

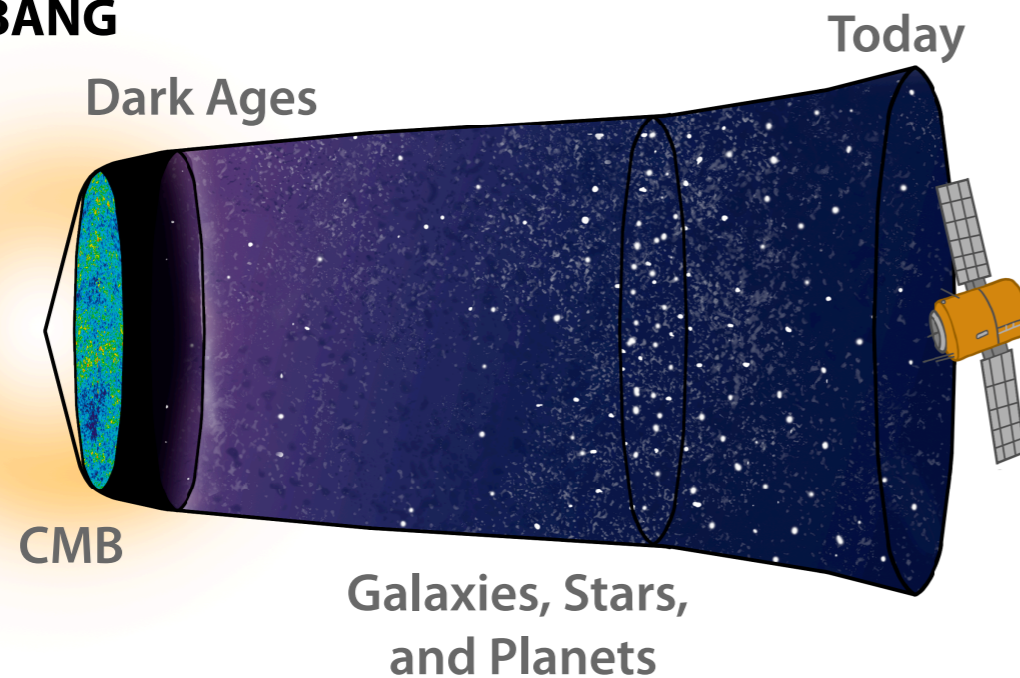
Viscosity versus Causality



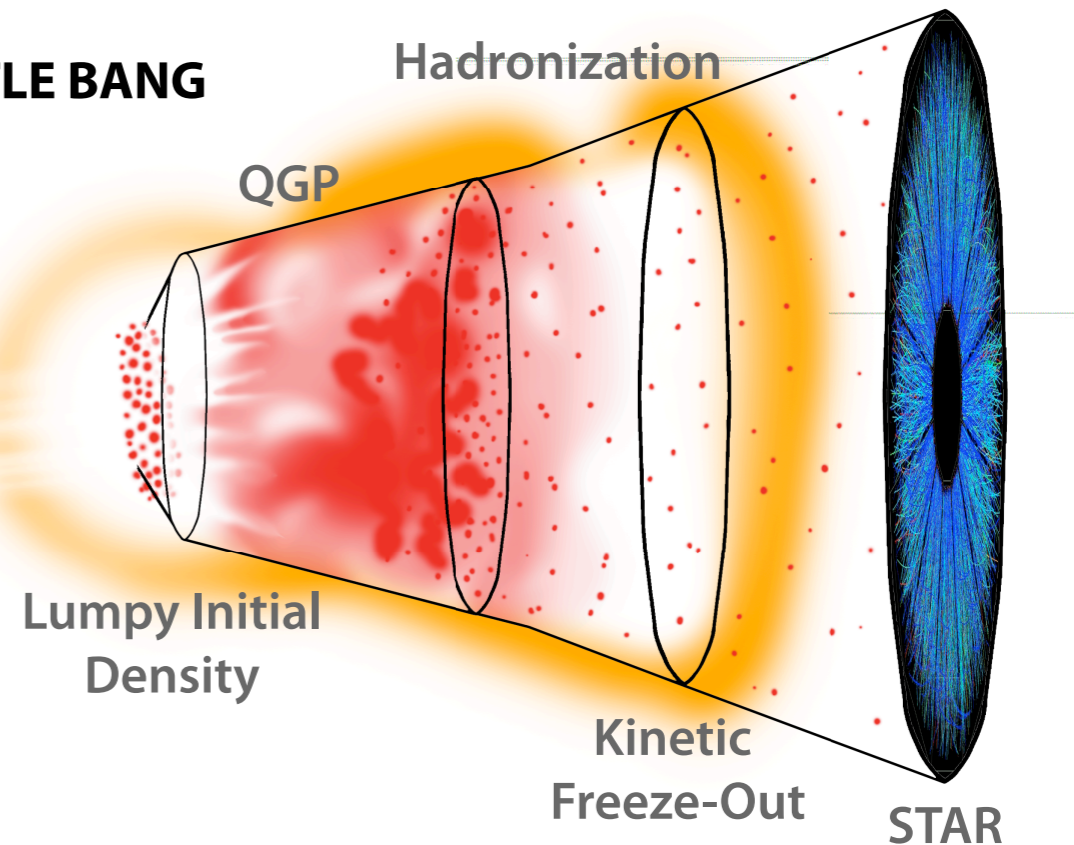
Analogy with the Early Universe

illustration: Alex Doig

BIG BANG

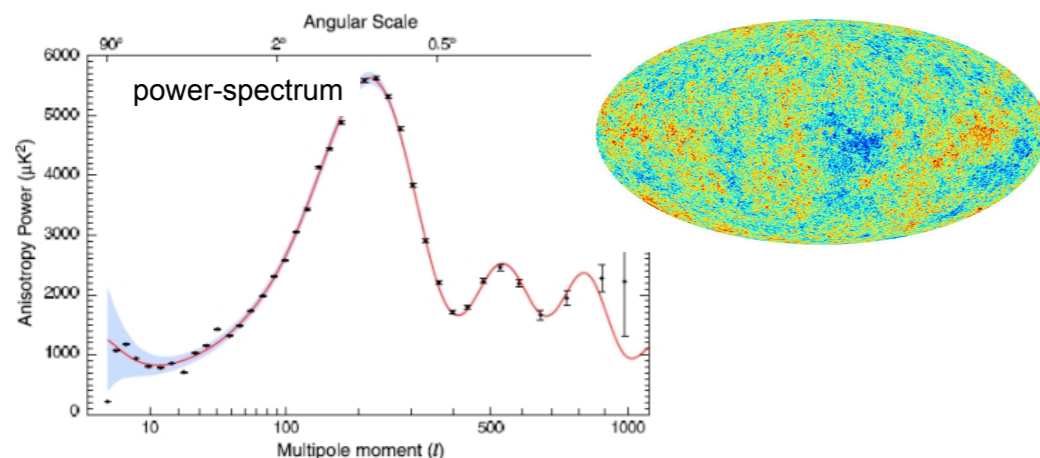


LITTLE BANG



Quantum fluctuations from the early universe show up as hotspots in the CMB.

Analogy for heavy-ion collisions?



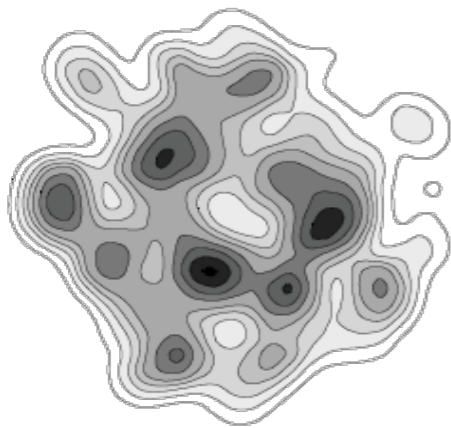
We expect fluctuations from the beginning of the little bangs show up in the data.

Lumpy Initial State

Expect: Initial density is inhomogeneous.

predicted by several models

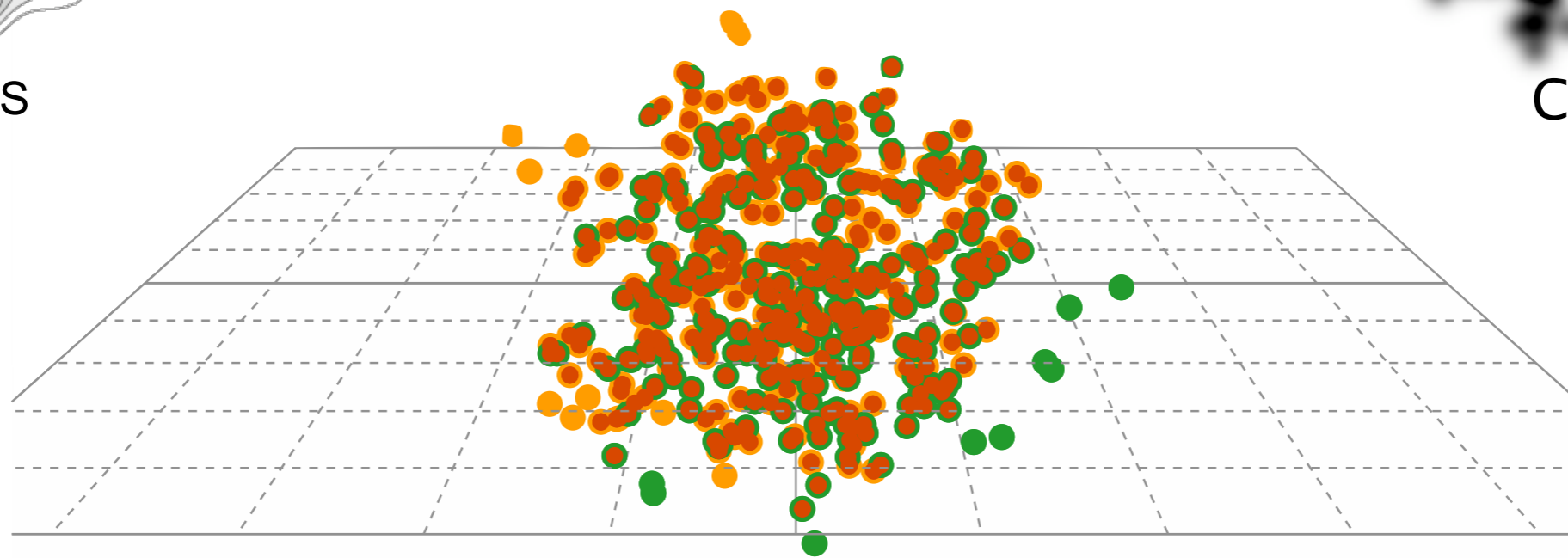
transverse projection of a central collision generated in



NEXUS



CGC



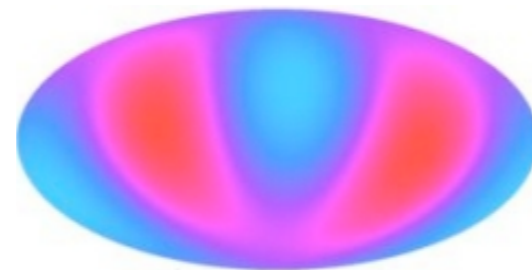
Glauber

How much of the initial inhomogeneity is transferred to the final state?

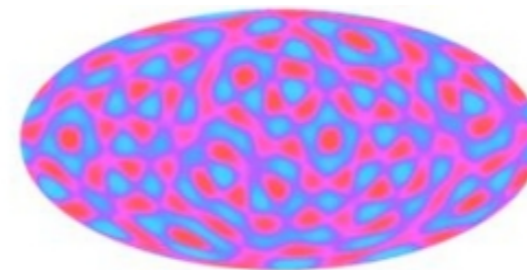
Length Scales

Higher harmonics probe smaller length-scales.

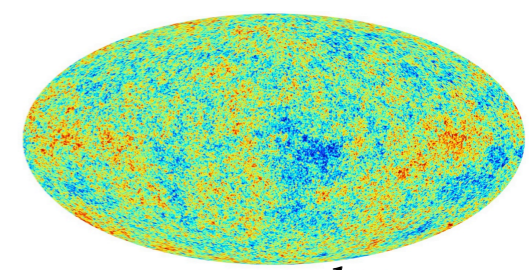
Spherical harmonic expansion of CMB



$l=2$

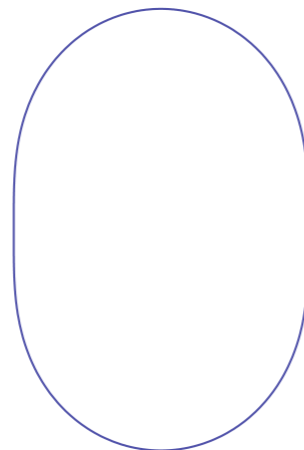


$l=16$

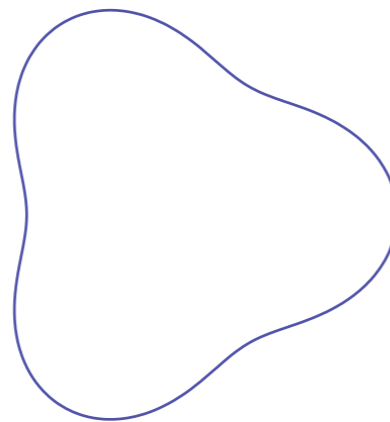


sum l

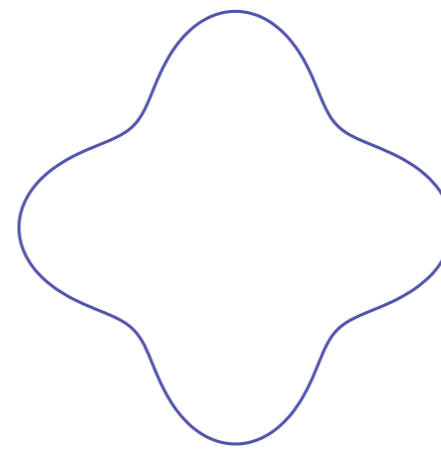
Fourier expansion of HIC



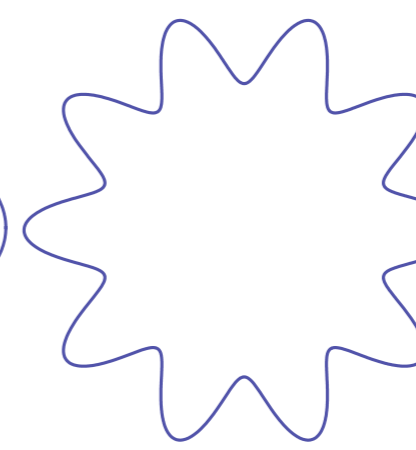
$n=2$



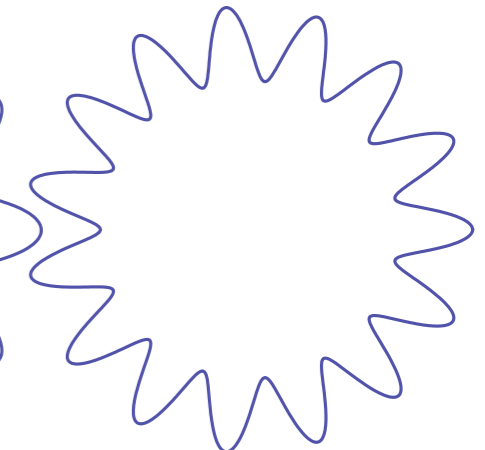
$n=3$



$n=4$



$n=10$

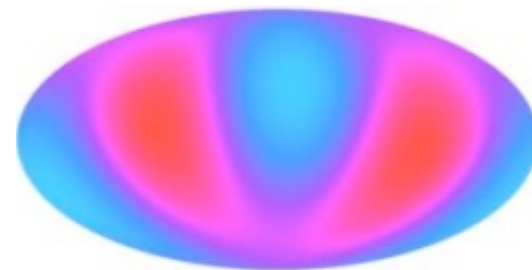


$n=15$

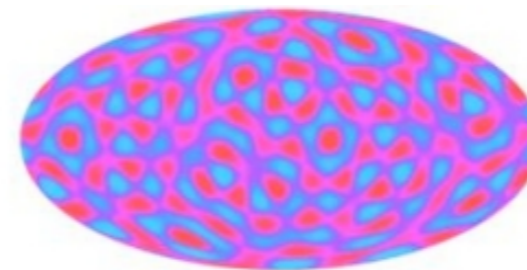
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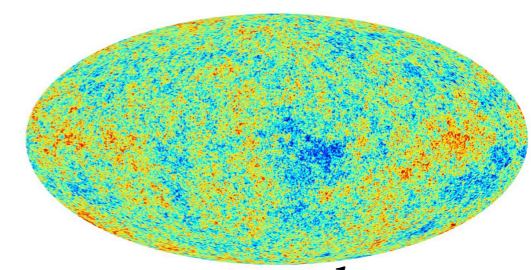
Spherical harmonic expansion of CMB



$l=2$

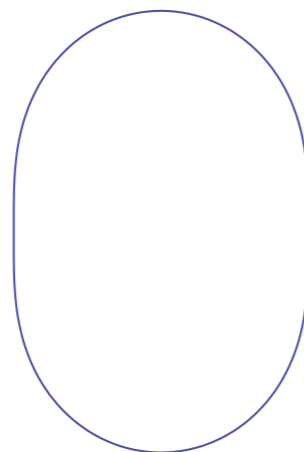


$l=16$

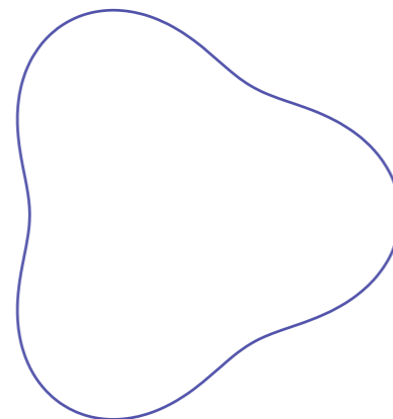


sum l

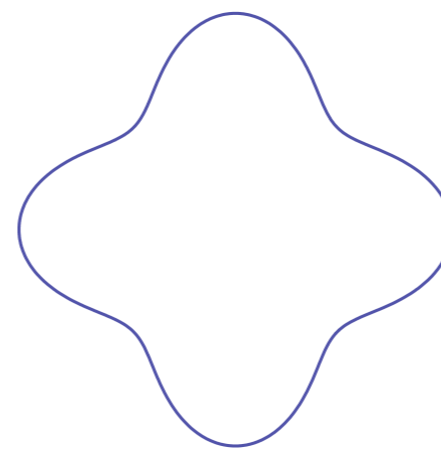
Fourier expansion of HIC



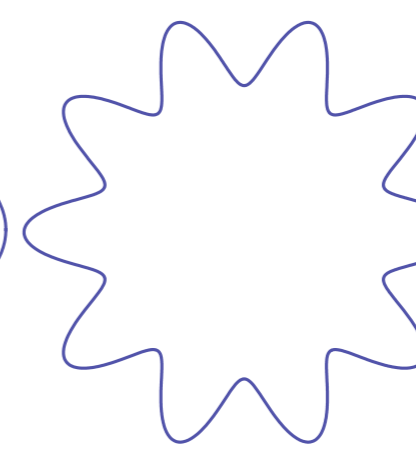
$n=2$



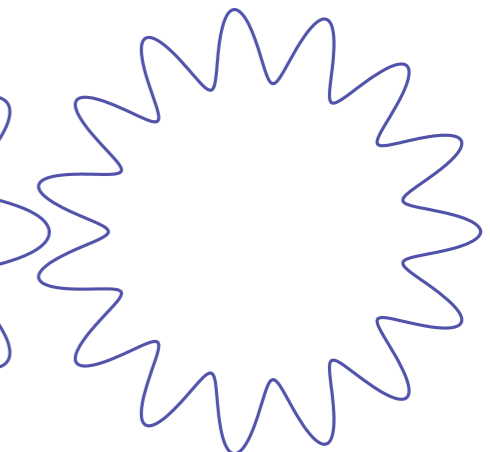
$n=3$



$n=4$



$n=10$



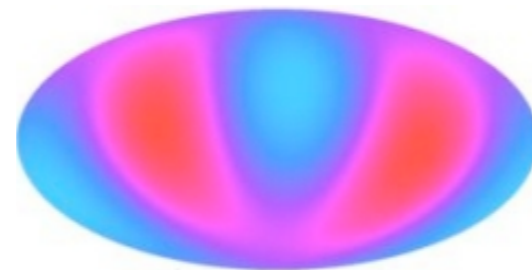
$n=15$

- Efficiency of conversion depends on the relation of various length scales, like the l_{mfp} to the scale probed at n

