

Is leptogenesis during gravitational reheating flavorful?

Based on:

Basabendu Barman, AD, Md Riajul Haque: [arXiv:2410.16381](https://arxiv.org/abs/2410.16381) [hep-ph]

also

AD, Rishav Roshan and Arunansu Sil: [Phys.Rev.Lett. 132 \(2024\) 6, 061802](#)

AD, Rishav Roshan and Arunansu Sil: [Phys.Rev.D 108 \(2023\) 3, 035029](#)

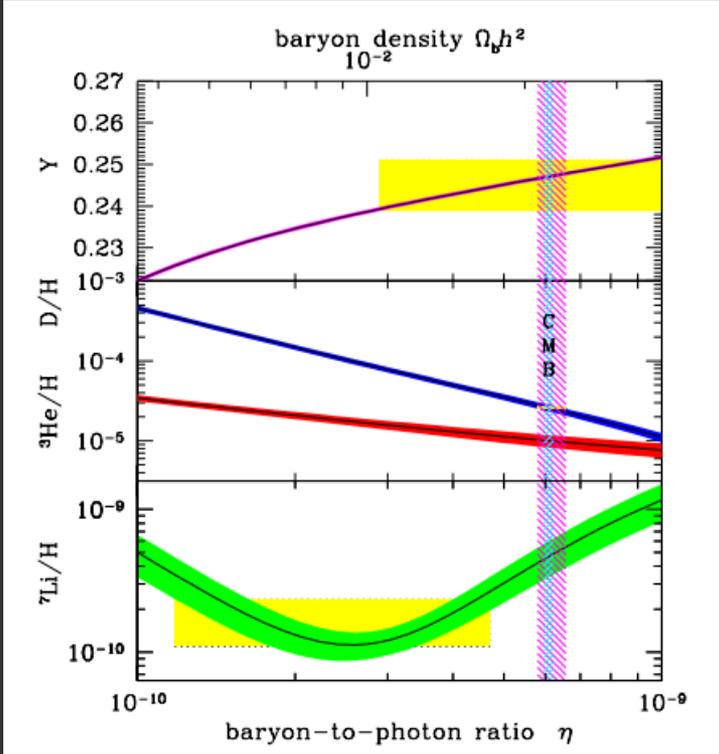
Arghyajit Datta
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Evidence of matter-antimatter asymmetry

Baryon to photon ratio:

$$\eta_B \equiv \frac{n_B - n_{\bar{B}}}{n_\gamma}$$

Both CMB and BBN provide similar bounds on this Baryon asymmetry Parameter



$$\eta_B = (6.047 \pm 0.074) \times 10^{-10}$$

[PLANCK, 2015]

[PDG, 2018]

Leptogenesis

Dynamically generates the baryon asymmetry by generating a lepton asymmetry first

Advantages: Neutrino Mass



Lepton asymmetry

Type-I Seesaw mechanism
(SM + 3 Right-Handed Neutrinos)

[Minkowsky, 1977]

[Yanagida, 1979]

[Gell-Mann, Ramond, Slansky, 1979]

[Mohapatra, Senjanovic, 1980]

$$m_D = \frac{Y_\nu v}{\sqrt{2}}$$

$$\mathcal{L}_{BSM} = Y_{\alpha i}^\nu \bar{\ell}_{L\alpha} \tilde{H} N_i + \frac{M_N}{2} \bar{N}_i^c N_i + h.c \longleftrightarrow m_\nu = -m_D M_N^{-1} m_D^T$$

Leptogenesis

Advantages: connects the origin of neutrino mass

Advantages: Neutrino Mass



Lepton asymmetry

Type-I Seesaw mechanism
(SM + 3 Right-Handed Neutrinos)

[Minkowsky, 1977]
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CP Violation

Lepton number Violation

Out-of equilibrium dynamics

[Sakharov, 1967]

Decay of RHN at $T < M_N$

$$[N \rightarrow \ell + H]$$

$$[N \rightarrow \bar{\ell} + \bar{H}]$$

$$\Delta L \neq 0 \xrightarrow{\text{Sphaleron Process}} \Delta B \neq 0$$

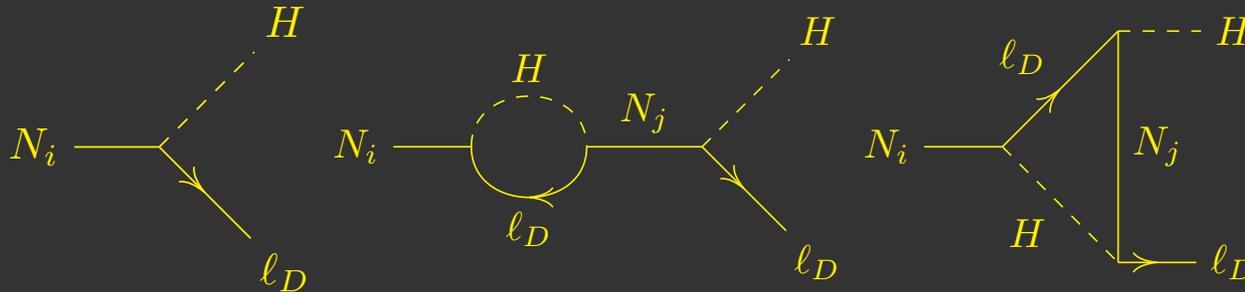
Leptogenesis

$$\mathcal{L}_{BSM} = Y_{\alpha i}^\nu \bar{\ell}_{L\alpha} \tilde{H} N_i + \frac{M_N}{2} \bar{N}_i^c N_i + h.c$$

Assumptions:

1) Hierarchical RHNs : only lightest RHN will generate the asymmetry.

2) $\ell_D = \frac{Y_{\alpha 1}^\nu}{\sqrt{(Y^{\nu\dagger} Y^\nu)_{11}}} \ell_\alpha$: asymmetry is generated along this direction



$$\epsilon_i = \frac{\Gamma(N_i \rightarrow \ell_D + H) - \Gamma(N_i \rightarrow \bar{\ell}_D + H^\dagger)}{\Gamma(N_i \rightarrow \ell_D + H) + \Gamma(N_i \rightarrow \bar{\ell}_D + H^\dagger)} = \frac{1}{8\pi(Y^{\nu\dagger} Y^\nu)_{ii}} \sum_{j \neq i} \text{Im} \left[(Y^{\nu\dagger} Y^\nu)_{ij}^2 \right] \mathcal{F} \left(\frac{M_j^2}{M_i^2} \right)$$

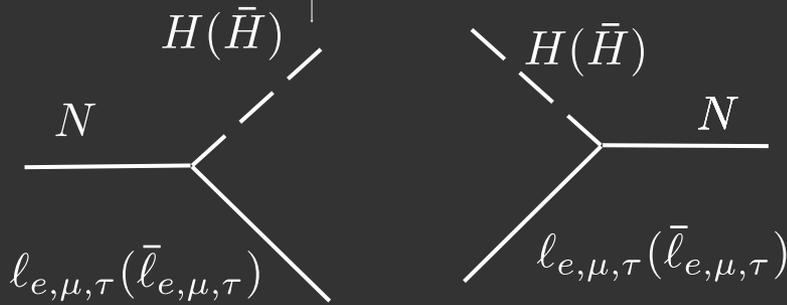
$$\mathcal{F}(x) = \sqrt{x} \left[1 + \frac{1}{1-x} + (1+x) \ln \left(\frac{x}{1+x} \right) \right]$$

Lepton & Baryon asymmetry

$$s\mathcal{H}z \frac{dY_{N_1}}{dz} = \left(\frac{Y_{N_1}}{Y_{N_1}^{\text{eq}}} - 1 \right) (\gamma_D + 2\gamma_{S_s} + 4\gamma_{S_t})$$

$$s\mathcal{H}z \frac{dY_{B-L}}{dz} = - \left\{ \left(\frac{Y_{N_1}}{Y_{N_1}^{\text{eq}}} - 1 \right) \varepsilon_1 \gamma_D - \frac{Y_{B-L}}{Y_\ell^{\text{eq}}} \left(2\gamma_N + 2\gamma_{S_t} + \gamma_{S_s} \frac{Y_{N_1}}{Y_{N_1}^{\text{eq}}} \right) \right\}$$

$$[M_1 \ll M_2, M_3]$$



**2-2 scattering
Washout**

Production

Washout

$$Y_B = \frac{28}{79} Y_{B-L}$$

(At sphaleron decoupling limit)

$$T \sim 150 \text{ GeV}$$

$$* z = \frac{M_1}{T}$$

$$* Y_x = \frac{n_x}{s}$$

$$* \gamma_D = \gamma(N \rightarrow \ell H) + \gamma(N \rightarrow \bar{\ell} \bar{H})$$

Flavor effect in Leptogenesis

$$\mathcal{L} = Y_{\alpha i}^{\nu} \bar{\ell}_{L\alpha} \tilde{H} N_i + Y_{\alpha} (\bar{\ell}_L)_{\alpha} H (\ell_R)_{\alpha} + h.c$$

[Credit to
Barbieria et. al., 2000; Nardi et. al., 2005, 2006;
Blanchet, Bari, 2006, 2007; A. Abada et.al., 2007;
,and many more...]

$$\Gamma_{\alpha} < \mathcal{H} \quad (T \gg 5 \times 10^{11} \text{ GeV})$$



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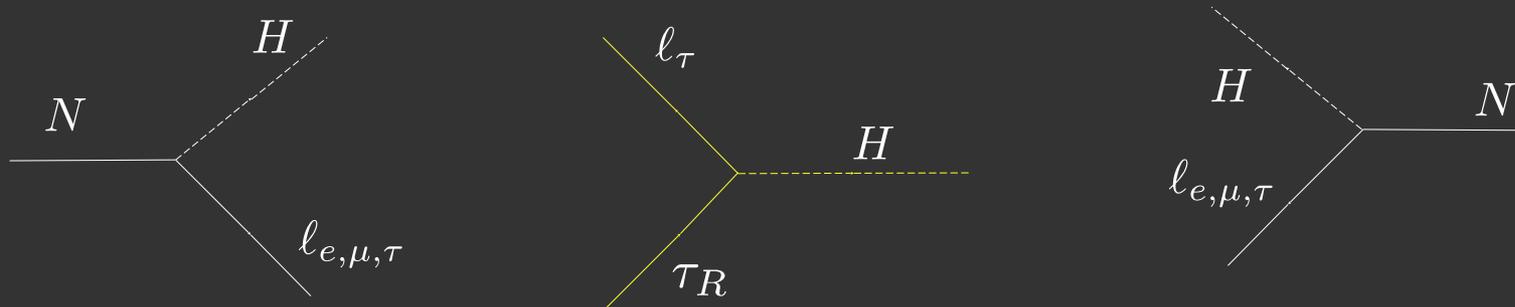
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$$\Gamma_\alpha < \mathcal{H} \quad (T \gg 5 \times 10^{11} \text{ GeV})$$



$$\Gamma_\tau (\propto m_h^2(T)/T) > \mathcal{H}$$

[right-handed tau enters equilibrium]



Washout along individual flavors become different

Flavor effect in Leptogenesis

$$\mathcal{L} = Y_{\alpha i}^\nu \bar{\ell}_{L\alpha} \tilde{H} N_i + Y_\alpha (\bar{\ell}_L)_\alpha H (\ell_R)_\alpha + h.c$$

T [GeV] ↑

No Flavor effect: $|\ell_D\rangle = \langle \ell_\alpha | \ell_D \rangle |\ell_\alpha\rangle$

