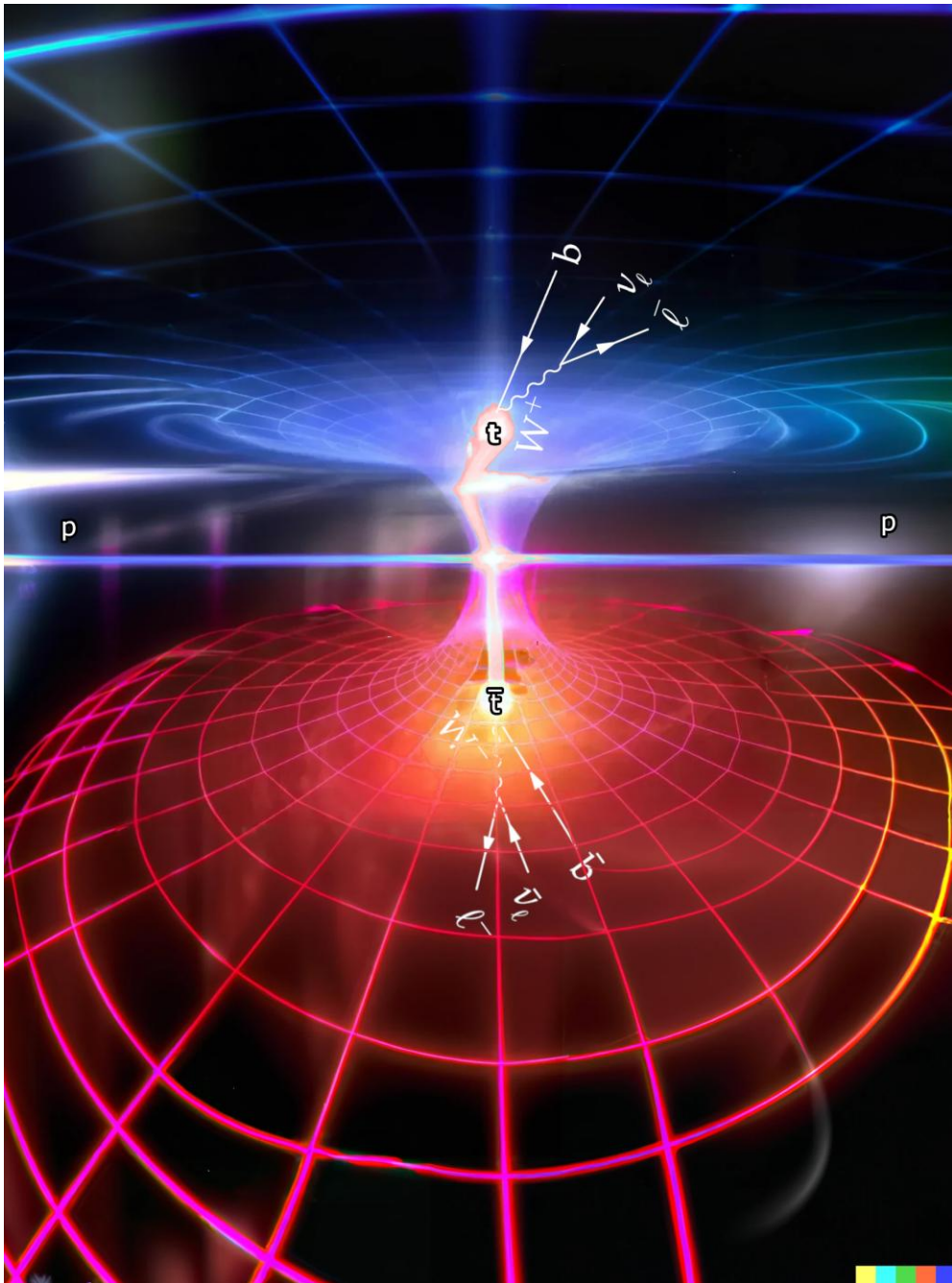


Observation of entangled top quarks with the CMS Detector

AJ Wildridge

LPC Physics Forum

Feb. 20, 2025



Entanglement in QM

- Classical physics is void of phenomenon featuring **entanglement**

$$|\psi\rangle = |a\rangle_A \otimes |b\rangle_B$$

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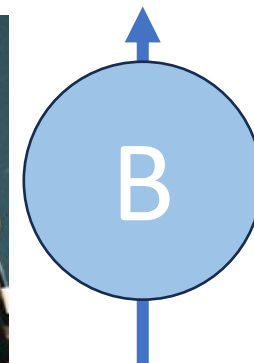
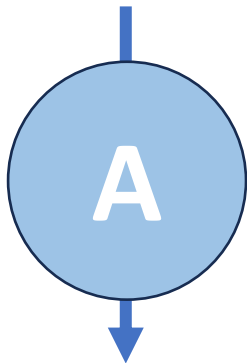
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- Simplest example of entanglement:
 - 2 two-level systems (A & B) in a superposition of anticorrelated states

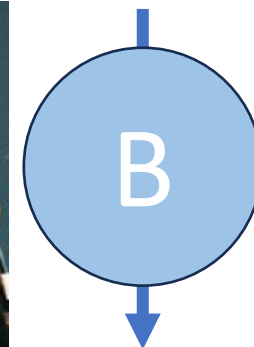
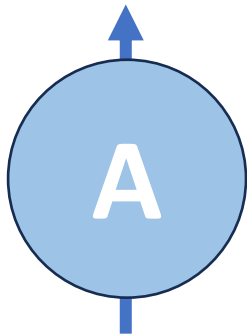


Entanglement in QM

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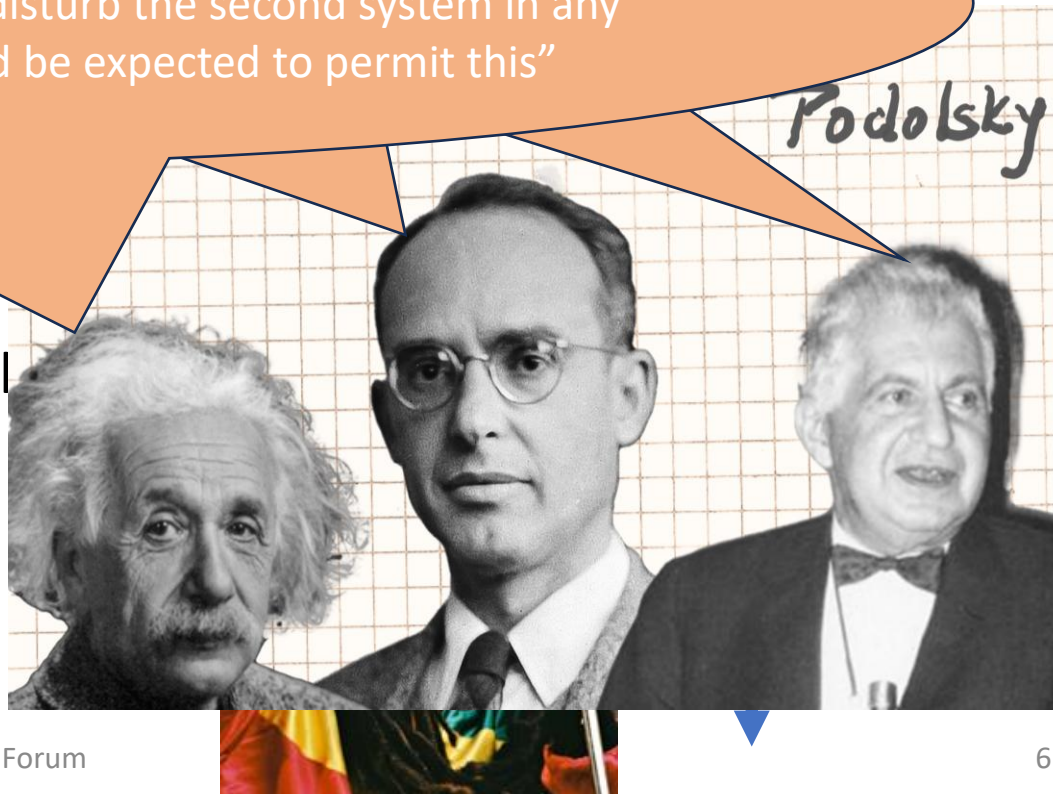
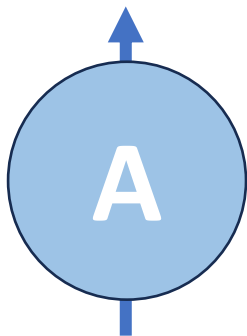
Can Quantum-Mechanical Description of Physical Reality Be Considered Complete?

A. EINSTEIN, B. PODOLSKY AND N. ROSEN, *Institute for Advanced Study, Princeton, New Jersey*

(Received March 25, 1935)

“This makes the reality of P and Q depend upon the process of measurement carried out on the first system, which does not disturb the second system in any way. No reasonable definition of reality could be expected to permit this”

- But classical physics can be ...
- Simplest example of entanglement ...
- 2 two-level systems (A & B) in a superposition ...



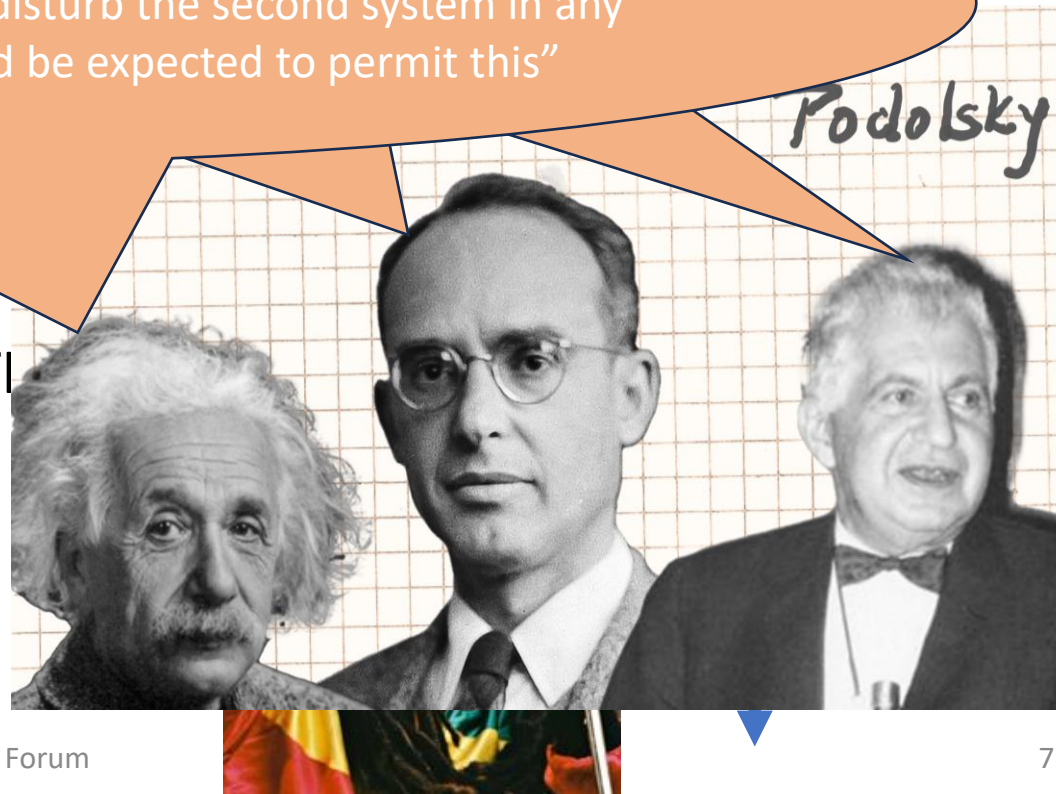
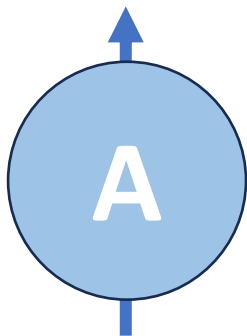
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- Simplest example of entanglement
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John Stewart Bell



John Stewart Bell, CERN, 1973

Physical Reality Be Considered Complete?

for Advanced Study, P

(1935)

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ON THE EINSTEIN PODOLSKY ROSEN PARADOX*

J. S. BELL†

Department of Physics, University of Wisconsin, Madison, Wisconsin

(Received 4 November 1964)

John



John Stewart

Illustrations: Niklas Elmehed

THE NOBEL PRIZE IN PHYSICS 2022



Alain Aspect

John F. Clauser

Anton Zeilinger

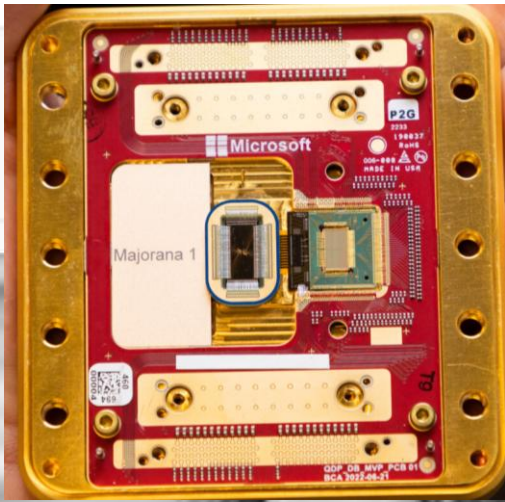
“for experiments with entangled photons, establishing the violation of Bell inequalities and pioneering quantum information science”

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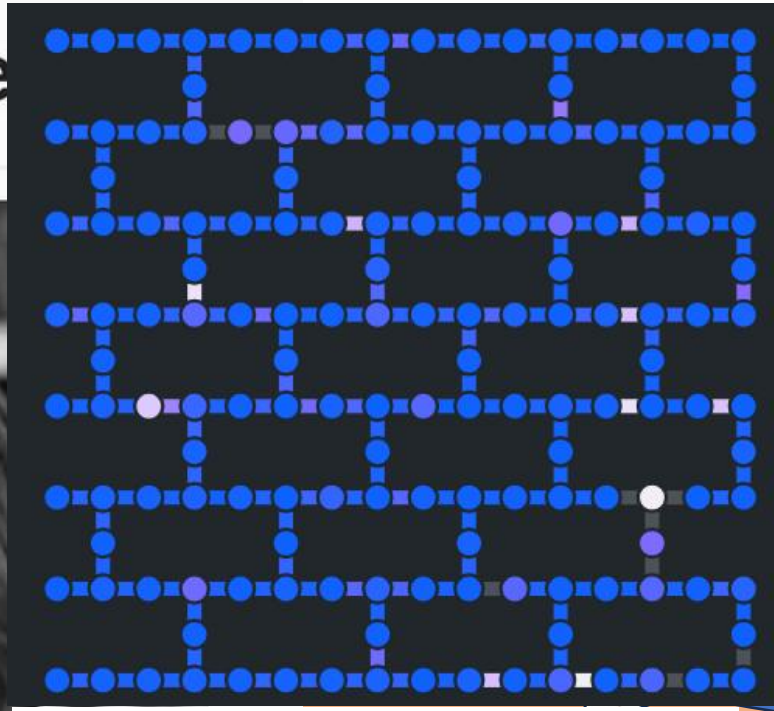


