



6BA Lattice for FCC_{ee} injector Damping Ring



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General considerations

The DR requirements are fixed by the Booster Ring (BR) parameters (see [Injector Table](#))

Land footprint is defined by the available space ($\sim 120 \times 120 \text{ m}^2$)

Realistic design would imply:

- Dipoles Field $< 1\text{T}$ (normal conducting)
- Wiggler Field $< 1.9 \text{ T}$ (normal conducting)
- Quadrupole Gradient $k_Q < 50 \text{ T/m}$ (5.25 m^{-2} in MAD units)
- Sextupole strength $k_S < 1700 \text{ T/m}^2$ (182 m^{-3} in MAD units)
- Minimal element spacing $L_\delta > 8 \text{ cm}$
- Element length: $L_{\text{QUA}} > 20 \text{ cm}$, $L_{\text{SXP}} (L_{\text{OCT}}/L_{\text{KCK}}/\dots) > 10 \text{ cm}$

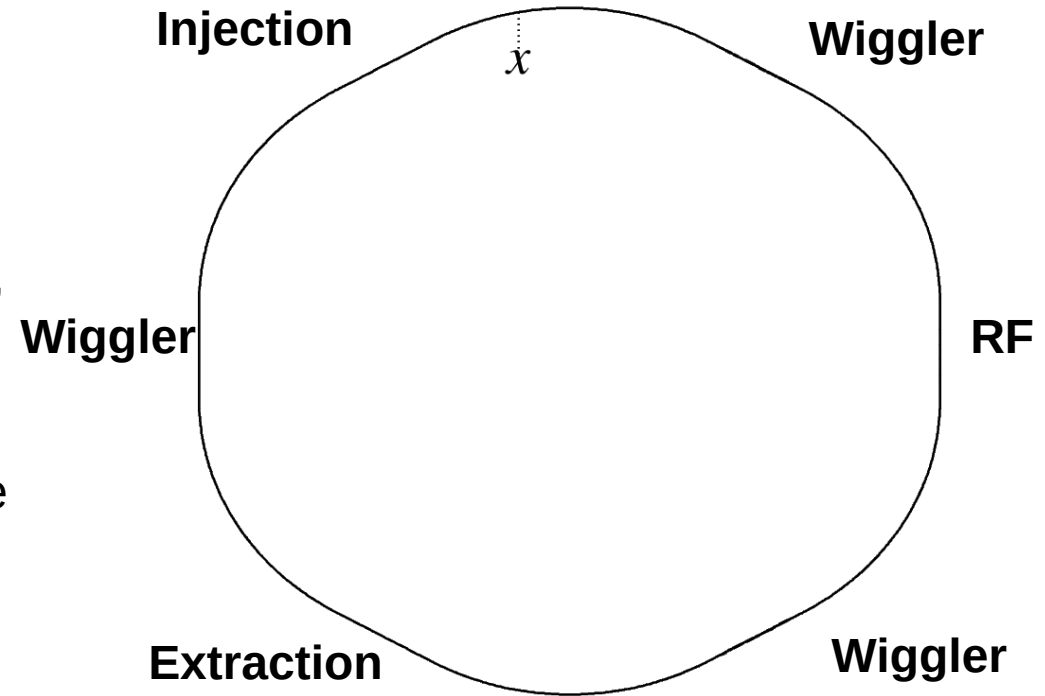
Ring layout

Hexagonal shape: 6 Arcs + 6 Straight

Arcs based on Six Bend Achromat (6BA)

Straight sections used for specialized purpose: Injection or extraction, wigglers, RF cavity

Playing with optical functions possible to have super-periodicity of three (as for the triangle shaped DR)





Six Bend Achromat (Mod 2)



Six Bend Achromat cell (6BA-v4.0)

$L_{\text{cell}} = 10.60 \text{ m}$

$L_{\text{dipole}} = 0.5\text{-}0.7 \text{ m}$ ($B_d = 0.7563 \text{ T}$)

$N_{\text{qua}} = 15$

$L_{\text{qua}} = 0.30 \text{ m}$

$N_{\text{sxp}} = 6$

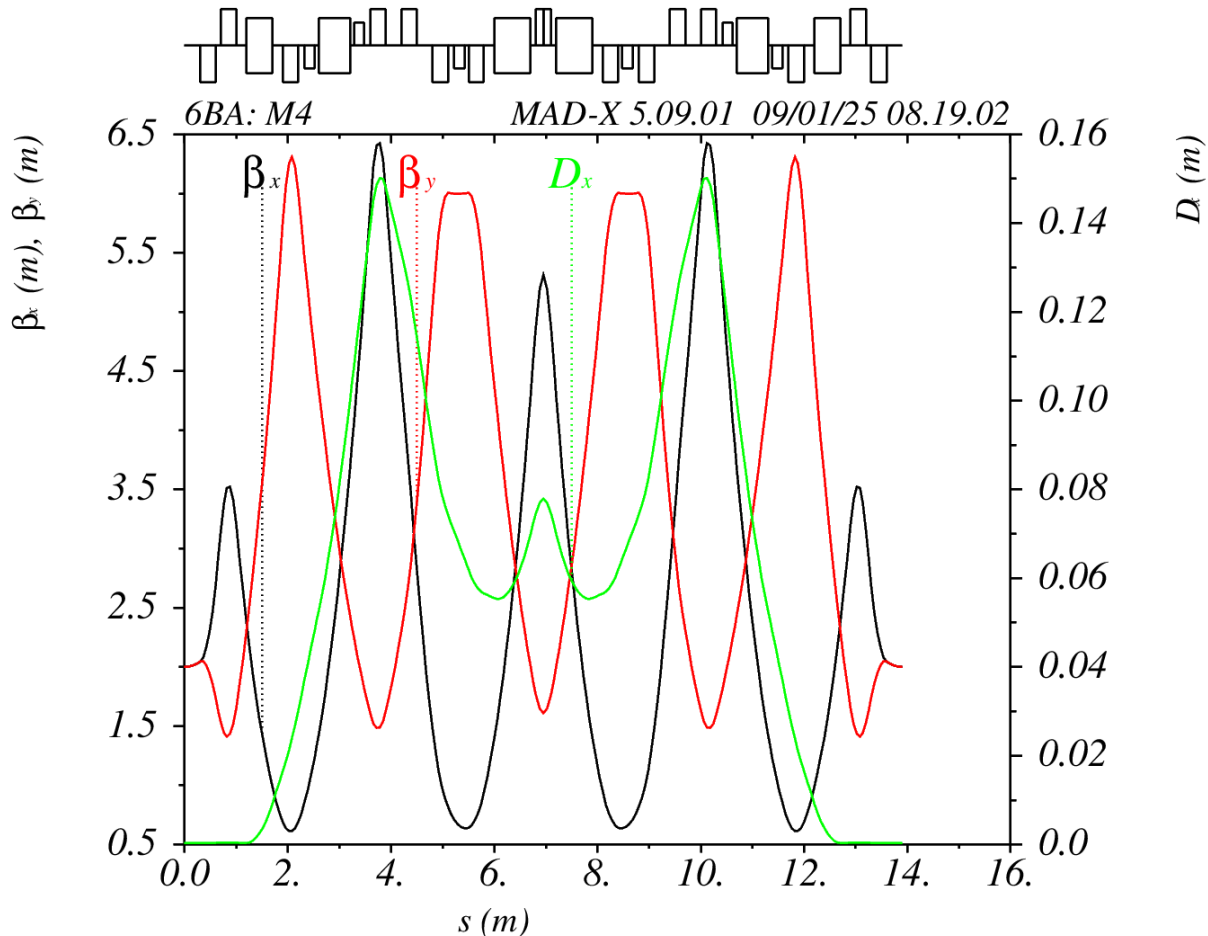
$L_{\text{sxp}} = 0.20 \text{ m}$

MAD-X Output:

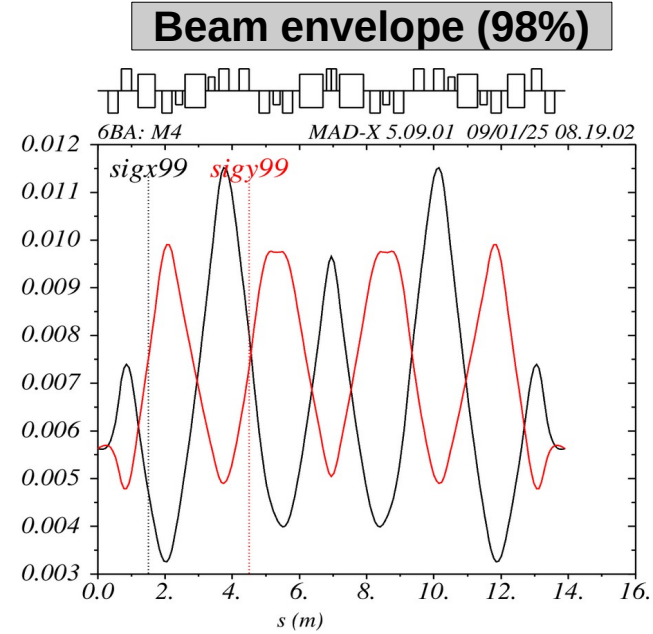
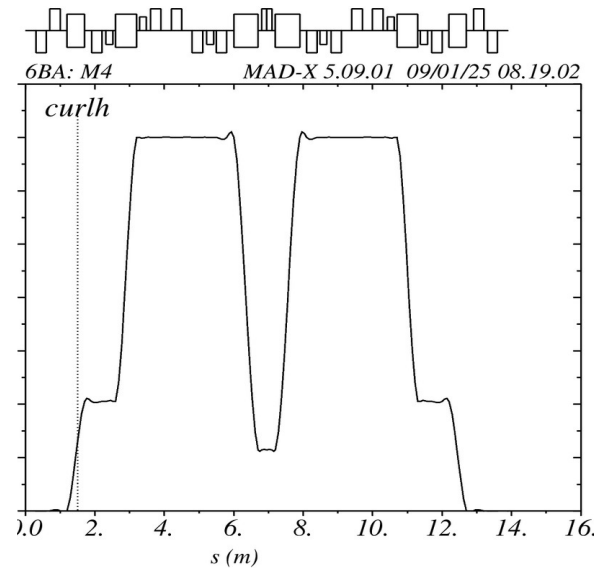
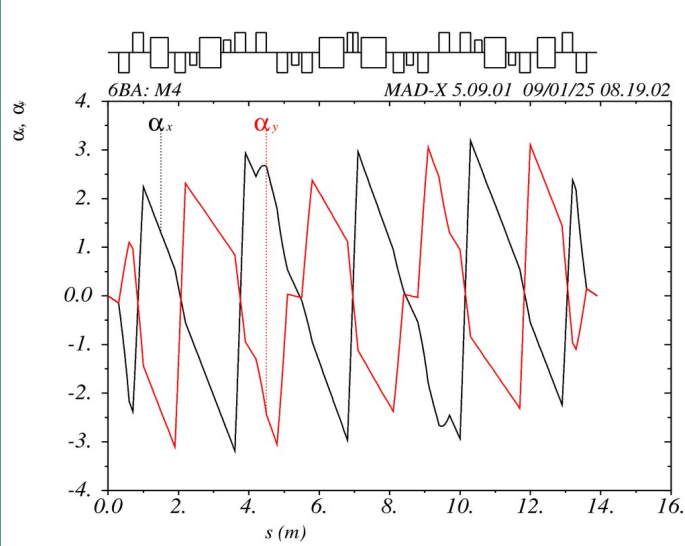
B6A CELL v4.0		
d_delta	=	0.08 ;
d_0	=	0.3 ;
d_1	=	0.1 ;
d_2	=	0.2 ;
d_3	=	0.2 ;
d_4	=	0.4 ;
d_5	=	0.4 ;
d_6	=	0.3 ;
d_7	=	0.3 ;
d_8	=	0.4 ;
d_9	=	0.2 ;
d_10	=	0.1 ;

b6a_kq1	=	-2.49899 ;
b6a_kq2	=	4.77148 ;
b6a_kq3	=	-3.03173 ;
b6a_kq4	=	3.36248 ;
b6a_kq5	=	0.803115 ;
b6a_kq6	=	-1.95099 ;
b6a_kq7	=	-1.48641 ;
b6a_kq8	=	3.98903 ;

b6a_ks1	=	-76.44393826 ;
b6a_ks2	=	142.8261129 ;
b6a_ks3	=	-161.0564271 ;



Six Bend Achromat cell (6BA)