$T_\tau^0 \sim 5 \times 10^{11}$ GeV

$\Gamma_\tau = \mathcal{H}$

Two Flavor: $|\ell_\alpha\rangle, |\ell_\tau\rangle$

$$Y_{B-L} = Y_{B/3-L_\alpha} + Y_{B/3-L_\tau}$$

$T_\mu^0 \sim 10^9$ GeV

$\Gamma_\mu = \mathcal{H}$

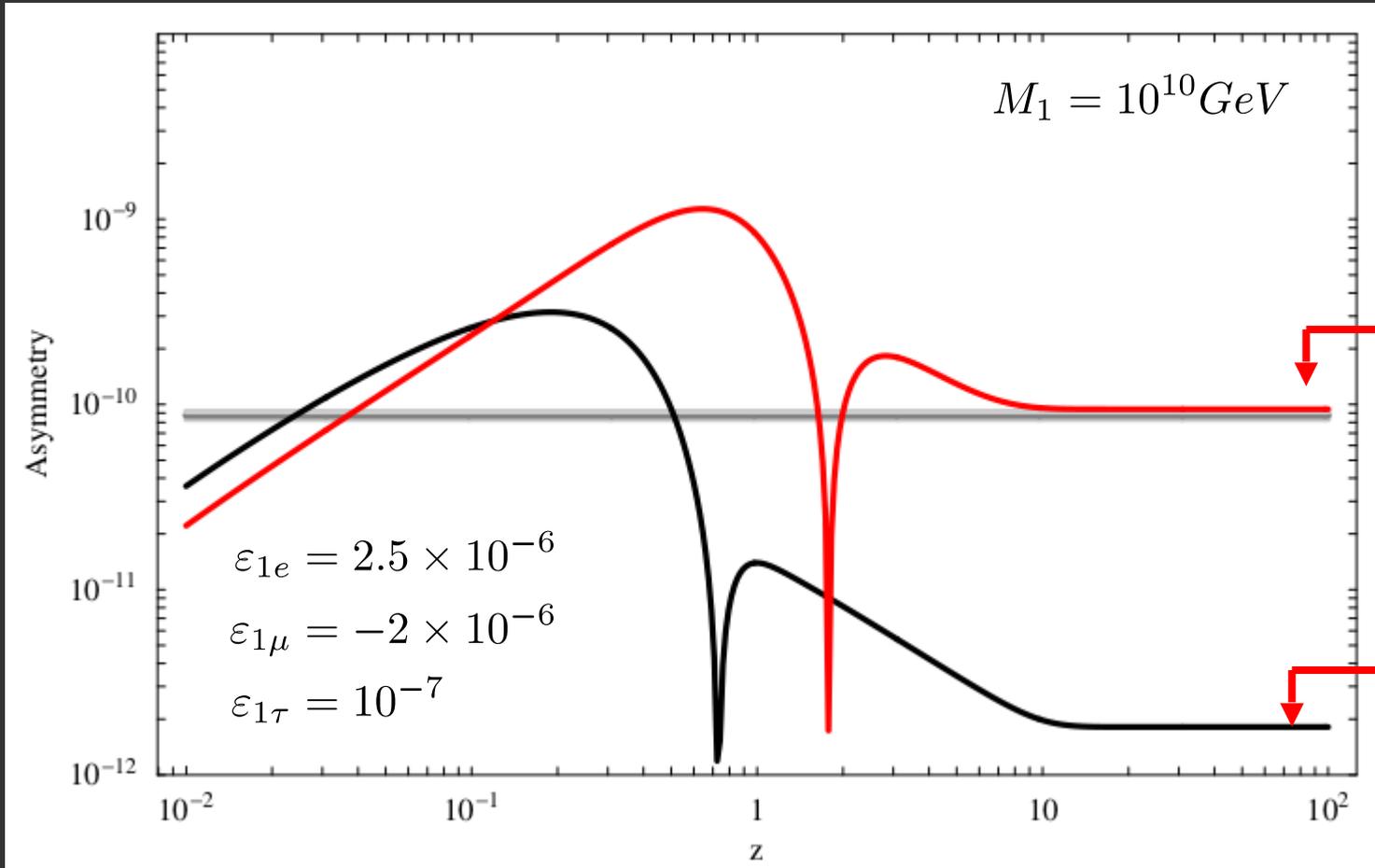
Three Flavor: $|\ell_e\rangle, |\ell_\mu\rangle, |\ell_\tau\rangle$

$$Y_{B-L} = Y_{B/3-L_e} + Y_{B/3-L_\mu} + Y_{B/3-L_\tau}$$

$$s\mathcal{H}z \frac{dY_{B/3-L_\alpha}}{dz} = - \left\{ \left(\frac{Y_{N_1}}{Y_{N_1}^{\text{eq}}} - 1 \right) \epsilon_{\ell_\alpha} + \frac{1}{2} K_\alpha^0 \sum_\beta (C_{\alpha\beta}^\ell + C_\beta^H) \frac{Y_{B/3-L_\beta}}{Y_\ell^{\text{eq}}} \right\} \gamma_D$$

Importance of flavor effect

[A. Abada, S. Davidson, A. Ibarra, F.-X. Josse-Michaux, M. Losada and A. Riotto, JHEP0609:010,2006]

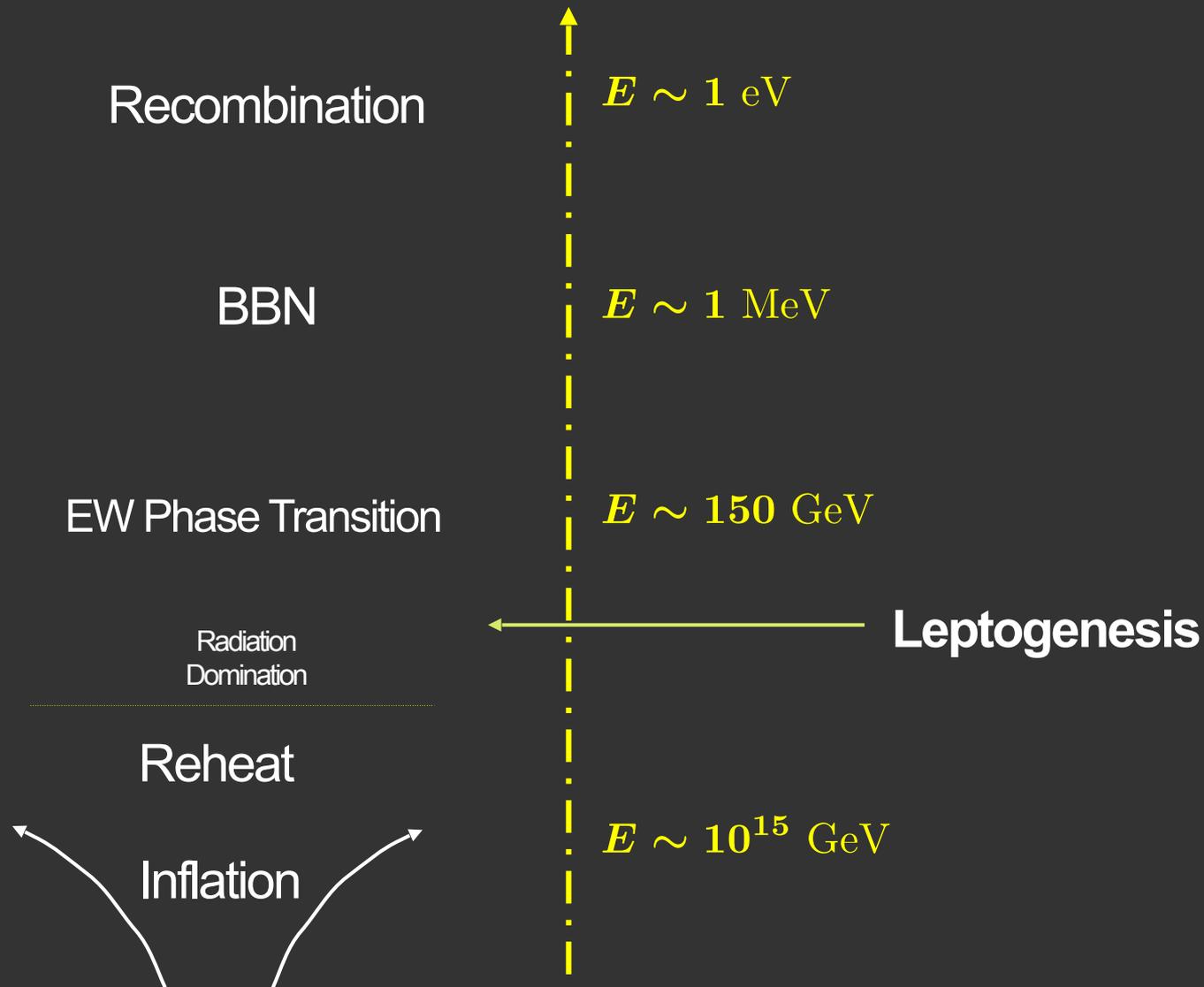


Two flavor

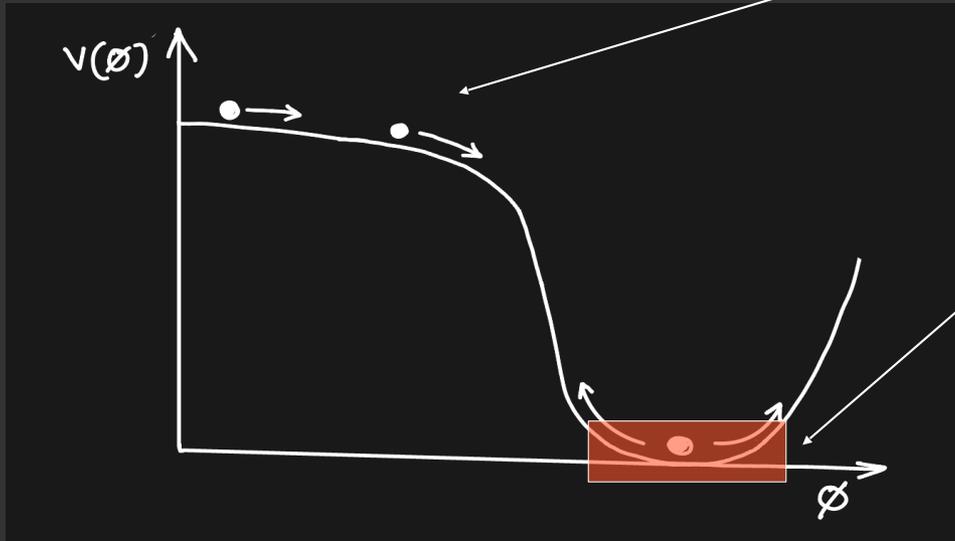
unflavor / one flavor

Almost one order shift in produced baryon asymmetry can be achieved

Timeline of Leptogenesis:



Inflationary Universe [exponential expansion: $a \sim e^{Ht}$]



