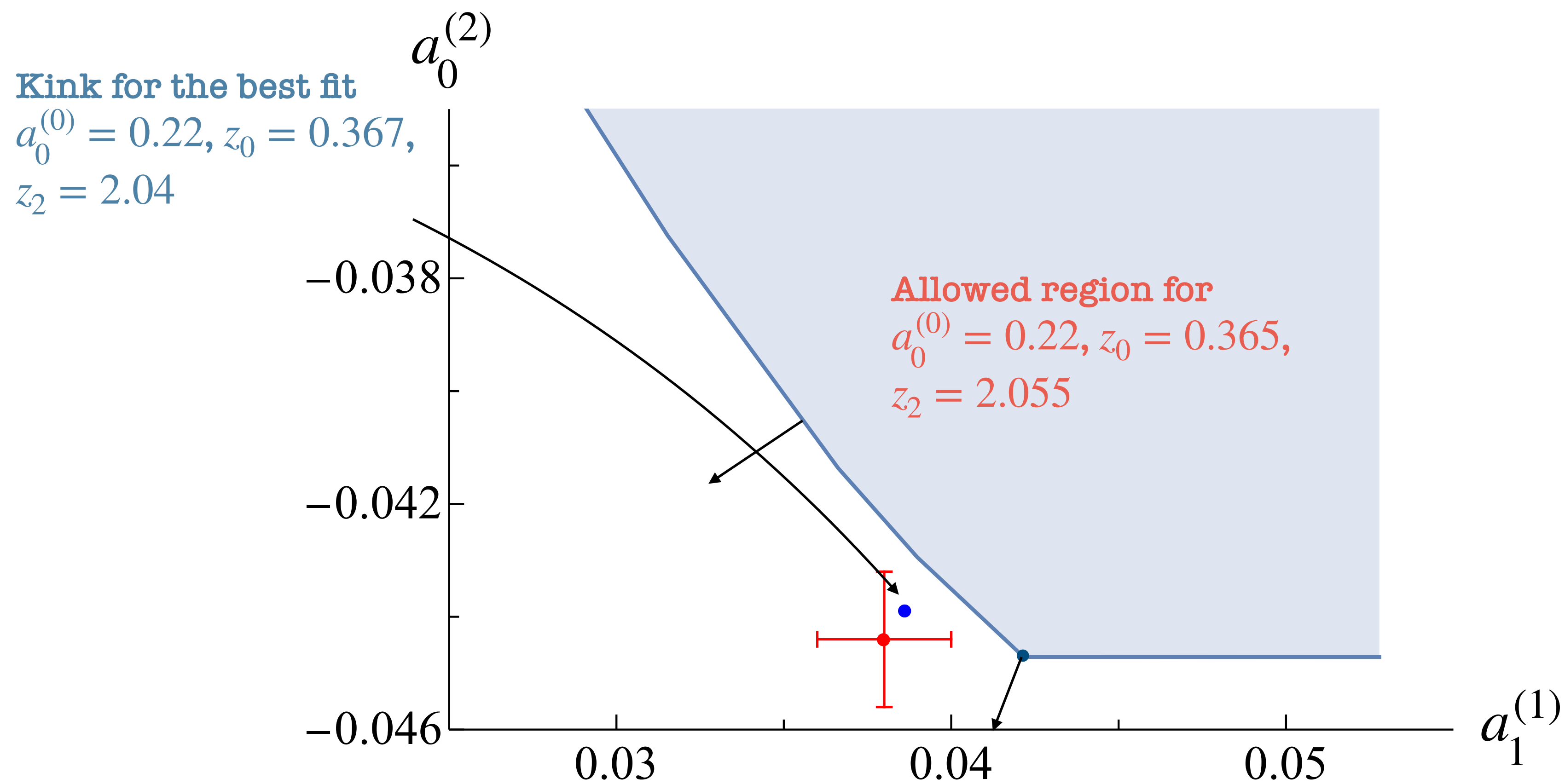


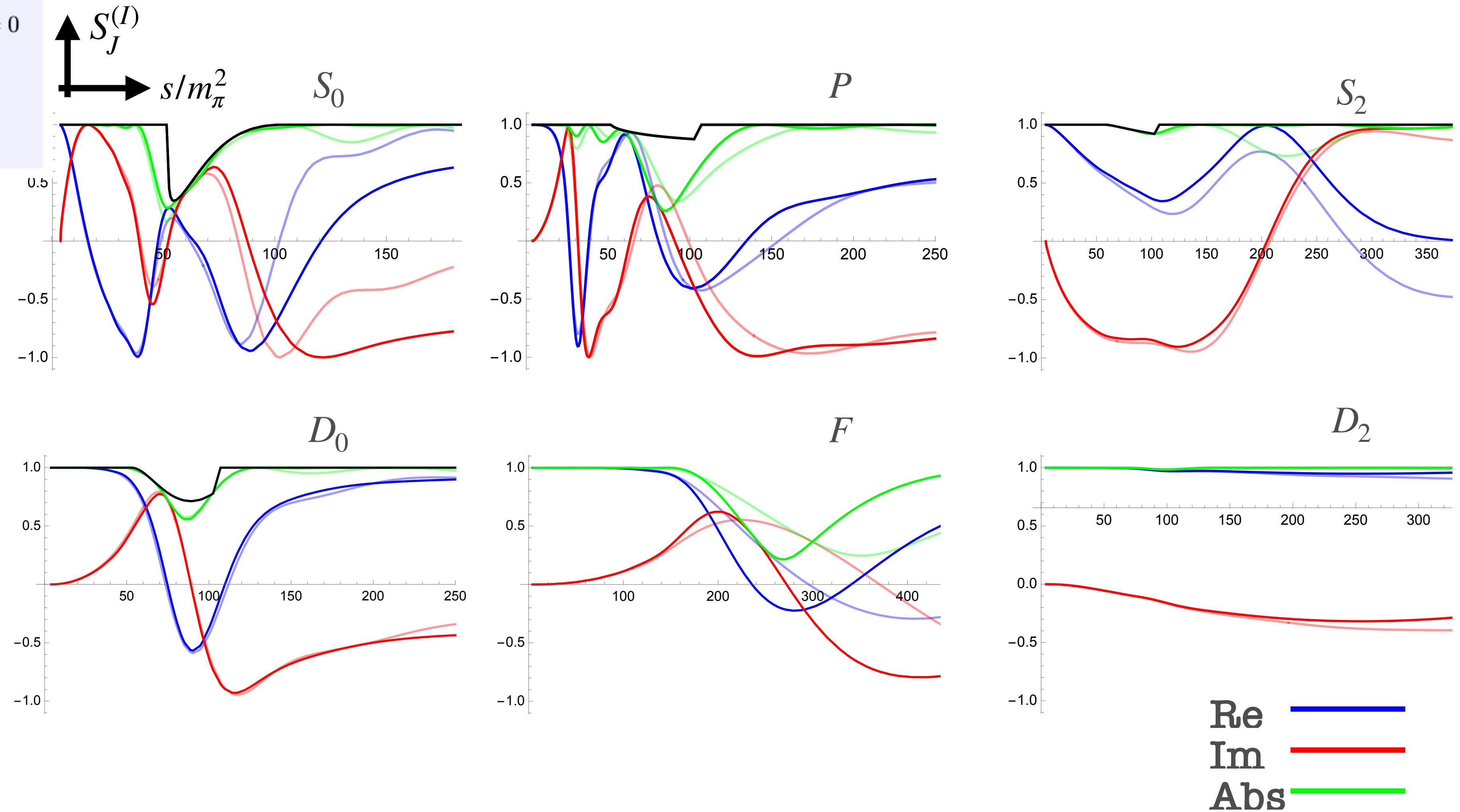
The Kink

$$Obj(\theta) = a_1^{(1)} \cos \theta + a_0^{(2)} \sin \theta$$



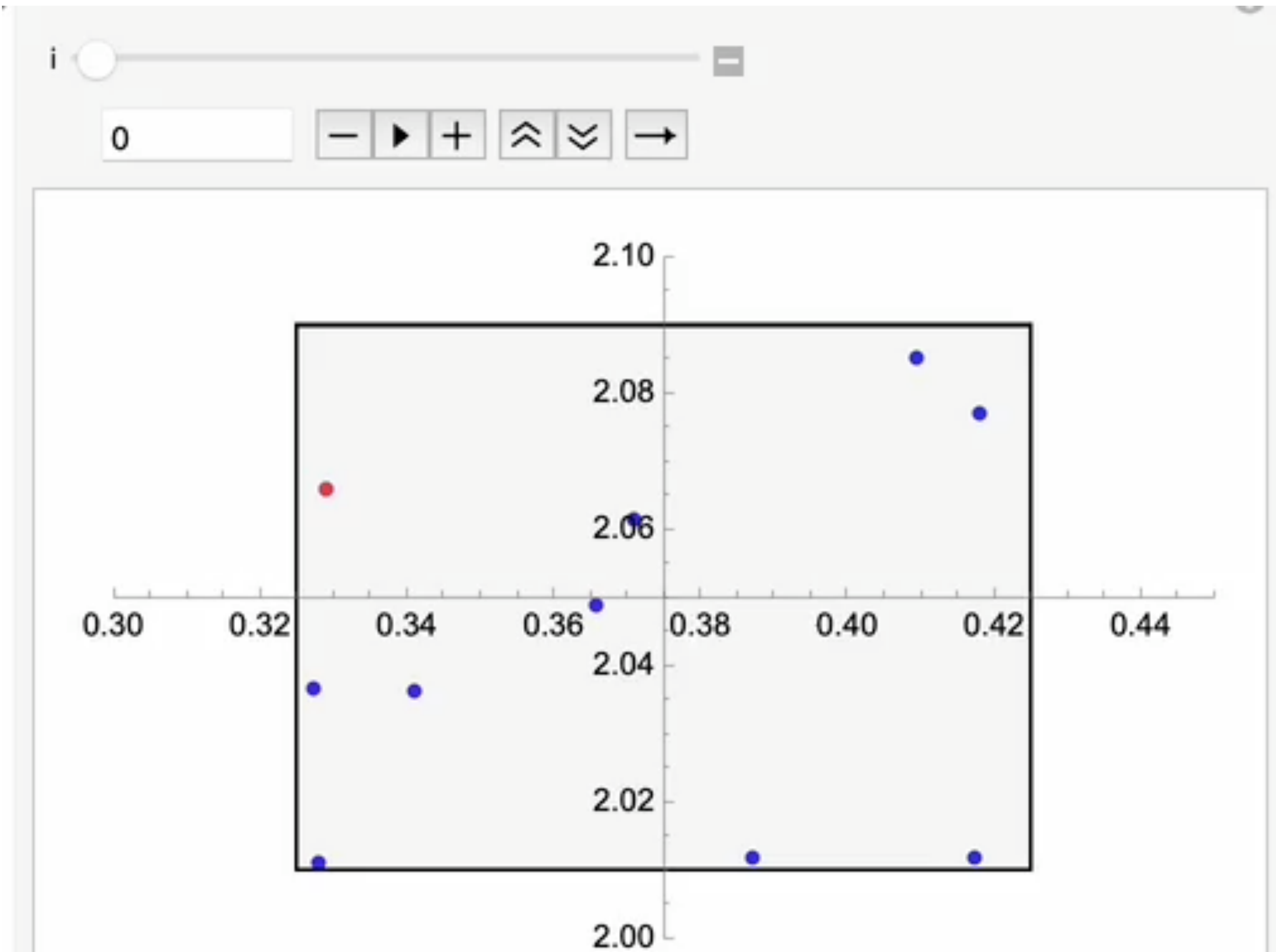
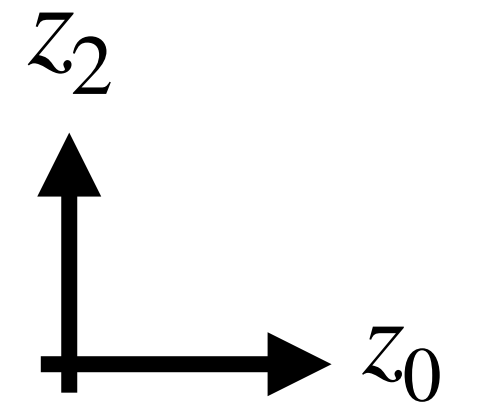
Step 1: Solution from the Bootstrap

