

# PION FEMTOSCOPY WITH LÉVY SOURCES: RECENT DEVELOPMENTS

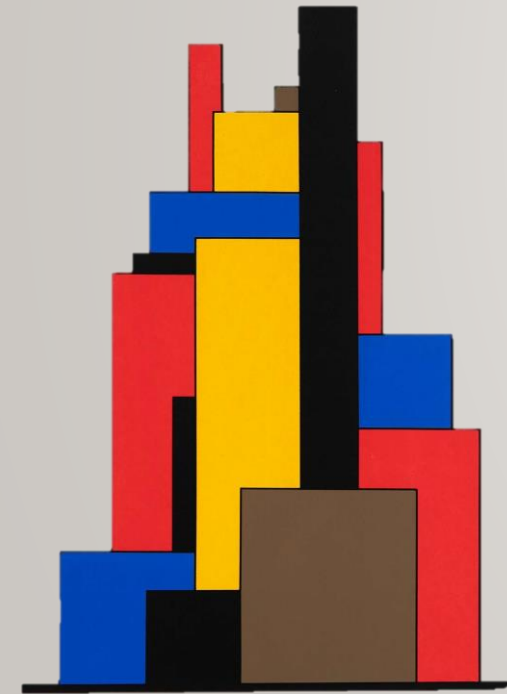


MÁTÉ CSANÁD (FOR THE EÖTVÖS U FEMTOSCOPY GROUP)  
2024 ZIMÁNYI SCHOOL WINTER WORKSHOP

ZHI MAN YI



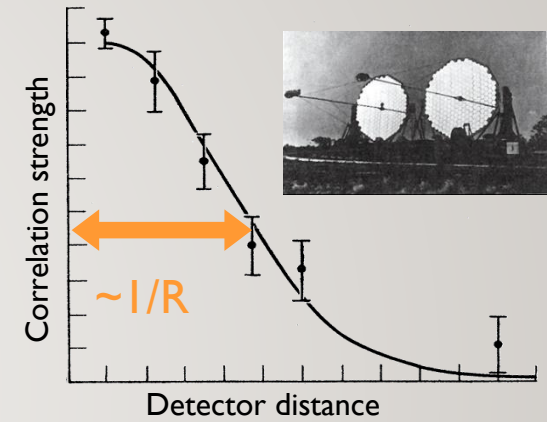
Overflowing with knowledge





# HBT OR FEMTOSCOPY IN HIGH ENERGY PHYSICS

- R. Hanbury Brown, R. Q. Twiss - observing Sirius with radio telescopes
  - Intensity correlations vs detector distance  $\Rightarrow$  source size
  - Measure the sizes of apparently point-like sources!
- Goldhaber et al: applicable in high energy physics
- Understanding: Glauber, Fano, Baym, ...  
Phys. Rev. Lett. 10, 84; Rev. Mod. Phys. 78 1267, ...
  - Momentum correlation  $C(q)$  related to source  $S(r)$



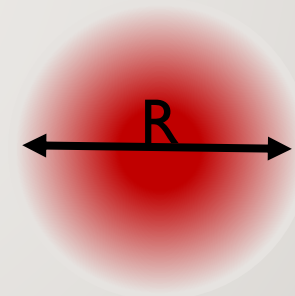
$$C(q) \cong 1 + \left| \int S(r) e^{iqr} dr \right|^2$$

(under some assumptions)

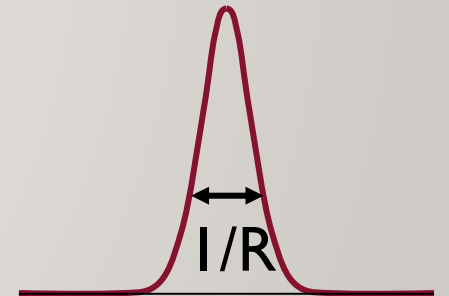
- Also with distance distribution  $D(r)$ :

$$C(q) \cong 1 + \int D(r) e^{iqr} dr$$

- Neglected: pair reconstruction, final state interactions, multi-particle correlations, coherence, ...



source function  $S(r)$



correlation funct.  $C(q)$

- What is the source shape? Can be explored via femtoscopy



# LÉVY DISTRIBUTIONS IN HEAVY ION PHYSICS

- Central limit theorem, diffusion, and thermodynamics lead to Gaussians
- Measurements suggest phenomena beyond Gaussian distribution

- Lévy-stable distribution:

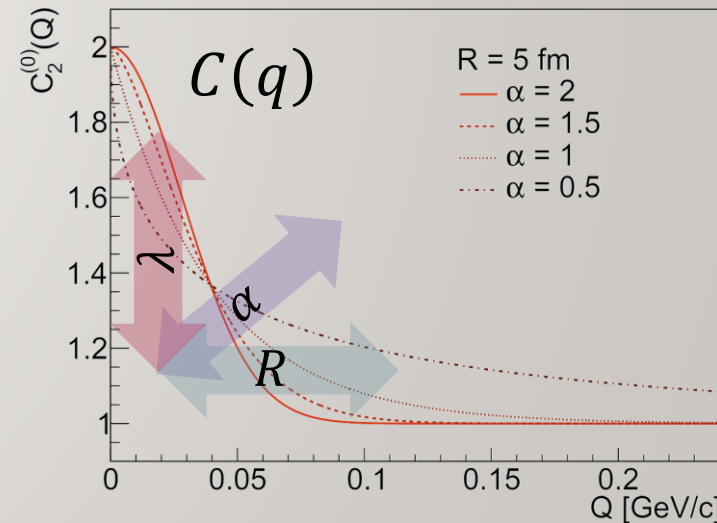
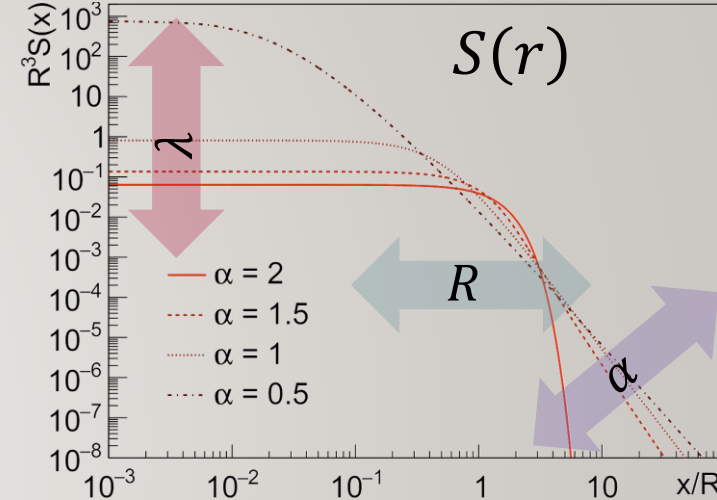
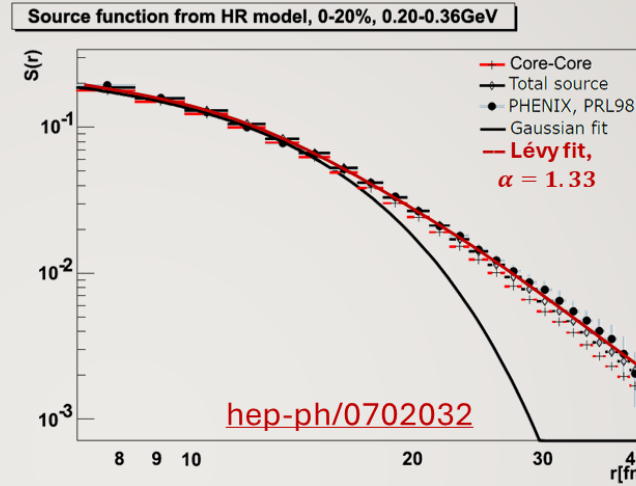
$$\mathcal{L}(\alpha, R; r) = \frac{1}{2\pi} \int d^3q e^{iqr} e^{-\frac{1}{2}|qR|^\alpha}$$

- From generalized central limit theorem
- Power-law tail  $\sim r^{-1-\alpha}$
- Special cases:  $\alpha = 2$  Gaussian,  $\alpha = 1$  Cauchy

- Shape of the correlation functions with Lévy source:

- $C_2(q) = 1 + \lambda \cdot e^{-|qR|^\alpha}$ ;  $\alpha = 2$ : Gaussian;  $\alpha = 1$ : exponential  
Csörgő, Hegyi, Zajc, Eur.Phys.J. C36 (2004) 67-78

- Lévy source seen & exponent measured from SPS through RHIC to LHC NA6I [[EPJC83\(2023\)919](#)], PHENIX [[PRC97\(2018\)064911](#), [PRC\(2024\)](#)], CMS [[PRCI09\(2024\)024914](#)]

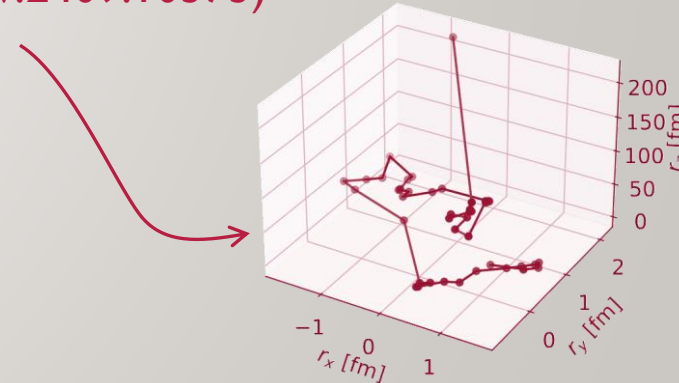
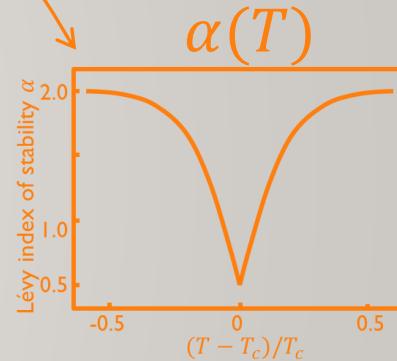
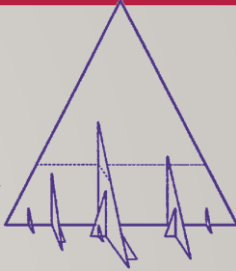






# WHY DO LÉVY SHAPES APPEAR, WHY IS IT IMPORTANT?

- A more comprehensive list of possible reasons:
  - Jet fragmentation (Csörgő, Hegyi, Novák, Zajc, *Acta Phys.Polon.* B36 (2005) 329-337)
    - See also Caucal, Mehtar-Tani, *JHEP* 09 (2022) 023
    - Important in  $e^+e^-$  and other small systems
  - Critical phenomena (Csörgő, Hegyi, Novák, Zajc, *AIP Conf.Proc.* 828 (2006) no.1, 525-532)
    - Role in the few GeV region? Affected by finite size effects?
  - Directional or event averaging (Cimerman et al., *Phys.Part.Nucl.* 51 (2020) 282)
    - Ruled out by event-by-event and 3D analyses
  - Lévy walk (BJP37(2007); PRB 103(2021), *Entropy*24(2022); PLB847(2023); arXiv:2409.10373)
    - Only plausible explanation at high energies
- Importance of utilizing Lévy sources, leaving  $\alpha$  as parameter:
  - Measuring  $\alpha$  and  $R$ : quark-hadron transition, critical point, etc
  - Measuring  $\lambda$ : In-medium mass modification, coherent pion production







# LÉVY PROCESSES IN NATURE AND IN SCATTERING

- Lévy walk and Lévy flight: known in ecology, climatology, etc.
  - If step size distribution has no finite width: generalized central limit theorem, Lévy-stable limiting distributions
- In HIC: increasing mean free path, step size increases
  - Seen in expansion under Coulomb potential in solid-state physics
- Observed in UrQMD [arXiv:[2409.10373](https://arxiv.org/abs/2409.10373)]
  - Scatterings, decays, coalescence (no Coulomb scattering)

E. I. Kiselev, [Phys. Rev. B 103, 235116 \(2021\)](https://doi.org/10.1103/PhysRevB.103.235116)

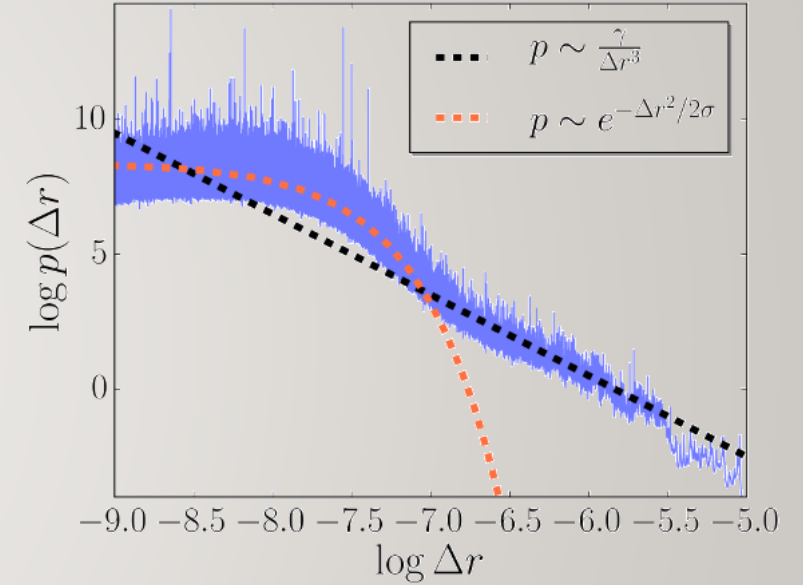
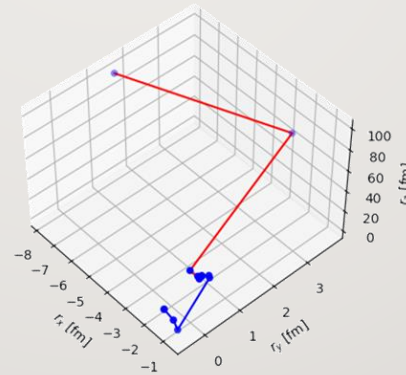
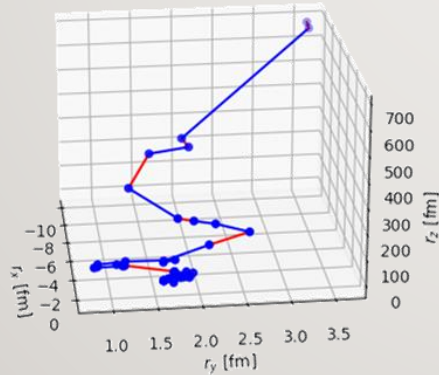
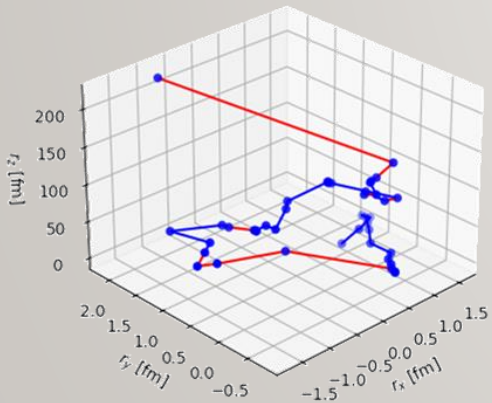


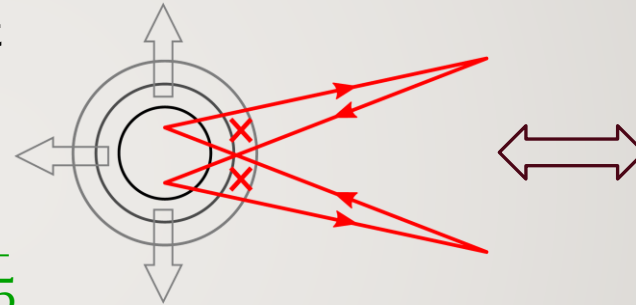
Figure 1. The Figure shows the step size distribution  $p(\Delta r)$  of a random walk as performed by Coulomb interacting, diffusing particles in two dimensions. At large step sizes, the distribution clearly follows the  $p \sim \Delta r^{-3}$  power-law which leads to the superdiffusive dynamics described by Eq. (1). The data was obtained by integrating the system of coupled Langevin equations of Eq. (56).



