

Synchro-Betatron Effects

R. Calaga, R. Miyamoto, S. White
BNL – USLARP

Thanks to S. Fartoukh and R. de Maria for the help with the HL-LHC
optics

Model

- Head-on interactions:
 - Self consistent 6D field calculations allowing for arbitrary distributions (BEAMBEAM3D, Ji Qiang)
 - Crossing angle implemented “a la Hirata”
- Long-range interactions:
 - Lumped 4D beam-beam kick at $\pm\pi/2$ from the IP (Gaussian approximation)
 - Underestimates the footprint area (constant separation for all interactions)
- Crab Cavities:
 - Thin crab cavity kick at $\pm\pi/2$ from the IP
 - Only the local scheme was considered
- Transport is done with a linear 6x6 transfer matrix. Chromaticity kick available

Beam Parameters

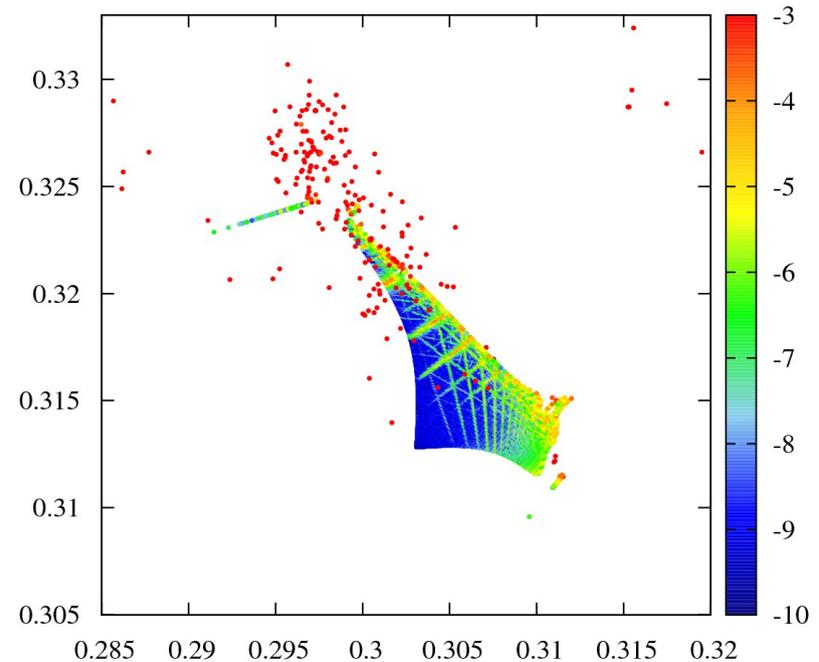
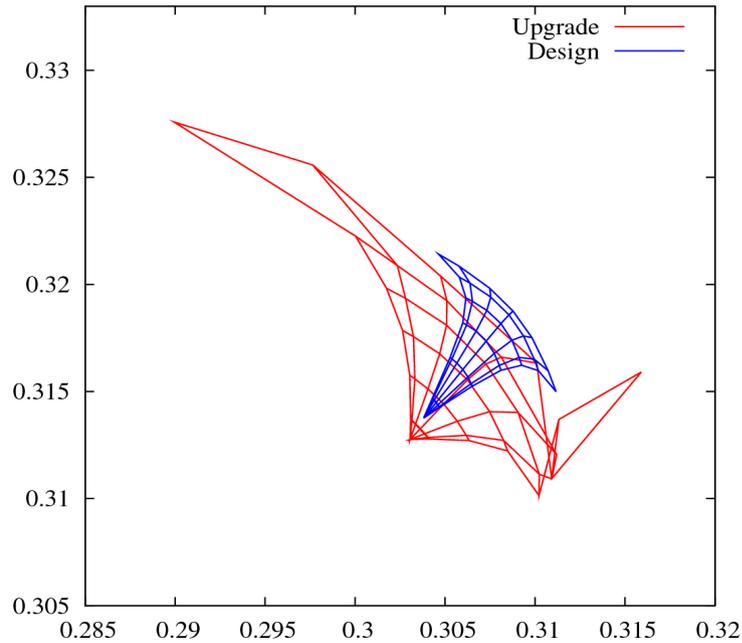
- Beam parameters with 25 ns from O.Bruning's talk in April 2011:

	Design Parameters	Upgrade Parameters
N [p/bunch]	1.15e11	2.0e11
ϵ_N [μm]	3.75	2.5
$Q_x / Q_y / Q_s$	0.31 / 0.32 / 0.002	0.31 / 0.32 / 0.002
β^* [m]	0.55	0.15
σ_s [m]	0.075	0.075
dp/p	1.129e-4	1.129e-4
θ [μrad]	285	475 ($\sim 10\sigma$)
N_{LR}	15	18-24
L_{peak} [$\text{cm}^{-2}\text{s}^{-1}$]	1.0e34	7.4e34 (2.0e35 w. CC)

- Target was at the time 1.0e35 (now 2.0e35) “virtual luminosity” leveled to 5.0e34 → **lots of margin w. CC**
- Number of long-range depends on the triplets: several options considered
- Crossing angle set to have 10σ separation: still valid for large N_{LR} / bunch intensity?