$$\epsilon_{inj}(h/v) = 2.38 \text{ mm mrad}$$

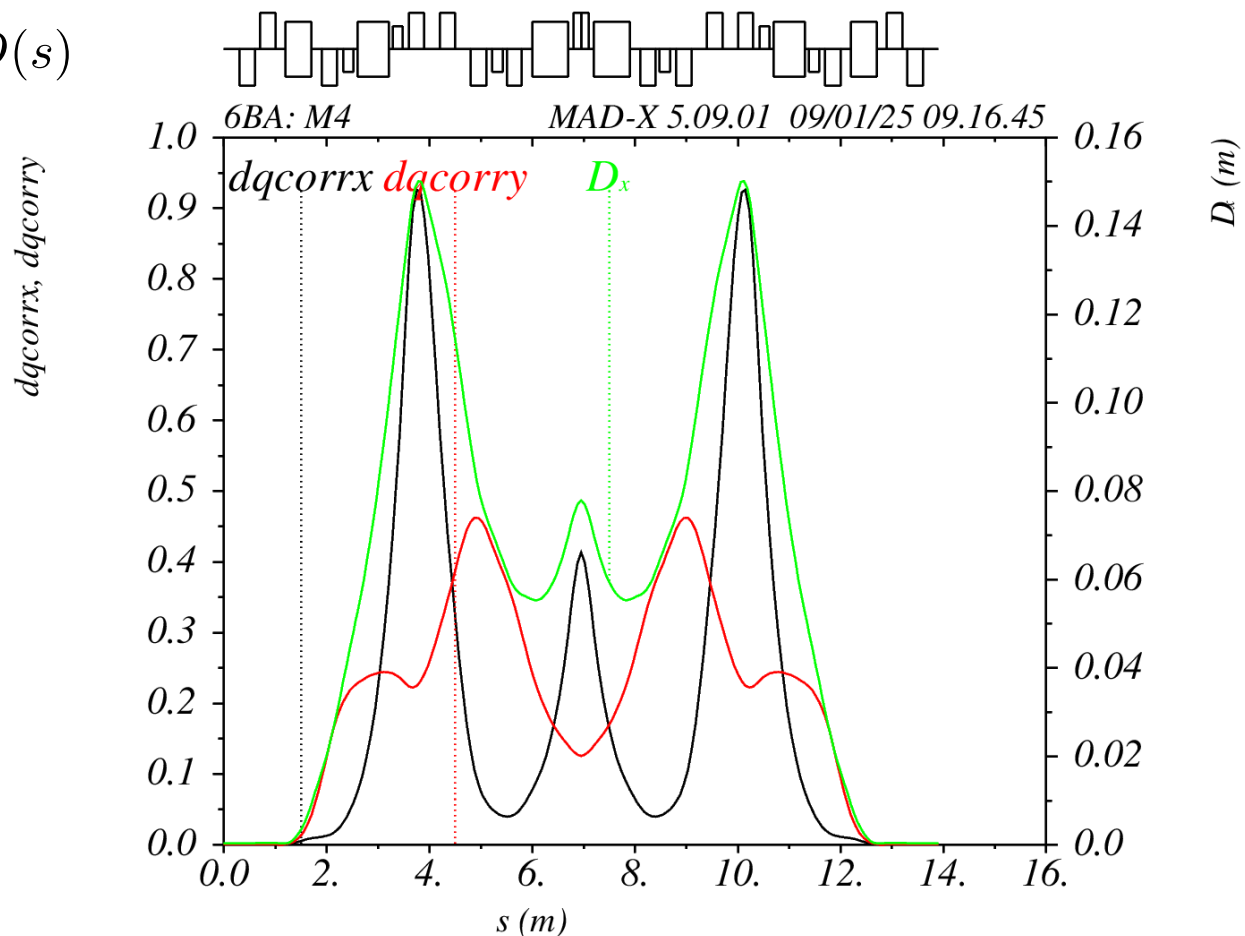
6BA Cell: Sextupoles

$$\Delta\xi_{xy}(m_S) \propto m_S \int ds \beta_{x,y}(s) D(s)$$

Sextupoles placements have been optimized in order to ensure the minimal strengths

Three family have been defined two for the vertical correction and one for the horizontal

The chromaticity correction is localized only in the arcs for the whole ring.





Straight sections elements



Injection/extraction sections

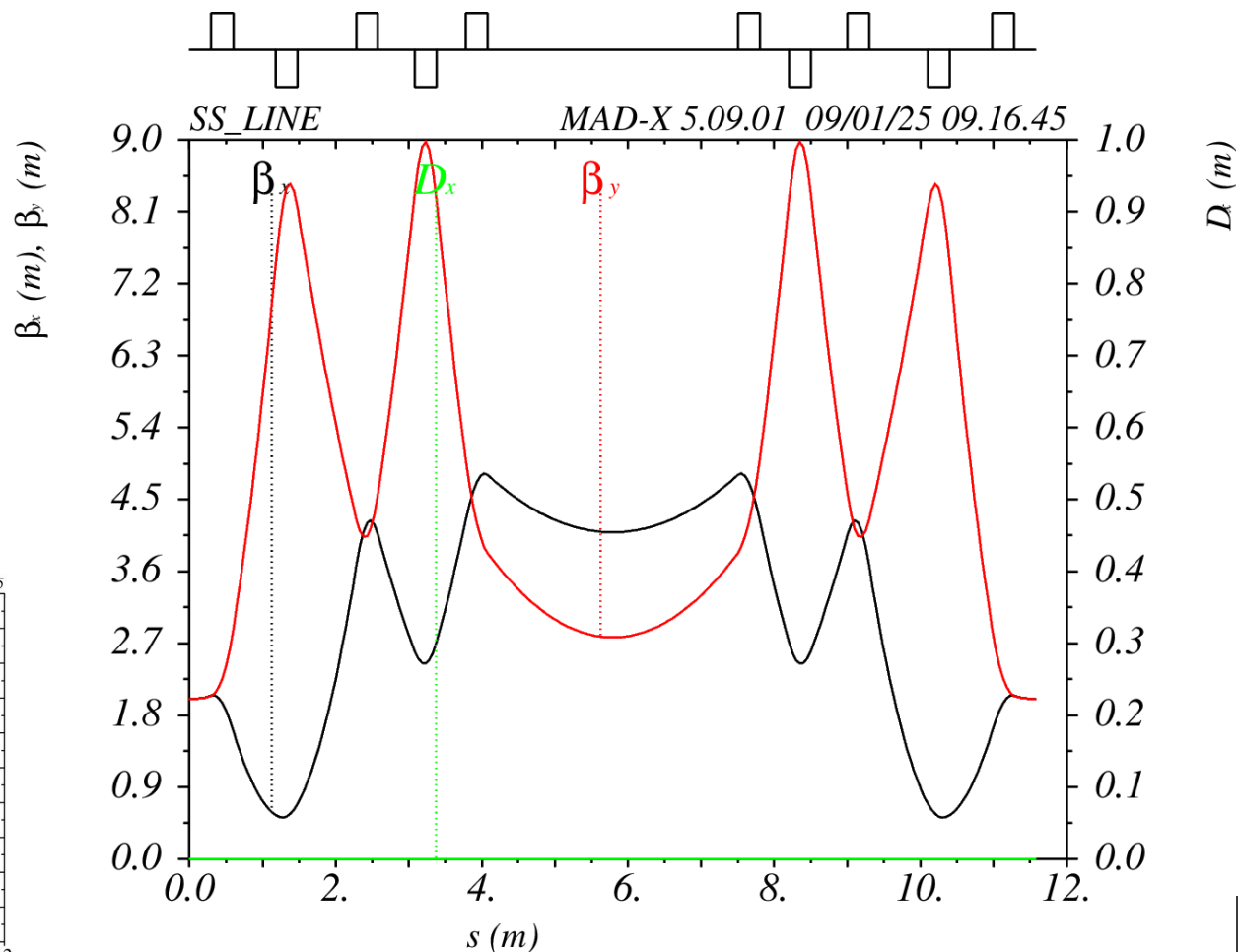
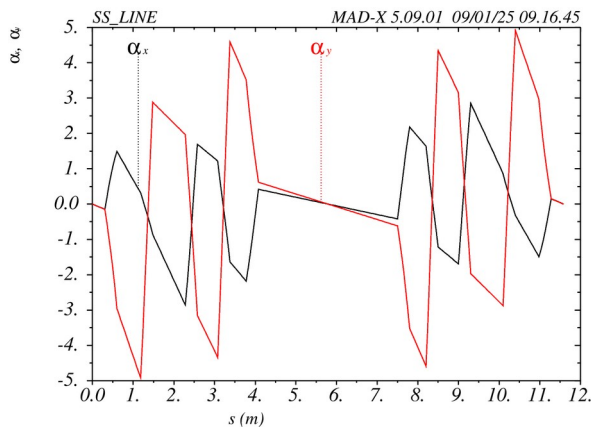
$L_{SS} = 11.58$

