

Eccentricity and v_2 in proton-proton collisions at the LHC

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in collaboration with

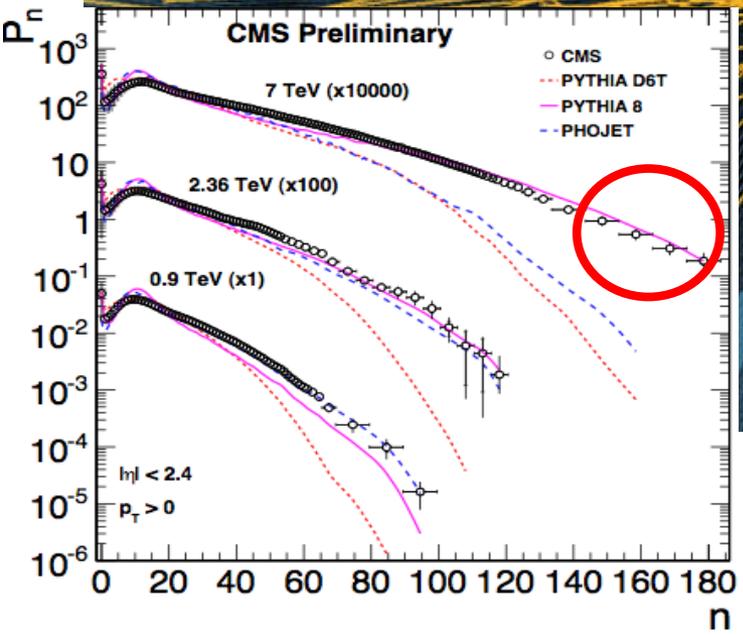
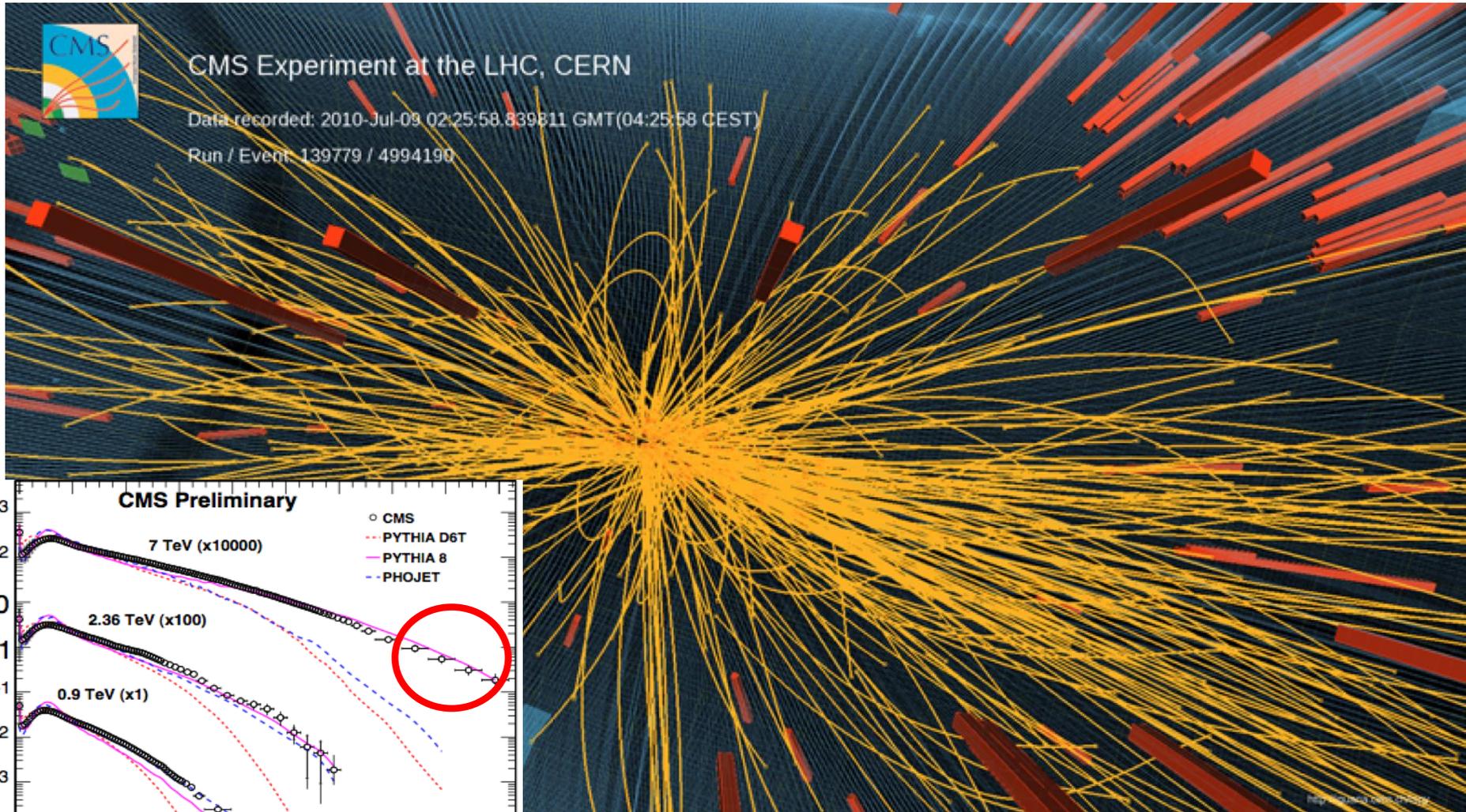
E. Avsar, C. Flensburg, J.-Y. Ollitrault, T. Ueda

Physics Letters B702, 394 (2011);
1106.4356 [hep-ph] (Quark Matter proceedings)

