

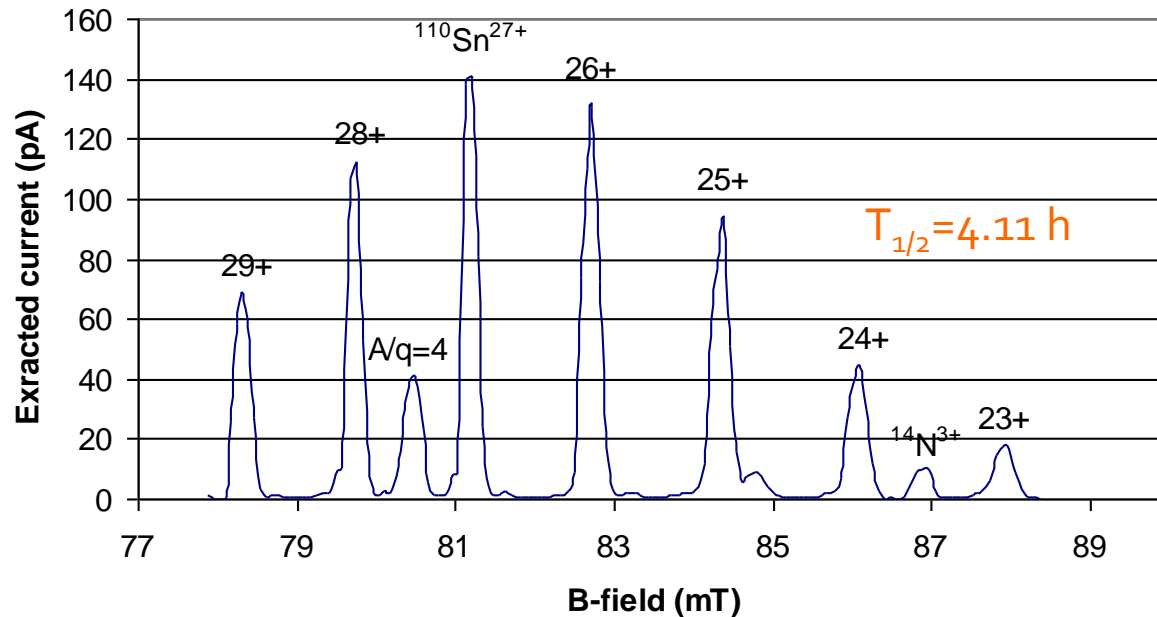
Charge breeding

aka

Charge state boosting

aka

$1+ \rightarrow n+$ transformation



Fredrik
Wenander



BE/CERN



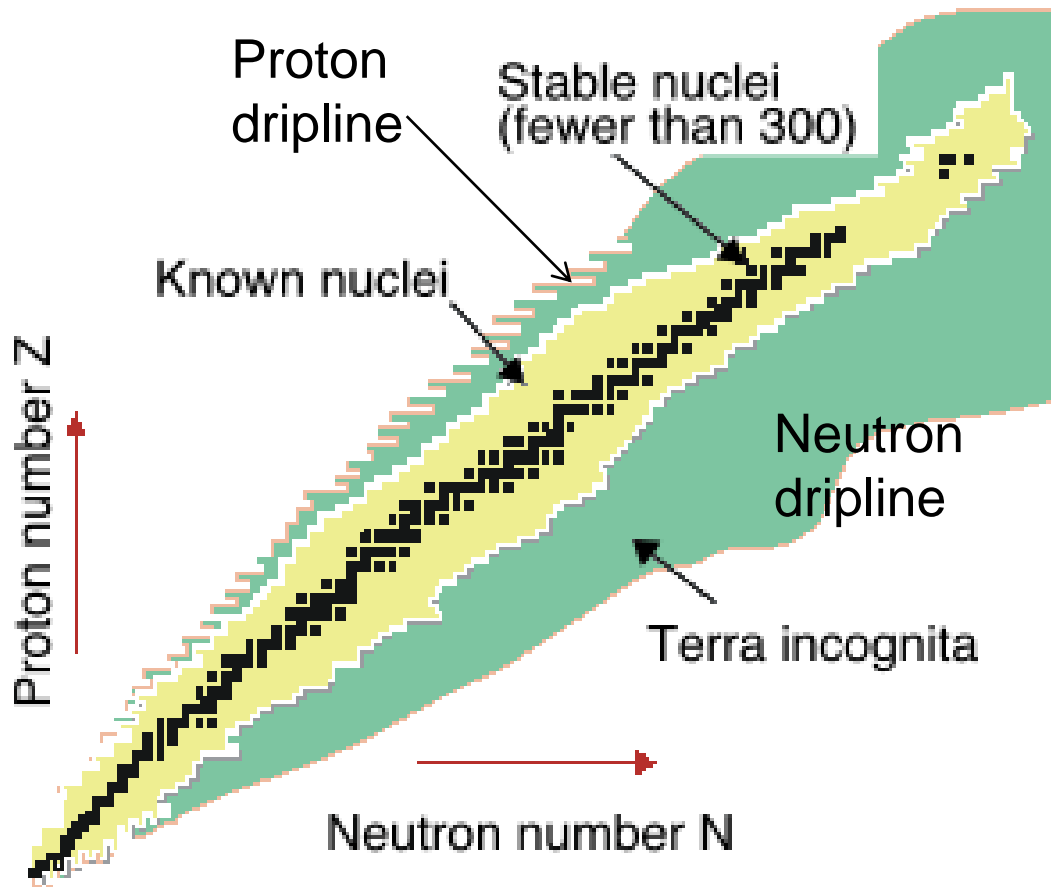
on Ion Sources, Senec Slovakia, 2012

Lecture layout

1. Introduction and motivation
2. ISOL beam parameters and breeder criteria
3. Atomic physics processes for multiply charged ions
4. The different concepts
 - Stripping
 - ECRIS
 - EBIS
5. Preparatory devices and tricks
6. Facilities and the future

Introduction and motivation

Setting the stage



Potential beams

To this date:

~6000 nuclei believed to 'exist'

~3000 different nuclides

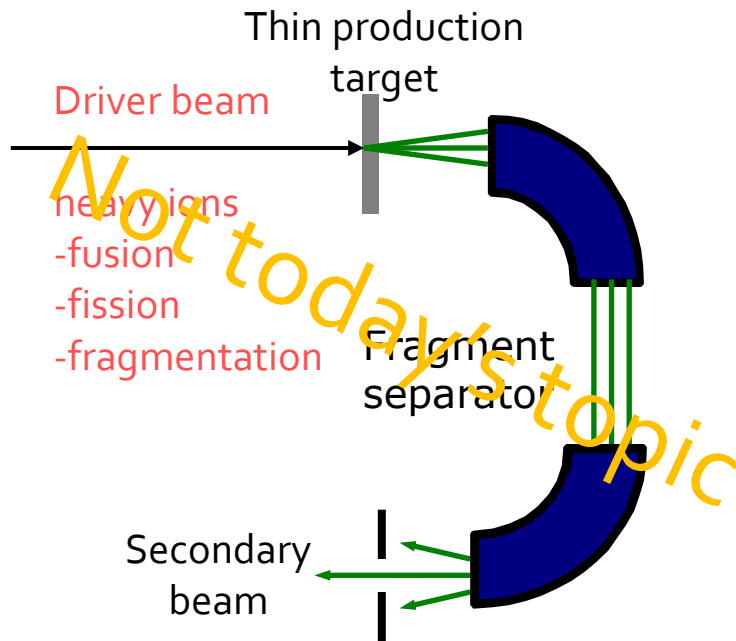
experimentally observed

Less than 10% stable

Radioactive nuclei: main interest for nuclear physics

RIB production techniques

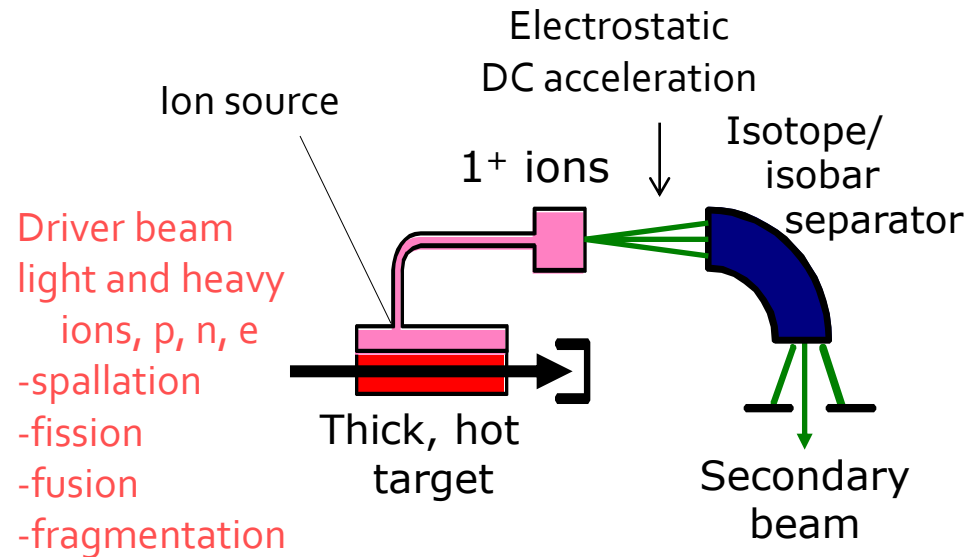
IF (In-Flight fragment separator)



Not today's topic

- Down to us lifetimes
- Large transverse emittance
- Large energy spread
- GeV beam energy

Isotope Separation Online (ISOL)



- Pencil-like beams
- Chemistry involved
- Higher beam intensities than IF
- Lifetimes > 10 ms
- $W_{total} < 100 \text{ keV}$

Interesting physics at 0.1 – 10 MeV/u

- Coulomb excitation
- Few-particle transfer
 - (d,p) , $({}^9\text{Be}, 2\alpha)$, $({}^{10}\text{Be}, 2\alpha)$, (p,γ) , $(p,p)_{\text{res}} \dots$
- Fusion reactions at the Coulomb barrier

NB! $W_{\text{kin}}(\text{total}) = \text{MeV/u} * A$

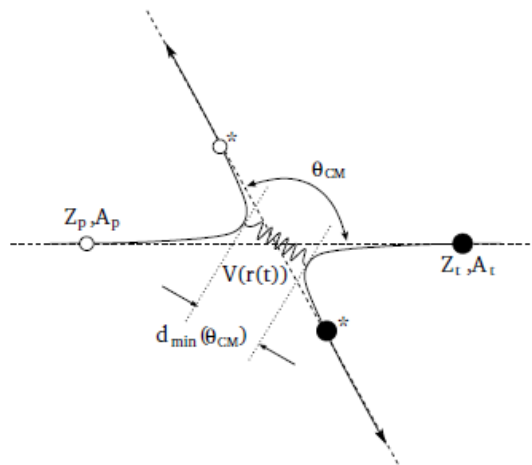
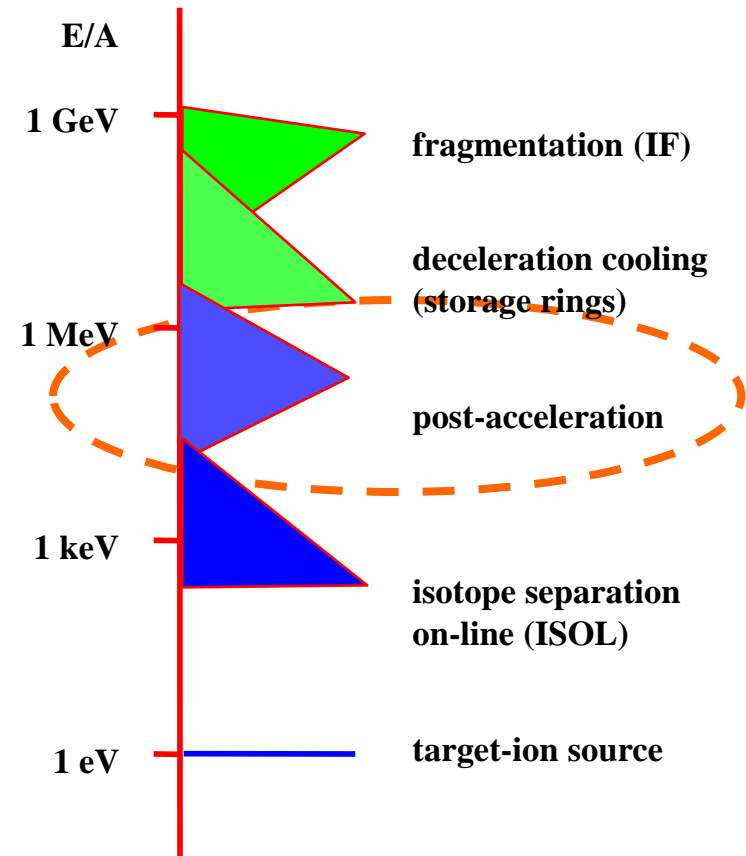


Figure 3.22: Schematic diagram of the Coulomb excitation process of a projectile nucleus (Z_p, A_p) , scattering inelastically on a target nucleus (Z_t, A_t) , in the center-of-mass system.

Closing the energy gap

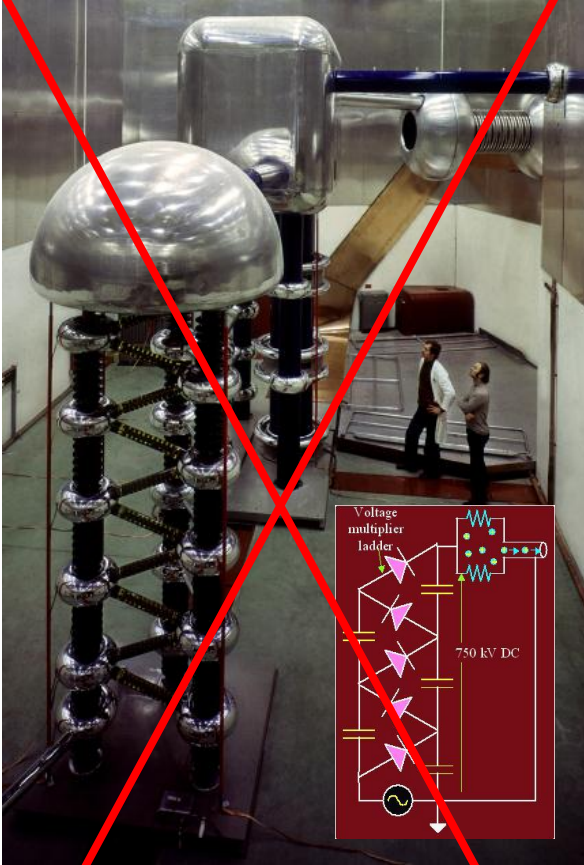


! Fill with *post-accelerated* ISOL-beams

Motivation for Q^+

1st motive for high Q

	W_{final} (MeV/u)	Time structure
Cyclotron	$K^*(Q/A)^2$	cw (micro structure)
$K \sim (Br)^2$, $[B]=T$, $[r]=m$ (cyclotron B-field and radius)		



Old 750 kV Cockcroft-Walton
proton source at CERN

$\Rightarrow 0.015$ MeV/u for $A=50$

2nd motive for high Q

If A/Q high => require low f_{RF} to achieve adequate :

- transverse focusing (focal strength $\sim 1/\sqrt{f_{RF}}$)
- period length (L_{period}) of the first RF structure as the source extraction velocity is limited

Extra

Example: $A=220$, $Q=1$, $U_{\text{extr}}=100$ kV, $L_{\text{period}}=2$ cm

$$v_{\text{extr}} = \sqrt{\frac{2U_{\text{extr}} Q e}{A u}} = 3E5 \text{ m/s}$$

$$f_{RF} \sim v_{\text{extr}}/L_{\text{gap}} = 15 \text{ MHz}$$

Motivation for Q⁺

open RFQ

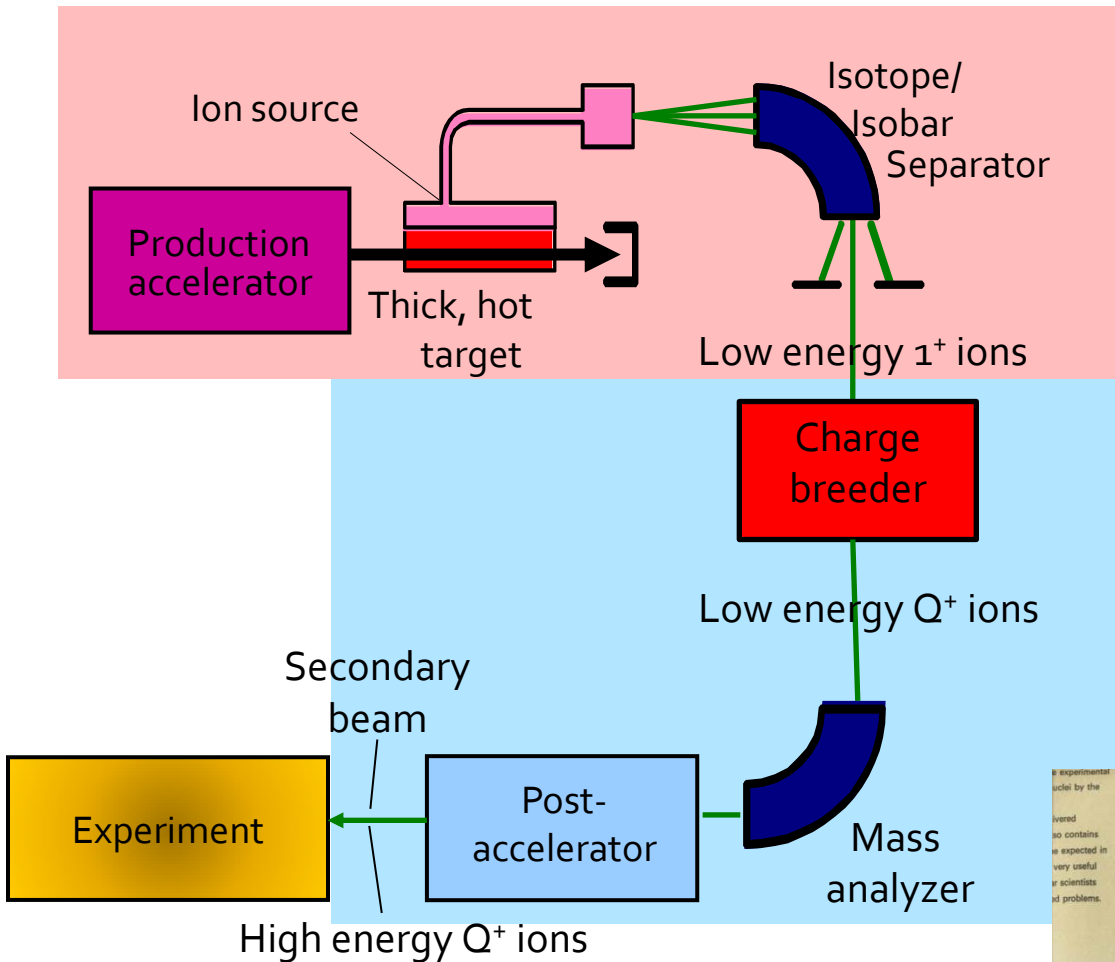


ISAC 35 MHz RFQ for $A/Q < 30$

Transverse tank dimensions scale with $1/f_{RF}$

Bottom line: low A/Q => + short linac
+ small transverse dimension

$$\text{Linac cost} \sim \text{length} * \text{radius}^p \quad 1 < p < 2$$

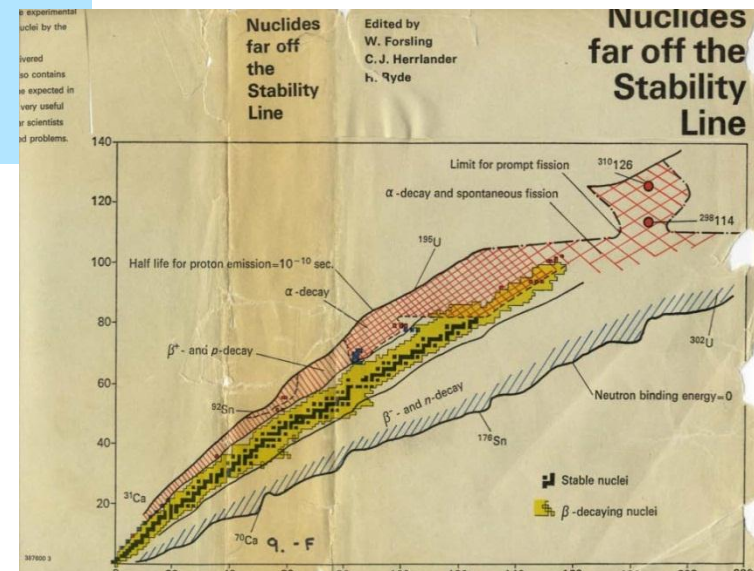


Post accelerator layout

Isotope Separation Online

Post accelerator

First ideas/suggestions for post-acceleration of radioactive ion beams: "Nuclides far off the Stability Line" (1966) Sweden



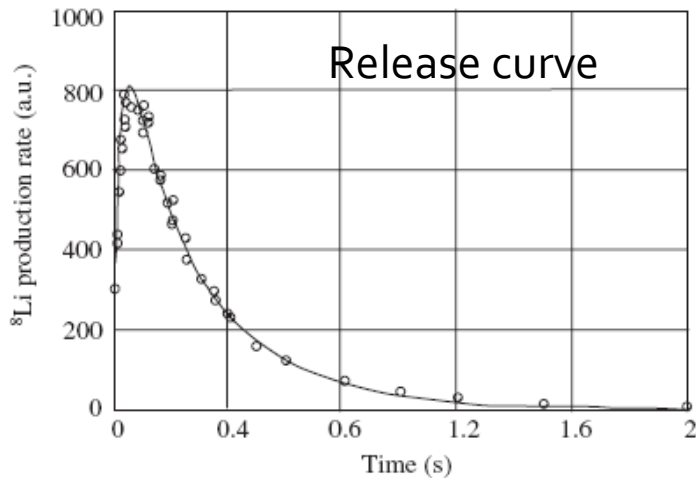
ISOL beam parameters and breeder criteria

What comes in and goes out

*For ion source details
see T. Stora's lecture*

ISOL beam parameters

Ion mass	4 to >250	He to >U
Intensity	few to >1E11 ions/s	Large dynamic range
Charge	1+	Some (undesired) 2 ⁺ , 3 ⁺ , ...
Energy	several tens keV	
Energy spread	few eV	
Temporal structure	cw or quasi-cw	Driver beam – cw or pulsed



