

# Eccentricity and $v_2$ in proton-proton collisions at the LHC

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in collaboration with

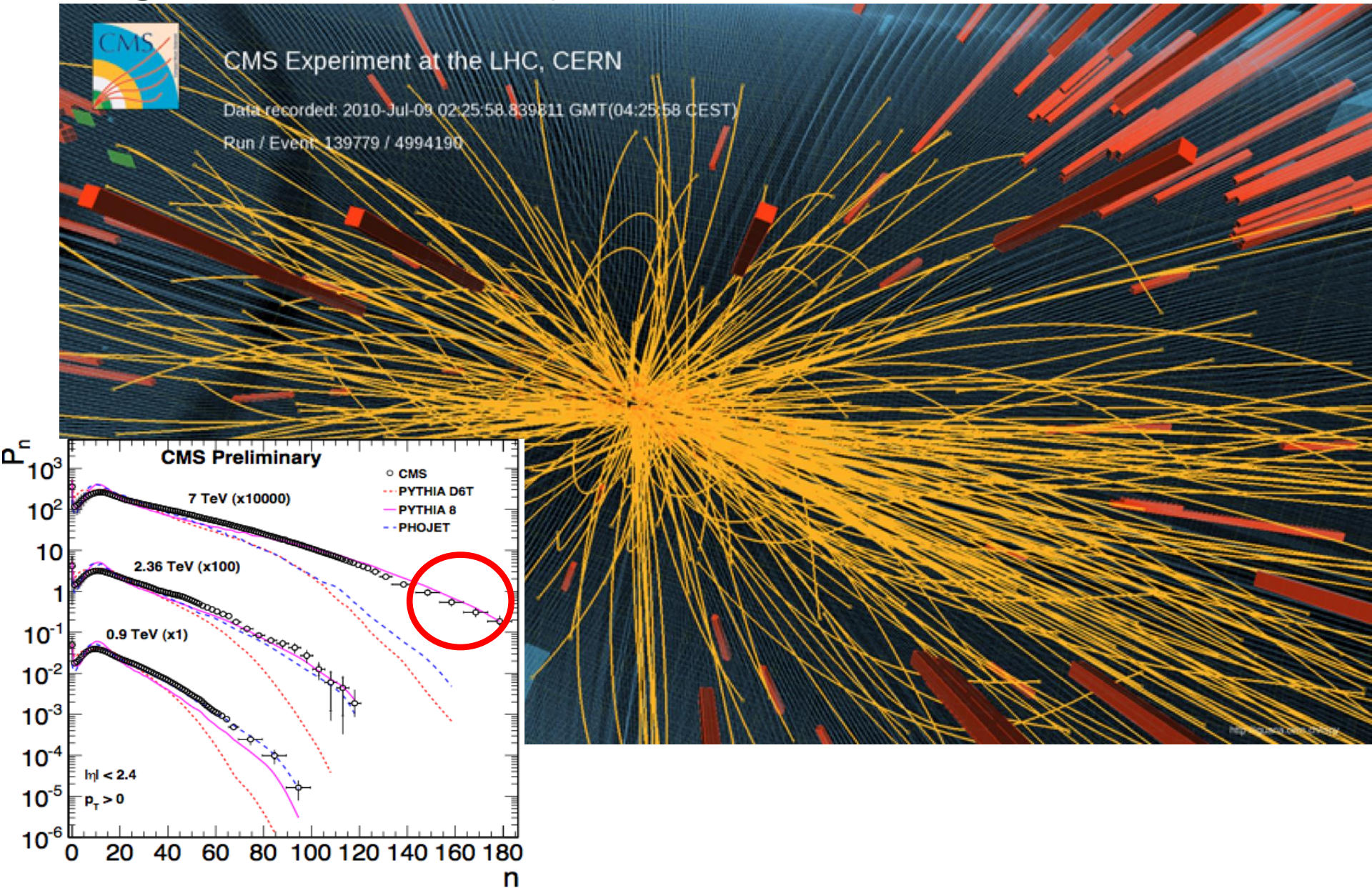
E. Avsar, C. Flensburg, J.-Y. Ollitrault, T. Ueda

Physics Letters B702, 394 (2011);  
1106.4356 [hep-ph] (Quark Matter proceedings)

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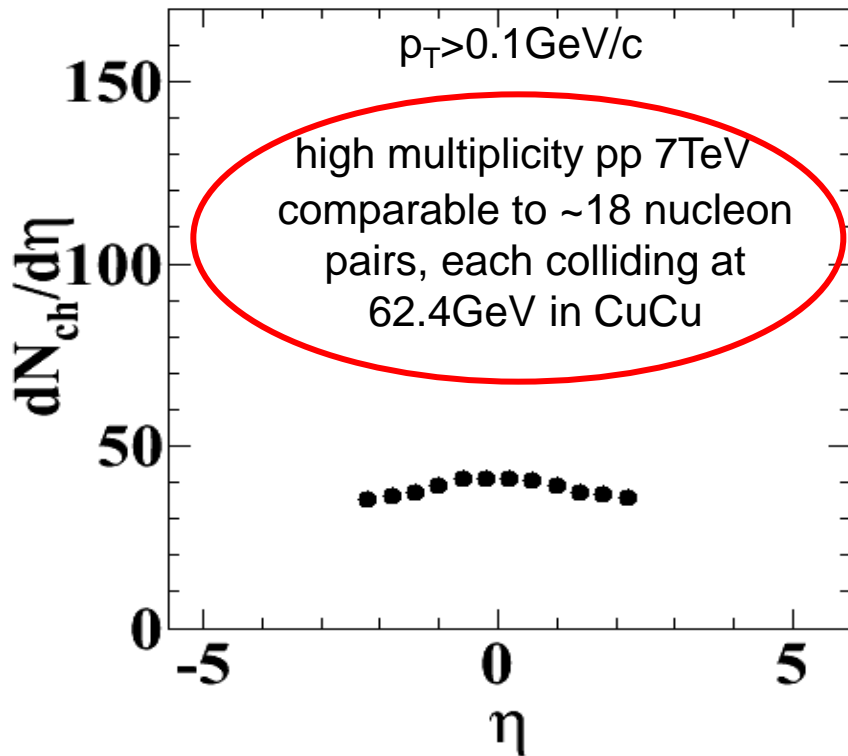
- High-multiplicity pp events at the LHC
- Flow in pp?
- DIPSY
- Eccentricity and  $v_2$  in pp

