

# Collective isovector valence-shell excitations in the N=84 isotone $^{138}\text{Xe}$



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(U. Sofia)

**F. Browne**  
(U. Manchester)

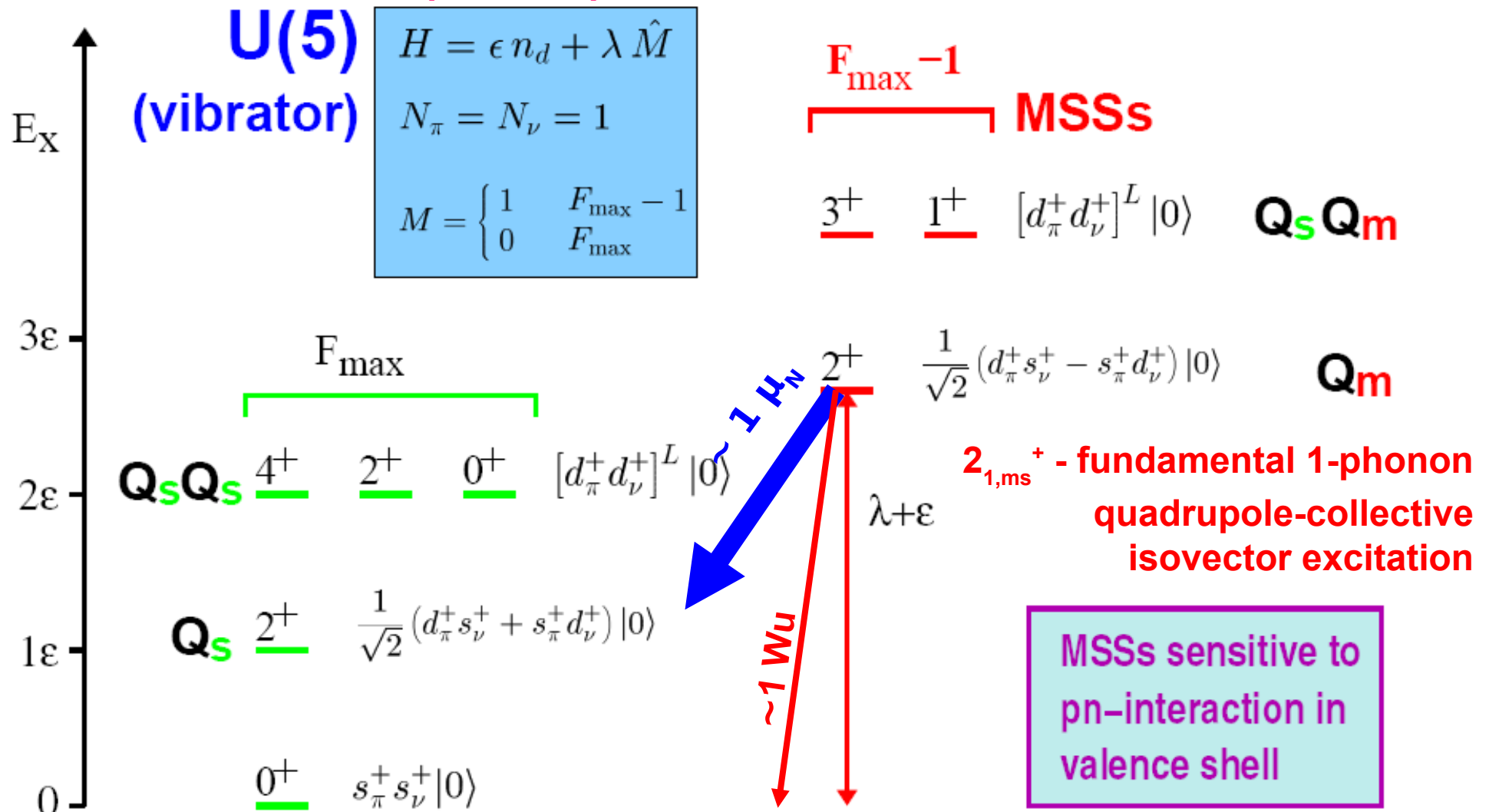
**N. Warr**  
(U. Cologne, U. Liverpool)

**Contact: C. Porzio**

# Mixed-Symmetry States (isovector)



Simple Example: Harmonic Oscillator,  $N=2$



IBM-2 A. Arima, F. Iachello

# Studies near N=82



- $^{142}\text{Sm}$ : ISOLDE (CoulEx)  
+ HIL (angular correlations)

Kern, PhD thesis TU Darmstadt  
Stetz, TU Darmstadt, in progress

- $^{140}\text{Nd}$ : ISOLDE (CoulEx)  
+ Yale, Cologne (ang. corr./DSAM)

Kern, PRC 102, 041304(R) (2020)  
Williams, PRC 80 / Gladniski PRC 82

- $^{138}\text{Ce}$ : ANL (CoulEx+ang. corr.)  
Rainovski, PRL 96, 122501 (2006)

- $^{136}\text{Ba}$ : Stuttgart (NRF)  
Pietralla, PRC 58, 796 (1998)

- $^{134}\text{Xe}$ : ANL (CoulEx)  
Ahn, PLB 679, 19 (2009)

- $^{132}\text{Te}$ : ORNL (CoulEx,  $\beta$ -decay)  
+ IFIN-HH (2n-transfer/DSAM)  
Danchev, PRC 84, 061306(R) (2011)  
Stetz/Mayr, TU Darmstadt, in progress

$^{142}\text{Eu}$ $\beta^+$	$^{143}\text{Eu}$ $\beta^+$	$^{144}\text{Eu}$ $\beta^+$	$^{145}\text{Eu}$ $\beta^+$	$^{146}\text{Eu}$ $\beta^+$	$^{147}\text{Eu}$ $\beta^+$	$^{148}\text{Eu}$ $\beta^+$
$^{141}\text{Sm}$ $\beta^+$	$^{142}\text{Sm}$ $\beta^+$	$^{143}\text{Sm}$ $\beta^+$	$^{144}\text{Sm}$ $2\beta^+$	$^{145}\text{Sm}$ e- capture	$^{146}\text{Sm}$ $\alpha$	$^{147}\text{Sm}$ $\alpha$
$^{140}\text{Pm}$ $\beta^+$	$^{141}\text{Pm}$ $\beta^+$	$^{142}\text{Pm}$ $\beta^+$	$^{143}\text{Pm}$ e- capture	$^{144}\text{Pm}$ e- capture	$^{145}\text{Pm}$ e- capture	$^{146}\text{Pm}$ e- capture
$^{139}\text{Nd}$ $\beta^+$	$^{140}\text{Nd}$ e- capture	$^{141}\text{Nd}$ $\beta^+$	$^{142}\text{Nd}$ Stable	$^{143}\text{Nd}$ Stable	$^{144}\text{Nd}$ $\alpha$	$^{145}\text{Nd}$ $\alpha$
$^{138}\text{Pr}$ $\beta^+$	$^{139}\text{Pr}$ $\beta^+$	$^{140}\text{Pr}$ $\beta^+$	$^{141}\text{Pr}$ Stable	$^{142}\text{Pr}$ $\beta^-$	$^{143}\text{Pr}$ $\beta^-$	$^{144}\text{Pr}$ $\beta^-$
$^{137}\text{Ce}$ $\beta^+$	$^{138}\text{Ce}$ $2\beta^+$	$^{139}\text{Ce}$ e- capture	$^{140}\text{Ce}$ Stable	$^{141}\text{Ce}$ $\beta^-$	$^{142}\text{Ce}$ $\alpha$	$^{143}\text{Ce}$ $\beta^-$
$^{136}\text{La}$ $\beta^+$	$^{137}\text{La}$ e- capture	$^{138}\text{La}$ $\beta^+$	$^{139}\text{La}$ Stable	$^{140}\text{La}$ $\beta^-$	$^{141}\text{La}$ $\beta^-$	$^{142}\text{La}$ $\beta^-$
$^{135}\text{Ba}$ Stable	$^{136}\text{Ba}$ Stable	$^{137}\text{Ba}$ Stable	$^{138}\text{Ba}$ Stable	$^{139}\text{Ba}$ $\beta^-$	$^{140}\text{Ba}$ $\beta^-$	$^{141}\text{Ba}$ $\beta^-$
$^{134}\text{Cs}$ $\beta^-$	$^{135}\text{Cs}$ $\beta^-$	$^{136}\text{Cs}$ $\beta^-$	$^{137}\text{Cs}$ $\beta^-$	$^{138}\text{Cs}$ $\beta^-$	$^{139}\text{Cs}$ $\beta^-$	$^{140}\text{Cs}$ $\beta^-$
$^{133}\text{Xe}$ $\beta^-$	$^{134}\text{Xe}$ $2\beta^-$	$^{135}\text{Xe}$ $\beta^-$	$^{136}\text{Xe}$ $2\beta^-$	$^{137}\text{Xe}$ $\beta^-$	$^{138}\text{Xe}$ $\beta^-$	$^{139}\text{Xe}$ $\beta^-$
$^{132}\text{I}$ $\beta^-$	$^{133}\text{I}$ $\beta^-$	$^{134}\text{I}$ $\beta^-$	$^{135}\text{I}$ $\beta^-$	$^{136}\text{I}$ $\beta^-$	$^{137}\text{I}$ $\beta^-$	$^{138}\text{I}$ $\beta^-$
$^{131}\text{Te}$ $\beta^-$	$^{132}\text{Te}$ $\beta^-$	$^{133}\text{Te}$ $\beta^-$	$^{134}\text{Te}$ $\beta^-$	$^{135}\text{Te}$ $\beta^-$	$^{136}\text{Te}$ $\beta^-$	$^{137}\text{Te}$ $\beta^-$
$^{130}\text{Sb}$ $\beta^-$	$^{131}\text{Sb}$ $\beta^-$	$^{132}\text{Sb}$ $\beta^-$	$^{133}\text{Sb}$ $\beta^-$	$^{134}\text{Sb}$ $\beta^-$	$^{135}\text{Sb}$ $\beta^-$	$^{136}\text{Sb}$ $\beta^-$
$^{129}\text{Sn}$ $\beta^-$	$^{130}\text{Sn}$ $\beta^-$	$^{131}\text{Sn}$ $\beta^-$	$^{132}\text{Sn}$ $\beta^-$	$^{133}\text{Sn}$ $\beta^-$	$^{134}\text{Sn}$ $\beta^-$	$^{135}\text{Sn}$ $\beta^-$