⁸Li (T_{1/2} = 840 ms) produced by target fragmentation of tantalum foils

at CERN period time = n*1.2 s

Extra

$$P(t, \lambda_r, \lambda_f, \lambda_s, \alpha) = \frac{(1 - e^{-\lambda_r t})}{Norm} \left[\alpha e^{-\lambda_f t} + (1 - \alpha) e^{-\lambda_s t} \right]$$

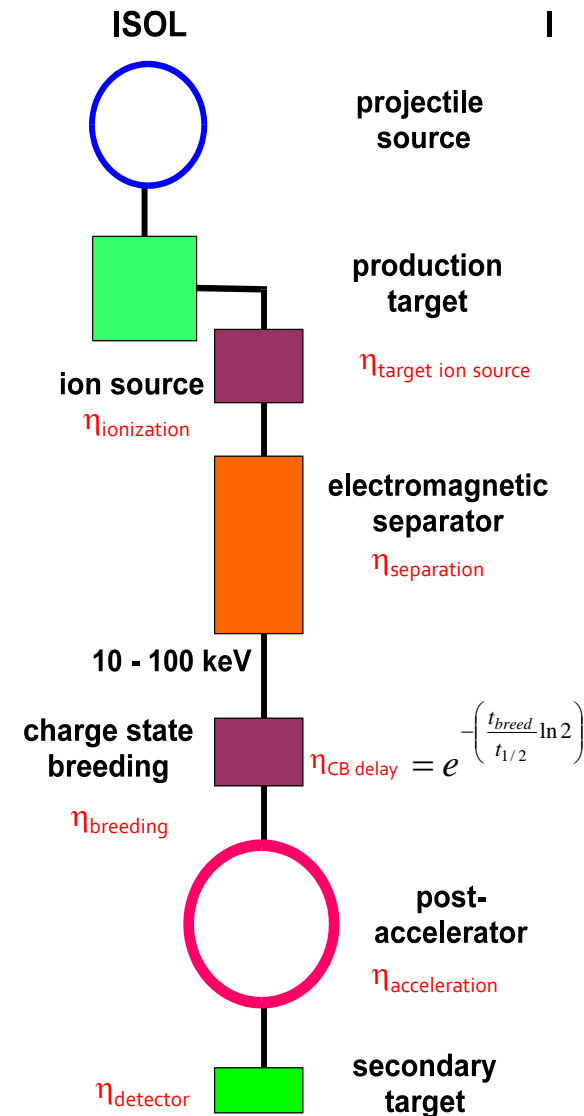
Semi-continuous

depending on release properties and ionization time
typical tens ms to minutes
(r=rise, f=fast, s=slow)

Checklist for breeder design

0	Achievable A/Q (3<A/Q<9)
1	High breeding efficiency rare radionuclides limit machine contamination chain of machines $\eta_{breed} = \frac{I(Q)}{Q \cdot I(1^+)}$
2	Short breeding / confinement time handle short-lived ions
3	Clean extracted beams
4	High ion throughput capacity
5	Good beam-quality (large α , small ϵ_{trans} , small ΔE_{extr}) good trapping efficiency high linac/separator transmission η good mass separation
6	Pulsed or cw machine / beam extraction time structure dependent on accelerator
7	Easy handling and reliable to be used in an accelerator chain on a production basis

Breeder criteria



Atomic physics processes for multiply charged ions

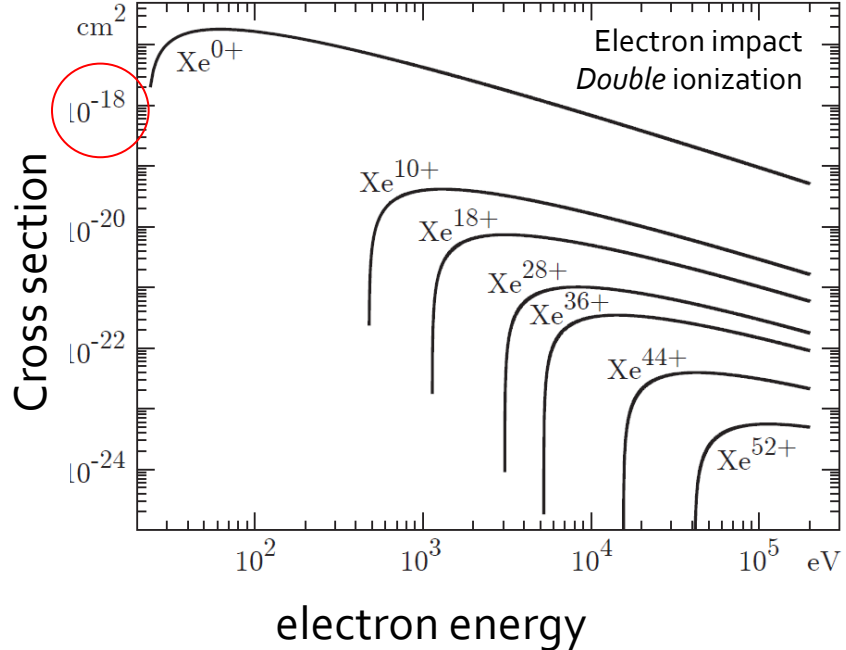
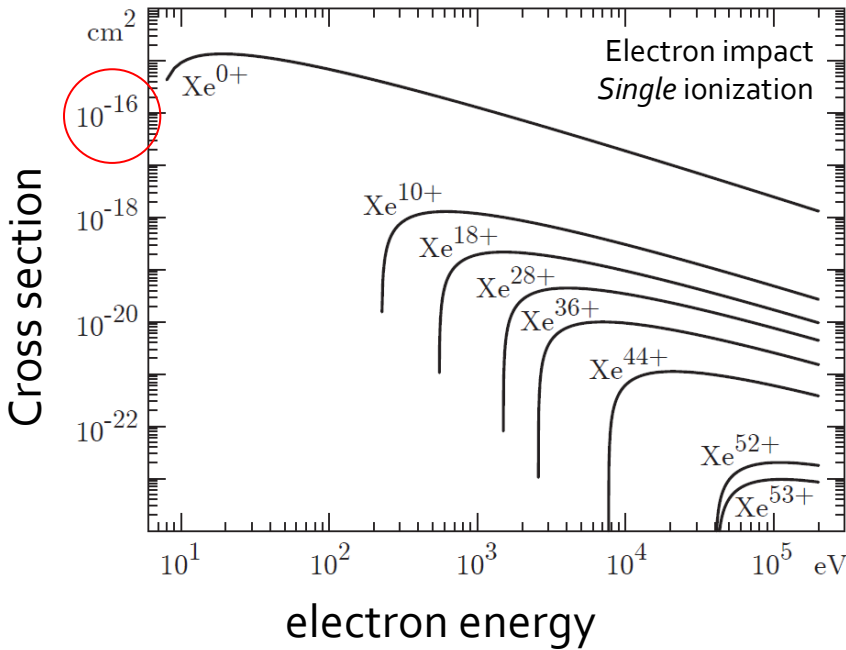
Short revision

*See also lectures by
M. Kowalska and G. Zschornack*

Ionization process

Electron impact ionization

more efficient than proton and photon impact $h\nu$



Multistep (successive) ionization
the process takes time



Ionization time has to be shorter than lingering time in the source

Ionization time

Average time to reach the charge state q with multistep ionization for electrons with *defined kinetic energy*:

$$\bar{\tau}_q = \sum_{i=1}^{q-1} \bar{\tau}_{i \rightarrow i+1} = \frac{e}{j_e} \sum_{i=1}^{q-1} \frac{1}{\sigma_{i \rightarrow i+1}}$$

Lotz's semi-empirical electron impact ionization cross-section formula for the case of high ionization energies $E_{kin} > P_i$ is:

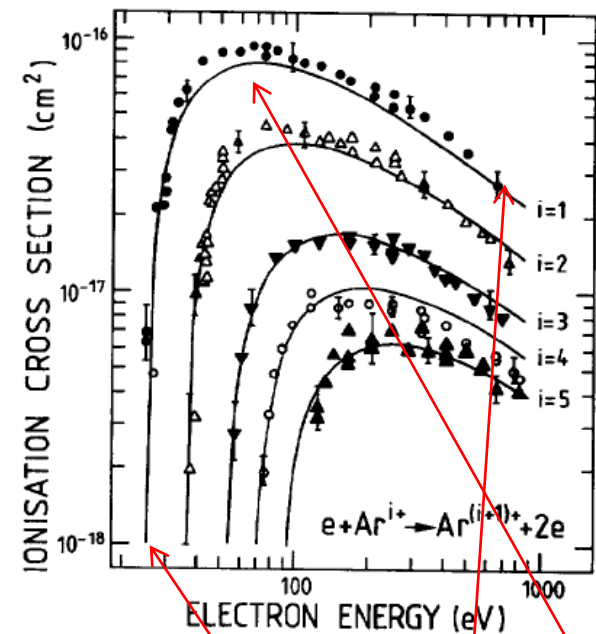
$$\sigma_{q \rightarrow q+1} = 4.5 \cdot 10^{-14} \cdot \sum_{nl} \frac{\ln\left(\frac{E_{kin}}{P_i}\right)}{E_{kin} \cdot P_i} \quad [\text{cm}^2]$$

Energies in eV and nl sum over n shell and subshell l

E_{kin} - energy of the incident electron

$P_i = E_{nl}$ - binding energy

σ – single ionization cross-section cm^2
 j_e – electron current density A/cm^2
 valid for electrons with fixed energy



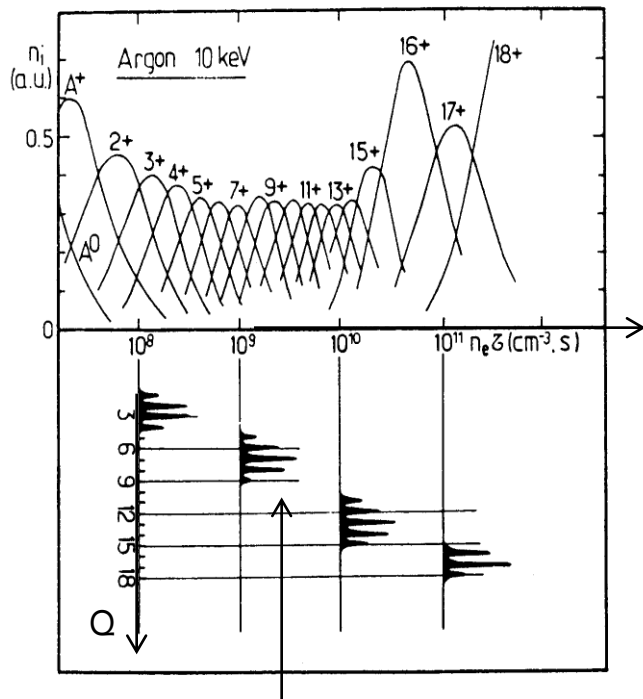
Cross-section

- * Energy threshold = ionization energy
- * Max at ~ 2.7 times the ionization potential
- * Decreases with charge state for very high electron energies

Charge state distribution

Ionization a statistical process
 \Rightarrow charge state distribution

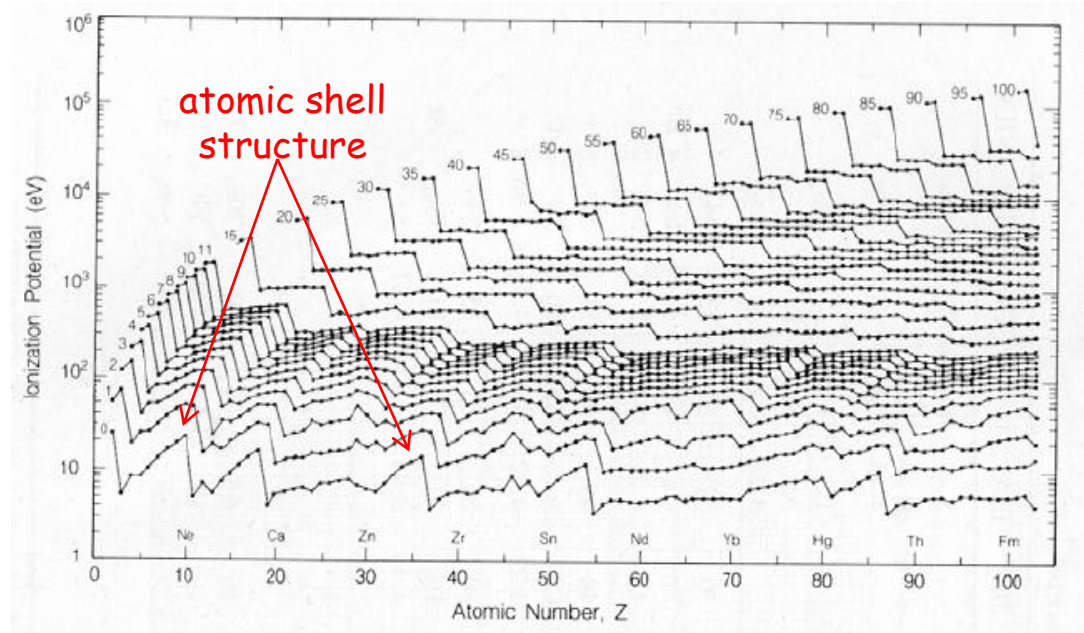
Typically 15-25% in most abundant state



Charge state distribution as function of $n_e * T_{\text{confinement}}$

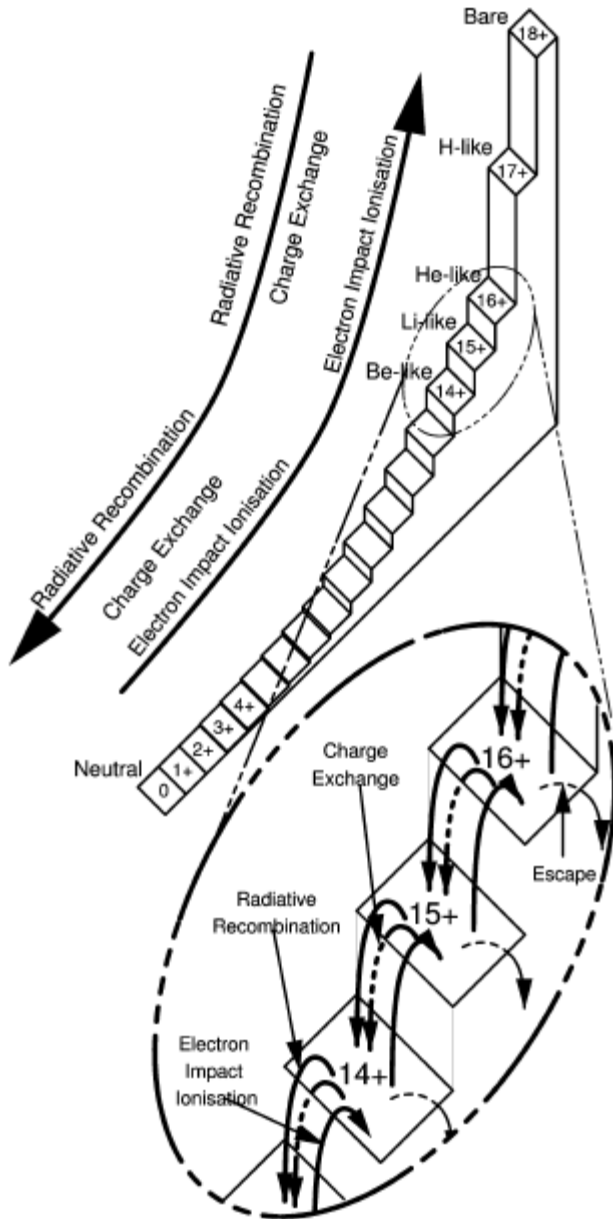
Electron energy

10 to 40 eV for singly charge ions
 several 100 eV for multi-charged states
 keV to tens of keV for highly charged ions



Competing processes

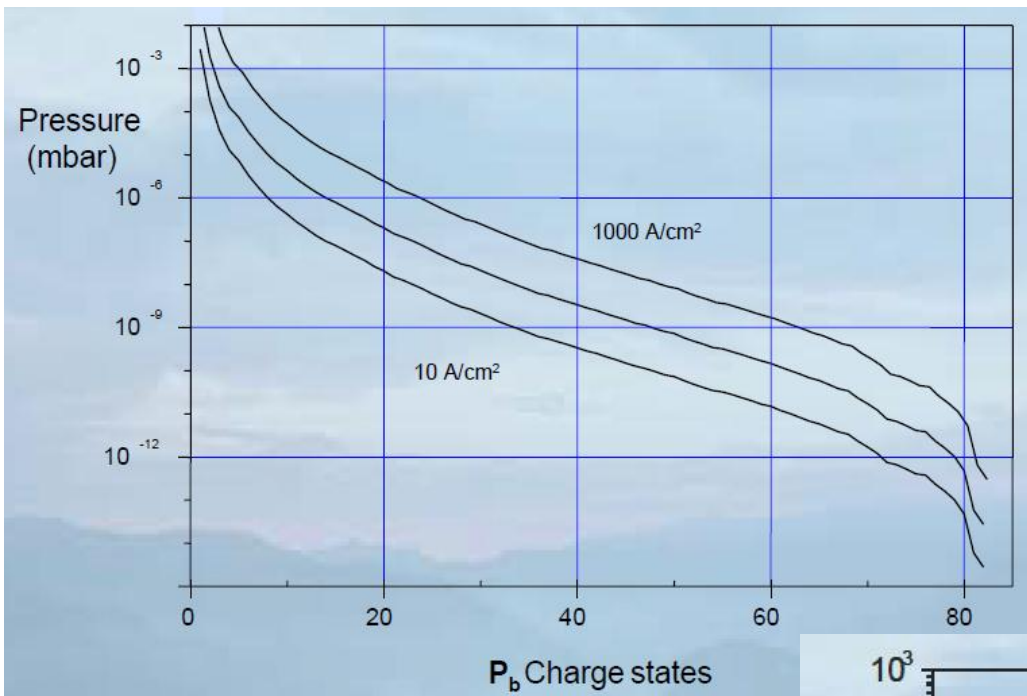
$$\frac{dN_i}{dt} = n_e v_e [\sigma_{i-1 \rightarrow i}^{EI} N_{i-1} - (\sigma_{i \rightarrow i+1}^{EI} + \sigma_{i \rightarrow i-1}^{RR} + \sigma_{i \rightarrow i-1}^{DR}) N_i + (\sigma_{i+1 \rightarrow i}^{RR} + \sigma_{i+1 \rightarrow i}^{DR}) N_{i+1}] - n_0 v_{ion} [\sigma_{i \rightarrow i-1}^{CX} N_i - \sigma_{i+1 \rightarrow i}^{CX} N_{i+1}] - N_i R_i^{ESC}$$



N_i – number of ions with charge i
 n_e, v_e – electron density and velocity
 n_0 – neutral particle density
 $v_{ion} = \sqrt{2kT_{ion} / M_{ion}}$ – averaged ion velocity

EI – electronic ionization
 RR – radiative recombination
 DR – dielectronic recombination
 CX – charge exchange
 R_i^{ESC} – escape rate

See also AIP Conf. Proc. 572, 119 (2001)



Charge exchange vs ionization

Vacuum pressure at which gain by ionization equals loss by charge exchange for lead ions

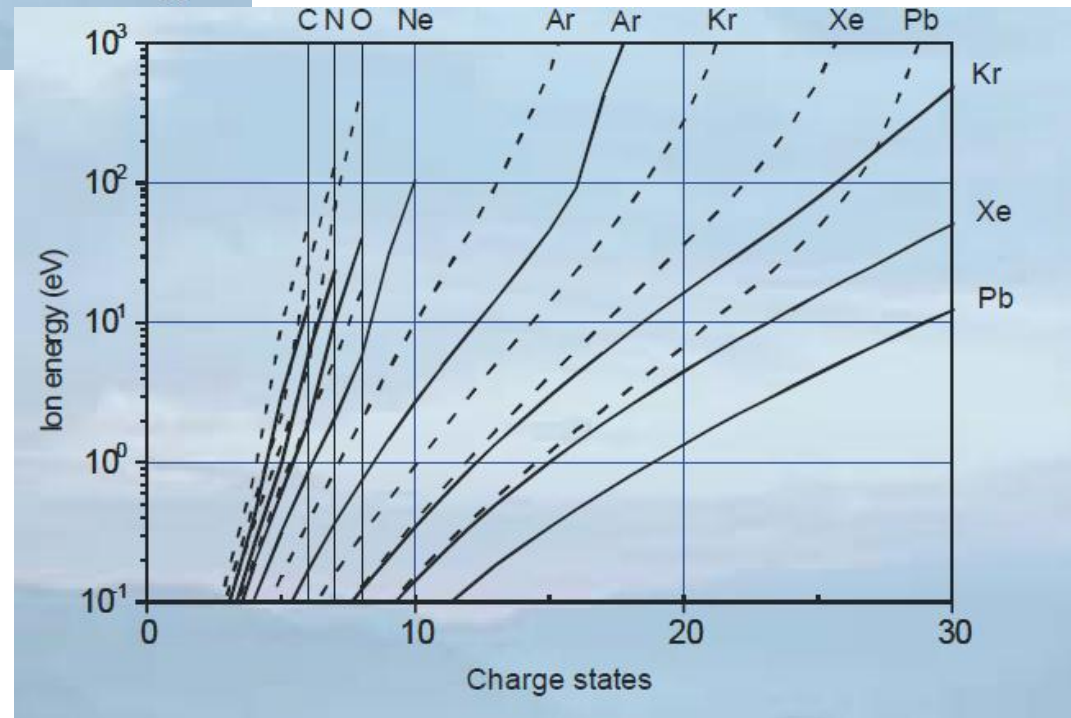
From R. Becker

Electron ion heating

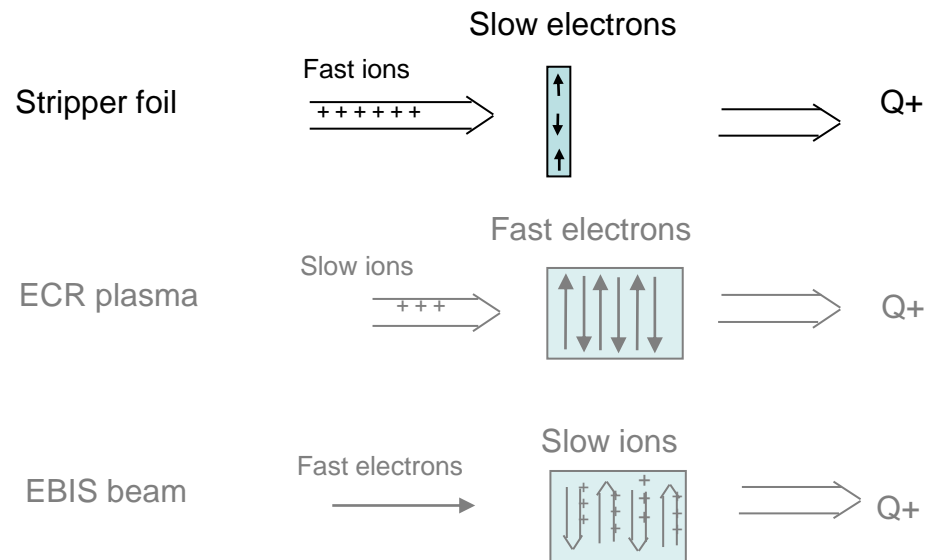
Radial well voltages $eU_{\text{trap}} = kT_{\text{ion}}$ to trap multiply charged ions heated by electrons of 1 keV (dashed line) and 10 keV (full lines)