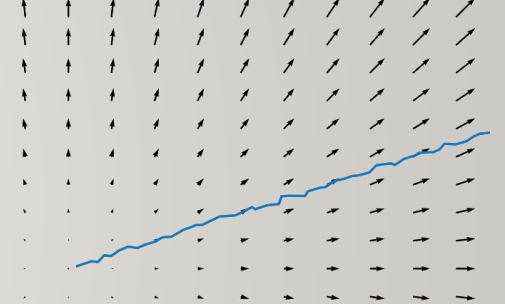


# CHARGED CLOUD: ANOTHER INTERESTING EFFECT

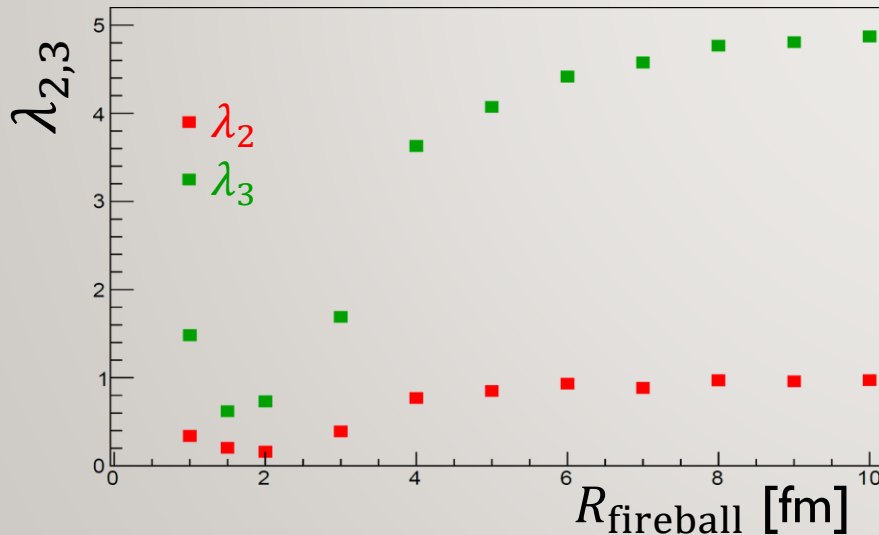
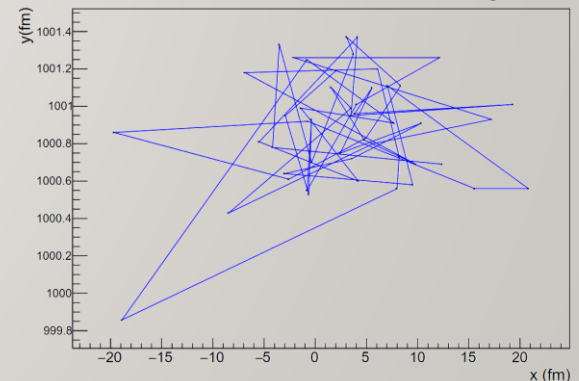
- Coulomb potential: infinite range, affecting evolution for a long time
- Solid-state physics (as mentioned on previous slide): may cause Lévy flight and power-law tails
- Another interesting effect: distortion of flight paths after kinetic freeze-out
  - Phase shift, similarly to an Aharonov-Bohm effect (arXiv:[2007.07167](https://arxiv.org/abs/2007.07167) and arXiv:[2410.15525](https://arxiv.org/abs/2410.15525))
- Phase shift decreases correlation strengths



exaggerated illustration



simulated transverse path



$\lambda_3 = 5$

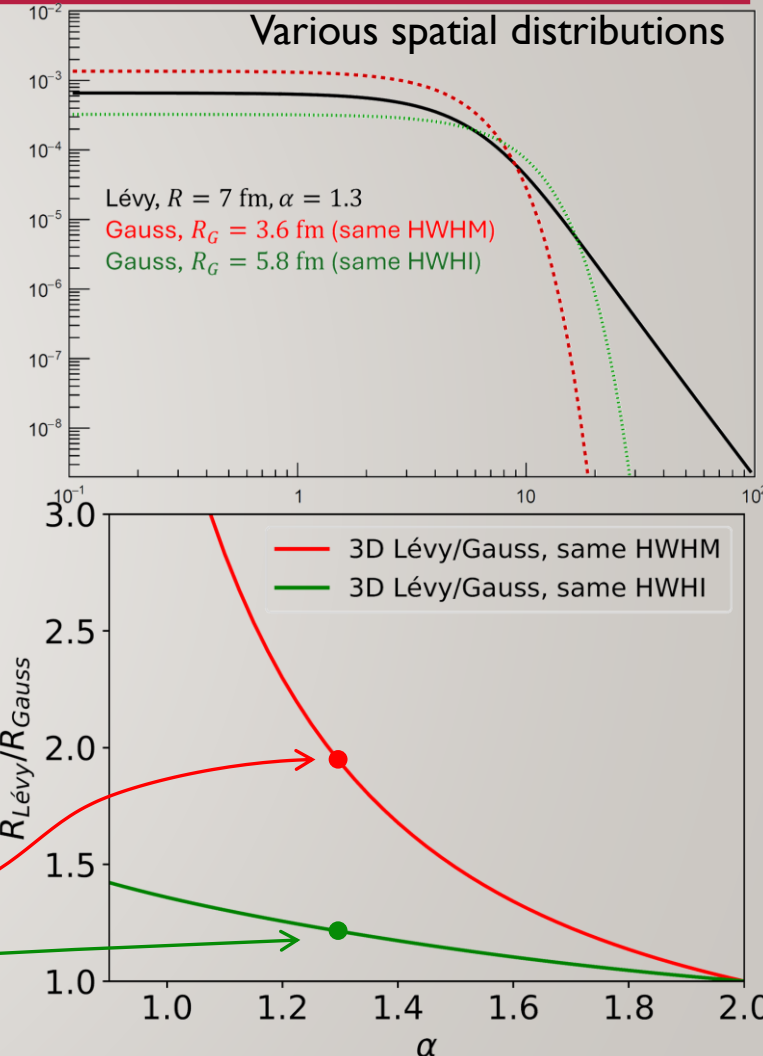
No A-B effect, pure core, fully chaotic source

$\lambda_2 = 1$



# SOURCE SIZE MEASURE CHANGE WITH $\alpha$

- No tail if  $\alpha = 2$ , power law and  $RMS = \infty$  if  $\alpha < 2$ : depends on cutoff
- What do Gaussian HBT radii mean? Important also w.r.t. CEP search
- Alternative measures (see arXiv:[2401.01249](https://arxiv.org/abs/2401.01249) for details)
  - **HWHM**: (half) width at half maximum
  - **HWHI**: (half) width at half integral
  - Width (normalized by  $R$ ) nontrivially depends on  $\alpha$
- Relations for 3D Gauss: **HWHM**  $\approx 1.17 \cdot R_G$ , **HWHI**  $\approx 1.54 \cdot R_G$
- For (e.g.) Lévy  $\alpha = 1.3$ : **HWHM**  $\approx 0.61 \cdot R_L$ , **HWHI**  $\approx 1.27 \cdot R_L$
- **Thus (e.g.)  $\alpha = 1.3$  and  $R_L = 7$  fm “means”:**
  - Same HWHM Gaussian:  $R_G \approx 3.61$  fm  $\leftarrow R_{Gauss} \approx R_{Lévy}/1.94$
  - Same HWHI Gaussian:  $R_G \approx 5.77$  fm  $\leftarrow R_{Gauss} \approx R_{Lévy}/1.21$







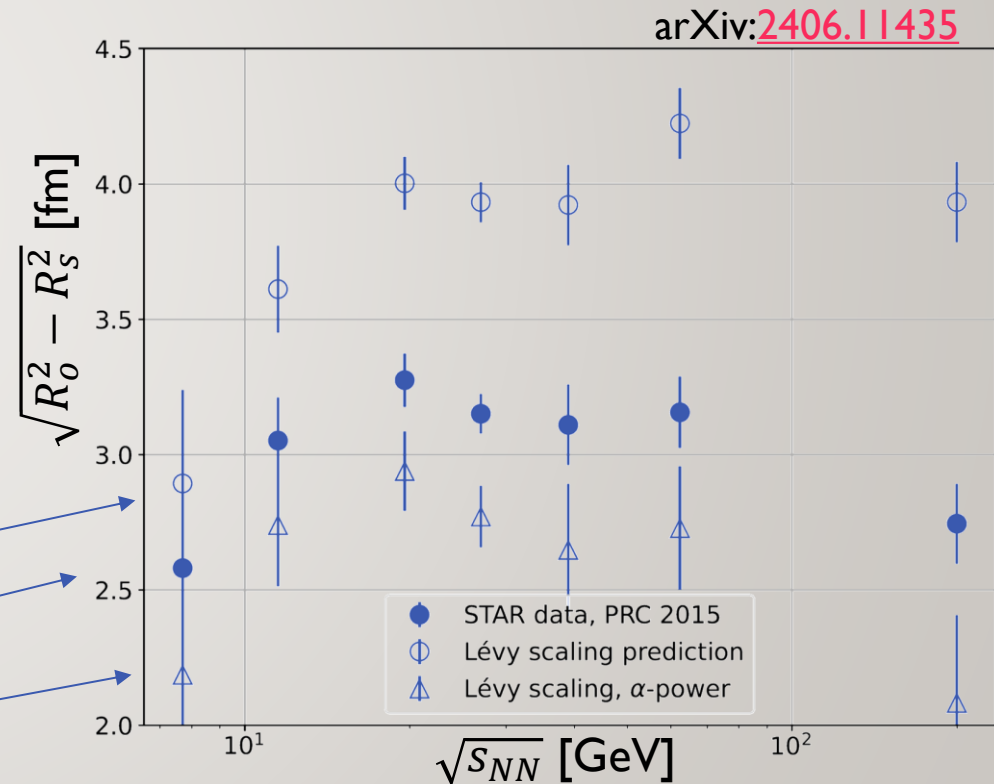
# ENERGY DEPENDENCE OF LÉVY SOURCE SIZE?

- Experimental observation:  $\hat{R} = \frac{R}{\lambda(1+\alpha)}$  doesn't depend on  $\alpha \rightarrow$  can estimate  $R_{\text{free } \alpha} = R_{\text{Gauss}} \frac{\lambda_{\text{free } \alpha}(1+\alpha)}{\lambda_{\text{Gauss}}(1+2)}$ 
  - Assuming trends of  $\alpha$  and  $\lambda$  as  $A \cdot \sqrt{s_{NN}}^B$ , with  $A_\alpha = 1.85, B_\alpha = -0.06, A_\lambda = 0.6, B_\lambda = 0.06$
- Different trends of guesstimated  $R_{\text{Lévy}}$  and  $R_{\text{Gauss}}$
- Caused by shape change with  $\sqrt{s_{NN}}$
- Connection of  $\sqrt{R_0^2 - R_s^2}$  to emission duration: based on Gaussian sources,
- Maybe  $(R_0^\alpha - R_s^\alpha)^{1/\alpha}$  for Lévy source, Csörgő, Hegyi, Zajc, EPJC36(2004)67
- Importance of measuring  $R_{o,s,l}$  with free  $\alpha$

$\hat{R}$  scaling guesstimate for Lévy radii

original Gaussian radii

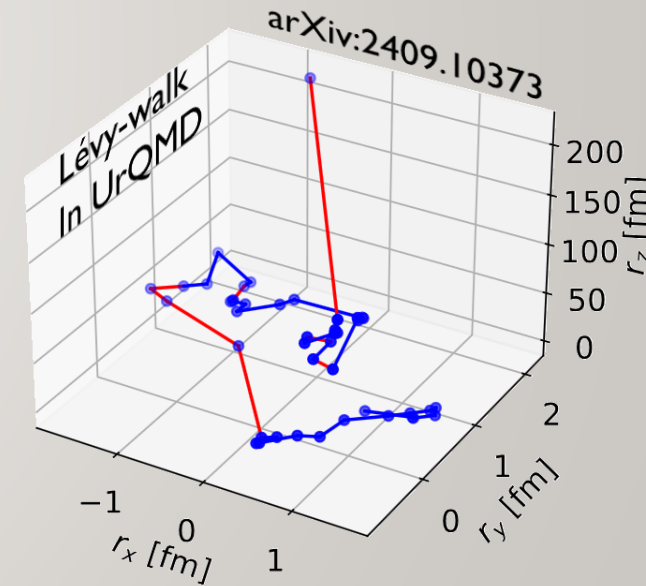
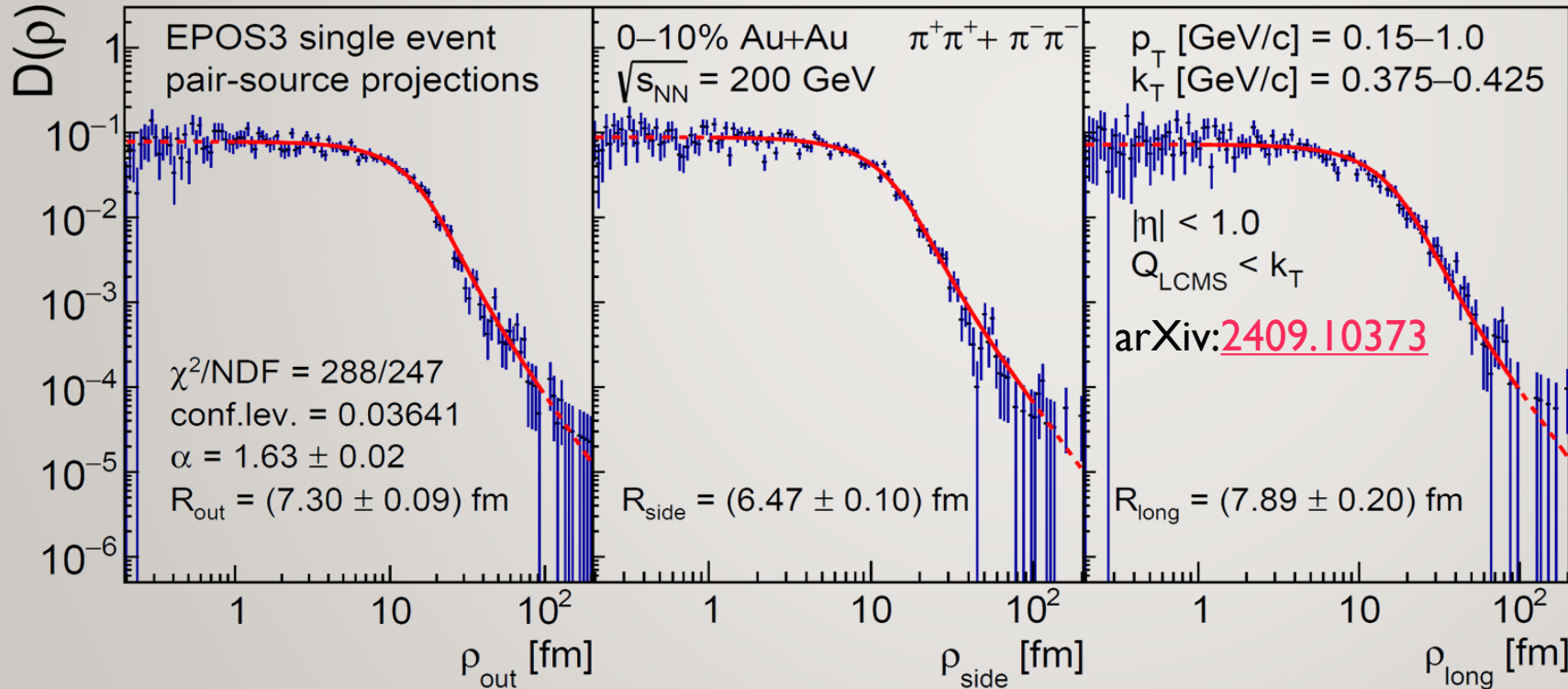
$\alpha$ -powered version