- $^{144}\text{Nd}$ : UKY ( $n, n'\gamma$ )  
Hicks, PRC 57, 2264 (1998)

- $^{142}\text{Ce}$ : UKY ( $n, n'\gamma$ )  
Vanhoy, PRC 52, 2387 (1995)

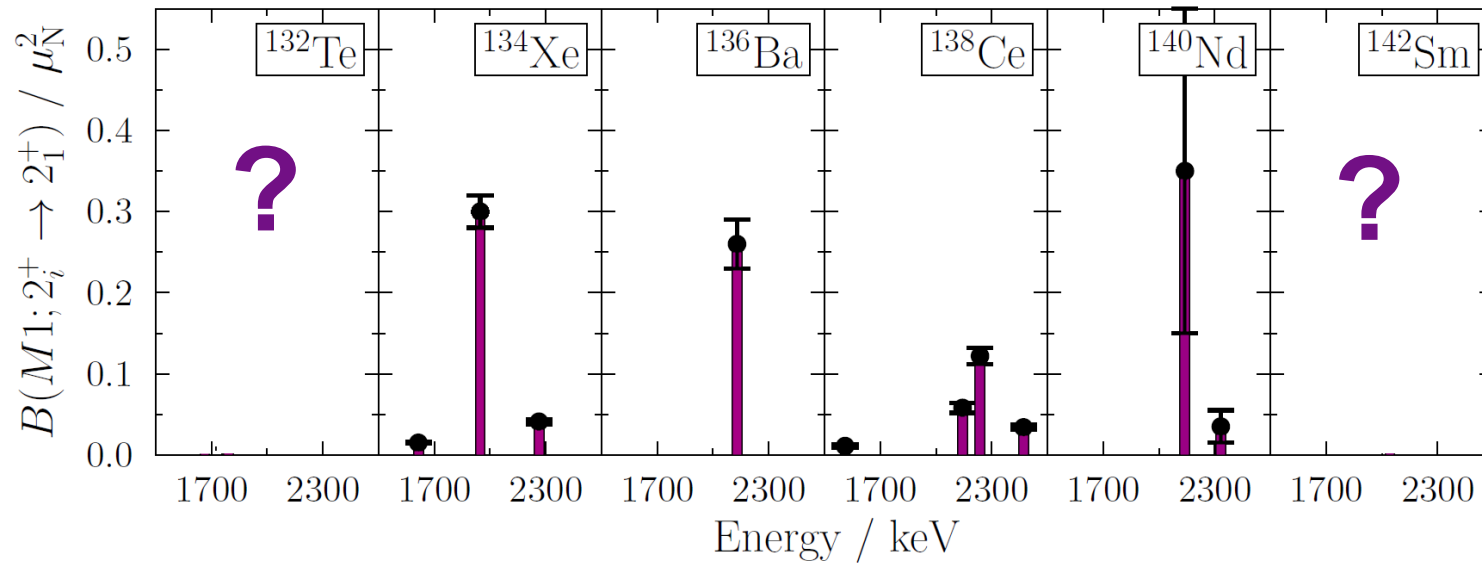
- $^{138}\text{Xe}$ : **This Proposal**

# N=80:

## $2_{ms}^+ \rightarrow 2_1^+$ systematics to date



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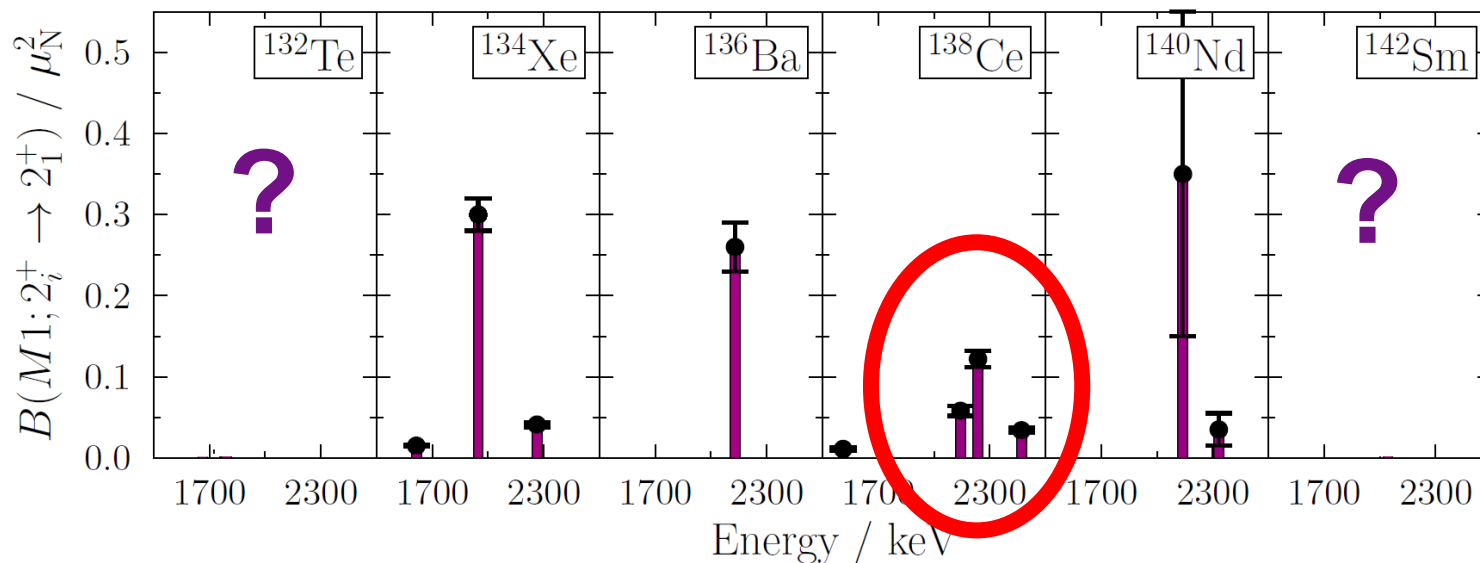