Fit Ansatz
 Given $\Theta = \{\theta, a_0^{(0)}, z_0, z_2, m_\rho^2, m_{f_0}^2, m_{f'_0}^2, m_{f_2}^2\}$
 Maximize $\text{Obj}(\theta)$
 in $\mathcal{A}^{\text{ansatz}}(s, t, u)$
 constr. by $t_0^{(0)}(4) = 2a_0^{(0)}, t_0^{(0)}(z_0) = 0, t_0^{(2)}(z_2) = 0$
 $S_1^{(1)}(m_\rho^2) = 0, S_0^{(0)}(m_{f_0}^2) = 0$
 $S_0^{(0)}(m_{f'_0}^2) = 0, S_2^{(0)}(m_{f_2}^2) = 0$
 $s \geq 4$ $\mathcal{U}_\ell^{(I)} \succeq 0$ for $\ell \in \mathbb{N}, I = 0, 1, 2$ (9)

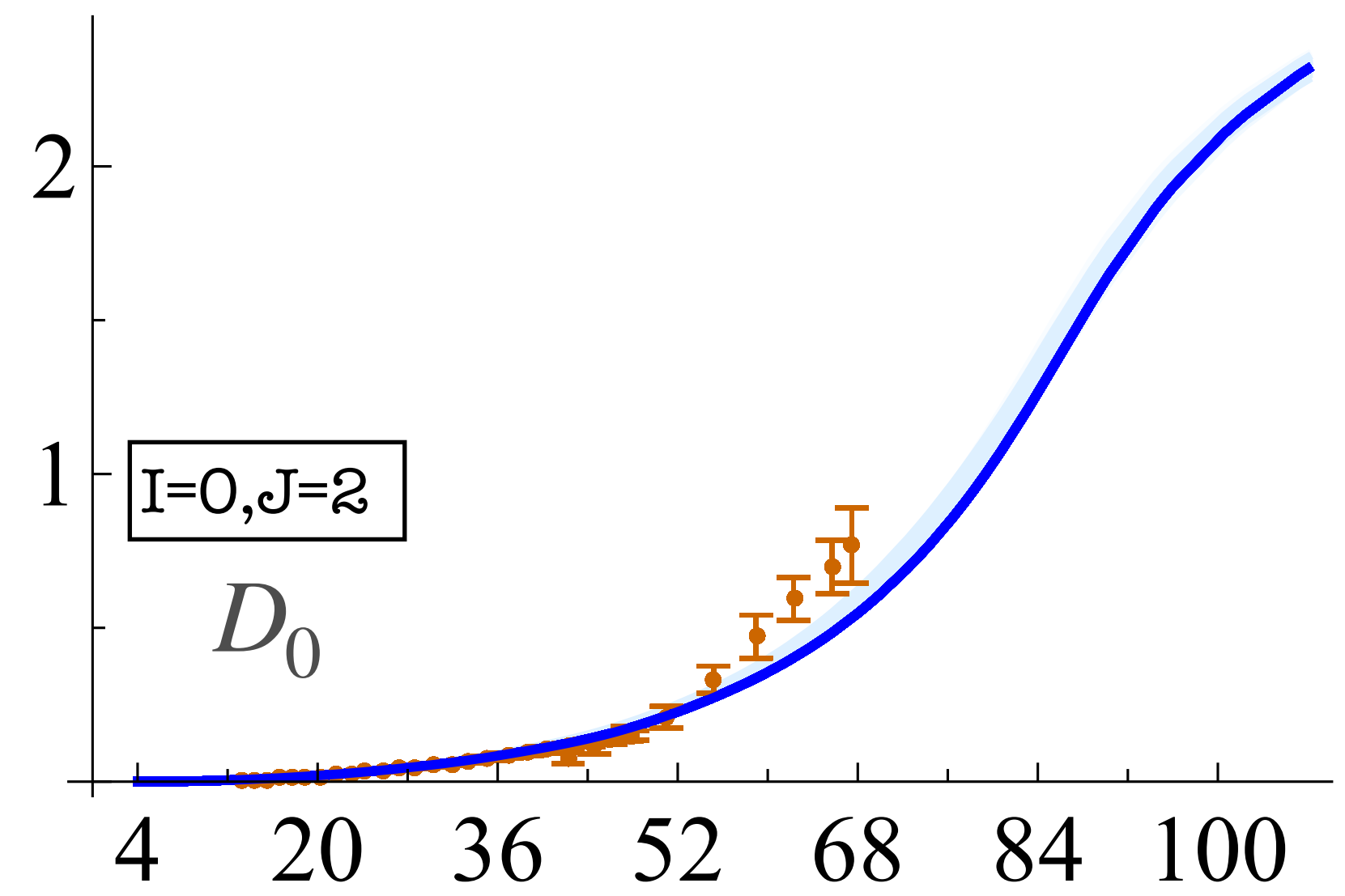
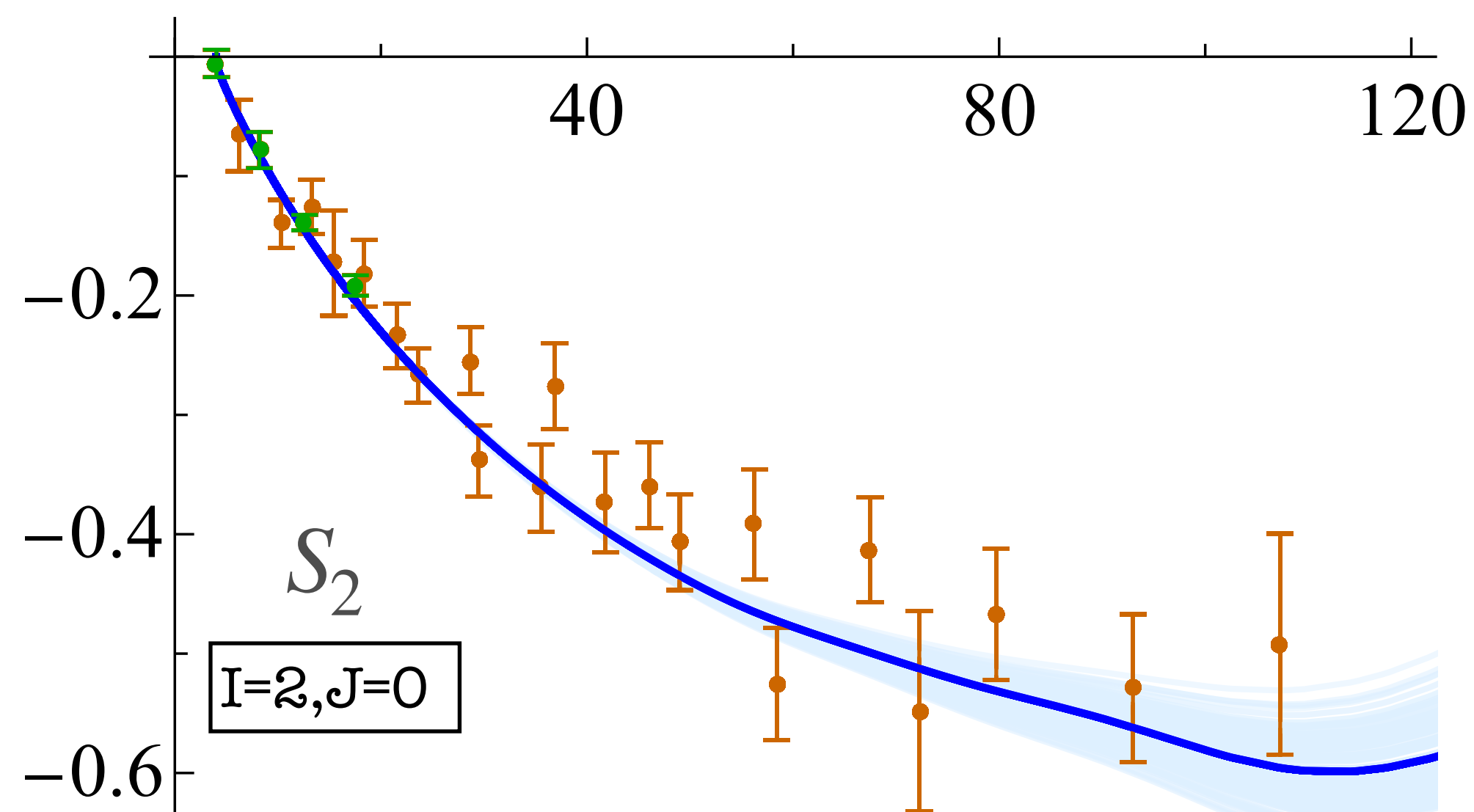
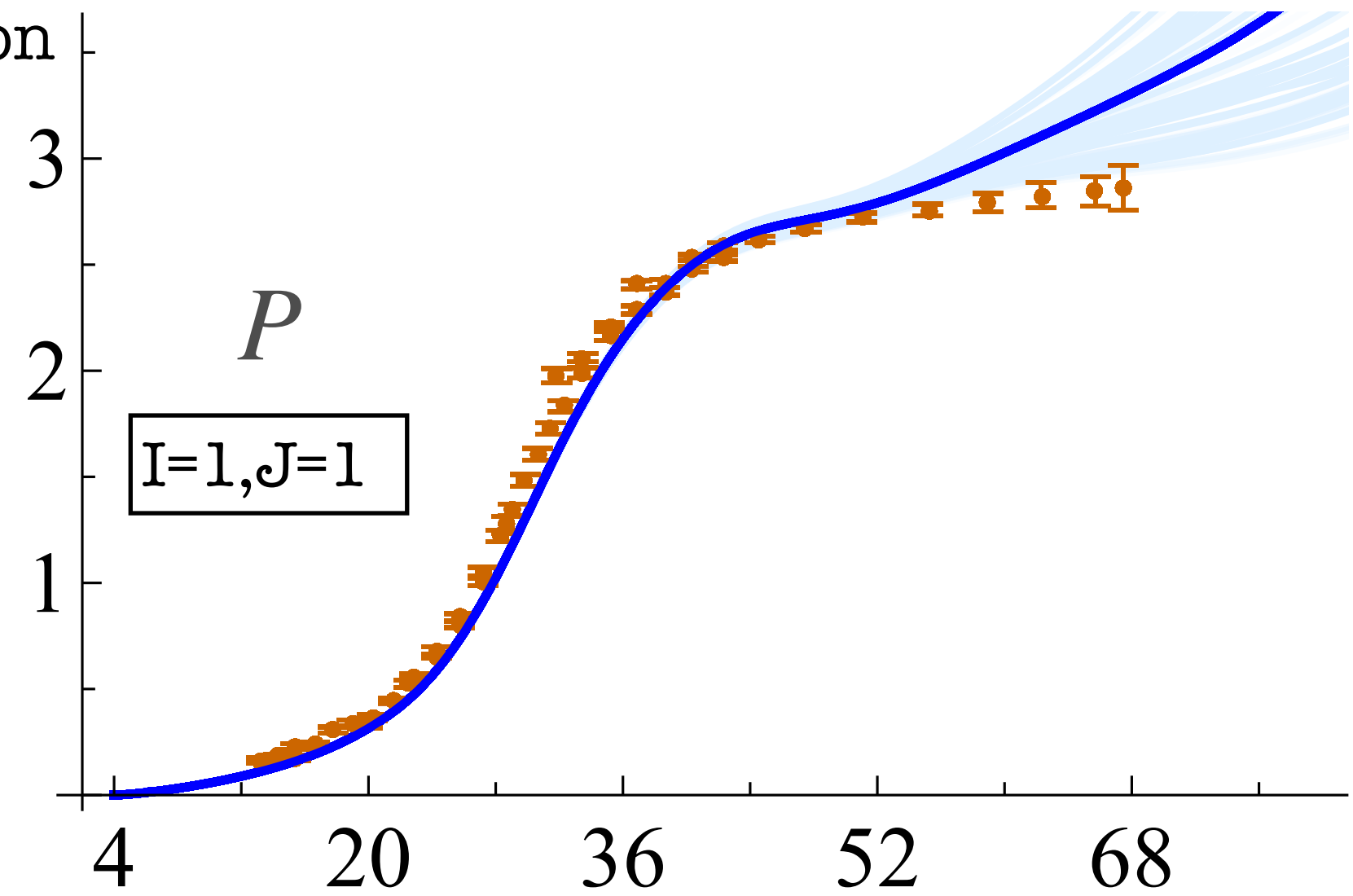
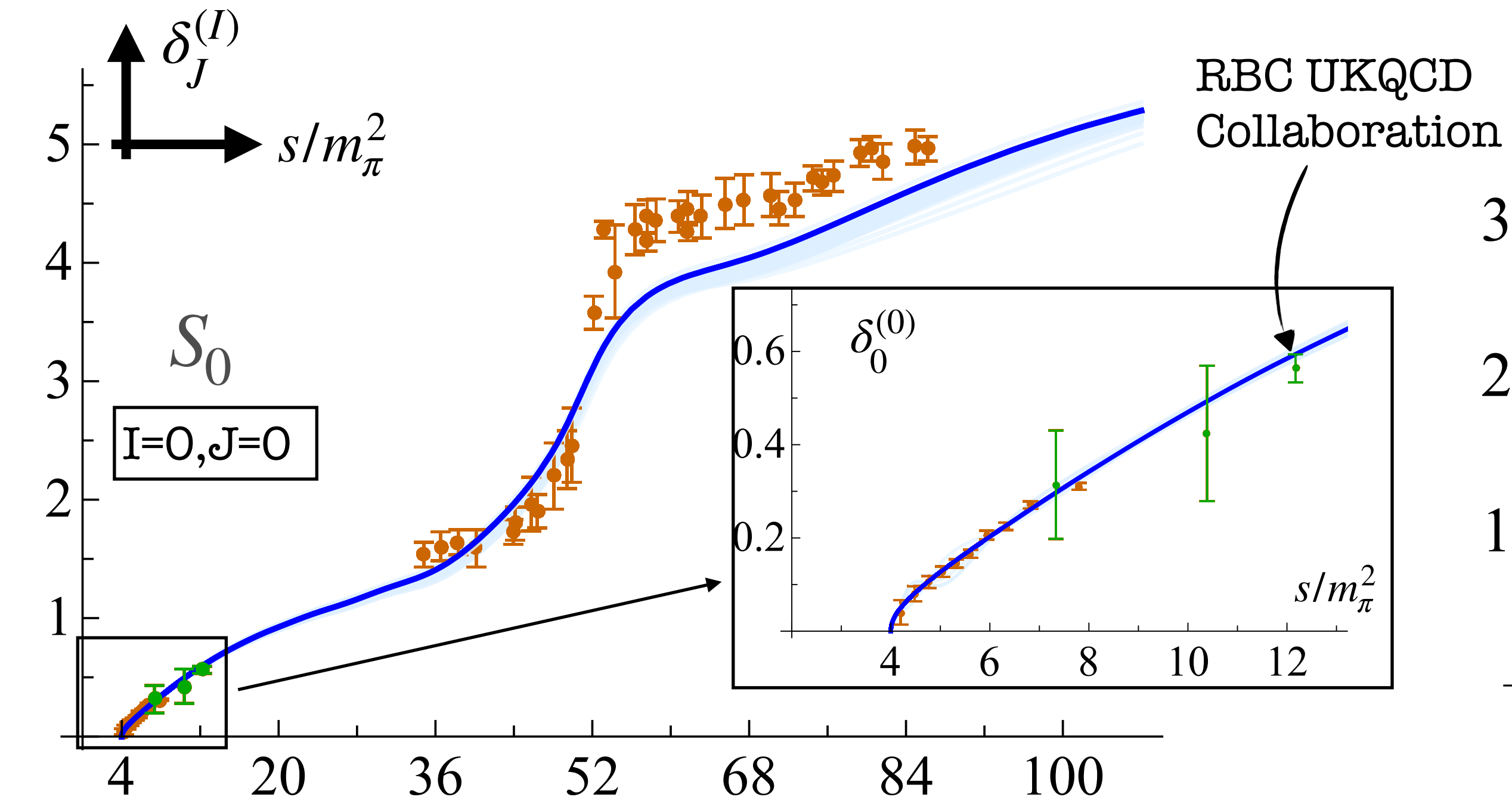