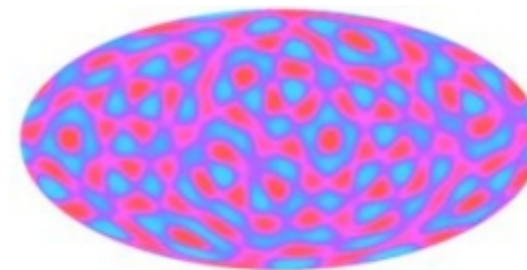
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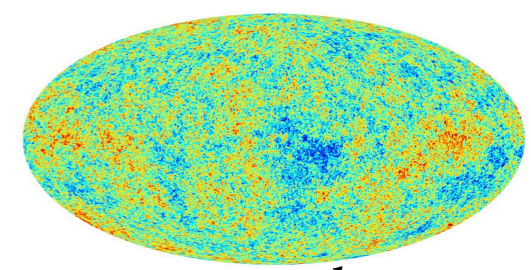
Spherical harmonic expansion of CMB



$l=2$

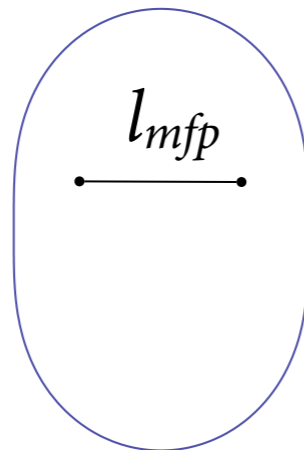


$l=16$

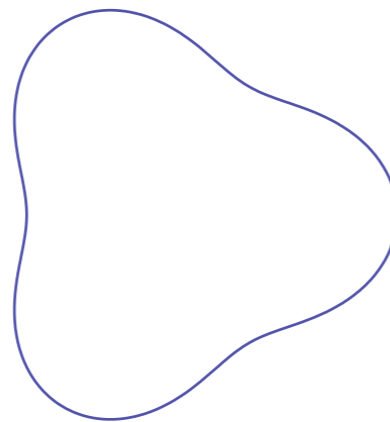


$sum l$

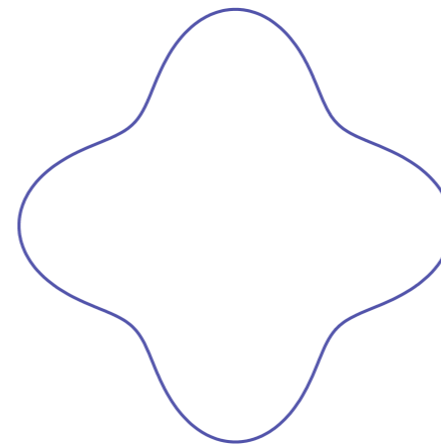
Fourier expansion of HIC



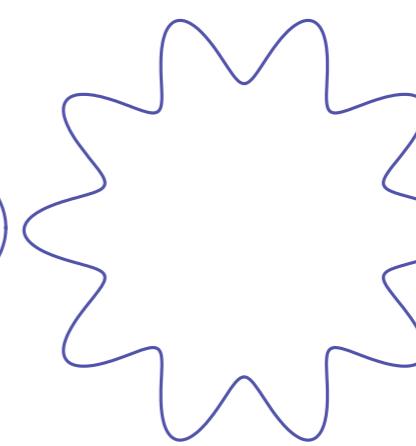
$n=2$



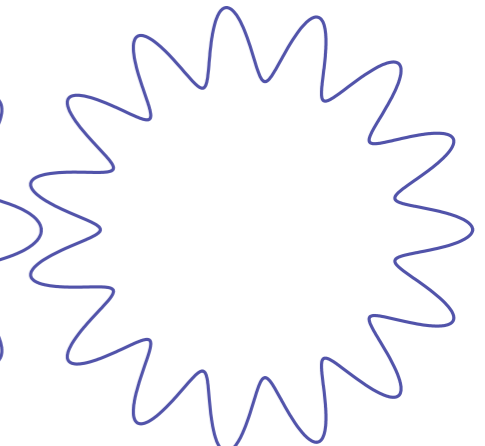
$n=3$



$n=4$



$n=10$



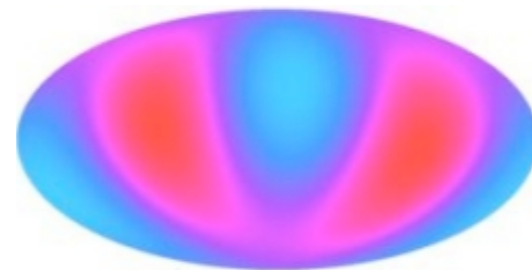
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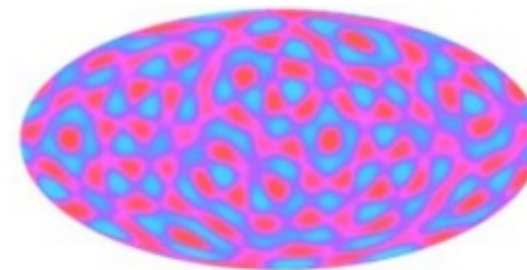
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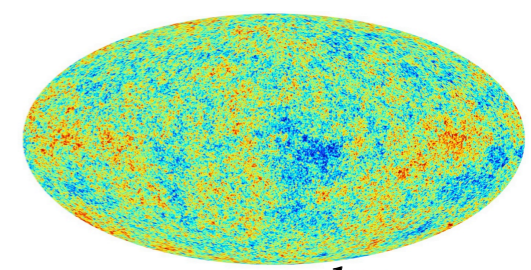
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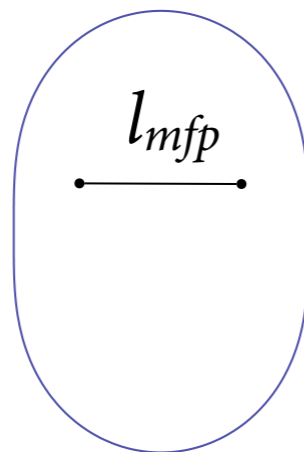


$l=16$

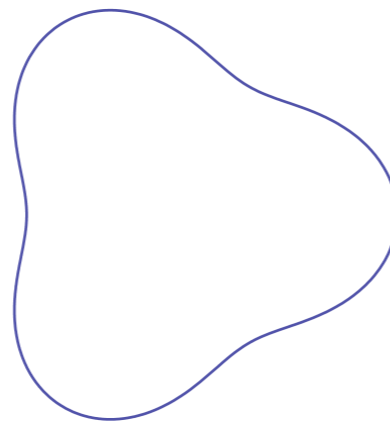


sum l

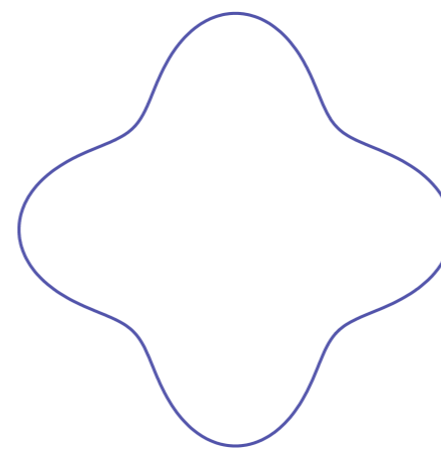
Fourier expansion of HIC



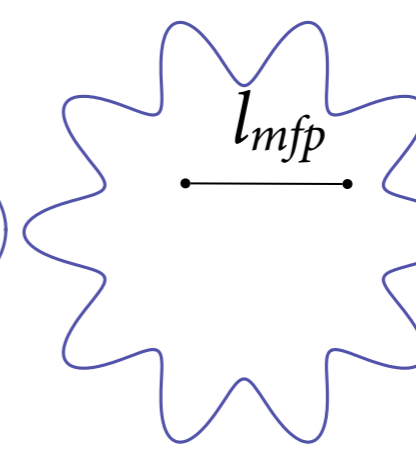
$n=2$



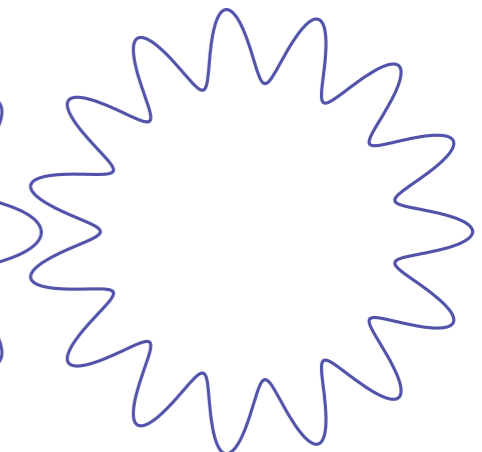
$n=3$



$n=4$



$n=10$



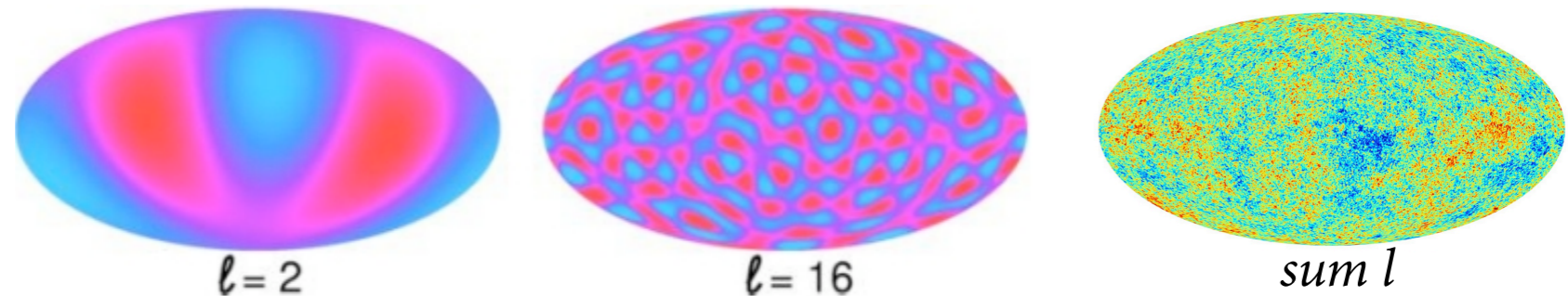
$n=15$

- Efficiency of conversion depends on the relation of various length scales, like the l_{mfp} to the scale probed at n

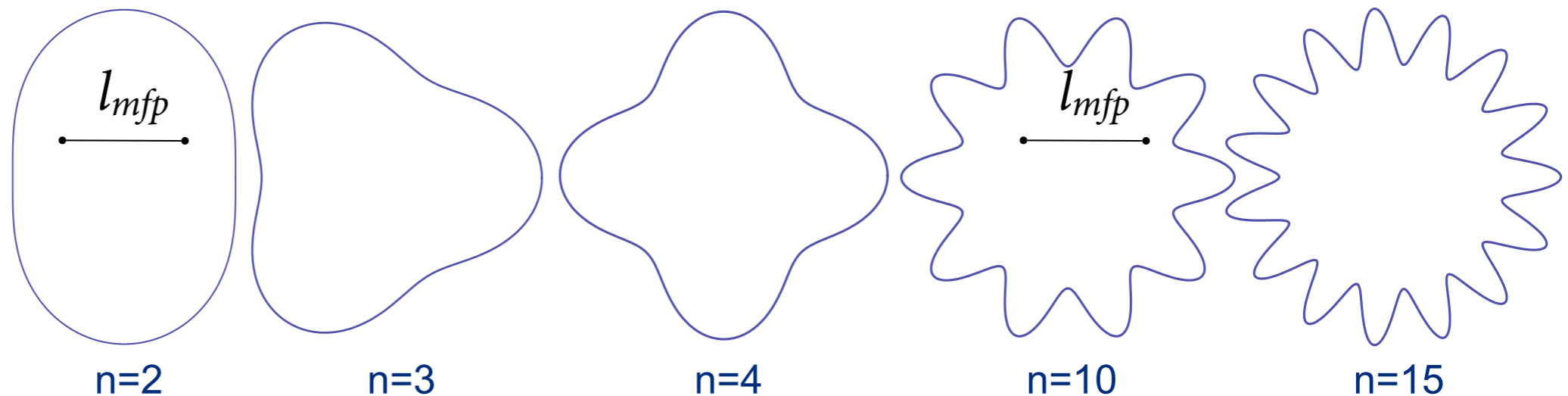
Length Scales

Higher harmonics probe smaller length-scales.

Spherical harmonic expansion of CMB



Fourier expansion of HIC

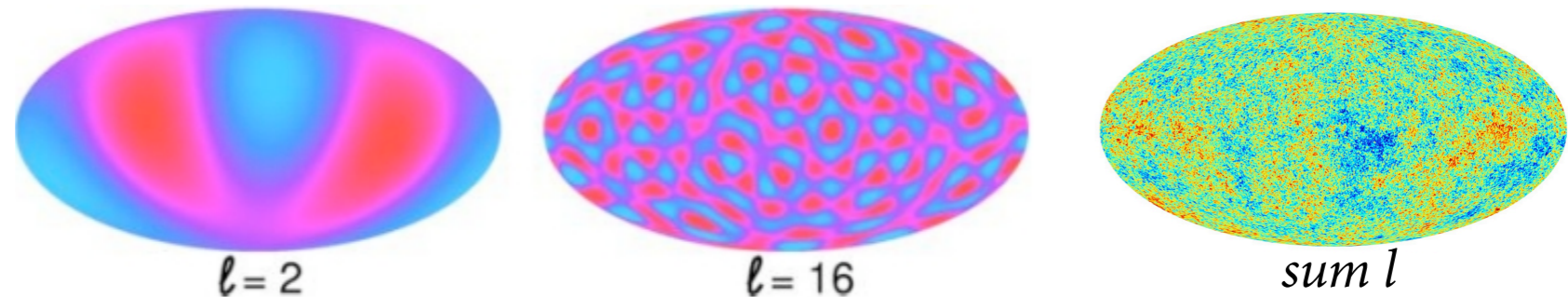


- Efficiency of conversion depends on the relation of various length scales, like the l_{mfp} to the scale probed at n
- **Power spectrum** measures how much anisotropy is in each harmonic n

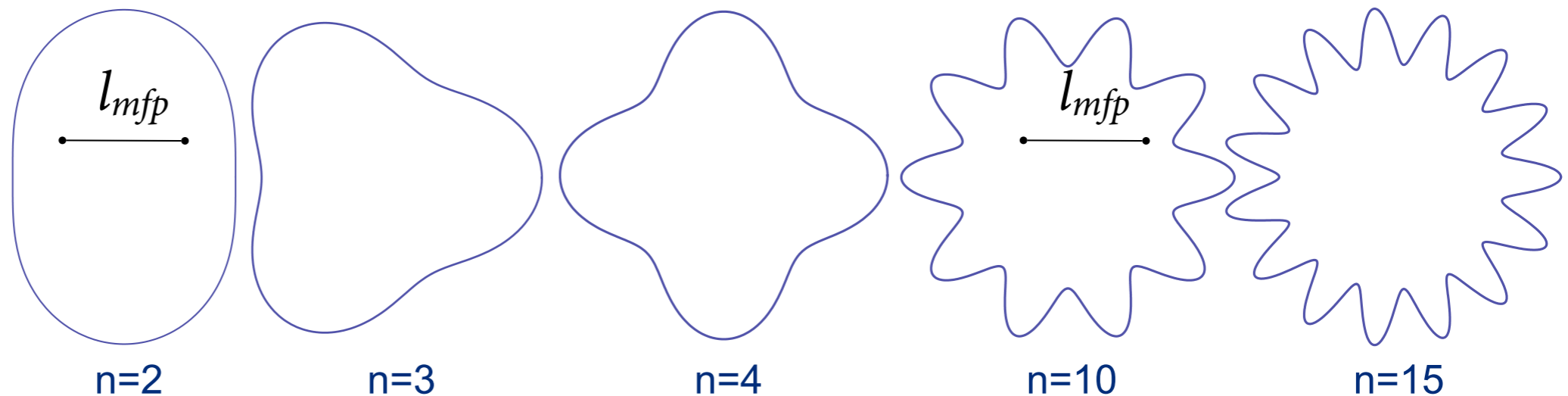
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Spherical harmonic expansion of CMB



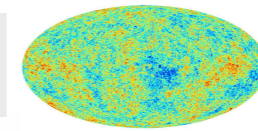
Fourier expansion of HIC



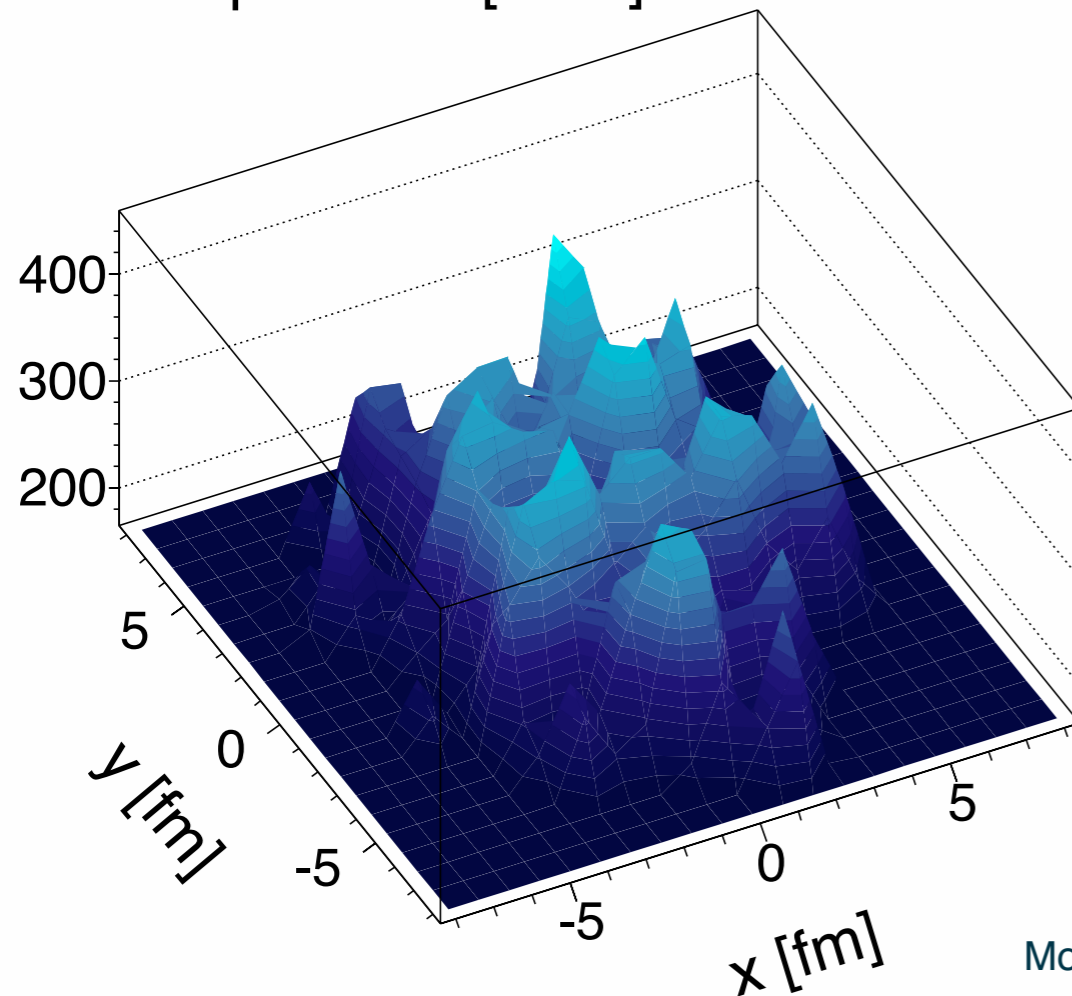
- Efficiency of conversion depends on the relation of various length scales, like the l_{mfp} to the scale probed at n
- **Power spectrum** measures how much anisotropy is in each harmonic n
- Can we obtain (constrain) the l_{mfp} ?