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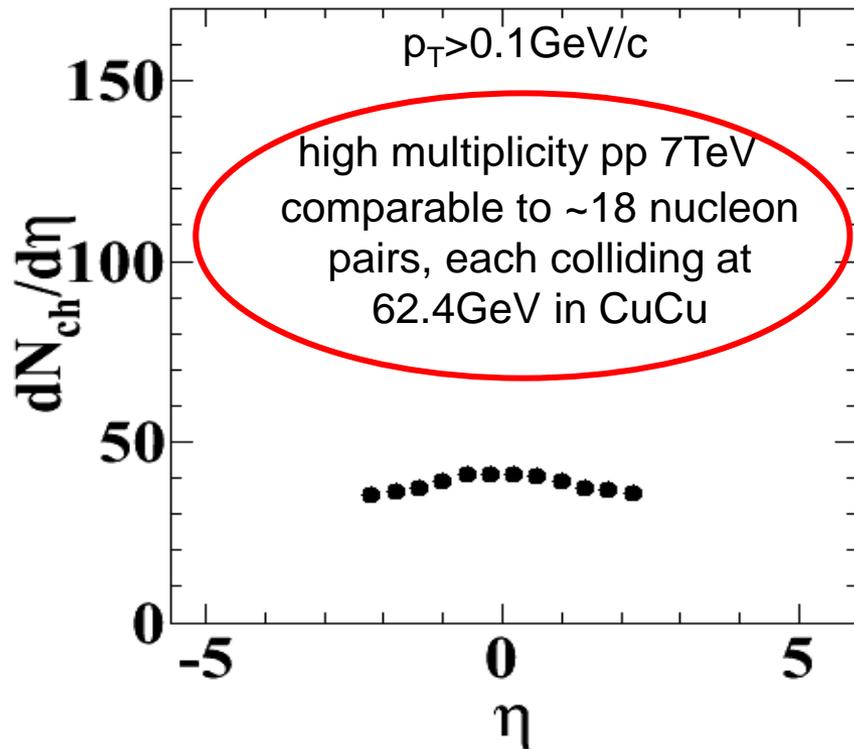
- High-multiplicity pp events at the LHC
- Flow in pp?
- DIPSY
- Eccentricity and v_2 in pp

High-multiplicity pp events at the LHC

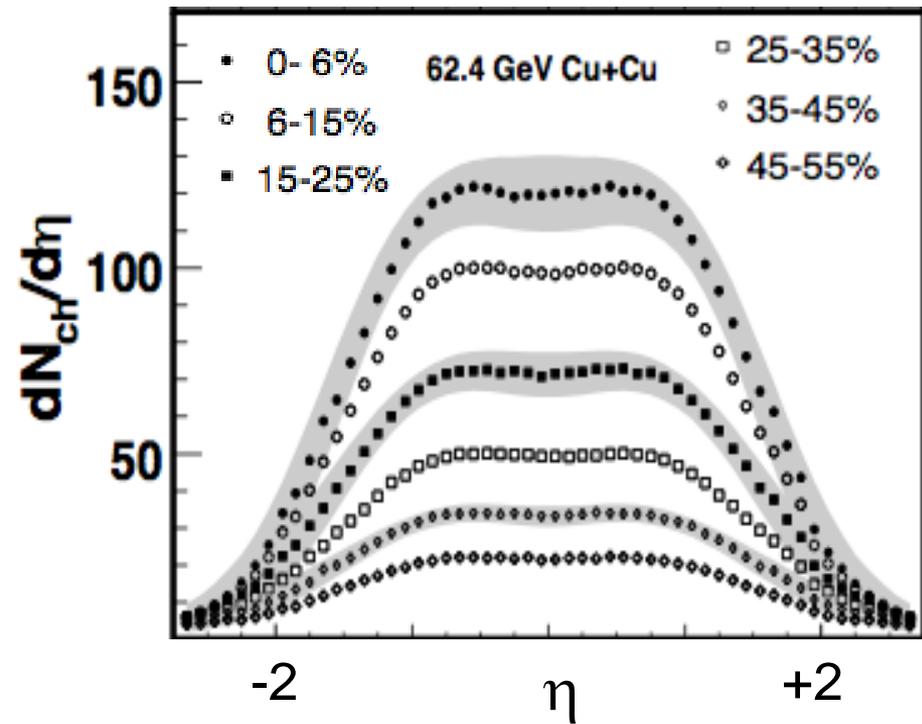


Like an AA collision !

CMS



PHOBOS

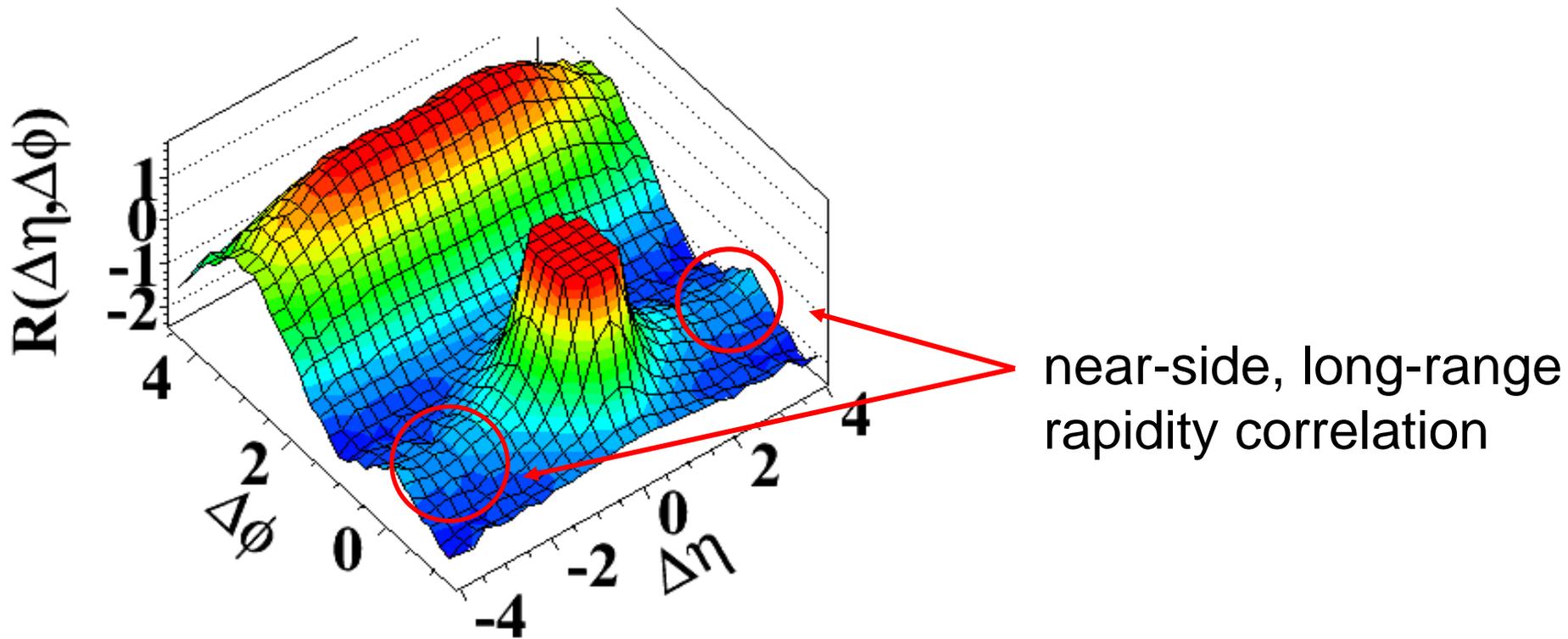


Phenomena usually discussed in the context of nucleus collisions may be observed in proton collisions !