# High-multiplicity pp events at the LHC

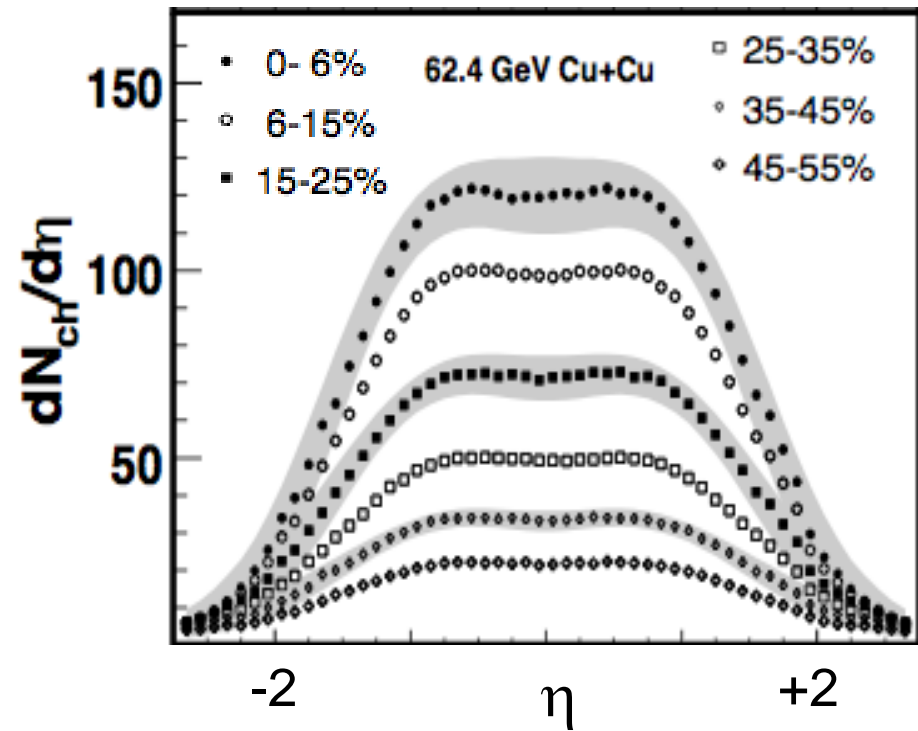


# Like an AA collision !

**CMS**



**PHOBOS**



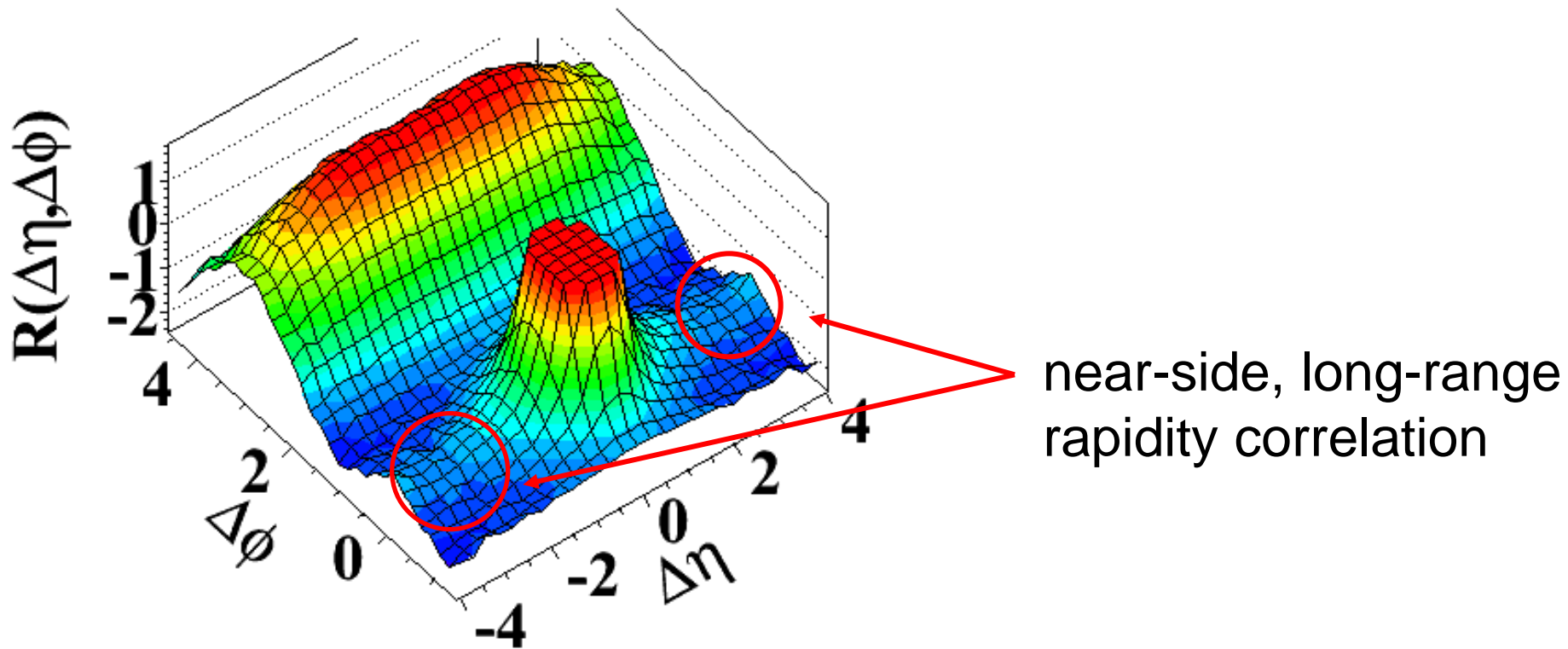
Phenomena usually discussed in the context of nucleus collisions may be observed in proton collisions !



# Ridge in pp

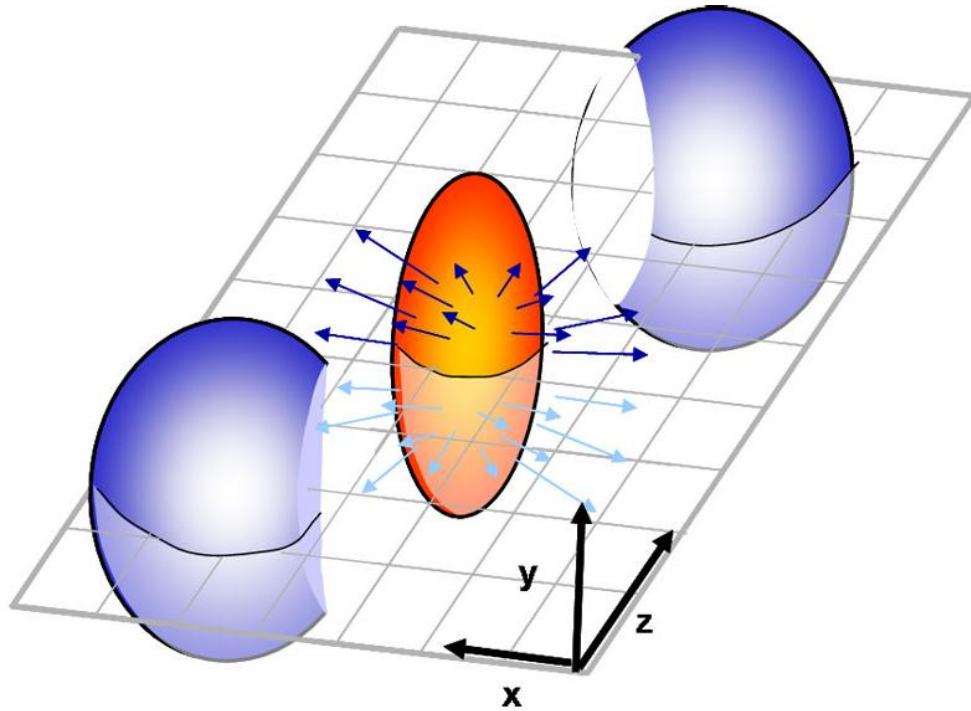
CMS Collaboration, arXiv:1009.4122

(d)  $N > 110$ ,  $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



First **un**expected result in pp at the LHC !  
Possible collective effects in pp?