Temperature Fluctuations in Model

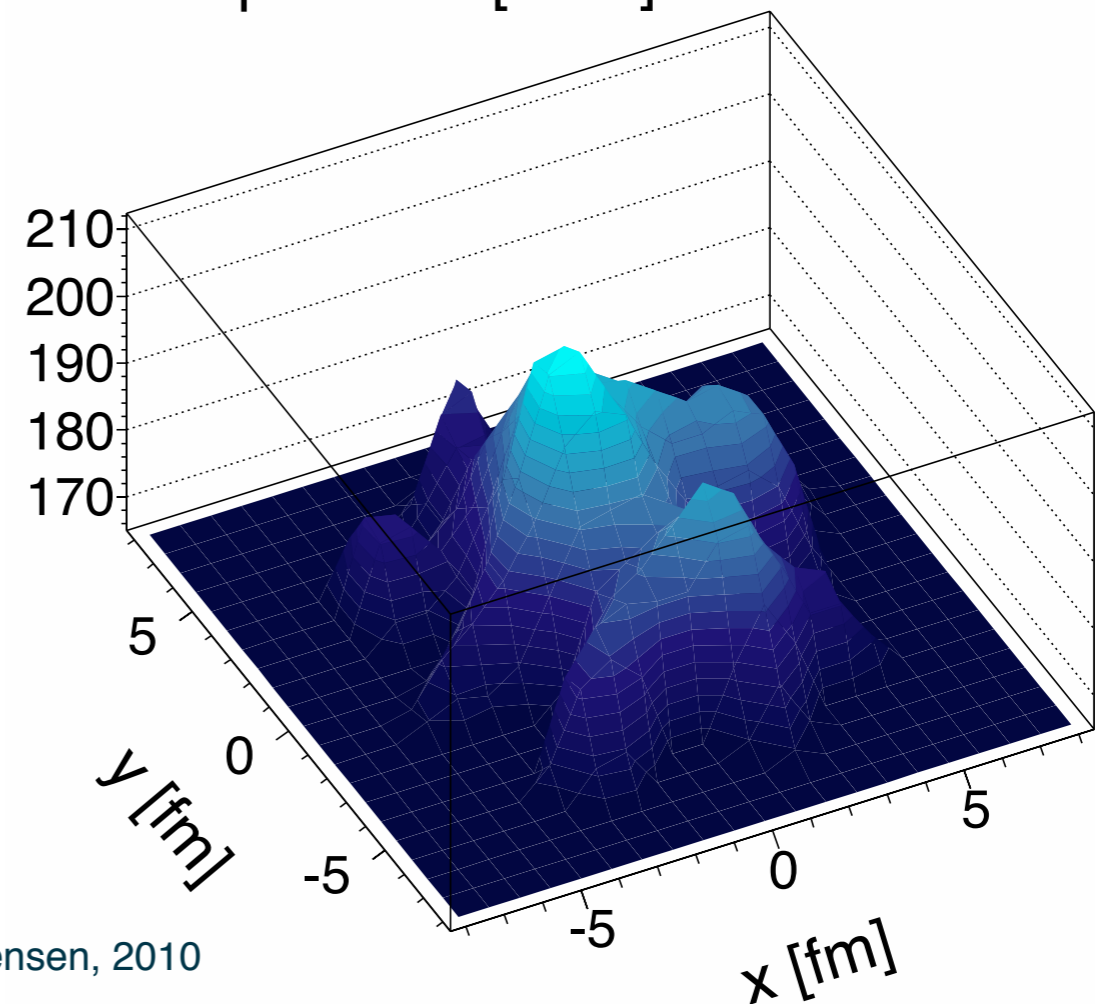
HIC analog of the CMB map



Temperature [MeV] $\tau = 0.6$ fm/c



Temperature [MeV] $\tau = 4.6$ fm/c



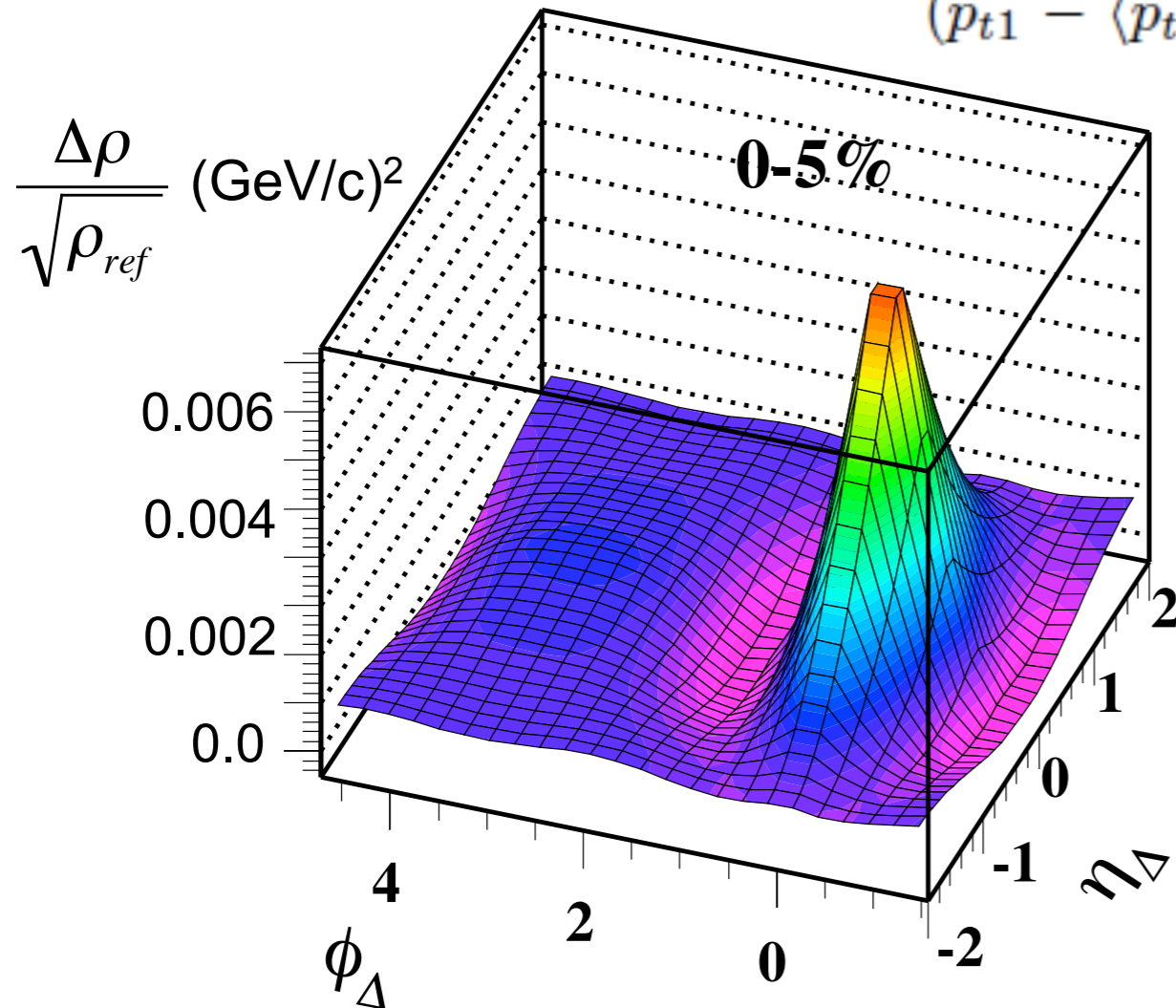
Mocsy, Sorensen, 2010

Au+Au collisions may initially contain hotspots of ~ 1.5 fm and remnants of these may persist

Temperature Fluctuations in Data

- We look for evidence for hotspots in p_t - p_t correlations

$(p_{t1} - \langle p_t \rangle)(p_{t2} - \langle p_t \rangle)$ sensitive to T-T correlations



STAR Collaboration J. Phys. G 32, L37 (2006)

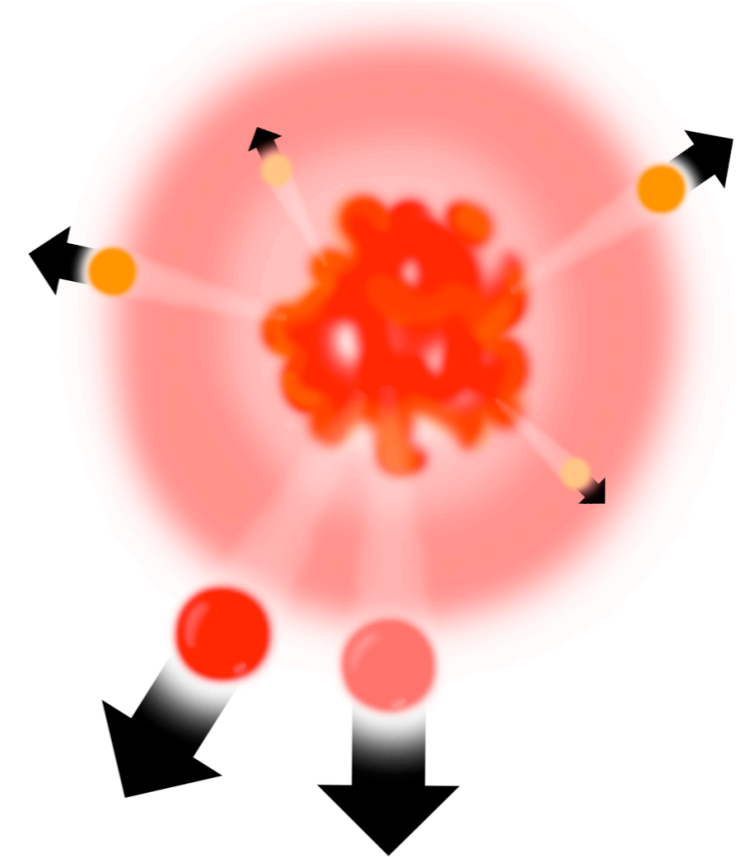


illustration: Alex Doig

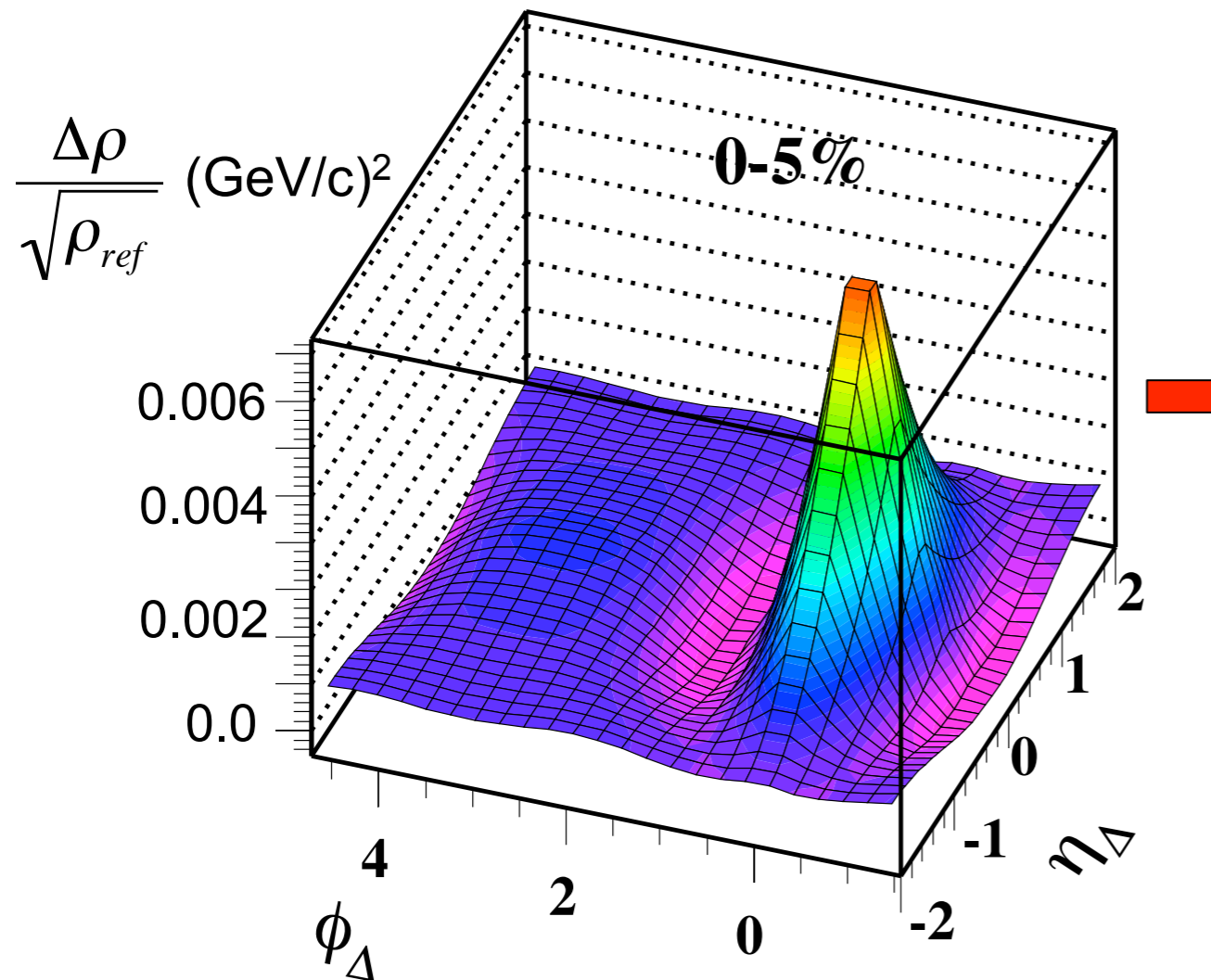
Peak indicates:

- particles with above average momentum tend to come out together
- consistent with being born out of the same high T lump (hotspot)

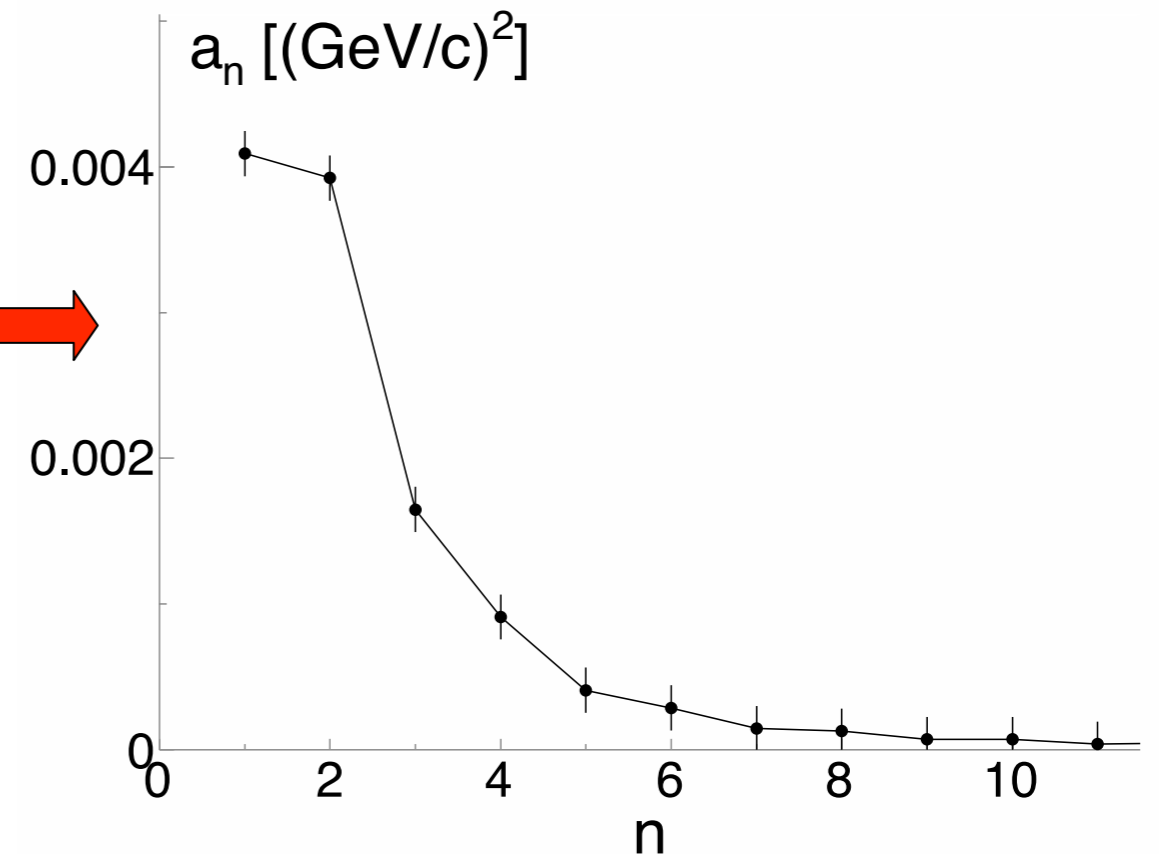
Power Spectrum

Au+Au at 200 GeV

$\Delta\eta = 0$



STAR Collaboration J. Phys. G 32, L37 (2006)