# LÉVY SHAPES IN SINGLE 3D EPOS EVENTS, 3D

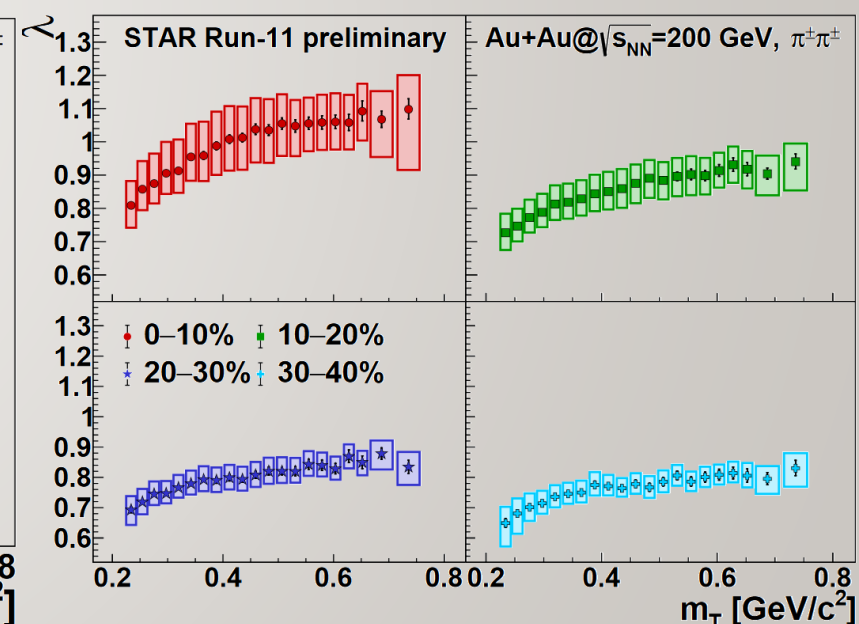
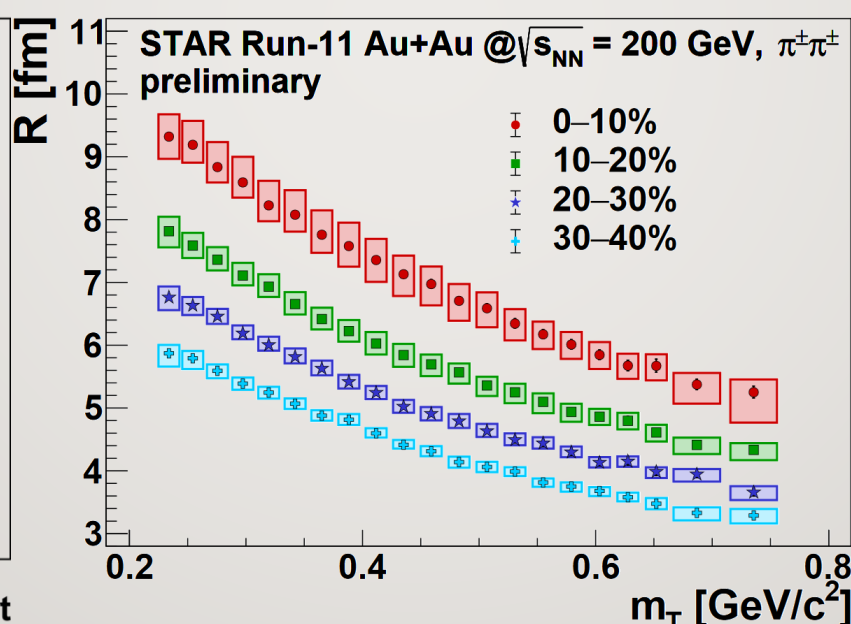
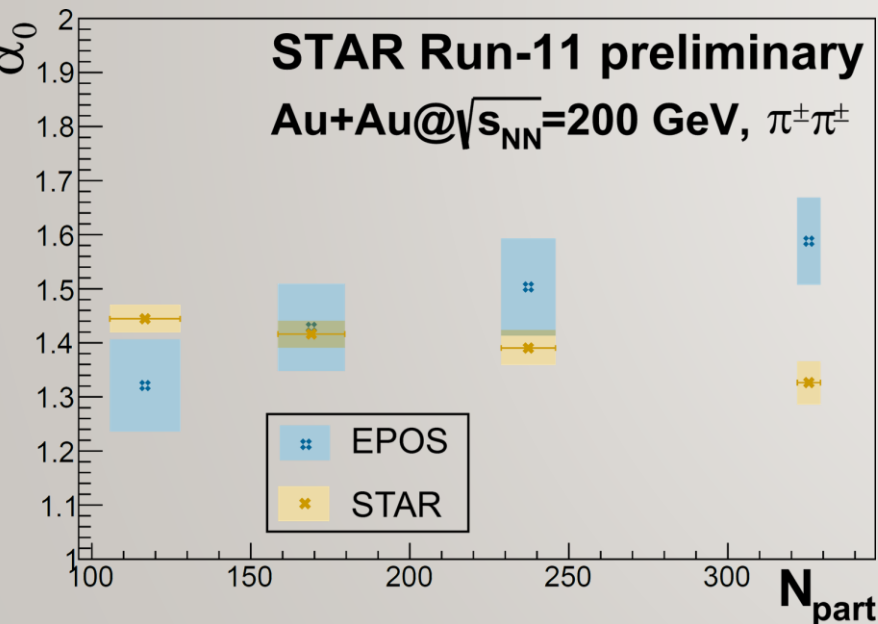
- What if the Lévy shapes appeared only because of directional averaging?
- Let's check 3D event shapes in EPOS! → Also Lévy, with similar  $\alpha$  and radii (as those in 1D)
- Clear physical reason: Lévy walk, see poster/talk by D. Kincses on Thu





# 10/19 CENTRALITY DEPENDENCE AT 200 GEV

- Lévy scale  $R$ : decreasing trend with  $m_T$  and with centrality
  - Connection to flow and initial geometry, similarly to Gaussian radii
- Lévy exponent  $\alpha$ : EPOS quantitatively close, largest discrepancy for central collisions
  - Effect of Coulomb scattering? [PRB103\(2021\)235116](#), [arXiv:2410.15525](#)
- Correlation strength  $\lambda$ : increase from low to high  $m_T$  and from peripheral to central collisions
  - $m_T$  dependence: modified in-medium  $\eta'$  mass? [PRL81\(1998\)2205](#), [PRL105\(2010\)182301](#), [arXiv:2407.08586](#) (see next talk by S. Lökös)

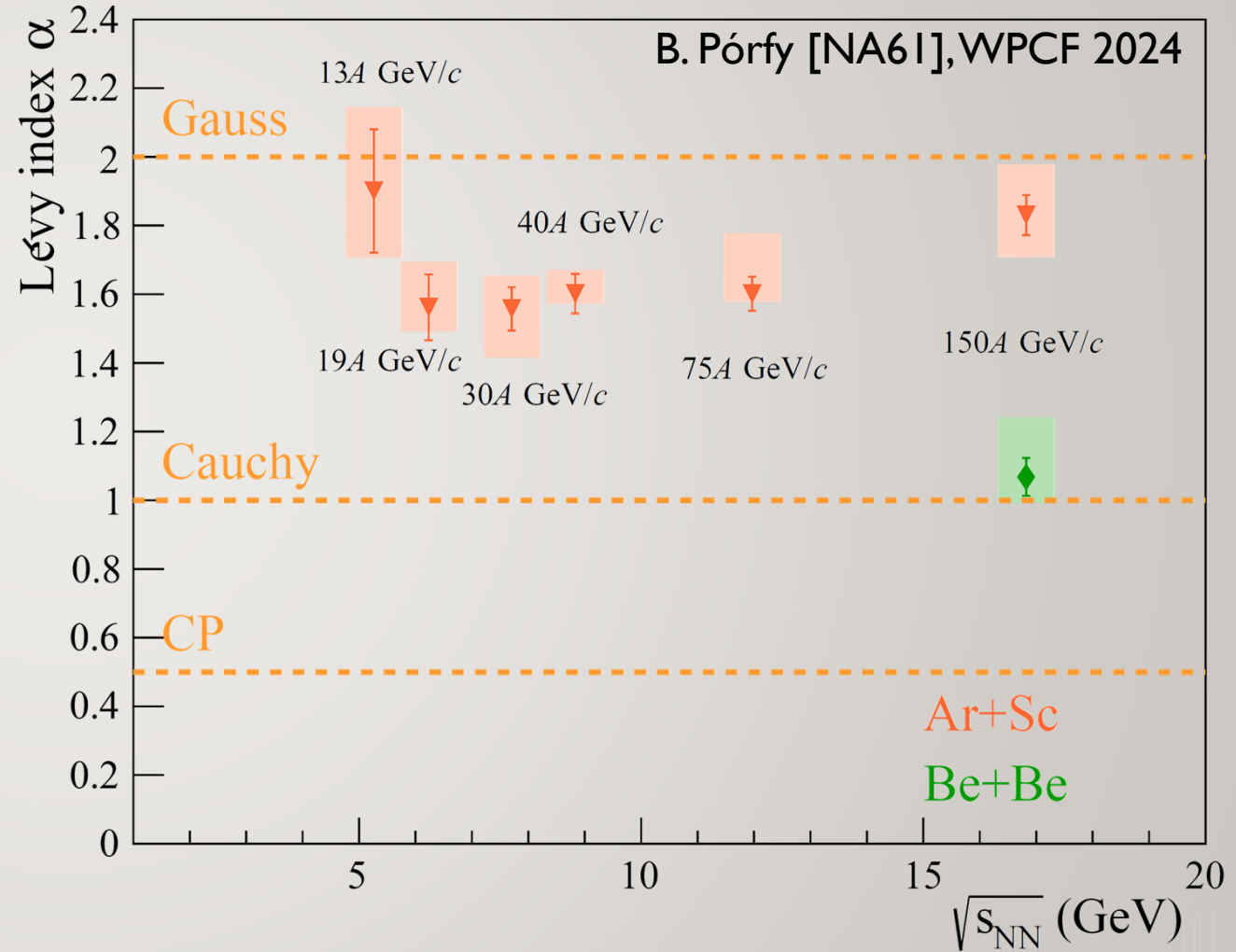






# NA6 I /SHINE RESULTS

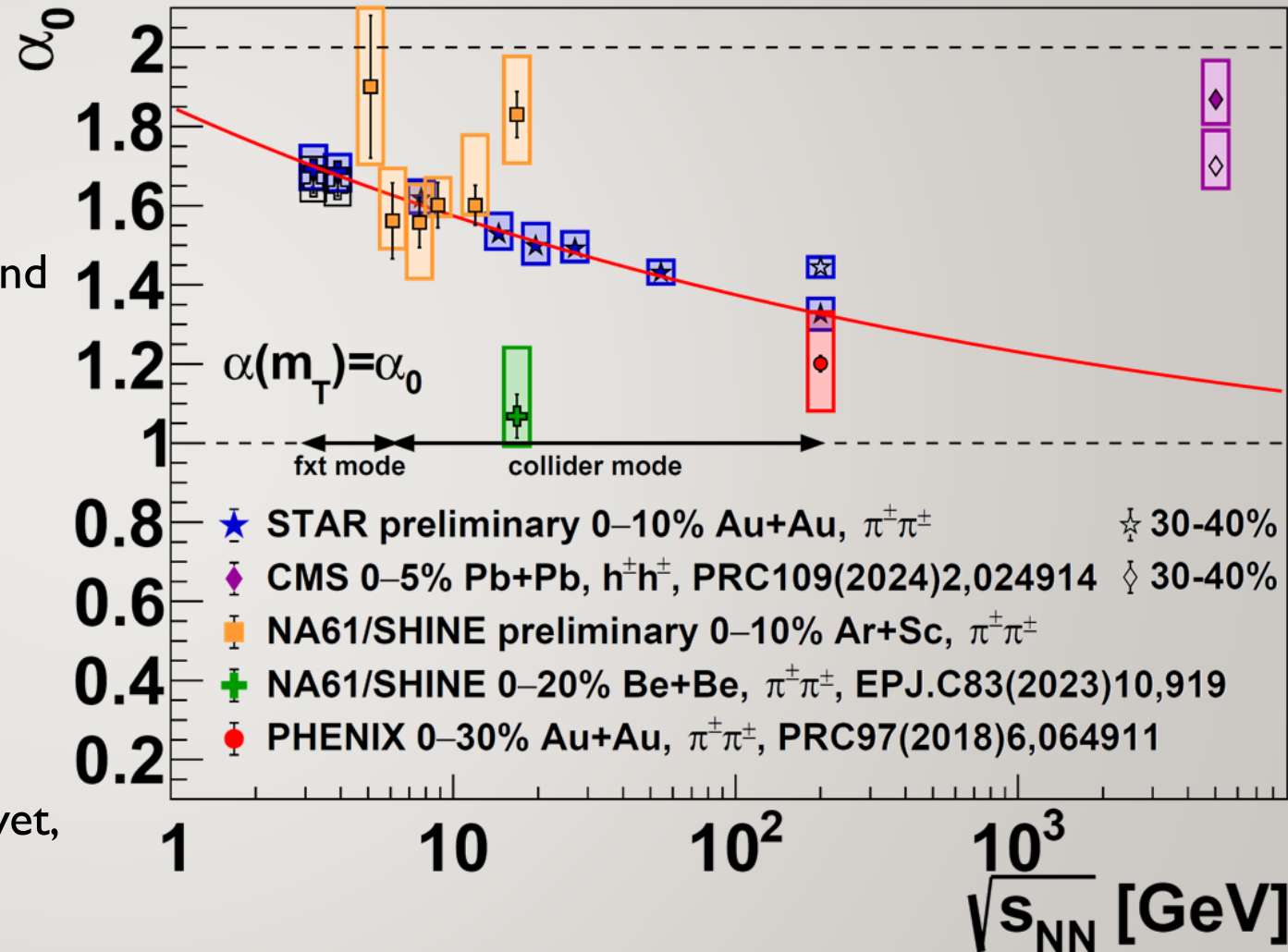
- At 150 AGeV:  $\alpha(\text{Be+Be}) < \alpha(\text{Ar+Sc})$
- Interesting trend of  $\alpha$  for smaller energies in Ar+Sc
  - (not incompatible with constant)
- Next step: Xe+La, 3D analysis
- See more details by B. Pórfy on Thu
  - $\alpha(m_T)$  approximately constant
  - $R(m_T)$  shows sign of flow
  - $\lambda(m_T)$  shows no „hole” at low  $m_T$
  - Compare to RHIC energies





# 12/19 LÉVY EXPONENT FROM 3.2 TO 200 GEV

- Non-gaussian values ( $\alpha \ll 2$ )
- Increasing density  $\rightarrow$  rescattering decreases  $\alpha$
- 200 GeV centrality dependence, same trend
  - Larger  $\alpha$  for peripheral collisions
- Trend described by power-law:
 
$$\alpha_0 \approx 0.85 + \sqrt{s_{NN}}^{-0.14}$$
- Good description by UrQMD at FXT energies, comprehensive energy scan is ongoing
- No non-monotonic trend in  $\alpha$  observed yet, far from conjectured critical value (0.5)





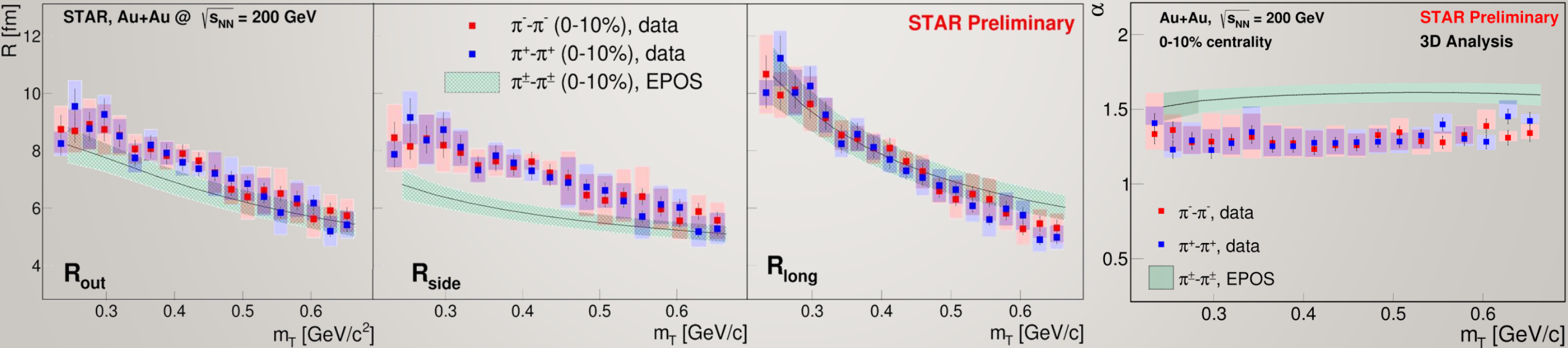
# STAR 3D PRELIMINARY DATA AT 200 GEV VS EPOS

- See STAR analysis in talk by S. Bhosale
- EPOS and data (both from 3D analysis) comparison shows good agreement for radii
  - EPOS from arXiv:2409.10373
- Moderate discrepancy for  $R_{side}$  and  $\alpha$ : maybe due to long-range Coulomb scattering (not in EPOS)

$R_{O,S,l}$  vs  $m_T$

S. Bhosale, WPCF 2024

$\alpha$  vs  $m_T$

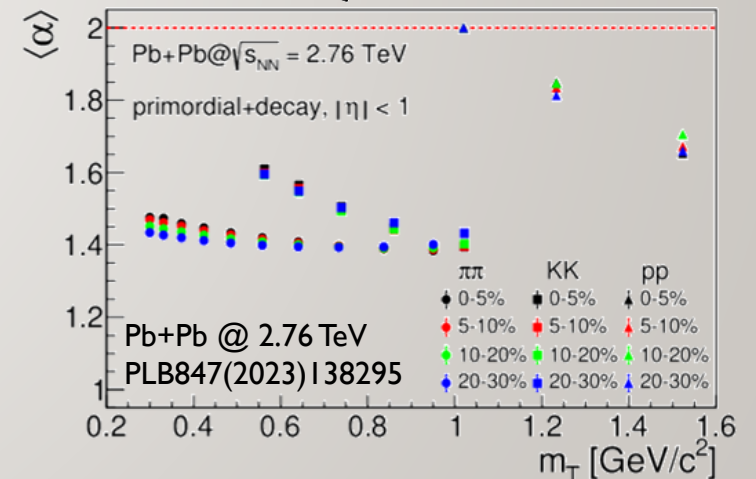
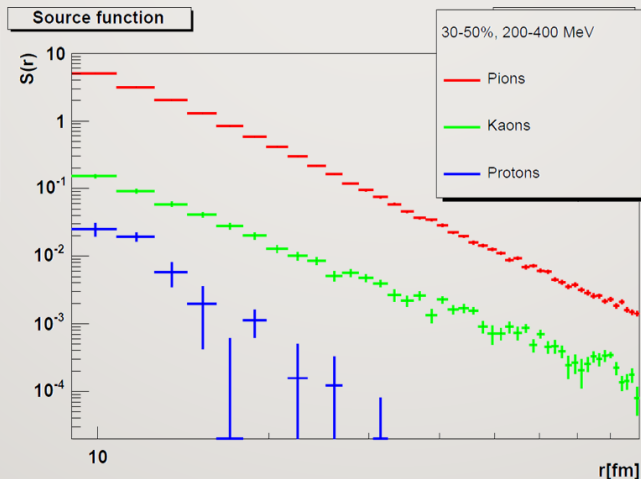
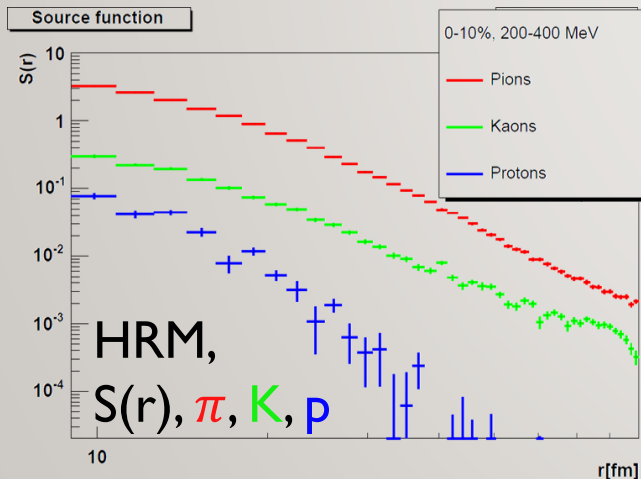
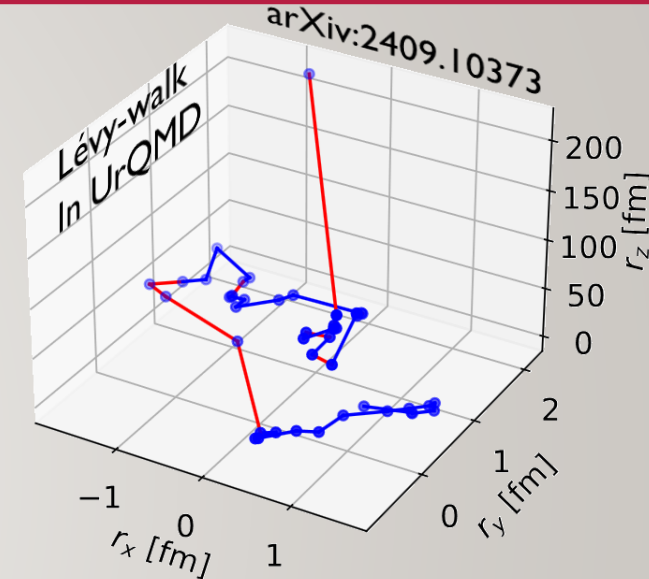






