

Bayesian Inference for QGP Properties: Integrating high- p_{\perp} and low- p_{\perp} data with Bayes-DREENA

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DREENA framework

- **Dynamical Radiative and Elastic ENergy loss Approach**
- fully optimized numerical procedure capable of generating high p_{\perp} predictions
- includes:
 - parton production
 - multi gluon-fluctuations
 - path-length fluctutations
 - fragmentation functions
- keeping all elements of the state-of-the art energy loss formalism, while introducing more complex medium evolutions:
 - **DREENA-C: constant temperature medium**
D. Z., I. Salom, J. Auvinen, M. Djordjevic and M. Djordjevic, J. Phys. G **46**, no. 8, 085101 (2019).
 - **DREENA-B: Bjorken expansion**
D. Z., I. Salom, J. Auvinen, M. Djordjevic and M. Djordjevic, Phys. Lett. B **791**, 236 (2019).
 - **DREENA-A: smooth (2+1)D temperature evolution**
D. Z., I. Salom, J. Auvinen, P. Huovinen and M. Djordjevic, Front. in Phys. **10**, 957019 (2022).
 - **ebe-DREENA: event-by-event fluctuating hydro background**
D. Z., J. Auvinen, I. Salom, P. Huovinen and M. Djordjevic, Phys. Rev. C **106**, no.4, 044909 (2022)

QGP tomography

Bulk QGP properties are traditionally explored by low- p_{\perp} observables that describe the collective motion of 99.9% of QCD matter



However, some important bulk QGP properties are known to be difficult to constrain by low- p_{\perp} observables and the corresponding theory / simulations



We advocate high- p_{\perp} QGP tomography, where low- and high- p_{\perp} physics jointly constrain bulk QGP parameters

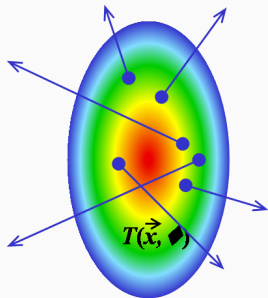
Rare high energy probes are, on the other hand, almost exclusively used to understand high- p_{\perp} parton - medium interactions



While high- p_{\perp} physics played a decisive role in QGP discovery, it has rarely been used to understand bulk QGP properties



QGP tomography

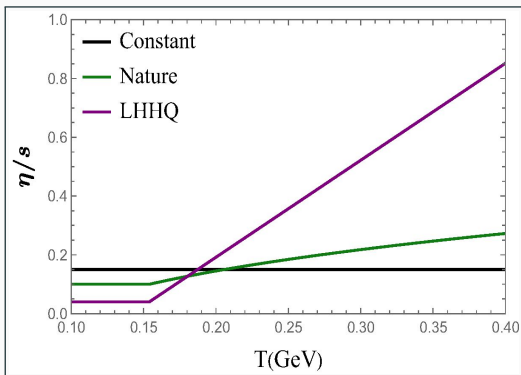


- high energy particles lose energy
- energy loss sensitive to QGP properties
- predict the energy loss of high p_{\perp} probes
- use high p_{\perp} probes to infer QGP properties:
 - QGP anisotropy
 - early evolution
 - η/s parametrization
 - initial stages

talk by Bithika, Tuesday 11:45

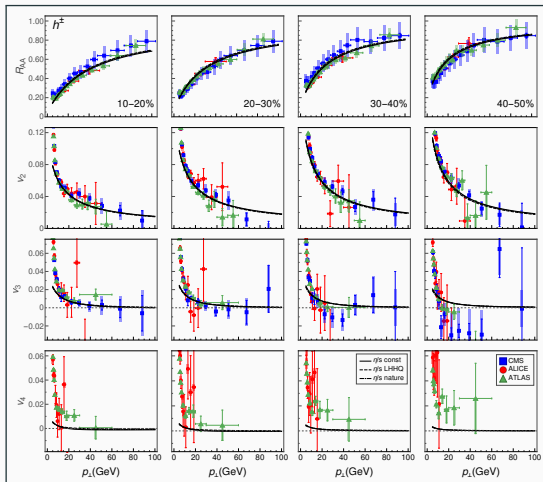
- DREENA-A on github:
<https://github.com/DusanZigic/DREENA-A>
<https://github.com/DusanZigic/ebeDREENA>