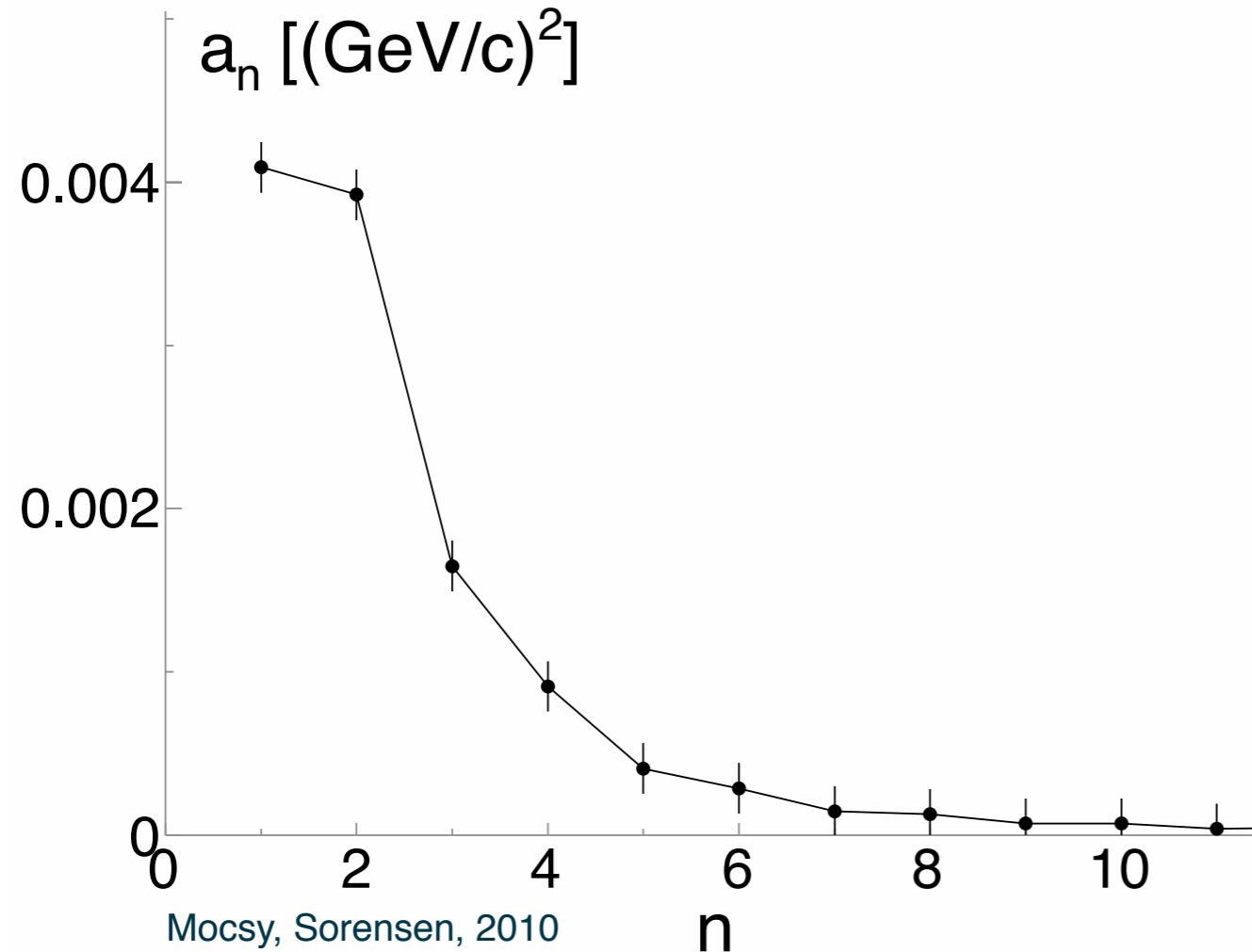


$$a_n = \frac{2}{\pi} \int_0^\infty f(\Delta\phi) \cos(n\Delta\phi) d(\Delta\phi)$$

This is the power of the harmonic \$n\$.

Power Spectrum

Au+Au at 200 GeV

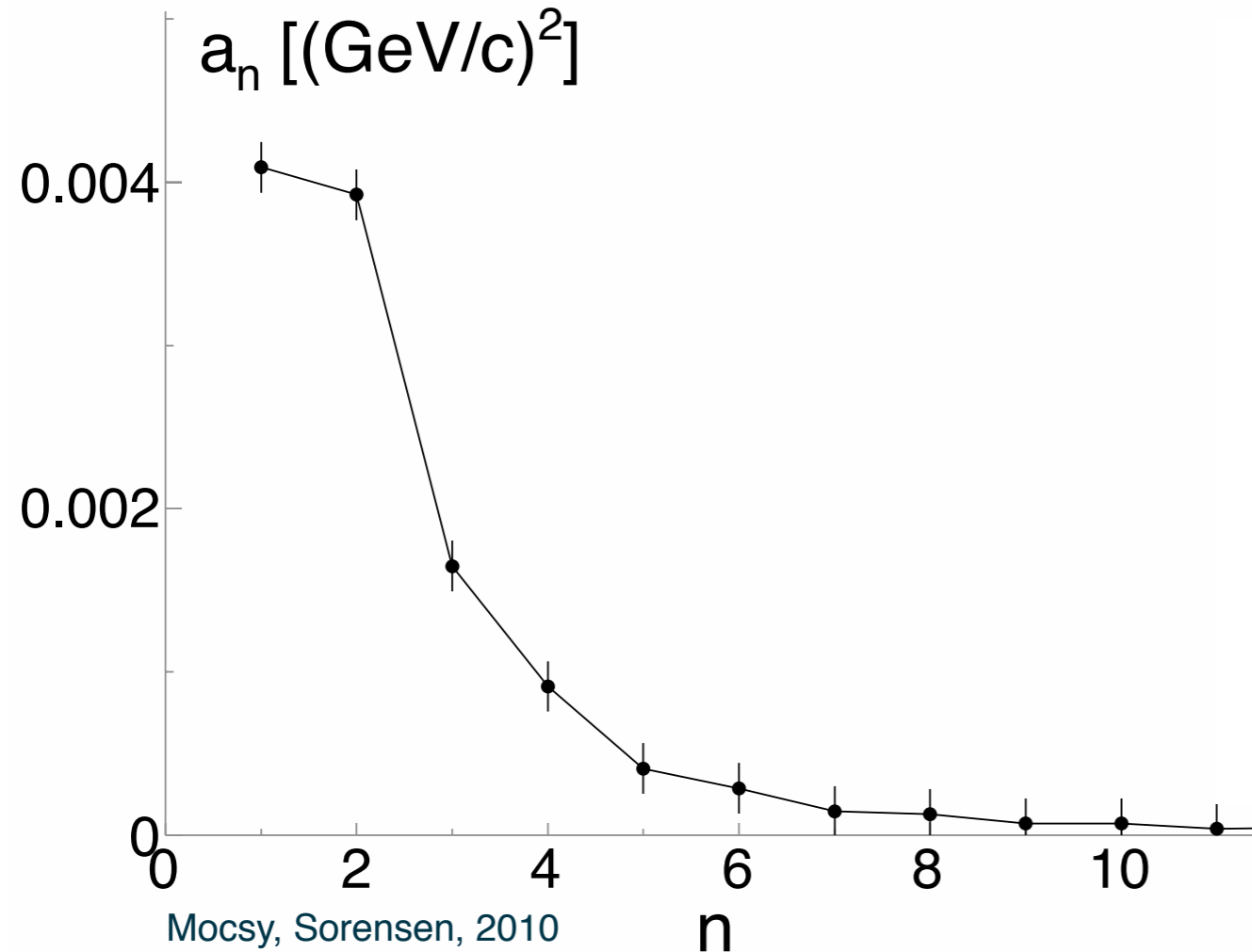


Most power in lowest modes.
Power drops off rapidly with n

Appears to be dominated by
viscous(-like) effects

Power Spectrum

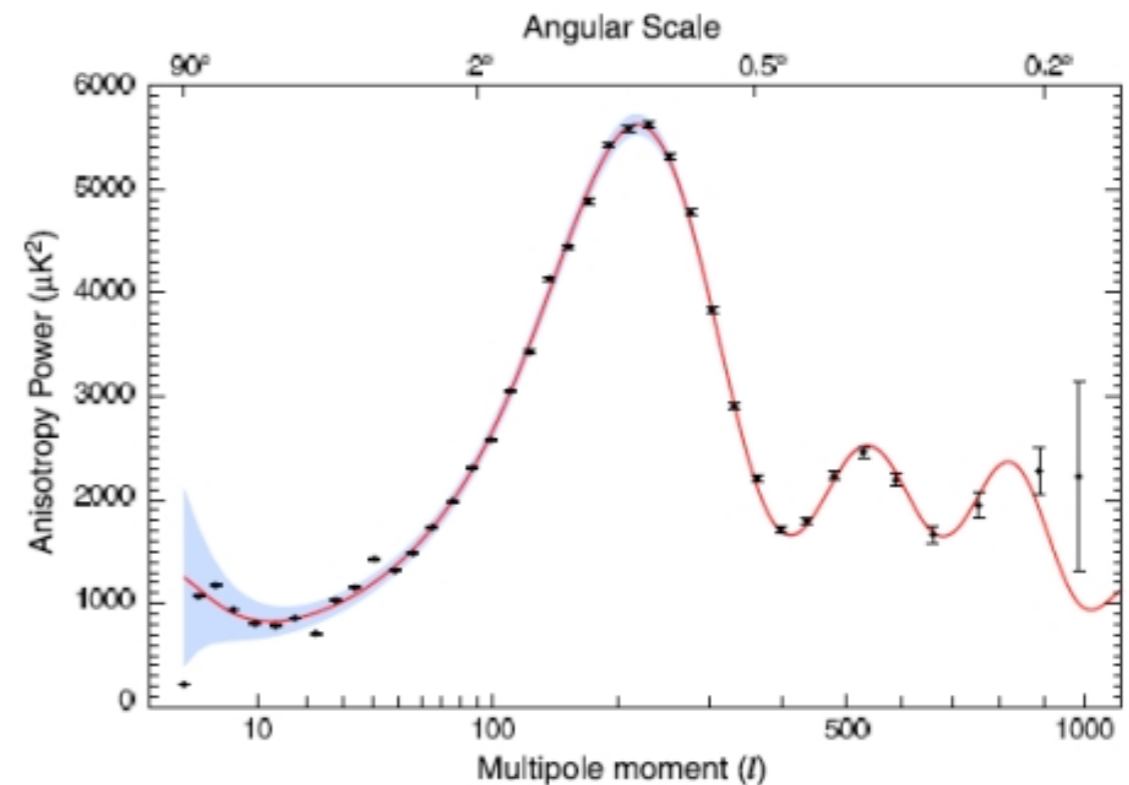
Au+Au at 200 GeV



Most power in lowest modes.
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Our universe



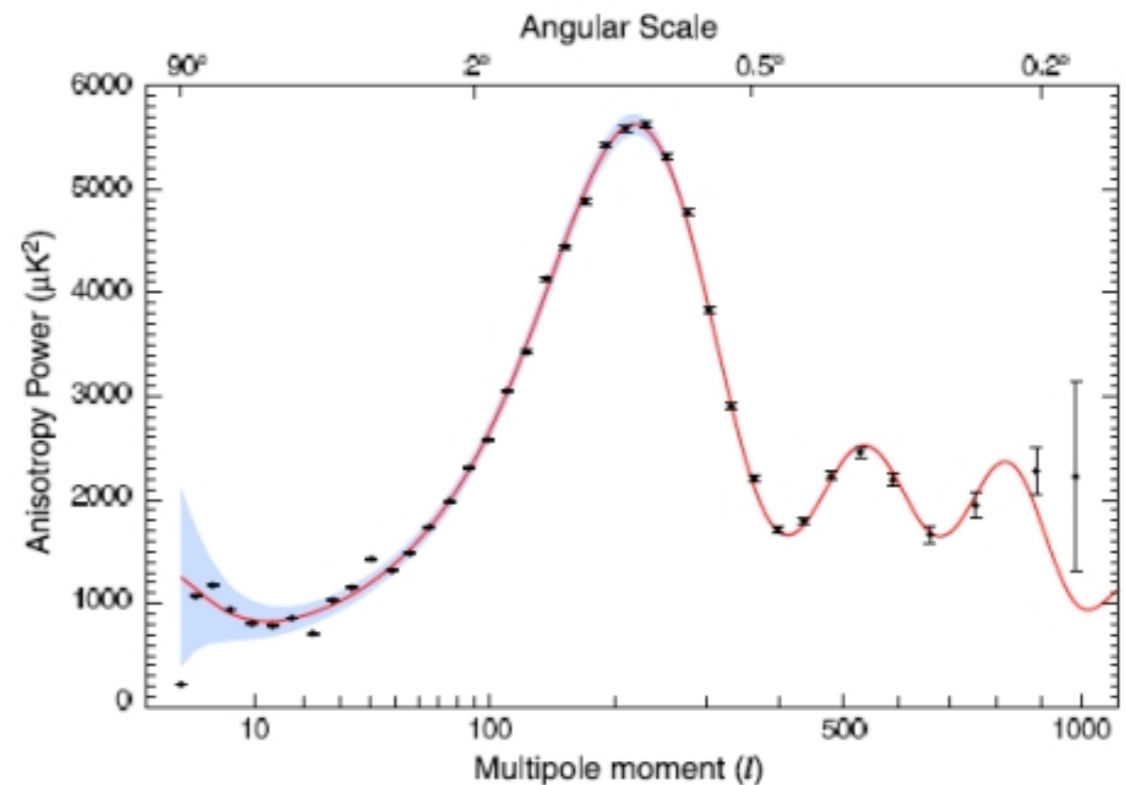
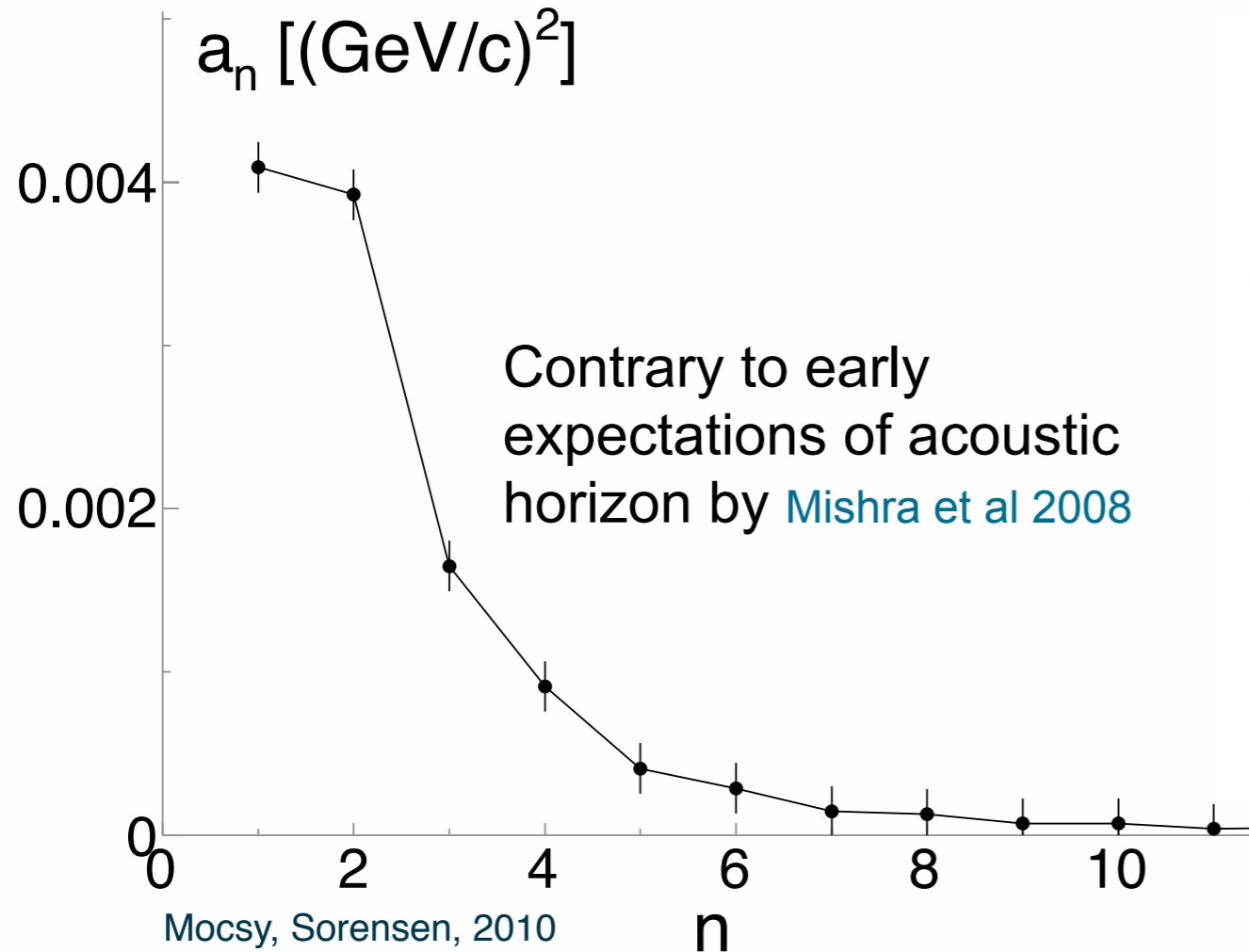
Low modes suppressed
Acoustic oscillations at high modes.