# SO WHEN DO THE POWER-LAW TAILS FORM?

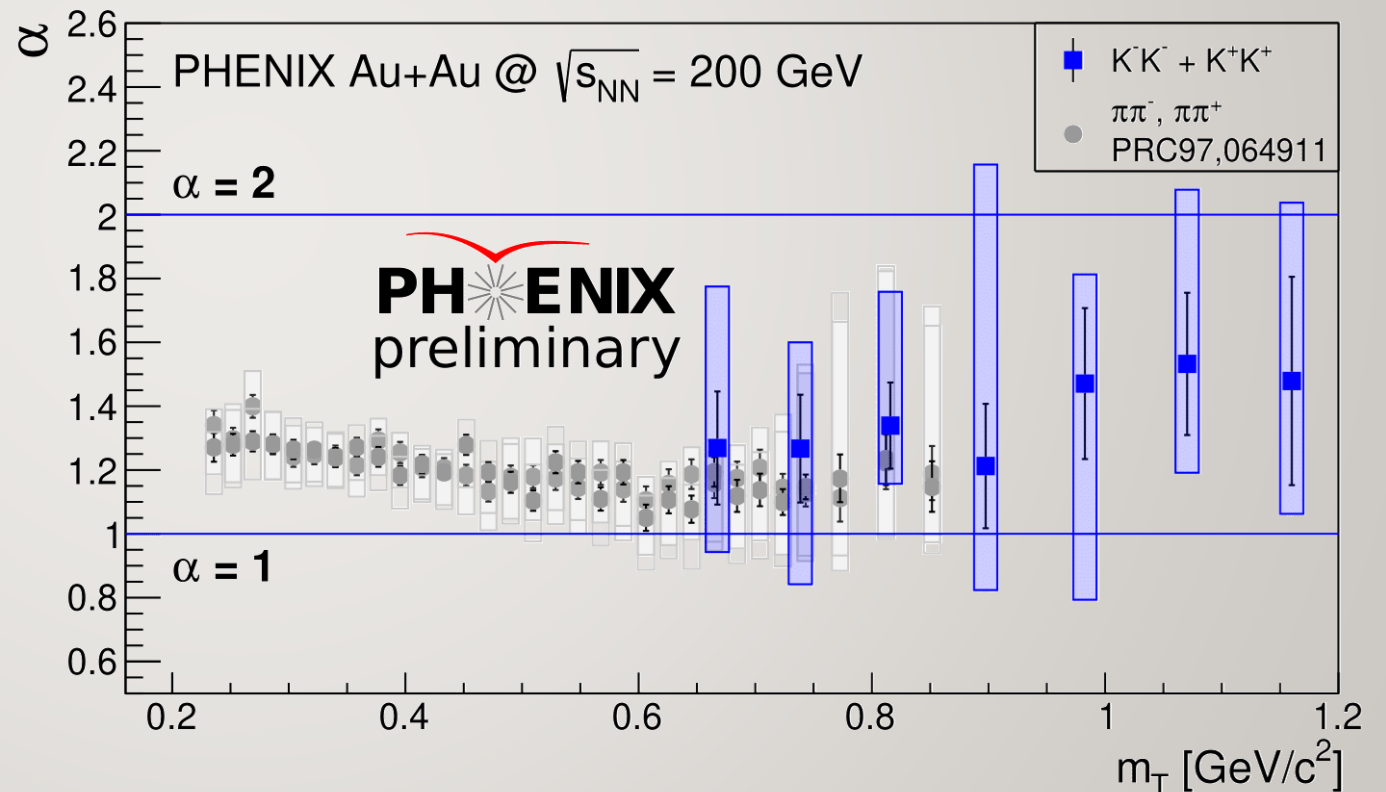
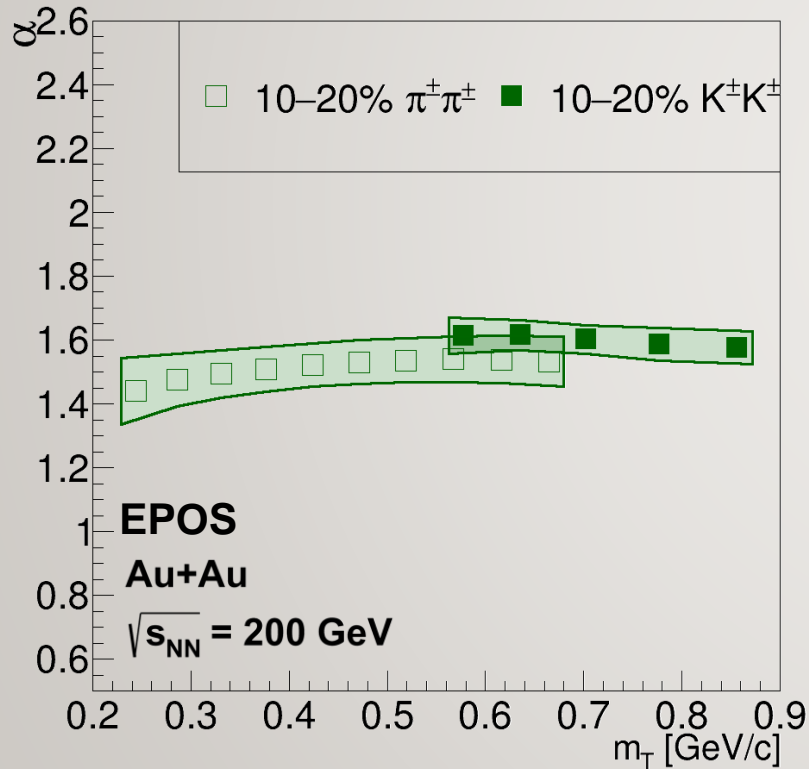
- Based on EPOS: apparently Gaussian in hydro phase
- Power-law tails due to Lévy-walk: scattering processes
  - 2-by-2, decay, coalescence, etc
- How to test? Particle type dependence!
  - Based on cross-sections:  $\alpha(p) > \alpha(\pi) > \alpha(K)$   
Humanic, IJMPE15(2006)197, Csanád, Csörgő, Nagy, BJP37(2007)1002
  - Not confirmed by EPOS! Role of decays and inelastic collisions?





# PARTICLE SPECIES COMPARISON, DATA VS EPOS, LÉVY $\alpha$

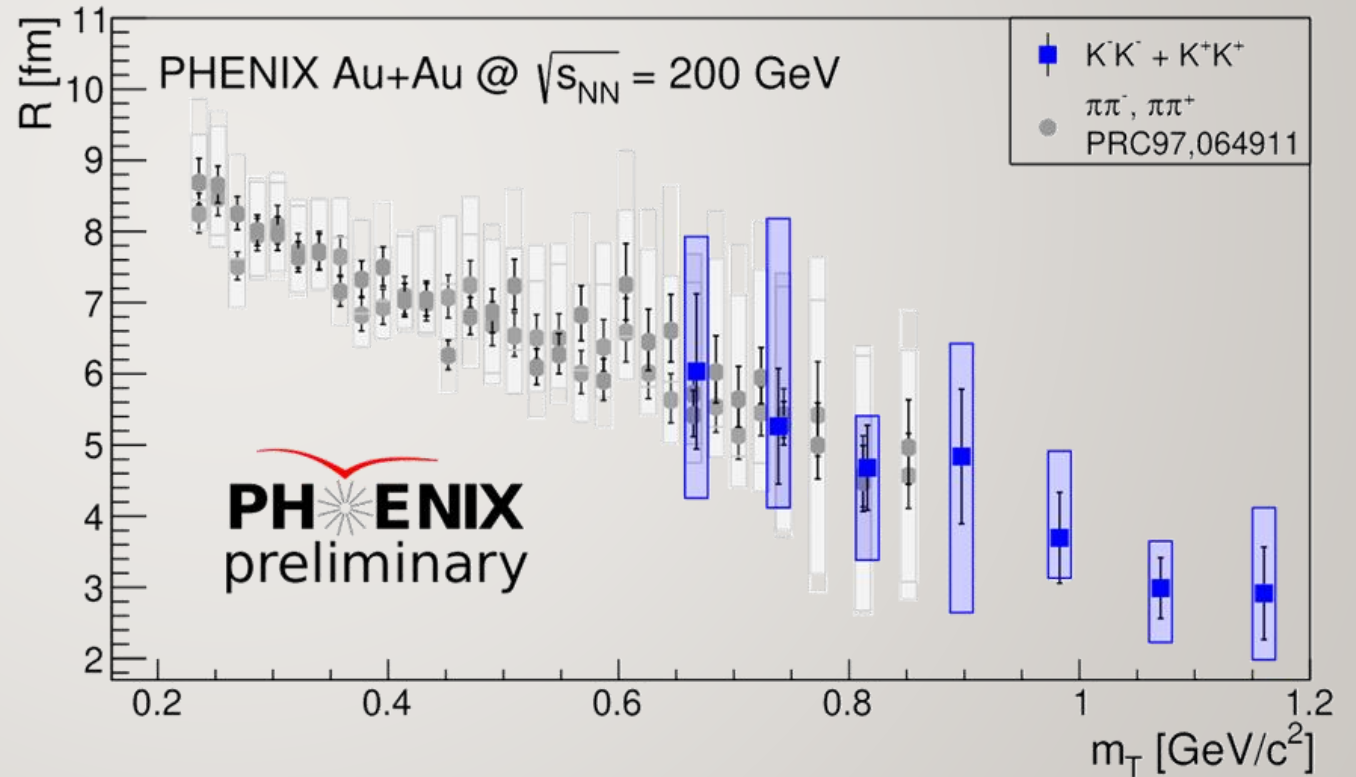
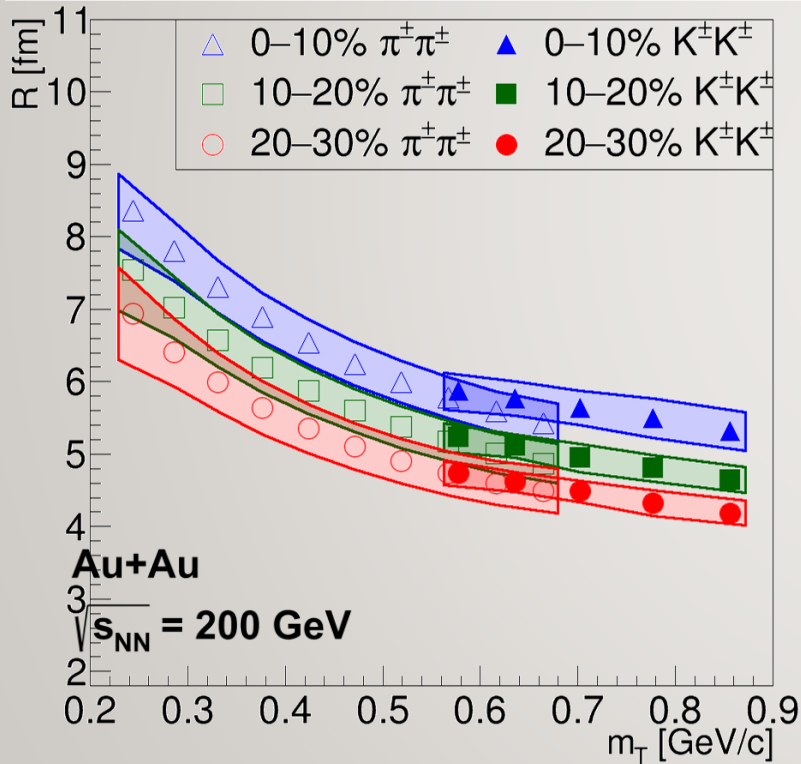
- Good agreement between kaons and pions, experiment and EPOS
  - Slightly surprising: same source for kaons and pions, despite role of scattering?
  - See talk/poster by L. Kovács on Thursday





# PARTICLE SPECIES COMPARISON, DATA VS EPOS, LÉVY $R$

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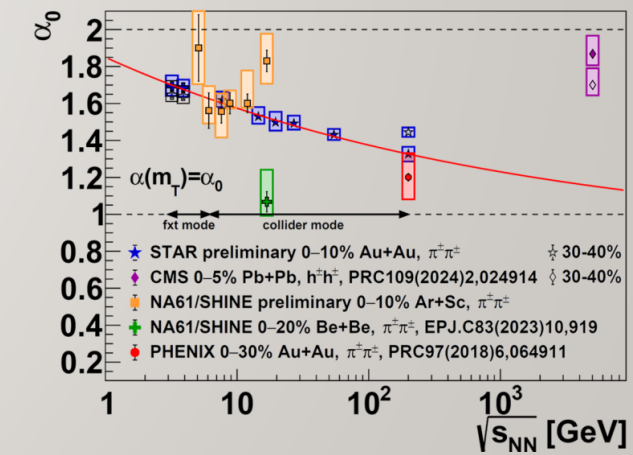
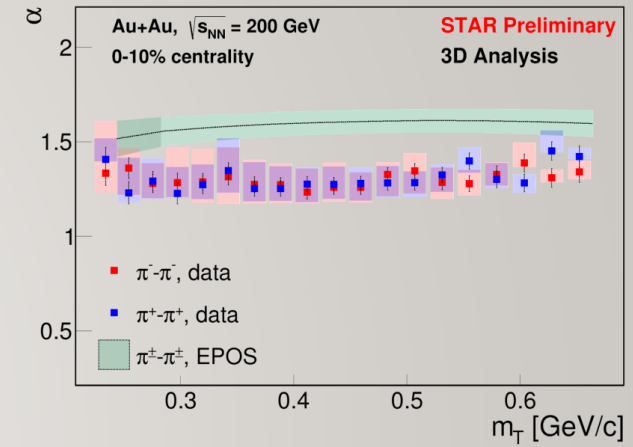