Transfer of energy of inflaton

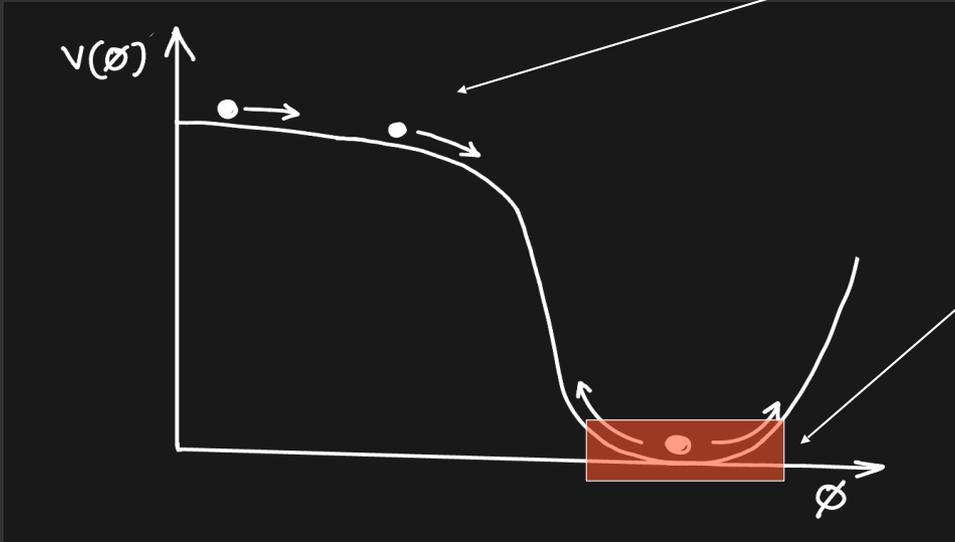
Reheating

- Beginning of the thermal history.
- All elementary particles (of SM) are generated

$$V(\phi) = \lambda M_p^4 \left[\sqrt{6} \tanh \left(\frac{\phi}{\sqrt{6} M_p} \right) \right]^k \longrightarrow \lambda M_p^4 \left(\frac{\phi}{M_p} \right)^k$$

[See Marcos Garcia, Yann Mambrini's Talk]

Inflationary Universe [exponential expansion: $a \sim e^{Ht}$]



Transfer of energy of inflaton

Reheating

- Beginning of the thermal history.
- All elementary particles (of SM) are generated

Most Minimal way

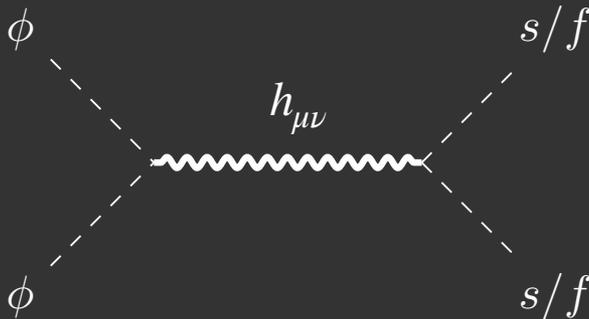
Universal Gravitational Coupling

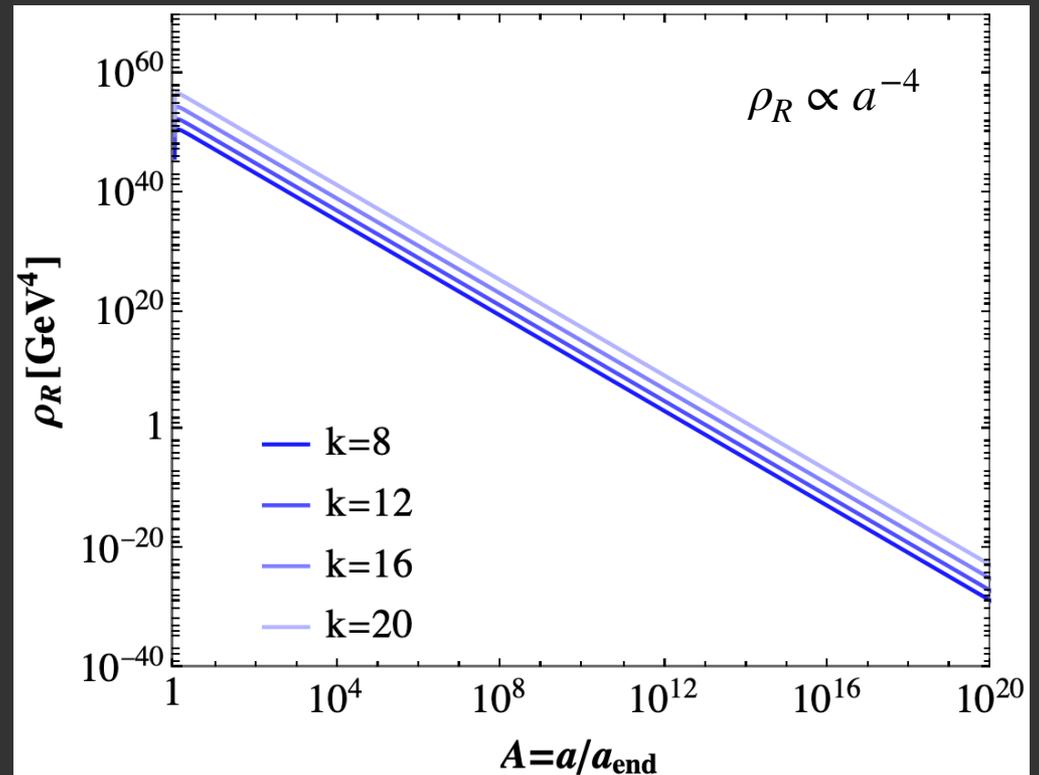
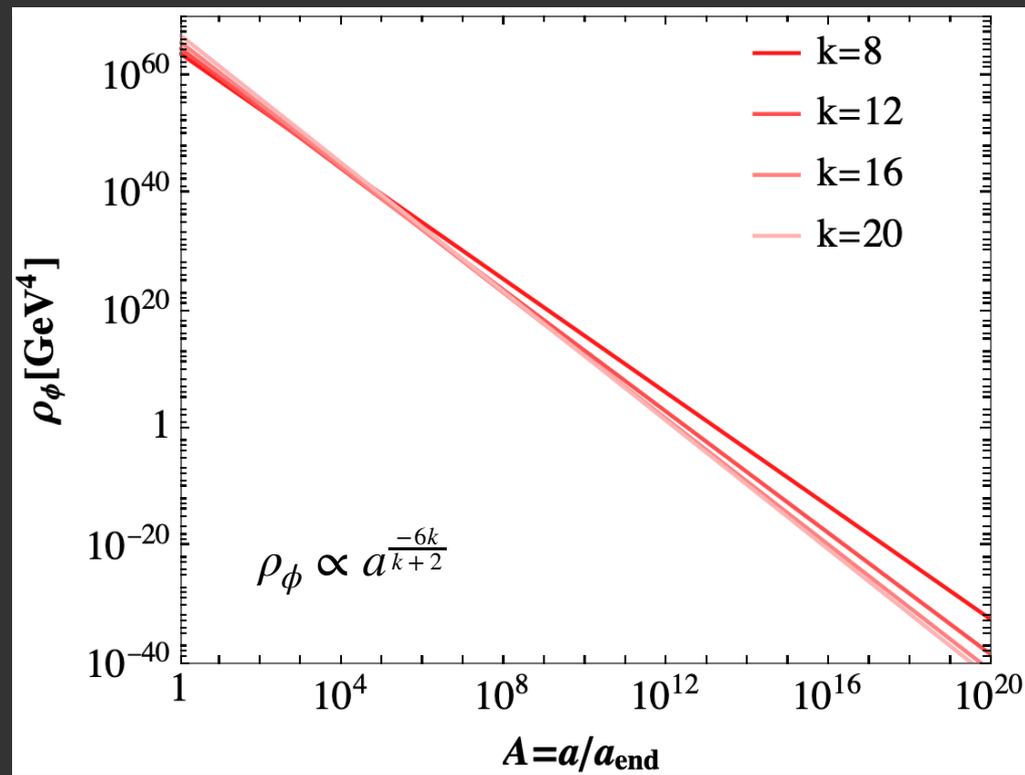
$$S = \int d^4x \sqrt{-g} \left[\frac{M_p^2}{2} R + \mathcal{L}_\phi + \mathcal{L}_{\text{SM}} \right]$$

$$g_{\mu\nu} \simeq \eta_{\mu\nu} + \frac{2}{M_p} h_{\mu\nu}$$

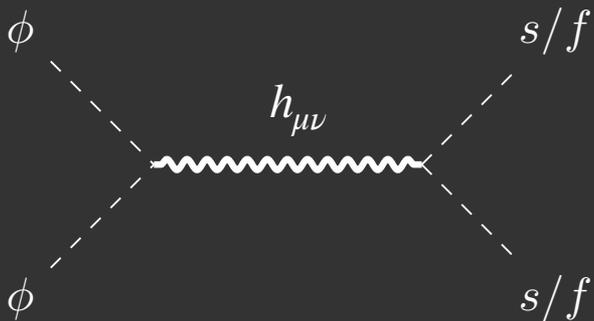
$$\sqrt{-g} \mathcal{L} = -\frac{1}{M_p} h_{\mu\nu} T_{s/f}^{\mu\nu}$$

$$V(\phi) = \lambda M_p^4 \left[\sqrt{6} \tanh \left(\frac{\phi}{\sqrt{6} M_p} \right) \right]^k \longrightarrow \lambda M_p^4 \left(\frac{\phi}{M_p} \right)^k$$