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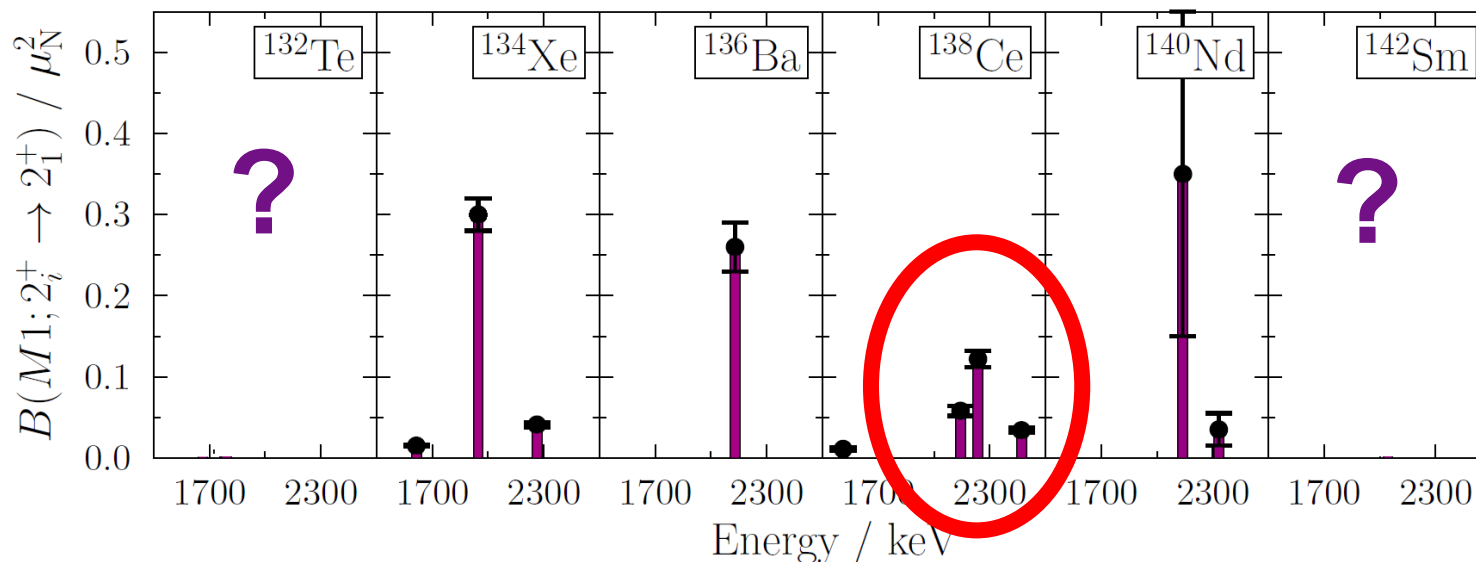
- Fragmentation at  $^{138}\text{Ce}$  – has been discussed in terms of  $\pi g_{7/2}$  sub-shell
- Complicated configurations lead to mixing with nearby symm. state(s)
- Restoration of “F-Spin” above  $^{138}\text{Ce}$

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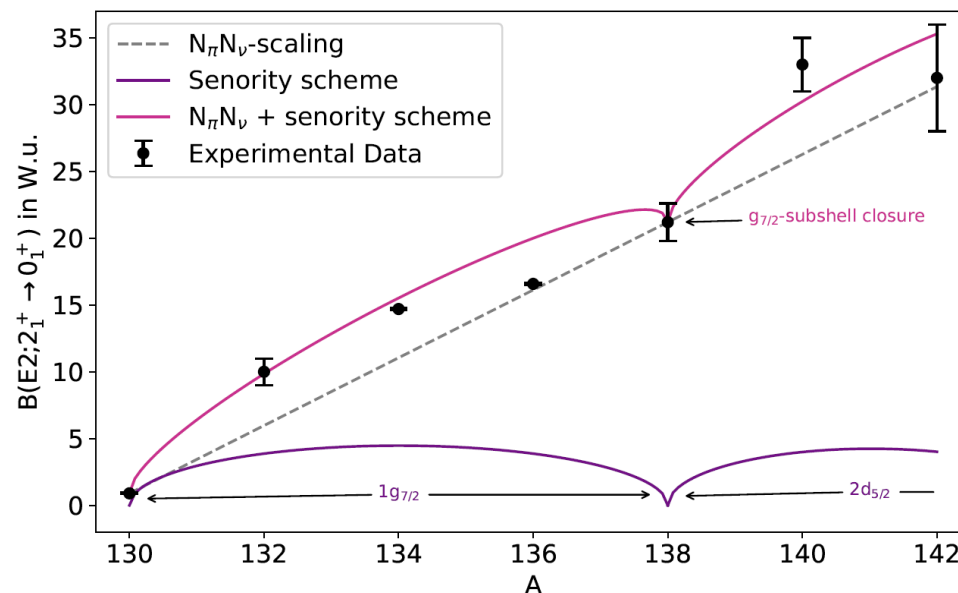
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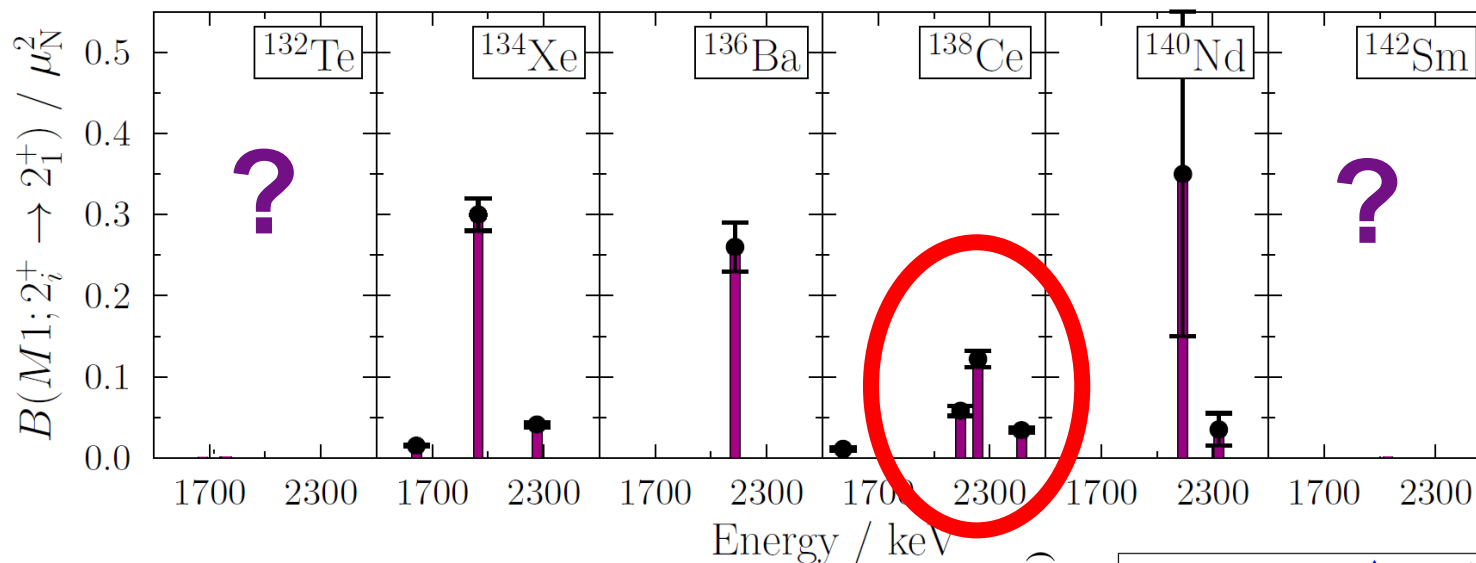


# N = 80:

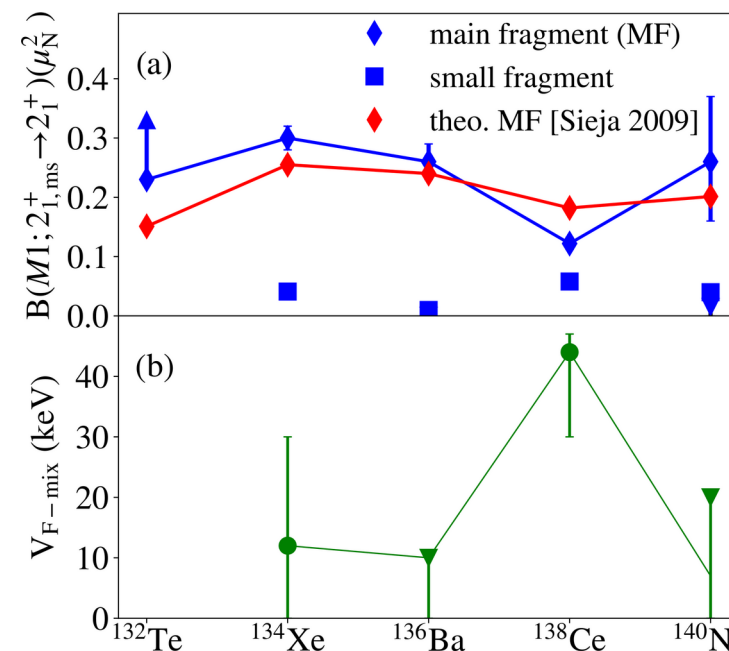
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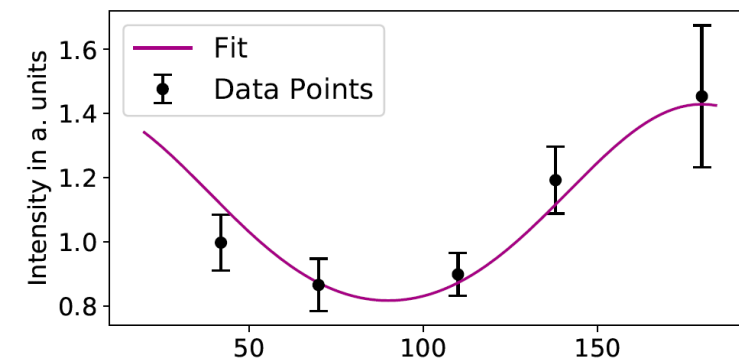
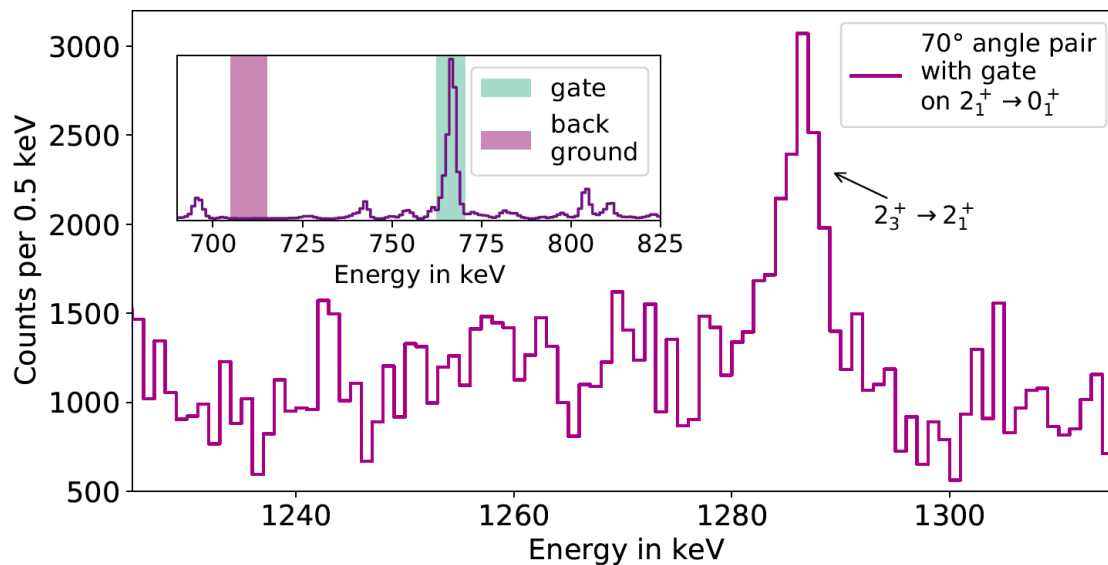
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# Most recent on $N = 80$ : $^{142}\text{Sm}$