Footprint

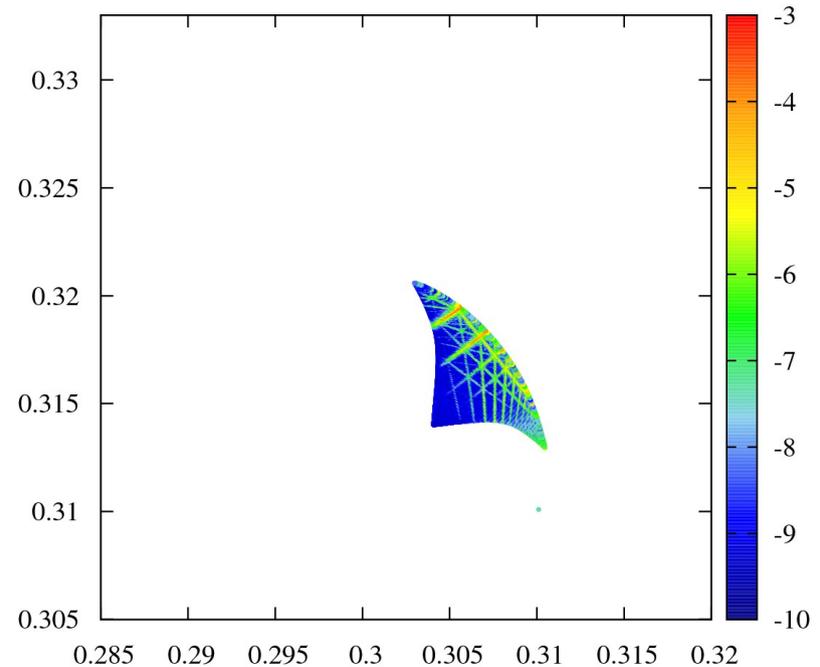
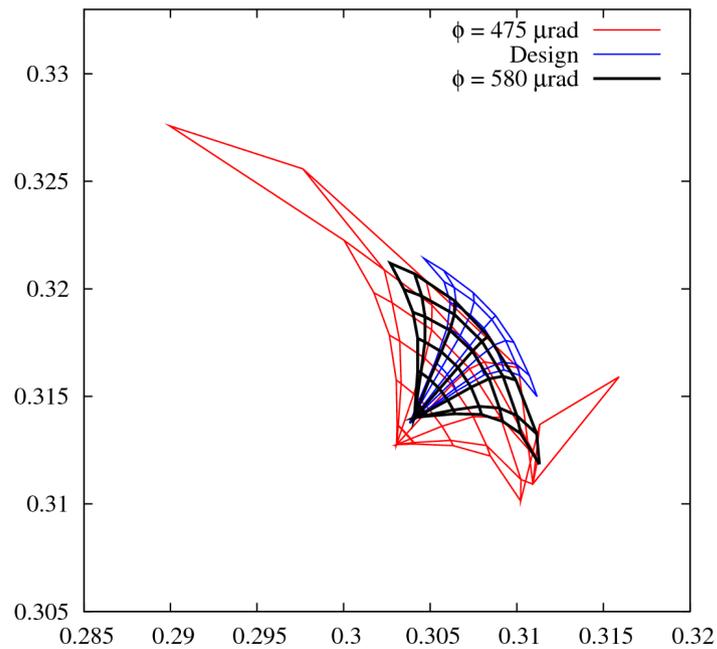
- Take 21 long range interactions as study case (IP1&5 only)



- 10σ separation: footprint strongly distorted (lattice resonances): detrimental effects clearly dominated by LR \rightarrow poor lifetime / DA (see W. Herr's talk)?
- **Reduce the effect of the long range interactions. Possible mitigations:**
 - Increased β^*
 - Increased crossing angle

Increased Crossing Angle

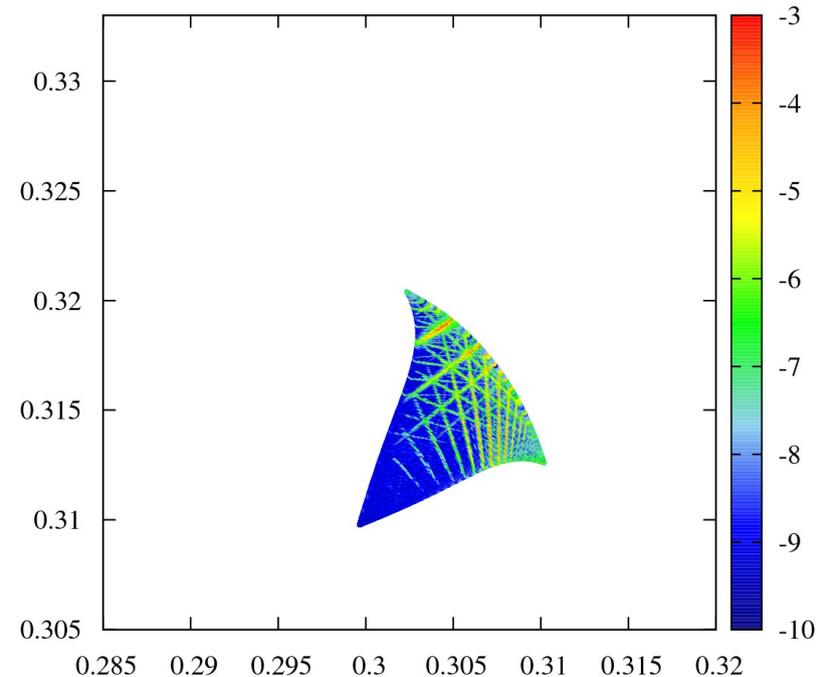
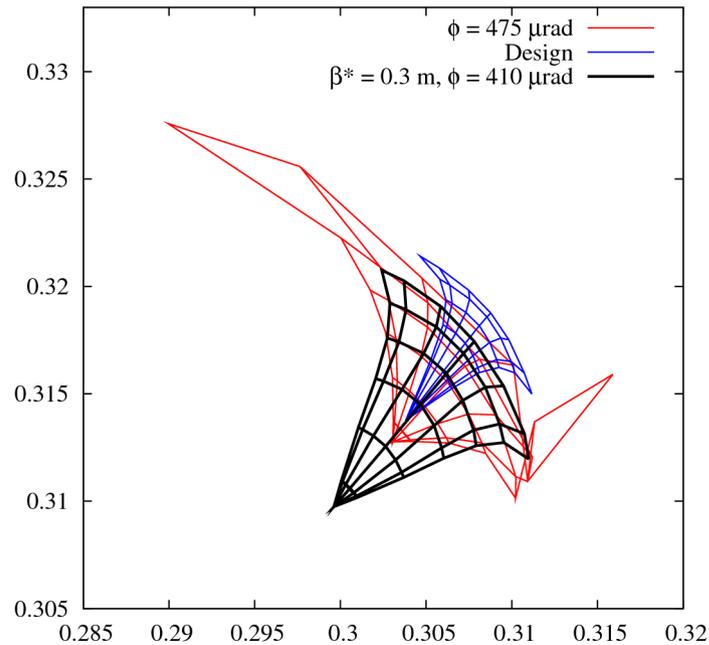
- Increased crossing angle to 580 μrad ($\sim 12.2 \sigma$ separation)



