



Update on SPS impedance reference measurements:

Head-tail mode zero growth rates
and tune slopes vs chromaticity

IPP MD days 2025

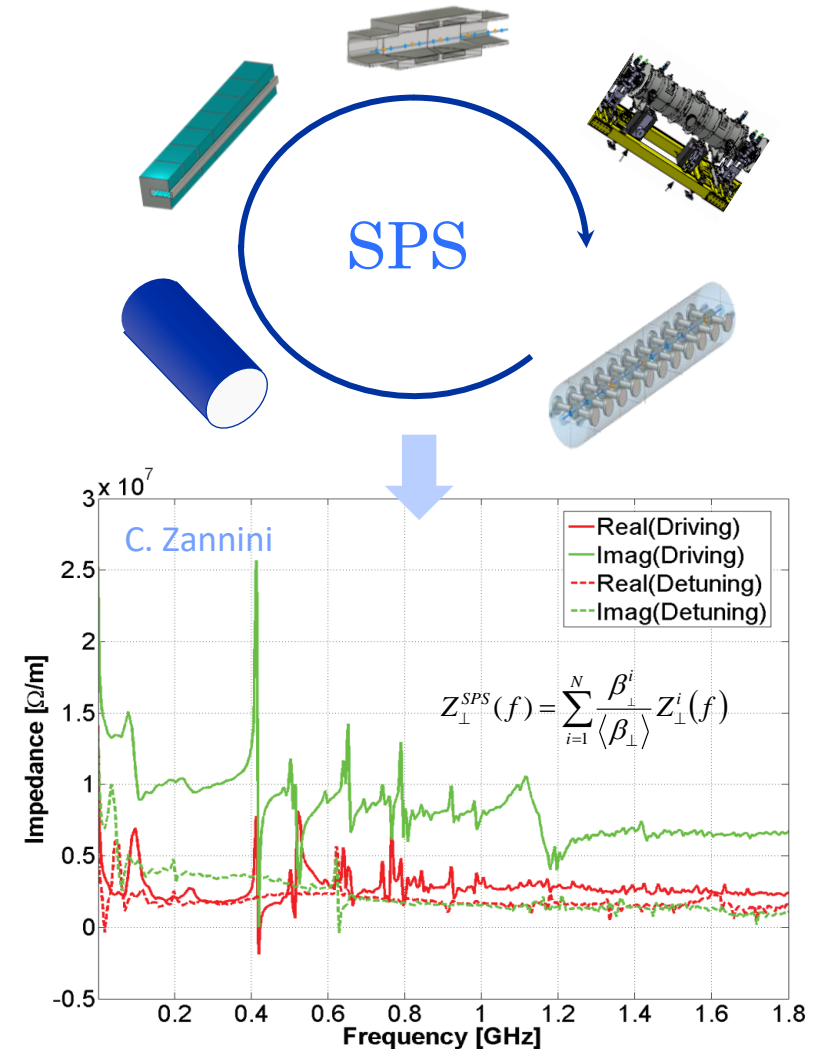
Miguel Gonzalez, Elena de la Fuente, Ingrid Mases, Carlo Zannini

Special thanks to the SPS & PSB operators for all the help during the MDs, and to all the colleagues that contributed to the project

Impedance reference measurements

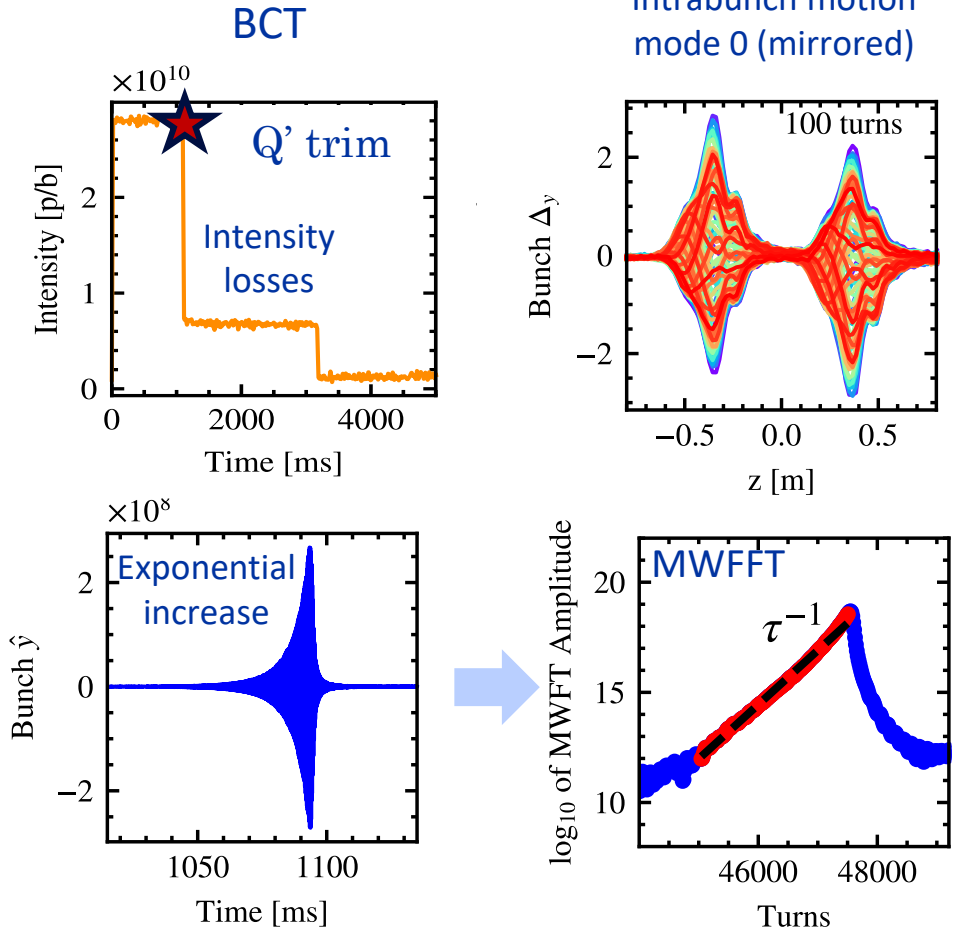
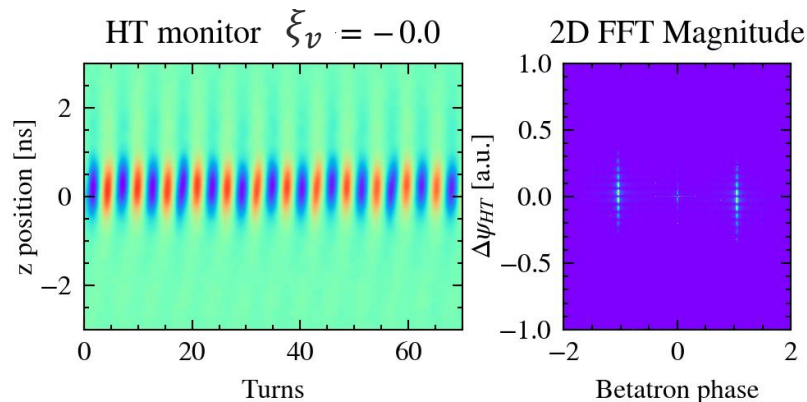
- The **SPS transverse impedance model** contains the major beam-coupling impedance sources in the accelerator.
 - Used as input for macroparticle tracking simulations (PyHeadtail, Xsuite) to predict beam behavior
- We **benchmark this model** with beam-based measurements.
 - The Head-Tail mode zero growth rates τ^{-1} vs **chromaticity** ξ gives us information on the **real part** of the **transverse effective impedance** $Z_{\perp,dip}^{eff}$

$$\tau^{-1}(\xi) = \Gamma \left(\frac{1}{2} \right) \frac{\text{Re} \left[Z_{\perp,dip}^{eff}(\xi) \right] N r_0 c^2}{8 \pi^2 \gamma Q_{\perp} \sigma_z}$$



Measurements methodology

- Measurements are performed with single bunch and low intensity $\sim 3e10$ p/b.
- The beam becomes **unstable** when the **negative chromaticity trim** (LSA QPH or QPV) is applied, triggering the Head-Tail mode zero observables.
- We perform a negative **chromaticity scan** in H or V plane, measuring the **growth rates** τ^{-1} for each LSA trim using the Moving Window FFT (MWFFT) technique.
- We crosscheck **chromaticity value on-the-fly from HT monitor data***