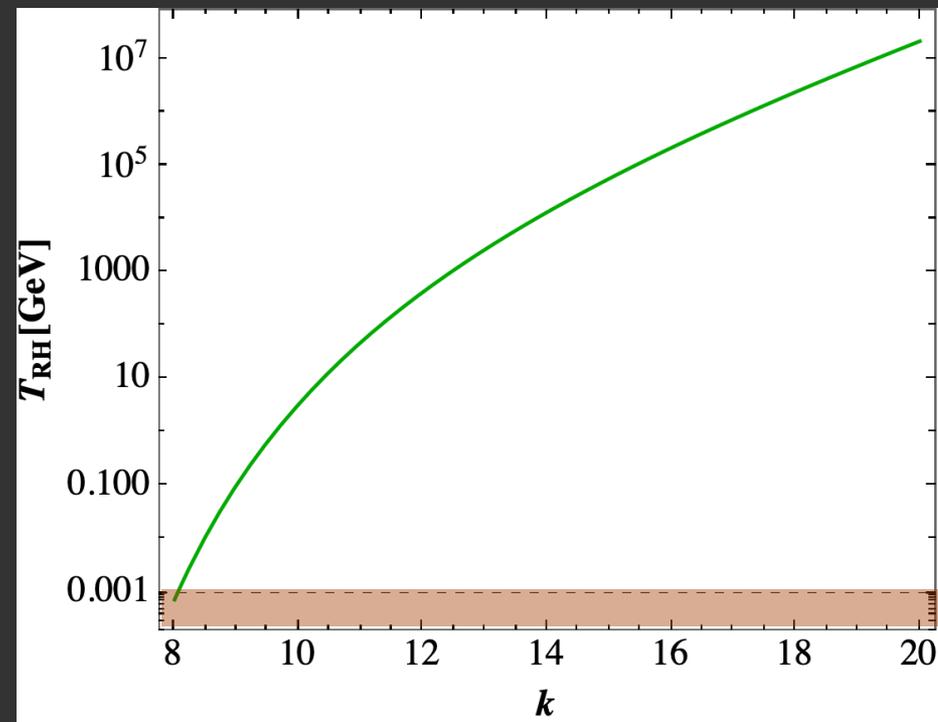
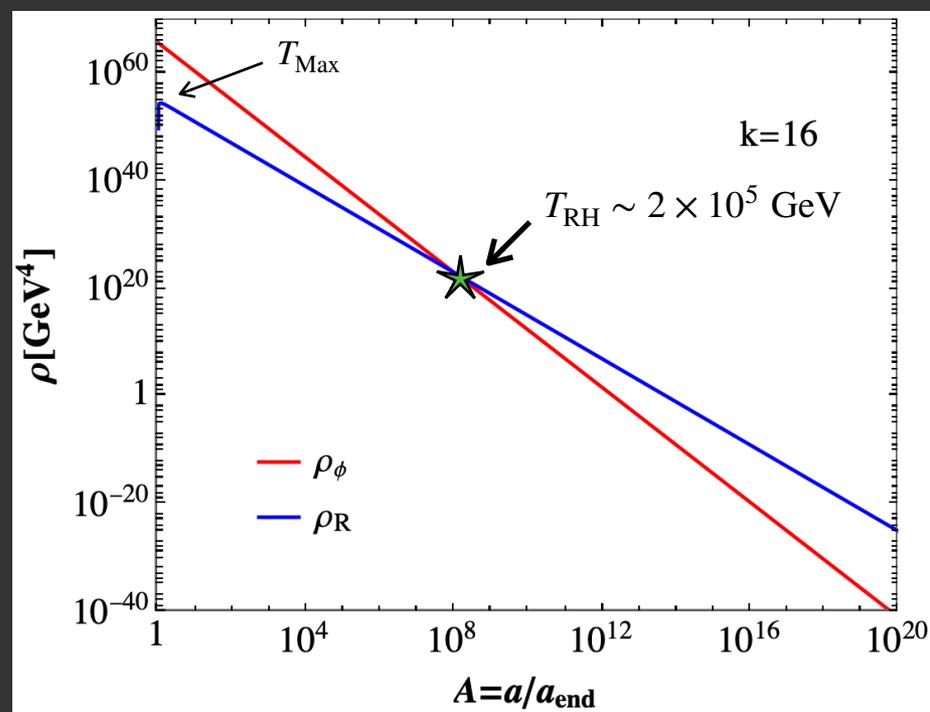
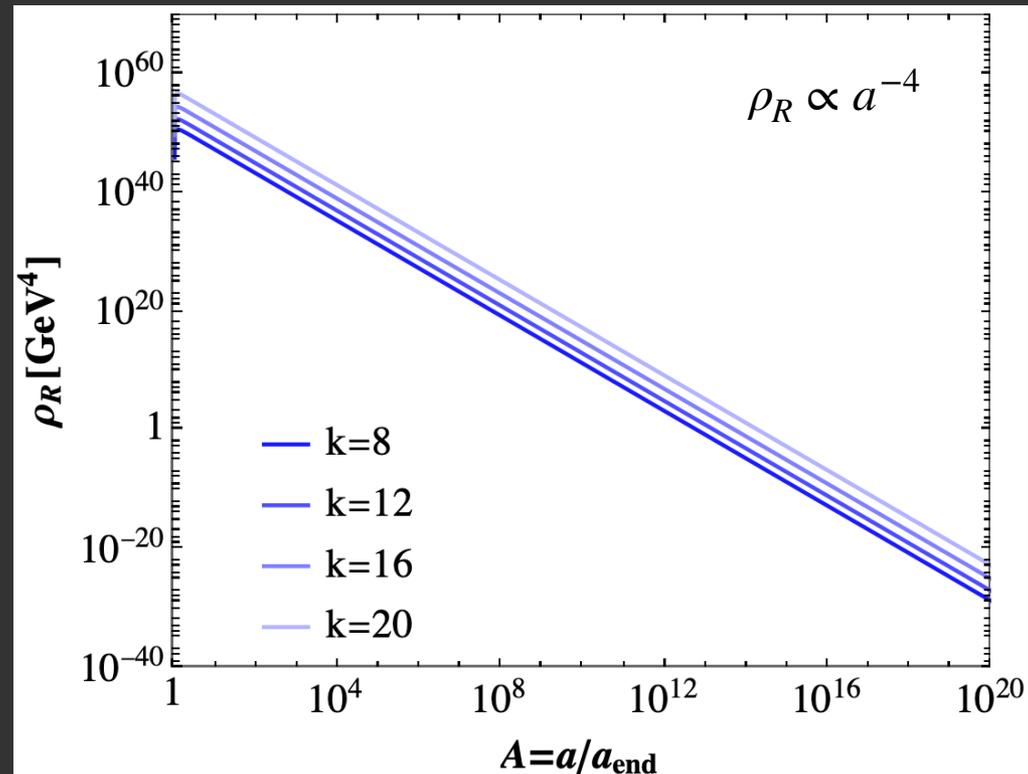
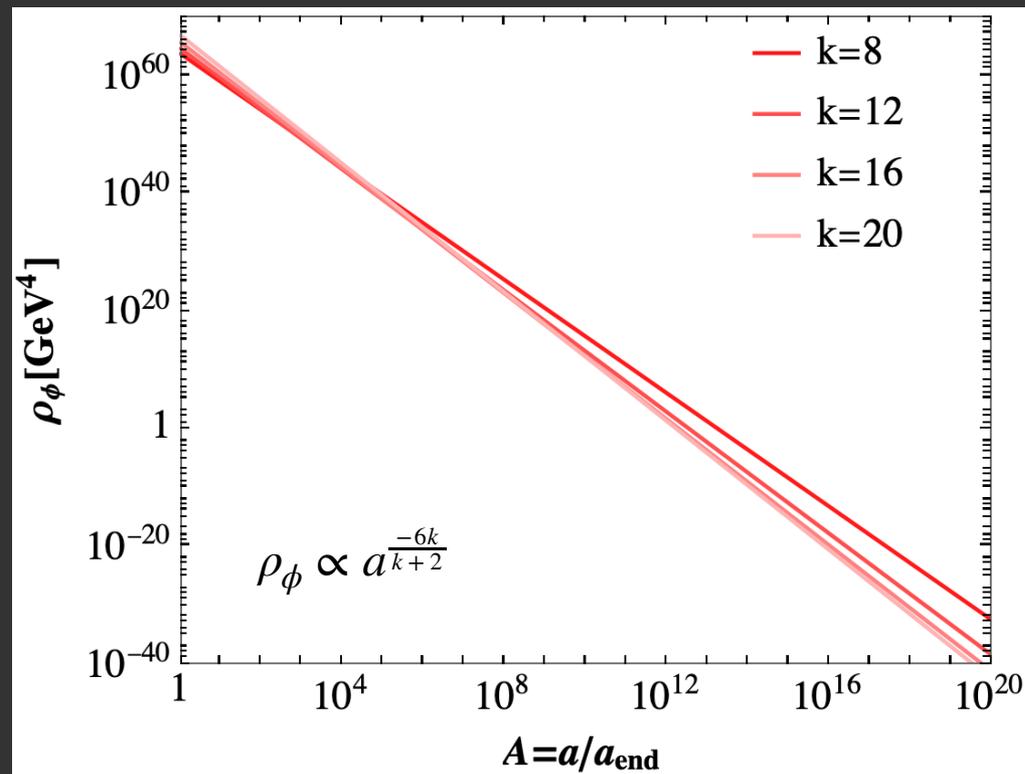


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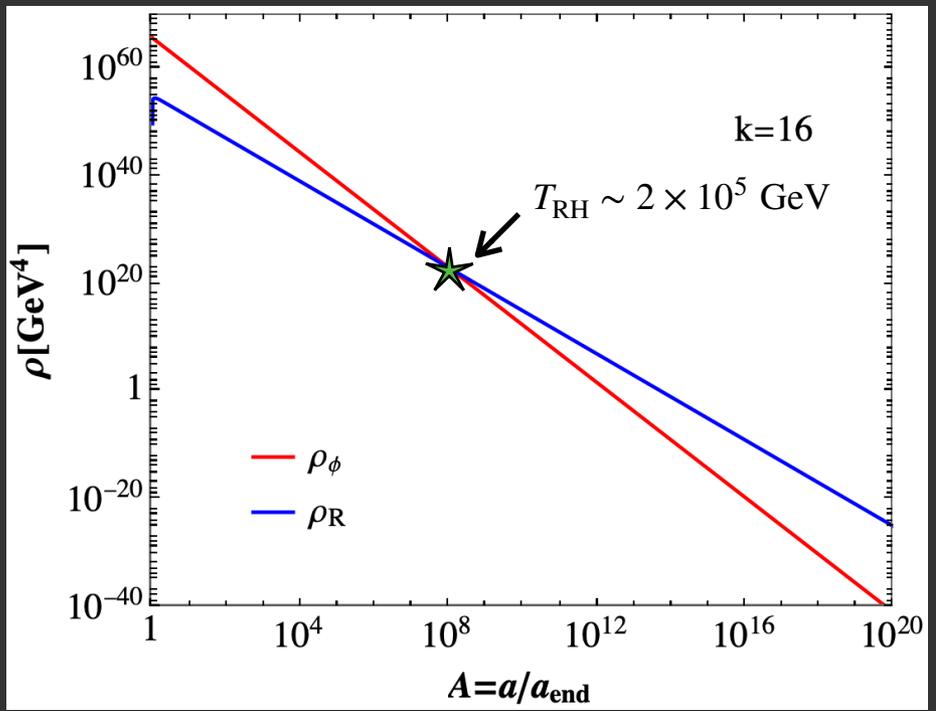
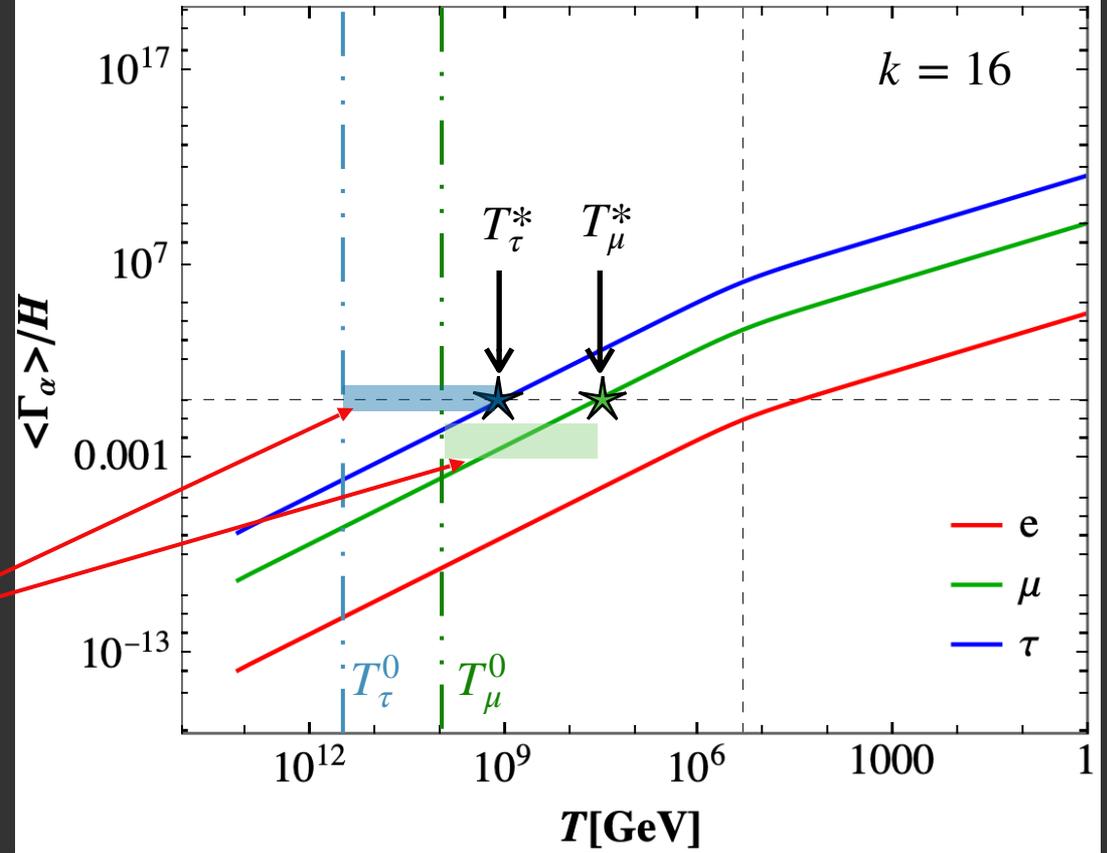
$$\frac{d\rho_\phi}{dt} + 3\mathcal{H}(1 + \omega_\phi)\rho_\phi = -(1 + \omega_\phi)\rho_\phi\Gamma_\phi$$

$$\frac{d\rho_R}{dt} + 4\mathcal{H}\rho_R = (1 + \omega_\phi)\rho_\phi\Gamma_\phi$$



$$\langle \Gamma_\alpha \rangle = \frac{\pi Y_\alpha^2}{192 \zeta(3)} \frac{m_h^2(T)}{T} = \mathcal{H}$$