PARADOX*

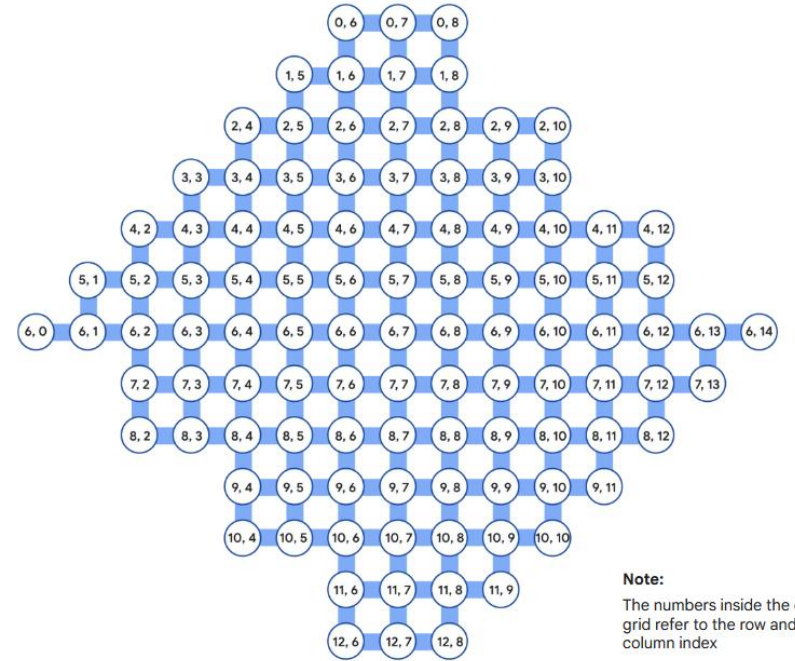
Madison, Wisconsin



Microsoft Majorana 1 QC

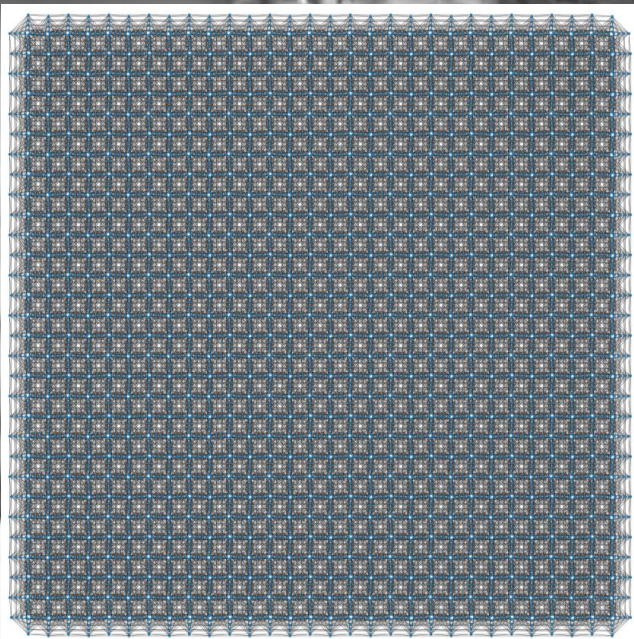


IBM Marrakesh QC

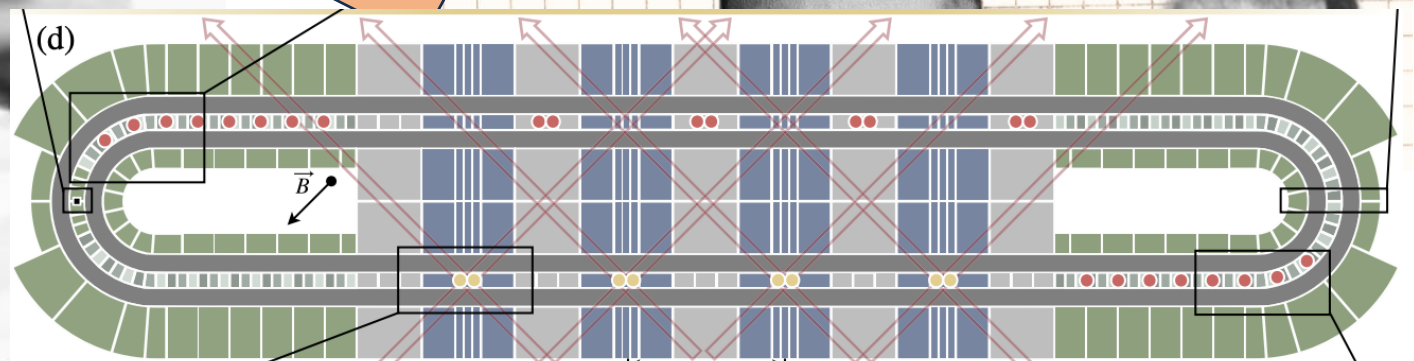


Google Willow QC

Note:
The numbers inside the qubit grid refer to the row and column index



D-Wave Advantage 2 QA



Quantinuum H2 QC

in, Madison, Wisconsin



SUISSE
FRANCE

CMS

LHCb

ATLAS

CERN Meyrin

CERN Provençassin

SPS 7 km

ALICE

LHC 27 km



SUISSE
FRANCE

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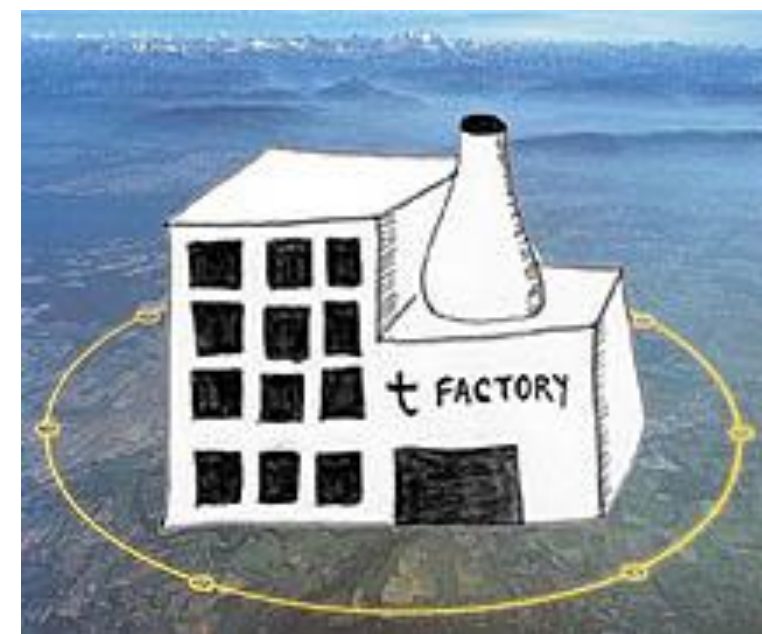
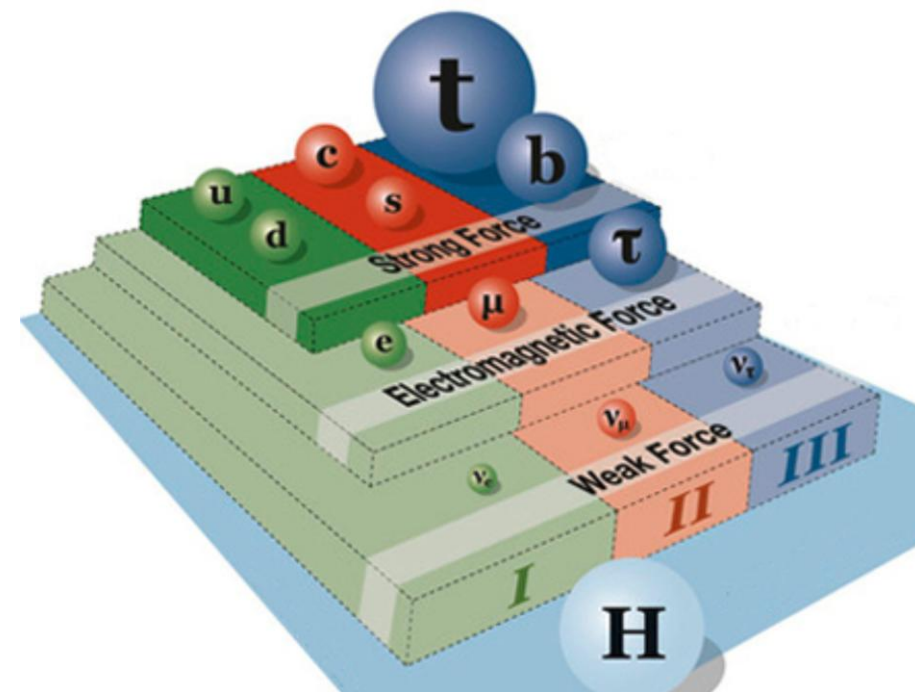
Top Quark Physics

- Top quark is the heaviest fundamental particle discovered thus far: $m_t = 172.52 \pm 0.33$ GeV

- Unique: $\frac{1}{m_t} < \frac{1}{\Gamma_t} < \frac{1}{\Lambda_{\text{QCD}}} < \frac{m_t}{\Lambda^2}$ [\[arXiv:2402.08713\]](https://arxiv.org/abs/2402.08713)

$\underbrace{\frac{1}{m_t}}$	$<$	$\underbrace{\frac{1}{\Gamma_t}}$	$<$	$\underbrace{\frac{1}{\Lambda_{\text{QCD}}}}$	$<$	$\underbrace{\frac{m_t}{\Lambda^2}}$
production 10^{-27} s		lifetime 10^{-25} s		hadronization 10^{-24} s		spin-flip 10^{-21} s

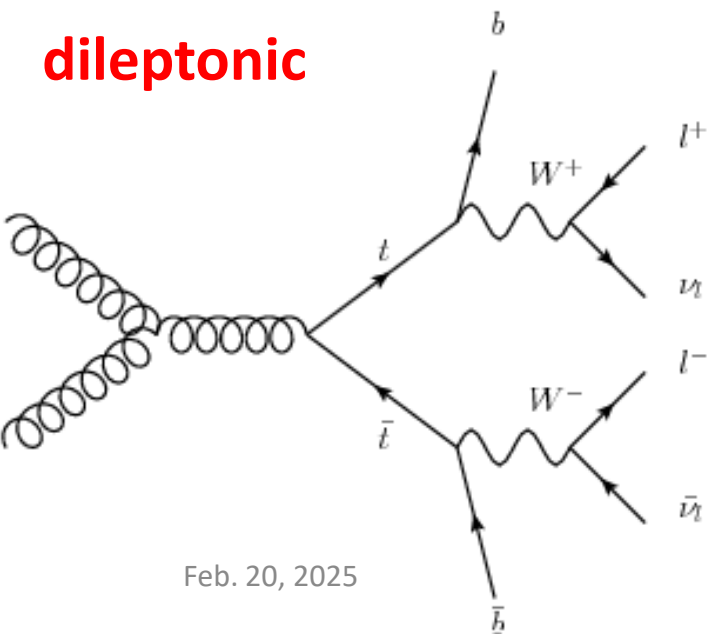
- LHC is a top quark factory (100m+ thus far)



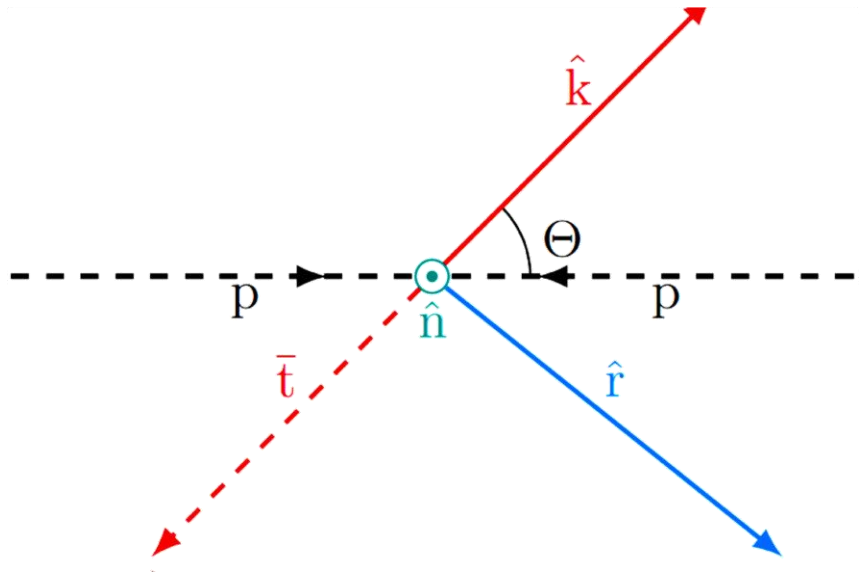
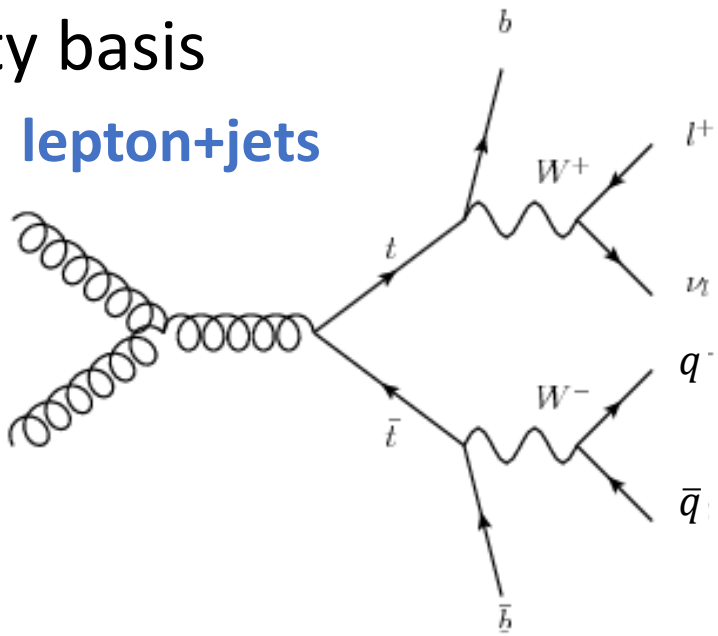
Top Quark Spin Correlations

- Spin correlations are dependent on **production mode** (gg vs. $q\bar{q}$) and higher orbital momenta \rightarrow function of e.g. $\Theta_t, m(t\bar{t})$
- Top quark spin cannot be measured directly
- Fully preserved in charged leptonic and down-type quark decays of W boson
- Measured in the helicity basis

dileptonic



lepton+jets



Measurement of Top Quark Spin Density Matrix in dilepton

- Spin density matrix fully captured by a four-fold angular distribution

$$\frac{1}{\sigma} \frac{d^4\sigma}{d\Omega d\bar{\Omega}} = \frac{1}{4\pi^2} (1 + \kappa \mathbf{B} \cdot \Omega + \bar{\kappa} \bar{\mathbf{B}} \cdot \bar{\Omega} - \kappa \bar{\kappa} \Omega \cdot (\mathbb{C} \bar{\Omega}))$$

- Spin Polarization $\mathbf{B}/\bar{\mathbf{B}} = \begin{pmatrix} B_k \\ B_r \\ B_n \end{pmatrix}$ Spin Correlation $\mathbb{C} = \begin{pmatrix} C_{kk} & C_{kr} & C_{kn} \\ C_{rk} & C_{rr} & C_{rn} \\ C_{nk} & C_{nr} & C_{nn} \end{pmatrix}$
- Can integrate above four-fold angular distribution to get 1D distributions for each spin coefficient

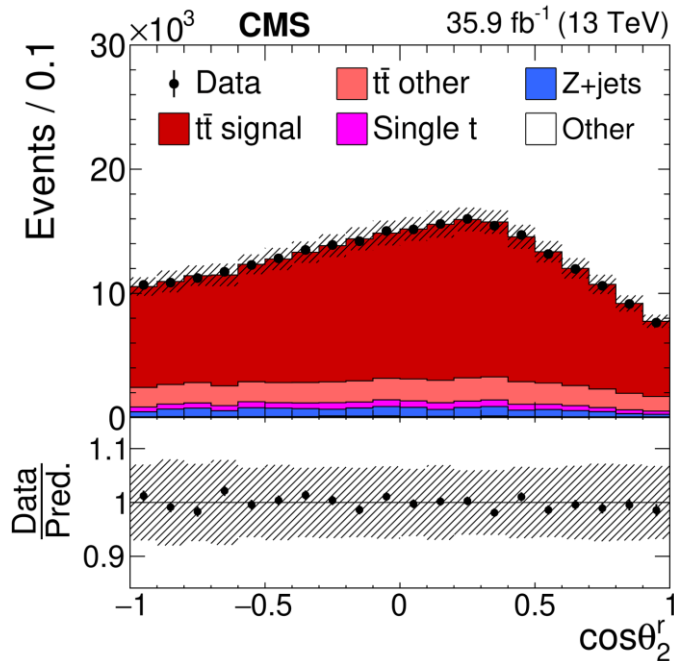
$$\int \frac{d^4\sigma}{d\Omega d\bar{\Omega}} \rightarrow \frac{1}{\sigma} \frac{d\sigma}{dx} = \frac{1}{2} (1 + [\text{Coef.}]x) f(x)$$

Measurement of Top Quark Spin Density Matrix in dilepton

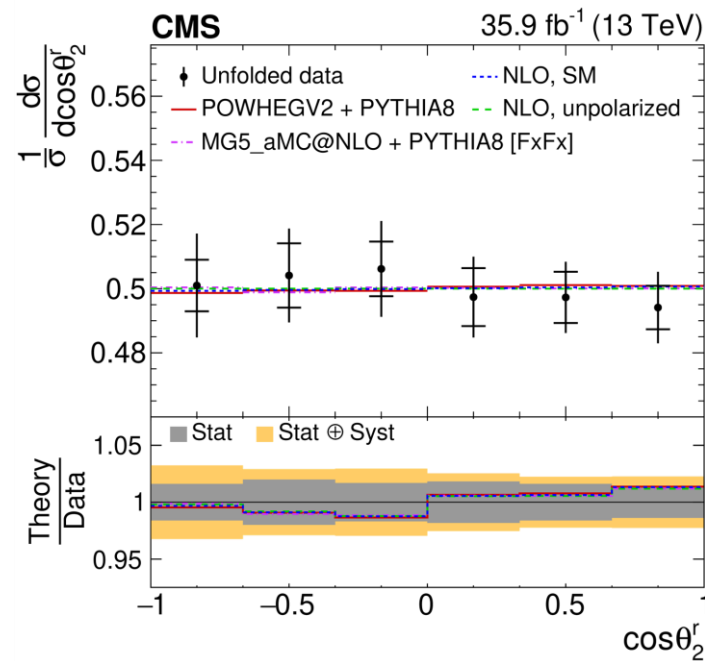
- SM predicts zero polarization for $t\bar{t}$ ($< 10^{-2}$) – QCD is CP even
 - Zero polarization \rightarrow zero slope at parton level

$$\frac{1}{\sigma} \frac{d\sigma}{d\cos\theta_{1/2}^i} = \frac{1}{2} (1 + B_i \cos\theta_{1/2}^i)$$

Reconstruction Level

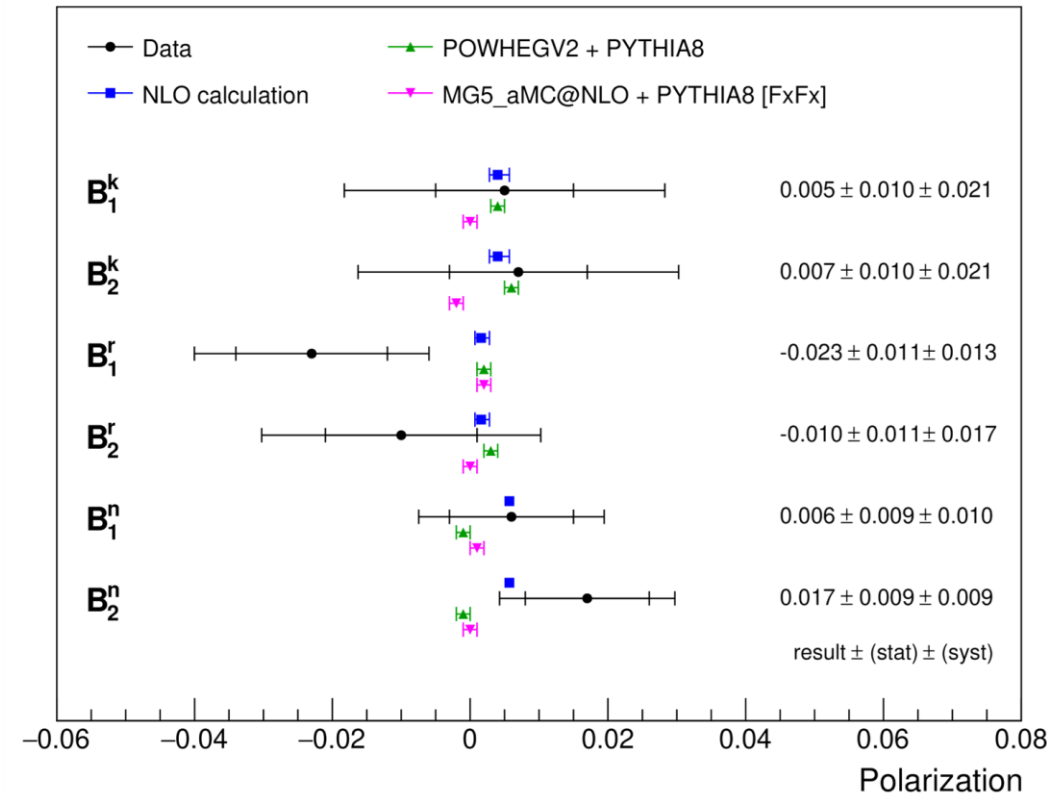


Parton level



CMS

35.9 fb⁻¹ (13 TeV)

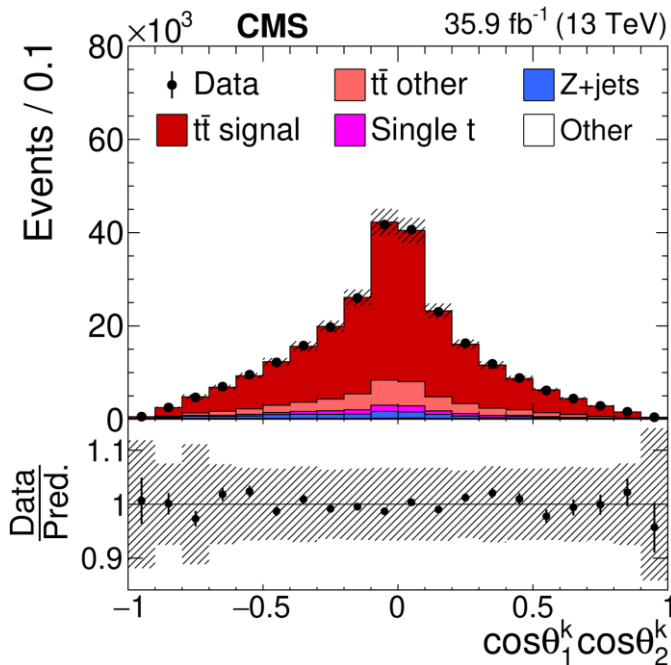


Measurement of Top Quark Spin Density Matrix in dilepton

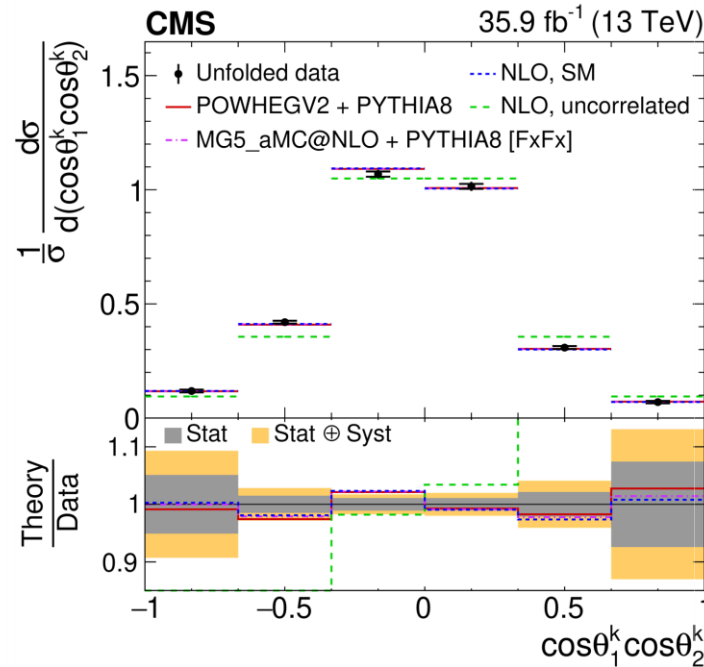
- SM predicts non-zero **correlation** for $t\bar{t}$
 - Non-zero **correlation** \rightarrow asymmetry in $\cos\theta_1^i \cos\theta_2^j$ distribution at parton level

$$\frac{1}{\sigma} \frac{d\sigma}{d\cos\theta_1^i \cos\theta_2^j} = \frac{1}{2} \left(1 + C_{ij} \cos\theta_1^i \cos\theta_2^j \right)$$