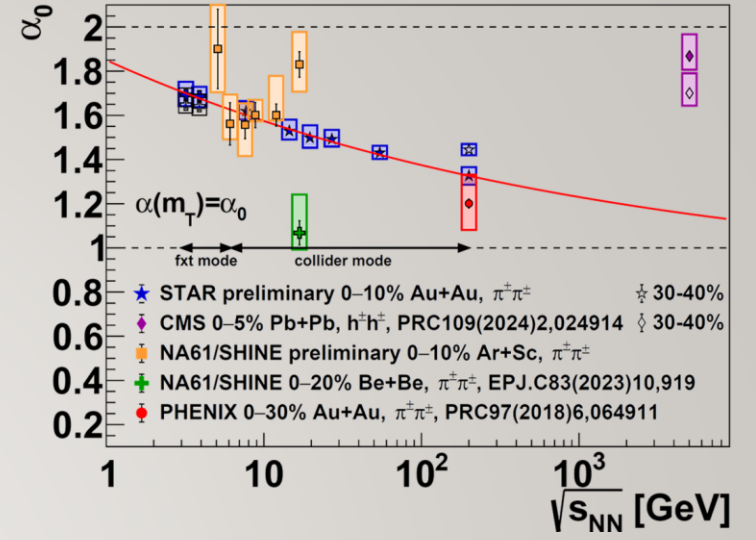
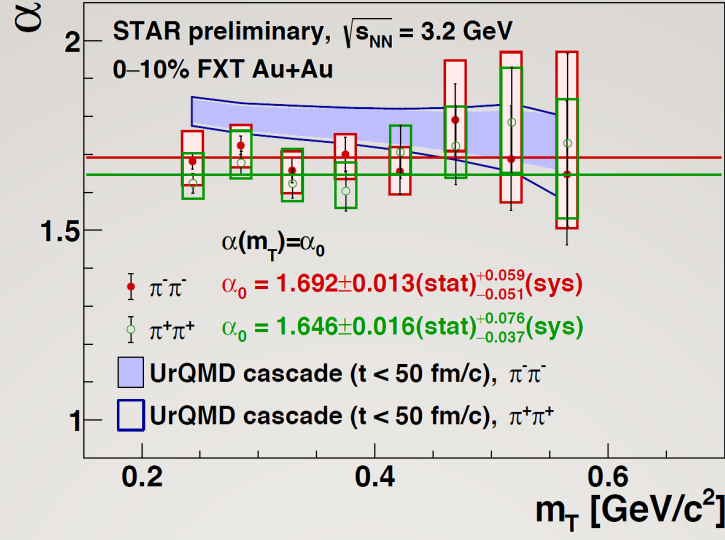
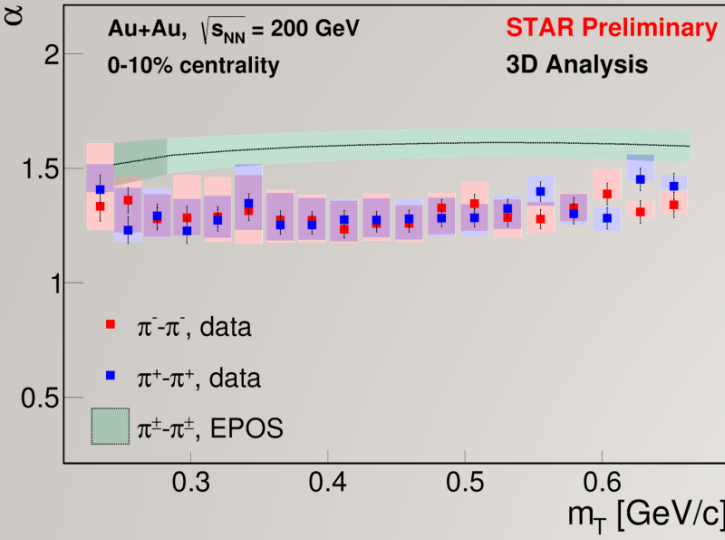




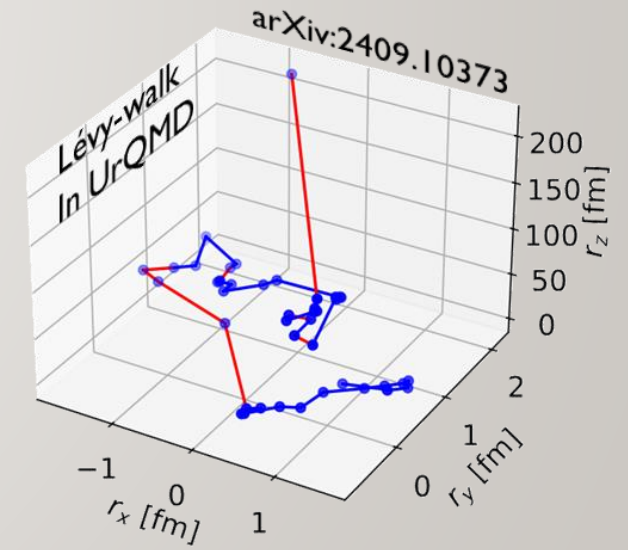
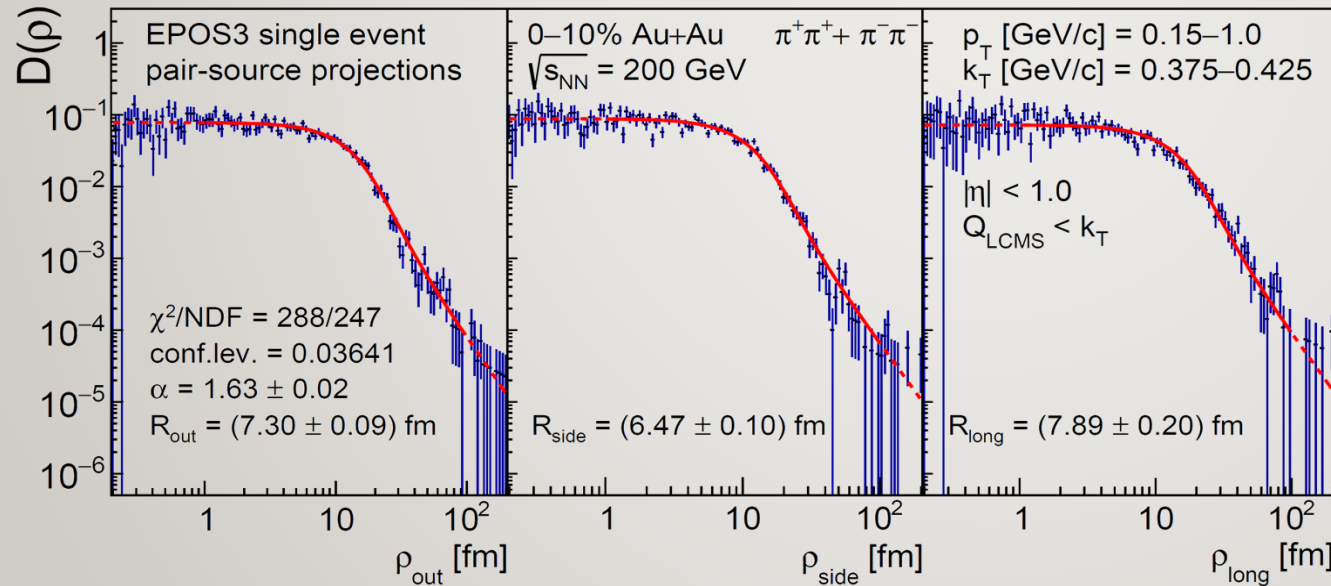
# CONCLUSIONS AND OUTLOOK

- Lévy sources for pions seen from 3.2 to 200 GeV with STAR, also in 3D
  - **Lévy  $\alpha$** : between 1 and 2, increases with  $\sqrt{s_{NN}}$
  - **Lévy  $R$** : hydro scaling, relation to Gaussian through HWHM/HWHI
  - **Lévy  $\lambda$** : decrease at low transverse mass
- Possible reasons:
  - ~~Jet fragmentation~~ → not dominant in AA collisions
  - **Critical phenomena** → no non-monotonicity seen, more energies to be investigated
  - ~~Directional averaging~~ → good fits and same Lévy exponent in 1D and 3D
  - ~~Event averaging~~ → event-by-event simulations show Lévy
  - **Resonance decays** → part of the reason, not enough alone
  - **Hadronic rescattering, Lévy walk** → good description of measurements
- Questions to be answered:
  - Effect of EoS on  $\alpha$  and  $R_{out}^2 - R_{side}^2$  versus  $\sqrt{s_{NN}}$ ?
  - What collision energy dependence do models predict?





# THANK YOU FOR YOUR ATTENTION



# BACKUP

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20/19

# INTERACTIONS

- Plane-wave result, based on  $|\Psi_{2,q}^{(0)}(r)|^2 = 1 + e^{iqr}$ , for pair source  $D(r)$

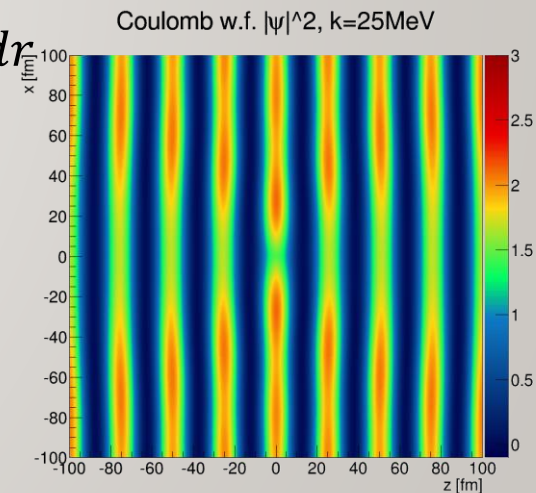
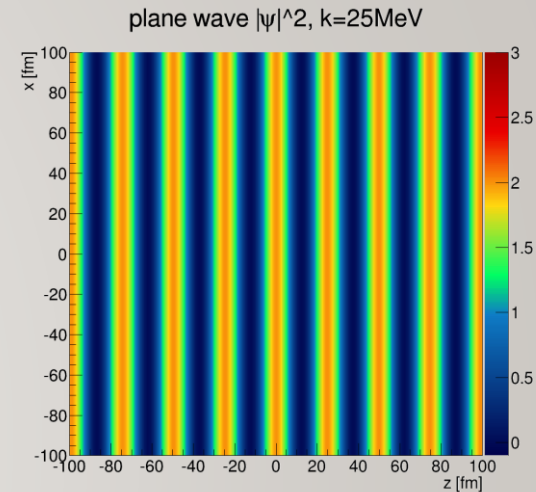
$$C_2(q, K) \cong \int D(r, K) |\Psi_{2,q}^{(0)}(r)|^2 dr = 1 + \int D(r, K) e^{iqr} dr$$

- If there are interactions, solve Schrödinger eq:  $\Psi_{2,q}^{(0)}(r) \rightarrow \Psi_{2,q}^{(\text{int})}(r_1, r_2)$
- For Coulomb, solution is known:  $|\Psi_{2,q}^{(C)}(r)|^2 = \frac{\pi\eta}{e^{2\pi\eta-1}}$  (hypergeometric expression)

- Direct fit with this, or the usual iterative Coulomb-correction:

$$C_{\text{Bose-Einstein}}(q)K(q), \text{ where } K(q) = \int D(r, K) |\Psi_{2,q}^{(C)}(r)|^2 dr / \int D(r, K) |\Psi_{2,q}^{(0)}(r)|^2 dr$$

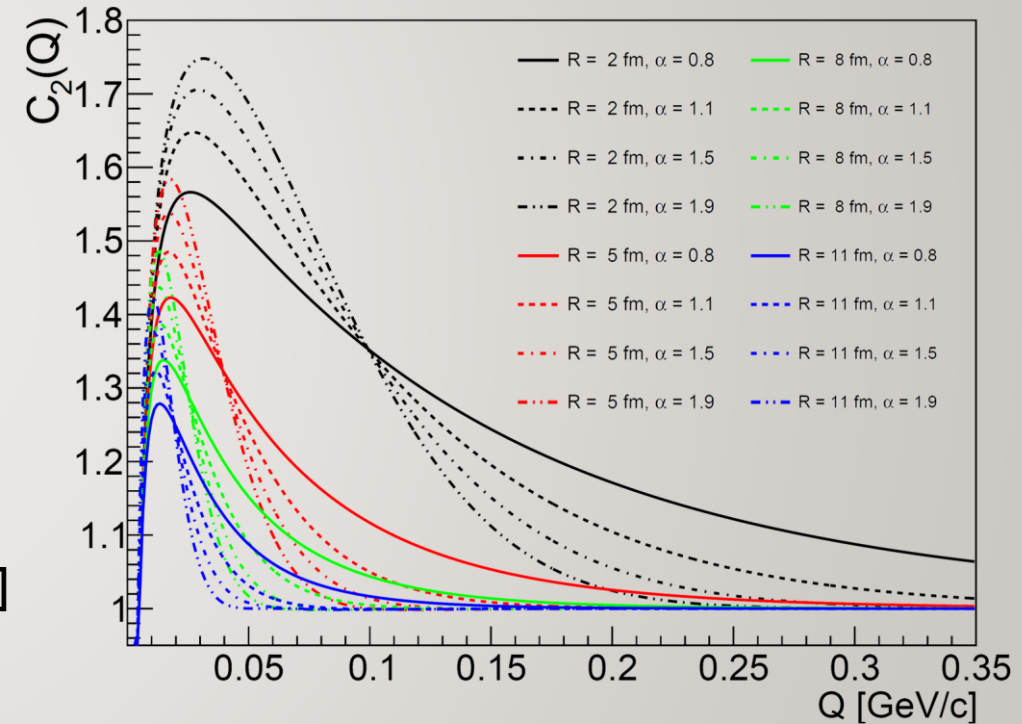
- Complication: need for integrating power-law tails**
  - Precalculated in a tabular form, iterative fitting, e.g., PHENIX, PRC97(2018)064911
  - Interpolating functional form, see Csanád, Lökös, Nagy, Phys.Part.Nucl. 51(2020)238
  - Role of the strong interaction, see Kincses, Nagy, Csanád, PRC102(2020)064912
  - Recent method: EPJC83(2023)1015, code at [github.com/csanadm/CoulCorrLevyIntegral](https://github.com/csanadm/CoulCorrLevyIntegral)
- Many new results, also for the strong interaction: see talk by M. Nagy on Tuesday





# HOW TO CALCULATE THE COULOMB EFFECT

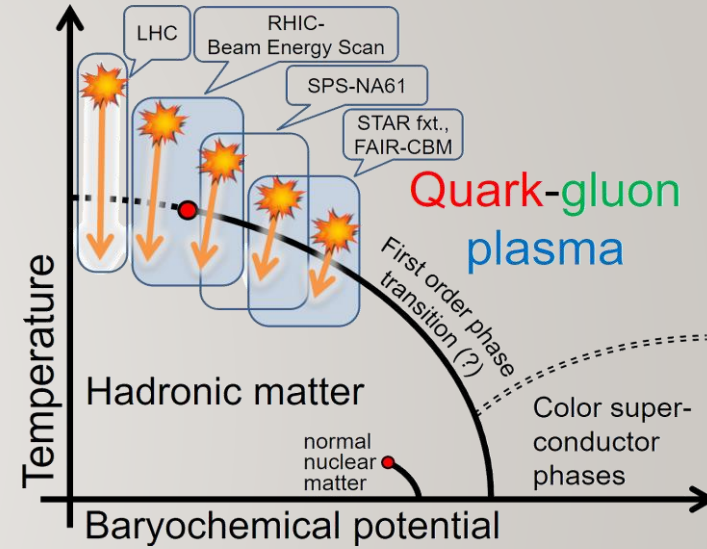
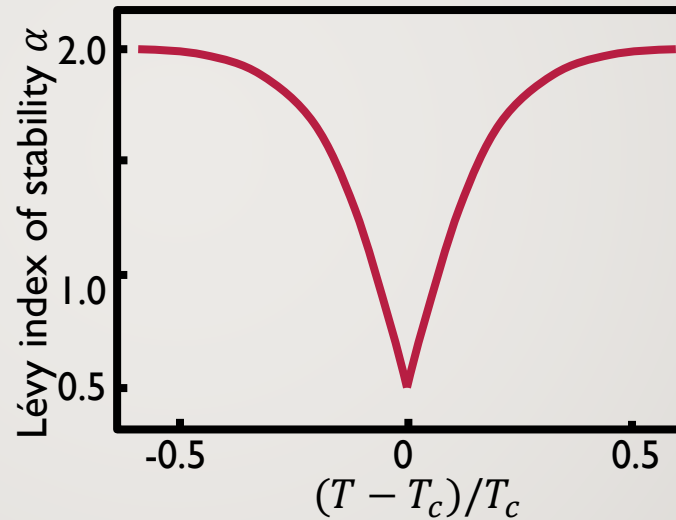
- Calculating correlation functions with the Coulomb effect included: **time consuming in the past**
- Method used in early analyses: Coulomb correction calculated for **fixed radius and shape**
  - For example, fixing  $R = 5$  fm and  $\alpha = 2$
- More consistent method: correlation function with Coulomb FSI **precalculated in a tabular form**
  - Iterative fitting, see e.g., PHENIX, PRC97 (2018) 6, 064911
- Convenient, but somewhat restricted method: **interpolating functional form**, in a limited  $R, \alpha$  range
  - See Csanád, Lökös, Nagy, Phys.Part.Nucl. 51 (2020) 238, used in arXiv:2306.11574 [CMS], arXiv:2302.04593 [NA61]
- **Recent method:** see talk by Márton Nagy
  - Nagy, Purzsa, Csanád, Kincses Eur. Phys. J. C 83, 1015 (2023), code at [github.com/csanadm/CoulCorrLevyIntegral](https://github.com/csanadm/CoulCorrLevyIntegral)
  - Recent developments: 3D calculation, protons, see talk by M. Nagy on Wednesday





# LÉVY INDEX AS A CRITICAL EXPONENT?

- Critical spatial correlation:  $\sim r^{-(d-2+\eta)}$ ; Lévy source:  $\sim r^{-(1+\alpha)}$ ;  $\alpha \Leftrightarrow \eta?$   
Csörgő, Hegyi, Zajc, Eur.Phys.J. C36 (2004) 67
- QCD universality class  $\leftrightarrow$  3D Ising  
Halasz et al., Phys.Rev.D58 (1998) 096007  
Stephanov et al., Phys.Rev.Lett.81 (1998) 4816
- At the critical point:
  - Random field 3D Ising:  $\eta = 0.50 \pm 0.05$   
Rieger, Phys.Rev.B52 (1995) 6659
  - 3D Ising:  $\eta = 0.03631(3)$   
El-Showk et al., J.Stat.Phys. 157 (4-5): 869
- Motivation for precise Lévy HBT!
- Change in  $\alpha_{\text{Lévy}}$  proximity of CEP?
- Finite-size/time & non-equilibrium effects  $\rightarrow$  what does power-law tail mean?
  - Finite-size effects not important? See e.g. Fytas et al, PRE93, 063308 (2016), Ballesteros et al., PLB387 (1996) 125