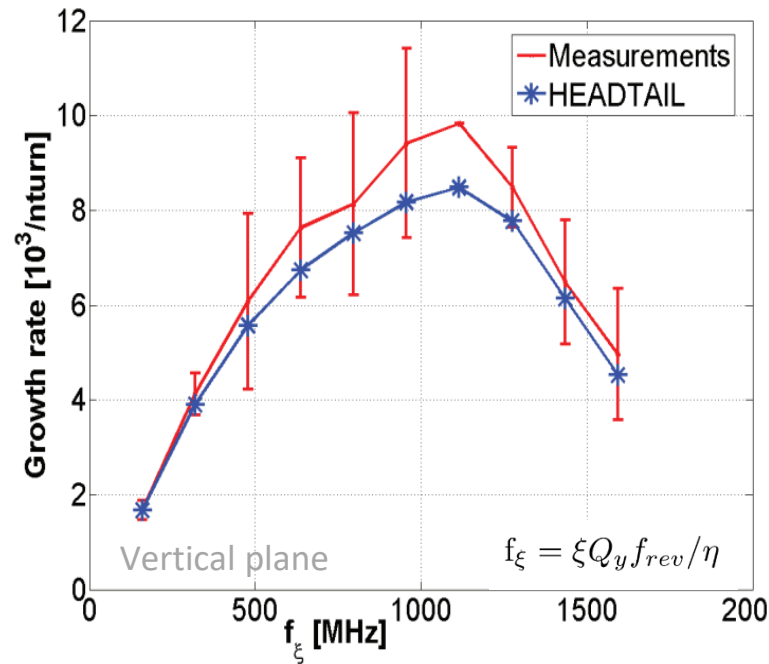


Previous findings

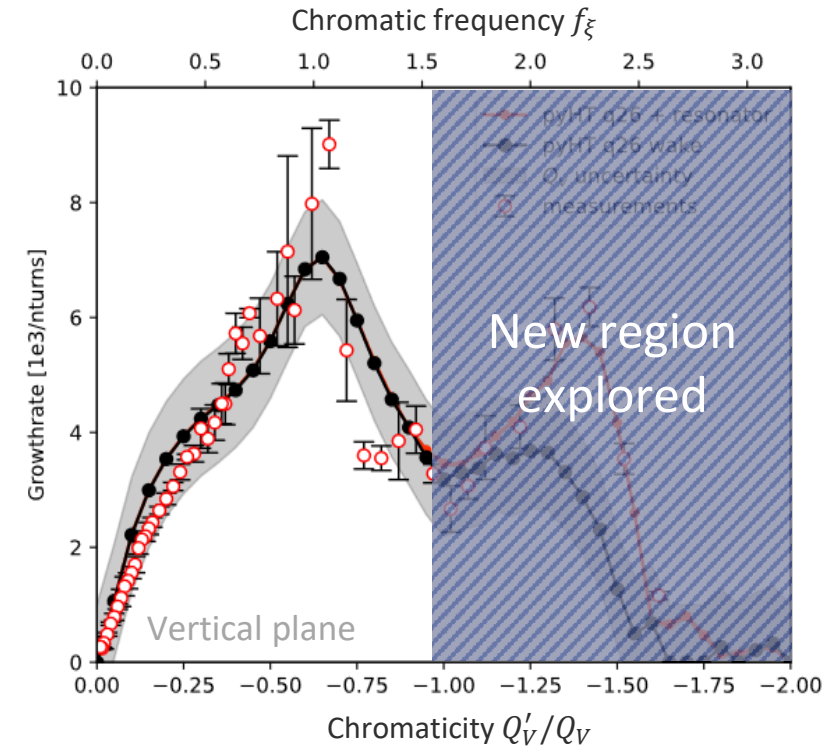
*C. Zannini, MOPJE049, IPAC 15
 **E. de la Fuente, WEPL155, IPAC 23

- During the **2022 campaign** we wanted to explore the high frequency region $f_\xi > 1.5$ GHz with **Q26 optics**.
 - ✓ We could reproduce the lower frequency region (<1.5GHz) as in Pre-LS2
 - ✗ The newly explored high frequency region showed an **unexpected discrepancy** with the model, hinting at a **missing impedance**
- In **2024**, new measurements to certify the existence of such impedance:
- Different working point / vertical tune
 - Different energy
 - Tune shift slope vs chromaticity