Delayed equilibration of charged lepton Yukawa interactions



Modification of Flavor effect

$$\mathcal{L} = Y_{\alpha i}^\nu \bar{\ell}_{L\alpha} \tilde{H} N_i + Y_\alpha (\bar{\ell}_L)_\alpha H (\ell_R)_\alpha + h.c$$

T [GeV] ↑

No Flavor effect: $|\ell_1\rangle = \langle \ell_\alpha | \ell_1 \rangle |\ell_\alpha\rangle$

$T_\tau^0 \sim 5 \times 10^{11}$ GeV

$$\Gamma_\tau = \mathcal{H}$$

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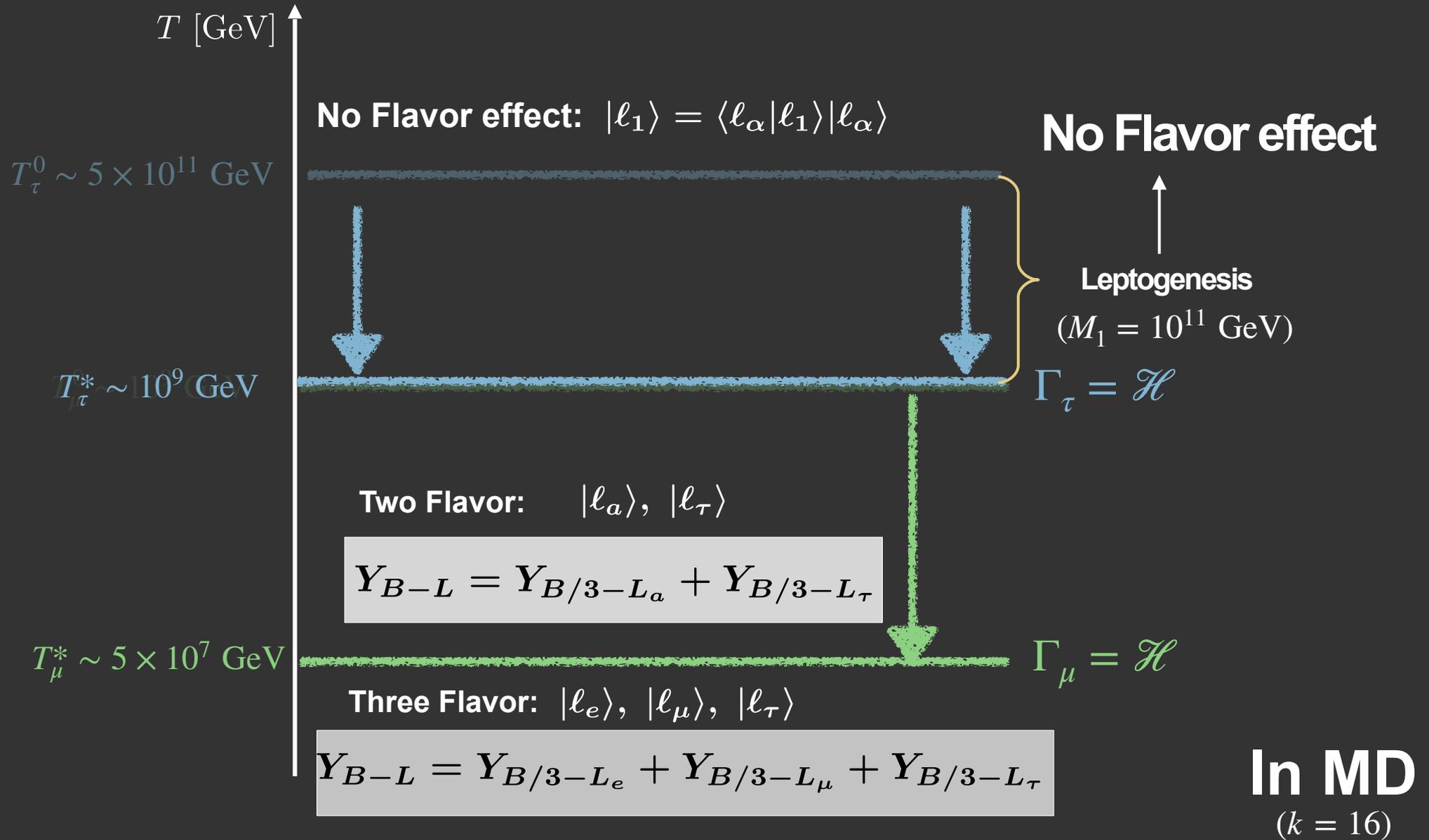
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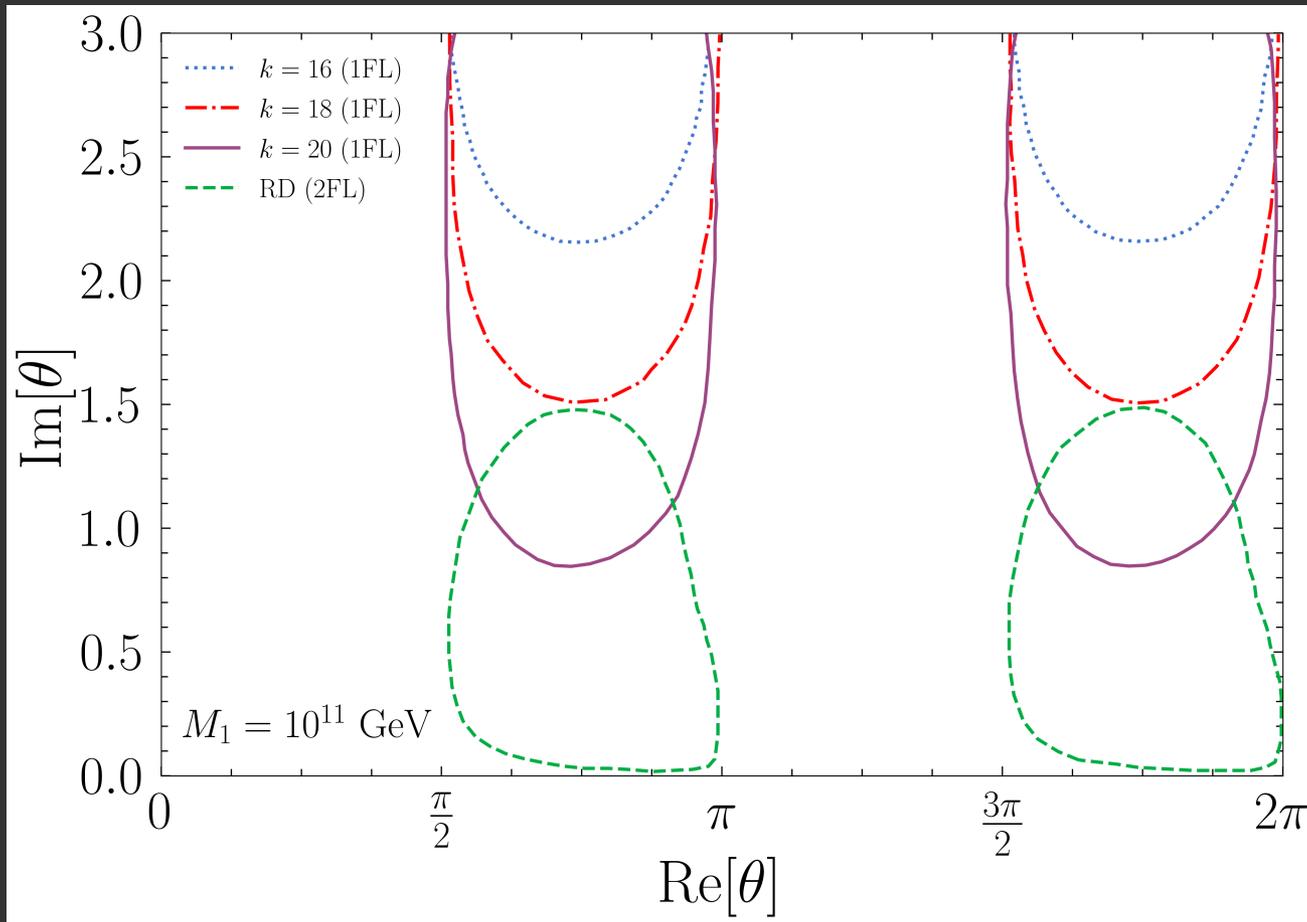
In RD

Modification of Flavor effect

$$\mathcal{L} = Y_{\alpha i}^\nu \bar{\ell}_{L\alpha} \tilde{H} N_i + Y_\alpha (\bar{\ell}_L)_\alpha H (\ell_R)_\alpha + h.c$$



Modification of Baryon asymmetry



$$Y^\nu = -i \frac{\sqrt{2}}{v} U D_{\sqrt{m}} R D_{\sqrt{M}}$$

[Casas, Ibarra, 2001]