- Original experiment at ISOLDE: Coulex of  $^{142}\text{Sm}$  beam
  - yielded CouEx cross sections
- Follow-up experiment at HIL:  $\gamma$ -spectroscopy after  $\beta$ -decays  $^{142}\text{Gd} \rightarrow ^{142}\text{Eu} \rightarrow ^{142}\text{Sm}$
- HIL Cyclotron + EAGLE HPGe Array



Preliminary result  
multipole mixing ratio:  
**-0.09(8)**  
→ almost pure M1  
transition

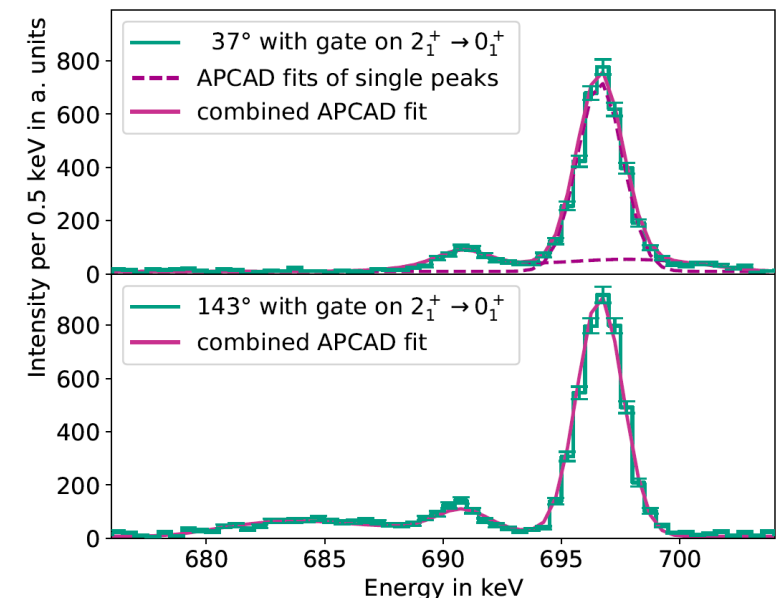
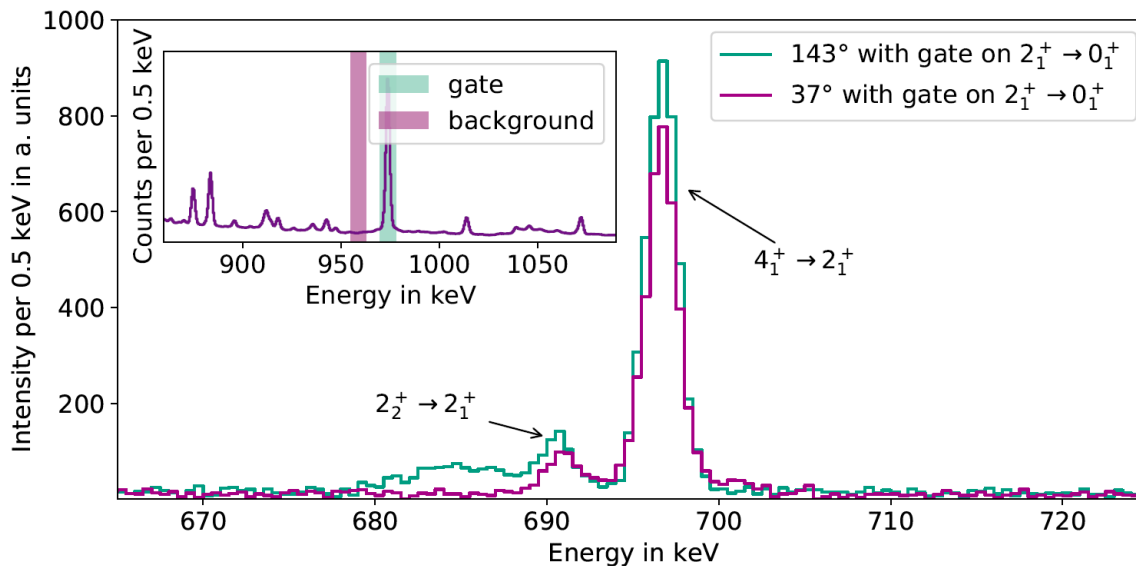
T. Stetz, PhD student, TU Darmstadt



# Most recent on $N = 80$ : $^{132}\text{Te}$



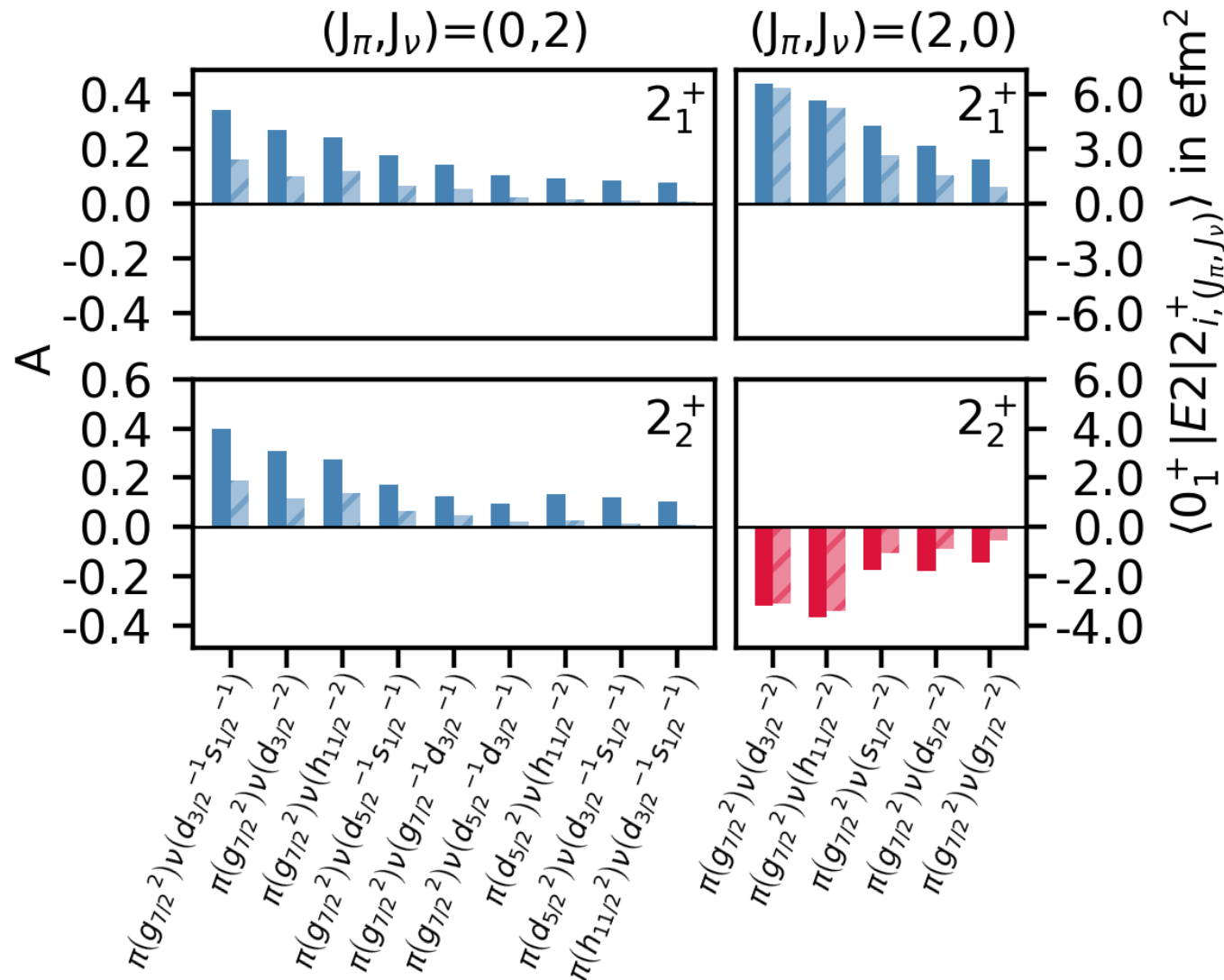
- CoulEx experiment ORNL (Danchev et al.):  $B(M1) > 0.23 \mu_N^2$ 
  - huge systematic uncertainties (g.s. branch intensity  $\sim 1.0(5) \%$ )
- In reach for ( $^{18}\text{O}, ^{16}\text{O}$ ) 2-n transfer
- IFIN-HH tandem + ROSPHERE + SORCERER