Reconstruction Level

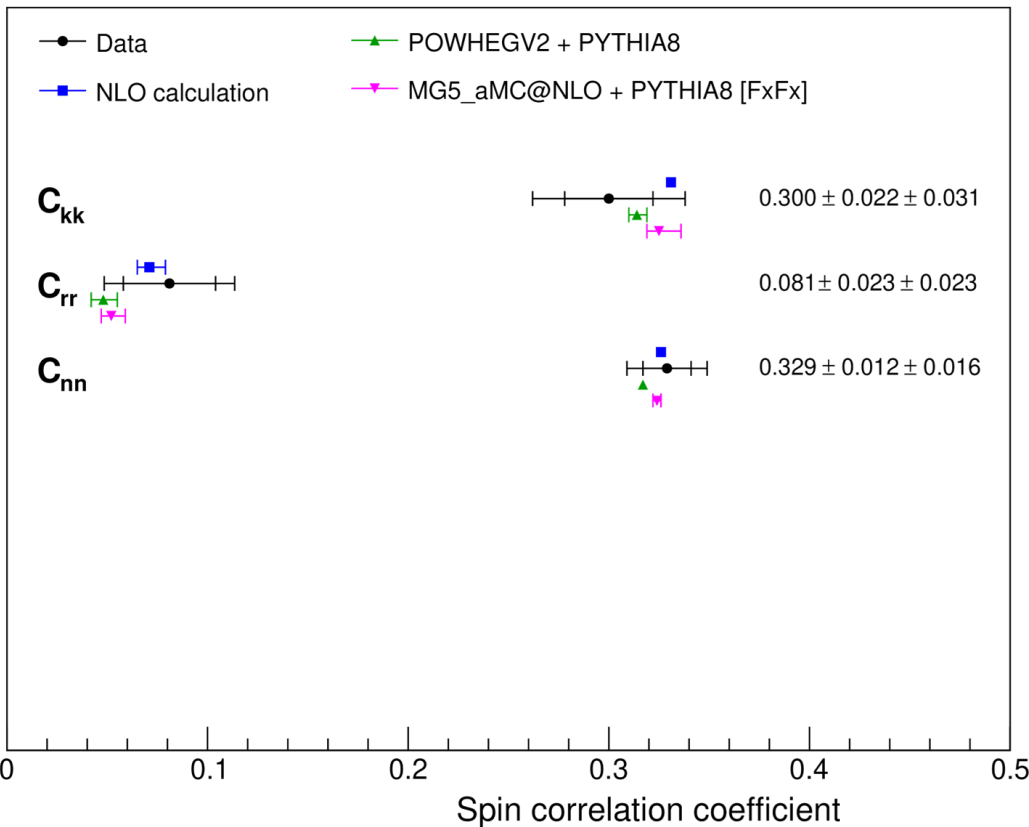


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How to probe **entanglement**

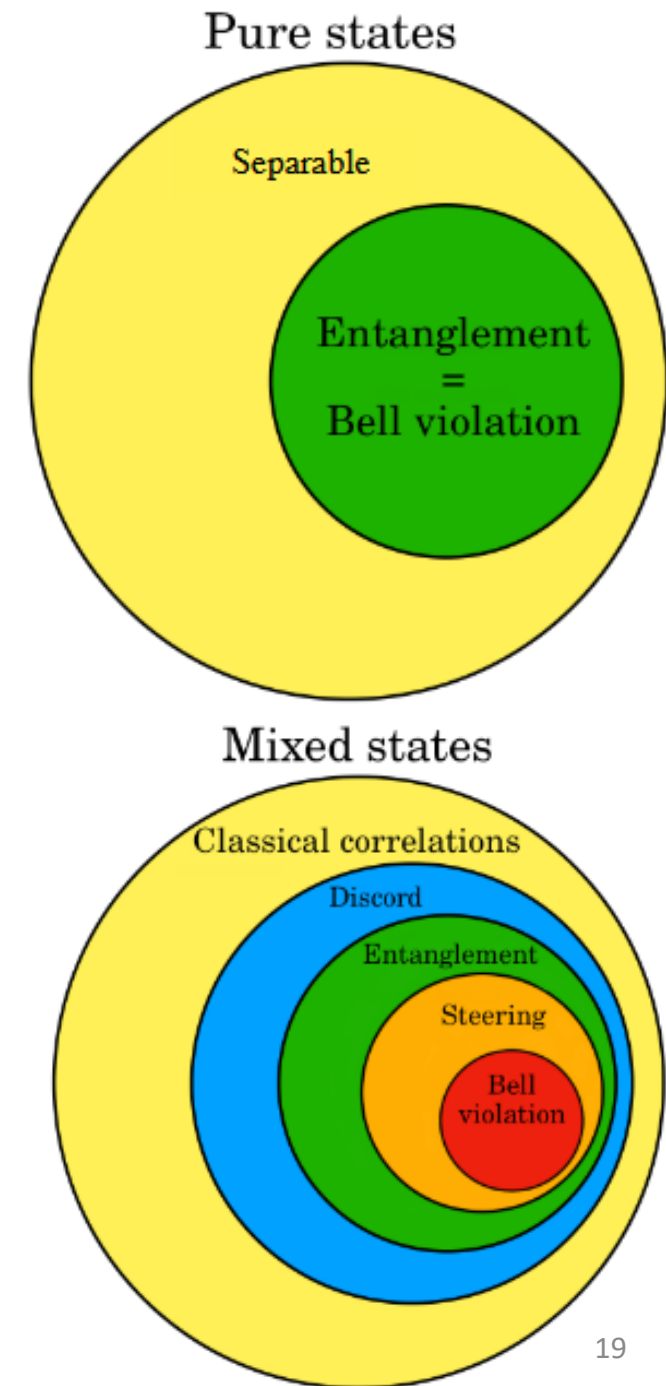
- What does it mean to be **not entangled**? **Separable!**

$$|\psi\rangle = |a\rangle_A \otimes |b\rangle_B$$

- For pure states this is easy \rightarrow measure **entanglement entropy**
- At the LHC top quarks are produced in a mixed state and thus can be represented as a density operator

$$\rho = \frac{1}{4} \left[I_4 + \sum_i (B_i^+ \sigma^i \otimes I_2 + B_i^- I_2 \otimes \sigma^i) + \sum_{i,j} C_{ij} \sigma^i \otimes \sigma^j \right]$$

- Need to determine an entanglement witness, Δ
- Hard to show density operator is separable but you can “easily” show it is non-separable \rightarrow **entangled!**



How to probe **entanglement**: Peres-Horodecki Criterion

- Perform operation (anti-unitary) on subspace (e.g. A)
- If a state is separable \rightarrow Unit trace, Hermitian, Eigenvalues ≥ 0
- Therefore, a state is **entangled** if the above conditions **don't** hold for the partial transpose of the spin density matrix, ρ
- A sufficient condition for **entanglement** using Peres-Horodecki Criterion:

$$\Delta = C_{nn} + |C_{kk} + C_{rr}| - 1 > 0 \quad [\textit{Eur. Phys. J. Plus 136, 907}]$$

At **low** $m(t\bar{t})$

$$C_{kk} > 0 \ \& \ C_{rr} > 0 \ \rightarrow \ tr[C] > 1$$

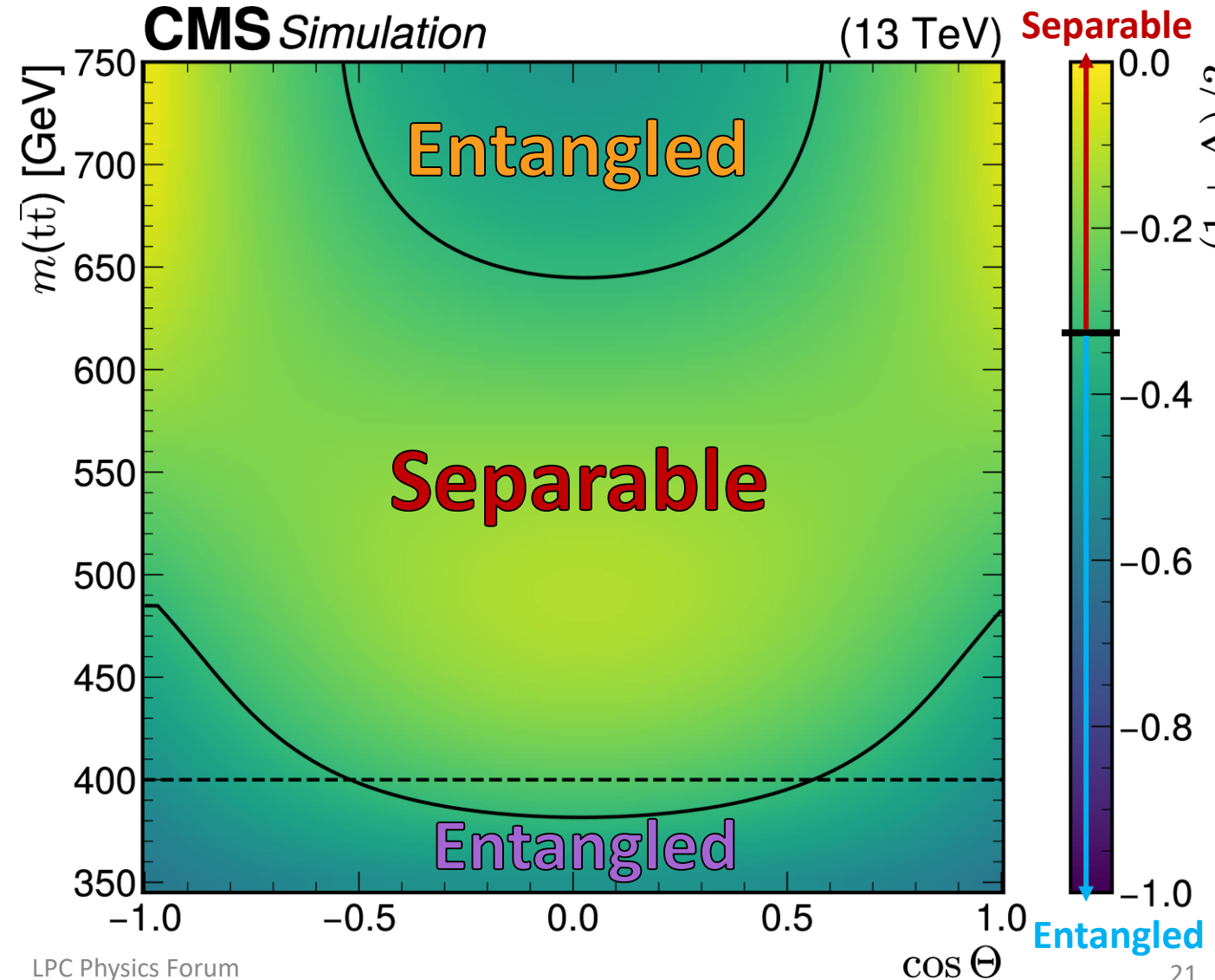
$$D = -\frac{tr[C]}{3} \quad \frac{1}{\sigma} \frac{d\sigma}{d \cos\varphi} = \frac{1}{2} (1 - D \cos\varphi)$$

$$D < -\frac{1}{3} \rightarrow \textbf{entangled!}$$

Measure D to access entanglement information!

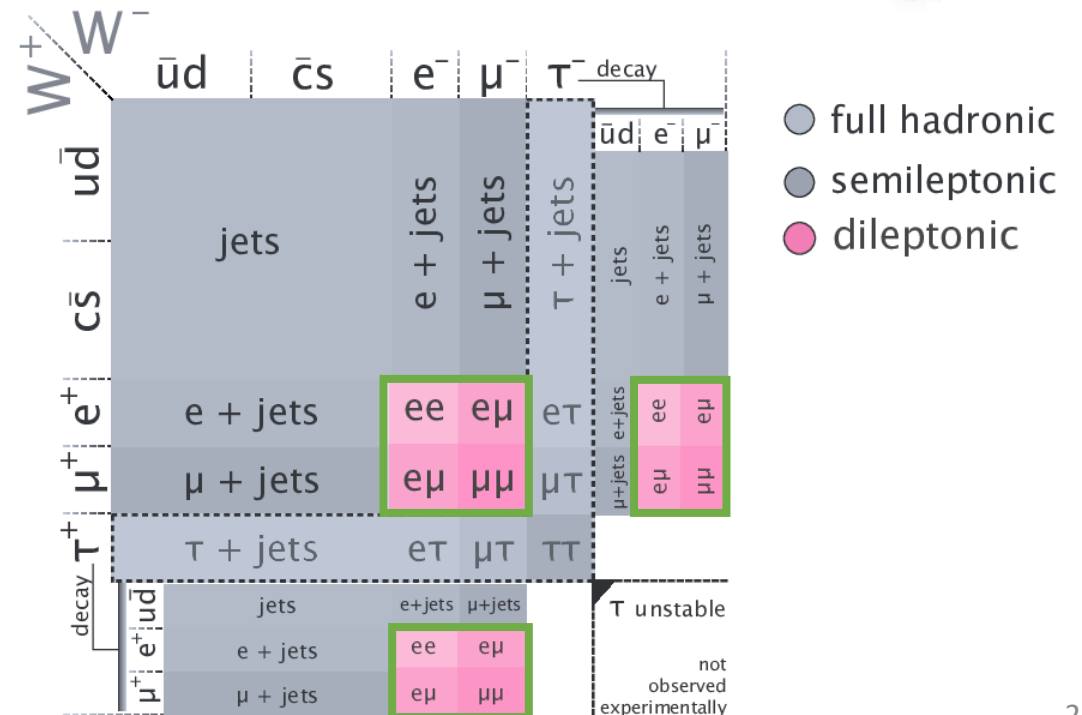
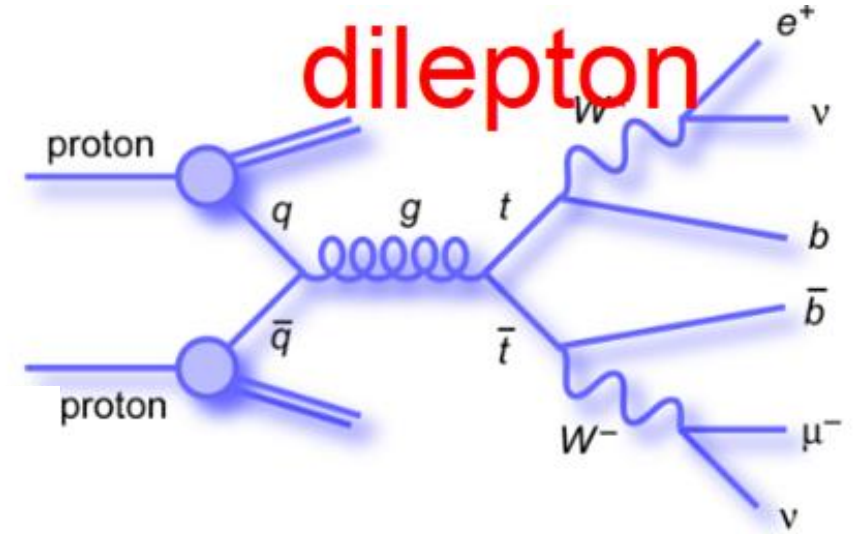
How to discover **entangled** top quarks

- CMS probed the **production threshold region** for entanglement
- Mostly **timelike (spacelike)** separated decays in **production threshold (boosted)** region



Event selection

- **Dileptonic** channel ($ee/\mu\mu/e\mu$) w/ 2016 data
- 2 oppositely charged isolated leptons (ee , $e\mu$ and $\mu\mu$)
 - Leptonic decays of taus included in signal
 - p_T & $|\eta|$ cuts applied to tight electrons & muons
 - Veto events with more than two leptons
- Low $m_{l\bar{l}}$ events rejected
- ≥ 2 anti- k_t jets ($R=0.4$)
 - p_T & $|\eta|$ cuts applied
 - Jet cleaning & iCSVv2 loose working point
- ee , $\mu\mu$ channels have additional selection criteria applied to reduce Drell-Yan background
- Reject events failing kinematic reconstruction constraints



Dileptonic Top Quark Reconstruction

- Use algebraic method to solve for neutrino 3-vectors
- Results in quartic equation for neutrino momenta

$$0 = \sum_{i=0}^4 c_i(m_t, p_{l^+}, p_{l^-}, p_b, p_{\bar{b}}) p_x(\bar{\nu})^i$$

- Pick solution that has lowest $m(t\bar{t})$

$$m_t^2 = (E_{l^+} + E_{\nu} + E_b)^2 - (p_{x,l^+} + p_{x,\nu} + p_{x,b})^2 - (p_{y,l^+} + p_{y,\nu} + p_{y,b})^2 - (p_{z,l^+} + p_{z,\nu} + p_{z,b})^2$$

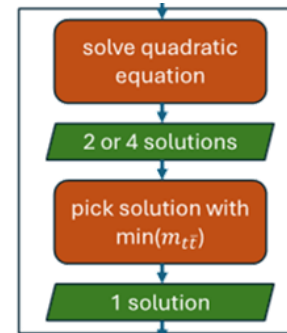
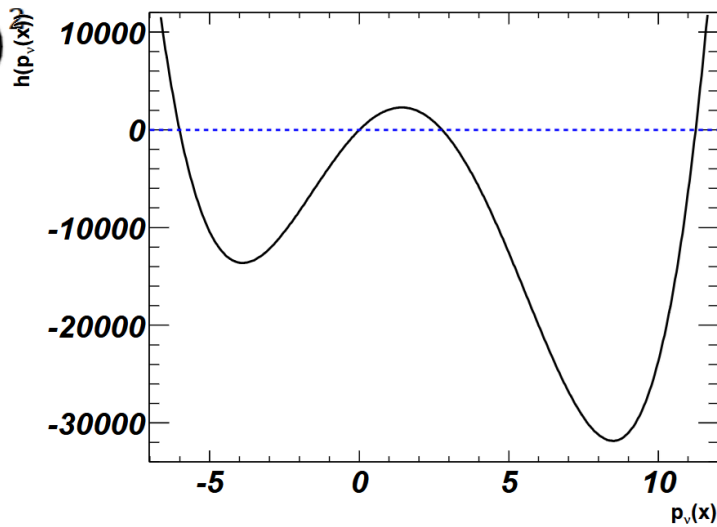
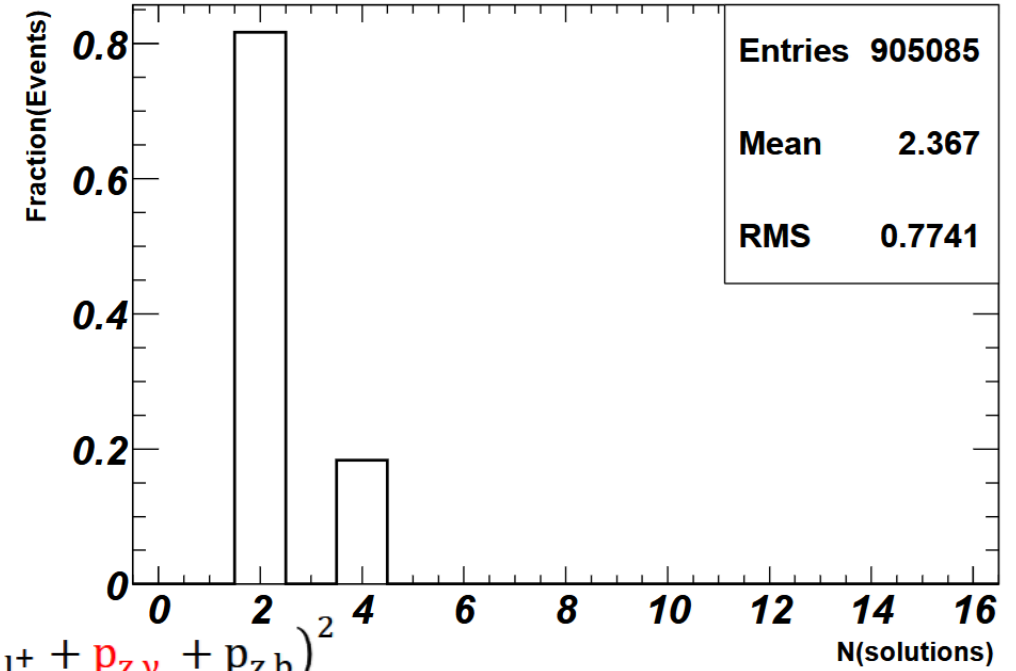
$$m_t^2 = (E_{l^-} + E_{\bar{\nu}} + E_{\bar{b}})^2 - (p_{x,l^-} + p_{x,\bar{\nu}} + p_{x,\bar{b}})^2 - (p_{y,l^-} + p_{y,\bar{\nu}} + p_{y,\bar{b}})^2 - (p_{z,l^-} + p_{z,\bar{\nu}} + p_{z,\bar{b}})^2$$