↓

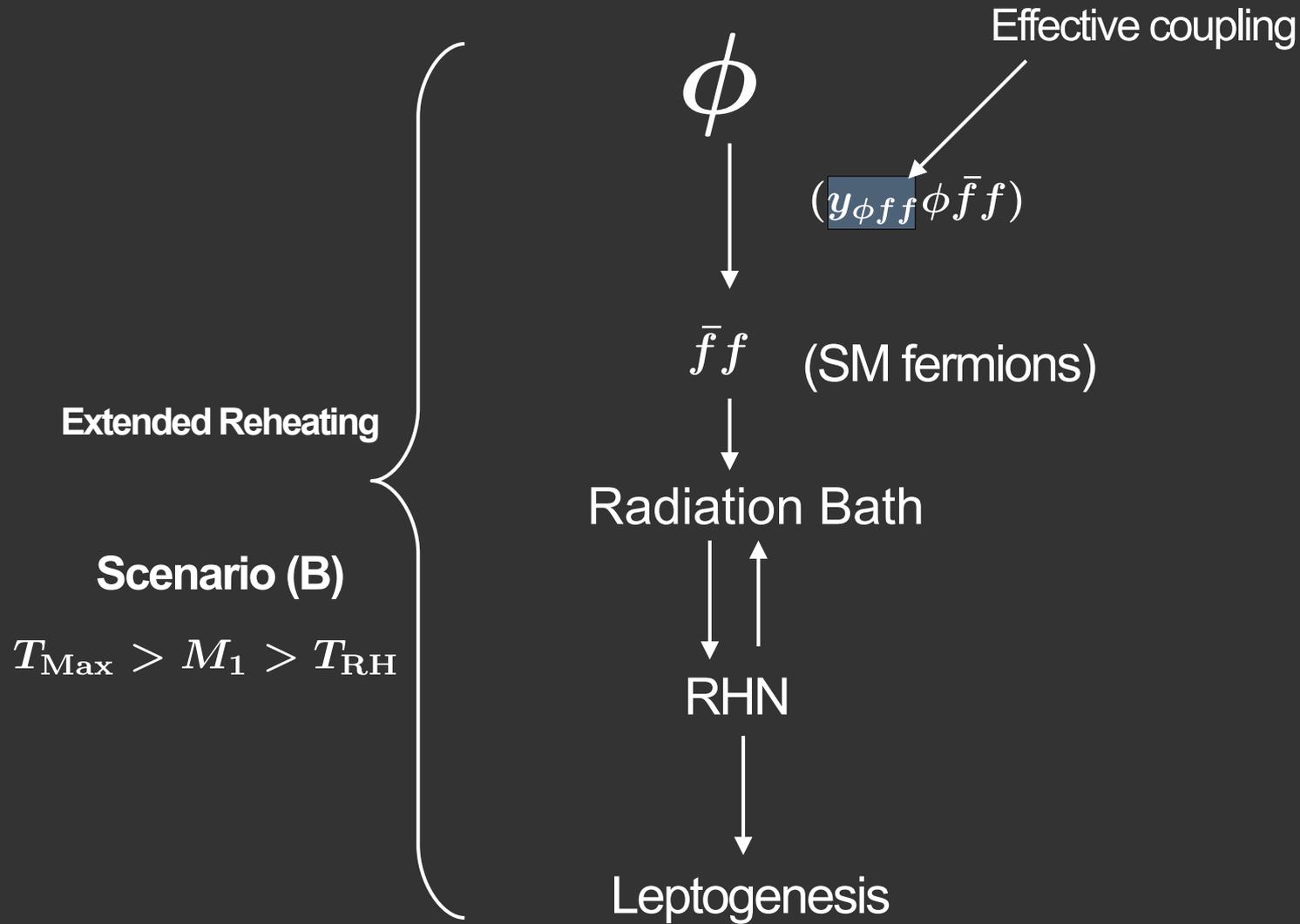
$$R = R(\theta)$$

↙

Complex Angle

- One needs larger Neutrino Yukawa coupling to produce the correct baryon asymmetry.
- Smaller $k(>8)$ values, although reheat the Universe, will not always generate the observed baryon asymmetry.

Setup 2:

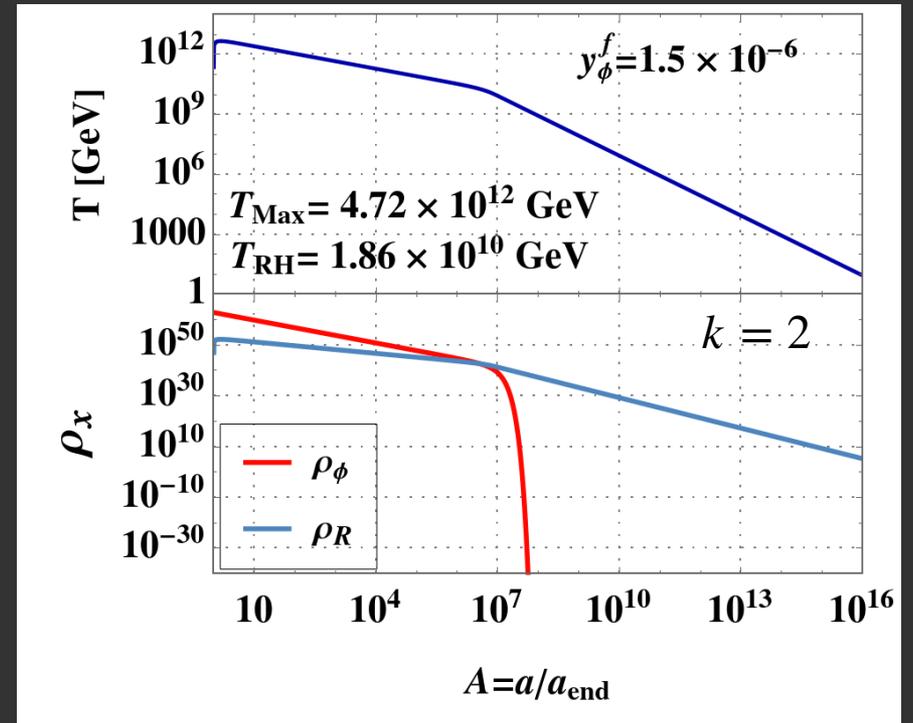


Boltzmann Equation and Temperature:

$$\frac{d(\rho_\phi a^3)}{da} = -\frac{\Gamma_\phi}{\mathcal{H}} \rho_\phi a^2$$

$$\frac{d(\rho_R a^4)}{da} = \frac{a^3}{\mathcal{H}} \Gamma_\phi \rho_\phi$$

$$\mathcal{H}^2 = \frac{\rho_\phi + \rho_R}{3M_P^2}$$



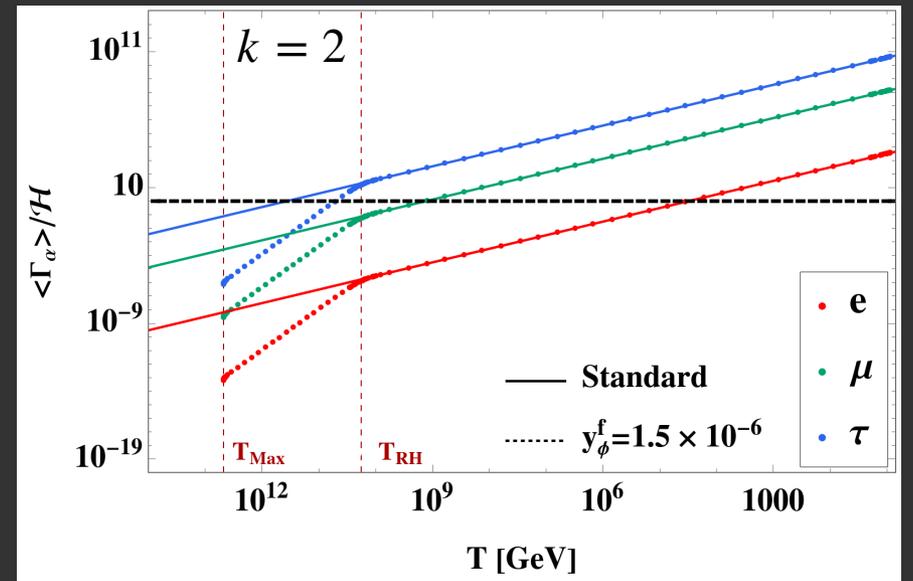
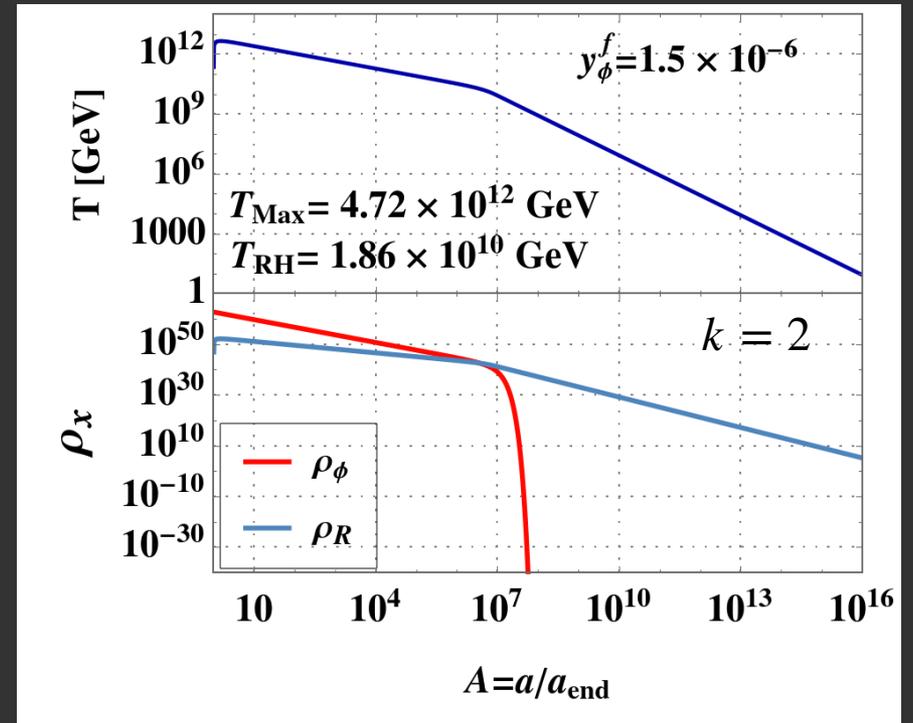
Equilibration of Charged lepton Yukawa:

$$\frac{d(\rho_\phi a^3)}{da} = -\frac{\Gamma_\phi}{\mathcal{H}} \rho_\phi a^2$$

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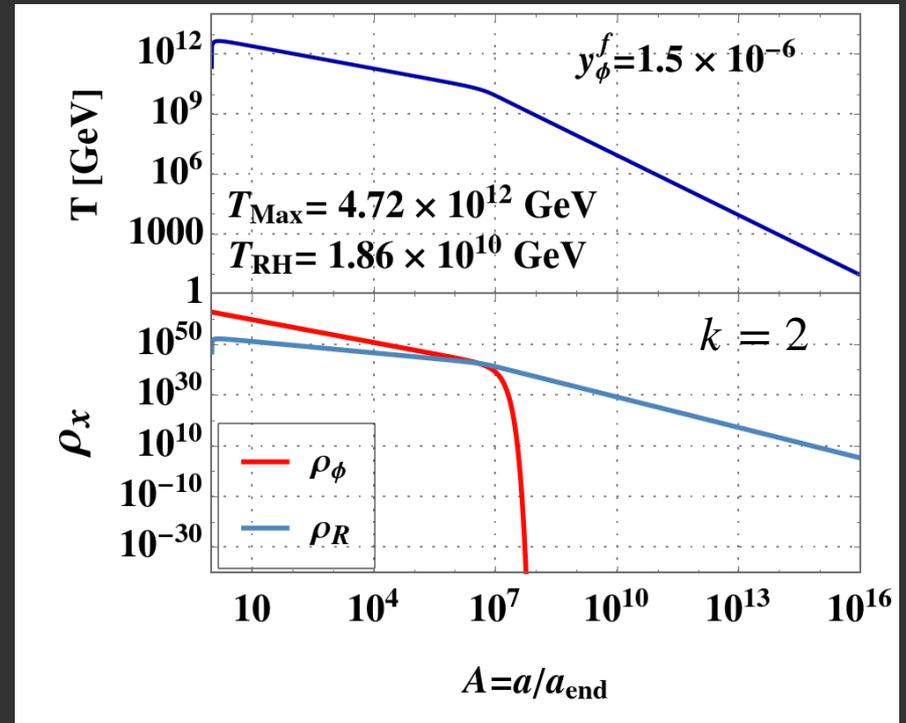