$L_{free} = 3.42$ m

STRAIGHT SECTIONS:

ss_ld1	=	0.3 ;
ss_ld2	=	0.58 ;
ss_ld3	=	0.8 ;
ss_ld4	=	0.5 ;
ss_ld5	=	0.4 ;
ss_ld6	=	1.71 ;

sstkq1	=	3.38578576 ;
sstkq2	=	-3.287172054 ;
sstkq3	=	3.906317017 ;
sstkq4	=	-3.514177296 ;
sstkq5	=	1.976167573 ;



Wiggler sections

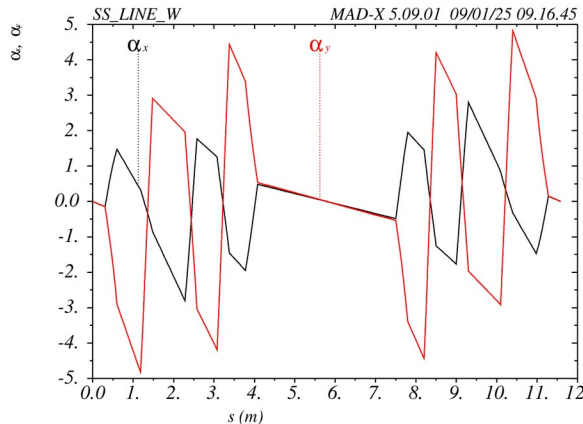
$L_{SS} = 11.58$

$L_{free} = 3.42$ m

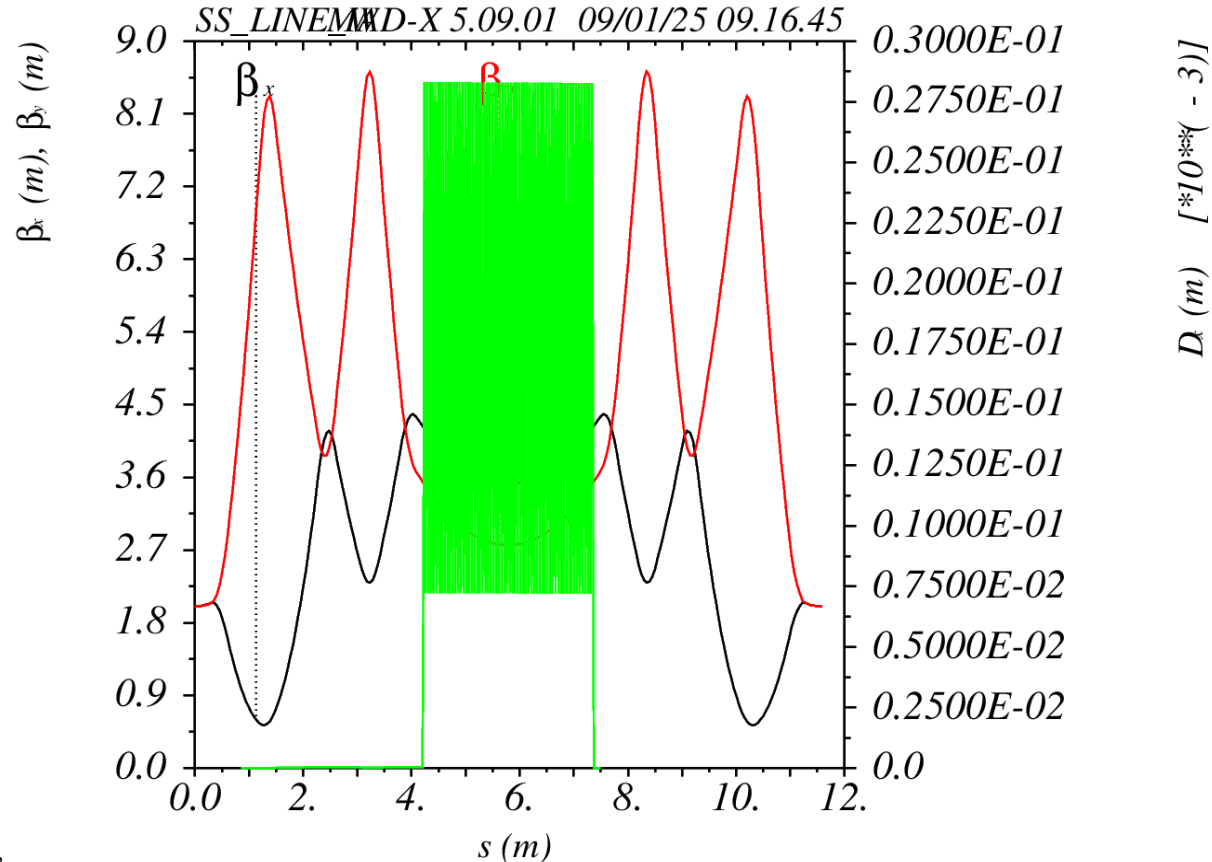
STRAIGHT SECTIONS:

ss_ld1	=	0.3 ;
ss_ld2	=	0.58 ;
ss_ld3	=	0.8 ;
ss_ld4	=	0.5 ;
ss_ld5	=	0.4 ;
ss_ld6	=	1.71 ;

sswkq1	=	3.333698249 ;
sswkq2	=	-3.307536882 ;
sswkq3	=	3.976927425 ;
sswkq4	=	-3.535394196 ;
sswkq5	=	2.033934488 ;