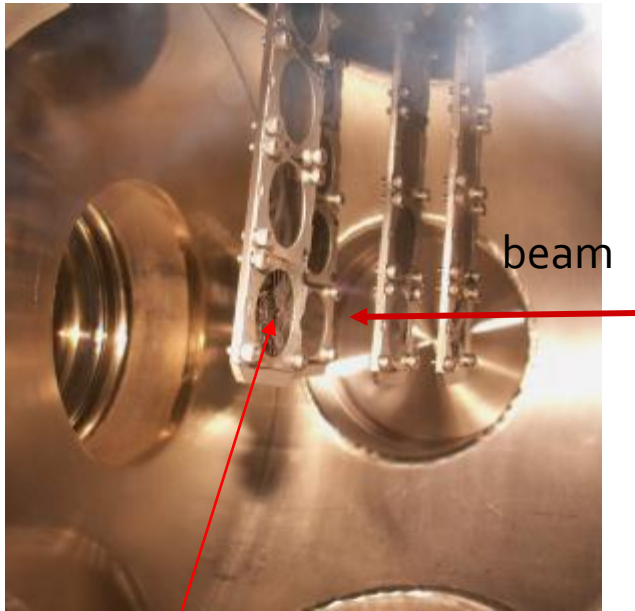
$$\Delta U_{\text{radial}} [\text{V}] = \frac{6.2}{Z \cdot A} e \sum_{i=1}^q \frac{i^2}{\sigma_{i \rightarrow i+1}^{\text{ionization}}}$$

See R. Becker, Proc 3rd EBIS Workshop 1985, Ithaca, eds. V. Kostroun and B.W. Schmieder, p.185



The First Alternative





carbon foils at CERN Linac3

Classic concept – stripping

* Doesn't really classify as charge breeder

- + Simple method, passive elements.
- + Sub-us half-life isotopes easily reachable
- + Very high beam capacity >100 eμA
- + No additional beam contamination

* Foil materials: Be, C, Al, Al₂O₃, mylar

* Bohr criterion: electrons whose orbital velocity is larger than projectile velocity are retained

Baron's formula for equilibrium charge state distribution (CSD)

$$\bar{Q} = Z_{proj} \cdot C_1 \left(1 - C_2 e^{-83.28\beta / Z_{proj}^{0.447}} \right)$$

$C_1 = 1$ for $Z_{proj} < 54$

$C_1 = 1 - \exp(-12.905 + 0.2124Z_{proj} - 0.00122Z_{proj}^2)$ for $Z_{proj} \geq 54$

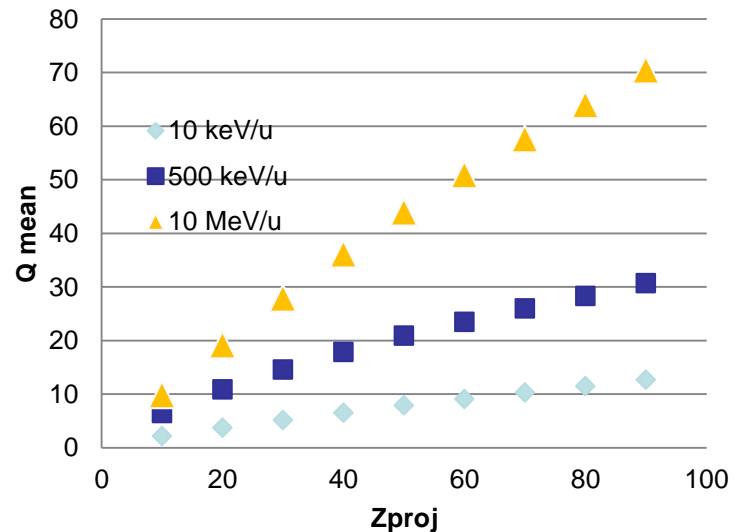
$C_2 = 1$ for energies $W > 1.3$ MeV/u

$C_2 = 0.9 + 0.0769W$ for $W < 1.3$ MeV/u

NB! ~only dependent on velocity

$$v_{proj} = \beta c \text{ and } Z_{proj}$$

Extra



Stripper foil CSD

Gaussian CSD distribution

- * assuming no significant atomic shell effects
- * \bar{Q} is not too close to Z

Extra

$$\sigma = 0.5 \sqrt{\bar{Q} \cdot \left(1 - \left(\frac{\bar{Q}}{Z_{proj}}\right)^{1.67}\right)}$$

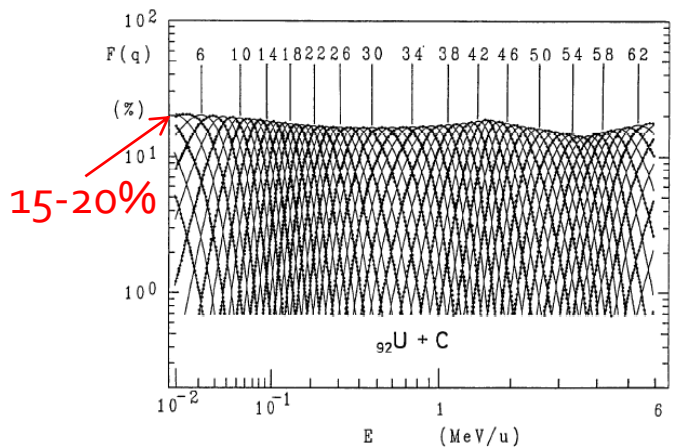
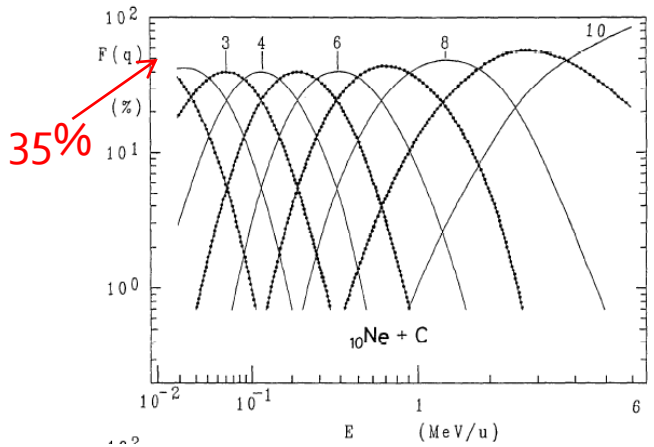
for $Z_{proj} < 54$

$$\sigma = \sqrt{\bar{Q} \cdot \left(0.07535 + 0.19\left(\frac{\bar{Q}}{Z_{proj}}\right) - 0.2657\left(\frac{\bar{Q}}{Z_{proj}}\right)^2\right)}$$

for $Z_{proj} \geq 54$

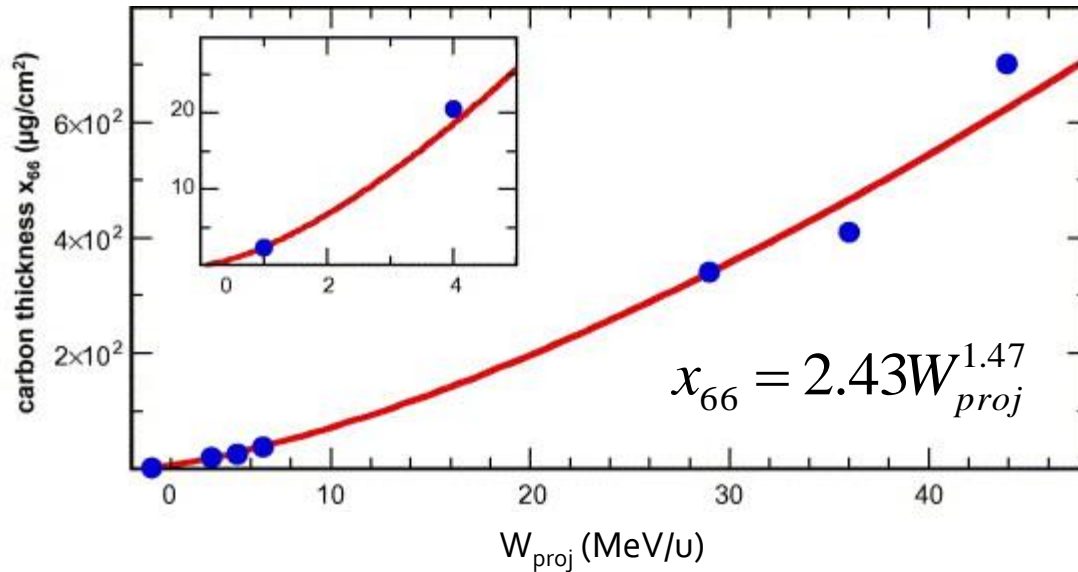
Light elements (low Z_{proj})
 => narrow distribution
 => high fraction in a single charge state

Heavy elements (high Z_{proj})
 => wide distribution
 => less fraction in a single charge state



See also: G. Schiwietz, P.L. Grande, Improved charge-state formulas NIMB 175-177 (2001) 125-131
 Refined formulae for foil and gas stripping

Foil equilibrium thickness



M. Toulemonde, 'Irradiation by swift...', Nucl Instrum Meth B250 (2006) 263-268

Equilibrium thickness =>
CSD do not change when
the target thickness is
further increased

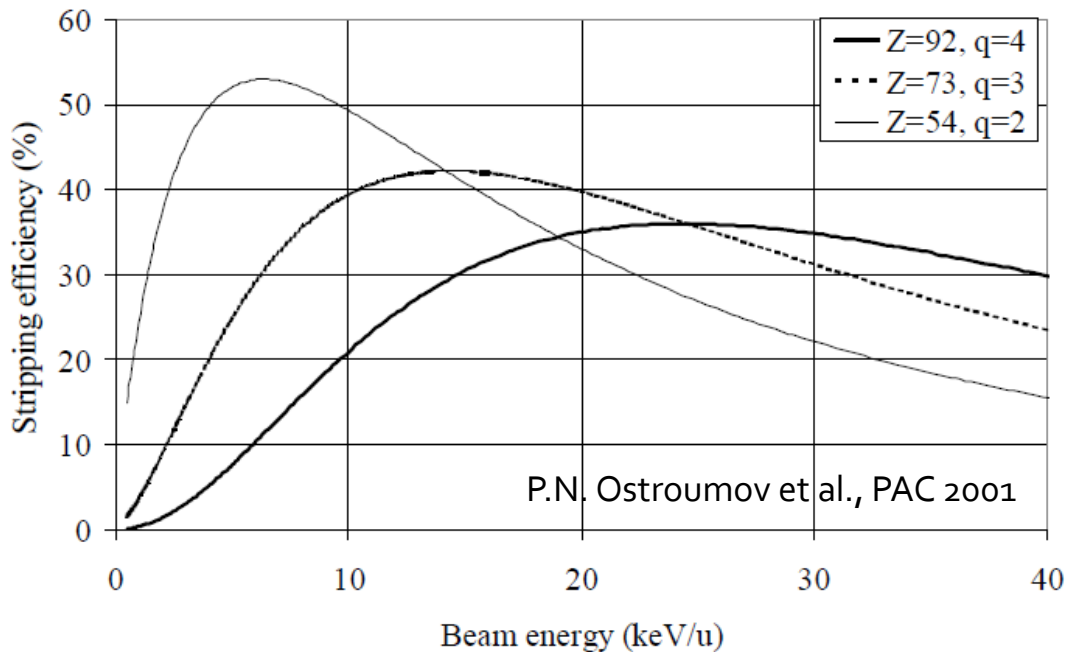
Equilibrium thickness $\approx 2 * x_{66}$

- * Typical carbon foil thicknesses: 5-1000 $\mu\text{g}/\text{cm}^2$ -> 25 nm to 5 μm
- * Pre-acceleration to >500 keV/u
- * Foil thicknesses $< 5 \mu\text{g}/\text{cm}^2$ (< 25 nm) practically difficult to mount
=> use gas strippers for low velocity beams

Extra

Gas stripping

- * Used for very low velocity: 5-25 keV/u
- * Very thin integrated thickness: fraction of $\mu\text{g}/\text{cm}^2$
- * Usually noble gases
- * Small charge increase from 1+ to 2+, 3+ or 4+



Helium stripping efficiency of heavy ions as a function of beam energy.

Extra

In solid stripper the collision frequency is larger the frequency of Auger and radiative decays => higher Q than in same integrated thickness for gas stripper

Facility based on stripping technique

Ideally strip as soon the increased velocity enables a higher charge state

+ make maximum use of the accelerating voltage

- but at each stripping stage the transmission is reduced due to the CSD

Example

Bunching efficiency 65%
 Gas stripping to 2+ at 8 keV/u ~55%
 Stripping foil to 23+ at 500 keV/u 20%
 In total (single charge acc of ^{132}Sn) 7%

A bunch rotating rf cavity is mandatory in order to generate a time focus at the stripper to minimise the longitudinal emittance growth due to energy straggling.

Extra

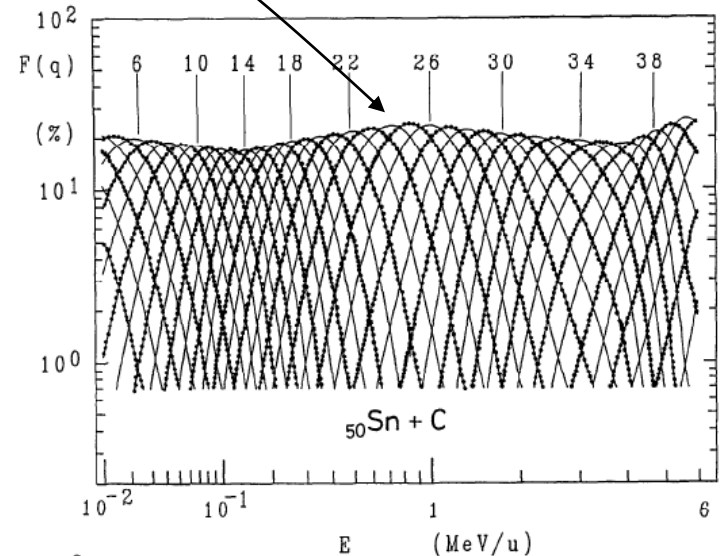
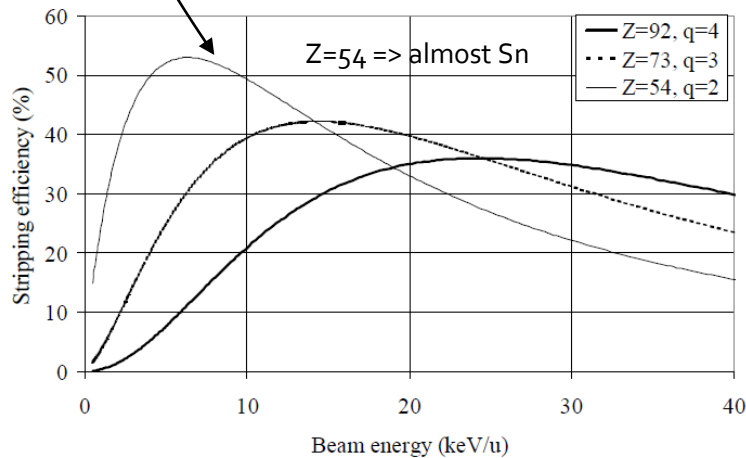
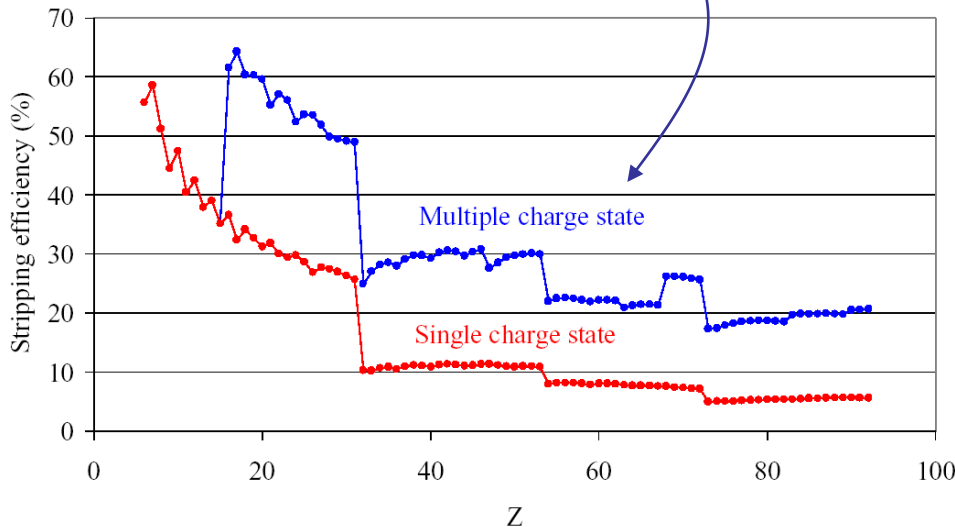


Figure 1: Helium stripping efficiency of heavy ions as a function of beam energy.

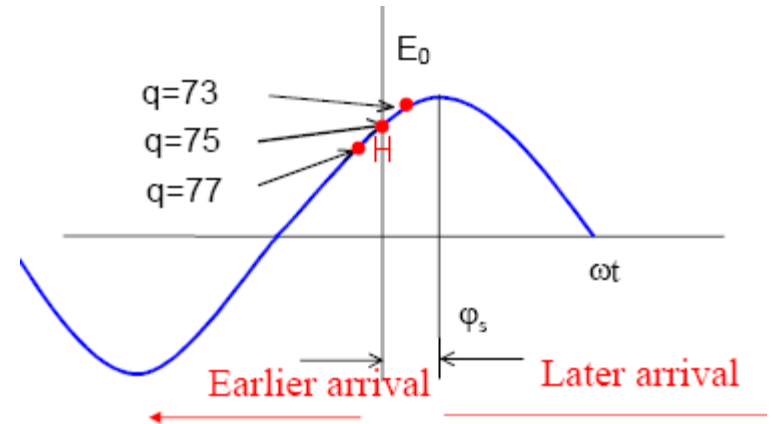
Extra

Multi-charge state acceleration

- * Accelerate multiple q after the stripper
- * $\Delta q/q$ of $\sim 20\%$ can be accepted
- ☺ Higher intensities



MCA and overall stripping efficiency (RIA proposal)



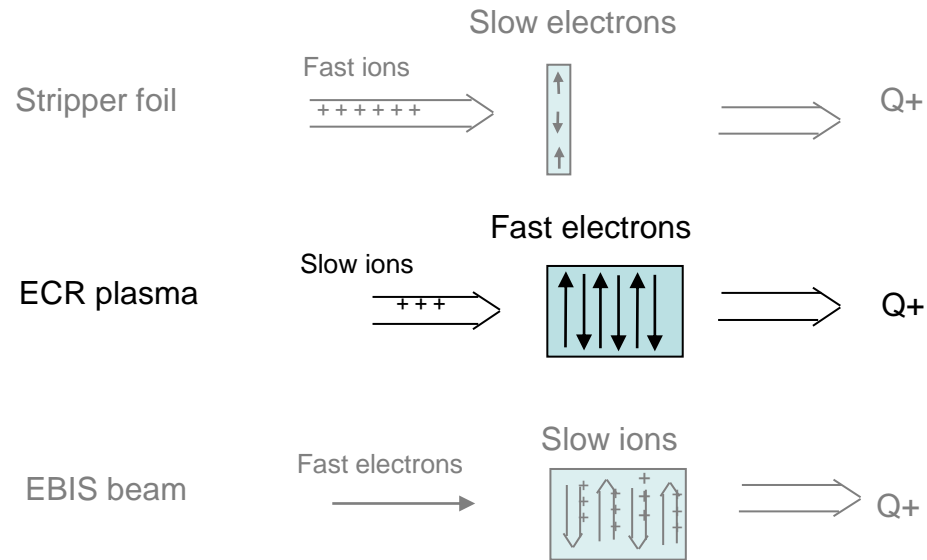
- * Synchronous phase of multi- q beam
- * The same final energy for all charge states