different parametrization of η/s



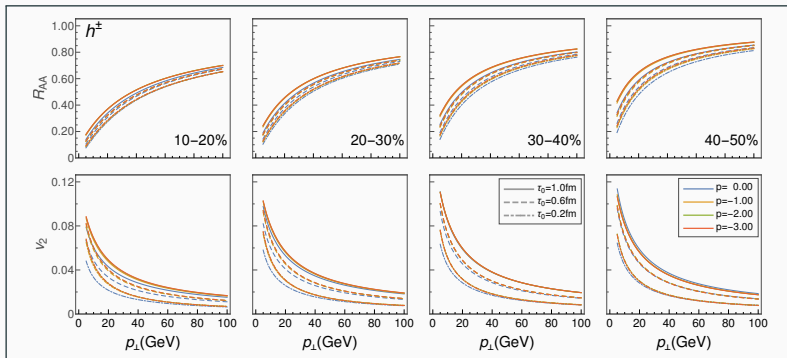
can high- p_{\perp} further constrain η/s ?

TRENTO+VISHNU+URQMD+DREENA

Pb+Pb, $\sqrt{s_{NN}}=5.02\text{TeV}$, h^\pm 

TRENTO+VISHNU+URQMD+DREENA

Pb+Pb, $\sqrt{s_{NN}}=5.02\text{TeV}$, h^\pm



could not compensate earlier hydro onset with p

Bayes theorem

A diagram illustrating Bayes' theorem. The equation is enclosed in a black rectangular box. The text 'posterior, \mathcal{P} ' is on the left, with a green arrow pointing to the left side of the equation. The text 'likelihood, \mathcal{L} ' is at the top center, with a red arrow pointing to the numerator's first term. The text 'prior, π ' is at the top right, with a blue arrow pointing to the numerator's second term. The text 'evidence, \mathcal{Z} , (marginal likelihood)' is at the bottom center, with a purple arrow pointing to the denominator. The equation itself is
$$P(\Theta|\mathcal{D},\mathcal{M}) = \frac{P(\mathcal{D}|\Theta,\mathcal{M})P(\Theta|\mathcal{M})}{P(\mathcal{D}|\mathcal{M})}$$

Bayes theorem

A diagram illustrating Bayes' theorem. The equation $P(\Theta|\mathcal{D}, \mathcal{M}) \propto P(\mathcal{D}|\Theta, \mathcal{M})P(\Theta|\mathcal{M})$ is shown. A teal arrow points from the label 'posterior, \mathcal{P} ' to the left side of the equation. A red arrow points from the label 'likelihood, \mathcal{L} ' to the middle term $P(\mathcal{D}|\Theta, \mathcal{M})$. A blue arrow points from the label 'prior, π ' to the right term $P(\Theta|\mathcal{M})$.

$$\text{posterior, } \mathcal{P} \rightarrow P(\Theta|\mathcal{D}, \mathcal{M}) \propto P(\mathcal{D}|\Theta, \mathcal{M})P(\Theta|\mathcal{M})$$

likelihood, \mathcal{L}

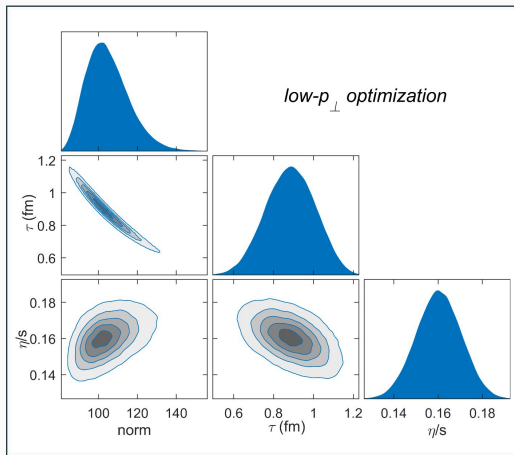
prior, π

- generate model predictions on latin hypercube
- PCA on model outputs
- Gaussian processes
- MCMC