$B_{wgl} = 1.7$ T



RF sections

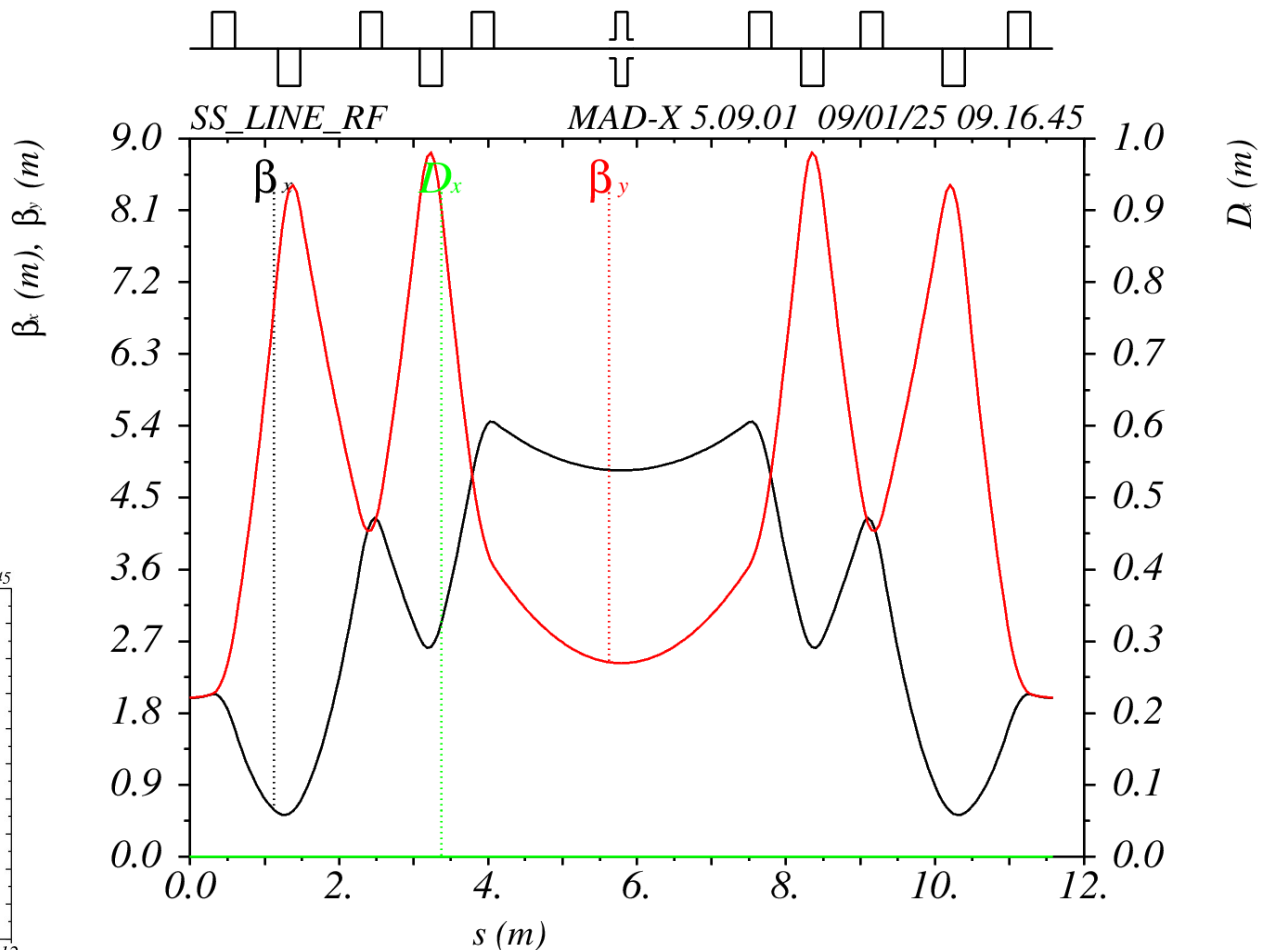
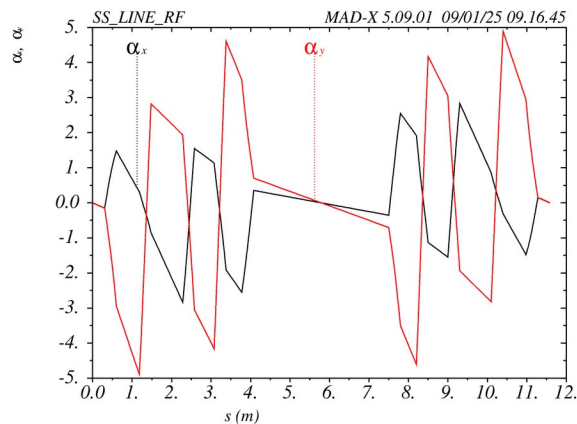
$L_{SS} = 11.58$

$L_{free} = 3.42$ m

STRAIGHT SECTIONS:

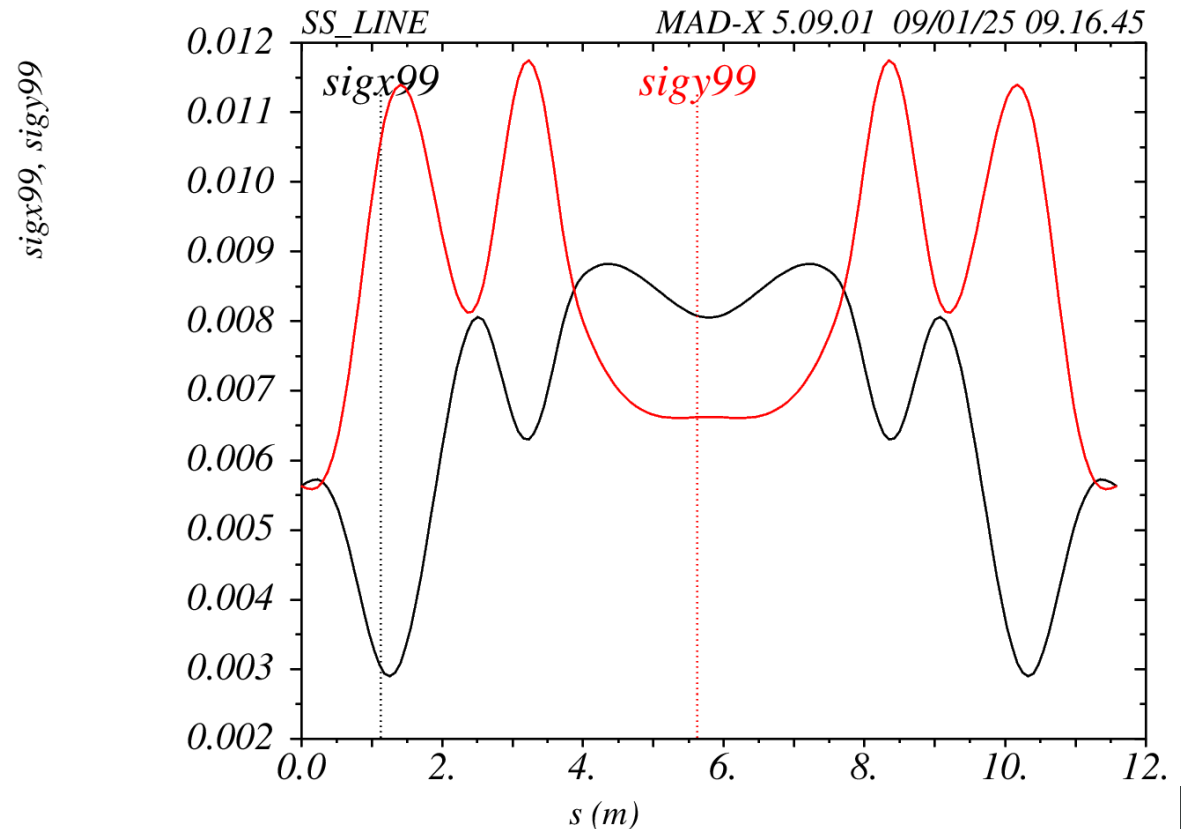
ss_ld1	=	0.3 ;
ss_ld2	=	0.58 ;
ss_ld3	=	0.8 ;
ss_ld4	=	0.5 ;
ss_ld5	=	0.4 ;
ss_ld6	=	1.71 ;

ssrfkq1	=	3.374849605 ;
ssrfkq2	=	-3.263965846 ;
ssrfkq3	=	3.771890122 ;
ssrfkq4	=	-3.513106207 ;
ssrfkq5	=	1.962597868 ;



