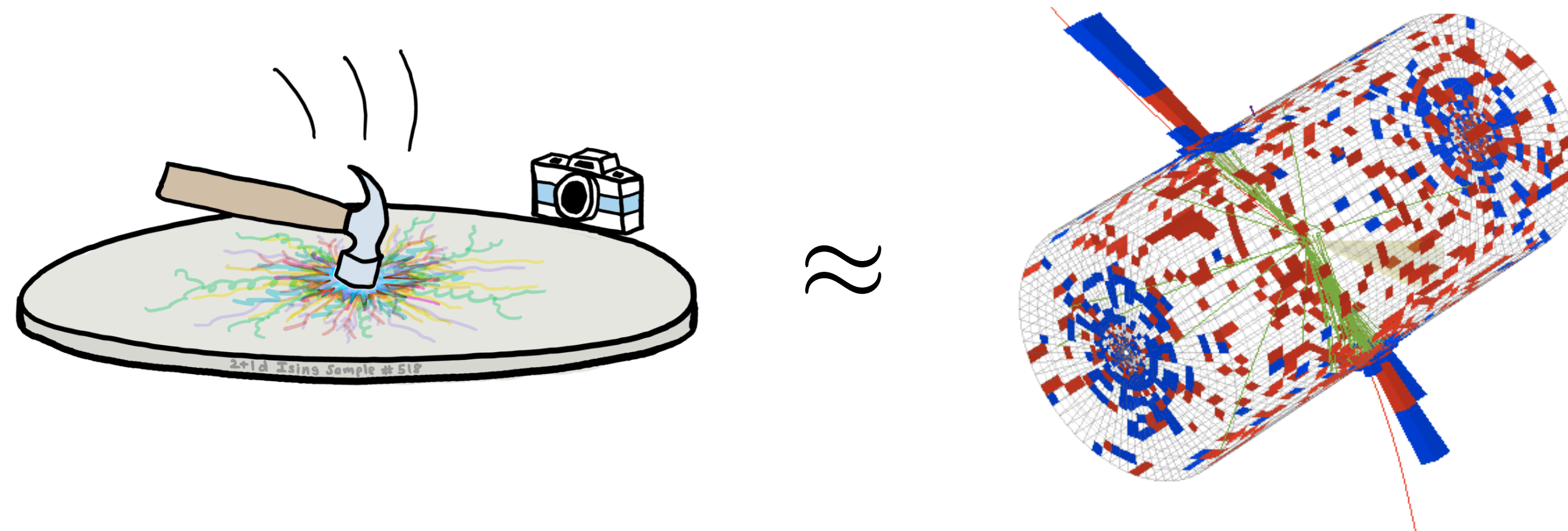
Jet evolution in the early stages

Momentum broadening in early stages: [Works by Avramescu et al](#); [Lindebauer et al](#); [Muller et al](#), ...

Radiative spectrum in “glasma”: [2306.20307 \[Photons\]](#), [2303.03914 \[Gluon branching\]](#), [2407.04774 \[Quark antenna\]](#), [2406.07615 \[Spatial correlations\]](#)

[See other talks by Kirill, Dusan and Bithika this week]

- The jet quenching program was initiated several decades ago; today it is one of the most active fields in the high-pt sector of HICs.
- Jets are ideal probes to resolve the spacetime structure of the plasma, and admit a perturbative treatment.
- In the future, we will need a more differential look into jets, keeping track of not only energy and momentum, but also other quantum numbers such as the spin distribution inside them.
- Many of these aspects have been studied by other communities (spin-hydro, soft sector, ...) and there is a large overlap that can be exploited!





Thank you !