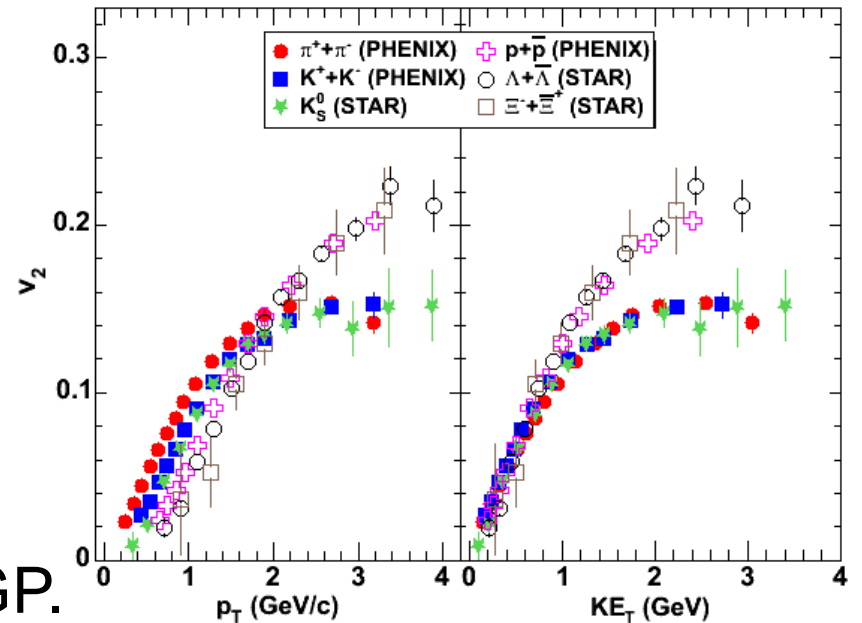
# Elliptic flow $v_2$



$$\frac{dN}{d\phi} \propto 1 + \underline{2v_2} \cos 2\phi$$

$$v_2 \propto \epsilon \quad \text{eccentricity}$$

Hallmark of collective expansion,  
widely seen as a signal of the QGP.



# Elliptic flow in pp : previous attempts

**Fixed distribution** (Woods-Saxon, Hard Sphere, Gaussian....)

Luzum, Romatschke 0901.4588

Prasad, Roy, Chattopadhyay 0910.4844

d'Enterria, et al. 0910.3029

Bozek 0911.2392

Ortona, Denicol, Mota, Kodama, 0911.5158

**Random distribution** (Flux tube model, Hot spot model)

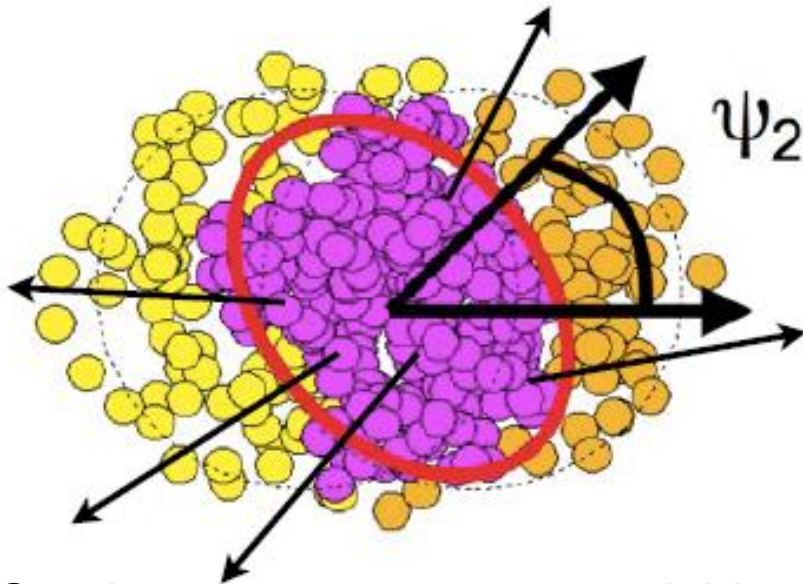
Bautista, Cunqueiro, de Deus, Pajares 0905.3058

Pierog, Porteboeuf, Karpenko, Werner, 1005.4526

Casalderrey-Solana, Wiedemann 0911.4400

# Participant eccentricity

Event plane may be different from the reaction plane.



$$\epsilon_{\text{part}} = \frac{\sqrt{(\sigma_y^2 - \sigma_x^2)^2 + 4\sigma_{xy}^2}}{\sigma_y^2 + \sigma_x^2}$$

Can be nonzero even at vanishing impact parameter due to fluctuations.

Important because high-multiplicity pp events mostly come from central collisions.

AA  $\rightarrow$  fluctuation of nucleons

pp  $\rightarrow$  fluctuation of small-x gluons



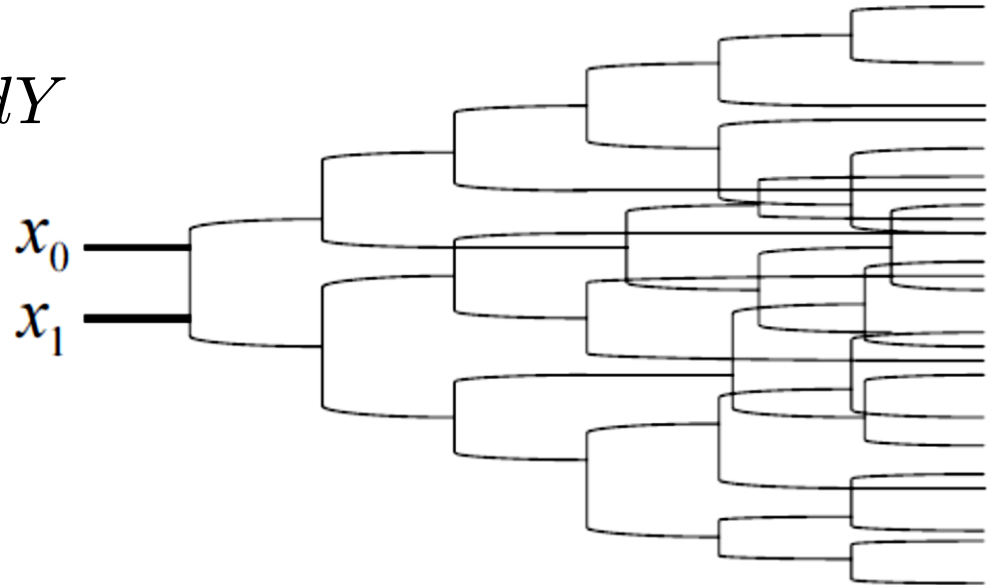
# QCD dipole model

Mueller (1994~)