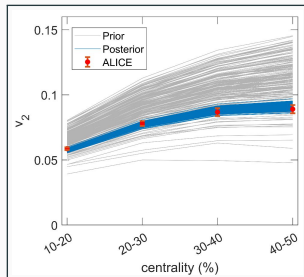
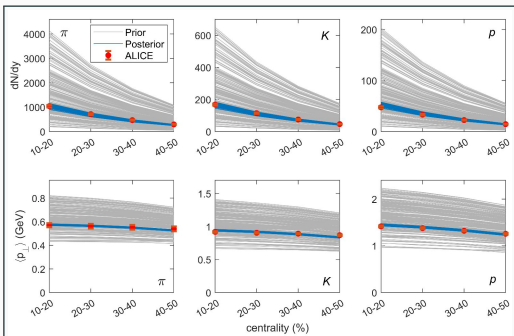
- TRENTO+VISHNU+URQMD+DREENA
 - τ_0 : 0.2-1.3fm
 - constant η/s : 0.02-0.2
 - norm: 60-360

Bayes inference

marginal distributions of parameters obtained with Bayesian inference on low- p_{\perp} data

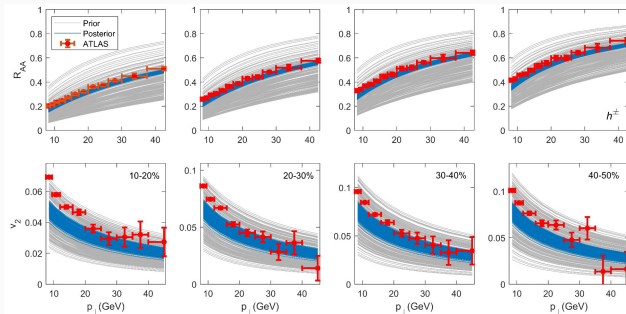


prior vs. posterior: low- p_{\perp} data

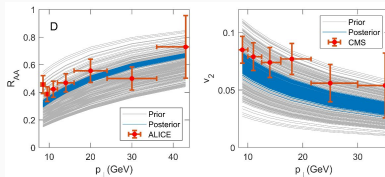


very good agreement with low- p_{\perp} data

prior vs. posterior: high- p_{\perp} data

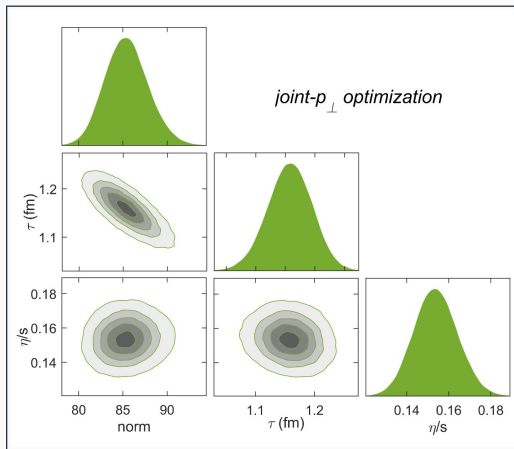


suboptimal
agreement
with high- p_{\perp}
data

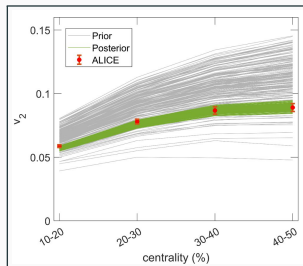
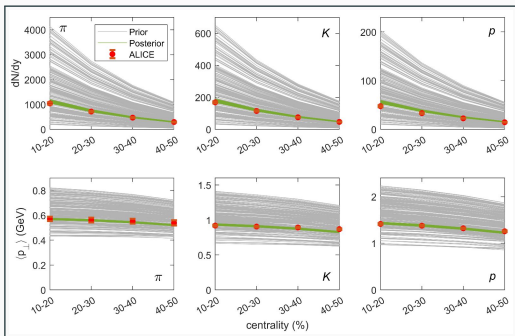