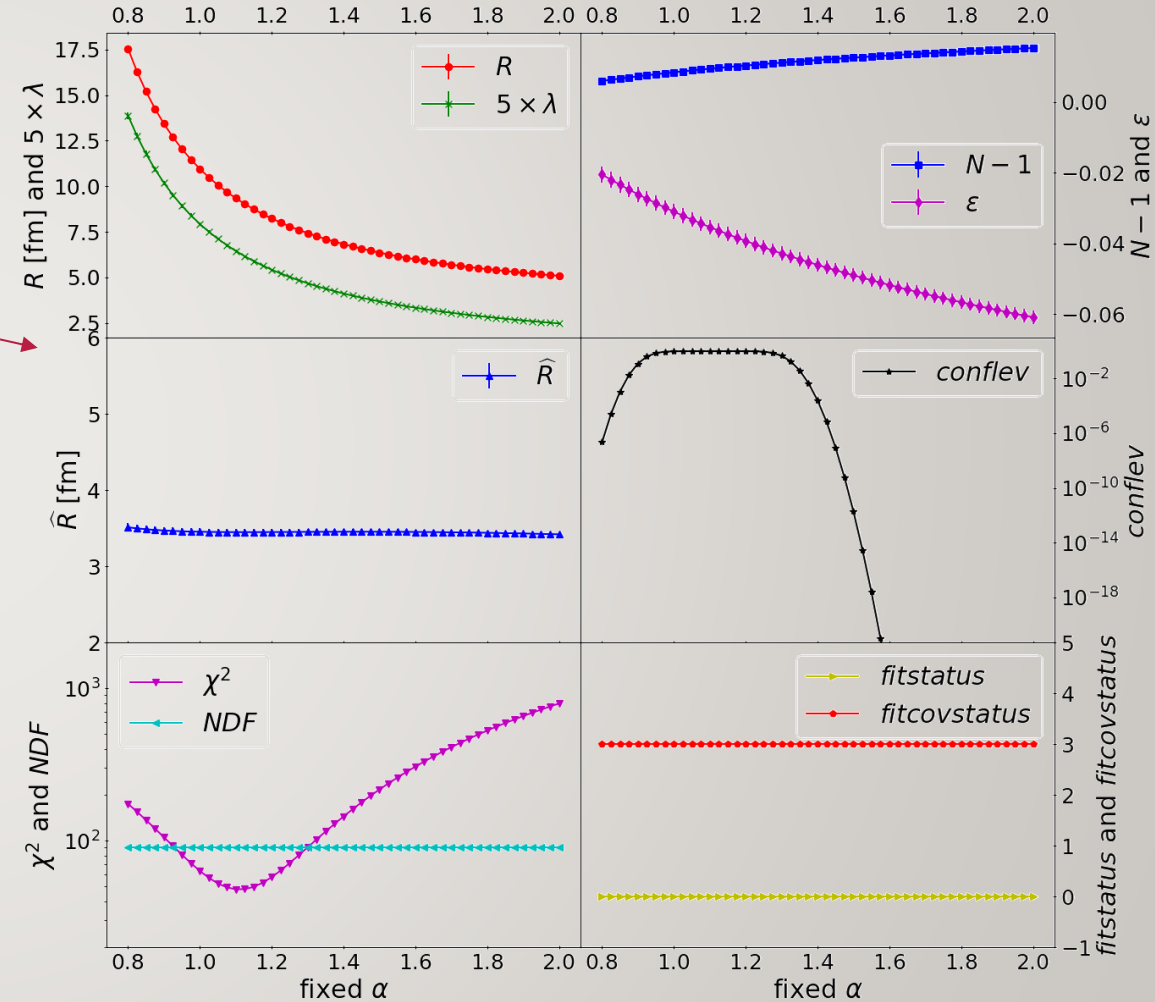
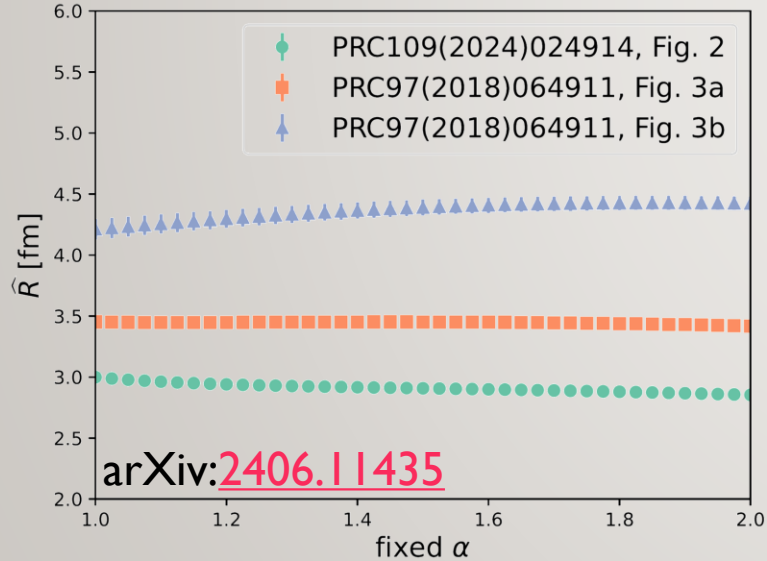






# RESCALING HBT RADII FROM GAUSS TO LÉVY

- Source shape and size entangled in Gaussian radii
- Fits possible with many  $\alpha$  values
  - Some statistically acceptable, some not
  - Fits to PHENIX HBT paper PRC 2018, Fig 3a
- $\hat{R} = R/[\lambda(1 + \alpha)]$  scaling observed generally



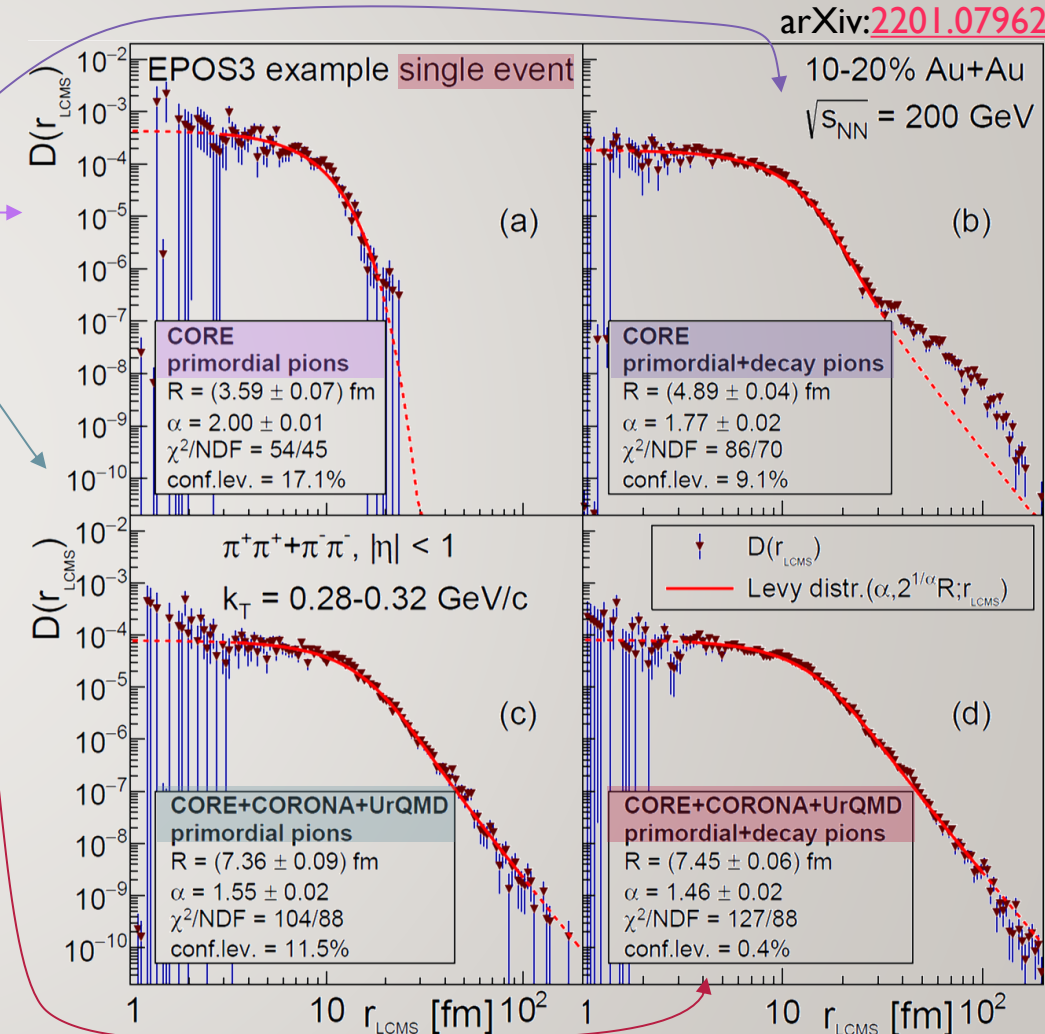


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# LÉVY SHAPES IN SINGLE EPOS EVENTS, 1D

- EPOS model: parton-based Gribov-Regge theory (PBGRT)
  - Werner et al., PRC82 (2010) 044904, PRC89 (2014) 064903, ...
- Source observed in four stages:
  - CORE, primordial pions: close to Gaussian
  - CORE, with decay products: power-law structures
  - CORE+CORONA+UrQMD, primordial pions: Lévy shape
  - CORE+CORONA+UrQMD, with decay products: Lévy shape
- Radii in the four stages (one example event)
 

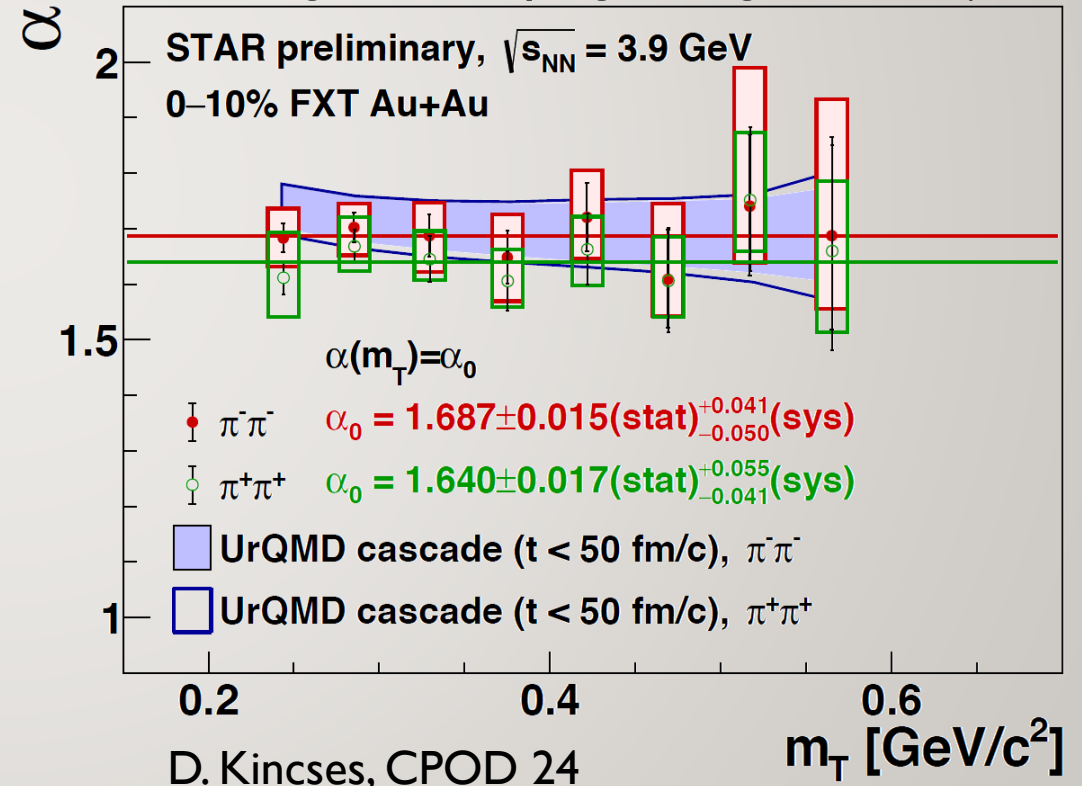
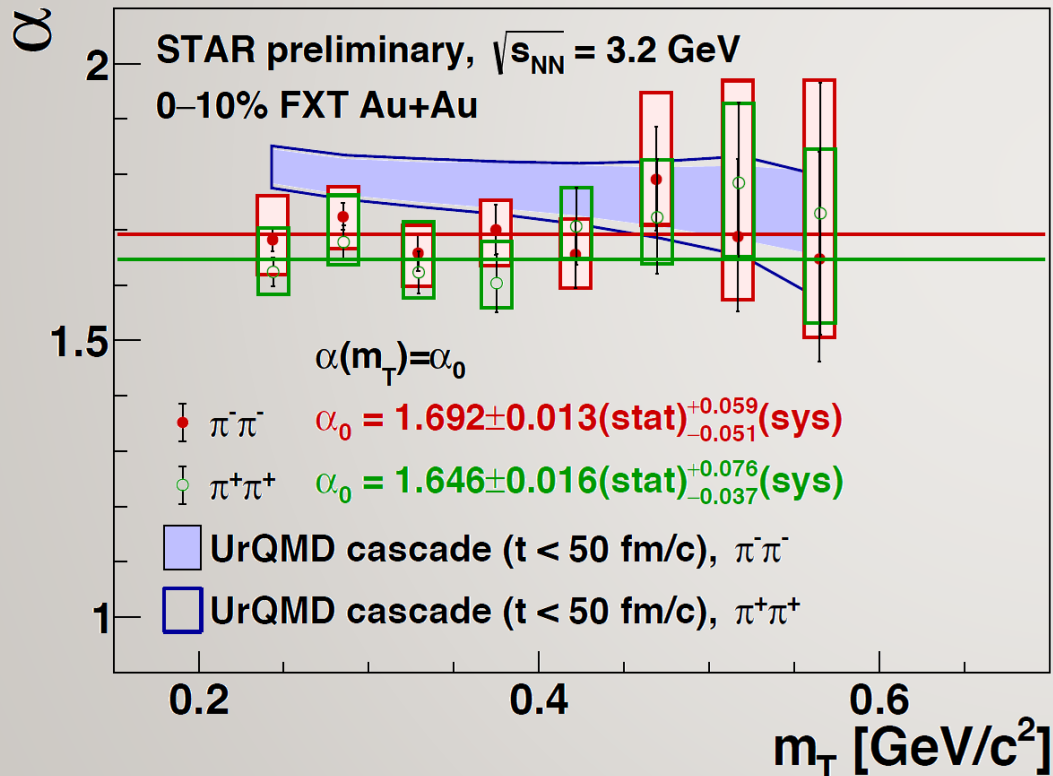
3.59 fm  $\rightarrow$  4.89 fm  $\rightarrow$  7.36 fm  $\rightarrow$  7.45 fm
- Shape ( $\alpha$ ) change: 2.00  $\rightarrow$  1.77  $\rightarrow$  1.55  $\rightarrow$  1.46
- Can one relate the observed HBT radii to the hydro phase homogeneity lengths?
- More investigations needed...
- See talks by D. Kincses, E. Árpási, L. Kovács, M. Molnár on Thu



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# FIXED TARGET ENERGIES: 3.2 AND 3.9 GEV

- Non-Gaussian values ( $\alpha < 2$ ); small systematic difference between  $\pi^- \pi^-$  and  $\pi^+ \pi^+$  pairs
- 3.9 and 3.2 GeV compatible, no  $m_T$  dependence observed
- UrQMD within uncertainties – no other effect but rescattering and decays, good agreement ( $t < 50$  fm/c!)