☹ ε (trans. and long.) ~ 3 larger compared with single charge state acceleration

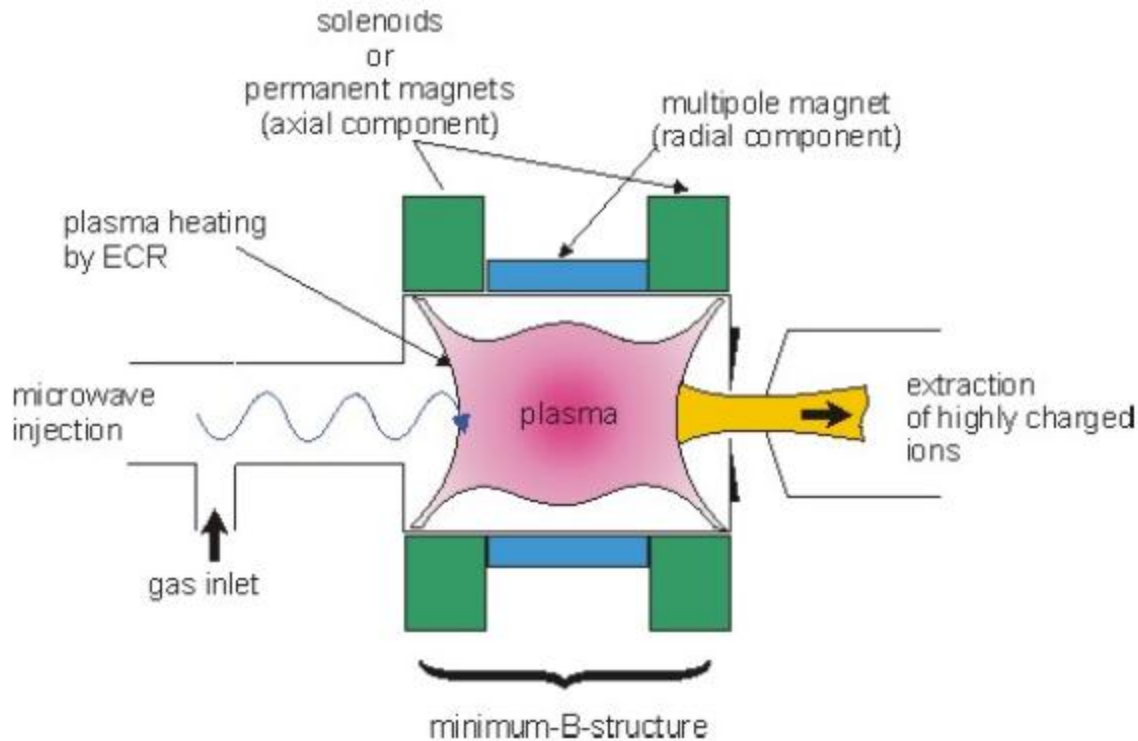
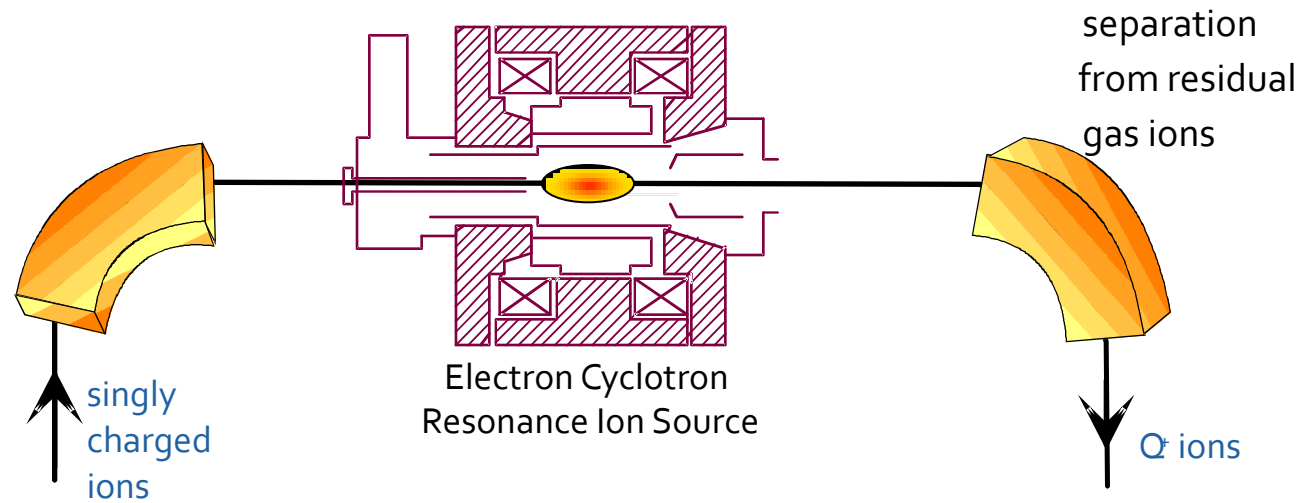
Stripping technique drawbacks

☹ Needs pre-acceleration	in gas stripping 8 to 20 keV/u in foil stripping ~500 keV/u
☹ Emittance increase	Energy straggling Angular straggling $\theta_{T1/2}^2 = \theta_{I1/2}^2 + \theta_{S1/2}^2$ $\mathcal{E}_T = \pi \cdot x_{T1/2} \cdot \theta_{T1/2}$ <p> $x_{T1/2} = x_{I1/2}$ = incident beam spot size $\theta_{T1/2}$ = divergence exiting beam I = Incident, T = traverse, S = Scattering </p>
☹ No macro-bunching capability	=> CW accelerator needed
? Foil lifetime	1. Radiation damage 2. Sublimation at high power levels (>150 W/cm ²) => Not limiting for radioactive beam intensities
☹ Limited efficiency for high-Z elements	

The Second Alternative



ECRIS as charge breeder



General principle

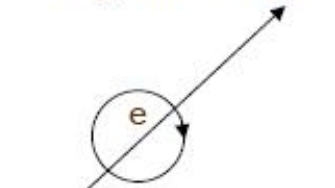
- inject very slow ions through a plasma of hot e^-

$$\omega_e = \frac{e \cdot B}{m} = \omega_{rf}$$

Plasma is resonantly heated with microwaves

ECRIS physics

Magnetic flux line



$$q \cdot v \cdot B = m \cdot \omega^2 \cdot r$$

$$\omega = \frac{v}{r}$$

B= 1T

f=28 GHz

$$r = \frac{m \cdot v}{q \cdot B}$$

$r_{Lamor} = 0.01 \dots 1 \text{ mm}$

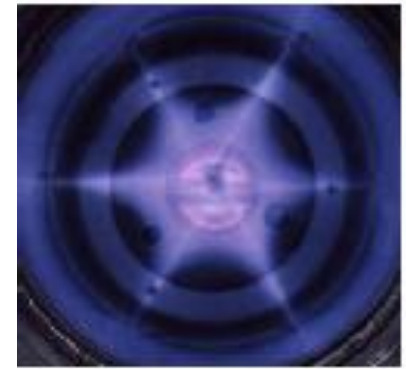
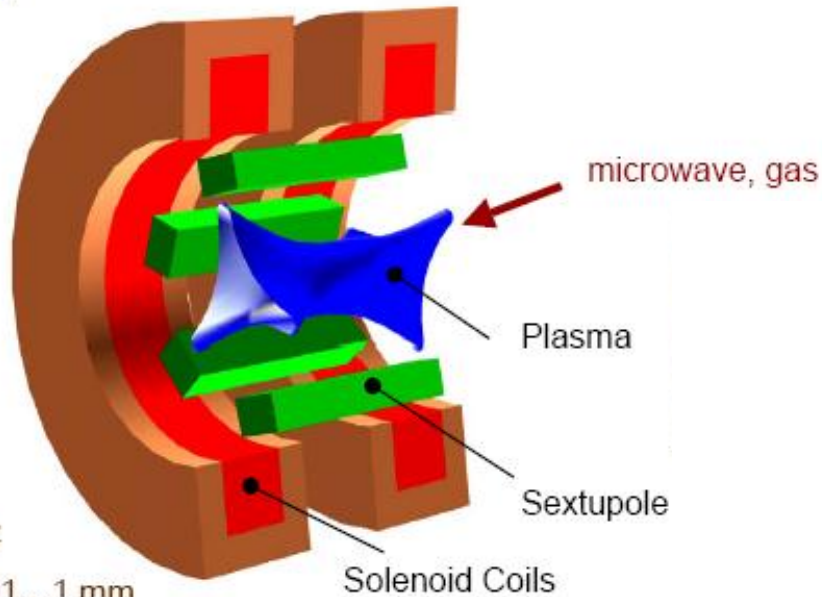


Photo of plasma

'Magnetic bottle' confinement of plasma

- * Longitudinally by Helmholtz coils
- * Radially by powerful permanent multipole
=> min-B field – increases in all directions

e⁻ temperature distributions

Cold <200 eV: lowest confinement time

Warm < 100 keV: ionization process
(main source of bremsstrahlung)

Hot > 100 keV: highly confined

Extra

Electron confinement time:

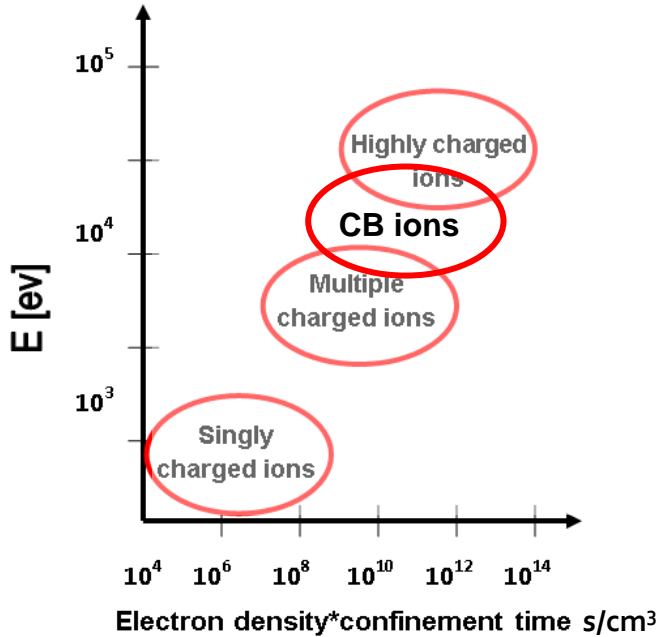
$$\tau_e = \frac{T_e^{3/2}}{n_e} \cdot const$$

What RF is needed?

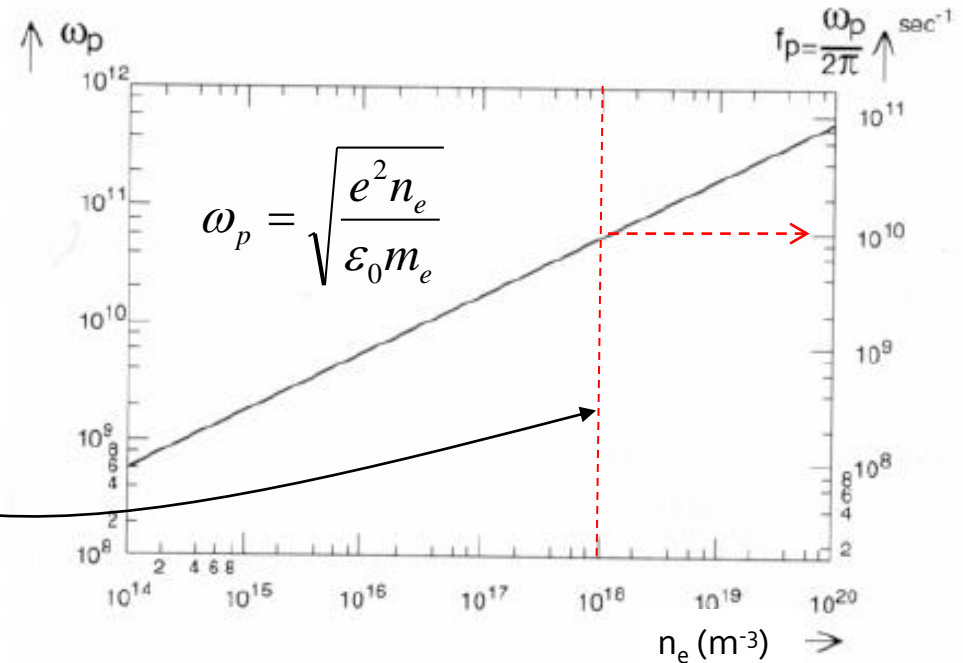
f_{RF} needs to be higher than the plasma frequency f_p (cut-off frequency)

$$n_e < 1.2 \times 10^{10} f_{RF}^2 \text{ cm}^{-3}$$

f_{RF} = in gigahertz



Typical confinement time 0.1 s
 \Rightarrow need $n_e \sim 1 \times 10^{12} \text{ cm}^{-3}$



Plasma frequency versus plasma density

Extra

Compare with stripper foils
 $n_e \sim 1 \times 10^{24} \text{ cm}^{-3}$ inside the foil
 $v_{ion} = 1 \times 10^9 \text{ cm/s}$, $d_{carbon_foil} = 0.5 \text{ um} \Rightarrow$
 $n_e * \tau = 5 \times 10^8 \text{ s/cm}^3$

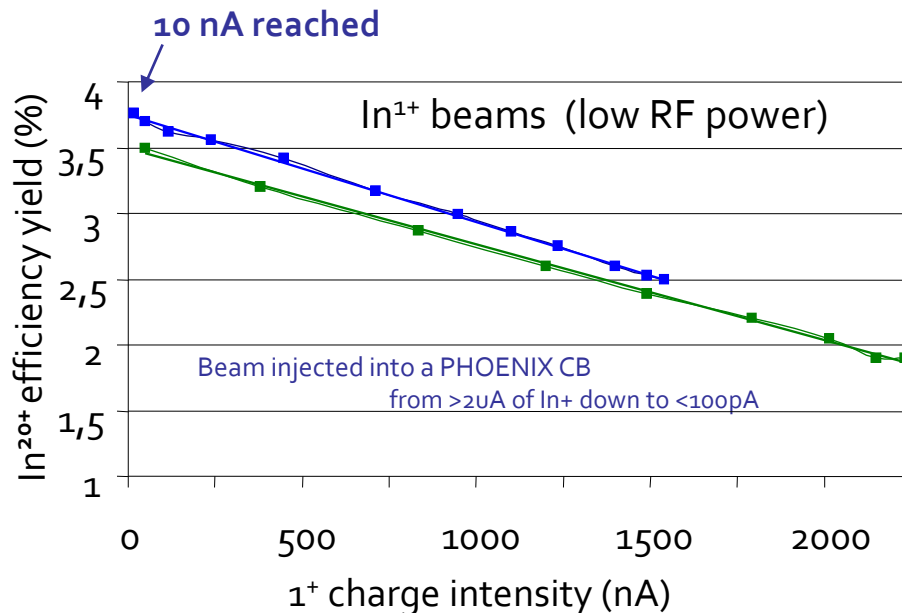
ECRIS capacity

We know $n_e \sim 1E12 \text{ cm}^{-3}$ for charge breeding ECRIS

Assume:

- * plasma volume $r=2 \text{ cm}$, $l=10 \text{ cm}$
- * confinement time 0.1 s
- * 10% radioactive ions
- * 20% in the desired charge state $10+$

=> $2.5E12$ radioactive ions/s extracted (0.4 pA)

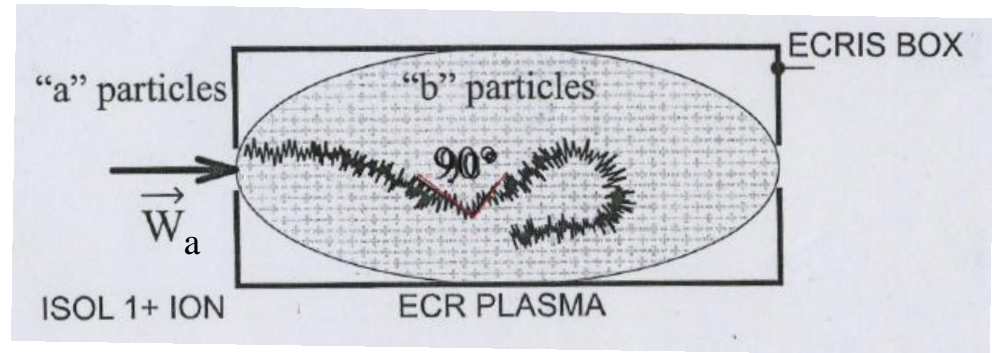


*The large capacity
– a major strength of
the ECRIS CB concept!*

Stopping ions in ECRIS plasma

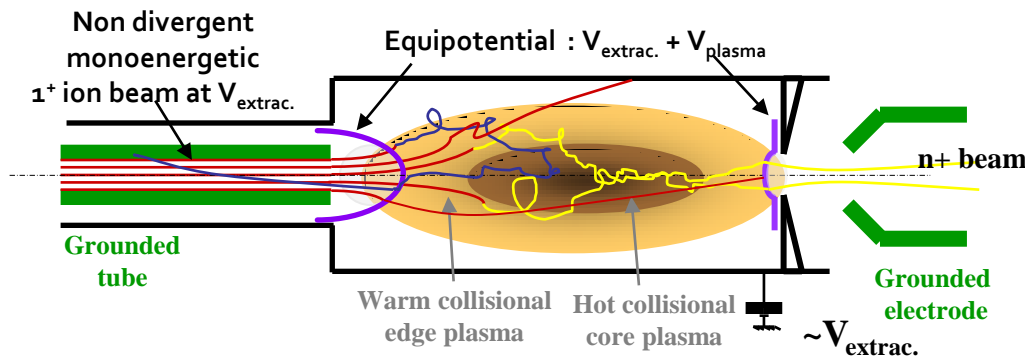
- * Stopping of ions tricky and critical
- * No wall-collision tolerated

- 1st electrostatic slow-down
- 2nd subsequent long-range ion-ion Coulomb collisions lead to 90° deflection*
- 3rd ionized => Ions trapped



* Cumulative deflection due to small-angle scattering is larger than those due to single large-angle scattering (Spitzer/Chandrasekhar theory)

Mean free path for 90° deviation smaller than plasma size?



$$\lambda_{90^\circ} \approx \frac{W_a}{4\pi n_e z_a z_b e^2 \ln \Lambda}$$

Coulomb logarithm

$$W_a = 10 \text{ eV}, z_a = 1, z_b = 10, \ln \Lambda = 10$$

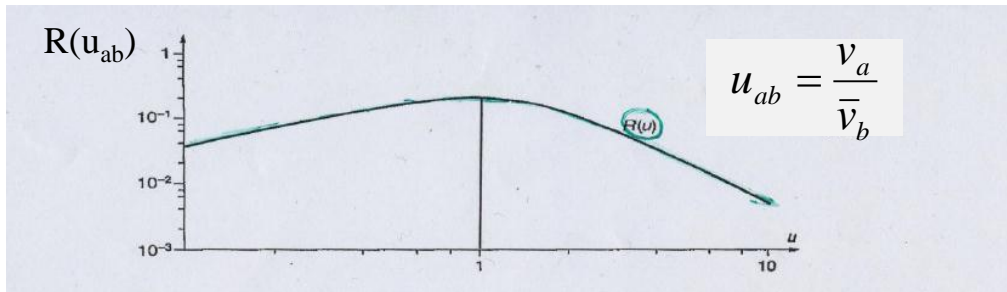
$$\Rightarrow \lambda_{90^\circ} \sim 5 \text{ cm}$$

Injection velocity into ECR plasma

Extra

What is the optimal velocity for stopping inside a plasma?

$$\frac{\Delta v_a}{\Delta t} \sim \frac{n_b}{2\pi\epsilon_0} \left[\frac{Z_a Z_b e^2}{m_a \bar{v}_b} \right]^2 R(u_{ab}) \ln \Lambda$$



Optimal slowing down when:

$$v_{\text{injected particle}} = \langle v \rangle_{\text{plasma particles}}$$

Assumption

1. low intensity of injected particles
2. only interaction via long distance cumulative plasma collisions
3. plasma particles Maxwellian velocity distribution
4. distance between 90° deviations < plasma size

Example

* ECR oxygen plasma $T^+ = 2$ eV

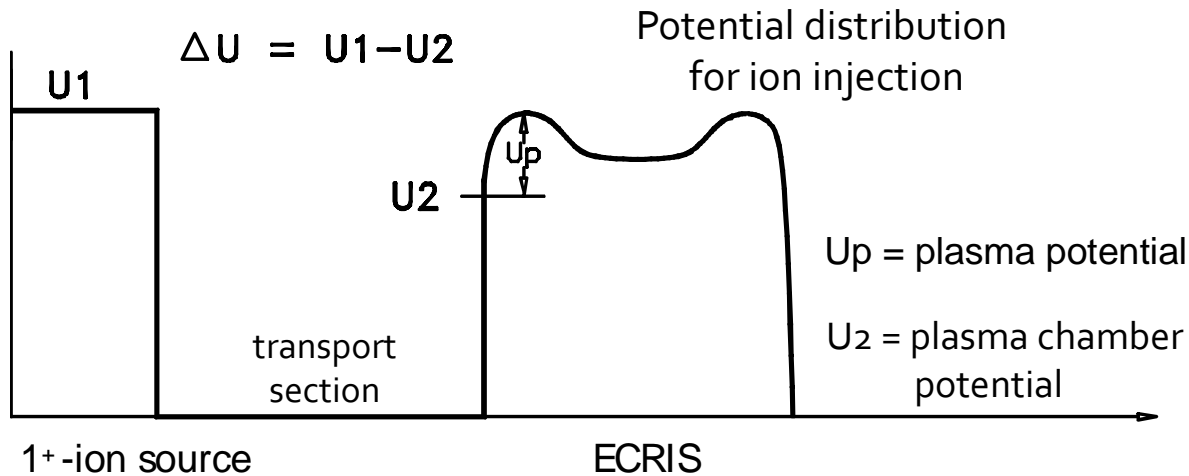
* Rb¹⁺ ISOL ions

$$\Rightarrow E_{\text{inj}}(\text{Rb}^{1+}) \sim 2\text{eV} * m_{\text{Rb}}/m_{\text{O}} \sim 10 \text{ eV}$$

If we'd like to inject ¹¹Li⁺, optimum energy would be <2 eV => difficult

Compatible with previous slide!

Longitudinal acceptance



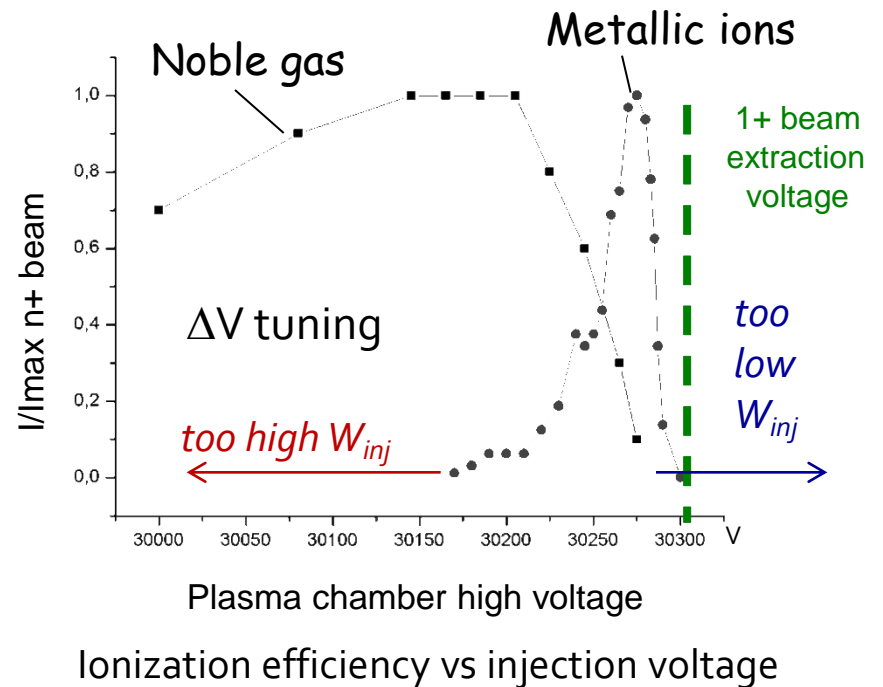
Noble gases
- wall recycling

Condensable/metallic elements
- only one trapping chance

Mean sojourn time given by Frenckel's law

$$\tau_d = \tau_0 e^{E_d/k_B T} \quad \tau_0 \sim 1E-13 \text{ s}, E_d - \text{binding energy}$$

Wide range: Ar 1E-11 s, Ni 100 years



Extra

The attainable charge state is mainly depending on the:

- electron density n_e
- confinement time τ_{ion}
- electron energy distribution EEDF

How to change the charge state?