Ridge in pp

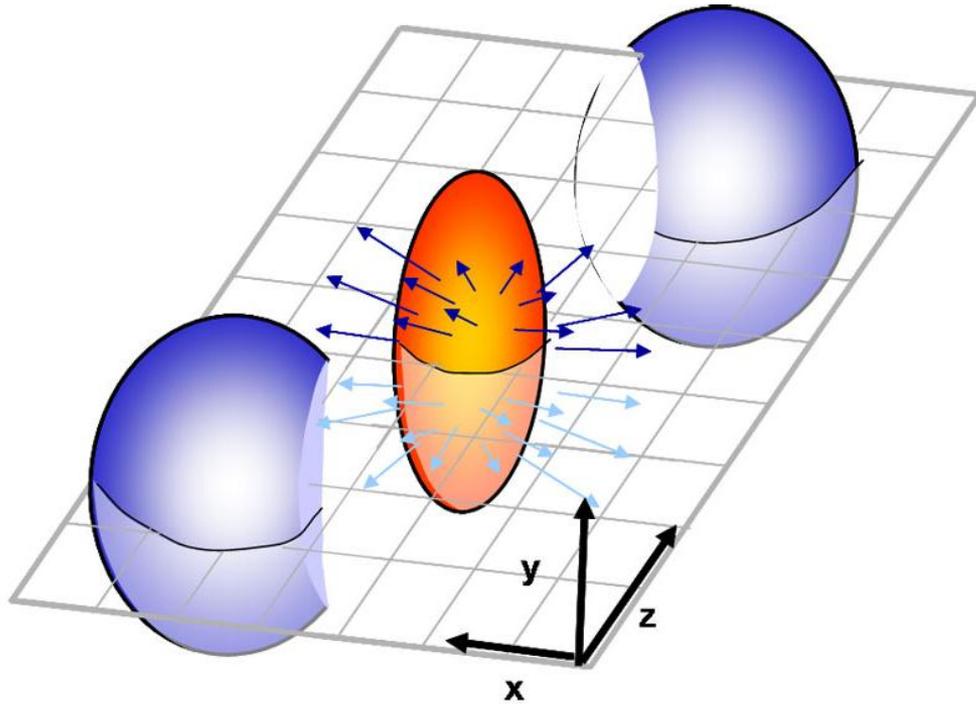
CMS Collaboration, arXiv:1009.4122

(d) $N > 110$, $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



First **un**expected result in pp at the LHC !
Possible collective effects in pp?

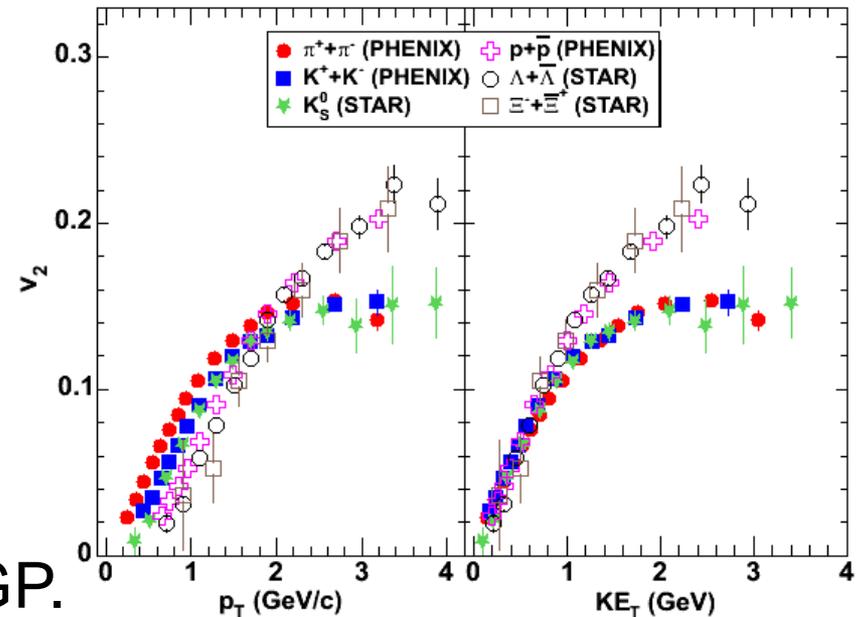
Elliptic flow v_2



$$\frac{dN}{d\phi} \propto 1 + \underline{2v_2} \cos 2\phi$$

$$v_2 \propto \epsilon \quad \text{eccentricity}$$

Hallmark of collective expansion,
widely seen as a signal of the QGP.



Elliptic flow in pp : previous attempts

Fixed distribution (Woods-Saxon, Hard Sphere, Gaussian....)

Luzum, Romatschke 0901.4588

Prasad, Roy, Chattopadhyay 0910.4844

d'Enterria, et al. 0910.3029

Bozek 0911.2392

Ortona, Denicol, Mota, Kodama, 0911.5158

Random distribution (Flux tube model, Hot spot model)

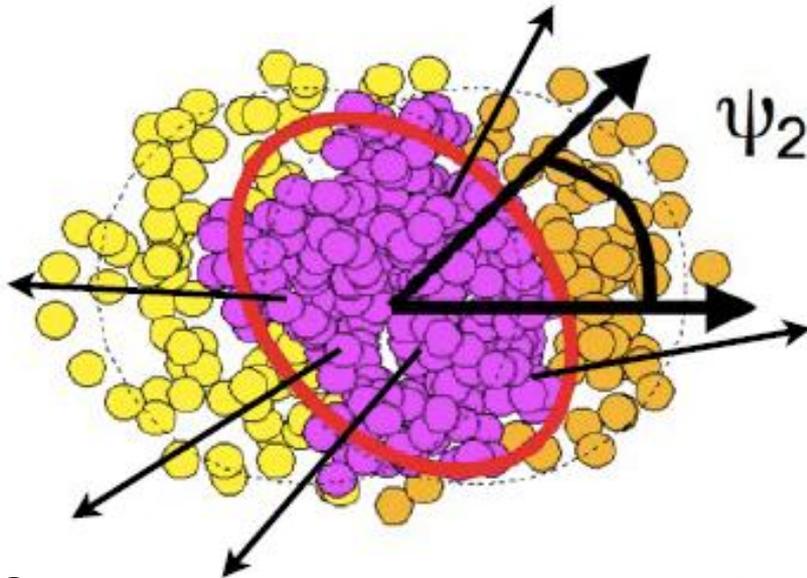
Bautista, Cunqueiro, de Deus, Pajares 0905.3058

Pierog, Porteboeuf, Karpenko, Werner, 1005.4526

Casalderrey-Solana, Wiedemann 0911.4400

Participant eccentricity

Event plane may be different from the reaction plane.



$$\epsilon_{\text{part}} = \frac{\sqrt{(\sigma_y^2 - \sigma_x^2)^2 + 4\sigma_{xy}^2}}{\sigma_y^2 + \sigma_x^2}$$

Can be nonzero even at vanishing impact parameter due to fluctuations.