Step 2: Particle Swarm Optimization

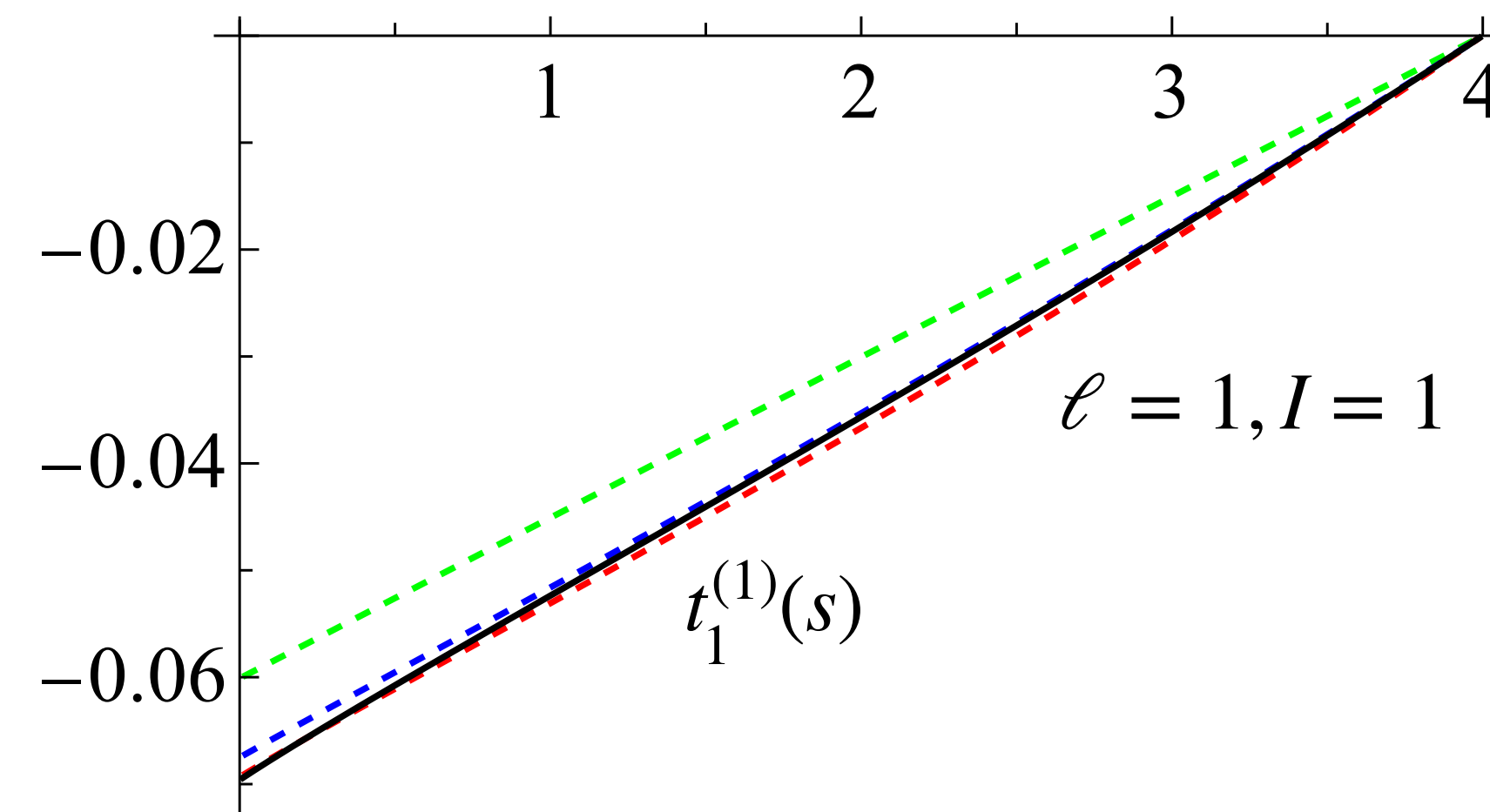
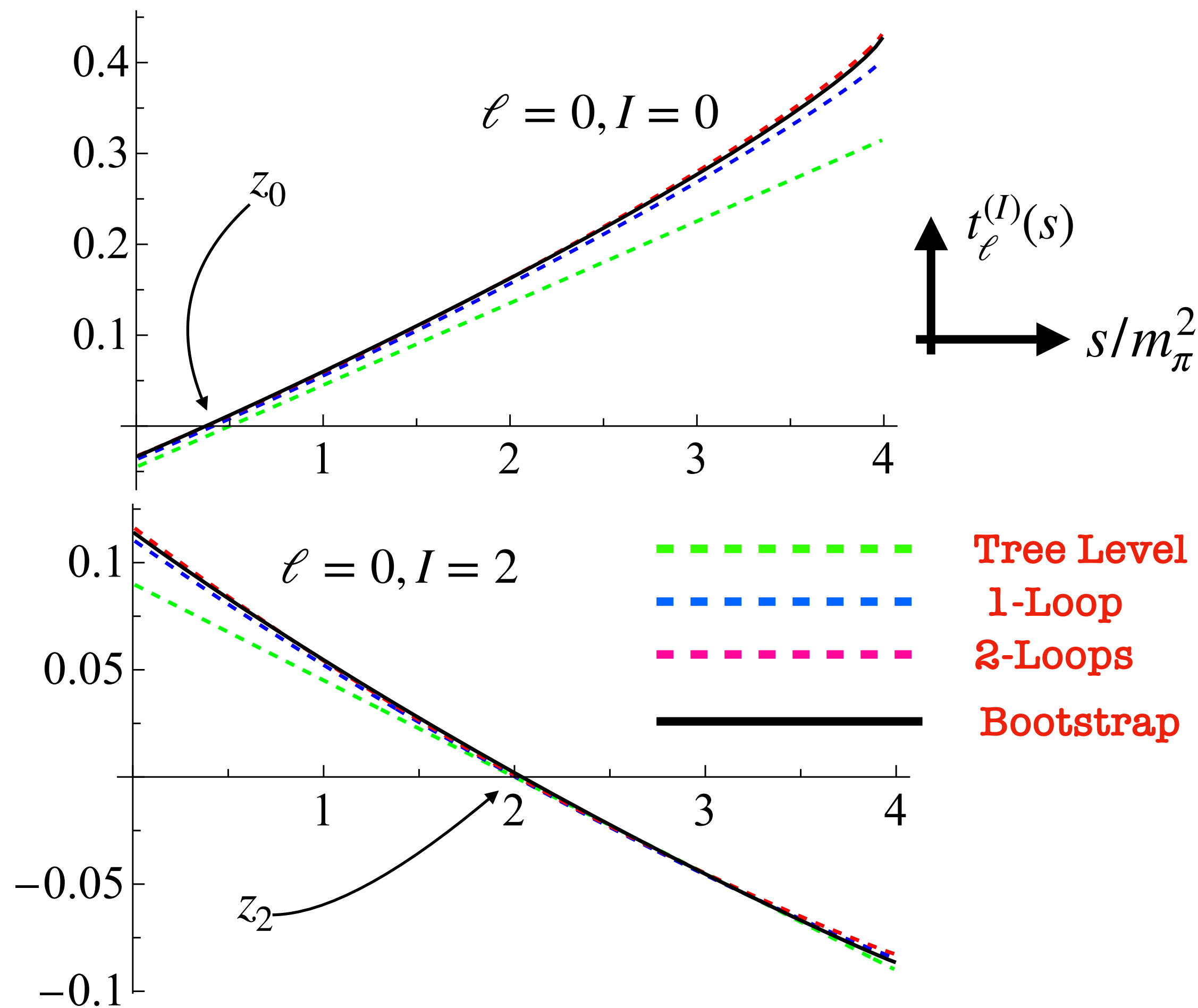
$$\begin{aligned}v_{n+1}^{(i)} &= \omega v_n^{(i)} + c_1 r_1 (\Theta_n^{(i)} - X_n^{(i)}) + c_2 r_2 (\Theta_n^{(i)} - Y_n), \\ \Theta_{n+1}^{(i)} &= \Theta_n^{(i)} + v_{n+1}^{(i)}.\end{aligned}\quad (11)$$



The Best-Fit

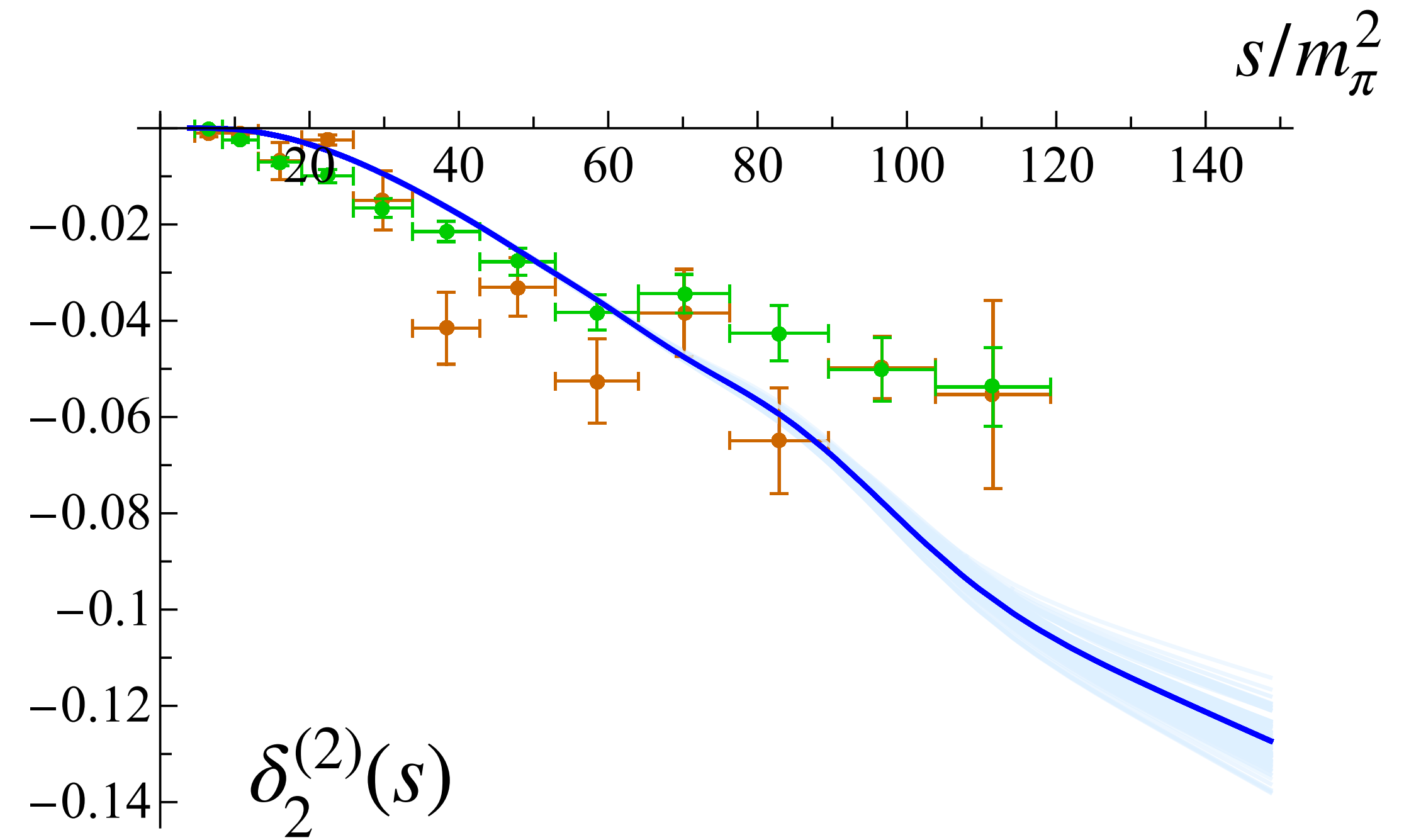
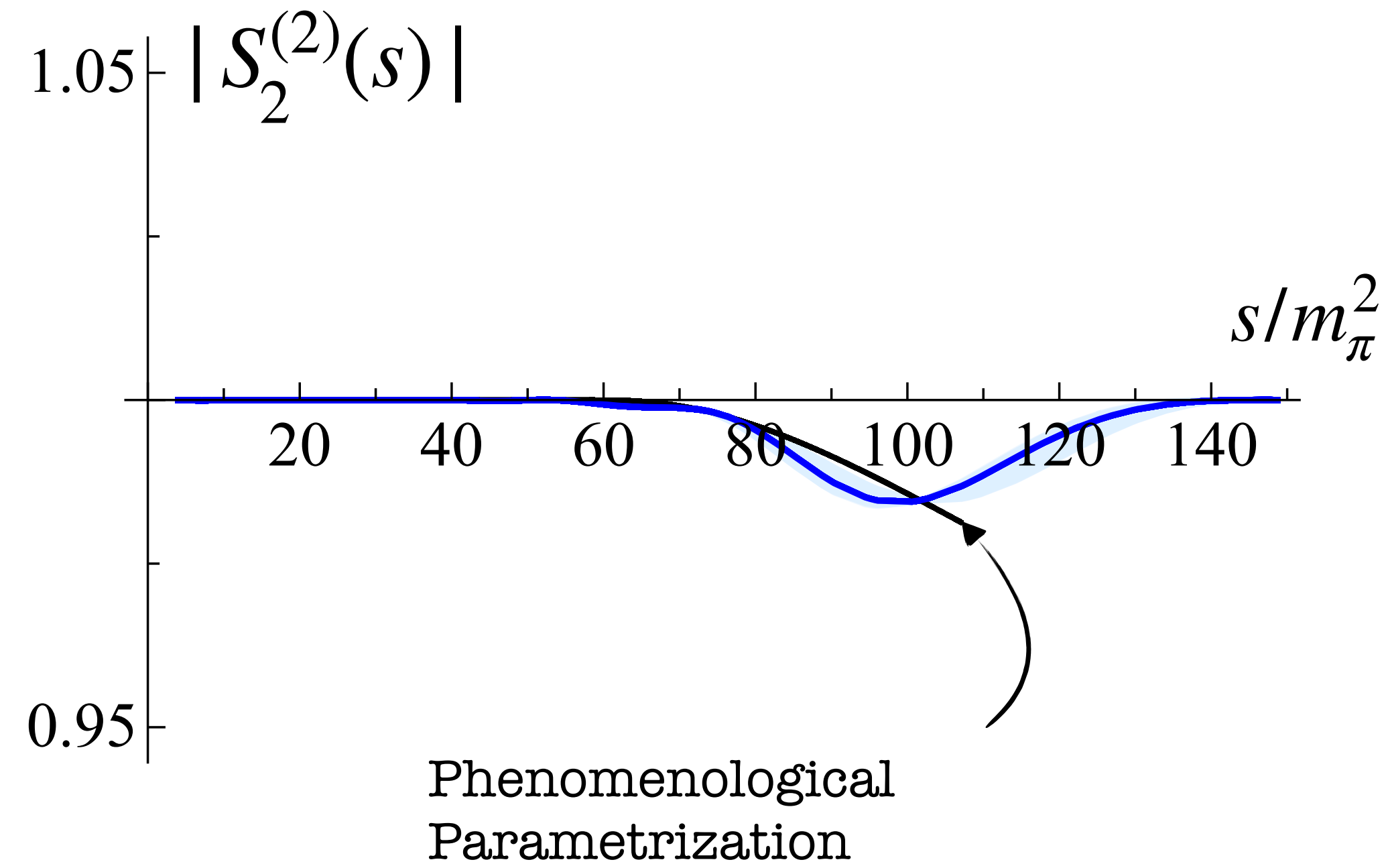


