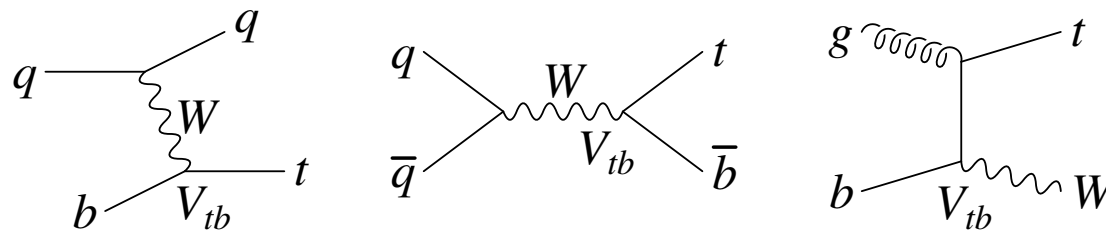


# WHAT DOES SINGLE-TOP-QUARK PRODUCTION TEACH US ABOUT LHC PHYSICS?



Zack Sullivan

Southern Methodist University

May 15, 2007



# Thanks

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For their elucidating insights:

Brian Harris, Eric Laenen, Pavel Nadolsky, Lucas Phaf, Tim Stelzer, Tim Tait,  
Stefan Weinzierl, Scott Willenbrock

CDF single-top group

$D\emptyset$  single-top group

For their direct support:

Southern Methodist University

Argonne National Laboratory

Fermi National Accelerator Laboratory

University of Chicago

University of Illinois



# Contents

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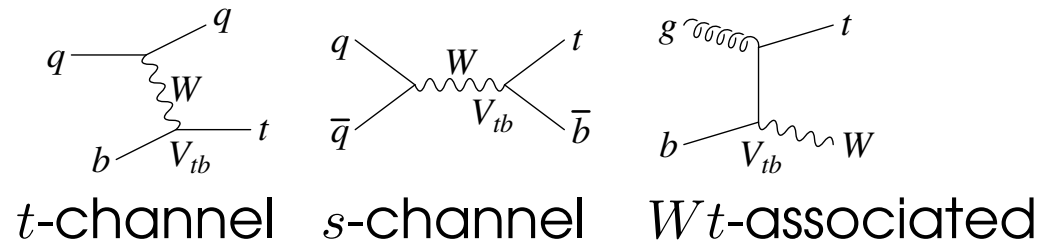
## 1. Why single-top-quark production?

- A traditional view
- A **lasting** view

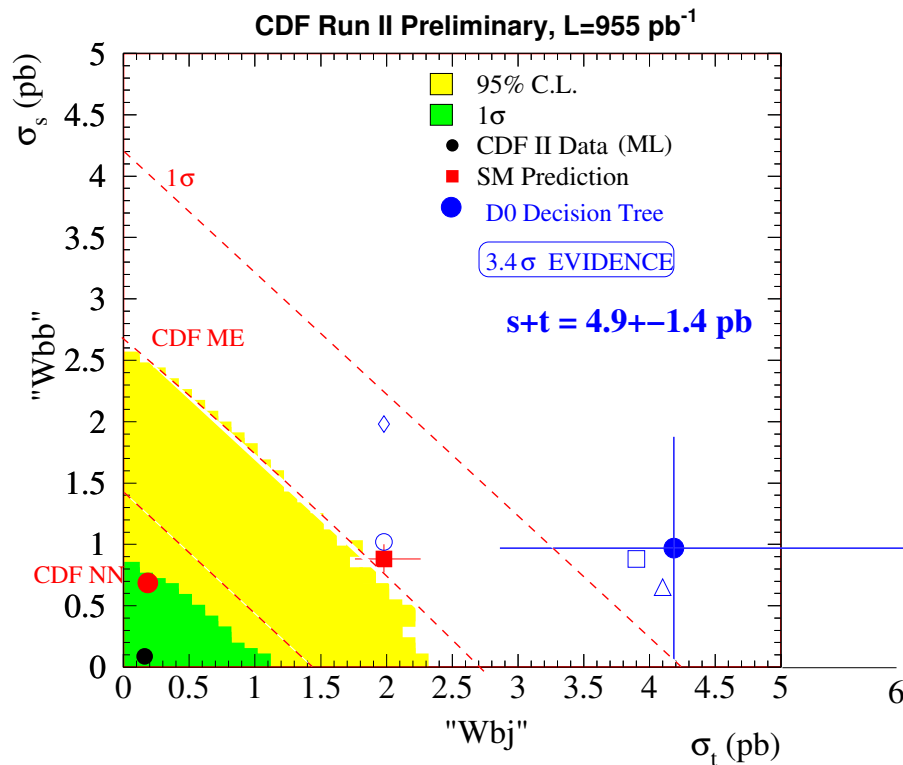
## 2. Angular correlations: the current frontier

## 3. What drives LHC physics?...

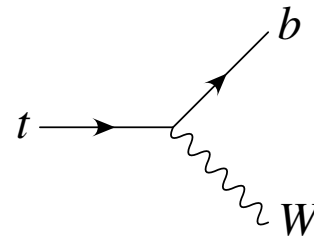
# Evidence for single-top-quark production



This flagship measurement of the Fermilab Tevatron has been sighted.

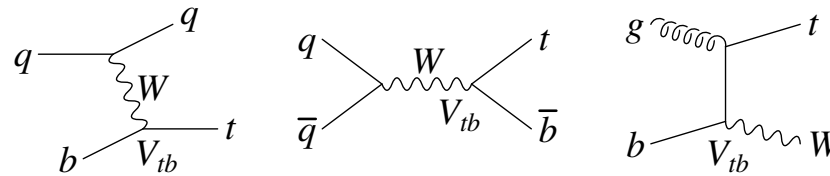


Production modes distinguished by the number of tagged  $b$  jets.

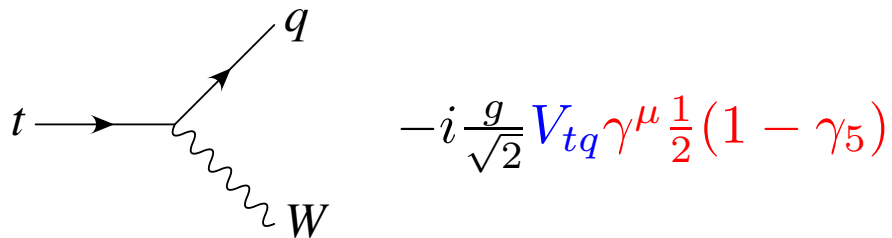


DATA DRIVEN THEORY

# Why we look at single-top-quark production



## Weak interaction structure



Goal: Determine the structure of the  $W$ - $t$ - $q$  vertex.

- Measure CKM couplings  
“direct measurement of  $V_{tb}$ ”
- Measure Lorentz structure  
“spin correlations”

# Why measure CKM elements $V_{tq}$ ?

Assuming 3 generations and unitarity,  $V_{tq}$  are well determined.

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 0.9739 - 0.9751 & 0.221 - 0.227 & 0.0029 - 0.0045 \\ 0.221 - 0.227 & 0.9730 - 0.9744 & 0.039 - 0.044 \\ 0.0048 - 0.014 & 0.037 - 0.043 & 0.9990 - 0.9992 \end{pmatrix}$$

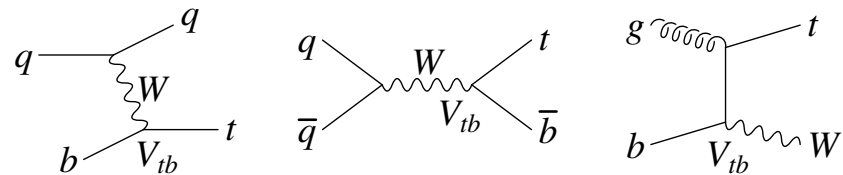
PDG, PLB 592, 1 (2004)

Relaxing the assumption of 3 generations,  $V_{tb}$  is barely constrained.

$$\Rightarrow \begin{pmatrix} 0.9730 - 0.9746 & 0.2174 - 0.2241 & 0.0030 - 0.0044 \dots \\ 0.213 - 0.226 & 0.968 - 0.975 & 0.039 - 0.044 \dots \\ 0 & -0.08 & 0 - 0.11 & 0.07 - 0.9993 \dots \\ \vdots & \vdots & \vdots & \vdots \end{pmatrix}$$

Single-top-quark production cross section proportional to  $|V_{tb}|^2$ .