Effects of horizon apparent

Power Spectrum

Au+Au at 200 GeV

Our universe



Most power in lowest modes.
Power drops off rapidly with n

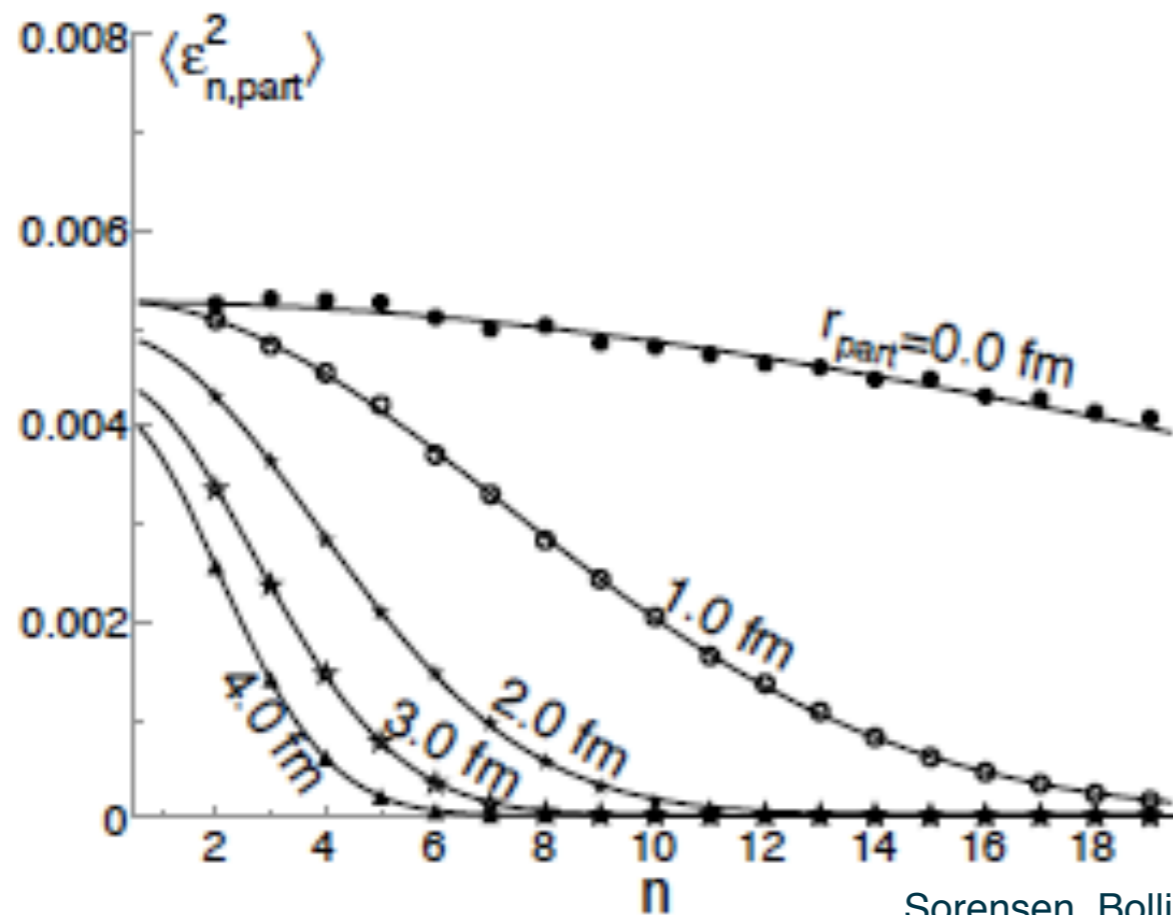
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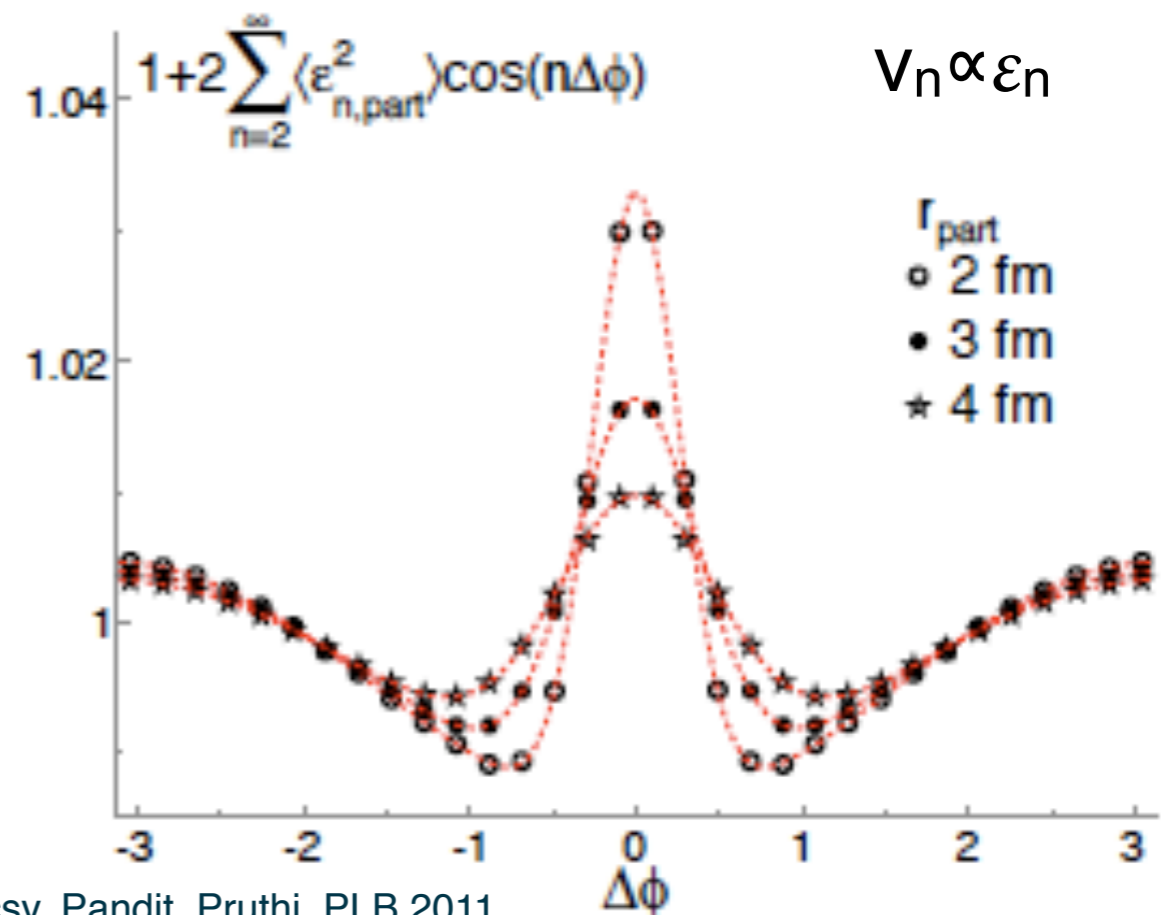
Effects of horizon apparent

Eccentricity and Correlations

Eccentricity at different harmonics leads to **two-particle correlations** similar to those observed in the data



Sorensen, Bolliet, Mocsy, Pandit, Pruthi, PLB 2011



Smearing out the positions of participants

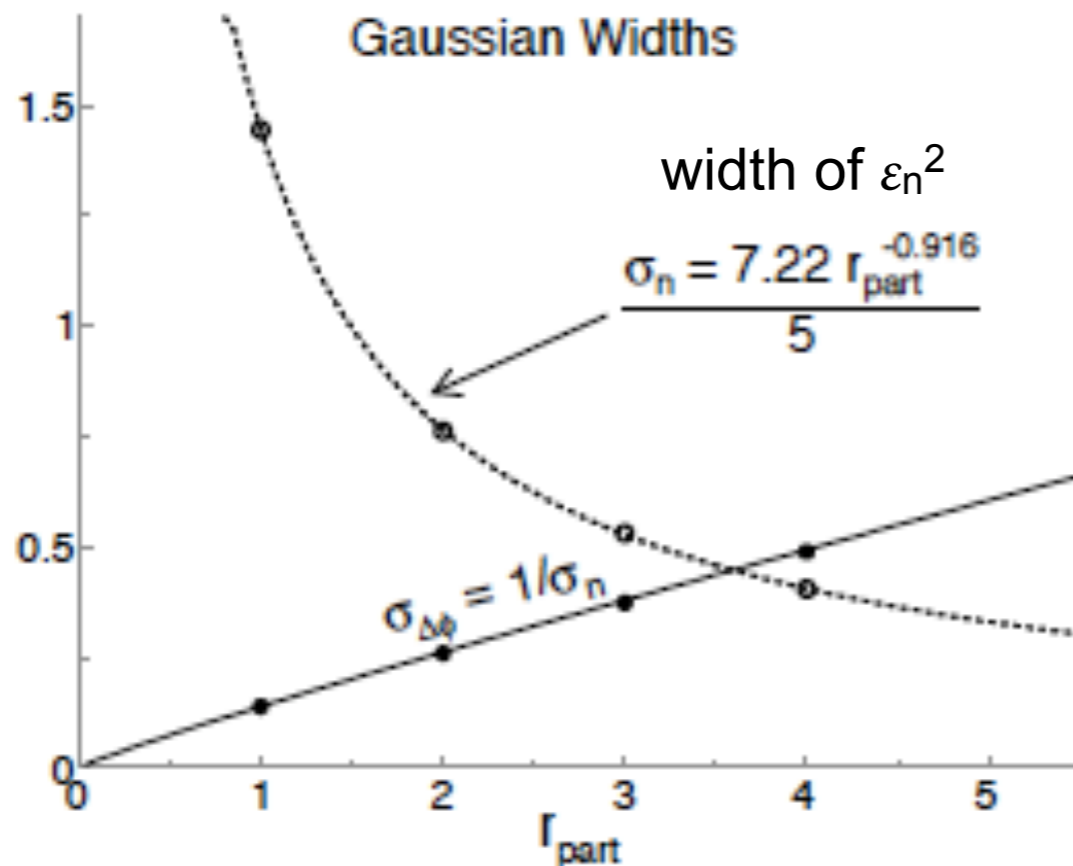
- washes out higher harmonics

- broadens the near-side peak

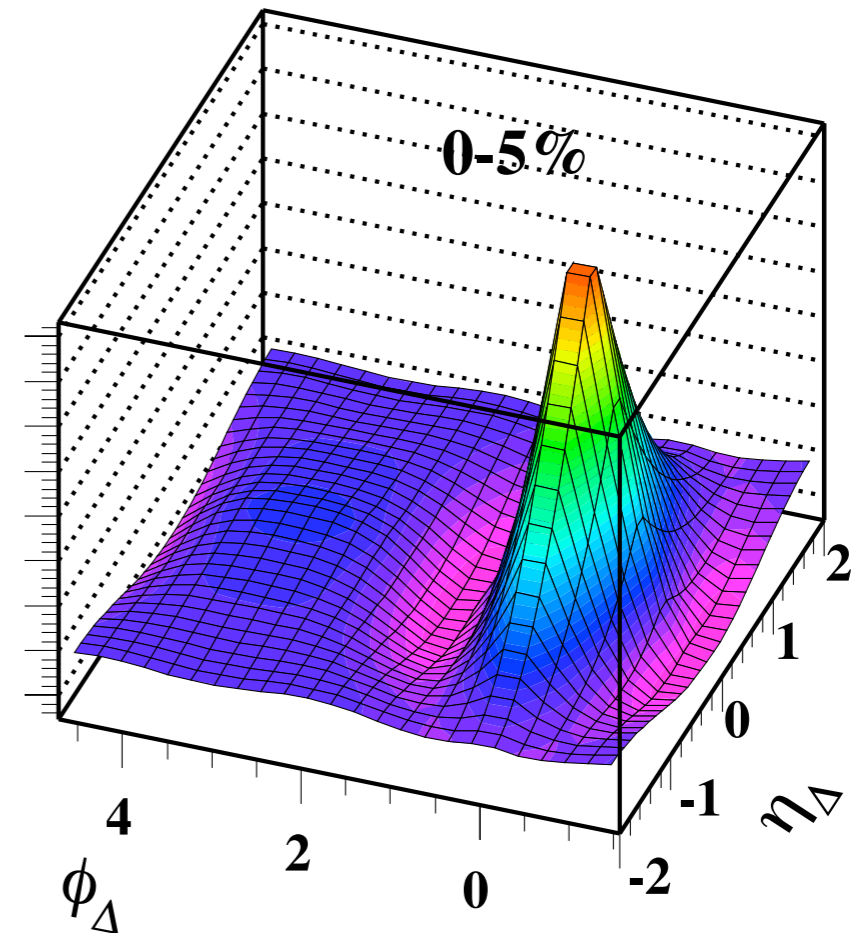
Several effects (like viscosity, free streaming) can have the same effect.

Width of the Correlations

The width depends on the length scales



Sorensen, Bolliet, Mocsy, Pandit, Pruthi, PLB 2011



STAR Collaboration J. Phys. G 32, L37 (2006)

$$\text{length scale } l = \left(7.22\sigma_{\Delta\phi}\right)^{1.09}$$

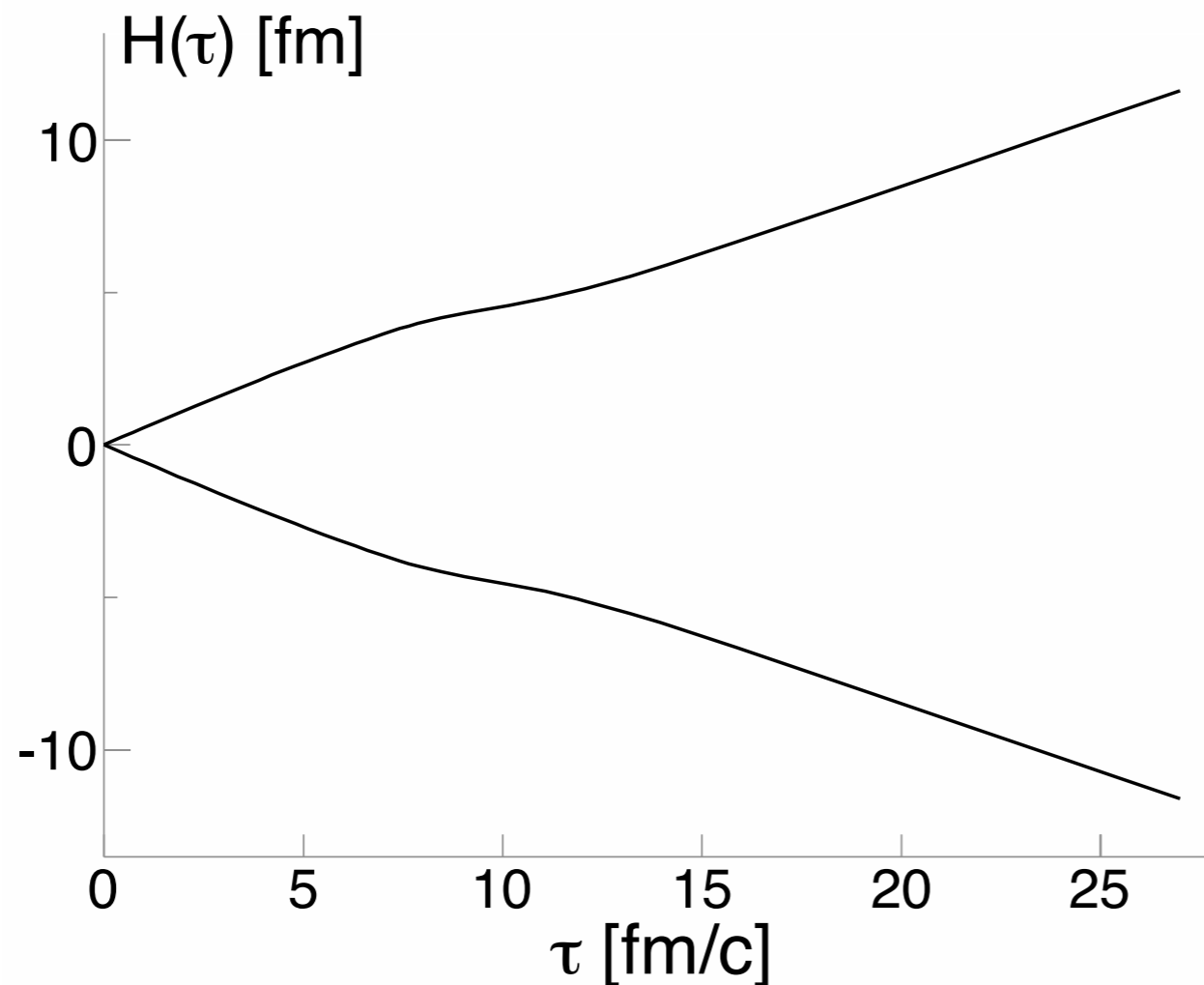
Width of pt correlations consistent with a length scale of 4-5 fm

Not a small viscosity?!