$$m_{W^+}^2 = (E_{l^+} + E_{\nu})^2 - (p_{x,l^+} + p_{x,\nu})^2 - (p_{y,l^+} + p_{y,\nu})^2 - (p_{z,l^+} + p_{z,\nu})^2$$

$$m_{W^-}^2 = (E_{l^-} + E_{\bar{\nu}})^2 - (p_{x,l^-} + p_{x,\bar{\nu}})^2 - (p_{y,l^-} + p_{y,\bar{\nu}})^2 - (p_{z,l^-} + p_{z,\bar{\nu}})^2$$

$$E_x^{MET} = p_{x,\nu} + p_{x,\bar{\nu}}$$

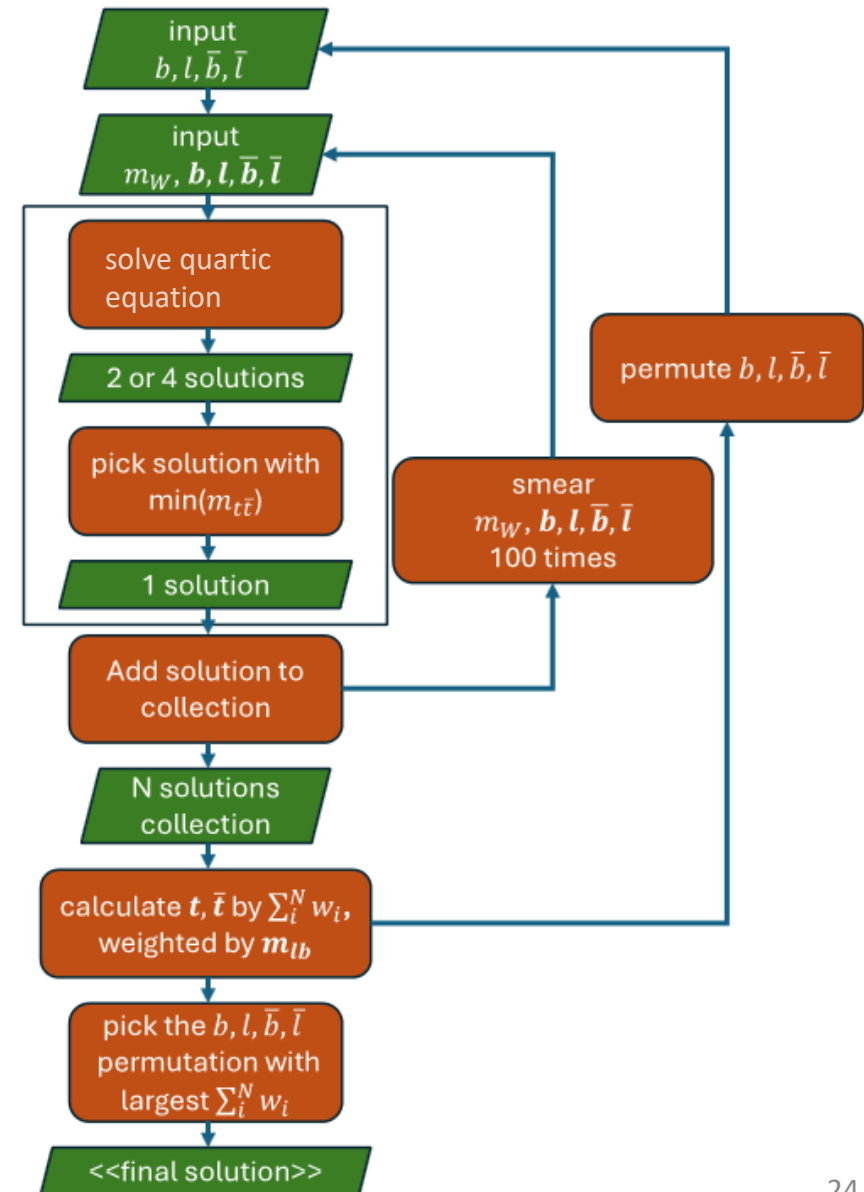
$$E_y^{MET} = p_{y,\nu} + p_{y,\bar{\nu}}$$



Top Quark Reconstruction – $m_{\ell b}$ method

TOP-23-006, TOP-23-001, TOP-20-006, TOP-18-006, TOP-18-004,
TOP-17-014, TOP-16-011, TOP-16-007, TOP-15-010, TOP-12-028

1. Sample W boson mass from Breit-Wigner
2. Solve quartic equation and pick solution that has lowest $m(t\bar{t})$
3. Repeat process 100x smearing leptons & b jets within resolution & resampling W mass
4. Compute solution as weighted sum from smears weighted by true $m_{\ell b}$ distribution
5. Pick jet-parton assignment that maximizes sum of weights



TOP-23-006, TO
TOP-17-014, TO

1. Sample
2. Solve q_i
has low
3. Repeat
within r
4. Comput
smears
5. Pick jet-
of weigh

Bumblebee: Foundation Model for Particle Physics Discovery

[arXiv:2412.07867v1](https://arxiv.org/abs/2412.07867v1)

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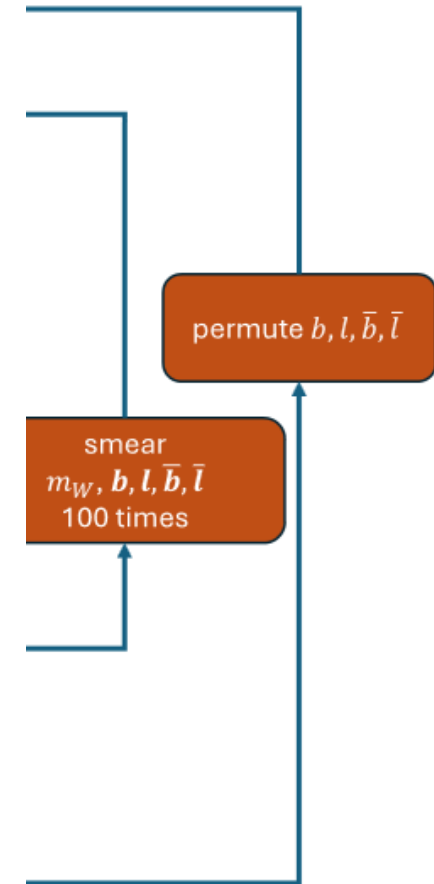
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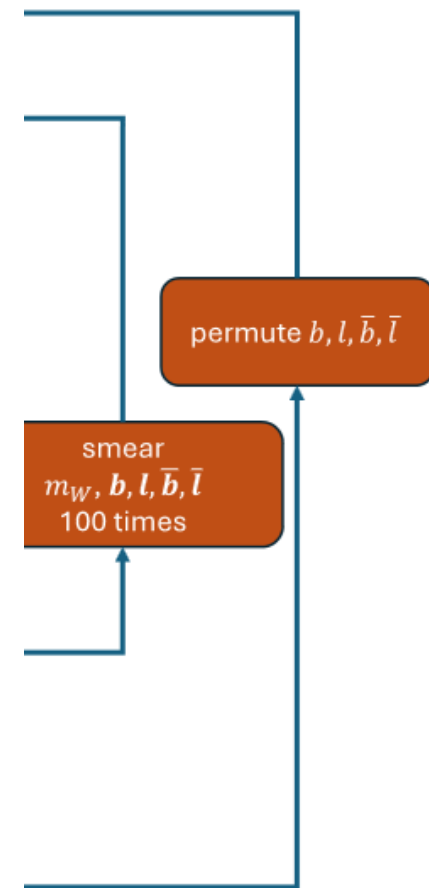
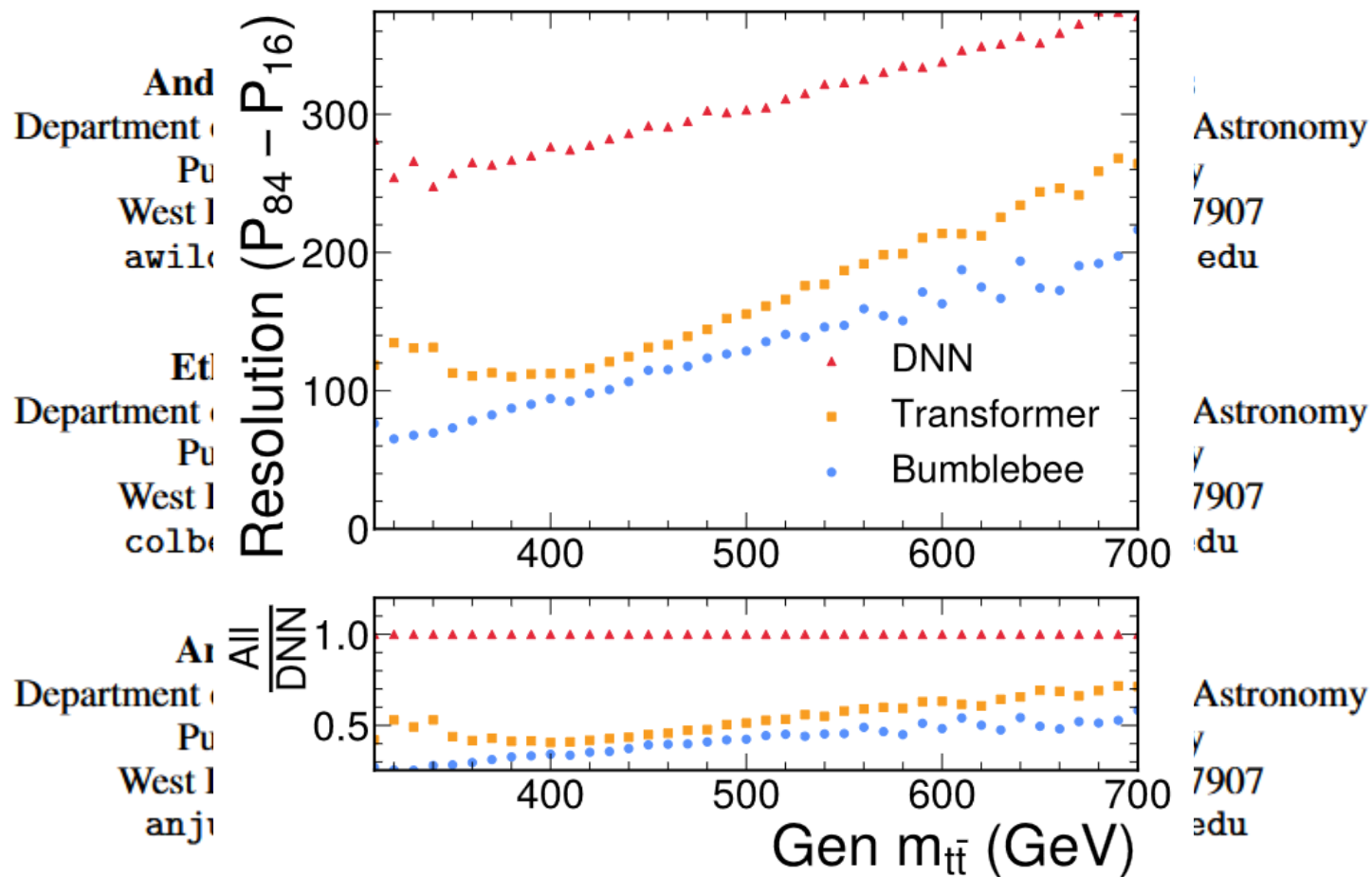


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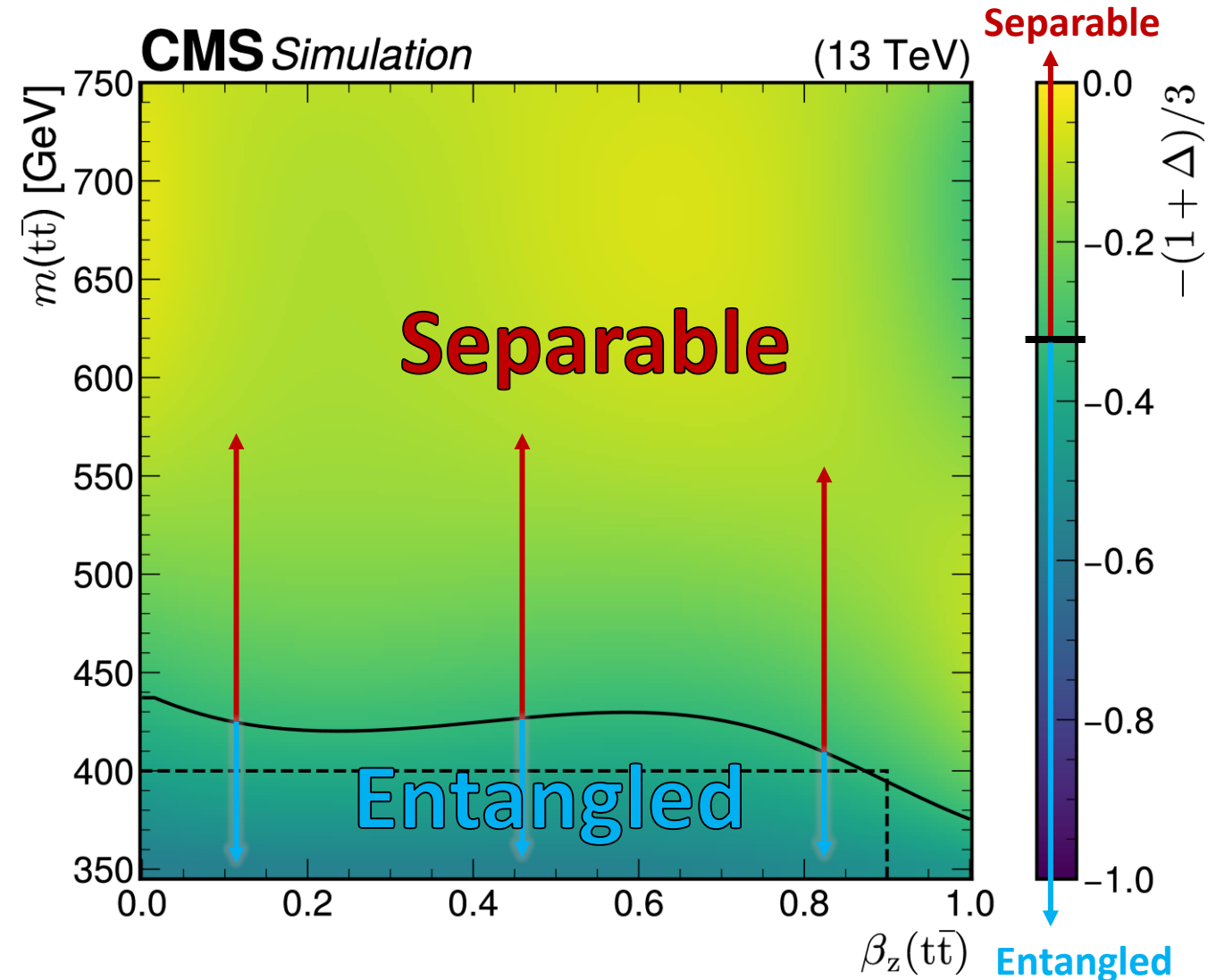
[arXiv:2412.07867v1](https://arxiv.org/abs/2412.07867v1)



Measurement of Entanglement in Threshold Region - Method

[Rep. Prog. Phys. 87 117801](#)

- Used m_{lb} method for reconstructing both neutrinos
- Measured D using a binned profile likelihood fit of $\cos \varphi$
 - Performed fit in:
 $345 < m(t\bar{t}) < 400$ GeV &
 $\beta_z(t\bar{t}) < 0.9$



Profile Maximum Likelihood fit - COMBINE

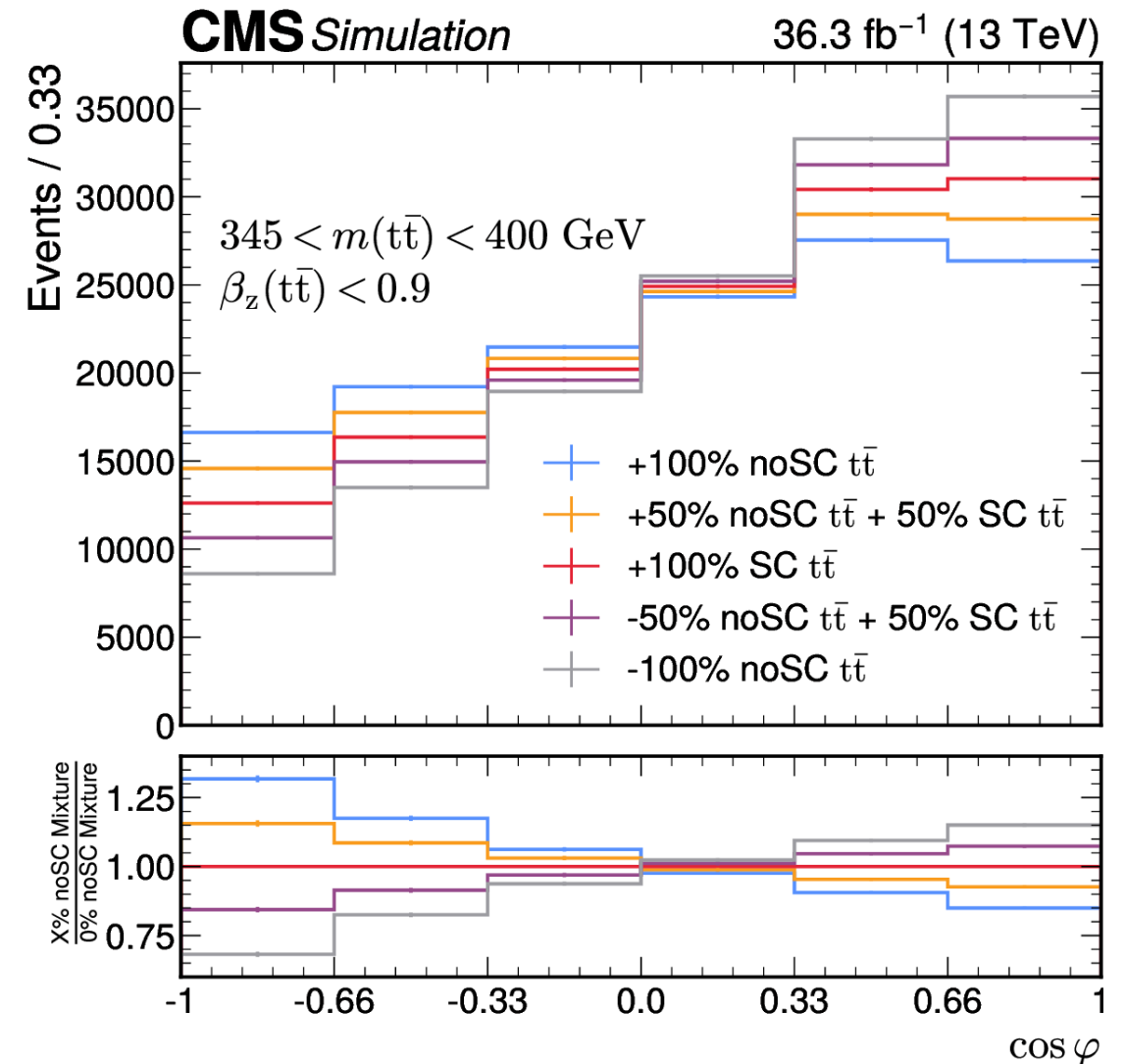
$$\mathcal{L} = \prod_{c \in \text{channels}} \prod_{b \in \text{bins}_c} \text{Pois}(n_{cb} | \nu_{cb}(\mathbf{H}, \mathbf{X})) \prod_{\chi \in \mathbf{X}} p_{\chi}(a_{\chi} | \chi)$$

- Channels are statistically independent “channels”. Can be decay topology for example (ee vs. eμ vs. μμ)
 - We only performed the fit in a single channel – “combined”
- n_{cb} is number of observed events
- ν_{cb} is number of expected events
- $\eta \in \mathbf{H}$ are unconstrained nuisance parameters meaning they have no prior
 - Signal strength modifier is typically an unconstrained nuisance
 - D is also unconstrained in our fit and we freeze signal strength modifier
- $\chi \in \mathbf{X}$ are constrained nuisance parameters meaning we know/can estimate their prior probability distribution
 - a_{χ} are parameters/inputs for the prior (auxiliary measurements)
 - All of our priors are either log normal or shape-based