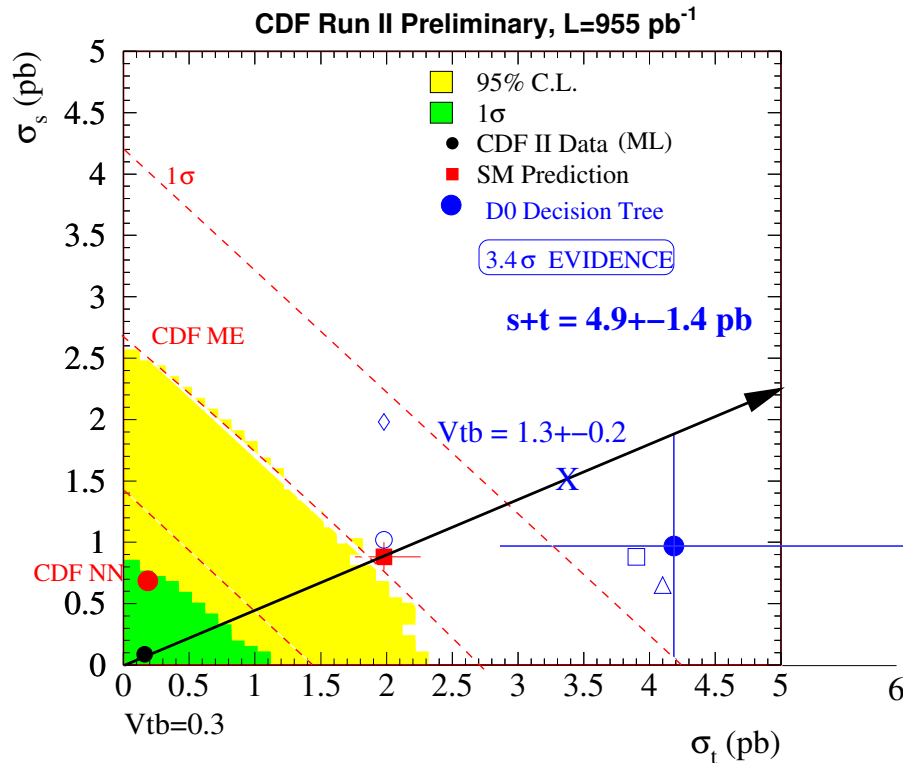
Measure  $\text{BR}(t \rightarrow Wb)$  in  $t\bar{t}$ , extract  $|V_{tb}|$  from  $\sigma_t$  with an error  $\sim \delta\sigma_t/2$ .



# First measurement(s) of $V_{tb}$

$\Delta V_{tb}$  falls along the black line.

DØ



- Extracted:  $V_{tb} = 1.3 \pm 0.2 (s + t)$
- $s$  only:  $V_{tb} \approx 1.0$ ;  
 $t$  only:  $V_{tb} \approx 1.5$

CDF

- $s + t$  (ME):  $V_{tb} \approx 1.0$
- $s$  or  $t$  (ML):  $V_{tb} \approx 0.3$
- $s$  only (NN):  $V_{tb} \approx 0.9$ ;  
 $t$  only (NN):  $V_{tb} \approx 0.3$

The additional  $1 \text{ fb}^{-1}$  of data on tape will clarify this.

# Observing Lorentz structure in single-top

$$\mathcal{L} = -\frac{g}{\sqrt{2}} \sum_{q=dsb} \bar{t} \gamma^\mu \frac{1}{2} (1 - \gamma_5) V_{tq} q W_\mu^+$$

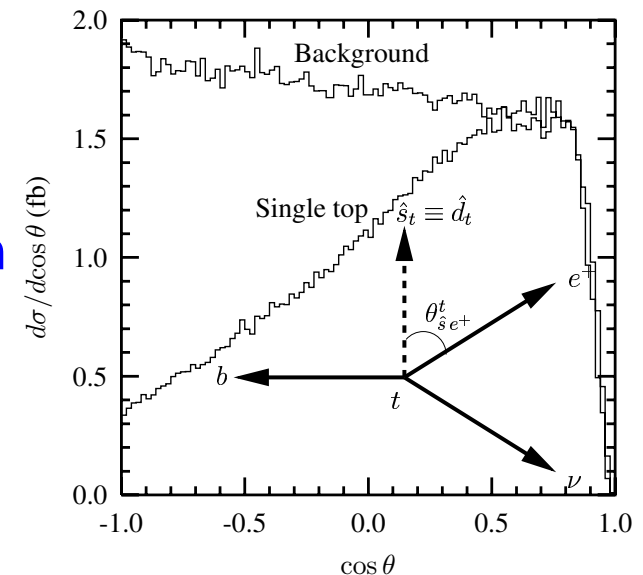
- The  $V - A$  structure of the Lagrangian produces a 100% correlation between the direction of the  $d$  quark and the spin  $s_t$  of the top quark.   
 M. Jezabek, NPBPS 37B, 197 (1994)
- The large width of the top quark ( $\sim 1.5$  GeV) allows it to decay before it depolarizes ( $\sim \lambda_{QCD}^2/m_t = 1$  MeV), or hadronizes ( $\sim \lambda_{QCD} = 300$  MeV).   
 A. Falk, M. Peskin, PRD 49, 3320 (1994)

$$\frac{1}{\Gamma_{(t \rightarrow bl\nu)}} \frac{d\Gamma_{(t \rightarrow bl\nu)}}{d \cos \theta} = \frac{1}{2} \left( 1 + \frac{N_\uparrow - N_\downarrow}{N_\uparrow + N_\downarrow} \cos \theta \right)$$

$\theta$  is the angle, in the top-quark rest frame, between the direction of the charged lepton and the spin of the top quark.

Does this hold at NLO? after cuts?

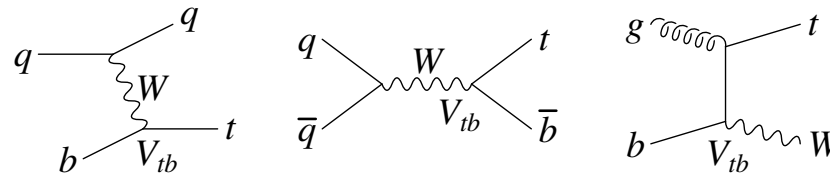
We'll come back to this...



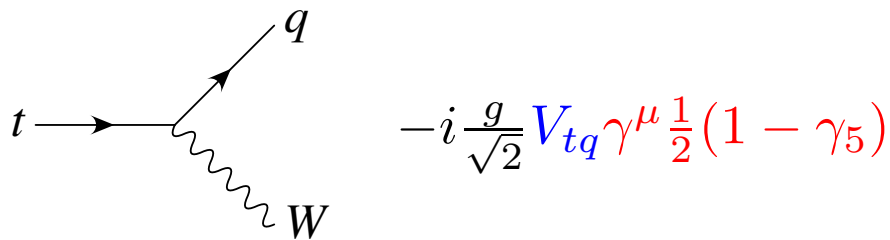
T. Stelzer, Z.S., S. Willenbrock PRD 58, 094021 (98)



# Why we look at single-top-quark production



## Weak interaction structure



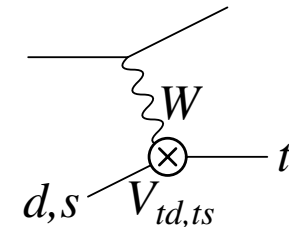
Goal: Determine the structure of the  $W$ - $t$ - $q$  vertex.

- Measure CKM couplings “direct measurement of  $V_{tb}$ ”
- Measure Lorentz structure “spin correlations”

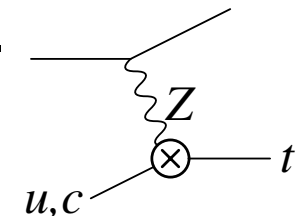
## Direct or indirect new physics

New  $t$ - $q$  couplings mostly affect  $t$ -channel measurement ( $Wbj$ ).

- Larger  $V_{ts}$  or  $V_{td}$  give PDF enhancement to  $\sigma_t$ .



- FCNC production modes from, e.g.  $Z$ - $t$ - $c$ , increase  $\sigma_t$ .

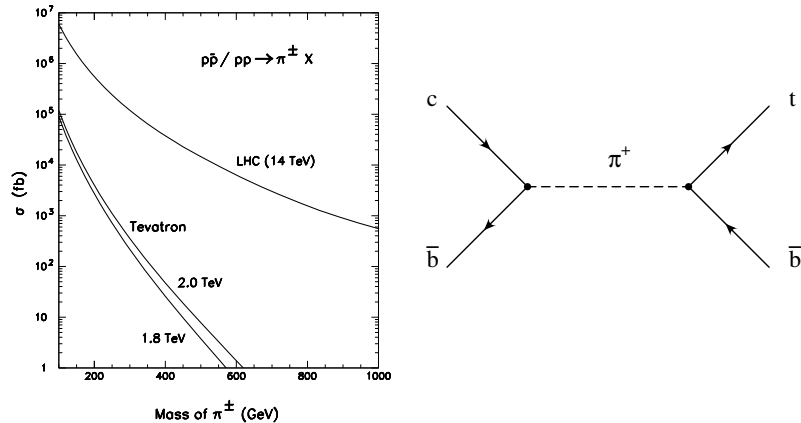


$s$ -channel looks like  $t$ -channel, since distinguished by number of  $b$ -tags.