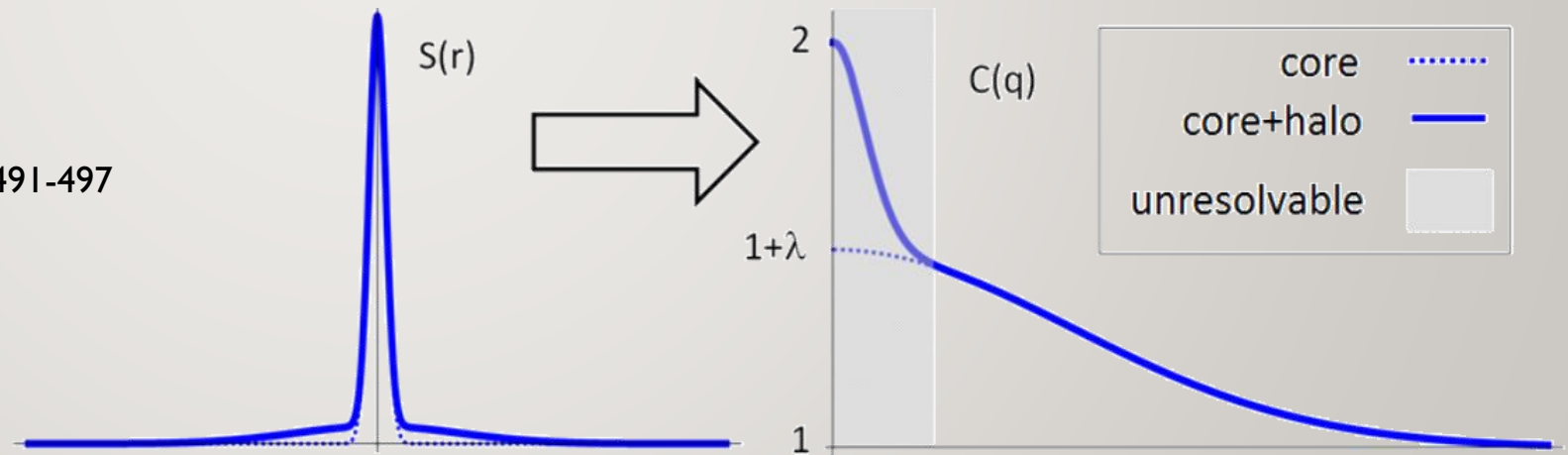
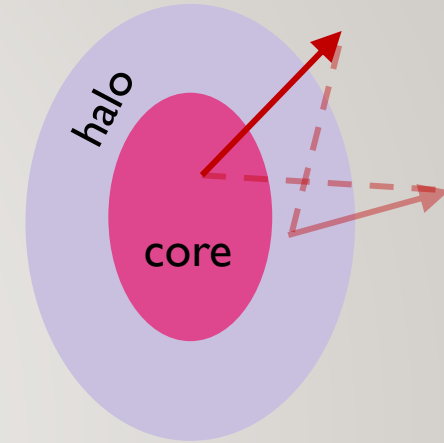
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# CORRELATION STRENGTH $\lambda$ : CORE/HALO

- Two-component core+halo source
  - Core: hydrodynamically expanding, thermal medium
  - Halo: long lived resonances ( $\gtrsim 10$  fm/c,  $\omega, \eta, \eta', K_0^S, \dots$ )
  - Unresolvable experimentally
  - Define  $f_C = N_{\text{core}}/N_{\text{total}}$
- True  $q \rightarrow 0$  limit:  $C(0) = 2$
- Apparently  $C(q \rightarrow 0) \rightarrow 1 + \lambda$
- $\lambda(m_T) = f_C^2(m_T)$

Bolz et al, Phys.Rev. D47 (1993) 3860-3870;

Csörgő, Lörstad, Zimányi, Z.Phys. C71 (1996) 491-497

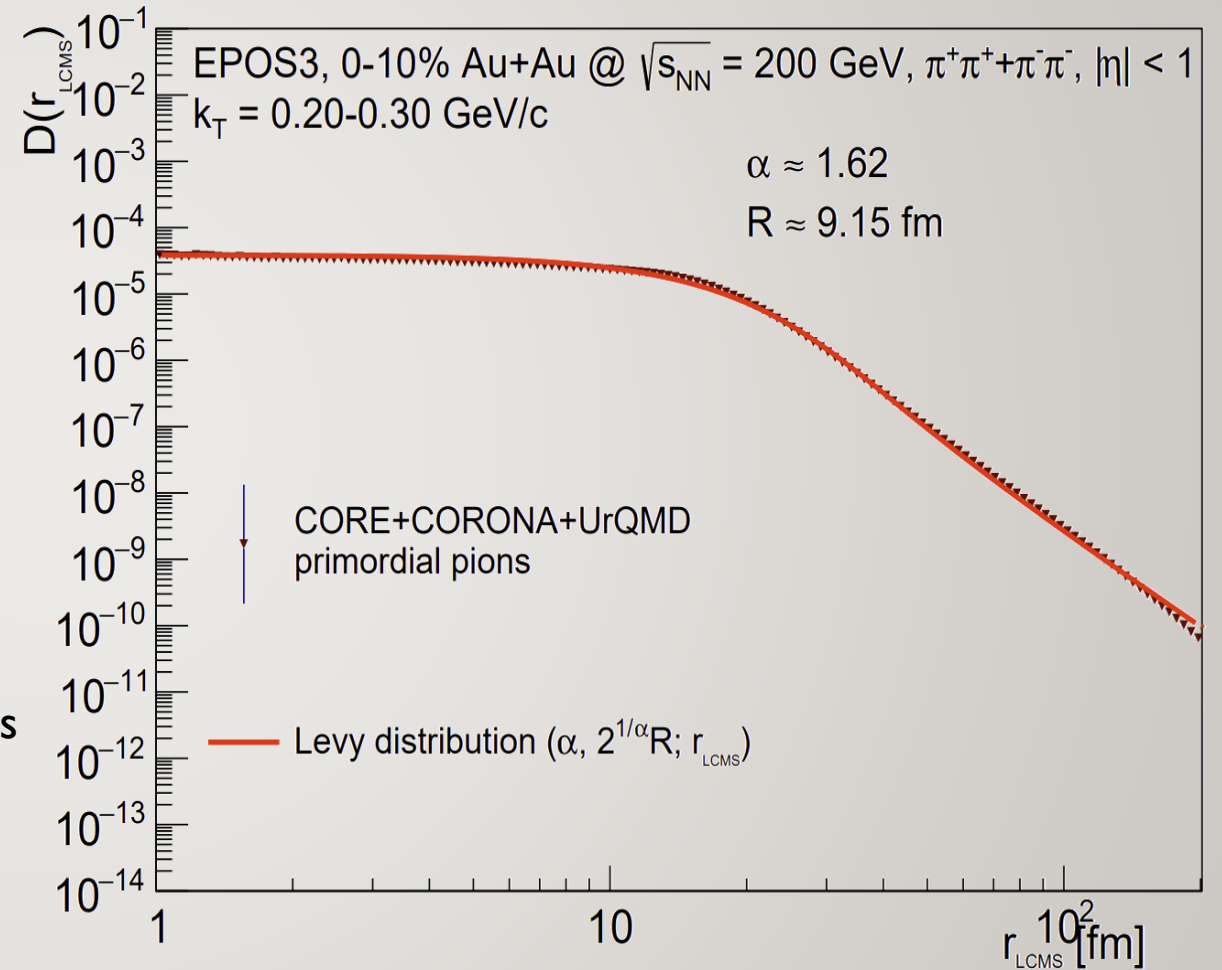




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# ROLE OF EVENT AVERAGING?

- Event-averaged source also analyzed
- Not perfectly Lévy shape, very large  $\chi^2$
- Nevertheless: similar parameters achieved
  - Event averaged:  
 $\alpha \approx 1.62, R \approx 9.15$  fm
  - Event-by-event:  
 $\alpha \approx 1.66, R \approx 8.96$  fm
- More reasonable approach for kaons
  - No event-by-event analysis possible for kaons



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# SOURCE OR PAIR DISTRIBUTION?

- Under some circumstances (thermal emission, no interactions, ...):

$$C_2(q, K) = \int S\left(r_1, K + \frac{q}{2}\right) S\left(r_2, K - \frac{q}{2}\right) |\Psi_2(r_1, r_2)|^2 dr_1 dr_2 \\ \cong 1 + \left| \int S(r, K) e^{iqr} dr \right|^2$$

- Let us introduce the spatial pair distribution:

$$D(r, K) = \int S\left(\rho + \frac{r}{2}, K\right) S\left(\rho - \frac{r}{2}, K\right) d\rho$$

- Then the Bose-Einstein correlation function becomes:

$$C_2(q, K) \cong \int D(r, K) |\Psi_2(r)|^2 dr = 1 + \int D(r, K) e^{iqr} dr$$

- **Bose-Einstein correlations measure spatial pair distributions!**
- Coulomb and strong Final State Interactions? Under control for Lévy sources

Csanad, Lökös, Nagy, Phys. Part. Nuclei 51 (2020) 238 [arXiv:1910.02231]

Kincses, Nagy, Csanad Phys. Rev. C102, 064912 (2020) [arXiv:1912.01381]



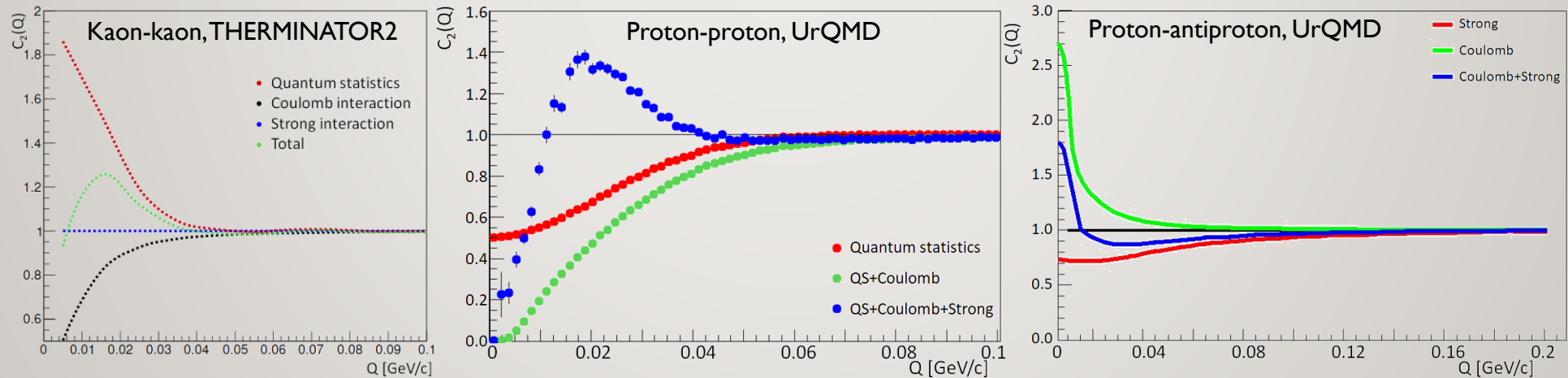


# ROLE OF THE STRONG INTERACTION

- In case of other interactions or not identical bosons, the formula still works:

$$C_2(q, K) \cong \int D(r, K) |\Psi_2(r)|^2 dr$$

- Pair wave function determines  $D \leftrightarrow C_2$  connection
- Mesons, baryons: strong interaction; fermions: anticorrelation
- Non-identical pairs: interaction modifies wave function



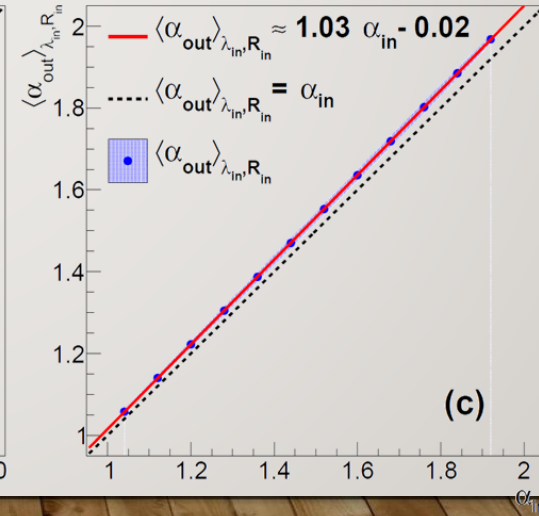
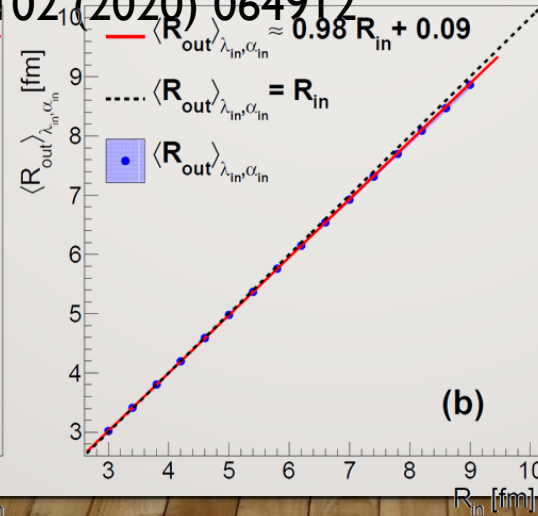
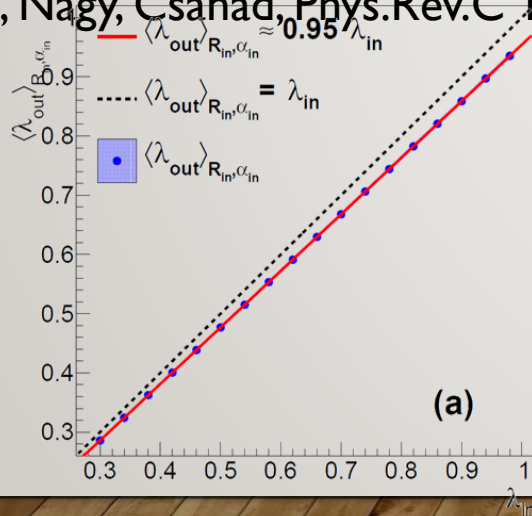
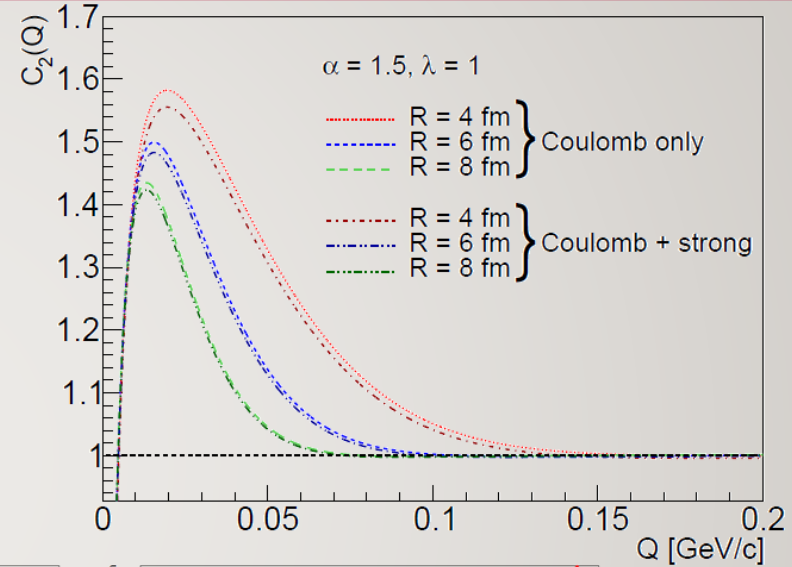
From e.g. H. Zbroszczyk's talk at Zimányi School 2019



# STRONG INTERACTION FOR PION PAIRS

- Additional potential appearing
- Possible handling: strong phase shift,  
Modify s-wave component in wave func.  
R. Lednicky, Phys. Part. Nucl.40, 307 (2009)
- Small difference in case of pions
- Few percent modification in  $\lambda, \alpha$

Kincses, Nagy, Csanád, Phys.Rev.C 102 (2020) 064912





# TWO-PARTICLE SPATIAL CORRELATIONS

- Object to be investigated: two-particle source

$$D(r, K) = \int d^4\rho S\left(\rho + \frac{r}{2}, K\right) S\left(\rho - \frac{r}{2}, K\right)$$

- Experimental results measure power-law tails, Lévy shapes
  - Measure momentum-space correlations, reconstruct  $D(r)$  or fit its parameters
- Why do these Lévy shapes appear?
  - What physics does contribute to it? Rescattering, decays?
  - What role does event averaging have in it?  
Cimerman, Plumberg, Tomasik, Phys.Part.Nucl. 51 (2020) 282, PoS ICHEP2020 538
  - What do specific  $\alpha$  values mean?
- Event generator models (like EPOS) – direct access to pair-source!
  - Phenomenological investigations of  $D(r)$  possible
  - Effects can be turned off or on, investigated separately