Check against 2-loops χ PT

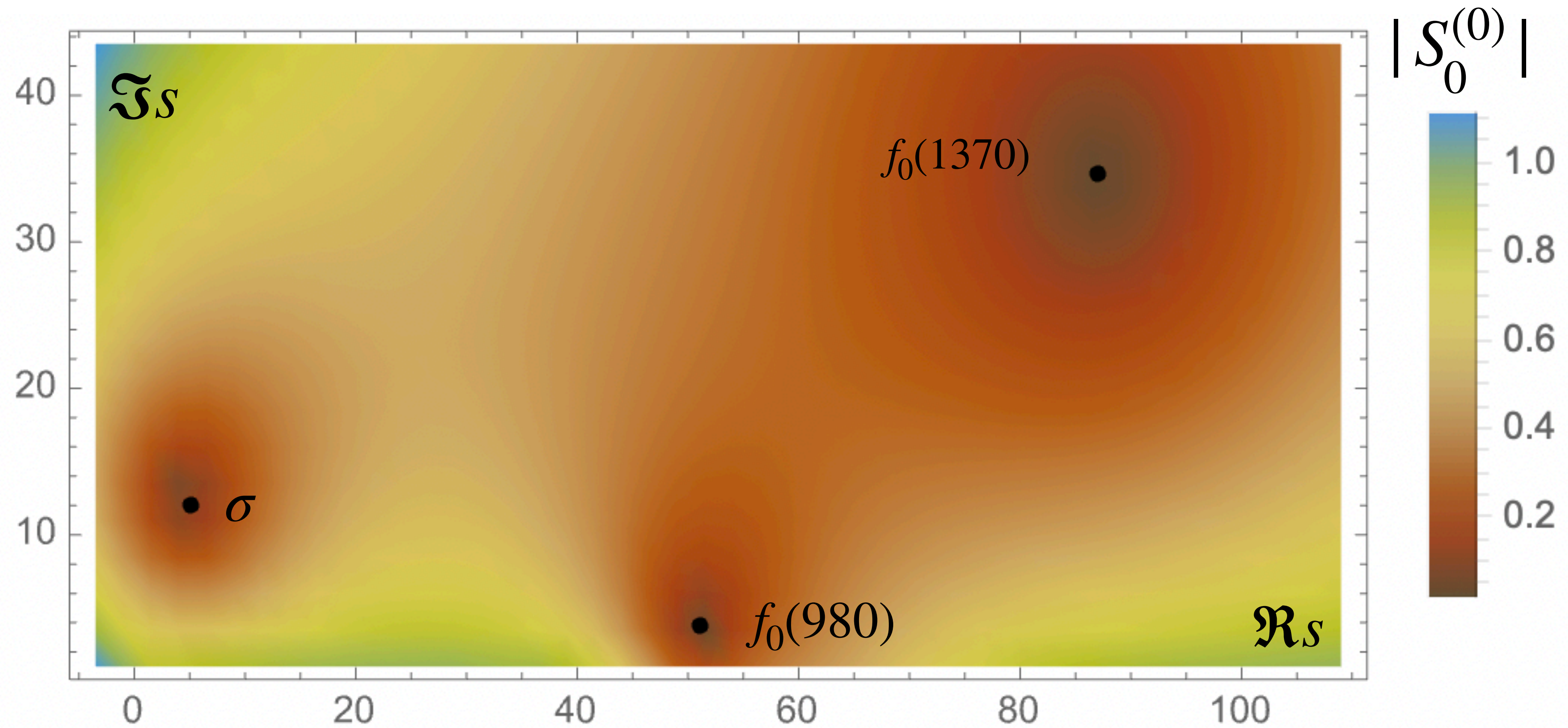


| | Bootstrap Fit | Literature |
|-------------|-------------------------------------|-------------------------------------|
| $a_0^{(2)}$ | $(-0.432 \pm 0.001) \times 10^{-1}$ | $(-0.444 \pm 0.012) \times 10^{-1}$ |
| $a_1^{(1)}$ | $(0.380 \pm 0.002) \times 10^{-1}$ | $(0.379 \pm 0.05) \times 10^{-1}$ |
| $b_0^{(0)}$ | 0.265 ± 0.030 | 0.276 ± 0.006 |
| $b_0^{(2)}$ | $(-0.797 \pm 0.002) \times 10^{-1}$ | $(-0.803 \pm 0.012) \times 10^{-1}$ |
| $b_1^{(1)}$ | $(0.61 \pm 0.02) \times 10^{-2}$ | $(0.57 \pm 0.01) \times 10^{-2}$ |
| $a_2^{(0)}$ | $(0.53 \pm 0.11) \times 10^{-2}$ | $(0.175 \pm 0.003) \times 10^{-2}$ |
| $a_2^{(2)}$ | $(0.51 \pm 0.18) \times 10^{-3}$ | $(0.170 \pm 0.013) \times 10^{-3}$ |
| $a_1^{(3)}$ | $(1.5 \pm 0.4) \times 10^{-4}$ | $(0.56 \pm 0.02) \times 10^{-4}$ |