Coordinate space formulation of the BFKL equation

Probability of gluon (dipole) splitting

$$dP = \bar{\alpha}_s \frac{(\vec{x} - \vec{y})^2}{(\vec{x} - \vec{z})^2 (\vec{z} - \vec{y})^2} d^2 \vec{z} dY$$



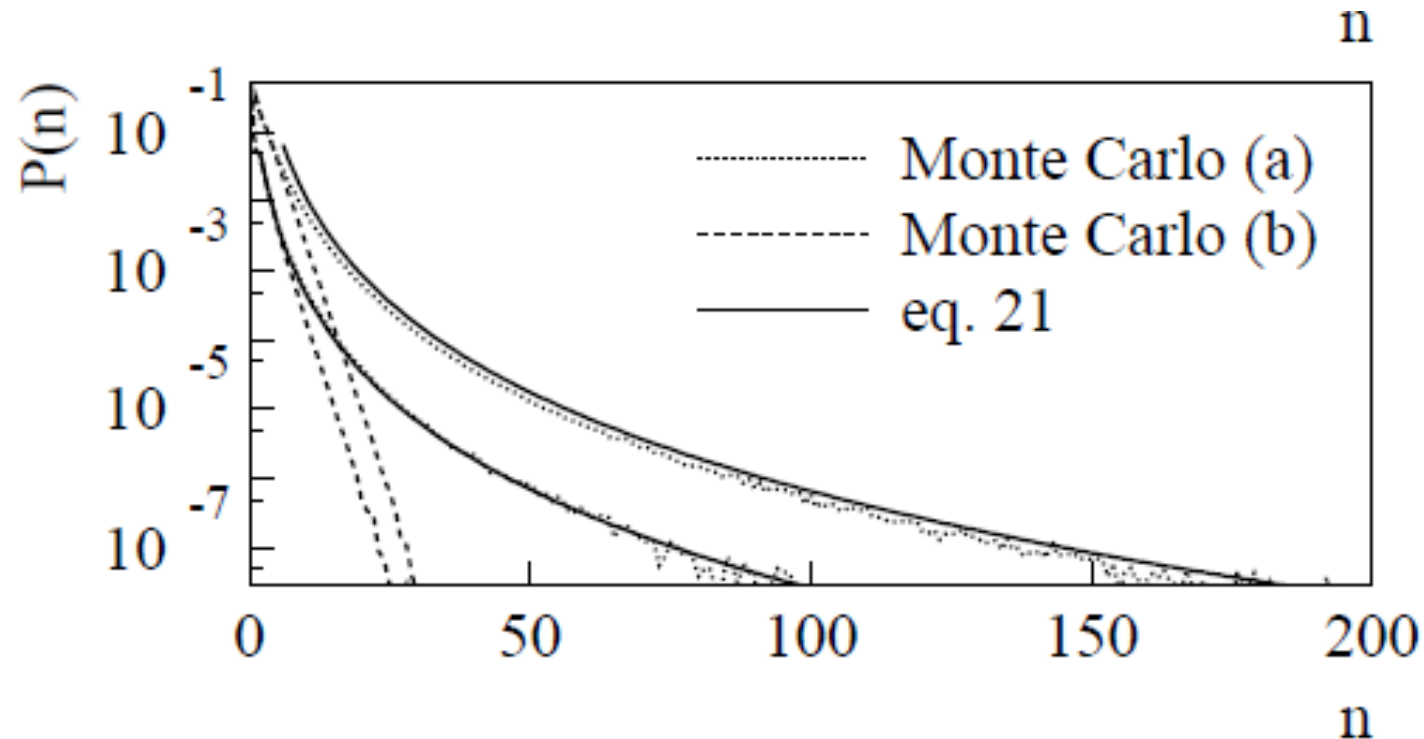
- **Very strong fluctuation** in the gluon multiplicity
- **Very strong correlation** in impact parameter space

Salam (1995)  
YH, Mueller (2007)  
Avsar, YH (2008)

# Gluon number fluctuation

Probability distribution of the number of gluons in the dipole model

Salam (1995)



# DIPSY

Full-fledged Monte Carlo event generator for pp based on the dipole model.

Flensburg, Gustafson, Lonnblad, arXiv:1103.4321  
extension of Avsar, Gustafson, Lonnblad (2005~)

## Featuring:

BFKL

Running coupling (NLO)

Energy conservation ( $N^n$ LO)

Saturation effects

Confinement effects

Multiple scattering,

Underlying events,

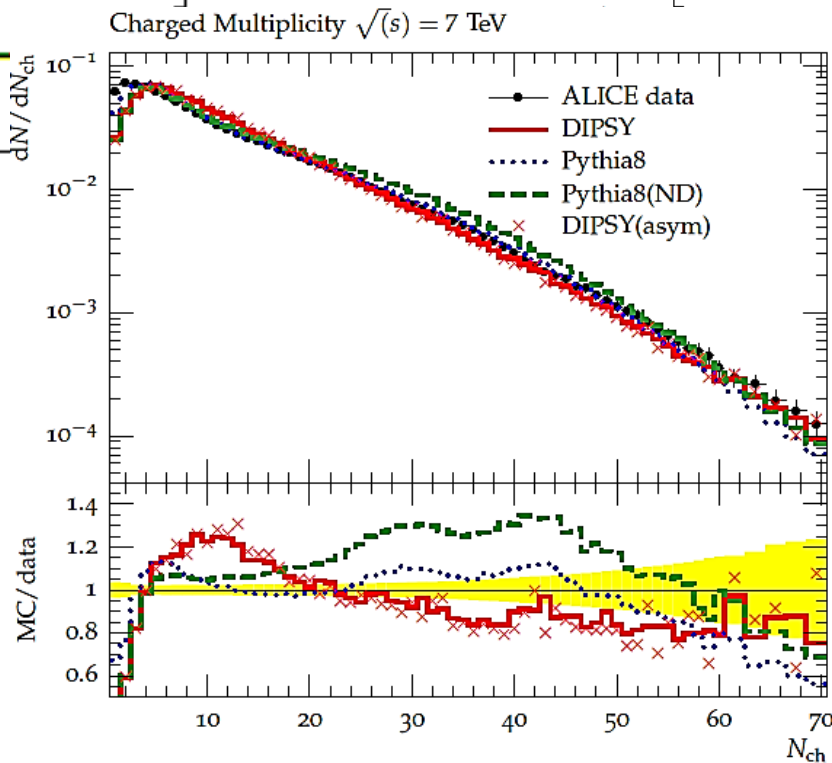
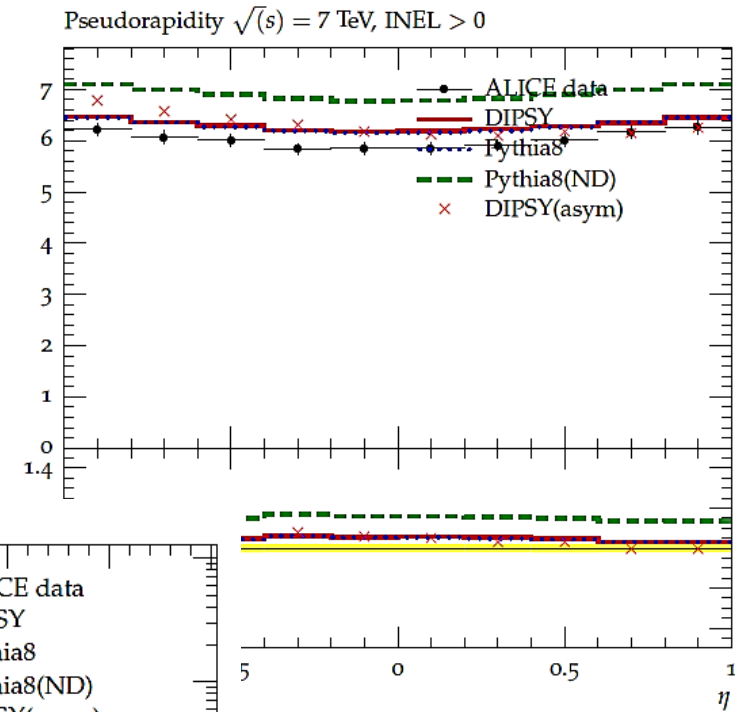
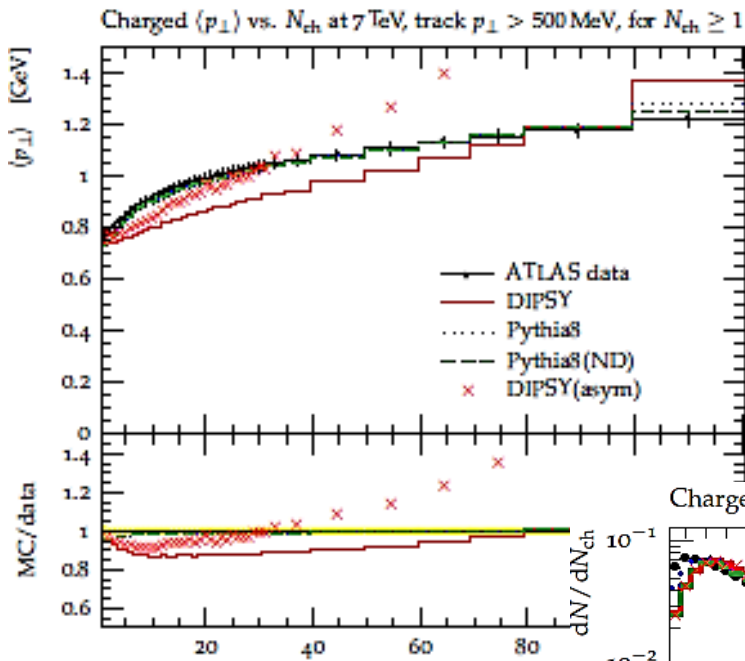
Parton shower (ARIADNE)