2013 measurements*
Pre-LS2



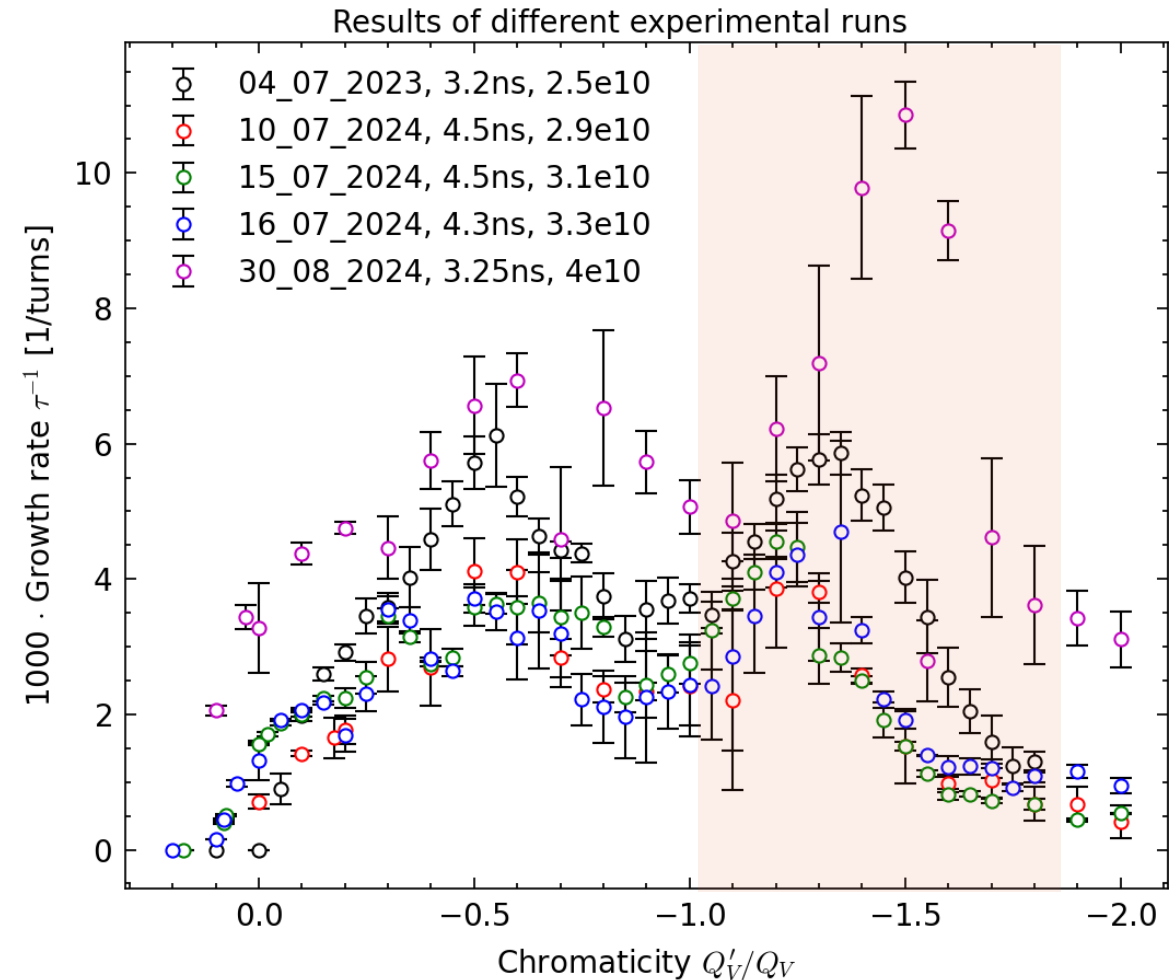
2022-23 measurements**



Added resonator parameters:
 $R_s=2e7\Omega/m$, $Q=100$, $f=2.5$ GHz

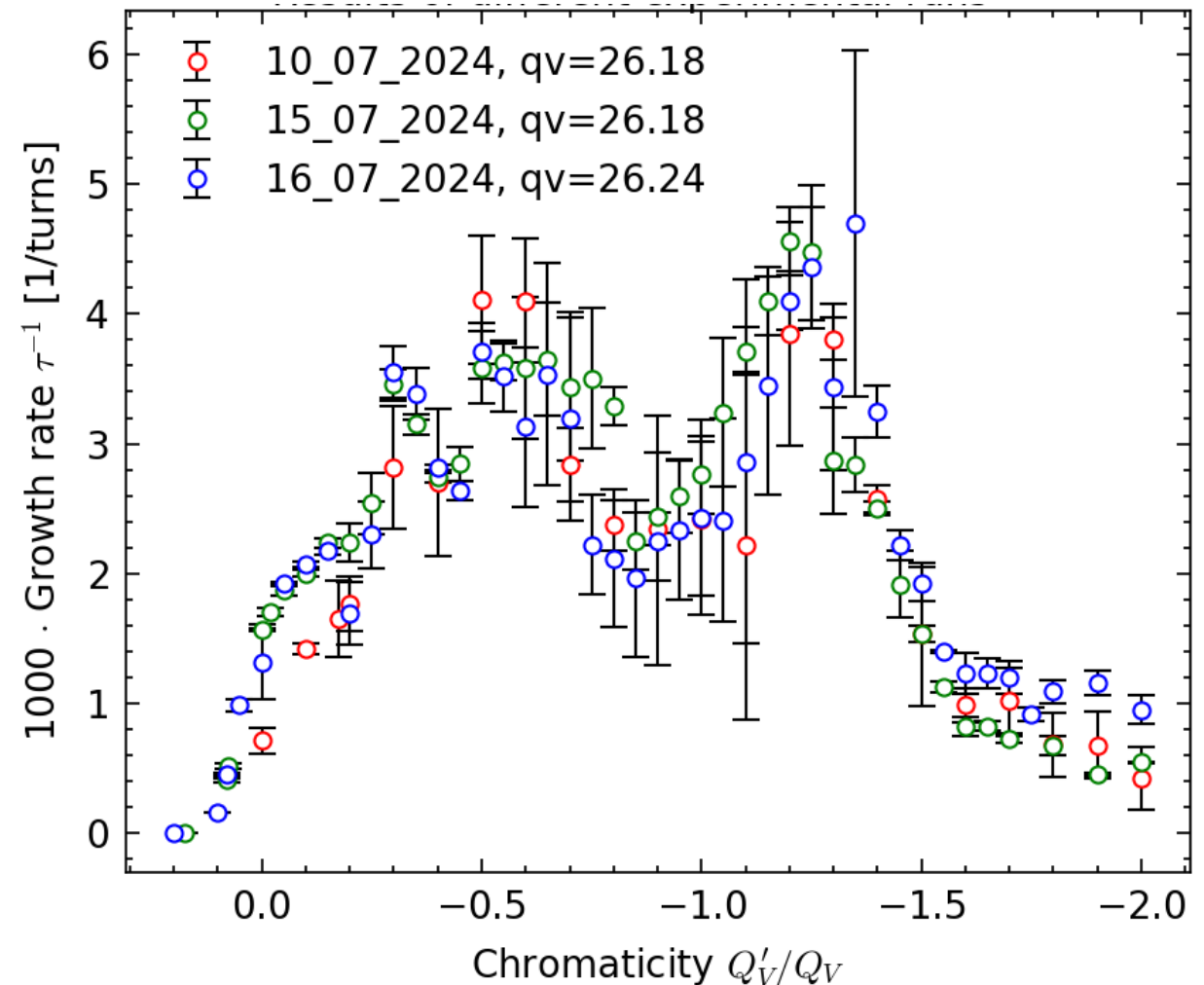
2024 Growth rate measurements*

- Growth rate MDs: [04_07_2023](#),
[10_07_2024](#), [15_07_2024](#), [16_07_2024](#),
[30_08_2024](#) (logbook links)
- Measurements taken at **different intensities** (2 - 4e10 p/b), **bunch lengths** (3 - 4.5 ns) and **emittances** (1.6 – 2.5 μm)
- **Second peak** at $\xi_V = -1.5$ ($f_\xi = 2.4$ GHz for Q26 optics) always observed



Changing working point (I)

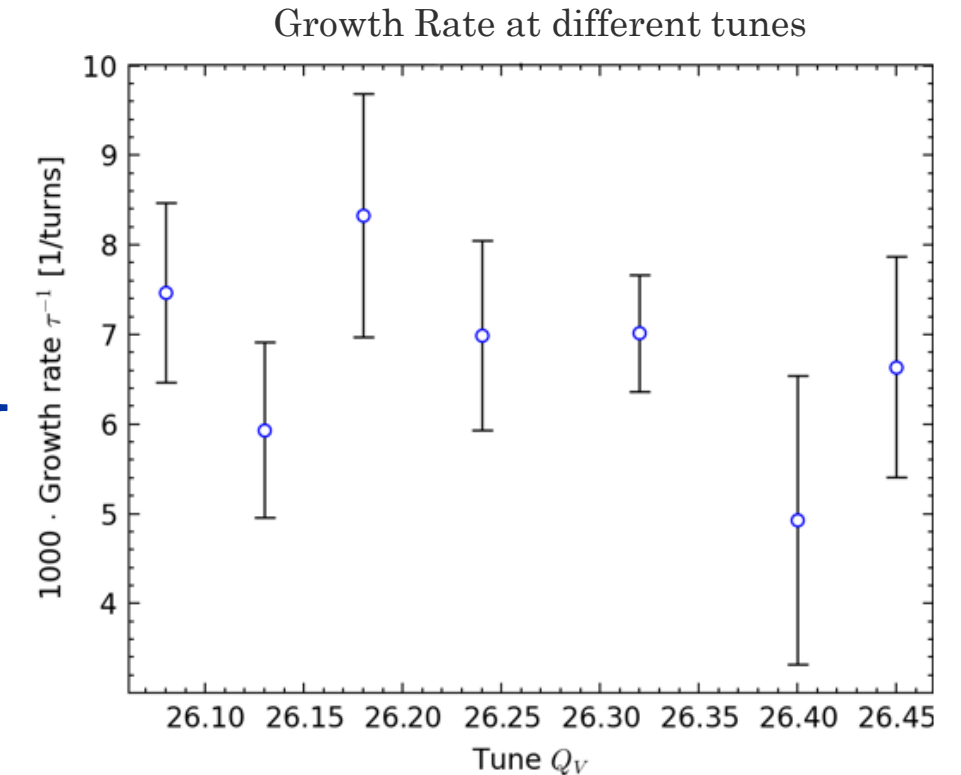
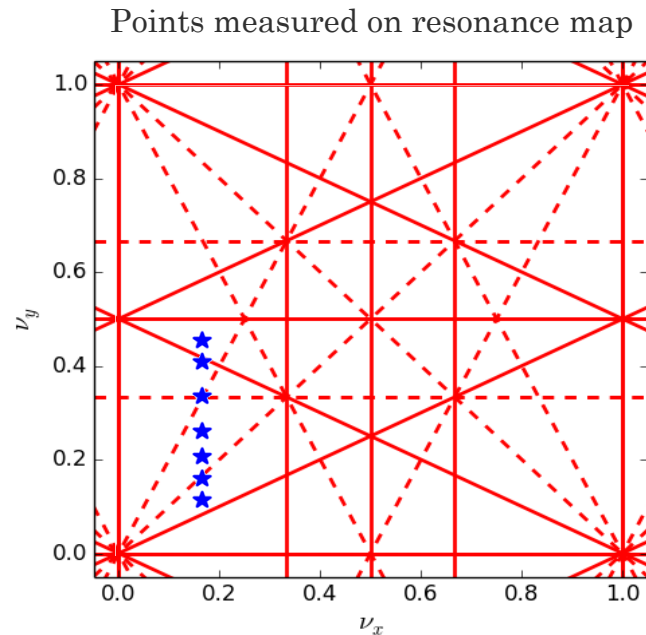
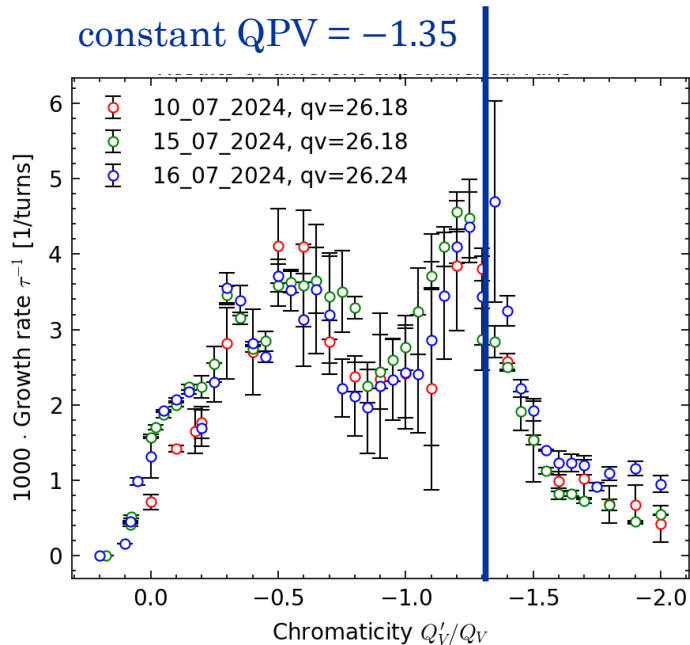
- Previous measurements were performed at Q26 nominal tune: (26.13, 26.18)
- Suspicion that the **second peak** could be caused by interaction with $\frac{1}{2}$ integer resonance due to high chroma*
- **Plot showing:** Results from the full scan performed at nominal vs working point (26.13, 26.24) with **no substantial change of 2nd peak amplitude/frequency**



*Many thanks to K. Paraschou

Changing working point (II)

- Performed a scan of vertical tune Q_V at the second peak chromaticity to exclude resonance effects and tune dependency