- Still larger than “design” but looks better
- “Virtual luminosity” remains the same assuming we have crab cavities → **plenty of space for leveling with crab cavities**
- Peak luminosity without crabs **$L = 6.2e34 \text{ cm}^{-2}\text{s}^{-1}$**

Increased β^*

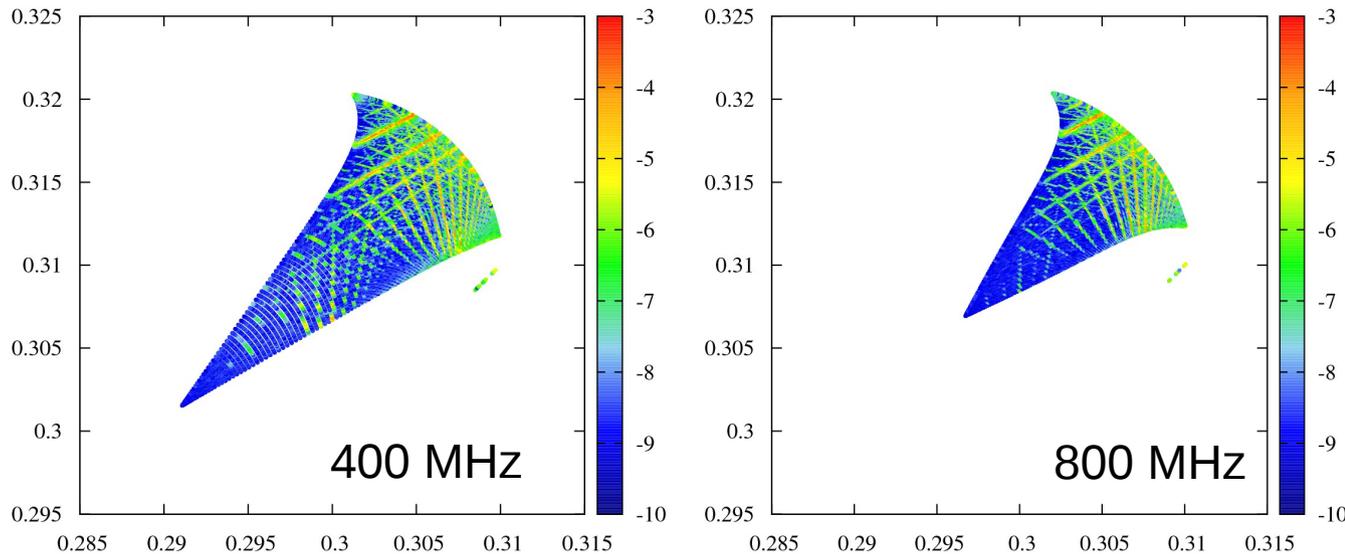
- Increased β^* to 0.3 m (ATS optics), 410 μrad (rescaled previous angle)



- Same LR as previous slide with larger HD ($\sim 1.0\text{e-}2$)
- “Virtual luminosity” with CC down by a factor ~ 2 **still reaching $1.0\text{e}35$**
- Peak luminosity without crabs **$L = 5.4\text{e}34 \text{ cm}^{-2}\text{s}^{-1}$** \rightarrow **leveling with crab cavities required**