Bayes inference

marginal distributions of parameters obtained with Bayesian inference on both low- and high- p_{\perp} data



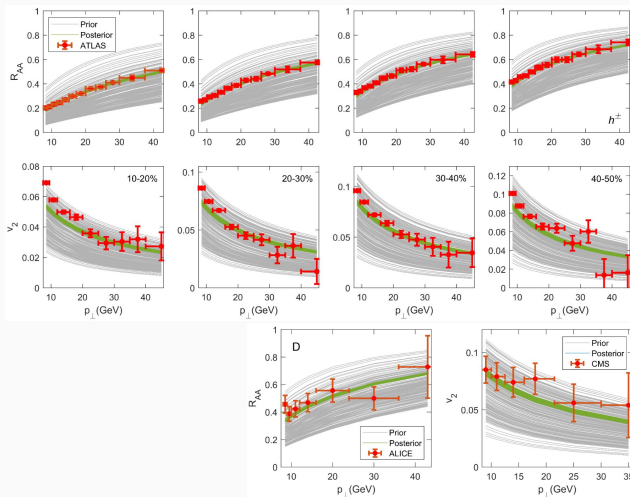
prior vs. posterior: low- p_{\perp} data



very good agreement with low- p_{\perp} data

Bayesian inference

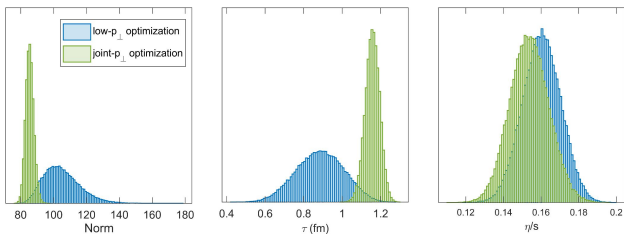
prior vs. posterior: high- p_{\perp} data



very good
agreement
with high- p_{\perp}
data as well



comparison of parameter distributions from low- and joint- p_{\perp} Bayesian inference



- distributions are not inconsistent with each other
- inclusion of high- p_{\perp} data significantly narrows the distributions of parameters
- high- p_{\perp} data is necessary for precision extraction of QGP parameters
- overall, jet tomography is crucial for constraining QGP properties

Summary

- manually:
 - η/s parametrization
 - initial stages
- Bayes rule and MCMC
 - distributions consistent with each other
 - high- p_{\perp} narrows distributions
- there are link for all papers, codes, youtube lectures,...

Acknowledgements



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**МИНИСТАРСТВО ПРОСВЕТЕ,
НАУКЕ И ТЕХНОЛОШКОГ РАЗВОЈА**

Thank you for your attention!

priors

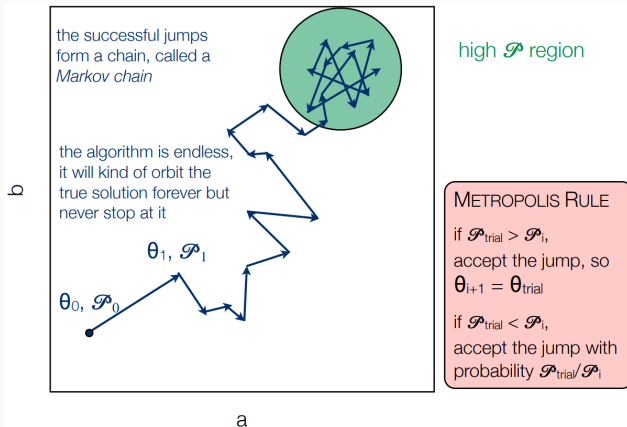
$$P(\boldsymbol{\theta}|\mathcal{M}) \propto \begin{cases} 1 & \text{if } \min(\theta_i) \leq \theta_i \leq \max(\theta_i) \text{ for all } i \\ 0 & \text{else} \end{cases}$$