# New physics in $s$ -channel vs. $t$ -channel

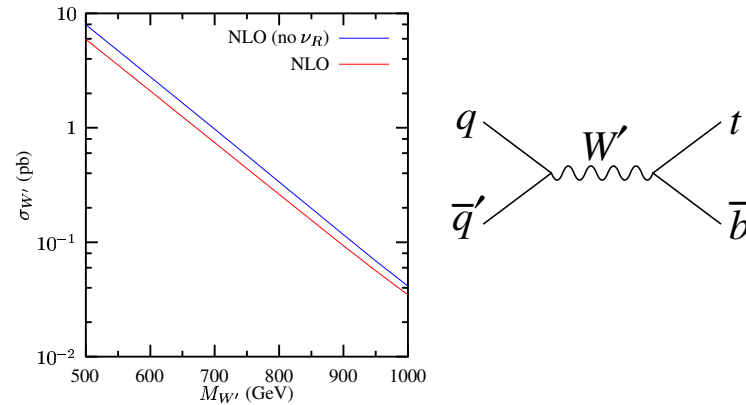
$t + b$  resonant production affects  $s$ -channel ( $Wbb$ )

Charged scalars (spin-0)

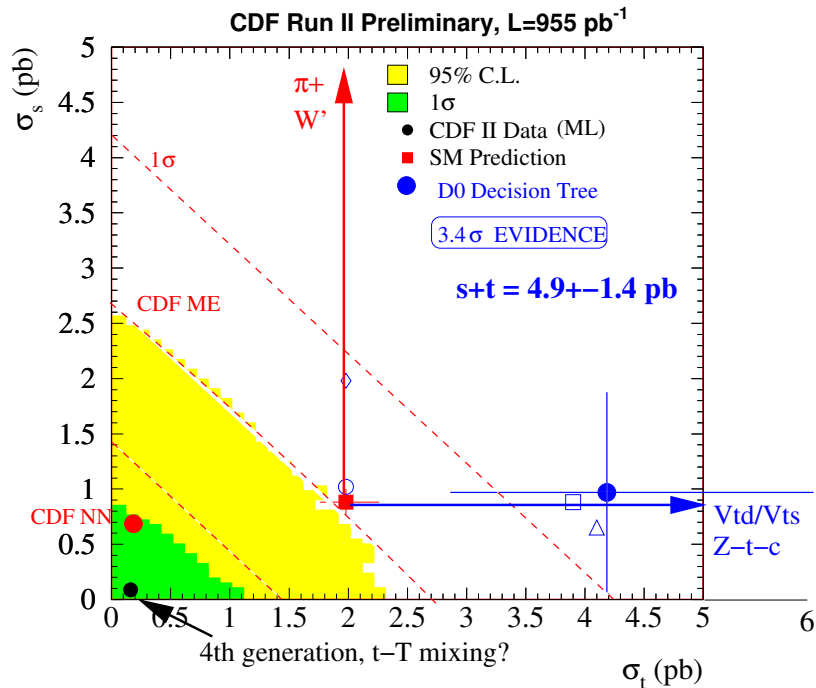


T. Tait, C.P. Yuan PRD 63, 014018 (2001)

$W'$  bosons (spin-1)

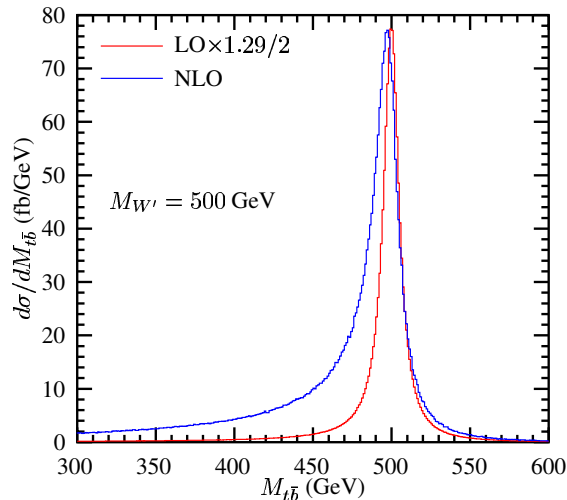


Z.S., PRD 66, 075011 (2002)



Measuring both production cross sections provides strong constraints on many new physics scenarios.

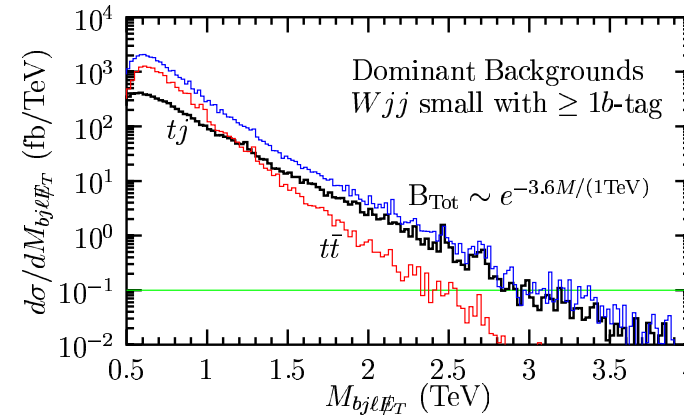
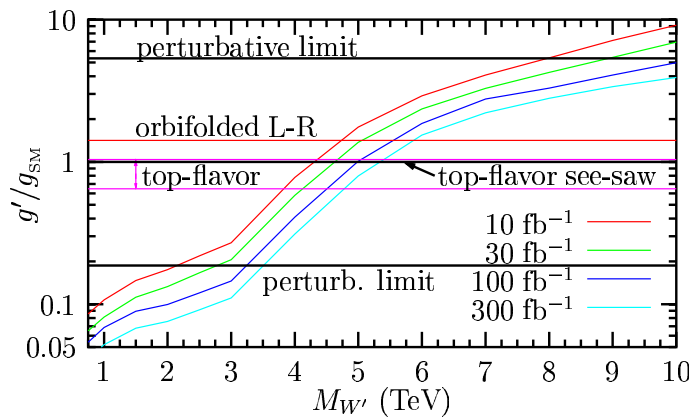
# Model-independent $W'$ searches



Z.S., PRD 66, 075011 (2002)

- Run I: CDF set bound  
 $M_{W'} > 536(566)$  GeV. PRL 90, 081802 (03)
- Run II:  
 $M_{W'} > 630(670)$  GeV. DØ, PLB 641, 423 (06)  
 $M_{W'} > 760(790)$  GeV. CDF, Note 8747
- Run II reach  $\sim 900$  GeV (w/  $2 \text{ fb}^{-1}$ ).
- Use spin correlations to tell if  $W'$  has left- or right-handed interactions.

## Model-independent $W'$ at LHC



Z.S., hep-ph/0306266

LHC can test SM-like  $W'$  bosons up to 5.5 TeV!