Measurement of Entanglement in Threshold Region - Method

- Need to fit POI D
 - Q: How to create variations of D ?
 - A: Generate top quark pairs with zero spin correlation $\rightarrow D = 0$
- Can create new samples with mixtures of SM and no spin corr.
- These mixtures only probe $[D_{SM}, 0] \rightarrow$ Mirror to probe $[-1, D_{SM}]$

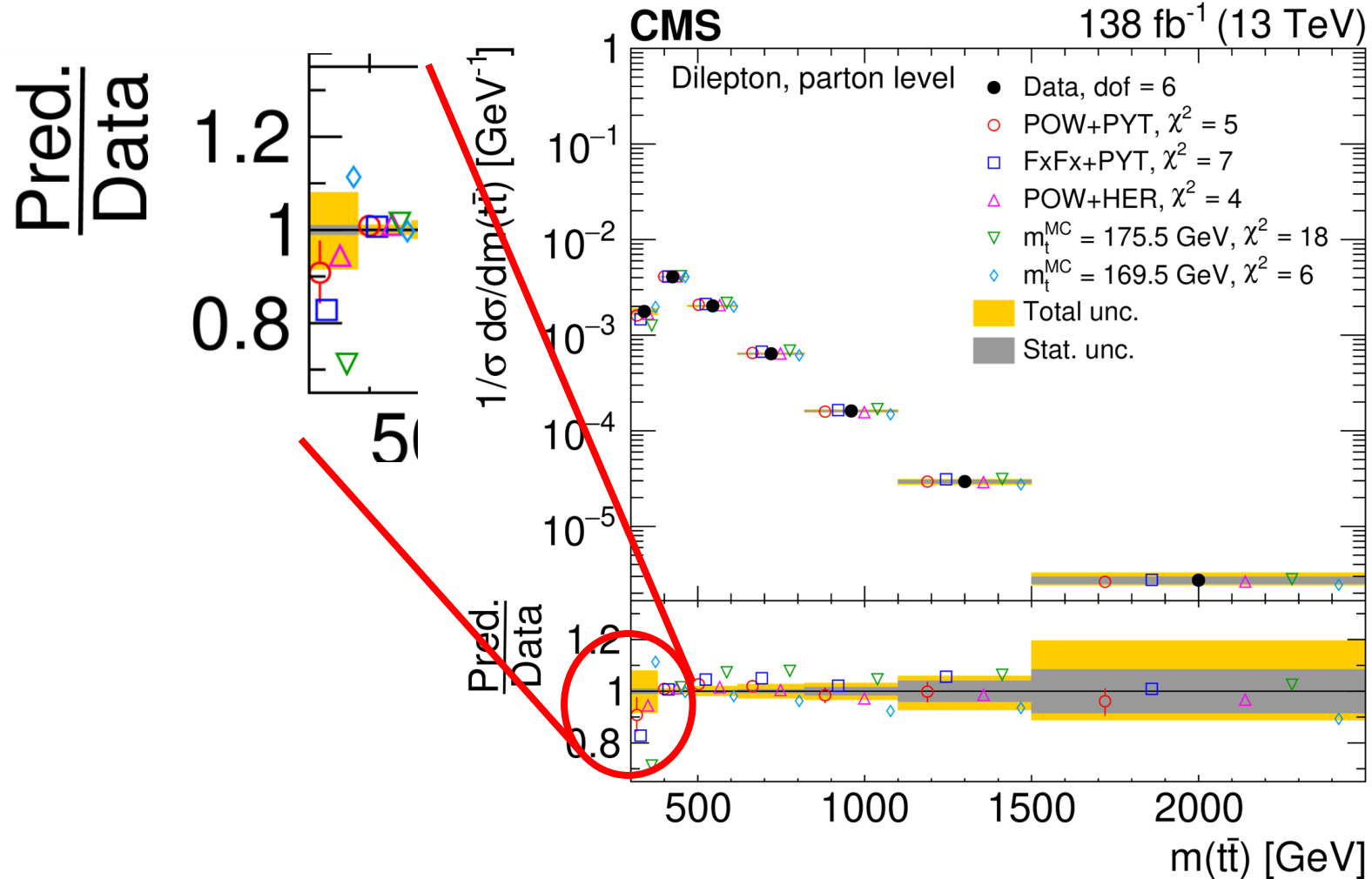
[Rep. Prog. Phys. 87 117801](#)



Measurement of Entanglement in Threshold Region

- Large mismodeling seen for $m(t\bar{t}) \approx 345$ GeV

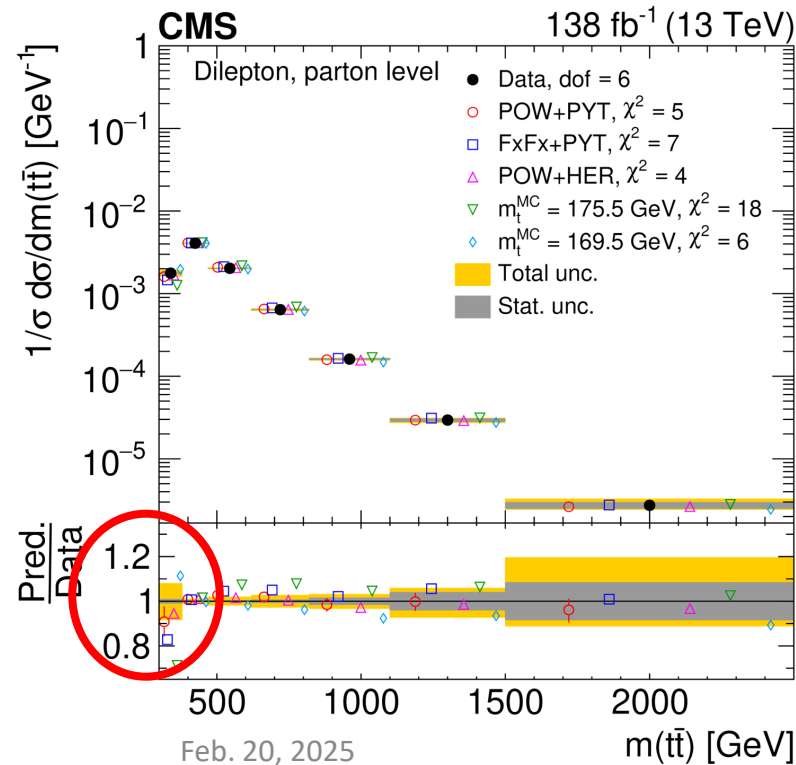
[JHEP \(2025\), 64](#)



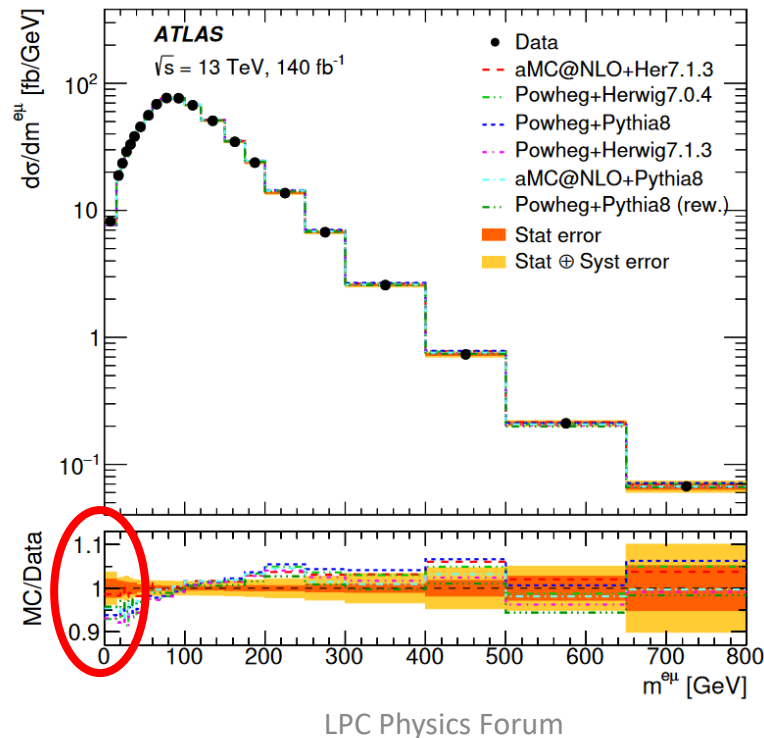
Measurement of Entanglement in Threshold Region

- Large mismodeling seen for $m(t\bar{t}) \approx 345$ GeV
- Consistent between dilepton & lepton+jets and CMS & ATLAS

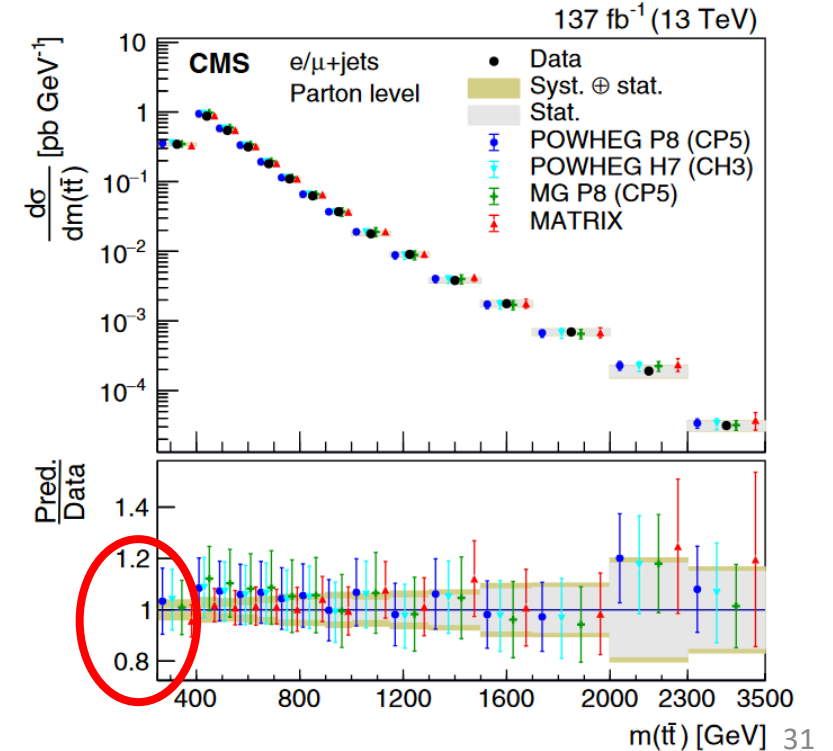
[JHEP \(2025\), 64](#)



[JHEP 07 \(2023\) 141](#)



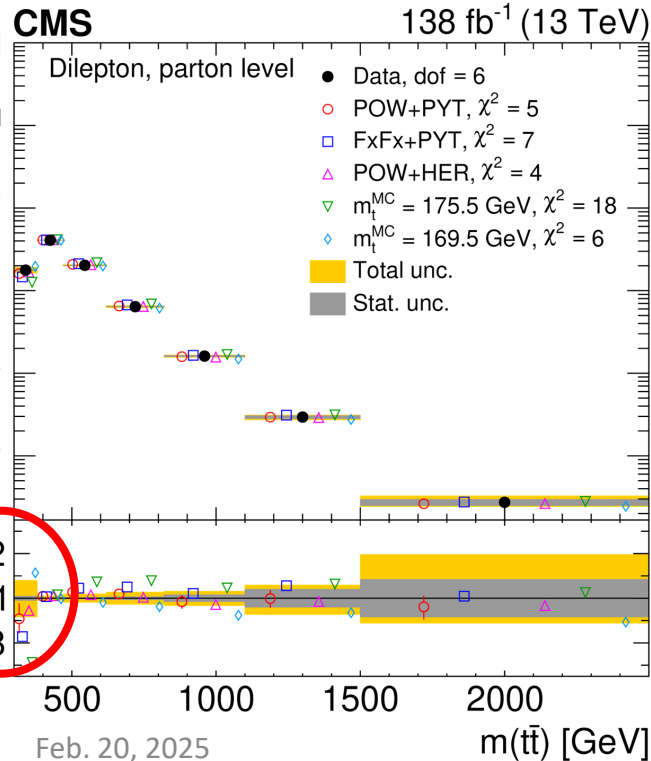
[Phys. Rev. D 104, 092013](#)



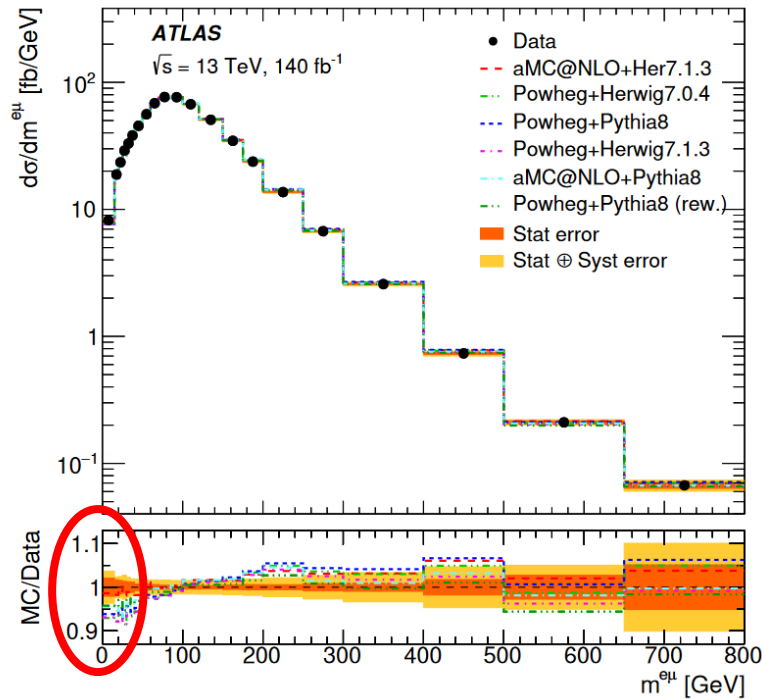
Measurement of Entanglement in Threshold Region

- Large mismodeling seen for $m_{t\bar{t}} \approx 345$ GeV
- Excesses seen could be from **toponium**
- New (hypothetical) exciting SM resonance
 - Spin singlet \rightarrow Maximally **entangled** $t\bar{t}$
 - Exciting implications for **entanglement** measurements!
- Signal model includes spin and color singlet $^1S_0^{[1]}$

[JHEP \(2025\), 64](#)

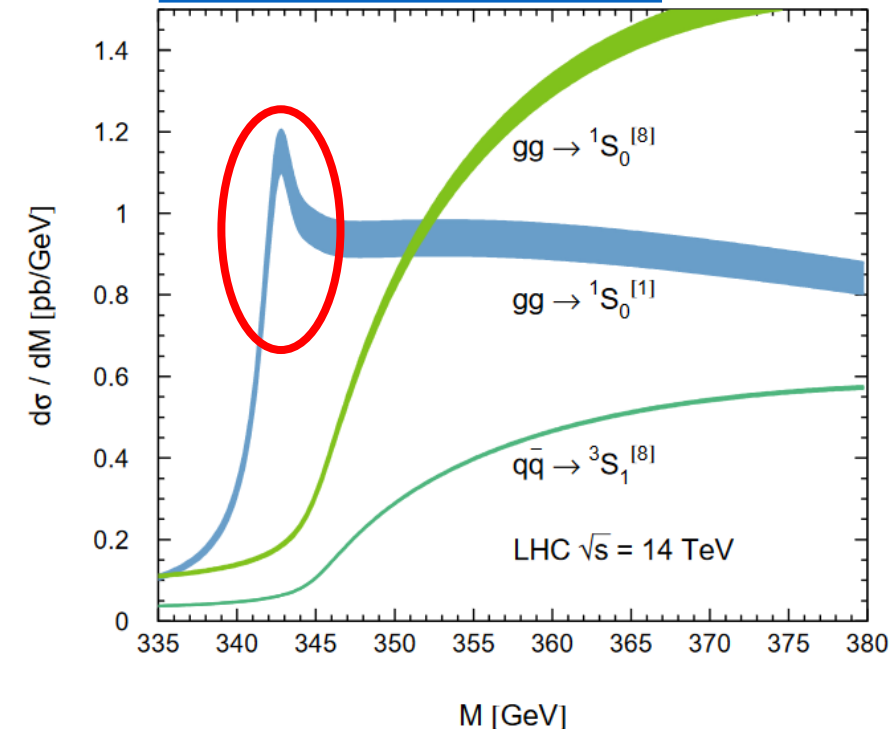


[JHEP 07 \(2023\) 141](#)



- Theory predictions with NRQCD
- Color **singlet** and **octet** contributions to spin singlet

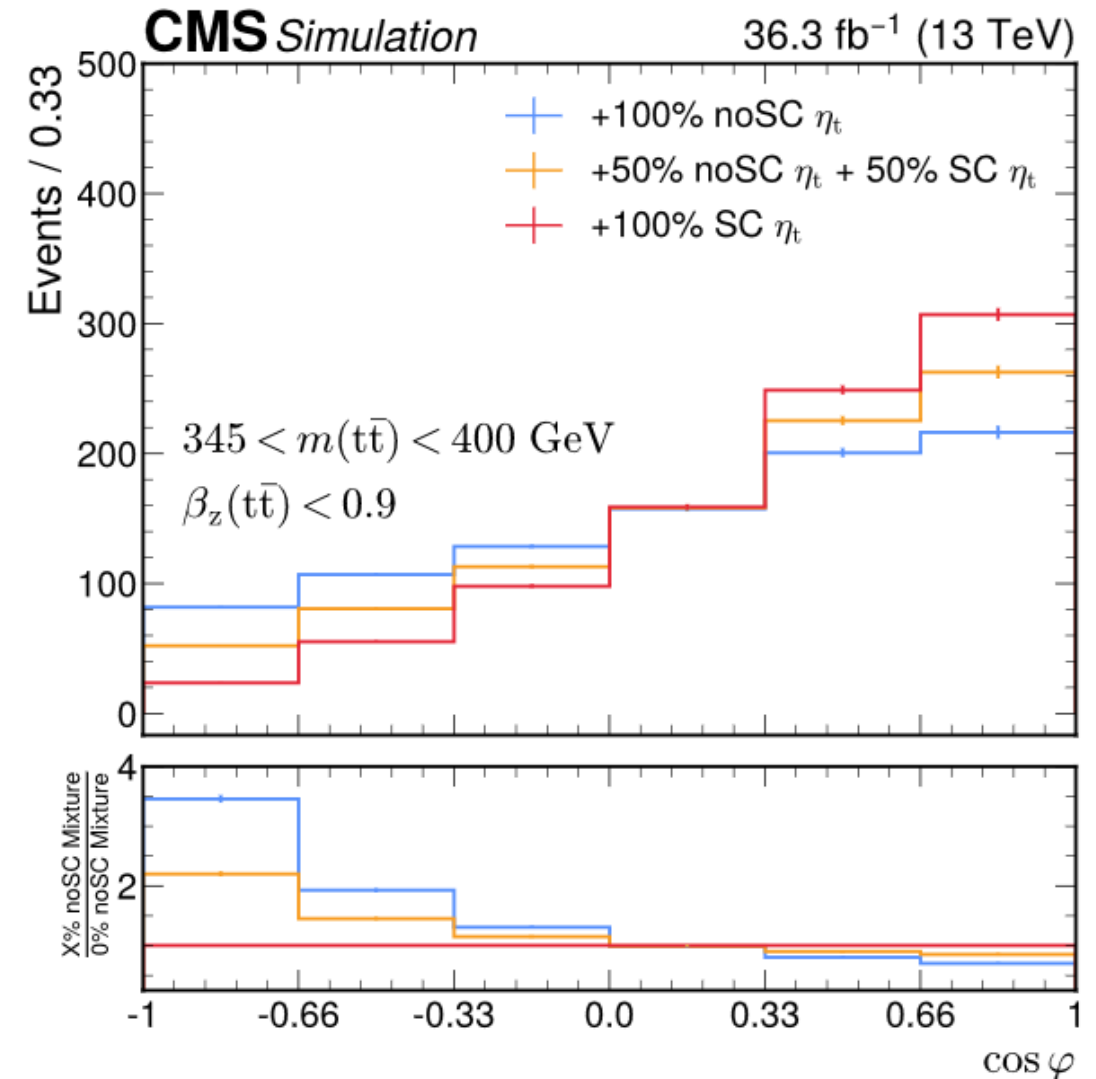
[EPJC 60, 375 \(2009\)](#)