But width can reflect many effects (e.g. thermal at hadronization)

Acoustic Horizon

- Another important length scale:
H = distance density perturbations will have travelled



$$H(\tau) = \int_0^{\tau} c_s(\tau') d\tau'$$

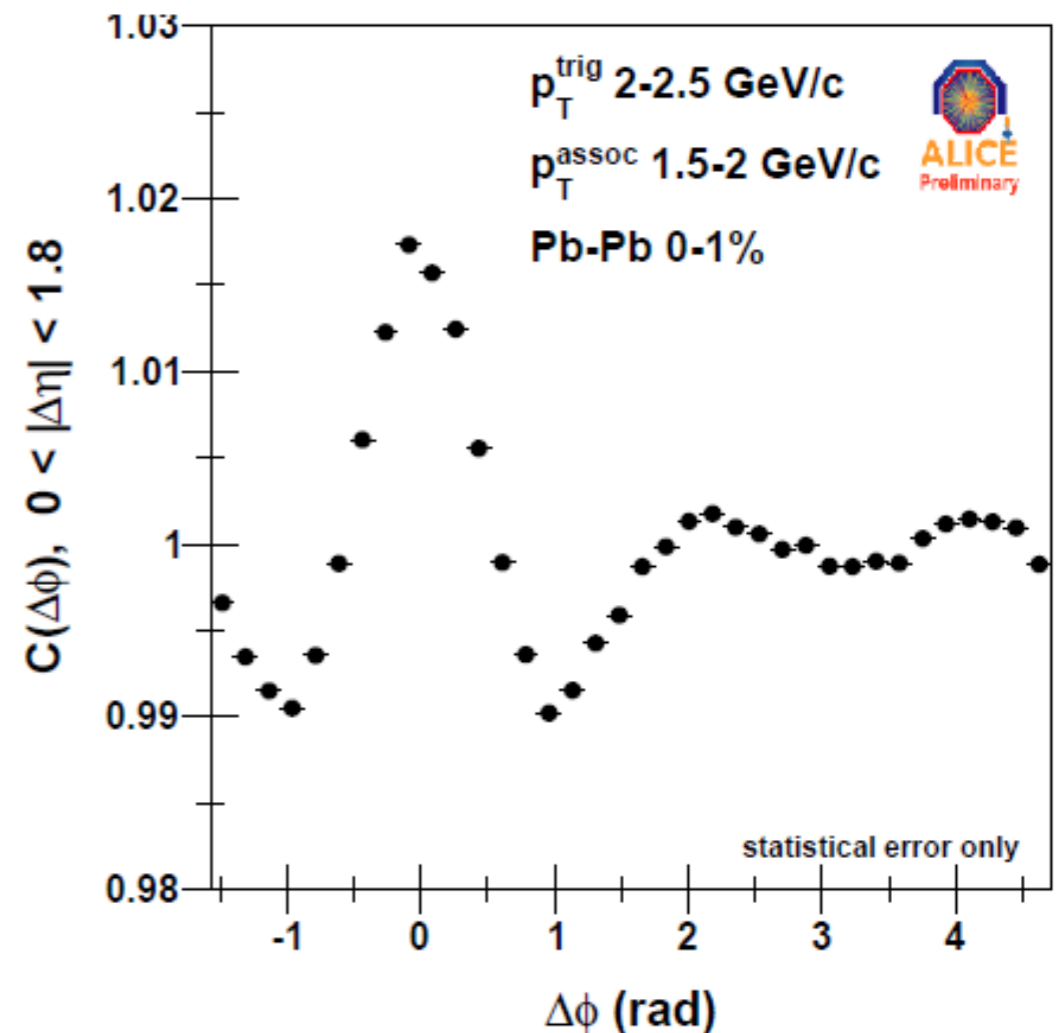
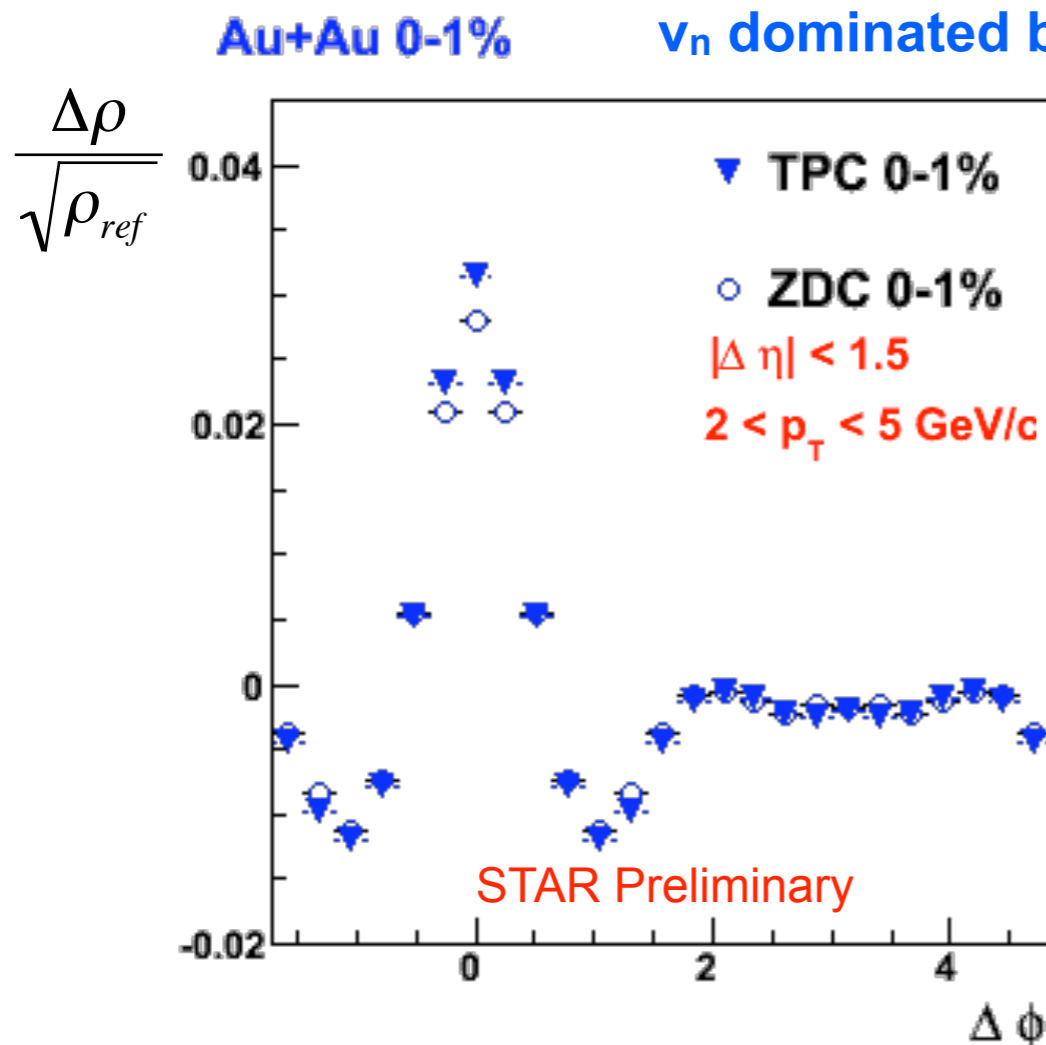
Mocsy, Sorensen, 2010
also Staig, Shuryak, 2010

$c_s(e)$ from lattice QCD
Huovinen, Petreczky, Nucl. Phys.A (2010)
 $e(t)$ from hydro to get $c_s(t)$
Kolb, Heavy Ion Phys. (2004)

- Effects of H freeze-out should show up in the power spectrum:
lengthscales larger than the horizon remain super-horizon

Effect of the Acoustic Horizon?

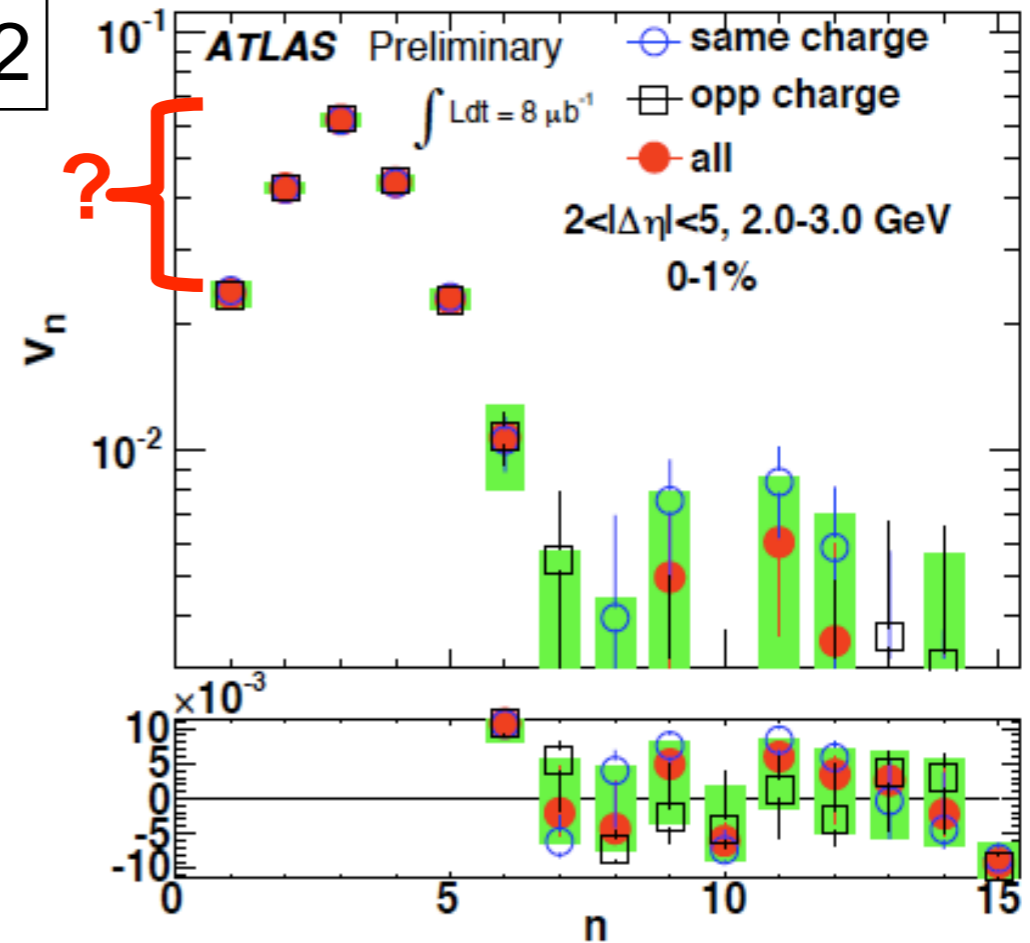
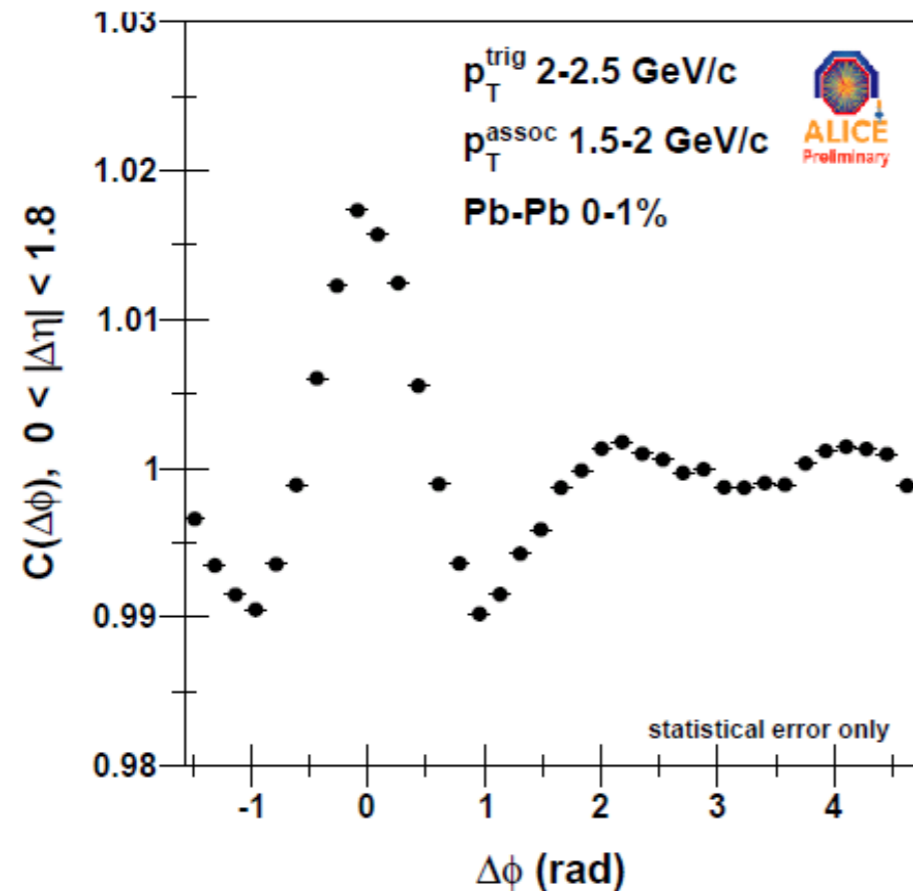
- An acoustic horizon should suppress lower harmonics compared to higher harmonics (Mishra et al); the opposite of viscous effects (Mocsy, Sorensen)



- At both RHIC and LHC, intermediate p_T correlations in very central collisions exhibit a strong $n=3$ modulation

Power Spectrum at Intermediate p_T

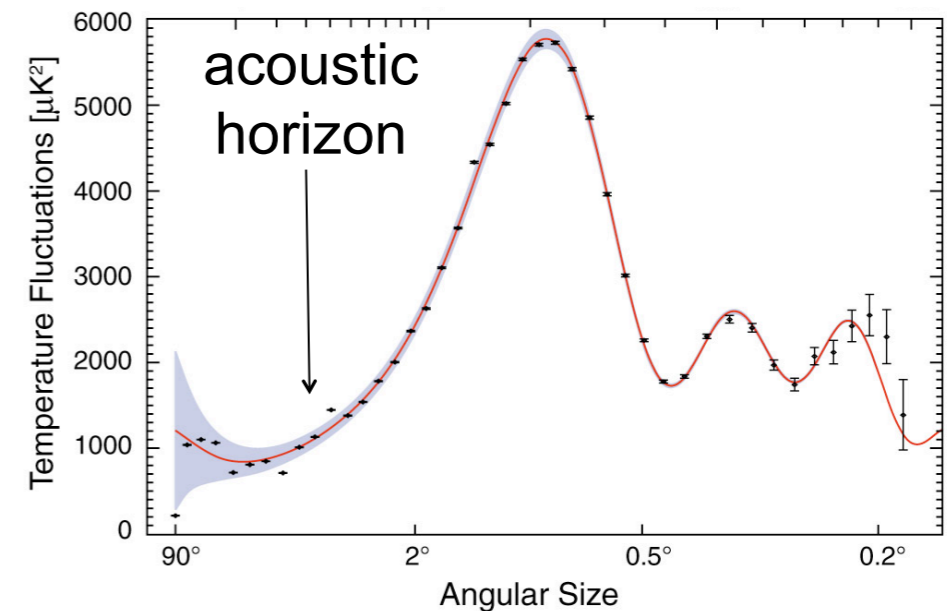
$n=3$ larger than $n=2$



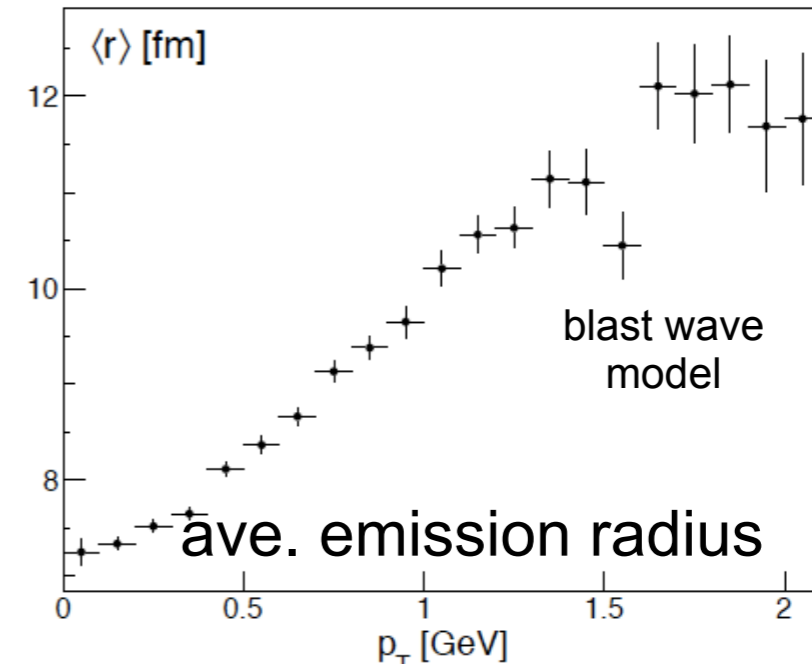
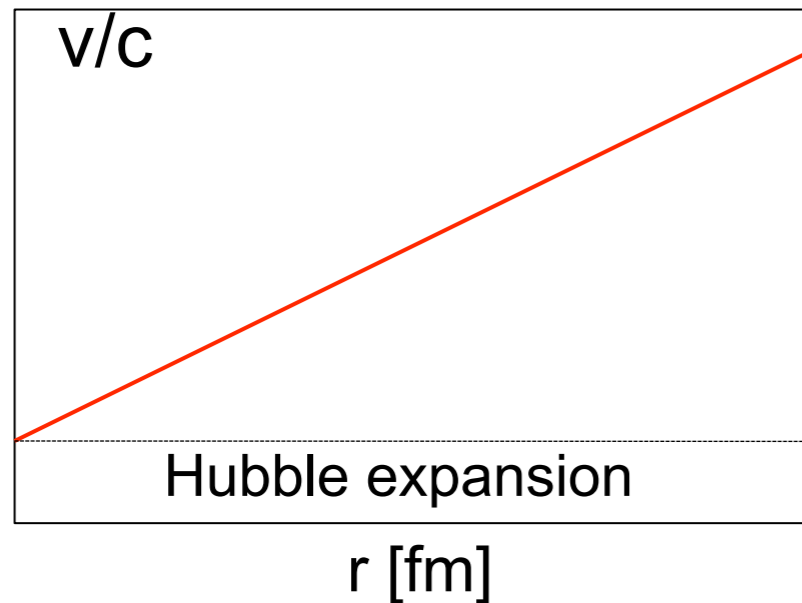
Is this caused by the acoustic horizon?

What other possible explanations?

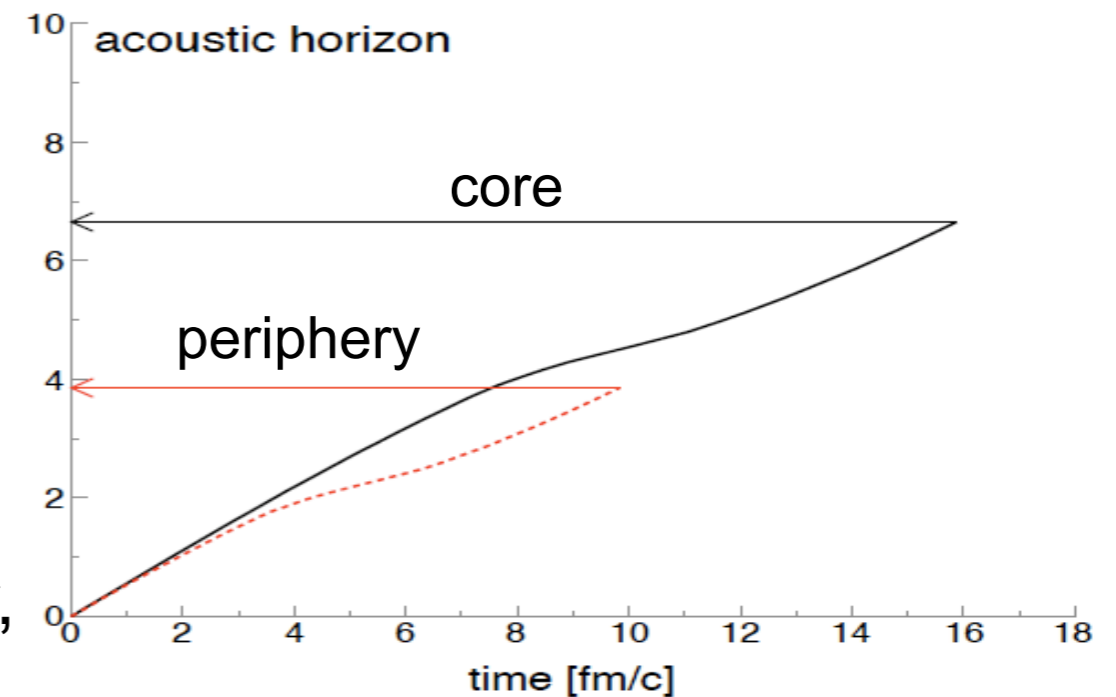
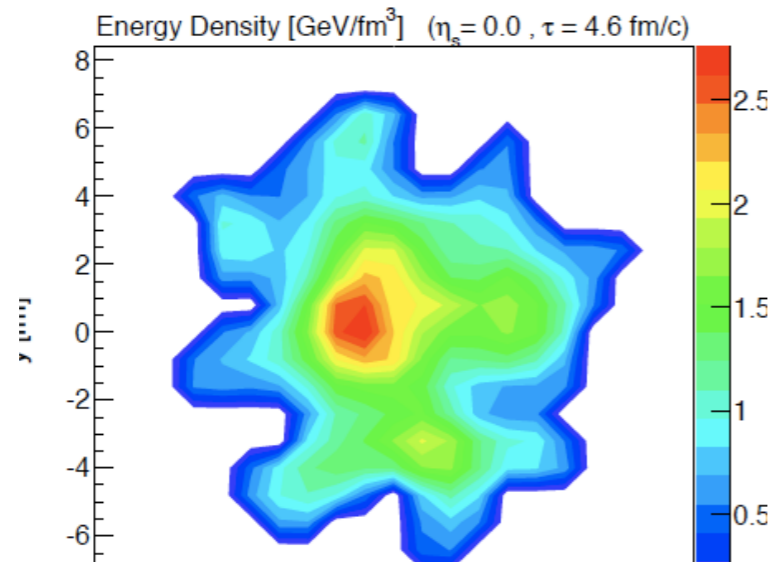
Why **only** at intermediate p_T ?



n=3 larger than n=2 Possible Explanation



In a medium undergoing hubble expansion, intermediate p_T particles are preferentially emitted from the periphery



Horizon should be smaller on the periphery, perhaps leading to $n=3 > n=2$

Summary/Conclusion

The **power spectrum** of heavy ion collisions shows that higher harmonics are suppressed: as expected for finite size participants and viscous effects

Identified a relevant large scale $\sim 4\text{-}5$ fm (implies a rather large viscosity)

mean free path? free-streaming? thermal broadening?