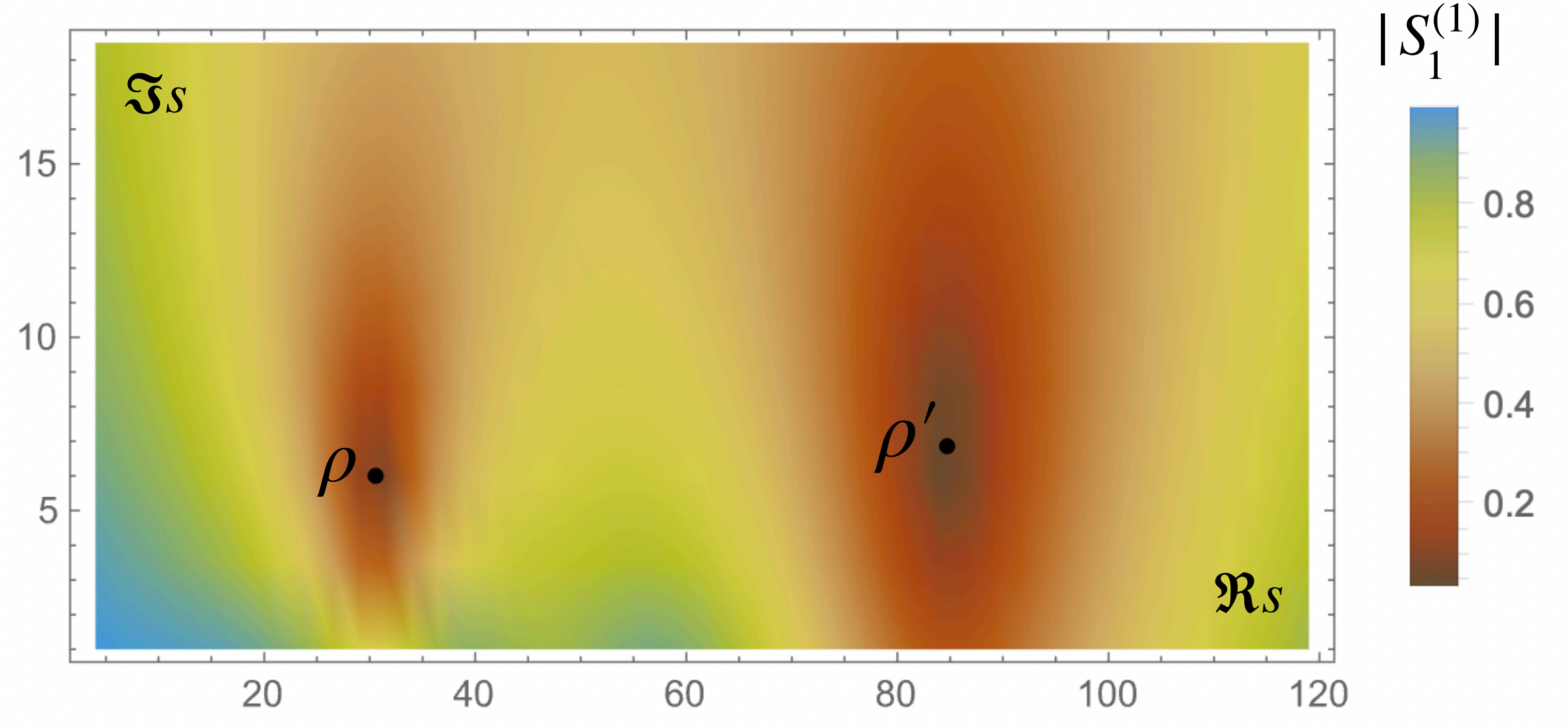
Prediction for I=2, J=2



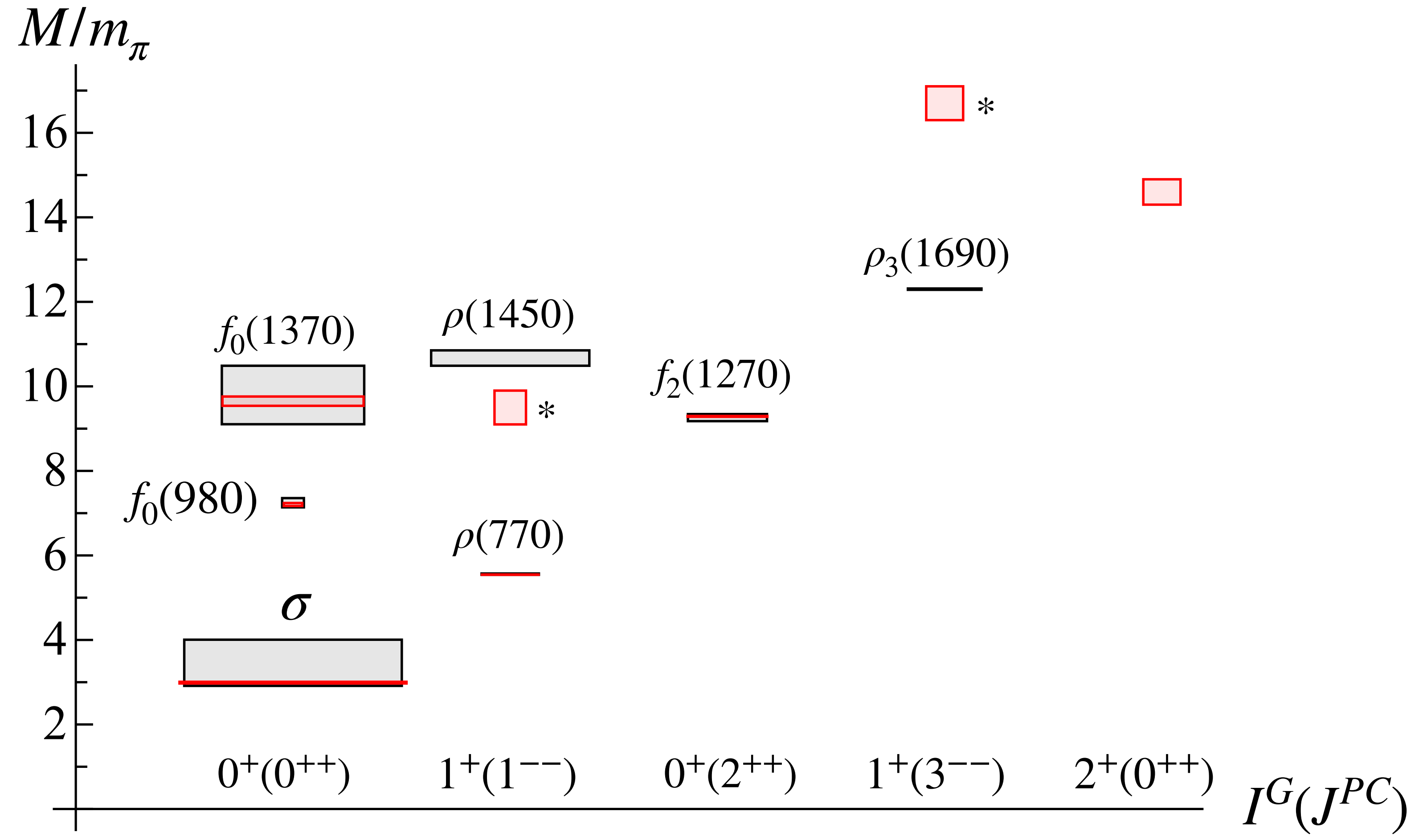
Spectrum for $I=0, J=0$



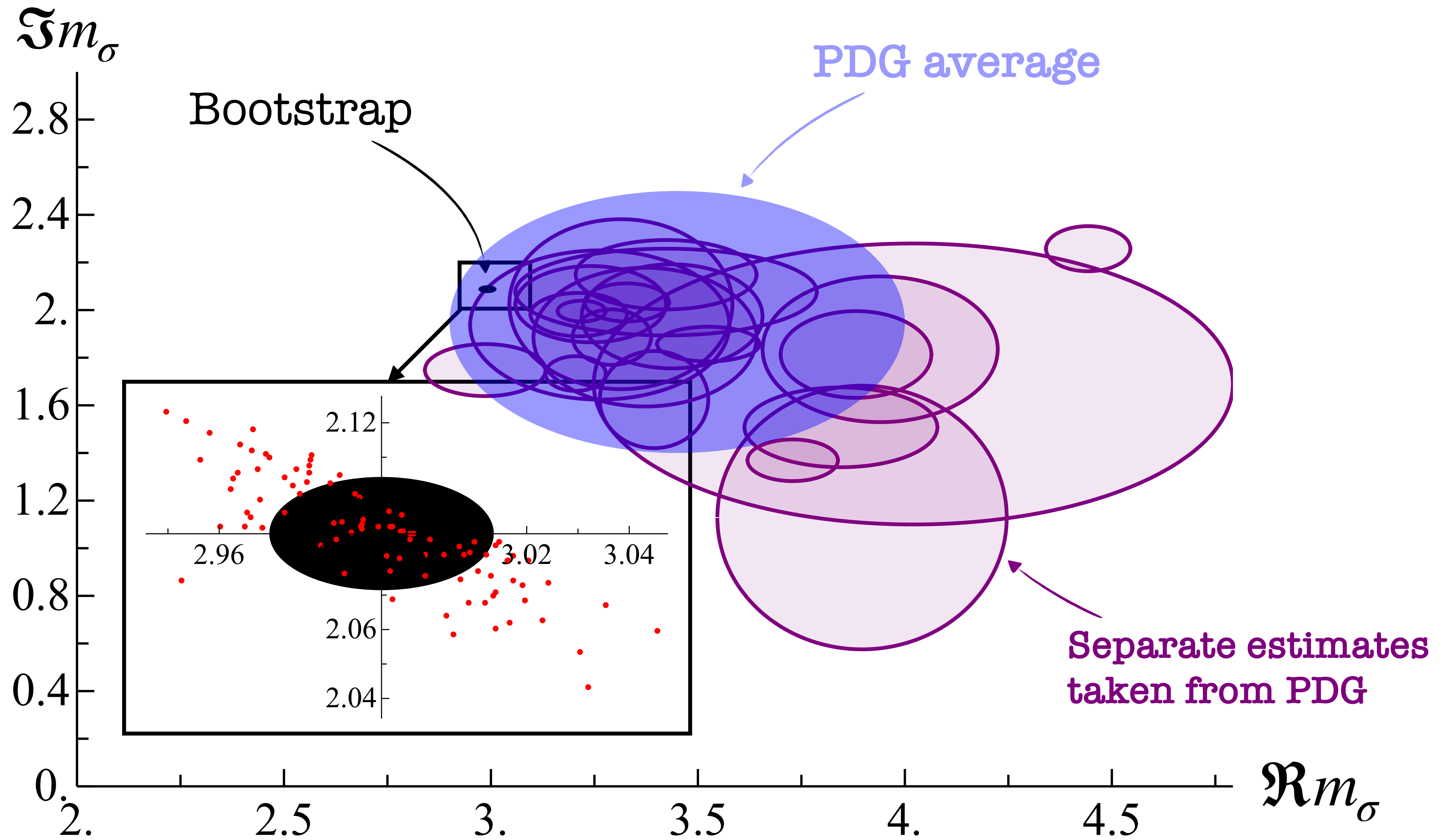
Spectrum for $I=1, J=1$



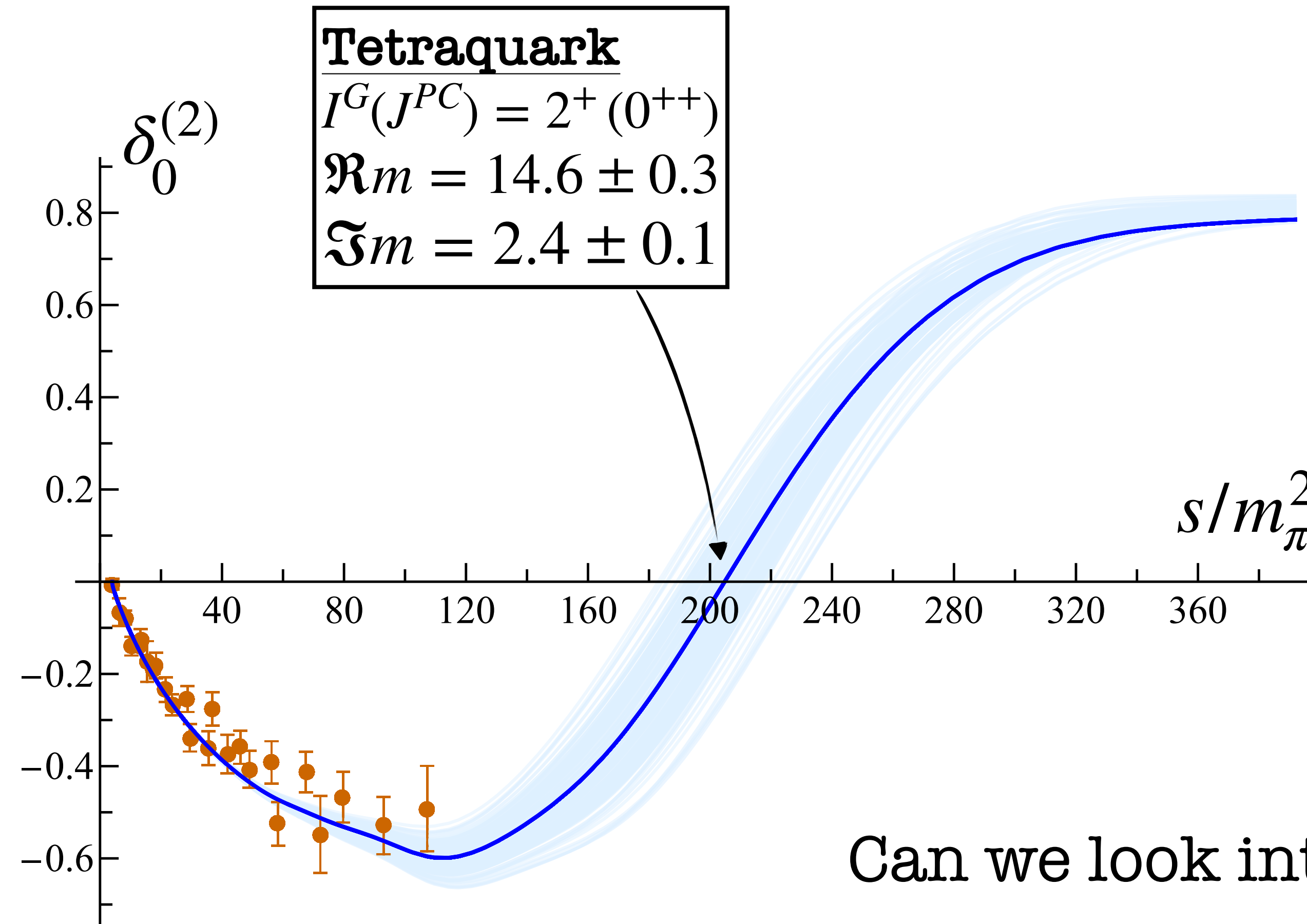