Hadronization (Pythia)

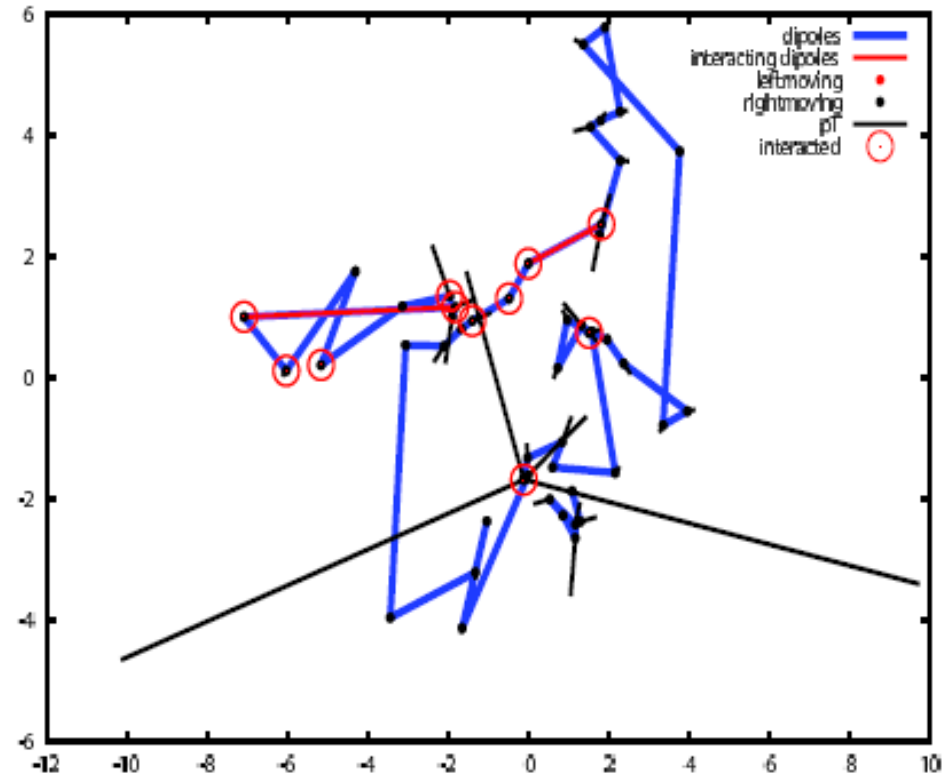
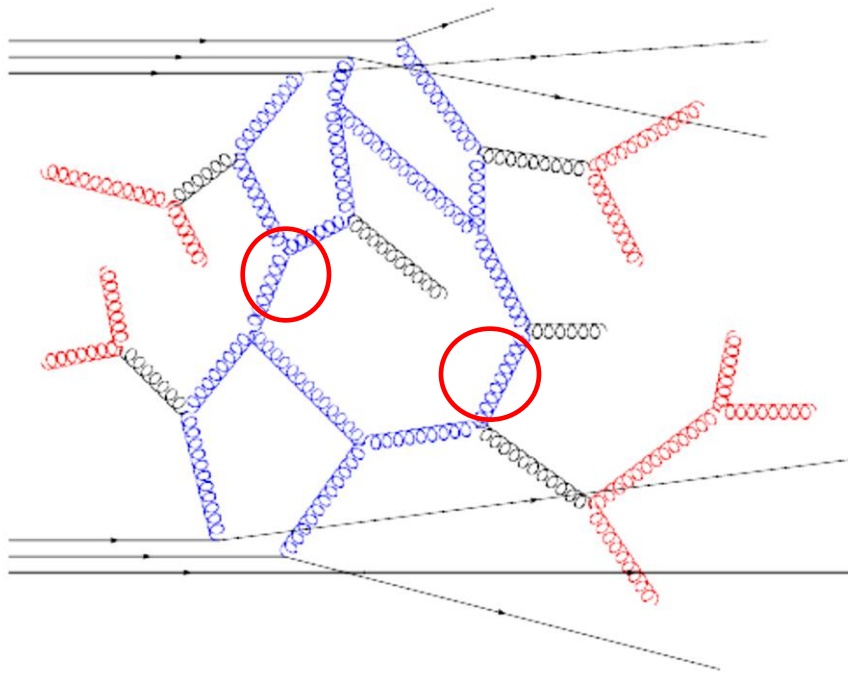
“Lund gang”

Energy dependence is a prediction. No ad hoc retuning of parameters at different energies.