Beam envelope in the Straight Sections

$$\epsilon_{inj}(h/v) = 2.38 \text{ mm mrad}$$





Full Ring



Full ring parameters (6BA v4.0)

$L = 403.09 \text{ m}$

$T_{\text{per}} = 1.343 \mu\text{s}$;

$\alpha_c = 0.000761$

$N_{\text{cel}} = 24$

$Q_x = 39.479$

$Q_y = 21.988$

$\xi_x = 7.1\text{e-}9 \text{ (corr) / -49.93 (nat)}$

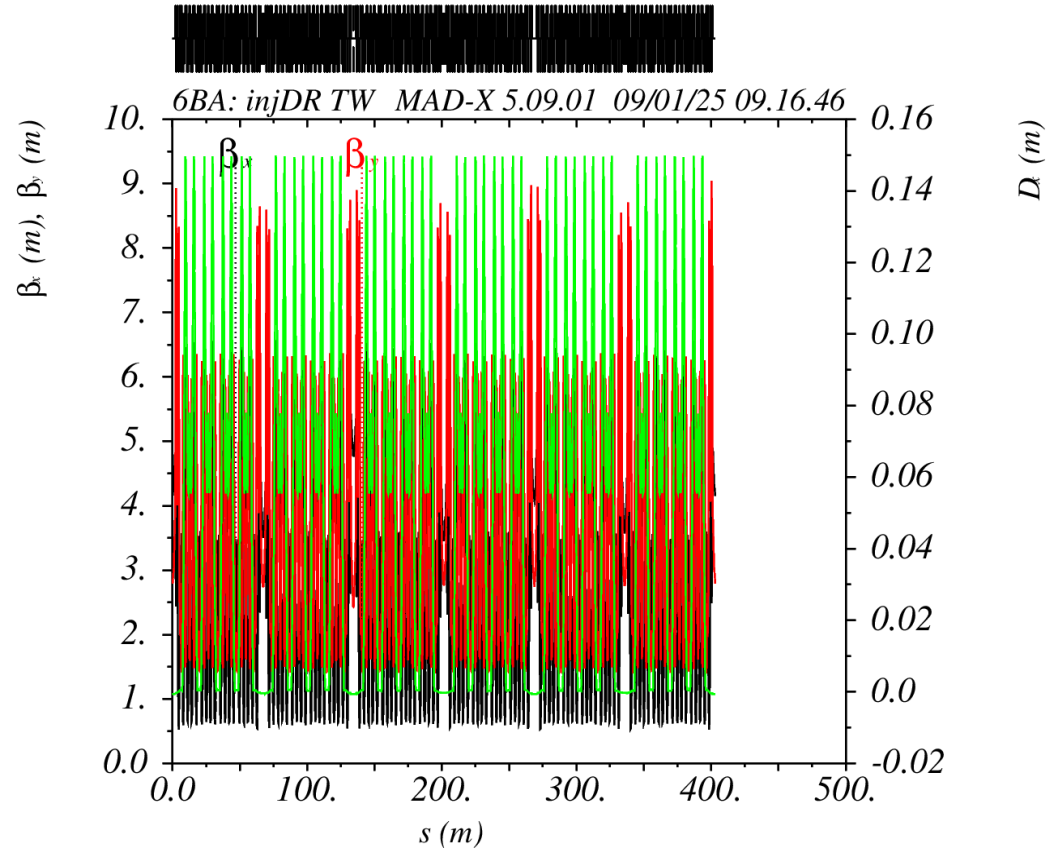
$\xi_y = 1.4\text{e-}8 \text{ (corr) / -37.99 (nat)}$

$\beta_x(\text{max}) = 6.67 \text{ m}$

$\beta_y(\text{max}) = 9.34 \text{ m}$

$U_0 = 571 \text{ keV}$

$\Delta E = 7.3\text{e-}4$



Full ring parameters (6BA Mod 2)

$$\epsilon = 1.81 \text{ nm rad}$$

$$\tau_x = 13.5 \text{ ms}$$

$$\tau_z = 6.7 \text{ ms}$$

Synchrotron integrals:

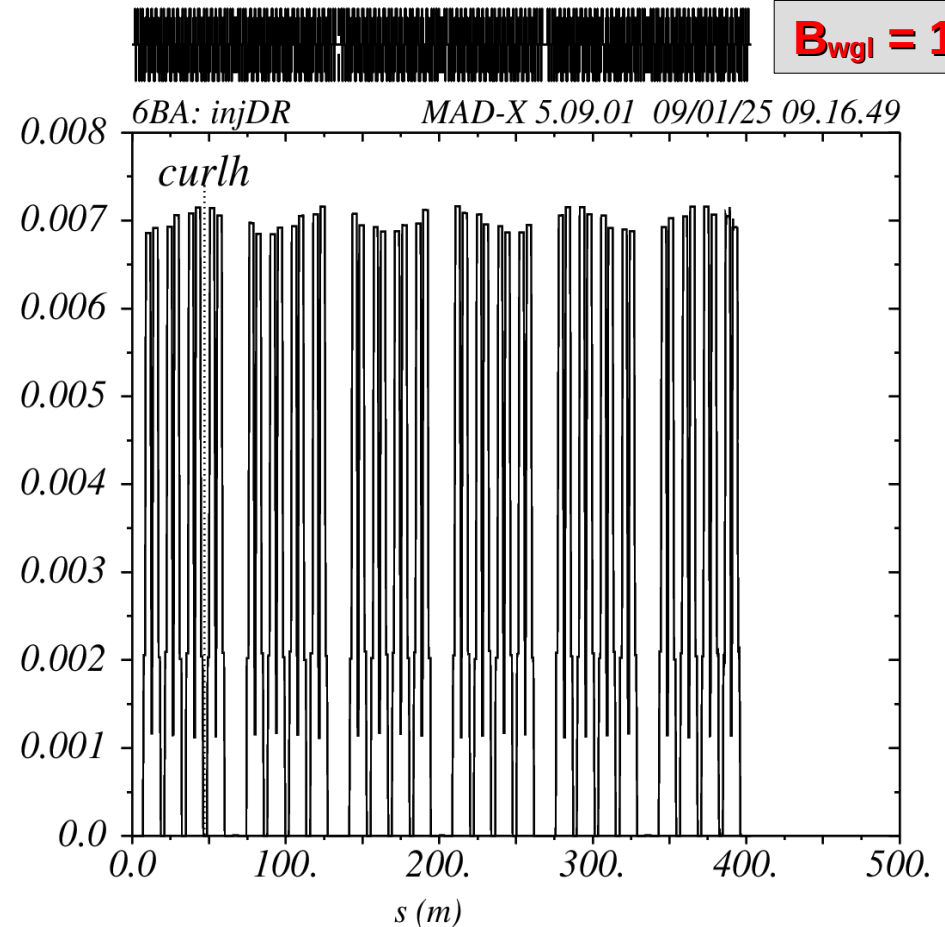
$$I_1 = 0.3069323495$$

$$I_2 = 0.6063789197$$

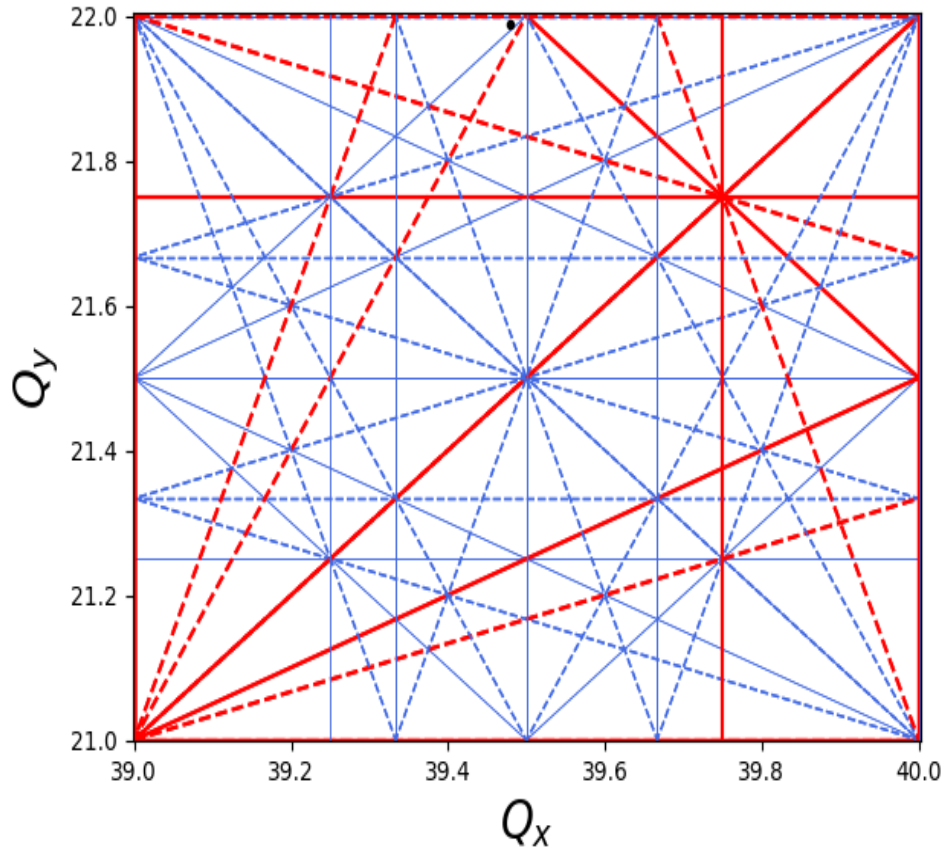
$$I_3 = 0.0541043725$$

$$I_4 = -7.663727305e-05$$

$$I_5 = 9.17944843e-05$$



Working point



Resonance Diagram:

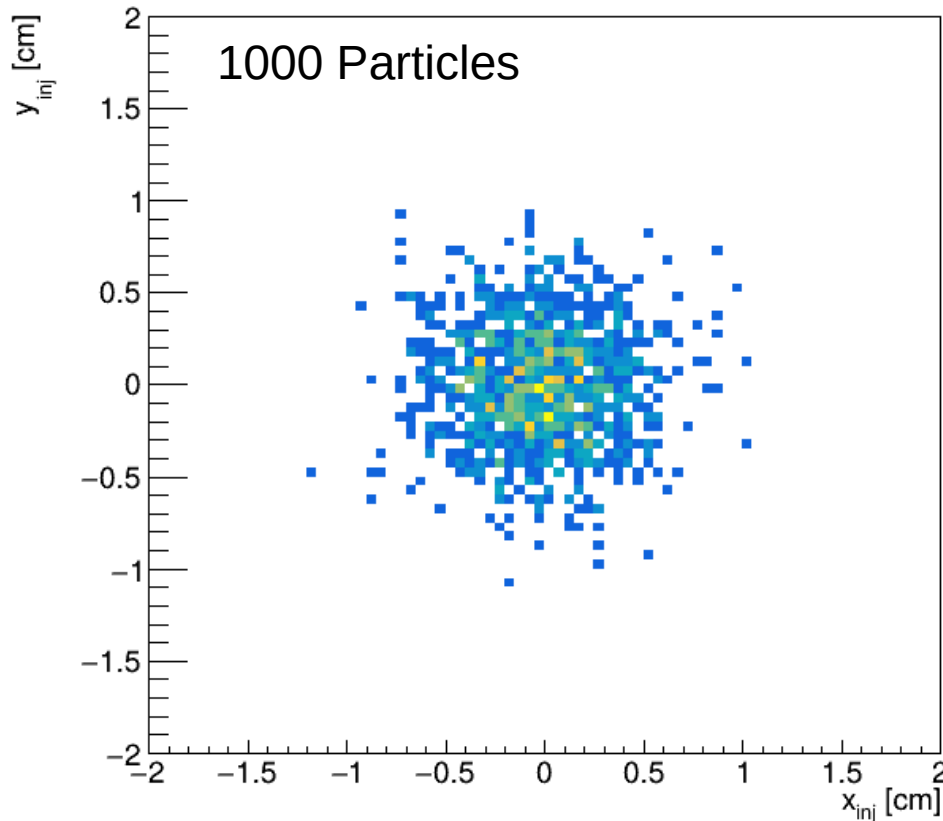
Solid lines are normal and dashed lines are skew resonance

Red and Blue are systematic and non-systematic resonances, respectively.

Superperiodicity of three (3) has been considered:
SS+Arc+SS_WGL+Arc

Working point have to be revised.
Too close to systematic resonances

Tracking results



Only Transverse motion (4D)