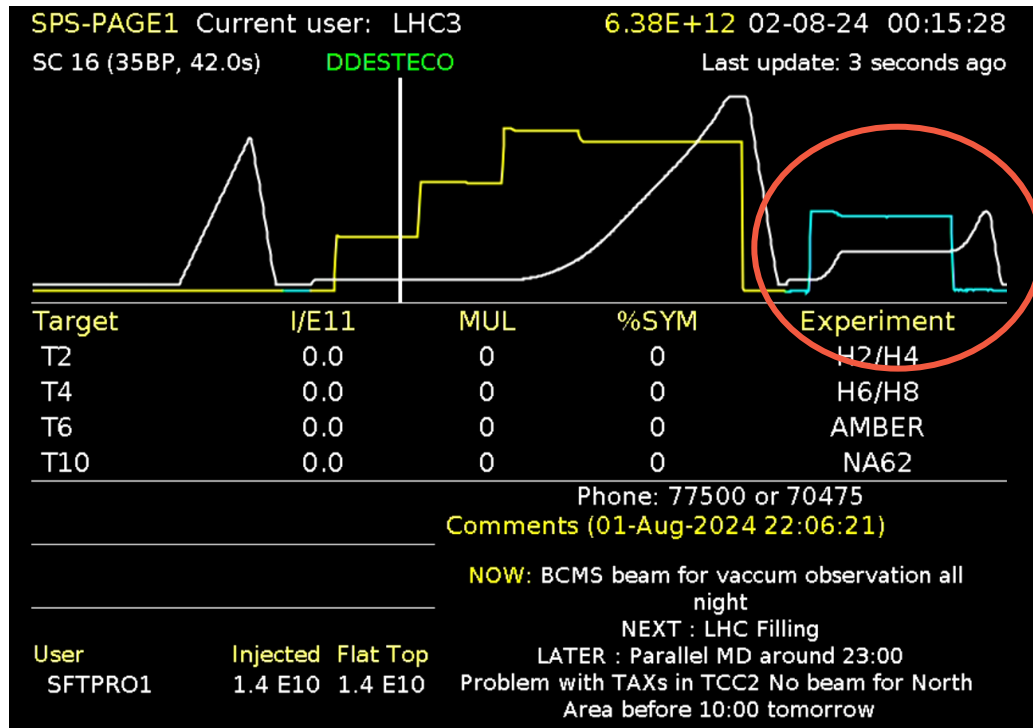


○ No clear correlation observed

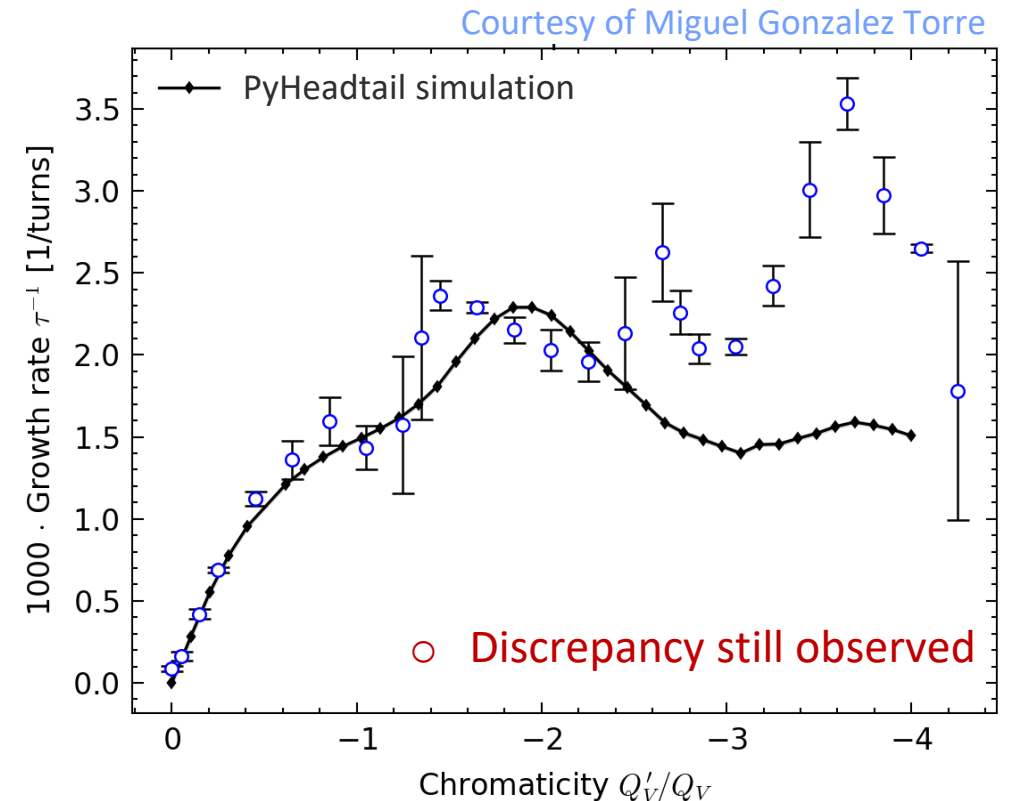
Measurements at 100 GeV

Logbook 02/08/24

- To exclude space charge effects, the cycle with a plateau at 100 GeV was used*
 - Measurements were performed well in the plateau, with bunch length ~ 2.5 ns
 - Change in γ , slip factor η -> needed to reach higher chromaticity values up to $\xi_V = -4.2$ knob

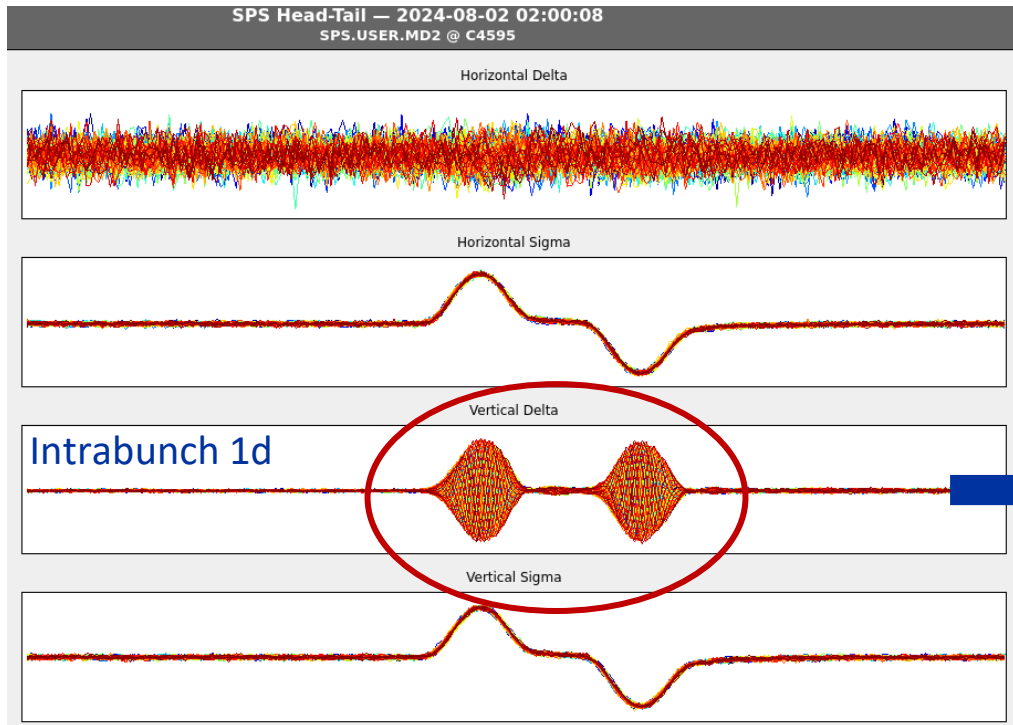


*Many thanks to D. Veres

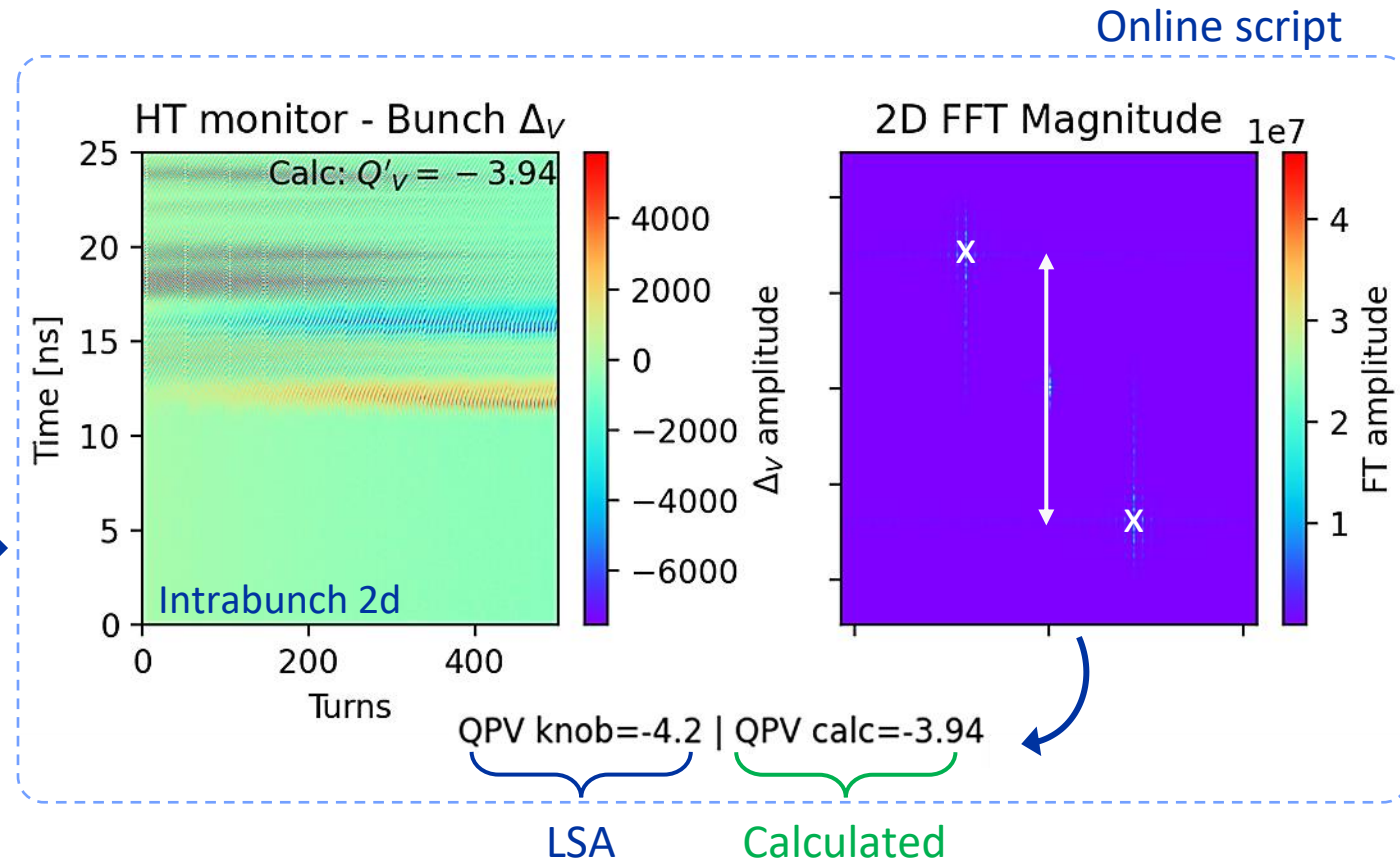


Measurements at 100 GeV (II)