Measurement of Entanglement in Threshold Region - Method

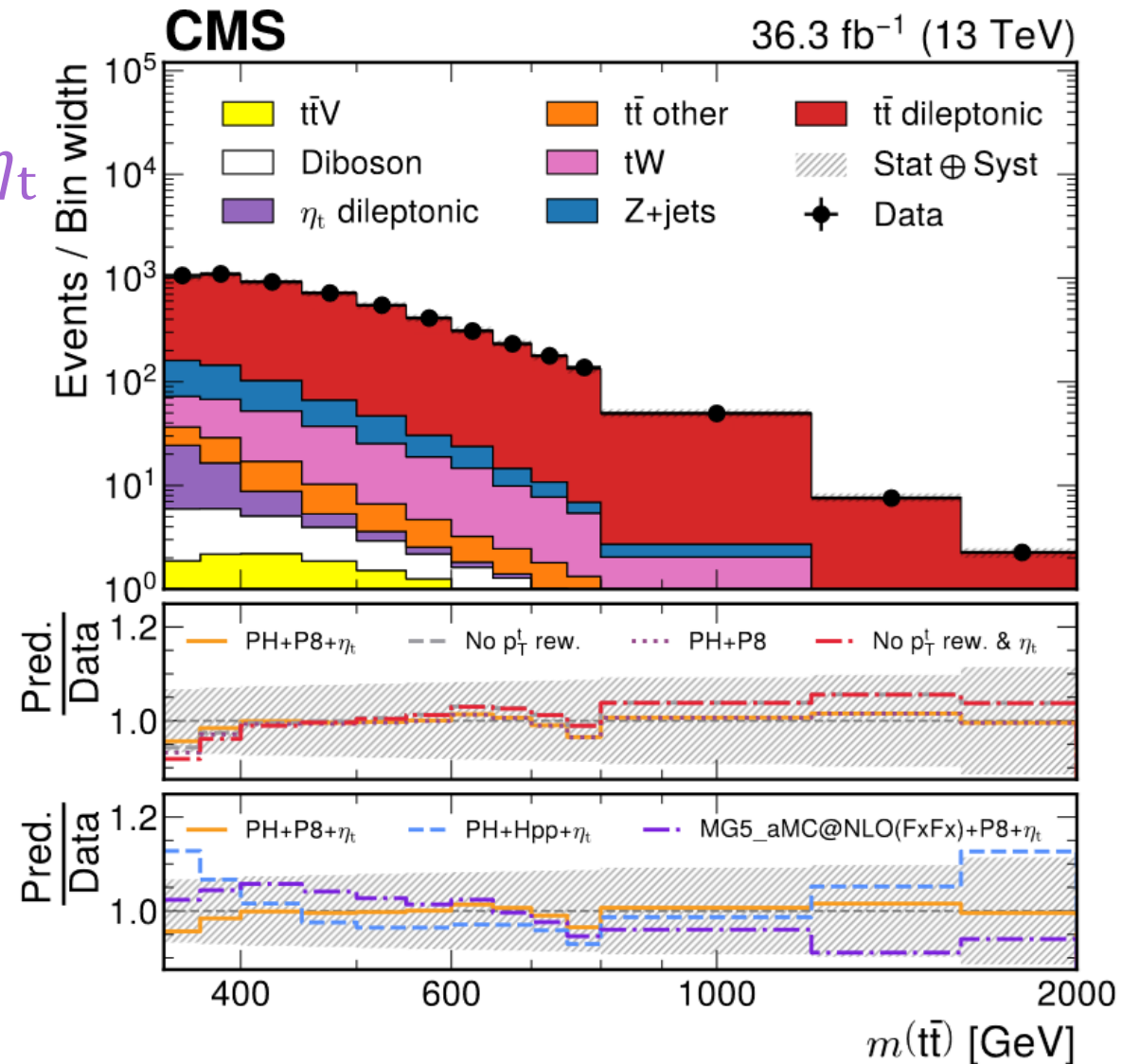
- Need to fit POI D
 - Q: How to create variations of D ?
 - A: Generate top quark pairs with zero spin correlation $\rightarrow D = 0$
- Can create new samples with mixtures of SM and no spin corr.
- These mixtures only probe $[D_{SM}, 0] \rightarrow$ ~~Mirror to probe $[-1, D_{SM}]$~~
- For η_t we cannot mirror templates \rightarrow
- Performed the fit both including & excluding the ground state of **toponium, η_t**

[Rep. Prog. Phys. 87 117801](#)



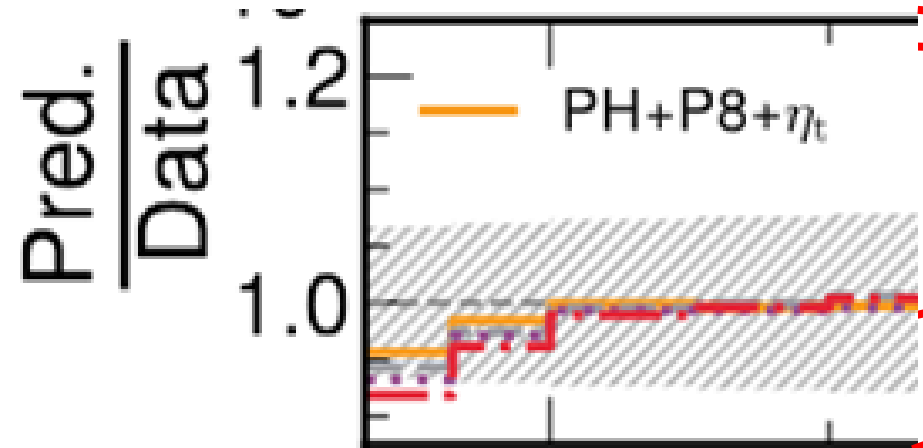
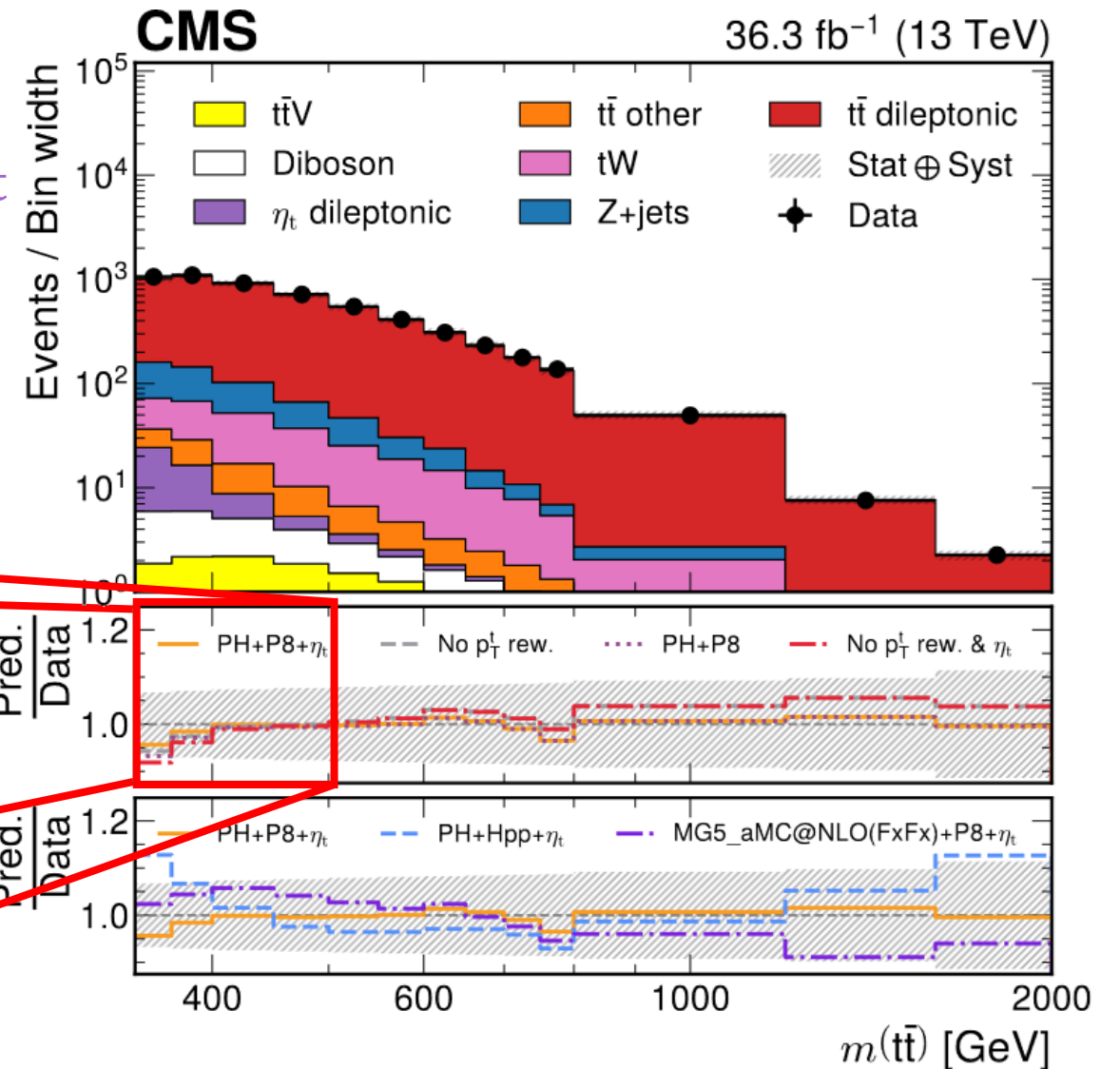
Pre-fit Distributions

- Better agreement when including η_t



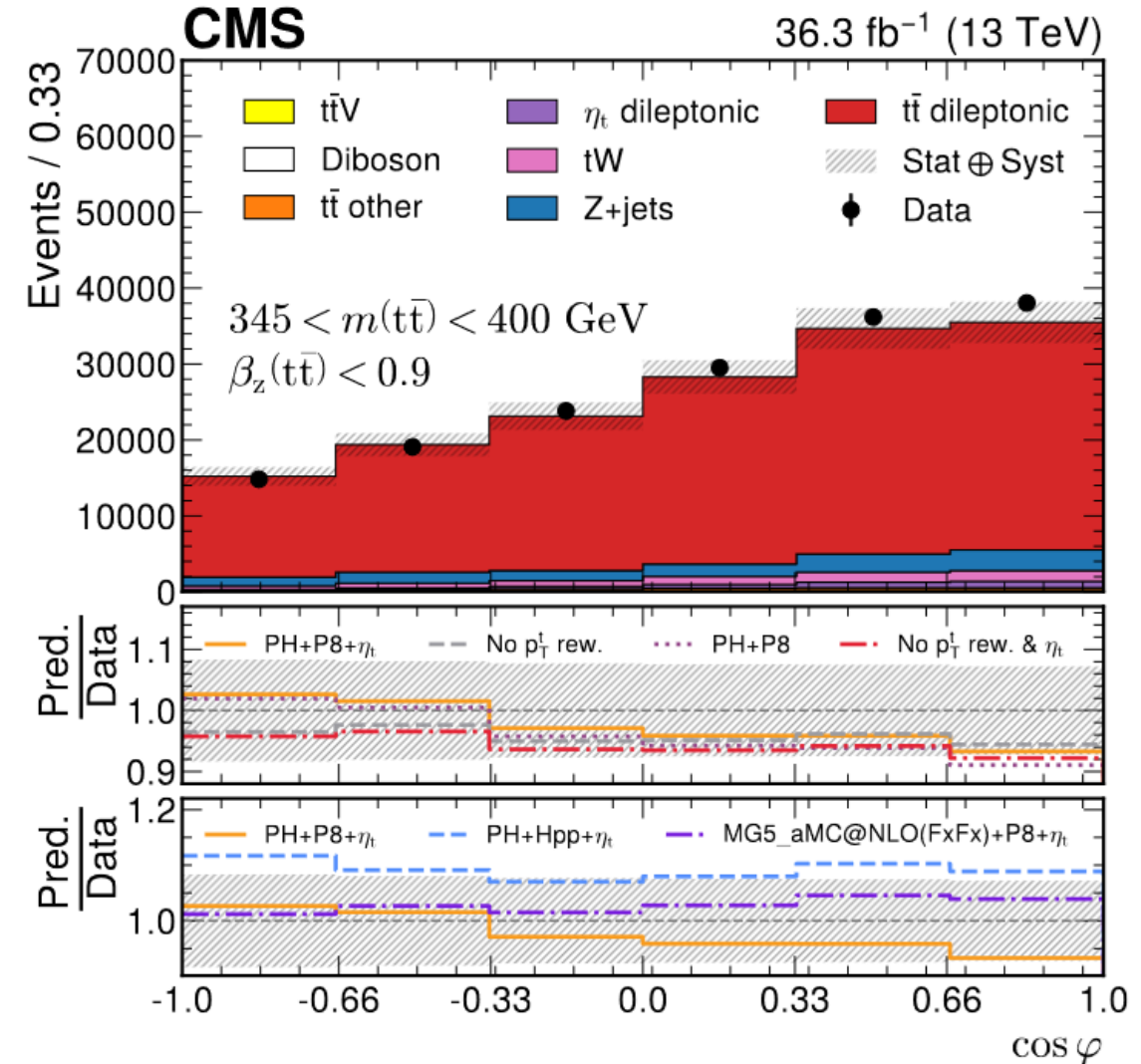
Pre-fit Distributions

- Better agreement when including η_t



Pre-fit Distributions

- Better agreement when including η_t
- MadGraph5 aMC@NLO+Pythia8 describes the $\cos \varphi$ distribution better near production threshold



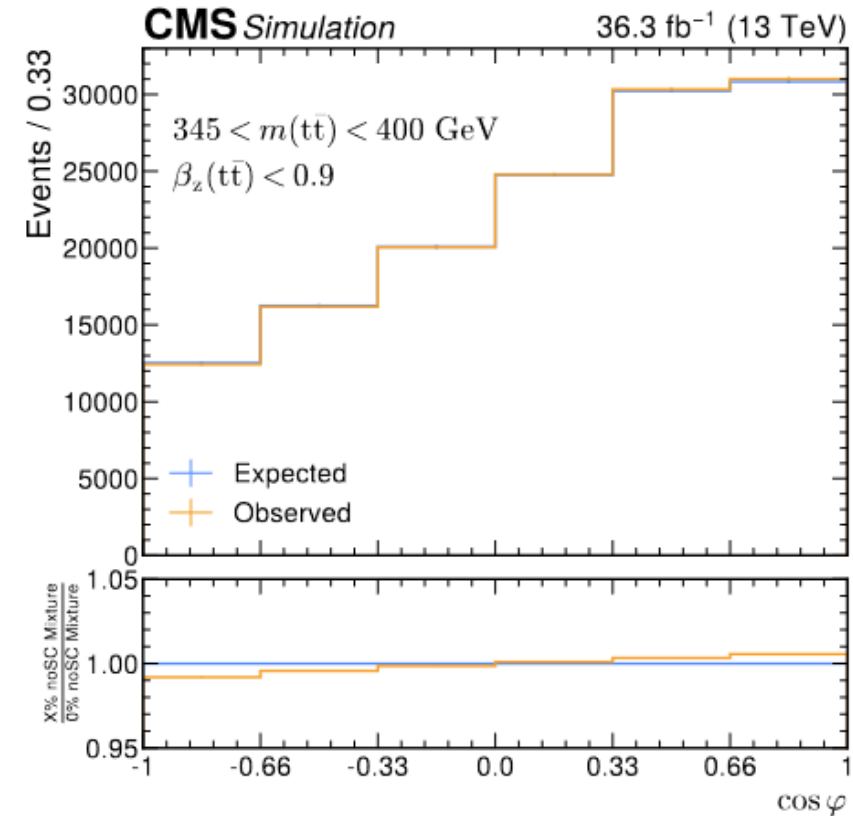
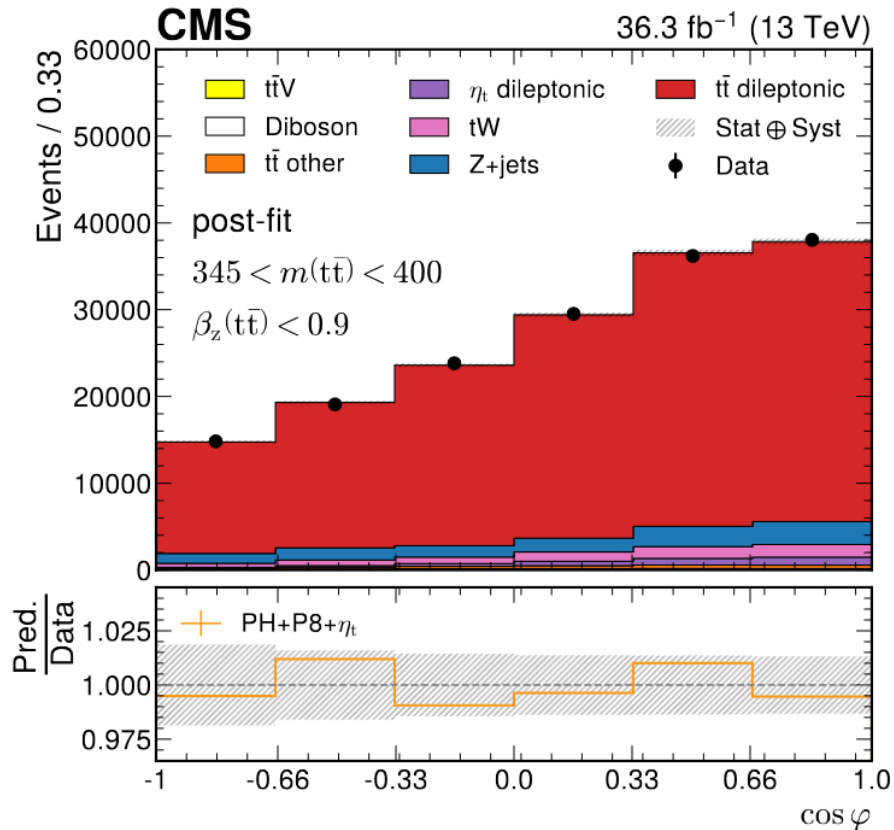
Corrections and Uncertainties

- Entanglement observed via slope parameter $D \rightarrow$ shape of $\cos\varphi$ is important
- Leading systematics
 - Jet Energy Scale (JES)
 - η_t normalization
 - Parton shower Initial state radiation (ISR)/Final state radiation (FSR)
 - Top quark mass
 - NNLO QCD reweighting
 - EWK corrections
 - Z+jets normalization