Important because high-multiplicity pp events mostly come from central collisions.

AA \rightarrow fluctuation of nucleons

pp \rightarrow fluctuation of small-x gluons

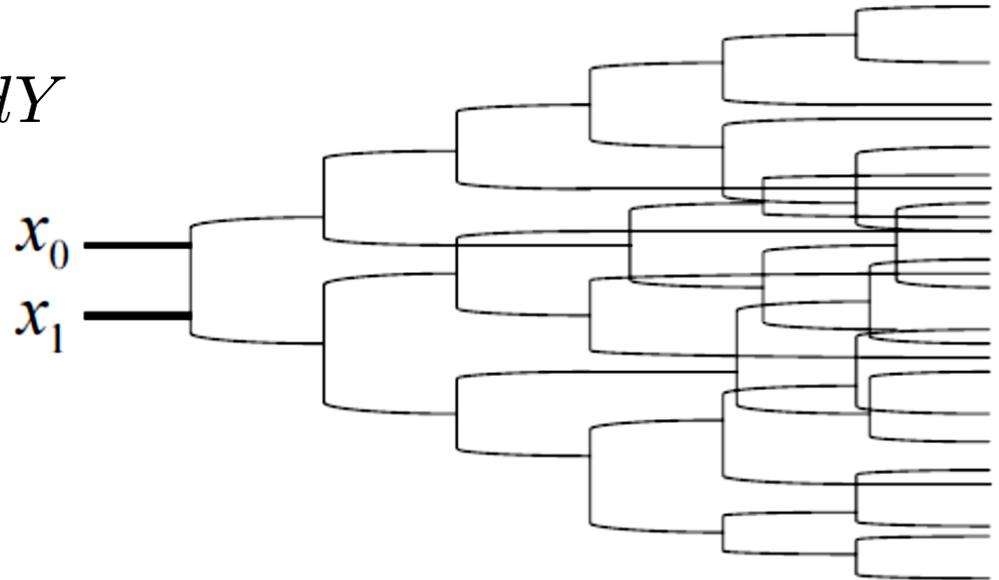
QCD dipole model

Mueller (1994~)

Coordinate space formulation of the BFKL equation

Probability of gluon (dipole) splitting

$$dP = \bar{\alpha}_s \frac{(\vec{x} - \vec{y})^2}{(\vec{x} - \vec{z})^2 (\vec{z} - \vec{y})^2} d^2 \vec{z} dY$$



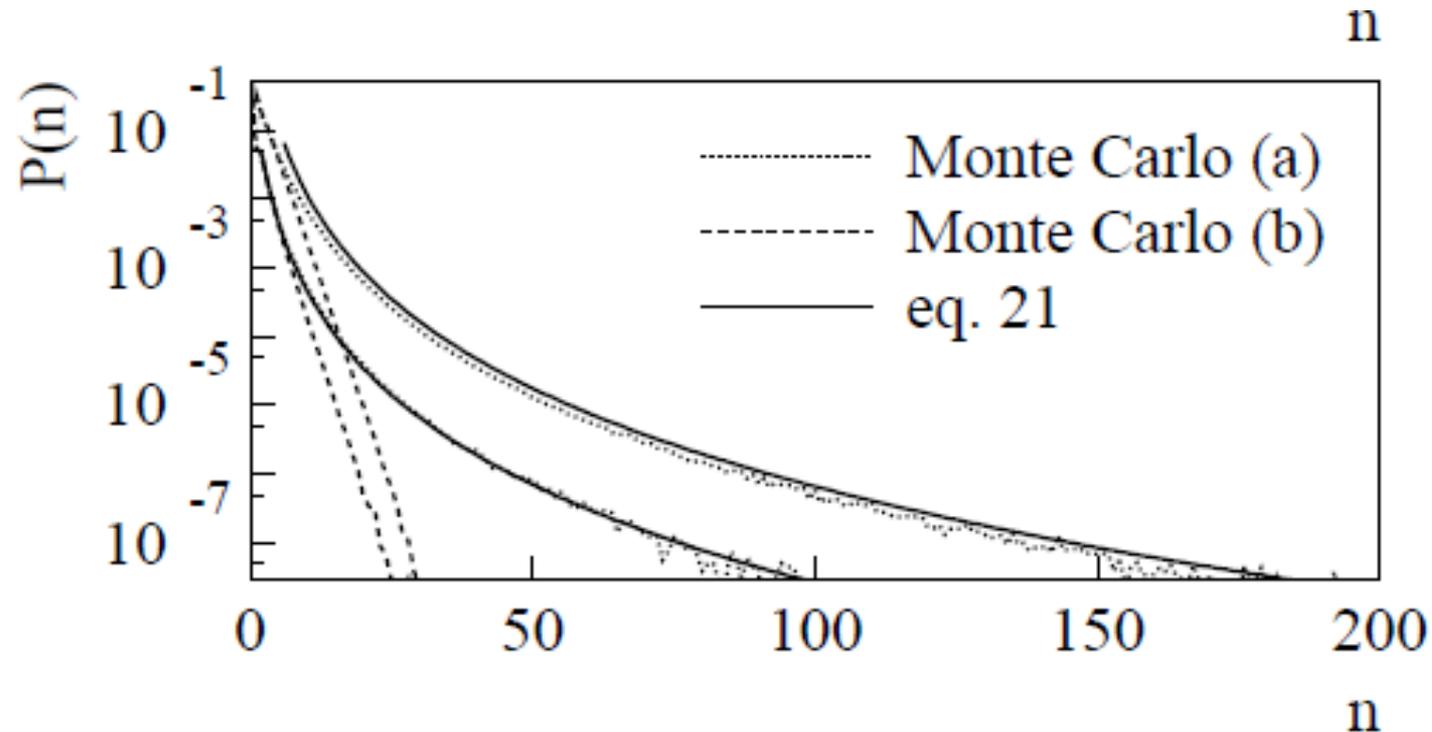
- **Very strong fluctuation** in the gluon multiplicity
- **Very strong correlation** in impact parameter space

Salam (1995)
YH, Mueller (2007)
Avsar, YH (2008)

Gluon number fluctuation

Probability distribution of the number of gluons in the dipole model

Salam (1995)



DIPSY

Full-fledged Monte Carlo event generator for pp based on the dipole model.