- The **instability intrabunch motion** captured with the **HT monitor** allows for a **shot-by-shot chromaticity measurement*** using a 2D-FFT analysis to verify we are measuring at the right chroma



**Based on the work by R. Jones and T. Levens, ROAB006, PAC'01



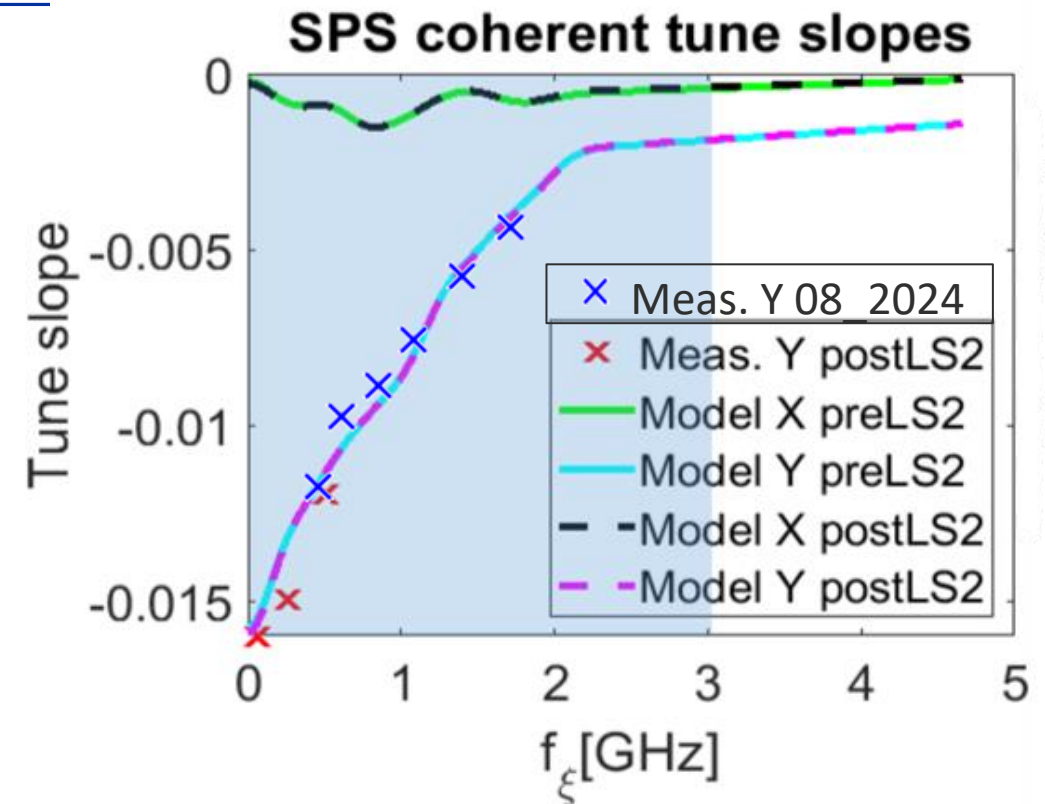
Tune slopes vs chromaticity measurements

Logbook links: [first MD](#), [second MD](#)

- Tune shift intensity slopes $\frac{\Delta Q_{\perp}}{N}$ allow to **benchmark the imaginary part** of the SPS transverse impedance model $\text{Im}[Z_{\perp}^{eff}(\xi)]$

$$\frac{\Delta Q_{\perp}}{N}(\xi) = -\Gamma \left(\frac{1}{2} \right) \frac{\text{Im}[Z_{\perp}^{eff}(\xi)] r_0 c^2}{8\pi^2 \gamma \omega_{\beta} \sigma_z}$$

- **Challenging measurements**, thanks to I. Mases and the SPS and PSB operators for the help
 - Each f_{ξ} point requires tune measurements over 10 intensity points $\{1e10 - 3e11\}$ depending on TMCI
- Explored further in chromatic frequency f_{ξ}^{**} using Q26 optics and LHC BPM data
 - **Very good agreement** with Sacherer theory's predicted coherent tune slopes

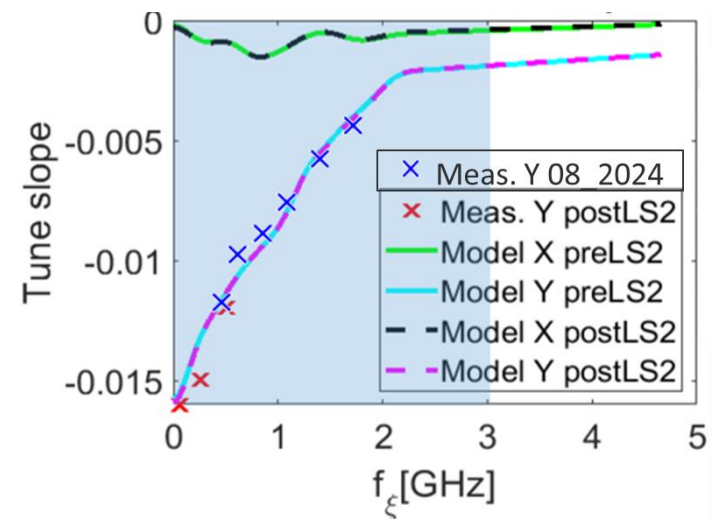
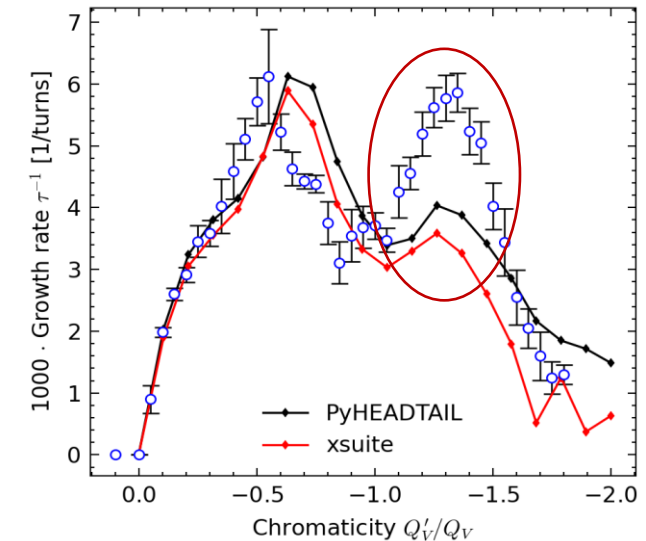


* Original plot C. Zannini, CEI meeting 21 Oct. 2021

** New points courtesy of Miguel Gonzalez Torre

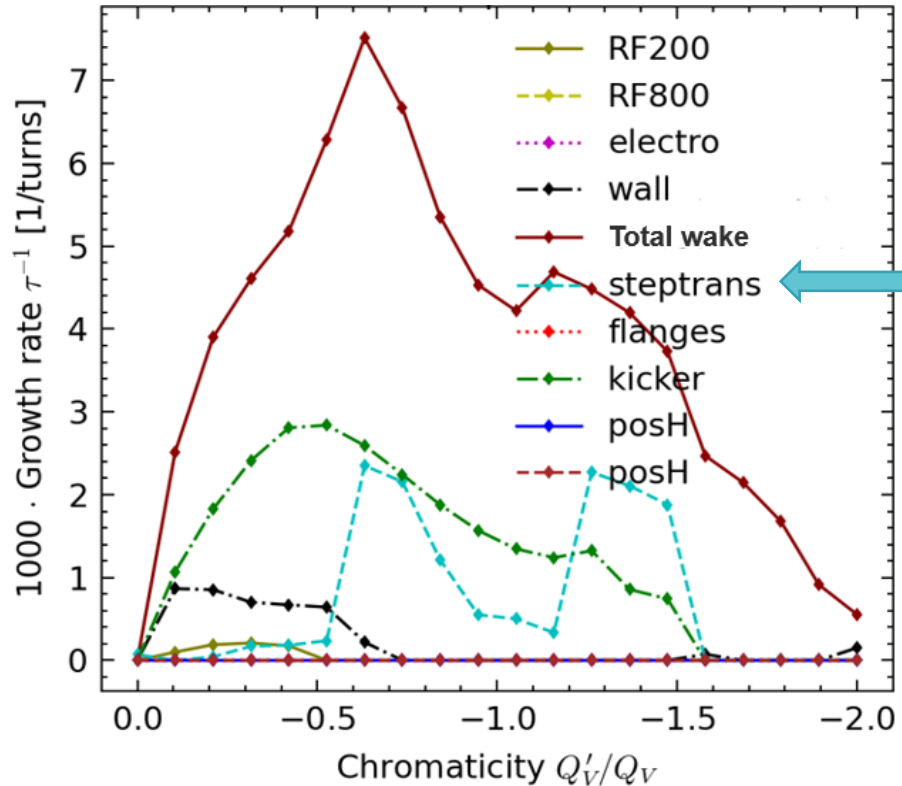
Conclusions

- Studied Head-Tail mode zero growth rate measurements to benchmark the **real part of the SPS transverse impedance model** and study the **discrepancy in the high frequency regime**
 - Changing working point: No dependency with vertical tune was observed
 - Measurements at higher energy: Discrepancy still observed in measurements at 100 GeV
 - PyHeadtail/Xsuite simulations: Latest impedance model in simulations **cannot reproduce the measurements for $f_\xi > 1.5$ GHz**
- Studied Tune slopes vs chromaticity to benchmark the **imaginary part of the model**
 - Found **very good agreement** with analytical predictions
 - Xsuite/PyHT simulations proven challenging & not available