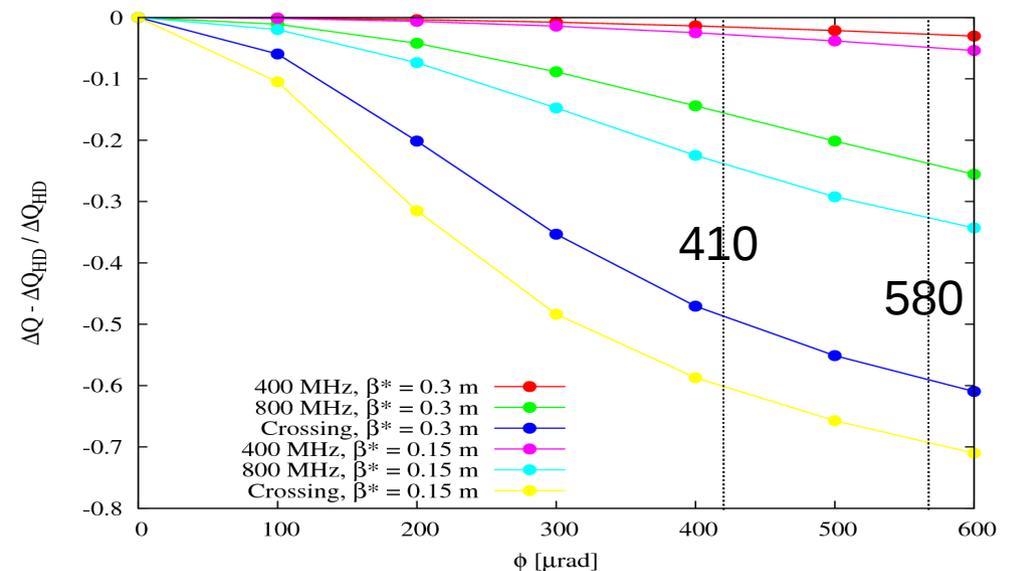
With Crab Cavities

- Check whether crabs + LR can degrade the situation



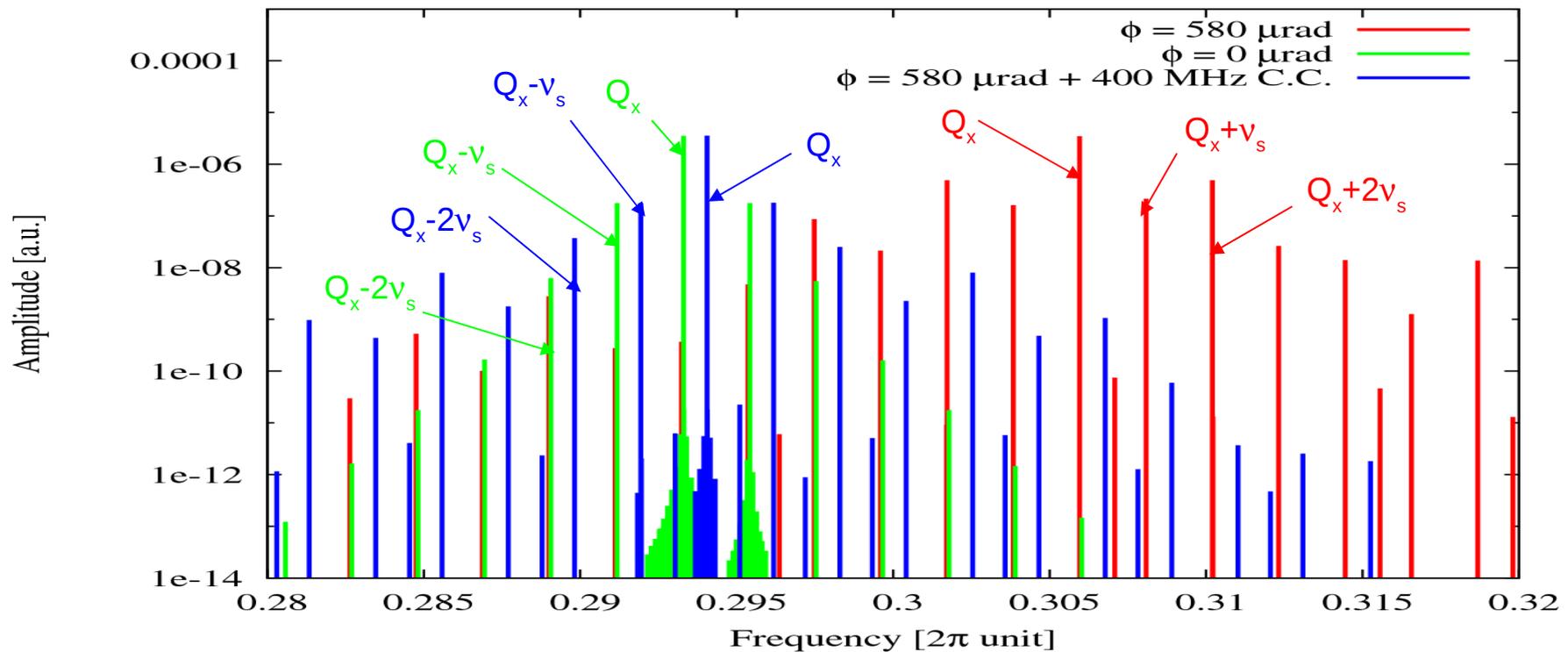
- Large crossing angle:
 - No significant differences observed with the case without compensation for either frequencies
 - Large difference in the efficiency of the crossing angle compensation

- Tune shift as a function of the crossing angle:
 - compensation works better for larger β^*
 - the values of the crossing angle considered clearly favor the 400MHz cavities



Synchro-Betatron Effects

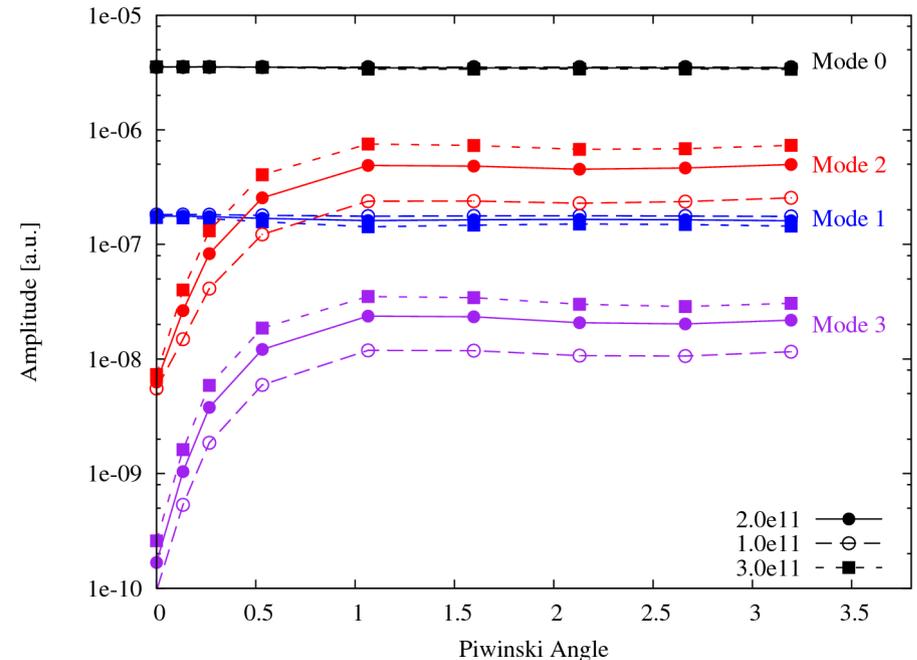
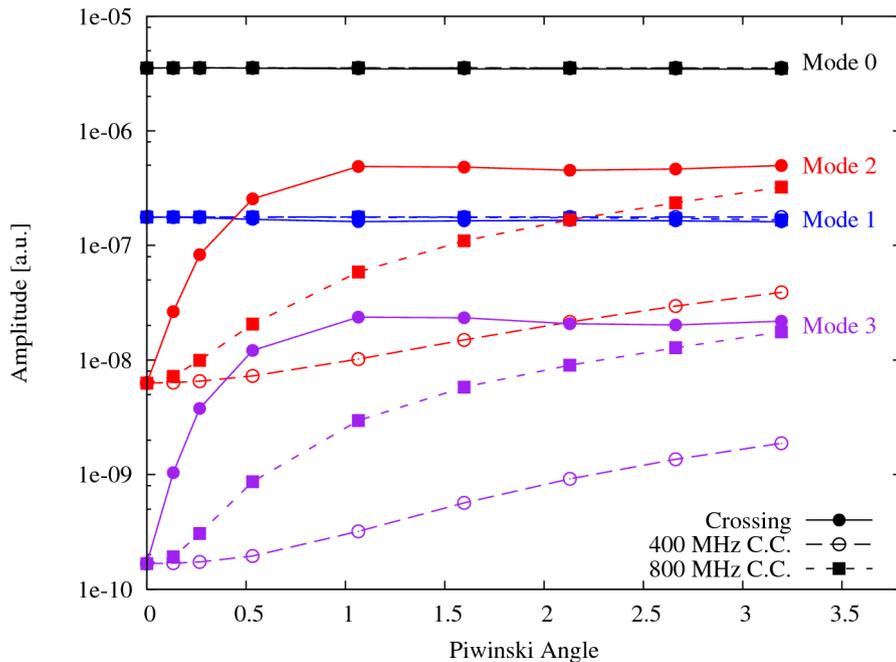
- It was shown by Y. Sun et al. that the crabs could damp the side-bands excited by the crossing angle (sixtrack). Initial amplitude $1 \sigma_x / 1 \sigma_s$:



- The results could be well reproduced with BB3D:
 - First side bands not affected
 - Higher order side bands excited by the crossing angle \rightarrow damped by the crab cavities

Amplitude vs Piwinski Angle

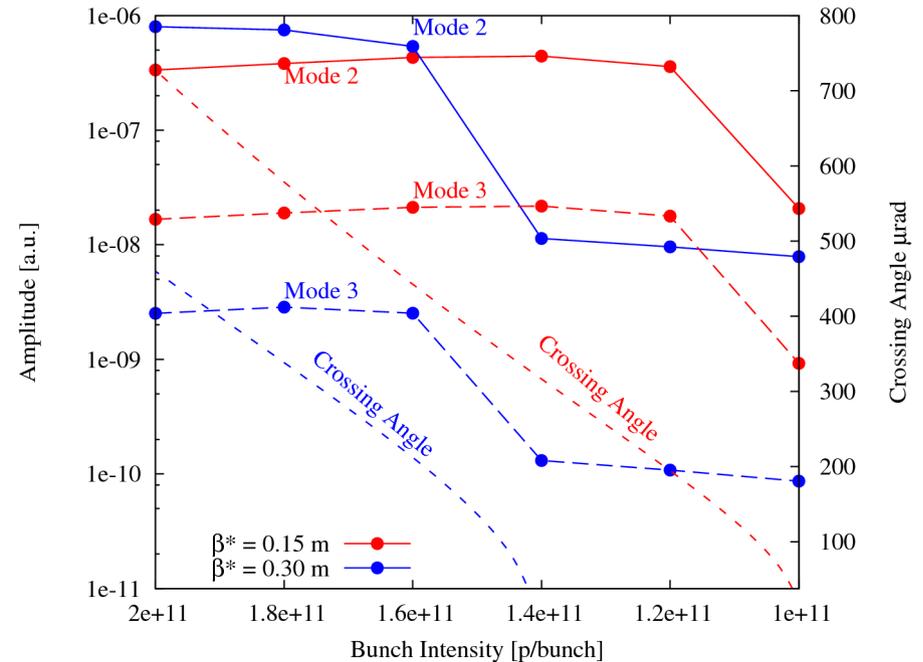
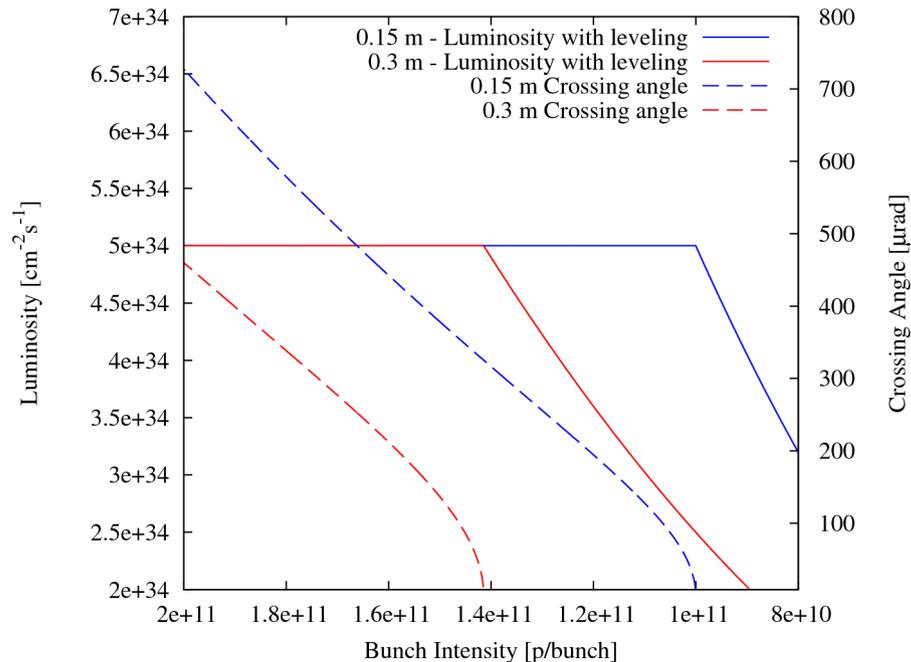
- Modes amplitude with and without crabs as function of the Piwinski angle:



- 2^{nd} side-band and up excited by the crossing angle, peak at $\Phi \sim 1 \rightarrow$ **clear damping effect from the crabs**
- Bunch intensity / ξ has little effect over the range relevant for LHC
- The HL-LHC regime ($\Phi \sim 2-3$) has not yet been probed by actual operation ($\Phi \sim 0.4$) but design parameters ($\Phi \sim 0.7$) should provide useful information**

Leveling Scenarios

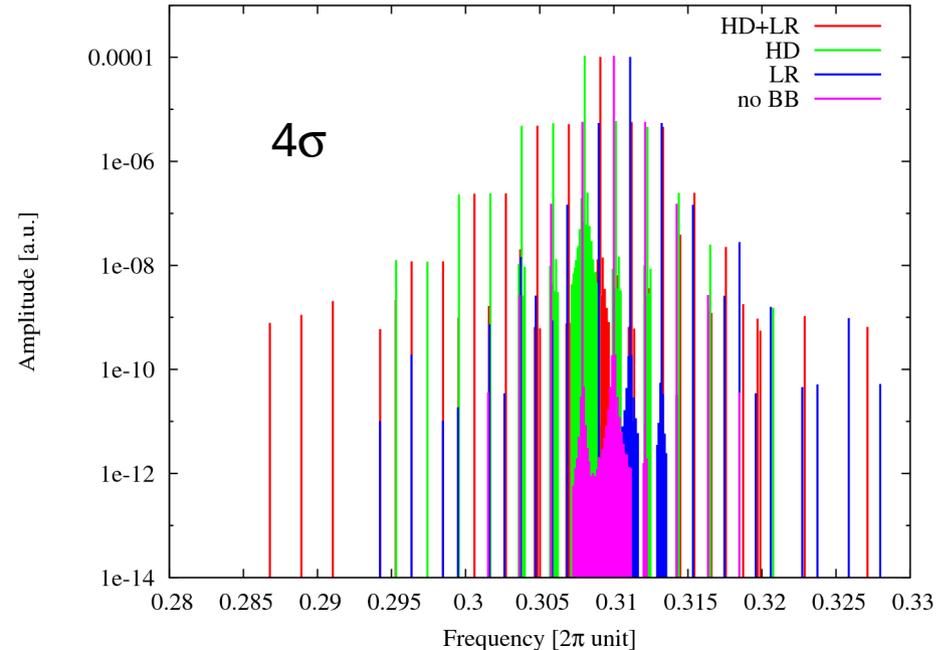
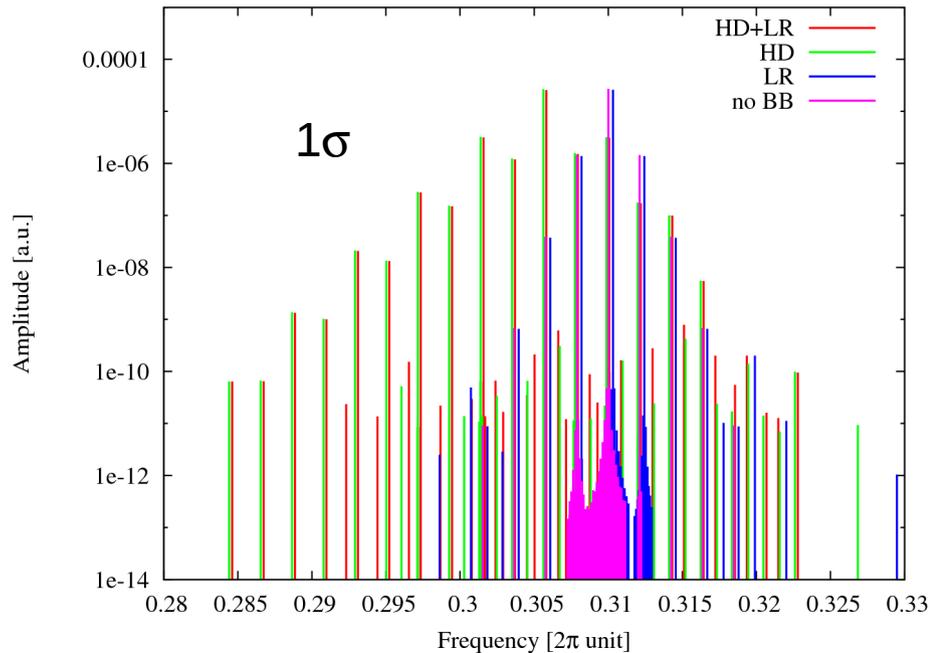
- Consider the simple model where the loss in luminosity comes only from intensity – level to $5e34$ using crab cavities until full compensation:



- Start “high” for both options (same regime) slightly better for 0.3m
- Damping comes faster for 0.3m but this option gives less margin for leveling
- Given the requirements in terms of luminosity it seems difficult to use the damping properties of the cavities (in case SBR are a problem) if they are used for leveling