Correlations can reflect a competition between causality (horizon) and viscosity

viscous effects suppress higher harmonics
causality suppresses lower harmonics

Identified the acoustic horizon as a possible explanation for $v_3 > v_2$ at intermediate p_T

The End

Final Note

Á.M., P. Sorensen arXiv: 1008.3381 [hep-ph]
Á.M., P. Sorensen arXiv: 1101.1926 [hep-ph]
P. Sorensen, B. Bolliet, Á.M., Y. Pandit, N. Pruthi arXiv:
1102.1403 [nucl-th]
and
[www. soundofthelittlebang.com](http://www.soundofthelittlebang.com)



illustration: Alex Doig

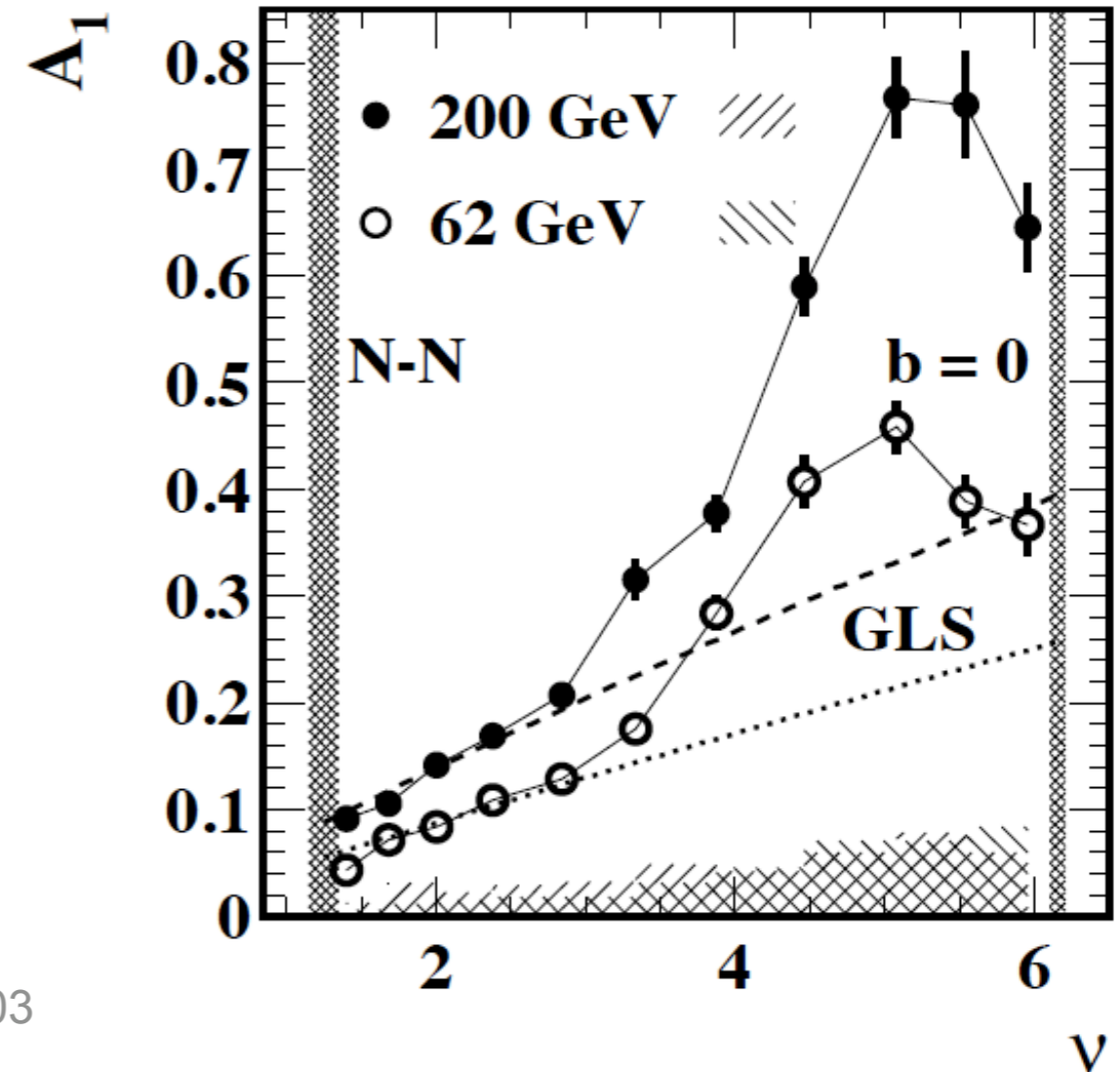
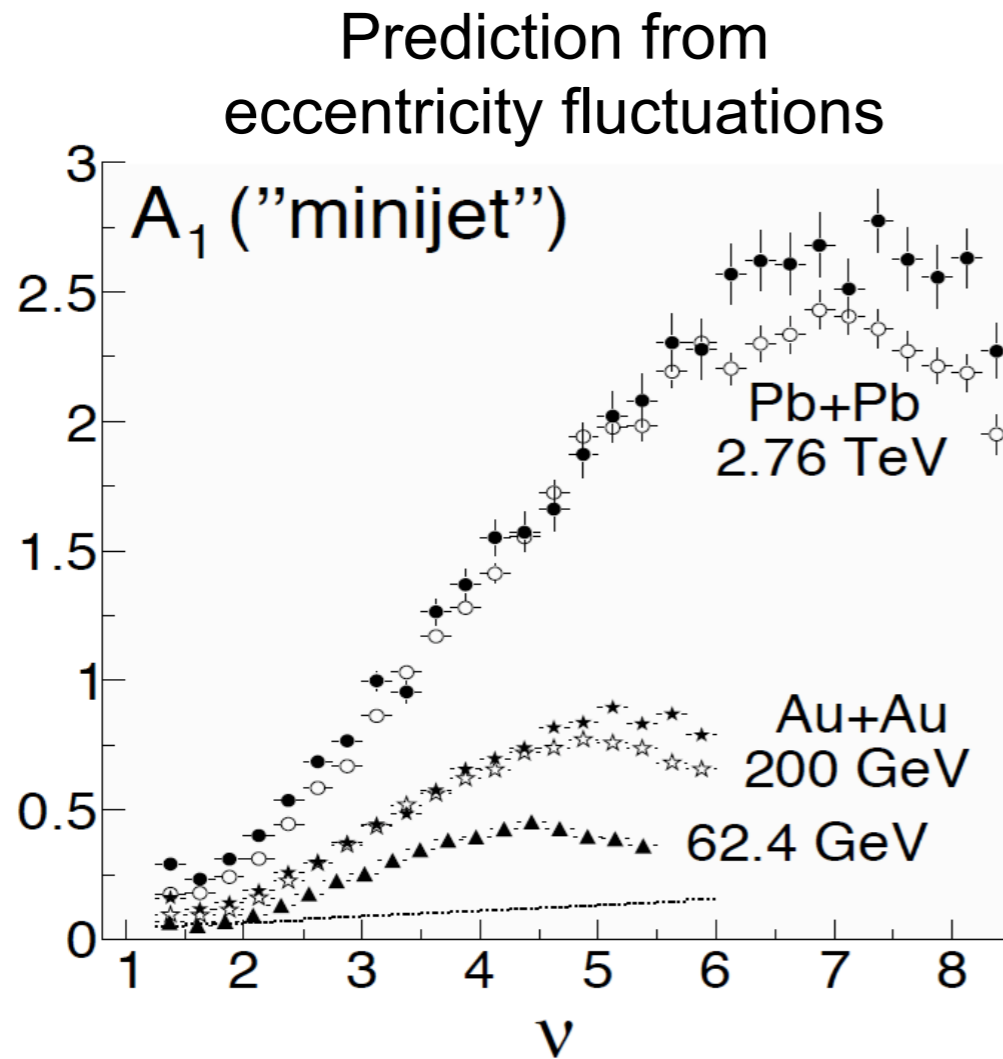
Backups

We demonstrated that **eccentricity fluctuations naturally lead to ridge-like correlations** with a width dependent on the length-scales in the system

Rise and Fall of the Ridge

The ridge amplitude A_1 exhibits a drop in central collisions. The drop is natural for eccentricity fluctuations.

STAR Data <http://arxiv.org/abs/1109.4380>

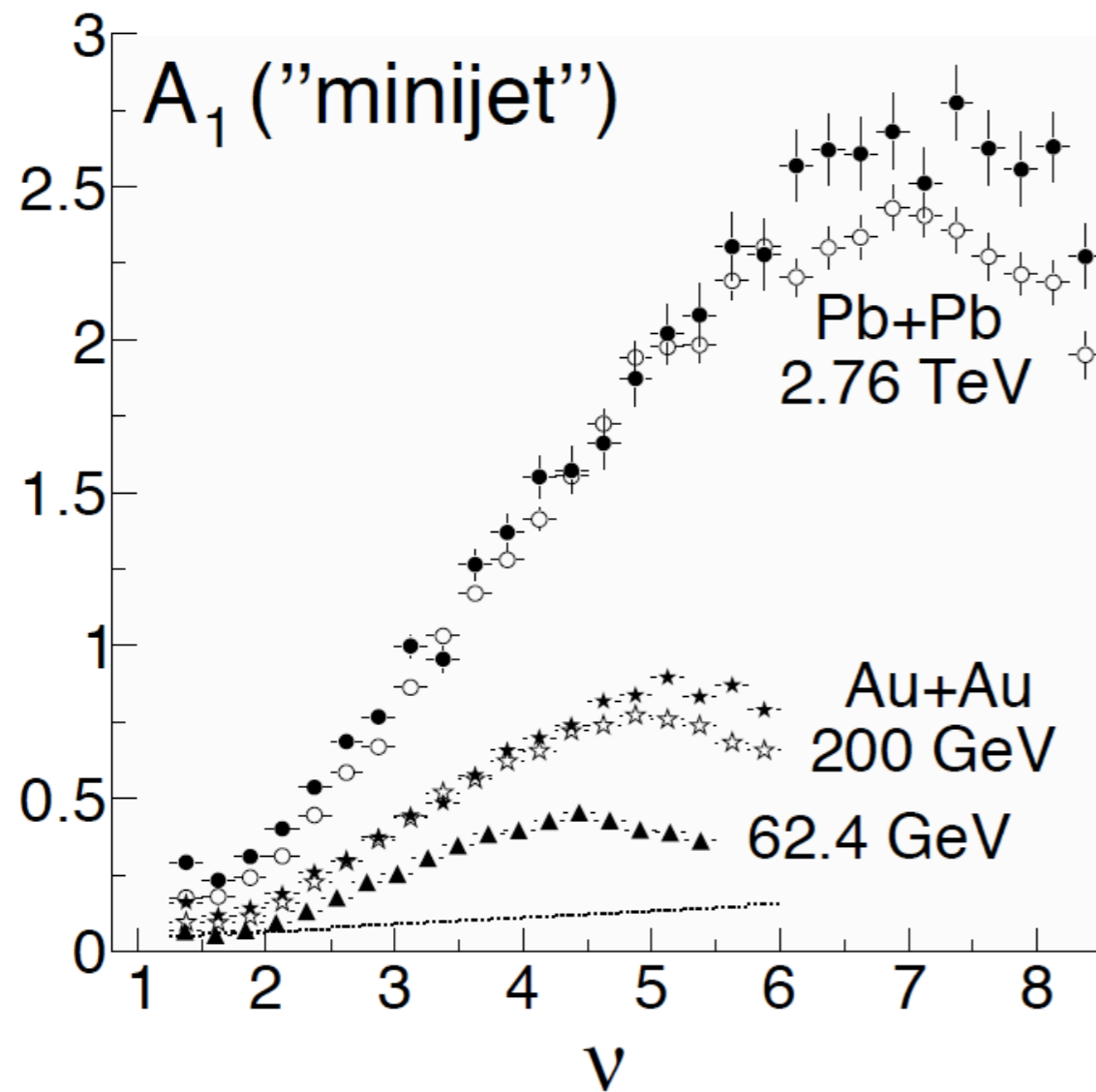


P. S., B. Bolliet, A. Mocsy, Y. Pandit, N. Pruthi, arXiv:1102.1403

Prediction: rise and fall of the ridge will be present at all energies: *it's a feature of the overlap geometry*

LHC Predictions

A_1 will be several times larger at the LHC: *driven by increased multiplicity and flow*

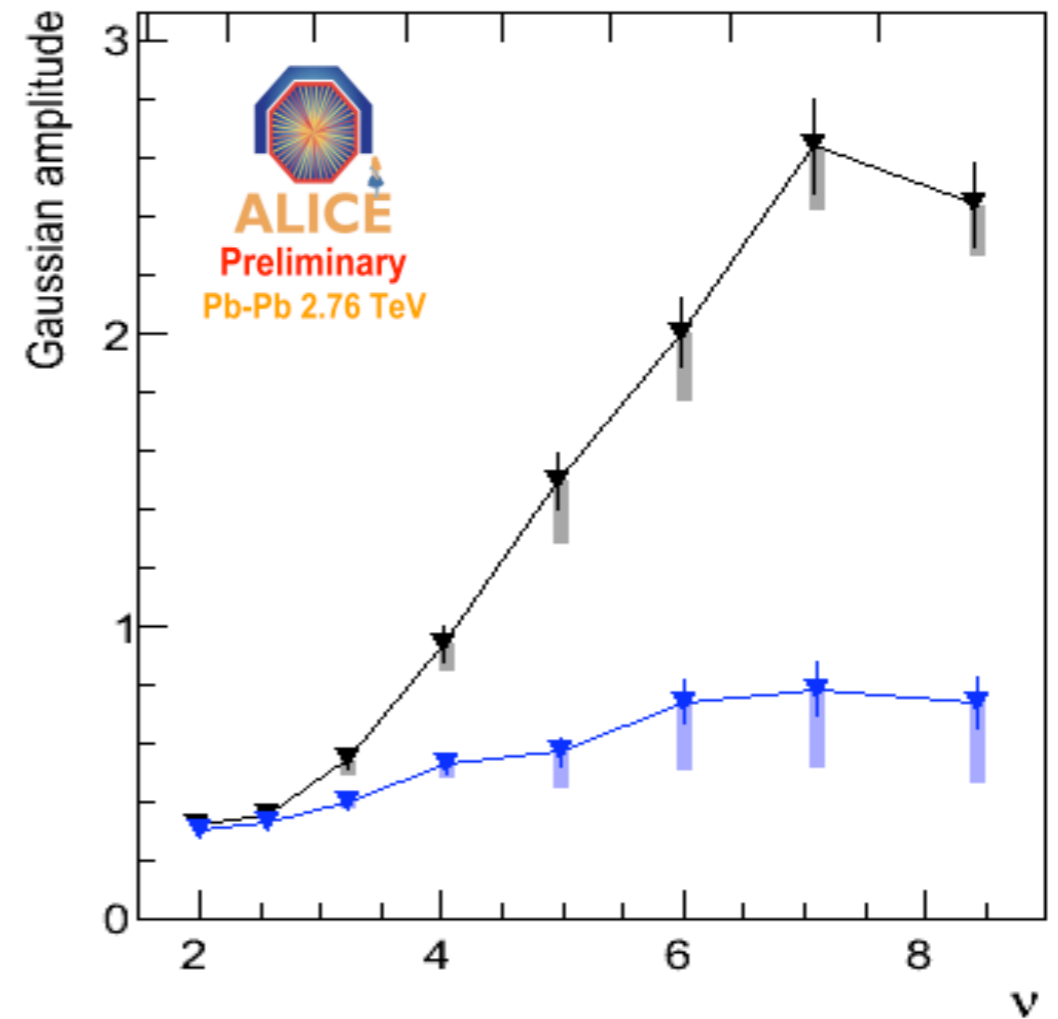
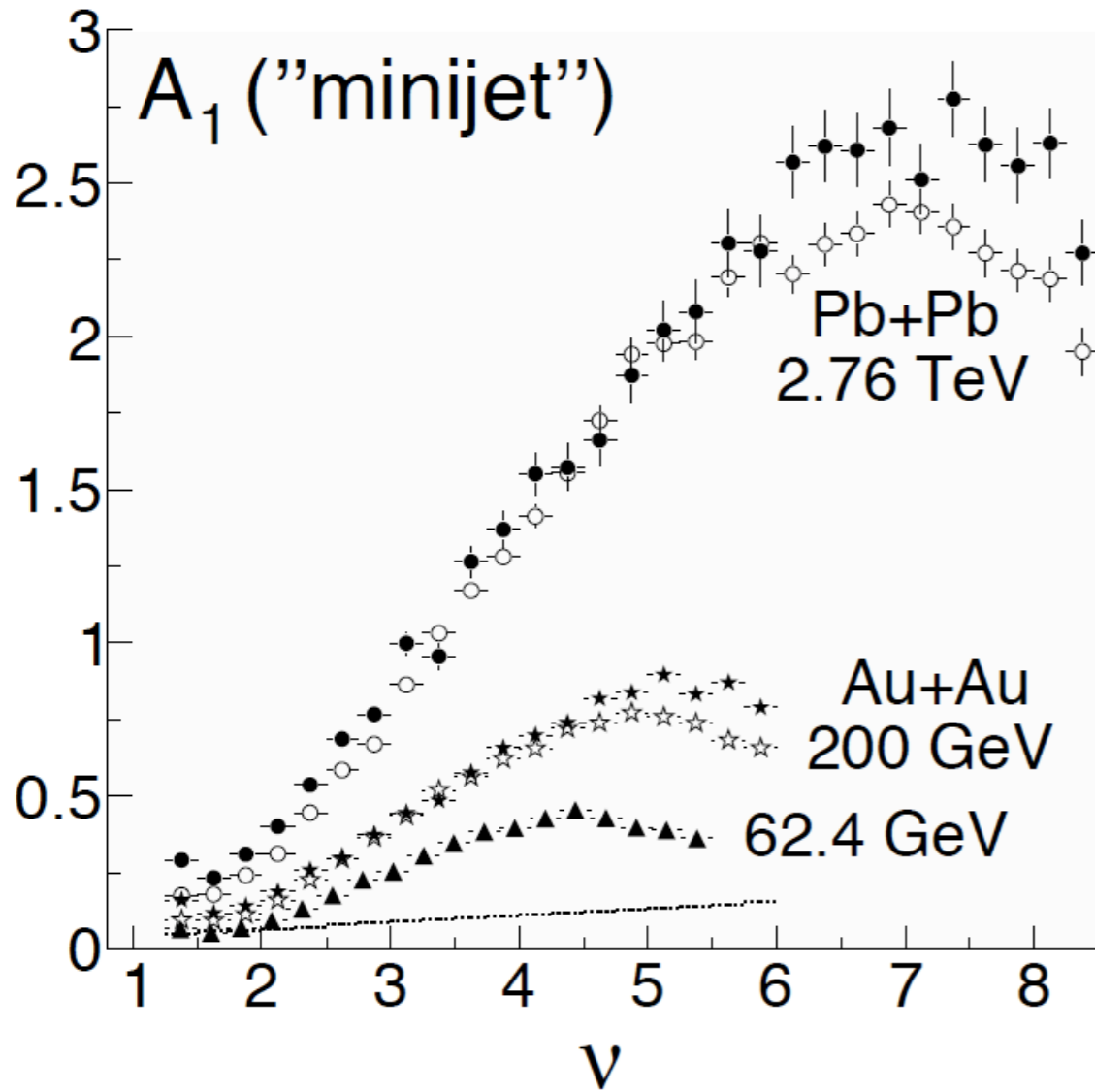