Conclusions & future work

Courtesy of Miguel Gonzalez Torre

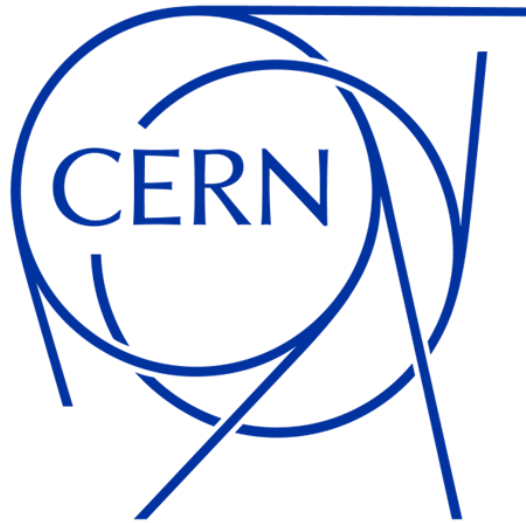


- Simulations of separated impedance contributions of the SPS model hint at the [step transitions](#)
 - Real-valued impedance contribution at the right frequency
 - Model developed focusing on the imaginary part to match the tune shifts

Future work:

- Transitions model will be revised and refined (ongoing)
- PyHeadtail/Xsuite simulations will be done with the refined impedance model
- No more MDs needed this year 😊

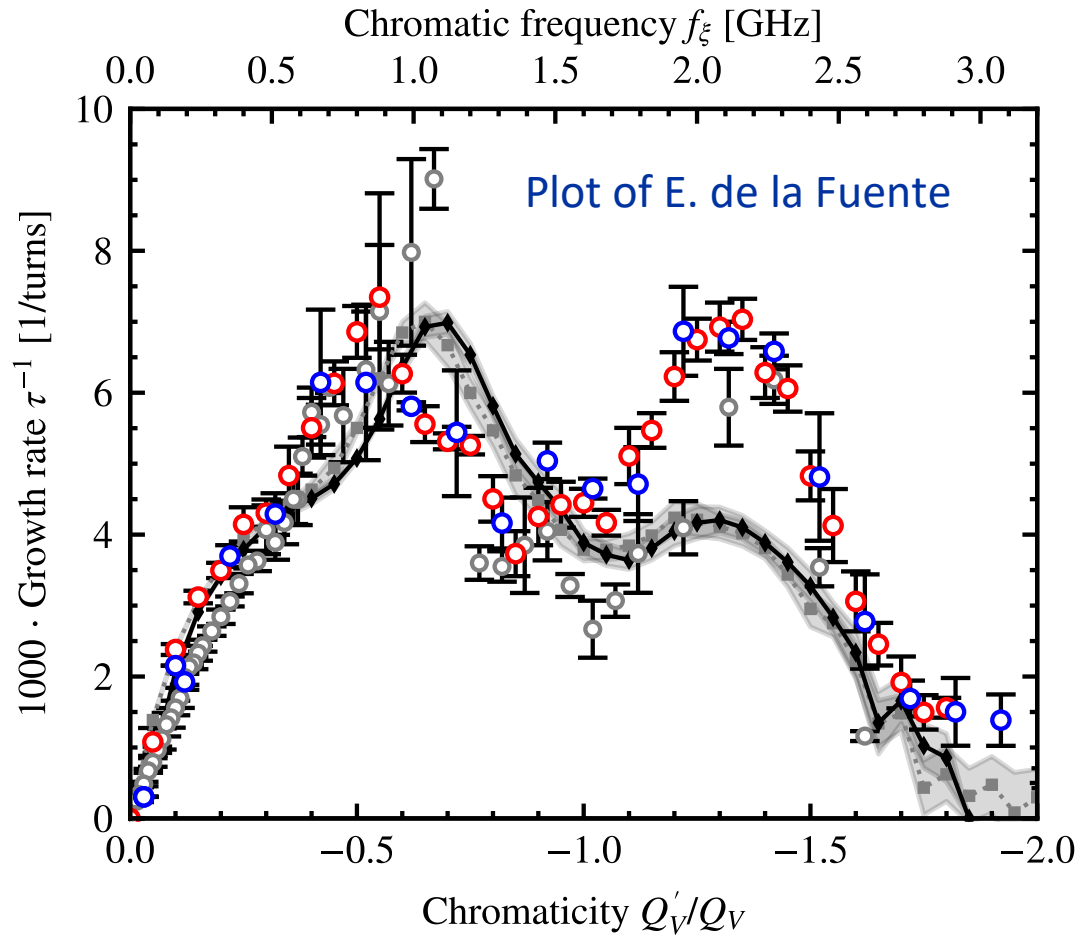
Thank you 😊



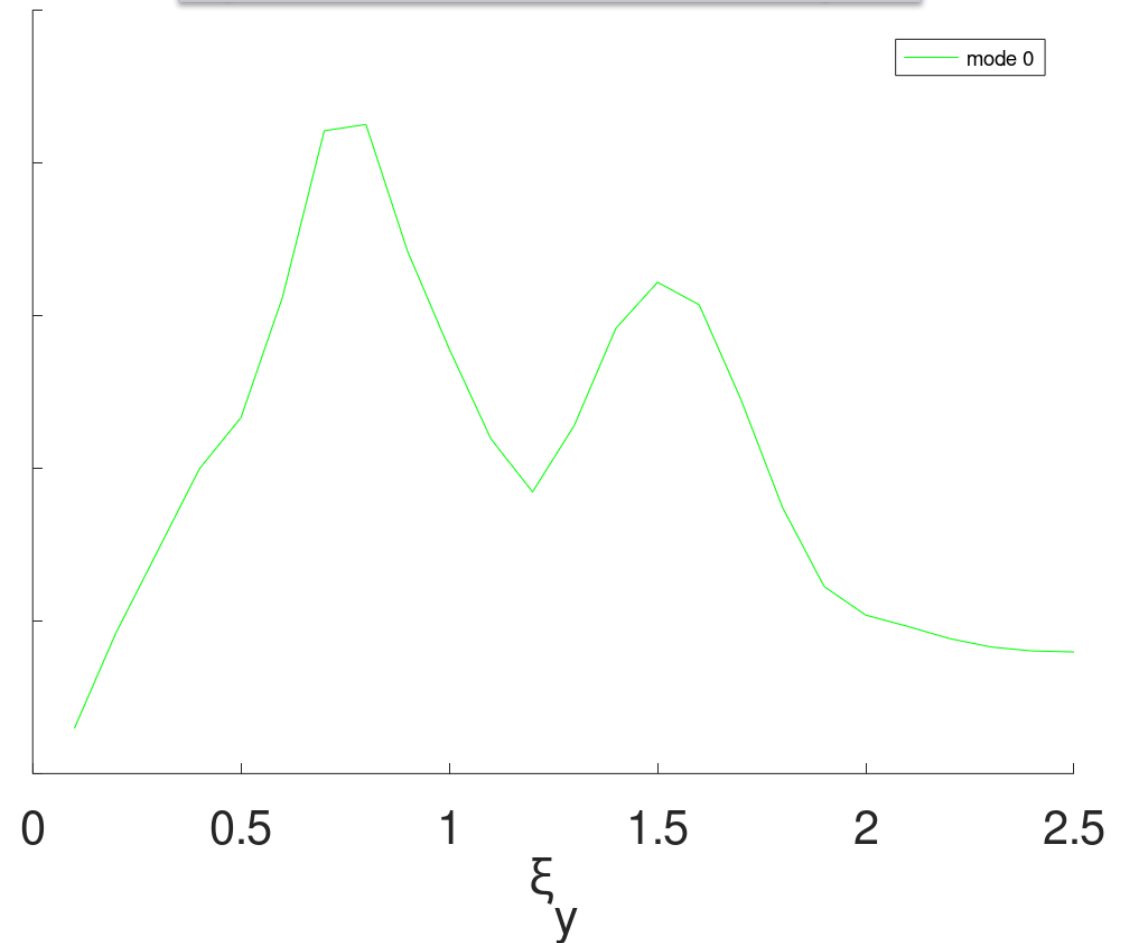
Update on SPS reference impedance
measurements

Elena de la Fuente García (BE-ABP-CEI)

SPS dark impedance



Expectation from Sacherer theory

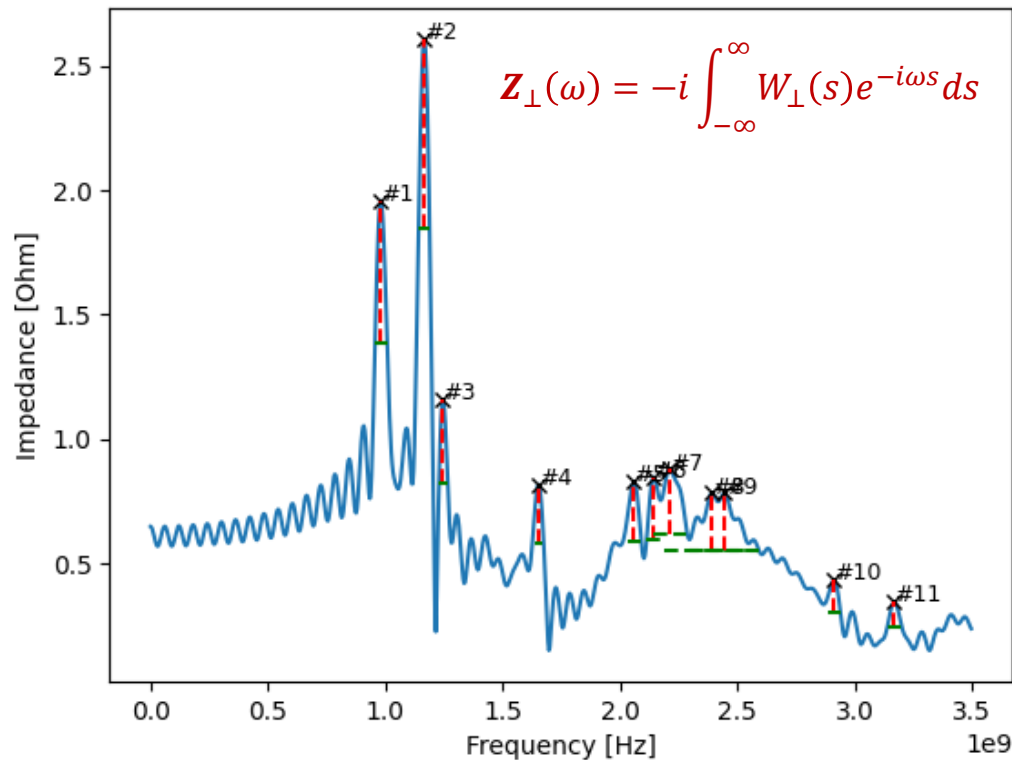


To be understood why is not observed in PyHEADTAIL simulations (wake potential approximation?)