Flensburg, Gustafson, Lonnblad, arXiv:1103.4321
extension of Avsar, Gustafson, Lonnblad (2005~)

Featuring:

BFKL

Running coupling (NLO)

Energy conservation (N^n LO)

Saturation effects

Confinement effects

Multiple scattering,

Underlying events,

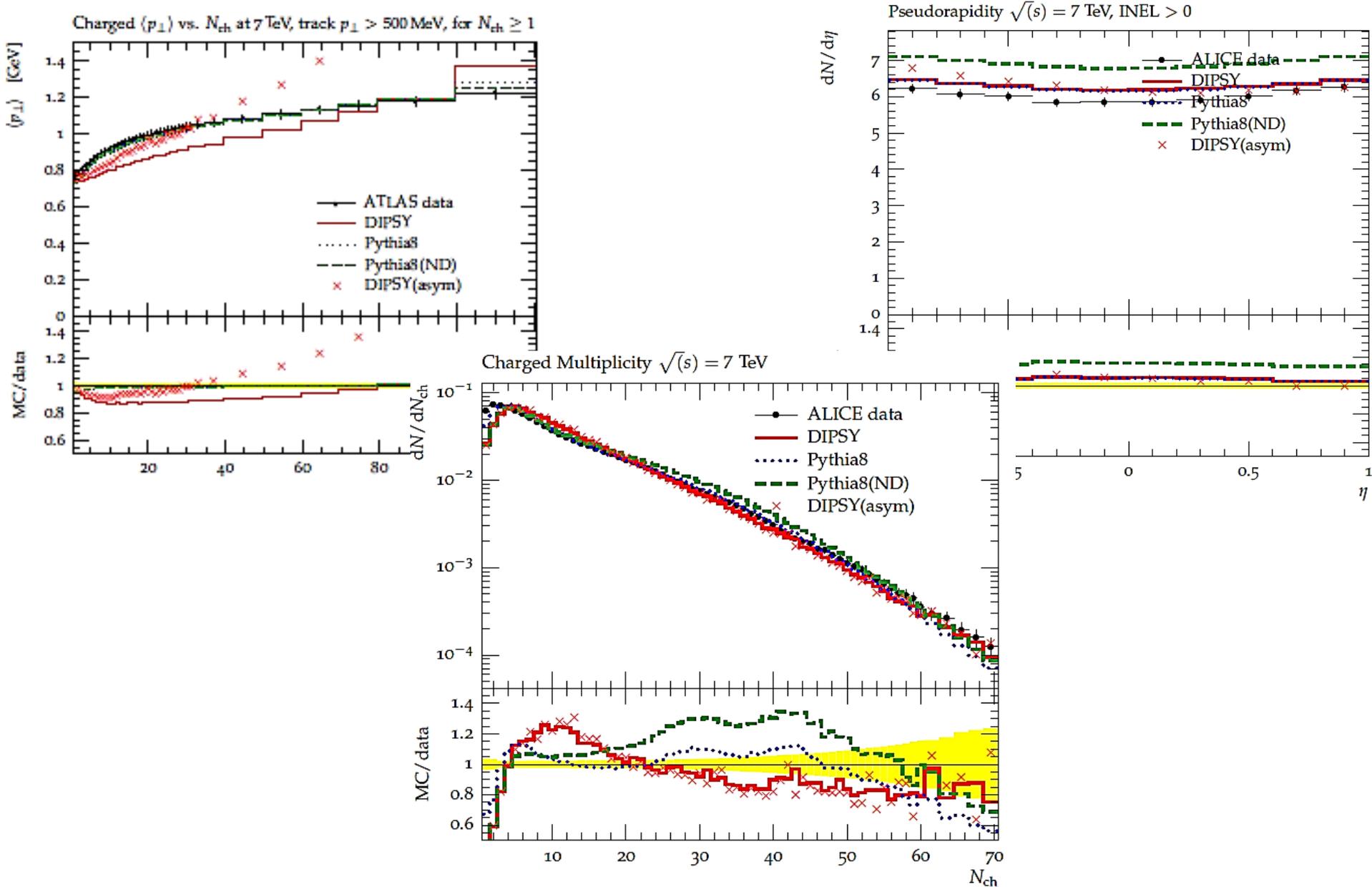
Parton shower (ARIADNE)

Hadronization (Pythia)