likelihood

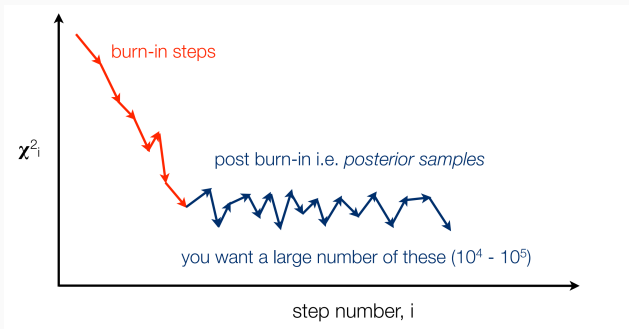
$$P(\mathcal{D}|\boldsymbol{\theta}, \mathcal{M}) = \prod_{i=1}^N \frac{1}{\sqrt{2\pi}\sigma_i} e^{-\frac{1}{2} \frac{(y_{m_i} - y_{e_i})^2}{\sigma_i^2}}$$

$$P(\mathcal{D}|\boldsymbol{\theta}, \mathcal{M}) = \frac{1}{\sqrt{2\pi \det \Sigma}} e^{-\frac{1}{2} [\mathbf{y}_m(\mathbf{x}) - \mathbf{y}_e]^T \Sigma^{-1} [\mathbf{y}_m(\mathbf{x}) - \mathbf{y}_e]}$$

MCMC



MCMC



energy loss:

$$\frac{dE_{col}}{d\tau} = \frac{2C_R}{\pi v^2} \alpha_S(E T) \alpha_S(\mu_E^2(T)) \times$$

$$\int_0^\infty n_{eq}(|\vec{k}|, T) d|\vec{k}| \left(\int_0^{|\vec{k}|/(1+v)} d|\vec{q}| \int_{-v|\vec{q}|}^{v|\vec{q}|} \omega d\omega + \int_{|\vec{k}|/(1+v)}^{|\vec{q}|_{max}} d|\vec{q}| \int_{|\vec{q}|-2|\vec{k}|}^{v|\vec{q}|} \omega d\omega \right) \times$$

$$\left(|\Delta_L(q, T)|^2 \frac{(2|\vec{k}| + \omega)^2 - |\vec{q}|^2}{2} + |\Delta_T(q, T)|^2 \frac{(|\vec{q}|^2 - \omega^2)((2|\vec{k}| + \omega)^2 + |\vec{q}|^2)}{4|\vec{q}|^4} (v^2|\vec{q}|^2 - \omega^2) \right)$$

$$\frac{d^2 N_{rad}}{dx d\tau} = \int \frac{d^2 k}{\pi} \frac{d^2 q}{\pi} \frac{2 C_R C_2(G) T}{x} \frac{\mu_E(T)^2 - \mu_M(T)^2}{(q^2 + \mu_M(T)^2)(q^2 + \mu_E(T)^2)} \frac{\alpha_S(E T) \alpha_S(\frac{\mathbf{k}^2 + \chi(T)}{x})}{\pi}$$

$$\times \frac{(\mathbf{k} + \mathbf{q})}{(\mathbf{k} + \mathbf{q})^2 + \chi(T)} \left(1 - \cos \left(\frac{(\mathbf{k} + \mathbf{q})^2 + \chi(T)}{xE^+} \tau \right) \right) \left(\frac{(\mathbf{k} + \mathbf{q})}{(\mathbf{k} + \mathbf{q})^2 + \chi(T)} - \frac{\mathbf{k}}{\mathbf{k}^2 + \chi(T)} \right)$$