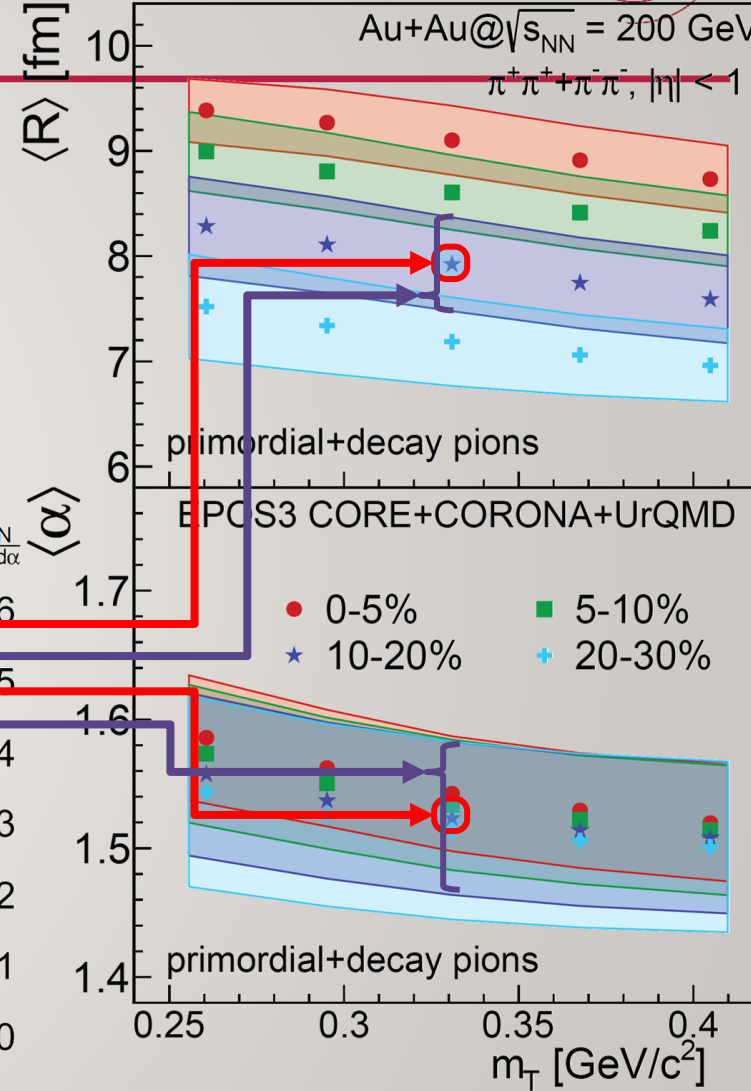
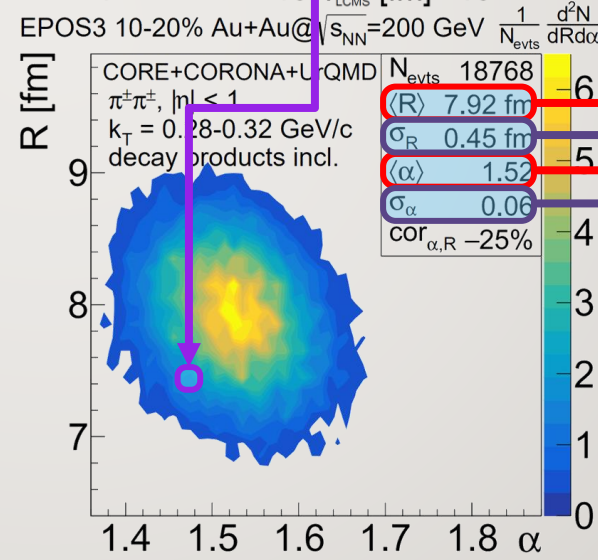
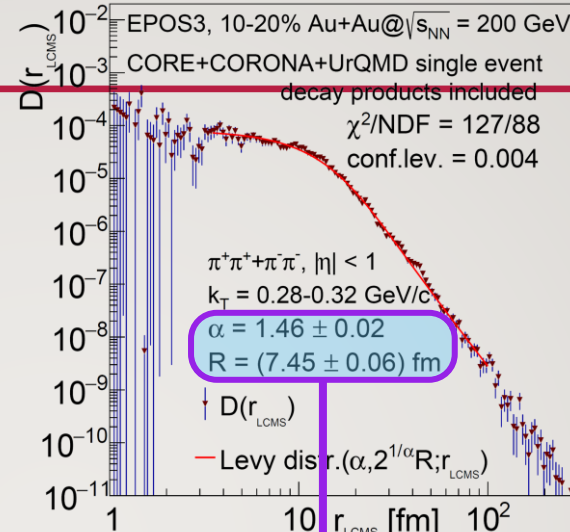




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# EPOS SUMMARY

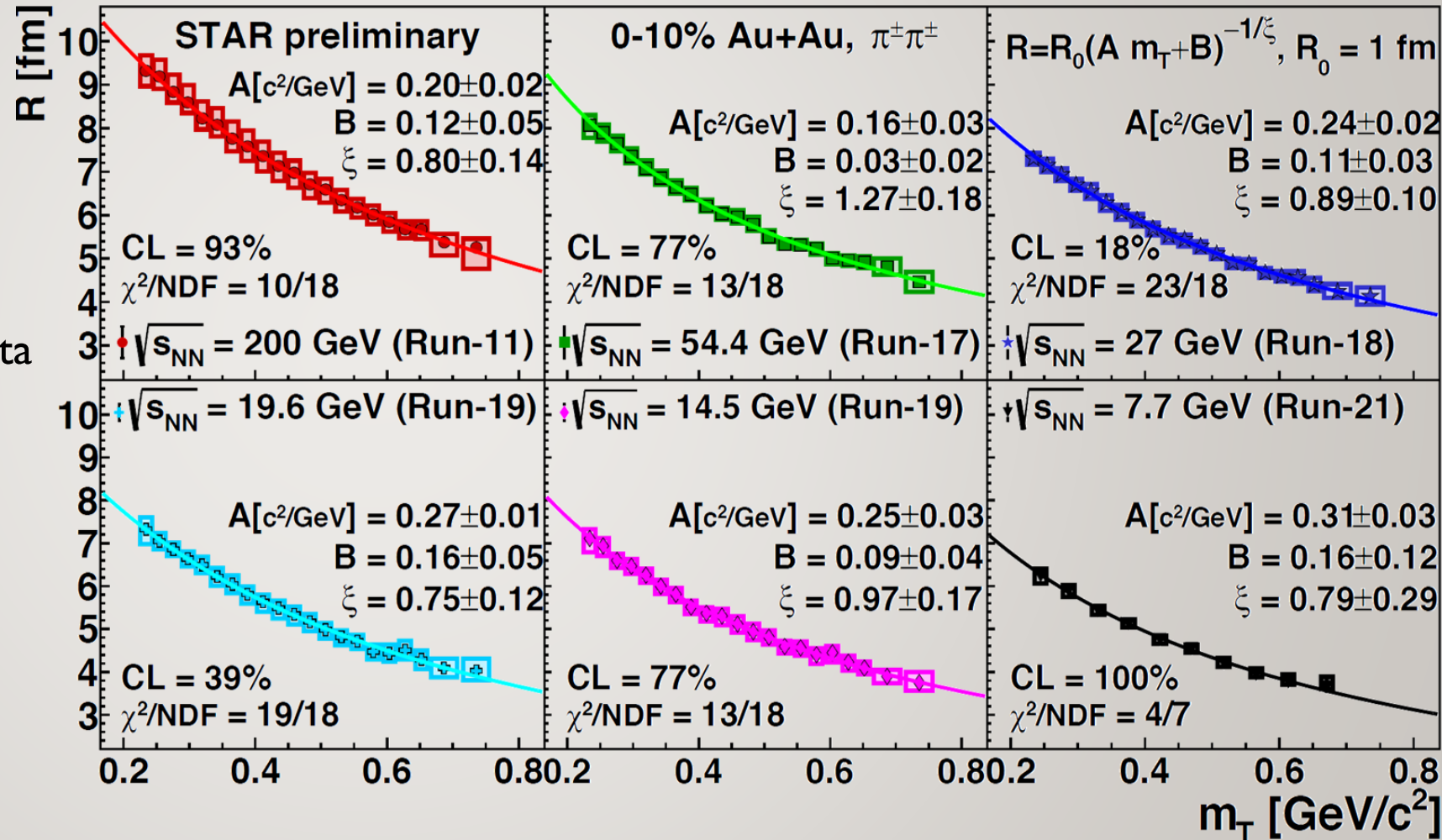
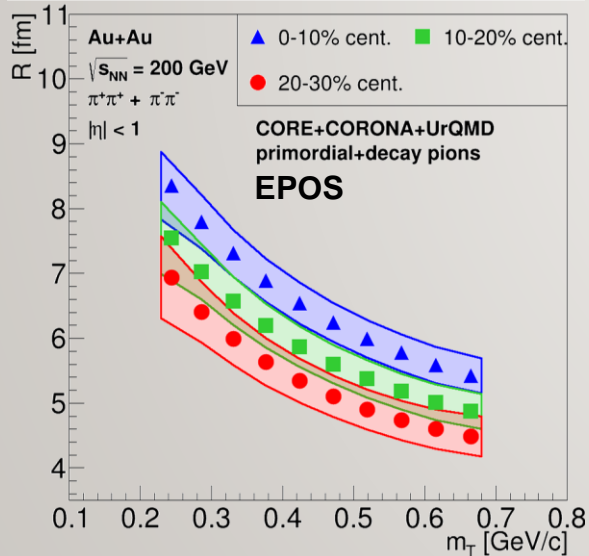
- $D(r)$  calculated in EPOS evt-by-evt
- Lévy fits done evt-by-evt
- Non-Gaussianity in single events
- Extracting mean, & std.dev. of  $R, \alpha$
- $m_T$  & centrality dependence





# RESULTS AT COLLIDER ENERGIES: 7.7 TO 200 GEV

- Slow decrease with  $\sqrt{s_{NN}}$  from 200 to 7.7 GeV
  - Same trend as Gaussian  $R$
- Decrease in  $R$  with  $m_T$ 
  - Connection to flow
- 200 GeV: EPOS close to data



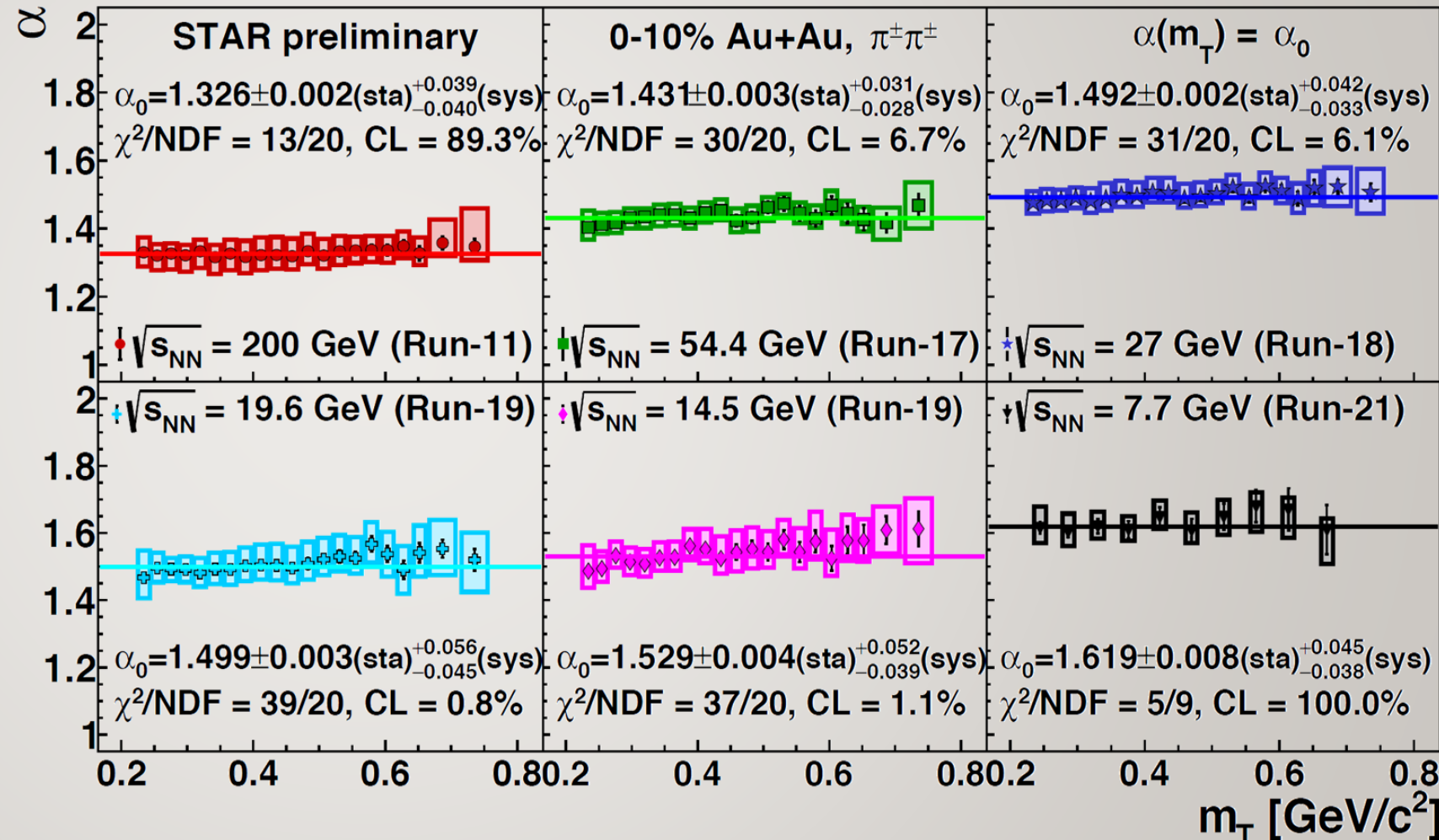




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# RESULTS AT COLLIDER ENERGIES: 7.7 TO 200 GEV

- Small, smooth increase in  $\alpha$  with  $\sqrt{s_{NN}}$  from 200 to 7.7 GeV
  - Connection to decreased density?
- No strong dependence on  $m_T$
- Average  $\alpha$ 
  - $\approx 1.33$  at 200 GeV
  - $\approx 1.62$  at 7.7 GeV
- Significantly below 2.0 and above 1.0



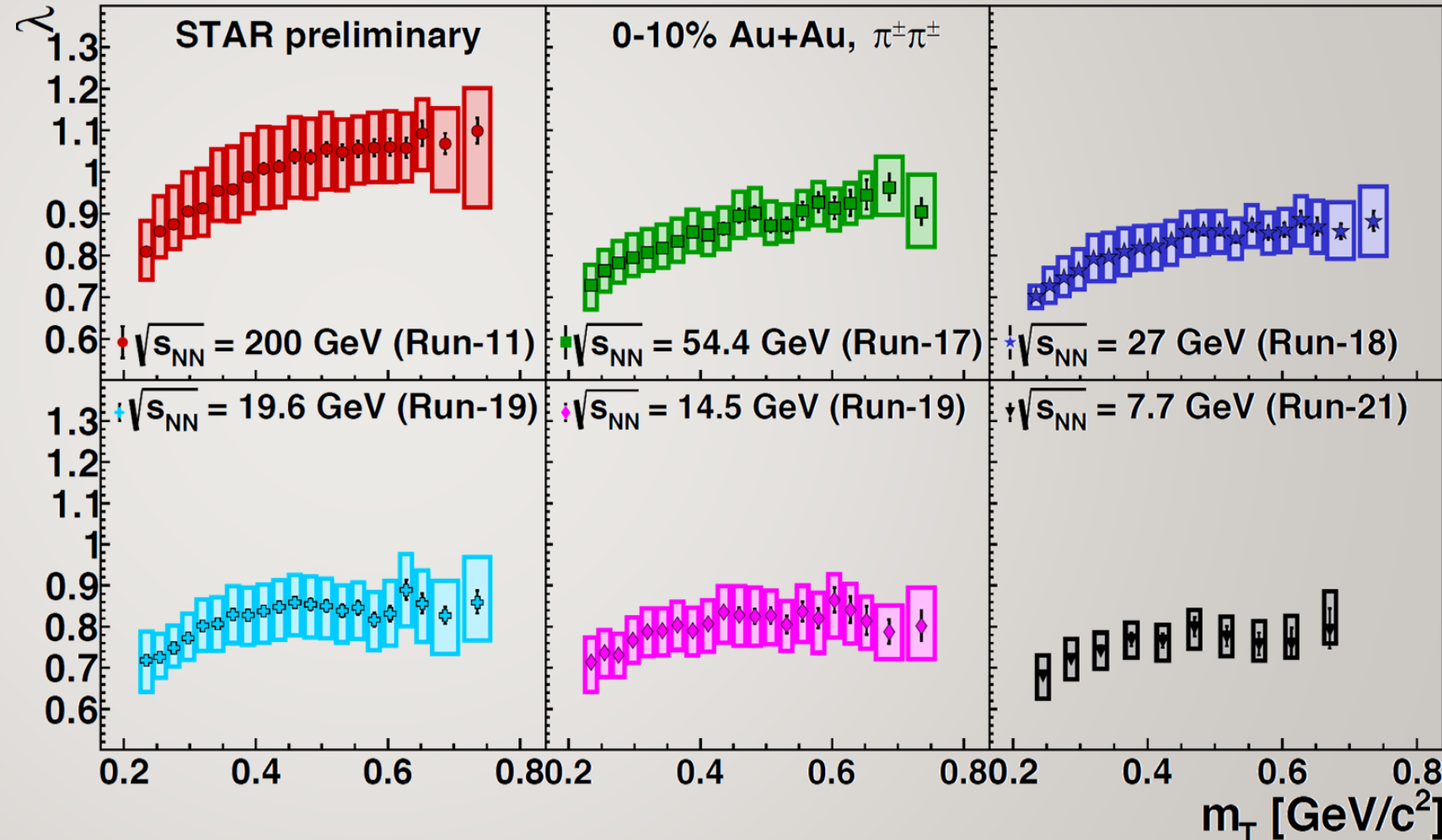




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# RESULTS AT COLLIDER ENERGIES: 7.7 TO 200 GEV

- Clear decrease in  $\lambda$  with  $\sqrt{s_{NN}}$  from 200 to 7.7 GeV
  - Decrease in multiplicity
  - Larger role of halo
- Decrease towards small  $m_T$  values
  - Increase in halo for small  $m_T$
  - Attributed to modified in-medium  $\eta'$  mass in literature



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# LÉVY SCALE R AT FXT ENERGIES

- Decreases towards higher  $m_T$  and lower energies
- Small systematic difference between  $\pi^-\pi^-$  and  $\pi^+\pi^+$  pairs
- Two FXT energies compatible
- UrQMD describes the trends qualitatively well, moderate quantitative mismatch, but ran only until 50 fm/c