# Some sample results from DIPSY @ 7TeV



# Deconstructing high-multiplicity events



High-multiplicity pp events

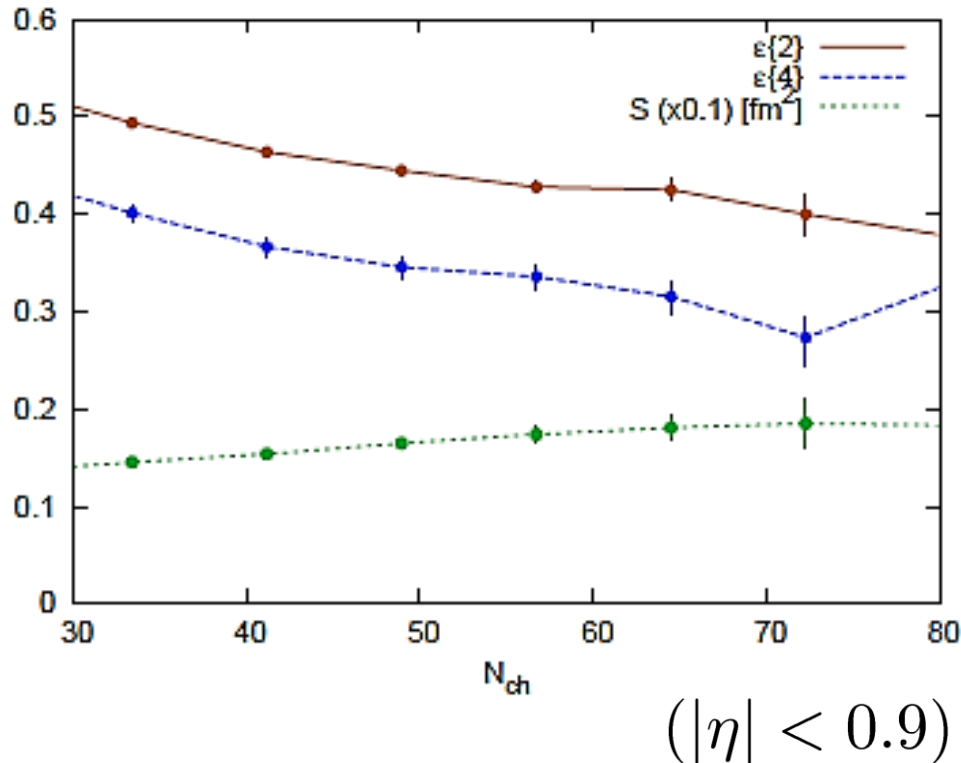
= Upward fluctuation in the gluon number in proton's w.f.

+ Multiple (more than 10) parton-parton interactions



# Eccentricity in pp at 7 TeV

Shape of the area occupied by the “liberated” gluons.



$$\epsilon_{\text{part}} = \frac{\sqrt{(\sigma_y^2 - \sigma_x^2)^2 + 4\sigma_{xy}^2}}{\sigma_y^2 + \sigma_x^2}$$

$$\epsilon\{2\} = \sqrt{\langle \epsilon_{\text{part}}^2 \rangle}$$

$$\epsilon\{4\} = \left( 2\langle \epsilon_{\text{part}}^2 \rangle^2 - \langle \epsilon_{\text{part}}^4 \rangle \right)^{\frac{1}{4}}$$

# Comparison with Pb-Pb

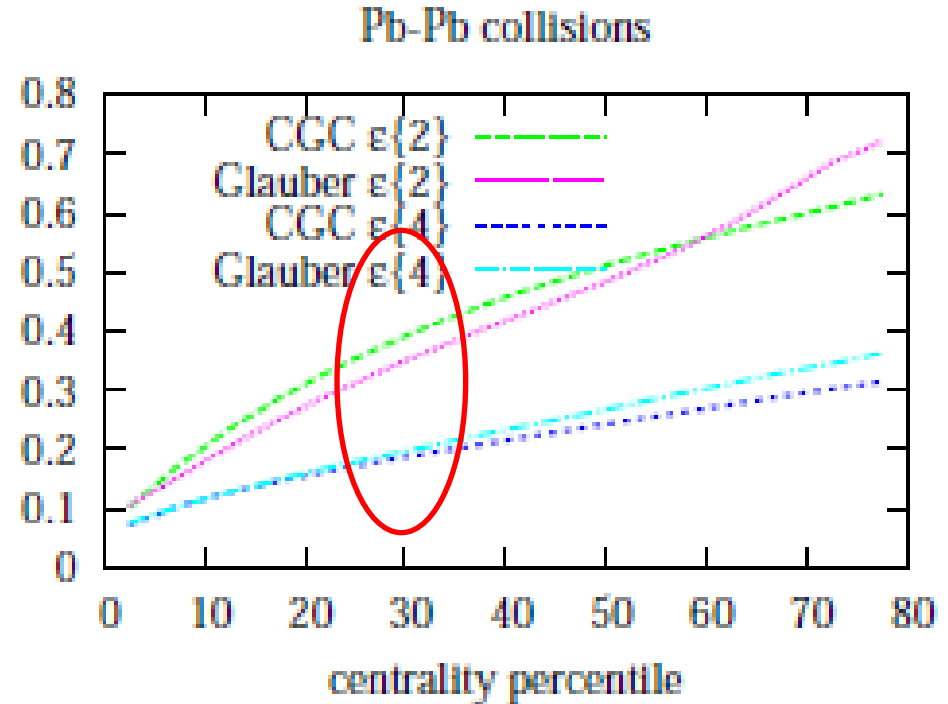
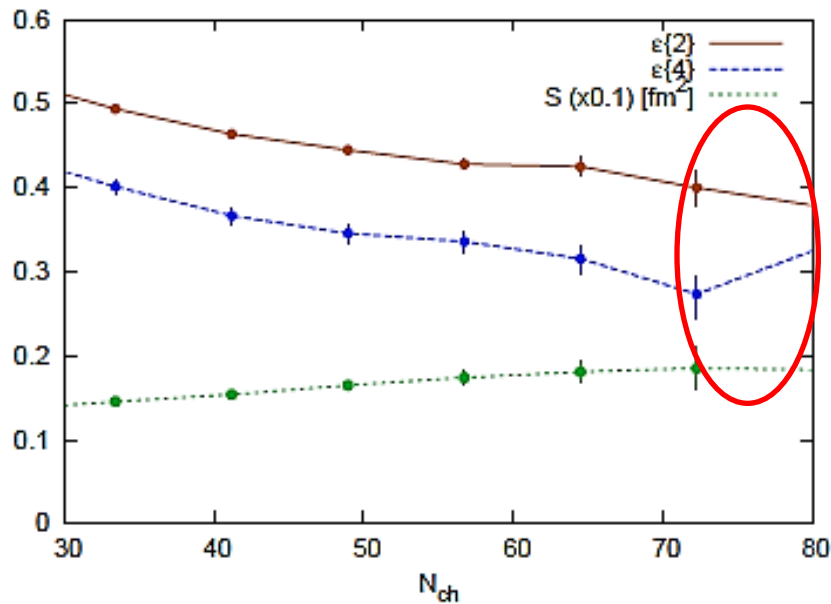