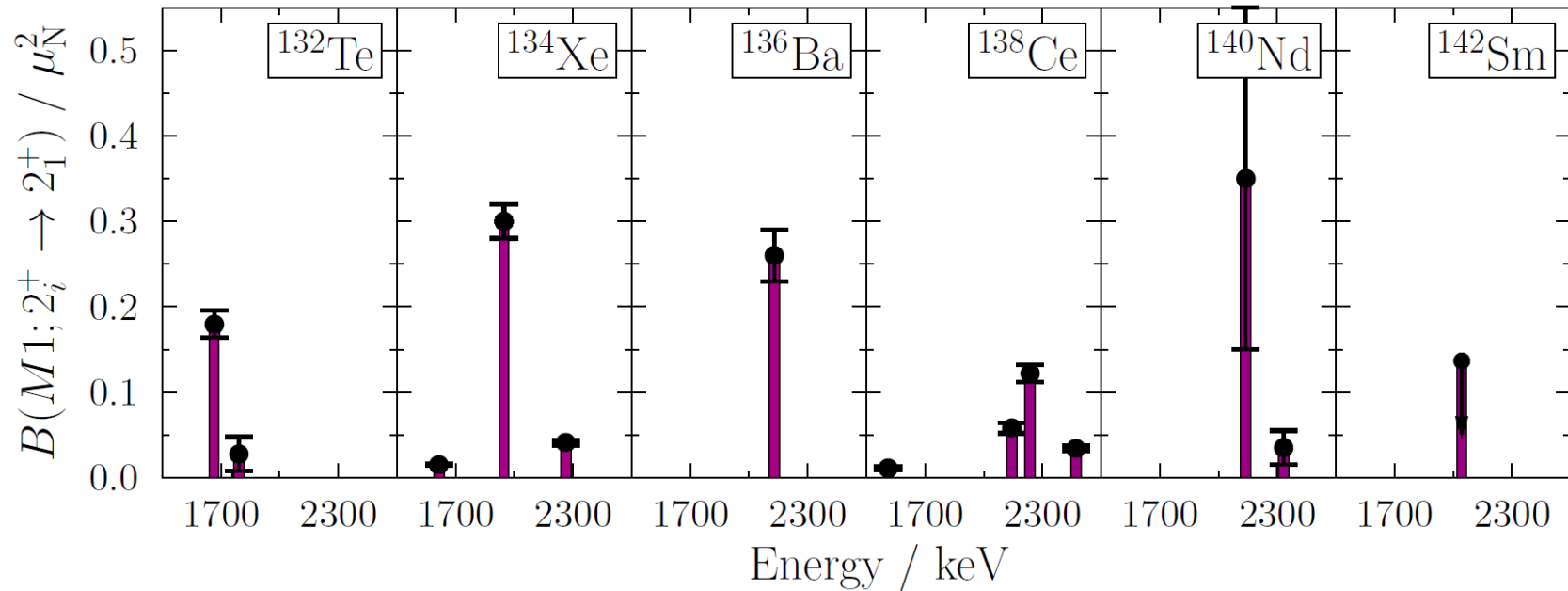
T. Stetz/H. Mayr, PhD students, TU Darmstadt  
submitted to Phys. Rev. C

**Result lifetime:**  
 **$(2^+_{ms,1}) = 0.92(7) \text{ ps}$**

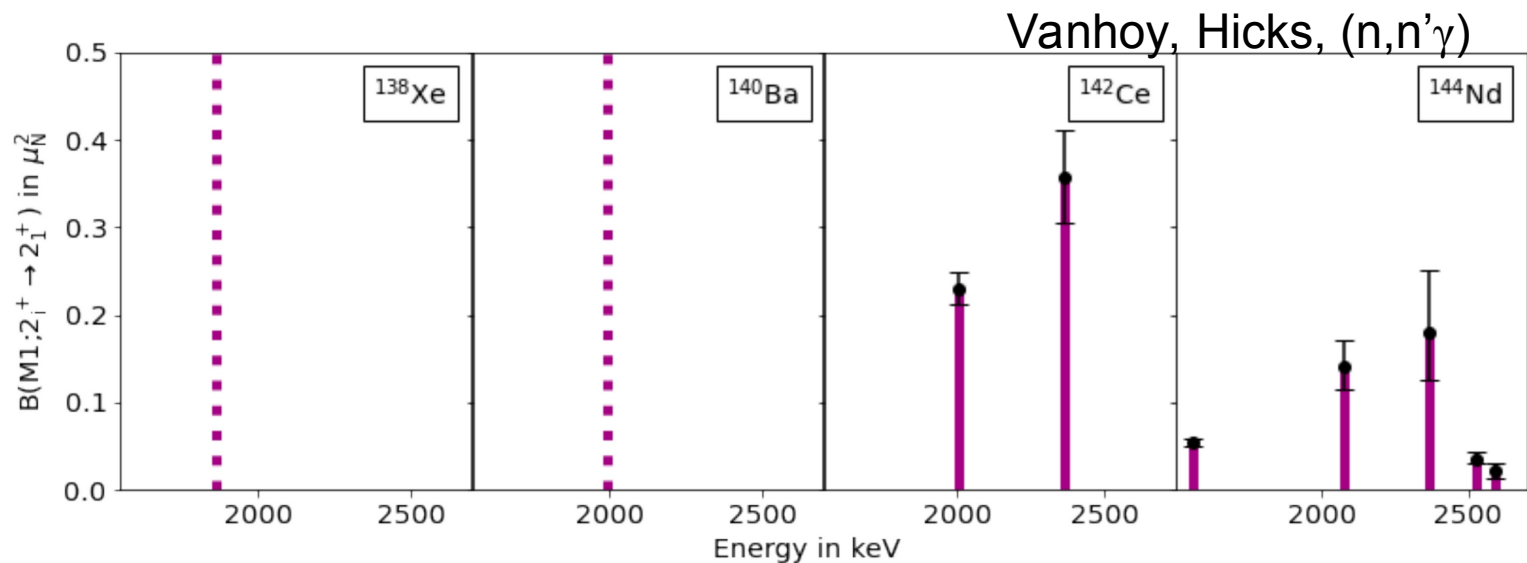
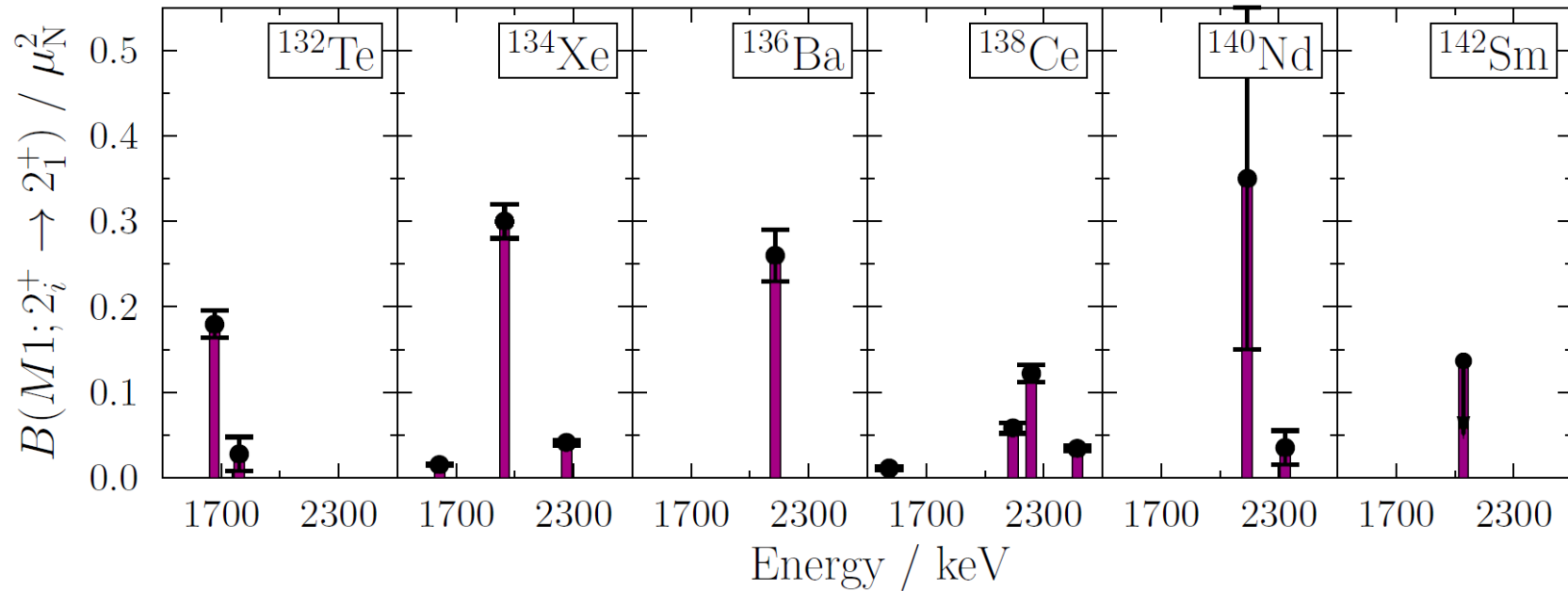
# $^{132}\text{Te}$ Wave Function Analysis