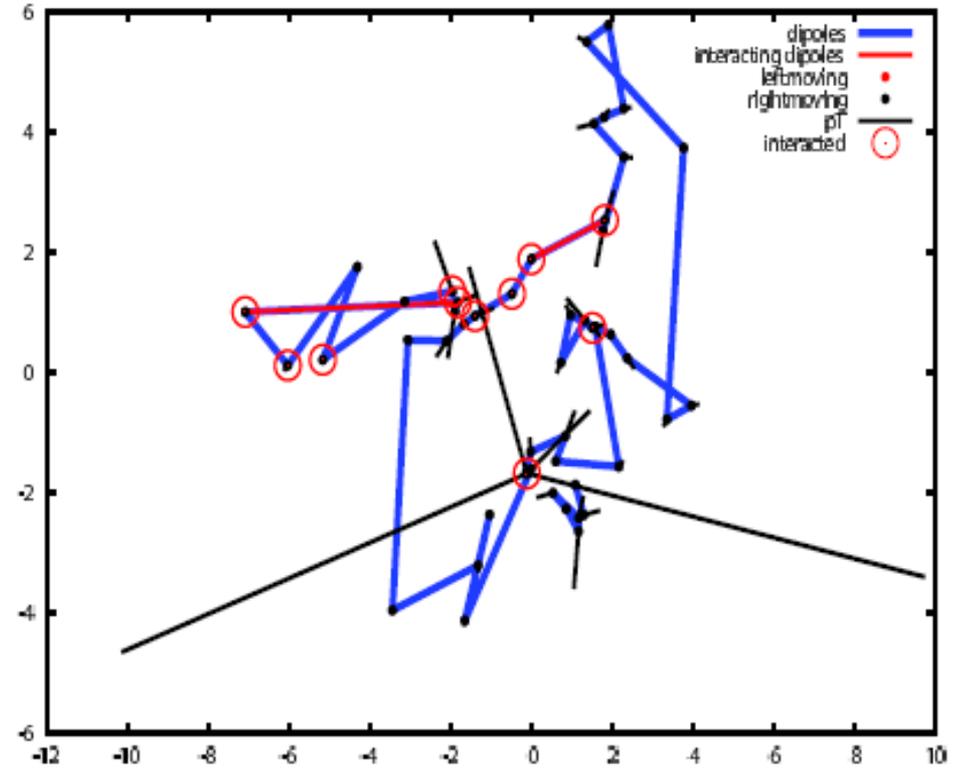
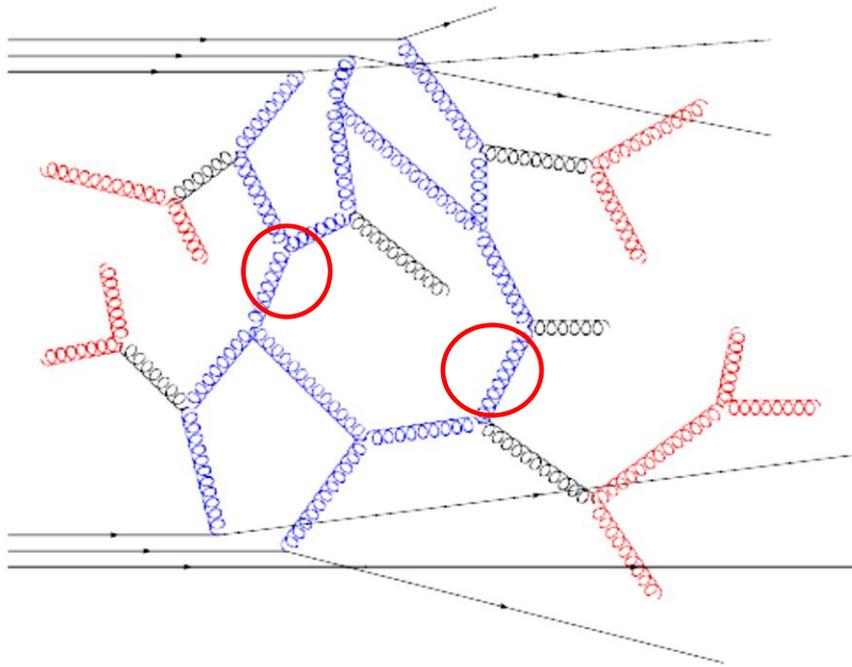
“Lund gang”

Energy dependence is a prediction. No ad hoc retuning of parameters at different energies.

Some sample results from DIPSY @ 7TeV



Deconstructing high-multiplicity events



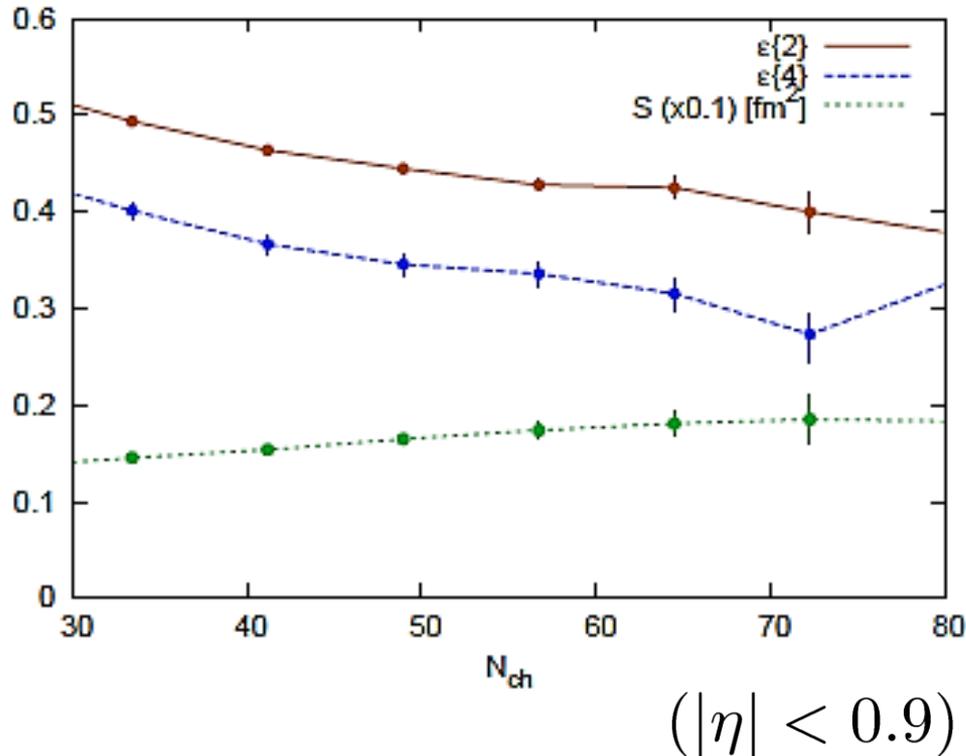
High-multiplicity pp events

= Upward fluctuation in the gluon number in proton's w.f.

+ Multiple (more than 10) parton-parton interactions

Eccentricity in pp at 7 TeV

Shape of the area occupied by the “liberated” gluons.



$$\epsilon_{\text{part}} = \frac{\sqrt{(\sigma_y^2 - \sigma_x^2)^2 + 4\sigma_{xy}^2}}{\sigma_y^2 + \sigma_x^2}$$

$$\epsilon\{2\} = \sqrt{\langle \epsilon_{\text{part}}^2 \rangle}$$

$$\epsilon\{4\} = \left(2\langle \epsilon_{\text{part}}^2 \rangle^2 - \langle \epsilon_{\text{part}}^4 \rangle \right)^{\frac{1}{4}}$$