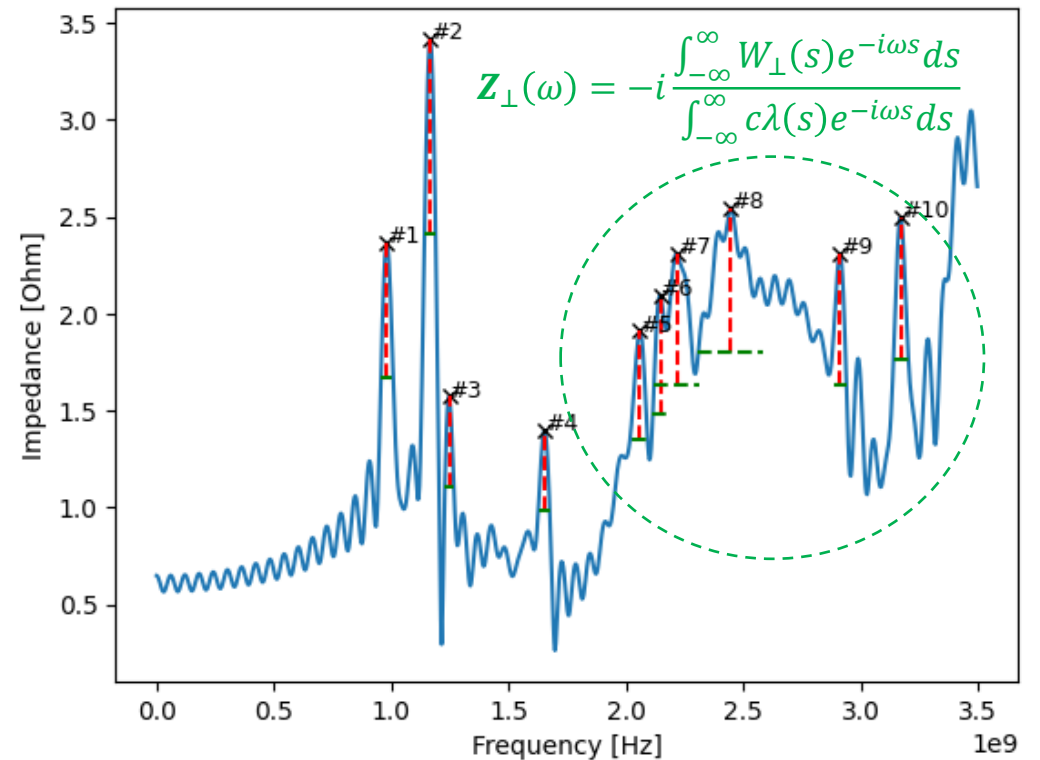
Step transitions revised [PRELIMINARY]

- **Step transitions** were simulated with CST Studio® wakefield solver with very short bunch $\sigma_z \sim 10^{-11}$ ns to consider the wake a **wake function** instead of a **wake potential**

Impedance from the wake model using **FFT only**



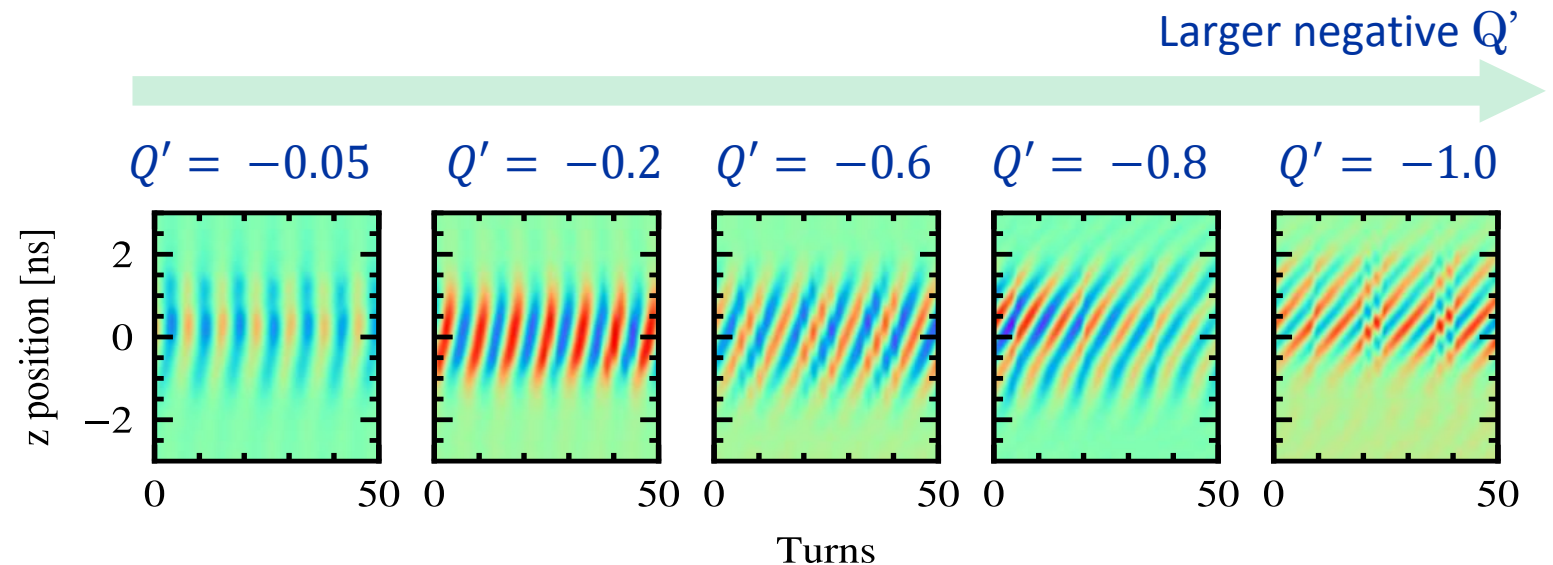
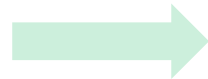
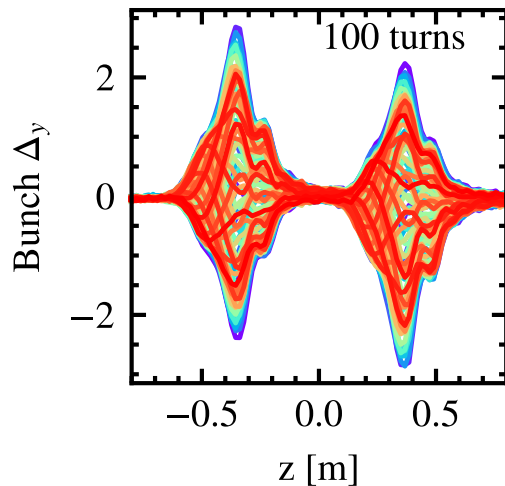
Impedance from the wake model using **deconvolution**