P. S., B. Bolliet, A. Mocsy, Y. Pandit, N. Pruthi, arXiv:1102.1403

Data seems to favor eccentricity fluctuations as the explanation for the ridge

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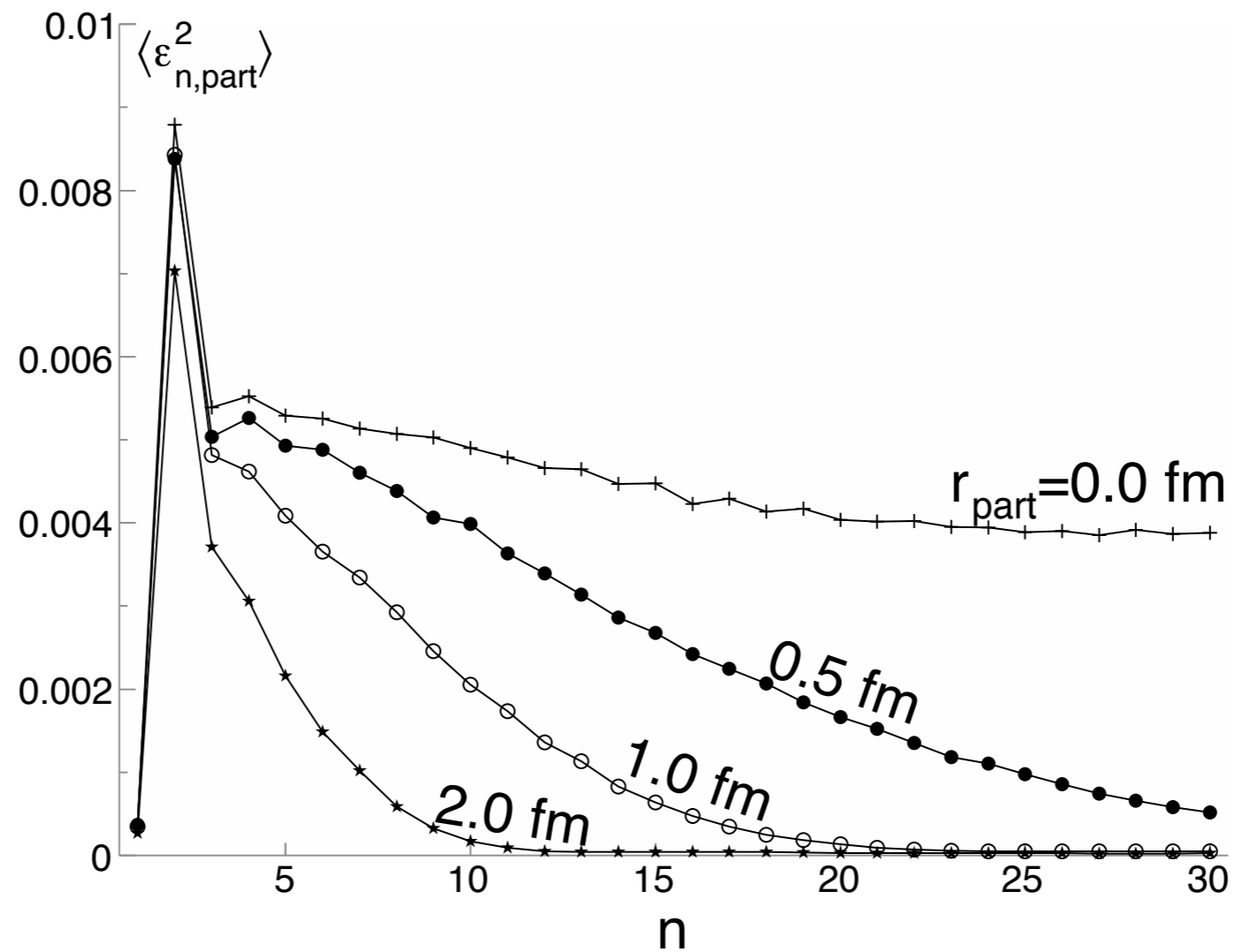


A. Timmins, QM2011

P. S., B. Bolliet, A. Mocsy, Y. Pandit, N. Pruthi, arXiv:1102.1403

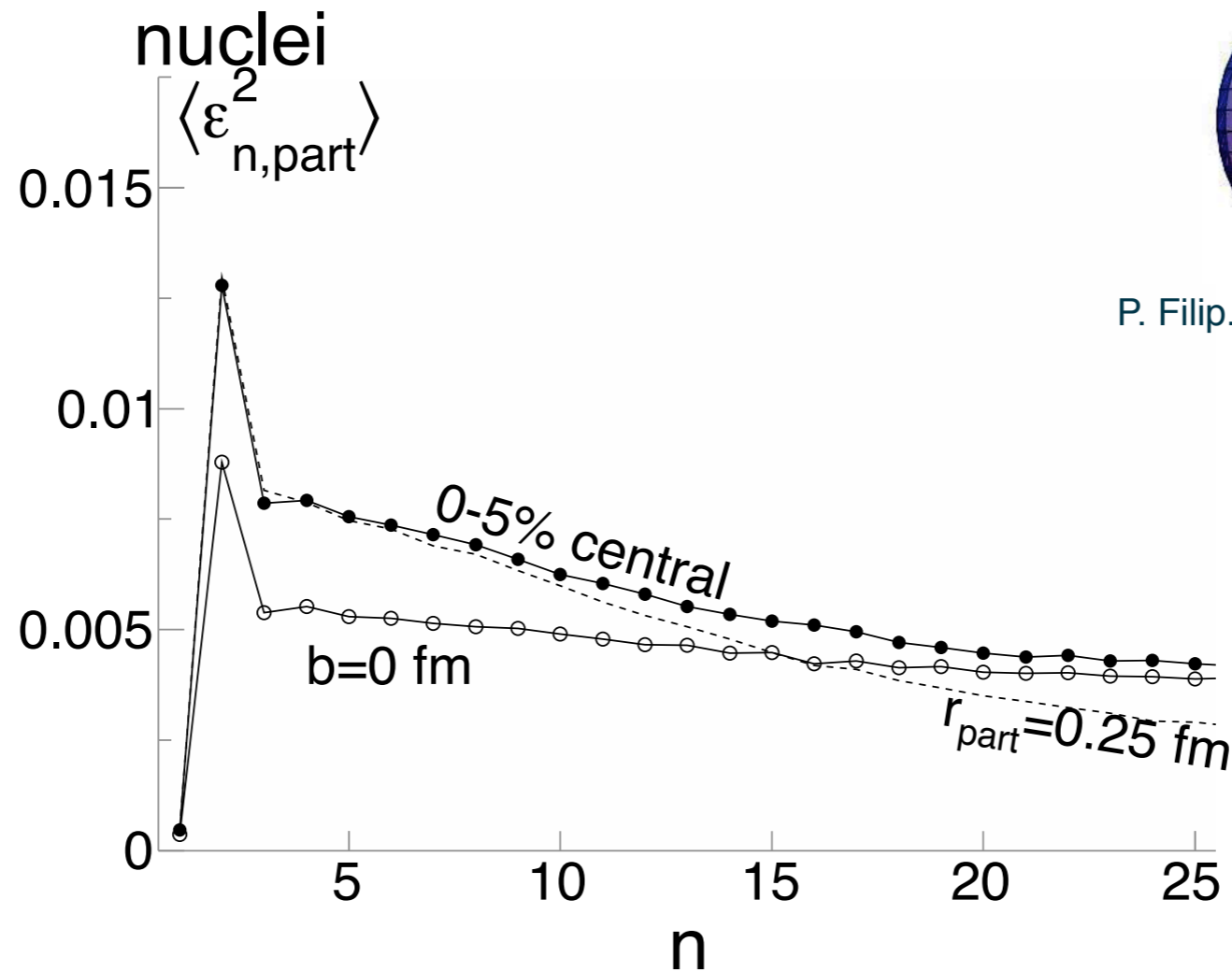
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Participant size dependence



Participant Eccentricity

Monte Carlo Glauber with non-spherical Au

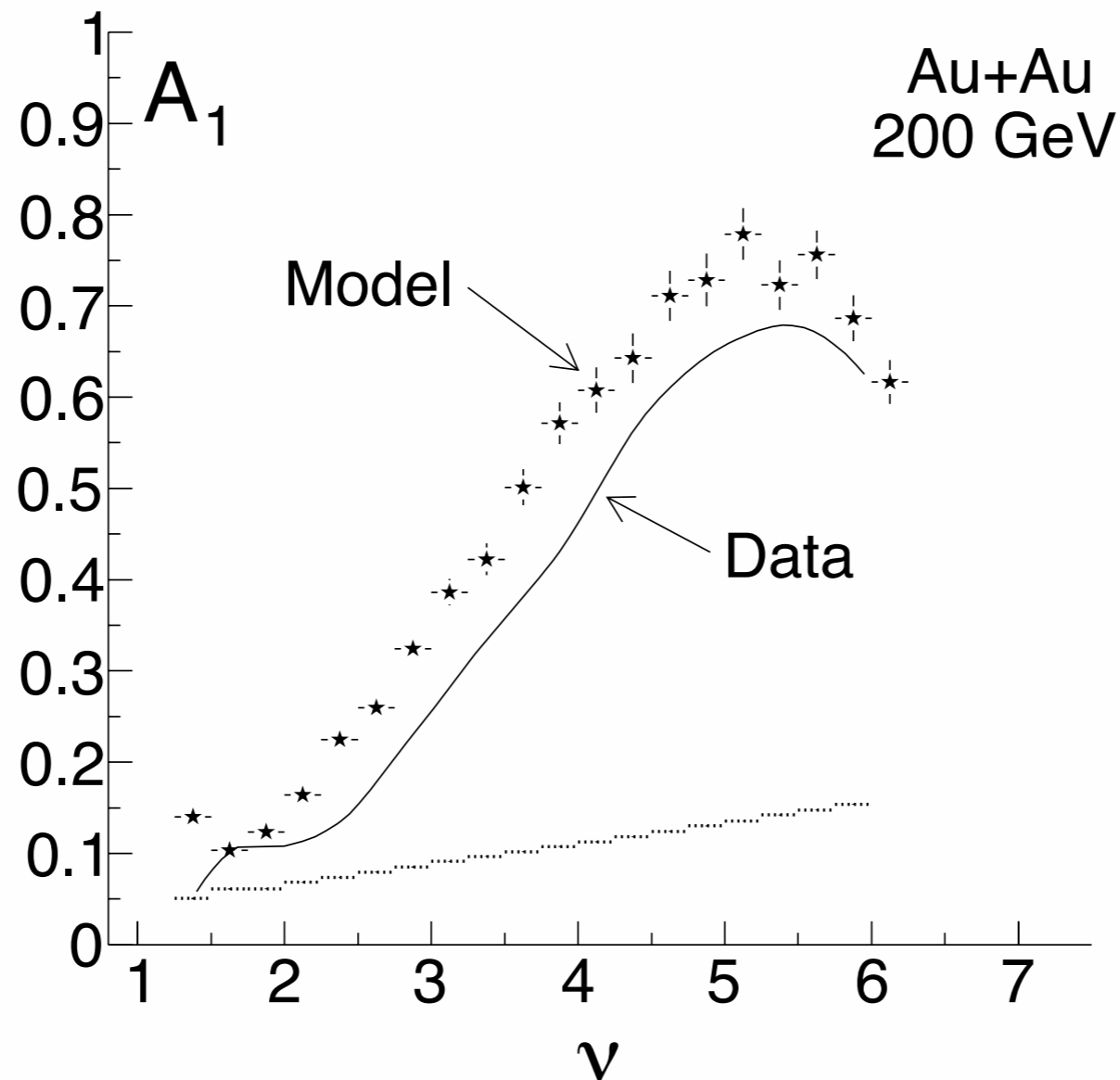


$n=2$ spike due to oblateness of the Au nucleus (even for $b=0$)

$n>2$ at $b=0$ participant eccentricity is nearly independent of n (only N_{part} dependence)

n.b. finite-sized participants or effect of free-streaming cause a drop with n

Correlations From Initial State



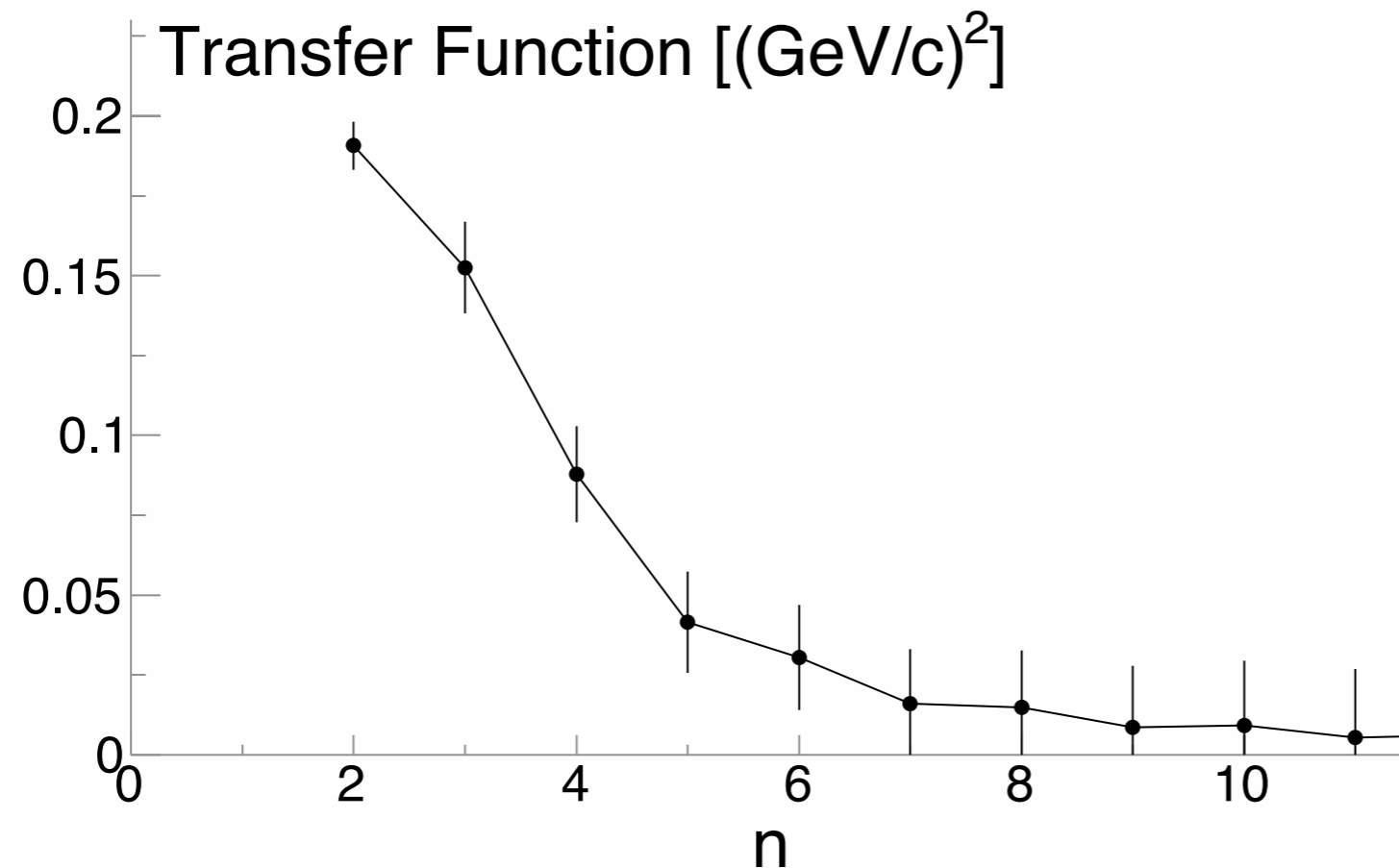
The correlations expected from the initial state density fluctuations transferred into momentum space matches the data

Heavy ion collisions convert spatial anisotropy to momentum anisotropy

Transfer-Function

tells how well coordinate space anisotropy is converted to momentum space

$$a_n / \langle \varepsilon_{part,n}^2 \rangle$$



$$l_{mfp} \cong 2\pi \langle R \rangle / n_c$$
$$\langle R \rangle \cong 3 \text{ fm}$$
$$n_c = 6$$
$$l_{mfp} \cong 3 \text{ fm}$$

$\langle R \rangle$ average radial position of participants

Drop expected due to l_{mfp} cutting off the smaller lengthscales (high n)

Conversion is inefficient for modes $n > 6$

Transfer function may be used to estimate the mean free path

n.b. full simulation needed, other scales ($1/Q_s$, $1/T$, $c\tau$, H , ...) could also be important