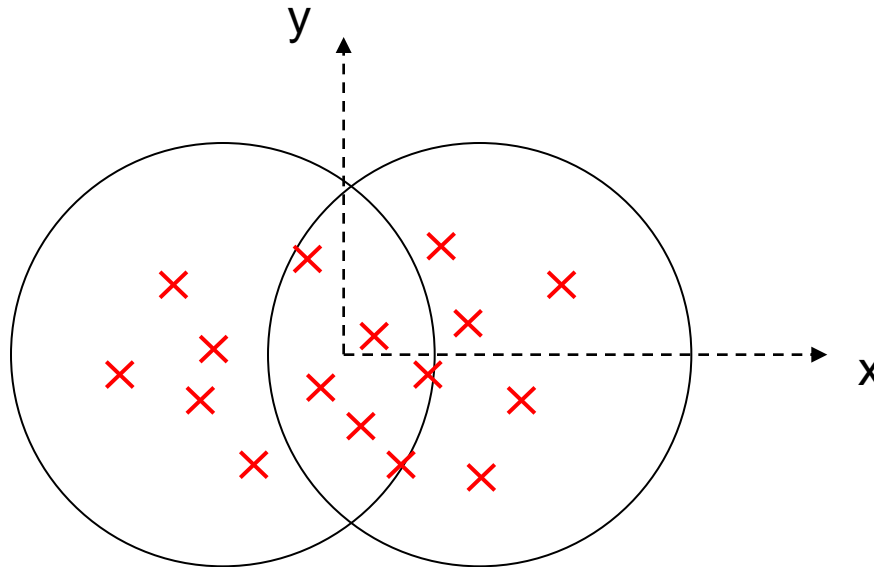
Figure by M. Luzum

Comparable to 30% central Pb-Pb collisions

# Nature of eccentricity in pp

Conventional definition of the eccentricity at fixed b

$$\epsilon_s = \frac{\sigma_y^2 - \sigma_x^2}{\sigma_y^2 + \sigma_x^2} \quad \text{is negative !}$$



Nominal “overlapping region” is a poor guide in pp.


$$\epsilon \longrightarrow v_2$$

Empirical relation between the eccentricity and  $v_2$ .

Drescher, Dumitru, Gombeaud, Ollitrault. (2007)

$$v_2\{2\} = \epsilon\{2\} \left(\frac{v_2}{\epsilon}\right)_{hydro} \frac{1}{1 + \frac{\lambda}{K_0} \frac{\langle S \rangle}{dN/d\eta}}$$

←  $\sim \frac{1}{(\text{density})}$   
 taking care of  
 incomplete equilibration

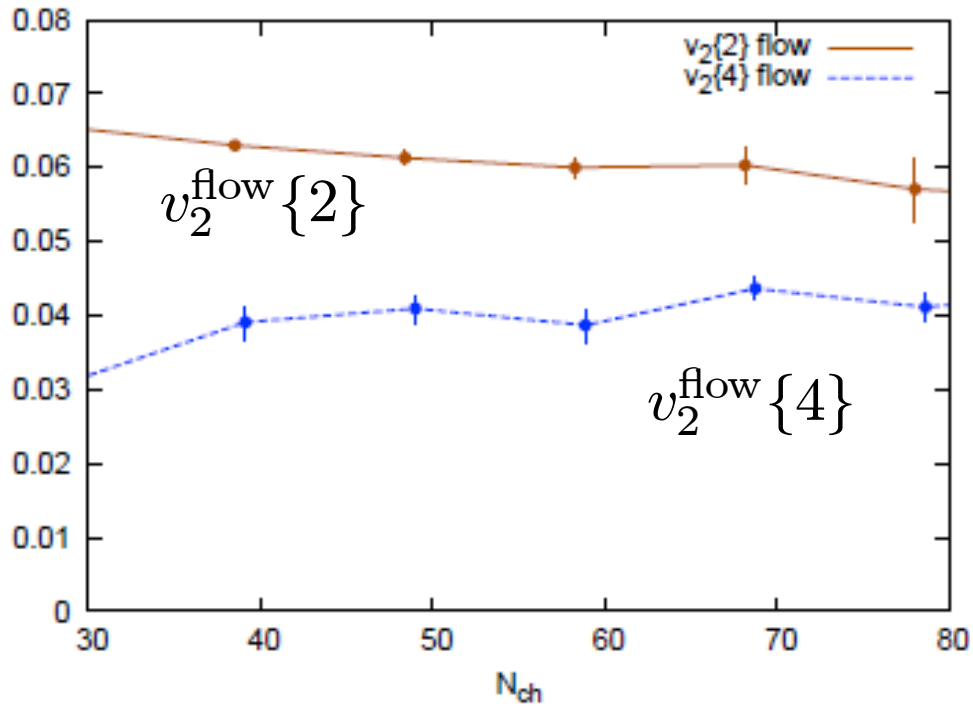


$$(v_2\{2\})^2 = \left(\frac{v_2}{\epsilon}\right)_{hydro}^2 \left\langle \frac{\epsilon_{part}^2}{\left(1 + \frac{\lambda}{K_0} \frac{S}{dN/d\eta}\right)^2} \right\rangle$$

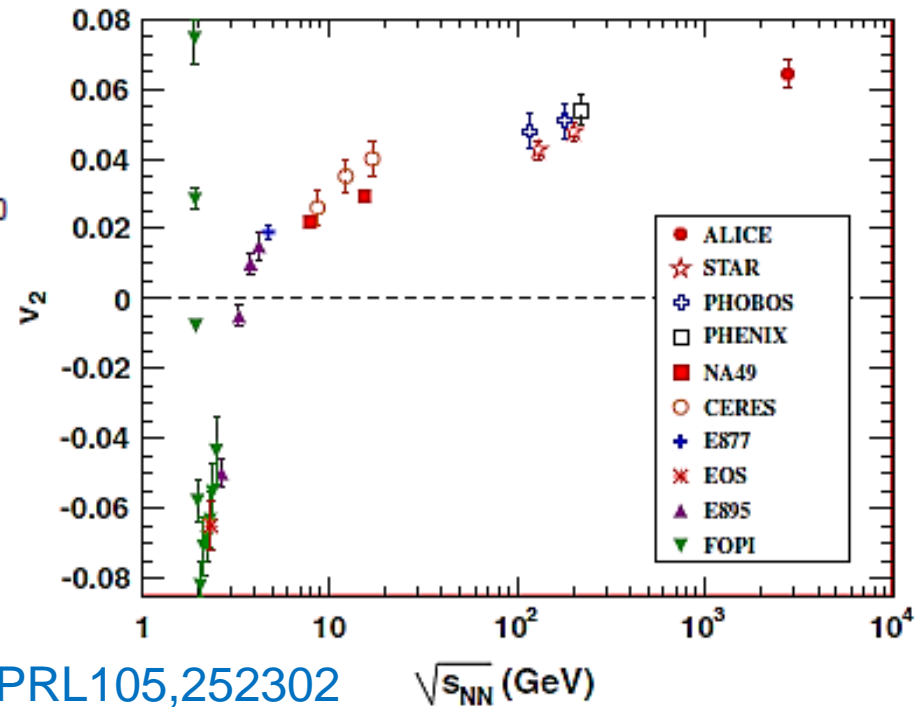
...and a similar relation between  $\epsilon\{4\}$  and  $v_2\{4\}$

In order to obtain large  $v_2$ , a single event has to be **both** elliptic in shape and have high density.