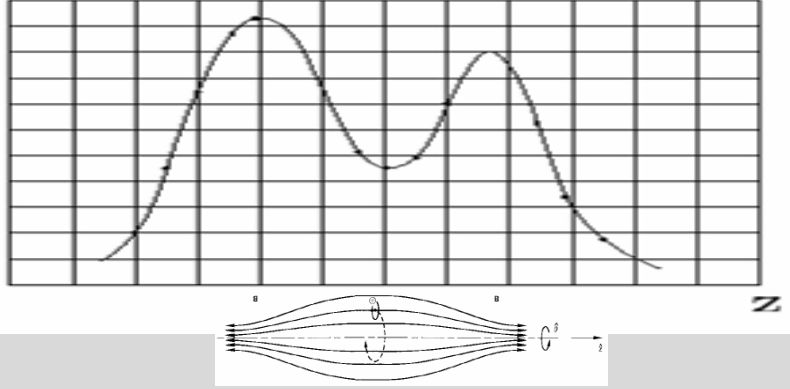
In reality adjust:

1. RF power $Q_{opt} = P_{RF}^{1/3}$
2. buffer gas pressure or mixture -> ion-ion cooling
charge exchange probability

3. B_{ext} since $Q_{opt} \propto \ln B_{ext}$

Axial B-field

B_z



$$F_z = -\frac{1}{2} \frac{mv_r^2}{B} \frac{\partial B_z}{\partial z} = -\mu \frac{\partial B_z}{\partial z}$$

Conserved total energy
magnetic moment μ

=> Magnetic bottle

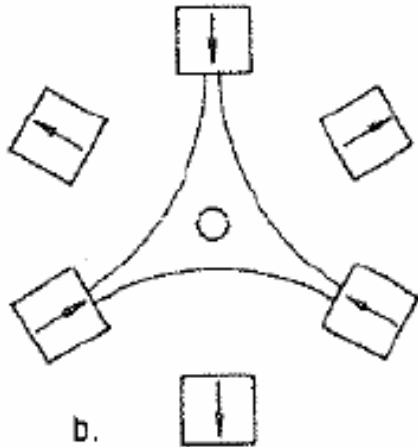
longer τ_e -> longer τ_{ion}

Extracted beam properties

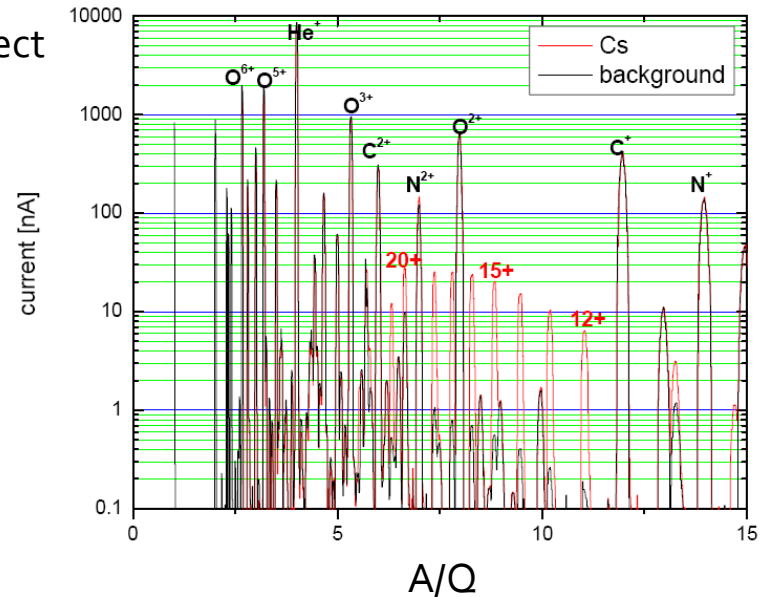
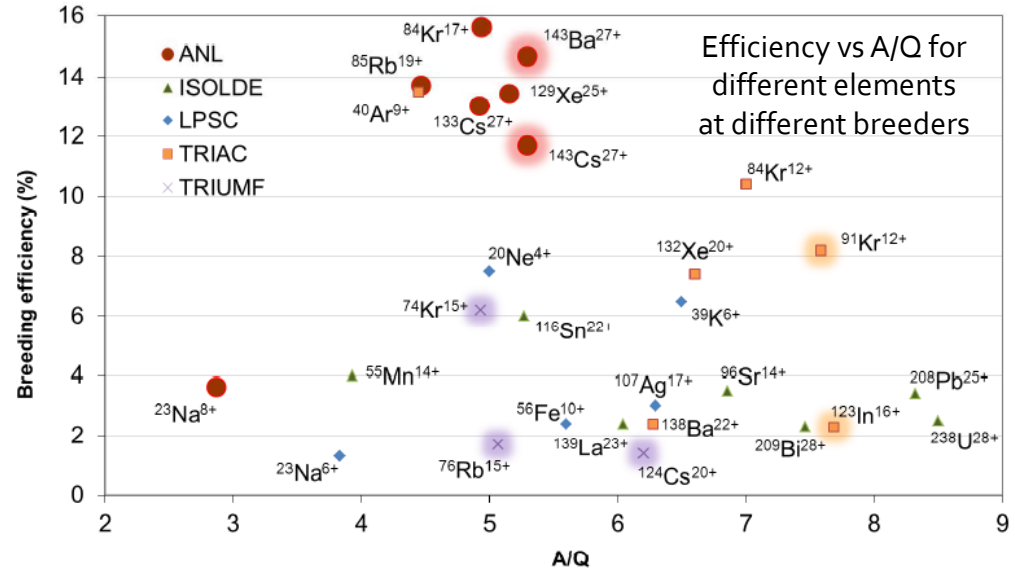
* Extracted energy spread few eV

* Total $I_{\text{extracted}} \sim 100 \mu\text{A}$:
+ radioactive ions

- buffer gas ions (He, Ne or O)
- ions from the plasma chamber sputtering of chamber material
- desorption of implanted ions – memory effect



Loss lines for a hexapole structure



Extracted beam with and without Cs+

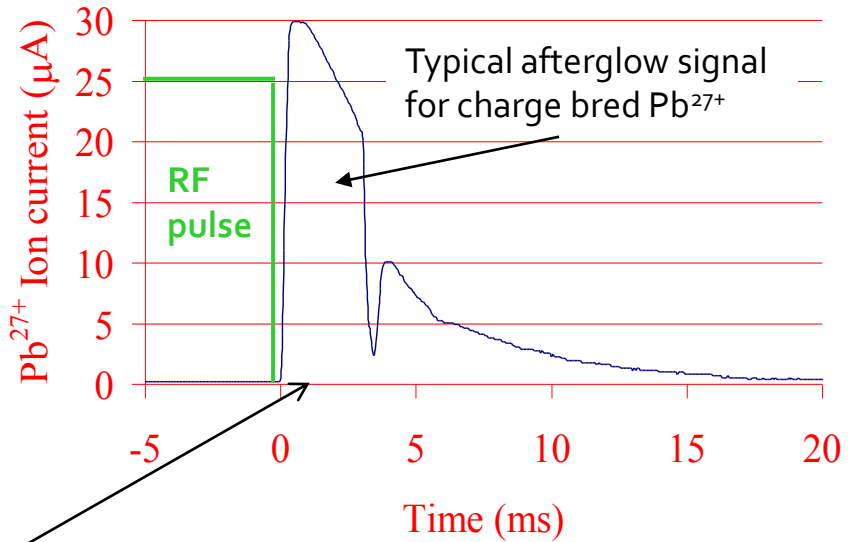
ECRIT mode

Normal operation mode:

- cw injection
- cw extraction

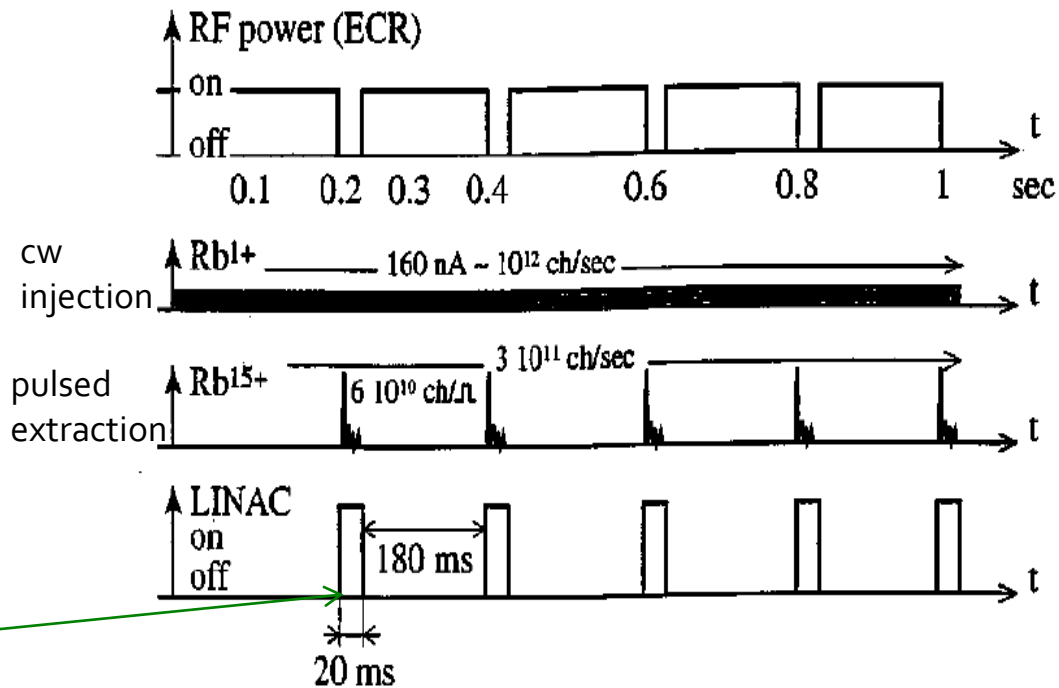
Make use of afterglow:

1. Switch off RF
2. Heating of electrons stops
3. Electron confinement stops
4. Plasma instability / Coulomb expulsion of trapped ions



Result:

- ion trapping (some 100 ms)
- pulsed beam extraction (some ms)



Pulsed linac operation possible

Extra

Practical design aspects

* Similar magnetic-field relations for charge breeding ECRIS CB as for high-Q ECRIS:

$$B_{inj}/B_{ecr} \sim 4, B_{ext}/B_{ecr} \sim 2, B_{min}/B_{ecr} \sim 0.8, B_{rad}/B_{ecr} > 2, B_{ext}/B_{rad} < 0.9$$

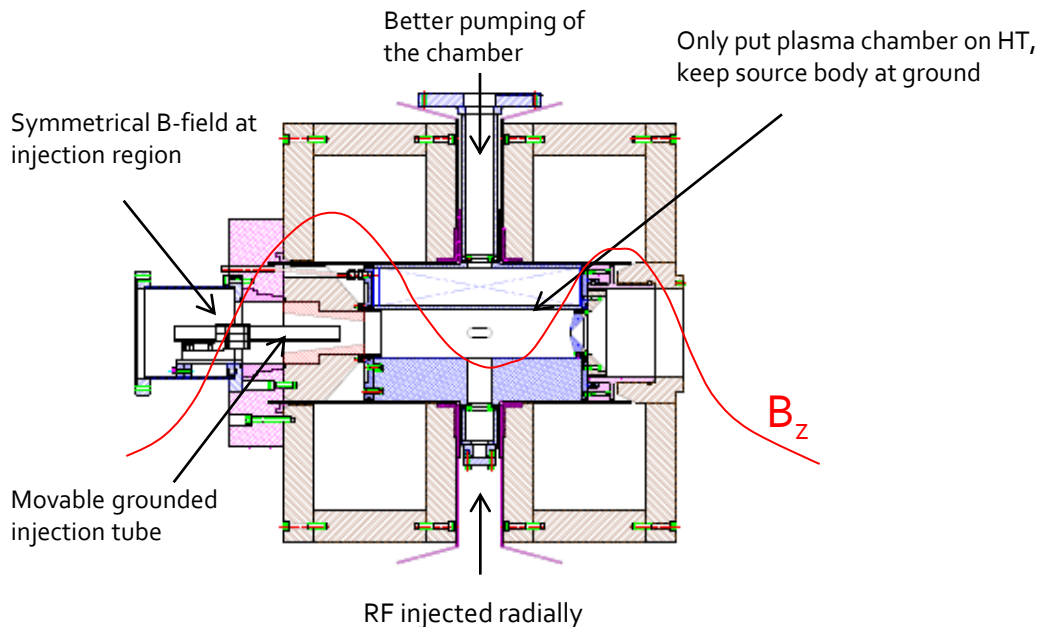
B_{inj} (B_{ext}) is the B-field max at injection side (extraction side)

B_{rad} the radial B-field of the sextupole at the plasma chamber wall

B_{min} the minimum B-field between the magnetic mirrors

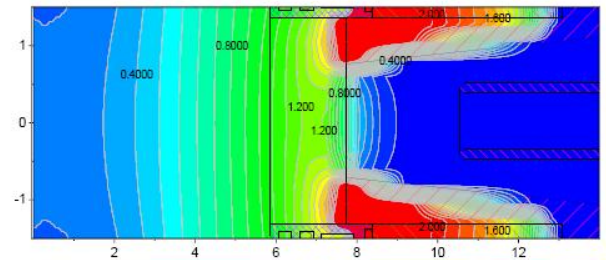
* Grounded injection tube just inside B_{inj}

* Radial RF injection preferred to axial

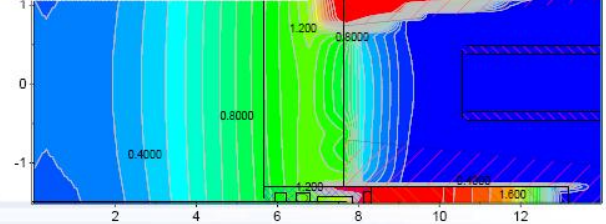


Radial RF wave-guide

$B_z(x,z) y=0$ symmetric



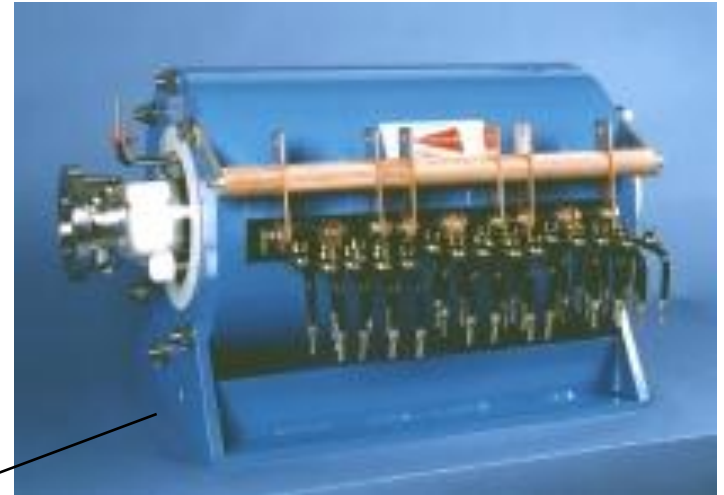
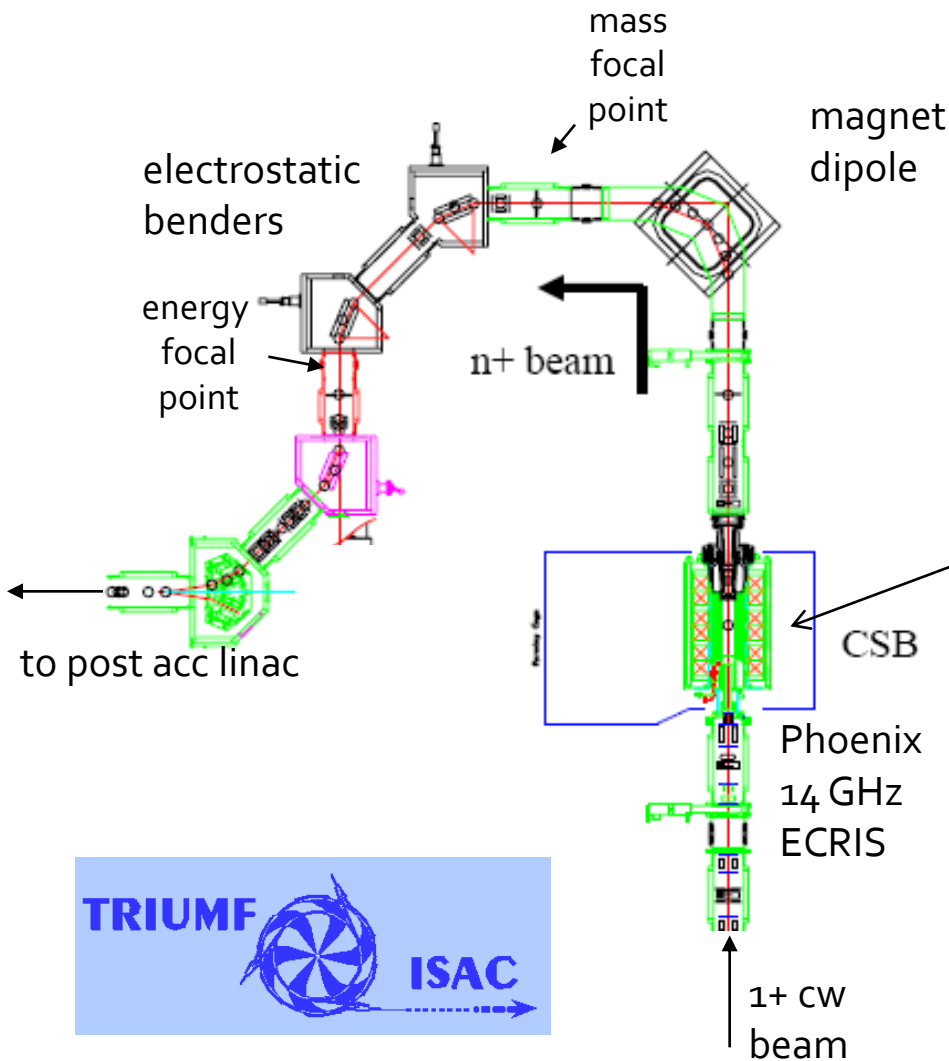
$B_z(x,z) y=0$ asymmetric



Axial RF wave-guide

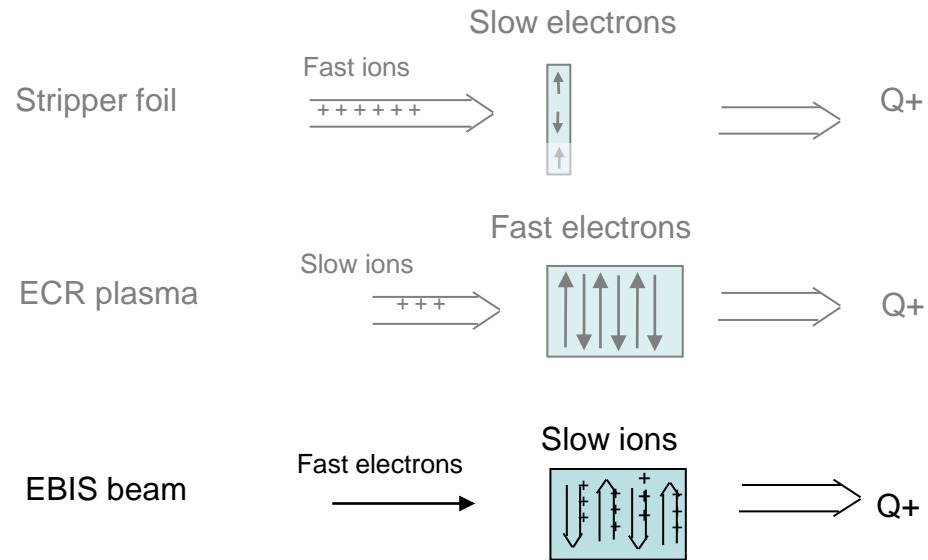
Asymmetric B-field deflects injected particles

ECRIS CB facility



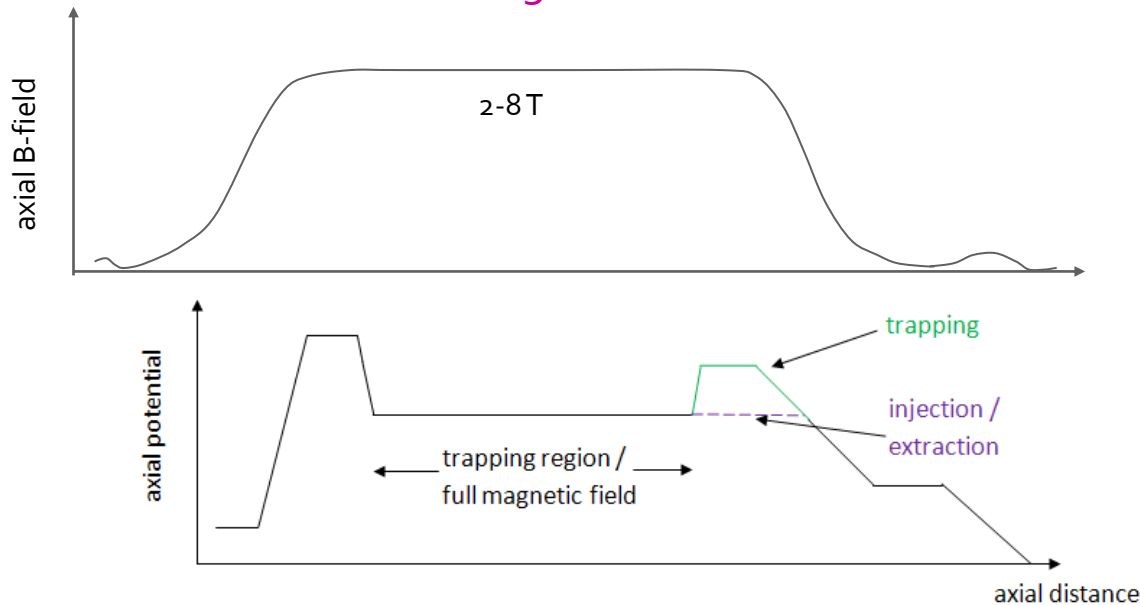
- * ECRIS charge breeder specifications:
 $A/Q < 7$ for $A < 150$
- * cw injection and extraction
- * Superconducting linac
- * Combined electrostatic and magnetic selection

The Third Alternative



- Produces highly charged ions
- e^- beam compressed by solenoid B-field
- Ions are trapped in a magneto-electrostatic trap
- Ionisation by e^- bombardment from a fast, dense mono-energetic e^- beam

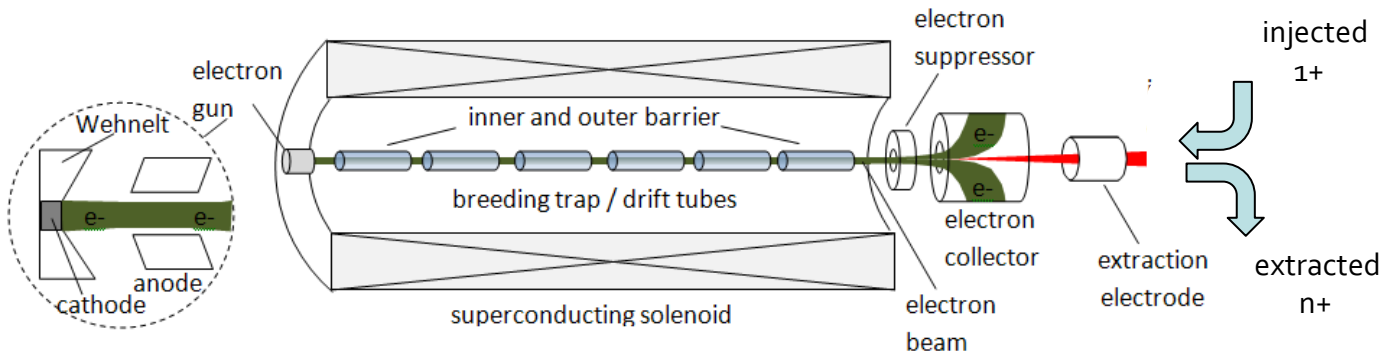
Electron Beam Ion Source / Trap



EBIT - in principle an EBIS but:

1. higher electron current density
2. shorter (few cm)
3. smaller r_{ebeam}

Some consequences for CB!