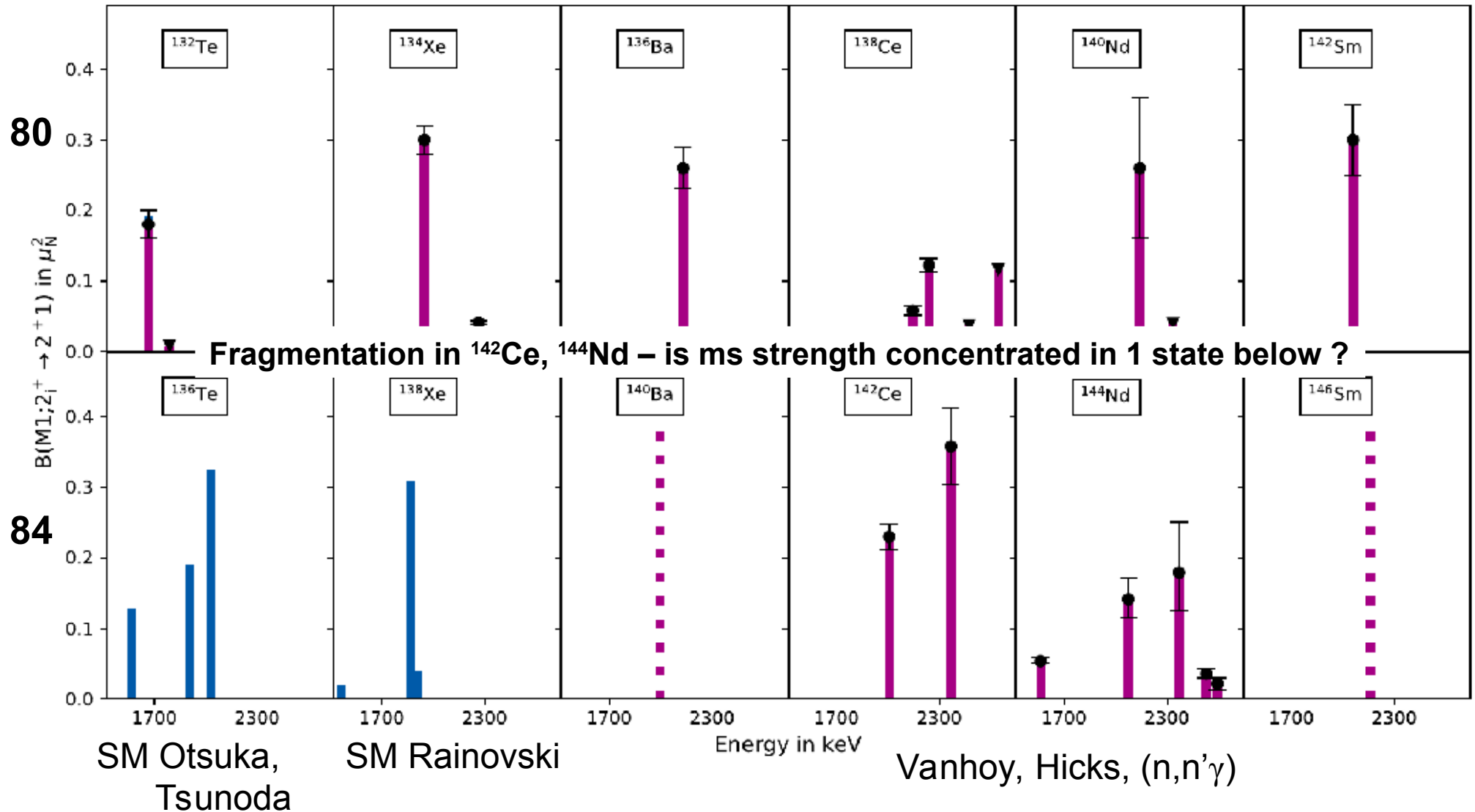
# M1 vs E2 strengths at N = 80



# M1 strengths N = 80 vs N = 84

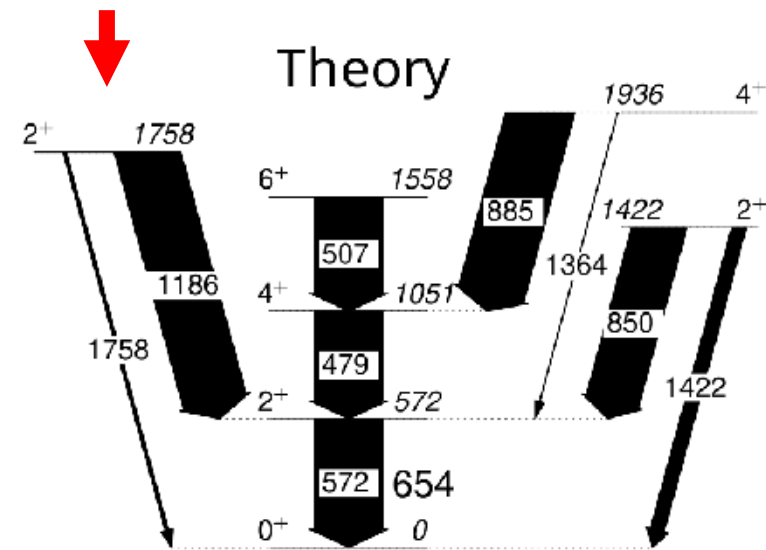
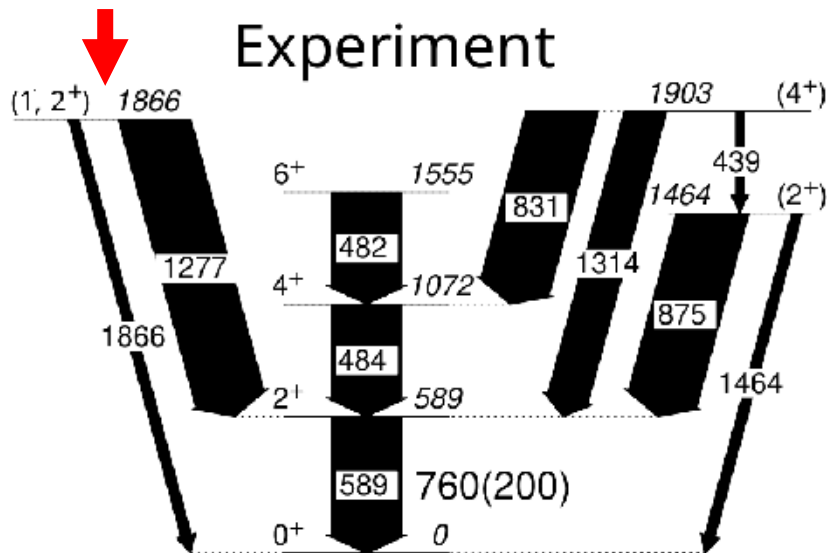