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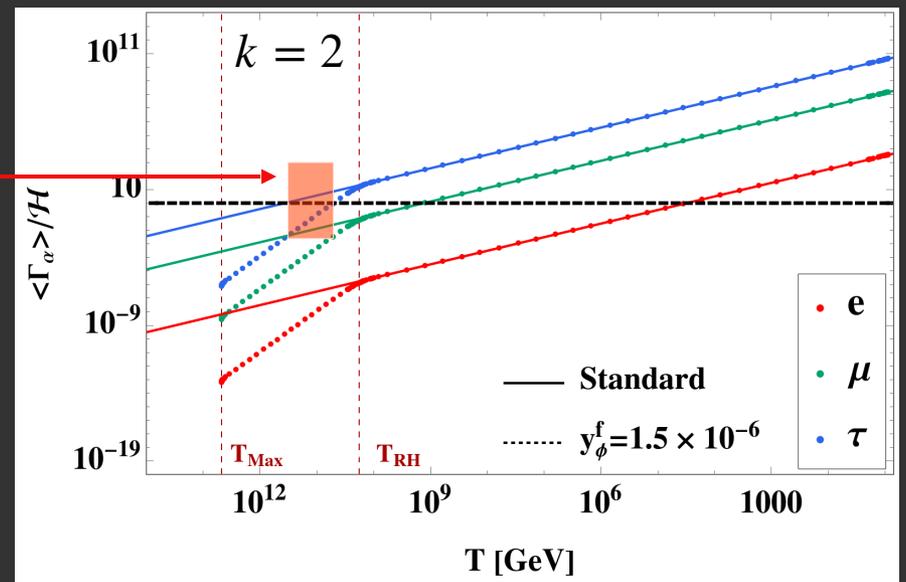
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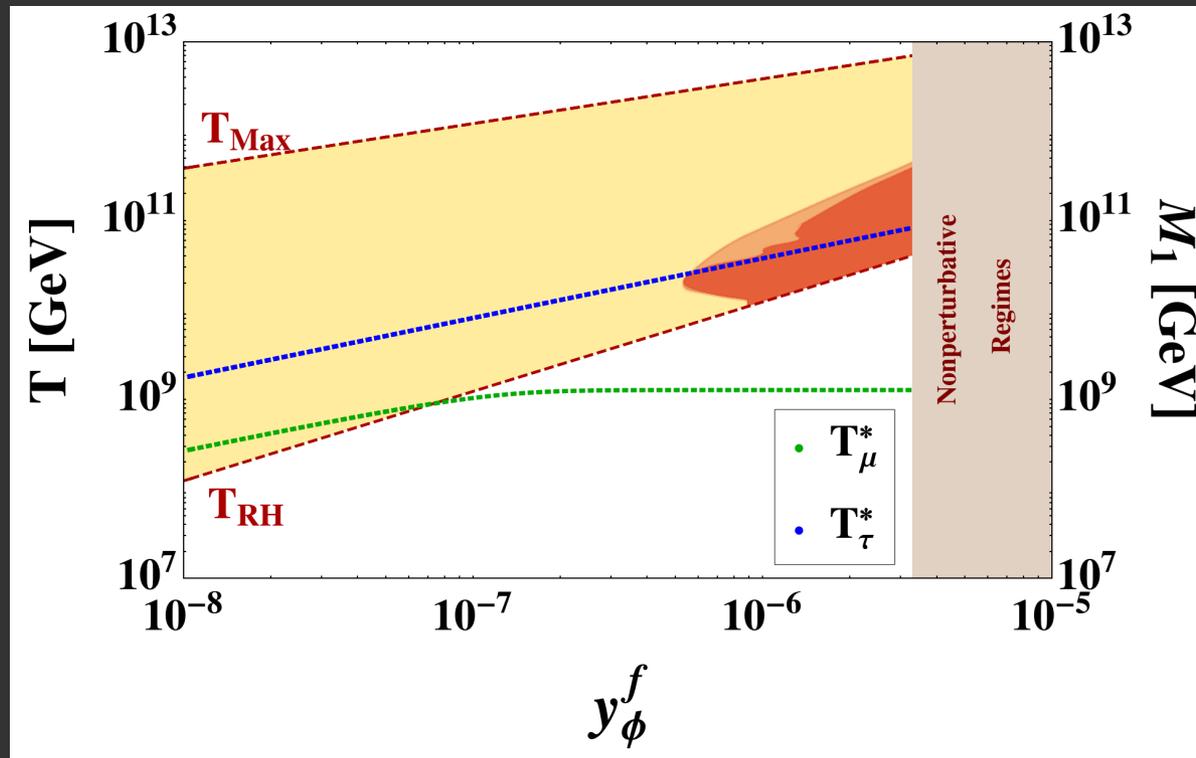
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Delayed equilibration of charged lepton Yukawa interactions

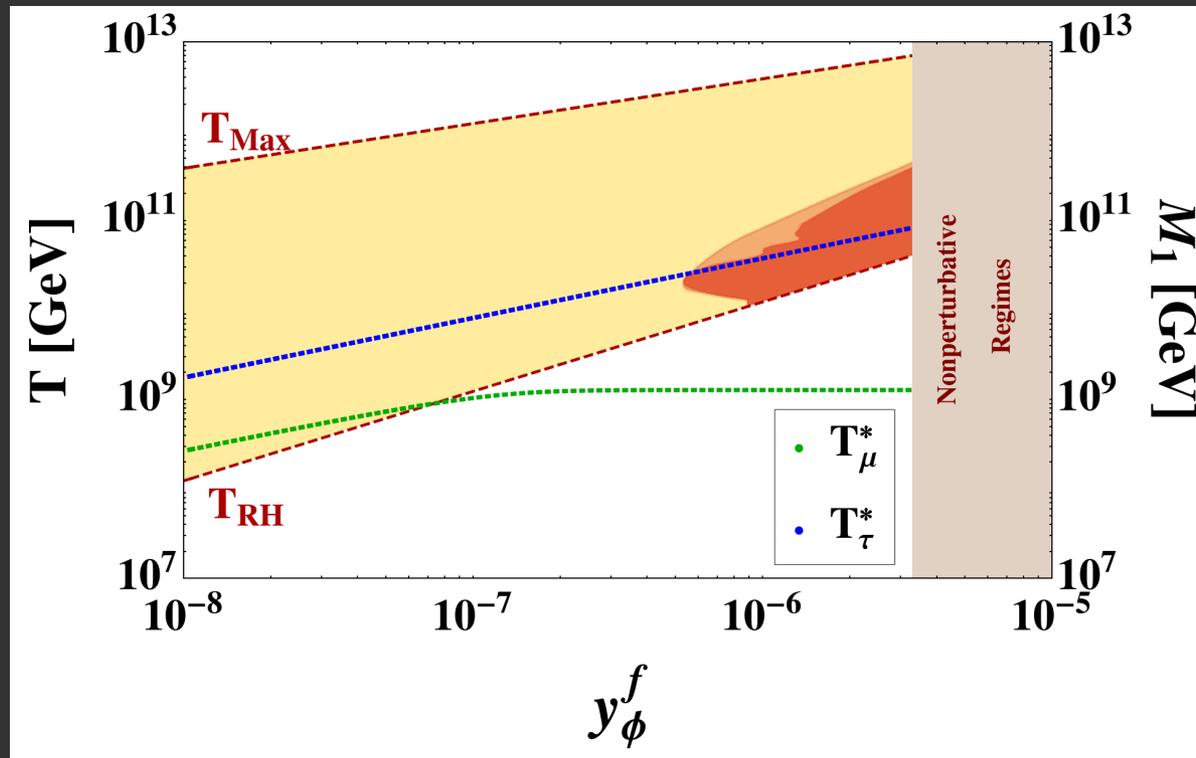


Modification of Baryon asymmetry



- **Prolonged Reheating** was achieved by varying the inflaton-SM fermion coupling.
- Due to the **nontrivial behaviour of Temperature** in between T_{\max} and T_{RH} , **equilibration temperature of charged lepton Yukawa interactions shift** from their standard thermal value.
- **More stringent parameter space** satisfying correct baryon asymmetry is observed due to the **modified flavor effect** as well as **dilution of baryon asymmetry** due to **entropy injection** from inflaton decay.

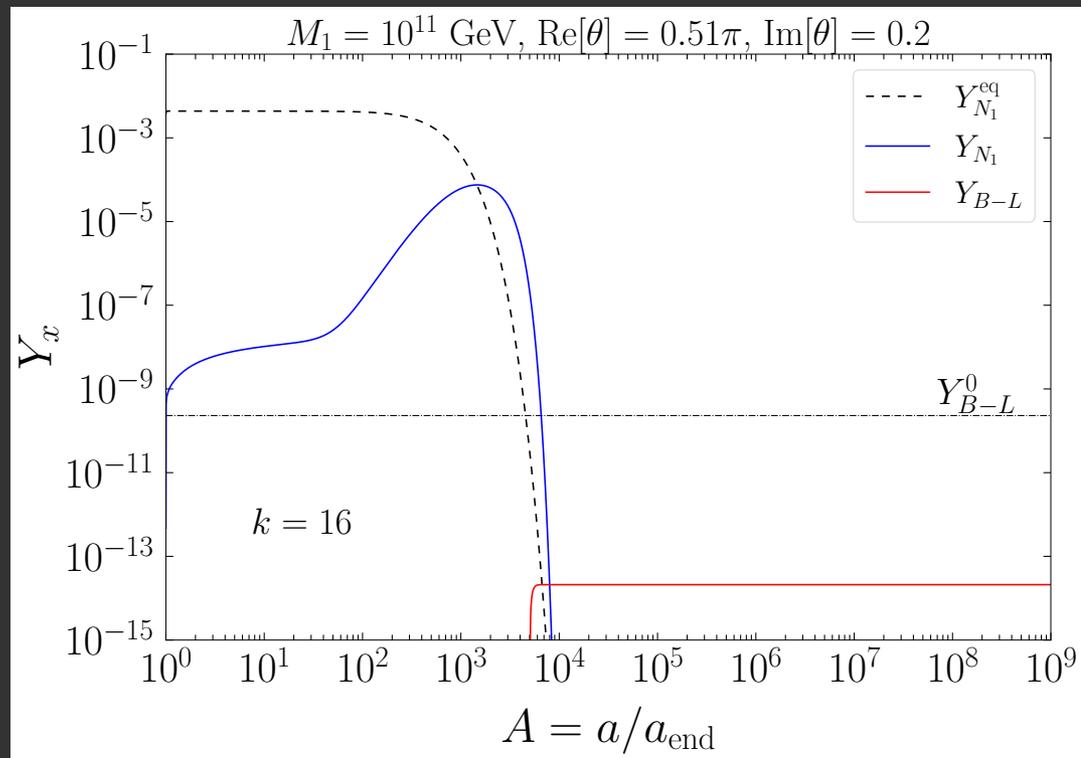
Modification of Baryon asymmetry



- Leptogenesis during reheating phase may not sometimes be flavorful.