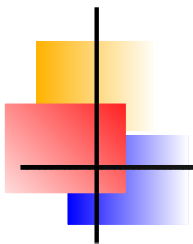


# Understanding Perturbative QCD

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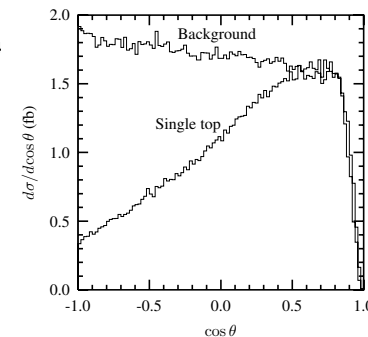
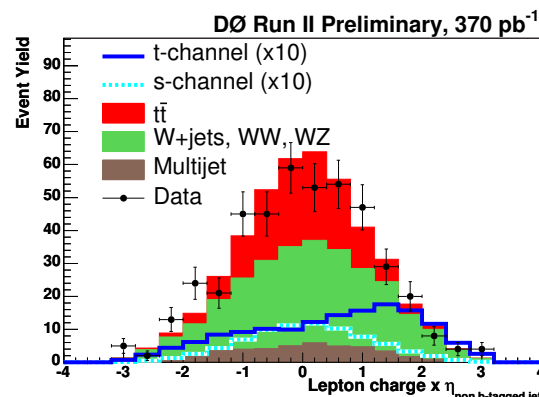
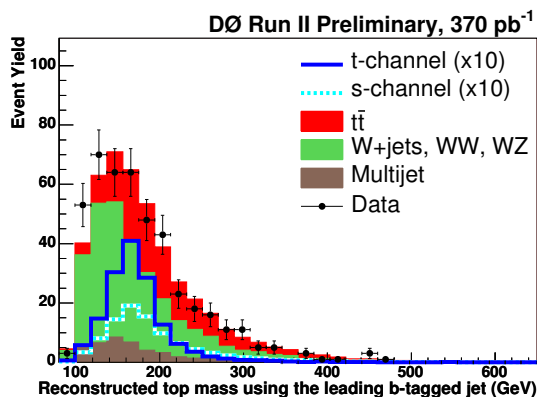
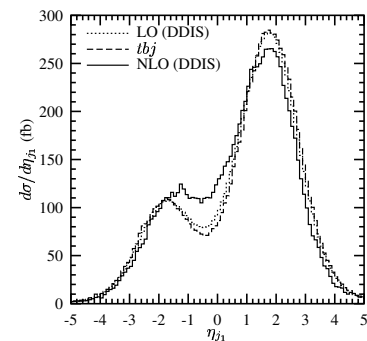
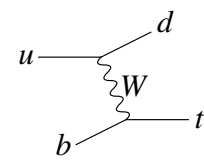
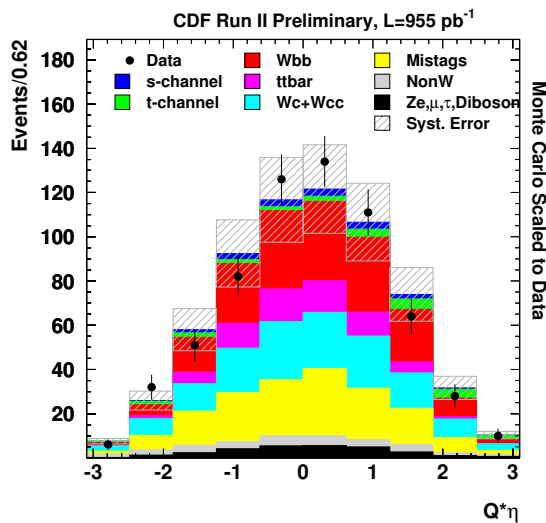
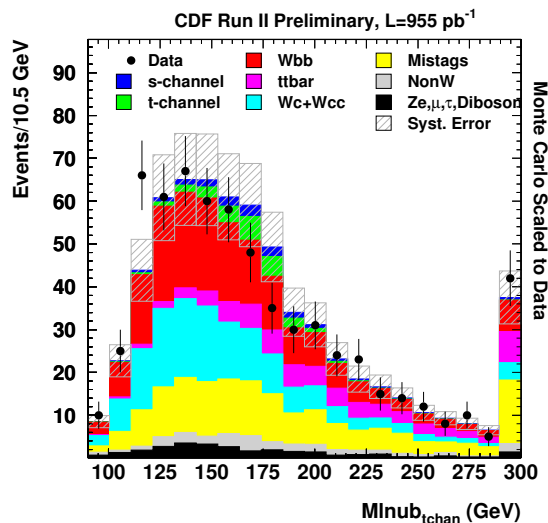
## The real reasons to study single-top-quark production

- A generalized Drell-Yan and DIS leads to deeper understanding.
- First **required** use of  $b$  PDF.
  - First real **test** of heavy-quark PDFs.
  - Progenitor of the PDF **uncertainty** formulae you currently use.
- Intrinsically multi-scale
- Progenitor of techniques to calculate **exclusive** final states of massive systems.
  - Massive dipole formalism (MDF), tightening up of PSSM2
- Clearest case where NLO jet matching is **required**.
- **and MUCH, MUCH more.**



# Angular correlations: the current frontier

# CDF and DØ have signals, and yet...



Single-top is dominated by a large  $W + 2$  jet background.

Can 100% spin correlations from  $V - A$  interactions help?

# Why the Mahlon-Parke spin-basis works

Both  $s$ - and  $t$ -channel single-top are matrix elements go like:

$$[p_d \cdot (p_t - m_t s_t)][p_e \cdot (p_t - m_t s_t)]$$

In top rest frame,  $p_t = m_t(1, 0, 0, 0)$ , and  $s_t = (0, \hat{s})$ .

Choose top spin projection  $\hat{s} = \hat{d}$ .  $\Rightarrow \sigma \propto (1 + \cos \theta_{e+d}^t)$

- $s$ -channel 98% of  $\bar{d}$  from  $\bar{p}$   
 $\Rightarrow \sigma \propto (1 + \cos \theta_{e+\bar{p}}^t)$
- $t$ -channel  $d$  in highest- $E_t$  non- $b$ -tagged jet  $j_1$

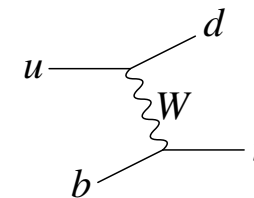
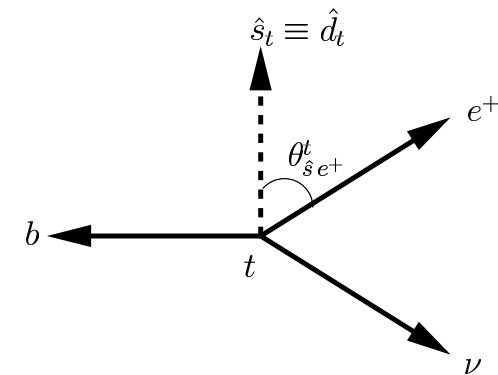
3/4 of the time.  $\Rightarrow \sigma \propto (1 + \cos \theta_{e+j_1}^t)$

For rest,  $\Rightarrow \sigma \propto (1 + \cos \theta_{d j_1}^t \cos \theta_{e+j_1}^t)$

dilution  $\cos \theta_{d j_1}^t = 1 - Q^2 / (E_d^t E_{j_1}^t) \sim 0.86$

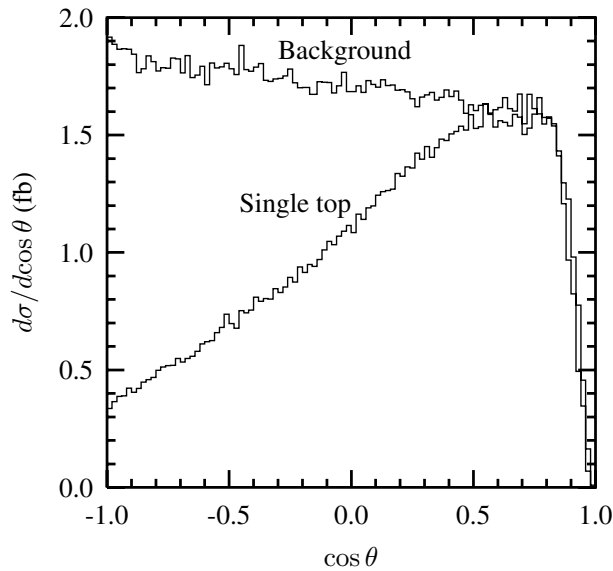
We are saved by kinematically-induced correlations.

i.e.,  $t$ -channel pole pushes jet forward.



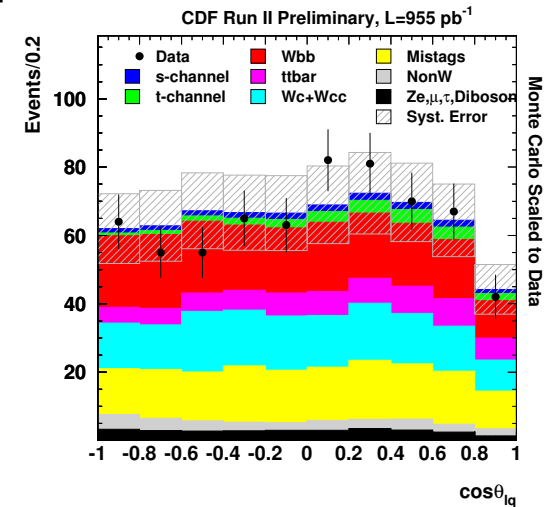
# Angular correlations in single-top-quark and $Wjj$ production at NLO

Z.S., PRD 72, 094034 (2005) (hep-ph/0510224)



Original comparison of  $t$ -channel single-top and  $Wjj$  background done at LO.

Used in neural-nets by CDF and DØ.



1. Do spin-induced angular correlations survive higher-order radiation?
2. Is the background really insensitive to the angular distributions that typify the signal? If so, does this survive complex cuts on the data?
3. The angular distributions are properly defined in the top quark rest frame. How much of these correlations is an artifact of that frame?
4. Does this lead to better discriminates between  $S, B$ ? e.g., ways to avoid  $b$ -tagging? Are there other useful particle correlations?



# LO vs. NLO at the Tevatron

## $t$ -channel

- Insensitive to top reconstruction (similar in LAB frame) — top is non-relativistic, so little boost.
- Additional ISR  $b$ -jets confuse which jet has the  $d$ .