Breeding time

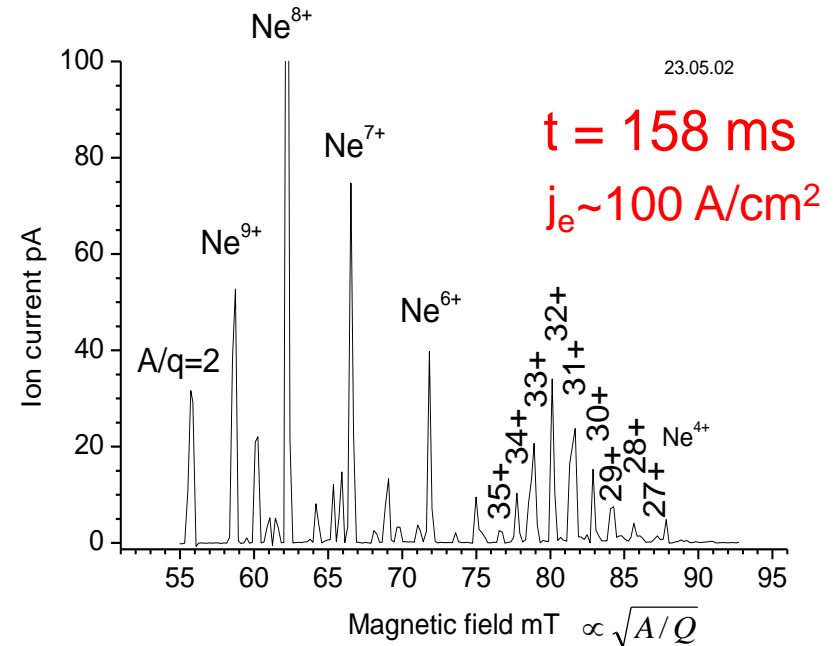
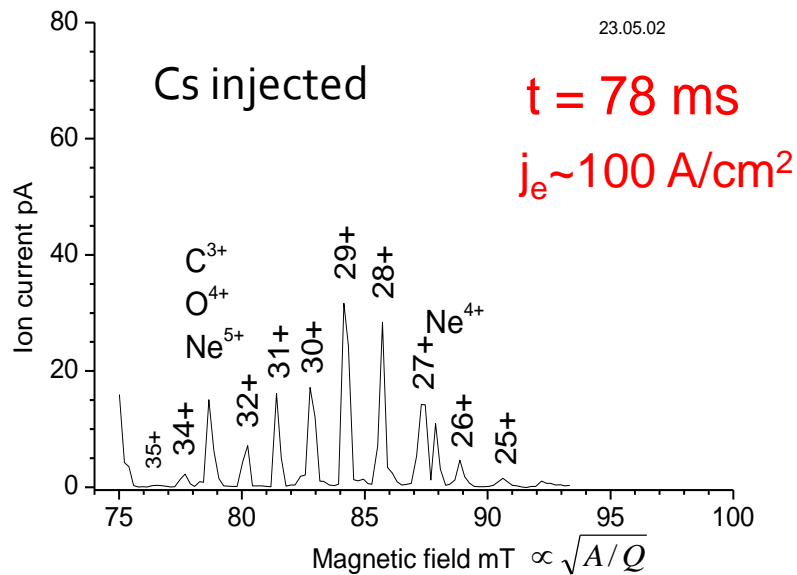
The average time necessary to reach the charge state q :

$$\bar{\tau}_q = \sum_{i=1}^{q-1} \bar{\tau}_{i \rightarrow i+1} = \frac{1}{j_e} \sum_{i=1}^{q-1} \frac{e}{\sigma_{i \rightarrow i+1}}$$

σ – single ionization cross-section cm²
 j_e – electron current density A/cm²
 valid for mono-energetic electrons

j_e usually machine fix
 j_e between 50 and 5000 A/cm²

⇒ Chose A/Q by adjusting the breeding time

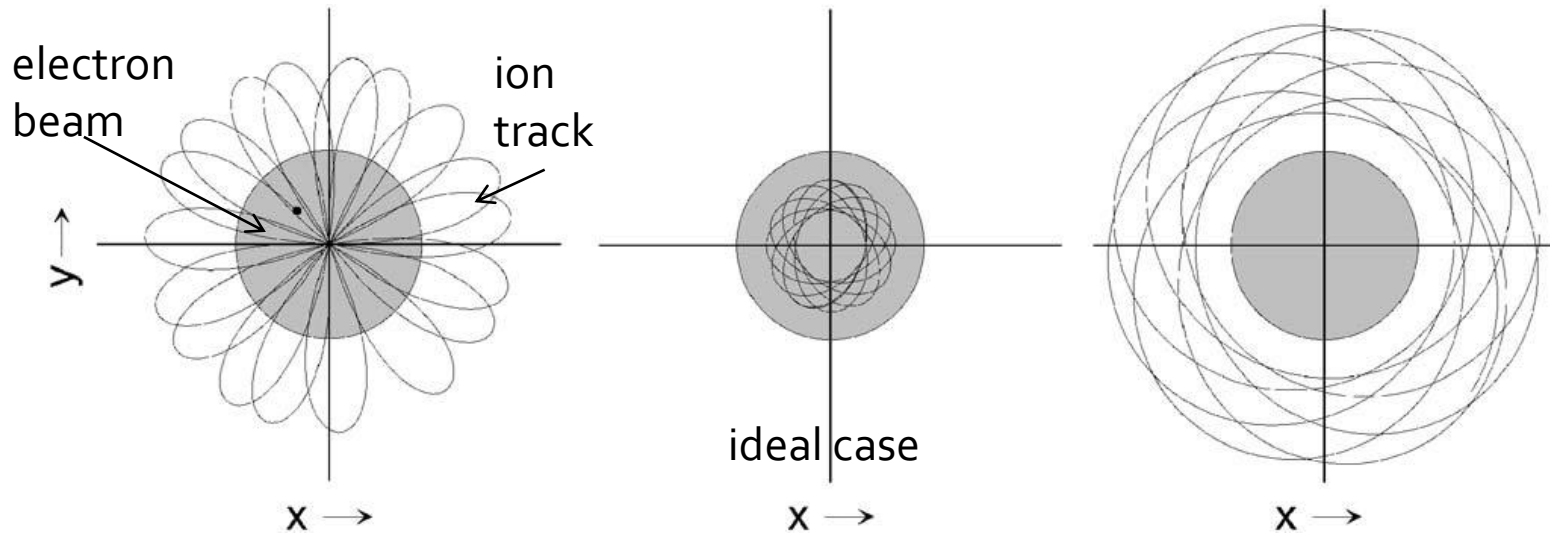


NB! $I_e = j_e * r_{\text{ebeam}}^2 * \pi$ **1st reason for high I_e**

Ion injection EBIS

Desired: overlap between injected ion beam and electron beam

If injection outside electron beam => effective j_e low => increased T_{breed}



Geometrical transverse acceptance

$$\alpha_{\max} = \pi \frac{r_{\text{ebeam}}}{\sqrt{2U_{\text{ext}}}} \cdot \left(Br_{\text{ebeam}} \sqrt{\frac{q}{m}} + \sqrt{\frac{qB^2 r_{\text{ebeam}}^2}{4m} + \frac{\rho_l}{2\pi\epsilon_0}} \right)$$

2nd reason for large I_e

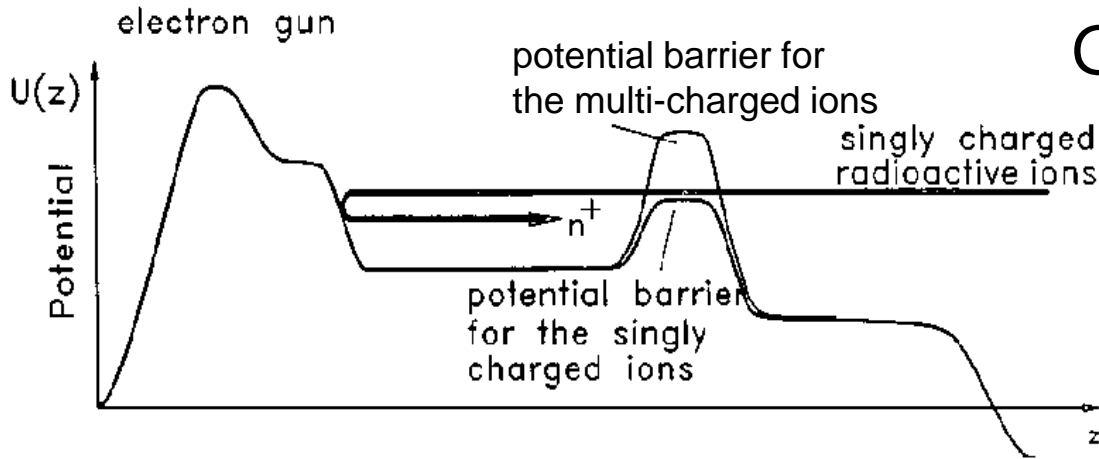
ebeam space charge per meter

NB1. ion neutralization reduces the acceptance

NB2.+ EBIS/T small ϵ ->
- EBIS/T small α

* REXEBIS value $\sim 10 \pi \text{ mm mrad}$ for 90% @ 60 keV

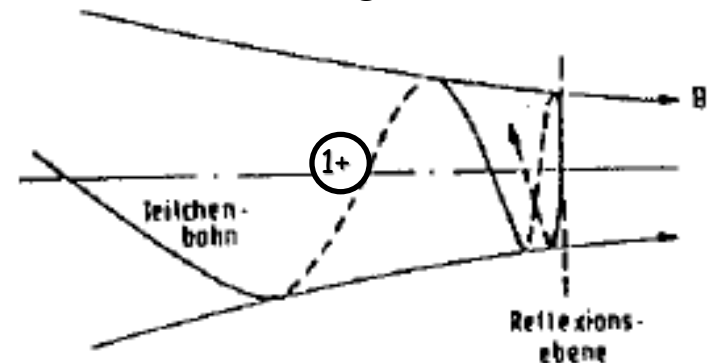
CW ion injection EBIS



Thus:

Inject with low energy for long round-trip time

But too low energy => magnetic reflection



Ion reflection in magnetic field

Condition for trapping

1. Transverse acceptance
2. Ionization

No dissipative forces but U_{barrier} doubles when $1^+ \rightarrow 2^+$
=> axially confined

$$t_{1 \rightarrow 2} \rightarrow e / (\sigma_{1 \rightarrow 2} \cdot j_e)$$

$$\text{Prob}(1^+ \rightarrow 2^+) = 1 - \exp(-t_{\text{inside_ebeam}} / t_{1 \rightarrow 2})$$

Example ^{14}N

$$\sigma_{1 \rightarrow 2} = 1 \text{E-}17 \text{cm}^2$$

$$j_e = 200 \text{ A/cm}^2$$

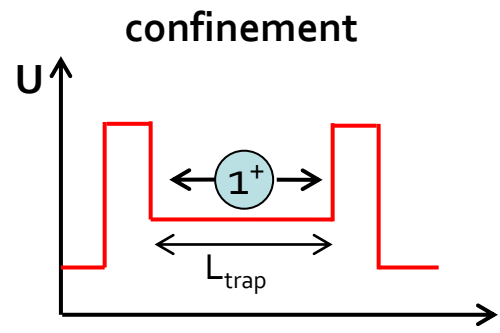
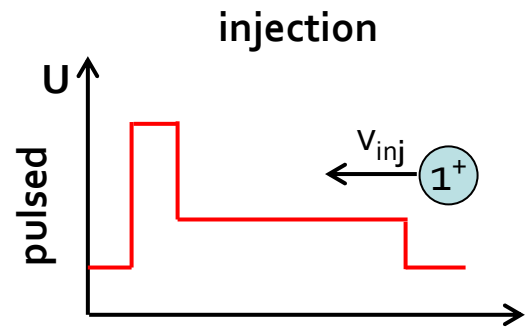
$$\text{Prob} = 0.5$$

$$t_{1 \rightarrow 2} = 55 \text{ us}$$

High acceptance for a CW injected beam is obtained, if a L_{trap} long and r_{ebeam} large and j_e large

(last two in contradiction as $I_e = j_e * r_{\text{ebeam}}^2 * \pi$)

Pulsed ion injection EBIS



Longitudinal acceptance:

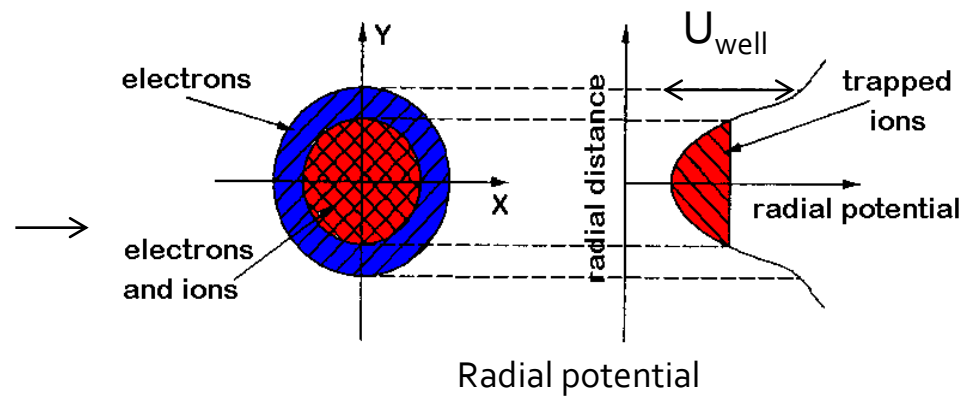
$$W_{inj} < e \cdot U_{well} \quad (\text{some } 100 \text{ eV})$$

$$\Delta T < 2 \cdot L_{trap} / v_{inj} \sim 50 \text{ } \mu\text{s}$$

($L_{trap}=1 \text{ m}$, $W_{inj}=100 \text{ eV}$, $A=14$)

Reality even more complicated...

1. Entangled parameters
 2. Benefits from reduced emittance
- preparatory RFQ buffer gas cooler or Penning trap



$$U_{well} = \frac{I_e}{4\pi\epsilon_0} \sqrt{\frac{m_e}{2eU_e}}$$

I_e – electron beam (A)
 U_e – electron beam voltage (V)

Extra

Extra

Electron beam energy

How to choose electron beam energy U_e for charge breeders?

1. Related to the available current through the perveance:
 $I_e = PU^{3/2}$ (practical limit $P \sim 5 \text{ uPerv}$) Example $I_e = 1 \text{ A} \Rightarrow U_e > 3500 \text{ eV}$
2. U_e has to be larger than the ionization potential I_p for required charge state Q .
Worst case - reach elements close to neutron dripline, since excess of neutrons.

Z	A (neutron rich)	Q (A/Q~4)	$I_{\text{ionization}}$ (eV)
20	60	15	900
40	110	27	1500
60	161	40	2800
80	210	52	3100

Cross section max at $2.7 * I_{\text{ionization}}$

\Rightarrow No need for $U_e > 9000 \text{ eV}$

EBIS capacity

Space charge capacity – determined mainly by the electron beam

$$N^- = k \frac{L_{\text{trap}} r_{\text{ebeam}}^2 \pi}{e} \rho_e \quad \rho_e = \frac{j_e}{v_e} = \frac{I_e}{\pi \cdot r_{\text{ebeam}}^2} \sqrt{\frac{m_e}{2eU_e}} \Rightarrow N^- = 1.05 \cdot 10^{13} \frac{k L_{\text{trap}} I_e}{\sqrt{U_e}}$$

N^- = number of elementary charges

I_e and U_e = electron beam current and energy

k = attainable space charge compensation degree

L_{trap} = trap length

3rd reason for high current

Example $^{132}\text{Sn}^{34+}$ using REXEBIS parameters:

$I_e = 0.5 \text{ A}$, $U_e = 5 \text{ keV}$, $L = 0.8 \text{ m}$, $k = 50\% \Rightarrow \sim 3 \cdot 10^{10}$ charges

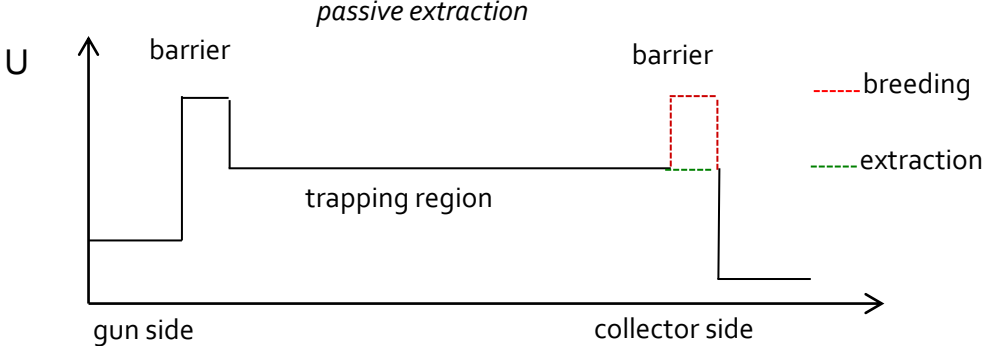
$\Rightarrow 3\text{E}10/34 * 0.2 = \mathbf{2\text{E}8 \text{ ions/pulse}}$



~20% in desired
charge state

*NB! Ion throughput (ions/s)
= (ions/pulse) / T_{breed}*

Beam extraction scenarios



For REXEBIS duty factor
 $T_{extr}/T_{breed} \sim 100 \mu s / 100 \text{ ms}$

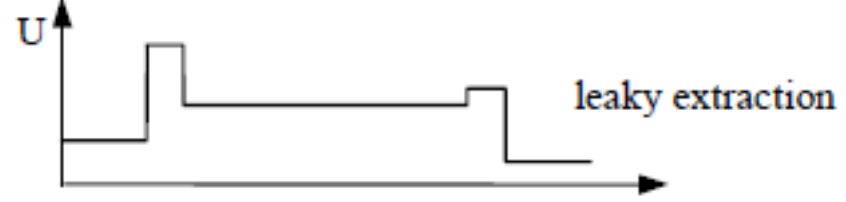
=> Good signal-to-noise-ratio

if heating by e- and ion-ion cooling neglected

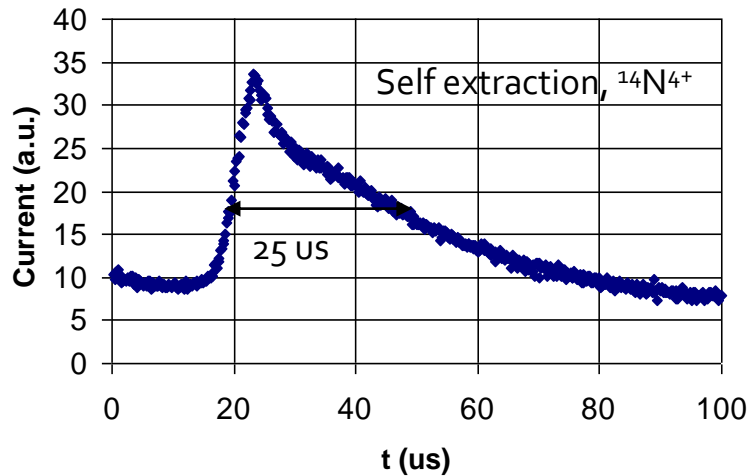
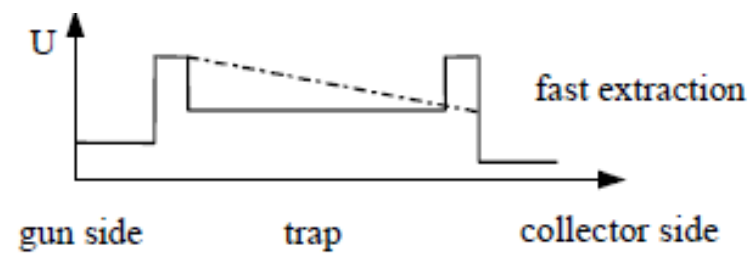
$v_{ion_extr} \sim v_{ion_inj} (W_{inj} \sim 100 \text{ eV})$

$\Delta T_{extr} \sim L_{trap} / v_{ion_extr} \sim 25 \mu s \text{ for } ^{14}\text{N}$