Thank You

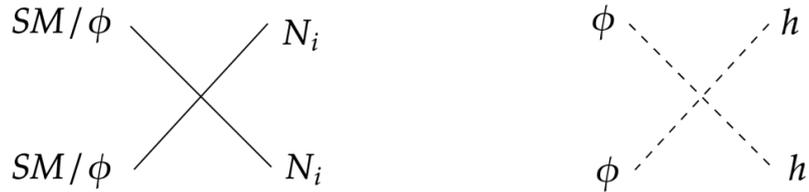
BACK UP



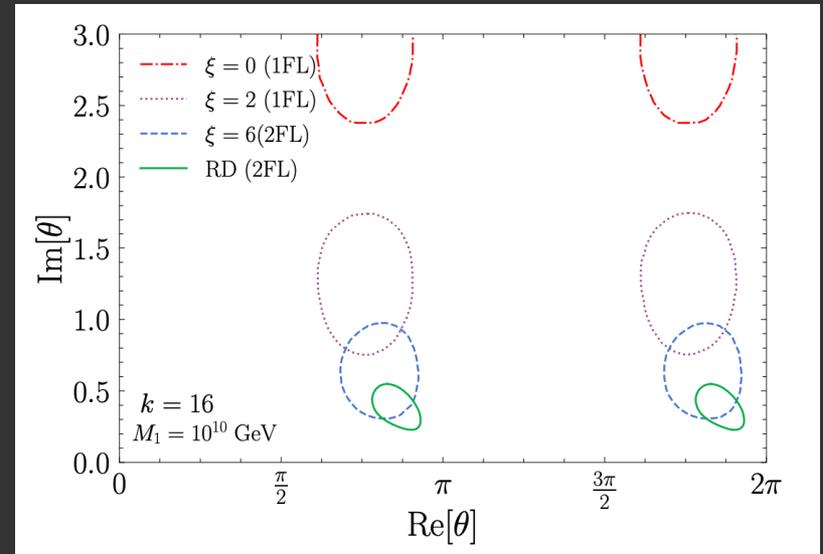
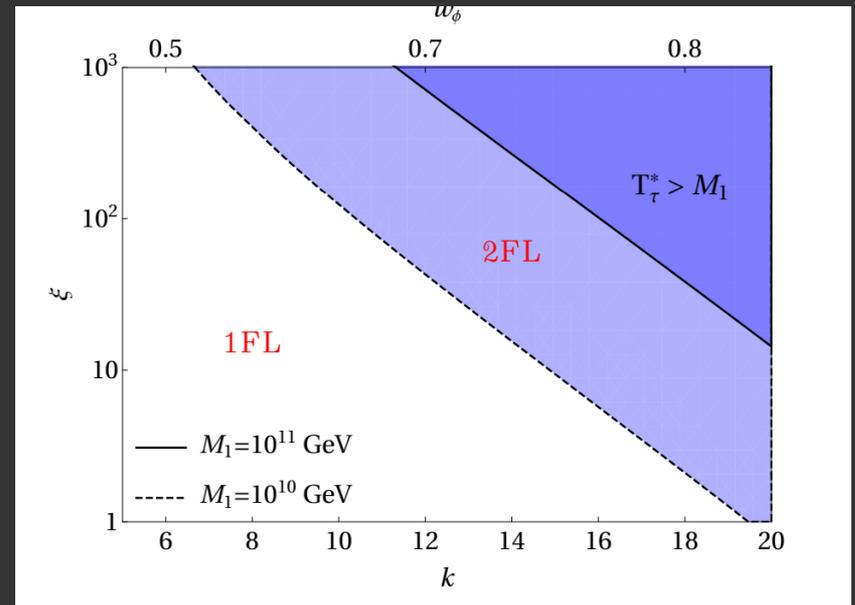
Jordan Frame + Unitary gauge

$$\mathcal{L} \sim (\xi_\phi \phi^2 + \xi_h h^2)R$$

Einstein Frame



negligible effects in RHN production for small ξ .



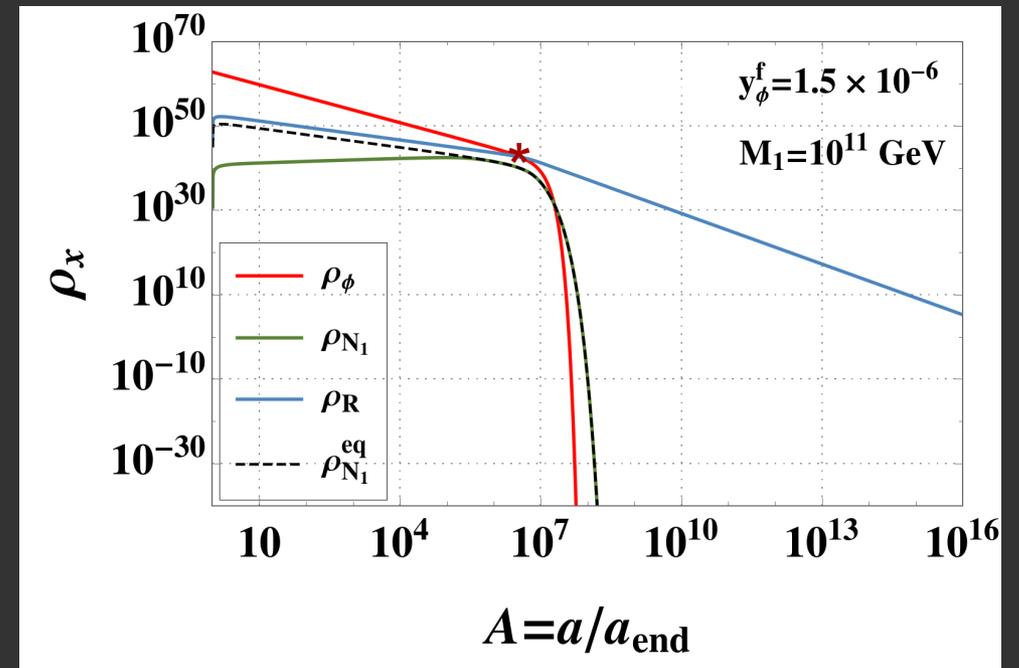
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$$\frac{d(\rho_{N_1} a^3)}{da} = -\frac{\langle \Gamma_{N_1} \rangle a^2}{\mathcal{H}} (\rho_{N_1} - \rho_{N_1}^{\text{eq}})$$

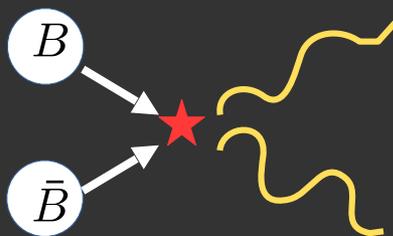
$$\mathcal{H}^2 = \frac{\rho_\phi + \rho_R + \rho_{N_1}}{3M_P^2}$$



Evidence of Anti-matter

From Solar System

To Cluster of Galaxy



$$\frac{n_{\bar{M}}}{n_M + n_{\bar{M}}} \lesssim 10^{-6} \quad \text{Upto } \sim 10^3 \text{ Mpc using EGRET}$$

[Steigman, JCAP 0810:001,2008]

From Cosmic Ray

Cosmic Ray anti-proton search by
PAMELA, AMS

$$\frac{\Phi_P^-}{\Phi_P} \lesssim 10^{-5}$$

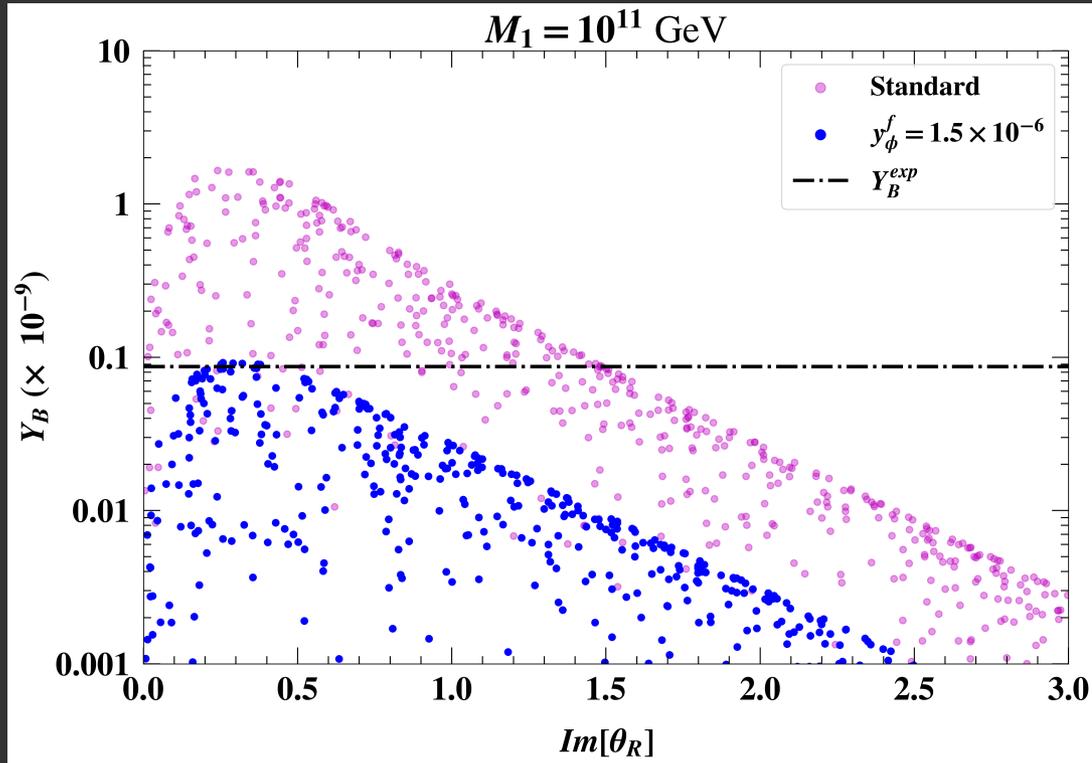
Explained by other
astrophysical processes

[O. Adriani et al., PRL 105, 121101 (2010)]

No evidence of anti-matter structure

Modification of Baryon asymmetry

$$\left. \begin{aligned}
 \frac{d(\rho_\phi a^3)}{da} &= -\frac{\Gamma_\phi}{\mathcal{H}} \rho_\phi a^2 \\
 \frac{d(\rho_R a^4)}{da} &= \frac{a^3}{\mathcal{H}} \Gamma_\phi \rho_\phi + \frac{a^3}{H} \langle \Gamma_{N_1} \rangle (\rho_{N_1} - \rho_{N_1}^{\text{eq}}) \\
 \frac{d(\rho_{N_1} a^3)}{da} &= -\frac{\langle \Gamma_{N_1} \rangle a^2}{\mathcal{H}} (\rho_{N_1} - \rho_{N_1}^{\text{eq}})
 \end{aligned} \right\} + \frac{d(n_{B-L} a^3)}{da} = -\frac{\langle \Gamma_{N_1} \rangle a^2}{\mathcal{H}} \left[\frac{\varepsilon_\ell}{M_1} (\rho_{N_1} - \rho_{N_1}^{\text{eq}}) + \frac{n_{N_1}^{\text{eq}}}{2n_\ell^{\text{eq}}} n_{B-L} \right]$$



Matter-Antimatter asymmetry

[Leptogenesis ← → Origin of Neutrino Mass]

decay of RHN: $N \rightarrow \ell H$ ($Y_\nu \bar{\ell} \tilde{H} N$)

Flavor Leptogenesis

Depend on when **charged lepton Yukawa of different flavors comes to equilibrium**

$$T_{\tau R}^0 \sim 5 \times 10^{11} \text{ GeV}$$

$$T_{\mu R}^0 \sim 10^9 \text{ GeV}$$

$$T_{e R}^0 \sim 5 \times 10^4 \text{ GeV}$$

Prolonged Reheating

If M_1 satisfy: $T_{\max} > M_1 > T_{RH}$



- 1) Effect on equilibration temperature of charged lepton Yukawa
- 2) Effect on flavor Leptogenesis

Should be generated after inflation

[Post inflationary epoch]

Perturbative Reheating: instantaneous/
extended

Universe reaches a maximum temperature T_{\max}

Reheating temperature T_{RH}

(onset of radiation domination)

$T_{\max} - T_{RH}$:

May differ by several orders of magnitude