Comparison with Pb-Pb

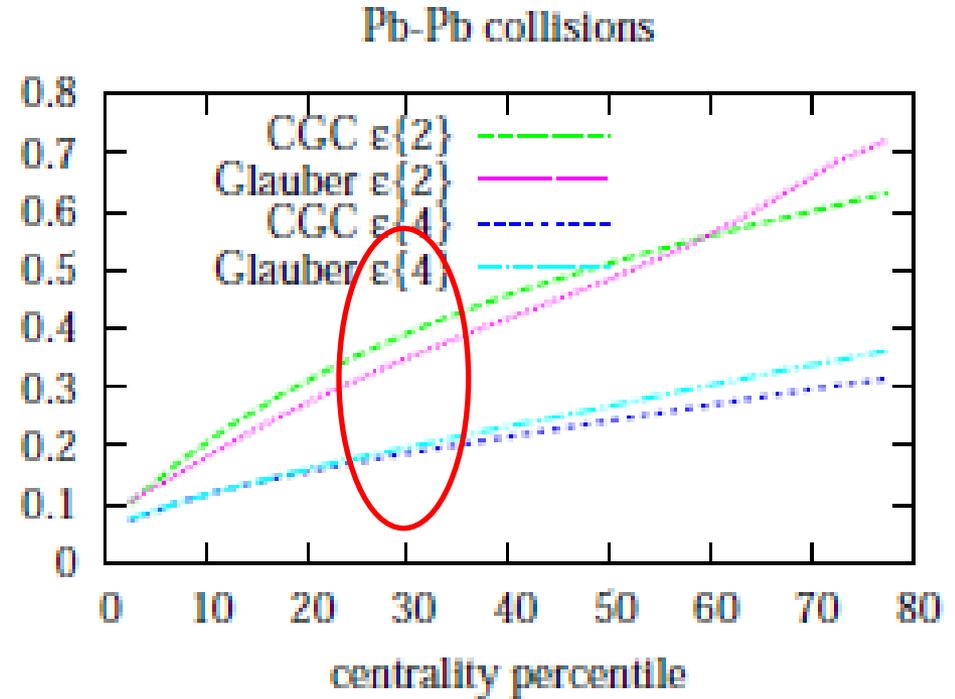
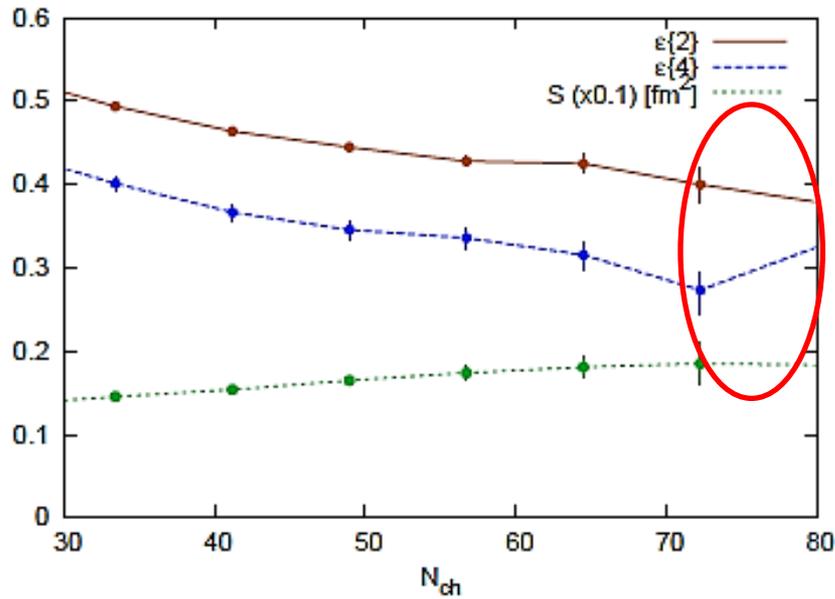


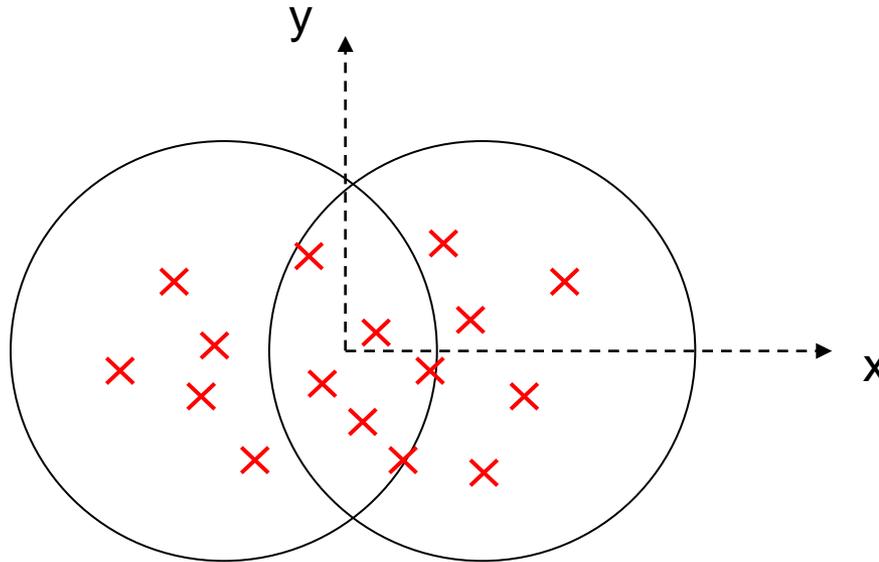
Figure by M. Luzum

Comparable to 30% central Pb-Pb collisions

Nature of eccentricity in pp

Conventional definition of the eccentricity at fixed b

$$\epsilon_s = \frac{\sigma_y^2 - \sigma_x^2}{\sigma_y^2 + \sigma_x^2} \quad \text{is negative !}$$



Nominal “overlapping region” is a poor guide in pp.

$$\epsilon \longrightarrow v_2$$

Empirical relation between the eccentricity and v_2 .

Drescher, Dumitru, Gombeaud, Ollitrault. (2007)

$$v_2\{2\} = \epsilon\{2\} \left(\frac{v_2}{\epsilon}\right)_{hydro} \frac{1}{1 + \frac{\lambda}{K_0} \frac{\langle S \rangle}{dN/d\eta}}$$

← $\sim \frac{1}{(\text{density})}$
 taking care of
 incomplete equilibration



$$(v_2\{2\})^2 = \left(\frac{v_2}{\epsilon}\right)_{hydro}^2 \left\langle \frac{\epsilon_{part}^2}{\left(1 + \frac{\lambda}{K_0} \frac{S}{dN/d\eta}\right)^2} \right\rangle$$

...and a similar relation between $\epsilon\{4\}$ and $v_2\{4\}$

In order to obtain large v_2 , a single event has to be **both** elliptic in shape and have high density.