Reduce instantaneous rate to experiment, 1 ms

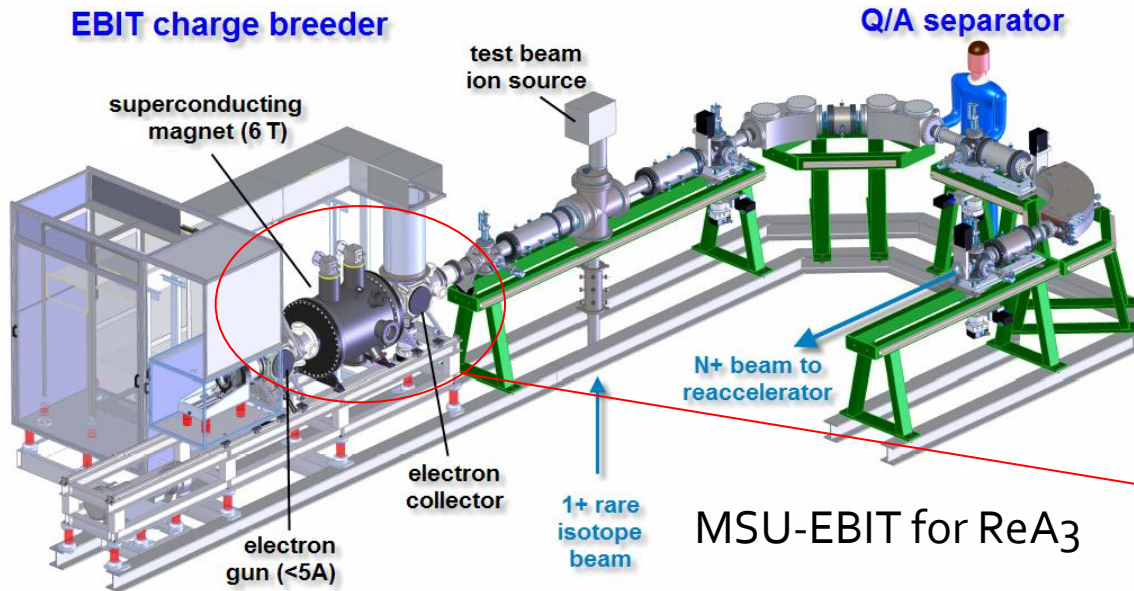


Speed up extraction for multi-turn injection into synchrotron <10 us



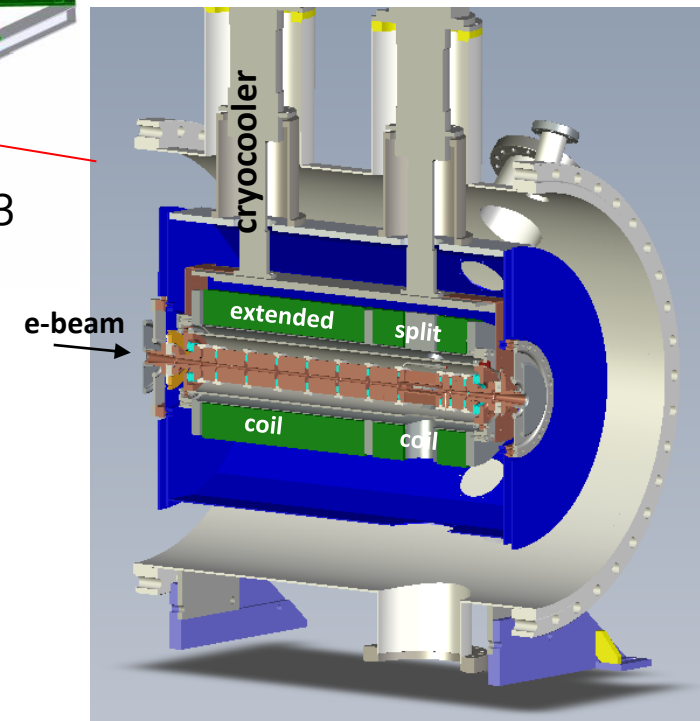
EBIT CB facility

3 MeV/u re-accelerator of thermalized projectile fragmentation and fission beams



With $1E_4$ A/cm² ->

1. charge breed ions with $Z < 35$ into Ne-like or higher within 10 ms
2. ionize from 1+ to 2+ within <math><1\ \mu s</math>



Cryogenic trapping region

Design goals

- Continuous injection and accumulation of ions
- Variable extraction duty cycle (ms pulse to quasi-continuous)
- Electron current density $>1E_4$ /cm²
- Beam rates $>1E_9$ ions/s
- Highest efficiency (> 50% in a single charge state)

Preparatory devices and tricks

Remember: often deal with $<1E_4$ pps => 1.7 fA

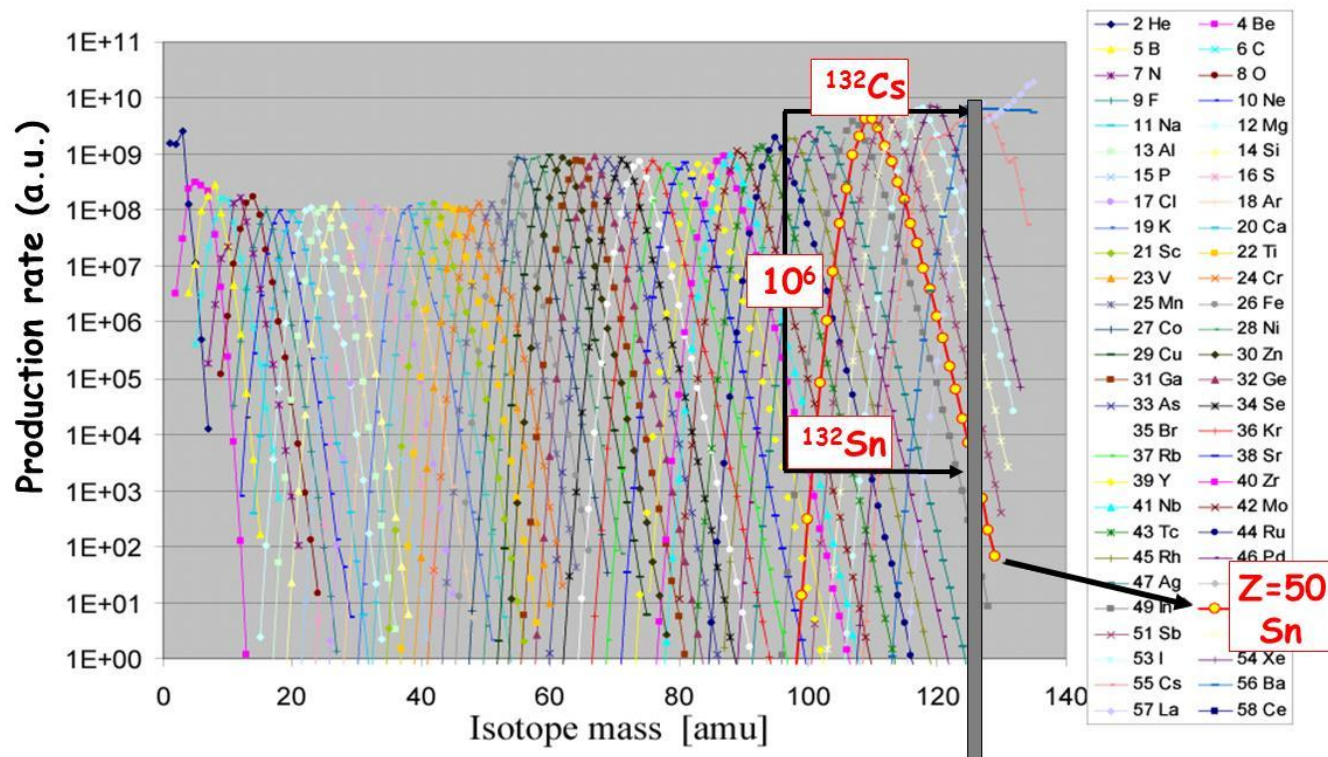
Beam contamination

Can't see the trees for the forest

Beam impurities:

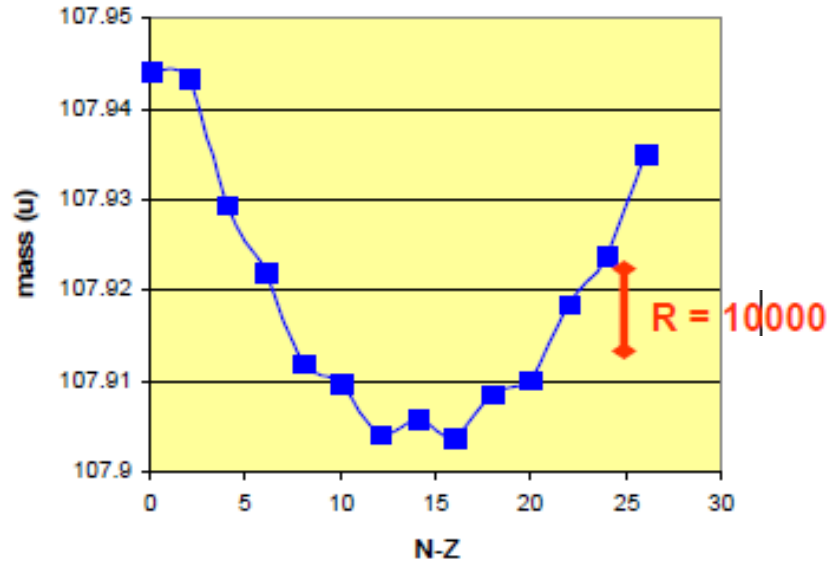
a. isobaric contamination
from ISOL-target

1 GeV proton beam on a lanthanum (La) target



Extra

Masses of A=108 isotopes



ISOL beam separation

Problem: isobaric separation difficult

* Requires RFQ cooler for pre-cooling of transverse ϵ

* Tails of high intensity masses may go through selection system

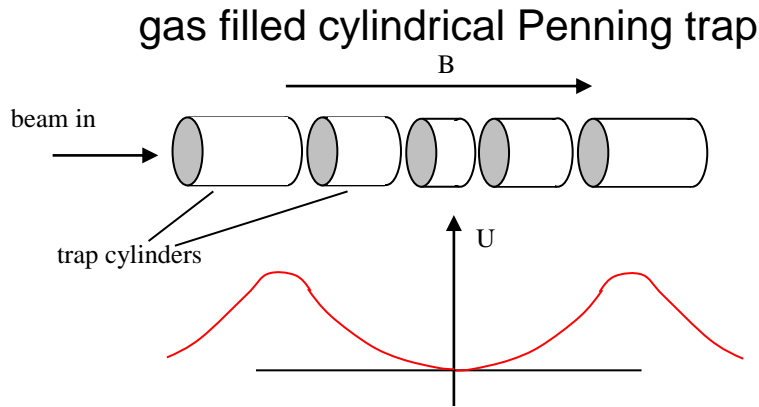
Resolution required to separate:

Neighbouring mass:	R=250
Molecular ions (e.g. CO from N ₂):	R=500-1000
Isobars (e.g. ⁹⁶ Sr from ⁹⁶ Rb):	R=5000-50000
Isomers:	R=1E5 - 1E6

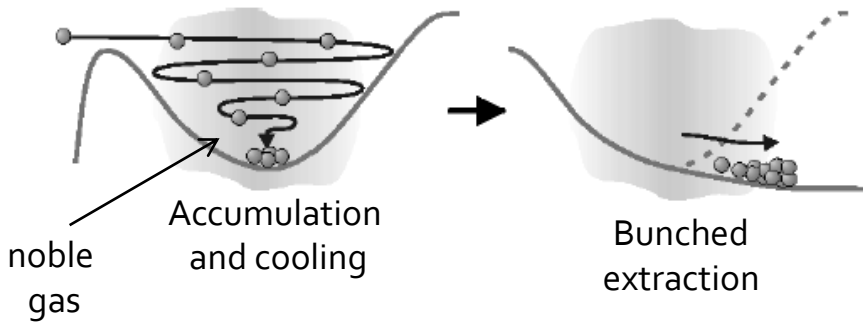
Solution

1. Isobaric mass resolution inside Penning trap
2. Molecular beams

Preparatory beam cooling

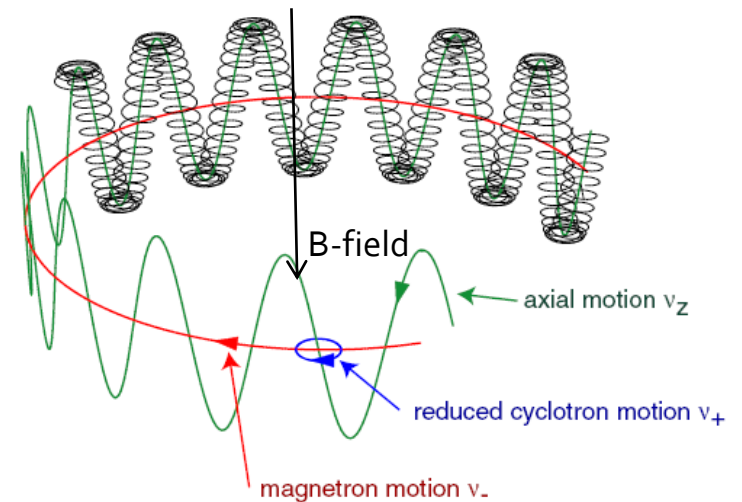


Axially - electrostatic field
 Radially - magnetic field



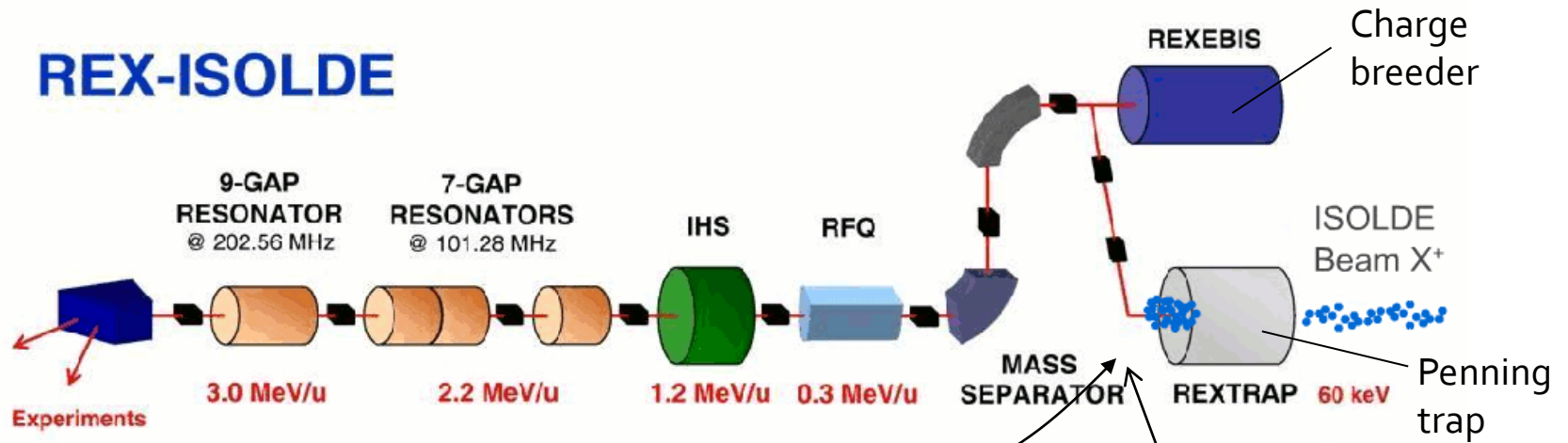
Energy loss due to buffer gas collisions: $F = -\delta m v$

Introduce a *Penning trap* in ISOL-line to:
 accumulate
 phase space cool
 bunch the beam

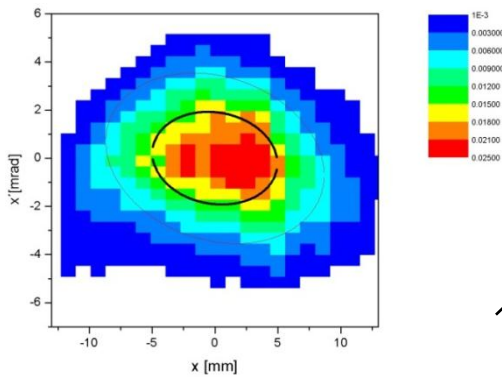


With buffer gas and RF coupling between v_+ and v_- all three motions cooled => amplitudes reduced

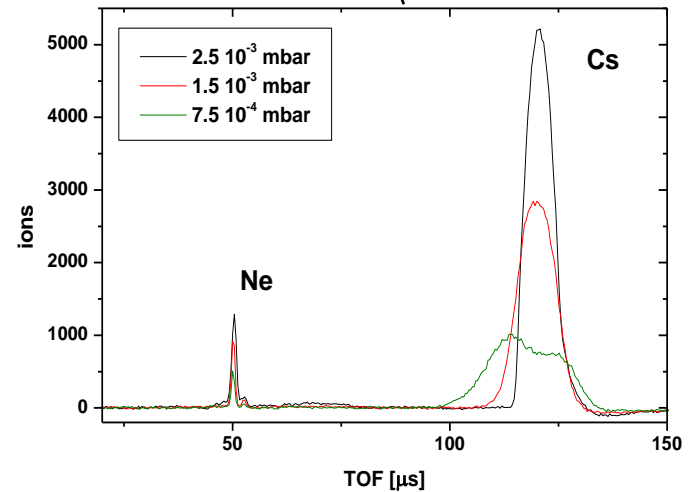
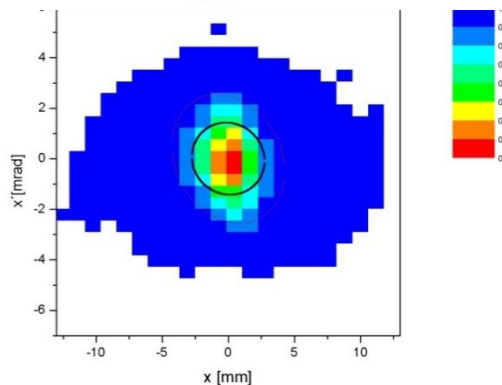
REX-ISOLDE



Non-cooled



Cooled



- * Bunching: few μs
- * Transverse emittance:
25 \rightarrow $\sim 10 \pi$ mm.mrad at 30 keV
- * $\Delta E \cdot \Delta t \sim 10$ eVus

EBIS
injection
ok!

Resolving isobars in Penning trap

- * Low $m/\Delta m \sim 300$ in REXTRAP in normal mode
- * Can be setup with $m/\Delta m > 10000$

Procedure

- cool down the ion cloud (normal operation)
- shift out the ion cloud (desired and contaminants) with a mass independent dipolar excitation $\nu_{RF} = \nu_-$ to $r > 5$ mm
- selectively re-centre the desired species with $\nu_{RF} = \nu_c$
- at extraction only the centered ions survive

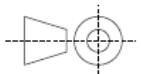
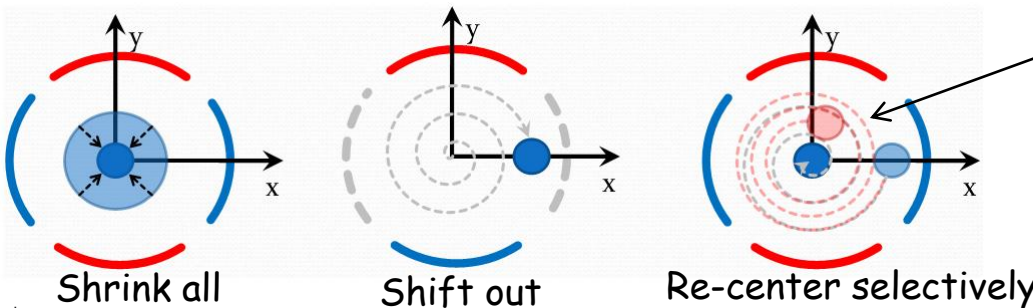
$$\omega_{\pm} = \frac{\omega_c}{2} \left(1 \pm \sqrt{1 - \frac{2\omega_z^2}{\omega_c^2}} \right)$$

cyclotron
axial

$$\omega_+ + \omega_- = \omega_c = \frac{e}{m} B$$

magnetron
reduced cyclotron

NB! Re-centering is mass dependent



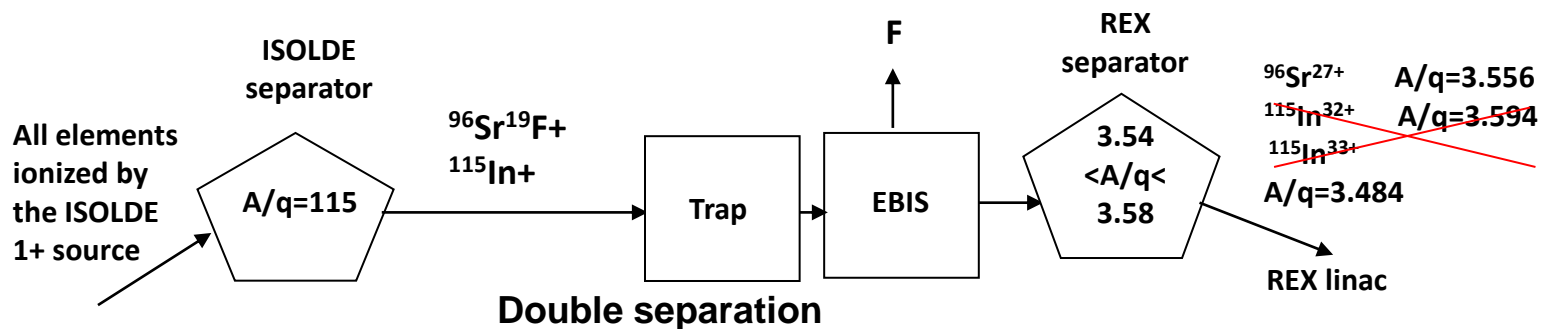
Extra

Molecular beams

The idea

1. Use chemical properties to separate isobars e.g. ^{96}Rb from ^{96}Sr
2. Create a molecular sideband ($^{96}\text{Sr}^{19}\text{F}^+$) with gas leak at ISOL-target
3. Molecular ions are extracted and selected in the separator (A=115 selection)
4. Keep molecules inside trap, break them in EBIS
5. Charge breed as usual and obtain clean ^{96}Sr

Works also
with ECRIS!