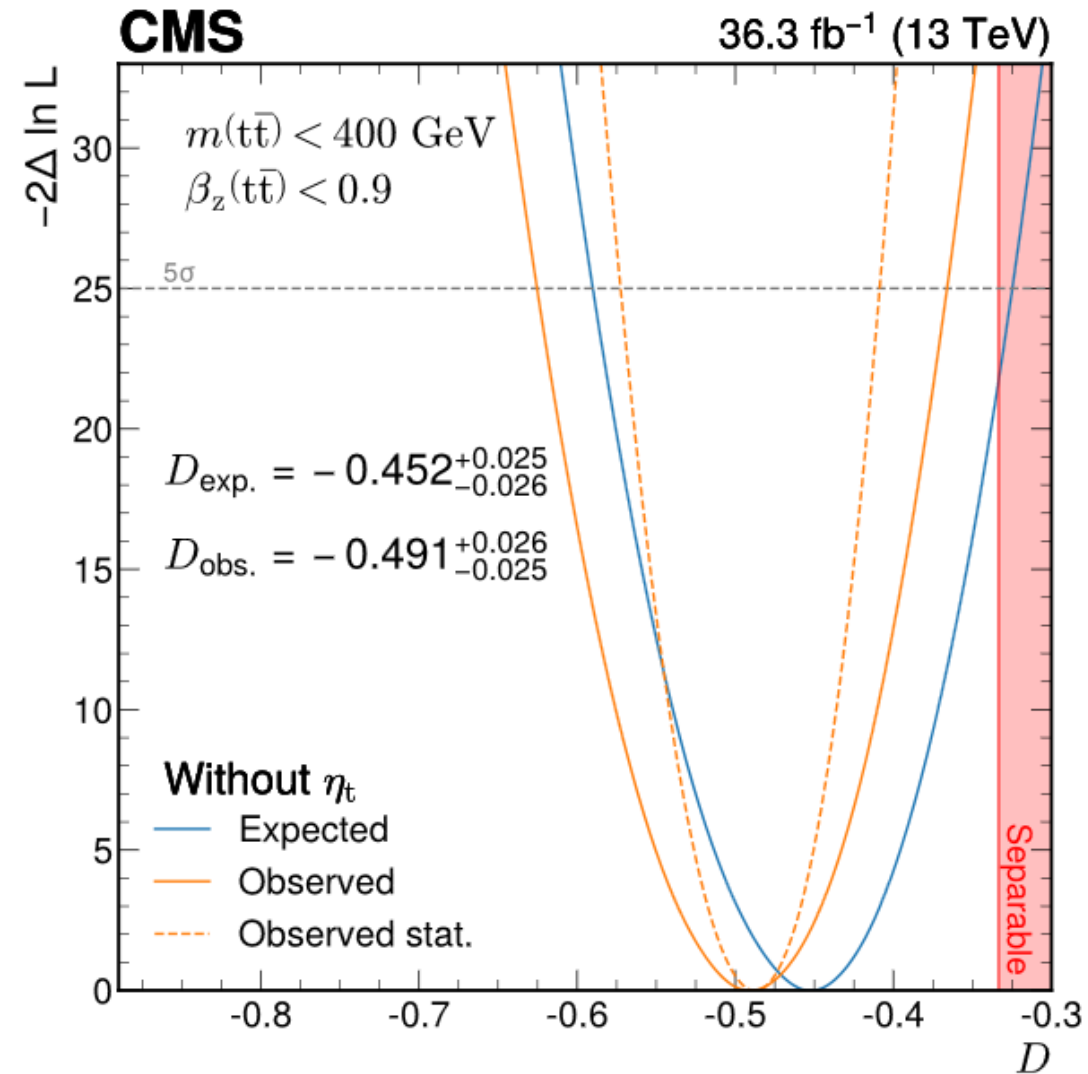
Uncertainty category	Type	Effect on yield	Effect on shape
<i>Experimental uncertainties</i>			
Trigger efficiency	Shape	0.5%	0.2%
Lepton ident./isolation	Shape	3.0%	0.2%
b tagging (heavy)	Shape	0.6%	0.1%
b tagging (light)	Shape	0.3%	0.2%
Kinematic reconstruction	Shape	0.3%	0.1%
JES: Absolute	Shape	0.9%	0.3%
JES: Absolute (stat)	Shape	0.4%	0.2%
JES: Pileup	Shape	0.5%	0.2%
JES: Flavor QCD	Shape	0.7%	0.2%
JES: Relative balance	Shape	0.4%	0.8%
JER	Shape	0.3%	0.3%
Unclustered energy	Shape	0.2%	0.3%
Pileup	Shape	0.4%	0.1%
$t\bar{t}$ normalization	Norm.	4.4%	0.3%
Z+jets normalization	Norm.	1.6%	0.4%
Z+jets shape	Shape	0.2%	0.2%
Luminosity	Norm.	1.2%	<0.1%
<i>Model uncertainties</i>			
Matrix-elem. renorm. scale variation	Shape	0.4%	0.3%
Matrix-elem. fact. scale variation	Shape	0.6%	0.2%
Parton shower: Initial-state radiation	Shape	0.8%	0.7%
Parton shower: Final-state radiation	Shape	2.1%	0.4%
Top quark mass	Shape	2.4%	0.5%
ME/parton shower matching	Norm.	0.8%	<0.1%
Underlying event	Norm.	0.8%	<0.1%
PDF	Shape	0.9%	0.1%
Color reconnection	Norm.	0.8%	<0.1%
b quark fragmentation	Shape	0.7%	0.4%
B hadron semilept. decays	Shape	0.3%	0.2%
Branching fraction	Norm.	1.9%	<0.1%
NNLO QCD reweighting	Shape	0.6%	0.4%
EWK corrections	Shape	0.6%	0.4%
η_t normalization	Norm.	0.7%	0.8%
η_t binding energy	Shape	0.2%	0.1%

Post-fit Distribution

- Good agreement within uncertainties
- Post-fit value of 2.53% more spin correlated $t\bar{t}$ contribution



Measurement of Entanglement in Threshold Region - Results

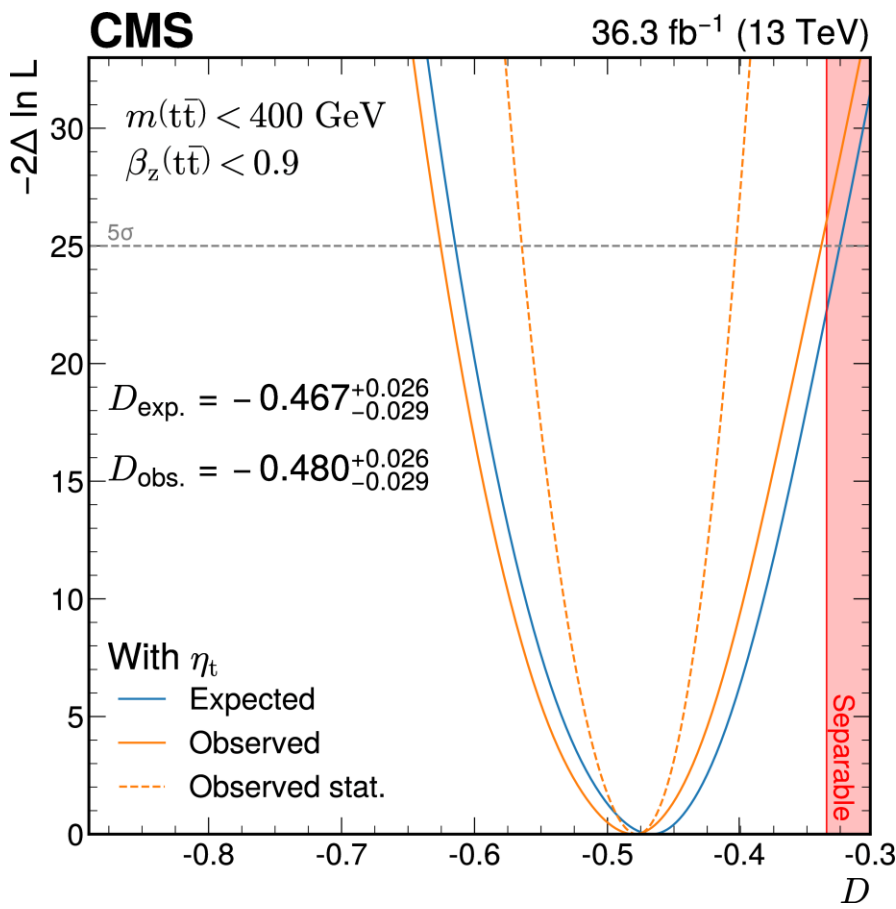


- Significance $> 5\sigma$ when not including uncertainty and effect of η_t
- Although η_t existence hasn't been confirmed experimentally, important to know possible bias & reduction of significance of measurement

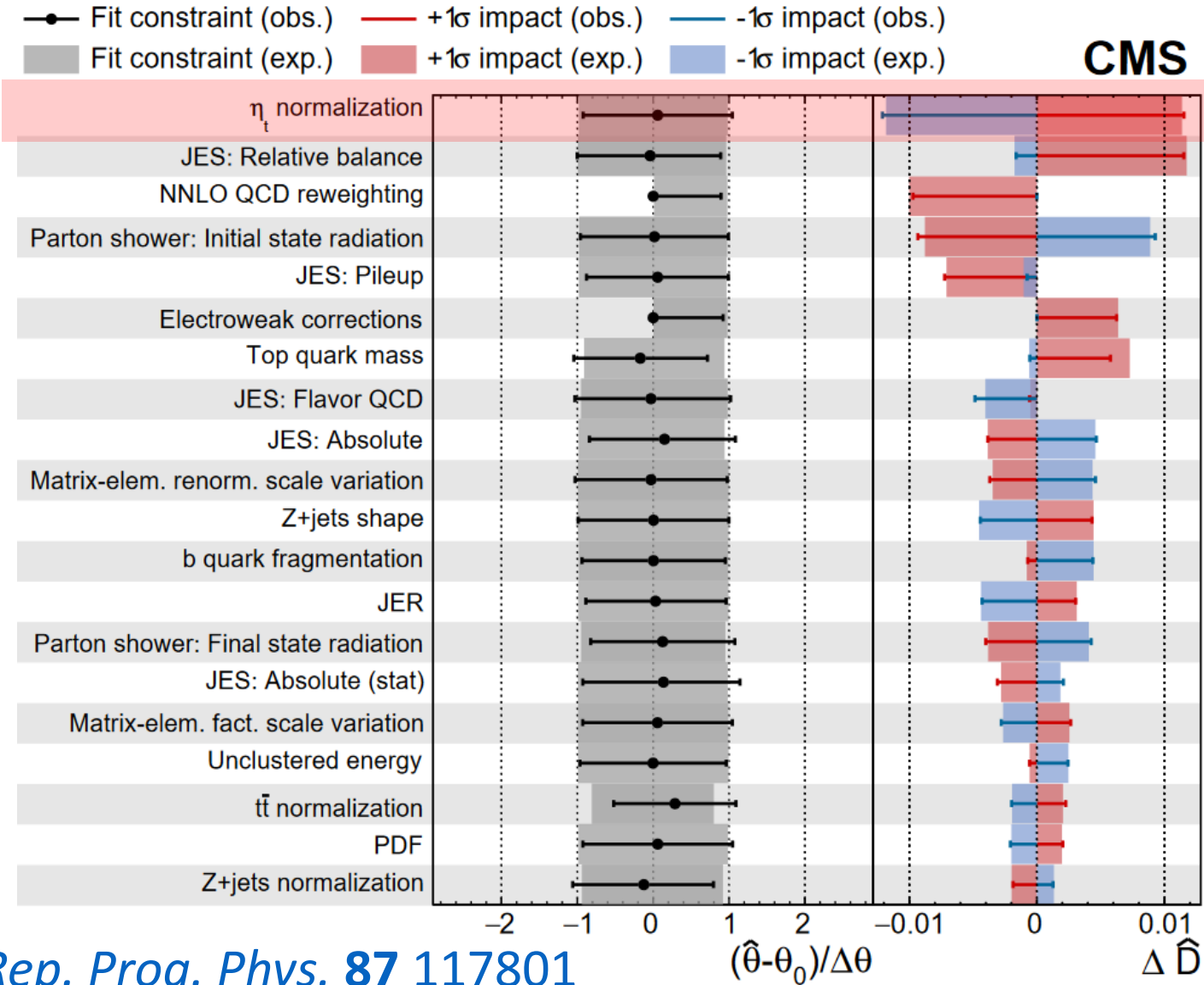
[Rep. Prog. Phys. **87** 117801](#)

Measurement of Entanglement in Threshold Region - Results

- Significance $> 5\sigma$
- Observation of **entangled top quarks!**



Feb. 20, 2025

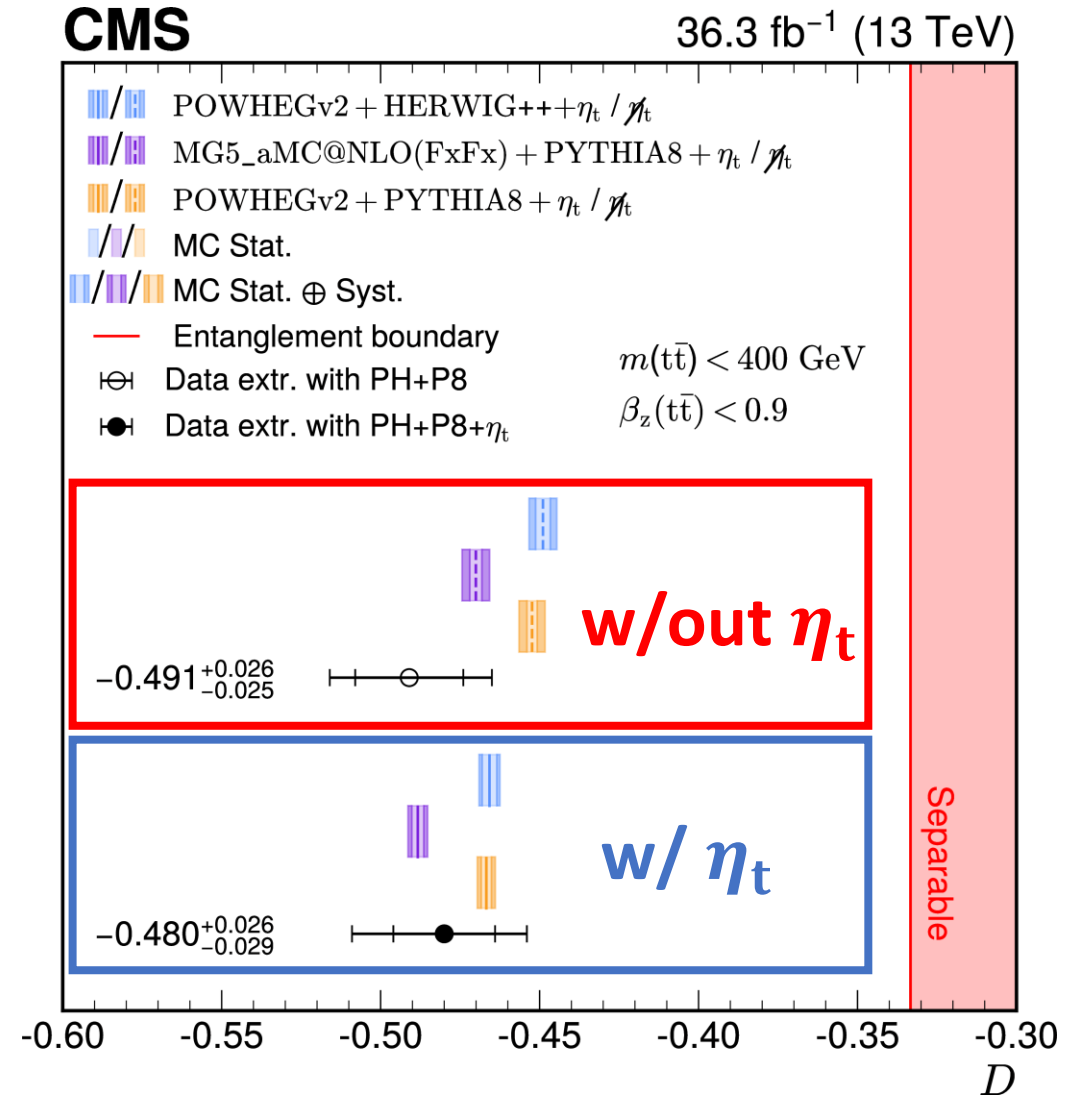


[Rep. Prog. Phys. 87 117801](#)

LPC Physics Forum

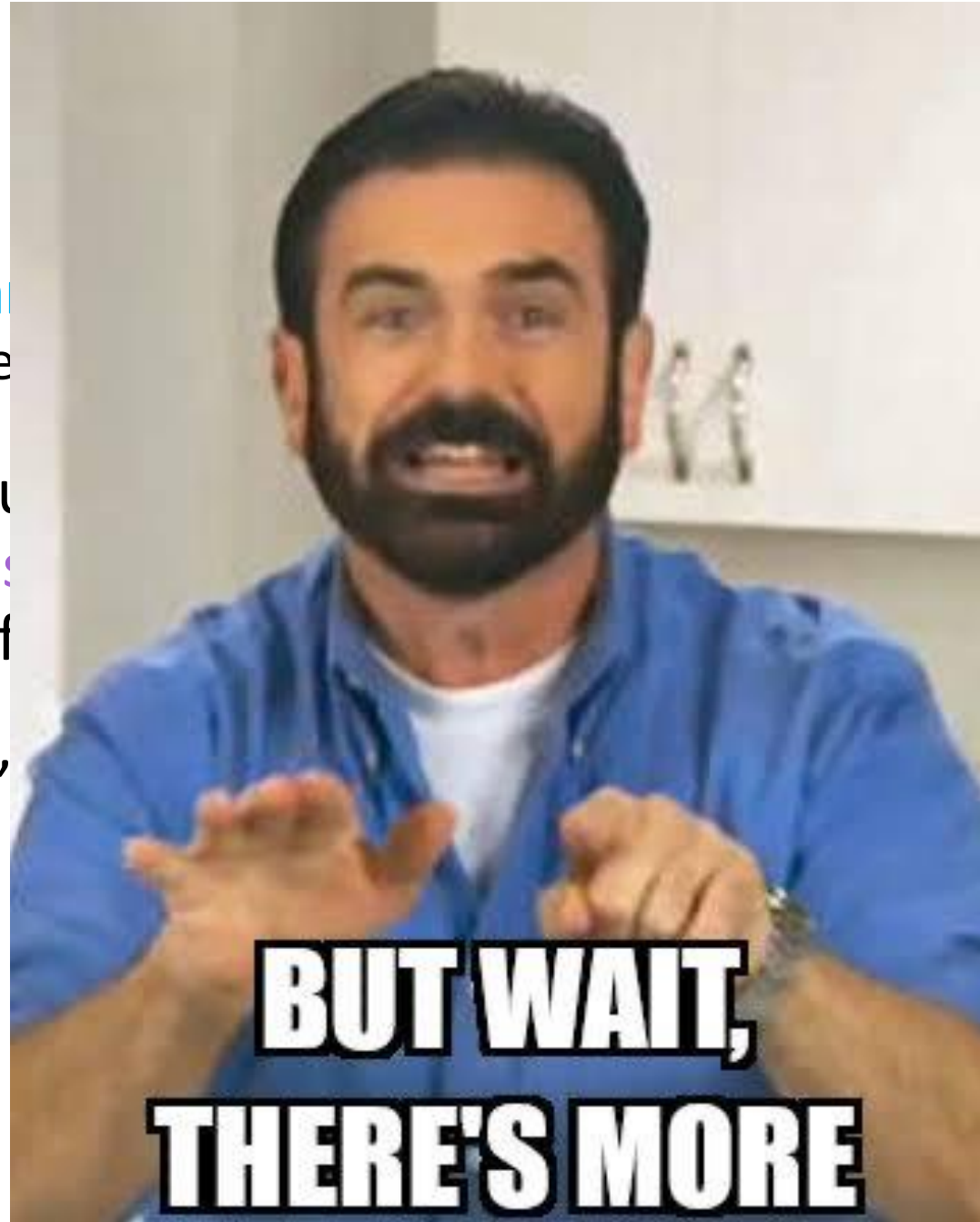
Conclusion

- Top quarks are **entangled**
 - Spins are correlated in a non-classical manner
- First inclusion of bound-state effects in the **production threshold** region via η_t
- Start of quantum information studies in high energy physics at the LHC
- New door into “old” physics



Conclusion

- Top quarks are **entangled**
 - Spins are correlated in a non-classical manner
- First inclusion of both production and decay in the **production threshold**
- Start of quantum information in high energy physics
- New door into “old” physics



[Phys. 87 117801](#)

36.3 fb⁻¹ (13 TeV)