“Nonflow” effect

v_2 from n-particle angular correlation

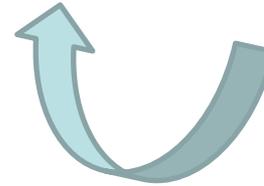
$$v_2^2\{2\} = \langle \{ \cos(2(\phi_i - \phi_j)) \} \rangle,$$

$$v_2^4\{4\} = 2(v_2\{2\})^4 - \langle \{ \cos(2(\phi_i + \phi_j - \phi_k - \phi_l)) \} \rangle$$

$$(v_2\{n\})^n = v_2^n + \delta_n$$

“flow” “nonflow”

jets, hard scattering,
resonance decay,
BFKL evolution,
color connection, etc.

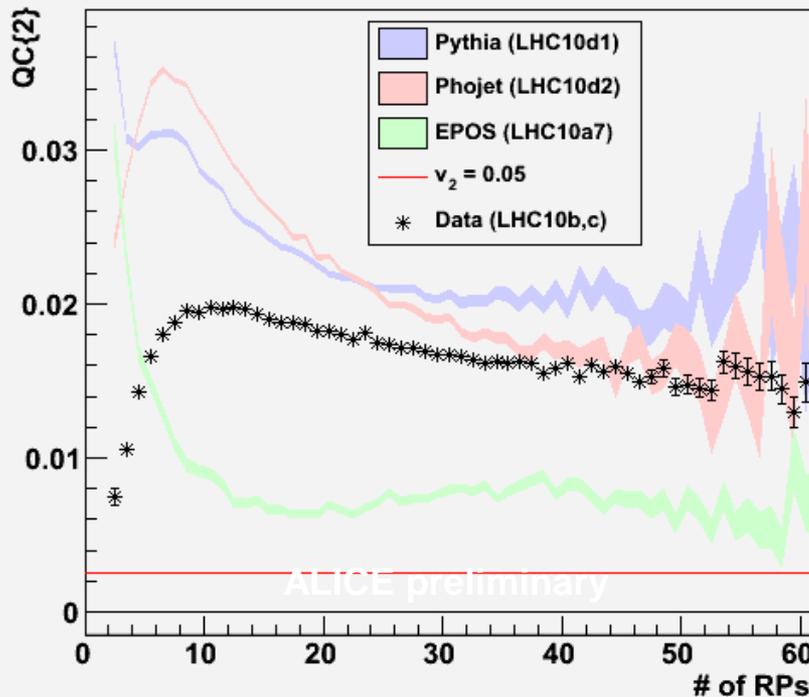


In AA, it is relatively innocuous $\delta_n \sim \left(\frac{1}{N_{ch}} \right)^{n-1}$

In pp, it could be very large...

ALICE data for $v_2\{2\}$

Bilandzic, talk at QCHS IX; AIP Conf. Proc. (2011)



$$\langle \cos 2\phi_{ij} \rangle = v_2^2 + \delta_2$$

“flow” “nonflow”

$$\sqrt{\langle \cos 2\phi_{ij} \rangle} \approx 0.14$$

Large nonflow contribution

dominate over the flow contribution.... $v_2^{\text{flow}}\{2\} \approx 0.06$

→ Necessary to go to higher cumulants.

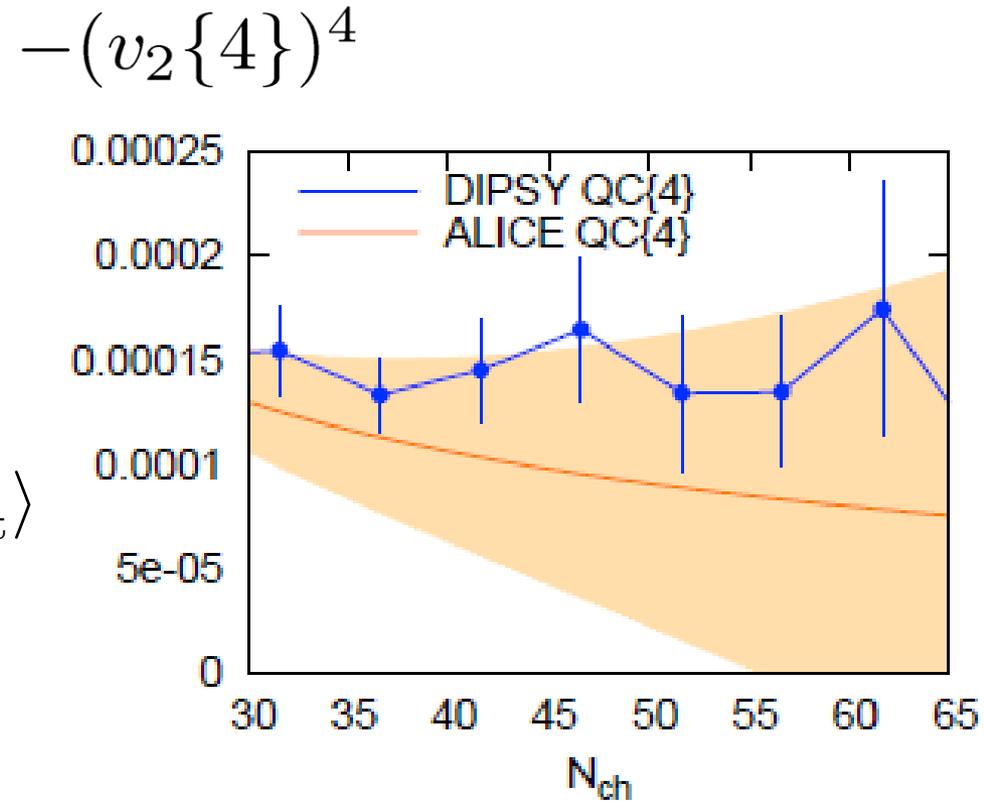
$v_2\{4\}$ ALICE data vs. DIPSY

Avsar et al., 1106.4356 [hep-ph]

$(v_2\{4\})^4$ **negative** in the data
and in MCs (no flow)

$$(v_2^{\text{flow}}\{4\})^4 \sim (\epsilon\{4\})^4 = 2\langle\epsilon_{\text{part}}^2\rangle^2 - \langle\epsilon_{\text{part}}^4\rangle$$

positive in the flow scenario



Sign change at large N_{ch} \rightarrow Possible signature of flow.

Conclusions

- DIPSY can simulate high-multiplicity pp events with proper QCD dynamics in the transverse plane.
- Eccentricity is 30%, comparable to semi-central Pb collisions.
- Challenging to distinguish flow from non-flow correlations. We suggest to look for the sign change of $(v_2\{4\})^4$.
- Extension to AA → talk by [C. Flensburg](#).