Remember: often deal with $<1E4$ pps => 1.7 fA

Beam contamination

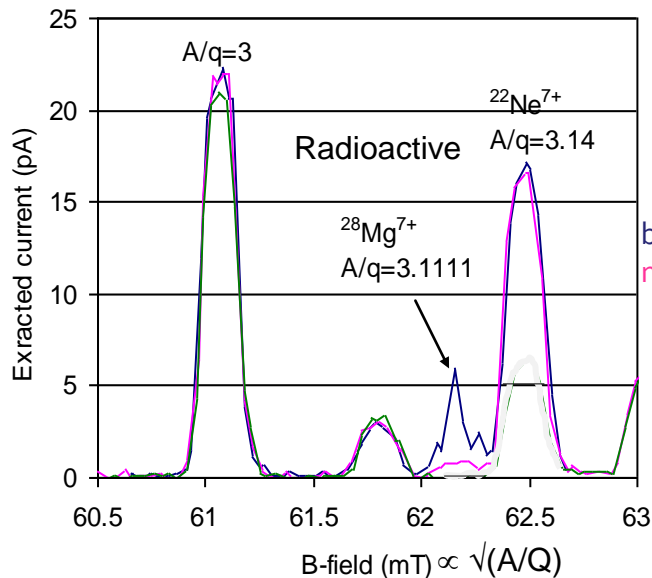
Can't see the trees for the forest

Beam impurities:

a. isobaric contamination from ISOL-target

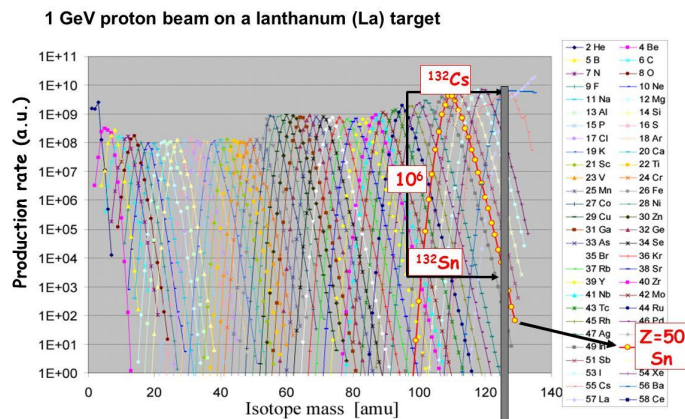
b. residual gases in CB

$$I_{\text{residual}} \propto \sigma_{0 \rightarrow 1+} P_{\text{res gas}}$$



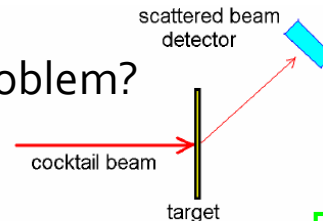
blue – with ^{28}Mg
magenta - background

EBIS extracted spectrum



J. Lettry, V. Fedoseev (CERN)

What's problem?



$$\text{Yield} = C \cdot \sigma \cdot \varepsilon \cdot \sum i_{\text{beam}}$$

10% impurity
small correction

75% impurity
determine Z
e-by-e

99% impurity
difficult

Extra

Separator after breeder

1. Separator magnet selects A/Q

$$B\rho = Av/Q$$

ambiguous A/Q if Δv large $\frac{\Delta x}{x} \approx \frac{\Delta A}{A} + \frac{\Delta v}{v}$

$$\text{Combine 1 \& 2} \Rightarrow \underbrace{E_{\text{def}} r_{\text{def}}}_{\text{fix}} = \underbrace{(B\rho)^2}_{\text{fix}} (A/Q)$$

- * Only a single A/Q transmitted
- * Can suppress ions with wrong energy

Even so, some A/Q contaminants difficult to resolve

${}^7\text{Be}^{3+}$ from ${}^{14}\text{N}^{6+}$

R=450

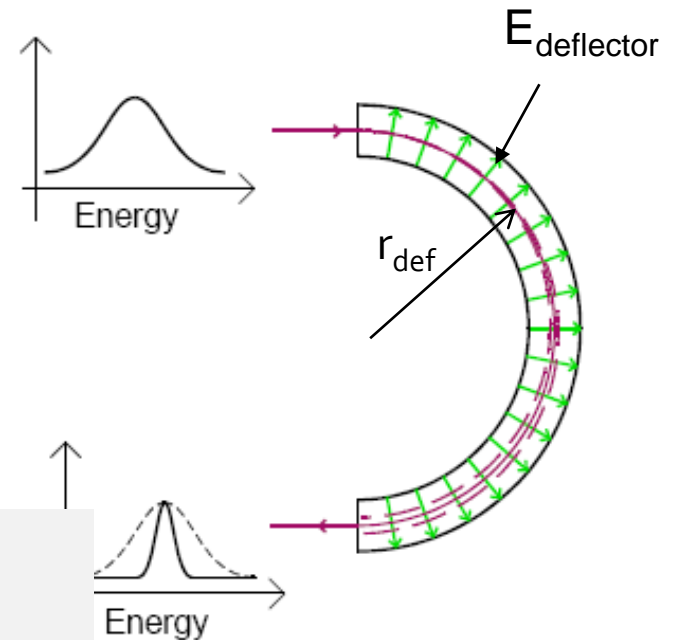
${}^{18}\text{F}^{9+}$ from ${}^{12}\text{C}^{6+}$

R=19200

$\frac{\Delta(A/Q)}{(A/Q)}$ typically a few hundred
for a breeder separator

2. Electrostatic deflector performs a potential selection

$$E_{\text{def}} r_{\text{def}} = 2U_{\text{ext}}$$



Facilities and the future

CB for low-energy experiments

* Not only for post-acceleration!

High precision mass measurements

$$\frac{\Delta m}{m} \sim \frac{m}{q T_{rf} B \sqrt{N}}$$

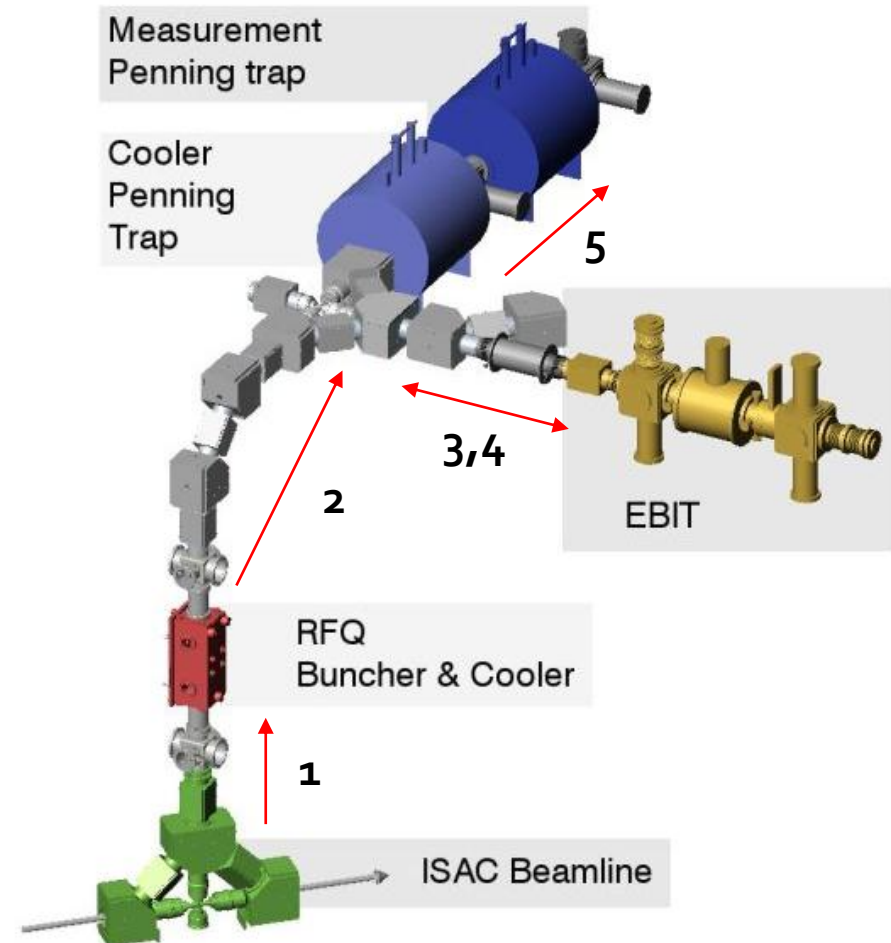
m – ion mass

q – ion charge

T_{rf} – rf excitation time

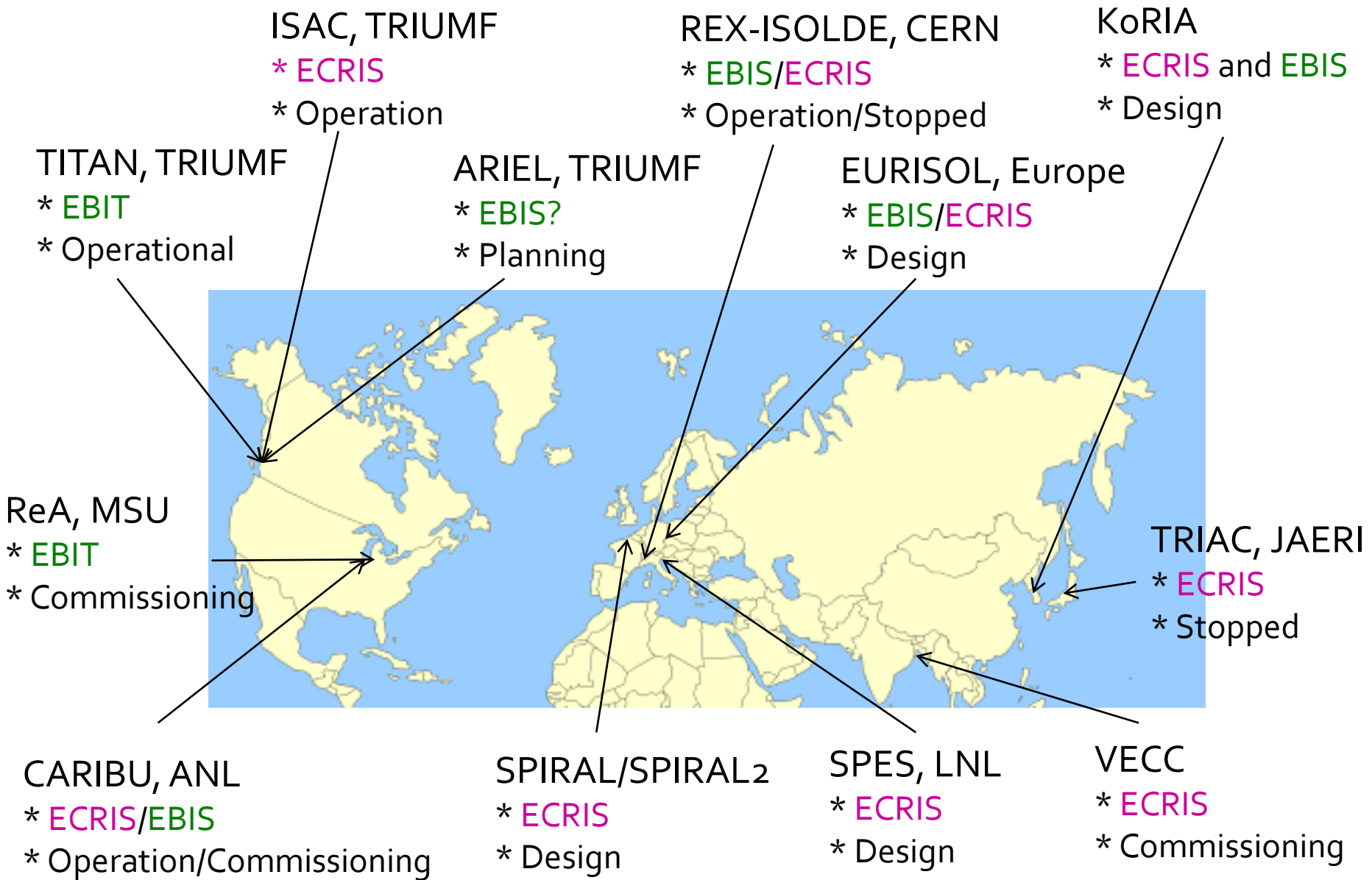
B – magnetic field

N – number of measurements

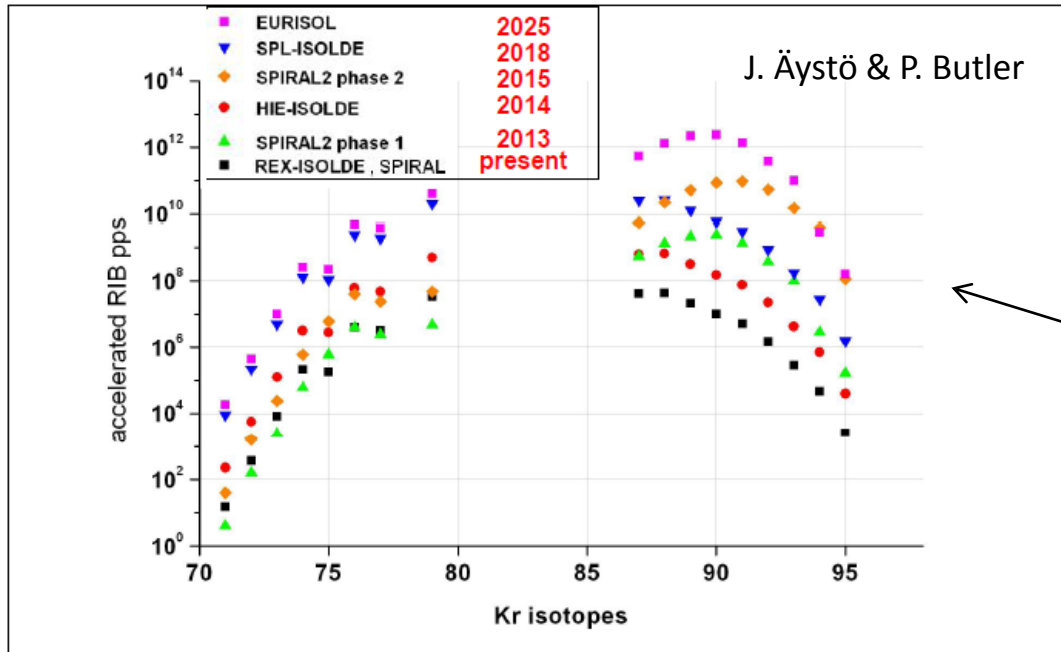


Ideally only one ion per measurement cycle

Charge breeders for RIBs worldwide



Radioactive ISOL beam yields

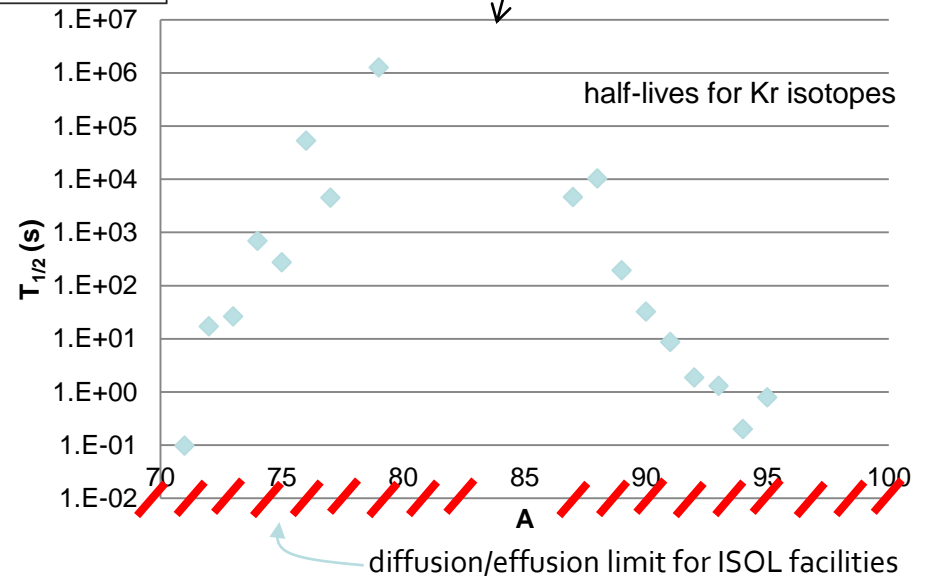


What to expect?

Next generation facilities

* Increased intensities

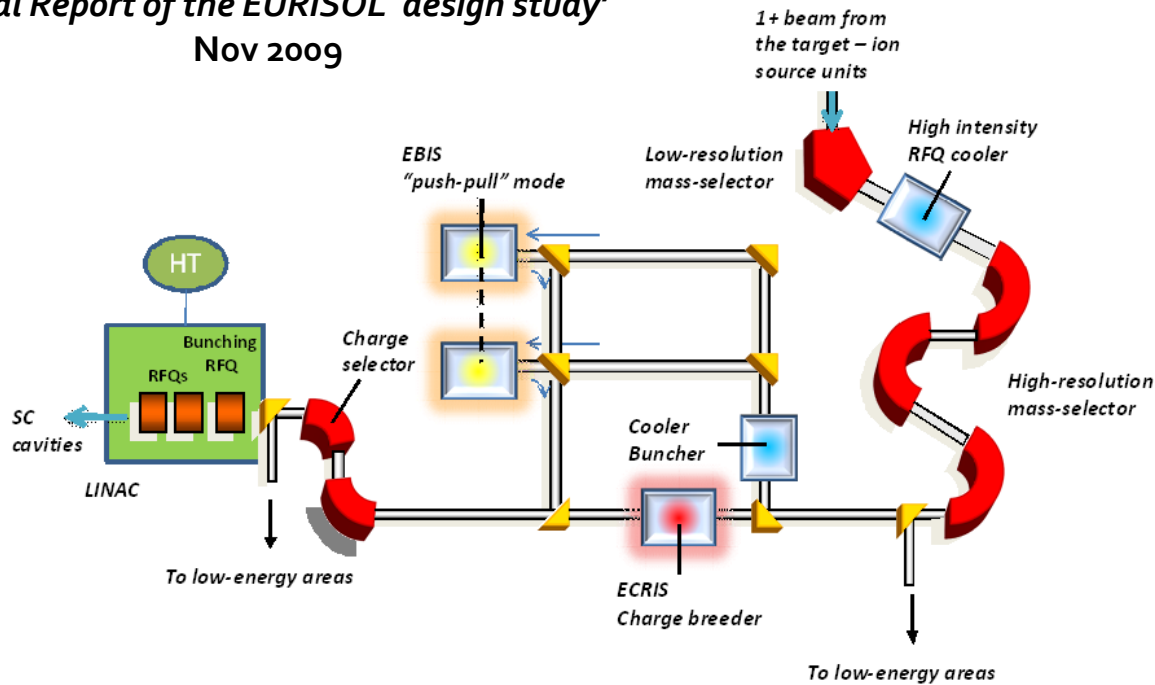
* Shorter half-life along drip lines



Further information

'Final Report of the EURISOL design study'

Nov 2009



Detail of the EURISOL Layout

Modified from P. Butler's presentation, NuPECC meeting June 2007

What to expect?

Two main paths

1. Very exotic low-intensity ($<1E7$ ions/s) beams for 'standard' experiments
2. High intensity beams ($>1E9$ ions/s) to generate even more neutron rich beams – beam purity not of utmost importance

Extra

The *real* challenges:

1. Inject ions into storage rings
⇒ fully stripped charge for $Z>60$
2. Breeding of beta beams
(e.g. ${}^6\text{He}$ and ${}^{18}\text{Ne}$)
⇒ 1 s trapping of high intensity

Weight function according personal preference

Extra

	Stripper	EBIS	ECRIS
Simplicity	3, passive element	1, complicated (SC, UHV, e-gun)	2, medium (RF, beam tuning)
Beam properties in	3, no special requirements	1, bunched, small acceptance	2, CW, medium acceptance
Beam properties out	1, emittance blow-up	3, us or ms bunch, small emittance	2, CW or ms bunch
Low intensities	3, no contamination	2, some <0.1 pA	1, high rest-gas level
Rapidity	3, instant, us isotopes	2, 10 to few 100 ms	1, some 10 ms to a few 100 ms
CSD	3, narrow, varying charge state	3, narrow, high charge state	2, broad CSD, moderate charge
CSD tuning	1, not tunable	3, change T_{breed}	2, many parameters
Machine contamination	2, foil exchange	1, multiple parts	2, change plasma liner
Storage time	1, non existing	3, up to several s	2, ~100 ms
Beam capacity	3, very high, 100 uA	1, limited to nA	2, several uA
Energy spread	1, $\Delta W/W \sim 1\%$	2, a few 10 eV*q	3, some eV
Efficiency	2, 5-15%	2, 5-20%	2, 5-20%
Mass range	1, heavy masses difficult	3, full mass range	1, light masses difficult
Life-time	2, foil breakage, 50 mC/cm ²	1, electron cathode	3, klystron lifetime
Price	1 high, (incl. pre-acc)	2, ~1 Meuro	3, ~0.5 Meuro



Bibliography

General books

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- Ion Sources, Zhang Hua Shun, Berlin: Springer, 1999.
- The Physics and Technology of Ion Source, I. G. Brown, New York, NY: Wiley, 1989
- Introduction to Plasma Physics and Controlled Fusion, Vol 1: Plasma Physics, F. F. Chen, Plenum Press 1974
- Electron Cyclotron Resonance ion Source and ECR Plasmas, R Geller, IOP 1996

General charge breeding papers

- Charge breeding results and future prospects with electron cyclotron resonance ion source and electron beam ion source, R. Vondrasek, Rev. Sci. Instrum. 83, 02A913 (2012)
- Charge breeding of radioactive ions with EBIS and EBIT, F. Wenander, J. Instrum. 5, C10004 (2010)
- Evaluation of charge-breeding options for EURISOL, P. Delahaye O. Kester, C. Barton, T. Lamy, M. Marie-Jeanne and F. Wenander, Eur. Phys. J. A 46, 421 (2010).
- Charge breeding application of EBIS/T devices, O. Kester, AIP Conf. Proc. Vol. 1099 (2009) 7-12.
- European research activities on charge state breeding related to radioactive ion beam facilities, T. Lamy, J. Angot, and T. Thuillier, Rev. Sci. Instrum. 79, 0A2909 (2008)
- Charge State Breeders: on-line results, F. Wenander, Nucl. Instrum. Methods Phys. Res. B 266, 4346 (2008).
- Status of charge breeding with electron cyclotron resonance ion sources, T. Lamy et al. Rev Sci Instrum. 77 (2006) 03B101
- Charge Breeding Techniques, F. Wenander Nucl Phys A746 (2004) 40c
(extended version as CERN note, CERN-AB-2004-035)

Miscellaneous relevant conference proceedings

- International Workshop on ECR ion sources
- International Symposium on EBIS/T
- Radioactive Nuclear Beams (discontinued)
- International Conference on Electromagnetic Isotope Separators and Techniques Related to their Applications (EMIS2012)

Executive summary

Stripper



Fast but expensive
(pre-acc. LINAC)

ECRIS



Large capacity but dirty

EBIS



Clean but low capacity