Full Spectrum < 1.4 GeV, with G-parity +1



Sigma parameters determination



The Tetraquark

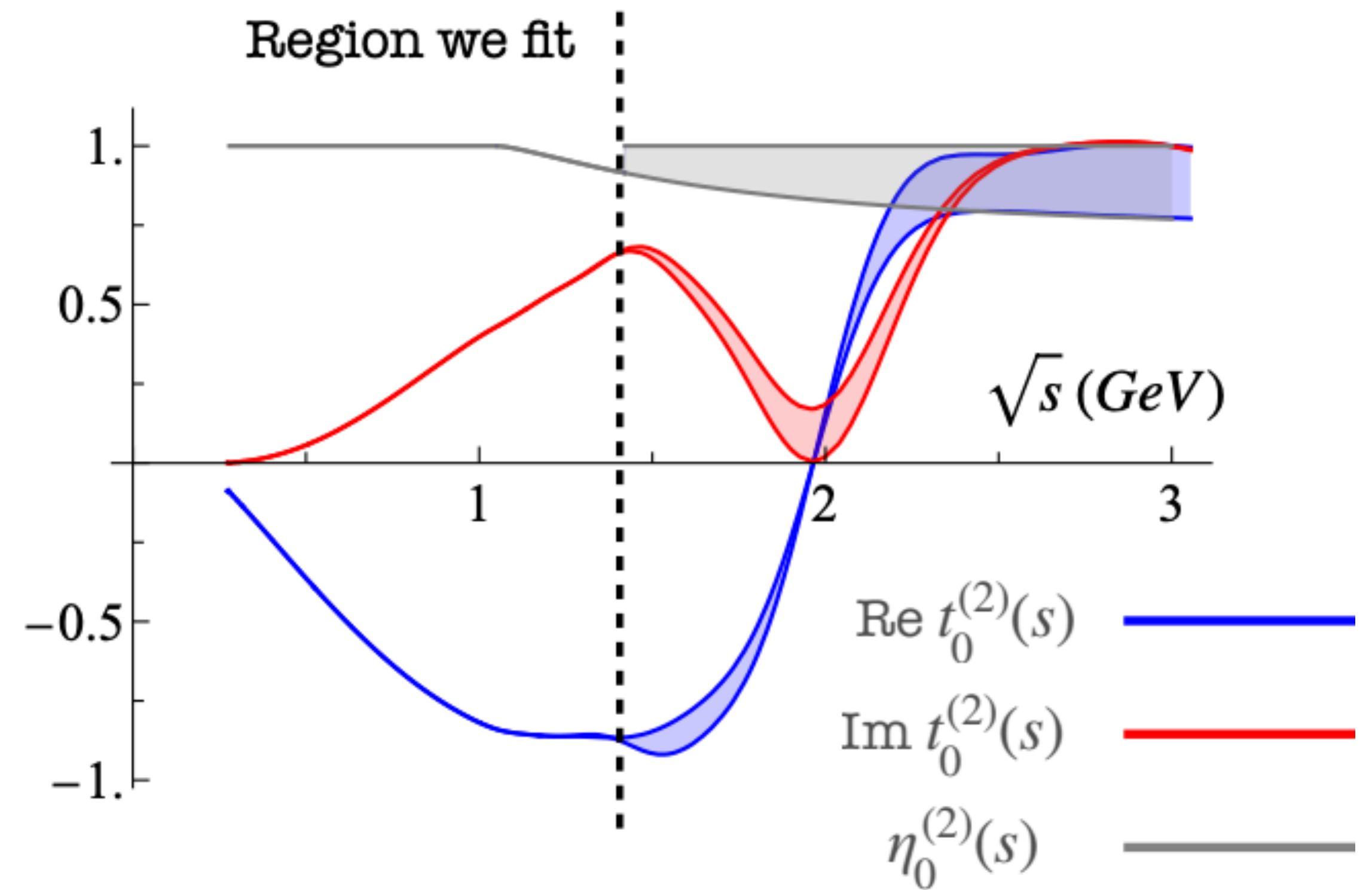
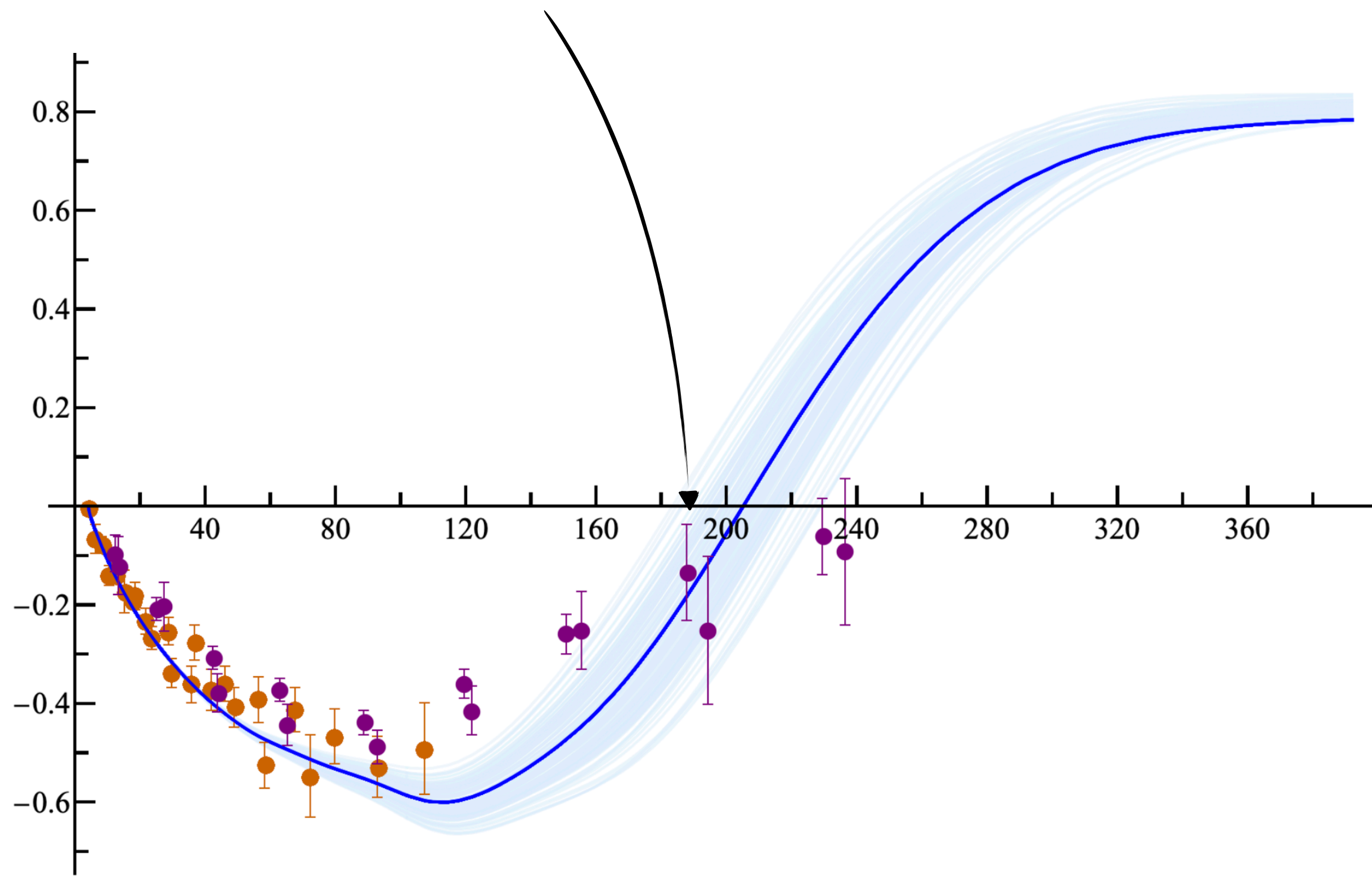


$$M \sim 2\text{GeV},$$
$$\Gamma \sim 600\text{MeV}$$

Can we look into $B^+ \rightarrow D^- \pi^+ \pi^+$?