# Elliptic flow at 7 TeV



~ 6%  
comparable to  
AA at LHC, RHIC





# “Nonflow” effect

$v_2$  from n-particle angular correlation


$$v_2^2\{2\} = \langle \{ \cos(2(\phi_i - \phi_j)) \} \rangle,$$

$$v_2^4\{4\} = 2(v_2\{2\})^4 - \langle \{ \cos(2(\phi_i + \phi_j - \phi_k - \phi_l)) \} \rangle$$

$$(v_2\{n\})^n = v_2^n + \delta_n$$

“flow”      “nonflow”

jets, hard scattering,  
resonance decay,  
BFKL evolution,  
color connection, etc.

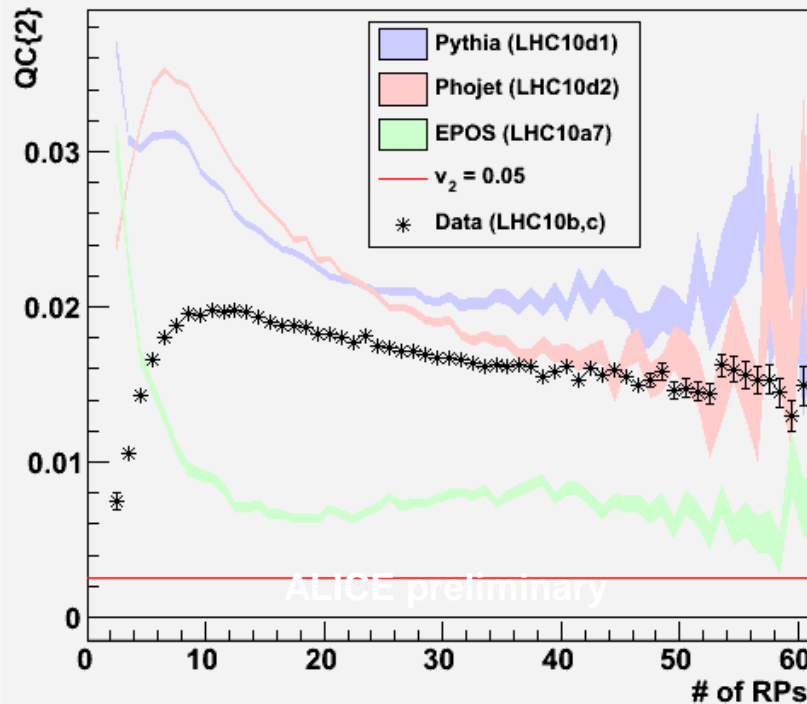


In AA, it is relatively innocuous  $\delta_n \sim \left( \frac{1}{N_{ch}} \right)^{n-1}$

In pp, it could be very large...

# ALICE data for $v_2\{2\}$

Bilandzic, talk at QCHS IX; AIP Conf. Proc. (2011)



$$\langle \cos 2\phi_{ij} \rangle = v_2^2 + \delta_2$$

“flow”    “nonflow”

$$\sqrt{\langle \cos 2\phi_{ij} \rangle} \approx 0.14$$

Large nonflow contribution

dominate over the flow contribution....  $v_2^{\text{flow}}\{2\} \approx 0.06$

→ Necessary to go to higher cumulants.

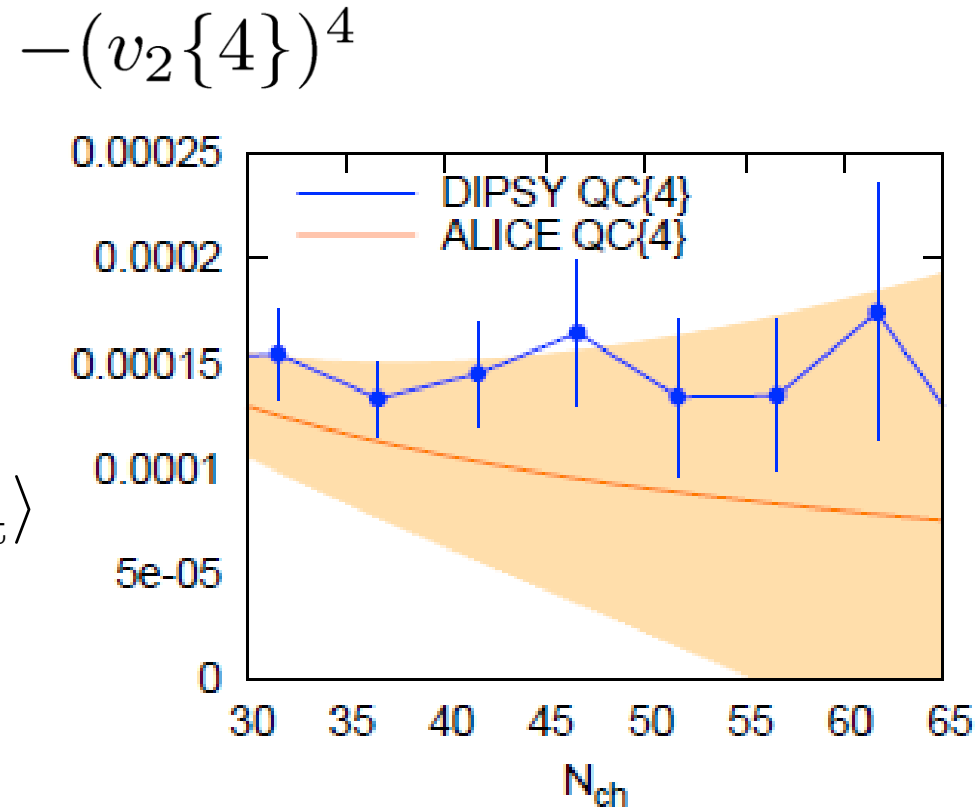
# $v_2\{4\}$ ALICE data vs. DIPSY

Avsar et al., 1106.4356 [hep-ph]

$(v_2\{4\})^4$  **negative** in the data  
and in MCs (no flow)

$$(v_2^{\text{flow}}\{4\})^4 \sim (\epsilon\{4\})^4 = 2\langle\epsilon_{\text{part}}^2\rangle^2 - \langle\epsilon_{\text{part}}^4\rangle$$

**positive** in the flow scenario



Sign change at large  $N_{\text{ch}}$   $\rightarrow$  Possible signature of flow.

# Conclusions

- DIPSY can simulate high-multiplicity pp events with proper QCD dynamics in the transverse plane.
- Eccentricity is 30%, comparable to semi-central Pb collisions.
- Challenging to distinguish flow from non-flow correlations. We suggest to look for the sign change of  $(v_2\{4\})^4$ .
- Extension to AA → talk by [C. Flensburg](#).