ERWIG+++ η_t / \mathcal{M}_t

)(FxFx) + PYTHIA8 + η_t / \mathcal{M}_t

PYTHIA8 + η_t / \mathcal{M}_t

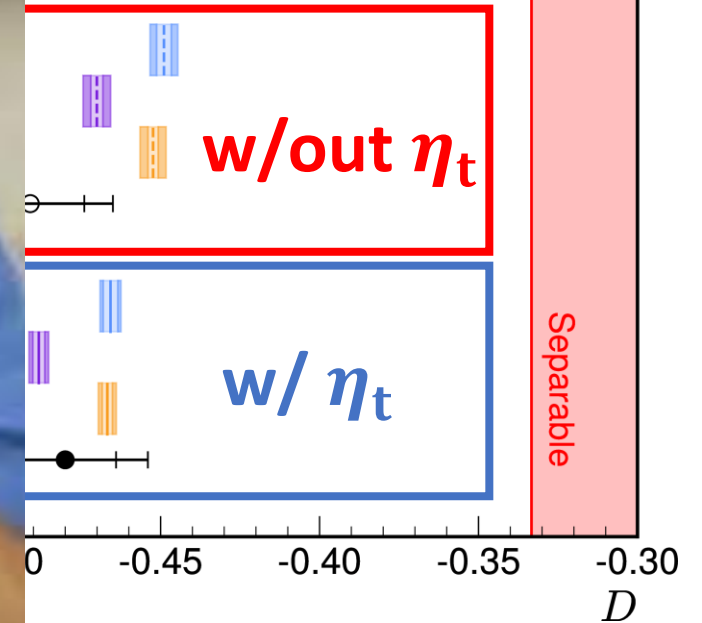
boundary

t+P8

t+P8+ η_t

$m(t\bar{t}) < 400$ GeV

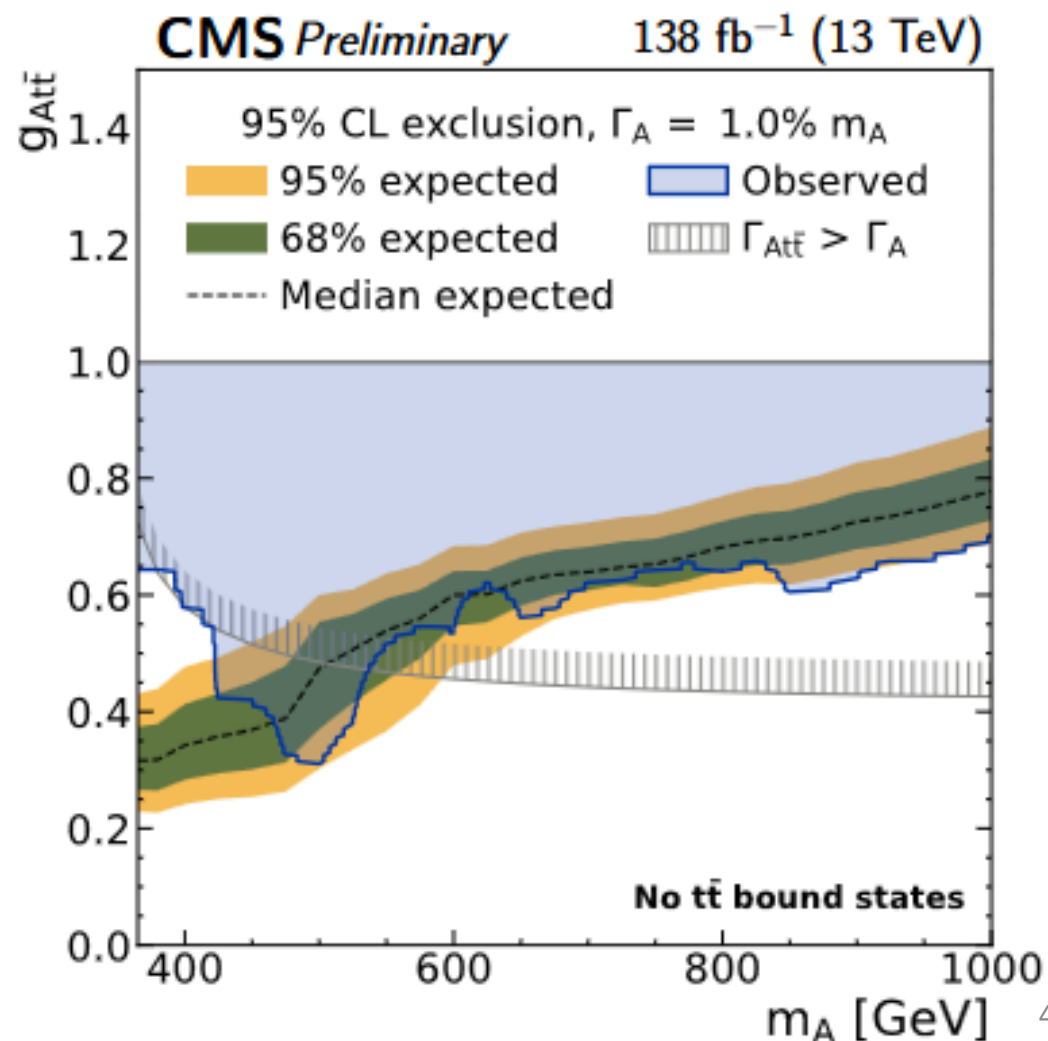
$\beta_z(t\bar{t}) < 0.9$



Discovery of a Pseudoscalar Structure

[HIG-22-013 PAS](#)

- CMS has now published a separate paper recognizing there is a pseudoscalar structure in the $m(t\bar{t})$ spectrum in the threshold region
- Consistent with $1S_0^{[1]}$ and fit $\sigma(\eta_t)$ of $7.1 \text{ pb} \pm 11\%$
- Further investigations by both the experimental and theoretical communities are necessary to elucidate the nature of this excess



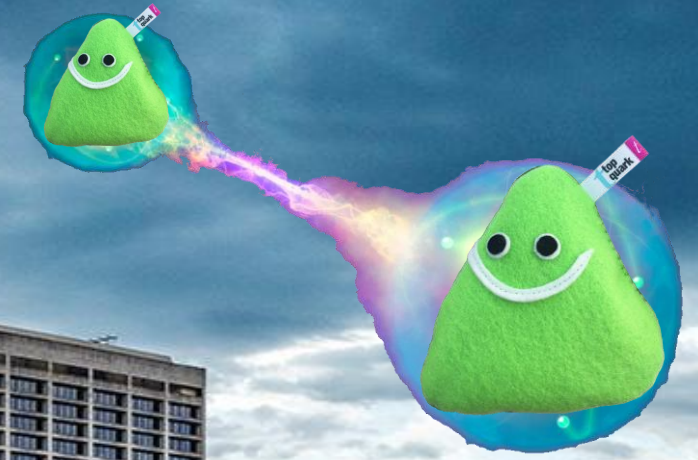
What's next? – My personal viewpoint

[Phys. Rev. D **108**, 076025](#) [Phys. Rev. D **109**, 096027](#)

- Does the wave function “collapse” after the top quarks decay?
 - Decoherence studied in a high energy environment – only @LHC!!
[Phys. Rev. Lett. **127**, 161801](#) [EPJC **82**, 666](#) [Phys. Rev. D **109**, 115023](#)
- Do top quarks violate Bell's inequality?
 - Cannot perform direct Bell test [PLB **280**, 3–4](#)
 - Measure expectation value of Bell operator
- What quantum observables are sensitive to new physics?
 - Entanglement witness has shown to give orthogonal directions [JHEP \(2023\)148](#)
 - Magic? – non-linear combination of correlations [Phys. Rev. D **110**, 116016](#)
 - Maybe something still new entirely
- Qutrit entanglement
 - $H \rightarrow WW, H \rightarrow ZZ$ [Phys. Rev. D **109**, 113004](#)
 - Double slit-like experiment [arXiv:2411.13464](#)

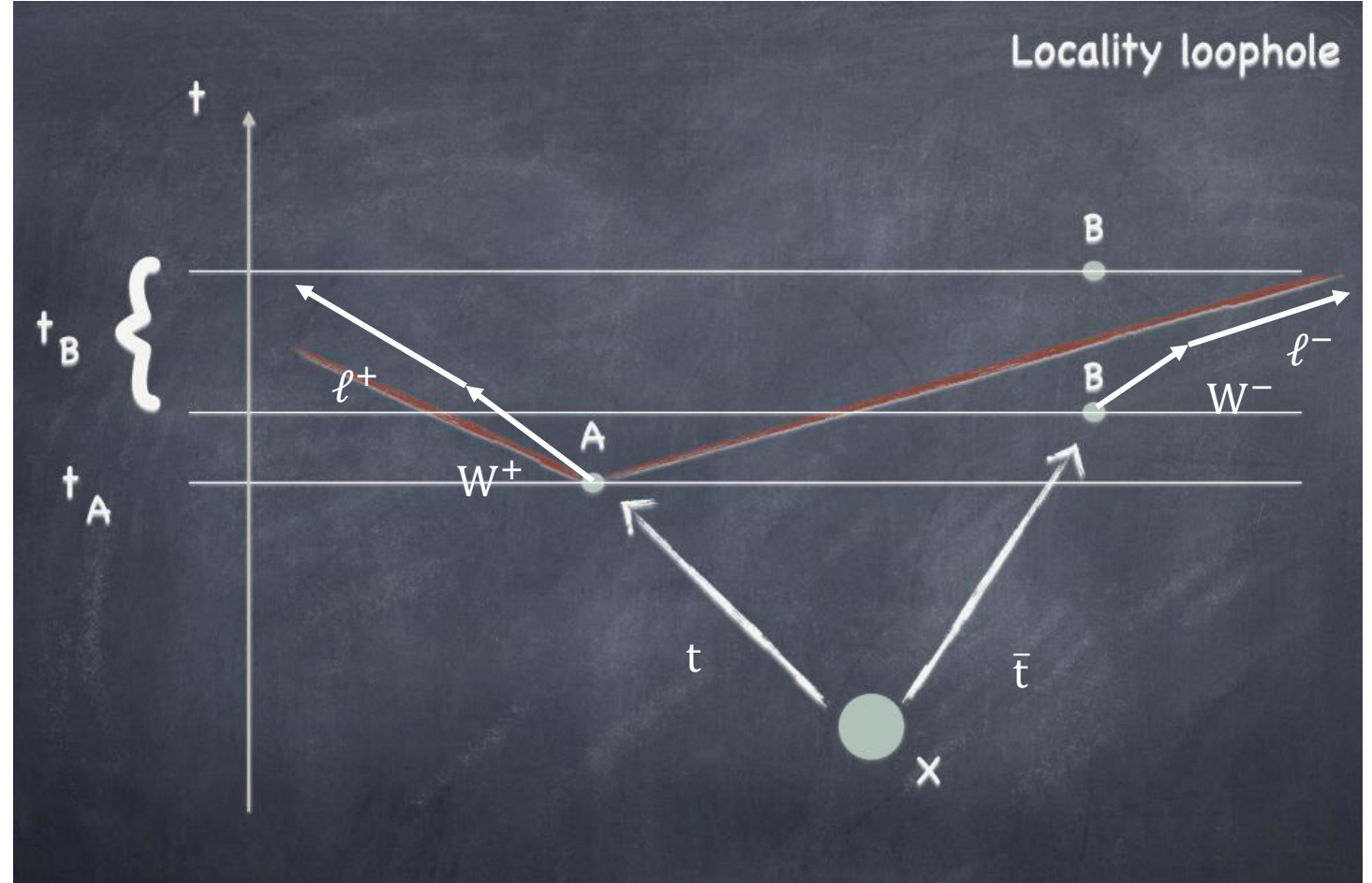
Thanks!

awildrid@purdue.edu



Spacelike separated entanglement

- First off, entanglement \neq violation of Bell inequality
- Because subsequent decays are **lighter**, spacelike separated events typically **stay spacelike separated**
- Closing locality loophole requirements:
 1. **spacelike separated measurements**
 2. **Random measurement settings**



Modified from [[2402.07972](#)]

Helicity Basis: Spin Quantization Axes $\{\hat{\mathbf{k}}, \hat{\mathbf{n}}, \hat{\mathbf{r}}\}$

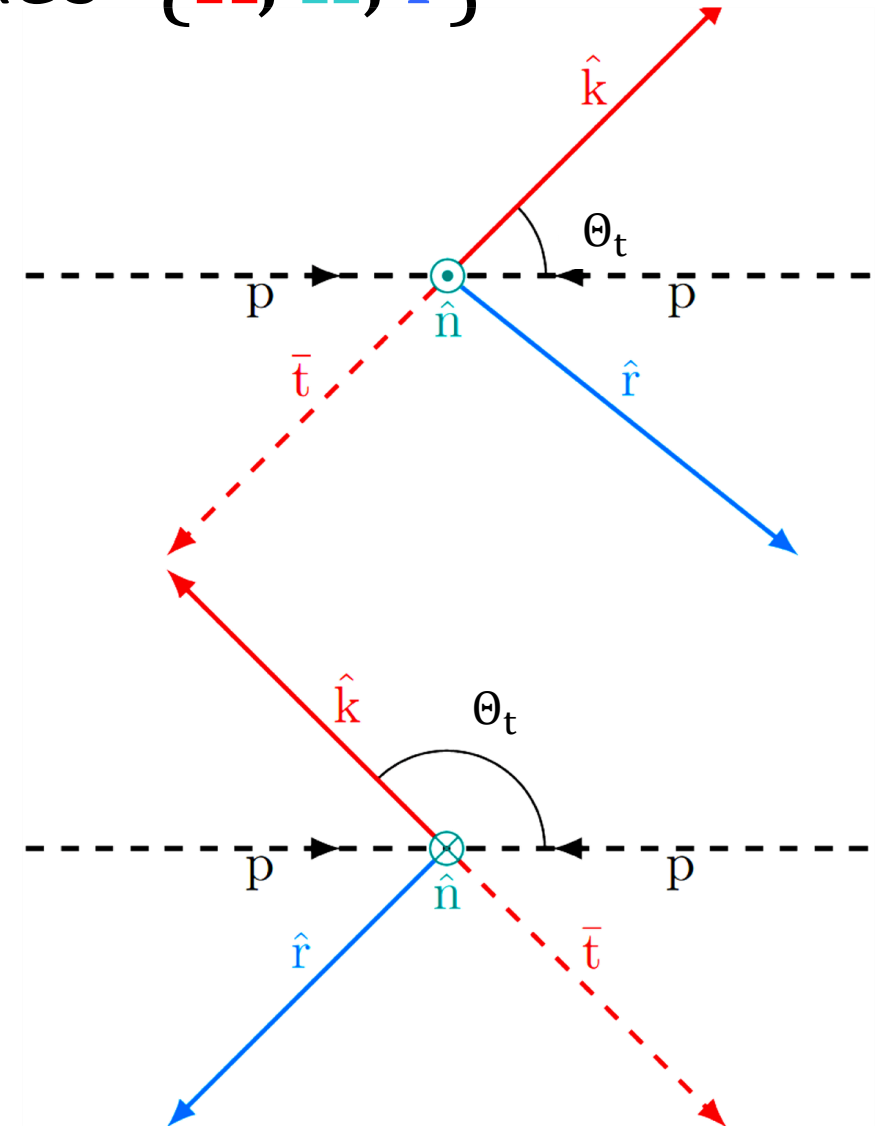
- Helicity $\hat{\mathbf{k}}$ -axis: top quark direction in $t\bar{t}$ rest frame
- Transverse $\hat{\mathbf{n}}$ -axis: transverse to production plane

$$\hat{\mathbf{n}} = \frac{\text{sign}(\cos \Theta_t)}{\sin \Theta_t} (\hat{\mathbf{p}} \times \hat{\mathbf{k}})$$

- $\hat{\mathbf{r}}$ -axis: orthogonal to the other two axes

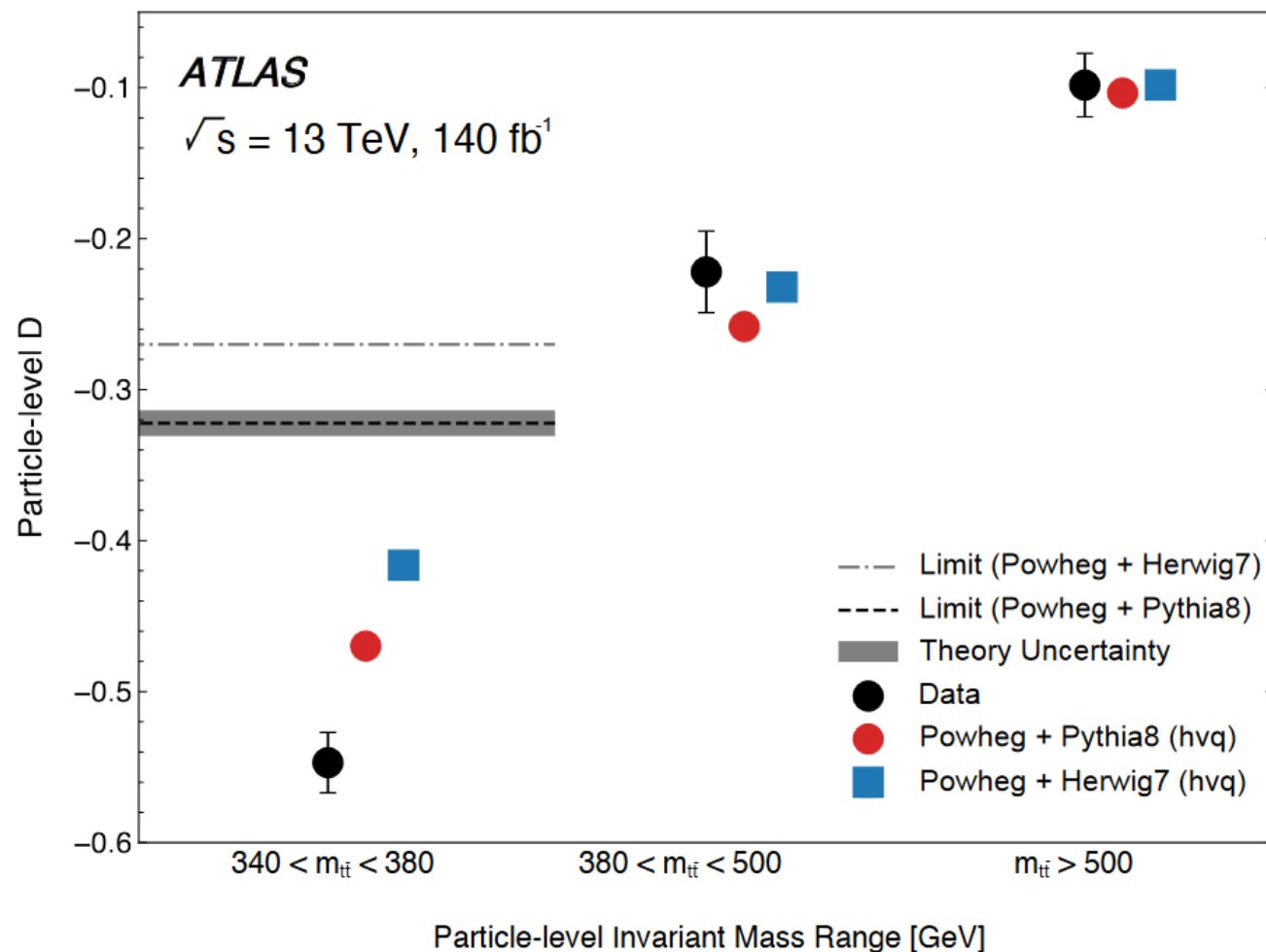
$$\hat{\mathbf{r}} = \frac{\text{sign}(\cos \Theta_t)}{\sin \Theta_t} (\hat{\mathbf{p}} - \hat{\mathbf{k}} \cos \Theta_t)$$

- $\hat{\mathbf{p}}$: direction of the incoming parton, i.e. the direction of the proton beam (z-direction in the laboratory frame)
- Θ_t : top quark scattering angle in $t\bar{t}$ rest frame



ATLAS top quark pair entanglement

- **ATLAS** observed entanglement last fall [[arXiv:2311.07288](https://arxiv.org/abs/2311.07288)]
- Significant differences to **CMS**
 - Calibrated results & entanglement boundary to particle-level
 - No **toponium** or electroweak corrections included in threshold treatment



Electroweak Corrections

- NLO EWK differential cross-section calculated using Hathor
- LO QCD for uncertainty generated with MadGraph5
- Uncertainty in EWK correction is taken as difference between multiplicative and additive approaches

$$\kappa_{NLO}^{EWK}(m_{t\bar{t}}, \cos\theta^*) = \frac{\left. \frac{d\sigma(m_{t\bar{t}})^{EWK}}{d\cos\theta} \right|_{NLO} \Big|_{\cos\theta^*} + \left. \frac{d\sigma(m_{t\bar{t}})^{QCD}}{d\cos\theta} \right|_{LO} \Big|_{\cos\theta^*}}{\left. \frac{d\sigma(m_{t\bar{t}})^{QCD}}{d\cos\theta} \right|_{LO} \Big|_{\cos\theta^*}}$$

$$n_{bin}^{NLO\ QCD \times EWK} = \kappa_{NLO}^{EWK} n_{bin}^{POWHEG}$$

$$n_{bin}^{NLO\ QCD+EWK} = n_{bin}^{LO\ QCD} + n_{bin}^{NLO\ QCD} + n_{bin}^{NLO\ EWK}$$

Electroweak Corrections

- Scale factors used to correct Powheg NLO MC
- Use generator level $m(t\bar{t})$ and $\cos(\theta)$ to look-up scale factor per event