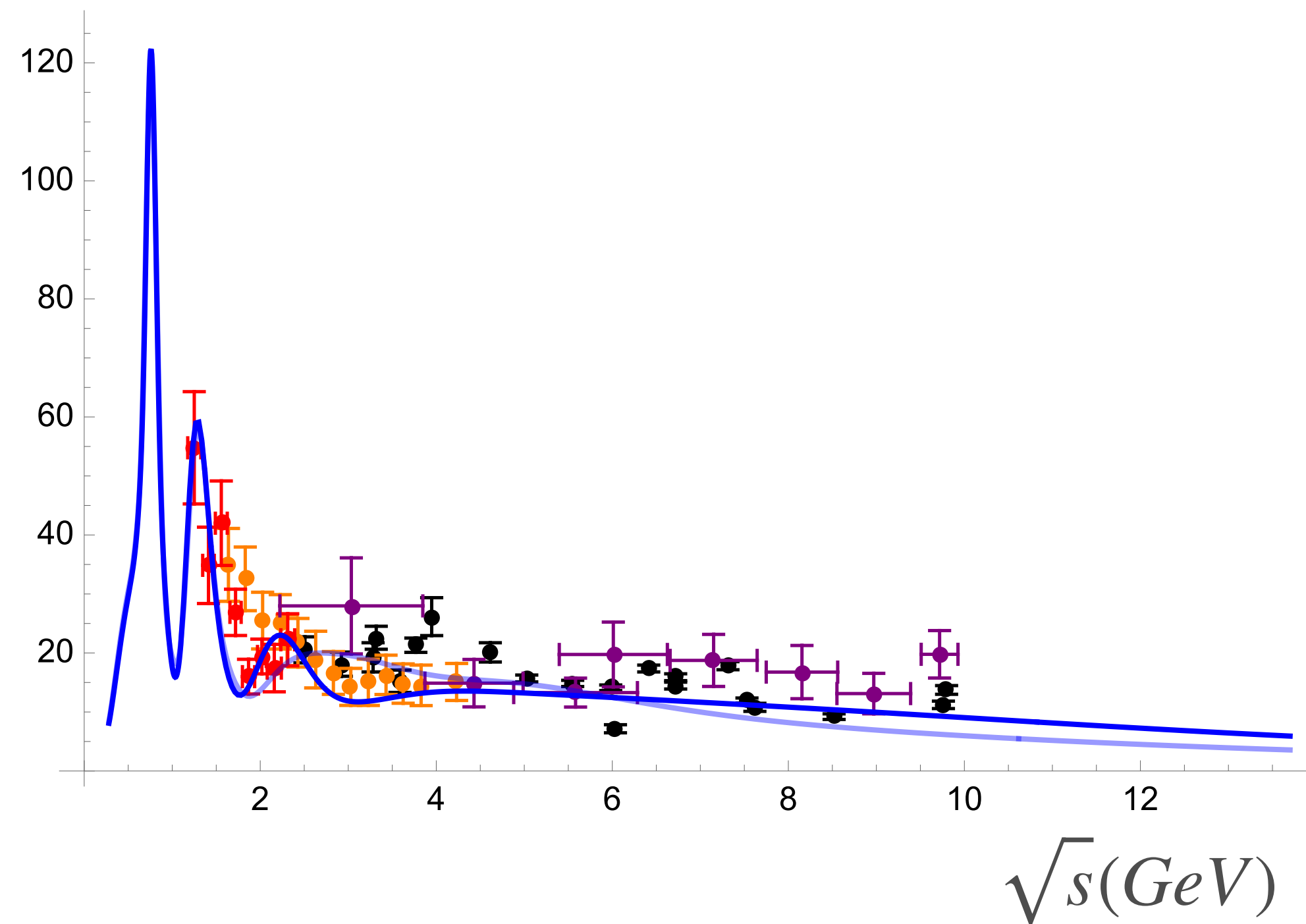
The Tetraquark (news)

Data we had no idea about

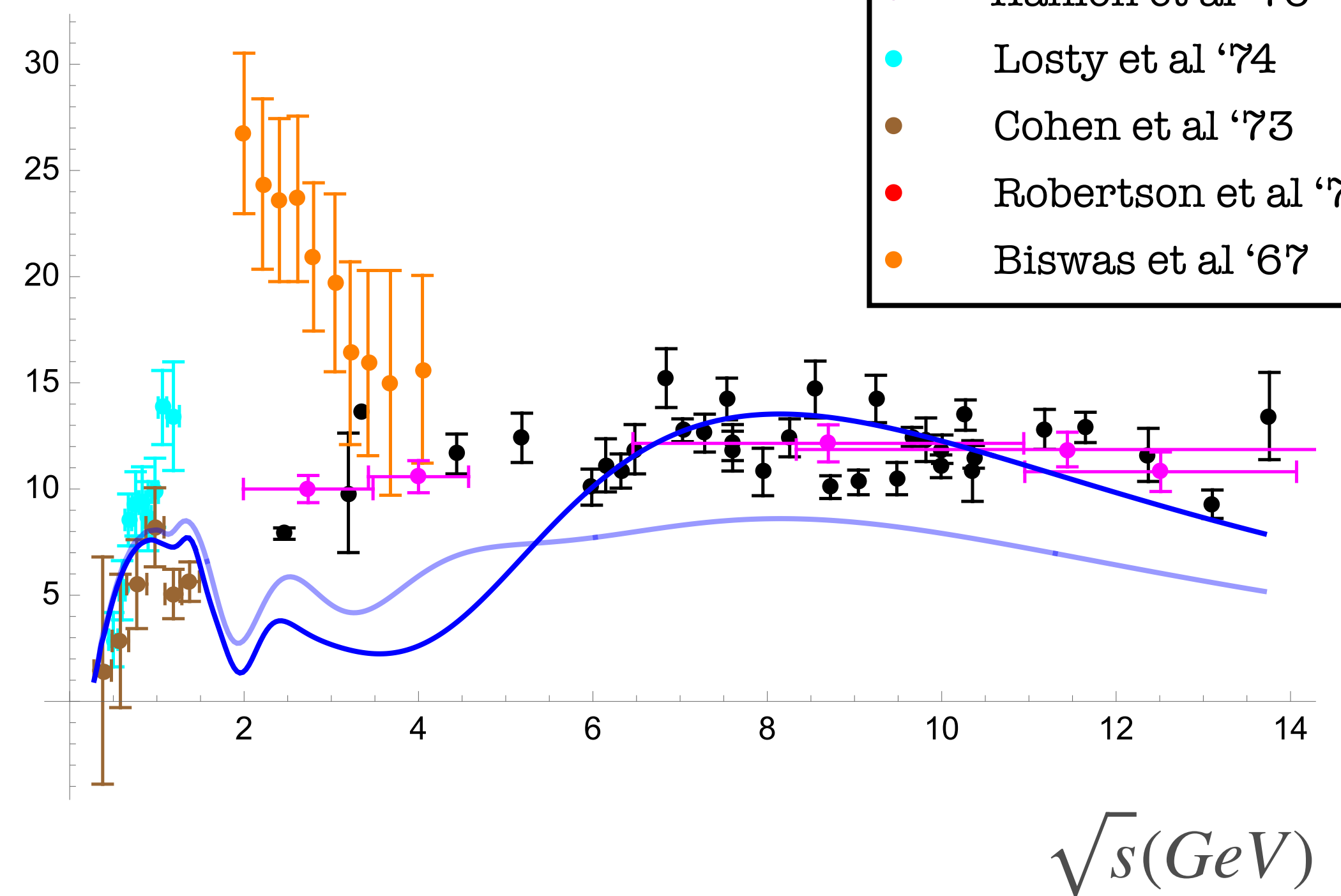


High energy behaviour

$\sigma_{\pi^+\pi^-}(mb)$



$\sigma_{\pi^-\pi^-}(mb)$



- Zacharov, Sergeev '84
- Abramowicz '80
- Hanlon et al '76
- Losty et al '74
- Cohen et al '73
- Robertson et al '73
- Biswas et al '67

Overview

Input

- ★ Experimental phase shifts data for S_0, S_2, P, D_0 waves
- ★ Inelasticity model for S_0, S_2, P, D_0 waves
- ★ \exists chiral zeros
- ★ \exists resonances $\rho(770), f_0(980), f_0(1370), f_2(1270)$

Output

- ♣ Fit for the phase shifts, chiral zeros, resonances positions
- ♣ Scattering lengths and effective ranges for any isospin and spin $\ell < 2$
- ♣ S_0, S_2, P waves for $0 < s < 4$ compatible with χ PT
- ♣ D_2 phase shift and inelasticity compatible with experiments
- ♣ Dynamical generation of $\sigma, \rho(1450), \rho_3$ resonances, plus a tetra quark
- ♣ $\sigma_{\pi^+\pi^-}$ and $\sigma_{\pi^-\pi^-}$ cross sections

Outlook

- 1) Remove Spectrum assumptions and generate the whole spectrum dynamically
- 2) Study complex spin Regge trajectories and understand their non-perturbative pattern
- 3) Include better data from lattice and other experiments
- 4) Study the couples system $\pi\pi \rightarrow \pi\pi$, $\pi\pi \rightarrow KK$, $KK \rightarrow KK$ and fit inelasticity (systematic at the moment)
- 5) Work in synergy with lattice groups and study properties of glueballs