# M1 strengths N = 80 vs N = 84



# Why $^{138}\text{Xe}$ ?

- Mid-shell ( $\pi g_{7/2}$ ) between  $^{132}\text{Sn}$  and  $^{142}\text{Ce}$ 
  - This is where the  $2_{\text{ms}}^+$  state should be “stabilized” (= good F-spin)
  - If so: expect concentration in one state
- First shell model calculation with NuShellX (jj56pnb)
  - $^{132}\text{Sn}$  core, N3LO+Coulomb
  - $e_v = 0.5$ ,  $e_\pi = 1.5$ ,  $g_{lv} = -0.065$ ,  $g_{l\pi} = 1.107$ ,  $g_{sv} = -2.083$ ,  $g_{s\pi} = 3.234$
  - **$B(M1; 2_3^+ \rightarrow 2_1^+) = 0.31 \mu_N^2$**



# Planned experiment



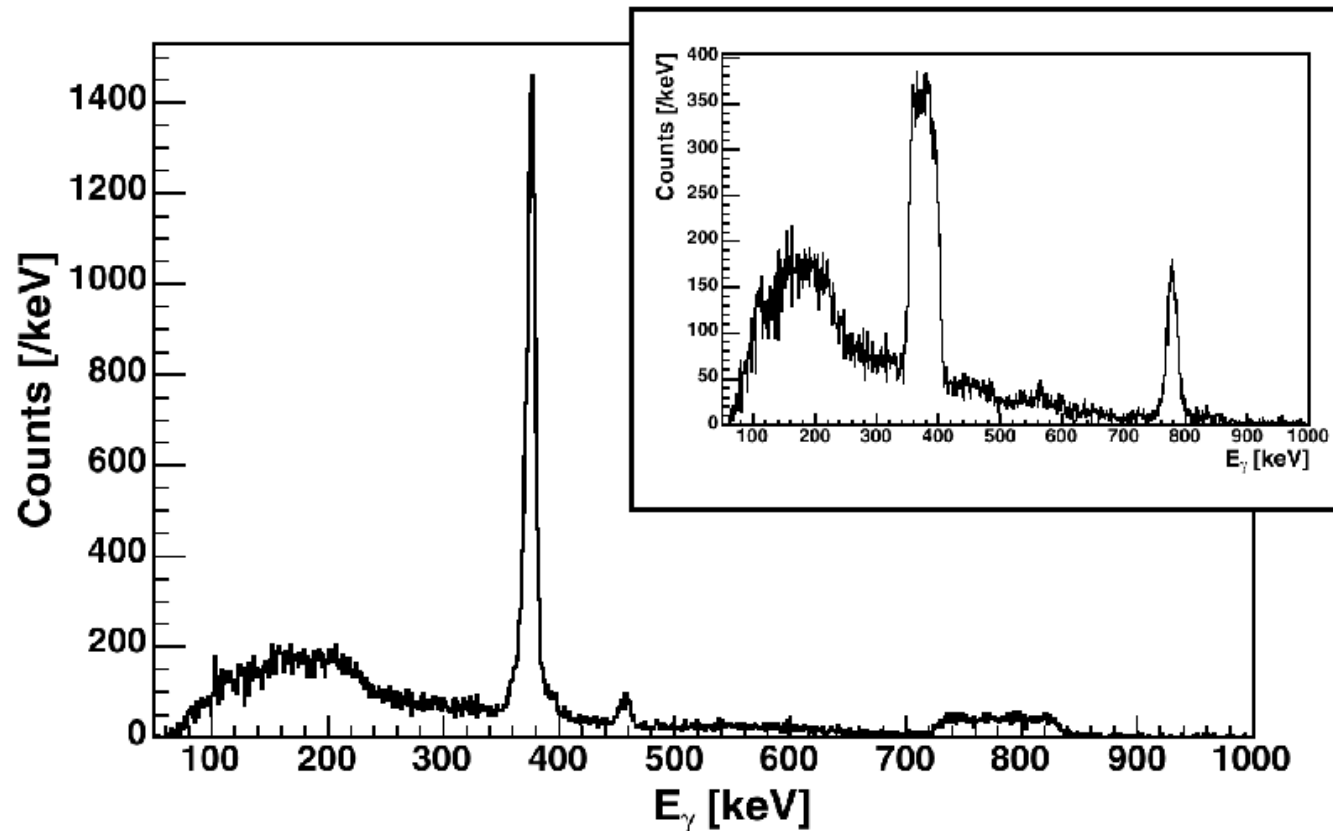
- Coulomb excitation of  $^{138}\text{Xe}$ 
  - Analog to previous work at ISOLDE
  - Optimum conditions at HIE-ISOLDE
- Determine CouEx yields –  $2_{\text{ms}}^+$  will stand out
  - Relative to target excitation
  - $^{206}\text{Pb}$ :  $B(\text{E}2; 2_1^+ \rightarrow 0_1^+) = 0.0204(7)$  @ 803 keV
  - If we see a ms-state, dominating M1 for the  $2^+ \rightarrow 2_1^+$  transition will be implied (unreasonably strong E2 ruled out)
- Nevertheless, multipole-mixing ratio desirable to fix M1/E2:
  - determine from angular correlations here, or follow up with another experiment like in other cases before (Sm, Nd)
- 15 shifts requested
- Beams are developed and available (cold plasma source, EBIS  $\rightarrow$  clean)
  - Been done with REX-ISOLDE, lower energies, lower-Z target  $\rightarrow 2_1^+$  only  
Th. Kröll, EPJ Sp. T. **150**, 127 (2007)
- Use standard setup of MINIBALL plus DSSD

# REX-ISOLDE Spectrum



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$^{140}\text{Xe}$  @ 2.84 MeV/u on  $^{96}\text{Mo}$



$^{138}\text{Xe}$ :  $B(E2; 2_1^+ \rightarrow 0_1^+) = 0.38(10) e^2b^2$   
(26%)

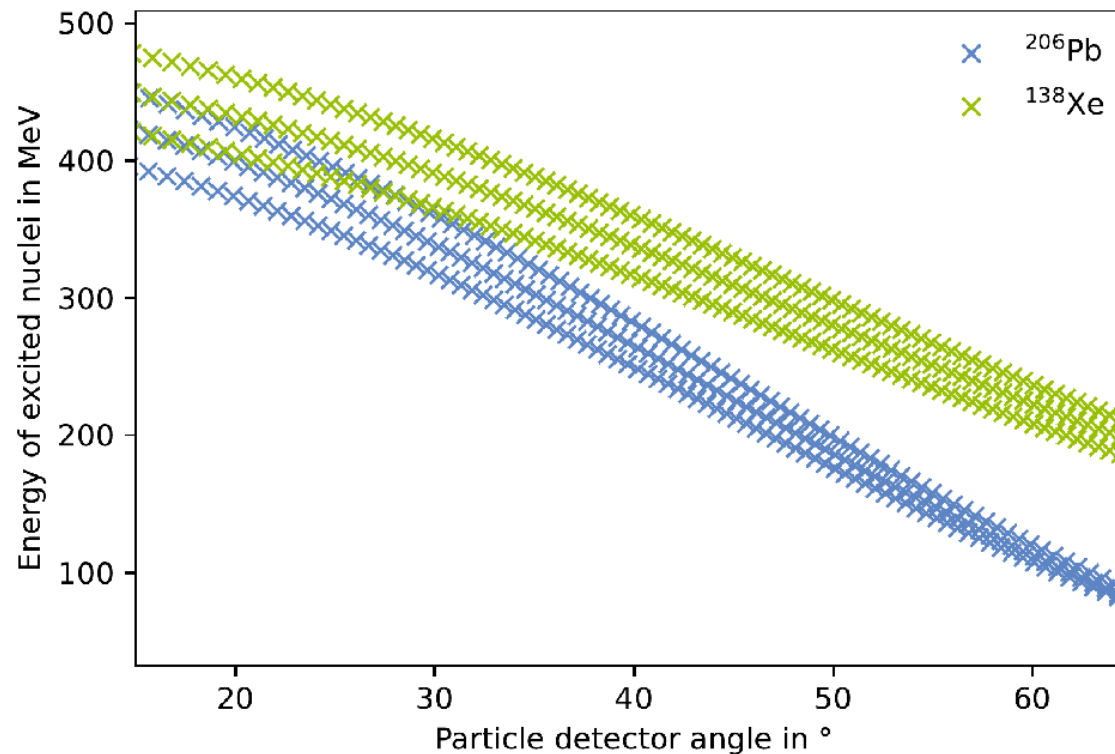
Th. Kröll, EPJ Sp. T. **150**, 127 (2007)



# Planned experiment



- HIE-ISOLDE: beams of 3.6 MeV/u
- Impinging on 2 mg/cm<sup>2</sup> <sup>206</sup>Pb target
  - well-known 2<sub>1</sub><sup>+</sup> target excitation for relative measurement
- DSSD ~ 25 mm behind target, 20 – 60 degrees angular coverage



# Planned experiment

- Determine e.-m. Matrix elements through GOSIA fit

- Yields in  $2^+$  states:

- Unknown Matrix elements calculated with NuShellX (jj56pnb)
- Cross sections obtained with CLX
- $1.5 \cdot 10^8$  pps after primary target
- 2% transmission efficiency  
=>  $3 \cdot 10^6$  pps @Miniball

$\epsilon_\gamma$  : 5 %

$I_{\text{beam}}$  :  $3 \cdot 10^6$  pps @Miniball

**Goal:**

**Rel. unc.  $\Delta A/A \sim 5$  %**

Excited state	Energy (keV)	$\sigma$ (mb)	Branching ratio to $2_1^+$	Yield/day	Total yield in $4\frac{2}{3}$ days	Statistical uncertainty
$2_1^+$	588	$2.9 \cdot 10^3$	—	$2.2 \cdot 10^5$	$1.0 \cdot 10^6$	0.1%
$2_2^+$	1463	8.0	93%	563	2630	2.0%
$2_3^+$	1866	1.3	87%	85	400	5.0%

# Request

14 shifts data taking + 1 shift beam setup/tuning

Total: 15 shifts

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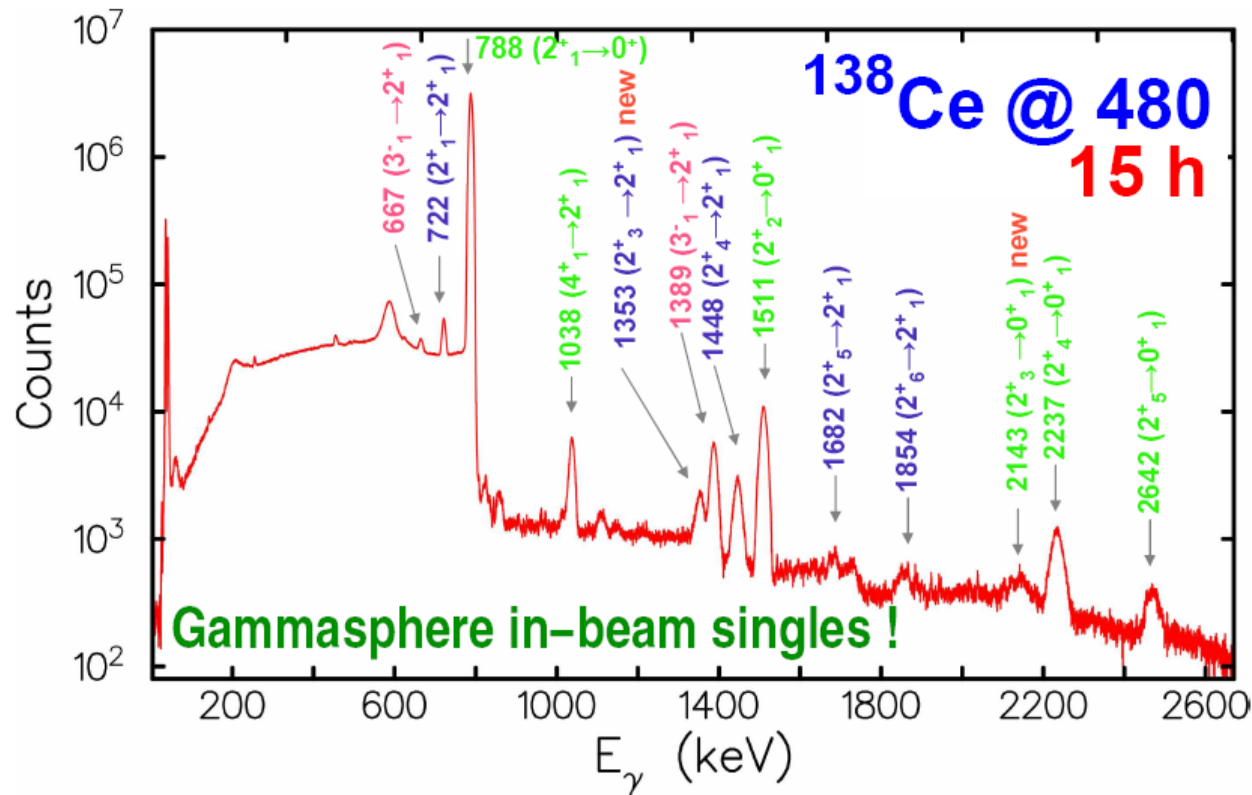
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$^{206}\text{Pb } 2_1^+$	803	$\sim 200$			$\sim 10^5$	$\sim 0.3\%$

# Example of Data: $^{138}\text{Ce}$ CoulEx on $^{12}\text{C}$ @ 480 MeV (ANL)

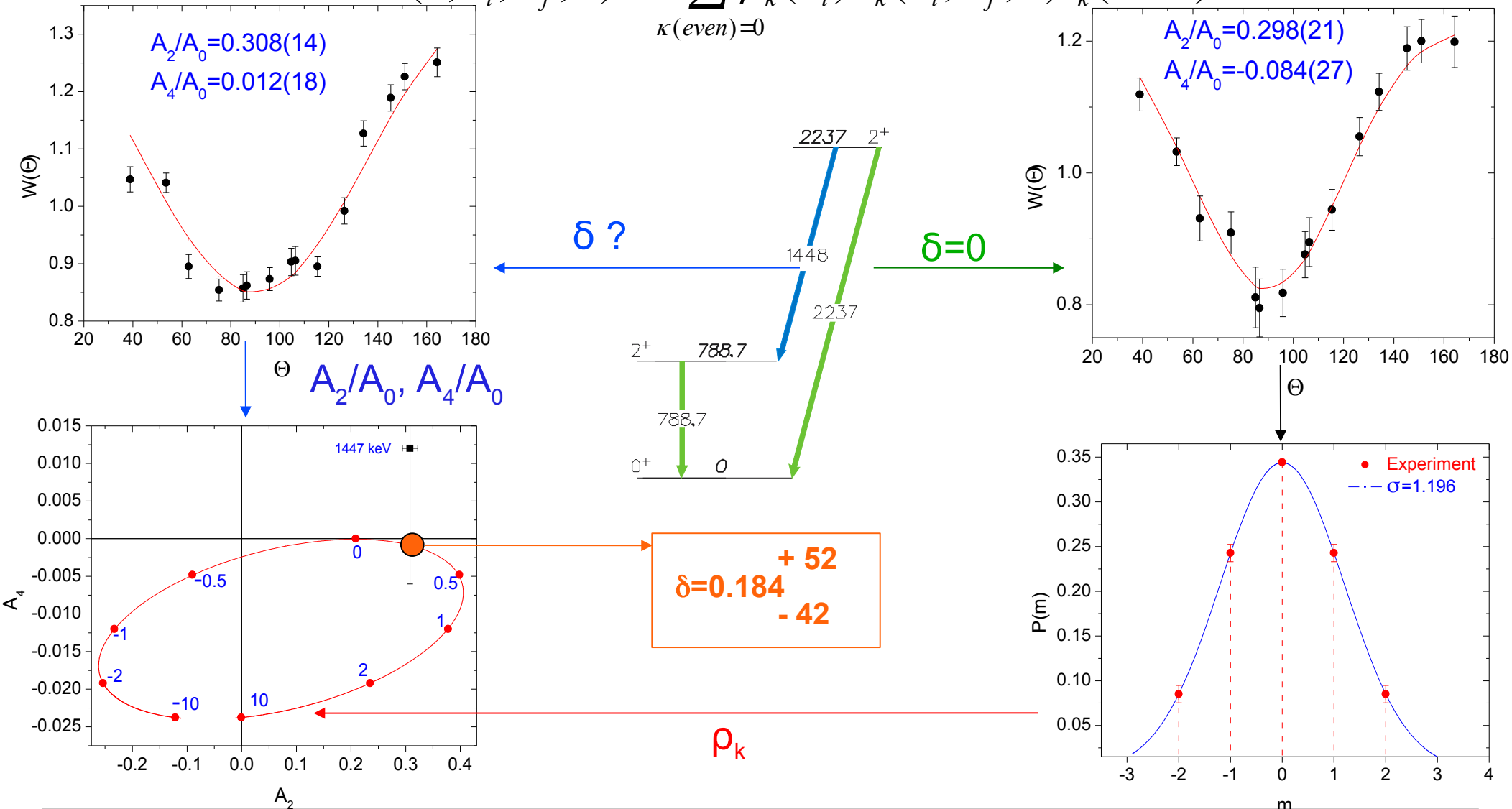


G.Rainovski, N. Pietralla et al., *Phys. Rev. Lett.* **96** 122501 (2006).

# Example of Data: $^{138}\text{Ce}$ CoulEx on $^{12}\text{C}$ @ 480 MeV (ANL)



$$W(\theta, J_i, J_f, \delta) = \sum_{\kappa(\text{even})=0}^2 \rho_{\kappa}(J_i) A_{\kappa}(J_i, J_f, \delta) P_{\kappa}(\cos \theta)$$



# M1 vs E2 strengths at N = 80