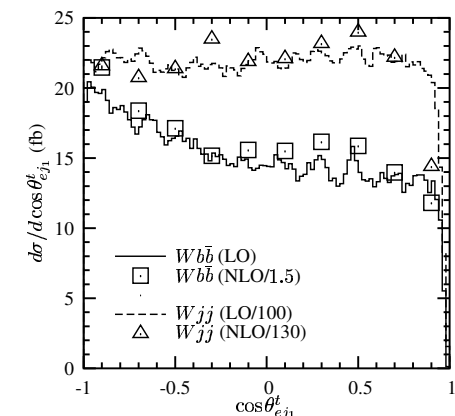
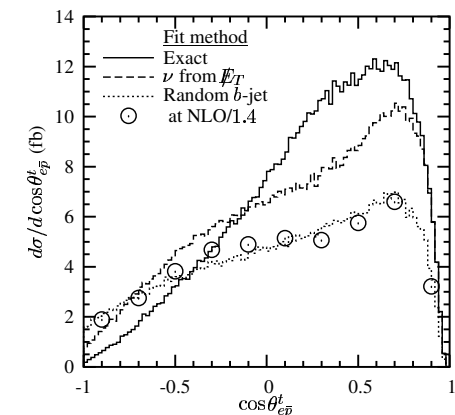
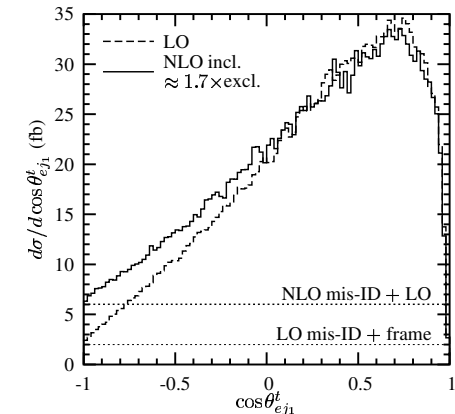
## $s$ -channel

- NLO = LO  $\times$   $K$ -factor
- **Issue:** Dominated by top reconstruction.
  - $W$  fit to  $e + \cancel{E}_T$ .
  - I naively assigned a random  $b$  jet to top decay.

## $Wjj$ (+ $Wb\bar{b}$ , $Wc\bar{c}$ )

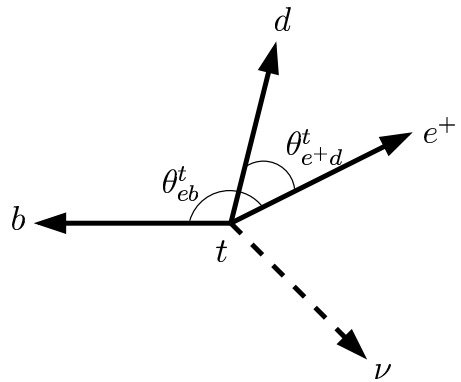
- NLO = LO  $\times$   $K$ -factor

Spin-dependent ME fed into PYTHIA/HERWIG get all correlations (not all shown), as long as NLO-matched ME are used for  $t$ -channel.



# Can you avoid $b$ -tagging? No, but it raises a subtlety...

In the top rest frame, the  $b$  recoils against the  $W$  (and the  $e$ ), while  $j_1$  wants to be close to  $e$ .



Proposal: Define "b" to be the jet with the largest angle w.r.t.  $e^+$  in the top rest frame.

Correct  $b > 80\%$  for  $s$ -/ $t$ -chan.

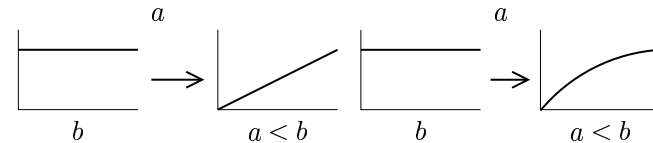
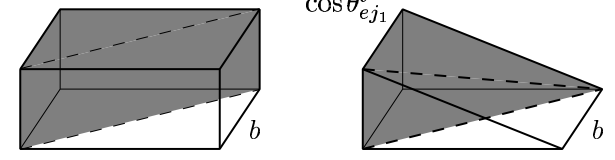
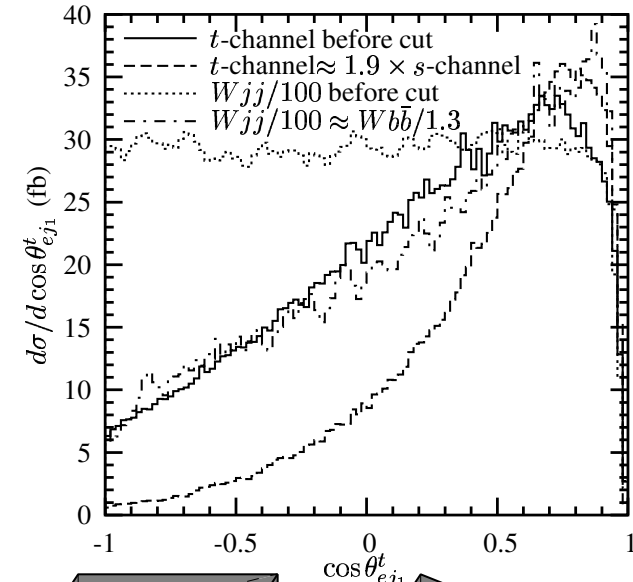
Equiv. cut:  $\cos \theta_{e''b''}^t < \cos \theta_{ej_1}^t$

Angular cuts generically induce correlations.  
This is why we need reliable predictions.

Warning: Two experimental biases select the largest angle jet (this cut):

1.  $b$ -tagging  $\propto E_{Tb}$ , picks jet recoiling vs.  $W$ .
2. Top-mass cut, also picks jet recoiling vs.  $W$ .

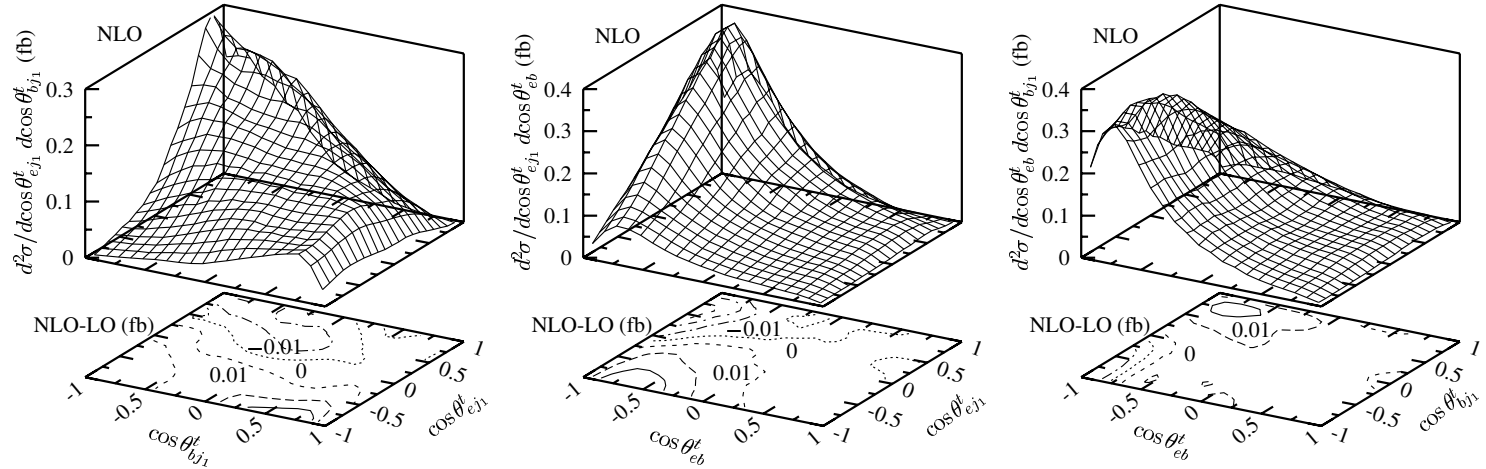
$Wjj$  looks like signal!