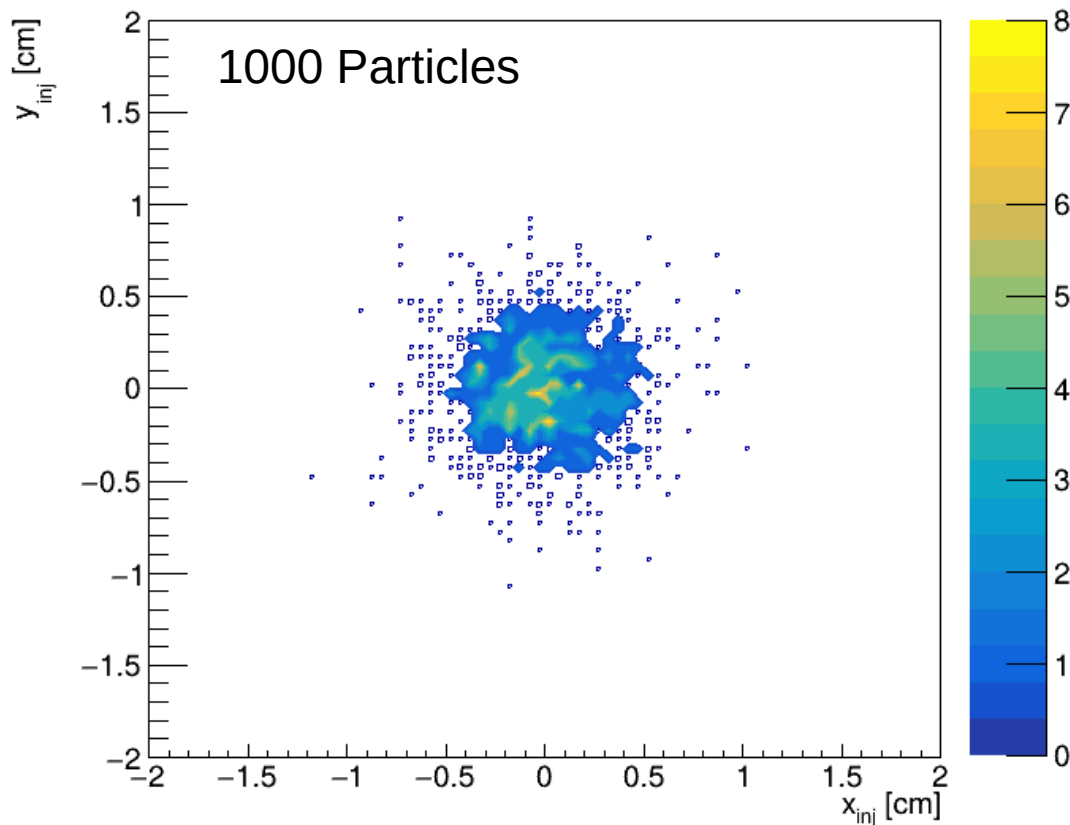
SXP ON

Beam injected in SS section with expected emittance (2.38 mm mrad) in both planes

Tracked for 1000 Turns

Beam Pipe physical apertures:
Horizontal: ± 3.0 cm
Vertical: ± 1.5 cm

Tracking results



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SXP ON

Beam injected in SS section with expected emittance (2.38 mm mrad) in both planes.

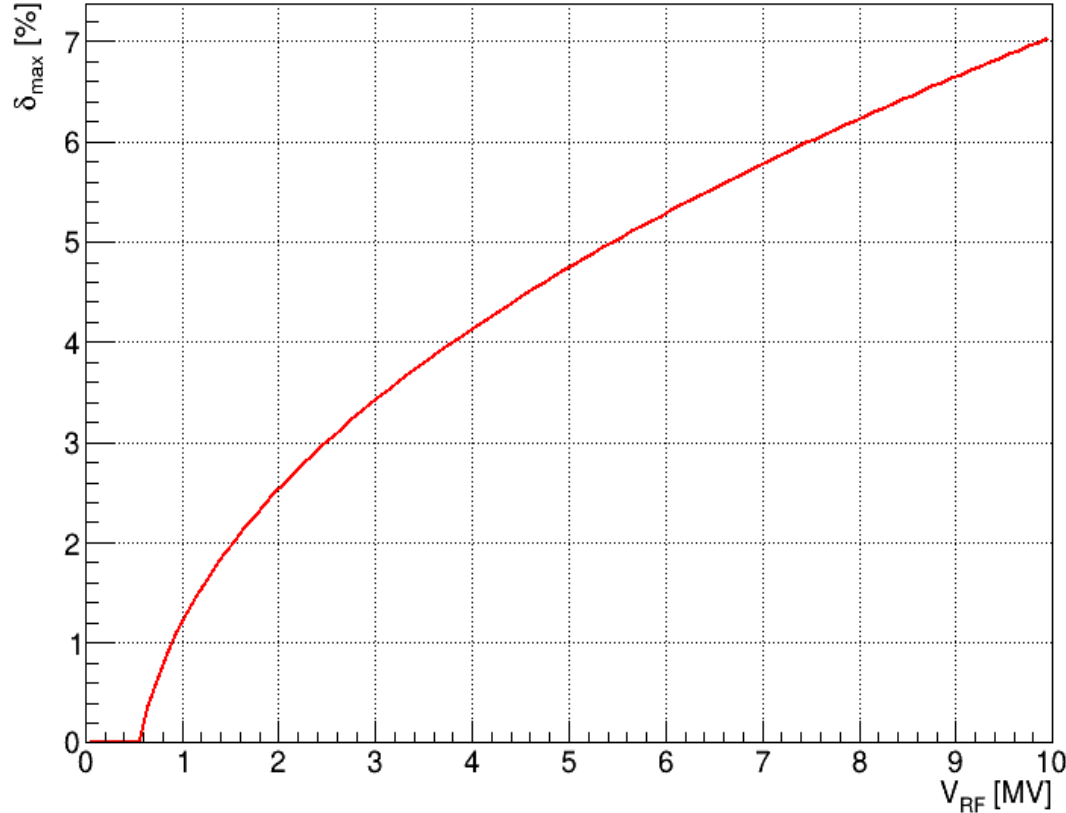
Tracked for 1000 Turns

Beam Pipe physical apertures:
Horizontal: ± 3.0 cm
Vertical: ± 1.5 cm

$$\epsilon_{acc} = \frac{432}{1000} = 43\%$$

Energy acceptance

6BA v4.0 energy acceptance



$$\alpha_p = 0.000761$$

$$h = 537$$

$$E_{\text{beam}} = 2.86 \text{ GeV}$$

Sync. phase

$$\phi_s = \pi - \sin^{-1} \left(\frac{U_0}{eV_{RF}} \right)$$

Sync. tune

$$\nu_s = \sqrt{-\frac{eV_{RF} h \alpha_p}{E_0} \cos \phi_s}$$

RF Acceptance

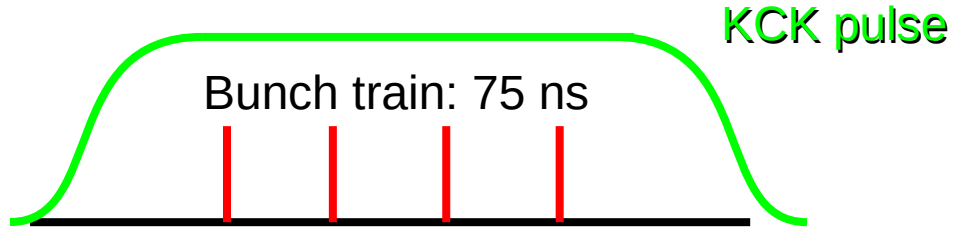
$$|\delta|_{\max, RF} = \frac{2\nu_s}{h\alpha_p} \sqrt{1 - \left(\frac{\pi}{2} - \phi_s \right) \tan \phi_s}$$



Timing considerations



Minimal damping time



$$n(\text{train}) = \frac{T_{per}}{\Delta t + t_K} \simeq 10$$

$$\epsilon(t) = \epsilon_{inj} e^{-\frac{2t}{\tau}}$$

$$T_{store} = -\frac{\tau}{2} \ln \frac{\epsilon_{ext}}{\epsilon_0} \simeq 5\tau$$

$$\tau \leq \frac{n(\text{train})T_{pulse}}{5(\Delta t + t_K)} \simeq 20 \text{ ms}$$