Effect of Long-Range Interactions

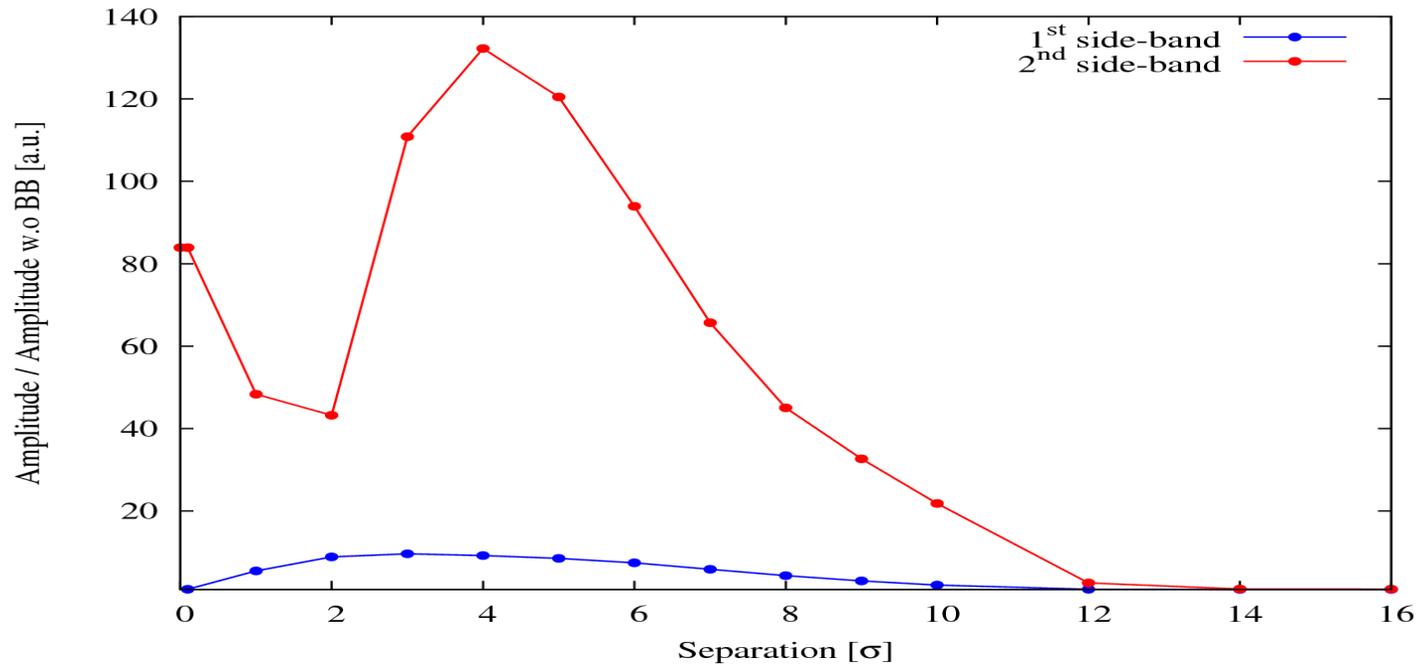
- Look at the effect of the long range interactions for a core particle (1σ) and a tail particle (4σ) – in this case LR are modeled with a 6D kick:



- Core particles:** not affected by long-range interactions: spectrum with LR only matches the case without beam-beam
- Tails particles:** no significant difference with respect to the case without beam beam
- Effect clearly driven by the head-on interactions**

6D Beam-beam Kick with Transverse Offset

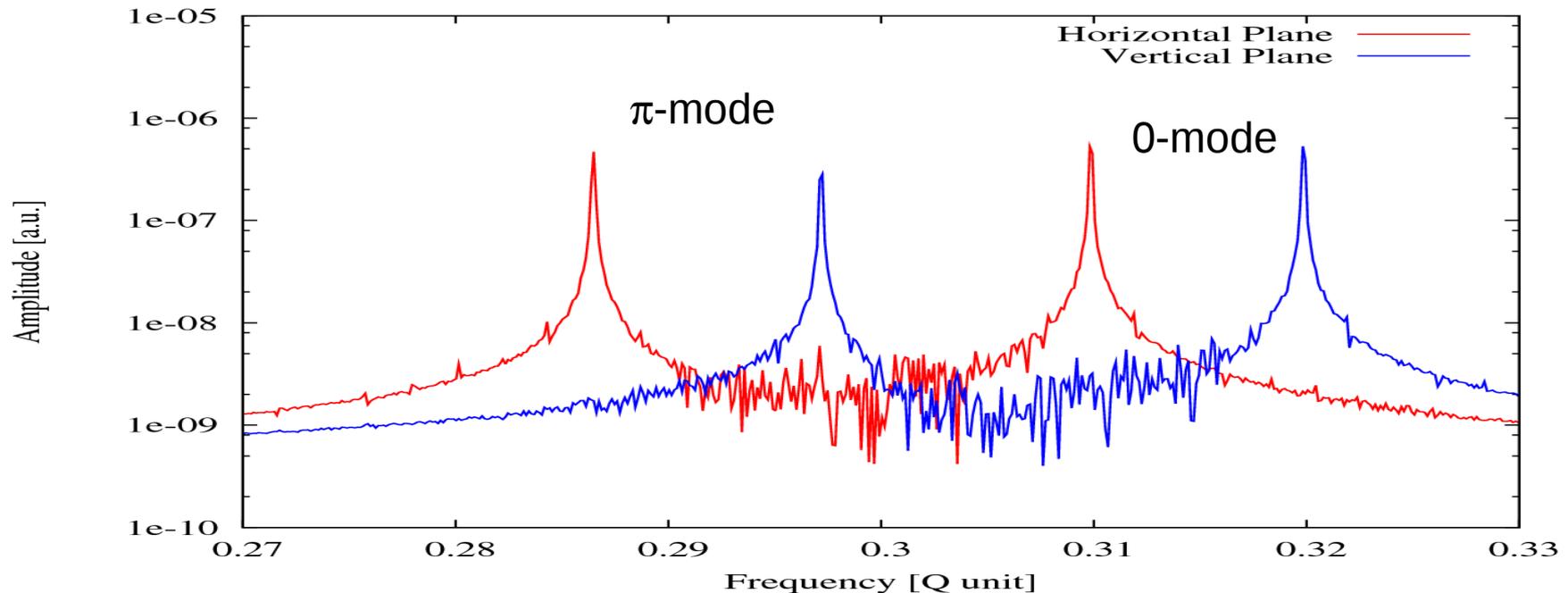
Head beam-beam collision with static offsets. Look at the evolution of the side-bands as a function of separation:



- Done for the 0.15 m option – the separation is applied in the crossing angle plane
- Side bands increase up to $\sim 4 \sigma$ separation converge to the case without BB for larger separations
- LR separation for 0.15 m $\sim 12-13 \sigma \rightarrow$ **SBR from LR should not significantly contribute to the overall effects**

Coherent Beam-beam Effects

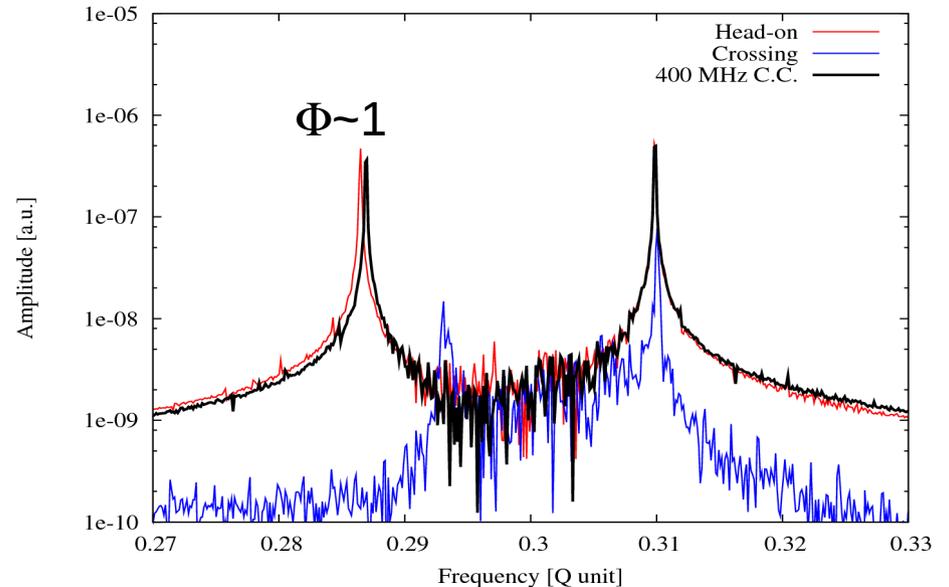
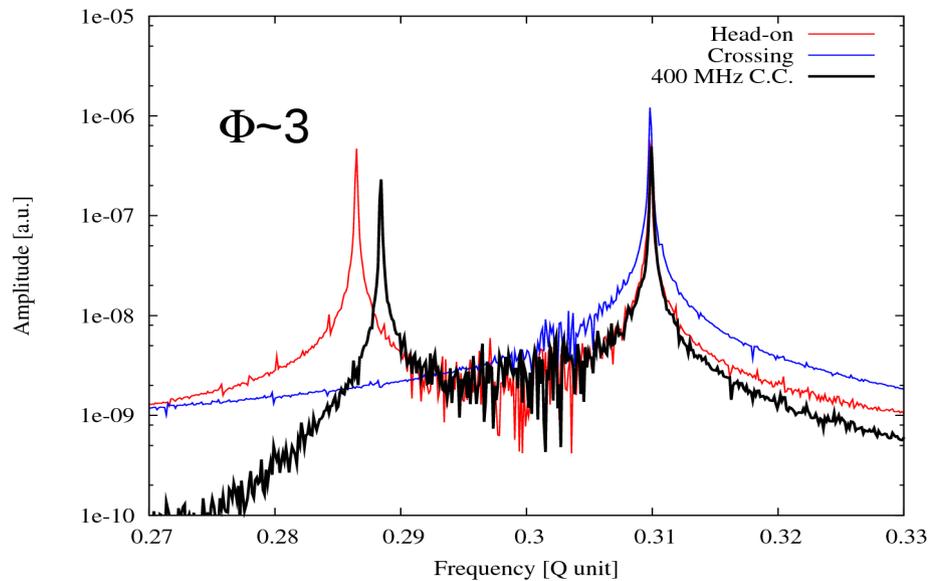
- Previous simulation using the weak-strong approximation. In reality the two beams couple and coherent beam modes develop:



- In the case of the LHC and for collisions in IP1 and IP5 only two modes develop: the 0-mode and the π -mode separated by $Y.\xi$
- This example shows the case of head-on collisions w.o. crossing angle using the 0.15 m beam parameters: what happens with crossing angle and C.C. ?

Damping of the π -mode

- It was shown by Y. Alexahin that for certain ratio of ξ / Q_s the side-bands of the continuum can overlap the π -mode and damp it. This effect should in principle be enhanced by the crossing angle



- $\Phi \sim 3$** : strong SB coupling + low $\xi \rightarrow \pi$ -mode fully damped
- $\Phi \sim 1$** : weaker SB coupling + higher $\xi \rightarrow \pi$ -mode not fully damped
- Crab cavities restore the π -mode**
- Short term simulations \rightarrow no information on lifetime/emittance but behavior for short term is very similar in all cases

Conclusions

- Taking the “nominal” HL-LHC beam parameters **the LR interactions seem to be a limitation**. Two mitigation scenarios were considered for this study:
 - **Increased β^*** : increased aperture, lower “virtual luminosity”
 - **Increased crossing angle**: enough aperture? High “virtual luminosity”
- Synchro-betatron effects looks similar for both cases:
 - Synchrotron sides-bands excited by the crossing angle
 - Under certain conditions they can damp the π -mode
 - **Removing the crossing angle w. C.C cancels these effects as well**
- **The effect of LR interactions needs to be assessed** to understand limitations
- **Experiments are required** to understand the detrimental/beneficiary effects of running with high synchro-betatron coupling
- C.C. are required to reach design goals for both scenarios considered