# NLO $\cos \theta_{ej_1}^t$ vs. $\cos \theta_{eb}^t$ vs. $\cos \theta_{bj_1}^t$ — correlations

## t-channel

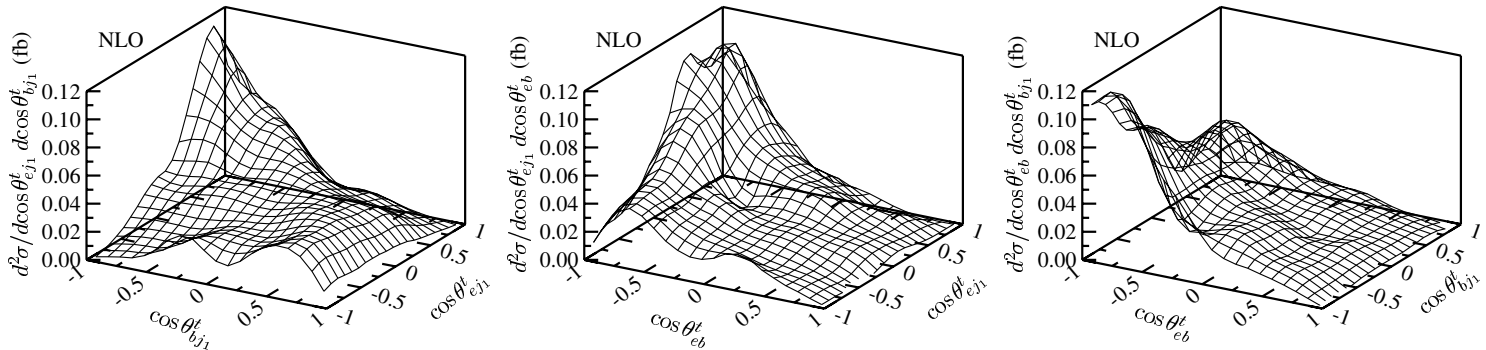
NLO-LO < 3%



## s-channel

NLO- $K \times$ LO

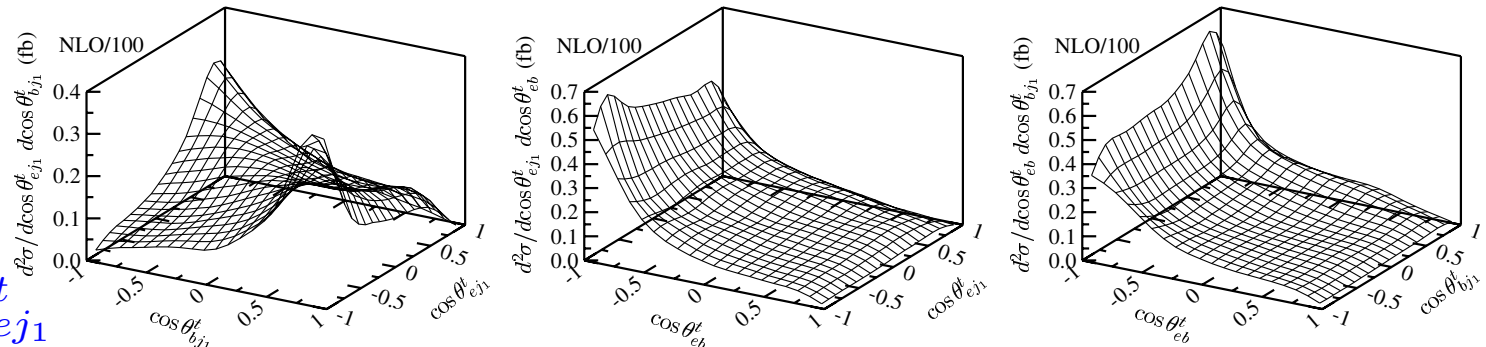
negligible,  
also true in



## all $Wjj$

$\cos \theta_{ej_1}^t$  looked  
flat, but sum of  
2 peaks + tails.

$\Rightarrow \cos \theta_{bj_1}^t < \cos \theta_{ej_1}^t$



# The power of reliable angular cuts

I propose these acceptance cuts as a starting point:

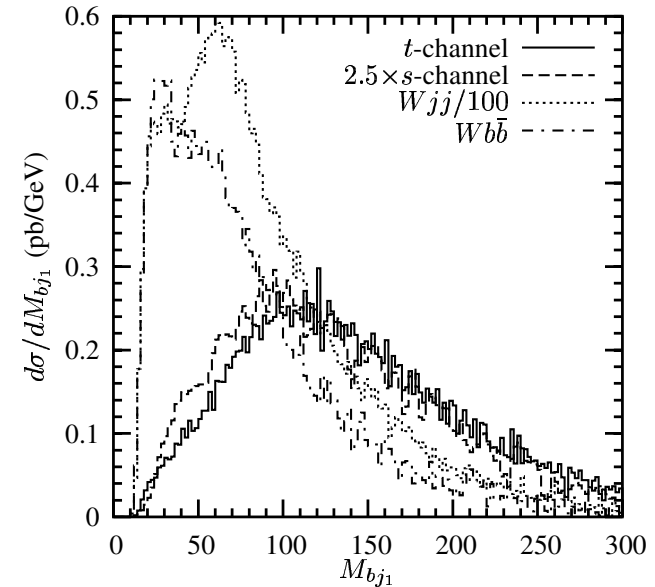
1.  $\cos \theta_{eb}^t < \cos \theta_{ej_1}^t$ .
2.  $\cos \theta_{bj_1}^t < \cos \theta_{ej_1}^t$ .
3.  $\cos \theta_{bj_1}^t < 0.6-0.8$ .
4.  $\cos \theta_{ej_1}^t > 0-0.4$  or  $\cos \theta_{eb}^t > -0.8$ .
5.  $M_{bj_1} > 80-120$  GeV

Result:  $S/\sqrt{B} \approx 1.25 \times S_0/\sqrt{B_0}$ ,

$$S/B \approx 3 \times S_0/B_0$$

Overall  $S \sim 0.4 \times S_0$ , but  $B \sim B_0/7$ !

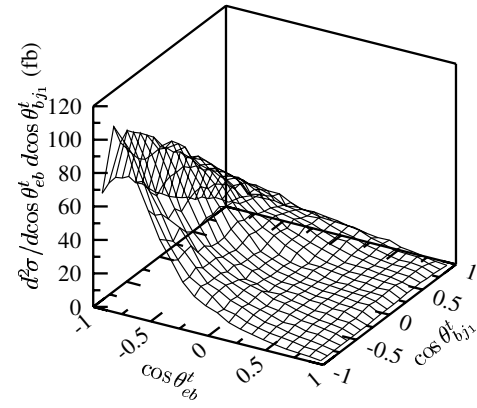
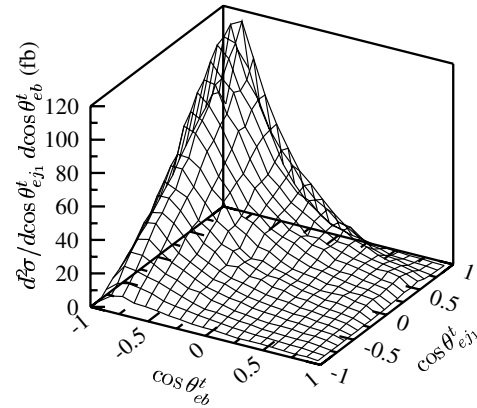
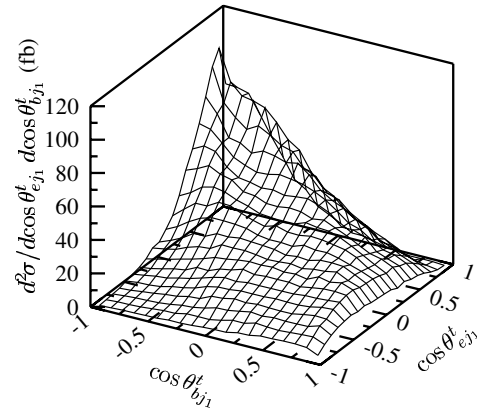
- These correlations are not completely utilized in the Tevatron analyses.
- Strong angular cuts are typical in difficult analyses: SUSY,  $H \rightarrow WW$ , ...  
We MUST check angular correlations for the LHC analyses for ALL processes.



# $\cos \theta_{ej_1}^t$ VS. $\cos \theta_{eb}^t$ VS. $\cos \theta_{bj_1}^t$ at LHC

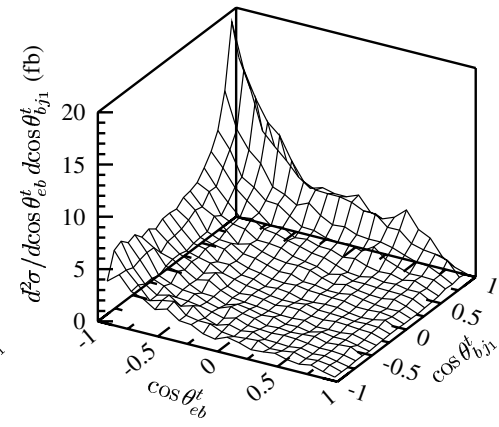
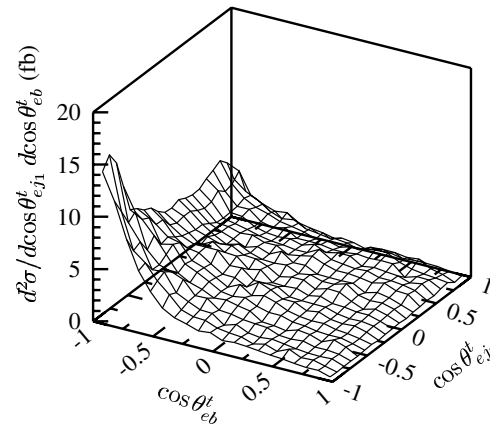
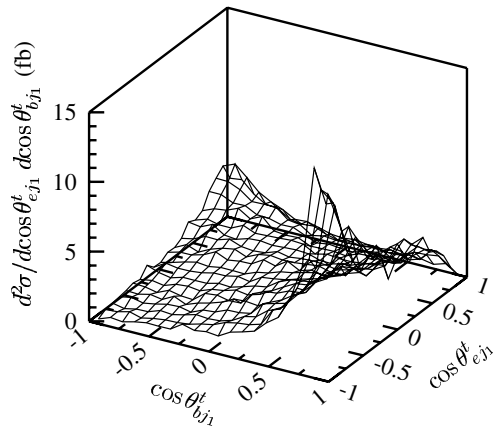
## $t$ -channel

Similar to  
Tevatron



## $Wb\bar{b}$

Small and  
**opposite**  
single-top!!!