Chromaticity from intrabunch motion

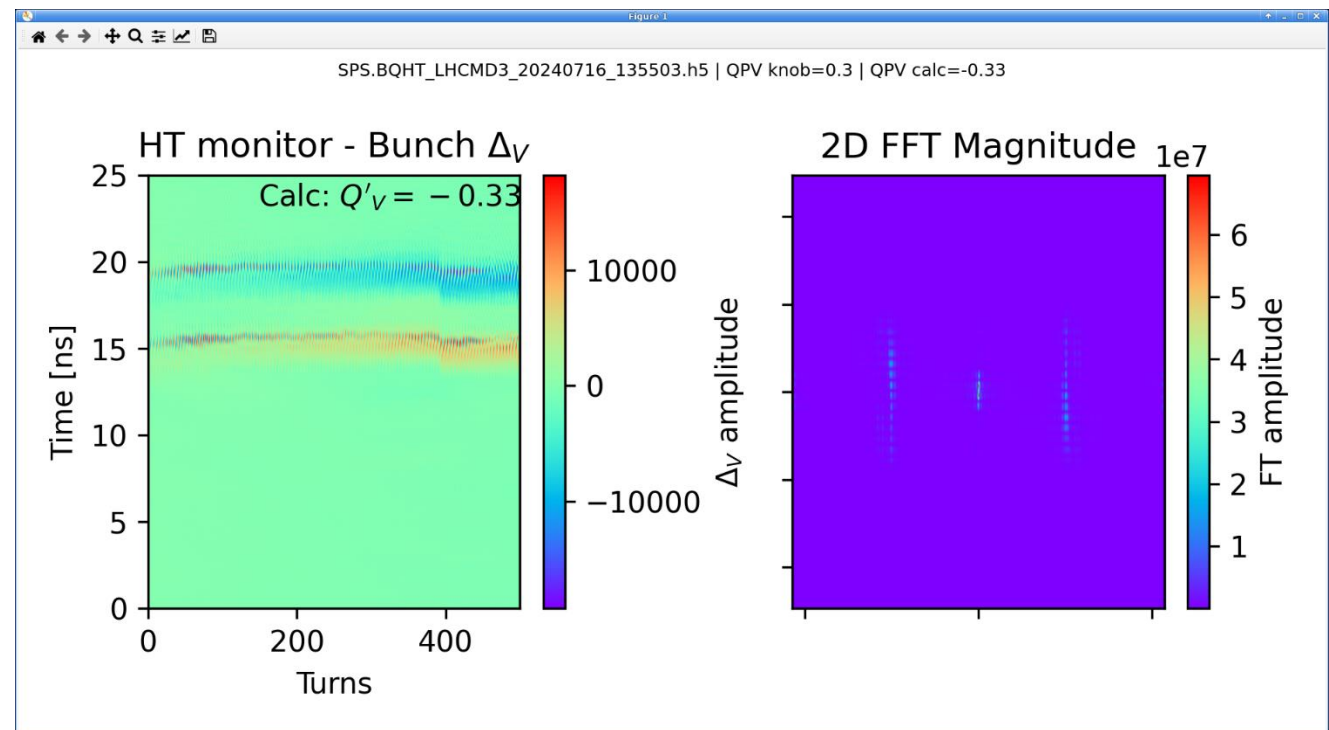
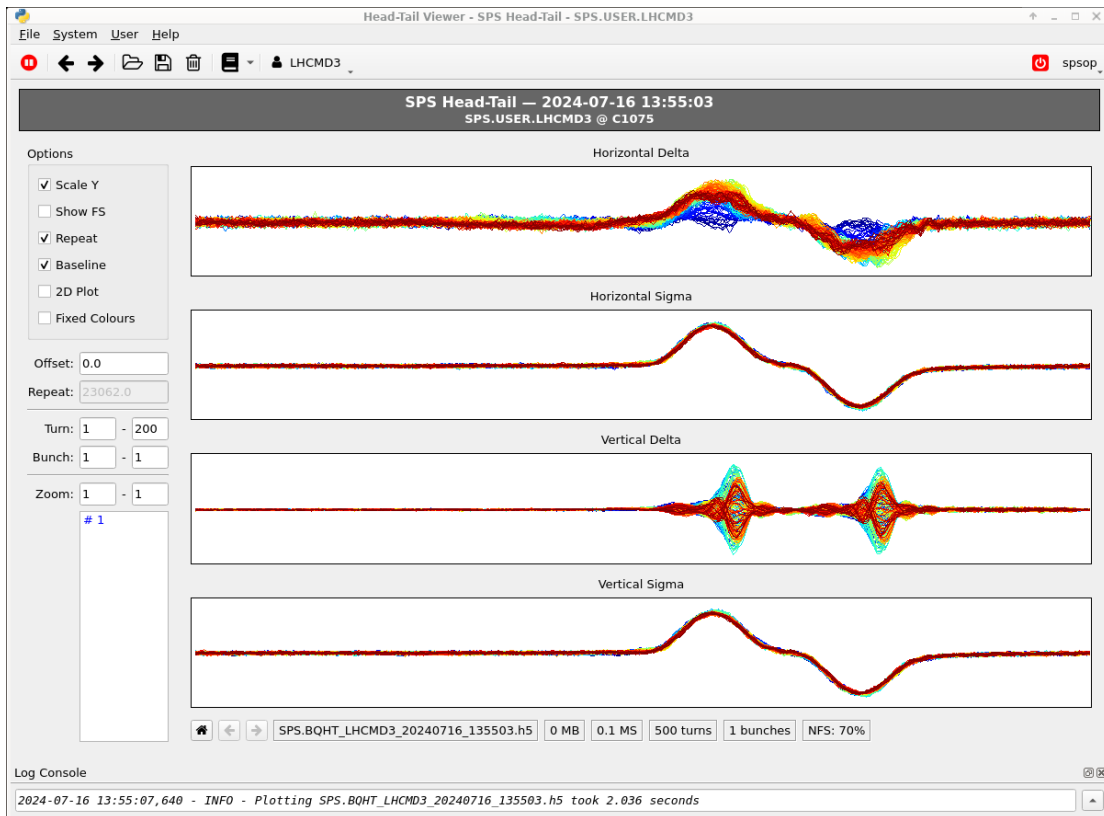
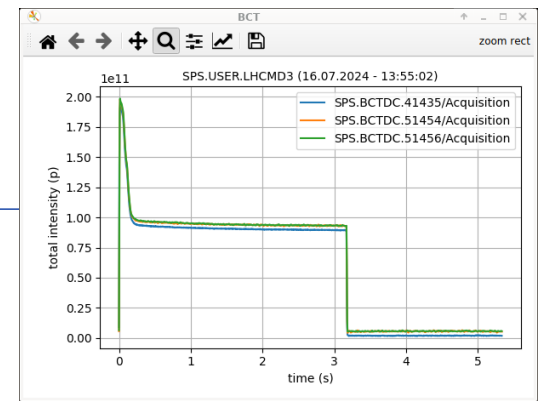
- When plotting the SPS Head-Tail Monitor measurements over the longitudinal position z and number of turns, we could observe a distinctive pattern when going to more negative values.
- The information of chromaticity Q' is encoded in the observed head-tail phase modulation*

$$y(n) = A \cos[2\pi nQ + \Delta\psi_{HT} \{\cos(2\pi Q_s n) - 1\}]$$



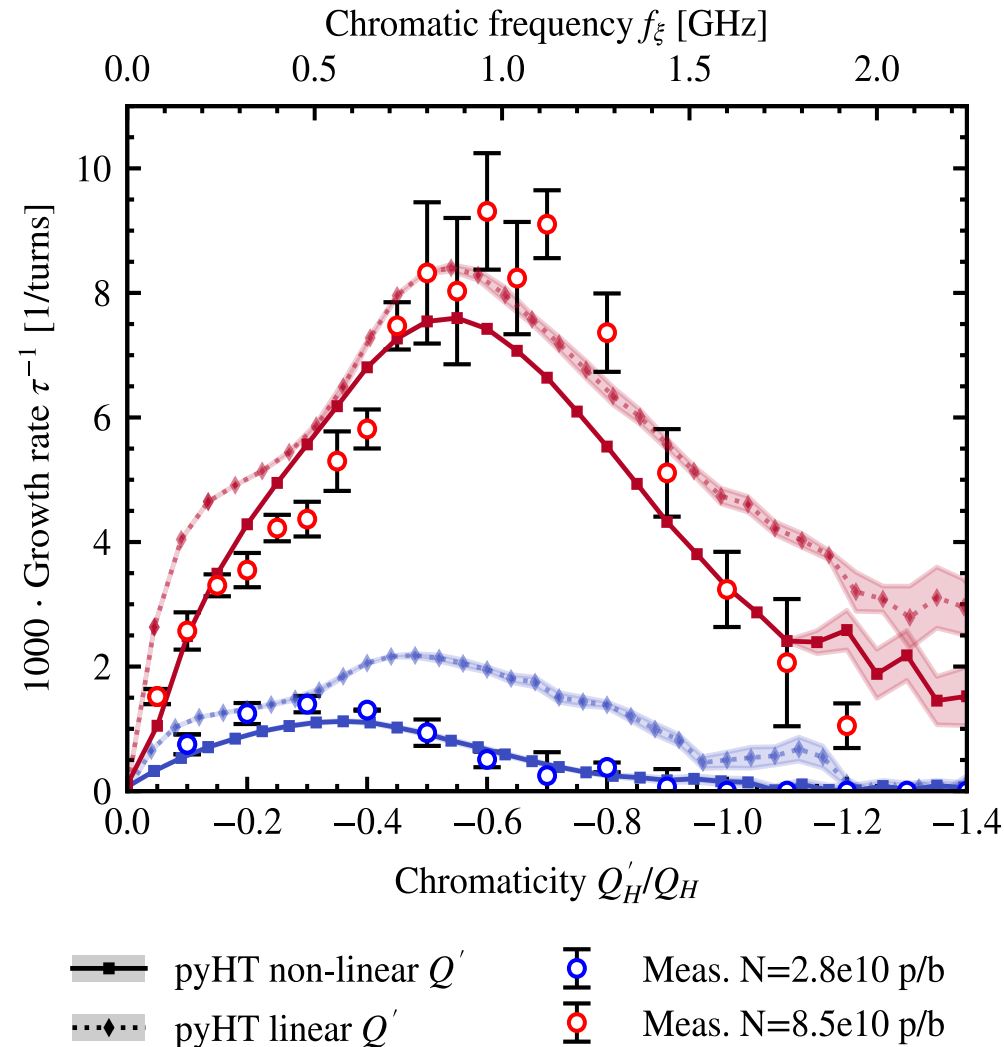
Positive chromaticity measurements TMCI

We tried to measure positive chromaticity by going above the TMCI threshold ($2e11$ for Q26) with our single bunch, and we successfully retrieved the intrabunch chromaticity



What about the Horizontal plane?

*E. de la Fuente, THAFP01, HB'23



Bunch-by-bunch tune shifts w/ dark impedance