The main background at LHC is from  $t\bar{t}$ , but there are large handles here.

**NOTE:**  $\bar{t}$  production is just like  $s$ -channel, i.e., if you boost the system to average  $\eta = 0$ ,  $\cos \theta_{ep}^{\bar{t}}$  is the relevant angle, where  $p$  is on the same side as the electron.



# Single-top-quark theory status

## NLO cross sections

	Tevatron( $t + \bar{t}$ )	LHC ( $t$ )	LHC ( $\bar{t}$ )
$t$ -channel	$1.98 \pm 0.2$ pb	$155.9 \pm 7.2$ pb	$90.7 \pm 4.2$ pb
$s$ -channel	$0.88 \pm 0.1$ pb	$6.6 \pm 0.6$ pb	$4.1 \pm 0.4$ pb
$Wt(p_{T\bar{b}} < 50$ GeV)	$\sim 0.07$ pb	$\sim 33$ pb	$\sim 33$ pb

Z.S., PRD 70, 114012 (2004); J. Campbell, F. Tramontano, NPB 726, 109 (2005)

## Spin-dependent NLO exclusive cross sections

### MCFM 5.1

Matrix-element calculation  
of  $t$ -, $s$ -channel,  $Wt$   
Gives distributions

### MC@NLO 3.3

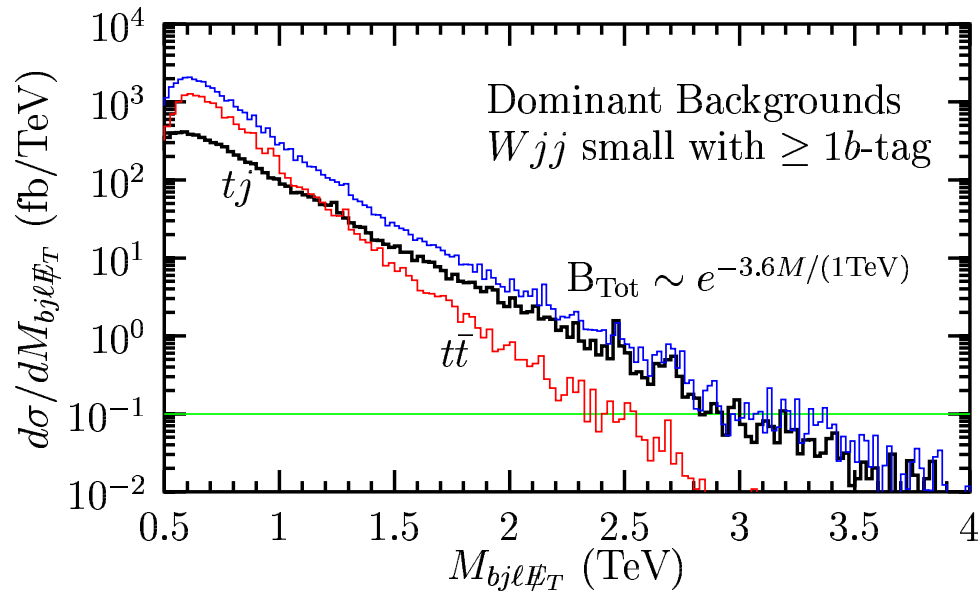
Showering MC (w/ HERWIG)  
of  $t$ -, $s$ -channel  
Gives events

Need to verify angular correlations

BOTH tools should be used to confirm quality of predictions.

Single-top-quark theory is in good shape.

# Dominant backgrounds to $W'$ production



Searching for peaks in the  $Wbj$  final state is proven to be the best way to look for  $W'$  production above 1 TeV.

cf. Full simulation in Z.S., [hep-ph/0306266](https://arxiv.org/abs/hep-ph/0306266)

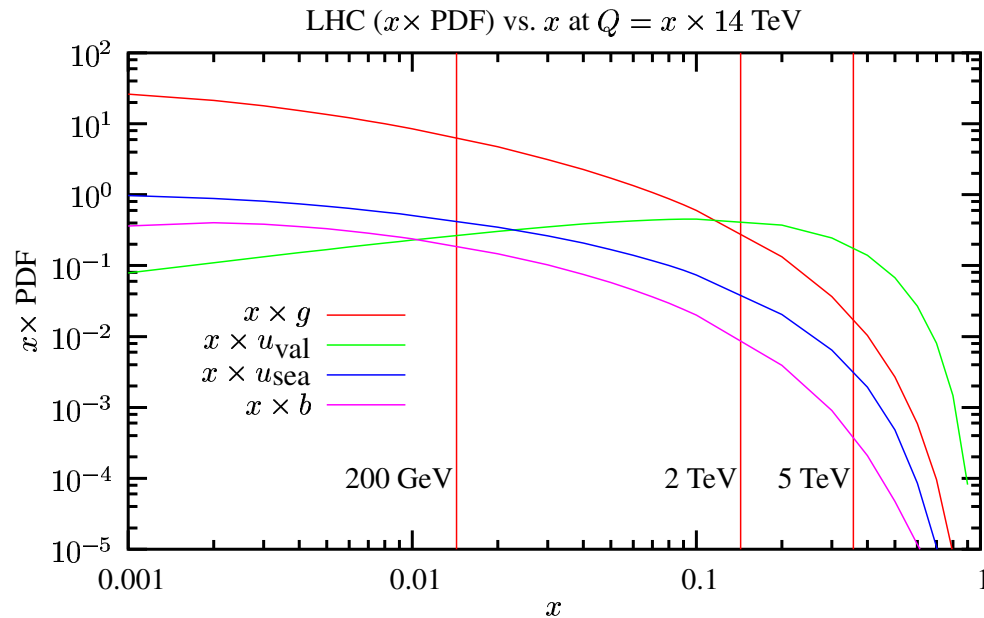
This is dominated by single-top-quark production at large invariant mass.

If the  $b$  tag is relaxed,  $Wjj > tj$ , with the same shape.

Both this figure, and the possibility of a 6 TeV  $W'$  signal, provide a clue to what really differentiates physics at the LHC vs. physics at the Tevatron...

And challenges one of the most common misstatements...

# PDFs control relevant physics at LHC



3 important pivot points:

- 200 GeV  $u_{\text{val}} \approx u_{\text{sea}}$  — valence is important here.
- 2 TeV  $u_{\text{val}} > g$  — above a TeV, valence quarks dominate.
- 5 TeV PDFs “running out” — nothing heavier gets produced on-shell.

This explains large average rapidity for  $q\bar{q}$ ,  $qg$  events

—  $q_{\text{val}}$  pulled to large  $x$ ,  $g$  and  $q_{\text{sea}}$  want small  $x$ .

The LHC is not a glue factory for physics you care about.

— Color-neutral particles couple to quarks, not gluons.

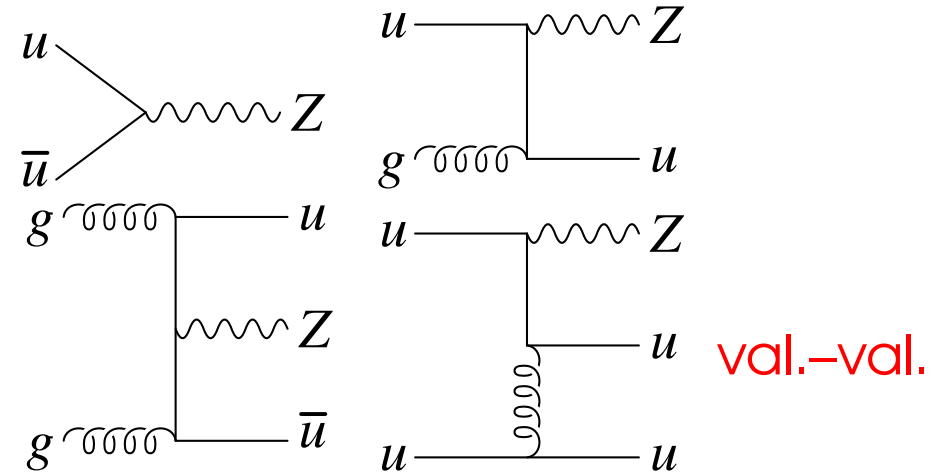
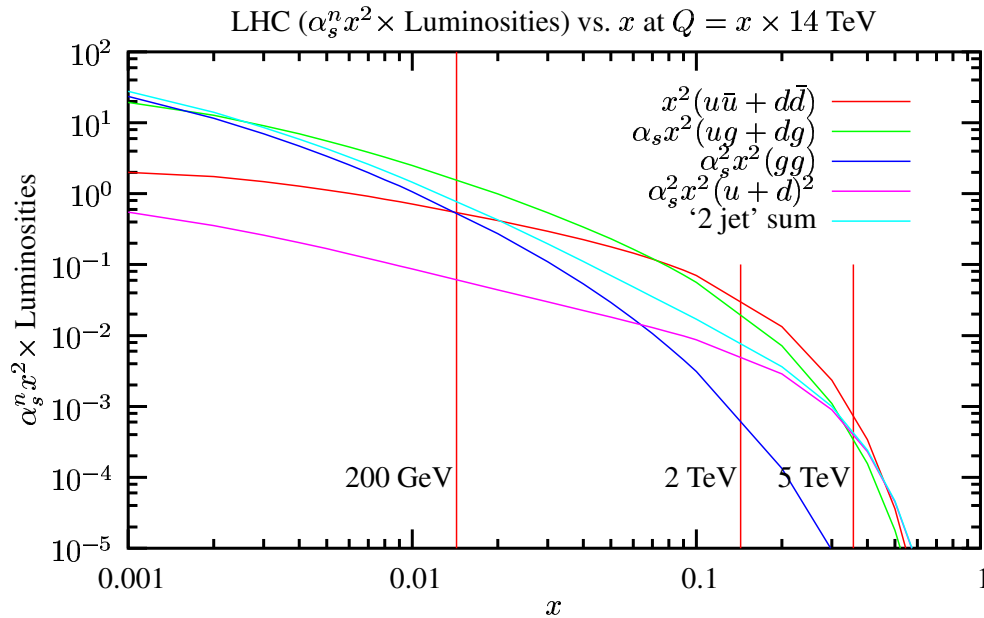
— New colored particles tend to be heavy (1+ TeV), and see valence.

This figure is almost identical to the Tevatron (at 7 times the energy).

What differs is that LHC is a  $pp$  collider. This changes everything.



# Example luminosity (with power counting) at LHC



From a luminosity (with power-counting) point of view,

$Z \approx Z + 1 \text{ jet} \approx Z + 2 \text{ jets!}$  (Same in  $W + X$ ,  $Wb\bar{b} + X$ ,  $Zb\bar{b} + X$ , etc.)

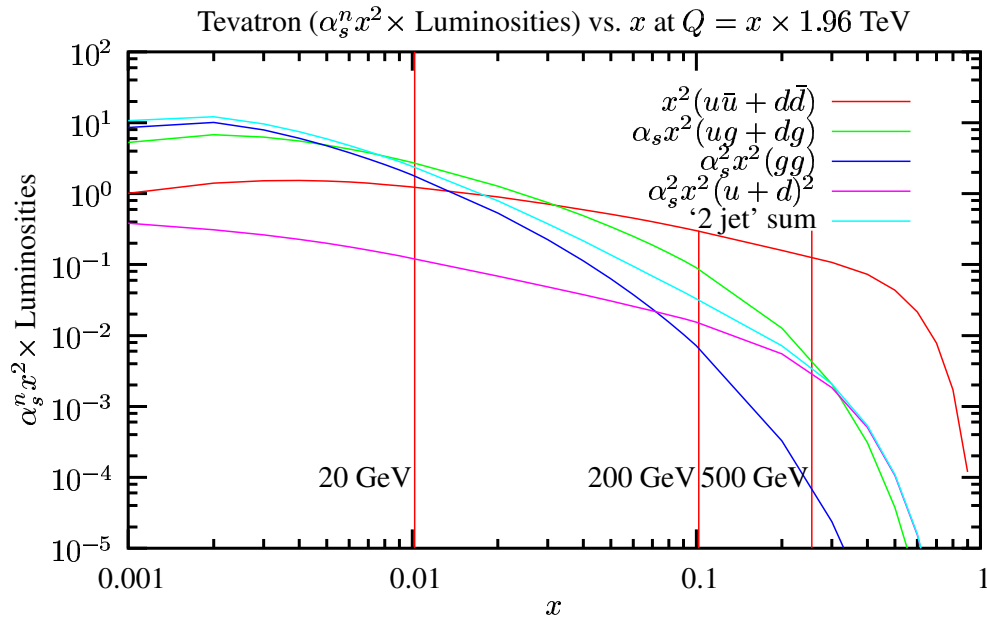
Color factors and topology are important:

$\Rightarrow$  This is **VERY** sensitive to cuts.

Naive jet counting  
is ill-defined  
or poorly-defined

In  $Wjj$  and  $t$ -channel single-top,  $u_{\text{val}}u_{\text{val}}$  is important at a few TeV.

# Tevatron is $p\bar{p}$ at lower energy — a totally different luminosity balance



This is what we are used to.

Above  $Z$  threshold:

$Z > Z + 1j > Z + 2j$ .

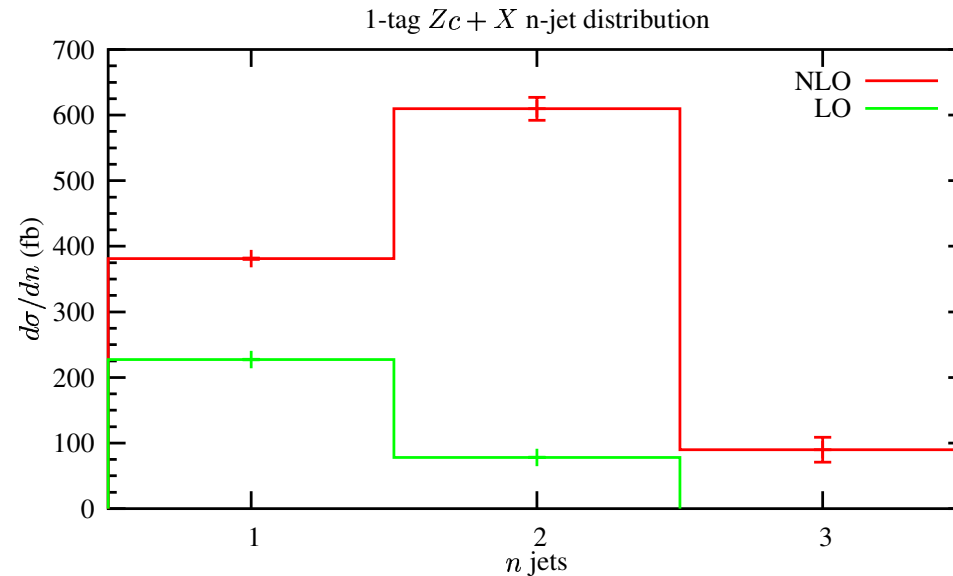
A nice ordering of jets.

## WATCH OUT

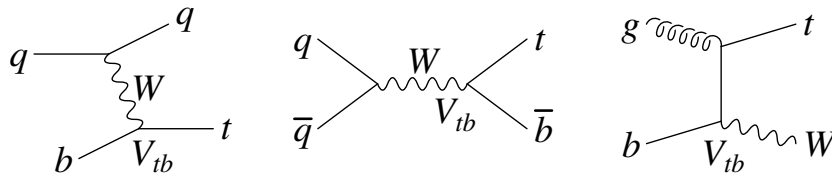
Jet counting fails in some cases at the Tevatron too!

$Zcj > Zc, Wcj > Wc$ , etc.

This is a teaser...



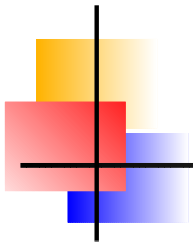
# Single-top-quark production is the new Drell-Yan and DIS



$$\sigma_{\text{tot}} = 4.9 \pm 1.4 \text{ pb (D}\phi\text{)}$$
$$2.7 \pm 1.5 \text{ pb (CDF)}$$

1. We study single-top-quark production to
  - measure  $V_{tb} = 1.3 \pm 0.2$  (D $\phi$ )
  - measure  $V - A$  interaction and top-quark polarization
  - search for entire classes of new physics (FCNC, charged currents)
  - most importantly, to **understand perturbative QCD**
2. We must critically examine correlated angular distributions
  - These are useful for single-top itself, and vital in backgrounds
3. LHC is a valence-quark factory (and quark-gluon, and gluon-gluon)
  - We must find a way to either calculate exclusive final states that are stable against experimental cuts or
  - look for alternate quantities for which we can calculate.

It will be vital to the success of the LHC to develop close interactions between theory and experiment of the type single-top-quark production has enjoyed.



# Extra slides

# PDFs at Tevatron $\sim$ scaled down LHC

